

# Hall C Winter Collaboration Meeting 2026

## KaonLT: preliminary high Q2 LT-separations

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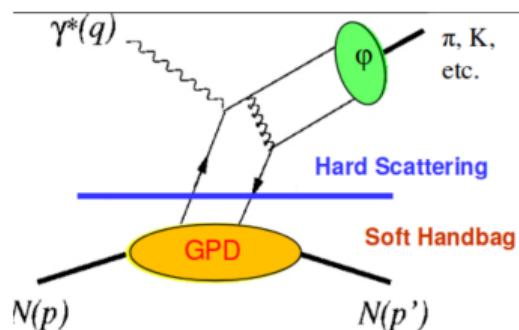
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# Physics Motivation: 3D Hadron Structure

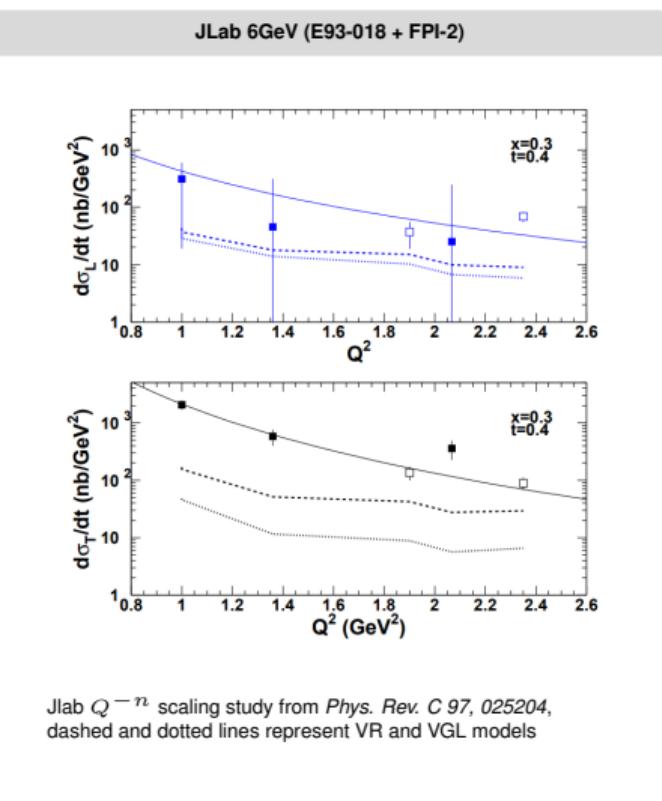
## Hard-Soft Factorization

Assumption that the **hard** scattering process can be separated from the **soft** hadronic structure.



## Power Scaling at fixed $x_B$

- Observed behavior at low  $Q^2$ :
  - $\sigma_L \sim Q^{-6}$
  - $\sigma_T \sim Q^{-8}$
- A first study of scaling behavior in a strange system at high  $Q^2$ .
- A direct testbed and bridge from *hadronic* to the *partonic* regime.

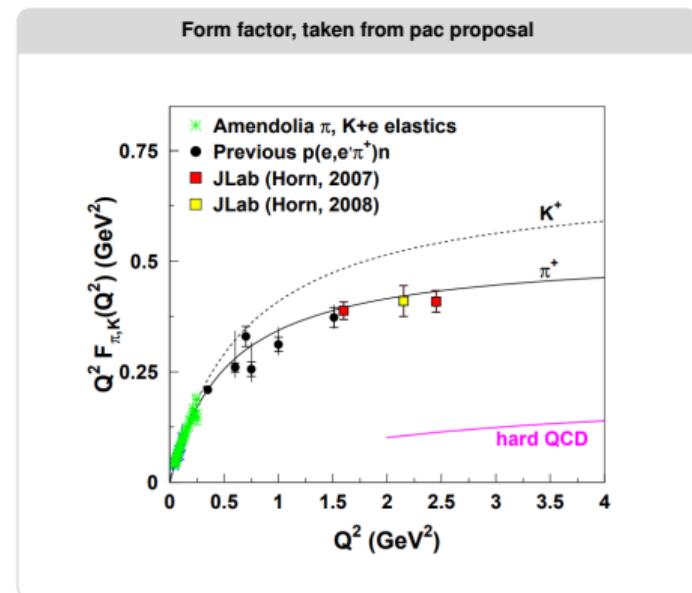


# Kaon Form Factor Extraction

**Kaon Form Factor  $F_K$  extraction from  $\sigma_L$  :**

$$\sigma_L \approx \frac{-tQ^2}{(t - m_K^2)^2} g_{KNN}^2(t) \underbrace{F_K^2(Q^2)}_{\text{Kaon FF}} \rightarrow F_K(Q^2) = \frac{1}{1 + Q^2 / \underbrace{\Lambda_K^2}_{\text{cutoff}}}$$

- Form factor related to longitudinal cross section  $\sigma_L$ .
- Kaon Form factor data is scarce at high  $Q^2$ .
- Study the transition from **non-perturbative** to **perturbative** QCD.
- Extract by measuring structure functions  $\sigma_{L,T,LT,TT}(t)$  at various kinematics and fit to Regge models.

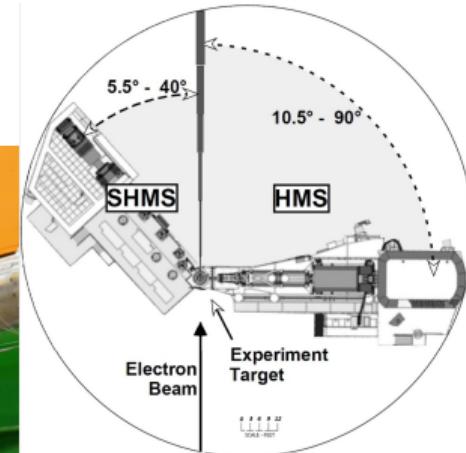


► **Experimental Requirement:** Need to run a dedicated experiment with **high statistics** for Kaon  $L/T$  separation to resolve the current uncertainties.

# Exclusive Meson Experiments in Hall C @ 12 GeV JLab

## **E12-09-011 : KaonLT experiment in Hall C at JLab**

- Exclusive electroproduction of kaons on protons  $e + p \rightarrow e' + K^+ + \Lambda, \Sigma^0$
- HMS as electron arm, SHMS as hadron arm for kaon



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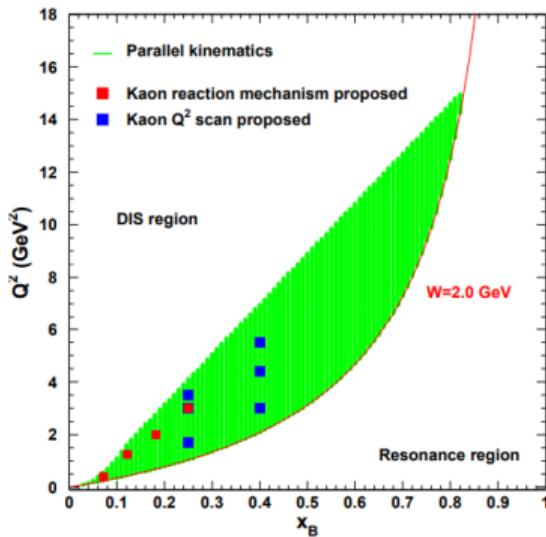
- ▶ First coincidence experiment (HMS-SHMS) in the 12 GeV era !
- ▶ 12 GeV electron beam + small angle in SHMS allows precise measurements at high  $Q^2$

# Kinematic region

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$E$ [GeV]	$Q^2$ [GeV $^2$ ]	$W$ [GeV]	$x_B$	$\epsilon$
10.6	5.5	3.02	0.40	0.53
8.2				0.18
10.6	4.4	2.74	0.40	0.72
8.2				0.48
10.6	3.0	2.32	0.40	0.88
8.2				0.57
10.6	3.0	3.14	0.25	0.67
8.2				0.39
10.6			0.21	0.79
8.2	2.115	2.95		0.25

$p(e, e' K^+) \Lambda \Sigma^0$



- **Virtual photon polarization:**  $\frac{1}{\epsilon} = 1 + 2\mathbf{q}^2/Q^2 \tan^2(\theta_e/2)$
- Measure at two  $\epsilon$  settings for Rosenbluth (LT) separation, large  $\Delta\epsilon$  to minimize uncertainty

# Technique for extracting $\sigma_L$ and $\sigma_T$ : Rosenbluth (LT) Separation

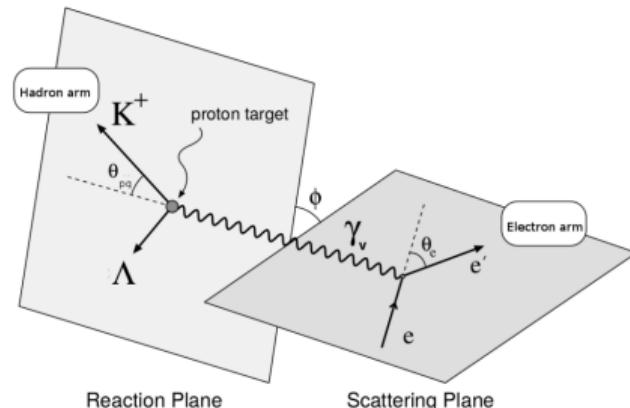
## Rosenbluth formula

$$2\pi \underbrace{\frac{d^2\sigma}{dtd\phi}}_{\text{Measured Data}} = \underbrace{\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt}}_{\text{Extracted Terms}} + \underbrace{\sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{LT}}{dt} \cos\phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi}_{\text{Interference Terms}}$$

- **Virtual photon polarization:**  $\frac{1}{\epsilon} = 1 + 2q^2/Q^2 \tan^2(\theta_e/2)$
- $\phi$  : azimuthal angle between scattering and reaction planes

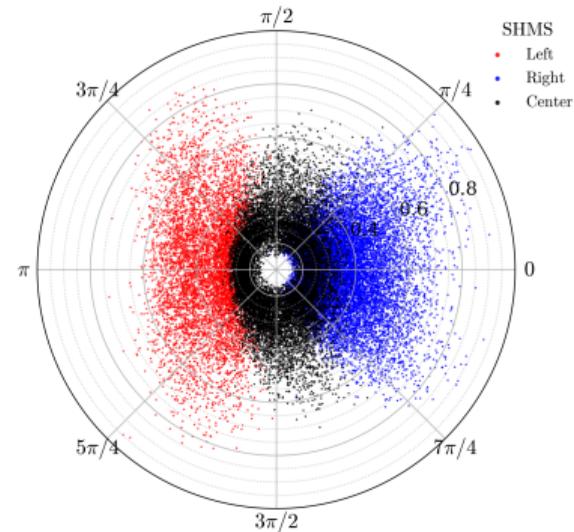
► Extract  $\sigma_L, \sigma_T, \sigma_{LT}, \sigma_{TT}$  via simultaneous fit at two  $\epsilon$  settings.

$$\chi_{\text{total}}^2 = \chi^2(\epsilon_{\text{high}}) + \chi^2(\epsilon_{\text{low}})$$



# Analysis Procedure : Adding $\phi$ coverage

	$E = 8.2 \text{ GeV}, \epsilon = 0.39$		$E = 10.6 \text{ GeV}, \epsilon = 0.53$	
Setting	HMS	SHMS	HMS	SHMS
Left	25.952°	9.973°	14.987°	12.523°
Center	25.952°	6.973°	14.487°	9.473°
Right	—	—	14.487°	6.558°

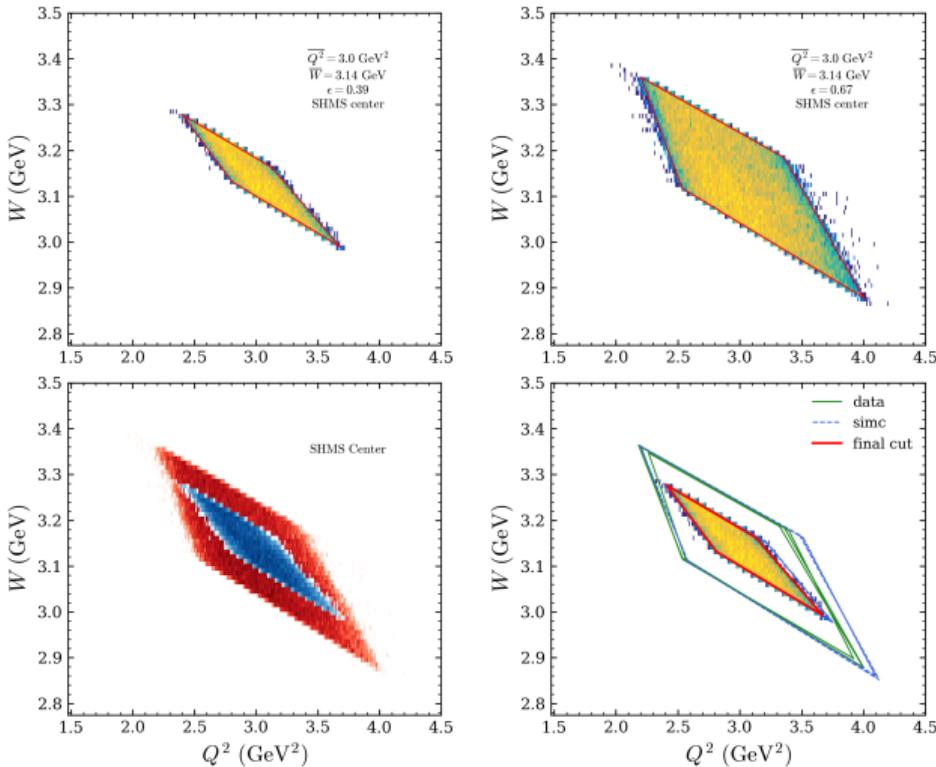


- Must Overlay data at Left/Center/Right SHMS settings to ensure a complete  $\phi$  coverage in each  $-t$  bin !

# Analysis Procedures : Coverage Selection by Diamond cut

## Phase space matching

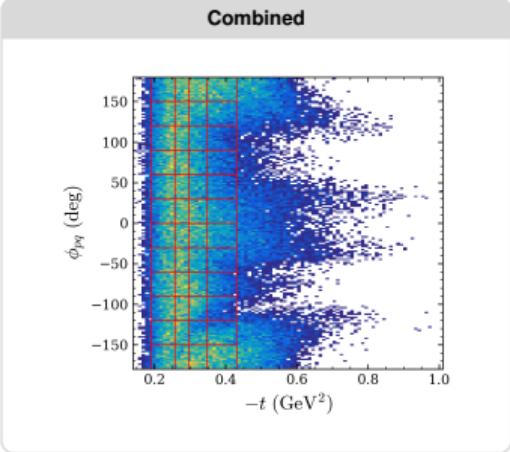
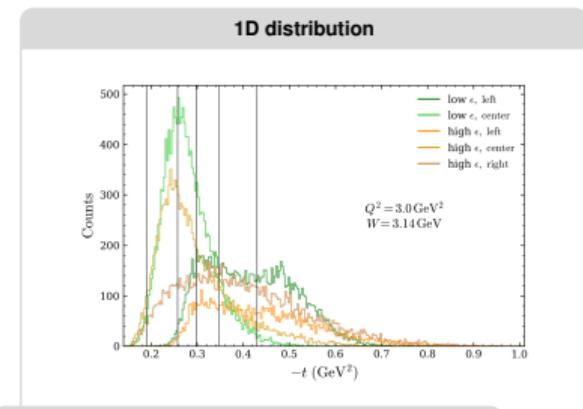
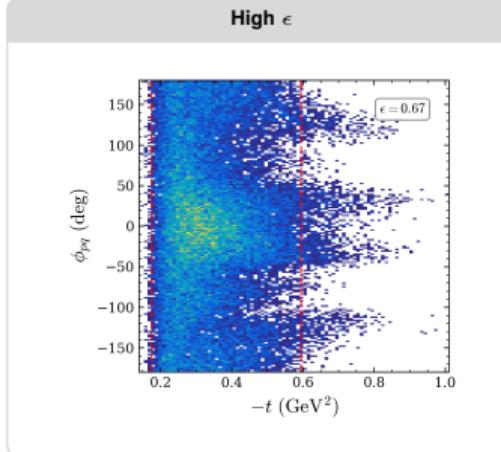
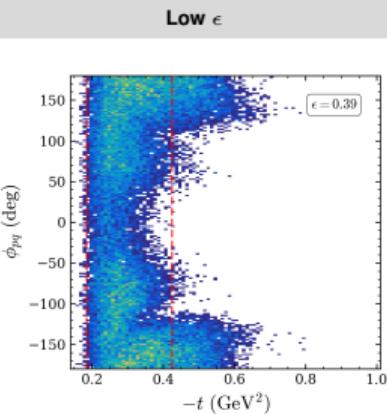
- LT separation requires consistent phase space between two  $\epsilon$  settings (e.g.  $Q^2$ ,  $W$ ,  $\theta$ )
- HMS, SHMS acceptance depend on  $\epsilon$  for fixed energy settings
- Apply diamond cut in both data and SIMC  $\rightarrow$  take the overlapping region



# Analysis Procedures : Binning selection in $| -t|$ and $\phi$

**Mandelstam variable**  $t = (p_\gamma - p_{K+})^2$

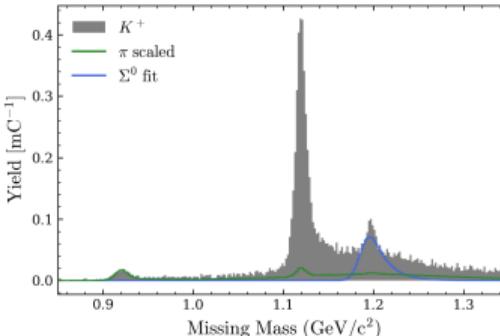
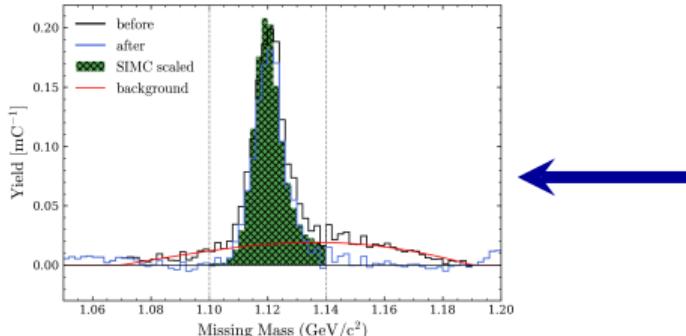
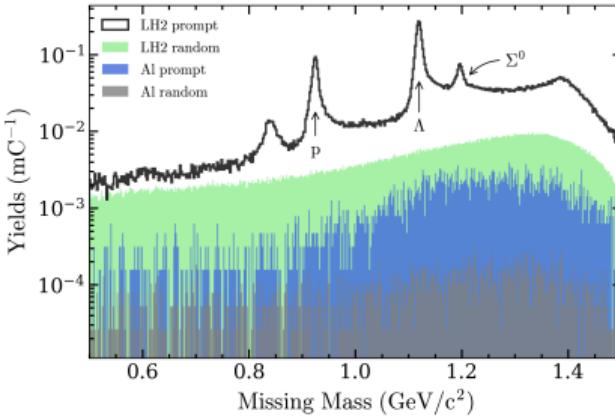
- LT separation requires at least one  $\epsilon$  setting has full  $\phi$  coverage
- Optimal binning choice due to scarce statistics
- Keep as many bins in  $| -t|$  for their dependence in  $\sigma_L$



# Analysis Procedures : Removing Background

## Background contributions

- ▷ Random coincidence ( $\sim 2\%$ )
- ▷ dummy Al target ( $\sim 5\%$ )
- ▷ pion contamination  $\rightarrow$  scale  $\pi$  data
- ▷  $\Sigma^0$  peak contamination
- ▷ empirical fit to match SIMC  $\Lambda$  shape



- ▶ Repeat for each  $t/\phi$  bin and extract yields  $M_X \in (1.10, 1.14) \text{ GeV}/c^2$

# Analysis Procedures: Functional Form for Monte Carlo

## Parameterization of cross section model in SIMC

- Used to weight each event in SIMC to match experimental kinematics and acceptance
- The choice of functional form must faithfully represent Hall C acceptance and kinematic distributions.

### Model Structure Functions

$$\sigma_L = w \cdot p_0 f(t) \exp(-p_1 t)$$

$$\sigma_T = w \cdot p_4 \exp(-p_5 t)$$

$$\sigma_{LT} = w \cdot p_8 \exp(-p_9 t) \sin(\theta^* + \delta)$$

$$\sigma_{TT} = w \cdot p_{12} \exp(-p_{13} t) \sin^2 \theta^*$$

### Physics

***t*-dependence:** Exponential terms included in every structure function to describe fall-off.

**Pole factor:**  $f(t) = \frac{1}{(t - M_K^2)^2}$  accounts for *t*-channel dominance in  $\sigma_L$ .

**Interference terms:** Angular  $\sin \theta^*$  dependence ensures  $\sigma_{LT}, \sigma_{TT} \rightarrow 0$  at parallel kinematics.

***W*-dependence:** Global weight *w* accounts for variations across different *t*-bins.

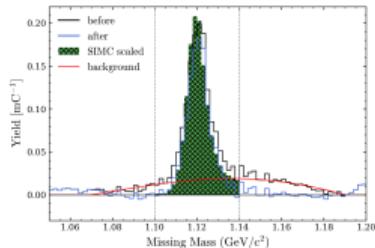
### Global W-Weight

$$w(W) = \frac{1}{(W^2 - M_p^2)^2}$$

**Note:** Any choice of form is valid as long as it correctly weights the cross-section within the Hall C acceptance.

## 0 Prepare Data Yields

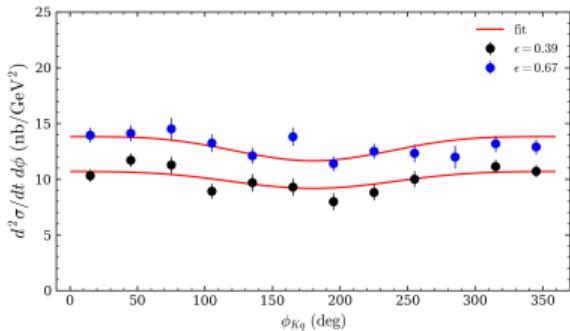
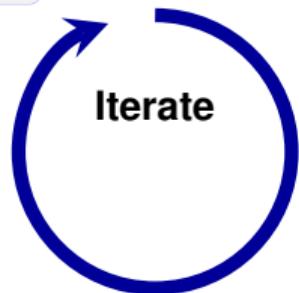
- diamond, acceptance, cointime
- subtract backgrounds
- $M_X$  cut



## 1 Prepare $\sigma_{\text{MC}}$ Model

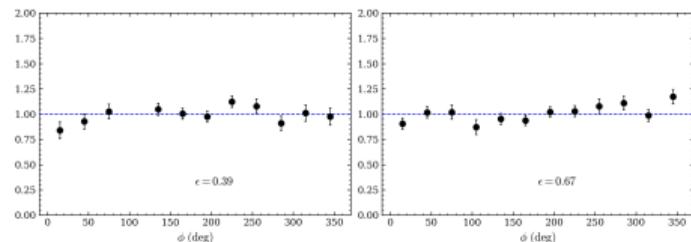
$$\sigma_L \equiv \sigma_L(t, \bar{Q}^2, \bar{W}, \bar{\theta}^*; p_0, p_1, \dots)$$

5 Fit  $\{p_i\}$  for next iteration



## 2 Compare Data Yields to SIMC Yields for each $t/\phi$ bin

$$R = Y_{\text{data}}/Y_{\text{SIMC}}$$



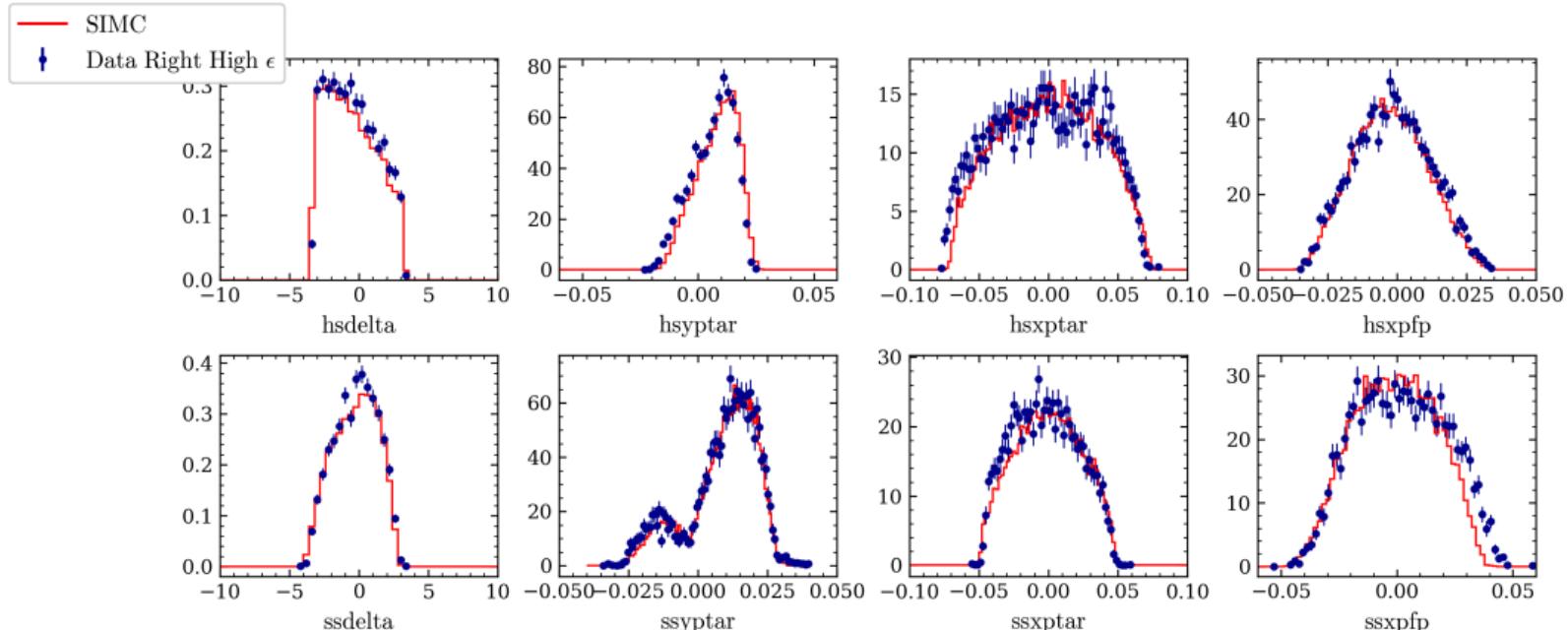
## 3 Normalize Cross Section with Yield Ratio

$$\sigma_{\text{EXP}} = \frac{Y_{\text{data}}}{Y_{\text{SIMC}}} \cdot \sigma_{\text{SIMC}}$$

## 4 Simultaneously fit $\sigma_L, \sigma_T, \sigma_{LT}, \sigma_{TT}$ for each $t$ bin

$$2\pi \frac{d^2\sigma}{dtd\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{LT}}{dt} \cos\phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$

# HMS and SHMS distributions



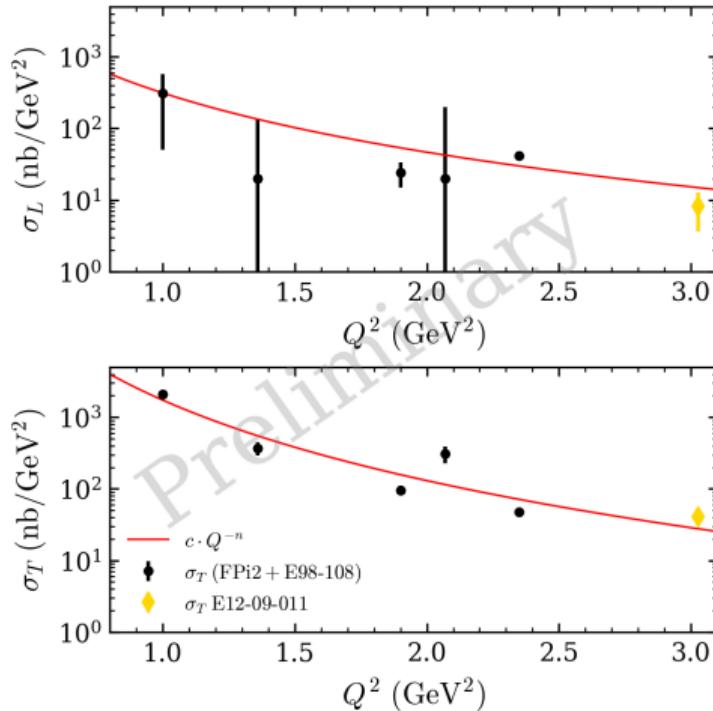
- Agreement between data and SIMC in both HMS and SHMS kinematic distributions after iteration.

# $Q^{-n}$ Scaling at $x_B \approx 0.3$

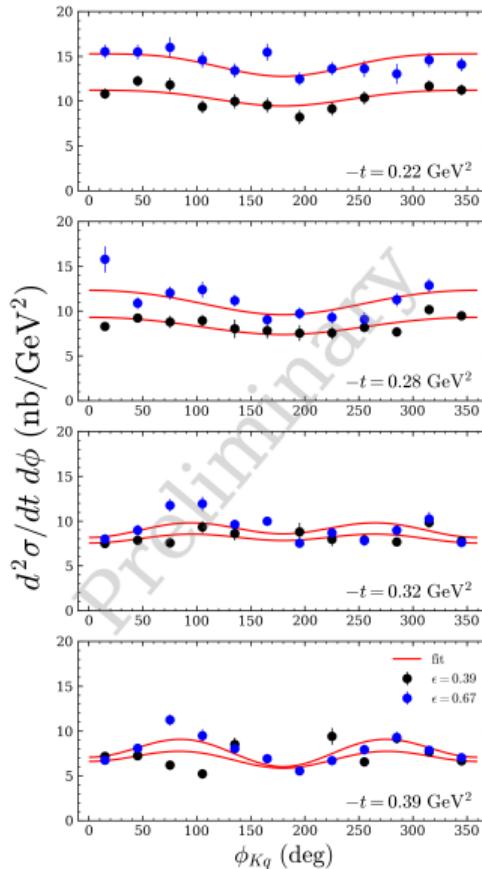
## Test QCD Scaling Predictions

- Existing data : E93-018 and FPI2 at  $x_B = 0.3, t = 0.4$ .
- This work :  $Q^2 = 3.0 \text{ GeV}^2, x_B = 0.25, t \approx 0.4 \text{ GeV}^2$ .
- Fit results:
  - $\sigma_L \sim Q^{-5.50 \pm 0.25}$
  - $\sigma_T \sim Q^{-7.47 \pm 0.13}$

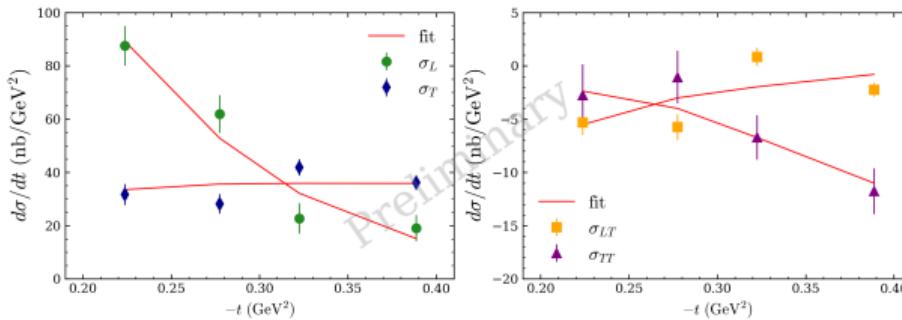
- ▶ Preliminary result shows consistency QCD scaling predictions.
- ▶ Further analysis required to scale new data to the same  $x_B$  and  $t$  using Regge model.



# Preliminary Result $Q^2 = 3.0 \text{ GeV}^2, W = 3.14 \text{ GeV}, x_B = 0.25$



$$2\pi \frac{d^2\sigma}{dtd\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{LT}}{dt} \cos \phi + \epsilon \frac{d\sigma_{TT}}{dt} \cos 2\phi$$



## Result Summary

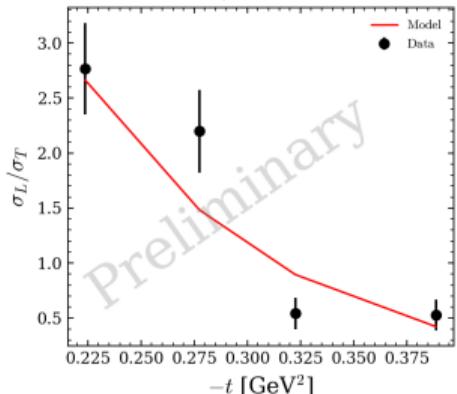
- Longitudinal term  $\sigma_L$  decreases exponentially with  $t$  indicating kaon pole dominance  $\rightarrow$  Form factor extraction
- Transverse term  $\sigma_T < \sigma_L$  and relatively flat across  $t \rightarrow$  non-pole contribution
- Interference terms  $\sigma_{TT} \rightarrow 0$  at low  $|t|$  and  $\sigma_{LT} \approx 0$  at all  $t$  (Only stat. uncertainty shown).

# Cross section extraction other settings

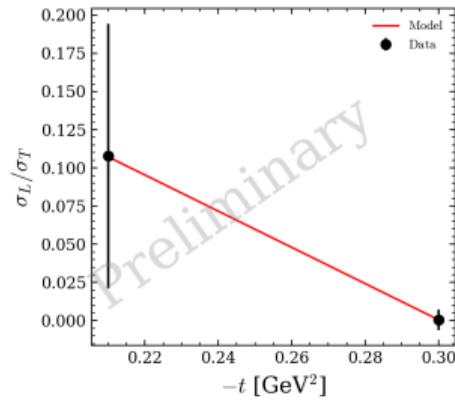
## Preliminary Findings $\sigma_L/\sigma_T$

- $\sigma_L \sim \exp(t)$  in all settings suggest kaon pole dominance
- Feasibility of form factor extraction at high  $Q^2 \approx 5 \text{ GeV}^2$ .
- $\sigma_T > \sigma_L$  at  $Q^2 = 2.1, 4.4 \text{ GeV}^2$
- relatively low statistics available these settings and further analysis required.

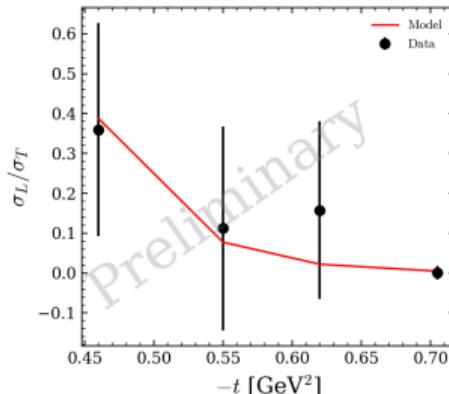
$$Q^2 = 3.0 \text{ GeV}^2, W = 3.14 \text{ GeV}$$



$$Q^2 = 2.1 \text{ GeV}^2, W = 2.95 \text{ GeV}$$



$$Q^2 = 4.4 \text{ GeV}^2, W = 2.74 \text{ GeV}$$



# Preliminary Form Factor Extraction

## Monopole Parameterization

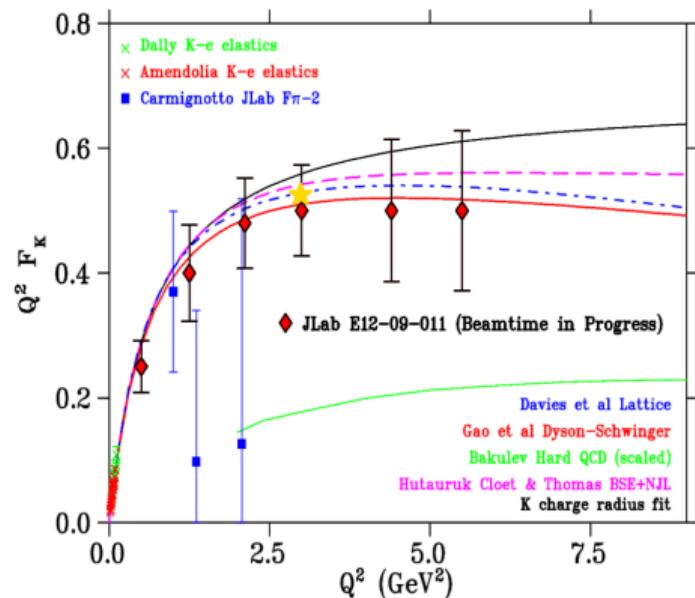
$$F_K(Q^2) = \frac{1}{1 + Q^2/\Lambda_K^2}$$

- Simultaneous fit of all structure functions using **VGL Regge model**.
- Model evaluated at precise kinematics  $(Q^2, W)$  for each  $t$ -bin.

## $\chi^2$ Minimization

$$\chi^2 = \sum_{i,j} \left( \frac{\sigma_{i,j}^{\text{data}} - \sigma_{i,j}^{\text{VGL}}(\Lambda_K)}{\delta\sigma_{i,j}^{\text{data}}} \right)^2$$

- **Best Fit:**  $\Lambda_K^2 \approx 0.6849 \pm 0.0562$
- **Result:**  $Q^2 F_K \approx 0.55$  at  $Q^2 = 3.0$



# Summary and Outlook

## Summary

- ✓ **E12-09-011 Data:** Collection complete; analysis in progress for  $Q^2 = 2.1 - 5.5 \text{ GeV}^2$ .
- ✓ **Methodology:** Successfully implemented iteration method for SIMC cross-section optimization.
- ✓ **Pole Dominance:** Preliminary results confirm Kaon pole dominance across multiple settings.
- ✓ **Extraction:** Preliminary  $F_K$  extraction at  $Q^2 = 3.0 \text{ GeV}^2$  via VGL Regge model.

## Outlook

- **Cross Analysis:** Verify results and perform rigorous systematic uncertainty studies.
- **Scaling Study:** Complete  $Q^2 = 2.1, 4.4, 5.5 \text{ GeV}^2$  analysis to fit  $\sigma_L$  scaling.
- **Modeling:** Incorporate  $Q^2$ -dependence into the global cross-section model.
- **Finalization:** Apply Coincidence Blocking and corrected HMS matrix values in Replay.

**Thank You for your attention!**

Questions?

Backup :  $Q^{-n}$  Scaling across  $x_B = 0.40$

## Backup : Systematic Uncertainties Study (To-be-done)