

Measurements of the $\text{Cos}\phi$ and $\text{Cos}2\phi$ Moments of the Unpolarized SIDIS π^+ Cross-section at CLAS12

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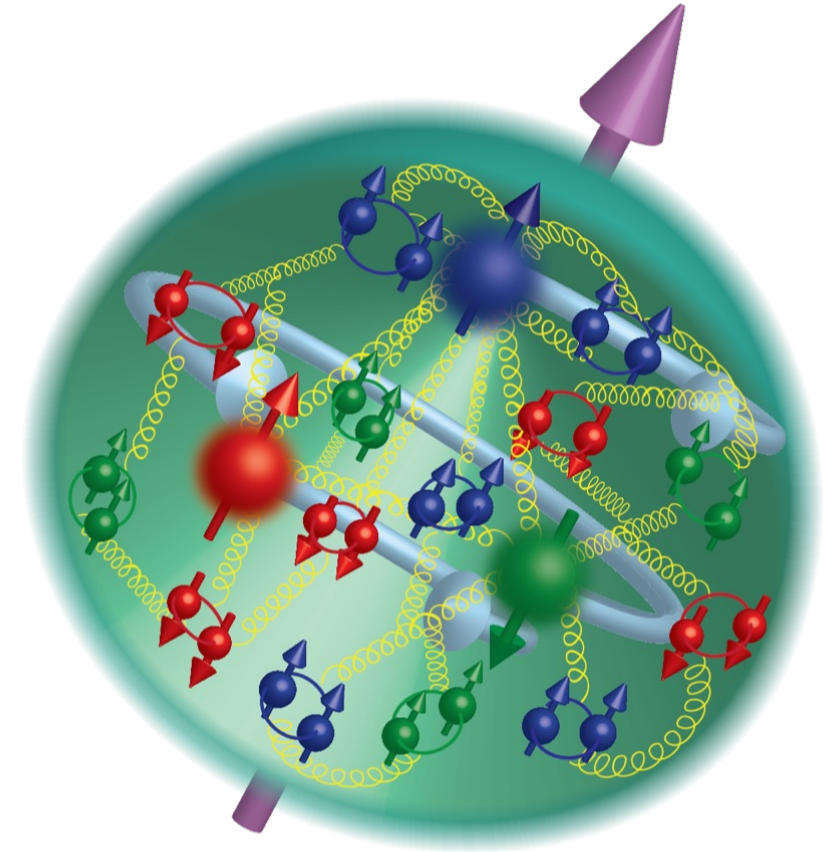
November CLAS Collaboration Meeting

LinkedIn



Motivation

- Semi-Inclusive Deep Inelastic Scattering: access to 3D structure of nucleons in momentum space
- Azimuthal modulations of unpolarized SIDIS cross-section for charged pion electroproduction can give access to the Cahn and Boer-Mulders effects
 - **Boer-Mulders Effect:** Sensitive to the correlation between the quark's transverse momentum and intrinsic transverse spin in an unpolarized nucleon
 - **Cahn Effect:** Sensitive to the transverse motion of quarks inside the nucleon
- A non-zero Boer-Mulders requires quark orbital angular momentum contributions to the proton spin



SIDIS Cross-Section and Boer-Mulders

Reaction Studied: $ep \rightarrow e\pi^+(X)$

$$\frac{d^5\sigma}{dx dQ^2 dz d\phi_h dP_{h\perp}^2} =$$

$$\underbrace{\frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) (F_{UU,T} + \epsilon F_{UU,L})}_{A_0} \left\{ 1 + \underbrace{\frac{\sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos\phi_h}} \cos\phi_h + \underbrace{\frac{\epsilon F_{UU}^{\cos 2\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos 2\phi_h}} \cos 2\phi_h \right\}$$

The Boer-Mulders and Cahn effects are present in the Structure Functions:

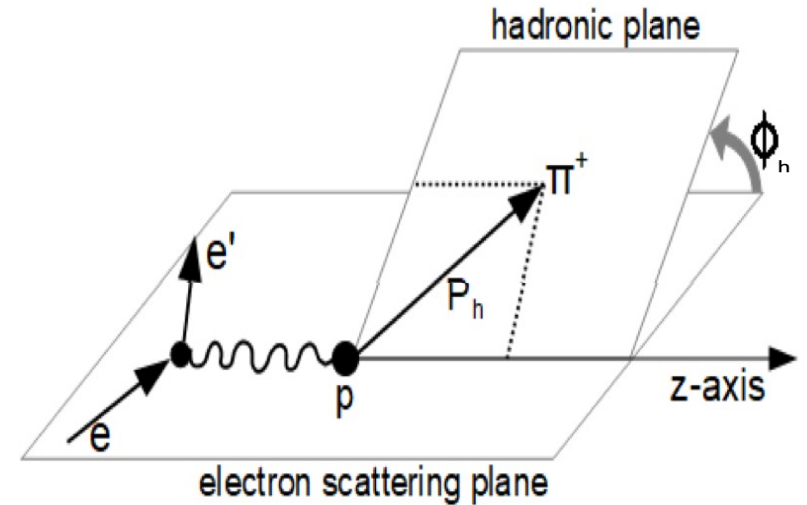
leading twist

$$F_{UU}^{\cos 2\phi_h} \propto C \left[\underbrace{-\frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h}}_{\text{BOER-MULDERS EFFECT}} - \underbrace{h_1^\perp H_1^\perp}_{\text{CAHN EFFECT}} + \dots \right]$$

next to leading twist

$$F_{UU}^{\cos\phi_h} \propto \frac{2M}{Q} C \left[\underbrace{-\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} x h H_1^\perp}_{\text{BOER-MULDERS EFFECT}} - \underbrace{\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1}_{\text{CAHN EFFECT}} + \dots \right]$$

Interaction dependent terms neglected



Event Selection

Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron (π^+) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity (β) and momentum

Using Data from RG-A Fall 2018
(Pass 2)

10.6 GeV Polarized Beam
Unpolarized Liquid Hydrogen Target
Inbending Forward Tracking Only

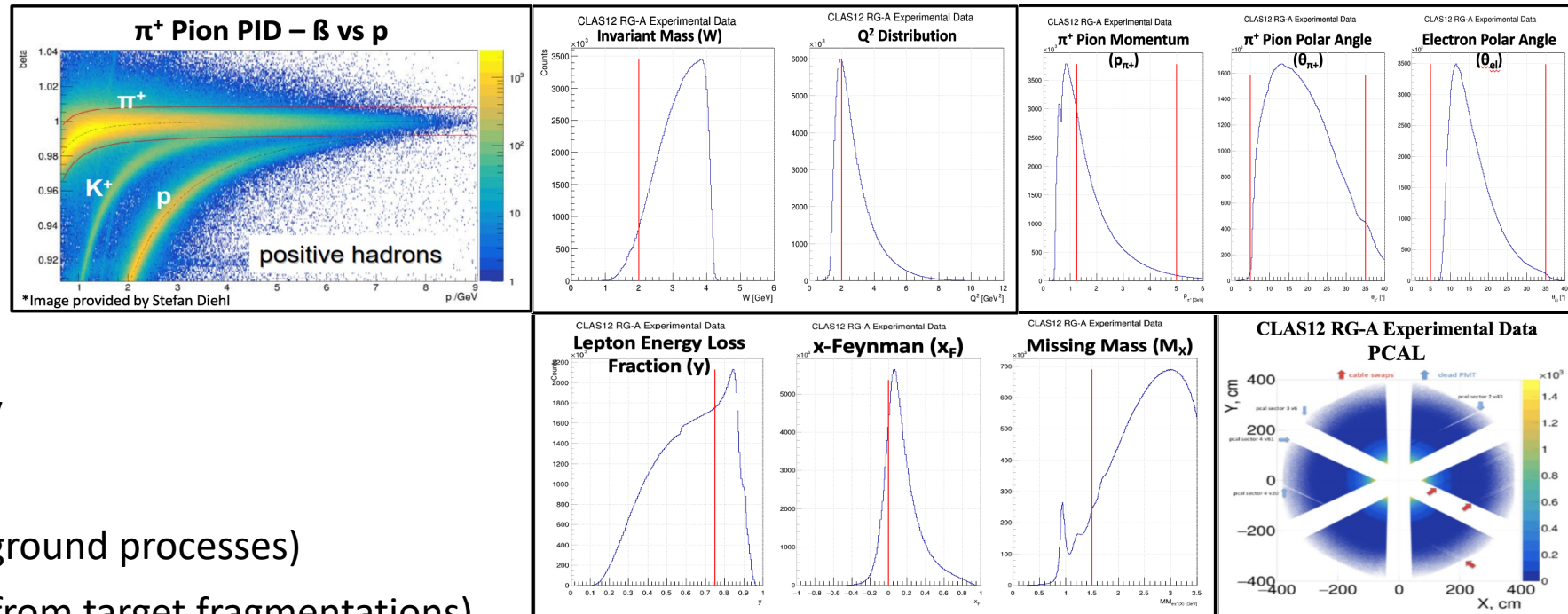
Analysis Cuts:

- **SIDIS Cuts:**

- $W > 2 \text{ GeV}$
- $Q^2 > 2 \text{ GeV}^2$

- **Other Analysis Cuts:**

- p_{π^+} Cut: $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- θ -angle Cut: $5^\circ < \theta_{\text{particle}} < 35^\circ$
- $y < 0.75$ (minimize other background processes)
- $x_F > 0$ (minimize contributions from target fragmentations)
- Missing Mass Cut: $M_x > 1.5 \text{ GeV}$ (limit on exclusive events)
- Fiducial Cuts (e.g., accounts for bad channels present in data)



Analysis Procedure

Experimental extraction of cross-section

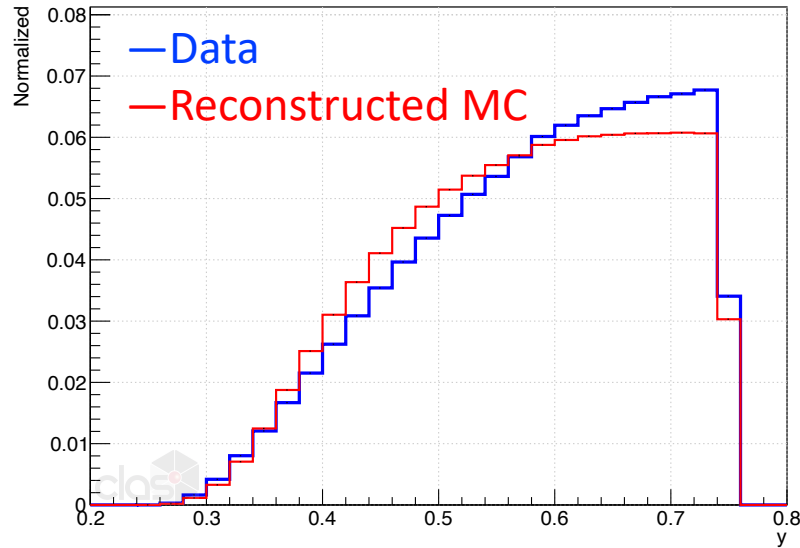
$$\frac{d^5\sigma}{dQ^2 dy dP_T dz d\phi_h} = \frac{1}{\underbrace{N_0 \left(N_A \cdot \rho \cdot \frac{t}{A_w} \right) \cdot \Gamma_\nu \cdot BC \cdot \Delta Q^2 \Delta y \Delta P_T \Delta z \Delta \phi_h}_{\text{Normalization factors that only impact } A_0}} \cdot \underbrace{\frac{N}{RC \cdot \eta}}_{\text{Needed to measure } A_{UU}^{\cos \phi_h} \text{ and } A_{UU}^{\cos 2\phi_h}} \Rightarrow A_0 (1 + A_{UU}^{\cos \phi_h} \cos \phi_h + A_{UU}^{\cos 2\phi_h} \cos 2\phi_h)$$

- η = Acceptance Correction 
 - RC = Radiative Correction 
 - N = Bin Yields
- Require Monte Carlo (MC) Simulations**

Acceptance corrections uses LEPTO (6.5) event generator
Radiative corrections uses “SIDIS-RC EvGen” — Event Generator*

Data and Monte Carlo Comparison

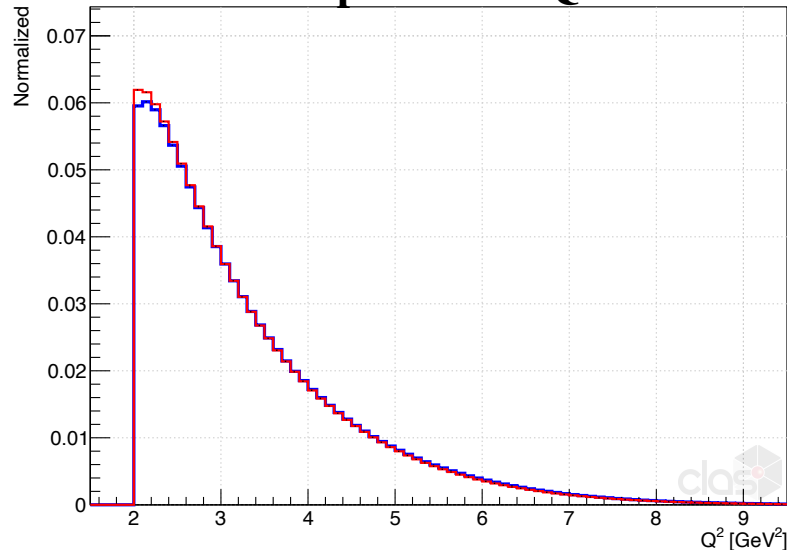
Comparison of y



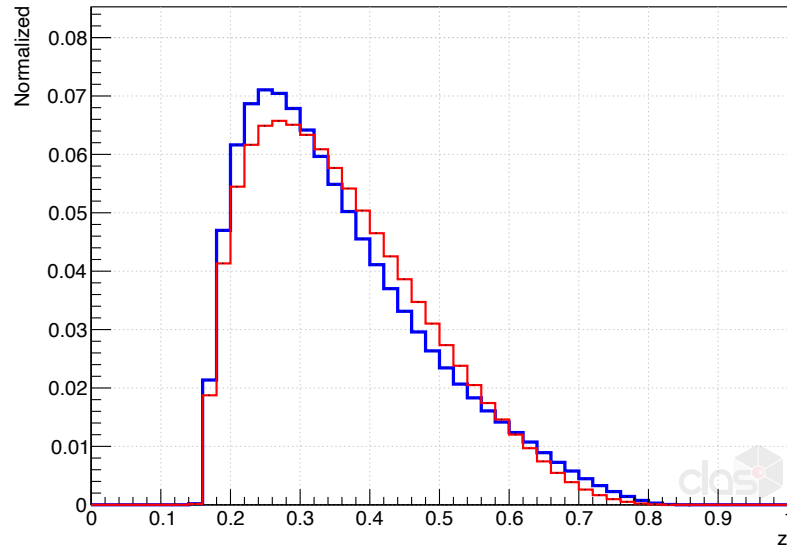
Reconstructed MC SIDIS π^+ Events (No radiative effects)

- These distributions have reasonable agreement
- Mismatch in high y is likely caused by the lack of radiative effects

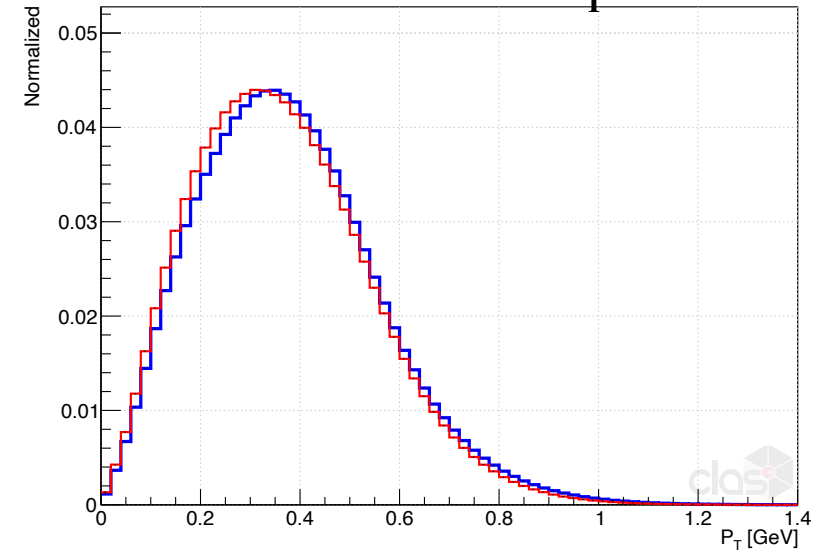
Comparison of Q^2



Comparison of z

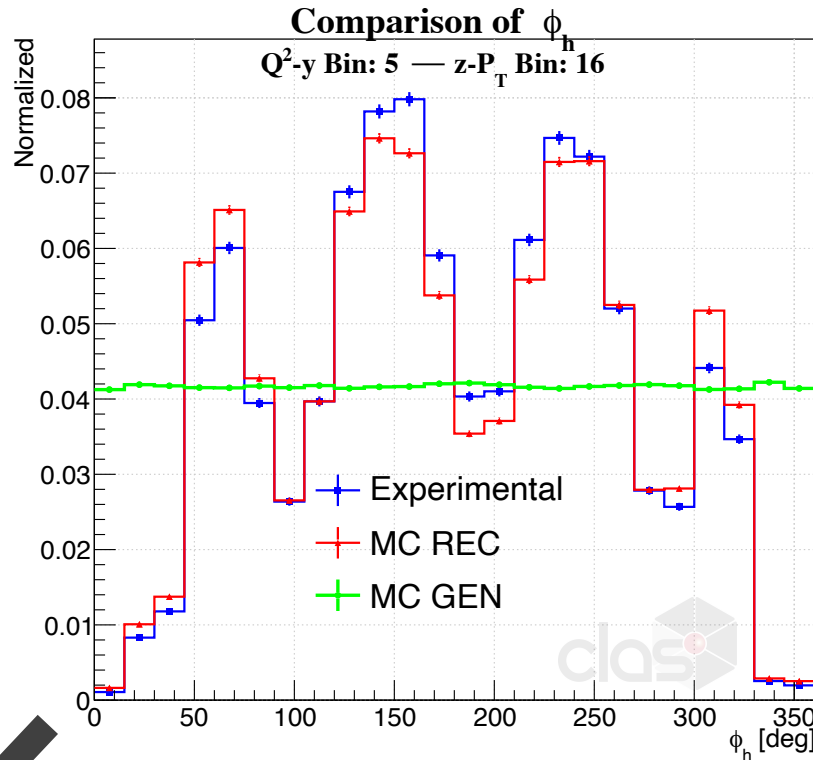


Comparison of P_T

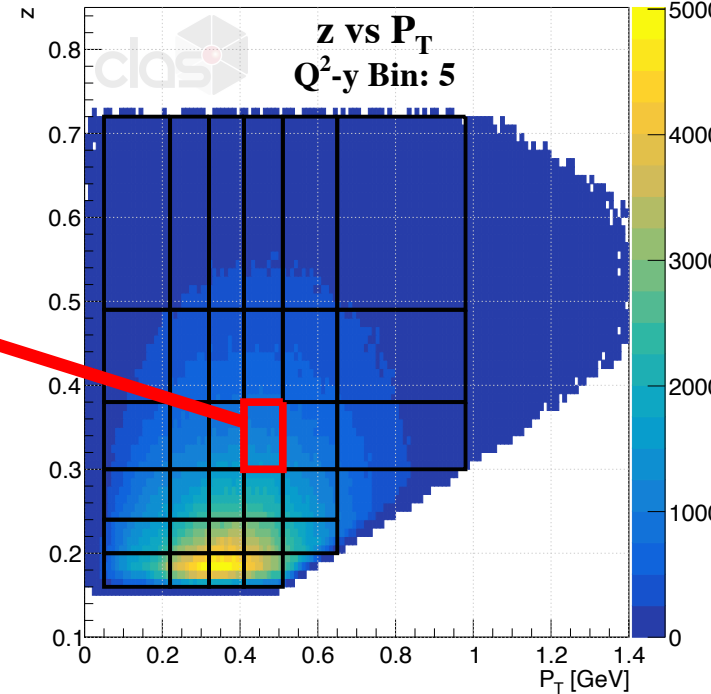


Multidimensional Analysis Procedures

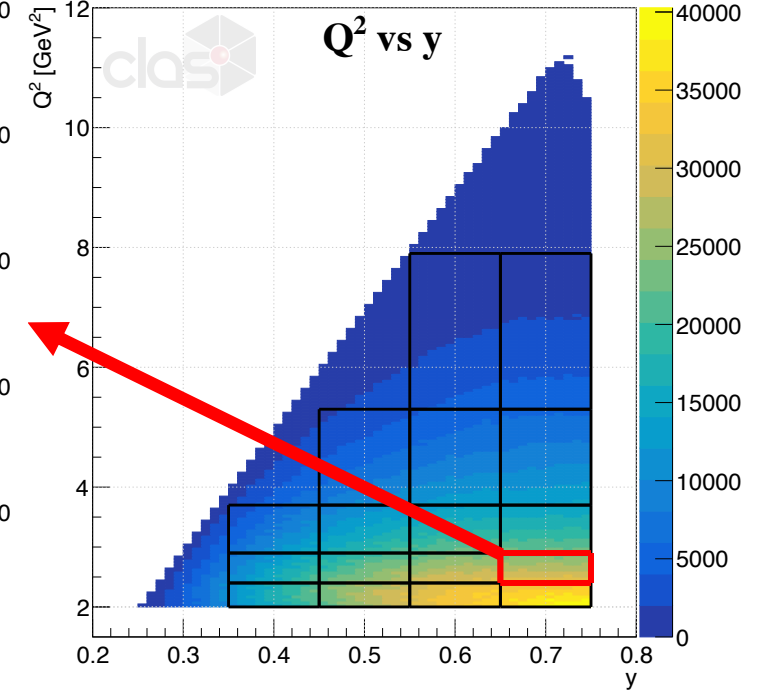
17 Q^2 - y Bins Total – 22-34 z - P_T Bins (per Q^2 - y bin) — Total: 486 Bins (with 24 ϕ_h bins each)



Experimental Data



Experimental Data



Apply Multidimensional Acceptance and Radiative Corrections

Fit with

$$A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$$

Where the parameters B, C give the cosine moments of the cross section

$$A_{UU}^{\cos \phi_h} = B$$

$$A_{UU}^{\cos 2\phi_h} = C$$

The three ϕ_h plots are normalized to their own total number of events

Acceptance Corrections and Bin Migration Study

- **Acceptance Matrix:** $A_{(i, j)}$ describes both Acceptance (including geometric acceptance and detector efficiency) and Bin Migration

- $A_{(i, j)} =$

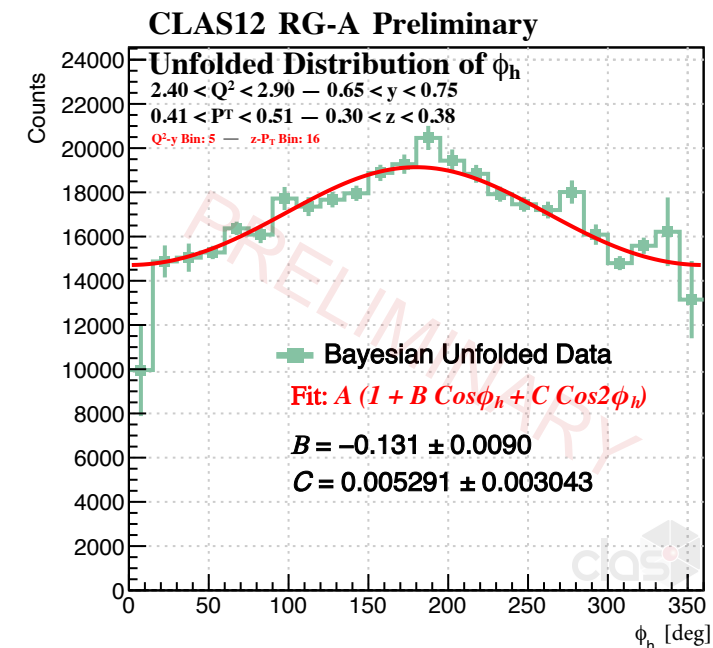
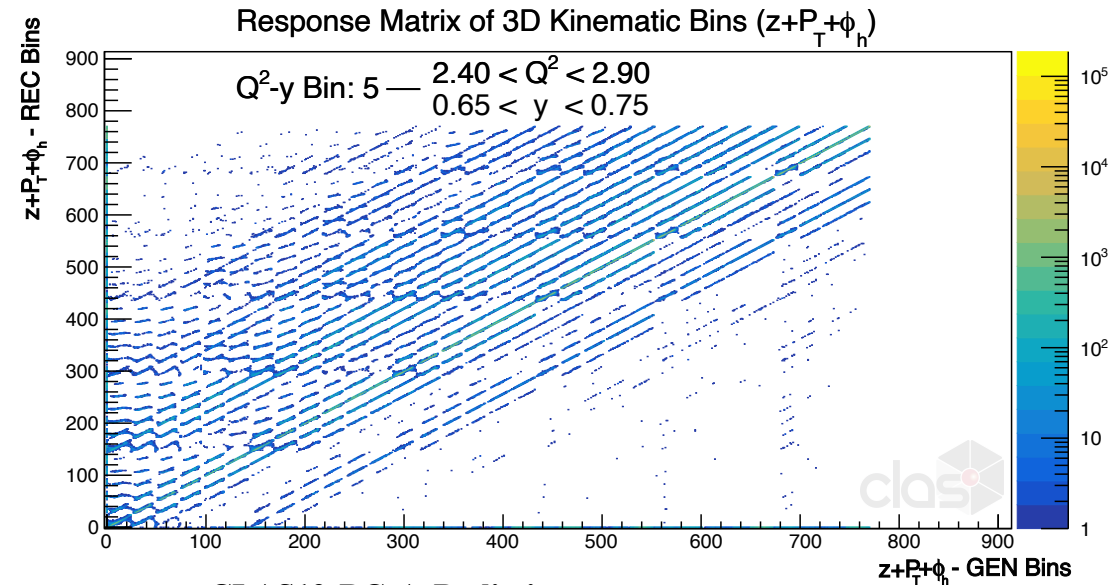
$$\frac{\text{Number of Events Generated in bin } j \text{ but Reconstructed in bin } i}{\text{Total Number of Events Generated in the } j\text{th bin}}$$

- Acceptance Unfolding:

$$Y_i = A_{(i, j)} X_j + \beta_i \Leftrightarrow X_j = A_{(i, j)}^{-1} (Y_i - \beta_i)$$

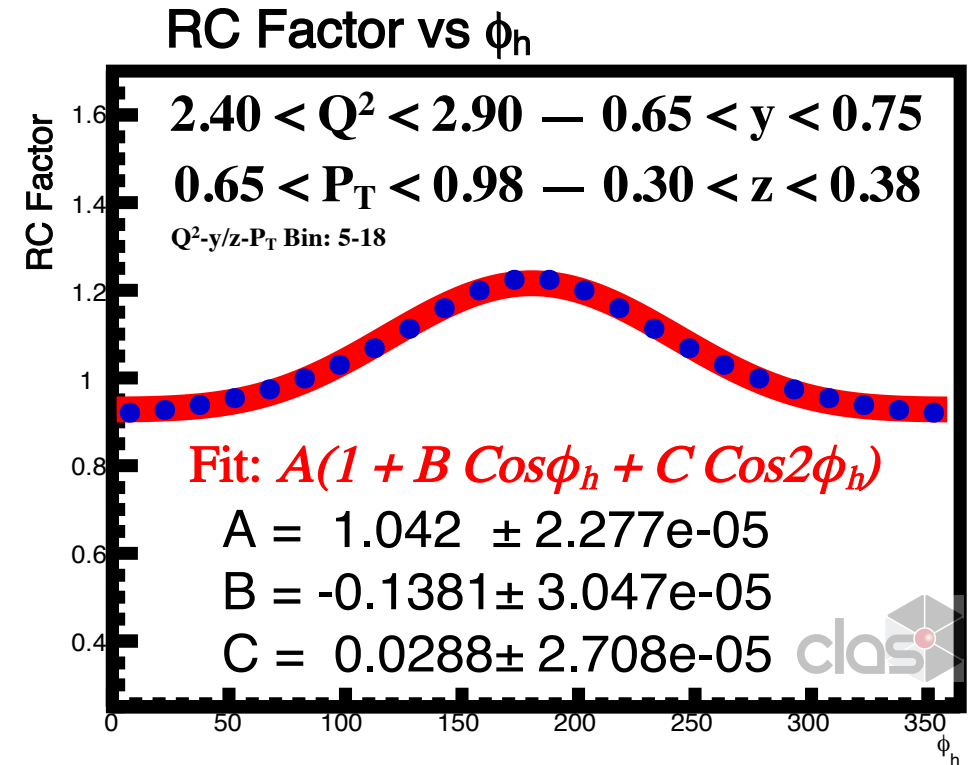
where:

- Y_i = Number of events experimentally measured in the i -th bin
- X_j = Number of acceptance-corrected events in the j -th bin
- β_i = Number of events from outside the signal region measured in the i -th bin



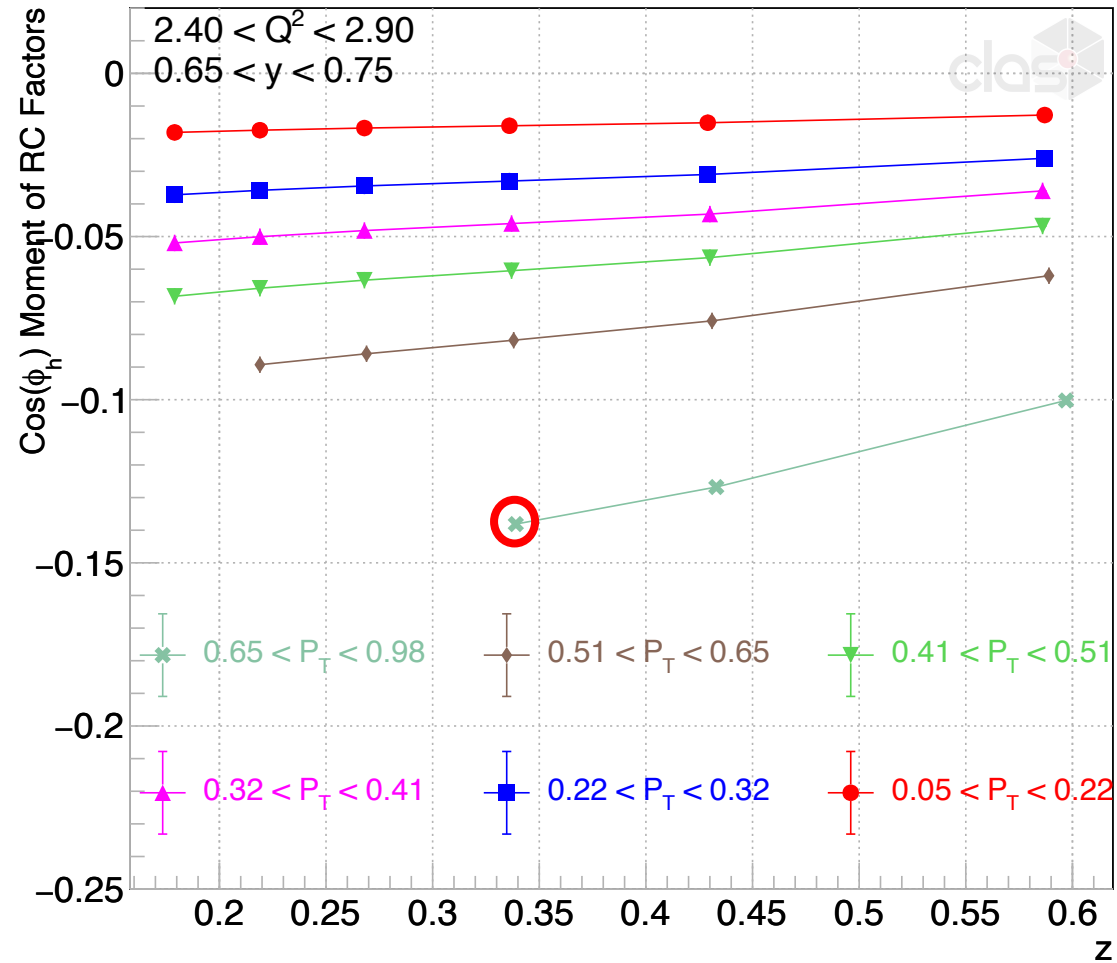
Importance of Radiative Corrections to the Cosine Moments

- **RC Factor** = $\frac{\sigma_{RAD}}{\sigma_{BORN}}$ (From EvGen)
- RC Factors are calculated for each Q^2 - y - z - P_T - ϕ_h bin (using bin centers)
- Will be applied as per bin weights to the differential cross section level
- RC Factors show a cosine-like dependence on ϕ_h
 - Fitting with the same formula for moment extraction can show the impact of these corrections on the final moments

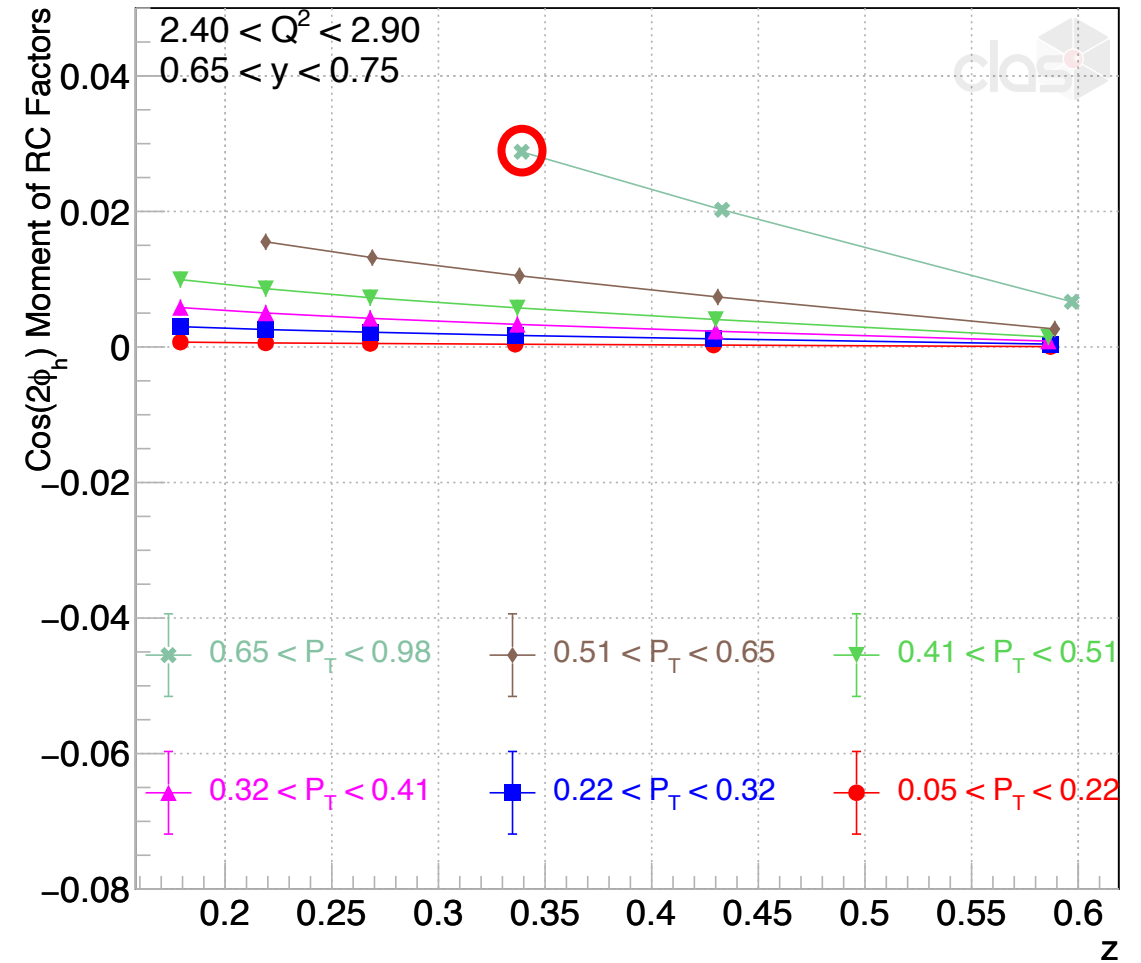


Importance of Radiative Corrections to the Cosine Moments

$\text{Cos}(\phi_h)$ Moments of the RC Factors



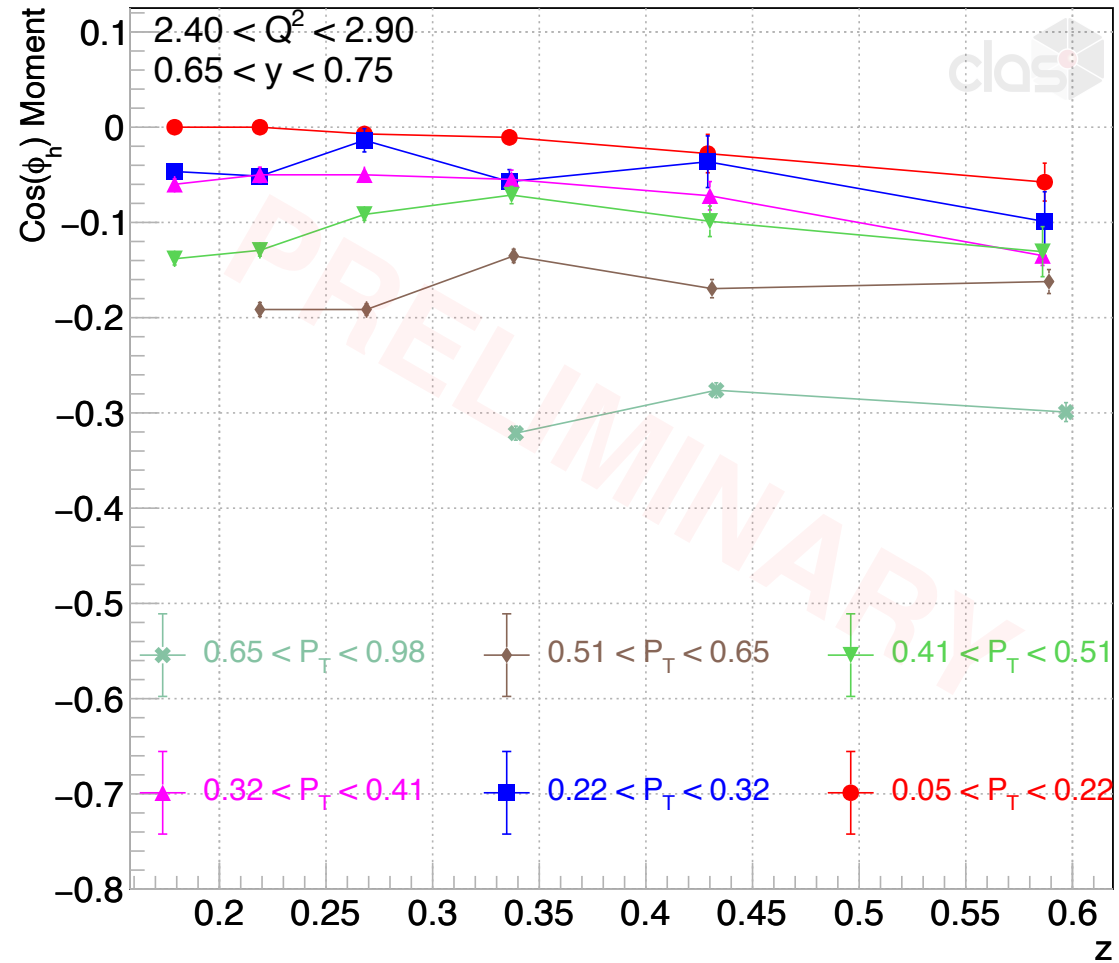
$\text{Cos}(2\phi_h)$ Moments of the RC Factors



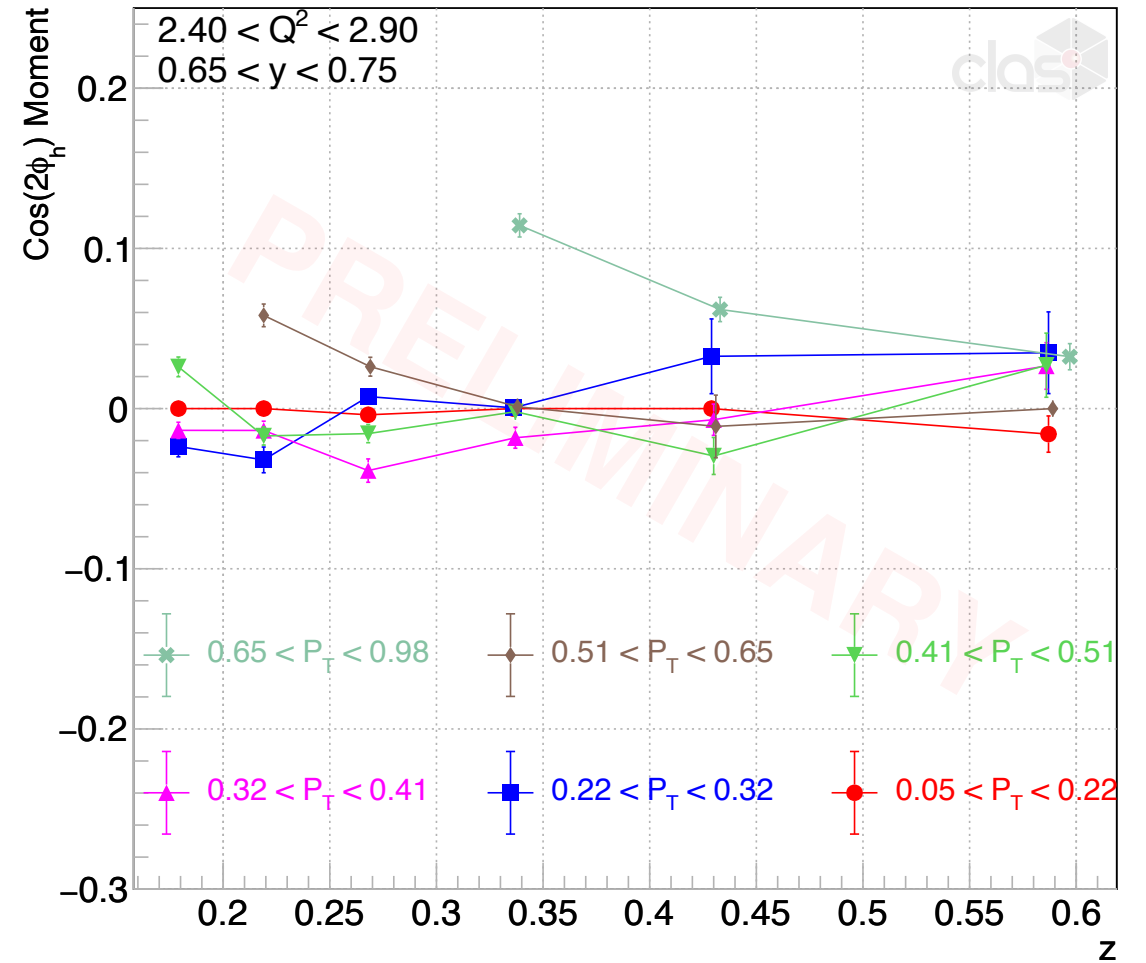
*Circled point is from the example on the last slide

Cosine Moments as Functions of z

CLAS12 Preliminary — $\text{Cos}(\phi_h)$ Moments
With RC Factors

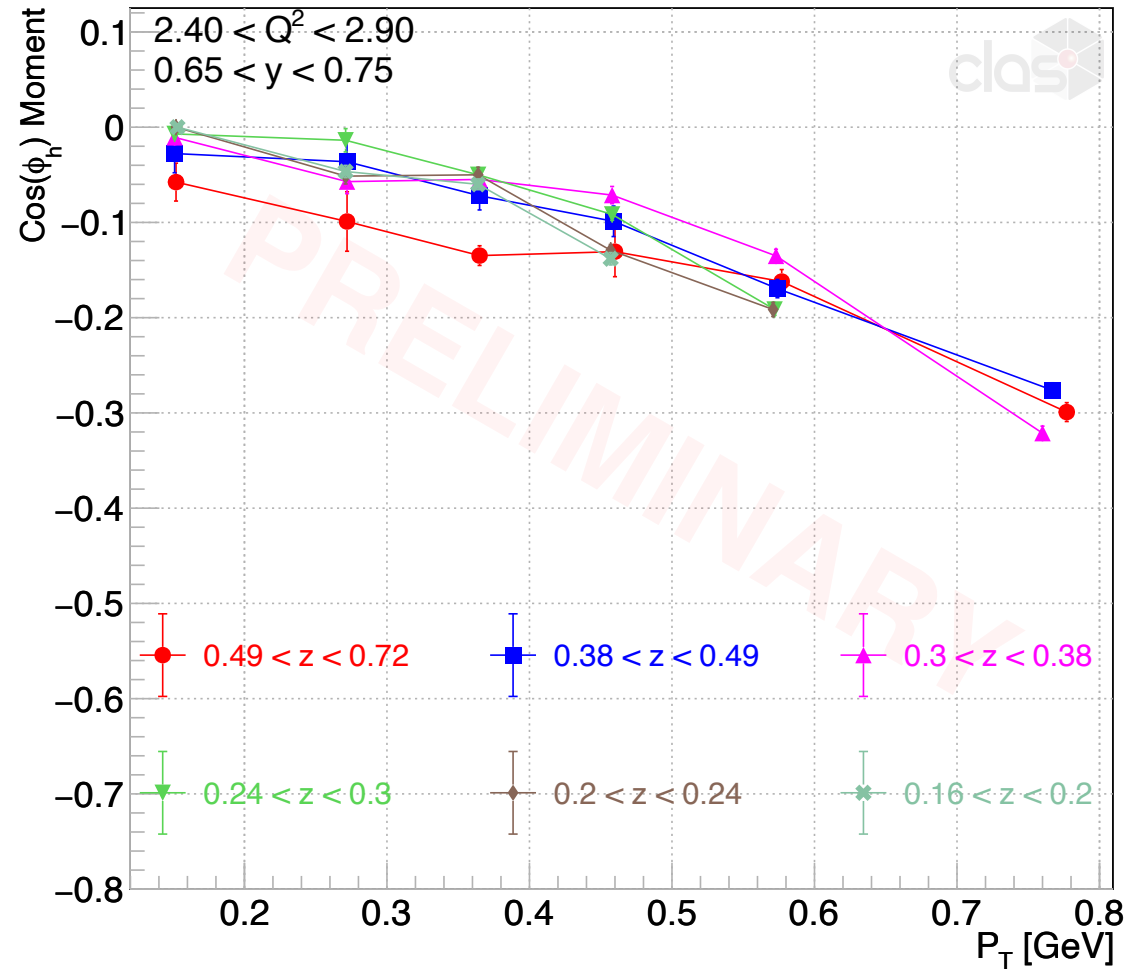


CLAS12 Preliminary — $\text{Cos}(2\phi_h)$ Moments
With RC Factors

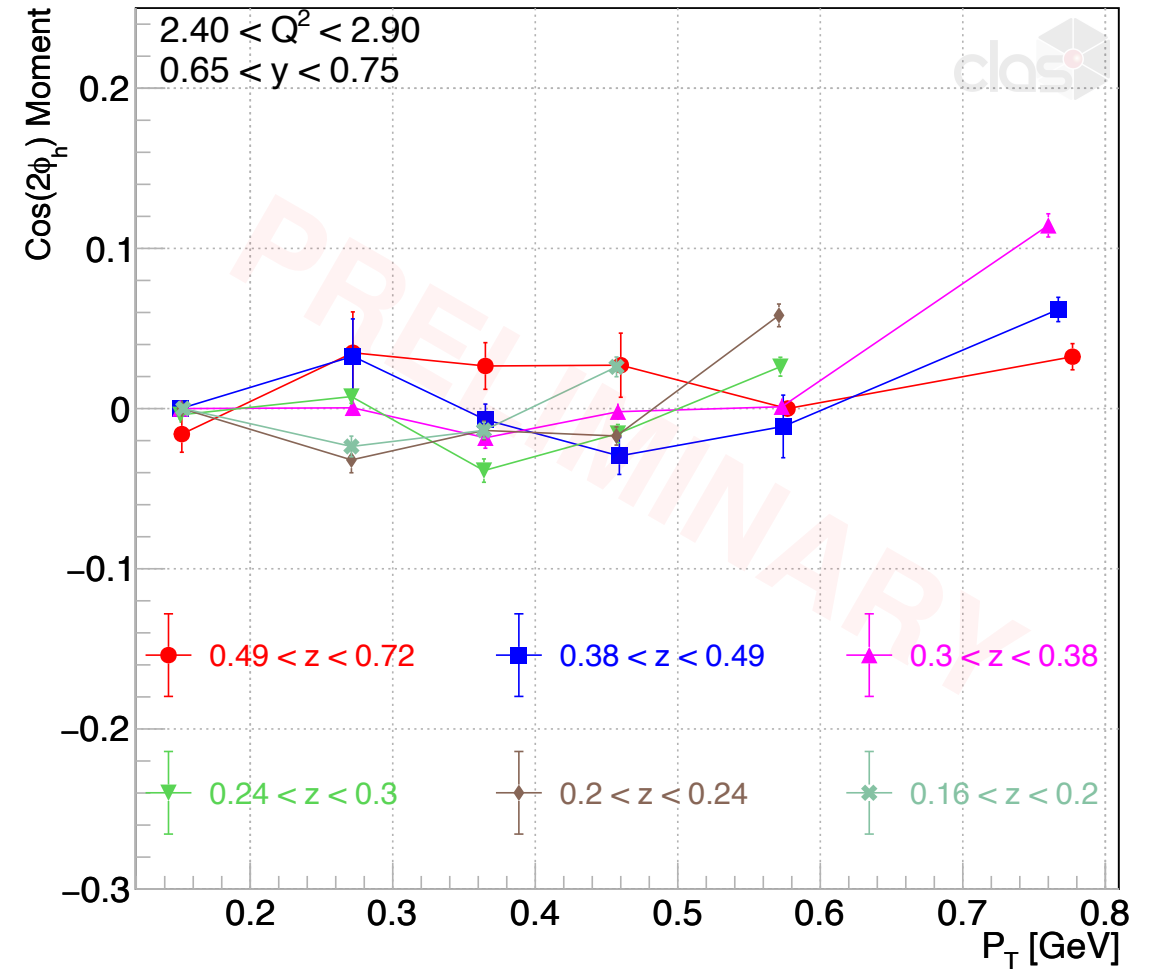


Cosine Moments as Functions of P_T

CLAS12 Preliminary — $\text{Cos}(\phi_h)$ Moments
With RC Factors

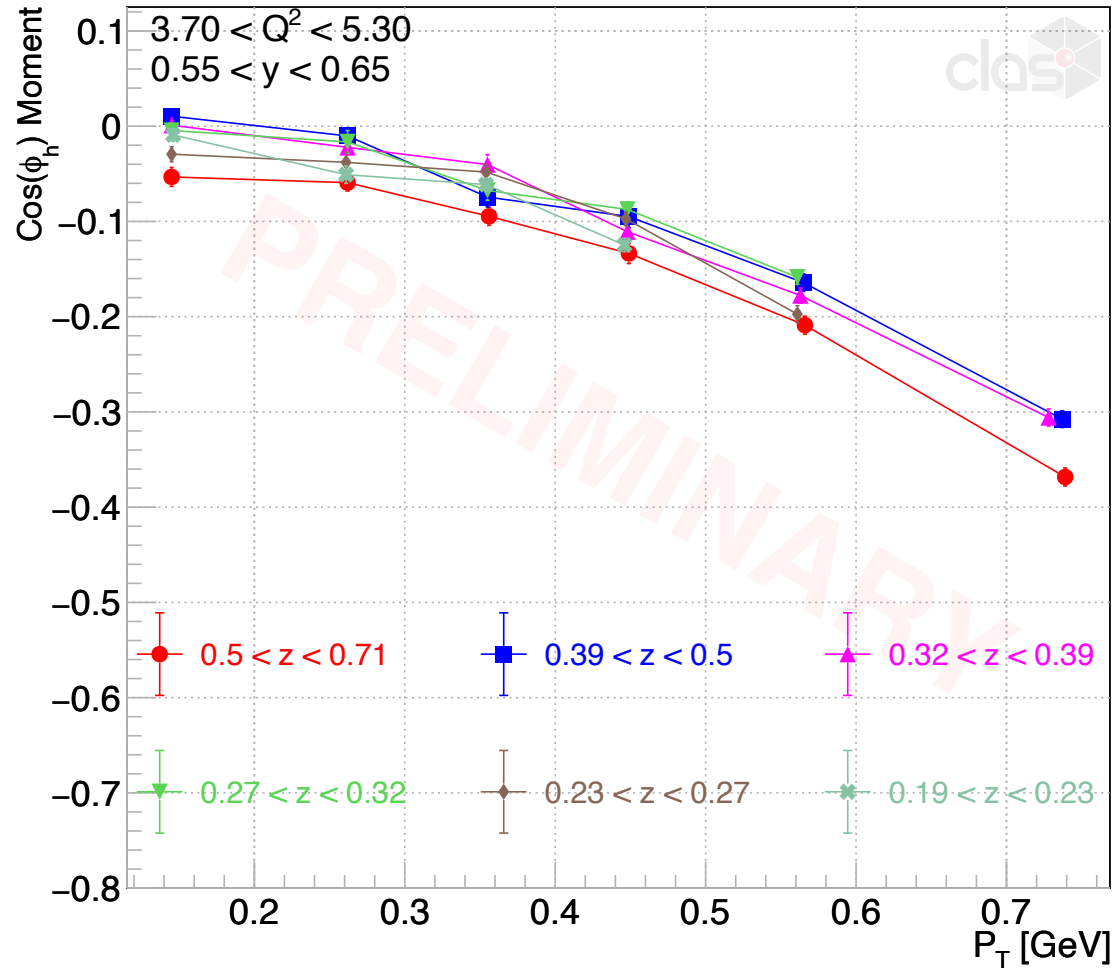


CLAS12 Preliminary — $\text{Cos}(2\phi_h)$ Moments
With RC Factors

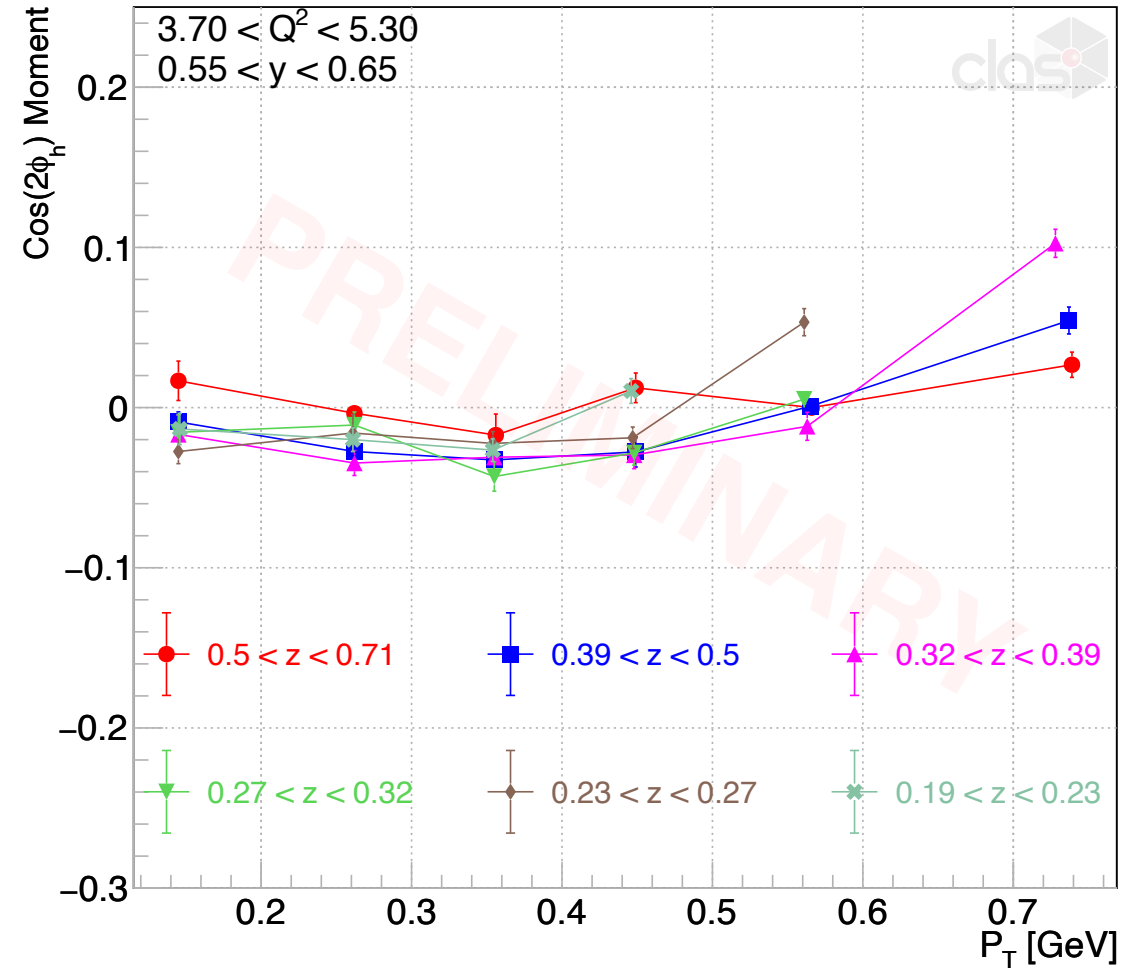


Cosine Moments as Functions of P_T — Secondary Example

CLAS12 Preliminary — $\text{Cos}(\phi_h)$ Moments
With RC Factors



CLAS12 Preliminary — $\text{Cos}(2\phi_h)$ Moments
With RC Factors



Summary & Outlook

- Preliminary extraction of the Cosine Moments in 486 Q^2 - y - z - P_T bins
 - Unfolded up to 3 dimensions
 - Introduced Radiative Corrections
- Measured $\text{Cos}(\phi)$ Moments with little z dependence and larger P_T dependence
 - Magnitude grows with P_T
- Measured $\text{Cos}(2\phi)$ Moments around 0 except for higher P_T
 - Magnitude decreases with z when not already suppressed for low P_T

➤ Work in progress:

- Extend to full 5D Unfolding
- Unfold with radiated Monte Carlo
- Assign systematic uncertainties

Thank you

Questions?

Acknowledgments and Thanks

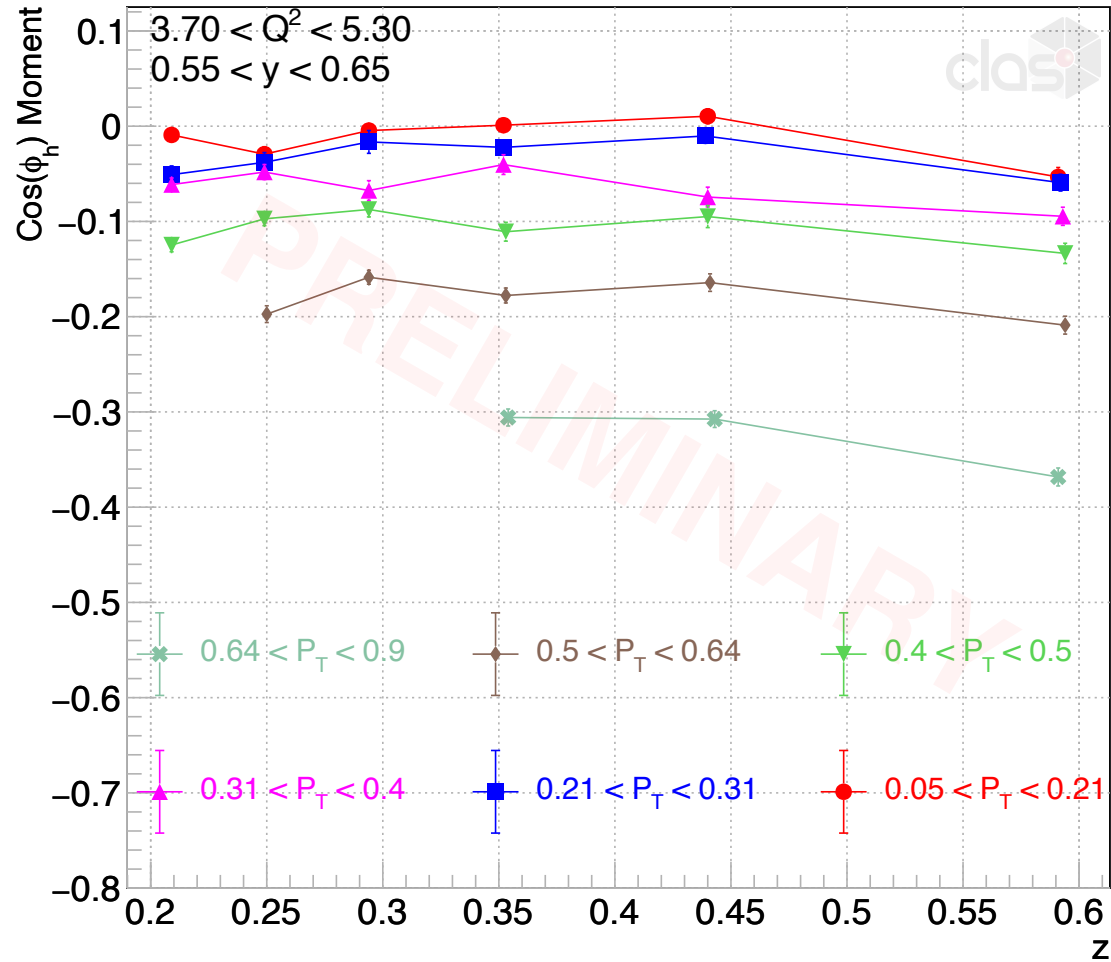
- Contributions made by other members of the CLAS Collaboration and researchers at Argonne National Lab
- This work is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under contract number DE-AC02-06CH11357



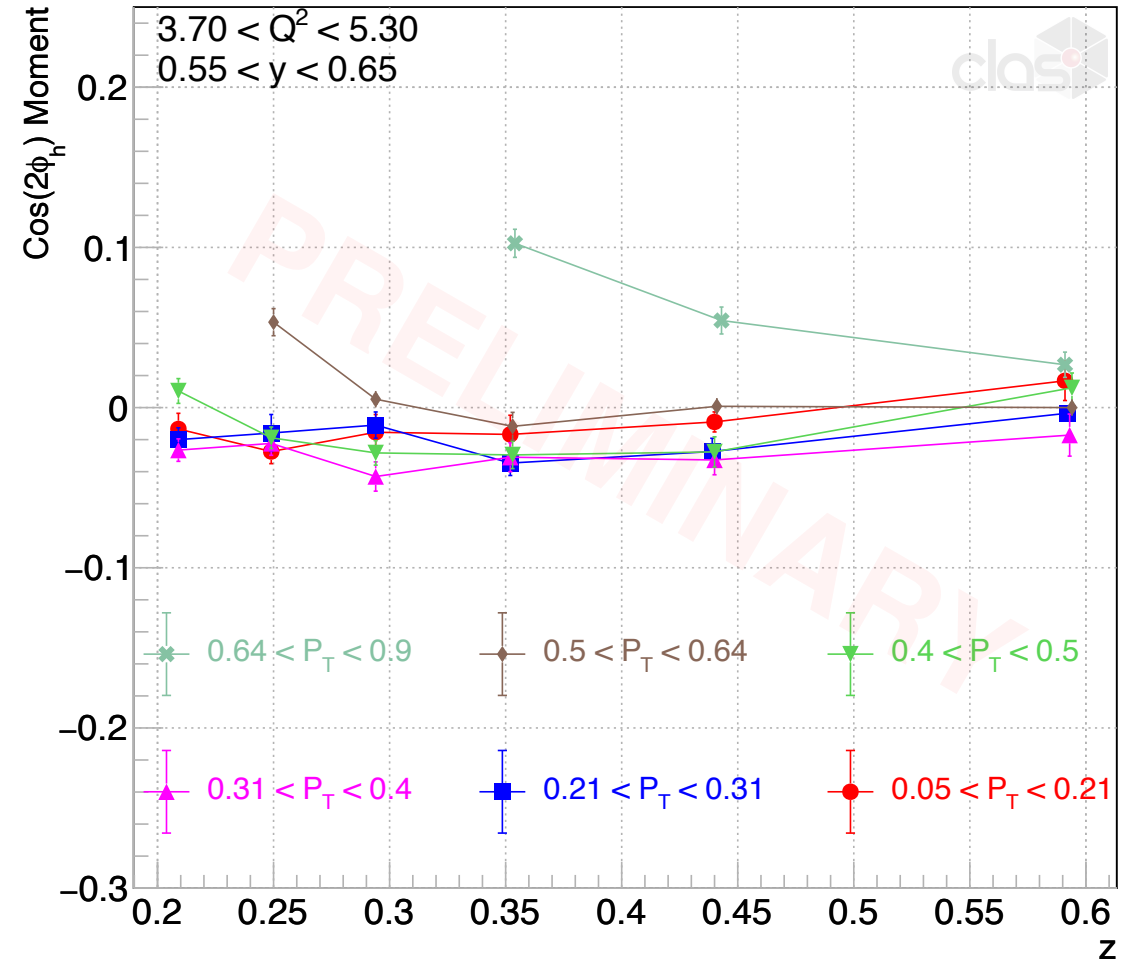
Backup Slides

Cosine Moments as Functions of z — Secondary Example

CLAS12 Preliminary — $\text{Cos}(\phi_h)$ Moments
With RC Factors

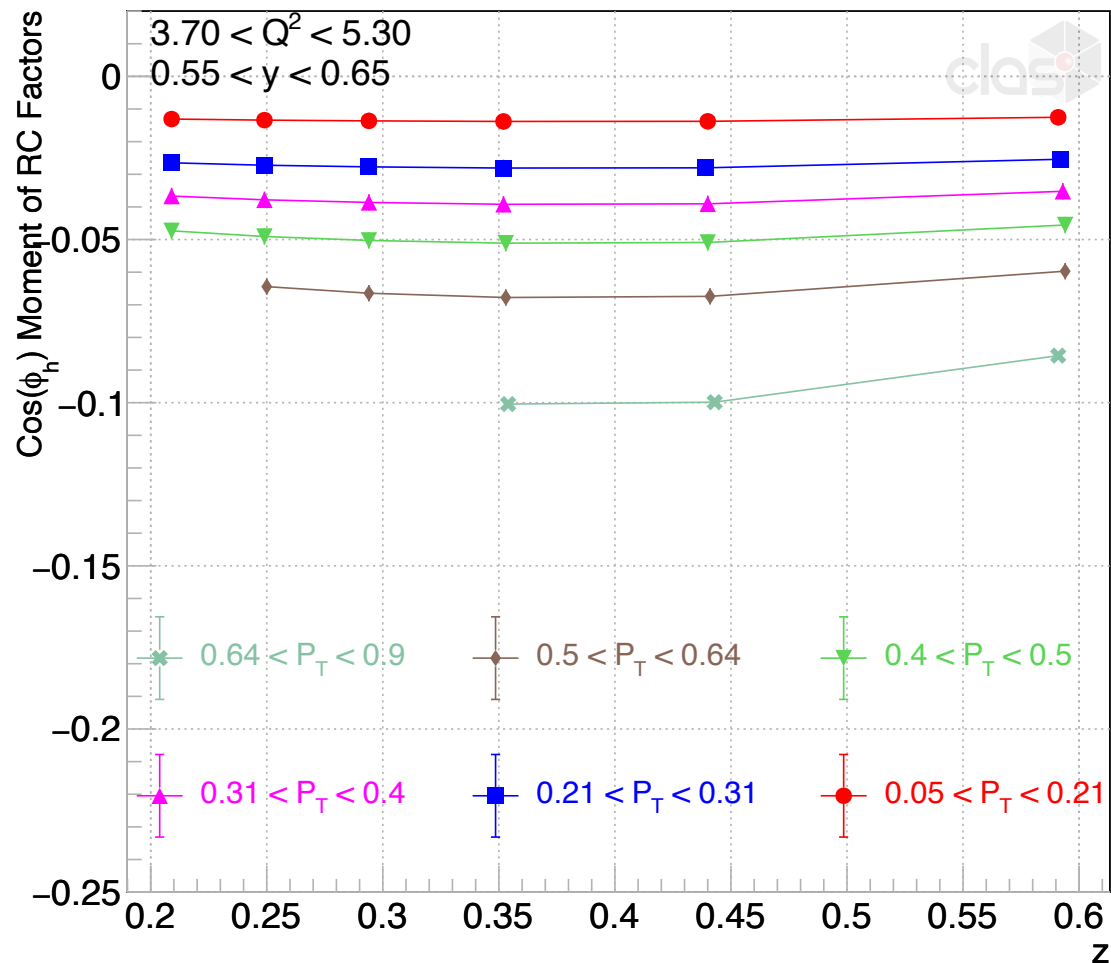


CLAS12 Preliminary — $\text{Cos}(2\phi_h)$ Moments
With RC Factors

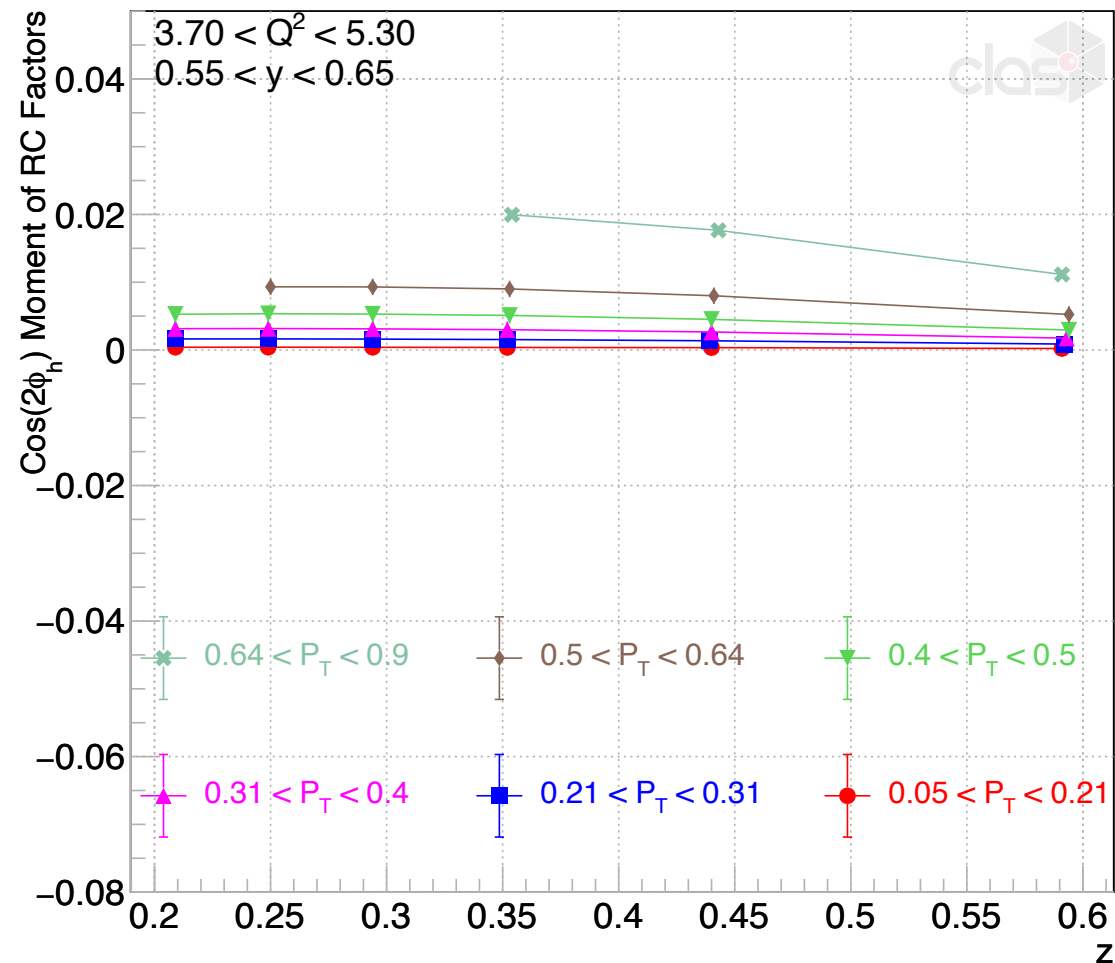


Importance of Radiative Corrections to the Cosine Moments — Secondary Example

$\text{Cos}(\phi_h)$ Moments of the RC Factors



$\text{Cos}(2\phi_h)$ Moments of the RC Factors



SIDIS-RC EvGen Overview

Is an RC Event Generator designed for SIDIS events ($ep \rightarrow e'\pi^+X$)

- Created by Duane Byer, et al. (Duke University) (see: <https://github.com/duanebyer/sidis/tree/8f9881ae958027c01daf3aa588caffcc47f6c11a>)
- Can generate radiated events and correction factors to go from the radiated cross-section to the Born level
- Generates the scattered lepton, hadron, and radiated photon (for radiated events)
- Just generates the selected SIDIS ($\pi^{+/-}$) process (No exclusive reactions or additional particles)
- Uses a six-fold differential cross-section for the non-radiated events and a nine-fold one for the radiated events
 - The extra 3 degrees of freedom in the radiated events are the photon kinematics
 - Includes ϕ_h modulations (unlike clasdis Monte Carlo)
 - Uses structure functions based on Gaussian and Wandzura-Wilczek-type approximations

Unpolarized Cross Section
used by EvGen:

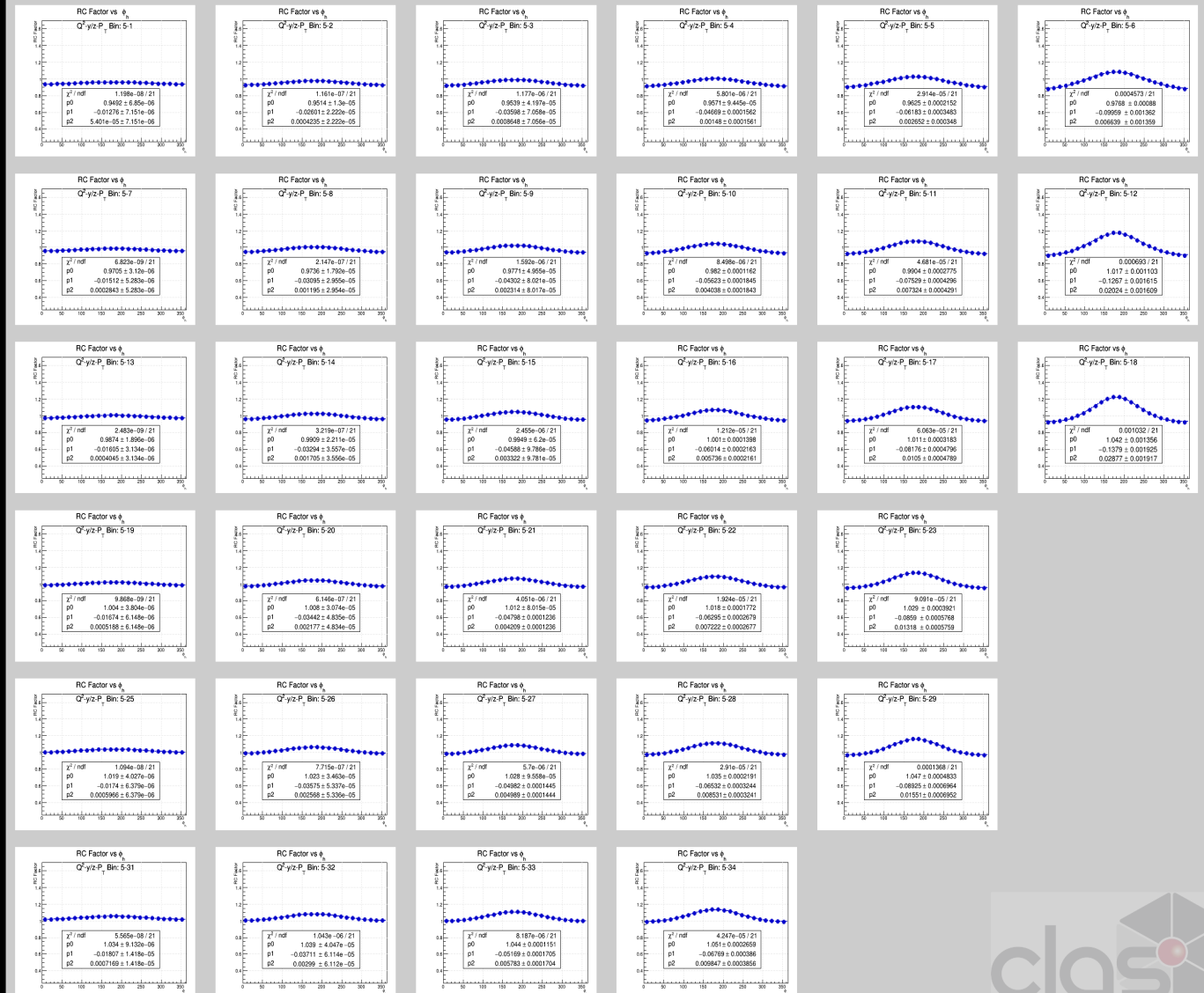
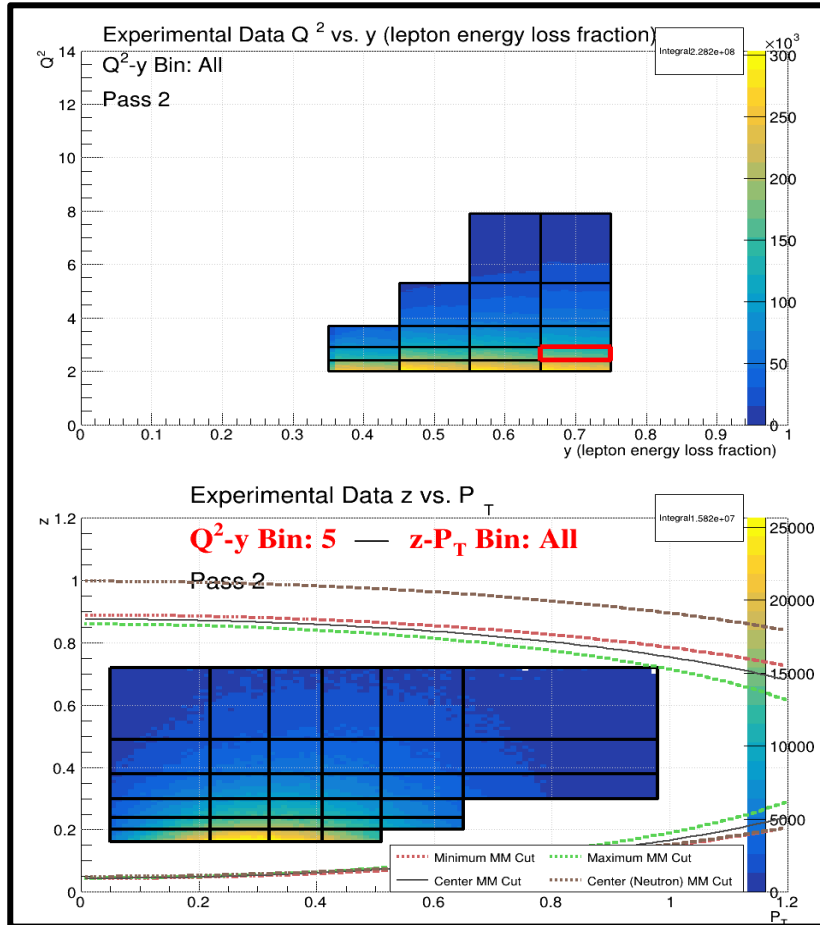
$$\frac{d\sigma_{\text{SIDIS}}}{dx_{Bj} dy dz_h dP_{hT}^2 d\phi_h d\phi_s} = \frac{\alpha^2}{x_{Bj} y Q^2} \left(1 + \frac{\gamma^2}{2x_{Bj}}\right) \times \left\{ \left[c_1 F_{UU,T} + c_2 F_{UU,L} + c_3 \cos(\phi_h) F_{UU}^{\cos(\phi_h)} + c_2 \cos(2\phi_h) F_{UU}^{\cos(2\phi_h)} \right] \right\}$$

$$\begin{aligned} \text{(i) Leading-twist } F_{UU}(x, z, P_{hT}) &= \{F_{UU} \equiv F_{UU,T}\} \\ &= x_{Bj} \sum_a e_a^2 f_c^a(x_{Bj}) D_c^a(z_h) \frac{e^{-P_{hT}^2 / \langle P_{hT}^2 \rangle}}{\pi \langle P_{hT}^2 \rangle}, \end{aligned} \quad (13)$$

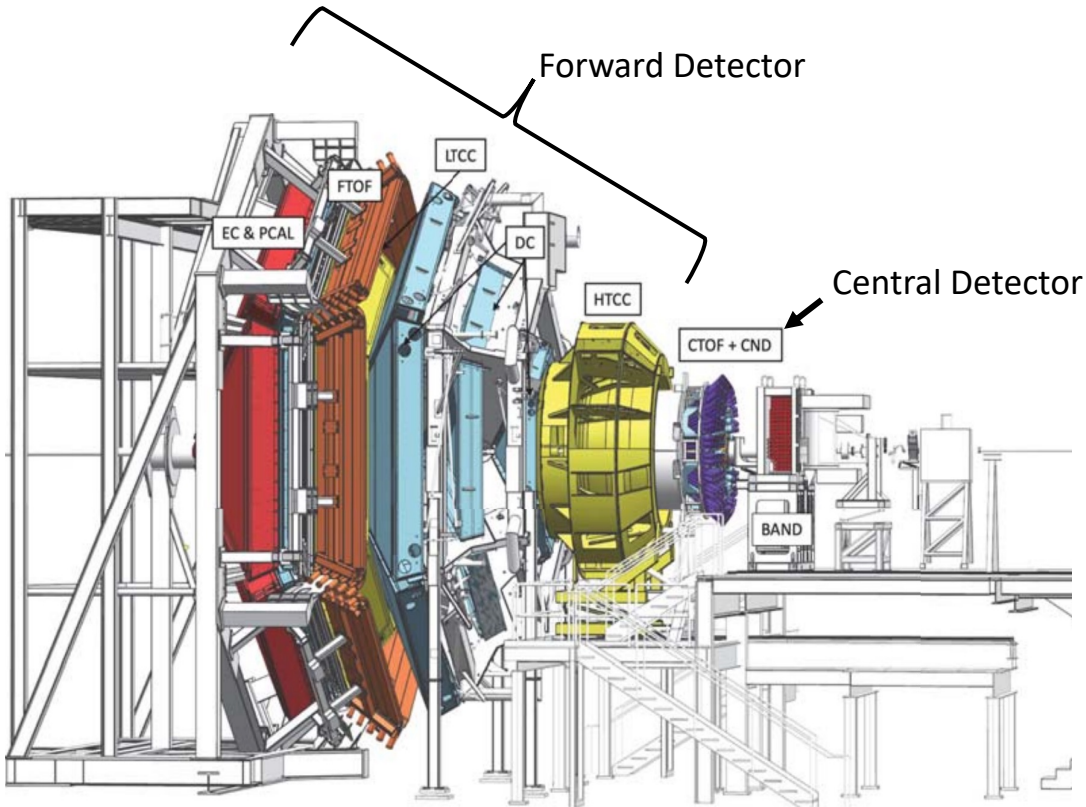
Example of Binned RC Factors

Q^2 -y Bin 5 (Low Q^2 —High y)

RC Factors as a function of ϕ_h



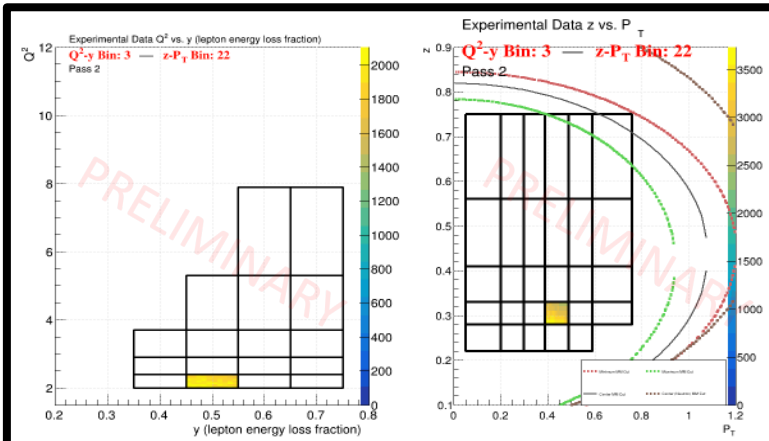
Experimental Setup and Data



CLAS12 Detector

- CLAS12 detector in Hall B at Jefferson Lab
 - Upgrade from the CLAS detector
 - Enabled the higher energy and statistics for our experiments, not previously accessible
- Used a 10.6 GeV polarized electron beam and unpolarized liquid hydrogen target
- Data presented uses forward detector only

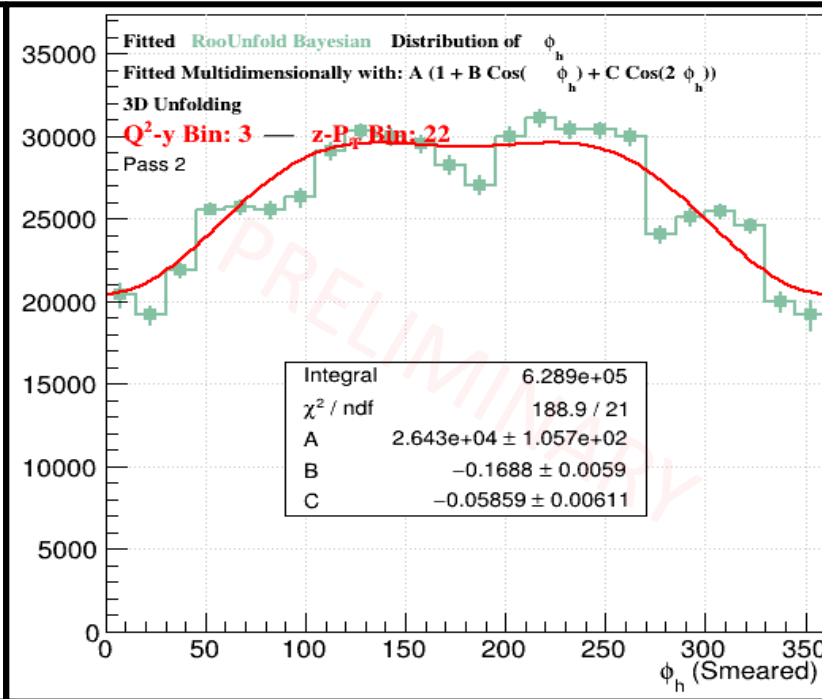
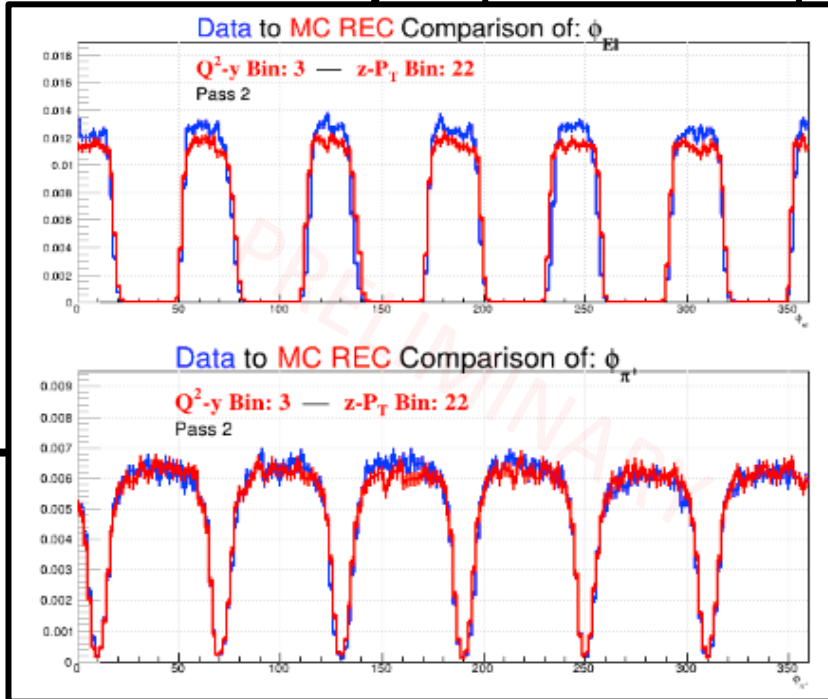
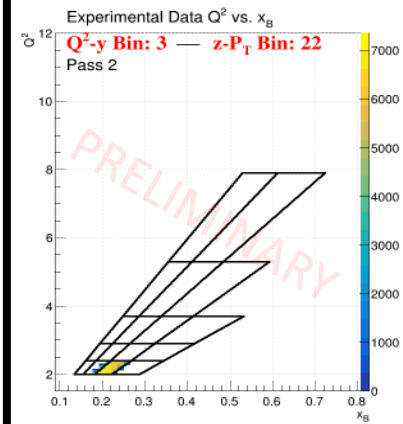
Sector Dependence in ϕ_h Distributions



Issue: Some bins seem to have additional modulations AFTER Acceptance Corrections not explained by the $\cos(\phi)$ and $\cos(2\phi)$ moments

- The 6 peak structure was found to be related to the forward detector sectors
- This suggested that the effect is related to mismatching in sector acceptance between Data and Monte Carlo

Comparison of
Lab ϕ angles of
both particles for
Data and MC



Solution: Revisit the Fiducial Cuts to improve this agreement

Refinement of Fiducial Cuts (on the Electron)

Drift Chamber Fiducial Cuts

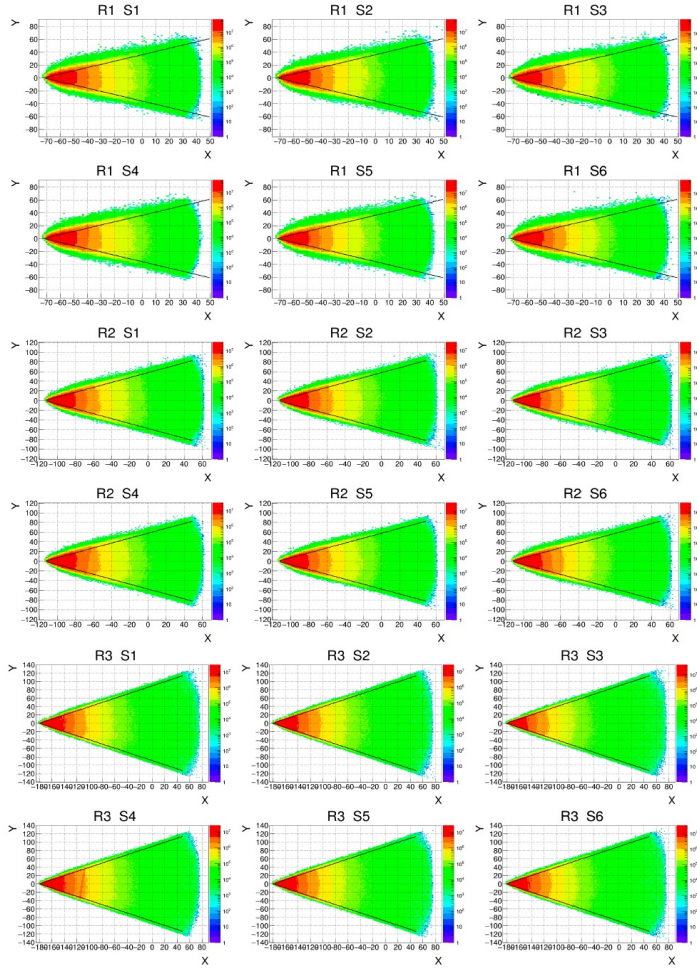
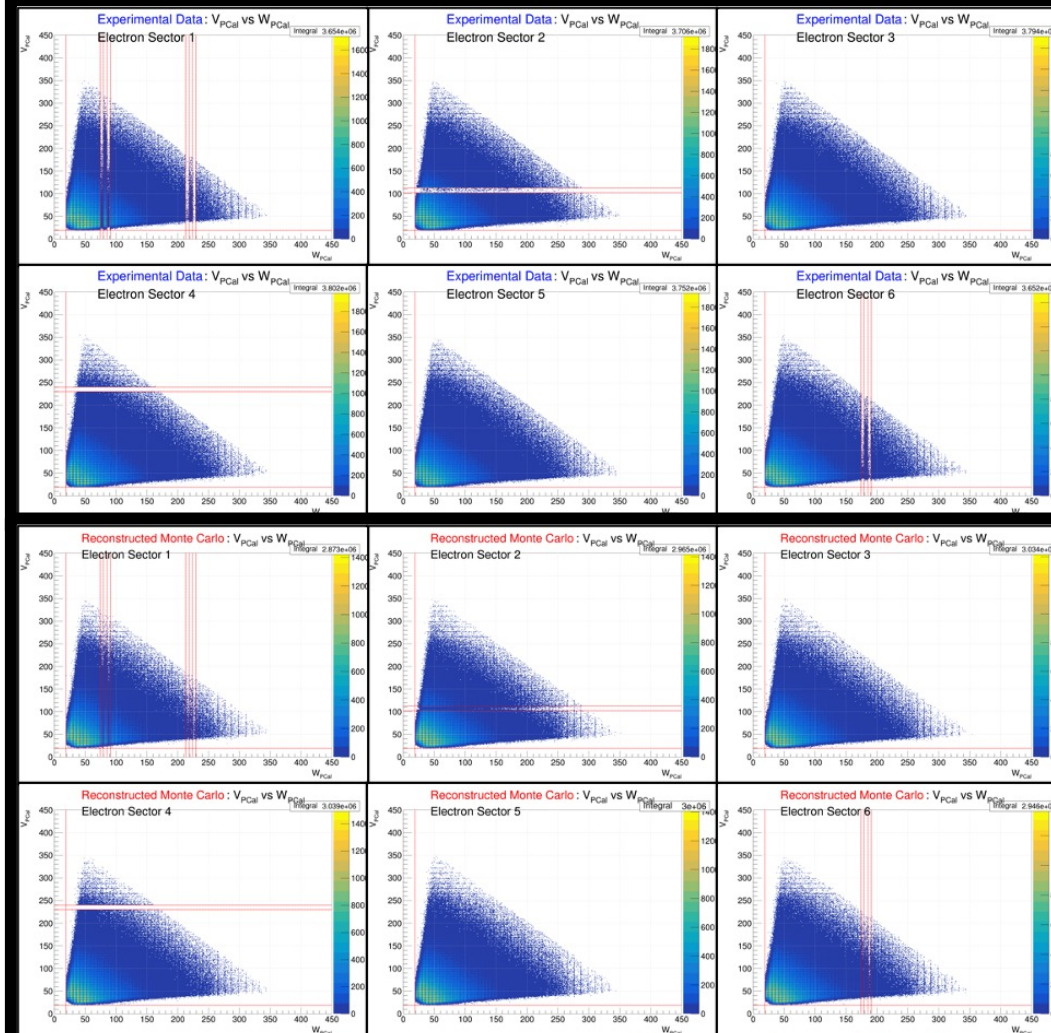


FIG. 10. χ^2 weighted drift chamber occupancy in the x and y detector variables for the three layers (R1, R2, R3) and six sectors. The black lines correspond to the DC fiducial cuts.

P calorimeter Fiducial Cuts on V and W (also cut on $U < 395$ cm)



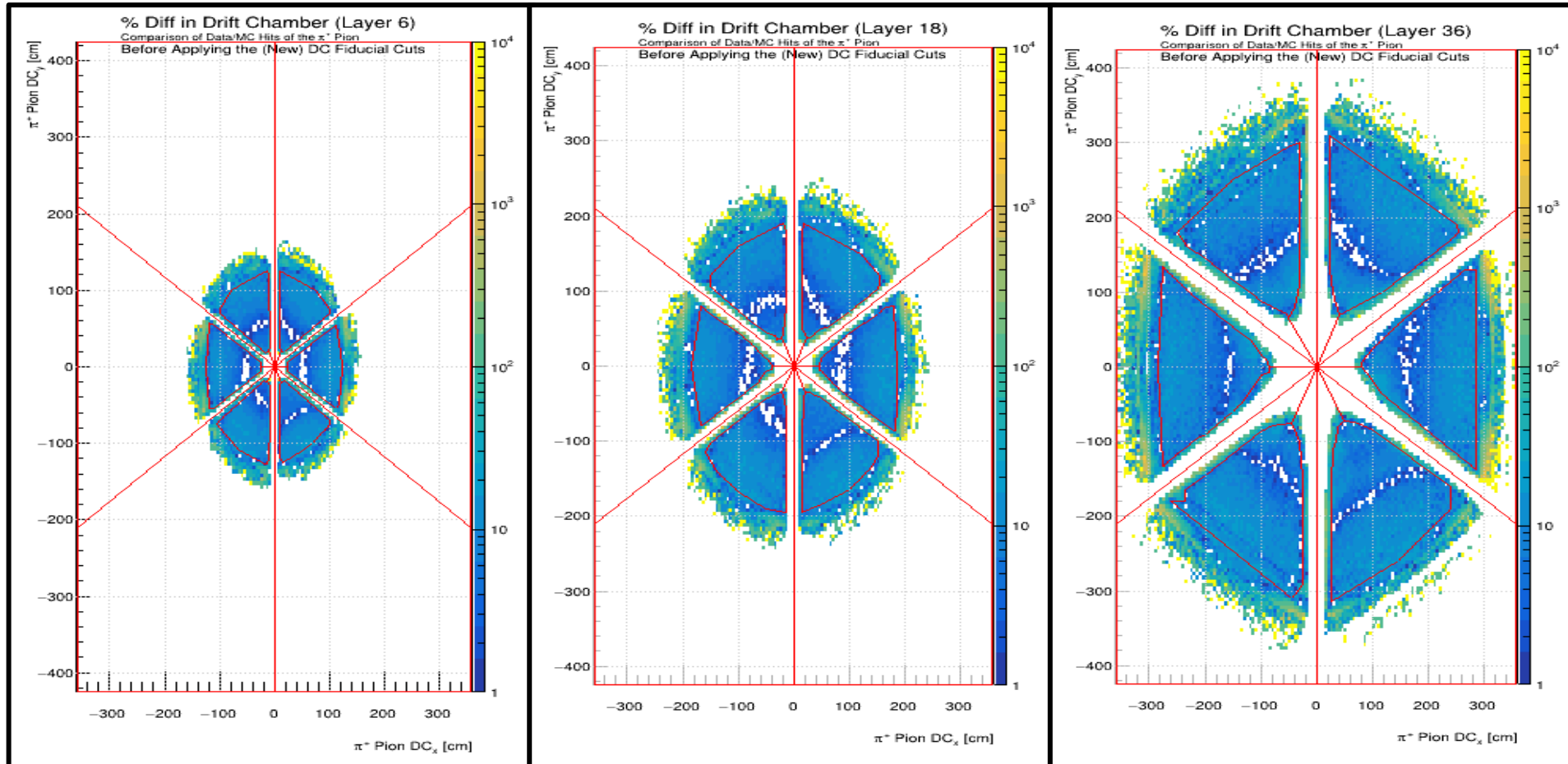
Experimental Data
(Before the Cuts)

Red lines show cuts to remove the dead channels in data from the simulation

Reconstructed Monte Carlo
(Before the Cuts)

Refinement of Fiducial Cuts (on the π^+ pion)

These images show the % Difference between the normalized event counts of where the π^+ pion hits each layer of the Drift Chamber in the Data and Monte Carlo datasets



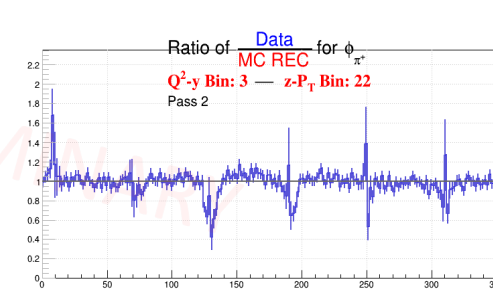
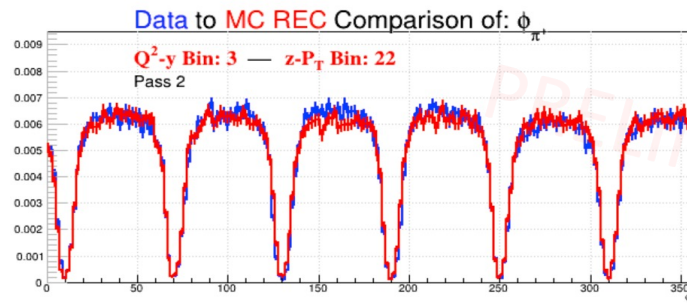
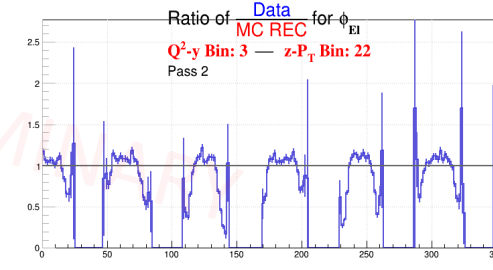
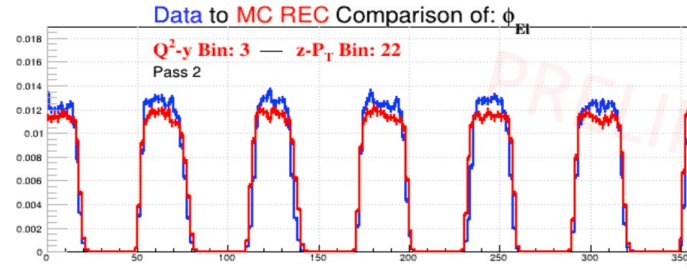
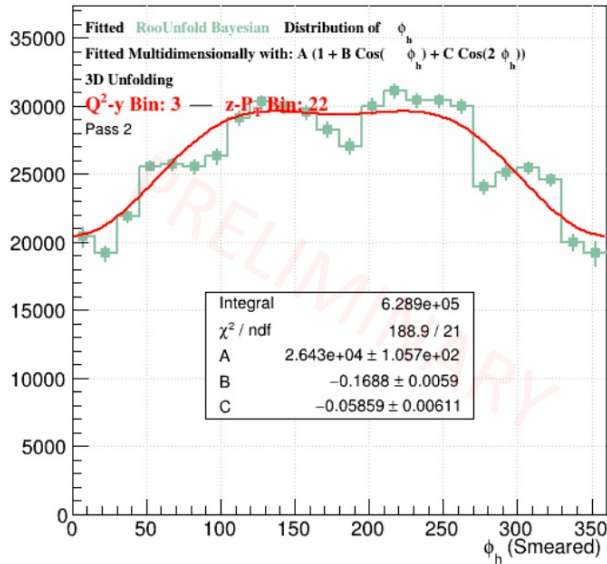
The Red lines show where the cuts are defined for each DC layer

Impact of New Fiducial Cuts

Before
New
Cuts

Top Rows:
Lab Angle of Electrons

Bottom Rows:
Lab Angle of π^+ Pions

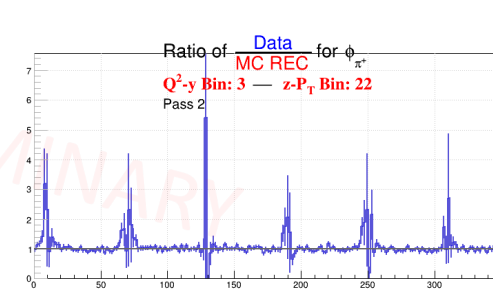
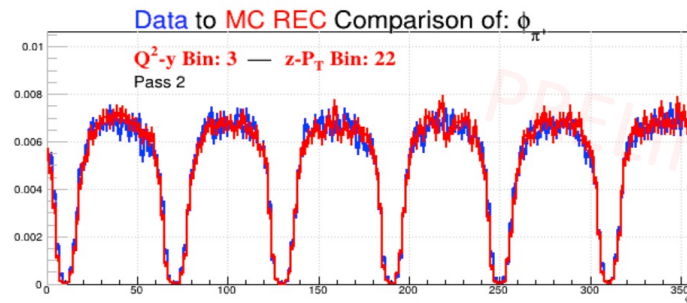
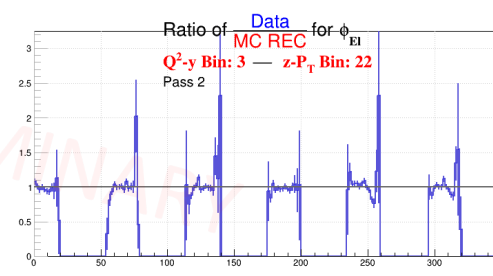
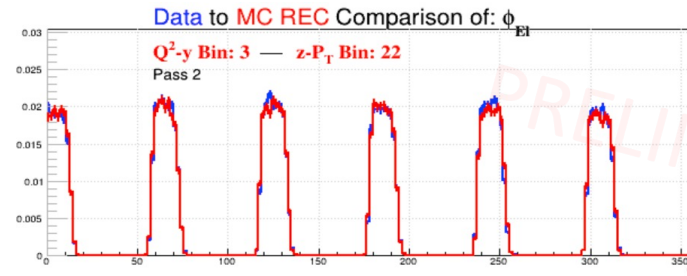
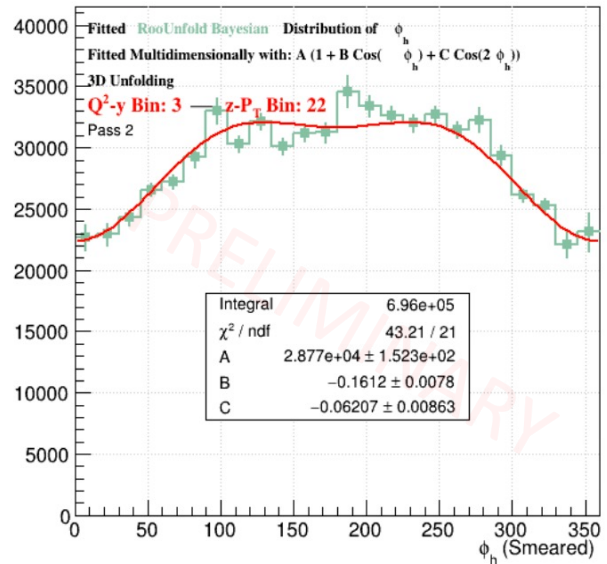


After
New
Cuts

← Much better agreement between the lab angles of both particles

← Much Better χ^2

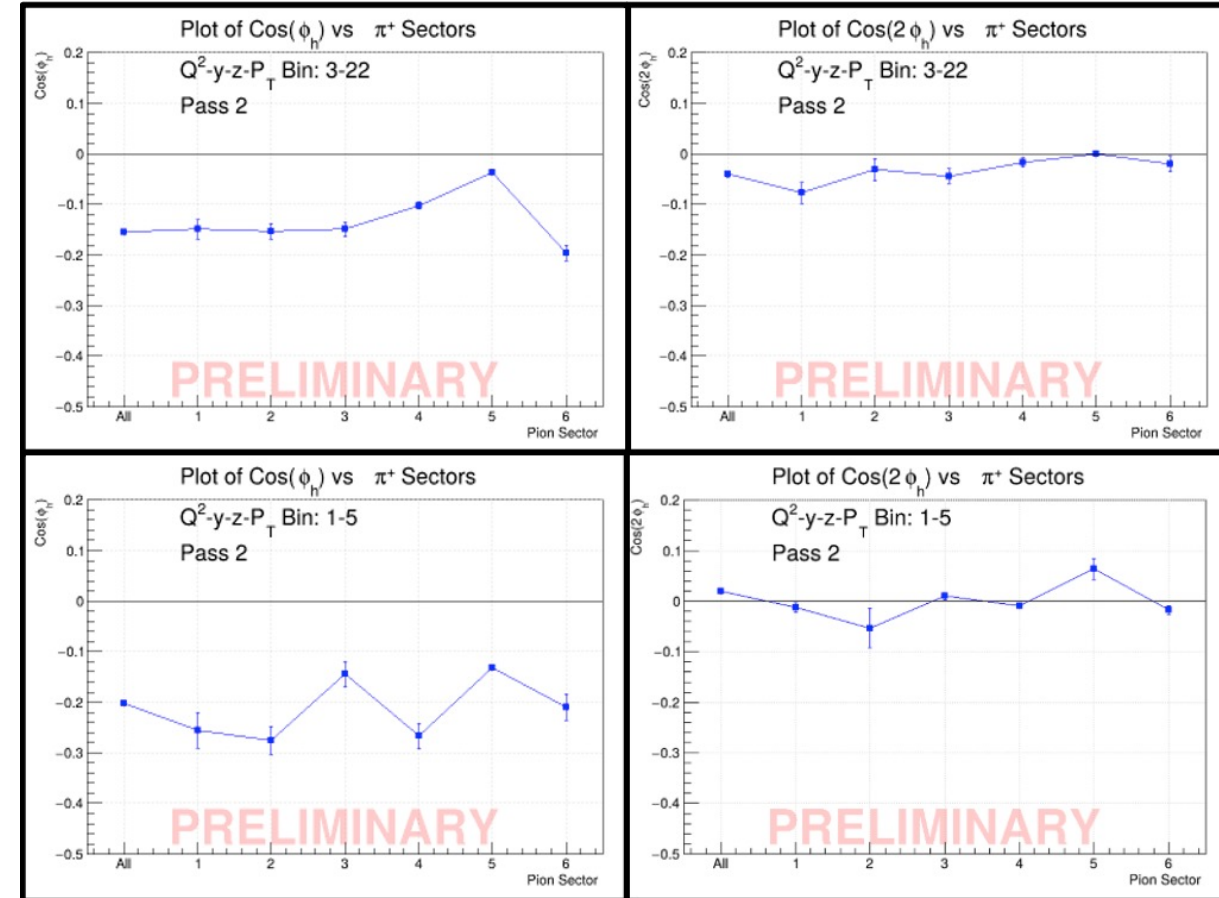
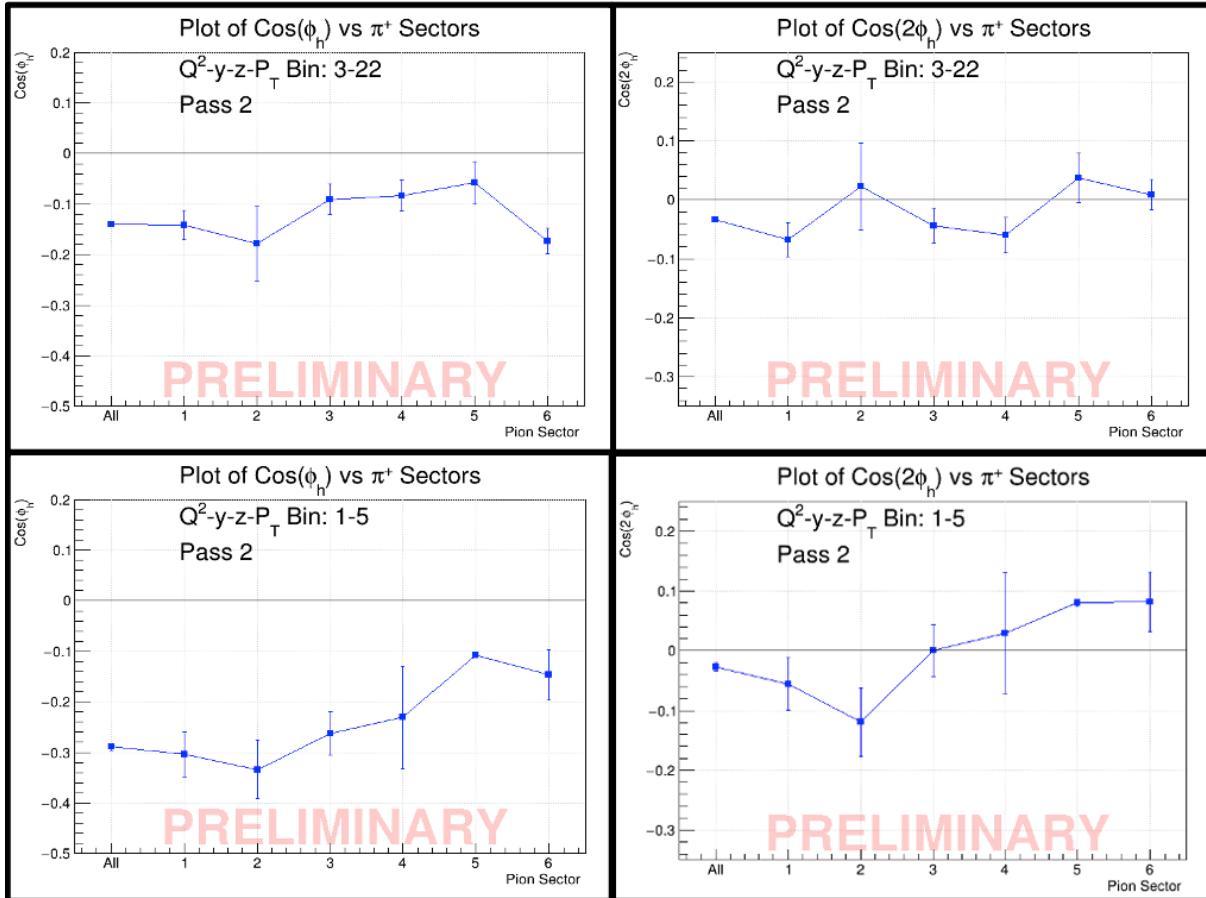
The cuts start to reduce the additional modulations for a smoother distribution of ϕ_h



(Pion) Sector Correlations with $\cos(\phi)$ and $\cos(2\phi)$ Measurements

Before Newest Fiducial Cuts

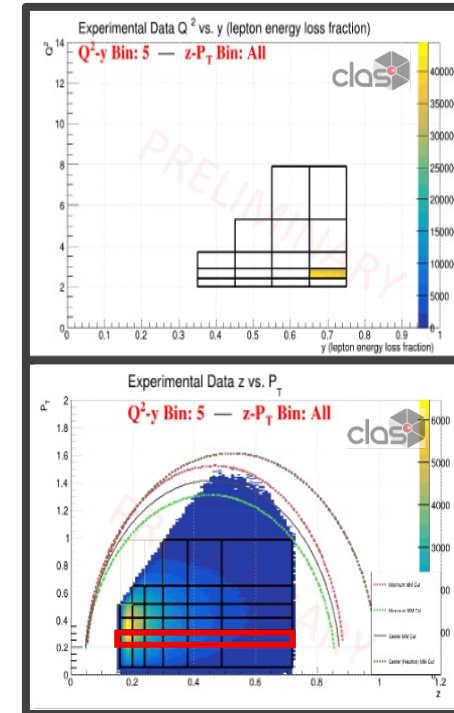
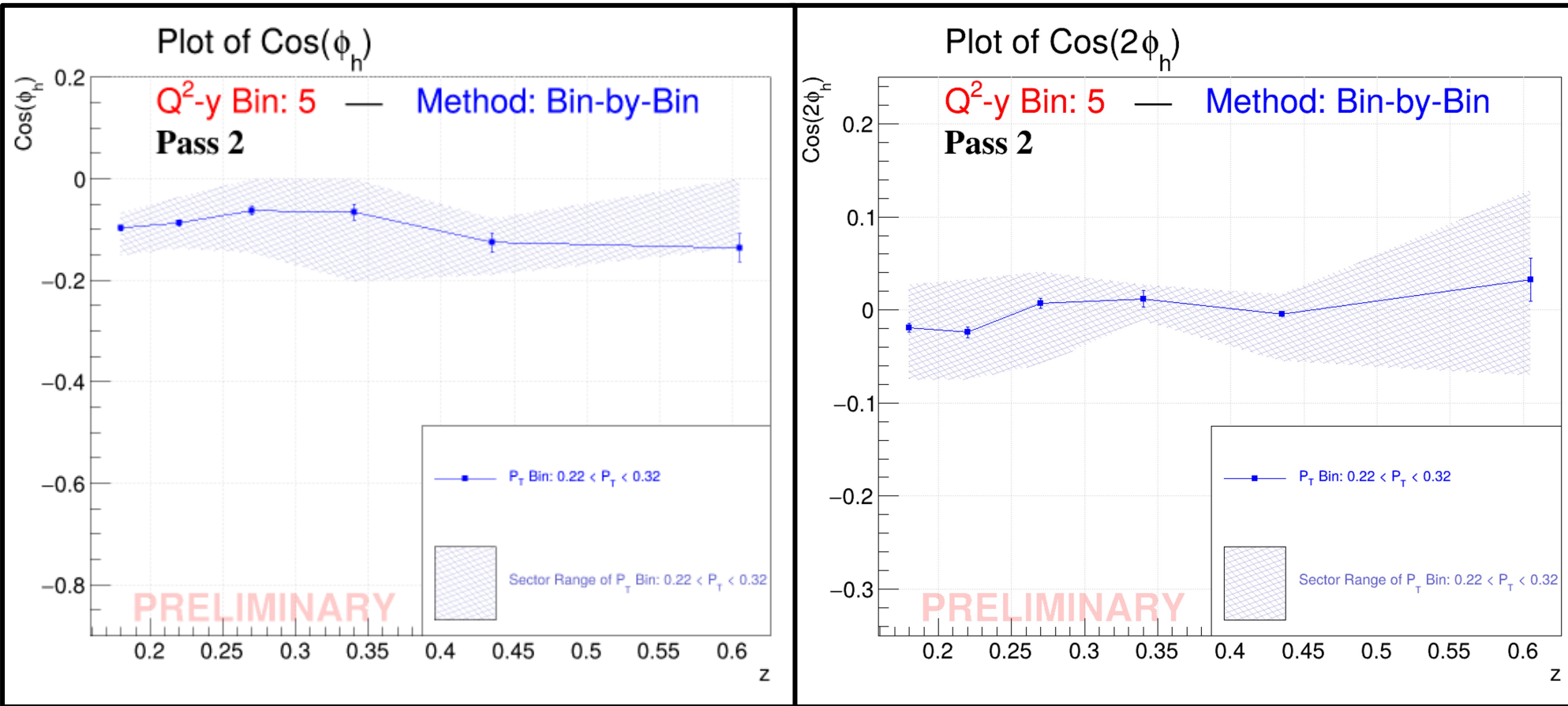
After Newest Fiducial Cuts



The new Fiducial Cuts reduce Sector dependence across many of my kinematic bins, though some dependence still remains

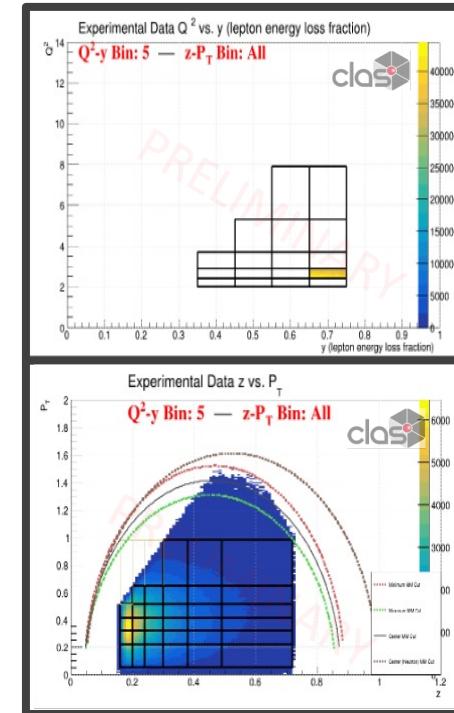
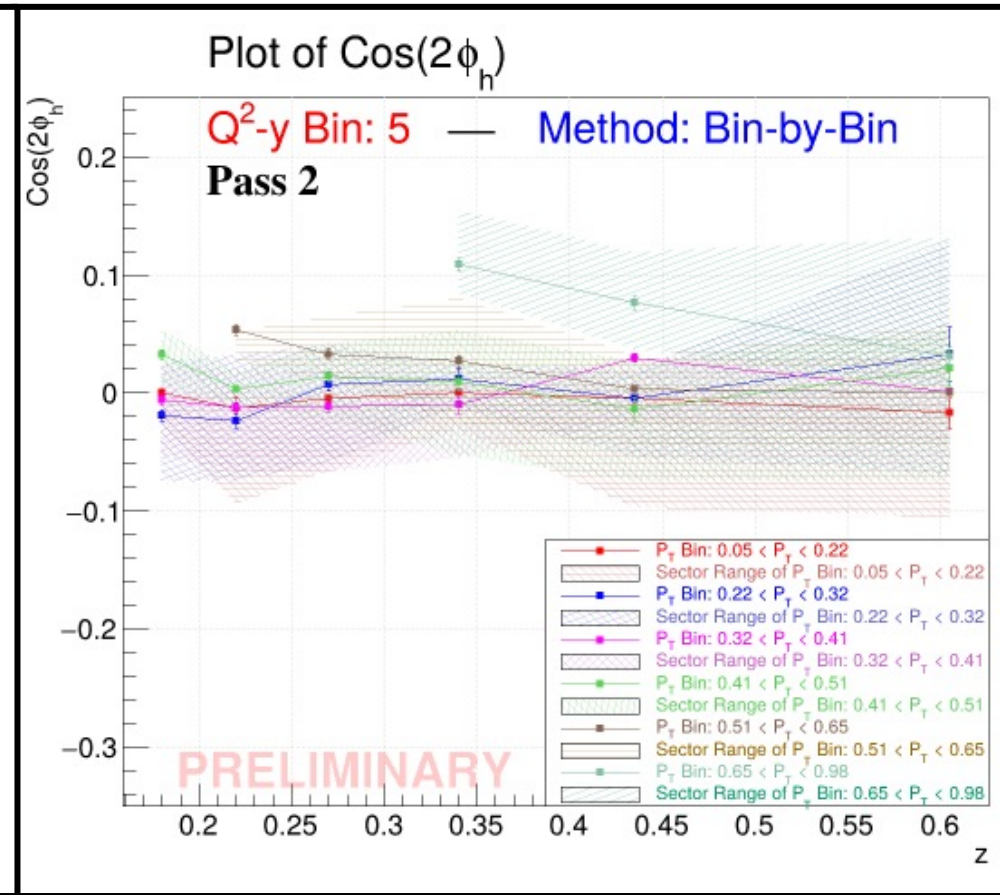
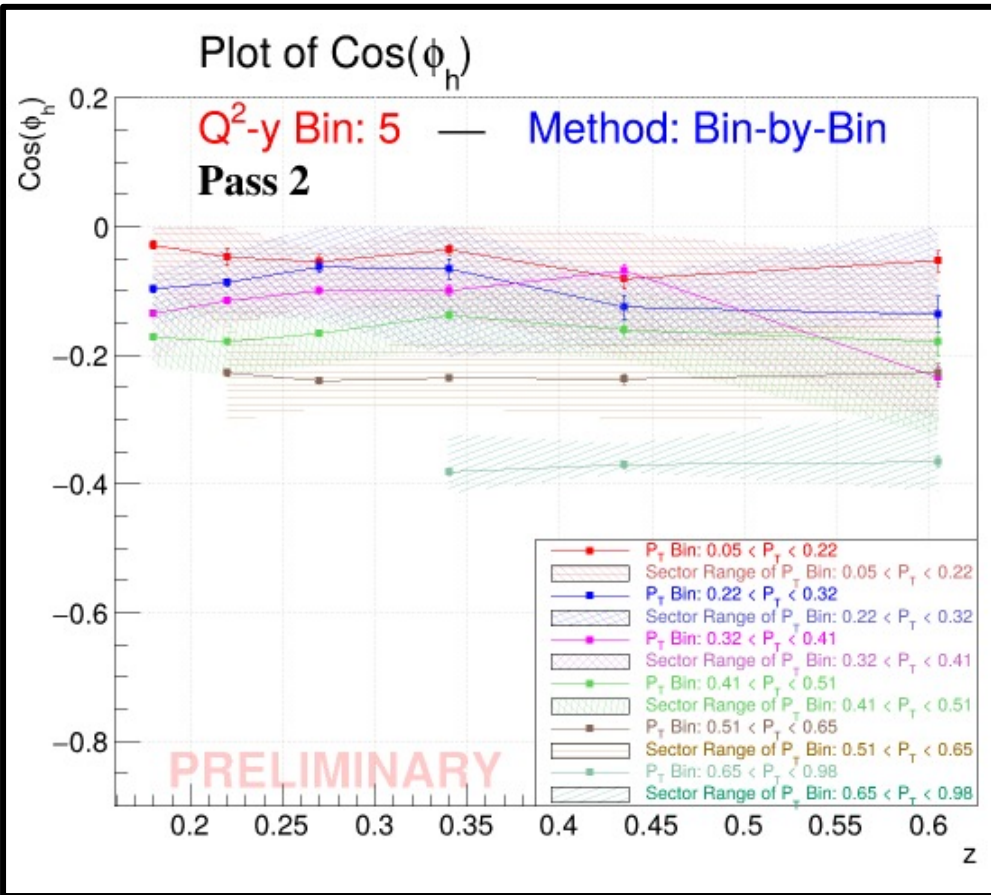
Will plan to account for these dependencies when taking the final measurements

(Pion) Sector Correlations with $\text{Cos}(\phi)$ and $\text{Cos}(2\phi)$ Measurements



The shaded regions show the ranges of sector dependence on these measurements

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