



U.S. DEPARTMENT OF
ENERGY

Office of
Science

Jefferson Lab
Thomas Jefferson National Accelerator Facility

Measuring CLAS12 $D(e, e' \pi)$ Cross Sections for e4v Update

Caleb Fogler for the CLAS Collaboration



OLD DOMINION
UNIVERSITY

I D E A FUSION



Neutrino Experiments and Validating GENIE

Neutrino experiments are difficult

- Large beam energy spread
- Small cross sections

PRD 91, 072010 (2015)

$$N_{\alpha}(E_{rec}, L) = \int \Phi_{\alpha}(E, L) \sigma(E) f_{\sigma}(E, E_{rec}) dE$$

Measured

Flux

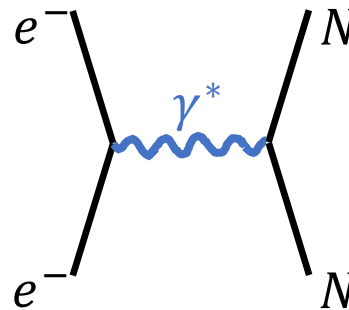
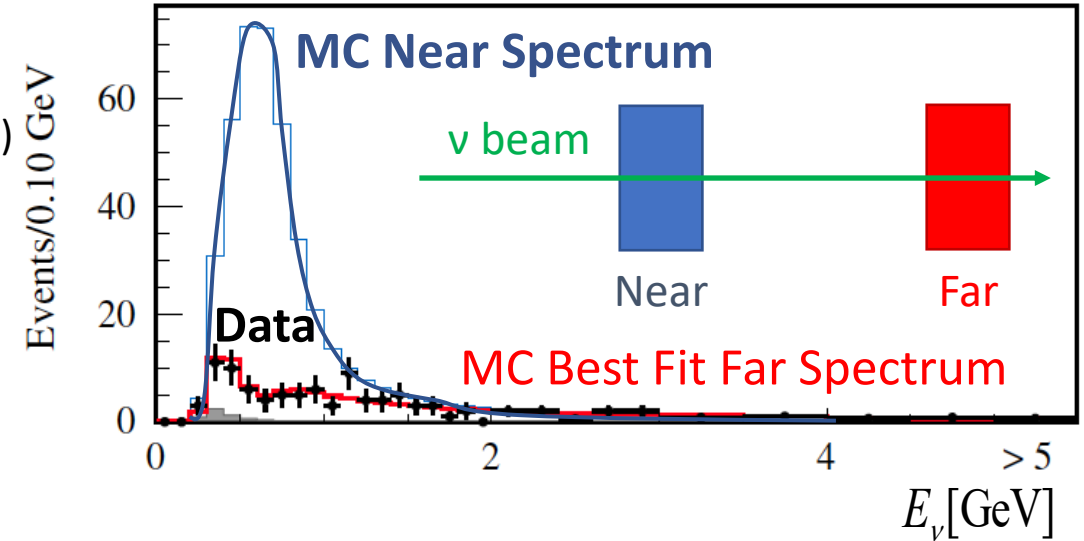
Simulated

Need GENIE to extract the neutrino flux from data

Use electrons to validate GENIE models:

- Monoenergetic
- Larger cross sections
- Similar interactions

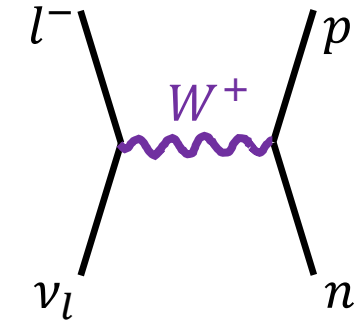
If GENIE can describe neutrinos, it can describe electrons



EM Current:

$$j_{em}^{\mu} = \bar{u} \gamma^{\mu} u$$

Vector



Charge-Coupling Weak Current:

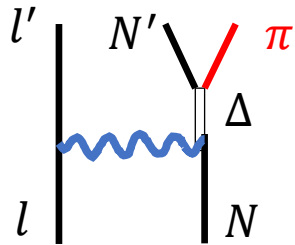
$$j_{\pm}^{\mu} = \bar{u} \frac{-ig_W}{2\sqrt{2}} (\gamma^{\mu} - \gamma^{\mu} \gamma^5) u$$

Vector Axial

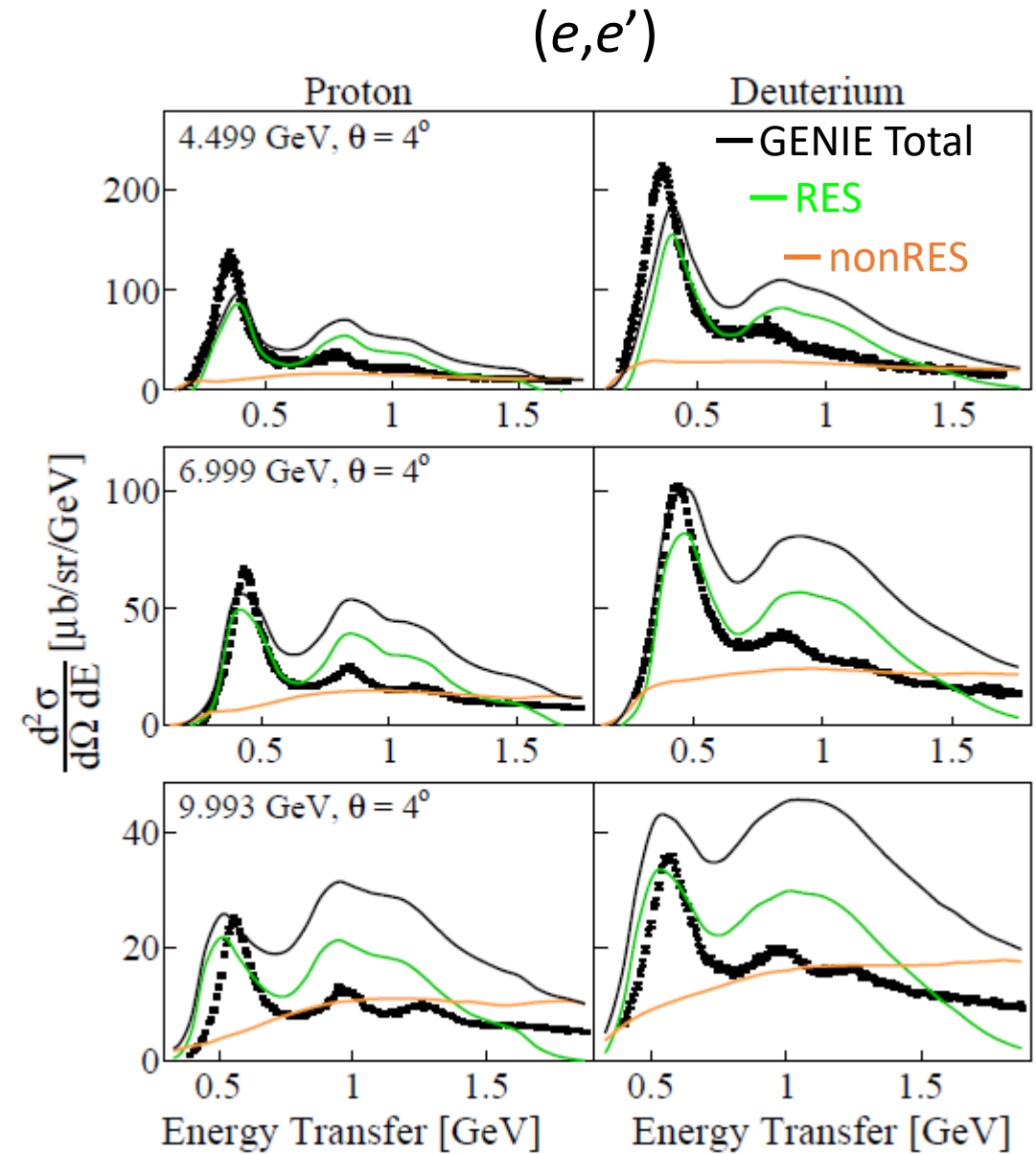
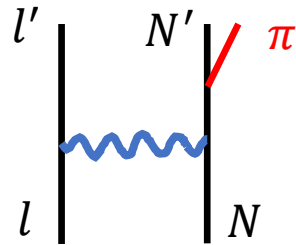
Motivation

- GENIE badly describes inclusive $p(e,e')$ and $d(e,e')$ scattering in pion production region
 - GENIE parameters are being tuned to better describe the data
- I measured 4.2 GeV RG-B $d(e,e'\pi)$ Forward Detector cross sections to test and improve GENIE

Resonance Decay



Non-Resonant



PRD 103, 113003 (2021)

GENIE and onepigen Pion Production Models

Onepigen

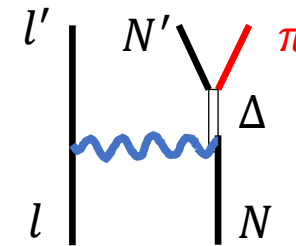
Nucl.Phys. A645 (1999) 145-174

arXiv:nucl-th/9807001v2

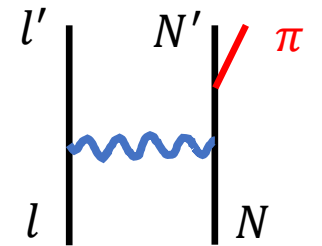
- Single pion event generator
- MAID2007 unitary isobar model

Eur. Phys. J. A**34**, (2007) 69-97

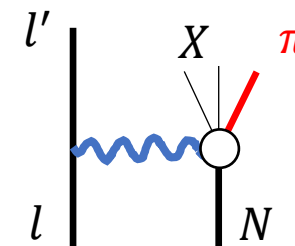
Resonant Production



Non-Resonant Production



DIS Production



GENIE

- Phenomenological semi-classical event generator

- Quasi-elastic scattering

PRD 103 (2021) 113003

- Baryon resonance production (Berger-Sehgal)

PRD 76 (2007) 113004

- DIS and non resonant production (Bodek-Yang)

J. Phys. G: Nucl. Part. Phys. 29 (2003) 1899–1905

Cuts, Corrections, and Uncertainties

Electron Cuts:

Electron PID
DC fiducial cuts
ECAL fiducial cuts
Vertex cuts

Pion Cuts:

Pion PID
DC fiducial cuts
Vertex cuts

Applied corrections and uncertainties

- Radiative corrections (GENIE) **THANKS JULIA!!!**
Replaces limited radiative corrections from onepigen
- Acceptance corrections (GENIE)
- Cut variance uncertainties
- Systematic uncertainties
- 10% normalization uncertainty (not shown)

GENIE Acceptance and Radiative Corrections

Acceptance corrections

- Calculate correction bin-by-bin by dividing generated with detected

$$AC = G_{Born}^{GEN} / G_{Born}^{det\pi}$$

- Uncertainty 10% of pion acceptance correction

$$\delta AC = 0.1 * (G_{Born}^{det_e} / G_{Rad}^{det\pi} - 1)$$

Radiative corrections [\(See March CLAS talk\)](#)

- Calculate correction bin-by-bin by dividing nonradiative with radiative

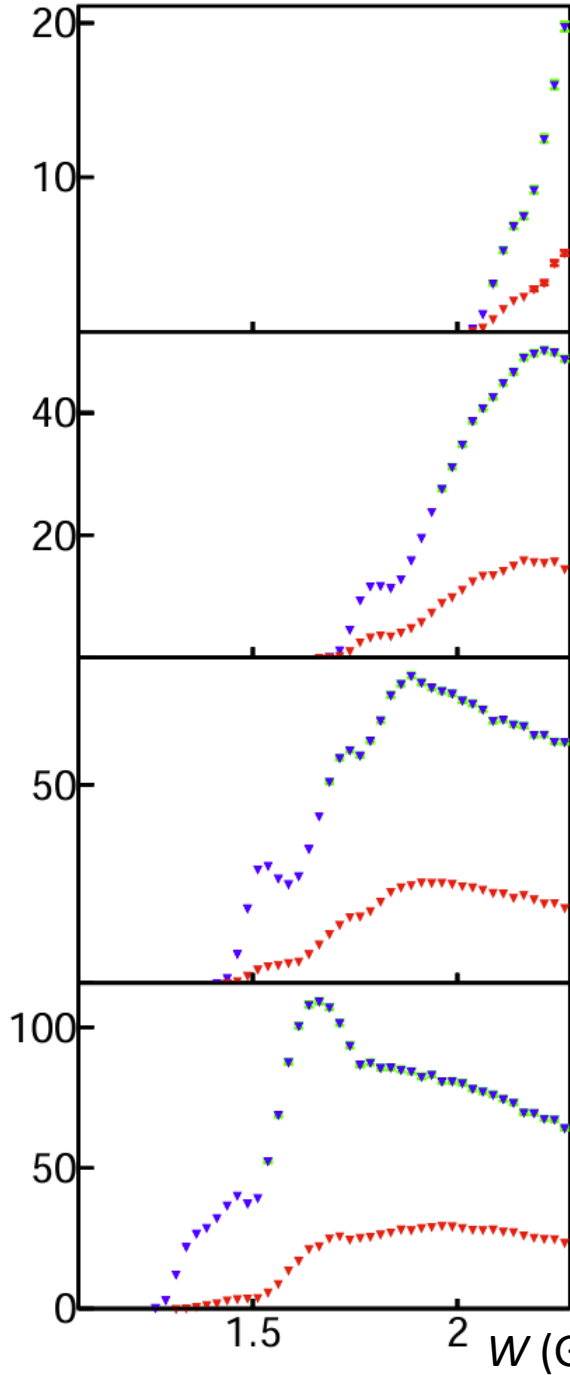
$$RC = G_{Born}^{det} / G_{Rad}^{det}$$

- Uncertainty 10% of correction

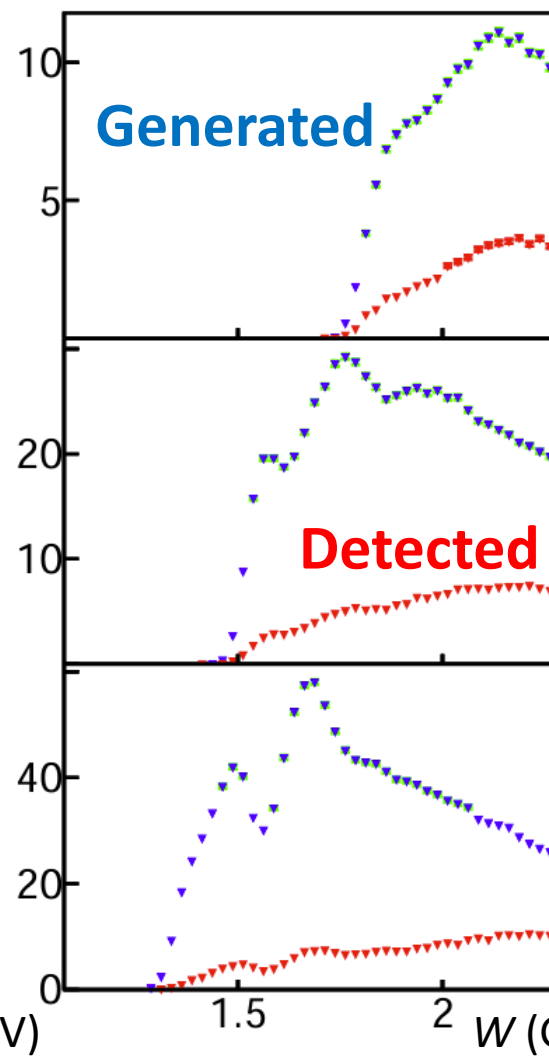
$$\delta RC = 0.1 * (RC - 1)$$

Higher P_π

GENIE Nonradiative Cross Sections



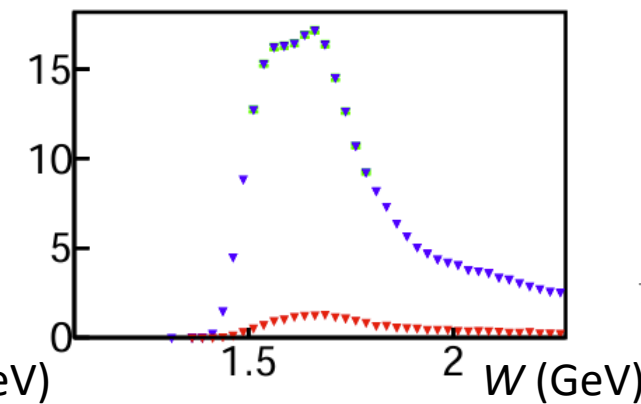
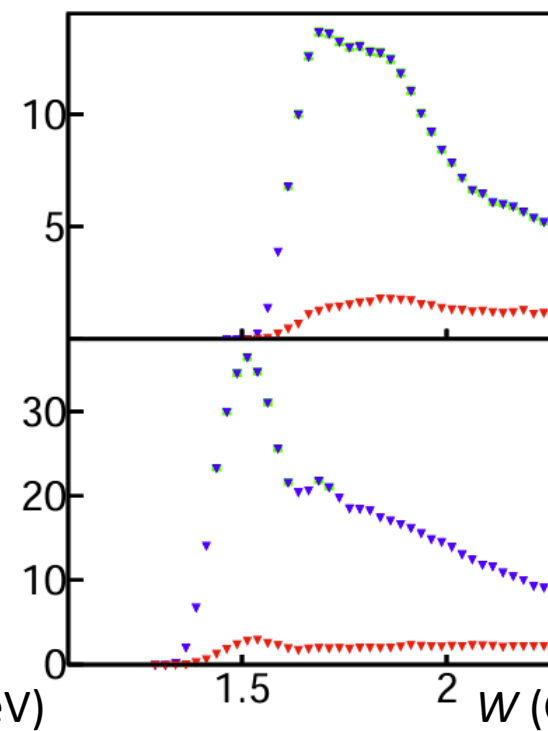
$$d(e, e' \pi^+)$$
$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$



Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

Higher $\theta_{\pi q}$

Higher P_π

Generated/Detected

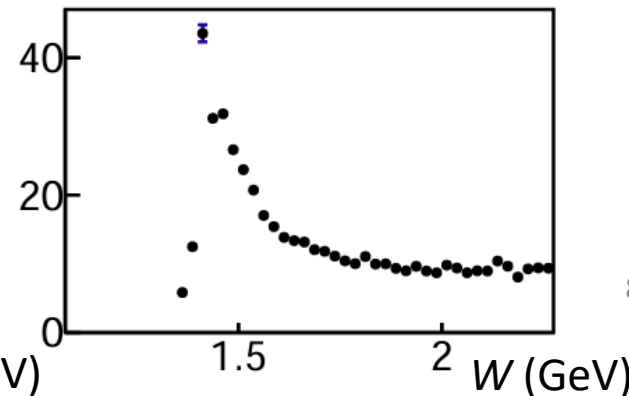
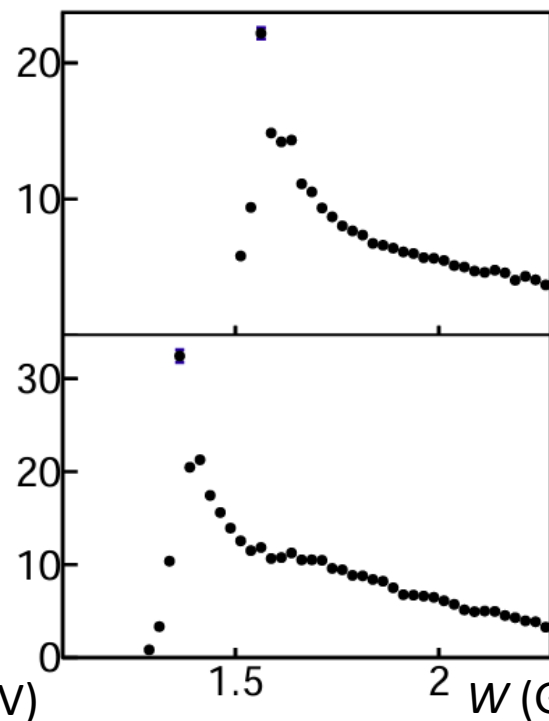
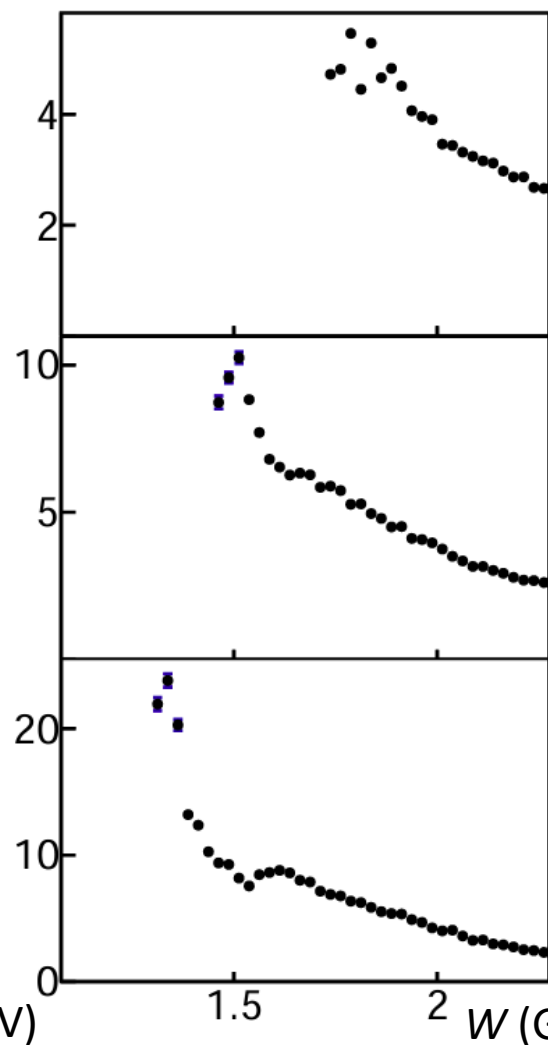
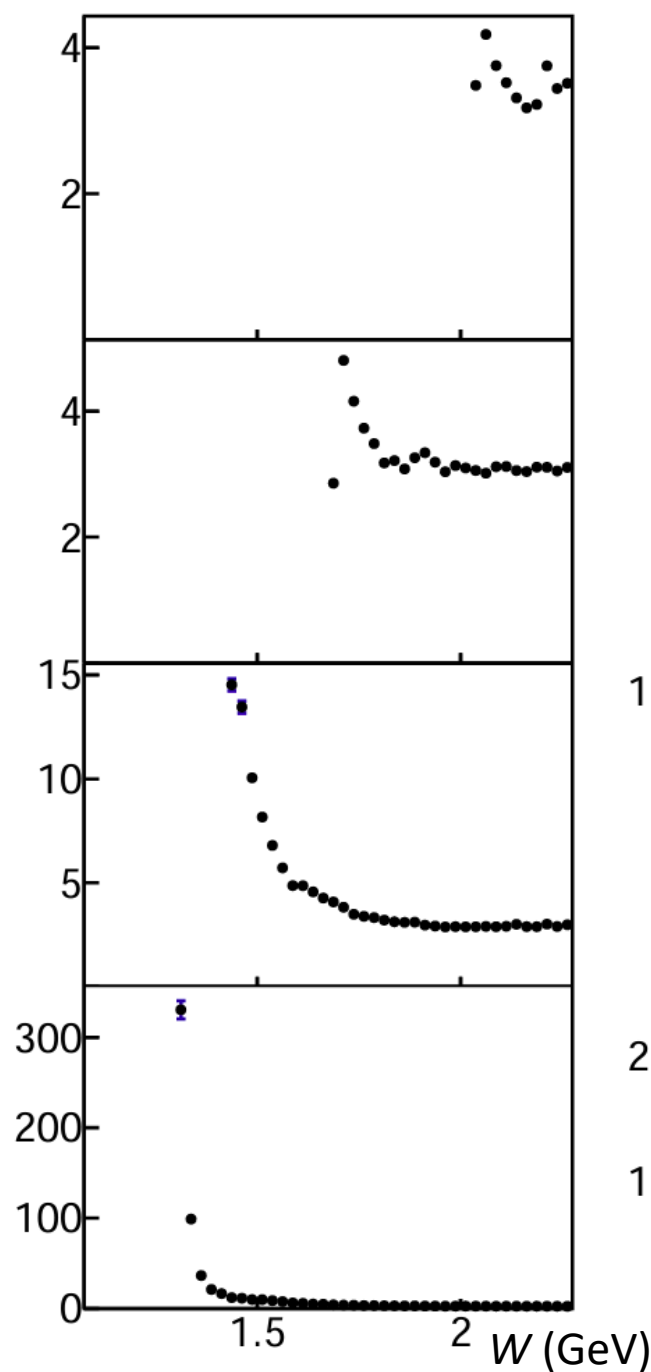
$$d(e, e' \pi^+)$$
$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

Removed bins
with $AC > 50$

Higher $\theta_{\pi q}$

Higher P_π



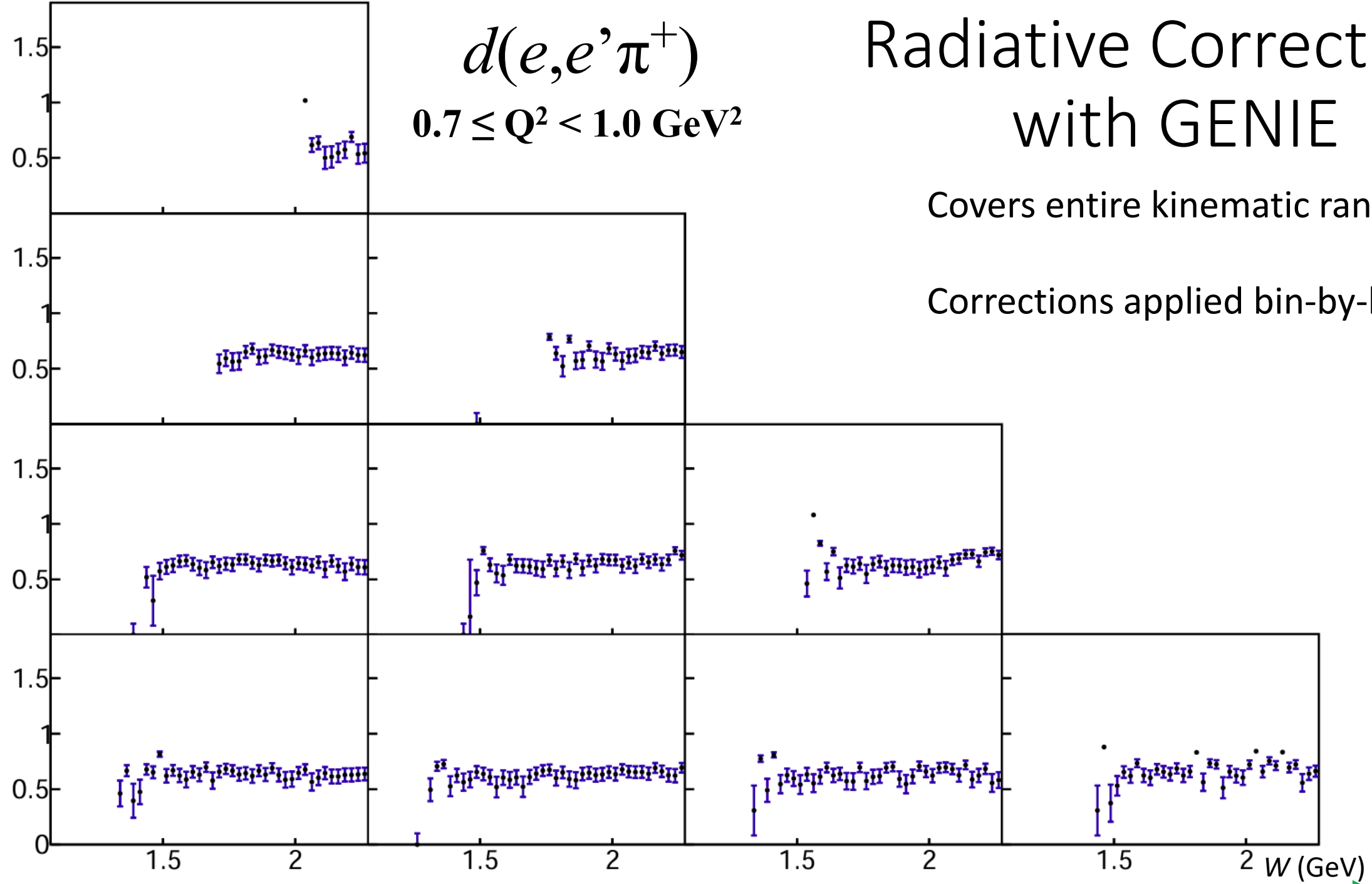
$$d(e, e' \pi^+) \\ 0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

Corrections applied bin-by-bin

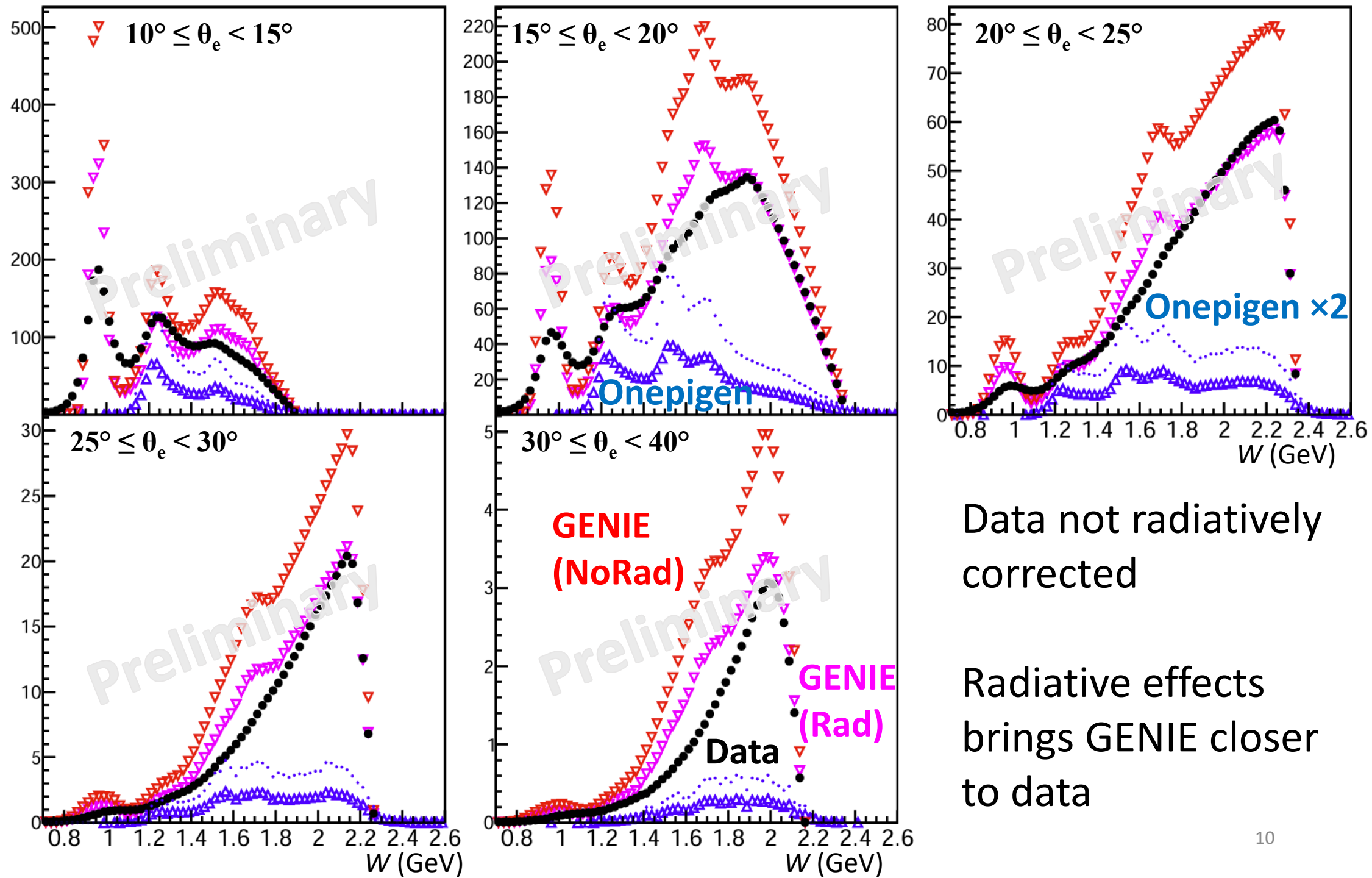
Rad/NoRad



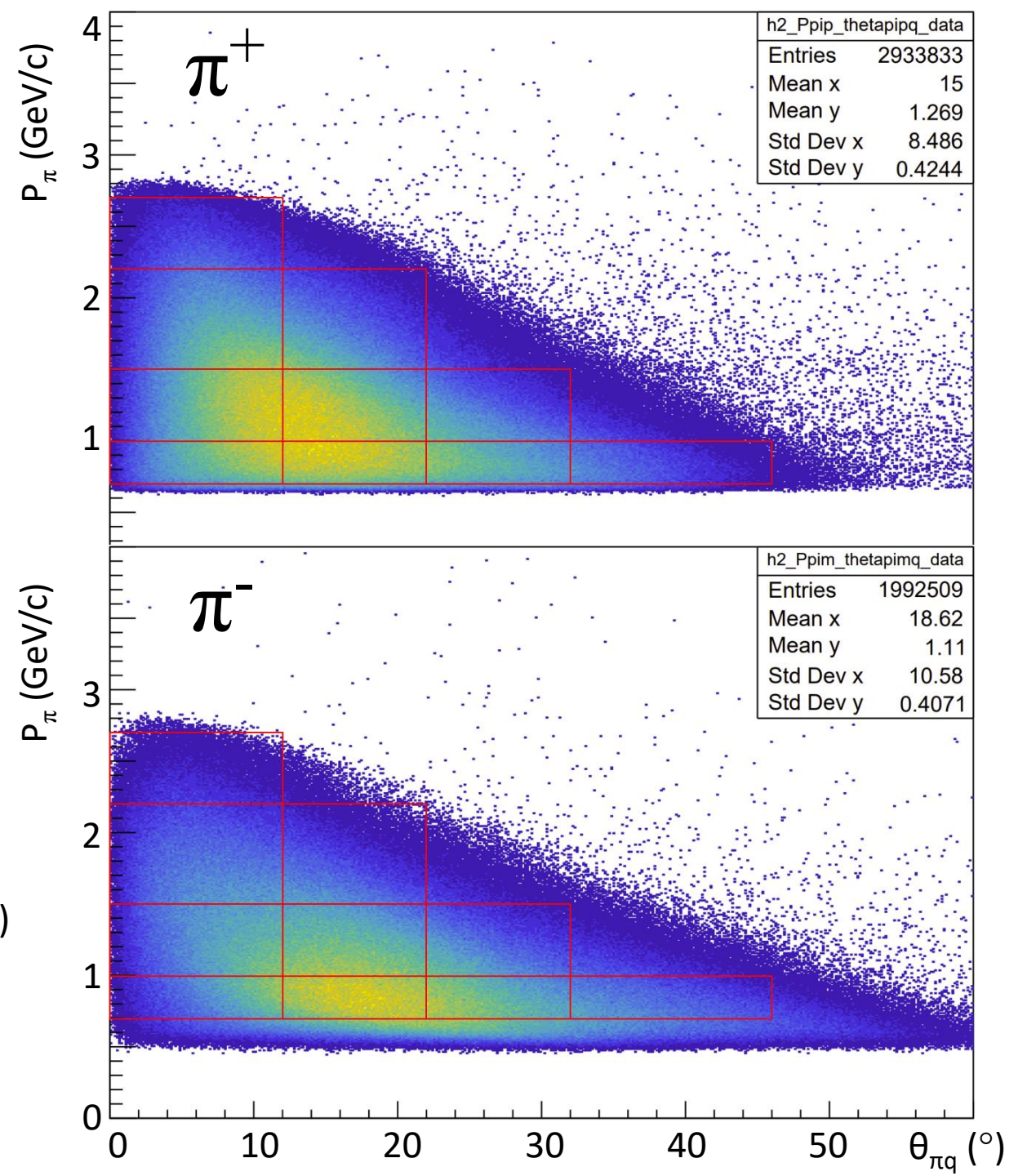
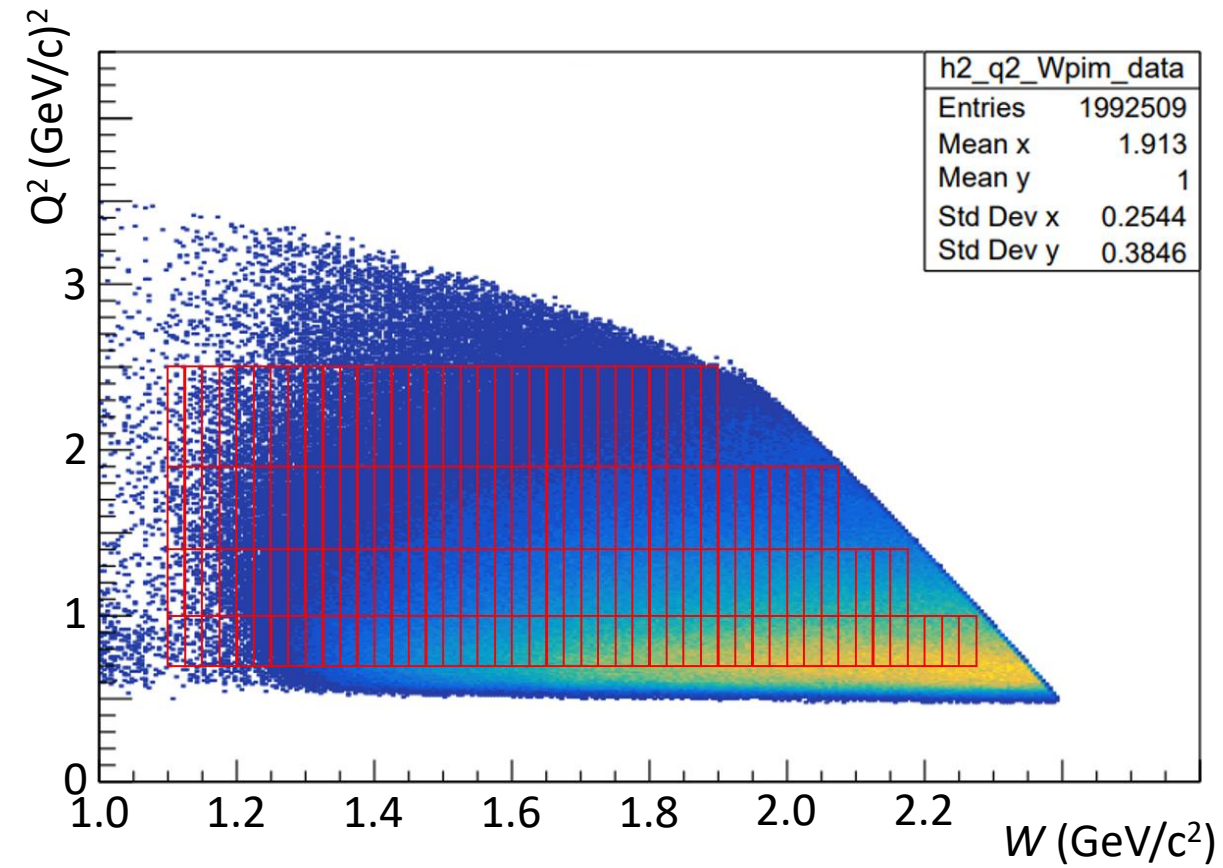
Higher $\theta_{\pi q}$

$d(e,e')$

Uncorrected Inclusive Cross Sections



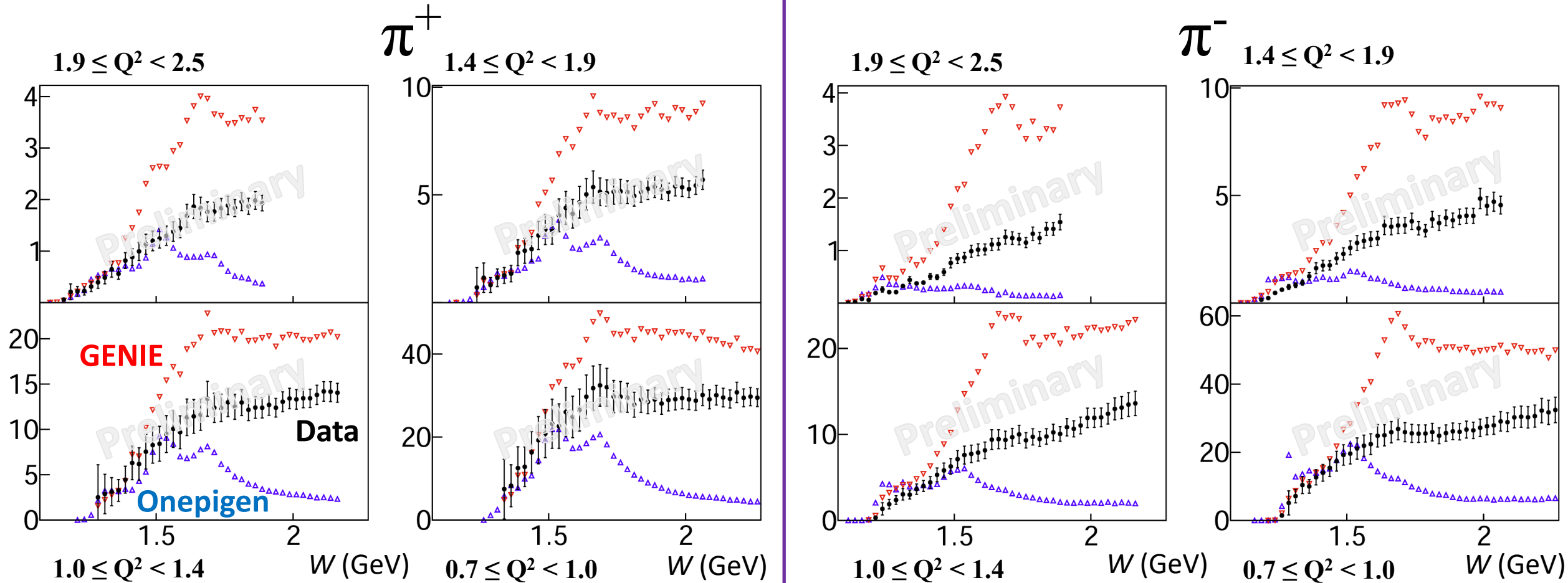
Binning (Q^2 , W , $\theta_{\pi q}$, P_π)



Cross Sections

- Includes radiative corrections, acceptance corrections, statistical uncertainties, and systematic uncertainties
- Binning
 - Q^2
 - Q^2 and $\theta_{\pi q}$
 - Q^2 and P_π
 - Q^2 , $\theta_{\pi q}$, and P_π

D(e,e'π) Cross Sections vs W binned in Q²

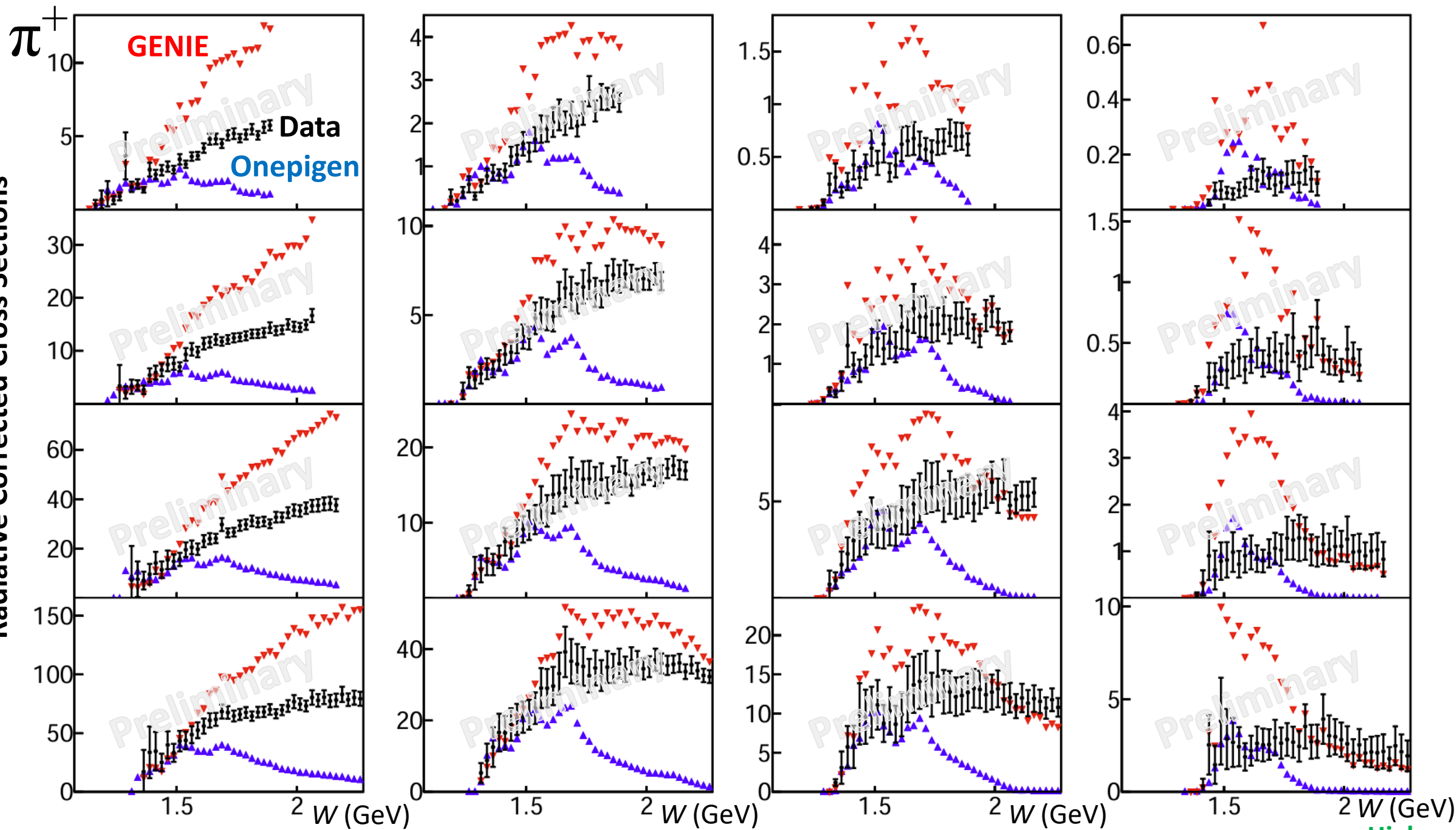


Cross Sections

- Includes radiative corrections, acceptance corrections, statistical uncertainties, and systematic uncertainties
- Binning
 - Q^2
 - **Q^2 and $\theta_{\pi q}$**
 - **Four Q^2 bins: $0.7 - 2.5 \text{ GeV}^2$**
 - **Four $\theta_{\pi q}$ bins: $0^\circ - 46^\circ$**
 - Q^2 and P_π
 - Q^2 , $\theta_{\pi q}$, and P_π

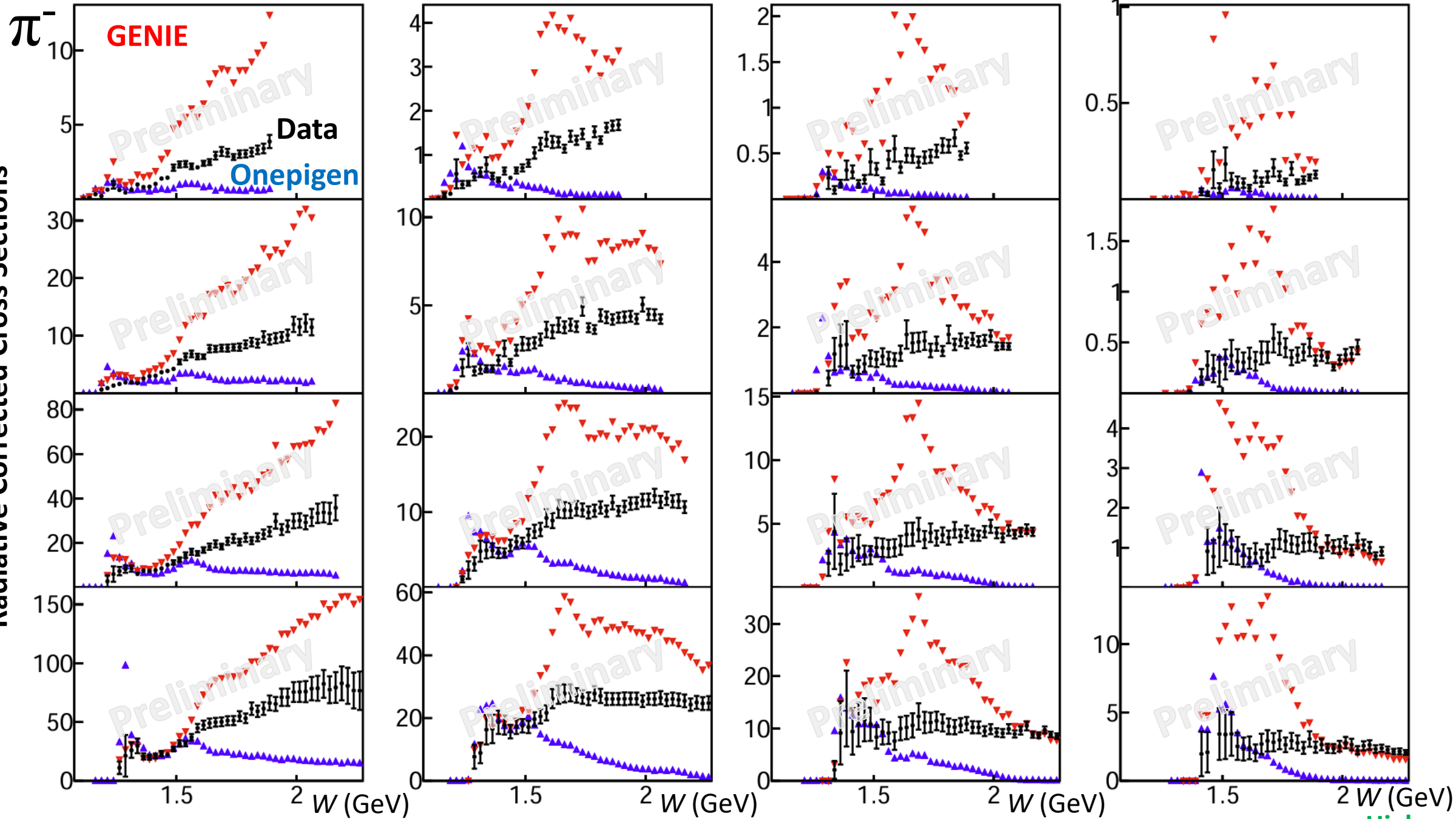
Higher Q^2

Radiative Corrected Cross Sections



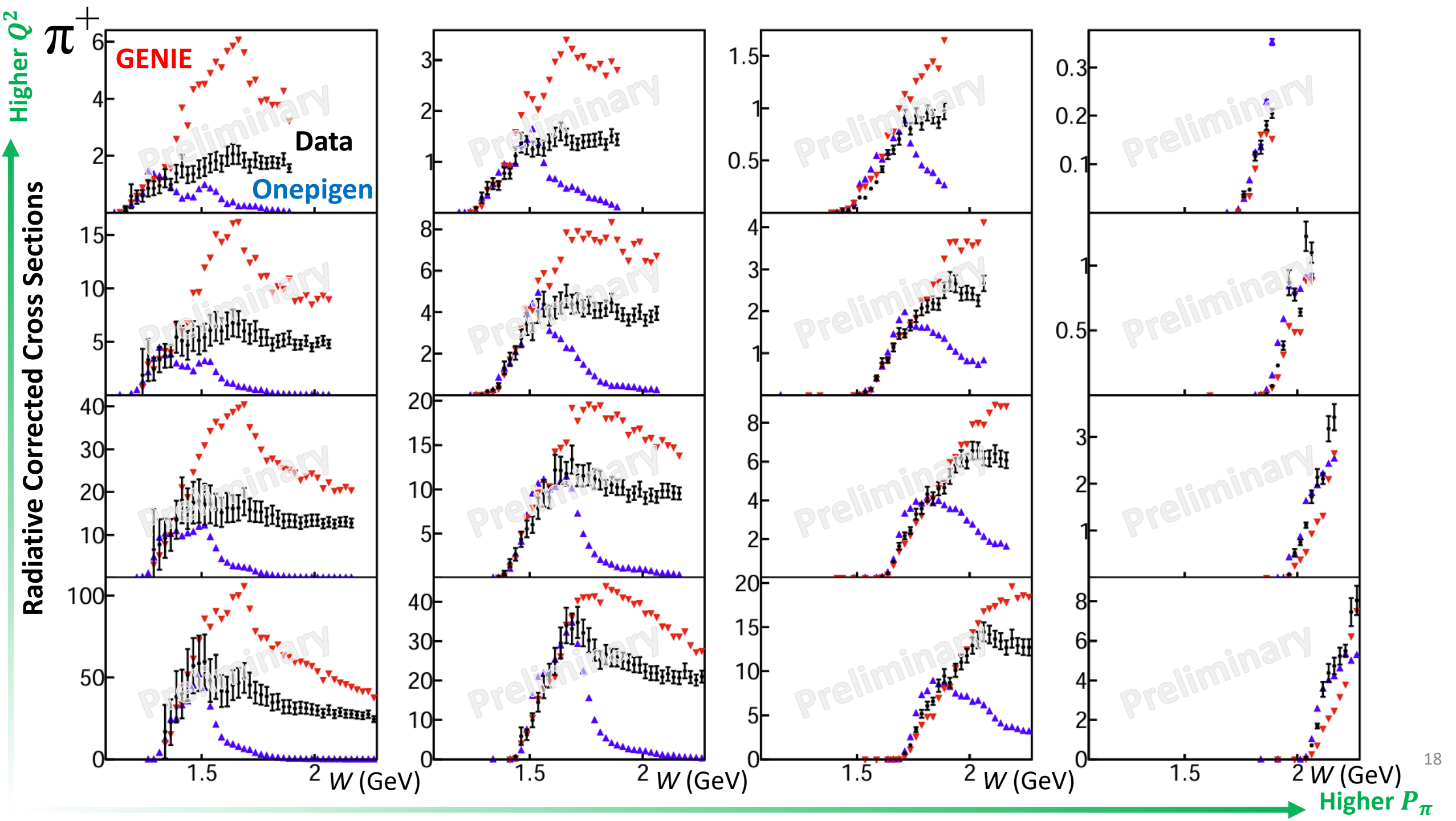
Higher Q^2

Radiative Corrected Cross Sections



Cross Sections

- Includes radiative corrections, acceptance corrections, statistical uncertainties, and systematic uncertainties
- Binning
 - Q^2
 - Q^2 and $\theta_{\pi q}$
 - **Q^2 and P_π**
 - **Four Q^2 bins: 0.7 – 2.5 GeV²**
 - **Four P_π bins: 0.7 – 2.7 GeV/c**
 - Q^2 , $\theta_{\pi q}$, and P_π



Higher Q^2

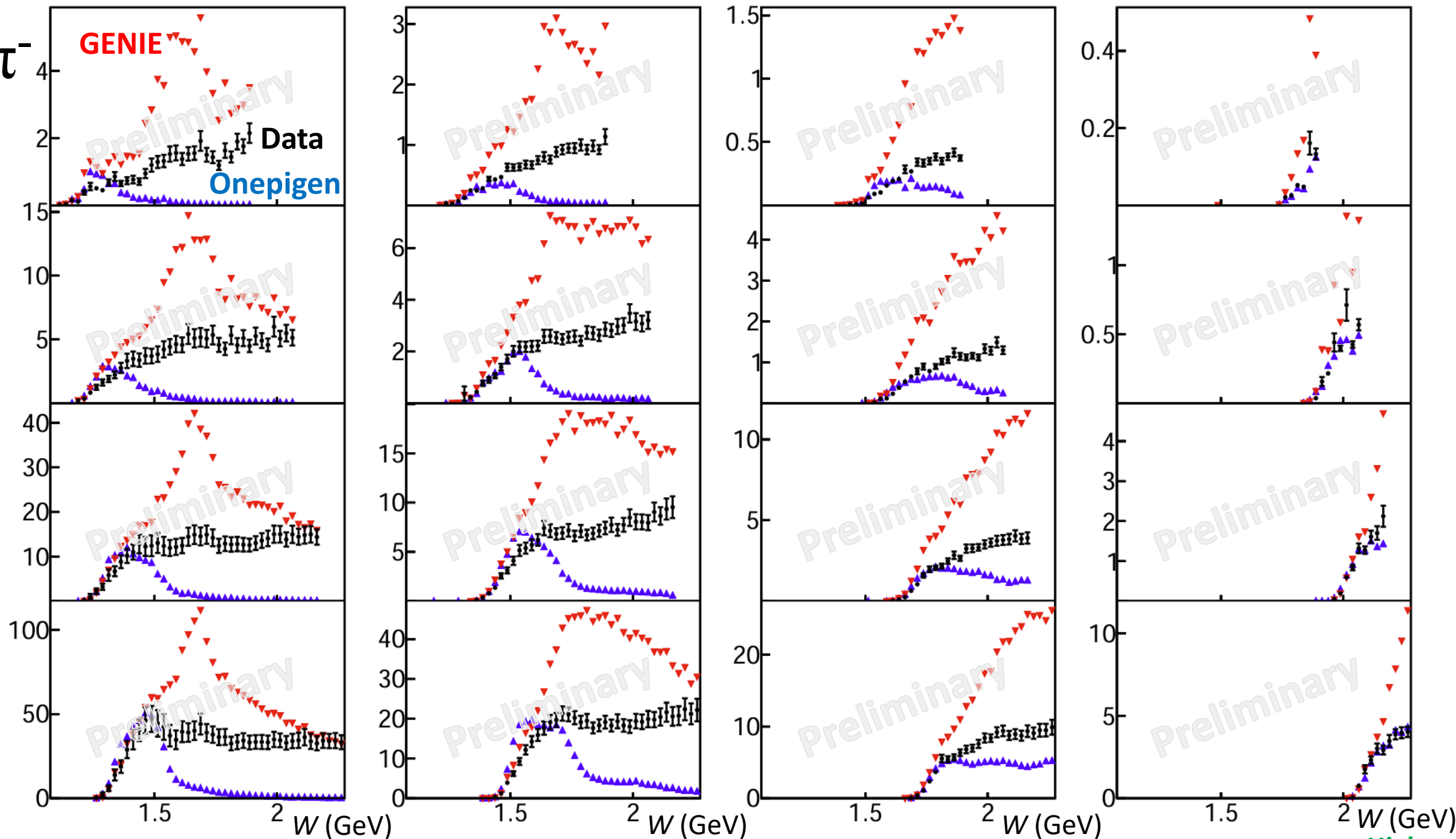
Radiative Corrected Cross Sections

 π^-

GENIE

Data

Onepigen



Cross Sections

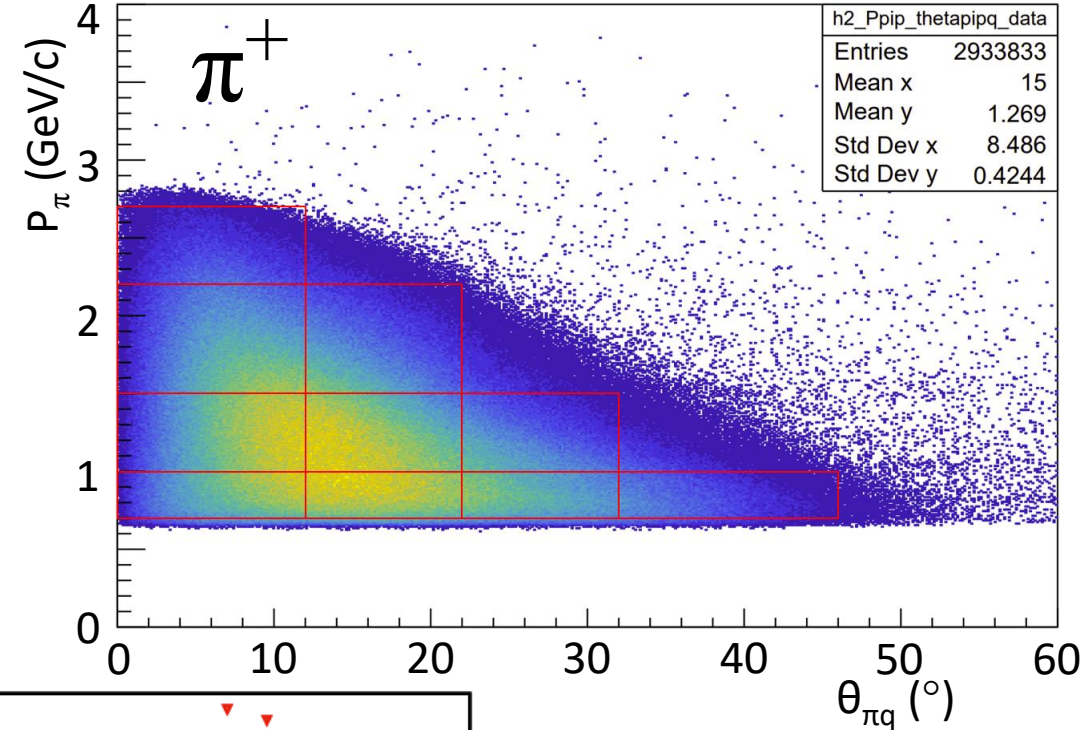
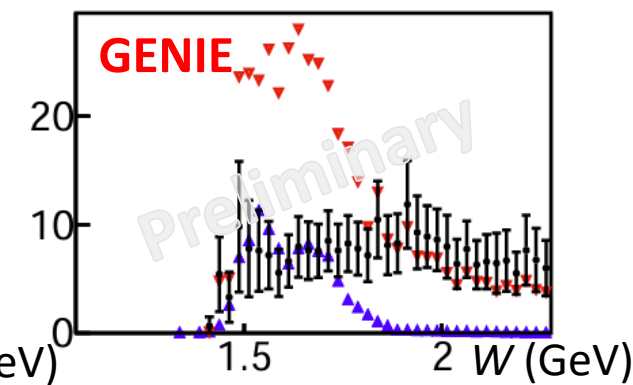
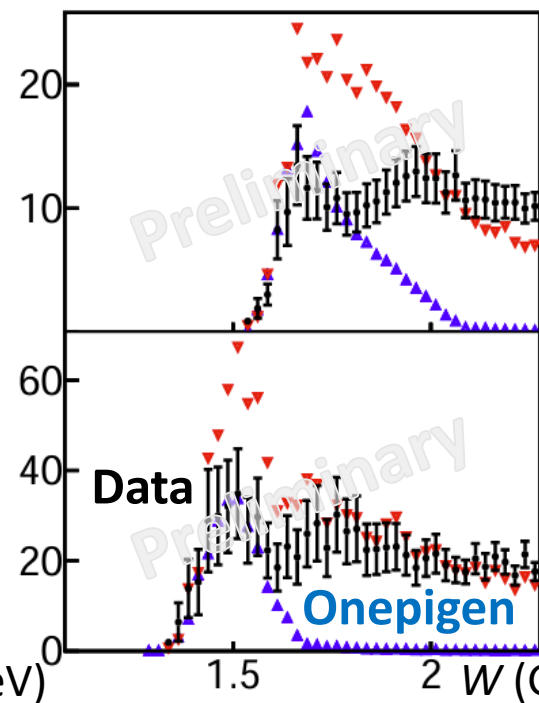
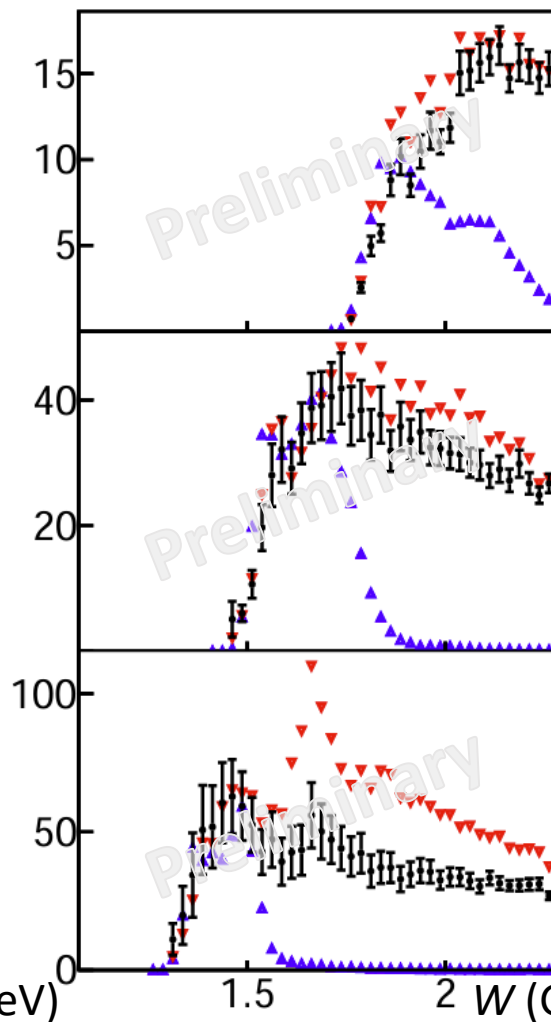
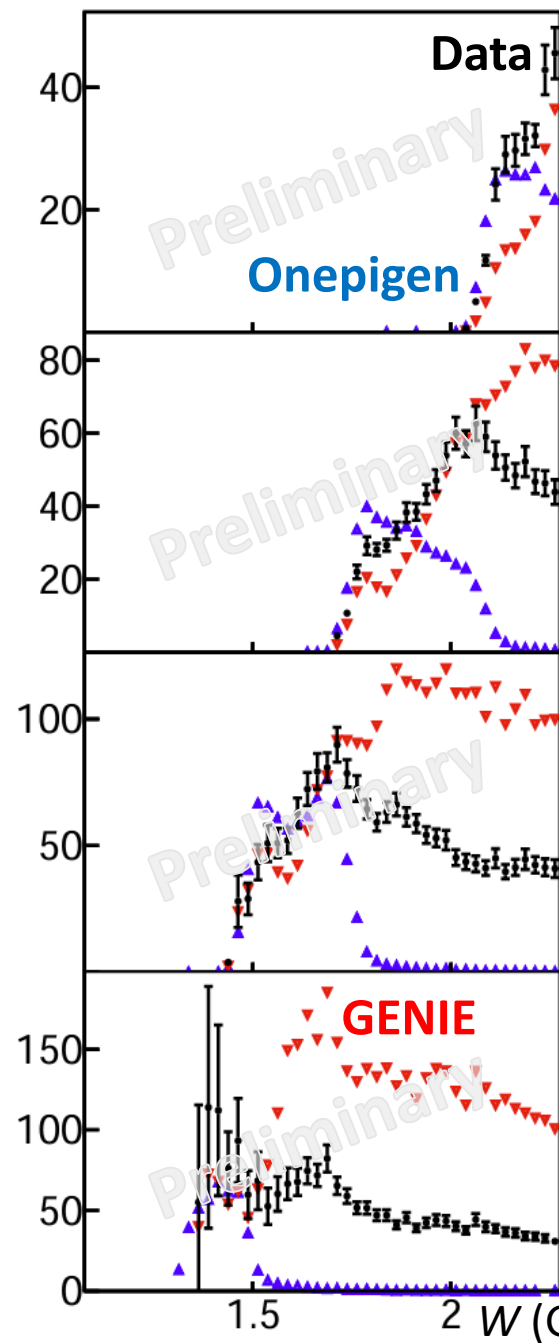
- Includes radiative corrections, acceptance corrections, statistical uncertainties, and systematic uncertainties
- Binning
 - Q^2
 - Q^2 and $\theta_{\pi q}$
 - Q^2 and P_π
 - **Q^2 , $\theta_{\pi q}$, and P_π**
 - **Four Q^2 bins: 0.7 – 2.5 GeV²**
 - **Four $\theta_{\pi q}$ bins: 0° – 46°**
 - **Four P_π bins: 0.7 – 2.7 GeV/c**

Higher P_π

Radiative Corrected Cross Sections

$$d(e, e' \pi^+)$$

$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$

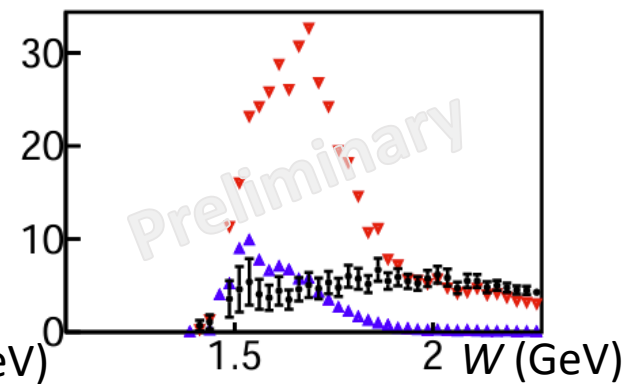
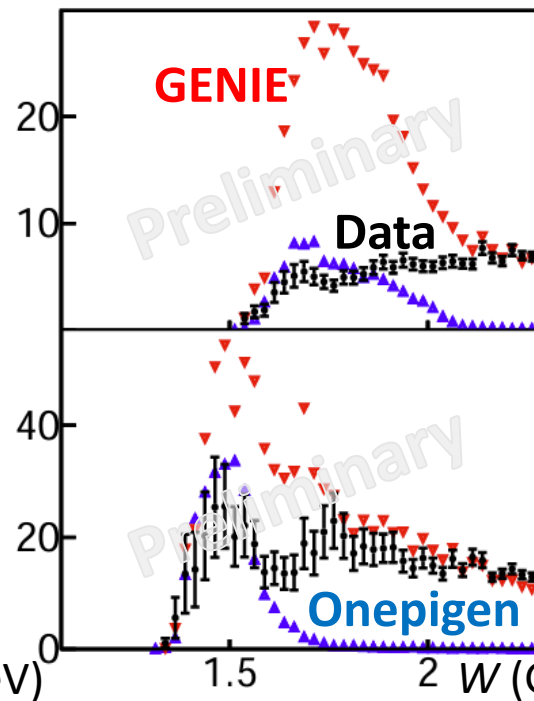
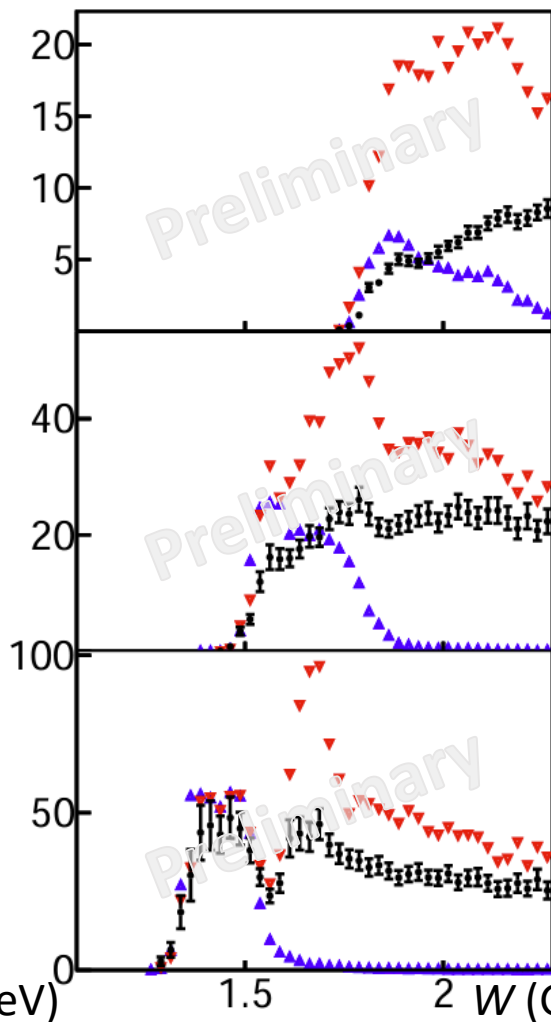
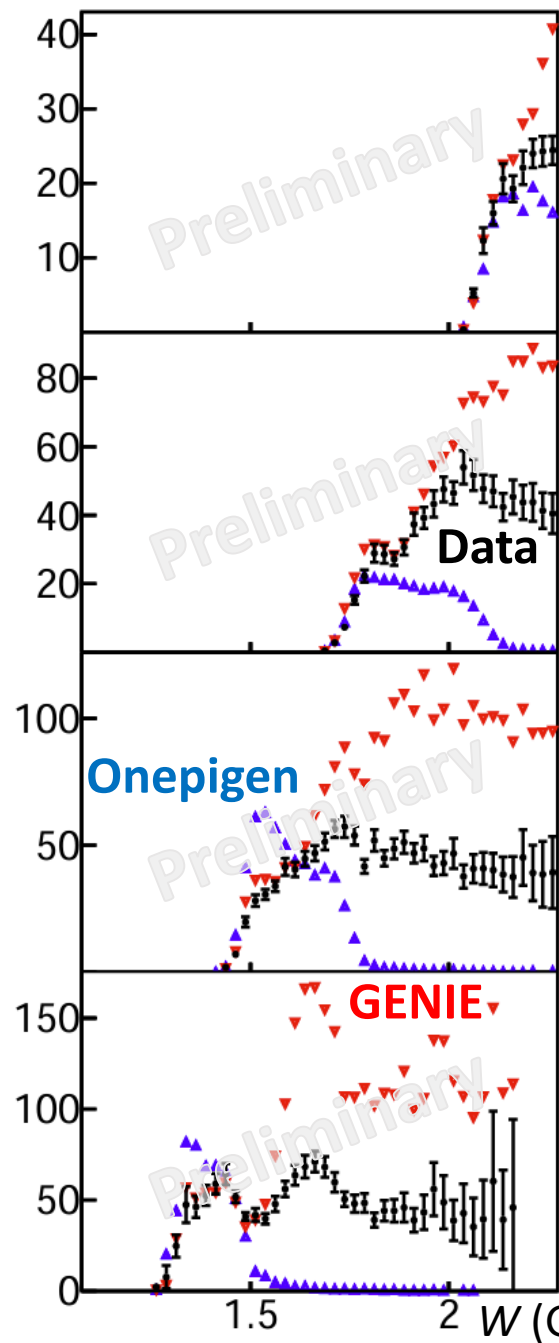
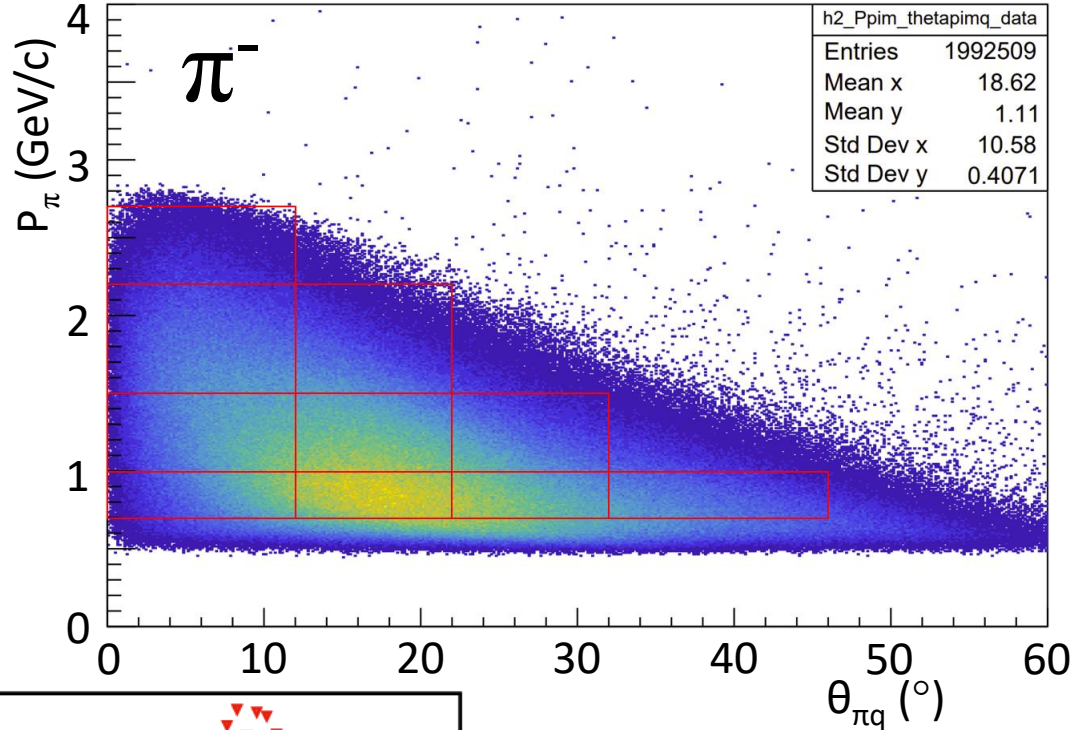
Higher $\theta_{\pi q}$

Higher P_π

Radiative Corrected Cross Sections

$$d(e, e' \pi^-)$$

$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$

Higher $\theta_{\pi q}$

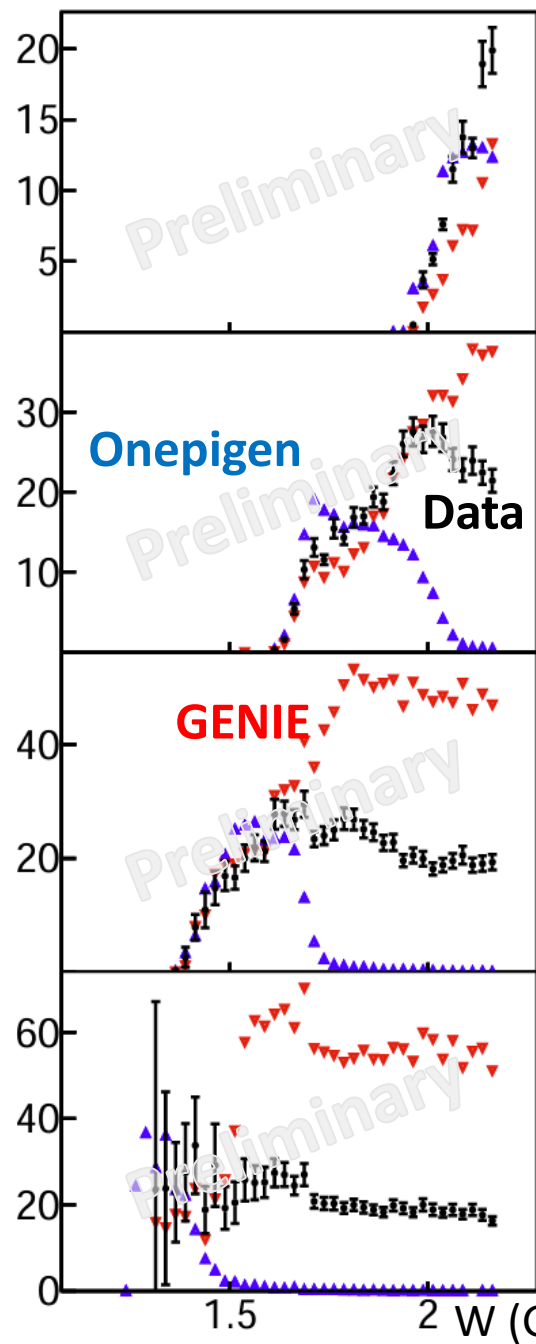
Conclusions

- Physics
 - GENIE and onepigen describe data well for $W < 1.5$ GeV
 - Significant discrepancies for $W > 1.5$ GeV
 - 4D binning shows specific areas to improve GENIE
- Request preliminary approval for data
- Analysis note in progress

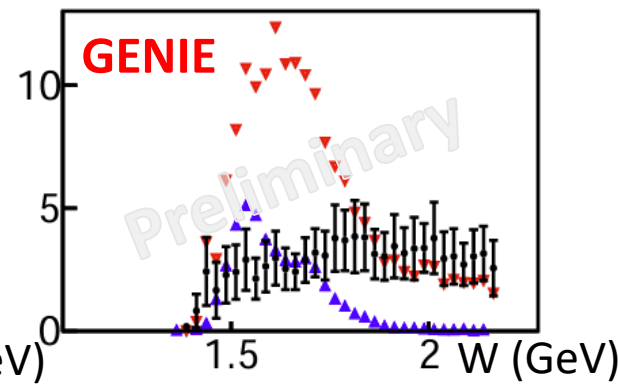
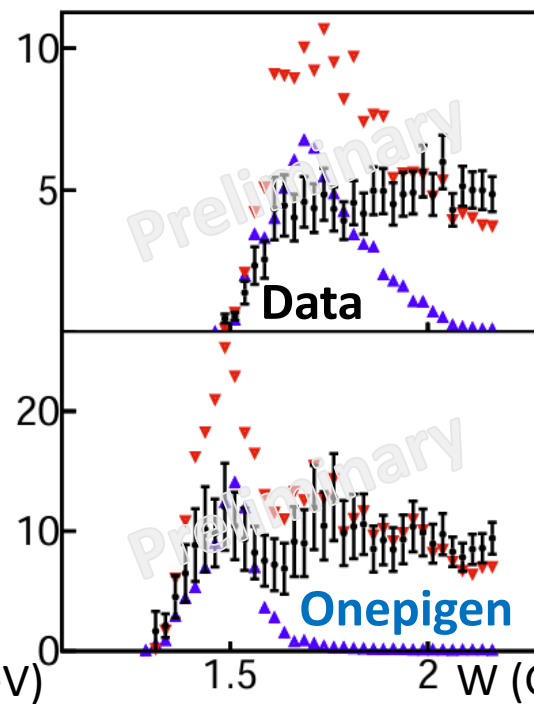
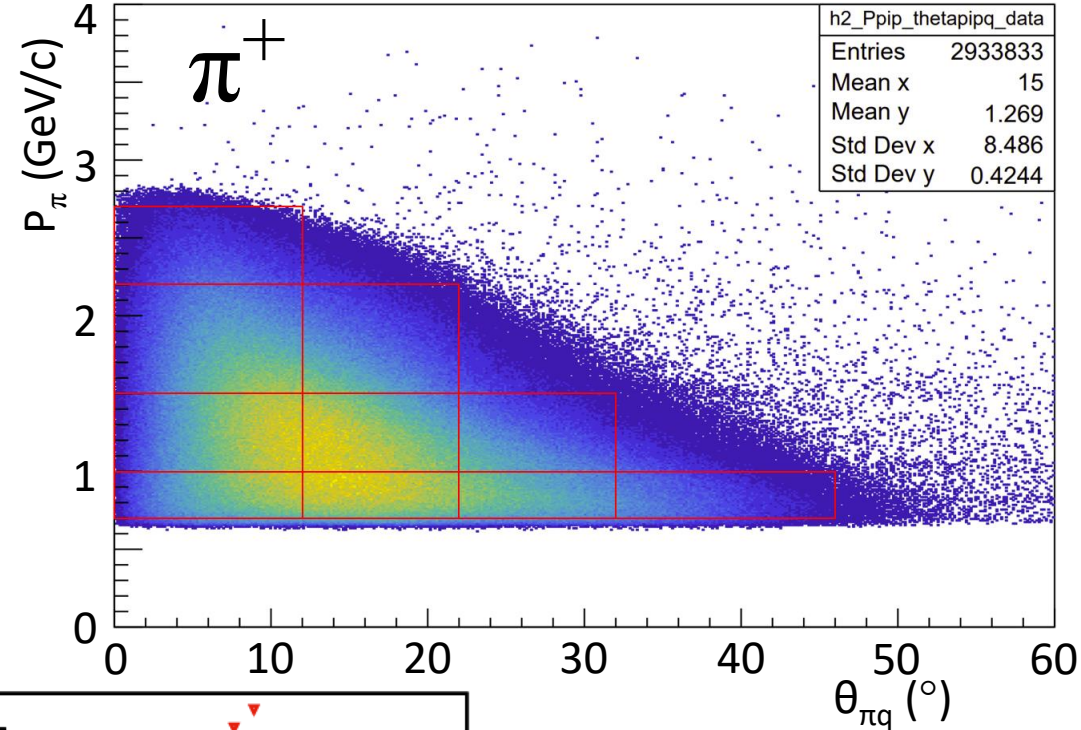
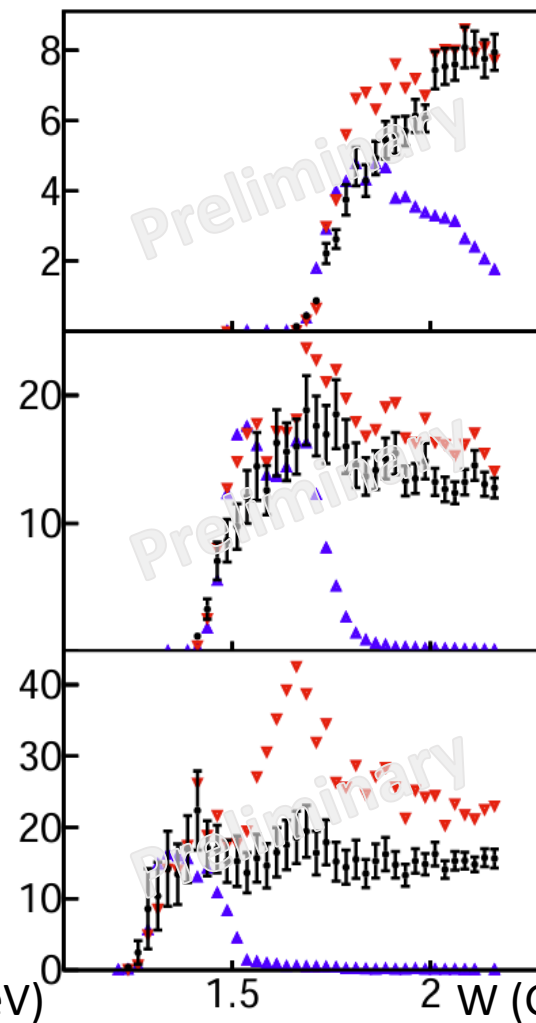
Backup Slides

Higher P_π

Radiative Corrected Cross Sections



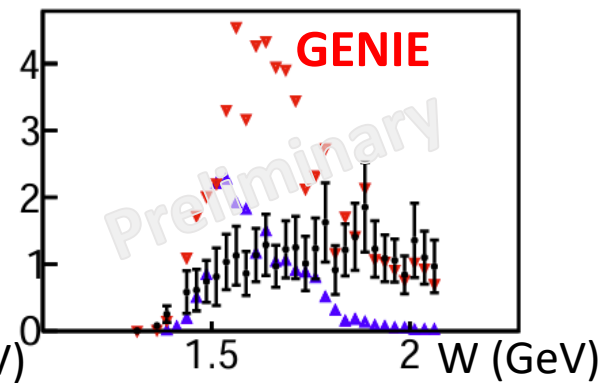
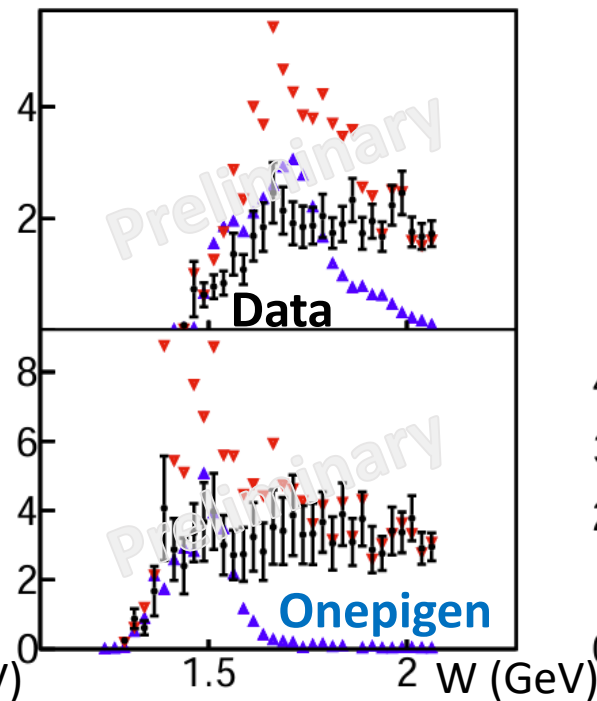
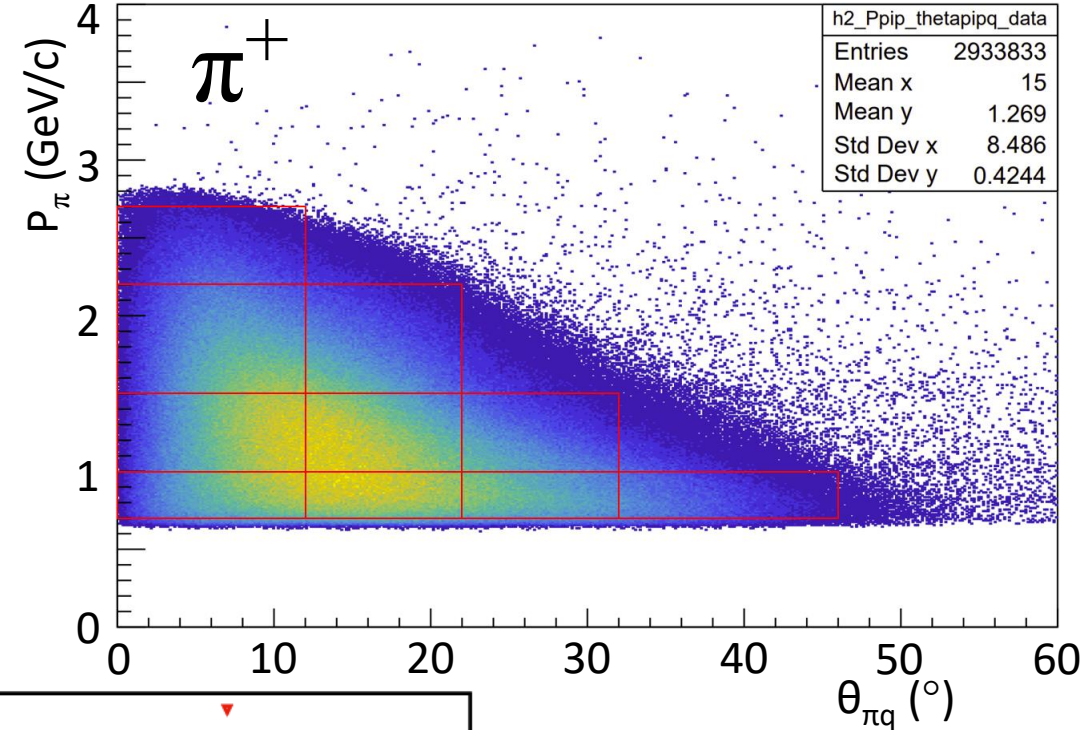
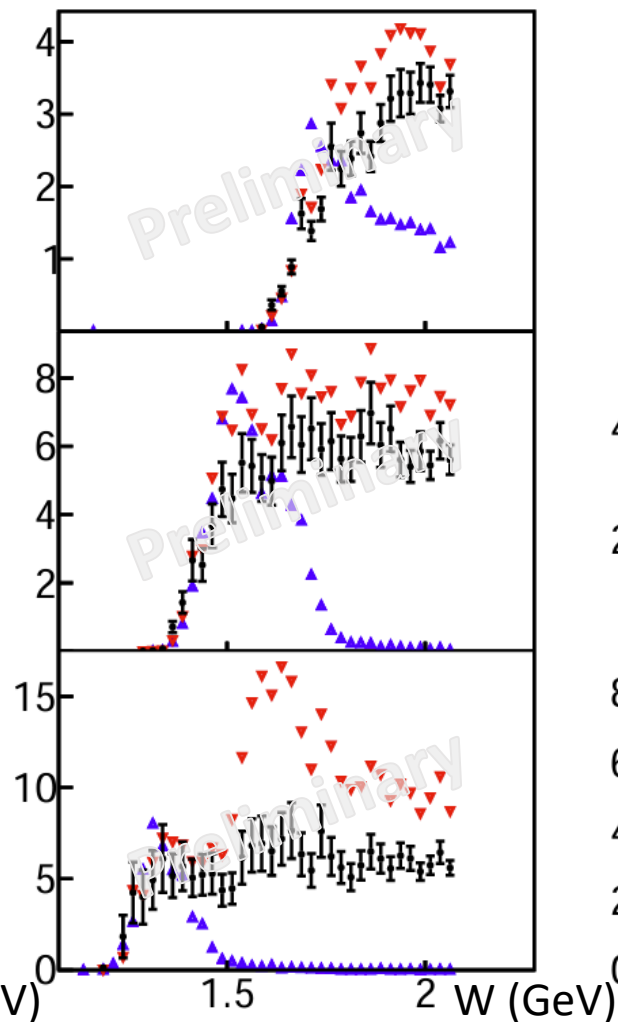
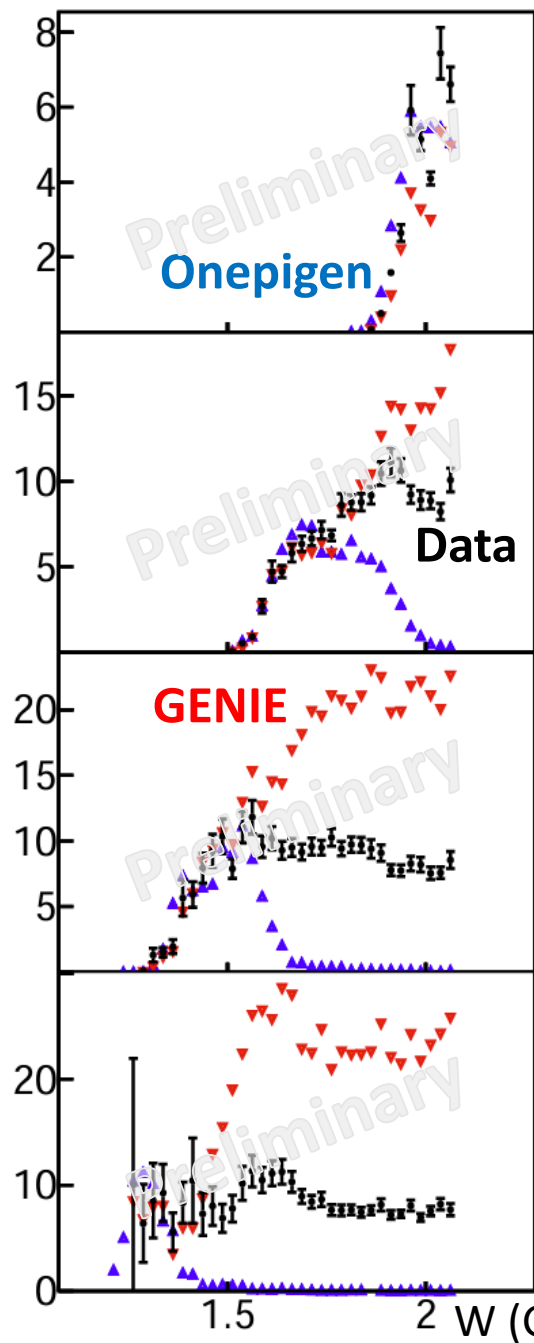
$$d(e, e' \pi^+) \\ 1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$

Higher $\theta_{\pi q}$

Higher P_π

Radiative Corrected Cross Sections

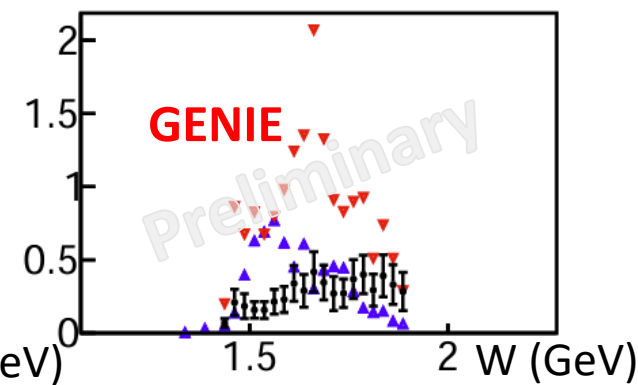
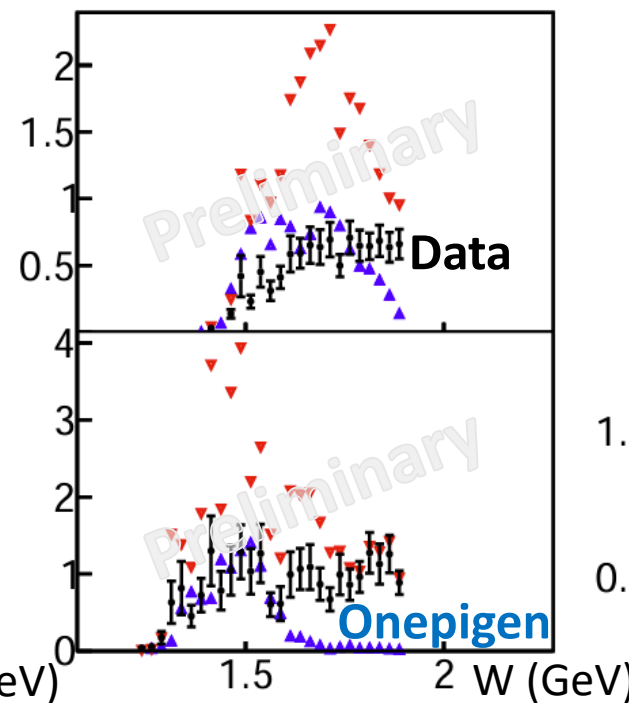
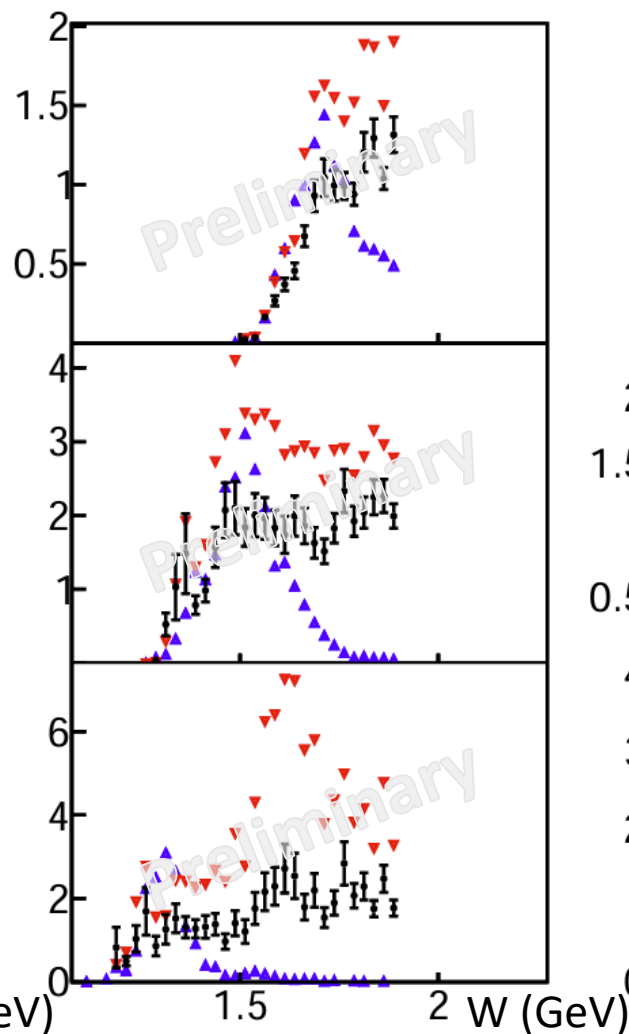
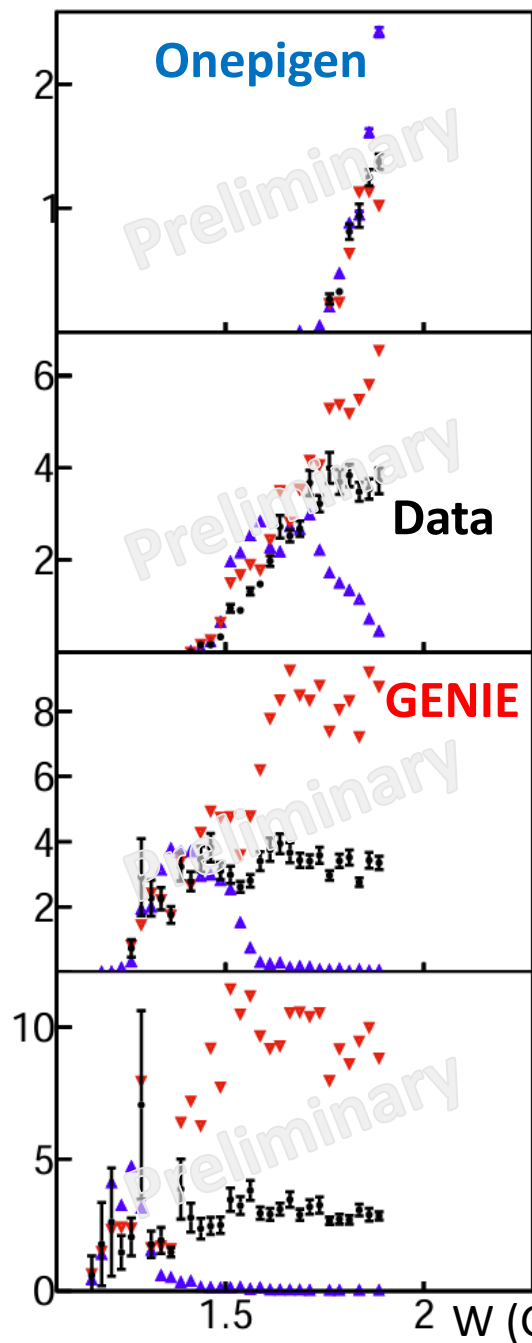
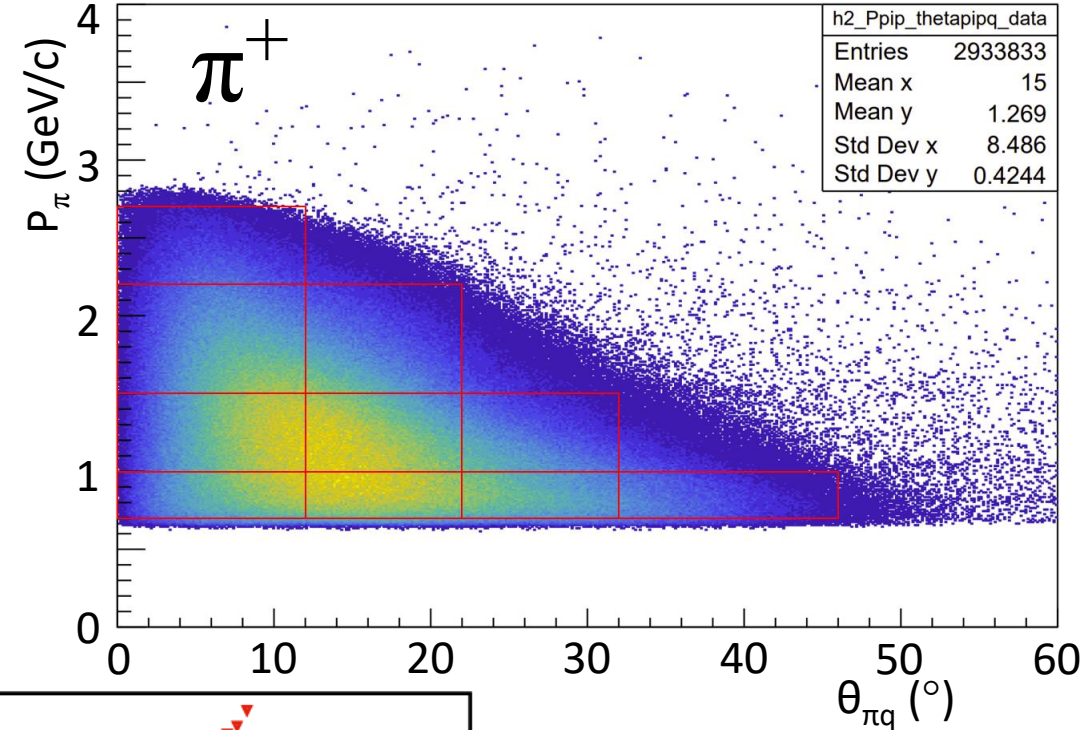
$$d(e, e' \pi^+) \\ 1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$

Higher $\theta_{\pi q}$

Higher P_π

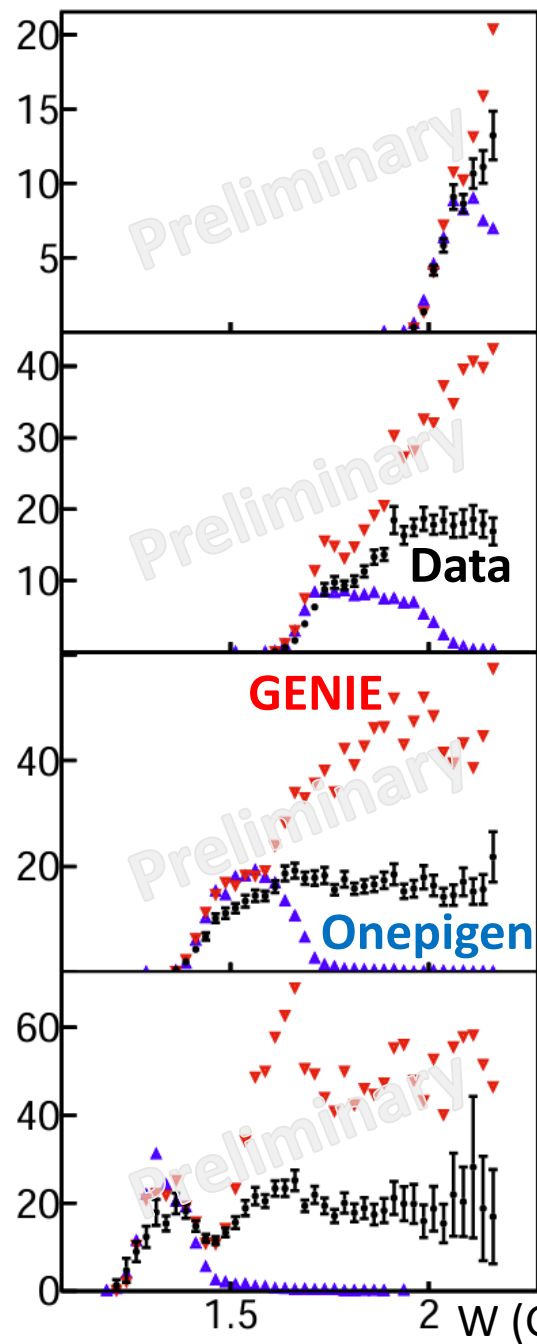
Radiative Corrected Cross Sections

$$d(e, e' \pi^+) \\ 1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$

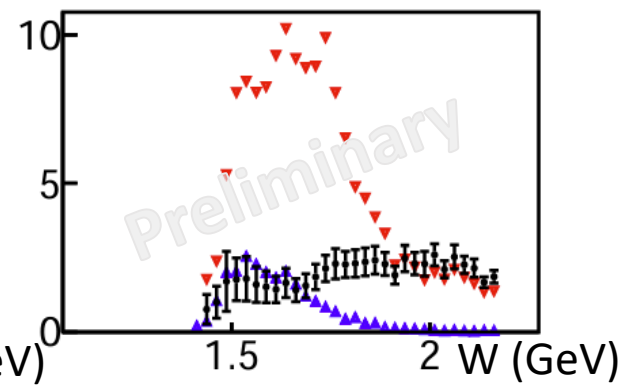
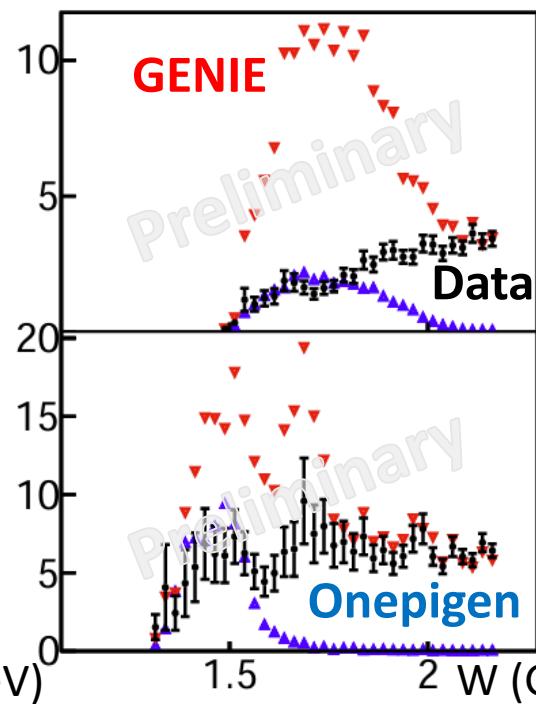
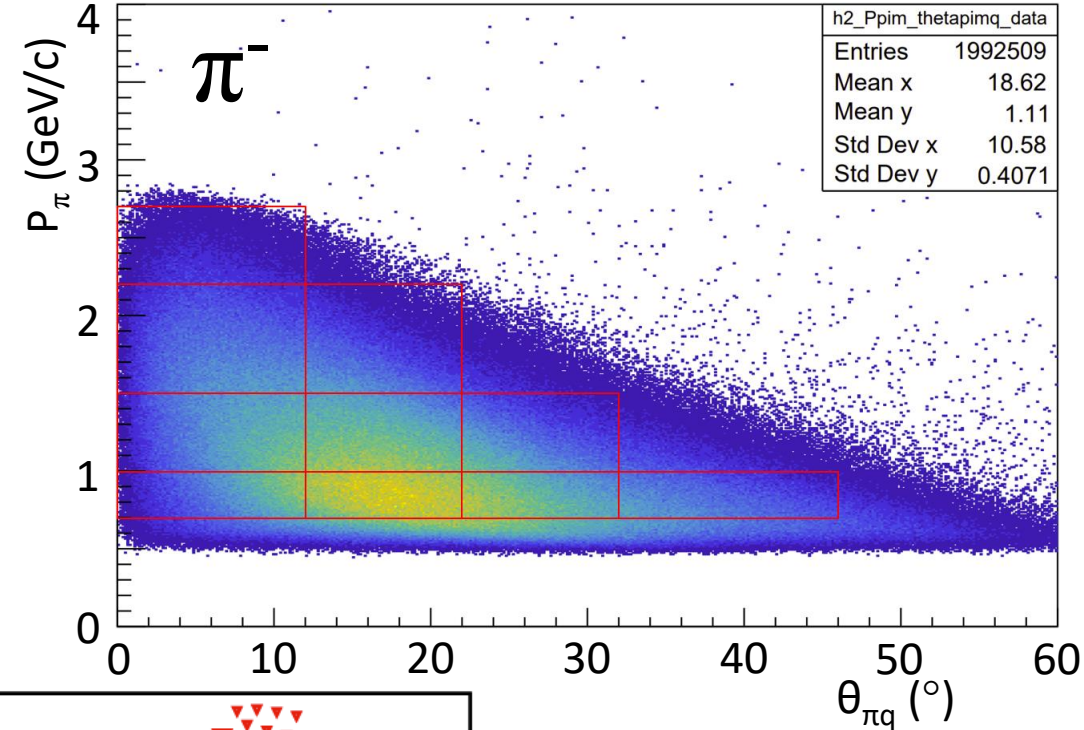
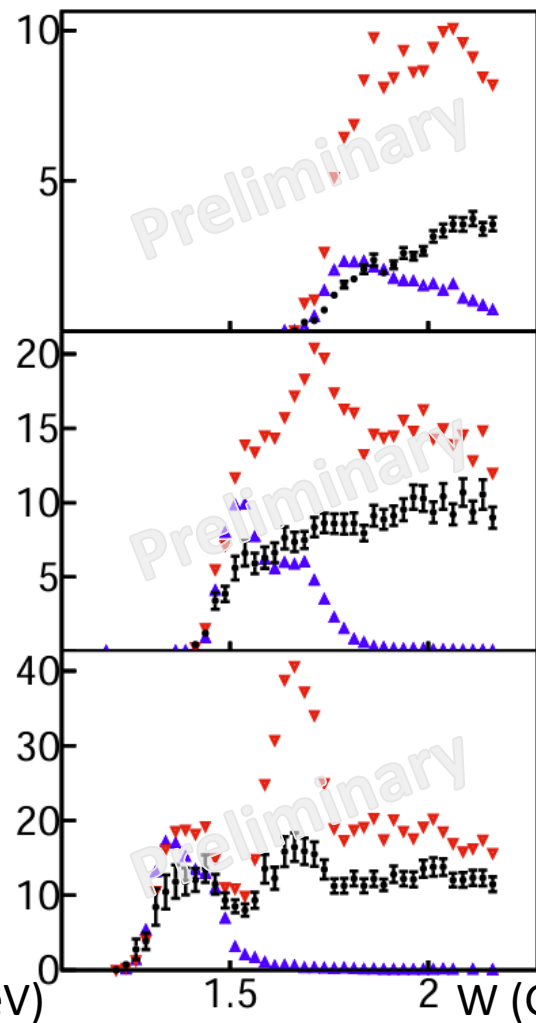
Higher $\theta_{\pi q}$

Higher P_π

Radiative Corrected Cross Sections



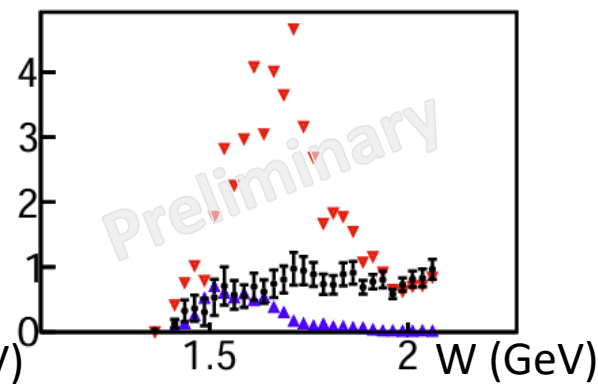
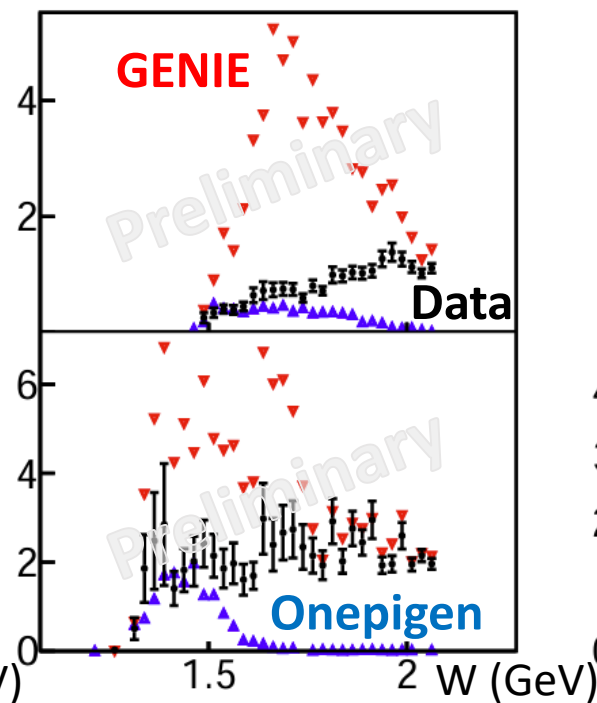
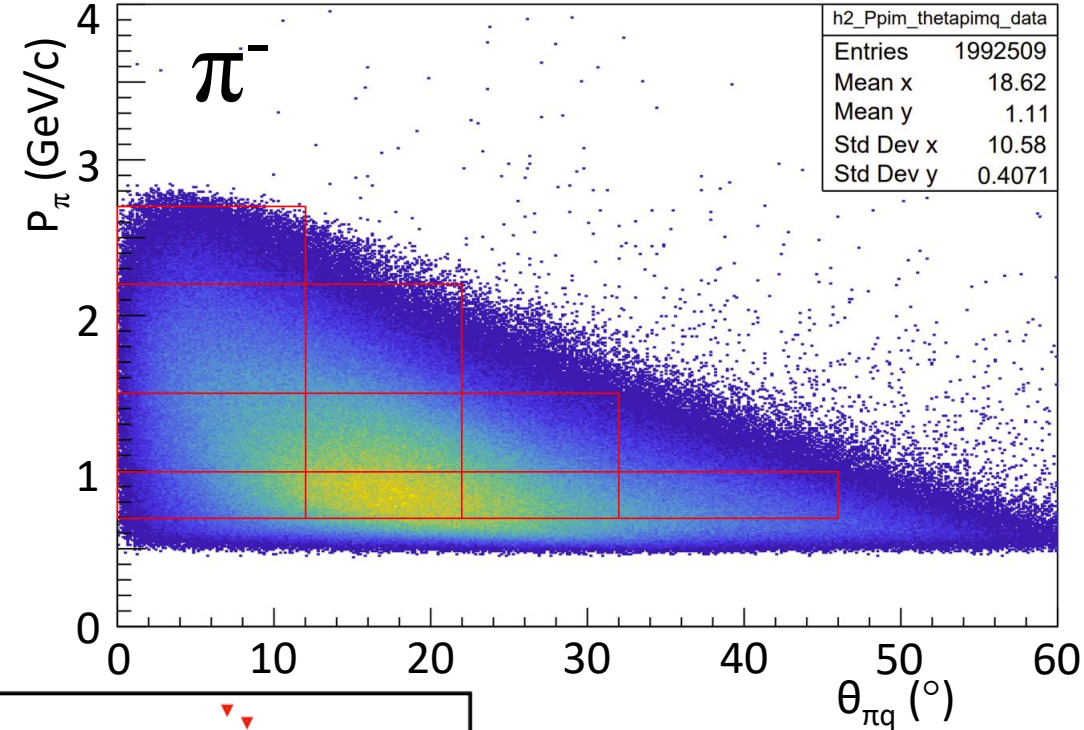
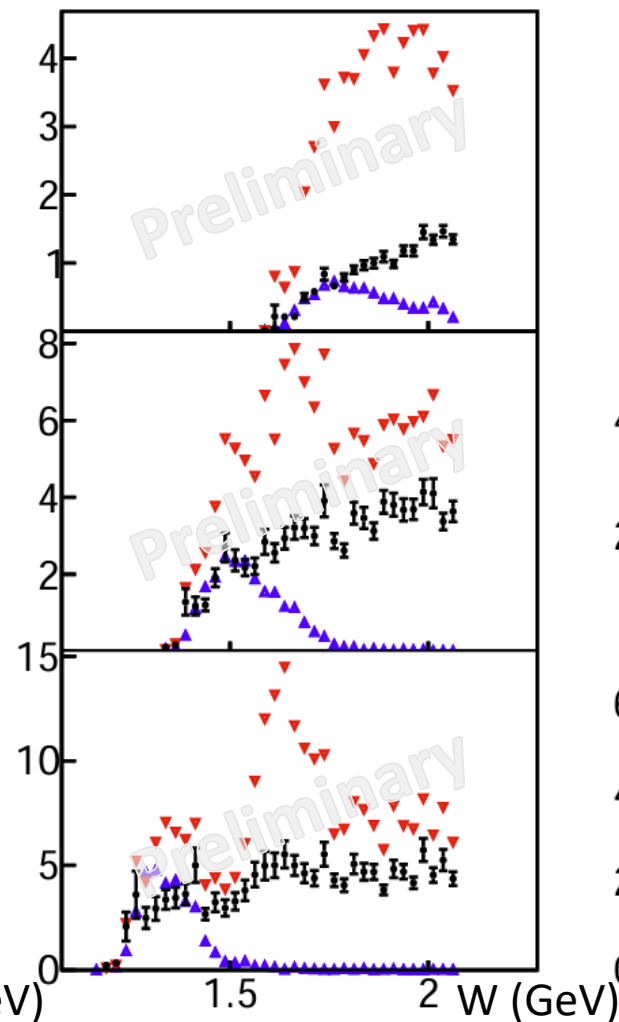
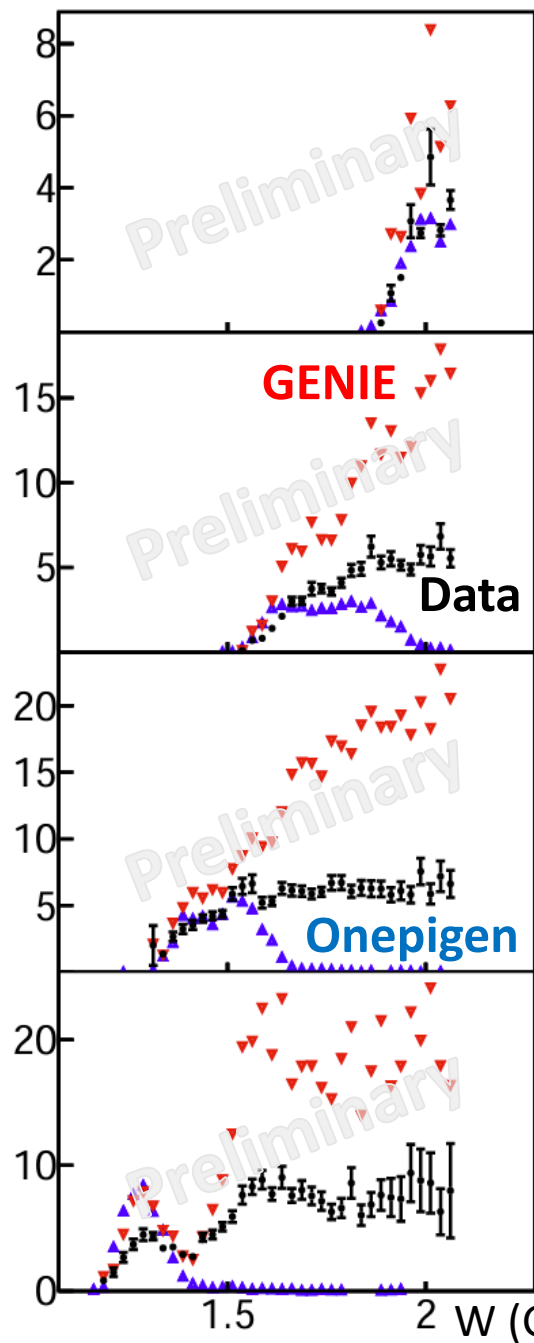
$$d(e, e' \pi^-)$$
$$1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$

Higher $\theta_{\pi q}$

Higher P_π

Radiative Corrected Cross Sections

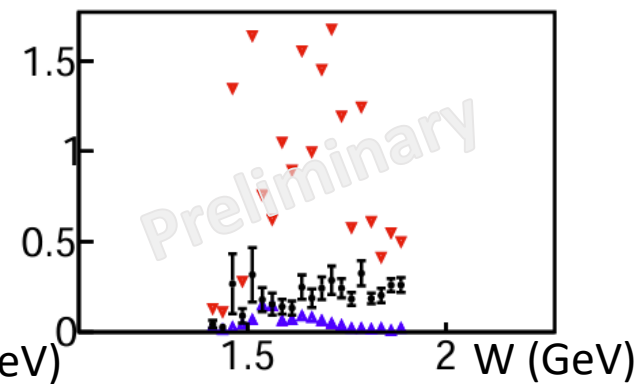
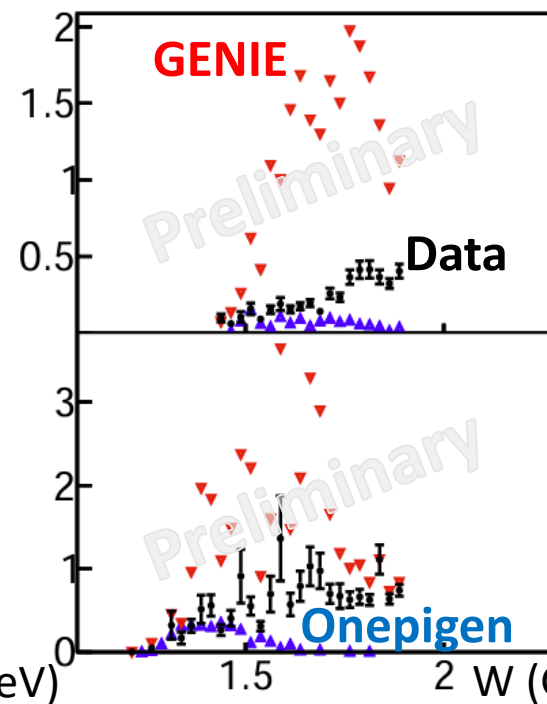
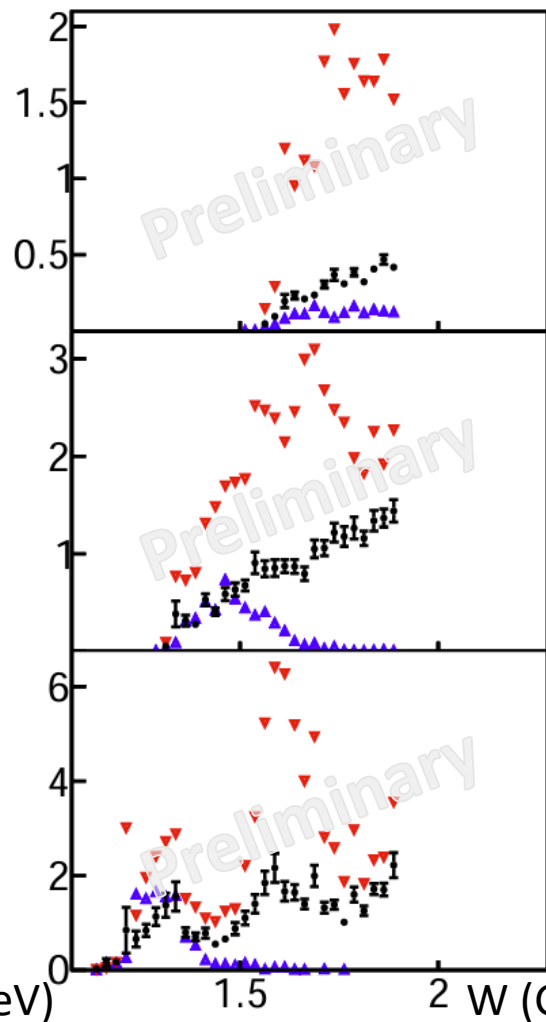
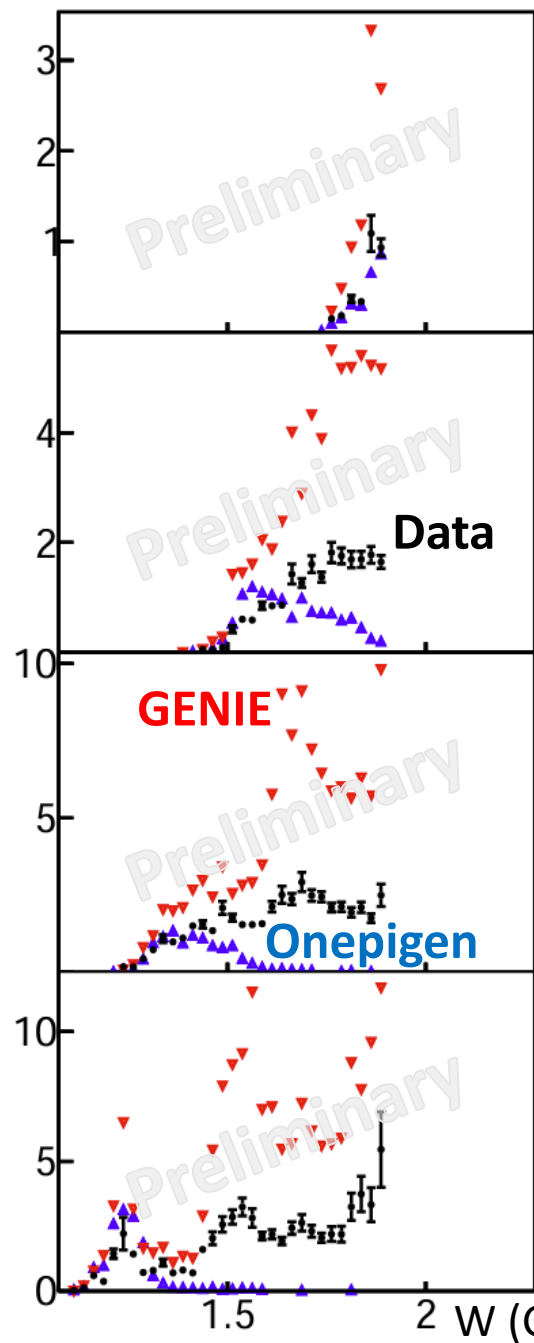
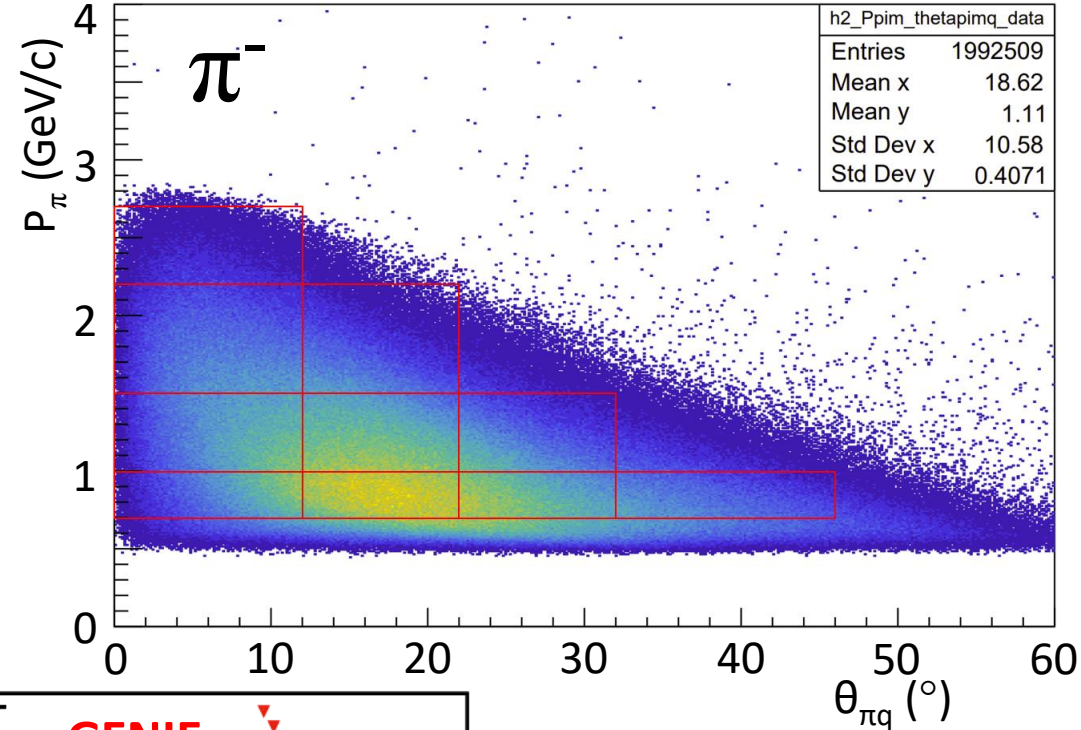
$$d(e, e' \pi^-)$$
$$1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$

Higher $\theta_{\pi q}$

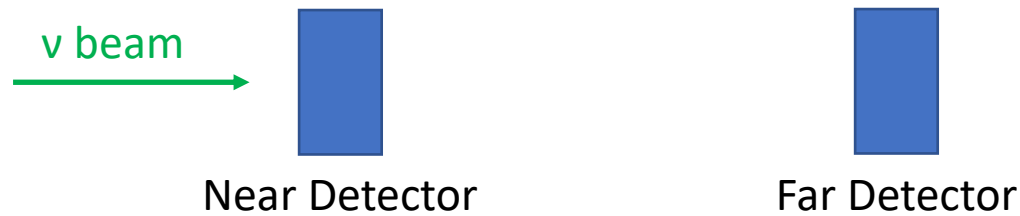
Higher P_π

Radiative Corrected Cross Sections

$$d(e, e' \pi^-)$$
$$1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$

Higher $\theta_{\pi q}$

Neutrino Experiments



Neutrino Flux:

$$\Phi_{\alpha}(E, L) = \left[1 - P_{\nu_{\alpha} \rightarrow \nu_{\beta}}(E, L) \right] \Phi_{\alpha}(E, 0)$$

Far Near

$$N_{\alpha}(E_{rec}, L) = \int \Phi_{\alpha}(E, L) \sigma(E) f_{\sigma}(E, E_{rec}) dE$$

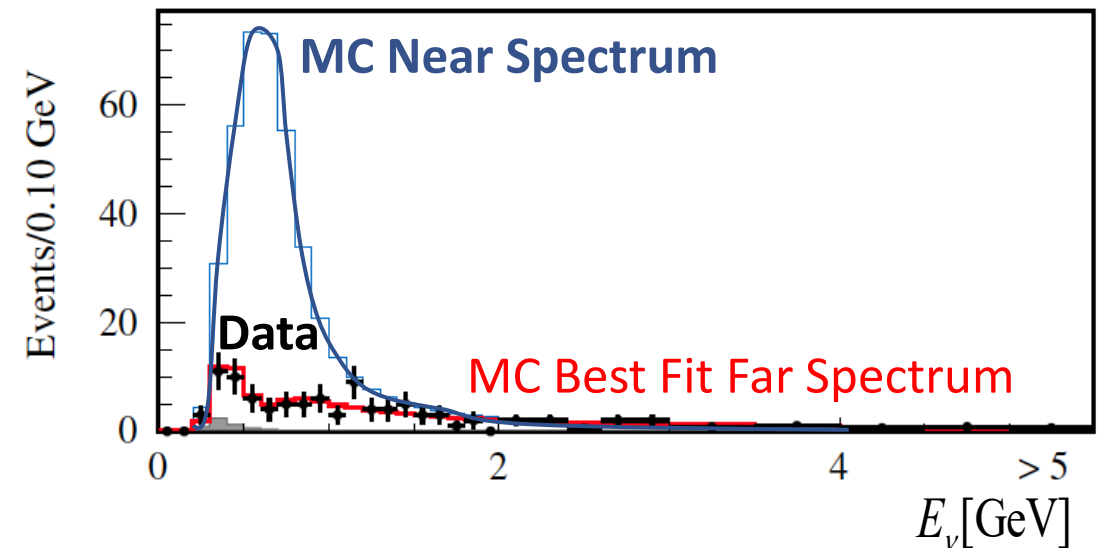
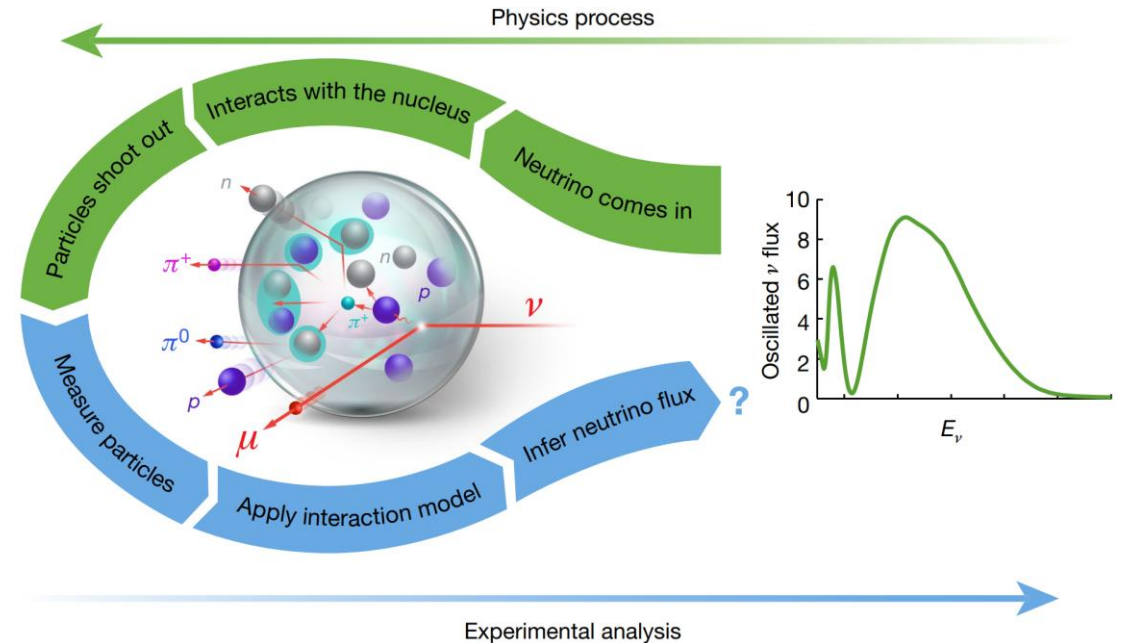
Measured Flux Simulated

Neutrino experiments are difficult

- Large beam energy spread
- Small cross sections

Need GENIE to extract the neutrino flux from data

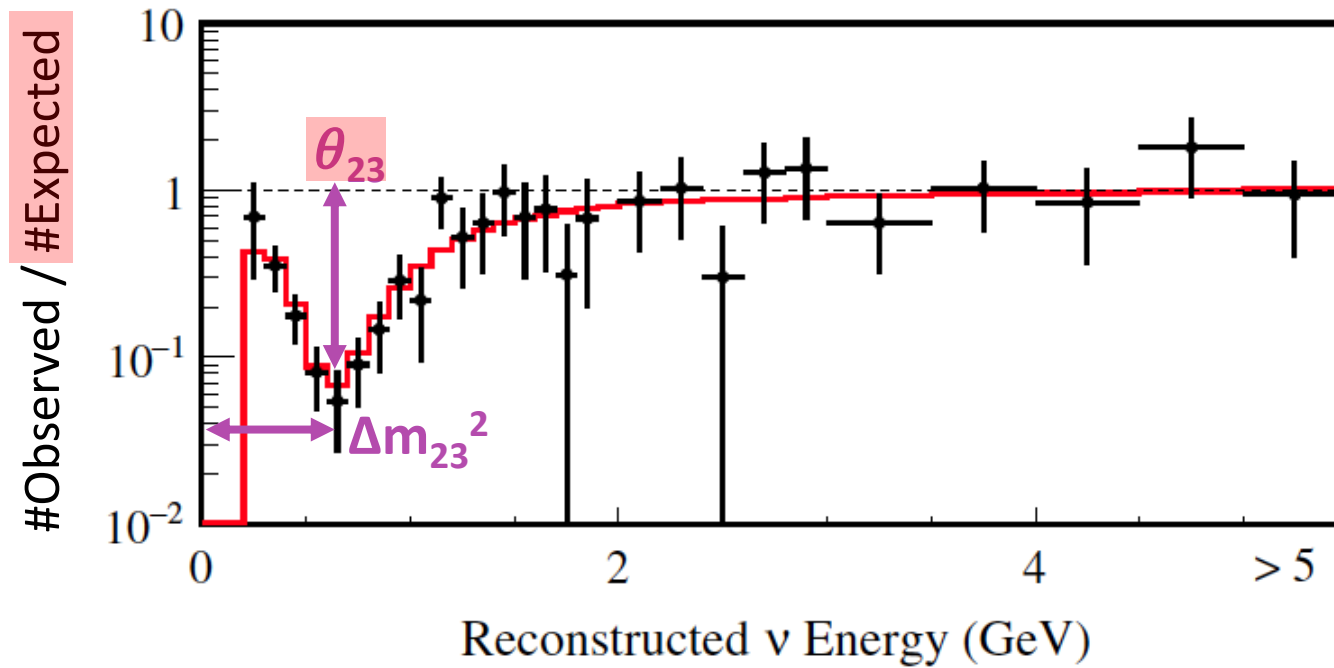
How to validate GENIE?



PRD 91, 072010 (2015)

Oscillation Probability

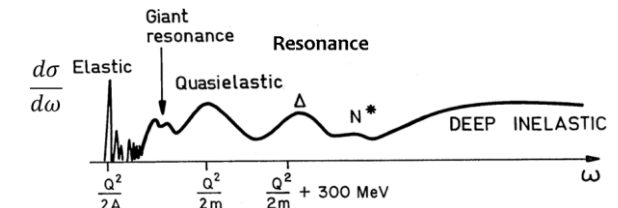
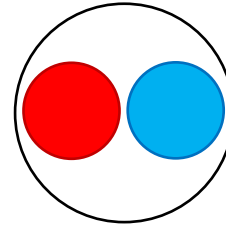
$$P(\nu_\mu \rightarrow \nu_\mu) = \sin^2(2\theta_{23}) \times \sin^2\left(\frac{\Delta m_{32}^2 L}{4E_\nu}\right)$$



T2K PRD (2015)

Pion Physics

- Mesons consisting of combinations of u and d quarks and antiquarks
- Commonly produced in scattering experiments



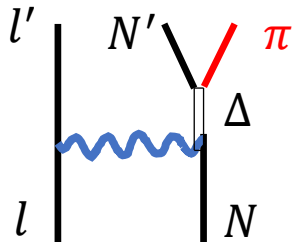
$$e + p \rightarrow e' + n + \pi^+$$

$$e + n \rightarrow e' + p + \pi^-$$

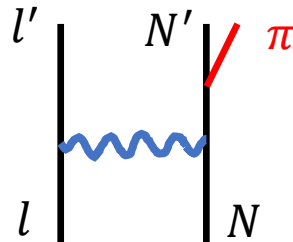
$$e + p \rightarrow e' + p + \pi^0$$

$$e + n \rightarrow e' + n + \pi^0$$

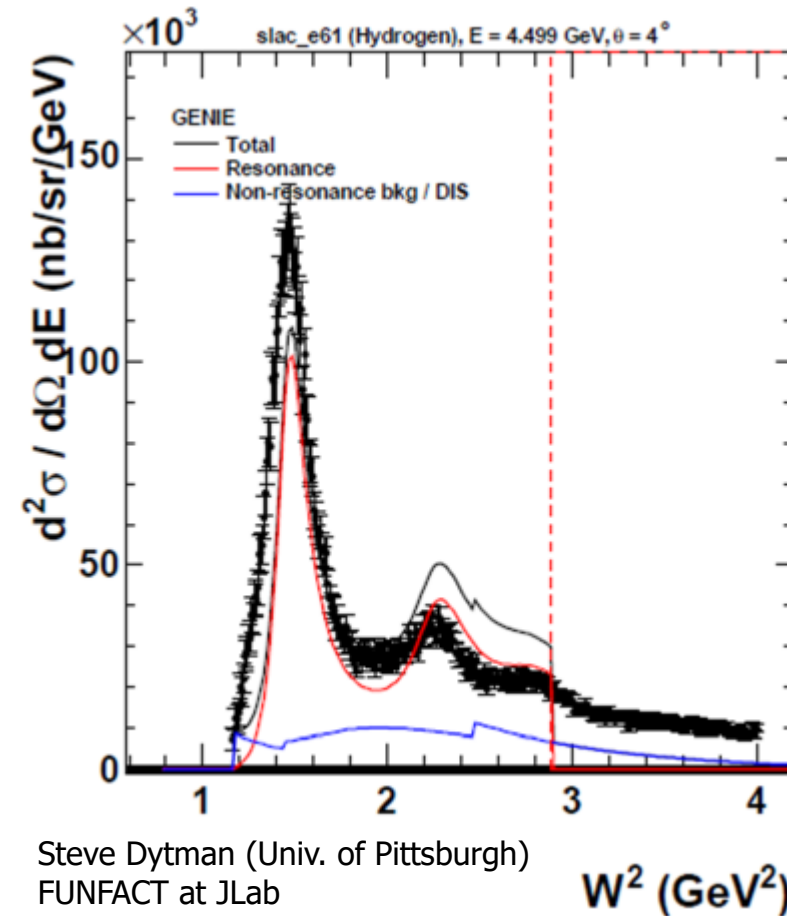
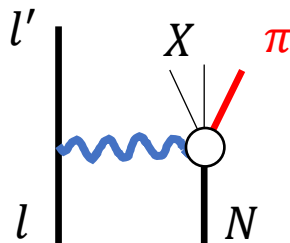
Resonance Decay Production



Non-Resonant Production



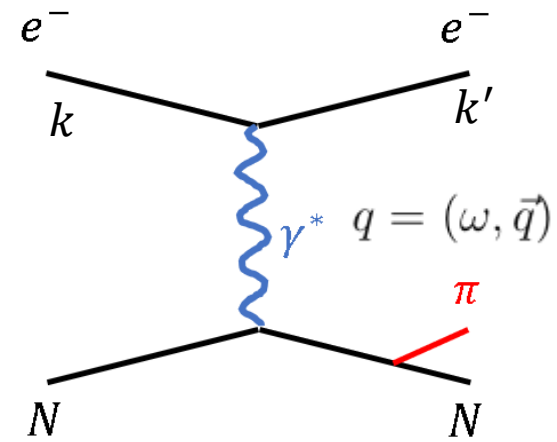
DIS Production



Steve Dytman (Univ. of Pittsburgh)
FUNFACT at JLab
May 15, 2015

$$Q^2 = -q^2 = (k - k')^2$$

$$W = \sqrt{M_N^2 + 2M_N\omega - Q^2}$$



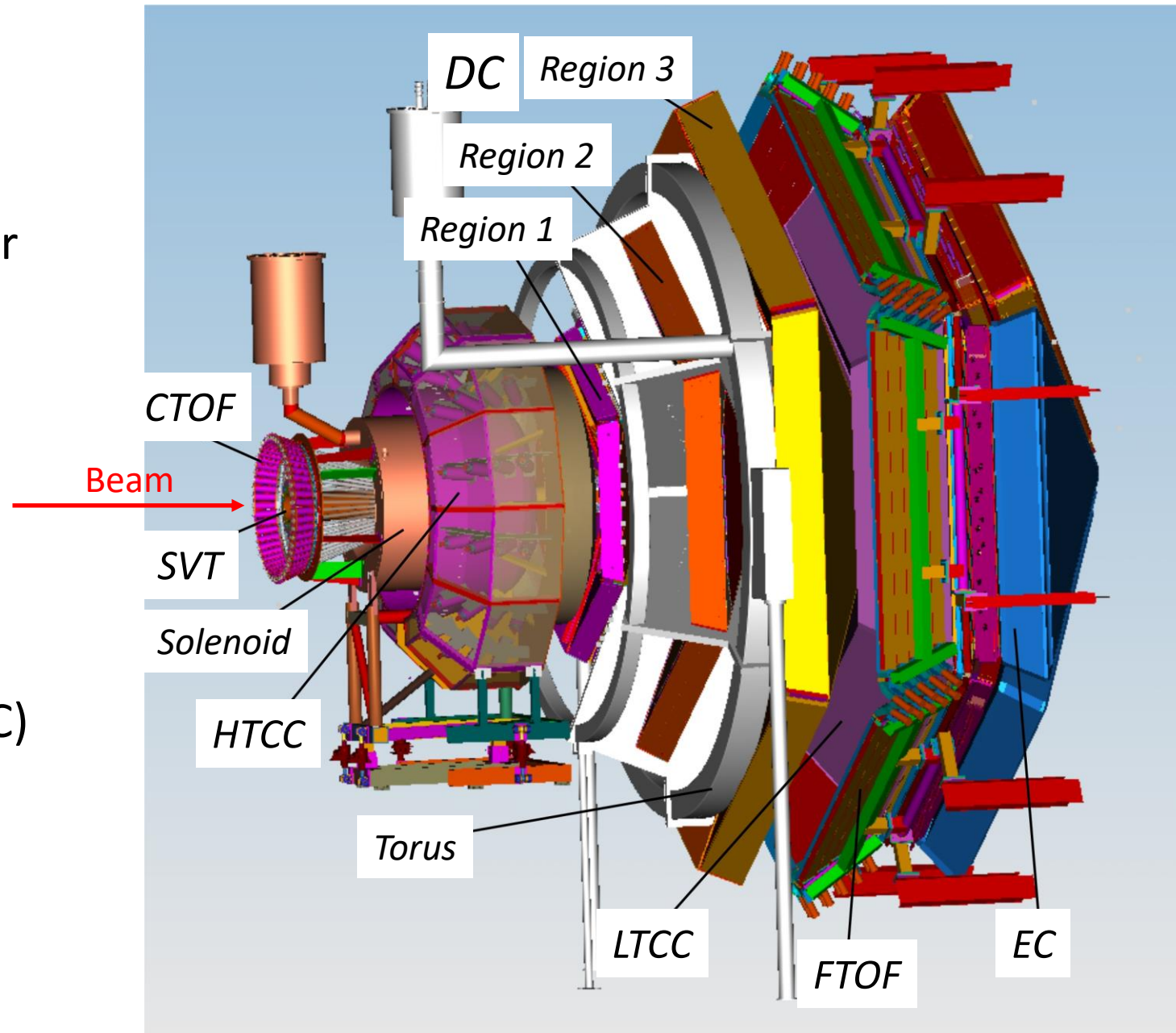
CLAS12

- Forward Detector:

- High Threshold Cerenkov Counter (HTCC) identifies scattered electrons
- Drift Chambers (DC) measure charged particle momenta
- Forward Time-of-Flight (FTOF) measures time-of-flight of charged particles
- Electromagnetic Calorimeters (EC) identifies scattered electrons
 - Includes Pre-shower Calorimeter (PCAL)

- Central Detector:

Not used in this analysis

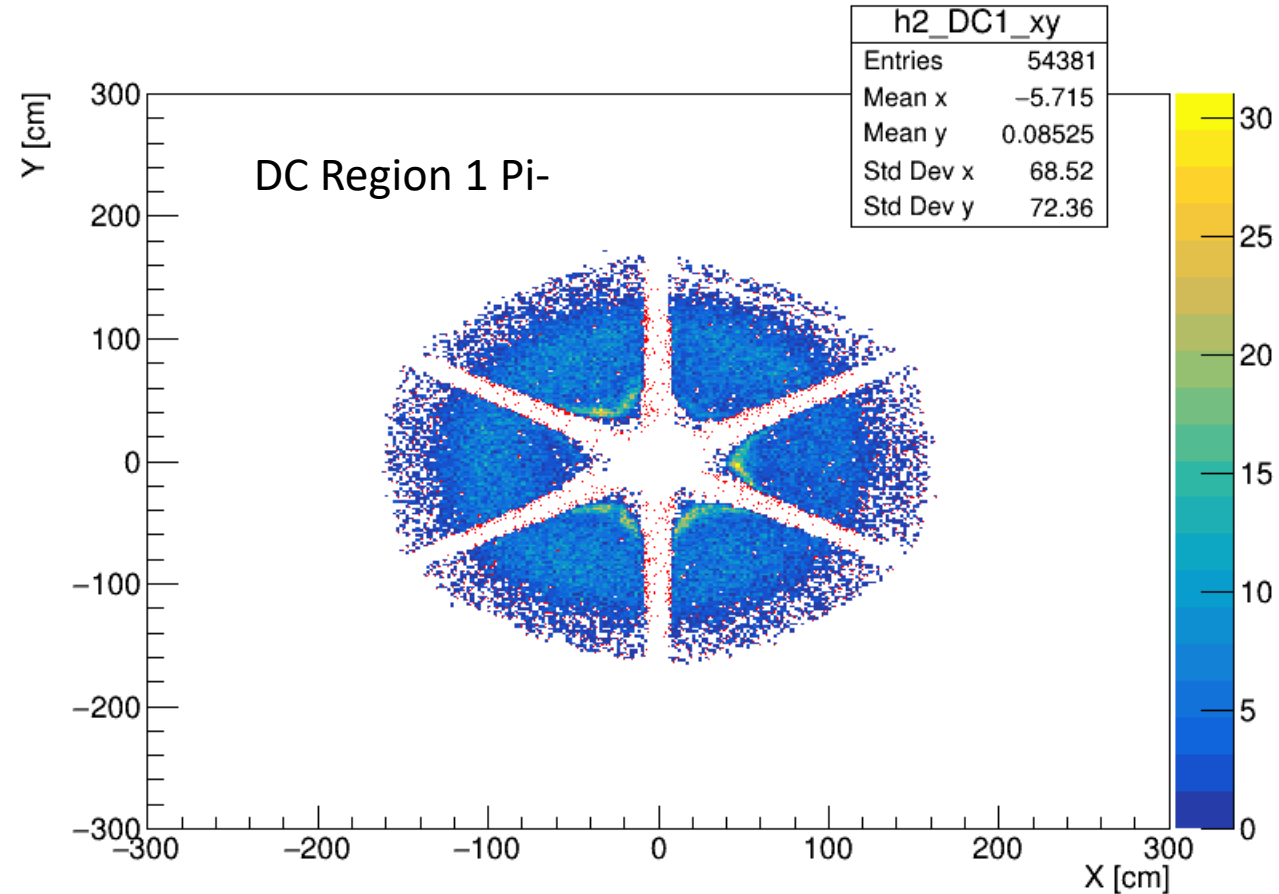
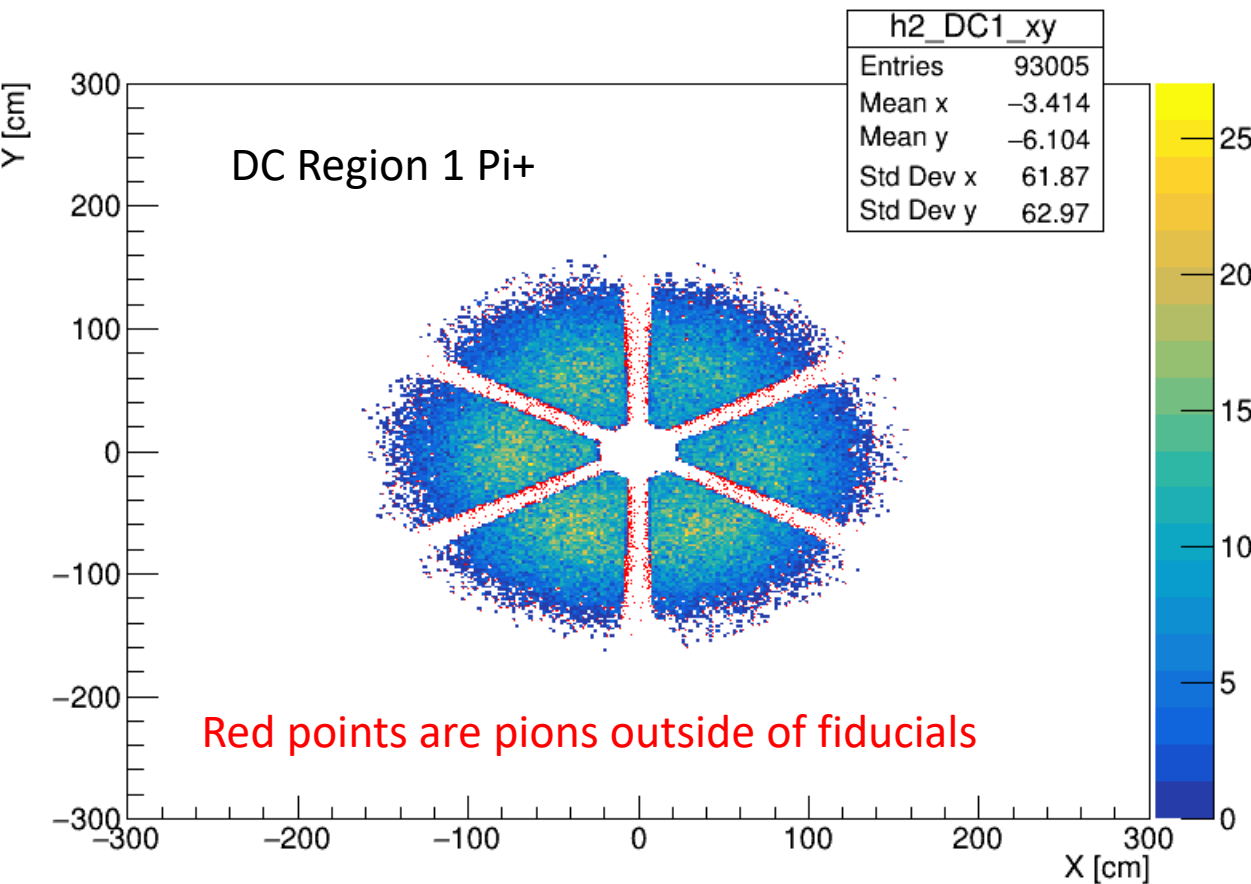


FTOF Best Fit

$$\Delta t = t_{start\ time} - \left[t_{FTOF} - \frac{L}{\beta_h(p)} \right]; \beta_h(p) = \frac{p}{\sqrt{p^2 + m^2}}$$

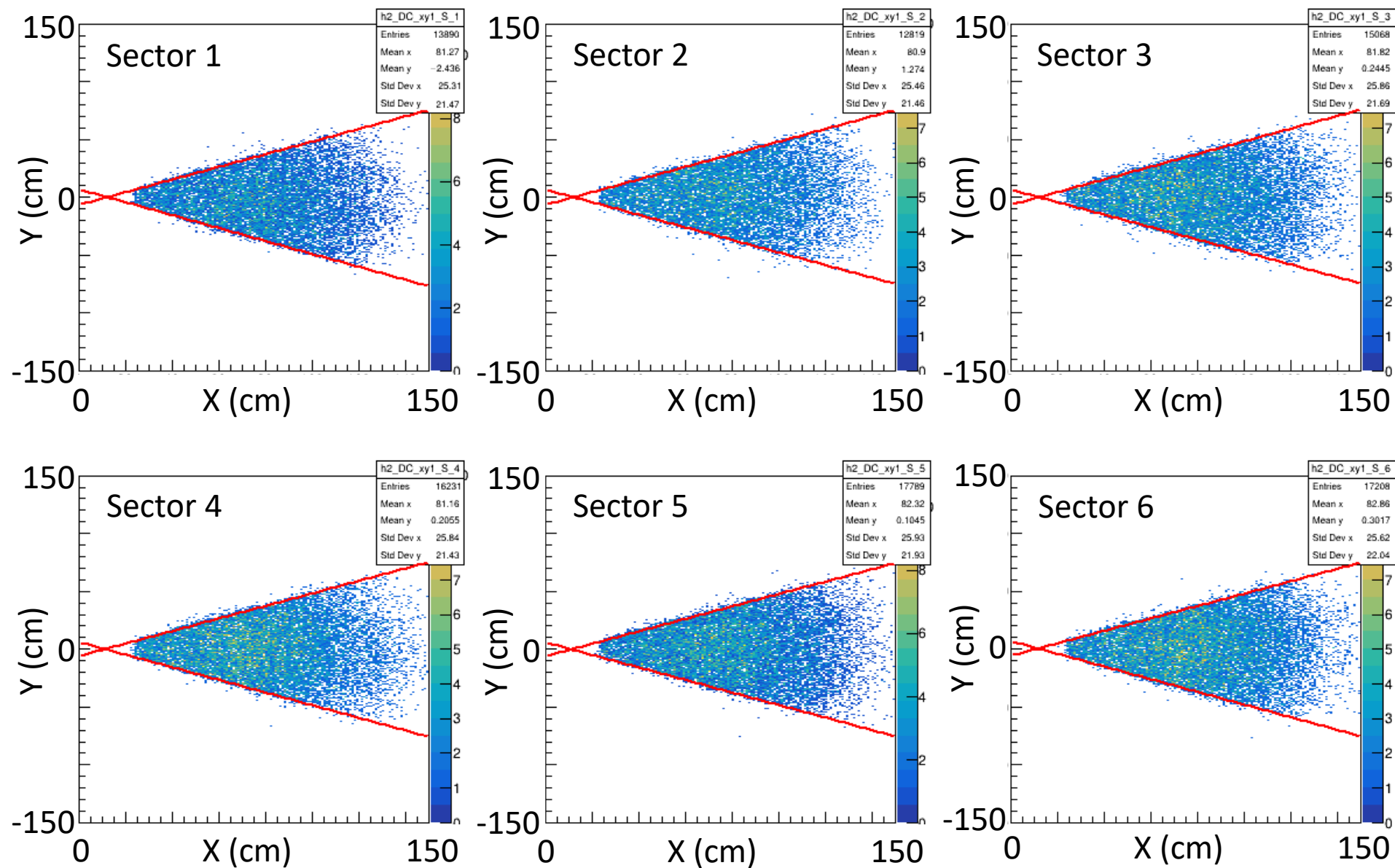
DC Fiducial Cuts

- Fiducial cuts select hits (or tracks) with near 100% efficiency



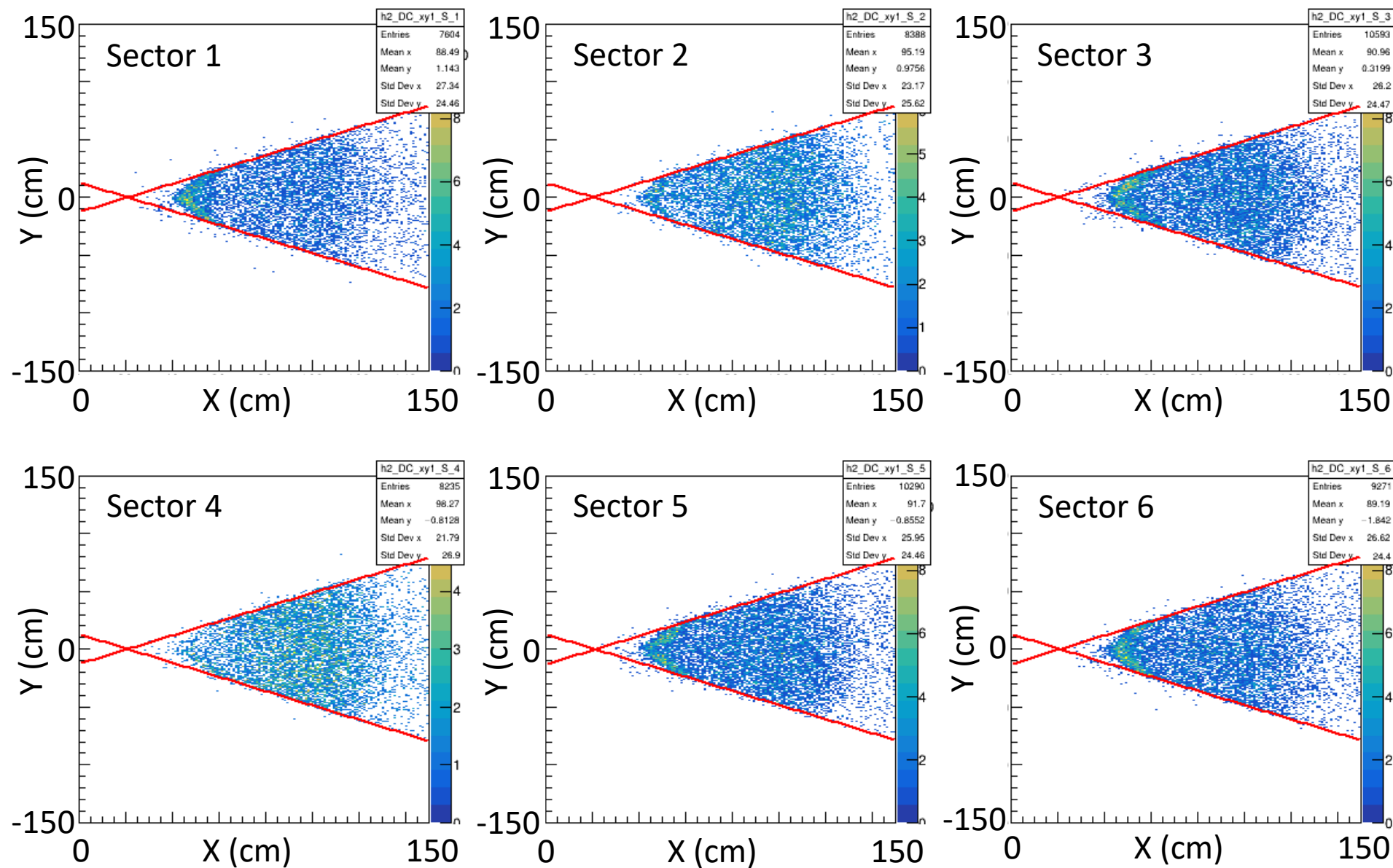
DC Fiducial Cuts

Region 1 (Pi+)

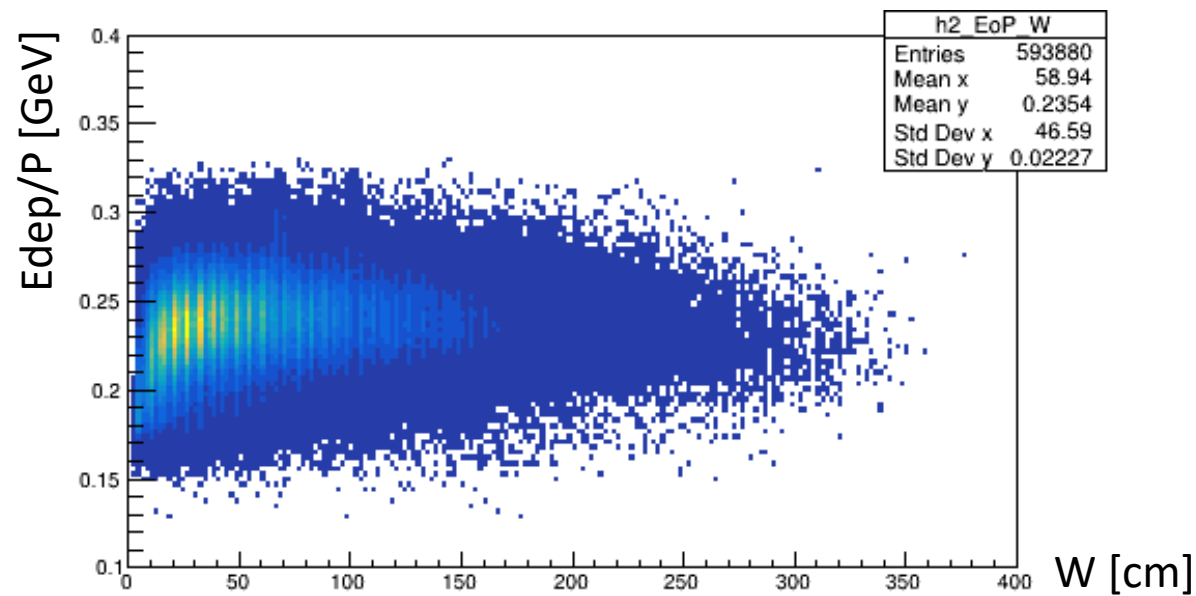
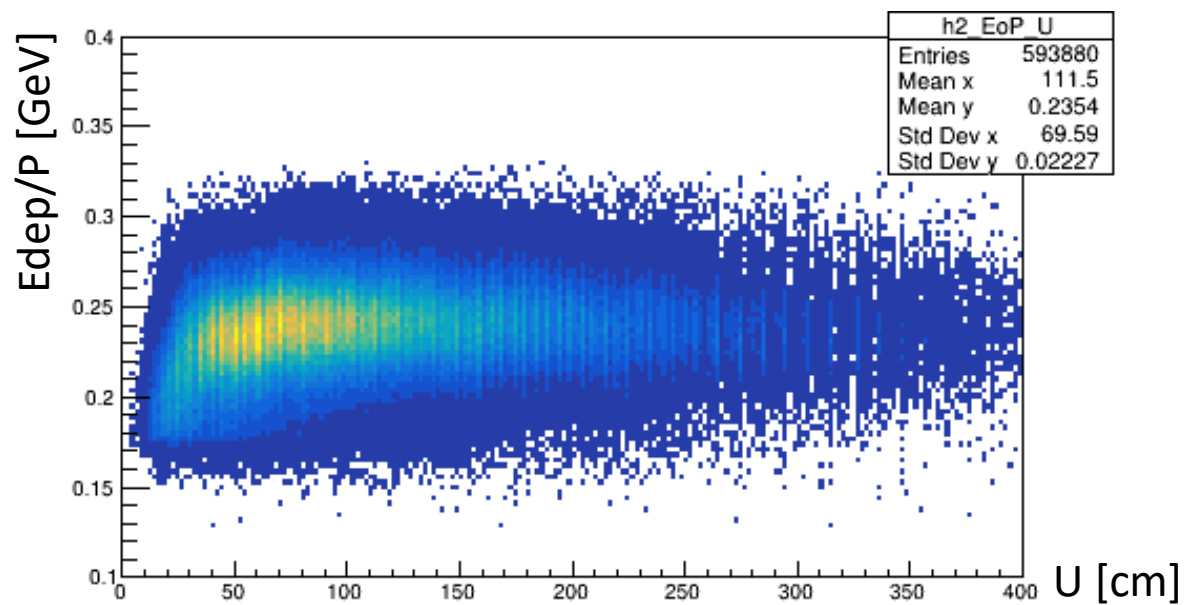
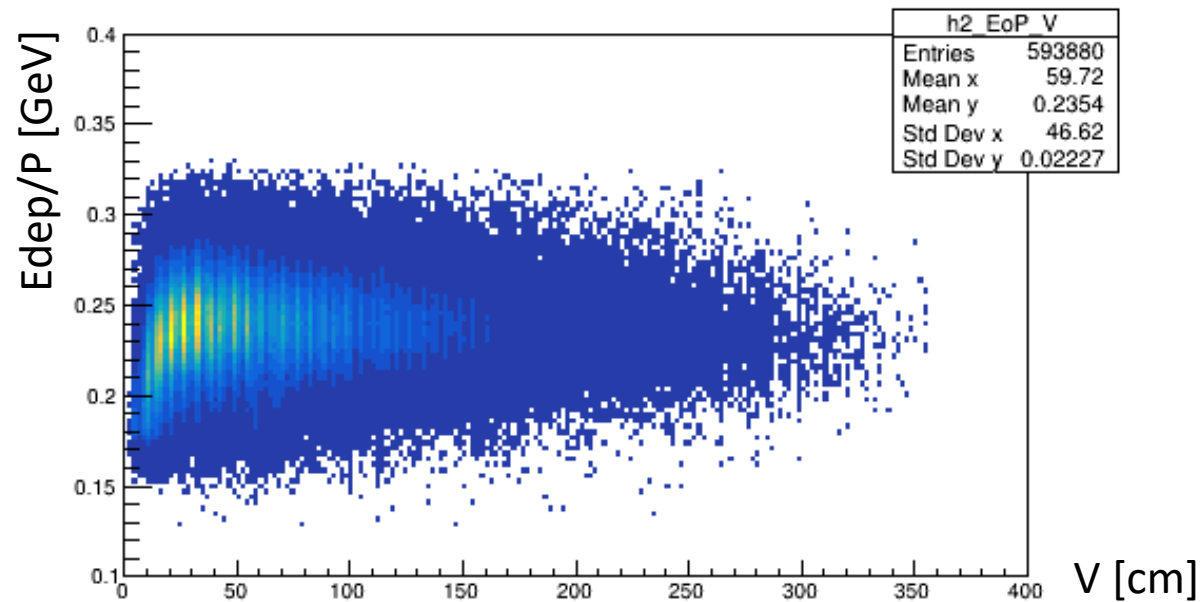
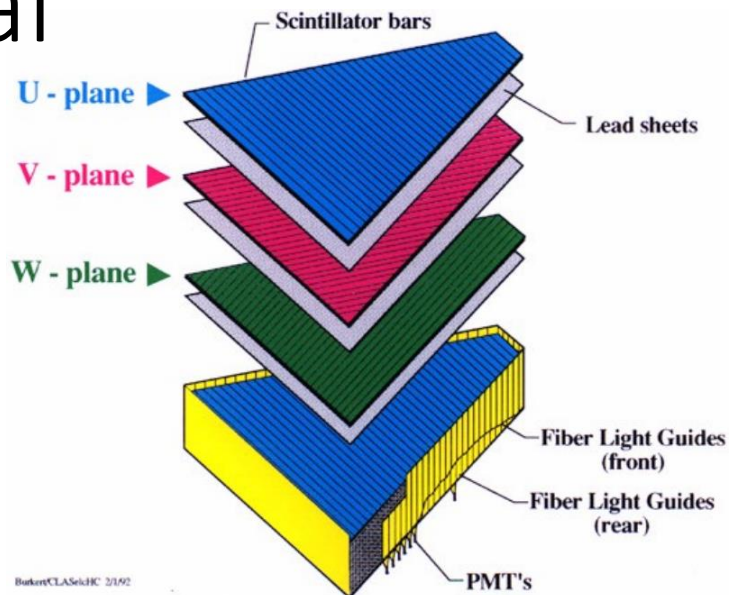
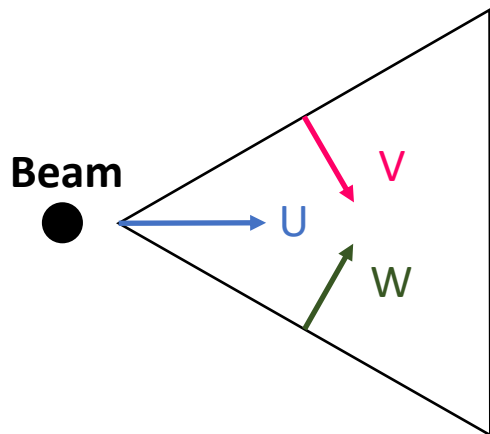


DC Fiducial Cuts

Region 1 (Pi-)

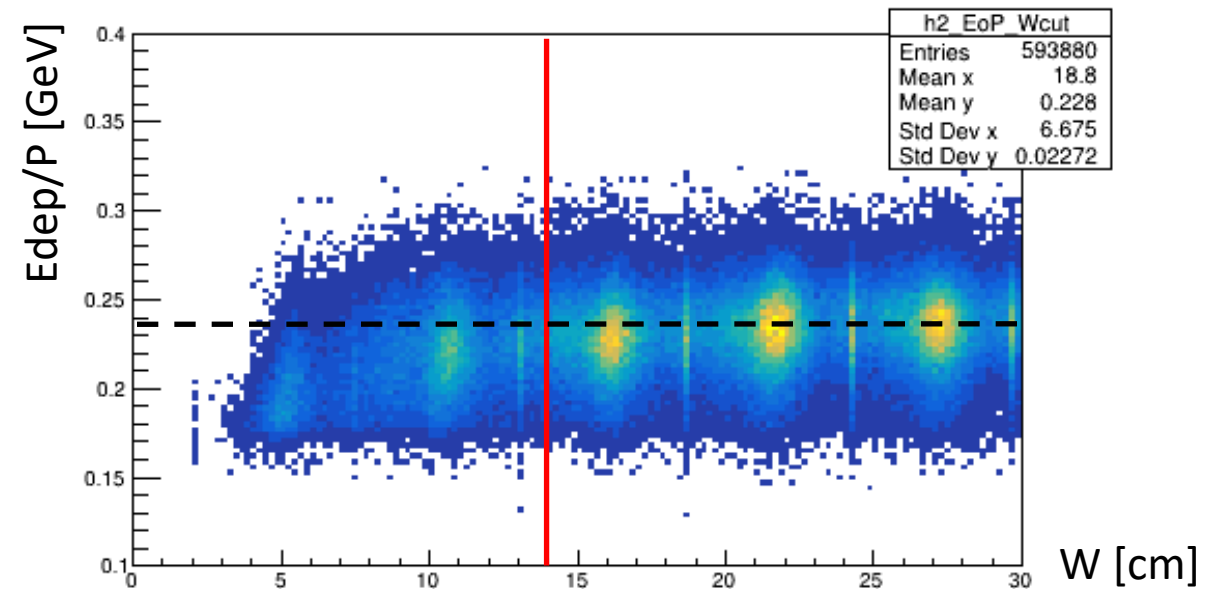
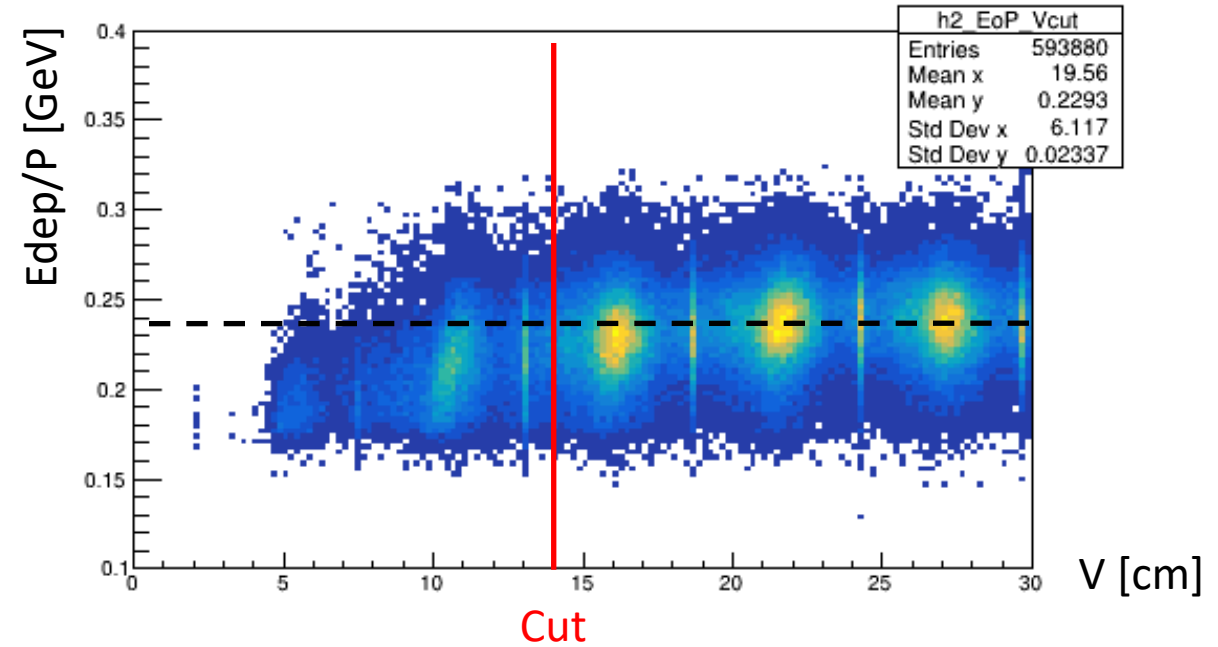
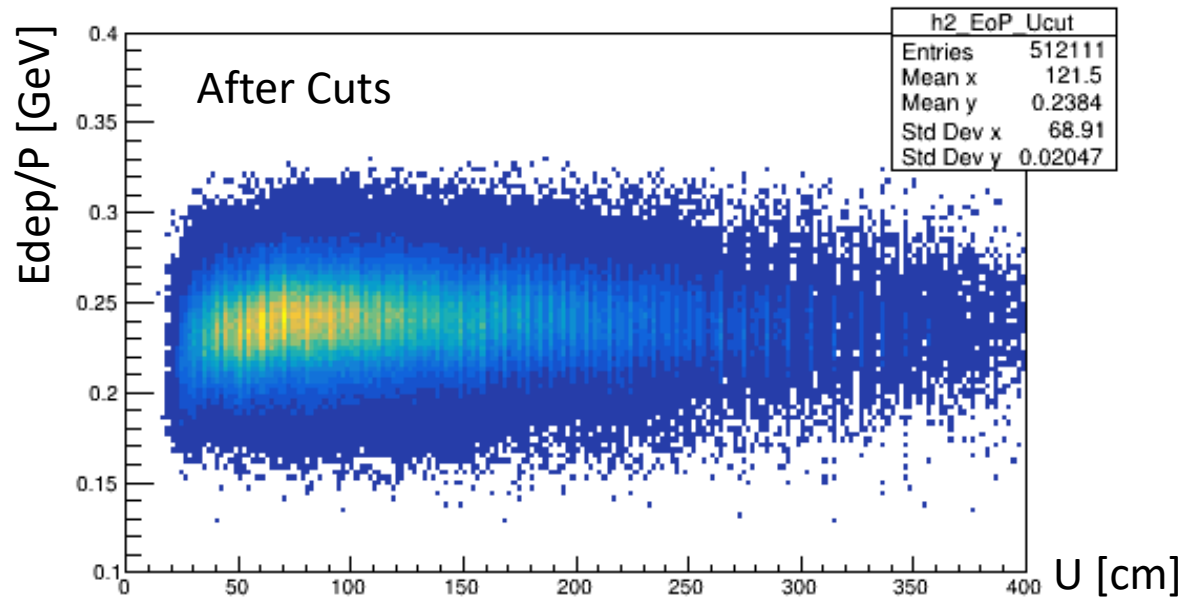


EC Fiducial Cuts



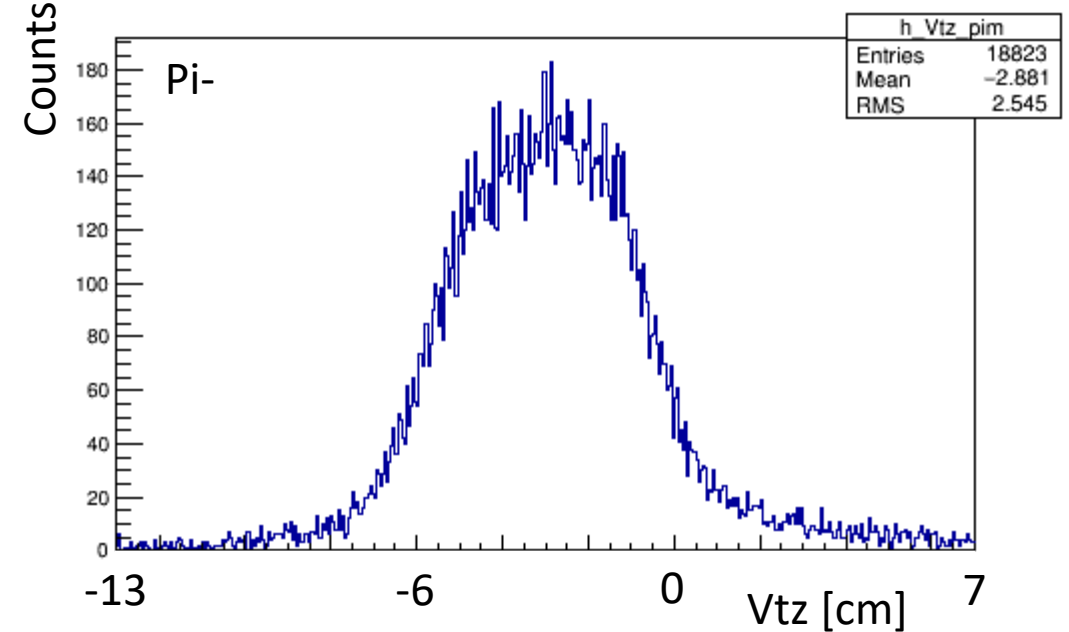
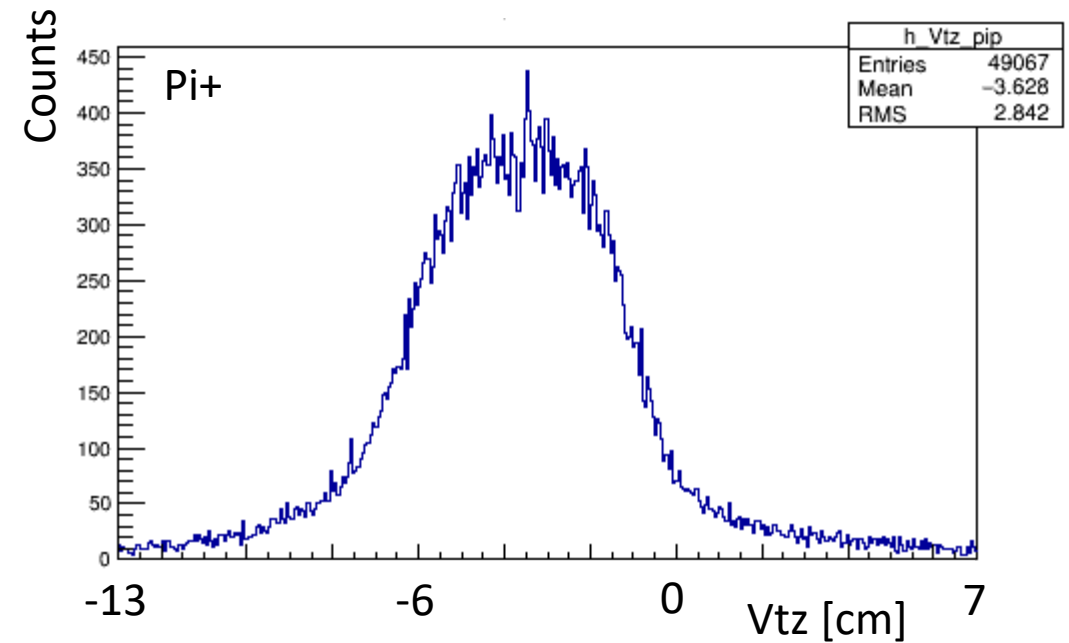
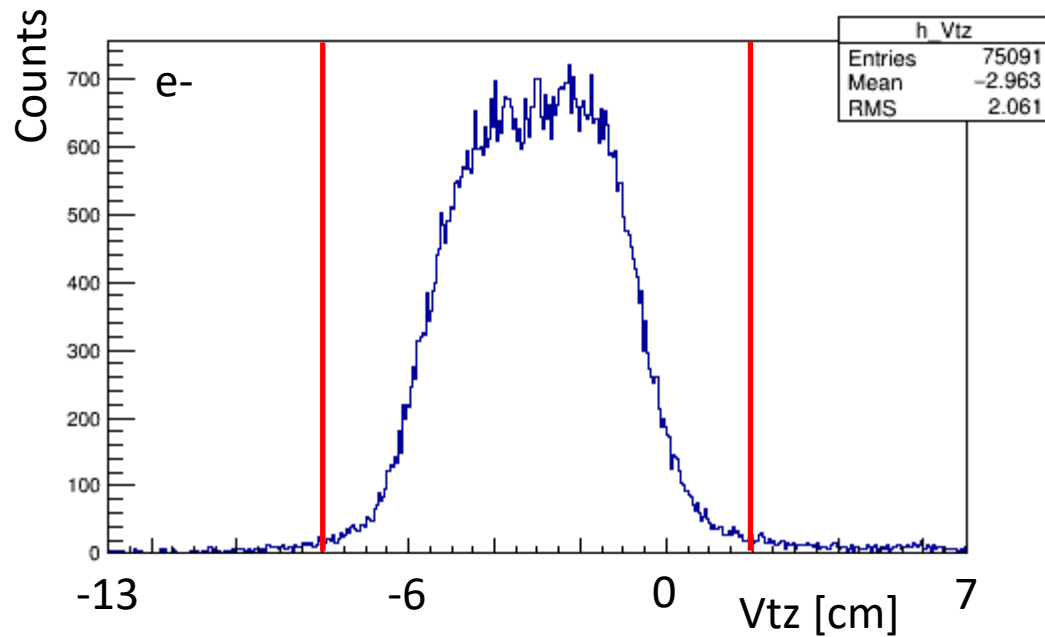
EC Fiducial Cuts

Required $V, W > 14$ cm (removed outer 2 bars)

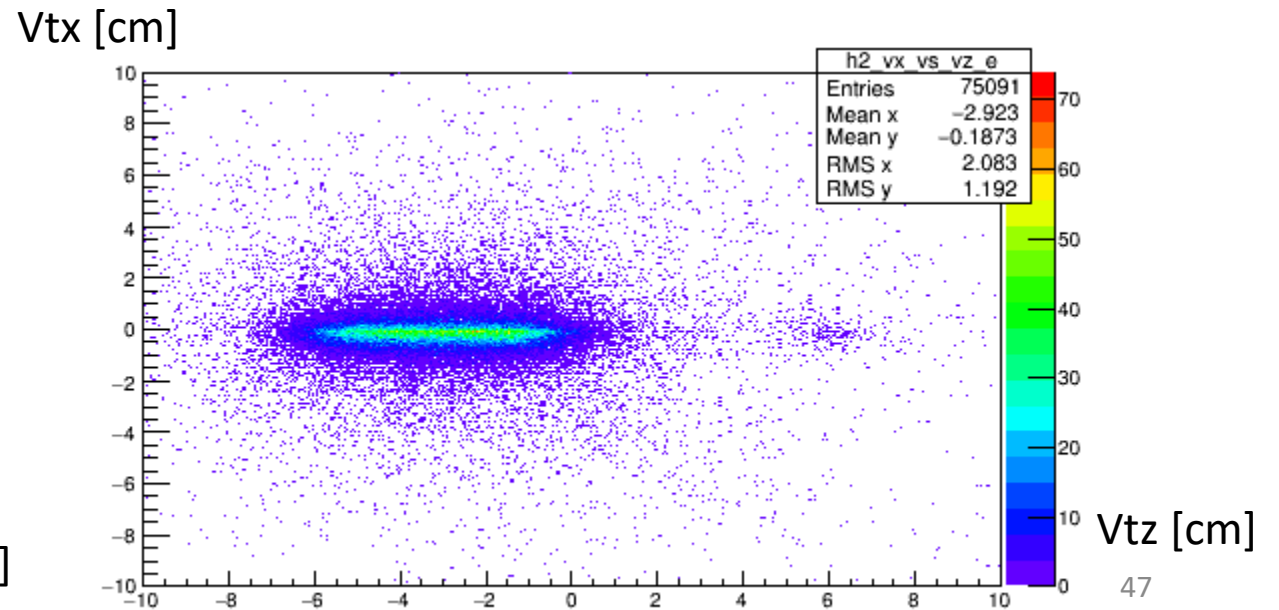
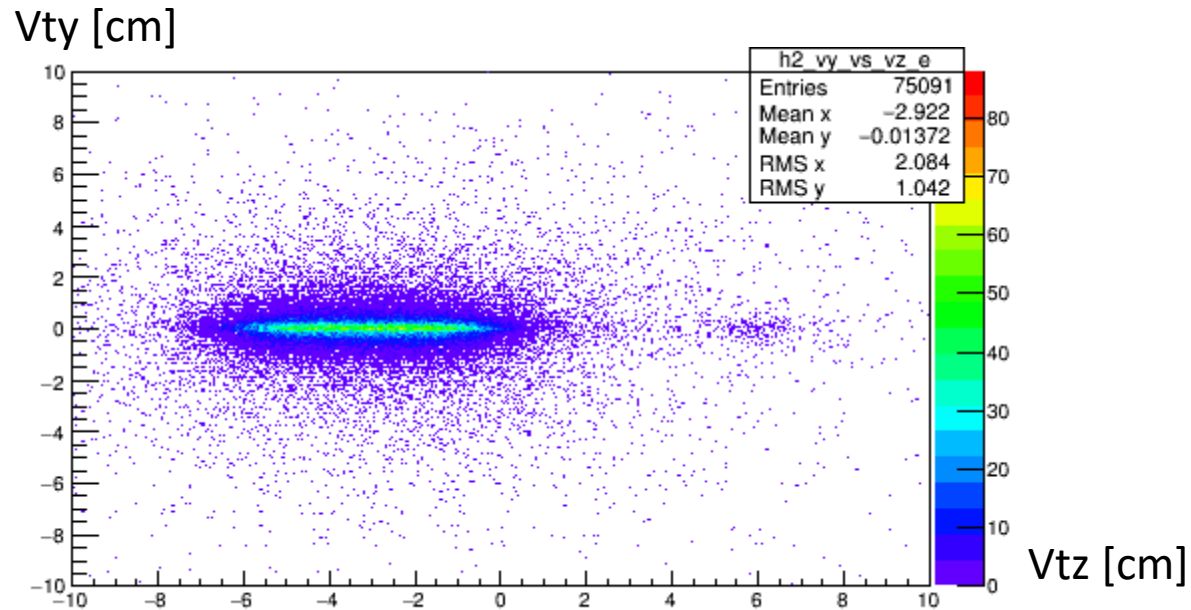
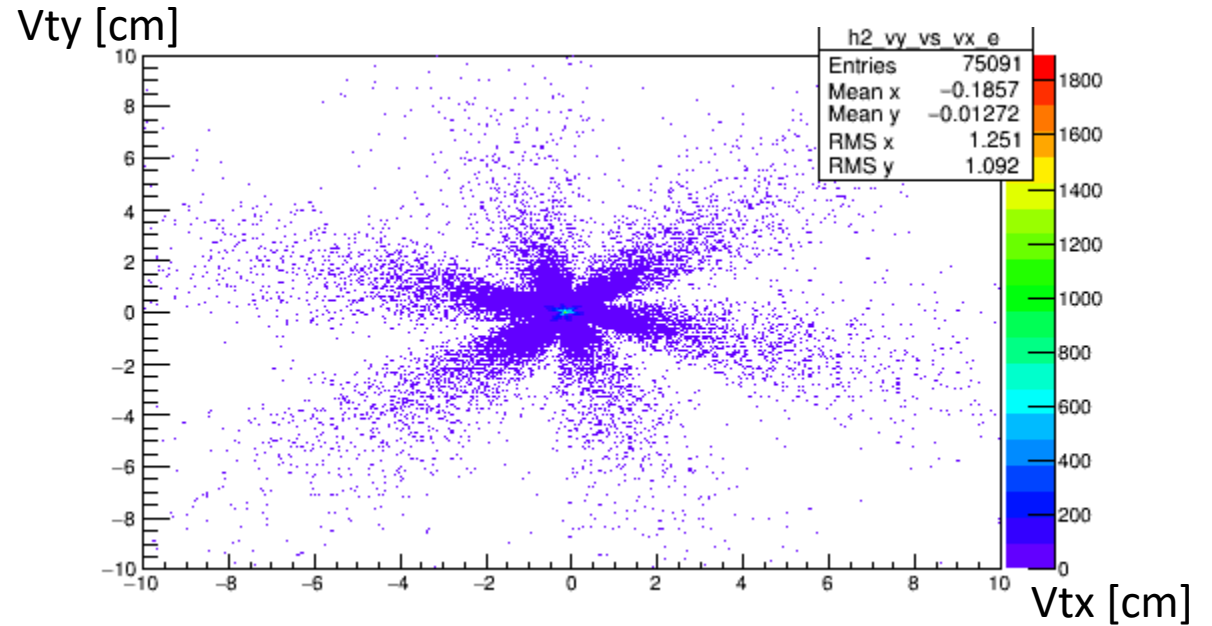
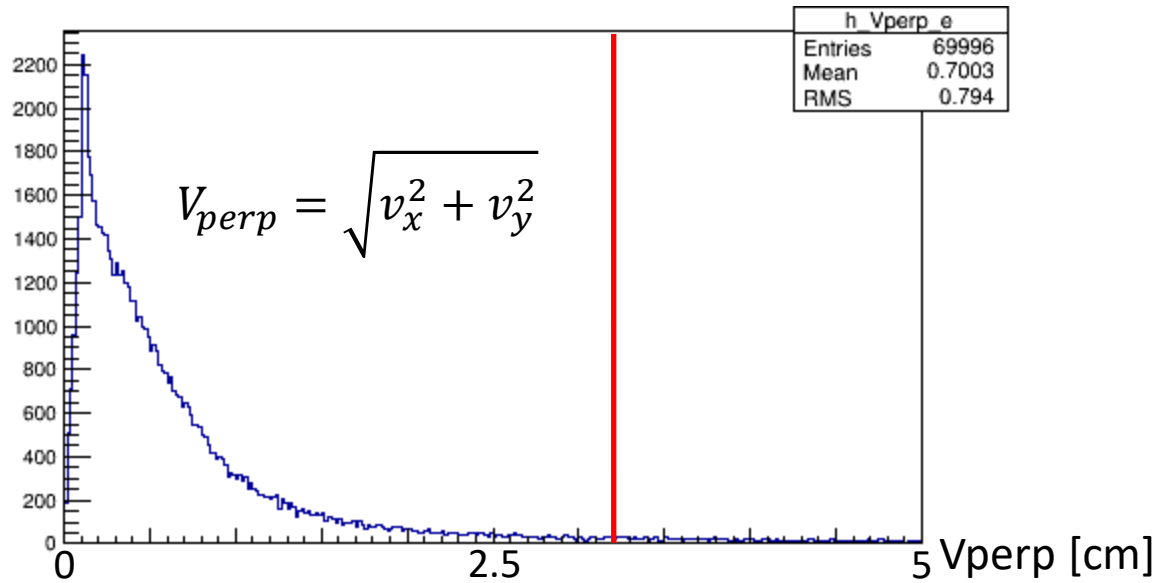


Electron and Pion z Vertices

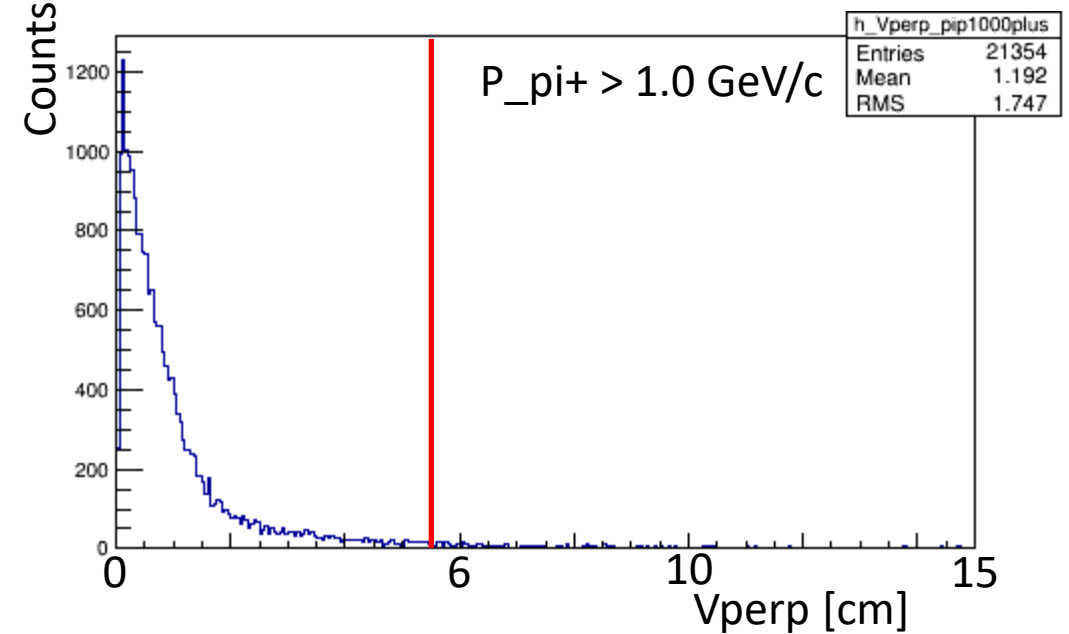
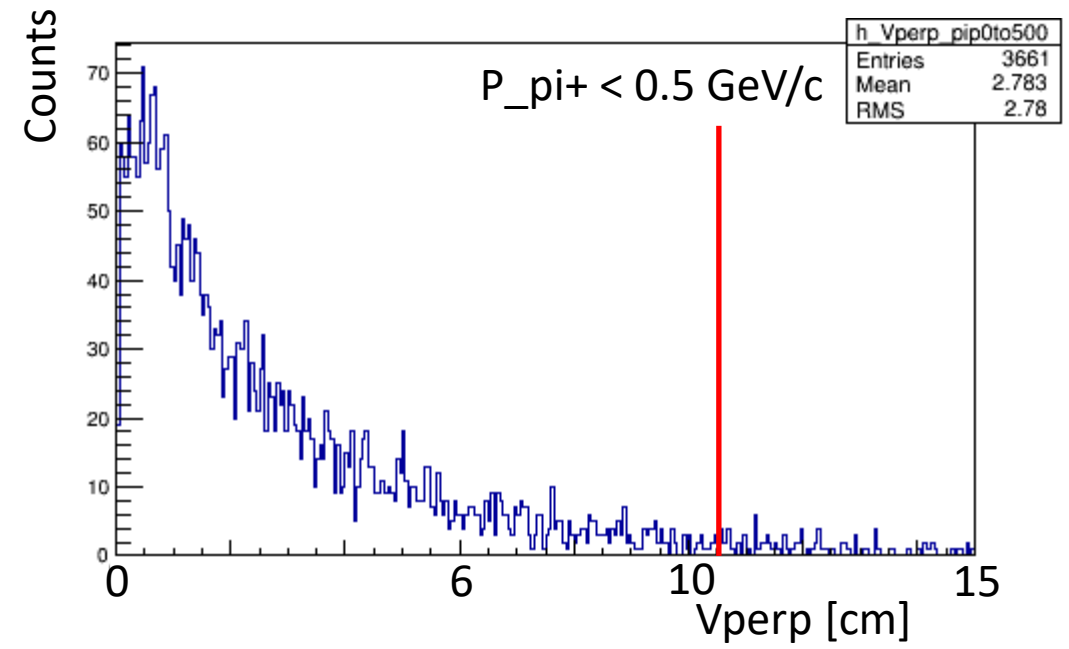
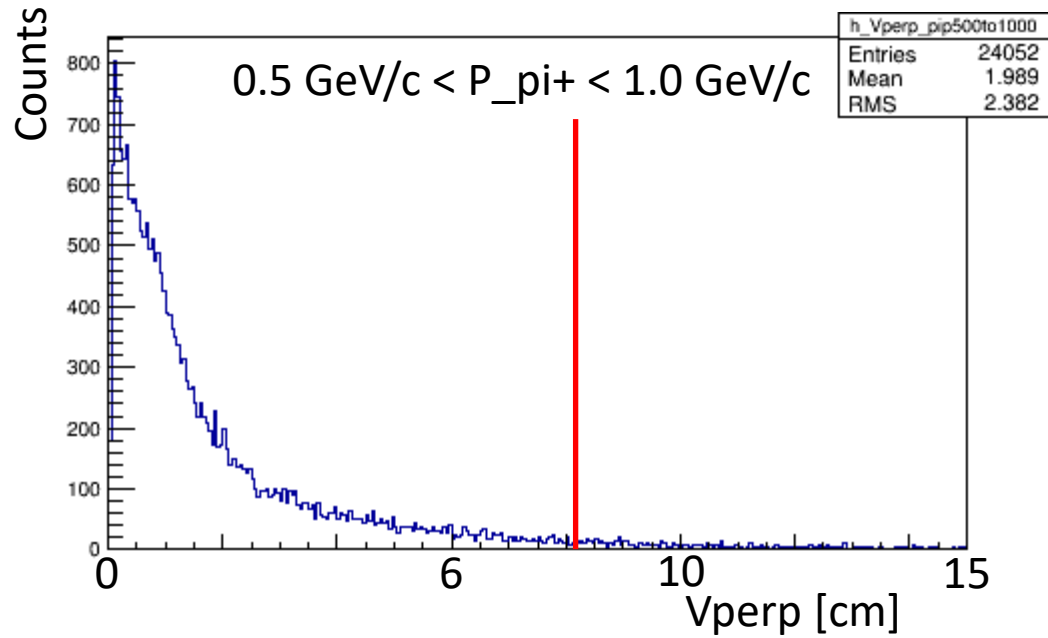
$$-8 \text{ cm} < Vtz_e < 2 \text{ cm}$$



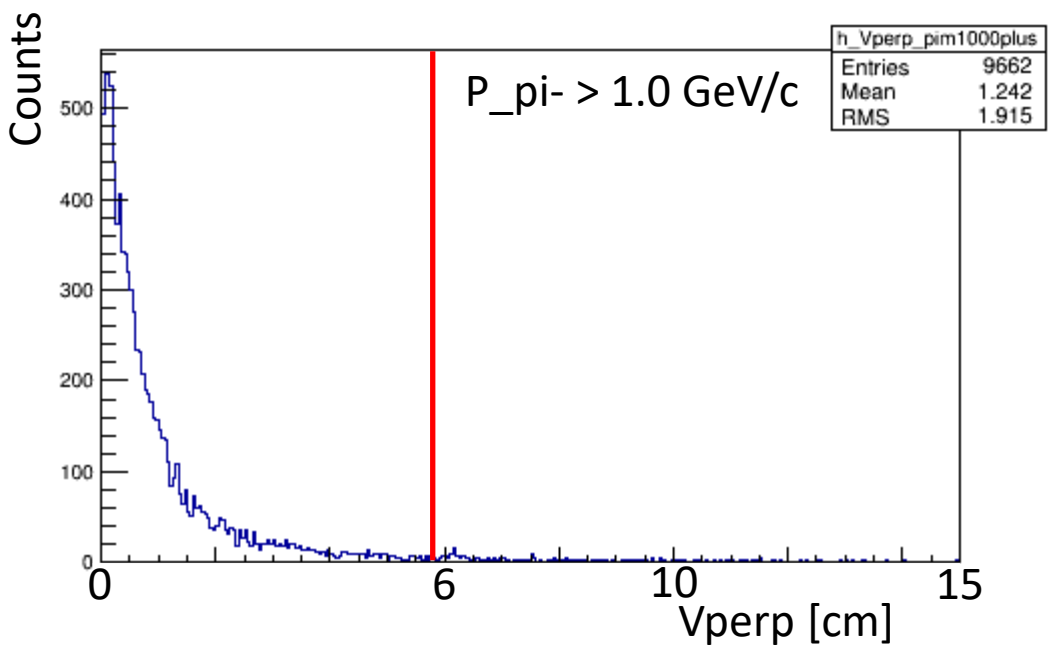
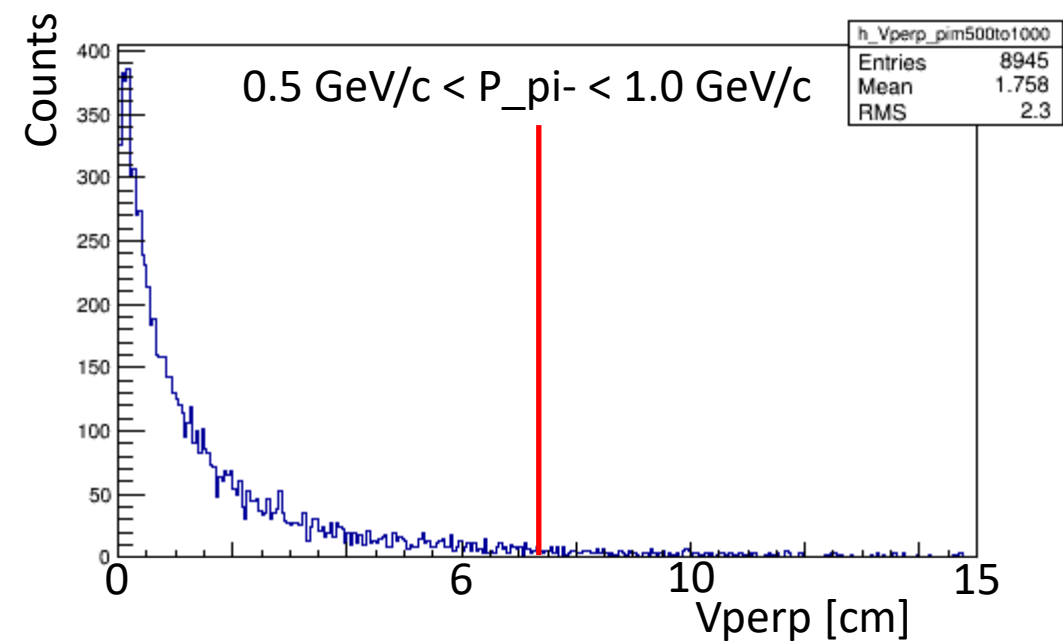
Electron Perpendicular Vertices



Pi+ Perpendicular Vertices



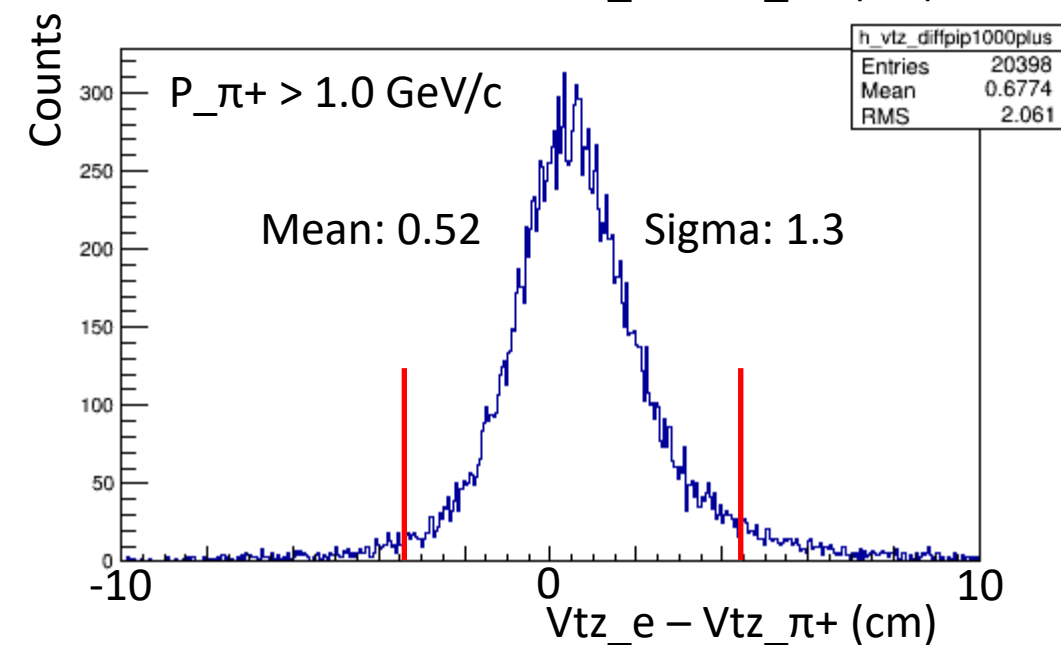
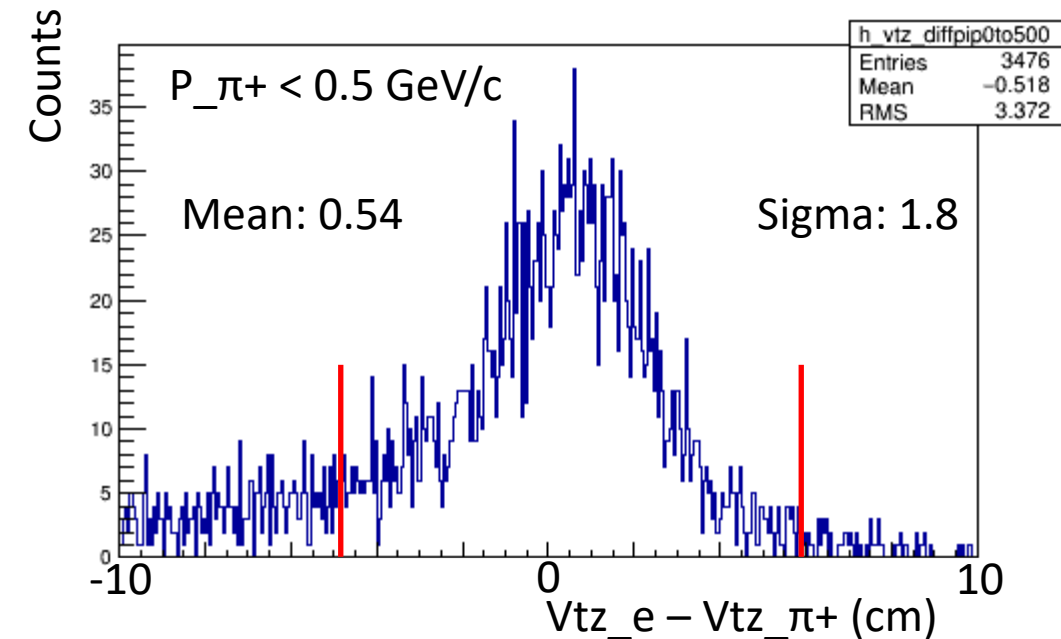
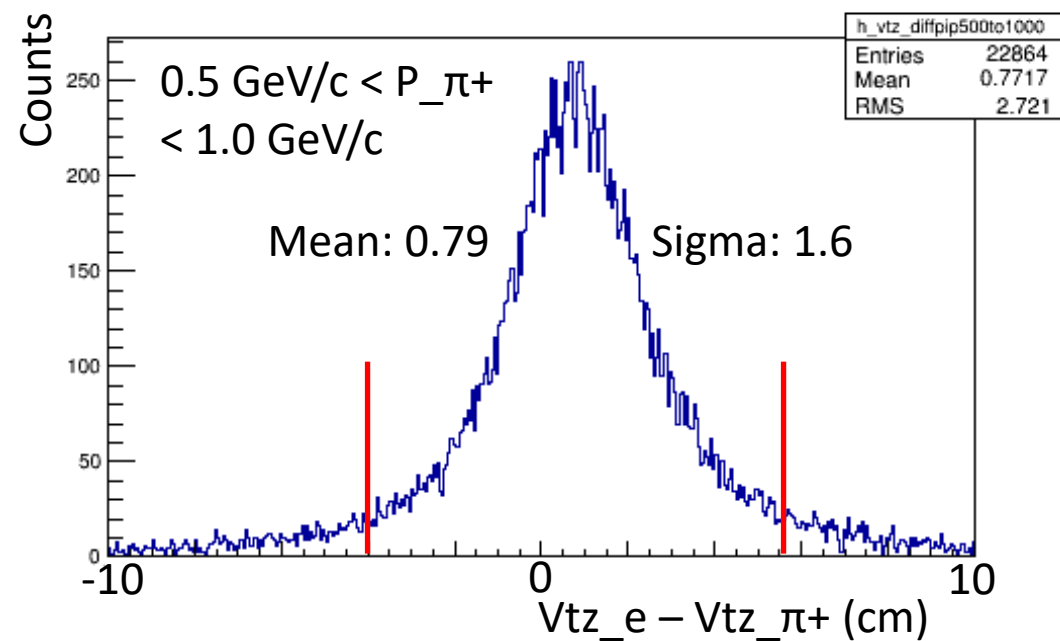
Pi- Perpendicular Vertices



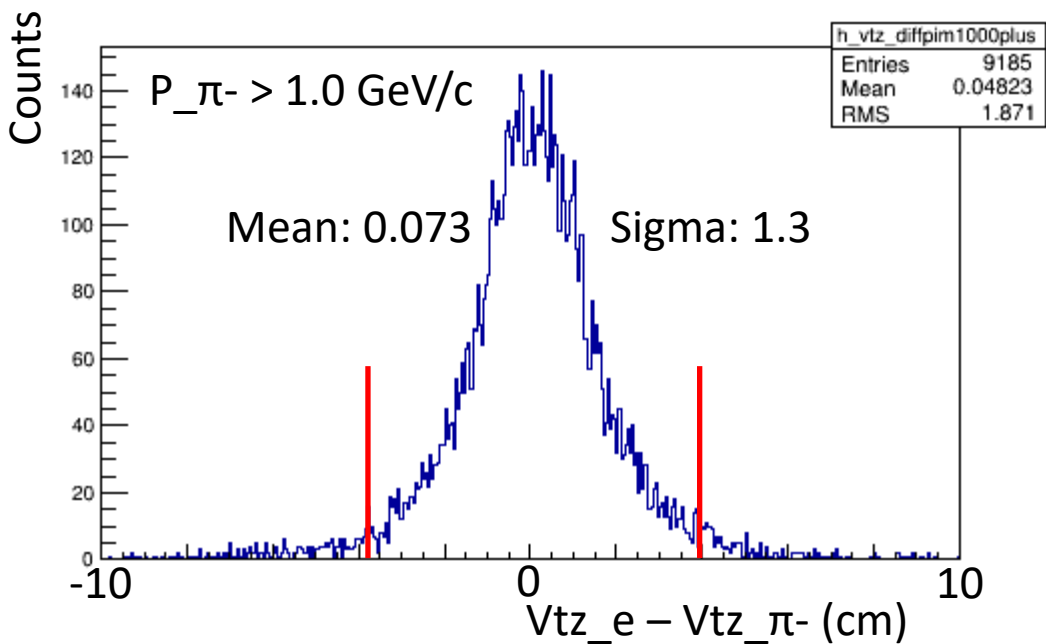
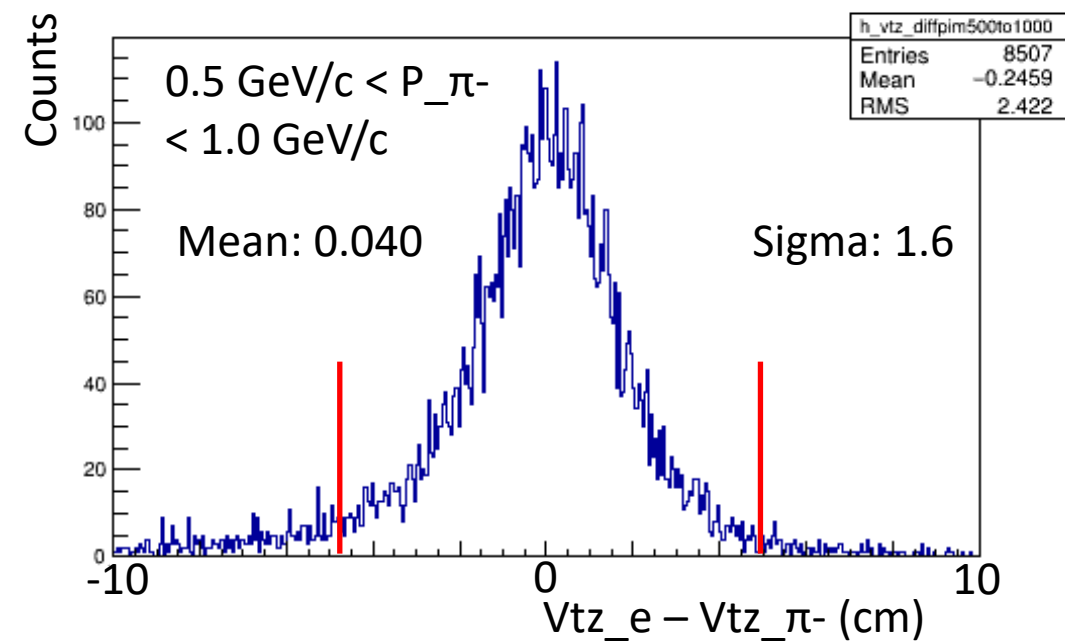
Vertex Z Difference (Electron – Pi+)

Fitted with gaussian

Cut = mean $\pm$ 3 * σ



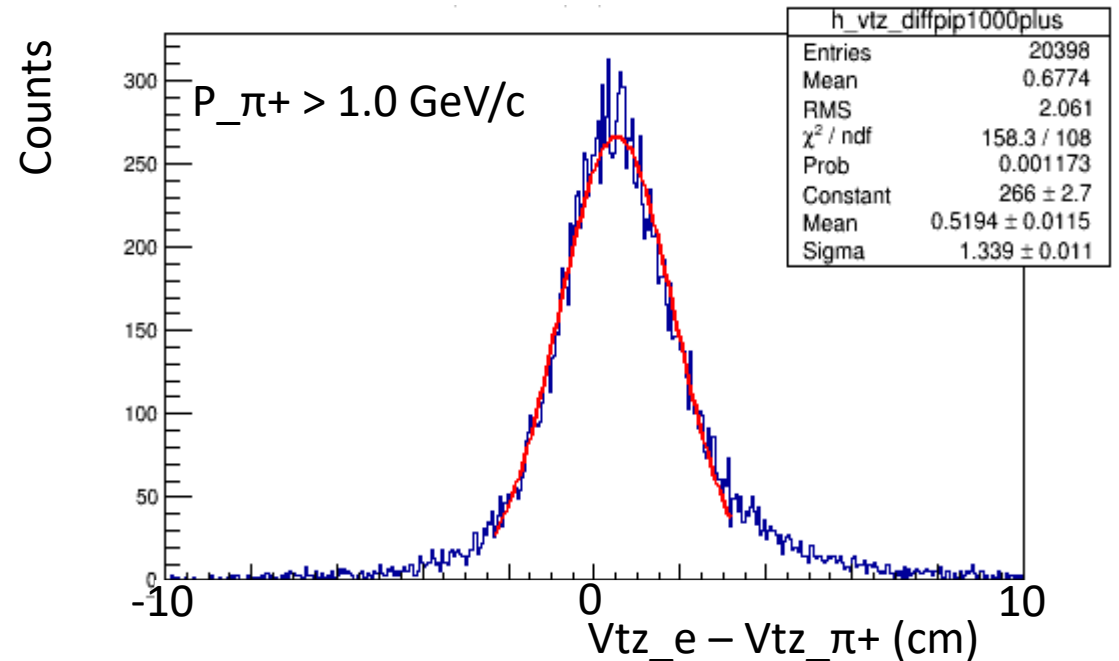
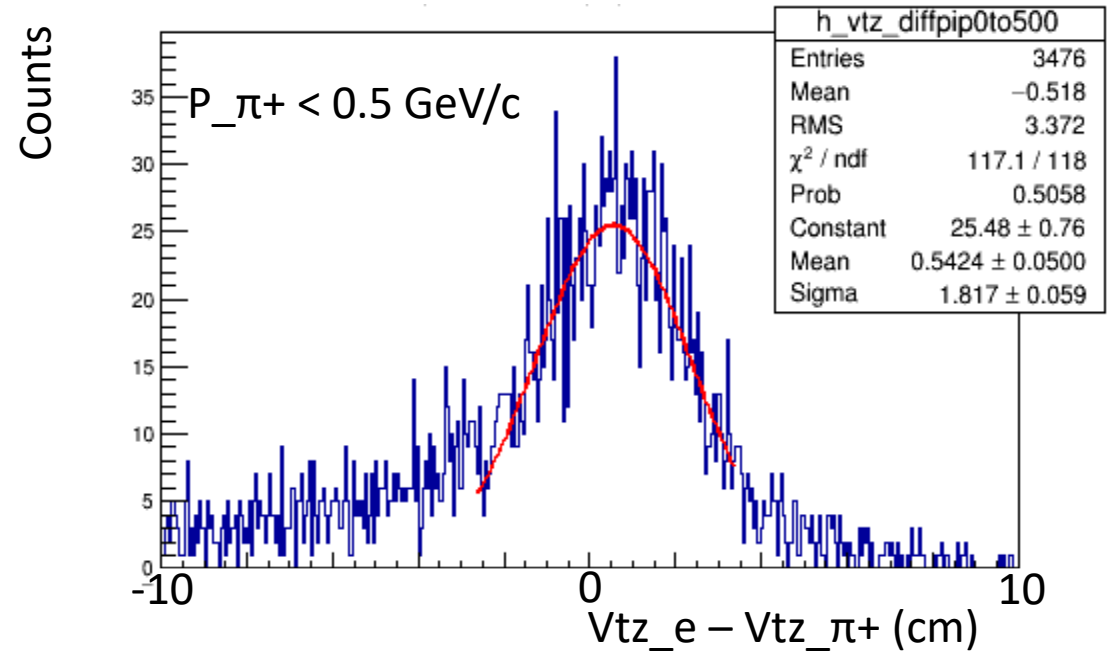
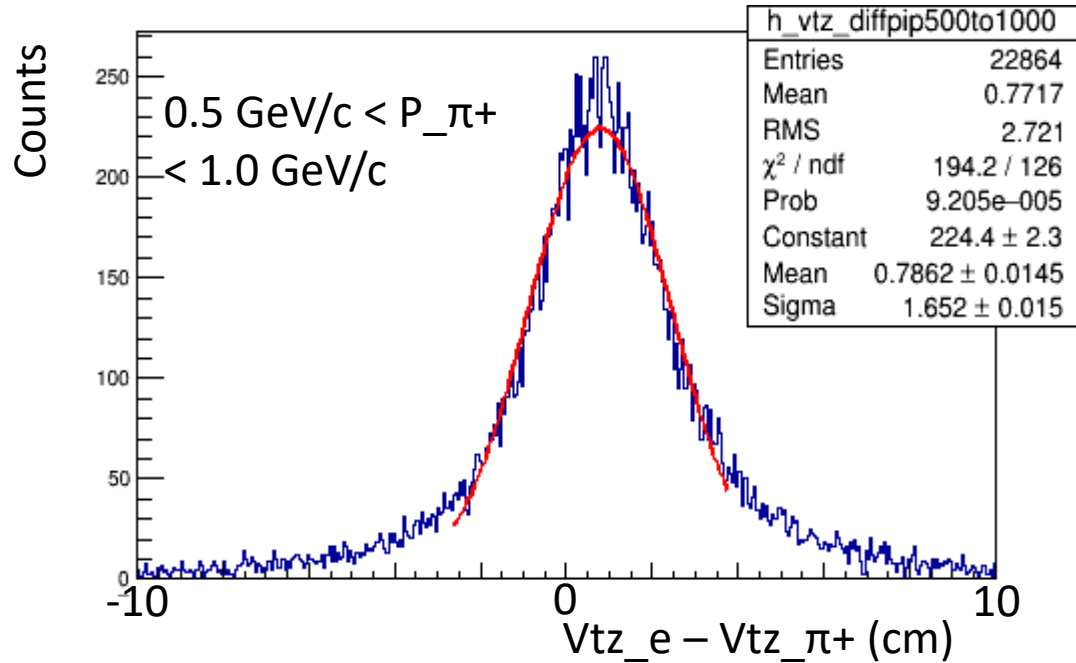
Vertex Z Difference (Electron – Pi-)



Vertex Z Difference (Electron – Pi+)

Fitted with gaussian

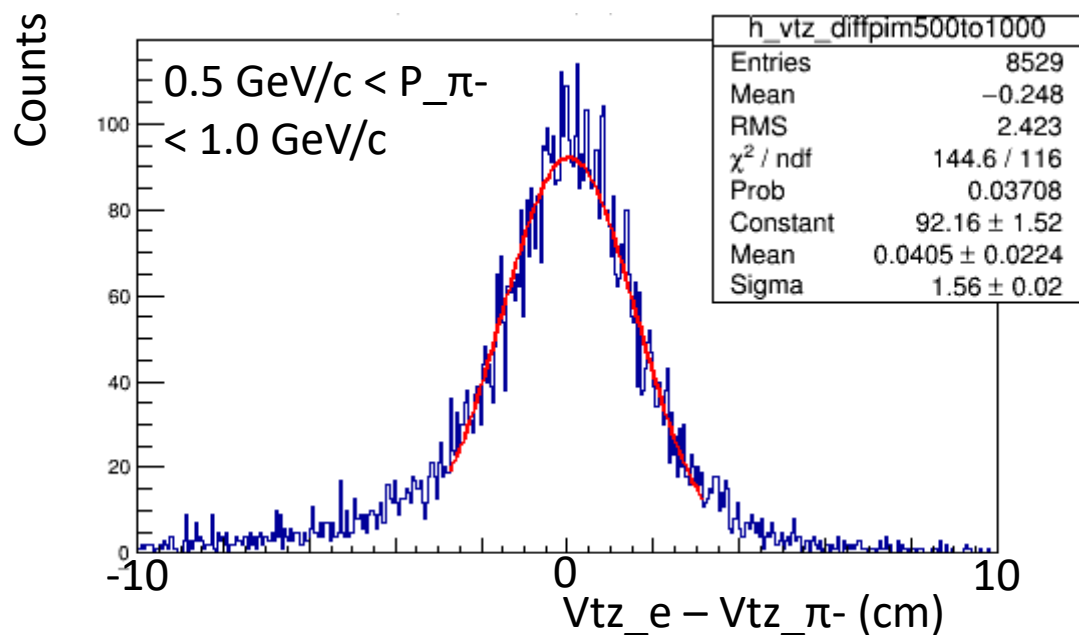
Cut = mean $\pm$ 3 * σ



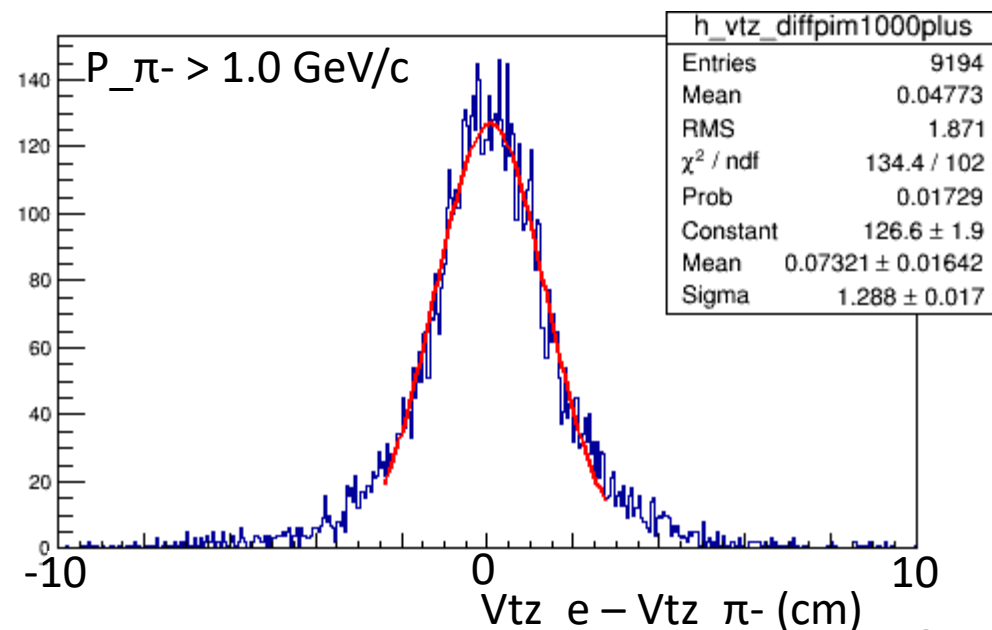
Vertex Z Difference (Electron – Pi-)

Fitted with gaussian

Cut = mean $\pm$ 3 * σ



Counts



Run Selection

Number of Trigger Electrons / Faraday Cup Charge



About 5 M $d(e,e'\pi^\pm)$ events after cuts

Sector $d(e,e'\pi^\pm)$ cross section issues after cuts

D(e,e'pi) Cross Sections

$$N_{events} = \frac{d^6\sigma}{d\Omega_E d\Omega_\pi dE' dT_\pi} \Delta\Omega_E \Delta\Omega_\pi \Delta E' \Delta T_\pi * N_e t_{tgt} * \text{correction factors}$$

What we want

$$N_{events} = \frac{d^2\sigma}{dW dT_\pi} \Delta W \Delta T_\pi * N_e t_{tgt} * \text{correction factors}$$

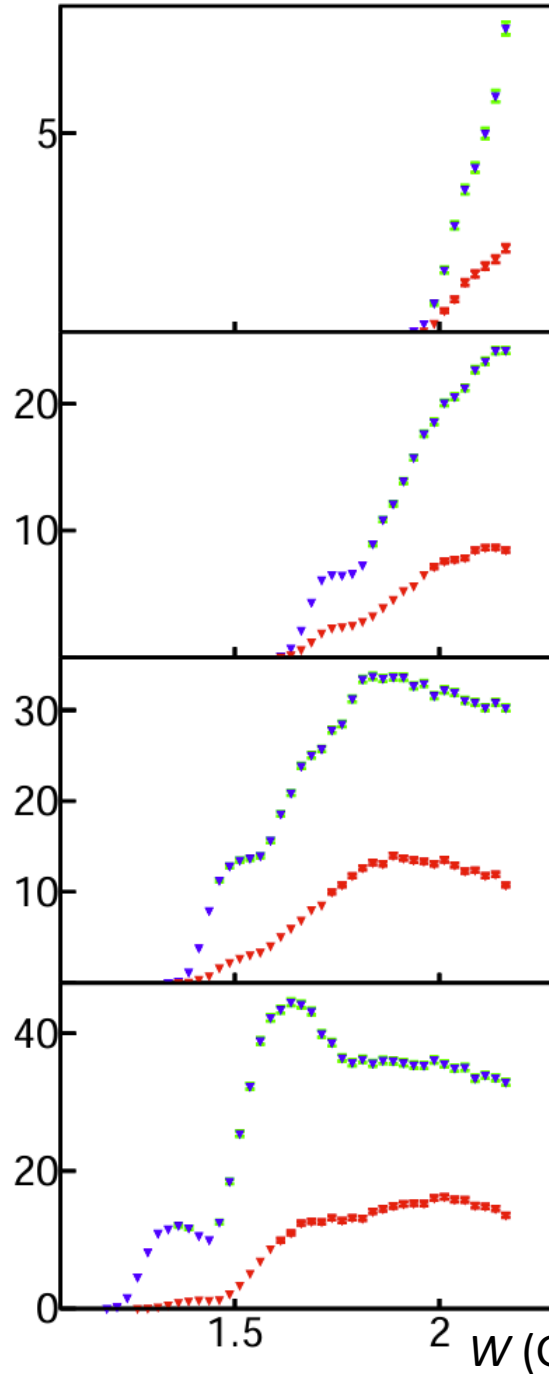
$$\frac{d^2\sigma}{d\omega dT_\pi} = \frac{N_{events}}{\Delta W \Delta T_\pi L} * \text{corr. factors}$$

Our formula

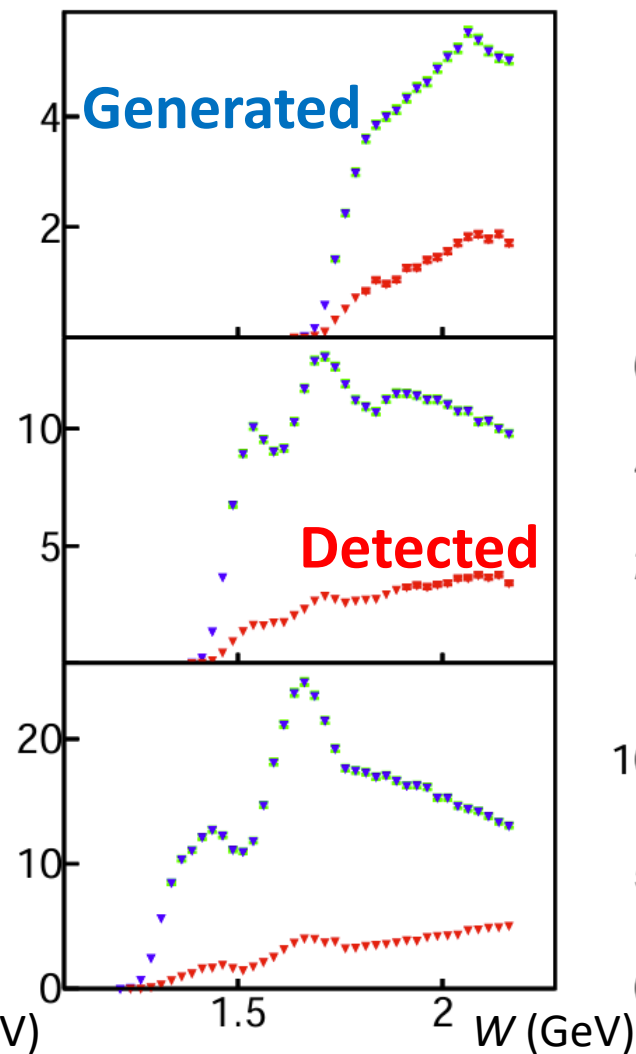
$$L = N_e * t_{tgt} \qquad N_e = \frac{Q_{tot}}{q_e} \qquad t_{tgt} = \frac{\rho_{tgt} l_{tgt} N_A}{mol_{tgt}}$$

Higher P_π

GENIE Nonradiative Cross Sections



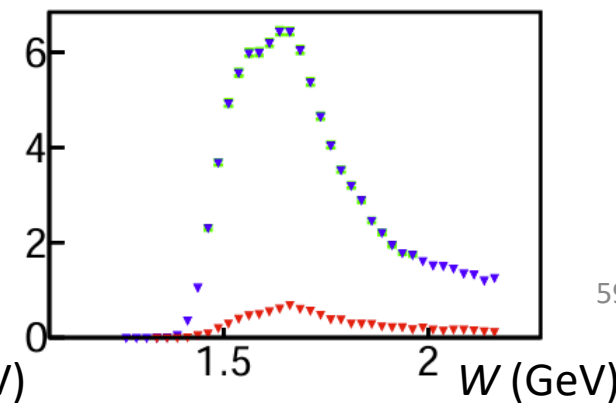
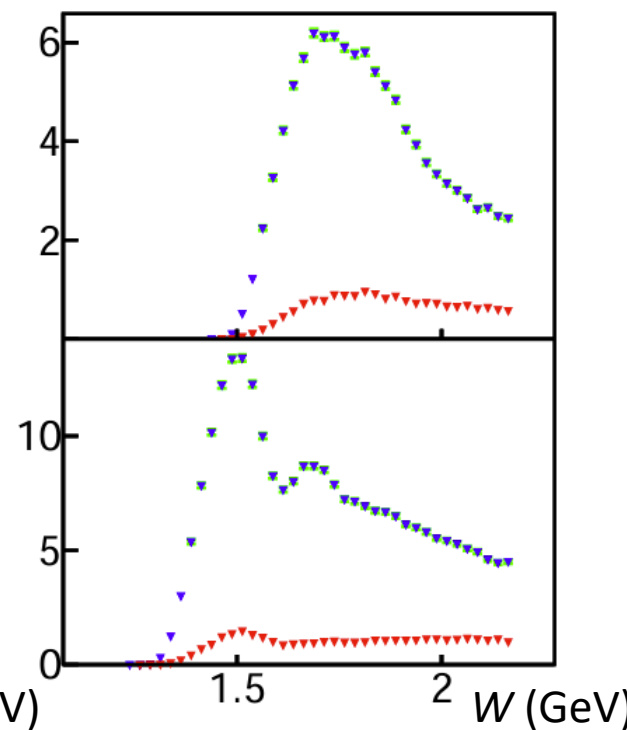
$$d(e, e' \pi^+)$$
$$1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$



Acceptance Corrections

Bin migration included in correction

Corrections applied point-to-point

Higher $\theta_{\pi q}$

Higher P_π

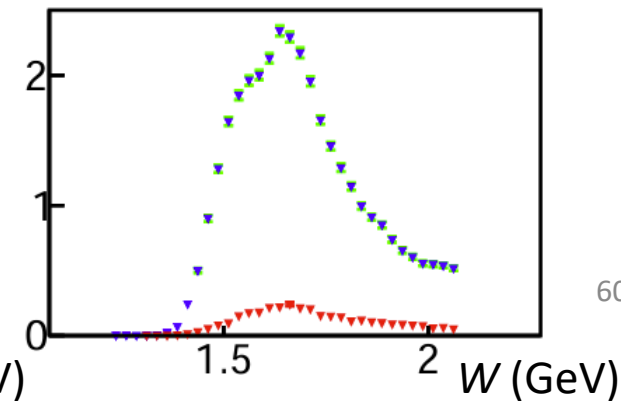
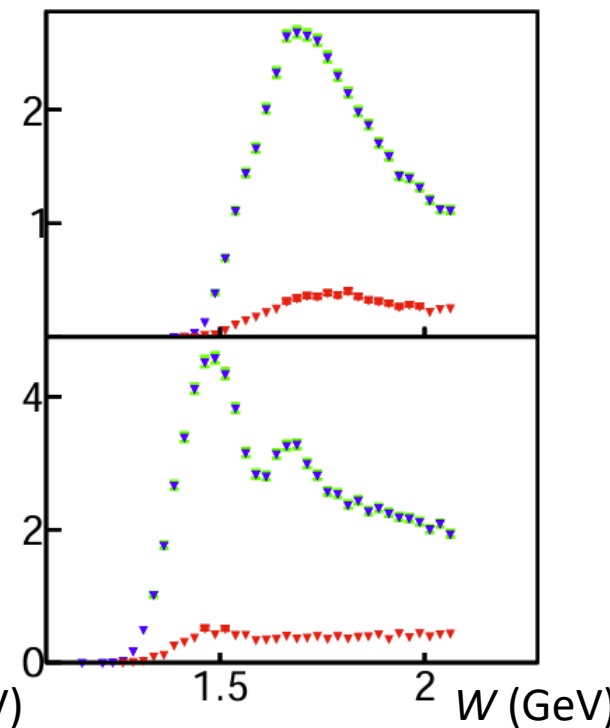
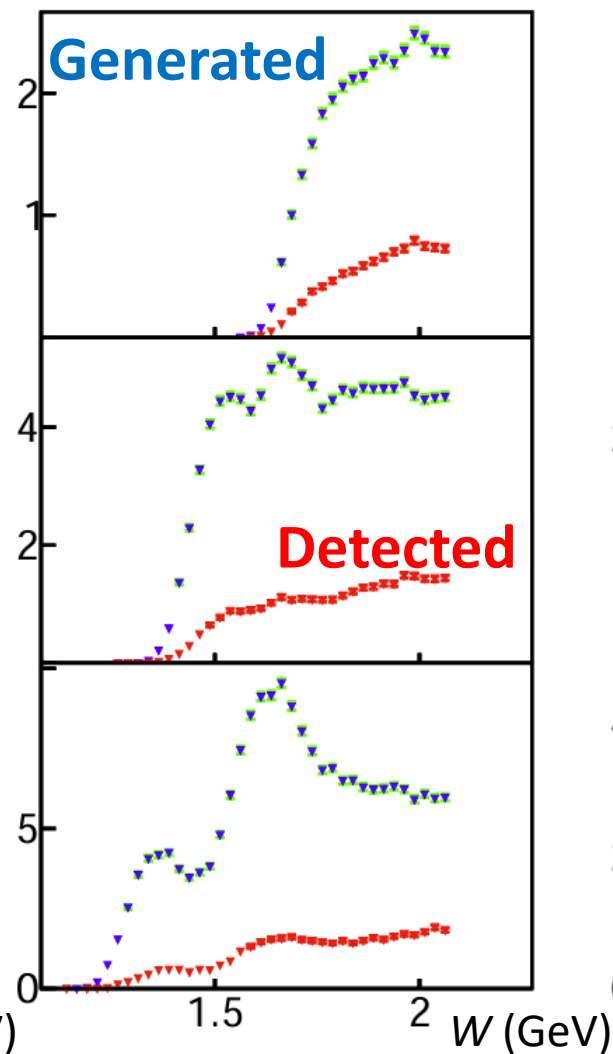
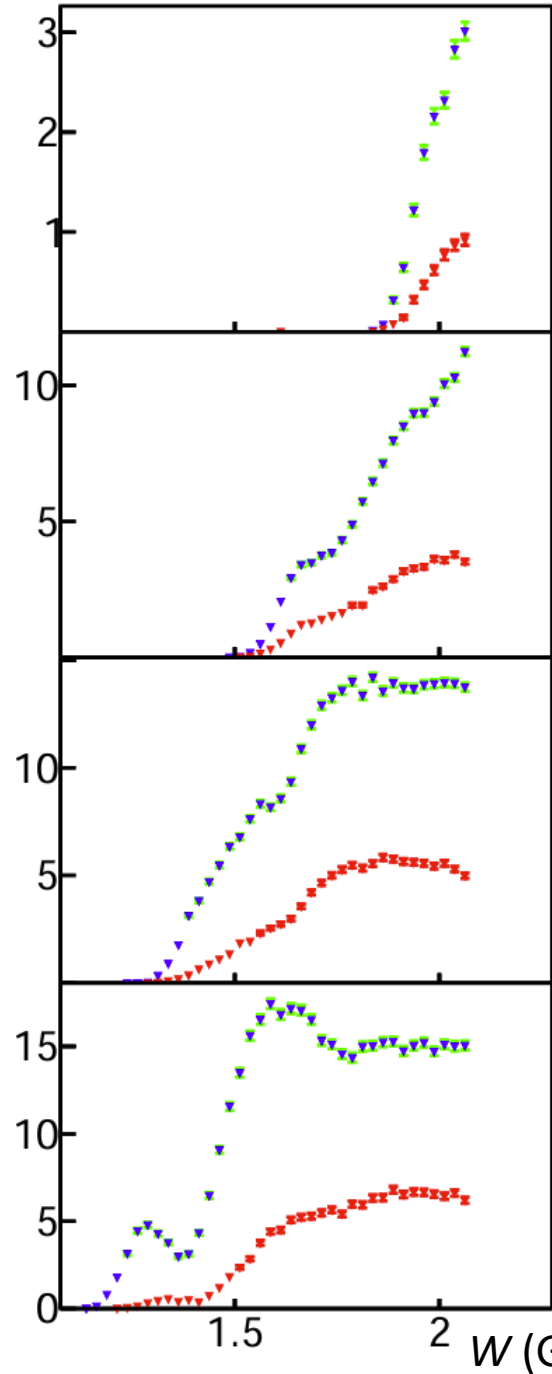
GENIE Nonradiative Cross Sections

$$d(e, e' \pi^+)$$
$$1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied point-to-point

Higher $\theta_{\pi q}$

Higher P_π

GENIE Nonradiative Cross Sections

$$d(e, e' \pi^+)$$
$$1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied point-to-point

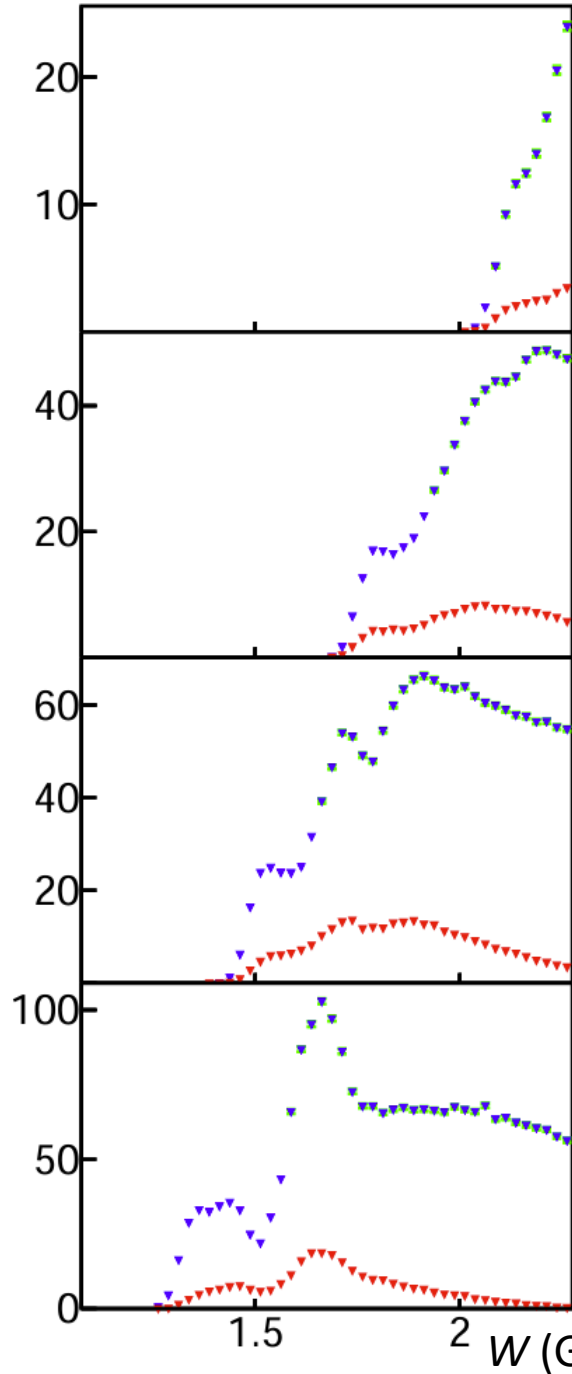
Generated

Detected

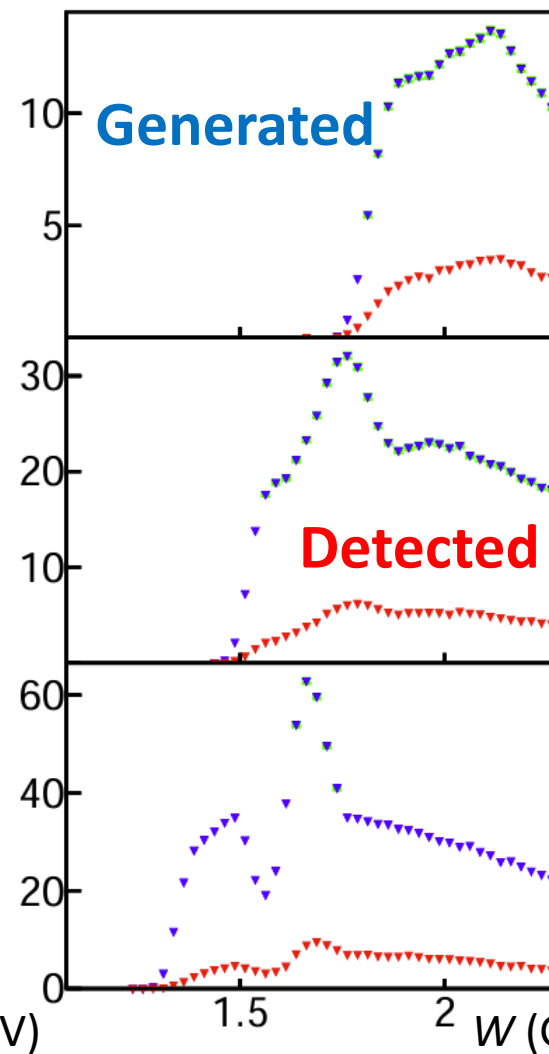
Higher $\theta_{\pi q}$

Higher P_π

GENIE Nonradiative Cross Sections



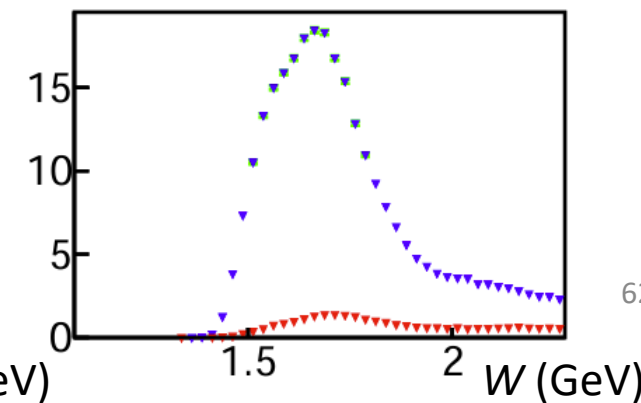
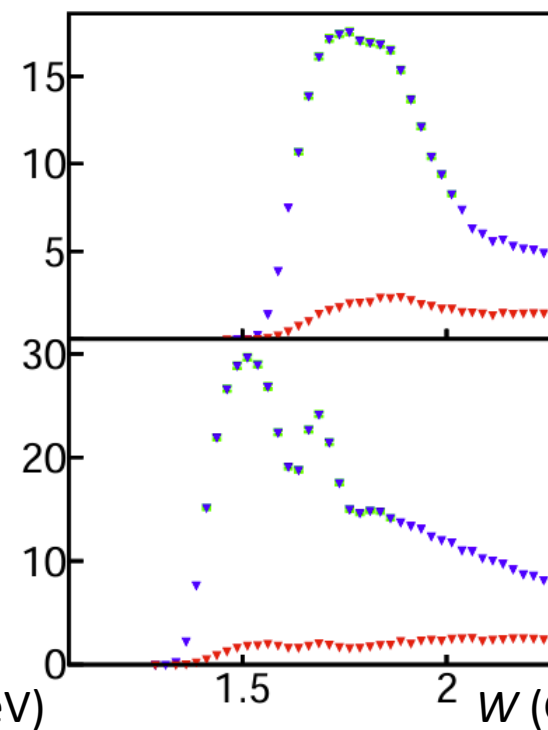
$$d(e, e' \pi^-)$$
$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$



Acceptance Corrections

Bin migration included in correction

Corrections applied point-to-point

Higher $\theta_{\pi q}$

Higher P_π

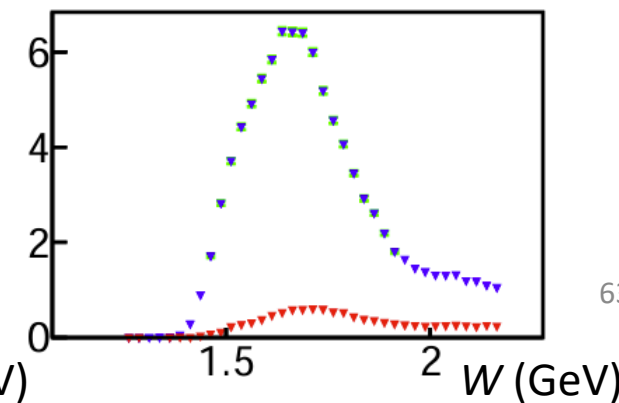
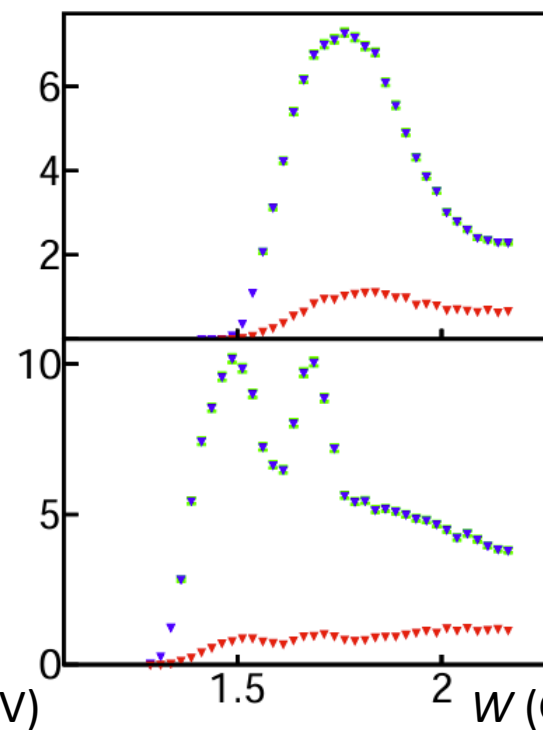
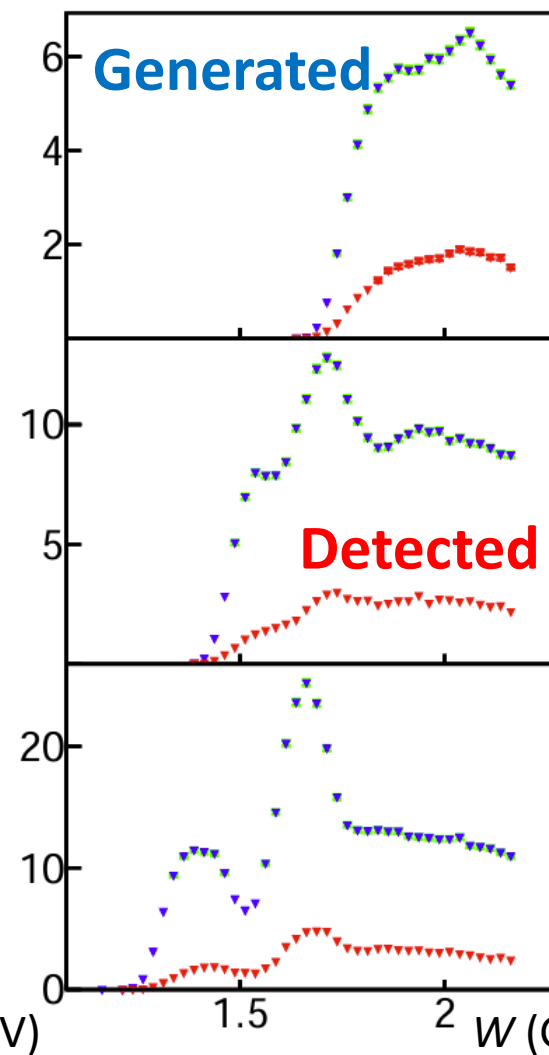
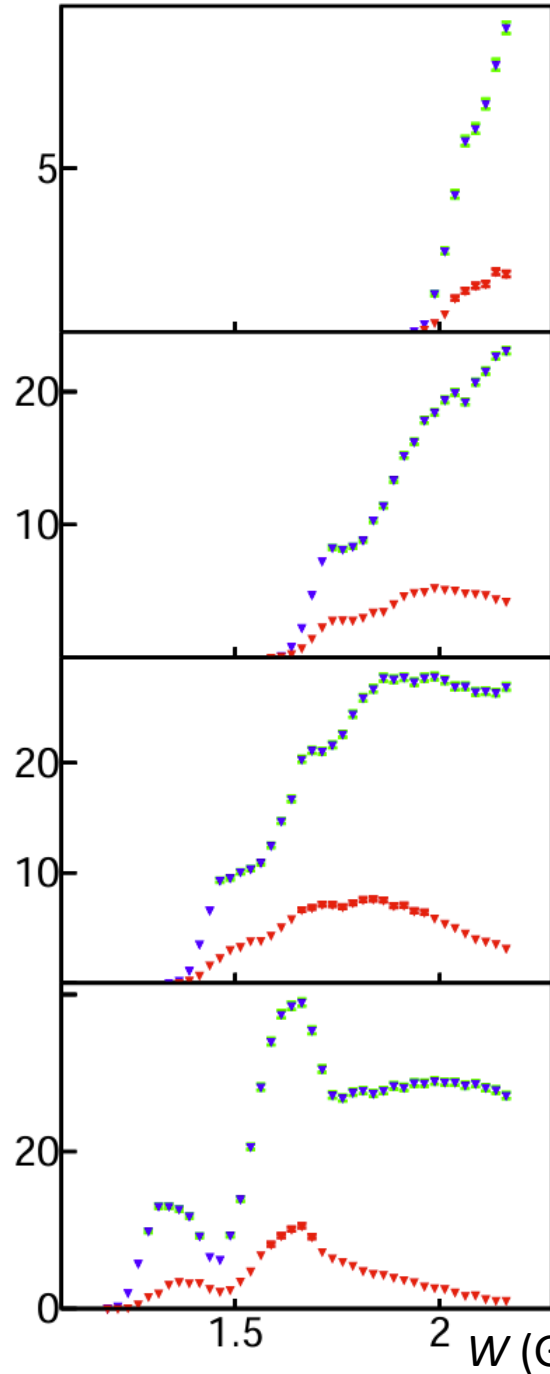
GENIE Nonradiative Cross Sections

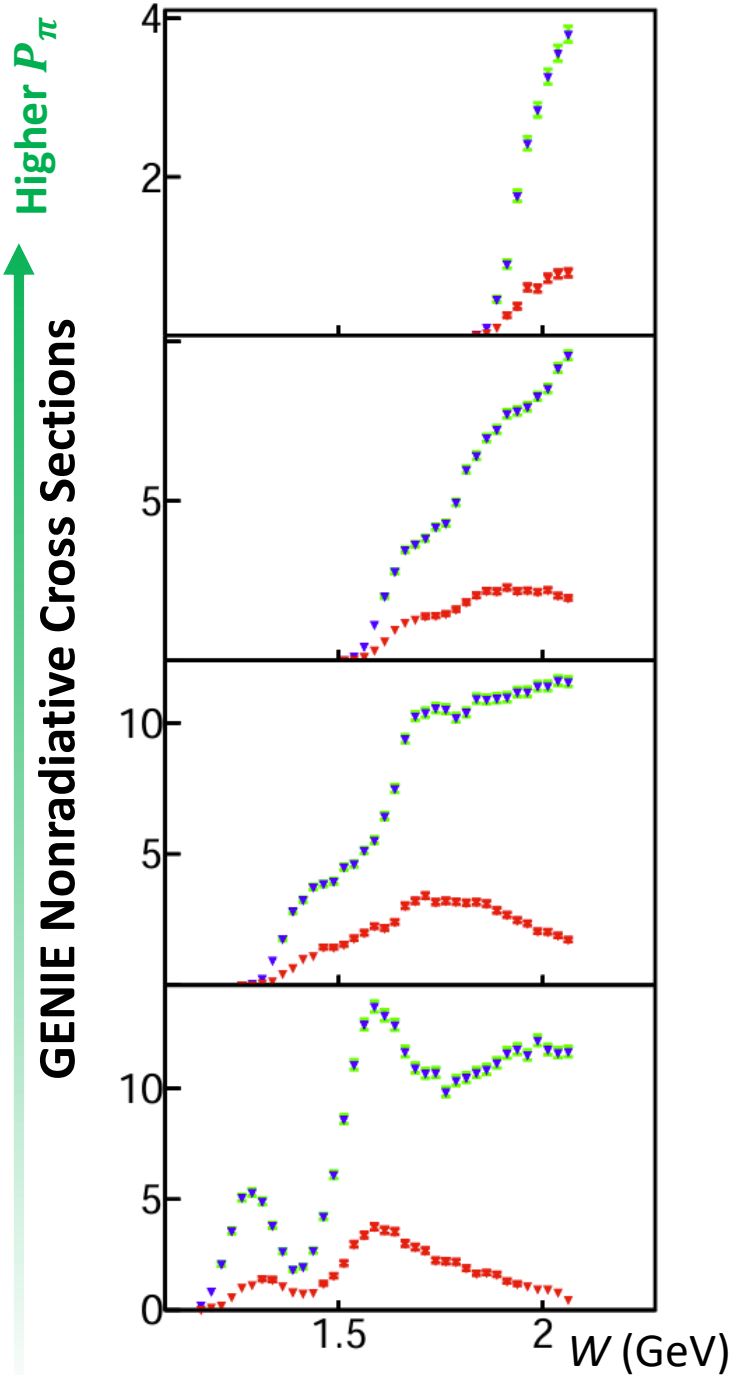
$$d(e, e' \pi^-)$$
$$1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

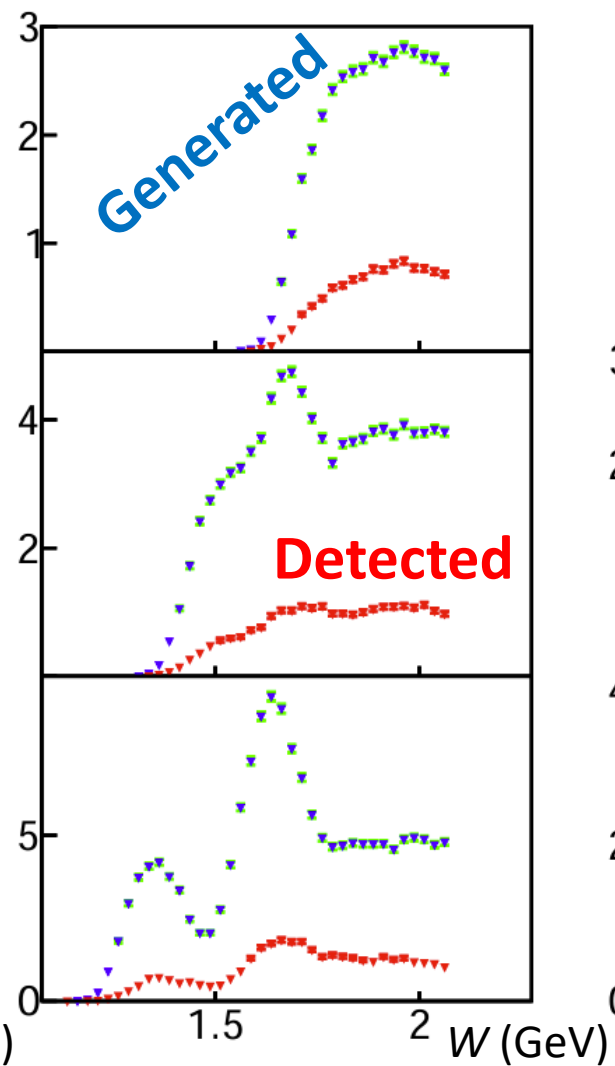
Corrections applied point-to-point

Higher $\theta_{\pi q}$



$$d(e, e' \pi^-)$$

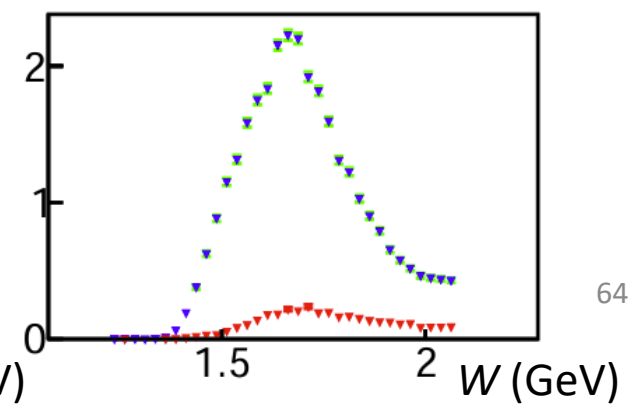
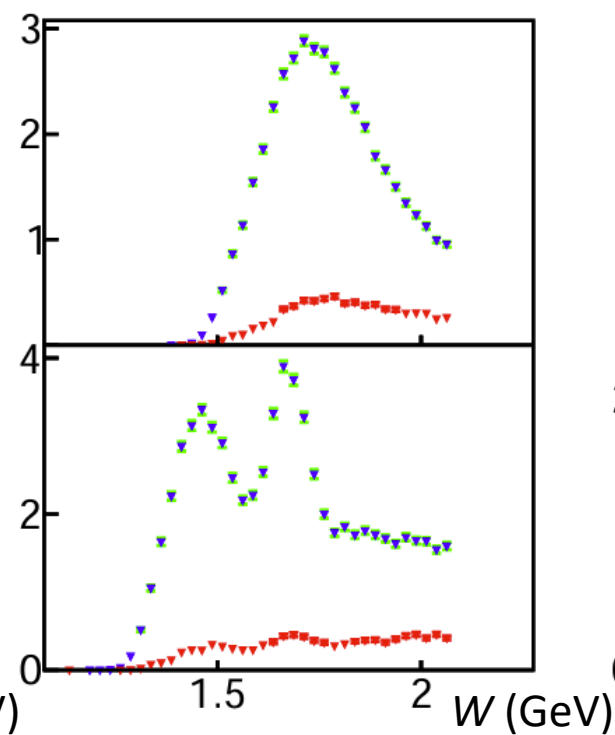
$$1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$



Acceptance Corrections

Bin migration included in correction

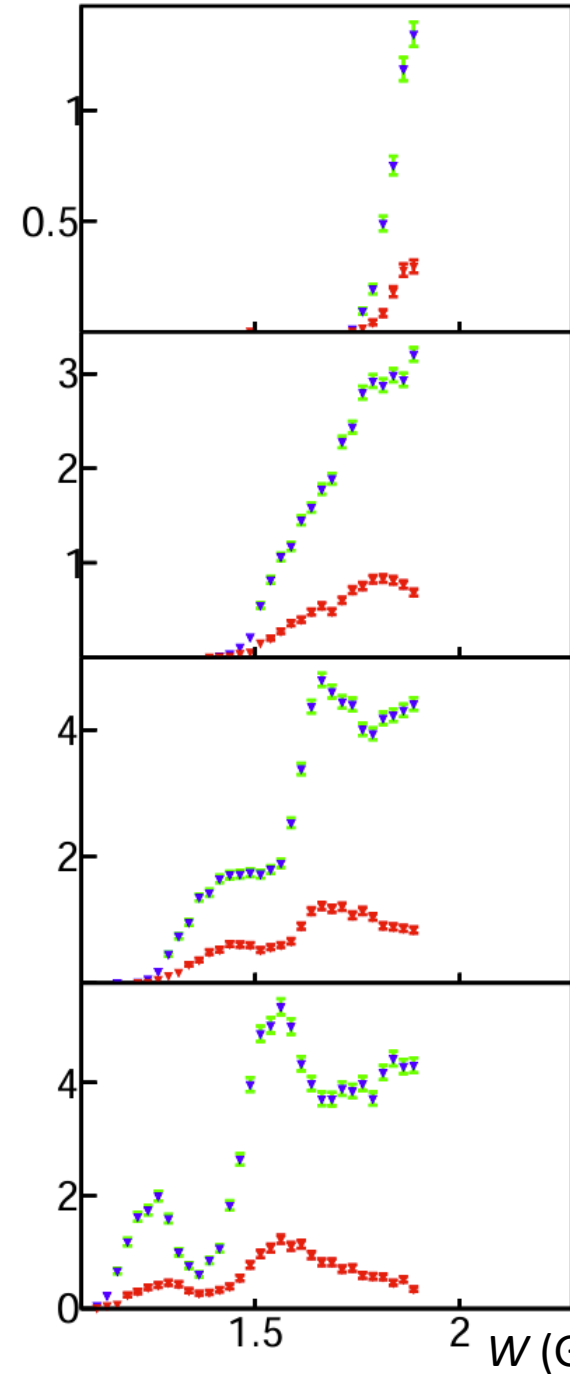
Corrections applied point-to-point



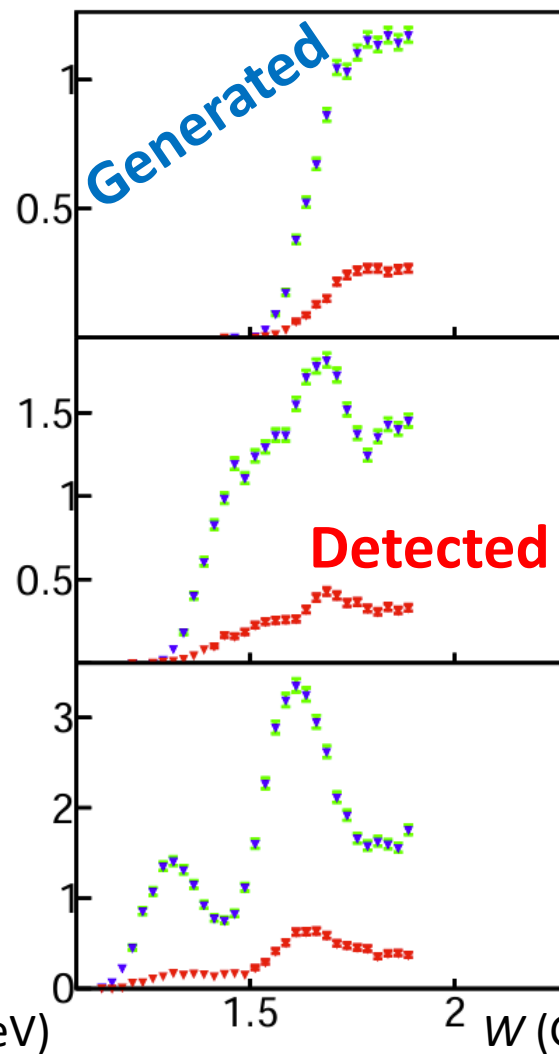
Higher $\theta_{\pi q}$

Higher P_π

GENIE Nonradiative Cross Sections



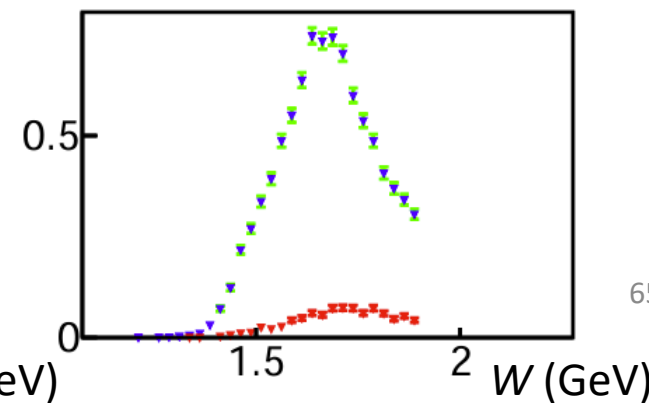
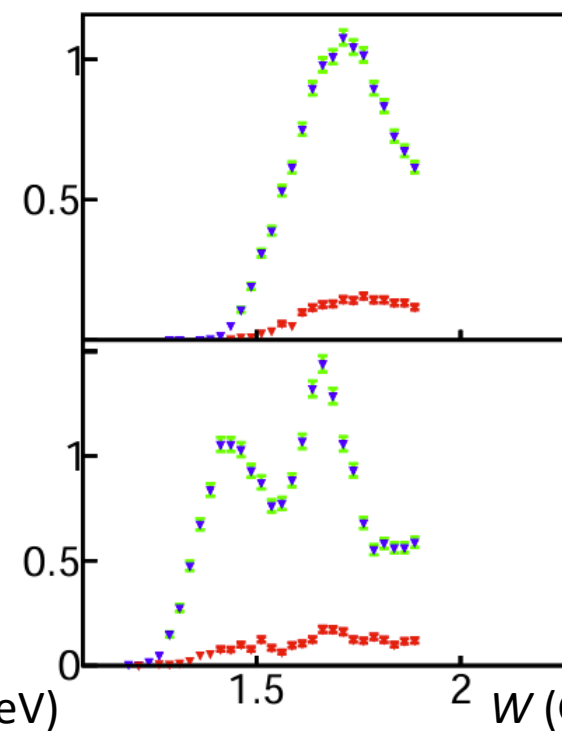
$$d(e, e' \pi^-)$$
$$1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$



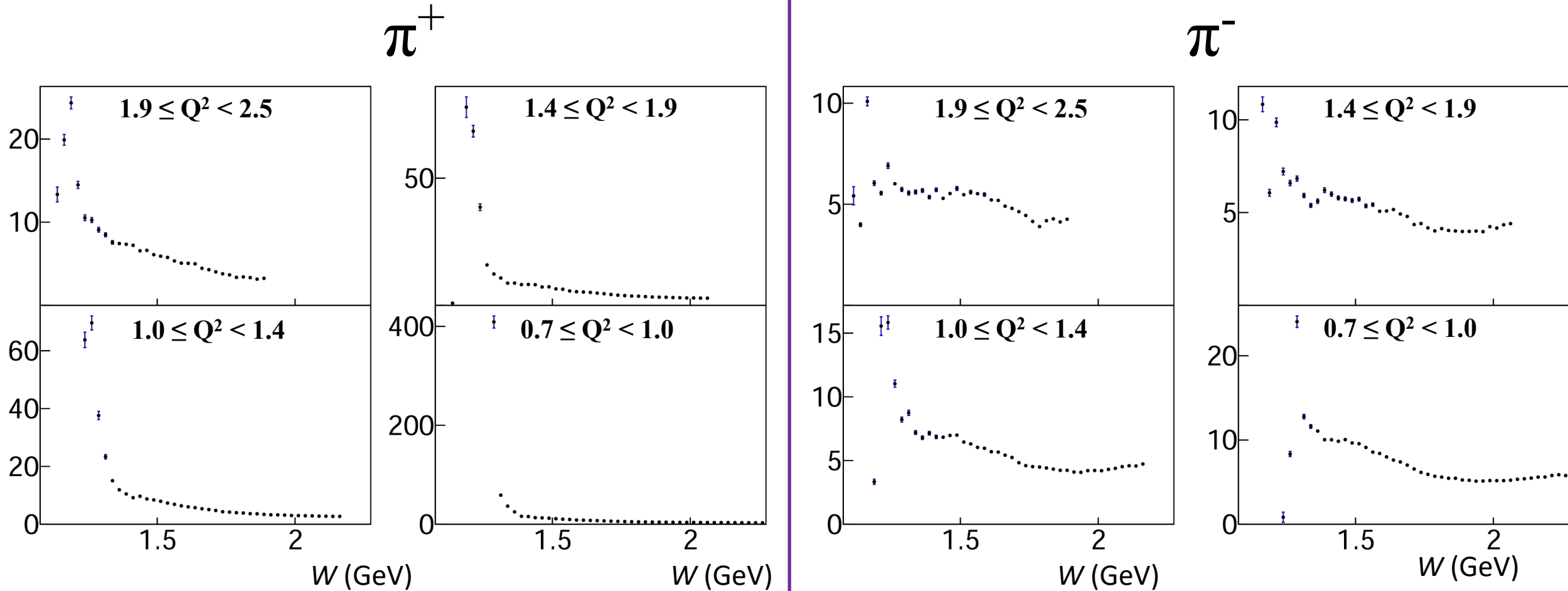
Acceptance Corrections

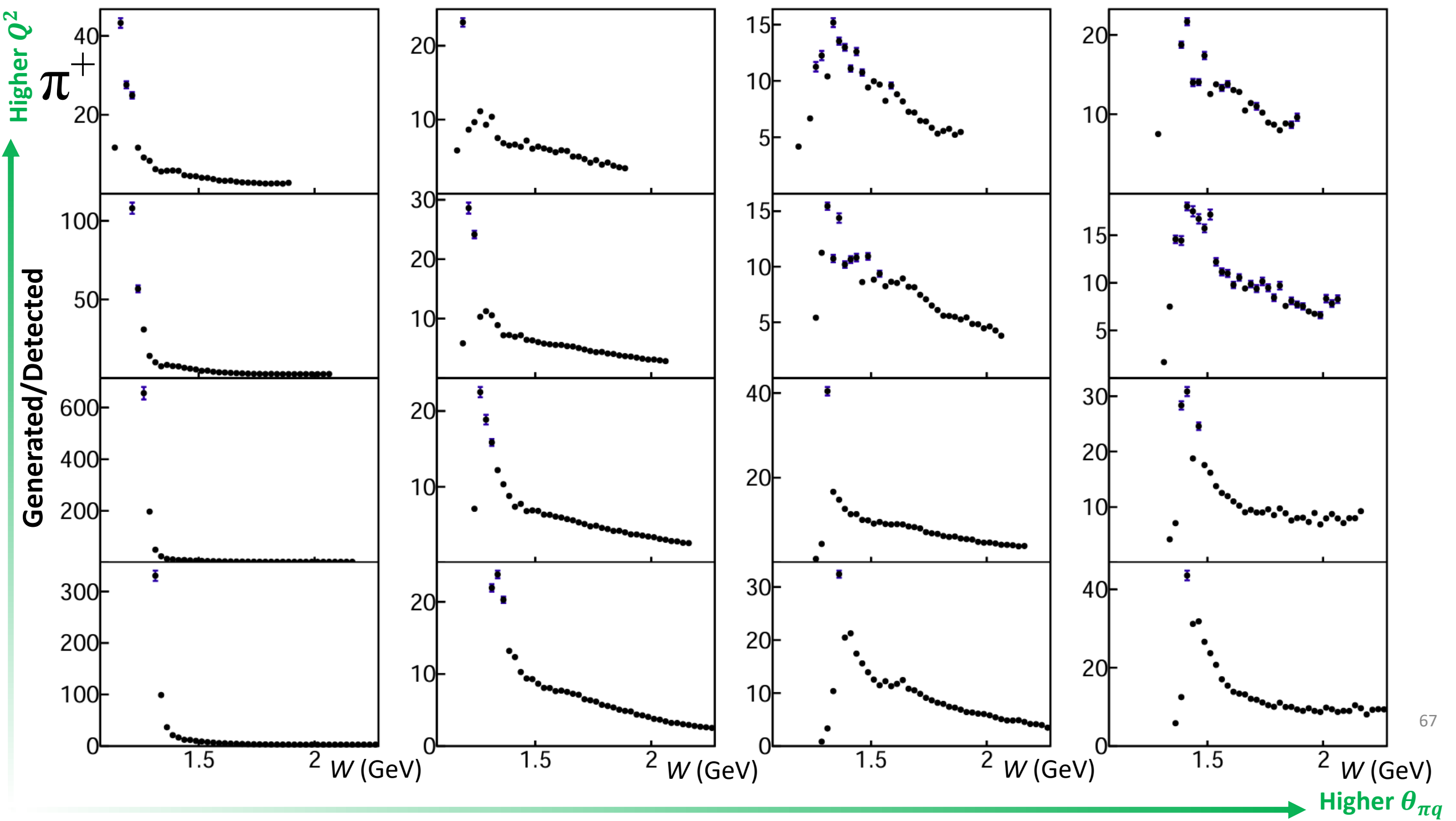
Bin migration included in correction

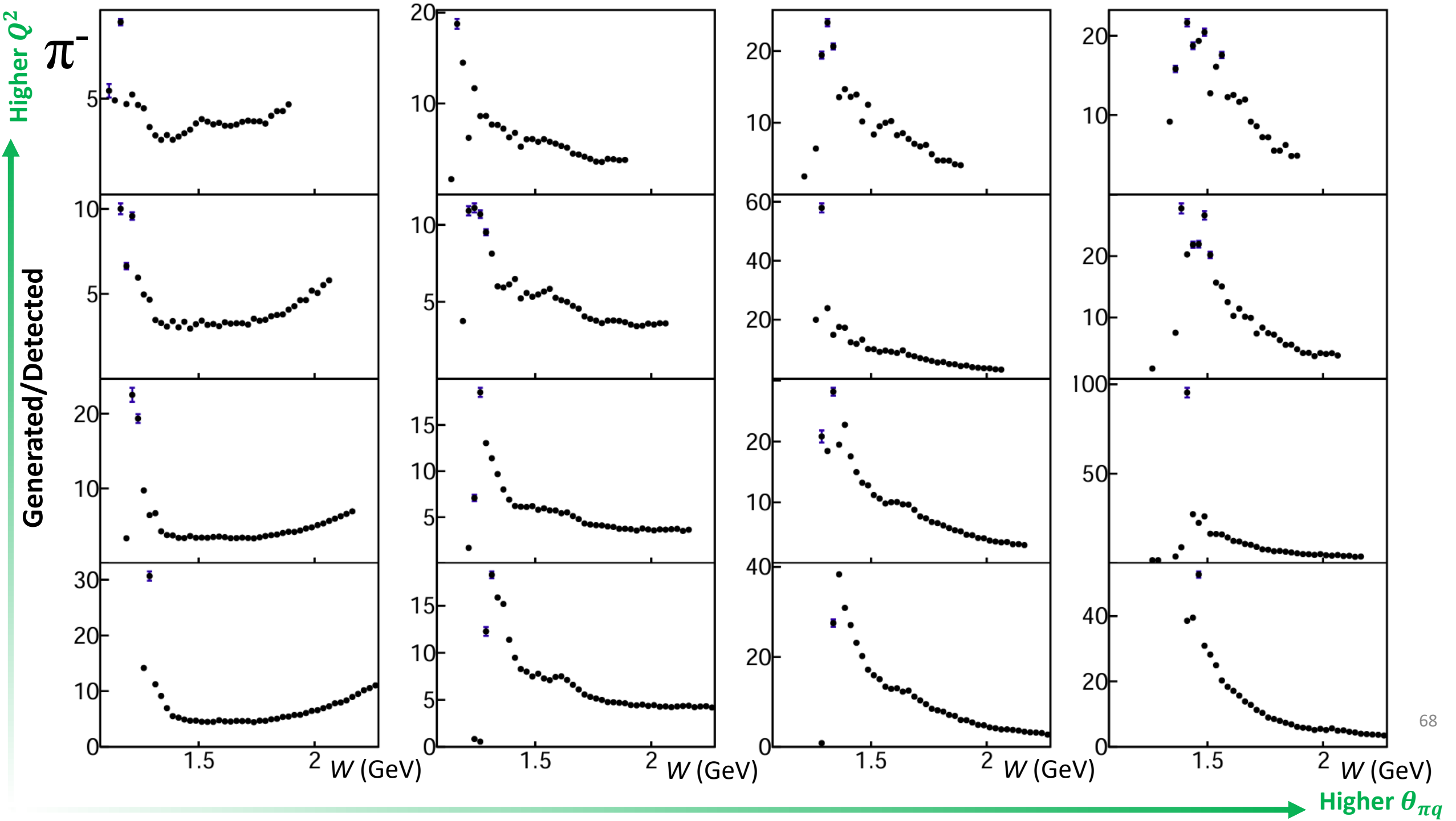
Corrections applied point-to-point

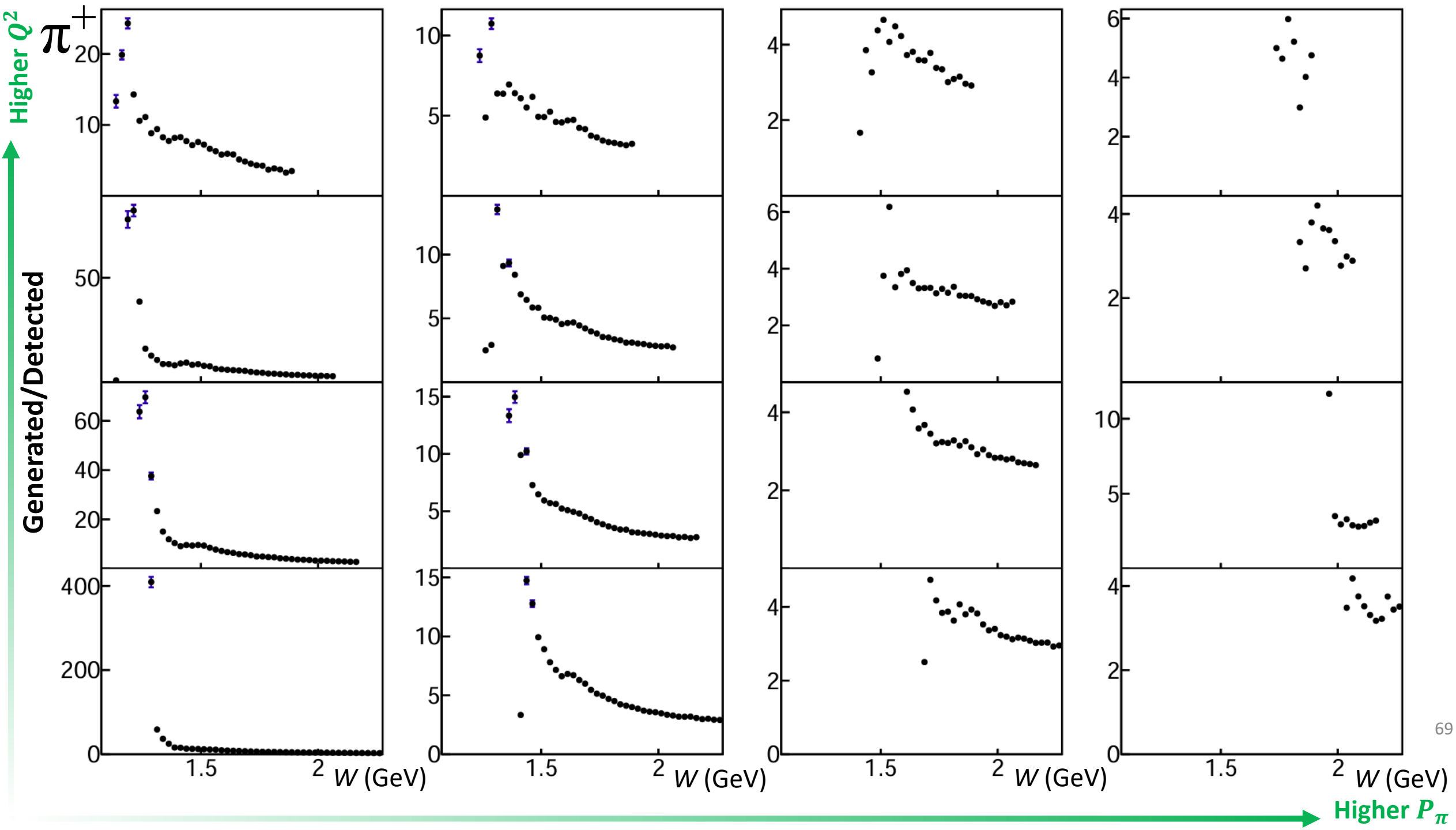
Higher $\theta_{\pi q}$

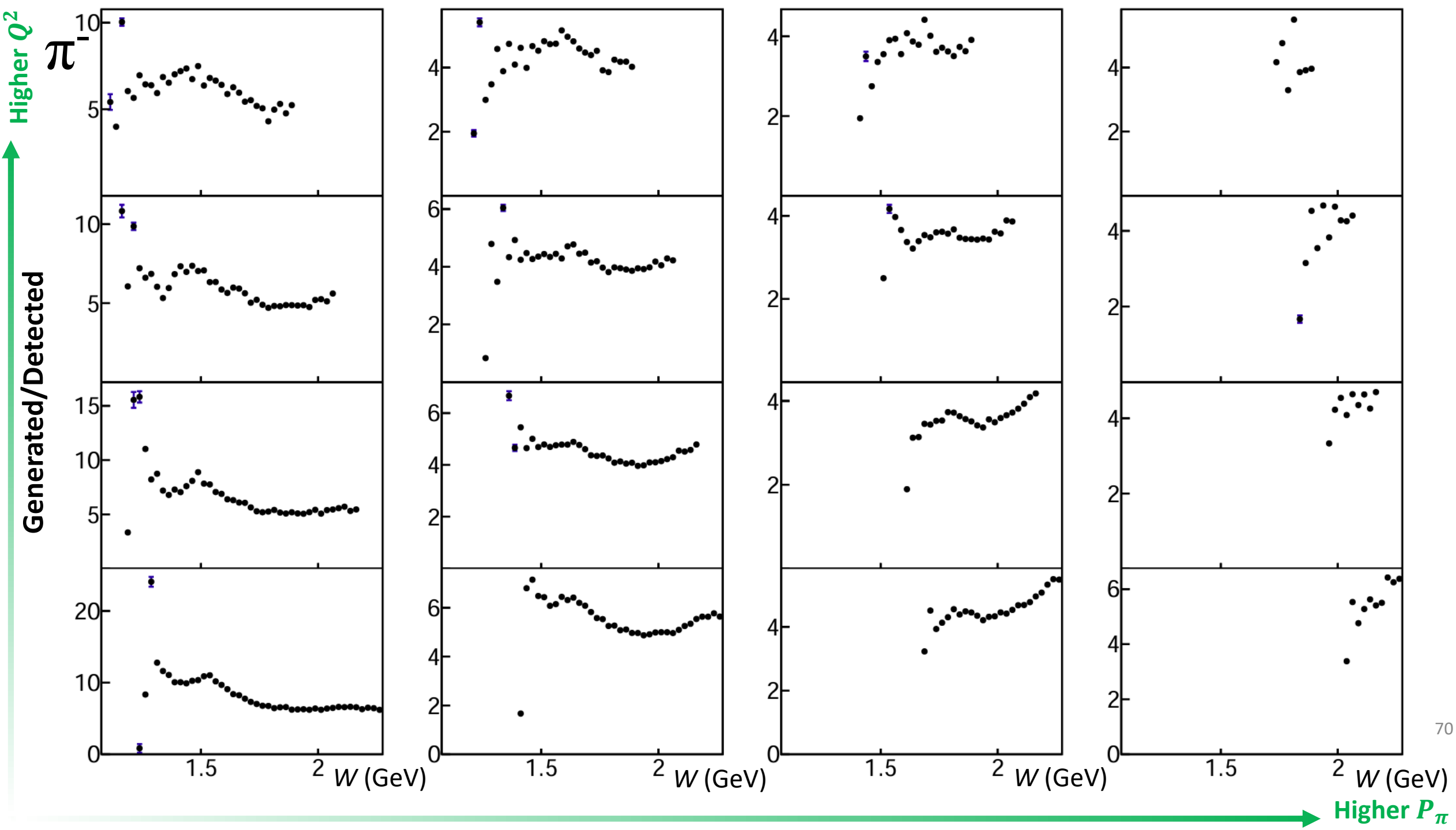
D(e,e' π) Acceptance Corrections vs W binned in Q^2





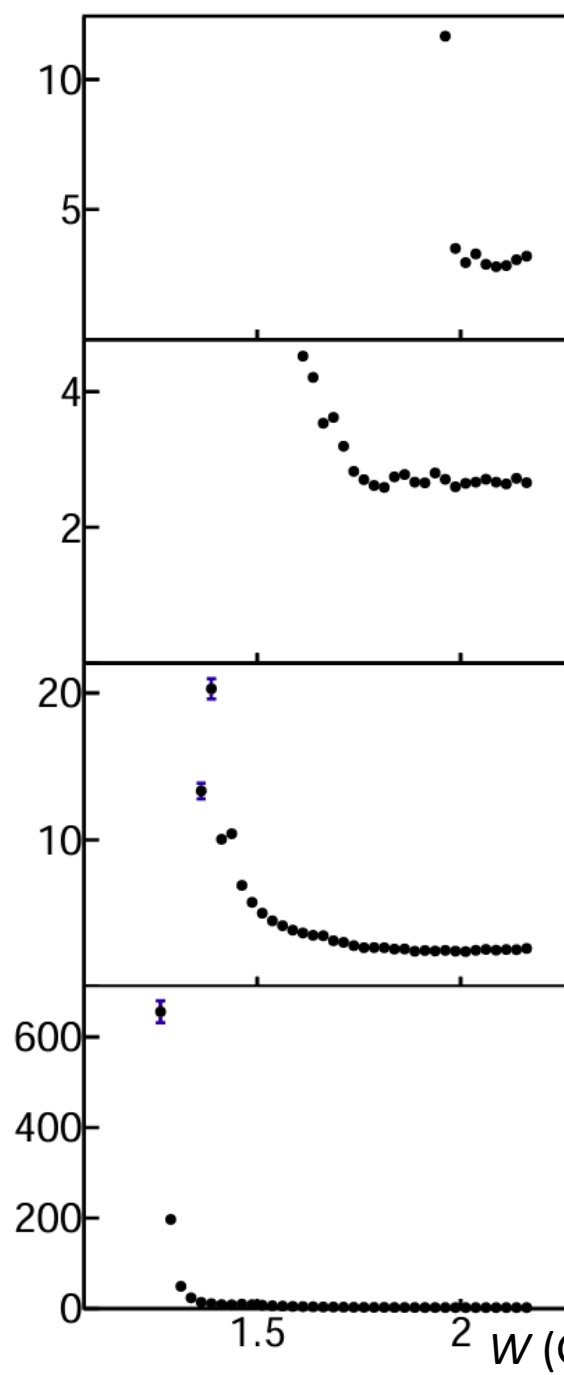




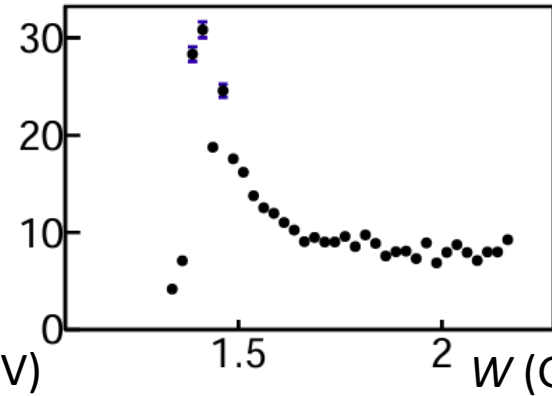
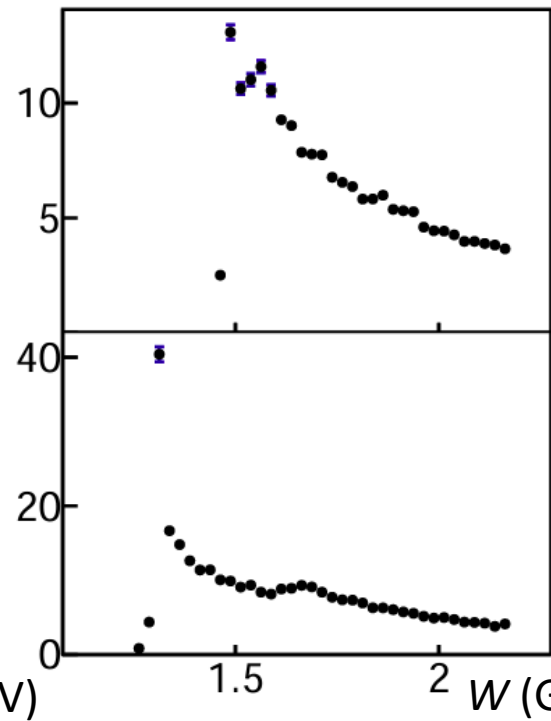
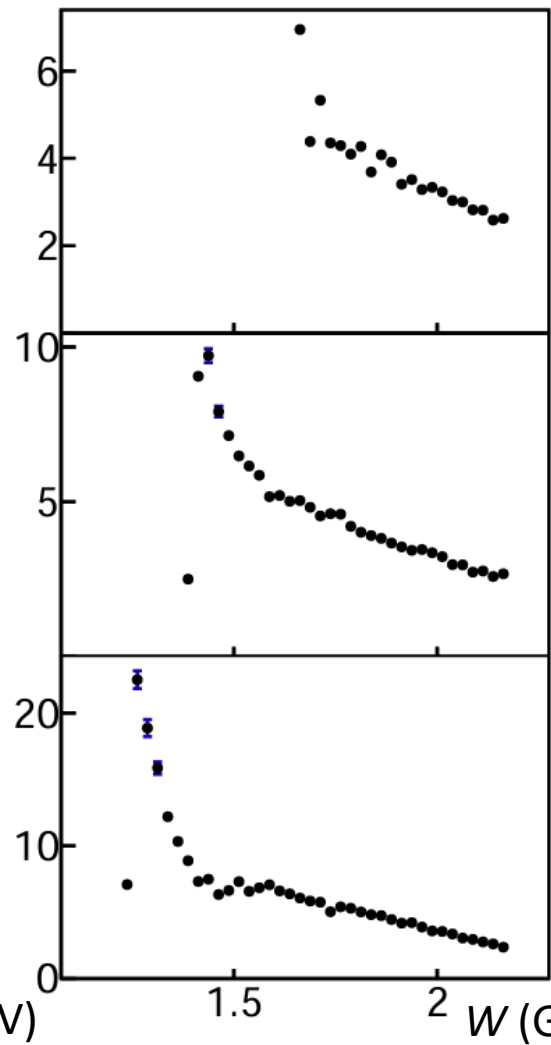


Higher P_π 

Generated/Detected



$$d(e, e' \pi^+)$$
$$1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$



Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

Higher $\theta_{\pi q}$ 

Higher P_{π}

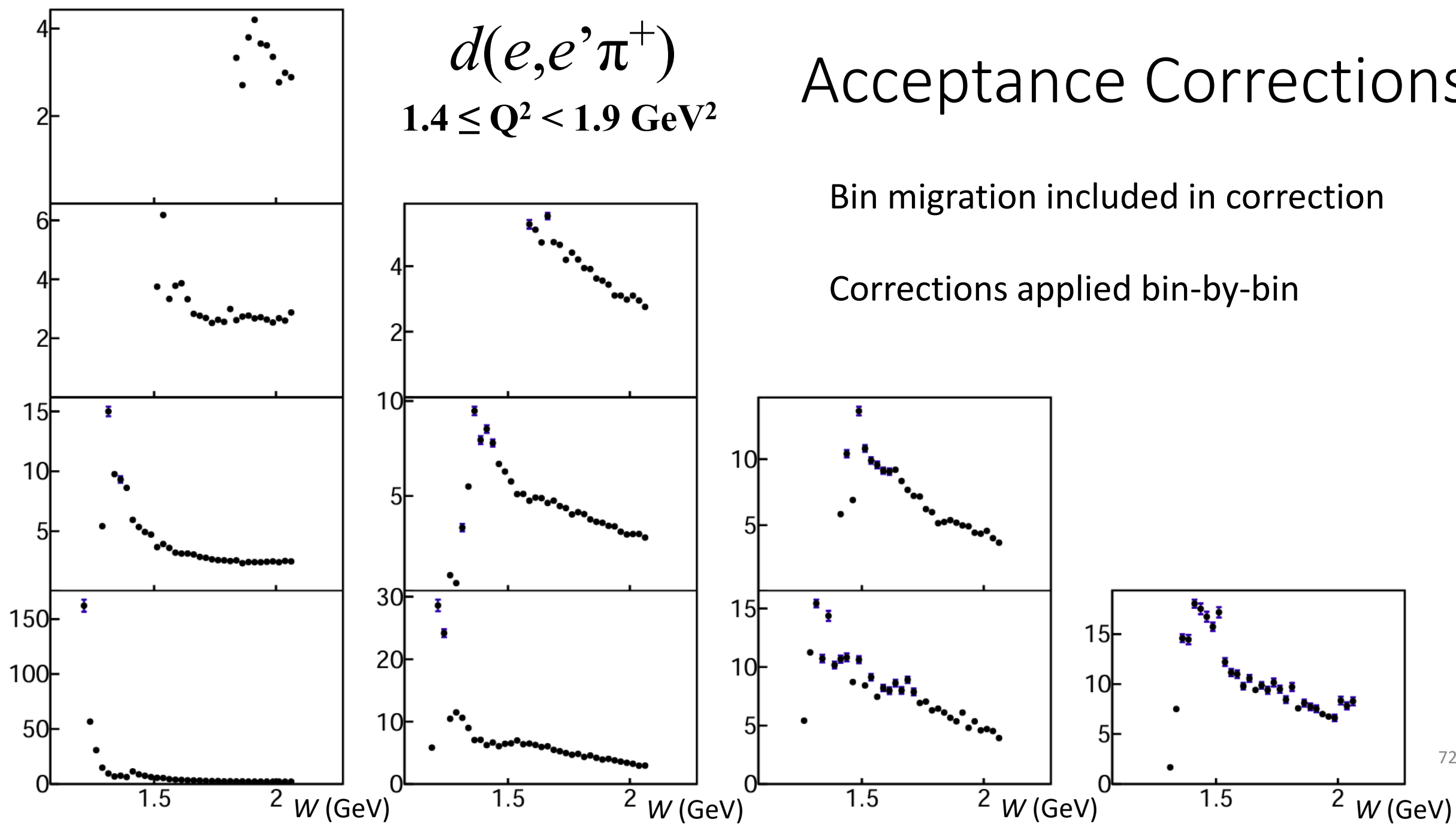
Generated/Detected

$$d(e, e' \pi^+)$$
$$1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

Higher $\theta_{\pi q}$

Higher P_π

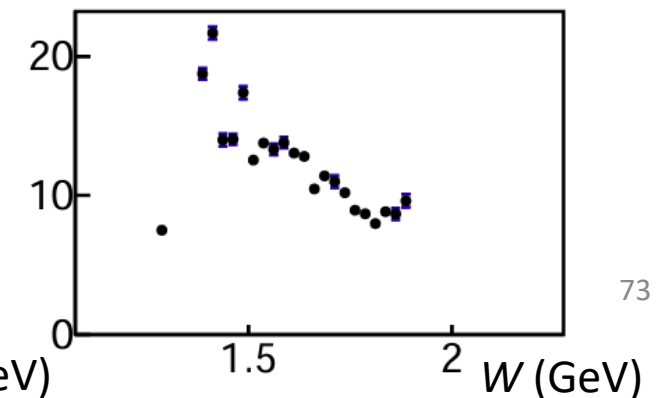
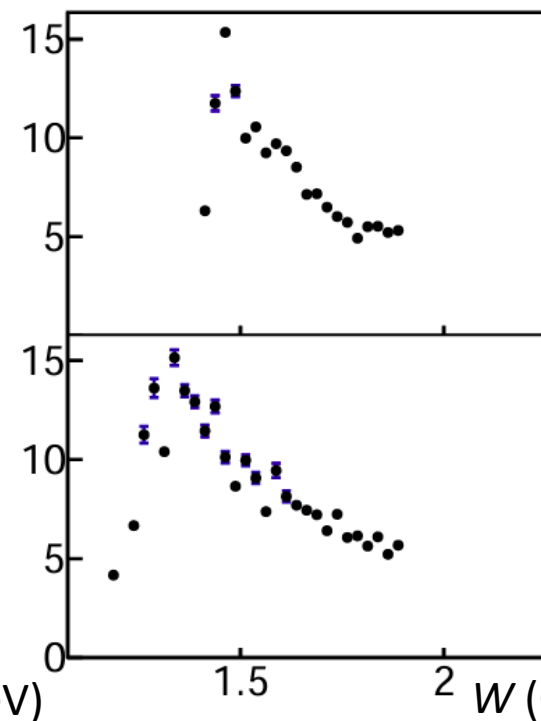
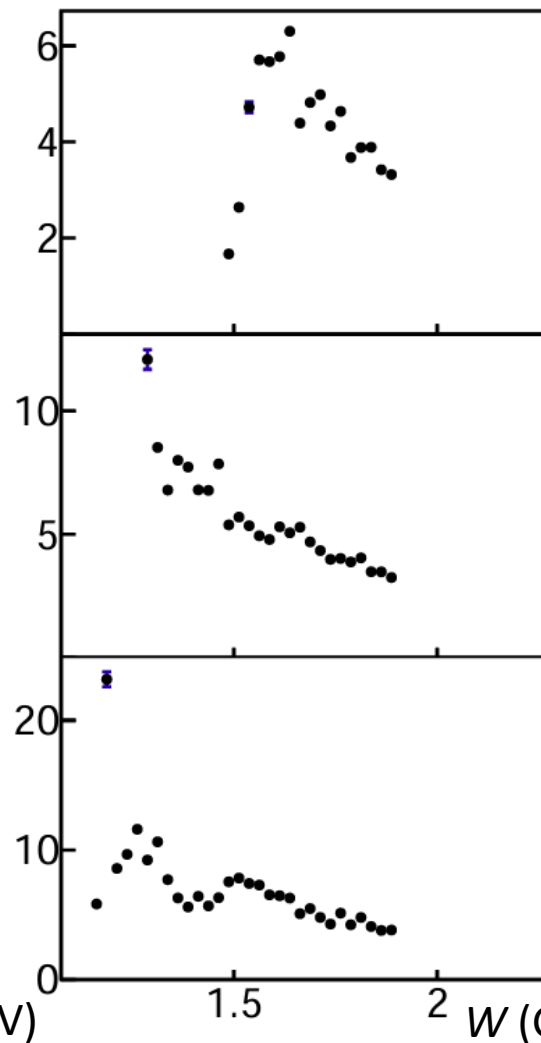
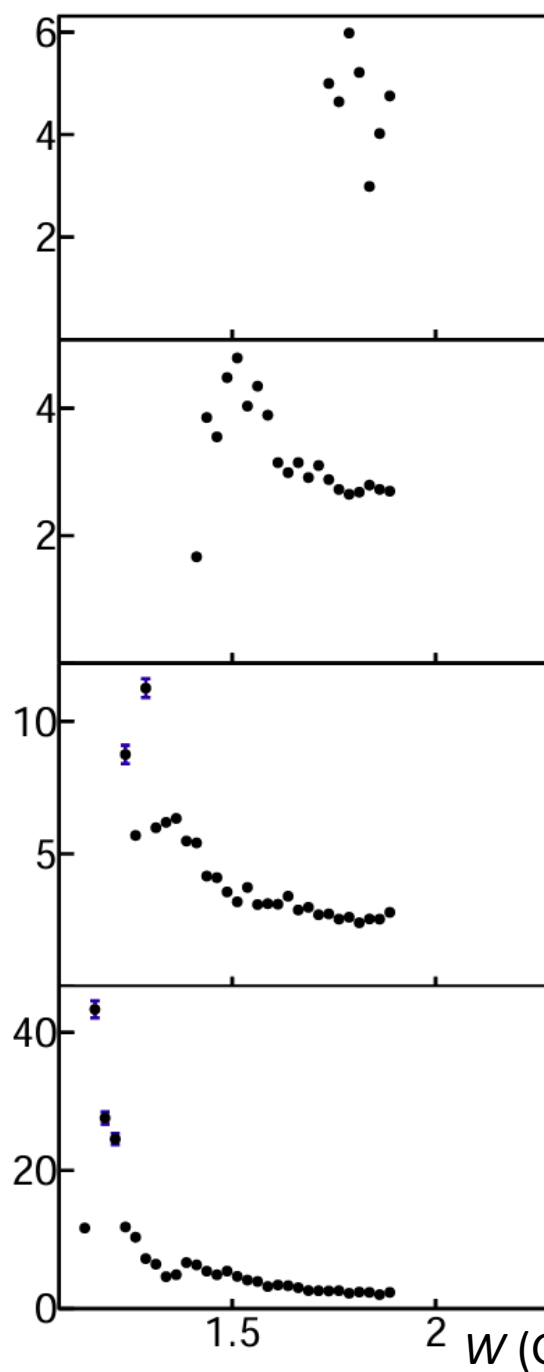
Generated/Detected

$$d(e, e' \pi^+)$$
$$1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

Higher $\theta_{\pi q}$

Higher P_π

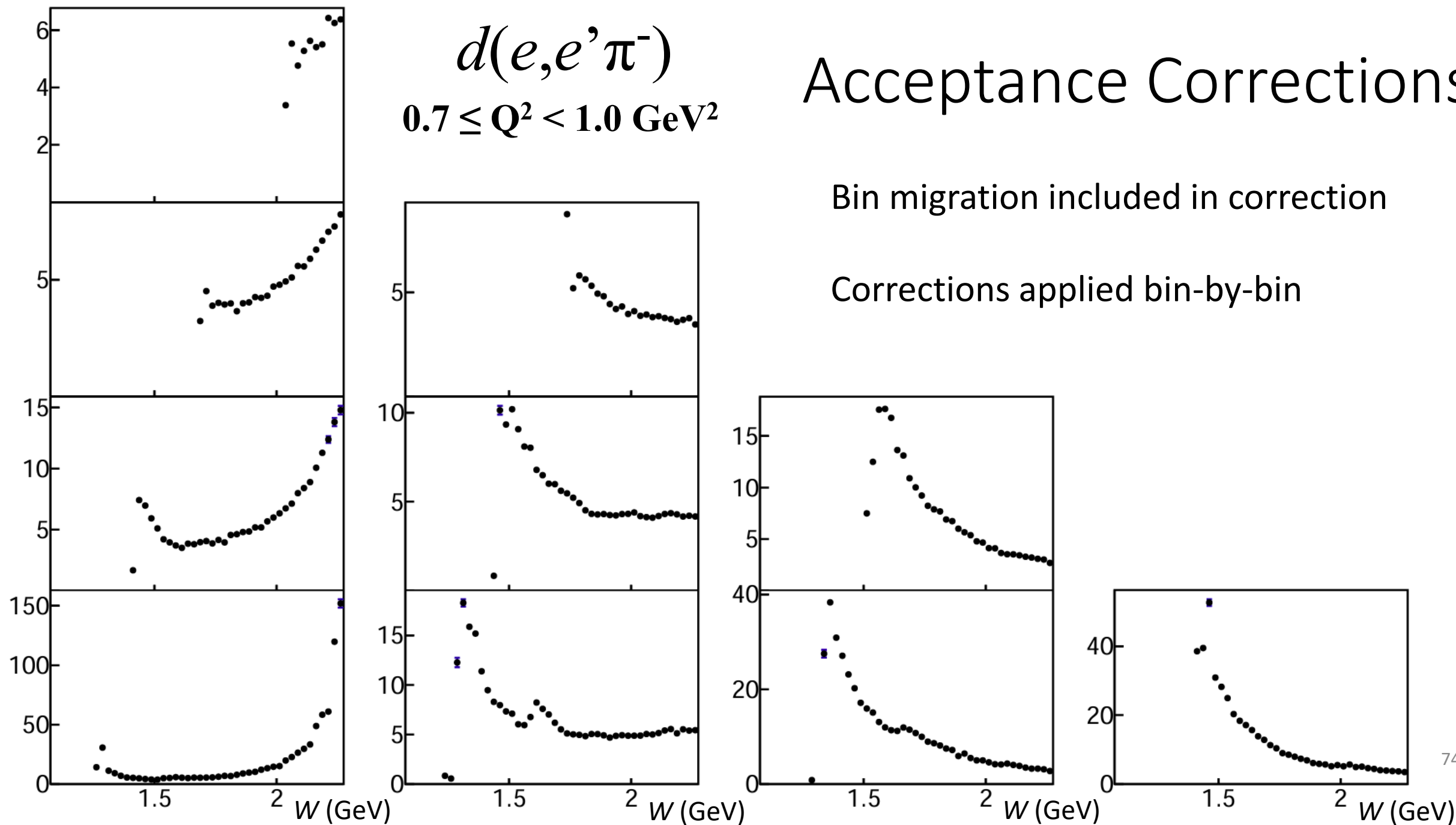
Generated/Detected

$$d(e, e' \pi^-)$$
$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

Higher $\theta_{\pi q}$

Higher P_π

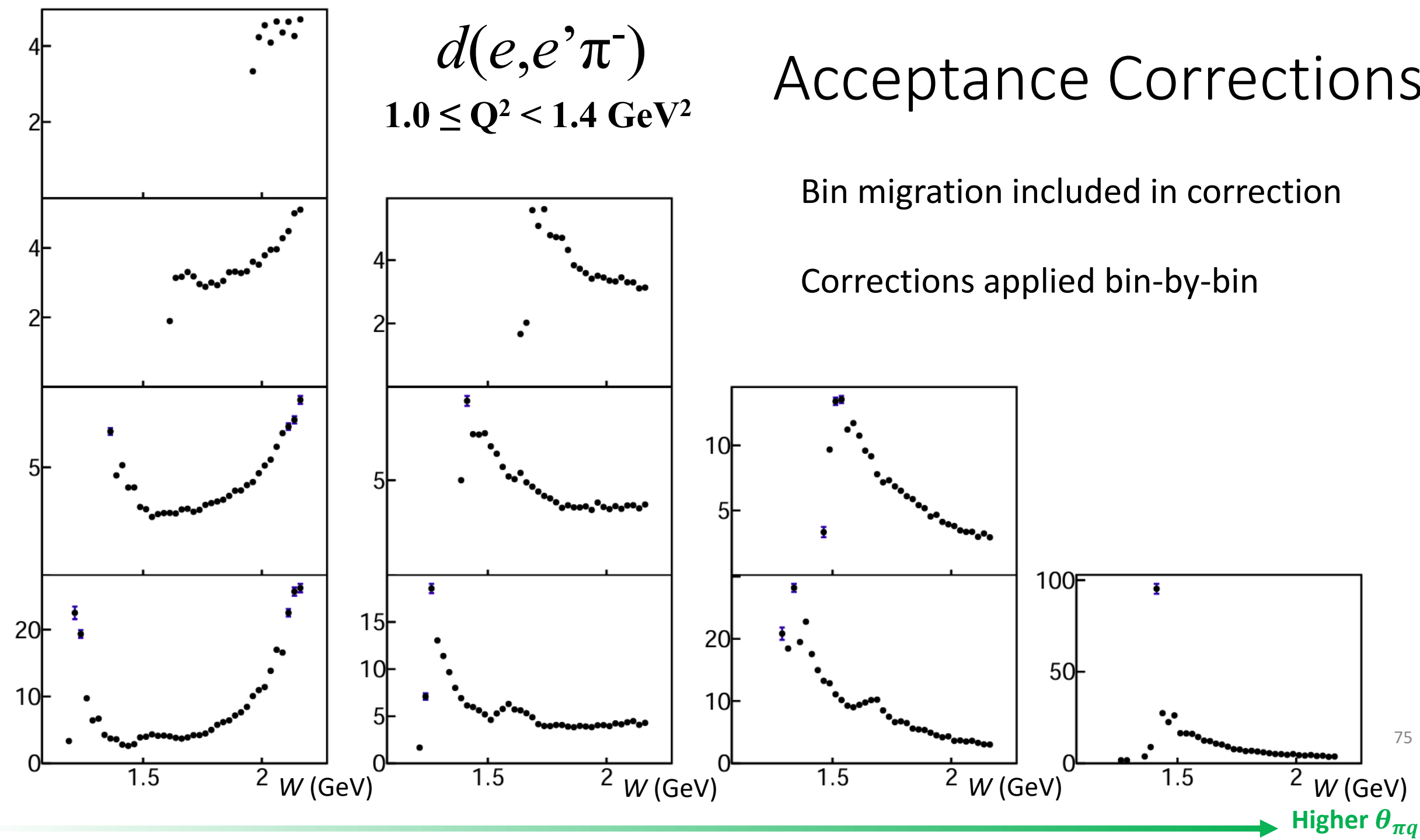
Generated/Detected

$$d(e, e' \pi^-)$$
$$1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin



Higher P_π

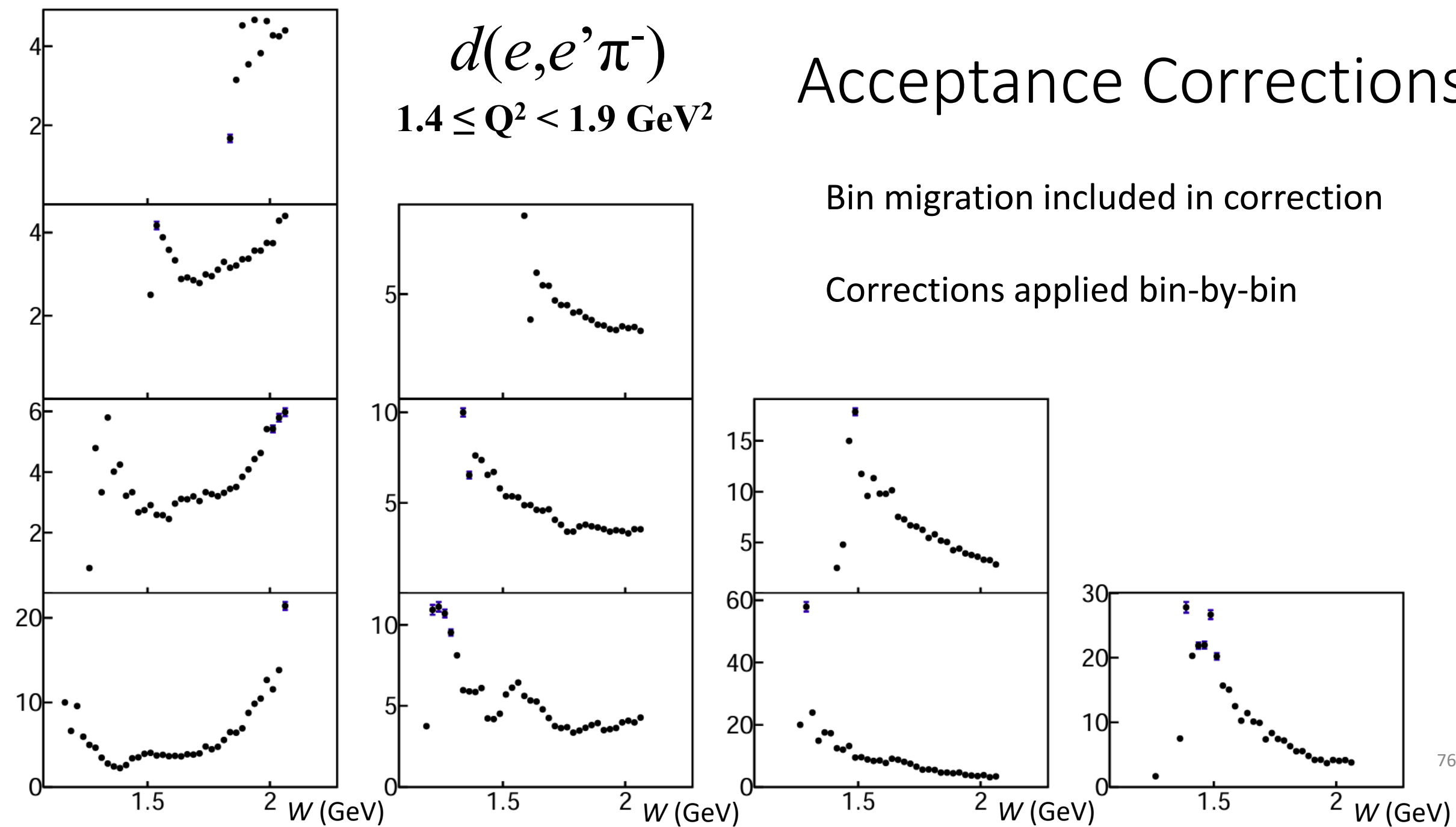
Generated/Detected

$$d(e, e' \pi^-)$$
$$1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

Higher $\theta_{\pi q}$

Higher P_π

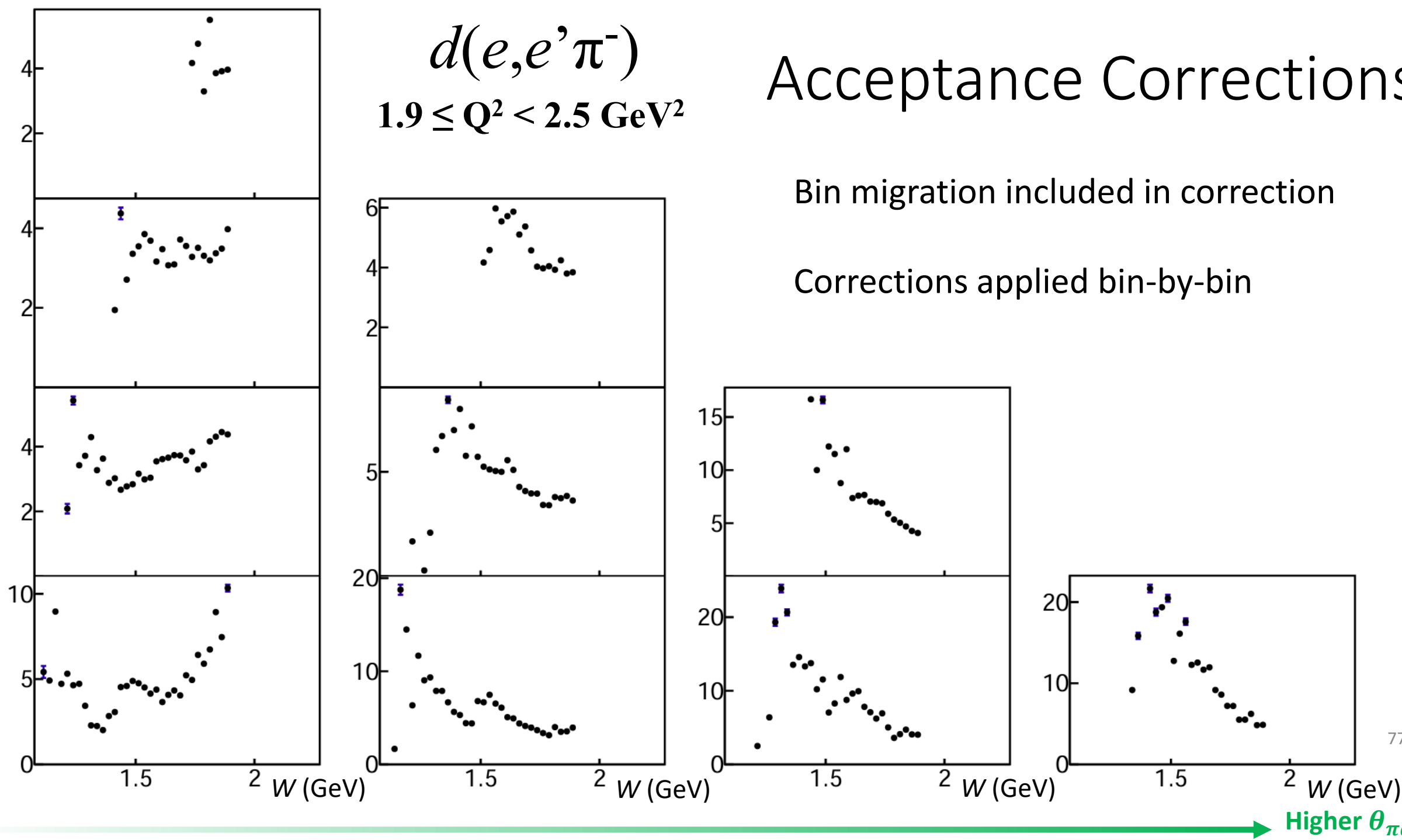
Generated/Detected

$$d(e, e' \pi^-)$$
$$1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$

Acceptance Corrections

Bin migration included in correction

Corrections applied bin-by-bin

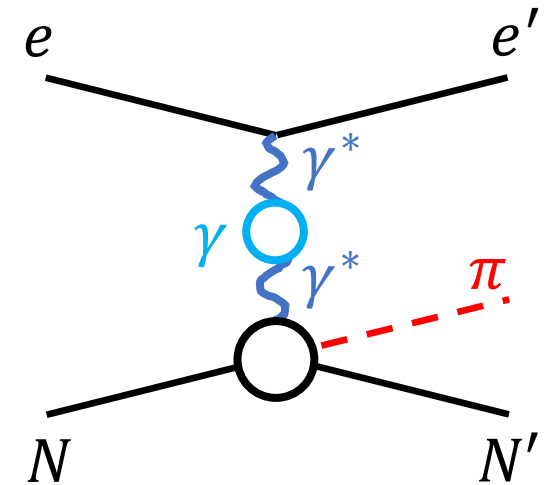
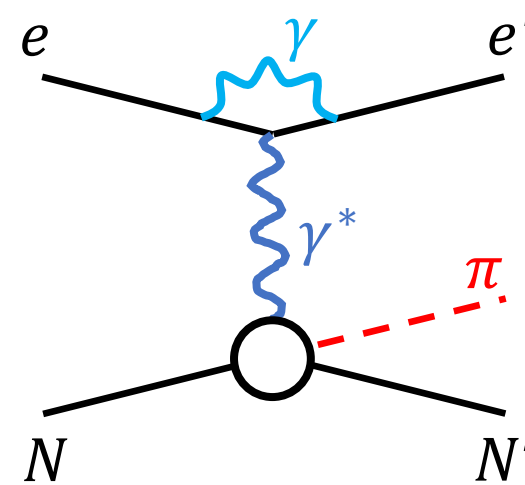
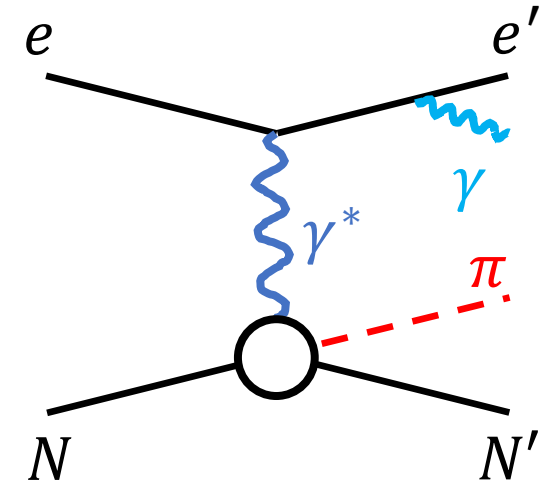
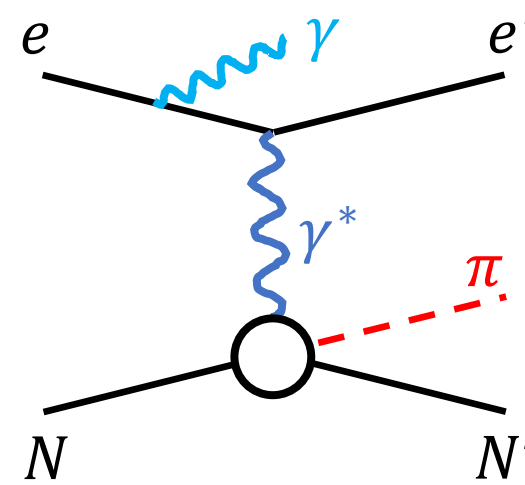
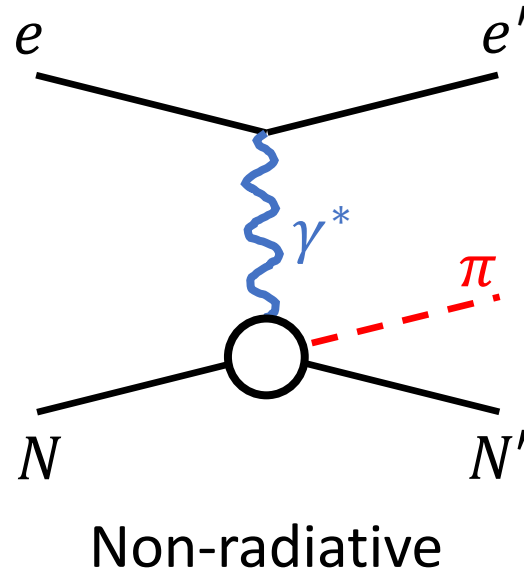


Radiative Correction

- with GENIE

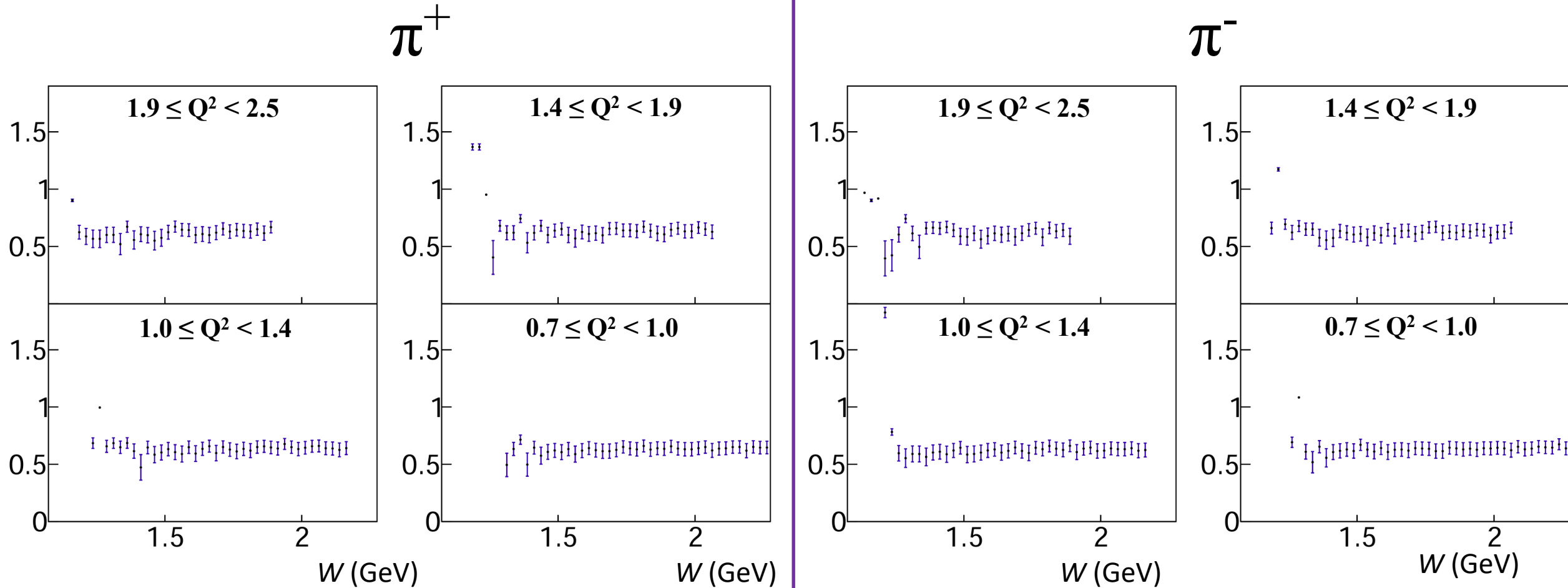
$$\frac{1}{RC} = \frac{CS_{rad}^{GENIE}}{CS_{norad}^{GENIE}}$$

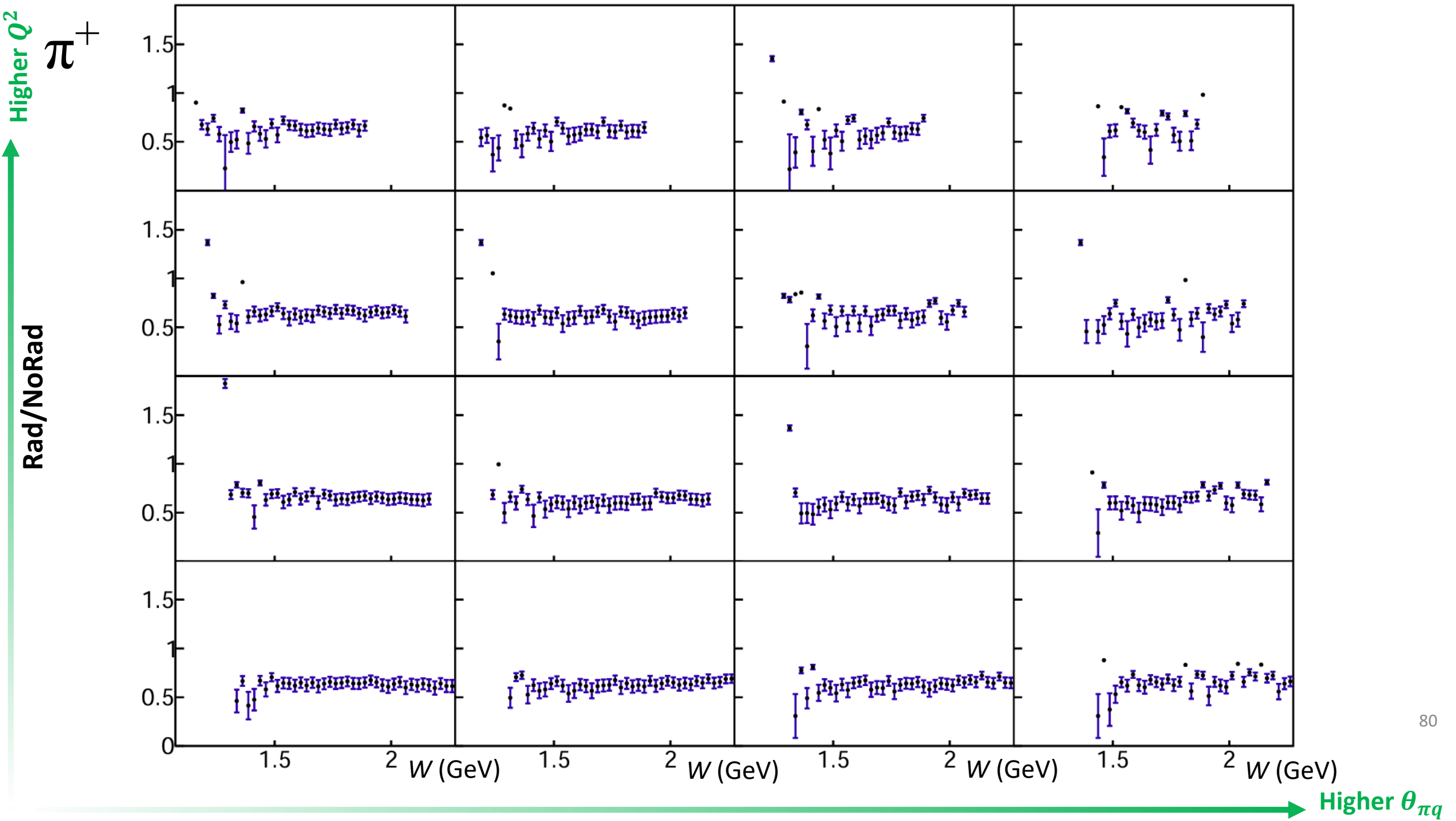
$$CS_{norad}^{data} = CS_{rad}^{data} * RC$$

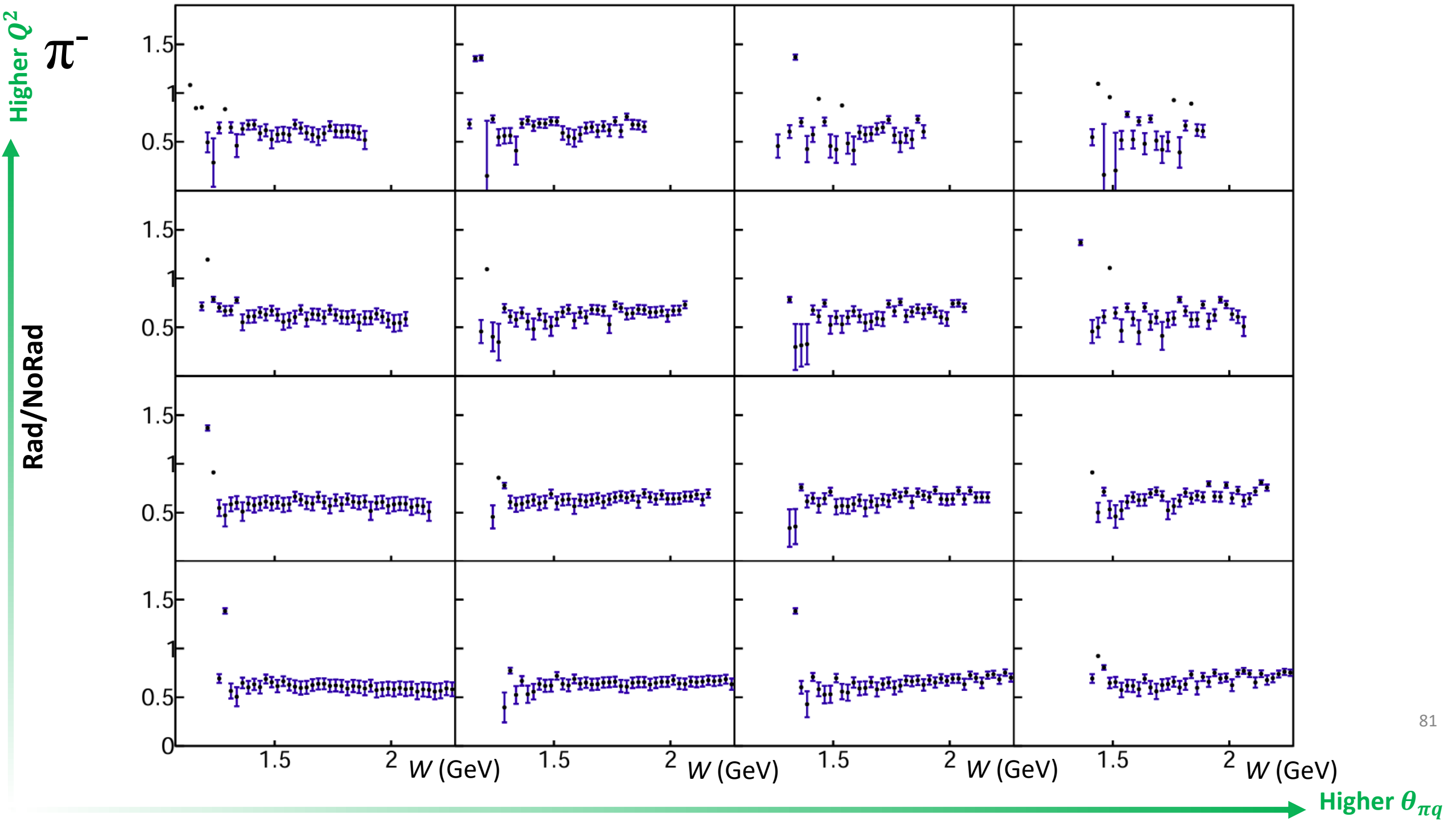


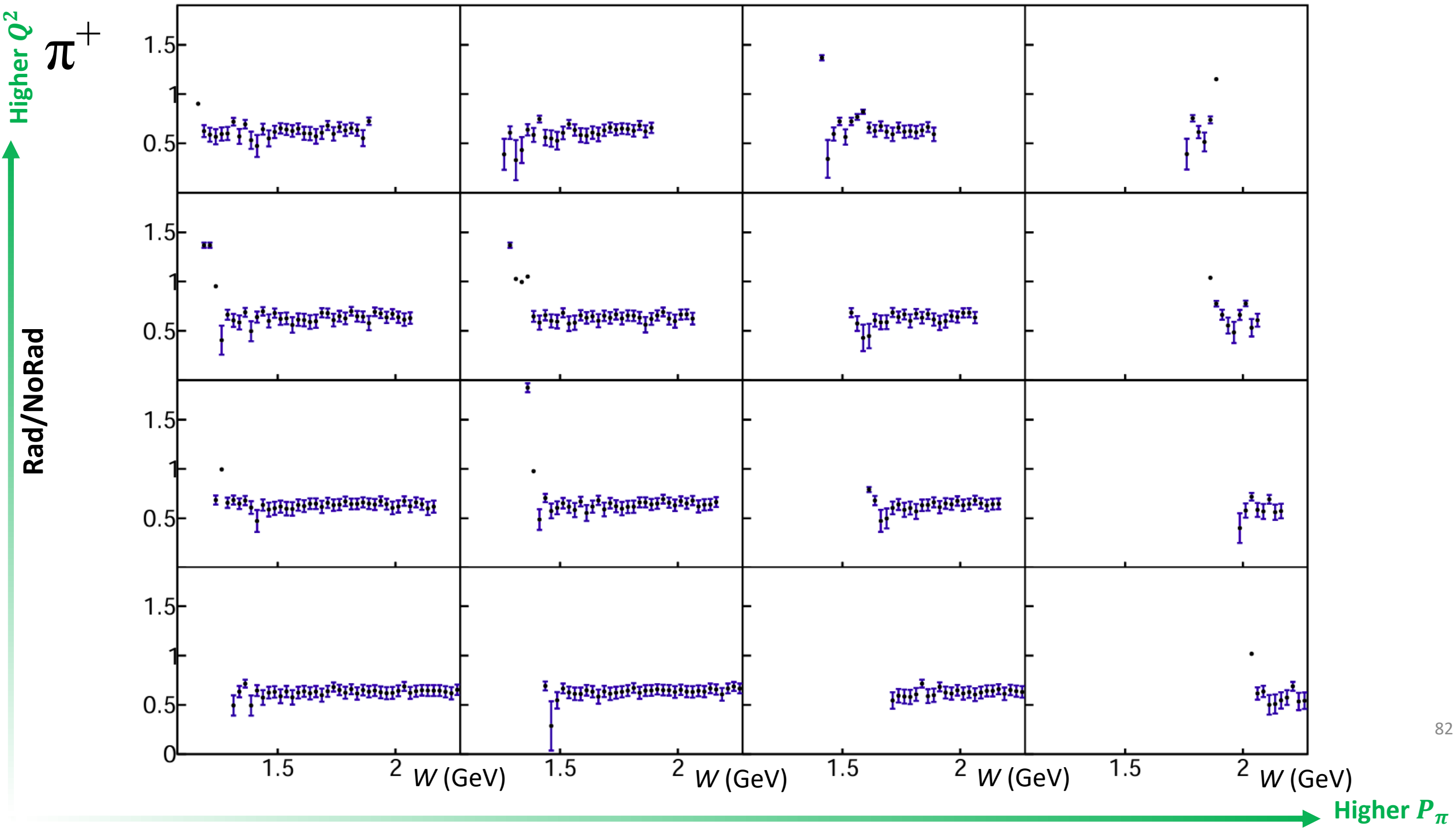
Radiative

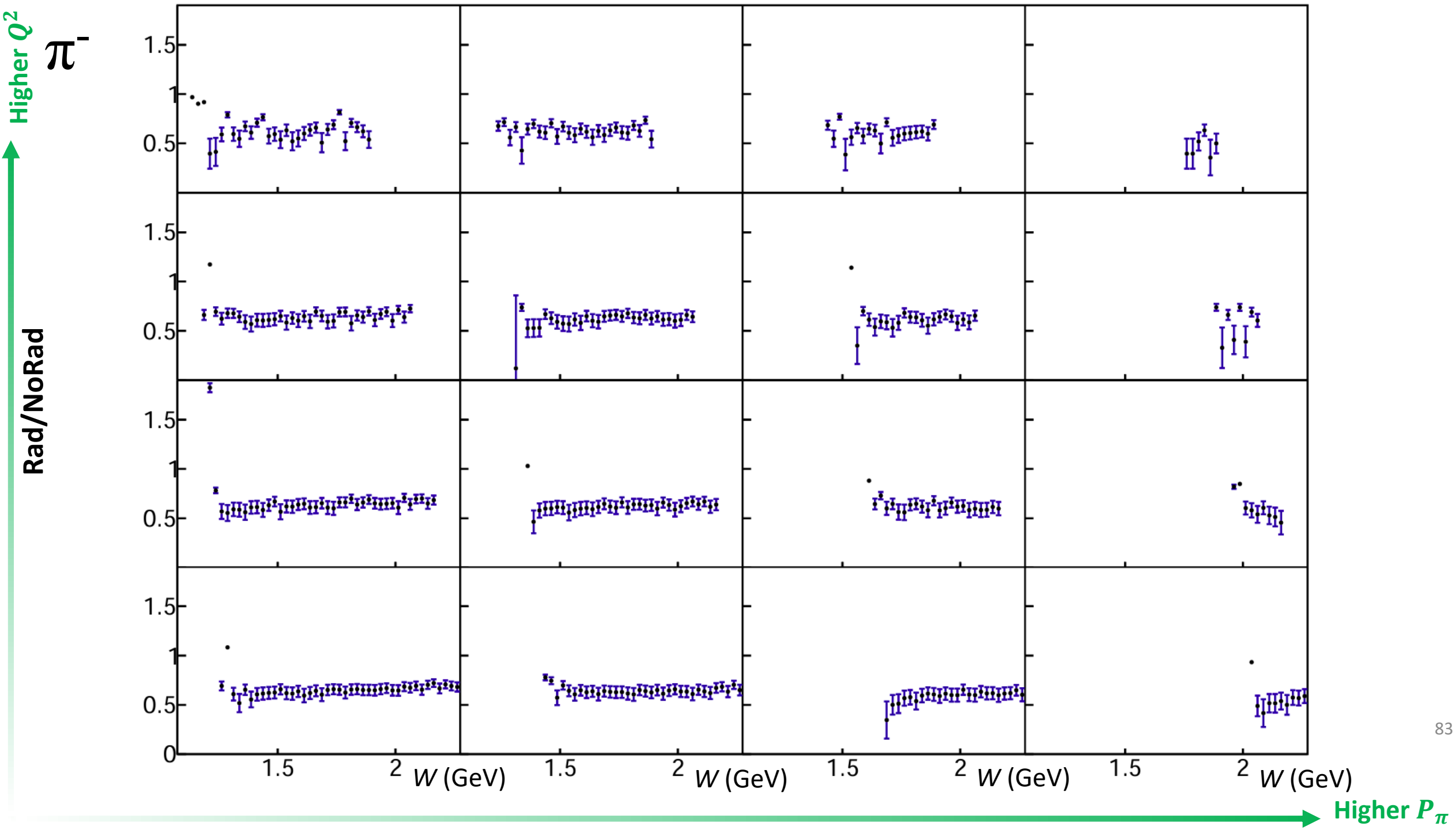
D(e,e'π) Radiative Corrections vs W binned in Q²











Higher P_π

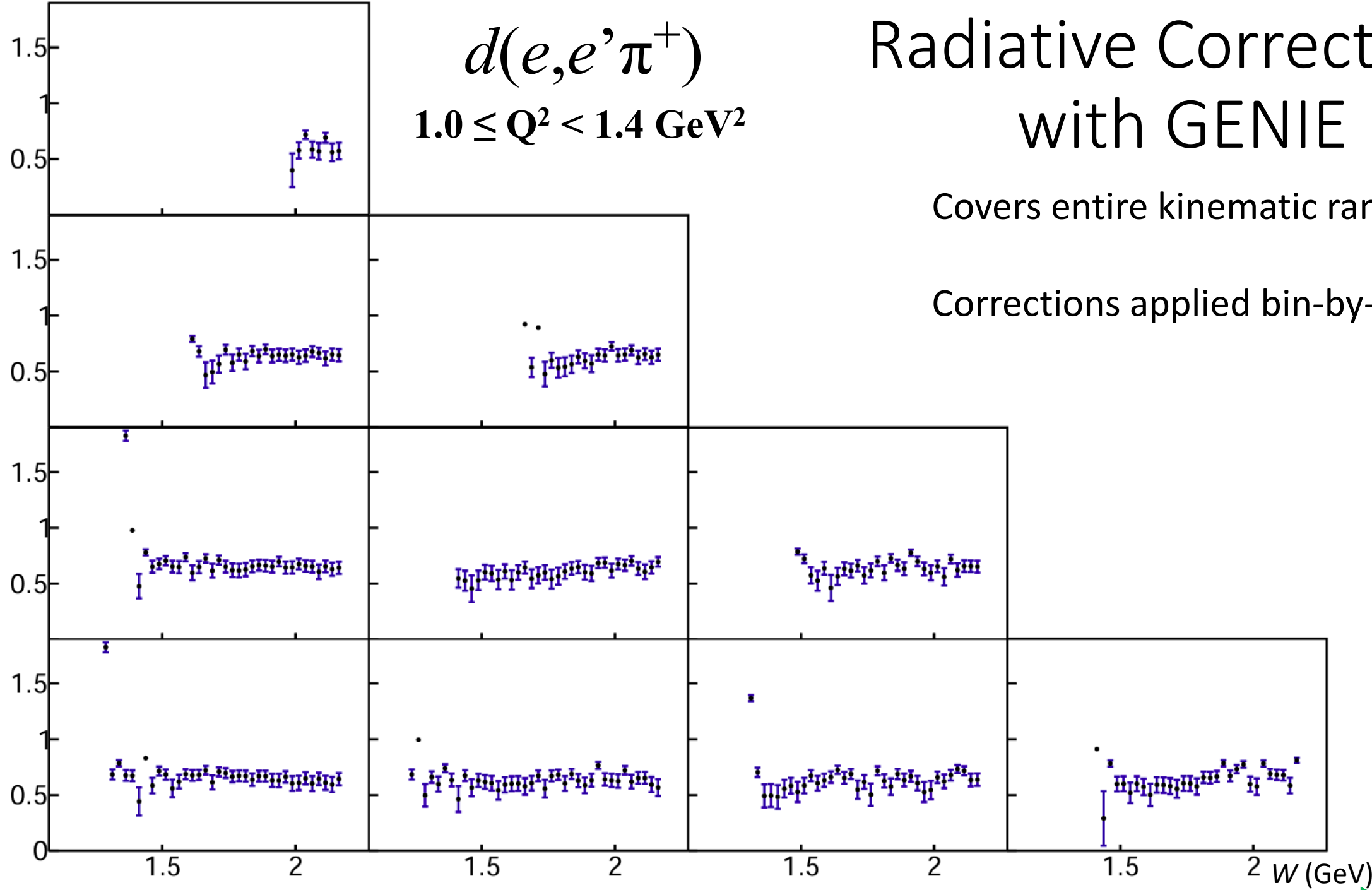
Rad/NoRad

$$d(e, e' \pi^+)$$
$$1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

Corrections applied bin-by-bin



Higher P_π 

Rad/NoRad

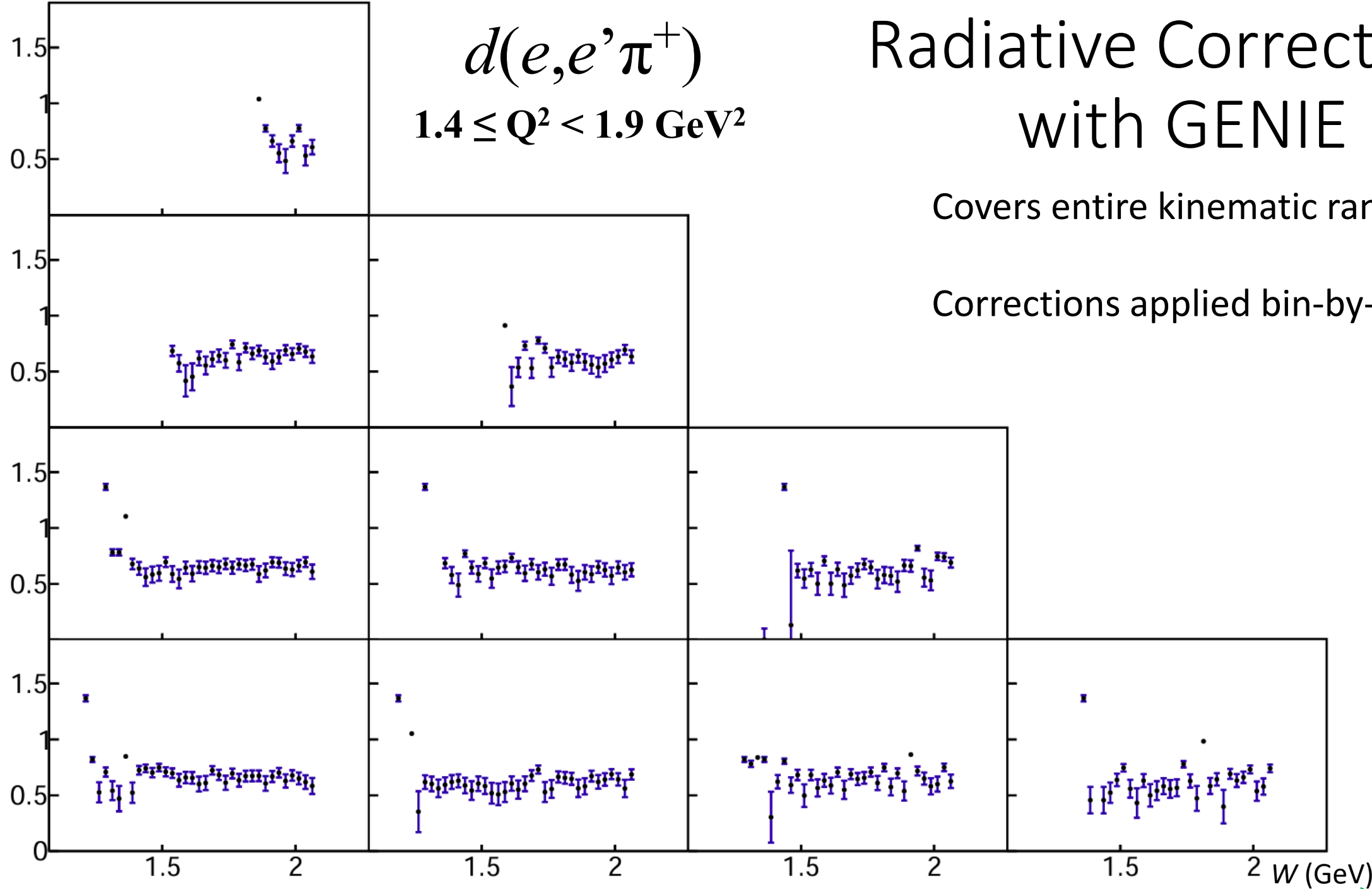


$$d(e, e' \pi^+)$$
$$1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

Corrections applied bin-by-bin

Higher $\theta_{\pi q}$

Higher P_π 

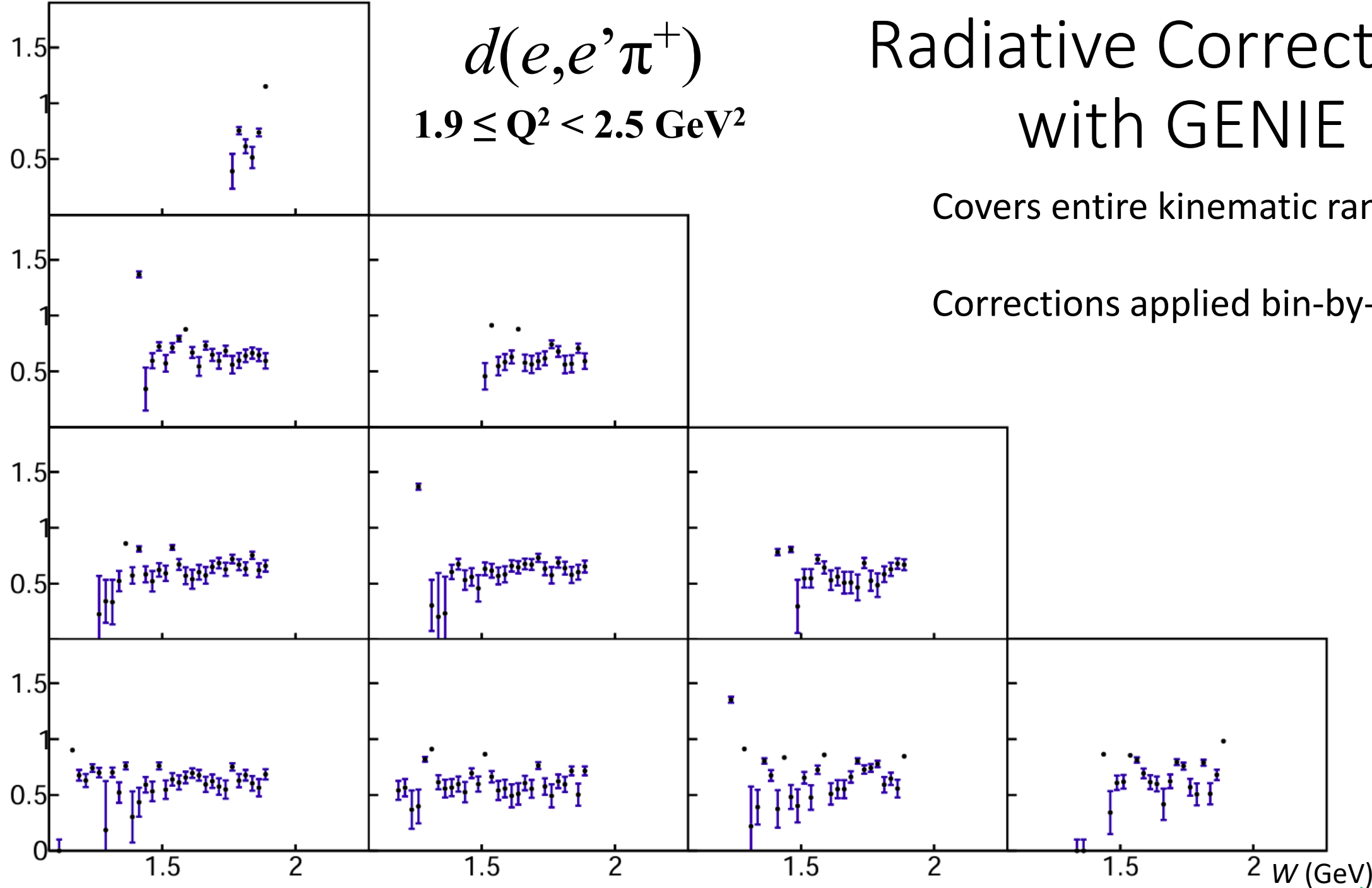
$$d(e, e' \pi^+)$$
$$1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

Corrections applied bin-by-bin

Rad/NoRad

Higher $\theta_{\pi q}$

Higher P_π



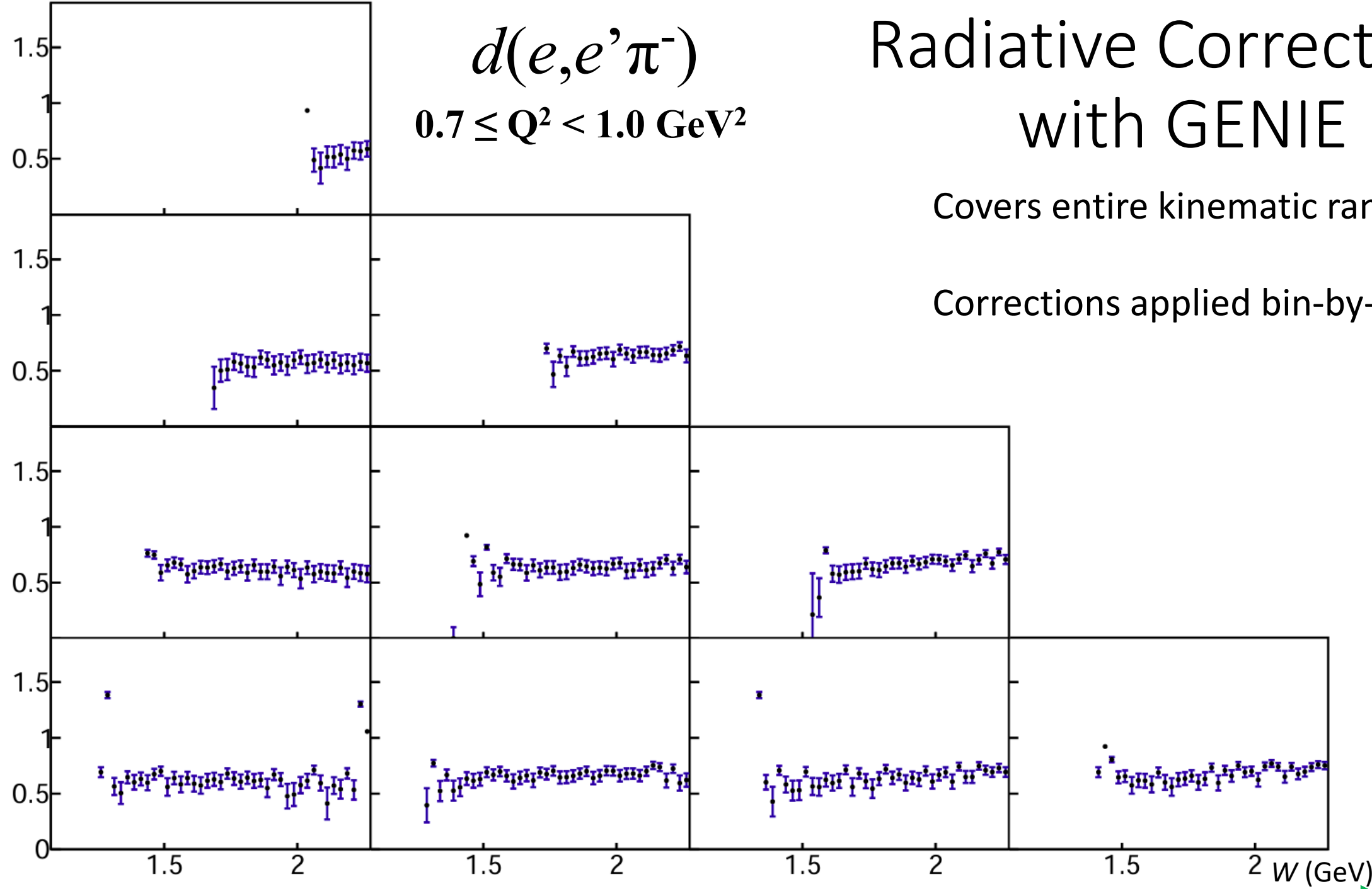
$$d(e, e' \pi^-)$$
$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

Corrections applied bin-by-bin

Rad/NoRad



Higher $\theta_{\pi q}$

Higher P_π

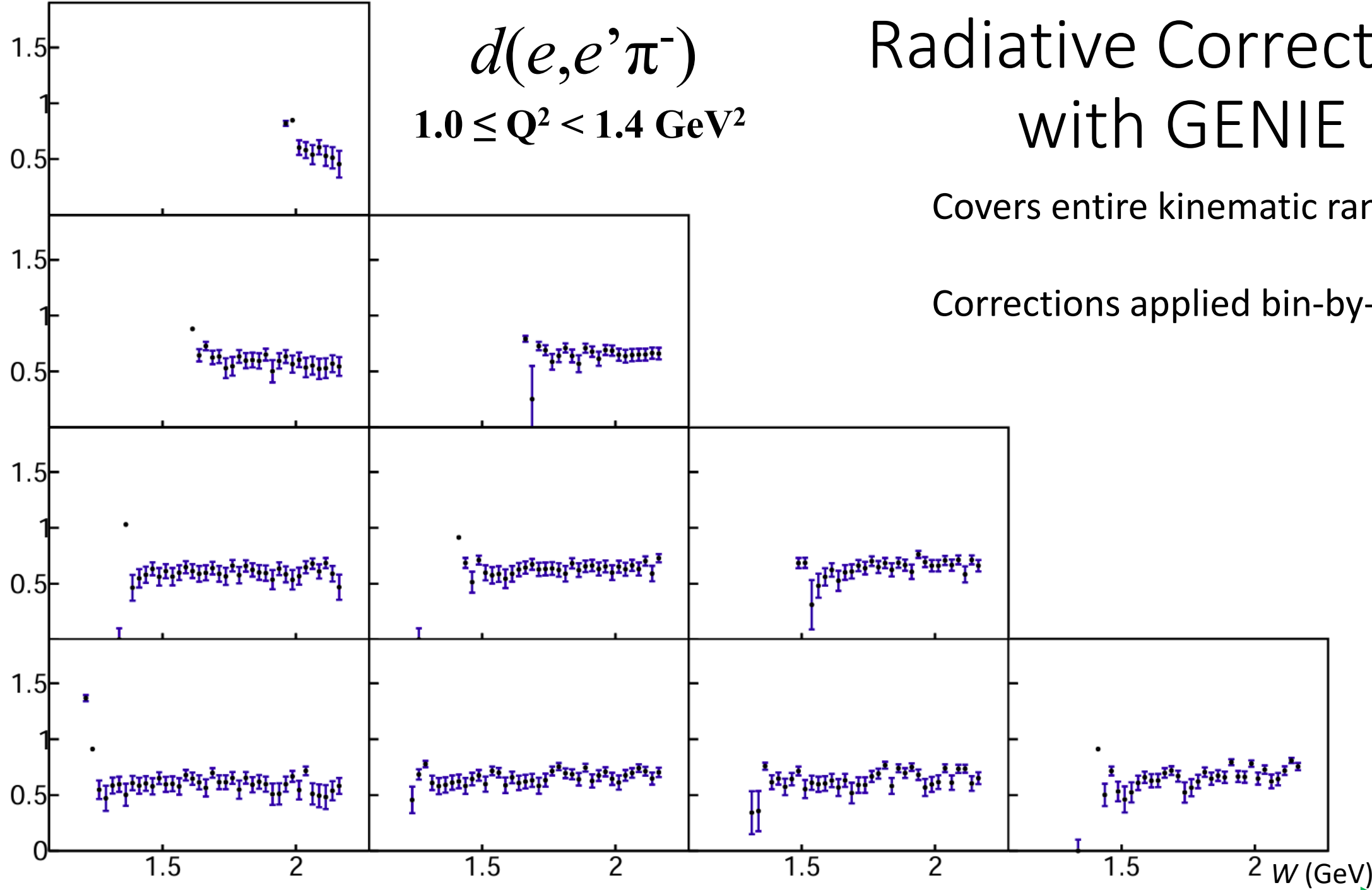
Rad/NoRad

$$d(e, e' \pi^-)$$
$$1.0 \leq Q^2 < 1.4 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

Corrections applied bin-by-bin



Higher P_π

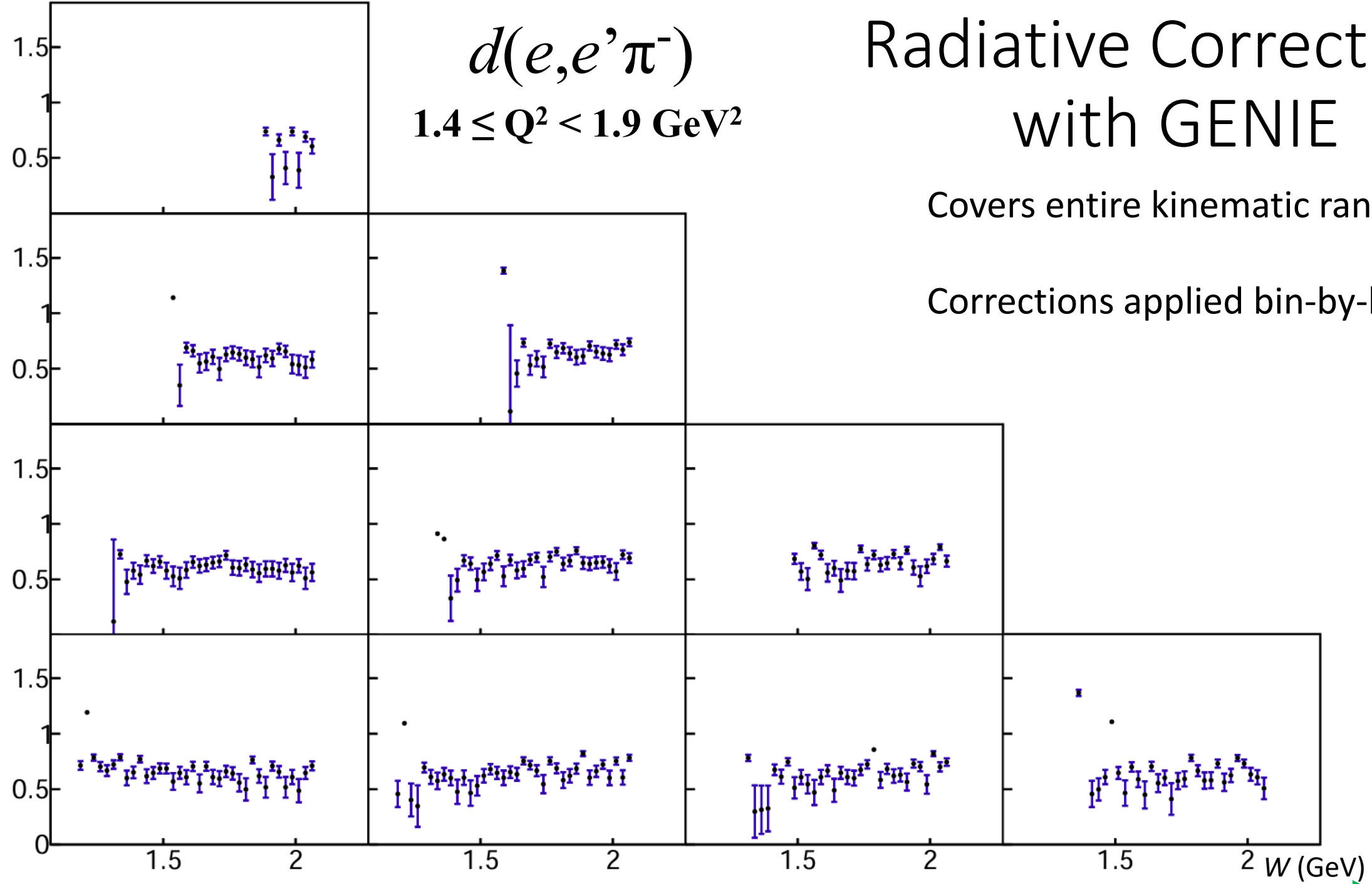
Rad/NoRad

$$d(e, e' \pi^-)$$
$$1.4 \leq Q^2 < 1.9 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

Corrections applied bin-by-bin



Higher P_π

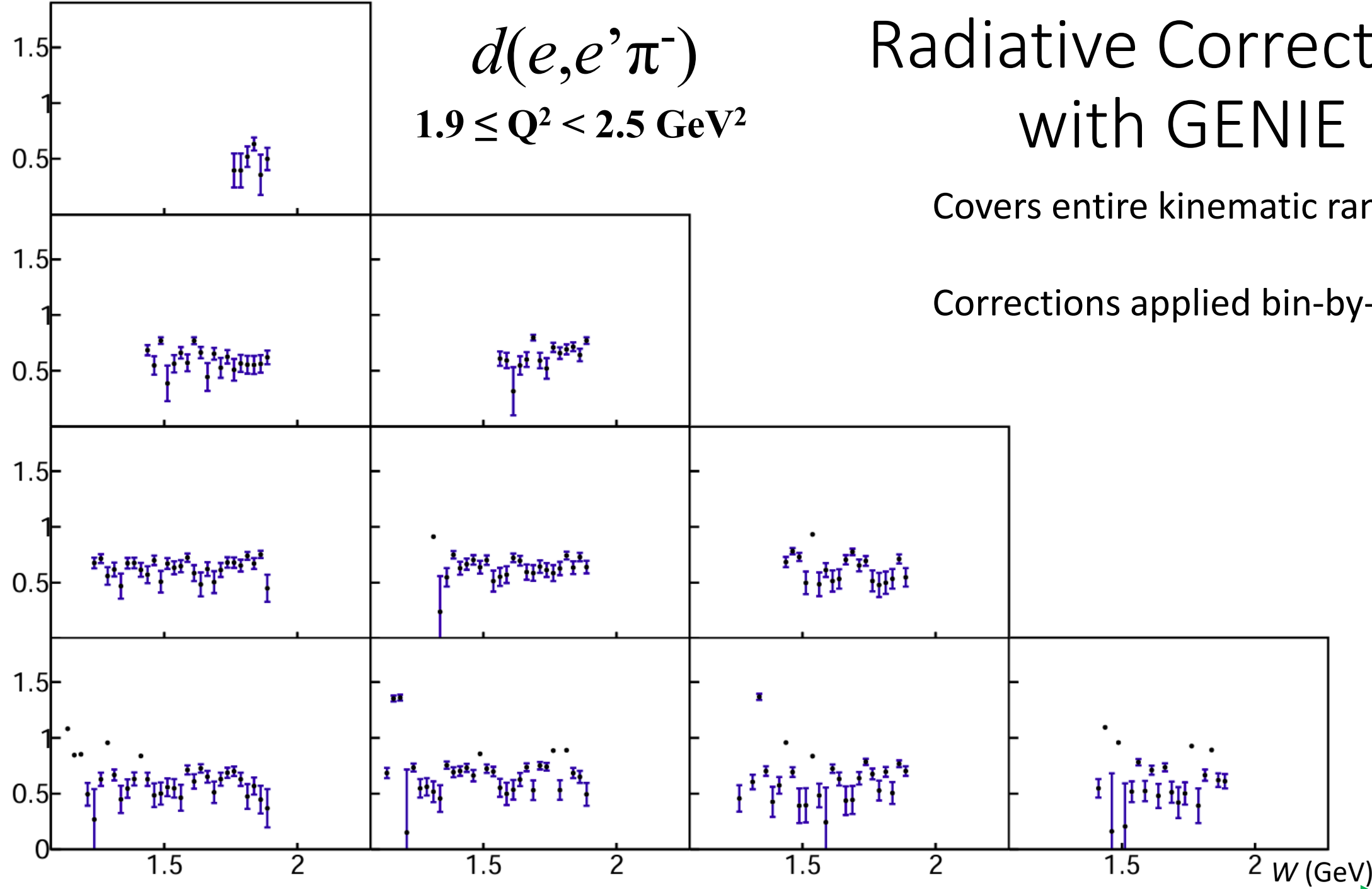
Rad/NoRad

$$d(e, e' \pi^-)$$
$$1.9 \leq Q^2 < 2.5 \text{ GeV}^2$$

Radiative Corrections with GENIE

Covers entire kinematic range

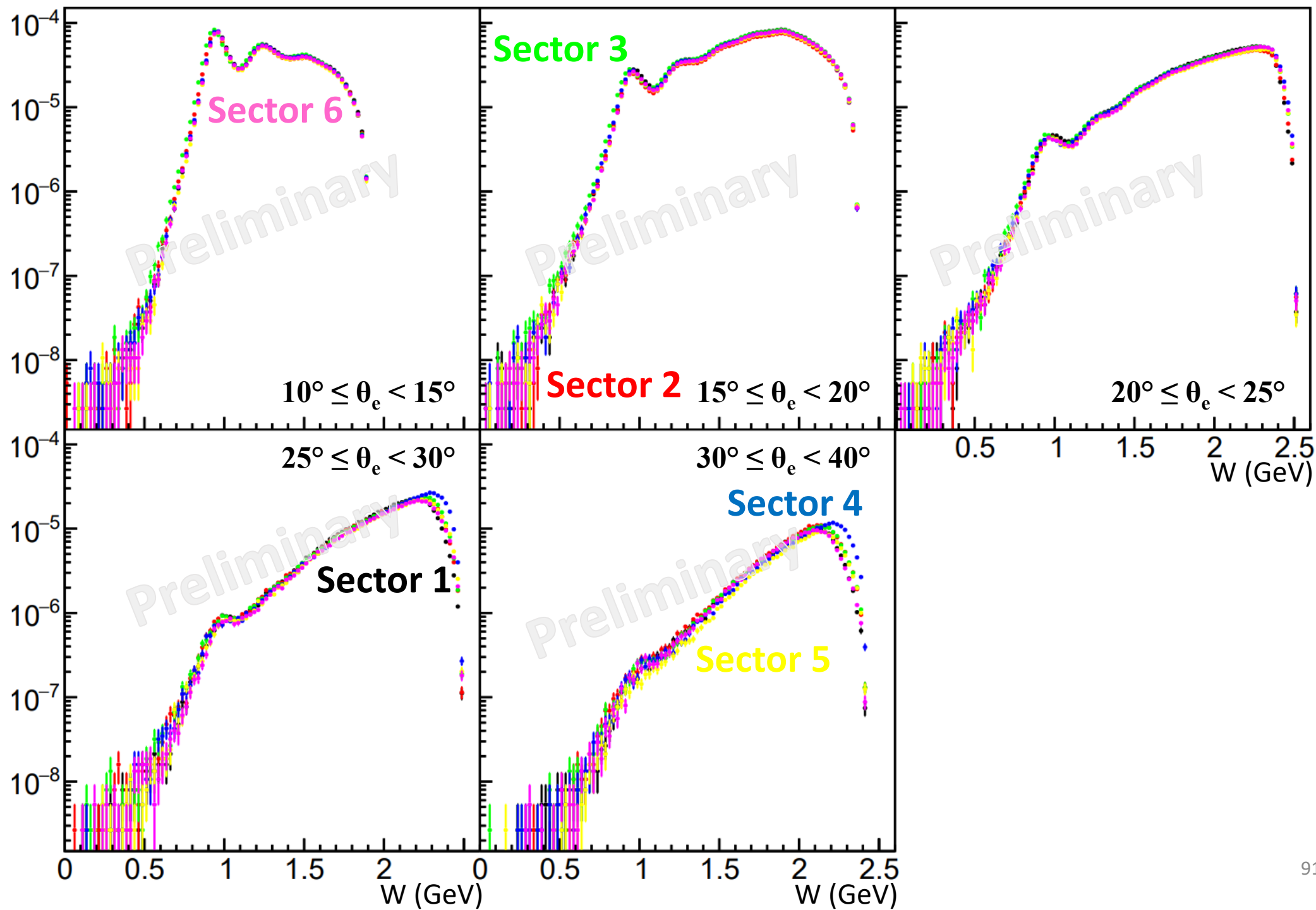
Corrections applied bin-by-bin



Higher $\theta_{\pi q}$

$d(e,e')$

Uncorrected Inclusive Cross Sections



Systematic Uncertainty

- Inclusive sector

$$SysUnc_{sec} = \sqrt{var}$$

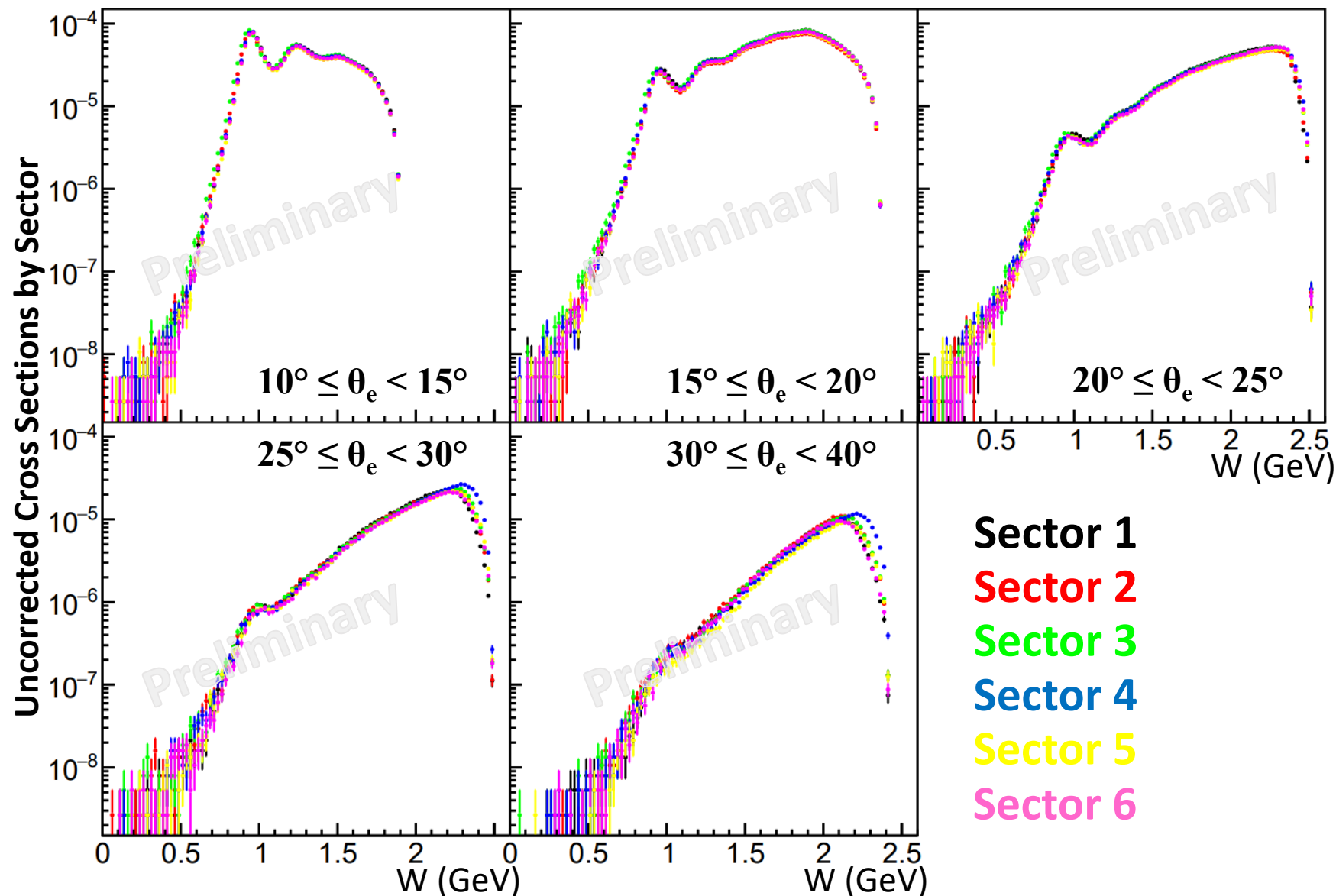
$$var = \frac{1}{5} \sum_i^{sec} (y_i - \bar{y})^2 - \frac{1}{6} \sum_i^{sec} \sigma_i^2$$

y_i = data point for sector i

$$\bar{y} = \frac{1}{6} \sum_i^{sec} y_i = \text{ave. for all sectors}$$

σ_i = statistical uncertainty of y_i

$d(e, e')$



Used similar procedure for semi-inc. cross sections

All sectors divided
by Sector 1

$$SysUnc_{sec} = \sqrt{var}$$

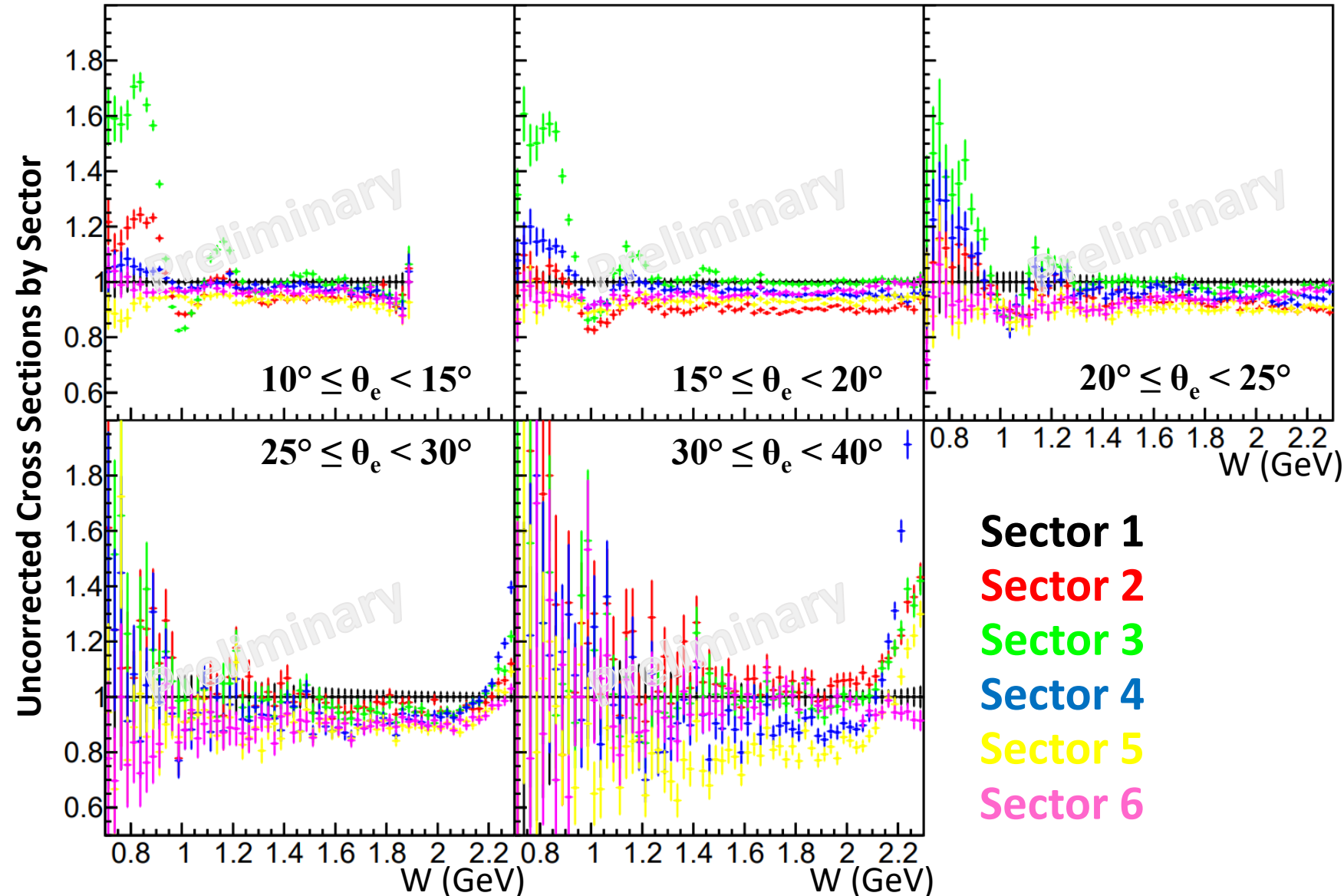
$$var = \frac{1}{5} \sum_i^{sec} (y_i - \bar{y})^2 - \frac{1}{6} \sum_i^{sec} \sigma_i^2$$

y_i = data point for sector i

$$\bar{y} = \frac{1}{6} \sum_i^{sec} y_i = \text{ave. for all sectors}$$

σ_i = statistical uncertainty of y_i

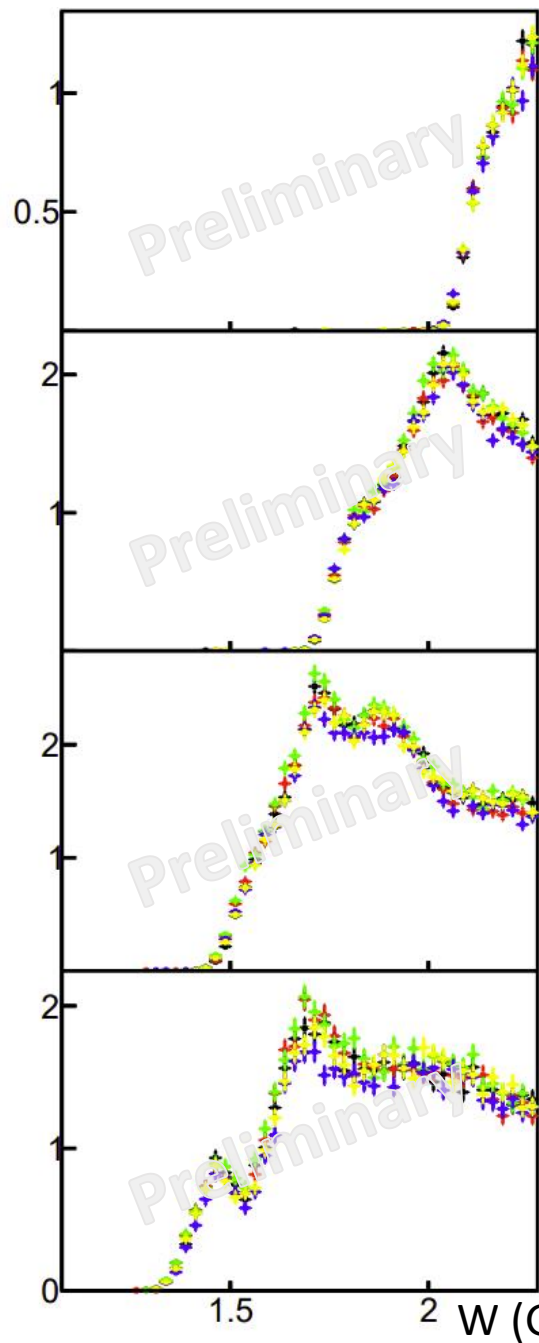
$d(e, e')$



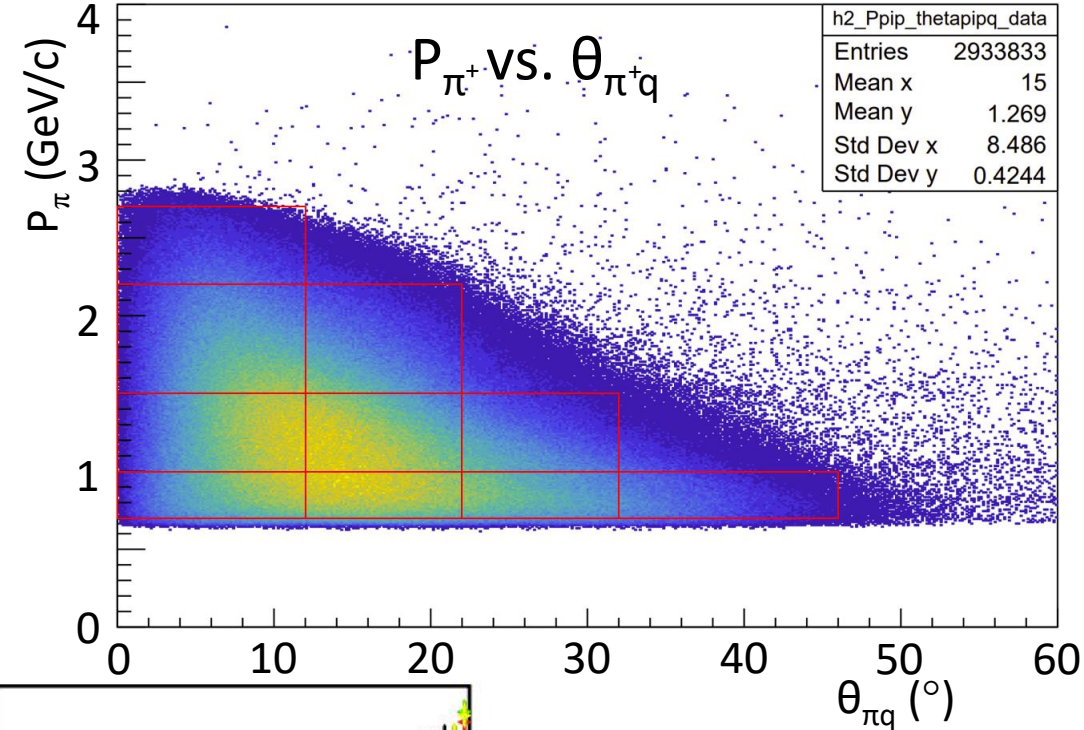
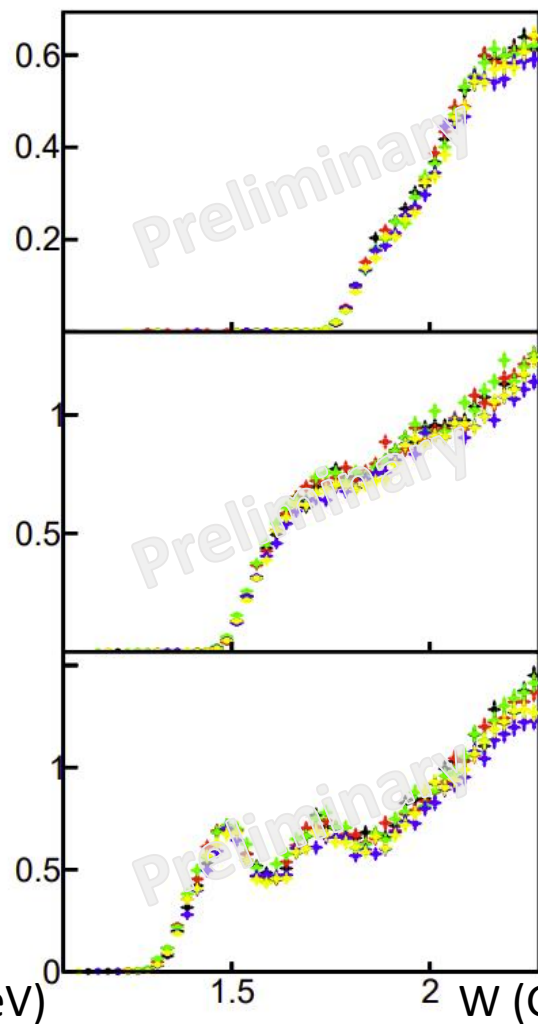
Used similar procedure for semi-inc. cross sections

Higher P_π

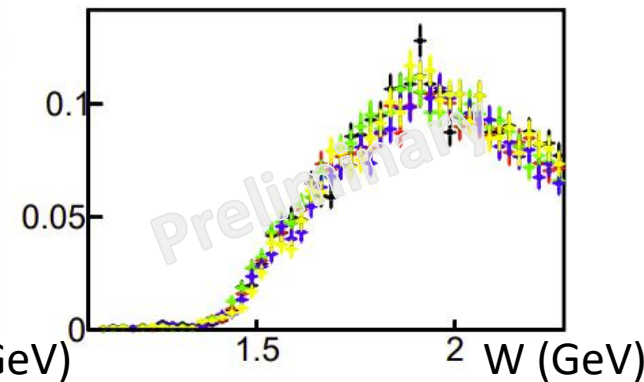
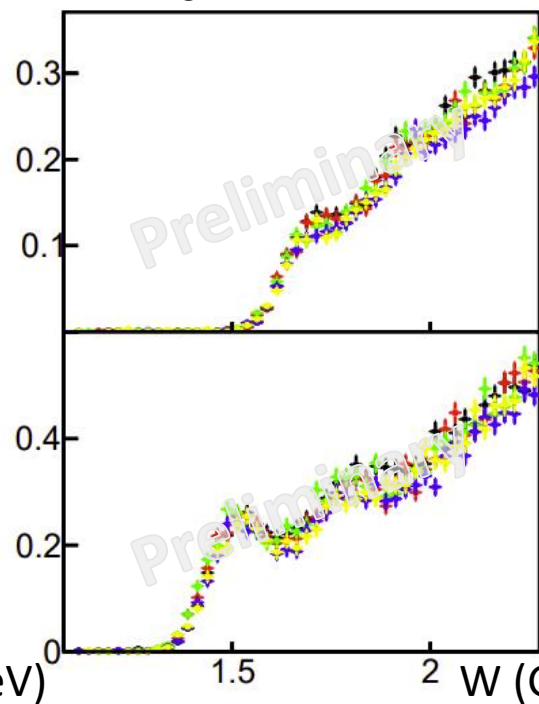
Uncorrected Cross Sections by Sector



$$d(e, e' \pi^+)$$
$$0.7 \leq Q^2 < 1.0 \text{ GeV}^2$$



Sector 1 **Sector 5**
Sector 2 **Sector 6**
Sector 3

Higher $\theta_{\pi q}$