

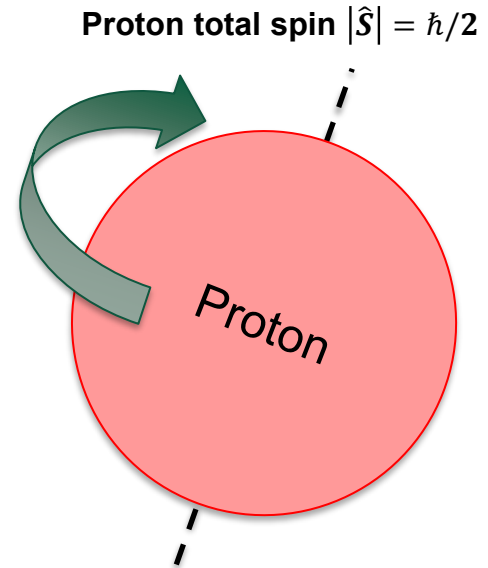
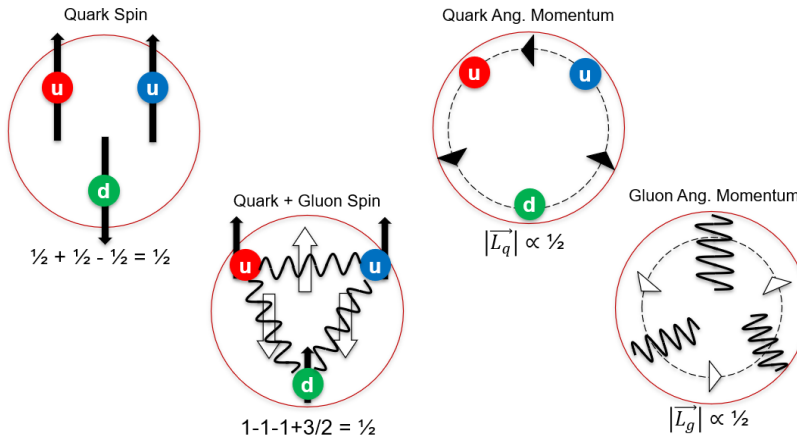
Proton Spin Structure in Run Group C

Derek Holmberg
7-9-25

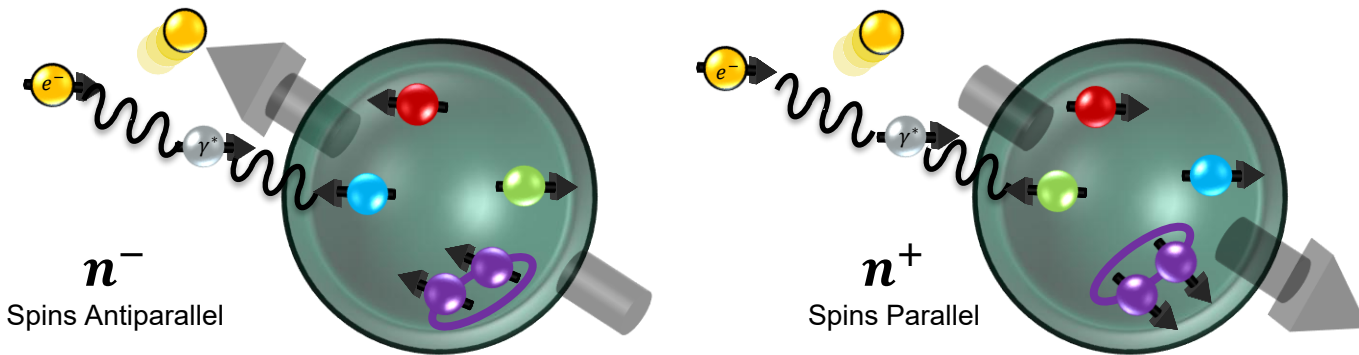


Where Does the Proton Spin Come From?

- Total proton spin $\frac{1}{2} = \text{quark spin} + \text{gluon spin} + \text{quark orbital momentum} + \text{gluon orbital momentum}$
- Quark spin contribution depends on polarized parton distribution functions (PDFs)
- **Polarized PDF:** $\Delta q_i(x) = q_i^\uparrow(x) - q_i^\downarrow(x)$
- $g_1(x) = \frac{1}{2} \sum_i e_i^2 \Delta q_i(x) \propto \frac{1}{2} \left[\frac{4}{9} \Delta u(x) + \frac{1}{9} \Delta d(x) + \frac{1}{9} \Delta s(x) + \dots \right]$
- Probed through polarized electron-proton scattering



Polarized ep Scattering



- Protons are polarized either parallel or antiparallel to the beam electrons' spins
- Deep inelastic scattering (DIS): electrons scatter off individual quarks ($Q^2 > 1 \text{ GeV}^2$, $W > 2 \text{ GeV}$)
- Scattering conserves spin (angular momentum), so any asymmetry between $n^\pm$ is related to spin structure

$$A_{||}(x, Q^2) = \frac{n^- - n^+}{n^- + n^+} = D(A_1(x, Q^2) + \eta A_2(x, Q^2))$$

- With $A_1, A_2 =$ virtual photon asymmetries

$$A_1(x, Q^2) \propto \frac{g_1(x, Q^2)}{F_1(x, Q^2)} = \frac{\sum_i e_i^2 \Delta q_i(x, Q^2)}{\sum_i e_i^2 q_i(x, Q^2)}$$

The CLAS12 Detector

- Inclusive electron scattering: $ep \rightarrow eX$, $ed \rightarrow eX$
- Consider electrons in the Forward Detector (FD): Drift chambers, ECAL, HTCC
- Electron EB PID:
 - Negative track in the DC (inbending data)
 - $E_{PCAL} > 60 \text{ MeV}$
 - Photoelectrons in HTCC $nphe > 2$
- Deep inelastic kinematic cuts:
 - $Q^2 > 1 \text{ GeV}^2$, $W > 2 \text{ GeV}$,
 - $E' > 2.6 \text{ GeV}$ (minimize radiative effects)
- Fiducial cuts (work in progress):
 - $-10 \text{ cm} < V_Z < 2 \text{ cm}$, $5^\circ < \theta < 40^\circ$, $|\chi_{PID}^2| < 3$
 - Investigating DC edge variable cut (edge $> 5 \text{ cm}$)
 - Investigating ECAL lu, lv, lw strip cuts

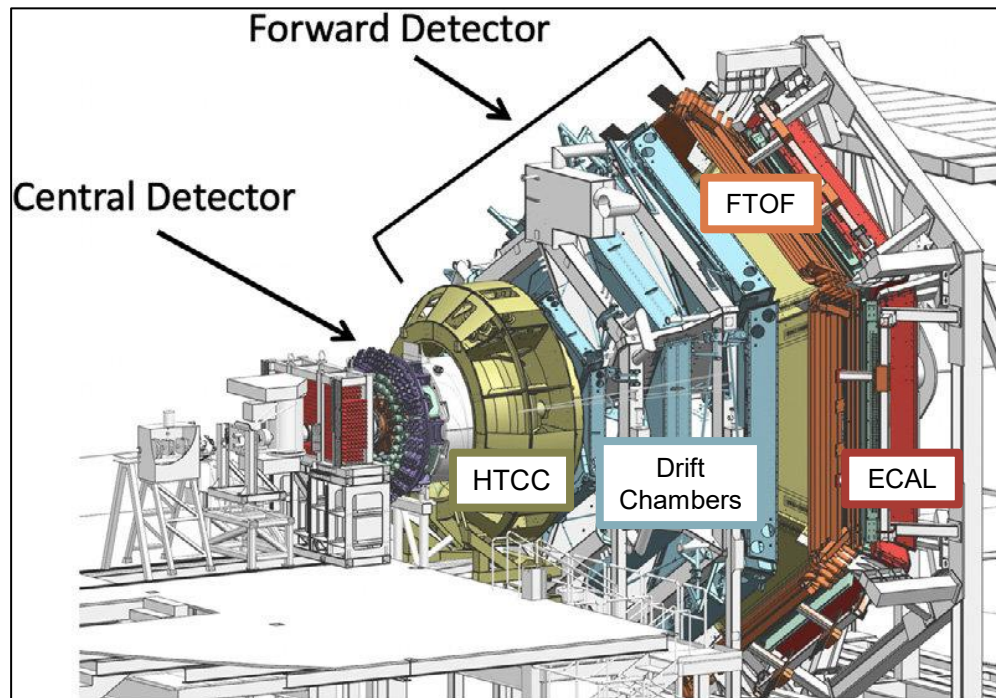


Diagram of CLAS12 Detector, Ziegler et. al.

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- Run Group C polarized target

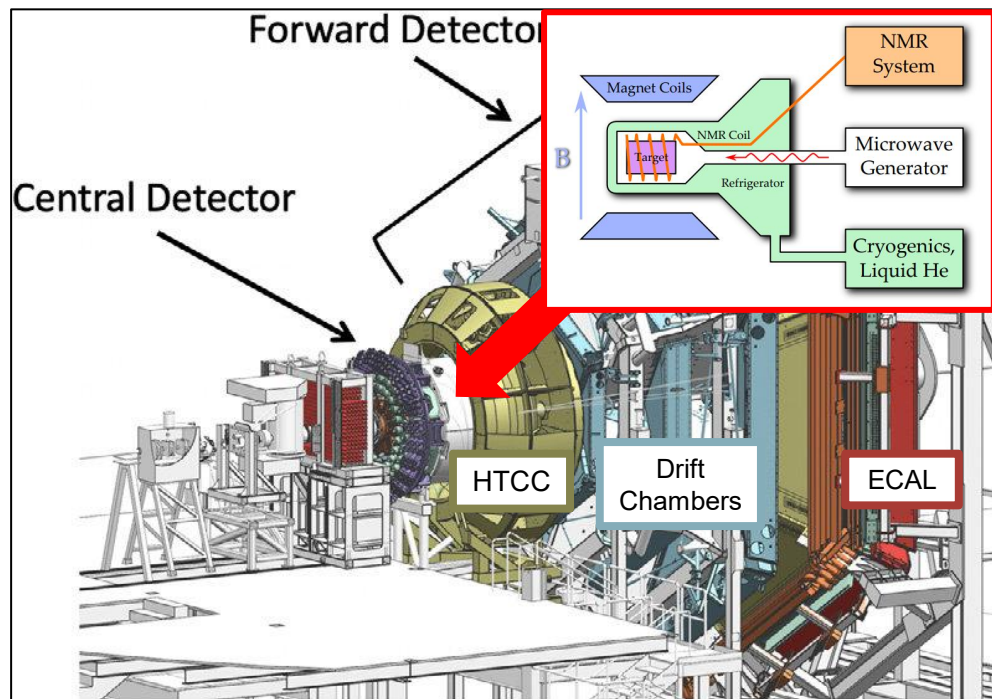
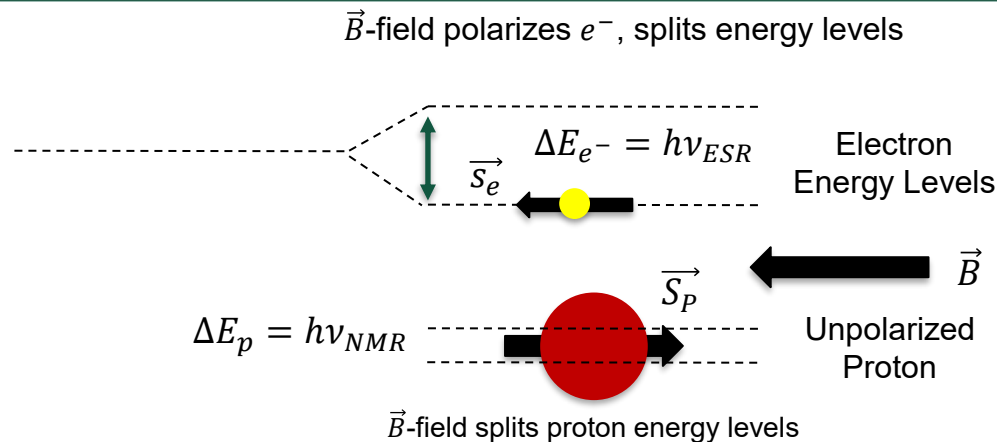
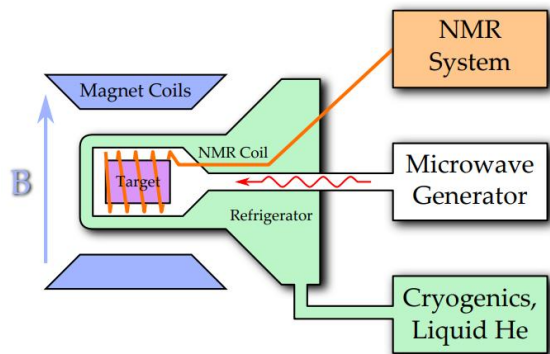


Diagram of CLAS12 Detector, Ziegler et. al.

Run Group C Polarized Target



Ammonia crystals unexposed to beam (left), crystals after beam exposure (right). Purple color from paramagnetic centers.

- Target material: frozen ammonia crystals
- Ammonia chosen for use in dynamic nuclear polarization
- Expose crystals to beam, creating free electron paramagnetic centers in target
- Cool to ~1 K in a 5 T field generated by solenoid, where free electrons almost completely polarize, but protons don't
- Exposing target to microwaves with a frequency of $\nu_{ESR} \pm \nu_{NMR}$ (~140 GHz), polarization of the electrons is transferred to the protons (or deuterons)
- ~90% for protons, ~40% for deuterons

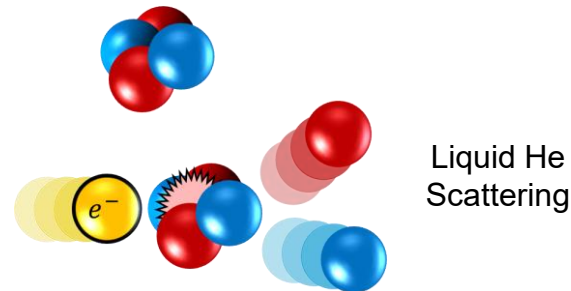
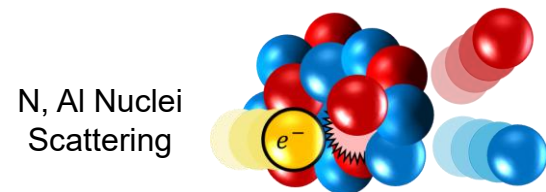
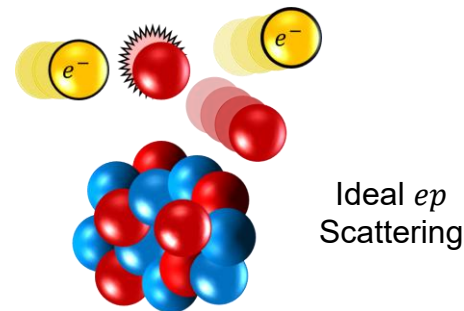
Unpolarized Background

- In addition to polarized scattering in the target, there's a large source of unpolarized background: N, Al, He nuclei in target/bath
- Reduces measured $A_{||}$, and cannot be removed with vertex/kinematic cuts
- Quantified using a dilution factor D_F

$$D_F = \frac{Y_H}{Y_{Ammonia}} = \frac{3\sigma_H \ell_H \rho_H}{3\sigma_H \ell_H \rho_H + \sigma_N \ell_N \rho_N + \sigma_{He} \ell_{He} \rho_{He} + \sigma_{Al} \ell_{Al} \rho_{Al}}$$

- Imperfect polarization of beam electrons and target particles: $P_b P_t$
- Dividing $A_{||}$ by D_F and $P_b P_t$ accounts for the background

$$A_{||,phys} = \frac{A_{||,raw}}{D_F P_b P_t} \propto A_1$$



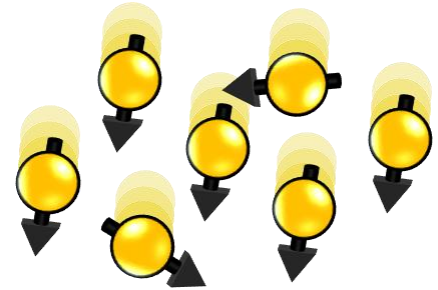
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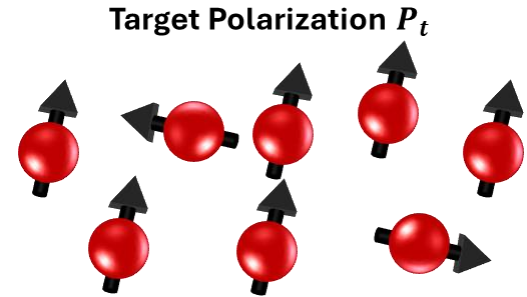
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Beam Electron Polarization P_b



Target Polarization P_t

Calculating the Dilution Factor

- Advantageous to write D_F in terms of scattering counts from background targets instead of cross sections

- $n_A \propto \sigma_{Al} + \sigma_{He} + \frac{7}{6}\sigma_C + \sigma_H$, where $\frac{7}{6}\sigma_C \approx \sigma_N$

- $n_{MT} \propto \sigma_{Al} + \sigma_{He}$

- $n_C \propto \sigma_{Al} + \sigma_{He} + \sigma_C$

- $n_{CH} \propto \sigma_{Al} + \sigma_{He} + \sigma_C + \sigma_H$

- $n_F \propto \sigma_{Al}$

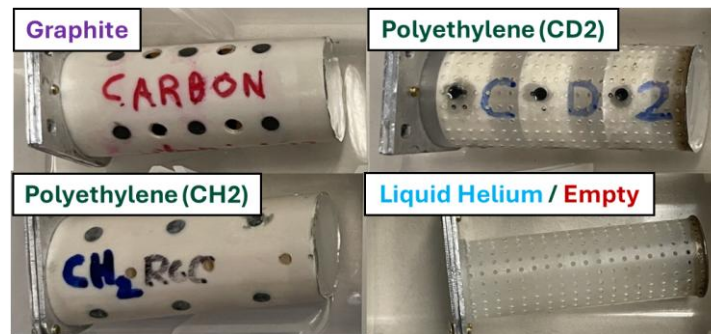
- Solving for cross sections and rewriting the D_F yields

$$D_F(x, Q^2) = P_F \frac{C_1 n_C + C_2 n_{MT} + C_3 n_{CH} + C_4 n_F}{C_5 n_A}$$

- Packing fraction P_F is the target volume fraction occupied by the ammonia crystals

$$P_F(x, Q^2) = \frac{D_1(n_A - n_{MT})}{D_2 n_{MT} + D_3 n_C + D_4 n_{CH} + D_5 n_F}$$

$$C_i, D_i \propto \ell_i, \rho_i \text{ of target materials}$$



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- $n_C \propto \sigma_{Al} + \sigma_{He} + \sigma_C$

- $n_{CH} \propto \sigma_{Al} + \sigma_{He} + \sigma_C + \sigma_H$

- $n_F \propto \sigma_{Al}$

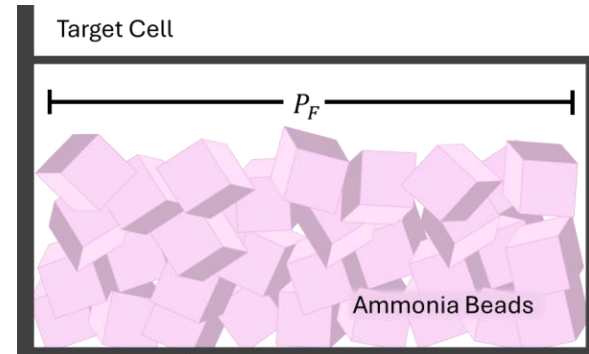
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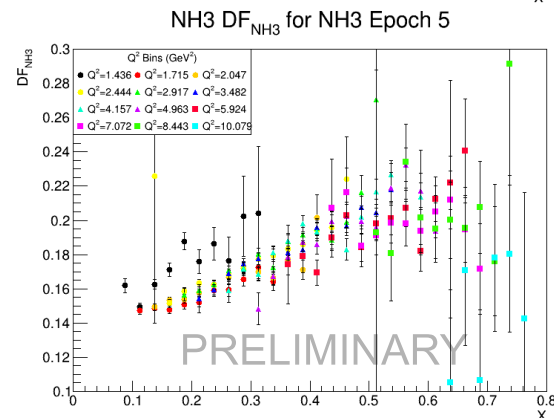
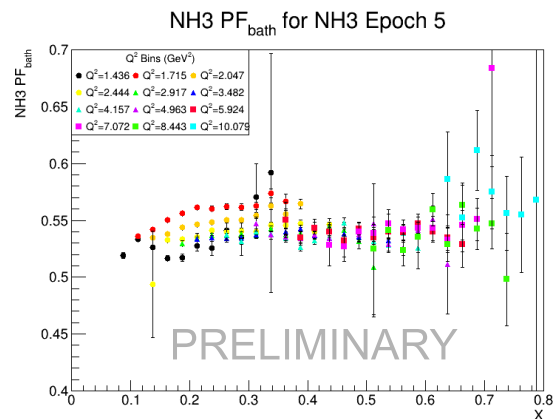
$$P_F(x, Q^2) = \frac{D_1(n_A - n_{MT})}{D_2 n_{MT} + D_3 n_C + D_4 n_{CH} + D_5 n_F}$$

$C_i, D_i \propto \ell_i, \rho_i$ of target materials



Calculating the Dilution Factor

- Two methods are used to calculate the dilution factor: a data-driven method and a model of the dilution factor
- Data-driven method:
 - Measure n_A n_{MT} n_C n_{CH} n_F from the data
 - Use these values to calculate a value of P_F for each x, Q^2 bin
 - Calculate a weighted average of all P_F
 - Use this $P_{F,avg}$ as an input to calculate D_F for each x, Q^2 bin
- Requires a radiation length correction to empty n_{MT} and foil n_F counts (haven't found a suitable model yet)
- Modeled dilution factor:
 - From modeled structure functions, "build" each target and simulate the counts n_A n_{MT} n_C n_{CH} n_F coming from the target
 - Allows for EMC effect, fermi motion, and radiative corrections to be built-in to the model
 - See Darren Upton's talk next for more details!
- Requires as an input values of P_F that must come from data



Preliminary Results

- Calculated preliminary D_F for the RGC dataset
- Datasets are broken up into different “epochs” that have different packing fraction
- D_F binned in x for each epoch
- Once D_F are calculated, use them to get $P_b P_t$

Summer 2022
Runs

Epoch 2: Runs 16137 – 16178
Epoch 3: Runs 16211 – 16260
Epoch 4: Runs 16318 – 16357
Epoch 5: Runs 16658 – 16695
Epoch 6: Runs 16709 – 16738
Epoch 7: Runs 16742 – 16772

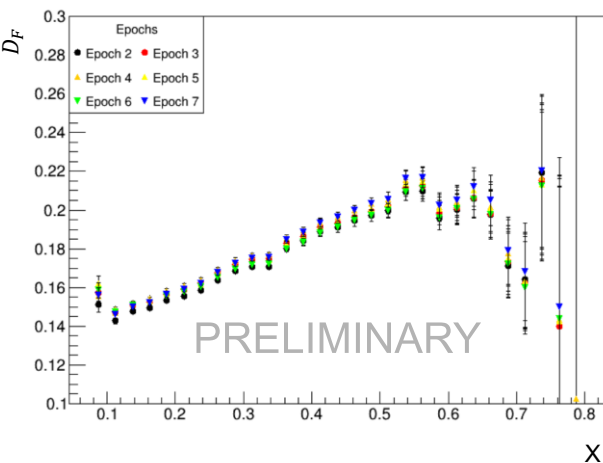
Fall 2022
Runs

Epoch 8: Runs 16982 – 16995
Epoch 9: Runs 16996 – 17032
Epoch 10: Runs 17067 – 17102
Epoch 11: Runs 17144 – 17169
Epoch 12: Runs 17185 – 17225
Epoch 13: Runs 17353 – 17368
Epoch 14: Runs 17371 – 17382

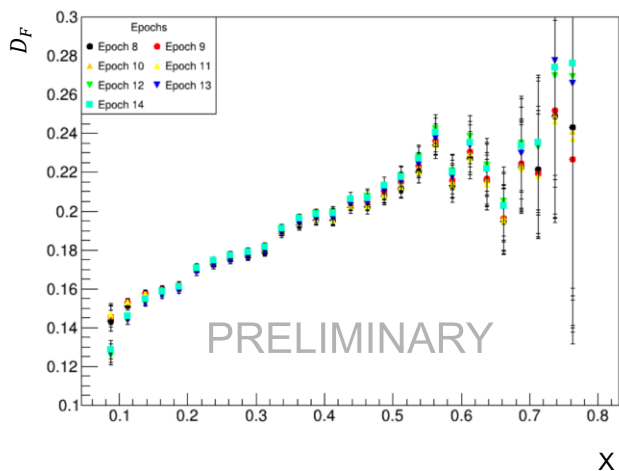
Spring 2023
Runs

Epoch 15: Runs 17575 – 17597
Epoch 16: Runs 17598 – 17617
Epoch 17: Runs 17720 – 17741
Epoch 18: Runs 17748 – 17762

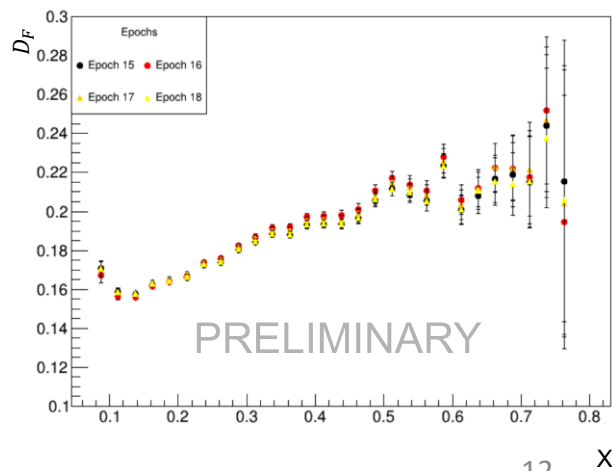
Summer 2022 D_F Data



Fall 2022 D_F Data



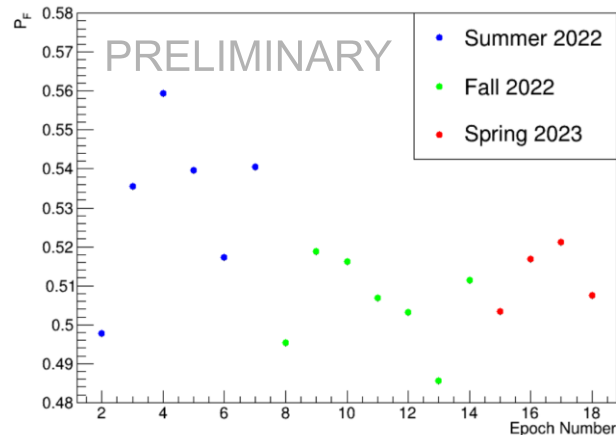
Spring 2023 D_F Data



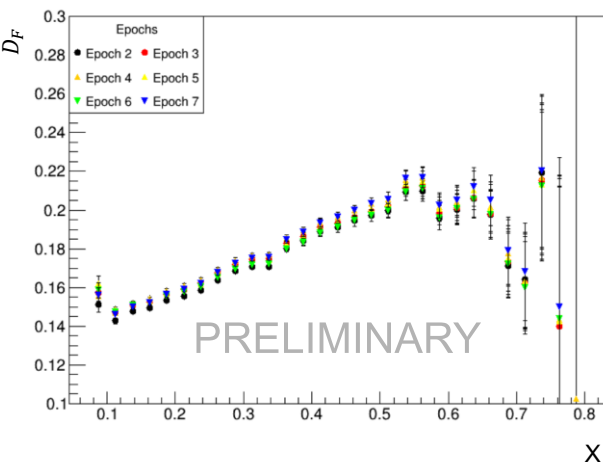
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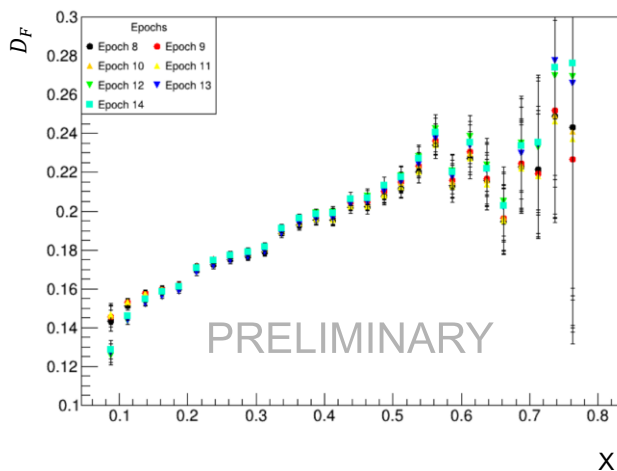
Packing Fractions for RGC Epochs



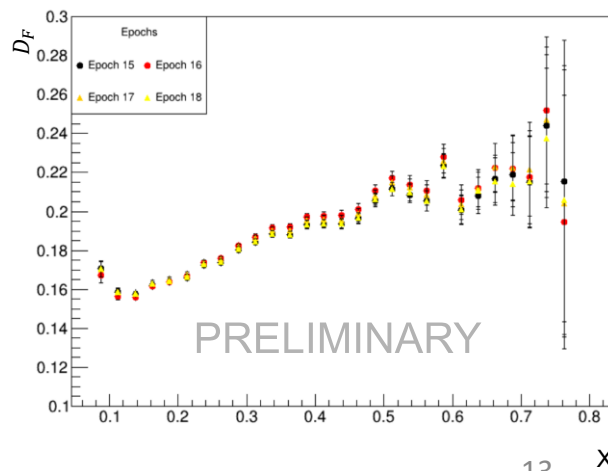
Summer 2022 D_F Data



Fall 2022 D_F Data



Spring 2023 D_F Data



Beam-Target Polarization Calculations

$$A_{||,phys} = \frac{A_{||,raw}}{D_F P_b P_t} \Rightarrow P_b P_t = \frac{A_{||,raw}}{D_F A_{||,phys}}$$

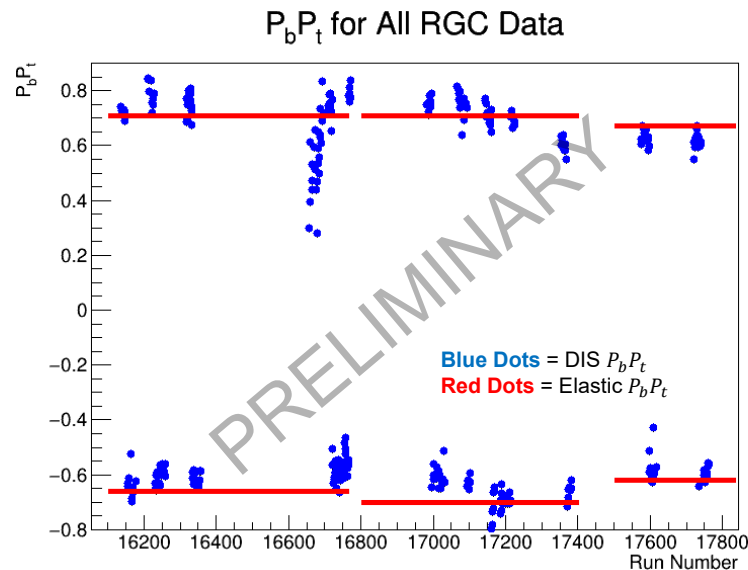
- Use a model to calculate $A_{||,phys}$
- Values of $P_b P_t$ were calculated for RGC data using exclusive elastic $ep \rightarrow e'p'$ scattering (Noemie Pilleux)

$$P_b P_t = \frac{\sum_{Q^2 \text{ bins}} d_{f,i} A_{th,i} (n_i^- - n_i^+)}{\sum_{Q^2 \text{ bins}} d_{f,i}^2 A_{th,i}^2 (n_i^- + n_i^+)}$$

- d_f = separate dilution factor, A_{th} = elastic asymmetry parameterized by Arrington et. al.
- For DIS $P_b P_t$, calculated in x, Q^2 bins using $A_{th} = D(A_1 + \eta A_2)$, with Values of D, η, A_1, A_2 come from S. Kuhn 's model
- Much greater statistics than elastic

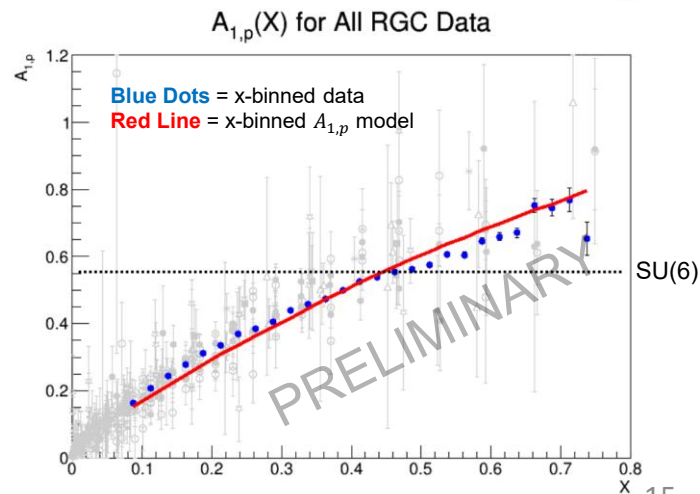
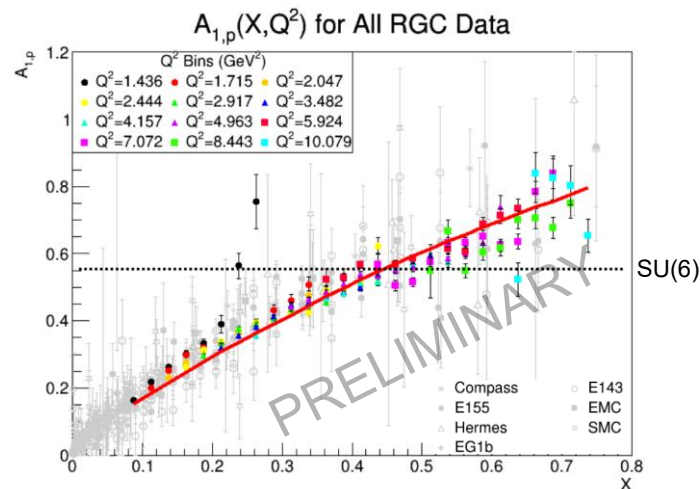
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Normalize DIS $P_b P_t$ to elastic $P_b P_t$ to avoid circular calculation!



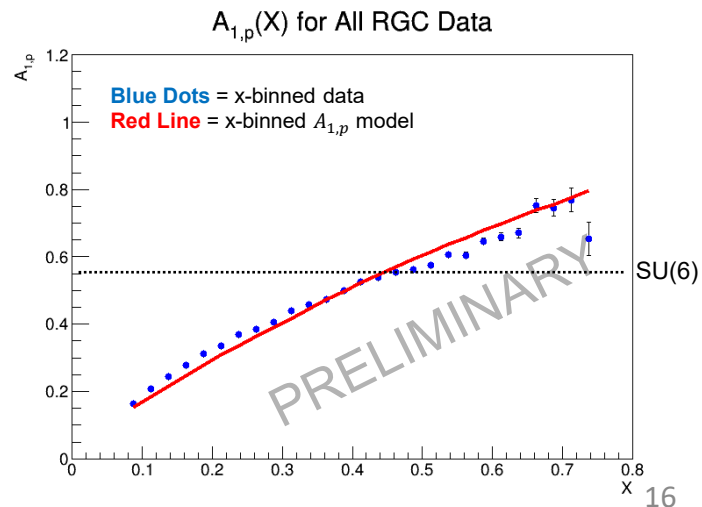
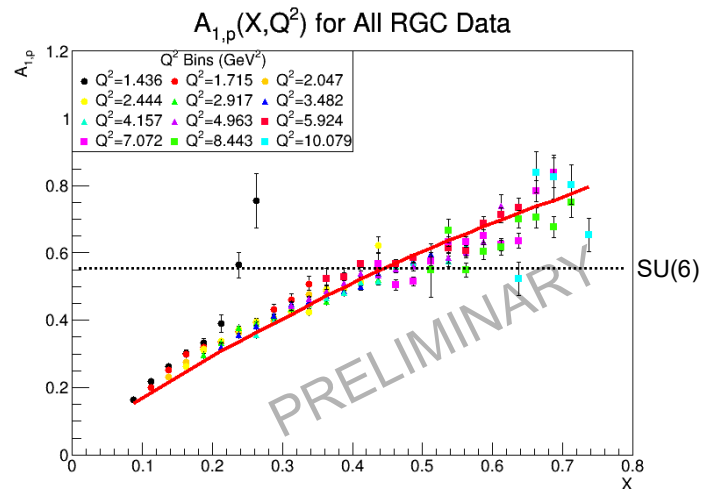
Preliminary Results

- To calculate $A_{1,p}$, rearrange $A_{||,phys} = D(A_1 + \eta A_2)$
- $A_1 = A_{||,phys}/D - \eta A_2$, with D, η, A_2 from S. Kuhn's model
- Values of η, A_2 are small for DIS kinematics, so smaller effects from model
- Spring 2023 data excludes outbending runs
- Data fluctuates around model values of $A_{1,p}$
- Slight dip at large x for Fall 2022 data
- Currently, we don't have data-driven $A_{1,d}$ results due to issues with calculating the ND3 D_F



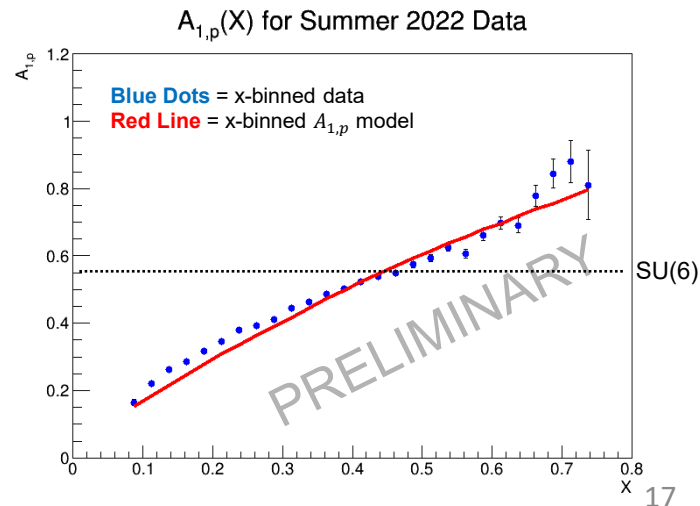
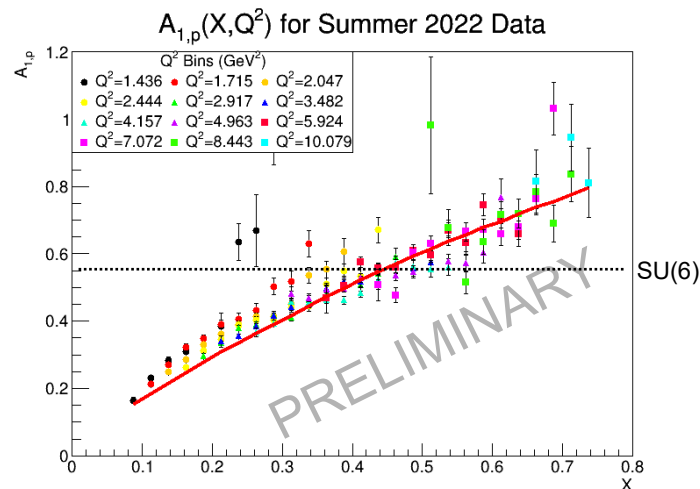
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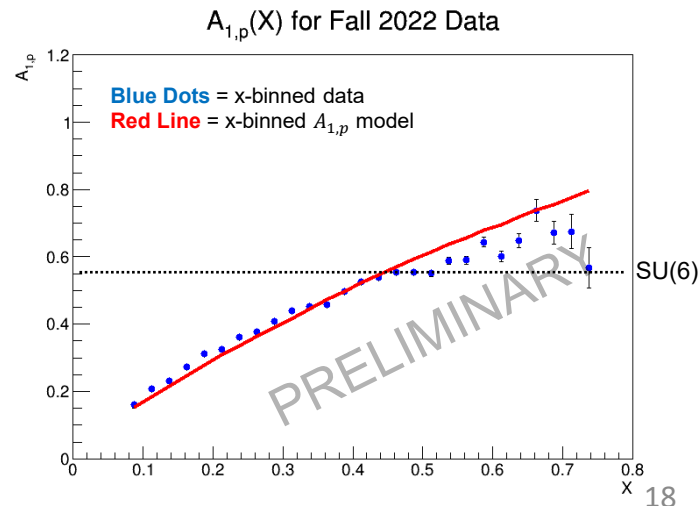
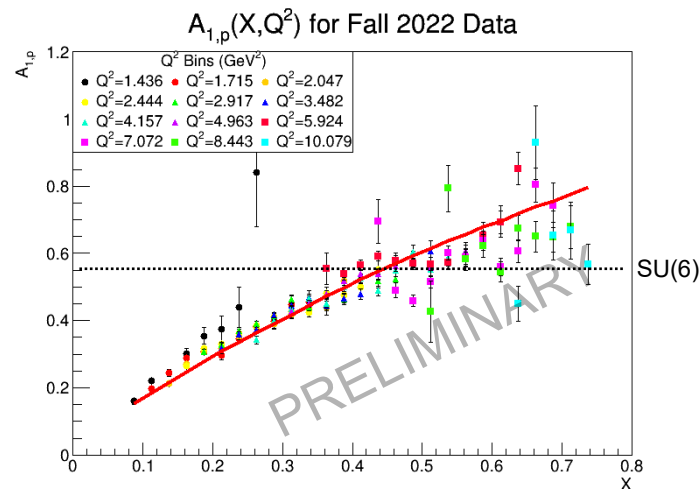
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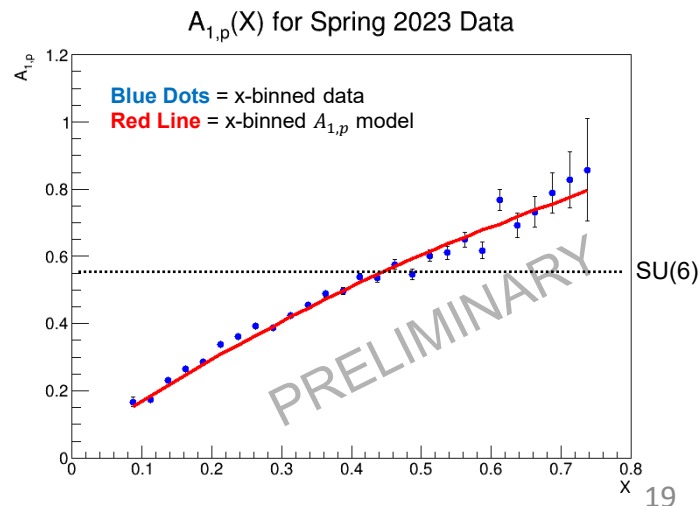
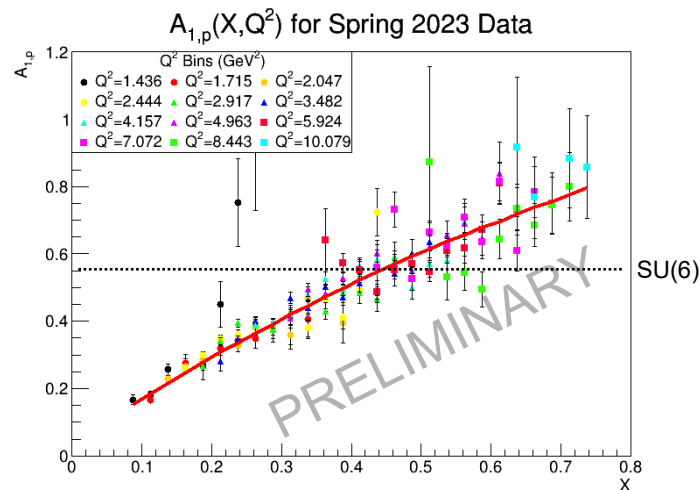
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Work Left To Do

- Study accuracy of thermal contractions applied to target geometries
- Incorporate radiation length corrections to n_{MT} , n_F counts
- Subtract background from misidentified π^- , e^+e^- pair production
- Correct $P_b P_t$ for polarized ^{14}N in target
- Figure out why low Q^2 looks so rough

- Finalize the D_F model-driven approach

- Fiducial Cuts
 - Cuts on DC hit position (either local θ , ϕ variables and/or edge variable cuts)
 - Cuts on ECAL hit position and sampling fraction values

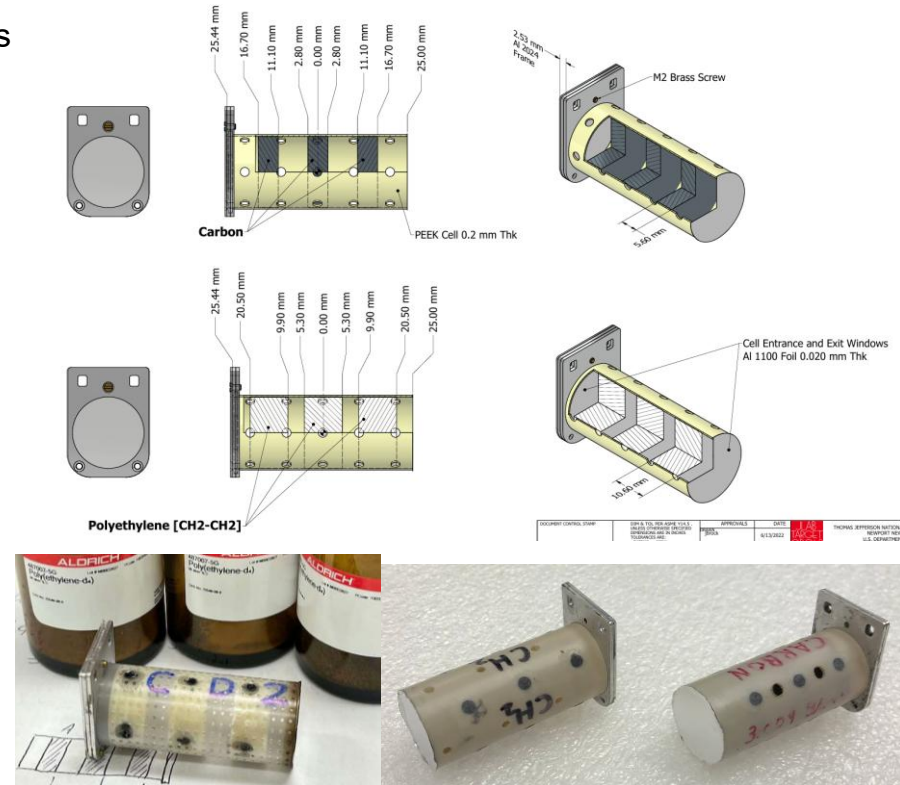
- Any Questions?

Backup Slides

- Thermal expansion corrections to targets
- Data Quality Per Q^2 Bin
- All D_F and P_F for NH3 targets across all x, Q^2 bins
- All D_F and P_F for ND3 targets across all x, Q^2 bins

Thermal Contraction of Targets

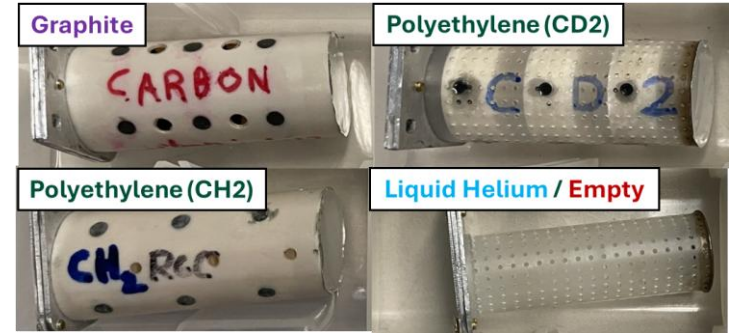
- Studying the impact of thermal contraction of the target cells on the dilution factor
- Carbon, CH₂, CD₂ targets' geometry measured at room temperature, cooled to ~1K, so there's some contraction of target length
- Modulate the sizes of the targets as follows:
 - $\ell_C * (1 - dL_C/L_C)$, with $dL_C/L_C = 0.5\%$
 - $\ell_{CH} * (1 - dL_{CH}/L_{CH})$, with $dL_{CH}/L_{CH} = 2.1\%$
 - $\ell_{CD} * (1 - dL_{CH}/L_{CH})$
 - $L * (1 - 0.018)$ (for Teflon contraction, 1.8%)
 - $\rho_C / (1 - dL_{CH}/L_{CH})^3$
 - $\rho_{CH} / (1 - dL_{CH}/L_{CH})^3$
 - $\rho_{CD} / (1 - dL_{CH}/L_{CH})^3$
 - ρ_A, ρ_D are unchanged



Calculating the Dilution Factor

- Advantageous to write D_F in terms of scattering counts from background targets instead of cross sections

- $n_A \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} (L - \ell_A) \rho_{He} + \left(\frac{7}{6} \sigma_C + 3 \sigma_H\right) \ell_A \rho_A$
- $n_{MT} \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} L \rho_{He}$
- $n_C \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} (L - \ell_C) \rho_{He} + \sigma_C \ell_C \rho_C$
- $n_{CH} \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} (L - \ell_{CH}) \rho_{He} + (\sigma_C + 2 \sigma_H) \ell_{CH} \rho_{CH}$
- $n_F \propto \sigma_{Al} \ell_{Al} \rho_{Al}$



- Solving for cross sections and rewriting the D_F yields

$$D_F(x, Q^2) = P_F \frac{3\rho_A}{2n_A \rho_C \rho_{CH}} \left(\frac{L}{\ell_{CH}} \rho_C (n_{CH} - n_{MT}) + (\rho_C - \rho_{CH}) (n_{MT} - n_F) - \frac{L}{\ell_C} \rho_{CH} (n_C - n_{MT}) \right)$$

- Packing fraction P_F is the target volume fraction occupied by the ammonia crystals

$$P_F(x, Q^2) = \frac{6 \ell_C \rho_C \ell_{CH} \rho_{CH} (n_A - n_{MT})}{2 \ell_{CH} \rho_{CH} L \rho_A (n_{MT} - n_C) + 9 \ell_C \rho_C L \rho_A (n_{CH} - n_{MT}) + \ell_C \ell_{CH} (n_{MT} - n_F) (9 \rho_A \rho_C - 2 (\rho_A + 3 \rho_C) \rho_{CH})}$$

Calculating the Dilution Factor

- Advantageous to write D_F in terms of scattering counts from background targets instead of cross sections

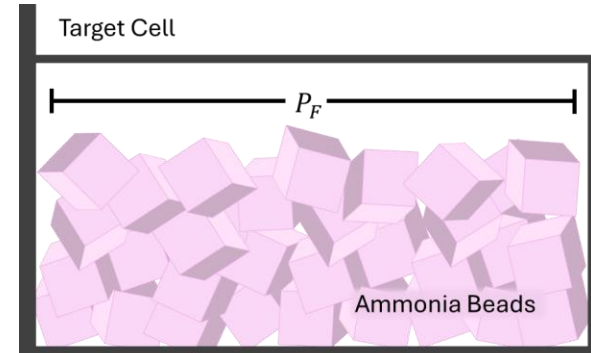
- $n_A \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} (L - \ell_A) \rho_{He} + \left(\frac{7}{6} \sigma_C + 3 \sigma_H\right) \ell_A \rho_A$
- $n_{MT} \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} L \rho_{He}$
- $n_C \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} (L - \ell_C) \rho_{He} + \sigma_C \ell_C \rho_C$
- $n_{CH} \propto \sigma_{Al} \ell_{Al} \rho_{Al} + \sigma_{He} (L - \ell_{CH}) \rho_{He} + (\sigma_C + 2 \sigma_H) \ell_{CH} \rho_{CH}$
- $n_F \propto \sigma_{Al} \ell_{Al} \rho_{Al}$

- Solving for cross sections and rewriting the D_F yields

$$D_F(x, Q^2) = P_F \frac{3\rho_A}{2n_A \rho_C \rho_{CH}} \left(\frac{L}{\ell_{CH}} \rho_C (n_{CH} - n_{MT}) + (\rho_C - \rho_{CH})(n_{MT} - n_F) - \frac{L}{\ell_C} \rho_{CH} (n_C - n_{MT}) \right)$$

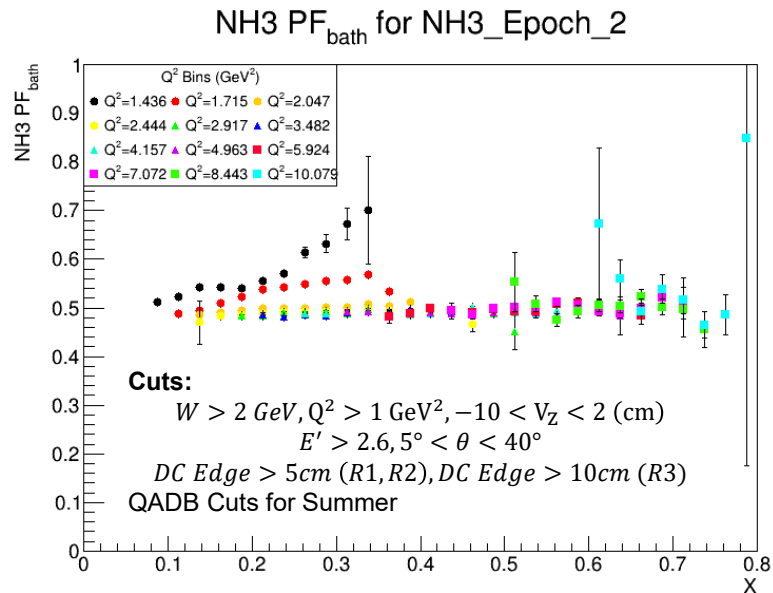
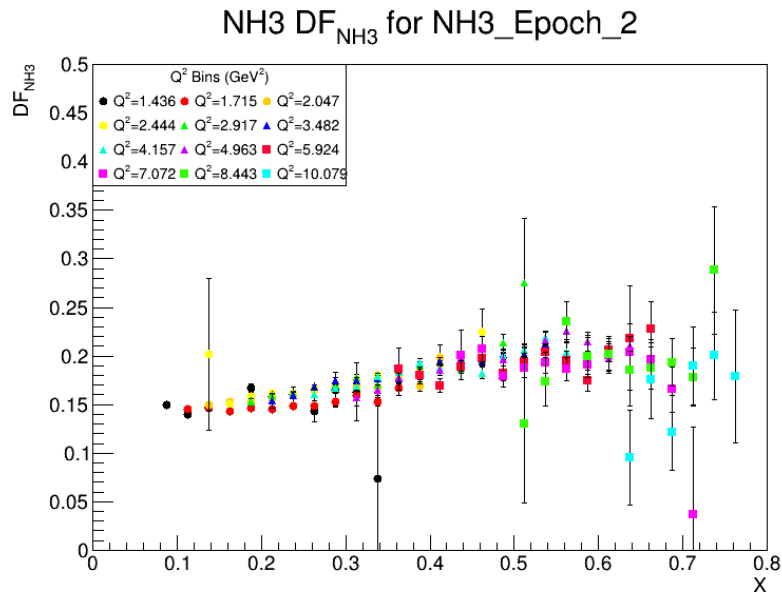
- Packing fraction P_F is the target volume fraction occupied by the ammonia crystals

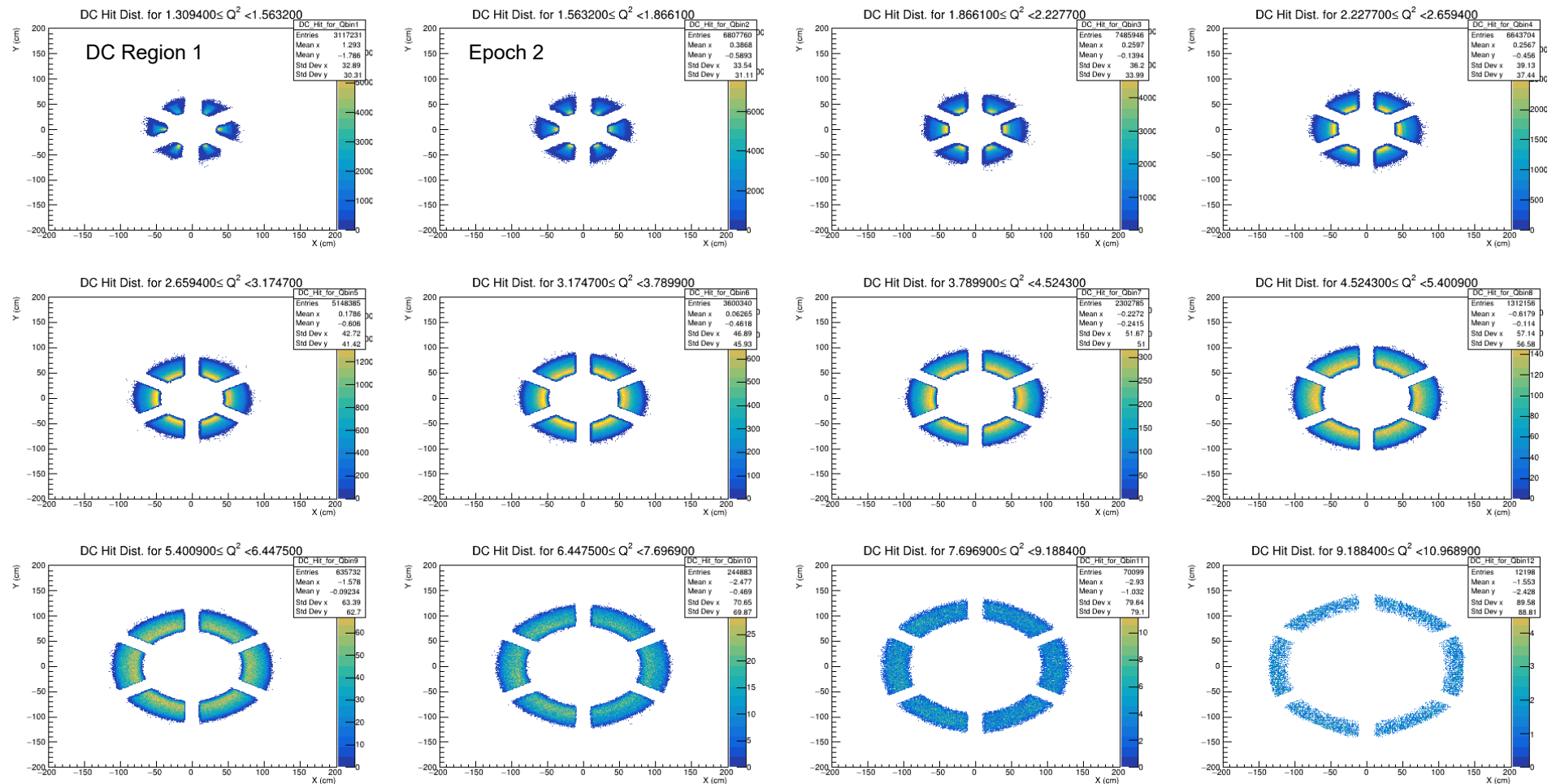
$$P_F(x, Q^2) = \frac{6 \ell_C \rho_C \ell_{CH} \rho_{CH} (n_A - n_{MT})}{2 \ell_{CH} \rho_{CH} L \rho_A (n_{MT} - n_C) + 9 \ell_C \rho_C L \rho_A (n_{CH} - n_{MT}) + \ell_C \ell_{CH} (n_{MT} - n_F) (9 \rho_A \rho_C - 2(\rho_A + 3 \rho_C) \rho_{CH})}$$

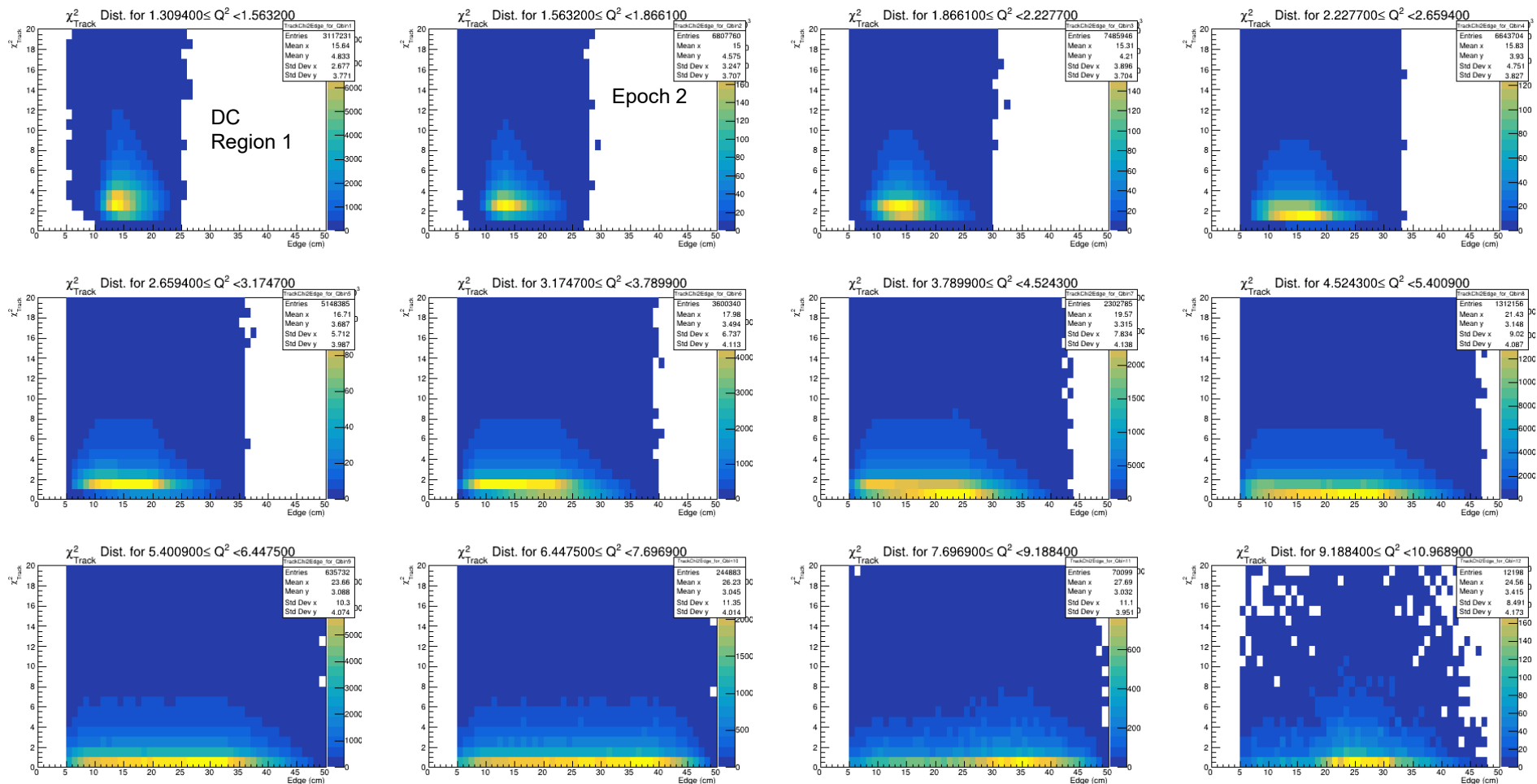


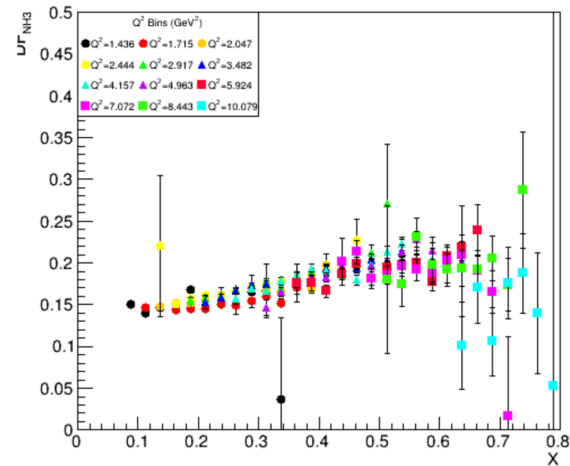
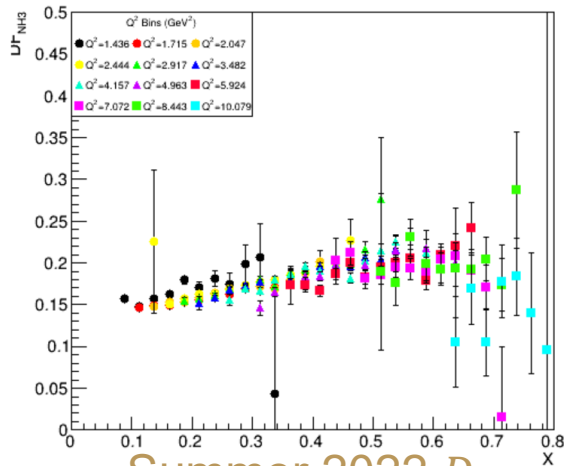
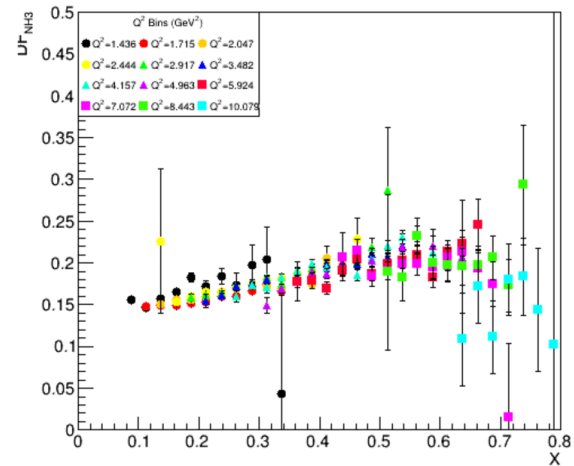
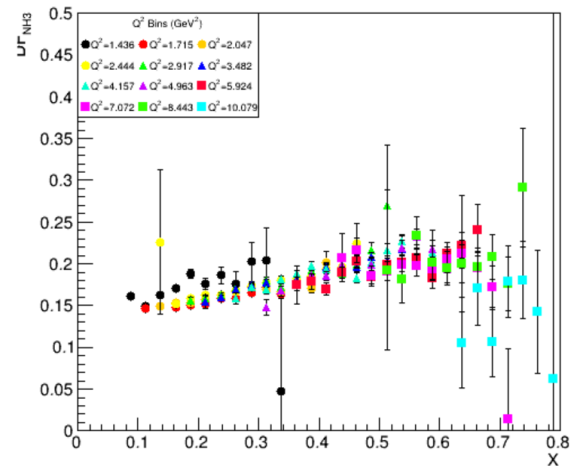
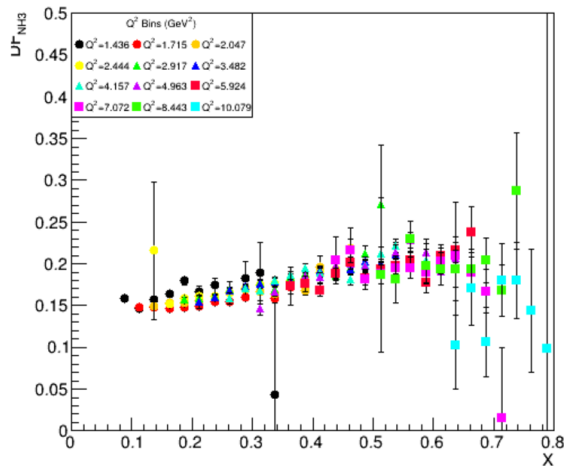
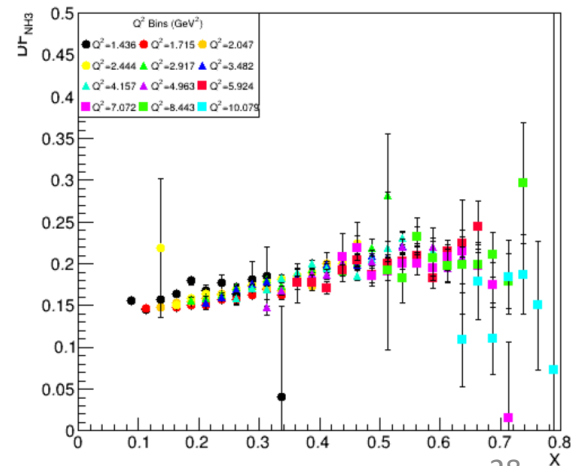
Data Quality Per Q^2 Bin

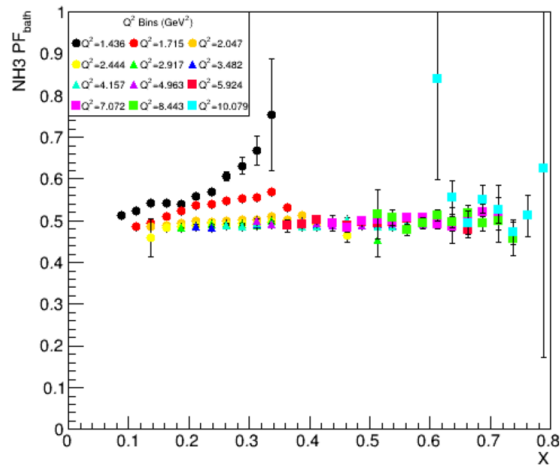
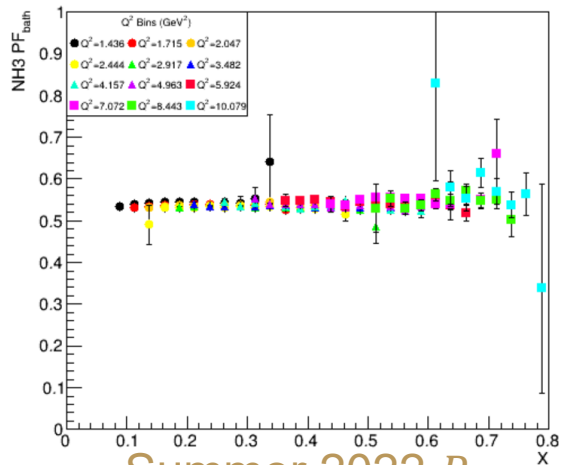
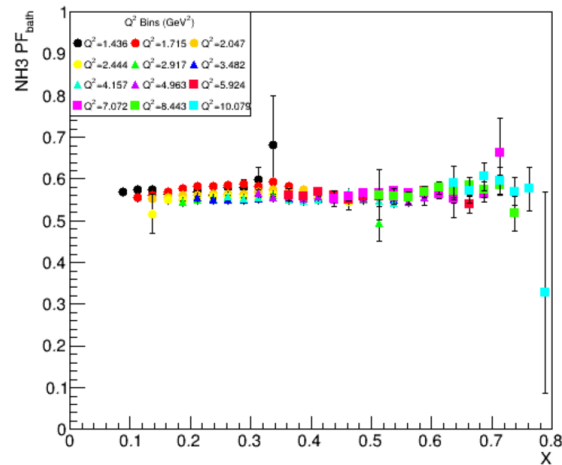
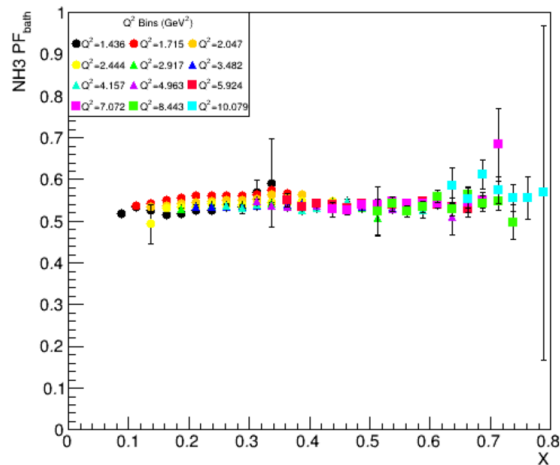
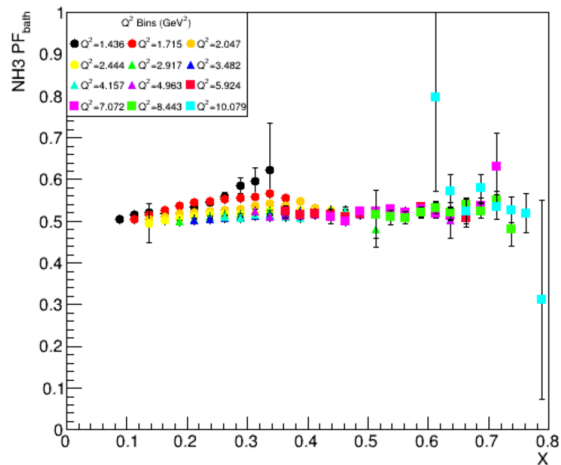
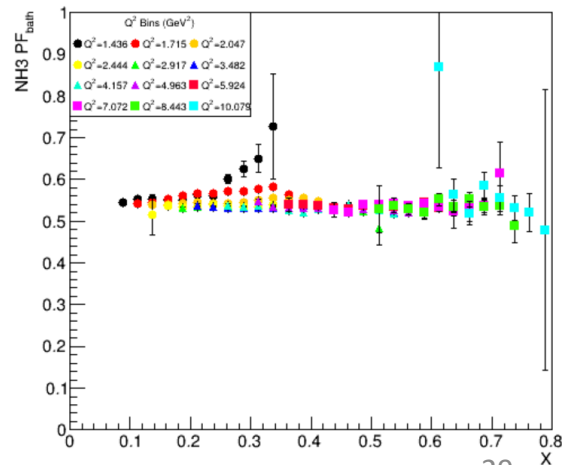
- Issue with CLAS12 data: inconsistent behavior of D_F , P_F in low Q^2 bins of data
- Plotted DC hit position, χ^2_{track}/NDF vs. edge, θ distributions for each bin in Q^2

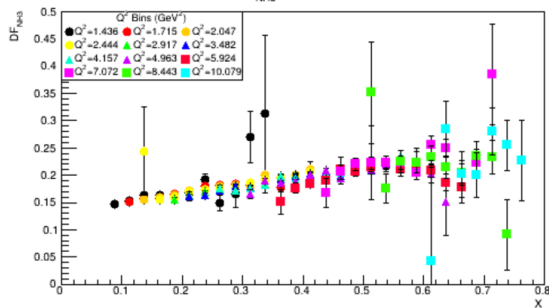
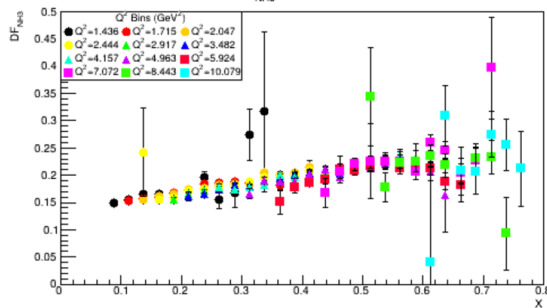
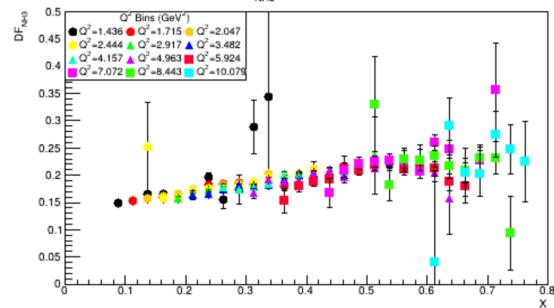
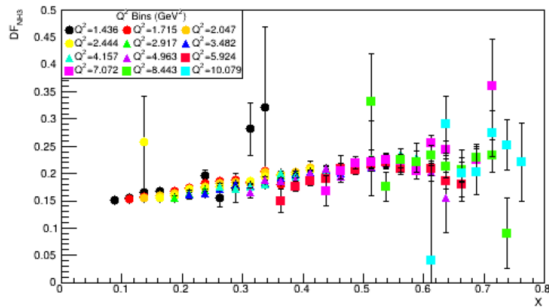
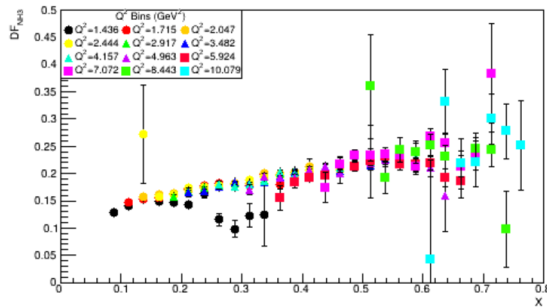
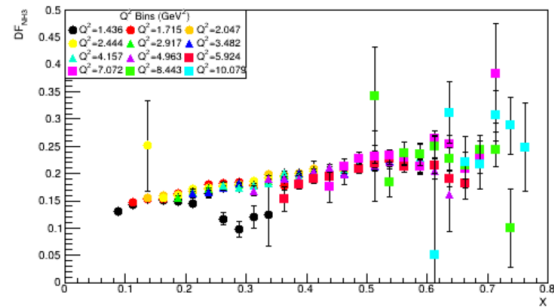
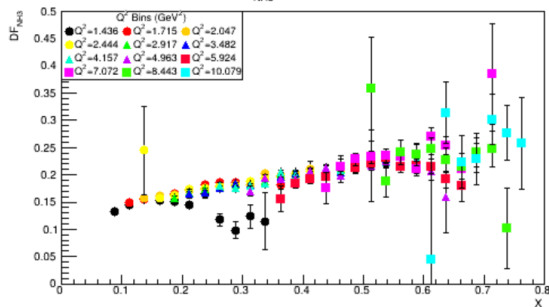


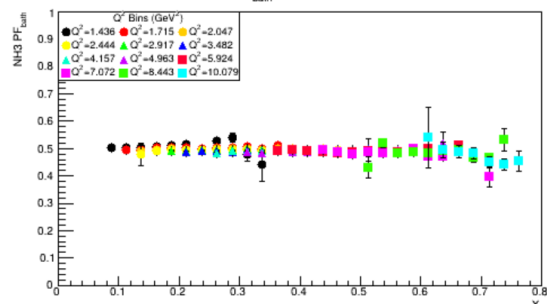
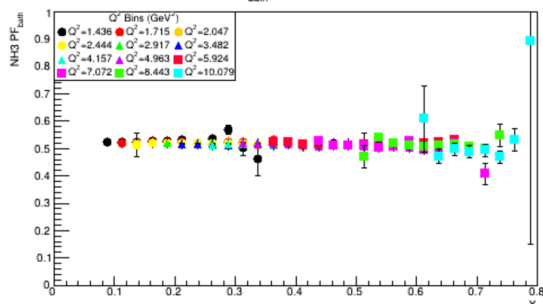
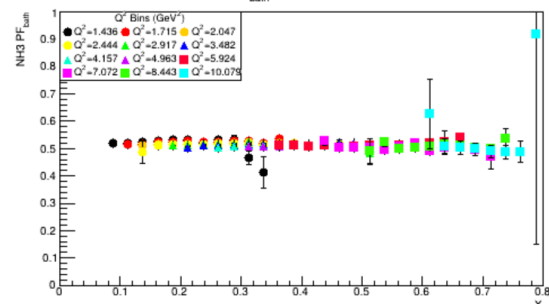
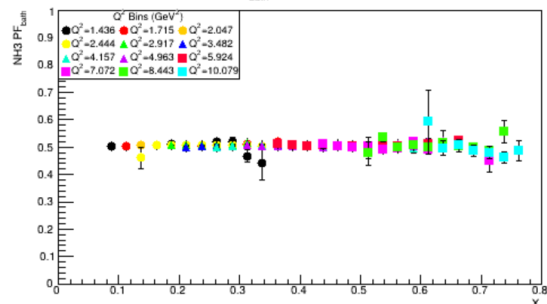
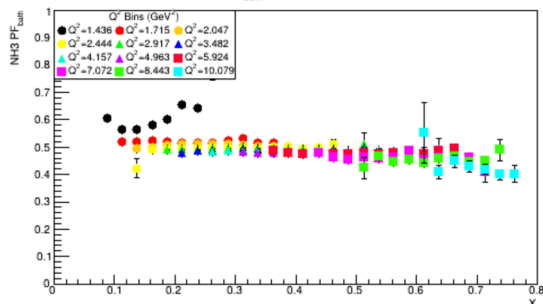
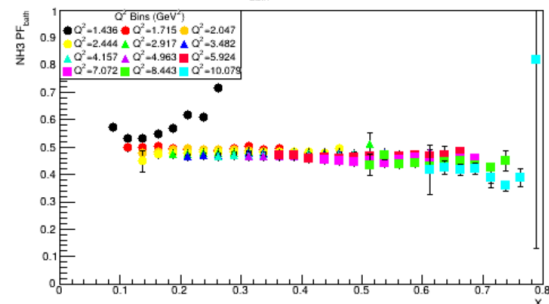
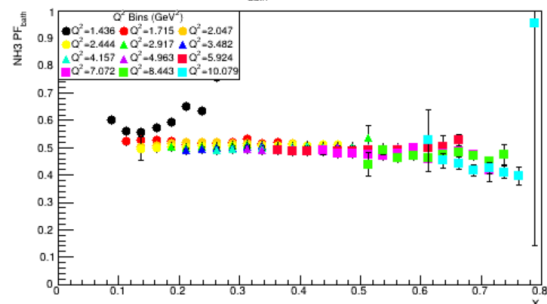


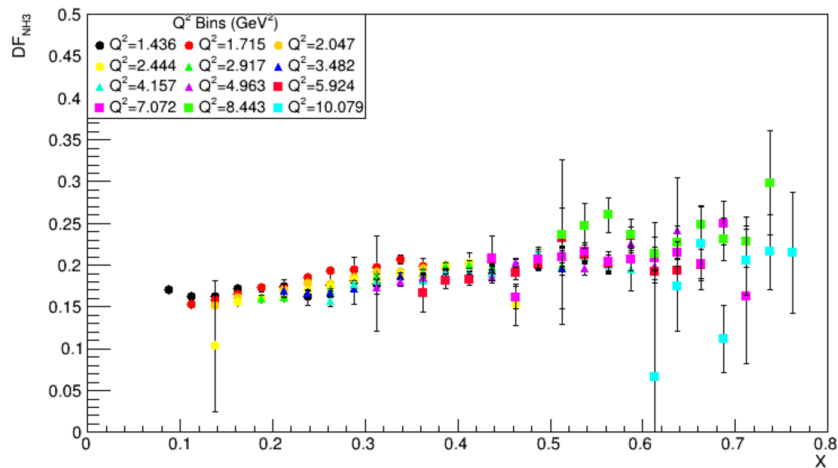
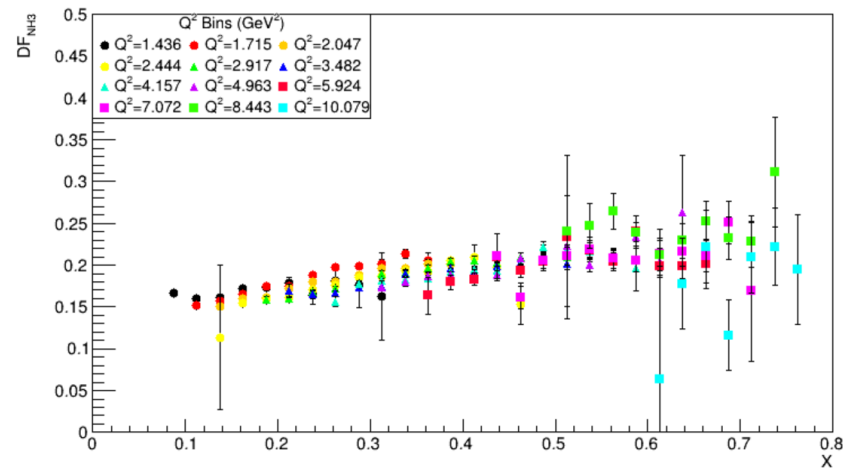
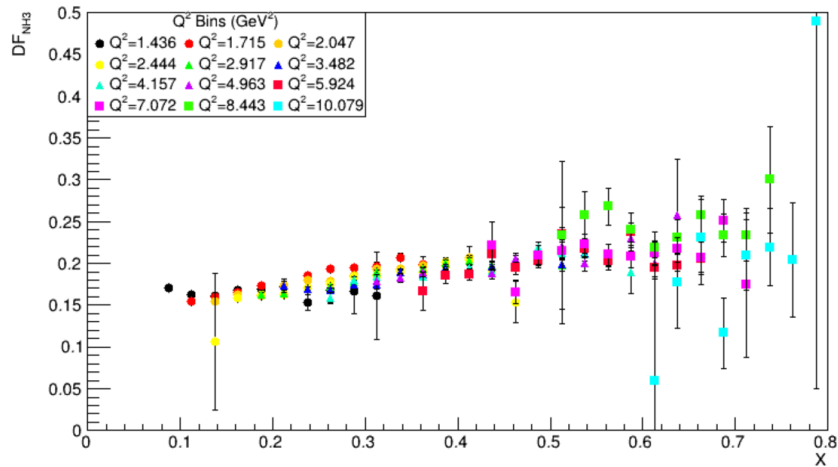
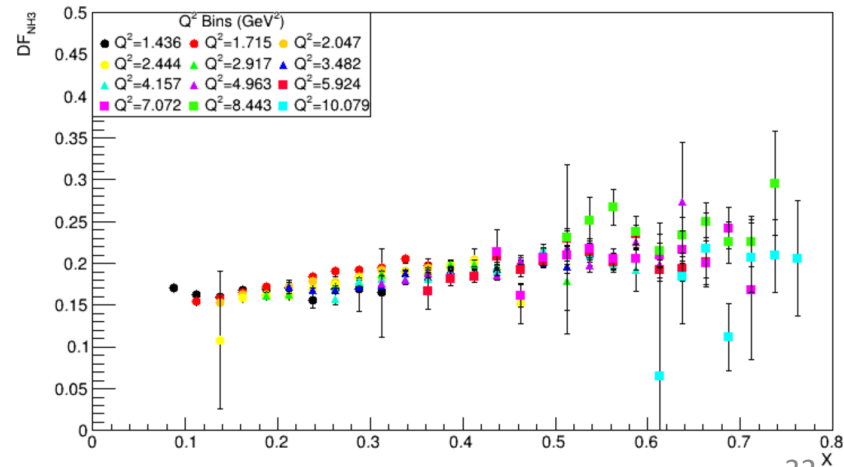


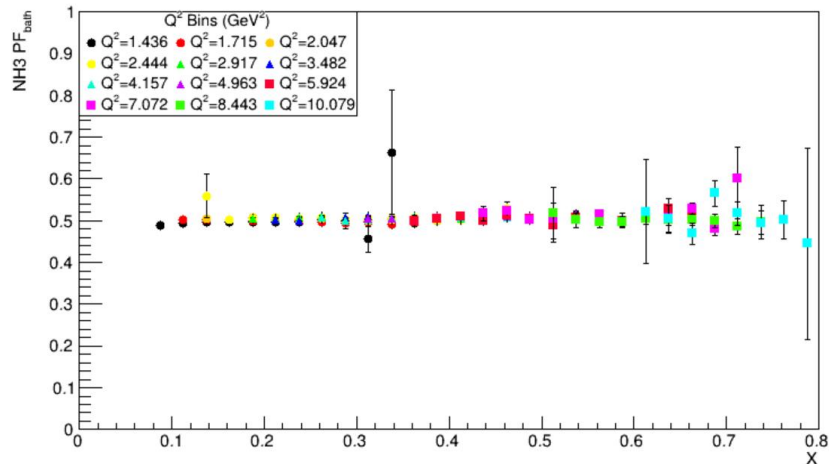
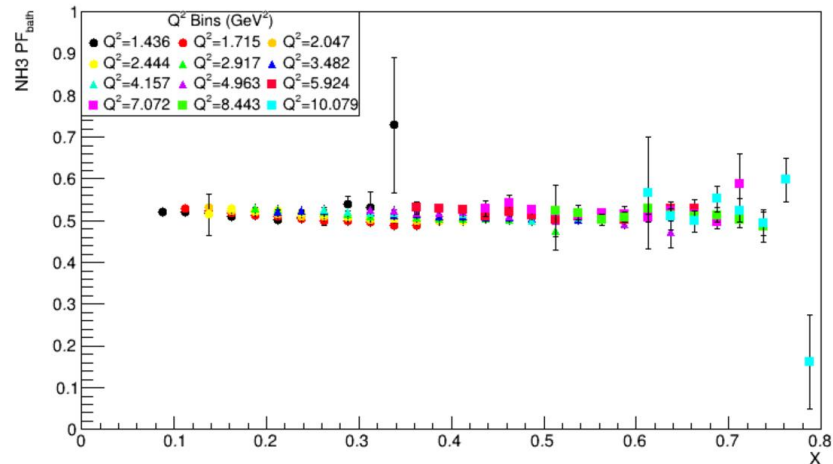
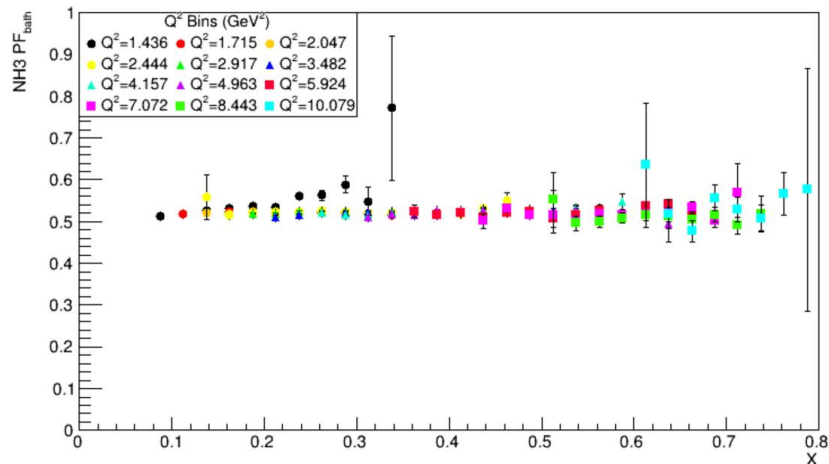
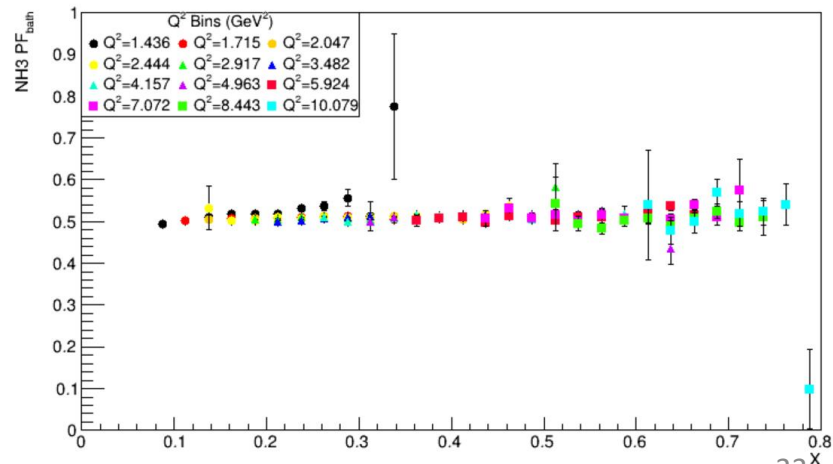
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NH3 PF_{bath} for NH3 Epoch 2NH3 PF_{bath} for NH3 Epoch 3NH3 PF_{bath} for NH3 Epoch 4Summer 2022 P_F NH3 PF_{bath} for NH3 Epoch 5NH3 PF_{bath} for NH3 Epoch 6NH3 PF_{bath} for NH3 Epoch 7

NH3 DF_{NH3} for NH3_Epoch_8NH3 DF_{NH3} for NH3_Epoch_9NH3 DF_{NH3} for NH3_Epoch_10NH3 DF_{NH3} for NH3_Epoch_11NH3 DF_{NH3} for NH3_Epoch_12NH3 DF_{NH3} for NH3_Epoch_13NH3 DF_{NH3} for NH3_Epoch_14Fall 2022 D_F

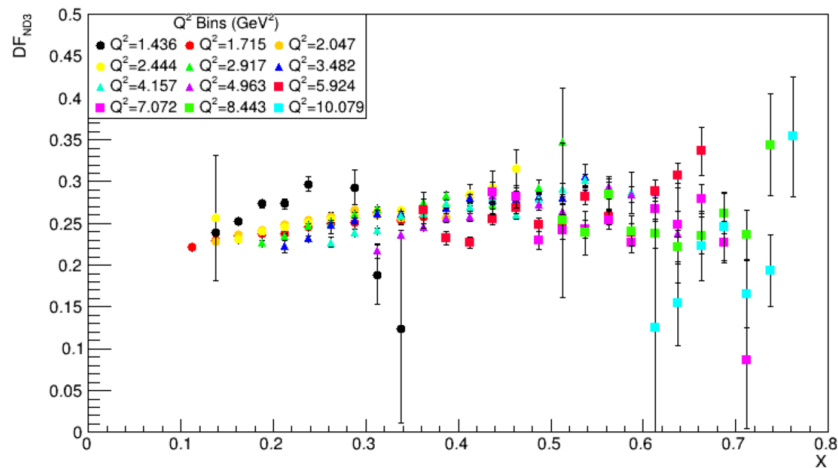
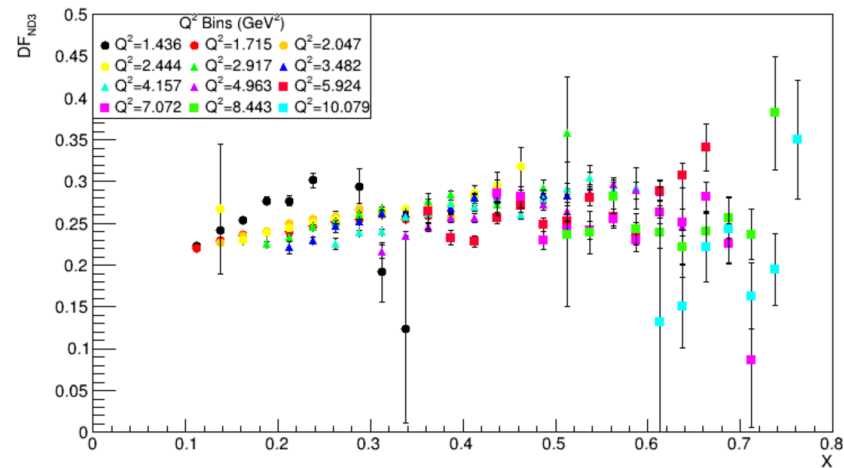
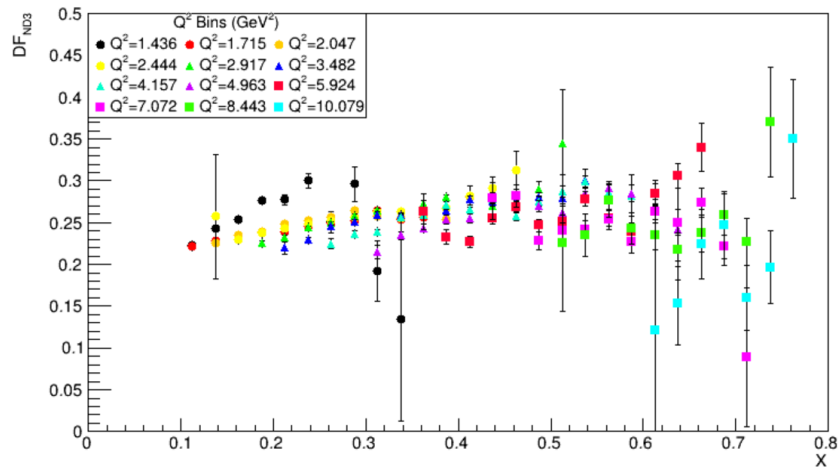
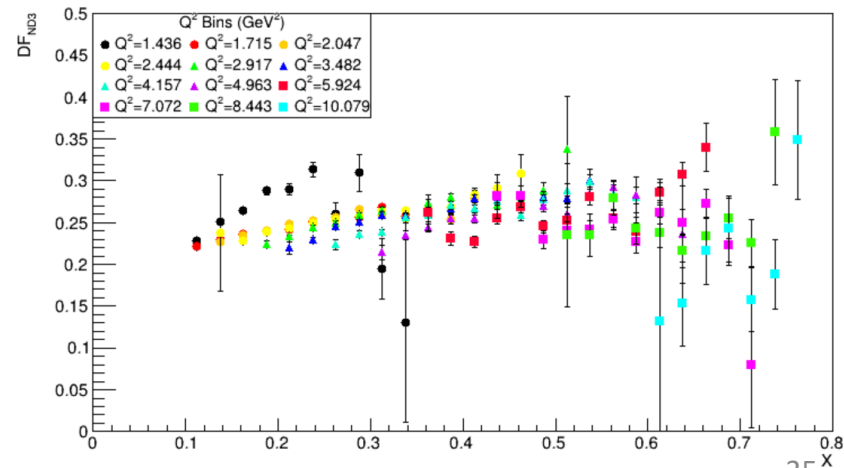
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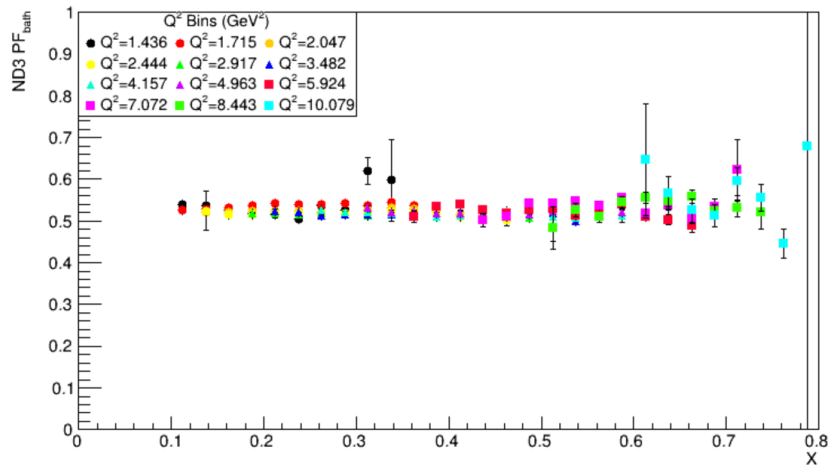
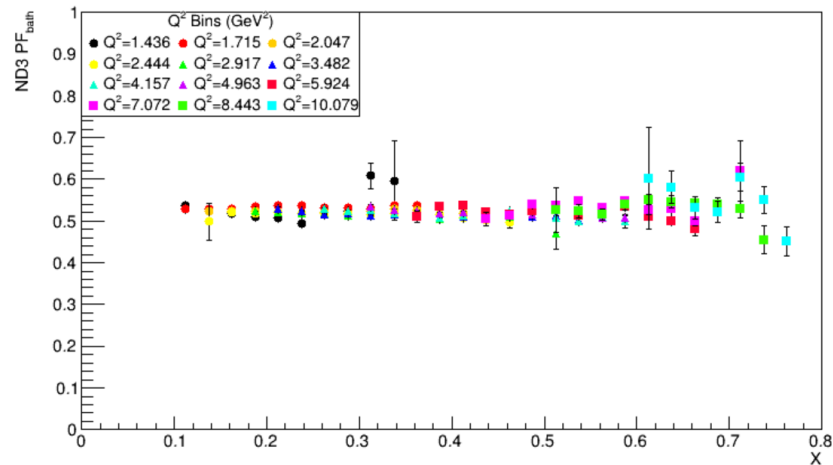
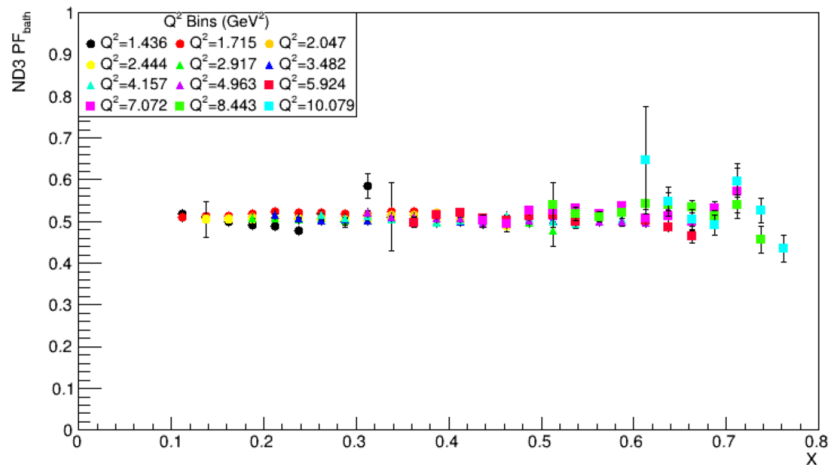
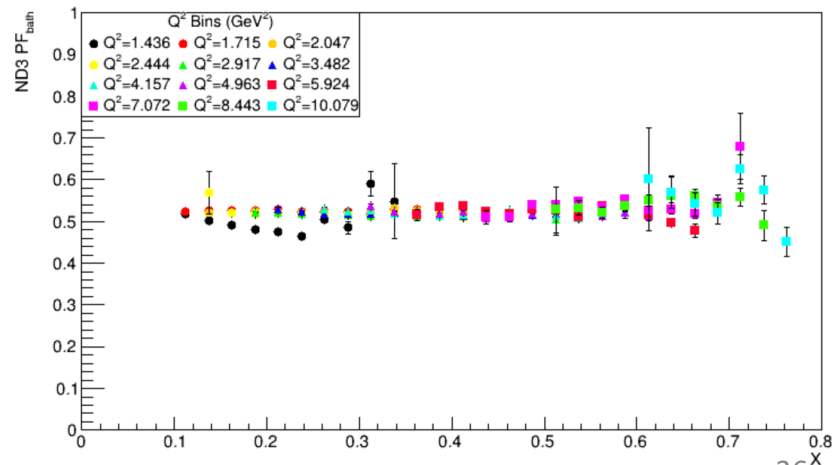
NH3 DF_{NH3} for NH3_Epoch_15NH3 DF_{NH3} for NH3_Epoch_16Spring 2023 D_F NH3 DF_{NH3} for NH3_Epoch_17NH3 DF_{NH3} for NH3_Epoch_18

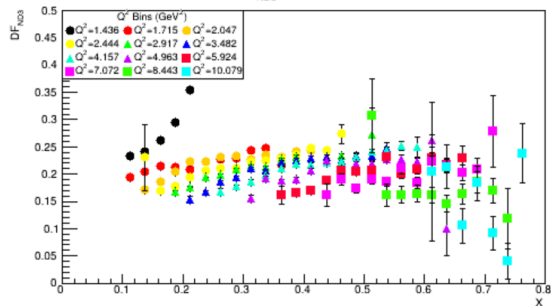
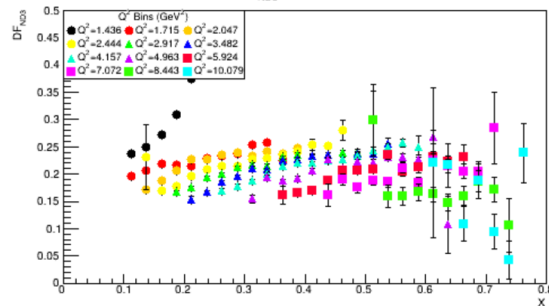
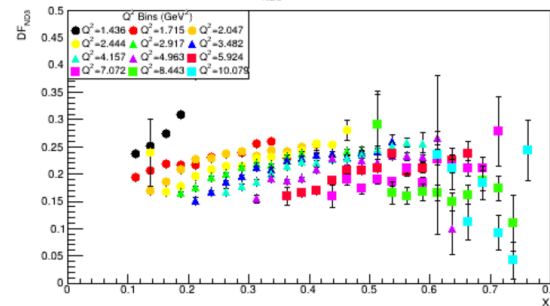
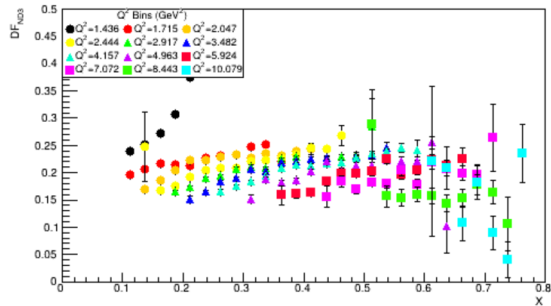
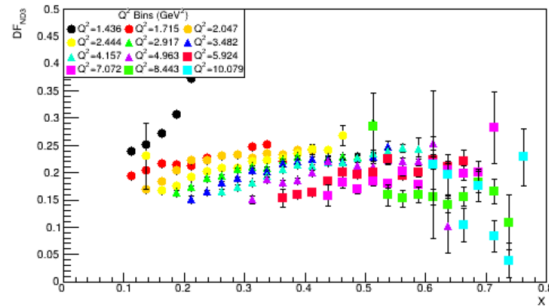
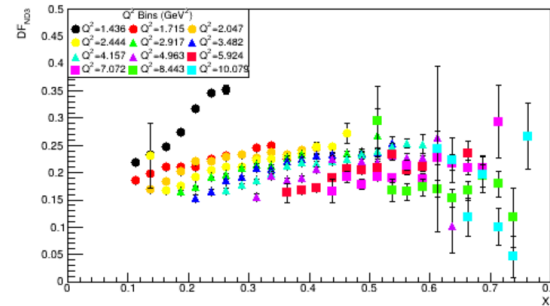
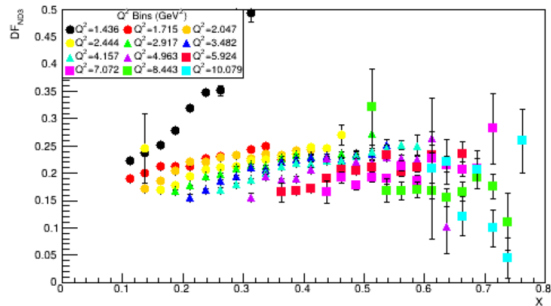
NH3 PF_{bath} for NH3_Epoch_15NH3 PF_{bath} for NH3_Epoch_16Spring 2023 P_F NH3 PF_{bath} for NH3_Epoch_17NH3 PF_{bath} for NH3_Epoch_18

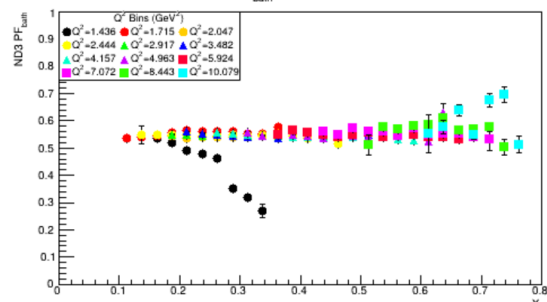
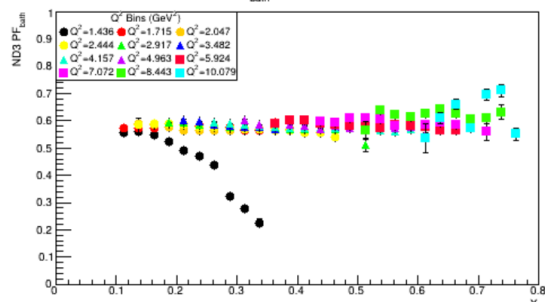
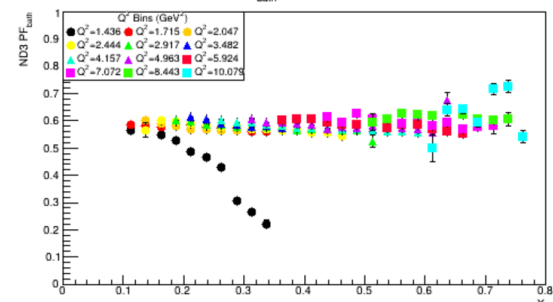
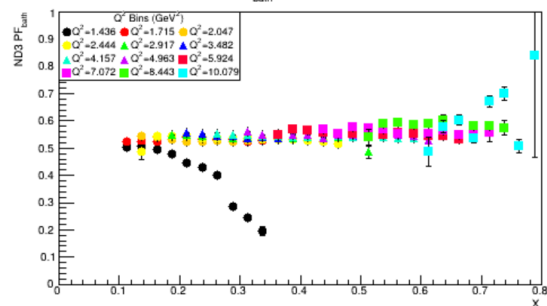
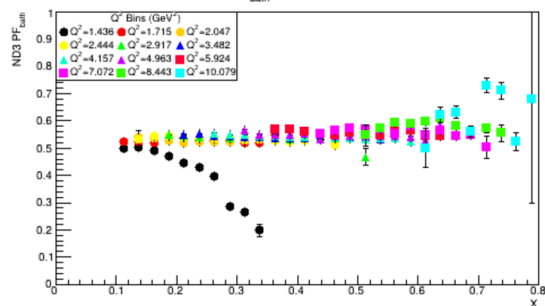
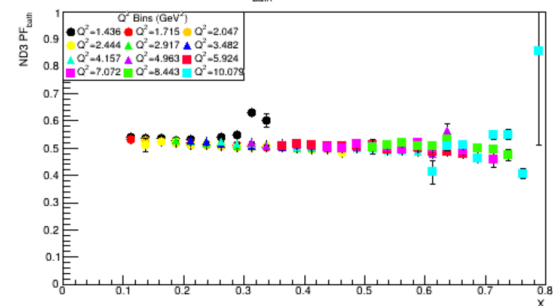
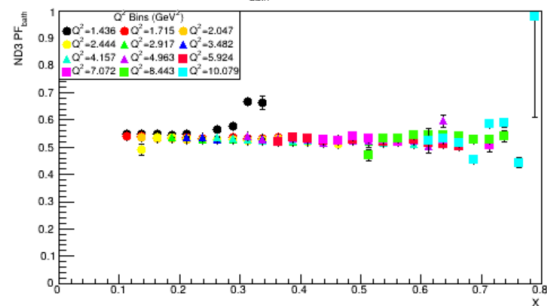
Issues with ND3 D_F

- $D_{F,ND3}$ deviated significantly from models as well as showed inconsistent behavior in the fall and spring data sets
- “Stratification” in the fall and spring data
- No CD2 runs were taken for summer and fall, so we had to generate pseudo-CD2 counts for the summer and fall datasets
- Scaled CH2 counts in the summer and fall using the CD2 and CH2 counts from the spring 23 dataset
- For each bin in x , Q^2 for summer/fall CH2 targets, multiplied counts by $\left(\frac{n_{CD2}}{n_{CH2}}\right)_{Sp23}$ to generate pseudo CD2:
- $(n_{CH2})_{SuFa22} * \left(\frac{n_{CD2}}{n_{CH2}}\right)_{Sp23} \approx (n_{CD2})_{SuFa22}$

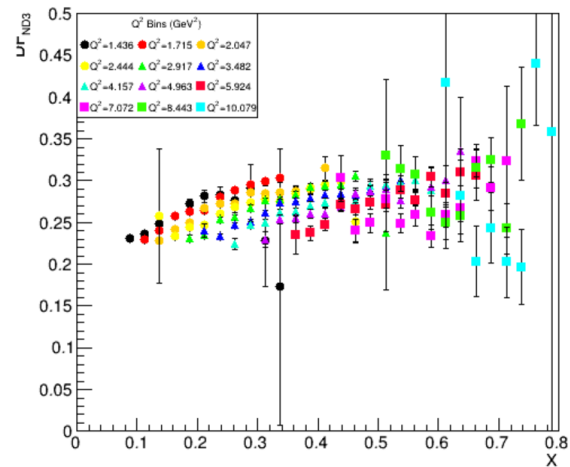
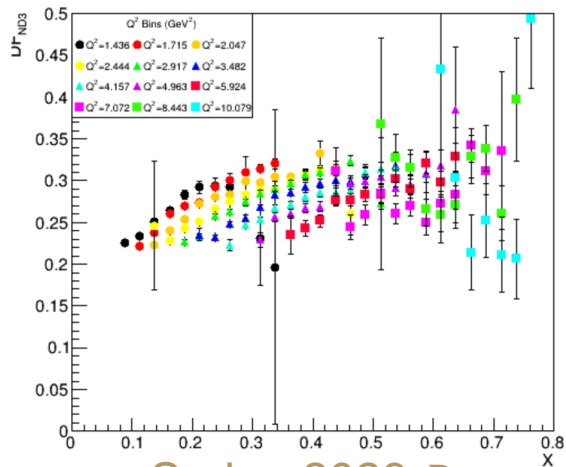
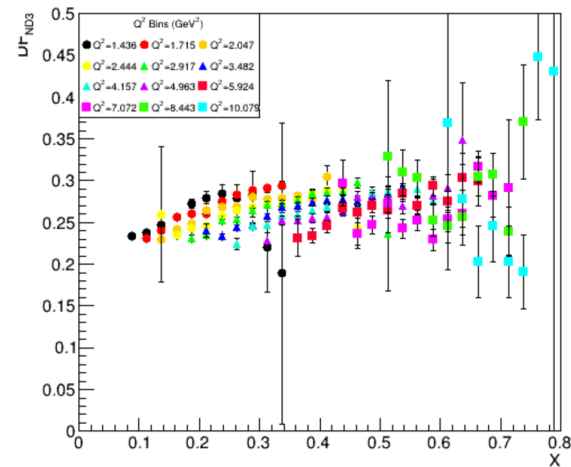
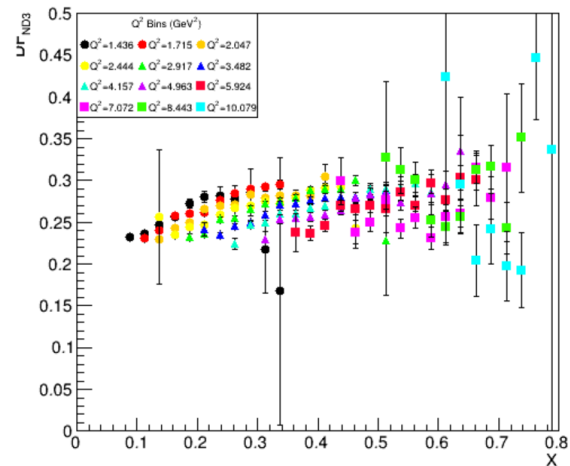
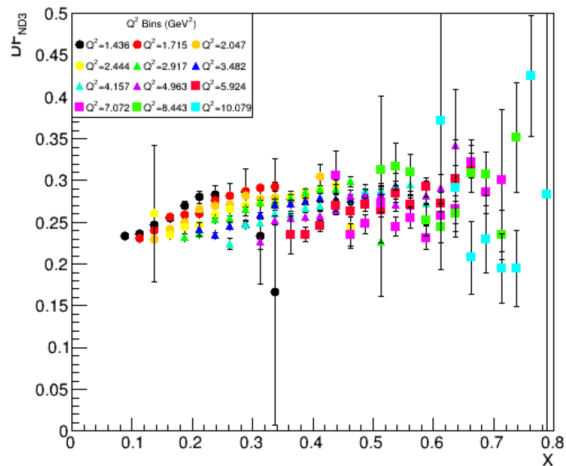
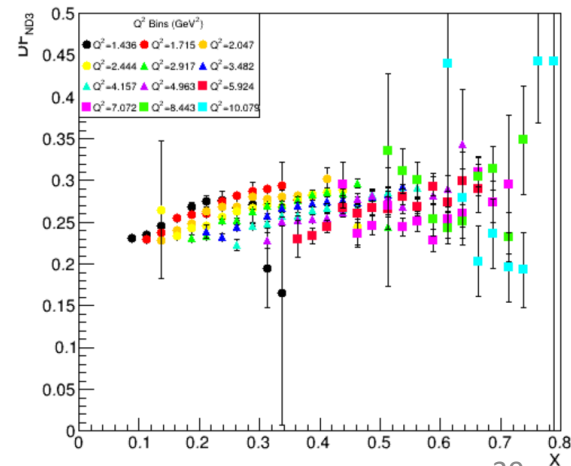
ND3 DF_{ND3} for ND3_Epoch_1ND3 DF_{ND3} for ND3_Epoch_2Summer 2022 D_F ND3 DF_{ND3} for ND3_Epoch_3ND3 DF_{ND3} for ND3_Epoch_4

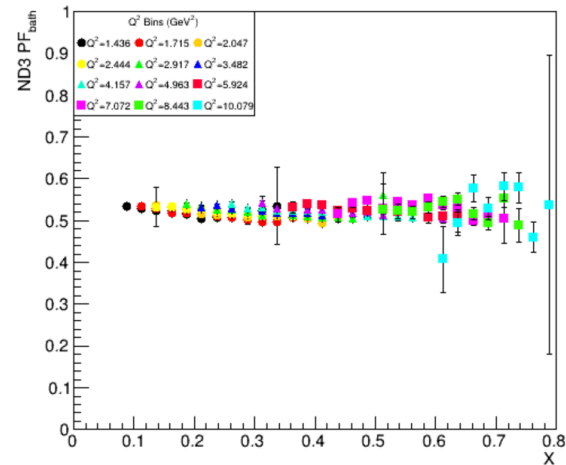
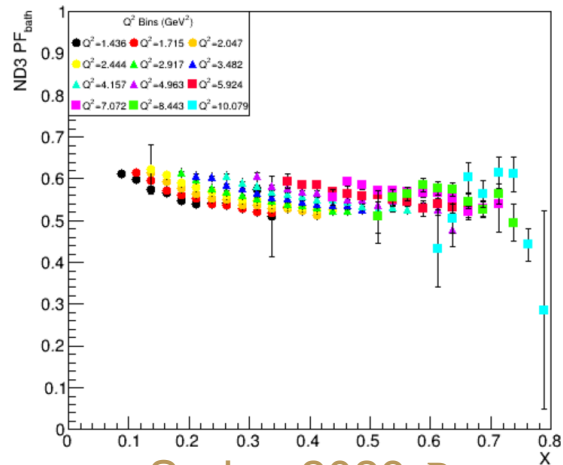
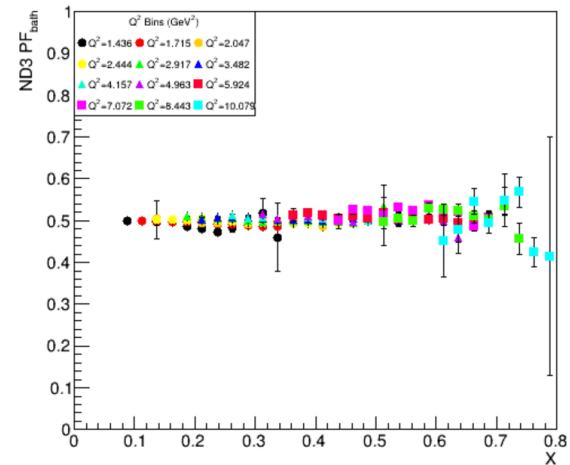
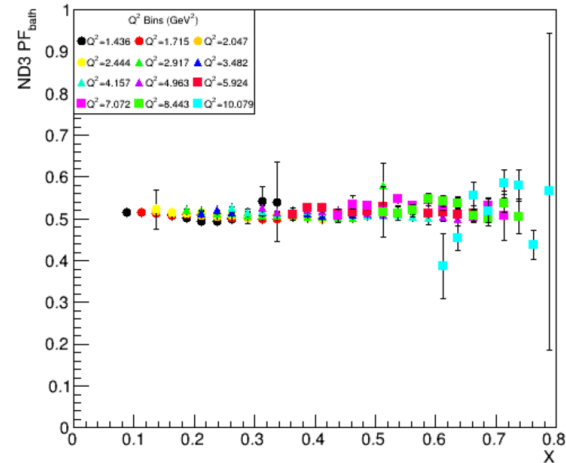
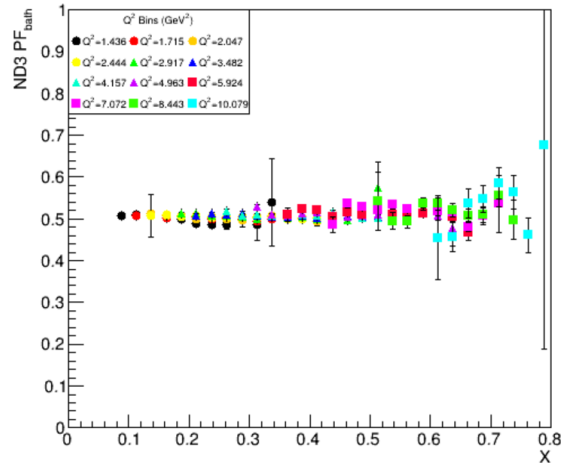
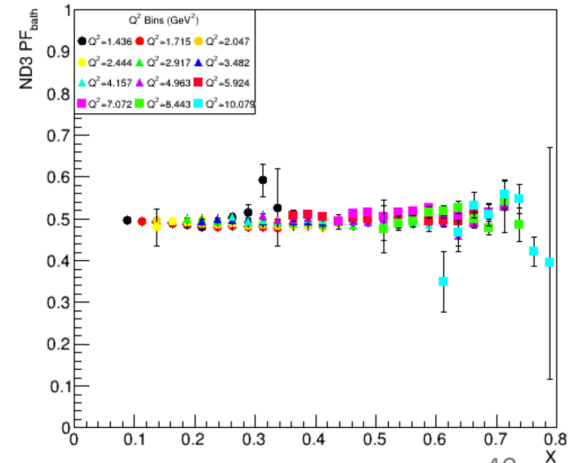
ND3 PF_{bath} for ND3_Epoch_1ND3 PF_{bath} for ND3_Epoch_2Summer 2022 P_F ND3 PF_{bath} for ND3_Epoch_3ND3 PF_{bath} for ND3_Epoch_4

ND3 DF_{ND3} for ND3_Epoch_5ND3 DF_{ND3} for ND3_Epoch_6ND3 DF_{ND3} for ND3_Epoch_7ND3 DF_{ND3} for ND3_Epoch_8ND3 DF_{ND3} for ND3_Epoch_9ND3 DF_{ND3} for ND3_Epoch_10ND3 DF_{ND3} for ND3_Epoch_11Fall 2022 D_F

ND3 PF_{bath} for ND3_Epoch_5ND3 PF_{bath} for ND3_Epoch_6ND3 PF_{bath} for ND3_Epoch_7ND3 PF_{bath} for ND3_Epoch_8ND3 PF_{bath} for ND3_Epoch_9ND3 PF_{bath} for ND3_Epoch_10ND3 PF_{bath} for ND3_Epoch_11

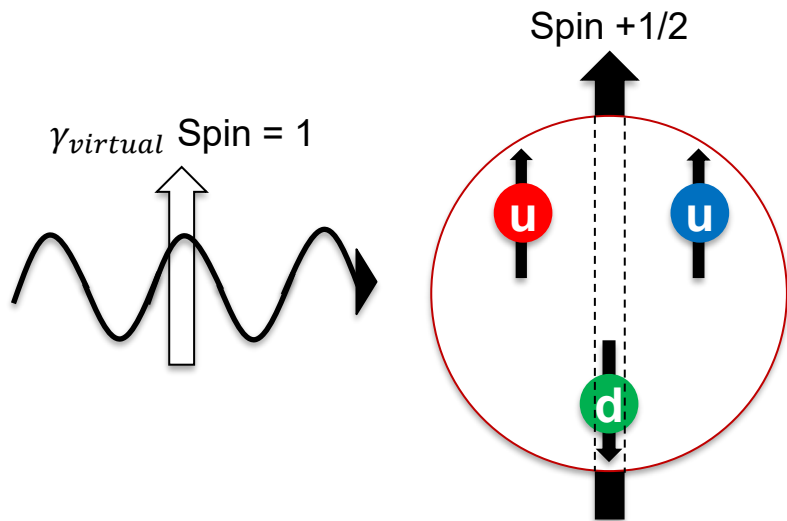
Fall 2022 P_F

ND3 DF_{ND3} for ND3_Epoch_12ND3 DF_{ND3} for ND3_Epoch_13ND3 DF_{ND3} for ND3_Epoch_14Spring 2023 D_F ND3 DF_{ND3} for ND3_Epoch_15ND3 DF_{ND3} for ND3_Epoch_16ND3 DF_{ND3} for ND3_Epoch_17

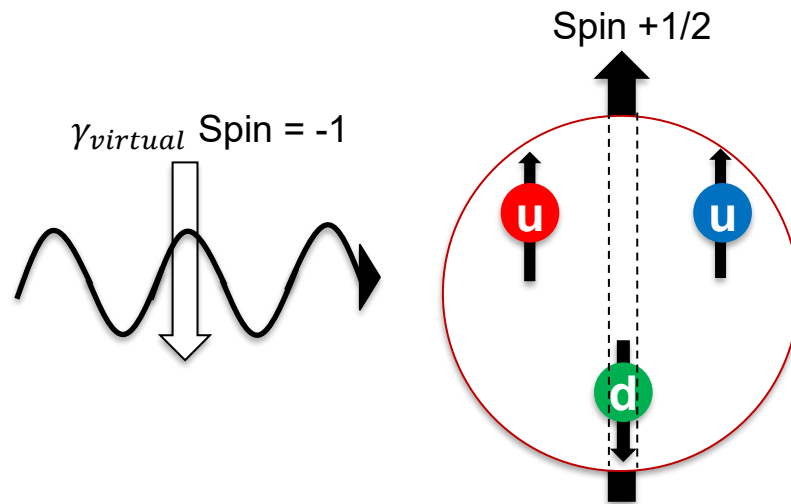
ND3 PF_{bath} for ND3_Epoch_12ND3 PF_{bath} for ND3_Epoch_13ND3 PF_{bath} for ND3_Epoch_14Spring 2023 P_F ND3 PF_{bath} for ND3_Epoch_15ND3 PF_{bath} for ND3_Epoch_16ND3 PF_{bath} for ND3_Epoch_17

Virtual Photon Asymmetries

$$A_1 \equiv \frac{(\sigma_{1/2} - \sigma_{3/2})}{(\sigma_{1/2} + \sigma_{3/2})} \quad A_2 \equiv \frac{2\sigma_{LT}}{(\sigma_{1/2} + \sigma_{3/2})}$$



$\sigma_{3/2}$ Cross Section



$\sigma_{1/2}$ Cross Section

Virtual Photon Asymmetries

- $\sigma_{LT} \propto \gamma[g_1 + g_2], \quad (\sigma_{1/2} - \sigma_{3/2}) \propto (g_1 - \gamma^2 g_2), \quad (\sigma_{1/2} + \sigma_{3/2}) \propto F_1$

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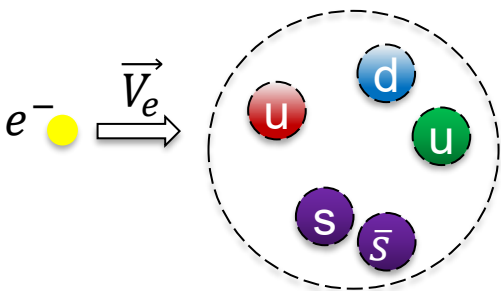
Virtual Photon Asymmetries

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$$A_1 = \frac{g_1 - \gamma^2 g_2}{F_1} \quad A_2 = \frac{\gamma[g_1 + g_2]}{F_1}$$

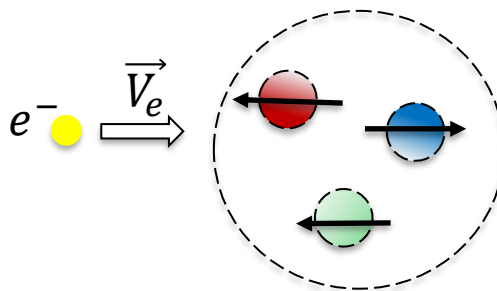
- $\gamma = 2M_p x / Q^2$ As $Q^2 \rightarrow \infty$, $A_1 \approx g_1 / F_1$
- F_1 **unpolarized structure function** (scattering probability)
- g_1 **spin structure function** (scattering probability asymmetry based on spin)

g_1 describes the proton's longitudinal spin structure!



Probability:

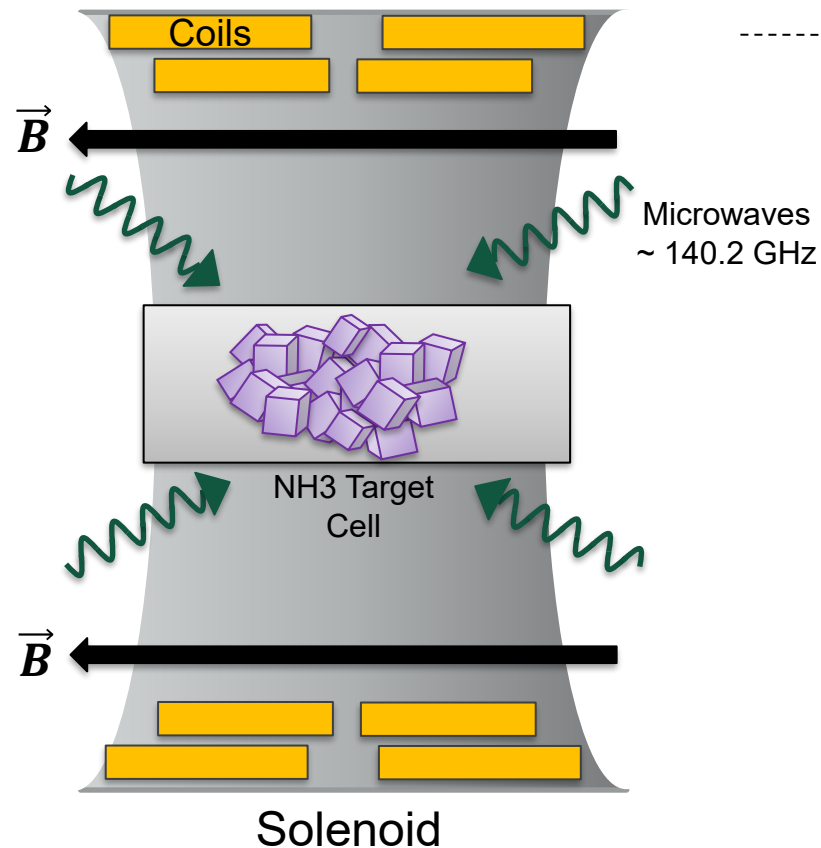
$$\begin{aligned} P_u(x) &= ? \\ P_d(x) &= ? \\ P_s(x) &= ? \\ P_{\bar{s}}(x) &= ? \end{aligned} \propto F_1$$



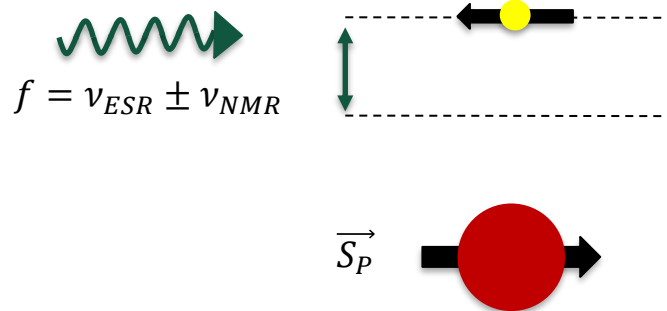
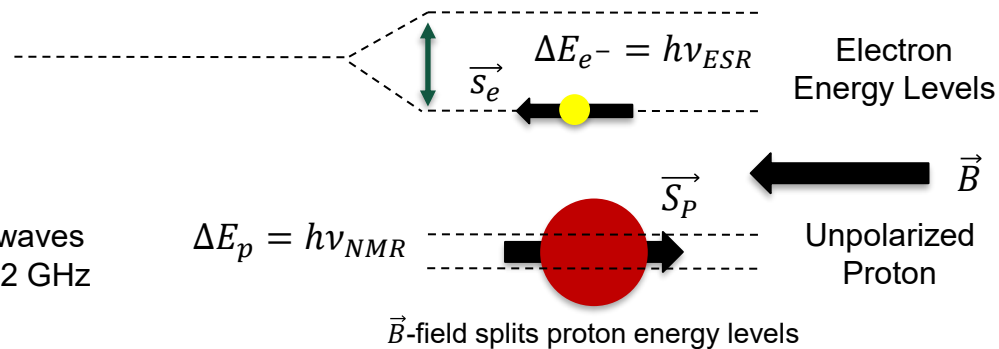
Probability:

$$P_{q\uparrow}(x) - P_{q\downarrow}(x) \propto g_1$$

Dynamic Nuclear Polarization



$\vec{B}$ -field polarizes e^- , splits energy levels



Beam-Target Polarization Calculations

$$A_{||,phys} = \frac{A_{||,raw}}{D_F P_b P_t} \Rightarrow P_b P_t = \frac{A_{||,raw}}{D_F A_{||,phys}}$$

- Use a model to calculate $A_{||,phys}$
- Values of $P_b P_t$ were calculated for RGC data using exclusive elastic $ep \rightarrow e'p'$ scattering (Noemie Pilleux)

$$P_b P_t = \frac{\sum_{Q^2 \text{ bins}} d_{f,i} A_{th,i} (n_i^- - n_i^+)}{\sum_{Q^2 \text{ bins}} d_{f,i}^2 A_{th,i}^2 (n_i^- + n_i^+)}$$

- d_f = separate dilution factor, A_{th} = elastic asymmetry parameterized by Arrington et. al.

$$A_{th} = \frac{2\tau r_g [M/E + r_g(\tau M/E + (1 + \tau)\tan^2(\theta/2))]}{1 + r_g^2 \tau / \epsilon} \quad r_g \equiv G_M / G_E$$

- For DIS $P_b P_t$, calculated in x, Q^2 bins using $A_{th} = D(A_1 + \eta A_2)$, with Values of D, η, A_1, A_2 come from S. Kuhn 's model
- Much greater statistics than elastic

$$P_b P_t = \frac{\sum_{x, Q^2 \text{ bins}} D_{f,i} A_{th,i} (n_i^- - n_i^+)}{\sum_{x, Q^2 \text{ bins}} D_{f,i}^2 A_{th,i}^2 (n_i^- + n_i^+)}$$

Normalize DIS $P_b P_t$ to elastic $P_b P_t$ to avoid circular calculation!

