

Dispersive effects in unpolarized inclusive elastic electron/positron-nucleus scattering

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Outline

Background on e[±] scattering

Physics Goals

- Nuclear charge radii
- Neutron skin puzzle & single spin asymmetries
- Coulomb Sum Rule
- Rare isotopes & nuclear structure
- Electron dipole moment

PAC53 proposal PR12+25-013

- Overview and request
- Technical Advisory Committee review responses
- Theory review responses

Summary



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Background: Electron Elastic Scattering





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Background: Electron Elastic Scattering



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Dispersive Effects Background – Relative Measurements e⁻ Experiments at NIKHEF [1]

Nationaal Instituut voor Kernfysica en Hoge Energie-Fysic (NIKHEF) [The Netherlands]





Comparison to static charge density

Fourier-Bessel parameterization Reuter et al., PRC **26** (806) 1982 L. Cardman et al., Nuc. Phys. **A216** 806 (1973)

E_{beam} = 238, 243, 419 & 431 MeV

Phase 1 (1986)

• <5% for 1.5 < q (fm⁻¹) < 2.3

Phase 2 (1991)

- 1st minimum of ¹²C
- Energy dependence
- Effect on ¹²C rms: 0.28%

Dispersive Effects Background – Absolute Measurements e[±] Experiments at ALS [2]



Comparison to static charge density

- E_{beam} = 450 MeV; I = 20 nA
- <2% for 1 < q (fm⁻¹) < 1.5



Status on Experiments vs. Theory

Energy dependence

- J. Friar & M. Rosen, Ann. Phys., 87:289 (1974)
- Theory : no
- Experiment : yes!

Sign between e⁻ & e⁺ in ¹²C minimum

- G. Rawitscher, Phys. Rev., 151:846 (1966)
 - Theory : positive
 - Experiment : negative!



Incident Electron Energy (GeV)



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scattering angle ----

Physics I: Charge Radii and IAEA Recommendation [1]





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Physics I: Charge Radii and IAEA Recommendation [2]

IAEA Technical Meeting

- Compilation and Evaluation of Nuclear Charge Radii
- January 27-30, 2025; 20 participants
- https://conferences.iaea.org/event/401

https://nds.ia	ea.org/public	cations/ind	lc/indc-nd	s-0918/

International Atomic Energy Agency Nuclear Data Services Provided by the Nuclear Data Section					
☆ Relevant Links NDS Home	Title	Compilation and Evaluation of Nuclear Charge Radii			
Publications Home	Author	Flanagan, H. Staiger, E. Takacs, P. Dimitriou			
Conterence Proceedings. IAEA NDS series INDC series NDS staff publications. Tecdocs	Date	un 2025			
	DOI	10.61092/iaea.vm5h-hmep			
	Note	Summary report of the Technical Meeting, 27-30 January 2025, Vienna, Austria			
	Last viewed	28-Jun-2025			
	Full text	4.2 M (Ctrl+L for full view)			



The meeting will comprise presentations with ample time for discussion, and roundtable discussions. A summary of the technical discussions and recommendations will be published in a report.



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Physics I: Charge Radii and IAEA Recommendation [3]

Outcomes

- · More accurate compilation of rms charge nuclear radii
 - » Angeli, I. & Marinova, K. P
 - Atom. Data Nucl. Data Table, **99**, 69 (2013)
 - >> Large uncertainties: mainly theory
 - >> Need guidance for experiments
 - >> Dispersive effects not accounted for in past compilations!
 - Best practices to extract precise RMS nuclear charge radii?
 - >> Stable : electron scattering (deVries, 1987!), muon spectroscopy and laser spectroscopy
 - >> Unstable : laser spectroscopy (ref. nuclei), electron (SCRIT @ RIKEN and ULQ2 @ Tohoku Univ.)
 - >> Standardize : e.g., Barrett moments from µ-spectroscopy (accuracy: ≤0.1%)
- Need to get there
 - >> Both experimental and theoretical sides
- Regular charge nuclear radii compilation "à la" AMDC





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Physics II: Neutron skin puzzle and single spin asymmetries

Coulomb potential

$$|V_C| = |V_C^{stat}| = \frac{KZ}{\langle r^2 \rangle^{1/2}}; K = 1/4\pi\varepsilon_0 \longrightarrow |V_C^{disp}| = |V_C^{stat}| / [1 + \beta\delta(E_e)]$$

Guèye et al., EPJ A56(5) 2020

²⁰⁸Pb charge radius: 0.07% effect [5.5012(13) fm → 5.5053(13) fm]

Single spin asymmetries (SSA)

- PV experiments measurements near diffraction minima
- Beam-normal SSA conserves parity
 » But 0 in the first Born (1-γ) approximation
- Past JLab experiments on SSA on nuclear targets [1, 2]
 - >> Unambiguous evidence of effects beyond the Born approximation
 - >> Coulomb distortions are insufficient
 - >> Excitation of nuclei during the scattering process (BNSSA) [3]
 - Played a defining role!
 - Light nuclei: OK
 - ²⁰⁸Pb : not satisfactory
 - [1] Abrahamyan et al., Phys. Rev. Lett., **109**(19):192501, 2012

[2] Adhikari et al., Phys. Rev. Lett., **128**(14):142501, 2022 Facility for Rare Isotope Beams









Physics III: Coulomb Sum Rule



Dispersive effects could have a non-negligible contribution to the CSR!



Physics IV: Rare Isotopes and Nuclear Structure [1]

Extension to rare isotopes

- MoNA Collaboration/PING Program
 >> Si-Be segmented target
 >> 4 TLPSDs + 3 Be
- Rutherford scattering-like data
- Preliminary results for matter radii
 >> Impact from charge radii
 - >> Sensitivity to neutron distribution (n-rich nuclei)?

Graduate student

- Paula Plazas Isanoa (MSU, Fall 2024)
- Joint thesis project
 - >> Laser spectroscopy (BECOLA)
 - >> Matter radii (MoNA Collaboration)

Undergraduate student

Makaila Parks (Spelman College, PING2024)

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Physics IV: Rare Isotopes and Nuclear Structure [2]

Double-folding model

- Optical potential to describe two colliding ions
 - Average an appropriate N-N interaction over the matter distributions
 Similar approach as treatment of the Coulomb interaction
- Two components: real (Coulomb) and imaginary (nuclear)
- Use two-Fermi parameter distribution





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G. Satchler, W. Love, Phys. Rep. **55**(3) (1979) 183–254 L. Chamon et al., Comp. Phys. Com. 267 (2021) 108061





	ρ ₀ (nucl/fm³)	R₀ (fm)	a (fm)
Charge	0.08	1.76Z1/3 - 0.96 fm	0.53
Matter	0.17	1.31A1/3 – 0.84 fm	0.56

Insights about neutron distributions!!

Physics IV: Rare Isotopes and Nuclear Structure [3]





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Physics IV: Rare Isotopes and Nuclear Structure [4]

FRIB PAC3 proposal

- PR25076: spokespersons are S. Ota (BNL), P. Capel (JHUM) & P. Guèye (FRIB)
- Establish a complete picture of the halo nucleus ¹⁹C using a novel technique: the ratio method



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Physics V: EDM Search [1]

Collaboration with Jaideep Singh @ MSU

Need: nuclei with spin >0

- Four electromagnetic form factors [1]
 - >> F₁ (charge) and F₂ (anomalous magnetic moment)
 - Experimentally measured
 - F₂ lead to 2-photon exchange puzzle [2]
 - >> F₃ (electron dipole moment)
 - No non-zero measured but possible [3,4]
 - >> F₄ (Zeldovich anapole moment)
 - No experimental evidence
 - Through coupling to off-shell photons (virtual exchanged between 2 fermions) [1]
 - PV through F4 competes with PV through Z0: very hard to disentangle!

	$F_1(0) = Q = e$	
	$\frac{1}{2m} \left[F_1(0) + F_2(0) \right] = \mu \to a = \frac{g}{2} - 1 = \frac{F_2}{e}$	
-	$-\frac{1}{2m}F_3(0) = d$	
i	$H_{\rm int}^{\rm NR}[F_4] \propto F_4(0)\sigma \cdot \left[\nabla \times \mathbf{B} - \frac{\partial \mathbf{E}}{\partial t} \right]$	

[1] M. Nowakowski, E. A. Paschos and J. M. Rodríguez, Eur. J. Phys. **26** 545–560 (2005) [2] Bosted P. E., Phys. Rev. **C51** 409–11 (1995)



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[3] Commins E. D., Advances in At., Mol. and Opt. Phys., **40** 1–55 (1999)
[4] Regan B. C. et al., Phys. Rev. Lett. **88** 071805 (2002)

Physics V: EDM Search [2]

Goal

- Constrain EDMs from electron scattering data in a model independent way
- Note on small Z: theory predicts that they are immeasurably small
 » No one has even tried to measure them!
- Experimental verification
 » Experimental limits (even if crude)
- Would need polarized experiments
 » Sensitivity with non-spin 0 targets

Targets

- Spin 0 :¹²C, ⁴⁸Ca, ⁵⁶Fe, ¹⁹⁶Pt, ²⁰⁸Pb
- Non-spin 0: ²⁷Al (5/2), ⁶³Cu (3/2), ²⁰⁹Bi (9/2)



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PR12+25-013: Overview [1]

LOI12-23-015 (PAC51)

Polarization (no!), theory, simulation

Collaborators

- 54 participants (+20 before PAC53)
- 26 institutions

Endorsement

Positron Working Group

Main goals

- Measure unpolarized $A(e^{\pm}, e^{\pm})$ cross section
- Map dispersive effects
 - >> Energy dependence
 - 0.7 GeV 4.24 GeV
 - >> Atomic mass dependence
 - 8 targets
 - ¹²C, ²⁷Al, ⁴⁸Ca, ⁵⁶Fe, ⁶³Cu, ¹⁹⁶Pt, ²⁰⁸Pb, ²⁰⁹Bi

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Experiment (Hall C)

- Phase 1: gualitative measurements
 - \gg Compare A(e⁻,e⁻) with theory
 - >> A. Afanasev group at GWU
- Phase 2: absolute direct measurements >> Compare A(e[±],e[±]) cross sections
- Received TAC comments (05/26/25)
- Received Theory comments (07/08/25)
- Received additional comments (07/08/25)

Physics

- Nuclear charge radii 1.
- Neutron skin puzzle & single spin 2. asymmetries
- Coulomb Sum Rule 3
- Rare isotopes & nuclear structure 4.
- 5. Electron dipole moment

PR12+25-013: Overview [2]





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Perform targeted measurements!

Low energy (0.7 MeV)

Multiple targets for A-dependency

High energies (1.06-4.2 GeV)

One target for detailed E-dependence study

Phases

- Phase 1: relative measurements (e⁻,e⁻) with $\sigma_{exp}/\sigma_{theo(GWU)}$
- Phase 2: absolute measurements (e[±],e[±]) with $\sigma_{exp}^- \sigma_{exp}^+$

	Phase 1	Phase 2
	(%)	(%)
Statistics	0.1	1.0
Acceptance	1.0	1.0
Tracking Efficiency	0.5	0.5
Radiative corr.	1.2	1.2
Target Thickness	0.5	0.5
Total	1.7	2.0

PR12+25-013: Overview [3]





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PR12+25-013: Overview [4]

Phase 1: $A(e^-, e^-)$ for 100 μA						
Target	$\mathbf{E}_{\mathbf{e}}$	$\theta_{\mathbf{e}'}$	q-range	q_{min}^1/q_{min}^2	Rates	
	(GeV)	(Deg.)	(fm^{-1})	(fm^{-1})	(Hz)	
¹² C		20,25,30,35,40	1.2-2.4	1.8	$2.8 - 1.3 \times 10^{6}$	
²⁷ Al		15,20,22.5,25,30	0.9-1.8	1.2	$2.6 imes 10^3 - 3.6 imes 10^7$	
⁴⁸ Ca	1	5.5,7.5,10,12.5,15	0.3-0.9	0.4/0.8	$2.6 imes 10^7 - 3.6 imes 10^{10}$	
⁵⁶ Fe	0 700	5.5,10,15,25	0.3-1.5	1.1	$6.8 imes 10^4 - 5.6 imes 10^{10}$	
⁶³ Cu	0.700	5.5,10,15,20,25	0.6-1.5	0.95	$4.8 \times 10^4 - 1.2 \times 10^9$	
¹⁹⁶ Pt	1	5.5,10,15,20	0.3-1.5	0.4/0.9	$8.4 imes 10^5 - 8.2 imes 10^{10}$	
²⁰⁸ Pb	1	5.5,10,15,20	0.3-1.2	0.4/0.8	$8.1 imes 10^5 - 8.3 imes 10^{10}$	
²⁰⁹ Bi		5.5,7.5,10,12.5	0.3-0.8	0.3/0.5	$1.6 imes 10^8 - 8.4 imes 10^{10}$	
¹² C		10,15,20,25,30	0.9-2.8	1.8	$20.8-5.2 imes10^7$	
¹³ Al	1	5.5,10,15,20	0.5-1.9	1.2	$19.9 - 7.0 \times 10^9$	
⁴⁸ Ca	1	5.5,10	0.5-0.9	0.4/0.8	$4.2 imes 10^6 - 6.6 imes 10^9$	
⁵⁶ Fe	1.060	5.5,10,15	0.5-1.4	1.1	$6.1 imes 10^5 - 1.0 imes 10^{10}$	
⁶³ Cu	1.000	5.5,10,15,20,25	0.5-2.3	0.95	$12.3 - 9.3 \times 10^9$	
¹⁹⁶ Pt		5.5,10,15	0.5-1.4	0.4/0.9	$3.5 imes 10^6 - 1.0 imes 10^{10}$	
²⁰⁸ Pb	1	5.5,10,15	0.5-1.4	0.4/0.8	$3.4 imes 10^6 - 1.0 imes 10^{10}$	
²⁰⁹ Bi		5.5,10	0.5-0.9	0.3/0.5	$4.7 imes 10^7 - 1.0 imes 10^{10}$	
¹² C	2.120	5.5,7.5,10	1.0-1.9	1.8	$1.4\times10^4-7.8\times10^7$	
¹² C	4.240	5.5	2.1	1.8	$6.5 imes 10^3$	

Phase 2: $A(e^{\pm}, e^{\pm})$ for 1 μA					
Target	t $\mathbf{E}_{\mathbf{e}}$ $\theta_{\mathbf{e}'}$		q-range	q_{\min}^1/q_{\min}^2	
	(GeV)	(Deg.)	(fm^{-1})	(fm ⁻¹)	
^{12}C		$20,\!25,\!30,\!35$	1.2-2.1	1.8	
²⁷ Al	0.700	20,25,30	1.2-1.8	1.2	
⁵⁶ Fe	0.700	15,20	0.9-1.2	1.1	
⁶³ Cu		$20,\!25,\!30$	1.2-1.8	0.95/1.8	
¹² C		15,20,25	1.4-2.3	1.8	
¹³ Al		15,20,25	1.4-2.3	1.2	
⁵⁶ Fe	1.060	15	1.4	1.1	
⁶³ Cu	1.000	$15,\!17.5,\!20$	1.4-1.9	0.95/1.8	
¹⁹⁶ Pt		10, 12.5, 15	0.9-1.4	0.4/0.9	
²⁰⁸ Pb		12.5	1.2	0.4/0.8	
¹² C	2.120	7.5,10,12.5	1.4-2.3	1.8	
¹² C	4.240	5.5	2.1	1.8	



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Phase 2: note on beam switch ($e^{\pm} \rightleftharpoons e^{\mp}$)

PWG recommendation for PAC53

• Plan for 1 week for switch $e^{\pm} \rightleftharpoons e^{\mp}$

Plan

- Take all data with electrons
- Switch lepton probe
- Take all data with positrons

Assumed 2 hrs/energy setting

- Best case scenario (e.g, bi-polar magnets)
- Total: 0.16 x 4 = 0.64 days (15.36 hrs)

If no bi-polar magnets

Add 7 days on overall schedule

Energy	Description	$\mathbf{A}(\mathbf{e}^-,\mathbf{e}^-)$	$\mathbf{A}(\mathbf{e}^{\pm},\mathbf{e}^{\pm})$
(GeV)	Description	(days)	(days)
	Calibration	0.500	1.00
	Production	6.19	1.60
0.70	Spectrometer Rotation	0.38	0.13
	Spectrometer Settings	0.75	0.25
	Target Change	0.03	0.01
	Beam switch $(e^{\pm} \leftrightarrow e^{\mp})$	-	0.16
	Calibration	0.500	1.00
	Production	8.21	24.0
1.06	Spectrometer Rotation	0.30	0.15
	Spectrometer Settings	0.60	0.29
	Target Change	0.03	0.02
	Beam switch $(e^{\pm} \leftrightarrow e^{\mp})$	-	0.16
	Calibration	0.500	1.00
	Production	0.60	2.04
2.12	Spectrometer Rotation	0.03	0.03
	Spectrometer Settings	0.06	0.06
	Target Change	0.003	0.003
	Beam switch $(e^{\pm} \leftrightarrow e^{\mp})$	2	0.16
	Calibration	0.500	1.00
	Production	1.02	0.02
4.24	Spectrometer Rotation	0.01	0.01
	Spectrometer Settings	0.02	0.02
	Target Change	0.003	0.003
	Beam switch $(e^{\pm} \leftrightarrow e^{\mp})$	-	0.16
Total		20.24 days	33.24 days



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PR12+25-013 (PAC53): TAC Review [1]

Target purity

• >99%

LH_2 for calibration

• No. Using ¹²C

Target ladder (J. Arrington)

- Will use the 13 target ladder developed for x>1 experiment
- Used: ¹²C (60 μA), ²⁷AI (40 μA), ⁴⁸Ca (60 μA), ⁵⁶Fe (40 μA), ⁶⁴Cu (60 μA)
- New: ¹⁹⁶Pt, ²⁰⁸Pb, ²⁰⁹Bi

Special cooling for Ca & Pb (D. Meekins)

- Was able to handle the significant power load on the targets (200 W)
- It is cooled by conduction thru the normal cryotarget connections

Heat dissipation for high current: could lower I_{beam} by x100

• $\Delta N/N$: 0.1% (10⁶ events) to 1% (10⁴ events) $\rightarrow (\Delta \sigma/\sigma)_{stat}$: 1.7% to 1.98%





PR12+25-013 (PAC53): TAC Review [2]

Low beam energy

- 700 MeV (phase 1) & 1.06 GeV (phase 2): should be possible
- Beam emittance
 - >> Saclay data with 6.28 mm.mrad (JLab projected: ≤40 mm.mrad) factor 7 worse!
 - >> Most important: same beam properties!
- Switch lepton probe ($e^{\pm} \rightleftharpoons e^{\mp}$): see slide 23
- Beam current uncertainty: should be <1%
- Rates for phase 2: 100 µA to 1 µA so 100x less than phase 1!



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PR12+25-013 (PAC53): Theory Review

"Summary: This is a well motivated experiment that could have significant impact."

Comment 1

- More details on data analysis
- Added in previous slides/more planned

Comment 2

- Interpretation of data using modern EFT calculations and two-body current operators
- Will provide data as clean as possible and leave it to theory for interpretation of the data

Comment 3

- Details on separating 2 photon exchange (Coulomb corrections) from dispersive effects
- Subtract Coulomb and radiative corrections (standard analysis procedure)
- Contribution from excited states
 - >> Can exclude1st excited state: spectrometer resolution <10⁻⁴
 - >> Study radiative tail region (excitation energy cut)

1 st Excited State					
¹² C	²⁷ AI	⁴⁸ Ca	⁵⁶ Fe	⁶³ Cu	²⁰⁸ Pb
4.43	0.84	3.83	0.85	0.67	2.61



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Summary

First ever comprehensive study and energy dependence of dispersive effects

• Measure elastic inclusive cross section in Hall C at ~1-2% level

Two phases

Phase 1: qualitative measurements – 20 days

- >> Compare A(e⁻,e⁻) with theory
- >> A. Afanasev group at GWU
- Phase 2: absolute direct measurements 33 days
 - >> Compare A(e[±],e[±]) cross sections

Physics

- 1. Nuclear charge radii
- 2. Neutron skin puzzle & single spin asymmetries
- 3. Coulomb Sum Rule
- 4. Rare isotopes & nuclear structure
- 5. Electron dipole moment (possible sensitivity)



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Thank You!

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