

Antonino Fulci

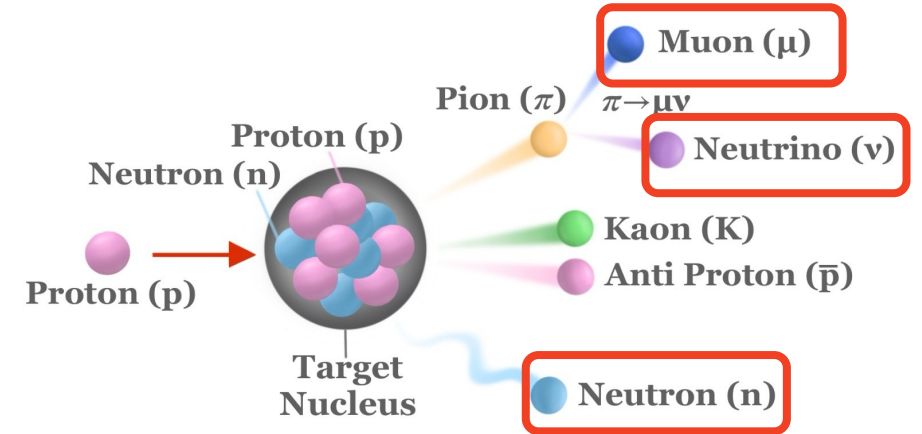
University of Messina

BDX & BEYOND WORKSHOP

**Simulation
of
Secondary Beam Fluxes**

Physics with secondary beams

- **Usually produced using proton beams**
 - Generally, they need to be focused and/or re-accelerated
- **Physic interest:**
 - Neutrinos: SM tests, neutrino properties, physics beyond SM, etc
 - Muons: muon scattering, dark matter search, etc.



Neutrinos



- Beam: proton
 - $E_p = 60 - 120 \text{ GeV}$
- Target: graphite
- $E_\nu = \mathcal{O}(\text{GeV})$
- $I_\nu = \mathcal{O}(10^3) \nu/\text{s}$

Muons



- Beam: proton
 - $E_p = 590 \text{ MeV}$
- Target: graphite
- $E_\mu = \mathcal{O}(\text{keV} - \text{MeV})$
- $I_\mu = \mathcal{O}(10^3 - 10^8) \mu/\text{s}$

Neutrons



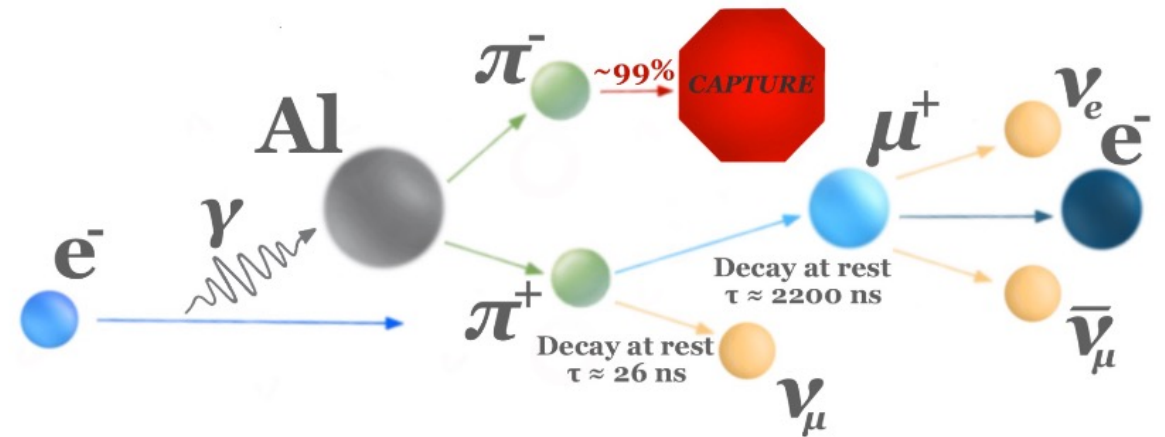
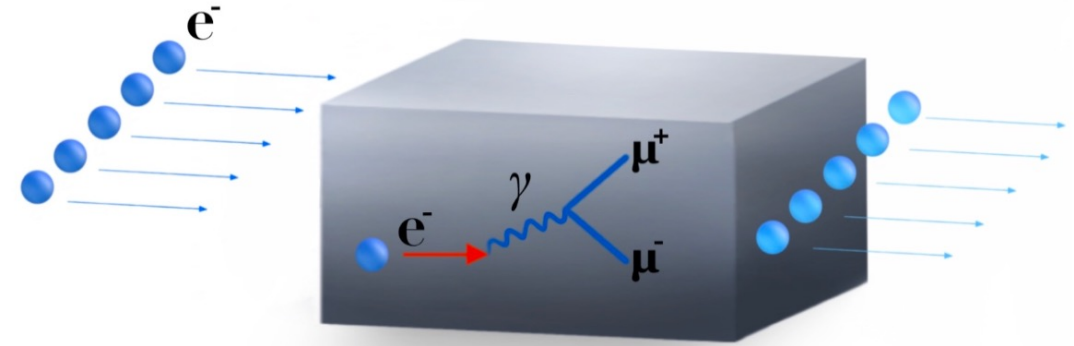
- Beam: proton
 - $E_p = 1 \text{ GeV}$
- Target: liquid mercury
- $E_n = \mathcal{O}(\text{meV} - \text{keV})$
- $I_n = \mathcal{O}(10^{15} - 10^{16}) \text{ n/s}$

Physics with secondary beams

- Also produced using **high-energy high-intensity e-beams**
 - Thick targets (>4 r.l.)
 - Primary production process:
 - Electron radiates photons
 - Photons pair produce secondary particles
 - Muons
 - Pions & Kaons: muons & neutrinos
- ~ 50 years ago: SLAC muon beam

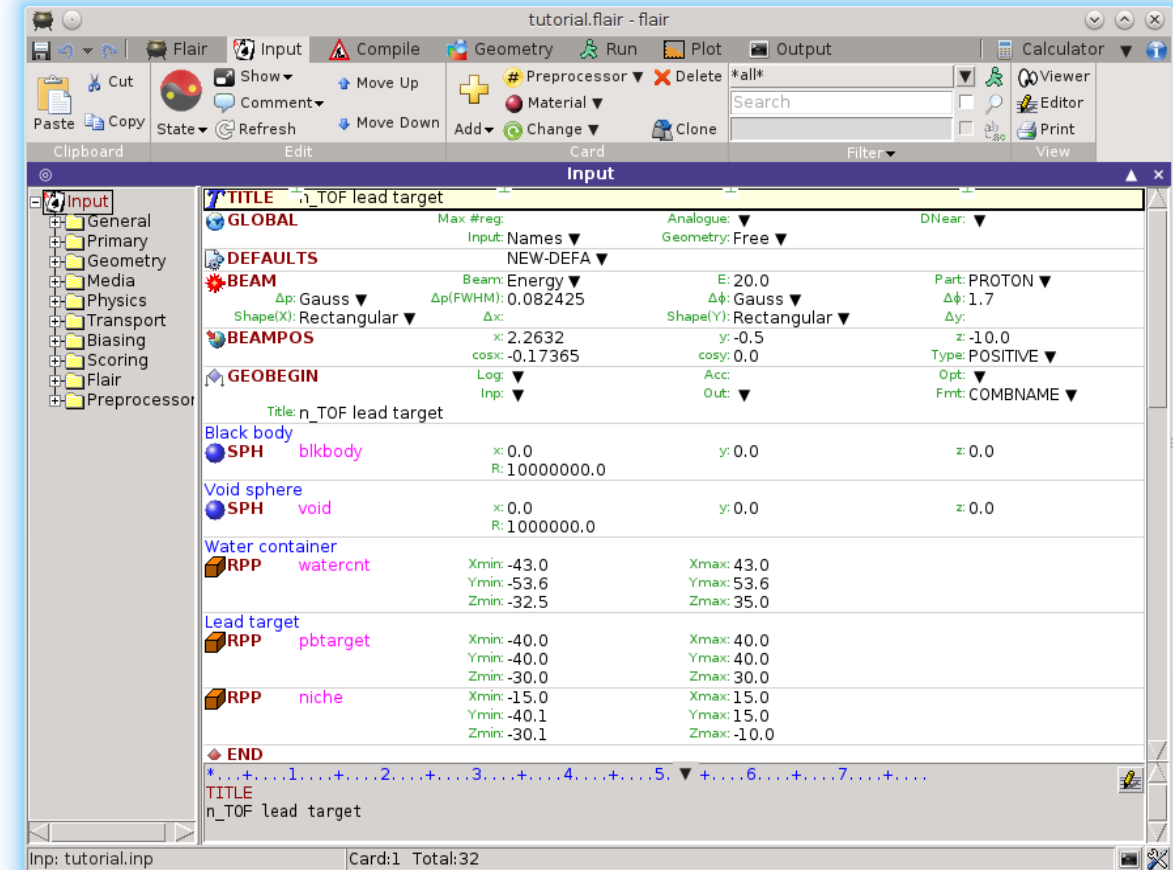


- Beam: electron
 - $E_{e^-} = 21$ GeV
- Target: copper
- $E_{\mu} = 14$ GeV
- $I_{\mu} = 10^4$ μ/s



Simulation Framework

- **Monte Carlo simulations**
 - Repeated sampling to obtain numerical results
 - Main Monte Carlo software in particle physics:
 - Geant4
 - FLUKA
- **FLUKA**
 - User interface (FLAIR)
 - **Ready-to-use biasing technique**
 - Importance region sampling, leading particle biasing, interaction length biasing, etc.
- **e^- + BD simulations needed bias**
 - Rare processes possible thanks to the high-intensity
 - **1 year of beam is $\sim 10^{22} e^-$ @HallA**
 - Standard & custom techniques used



Geometry

BD & Concrete Vault geometry cross-checked with civil drawings
Framework: FLUKA 4-5.0

Beam: e^- @ 11 GeV
Position: on the dump

Physics:

- Muon photon nuclear interactions
- Pair production and bremsstrahlung by muons on
- Photo-nuclear interactions on
- Pair production of muons on with bias (x1M)
- Electro-nuclear interactions on
- Decay of $\mu^\pm, \pi^\pm, K^\pm, K^0$
- Evaporation model on
- Colaescence model on

Transport:

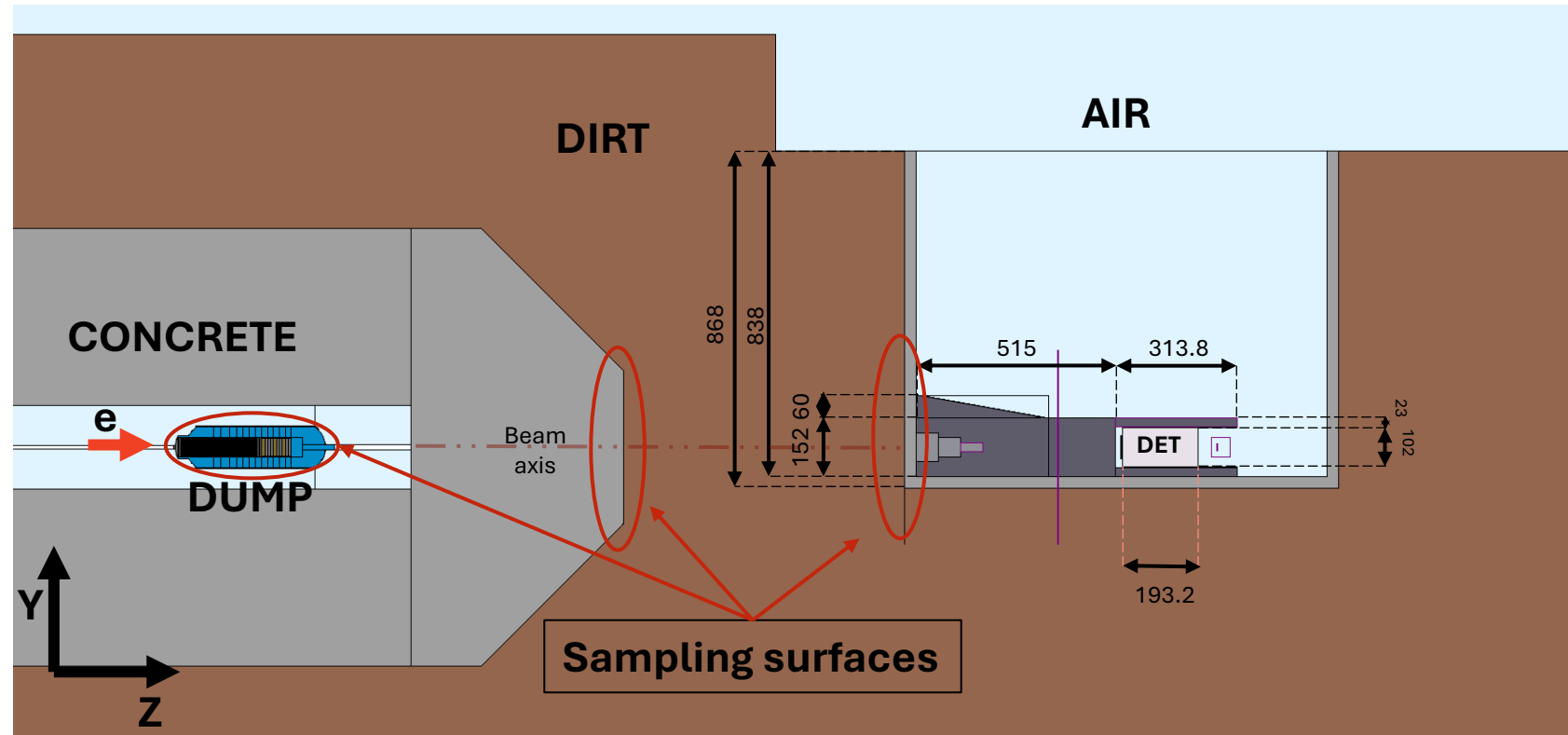
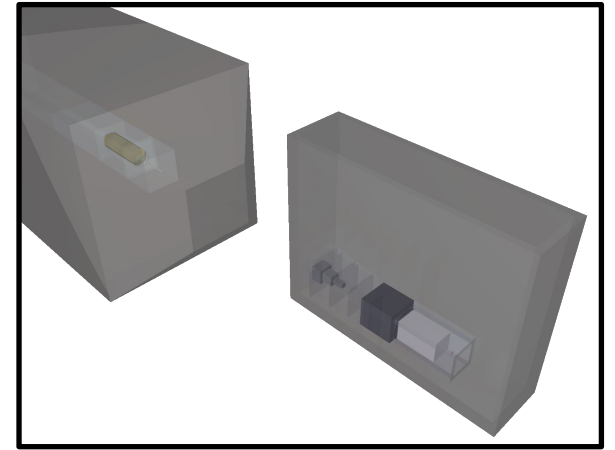
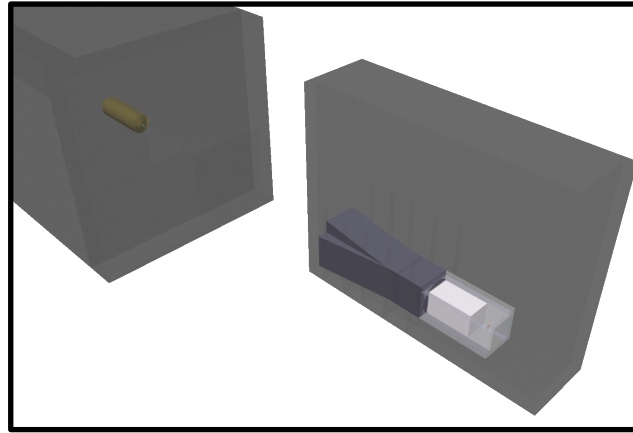
- $\mu^\pm, \pi^\pm, K^\pm, K^0$ activated decay-at-rest
- $\gamma, e^\pm$ cut < 0.1 GeV

Bias:

- Leading-particle
- Lambda bias inelastic (x100)
- Custom for neutrons

Scoring: boundary crossing with user routines

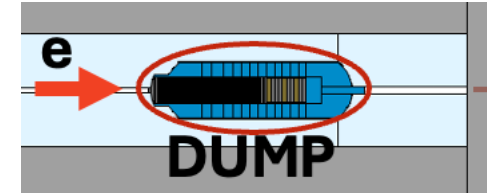
Results normalized to “Electron On Target” (EOT)



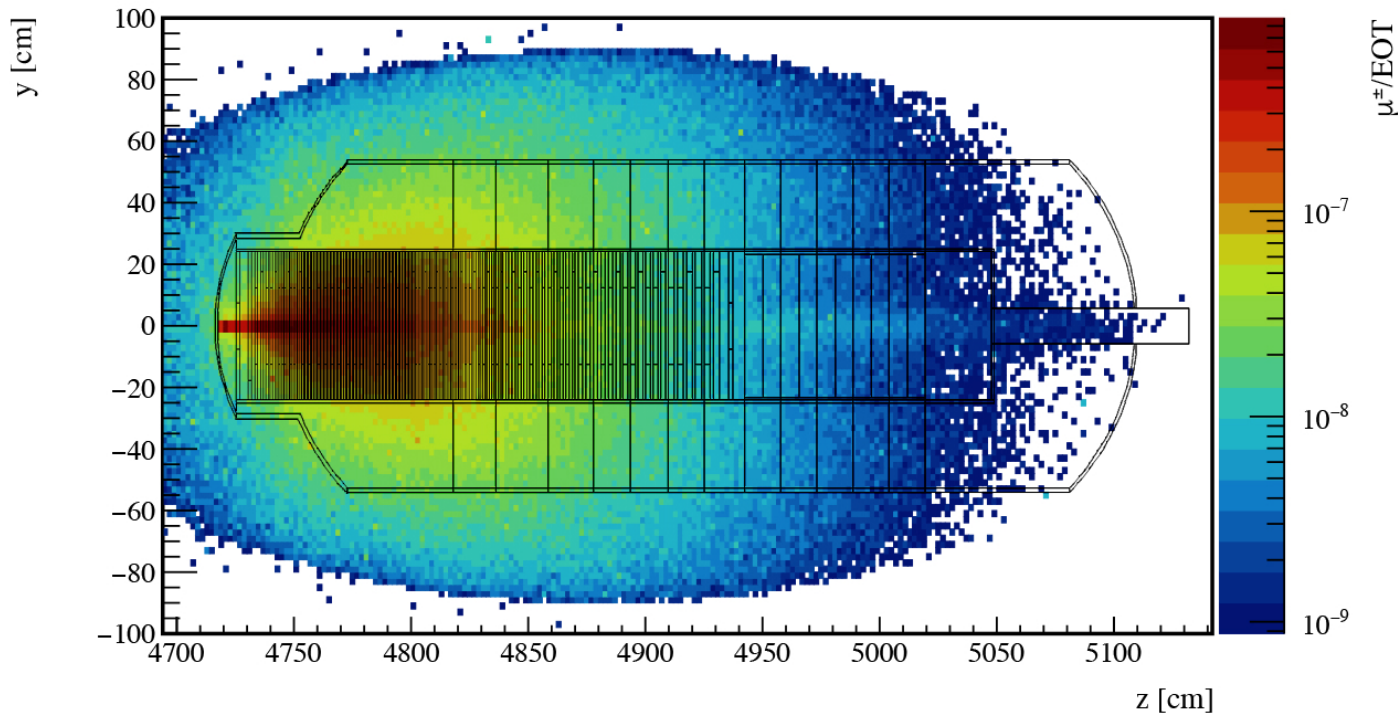
MUON RESULTS

Secondary Muon Beam

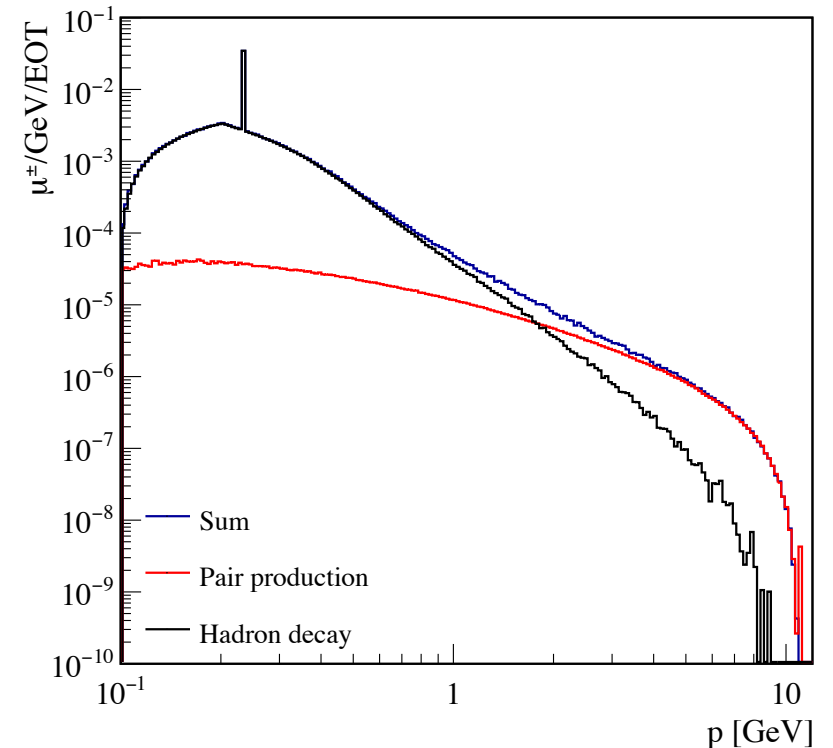
- Muons sampled around the beam-dump
- ~90% of muons produced at the beginning of the beam-dump
- High energy muons: **photoproduction**
- Low energy muons: **hadron decays (pions & kaons)**
 - Peak at 235 MeV: $K \rightarrow \mu + \nu_e$



Muons sampled around the beam-dump



Muon production vertexes with beam-dump outline

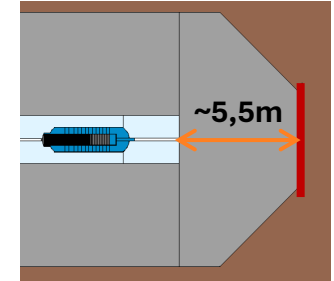


Muon production

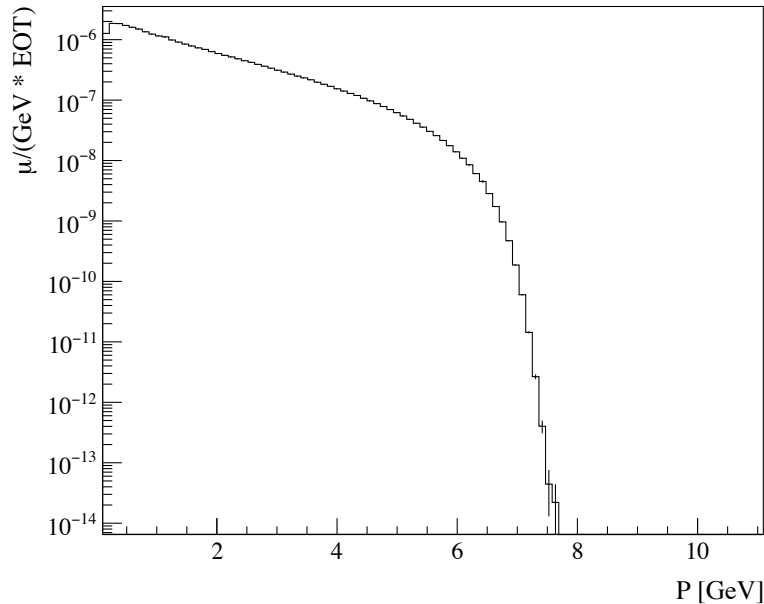
Secondary Muon Beam

- Muons sampled at the end of the BD's concrete vault
- Main features:
 - Typical of bremsstrahlung
 - Cut $E_{\text{kin}} > 100 \text{ MeV}$
 - Beam partially focused
 - $\sim 50\%$ are contained within $r \approx 25 \text{ cm}$
 - Higher energy muons produced at small angles

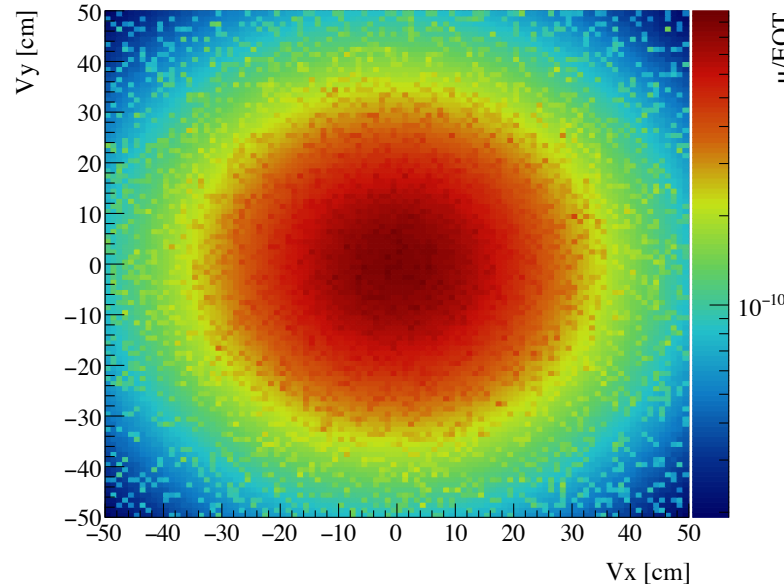
- Estimated flux:
 - $100 \times 100 \text{ cm}^2$: $2.5 \times 10^{-6} \mu^\pm / \text{EOT}$
- Spatial distribution:
 - $\sigma_x \approx \sigma_y \approx 24 \text{ cm}$
- Distance from the BD's tunnel end: $\sim 5.5 \text{ m}$



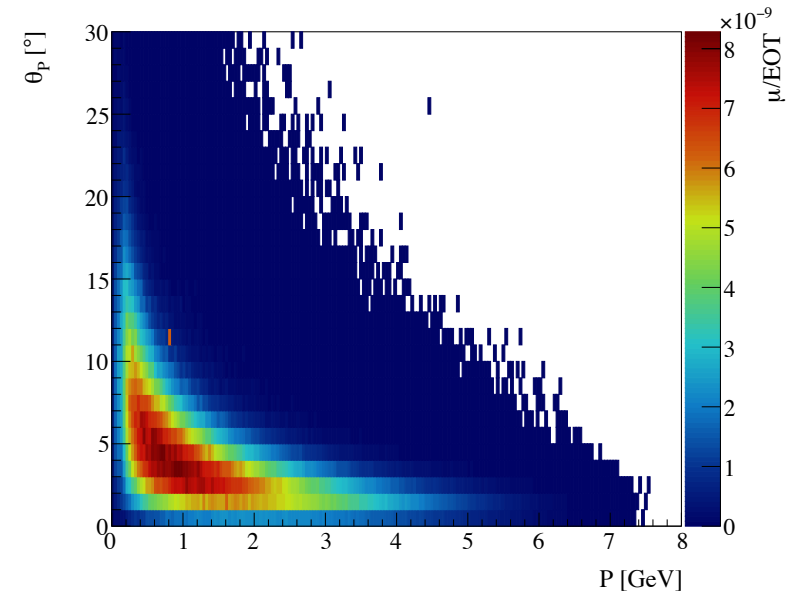
Muons sampled at the end of the beam-dump's concrete vault (1 m^2)



Muon beam spectrum



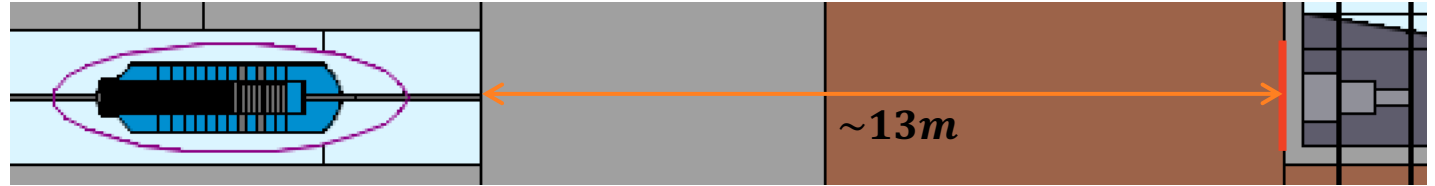
Muon beam spatial distribution



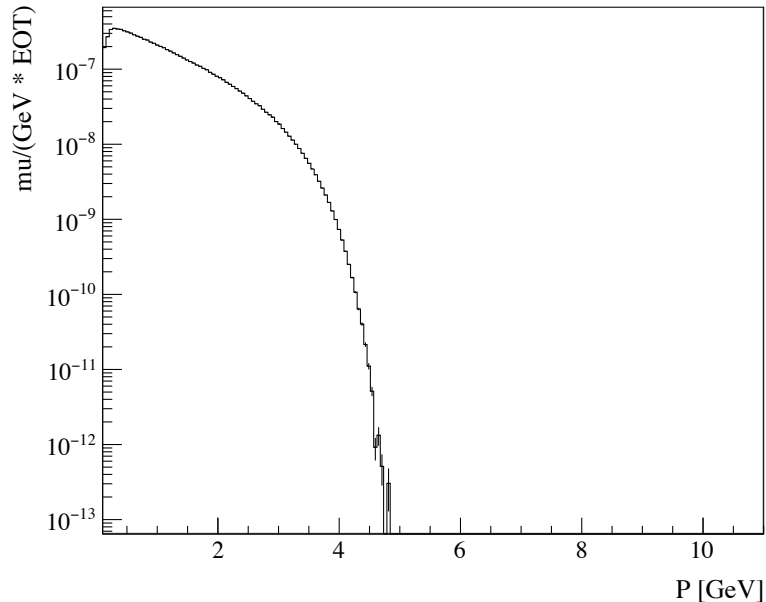
Muon beam energy-angle distribution

Secondary Muon Beam

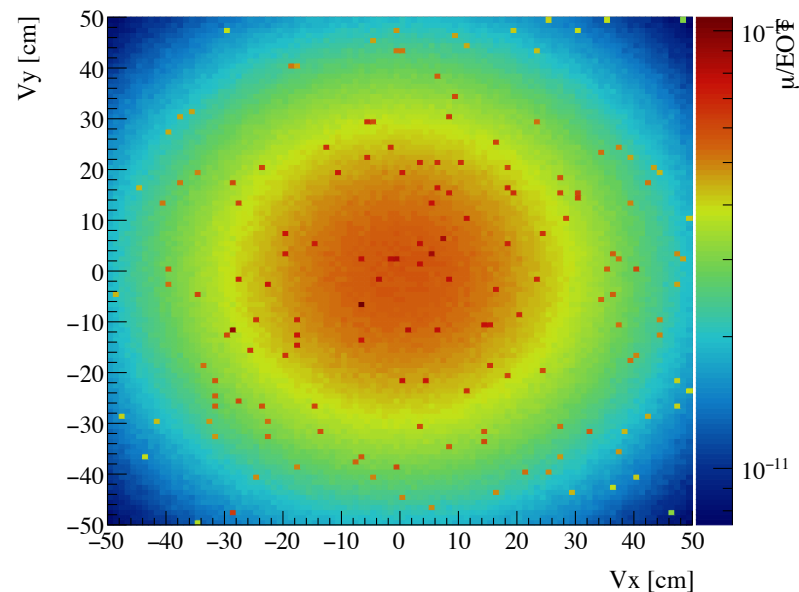
- Muons sampled at the beginning of the BDX pit
- Estimated flux:
 - $100 \times 100 \text{ cm}^2$: $3.0 \times 10^{-7} \mu^\pm/\text{EOT}$
- Spatial distribution:
 - $\sigma_x \approx \sigma_y \approx 35 \text{ cm}$
- Distance from the BD's tunnel end: $\sim 13\text{m}$



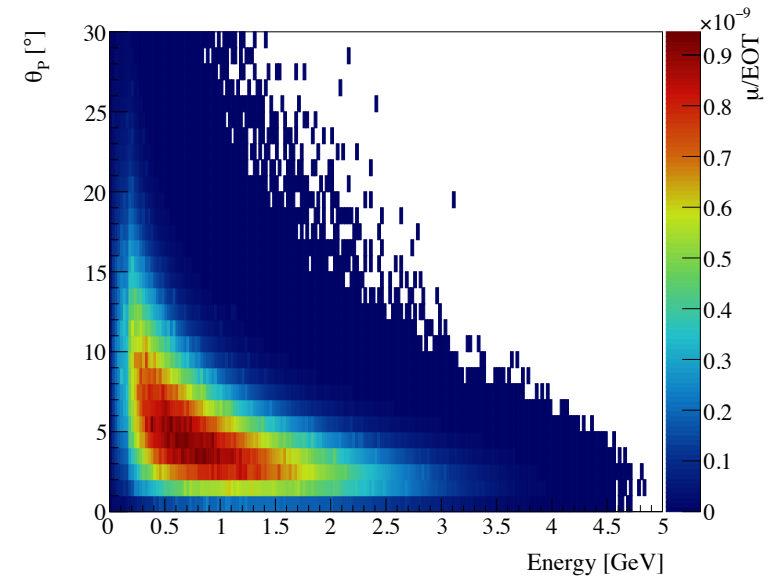
Muons sampled at the beginning of the BDX pit (1m^2)



Muon beam spectrum



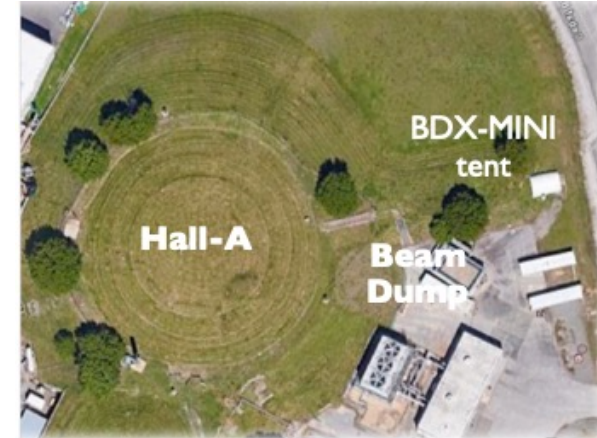
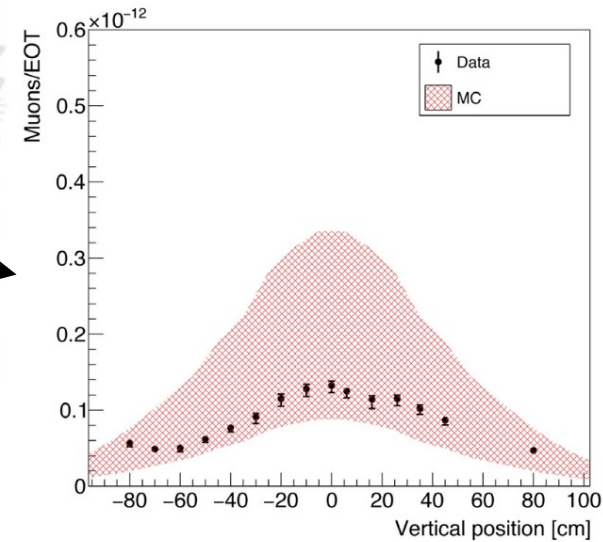
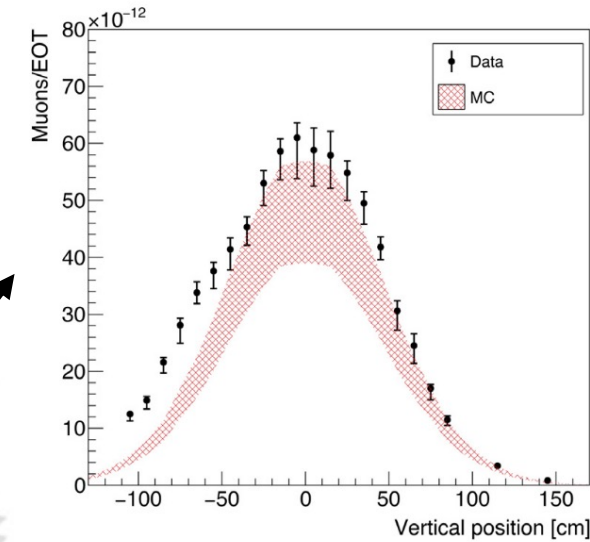
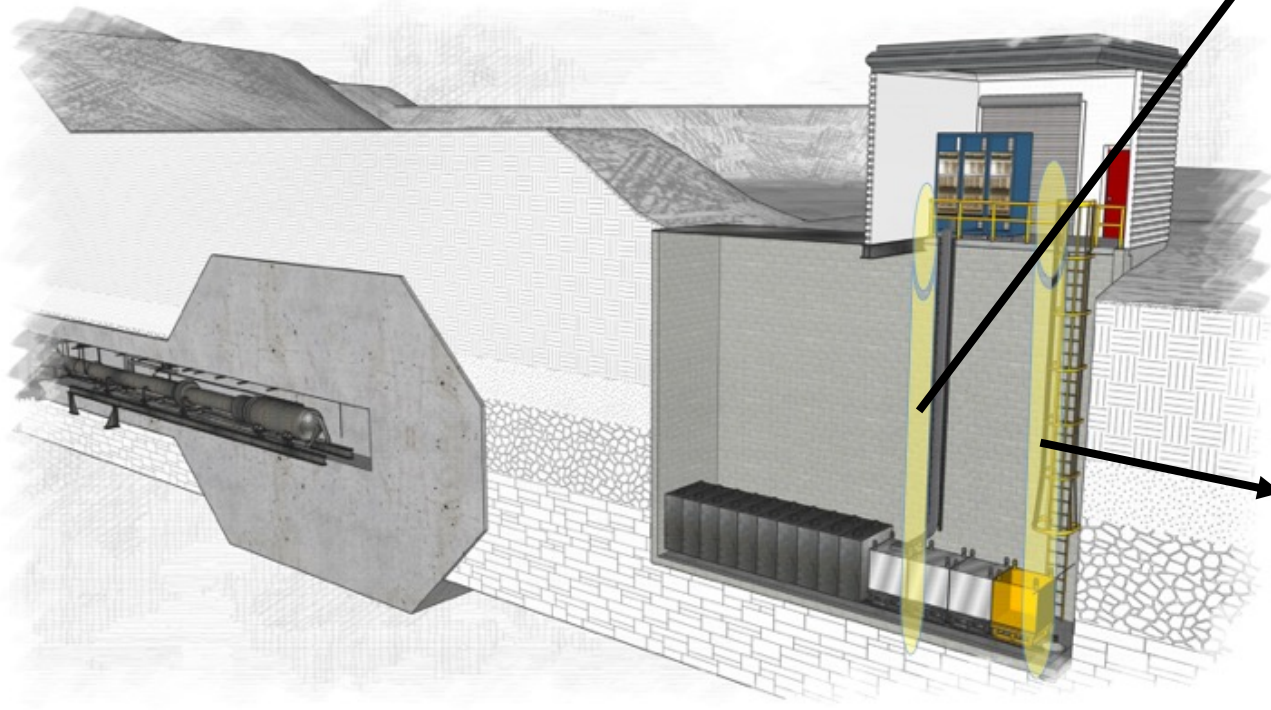
Muon beam spatial distribution



Muon beam energy-angle distribution

Simulation framework validation with μ BDX experiment

- Comparison between simulated and measured muon rates as a function of vertical height
 - Flux dependant on density variation
 - Simulation ran with $\rho_{dirt} = 1.93 \text{ g/cm}^3$ and $\rho_{concrete} = 2.3 \text{ g/cm}^3$



NEUTRINO RESULTS

Secondary Neutrino Beam

➤ Main features:

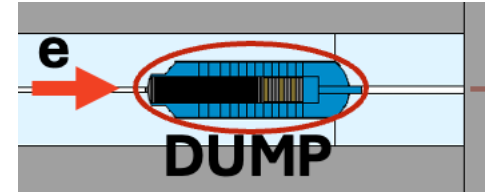
- Isotropic distribution
- Peak at 29.8 MeV:
- Neutrinos from $0 < E_\nu < 52.8$ MeV:
- Peak at 236 MeV:
- Peak at 70 MeV (suppressed):

$$\pi^+ \rightarrow \mu^+ + \nu_\mu$$

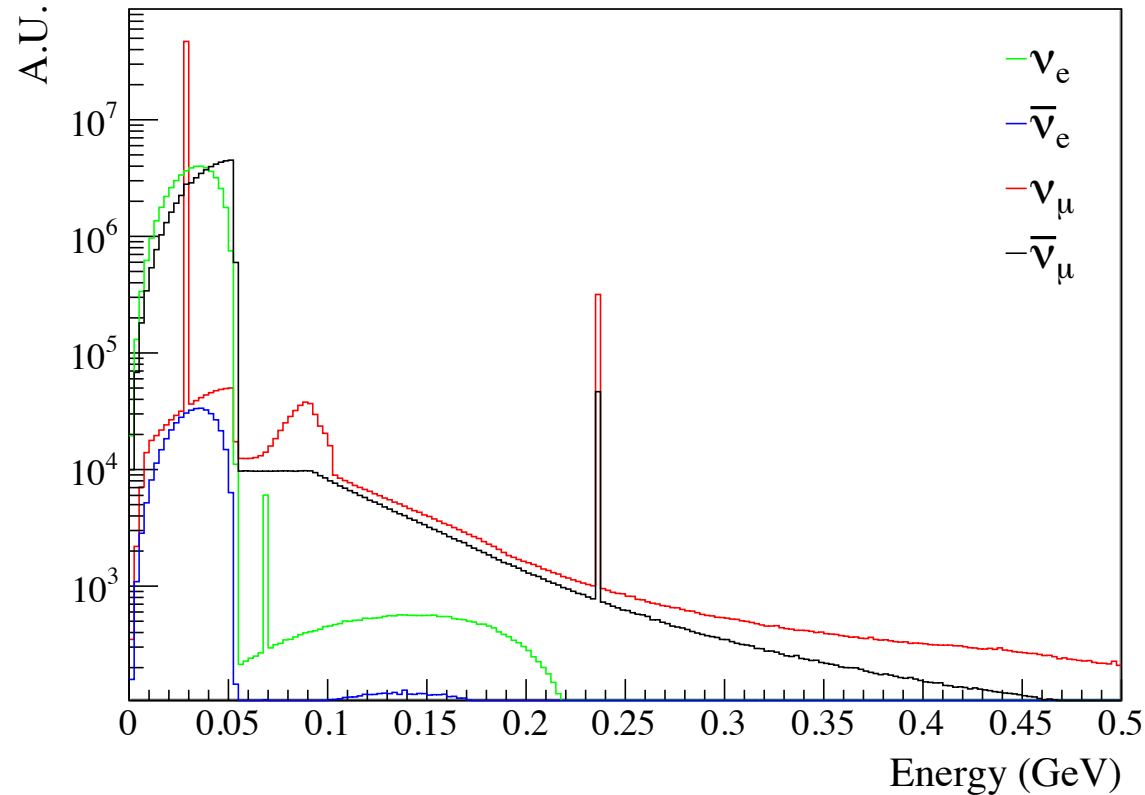
$$\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

$$K^+ \rightarrow \mu^+ + \nu_\mu$$

$$\pi^+ \rightarrow e^+ + \nu_e$$



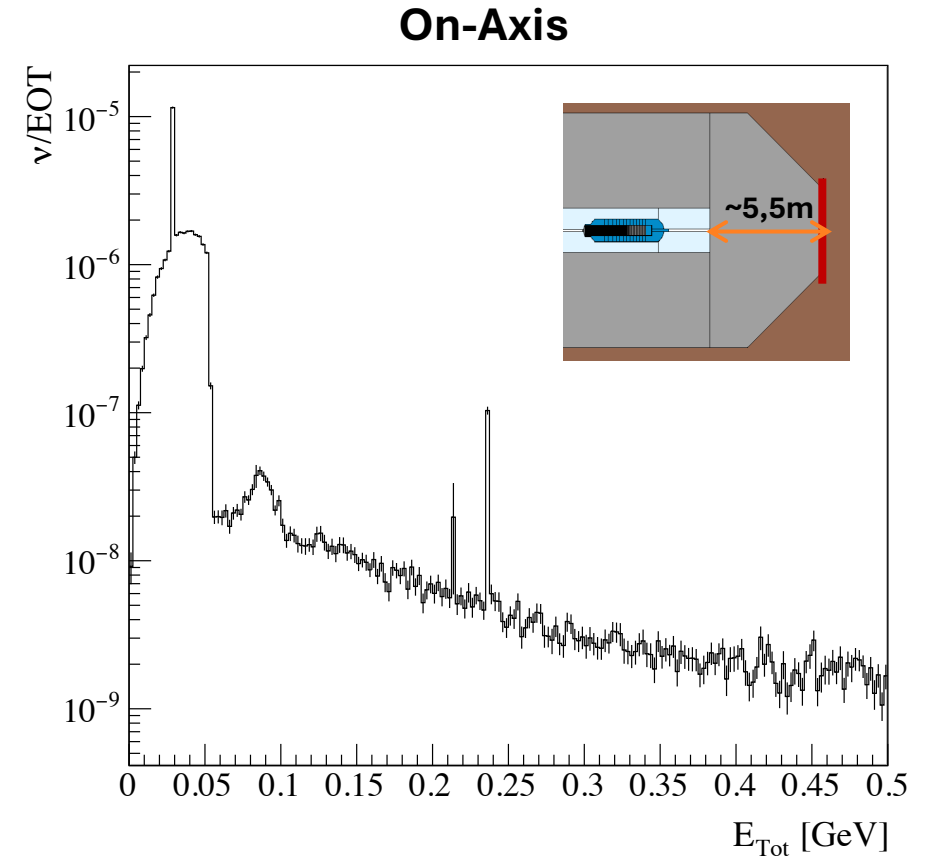
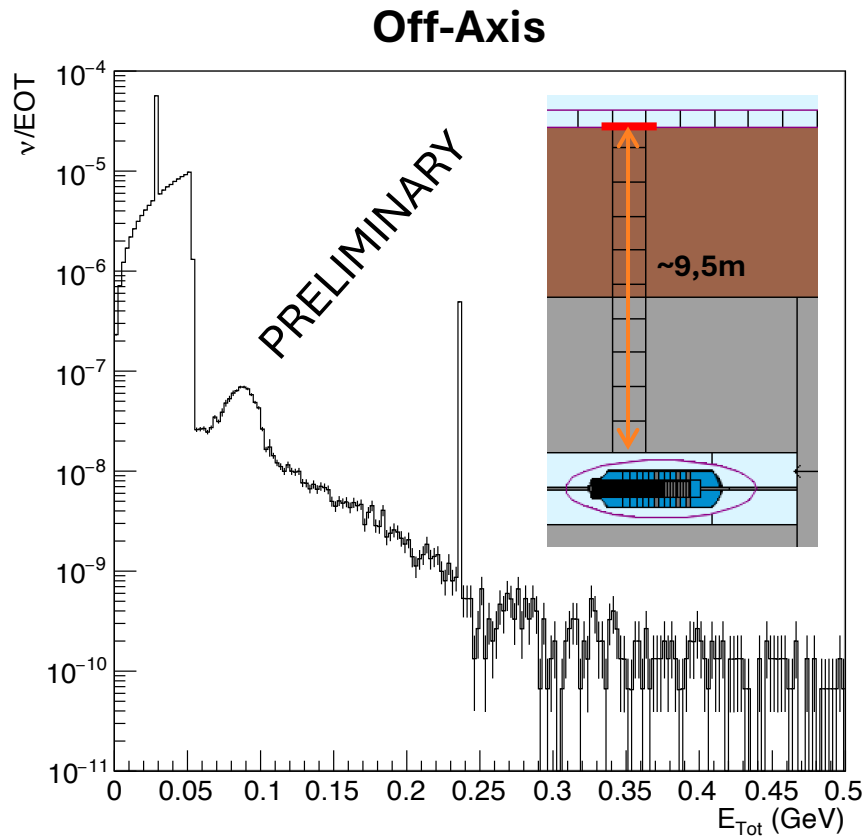
Neutrino sampled around the beam-dump



On/Off axis neutrino flux

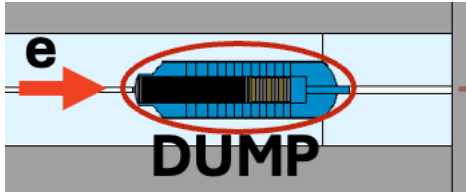
➤ Estimated flux:

- On-Axis: $\sim 3.0 \times 10^{-5} \nu/\text{EOT}$ @ 11 GeV e^- beam
- Off-Axis: $\sim 6.7 \times 10^{-5} \nu/\text{EOT}$ @ 11 GeV e^- beam



NEUTRON RESULTS

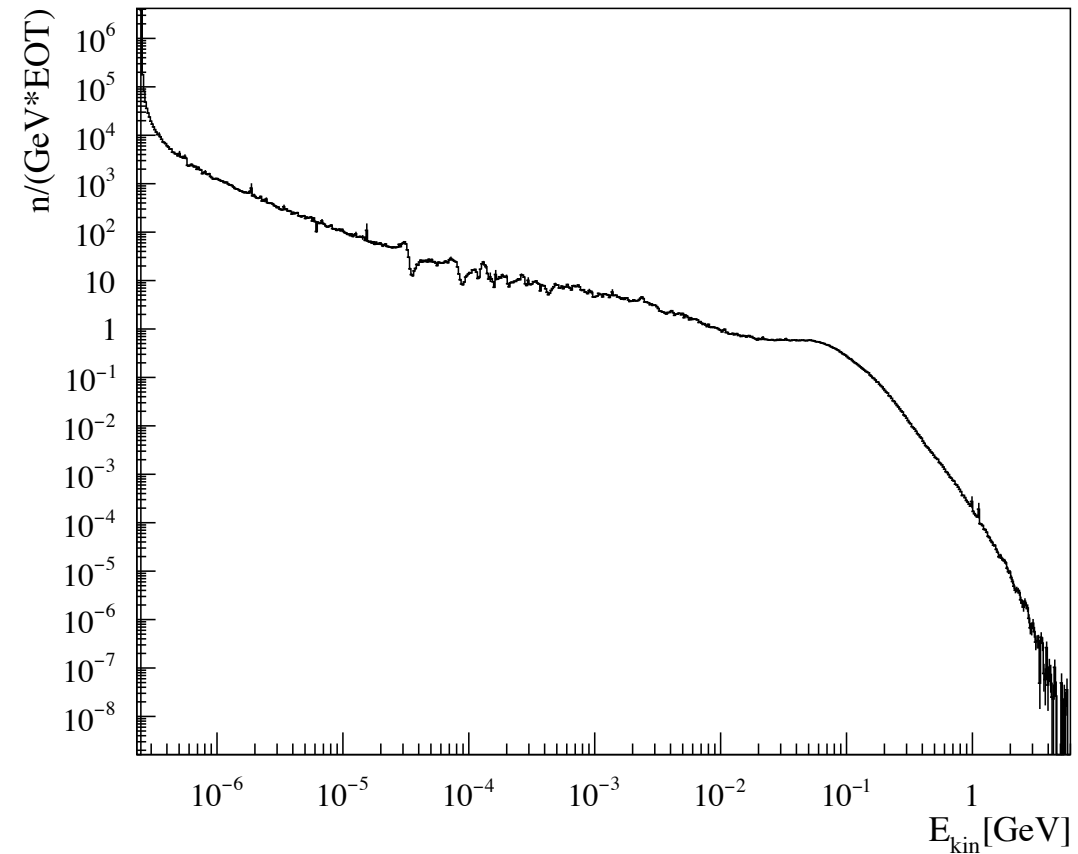
Secondary Neutron production



Neutrons sampled around the beam-dump

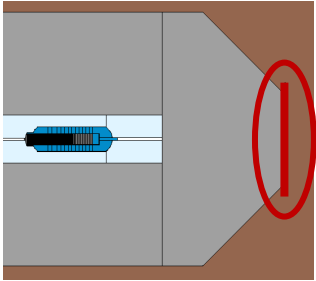
Energy Range	n/EOT
0 - 6GeV	1.26e-01
0.1eV - 100.0eV	0.00e+00
100.0eV - 100.0keV	3.42e-02
100.0keV - 1.0MeV	7.23e-03
1.0MeV - 100.0MeV	6.66e-02
100.0MeV - 2.0GeV	1.82e-02
2.0GeV - 6.0GeV	3.31e-06

$$0.1 \text{ eV} < E_{kin} < 6 \text{ GeV}$$

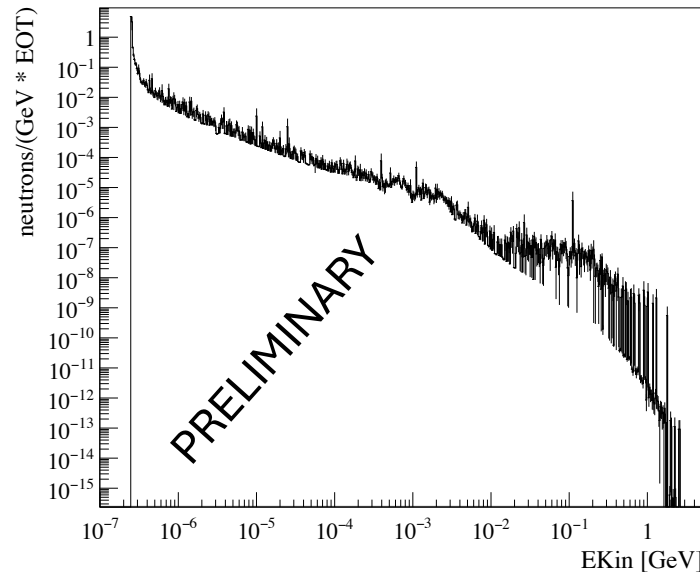


Neutron propagation

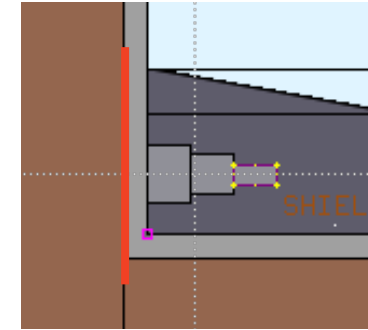
- Low statistics simulations
 - Right now implementing ad hoc biasing techniques



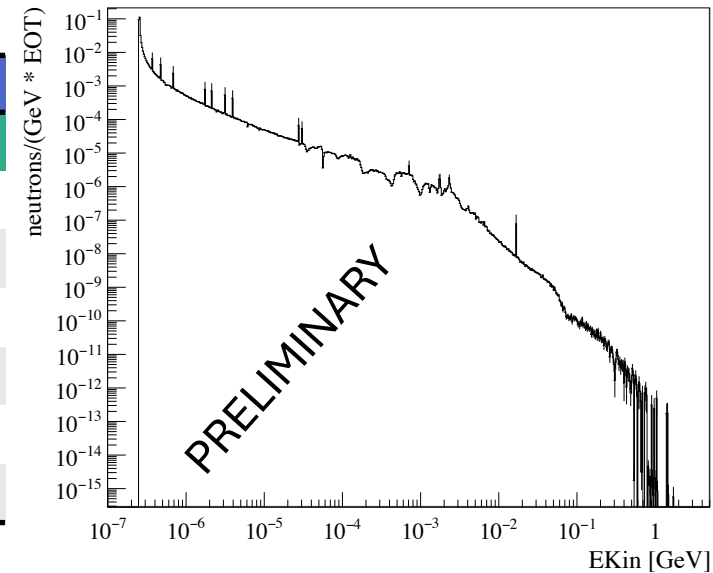
Neutrons sampled at the end of the beam-dump's concrete vault
500x500cm²



Energy Range	n/EOT
0 - 6GeV	3.87E-08
0.1eV - 100.0eV	0
100.0eV - 100.0keV	2.25E-08
100.0keV - 1.0MeV	4.31E-09
1.0MeV - 100.0MeV	6.9E-09
100.0MeV - 2.0GeV	5.03E-09
2.0GeV - 6.0GeV	5.87E-15



Neutrons sampled at the start of the BDX pit
500x500cm²



Energy Range	n/EOT
0 - 6GeV	2.63E-09
0.1eV - 100.0eV	0
100.0eV - 100.0keV	1.40E-09
100.0keV - 1.0MeV	5.55E-10
1.0MeV - 100.0MeV	6.78E-10
100.0MeV - 2.0GeV	2.23E-12
2.0GeV - 6.0GeV	0

THANK YOU!

Neutrons Jlab - Propagation

The neutrons are then propagated to the BDX room.

In doing this a custom bias is used in order to give more importance to the neutrons moving towards the CCD.

This is done by implementing a custom directional biasing using a FLUKA Fortran user routine (usimbs.f)

The implementation implements **importance biasing** for neutrons to improve simulation efficiency by "steering" neutrons toward a detector region.

Directional Biasing Algorithm

Calculates distance from current neutron position to target

Computes cosine of angle between neutron direction and target direction

Adjusts particle importance based on this angle:

cos = 1: Neutron heading directly toward target → no change

cos = 0: Neutron perpendicular to target → importance reset to 1

cos < 0: Neutron heading away from target → Russian Roulette applied

Importance Modification

$Weight = Weight \times \cos_direc$

Increases survival probability for neutrons heading toward detector

Decreases survival probability for neutrons heading away

EXAMPLE:

If a neutron has $FIMP = 0.1$:

- 90% chance the particle is killed
- 10% chance it survives with 10× higher weight

Result: Same expected contribution, but 90% fewer particles to track

PROs:

Eliminates neutrons unlikely to reach the detector

Focuses computing power on important particles

Expected values remain unchanged

Variance may actually decrease

FLUKA automatically applies Russian Roulette when $FIMP < 1.0$

No additional coding required