

Short-Range Nuclear Structure: First Experimental Results

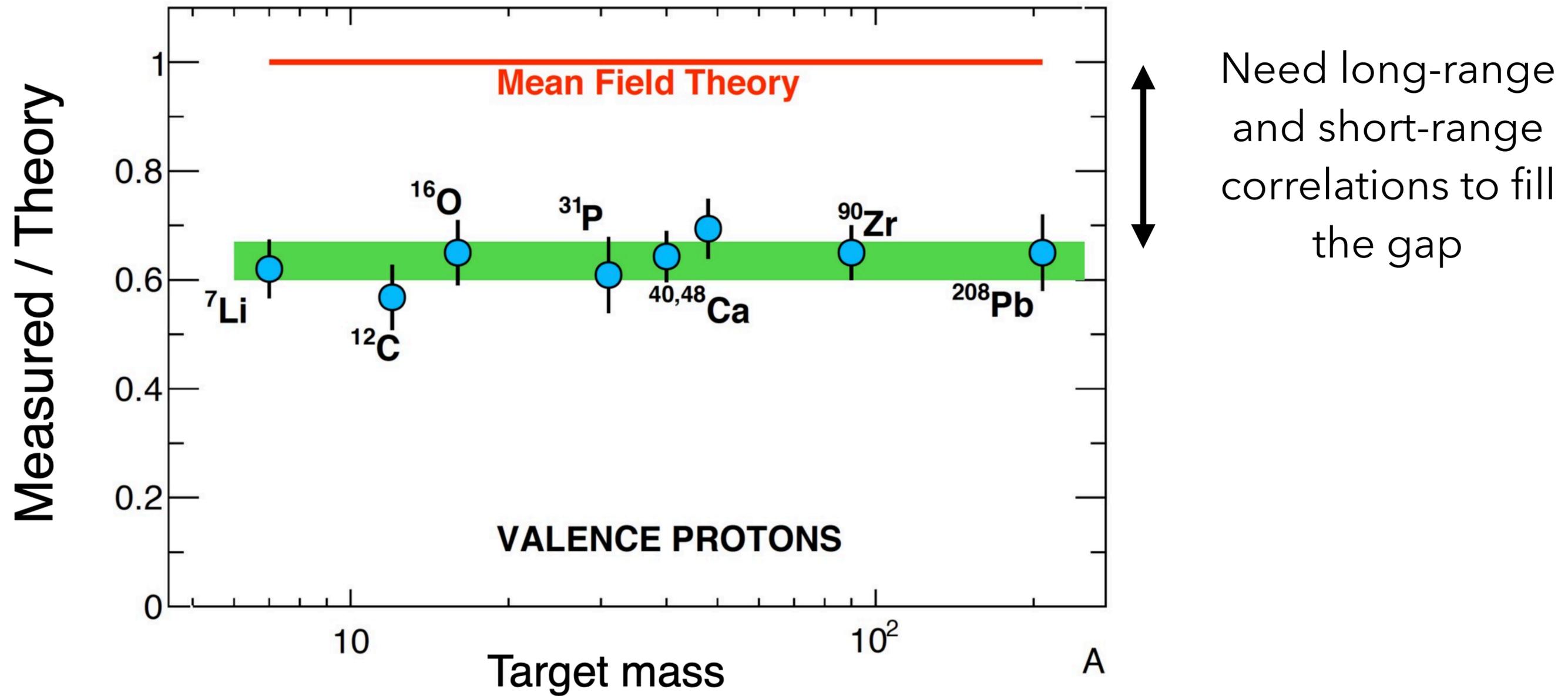
Jackson Pybus

Directors' Fellow, Los Alamos National Laboratory

"Light-ion physics in the EIC era"

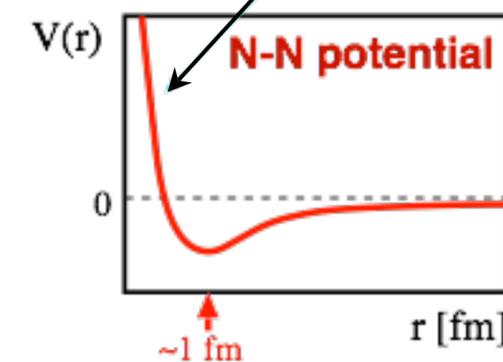
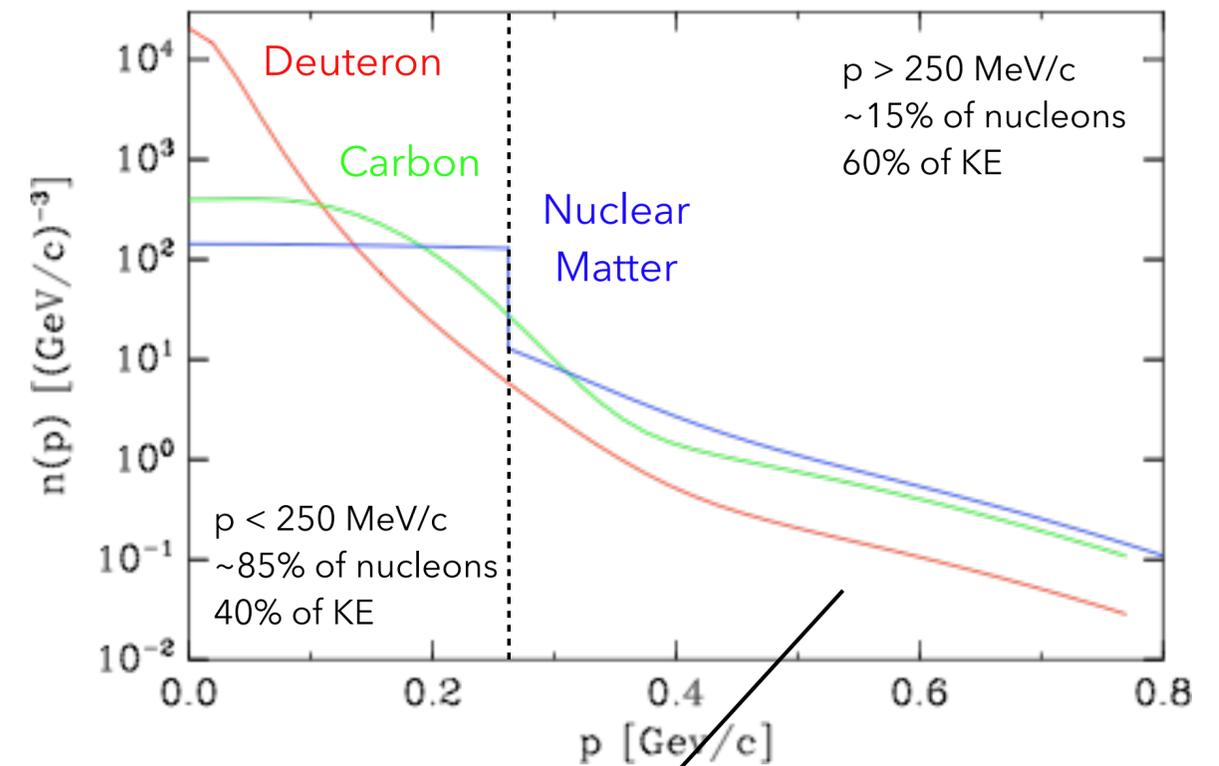
June 2025, Florida International University, Miami, FL

Nuclear Shell Model cannot explain the entire nucleus



Short-Range Correlations

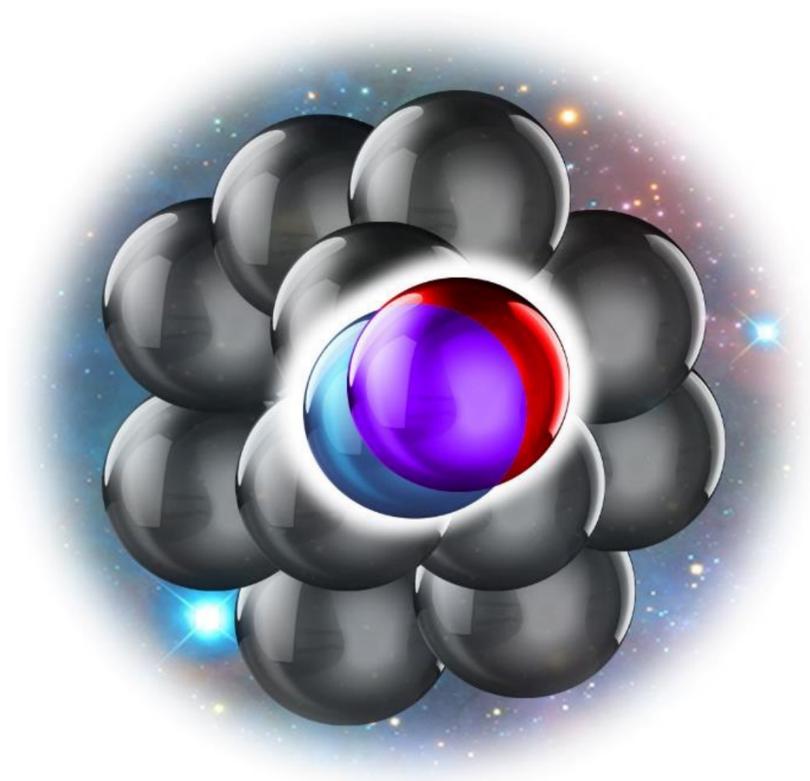
- IPSM describes $k < k_{Fermi} \approx 250 \text{ MeV}/c$ well, but missing strength
- Nuclear structure calculations show high-momentum tail $k > k_{Fermi}$
 - Dominated by two-nucleon "Short-Range Correlations" (SRCs)
- Small fraction (10-20%) of nucleons, but large impact on overall structure



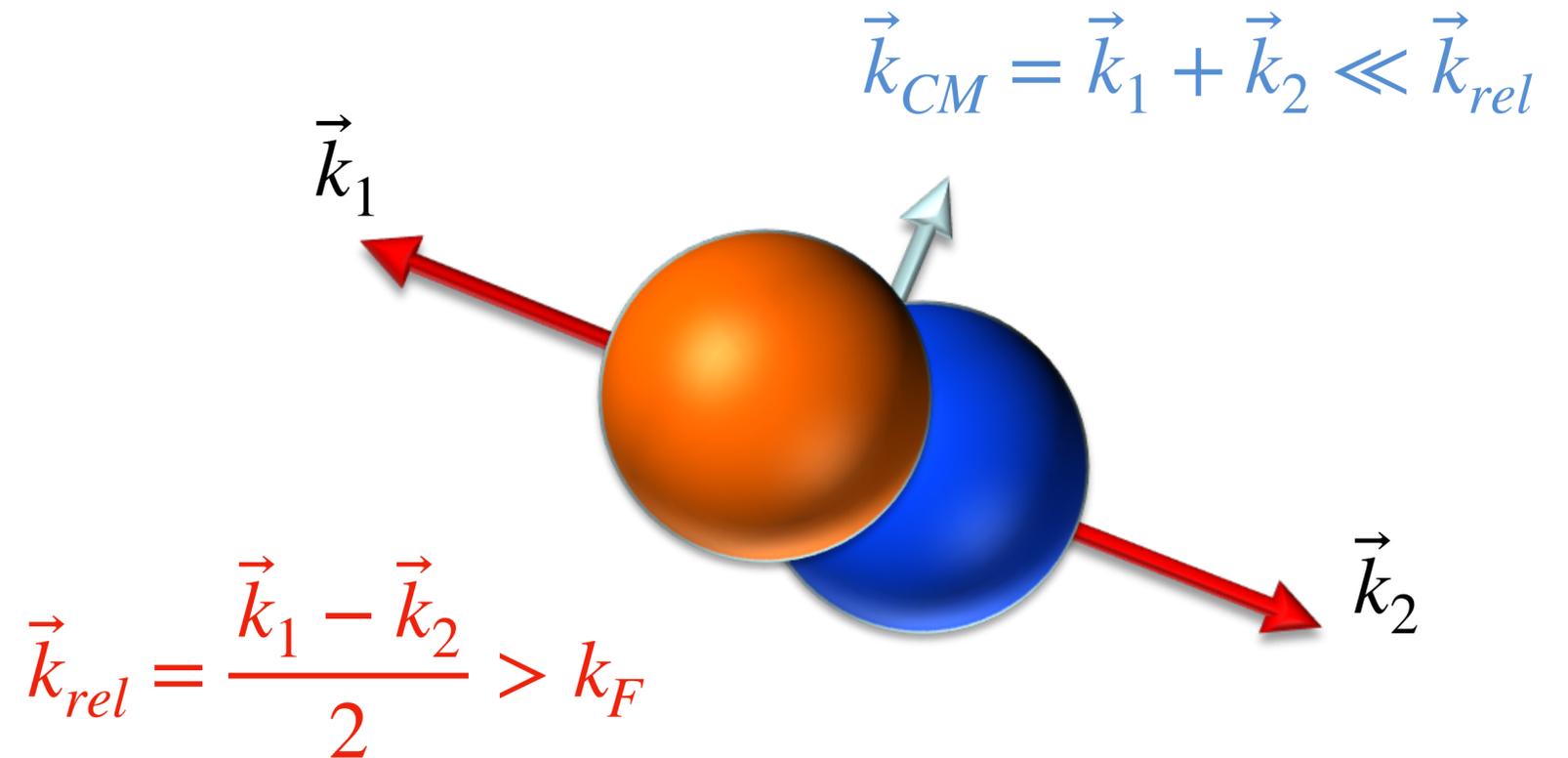
Short-Range Correlations

Nucleon pairs that are very close together in the nucleus

Momentum-space: Large **relative** and lower **C.M.** momentum



Position-space

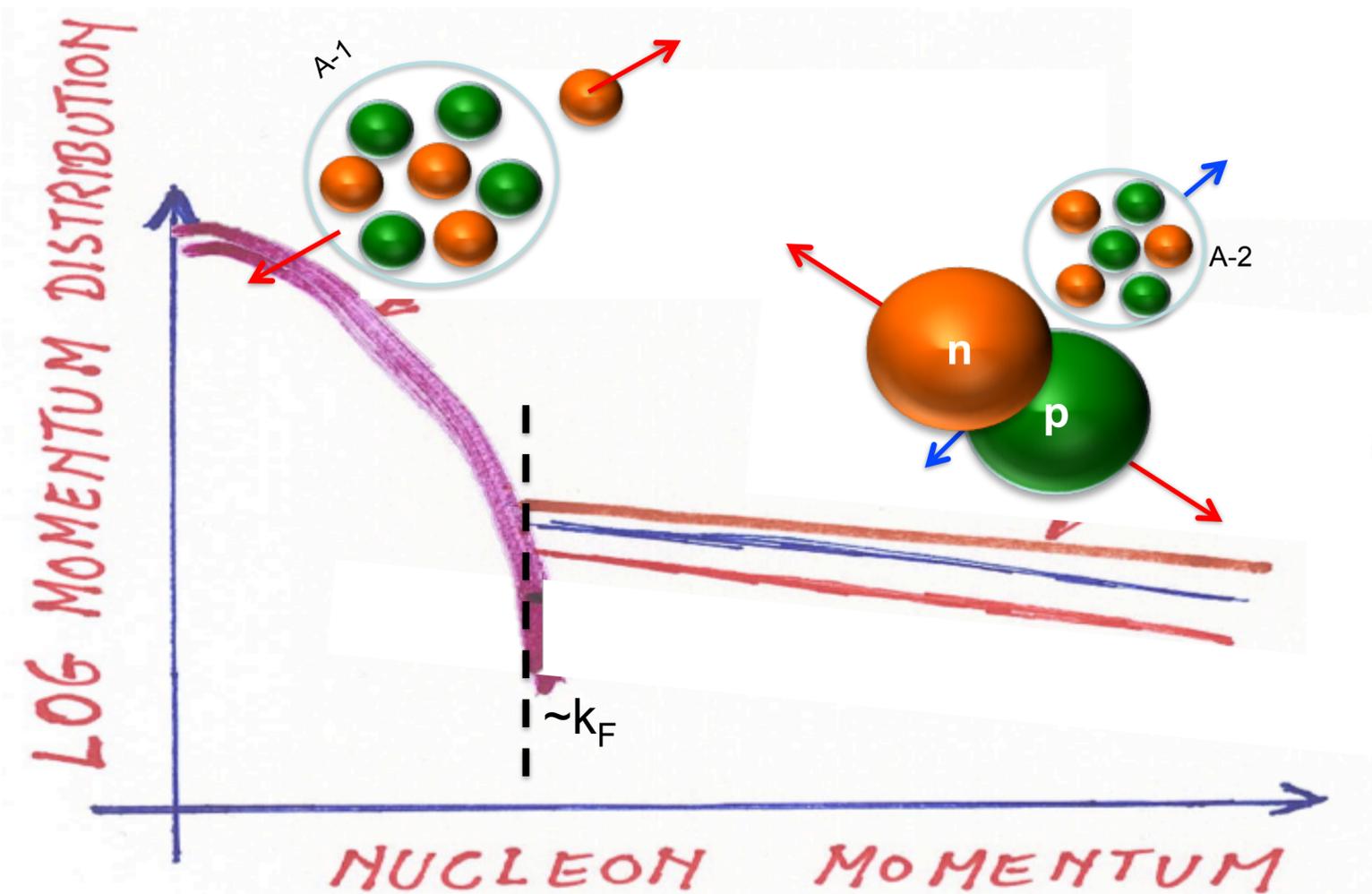


Momentum-space

Shell model + LRCs
(Mean field)

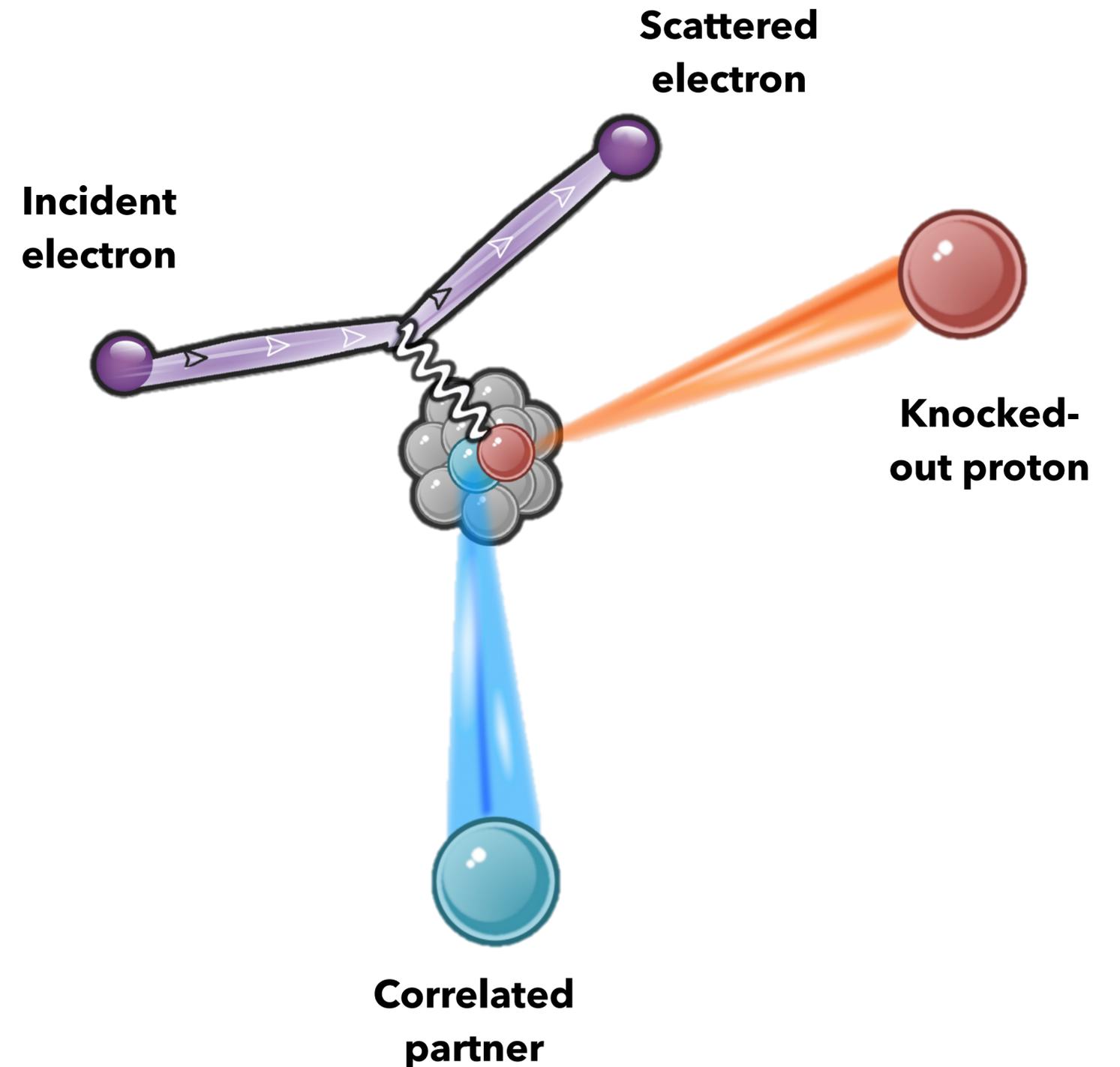
+

SRC Pairs



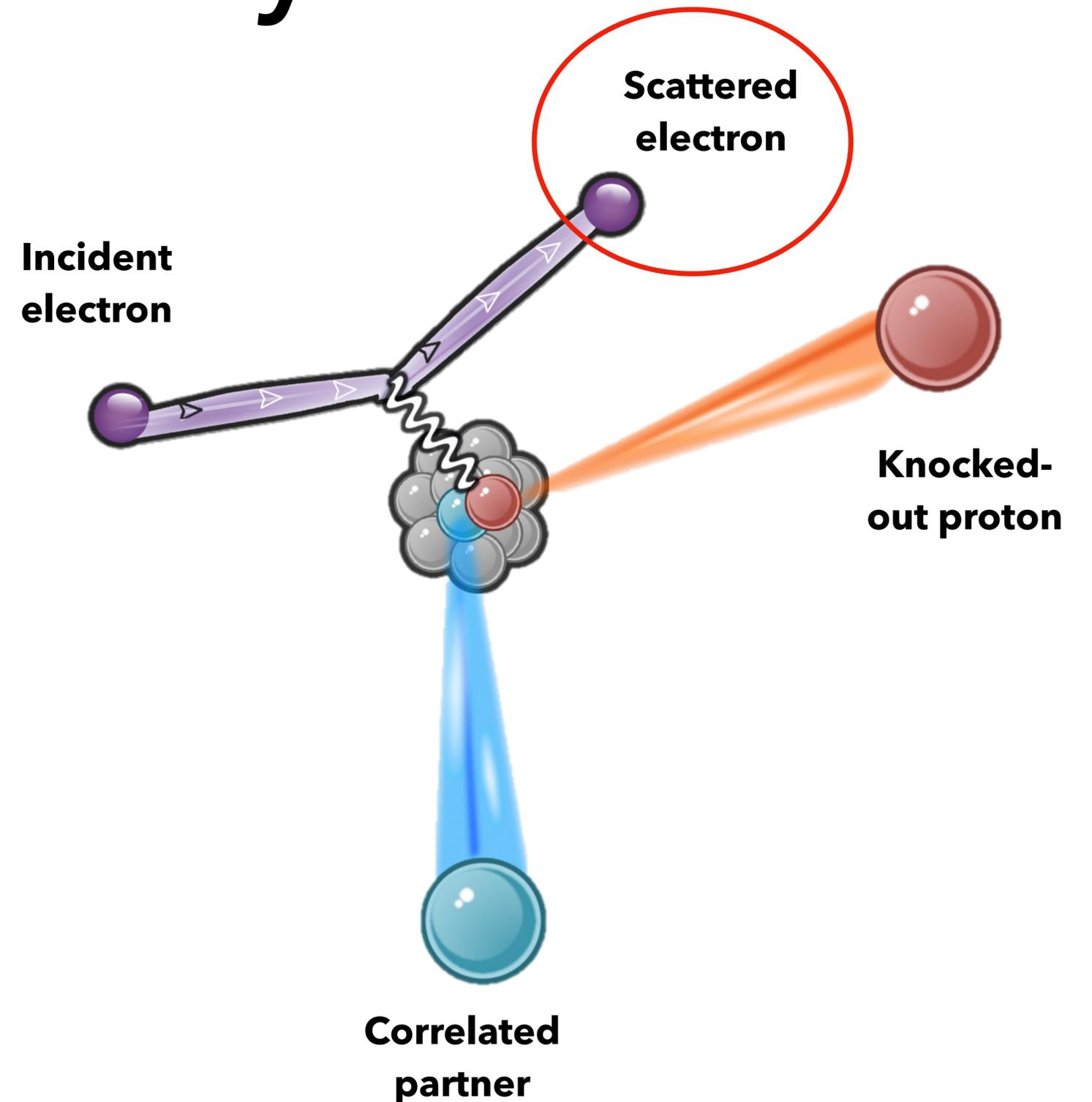
How do we study SRC?

- Hard knockout reactions – large momentum-transfer to a bound nucleon in the nucleus
- For SRC pairs, partner/spectator nucleon also recoils from the nucleus
- Different channels for studying SRCs:
 - Inclusive (e, e')
 - Semi-inclusive ($e, e'N$)
 - Exclusive ($e, e'NN$)



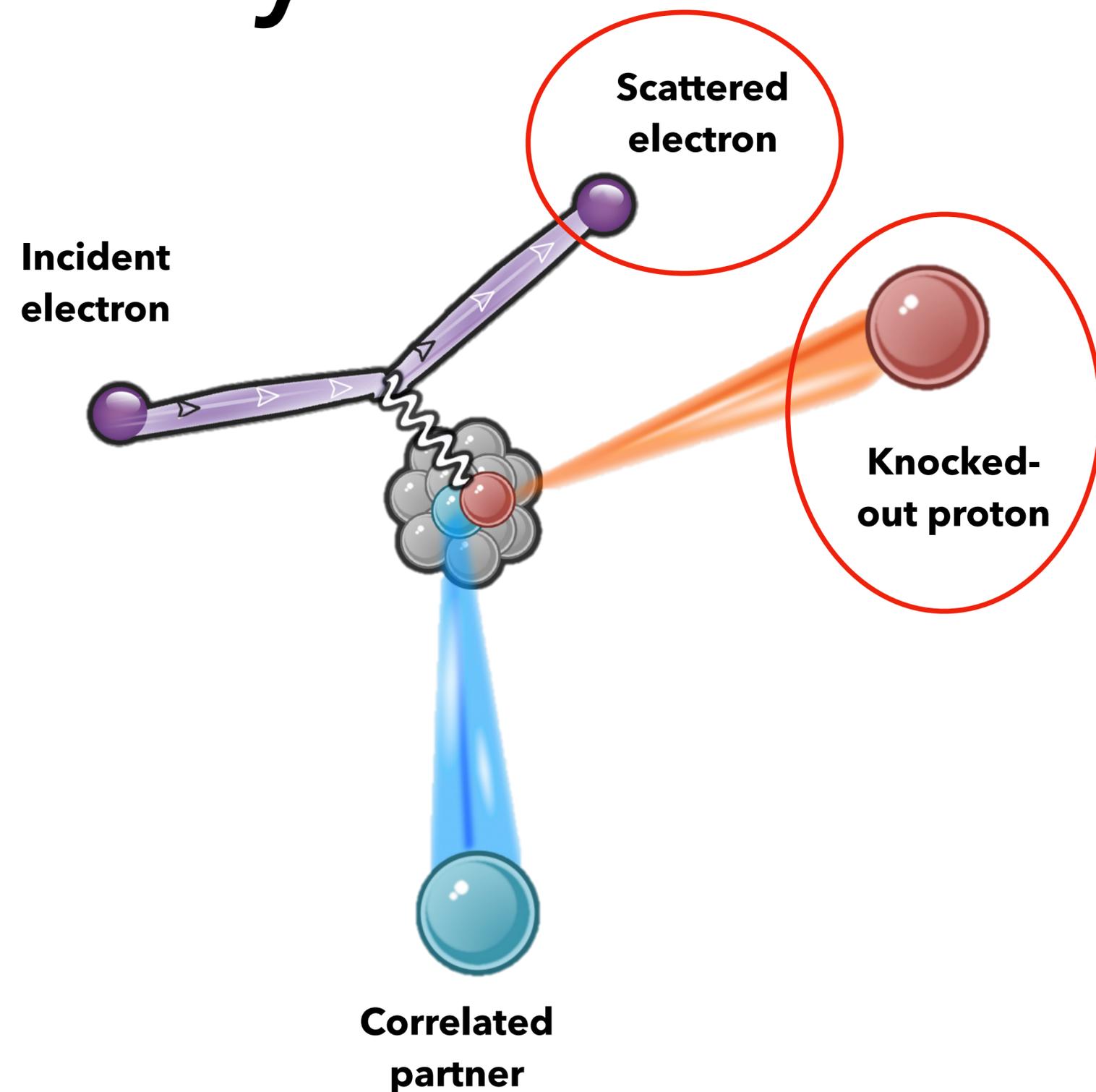
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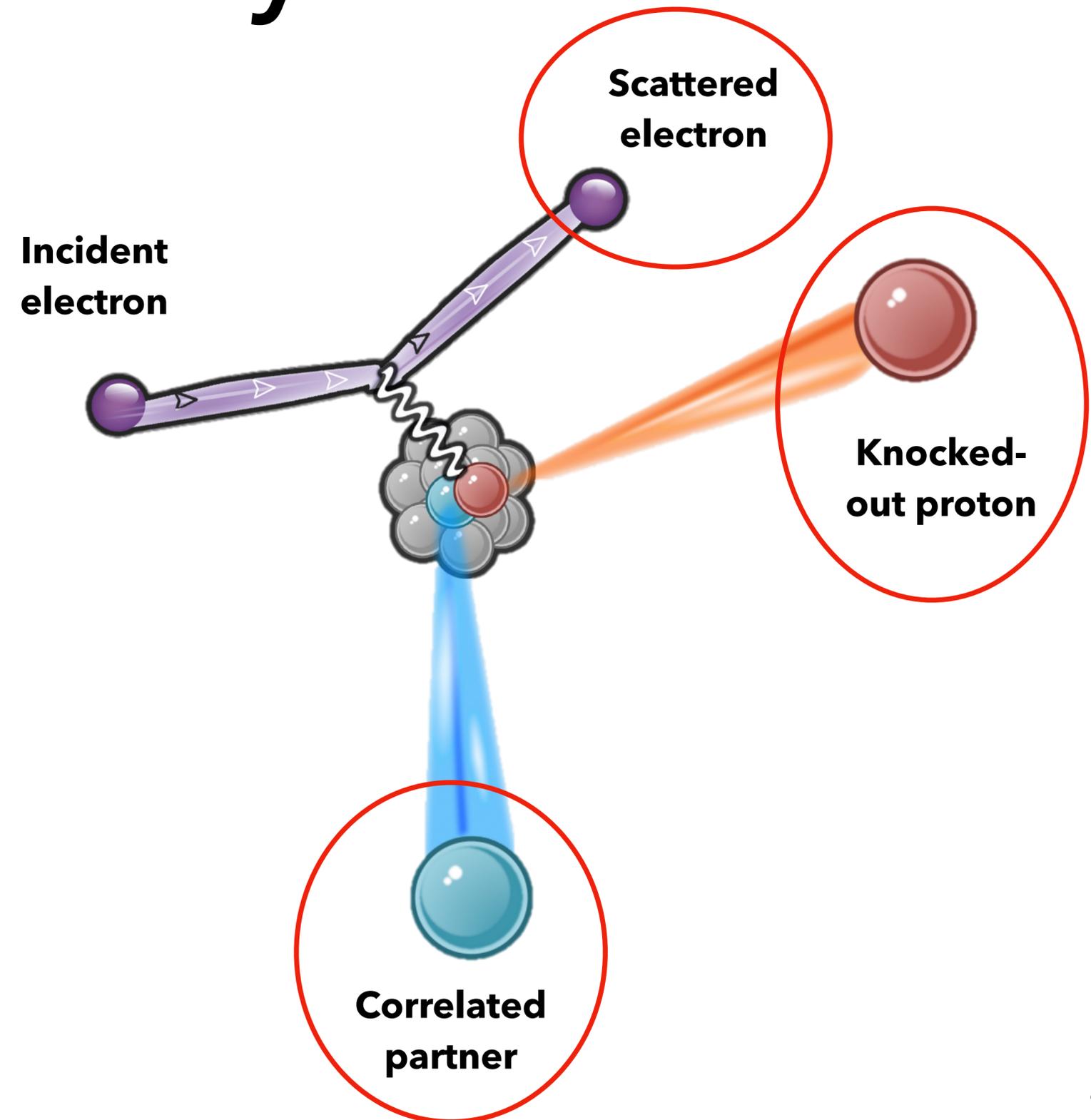
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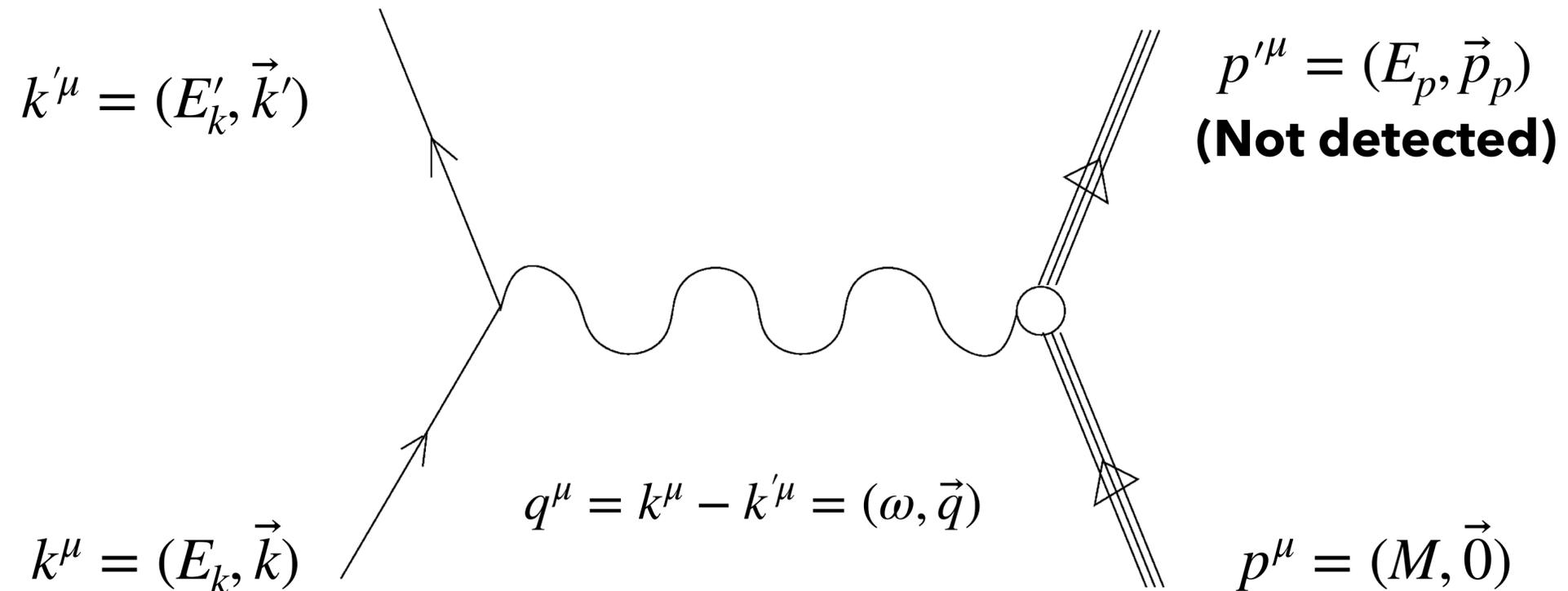


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Inclusive Electron Scattering



Kinematic invariants:

$$p^\mu p_\mu = M^2$$

$$p_\mu q^\mu = M\omega$$

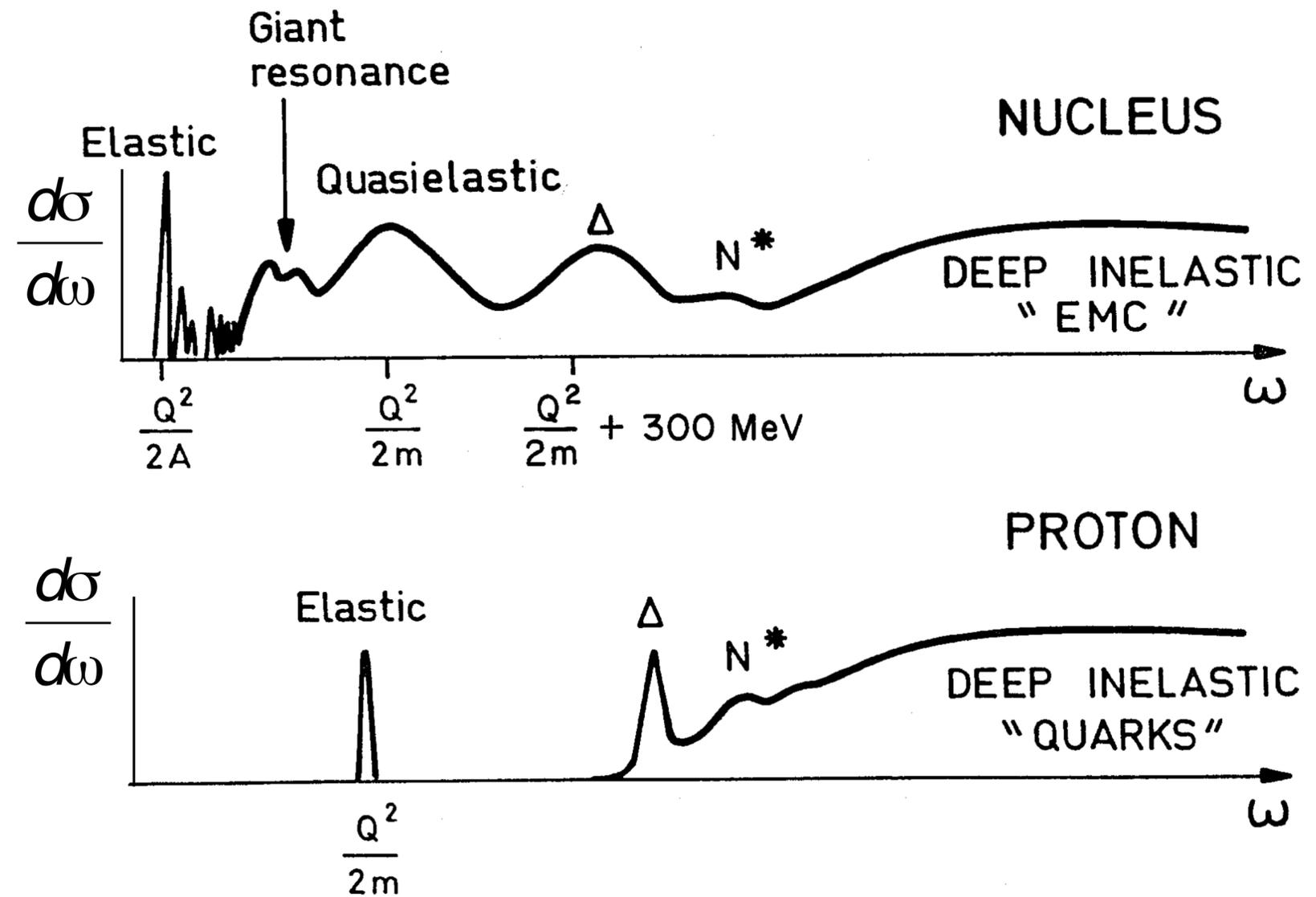
$$Q^2 = -q^\mu q_\mu = |\vec{q}|^2 - \omega^2$$

$$W^2 = p'^\mu p'_\mu = (q^\mu + p^\mu)^2$$

(e, e') Energy Spectrum

Generic electron scattering at fixed momentum-transfer

The energy deposited by the electron can tell us about the underlying process we're measuring



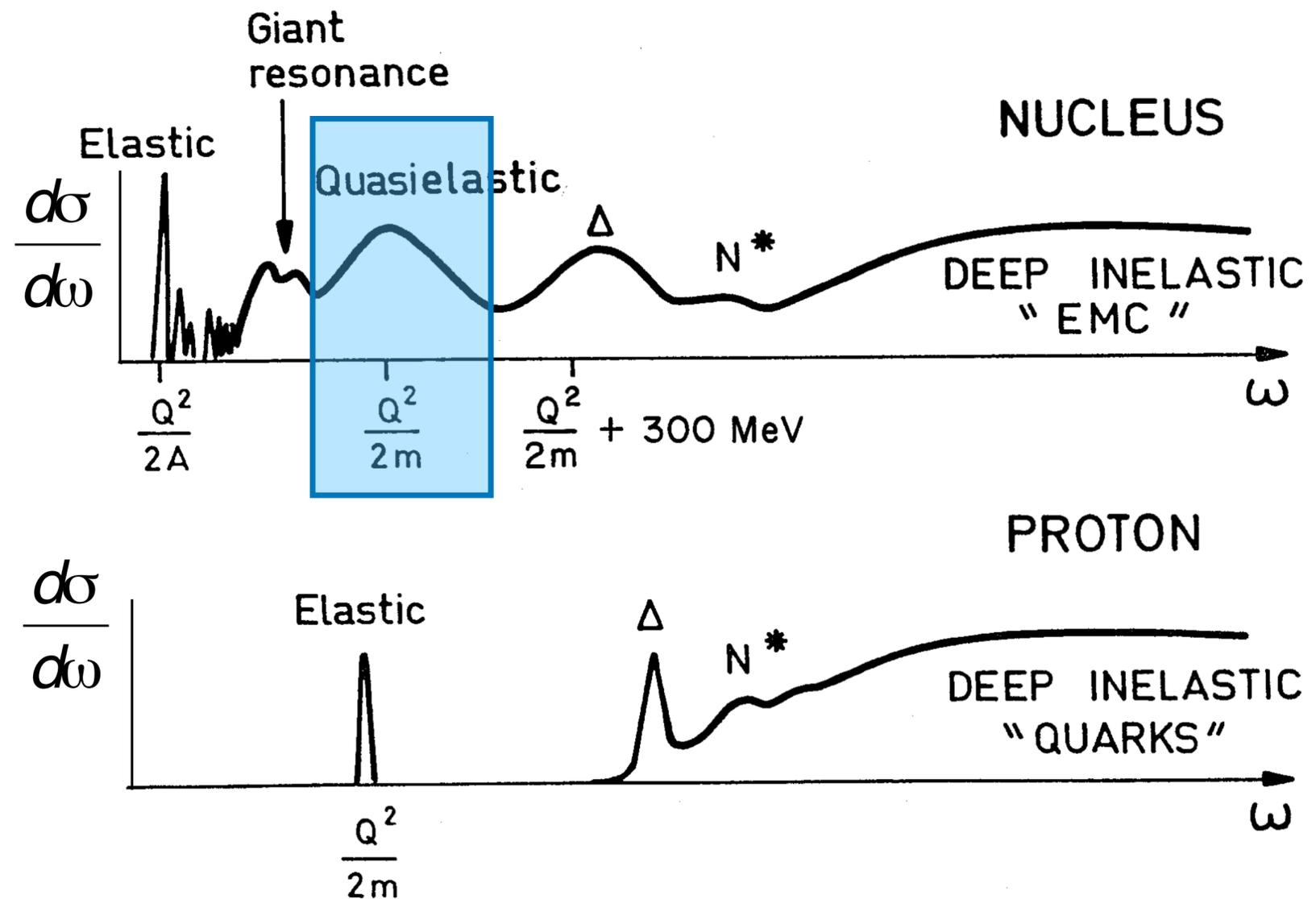
(e, e') Energy Spectrum

Generic electron scattering at fixed momentum-transfer

The energy deposited by the electron can tell us about the underlying process we're measuring

"Quasielastic" scattering occurs

$$\text{at } \frac{Q^2}{2m\omega} \equiv x_B \sim 1$$



Quasielastic Electron Scattering

- Neglecting off-shell effects, we can use conservation of 4-momentum:

$$p_i + q = p_f$$

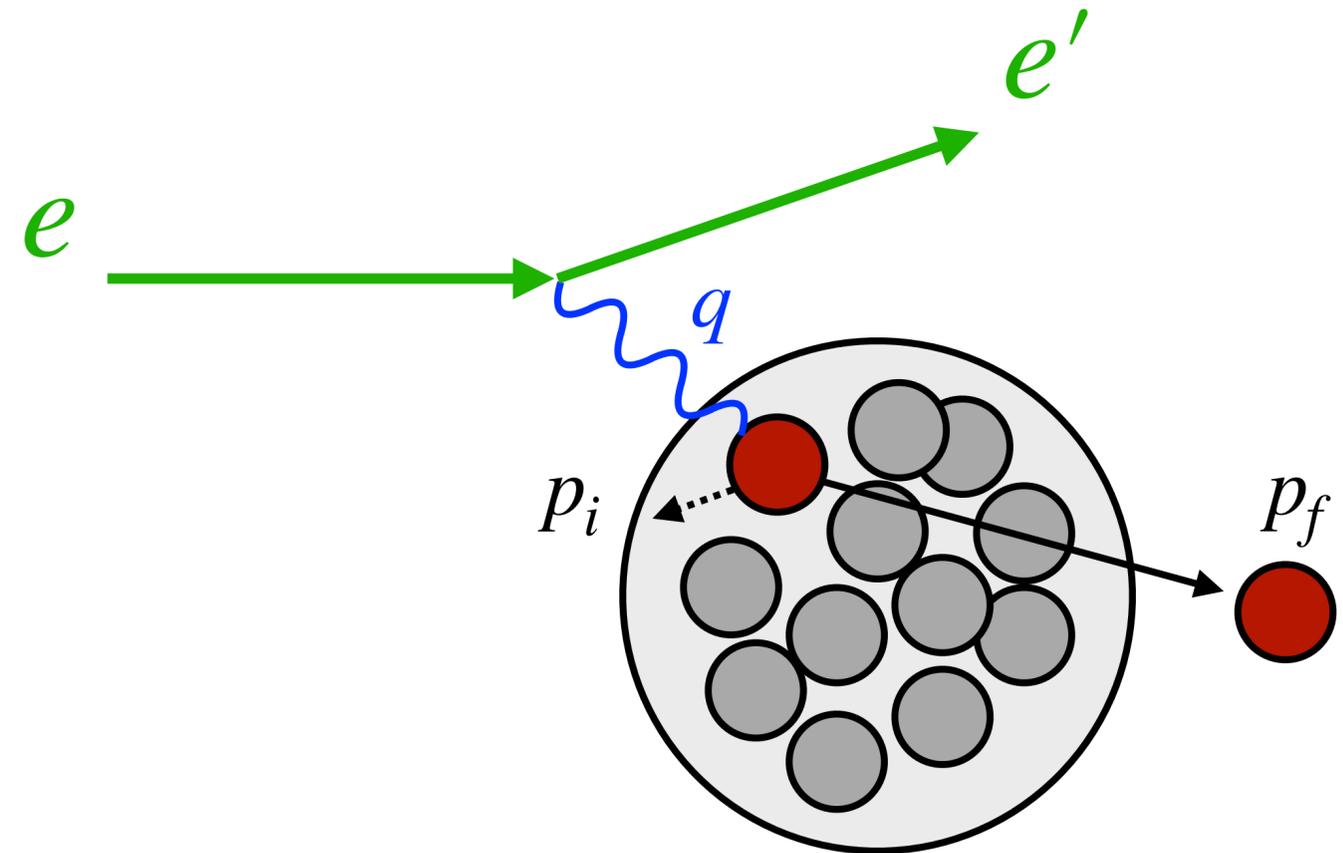
$$(p_i + q)^2 = p_i^2 + 2p_i \cdot q + q^2 = p_f^2$$

$$Q^2 = 2p_i \cdot q = 2E_i\omega - 2\vec{p}_i \cdot \vec{q}$$

$$x_B = \frac{Q^2}{2m_N\omega} = \frac{2E_i\omega - 2\vec{p}_i \cdot \vec{q}}{2m_N\omega}$$

- If we assume Q^2 is large and $|\vec{p}_i|$ is small,

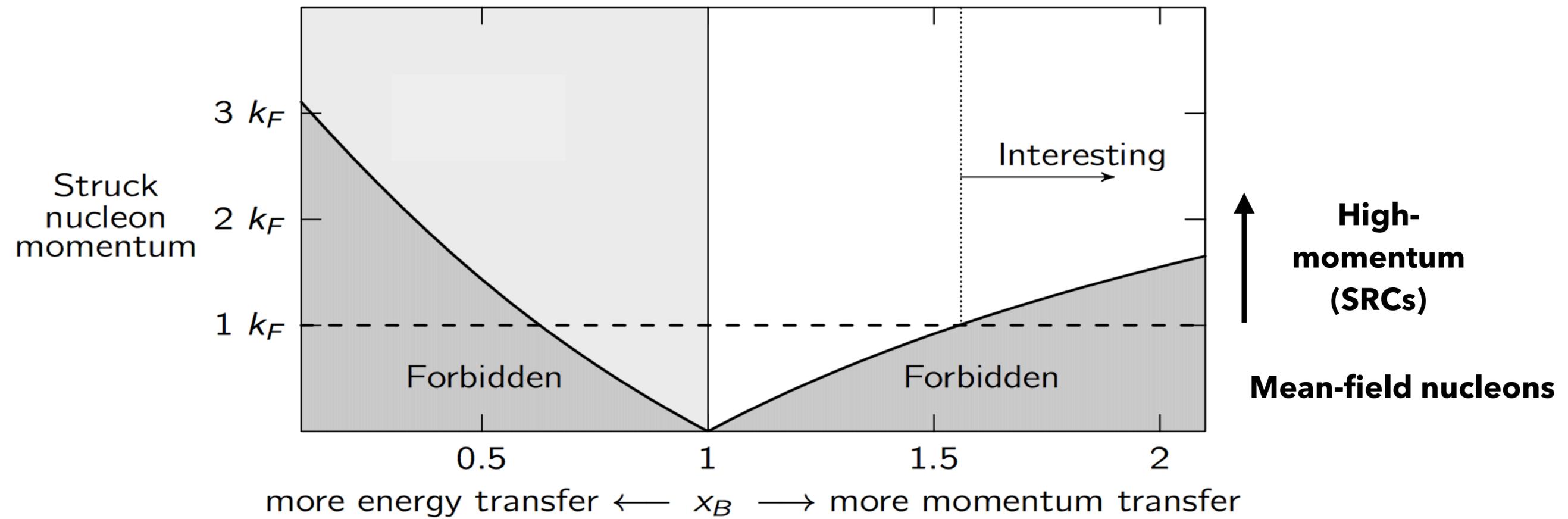
$$x_B \approx 1 - \frac{\vec{p}_i \cdot \hat{q}}{m_N}$$



Inclusive (e, e') Scattering

Inclusive (e, e') cross section at different kinematics are sensitive to the nuclear momentum distribution

Minimum momentum for the struck nucleon is set by x_B



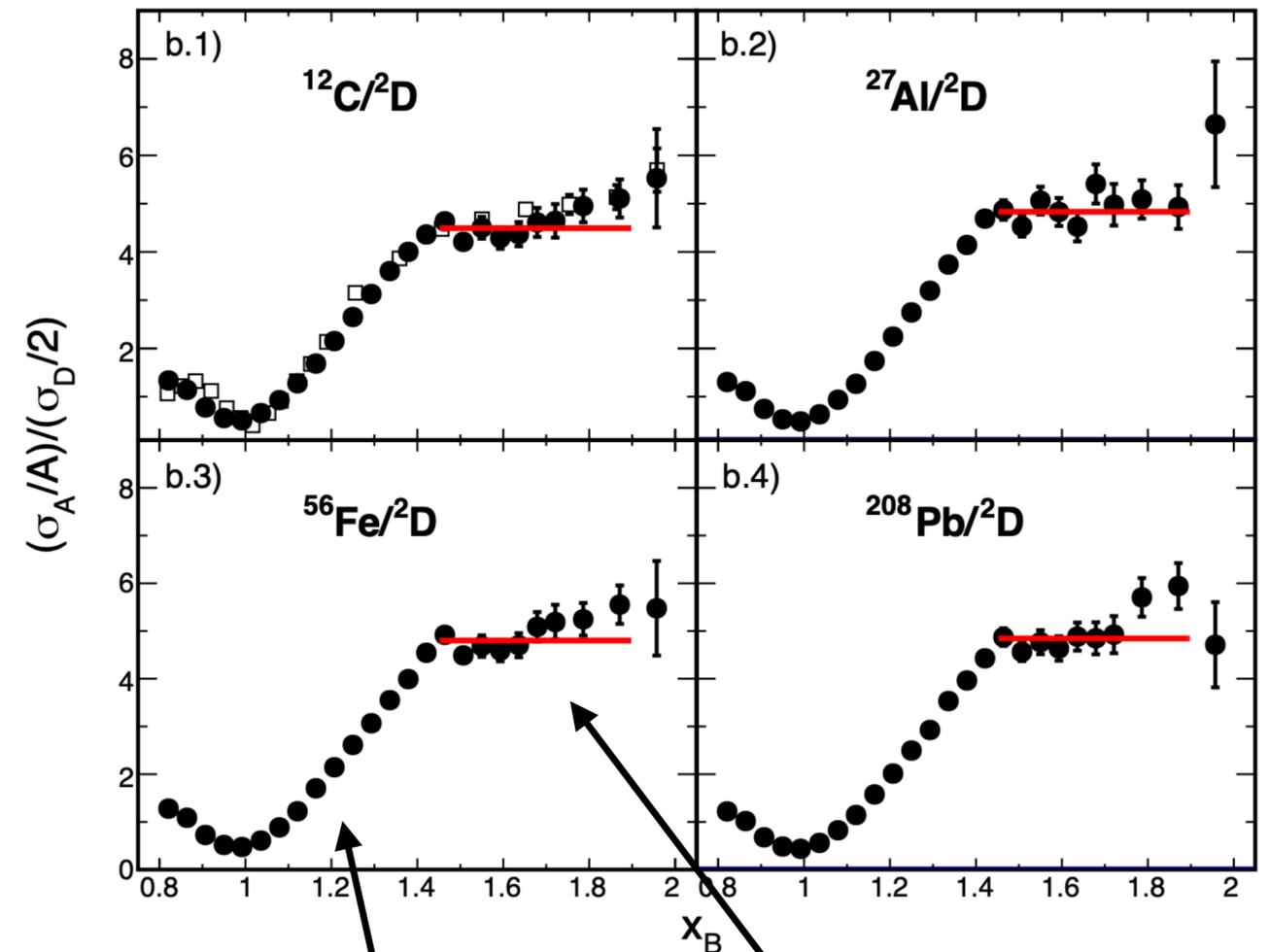
Inclusive (e, e') Scattering

- Measuring (e, e') cross section as function of x_B tells us about the nuclear momentum distribution $n(k)$ – at least in one dimension
- **Ratios** between nuclear cross sections can let us compare nuclear momentum distributions
- Areas where the ratio is constant represent **scaling**, where the cross section depends only on x_B and not on A
 - Scaling → **Universal behavior**

Inclusive (e, e') Scattering

- Measured σ_A/σ_d cross section for (e, e') , sensitive to $n_A(k)/n_d(k)$
- Scaling observed for $x_B > 1.5$ – above “Fermi momentum” where shell-model dominates
- Scaling down to $A = 2$ deuteron suggests **universal two-nucleon pairing behavior**

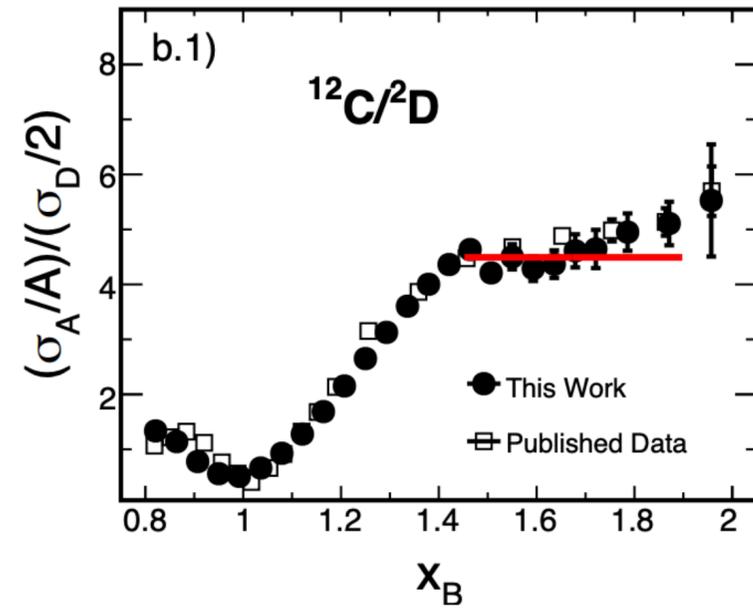
$$a_2(A) = \frac{n_A(k > k_F)}{n_d(k > k_F)} \sim \# \text{ Nucleon pairs}$$



Different mean-field shell structure

Universal high-momentum 2N pairs

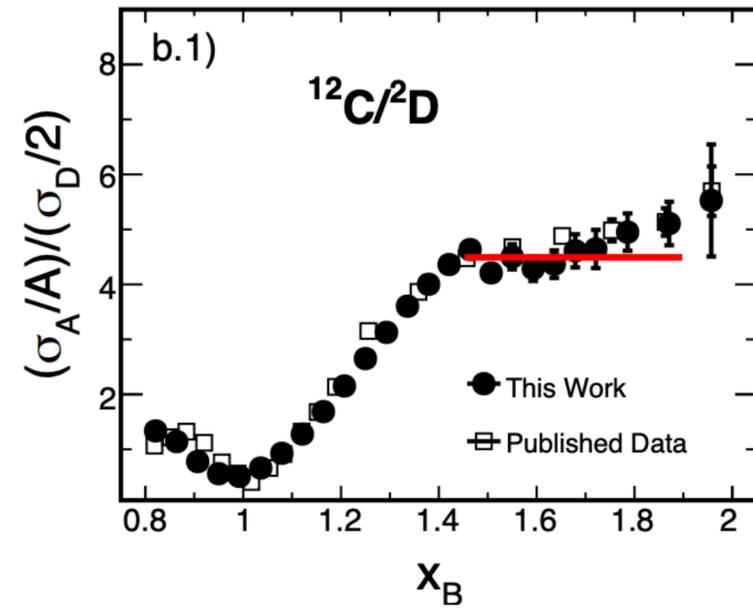
First estimate of SRC fraction in nuclei



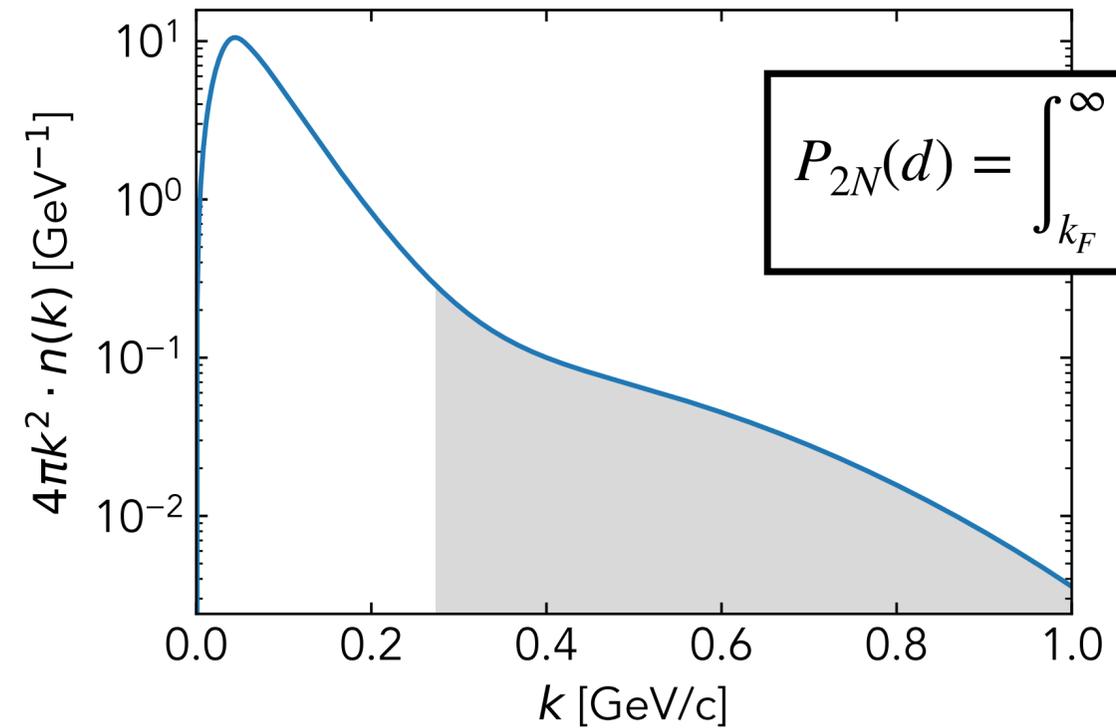
A	$a_{2N}(A/d)$
^3He	2.08 ± 0.01
^4He	3.47 ± 0.02
Be	4.03 ± 0.04
C	4.95 ± 0.05
Cu	5.48 ± 0.05
Au	5.43 ± 0.06

Measure of SRC relative to deuteron comes from a_2

First estimate of SRC fraction in nuclei



Deuteron momentum distribution

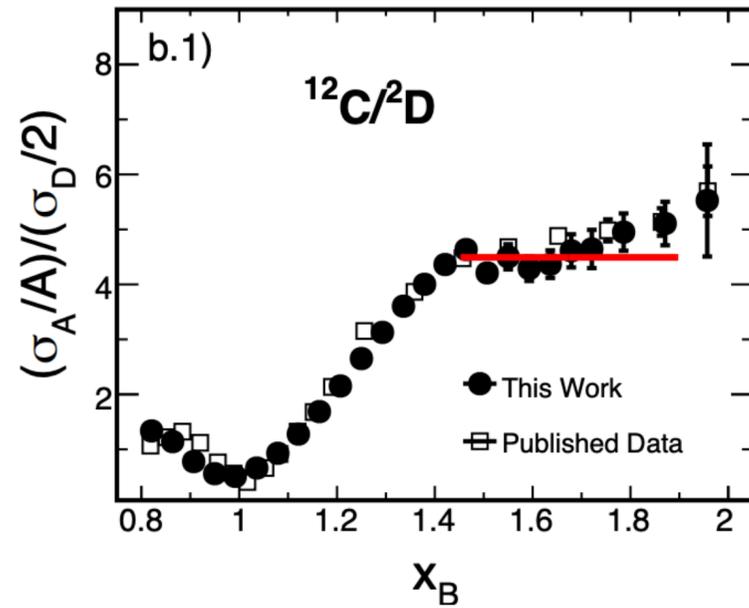


2-body calculations of deuteron wavefunction:
About **4%** short-distance

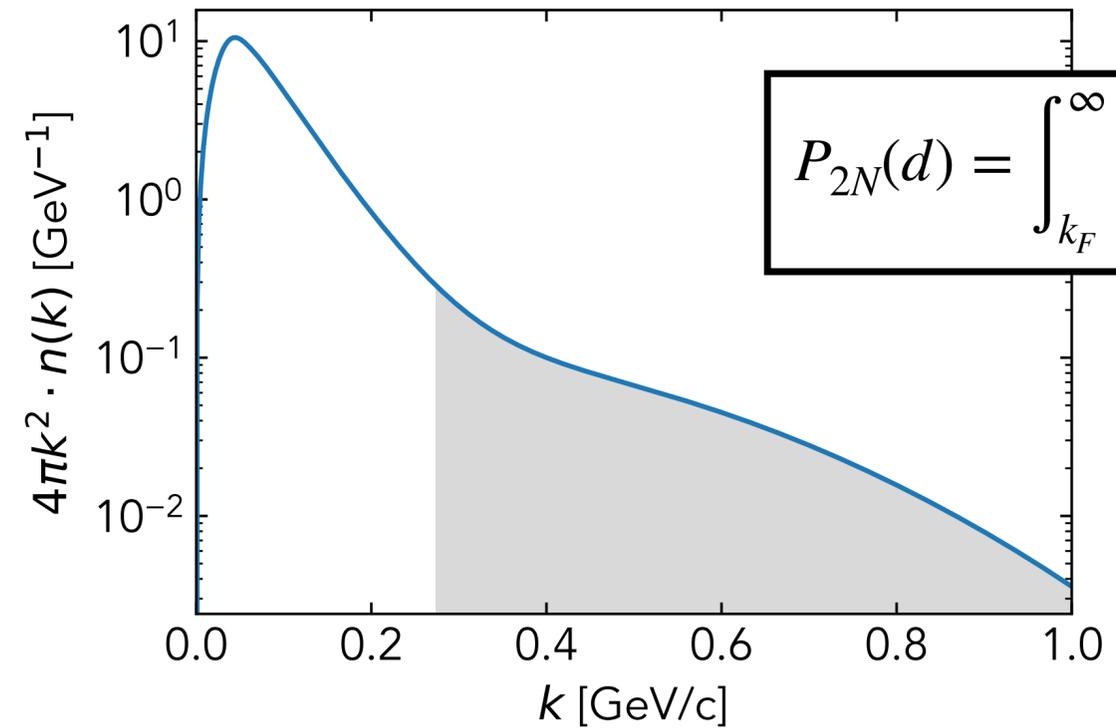
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Deuteron momentum distribution



$$P_{2N}(d) = \int_{k_F}^{\infty} n_d(k) d^3k = 4.1 \pm 0.8 \%$$

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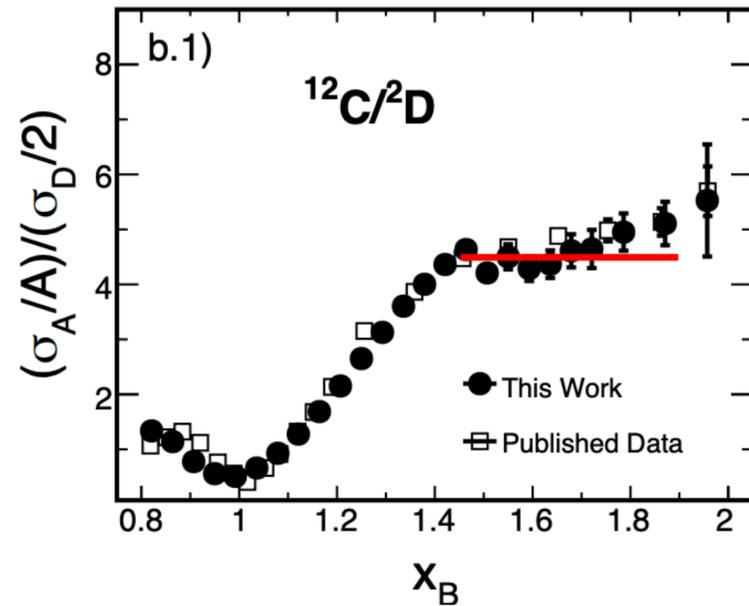
Measure of SRC relative to deuteron comes from a_2

$$P_{2N}(A) \approx a_{2N}(A/d) \cdot P_{2N}(d)$$

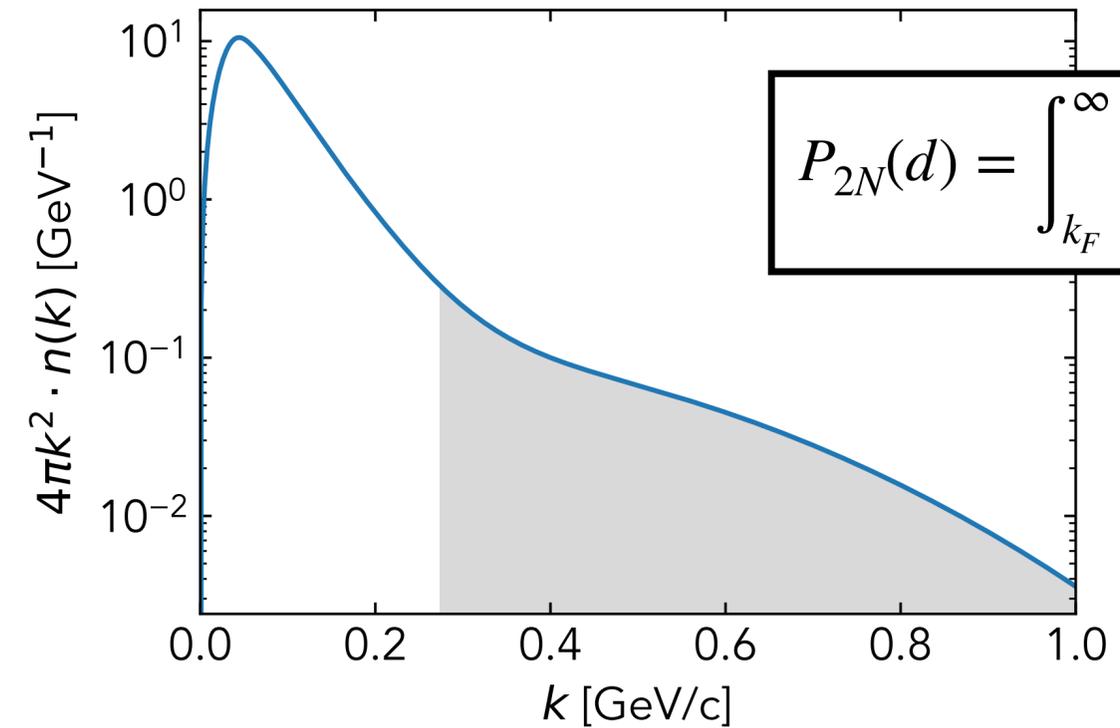
Measurement

Theory

First estimate of SRC fraction in nuclei



Deuteron momentum distribution



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Measure of SRC relative to deuteron comes from a_2

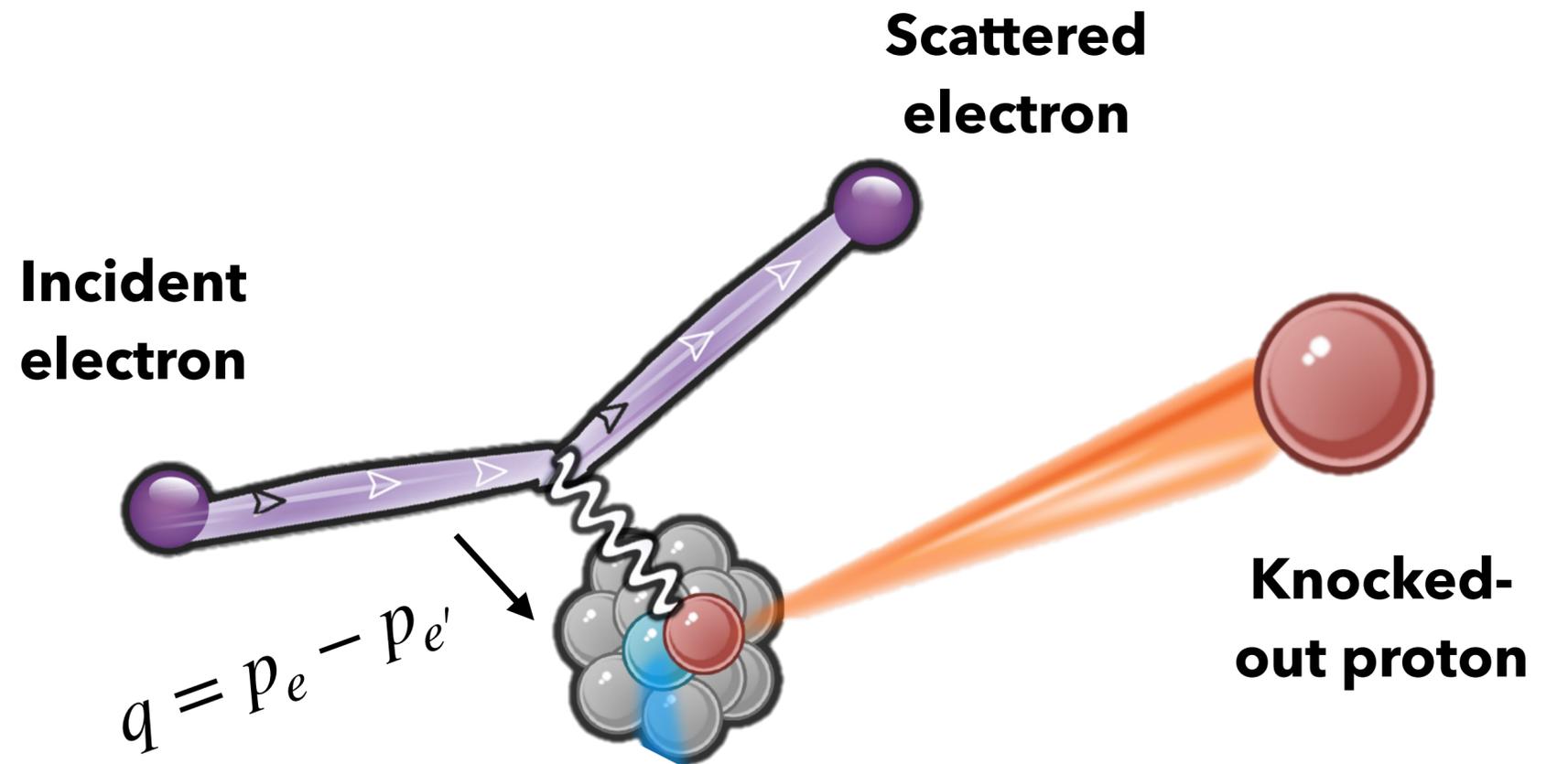
$$P_{2N}(A) \approx \boxed{a_{2N}(A/d)} \cdot \boxed{P_{2N}(d)}$$

Carbon: $P_{2N}(^{12}\text{C}) \approx \boxed{5} \cdot \boxed{4\%} = 20\% \text{ SRC}$

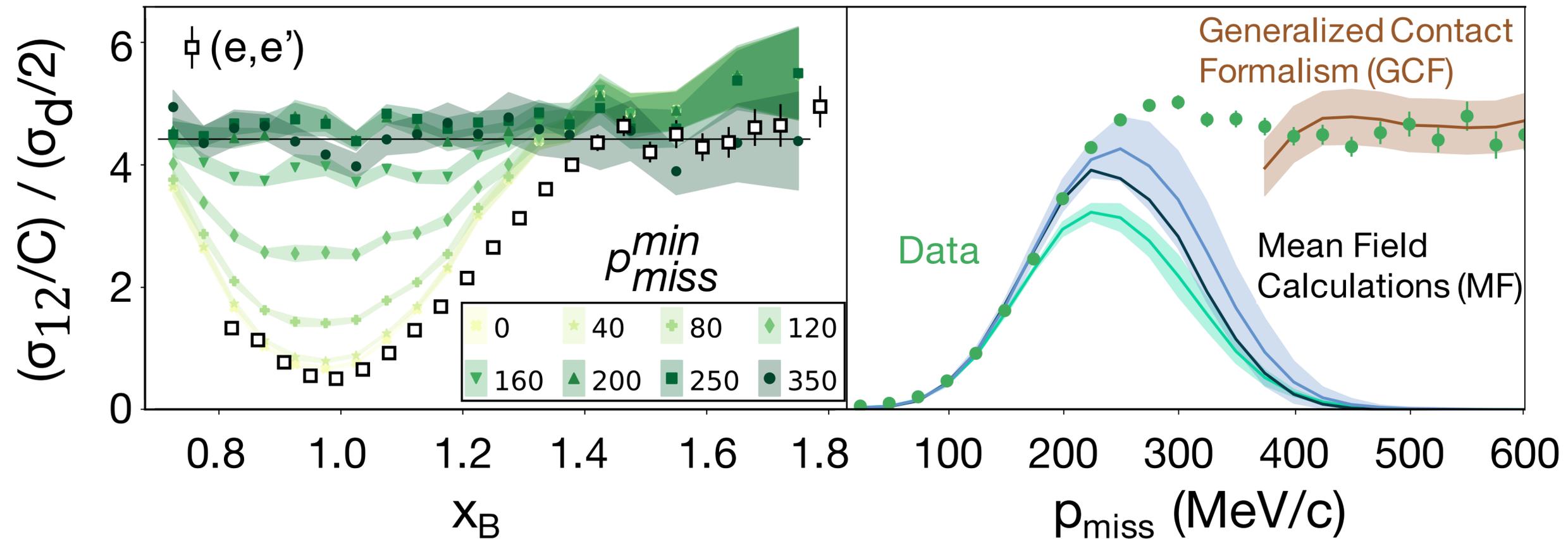
Semi-inclusive ($e, e'p$)

Detecting knocked-out nucleon – **reconstruct initial-state nucleon:**

$$p_i \approx p_{miss} = p_N - q$$



High-Momentum SRC Dominance

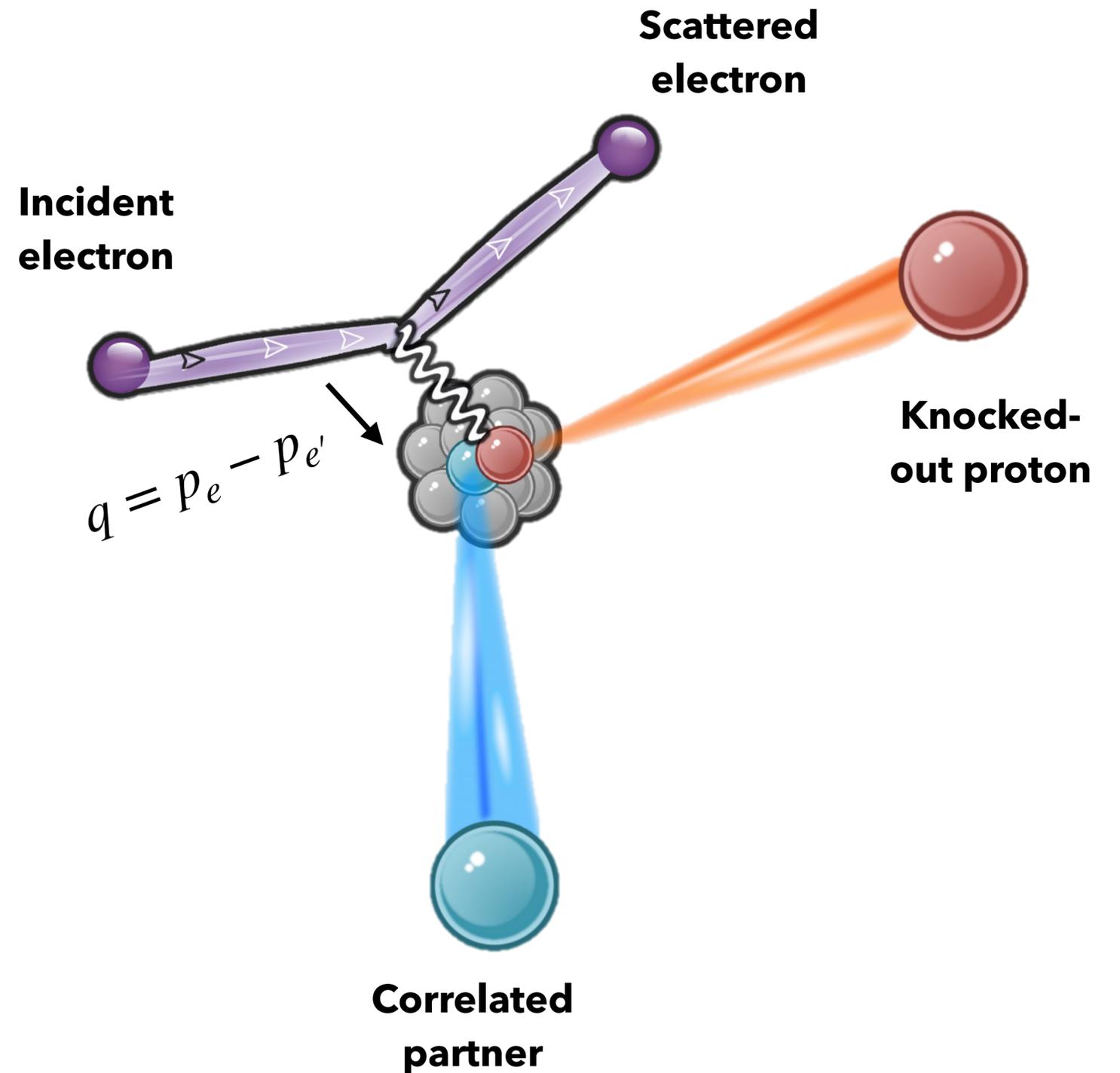


Semi-inclusive $(e, e'p)$ data extends inclusive large- x_B A/d scaling

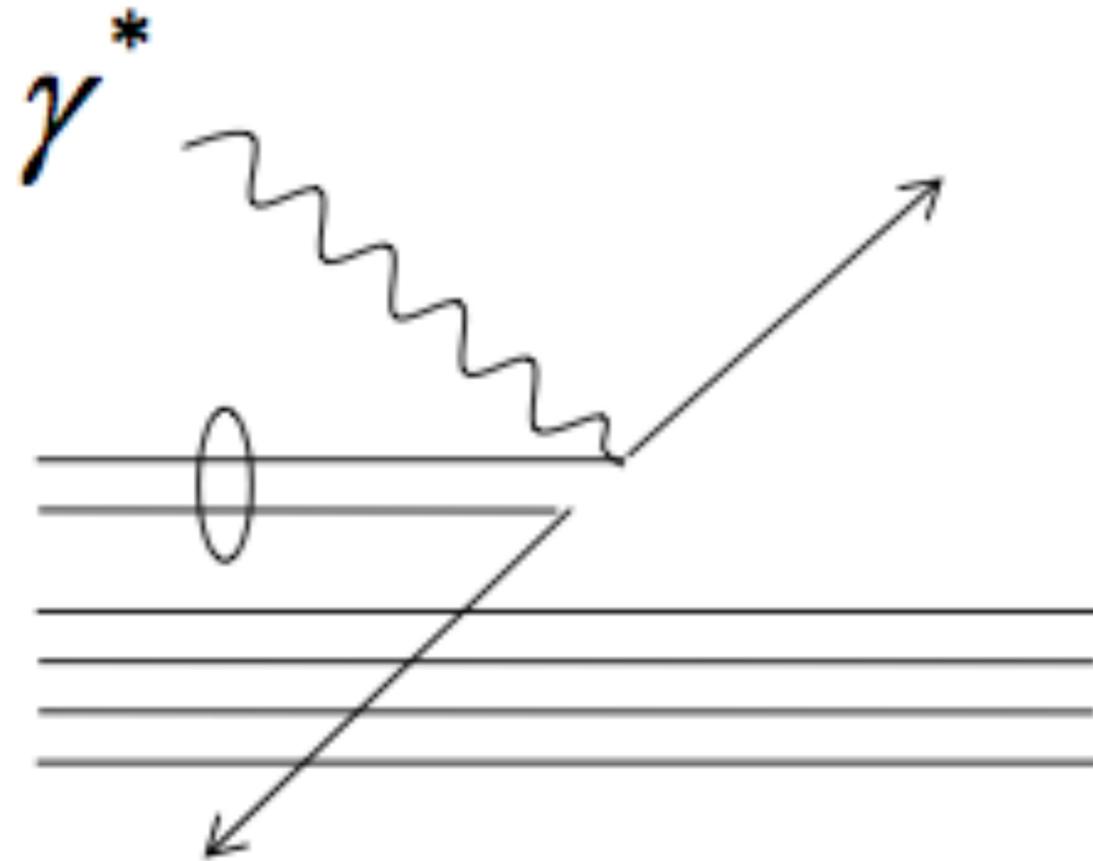
Everything above $p_{miss} \sim 250$ MeV/c looks like a deuteron

Exclusive ($e, e'pN$)

- Breakup the pair
- Detect **both** nucleons
- Reconstruct initial-state pair
- Allows direct measurement of center-of-mass and relative momentum
- Gives access to full isospin information of the pair



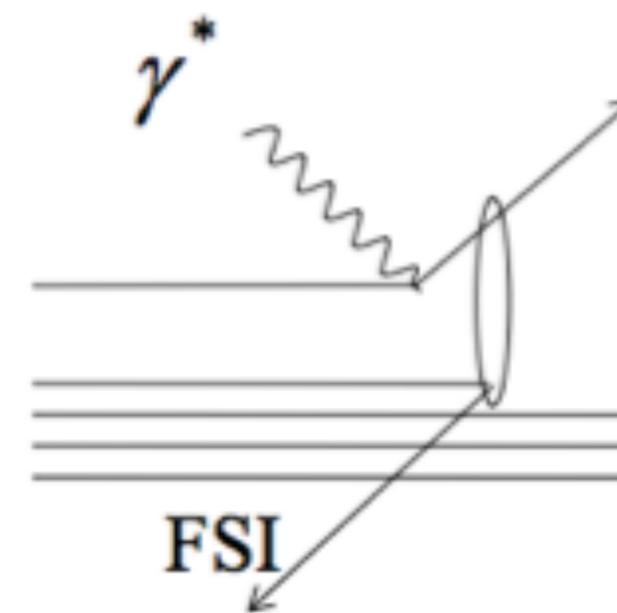
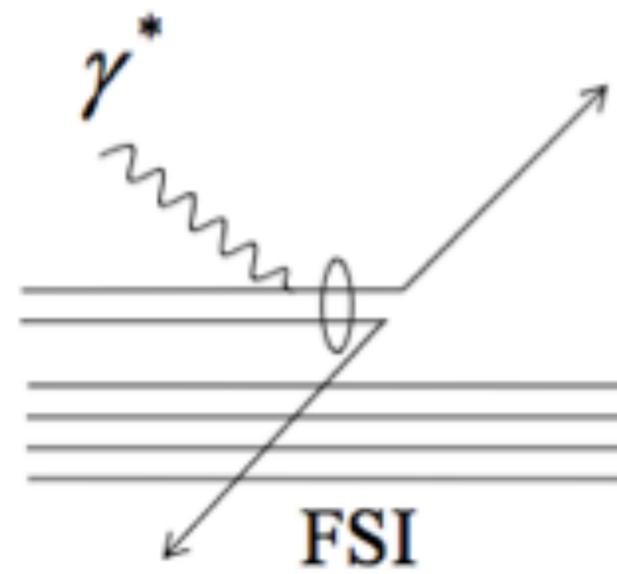
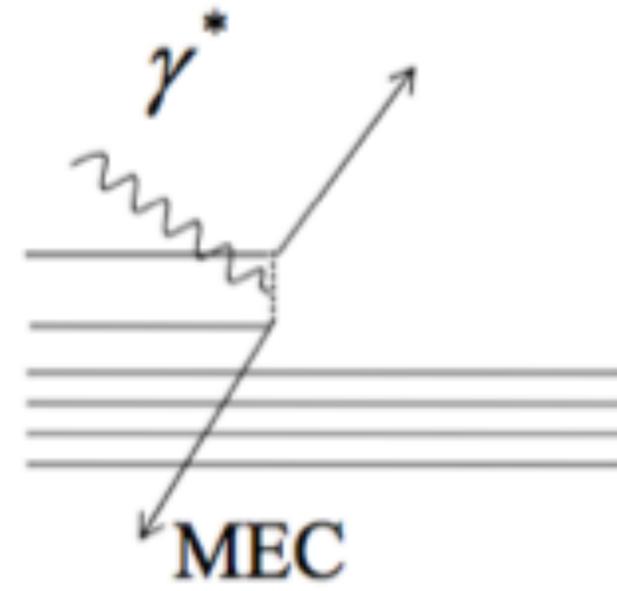
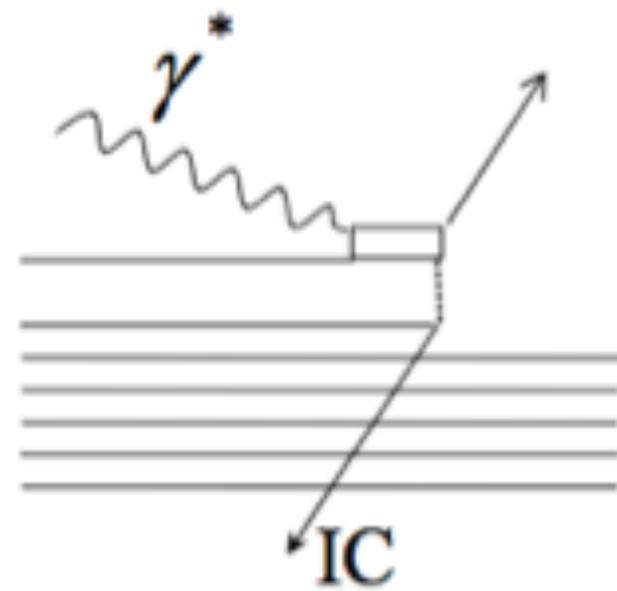
Two-Nucleon Knockout



SRC



Reaction Mechanisms!





Reaction Mechanisms!

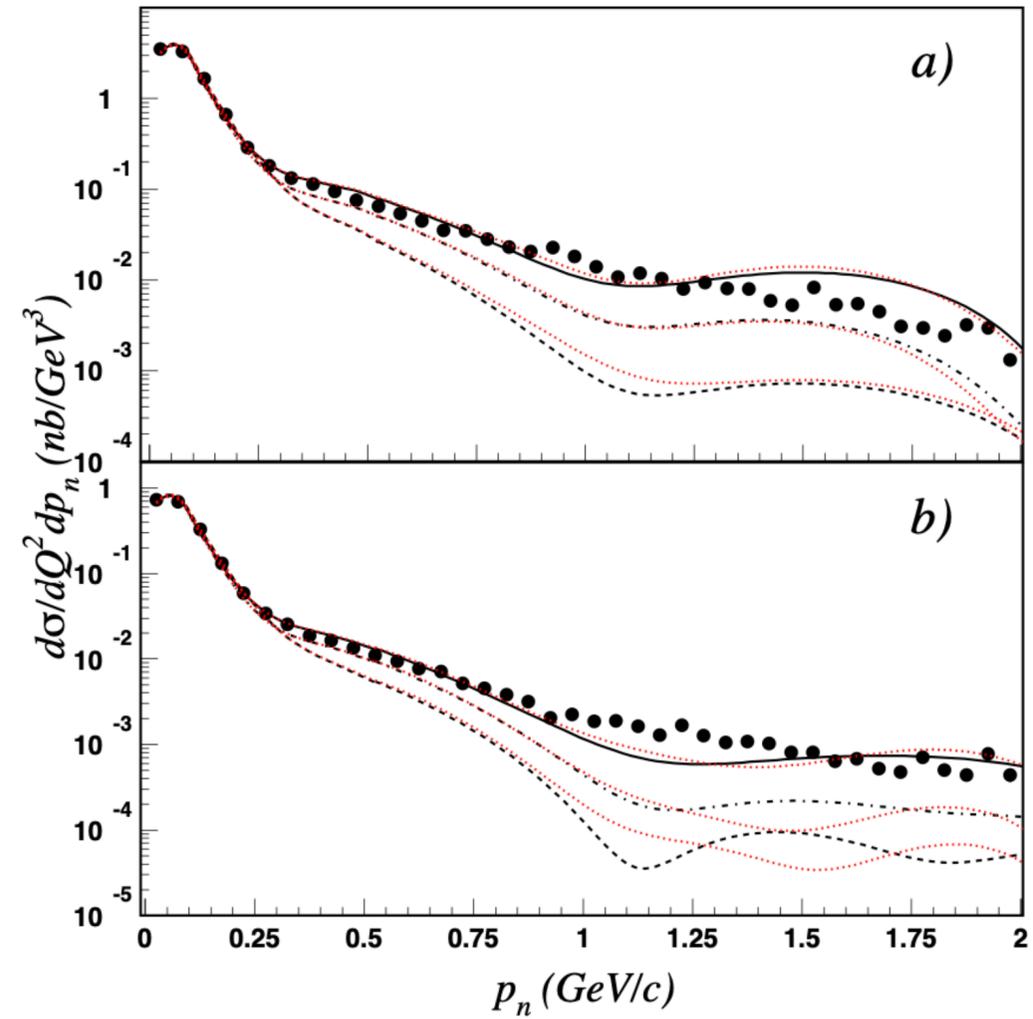
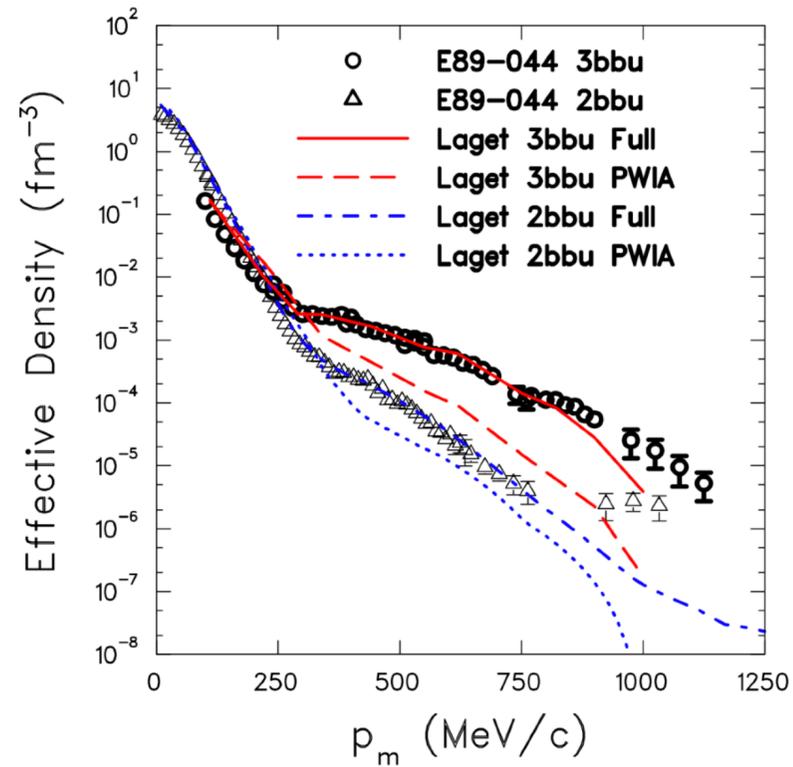


FIG. 1: Color online. The recoil neutron momentum distribution for (a) $Q^2 = 2 \pm 0.25 \text{ GeV}^2$ and (b) $Q^2 = 3 \pm 0.5 \text{ GeV}^2$. Dashed, dash-dotted and solid curves are calculations with the Paris potential for PWIA, PWIA+FSI and PWIA+FSI+MEC+N Δ , respectively. Dotted (red) curves are calculations with the AV18 potential.

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Reaction Mechanisms!

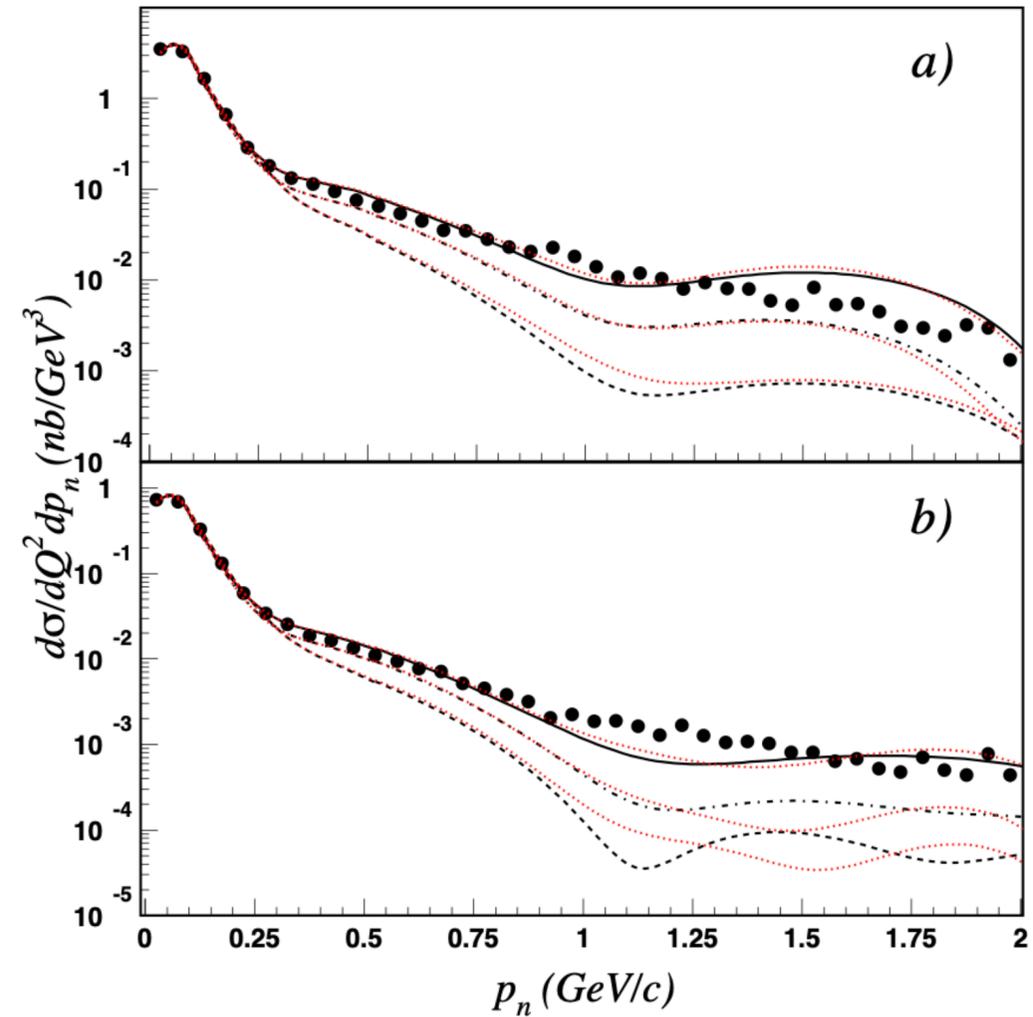
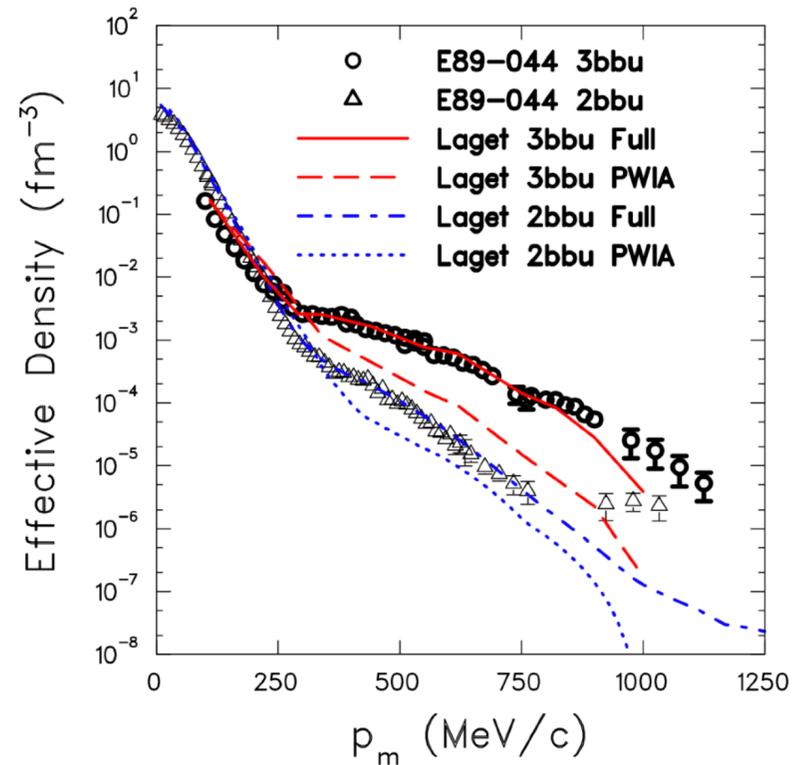
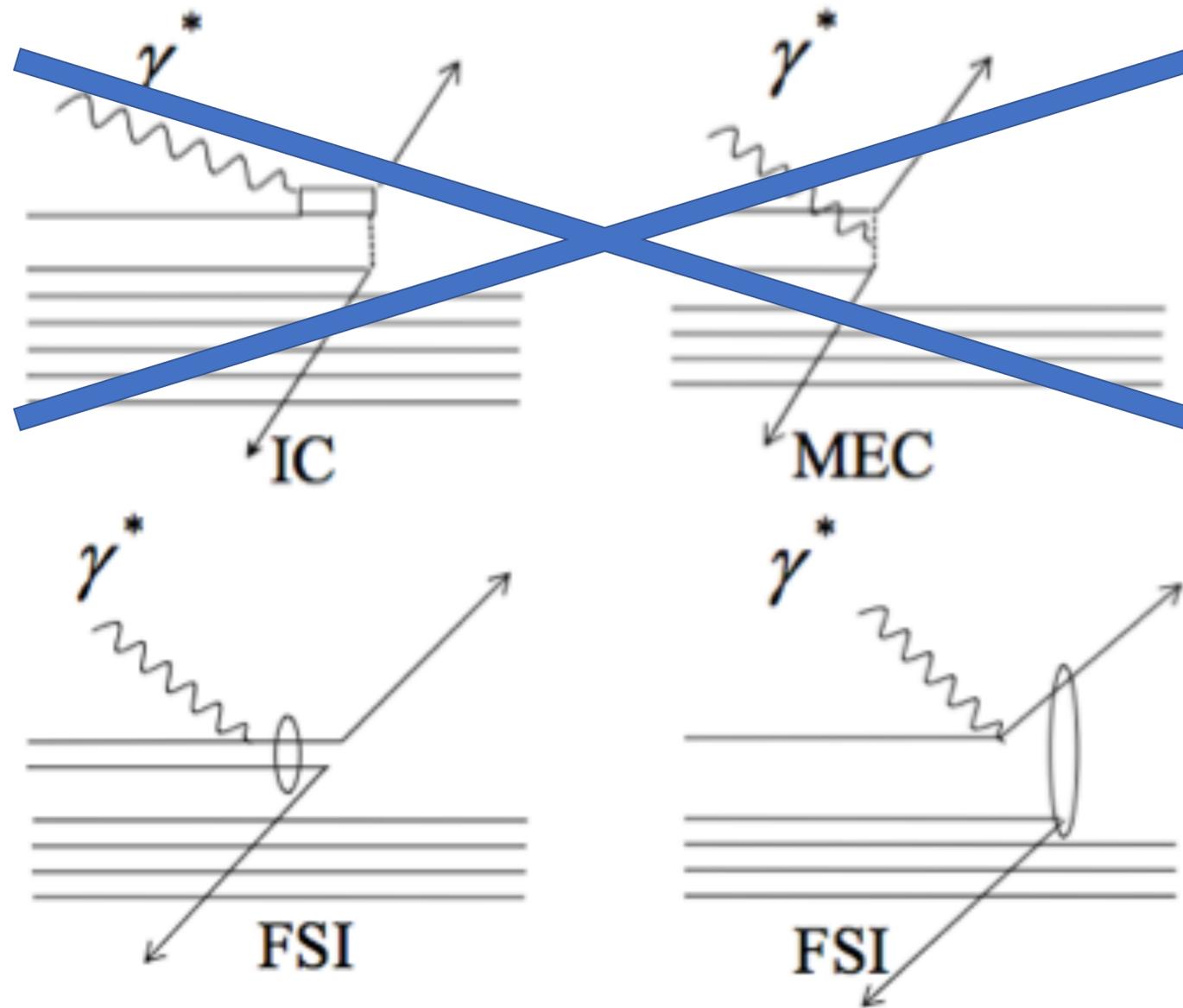


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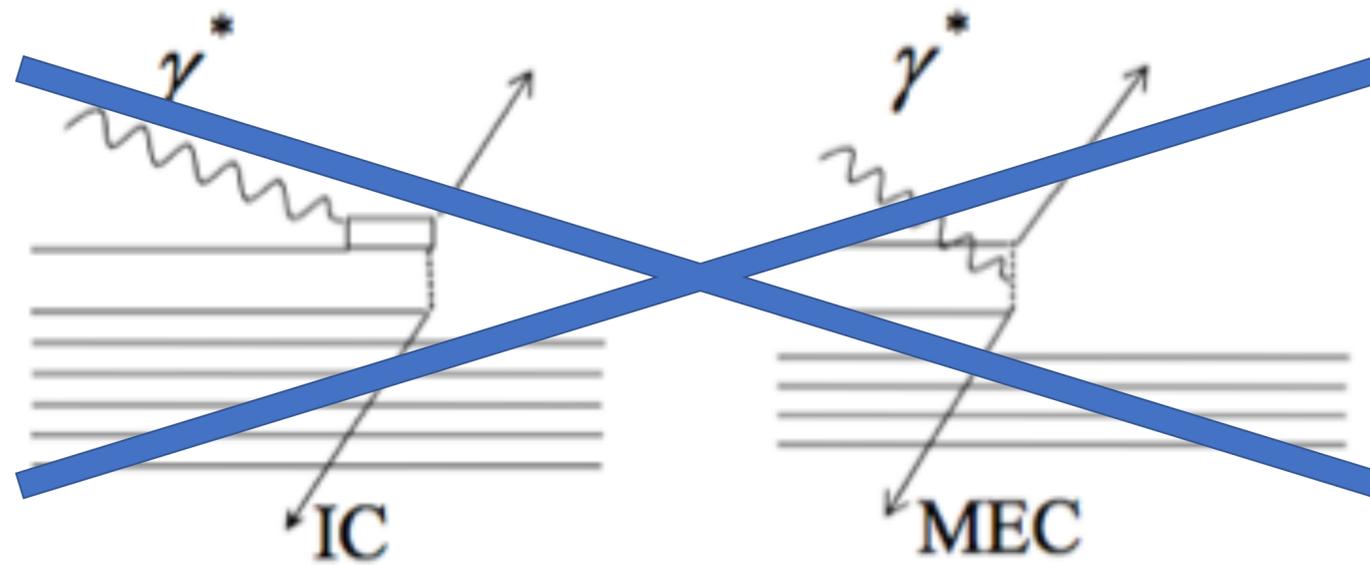
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Suppressing competing reaction effects

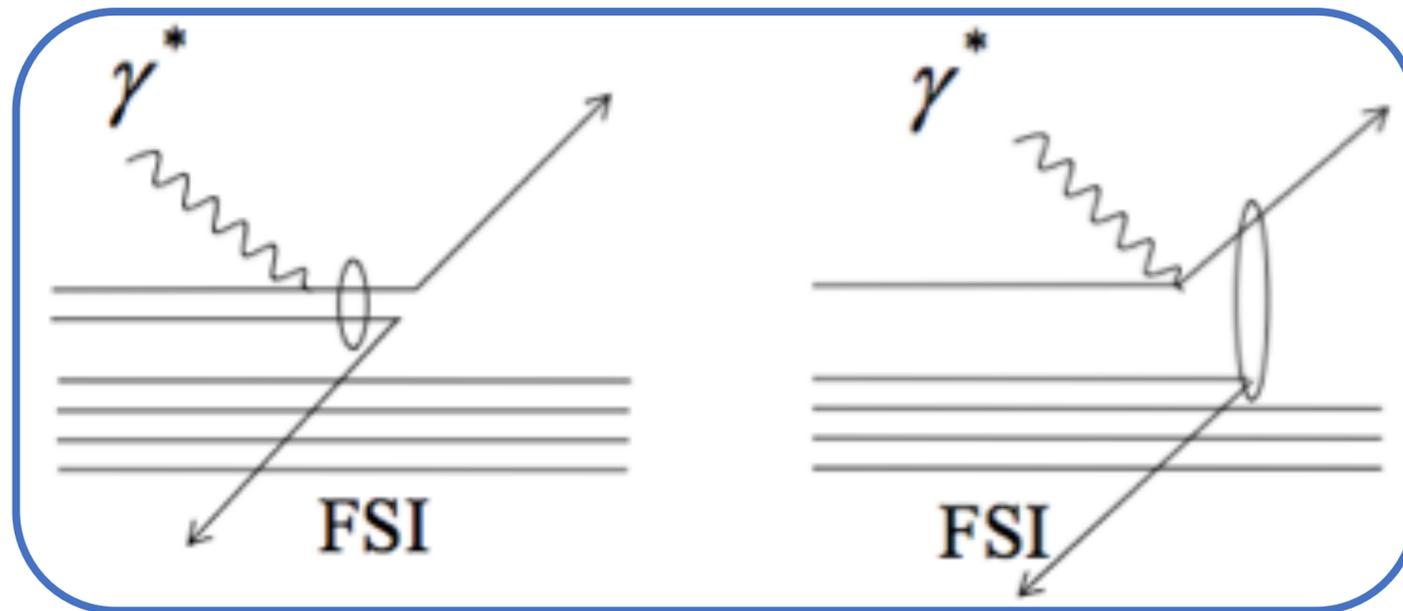


MEC suppressed @ **high- Q^2**
IC suppressed at **$x_B > 1$**

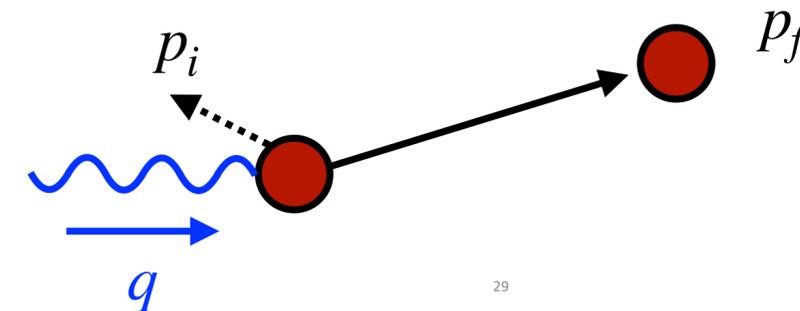
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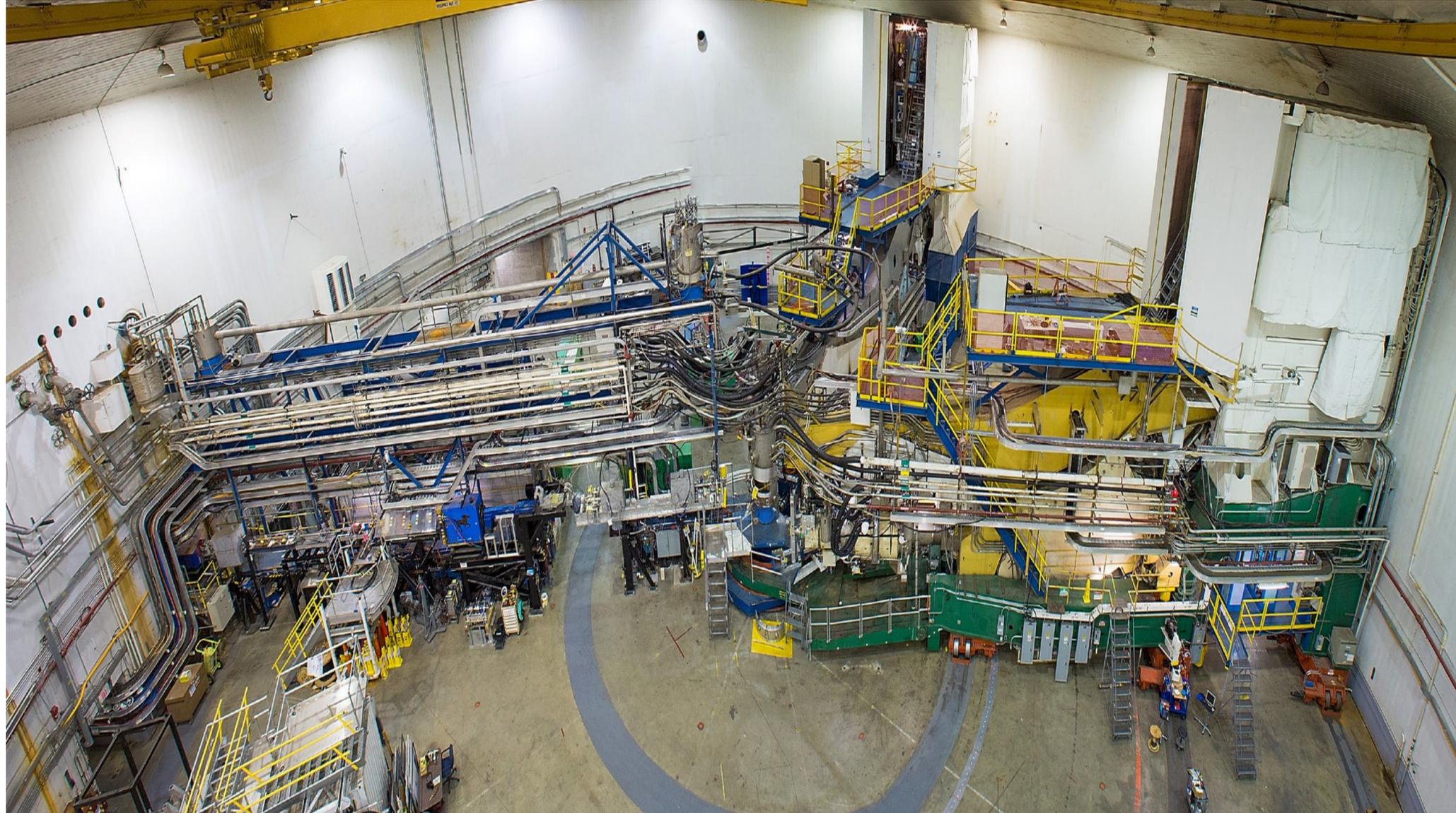
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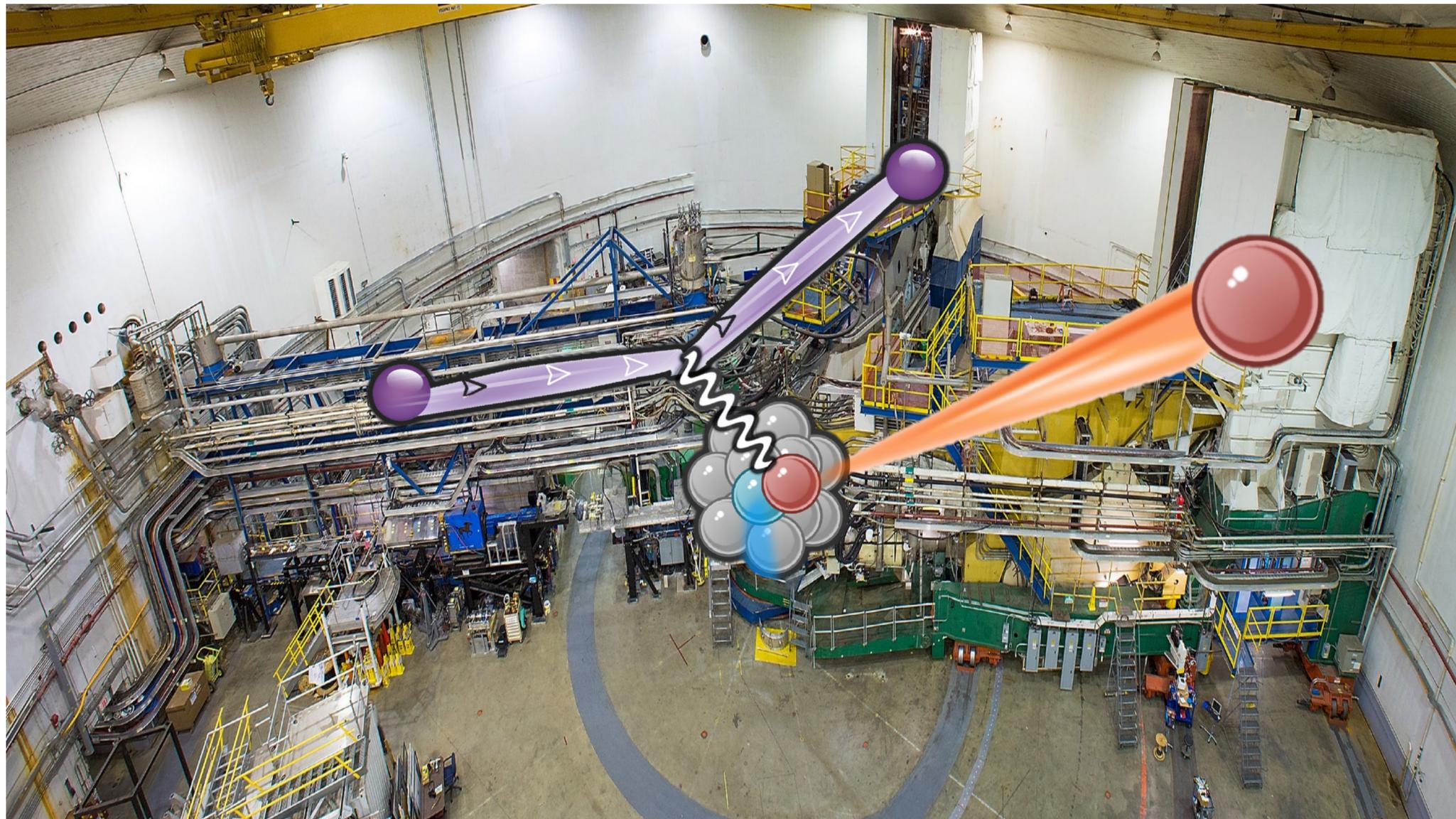
FSI suppressed in **anti-parallel** kinematics. Treated using **Glauber** approximation



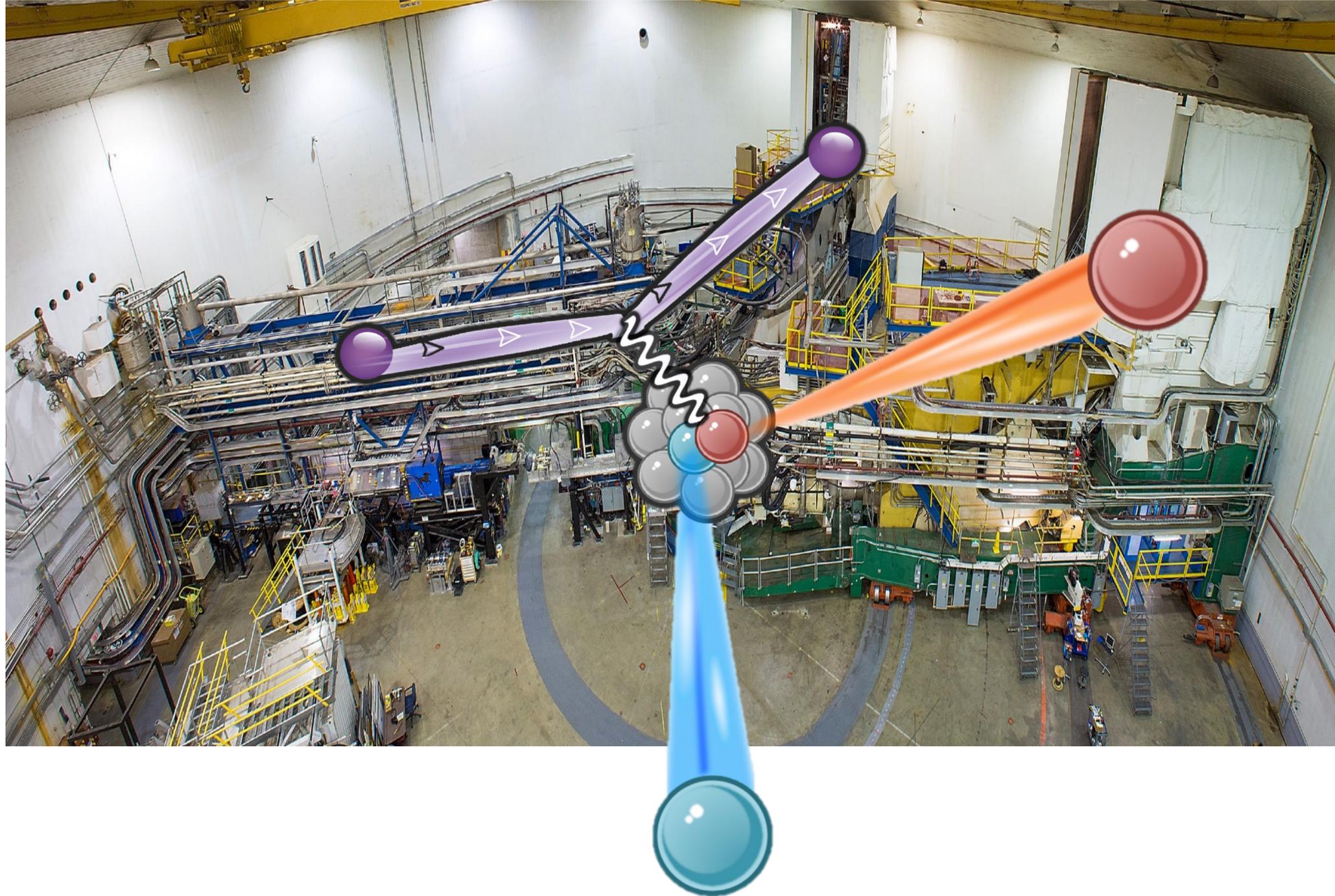
Jefferson Lab Hall A



Hall A: $A(e, e'pN)$

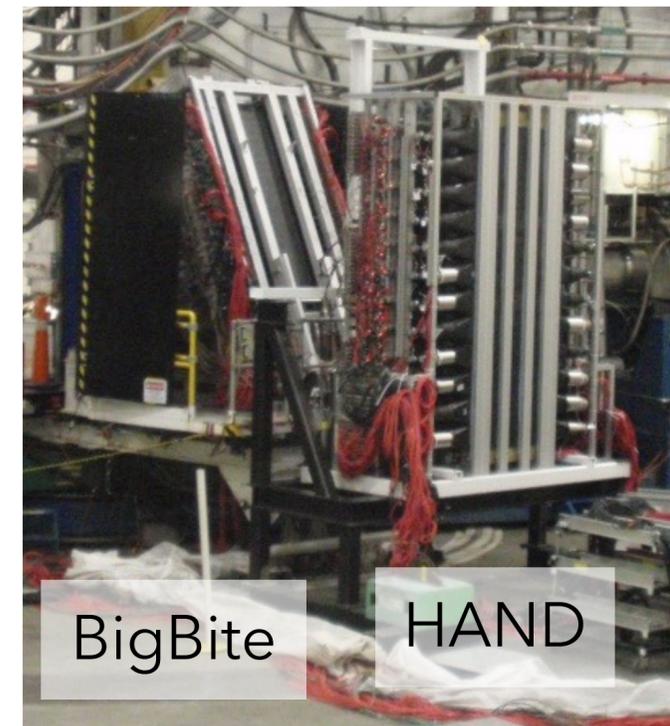
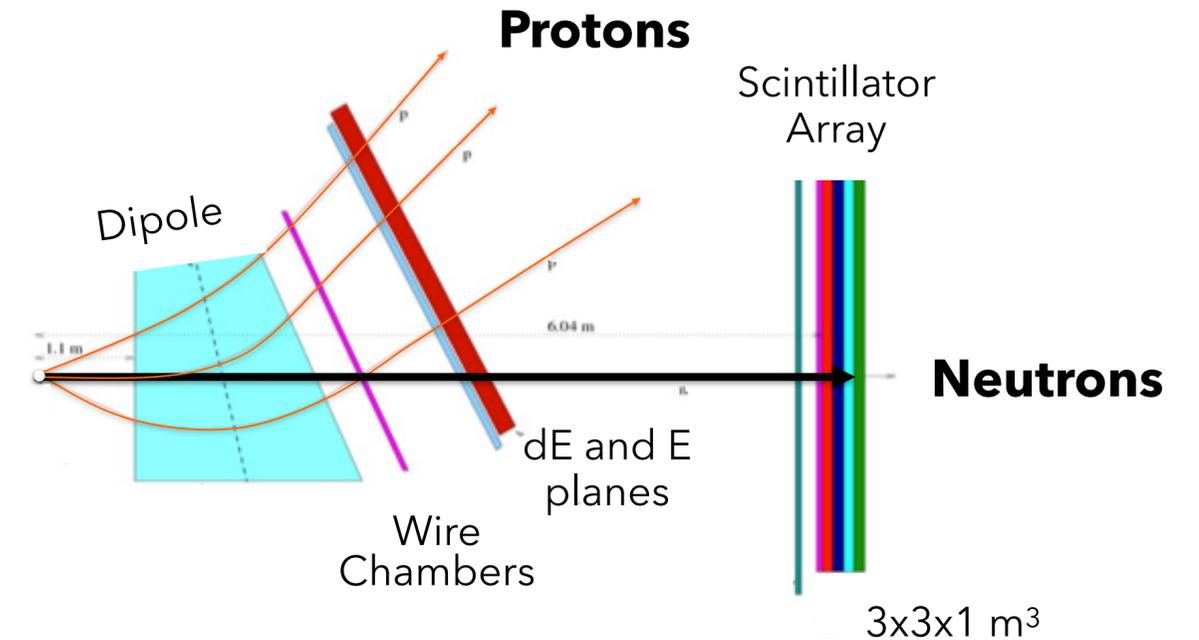


Hall A: $A(e, e'pN)$

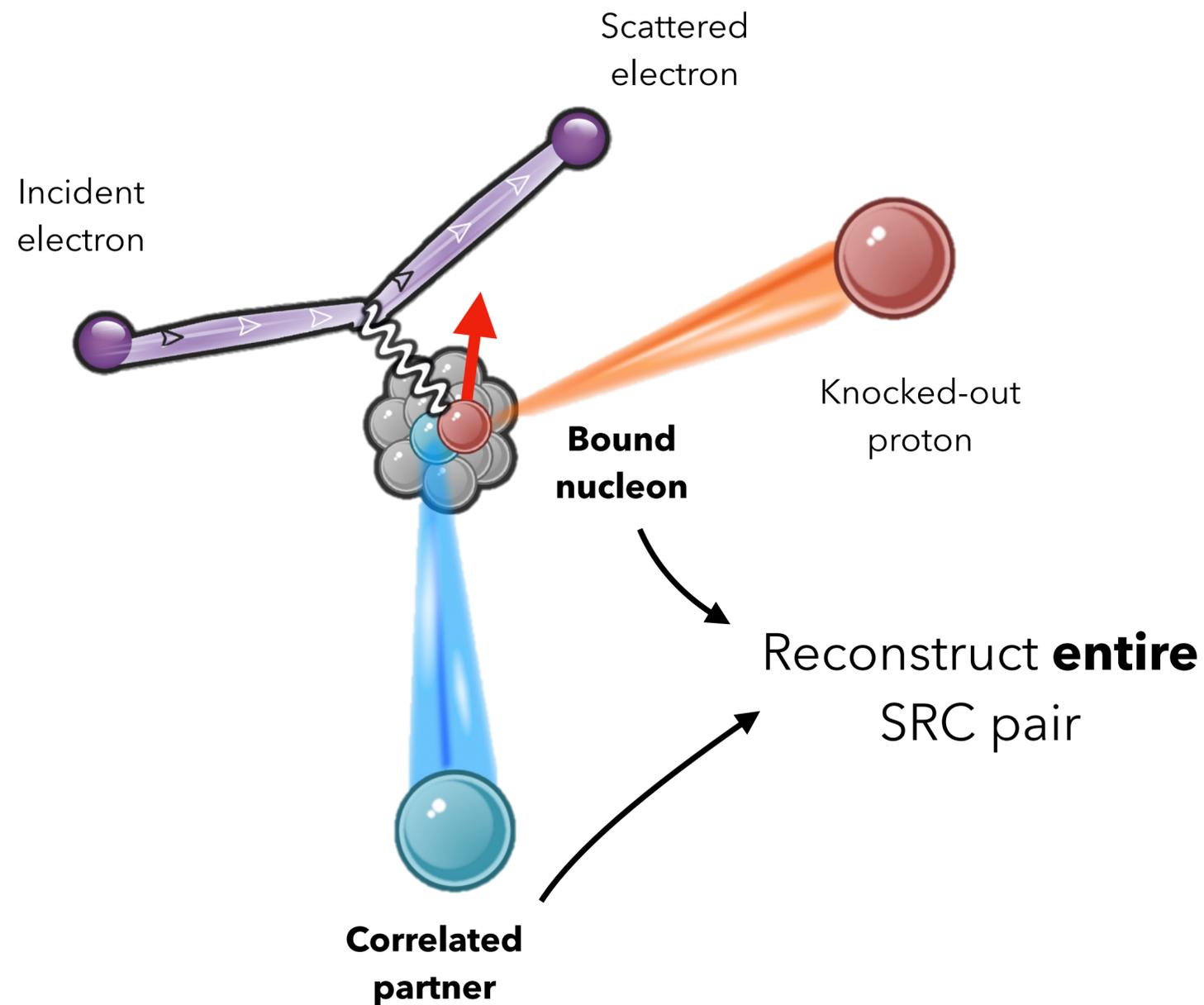


Hall A: $A(e, e'pN)$

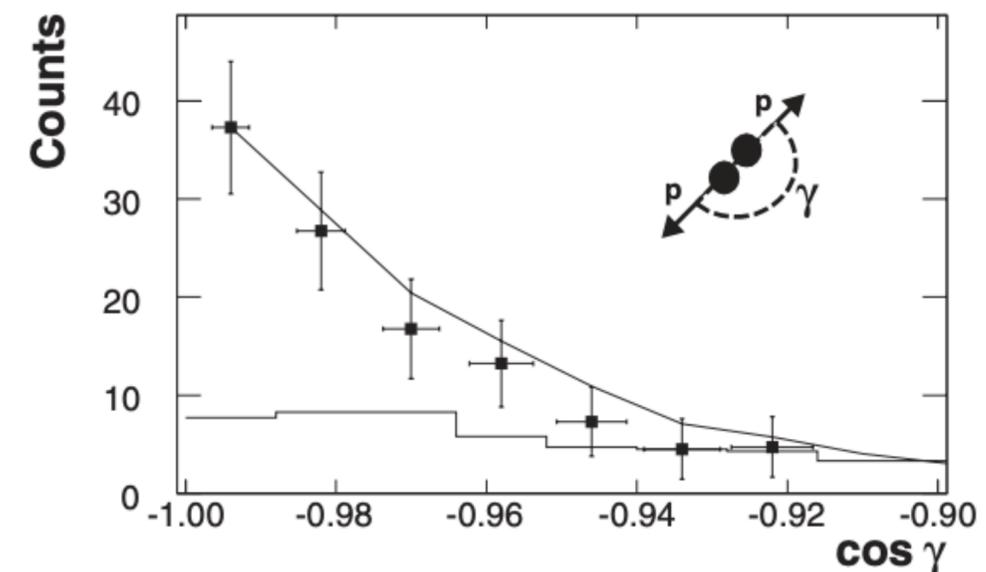
- $E_{beam} = 4.6 \text{ GeV}$
- $Q^2 \sim 2 \text{ GeV}^2$
- $x_B \sim 1.2$
- $300 < p_{miss} < 800 \text{ MeV}/c$
- Detect knocked-out proton, look for partner nucleon



$(e, e'pp)$ – First direct observation of SRC knockout in electron-scattering

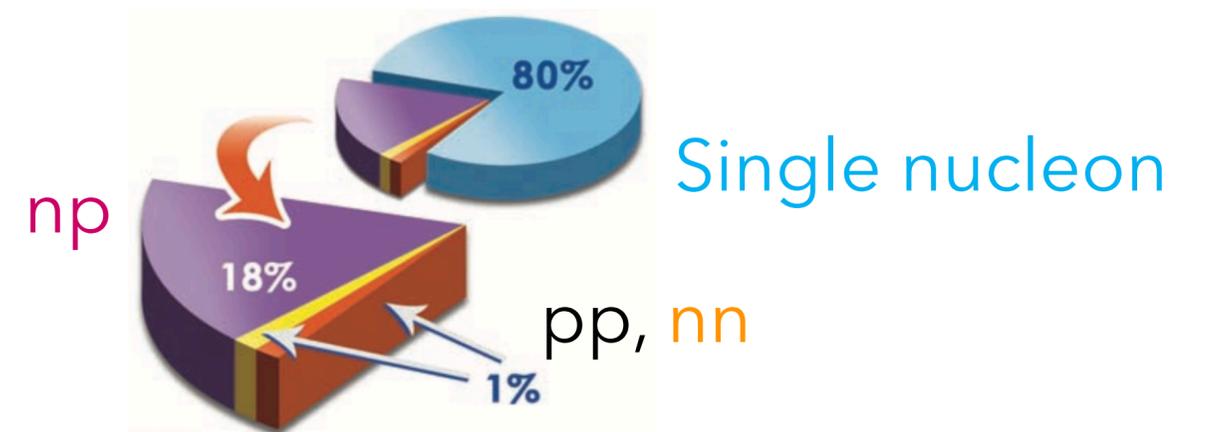
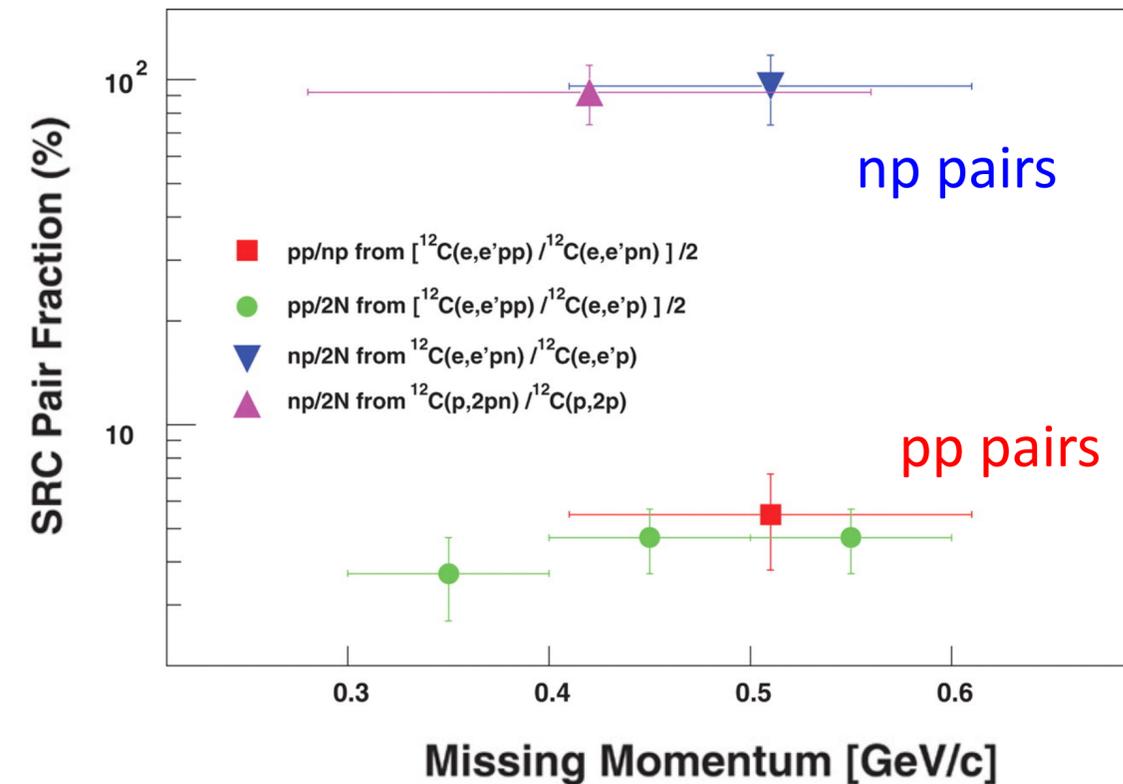


- Reconstruct struck proton, measure recoiling partner
- Protons in pair have high “back-to-back” momentum in **opposite directions**
- High momentum comes from strong, short-distance interactions **within** the pair

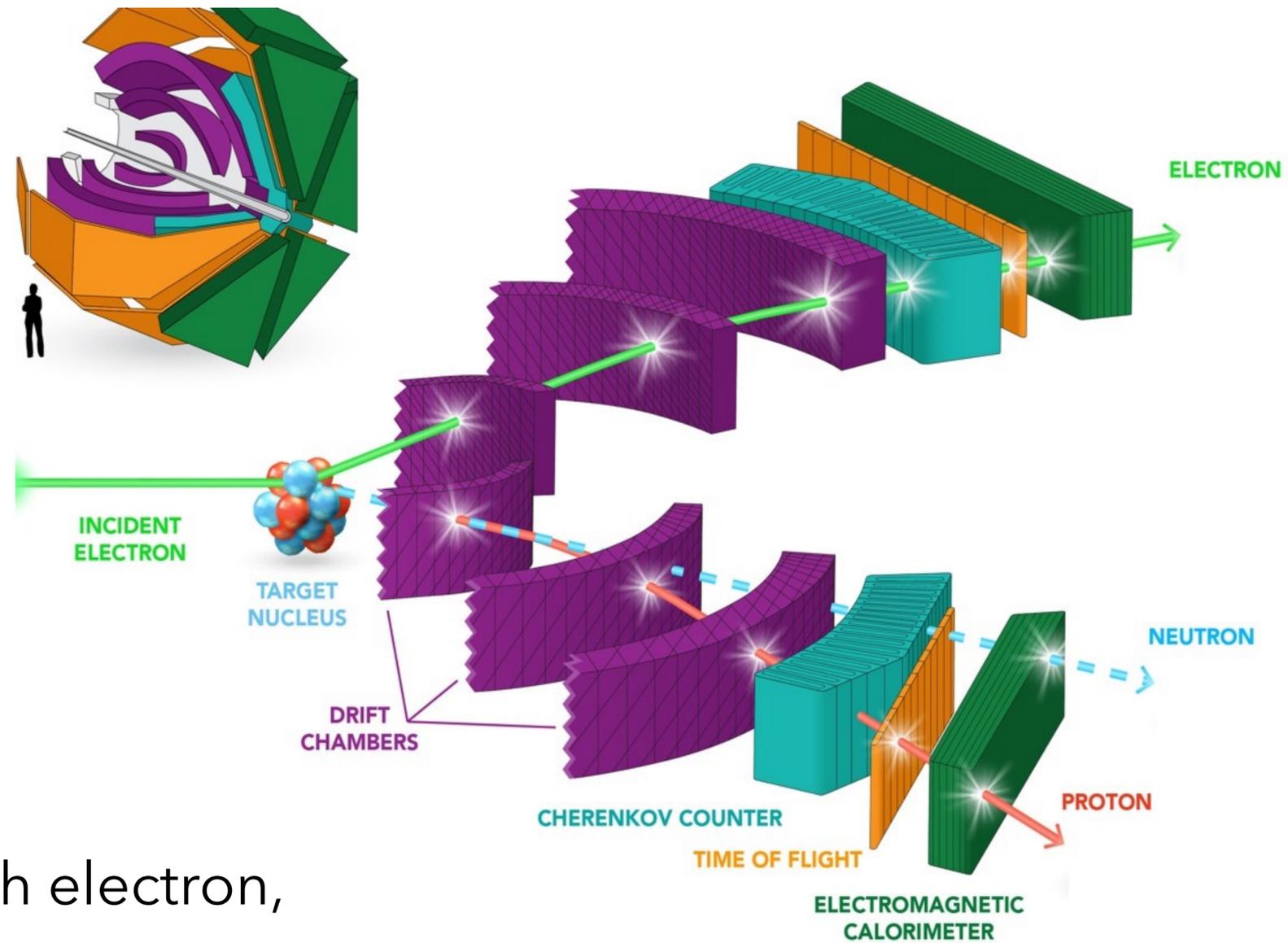


$(e, e'pp)$ vs. $(e, e'pn)$: What kind of pairs do we see?

- BigBite and HAND measure the recoil nucleon isospin
- We find about $10 \times$ as many recoil neutrons for a leading proton!
- **Neutron-proton pairs** dominate at $300 < p_i < 600$ MeV/c



Jefferson Lab Hall B

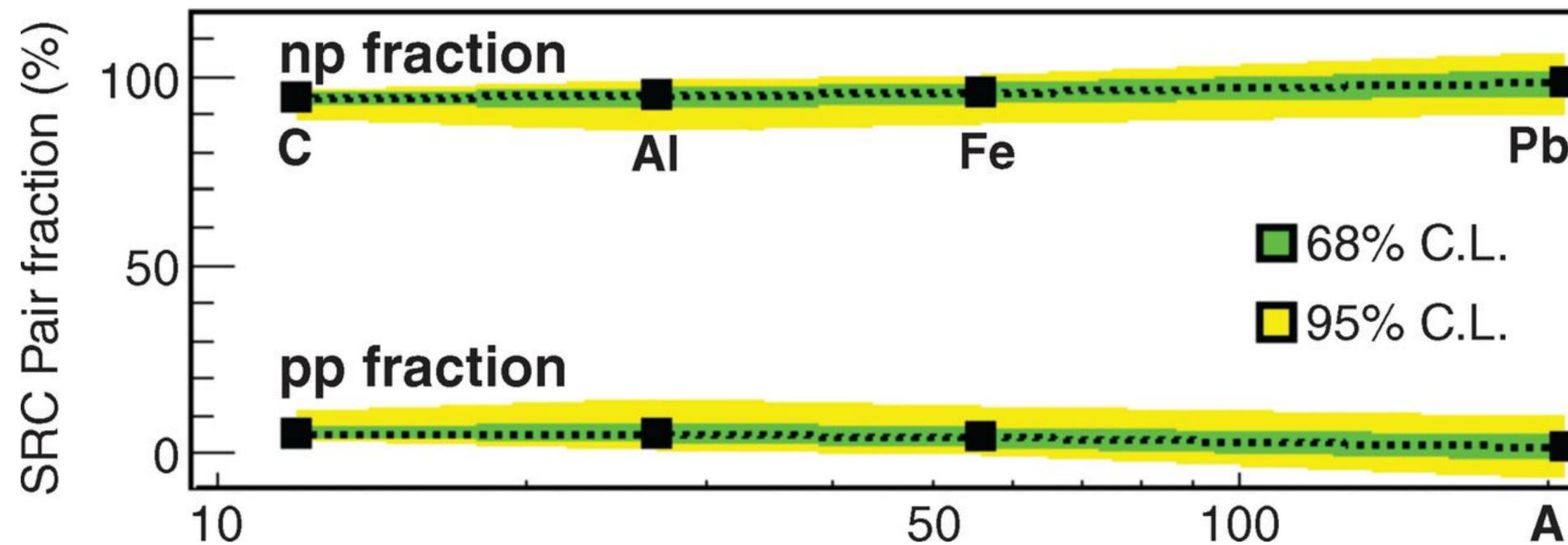


CLAS6 data-mining

- Large-acceptance detector with electron, proton and neutron detection
- Existing nuclear-target data to analyze

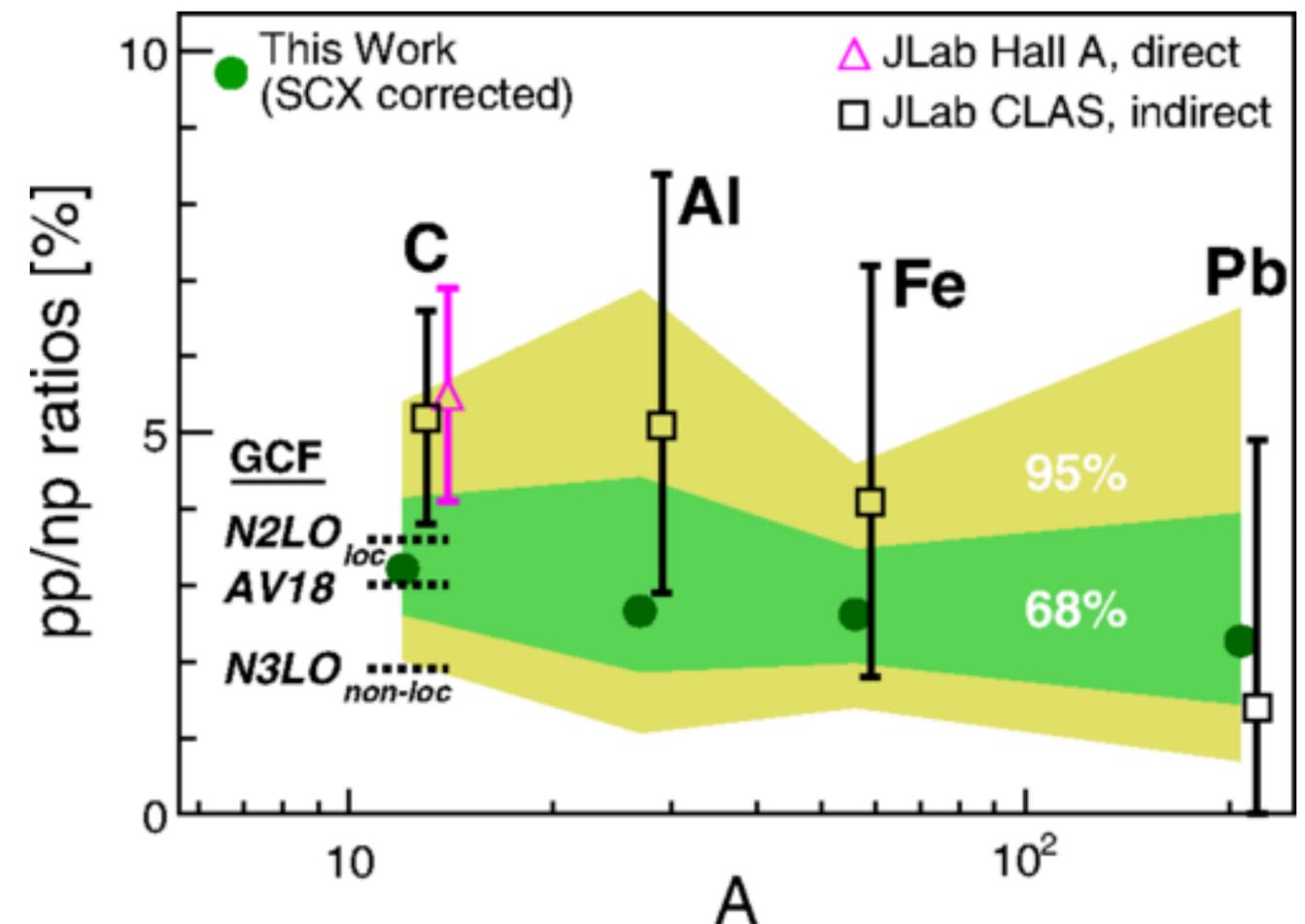
NP-dominance across nuclei

- Used $\sigma_A(e, e'pp)/\sigma_A(e, e'p)$ ratio to estimate pp fraction
 - Assume all high- p_{miss} nucleons have a correlated partner
- NP-SRC pair dominance holds across nuclei, even in highly asymmetric systems



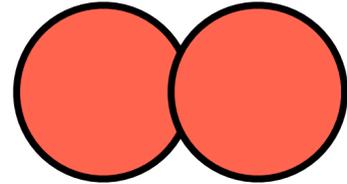
Direct measurement with $(e, e'pp)/(e, e'np)$

- Direct observation using $(e, e'pp)$ and $(e, e'np)$ across nuclei
- NP-SRC pairs dominate in all nuclei by more than an order of magnitude
- **This is the product of short-distance nuclear interactions that drive SRCs**

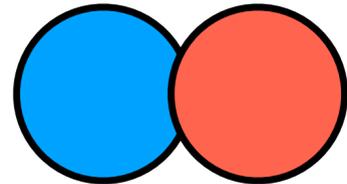


How can we build $2N$ -SRCs?

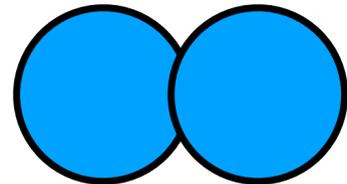
Proton-Proton Pairs:



Neutron-Proton Pairs:

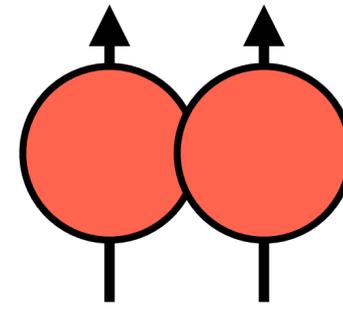
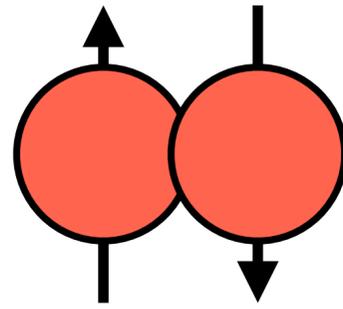


Neutron-Neutron Pairs:

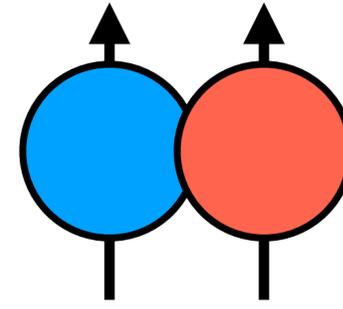
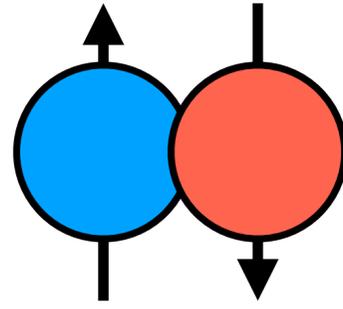


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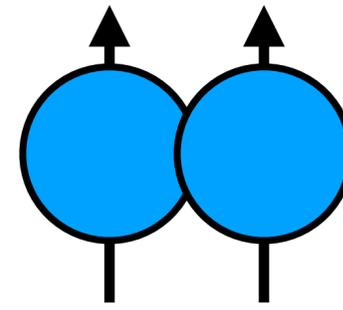
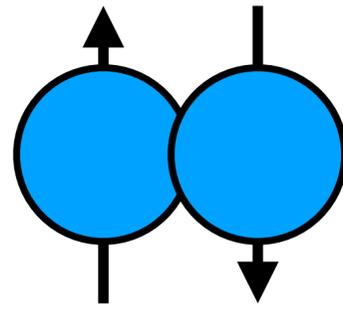
Proton-Proton Pairs:



Neutron-Proton Pairs:



Neutron-Neutron Pairs:



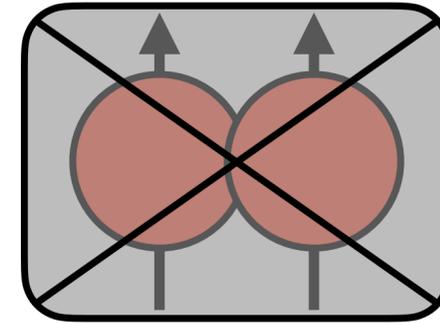
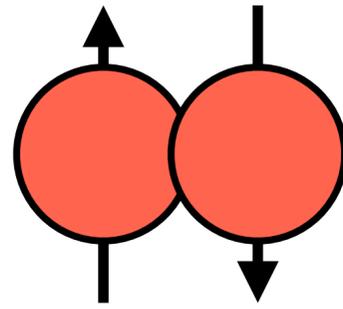
$$S = 0$$

$$S = 1$$

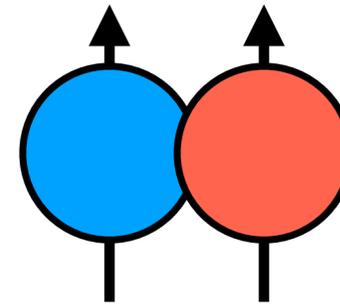
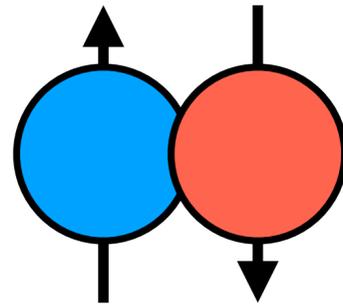
$3 \times 2 = 6$ types of pairs?

How can we build $2N$ -SRCs?

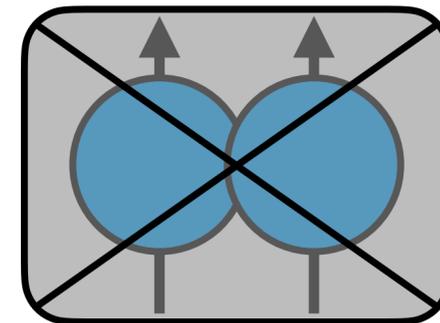
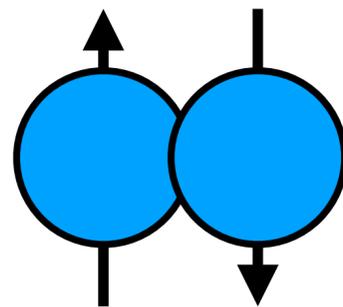
Proton-Proton Pairs:



Neutron-Proton Pairs:



Neutron-Neutron Pairs:



$S = 0$

$S = 1$

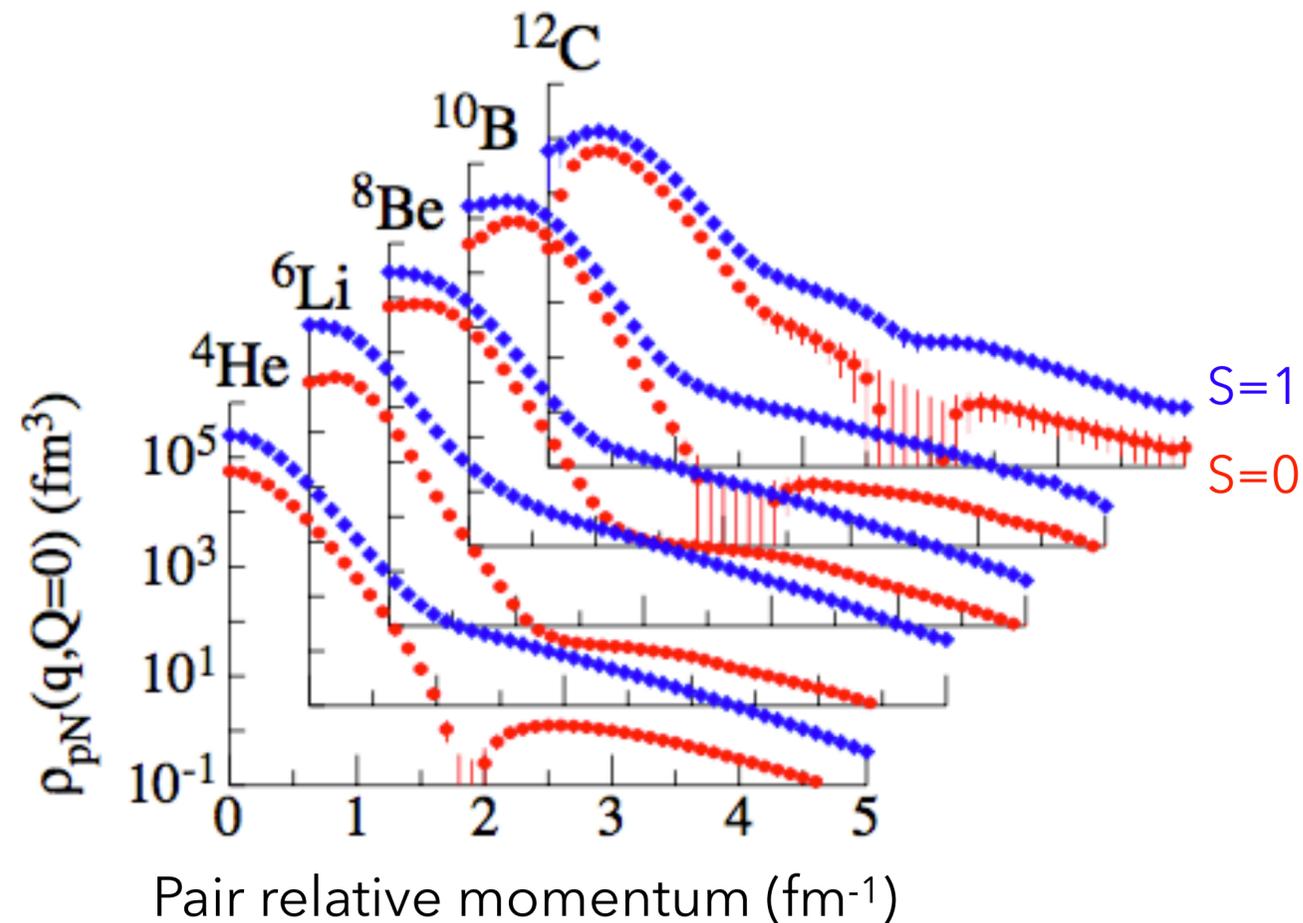
$3 \times 2 = 6$ types of pairs?

Pauli disagrees!

Only neutron-proton can have aligned spin $S = 1$

Nucleons prefer $S=1$ pairing

Carlson et al., RMP **87** (2015) 1067



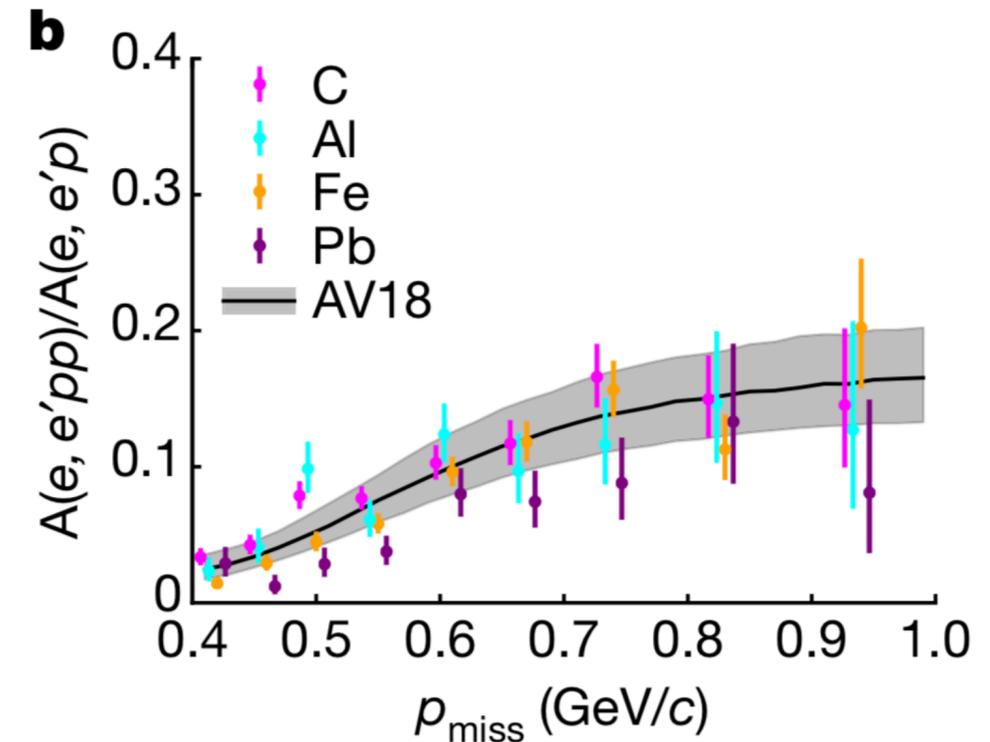
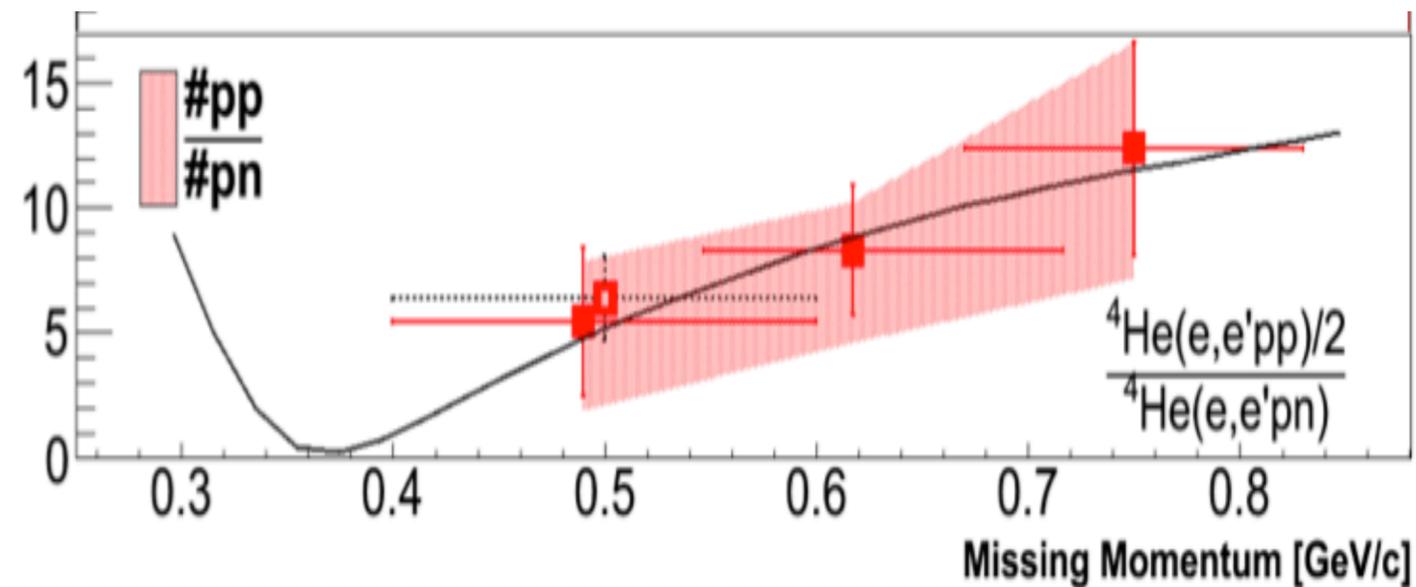
- At $p_{rel} = 300 - 500$ MeV/c, the s-wave momentum distribution has a minimum (node)
- Filled in by **tensor correlations** when $S = 1$:

$$V_{NN}(r) = V_c(r) + V_T(r)S_{12}$$

$$S_{12} = 3(\sigma_1 \cdot \hat{r})(\sigma_2 \cdot \hat{r}) - \sigma_1 \cdot \sigma_2$$

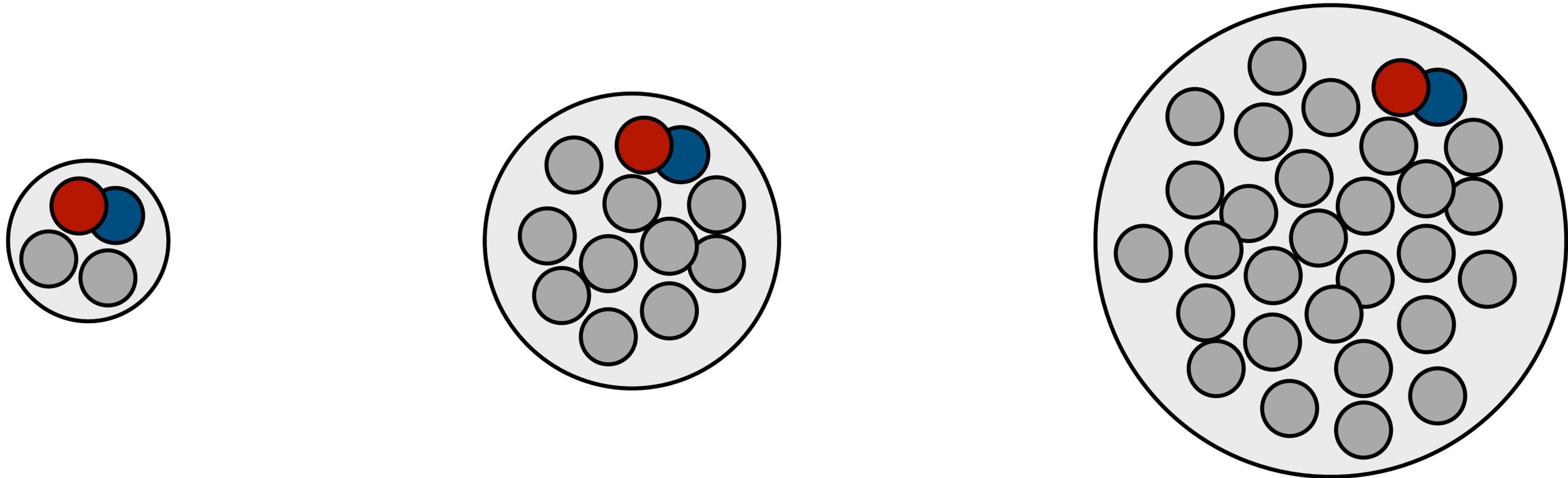
- Think about the deuteron – np , $S = 1$ is bound, while pp and nn are not!

But this is not constant!



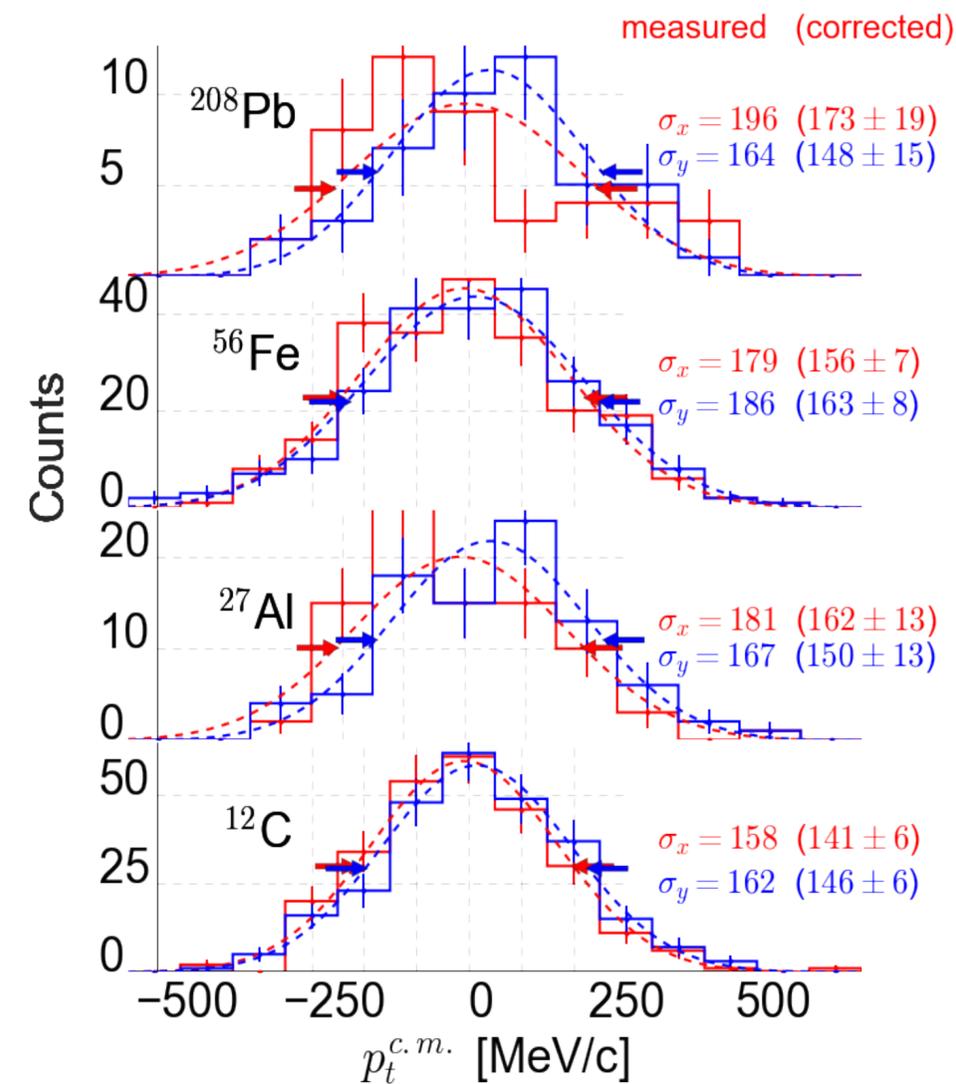
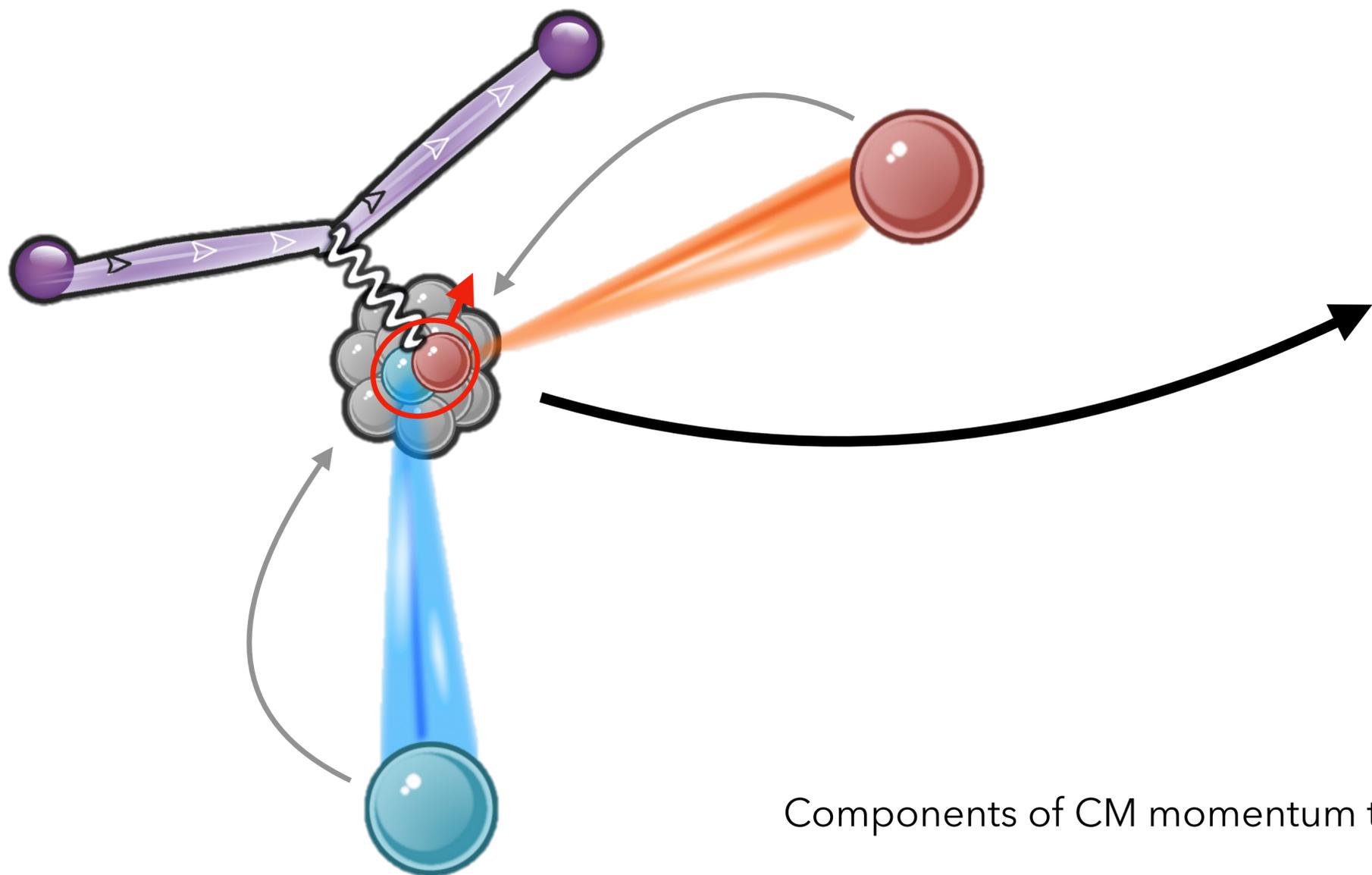
- Higher missing momentum moves us away from the $S=0$ node at $p_{\text{rel}} \approx 400$ MeV/c
- Tensor force does not dominate everywhere – pp -pair fraction increases with momentum
- We will see this relates to changing structure of nucleon-nucleon force at shorter distances

How does the nuclear medium affect SRC behavior?



- We know from a_2 that SRC **abundances** differ across nuclei, increasing with A
 - More nucleons together \rightarrow greater chance of pairing up
- How else does SRC formation impact their behavior?

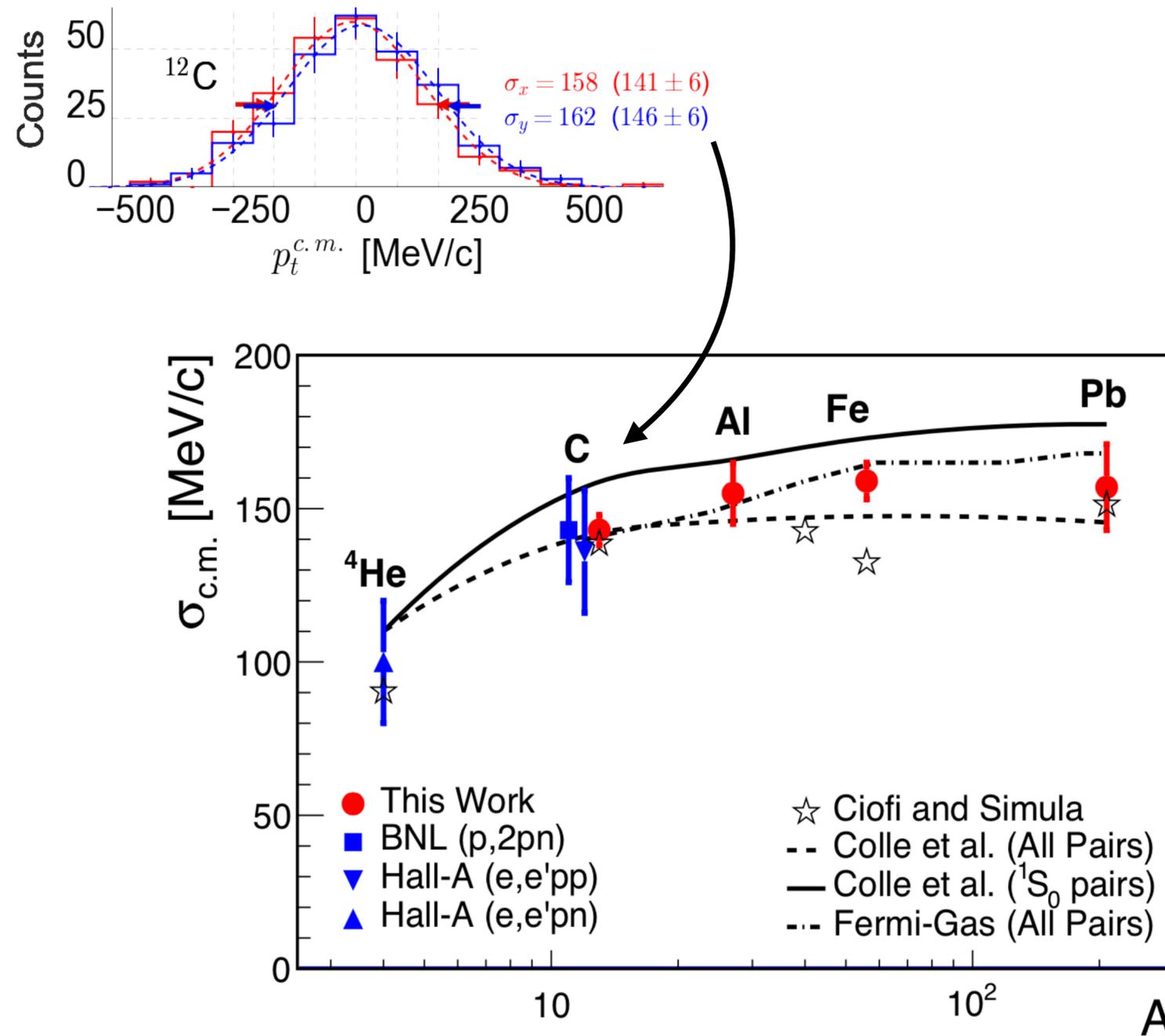
Exclusive $(e, e'pp)$ let us reconstruct pair center-of-mass motion



Components of CM momentum transverse to p_{miss}

→ Minimizes impact of final-state rescattering

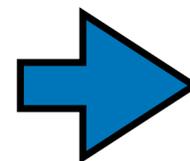
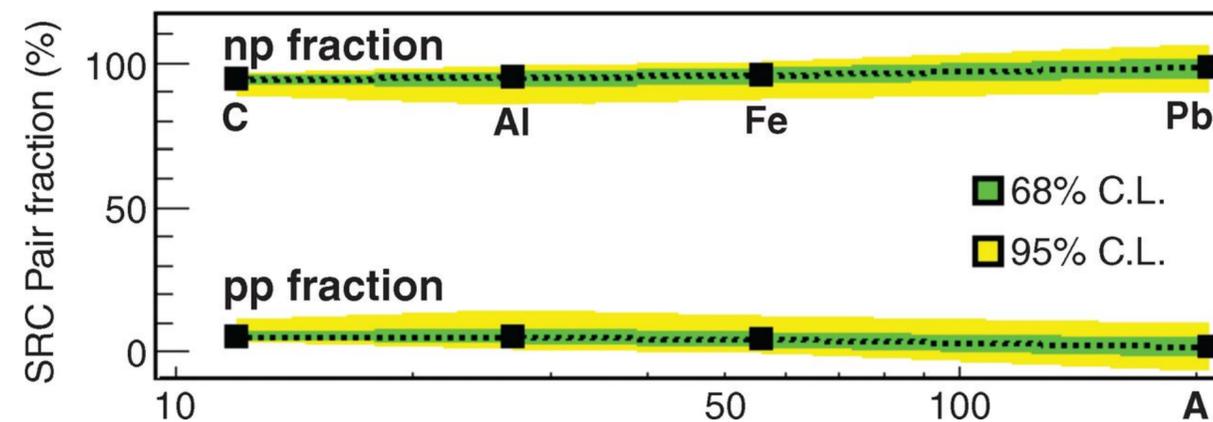
Extract CM across different nuclei



- Larger nuclei \rightarrow pairs are moving more within
- Higher average momentum of pairing nucleons \rightarrow higher total momentum of pairs
- **Nucleon pairing into SRCs is a mean-field phenomenon!**

Which nucleons pair together?

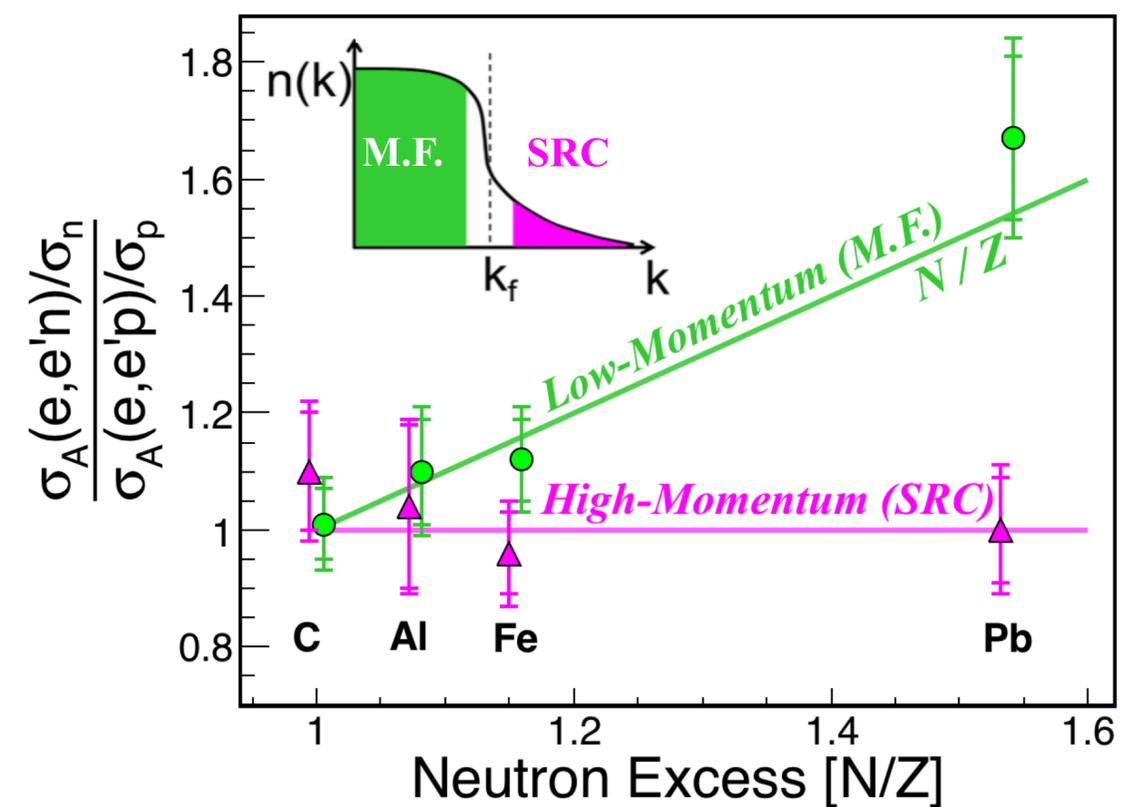
We know that NP-SRC dominance holds even for heavy nuclei



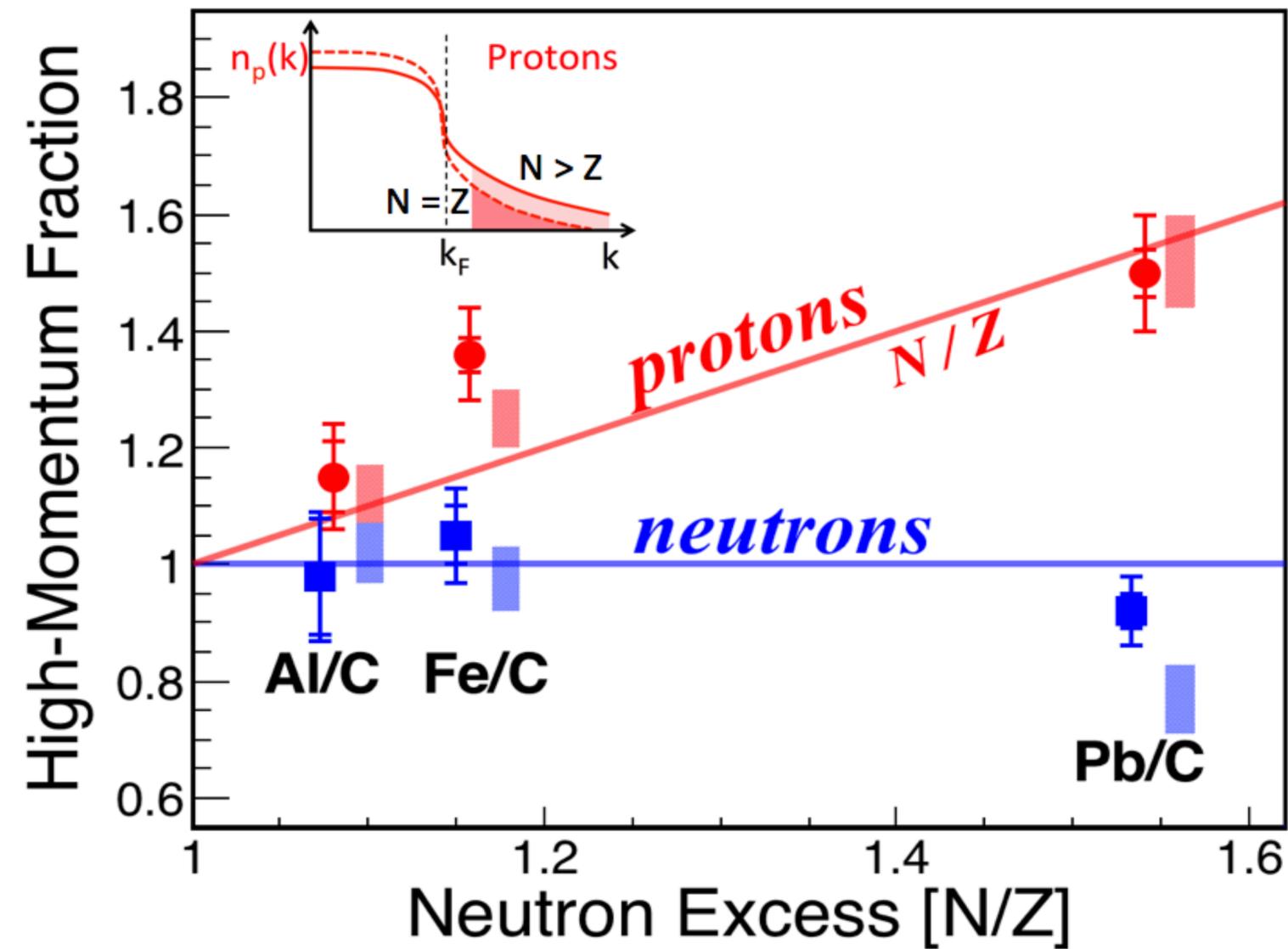
As we add neutrons:

Larger neutron fraction in mean-field

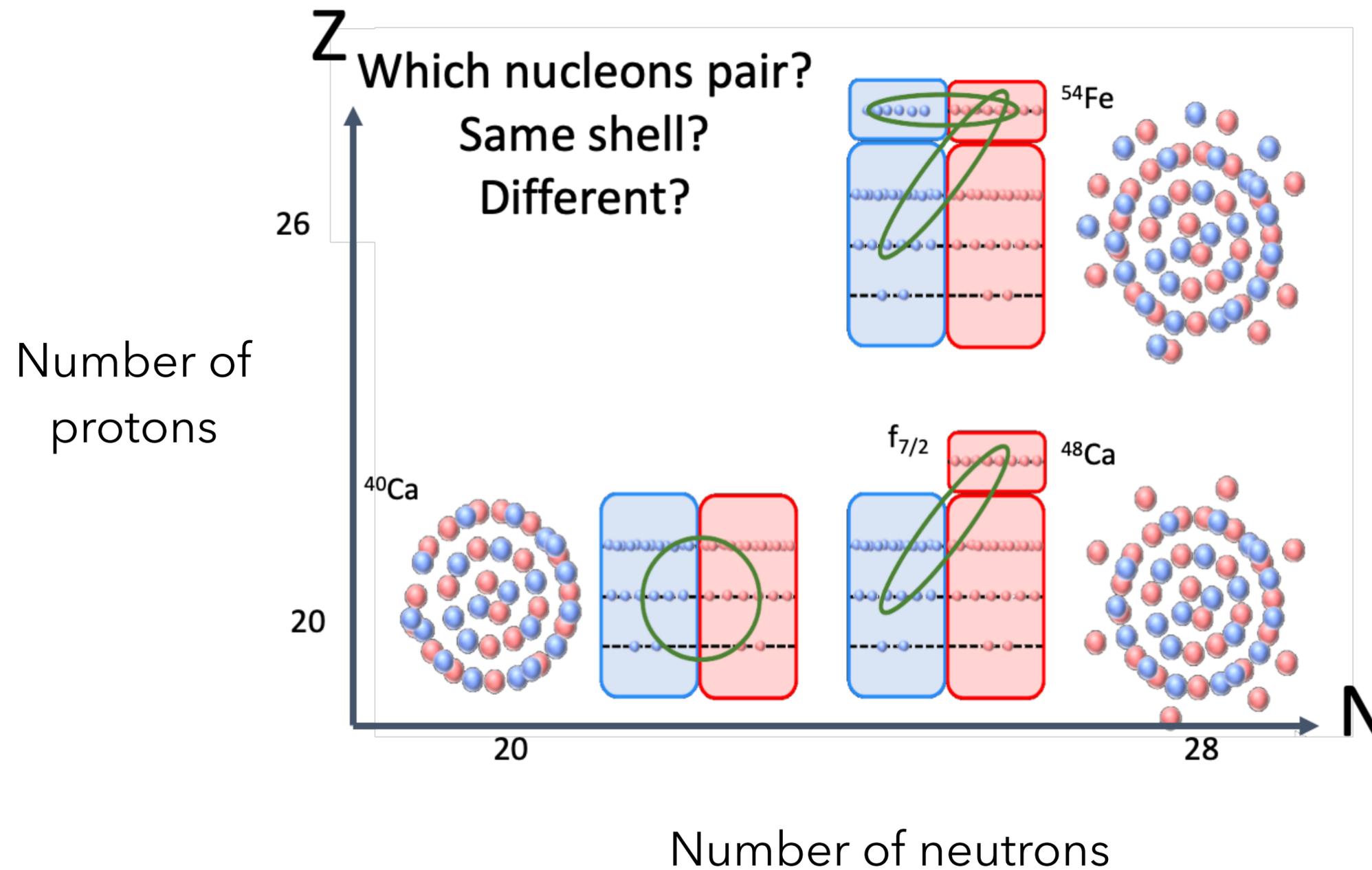
SRCs remain $N \approx Z$!



In $N > Z$, Protons correlate, Neutrons saturate

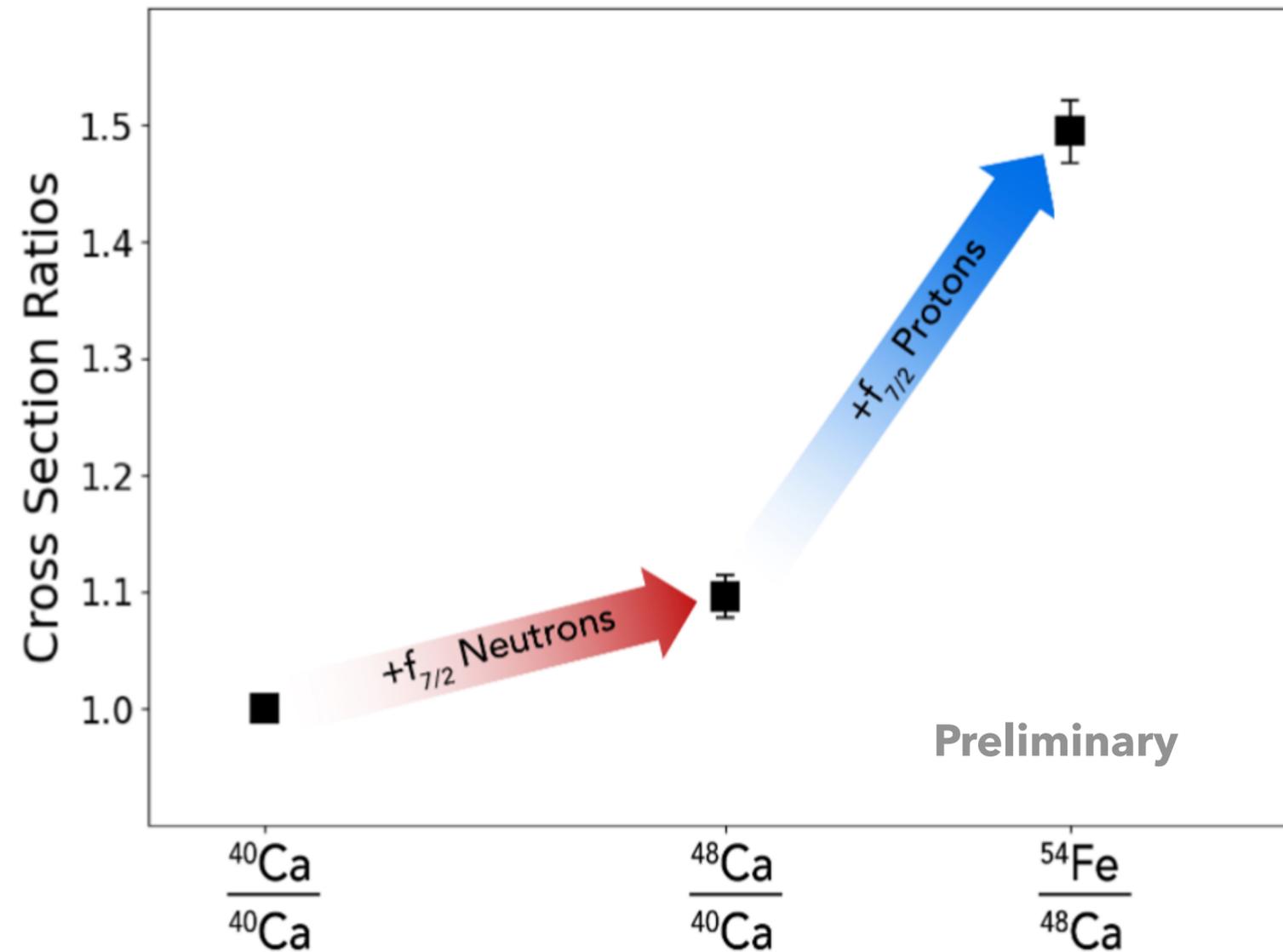


^{40}Ca , ^{48}Ca , ^{54}Fe can teach us about pairing mechanisms



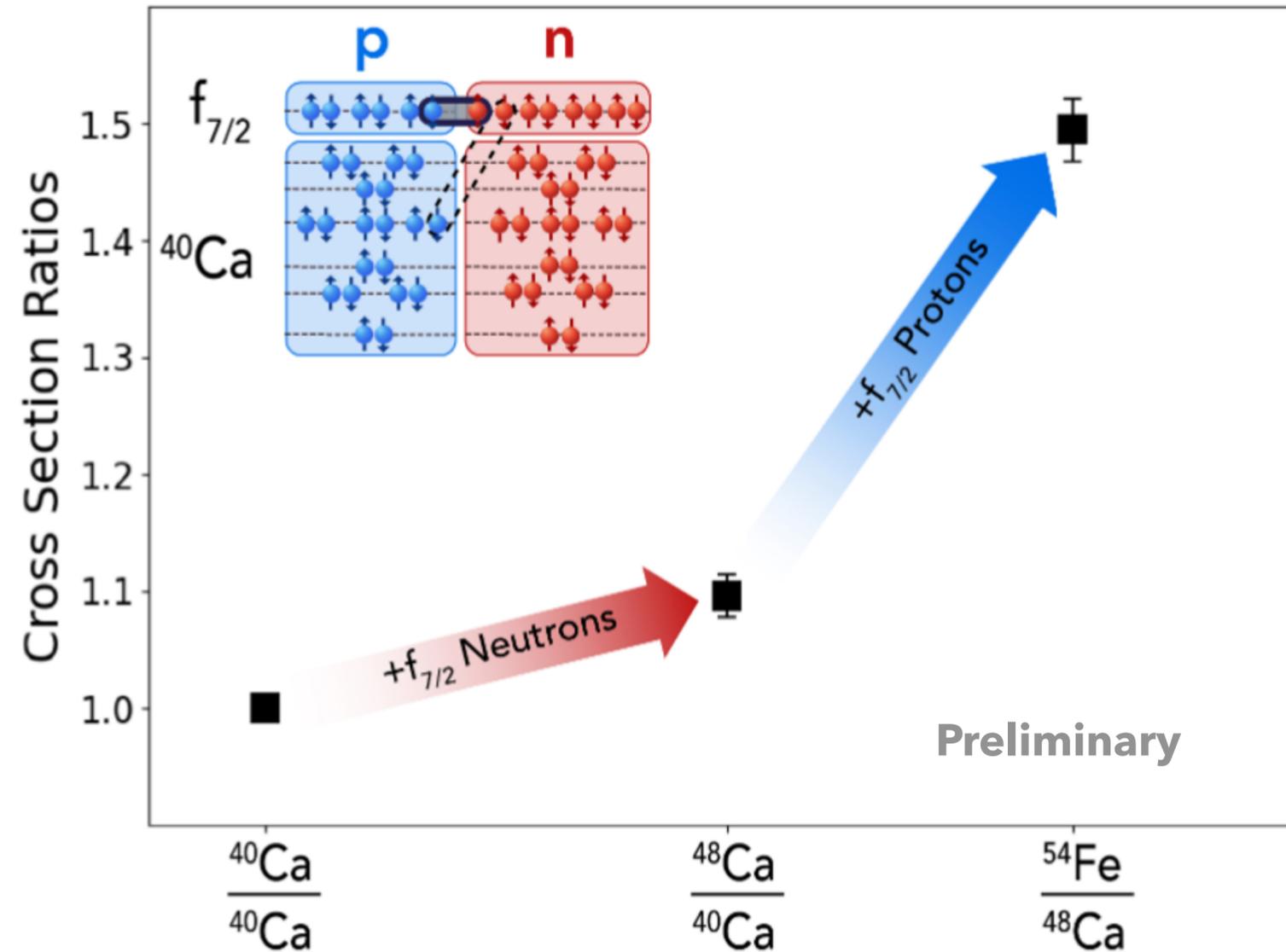
^{40}Ca , ^{48}Ca , ^{54}Fe can teach us about pairing mechanisms

New Hall C data: CaFe ($e, e'p$)



^{40}Ca , ^{48}Ca , ^{54}Fe can teach us about pairing mechanisms

New Hall C data: CaFe ($e, e'p$)



Nucleons pair within their shells

New Hall C data: CaFe ($e, e'p$)

