

# Light Ion Physics in EIC era: From nuclear structure to high-energy processes

Summer School, Florida International University, 19-27 June 2025

Wim Cosyn, Christian Weiss, Dien Nguyen, Organizer



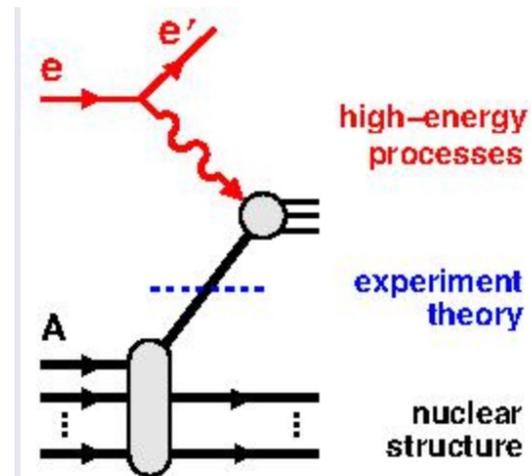
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**FIU** | FLORIDA  
INTERNATIONAL  
UNIVERSITY

# Nuclear Structure and Short-Range Correlations

## Experimental approach using Electron Probe

Dien Nguyen  
University of Tennessee



# Lectures format

## □ Cover the basics level for PhD students

- Little formalism, more conception
- Including Basic Experimental information
- Experimental Results and their interpretations

## □ Style

- Informal, encouraging the interaction
- Interrupt any time for questions

Many slides are adapted from my collaborators.

Special Thanks to Prof. L. Weinstein, Dr. Holly Szumila-Vance, Prof. O. Hen, Prof. D. Day, Prof. A. Schmidt, Dr. F. Hauenstein, Dr. Arun and More

# Lectures Outlines:

## Lecture 1:

Dien Nguyen

- Overview of an electron scattering probe
  - Elastic scattering
  - Quasi-elastic scattering
  - Deep inelastic scattering
  - Introduction to short range correlations

## Lecture 2:

Jackson Pybus

- Short Range correlations (SRCs) status
  - Experimental results
  - Short range correlation properties

## Lecture 3:

Jackson Pybus

- SRC factorization
  - GCF: contact formalism
  - Nuclear ground state

## Lecture 4:

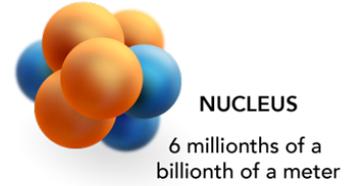
Jackson Pybus

- SRC beyond electron probe
  - Hadron probe
  - Photon probe
  - Future direction

# Systems

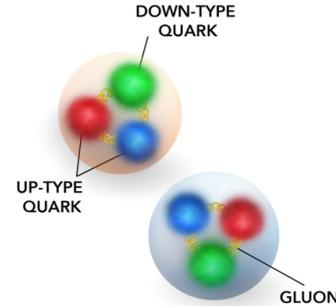
## Nucleus as a system

- Collection of bound protons and neutrons



## Nucleons as a system

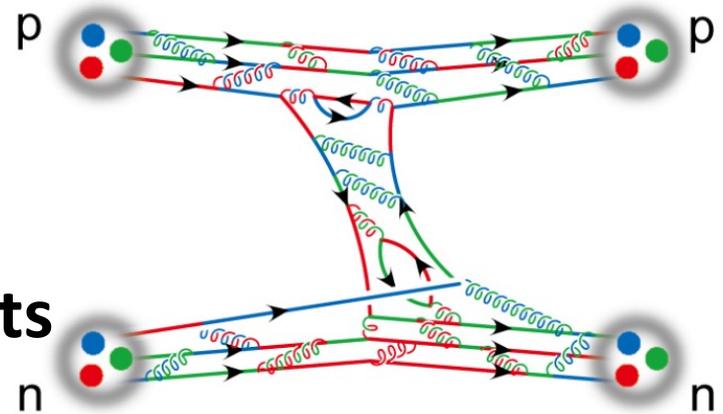
- Collection of bound quarks



# Interactions

## Nucleon-nucleon interaction

Arises from quark interactions

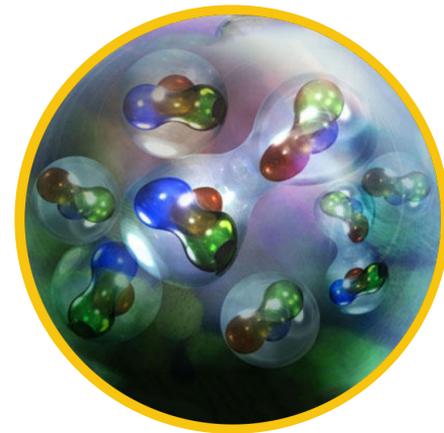


## Nucleon in-nuclear medium effects

Affecting quark distributions

# Electron Scattering: Nuclear Microscope

**Goal:** Study the internal structure (and dynamics) of complex objects

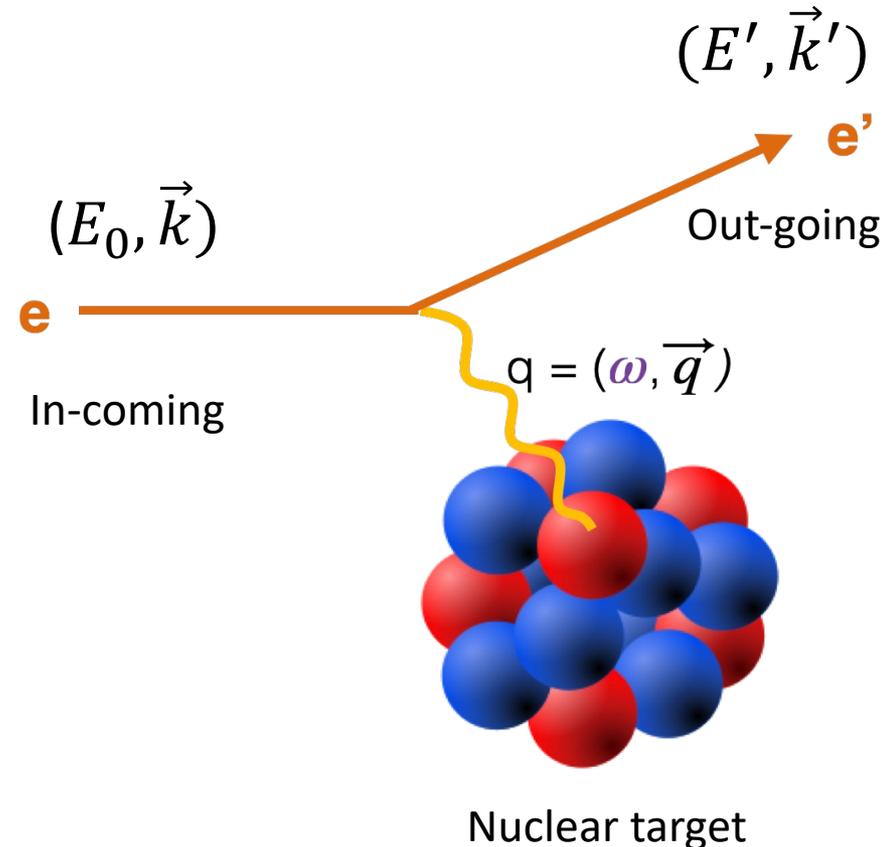


# Electron Scattering: Nuclear Microscope

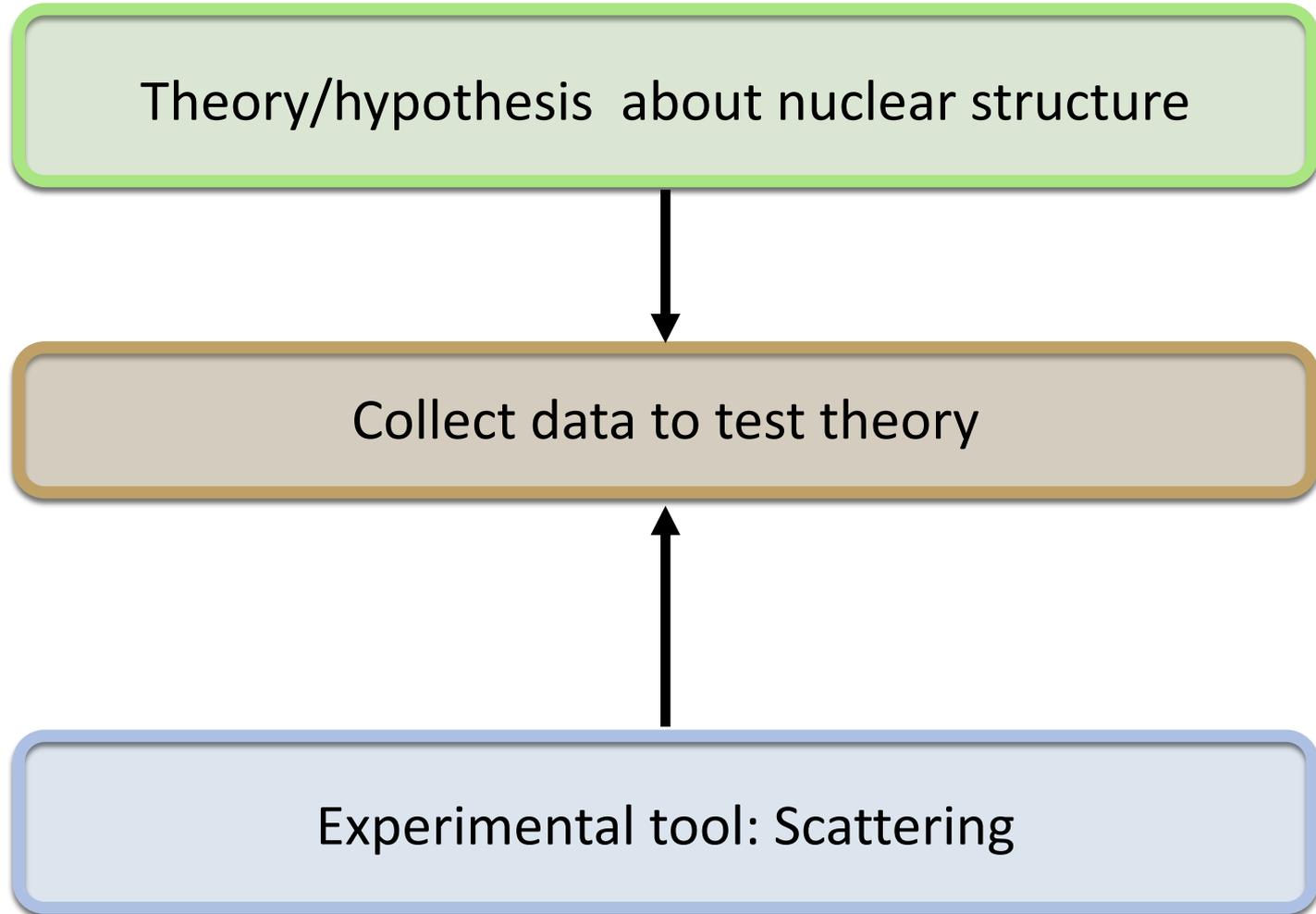
**Goal:** Study the internal structure (and dynamics) of complex objects

**Means:**

- Using high energy electron scattering off nuclear target
- Detecting final states particles
- Using detected particle's information to infer the nuclear structure

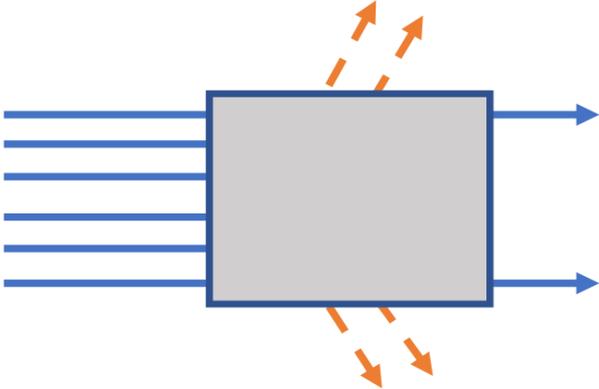


# Scientific Method

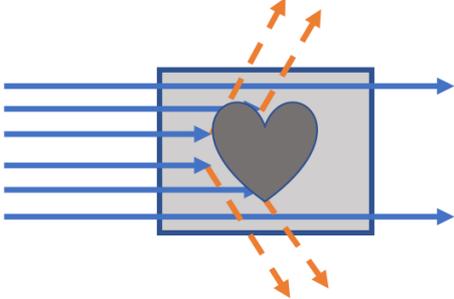
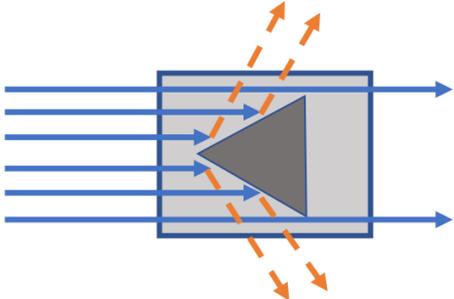
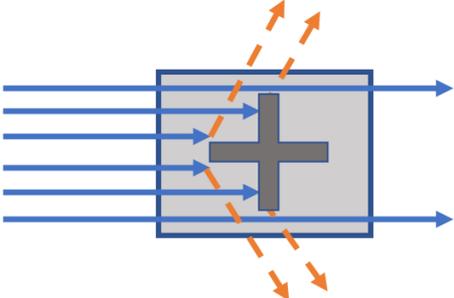


# Determine Internal Structure with Scattering

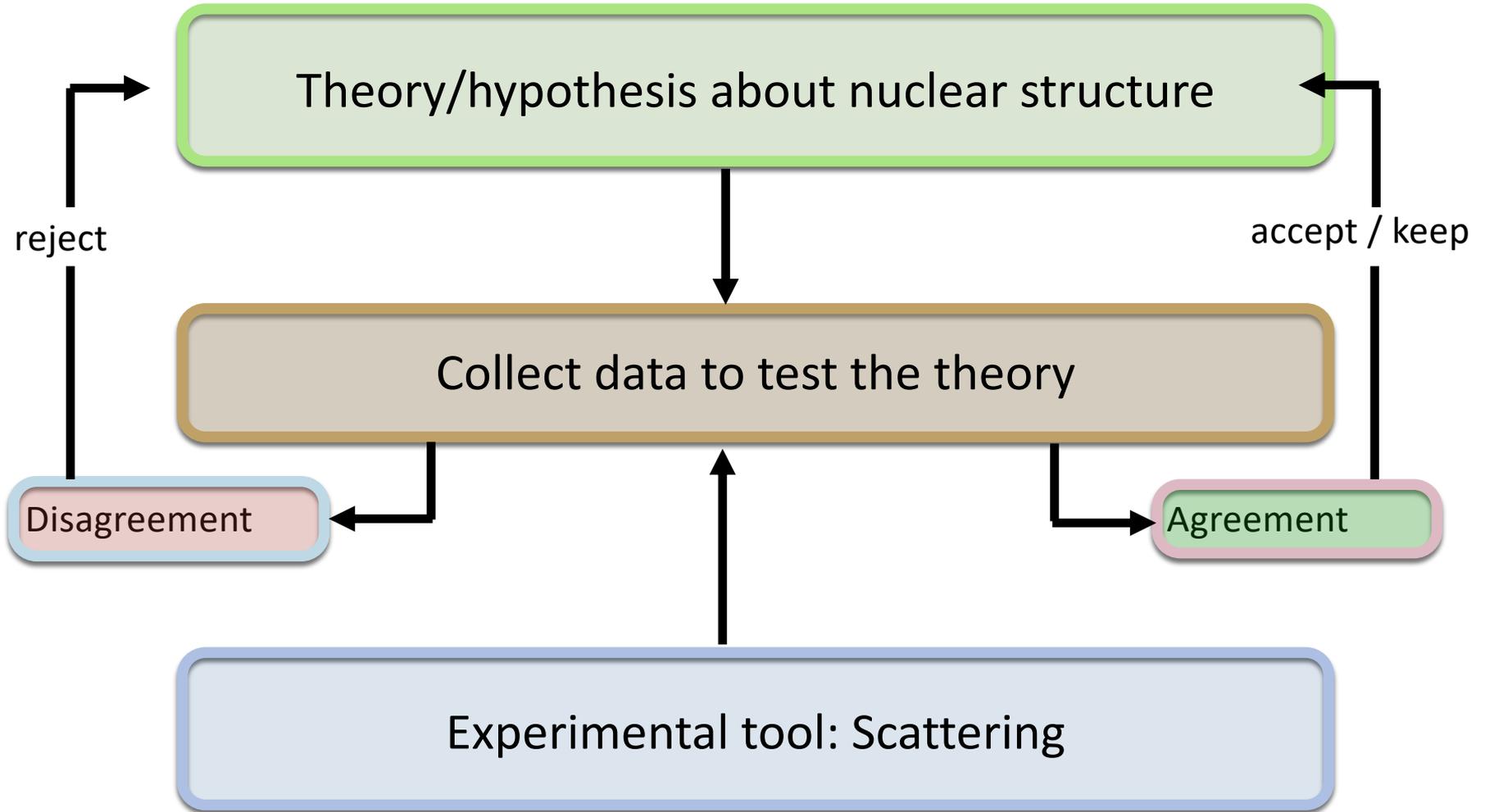
Measured



Hypotheses



# Scientific Method



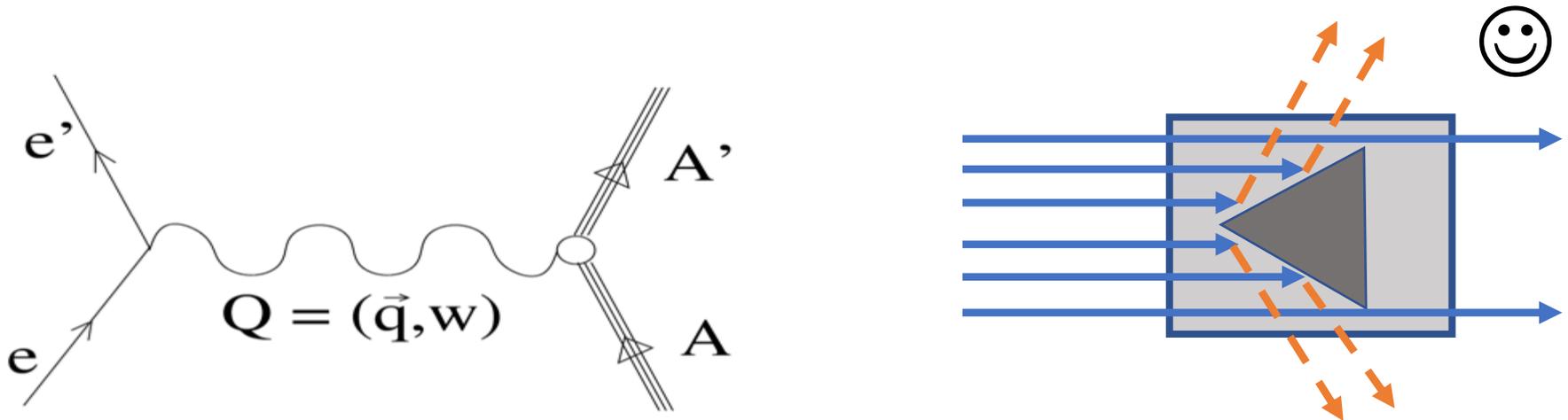
# Electron Scattering: Nuclear Microscope

**Goal:** Study the internal structure (and dynamics) of complex objects

**Means:** Using high energy electron scattering

Reaction determined by kinematic variables:

- $Q^2 = -q^2$  Interaction-Scale
- $x_B = Q^2/(2m_p v)$  Dynamics
- $\omega(\nu) = E - E'$  Energy transfer

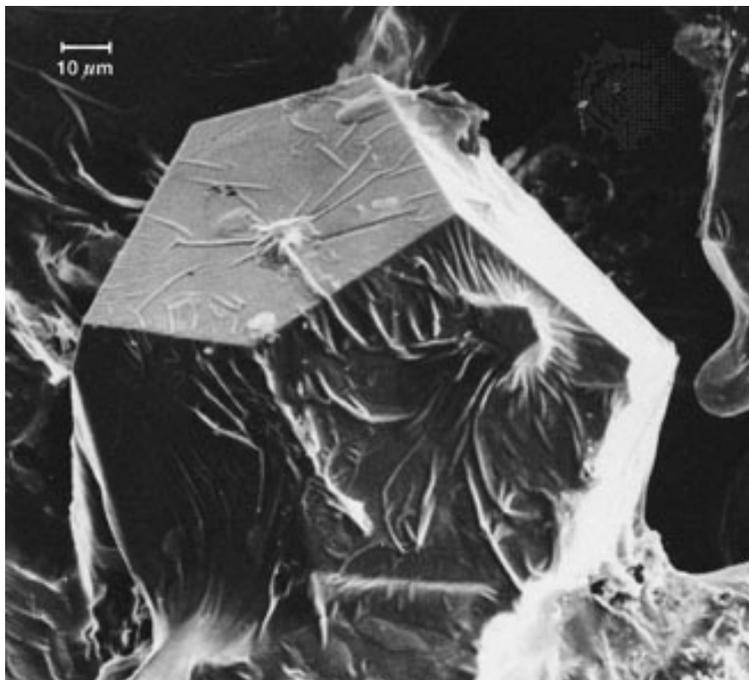


# Electron Scattering: Nuclear Microscope

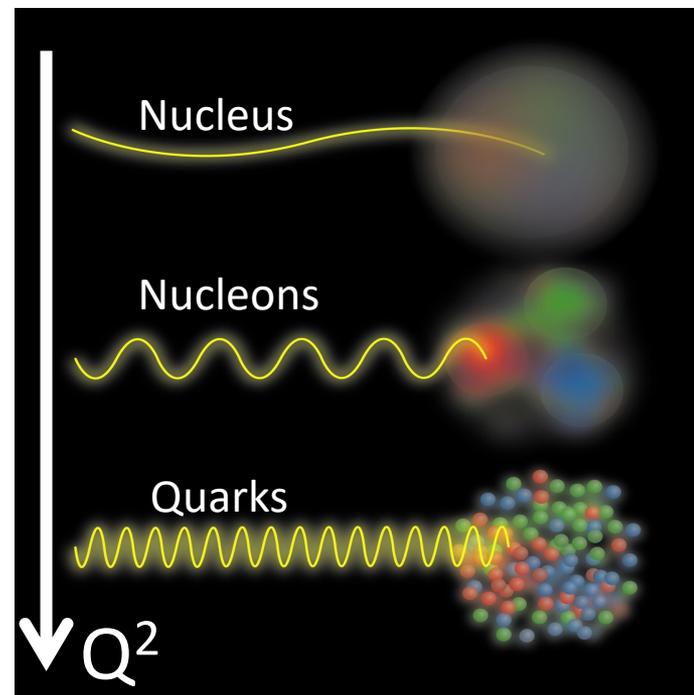
**Goal:** Study the internal structure (and dynamics) of complex objects

**Means:** Using high energy electron scattering

100s eV – 100s keV:  
Material structure



100s MeV – 10s GeV:  
Nuclear structure

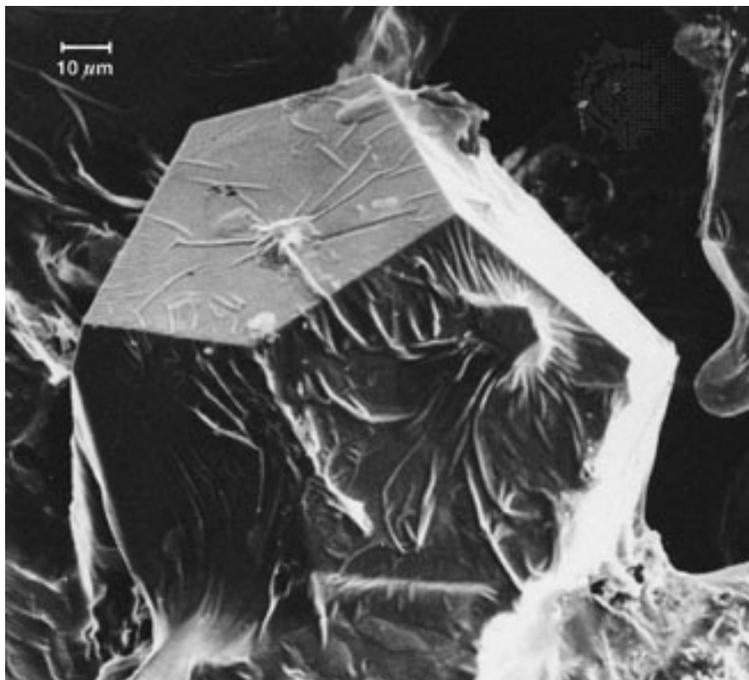


# Electron Scattering: Nuclear Microscope

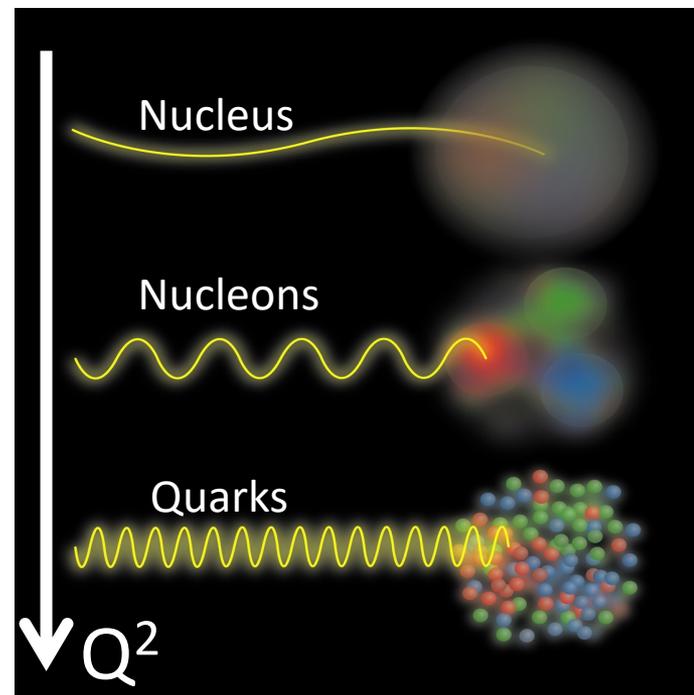
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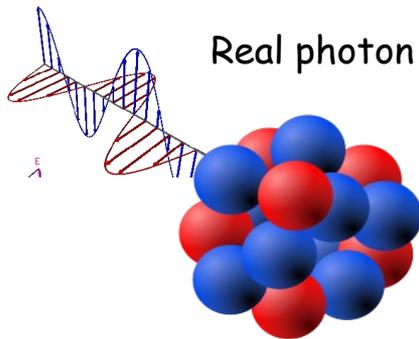
100s MeV – 10s GeV:  
Nuclear structure



Energy  
=  
Resolution !

# It's all photons!

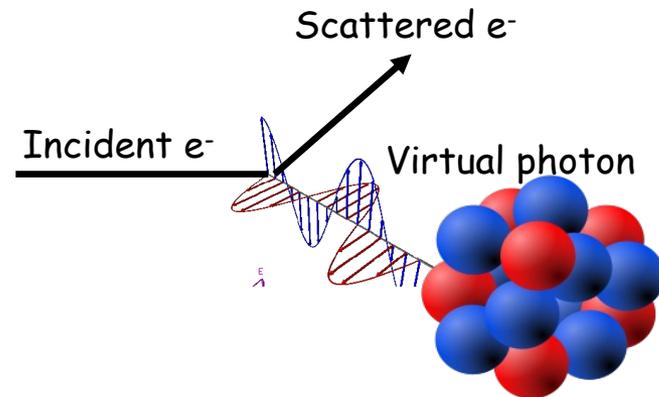
- An electron interacts with a nucleus by exchanging a single **virtual photon**.



**Real photon:**

Momentum  $q = \text{energy } v$

Mass =  $Q^2 = |\mathbf{q}|^2 - v^2 = 0$



**Virtual photon:**

Momentum  $q > \text{energy } v$

$Q^2 = -q_\mu q^\mu = |\mathbf{q}|^2 - v^2 > 0$

Virtual photon "has mass"!

# Energy vs length

Select spatial resolution and excitation energy independently

- Photon energy  $\nu$  determines excitation energy
- Photon momentum  $q$  determines spatial resolution:  $\lambda \approx \frac{\hbar}{q}$

$$\lambda \gg r_p$$

Very low electron energies, scattering is equivalent to that from a “point-like” spin-less object

$$\lambda \sim r_p$$

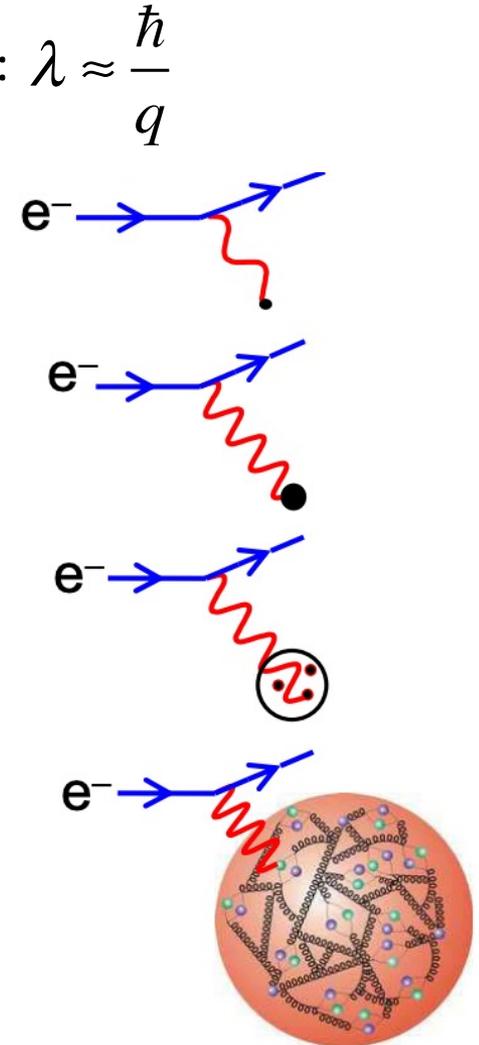
Low electron energies (0.2-1 GeV/c), scattering is equivalent to that from extended charged object

$$\lambda < r_p$$

High electron energies (1 GeV/c +), scattering from constituent quarks and resolve sub-structure

$$\lambda \ll r_p$$

Very high electron energies, proton appears to be a sea of quarks and gluons

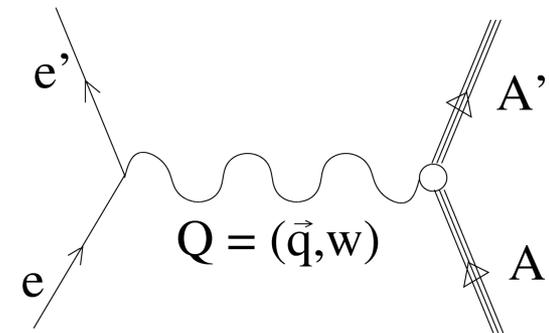


# Why use electrons?

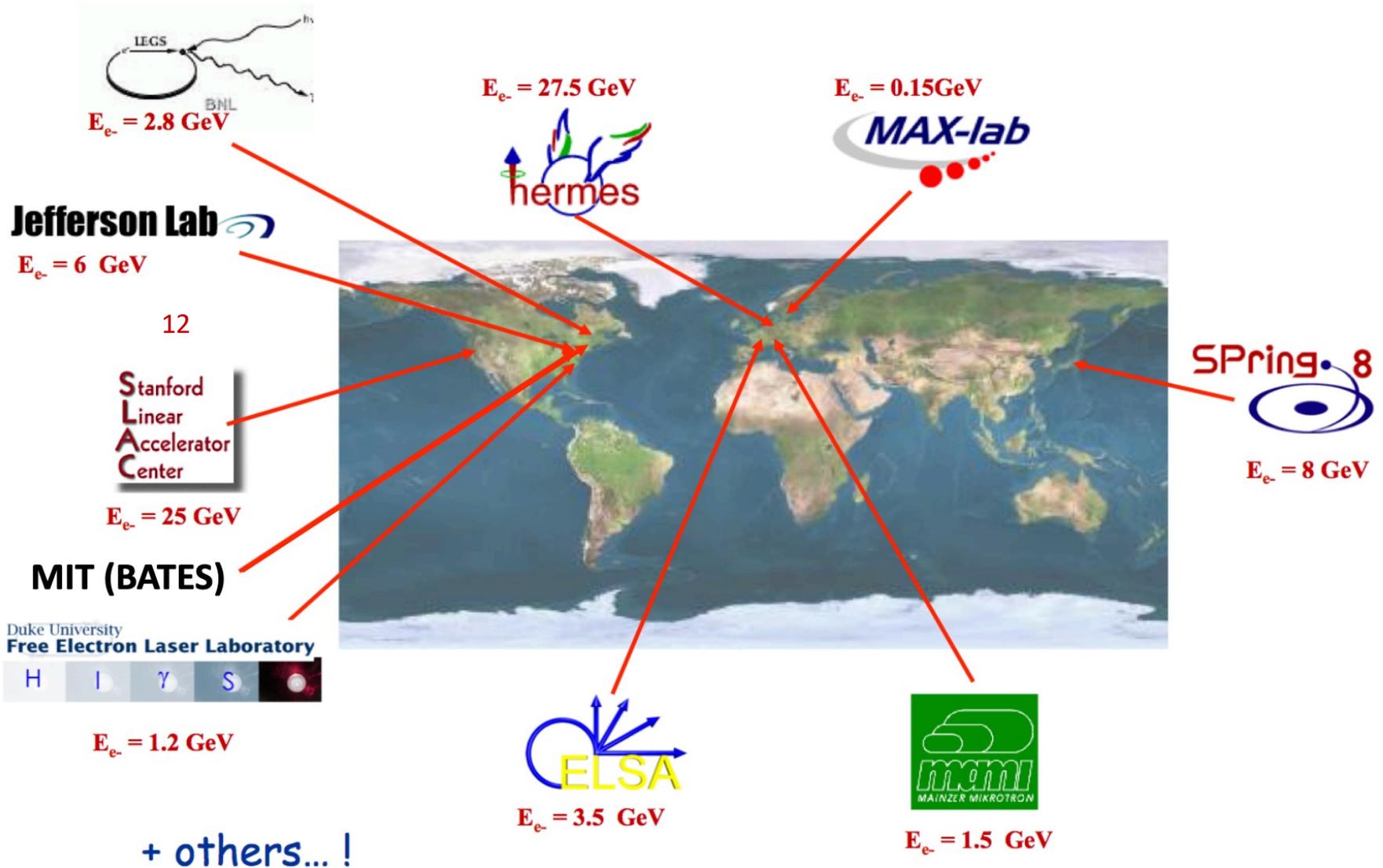
- ❑ Probe structure understood (point particles)
- ❑ Electromagnetic interaction understood (QED)
- ❑ Interaction is weak ( $\alpha = 1/137$ )
  - Theory works: First Born approx / one photon exchange
  - Probe interacts only once
  - Study the entire nuclear volume

## Drawback:

- ❑ Cross sections are small
- ❑ Electrons radiate

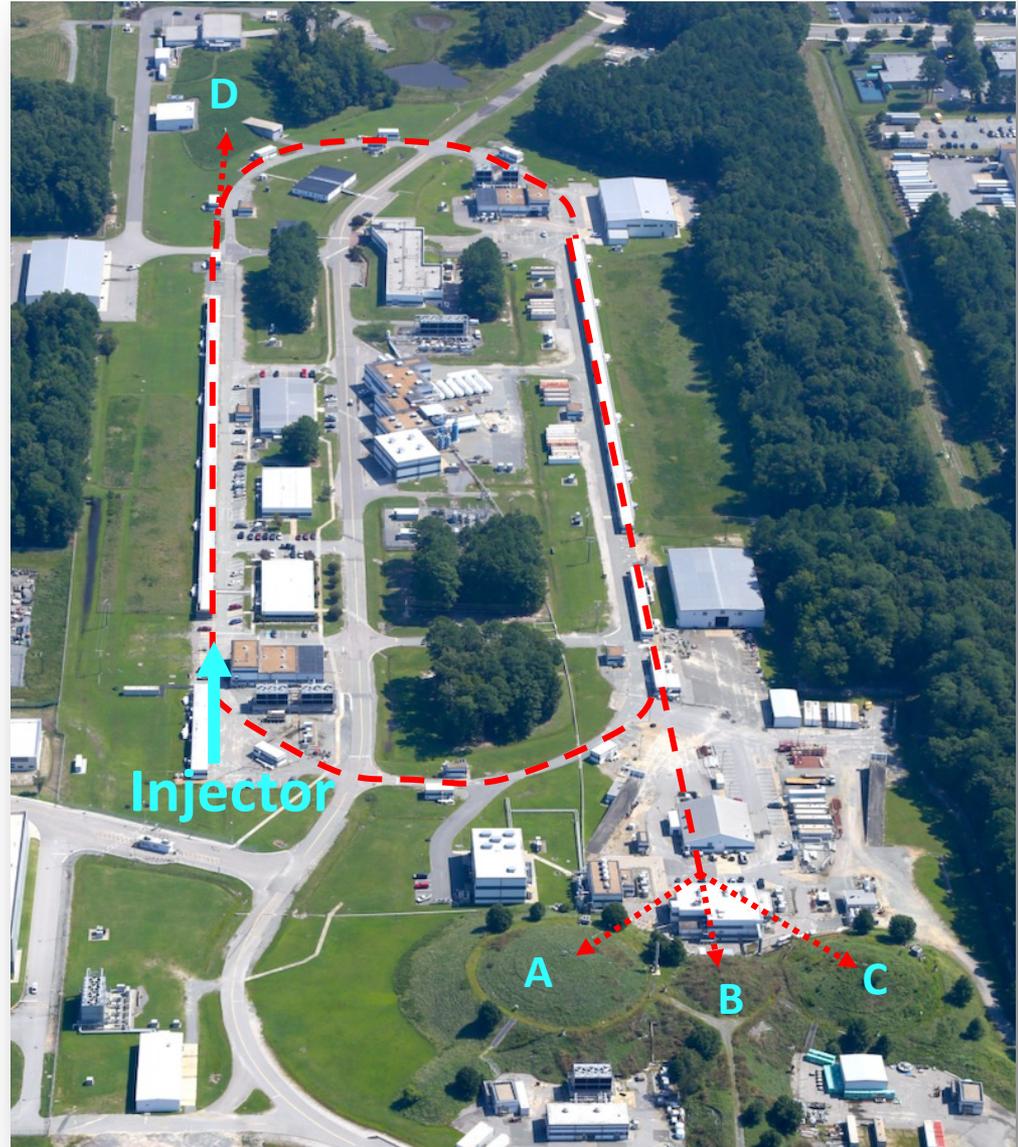


# Worldwide effort



# Jefferson Lab

- ❑ Virginia, USA
- ❑ 1- 11 GeV Electron beam
- ❑ Polarized beams and targets (spin study)
- ❑ 4 experimental halls

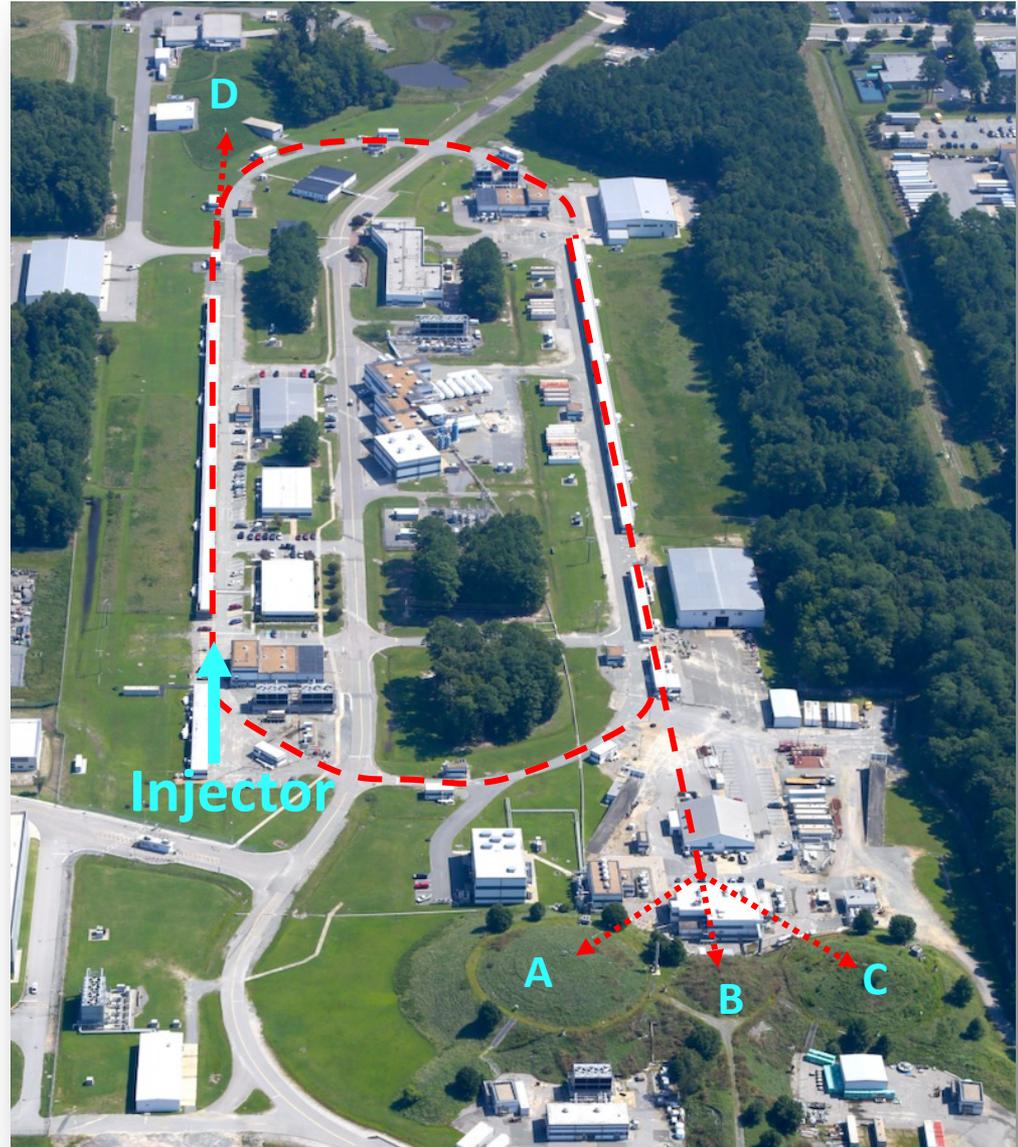
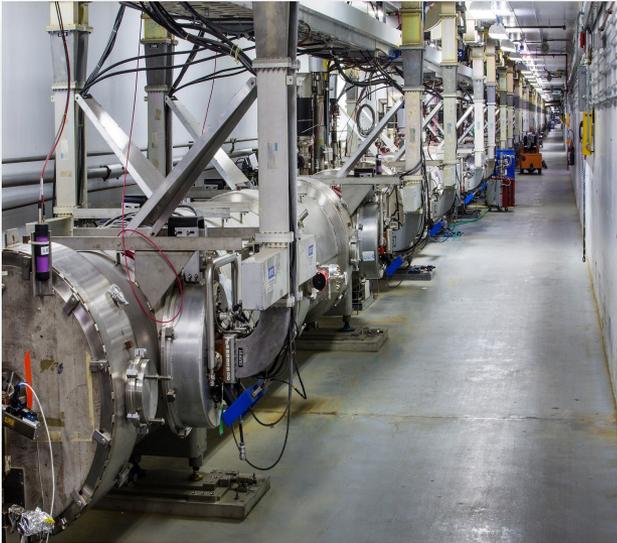


# Jefferson Lab

From Heisenberg's Uncertainty Principle:

$$\Delta x \Delta p \geq \hbar/2 \sim 0.2 \text{ GeV fm}$$

Proton is  $\sim 1 \text{ fm}$  in size ( $10^{-15} \text{ m}$ )  
 $\Rightarrow$  To "see"  $0.02 \text{ fm}$  one needs approx.  $10 \text{ GeV}$  momentum



# 4 experimental Halls

Hall A

Hall C

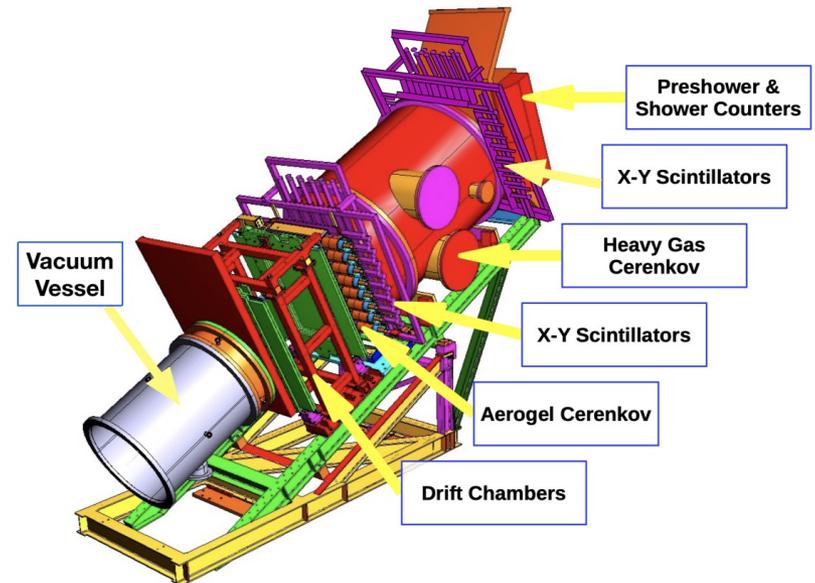
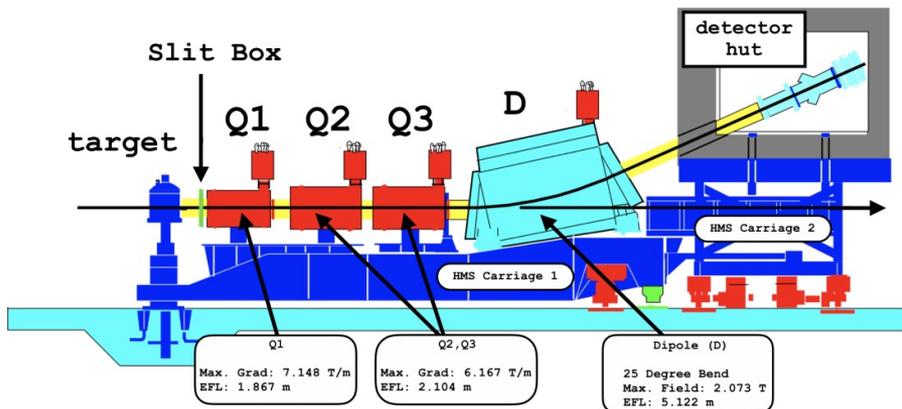
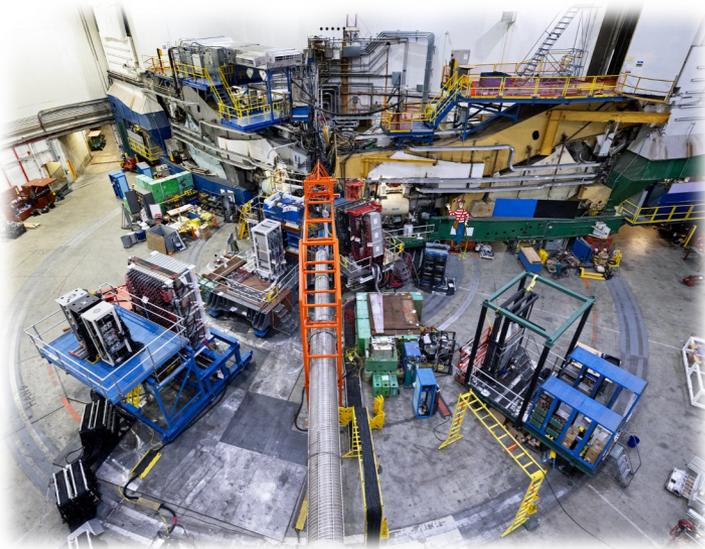
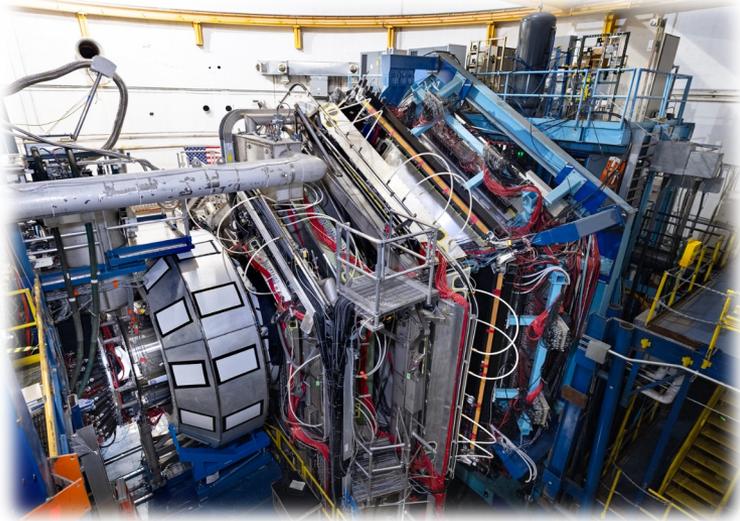


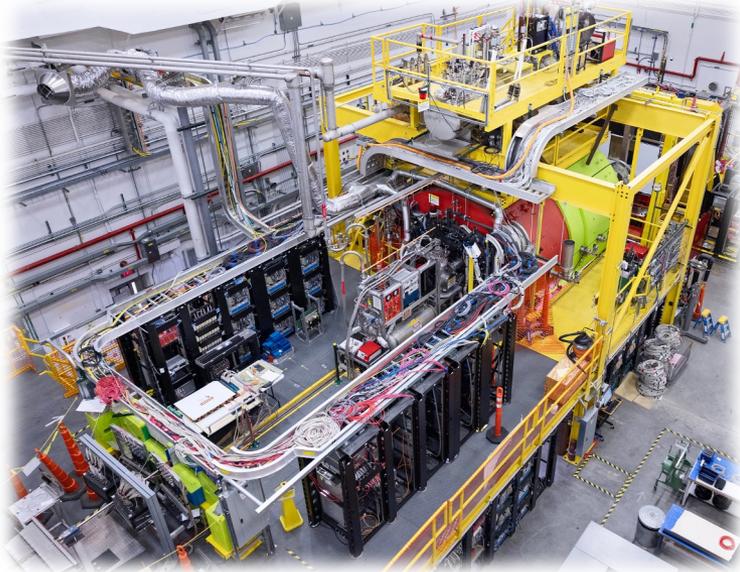
Figure 3.22: High Momentum Spectrometer (HMS) detector stack.

# 4 experimental Halls

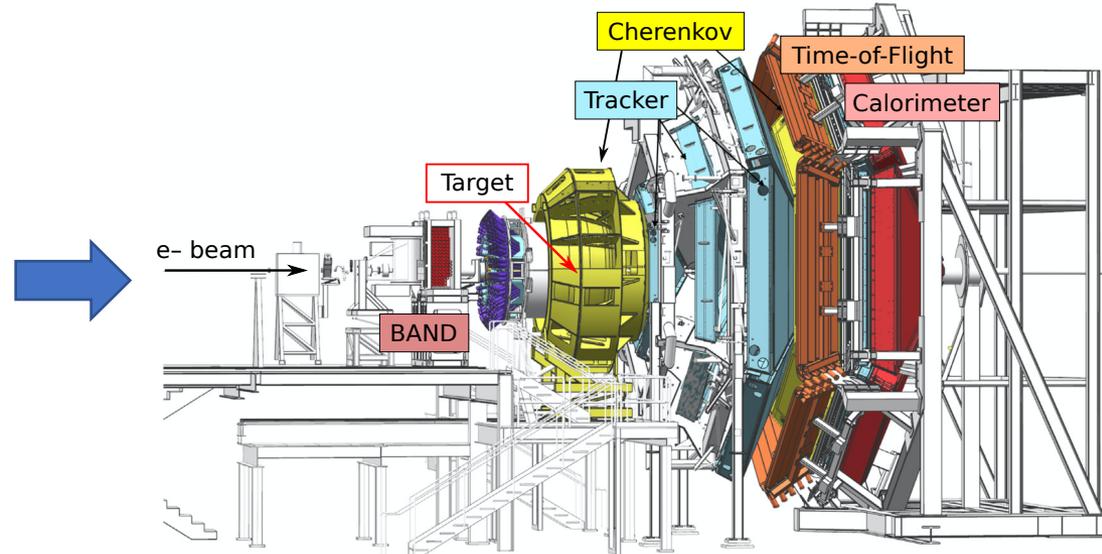
Hall B



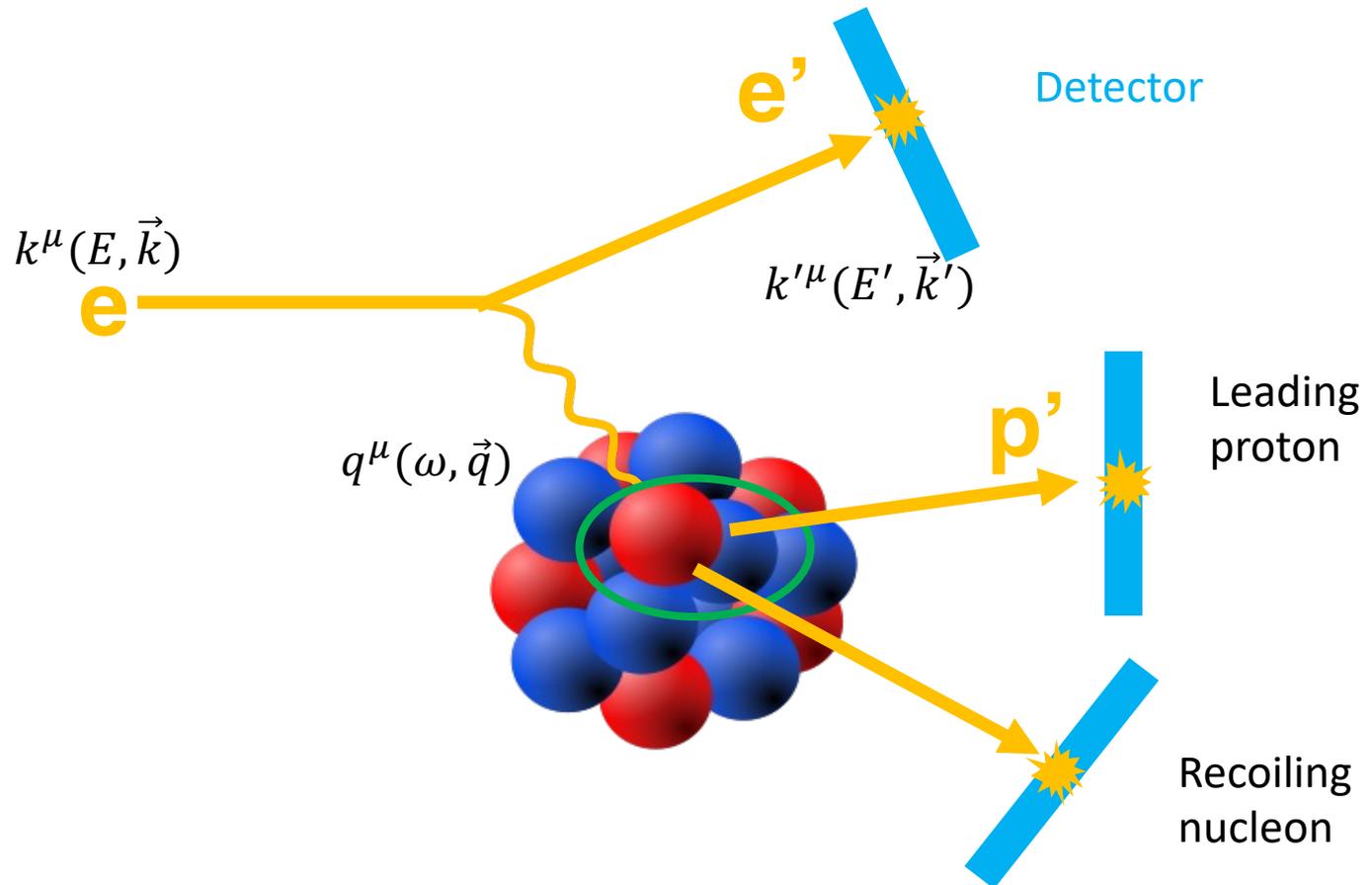
Hall D



Large acceptance detector

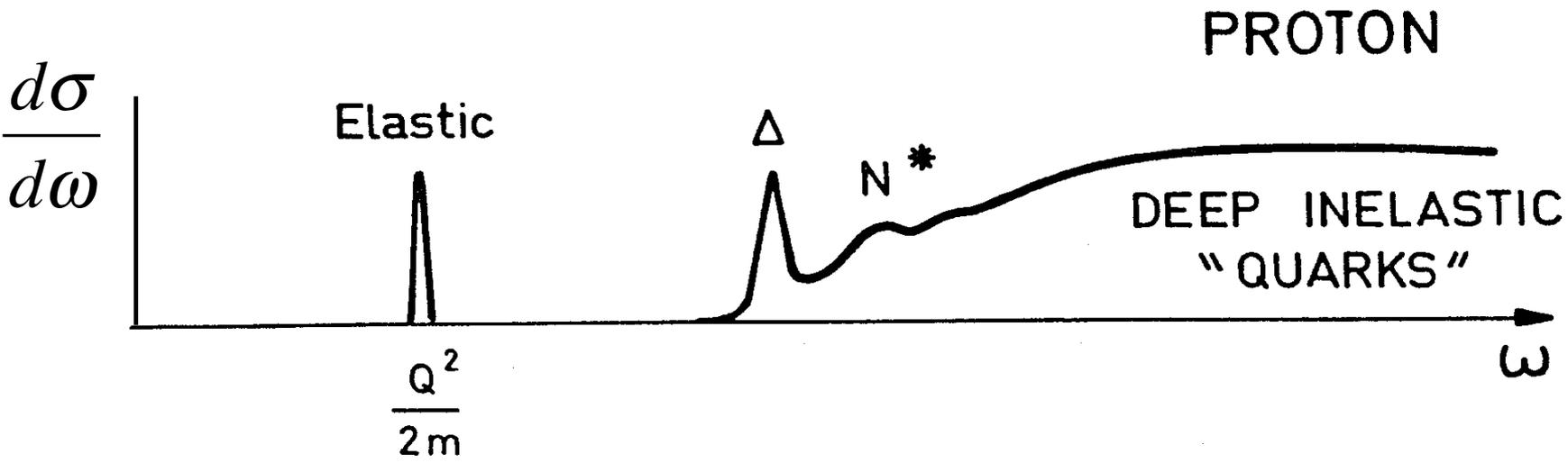


# How experimentalist study the reactions

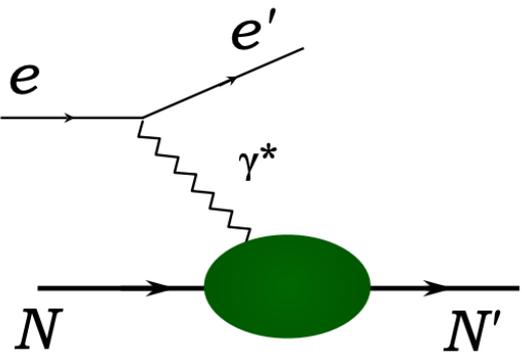


- $(e, e')$ : inclusive: Detect only scattering electron ( $e'$ )
- $(e, e'P)$ : Single knock out proton: Detect  $e'$  and knock-out proton
- $(e, e'NN)$ : Two knockout nucleons: Detect  $e'$  and two knock-out nucleon

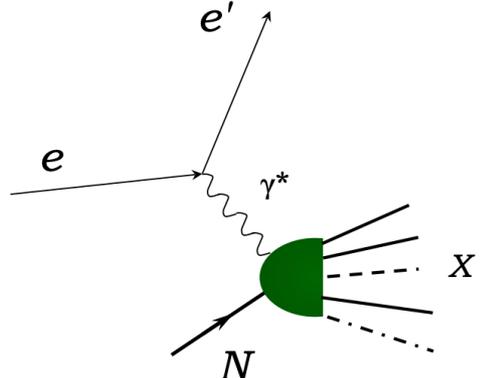
# Generic (e,e') at fixed momentum transfer



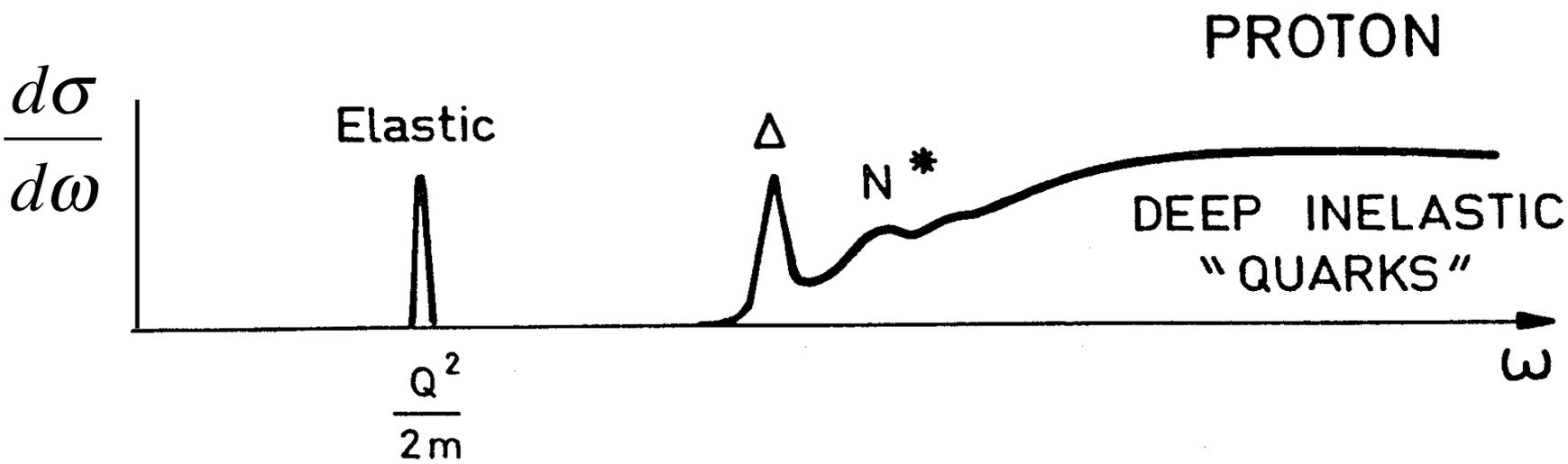
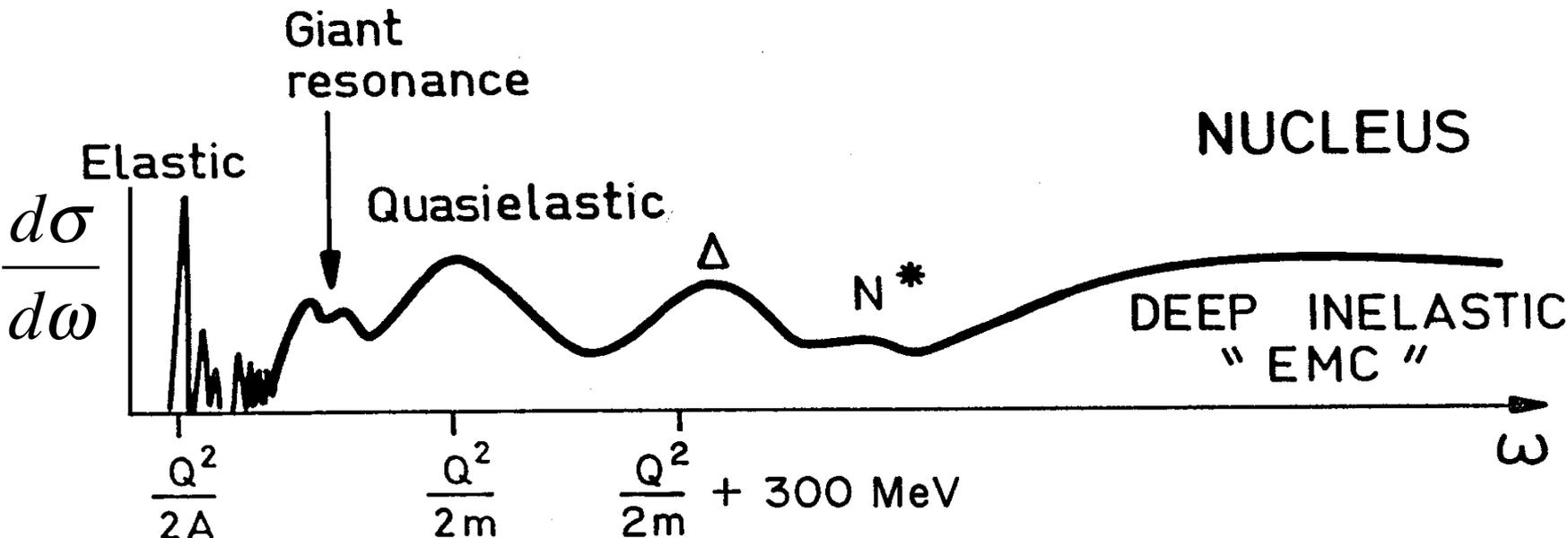
**Elastic scattering:**  
nucleon initial and final state the same



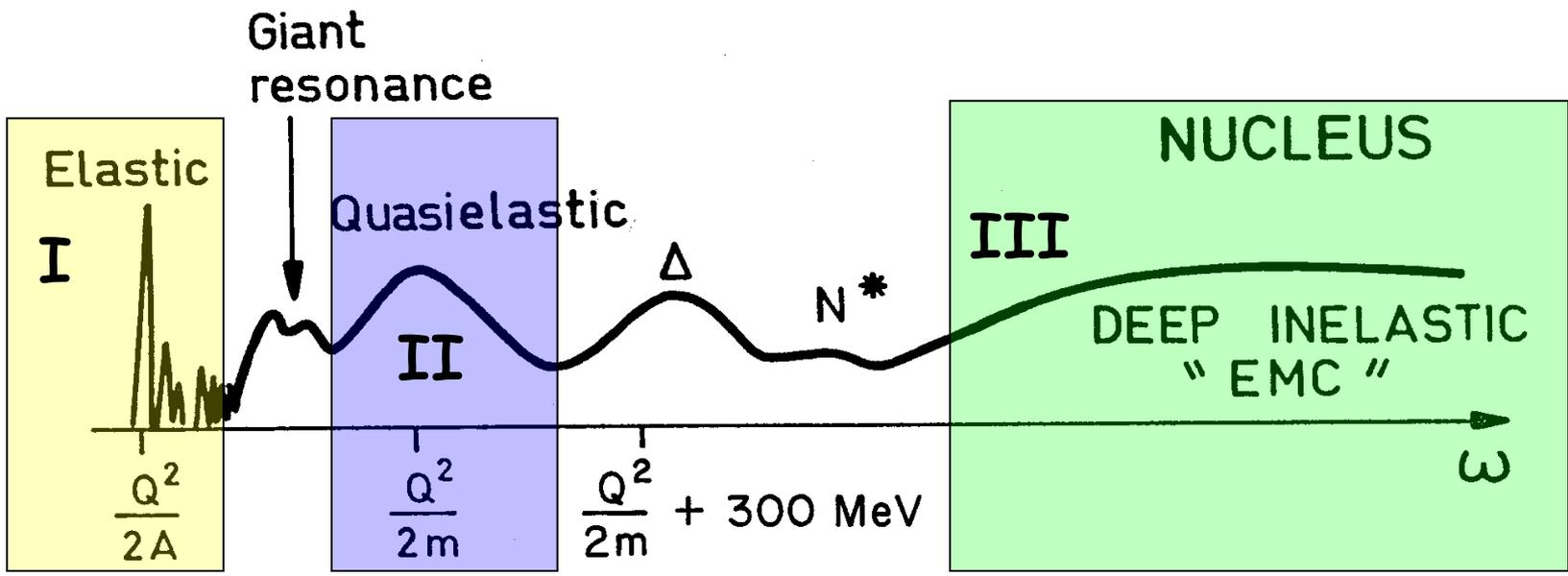
**Deep inelastic scattering:**  
nucleon state has changed, creates new particles



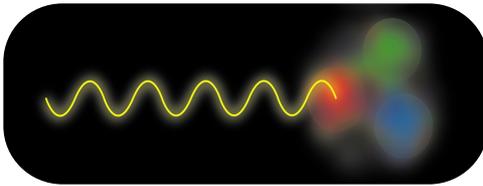
# Generic (e,e') at fixed momentum transfer



# Different reactions teach us different things



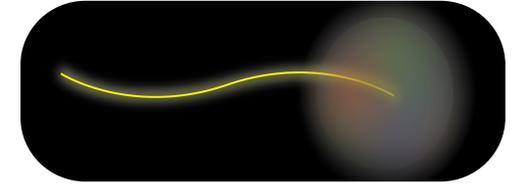
**Quasi-elastic:** electron scatters elastically off an almost free nucleon.



# What can we learn?

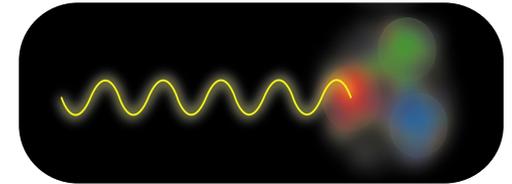
## 1. Elastic

- structure of the nucleon/nucleus
  - Form factors, charge distributions



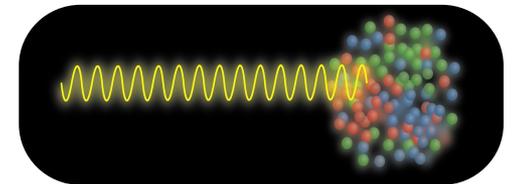
## 2. Quasi-elastic (QE)

- Shell structure
  - Momentum distributions
  - Occupancies
- Short Range Correlated nucleon pairs

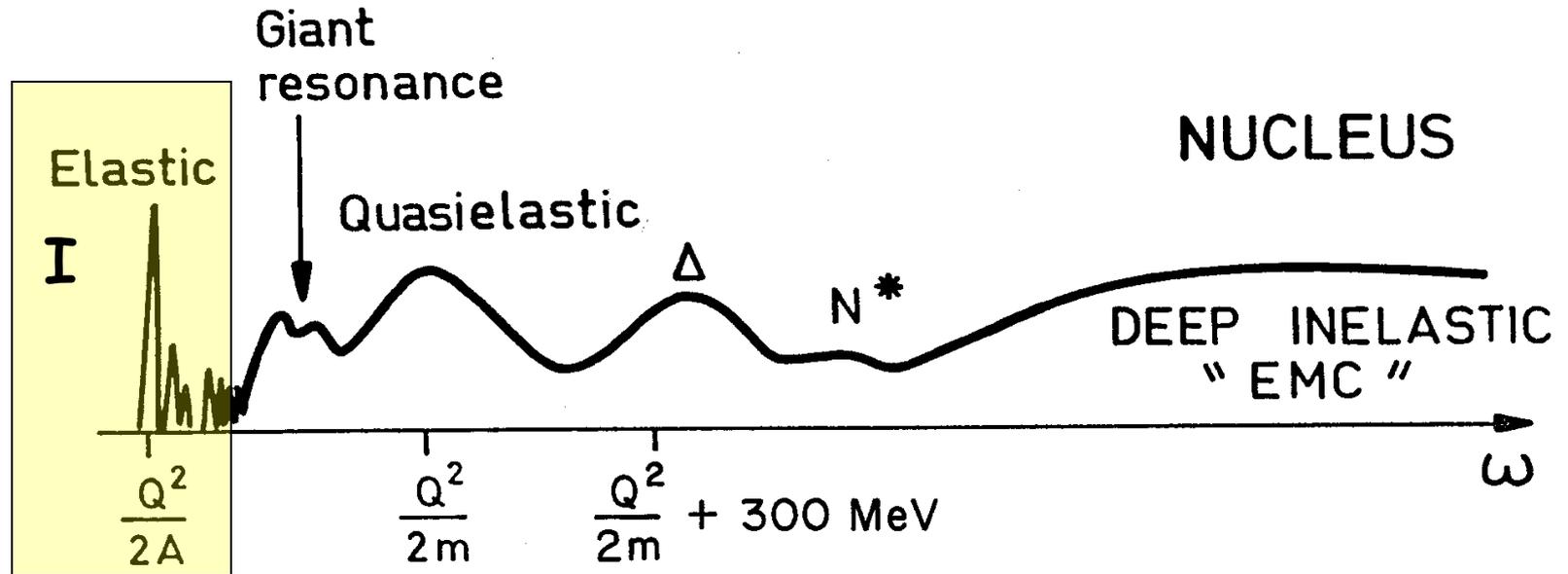


## 3. Deep Inelastic Scattering (DIS)

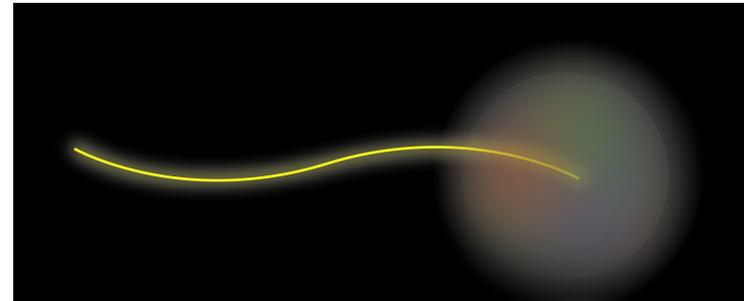
- The EMC Effect and Nucleon modification
- Quark Hadronization in nuclei



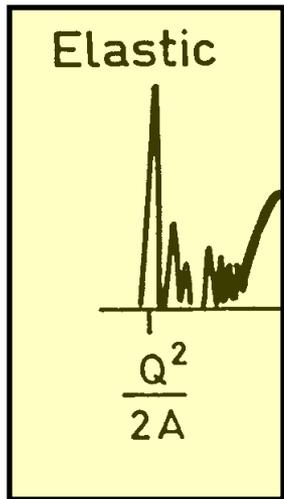
# Quick Overview: Elastic



- Elastic scattering
  - Charge distribution
  - Form Factors



# Elastic Electron Scattering: form factor



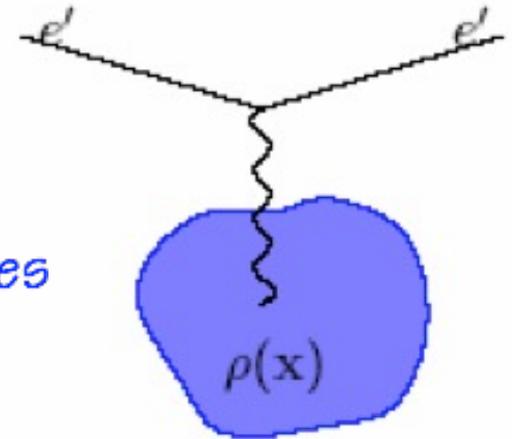
## Fermi's Golden Rule

$$\frac{d\sigma}{d\Omega} = \frac{2\pi}{\hbar} |M_{fi}|^2 D_f$$

$M_{fi}$ : scattering amplitude

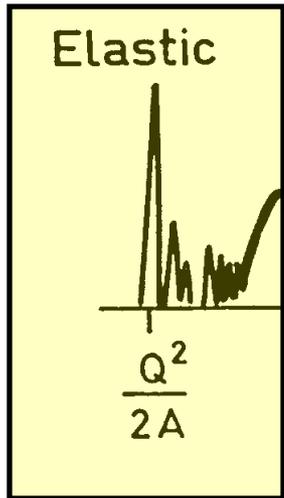
$D_f$ : density of the final states  
(or phase factor)

$$\begin{aligned} M_{fi} &= \int \Psi_f^* V(x) \Psi_i d^3x \\ &= \int e^{-k_f \cdot x} V(x) e^{-k_i \cdot x} d^3x \\ &= \int e^{iq \cdot x} V(x) d^3x \end{aligned}$$



Plane wave approximation for incoming and outgoing electrons  
Born approximation (interact only once)

# Elastic Electron Scattering: form factor



## Form Factor and Charge Distribution

Using Coulomb potential from a charge distribution,  $\rho(x)$ ,

$$V(x) = -\frac{Ze^2}{4\pi\epsilon_0} \int \frac{\rho(x')}{|x-x'|} d^3x'$$

$$\begin{aligned} M_{fi} &= -\frac{Ze^2}{4\pi\epsilon_0} \int e^{iq \cdot x} \int \frac{\rho(x')}{|x-x'|} d^3x' d^3x \\ &= -\frac{Ze^2}{4\pi\epsilon_0} \int e^{iqR} \left[ \int \frac{e^{iq \cdot x'} \rho(x')}{|R|} d^3x' \right] d^3R \\ &= -\frac{Ze^2}{4\pi\epsilon_0} \int \frac{e^{iqR}}{R} d^3R \int e^{iq \cdot x'} \rho(x') d^3x' \end{aligned}$$

$$F(q) = \int e^{iq \cdot x'} \rho(x') d^3x'$$

Charge form factor  $F(q)$  is the **Fourier transform** of the charge distribution  $\rho(x)$

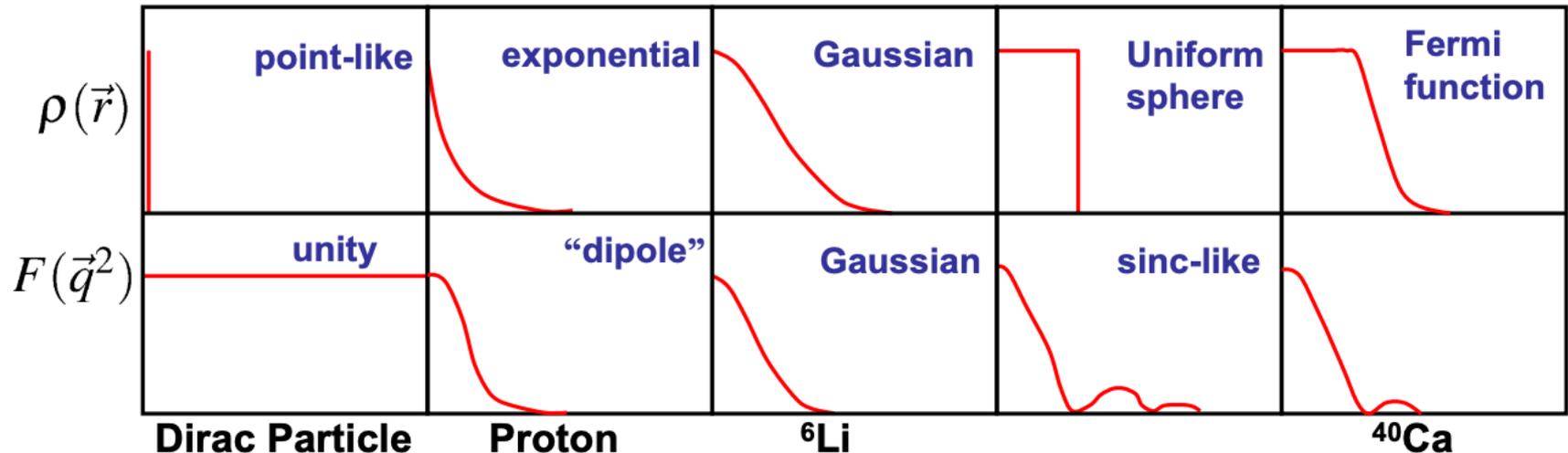
# Elastic scattering: Form factors

Mott cross section:

- Scattering from point-like object
- Target recoil neglected
- Scattered particle relativistic ( $E \gg m_e$ )

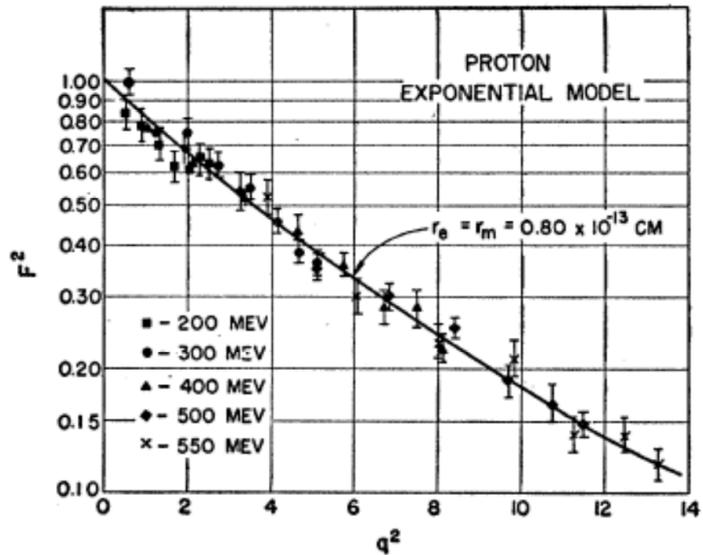
$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \rightarrow \underbrace{\frac{\alpha^2}{4E^2 \sin^4 \theta/2}}_{\text{Mott XS}} \underbrace{\cos^2 \frac{\theta}{2} |F(\vec{q}^2)|^2}_{\text{FF}}$$

$$F(\vec{q}^2) = \int \rho(\vec{r}) e^{i\vec{q} \cdot \vec{r}} d^3\vec{r}$$



# Elastic scattering: Form factors

Elastic e-p scattering



Robert Hofstadter, Nobel prize in physics 1961

For his pioneering studies of electron scattering in atomic nuclei and for his thereby achieved discovery concerning the structure of nucleons

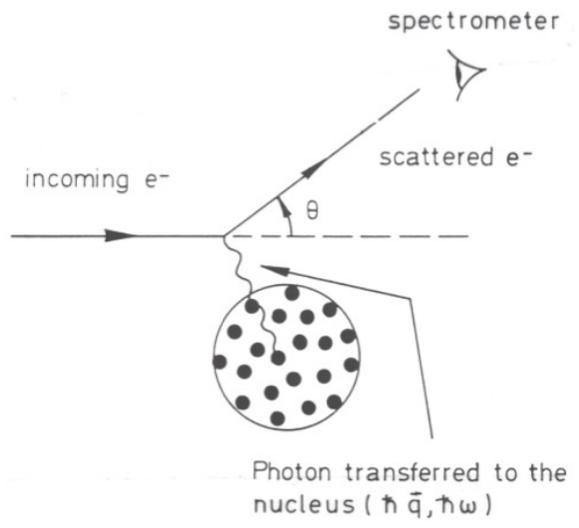
**Proton is not a point-like particle but has finite size!**

**Form factors  $\rightarrow$  charge distributions**

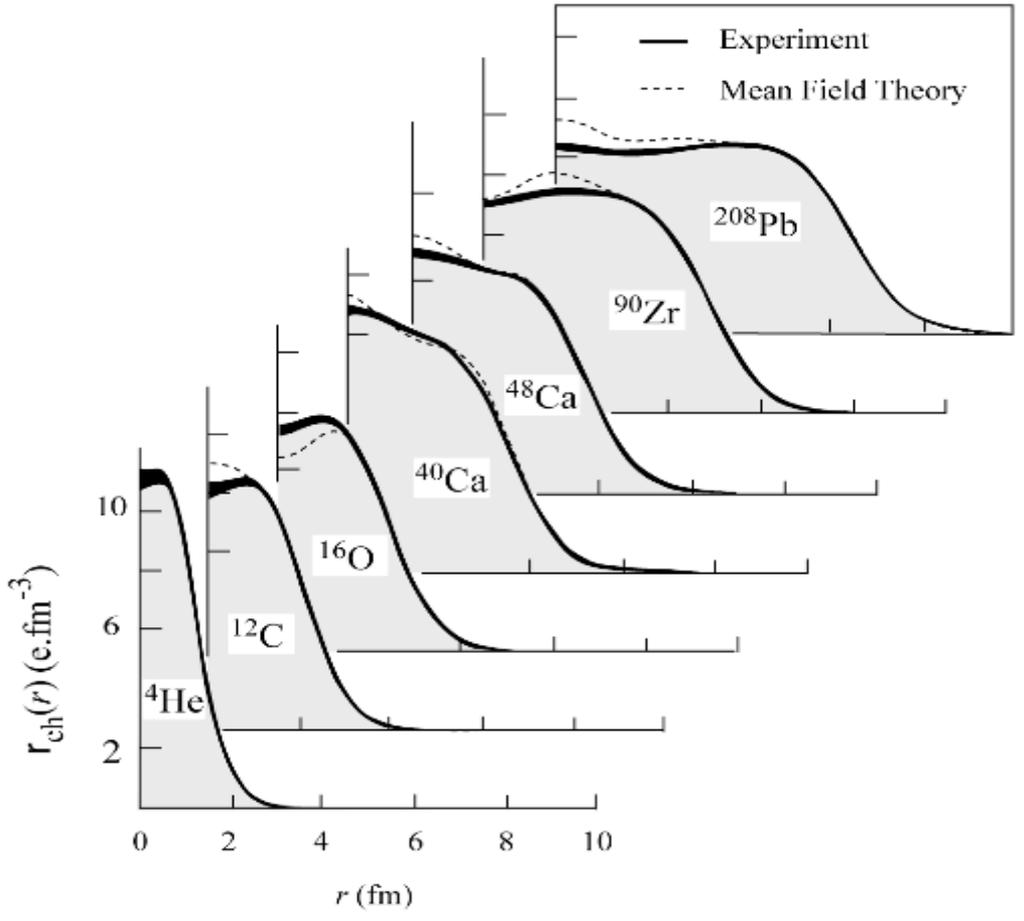
# Elastic (e,e') Scattering

## Cross-section $\Rightarrow$ Charge distributions

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{mott} |F(q)|^2$$



**Charge Distribution,  $r_{ch}(r)$ , is a Fourier Transform of the Charge Form Factor,  $F(q)$**



# Proton recoiling and finite size

Elastic scattering (relativistic) from a point-like Dirac proton:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E_1^2 \sin^4 \theta / 2} \frac{E_3}{E_1} \left( \underbrace{\cos^2 \frac{\theta}{2}}_{\text{Rutherford}} - \underbrace{\frac{q^2}{2M^2} \sin^2 \frac{\theta}{2}}_{\text{Proton recoil}} \right)$$

Rutherford
Proton recoil
Electric/  
Magnetic  
scattering
Magnetic term  
due to spin

But the proton is not point-like!

The finite size of the proton accounted for by 2 form factors:

- Charge distribution described by  $G_E(q^2)$
- Magnetic moment distribution described by  $G_M(q^2)$

Rosenbluth Formula:

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E_1^2 \sin^4 \theta / 2} \frac{E_3}{E_1} \left( \frac{G_E^2 + \tau G_M^2}{(1 + \tau)} \cos^2 \frac{\theta}{2} + 2\tau G_M^2 \sin^2 \frac{\theta}{2} \right)$$

# Descriptions of the proton

Recall, the Mott XS:  $\sigma_M = \frac{\alpha^2 \cos^2 \left( \frac{\theta_e}{2} \right)}{4E^2 \sin^4 \left( \frac{\theta_e}{2} \right)}$

$$\begin{aligned} \frac{d\sigma}{d\Omega} &= \underbrace{\sigma_M}_{\text{Recoil factor}} \underbrace{\left( \frac{E'}{E} \right)}_{\text{Form factors}} \left\{ \left[ F_1^2(Q^2) + \frac{Q^2}{4M^2} \kappa^2 F_2^2(Q^2) \right] + \frac{Q^2}{2M^2} [F_1(Q^2) + \kappa F_2(Q^2)]^2 \tan^2 \frac{\theta}{2} \right\} \\ &= \sigma_M \left( \frac{E'}{E} \right) \left[ \frac{G_E^2(Q^2) + \tau G_M^2(Q^2)}{1 + \tau} + 2\tau \tan^2 \frac{\theta}{2} G_M^2(Q^2) \right] \\ &= \sigma_M \left( \frac{E'}{E} \right) \left[ \frac{Q^4}{\vec{q}^4} R_L(Q^2) + \left( \frac{Q^2}{2\vec{q}^2} + \tan^2 \frac{\theta}{2} \right) R_T(Q^2) \right] \end{aligned}$$

Nucleon Form Factors

- $F_1, F_2$ : Dirac and Pauli form factors
- $G_E, G_M$ : Sachs form factors (electric and magnetic)
  - $G_E(Q^2) \equiv F_1(Q^2) - \tau \kappa F_2(Q^2)$
  - $G_M(Q^2) \equiv F_1(Q^2) + \kappa F_2(Q^2)$
- $R_L, R_T$ : Longitudinal and transverse response fn

where  $\tau \equiv \frac{Q^2}{4M_N^2}$ ,  $\kappa$  is the anomalous magnetic moment

# Measuring the form factors

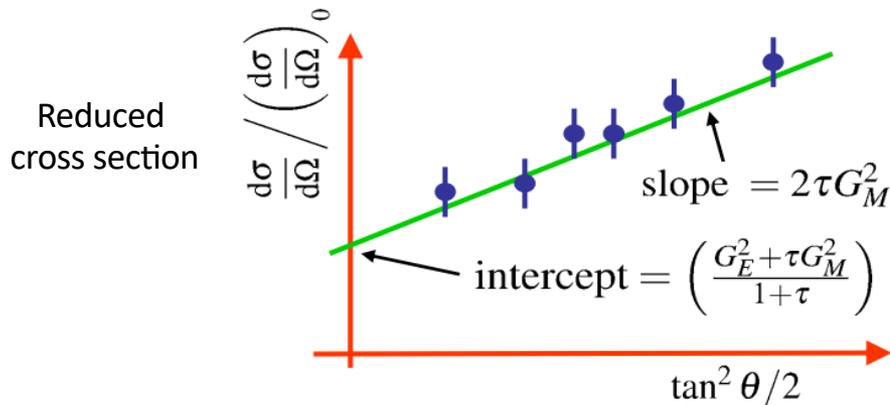
We can rewrite the cross section as:

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_0 \left( \frac{G_E^2 + \tau G_M^2}{(1 + \tau)} + 2\tau G_M^2 \tan^2 \frac{\theta}{2} \right)$$

Where we have the Mott cross section including the proton recoil as:

$$\left(\frac{d\sigma}{d\Omega}\right)_0 = \frac{\alpha^2}{4E_1^2 \sin^4 \theta/2} \frac{E_3}{E_1} \cos^2 \frac{\theta}{2}$$

Experimentally, we can study the angular dependence of the cross section at fixed  $Q^2$



Rosenbluth separation, technique:  
note the sensitivity is to the squares of the FFs

# Charge Radius of the Proton using e-p elastic scattering

- For the proton we make use of the fact that as  $Q^2$  goes to zero the charge radius is proportional to the slope of  $G_E$

$$G_E(Q^2) = 1 + \sum_{n \geq 1} \frac{(-1)^n}{(2n + 1)!} \langle r^{2n} \rangle Q^{2n}$$

$$r_p \equiv \left( -6 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2=0} \right)^{1/2}$$

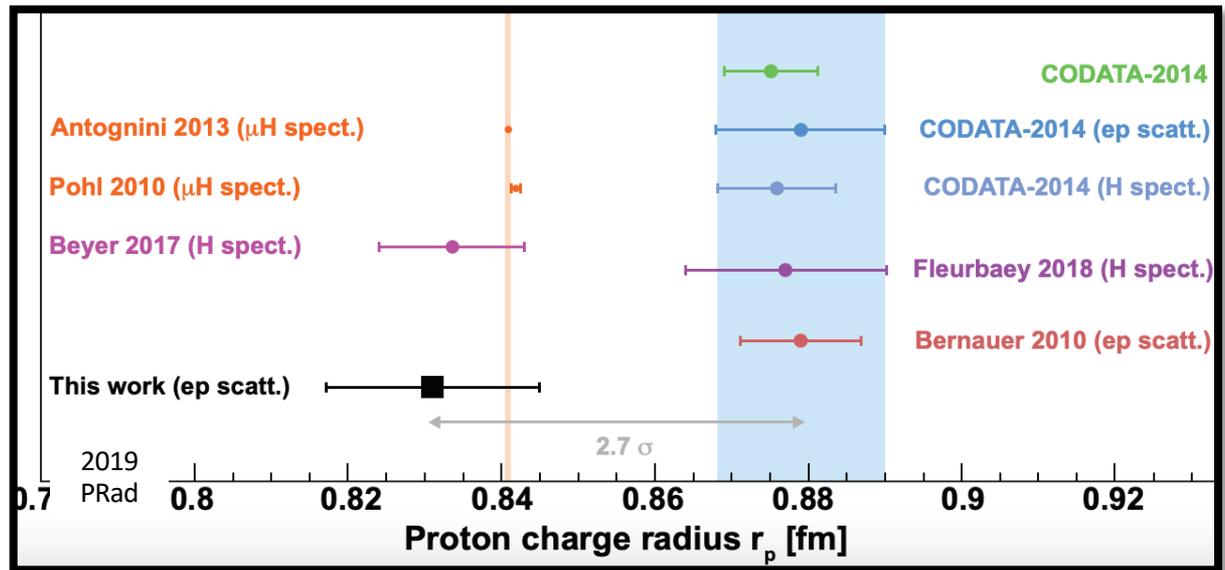
This definition of  $r_p$  has been shown to be consistent with the radius extracted from the muonic hydrogen data.

# Determining the proton charge radius



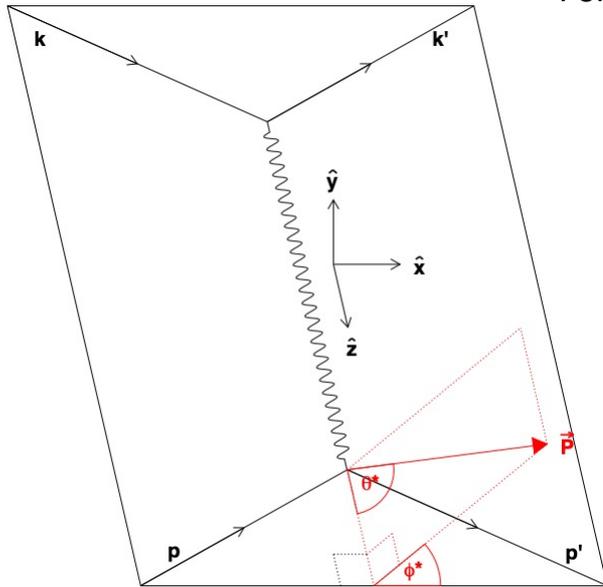
- Atomic Hydrogen Lamb Shift (  $\sim 0.88$  fm )
- Muonic Hydrogen Lamb Shift (  $\sim 0.84$  fm )
- Elastic electron scattering!

While the proton radius definition is the same whether done on muonic hydrogen or elastic electron-proton scattering, there is a historical division amongst the results.



# Form factors: polarization measurement

Longitudinally polarized beam and measuring the polarization transferred to the recoiling nucleon



Polarization transfer:  $\vec{e}N \rightarrow e\vec{N}$  or spin-target asymmetry:  $\vec{e}\vec{N} \rightarrow eN$ ,

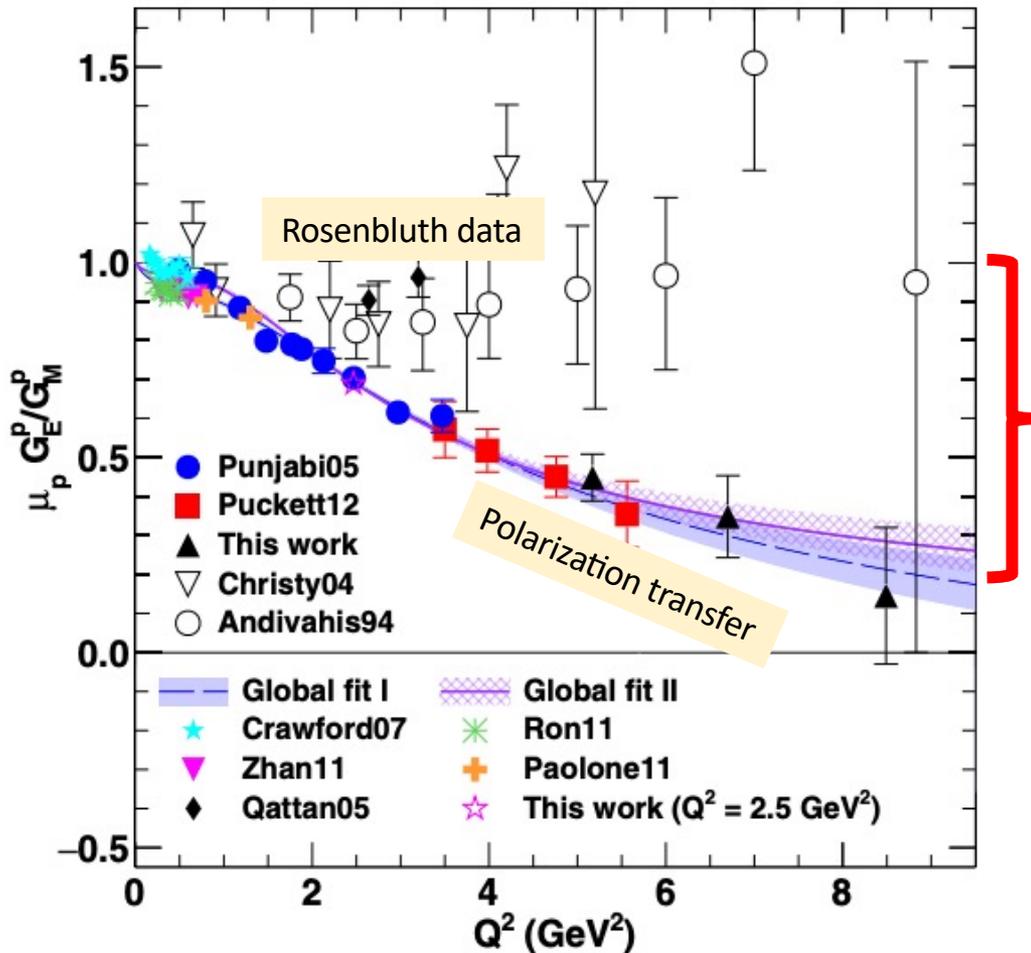
$$P_t = -hP_e \sqrt{\frac{2\epsilon(1-\epsilon)}{\tau}} \frac{G_E G_M}{G_M^2 + \frac{\epsilon}{\tau} G_E^2},$$

$$P_\ell = hP_e \sqrt{1-\epsilon^2} \frac{G_M^2}{G_M^2 + \frac{\epsilon}{\tau} G_E^2},$$

$$\frac{G_E}{G_M} = -\frac{P_t}{P_\ell} \sqrt{\frac{\tau(1+\epsilon)}{2\epsilon}} = -\frac{P_t}{P_\ell} \frac{E_e + E'_e}{2M} \tan\left(\frac{\theta_e}{2}\right)$$

Enhanced sensitivity to the ratio  $\rightarrow$   
increased sensitivity to  $G_E$  for large  $Q^2$  and  $G_M$  for small  $Q^2$

# Form factor ratio



Puckett et al., PRC 96, 055203 (2017)

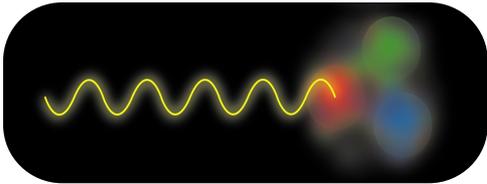
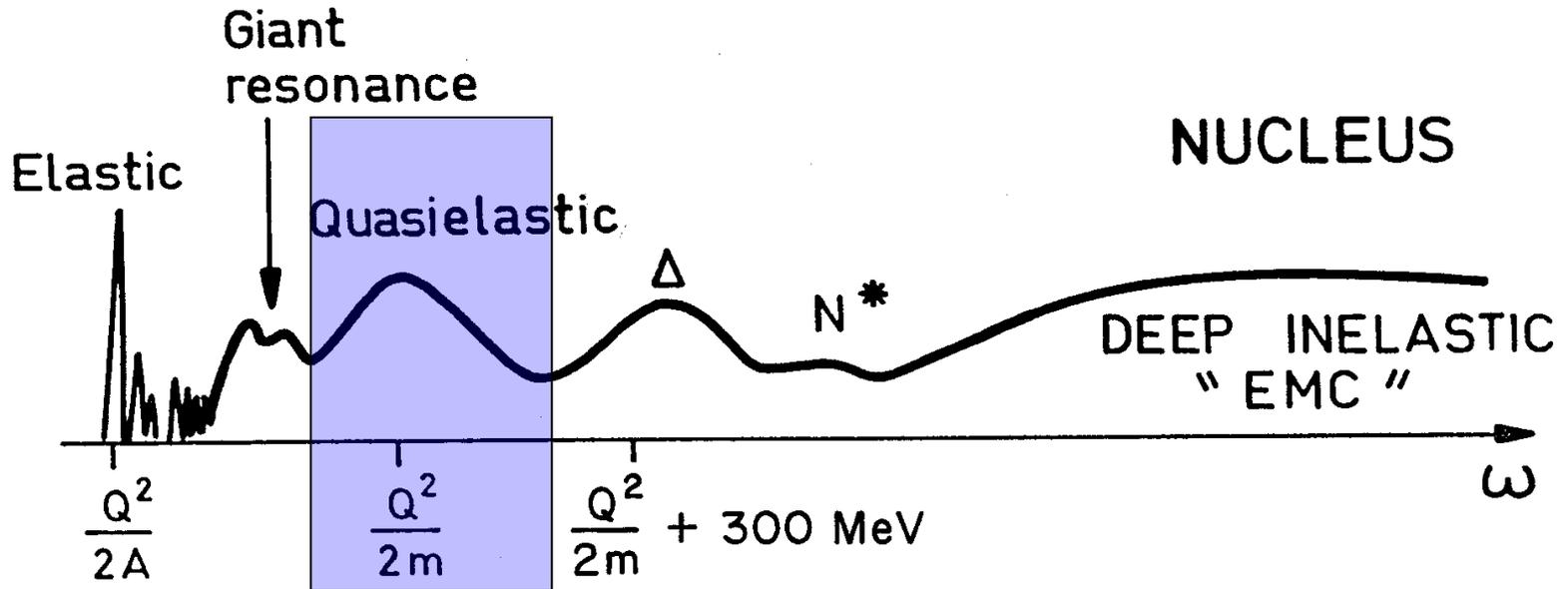
Large discrepancy between Rosenbluth-extracted data and polarization transfer measurements!

Two photon exchange correction neglected in Rosenbluth data is significant to the radiative corrections.

# Elastic scattering summary

- We can measure things like the charge and magnetic moment distributions of the nucleons.
- These are described in terms of form factors (a Fourier transformation of the distributions).
- We can use form factors to extract the radius.
- This tells us about the structure of nucleons and nuclei.
- Nucleons are not point-like!

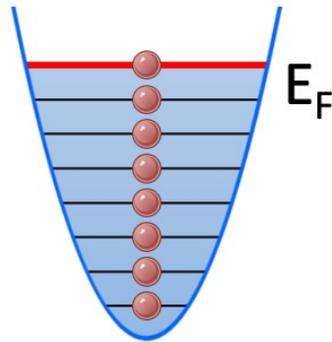
# Quick overview: Quasi-elastic scattering



- Shell structure
  - Momentum distributions
  - Occupancies
- Short Range Correlated nucleon pairs

# Effective descriptions of the nucleus

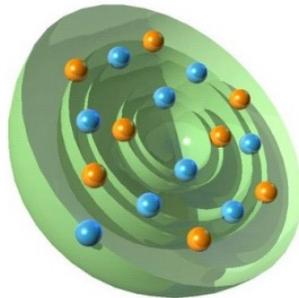
Fermi  
Gas  
Model



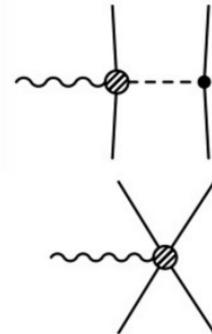
Liquid  
Drop  
Model



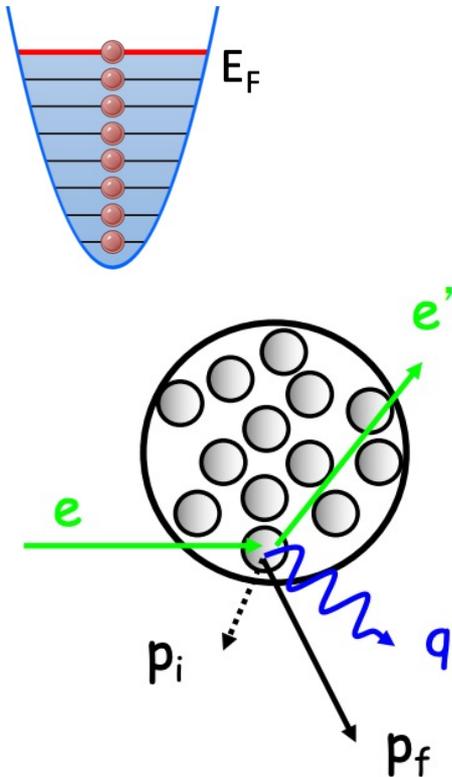
Shell  
Model



Chiral  
Perturbation  
Theory\*



# The nucleus as a Fermi gas



Initial nucleon energy:  $KE_i = p_i^2 / 2m_p$

Final nucleon energy:  $KE_f = p_f^2 / 2m_p = (\vec{q} + \vec{p}_i)^2 / 2m_p$

Energy transfer:  $\nu = KE_f - KE_i = \frac{\vec{q}^2}{2m_p} + \frac{\vec{q} \cdot \vec{p}_i}{m_p}$

We can expect:

peak centroid of  $\nu = q^2/2m_p + \epsilon$

peak width is  $2qp_{\text{fermi}}/m_p$

Total peak cross section would be  $Z\sigma_{\text{ep}} + N\sigma_{\text{en}}$

Good approximation of the cross section, but not descriptive of structure.

# Early 1970s quasielastic data

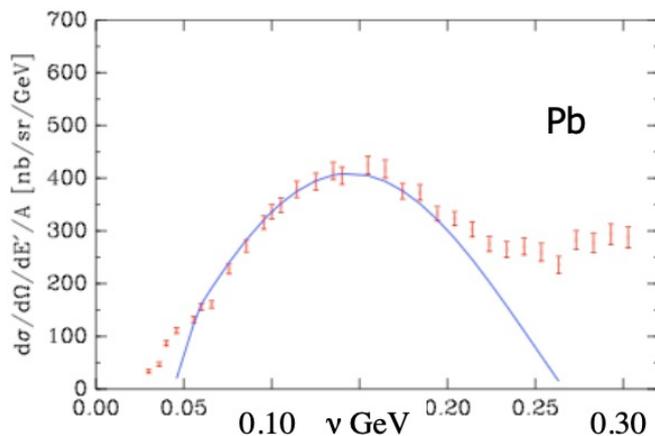
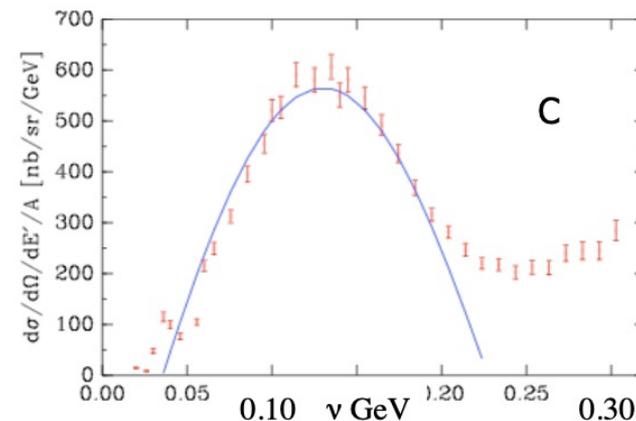
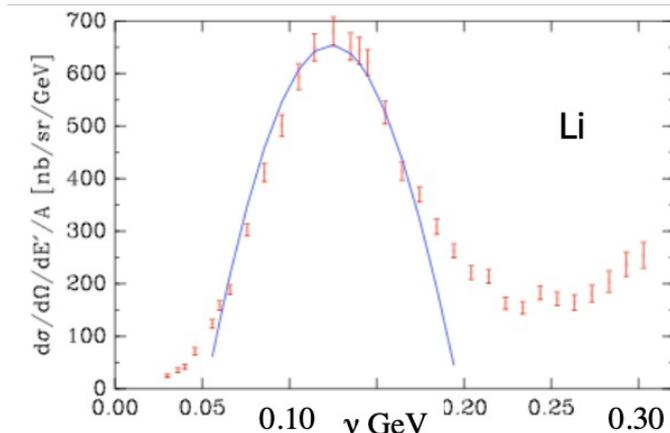
500 MeV, 60 deg  
 $q \approx 500$  MeV/c

R.R. Whitney et al, PRC 9, 2230 (1974).

Width  $\sim k_F$   
 (Fermi momentum)

Mean  $\sim \bar{\epsilon}$   
 (separation energy)

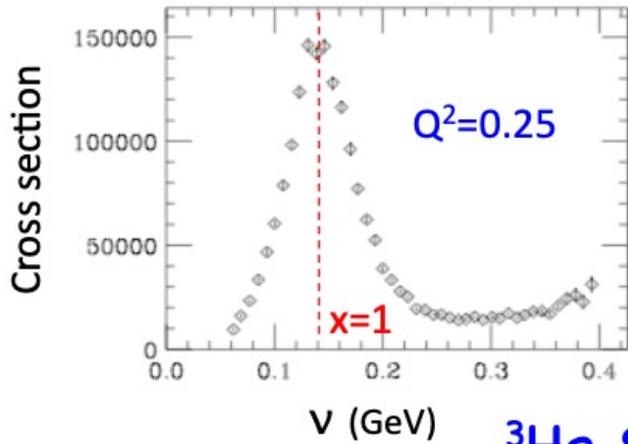
- Peak broadens with increasing A



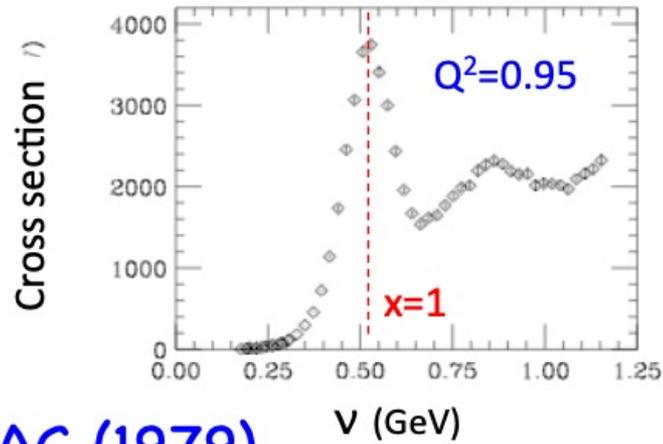
Nucleus	$k_F$ MeV/c	$\bar{\epsilon}$ MeV
${}^6\text{Li}$	169	17
${}^{12}\text{C}$	221	25
${}^{24}\text{Mg}$	235	32
${}^{40}\text{Ca}$	251	28
<i>nat</i> Ni	260	36
${}^{89}\text{Y}$	254	39
<i>nat</i> Sn	260	42
${}^{181}\text{Ta}$	265	42
${}^{208}\text{Pb}$	265	44

compared to Fermi model: fit parameter  $k_F$  and  $\bar{\epsilon}$

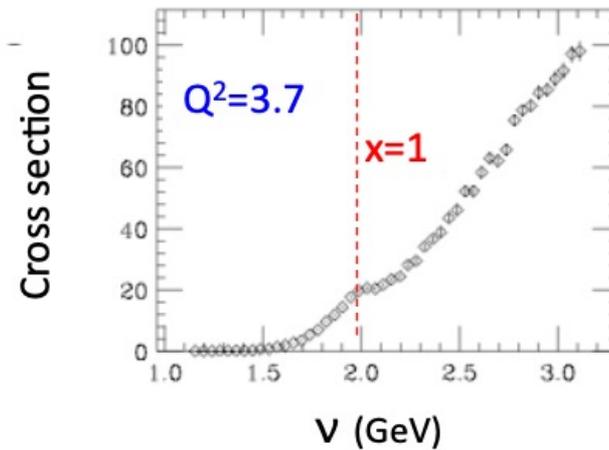
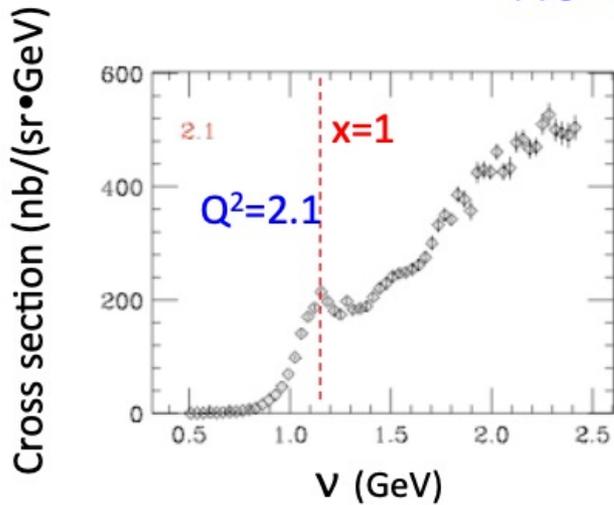
# Quasielastic peak



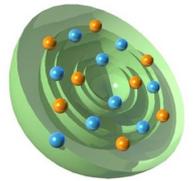
$^3\text{He}$  SLAC (1979)



Inelastic scattering begins to dominate at  $Q^2 \gg 1 \text{ GeV}^2$



# Independent particle shell model

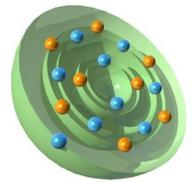


$$H = \underbrace{[T + V_M]}_{\text{IPSM}} + \underbrace{[V_{2\text{-body}} + V_{3\text{-body}} + \dots - V_M]}_{\text{neglected in IPSM}}.$$

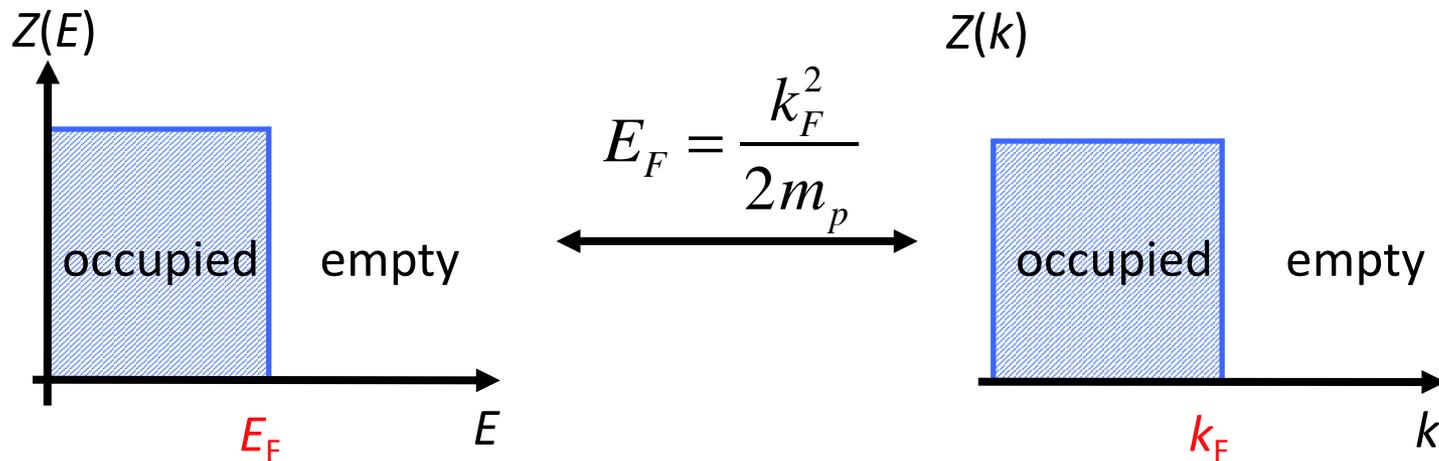
## Assumptions:

- ❑ Nucleon moves in a mean-field created by surrounding nucleons
- ❑ No interaction at a short distance
- ❑ Nucleons fill up distinct energy level defined by quantum numbers, highest energy level is called Fermi-energy, corresponding to Fermi-momentum

# Independent particle shell model



$$H = \underbrace{[T + V_M]}_{\text{IPSM}} + \underbrace{[V_{2\text{-body}} + V_{3\text{-body}} + \dots - V_M]}_{\text{neglected in IPSM}}.$$

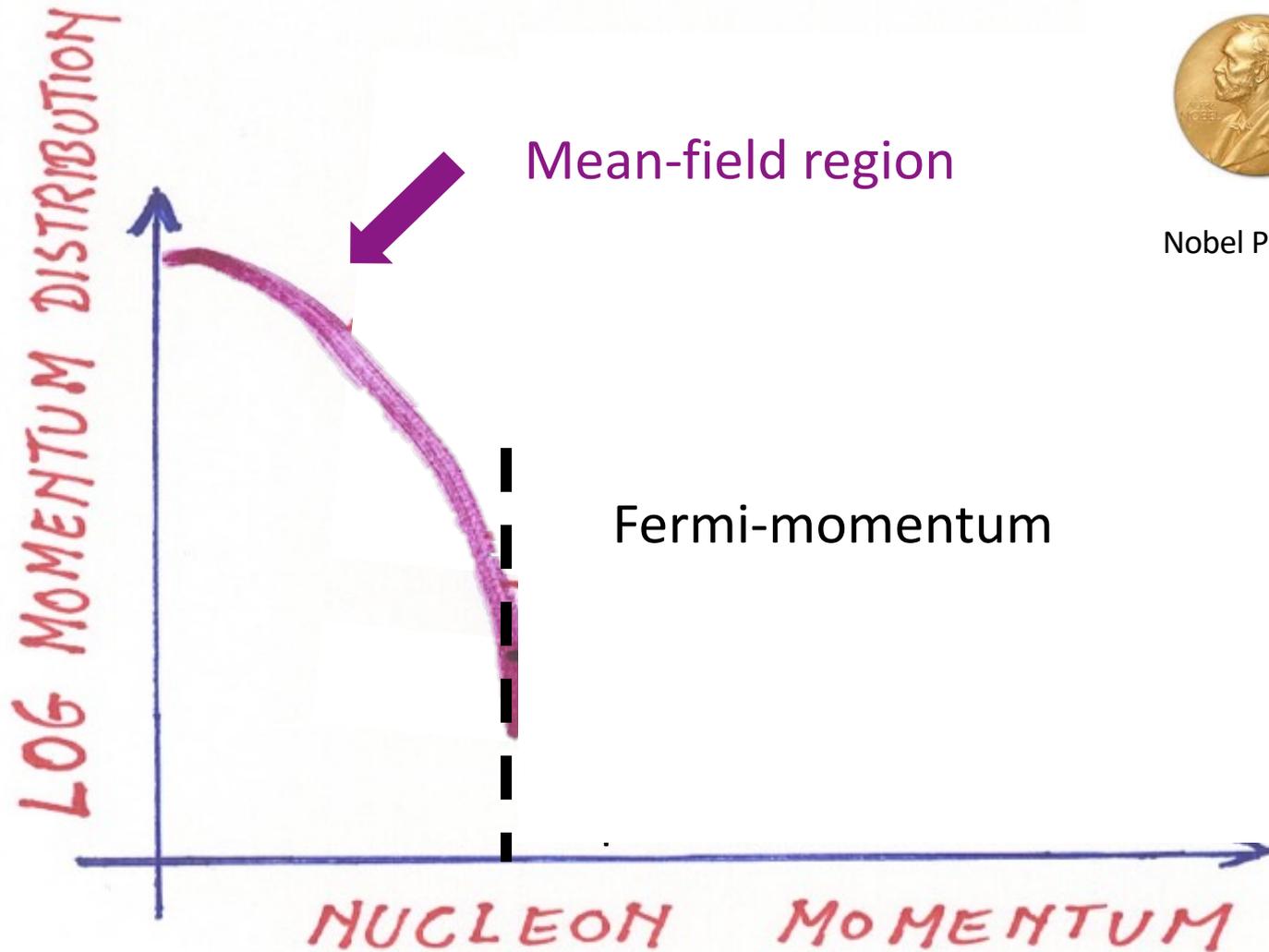


## Pauli's principle:

- Forbids nucleon scattering to occupied shell: Suppressed the nucleon interaction

- Ground state energies
- Excitation Spectrum
- Spins
- Parities
- ...

# Momentum distribution:



Nobel Prize 1963

# (e,e'p) Plane Wave Impulse Approximation (PWIA)

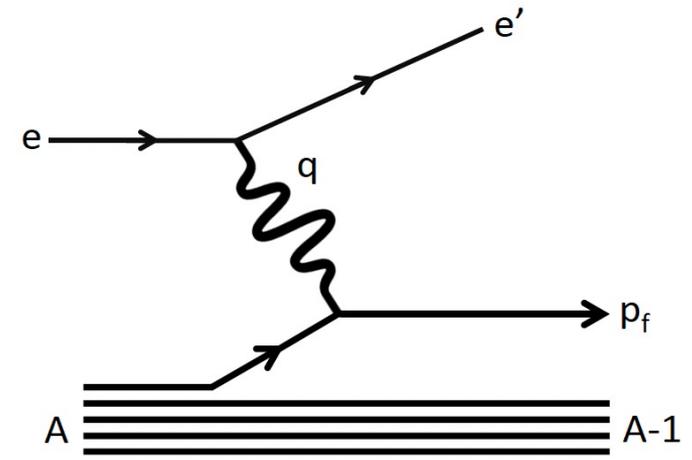
1. Only one nucleon absorbs the virtual photon
2. That nucleon does not interact further
3. That nucleon is detected

- Missing energy,  $E_m = \nu - T_{pf} - T_{A-1}$
- Missing momentum,  $p_m = q - p_f$

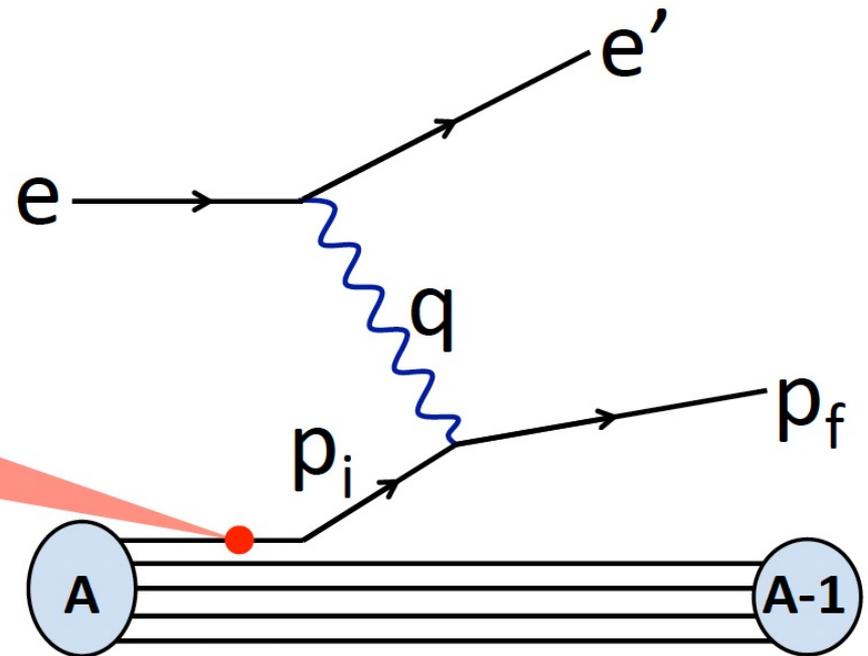
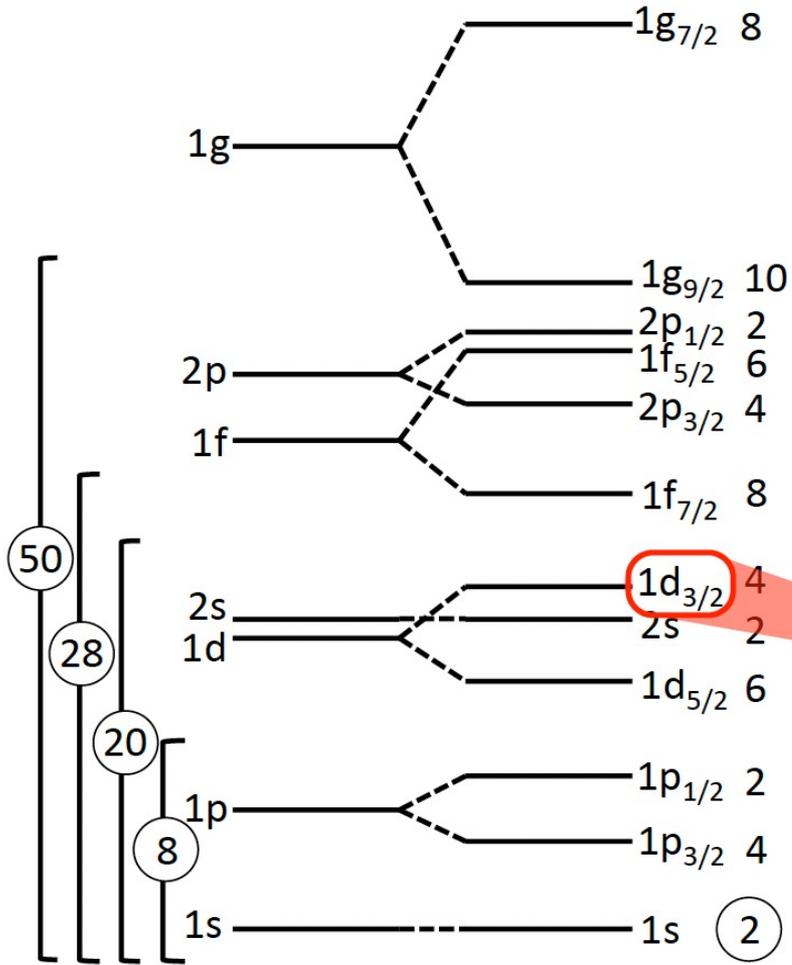
PWIA implies:  $p_i = -p_m$ ,  $|E| = E_m$

Cross-section factorization

$$\sigma = K \sigma_{ep} S(|\vec{P}_i|, E_i)$$

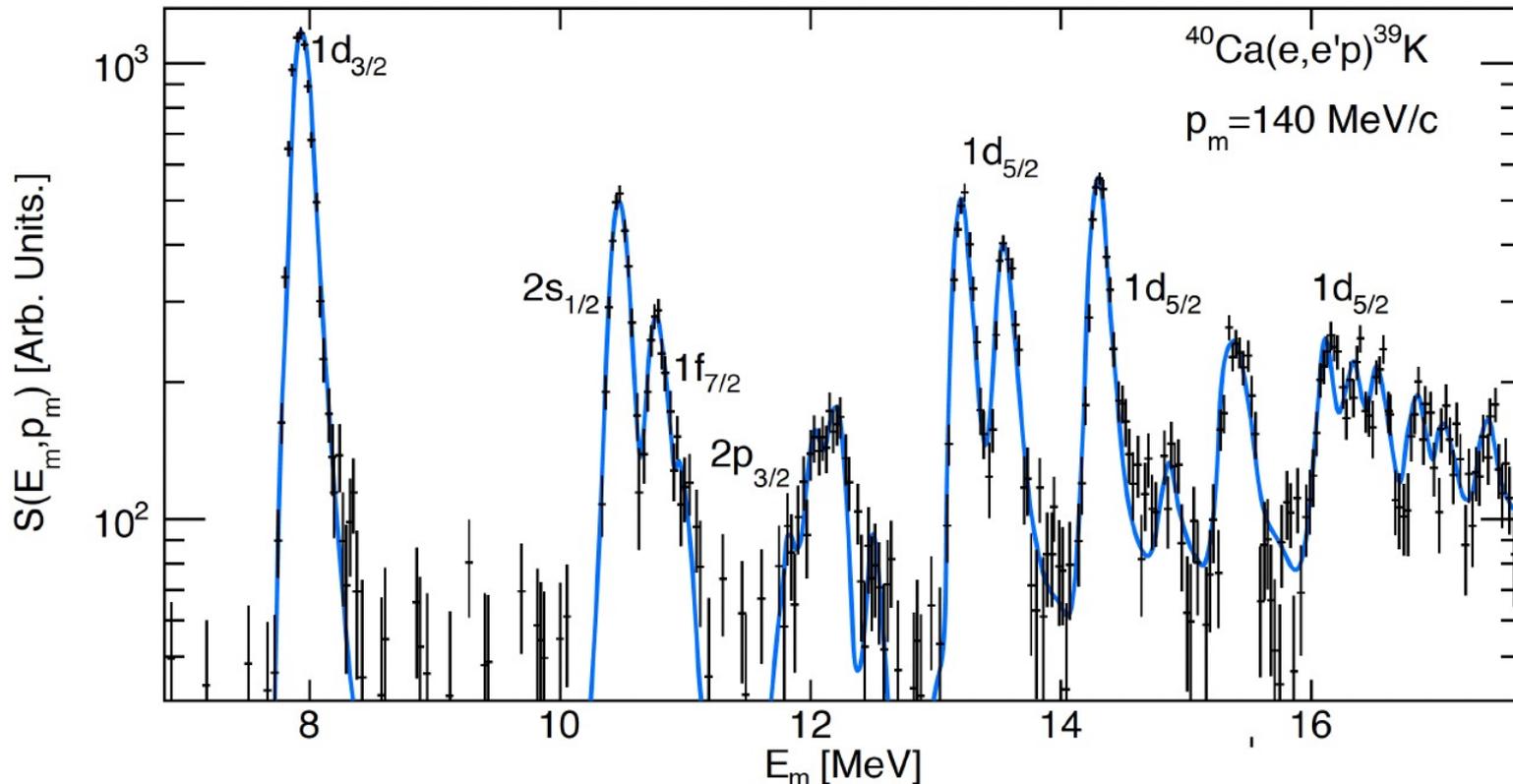


# (e,e'p) scattering off shell orbitals



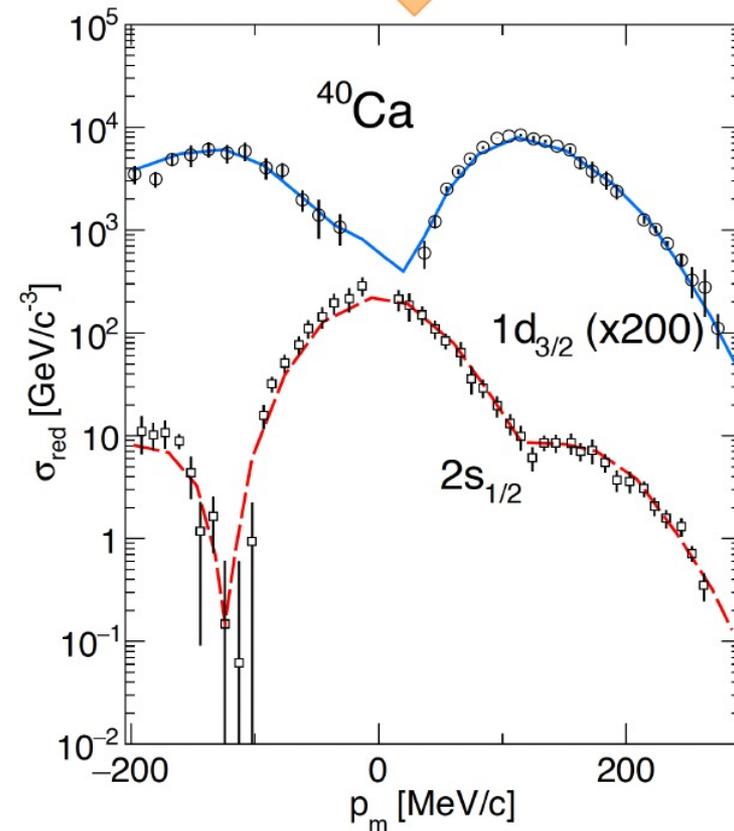
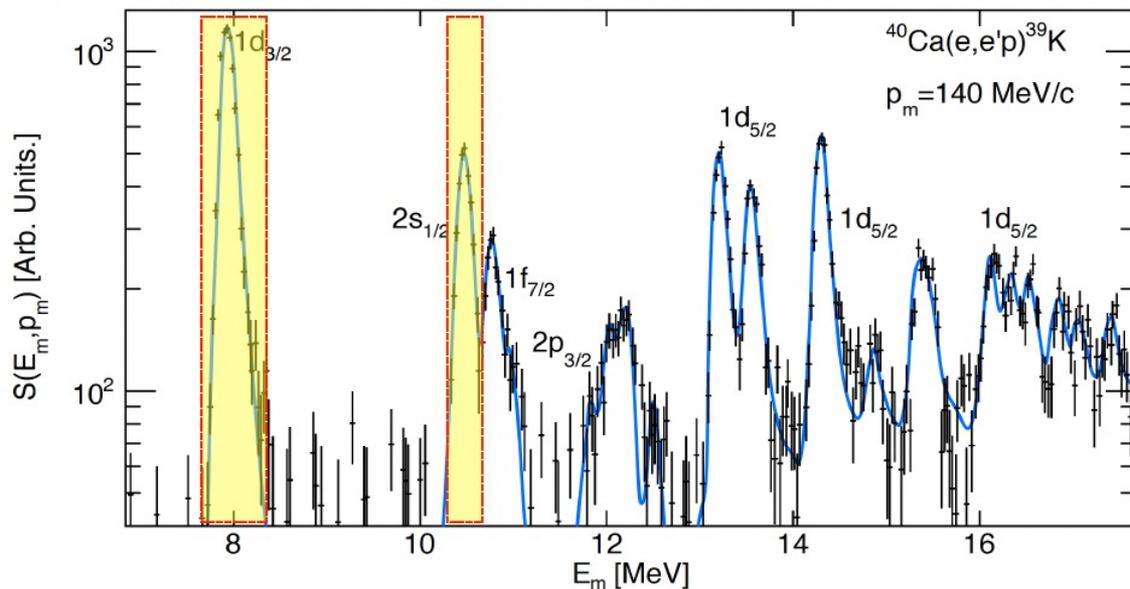
# (e,e'p) scattering off shell orbitals

The missing energy spectrum shows shells occupancy



L. Lapikas, Nuclear Phys. A553, 297c (1993)

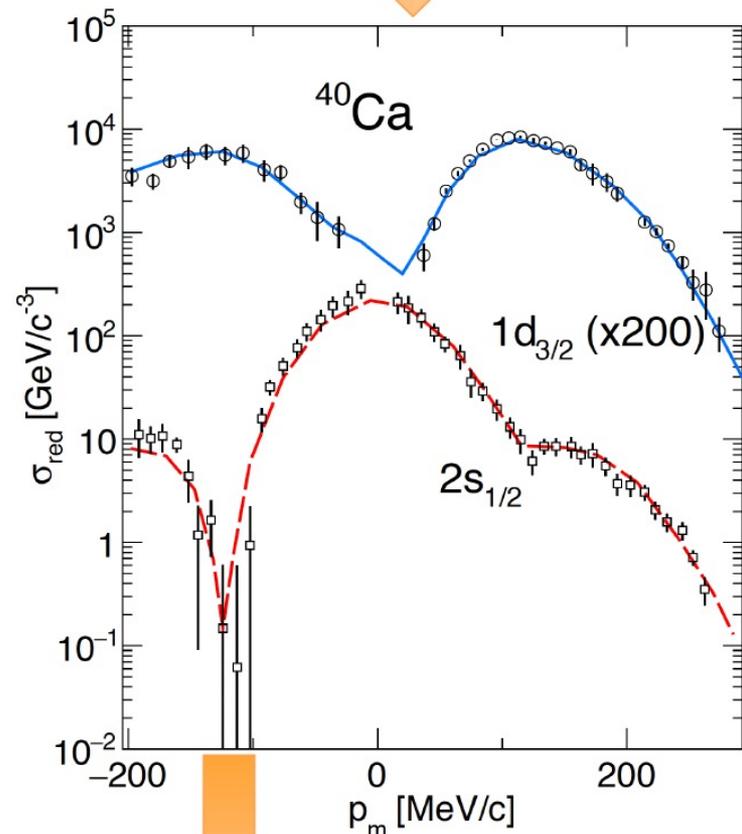
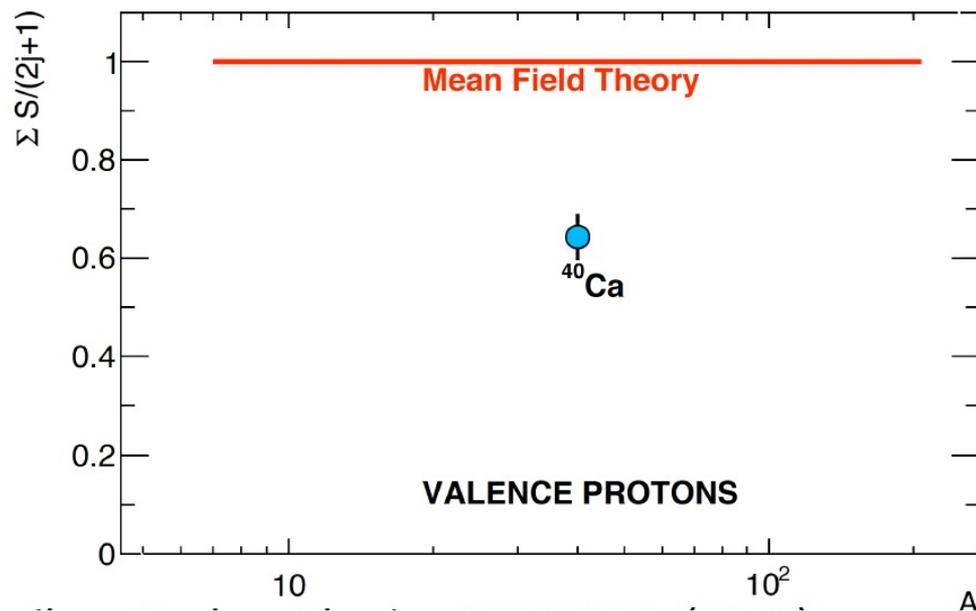
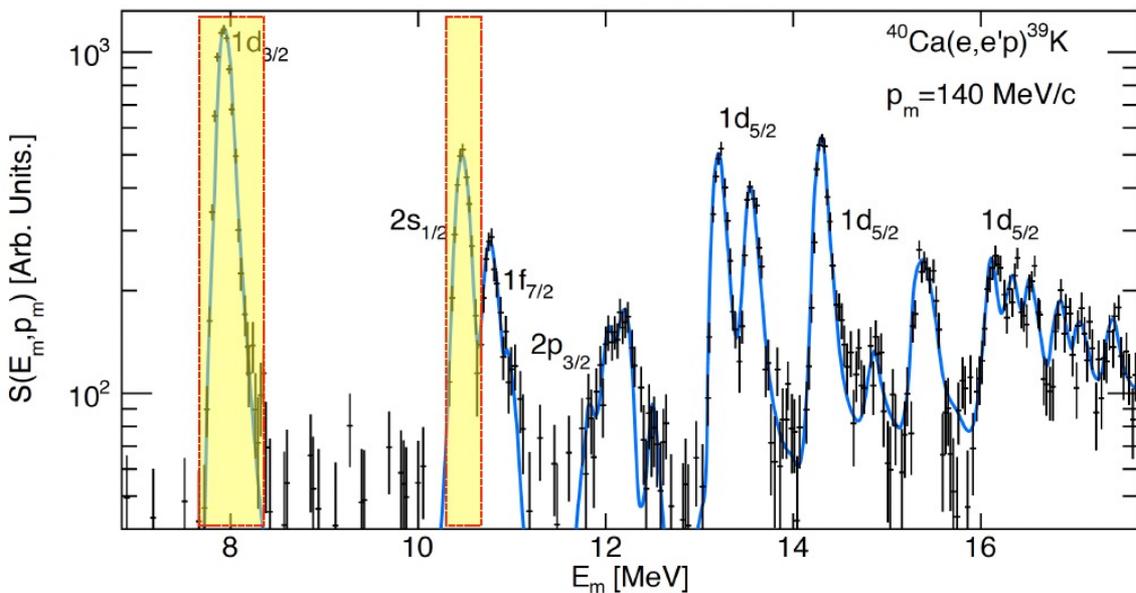
# (e,e'p) scattering off shell orbitals



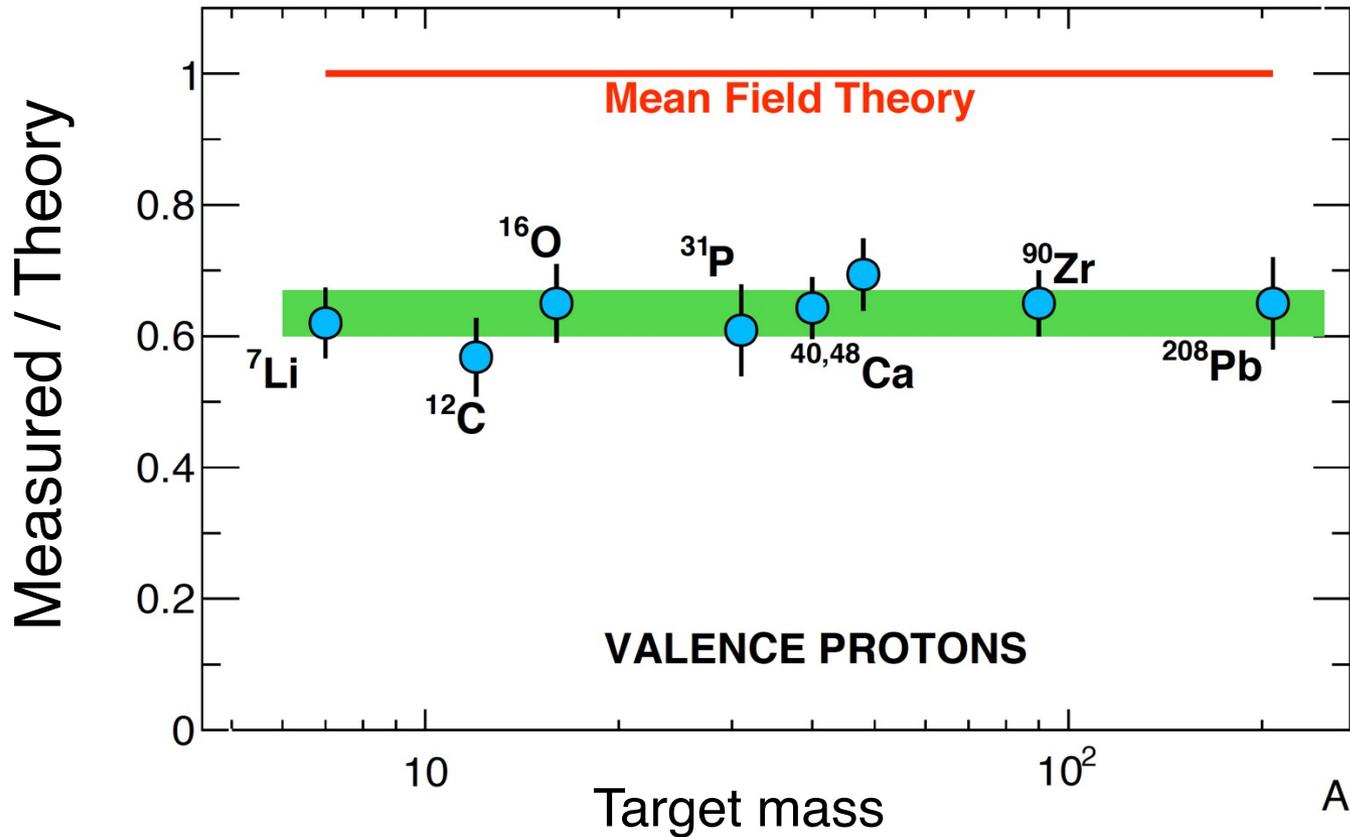
Compare to Shell Model predictions:

- Shapes well described
- Normalization...

# (e,e'p) scattering off shell orbitals

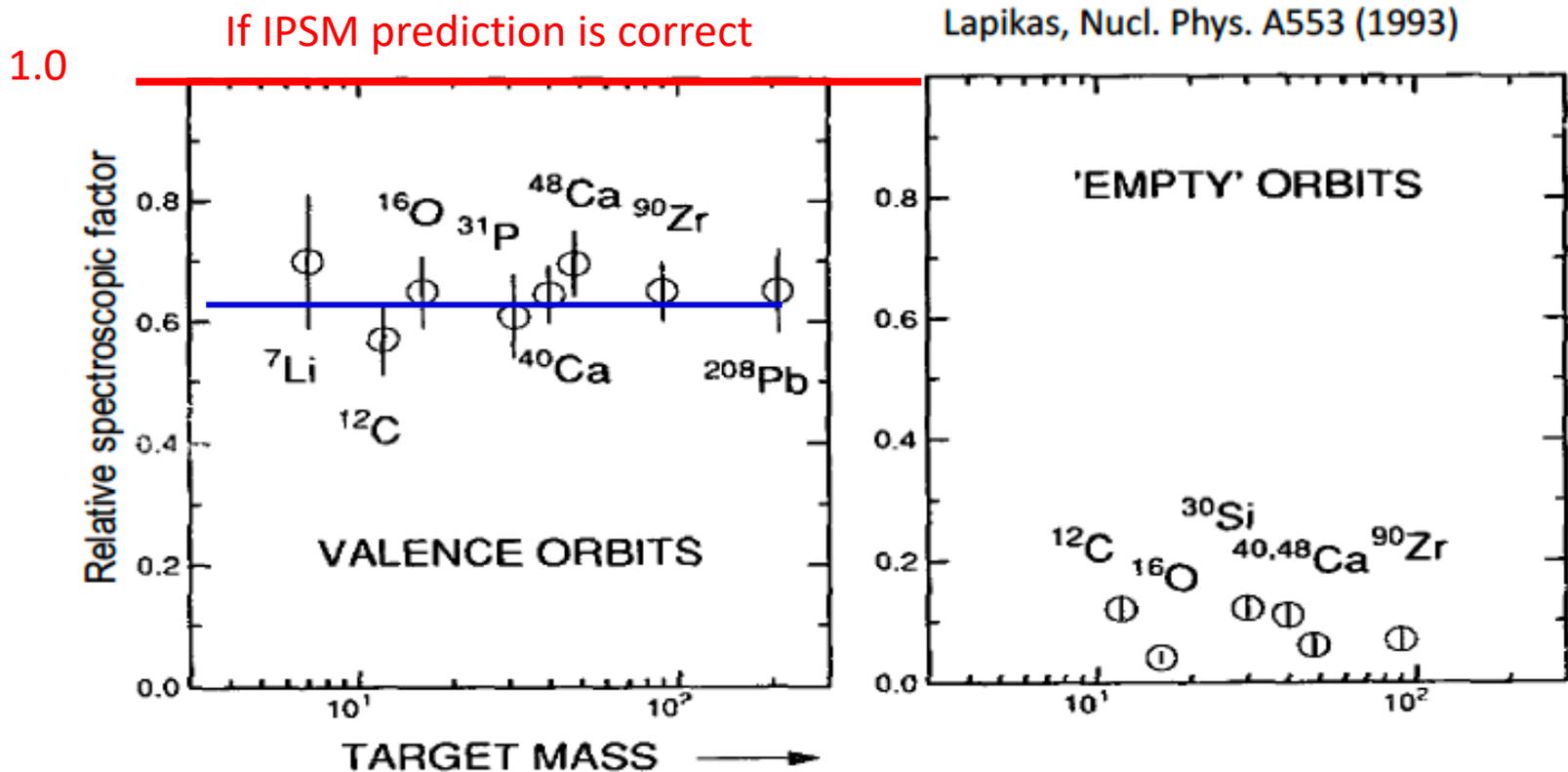


# Nucleon went missing??



L. Lapikas, Nuclear Phys. A553, 297c (1993)

# Nucleons went missing?



- Some strength was detected in the shell above the fermi edge which is predicted to be empty in IPSM


$$H = \underbrace{[T + V_M]}_{\text{IPSM}} + \underbrace{[V_{2\text{-body}} + V_{3\text{-body}} + \dots - V_M]}_{\text{neglected in IPSM}}.$$

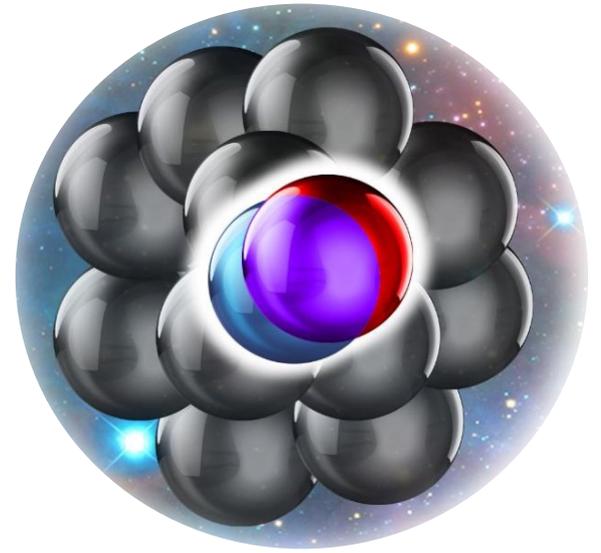
- ❑ Long range correlations can not account for the spectroscopic factor difference
- ❑ Short Range Correlations (SRCs) is possible solution

## Welcome to SRCs

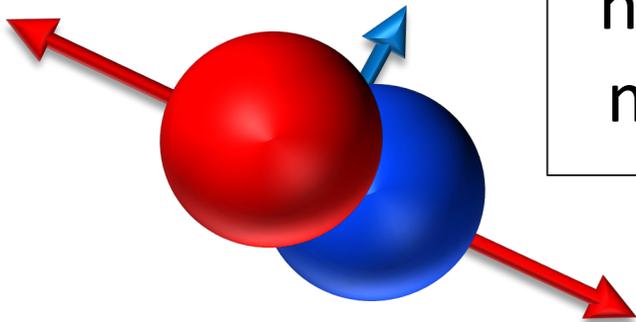
# What are Short Range Correlations (SRCs) ?

Nucleon pairs that are close together in the nucleus

r-space



k-space

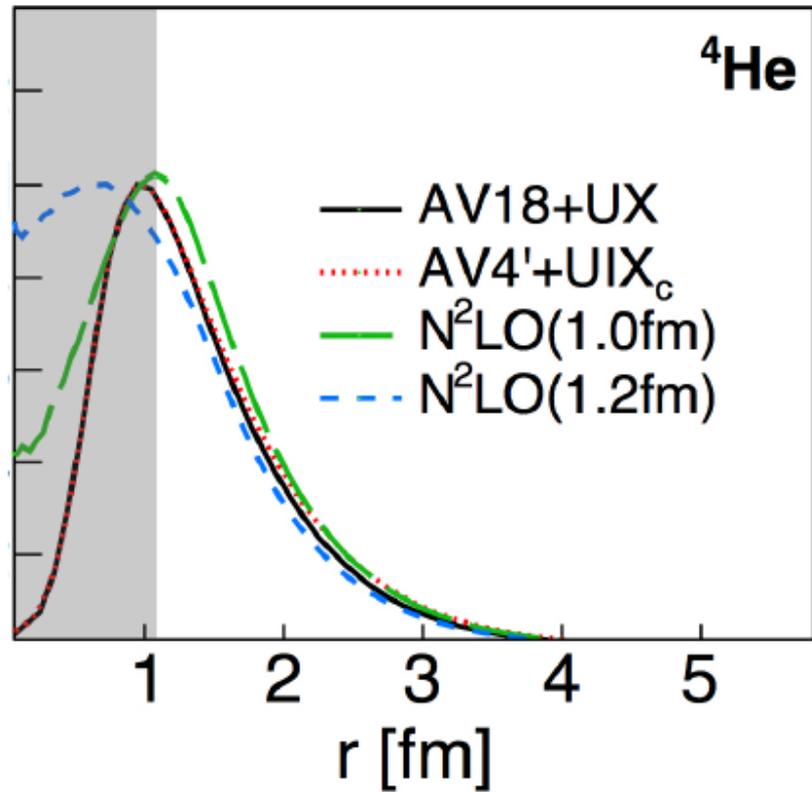


high *relative* and lower *c.m.* momentum compared to  $k_F$

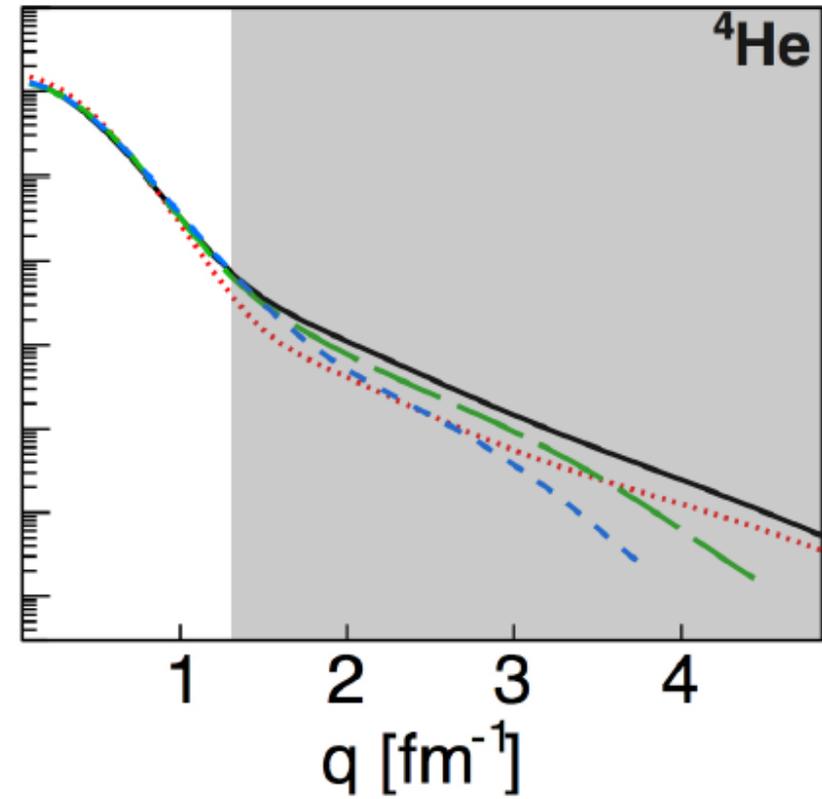
*More on this in next lectures*

# NN interaction at short distance

Probability to find two nucleons with relative distance  $r$



Probability to find two nucleons with relative momentum  $q$ .

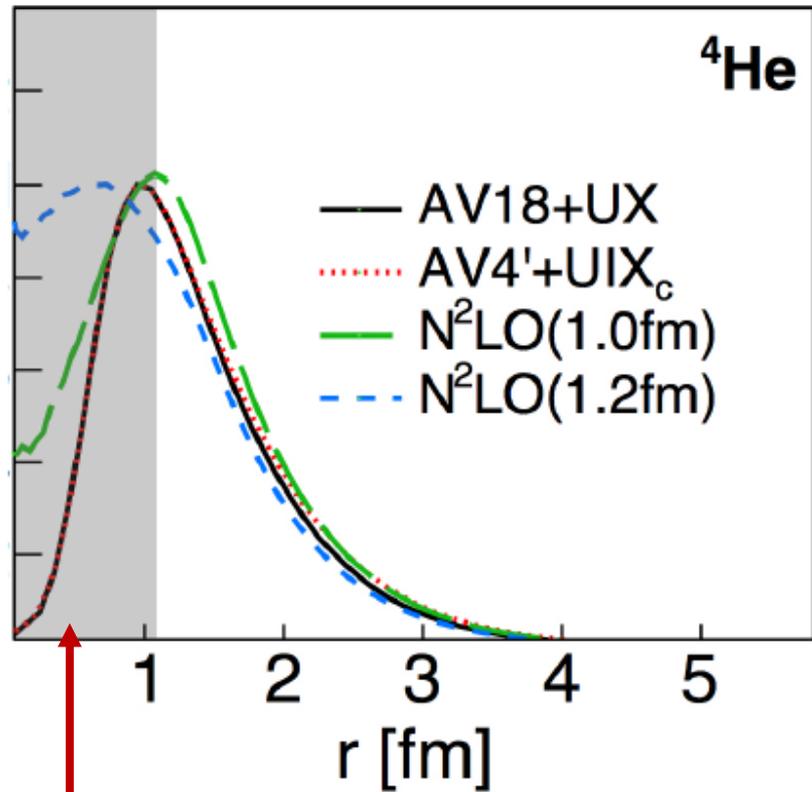


200 MeV/c  $\approx$  1  $\text{fm}^{-1}$

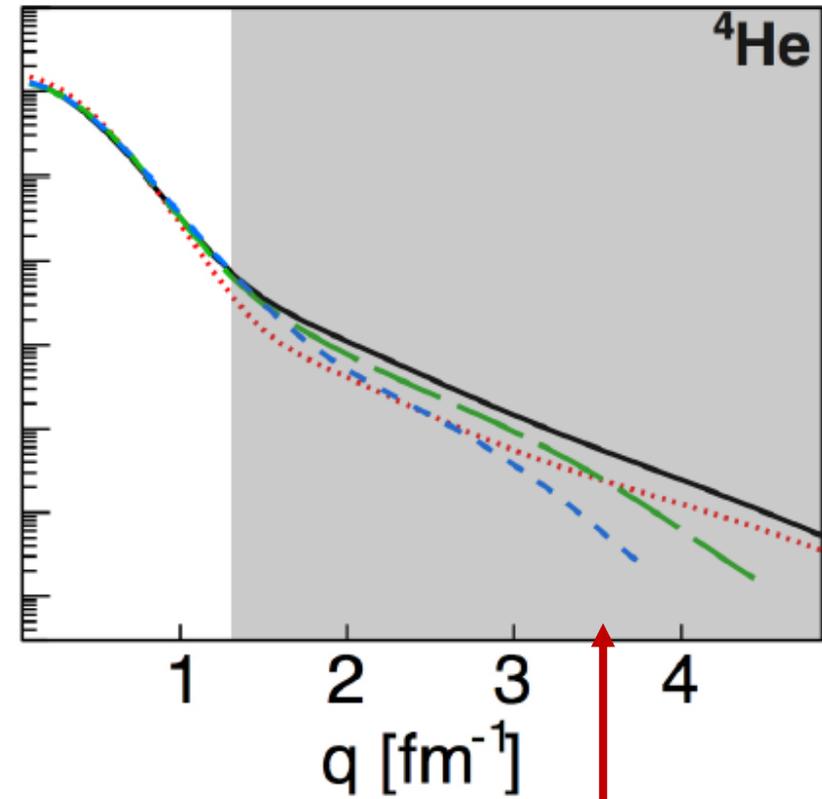
Need to put these to test

# Large model dependence at small-r/high-k

Probability to find two nucleons with relative distance  $r$



Probability to find two nucleons with relative momentum  $q$ .



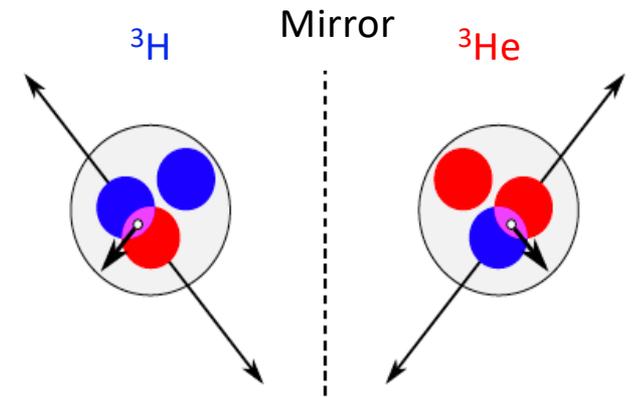
SRCs

Need to put these to test

# Why light nuclei?

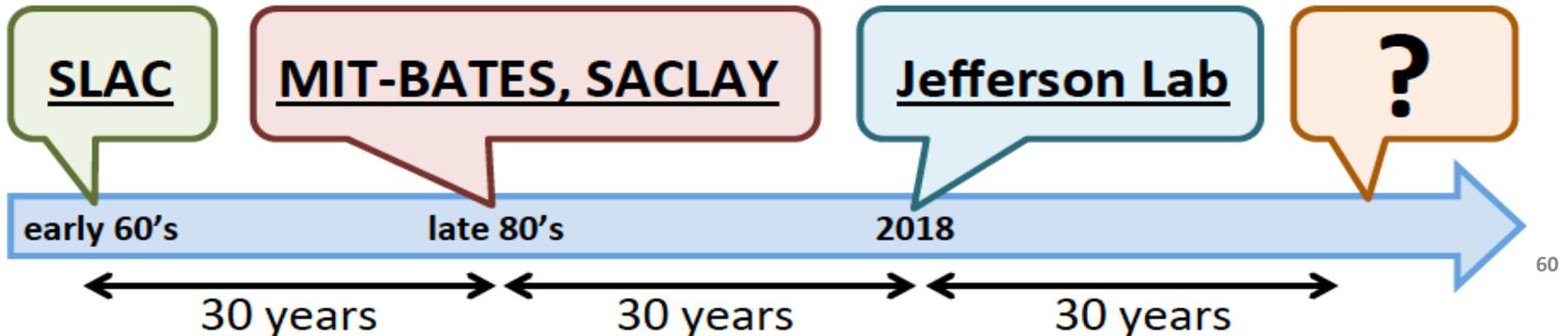
## 3-Body system:

- Exactly calculatable
- Test & benchmark theory



## Why Tritium?

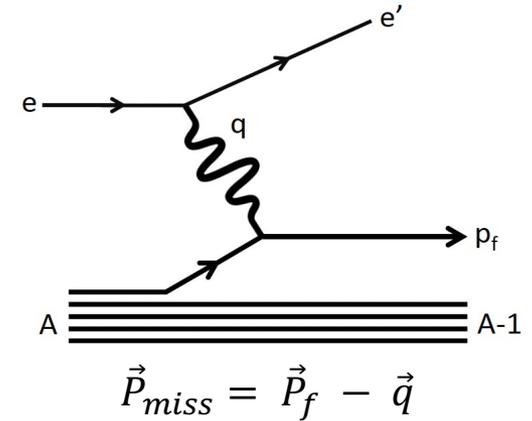
- Proton in  ${}^3\text{He}$  = Neutron in  ${}^3\text{H}$
- Constraint reaction mechanism



# High $Q^2$ : PWIA factorized approximation

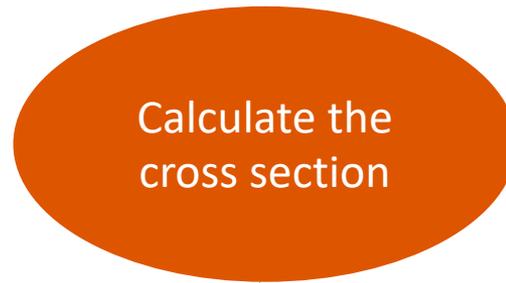
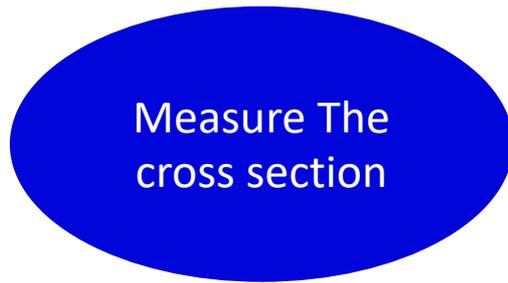
Cross-section (Observation) (e,e'p)

$$\frac{d^6\sigma}{d\omega dE_p d\Omega_e d\Omega_p} = K \sigma_{ep} S(|\vec{p}_i|, E_i)$$



Experiment:

Theory



Comparison



Reaction mechanism

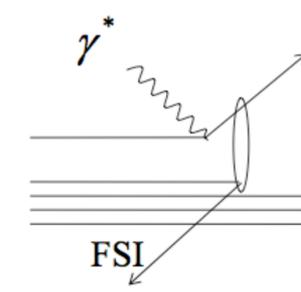
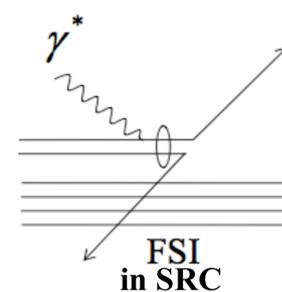
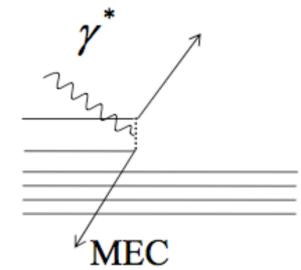
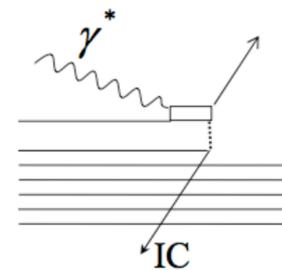
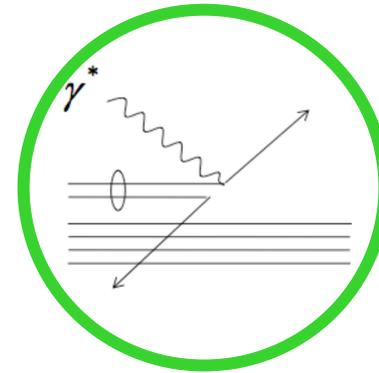
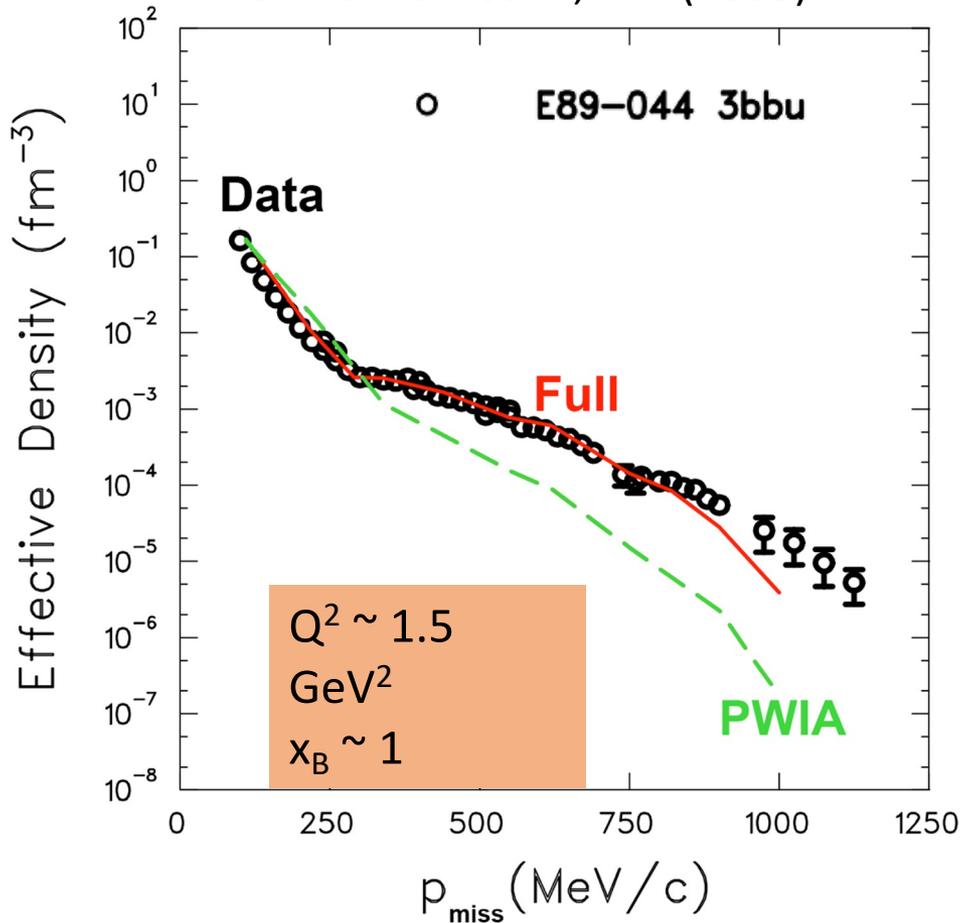


NN interaction

CD-Bonn NN potential

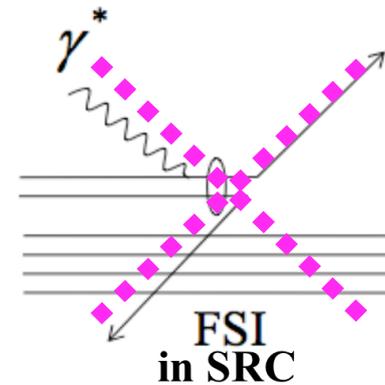
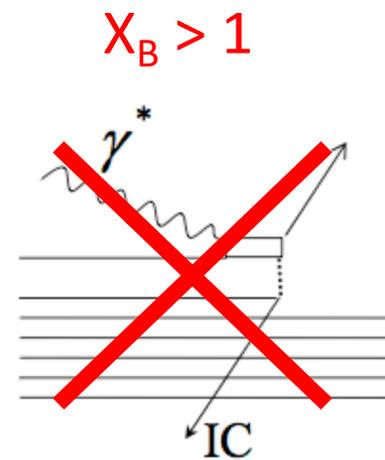
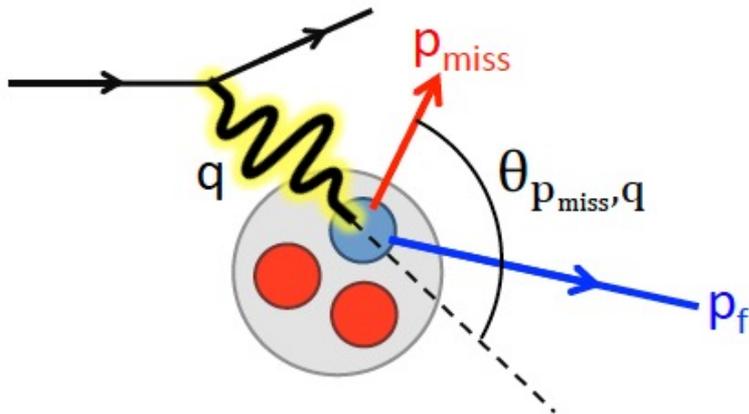
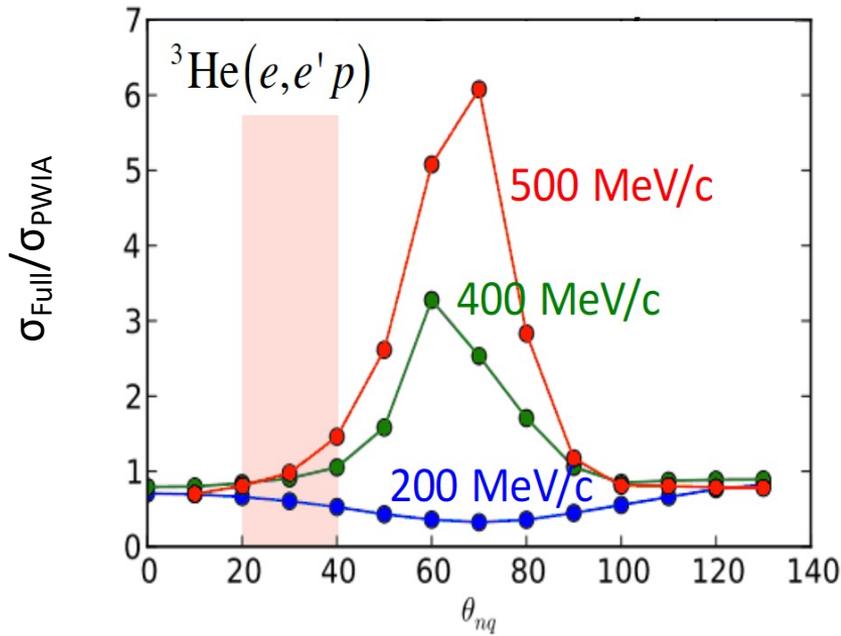
# Non-QE mechanisms contribution

F. Benmokhtar et al., PRL (2005)

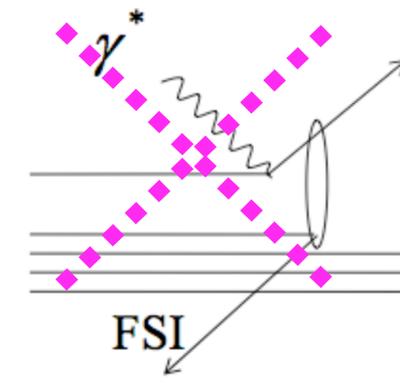
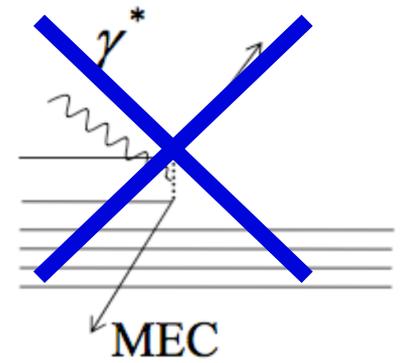


□ Non-QE mechanisms can be minimized using selected kinematic region

# Minimizing non-QE mechanisms

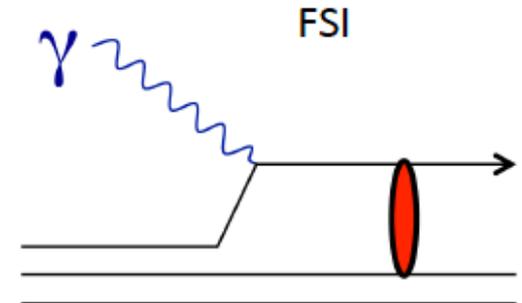
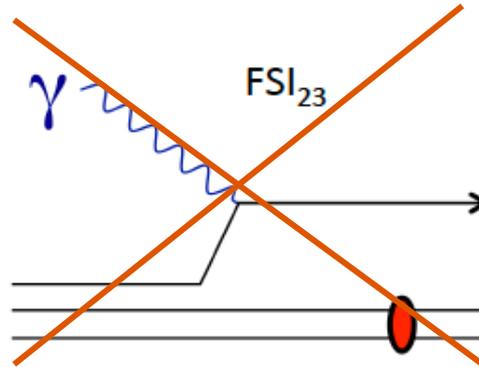
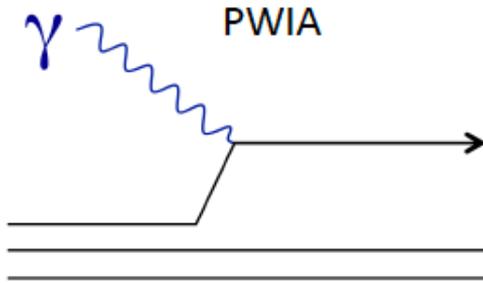


$Q^2 > 2 \text{ GeV}^2$



$\theta_{qr} < 35^\circ$

# Compare to different theory calculation



## Cracow:

- Faddeev-formulation-based calculations
- Continuum interaction between two spectator nucleons (FSI<sub>23</sub>)

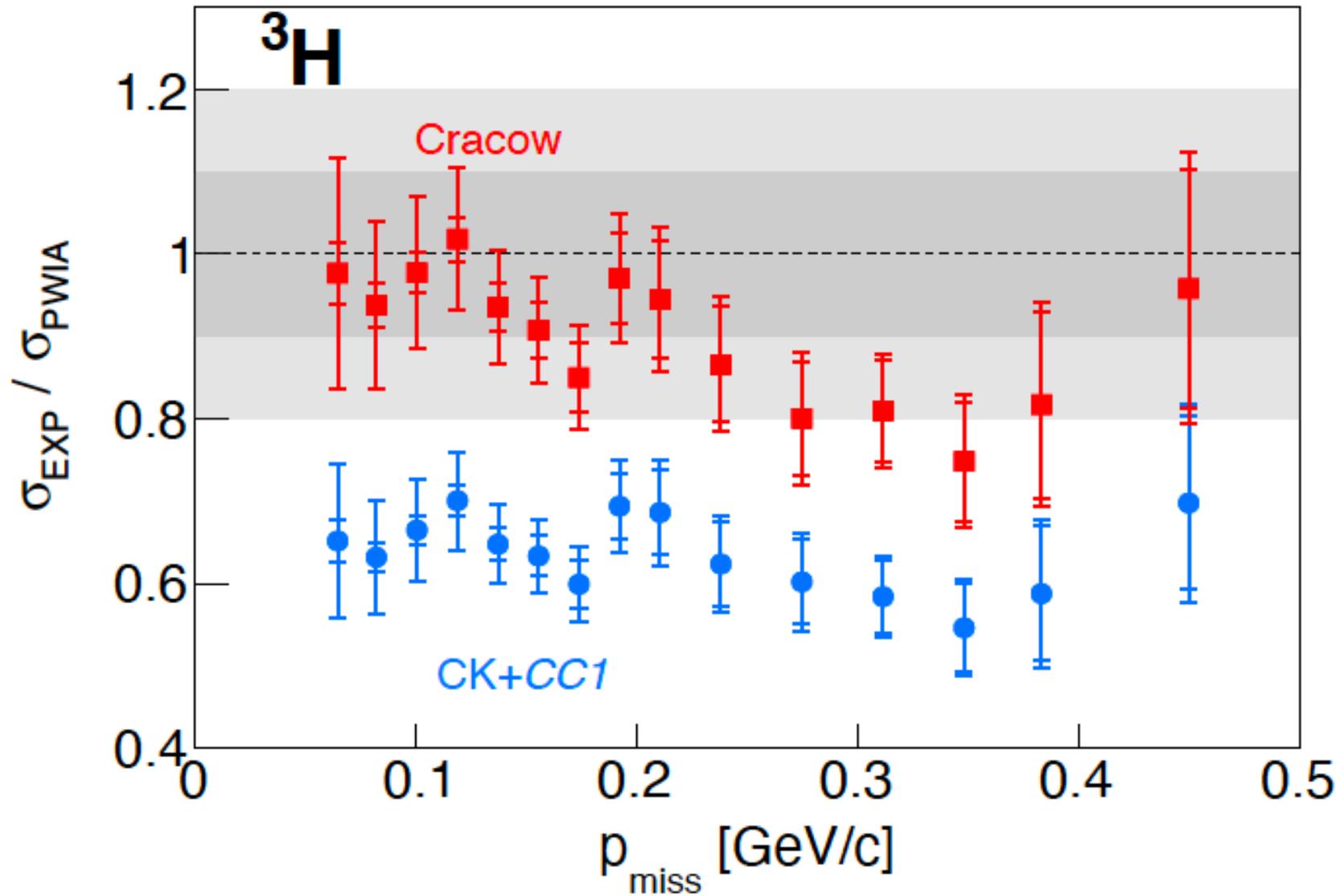
## CK + CC1:

- <sup>3</sup>He spectral function of C. Cio degli Atti and L. P. Kaptari and electron off-shell nucleon cross-section
- Including FSI<sub>23</sub>

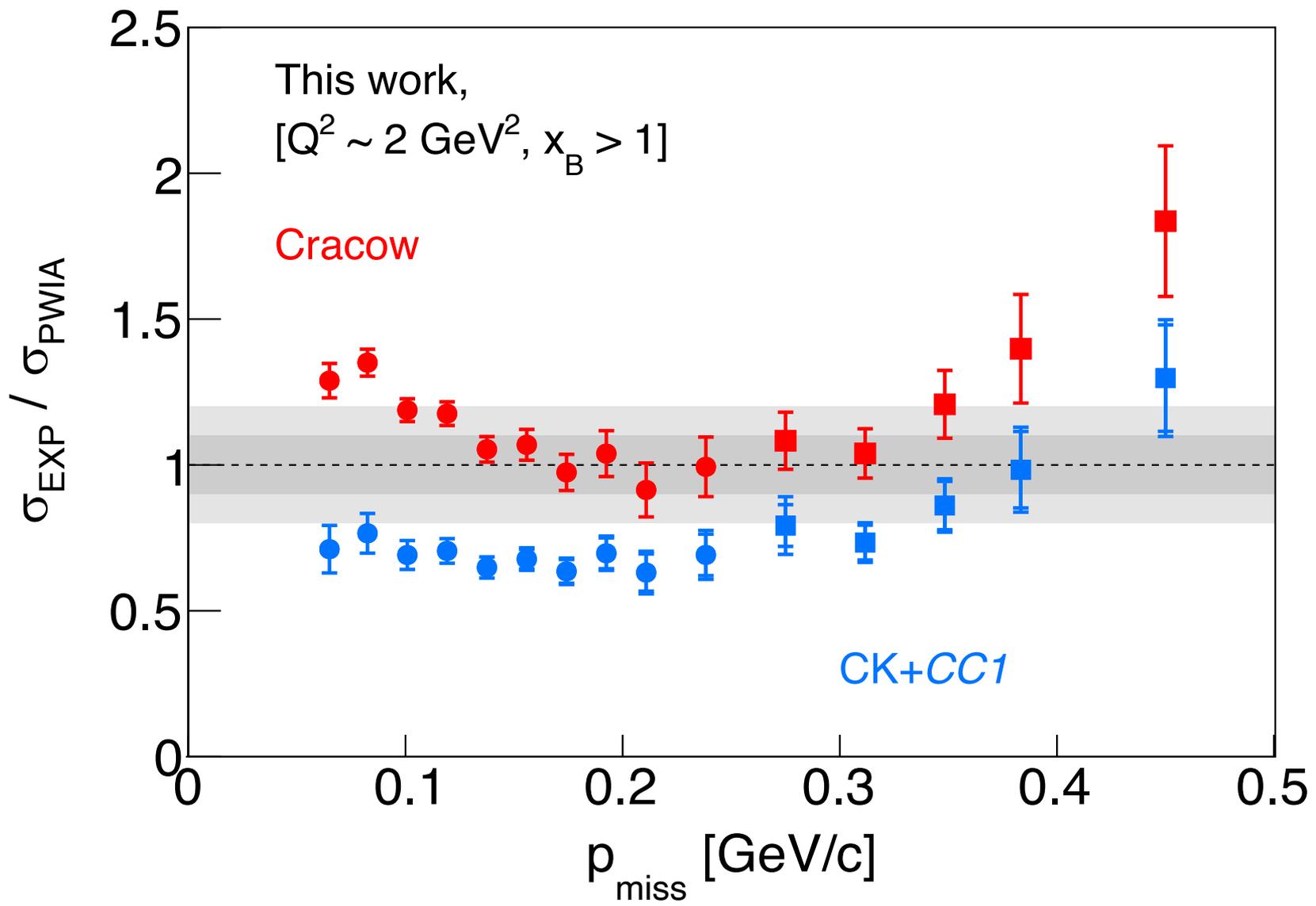
## M. Sargian (FSI):

- FSI calculation based on generalized Eikonal approximation
- Does not include FSI<sub>23</sub>

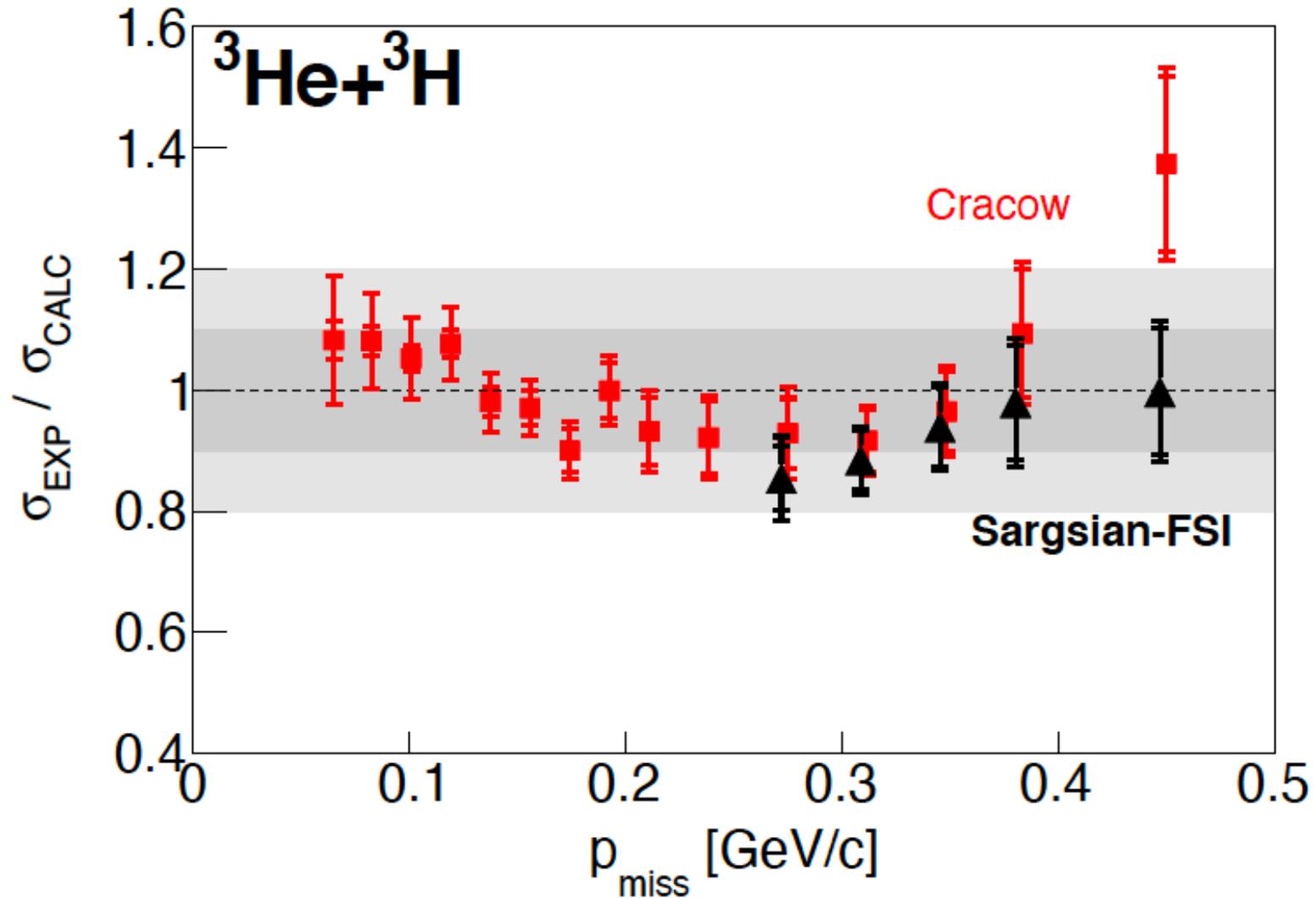
# Exp/PWIA: Cracow and CK+CC1 For $^3\text{H}$



# Exp/PWIA: Cracow and CK+CC1 For $^3\text{He}$

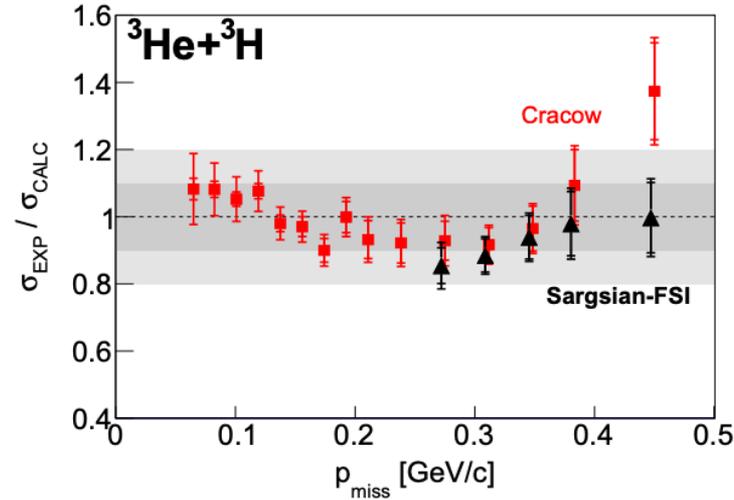


# Isoscalar Sum good better agreement



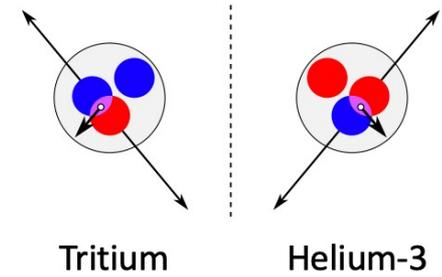
## What we have learned in A= 3:

- ❑  ${}^3\text{H}$  has better agreement to calculation than  ${}^3\text{He}$
- ❑ Data/PWIA  $\sim 20\%$  at high  $P_{\text{miss}}$
- ❑ Theory describes  ${}^3\text{H}+{}^3\text{He}$  data within 10% up to  $P_{\text{miss}} = 500 \text{ MeV}/c$

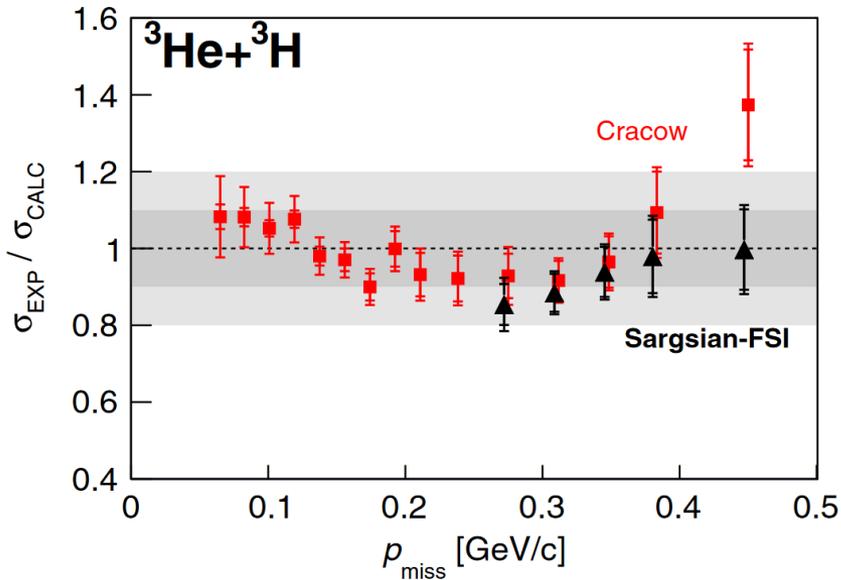


Crucial benchmark for few-body nuclear theory  
and essential test of theoretical calculation

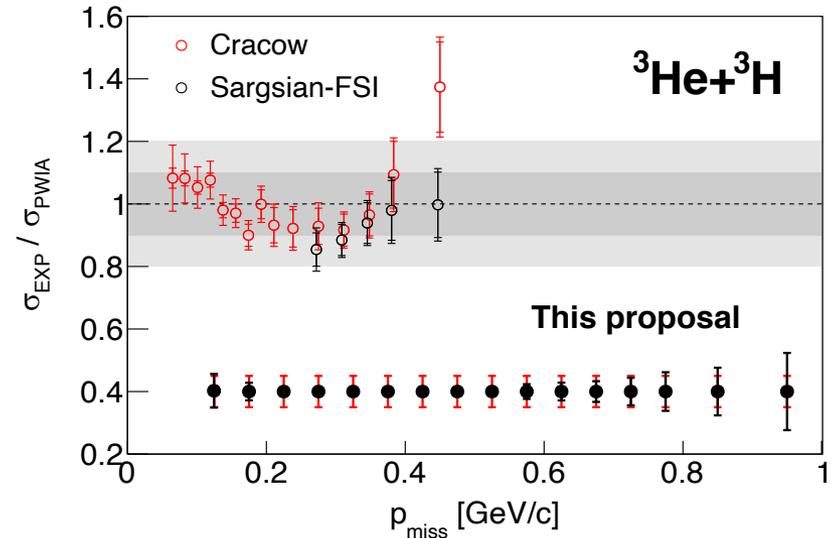
# A=3 nuclei: Ideal systems to test theory calculations



(e,e'p) data from Hall A JLab



Future measurement with CLAS12



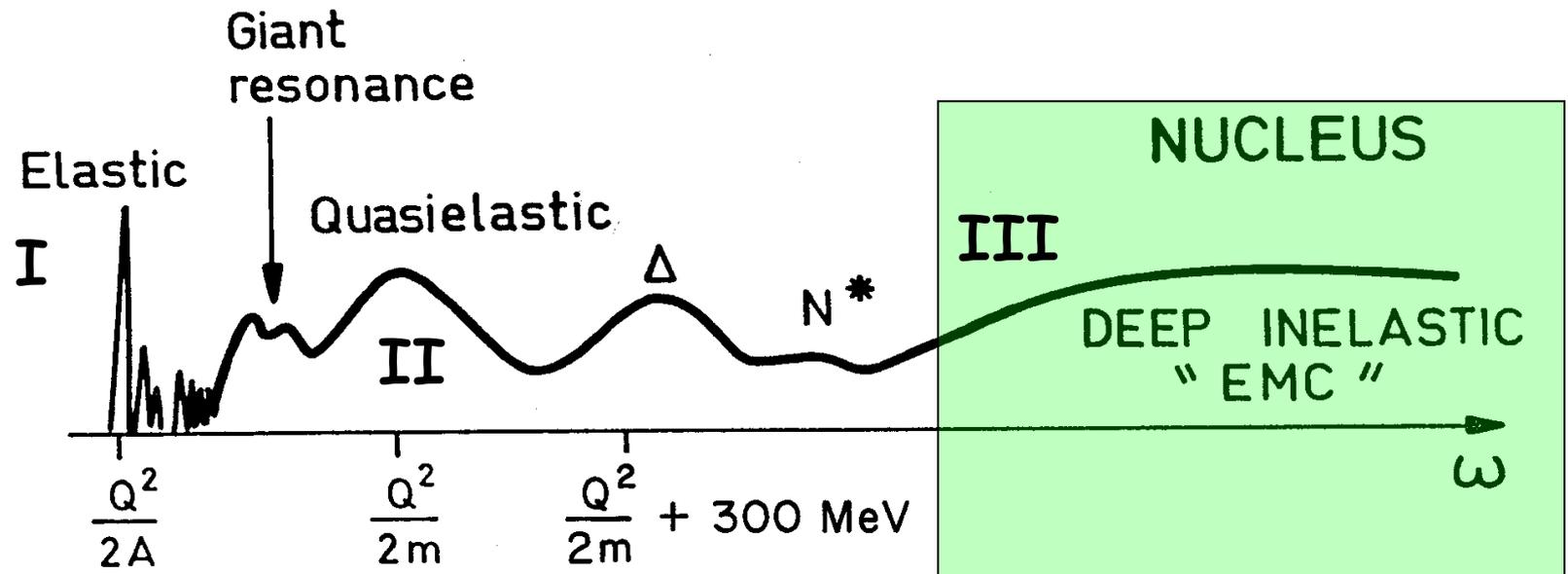
R. Cruz-Torres, D. Nguyen, PRL(2020).  
R. Cruz-Torres PLB (2019).

*See Ronen's talk*

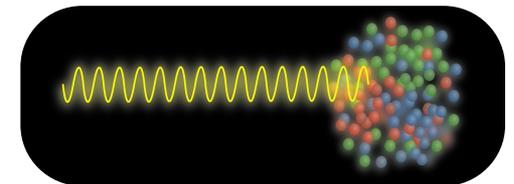
# Quasi-elastic Summary

- ❑ Measures shell structure directly
- ❑ Provide information on nucleon momentum distribution
- ❑ Nucleon went missing, provide the hint to SRCs
- ❑ Measurement on light nuclei benchmark theory  
calculation up to high momentum 500 MeV

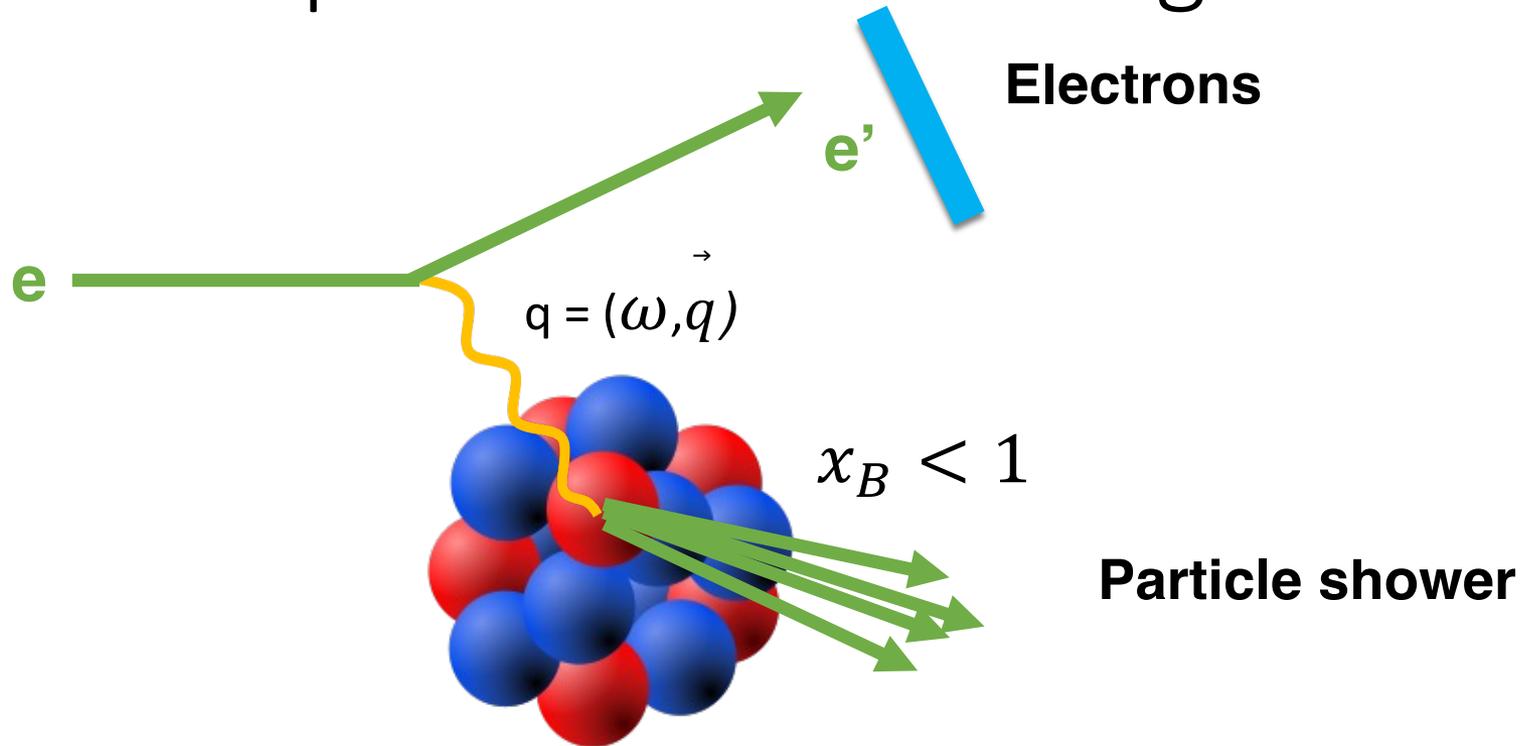
# Overview: Deep Inelastic Scattering (DIS)



- Structure Functions
- EMC Effect



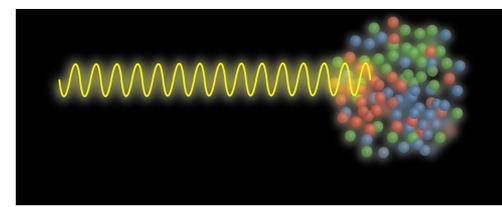
# Deep Inelastic Scattering



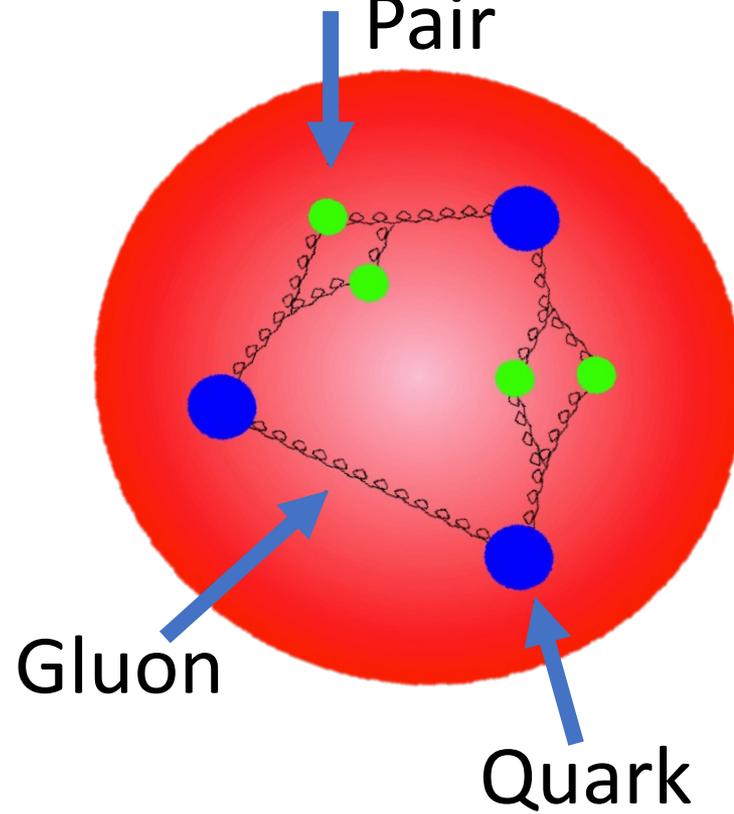
- ❑ Interacting nucleon destroyed
- ❑ Interaction with Parton (quark) inside the nucleon
- ❑ Cross-section depends on **Nucleon structure function  $F_2$**

$$\frac{d^2\sigma}{d\Omega dE'} = \sigma_A = \frac{4\alpha^2 E'^2}{Q^4} \left[ 2 \frac{F_1}{M} \sin^2 \left( \frac{\theta}{2} \right) + \frac{F_2}{\nu} \cos^2 \left( \frac{\theta}{2} \right) \right] \approx K(E, \theta, E') F_2(x)$$

# Partonic Structure

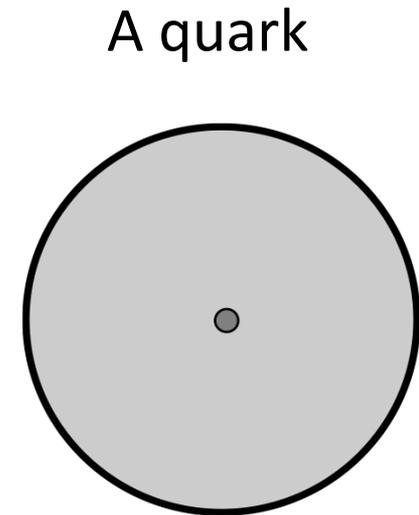
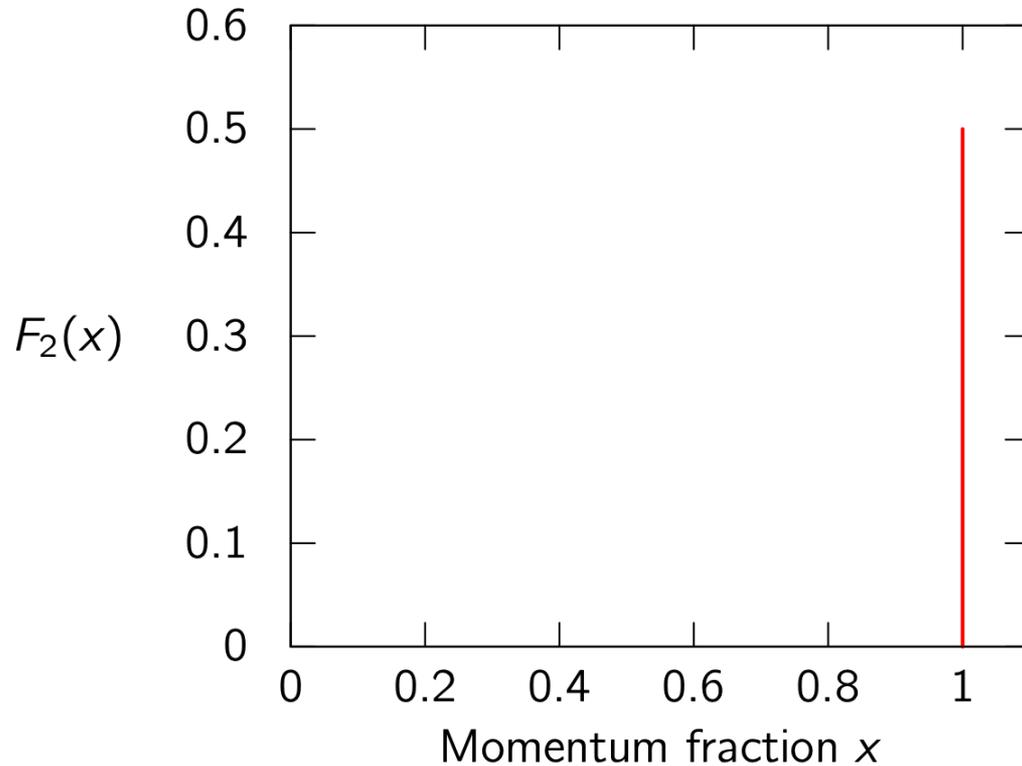


Quark –  
Anti-quark  
Pair



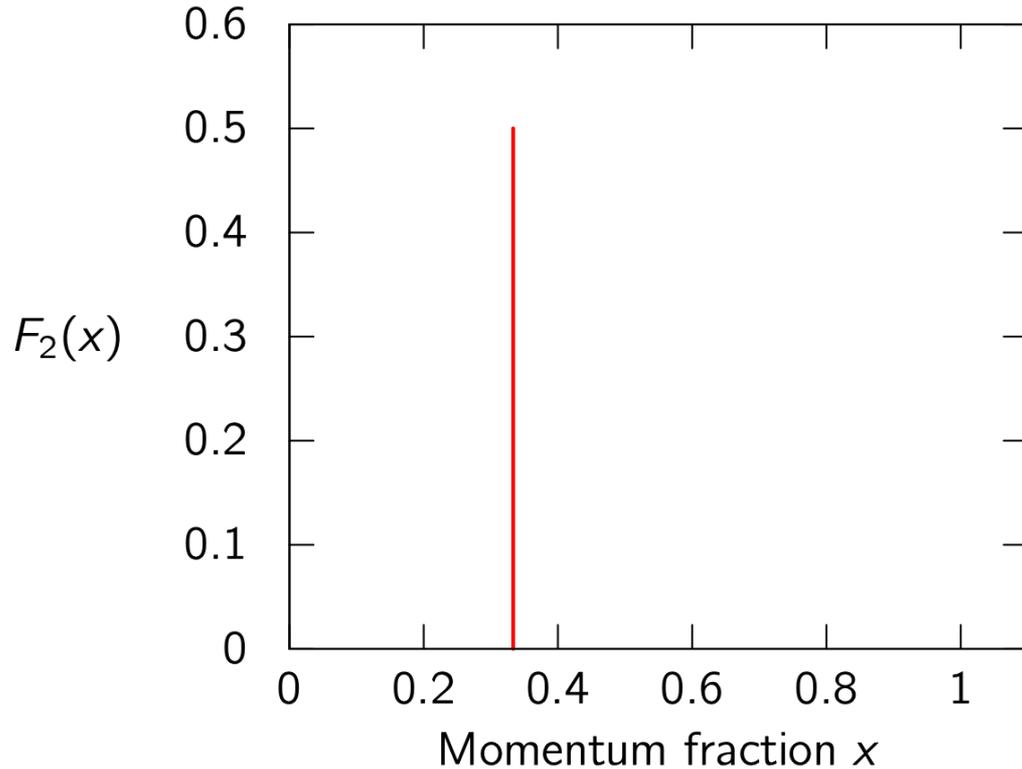
# What $F_2$ can tell us about the nucleon

$$F_2(x, Q^2) = \sum_i e_i^2 \cdot x \cdot f_i(x)$$

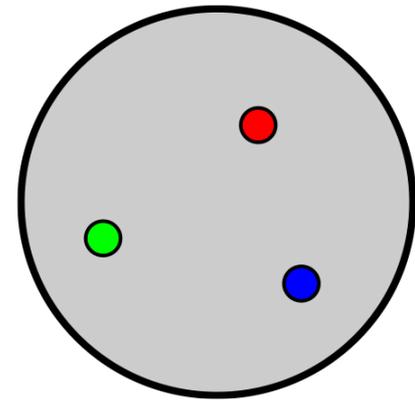


# What $F_2$ can tell us about the nucleon

$$F_2(x, Q^2) = \sum_i e_i^2 \cdot x \cdot f_i(x)$$

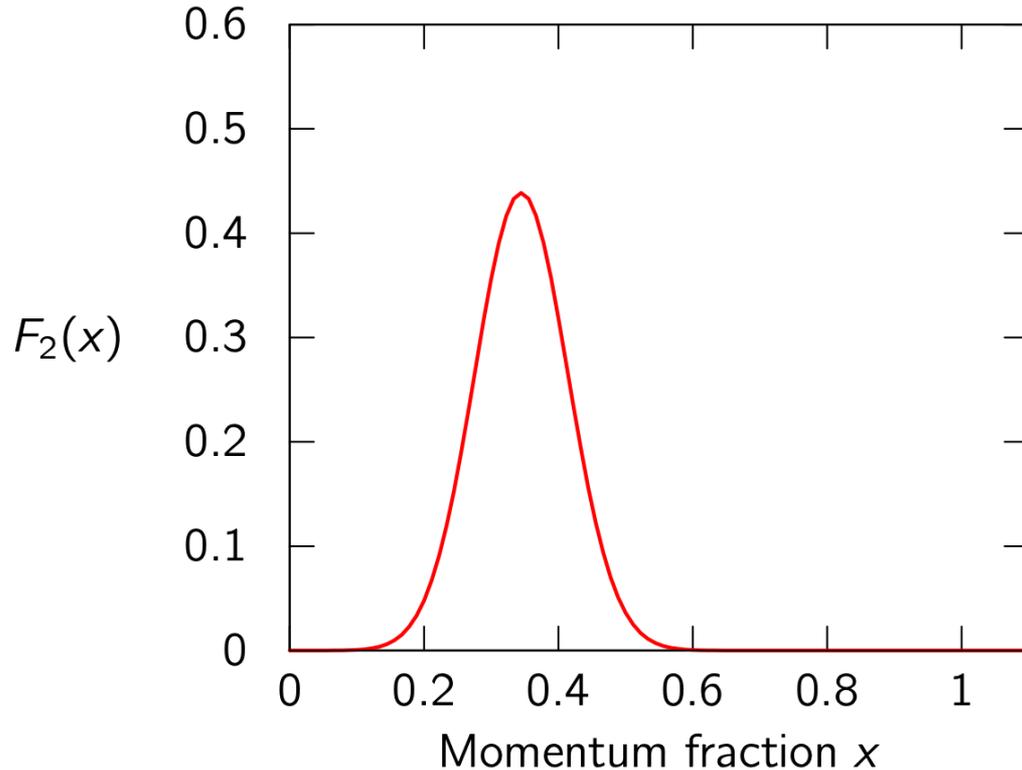


Three valence quarks

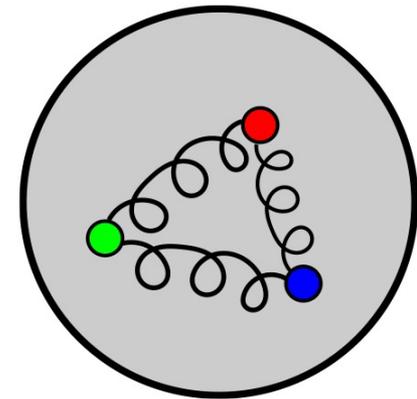


# What $F_2$ can tell us about the nucleon

$$F_2(x, Q^2) = \sum_i e_i^2 \cdot x \cdot f_i(x)$$

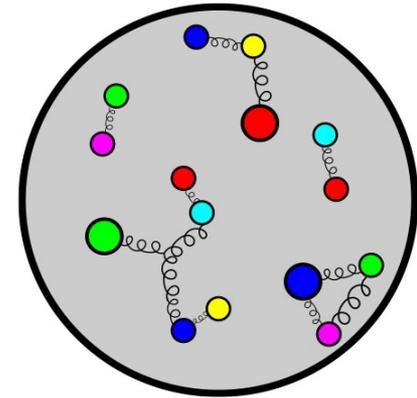
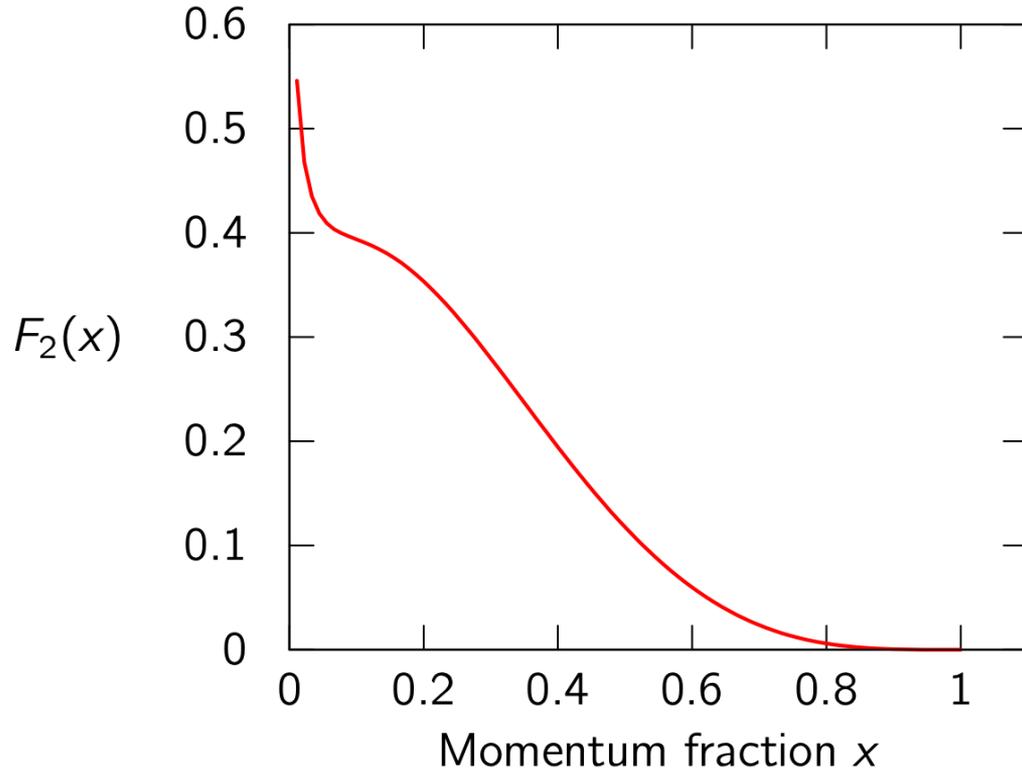


Three bound  
valance quarks

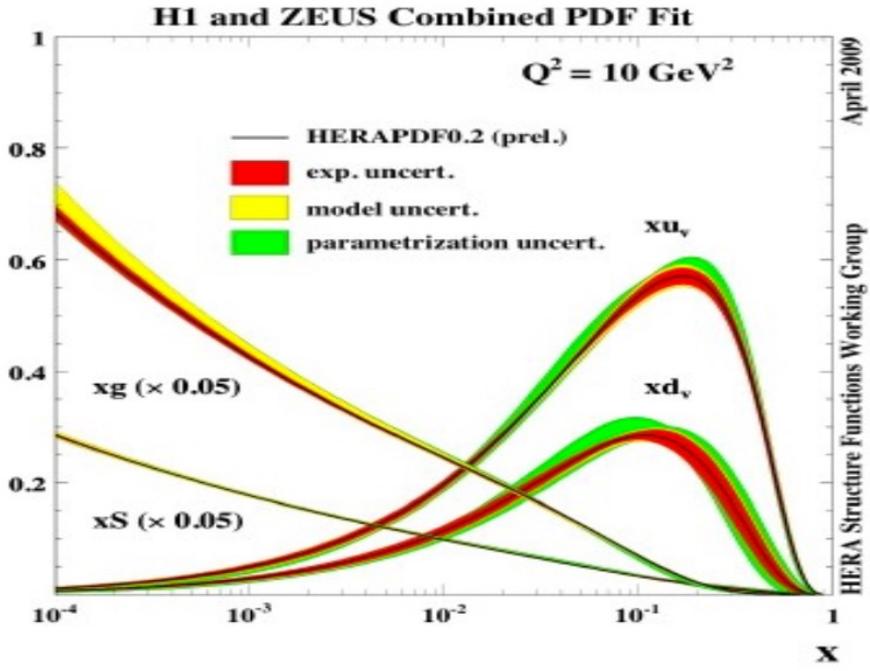
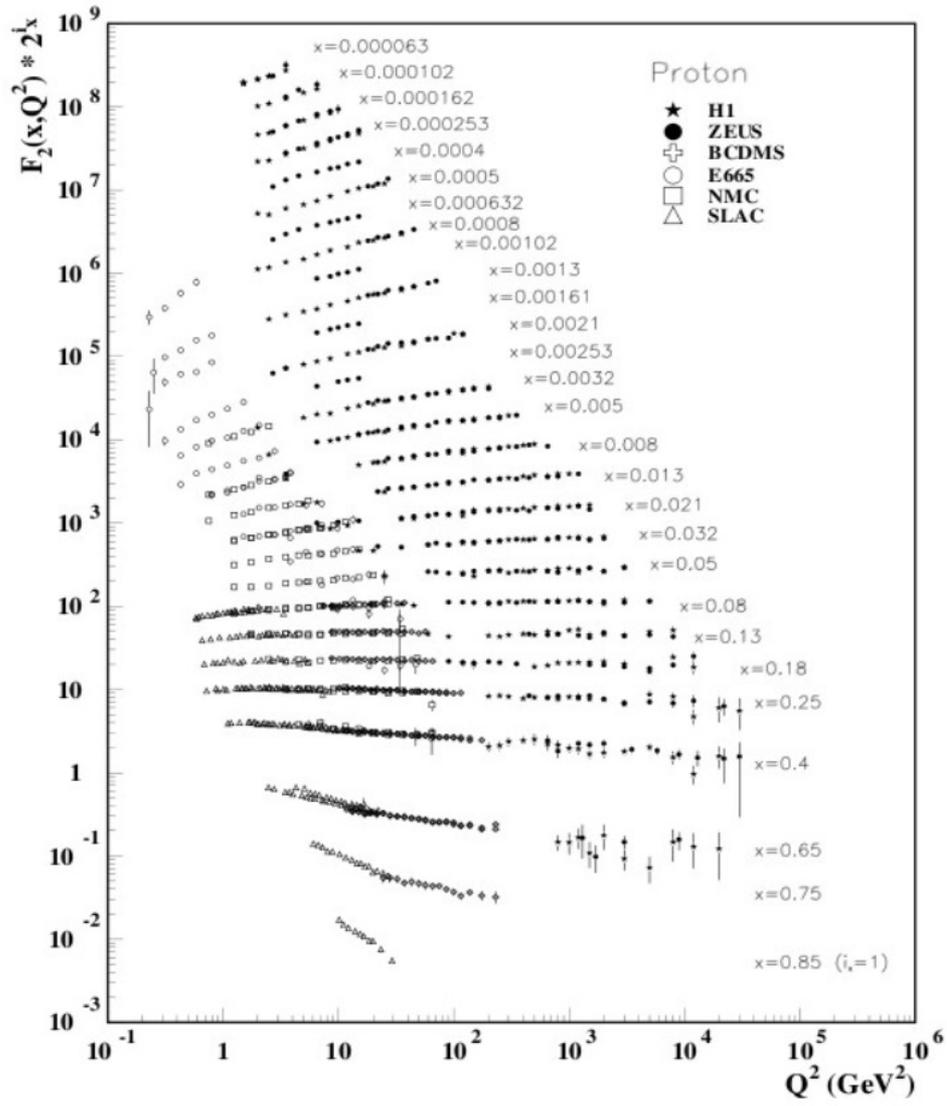


# What $F_2$ can tell us about the nucleon

$$F_2(x, Q^2) = \sum_i e_i^2 \cdot x \cdot f_i(x)$$



# Decade of measurement gives us Proton's $F_2$ and PDFs



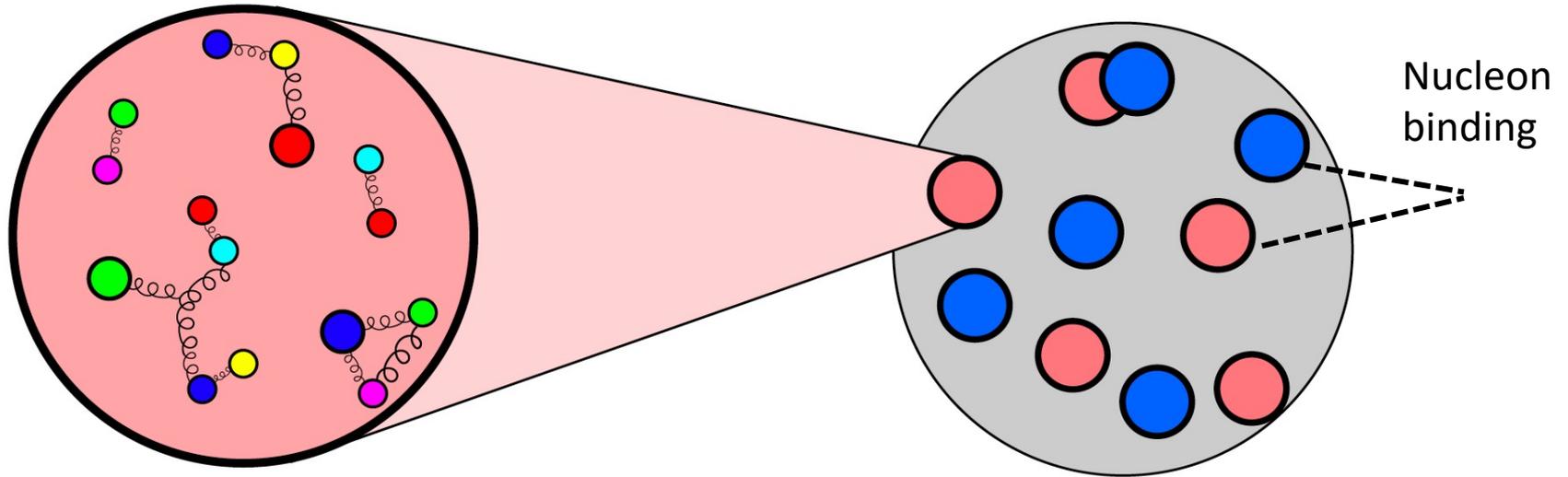
# What is $F_2$ for a nucleus A

$$F_2^A = Z F_2^P + N F_2^N ??$$

## Questions:

1. Do quarks move differently in Nuclei?
2. Does the nuclear environment affect quark?

# Quark and Nuclei are scale-separated



The scale of GeV

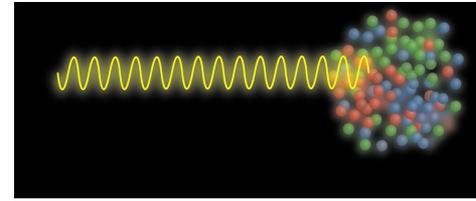
The scale of MeV

**Naive expectation :**

**Bound nucleon = Free nucleon**

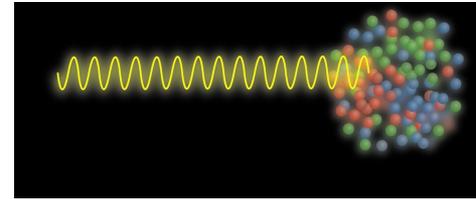
(Except some small Fermi motion correction)

# Partonic – Nucleonic Interplay



**Question:** What is the *simplest* example of nuclear interaction affecting partonic properties?

# Partonic – Nucleonic Interplay



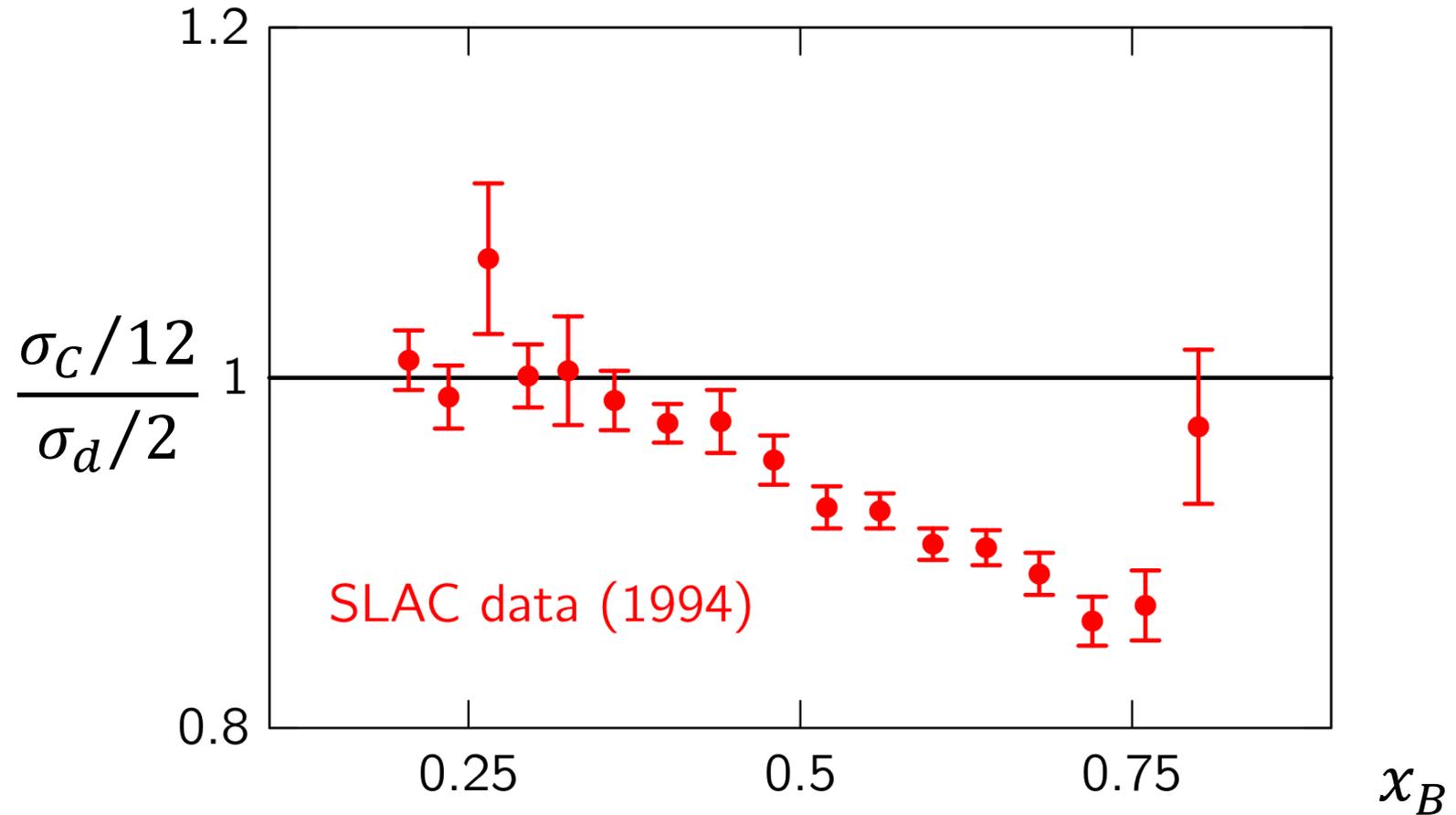
**Question:** What is the simplest example of nuclear interaction affecting partonic properties?

**Answer:**

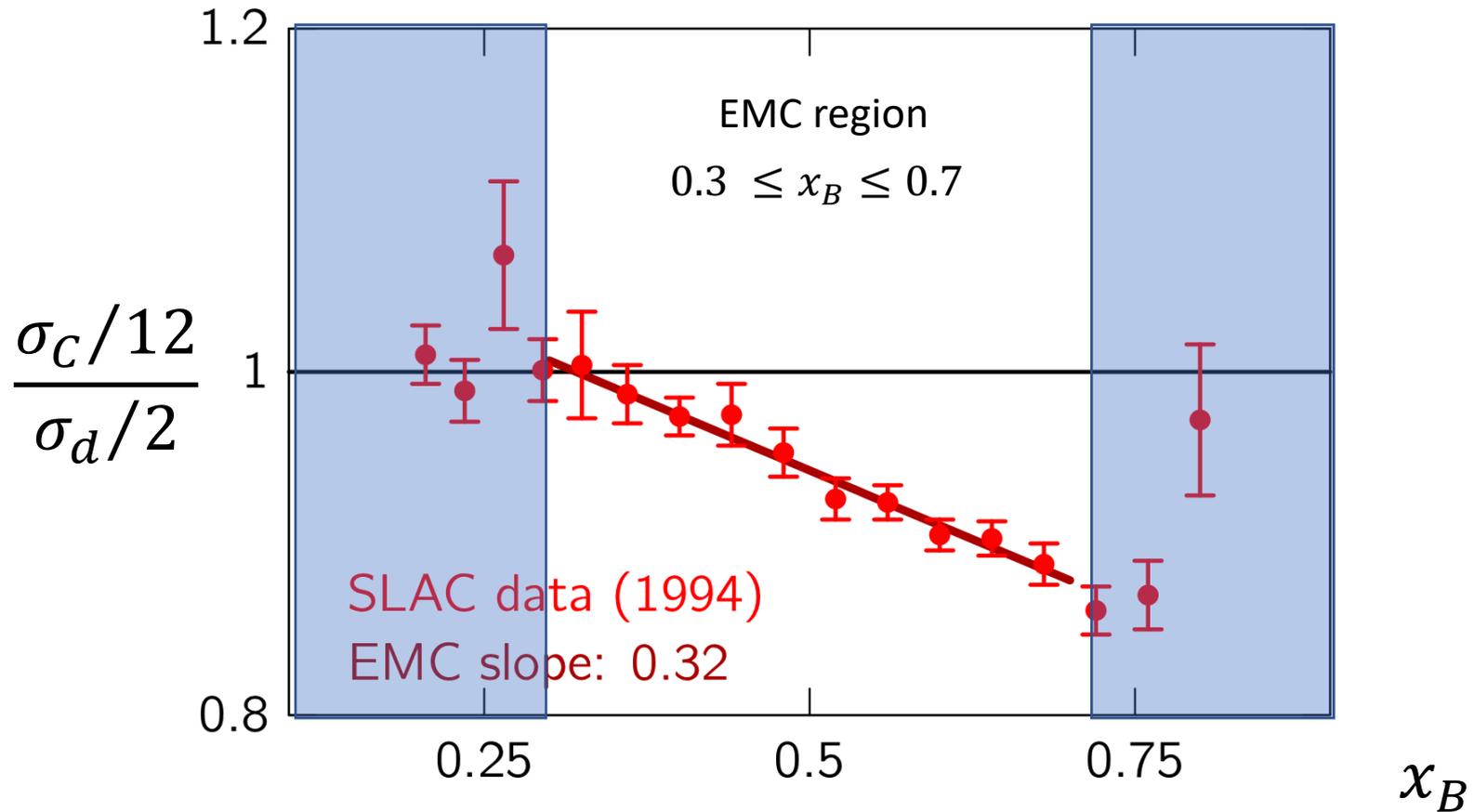
**The nuclear interaction that binds the deuteron also makes the neutron stable.**

- Simplest nuclear system = Deuteron,
- Free neutron is unstable: decays in  $\sim 10$  minutes,
- Bound in the Deuteron, a neutron can live forever!

# The nuclear environment affects quarks!



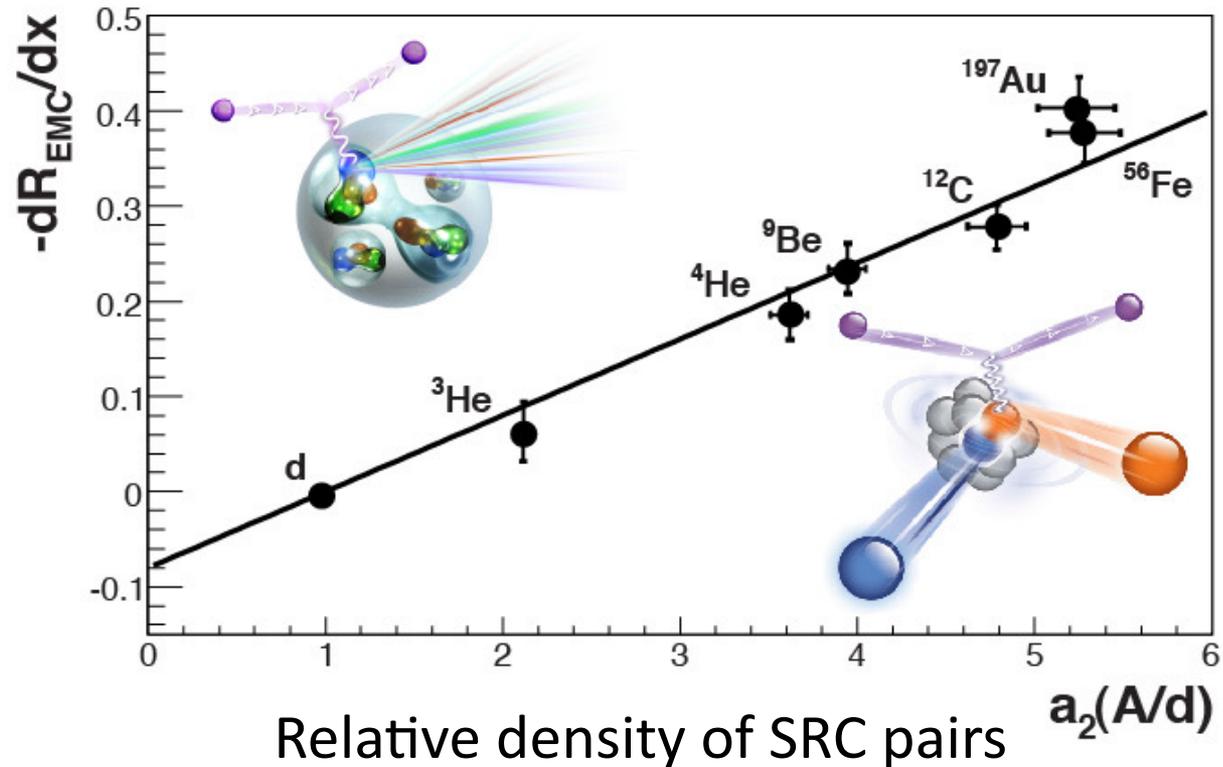
# The EMC effect!



- Size of EMC effect is characterized by the slope

The frequency of SRC pairs correlates with the strength of the EMC Effect.

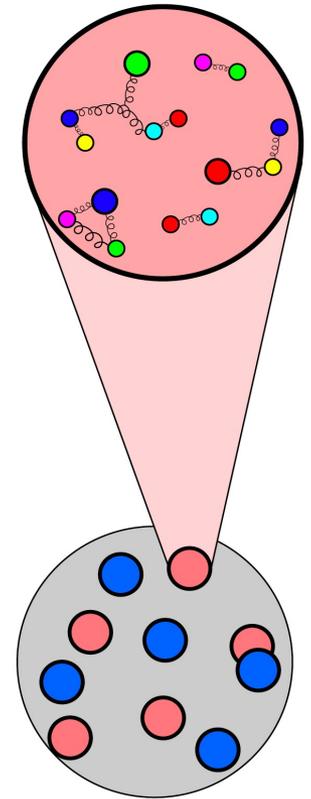
Magnitude of the EMC Effect



*More on this in next lectures*

# Deep inelastic scattering summary

- DIS is scattering from a quasi-free quark.
- Structure functions contain the quark momentum density information.
- Bridging between nucleon and parton regiem
- EMC Effect:
  - Bound nucleon  $\neq$  free nucleon
  - Many models try to explain the data.
  - Many experiments try to understand the problem.
  - Hint in correlation EMC vs SRC



# Summary of the physics

- Nuclear strong interaction that binds nuclei is the residual from the strong interaction between quarks!



- Elastic scattering:
  - Form factors describe the nuclear and nucleon structure in terms of charge and magnetic moment
- Quasielastic scattering:
  - Shell structure, momentum distributions, correlations
- Deep inelastic scattering:
  - Quark-parton picture, structure functions describe quark momentum distributions