

## Harut Avakian

CLAS12 Collaboration Meeting, March 6, 2025

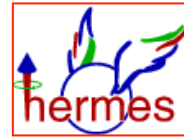
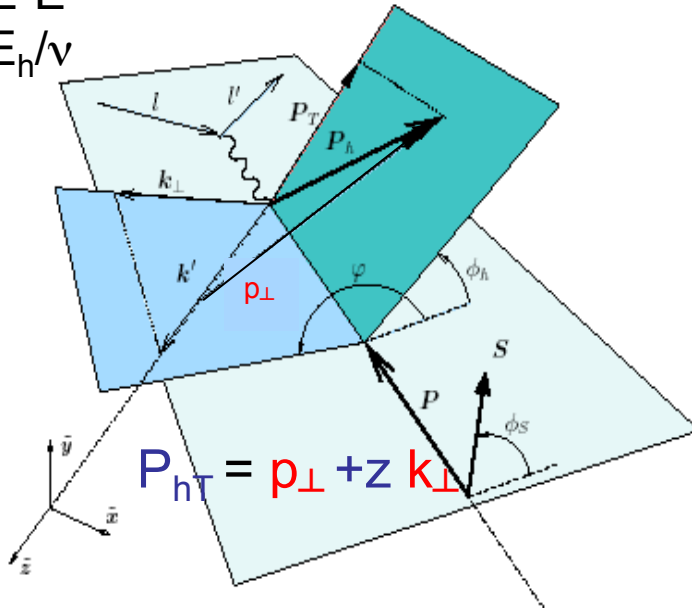
- Why measurements of exclusive VMs are critical?
  - Access to OAM and GPD E
  - Understanding of the impact of diffractive VMs on studies of the 3D structure and PDF, Sivers in particular
- Challenges in interpretation of exclusive rhos
  - separation of exclusive rhos from semi-exclusive rhos
  - separation of transverse rho from longitudinal rhos
  - separation of transverse photon contributions from longitudinal
- Proposal to measure exclusive diffractive VMs with transversely polarized target
- Summary

\*) RGH run group addition

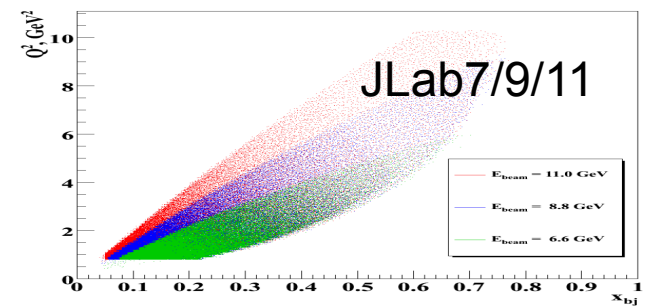
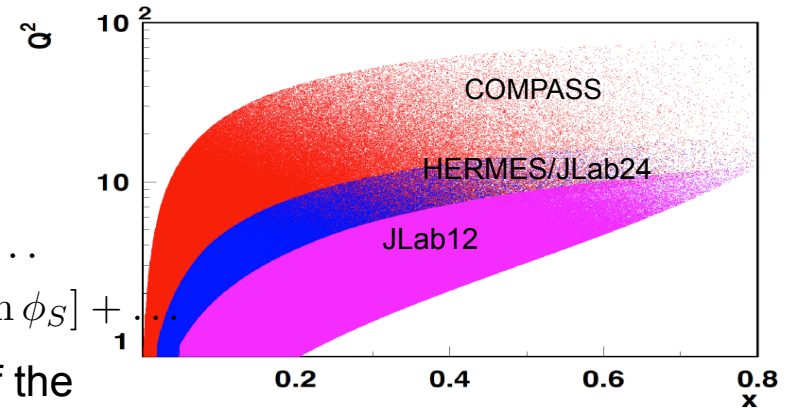
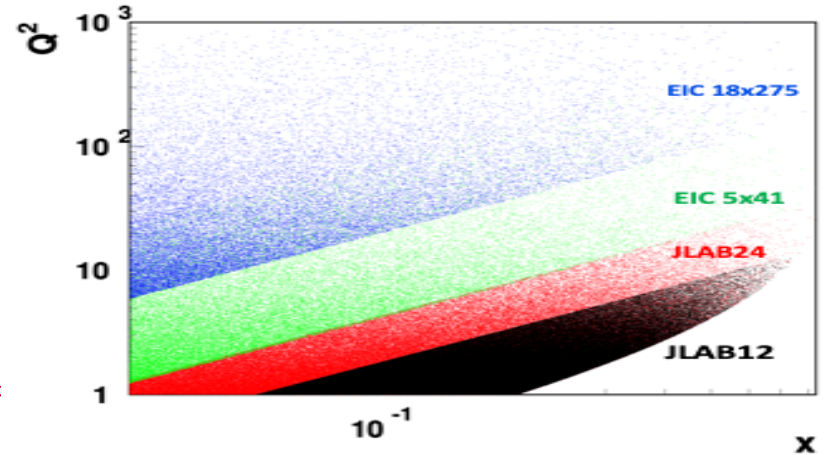
# SIDIS kinematical coverage and observables

$$v = E - E'$$

$$z = E_h / v$$



EIC



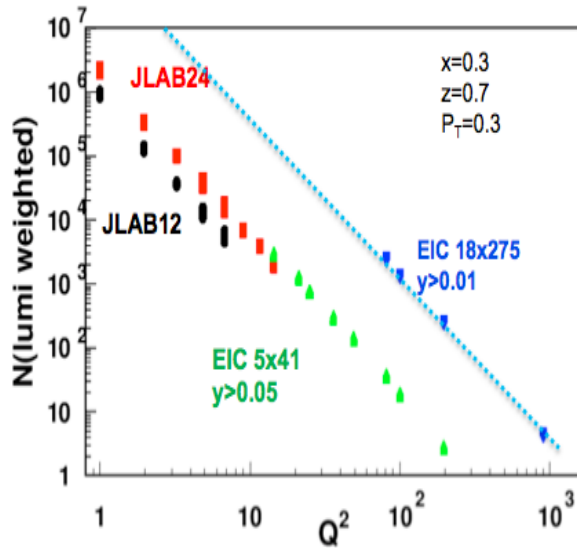
$$\sigma \propto F_{UU} + P_b \sqrt{2\epsilon(1-\epsilon)} F_{LU}^{\sin \phi} \sin \phi + P_t \epsilon F_{UL}^{\sin 2\phi} \sin 2\phi + \dots$$

$$+ \epsilon F_{UU,L} + |S_{\perp}| [F_{UT}^{\sin \phi - \phi_S} \sin(\phi - \phi_S) + \sqrt{2\epsilon(1+\epsilon)} F_{UT}^{\sin \phi_S} \sin \phi_S] + \dots$$

- Experiments measure the full azimuthal dependence of the cross section  $(x, y, z, P_T, \phi, \phi_S)$  and try to separate different modulations
- Some model dependent systematics introduced in modeling of acceptance and account of radiative corrections
- Large acceptance and multiparticle detection capabilities allow tests of all kind of assumptions used by theory

# Structure functions and depolarization factors

- At large x fixed target experiments are sensitive to ALL Structure Functions
- At higher energies (EIC), observables surviving the  $\epsilon \rightarrow 1$  limit ( $F_{UU}$ ,  $F_{UL}$ , Transversely pol.  $F_{UT}$ )



x-section from Bacchetta et al, 1703.10157

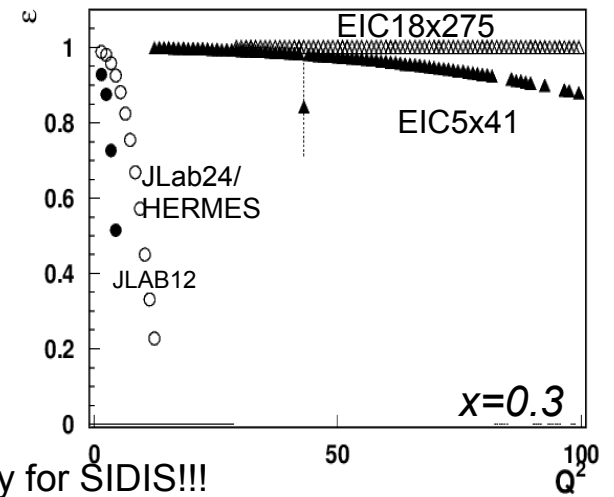
Combination of statistics and depolarization factors defines measurable SFs

Measurements of correlations of spin and transverse momenta provides direct access to details of QCD dynamics

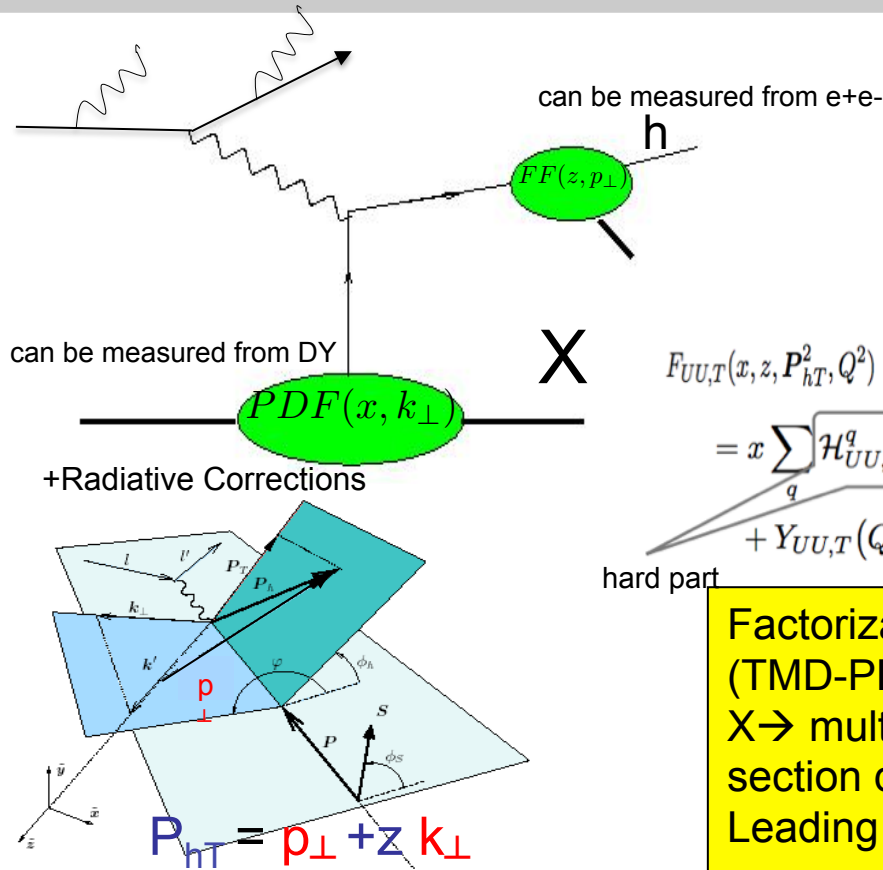
Measurements of  $F_{UU,T}$  and Sivers requires *separation*, evaluation of longitudinal photon (JLab)

Full decomposition of SFs to underlying 3D PDFs up to twist 3 level exist only for SIDIS!!!

$$\begin{aligned}
 & \frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h, \perp}^2} \quad \text{x-section for } eN \rightarrow e'hX \\
 &= \frac{\alpha^2}{x y Q^2} \frac{y^2}{2(1-\epsilon)} \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_h F_{UU}^{\cos \phi_h} + \epsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right. \\
 &+ \lambda_e \left[ \sqrt{2\epsilon(1-\epsilon)} \sin \phi_h F_{LU}^{\sin \phi_h} + S_L \left[ \sqrt{2\epsilon(1+\epsilon)} \sin \phi_h F_{UL}^{\sin \phi_h} + \epsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} \right] \right. \\
 &+ S_L \lambda_e \left[ \sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos \phi_h F_{LL}^{\cos \phi_h} \right] \\
 &+ S_T \left[ \sin(\phi_h - \phi_S) \left( F_{UT,T}^{\sin(\phi_h - \phi_S)} + \epsilon F_{UT,L}^{\sin(\phi_h - \phi_S)} \right) + \epsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right. \\
 &+ \epsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} + \sqrt{2\epsilon(1+\epsilon)} \sin \phi_S F_{UT}^{\sin \phi_S} \\
 &+ \left. \left. \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi_h - \phi_S) F_{UT}^{\sin(2\phi_h - \phi_S)} \right] + S_T \lambda_e \left[ \sqrt{1-\epsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} \right. \right. \\
 &+ \left. \left. \sqrt{2\epsilon(1-\epsilon)} \cos \phi_S F_{LT}^{\cos \phi_S} + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi_h - \phi_S) F_{LT}^{\cos(2\phi_h - \phi_S)} \right] \right\}
 \end{aligned}$$



# SIDIS as THE theory describes it



Probability to produce 1 or 2 hadrons in single photon exchange

$$\frac{d\sigma}{dx dy d\phi_S dz d\phi_h dP_{h\perp}^2} \quad eN \rightarrow e'hX$$

$F_{UU,T}(x, z, P_{hT}^2, Q^2)$  TMD Parton Distribution Functions TMD Parton Fragmentation Functions

$$= x \sum_q \mathcal{H}_{UU,T}^q(Q^2, \mu^2) \int d^2\mathbf{k}_{\perp} d^2\mathbf{P}_{\perp} f_1^a(x, \mathbf{k}_{\perp}^2; \mu^2) D_1^{a \rightarrow h}(z, \mathbf{P}_{\perp}^2; \mu^2) \delta(z\mathbf{k}_{\perp} - \mathbf{P}_{hT} + \mathbf{P}_{\perp})$$

+  $Y_{UU,T}(Q^2, P_{hT}^2) + \mathcal{O}(M^2/Q^2)$

hard part

Factorization allowing description using distribution functions (TMD-PDF) and fragmentation functions (TMD FF)  
 $X \rightarrow$  multiplicity of unobserved hadrons LARGE, and x-section doesn't depend on X (independent fragmentation)  
 Leading twist dominates,  
 $Q^2 \gg 1$   
 $k_{\perp}/Q \ll 1$

Conclusions in case of apparent disagreement:

- 1) factorization is broken?
- 2) unaccounted terms may contribute (assumptions are not good in certain kinematics,...)

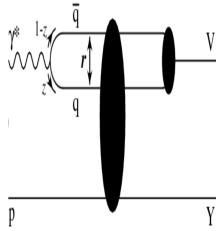
“much bigger/smaller” defined in comparison with experiment

Data has it all!!! Dealing with unaccounted terms:

- Theory accounts for them (ex. VMs)
- **Experiment measures and excludes them!!! (ex. VMs)**

# Theory predictions for transverse SSAs for rho

Goeke et al: hep-ph/0106012



$$A_{\rho_L^0 p} = \int_{-1}^1 dx \frac{1}{\sqrt{2}} (e_u H^u - e_d H^d) \left\{ \frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right\}$$

$$B_{\rho_L^0 p} = \int_{-1}^1 dx \frac{1}{\sqrt{2}} (e_u E^u - e_d E^d) \left\{ \frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right\}$$

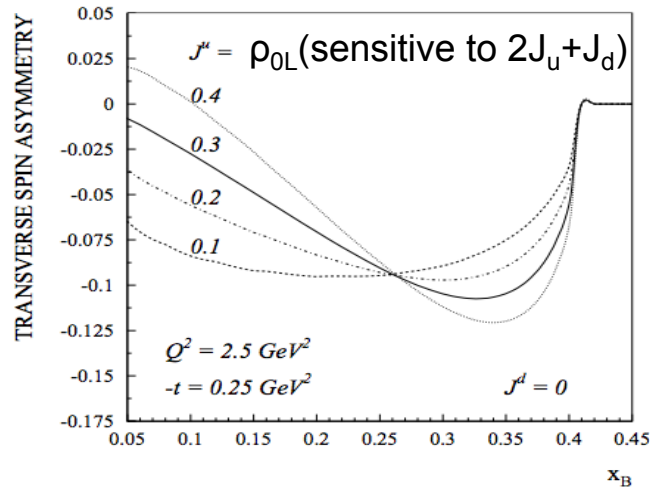
$$A_{\rho_L^+ n} = - \int_{-1}^1 dx (H^u - H^d) \left\{ \frac{e_u}{x - \xi + i\epsilon} + \frac{e_d}{x + \xi - i\epsilon} \right\}$$

$$B_{\rho_L^+ n} = - \int_{-1}^1 dx (E^u - E^d) \left\{ \frac{e_u}{x - \xi + i\epsilon} + \frac{e_d}{x + \xi - i\epsilon} \right\}$$

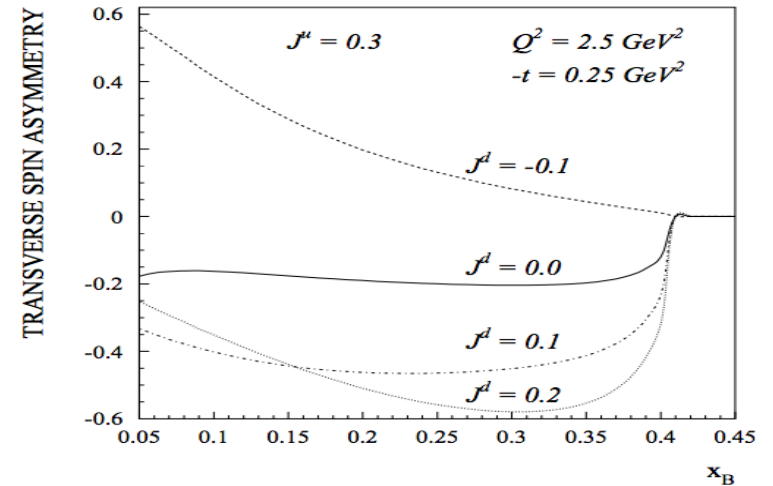
$$\frac{d\sigma_L}{dt} = \frac{1}{16\pi (s - m_N^2) \Lambda(s, -Q^2, m_N^2)} \frac{1}{2} \sum_{h_N} \sum_{h'_N} |\mathcal{M}^L(\lambda_M = 0, h'_N; h_N)|^2$$

$$\mathcal{A}_{V_L N} = - \frac{2 |\Delta_{\perp}|}{\pi} \frac{\text{Im}(AB^*)/m_N}{|A|^2 (1 - \xi^2) - |B|^2 (\xi^2 + t/(4m_N^2)) - \text{Re}(AB^*) 2\xi^2}$$

$\gamma_L^* + p \rightarrow \rho_L^0 + p$



$\rho_{+L}$  (sensitive to  $J_U - J_D$ )  
 $\gamma_L^* + p \rightarrow \rho_L^+ + n$



Significant SSAs predicted, sensitive to OAM contributions

# Theory predictions for transverse SSAs for rho

Goloskokov&Kroll 0809.4126

$$t_{\min} = -\frac{2\xi}{1-\xi^2} [(1+\xi)M^2 - (1-\xi)m^2]$$

$$\frac{d\sigma_{L(T)}}{dt} = \frac{1}{16\pi(W^2 - m^2)\sqrt{\Lambda(W^2, -Q^2, m^2)}} \sum_{\nu'} |\mathcal{M}_{0(+)\nu',0(+)+}|^2 \quad \xi \simeq \frac{x_{Bj}}{2-x_{Bj}} [1 + m_V^2/Q^2]$$

$$\Lambda(s, -Q^2, m_N^2) = 2m_N |\vec{q}_L|$$

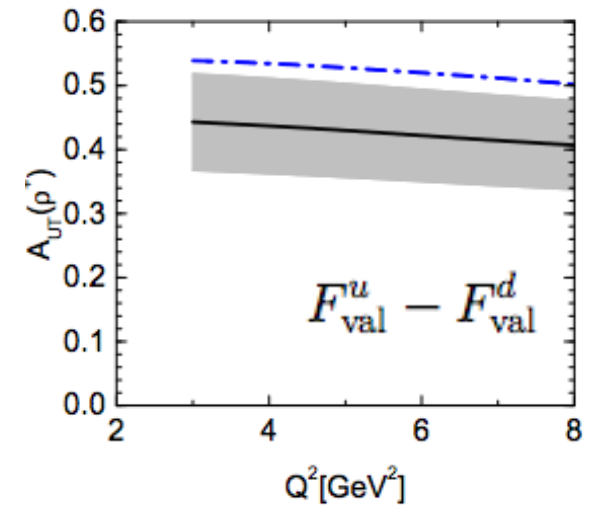
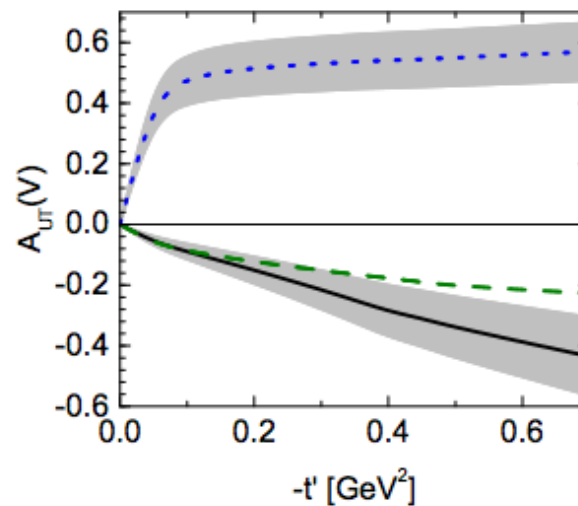
$$A_{UT} = -2 \frac{\text{Im}[\mathcal{M}_{+-,++}^* \mathcal{M}_{++,++}] + \varepsilon \text{Im}[\mathcal{M}_{0-,0+}^* \mathcal{M}_{0+,0+}]}{\sum_{\nu'} [|\mathcal{M}_{+\nu',++}|^2 + \varepsilon |\mathcal{M}_{0\nu',0+}|^2]}$$

$$\mathcal{M}_{\mu-, \mu+}(\rho^0) \sim \langle e_u E_{\text{val}}^u - e_d E_{\text{val}}^d \rangle$$

Opposite signs from HERMES!!

$$A_{UT}(\rho_L^0) = 0.04 \pm 0.12$$

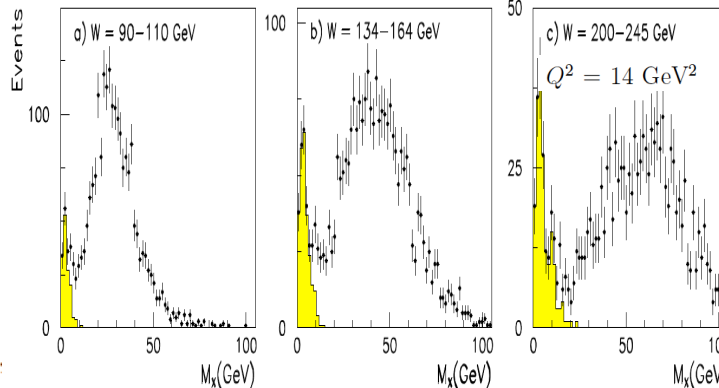
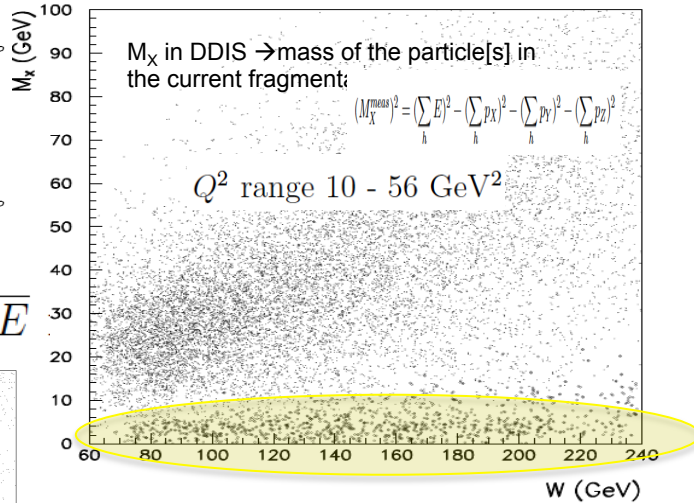
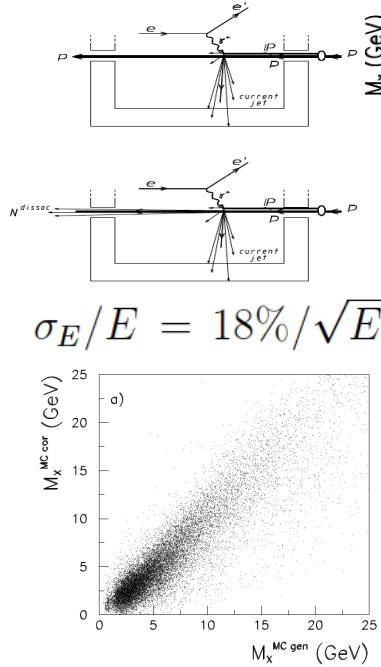
$$\bar{A}_{UT}(\rho_T^0) = -\hat{0}.08 \pm 0.10$$



Significant SSAs for VMs



# Measured x-section: DDIS vs DIS



Weak increase with  $W$  in photoproduction  
 Strong increase in electroproduction (longitudinal rho?)

$\eta$  is defined as  $-\ln(\tan \frac{\theta}{2})$ .

For  $\eta_{max} < 1.5$  the contribution from nondiffractive scattering is expected to be negligible

No dependence of DDIS/DIS on  $W$ , decrease with  $Q^2$  indicating the VMs can be the main contributor  
 At lowest  $M_x$  seem to be  $\sim 1/Q^2$ , at higher  $M_x$  there seem to be no  $Q^2$ -dependence

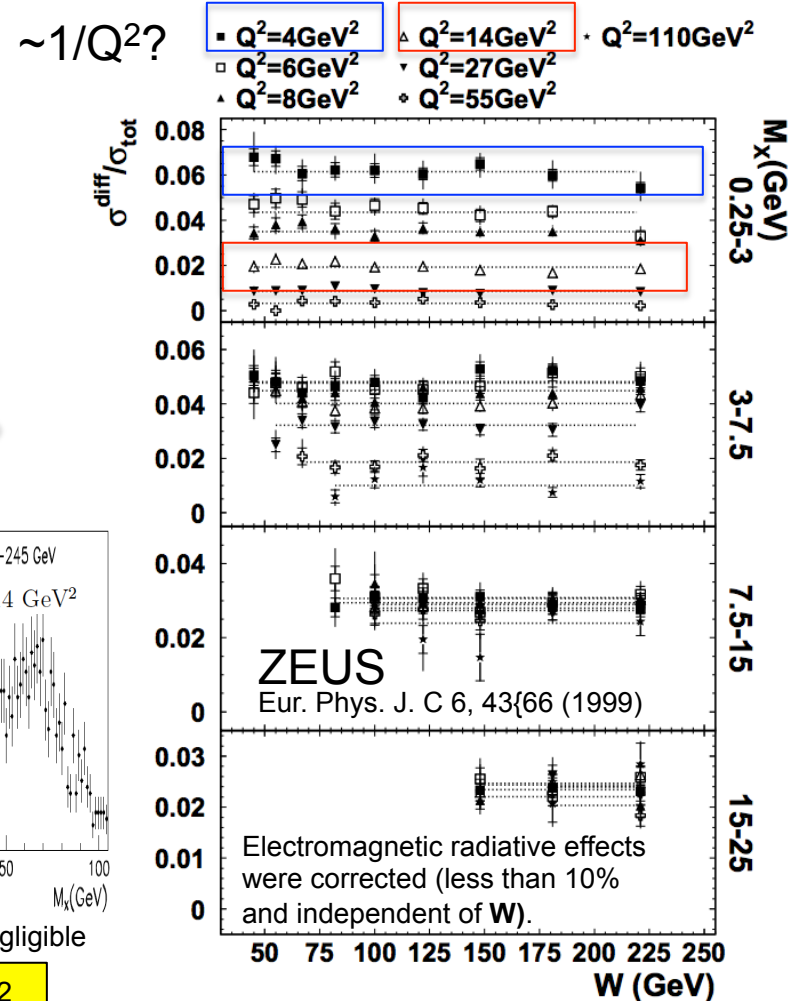
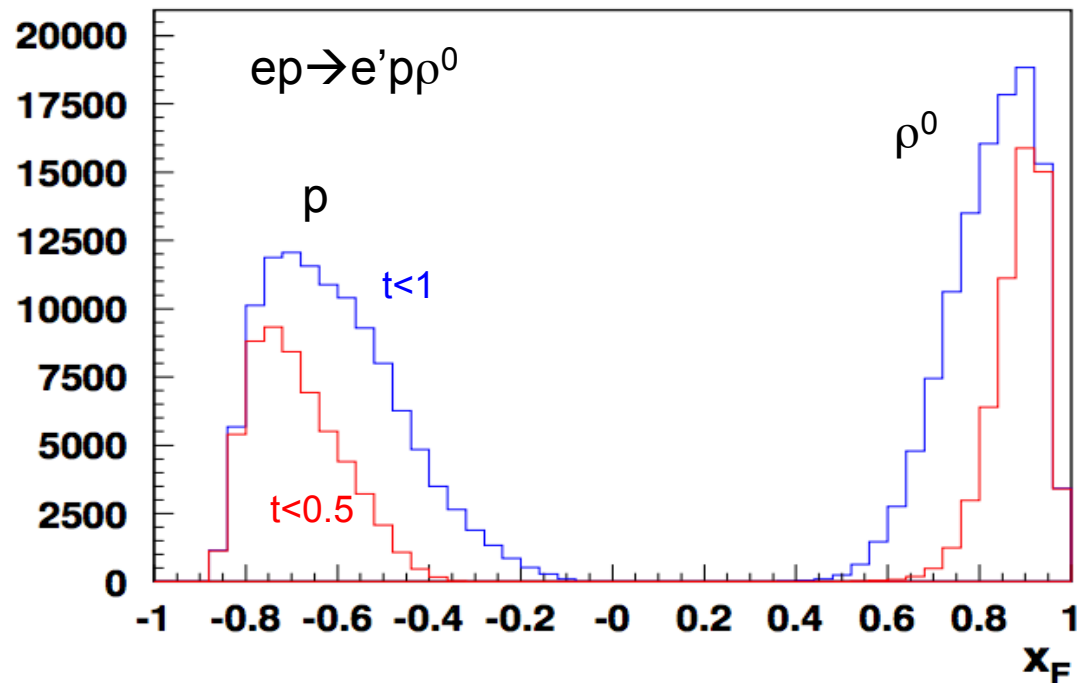
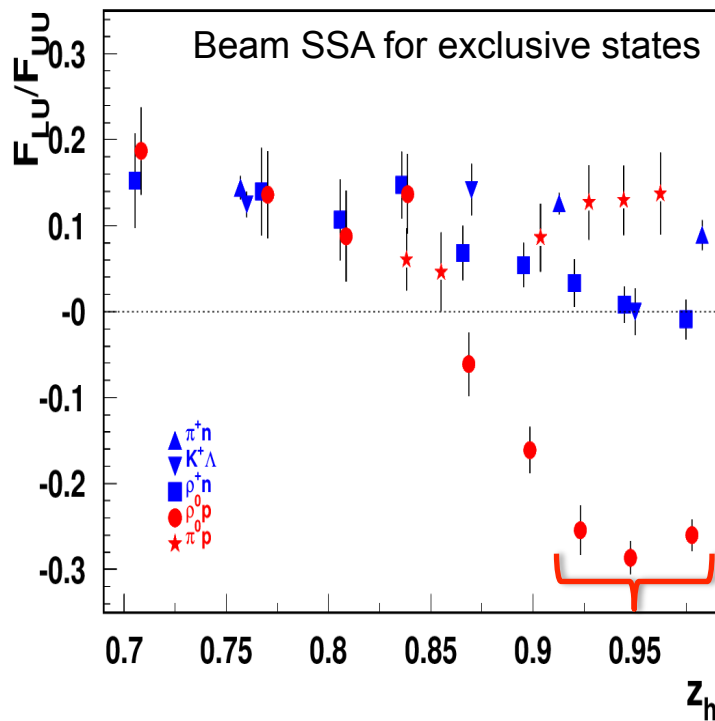
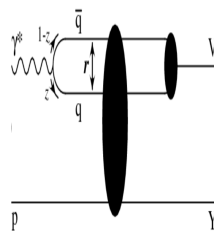


Figure 11.6: The ratio of the diffractive cross section  $\sigma^{diff}$ , integrated over the bin width  $M_a < M_x < M_b$ , and the total  $\gamma^*p$  cross section  $\sigma^{tot}$  is shown as a function of  $W$  for different bins of  $M_x$  and  $Q^2$ . The dotted lines indicate the average values of  $\sigma^{diff}/\sigma^{tot}$  in the measured  $W$  region for each bin in  $Q^2$  and  $M_x$ .

# “diffractive” VMs: rapidity gap



Diffractive VMs ( $\rho^0$ )



Significant rapidity gap between protons (backward) and rho (forward)

What is the fraction of VMs in DDIS?

What is the relative fraction of VMs as a function of  $W$  and  $Q^2$ ?

Identify kinematics of “diffractive”  $\rho^0$  by comparison with  $\rho^+$



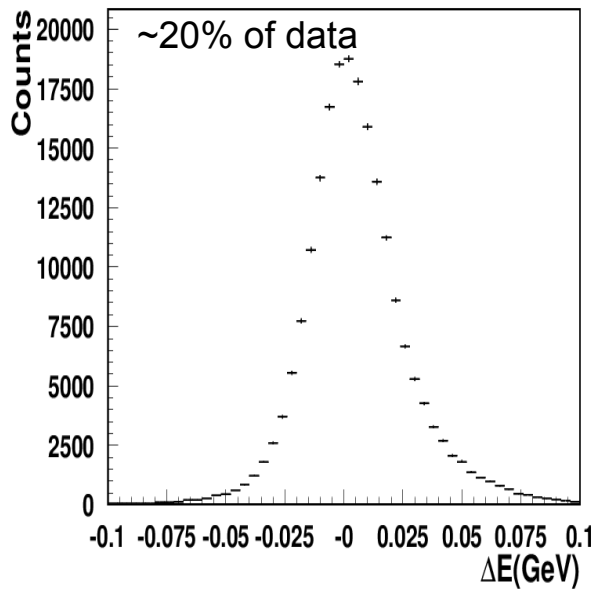
# CLAS12 Experiments involved: Exclusive rhos

Exclusivity condition defined by the missing Energy:

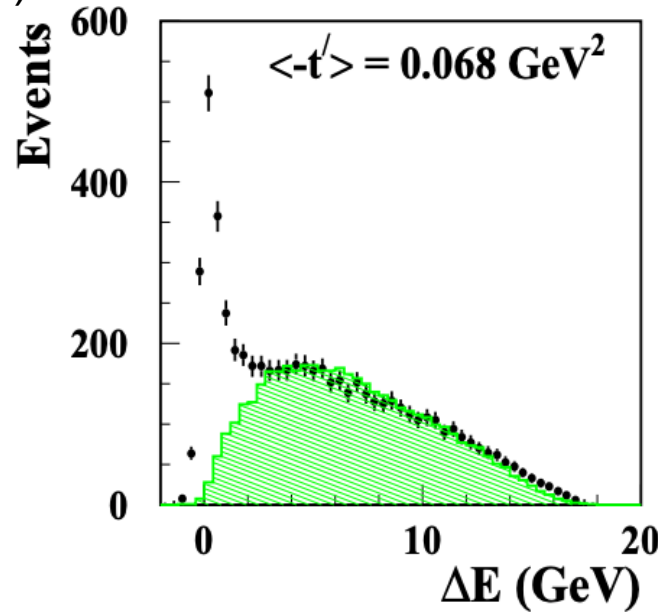
$$M_X^2 = (p + q - p_{\pi^+} - p_{\pi^-})^2$$

$$E_{\text{miss}} = \frac{M_X^2 - M^2}{2M}$$

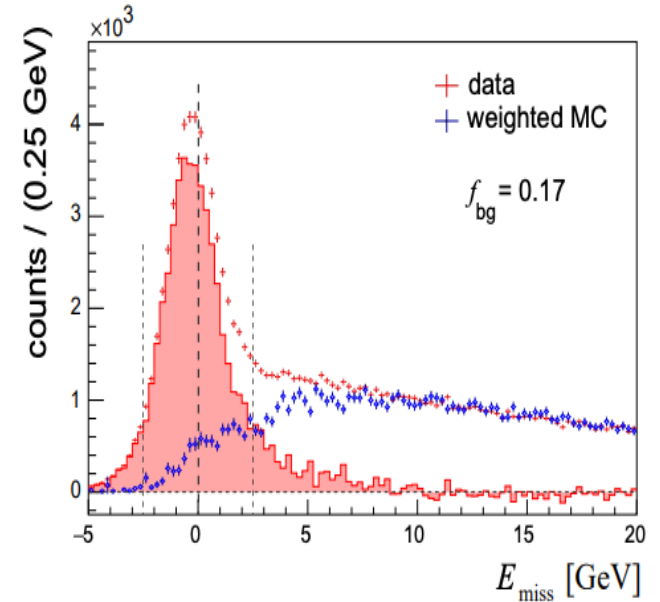
CLAS12 (width <0.1GeV)



HERMES(width ~0.6GeV)

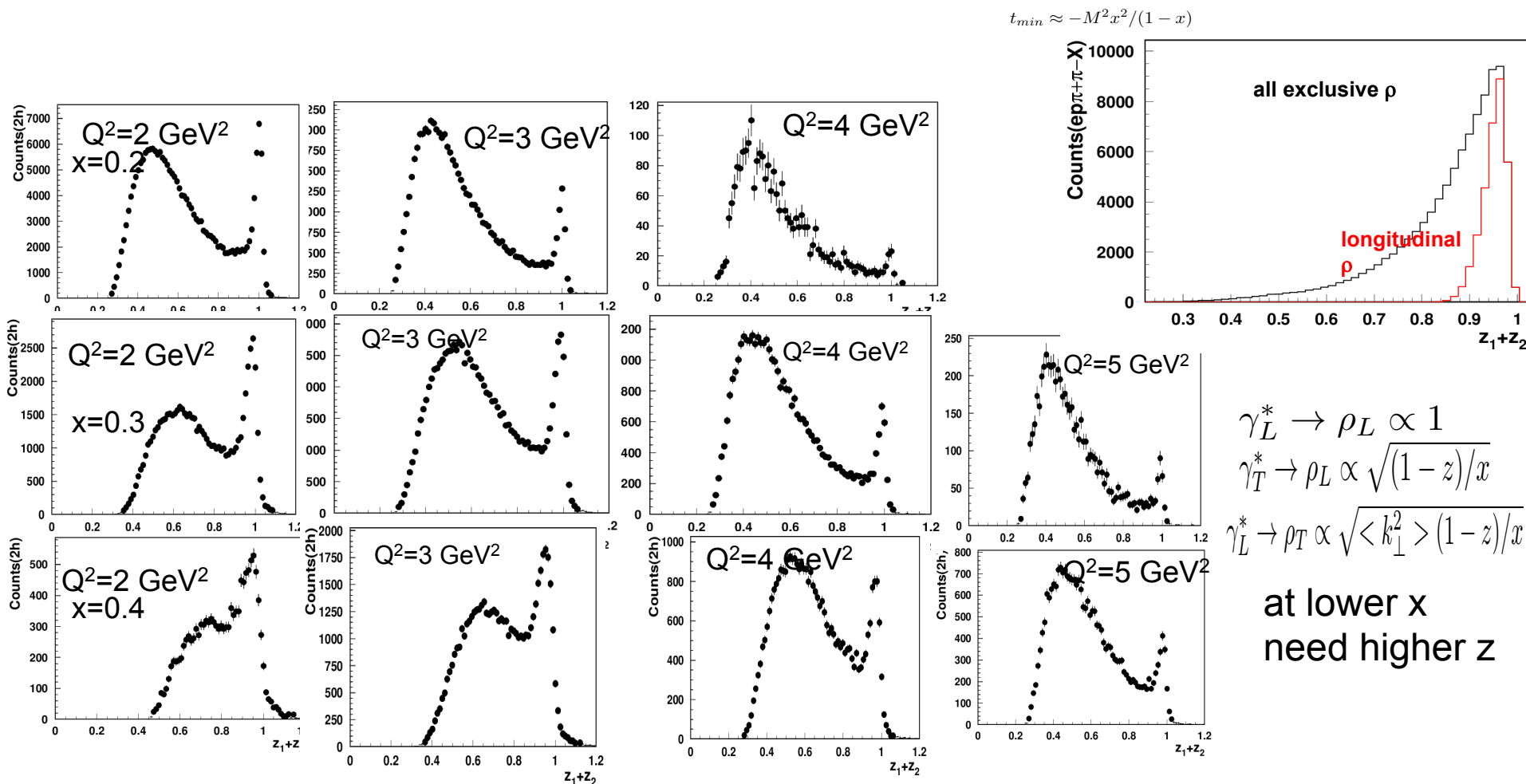


COMPASS(width ~2GeV)



- Guarantying the “exclusivity” requires **good resolutions** (get worse at higher energies)
- Subtraction procedure relays on normalization, based on exclusive limit of LUND-MC
- All distributions have tails, indicating the RC may not be negligible
- Extraction of SDMEs, will require validation in the multi-D space (significant samples)

# Exclusive dihadrons from CLAS12



The exclusive rho contributions in SIDIS drop with  $Q^2$  ( $\sim 1/Q^2$ )  
At large  $z = z_1 + z_2$  the transverse photon contributions to  $\rho_L$  suppressed

# VM contributions

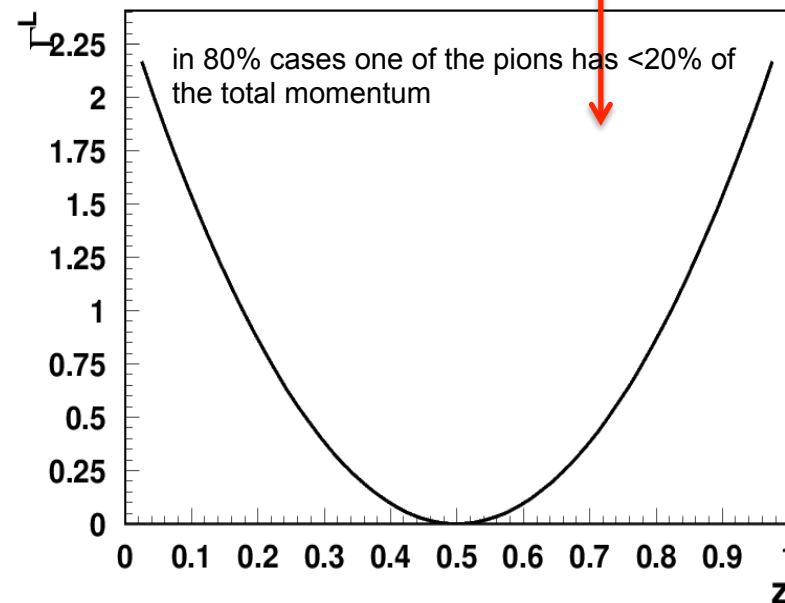
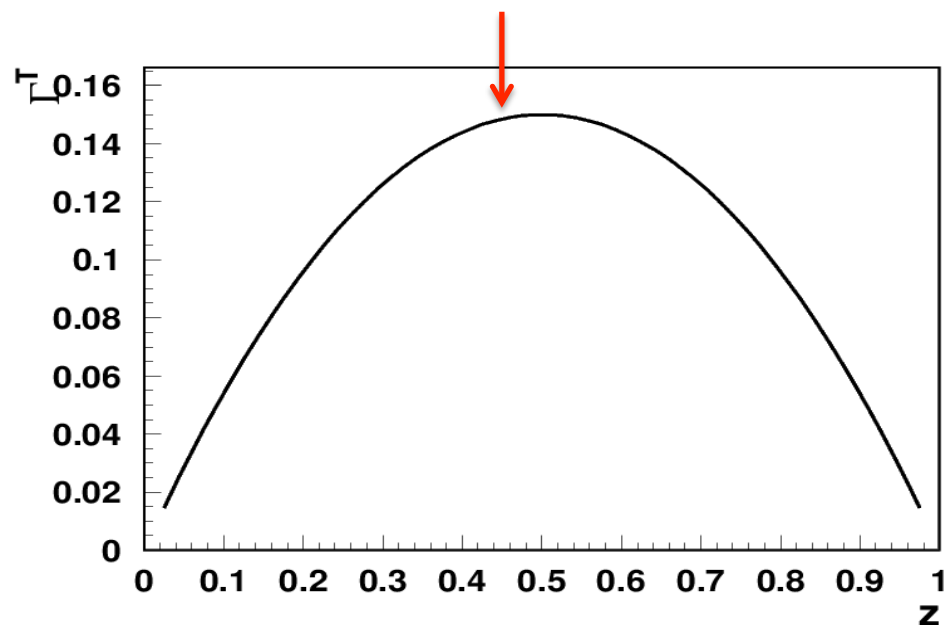
$$\rho^0 \rightarrow \pi^+ \pi^-$$

Yuri Kovchegov

$$k_T^2 = z(1-z) M_\rho^2 - m_\pi^2.$$

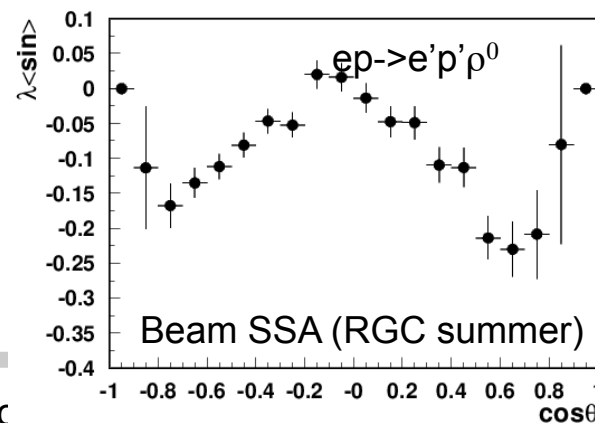
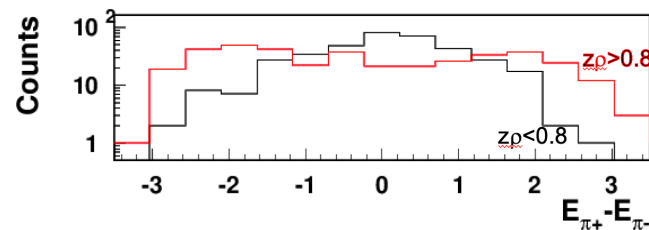
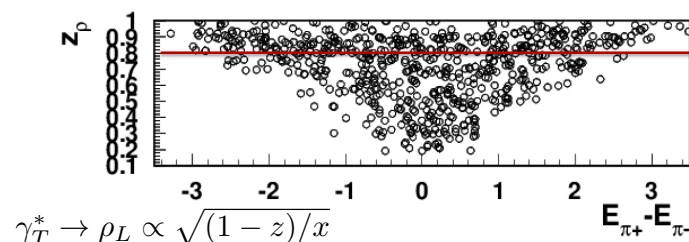
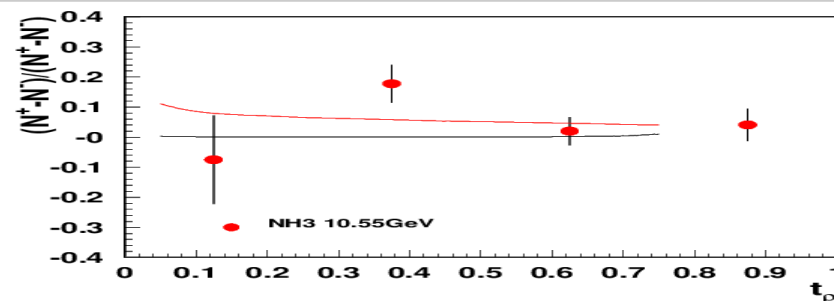
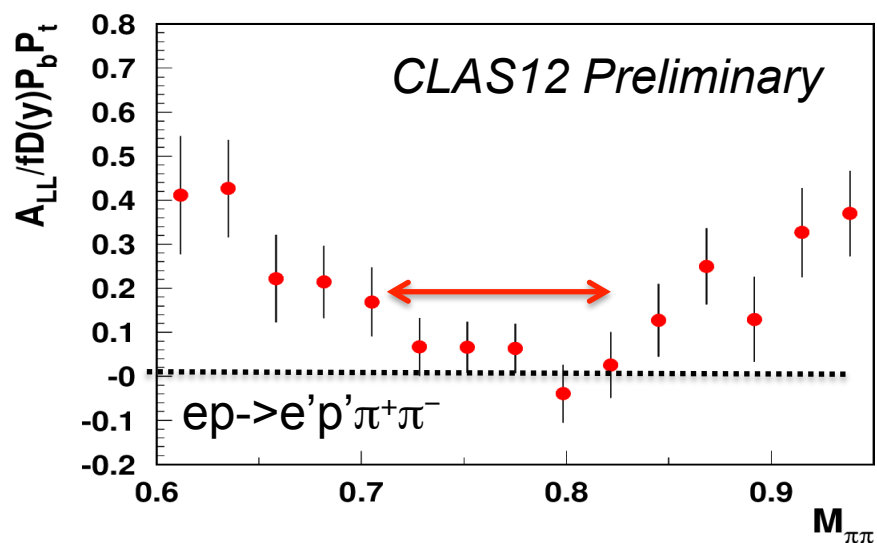
$$\Gamma_{\rho^0 \rightarrow \pi^+ \pi^-}^L \sim |M_{\rho^0 \rightarrow \pi^+ \pi^-}^L|^2 \sim \left| \frac{k_\perp^2 + m_\pi^2}{M_\rho} \left( \frac{1}{z} - \frac{1}{1-z} \right) + M_\rho (1-2z) \right|^2 = 4 M_\rho^2 (1-2z)^2.$$

$$\Gamma_{\rho^0 \rightarrow \pi^+ \pi^-}^T \sim k_T^2 \sim z(1-z) M_\rho^2 - m_\pi^2$$



Asymmetric decays of longitudinal rho lead to much smaller acceptance  
 Similar but inverted distributions for e+e- decays

# Studies of $\rho^0$ impact with longitudinally polarized $\text{NH}_3$ target

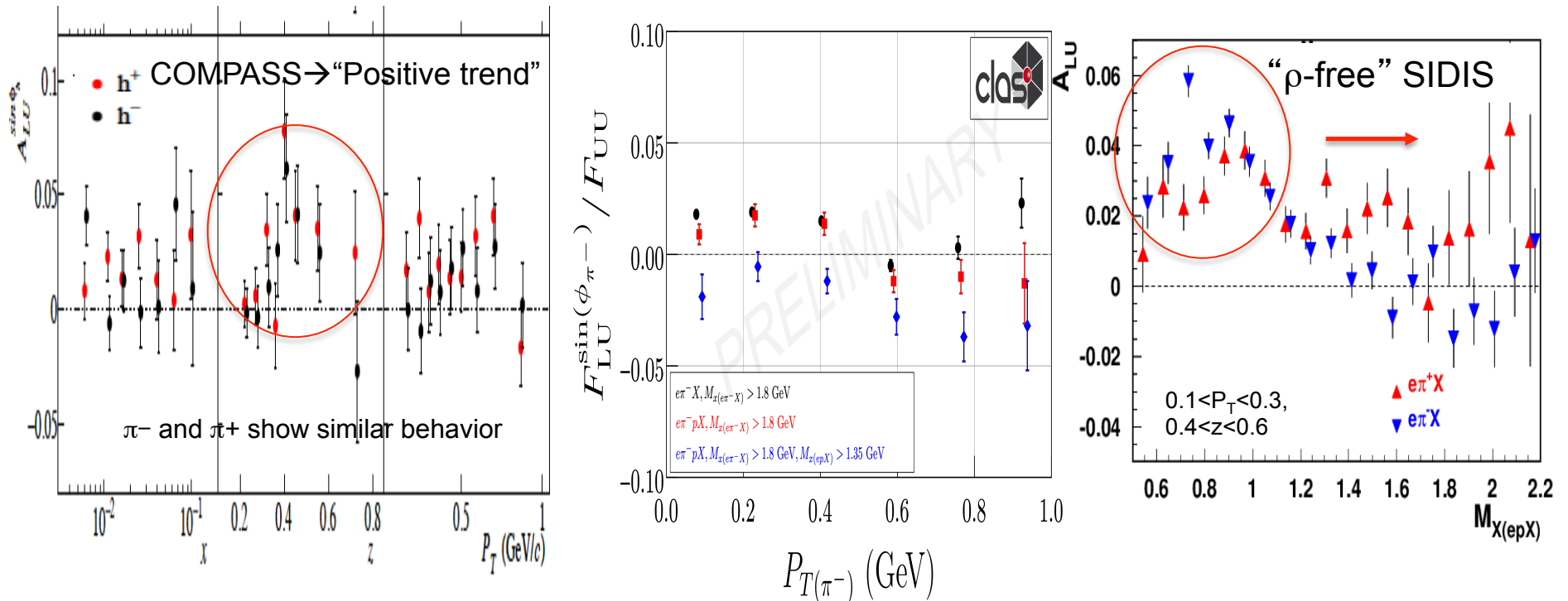


Need clear separation of hydrogen from  $\text{NH}_3$   
and diffractive exclusive  $\rho^0$ s from exclusive  $\pi^+\pi^-$

- DSA is P-even, SSA is P-odd
  - longitudinal photon cross section is P-odd
- contribution appears only in the SSA, a P-odd observable, and does not appear in DSA

With x10 less statistics than RGC, RGH can provide a significant measurement of  $\rho^0$  SSAs

# Exclusive $\rho$ contributions to $\pi$ : $P_T$ -dependence



COMPASS  $\rightarrow$  "Positive trend" also reproduced when additional proton in TFR detected (red)

- The same sign and size of  $\pi^+$  and  $\pi^-$  SSA indicates the  $\rho^0$  may not be properly subtracted (require detailed MC studies, which require proper SDMEs)
- While VM contributions are  $\sim 20\%$  in multiplicities in SSA they can be  $> 100\%$
- Detection of the target proton introduces much smaller bias on the inclusive charged pion SSA, than the exclusive  $\rho$  contributions

# SUMMARY

Measurements of diffractive exclusive  $\rho$  with transversely polarized target will be crucial for completeness of the measurements of 3D structure, including GPDs and TMDs

- Significant transverse single-spin asymmetries were predicted for exclusive  $\rho_0$  and  $\rho^+$
- CLAS12 has significant advantage compared to higher energy experiments in resolution and statistics, required for proper separation of exclusive VMs from semi-exclusive VMs, and separation of transverse rhos from longitudinal
- Target and beam SSAs and DSA can help to separate diffractive  $\rho$  from other exclusive and semi-exclusive processes
- The diffractive VM contributions, violate the factorized picture of SIDIS based on the dominance of the leading twist contributions, and detailed understanding of exclusive  $\rho$  contributions in the multi-D space will be critical to address the challenges of phenomenology (“ $\rho$ -subtracted SIDIS”)

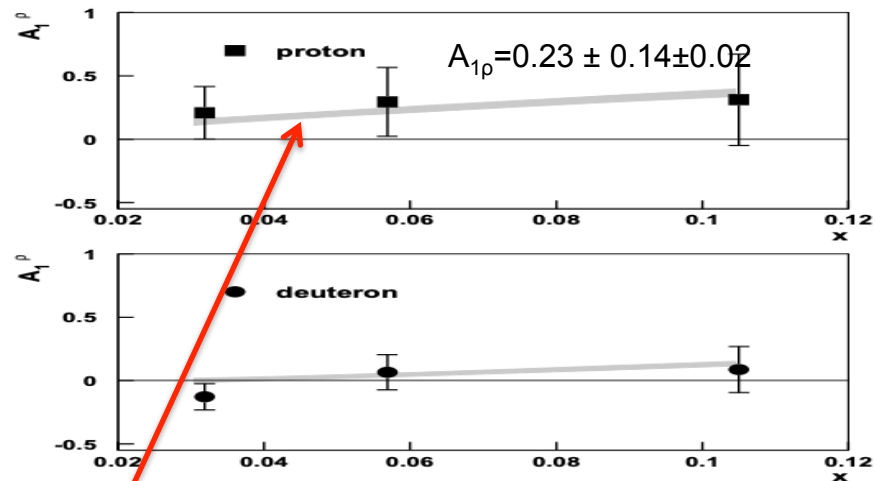
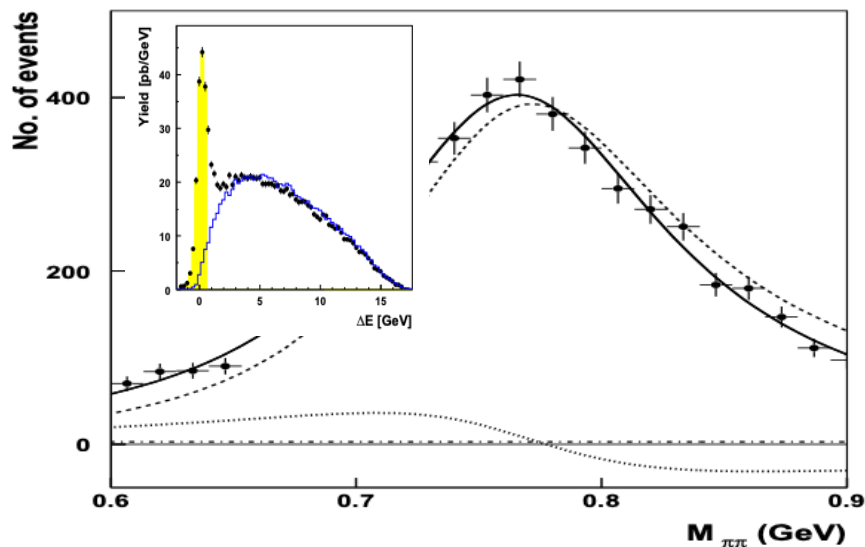
Submit a proposal to study SSAs for exclusive VMs with transversely polarized target  
→run group extension to RGH (involved Duke, MSU, Argonne, Duquesne)

Combine efforts of CLAS+COMPASS communities (ex. generator development) in understanding the diffractive  $\rho$  and sort out the impact on OAM, TMD-PDFs, including the helicity and Sivers



- 
- support slides

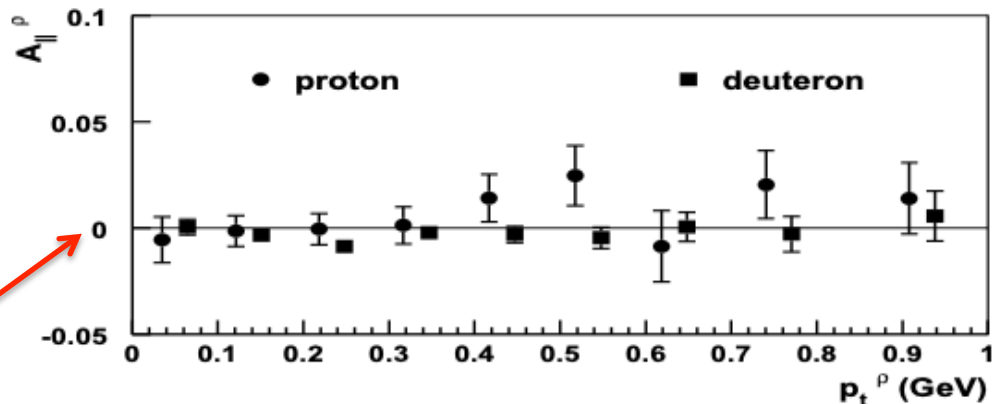
# $A_{LL}$ studies of exclusive $\rho^0$ : HERMES



1D plots can be really misleading need multi-D

For a proper extraction of multiplicities and spin-azimuthal modulations of exclusive  $\rho$ s, clean separation is needed for  $\rho^0$ , and longitudinally polarized  $\rho^0$  signal, in particular

At low  $P_T$ , where the background is smaller, the asymmetry indeed tend to be negative



Accounting of  $\rho^0$  will change the phenomenology of helicity distributions

# Excluding the “diffractive” rho from SIDIS

Depending on how we exclude the exclusive rho we can have several versions of experimental samples of inclusive hadrons, each with their own bias:

1) Standard SIDIS ( $eN \rightarrow ehX$ ,  $h=\pi, K, \dots$ ) within the full accessible kinematics, corrected for acceptance and RC, measured in the multidimensional space

→  $e\pi X$  biased with respect to theory by presence of contributions from diffractive rho, contributing to ~20% of counts, in low  $P_T$ , with contributions to SSA ~10 times higher

2) Standard SIDIS ( $eN \rightarrow e\pi X$ ) within the full accessible kinematics, corrected for acceptance and RC, measured in the multidimensional space, with subtracted in multi-D bins for rho0 contributions (“rho-subtracted SIDIS”)

→ requires measurements of pions from diffractive rho in multidimensional space, means detailed studies of SDMEs of rhos, requiring good precisions and huge statistics, develop MC (ex. HEPGEN) also for all polarization observables, extensive validation needed, little known RC

3) SIDIS subsamples ( $eN \rightarrow ep\pi X$ ,  $eN \rightarrow e\pi\pi X$ ) within the full accessible kinematics, allowing clear elimination of rho0 contributions using cuts on missing masses of  $epX$  or  $e\pi\pi X$

(“rho-free SIDIS”)

→ biased by the presence of additional hadron in TFR ( $epX$ ) or CFR ( $eppX$ ), may need a new phenomenology

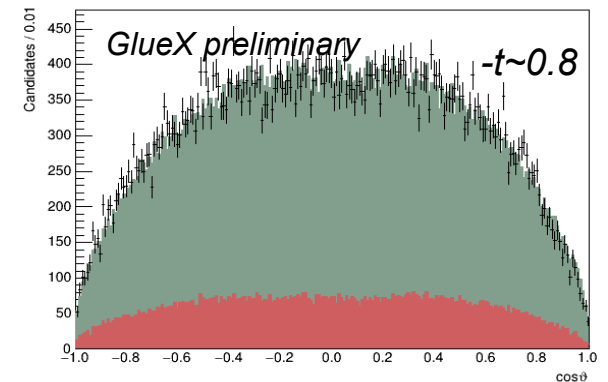
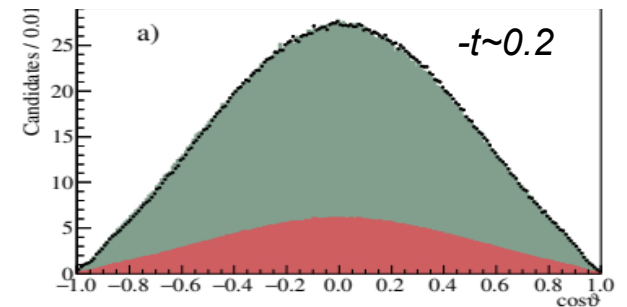
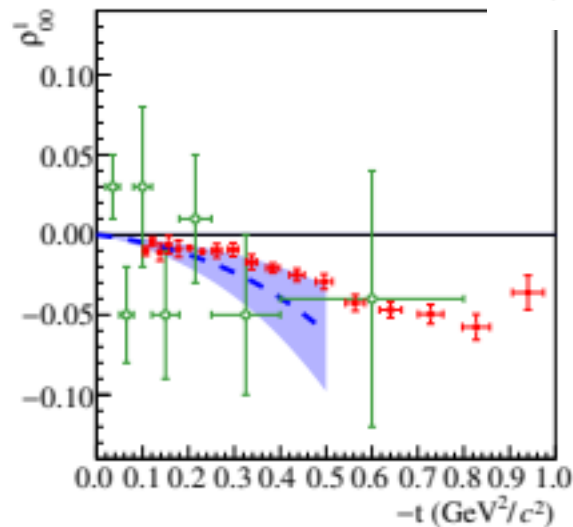
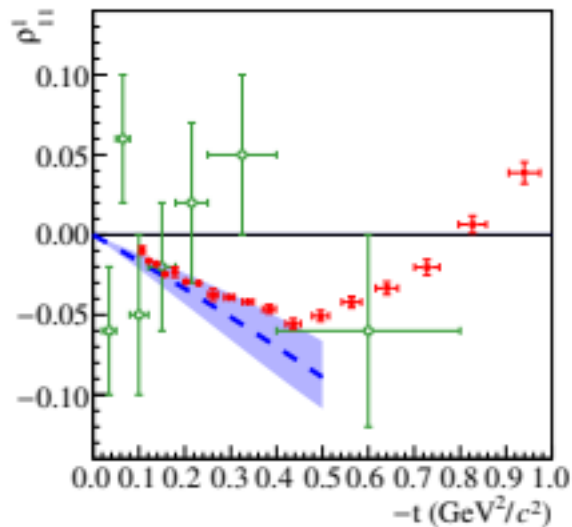
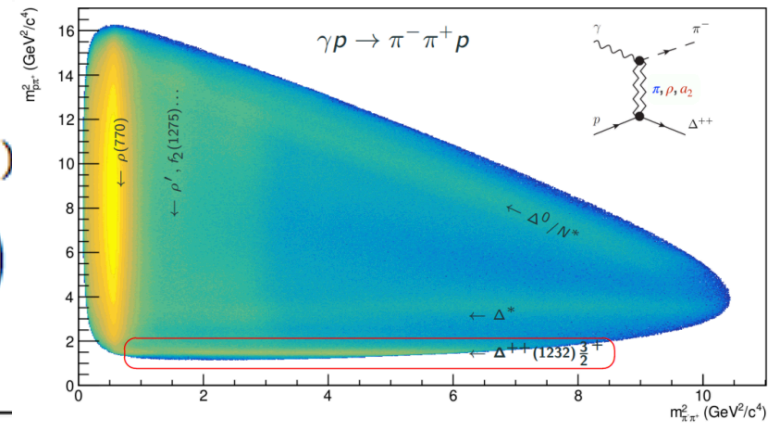
requires measurements of dependence on  $M_X$  to understand the bias,

Theory should be able to evaluate the bias from the presence of an additional hadron

# SDMEs from photoproduction

JLab/GlueX, S. Adhikari et al, Phys.Rev.C 108 (2023), 055204: ArXiv:2305.09047

$$W^1(\cos\vartheta, \varphi) = \frac{3}{4\pi} (\rho_{11}^1 \sin^2\vartheta + \rho_{00}^1 \cos^2\vartheta - \sqrt{2}\text{Re}\rho_{10}^1 \sin 2\vartheta \cos\varphi - \rho_{1-1}^1 \sin^2\vartheta \cos 2\varphi) \quad (11)$$

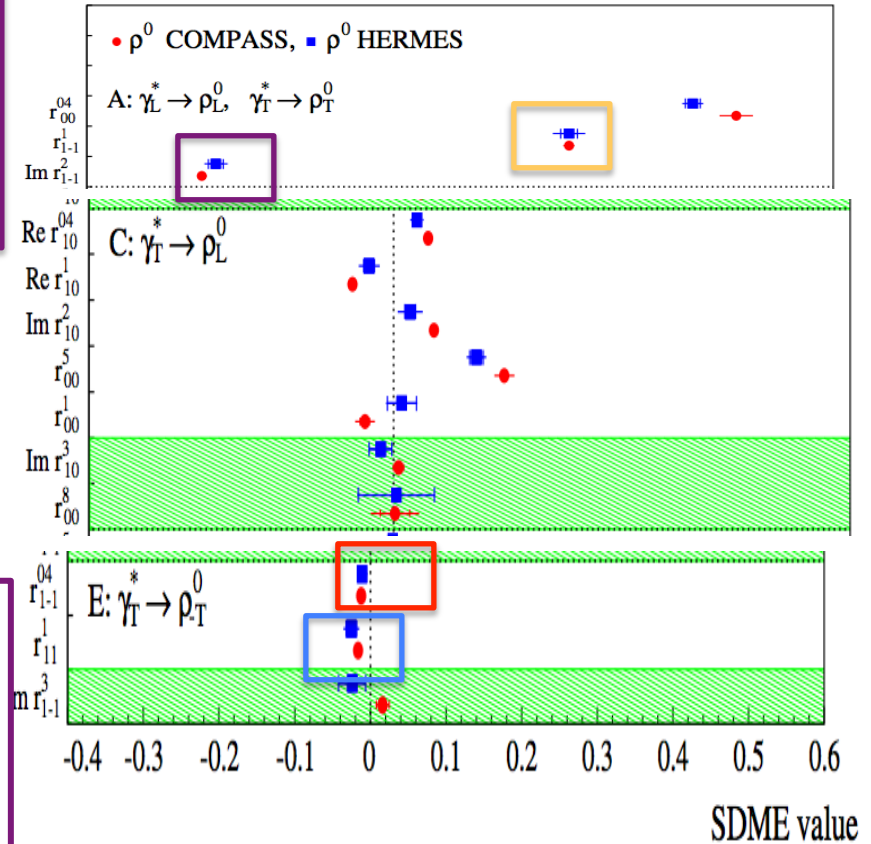
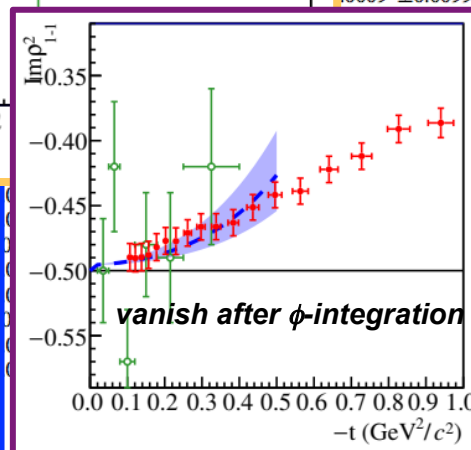
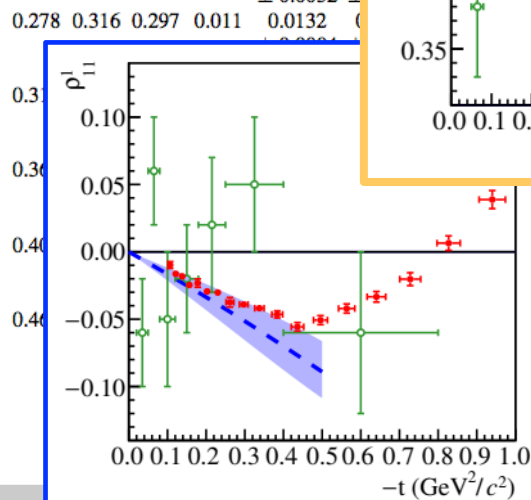
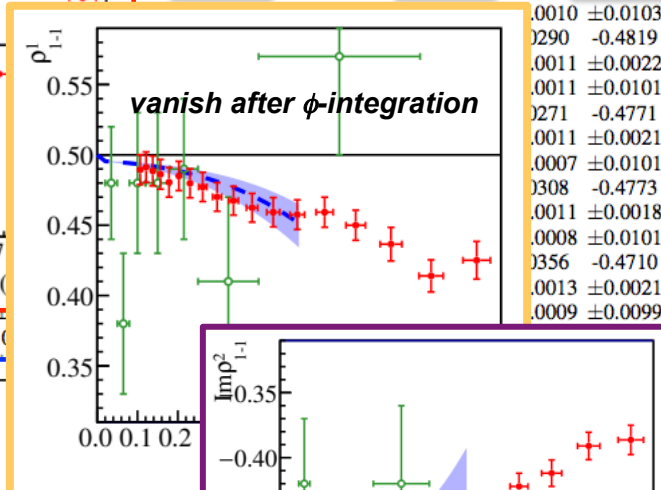
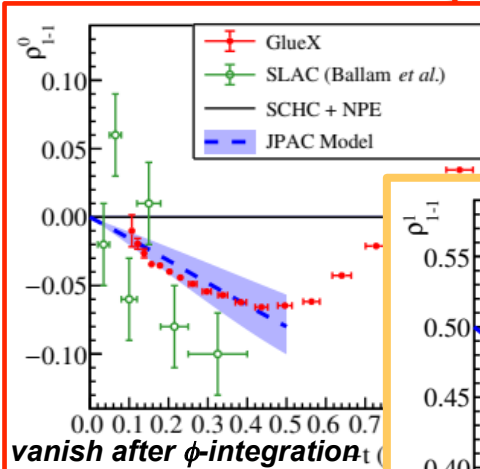


While at small  $t$  (dominant part of the statistics) the transverse rhos dominate, at large  $t$  the contribution from transverse photons going to longitudinal rho becomes more significant

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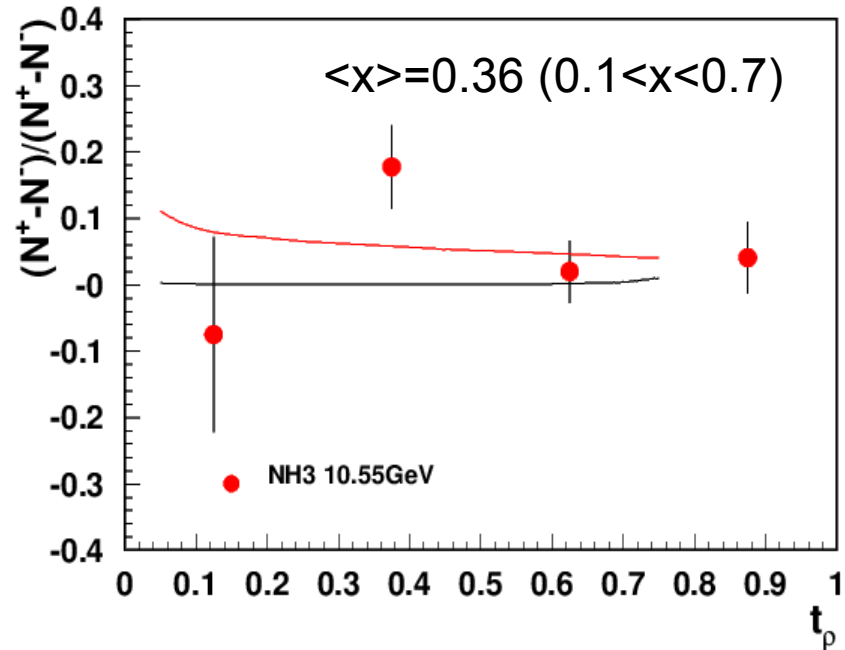
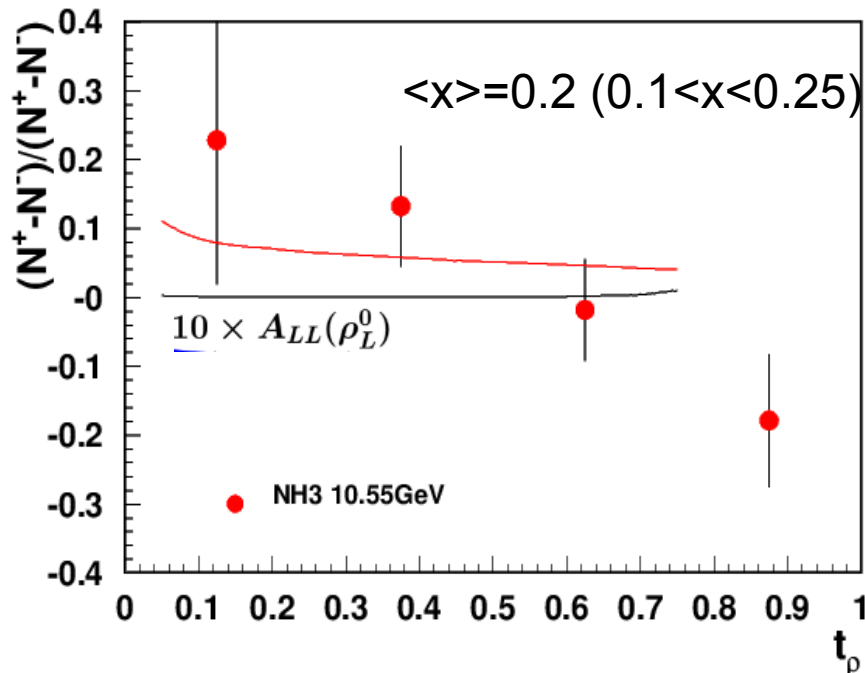
JLab/Gluex. S. Adhikari et al: <https://arxiv.org/pdf/2305.09047>

| $-t_{\min}$ | $-t_{\max}$ | $-\bar{t}$ | $-t_{\text{RMS}}$ | $\rho_{00}^0$ | $\text{Re}\rho_{10}^0$ | $\rho_{1-1}^0$ | $\rho_{11}^1$ | $\rho_{00}^1$ | $\text{Re}\rho_{10}^1$ | $\rho_{1-1}^1$ | $\text{Im}\rho_{10}^2$ | $\text{Im}\rho_{1-1}^2$ |
|-------------|-------------|------------|-------------------|---------------|------------------------|----------------|---------------|---------------|------------------------|----------------|------------------------|-------------------------|
| 0.100       | 0.114       | 0.107      | 0.004             | 0.0008        | 0.0171                 | -0.0100        | -0.0098       | -0.0101       | -0.0252                | 0.4895         | 0.0200                 | -0.4897                 |
|             |             |            |                   | $\pm 0.0003$  | $\pm 0.0005$           | $\pm 0.0007$   | $\pm 0.0020$  | $\pm 0.0010$  | $\pm 0.0020$           | $\pm 0.0024$   | $\pm 0.0014$           | $\pm 0.0023$            |
|             |             |            |                   | $\pm 0.0045$  | $\pm 0.0066$           | $\pm 0.0116$   | $\pm 0.0016$  | $\pm 0.0025$  | $\pm 0.0012$           | $\pm 0.0103$   | $\pm 0.0010$           | $\pm 0.0104$            |
| 0.114       | 0.129       | 0.121      | 0.004             | 0.0025        | 0.0209                 | -0.0194        | -0.0163       | -0.0043       | -0.0247                | 0.4914         | 0.0205                 | -0.4904                 |
|             |             |            |                   | $\pm 0.0018$  | $\pm 0.0012$           | $\pm 0.0017$   | $\pm 0.0025$  | $\pm 0.0013$  | $\pm 0.0022$           | $\pm 0.0011$   | $\pm 0.0021$           | $\pm 0.0022$            |
|             |             |            |                   | $\pm 0.0015$  | $\pm 0.0026$           | $\pm 0.0014$   | $\pm 0.0105$  | $\pm 0.0012$  | $\pm 0.0103$           | $\pm 0.0011$   | $\pm 0.0103$           | $\pm 0.0103$            |
|             |             |            |                   | $\pm 0.0182$  | $\pm 0.0108$           | $\pm 0.0257$   | $\pm 0.4886$  | $\pm 0.0257$  | $\pm 0.4896$           | $\pm 0.0257$   | $\pm 0.4896$           | $\pm 0.4896$            |
|             |             |            |                   | $\pm 0.0017$  | $\pm 0.0010$           | $\pm 0.0017$   | $\pm 0.0022$  | $\pm 0.0011$  | $\pm 0.0021$           | $\pm 0.0011$   | $\pm 0.0021$           | $\pm 0.0021$            |
|             |             |            |                   | $\pm 0.0018$  | $\pm 0.0052$           | $\pm 0.0015$   | $\pm 0.0104$  | $\pm 0.0011$  | $\pm 0.0103$           | $\pm 0.0011$   | $\pm 0.0103$           | $\pm 0.0103$            |
|             |             |            |                   | $\pm 0.0246$  | $\pm 0.0061$           | $\pm 0.0297$   | $\pm 0.4862$  | $\pm 0.0287$  | $\pm 0.4879$           | $\pm 0.0287$   | $\pm 0.4879$           | $\pm 0.4879$            |
|             |             |            |                   | $\pm 0.0017$  | $\pm 0.0010$           | $\pm 0.0015$   | $\pm 0.0023$  | $\pm 0.0011$  | $\pm 0.0020$           | $\pm 0.0011$   | $\pm 0.0020$           | $\pm 0.0020$            |



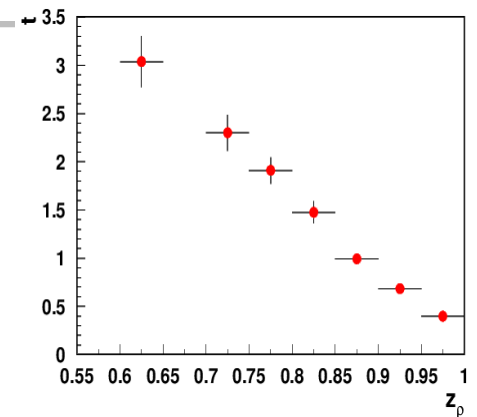
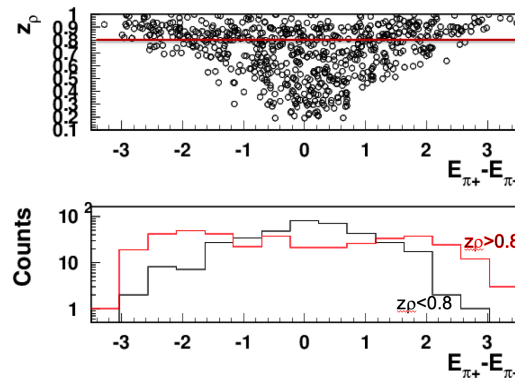
The SDMEs for transverse photons with  $\sin^2\theta$  (to transverse rho?) at  $Q^2 > 0$  seem to be smaller (detailed comparison vs  $Q^2$ ).

# What is the gluon polarization at large x?



Curves calculated by Kroll & Goloskokov ( $x=0.12$ )  
 The full sample would allow fine binning in  $t_p$   
 and separation of longitudinal/transverse  $\rho$

Polarization of rho

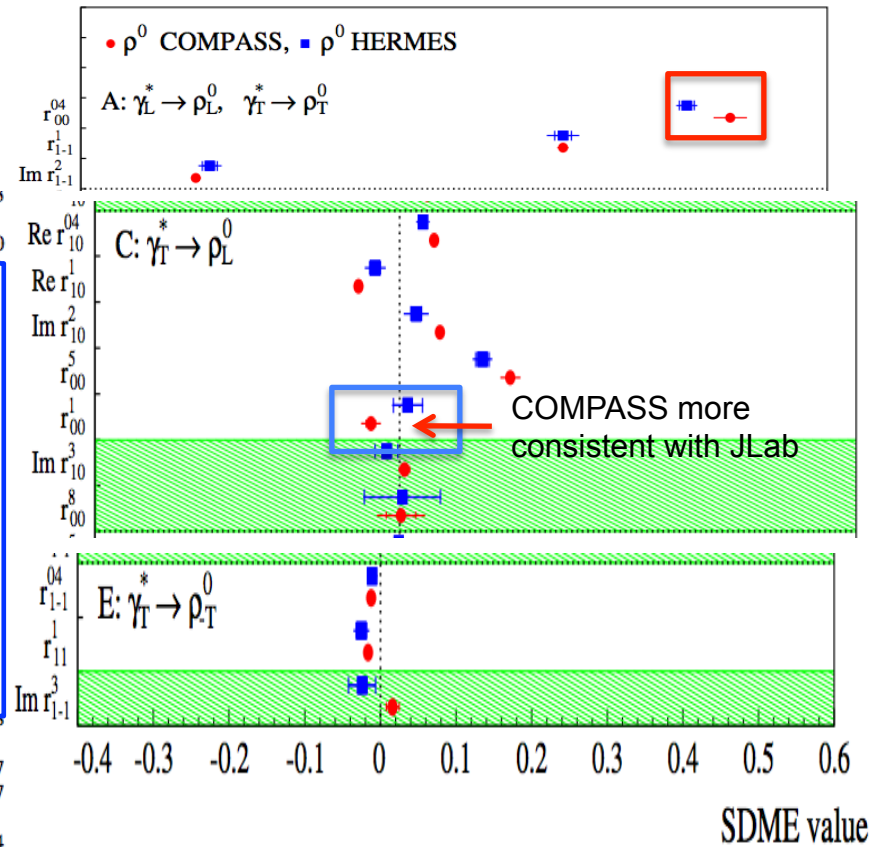
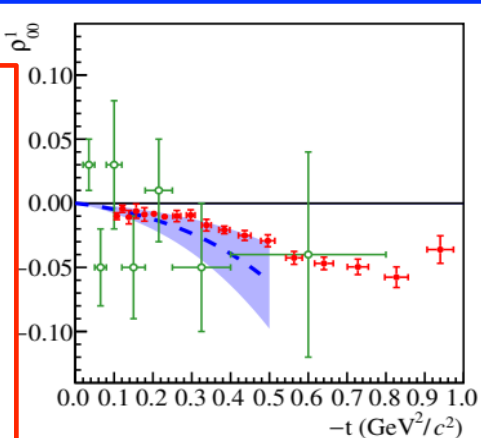
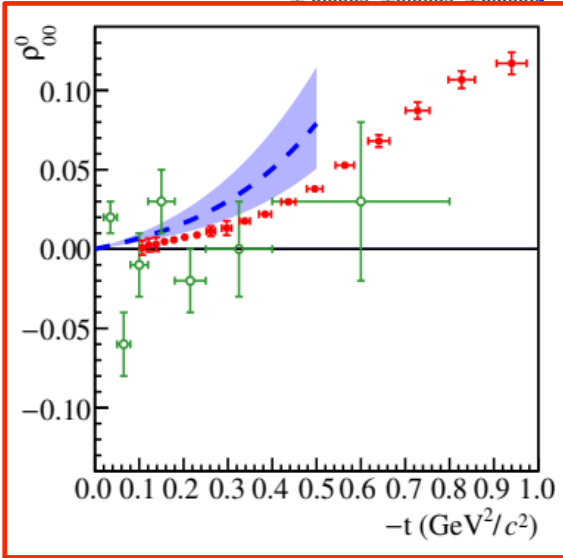




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JLab/Gluex. S. Adhikari et al: <https://arxiv.org/pdf/2305.09047>

| $-t_{\min}$ | $-t_{\max}$ | $-\bar{t}$ | $-t_{\text{RMS}}$ | $\rho_{00}^0$ | $\text{Re}\rho_{10}^0$ | $\rho_{1-1}^0$ | $\rho_{11}^0$ | $\rho_{00}^1$ | $\text{Re}\rho_{10}^1$ | $\rho_{1-1}^1$ | $\text{Im}\rho_{10}^2$ | $\text{Im}\rho_{1-1}^2$ |
|-------------|-------------|------------|-------------------|---------------|------------------------|----------------|---------------|---------------|------------------------|----------------|------------------------|-------------------------|
| 0.100       | 0.114       | 0.107      | 0.004             | 0.0008        | 0.0171                 | -0.0100        | -0.0098       | -0.0101       | -0.0252                | 0.4895         | 0.0200                 | -0.4897                 |
|             |             |            |                   | $\pm 0.0003$  | $\pm 0.0005$           | $\pm 0.0007$   | $\pm 0.0020$  | $\pm 0.0010$  | $\pm 0.0020$           | $\pm 0.0024$   | $\pm 0.0014$           | $\pm 0.002$             |
|             |             |            |                   | $\pm 0.0045$  | $\pm 0.0066$           | $\pm 0.0116$   | $\pm 0.0016$  | $\pm 0.0025$  | $\pm 0.0012$           | $\pm 0.0103$   | $\pm 0.0010$           | $\pm 0.010$             |
| 0.114       | 0.129       | 0.121      | 0.004             | 0.0025        | 0.0209                 | -0.0194        | -0.0063       | -0.0043       | -0.0242                | 0.4914         | 0.0205                 | -0.4904                 |
|             |             |            |                   | $\pm 0.0003$  | $\pm 0.0004$           | $\pm 0.0006$   | $\pm 0.0018$  | $\pm 0.0012$  | $\pm 0.0017$           | $\pm 0.0025$   | $\pm 0.0013$           | $\pm 0.002$             |
|             |             |            |                   | $\pm 0.0042$  | $\pm 0.0030$           | $\pm 0.0038$   | $\pm 0.0015$  | $\pm 0.0026$  | $\pm 0.0014$           | $\pm 0.0105$   | $\pm 0.0012$           | $\pm 0.010$             |
| 0.129       | 0.147       | 0.138      | 0.005             | 0.0030        | 0.0244                 | -0.0264        | -0.0082       | -0.0108       | -0.0257                | 0.4886         | 0.0257                 | -0.4896                 |
|             |             |            |                   | $\pm 0.0003$  | $\pm 0.0004$           | $\pm 0.0006$   | $\pm 0.0017$  | $\pm 0.0010$  | $\pm 0.0017$           | $\pm 0.0022$   | $\pm 0.0011$           | $\pm 0.002$             |
|             |             |            |                   | $\pm 0.0044$  | $\pm 0.0023$           | $\pm 0.0032$   | $\pm 0.0018$  | $\pm 0.0052$  | $\pm 0.0015$           | $\pm 0.0104$   | $\pm 0.0011$           | $\pm 0.0105$            |
| 0.147       | 0.167       | 0.157      | 0.006             | 0.0047        | 0.0283                 | -0.0344        | -0.0046       | -0.0061       | -0.0294                | 0.4862         | 0.0287                 | -0.4879                 |
|             |             |            |                   | $\pm 0.0002$  | $\pm 0.0004$           | $\pm 0.0005$   | $\pm 0.0010$  | $\pm 0.0010$  | $\pm 0.0016$           | $\pm 0.0023$   | $\pm 0.0012$           | $\pm 0.0020$            |
|             |             |            |                   | $\pm 0.0022$  | $\pm 0.0011$           | $\pm 0.0009$   |               |               |                        |                |                        |                         |
| 0.167       | 0.190       | 0.178      | 0.007             | 0.0058        | 0.0295                 | -0.0353        |               |               |                        |                |                        |                         |
|             |             |            |                   | $\pm 0.0003$  | $\pm 0.0003$           | $\pm 0.0006$   |               |               |                        |                |                        |                         |



The SDMEs for transverse photons with  $\cos^2\theta$  (to longitudinal rho?) at  $Q^2 > 0$  different, in particular  $r_{00}^1$  (relevant for BM).

# Understanding exclusive rhos and SDME validations

$$\mathcal{W}^U(\Phi, \phi, \cos \Theta)$$

$$+ \sqrt{2\epsilon(1+\epsilon)} \cos \Phi (r_{11}^5 \sin^2 \Theta + r_{00}^5 \cos^2 \Theta)$$

corr. with  $r_{1-1}^5, r_{1-1}^6, r_{00}^5$  (Hermes, COMPASS)

$$\mathcal{W}^L(\Phi, \phi, \cos \Theta)$$

$$+ \sqrt{2\epsilon(1-\epsilon)} \sin \Phi (r_{11}^8 \sin^2 \Theta + r_{00}^8 \cos^2 \Theta - \sqrt{2} \operatorname{Re}\{r_{10}^8\} \sin 2\Theta \cos \phi - r_{1-1}^8 \sin^2 \Theta \cos 2\phi)$$

corr. with  $r_{1-1}^8, r_{00}^8$  (Hermes, COMPASS)

$$\gamma_L^* \rightarrow \rho_T^0, \tau_{10} \approx \frac{\sqrt{(r_{11}^5 + \operatorname{Im}\{r_{1-1}^6\})^2 + (\operatorname{Im}\{r_{1-1}^7\} - r_{11}^8)^2}}{\sqrt{2(r_{1-1}^1 - \operatorname{Im}\{r_{1-1}^2\})}}$$

Since the decay angle is correlated with the polarization of the rho, then  $r_{11}^8$  and  $r_{11}^5$  will be responsible for transverse rho (no Cahn?)

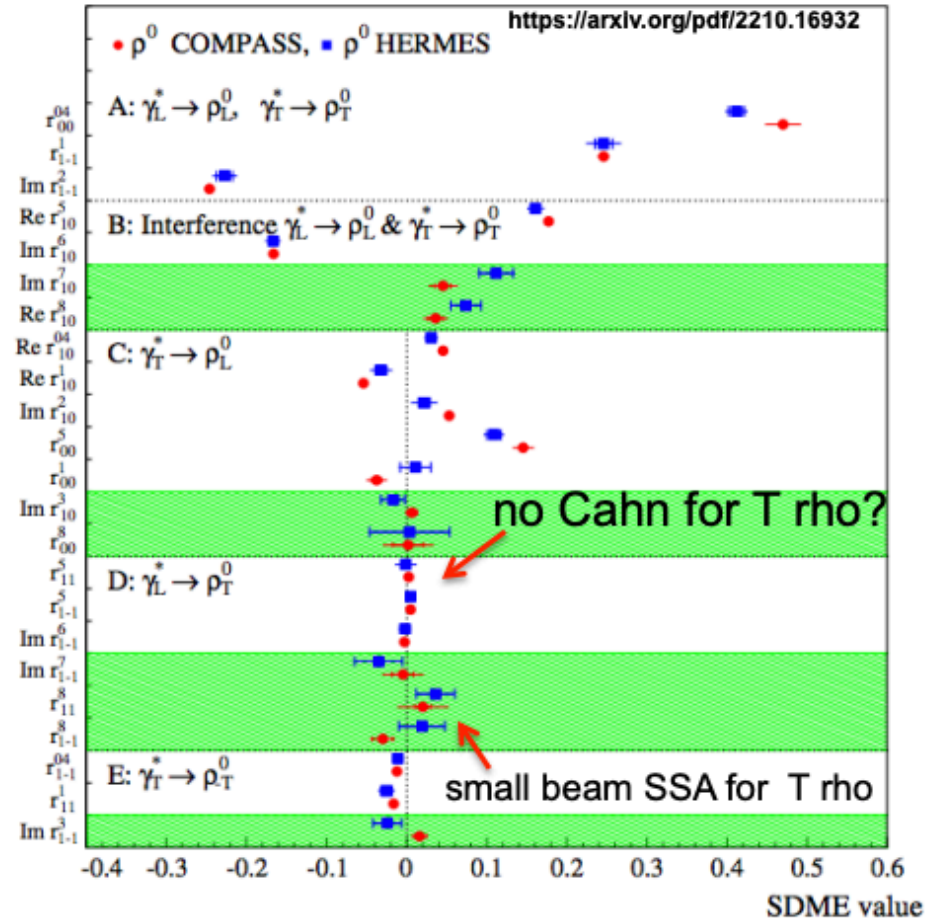


Fig. 12: Comparison of the 23 SDMEs for exclusive  $\rho^0$  lepton production on the proton extracted in the entire kinematic regions of the HERMES and COMPASS experiments. For HERMES the average kinematic values are  $\langle Q^2 \rangle = 1.96 \text{ (GeV}/c^2)^2$ ,  $\langle W \rangle = 4.8 \text{ GeV}/c^2$ ,  $\langle |r'| \rangle = 0.13$ , while those for COMPASS are  $\langle Q^2 \rangle = 2.40 \text{ (GeV}/c^2)^2$ ,  $\langle W \rangle = 9.9 \text{ GeV}/c^2$ ,  $\langle p_T^2 \rangle = 0.18 \text{ (GeV}/c)^2$ . Inner error bars represent statistical uncertainties and outer ones statistical and systematic uncertainties added in quadrature. Unpolarised (polarised) SDMEs are displayed in unshaded (shaded) areas.

# Understanding exclusive rhos and SDME validations

$$\mathcal{W}^U(\Phi, \phi, \cos \Theta)$$

$$+ \sqrt{2\epsilon(1+\epsilon)} \cos \Phi (r_{11}^5 \sin^2 \Theta + r_{00}^5 \cos^2 \Theta)$$

corr. with  $r_{10}^5$  (Hermes) no corr (COMPASS)

$$\mathcal{W}^L(\Phi, \phi, \cos \Theta)$$

$$+ \sqrt{2\epsilon(1-\epsilon)} \sin \Phi (r_{11}^8 \sin^2 \Theta + r_{00}^8 \cos^2 \Theta)$$

corr. with  $r_{1-1}^8$  (Hermes) no corr (COMPASS)

$$\gamma_T^* \rightarrow \rho_L^0 \quad \tau_{01} \approx \sqrt{\epsilon} \frac{\sqrt{(r_{00}^5)^2 + (r_{00}^8)^2}}{\sqrt{2r_{00}^{04}}}$$

Since the decay angle is correlated with the polarization of the rho, then  $r_{00}^8$  and  $r_{00}^5$  will be responsible for longitudinal rho, so tiny beam SSA expected for longitudinal rho

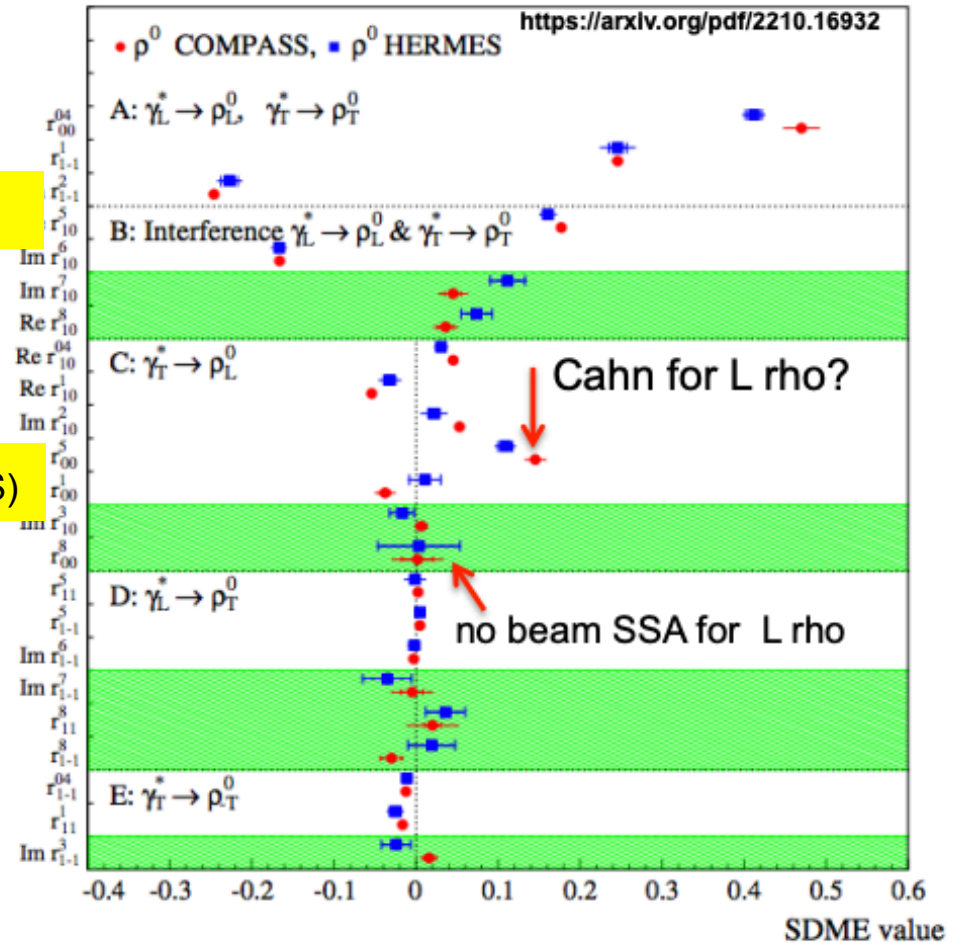
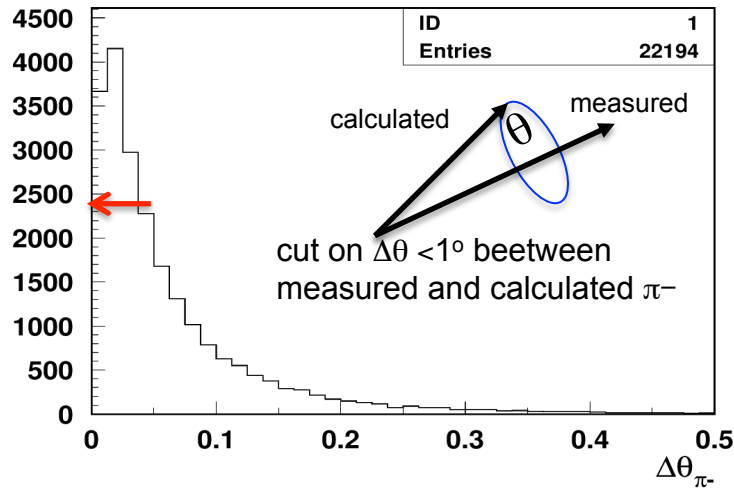


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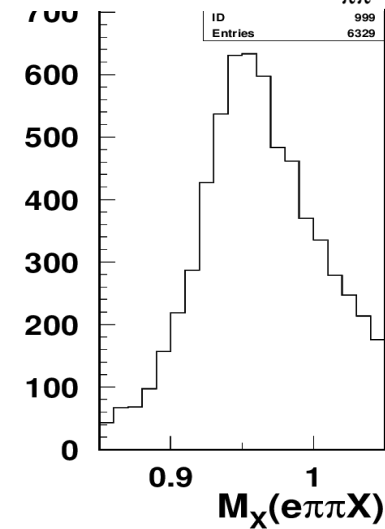
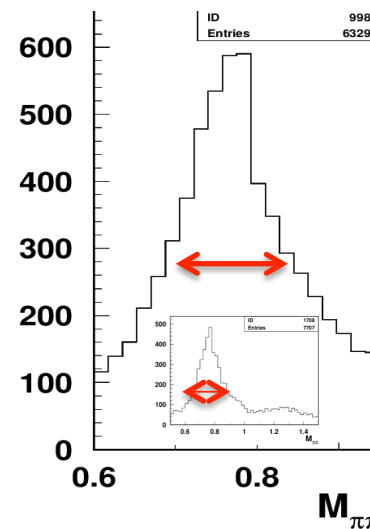
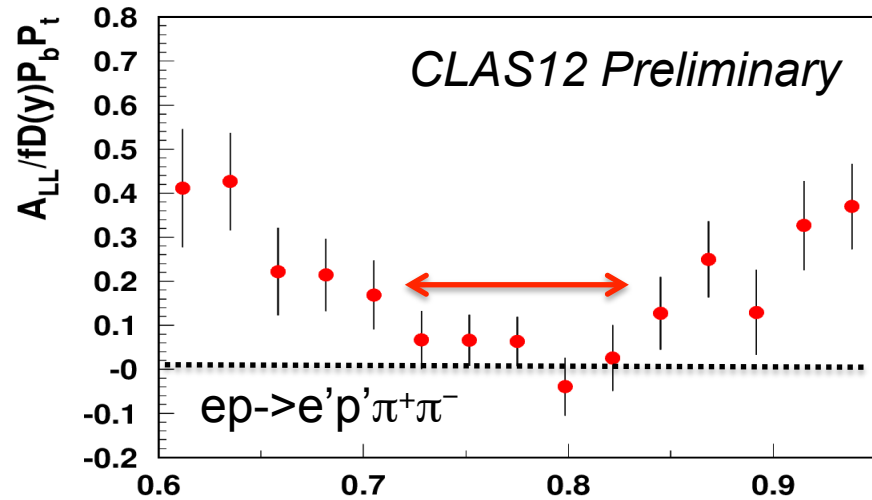
# Studies of $\rho^0$ impact with longitudinally polarized $\text{NH}_3$ target

## Separating exclusive dihadrons



- Require the angle of negative pions is within a degree from calculated from  $e', p, \pi^+$  assuming exclusive  $e', p, \pi^+\pi^-$  event.
- Measurements of  $A_{LL}$  for  $\rho^0$  indicate very small values (with  $\sim 10\text{-}20\%$  bck, likely negative  $\sim -2\text{-}10\%$ ), and can be one of the reasons for higher  $A_{LL}$  with protons with a  $M_X$  cuts above 1.35 GeV (excluding exclusive  $\rho^0$ )

**Request to theory  $\rightarrow$  evaluate the impact on  $g_1(x, k_T)$  with all  $A_{LL}$ s increasing 10-20%**



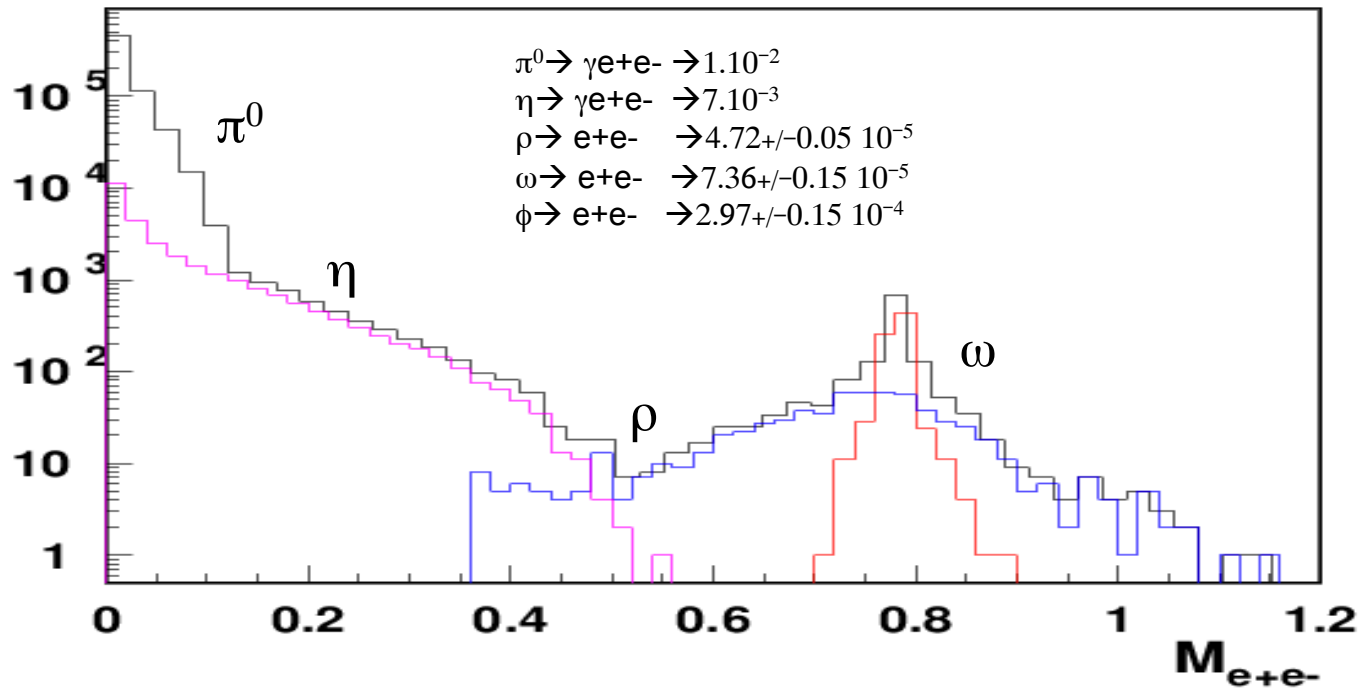
Need clear separation of hydrogen from  $\text{NH}_3$  and diffractive exclusive  $\rho^0$ s from exclusive  $\pi^+\pi^-$



# Using $e^+e^-$ to estimate vector mesons

The invariant mass of dihadrons is contaminated by other vector mesons, with shape not changing significantly with hadronization fraction to spin-1 vs spin-0 mesons

decays of  $\pi$  and  $\eta$  are kinematically separated from  $\omega$  and  $\rho^0$



Vector meson per electron can be independently estimated from  $ep \rightarrow e'e^+e^-X$   
Significant fraction of VM may affect DY studies.