

Reframing Azimuthal Modulations in Hard Exclusive Diffraction Processes

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In collaboration with Jianwei Qiu and Nobuo Sato

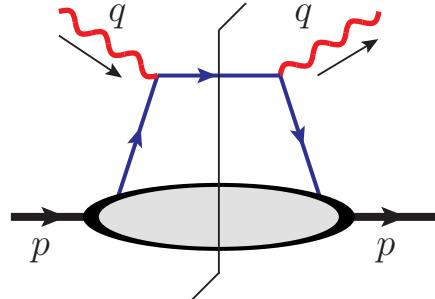
PRD 107 (2023) 014007

PRD 111 (2025) 094014

papers in preparation

Deeply Virtual Compton Scattering (DVCS)

□ DIS

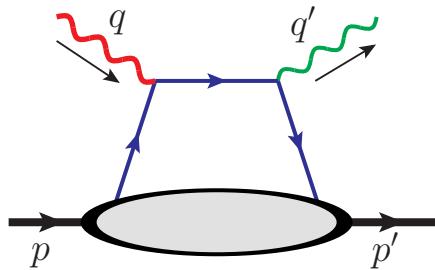


$$\begin{aligned} W^{\mu\nu}(p, q) &= \frac{1}{4\pi} \int d^4z e^{iq\cdot z} \langle p | J^\nu(z/2) J^\mu(-z/2) | p \rangle \\ &\simeq \left(-g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) \underbrace{\left[\frac{1}{2} \sum_q e_q^2 f_q(x_B) \right]}_{F_1(x_B, Q^2)} + \frac{1}{p \cdot q} \left(p^\mu - \frac{p \cdot q}{q^2} q^\mu \right) \left(p^\nu - \frac{p \cdot q}{q^2} q^\nu \right) \underbrace{\left[\sum_q e_q^2 x_B f_q(x_B) \right]}_{F_2(x_B, Q^2)} \end{aligned}$$

$$\frac{d\sigma}{dx_B dQ^2} = \frac{4\pi\alpha_e^2}{x_B Q^4} \left[x_B \cancel{y^2} F_1(x_B, Q^2) + \left(1 - \cancel{y} - x_B^2 \cancel{y^2} \frac{m^2}{Q^2} \right) F_2(x_B, Q^2) \right]$$

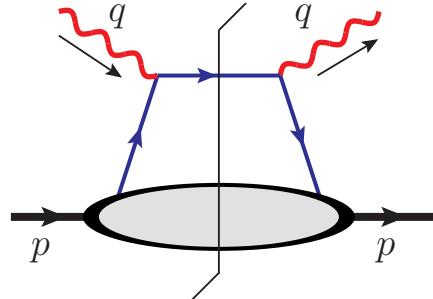
Different y dependence → Separate F_1 and F_2
Rosenbluth method

□ DVCS



Deeply Virtual Compton Scattering (DVCS)

□ DIS



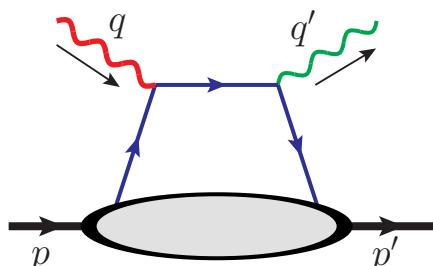
$$W^{\mu\nu}(p, q) = \frac{1}{4\pi} \int d^4z e^{iq \cdot z} \langle p | J^\nu(z/2) J^\mu(-z/2) | p \rangle$$

$$\simeq \left(-g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) \underbrace{\left[\frac{1}{2} \sum_q e_q^2 f_q(x_B) \right]}_{F_1(x_B, Q^2)} + \frac{1}{p \cdot q} \left(p^\mu - \frac{p \cdot q}{q^2} q^\mu \right) \left(p^\nu - \frac{p \cdot q}{q^2} q^\nu \right) \underbrace{\left[\sum_q e_q^2 x_B f_q(x_B) \right]}_{F_2(x_B, Q^2)}$$

$$\frac{d\sigma}{dx_B dQ^2} = \frac{4\pi\alpha_e^2}{x_B Q^4} \left[x_B y^2 F_1(x_B, Q^2) + \left(1 - y - x_B^2 y^2 \frac{m^2}{Q^2} \right) F_2(x_B, Q^2) \right]$$

Different y dependence
Rosenbluth method → Separate F_1 and F_2

□ DVCS



$$T^{\mu\nu}(p, p', q) = i \int d^4z e^{i(q+q') \cdot z} \langle p' | \mathcal{T}\{J^\nu(z/2) J^\mu(-z/2)\} | p \rangle$$

(depends on the choice of n)

$$\simeq \frac{\bar{u}(p', s')}{2P \cdot n} \left\{ \left[\mathcal{H}(\xi, t) \gamma \cdot n - \mathcal{E}(\xi, t) \frac{i\sigma^{n\Delta}}{2m} \right] (g_\perp^{\mu\nu}) + \left[\tilde{\mathcal{H}}(\xi, t) \gamma \cdot n \gamma_5 - \tilde{\mathcal{E}}(\xi, t) \frac{\gamma_5 \Delta \cdot n}{2m} \right] (-i \epsilon_\perp^{\mu\nu}) \right\} u(p, s)$$

$$\Delta = p - p'$$

$$P = (p + p')/2$$

$$\{\mathcal{H}, \mathcal{E}\}(\xi, t) \equiv \sum_q e_q^2 \int_{-1}^1 dx \{H^q, E^q\}(x, \xi, t) \left[\frac{1}{x - \xi + i\epsilon} + \frac{1}{x + \xi - i\epsilon} \right]$$

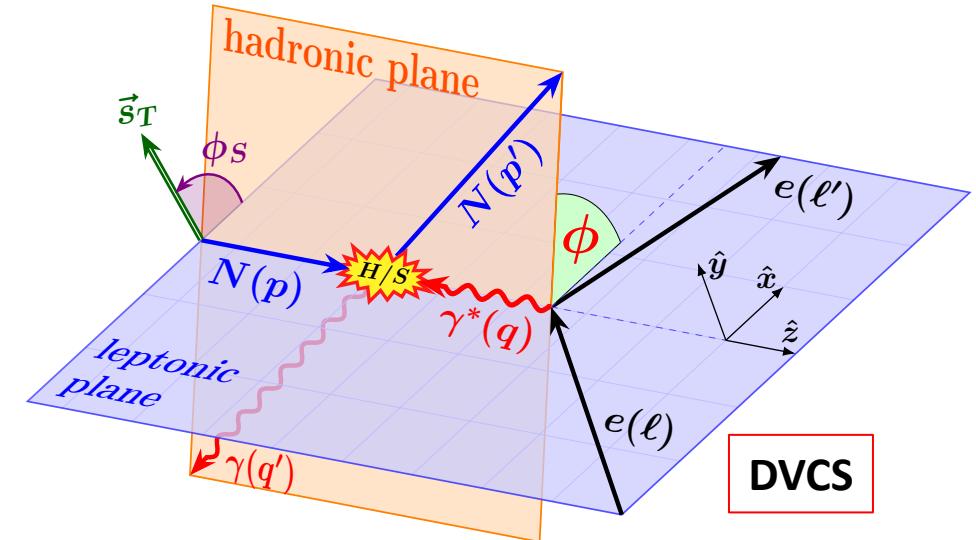
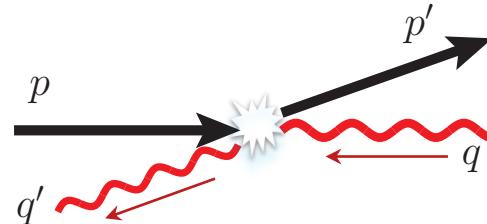
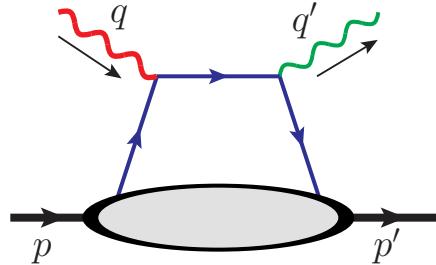
$$\{\tilde{\mathcal{H}}, \tilde{\mathcal{E}}\}(\xi, t) \equiv \sum_q e_q^2 \int_{-1}^1 dx \{\tilde{H}^q, \tilde{E}^q\}(x, \xi, t) \left[\frac{1}{x - \xi + i\epsilon} - \frac{1}{x + \xi - i\epsilon} \right]$$

← GPD moments

- Both Re and Im parts
- 8 real dof's in total!

How to separate the GPD moments in DVCS?

□ Azimuthal dependence in the Breit frame?



Breit frame observables: $(x_B, Q^2, t, \phi_S, \phi)$



$$\frac{d\sigma}{dx_B dQ^2 dt d\phi_S d\phi}$$

[A.V. Belitsky et al., 2002]

[B. Kriesten et al., 2020, 2022]

[Y. Guo et al., 2021, 2022]

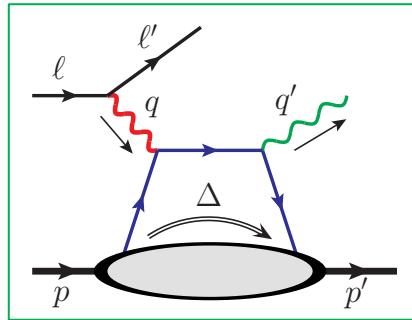
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ϕ dependence in the DVCS amplitude: $e^{i(\lambda_N - \lambda_{\gamma^*})\phi}$ + polarization → separate GPDs (?)

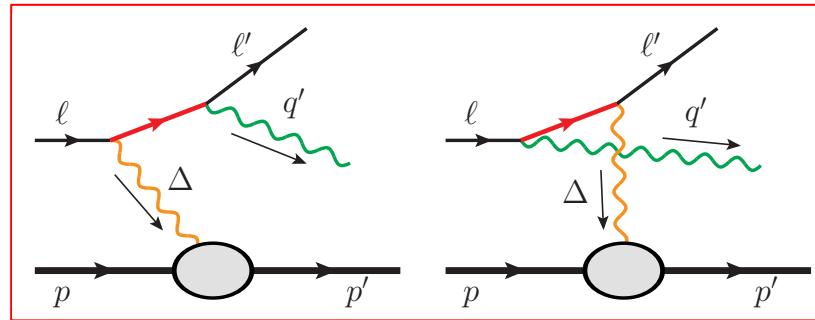
Bethe-Heitler subprocess!

□ DVCS is not a physical process

$$N(p) + e(\ell) \rightarrow N(p') + e(\ell') + \gamma(q')$$

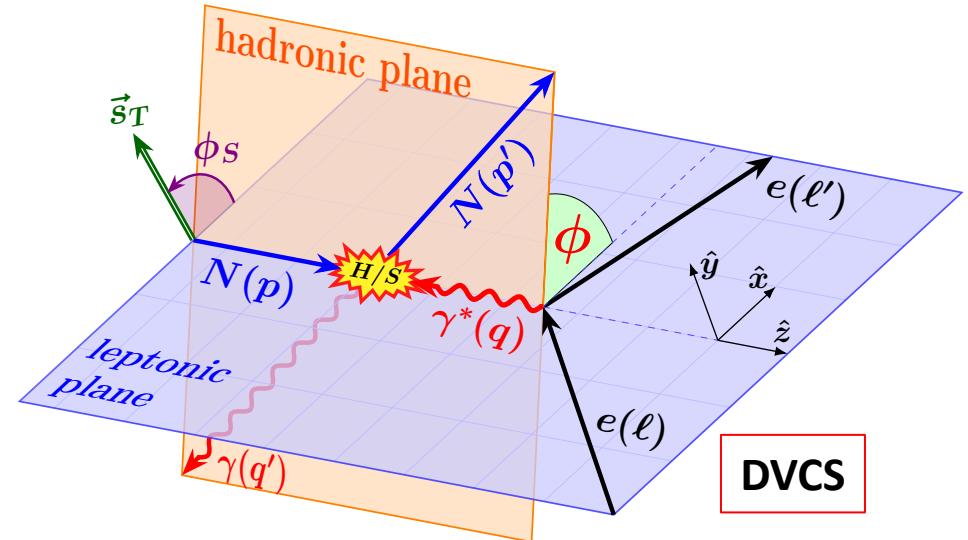


DVCS



Bethe-Heitler (BH) process

$$\Delta = p' - p$$



DVCS

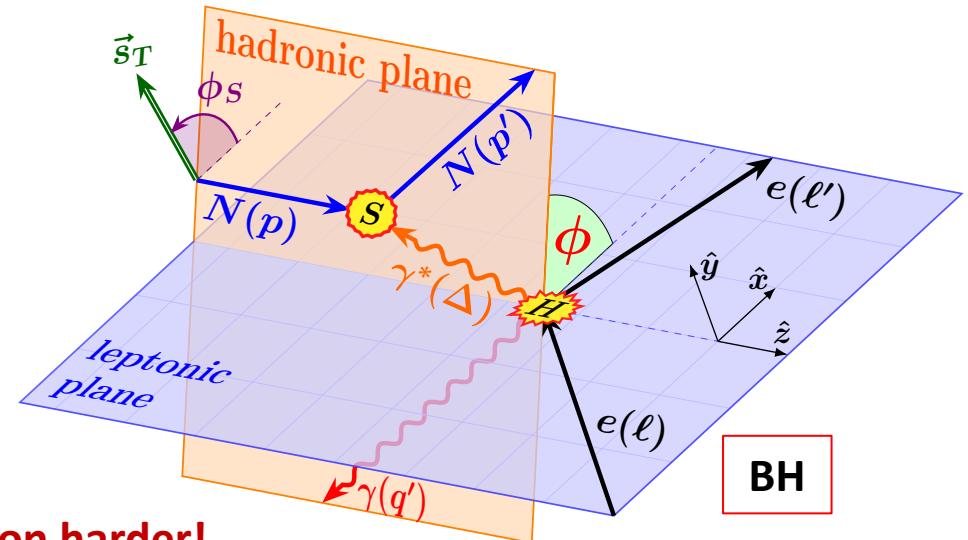
□ Breit frame is **NOT** convenient for describing BH

- The virtual photon $\gamma^*(q)$ does not exist
- The z axis is purely kinematical
- ϕ dependence in the denominators

$$\mathcal{P}_1 = (\ell - \Delta)^2 = -2\ell \cdot \Delta + t \quad \supset 2\ell_x \Delta_x \propto \cos \phi$$

$$\mathcal{P}_2 = (\ell - q')^2 = -2\ell \cdot q' \quad \supset 2\ell_x q'_x \propto \cos \phi$$

BH contaminates the azimuthal distribution \Rightarrow makes GPD extraction harder!



BH

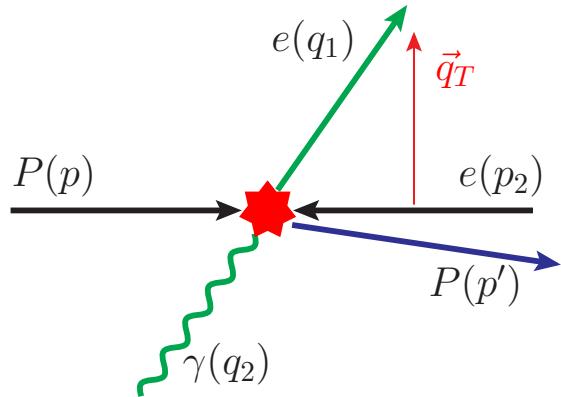
A better way to think about DVCS

□ Single diffractive hard exclusive process (SDHEP)

DVCS in **lab** frame

$$N(p) + e(p_2) \rightarrow N(p') + e(q_1) + \gamma(q_2)$$

[Qiu & Yu, PRD 107 (2023) 014007]
[Qiu, Sato, Yu, PRD 111 (2025) 094014]
[in preparation]



Two scales:

- Hard q_T
- Soft t

$$t = (p - p')^2$$

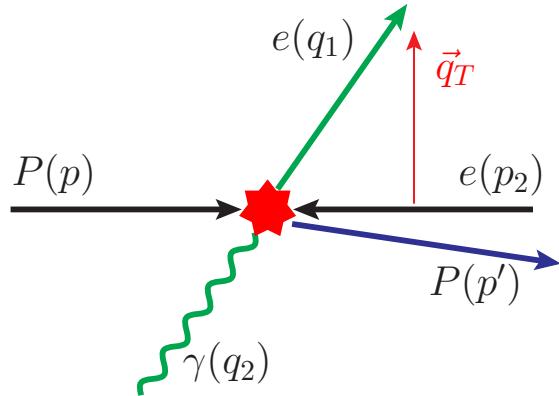
A better way to think about DVCS

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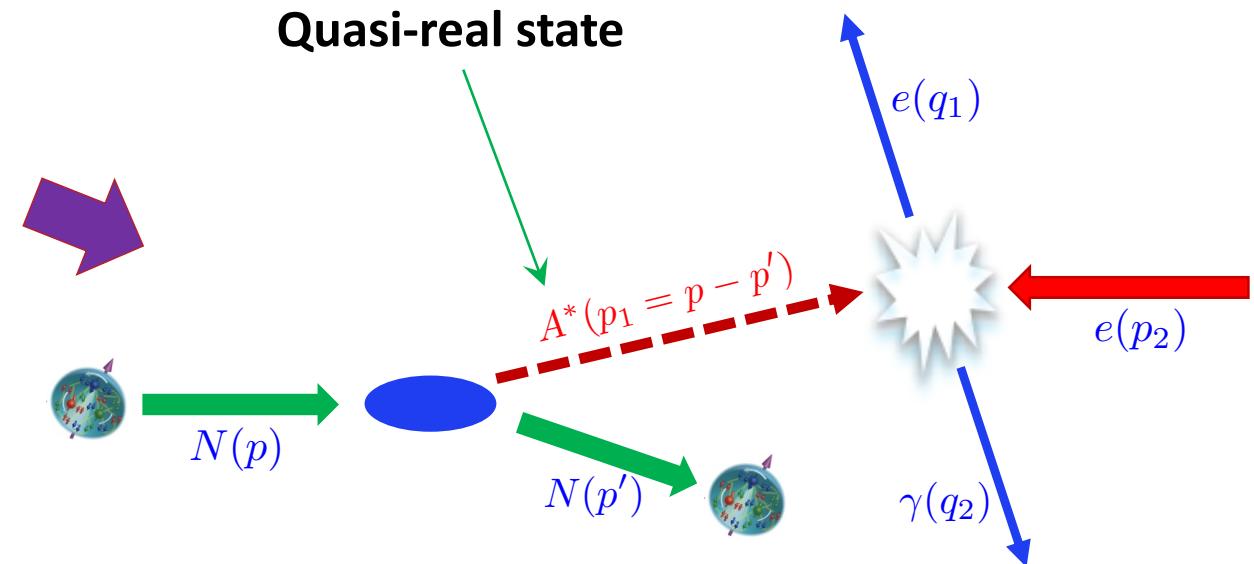
[Qiu & Yu, PRD 107 (2023) 014007]
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[in preparation]



Two scales:

- Hard q_T
- Soft t

$$t = (p - p')^2$$



□ Two-stage process paradigm

Single diffractive: $N(p) \rightarrow N(p') + A^*(p_1 = p - p')$

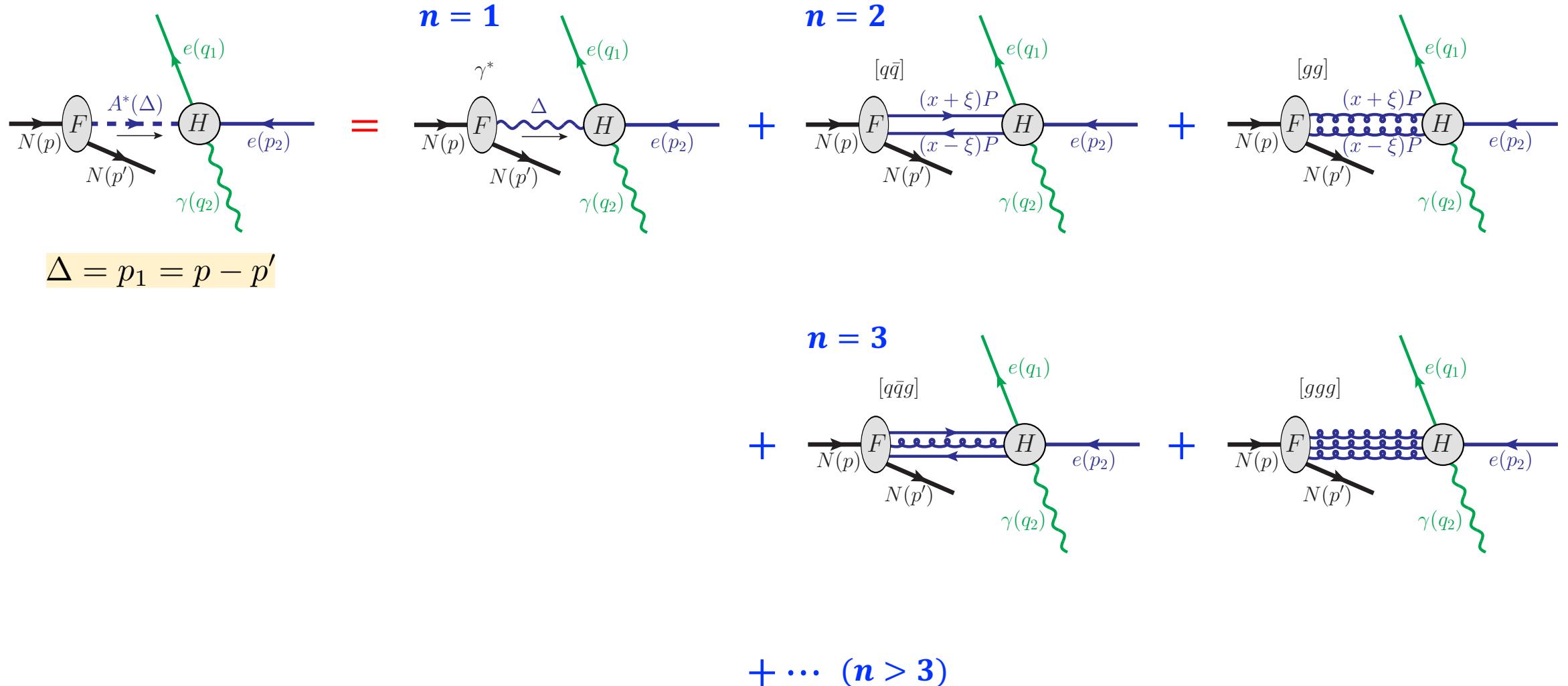
↓
factorize

Hard exclusive: $A^*(p_1) + e(p_2) \rightarrow e(q_1) + \gamma(q_2)$

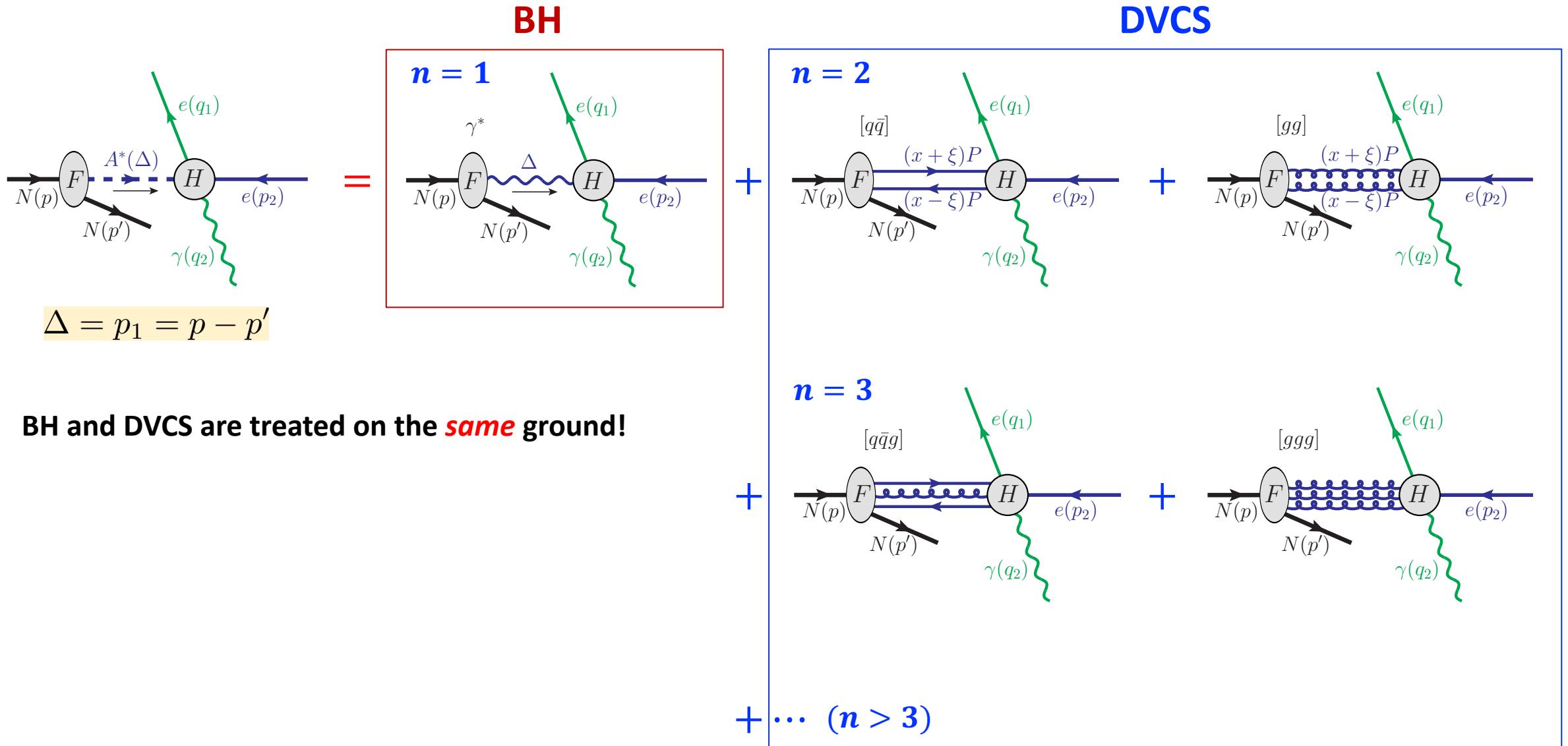
Necessary condition for factorization:

$$q_T \gg \sqrt{-t} \simeq \Lambda_{\text{QCD}}$$

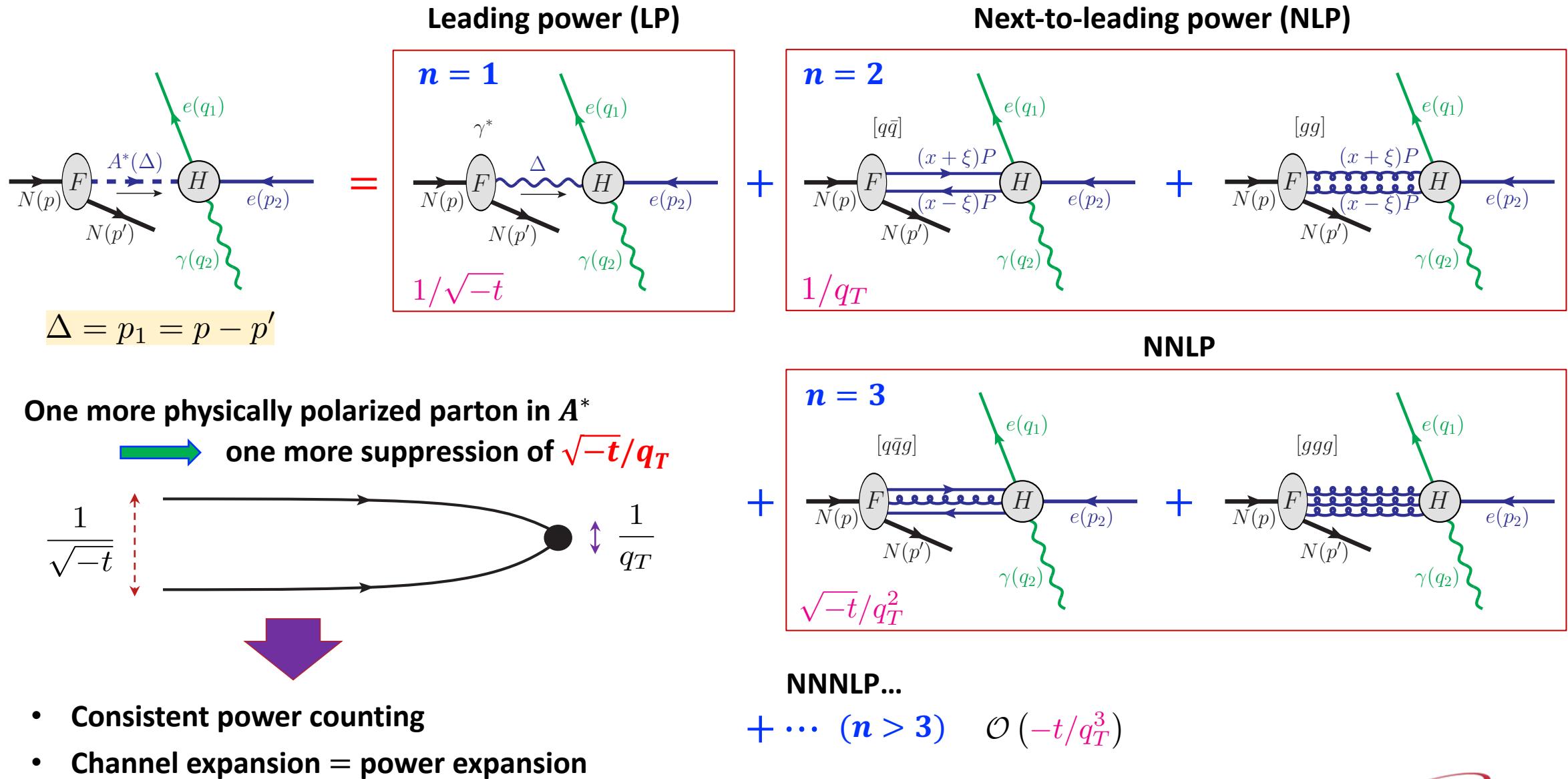
Channel expansion and power counting



Channel expansion and power counting



Channel expansion and power counting

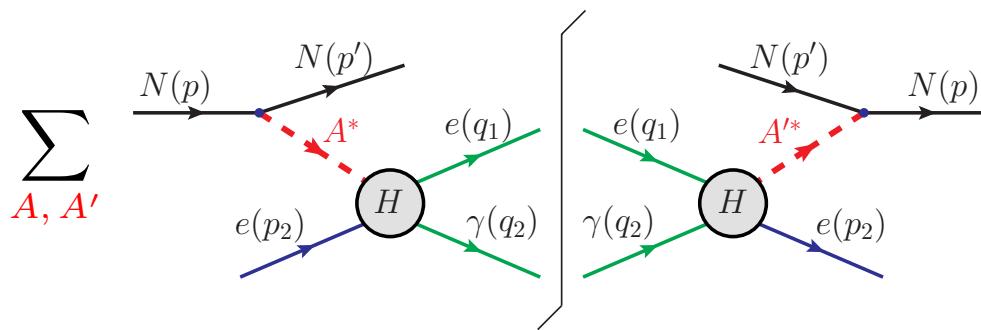


SDHEP frame and ϕ distribution

SDHEP frame observables: $(t, \xi, \phi_S, \theta, \phi)$

$$\mathcal{M}(t, \xi, \phi_S, \theta, \phi) = \sum_{A^*} e^{i(\lambda_A - \lambda_e)\phi} F_{N \rightarrow N A^*} \otimes G_{A^* e \rightarrow e\gamma}$$

$$|\mathcal{M}|^2$$

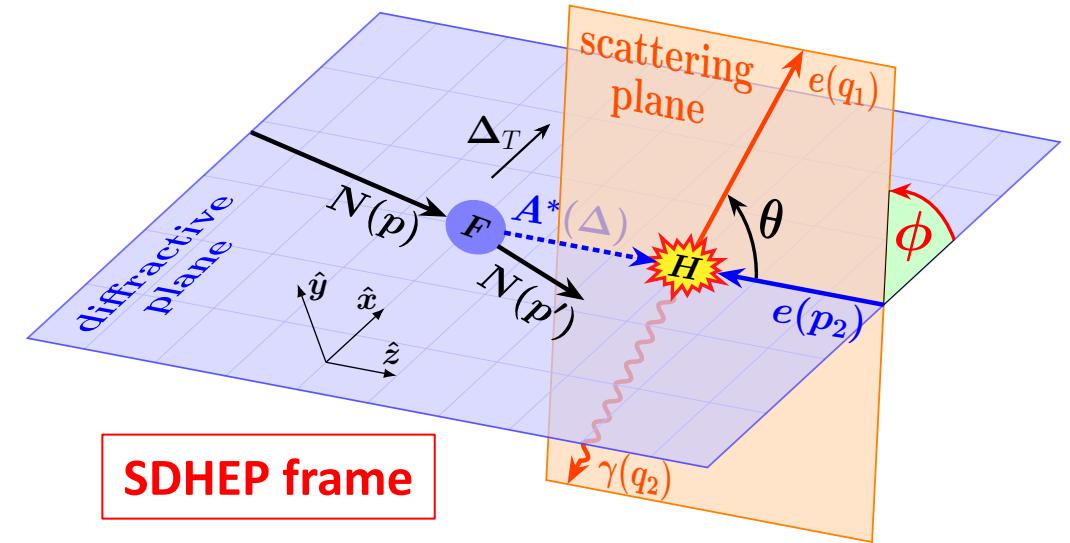


Interference of (λ_A, λ'_A) channels

$$\Delta\lambda_A = \lambda_A - \lambda'_A$$

$$\begin{aligned} &\cos[(\Delta\lambda_A)\phi] \\ &\sin[(\Delta\lambda_A)\phi] \end{aligned}$$

\rightarrow ϕ distribution is determined by A^* spin states!



$n = 1$: γ^* channel --- BH subprocess

□ Advantage: the quasi-real state A^* has well-defined helicity for all $n = 1, 2, 3, \dots$

$$F_N^\mu(p, p') = \langle N(p') | J^\mu(0) | N(p) \rangle = \bar{u}(p', s') \left[F_1(t) \gamma^\mu - F_2(t) \frac{i\sigma^{\mu\nu} \Delta_\nu}{2m} \right] u(p, s)$$

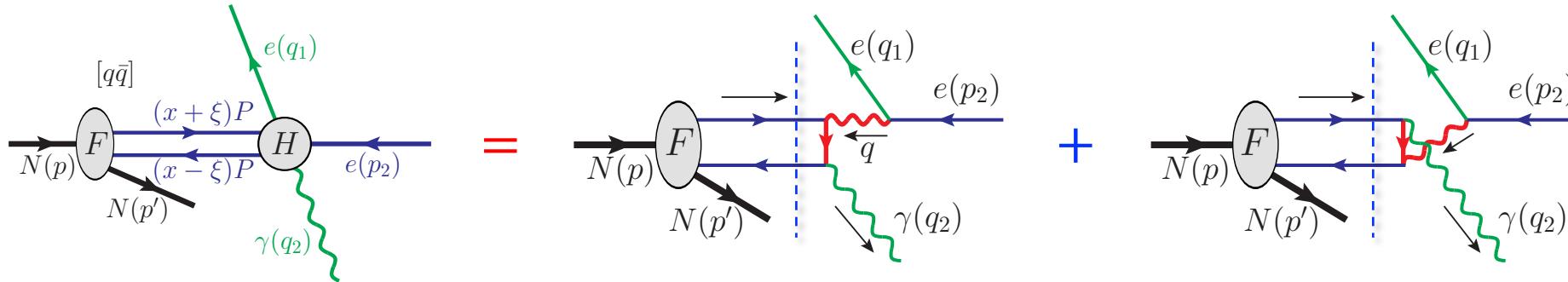
$$\mathcal{M}^{[1]} = \frac{-e}{t} F_N^\mu(p, p') G_\mu^\gamma(\Delta, p_2, q_1, q_2) = \frac{e}{t} \left[\sum_{\lambda=\pm 1} (\mathbf{F}_N \cdot \epsilon_\lambda^*) (\epsilon_\lambda \cdot \mathbf{G}^\gamma) - 2(\mathbf{F}_N \cdot \mathbf{n})(\bar{\mathbf{n}} \cdot \mathbf{G}^\gamma) \right]$$

$$\lambda_A^\gamma = \pm 1 \quad \lambda_A^\gamma = 0$$

- Only the transverse polarization γ_T^* is at LP $\mathcal{O}(1/\sqrt{-t})$
- The longitudinal polarization γ_L^* is at NLP $\mathcal{O}(1/q_T)$ \longleftrightarrow Combine with $n = 2$ (DVCS)

$n = 2$: $[q\bar{q}]$ channel --- DVCS (twist-2)

□ Advantage: the quasi-real state A^* has well-defined helicity for all $n = 1, 2, 3, \dots$



$$\mathcal{M}^{[2]} \simeq \sum_q \int_{-1}^1 dx [F^q(x, \xi, t) G^q(x, \xi; \hat{s}, \theta, \phi) + \tilde{F}^q(x, \xi, t) \tilde{G}^q(x, \xi; \hat{s}, \theta, \phi)] + \mathcal{O}(\sqrt{-t}/q_T^2)$$

GPDs (H, E) : defined with γ^+

(\tilde{H}, \tilde{E}) : defined with $\gamma^+ \gamma_5$

$$\lambda_A^{q\bar{q}} = 0$$

Combine $n = 1$ and $n = 2$ channels

□ Amplitude level

LP $\mathcal{M}_I : A^* = \gamma_T^* (\lambda_A^\gamma = \pm 1)$

NLP $\mathcal{M}_{II} : (1) A^* = \gamma_L^* (\lambda_A^\gamma = 0); (2) A^* = [q\bar{q}] (\lambda_A^q = 0) + [gg] \text{ (high order)}$

NNLP: ...

□ Cross section level

$$|\mathcal{M}_I + \mathcal{M}_{II} + \dots|^2 = \underbrace{|\mathcal{M}_I|^2}_{\text{LP}} + \underbrace{2 \operatorname{Re}(\mathcal{M}_I \mathcal{M}_{II}^*)}_{\text{NLP}} + \dots$$

Combine $n = 1$ and $n = 2$ channels

□ Amplitude level

LP $\mathcal{M}_I : A^* = \gamma_T^* (\lambda_A^\gamma = \pm 1)$

NLP $\mathcal{M}_{II} : (1) A^* = \gamma_L^* (\lambda_A^\gamma = 0); (2) A^* = [q\bar{q}] (\lambda_A^q = 0) + [gg] \text{ (high order)}$

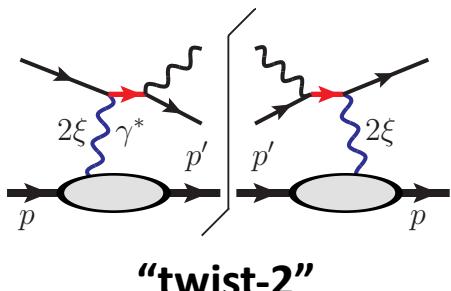
NNLP: ...

□ Cross section level

$$|\mathcal{M}_I + \mathcal{M}_{II} + \dots|^2 = \underbrace{|\mathcal{M}_I|^2}_{\text{LP}} + \underbrace{2 \operatorname{Re}(\mathcal{M}_I \mathcal{M}_{II}^*)}_{\text{NLP}} + \dots$$

$$\begin{aligned} & \cos[(\Delta\lambda_A)\phi] \\ & \sin[(\Delta\lambda_A)\phi] \end{aligned} \quad \Delta\lambda_A = \lambda_A - \lambda'_A$$

LP $|\mathcal{M}|_{\text{LP}}^2 = |\mathcal{M}_I|^2$ **No ϕ modulation.** $\lambda_A^\gamma = +1$ and $\lambda_A^\gamma = -1$ do NOT interfere until NNLP.



Combine $n = 1$ and $n = 2$ channels

□ Amplitude level

LP $\mathcal{M}_I : A^* = \gamma_T^* (\lambda_A^\gamma = \pm 1)$

NLP $\mathcal{M}_{II} : (1) A^* = \gamma_L^* (\lambda_A^\gamma = 0); (2) A^* = [q\bar{q}] (\lambda_A^q = 0) + [gg] \text{ (high order)}$

NNLP: ...

□ Cross section level

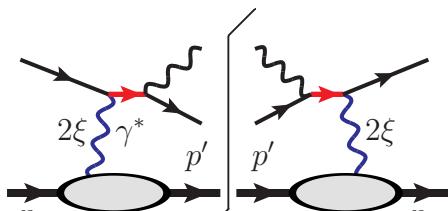
$$|\mathcal{M}_I + \mathcal{M}_{II} + \dots|^2 = \underbrace{|\mathcal{M}_I|^2}_{\text{LP}} + \underbrace{2 \operatorname{Re}(\mathcal{M}_I \mathcal{M}_{II}^*)}_{\text{NLP}} + \dots$$

$$\begin{aligned} & \cos[(\Delta\lambda_A)\phi] \\ & \sin[(\Delta\lambda_A)\phi] \end{aligned}$$

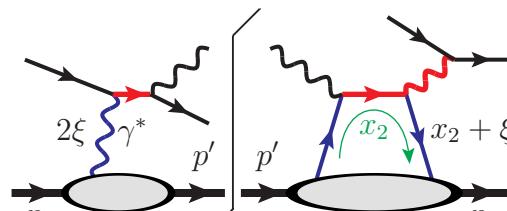
$$\Delta\lambda_A = \lambda_A - \lambda'_A$$

LP $|\mathcal{M}|_{\text{LP}}^2 = |\mathcal{M}_I|^2$ **No ϕ modulation.** $\lambda_A^\gamma = +1$ and $\lambda_A^\gamma = -1$ do NOT interfere until NNLP.

NLP $|\mathcal{M}|_{\text{NLP}}^2 = 2 \operatorname{Re}(\mathcal{M}_I \mathcal{M}_{II}^*) \rightarrow \cos\phi \text{ or } \sin\phi \text{ modulation.}$



“twist-2”



“twist-3”

15

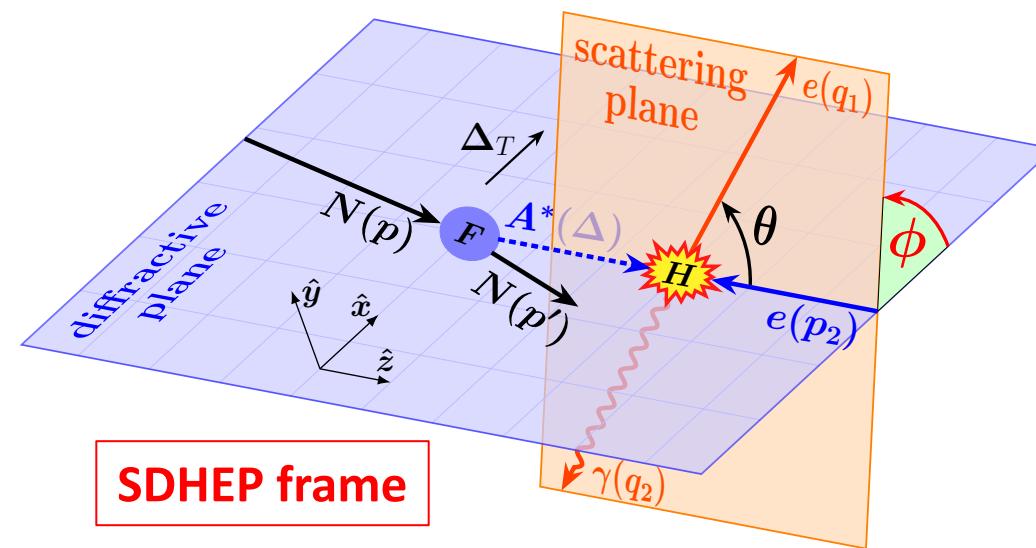


Interference of different numbers of particles.

Unique signal of GPDs.

Cross section within NLP: unpolarized proton

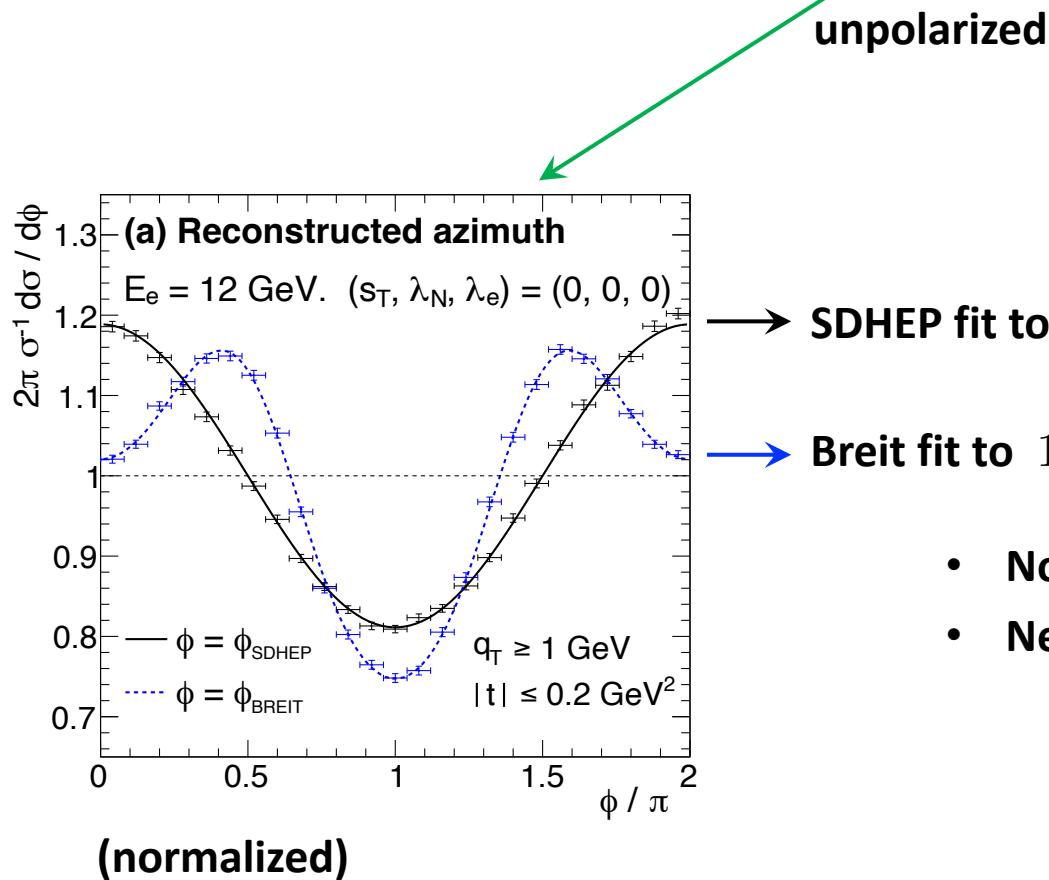
$$\frac{d\sigma}{dt d\xi d \cos \theta d\phi} = \frac{1}{2\pi} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \underbrace{\left[1 + A_{UU}^{\text{NLP}}(t, \xi, \cos \theta) \cos \phi + \lambda_e A_{UL}^{\text{NLP}}(t, \xi, \cos \theta) \sin \phi \right]}_{\text{Interference of } \gamma_T^* \text{ and GPD moments}}$$



Cross section within NLP: unpolarized proton

$$\frac{d\sigma}{dt d\xi d \cos \theta d\phi} = \frac{1}{2\pi} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \left[1 + A_{UU}^{\text{NLP}}(t, \xi, \cos \theta) \cos \phi + \lambda_e A_{UL}^{\text{NLP}}(t, \xi, \cos \theta) \sin \phi \right]$$

Generate 10^6 events and reconstruct



→ SDHEP fit to $1.00 + 0.190 \cos \phi$ → $\langle A_{UU}^{\text{NLP}} \rangle = 0.190$

→ Breit fit to $1.00 + 0.15 \cos \phi - 0.12 \cos 2\phi - 0.01 \cos 3\phi + 0.01 \cos 4\phi$

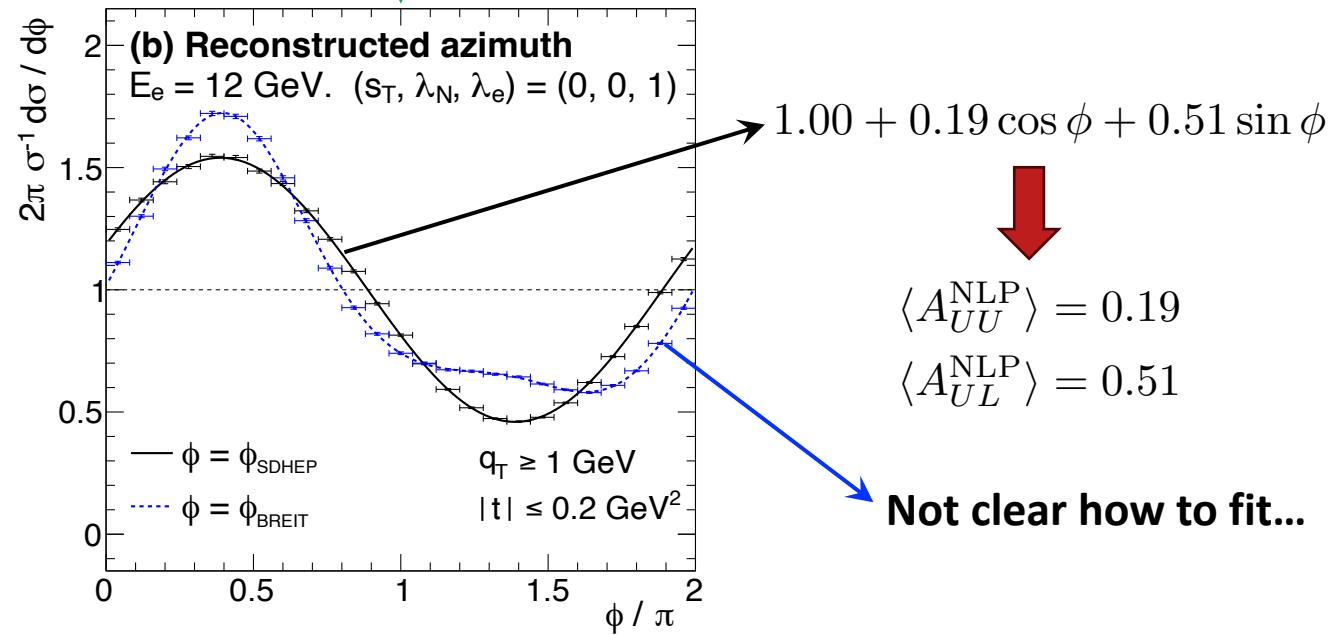
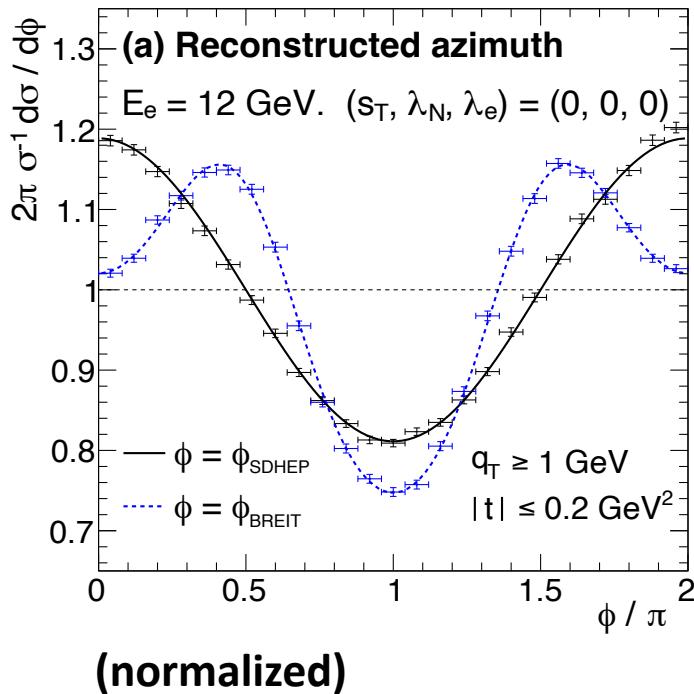
- No straightforward interpretation of the coefficients.
- Need to introduce more gears in GPD extraction.

[A.V. Belitsky et al., 2002]
[B. Kriesten et al., 2020, 2022]
[Y. Guo et al., 2021, 2022]
...

Cross section within NLP: unpolarized proton

$$\frac{d\sigma}{dt d\xi d \cos \theta d\phi} = \frac{1}{2\pi} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \left[1 + A_{UU}^{\text{NLP}}(t, \xi, \cos \theta) \cos \phi + \lambda_e A_{UL}^{\text{NLP}}(t, \xi, \cos \theta) \sin \phi \right]$$

Generate 10^6 events and reconstruct



Cross section within NLP: introducing proton spin

$$\frac{d\sigma}{dt d\xi d\phi_S d \cos \theta d\phi} = \frac{1}{(2\pi)^2} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \left[1 + \lambda_e \lambda_N A_{LL}^{\text{LP}} + \lambda_e s_T A_{TL}^{\text{LP}} \cos \phi_S \right.$$

$$+ (A_{UU}^{\text{NLP}} + \lambda_e \lambda_N A_{LL}^{\text{NLP}}) \cos \phi + (\lambda_e A_{UL}^{\text{NLP}} + \lambda_N A_{LU}^{\text{NLP}}) \sin \phi$$

$$+ s_T (A_{TU,1}^{\text{NLP}} \cos \phi_S \sin \phi + A_{TU,2}^{\text{NLP}} \sin \phi_S \cos \phi)$$

$$\left. + \lambda_e s_T (A_{TL,1}^{\text{NLP}} \cos \phi_S \cos \phi + A_{TL,2}^{\text{NLP}} \sin \phi_S \sin \phi) \right]$$

In the experimental setting (fixed lab frame),

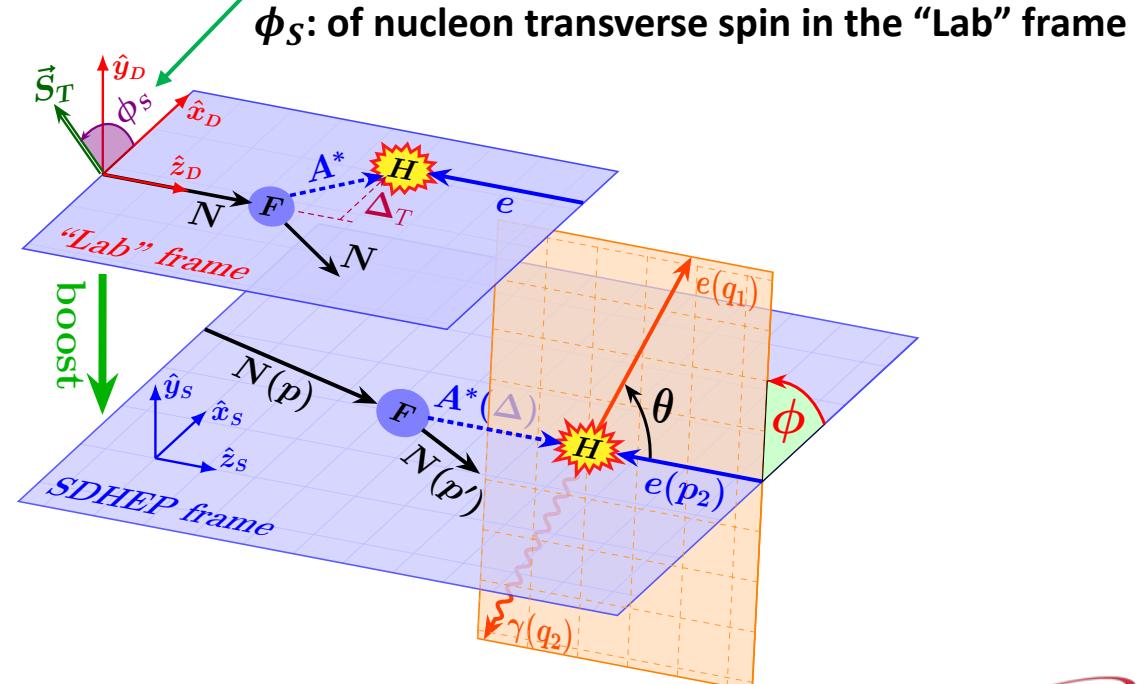
- Nucleon spin vector $\vec{s}_N = (s_T, 0, \lambda_N)$
- Electron spin vector $\vec{s}_e = (0, 0, \lambda_e)$

Subscripts: (nucleon, electron)

U = Unpolarized

L = Longitudinally polarized

T = Transversely polarized



Cross section within NLP: full polarization

$$\frac{d\sigma}{dt d\xi d\phi_S d \cos \theta d\phi} = \frac{1}{(2\pi)^2} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \left[1 + \lambda_e \lambda_N A_{LL}^{\text{LP}} + \lambda_e s_T A_{TL}^{\text{LP}} \cos \phi_S \right.$$

LP: from γ_T^* squared

$$+ (A_{UU}^{\text{NLP}} + \lambda_e \lambda_N A_{LL}^{\text{NLP}}) \cos \phi + (\lambda_e A_{UL}^{\text{NLP}} + \lambda_N A_{LU}^{\text{NLP}}) \sin \phi \\ + s_T (A_{TU,1}^{\text{NLP}} \cos \phi_S \sin \phi + A_{TU,2}^{\text{NLP}} \sin \phi_S \cos \phi) \\ + \lambda_e s_T (A_{TL,1}^{\text{NLP}} \cos \phi_S \cos \phi + A_{TL,2}^{\text{NLP}} \sin \phi_S \sin \phi) \left. \right]$$

$$\frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} = \frac{\alpha_e^3}{(1+\xi)^2} \frac{m^2}{s t^2} \Sigma_{UU}^{\text{LP}}$$

$$\Sigma_{UU}^{\text{LP}} = \left[\frac{1}{\sin^2(\theta/2)} + \sin^2(\theta/2) \right] \left[\left(\frac{1-\xi^2}{2\xi^2} \frac{-t}{m^2} - 2 \right) \left(F_1^2 - \frac{t}{4m^2} F_2^2 \right) - \frac{t}{m^2} (F_1 + F_2)^2 \right]$$

$$A_{LL}^{\text{LP}} = \frac{1}{\Sigma_{UU}^{\text{LP}}} \cdot \left[\frac{1}{\sin^2(\theta/2)} - \sin^2(\theta/2) \right] (F_1 + F_2) \left[F_1 \left(\frac{-t}{\xi m^2} - \frac{4\xi}{1+\xi} \right) - \frac{t}{m^2} F_2 \right]$$

$$A_{TL}^{\text{LP}} = \frac{1}{\Sigma_{UU}^{\text{LP}}} \cdot \frac{\Delta_T}{2m} \left[\frac{1}{\sin^2(\theta/2)} - \sin^2(\theta/2) \right] (F_1 + F_2) \left[-4F_1 + \frac{1+\xi}{\xi} \frac{-t}{m^2} F_2 \right]$$

Quadratic in (F_1, F_2)

Control the **rate** (unpolarized cross section). **No ϕ modulation.**

Cross section within NLP: full polarization

$$\frac{d\sigma}{dt d\xi d\phi_S d \cos \theta d\phi} = \frac{1}{(2\pi)^2} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \left[1 + \lambda_e \lambda_N A_{LL}^{\text{LP}} + \lambda_e s_T A_{TL}^{\text{LP}} \cos \phi_S \right.$$

$$+ (A_{UU}^{\text{NLP}} + \lambda_e \lambda_N A_{LL}^{\text{NLP}}) \cos \phi + (\lambda_e A_{UL}^{\text{NLP}} + \lambda_N A_{LU}^{\text{NLP}}) \sin \phi$$
$$+ s_T (A_{TU,1}^{\text{NLP}} \cos \phi_S \sin \phi + A_{TU,2}^{\text{NLP}} \sin \phi_S \cos \phi)$$
$$\left. + \lambda_e s_T (A_{TL,1}^{\text{NLP}} \cos \phi_S \cos \phi + A_{TL,2}^{\text{NLP}} \sin \phi_S \sin \phi) \right]$$

NLP: from $\gamma_T^* - \gamma_L^*$ and $\gamma_T^* - [q\bar{q}]$ interference

No contribution to the rate,

⇒ only to azimuthal modulations ($\cos \phi, \sin \phi$)

Cross section within NLP: full polarization

$$\frac{d\sigma}{dt d\xi d\phi_S d \cos \theta d\phi} = \frac{1}{(2\pi)^2} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \left[1 + \lambda_e \lambda_N A_{LL}^{\text{LP}} + \lambda_e s_T A_{TL}^{\text{LP}} \cos \phi_S \right.$$

$+ (A_{UU}^{\text{NLP}} + \lambda_e \lambda_N A_{LL}^{\text{NLP}}) \cos \phi + (\lambda_e A_{UL}^{\text{NLP}} + \lambda_N A_{LU}^{\text{NLP}}) \sin \phi$

$+ s_T (A_{TU,1}^{\text{NLP}} \cos \phi_S \sin \phi + A_{TU,2}^{\text{NLP}} \sin \phi_S \cos \phi)$

$\left. + \lambda_e s_T (A_{TL,1}^{\text{NLP}} \cos \phi_S \cos \phi + A_{TL,2}^{\text{NLP}} \sin \phi_S \sin \phi) \right]$

NLP: from $\gamma_T^* \cdot \gamma_L^*$ and $\gamma_T^* \cdot [q\bar{q}]$ interference

$$\downarrow \quad A_{XX}^{\text{NLP}} = \frac{1}{\Sigma_{UU}^{\text{LP}}} \cdot \left(\frac{-t}{m\sqrt{\hat{s}}} \right) \Sigma_{XX}^{\text{NLP}}$$

$$\Sigma_{UU}^{\text{NLP}} = \frac{\Delta_T}{2m} \frac{1+\xi}{\xi} \left[\frac{2 \sin \theta}{\xi} \left(F_1^2 - \frac{t}{4m^2} F_2^2 \right) - \frac{4 + (1 - \cos \theta)^2}{\sin \theta \cos^2(\theta/2)} (\mathbf{M}_1 \cdot \text{Re } V_F) \right],$$

$$\Sigma_{LL}^{\text{NLP}} = -\frac{\Delta_T}{m} \left[\sin \theta (F_1 + F_2) \left(\frac{1+\xi}{\xi} F_1 + F_2 \right) + \frac{3 - \cos \theta}{\sin \theta} (\mathbf{M}_2 \cdot \text{Re } V_F) \right],$$

$$\Sigma_{TL,1}^{\text{NLP}} = 2 \sin \theta (F_1 + F_2) \left[F_1 + \left(\frac{\xi}{1+\xi} + \frac{t}{4\xi m^2} \right) F_2 \right] + \frac{2(3 - \cos \theta)}{\sin \theta} (\mathbf{M}_3 \cdot \text{Re } V_F),$$

$$\Sigma_{TL,2}^{\text{NLP}} = 2 \sin \theta (F_1 + F_2) \left(F_1 + \frac{t}{4m^2} F_2 \right) - \frac{2(3 - \cos \theta)}{\sin \theta} (\mathbf{M}_4 \cdot \text{Re } V_F),$$

$$\Sigma_{UL}^{\text{NLP}} = -\frac{\Delta_T}{m} \frac{1+\xi}{\xi} \frac{3 - \cos \theta}{\sin \theta} (\mathbf{M}_1 \cdot \text{Im } V_F),$$

$$\Sigma_{LU}^{\text{NLP}} = -\frac{\Delta_T}{2m} \frac{4 + (1 - \cos \theta)^2}{\sin \theta \cos^2(\theta/2)} (\mathbf{M}_2 \cdot \text{Im } V_F),$$

$$\Sigma_{TU,1}^{\text{NLP}} = \frac{4 + (1 - \cos \theta)^2}{\sin \theta \cos^2(\theta/2)} (\mathbf{M}_3 \cdot \text{Im } V_F),$$

$$\Sigma_{TU,2}^{\text{NLP}} = \frac{4 + (1 - \cos \theta)^2}{\sin \theta \cos^2(\theta/2)} (\mathbf{M}_4 \cdot \text{Im } V_F).$$

- **Linear in GPD moments** $V_F = (\mathcal{H}, \mathcal{E}, \tilde{\mathcal{H}}, \tilde{\mathcal{E}})^T$
- **Controlled by the real matrix M , same for real and imaginary parts of GPD moments**

$$M_i = (M_{i1}, M_{i2}, M_{i3}, M_{i4}) \text{ (see next slide)}$$

- **8 asymmetries \Leftrightarrow 8 (real) GPD moments**

Cross section within NLP: full polarization

$$\frac{d\sigma}{dt d\xi d\phi_S d \cos \theta d\phi} = \frac{1}{(2\pi)^2} \frac{d\sigma^{\text{unpol}}}{dt d\xi d \cos \theta} \cdot \left[1 + \lambda_e \lambda_N A_{LL}^{\text{LP}} + \lambda_e s_T A_{TL}^{\text{LP}} \cos \phi_S \right.$$

$+ (A_{UU}^{\text{NLP}} + \lambda_e \lambda_N A_{LL}^{\text{NLP}}) \cos \phi + (\lambda_e A_{UL}^{\text{NLP}} + \lambda_N A_{LU}^{\text{NLP}}) \sin \phi$

$+ s_T (A_{TU,1}^{\text{NLP}} \cos \phi_S \sin \phi + A_{TU,2}^{\text{NLP}} \sin \phi_S \cos \phi)$

$\left. + \lambda_e s_T (A_{TL,1}^{\text{NLP}} \cos \phi_S \cos \phi + A_{TL,2}^{\text{NLP}} \sin \phi_S \sin \phi) \right]$

NLP: from $\gamma_T^* - \gamma_L^*$ and $\gamma_T^* - [q\bar{q}]$ interference

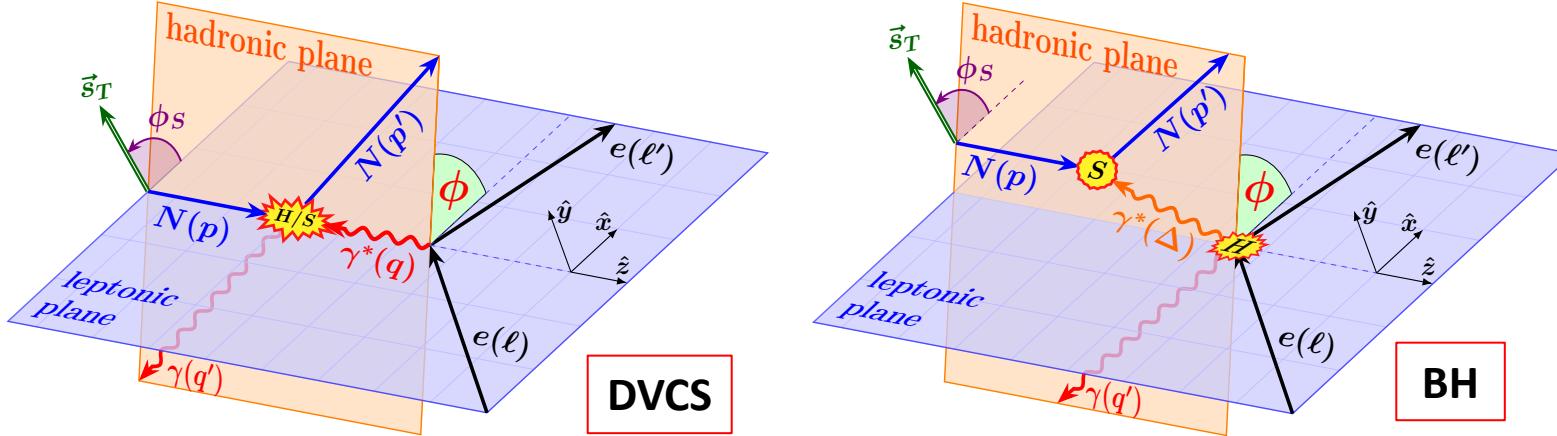


$$M = \begin{bmatrix} F_1 & -\frac{t}{4m^2}F_2 & \xi(F_1 + F_2) & 0 \\ (1+\xi)(F_1 + F_2) & \xi(F_1 + F_2) & \frac{1+\xi}{\xi}F_1 & -\xi F_1 - (1+\xi)\frac{t}{4m^2}F_2 \\ \xi(F_1 + F_2) & \left(\frac{\xi^2}{1+\xi} + \frac{t}{4m^2}\right)(F_1 + F_2) & -\xi F_1 + \frac{t}{4m^2}\frac{1-\xi^2}{\xi}F_2 & -\left(\frac{\xi^2}{1+\xi} + \frac{t}{4m^2}\right)F_1 - \frac{\xi t}{4m^2}F_2 \\ \xi(F_1 + F_2) & \frac{\xi t}{4m^2}(F_1 + F_2) & -\xi F_1 + \frac{t}{4m^2}\frac{1-\xi^2}{\xi}F_2 & -\left(\xi + \frac{t}{4\xi m^2}\right)F_1 - \frac{\xi t}{4m^2}F_2 \end{bmatrix} \quad \begin{array}{l} \leftarrow M_1 \\ \leftarrow M_2 \\ \leftarrow M_3 \\ \leftarrow M_4 \end{array}$$

$$\rightarrow M \cdot \begin{bmatrix} \mathcal{H} \\ \mathcal{E} \\ \tilde{\mathcal{H}} \\ \tilde{\mathcal{E}} \end{bmatrix} = \begin{bmatrix} \hat{V}_1 \\ \hat{V}_2 \\ \hat{V}_3 \\ \hat{V}_4 \end{bmatrix} \quad \begin{array}{l} \text{Reconstructed from experiments} \\ \text{(complex valued)} \end{array} \quad \det M \neq 0 \quad \rightarrow \text{Unique solution for GPD moments!}$$

Summary --- SDHEP frame vs. Breit frame

□ Breit frame: centered around $\gamma^*(q)$

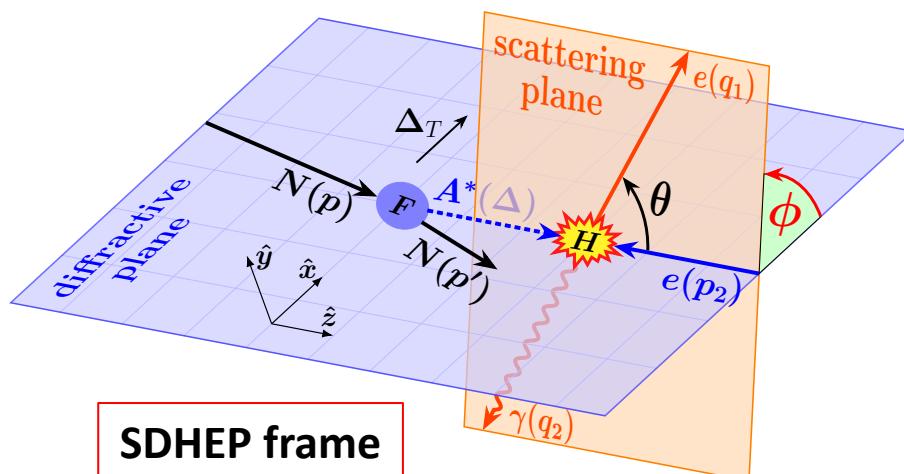


Inconsistent treatments
for DVCS and BH



Makes their interference
calculation difficult

□ SDHEP frame: centered around $A^*(\Delta)$



- Clear physical picture: scale separation
- $A^* = \gamma^*, [q\bar{q}], [gg], [q\bar{q}g], [ggg], \dots$
- Generalizable to high orders and twists
- Clear azimuthal distribution

Thank you!