

# The CaFe Experiment

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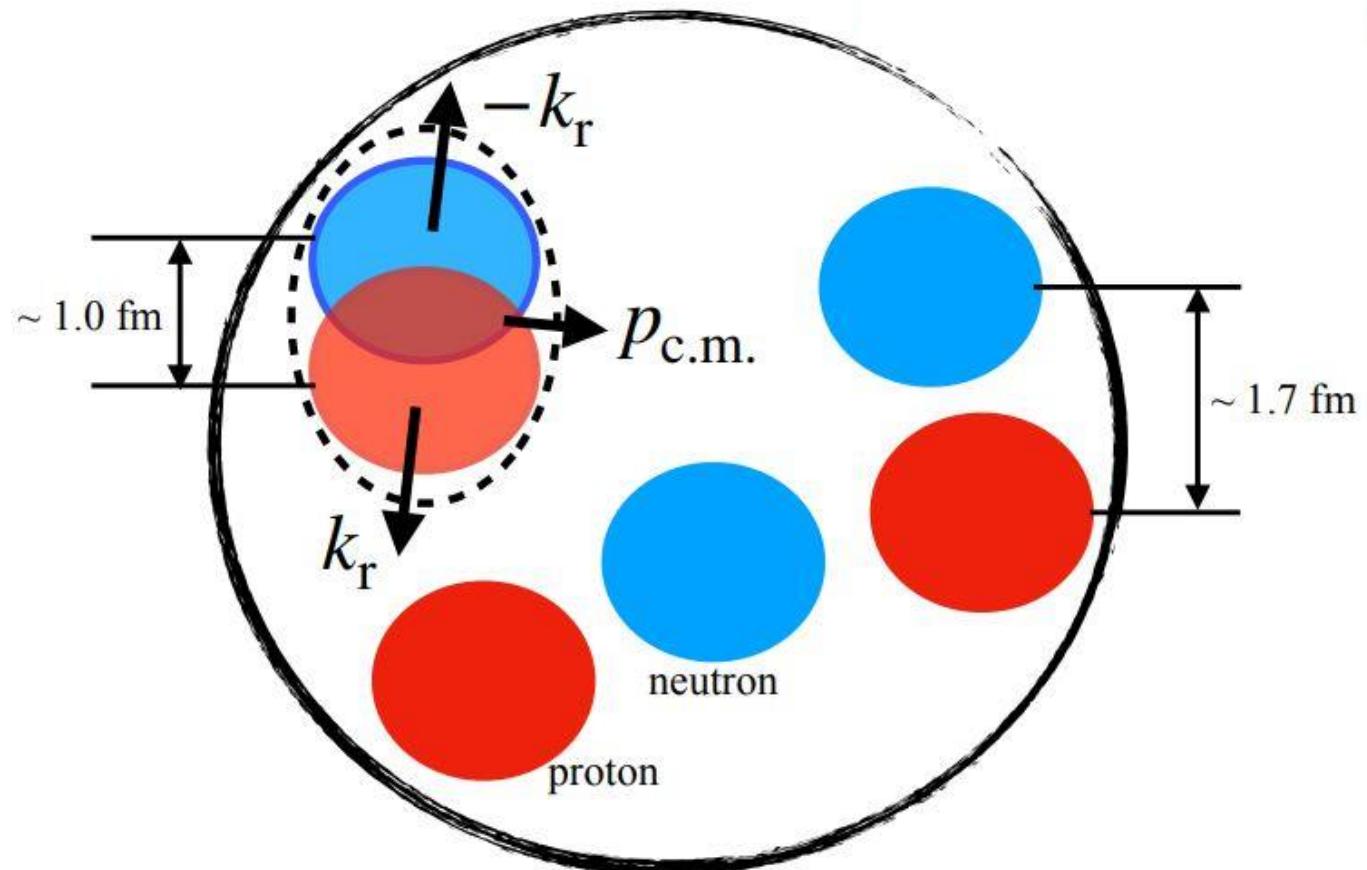


# Outline

- Motivation
- Systematic Uncertainties
  - Cut Variations
  - Radiative Corrections
  - Transparency
- Results

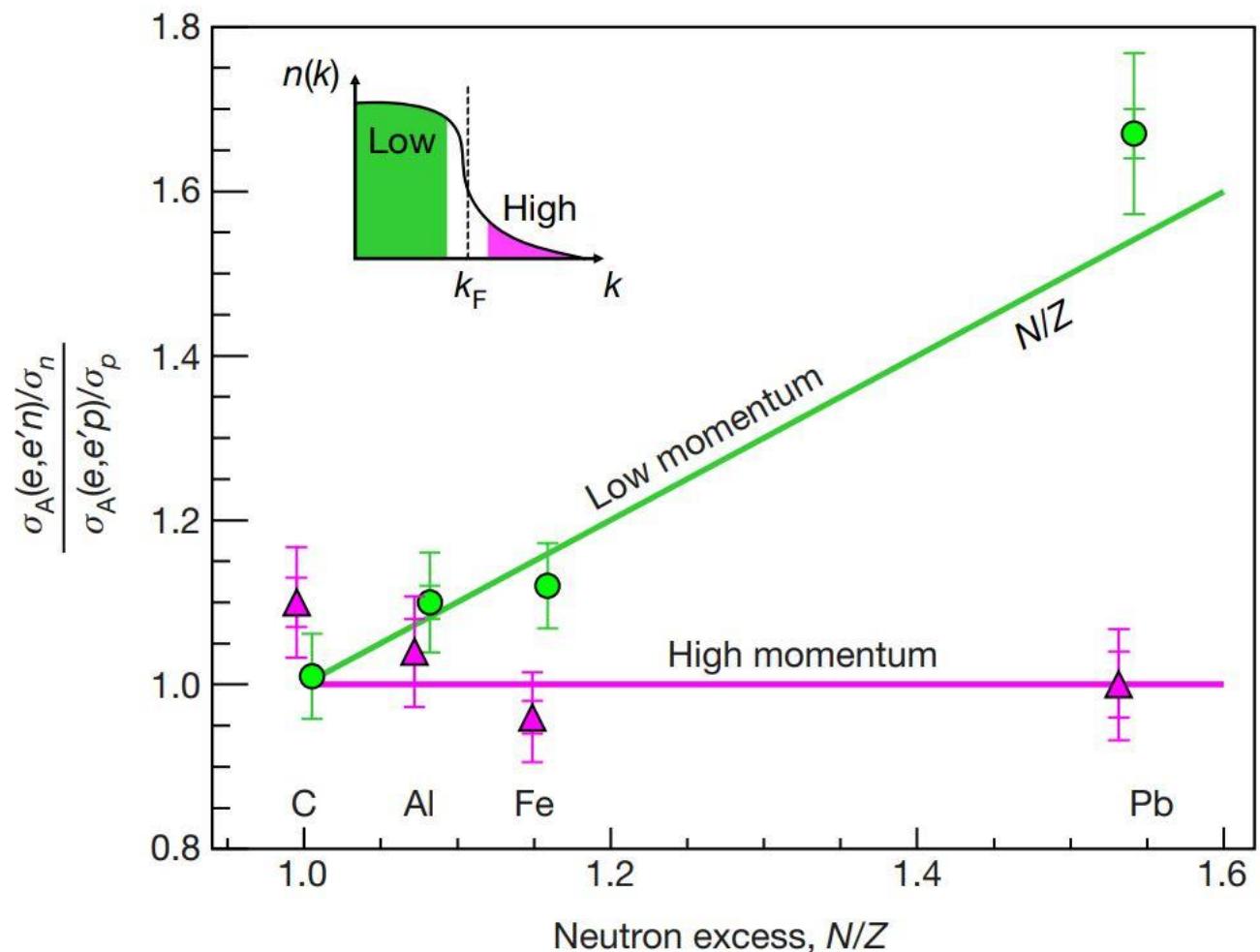
# Short Range Correlations

- SRCs are temporary short distance high momentum fluctuations
- High relative momentum ( $k_r > k_F \sim 250 \text{ MeV}/c$ )
  - Depends on the short-range part of the N-N interaction
- Unchanged center-of-mass momentum
- Open questions
  - Momentum structure
  - 3 nucleon correlations
  - Which nucleons pair



# $np$ -dominance in Asymmetric Nuclei

- $A(e,e'n)/A(e,e'p)$  cross-section ratio
- Low missing momentum n/p ratio grows like  $N/Z$
- High missing momentum n/p ratio is constant
- This is consistent with np pair dominance

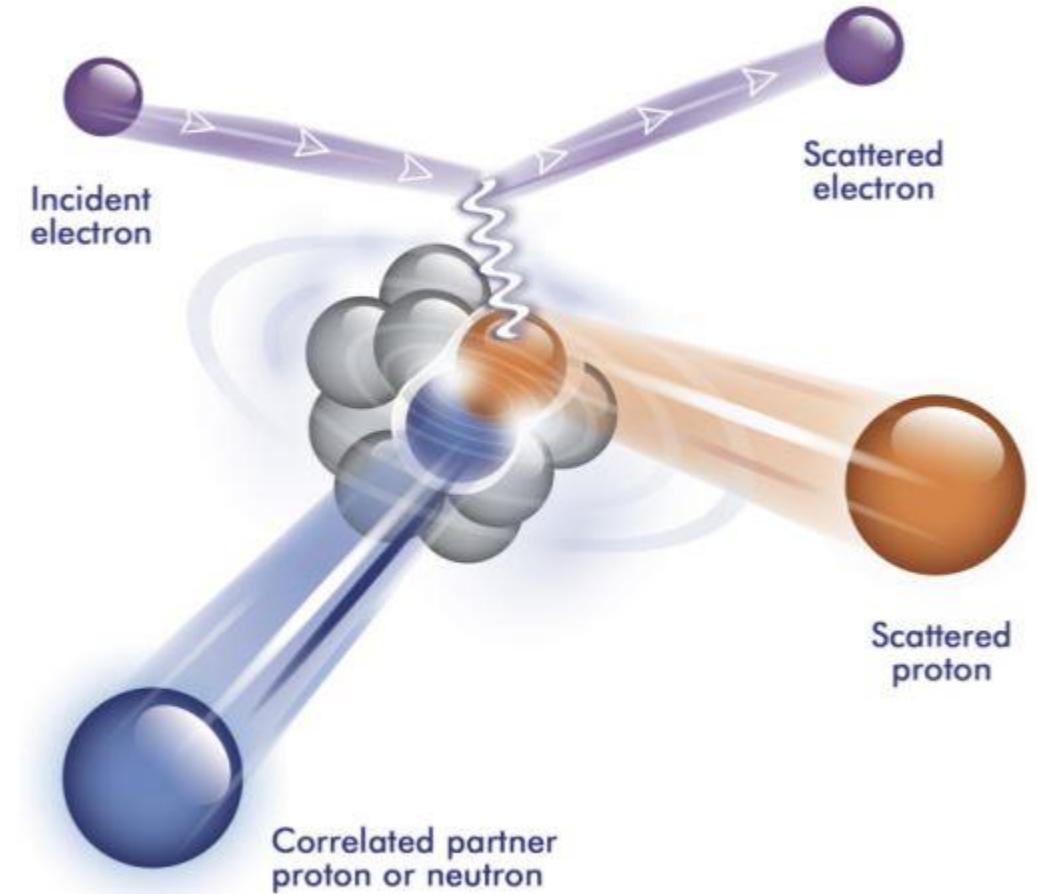


M. Duer et al., Nature 560, 617 (2018)  
<https://www.nature.com/articles/s41586-018-0400-z>

# CaFe Motivation

## Which nucleons form SRC pairs?

- Compare number of high-momentum (paired) protons in  $^{40}\text{Ca}$ ,  $^{48}\text{Ca}$ , and  $^{54}\text{Fe}$ 
  - $^{40}\text{Ca}$ : filled 1s, 1p, and 2s/1d p and n shells
  - $^{48}\text{Ca}$ : add 8  $f_{7/2}$  neutrons
  - $^{54}\text{Fe}$ : add 6  $f_{7/2}$  protons
  - First Paper
- Measure  $A(e,e'p)$  on d,  $^9\text{Be}$ ,  $^{10,11}\text{B}$ ,  $^{12}\text{C}$ ,  $^{40,48}\text{Ca}$ ,  $^{54}\text{Fe}$ , and  $^{197}\text{Au}$  at high and low missing momentum
  - $^9\text{Be}$ - $^{10}\text{B}$ - $^{11}\text{B}$ - $^{12}\text{C}$  quartet and  $^{40}\text{Ca}$ - $^{48}\text{Ca}$ - $^{54}\text{Fe}$  triplet



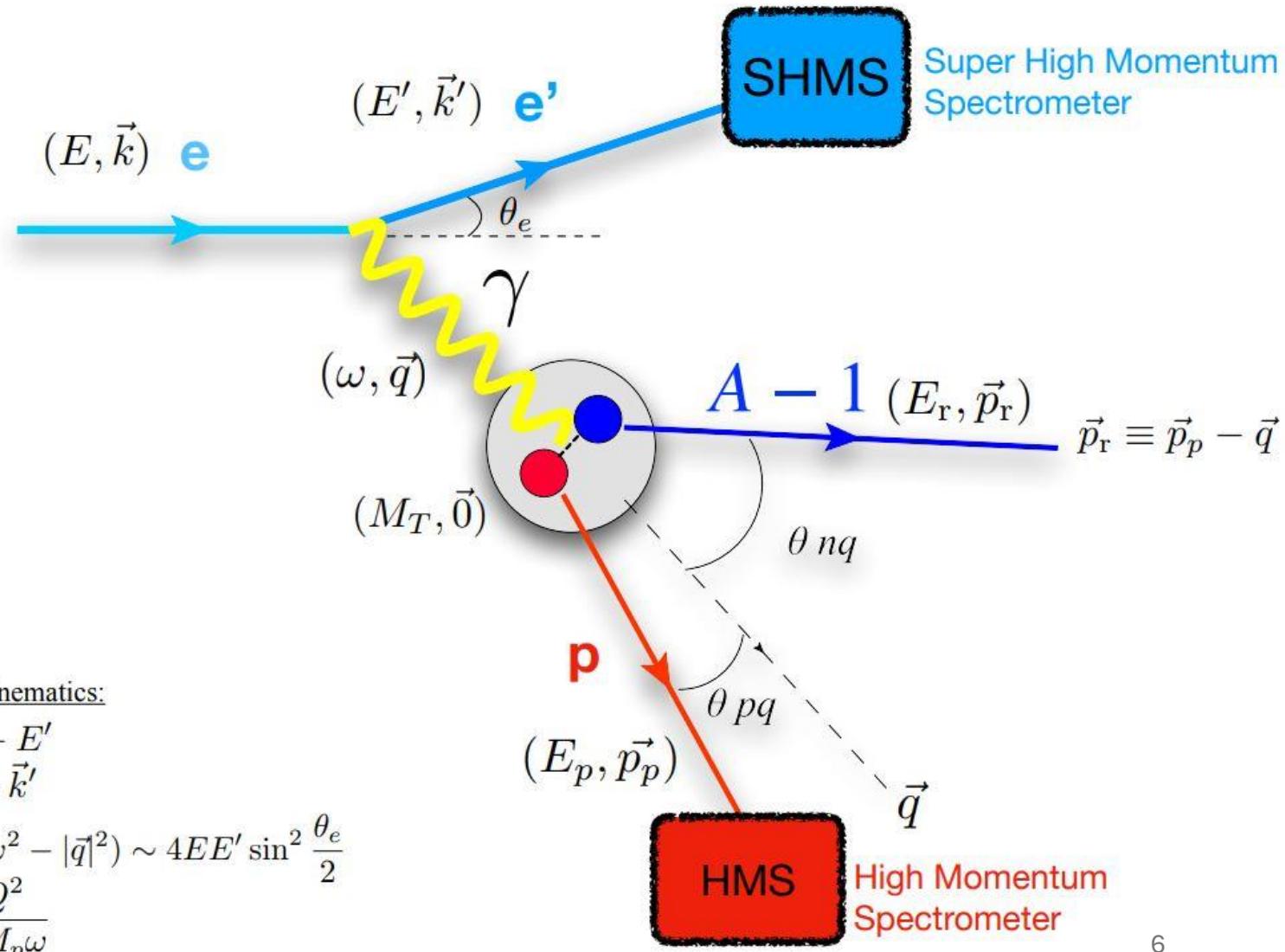
Separate A and N/Z dependence on pairing

# Hall C: Experimental Setup Cont.

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- $E_0 = 10.6 \text{ GeV}$
- $E' = 8.55 \text{ GeV}$
- $\Theta_e = 8.3 \text{ Degrees}$
- $Q^2 = 2.1 (\text{GeV}/c)^2$
- $P_{\text{miss}} \approx 400 \text{ MeV}/c$ 
  - $|P_p| = 1.325 \text{ GeV}/c$
  - $\Theta_p = 66.4^\circ$
- $P_{\text{miss}} \approx 150 \text{ MeV}/c$ 
  - $|P_p| = 1.820 \text{ GeV}$
  - $\Theta_p = 48.3 \text{ Degrees}$

General  $A(e, e'p)$  Kinematics

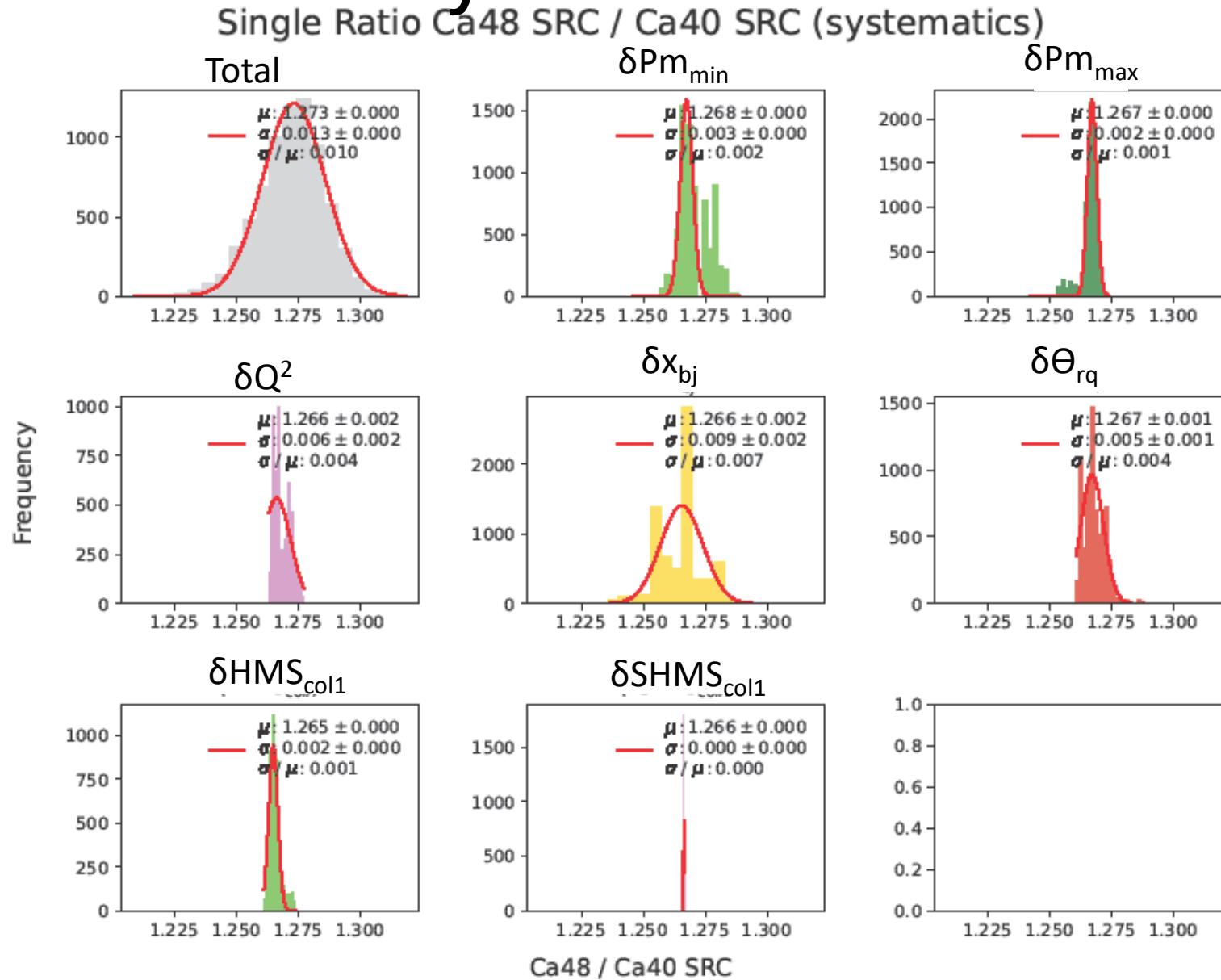


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# Cut Variations

- Examine how sensitive the data is to cuts (systematic uncertainty)
- Data Selection Cuts (**and  $2\sigma$  cut variations**)
  - PID
    - $0.8 < \frac{E_{\text{tot}}}{P_{\text{cent}}} < 1.3$
    - $-2.0 < \text{ep Coin Time} < 2 \text{ ns}$
  - Acceptance
    - Collimator Cut  $\pm 8 \%$
  - Kinematics
    - $Q^2 > 1.8 \pm 0.1 \text{ GeV}/c^2$
    - MF
      - $P_m < 0.27 \pm 0.02 \text{ GeV}/c$
      - $-0.02 < E_m < 0.09 \pm 0.005 \text{ GeV}$
    - SRC
      - $0.375 \pm 0.025 < P_m < 0.7 \pm 0.1 \text{ GeV}/c$
      - $x_{bj} > 1.2 \pm 0.1$
      - $\theta_{rq} < 40 \pm 4 \text{ deg}$

# SRC Ratio Uncertainty



# Cut Variation: Single & Double Ratios

Ratios to C							
Single Ratio (%)	Be9/C12	B10/C12	B11/C12	Ca40/C12	Ca48/C12	Fe54/C12	Au197/C12
$\sigma/\mu$ (MF)	0.4	0.2	0.1	0.3	0.5	0.3	0.7
$\sigma/\mu$ (SRC)	1.3	1.0	0.9	2.2	3.1	2.4	4.9
Double Ratio (%)	Be9/C12	B10/C12	B11/C12	Ca40/C12	Ca48/C12	Fe54/C12	Au197/C12
$\sigma/\mu$	1.4	1.0	0.9	2.2	3.1	2.4	4.9

Ratio to Ca40		
Single Ratio (%)	Fe54/Ca40	Ca48/Ca40
$\sigma/\mu$ (MF)	0.4	0.3
$\sigma/\mu$ (SRC)	1.0	1.0
Double Ratio (%)	Fe54/Ca40	Ca48/Ca40
$\sigma/\mu$	1.1	1

SRC uncertainties dominate and increase with larger differences between nuclei.

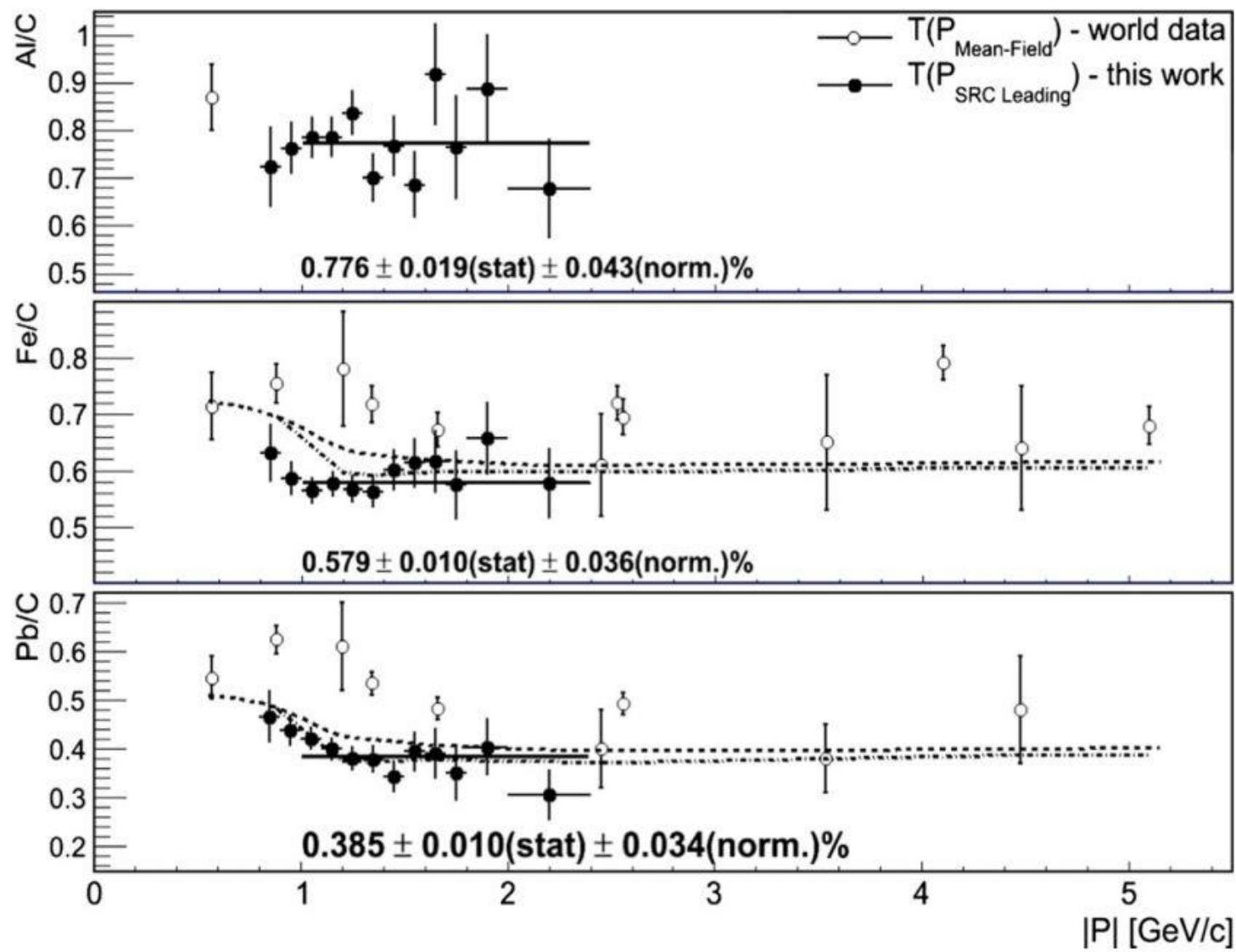
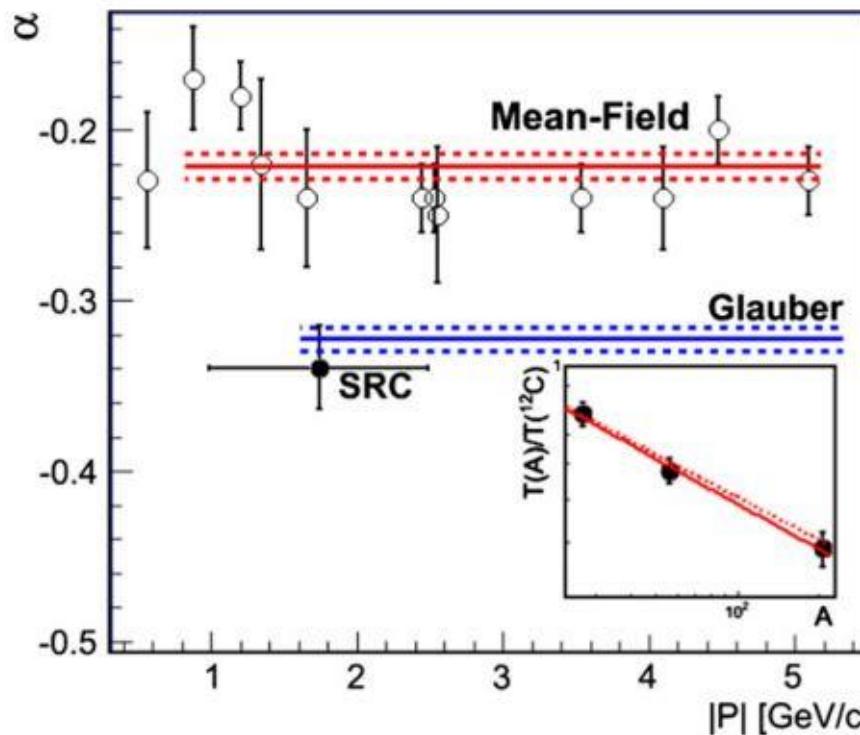
# Radiative Correction Factors

Kinematics	MF			SRC		
Target	C12	Fe56	Au197	C12	Fe56	Au197
Rad/Norad Ratio	0.618	0.577	0.451	0.742	0.734	0.604
Stat Uncertainty	0.009	0.006	0.005	0.007	0.012	0.014
Cut Var. Uncertainty	0.005	0.004	0.003	0.03	0.04	0.04

- Ratios of corrections are important
  - MF to SRC
  - Different Nuclei
  - Small A dependence implies corrections mostly cancel

# Proton Transparency

- Use measured ratios to C
- $T(A) \propto A^{-0.34 \pm 0.02}$



# Systematic Uncertainties CaFe Triplet

Systematic Uncertainties (%)				
Ratio	Radiative Correction	Transparency	Cut Variation	Net
MF Single Ratio				
Ca48/Ca40	0	0.4	0.3	0.7
Fe54/Ca48	1.0	0.6	0.4	1.2
SRC Single Ratio				
Ca48/Ca40	0	0.4	0.7	0.8
Fe54/Ca48	1.0	0.6	1	1.5
Double Ratio				
Ca48/Ca40	0	0.0	0.8	0.8
Fe54/Ca48	1.0	0.0	1.1	1.5

# Ratios

- Single
  - $R = \frac{Y_A}{Y_{C^{12}}}$
- Double
  - Normalization Factors Cancel
  - MF should be proportional to number protons
  - SRC should reflect probability of being in SRC
  - Additional Corrections for
    - Random coincidences
    - Oil contamination (Ca targets)
    - Isotopic Impurity (Ca48 90.5%)
    - Chemical Impurity ( $B_4C$ )

$$Y_A : \frac{N}{Q \cdot \epsilon_i \cdot T_N \cdot \sigma_t \cdot Z/A}$$

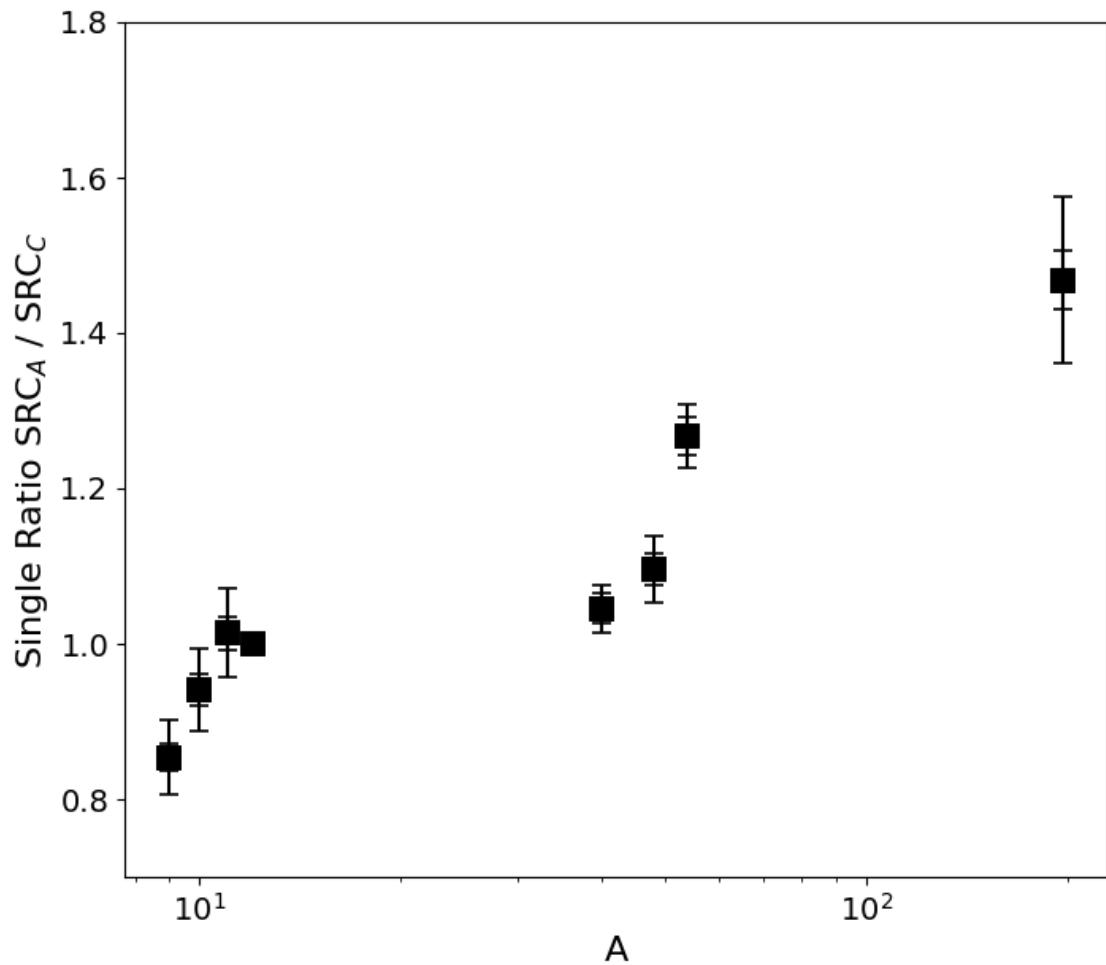
$Y_A$  : nucleus A yield  
 $N$  :  $(e, e'p)$  coincidence counts  
 $Q$  : total charge [mC]  
 $\epsilon_i$  : detector/DAQ efficiencies  
 $T_N$  : nuclear transparency  
 $\sigma_t$  : target thickness [ $g/cm^2$ ]

Double Ratios

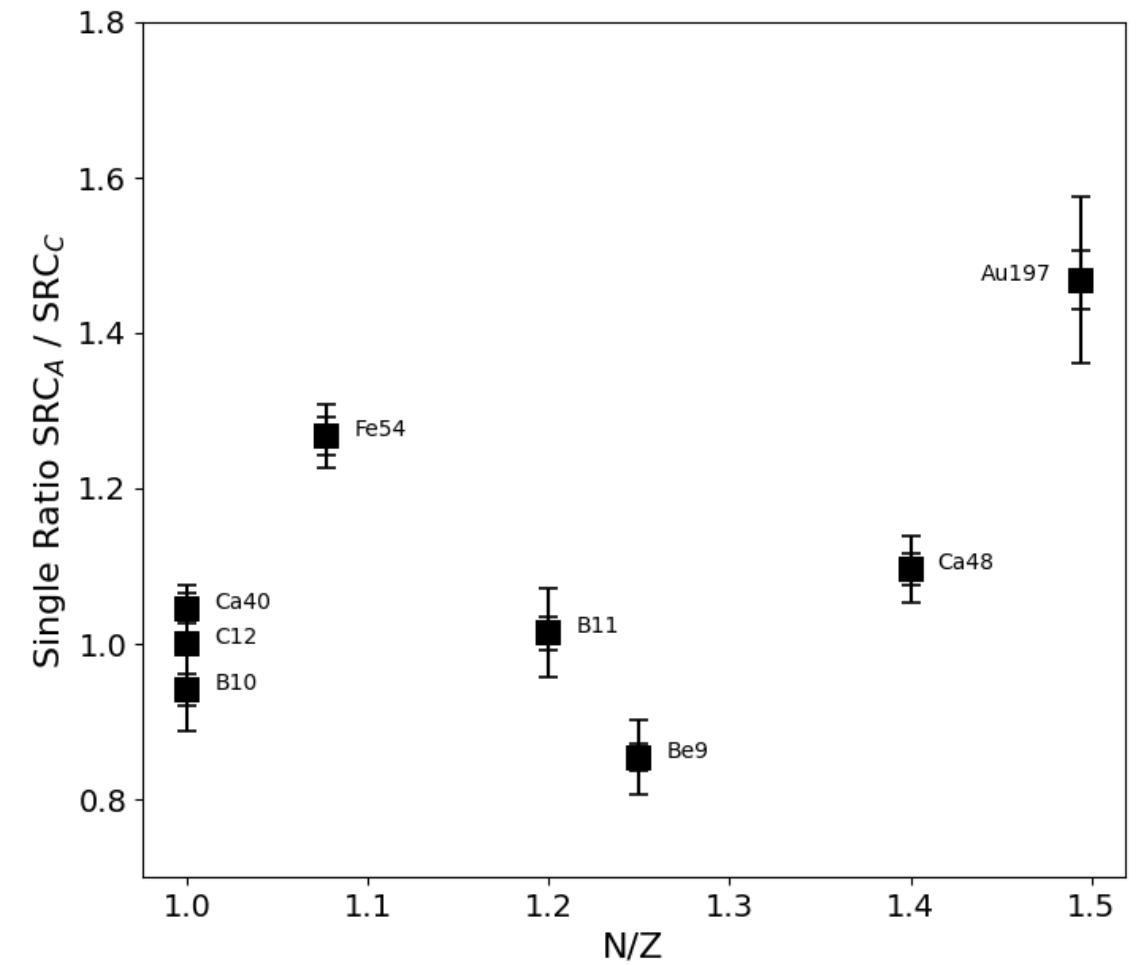
$$\frac{A(e, e'p)^{SRC}/A(e, e'p)^{MF}}{^{12}C(e, e'p)^{SRC}/^{12}C(e, e'p)^{MF}}$$

Pairing depends on A (not N/Z)

SRC Single Ratio increases with A



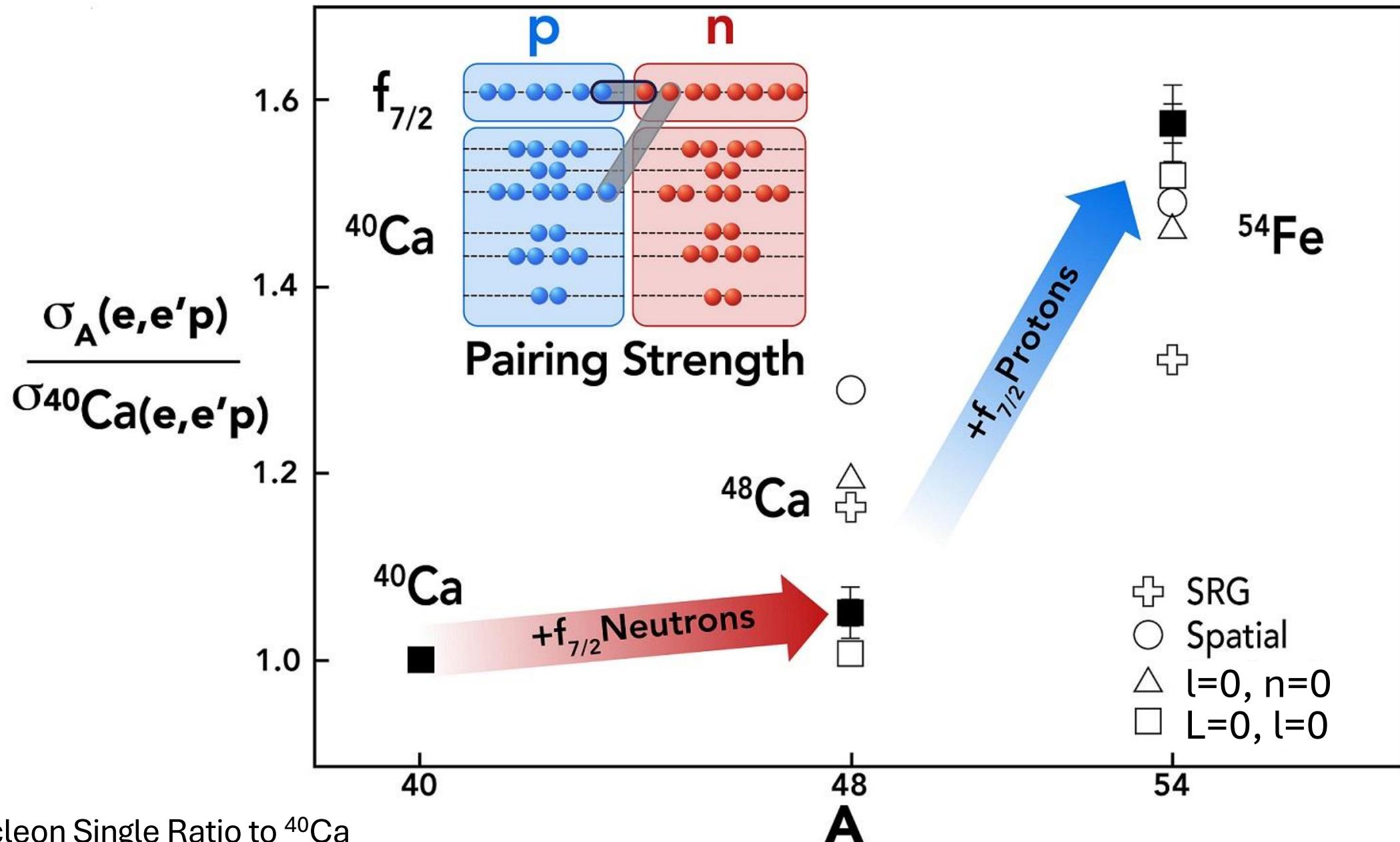
Per Proton Single SRC Ratio to C



# Models

- SRG
  - Calculation of the nuclear momentum distribution
- Spatial
  - Counts the number of protons and neutrons within 1 Fermi of each other
    - A. Denniston & J. Estee, personal communication
- $l=0, n=0$ 
  - Counts the number of proton-neutron pairs in a relative  $l=0, n=0$  state.
    - Colle et al, Physical Review C 92 (2015)
- $L=0, l=0$ 
  - Counts the number of proton-neutron pairs in a relative  $L=0, l=0$  state.
    - Jerry Miller, personal communication

# SRC Enhancement



# Conclusion

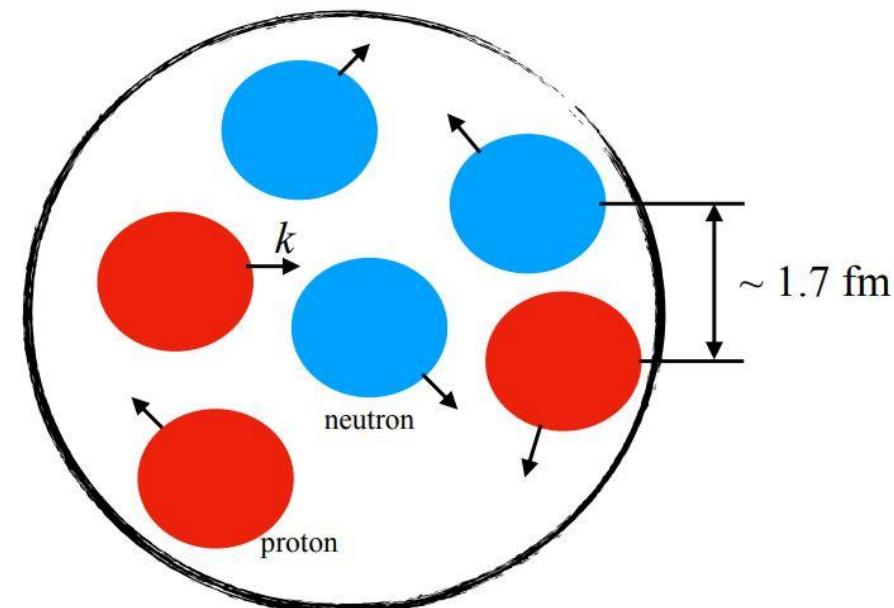
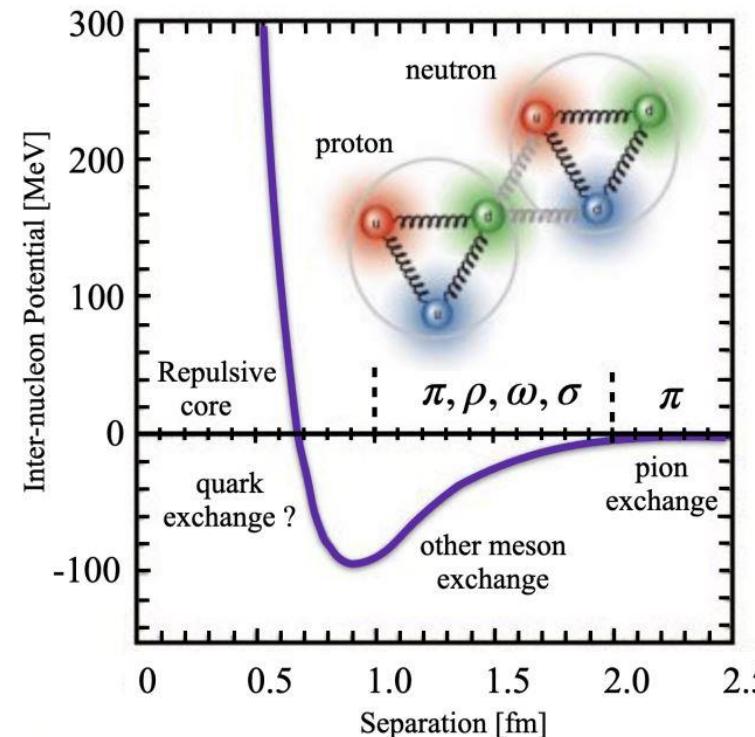
- The SRC Single Ratio is A dependent
- The  $^{48}\text{Ca}/^{40}\text{Ca}$  SRC Single Ratio lower than expected
- The  $^{54}\text{Fe}/^{40}\text{Ca}$  SRC Single Ratio higher than expected
- Implies
  - Strong **Intra**-shell pairing in the  $f^{7/2}$  shell
  - Weak **Inter**-shell pairing between the  $f^{7/2}$  shell and  $^{40}\text{Ca}$  core

# Questions?

# Backup

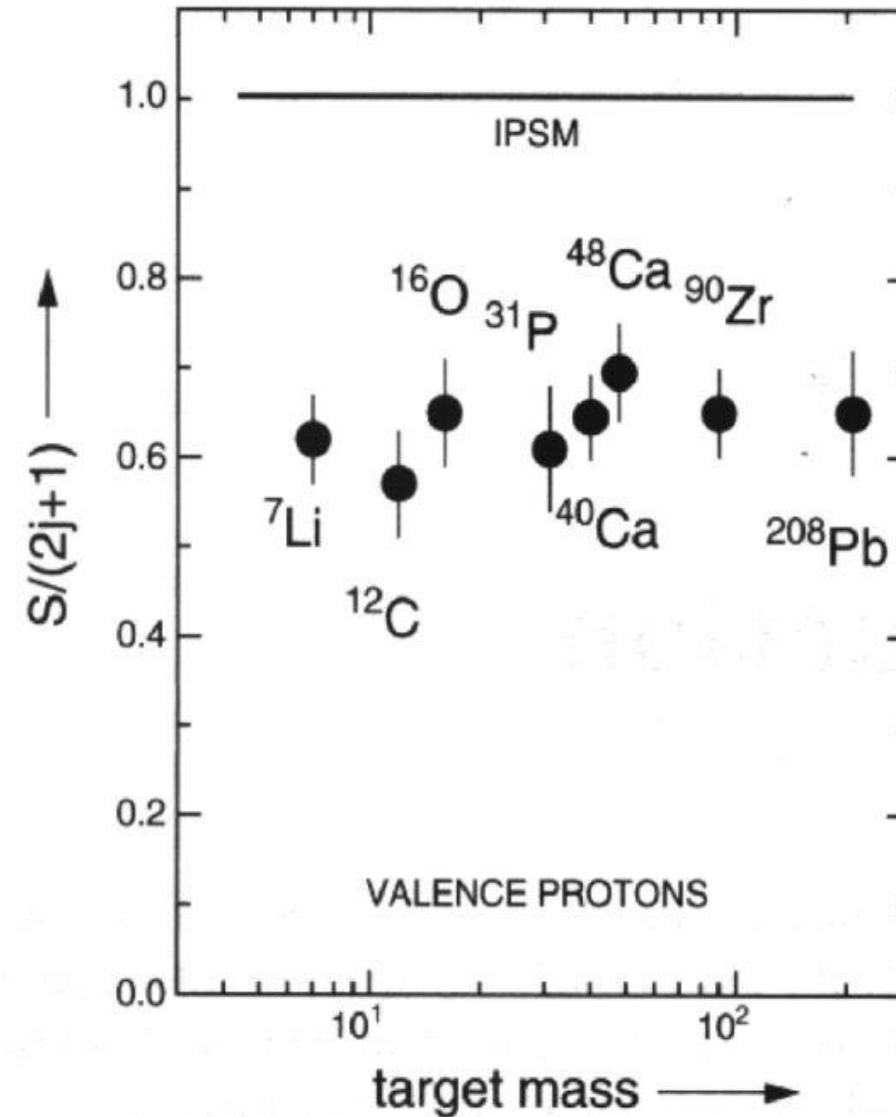
# Nuclear Shell Model

- The nucleus consists of  $A$  nucleons interacting via the Strong Interaction
- Nucleons move independently in a mean field generated by the other ( $A-1$ ) nucleons
- Successfully describes bulk properties of nuclei
  - Shell structure
  - Excitation energies
  - Spin, parities
  - Nuclear magic numbers
- Typical momentum less than Fermi momentum,  $k_F \sim 250$  MeV/C



# Limitations of the Nuclear Shell Model

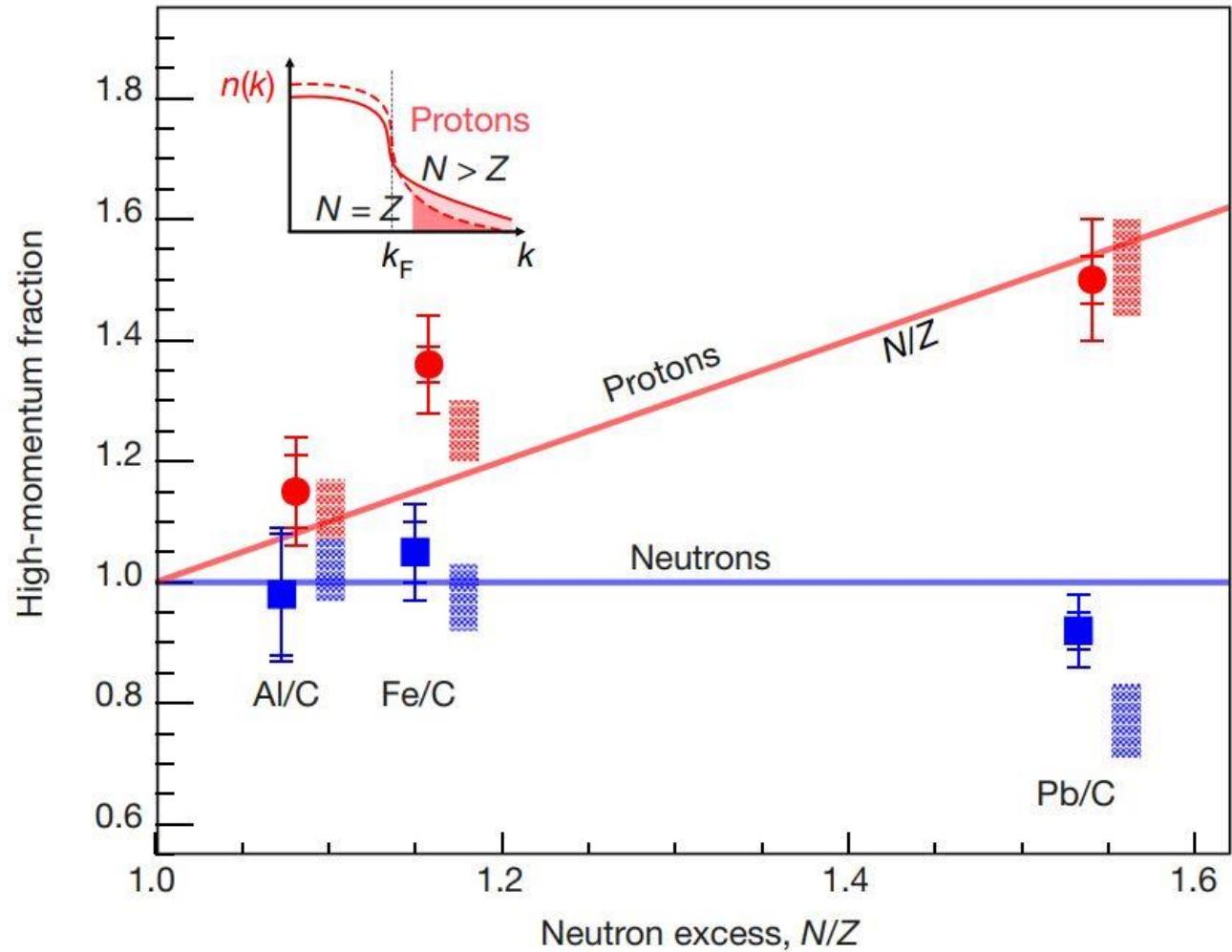
- Measured ( $e, e' p$ ) proton knockout from valence shells
  - Found ~60-70% of predicted occupancy
- Corrections
  - Long range correlations
  - Short range correlations (SRCs)
    - 20-25%



O. Hen, G. A. Miller, E. Piasetzky, and L.B. Weinstein, Rev. Mod. Phys. 89, 045002 (2017). [[1611.09748](https://arxiv.org/abs/1611.09748)] Nucleon-Nucleon Correlations, Short-lived Excitations, and the Quarks Within (arxiv.org)

# $np$ -dominance in Asymmetric Nuclei Cont.

- double ratio of  $(e, e' p)$ 
  - $(\text{high momentum } p \text{ or } n) / (\text{low momentum } p \text{ or } n)$  for nucleus A relative to  $^{12}\text{C}$
  - Proton ratio grows like  $N/Z$
  - Neutron ratio is near constant



M. Duer et al., Nature 560, 617 (2018)

<https://www.nature.com/articles/s41586-018-0400-z>

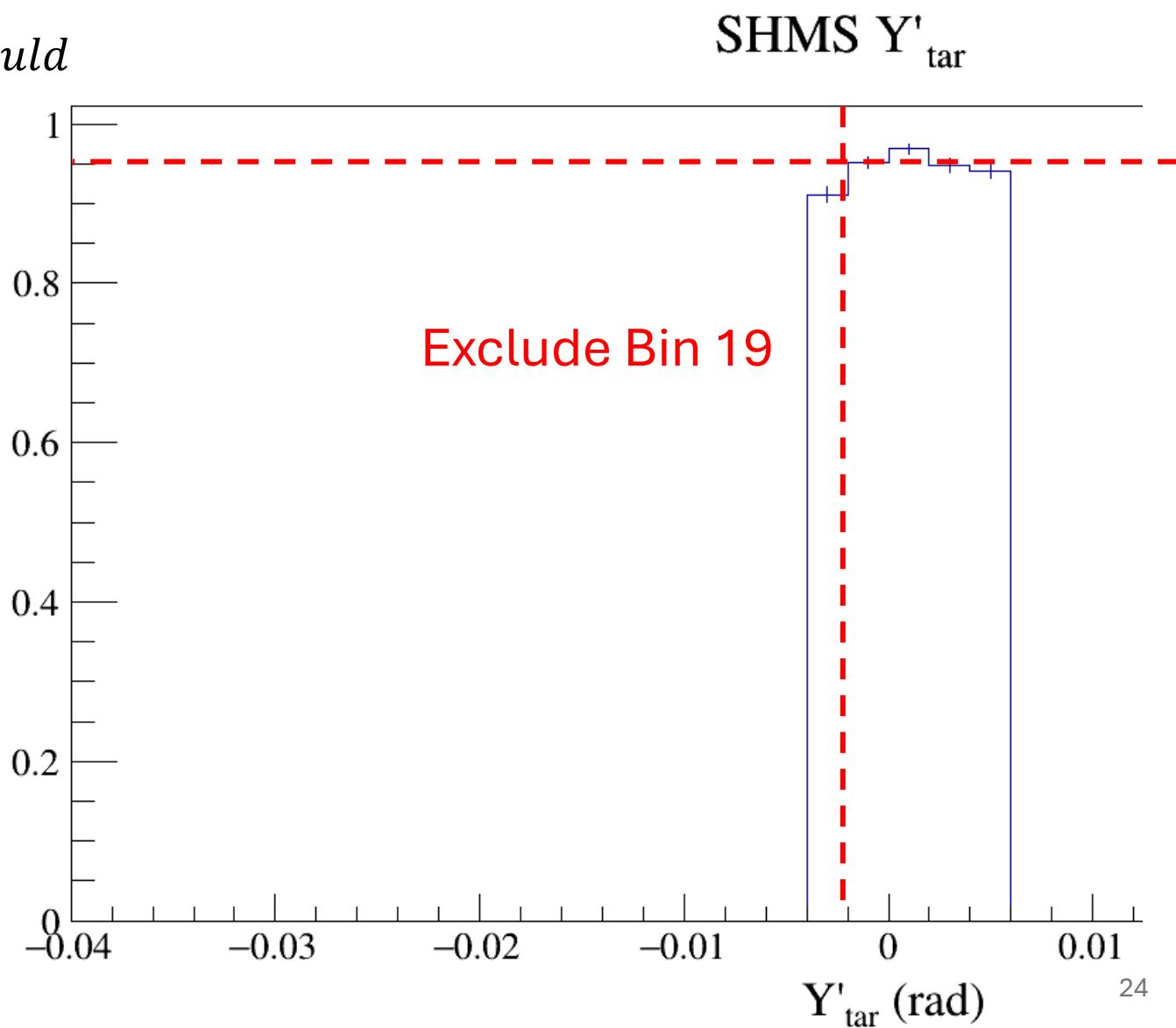
# HMS Proton Efficiency

- Measure  $H(e,e'p)/H(e,e')p$
- Select  $H(e,e')$  events that should have a proton in the HMS
  - $0.92 < W < 0.97 \text{ GeV}$
  - $-2 < z - \text{Target} < 2 \text{ cm}$
  - $-0.01 < \text{SHMS } x'_{\text{tar}} < 0.01 \text{ rad (phi)}$
  - $-0.002 < \text{SHMS } y'_{\text{tar}} < 0.006 \text{ rad (theta)}$
  - $0.8 < \frac{E_{\text{tot}}}{P_{\text{cent}}} < 1.8$
- $H(e,e'p)$  events
  - Should +
  - $-5 < \text{ep Coin Time} < 5 \text{ ns}$
  - $-0.02 < E_m < 0.9 \text{ GeV}$
- Iteratively tightened **cuts** until ratios became flat

# HMS Proton Efficiency

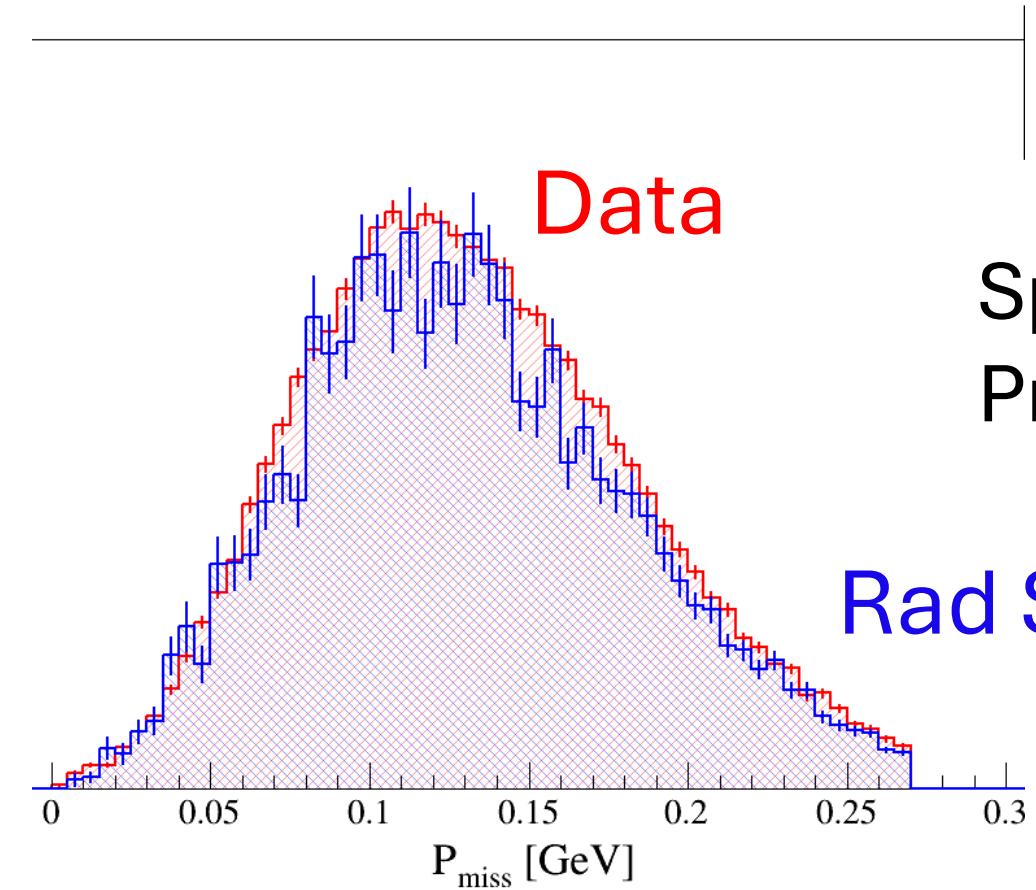
$$\sigma_{ratio}^{exact} = \sqrt{should \frac{did}{should} \left(1 - \frac{did}{should}\right) / should}$$

Proton Efficiency:  $0.952 \pm 0.004$



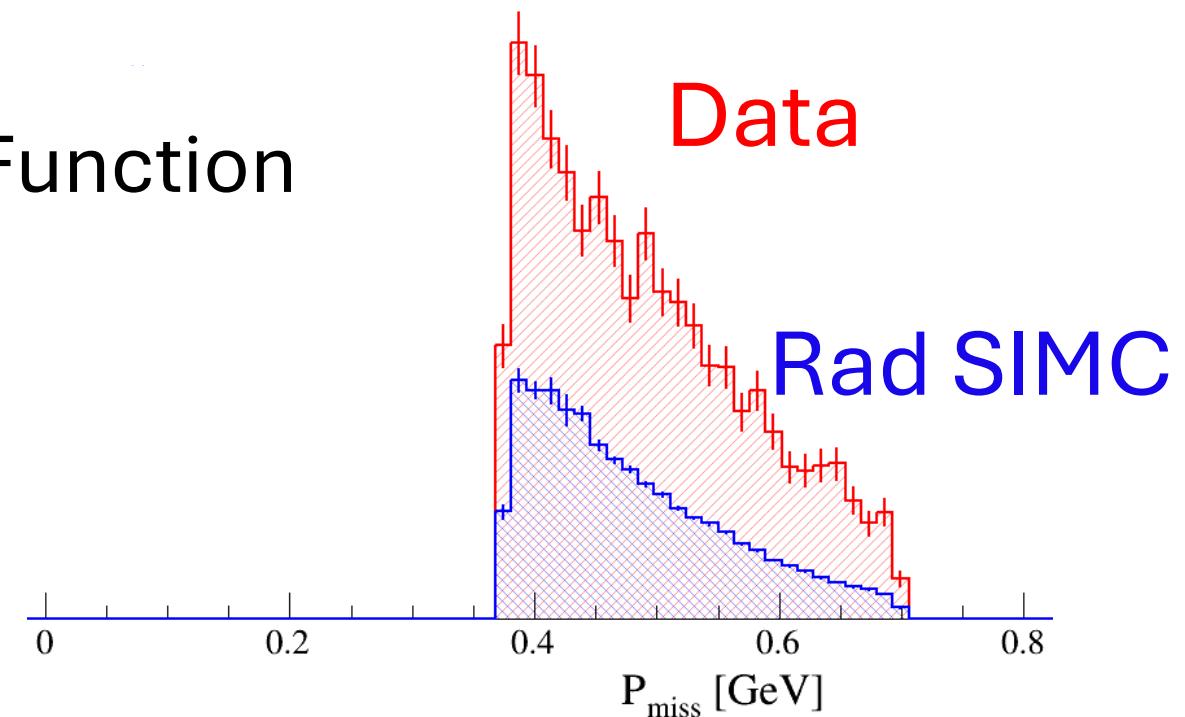
# Radiative Correction: $^{12}\text{C}$ Benhar Simc vs Data

MF Missing Momentum

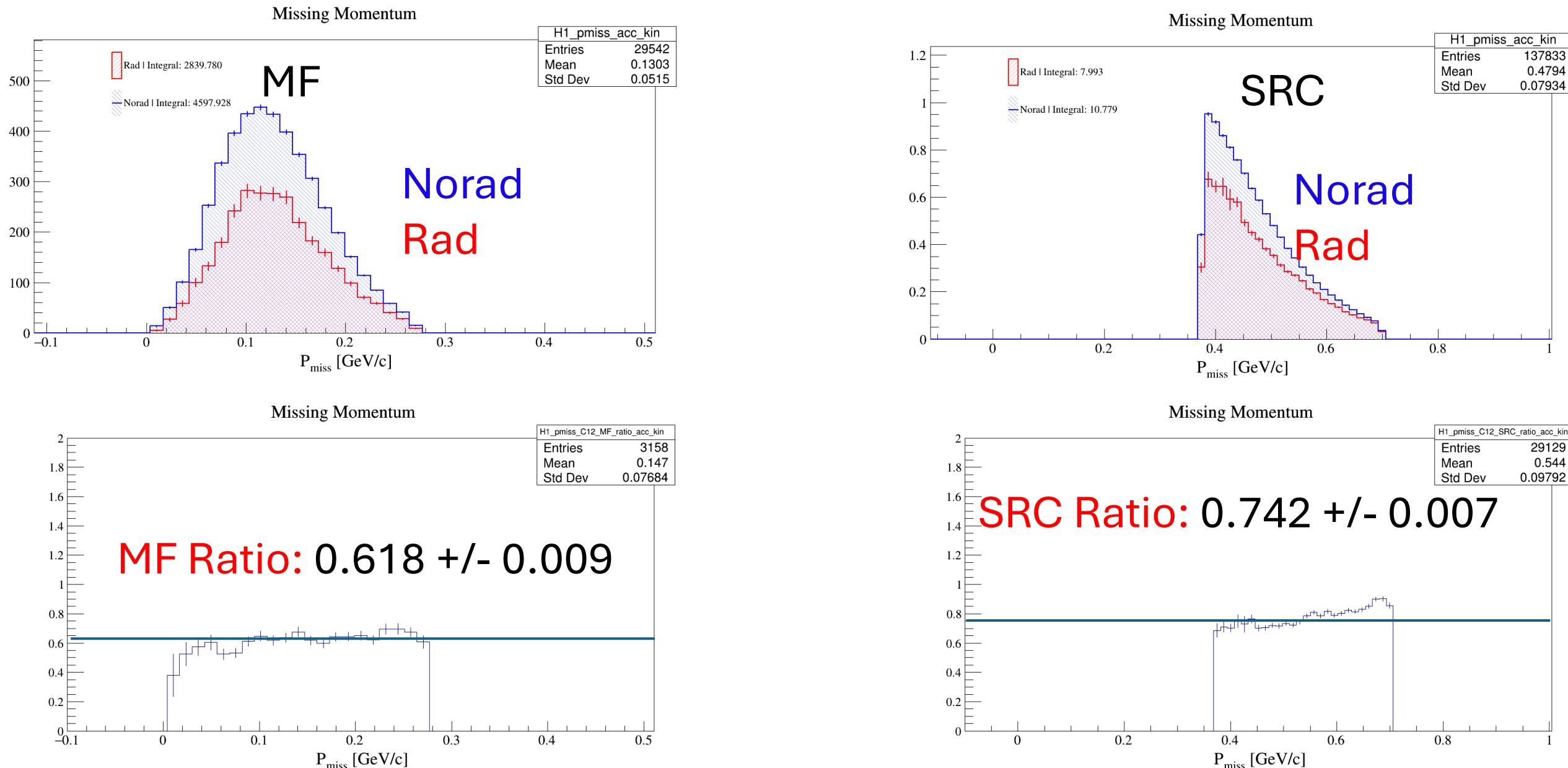


SRC Missing Momentum

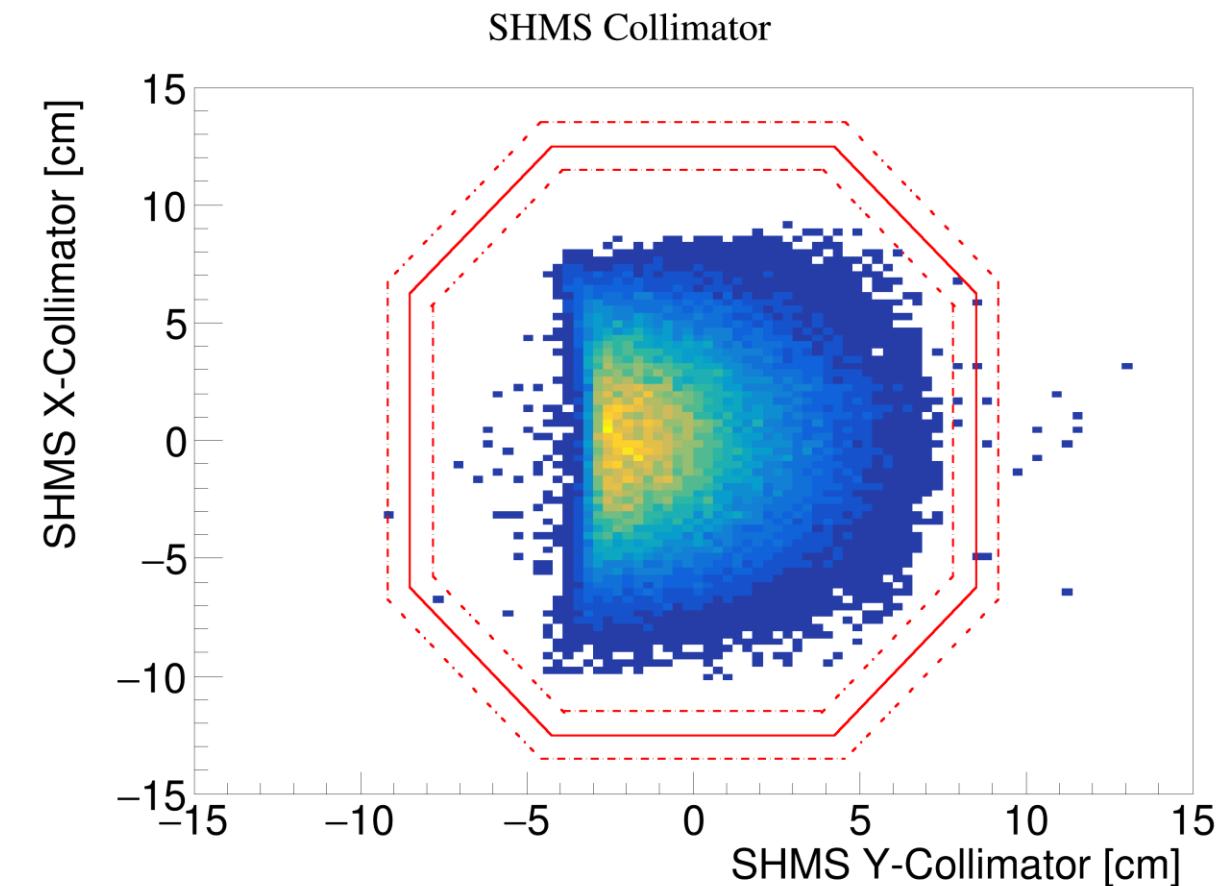
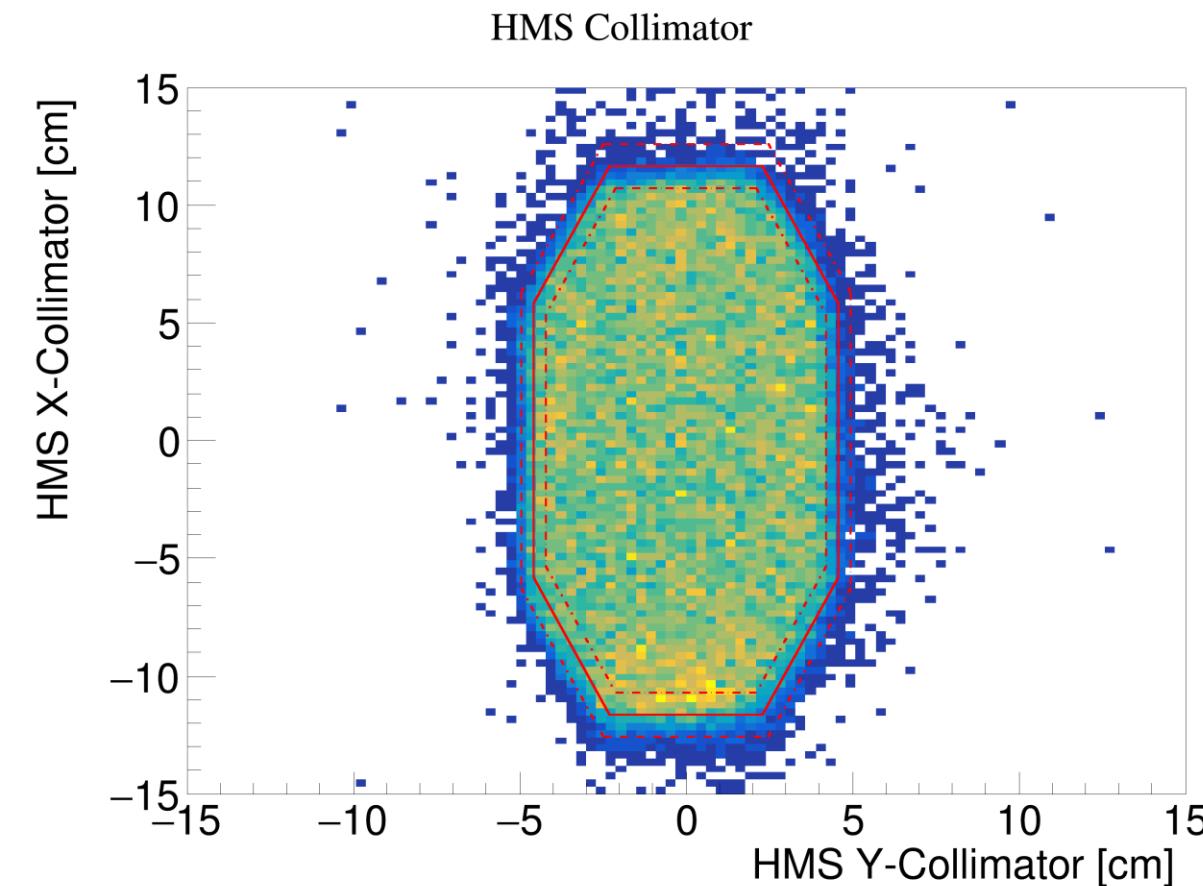
Spectral Function  
Problems



# MF & SRC $^{12}\text{C}$ $p_{\text{miss}}$ Radiative Correction

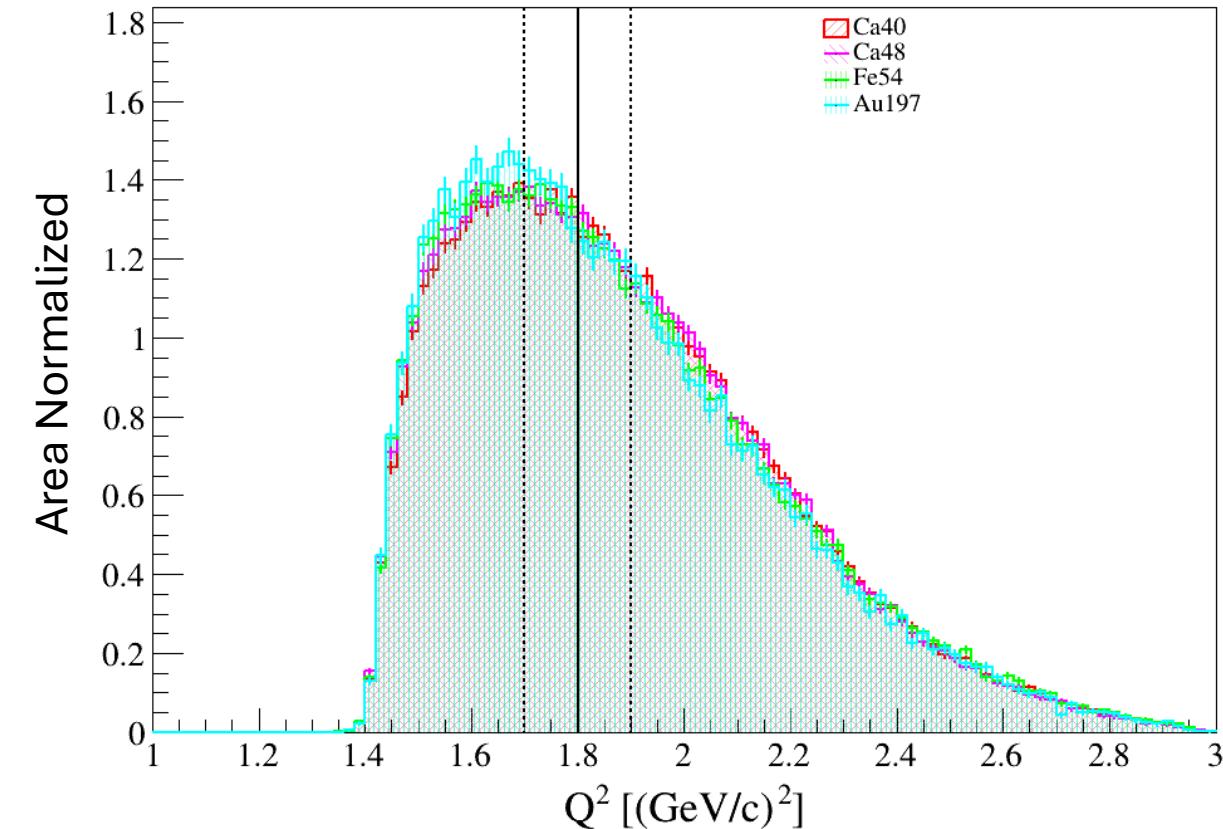


# MF HMS & SHMS Collimator Cuts ( $\pm 2\sigma$ )

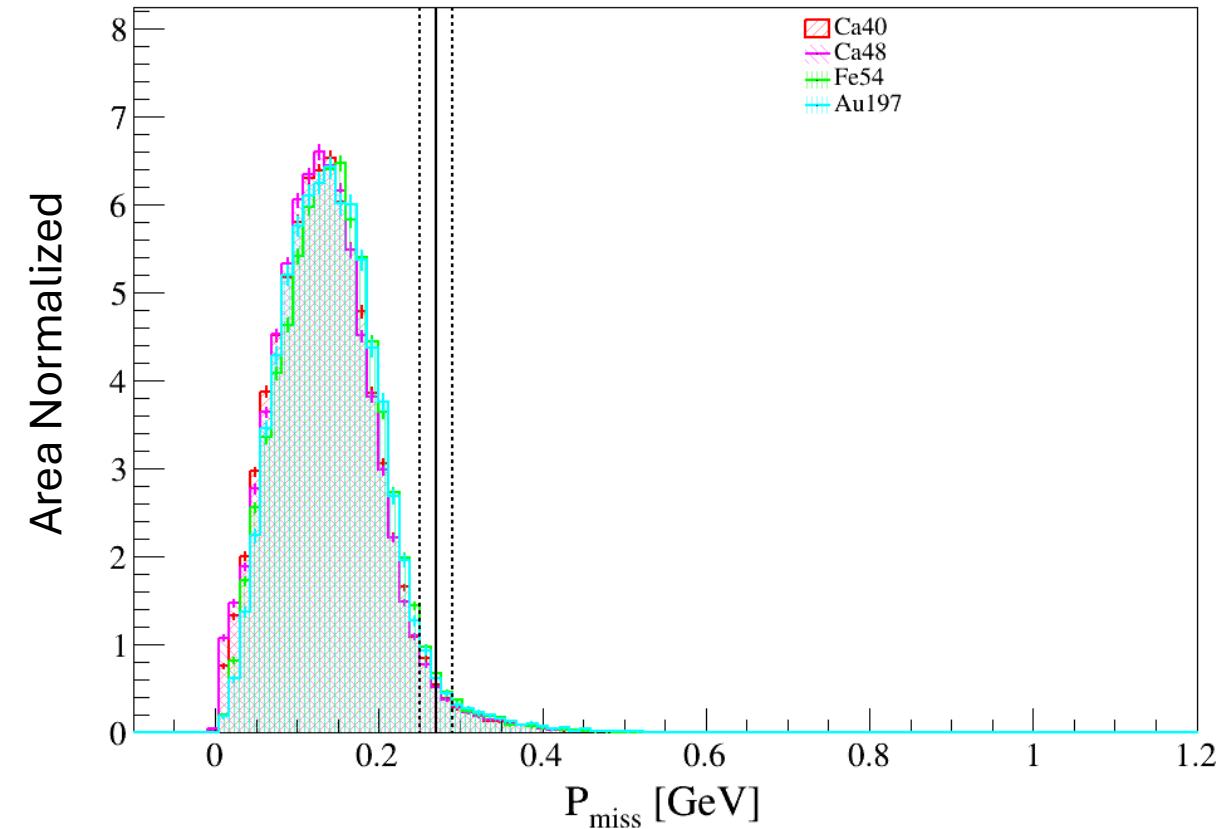


# MF $Q^2$ & $P_m$ Cuts ( $\pm 2\sigma$ )

Heavy MF 4-Momentum Transfer

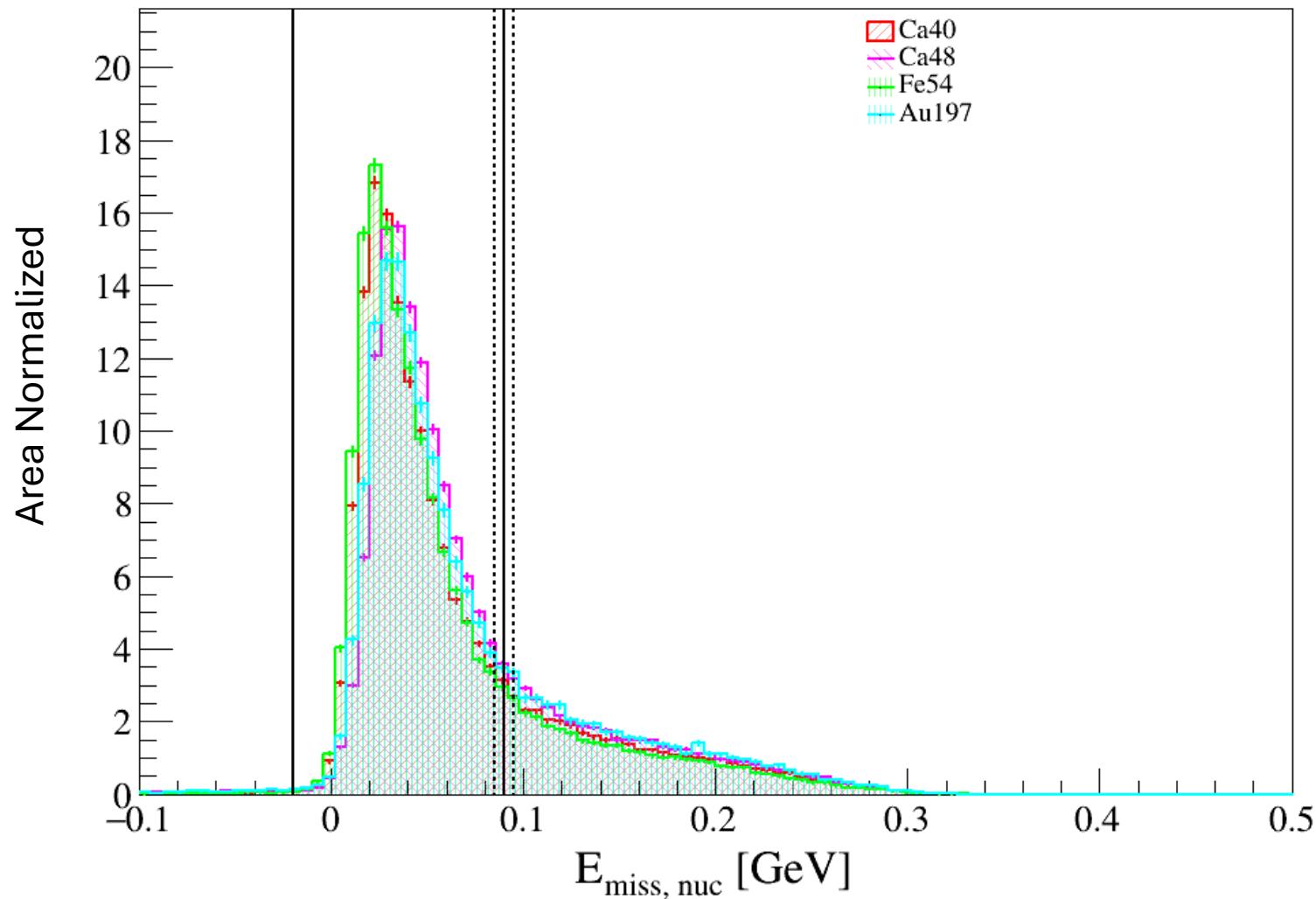


Heavy MF Missing Momentum

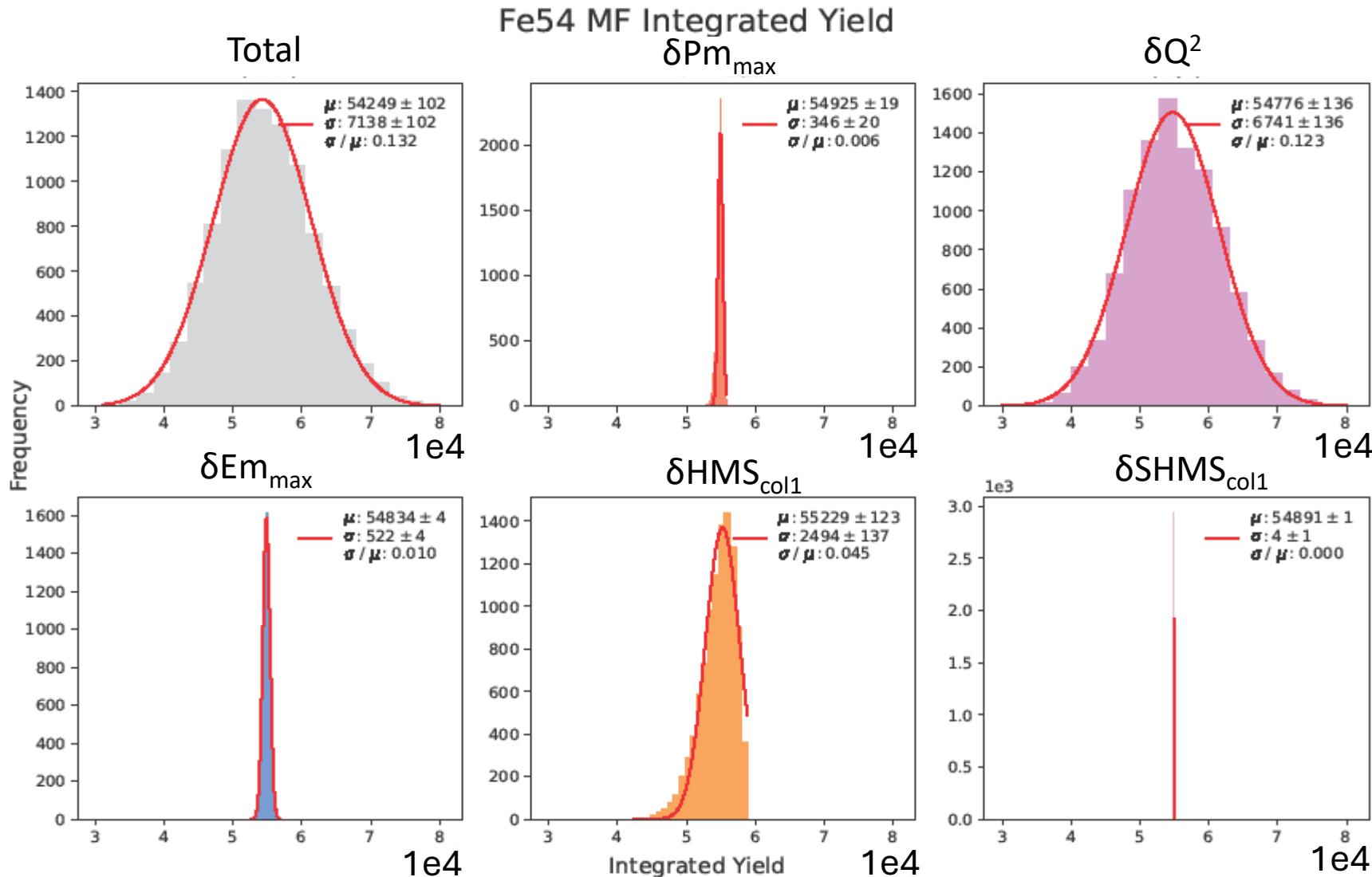


# MF $E_m$ Cuts ( $\pm 2\sigma$ )

Heavy MF Missing Energy (Nuclear Physics)



# Mean and $\sigma/\text{mean}$ : MF



$\sigma/\text{mean} \approx 13\%$  for all targets

# MF $^{48}\text{Ca}$ Em vs Pm

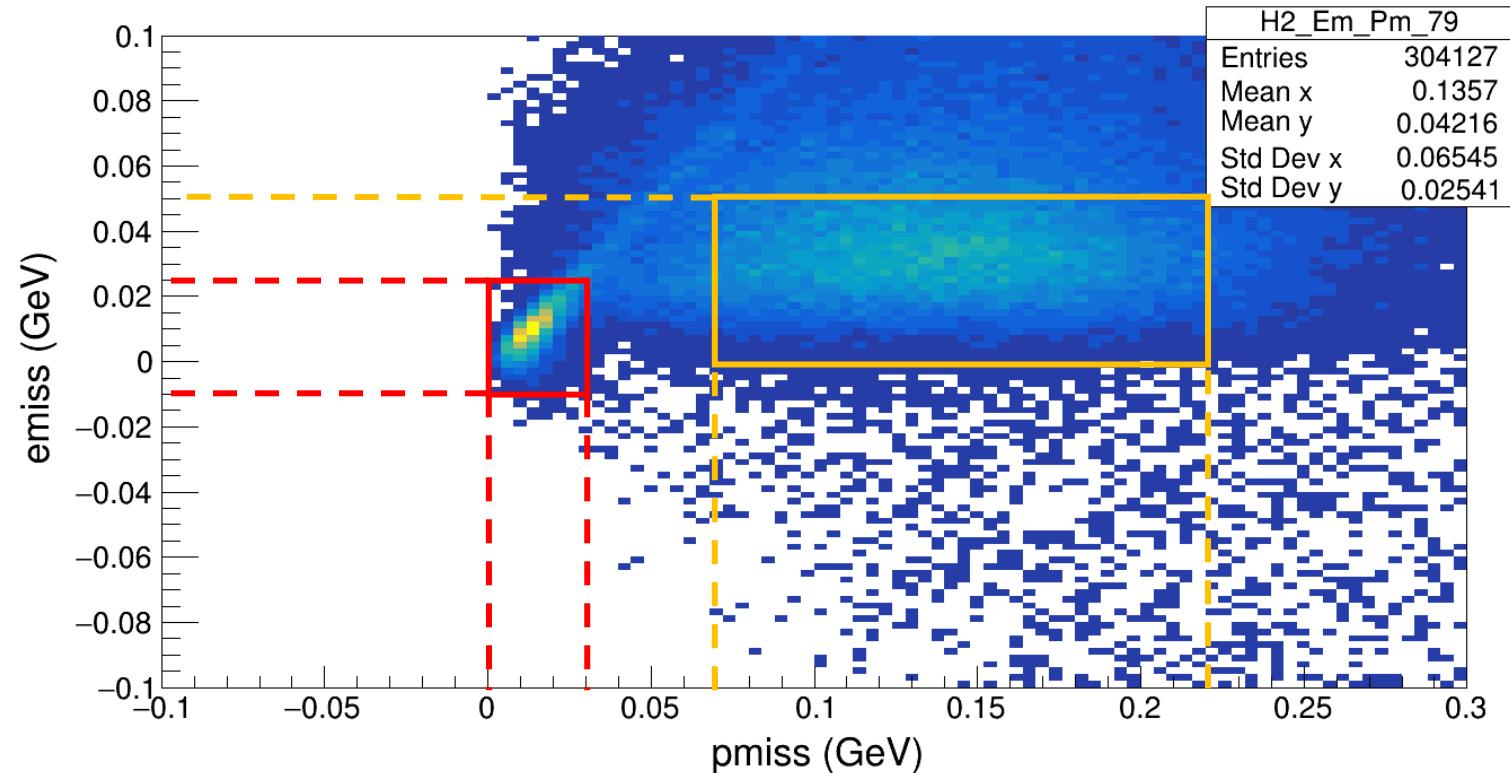
- **Hydrogen Peak**

- $-0.01 < \text{emiss} < 0.025$  (GeV)
- $0 < \text{pmiss} < 0.03$  (GeV)

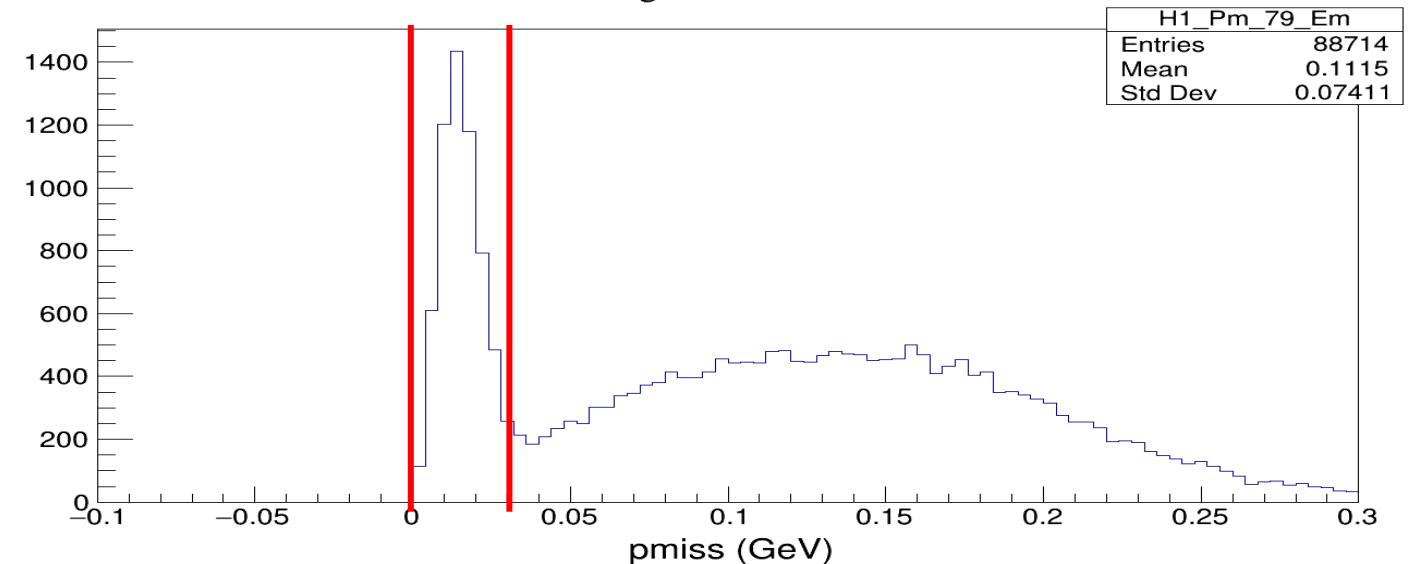
- **Signal Region**

- $0 < \text{emiss} < 0.05$  (GeV)
- $0.07 < \text{pmiss} < 0.220$  (GeV)

Missing Energy vs Missing Momentum



Missing Momentum



# $^{48}\text{Ca}$ Contamination

MF $^{48}\text{Ca}$ Data			
Run	H (mg/cm <sup>2</sup> )	Carbon (mg/cm <sup>2</sup> )	Carbon (%)
16978	6.4	38.4	3.65
16979	5.2	31.2	2.97
17093	1	6	0.57
17094	0.9	5.2	0.49
17096	0.9	5.2	0.49

# MF $^{48}\text{Ca}$ H-thickness (SIMC)

- $48Ca_{thick} = 1051 \text{ mg/cm}^2$
- $H_{thick} = \frac{\text{Data Counts}}{\text{Data Q/Simc Q} * \text{Simc Counts}} * \text{LH2 Simc thickness}$
- Run 16979
  - $H_{thick} = \frac{5969}{75.99\text{mC}/1\text{mC} * 10857.2} * 723.1 \text{ mg/cm}^2 = 5.232 \text{ mg/cm}^2$

MF $^{48}\text{Ca}$ Data				
	Run	Data Counts	Q (mC)	H-thick (mg/cm <sup>2</sup> )
MF	16978	528	5.5	6.4
	16979	5969	76.0	5.2
	17093	748	49.6	1.0
	17094	165	12.6	0.87
	17096	1290	98.5	0.87

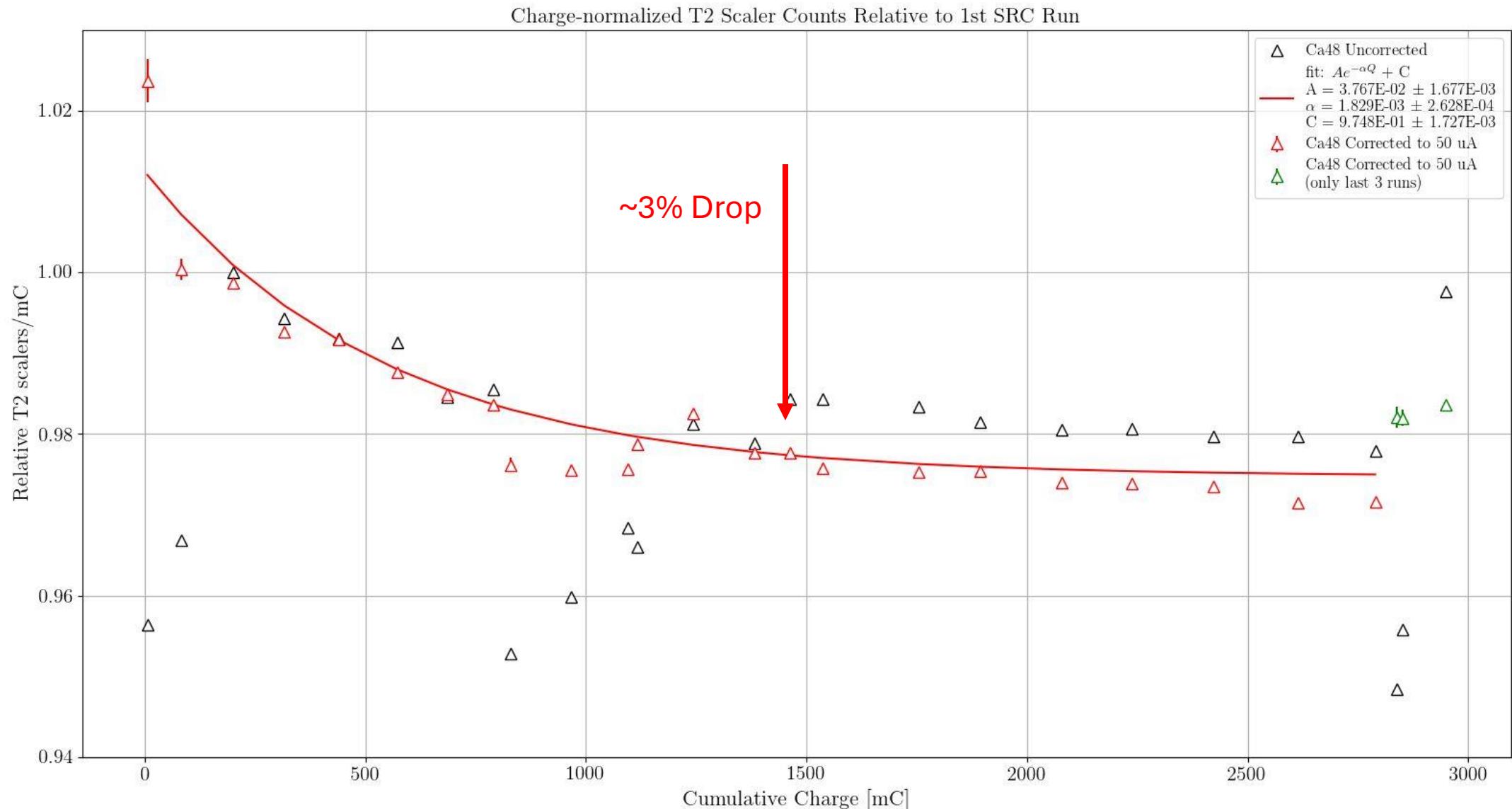
# $^{48}\text{Ca}$ : $^{12}\text{C}$ -thick

- $C_{thick} = H_{thick} \frac{12.011 \text{ g/mol}}{1.00794 \text{ g/mol}} * \frac{1 \text{ C-atom}}{2 \text{ H-atom}}$
- $\%C = \frac{C_{thick}}{^{48}\text{Ca}_{thick}} * 100$

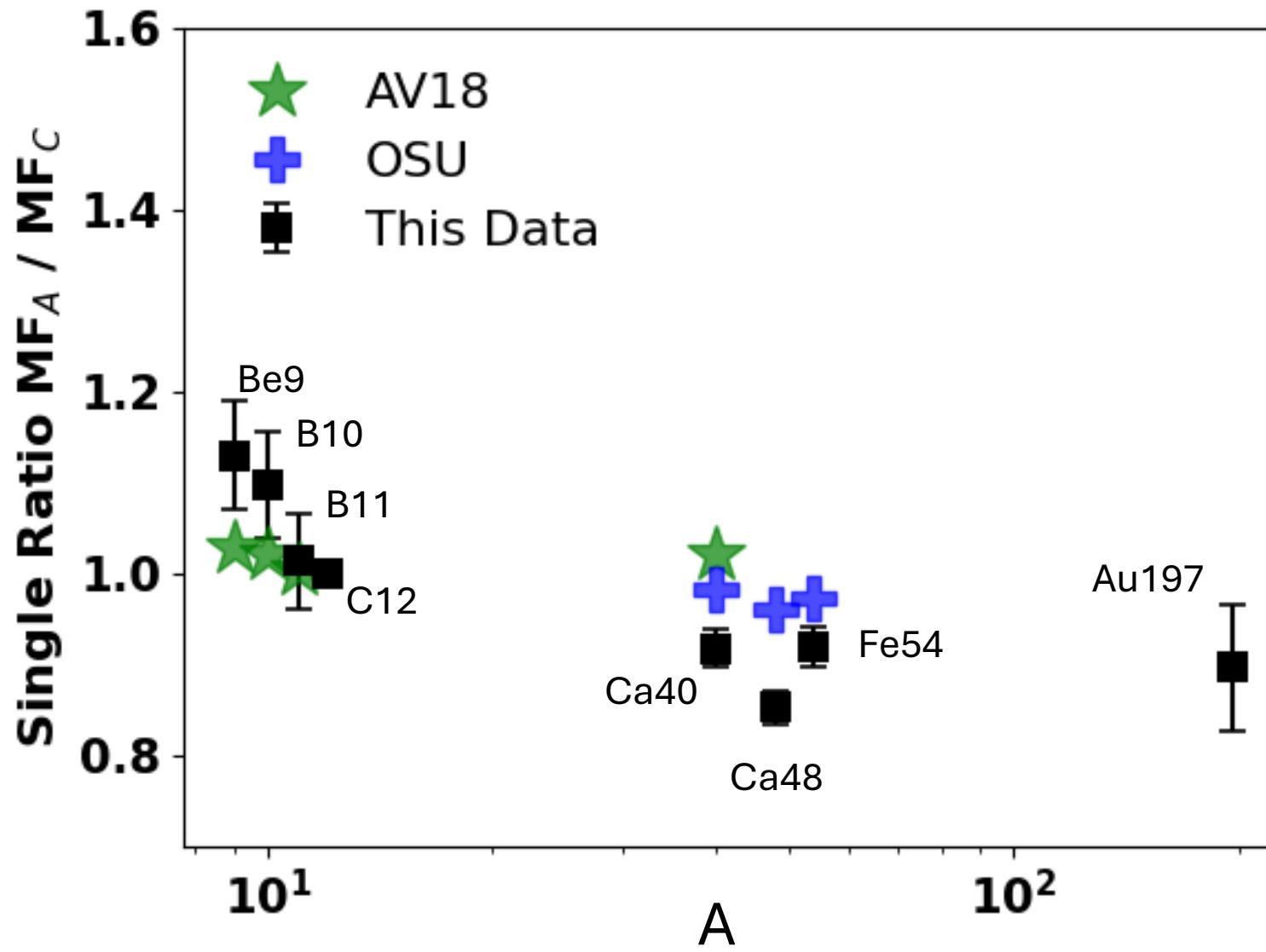
Mf $^{48}\text{Ca}$ Data			
Run	H (mg/cm <sup>2</sup> )	Carbon (mg/cm <sup>2</sup> )	Carbon (%)
16978	6.4	38.4	3.65
16979	5.2	31.2	2.97
17093	1	6	0.57
17094	0.9	5.2	0.49
17096	0.9	5.2	0.49

# <sup>48</sup>Ca

- A ~3% drop corresponds to the prediction of having 1 C per 2 H



# MF Single Ratio to C



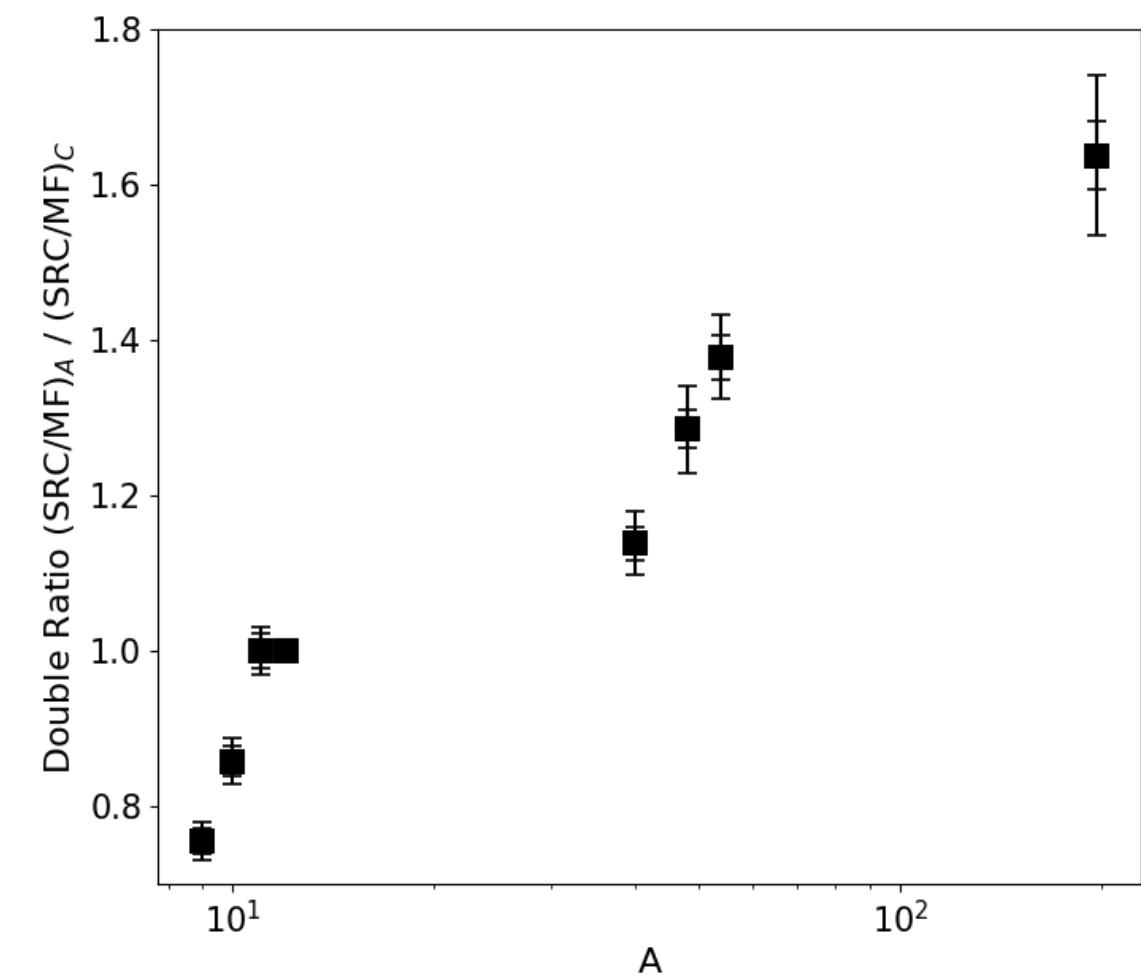
- MF Single Ratio decreases with  $A$
- Models are flat

[R.J.Furnstahl et al. arXiv:2402.00634v2 \(OSU\)](#)

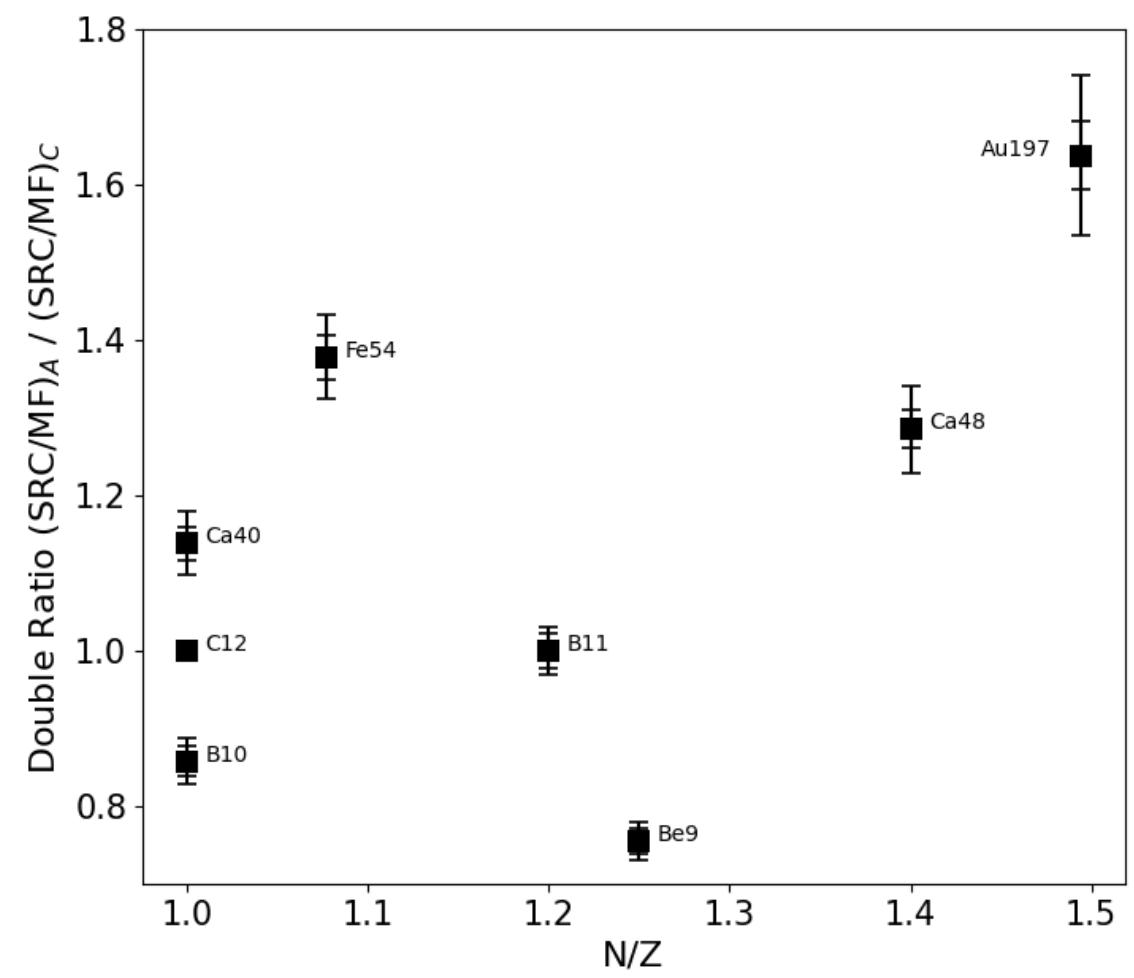
[Wiringa et al, Phys.Rev.C89 \(AV18\)](#)

Pairing depends on A (not N/Z)

Double Ratio increases with A



Per Proton Double Ratio to C



# Calculating Electron Cross Section

- $N_{events \text{ into solid angle } \Delta\Omega} = Data \text{ Counts} * SIMC \text{ Ratio}$
- $N_{incident} = \frac{Q(C)}{1.602*10^{-19}(C)}$
- $nx = \rho_{H2} * Target \text{ Length} * N_A$ 
  - Target Length modified by z-Target cut
- Electron solid angle modified by hxptar and hyptar cuts

Central Kinematics

---

H(e, e'p) Elastics for  
Beam Energy (Eb) = 10.549 GeV  
e- angle (th\_e) = 8.300 deg

---

e- momentum (kf) = 9.438 GeV/c  
proton angle (th\_p) = 48.384 deg  
proton momentum (Pf) = 1.822 GeV/c  
4-momentum transfer (Q2) = 2.086 (GeV/c)^2  
3-momentum transfer (|q|) = 1.822 GeV/c  
energy transfer = 1.111 GeV  
x-Bjorken = 1.000

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H(e, e') Cross Section @ Central Kinematics

H(e,e') Elastic Cross Section:  
Eb = 10549.0 MeV  
kf = 9438.0 MeV  
th\_e = 8.3 deg  
d\_sig/d\_omega\_e [ub/sr] (Bosted parametrization) = 2.449E-02  
d\_sig/d\_omega\_e [ub/sr] (Arrington parametrization) = 2.409E-02

- Use J. Arrington form-factor parametrization (more recent)

## Definition of cross section for scattering or reactions

Let  $N_{incident}$  = number of incident (beam) particles

$N_{events}$  = number of events (beam-target interactions)

$$n = \text{target atoms per unit volume} = \frac{\rho N_{Avogadro}}{A}$$

$A$  = mass number of target (assuming a single pure isotope)

$\rho$  = mass density of target (g/cm<sup>3</sup>)

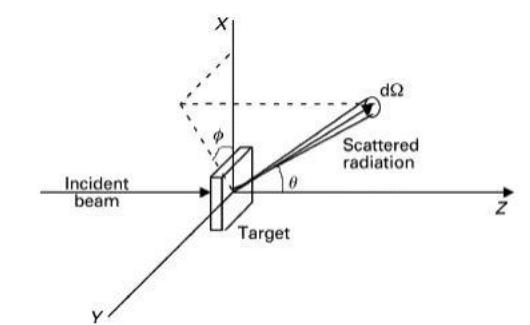
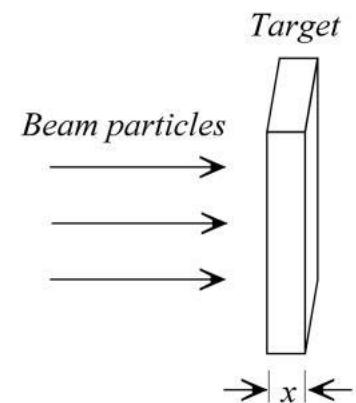
$x$  = thickness of target (cm)

$\rho x$  = areal density of target (g/cm<sup>2</sup>)

$$nx = \text{areal number density (atoms/cm}^2) = \frac{\rho x N_{Avogadro}}{A}$$

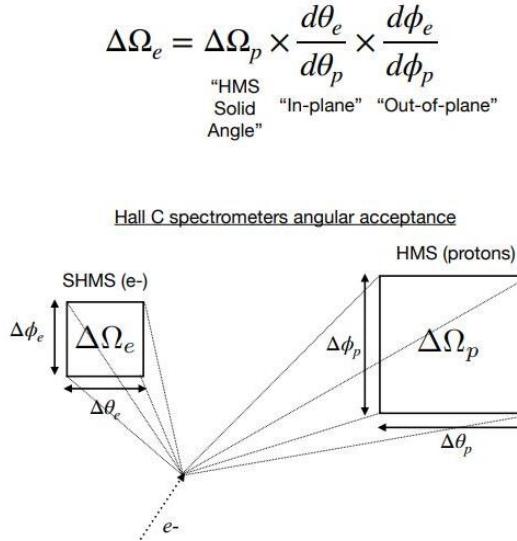
$$N_{\text{events into solid angle } \Delta\Omega_e} = N_{\text{incident}} nx \frac{d\sigma}{d\Omega_e} \Delta\Omega_e$$

Need to determine total # of H atoms per area that contaminate the Ca48 target



# Solid Angle

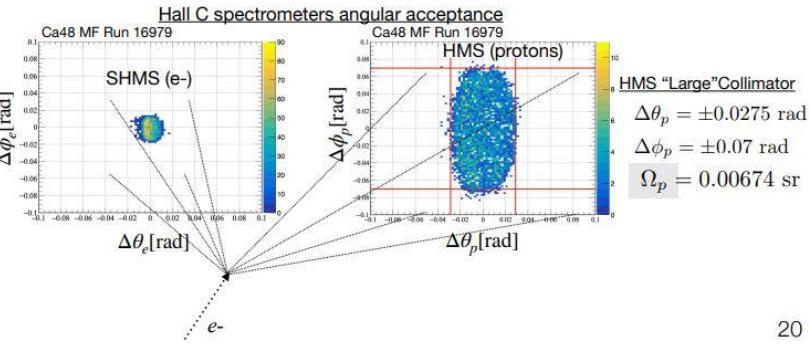
$$N_{\text{events into solid angle } \Delta\Omega_e} = N_{\text{incident}} n x \frac{d\sigma}{d\Omega_e} \Delta\Omega_e$$



$$N_{\text{events into solid angle } \Delta\Omega_e} = N_{\text{incident}} n x \frac{d\sigma}{d\Omega_e} \Delta\Omega_e$$

$$\Delta\Omega_e = \Delta\Omega_p \times \frac{d\theta_e}{d\theta_p} \times \frac{d\phi_e}{d\phi_p}$$

"HMS  
Solid  
Angle"



$$N_{\text{events into solid angle } \Delta\Omega_e} = N_{\text{incident}} n x \frac{d\sigma}{d\Omega_e} \Delta\Omega_e$$

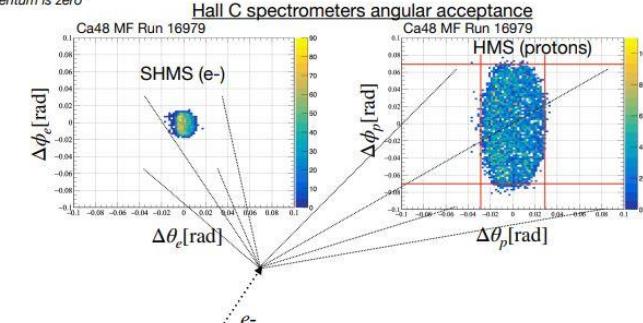
$$\Delta\Omega_e = \Delta\Omega_p \times \frac{d\theta_e}{d\theta_p} \times \frac{d\phi_e}{d\phi_p}$$

"Out-of-plane"

Momentum conservation (out-of-plane):

$$k_{i,\perp} = |k_f| \sin(\phi_e) + |p_f| \sin(\phi_p) = 0 \implies \frac{\delta\phi_e}{\delta\phi_p} \sim \frac{|p_f|}{|k_f|} = \frac{1.822 \text{ GeV/c}}{9.438 \text{ GeV/c}} \sim 0.193$$

" $\perp$  component of beam momentum is zero"



20

$$N_{\text{events into solid angle } \Delta\Omega_e} = N_{\text{incident}} n x \frac{d\sigma}{d\Omega_e} \Delta\Omega_e$$

numerical approach

H(e,e'p) Elastics for Beam Energy (E<sub>b</sub>) = 10.549 GeV e- angle (th<sub>e</sub>) = 8.200 deg e- momentum (kf) = 9.461 GeV/c proton angle (th<sub>p</sub>) = 48.738 deg

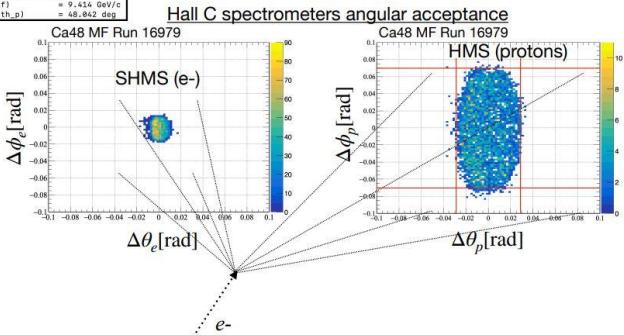
H(e,e'p) Elastics for Beam Energy (E<sub>b</sub>) = 10.549 GeV e- angle (th<sub>e</sub>) = 8.300 deg e- momentum (kf) = 9.438 GeV/c proton angle (th<sub>p</sub>) = 48.384 deg

H(e,e'p) Elastics for Beam Energy (E<sub>b</sub>) = 10.549 GeV e- angle (th<sub>e</sub>) = 8.400 deg e- momentum (kf) = 9.434 GeV/c proton angle (th<sub>p</sub>) = 48.642 deg

$$\Delta\Omega_e = \Delta\Omega_p \times \frac{d\theta_e}{d\theta_p} \times \frac{d\phi_e}{d\phi_p}$$

"In-plane"

"In-plane" (numerical approach):  
vary in-plane (e-) angle by +/- 0.1 deg  
and determine the variation in proton angle

$$\frac{\delta\theta_e}{\delta\theta_p} \sim 0.2907$$


$$N_{\text{events into solid angle } \Delta\Omega_e} = N_{\text{incident}} n x \frac{d\sigma}{d\Omega_e} \Delta\Omega_e$$

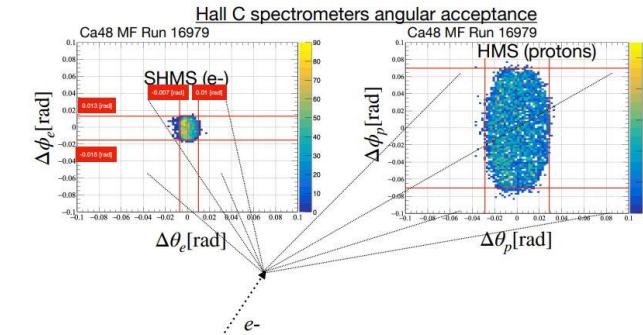
$$\Delta\Omega_e = \Delta\Omega_p \times \frac{d\theta_e}{d\theta_p} \times \frac{d\phi_e}{d\phi_p}$$

$$\Omega_p \sim 0.00674 \text{ sr}$$

$$\frac{\delta\theta_e}{\delta\theta_p} \sim 0.2907$$

$$\Delta\Omega_e \sim 0.000378 \text{ sr}$$

$$\frac{\delta\phi_e}{\delta\phi_p} \sim 0.193$$



22

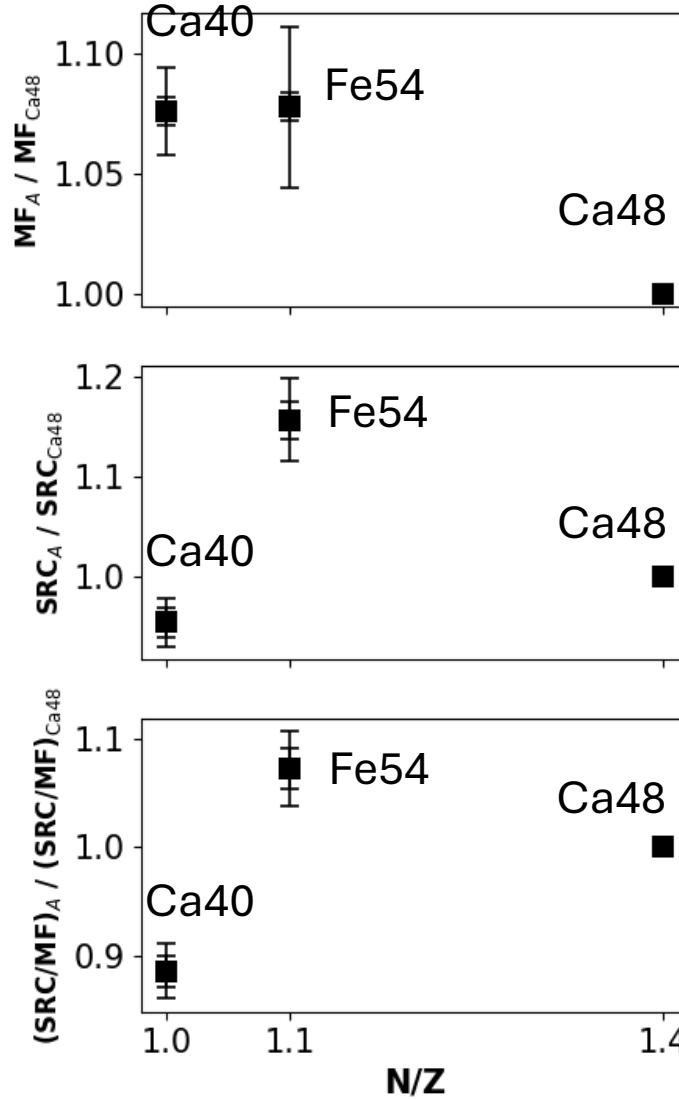
21

# Electron Cross Section Ratio (e,e') Data

- $$\frac{d\sigma}{d\Omega_e} = \frac{N_{events \text{ into solid angle}}}{N_{incident} * nx * d\Omega_e}$$

e,e'										
loose rad (e,e') cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
26293	410267.38	224189.82	1.83	19.284	1.20E+17	4.35E+23	3.78E-04	2.07E-02	0.859	
tight rad (e,e') cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
2996	53625.03	29303.30	1.83	19.284	1.20E+17	1.74E+23	1.08E-04	2.37E-02	0.983	

# CaFe Triplet Ratios



# Electron Cross Section Ratio (e,e'p) Data

- $$\frac{d\sigma}{d\Omega_e} = \frac{N_{events \text{ into solid angle}}}{N_{incident} * nx * d\Omega_e}$$

e,e'p										
loose rad (e,e'p) cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
205041	500254.81	273363.28	1.83	26.61	1.66E+17	4.35E+23	3.78E-04	1.83E-02	0.760	
tight rad (e,e'p) cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
30823	81242.86	44395.01	1.83	26.61	1.66E+17	1.74E+23	1.08E-04	2.60E-02	1.079	

# Electron Cross Section Ratio SIMC

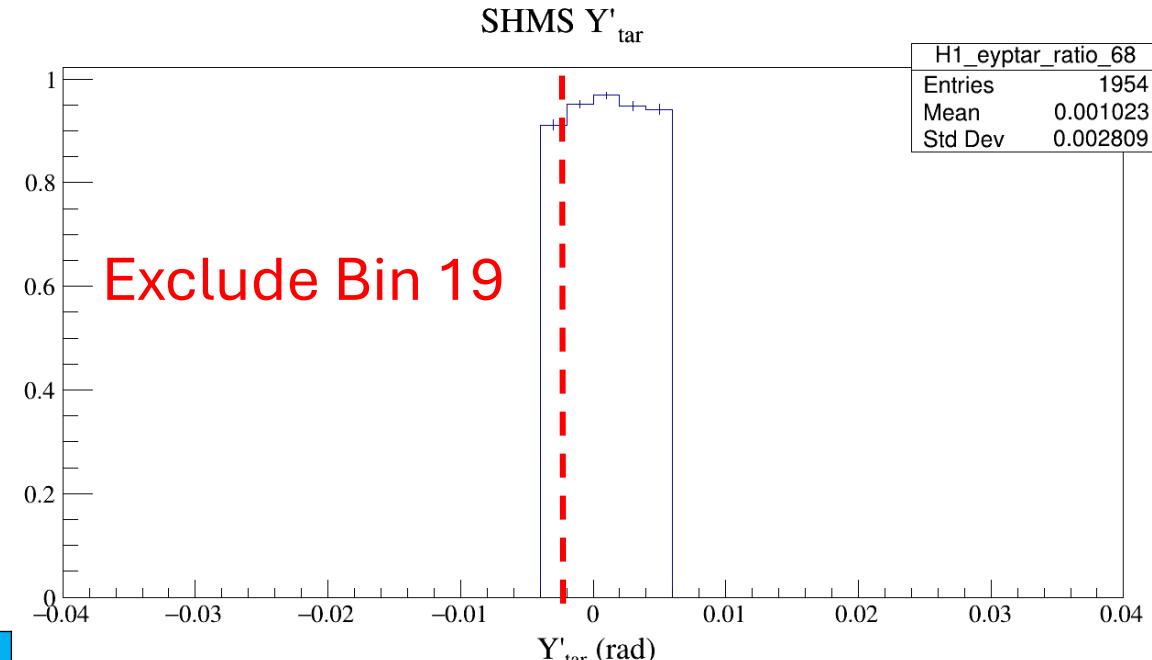
- $$\frac{d\sigma}{d\Omega_e} = \frac{N_{events \text{ into solid angle}}}{N_{incident} * nx * d\Omega_e}$$

Simulation										
loose rad (e,e'p) cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
1034393	442391.78	260091.86	1.70	26.61	1.66E+17	4.35E+23	3.78E-04	1.62E-02	0.672	
tight rad (e,e'p) cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
116625	74182.28	48370.63	1.53	26.61	1.66E+17	1.74E+23	1.08E-04	2.37E-02	0.986	
loose rad (e,e') cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
625496	429131.21	250013.25	1.72	19.284	1.20E+17	4.35E+23	3.78E-04	2.17E-02	0.899	
tight rad (e,e') cuts										
Raw Count	Norad Count	Rad Count	Rad Corr	q (mC)	Nicident	nx (atoms / cm^2)	ΔΩe (sr)	dσ/dΩe (μb/sr)	Norm	
70140	53874.13	31529.92	1.71	19.284	1.20E+17	1.74E+23	1.08E-04	2.38E-02	0.988	

# HMS Proton Efficiency

$$\sigma_{ratio}^{exact} = \sqrt{should \frac{did}{should} (1 - \frac{did}{should}) / should}$$

SHMS Y'tar							
Bin	Should Count	Did Count	$\sigma_{approx}$	$\sigma_{exact}$	Did/Should	Weight	Numerator
19	1012	919.8	0.009	0.009	0.91	12216.4	11102.9
20	960	907.7	0.008	0.007	0.95	18644.5	17629.2
21	873	845.5	0.006	0.006	0.97	28652.5	27751.1
22	713	680.0	0.008	0.008	0.95	16171.4	15423.8
23	669	628.9	0.009	0.009	0.94	11869.2	11157.5
Total	3215	3062.2	0.004	0.004			

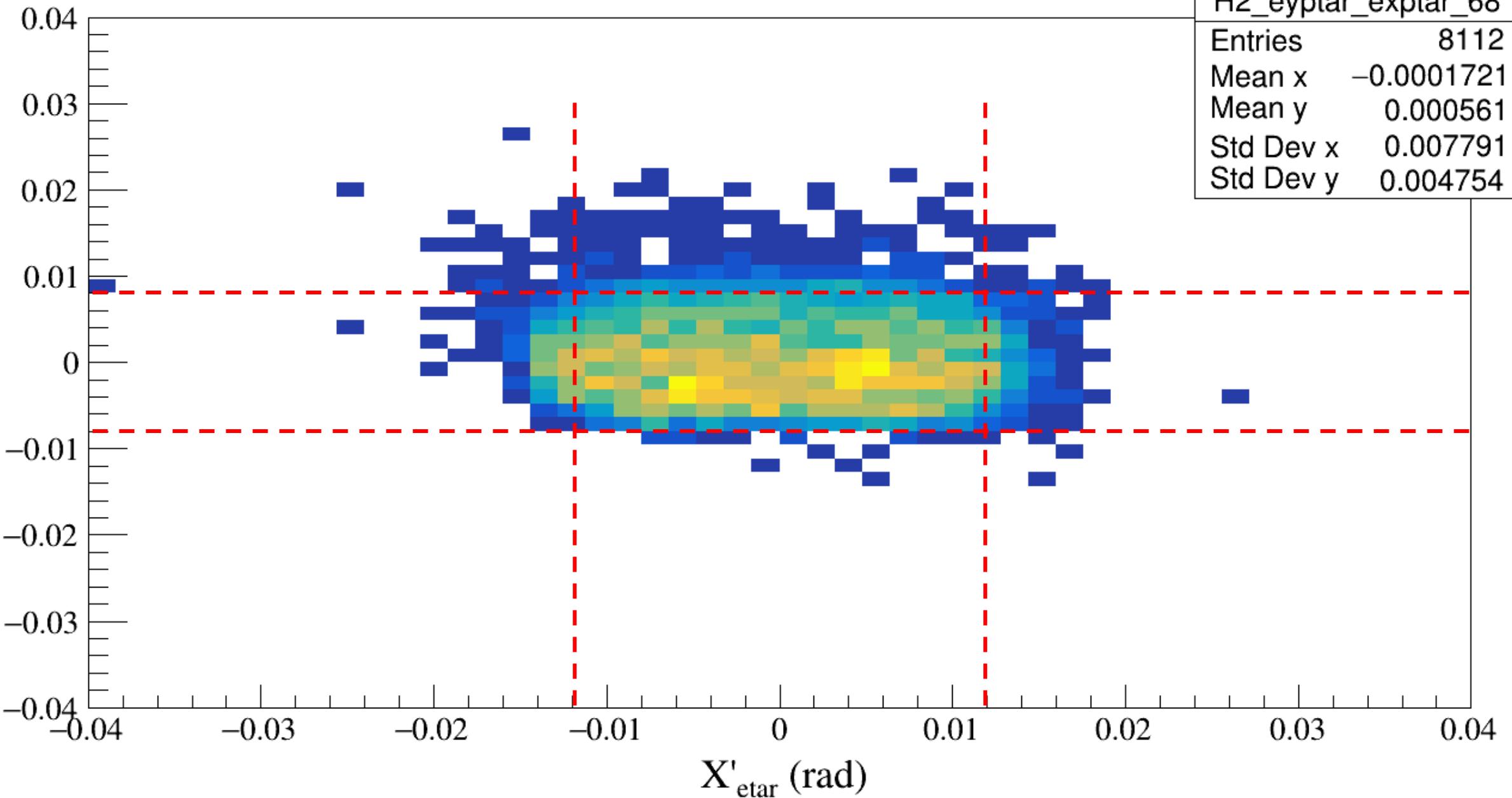


Result		
Unweighted Proton Transmission	Weighted Proton Transmission	Uncertainty
0.952	0.955	0.004

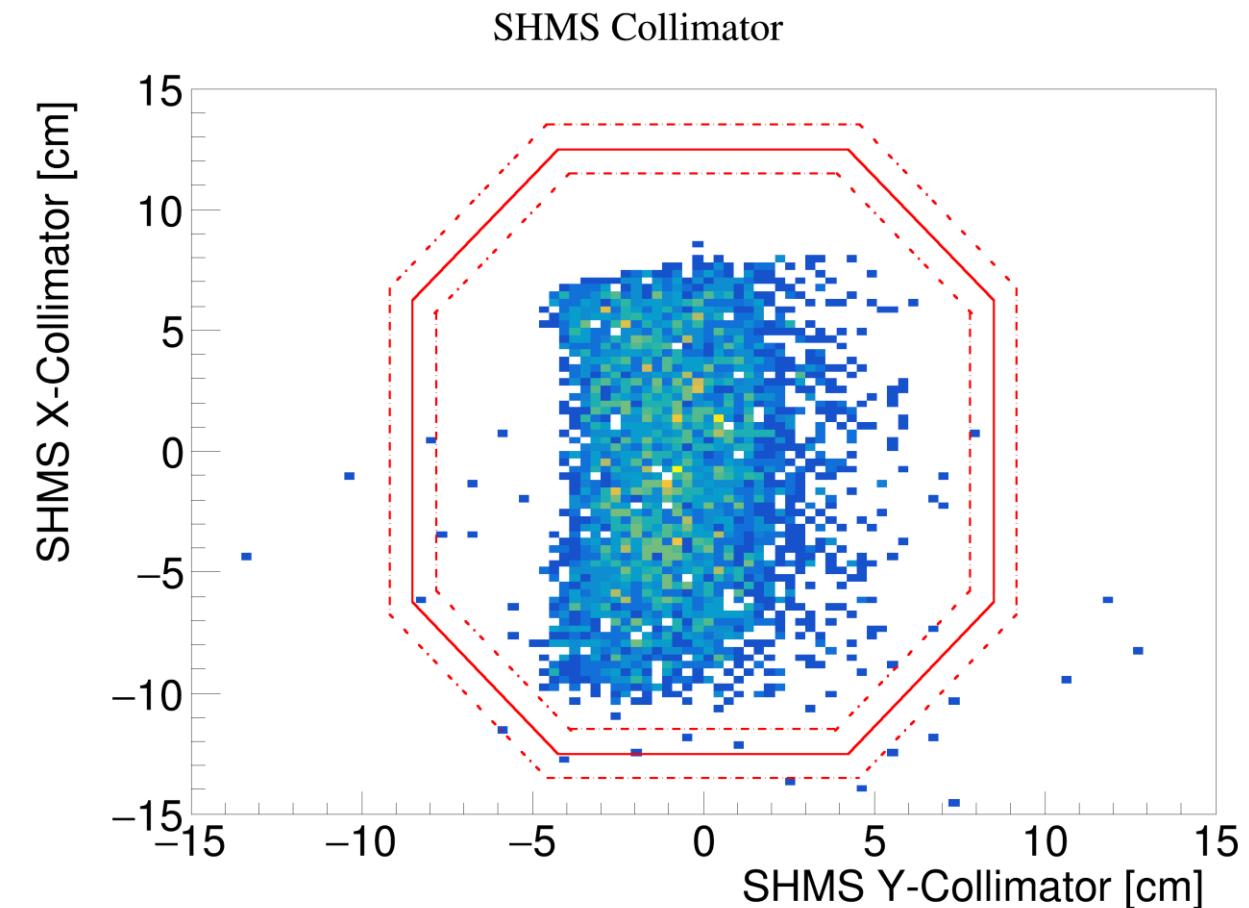
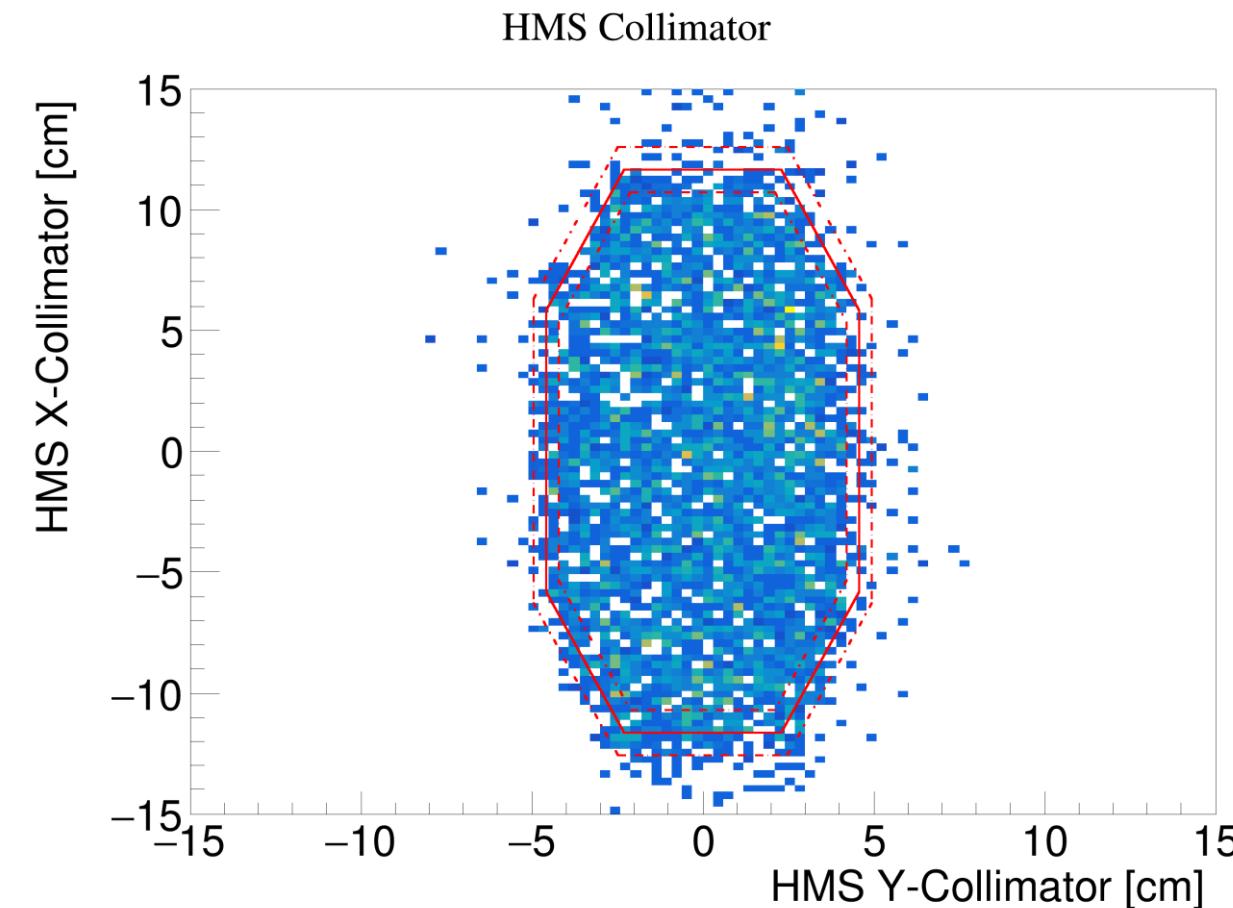
# SHMS $X'_{\text{tar}}$ vs SHMS $Y'_{\text{tar}}$

H2_eyptar_exptar_68	
Entries	8112
Mean x	-0.0001721
Mean y	0.000561
Std Dev x	0.007791
Std Dev y	0.004754

$Y'_{\text{tar}}$  (rad)

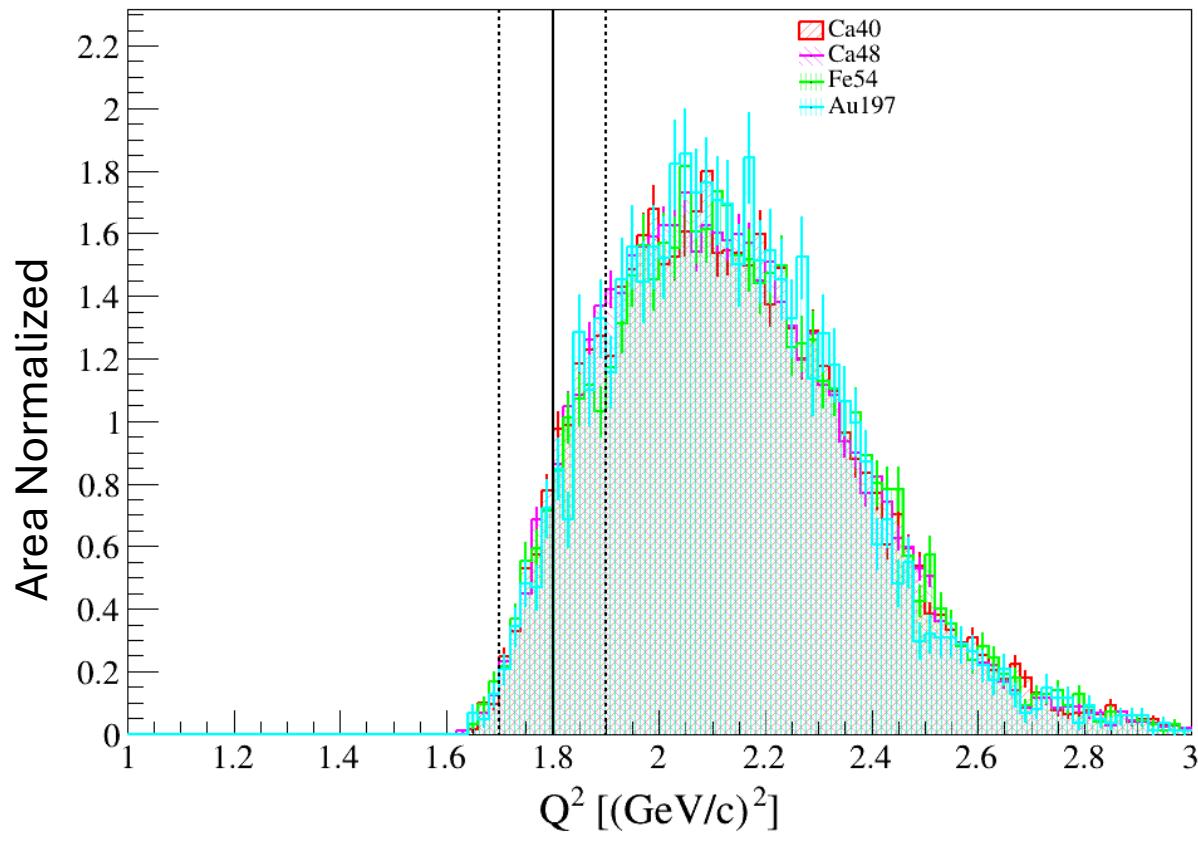


# SRC HMS & SHMS Collimator Cuts ( $\pm 2\sigma$ )

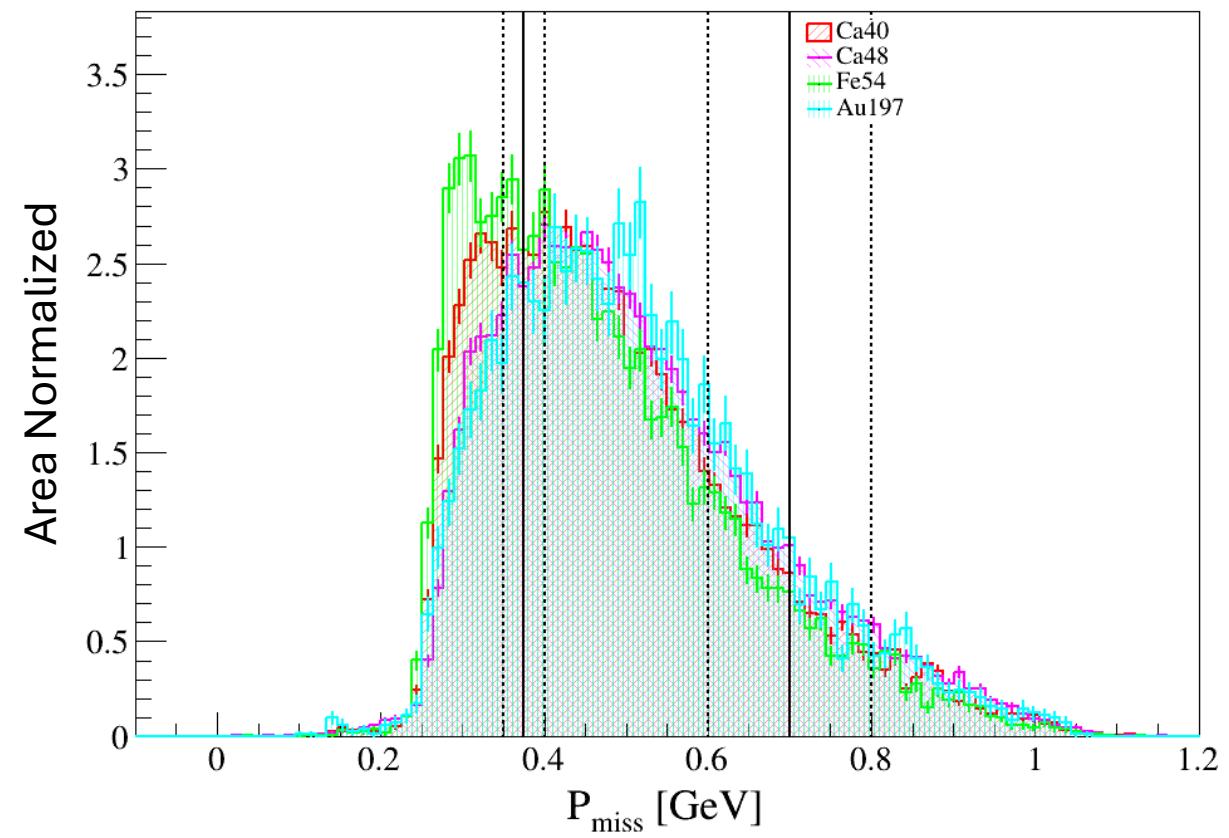


# SRC $Q^2$ & $P_m$ Cuts ( $\pm 2\sigma$ )

Heavy SRC 4-Momentum Transfer

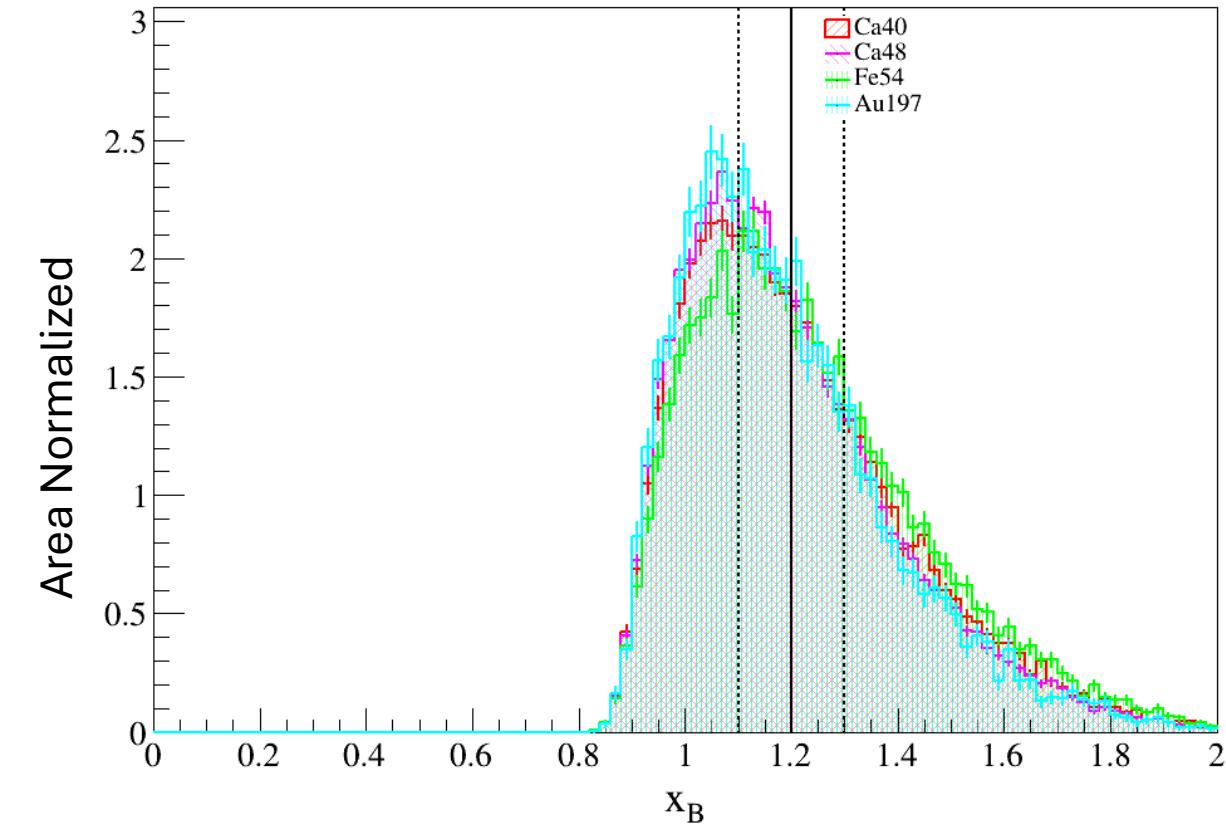


Heavy SRC Missing Momentum



# SRC $x_{bj}$ & $\theta_{rq}$ Cuts ( $\pm 2\sigma$ )

Heavy SRC x-Bjorken



Heavy SRC In-Plane (recoil) Angle

