



# Update on pT-SIDIS Experiment E12-09-017



Edward R. Kinney, University of Colorado at Boulder

On behalf of **P. Bosted** (William & Mary)

- Brief review of motivation
- Results of Parameter Fit
- To-Do List

**E12-09-017:**  
**Precision  $(e,e'\pi^\pm),(e,e'K^\pm)$  cross sections at low  $P_{h\perp}$**

- Precision measurements to test the assumptions in factorization of SIDIS
- Explore assumptions of favored/disfavored fragmentation of different flavor quarks
- Look for target mass effects
- Higher twist effects
- Complementary to Hall B SIDIS measurements

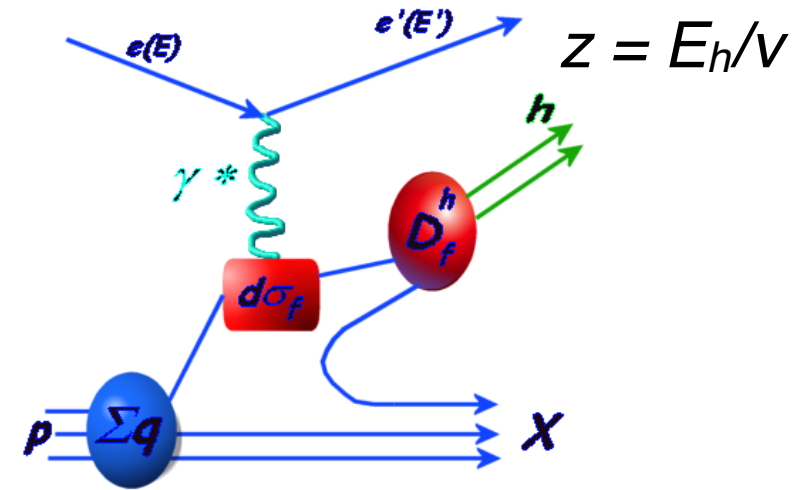
# Do parton distributions and fragmentation functions factorize at Jefferson Lab energies?

## Flavor Decomposition of SIDIS

$$\frac{1}{\sigma_{(e,e')}} \frac{d\sigma}{dz} (ep \rightarrow hX) = \frac{\sum_q e_q^2 f_q(x) D_q^h(z)}{\sum_q e_q^2(x) f_q(x)}$$

$f_q(x)$  : parton distribution function

$D_q^h(z)$  : fragmentation function



$$M_x^2 = W'^2 \sim M^2 + Q^2 (1/x - 1)(1 - z)$$

- Leading-Order (LO) QCD
- after integration over  $p_{h\perp}$  and  $\phi_h$
- NLO: gluon radiation mixes  $x$  and  $z$  dependences
- Target-Mass corrections at large  $z$
- $\ln(1-z)$  corrections at large  $z$

With  $p_T$  and  $k_T$  dependences, some kind of convolution is necessary to obtain final  $P_{h\perp}$

## Kinematic Plan at 11 GeV

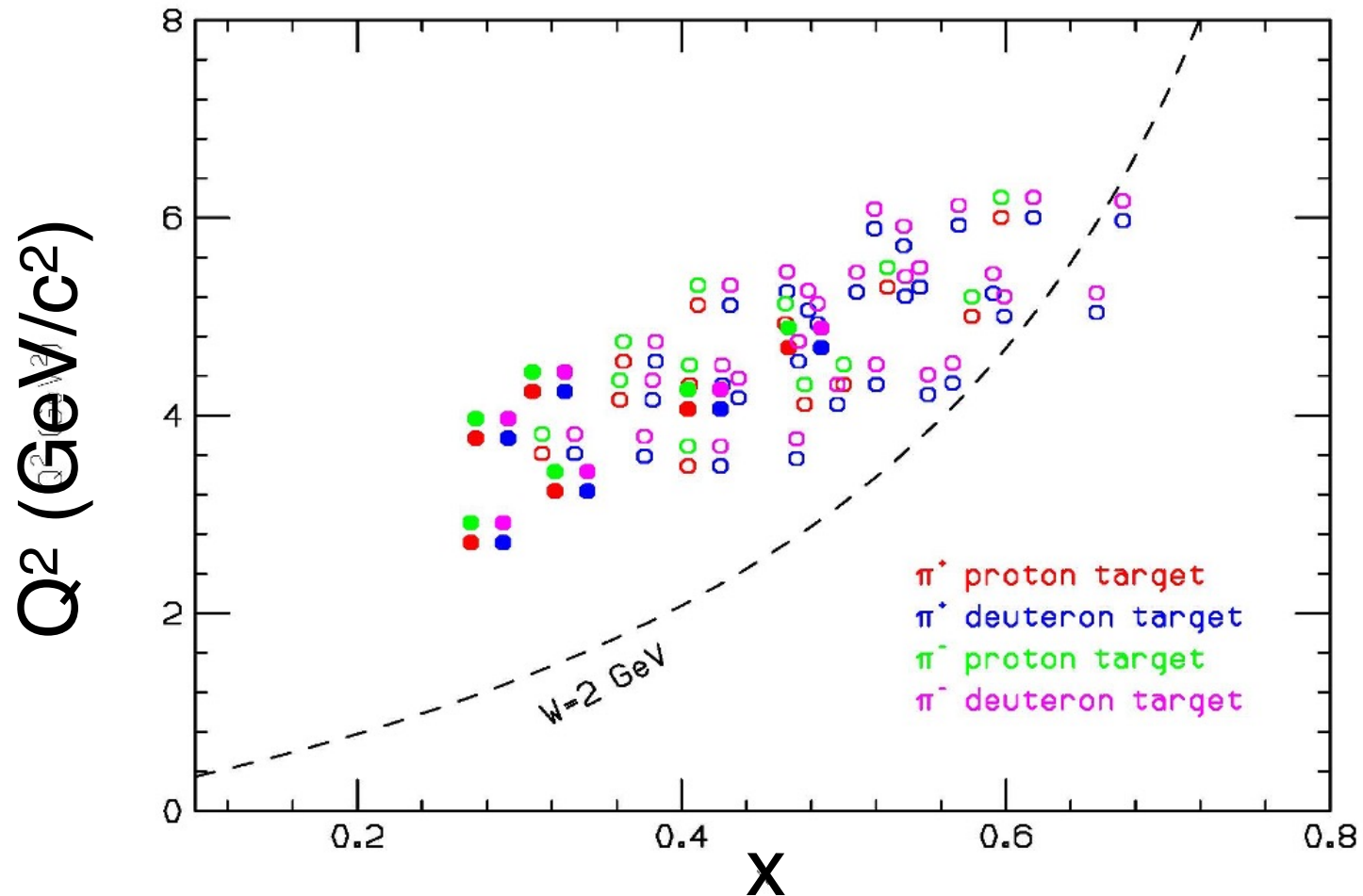
- $W^2 = 5.08 \text{ GeV}^2$  and larger (up to  $11.38 \text{ GeV}^2$ )
- Used SHMS angle down to 6.6 degrees (for  $\pi$  detection)  
HMS angle down to 13.5 degrees ( $e^-$  detection)  
separation HMS-SHMS  $> 17.5$  degrees
- $M_X^2 = M_p^2 + Q^2(1/x - 1)(1 - z) > 2.9 \text{ GeV}^2$  (up to  $7.8 \text{ GeV}^2$ )
- Improved coverage in all kinematic variables, especially  $\phi$  and  $p_T$
- Choice to keep  $Q^2/x$  fixed  $q_y \sim \text{constant}$  (exception are data scanning  $Q^2$  at fixed  $x$ )
- All kinematics both for  $\pi^+$  (and  $K^+$ ) and  $\pi^-$  (and  $K^-$ ), both for LH2 and LD2 (and Aluminum dummy)

## Status of Pion SIDIS

- Table with 21,000 cross section and multiplicity results for charged pion SIDIS pretty much finalized.
- The table includes both the subtractive and multiplicative radiative corrections used.
- The table includes one estimate of diffractive rho(DVM) contributions, which can be applied to the results by the user if desired.
- The results ideally will be incorporated into large global analyses by groups such as JAM, updated with new results from CLAS12, COMPASS, NPS, and R\_SIDIS as they become available.
- Meanwhile, have begun interpretation using our data only.

## Kinematic Coverage in (x, Q<sup>2</sup>)

- Solid circles are from pt-SIDIS, open circles CSV SIDIS
- Each circle represents 10,000 to 1,000,000 events
- Dominated by valance quark distributions



# SIDIS Differential Cross Section

Measurement of 6-fold differential cross section with unpolarized target has five structure functions (formalism from Bacchetta *et al.*, JHEP 0702, 93 (2007).)

$$\frac{d\sigma}{dx dy d\psi dz d\phi_h dP_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos\phi_h F_{UU}^{\cos\phi_h} + \epsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} + \lambda_e \sqrt{2\epsilon(1-\epsilon)} \sin\phi_h F_{LU}^{\sin\phi_h} \right\}$$

Virtual Photon Polarization:  $\epsilon$

Electron helicity:  $\lambda_e$

Hadron azimuthal angle:  $\phi_h$

Structure functions depend on  $x$ ,  $Q^2$ ,  $p_T$ !

# SIDIS cross section model with Transverse Momentum-dependent Parton and Fragmentation Distributions (TMDs)

$f_q(x, \mathbf{k}_\perp)$  : *parton distribution function as function of intrinsic parton  $k_T$*

$D_q^h(z, \mathbf{p}_\perp)$  : *fragmentation function as a function of fragmentation  $p_T$*

Cross section for SIDIS hadron of fractional energy  $z_h$  and transverse momentum  $P_T$

$$\frac{d^5 \sigma^{\ell p \rightarrow \ell h X}}{dx_B dQ^2 dz_h d^2 \mathbf{P}_T} = \sum_q e_q^2 \int d^2 \mathbf{k}_\perp f_q(x, \mathbf{k}_\perp) \frac{2\pi\alpha^2}{x_B^2 s^2} \frac{\hat{s}^2 + \hat{u}^2}{Q^4} \\ \times D_q^h(z, \mathbf{p}_\perp) \frac{z}{z_h} \frac{x_B}{x} \left( 1 + \frac{x_B^2 k_\perp^2}{x^2 Q^2} \right)^{-1}$$

*from Anselmino et al. (hep-ph/0412316v1)*



## Multiplicity Parameterization

Now perform  $k_{\perp}$  integration and keep terms order  $O(k_{\perp}/Q)$  on previous cross section expression to get

$$\frac{d^5 \sigma^{\ell p \rightarrow \ell h X}}{dx_B dQ^2 dz_h d^2 \mathbf{P}_T} \simeq \sum_q \frac{2\pi \alpha^2 e_q^2}{Q^4} f_q(x_B) D_q^h(z_h) \left[ (1 + (1 - y)^2) - 4 \frac{(2 - y) \sqrt{1 - y} \langle k_{\perp}^2 \rangle z_h P_T}{\langle P_T^2 \rangle Q} \cos \phi_h \right] \frac{1}{\pi \langle P_T^2 \rangle} e^{-P_T^2 / \langle P_T^2 \rangle},$$

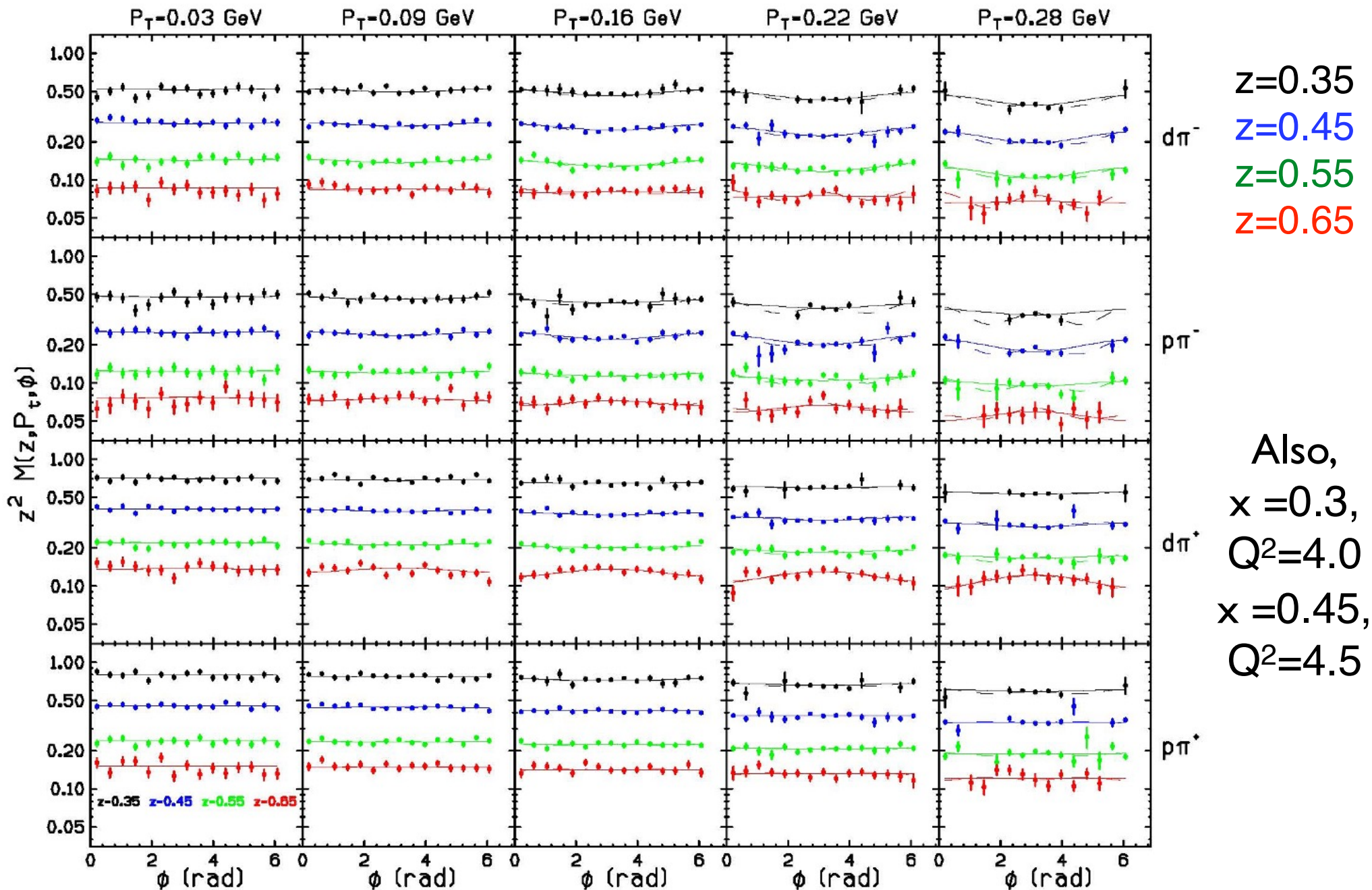
$$\text{where } \langle P_T^2 \rangle = \langle p_{\perp}^2 \rangle + z^2 \langle k_{\perp}^2 \rangle$$

We divide by DIS cross section and fit the multiplicities with:

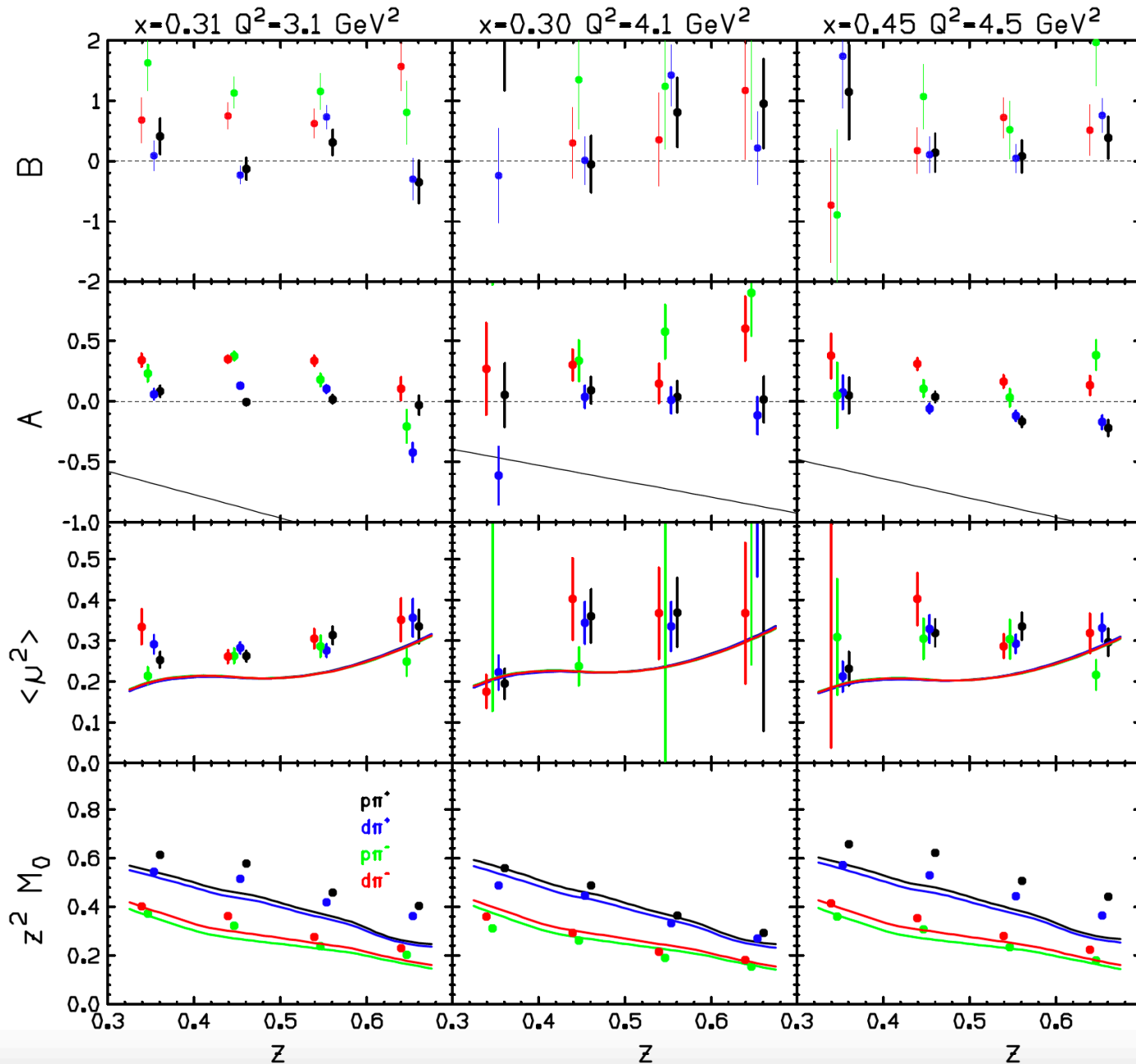
$$M(x, Q^2, z, P_{hT}, \phi) = \frac{d\sigma_{ee'\pi X}}{d\sigma_{ee'X}} = \frac{M_0}{2\pi \langle \mu^2 \rangle} e^{-P_{hT}^2 / \langle \mu^2 \rangle} (1 + A \cos \phi + B \cos 2\phi)$$

$$M_0, \langle \mu^2 \rangle, A, B \text{ are fit parameters}$$

# Azimuthal Dependence at $x=0.3$ , $Q^2 = 3.0 \text{ GeV}/c^2$



# Four-parameter Fit Results (1st 5 $p_T$ bins)



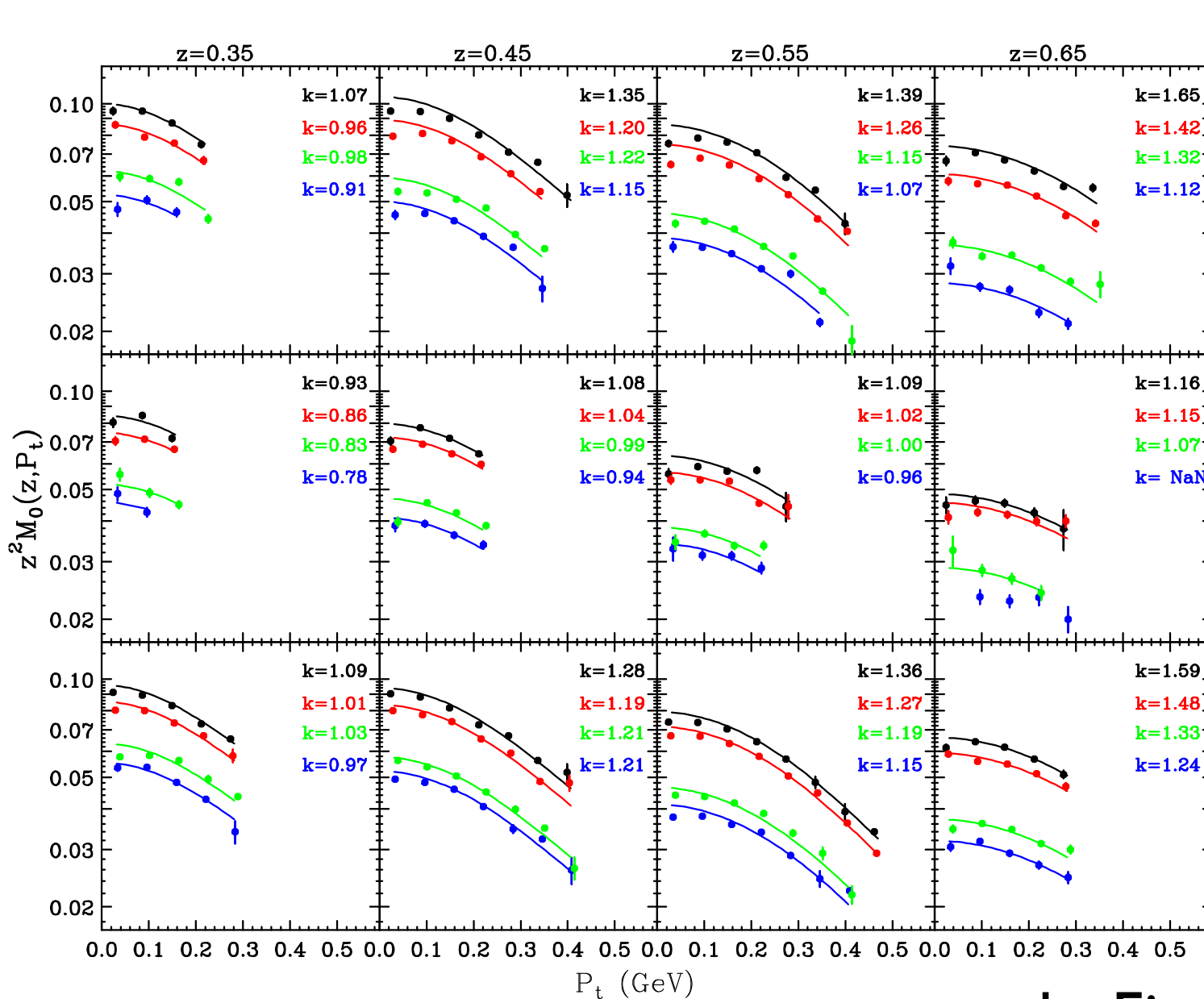
$p\pi^+$   $d\pi^+$   $p\pi^-$   $d\pi^-$

$A, B \approx 0$  for  $\pi^+$

$A, B > 0$  for  $\pi^-$

Qualitative agreement  
with MAP (colored solid  
curves)

# Multiplicities



$p\pi^+$   $d\pi^+$   $p\pi^-$   $d\pi^-$

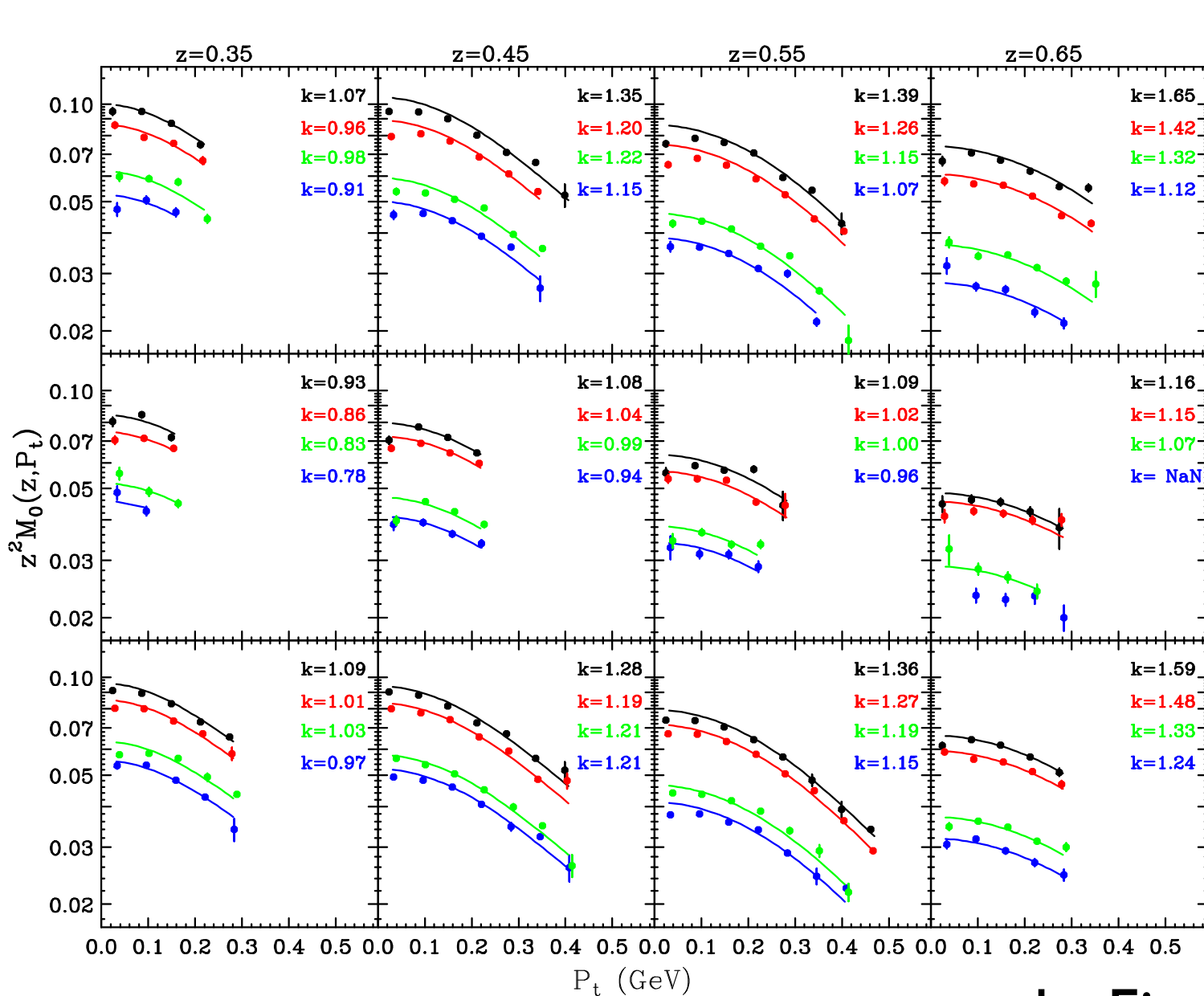
I  $x=0.45, Q_2=4.5$

II  $x=0.3, Q_2=4.0$

III  $x=0.3, Q_2=3.0$

$k = \text{Fit of MAPS to data}$

# Multiplicities



$p\pi^+$   $d\pi^+$   $p\pi^-$   $d\pi^-$

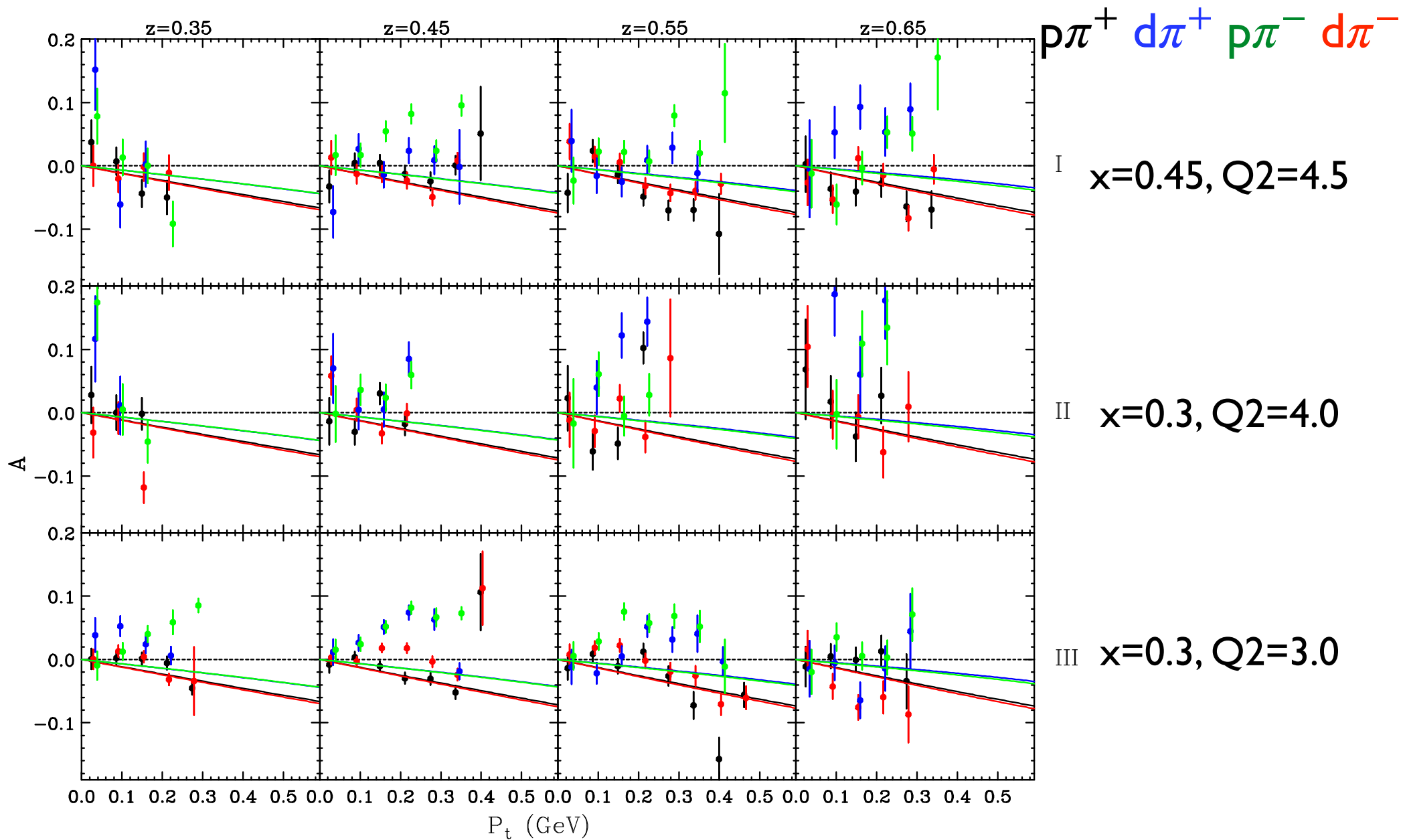
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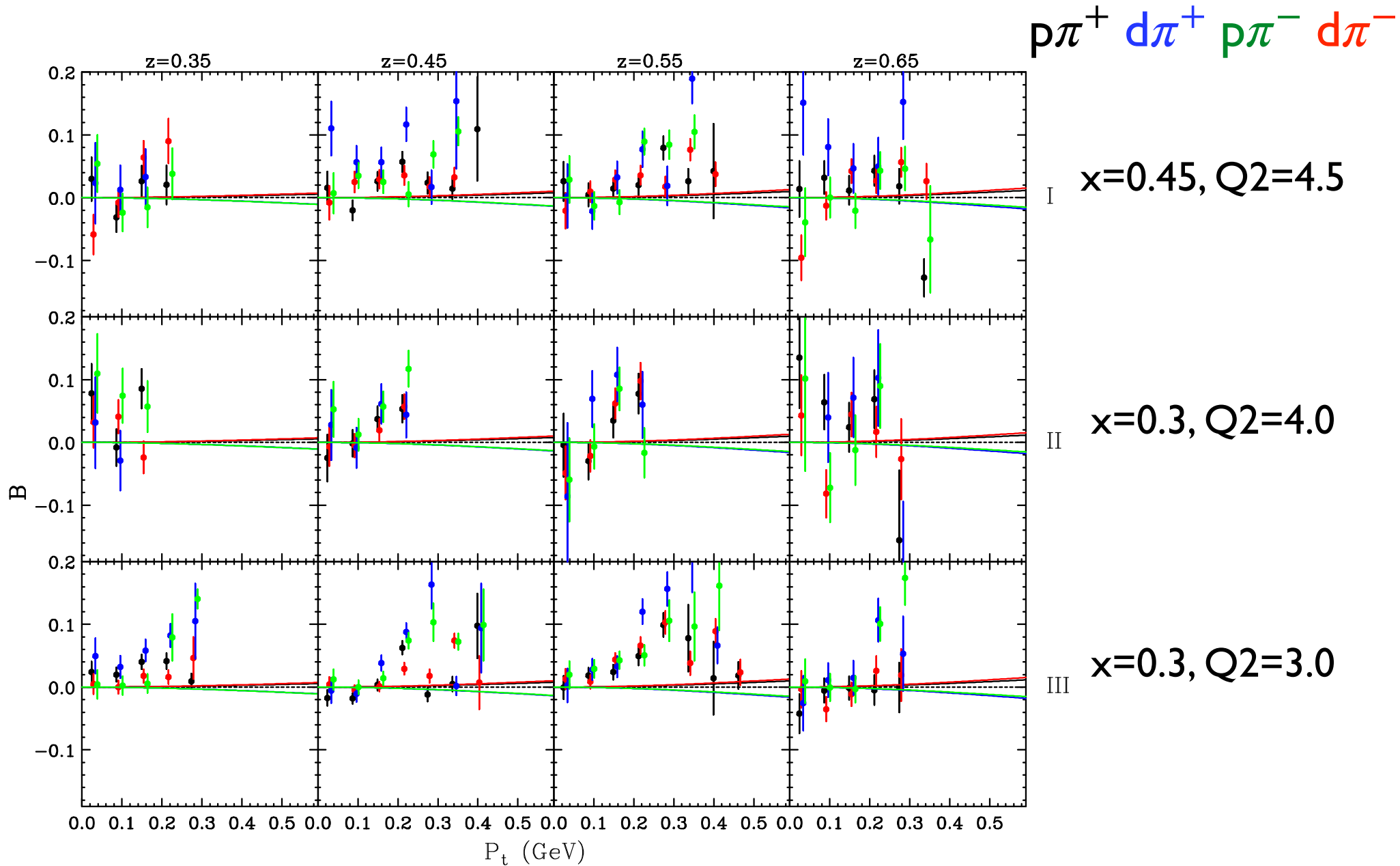
$k = \text{Fit of MAPS to data}$

# Phi Coefficient (A)

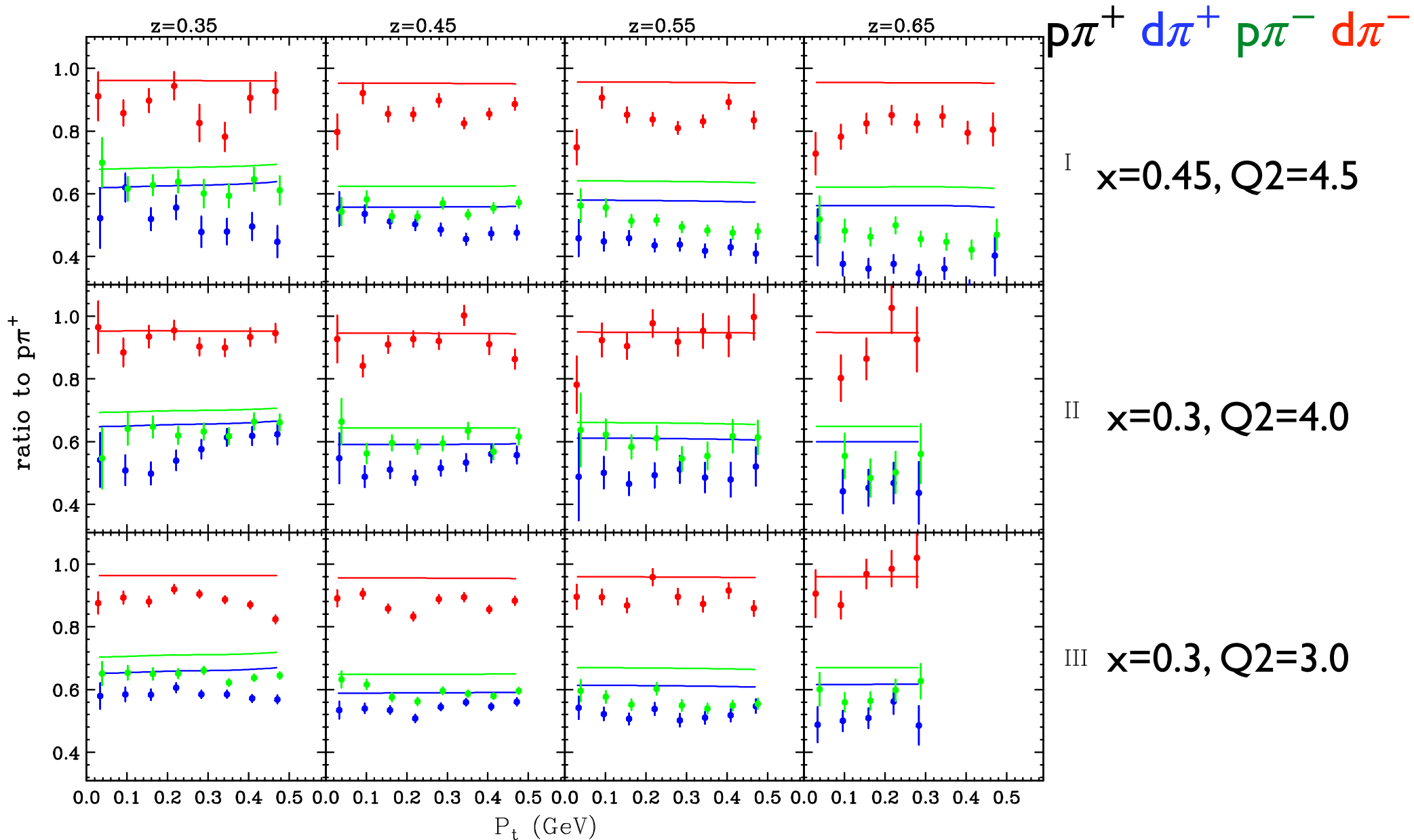




# 2\*Phi Coefficient (B)



# Ratio of Multiplicities





## Plans for future

- Develop pion fits further, understand systematics
- Understand 5% normalization difference between inclusive  $d$  cross section and world data parameterizations
- Determine kaon cross sections
- Manuscript in preparation for Phys Rev D containing all data with fits plus beam spin asymmetries. Goal to submit before start of R-SIDIS