

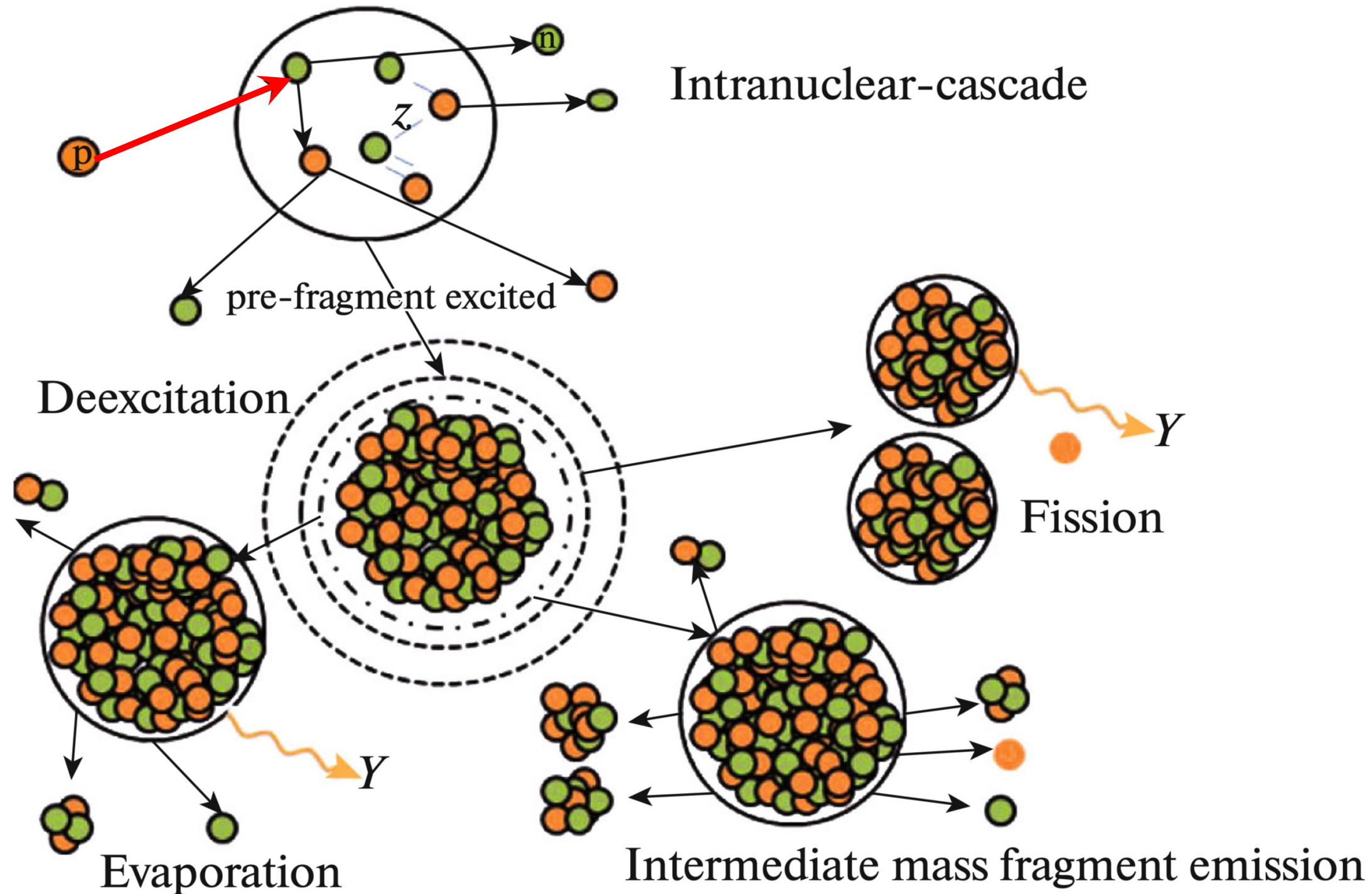
Nuclear Fragmentation at the Future Electron-Ion Collider

C.A. Bertulani

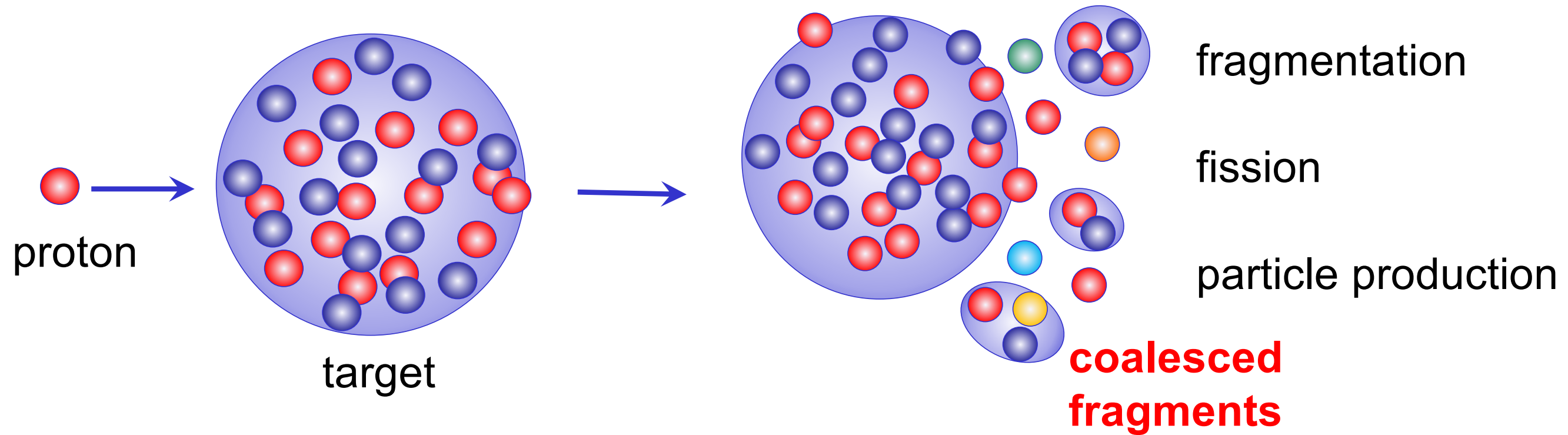


EAST TEXAS A&M
— UNIVERSITY —

Fragment production: Cascade & coalescence & evaporation



Transport equations + coalescence

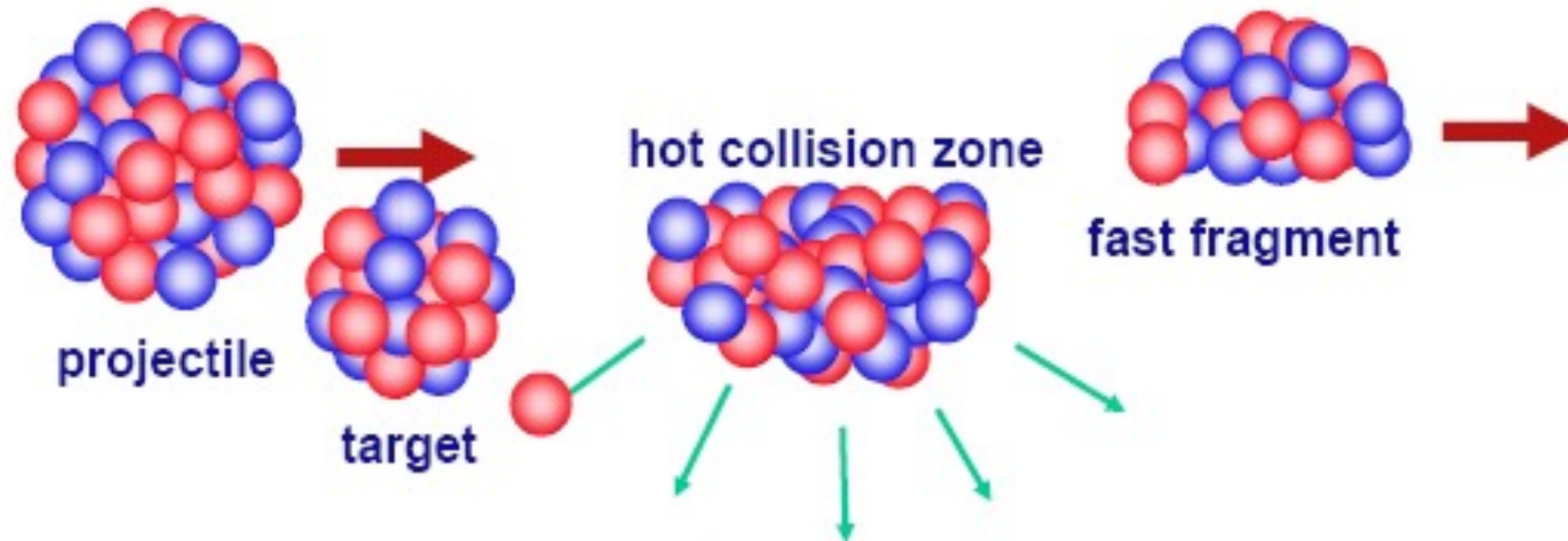


$$C_A = \frac{2J_A + 1}{2^A} \frac{1}{\sqrt{A} m_T^{A-1}} \left(\frac{2\pi}{R^2 + \left(\frac{r_A}{2}\right)^2} \right)^{\frac{3}{2}(A-1)}$$

Particles produced coalesce into nuclei if they are close in space and momentum.

R = source size, r_A = nuclear size
 m_T = transverse mass of coalesc. part.

Glauber models + coalescence

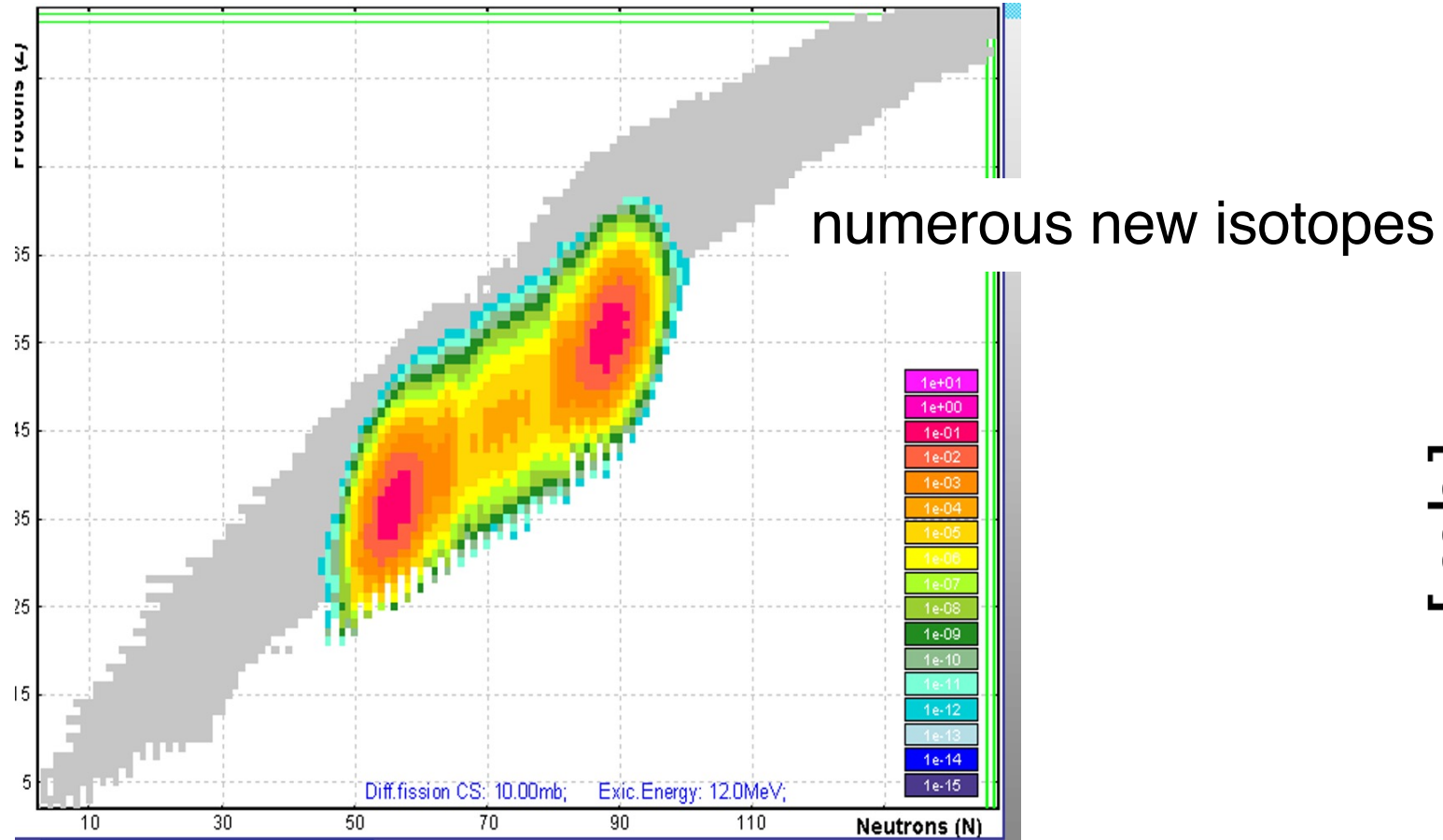


Glauber →
fragment (N_F Z_F)
+
evaporation

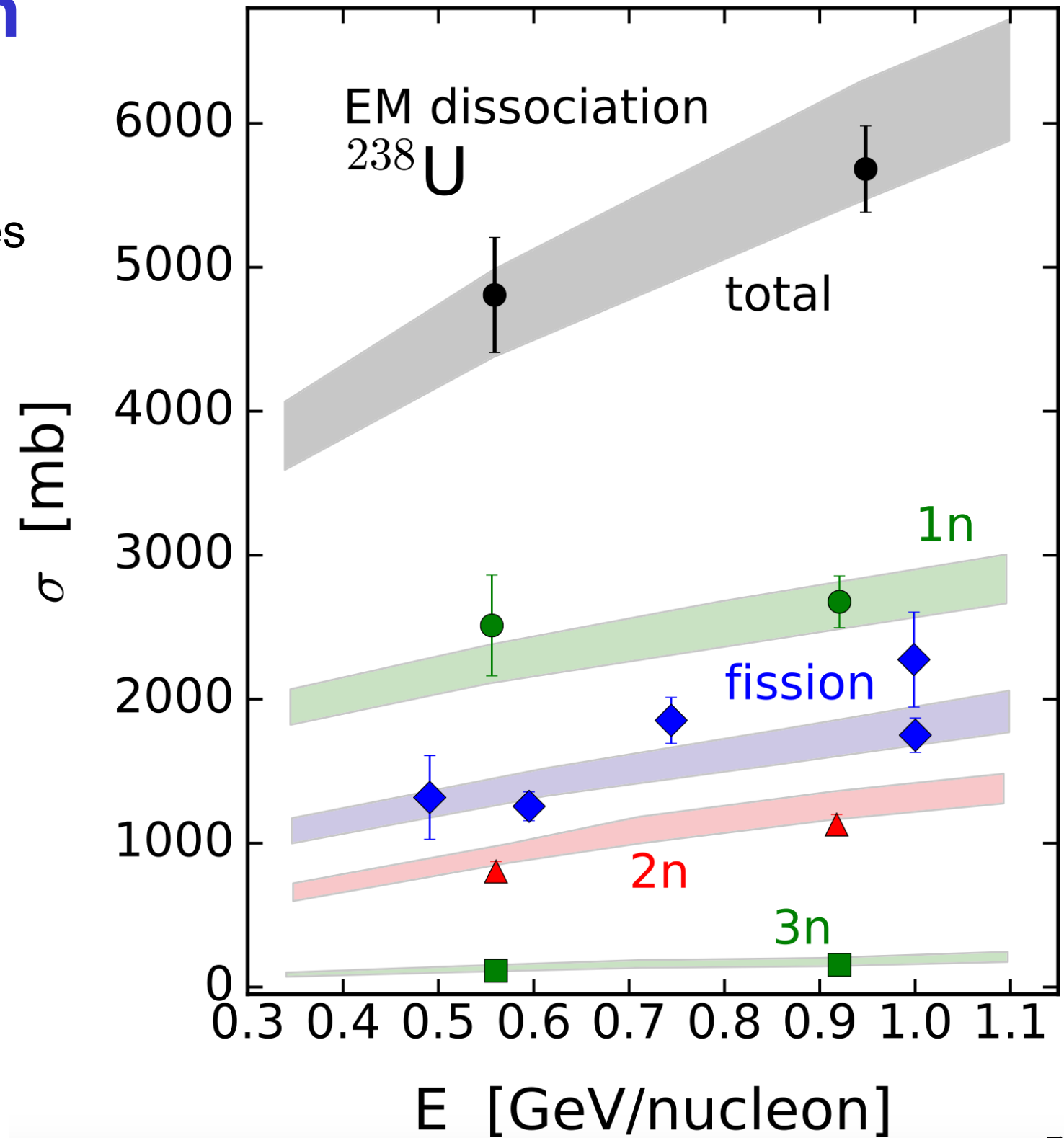
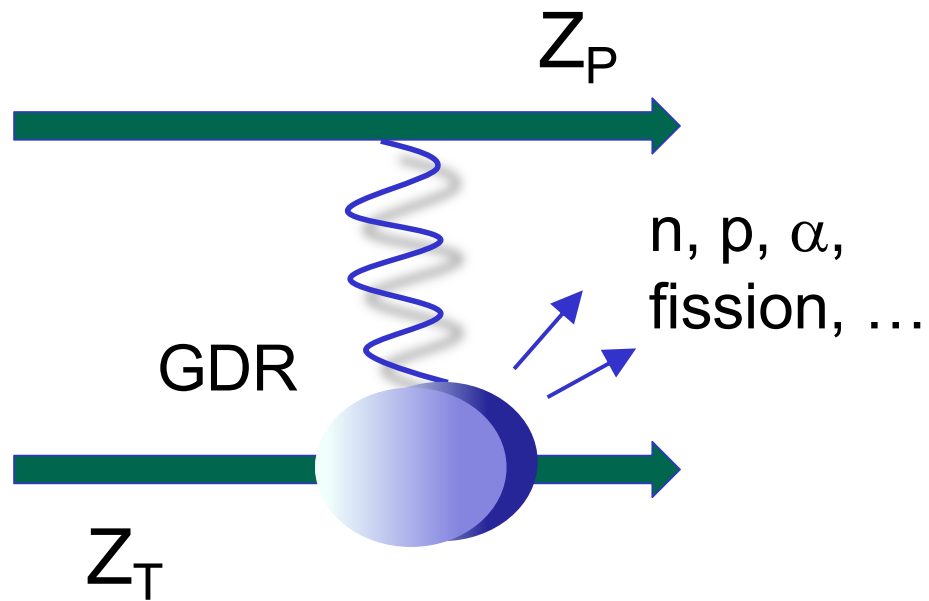
$$\sigma(N_F, Z_F) = \binom{N_P}{N_F} \binom{Z_P}{Z_F} \int d^2b [P_p(\mathbf{b})]^{Z_F} [P_n(\mathbf{b})]^{N_F} \times [1 - P_n(\mathbf{b})]^{N_P - N_F} [1 - P_p(\mathbf{b})]^{Z_P - Z_F}$$

$$P_p(\mathbf{b}) = \int dz d^2s \rho_p^P(\mathbf{s}, z) \exp \left[-\sigma_{pp} Z_T \int d^2s \rho_p^T(\mathbf{b} - \mathbf{s}, z) - \sigma_{pn} N_T \int d^2s \rho_n^T(\mathbf{b} - \mathbf{s}, z) \right]$$

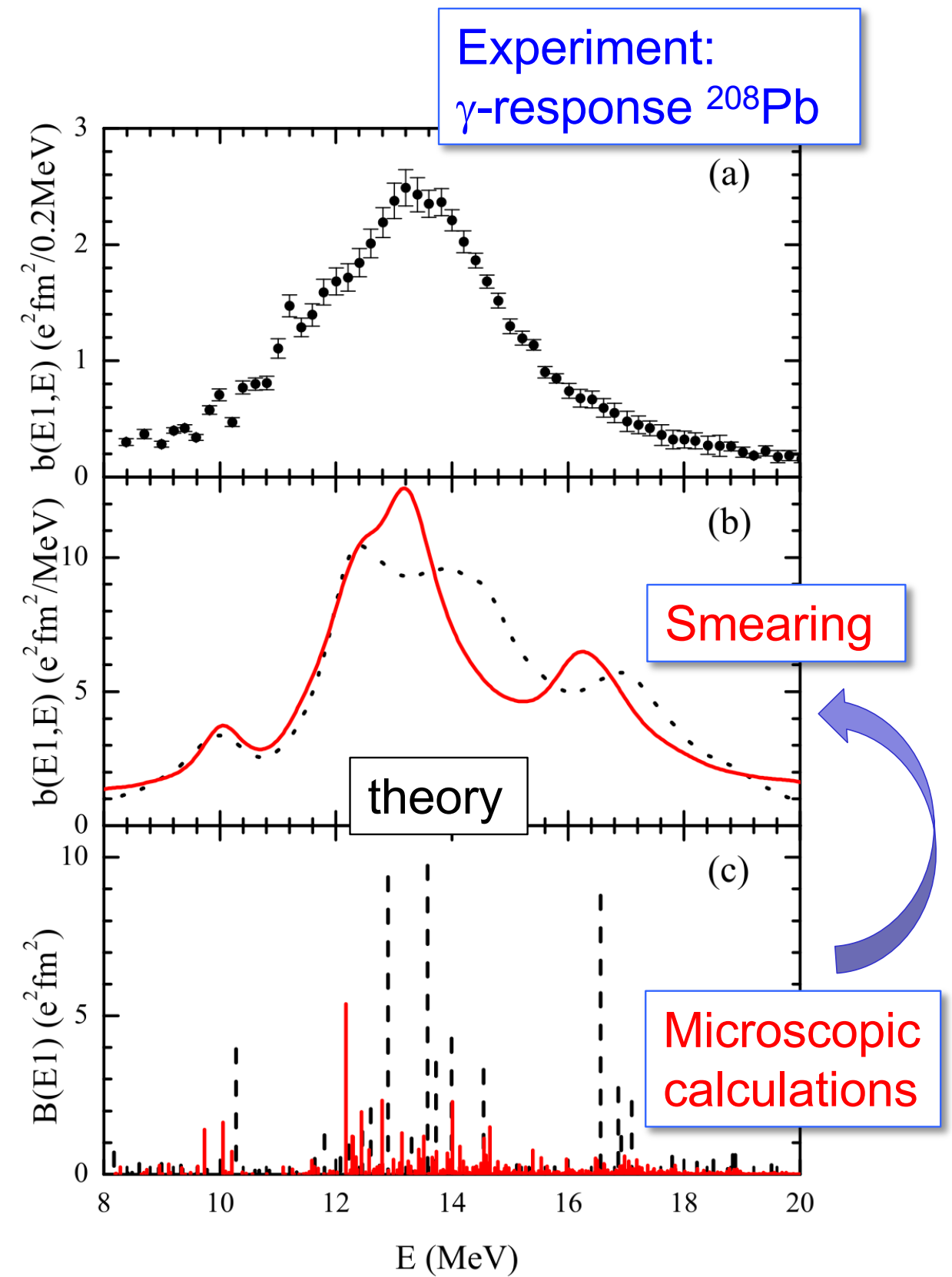
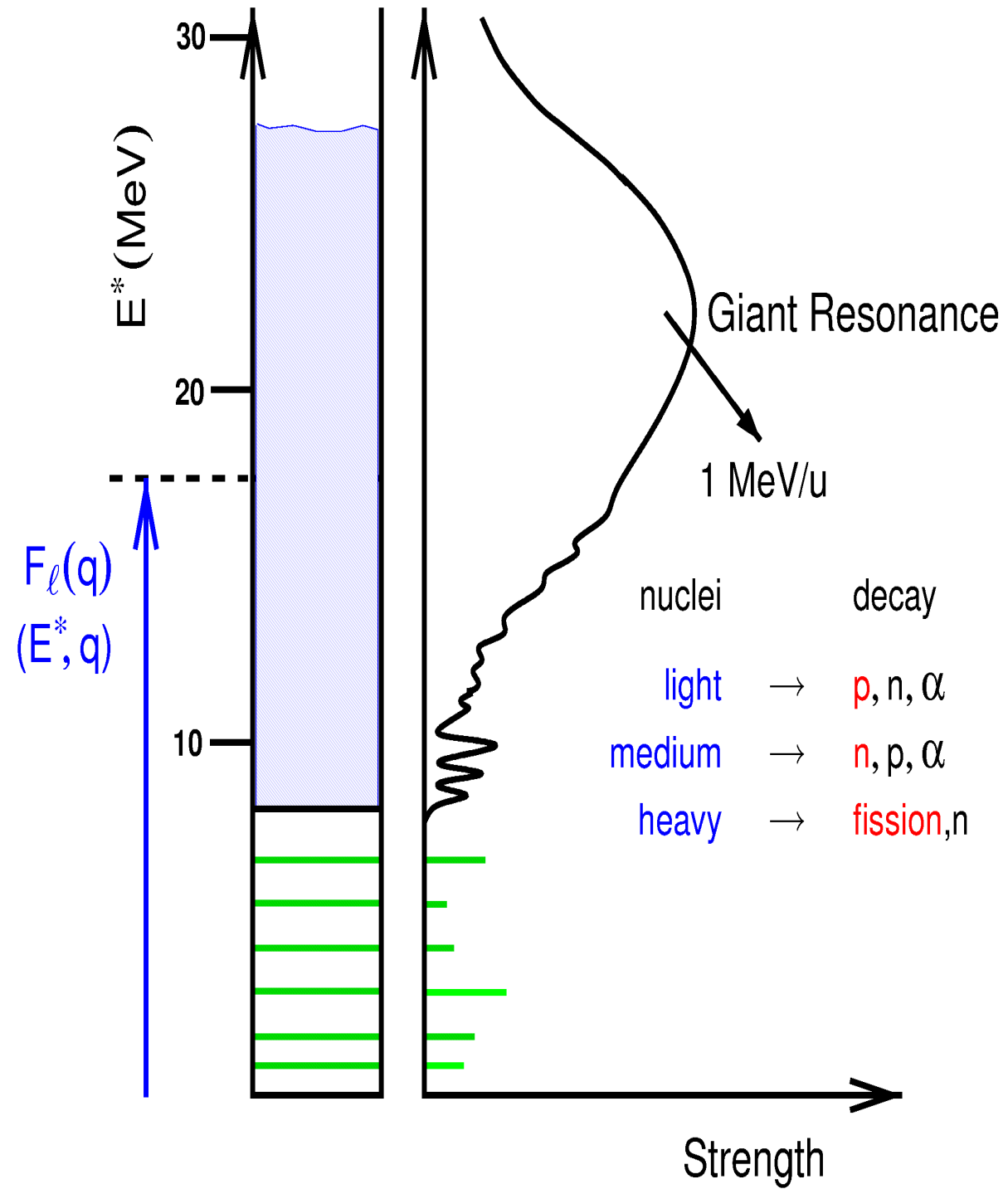
Electromagnetic fragmentation



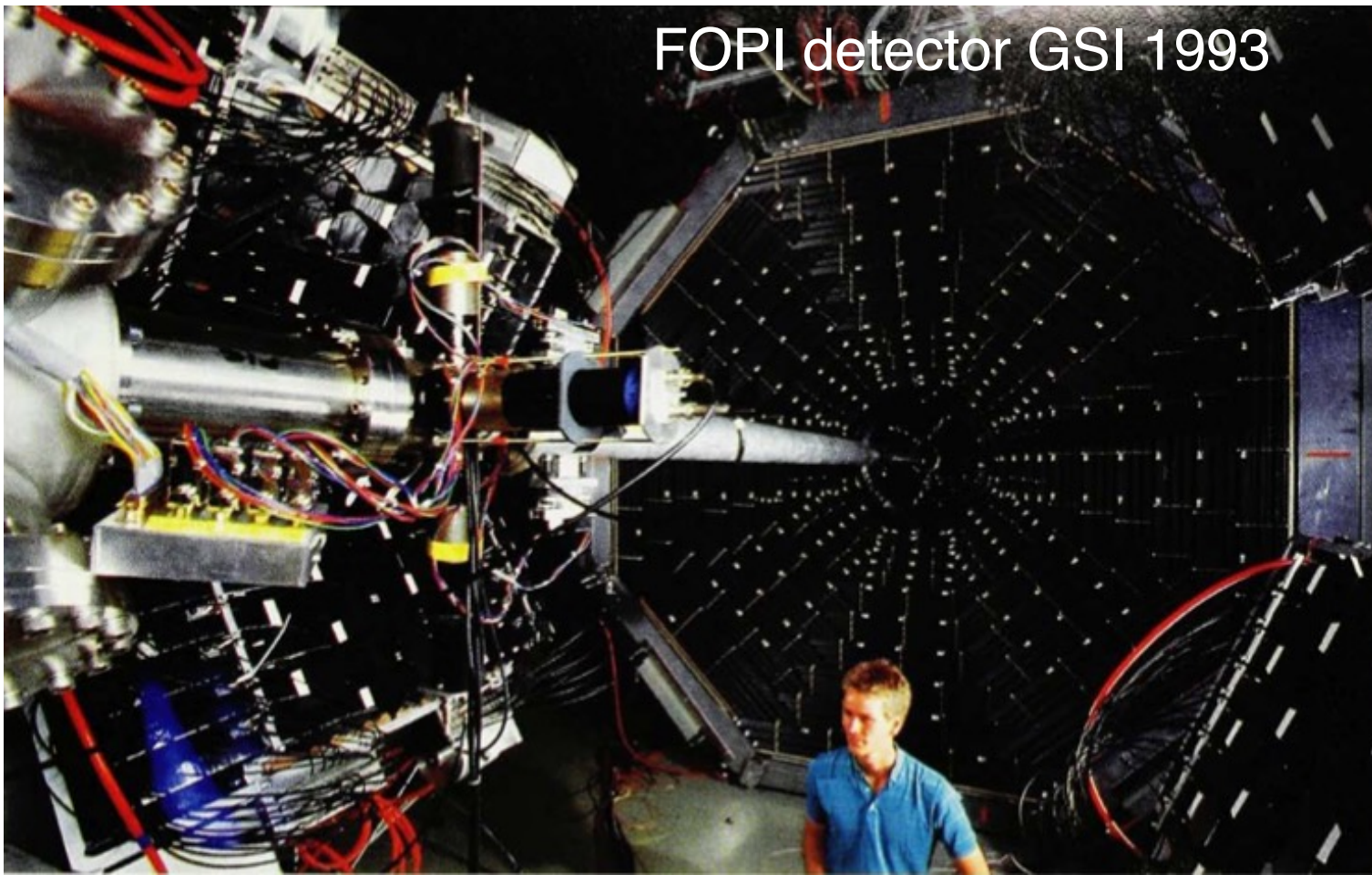
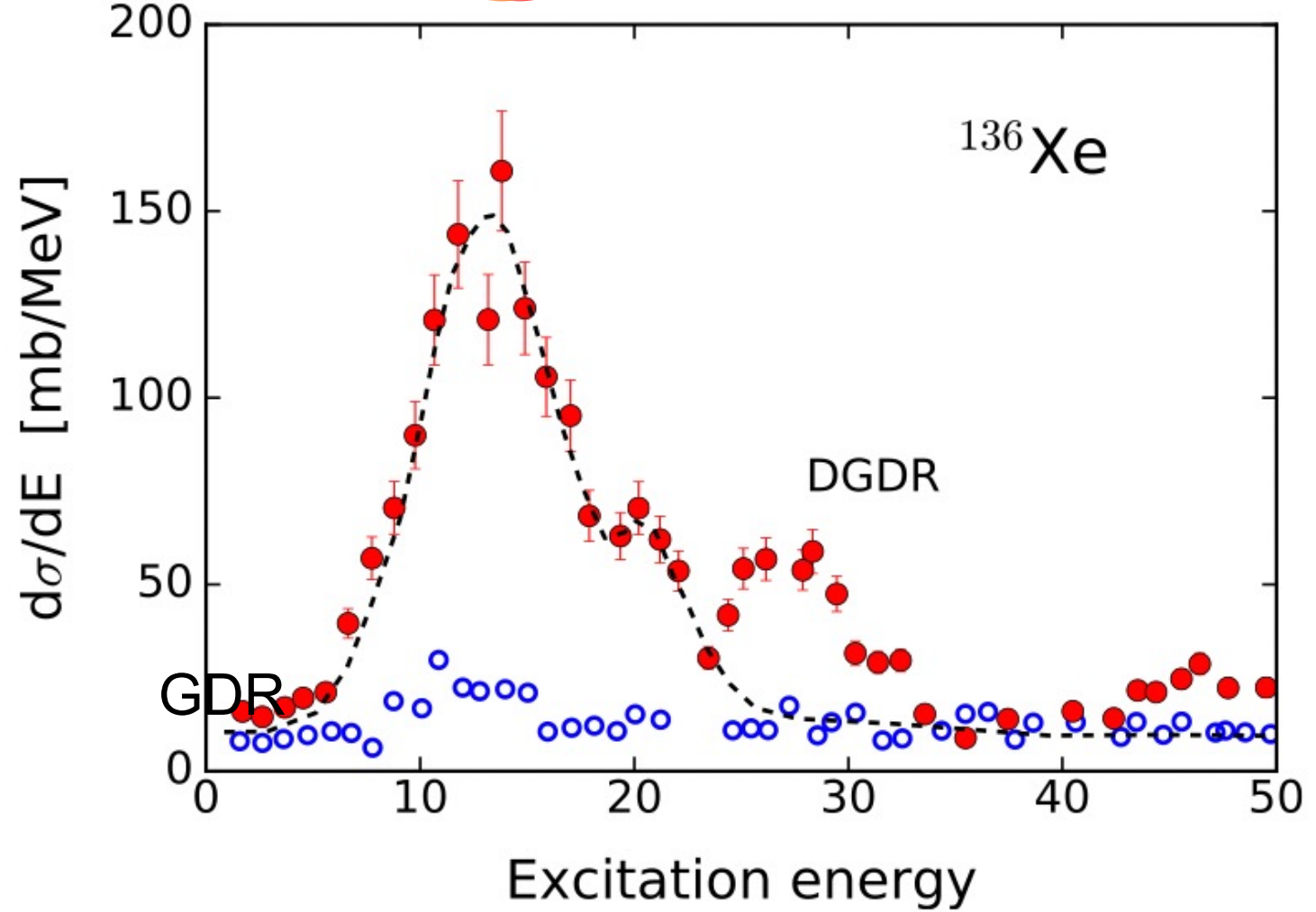
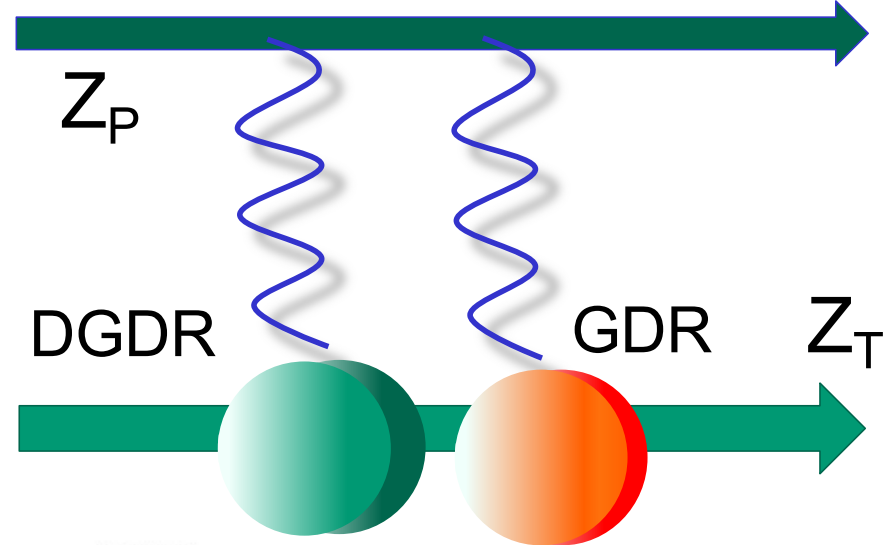
numerous new isotopes

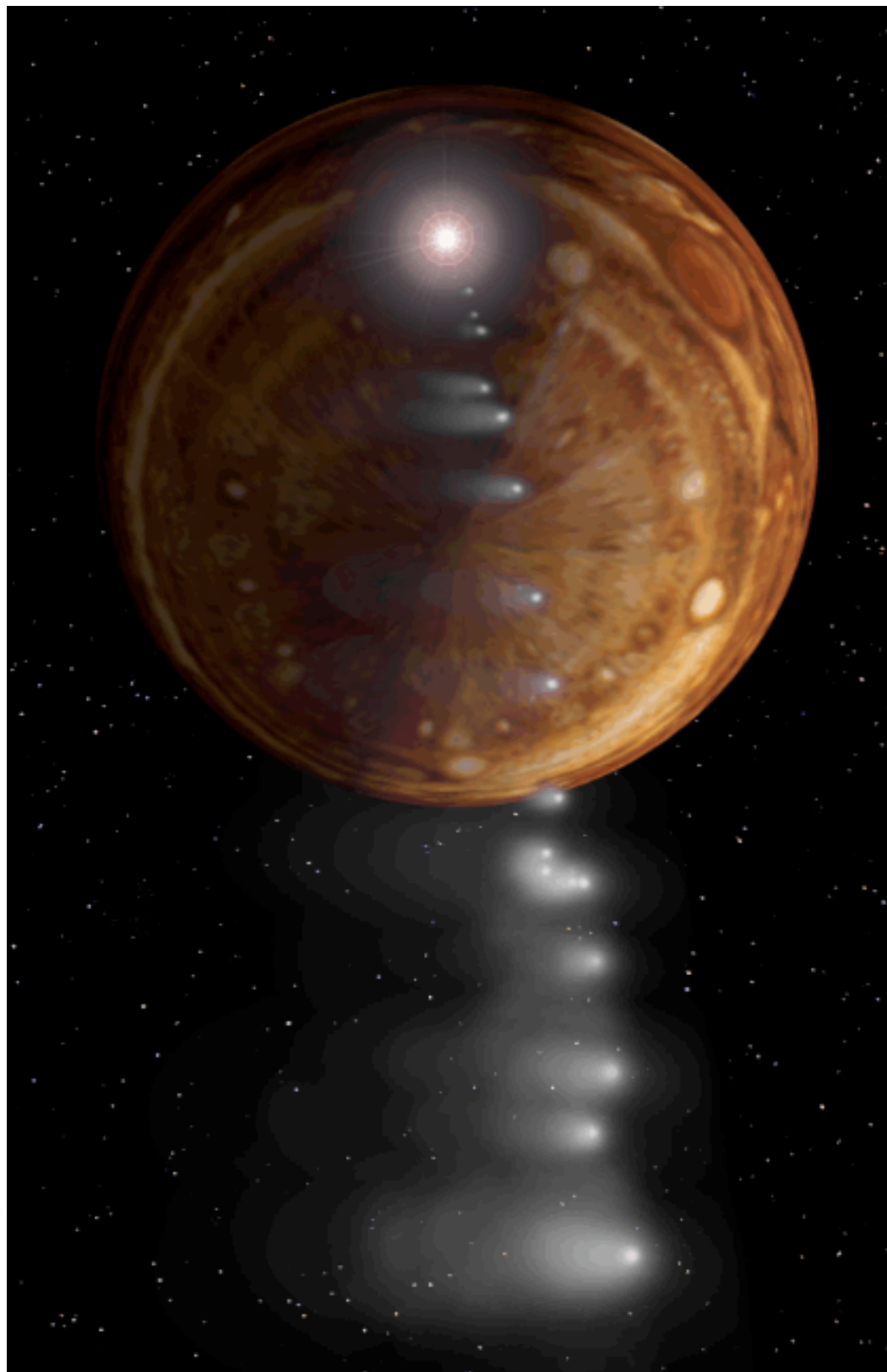


Giant resonances in nuclei



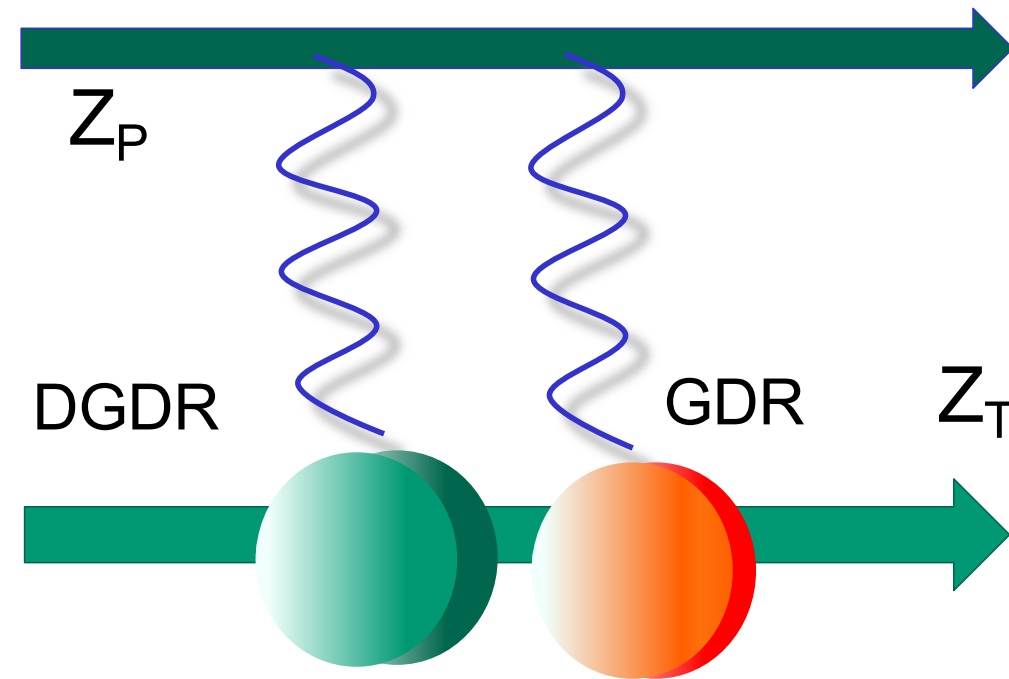
Double giant dipole resonance





Shoemaker-Levi comet (July 1992)

Fragmentation: **Classical and complicated**



Fragmentation: **Quantum and simpler**

Evaporation

Compound nucleus theory

Heisenberg relation: \rightarrow for a state with width Γ

$$\Delta E \Delta t \sim \hbar$$

\rightarrow decay time:

$$\Delta t \sim \frac{\hbar}{\Gamma_\alpha}$$

If many decay channels \rightarrow decay probability =

$$\frac{\Gamma_\alpha}{\sum_\alpha \Gamma_\alpha} = \frac{\Gamma_\alpha}{\Gamma}$$

Bohr hypothesis: formation independent of decay

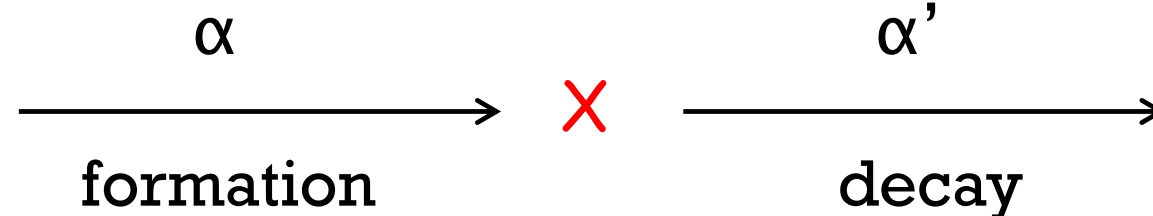
$$\sigma_{\alpha\alpha'} = \sigma_{CN}(\alpha) \frac{\Gamma_{\alpha'}}{\Gamma}$$

$a + b$

or

$c + d$

or ...



Ewing-Weisskopf theory

detailed balance:

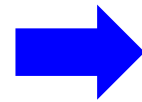
$$g_{\alpha} k_{\alpha}^2 \sigma_{\alpha\alpha'} = g_{\alpha'} k_{\alpha'}^2 \sigma_{\alpha'\alpha}$$

spin counting

for CN:

$$g_{\alpha} k_{\alpha}^2 \sigma_{CN}(\alpha) \Gamma_{\alpha'} = g_{\alpha'} k_{\alpha'}^2 \sigma_{CN}(\alpha') \Gamma_{\alpha}$$

$$\frac{\Gamma_{\alpha'}}{g_{\alpha'} k_{\alpha'}^2 \sigma_{CN}(\alpha')} = \frac{\Gamma_{\alpha}}{g_{\alpha} k_{\alpha}^2 \sigma_{CN}(\alpha)}$$



$$\Gamma_{\alpha} = g_{\alpha} k_{\alpha}^2 \sigma_{CN}(\alpha)$$

introducing density of levels ρ of final states:

$$\sigma_{\alpha\alpha'} = \sigma_{CN}(\alpha) \frac{\mu_{\alpha'} E_{\alpha'} \sigma_{CN}(\alpha') \rho(E_{\alpha'})}{\sum_{\alpha} \int \mu_{\alpha} E_{\alpha} \sigma_{CN}(\alpha) \rho(E_{\alpha}) dE_{\alpha}}$$

Hauser-Feshbach theory

Include angular momentum conservation in the Ewing-Weisskopf theory

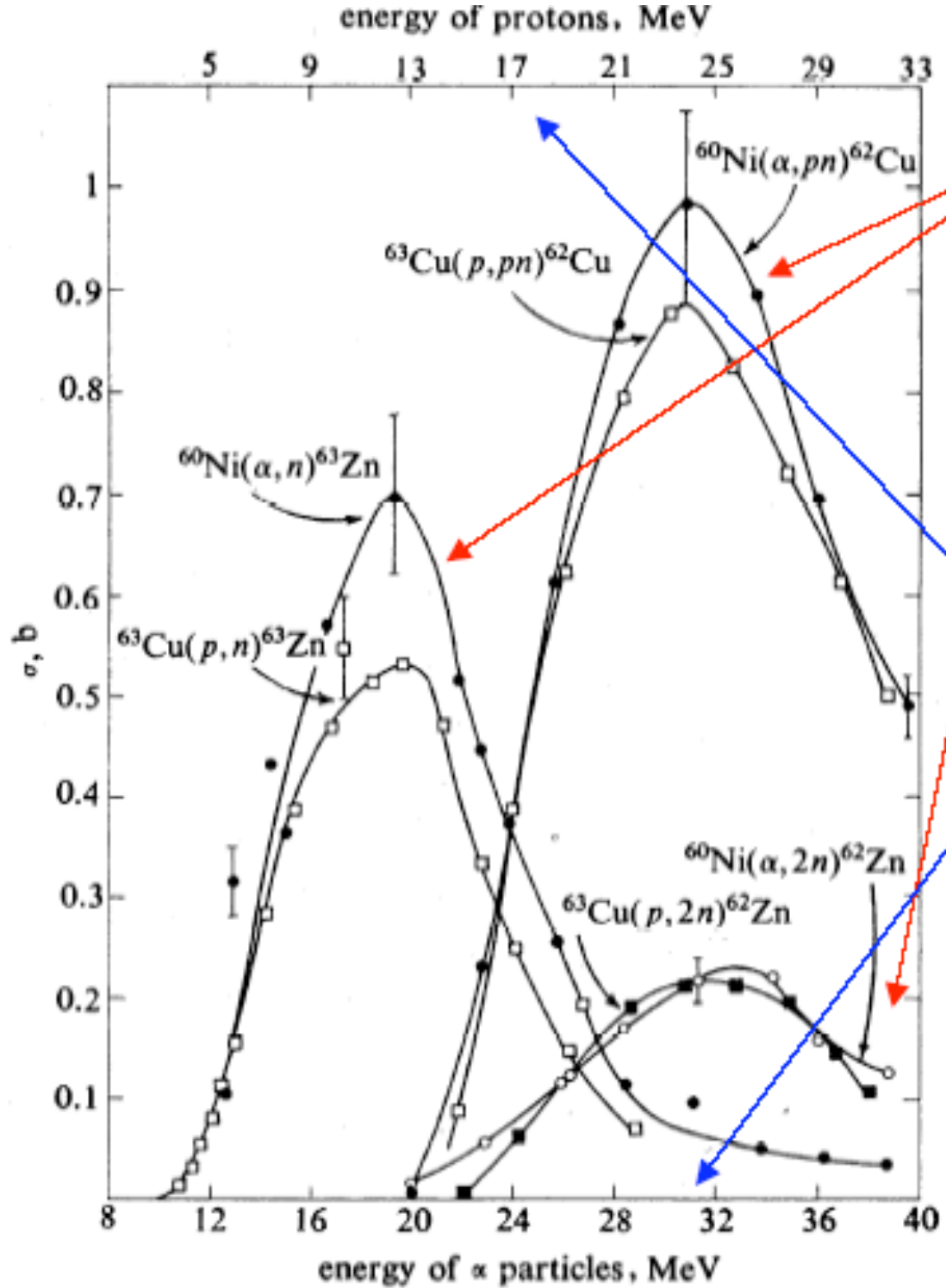
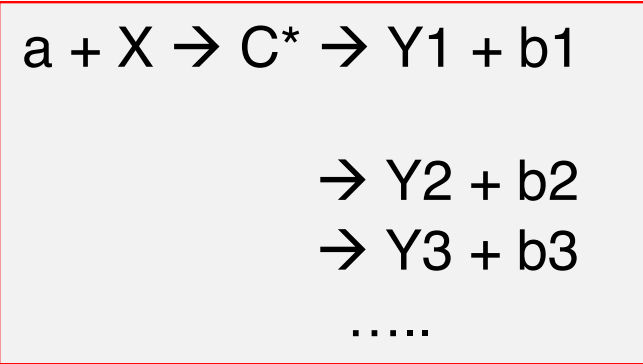
CN ang. mom. transmission probability

$$\sigma_{CN}(\alpha) = \frac{\pi}{k^2} \sum_J \frac{2J + 1}{(2j_a + 1)(2j_b + 1) \prod_{l,s,\alpha'} T_{l,s}(\alpha')}$$

projectile spin target spin

Optical potentials

Compound nucleus formation & decay

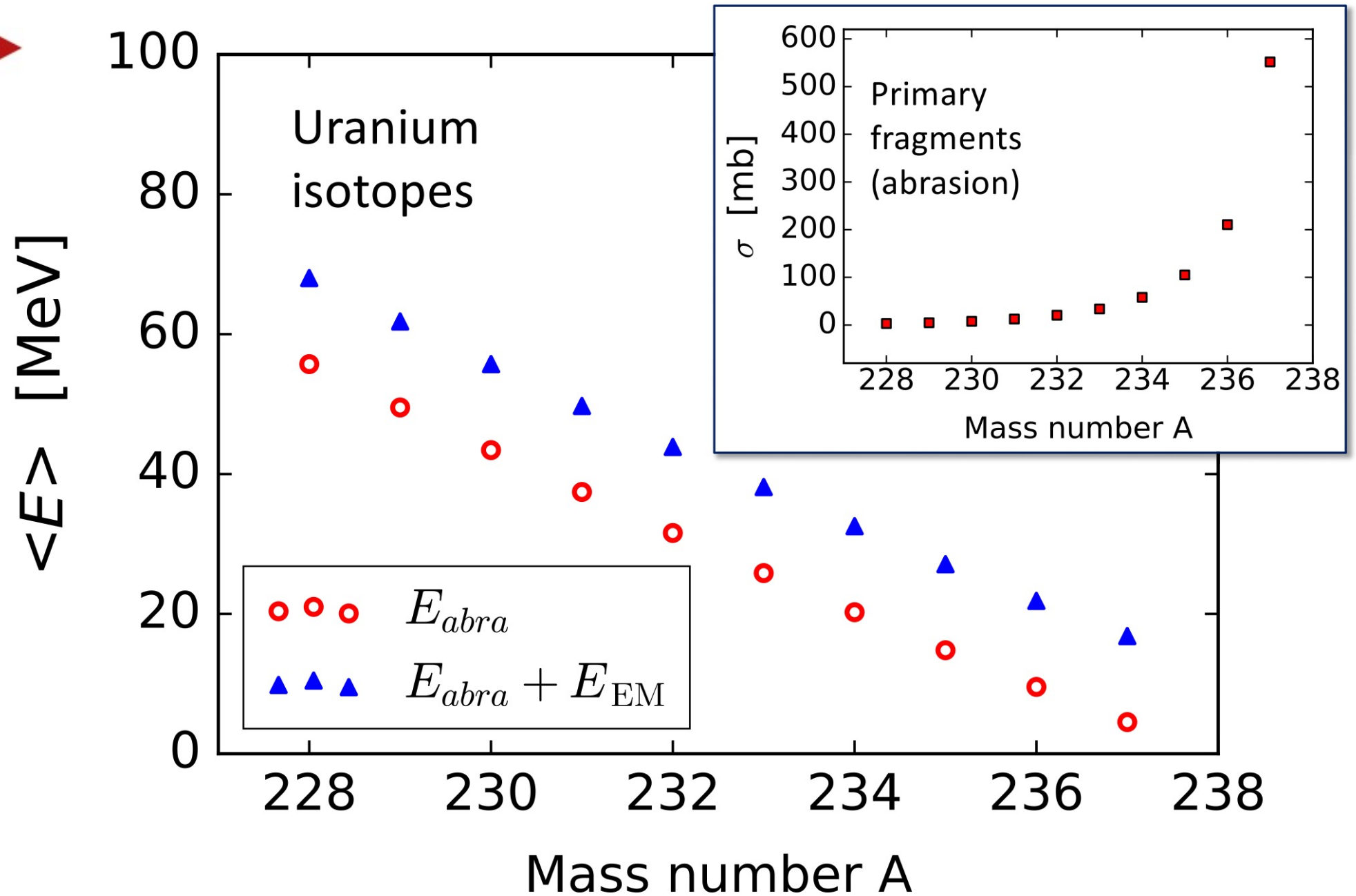
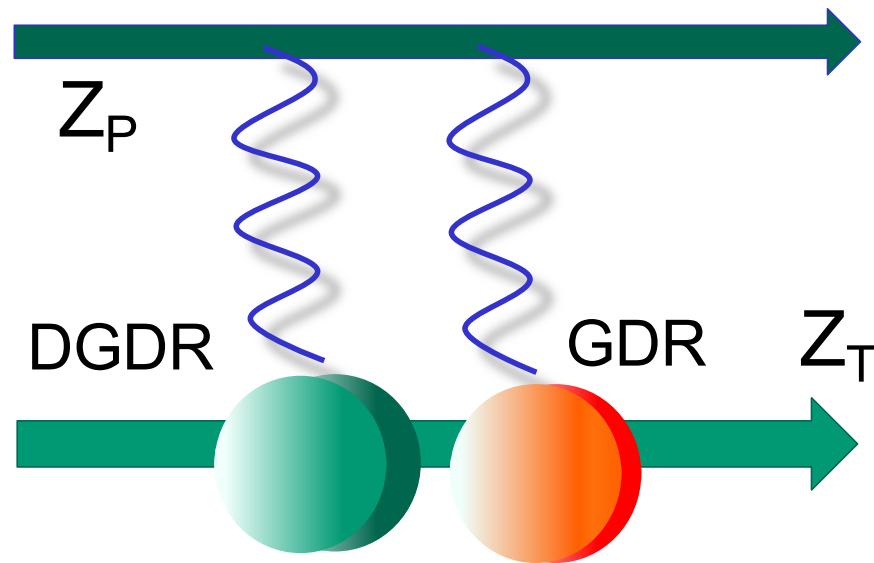
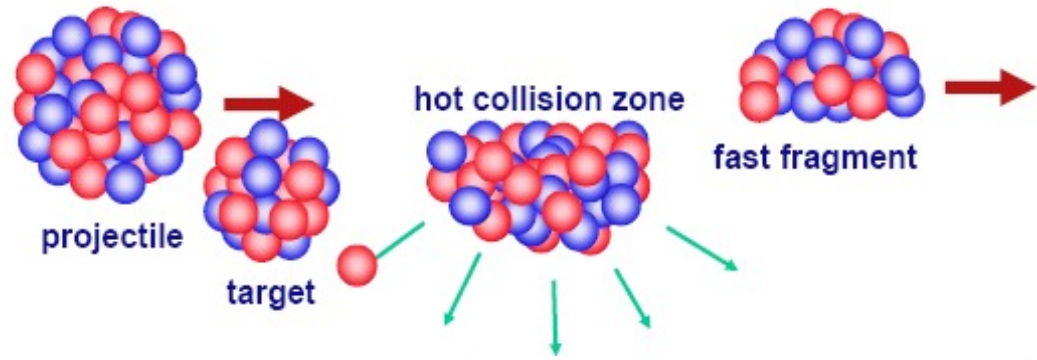


*Same final state;
different initial state*

*Varying energies
for p and alpha*

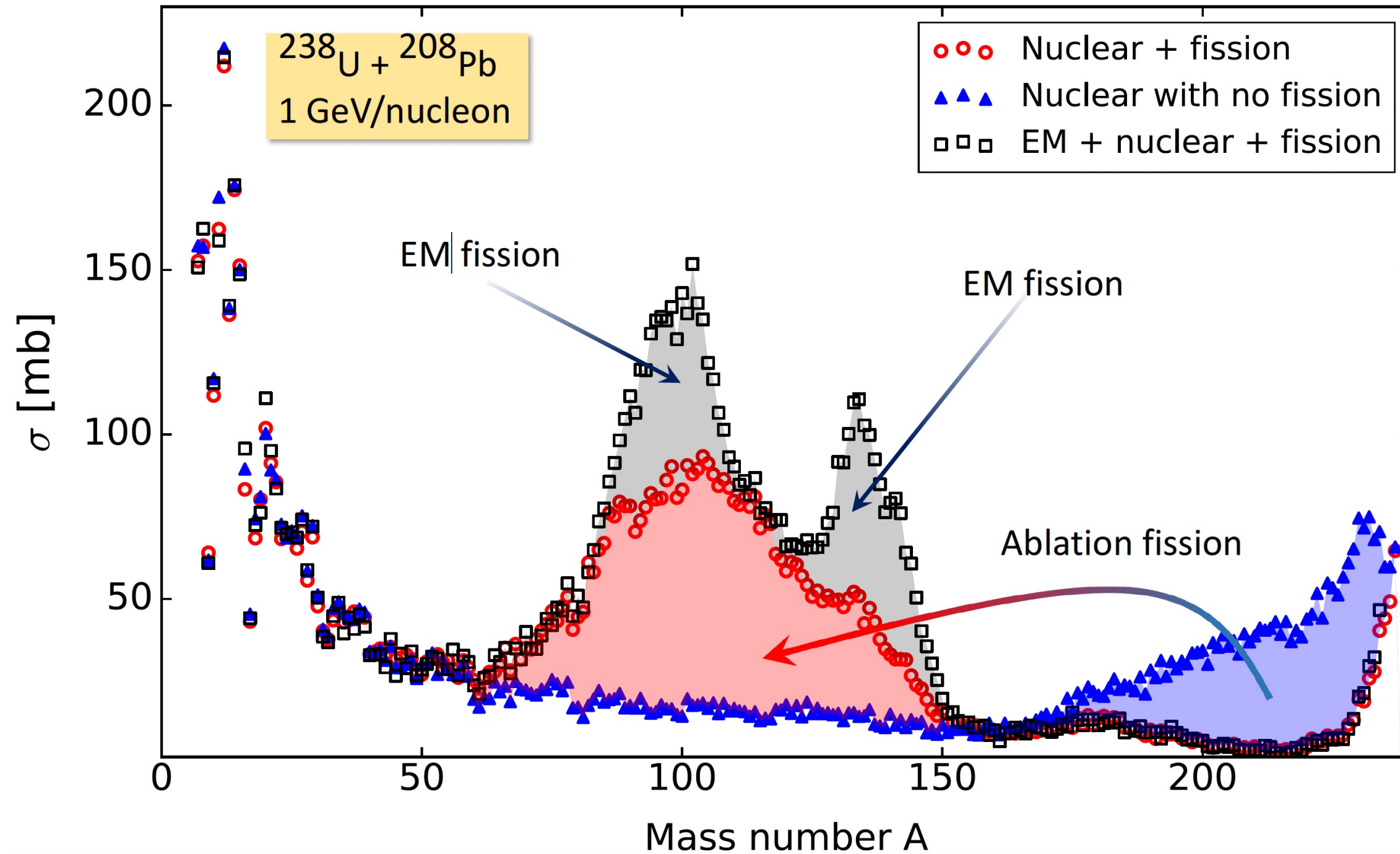
Textbook example

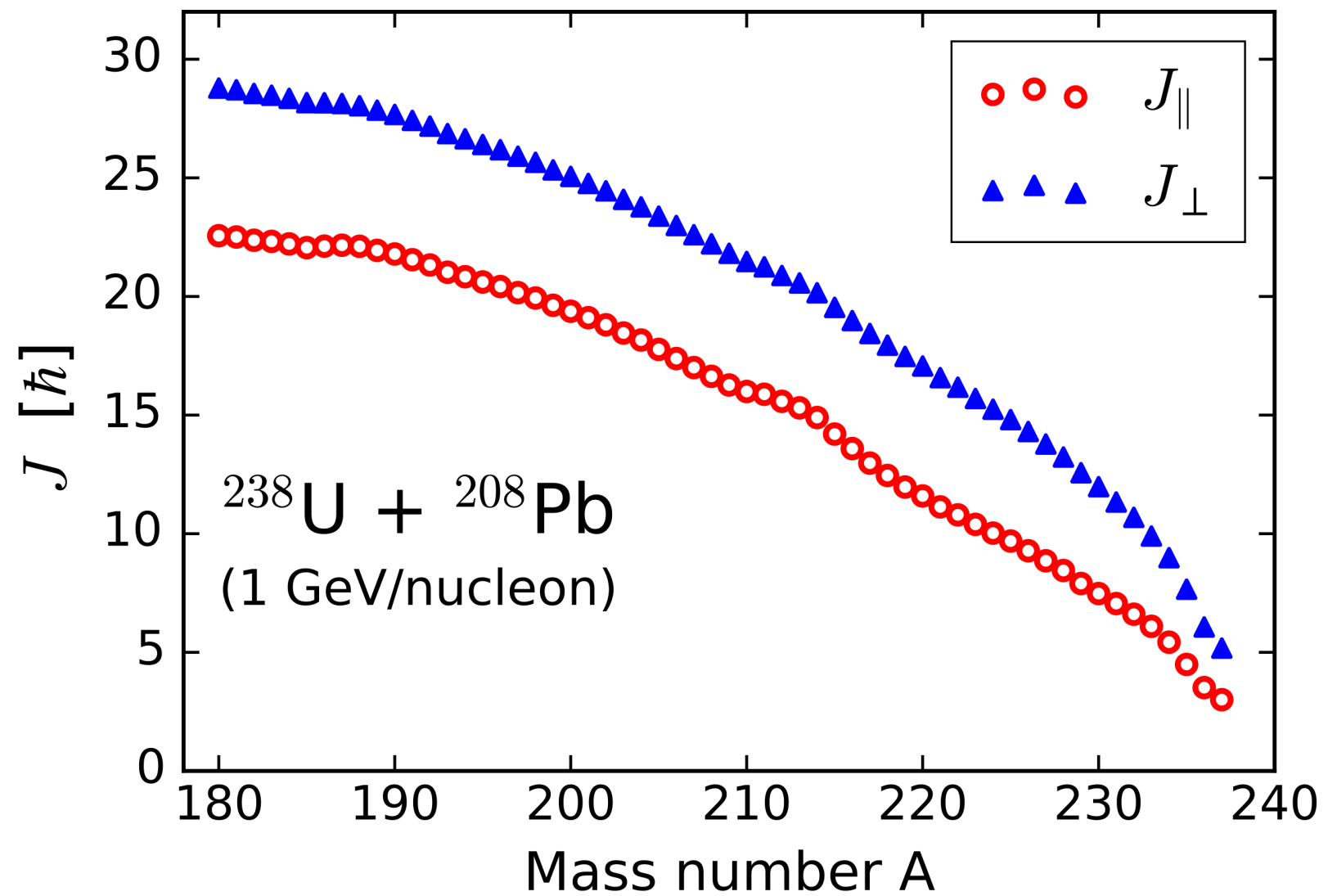
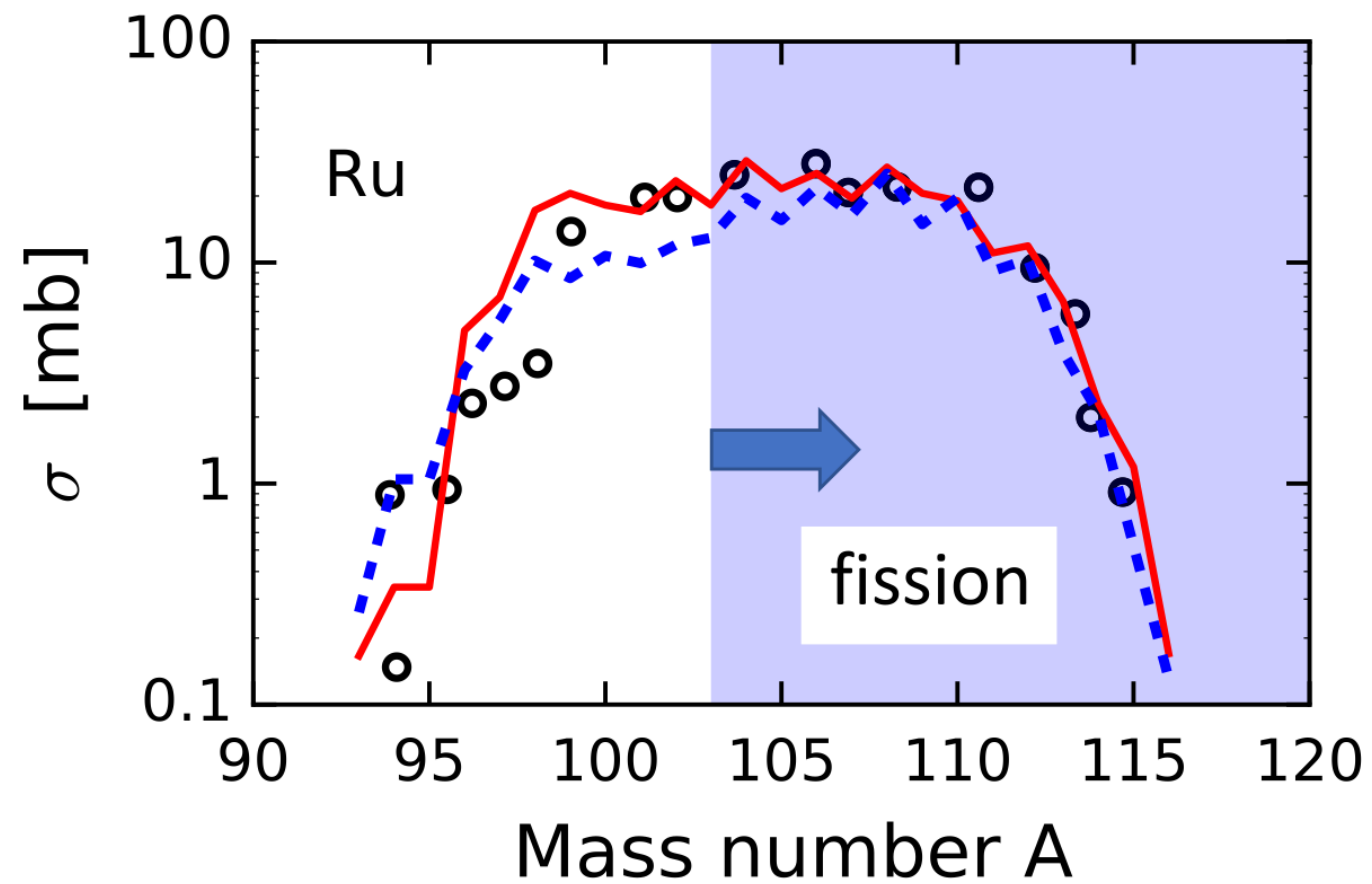
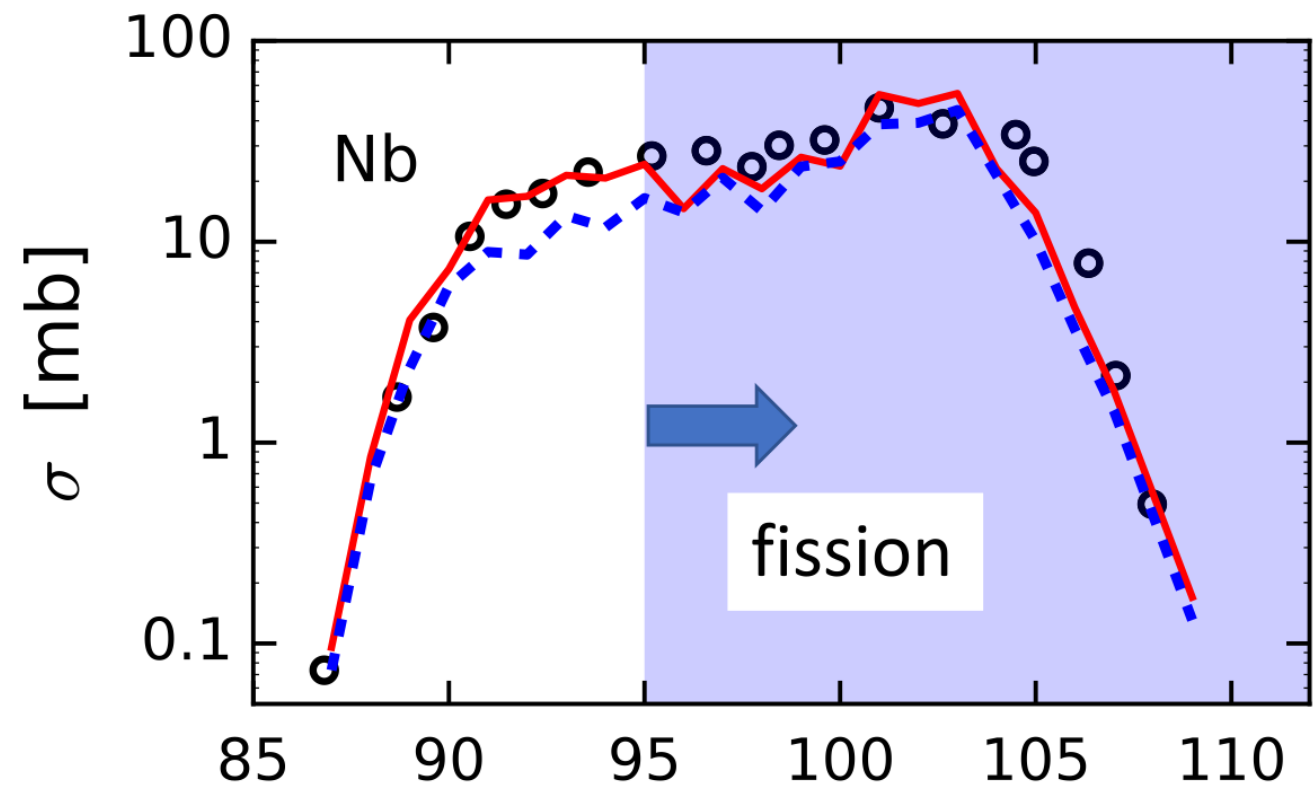
Fragmentation in heavy ion collisions



Fragmentation in heavy ion collisions

CB, Kucuk, Lozeva, PRL 124, 132301 (2020)





Five previously unknown isotopes
(182;183Tm, 186;187Yb, 190Lu)
[PRL 132, 072501 \(2024\)](#)

“Static” NS

Tolman-Oppenheimer-Volkoff +

$$K_{\infty} = 9\rho_0^2 \left. \frac{d^2 [E/A]}{d\rho^2} \right|_{\rho_0}$$

NM
incompressibility

$$S \equiv J = \frac{1}{2} \left. \frac{d^2 [E/A]}{d\delta^2} \right|_{\delta=0}$$

Symmetry energy

$$\delta = \frac{\rho_n - \rho_p}{\rho}$$

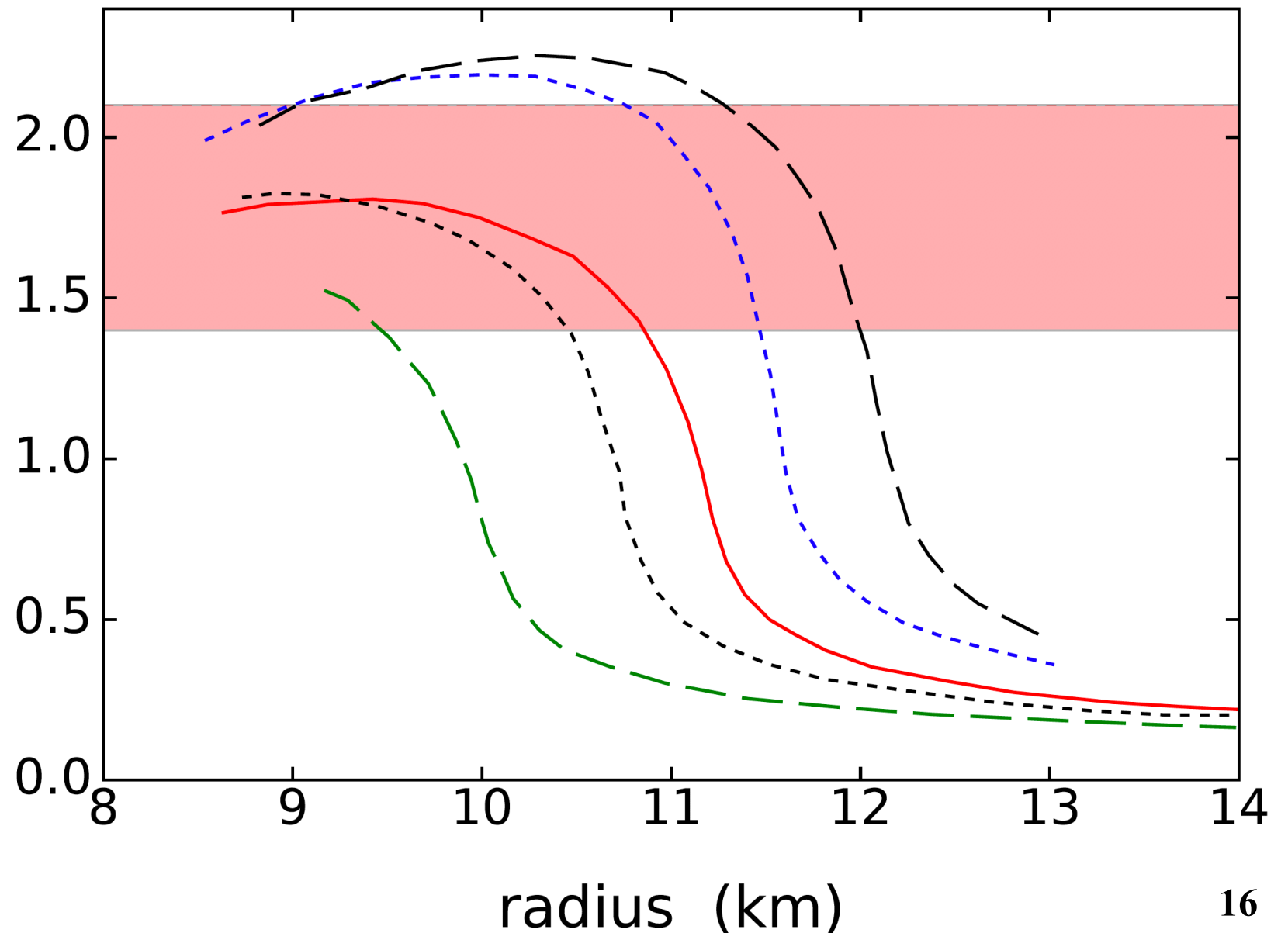
$$L = 3\rho_0 \left. \frac{dS}{d\rho} \right|_{\delta=0}$$

Slope parameter

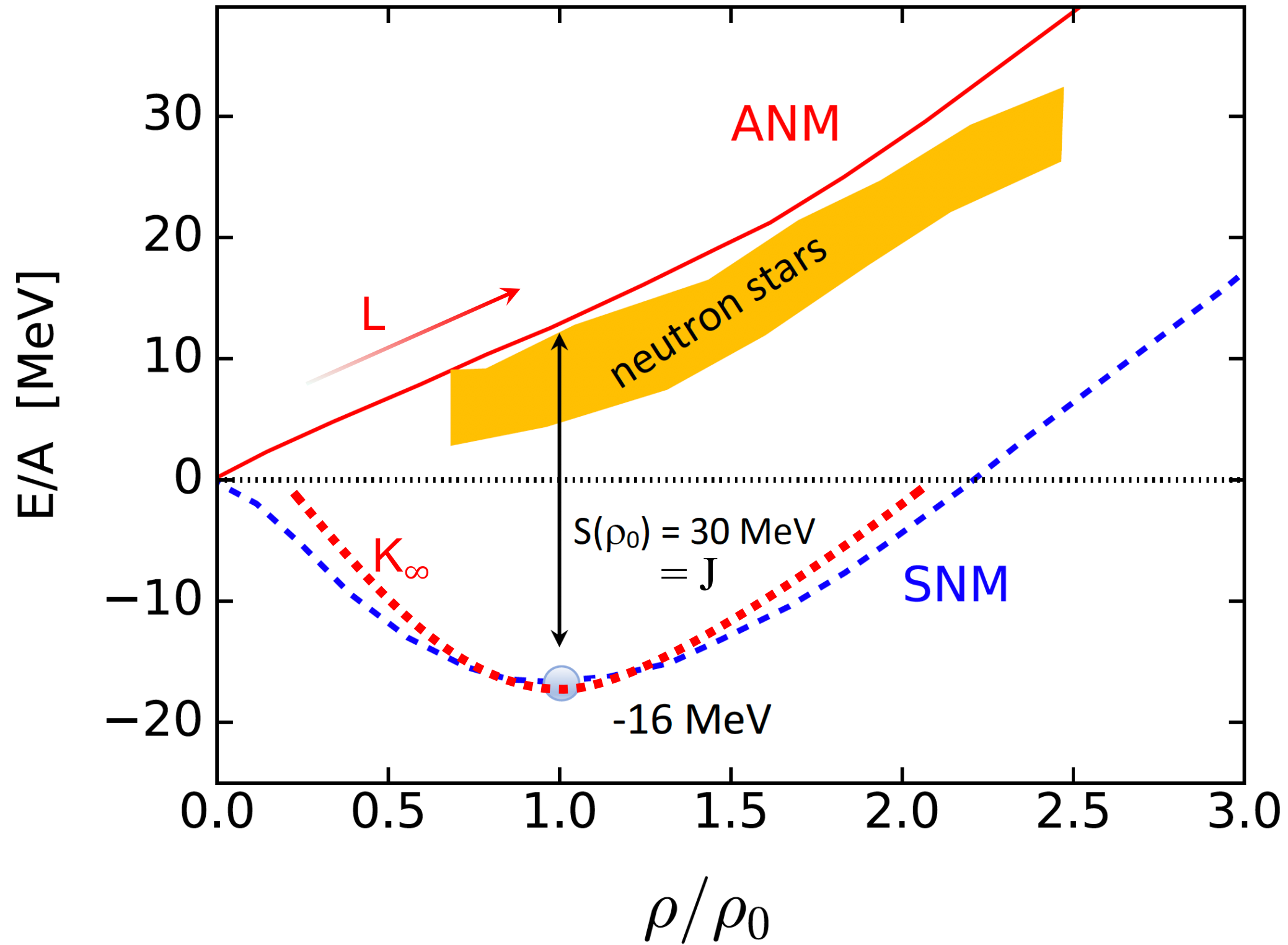
EOS

$$p[\rho] = \rho^2 \frac{d}{d\rho} \left(\frac{E}{A}[\rho] \right)$$

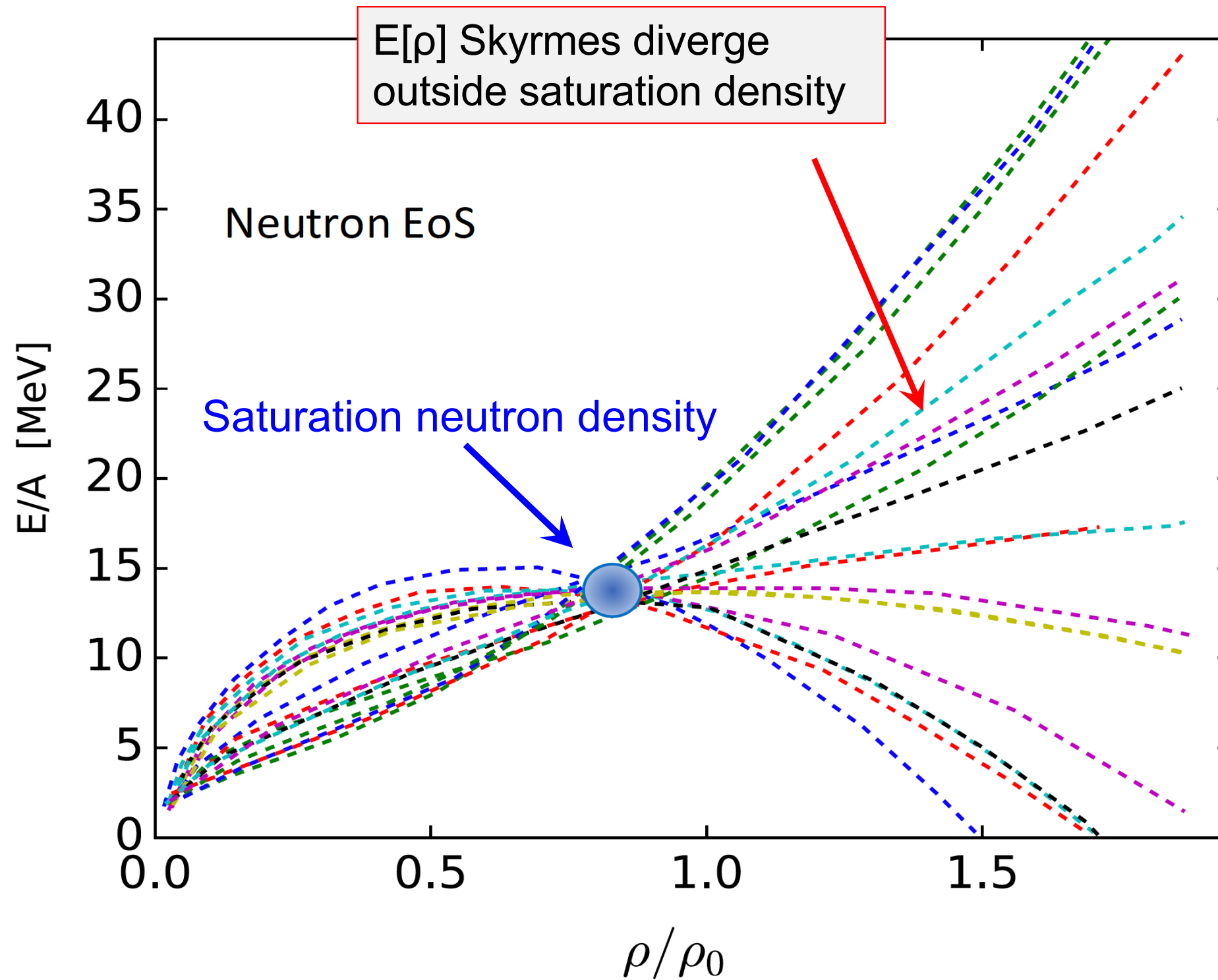
$E(\rho)/A$ from
microscopic
calculations



EOS of nuclear matter



EOS & Neutron stars



EOS + symmetry energy

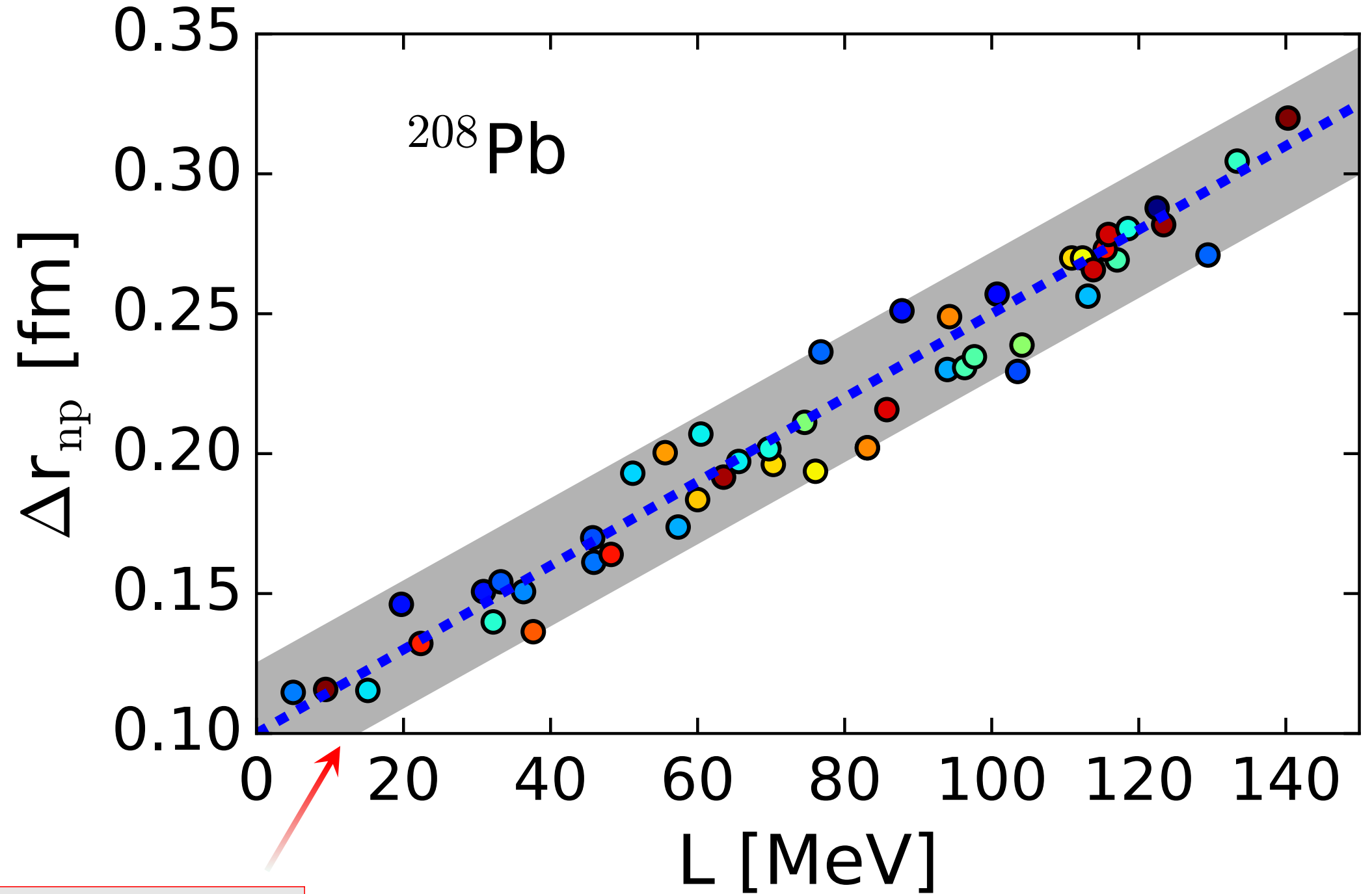
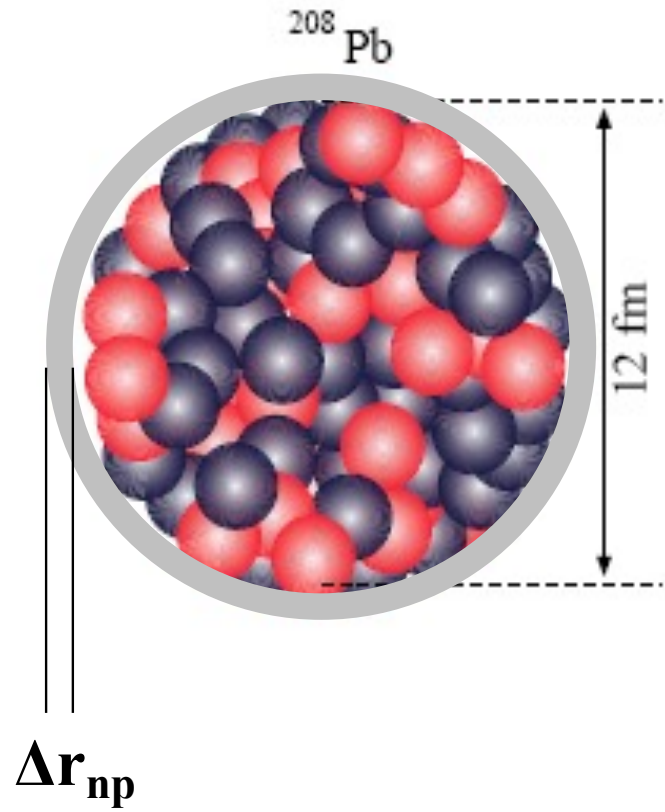
$$\text{For } \rho \sim \rho_0 \text{ and } \rho_p \sim 0, \quad \Rightarrow \quad p \sim \frac{\rho_0}{3} L$$

L crucial for
neutron matter

Skyrme	ρ_0	E_0	K_∞	J	L
MSk6	0.157	-15.79	-231.17	28.00	9.63
SKS4	0.163	-15.88	228.08	28.35	23.28
SLy5	0.161	-15.99	229.92	32.01	48.15
Skxs20	0.162	-15.81	201.95	35.50	67.06
SkI5	0.156	-15.82	255.57	36.63	129.27

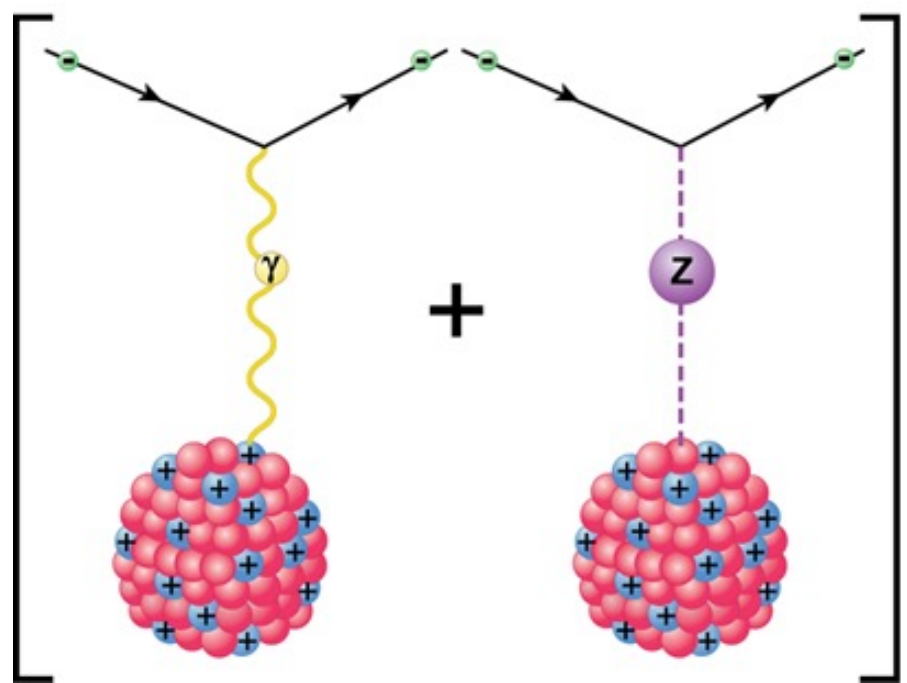
L not well known

Neutron skins in nuclei



Numerous EDF

n-skin from PV e⁻ scattering

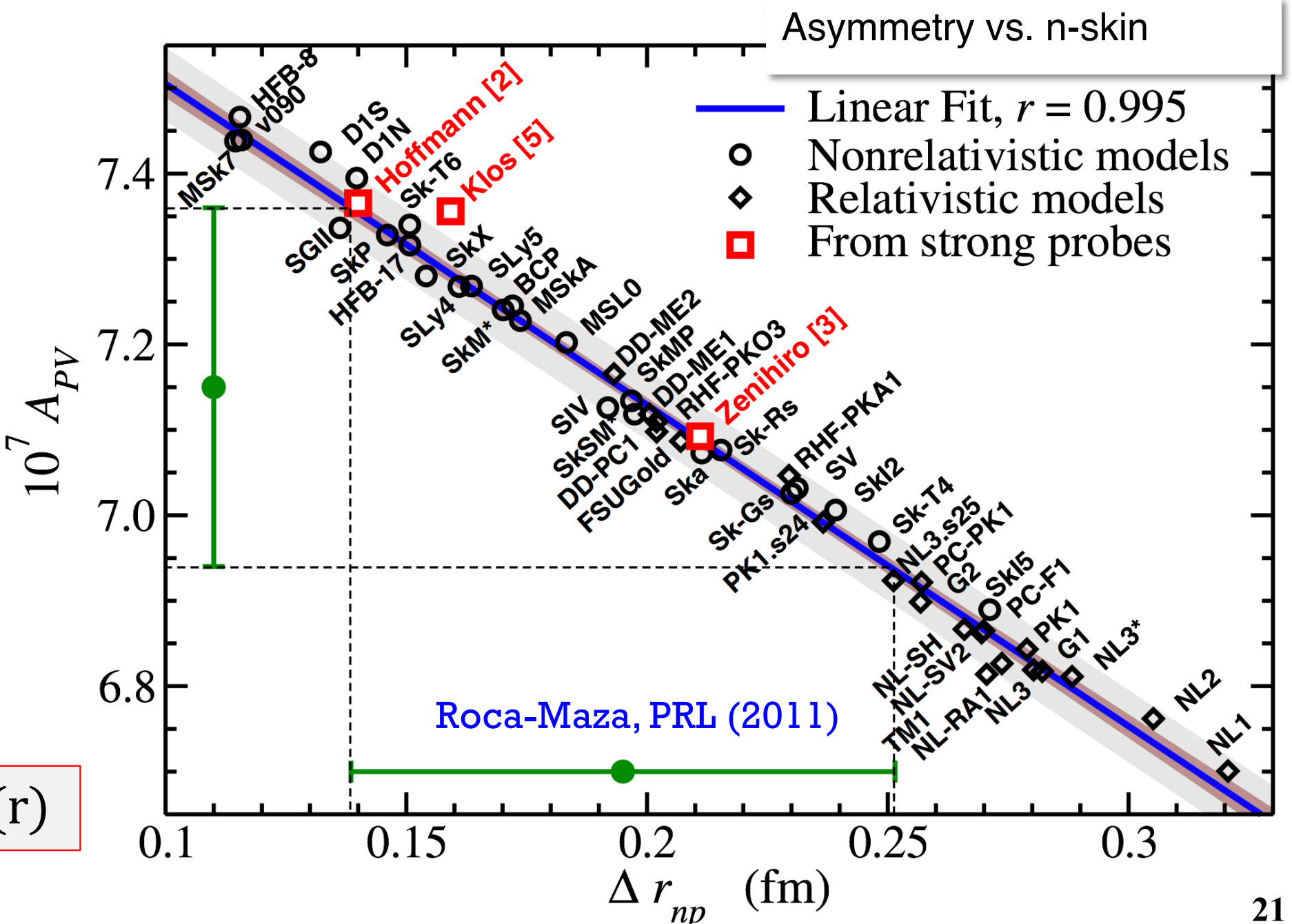


$$A_{PV} = \frac{d\sigma_R - d\sigma_L}{d\sigma_R + d\sigma_L}$$

$$A_{PV}(Q^2) \sim \frac{F_W(Q)}{F_{ch}(Q)}$$

$$F_W \sim \int dr \frac{\sin(Qr)}{Qr} \rho_w(r)$$

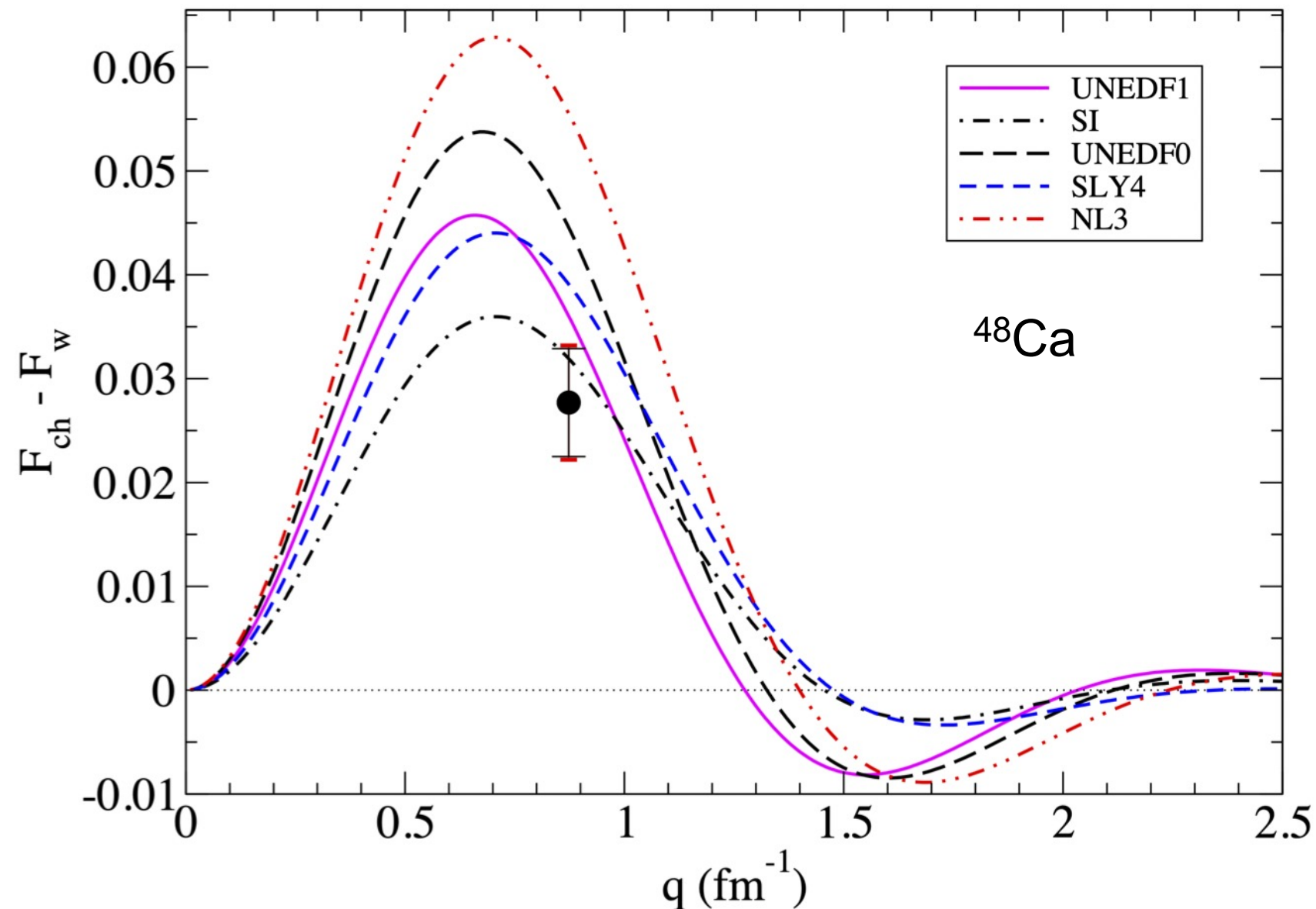
$$\rho_w(r) \sim \rho_{ch}(r) + c_n \rho_n(r) + c_p \rho_p(r)$$



n-skin from e⁻ PV scattering

$$F(Q^2) \sim 1 - \frac{1}{6}q^2 \langle r^2 \rangle$$

$$\langle r^2 \rangle \cong -6 \frac{dF(Q^2)}{dQ^2}$$



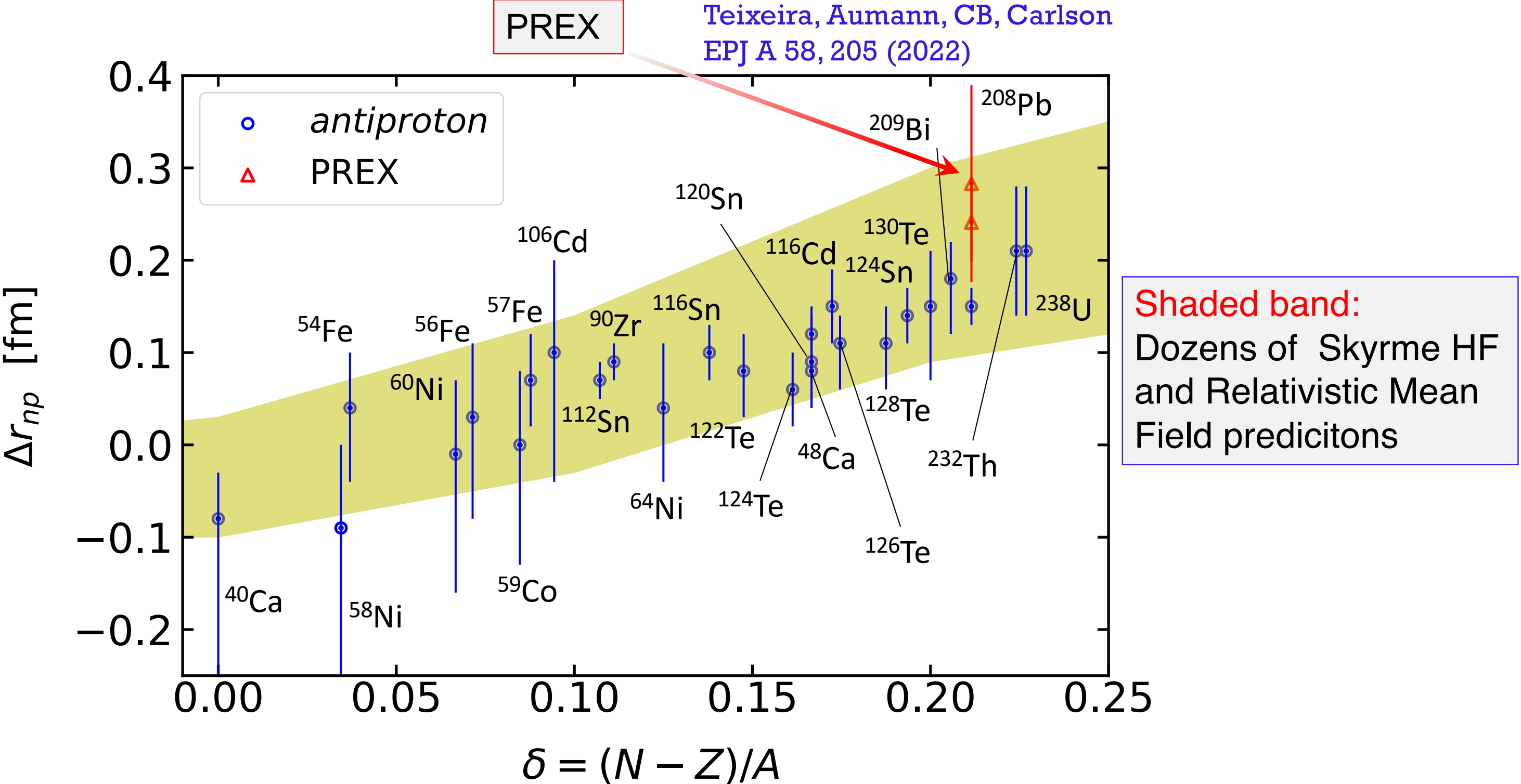
- PREX & CREX: measurement of parity violating asymmetry
- Determine n-skin and/or L by comparison to predictions from DFT

$$(R_n - R_p)_{48\text{Ca}} = 0.121 \pm 0.025 \text{ fm}$$

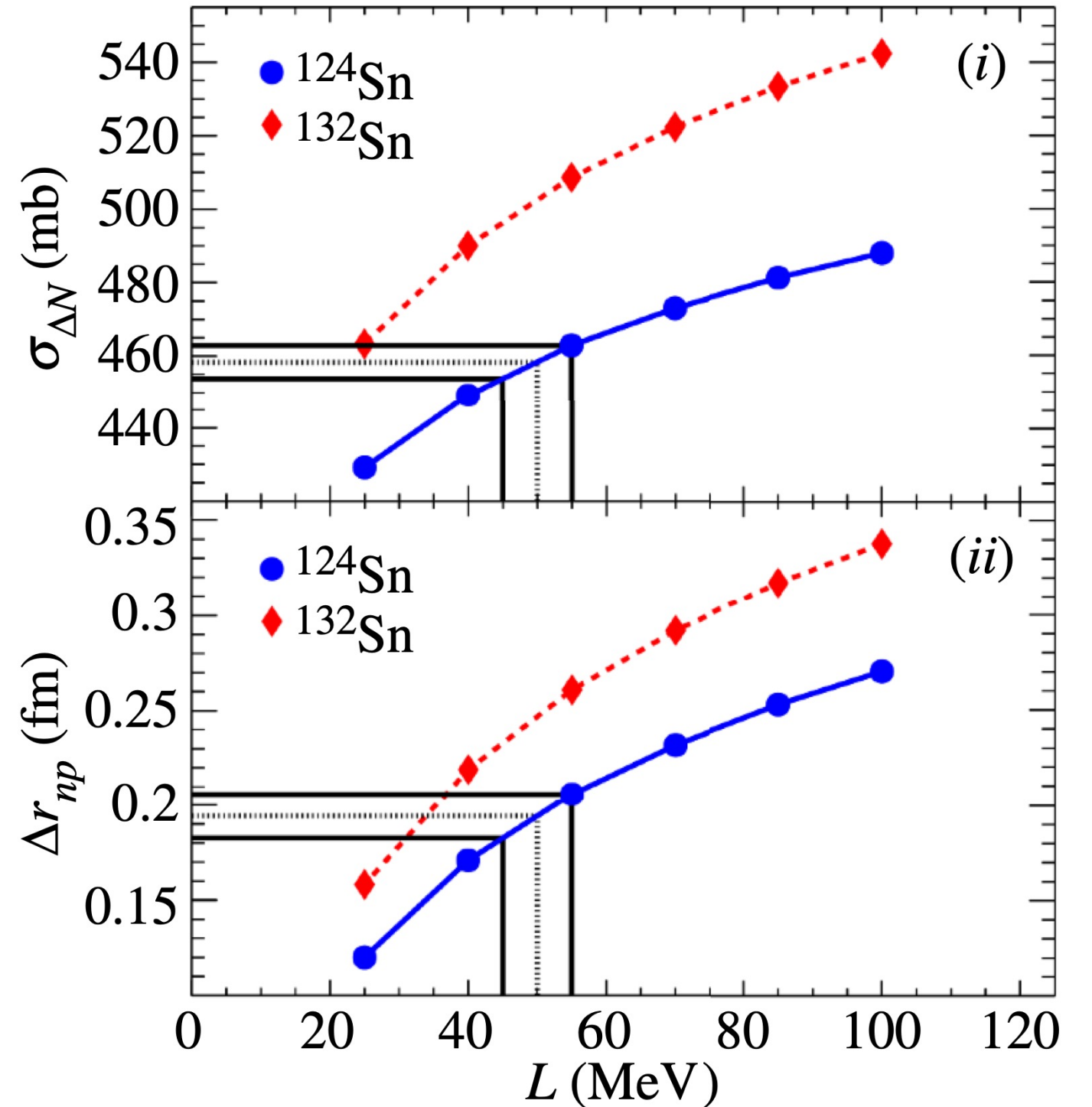
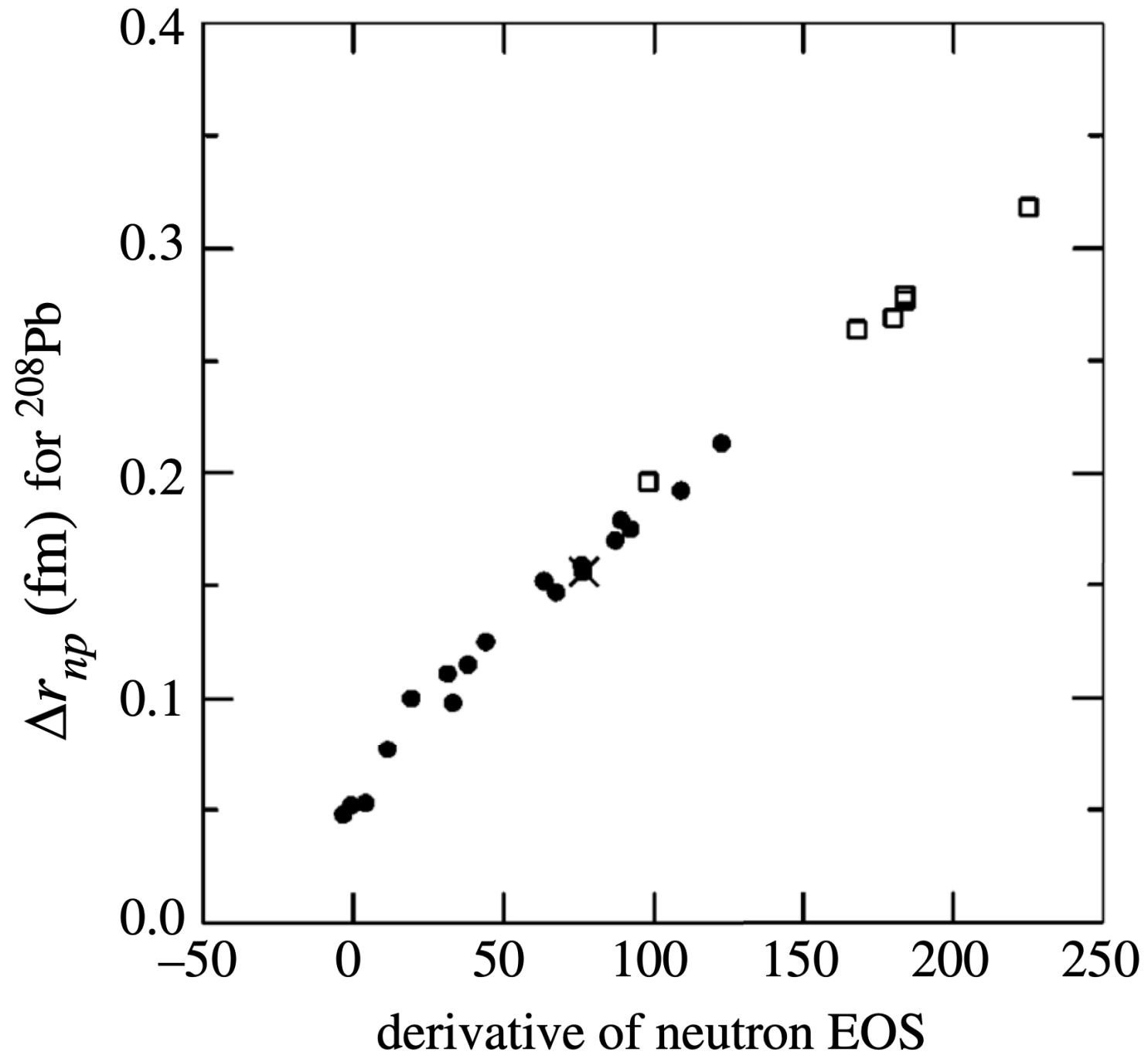
$$(R_n - R_p)_{208\text{Pb}} = 0.33 \pm 0.17 \text{ fm}$$

Adhikari et al, PRL 126, 172502 (2021)
PRL 129, 042501 (2022)

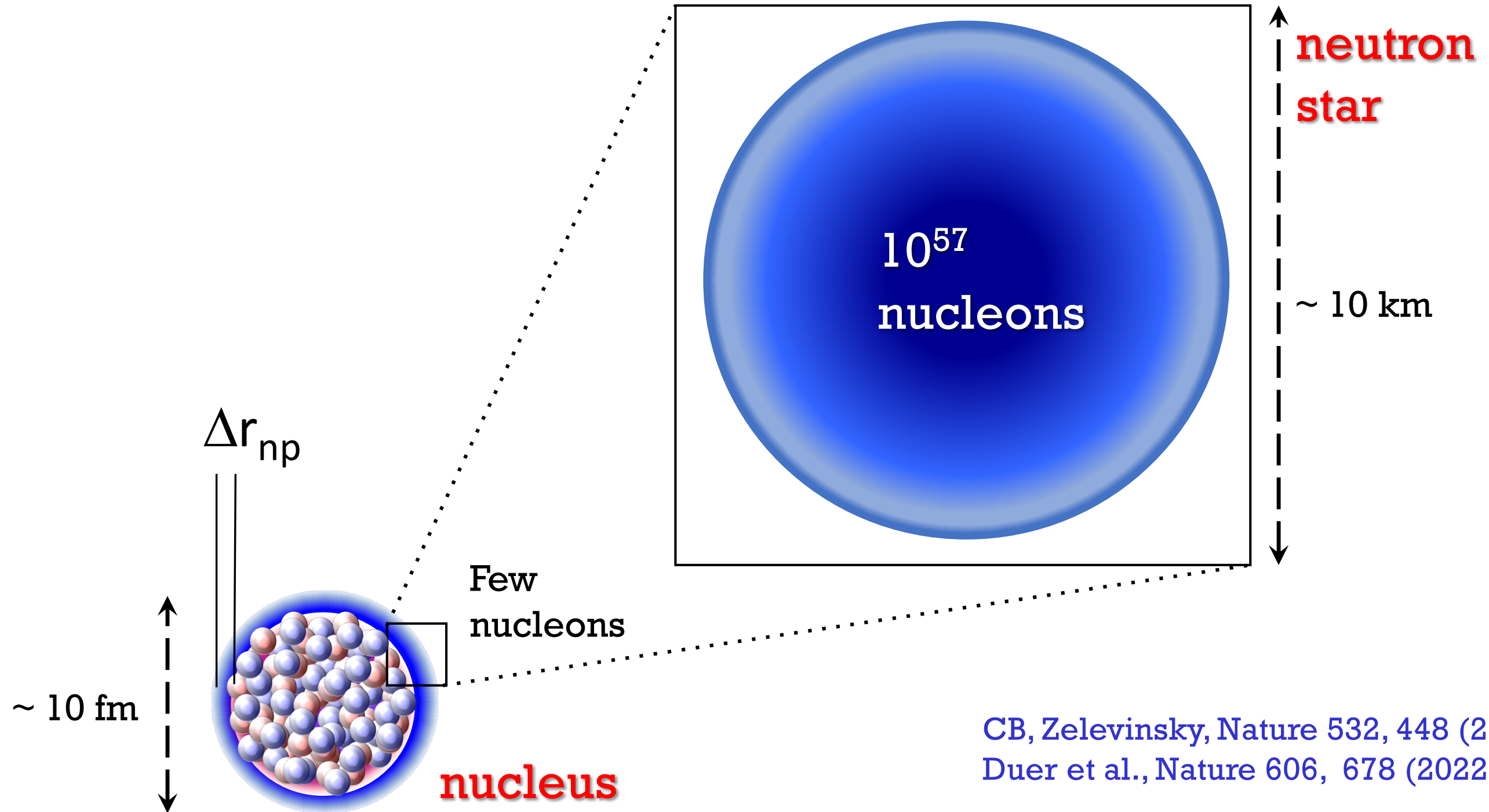
Status of neutron skins



Fragmentation and symmetry energy

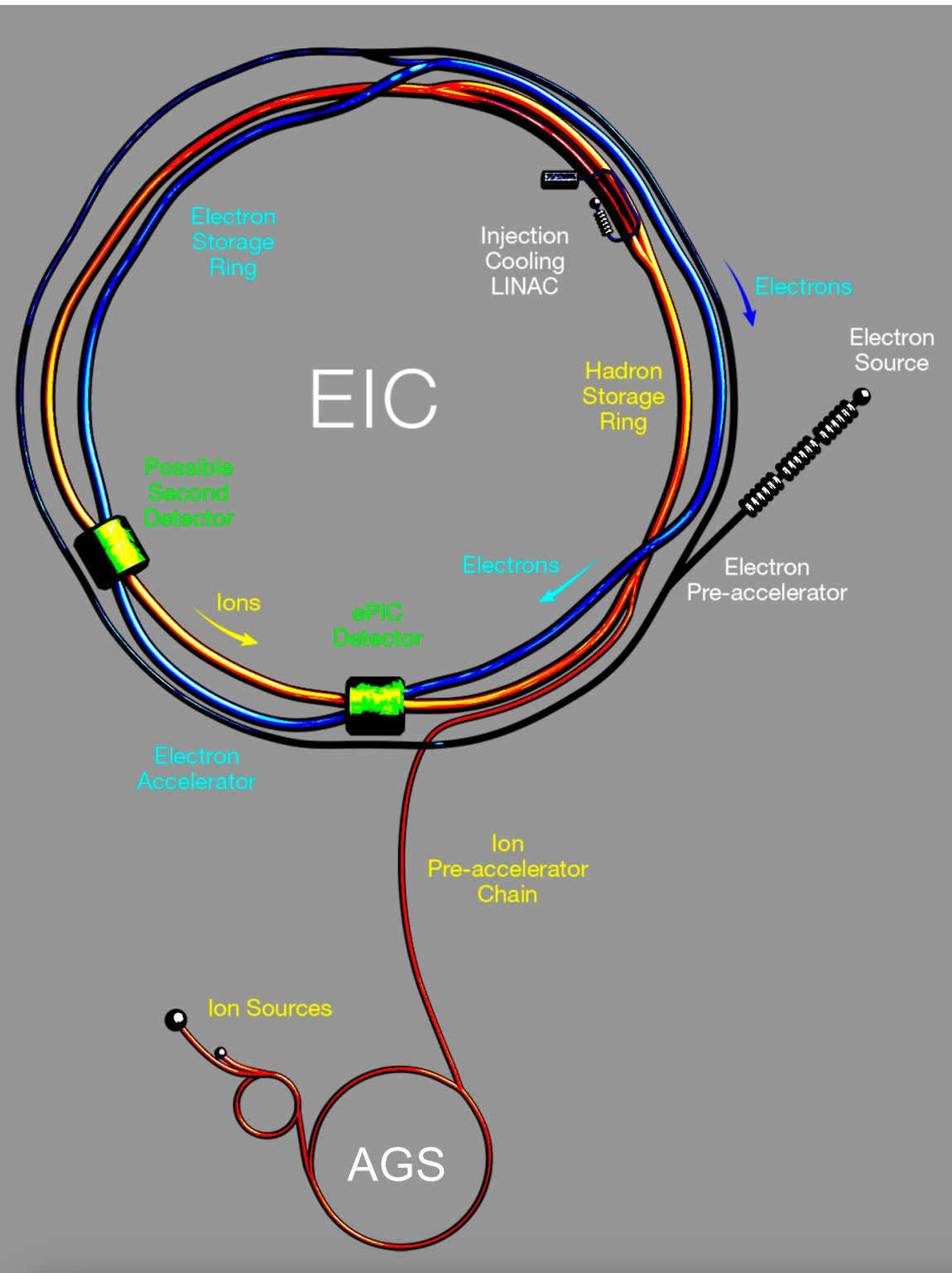


EM nuclear response and neutron stars



CB, Zelevinsky, Nature 532, 448 (2016)
Duer et al., Nature 606, 678 (2022)

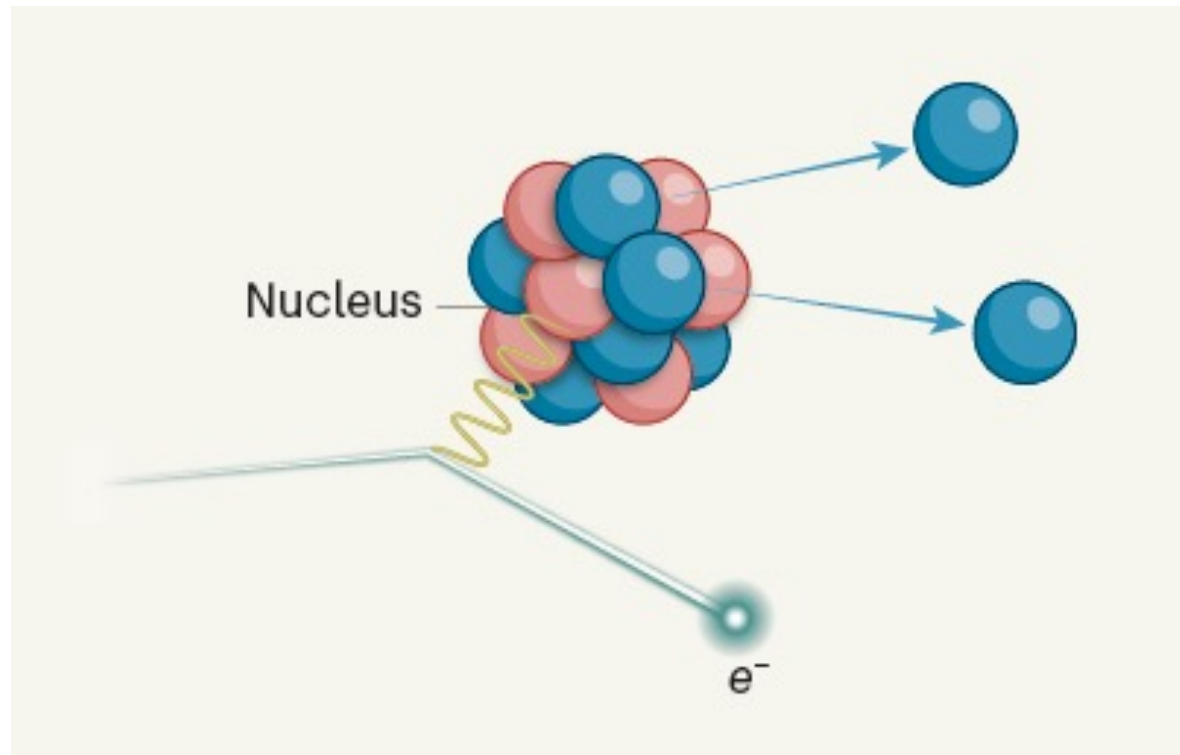
Electron Ion Collider (EIC)



- High Luminosity: $L = 10^{33} - 10^{34} \text{cm}^{-2}\text{sec}^{-1}$, $10 - 100 \text{fb}^{-1}/\text{year}$
- Polarized beams: e, p, d, ^3He
- Large Center of Mass Energy Range:
 $E_{\text{cm}} = 29 - 140 \text{ GeV}$
- Large Ion Species Range: protons – Uranium

- **How does the mass of the nucleon arise?**
The Higgs mechanism accounts for only $\sim 1\%$ of the mass of the proton.
- **How does the spin of the nucleon arise?**
The spin of the quarks accounts for only one-third of the spin of the proton.
- **What are the emergent properties of dense system of gluons?**
The gluon saturation describes a new state of matter at extreme high density.

Zero degree physics at the EIC



No zero degree detector has been commissioned for the EIC, yet.

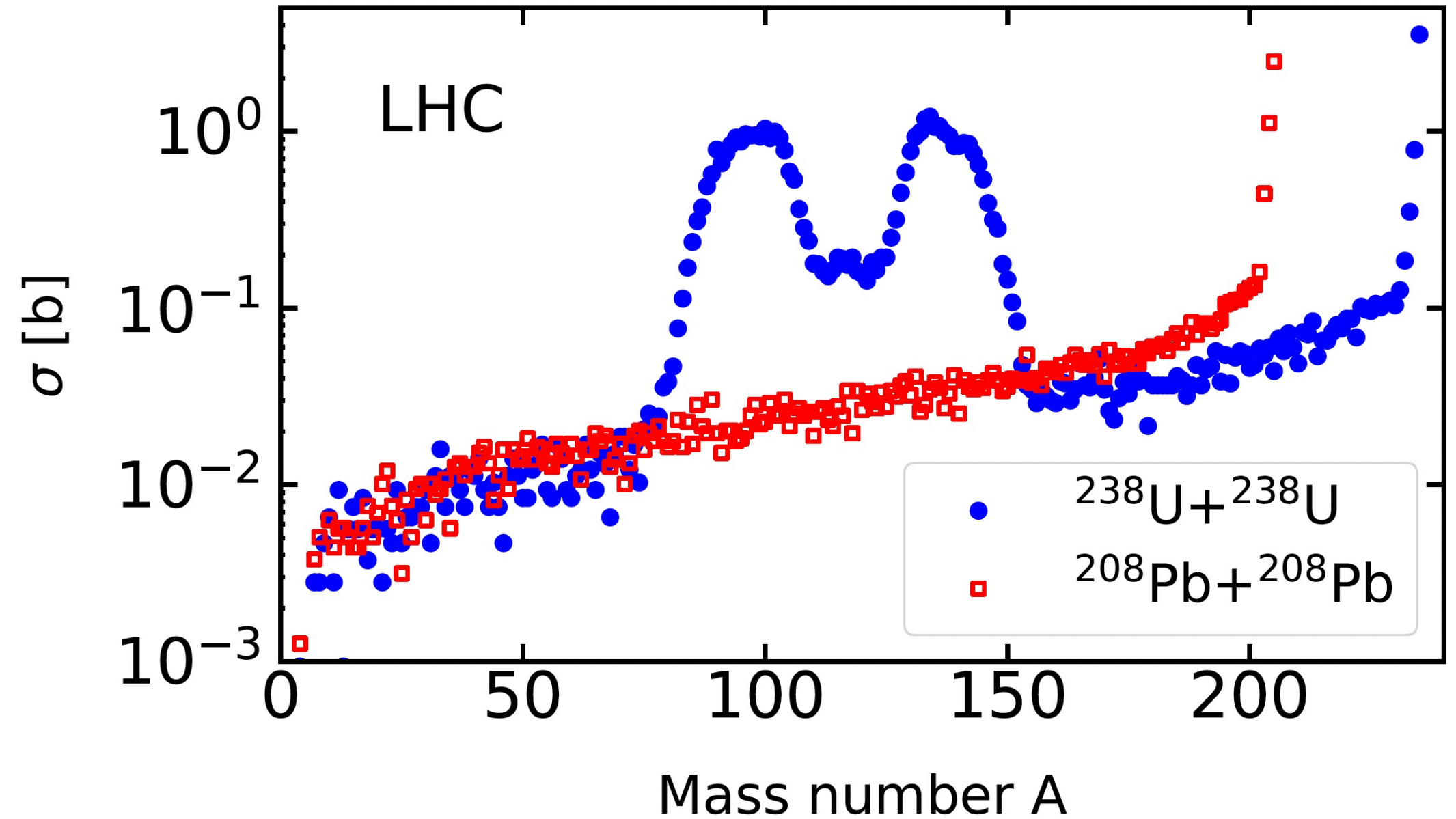
- Fragments move at high energies (> 100 GeV/nucleon). Time dilation allows detection for lifetimes > 1 ns.
- De-excitation photons are boosted to energies much larger than background photons

➔ Possible study of low energy physics of the isotopes.

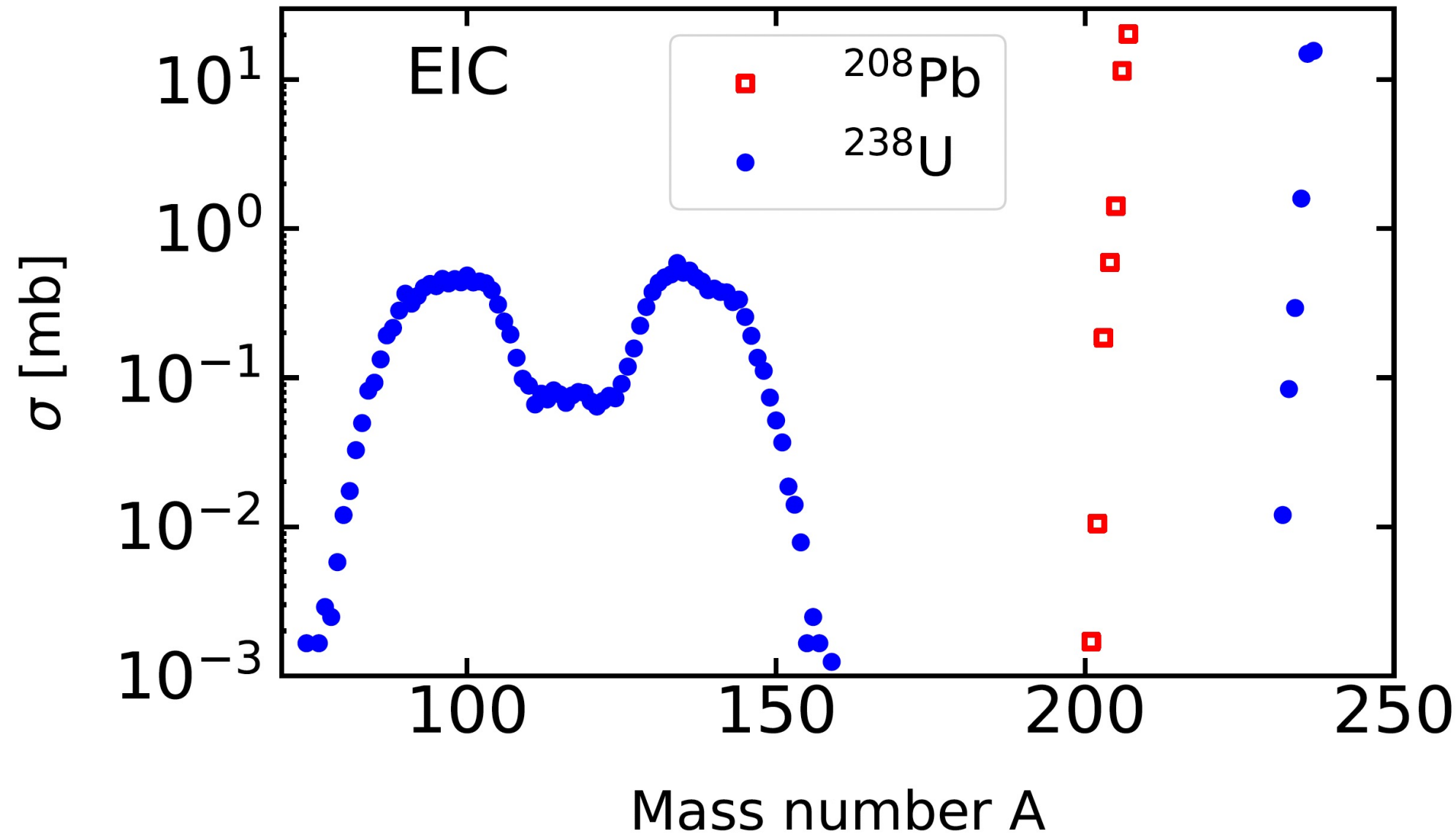
Nuclear fragmentation at the LHC

Excitation of GRs
+
evaporation

CB, Kucuk, Navarra,
arXiv:2408.10157 (2024)



Nuclear fragmentation at the EIC



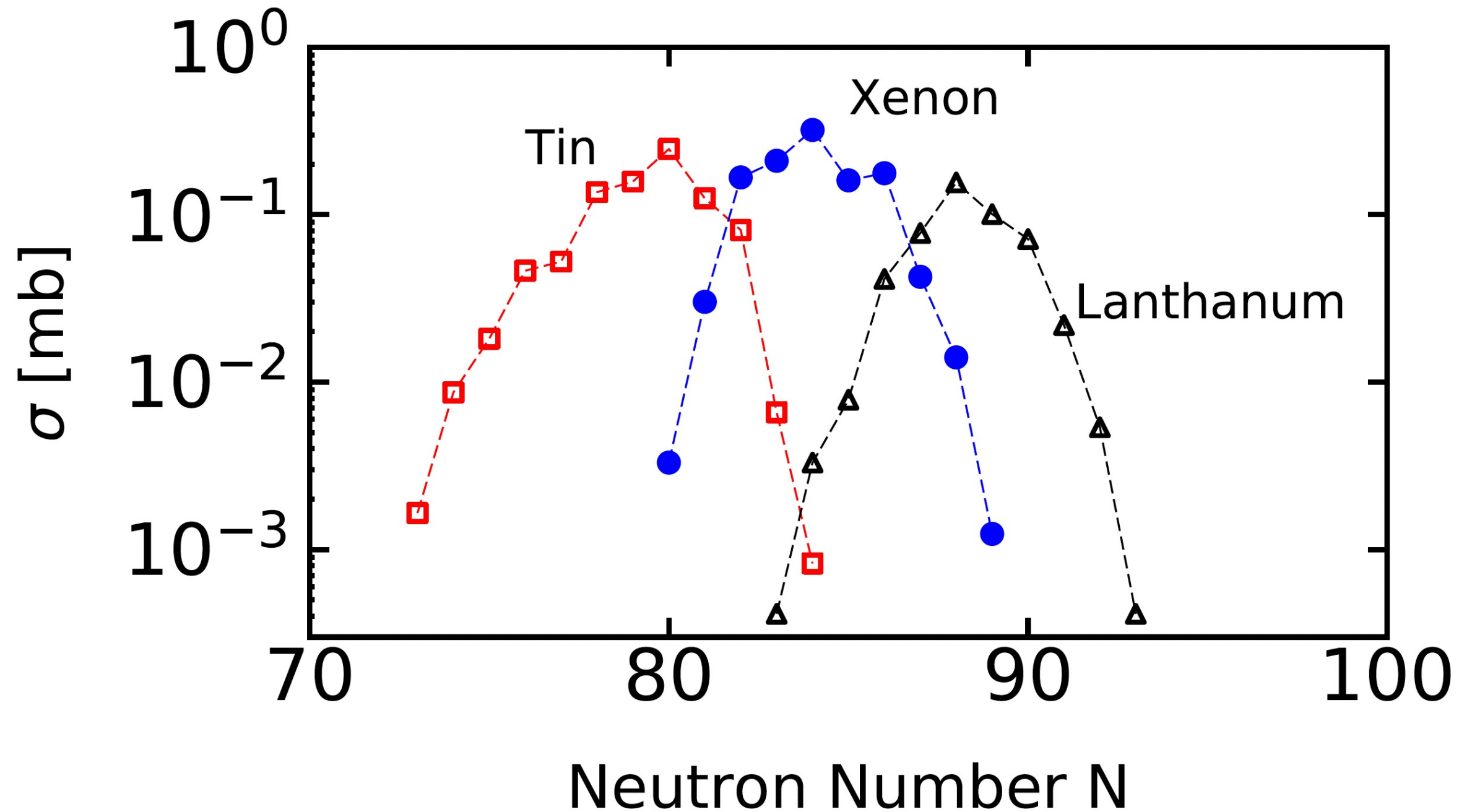
$$\frac{d\sigma}{d\omega dQ^2} = \sum_{\lambda} \frac{dN_{\lambda}}{d\omega dQ^2} \sigma_{\gamma}^{\lambda}(\omega)$$

$$\sigma_x^{GR}(\omega) = b_x(\omega) \sum_{GR} \sigma_{\gamma}^{GR}(\omega)$$

$$b_x(\omega) = \frac{\Gamma_x(\omega)}{\Gamma_{tot}(\omega)}$$

$x = \text{fragment}$

Nuclear fragmentation at the EIC



Nuclear fragmentation at the EIC

Cross sections	LHC	LHC	EIC	EIC
	Pb + Pb [b]	U + U [b]	e-Pb [mb]	e-U [mb]
σ_{-1n}	33.93	33.20	20.24	15.58
σ_{-2n}	18.89	30.59	11.45	14.88
σ_{-3n}	2.546	3.537	1.416	1.591
σ_{-4n}	1.091	0.784	0.5933	0.2934
$\sigma_{fission}$	0	18.24	0	8.867
σ_{total}	55.74	85.48	33.90	41.32
Fission b.r.	0%	19.54%	0%	21.45%

Summary

Physics at EIC

- Origin of nucleon mass and spin
- 3D structure of the nucleon and nucleus
- Gluon saturation
- Hadronization

Physics at zero degree of EIC

- EIC is a cleaner probe
- EIC has the potential to produce new nuclear isotopes
- Fragments can be detected and identified using particle ID, ZDC, and other yet to be proposed detectors
- Level structure of produced isotopes would be assessed through the detection of the de-excitation photons

Hauser-Feshbach formula & resonances

$$\langle \sigma \rangle = 2\pi^2 \omega \frac{\Gamma_a \Gamma_b}{\Gamma D} = \pi D^2 \omega \frac{T_a T_b}{T_{tot}}$$

where

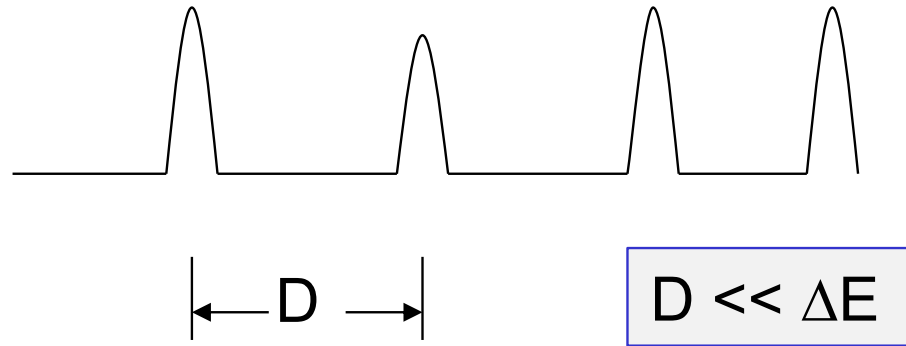
$$T_a = 2\pi \left\langle \frac{\Gamma_a}{D} \right\rangle$$

- T_a = dimensionless number between 0 and 1 = probability that a particle of type a crosses the nuclear surface (with angular momentum l)
- T_a is related to the “*strength function*”, $\langle \Gamma/D \rangle$, describing how width is distributed smoothly in the nucleus.
- These functions still contain the barrier penetration functions.
- This yields the Hauser-Feshbach formula for estimating cross sections where the density of resonances is high.

$$\bar{\sigma}_{ab} = \frac{\pi/k^2}{(2J_a + 1)(2J_b + 1)} \sum_{J^\pi} (2J^\pi + 1) \frac{T_a^{l,s}(J^\pi, E) T_b^{l,s}(J^\pi, E)}{T_{tot}(J^\pi, E)}$$

Hauser-Feshbach formula & resonances

Assume $N (\gg 1)$ equally spaced identical resonances in an energy interval ΔE



Define average cross section:

$$\langle \sigma \rangle = \frac{\int_E^{E+\Delta E} \sigma(E) dE}{\Delta E}$$

$$\langle \sigma \rangle = \frac{1}{\Delta E} \int_E^{E+\Delta E} \frac{\Gamma_a \Gamma_b dE}{(E - E_r)^2 + \Gamma^2/4} = \frac{\Gamma_a \Gamma_b}{\Delta E} \int_0^\infty \frac{dE}{(E - E_r)^2 + \Gamma^2/4}$$

$$\int_0^\infty \frac{dE}{(E - E_r)^2 + \Gamma^2/4} = \frac{2\pi}{\Gamma}$$

$$\frac{N}{\Delta E} = \frac{1}{D}$$

and normalizing over the average distance D :

$$\frac{1}{\Delta E} = \frac{1}{D}$$