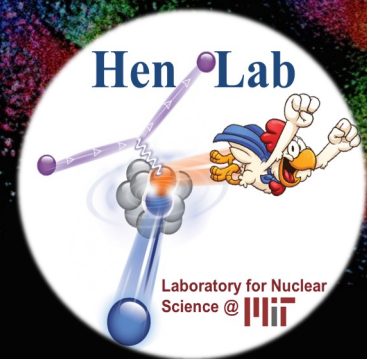
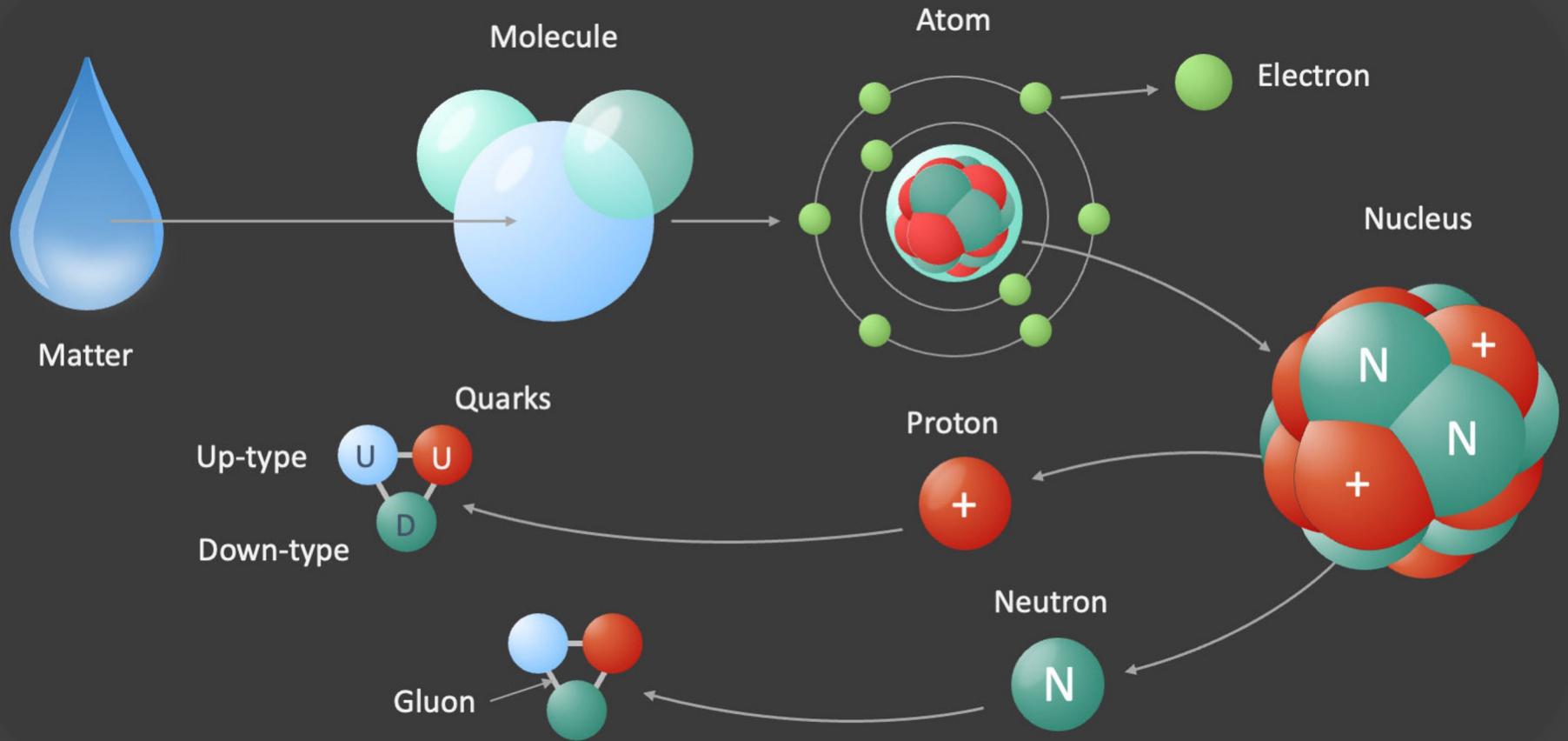


# EIC Physics: Experimental Perspective (1)

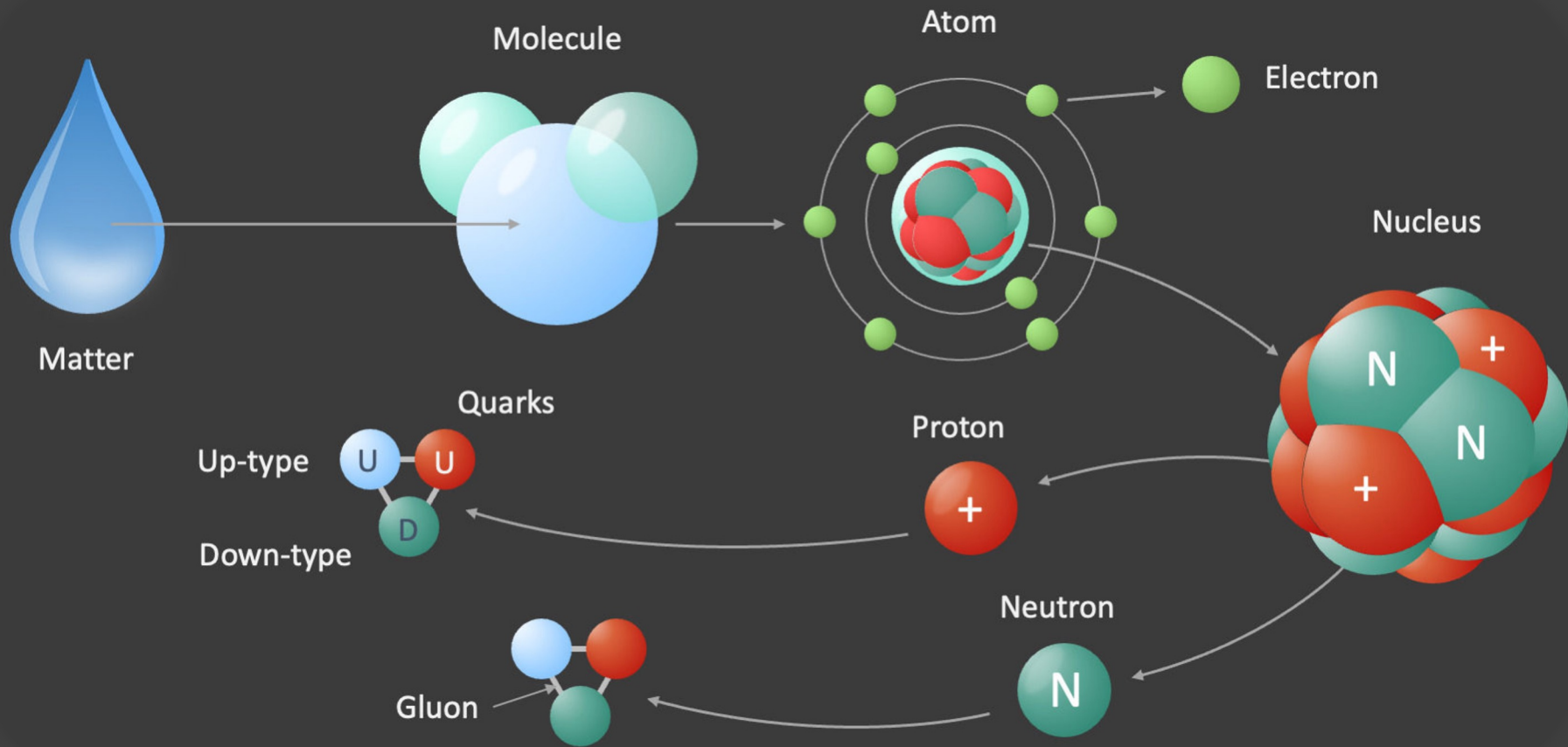
Or Hen  
(MIT)



# Fundamental Structure of Matter



# Fundamental Structure of Matter *constituents*



Discovering the constituents of matter is often viewed as telling us about its structure

However, the emergence of structure is a complex process;

Its understanding goes beyond knowing its constituents and their interactions

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However, the emergence of structure is a complex process;

Its understanding goes beyond knowing its constituents and their interactions

# Structure Probes Lead to new Frontiers

# Dynamical System

# Fundamental Knowns

# Unknowns

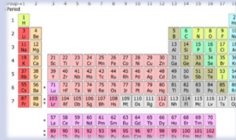
# Breakthrough Structure Probes

# New Sciences, New Frontiers

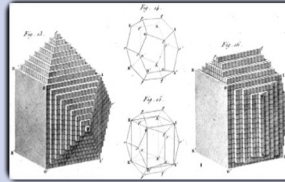
Solids



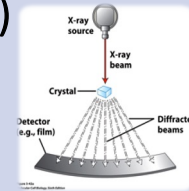
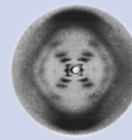
Electromagnetism and Atoms



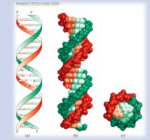
Structure



X-ray Diffraction (~1920)



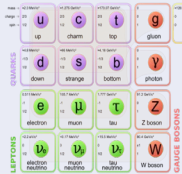
Solid state physics  
Molecular biology



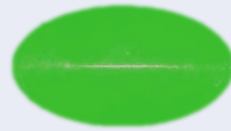
Universe



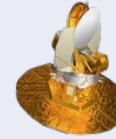
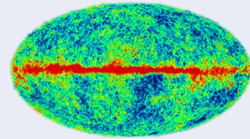
General Relativity  
Standard Model



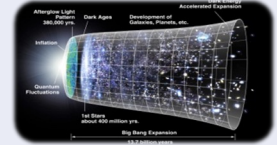
Quantum Gravity,  
Dark matter, Dark energy. Structure



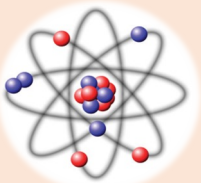
Large Scale Surveys  
CMB Probes (~2000)



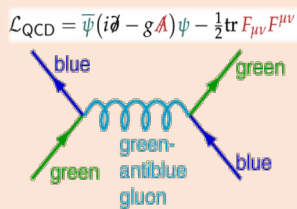
Precision  
Cosmology



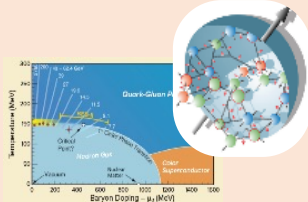
Nucleons and Nuclei



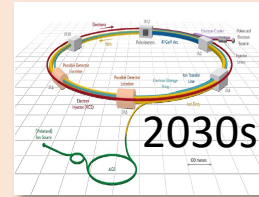
Perturbative QCD  
Quarks and Gluons



Non-perturbative QCD. Structure



DIS (1970s) →  
Electron-Ion



Structure &  
Dynamics in QCD

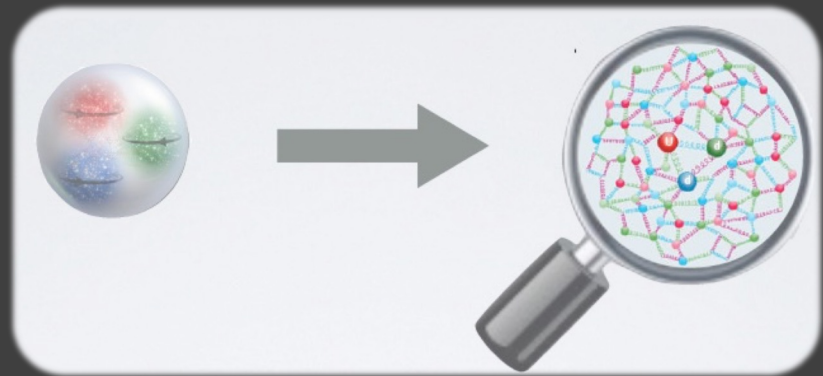




# Special Challenge as QCD Matter is Unique

Interactions & structures inextricably mixed

Observed **properties** such as mass & spin,  
*emerge* out of this complex system



To understand QCD matter we need  
to Image it

# First Elastic scattering show protons are not point particles



The Proton  
(early 1900s)

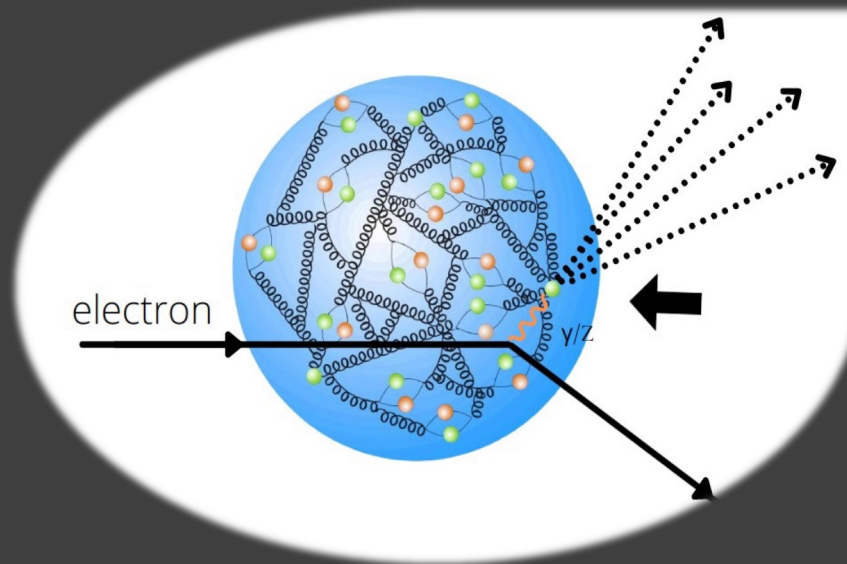


1961

# Deep Inelastic Scattering reveal point like constituents!

$$\underline{e + p \rightarrow e' + X}$$

Golden process, utilizing unmatched precision of electromagnetic interactions



$Q^2$  – resolution power (virtuality of the photon)

$s$  – center-of-mass energy squared

$x$  – the fraction of the nucleon's momentum carried by the struck quark

$y$  – inelasticity

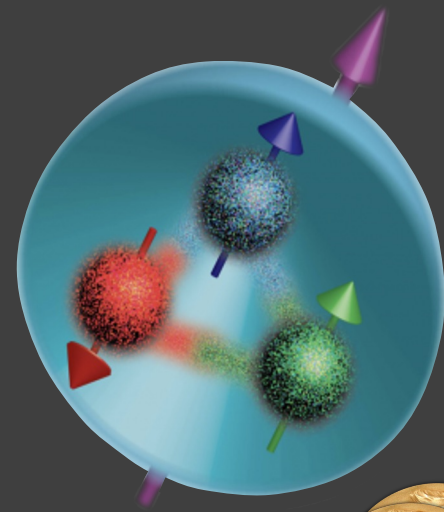
# → Imaging the subatomic world was key for gaining new understanding

The Proton  
(early 1900s)



1961

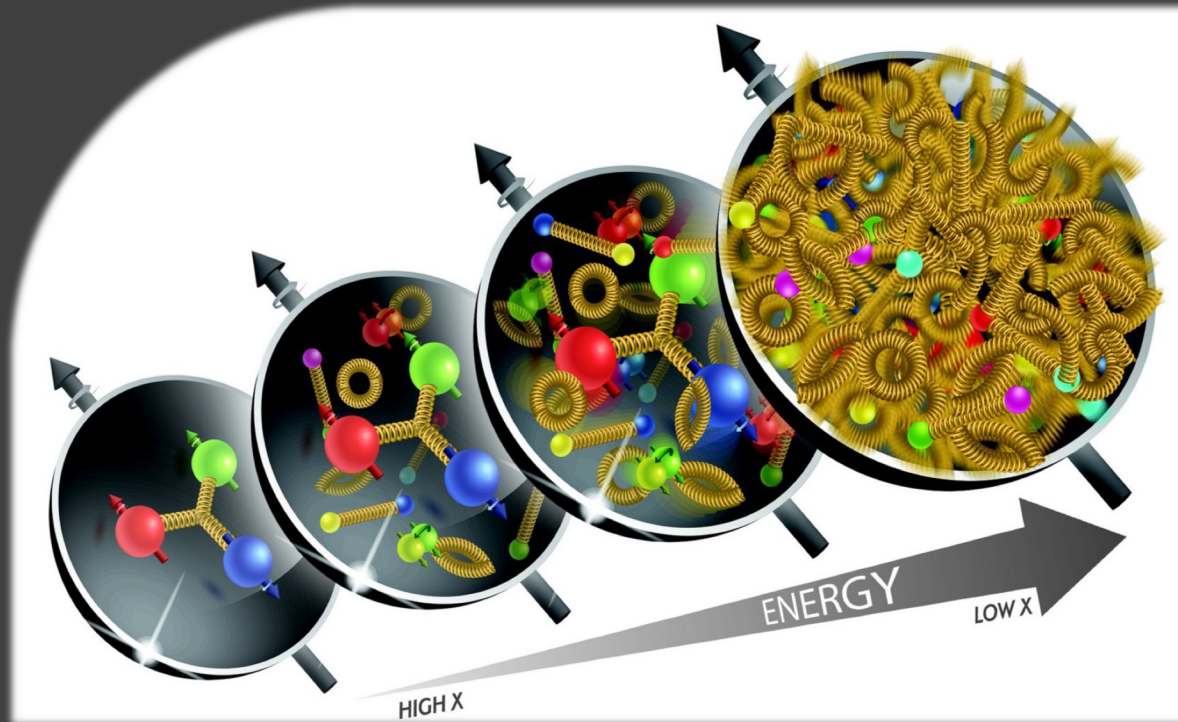
The Proton  
(1970s)



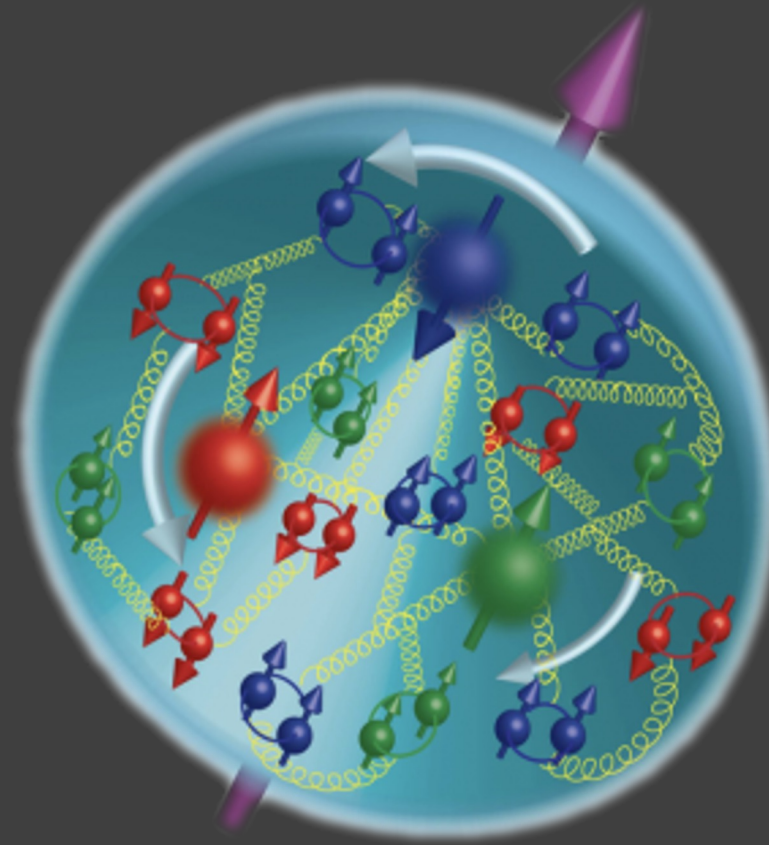
1990, 2004

QCD!

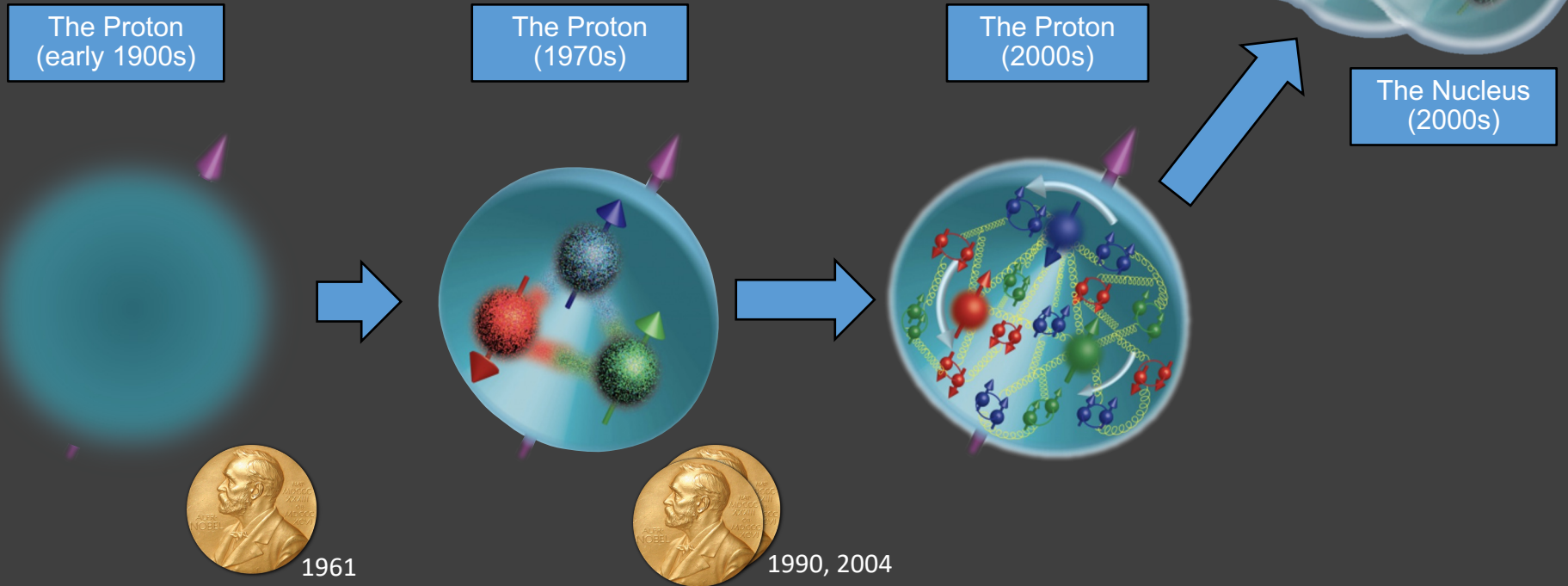
Improved measurements, incl. polarization observables, led to new insights!



“Today’s” proton is one of the most complex QM systems we know

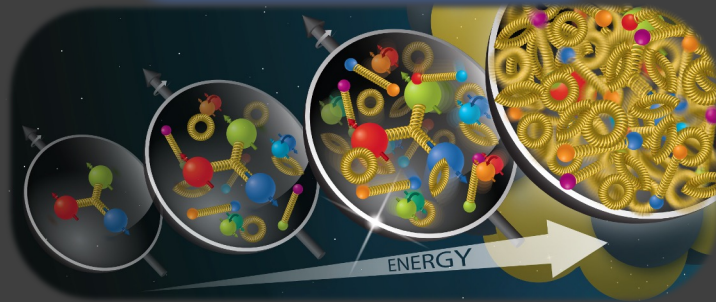


# The Electron-Ion Collider: Imaging Nucleons and Nuclei





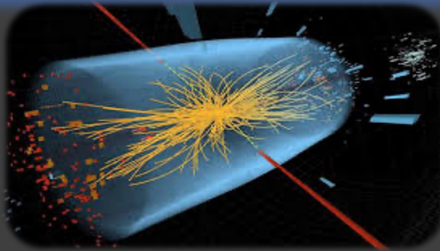
Dense Gluons



Nuclei

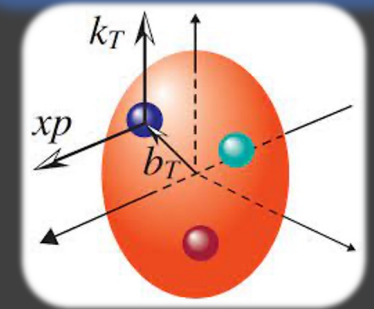


Standard Model

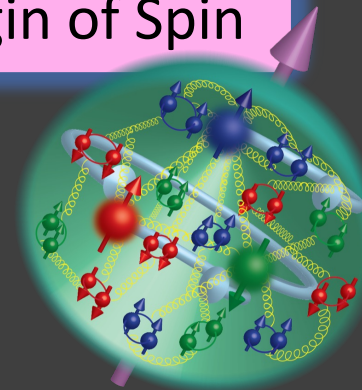


# QCD Science

Femtography



Origin of Spin



Origin of  
Mass



# Back to basics: Electron Scattering

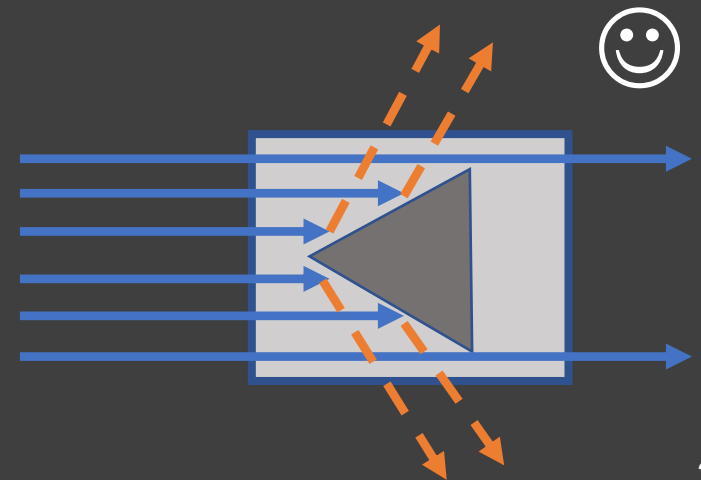
# Electron Scattering: Nuclear Microscope

Goal: Study the internal structure (and dynamics) of complex objects

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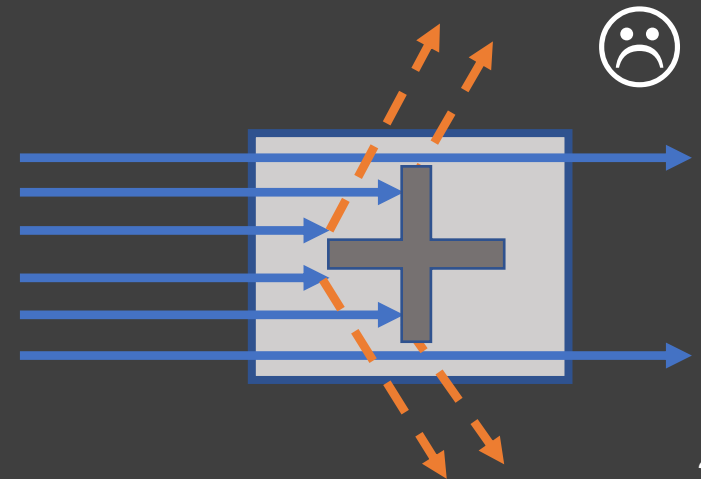
Means: using high energy lepton scattering



# Electron Scattering: Nuclear Microscope

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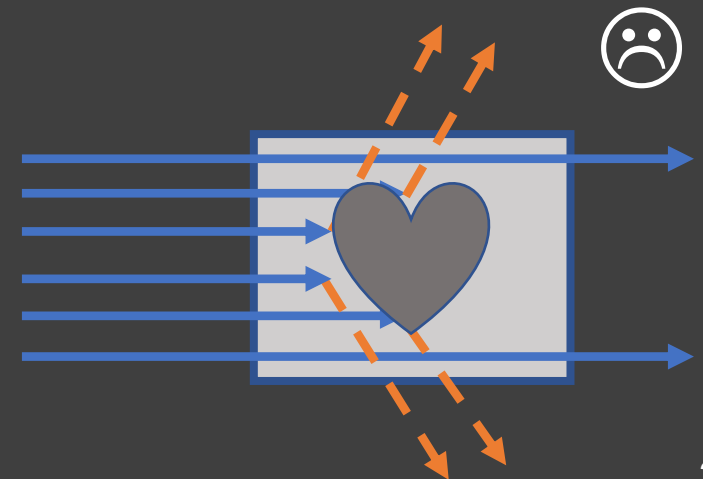
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Goal: Study the internal structure (and dynamics) of complex objects

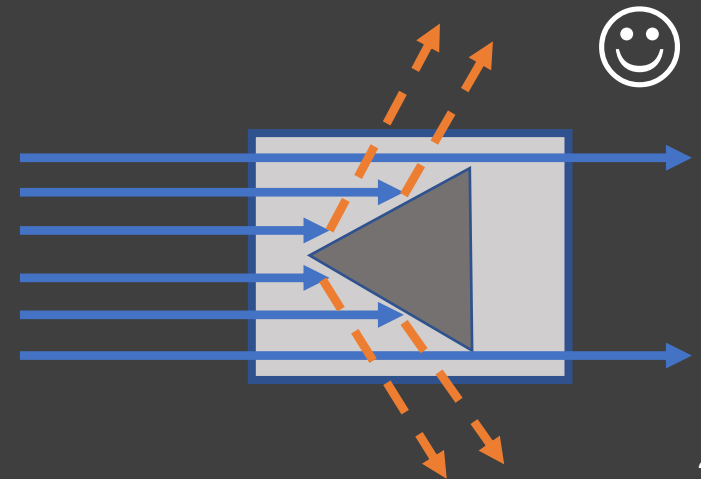
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Goal: Study the internal structure (and dynamics) of complex objects

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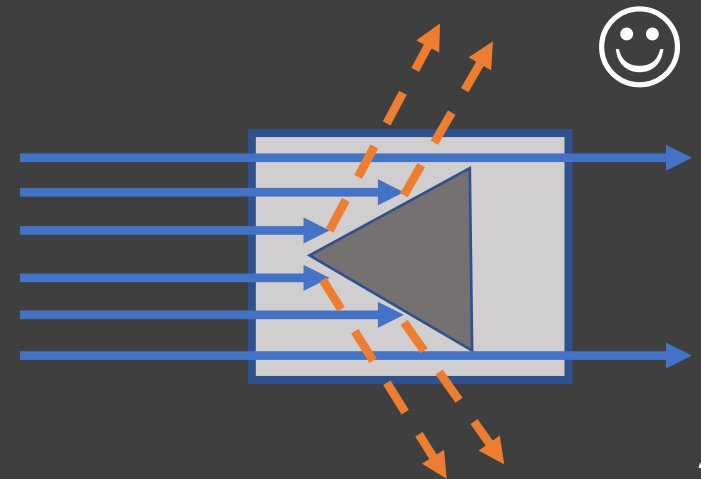
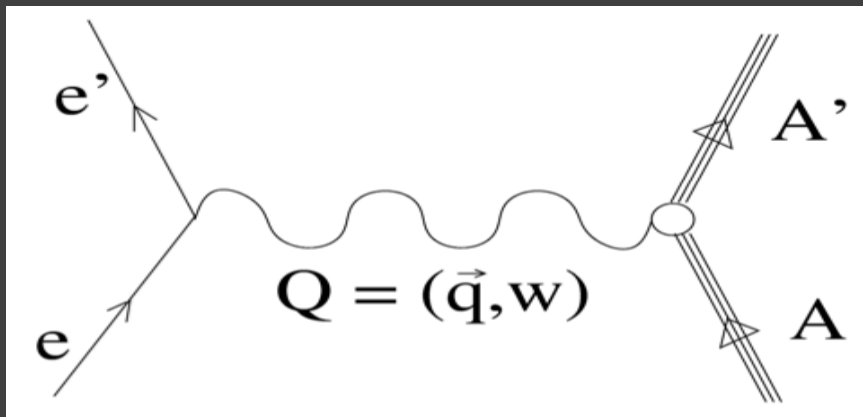
# Electron Scattering: Nuclear Microscope

Goal: Study the internal structure (and dynamics) of complex objects

Means: using high energy lepton scattering

Reaction determined by two variables:

- $Q^2 = -q^2$  Interaction-Scale
- $x_B = Q^2/(2m_p v)$  Dynamics



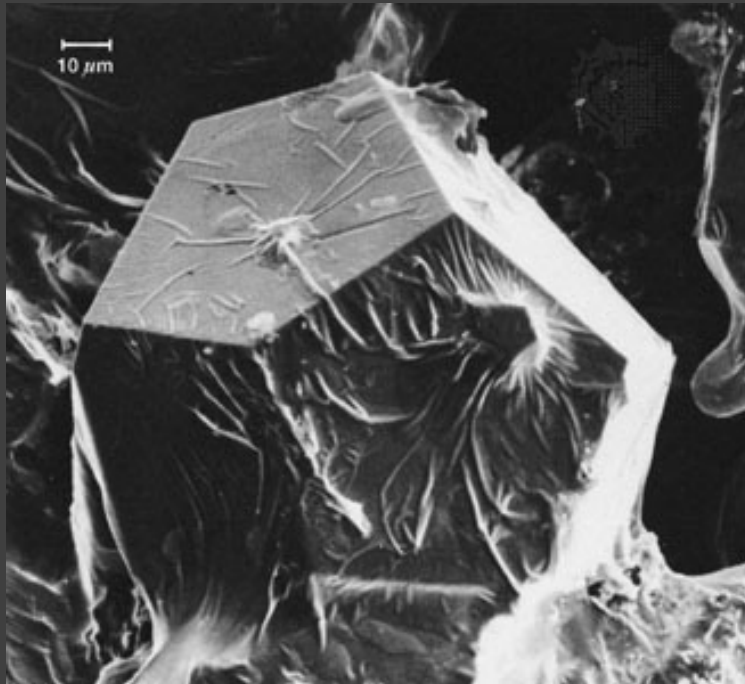


# Electron Scattering: Nuclear Microscope

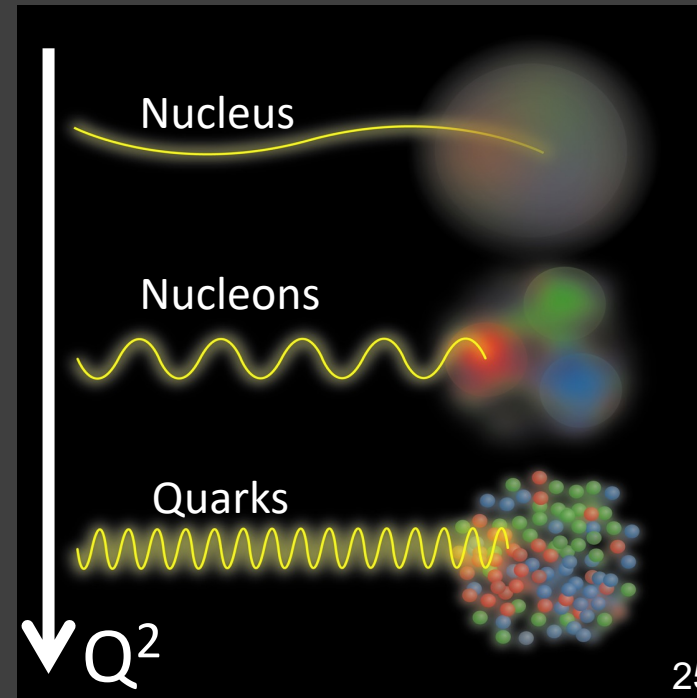
Goal: Study the internal structure (and dynamics) of complex objects

Means: using high energy lepton scattering

100s eV – 100s keV:  
Material structure



100s MeV – 10s GeV:  
Nuclear structure

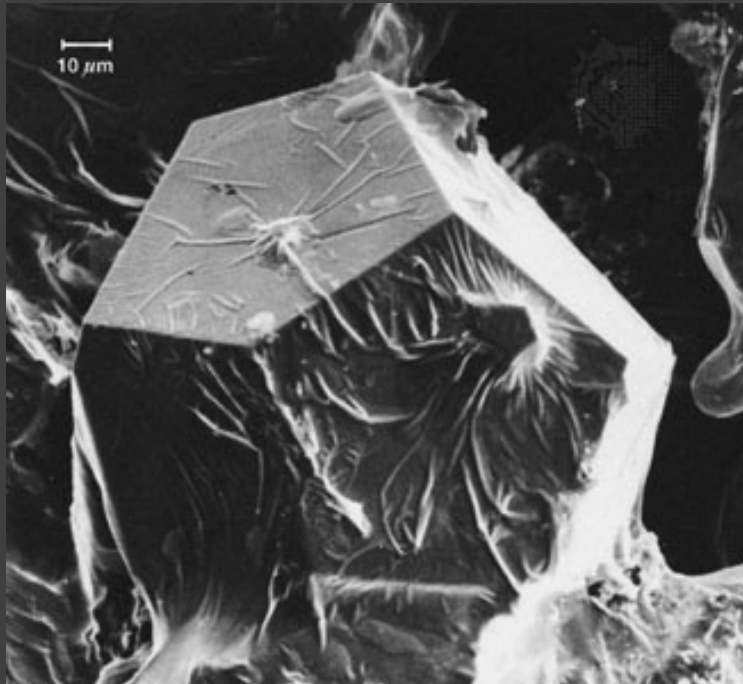


# Electron Scattering: Nuclear Microscope

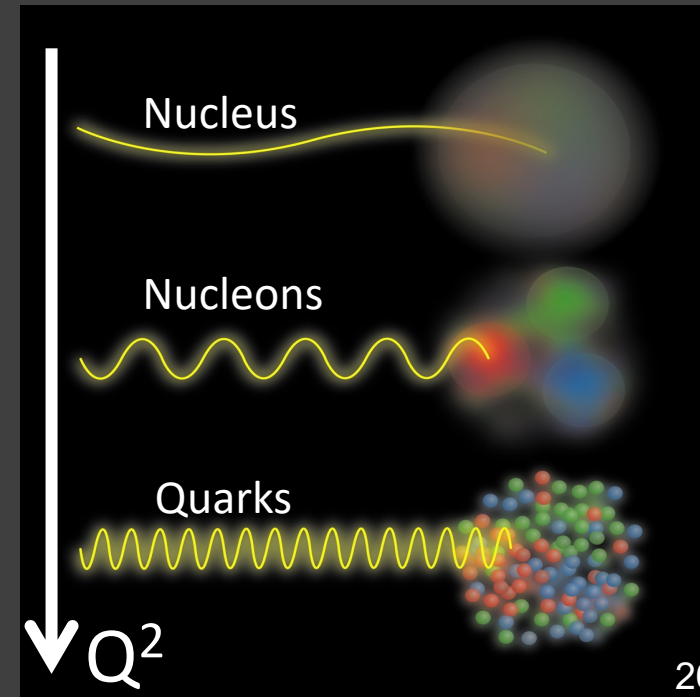
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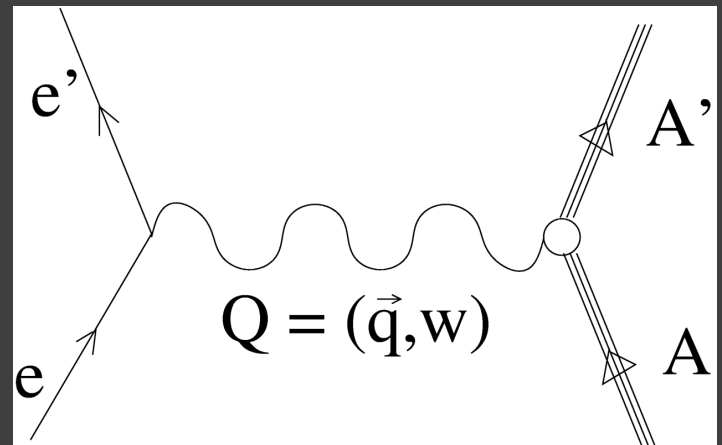
Energy  
=  
Resolution !

# Why use electrons?

- Probe structure understood (point particles)
- Electromagnetic interaction understood (QED)
- Interaction is weak ( $\alpha = 1/137$ )
  - Theory works!
    - First Born Approx / one photon exchange
  - Probe interacts only once
  - Study the entire nuclear volume

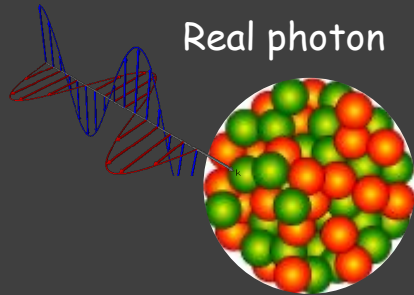
BUT:

- Cross sections are small
- Electrons radiate



# It's all photons!

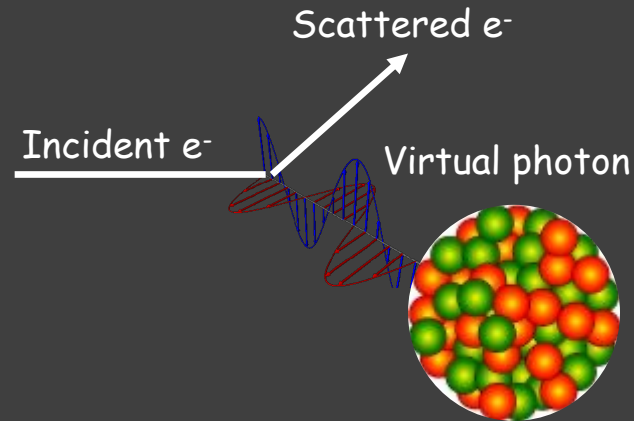
- An electron interacts with a nucleus by exchanging a single virtual photon



Real photon:

Momentum  $q = \text{energy } v$

Mass =  $Q^2 = |\mathbf{q}|^2 - v^2 = 0$



Virtual photon:

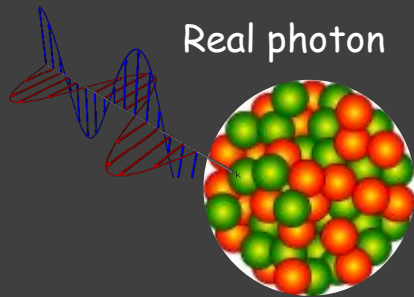
Momentum  $q > \text{energy } v$

$Q^2 = -q_\mu q^\mu = |\mathbf{q}|^2 - v^2 > 0$

Virtual photon "has mass"!

# It's all photons!

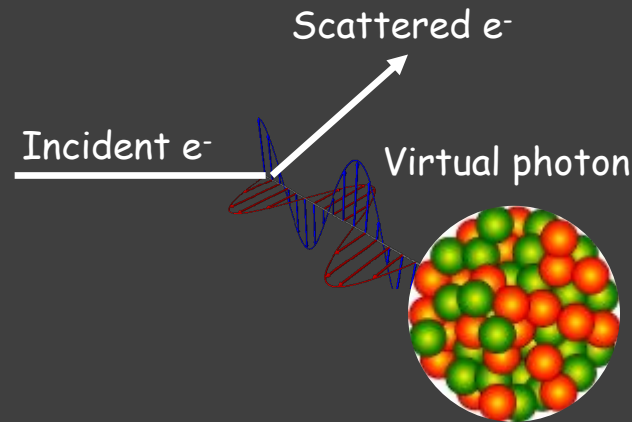
- An electron interacts with a nucleus by exchanging a single virtual photon



Real photon:

Momentum  $q = \text{energy } \nu$

Mass =  $Q^2 = |\mathbf{q}|^2 - \nu^2 = 0$



Virtual photon:

Momentum  $q > \text{energy } \nu$

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Virtual photon "has mass"!

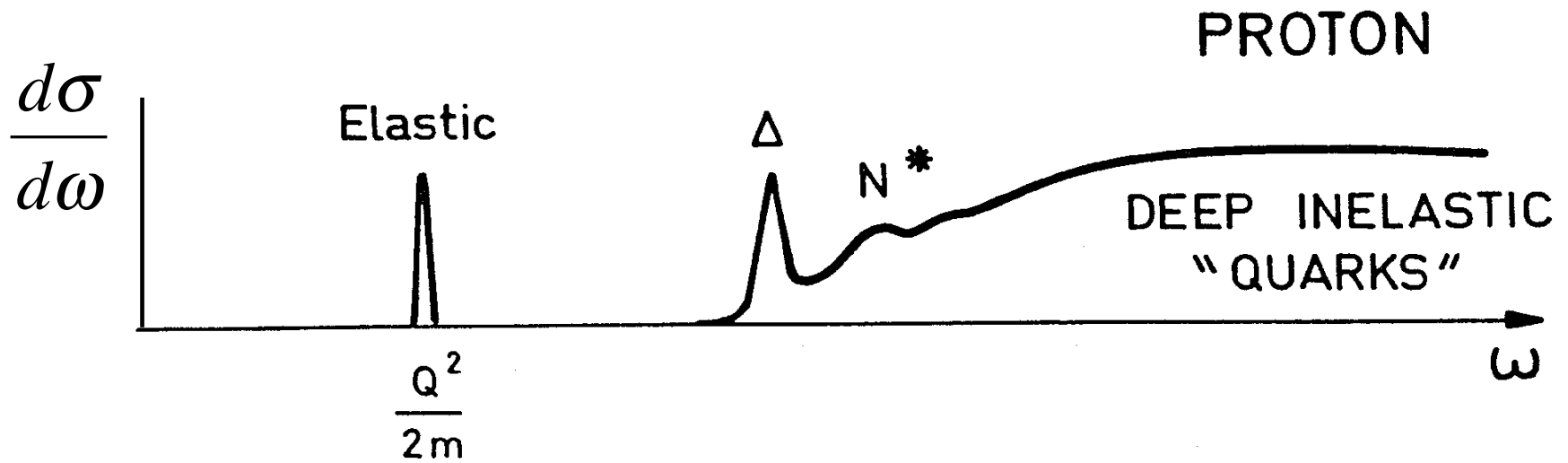
( $\nu$  and  $\omega$  are both used for energy transfer)

# Electron beams need ...

- High **energy**
  - $q \sim 2E \sin(\theta_e/2)$
  - $\Delta x < 0.2 \text{ fm} \rightarrow q > 1 \text{ GeV}/c$
- High **duty cycle** (no large beam current variation)
  - Reduces accidental coincidences for multiparticle detection
  - Reduces detector rates, multiple hits, ...
- High **intensity** (since cross sections are small)
- High **resolution** to separate nuclear levels
- High **polarization** (for spin asymmetry measurements)

# $(e, e')$ Kinematics

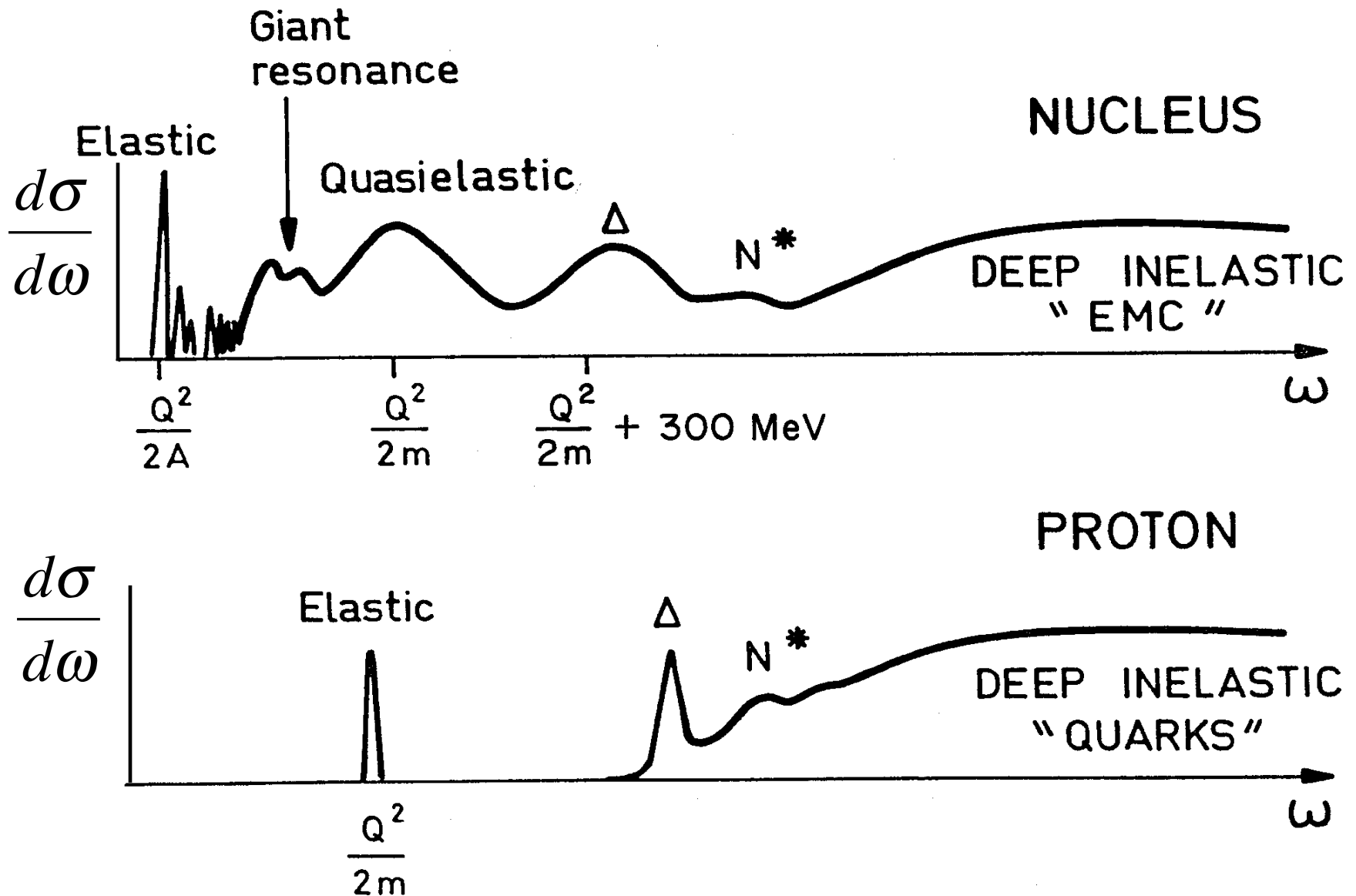
# (e,e'): Energy transfer defines physics



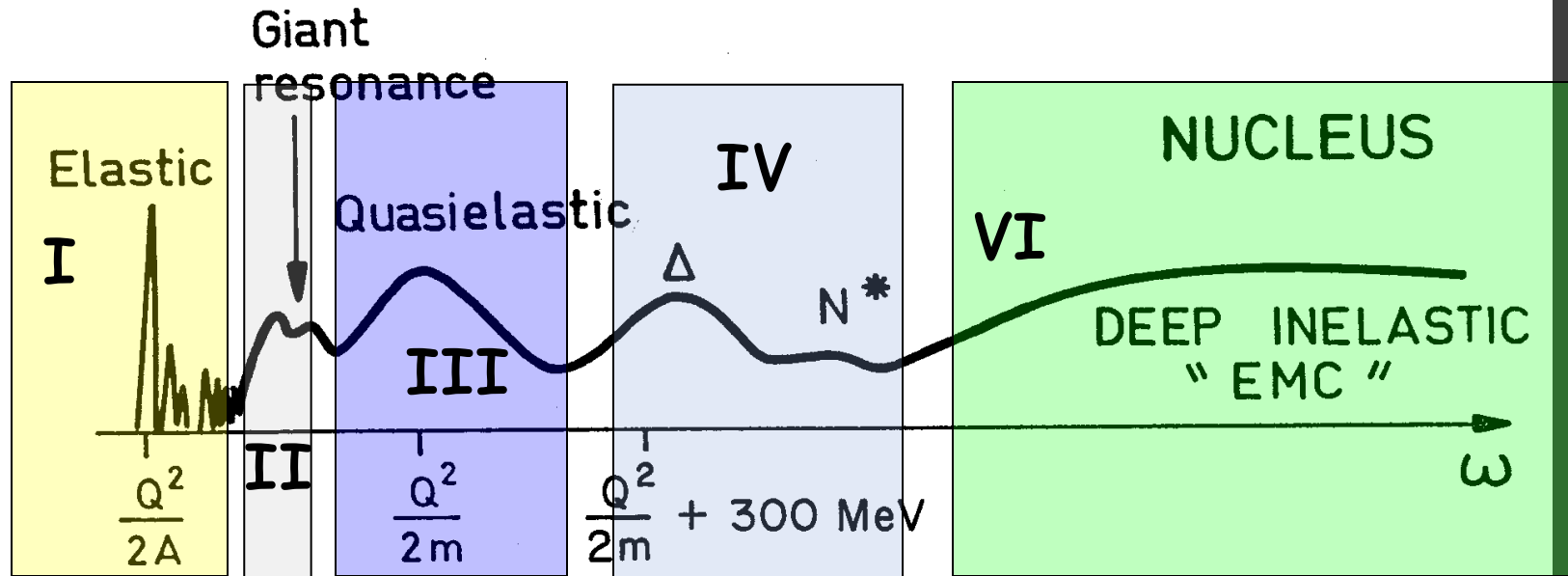
Generic Electron Scattering  
at fixed momentum transfer



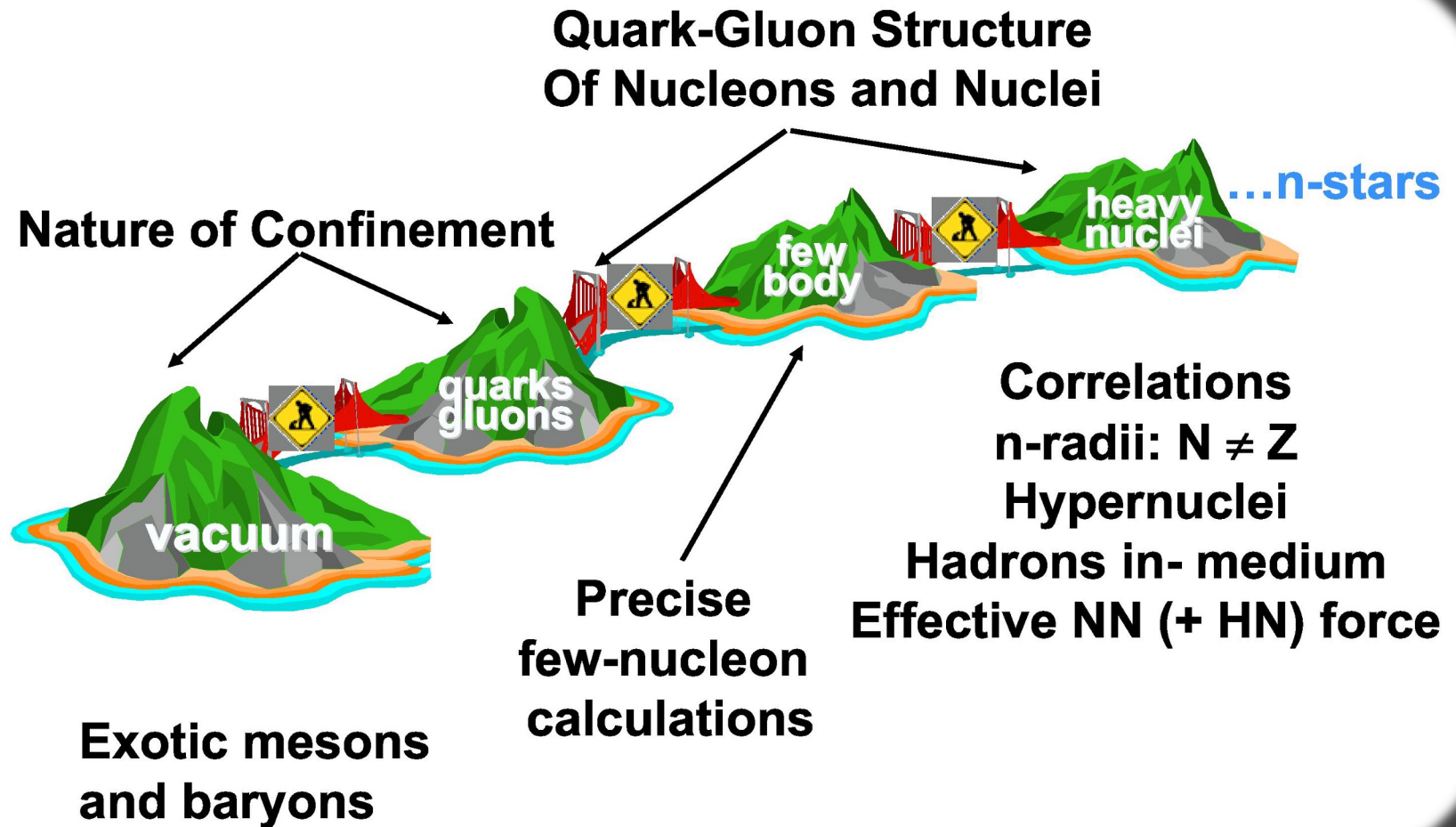
# (e,e'): Energy transfer defines physics



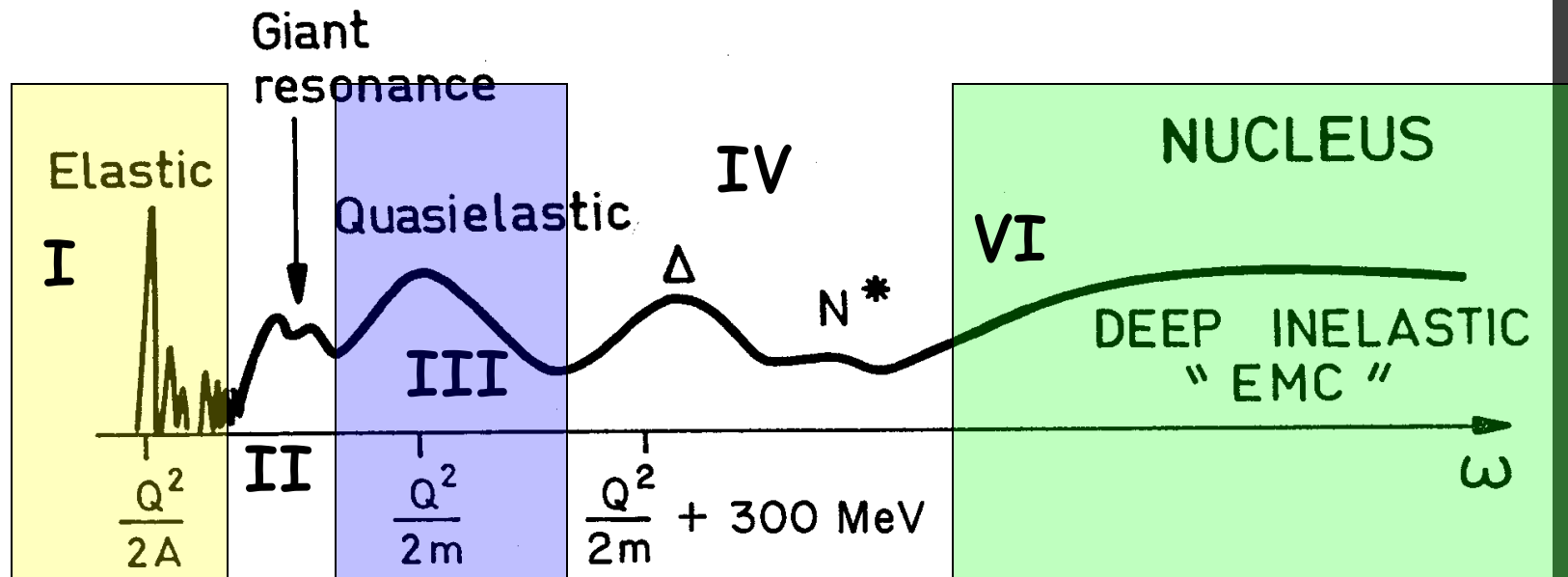
# Everything is interesting...

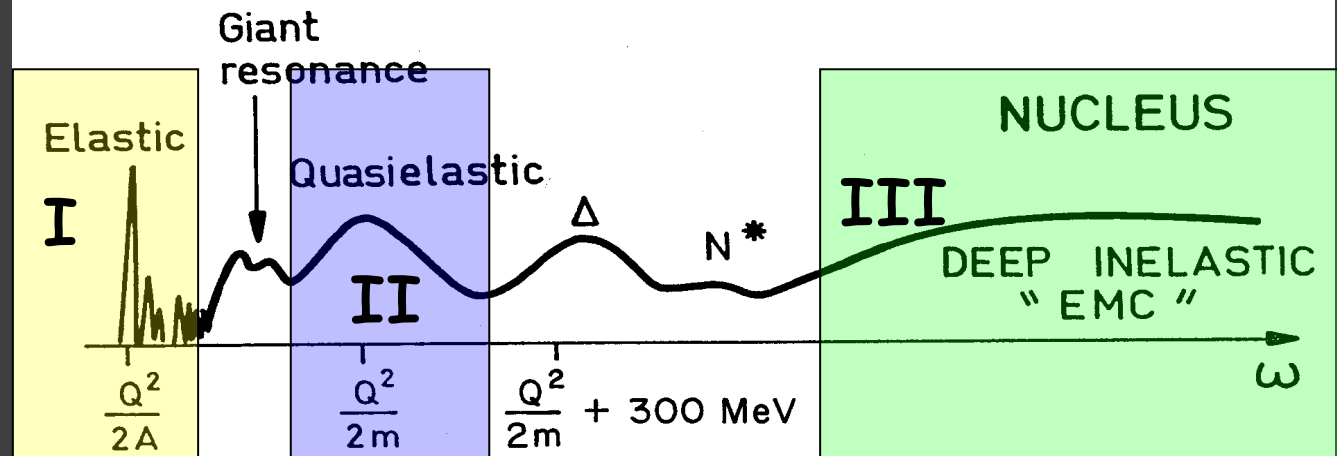


# Program central to all of nuclear science



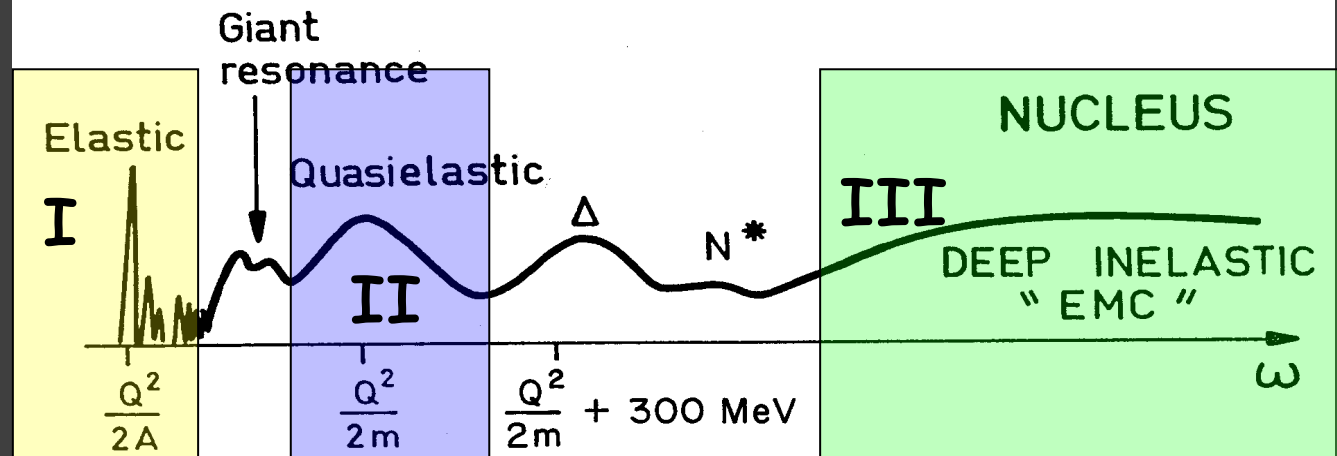
...But we will focus on 3 regions





## 1. Elastic

- structure of the nucleon / nucleus
  - Form factors, charge distributions, spin dependent FF

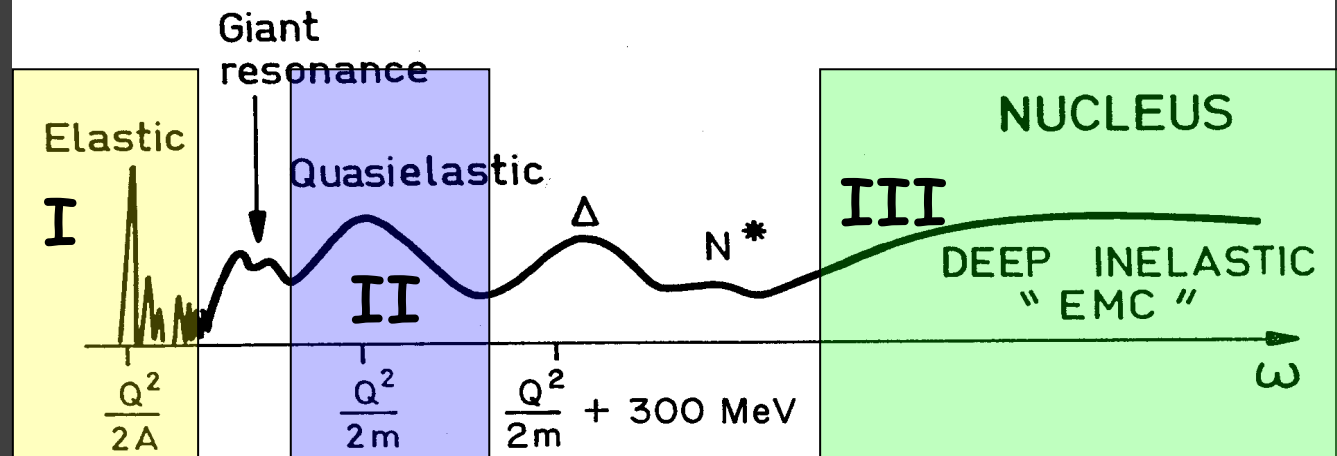


## 1. Elastic

- structure of the nucleon / nucleus
  - Form factors, charge distributions, spin dependent FF

## 2. Quasielastic (QE)

- Shell structure
  - Momentum distributions
  - Occupancies
- Short Range Correlated nucleon pairs
- Nuclear transparency and color transparency



## 1. Elastic

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  - Occupancies
- Short Range Correlated nucleon pairs
- Nuclear transparency and color transparency

## 3. Deep Inelastic Scattering (DIS)

- The EMC Effect and Nucleon modification
- Quark hadronization in nuclei

# Energy vs length

Select spatial resolution and excitation energy independently

- Photon energy  $\nu$  determines excitation energy
- Photon momentum  $q$  determines spatial resolution:

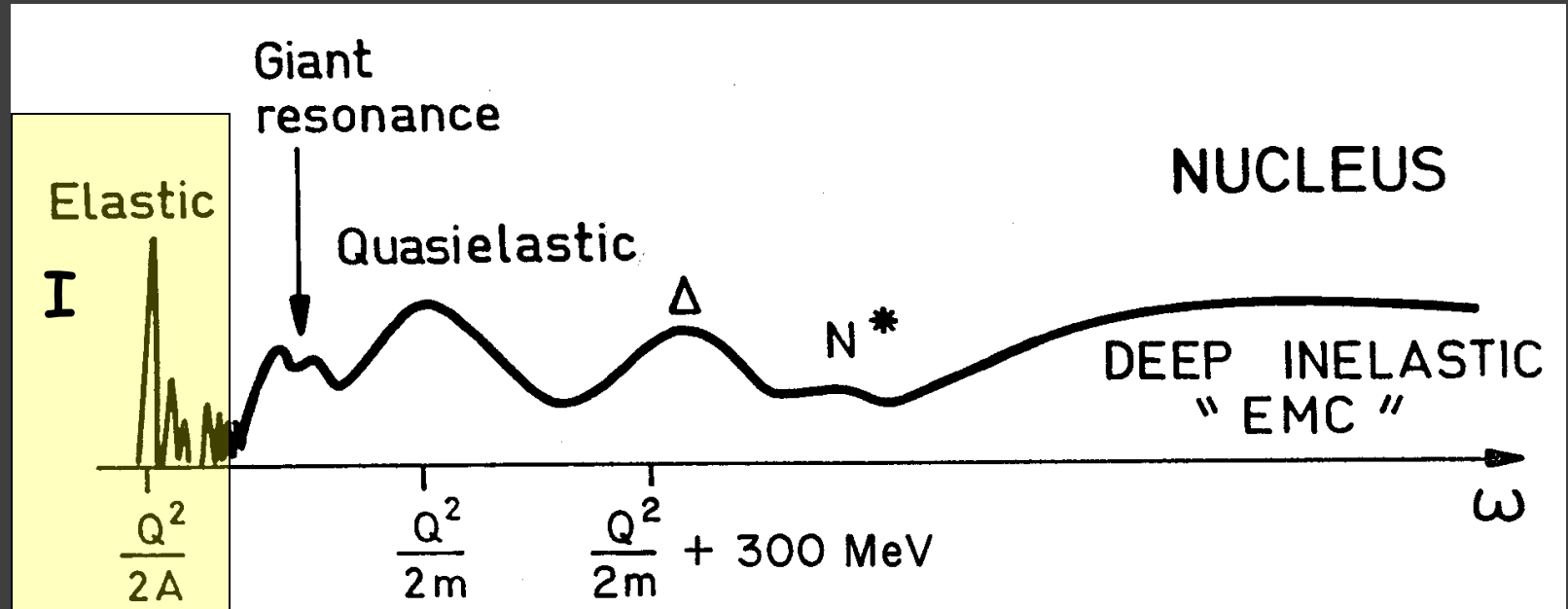
$$\lambda \approx \frac{\hbar}{q}$$

Three cases:

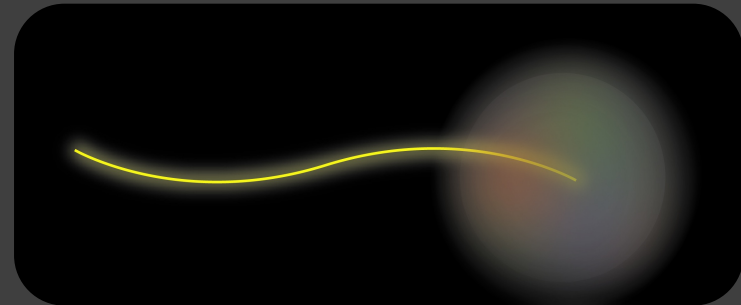
- Low  $q$ 
  - Photon wavelength  $\lambda$  larger than the nucleon size ( $R_p$ )
- Medium  $q$ :  $0.2 < q < 1$  GeV/c
  - $\lambda \sim R_p$
  - Nucleons resolvable
- High  $q$ :  $q > 1$  GeV/c
  - $\lambda < R_p$
  - Nucleon structure resolvable



# Quick Overview: Elastic



- Nuclear charge (proton) radius
- Nuclear Neutron radius
- Nucleon Form-Factors and charge densities

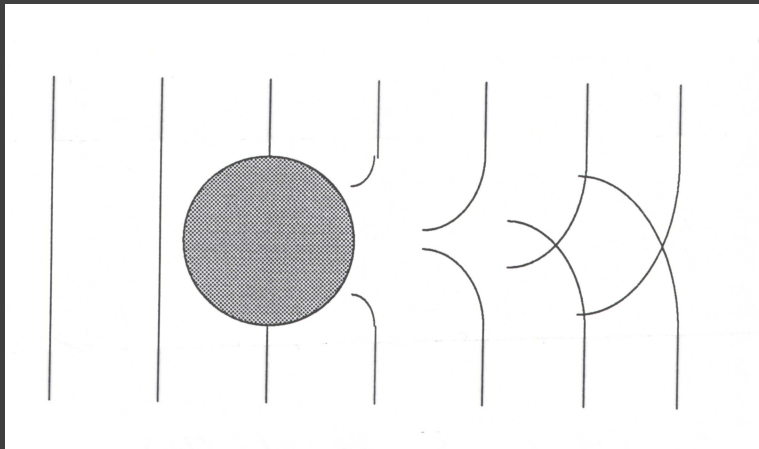


# Electrons as Waves

Scattering process is quantum mechanical

De broglie wavelength:

$$\lambda = \frac{h}{p}$$



Electron energy:

$$E_e \approx pc$$

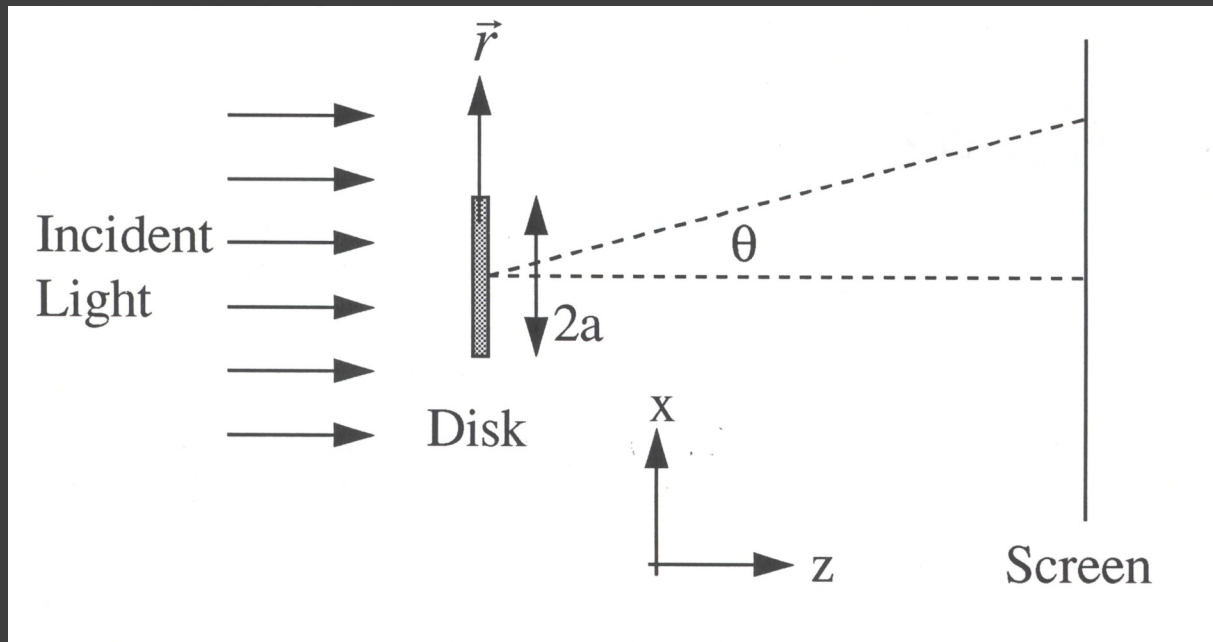
$$\hbar c = 197 \text{ MeV}\cdot\text{fm}$$

$\lambda$  resolving “scale”:

$$\lambda = \frac{2\pi(197 \text{ MeV}\cdot\text{fm})}{E_e}$$

Simple analogy for elastic electron scattering....

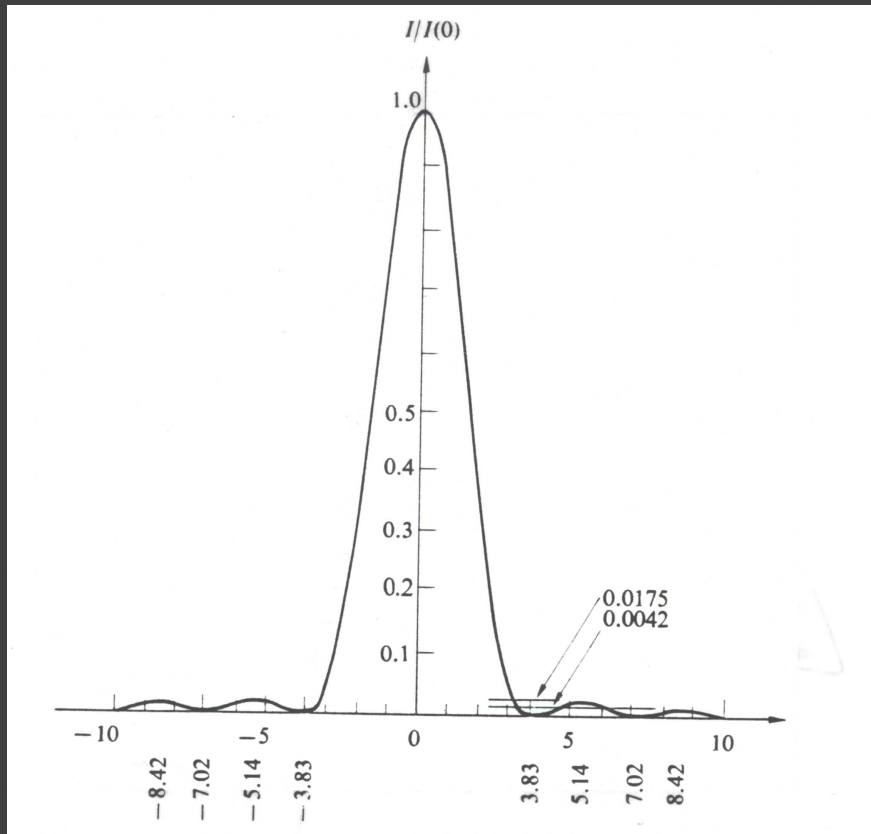
## Classical Fraunhofer Diffraction



Amplitude of wave at screen:

$$\Phi \propto \int_0^a \int_0^{2\pi} \exp(ibr \cos \phi) r d\phi dr$$

# Classical Fraunhofer Diffraction



Intensity:

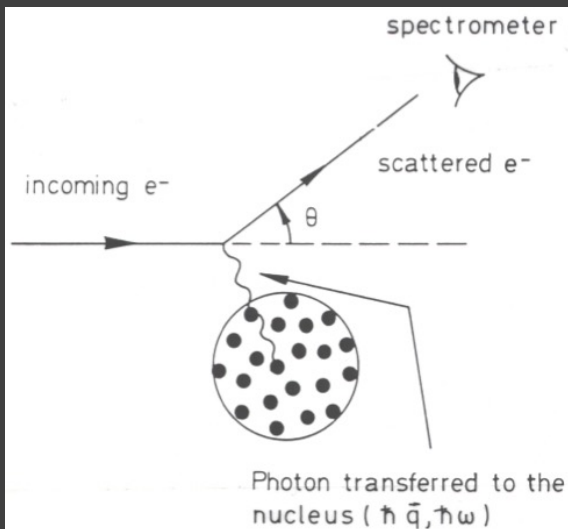
$$\Phi^2 \propto \left( \frac{J_1 \left( \left( \frac{2\pi a}{\lambda} \right) \sin \theta \right)}{\sin \theta} \right)^2$$

Minima occur at zeroes of Bessel function. 1<sup>st</sup> zero:  $x = 3.8317$

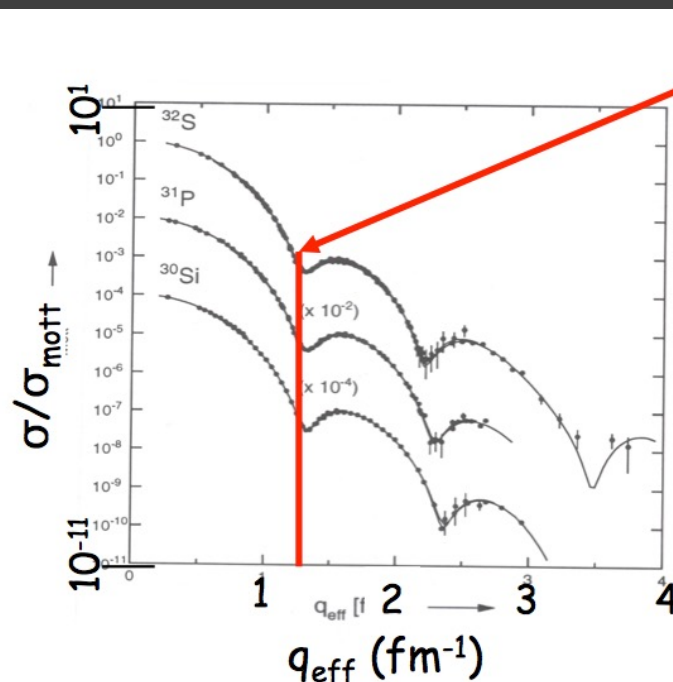
...some algebra...

Hence  $2a \approx \frac{1.22\lambda}{\sin \theta_{min}}$

# Example: $^{30}\text{Si}(e,e')$



Cross Section  $\Leftrightarrow$  Charge Form Factor



1<sup>st</sup> minimum =  $1.3 \text{ fm}^{-1}$

$\rightarrow \theta = 32.8^\circ$

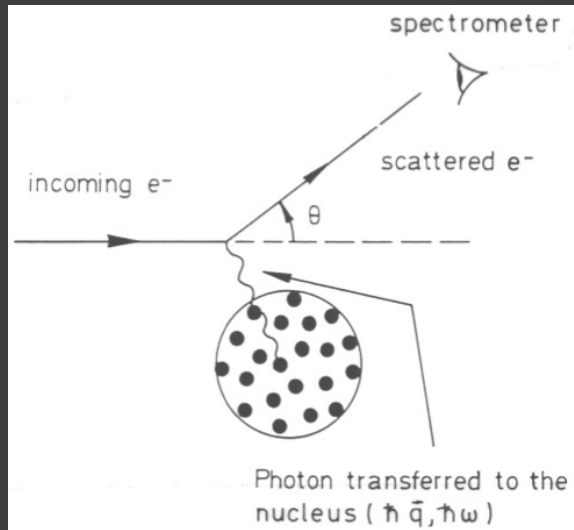
Electron energy =  $454.3 \text{ MeV}$

$\rightarrow \lambda = 2.73 \text{ fm}$

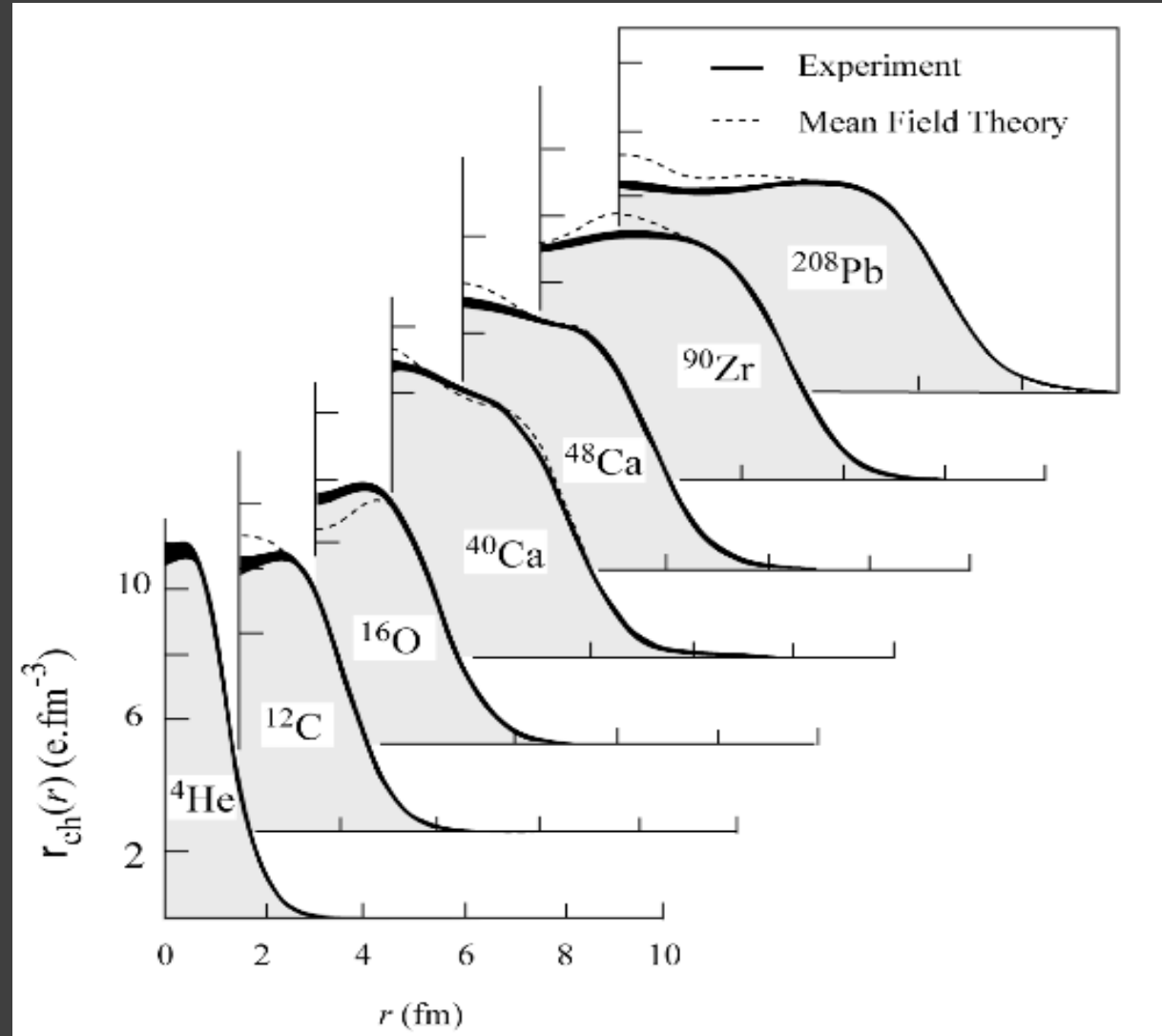
Calculated radius =  $3.07 \text{ fm}$

Measured rms radius =  $3.19 \text{ fm}$

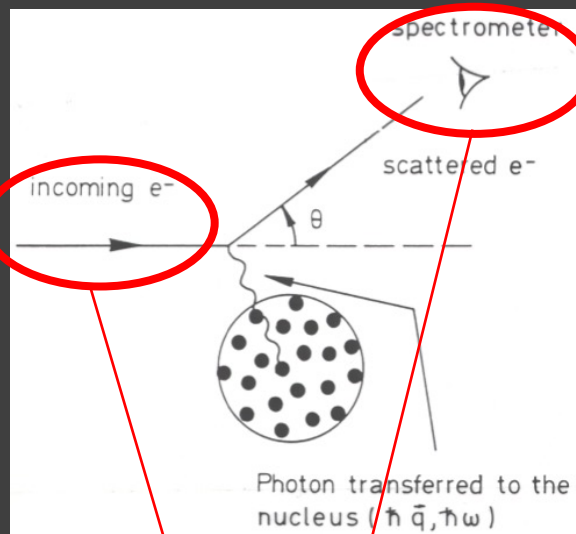
# Diffraction Measurements of Small Radii



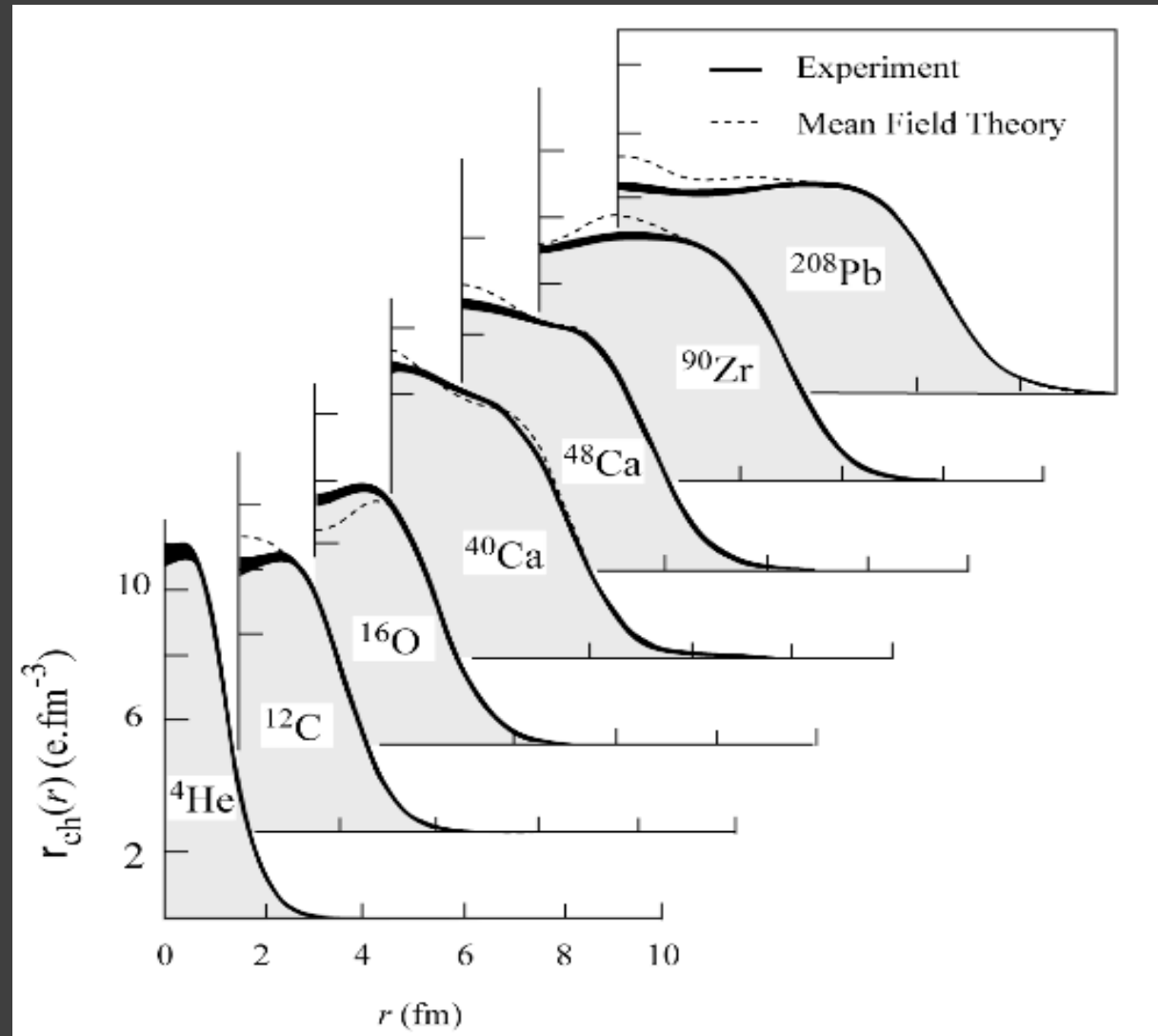
**Charge Distribution,  $r_{\text{ch}}(r)$ , is a Fourier Transform of the Charge Form Factor,  $F(q)$**



# Diffraction Measurements of Small Radii

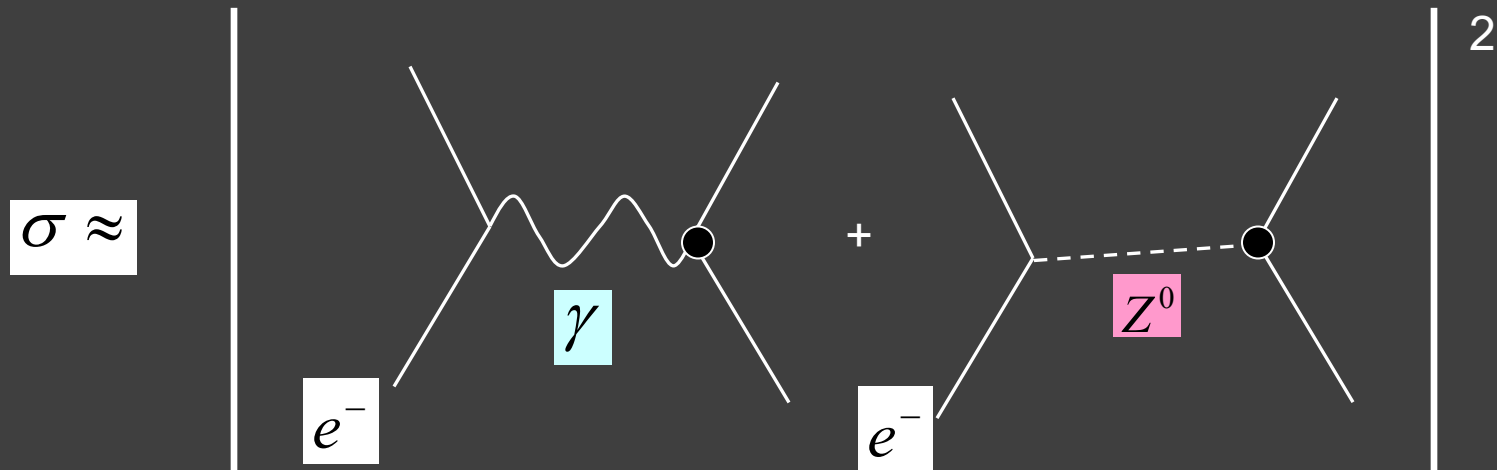


**10s – 100s  
Million Dollar  
Machines**




# Weak Interaction: Neutron Distribution

## Parity Violating Asymmetry



## Applications of PV at Jefferson Lab

- Nucleon Structure (strangeness) -- HAPPEX / G0
- Standard Model Tests ( $\sin^2 \theta_W$ ) -- e.g. Qweak
-  Nuclear Structure (neutron density) : PREX



# Weak Interaction: Neutron Distribution

$Z^0$  of Weak Interaction:  
Clean Probe Couples Mainly to Neutrons

$F_W(Q^2)$ :  $^{208}\text{Pb}$   
Weak Form Factor

$$A = \frac{\left(\frac{d\sigma}{d\Omega}\right)_R - \left(\frac{d\sigma}{d\Omega}\right)_L}{\left(\frac{d\sigma}{d\Omega}\right)_R + \left(\frac{d\sigma}{d\Omega}\right)_L} = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[ \underbrace{1 - 4\sin^2\theta_W}_{\approx 0} - \frac{F_W(Q^2)}{F_P(Q^2)} \right]$$

$F_P(Q^2)$ :  $^{208}\text{Pb}$   
Charge Form Factor

# Weak Interaction: Neutron Distribution

$Z^0$  of Weak Interaction:  
Clean Probe Couples Mainly to Neutrons

$F_W(Q^2)$ :  $^{208}\text{Pb}$   
Weak Form Factor

$$A = \frac{\left(\frac{d\sigma}{d\Omega}\right)_R - \left(\frac{d\sigma}{d\Omega}\right)_L}{\left(\frac{d\sigma}{d\Omega}\right)_R + \left(\frac{d\sigma}{d\Omega}\right)_L} = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[ \underbrace{1 - 4\sin^2\theta_W}_{\approx 0} - \frac{F_W(Q^2)}{F_P(Q^2)} \right]$$

Clean Probe Couples Mainly to Neutrons

$F_p(Q^2)$ :  $^{208}\text{Pb}$   
Charge Form Factor

	proton	neutron
Electric charge	1	0
Weak charge	0.08	1

$$Q_w = 2T_3 - 4Q_e \sin^2\theta_w = 2 \cdot \left(-\frac{1}{2}\right) = -1 \approx -0.99$$

$$Q_w = 2T_3 - 4Q_e \sin^2\theta_w = 2 \cdot \frac{1}{2} - 4 \sin^2 29^\circ \approx 1 - 0.94016 = 0.0598$$

# Weak Interaction: Neutron Distribution

Z<sup>0</sup> of Weak Interaction:  
Clean Probe Couples Mainly to Neutrons

$F_W(Q^2)$ : <sup>208</sup>Pb  
Weak Form Factor

$$A = \frac{\left(\frac{d\sigma}{d\Omega}\right)_R - \left(\frac{d\sigma}{d\Omega}\right)_L}{\left(\frac{d\sigma}{d\Omega}\right)_R + \left(\frac{d\sigma}{d\Omega}\right)_L} = \frac{G_F Q^2}{2\pi\alpha\sqrt{2}} \left[ \underbrace{1 - 4\sin^2\theta_W}_{\approx 0} - \frac{F_W(Q^2)}{F_P(Q^2)} \right]$$

$F_P(Q^2)$ : <sup>208</sup>Pb  
Charge Form Factor

High Accuracy:

$$\frac{dA}{A} = 3\% \rightarrow \frac{dR_n}{R_n} = 1\%$$

$R_n$  = neutron matter radius

# From Intuition to Formalism

Lab frame kinematics

$$k'^{\mu} = (E', \vec{k}')$$

$$k^{\mu} = (E, \vec{k})$$

$$q^{\mu} = (\omega, \vec{q})$$

$$q^{\mu} = k^{\mu} - k'^{\mu}$$

$$p'^{\mu} = (E_p, \vec{p}_p)$$

(not always detected)

$$p^{\mu} = (M, \vec{0})$$

Invariants:

$$p^{\mu} p_{\mu} = M^2$$

$$Q^2 = -q^{\mu} q_{\mu} = |\vec{q}|^2 - \omega^2$$

$$p_{\mu} q^{\mu} = M\omega$$

$$W^2 = (q^{\mu} + p^{\mu})^2 = p'_{\mu} p'^{\mu}$$

# From Intuition to Formalism

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$$W^2 = (q^{\mu} + p^{\mu})^2 = p'_{\mu} p'^{\mu}$$

# From Intuition to Formalism (Elastic)

Mott cross section:

$$\sigma_M = \frac{\alpha^2 \cos^2\left(\frac{\theta_e}{2}\right)}{4E^2 \sin^4\left(\frac{\theta_e}{2}\right)}$$

# From Intuition to Formalism (Elastic)

Recoil factor

Form factors

$$\frac{d\sigma}{d\Omega} = \sigma_M \left( \frac{E'}{E} \right) \left\{ \left[ F_1^2(Q^2) + \frac{Q^2}{4M^2} \kappa^2 F_2^2(Q^2) \right] + \frac{Q^2}{2M^2} [F_1(Q^2) + \kappa F_2(Q^2)]^2 \tan^2 \frac{\theta}{2} \right\}$$

Mott cross section:

$$\sigma_M = \frac{\alpha^2 \cos^2 \left( \frac{\theta_e}{2} \right)}{4E^2 \sin^4 \left( \frac{\theta_e}{2} \right)}$$

# From Intuition to Formalism (Elastic)

Recoil factor

Form factors

$$\begin{aligned}
 \frac{d\sigma}{d\Omega} &= \sigma_M \left( \frac{E'}{E} \right) \left\{ \left[ F_1^2(Q^2) + \frac{Q^2}{4M^2} \kappa^2 F_2^2(Q^2) \right] + \frac{Q^2}{2M^2} [F_1(Q^2) + \kappa F_2(Q^2)]^2 \tan^2 \frac{\theta}{2} \right\} \\
 &= \sigma_M \frac{E'}{E} \left[ \frac{G_E^2(Q^2) + \tau G_M^2(Q^2)}{1 + \tau} + 2\tau \tan^2 \frac{\theta}{2} G_M^2(Q^2) \right] \\
 &= \sigma_M \frac{E'}{E} \left[ \frac{Q^4}{\vec{q}^4} R_L(Q^2) + \left( \frac{Q^2}{2\vec{q}^2} + \tan^2 \frac{\theta}{2} \right) R_T(Q^2) \right]
 \end{aligned}$$



# From Intuition to Formalism (Elastic)

Recoil factor

Form factors

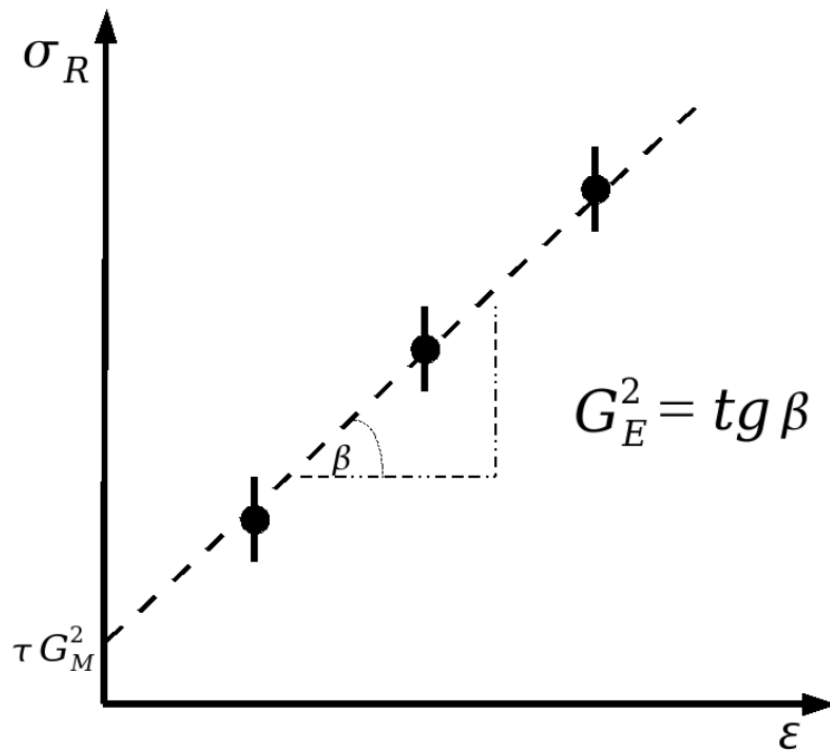
$$\begin{aligned}
 \frac{d\sigma}{d\Omega} &= \sigma_M \left( \frac{E'}{E} \right) \left\{ \left[ F_1^2(Q^2) + \frac{Q^2}{4M^2} \kappa^2 F_2^2(Q^2) \right] + \frac{Q^2}{2M^2} [F_1(Q^2) + \kappa F_2(Q^2)]^2 \tan^2 \frac{\theta}{2} \right\} \\
 &= \sigma_M \frac{E'}{E} \left[ \frac{G_E^2(Q^2) + \tau G_M^2(Q^2)}{1 + \tau} + 2\tau \tan^2 \frac{\theta}{2} G_M^2(Q^2) \right] \\
 &= \sigma_M \frac{E'}{E} \left[ \frac{Q^4}{\vec{q}^4} R_L(Q^2) + \left( \frac{Q^2}{2\vec{q}^2} + \tan^2 \frac{\theta}{2} \right) R_T(Q^2) \right]
 \end{aligned}$$

nucleons {

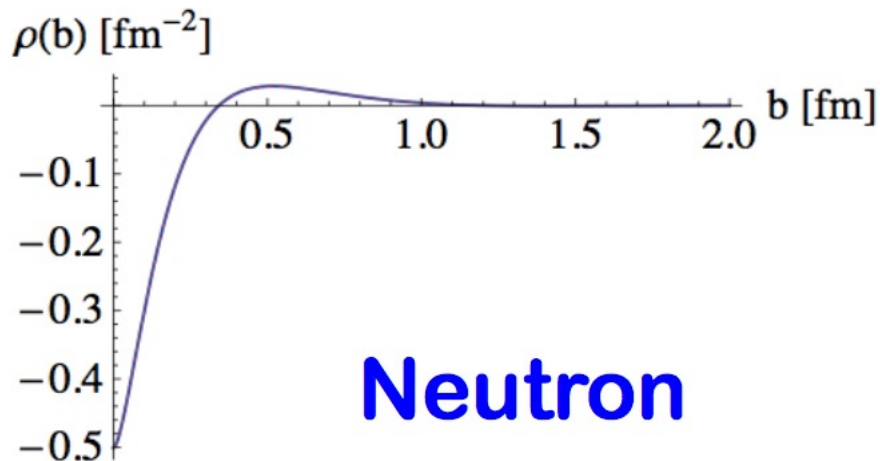
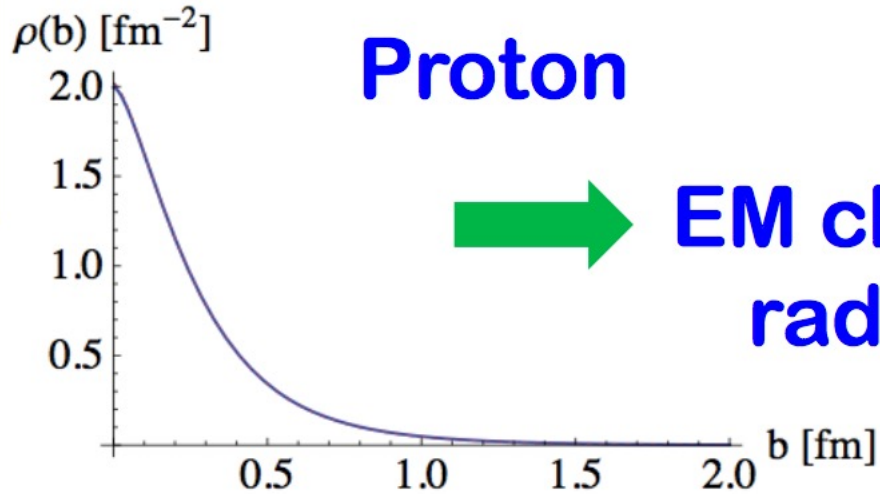
- $F_1, F_2$ : Dirac and Pauli form factors
- $G_E, G_M$ : Sachs form factors (electric and magnetic)
  - $G_E(Q^2) = F_1(Q^2) - \tau F_2(Q^2)$        $\tau = Q^2/4M^2$
  - $G_M(Q^2) = F_1(Q^2) + F_2(Q^2)$       (more standard definition of  $F_1$  and  $F_2$ )
- $R_L, R_T$ : Longitudinal and transverse response functions

# Form Factors: Cross-Sections

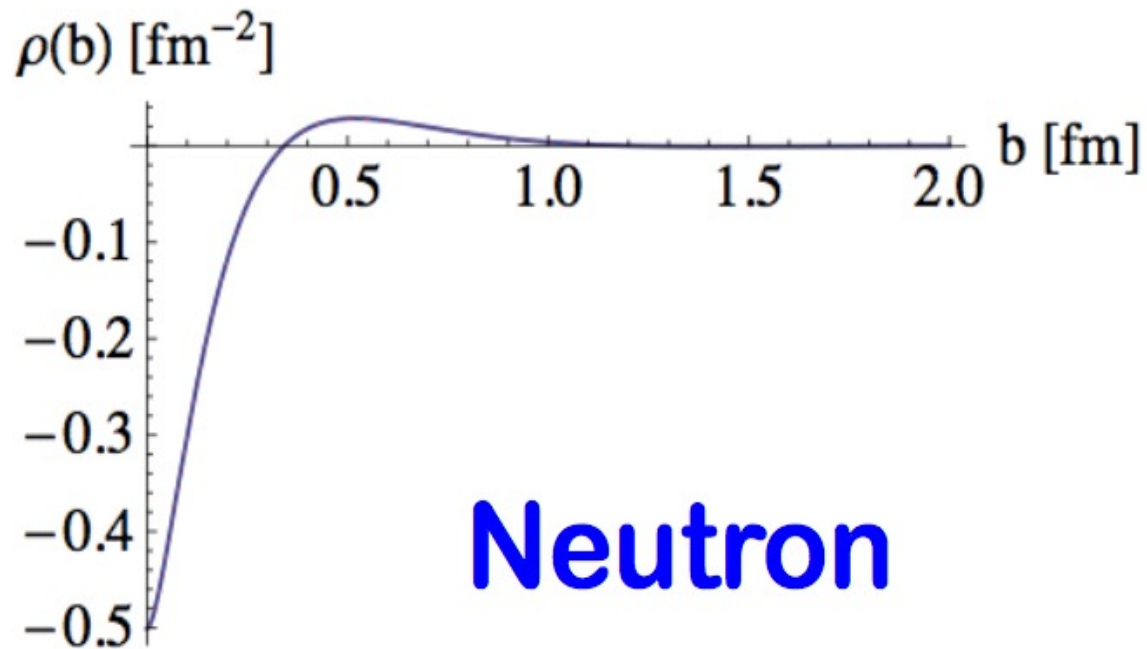
$$\frac{\varepsilon}{\tau} G_E^2 + G_M^2 = \frac{\varepsilon(1+\tau)}{\tau} \left[ \frac{d\sigma}{d\Omega} / \left( \frac{d\sigma}{d\Omega} \right)_{Mott+recoil} \right]$$



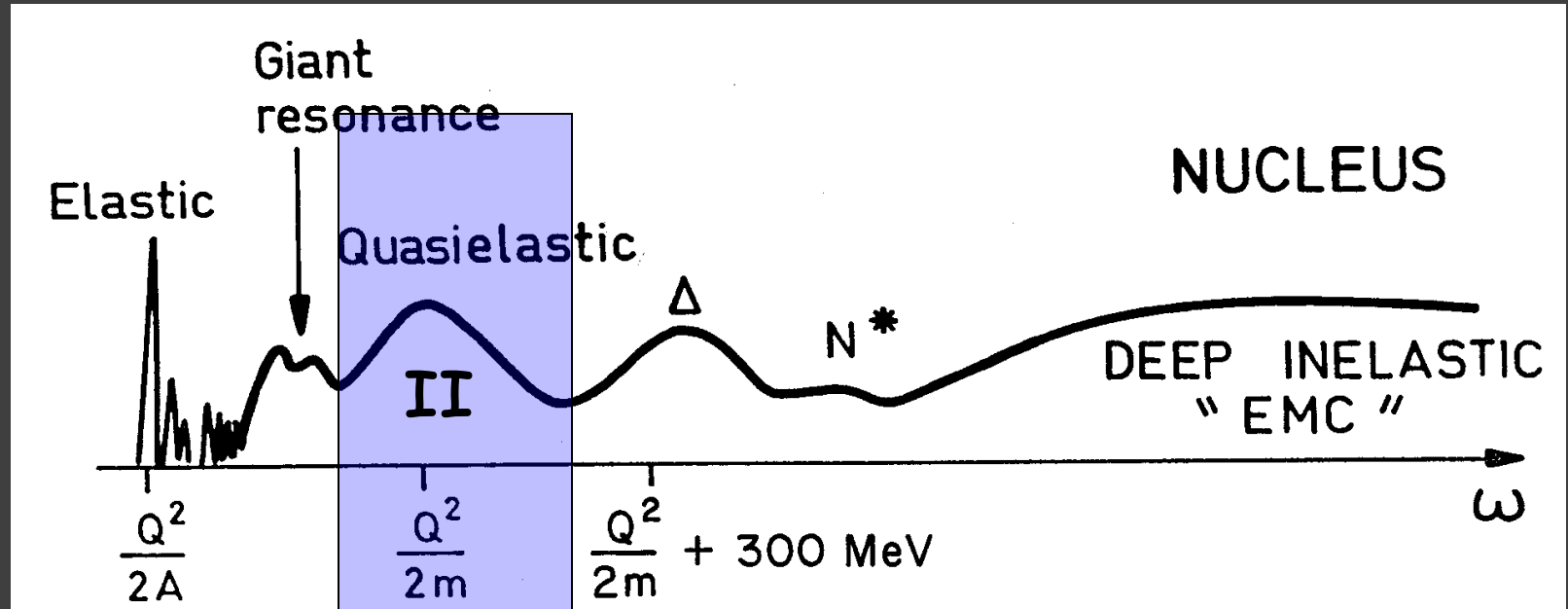
# *Electric charge distribution*



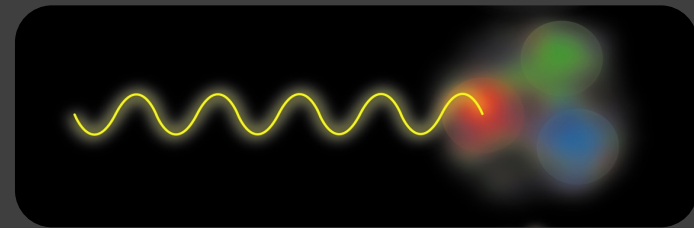
Neutron is negative in its center and positive in the edge!



# Quick Overview: Quasi-Elastic

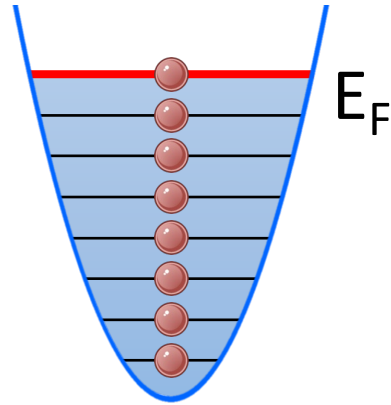


- Momentum Densities: Fermi Gas
- Y-Scaling
- Shell Structure and spectroscopic factors

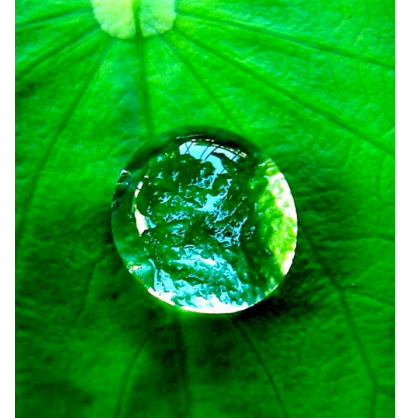


# What is a Nucleus ?

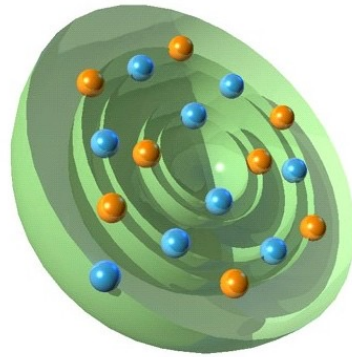
Fermi  
Gas  
Model



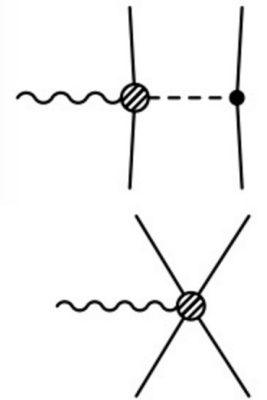
Liquid  
Drop  
Model



Shell  
Model



Chiral  
Perturbation  
Theory\*

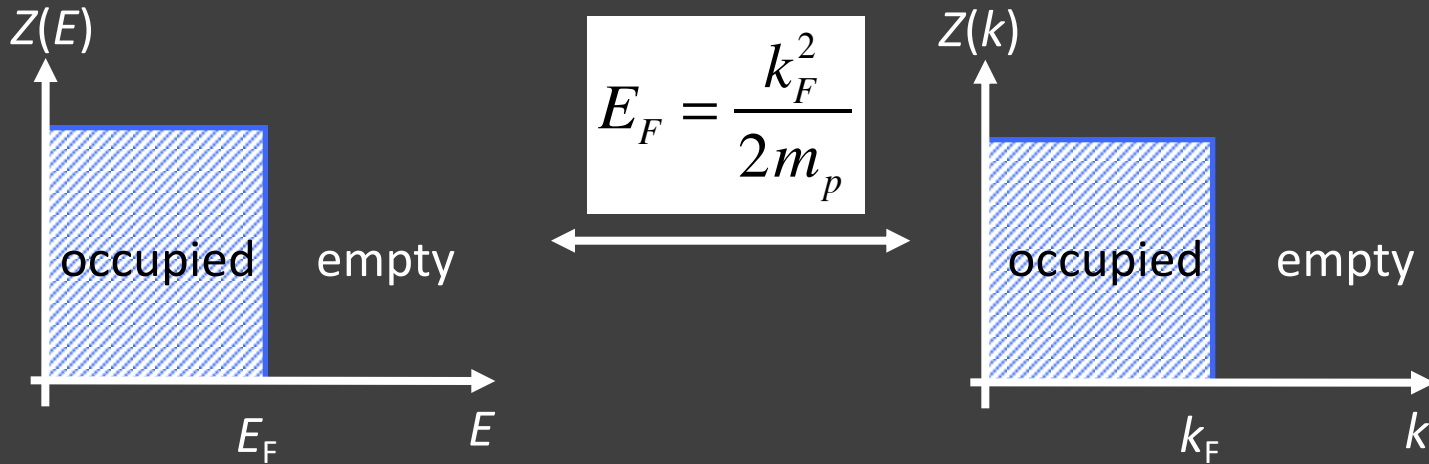


\* Should converge to exact solution

# Independent Particle Shell model (IPSM)

- single particle approximation:  
nucleons move independently from each other  
in an average potential created by the other nucleons (mean field)  
spectral function  $S(E,k)$ :  
probability of finding a proton with initial momentum  $k$  and  
energy  $E$  in the nucleus
- factorizes into energy & momentum part

nuclear matter:

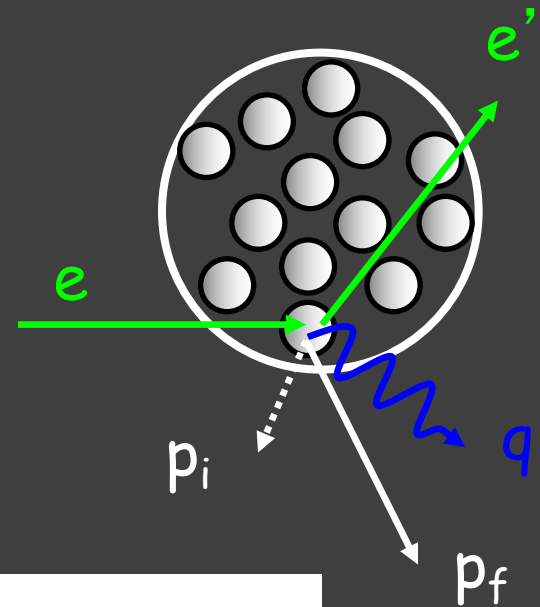


nuclei: 
$$S(\vec{p}, E) = \sum_i |\Phi_a(p)|^2 \delta(E + \epsilon_a)$$

Not 100% accurate, but a good starting point

# Fermi gas model:

how simple a model can you make ?



Initial nucleon energy:

$$KE_i = p_i^2 / 2m_p$$

Final nucleon energy:

$$KE_f = p_f^2 / 2m_p = (\vec{q} + \vec{p}_i)^2 / 2m_p$$

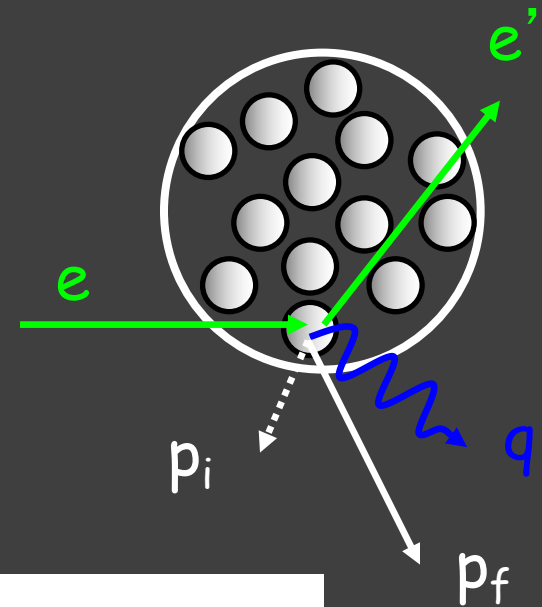
Energy transfer:

$$\nu = KE_f - KE_i = \frac{\vec{q}^2}{2m_p} + \frac{\vec{q} \cdot \vec{p}_i}{m_p}$$



# Fermi gas model:

how simple a model can you make ?



Initial nucleon energy:

$$KE_i = p_i^2 / 2m_p$$

Final nucleon energy:

$$KE_f = p_f^2 / 2m_p = (\vec{q} + \vec{p}_i)^2 / 2m_p$$

Energy transfer:

$$\nu = KE_f - KE_i = \frac{\vec{q}^2}{2m_p} + \frac{\vec{q} \cdot \vec{p}_i}{m_p}$$

Expect:

- Peak centroid at  $\nu = q^2/2m_p + \epsilon$
- Peak width  $2qp_{\text{fermi}}/m_p$
- Total peak cross section =  $Z\sigma_{\text{ep}} + N\sigma_{\text{en}}$

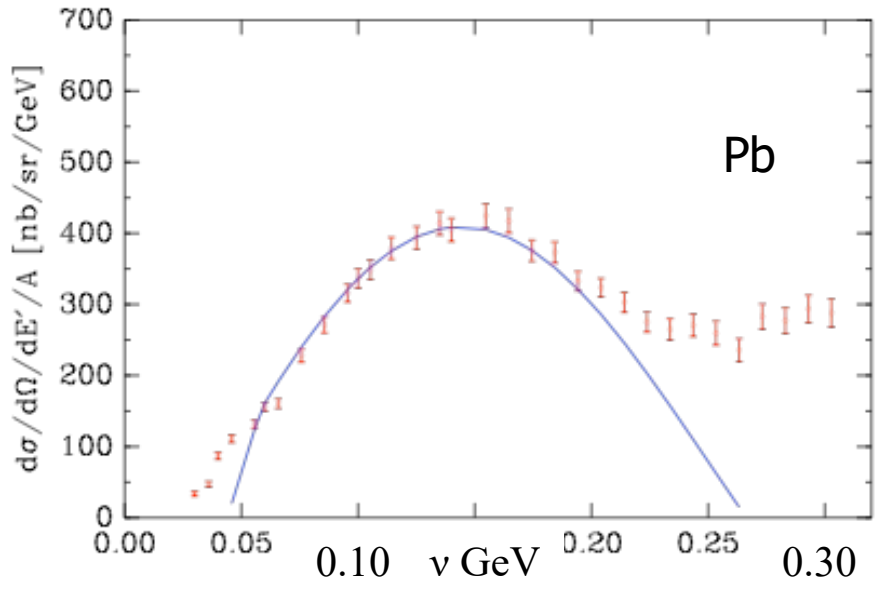
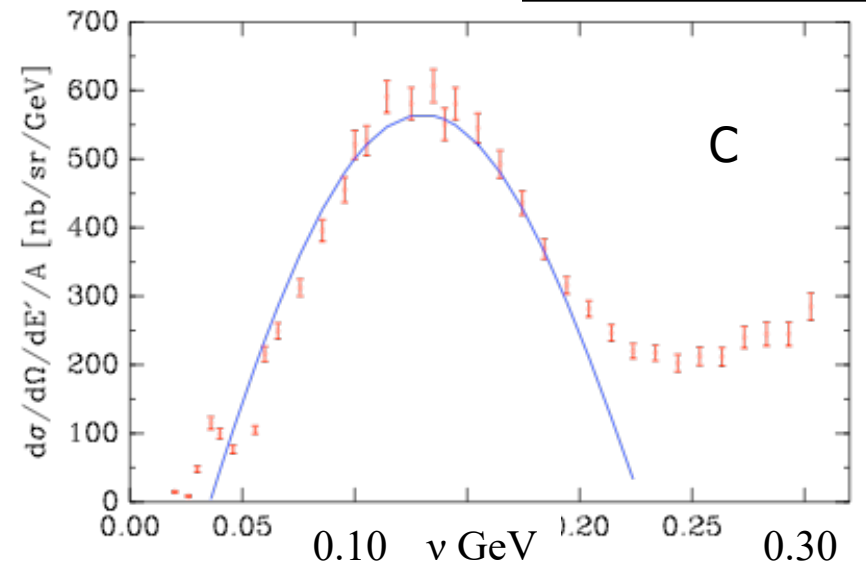
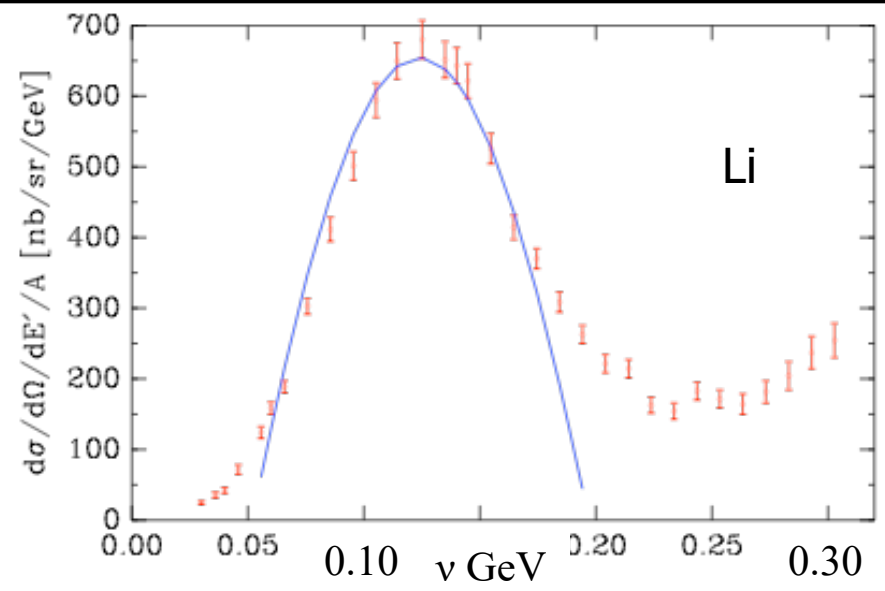
# Early 1970's Quasielastic Data

-> getting the bulk features

500 MeV, 60 degrees

$\vec{q} \approx 500 \text{ MeV}/c$

R.R. Whitney et al.,  
PRC 9, 2230 (1974).



Nucleus	$k_F$ MeV/c	$\bar{\epsilon}$ MeV
${}^6\text{Li}$	169	17
${}^{12}\text{C}$	221	25
${}^{24}\text{Mg}$	235	32
${}^{40}\text{Ca}$	251	28
<i>nat</i> Ni	260	36
${}^{89}\text{Y}$	254	39
<i>nat</i> Sn	260	42
${}^{181}\text{Ta}$	265	42
${}^{208}\text{Pb}$	265	44

compared to Fermi model: fit parameter  $k_F$  and  $\epsilon$

# Scaling

- The dependence of a cross section, in certain kinematic regions, on a single variable.
  - **scaling** validates the scaling assumption.
  - **Scale-breaking** indicates new physics.
- At moderate  $Q^2$  and  $x > 1$  we expect to see evidence for **y-scaling**, indicating that the electrons are scattering from quasifree nucleons
  - $y$  = minimum momentum of struck nucleon
- At high  $Q^2$  we expect to see evidence for **x-scaling**, indicating that the electrons are scattering from quarks.
  - $x = Q^2/2mv =$  fraction of nucleon momentum carried by struck quark (in infinite momentum frame)

Assumption: scattering takes place from a quasi-free proton or neutron in the nucleus.

$y$  is the momentum of the struck nucleon parallel to the momentum transfer:

$$y \approx -q/2 + mv/q \text{ (nonrelativistically)}$$

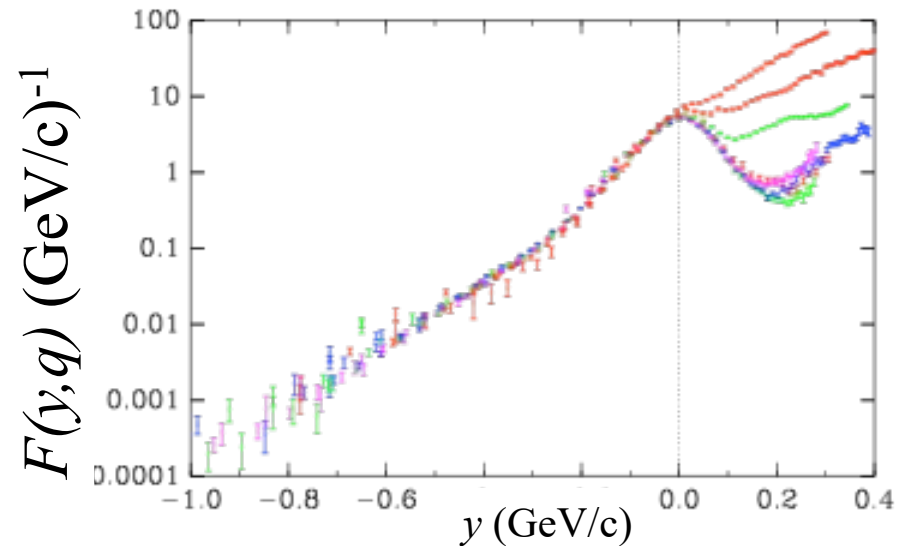
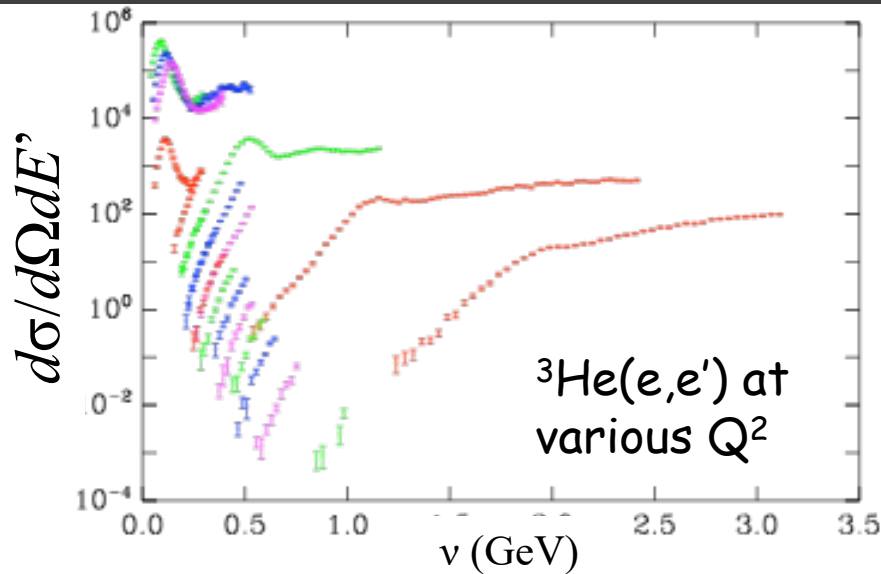
IF the scattering is quasifree, then  $F(y)$  is the integral over all perpendicular nucleon momenta (nonrelativistically).

Goal: extract the momentum distribution  $n(k)$  from  $F(y)$ .

$$F(y) = \frac{\sigma^{\text{exp}}}{(Z\tilde{\sigma}_p + N\tilde{\sigma}_n)} \cdot K$$

$$n(k) = -\frac{1}{2\pi y} \frac{dF(y)}{dy}$$

# y-scaling: inclusive scattering from $^3\text{He}$



$$F(y) = \frac{\sigma^{\text{exp}}}{(Z\tilde{\sigma}_p + N\tilde{\sigma}_n)} \cdot K$$

$$n(k) = -\frac{1}{2\pi y} \frac{dF(y)}{dy}$$

**Assumption:** scattering takes place from a **quasi-free** proton or neutron in the nucleus.

$y$  is the momentum of the struck nucleon parallel to the momentum transfer:  
 $y \approx -q/2 + mv/q$  (nonrelativistically)

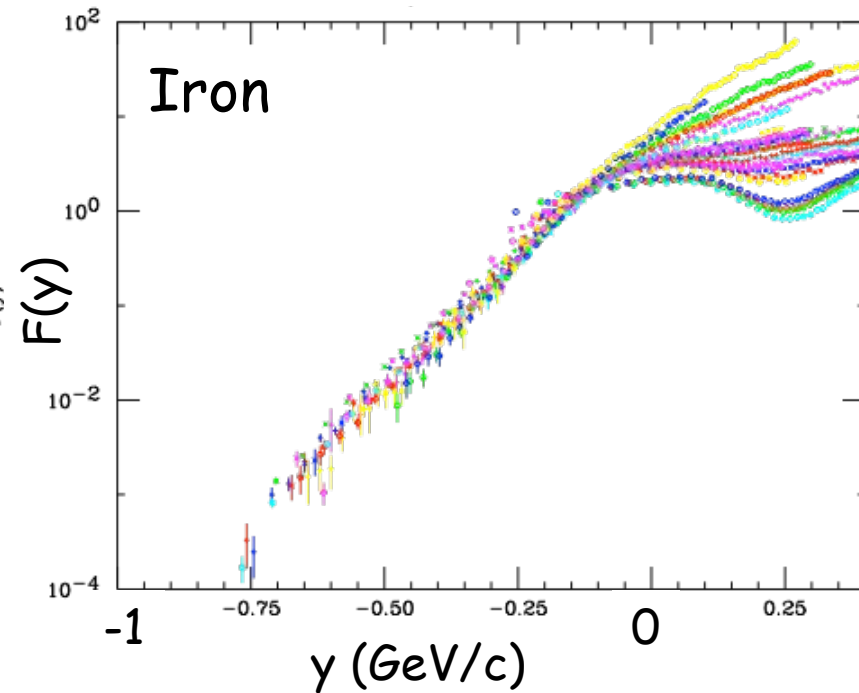
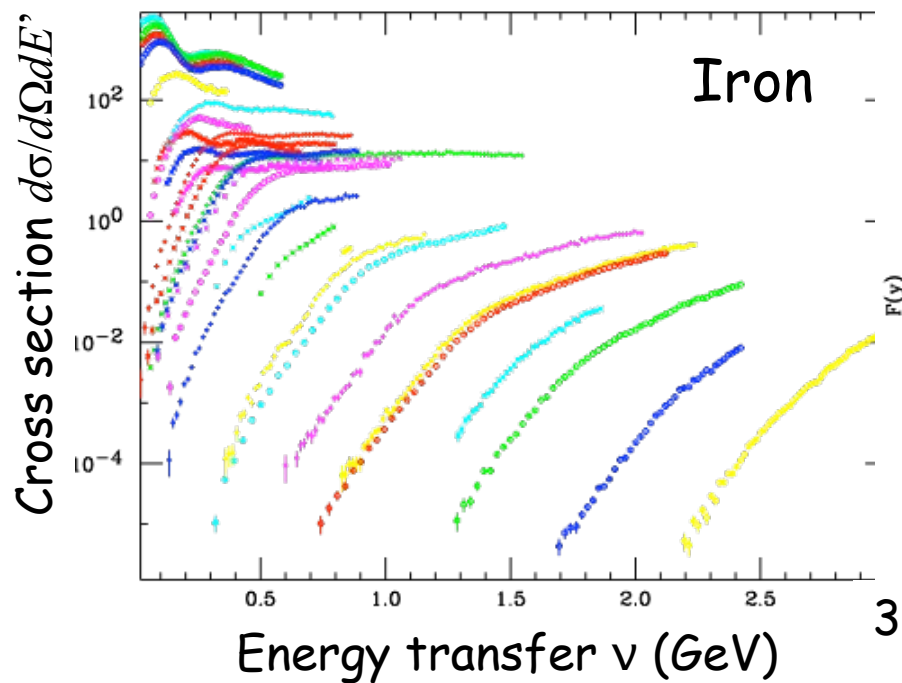
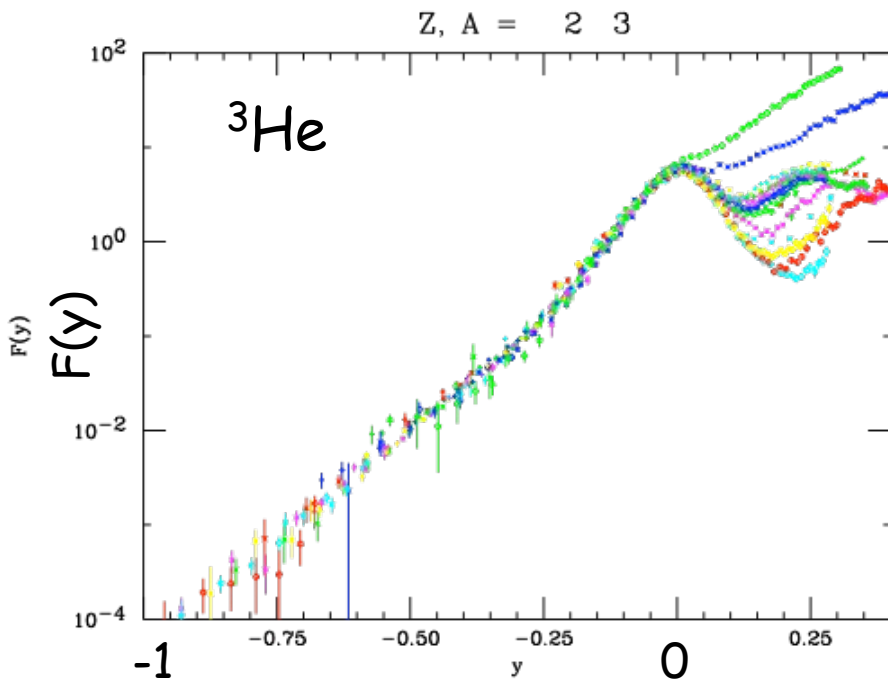
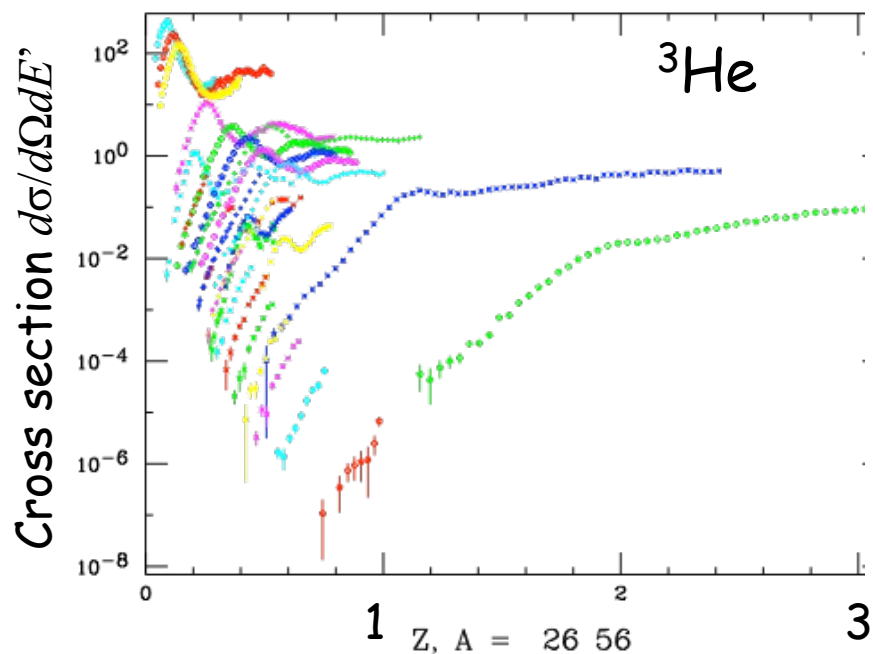
**IF** the scattering is quasifree, **then**  $F(y)$  is the integral over all perpendicular nucleon momenta (nonrelativistically).

**Goal:** extract the momentum distribution  $n(k)$  from  $F(y)$ .

# Assumptions & Potential Scale Breaking Mechanisms

- No Final State Interactions (FSI)
- No internal excitation of (A-1)
- Full strength of Spectral function can be integrated over at finite  $q$
- No inelastic processes (choose  $\gamma < 0$ )
- No medium modifications (discussed later)

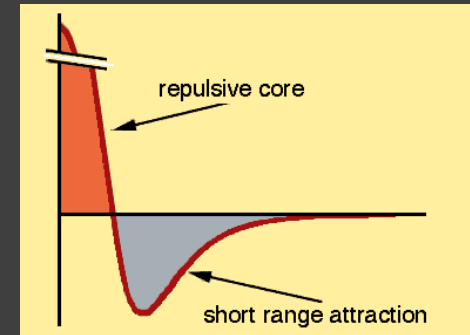
Y-scaling works!



# But what about the Shell Model?

- Many-Body Hamiltonian:

$$H = \sum_{i=1}^A \frac{p^2}{2m_N} + \sum_{i<j=1}^A v_{2body}(i,j) + \sum_{i<j<k=1}^A v_{3body}(i,j,k) + \dots$$

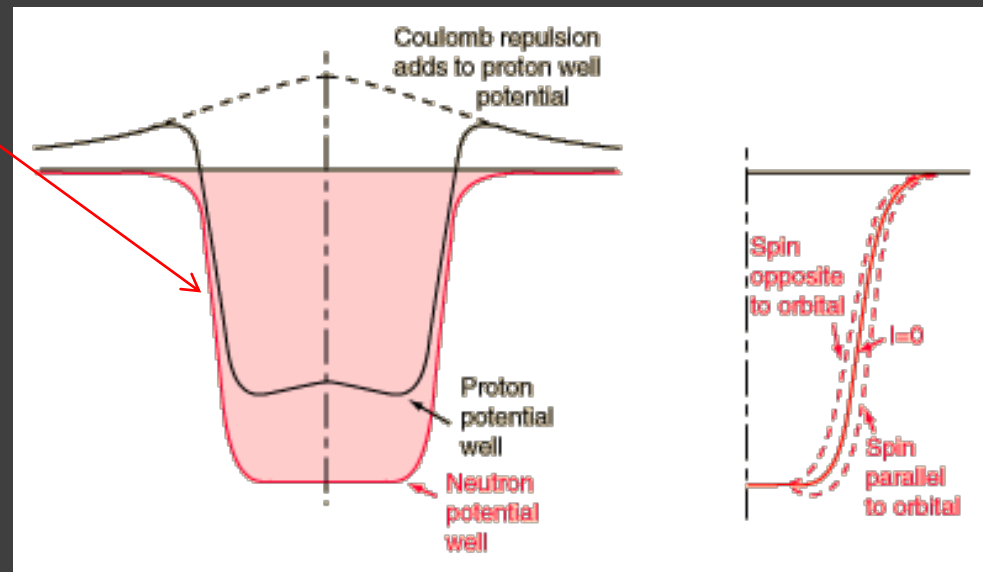


- Mean-Field Approximation:

$$H = \sum_{i=1}^A \frac{p^2}{2m_N} + \sum_{i=1}^A V(i)$$

Results in an “atom-like” shell model:

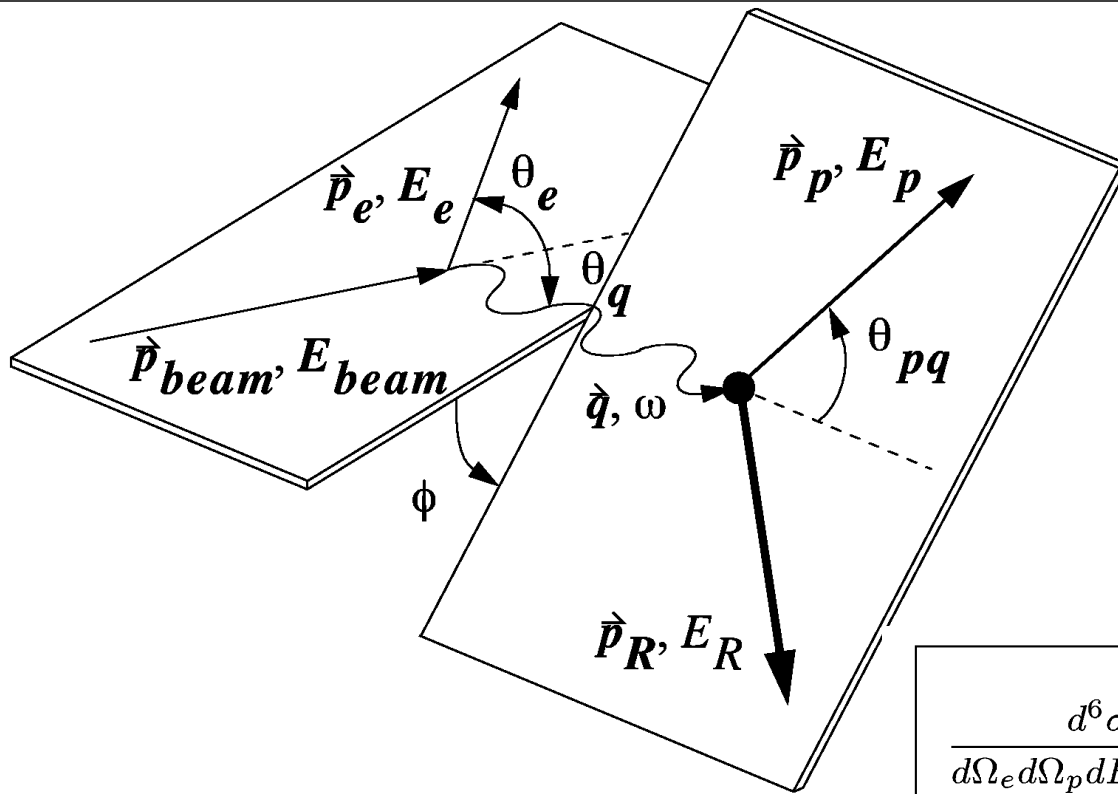
- Ground state energies
- Excitation Spectrum
- Spins
- Parities
- ...



E. Wigner, M. Mayer, and J. Jenson,  
1962 Nobel Prize



# (e,e'p) Spectroscopy



$$\frac{d^6\sigma}{d\Omega_e d\Omega_p dE_{miss} d\omega} = K\sigma_{Mott} [ v_L \mathbf{R}_L + v_T \mathbf{R}_T + v_{LT} \mathbf{R}_{LT} \cos(\phi) + v_{TT} \mathbf{R}_{TT} \cos(2\phi) ]$$

where

$K$  = (phase space)

$\sigma_{Mott}$  = (relativistic Rutherford scattering)

$v = v(q, \omega)$  (electron kinematics)

Each  $\mathbf{R}$  now depends on more variables

$$\mathbf{R} = \mathbf{R}(q, \omega, p_{miss}, E_{miss})$$

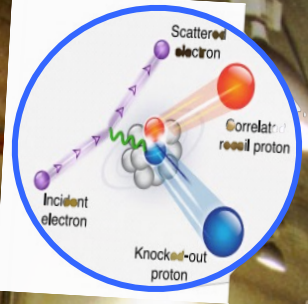
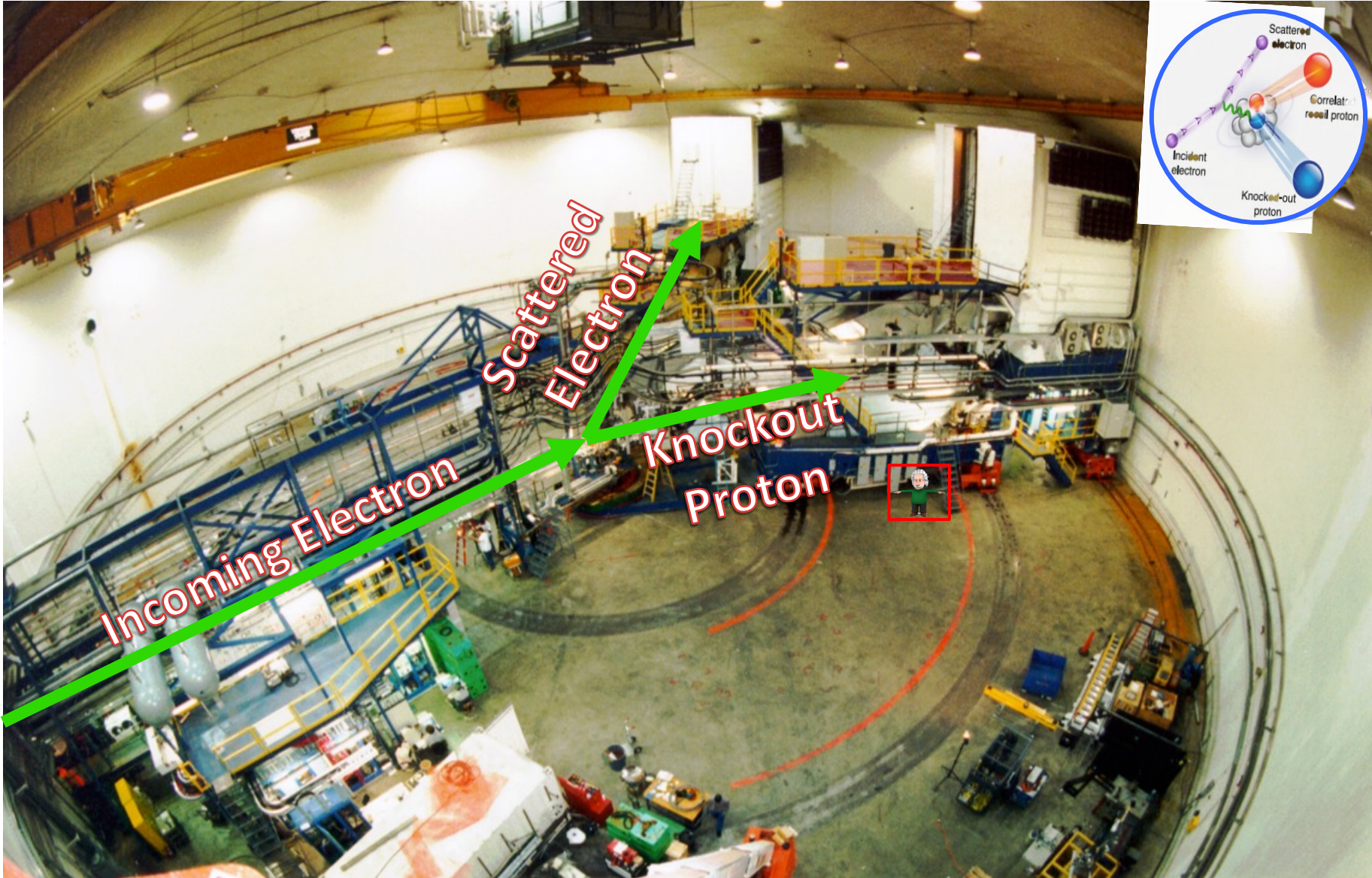
And then there were four

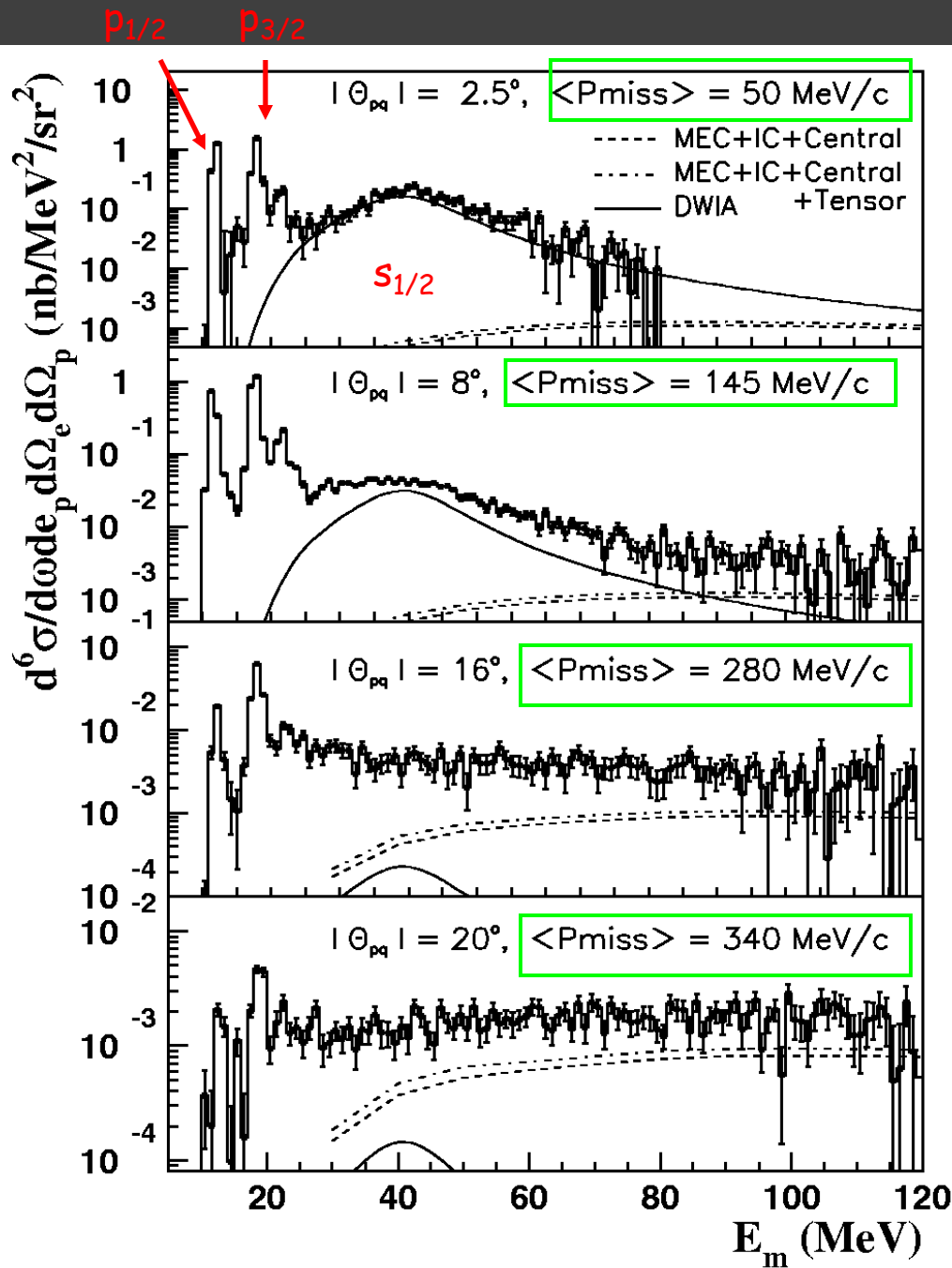
(response functions, that is)

(When you include electron and proton spin, there are 18!)

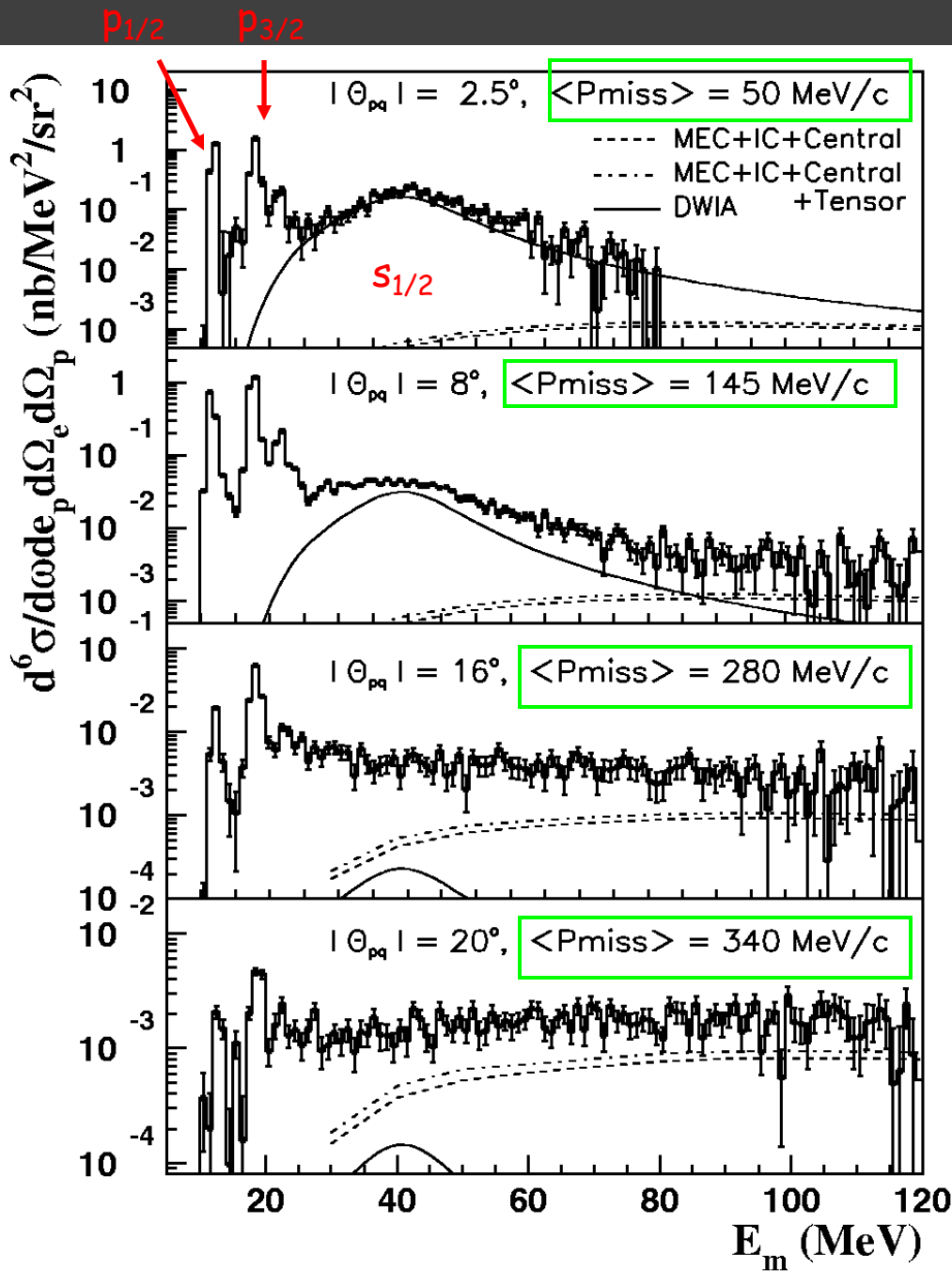
(And if you scatter from a polarized spin-1 target, there are 41. Double Yikes!!)

# Hall-A: High-Resolution Spectrometers

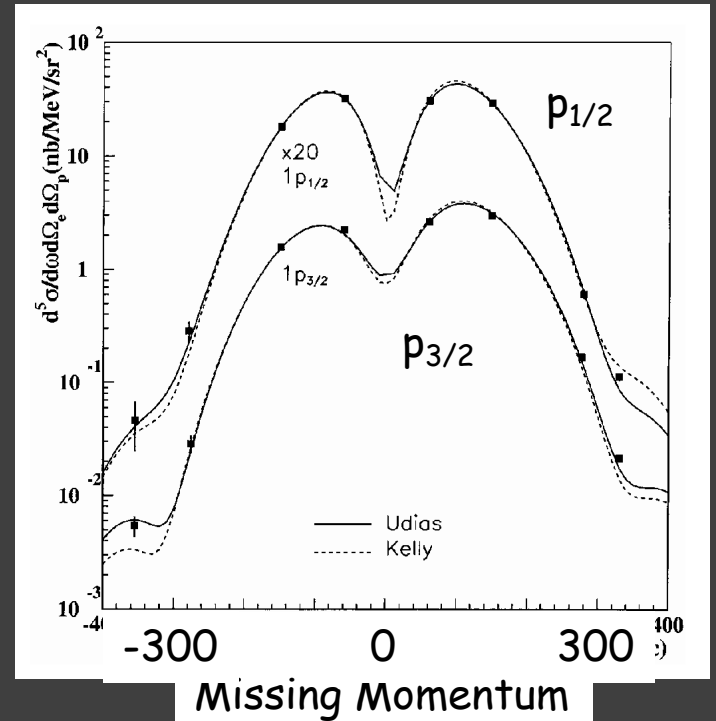




$^{16}\text{O}(e,e'p)$  and shell structure



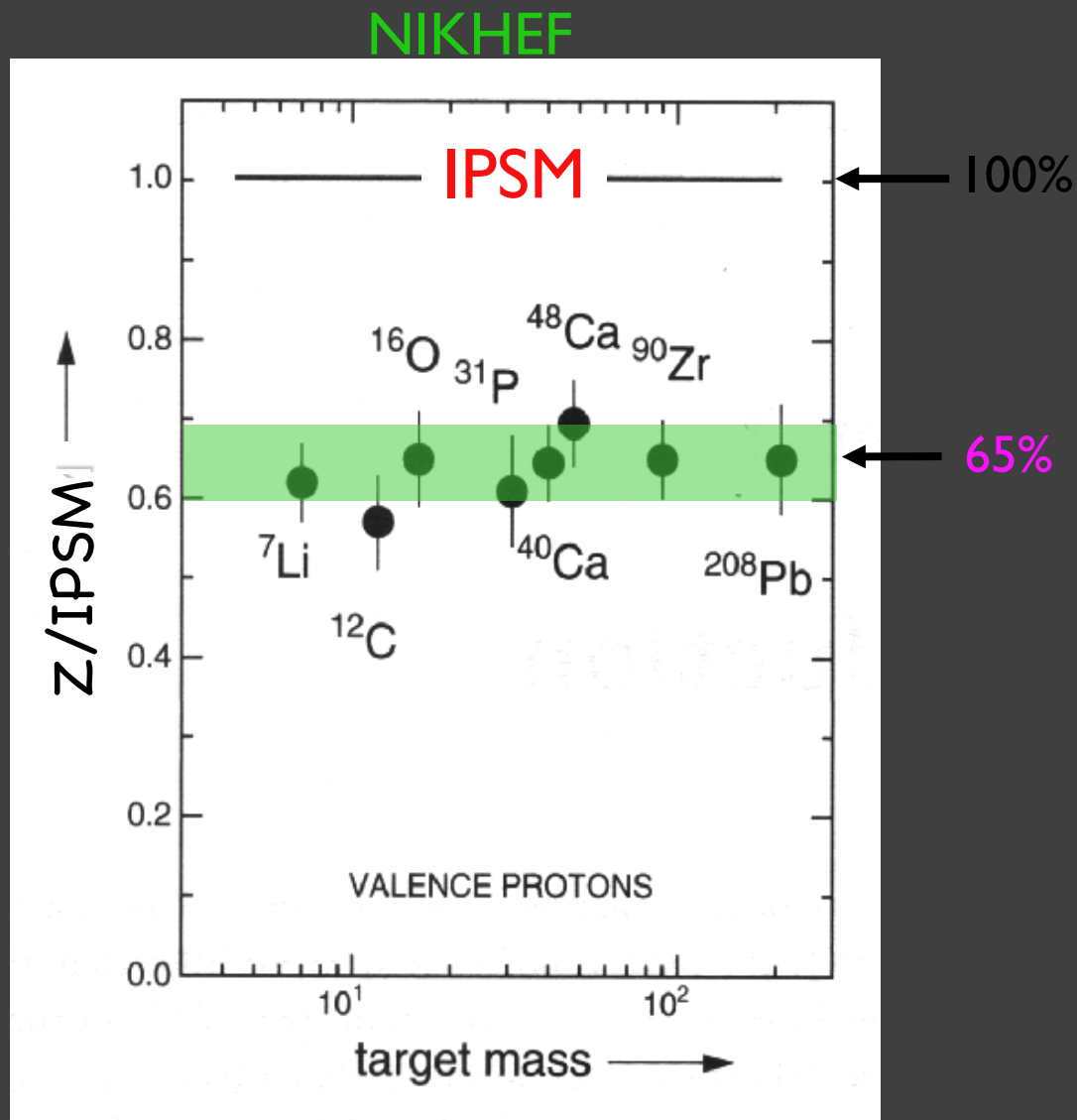
# $^{16}\text{O}(e,e'p)$ and shell structure



1p<sub>1/2</sub>, 1p<sub>3/2</sub> and 1s<sub>1/2</sub> shells visible

Momentum distribution as expected for  $l=0, 1$

# But we do not see enough protons!



But we do not see enough protons!

