

Status of the Muon $g-2$ Experiment at Fermilab

Sean Foster, University of Kentucky
On behalf of the Muon $g-2$ Collaboration
August 9, 2024



2024 Joint Photonuclear Reactions
and Frontiers & Careers Workshop
MIT Laboratory for Nuclear Science



Wilson Hall Fermilab Batavia, IL



Photo taken in 2013!

Muon g-2 storage ring



The Muon g-2 Collaboration



US Universities

- Boston
- Cornell
- UIUC
- James Madison
- Kentucky
- Massachusetts
- Michigan
- Michigan State
- Mississippi
- North Central College
- Regis
- Virginia
- Washington

US National Labs

- Argonne
- Brookhaven
- Fermilab



China

- Shanghai Jiao Tong



Germany

- Dresden
- Mainz



Italy

- Frascati
- Molise
- Naples
- Pisa
- Roma Tor Vergata
- Trieste
- Udine



Korea

- CAPP/IBS/KAIST



Russia

- Budker/Novosibirsk
- JINR Dubna



United Kingdom

- Lancaster/Cockcroft
- Liverpool
- Manchester
- University College London



Collaboration Meeting
Ann Arbor, MI July 2024

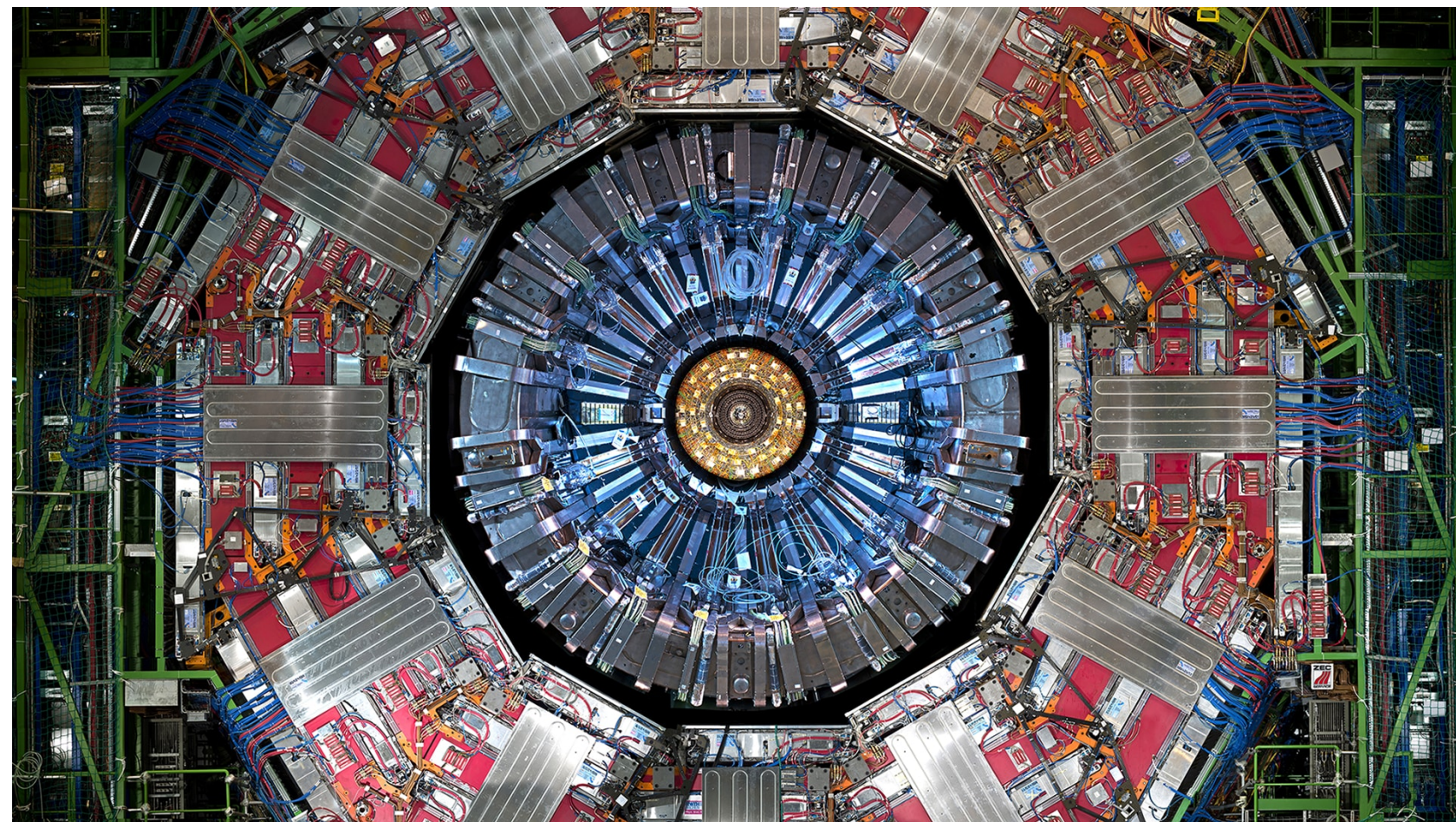
- Collaboration formed in the mid/late 2000s
- Technical Design Report in 2015
- First beam in 2017 commissioning run
- Goal: measure the **muon magnetic anomaly** to a precision of **140 parts-per billion**, x4 more precise than previous best measurement

181 collaborators
33 Institutions
7 countries

Motivation

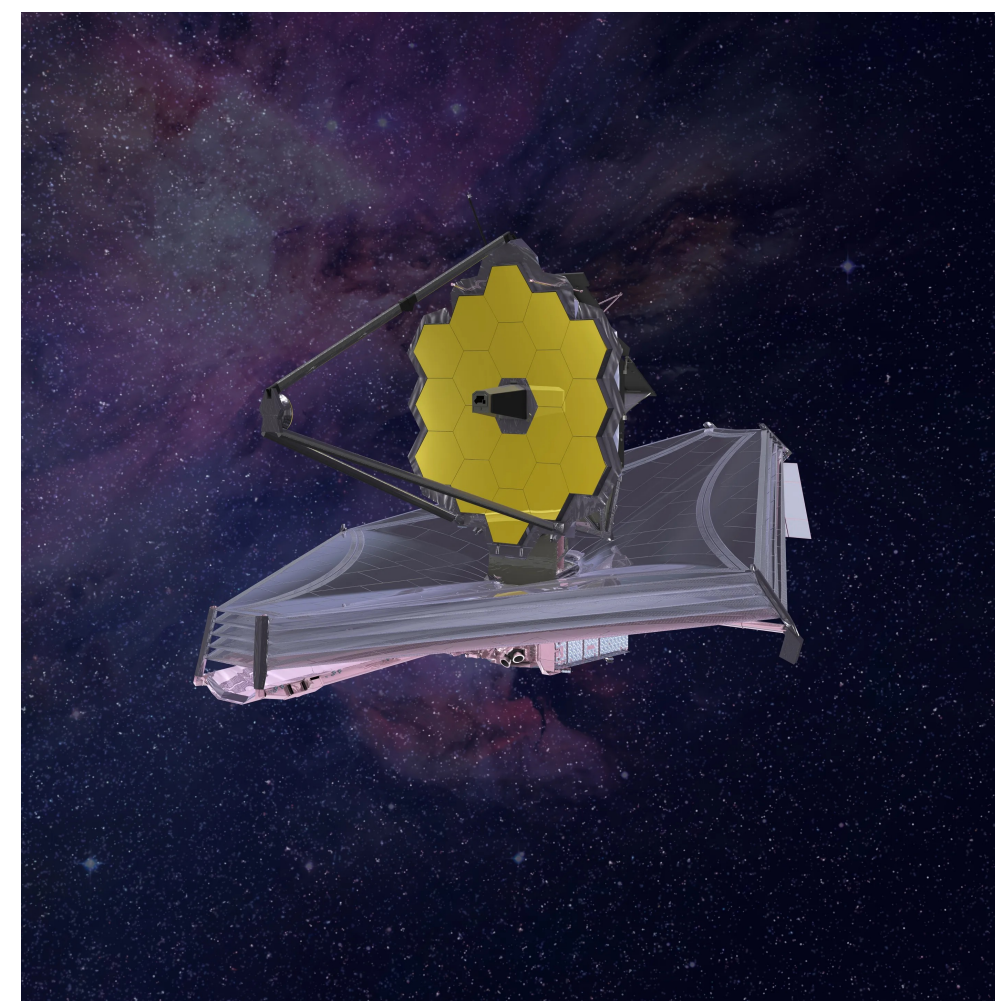
- **Test the Standard Model (SM) of particle physics and search for new physics**
 - Evidence aplenty that the SM is incomplete, e.g. what is the nature of dark matter? origin of matter/anti-matter asymmetry in the universe? etc.
- How to test SM and search for new physics?

Go to high energy!



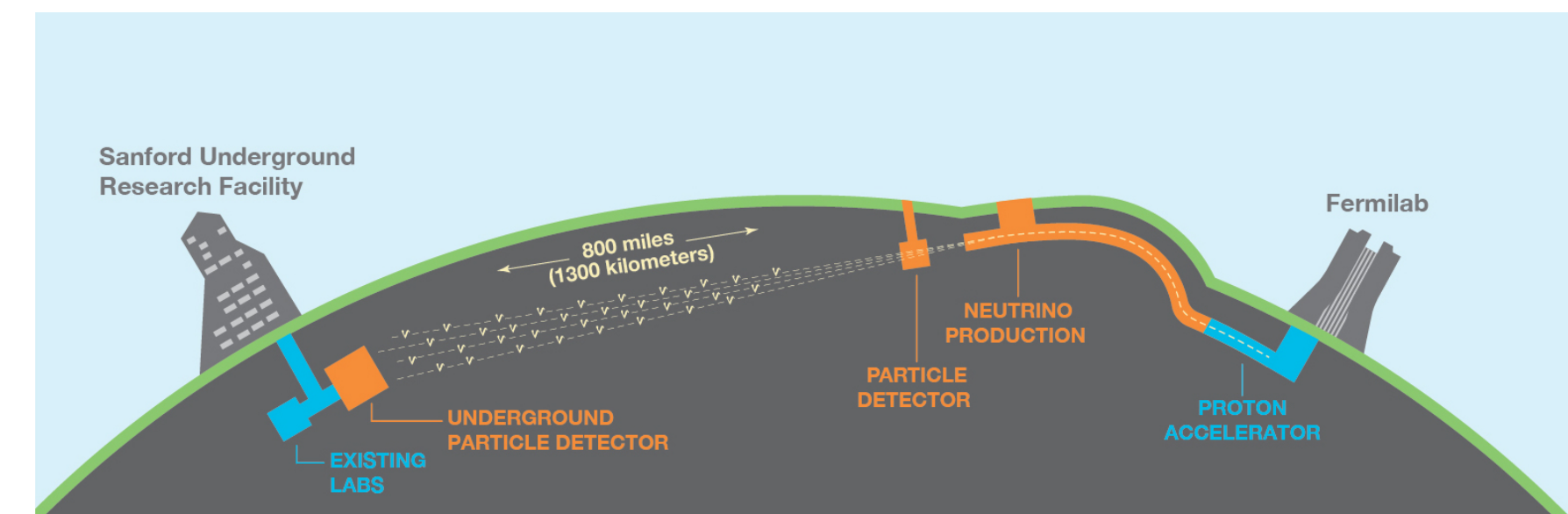
CMS, LHC CERN

Look out into the universe!



JWST, NASA

Study lots of particles!



DUNE, Fermilab

Motivation

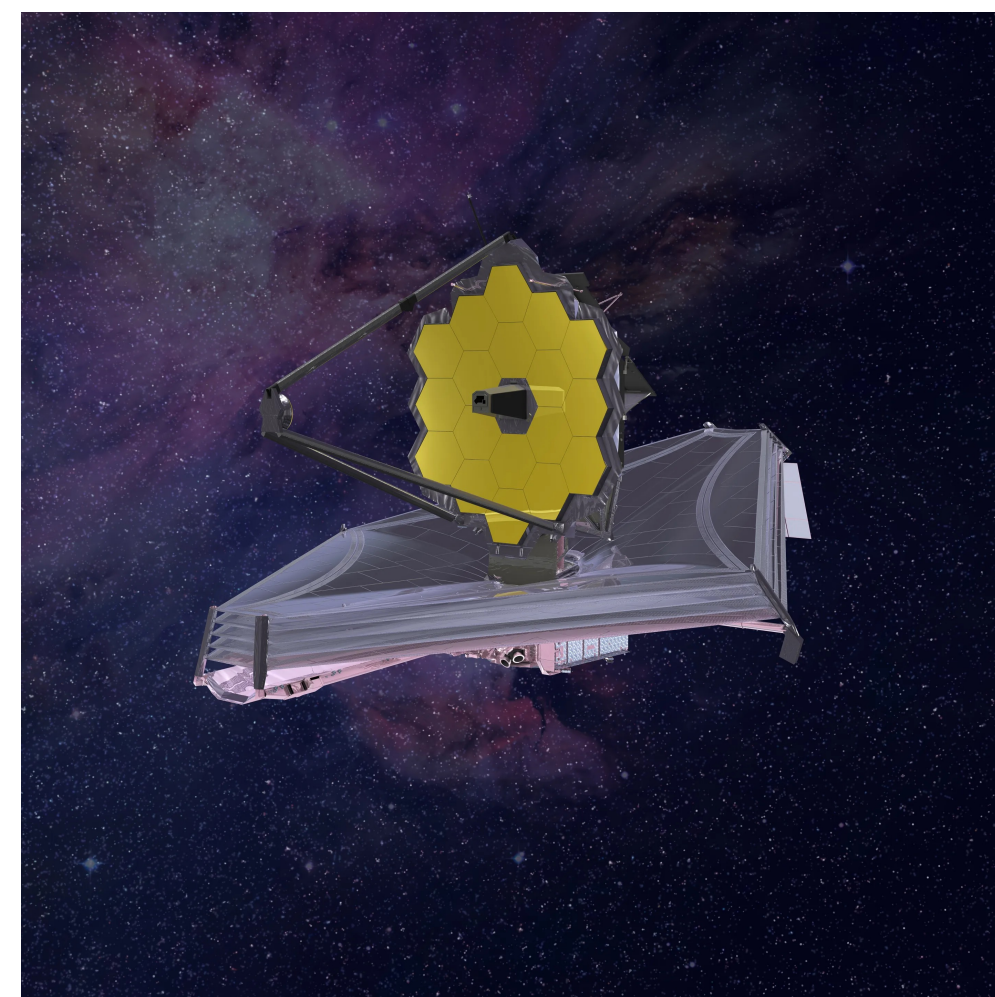
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Go to high energy!



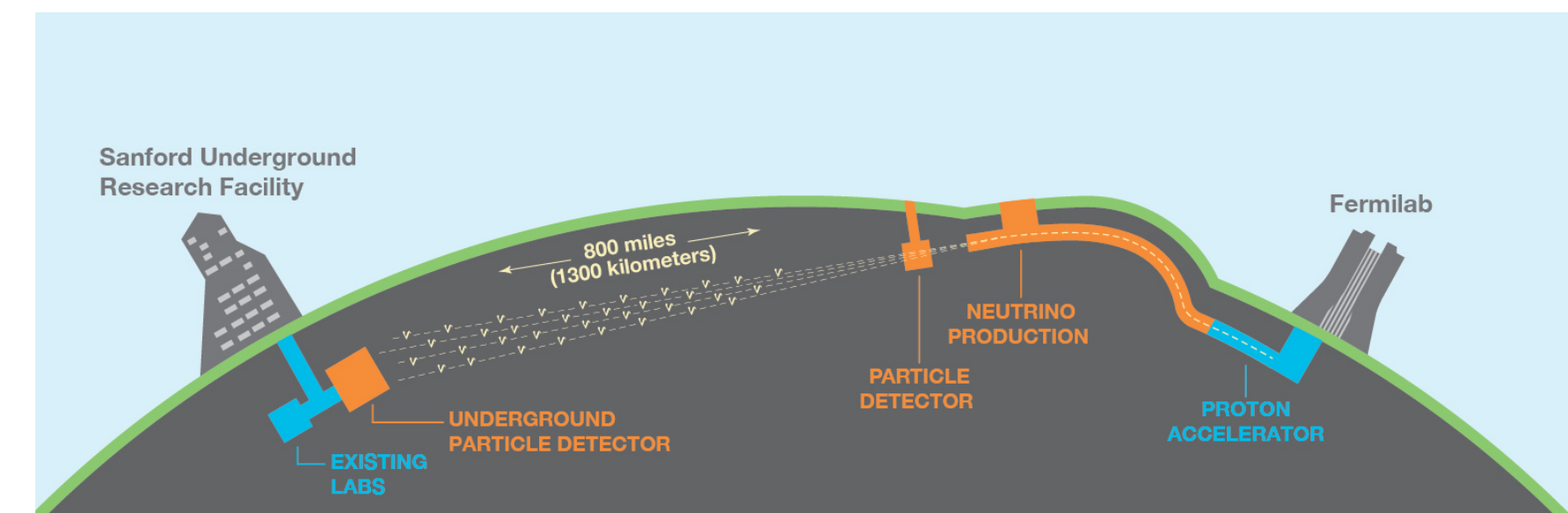
CMS, LHC CERN

Look out into the universe!



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DUNE, Fermilab



Magnetic moments can test the Standard Model

- Magnetic moments are sensitive to particles in nature through the “g-factor”

magnetic moment

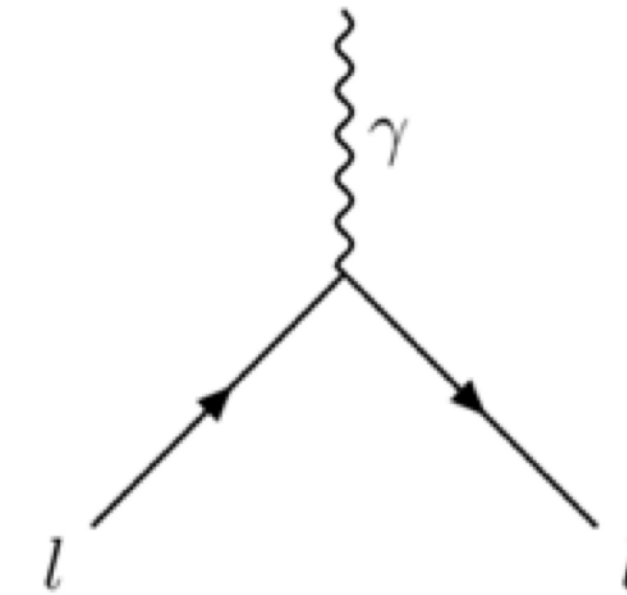
$$\mu = g \frac{e}{2m} s$$

gyromagnetic (“g”) factor

spin

$$a = \frac{g - 2}{2}$$

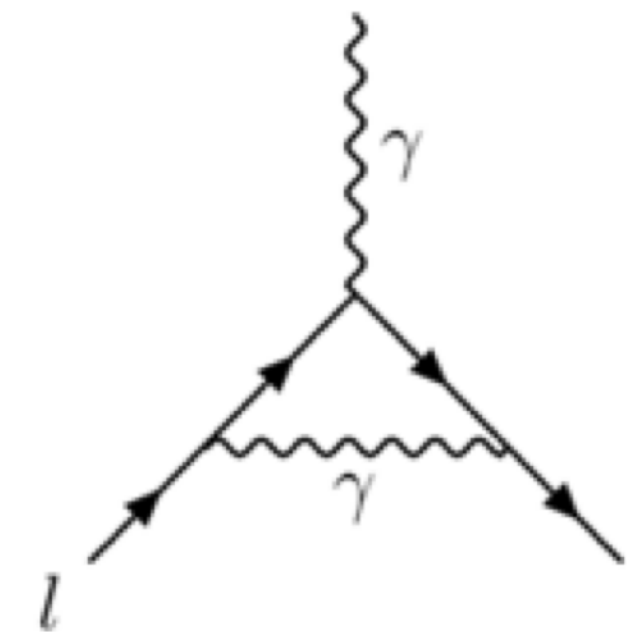
magnetic anomaly



$$g = 2$$

- Dirac’s theory of spin-1/2 fermions predicts $g = 2$ ($a = 0$)

- Loop corrections cause g to deviate from 2 ($a \neq 0$)



$$+ \frac{\alpha}{\pi}$$

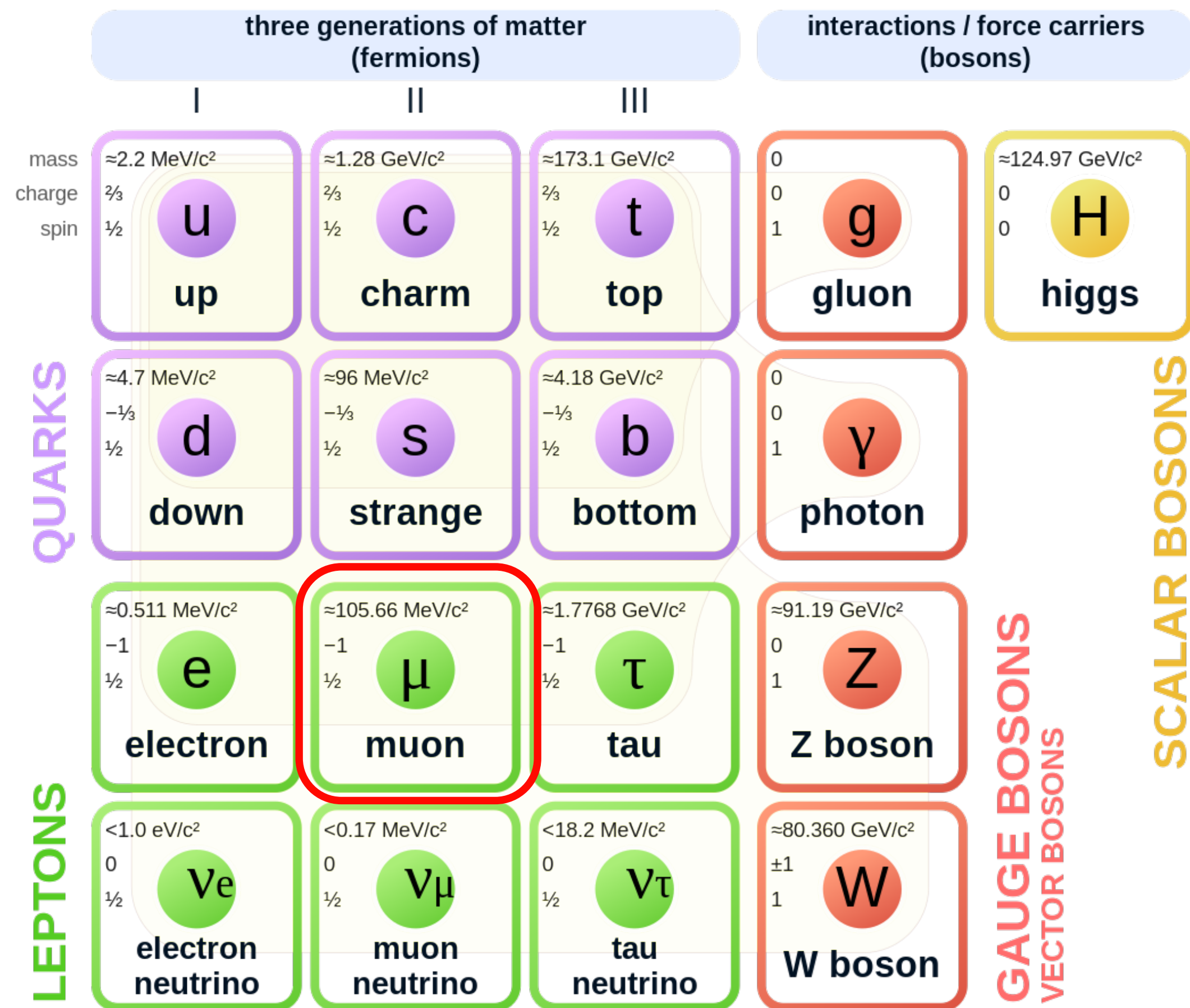
“Schwinger” term

- Size of a set by particles in nature, so a measurement of anomaly can test the **completeness of the Standard Model**

$$+ \dots$$

Pick the muon!

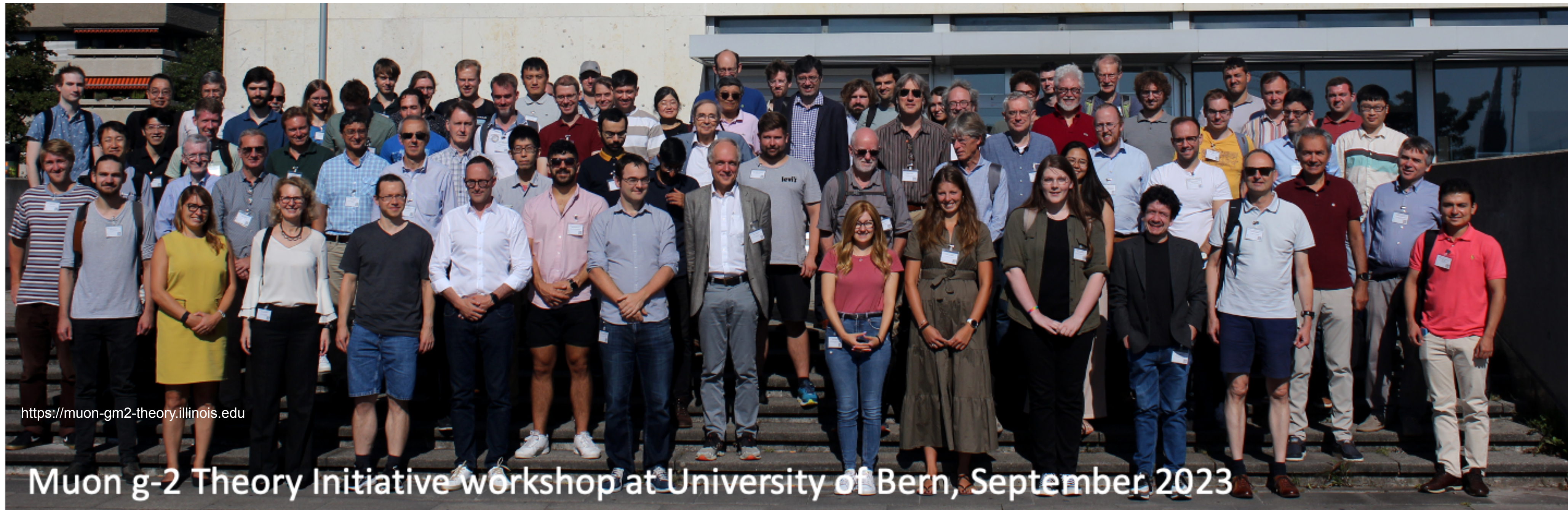
Standard Model of Elementary Particles



- The **muon** is a second generation charged lepton
- Decays into an electron and two neutrinos with a lifetime of $\sim 2.2\mu s$
- **207x** more massive than the electron
- Sensitivity to virtual particles $\propto m_l^2/M^2$, so muon is 40,000x more sensitive than electron

$$g = 2 + \frac{\alpha}{\pi} + \dots$$

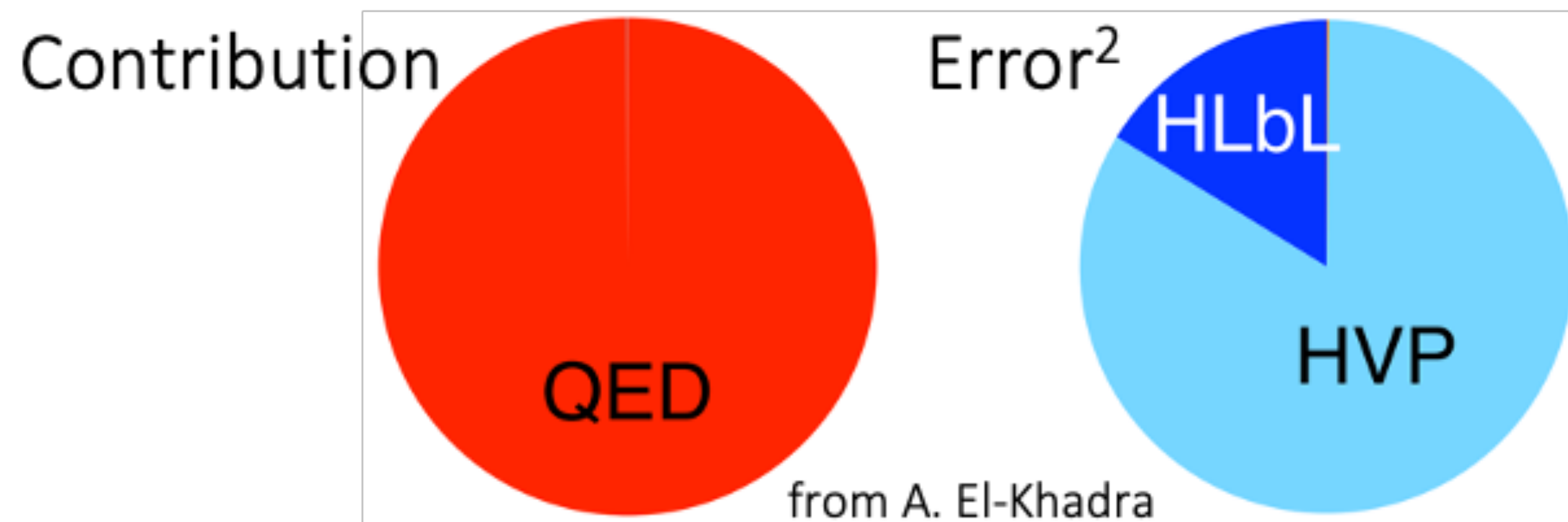
Muon $g-2$ Theory Initiative



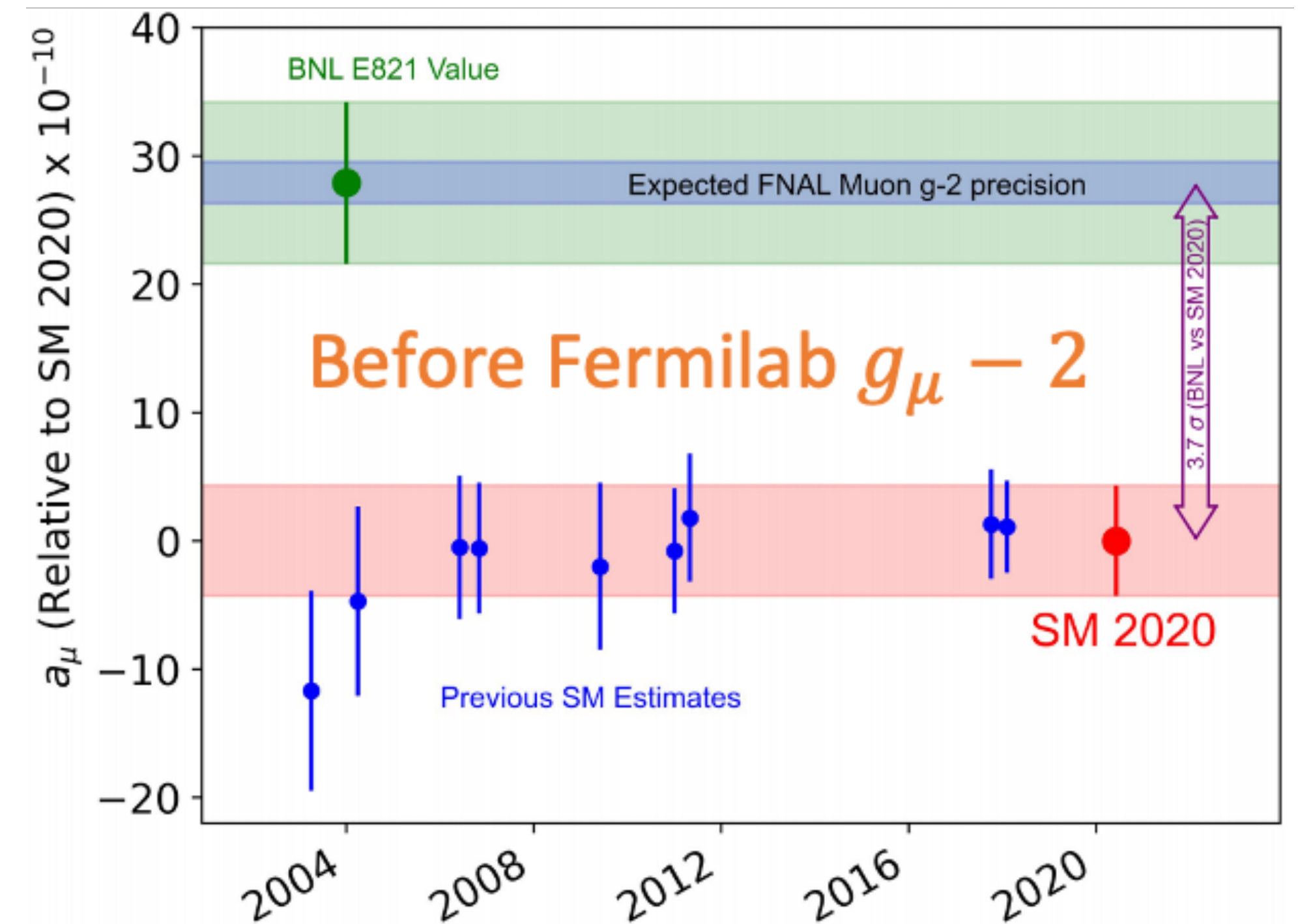
- Group of scientists working to compile all inputs to Standard Model prediction of the muon magnetic anomaly
- Published a White Paper in 2020 White Paper: Phys. Rept. 887 (2020) 1-166
<https://doi.org/10.1016/j.physrep.2020.07.006>

Theory prediction

- **SM value** is dominated by QED contributions, over 99.99% of total
- But, **uncertainty** is dominated by Hadronic contributions, which are notoriously difficult to calculate: hadronic light-by-light (HLbL) and hadronic vacuum polarization (HVP)

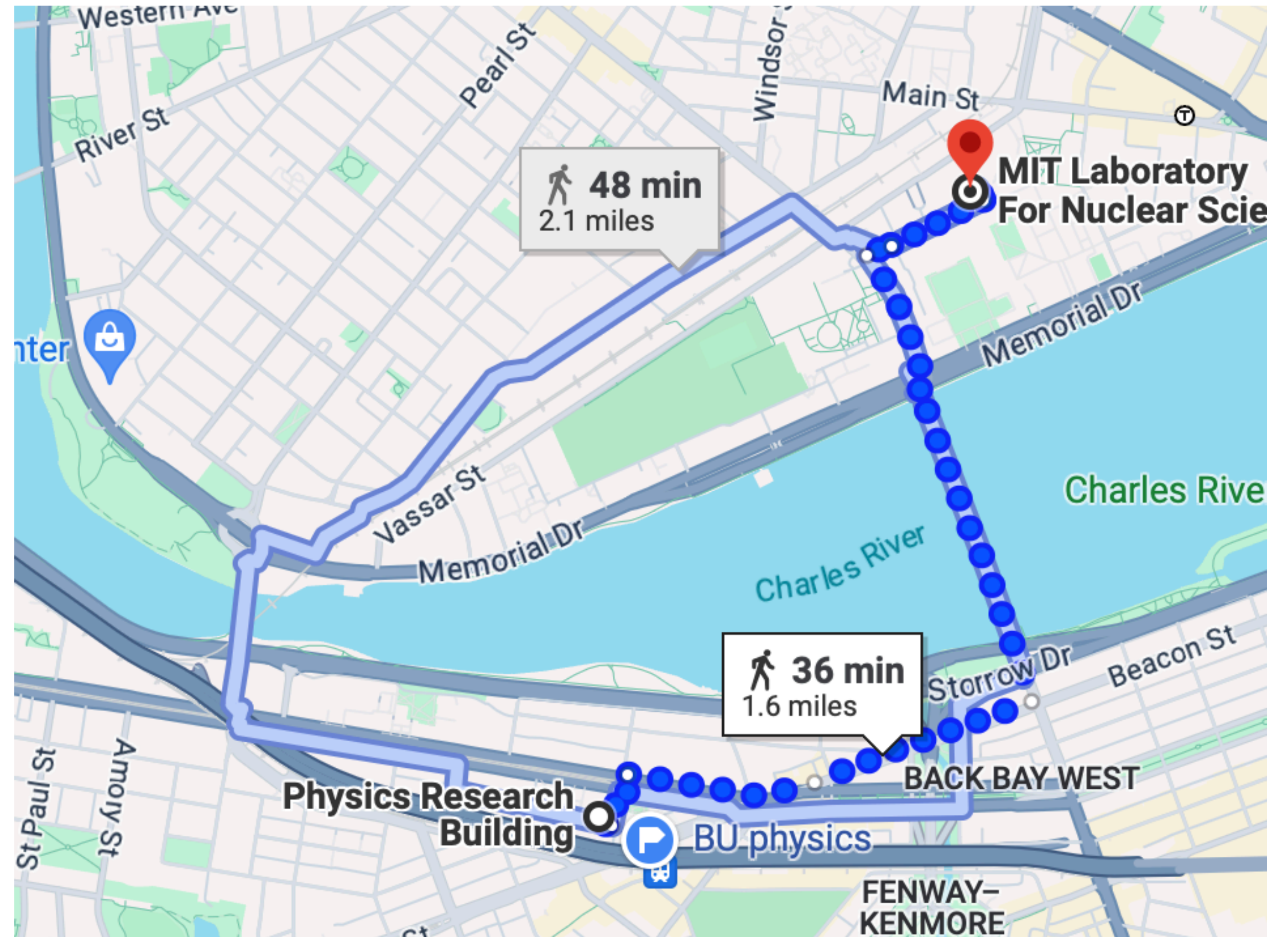


White Paper uncertainty: 369 ppb



How precise is 369 ppb?

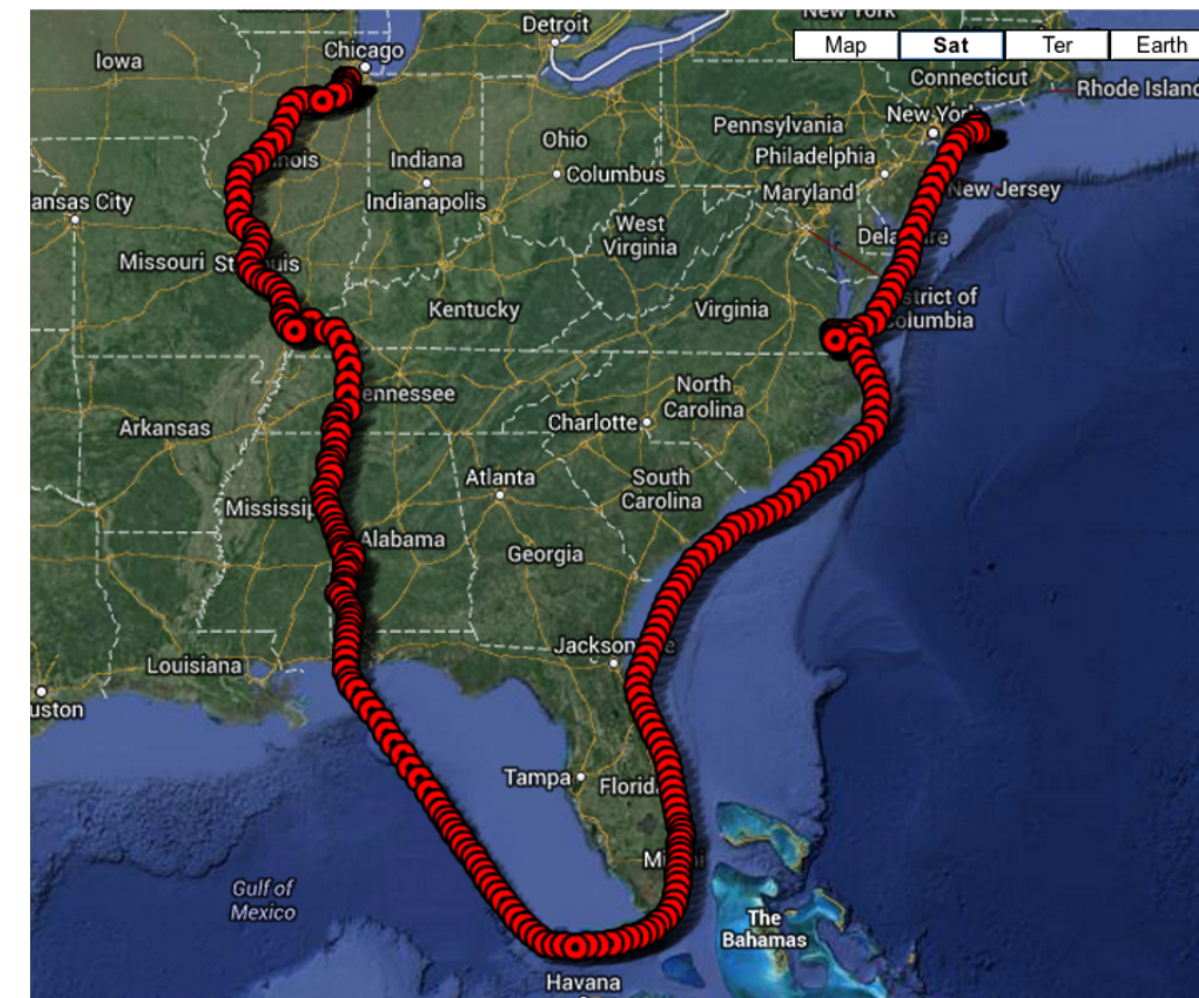
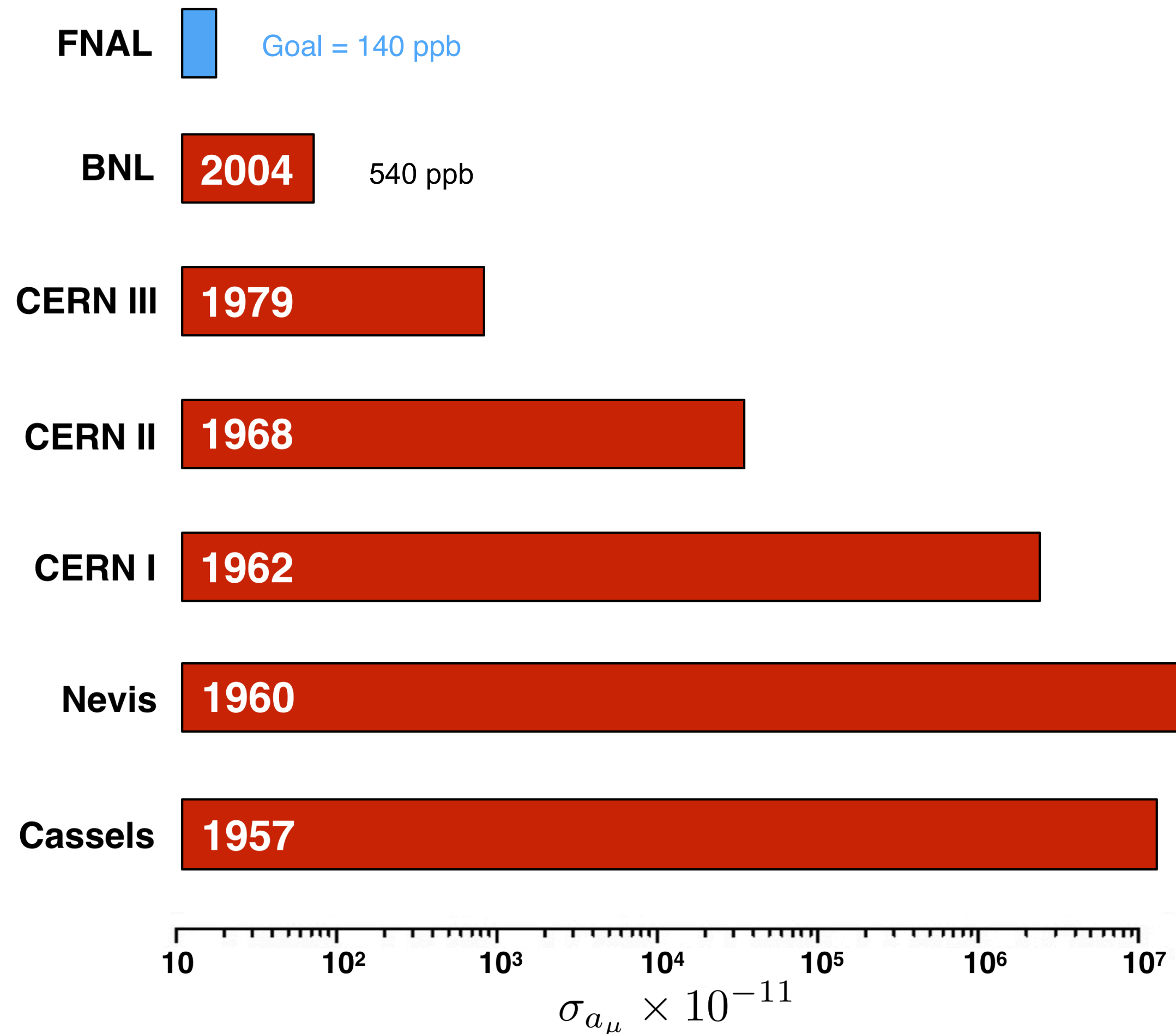
- I went to BU for my PhD and the physics department is about a 1.6 mile walk from here
- If I wanted to precisely determine that distance to 369 ppb: get it right to **1 mm!**
- 369 ppb sets scale for what experiment should achieve



Fermilab experiment continues the effort

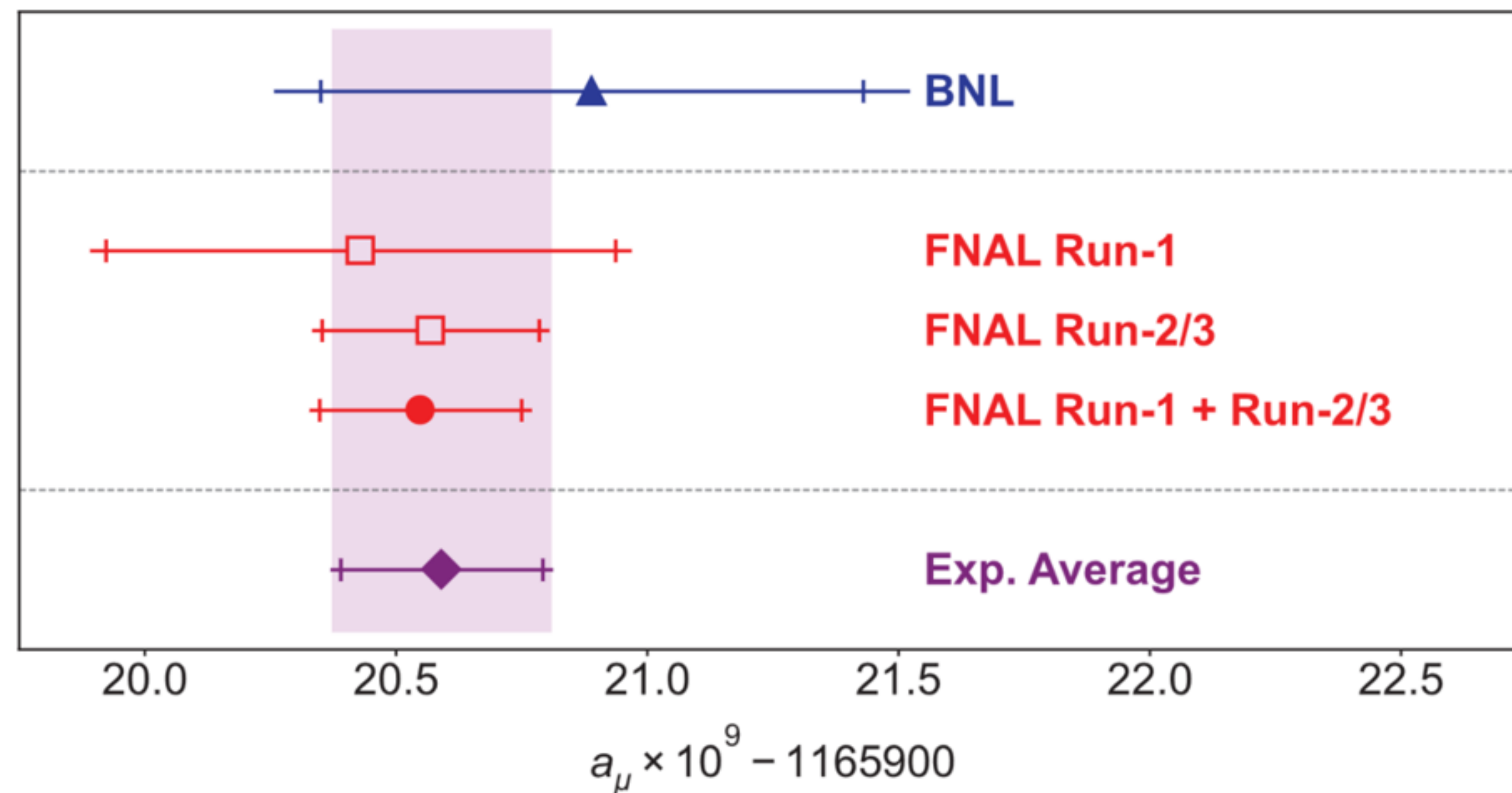
- 60+ year history of measuring muon g-2
- Previous experiment took place at Brookhaven National Lab (BNL)
- Fermilab experiment uses the same magnet -> the big move!

Experiment



Fermilab results from first 3 Runs

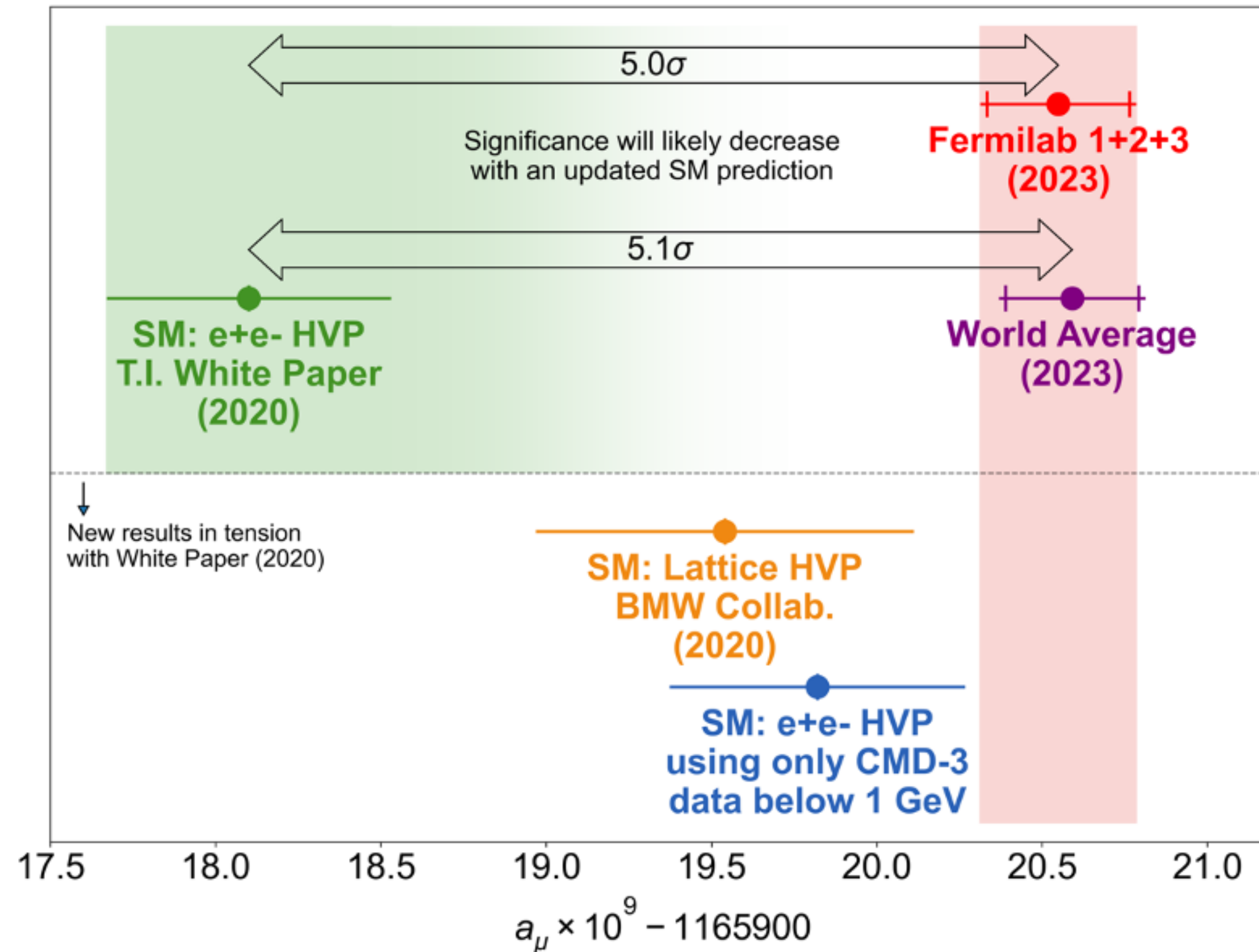
- First result (2021) based on Run-1 data: comparable uncertainty & consistent with BNL
- Second result (2023) based on Run-2/3 data: reduced uncertainty by x2 and consistent again!



$$a_\mu(\text{Exp}) = 0.00116592059(22) \text{ [190 ppb]}$$

PRL 126, 141801 (2021)
PRL 131, 161802 (2023)
Published yesterday! PRD 110, 032009 (2024)

Compare to theory after our Run-2/3 result



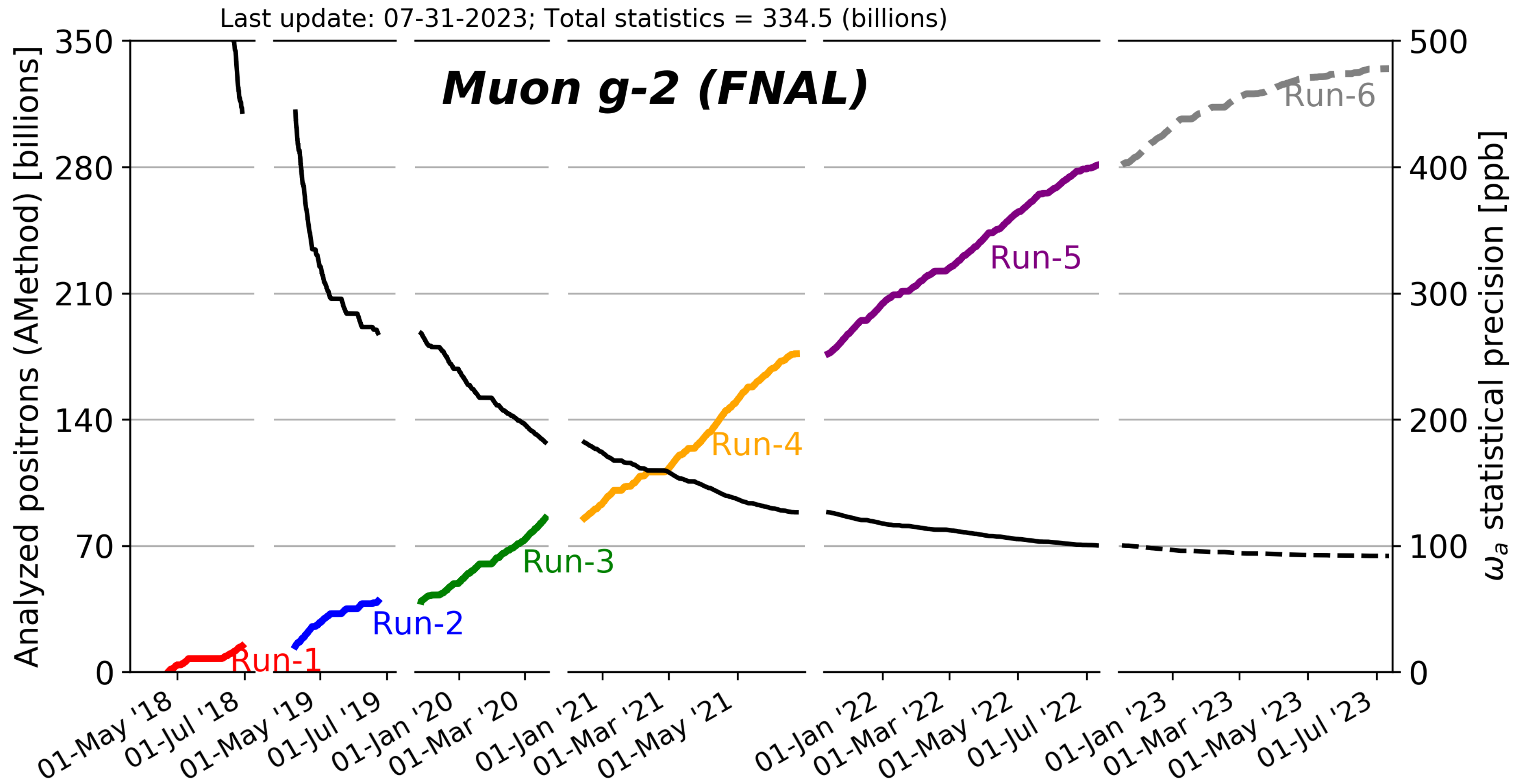
- Since theory White Paper, new results for HVP contributions
- Different methods disagree with each other
- Two methods are a **dispersive approach** (used in White Paper) and **lattice QCD**
- Theory initiative working to understand these tensions
- For now, hard to draw conclusions

*Disclaimer from A. Keshavarzi's Lattice 2023 talk:

IMPORTANT: THIS PLOT IS VERY ROUGH!

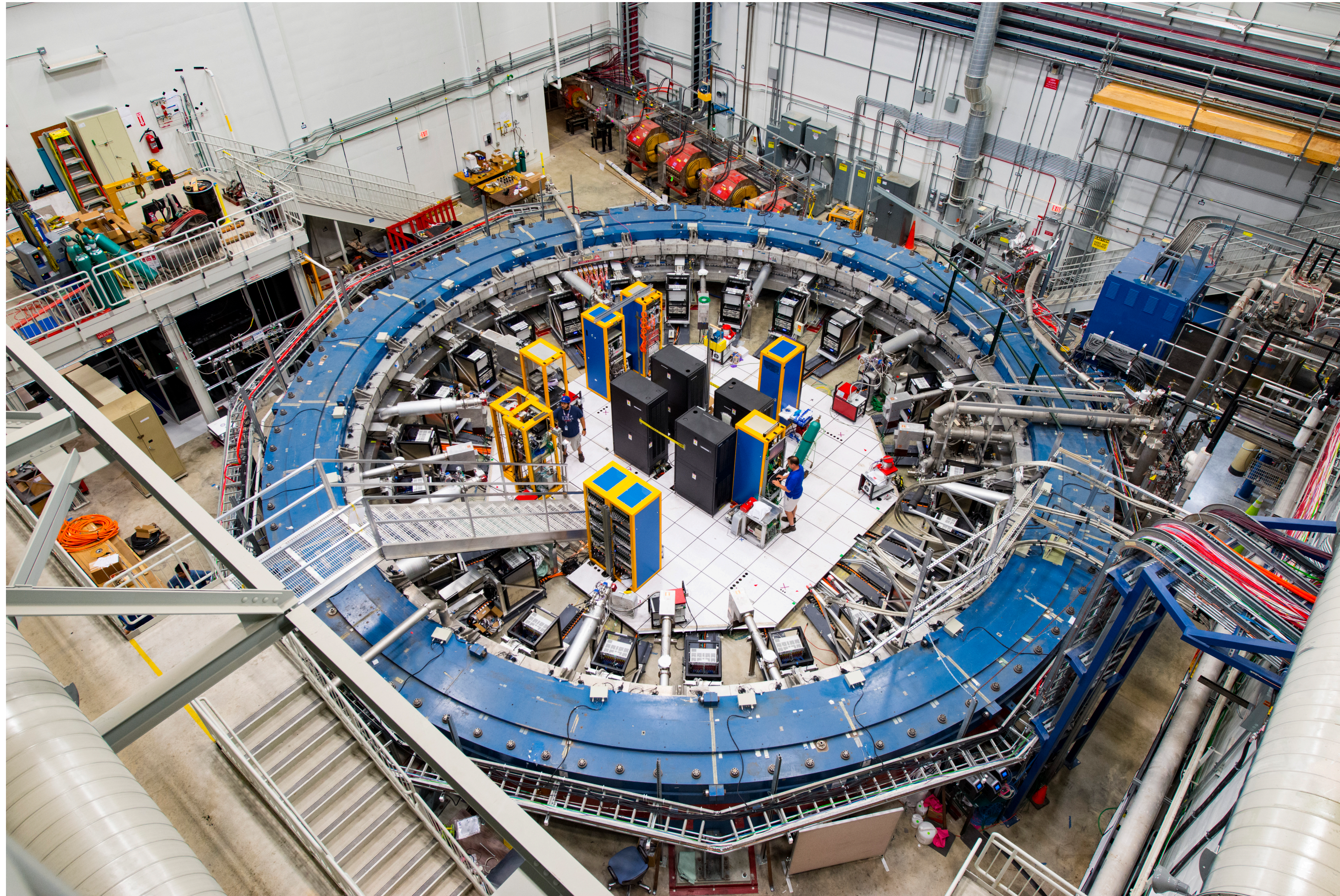
- T.I. White Paper result has been substituted by CMD-3 only for 0.33 \rightarrow 1.0 GeV.
- The NLO HVP has not been updated.
- It is purely for demonstration purposes \rightarrow should not be taken as final!

We surpassed goal of x21 statistics of BNL

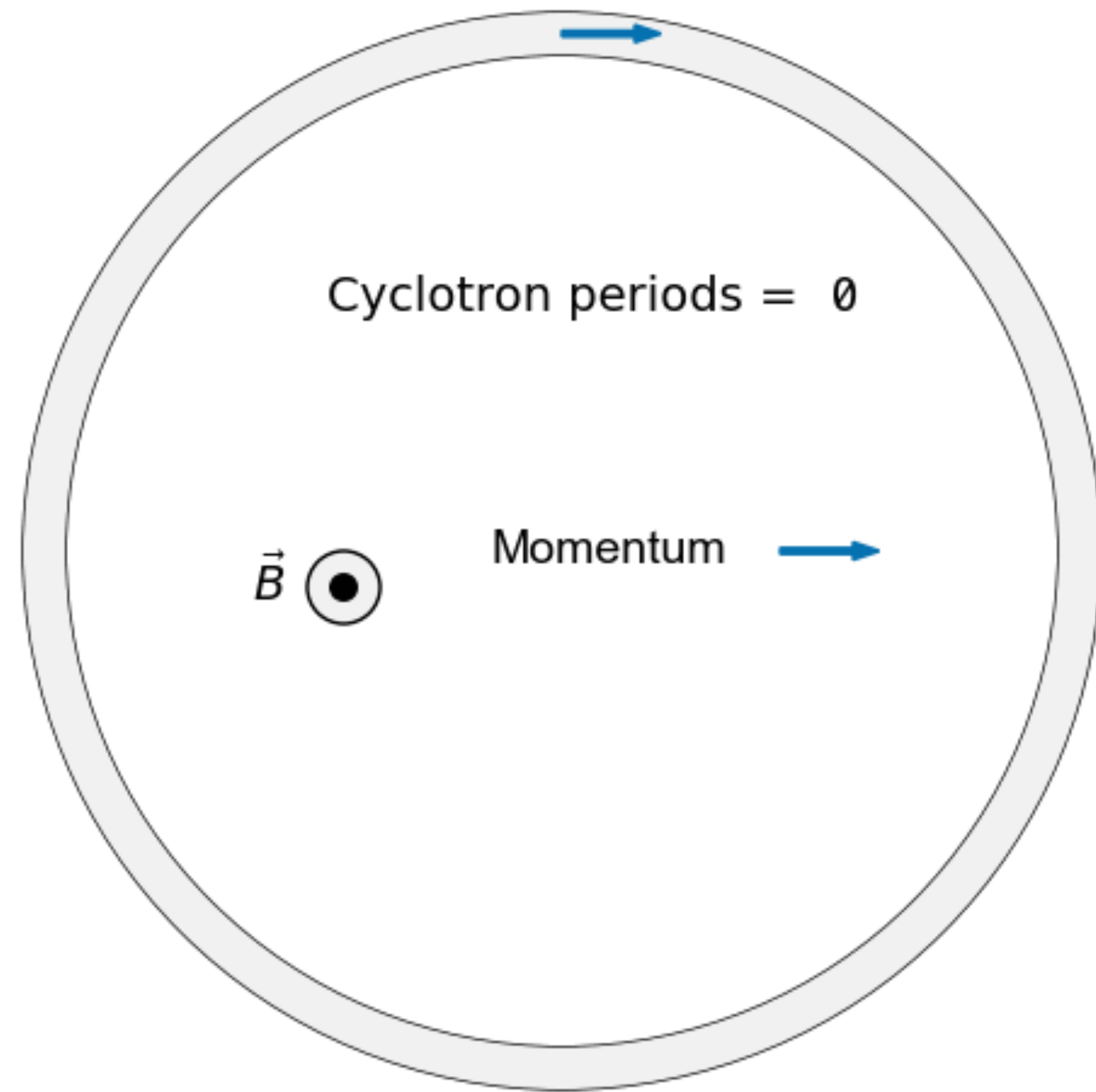


- Completed data collection in June 2023
- Reached TDR goal
- **Run-4/5/6:** analysis underway, expected to surpass target of 140 ppb
- Last result anticipated in 2025

Measurement details



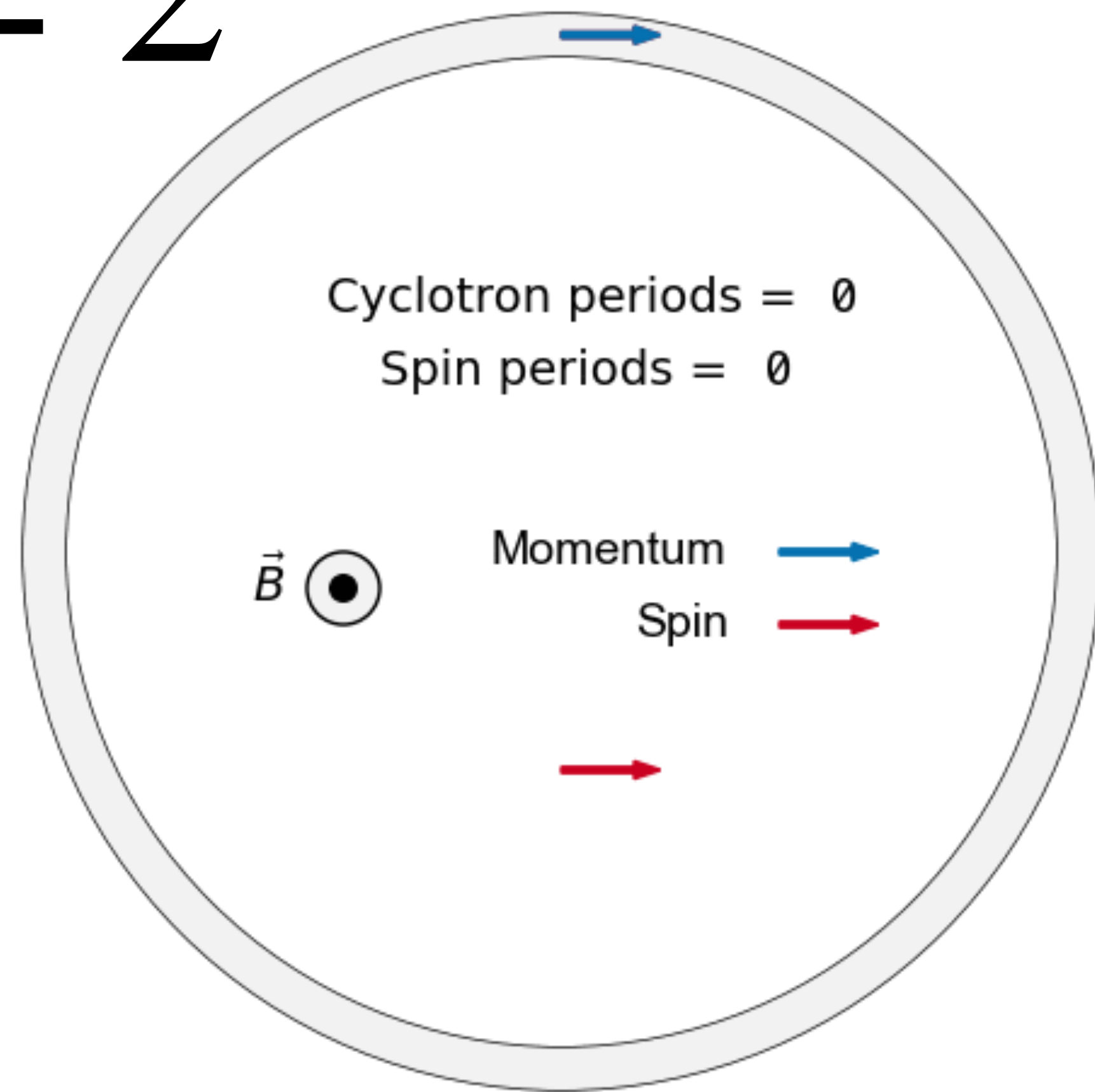
Place muon in a magnetic field



- Momentum vectors rotates at \rightarrow cyclotron frequency $\propto B$

If $g = 2$ (not our universe!)

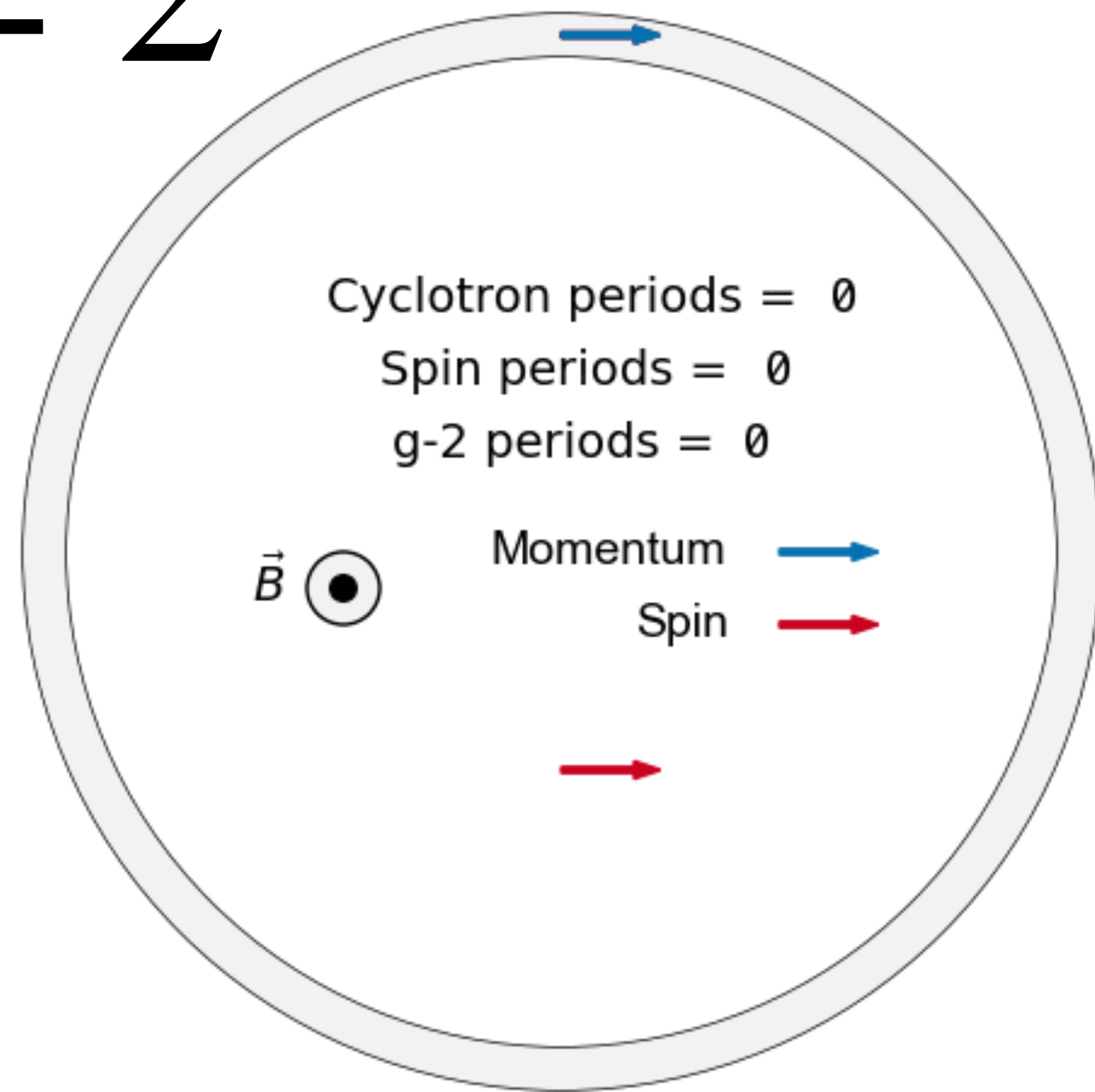
$$g = 2$$



- Momentum vectors rotates at cyclotron frequency $\propto B$
- Spin precession is $\propto B$ and g (want to measure this!)

If $g \neq 2$ (our universe!)

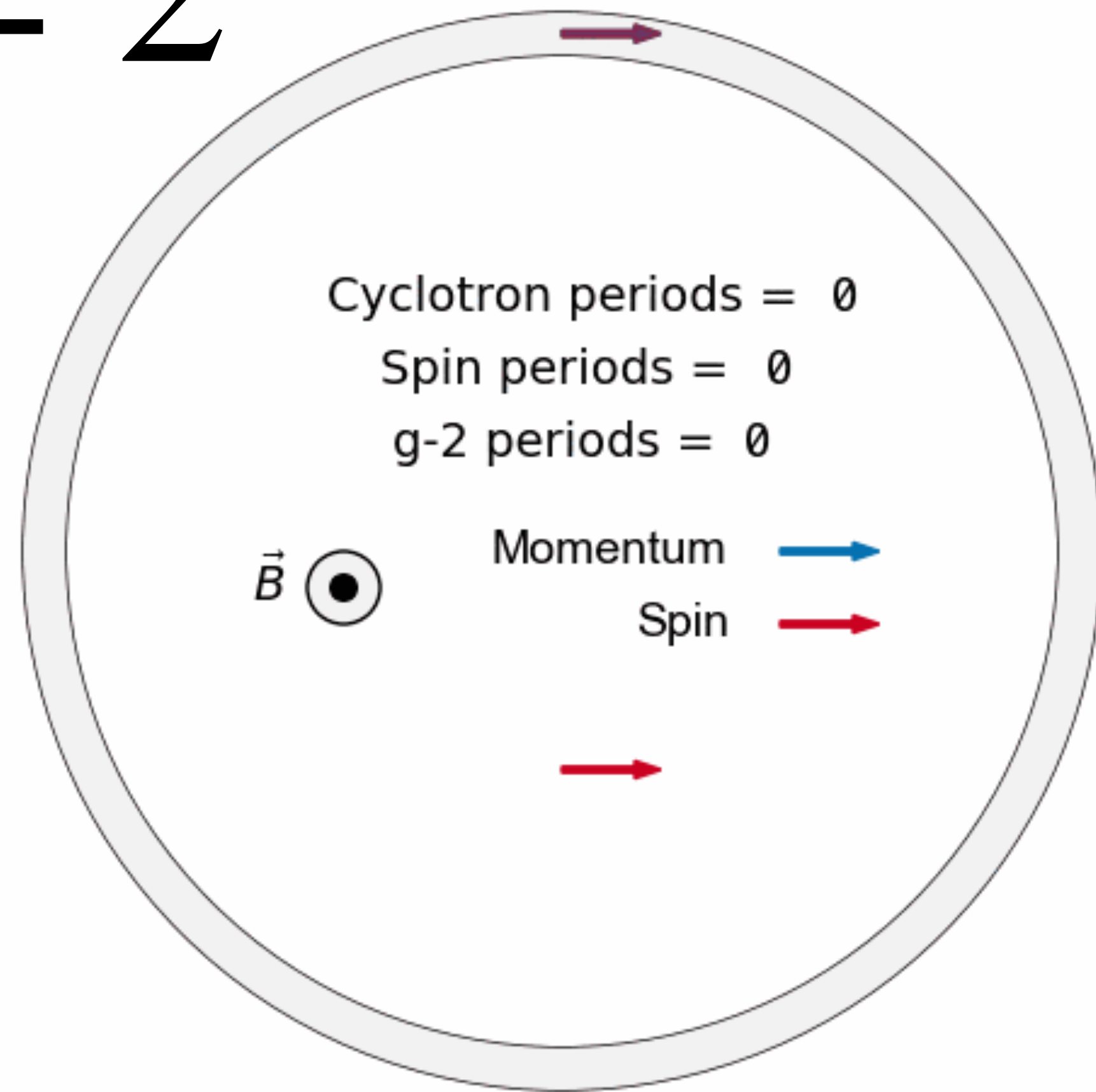
$g \neq 2$



- Momentum vectors rotates at cyclotron frequency $\propto B$
- Spin precession is $\propto B$ and g (want to measure this!)

Difference frequency \propto anomaly

$$g \neq 2$$

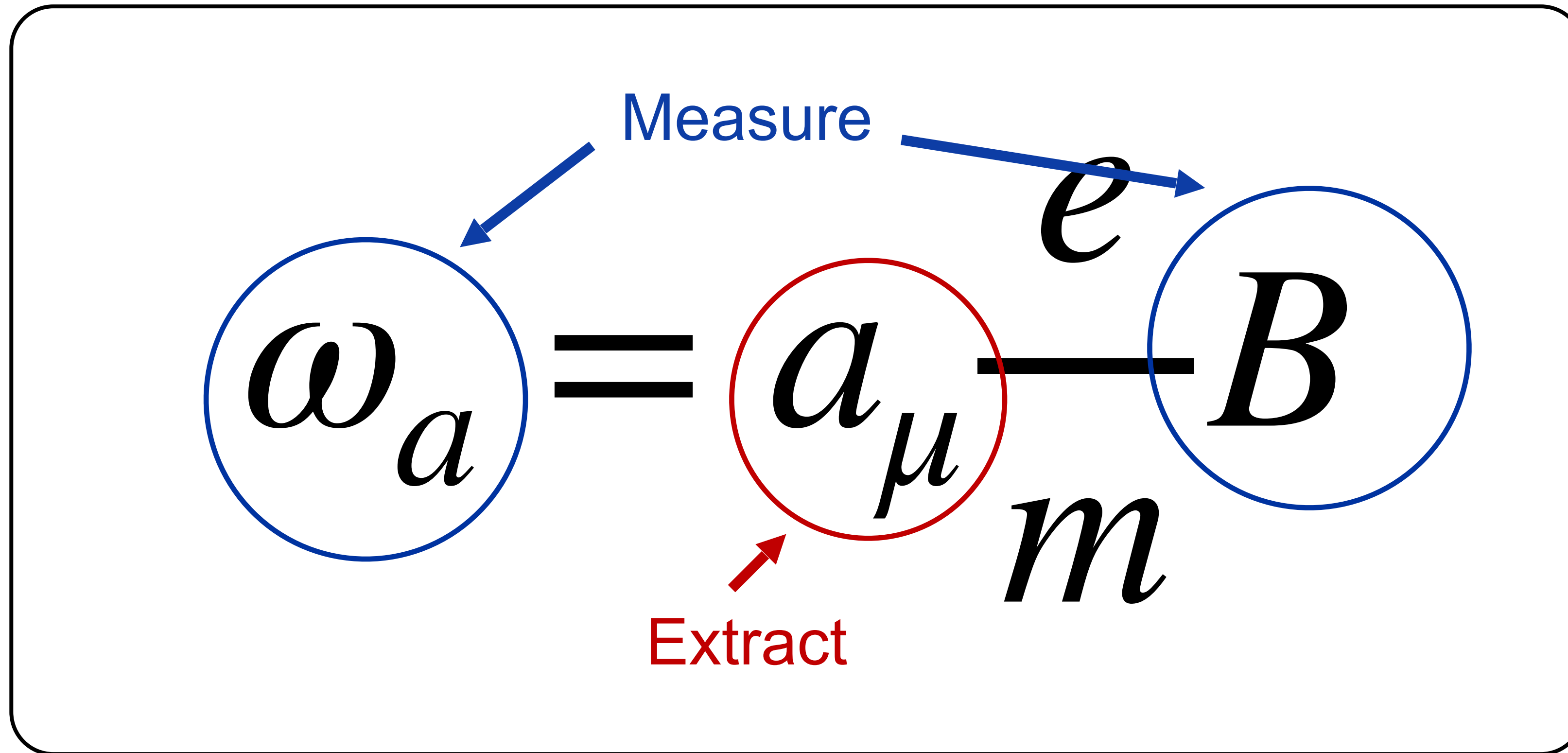


- **Difference frequency \propto anomaly!**

$$\omega_a = a_\mu \frac{e}{m} B$$

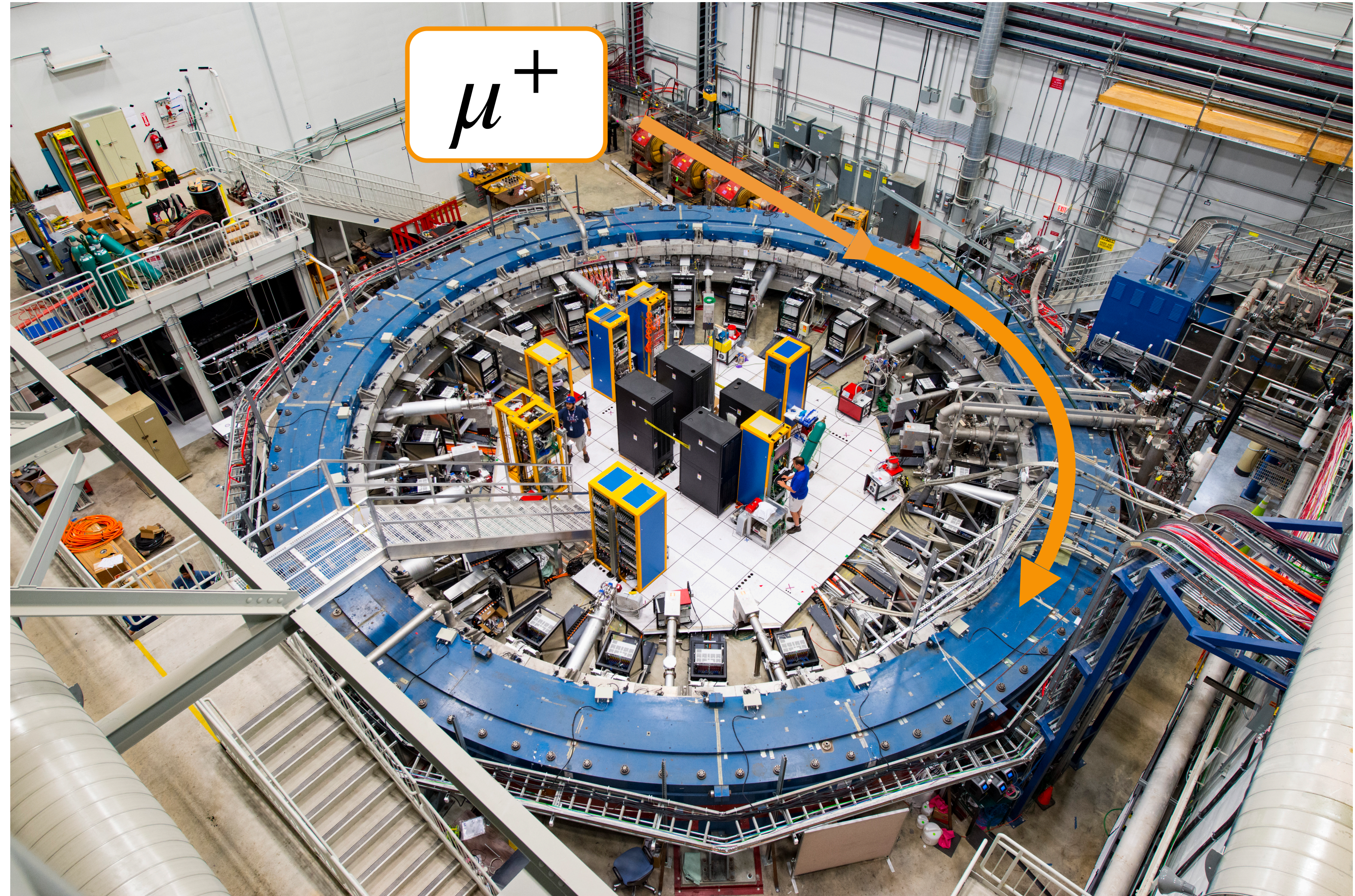
- At **fixed locations** around ring, spins rotate at ω_a

Measurement recipe



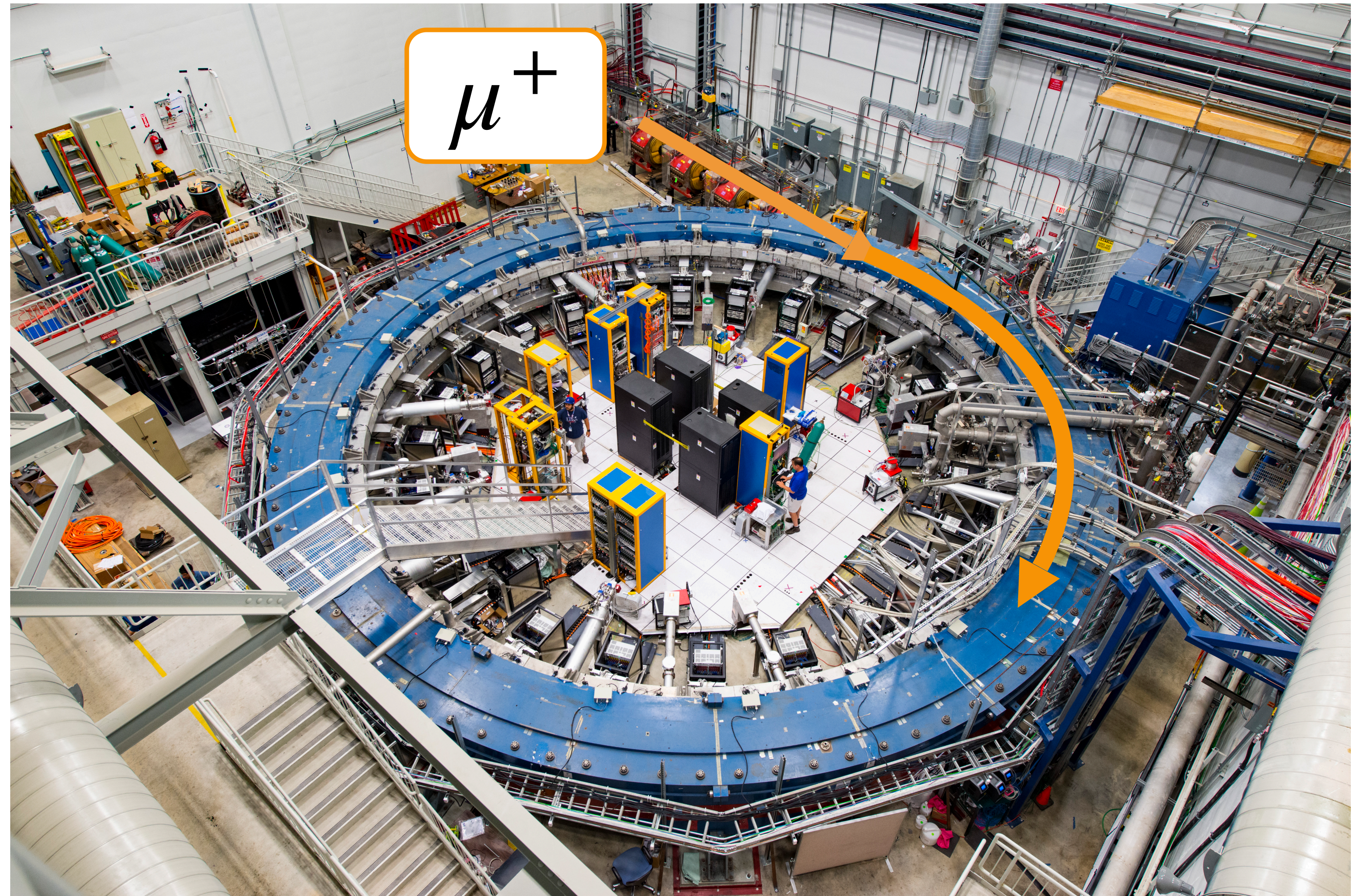
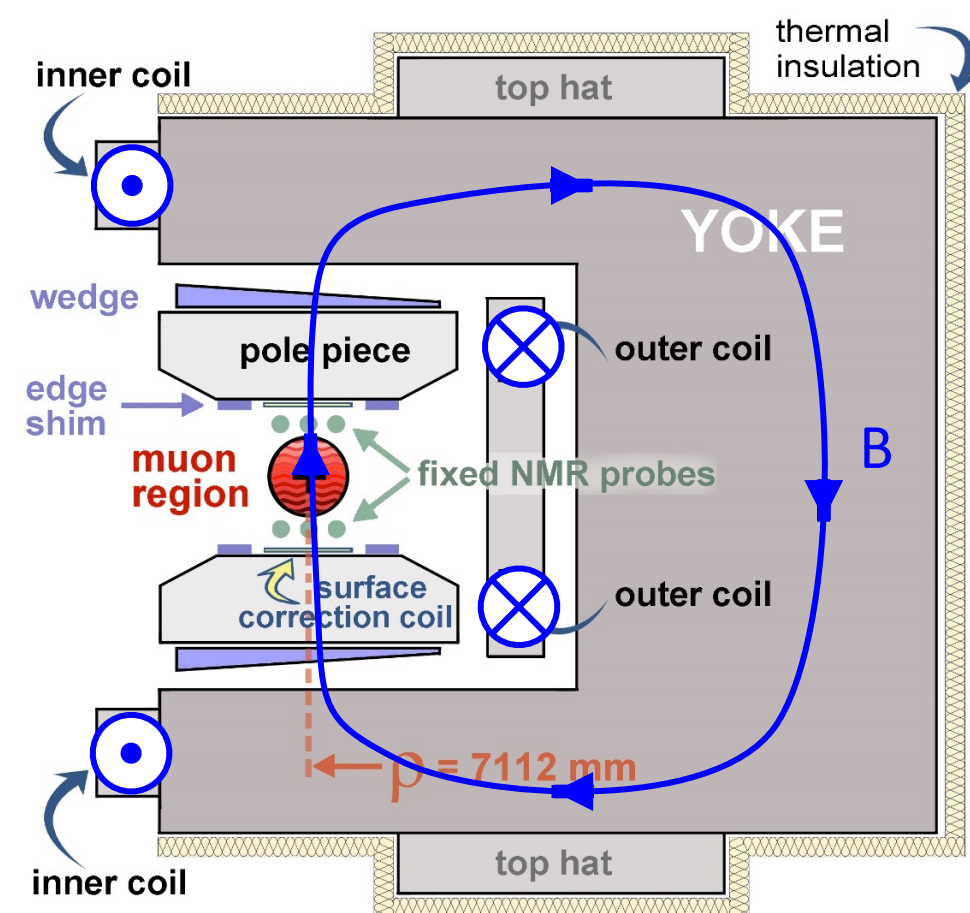
Experiment at Fermilab: Beam

- Polarized muons from pion decay
- Momentum selected to ~ 3.1 GeV/c
- Stored muons are within $dp/p \sim 0.1\%$
- Average rate of 11.4 “fills” per second
- ~ 120 ns wide pulses
- $\sim 10,000$ stored muons per fill
- Each fill lasts about 1 ms



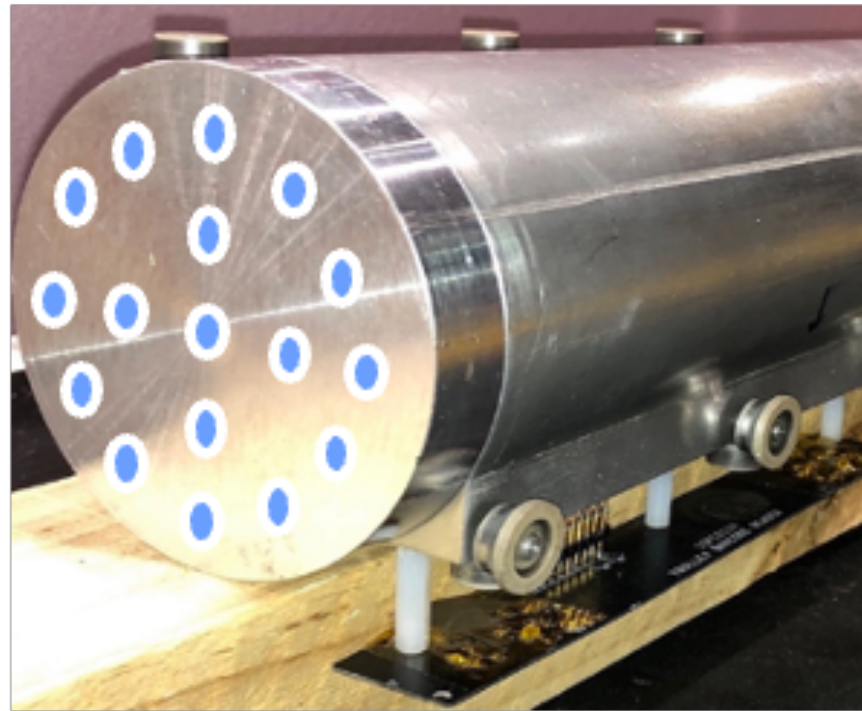
Experiment at Fermilab: Storage Ring Magnet

- 7.112 meter radius superconducting storage ring magnet
- 1.45 T uniform field
- Muons precess in the magnetic field

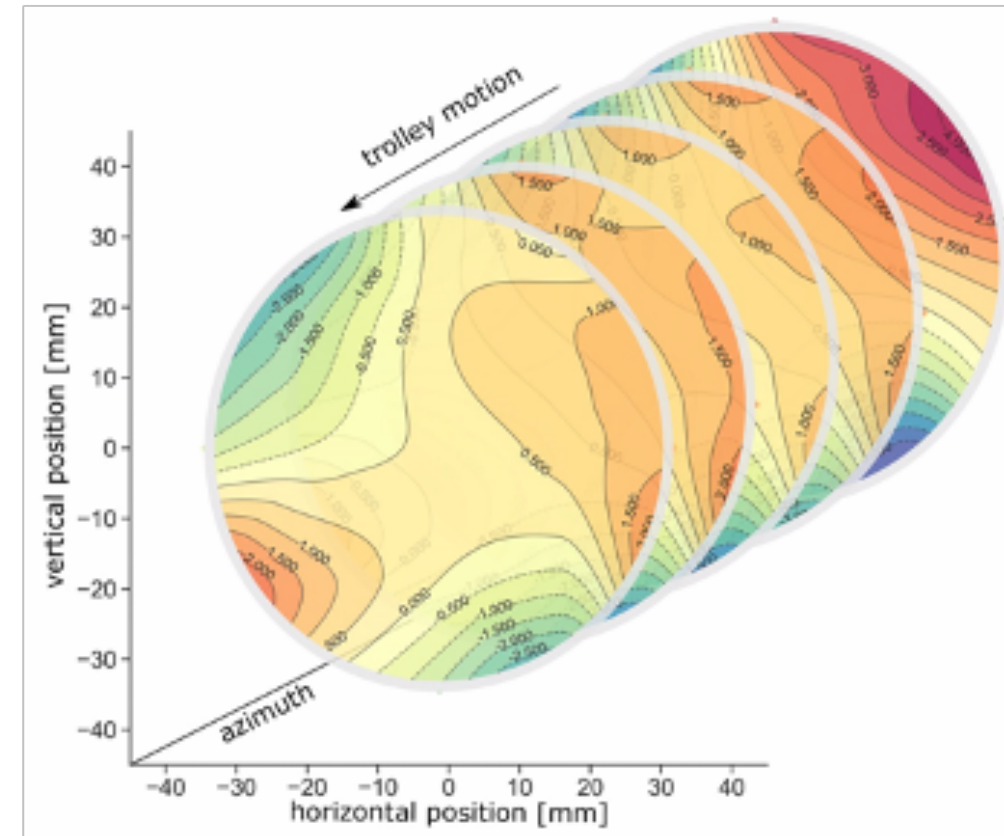


Field Measured with NMR

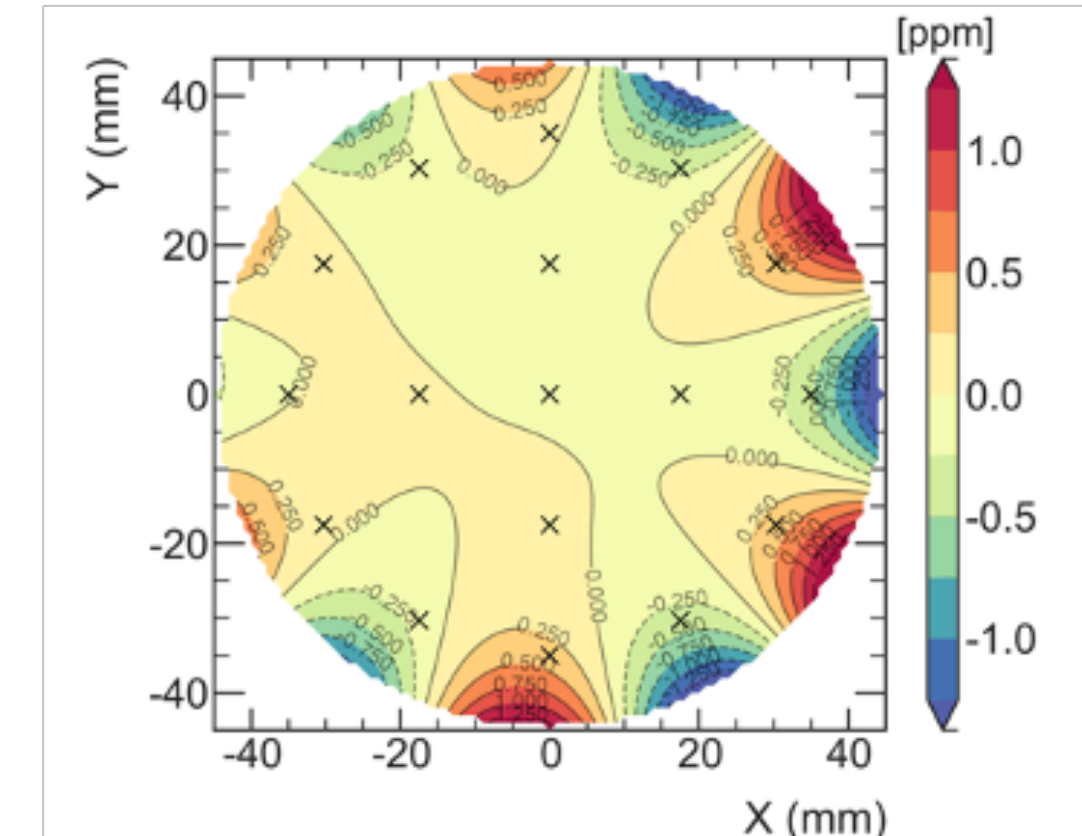
- Use proton nuclear magnetic resonance (NMR) to measure B-field (also a precession frequency!)



17 petroleum jelly NMR probes

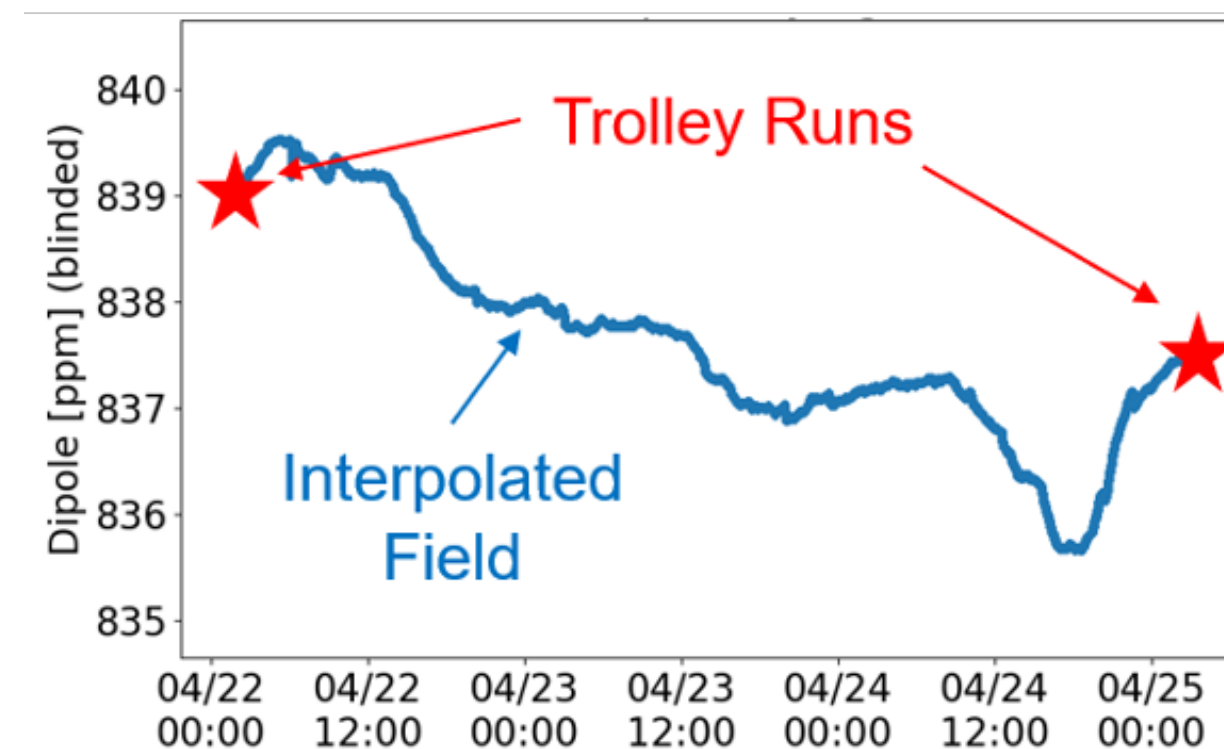
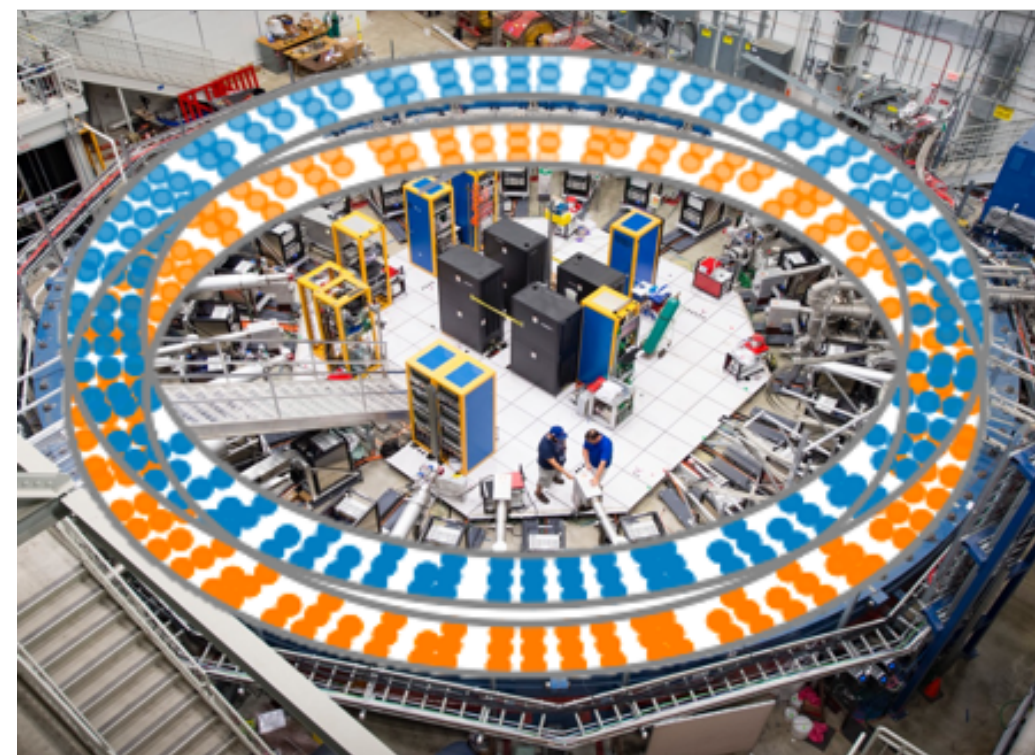


2D field maps (~8000 points)



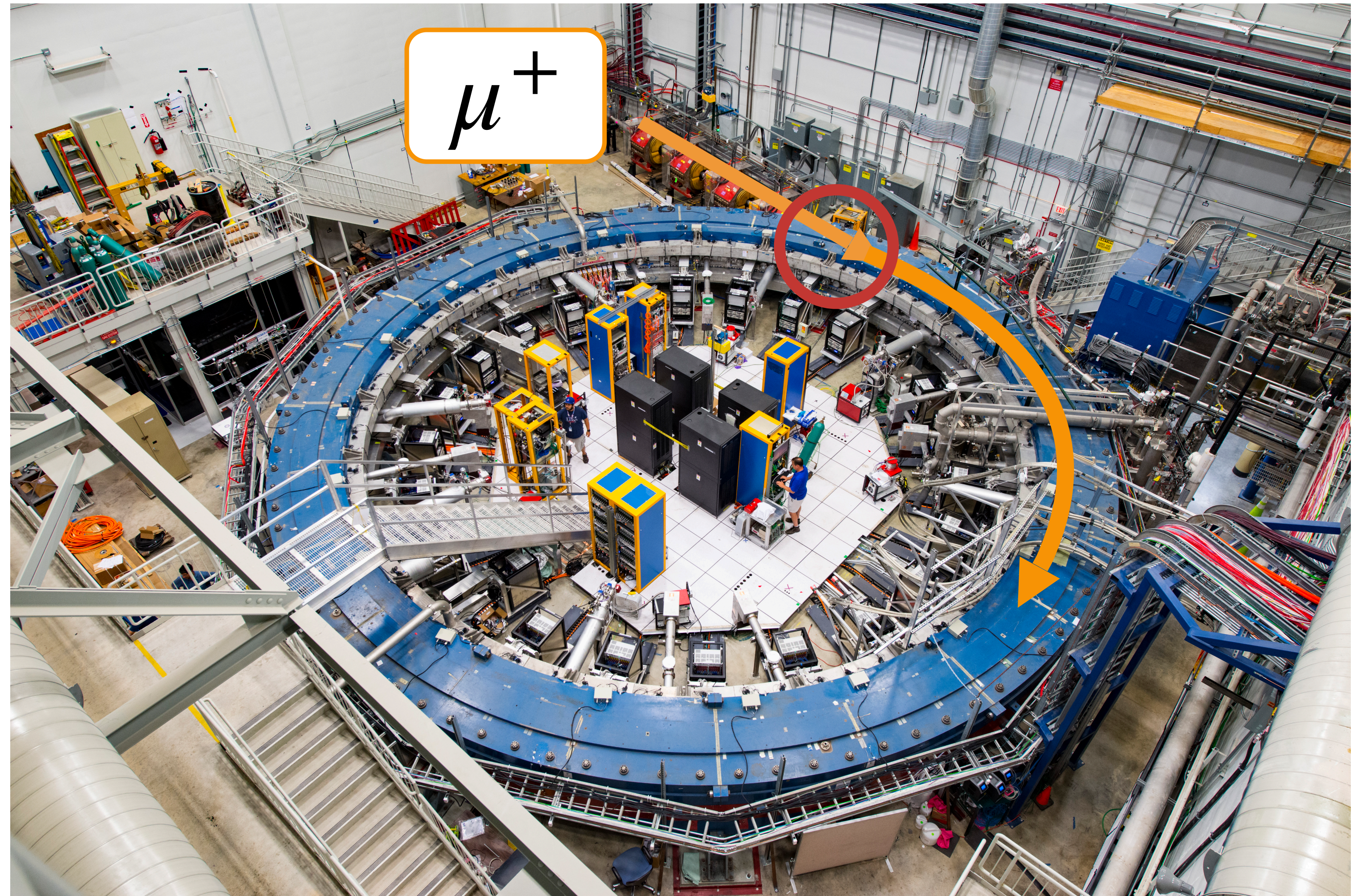
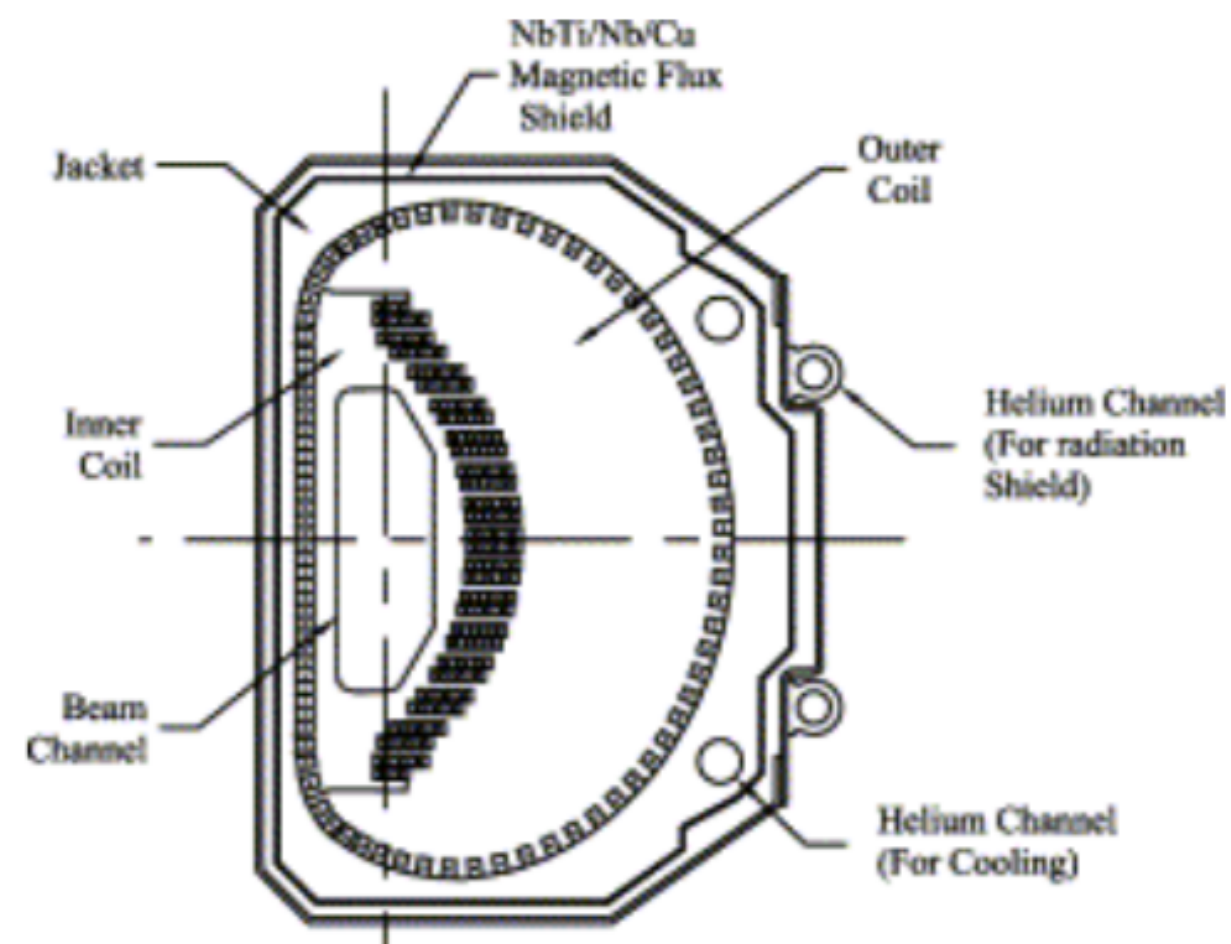
Azimuthally-Averaged
Variation < 1 ppm

Fixed probes
above/below muon
storage region



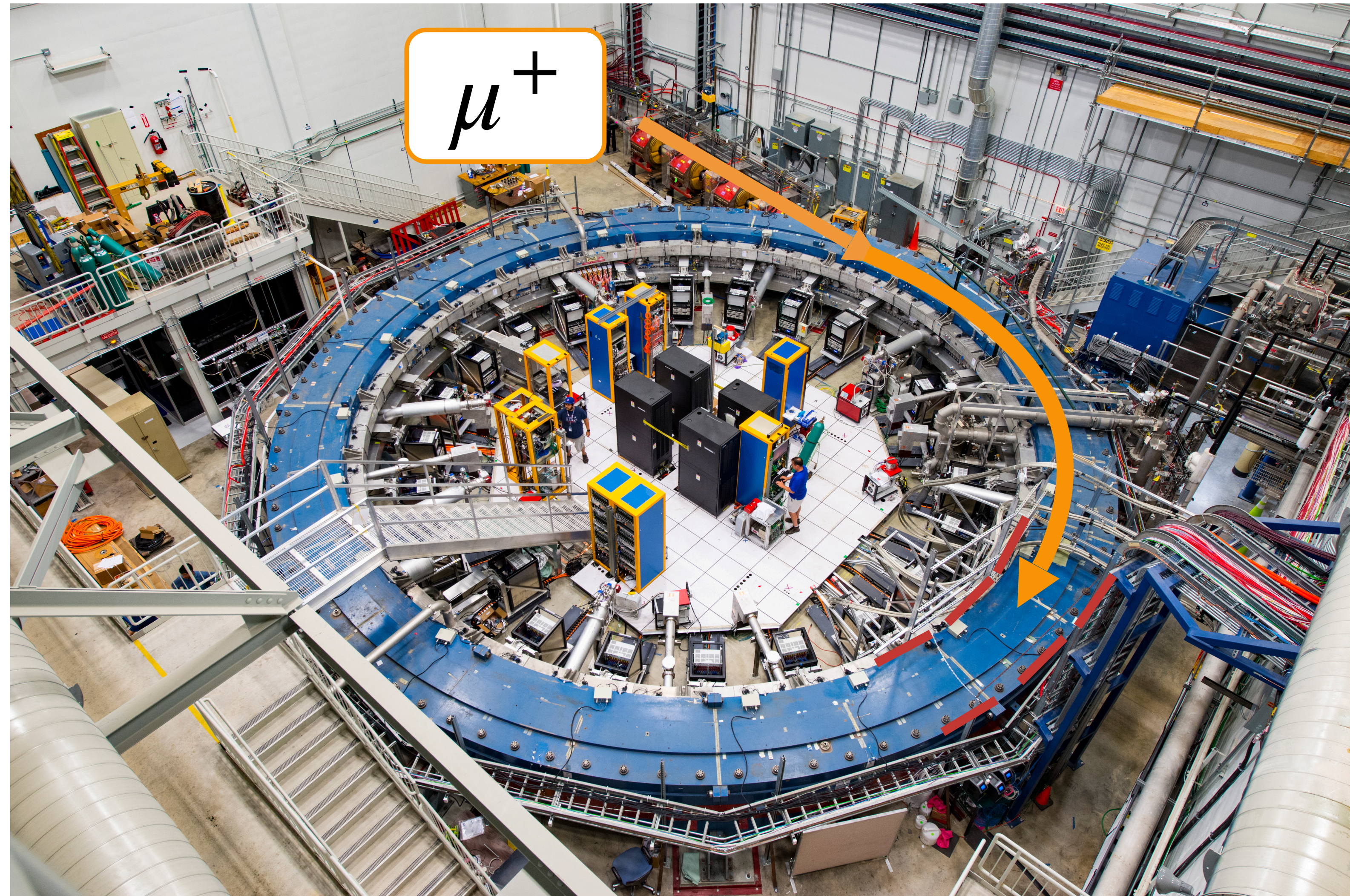
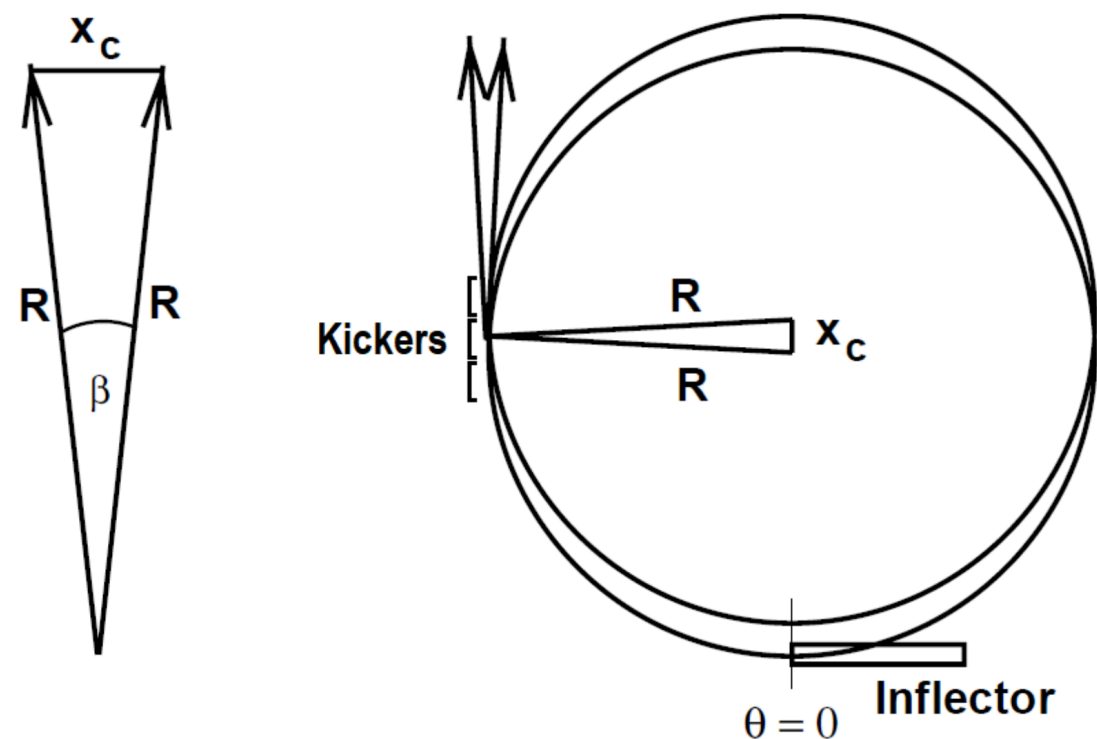
Experiment at Fermilab: Injection

- Muons injected through hole in backleg of the magnet
- Inflector magnet cancels main field to allow muons straight path into the ring



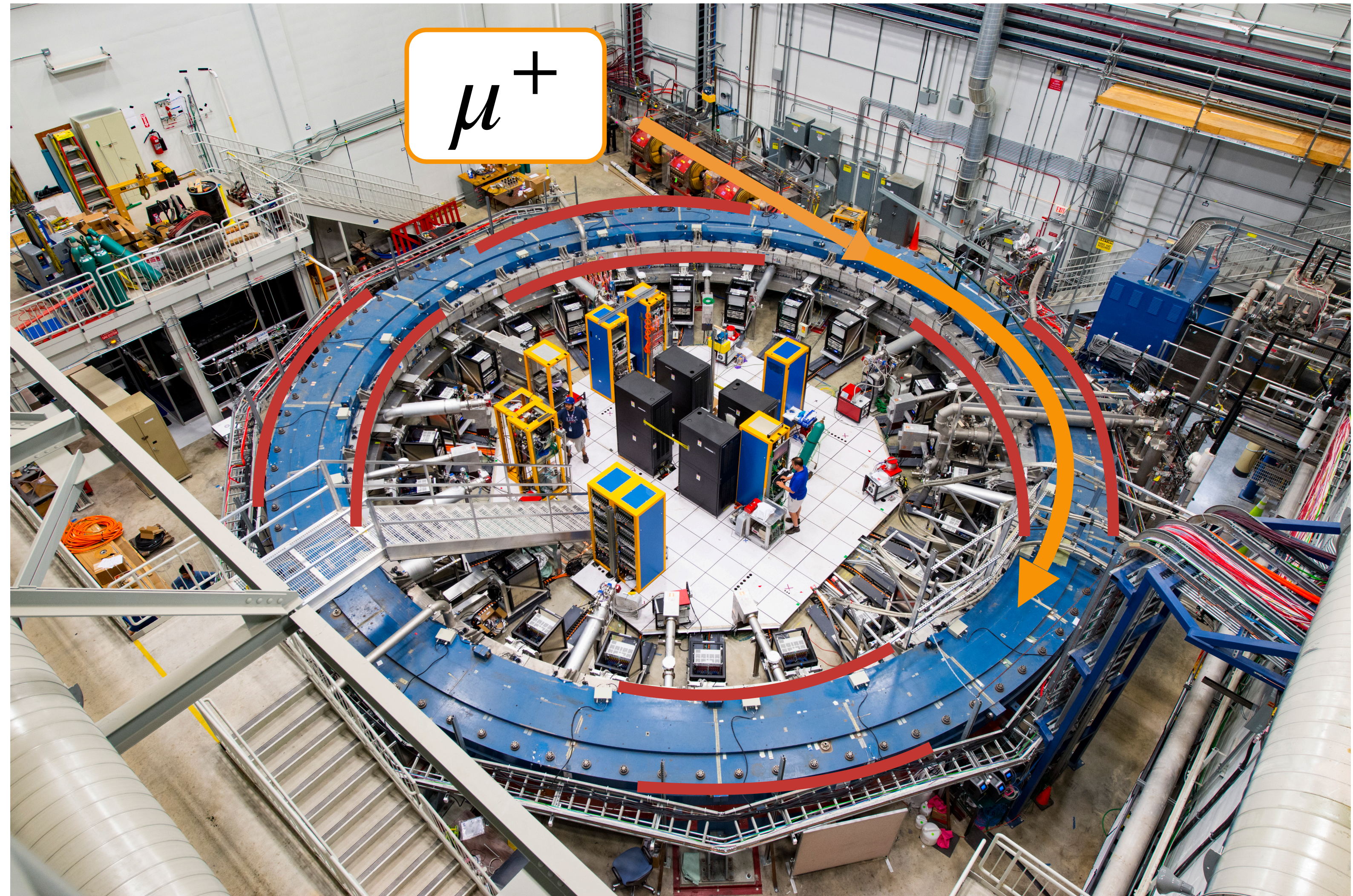
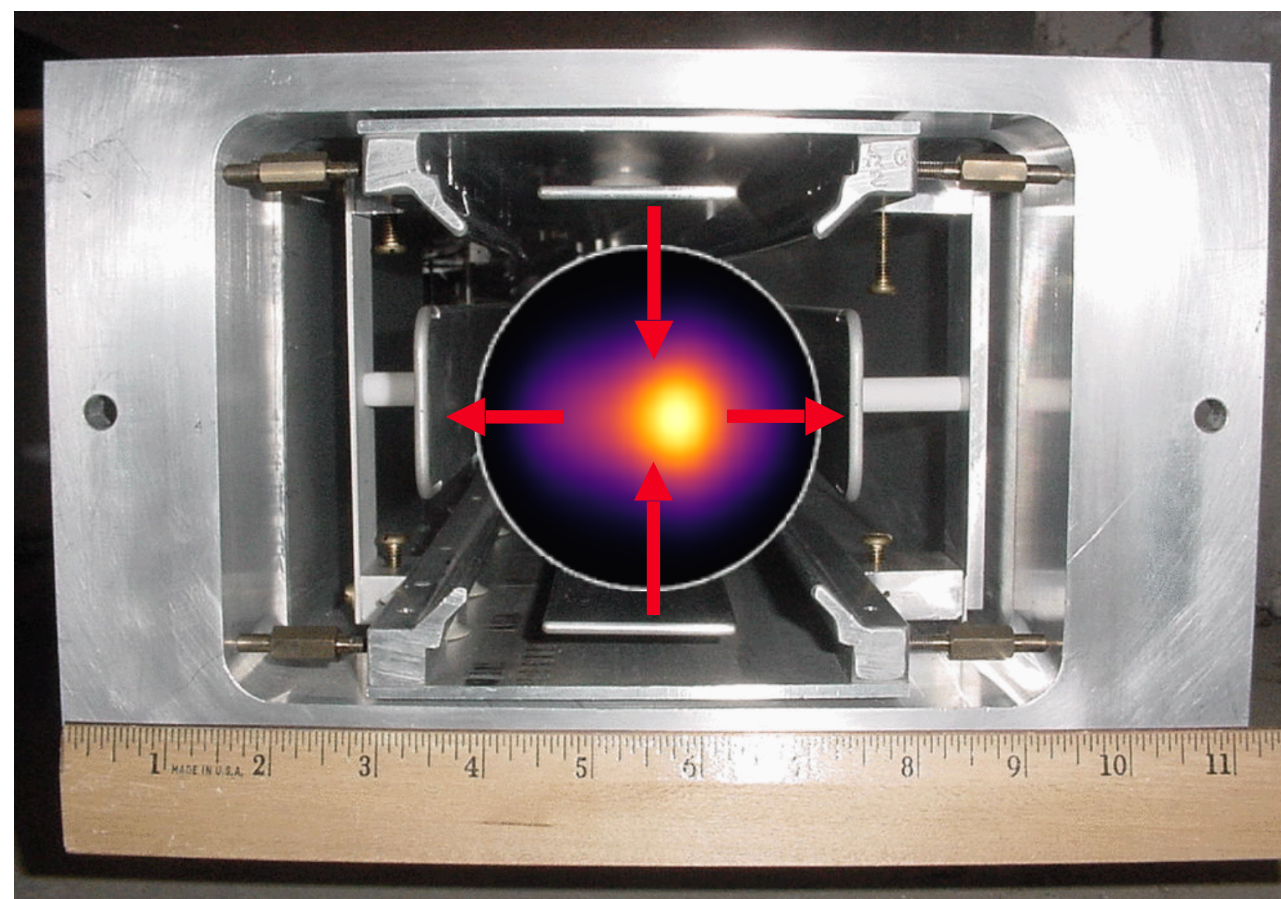
Experiment at Fermilab: Kickers

- Muons initial phase space not matched to ring admittance
- Needs ~ 10 mrad radial “kick” to get onto design orbit
- Kick achieved with **three** fast kicker magnets, 90 degrees from injection



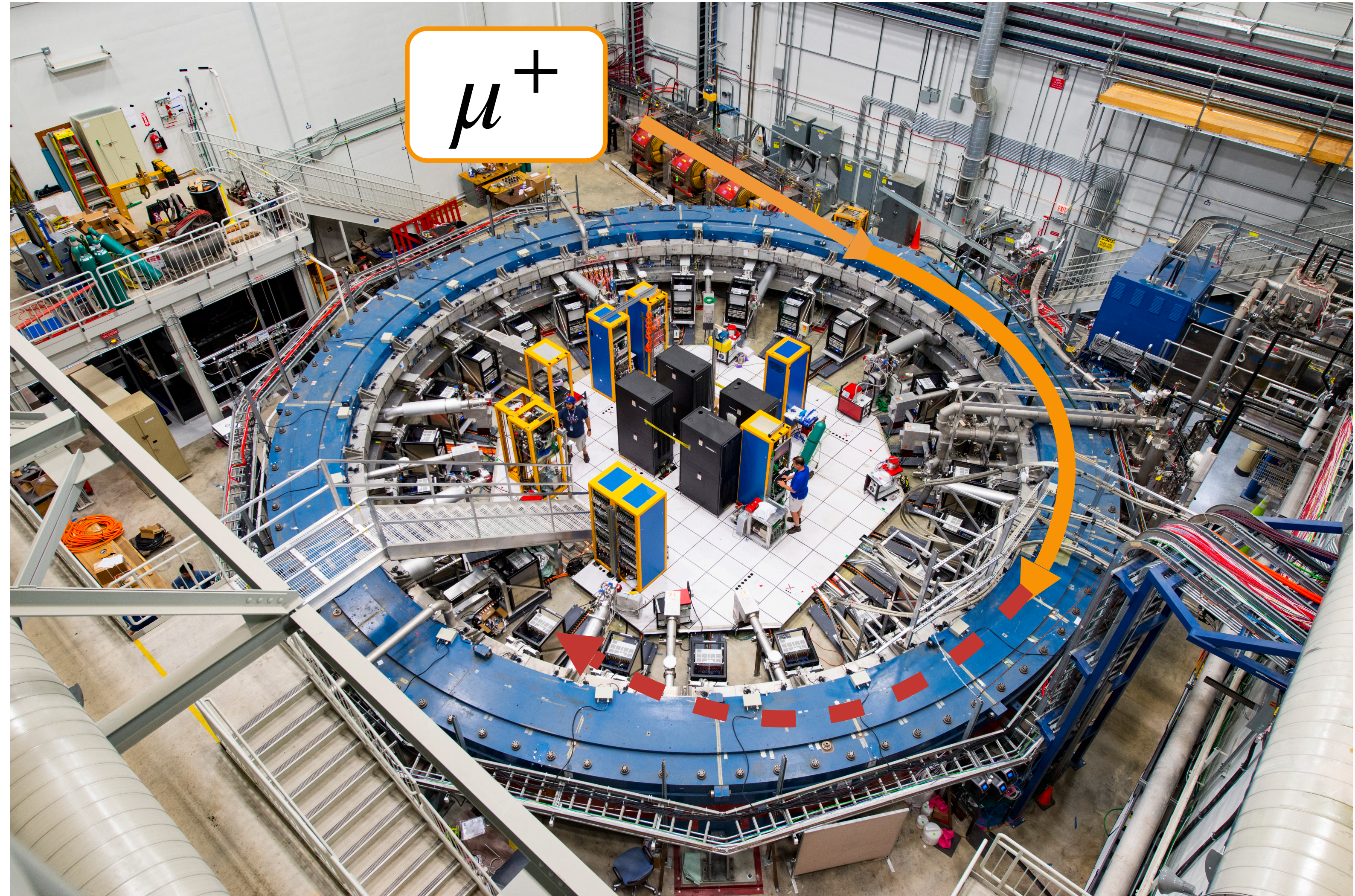
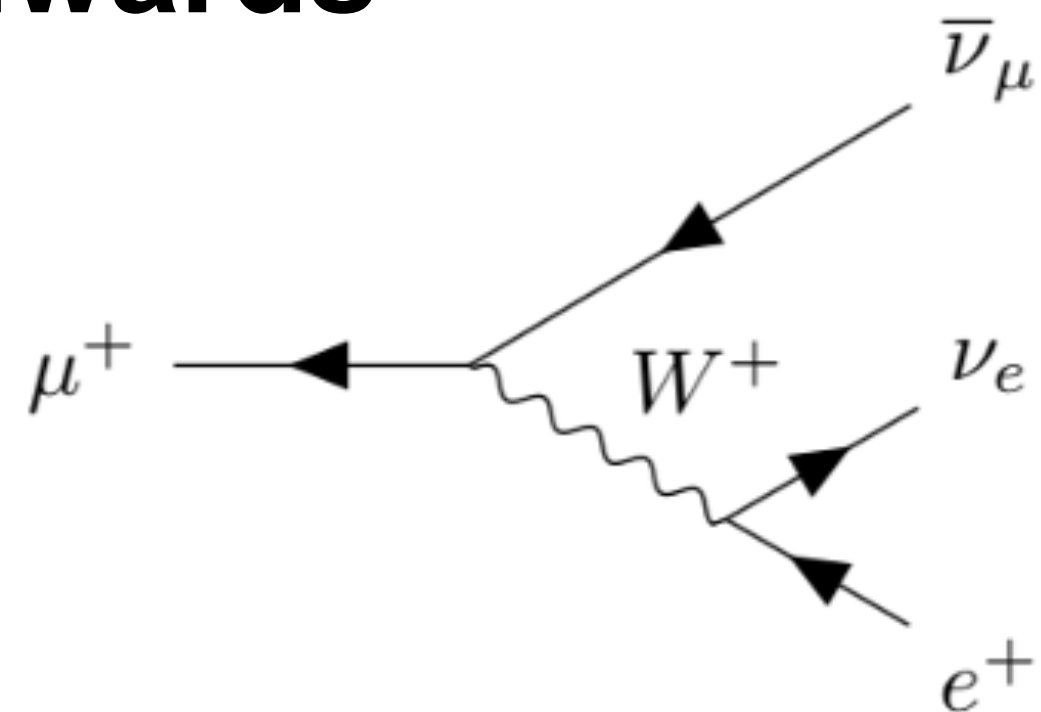
Experiment at Fermilab: Quadrupoles

- Vertical focusing achieved with electrostatic quadrupoles
- Spans ~43% of the ring azimuth, symmetrically
- E and B fields lead to betatron motion; muon beam “swims” around the storage region radially and vertically



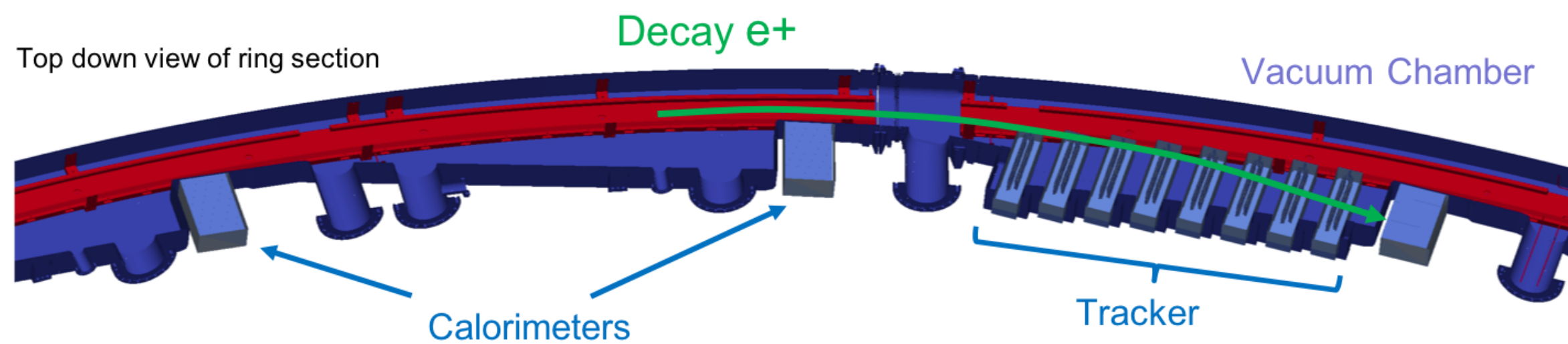
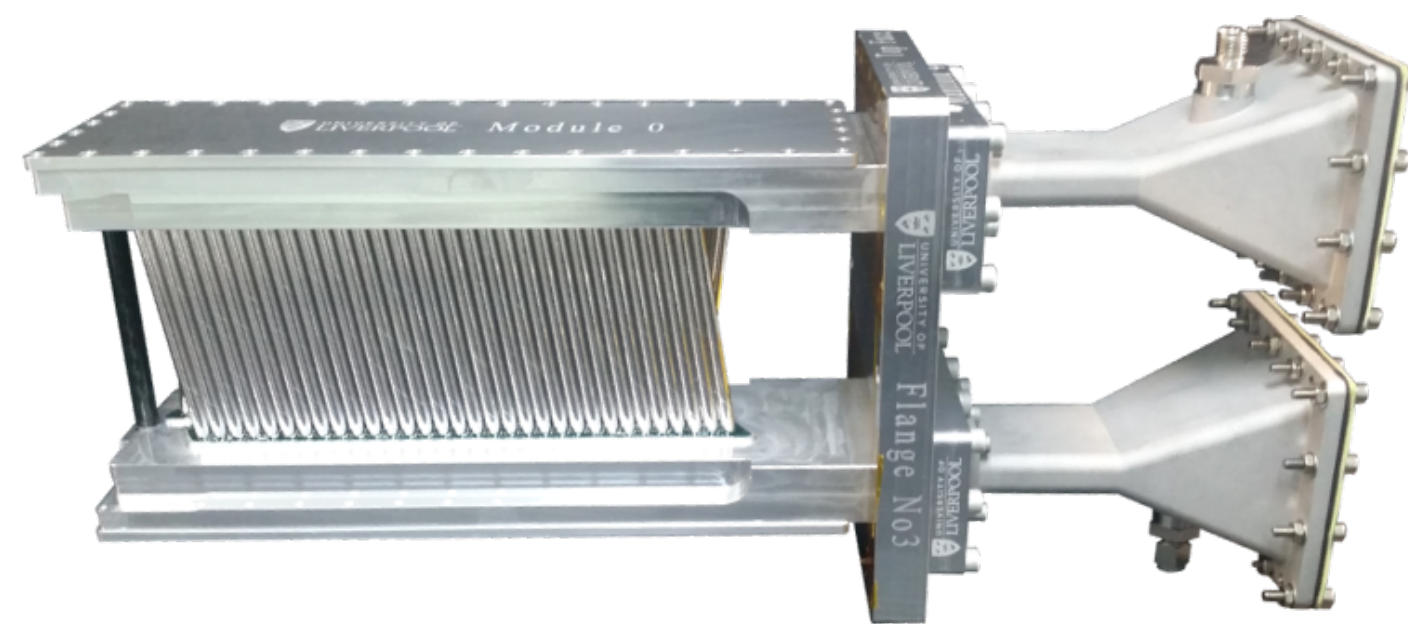
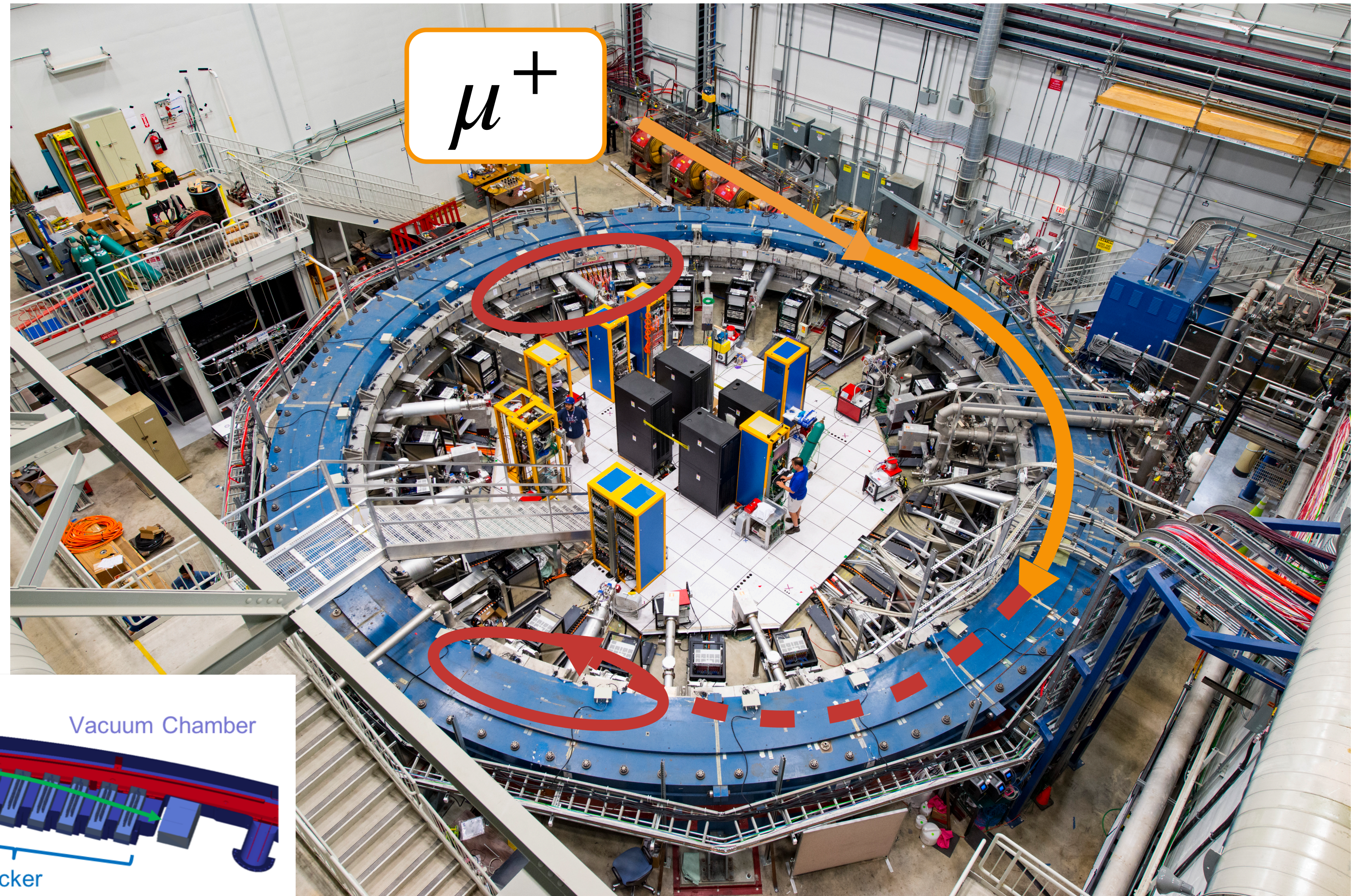
Experiment at Fermilab: Storage & Decay

- At this point, muons are stored and importantly the spins are precessing!
- With a momentum of ~ 3.1 GeV/c, our muons have a boosted lifetime $\sim 64\mu\text{s}$
- Then, they decay and **decay positron spirals inwards**



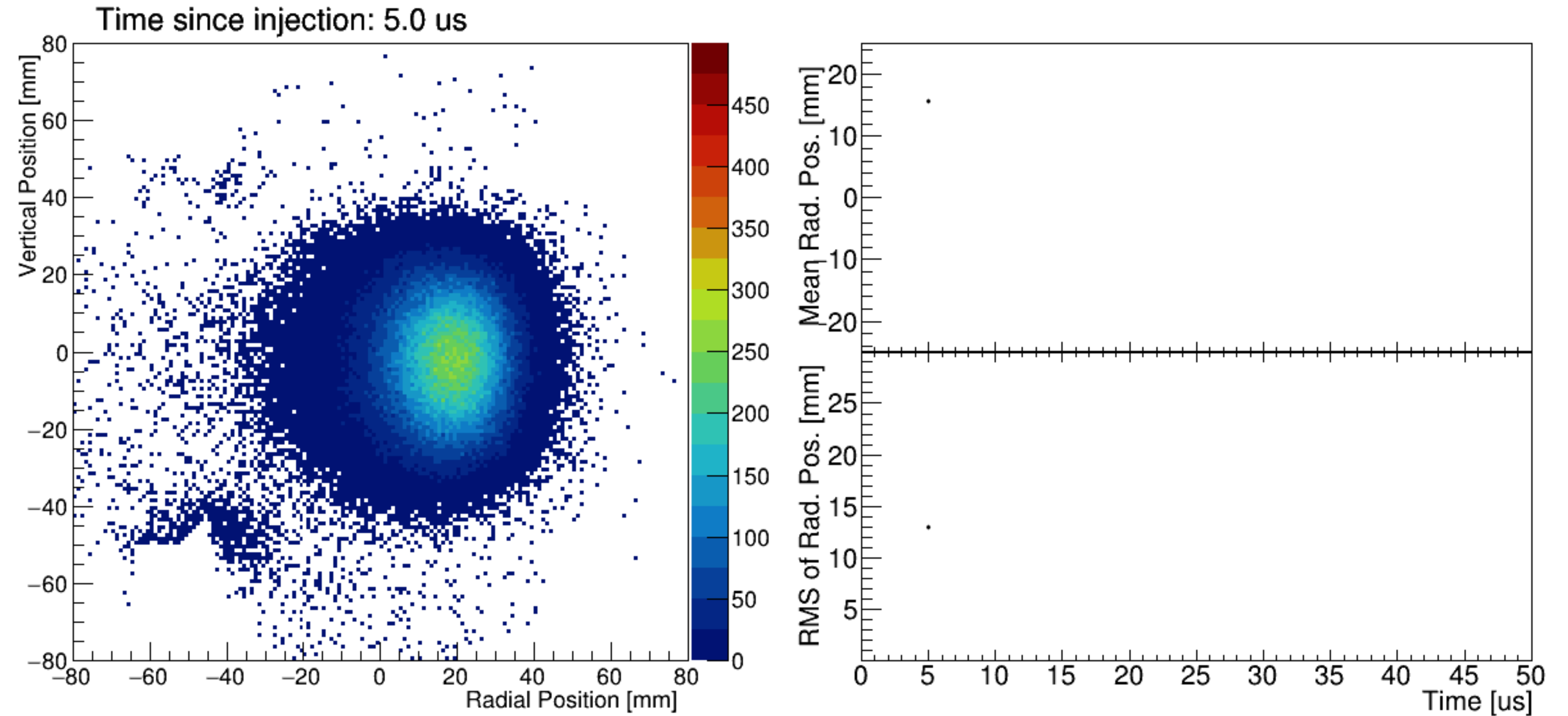
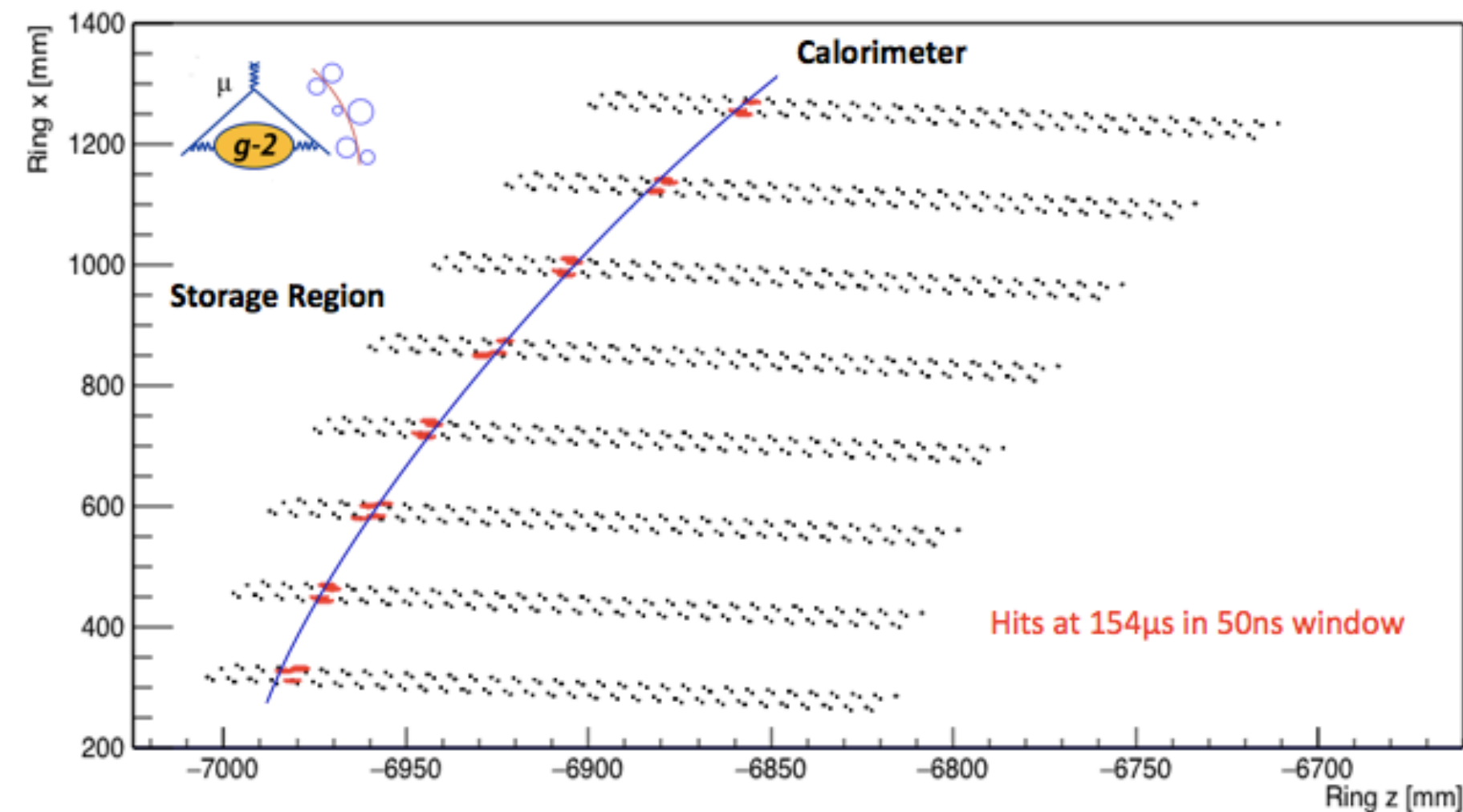
Experiment at Fermilab: Trackers

- Two straw tube tracker stations placed on inside of the ring 180 and 270 degrees from injection
- Each station composed of 8 "modules"



Experiment at Fermilab: Muon Distribution from Trackers

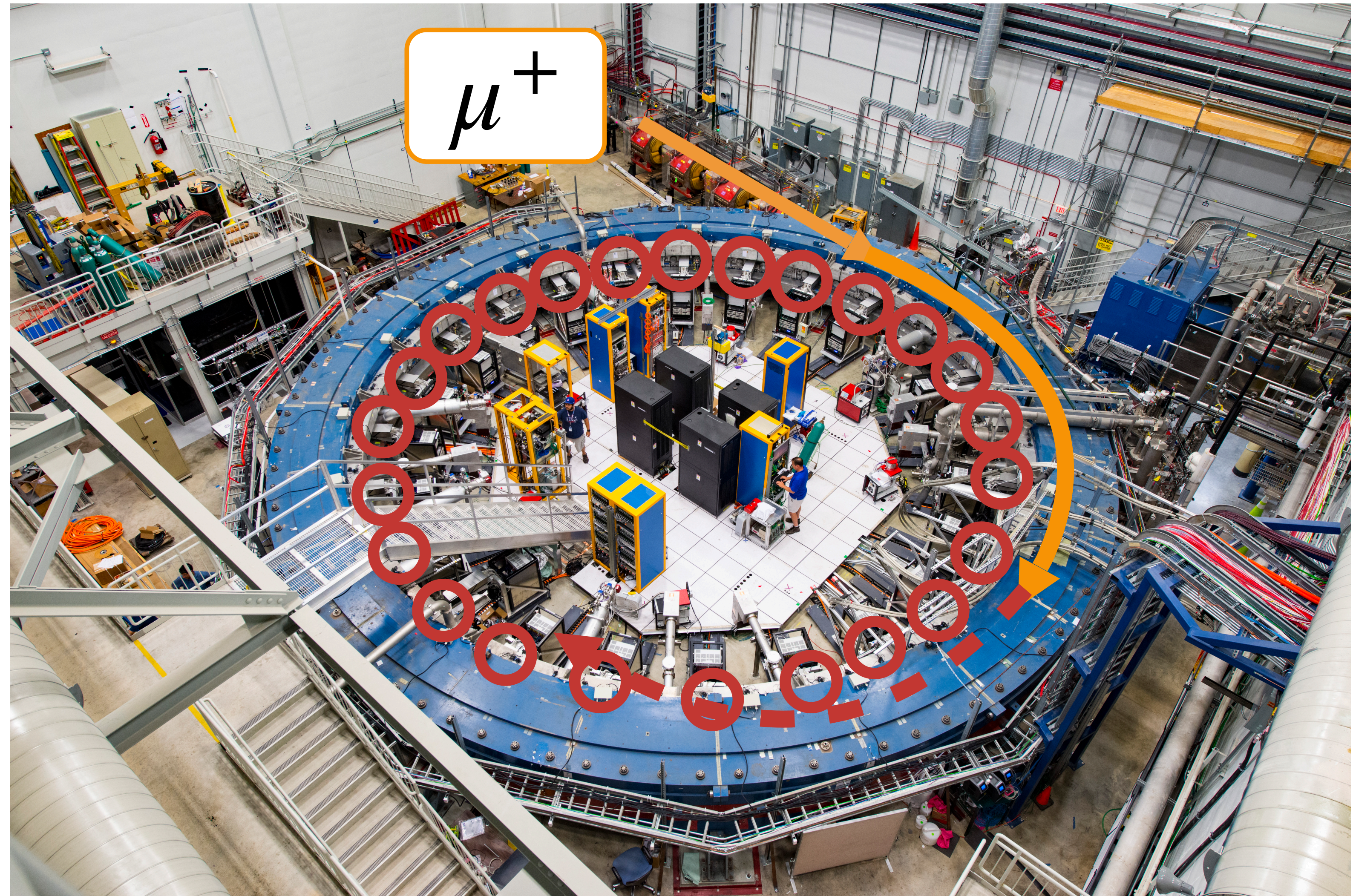
- Form tracks from straw hits
- Extrapolating backwards allows reconstruction of the muon beam over time
- Muons undergo betatron motion



- Need to weight magnetic field with muon distribution to get magnetic field “seen” by the muons

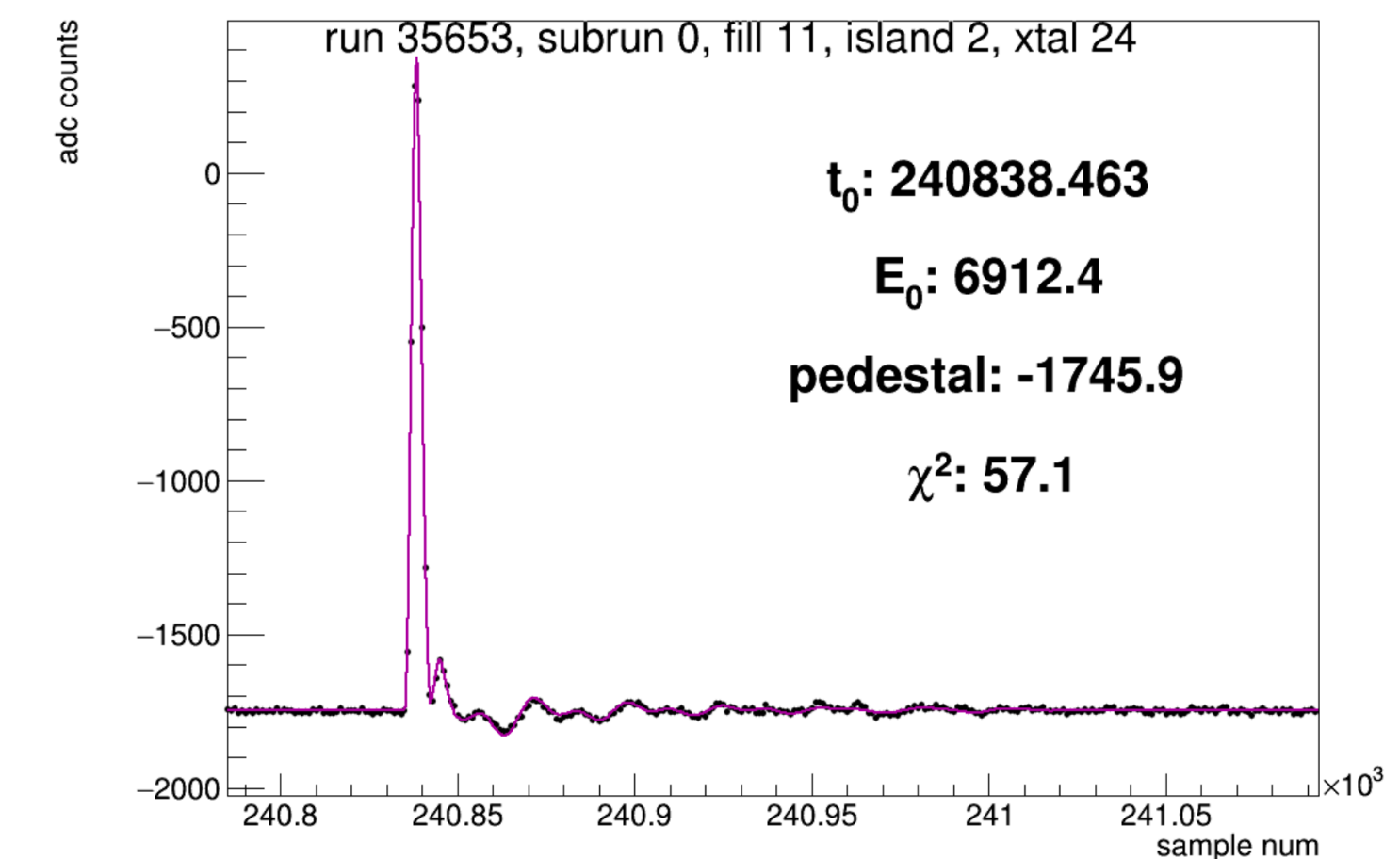
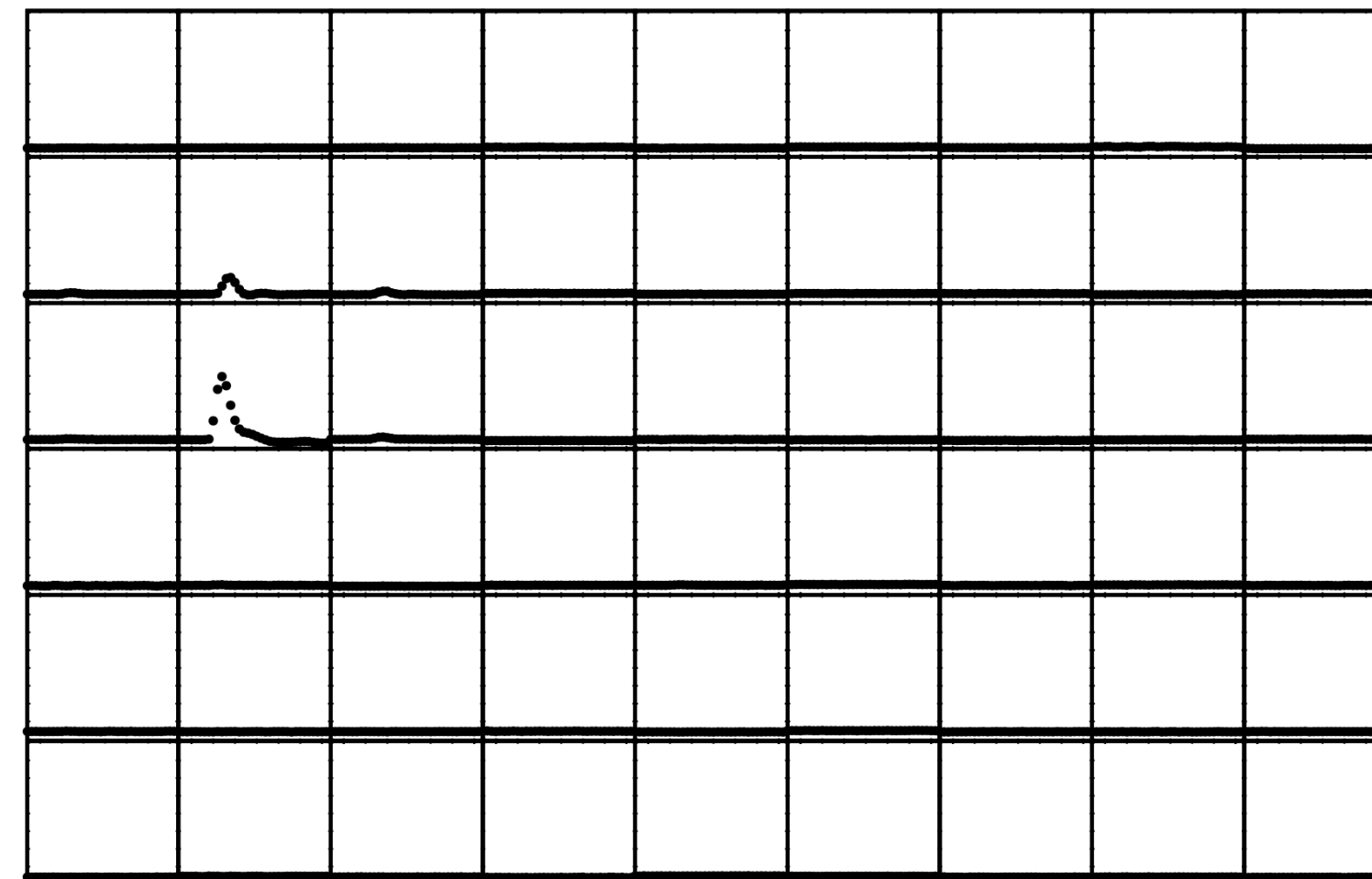
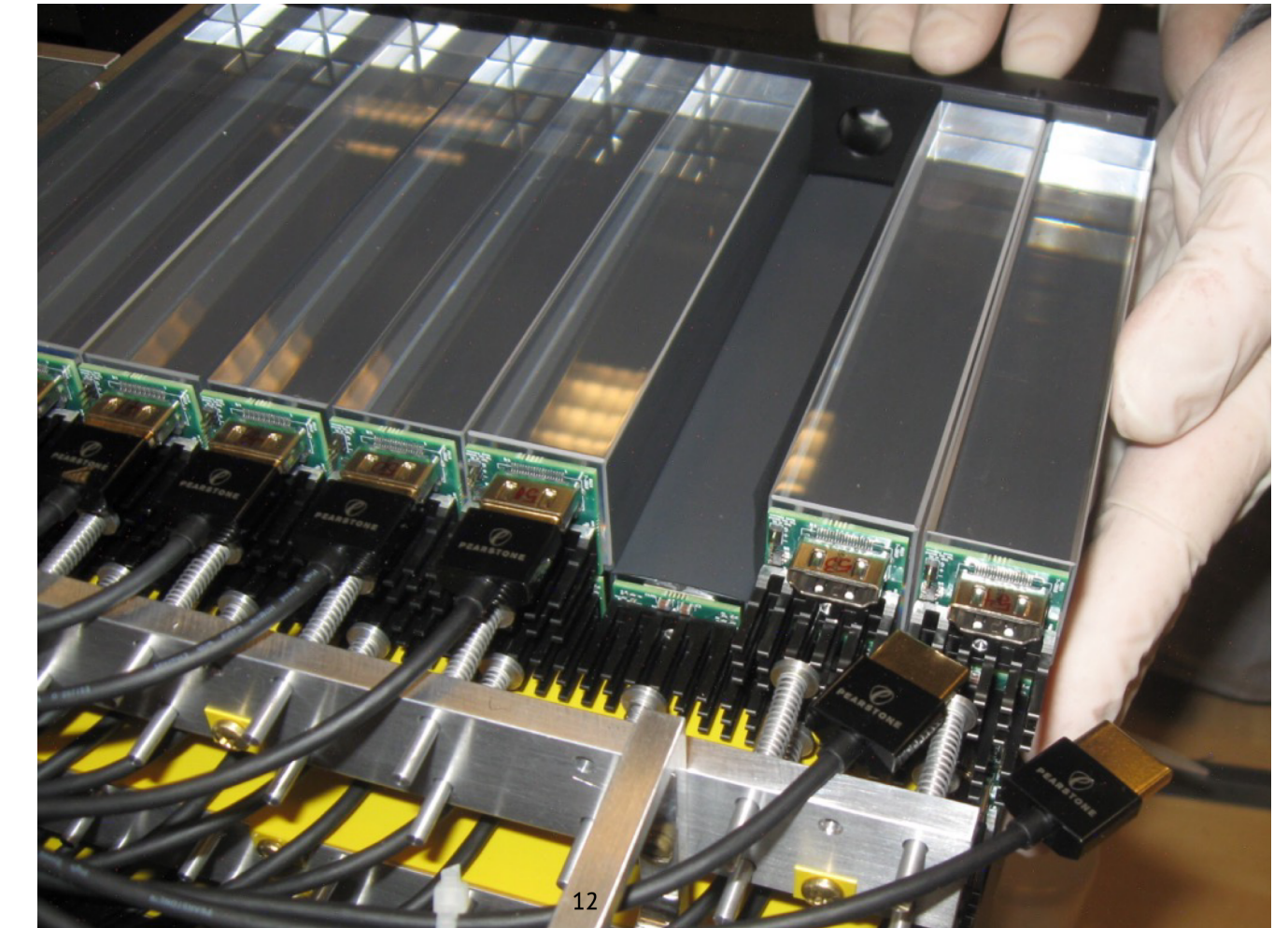
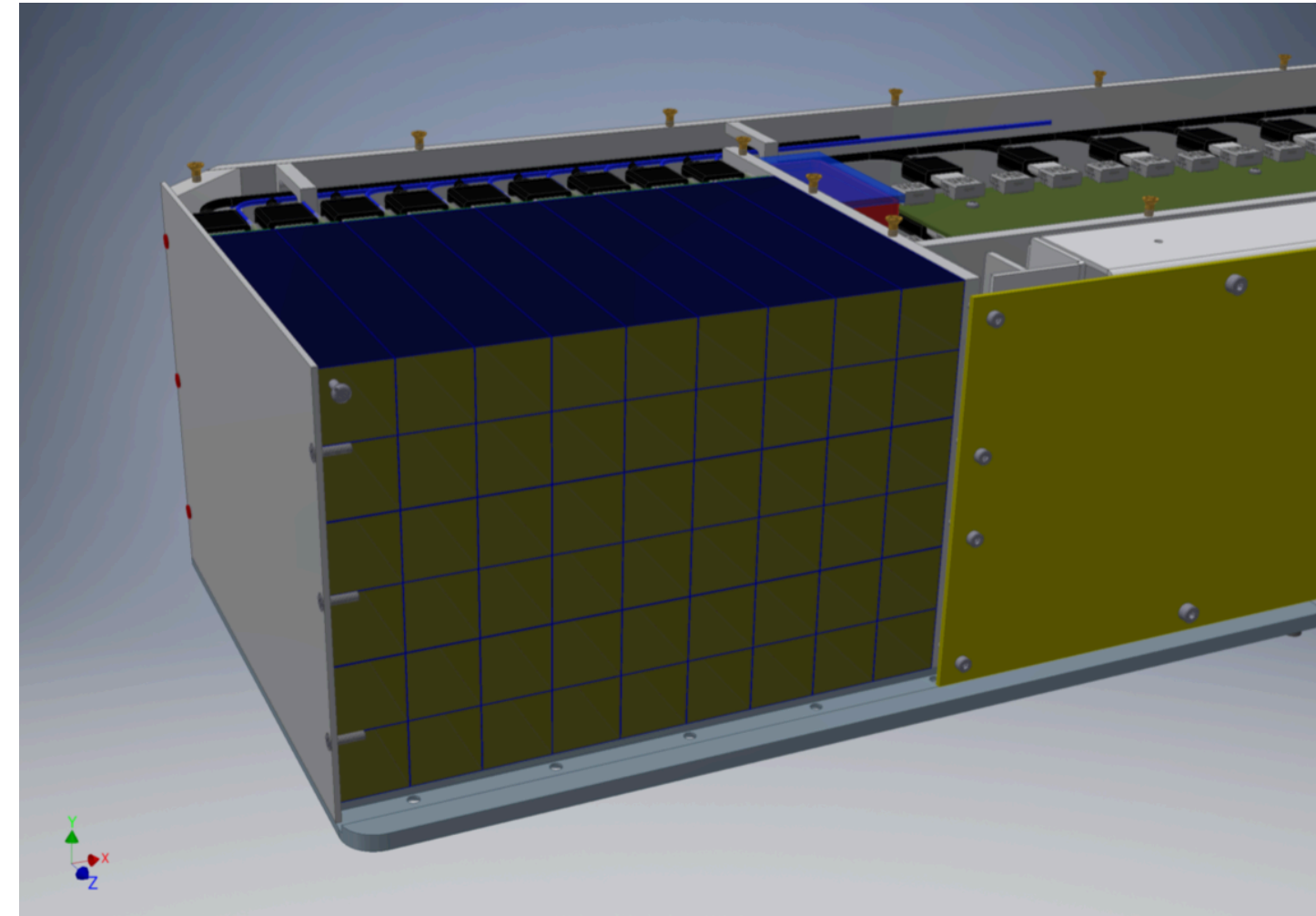
Experiment at Fermilab: Calorimeters

- 24 electromagnetic calorimeters line inside of ring to decay spiraling positrons



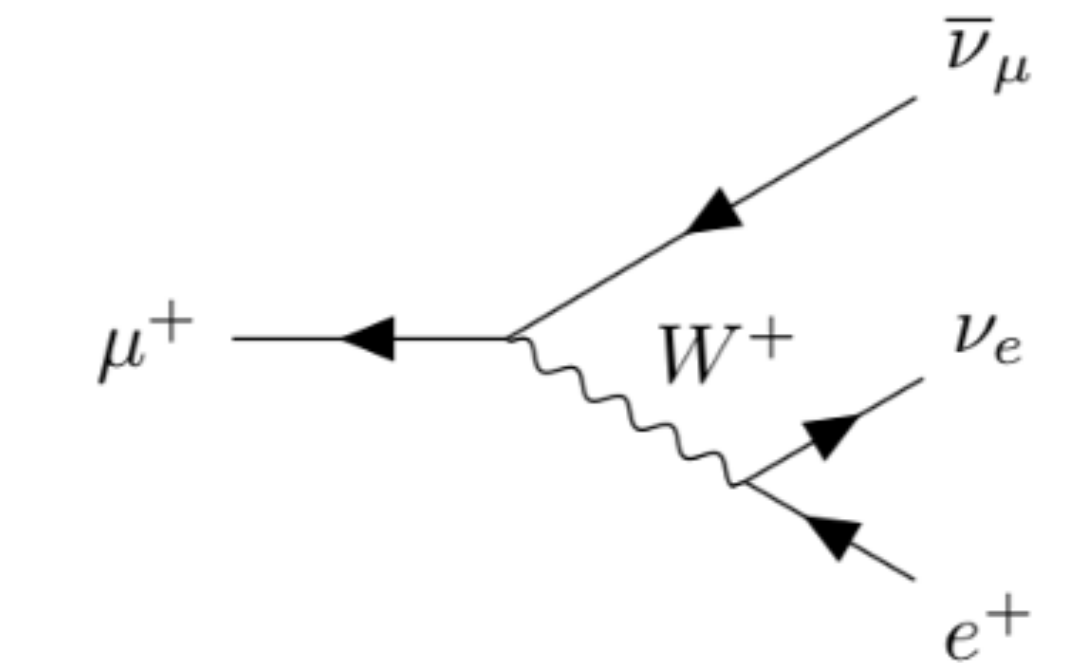
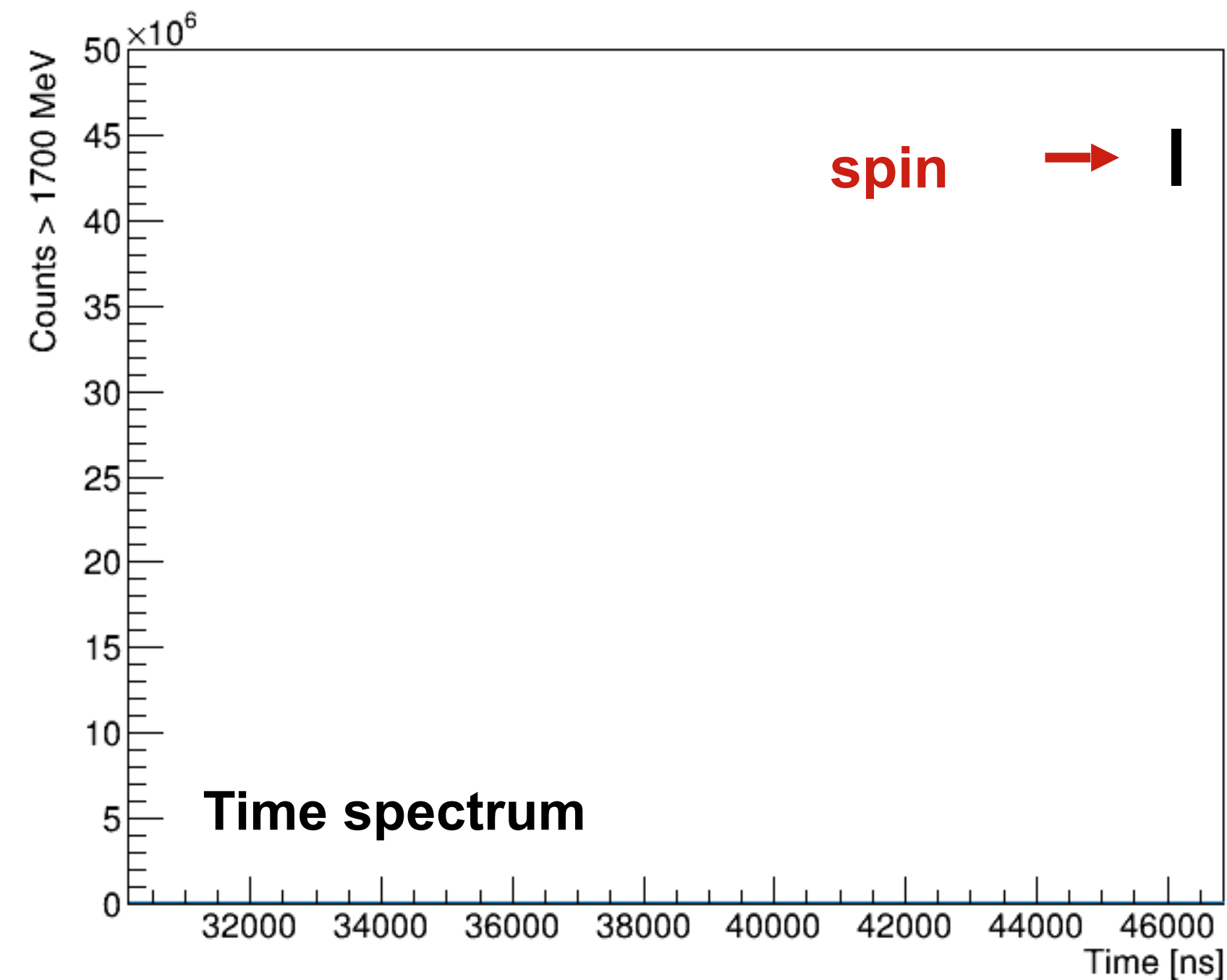
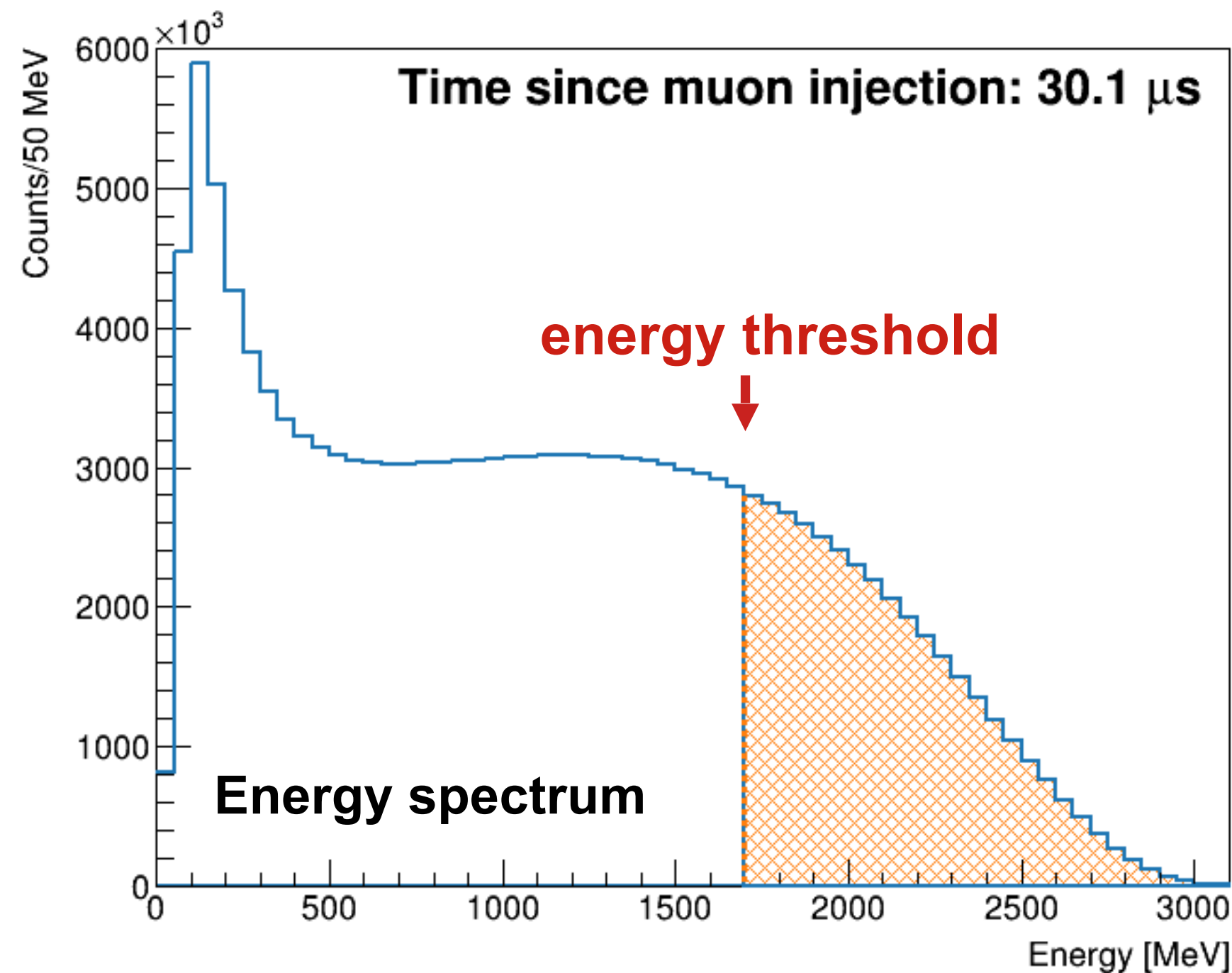
Experiment at Fermilab: Calorimeters

- 24 electromagnetic calorimeters line inside of ring
- Each “calo” is a 6x9 grid of PbF_2 Cherenkov crystals
- Light collected by SiPMs
- Laser calibration system ensures gain stability
- Energy & time of each positron arrival is reconstructed

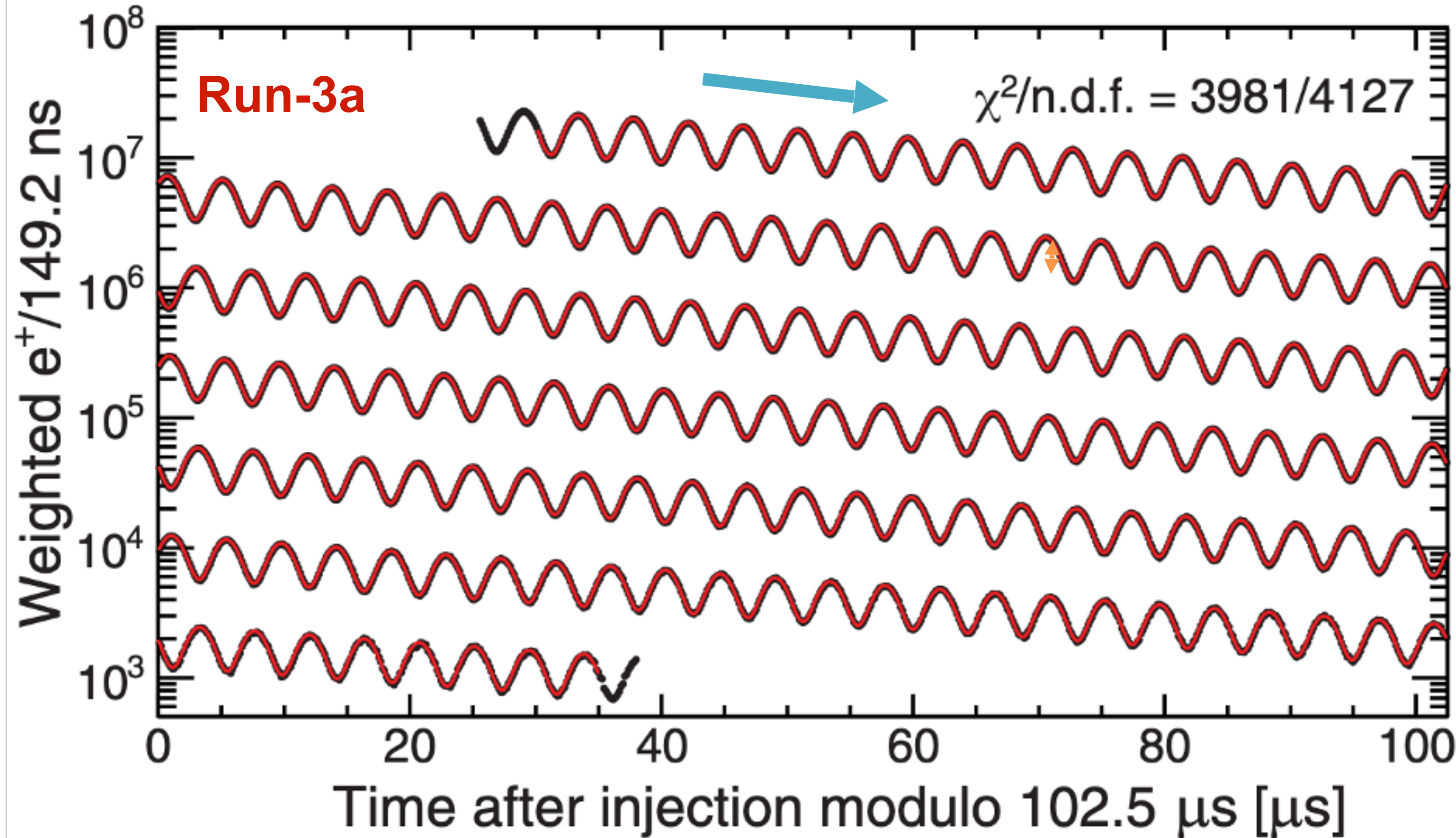


Use muon decay to access ω_a

- Parity violation of muon decay leads to a correlation between momentum direction of **highest energy decay positron** and the **muon spin**
- In lab frame, decay positron energy spectra is modulated by ω_a



“Wiggle” plot from Run-3a



exponential decay:
boosted lifetime $\approx 64.4\mu\text{s}$

wiggle is $\omega_a \propto g - 2$ (signal!)

relative size of wiggle:
asymmetry ≈ 0.35

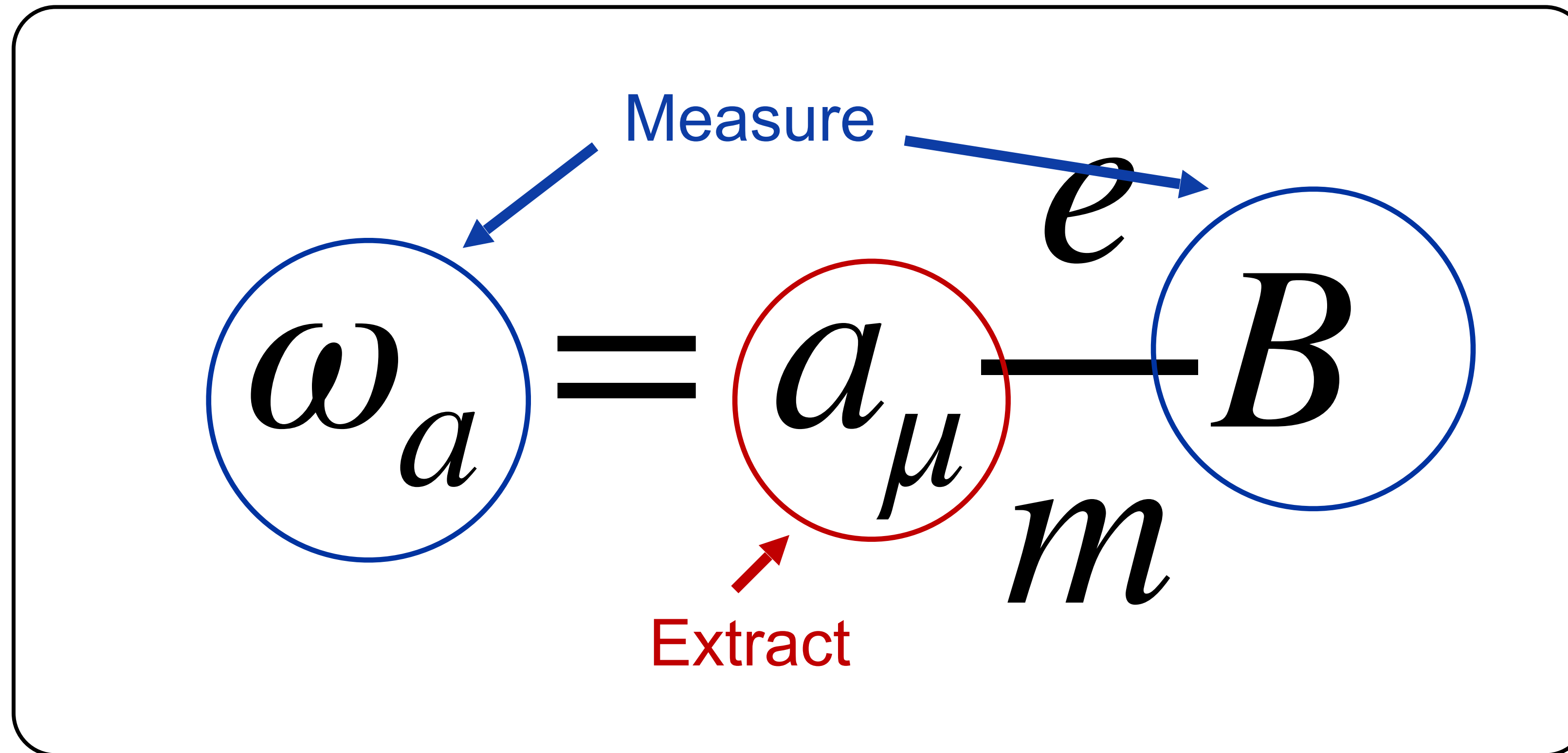
Fit to extract frequency
(simplified function):

$$N(t) = N_0 e^{(-t/\tau)} [1 + A \cos(\omega_a t - \phi)]$$

$$\delta\omega_a(\text{stat}) = \frac{\sigma_{\omega_a}}{\omega_a} = \frac{\sqrt{2}}{\sqrt{NA\gamma\tau\omega_a}}$$

Bringing it all together

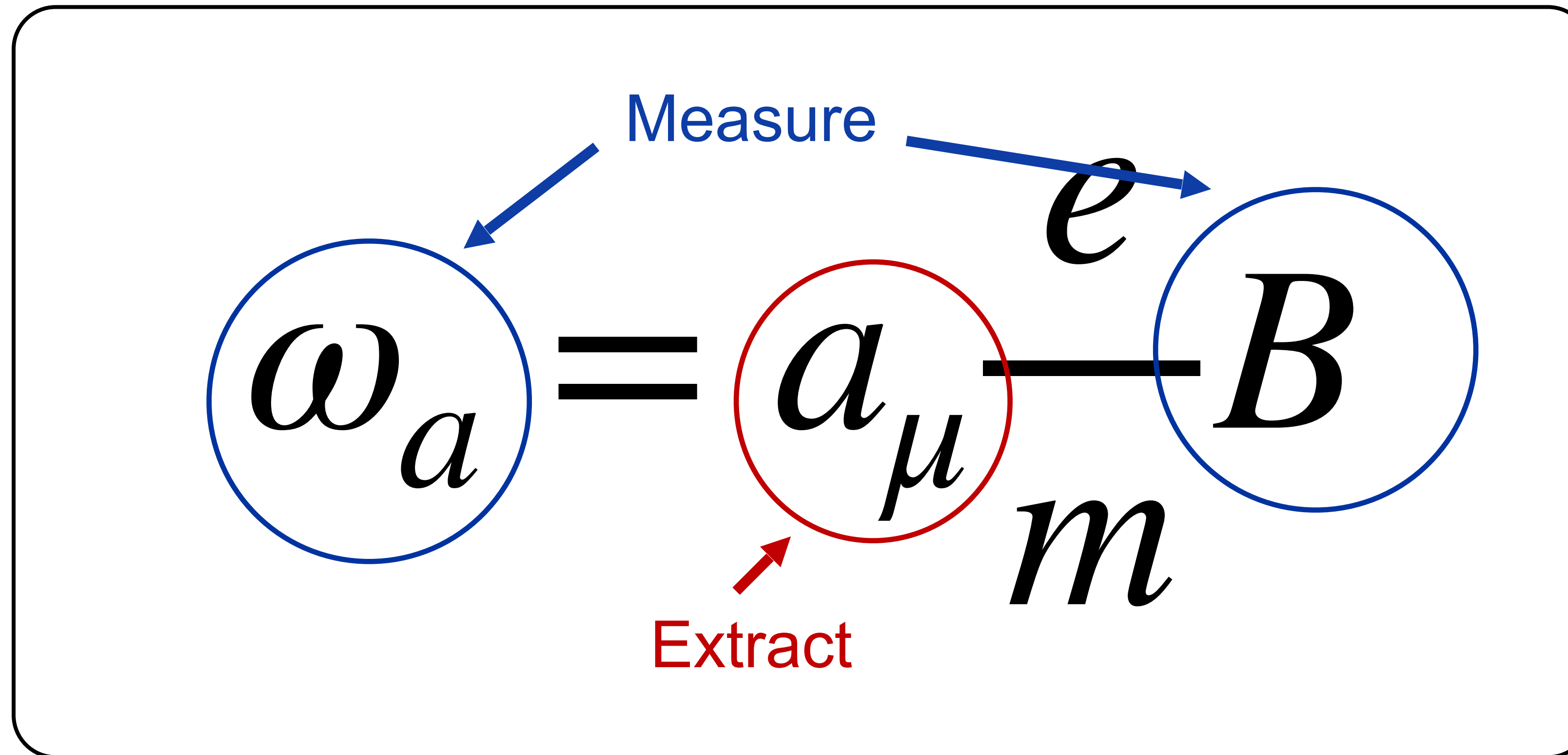
ω_a from fitting the
“wobble” plot



B-field from **proton NMR** and weighted by **muon distribution** from trackers

Bringing it all together

ω_a from fitting the “wobble” plot



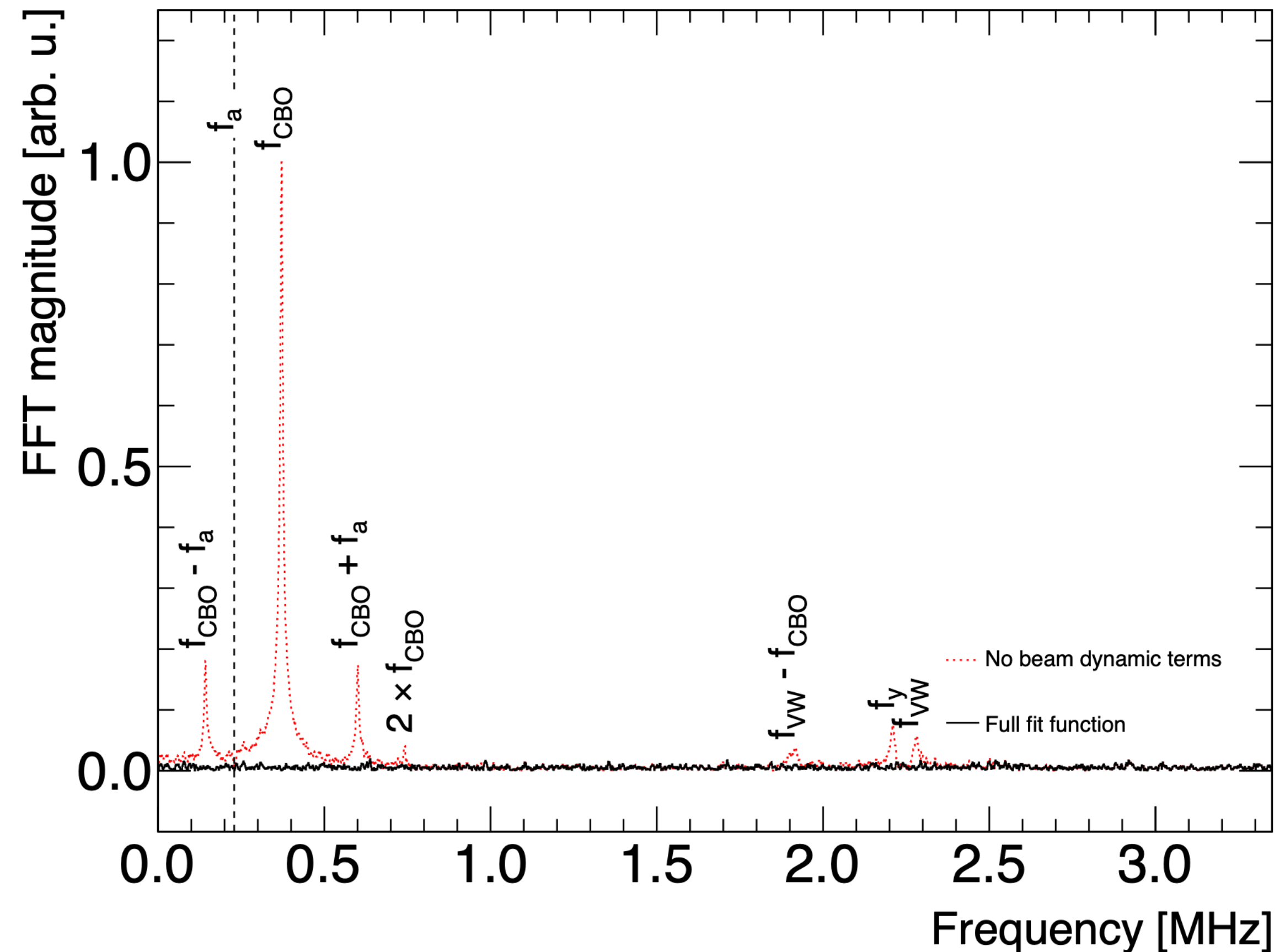
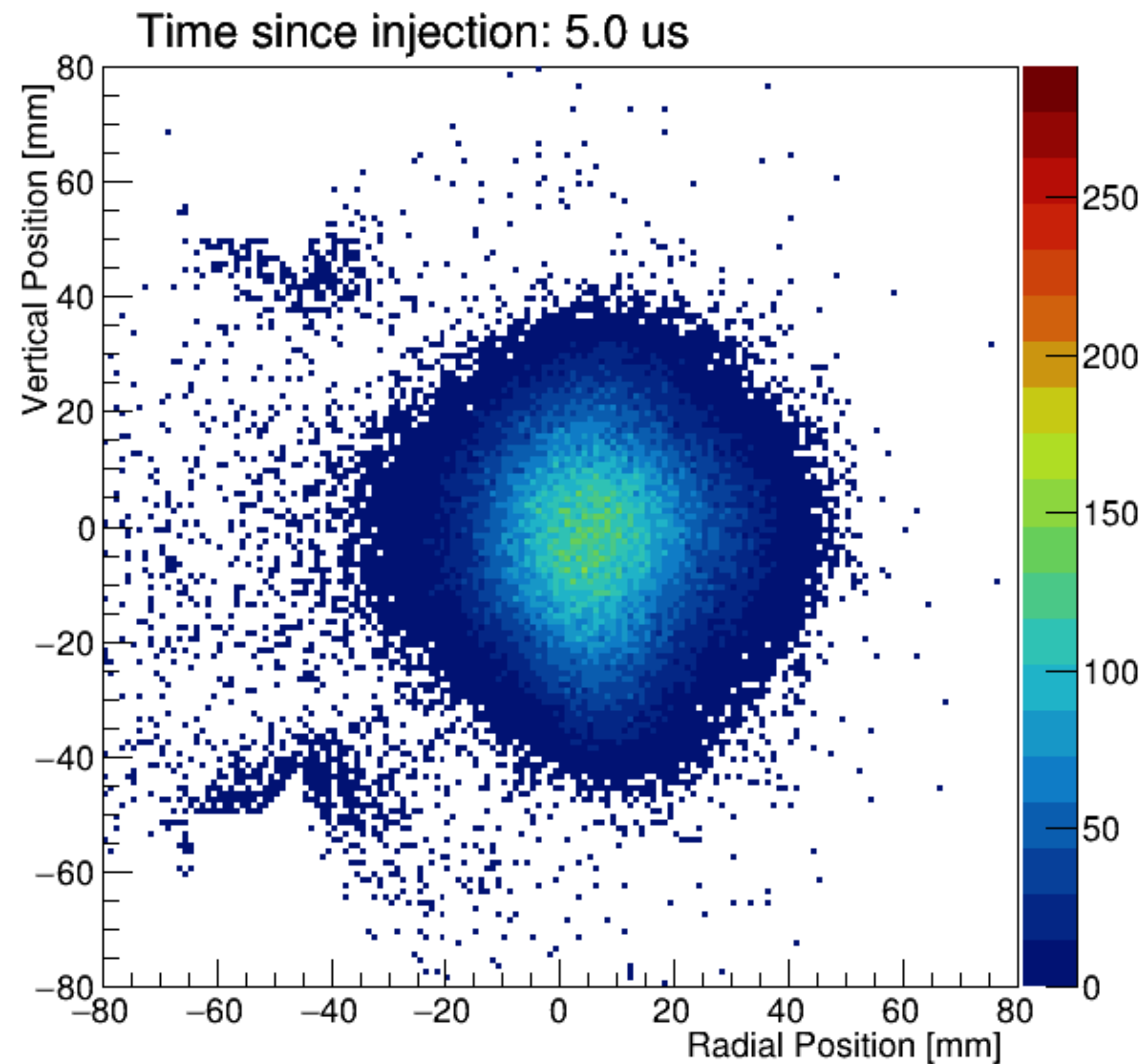
B-field from **proton NMR** and weighted by **muon distribution** from trackers

$$\mathcal{R}'_\mu = \frac{\omega_a}{\omega_p(T_r)} = \frac{f_{\text{clock}} \omega_a^m (1 + C_e + C_p + C_{ml} + C_{pa} + C_{dd})}{f_{\text{calib}} \left\langle \omega_p(x, y, \phi) \times M(x, y, \phi) \right\rangle (1 + B_k + B_q)}$$

In reality, some complications from beam dynamics and magnetic transients

Systematic uncertainty example

- Coherent betatron oscillation (CBO) is the radial motion of the beam
- Visible in the calorimeter data and must be accounted for in fit

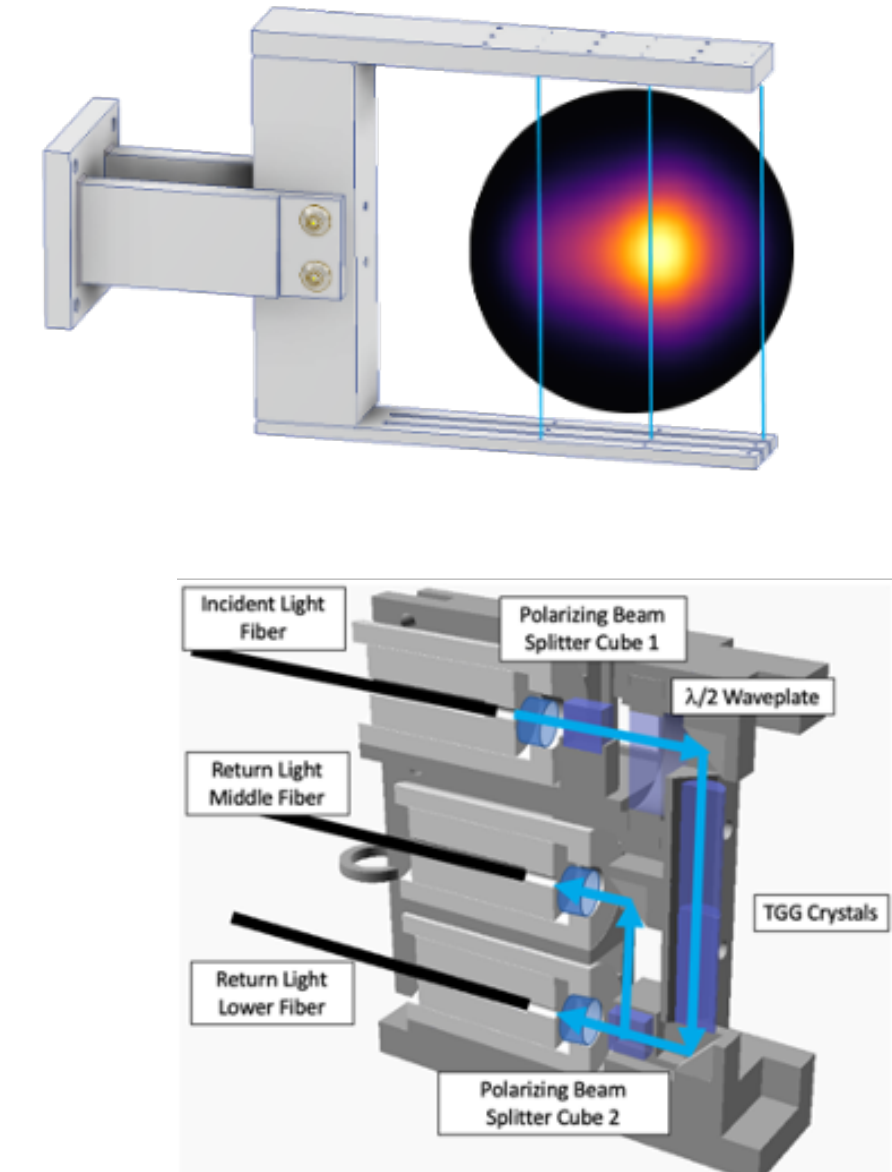
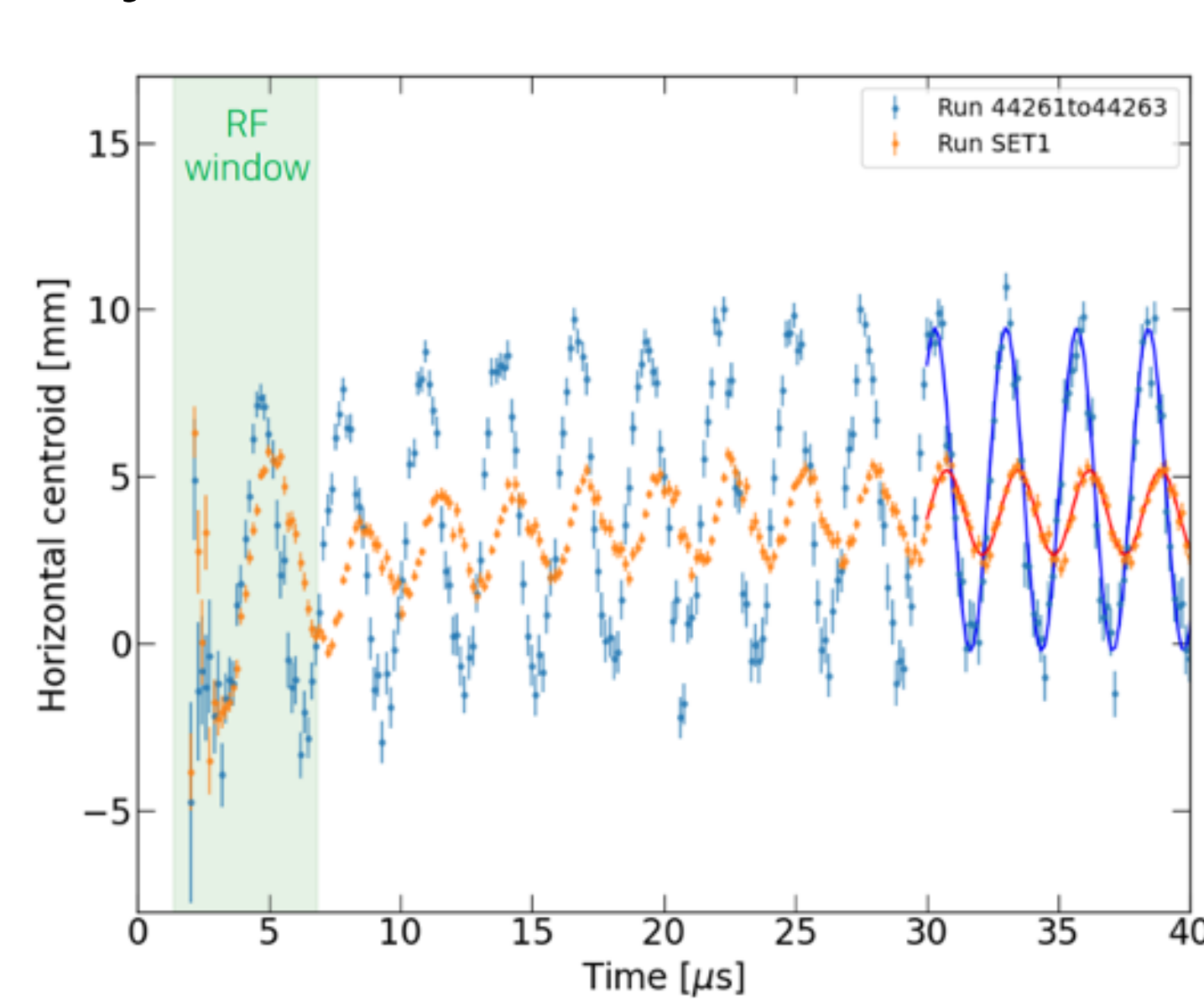


Uncertainties in Run-2/3 and improvements

TABLE I. Values and uncertainties of the \mathcal{R}'_μ terms in Eq. (2), and uncertainties due to the external parameters in Eq. (1) for a_μ . Positive C_i increases a_μ ; positive B_i decreases a_μ [see Eq. (2)]. The ω_a^m uncertainties are decomposed into statistical and systematic contributions. All values are computed with full precision and then rounded to the reported digits.

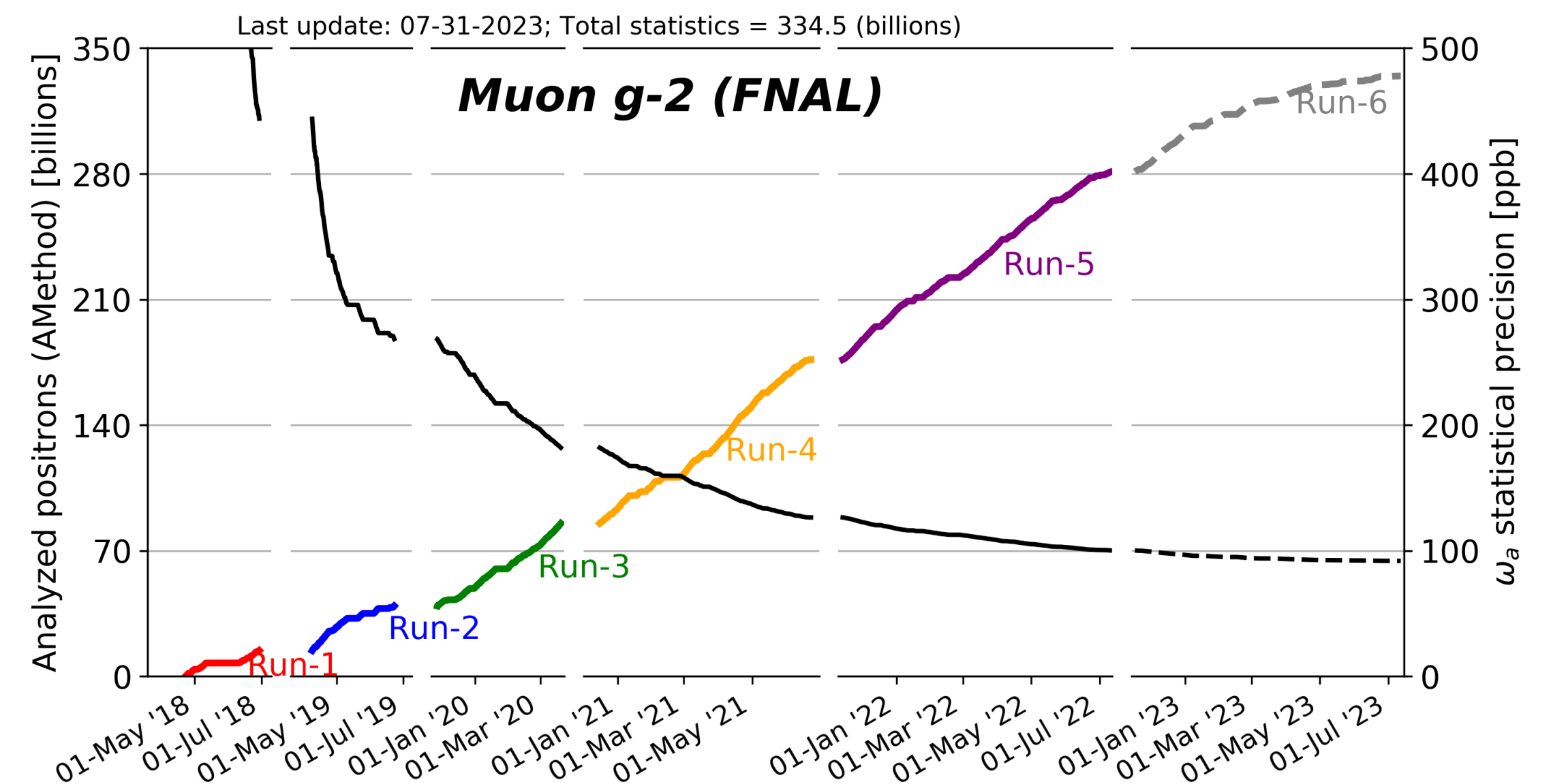
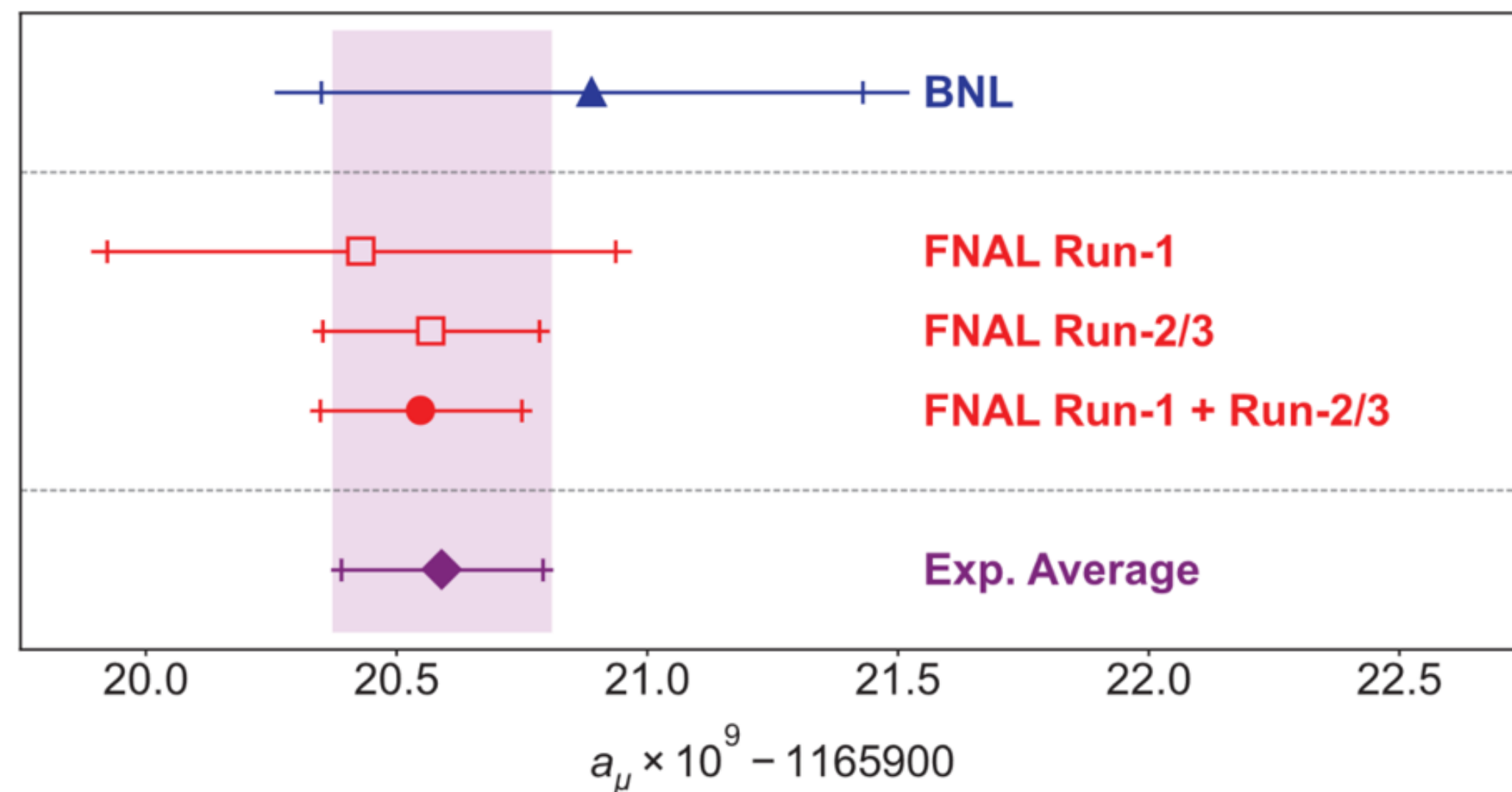
| Quantity | Correction (ppb) | Uncertainty (ppb) |
|-------------------------------------------------------------------------------|------------------|-------------------|
| ω_a^m (statistical) | ... | 201 |
| ω_a^m (systematic) | ... | 25 |
| C_e | 451 | 32 |
| C_p | 170 | 10 |
| C_{pa} | -27 | 13 |
| C_{dd} | -15 | 17 |
| C_{ml} | 0 | 3 |
| $f_{\text{calib}} \cdot \langle \omega'_p(\vec{r}) \times M(\vec{r}) \rangle$ | ... | 46 |
| B_k | -21 | 13 |
| B_q | -21 | 20 |
| $\mu'_p(34.7^\circ)/\mu_e$ | ... | 11 |
| m_μ/m_e | ... | 22 |
| $g_e/2$ | ... | 0 |
| Total systematic for \mathcal{R}'_μ | ... | 70 |
| Total external parameters | ... | 25 |
| Total for a_μ | 622 | 215 |

- Run-2/3 uncertainty was **statistics** dominated 201 ppb
 - Run-4/5/6 to reduce this to ~100 ppb!
- Run-5 onwards, implemented RF pulse to electrostatic quadrupole plates to **dampen CBO signal**
- **Dedicated measurements** to better constrain beam dynamics corrections and magnetic transients



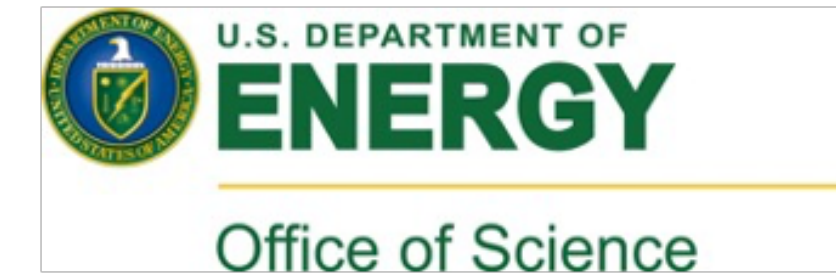
Summary and Outlook

- Muon g-2 experiment at Fermilab poised to surpass goal of 140 ppb measurement of muon magnetic anomaly
- Based on first three years of data, we've determined a_μ to **203 ppb**
- Current comparison with theory is difficult due to tension among different HVP calculations; lots of active work in theory community
- We also have other measurement efforts: muon EDM, CPT/Lorentz violation, dark matter search



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