

# Measurements of the $\text{Cos}\phi$ and $\text{Cos}2\phi$ Moments of the Unpolarized SIDIS $\pi^+$ Cross-section at CLAS12

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LinkedIn



# Motivation

- Semi-Inclusive Deep Inelastic Scattering (SIDIS) experiments allow us to address questions about the 3D structure of nucleons
- Azimuthal modulations in unpolarized SIDIS cross-section for charged pion electroproduction can give access to the Cahn and Boer-Mulders effects
  - **Boer-Mulders Effect:** Sensitive to the correlation between the quark's transverse momentum and intrinsic transverse spin in an unpolarized nucleon
  - **Cahn Effect:** Sensitive to the transverse motion of quarks inside the nucleon
- A non-zero Boer-Mulders requires quark orbital angular momentum contributions to the proton spin (aspect of the proton missing spin puzzle)

# SIDIS Cross-Section and Boer-Mulders

The lepton-hadron Unpolarized SIDIS Cross-Section:

$$\frac{d^5\sigma}{dydQ^2dzd\phi_h dP_{h\perp}^2} = \underbrace{\frac{x_B}{y} \frac{2\pi\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) (F_{UU,T} + \epsilon F_{UU,L})}_{A_0} \left\{ 1 + \underbrace{\frac{\sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos\phi_h}} \cos\phi_h + \underbrace{\frac{\epsilon F_{UU}^{\cos 2\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos 2\phi_h}} \cos 2\phi_h \right\}$$

The Boer-Mulders and Cahn effects are present in the Structure Functions:

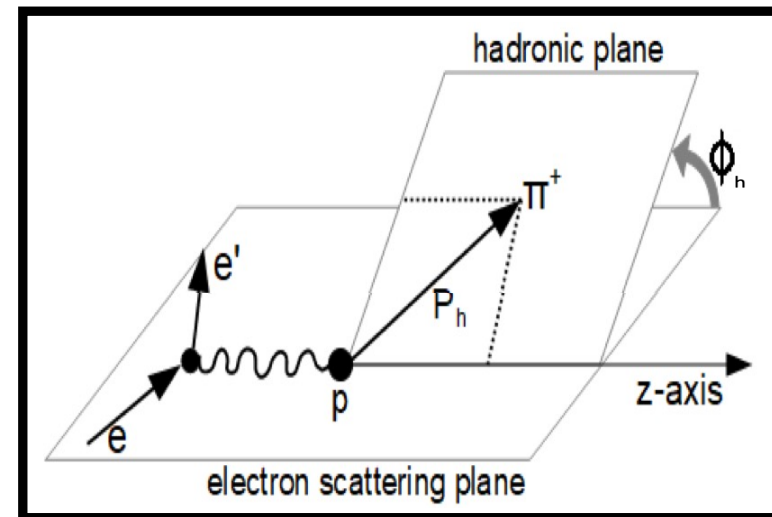
leading twist  $F_{UU}^{\cos 2\phi_h} \propto C$  BOER-MULDERS EFFECT

$$\left[ \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} h_1^\perp H_1^\perp + \dots \right]$$

CAHN EFFECT

next to leading twist  $F_{UU}^{\cos\phi_h} \propto \frac{2M}{Q} C$  Interaction dependent terms neglected

$$\left[ -\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} x h H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1 + \dots \right]$$



Reaction Studied:  $e p \rightarrow e \pi^+(X)$

# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum

Using Data from RG-A Fall 2018  
 10.6 GeV Polarized Beam  
 Unpolarized Liquid Hydrogen Target  
 Inbending Forward Tracking Only

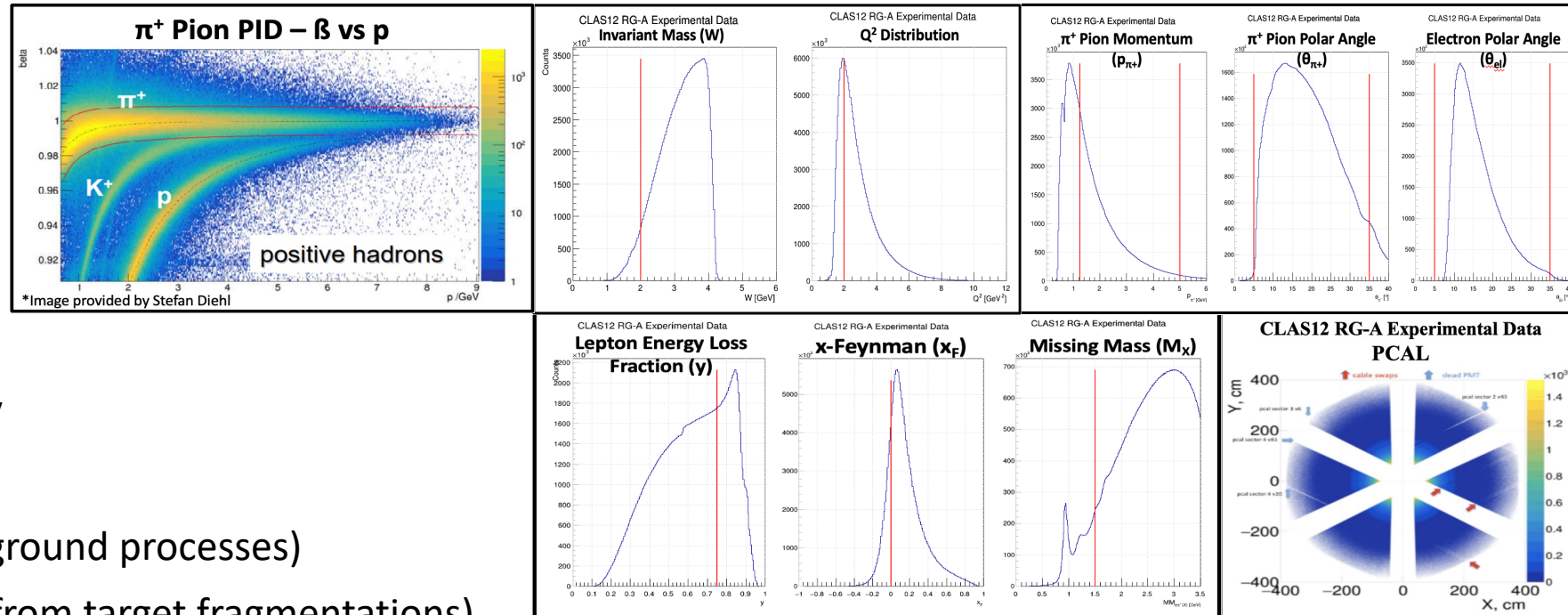
## Analysis Cuts:

### SIDIS Cuts:

- $W > 2 \text{ GeV}$
- $Q^2 > 2 \text{ GeV}^2$

### Other Analysis Cuts:

- $p_{\pi^+}$  Cut:  $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- $\theta$ -angle Cut:  $5^\circ < \theta_{\text{particle}} < 35^\circ$
- $y < 0.75$  (minimize other background processes)
- $x_F > 0$  (minimize contributions from target fragmentations)
- Missing Mass Cut:  $M_x > 1.5 \text{ GeV}$  (limit on exclusive events)
- Fiducial Cuts (e.g., accounts for bad channels present in data)



# Analysis Procedure

## Experimental extraction of cross-section

$$\frac{d^5\sigma}{dQ^2 dy dP_T dz d\phi_h} = \frac{1}{\Gamma_\nu} \underbrace{\frac{1}{\Delta Q^2 \Delta y \Delta P_T \Delta z \Delta \phi_h}}_{\text{Bin Volume}} \frac{N}{R \cdot BC \cdot \eta \cdot N_0} \underbrace{\frac{1}{(N_A \cdot \rho \cdot t / A_w)}}_{\text{Target Number Density}}$$

Where:

Bin Volume

Target Number Density

- R = Radiative Correction
- $\eta$  = **Acceptance Correction** → Requires Monte Carlo (MC) Simulation
- N = Bin Yields
- $N_0$  = Life-time corrected incident electron flux
- BC = factor which evolves bin-averaged differential cross-section

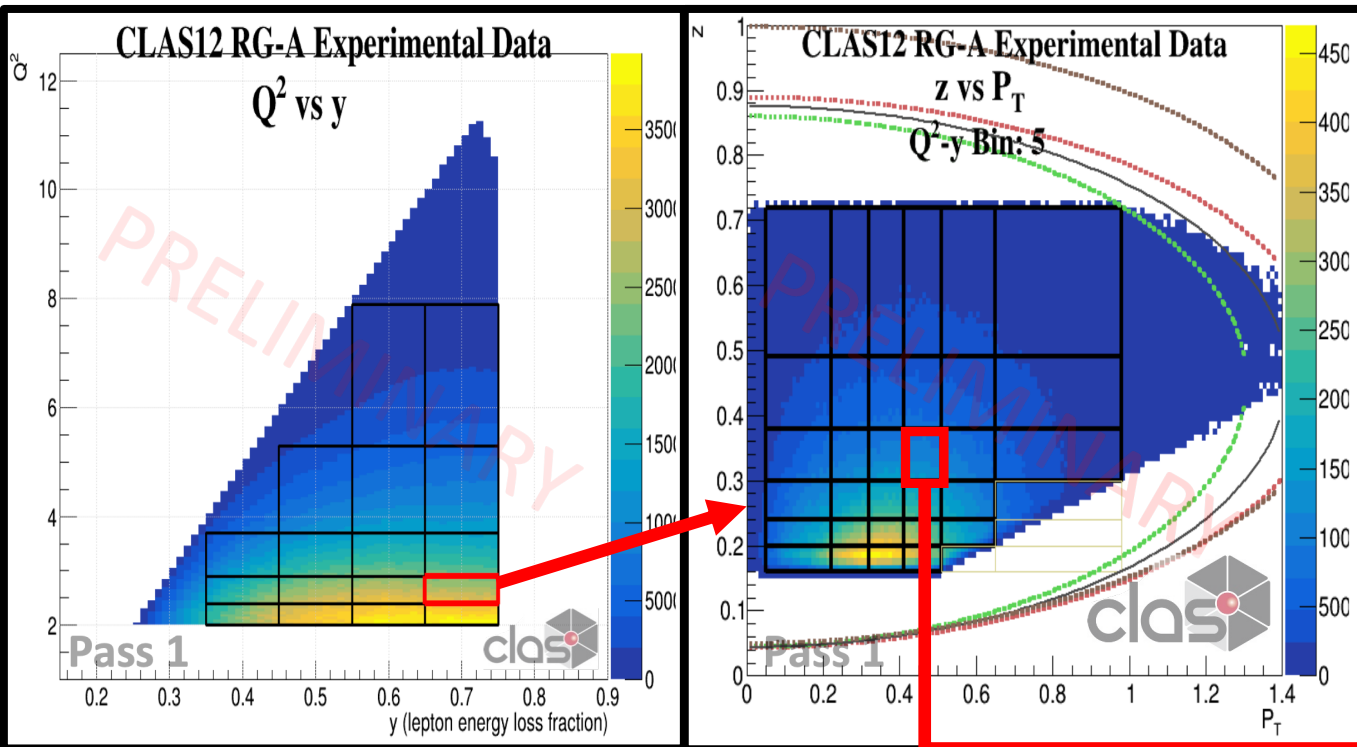
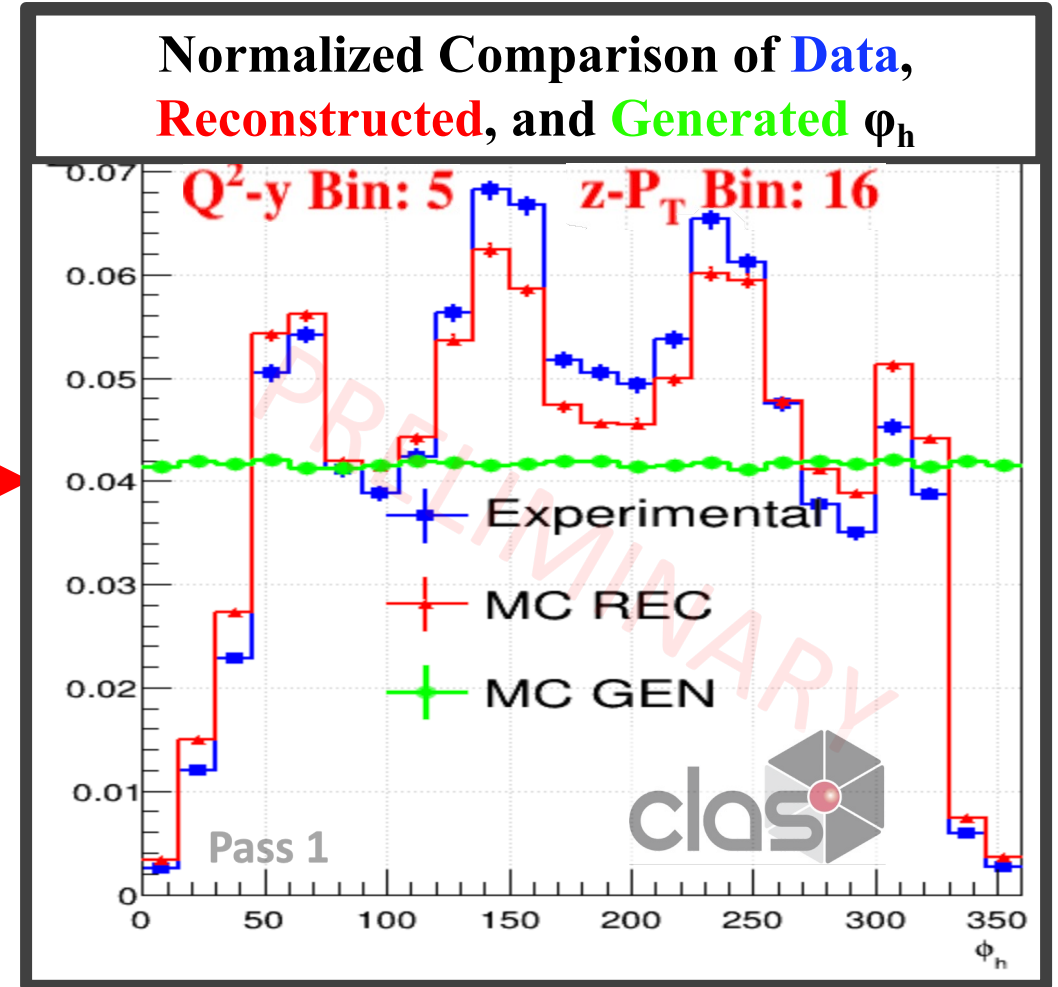
SIDIS MC are generated with LEPTO event generator

# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (5 Dimensions)

17  $Q^2$ - $y$  Bins Total – 25-36  $z$ - $P_T$  Bins (per  $Q^2$ - $y$  bin)

$\phi_h$  distribution for the  $Q^2$ - $y$ - $z$ - $P_T$  bin shown in red



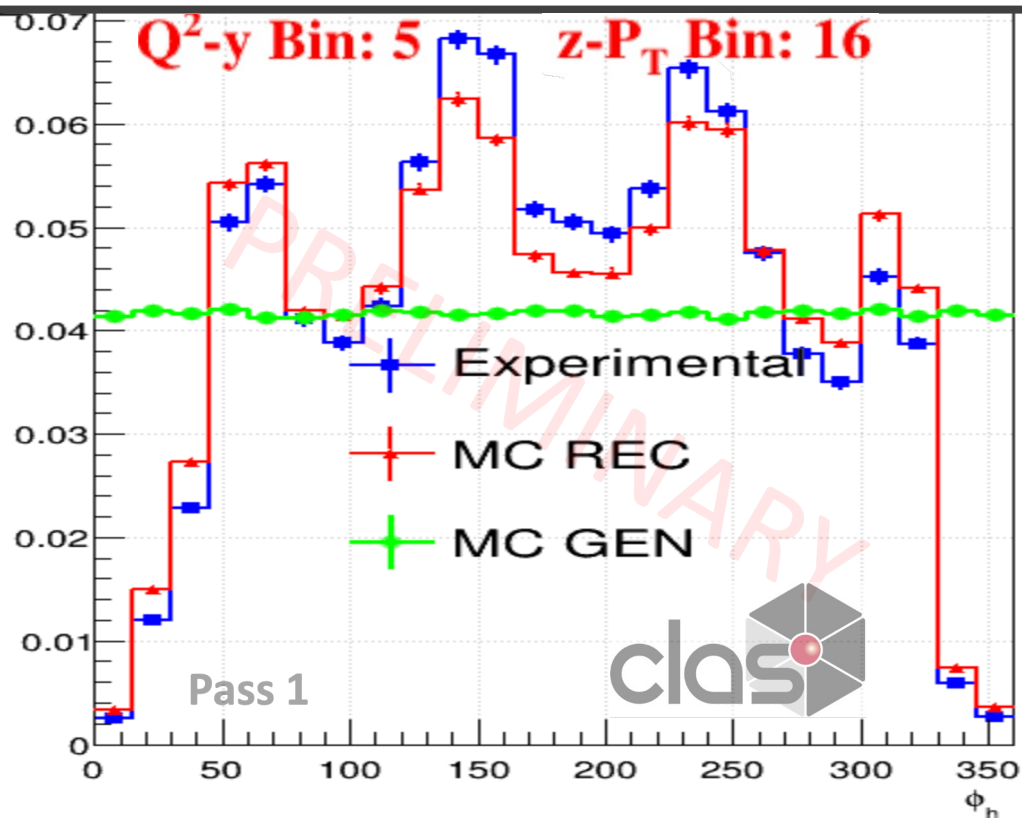
Missing Mass Cut Lines:



# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (5 Dimensions)

Normalized Comparison of **Data**,  
**Reconstructed**, and **Generated**  $\phi_h$



Apply  
Multidimensional  
Acceptance  
Corrections and  
convert to a  
cross-section  
measurement

$\phi_h$  fit for  
every bin

$A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$   
Where the parameters A, B, C  
give the cross-section moments

$$A_{UU}^{\cos \phi_h} = B \quad A_{UU}^{\cos 2\phi_h} = C$$

### Methods used for Acceptance Corrections:

- **Bin-by-bin Correction**
  - Simple method which just needs the 1D plots shown here
- **Bayesian Unfolding**
  - Bayesian Unfolding Method uses Acceptance Matrices to correct the data

# Acceptance Corrections and Bin Migration Study

- **Acceptance Matrix:**  $A_{(i,j)}$  describes both Acceptance (including geometric acceptance and detector efficiency) and Bin Migration
- $$A_{(i,j)} = \frac{\text{Number of Events Generated in bin } j \text{ but Reconstructed in bin } i}{\text{Total Number of Events Generated in the } j\text{th bin}}$$
- Acceptance Unfolding:  $Y_i = A_{(i,j)}X_j + \beta_i \Leftrightarrow X_j = A_{(i,j)}^{-1}(Y_i - \beta_i)$

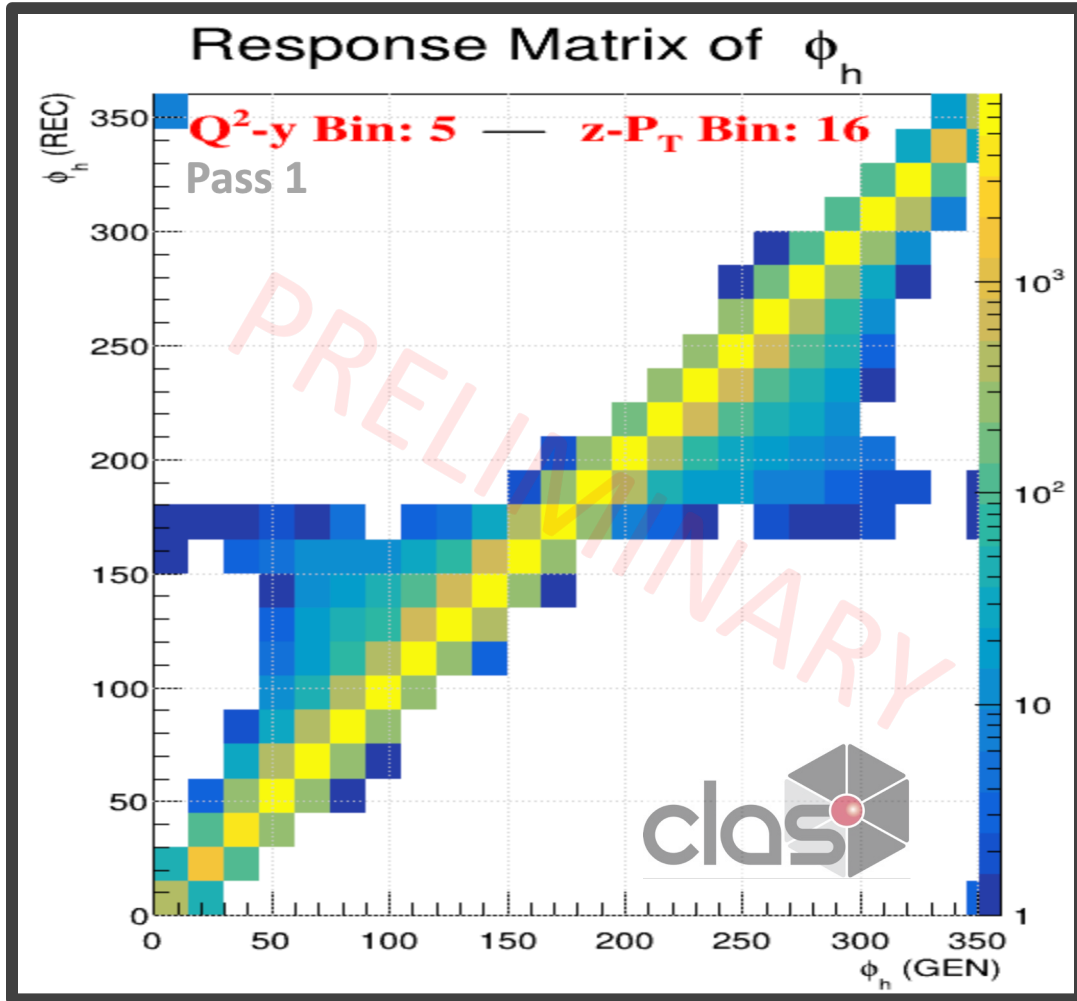
where:

- $Y_i$  = Number of events experimentally measured in the  $i$ -th bin
- $X_j$  = Number of acceptance-corrected events in the  $j$ -th bin
- $\beta_i$  = Number of events from outside the signal region measured in the  $i$ -th bin

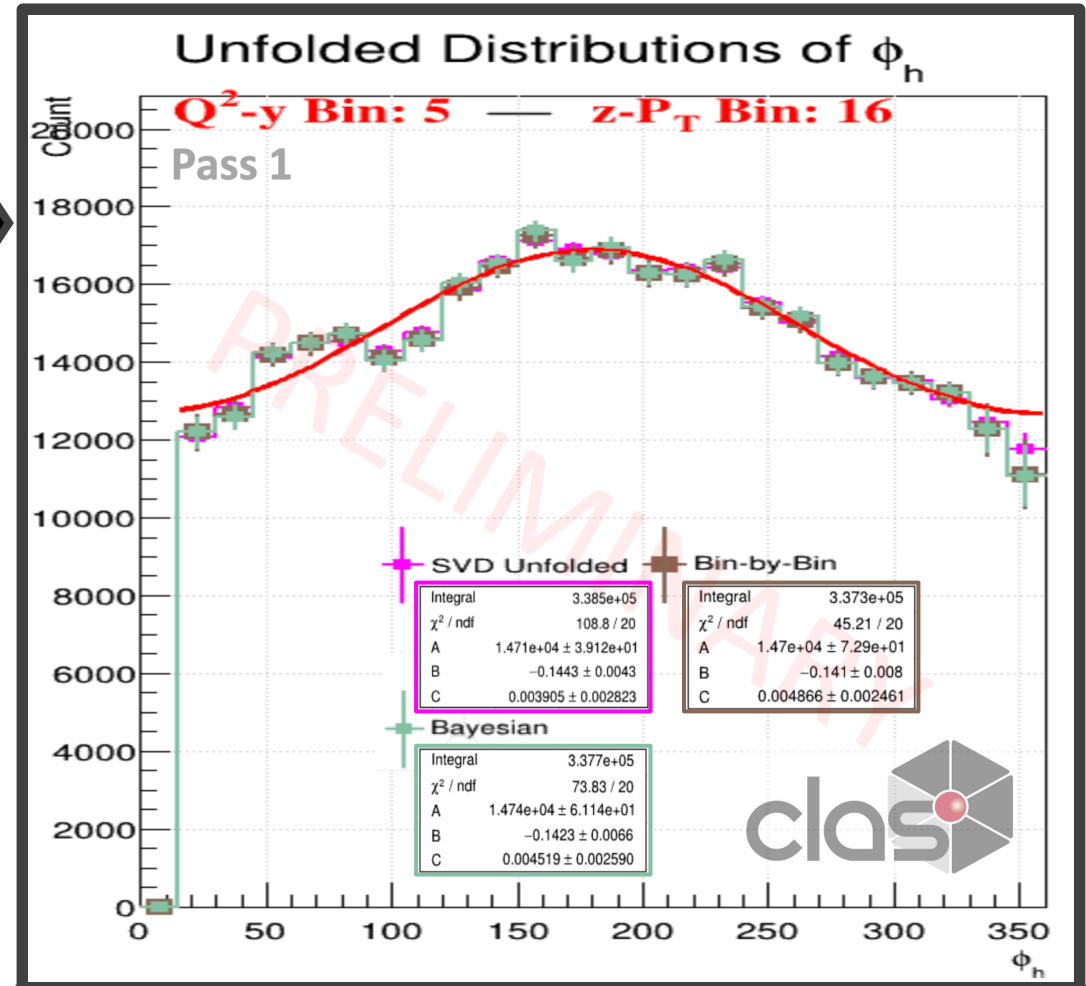


# 1D Unfolding

Using the Multidimensional Kinematic Bin from prior example



Unfolding Procedures

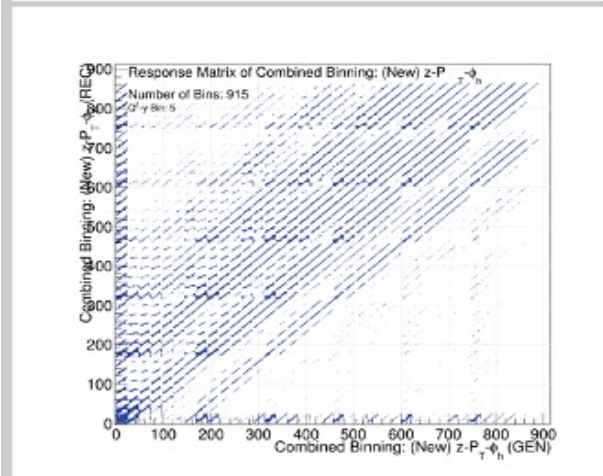
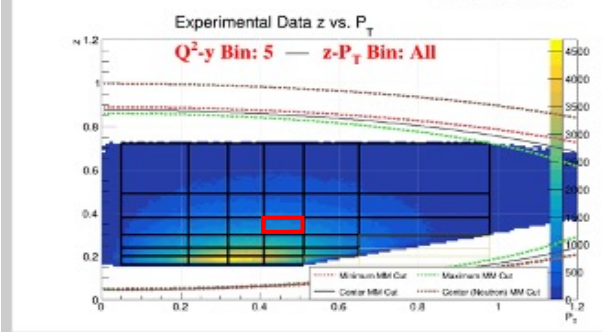
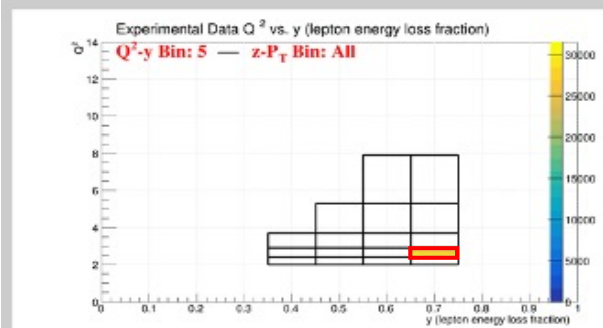


Parameters shown are from the fits previously described

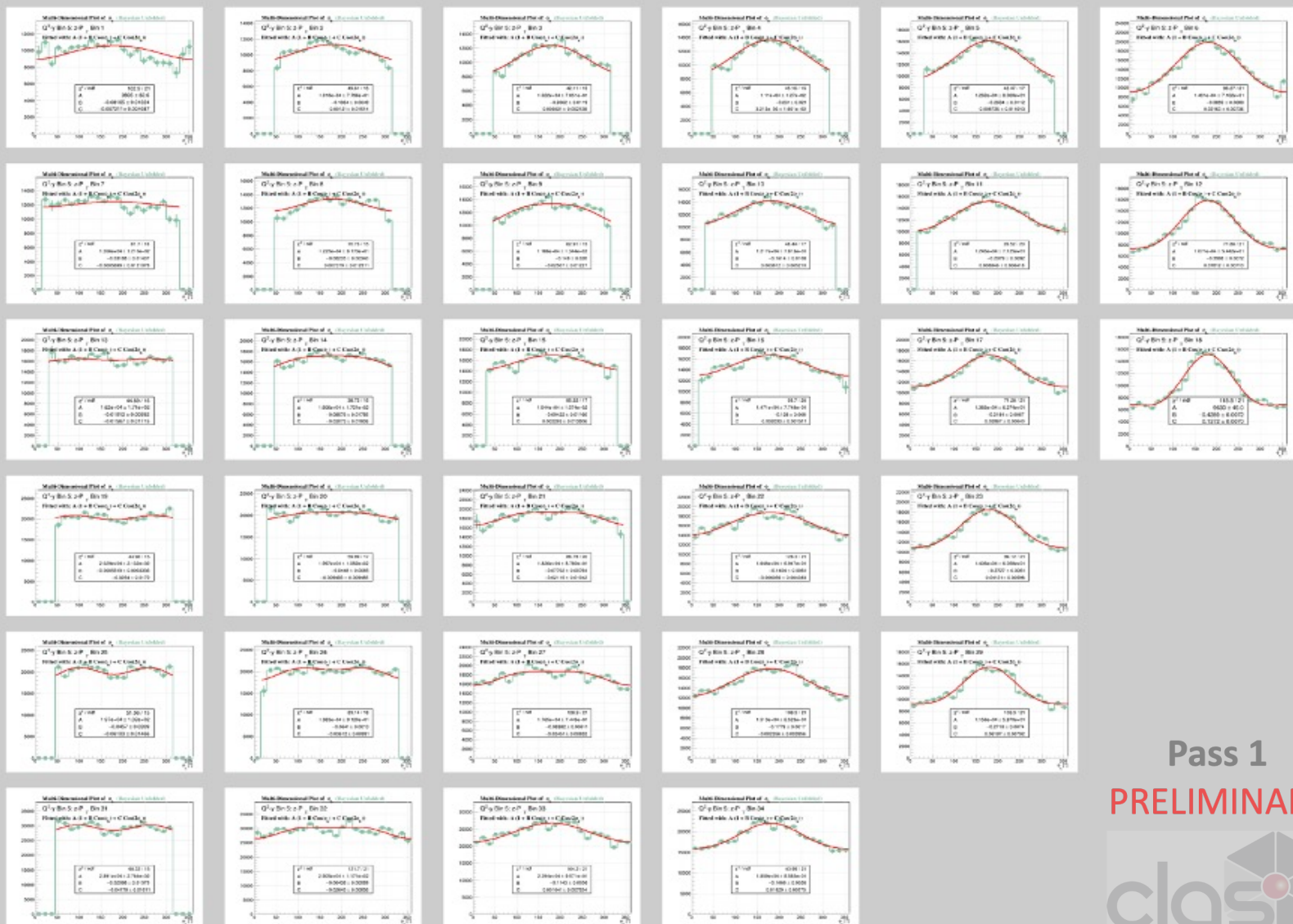
# 3D Unfolding

## Using $z$ - $P_T$ - $\phi_h$ Multidimensional Bins

$Q^2$ -y Bin 5



## Unfolded with Bayesian Method



Pass 1

PRELIMINARY

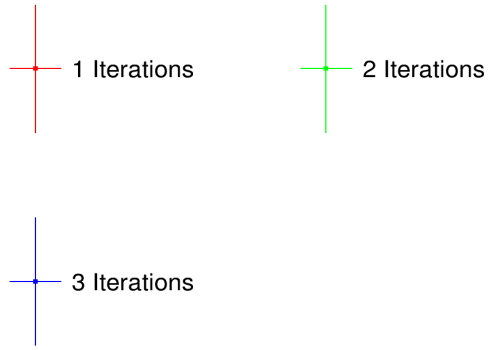


# 5D Unfolding – Iteration Test

Using  $Q^2$ - $y$ - $z$ - $P_T$ - $\phi_h$  Multidimensional Bins

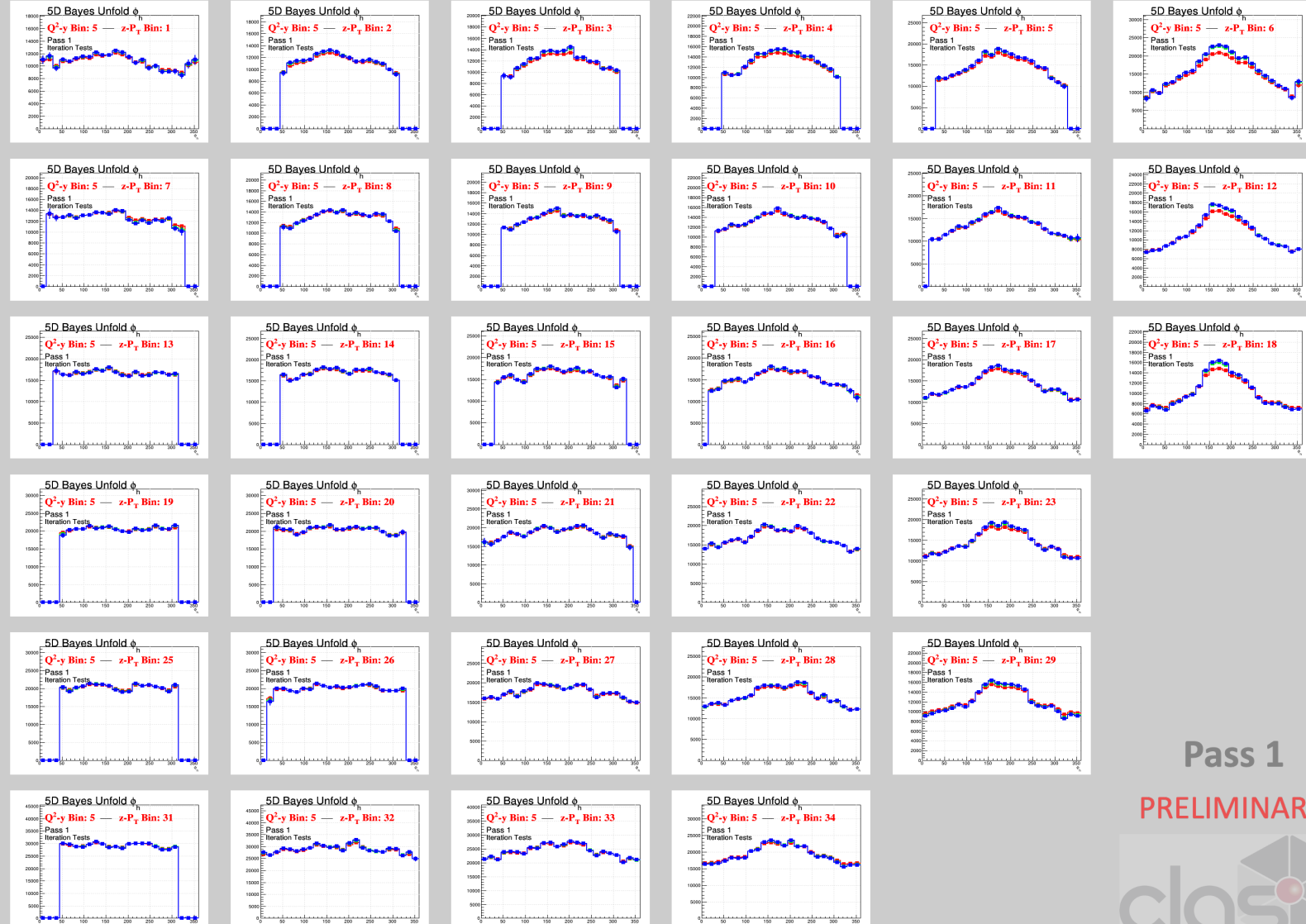
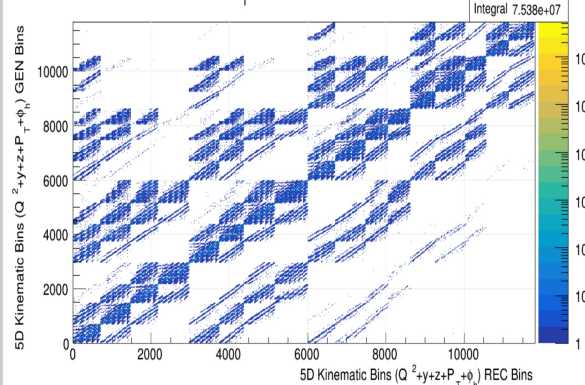
$Q^2$ -y Bin 5

Number of Bayesian Iterations



Response Matrix of 5D Kinematic Bins ( $Q^2+y+z+P_T+\phi_h$ )

Pass 1 — All  $Q^2$ -y-z- $P_T$  Bins — Total Number of Bins: 11816



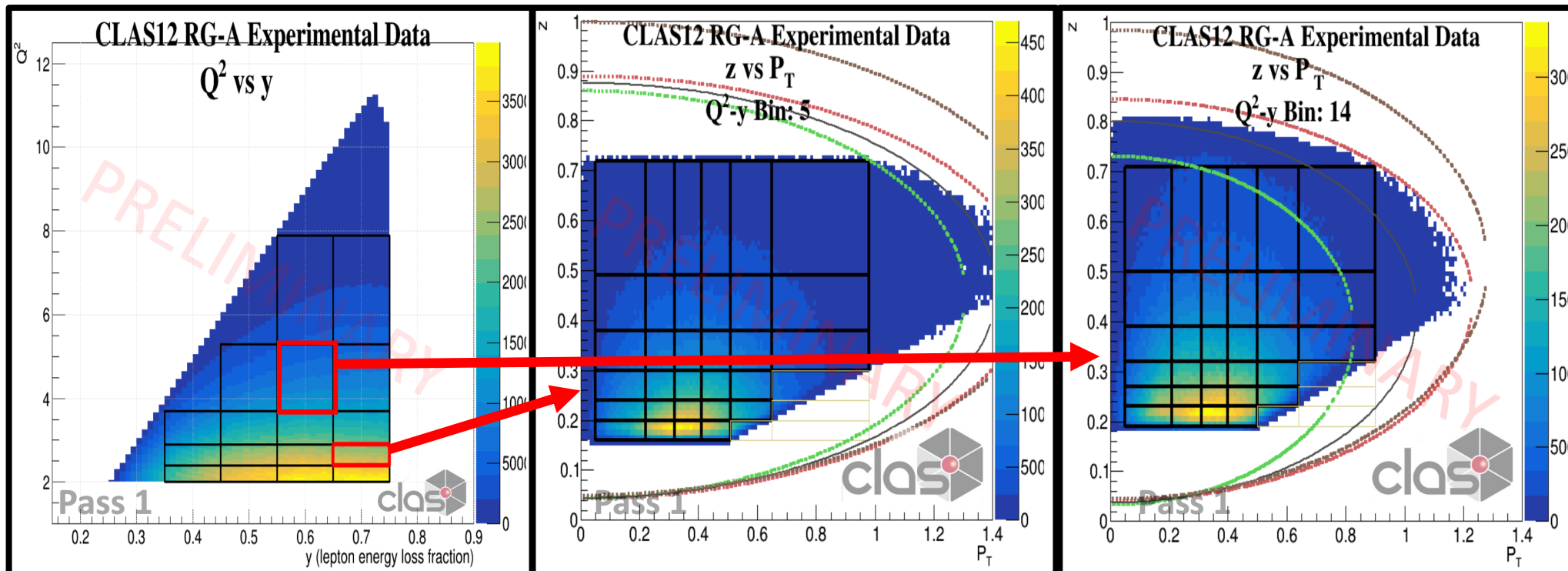
Pass 1

PRELIMINARY



# Migrations from Outside Kinematic Regions

Lines drawn here show Missing Mass Cuts in different  $Q^2$ - $y$  bins



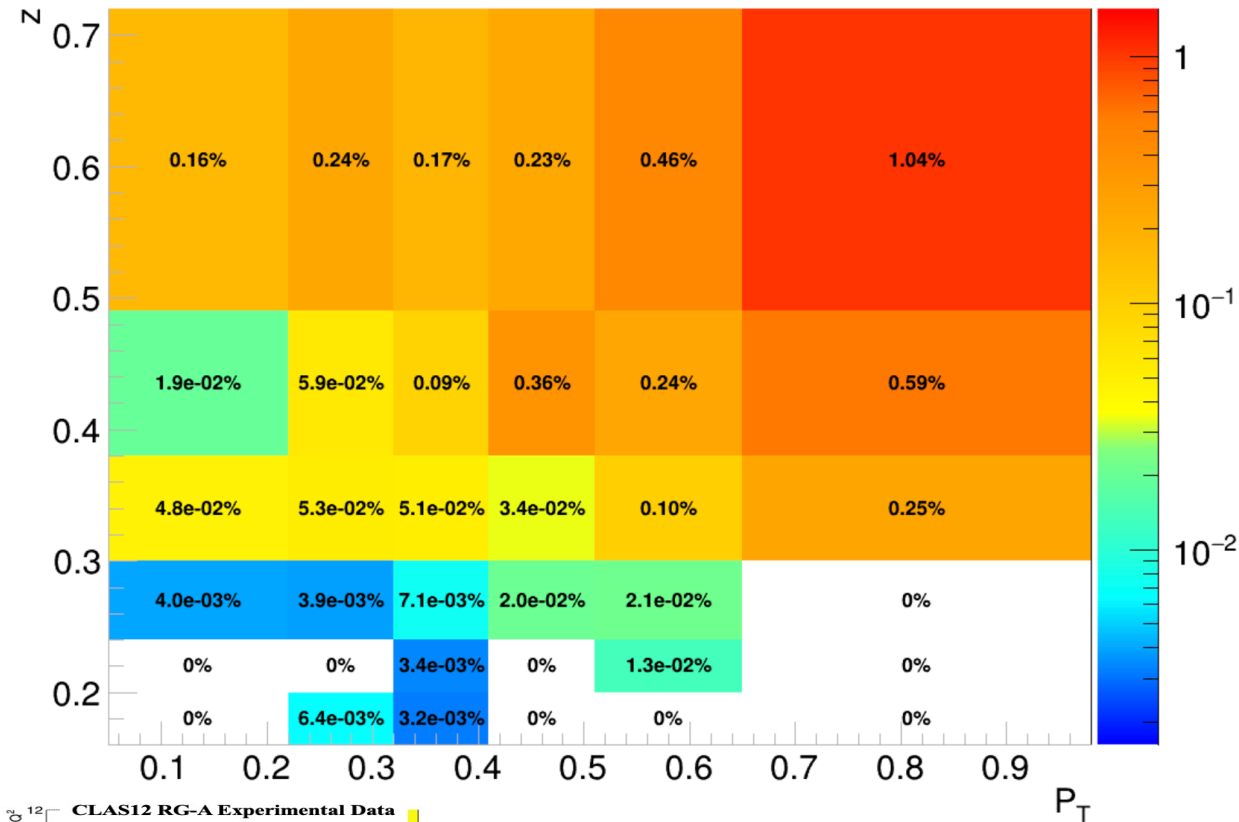
Events migrated from outside the borders of the signal region are removed with  $\beta$  vector in the unfolding procedure

Missing Mass Cut Lines:

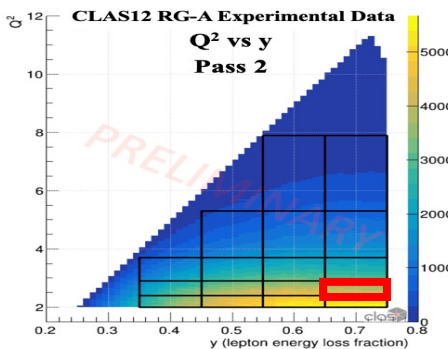
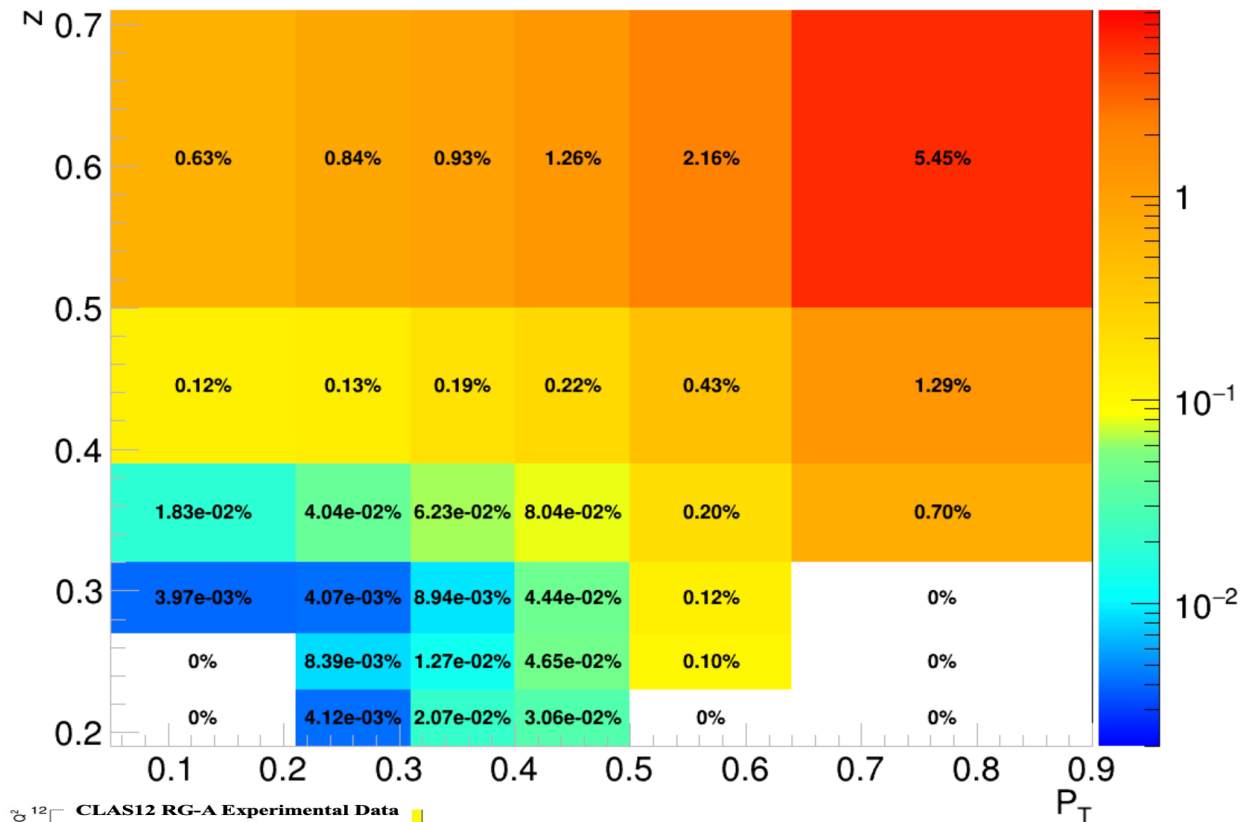


# Missing Mass Migration Contributions (Per $Q^2$ - $y$ Bin)

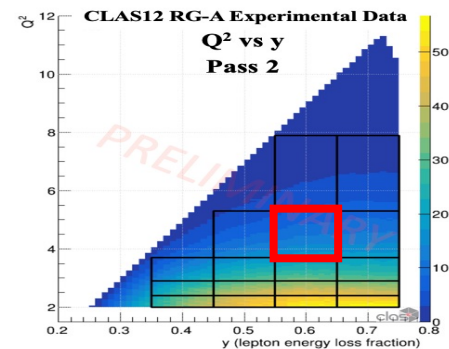
Ratio of Missing Mass Bin Migrations to Total MC Events  
 $Q^2$ - $y$  Bin 5



Ratio of Missing Mass Bin Migrations to Total MC Events  
 $Q^2$ - $y$  Bin 14



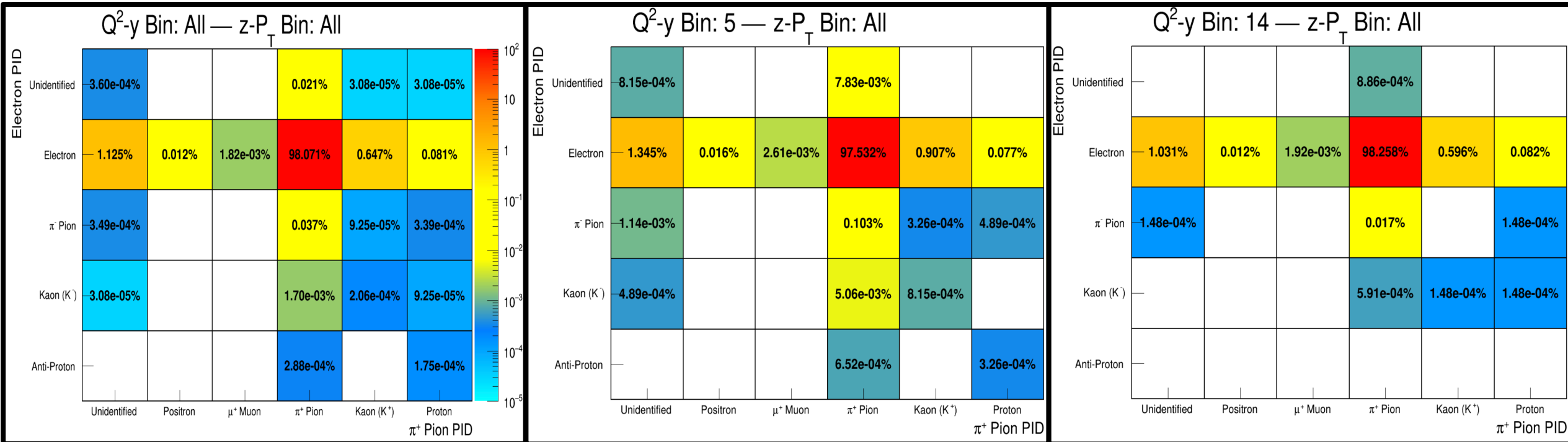
Average Contribution to MC statistics from Missing Mass Migrations per  $z$ - $P_T$  bin in this  $Q^2$ - $y$  region is **0.74%**



Average Contribution to MC statistics from Missing Mass Migrations per  $z$ - $P_T$  bin in this  $Q^2$ - $y$  region is **3.29%**

# Particle Misidentification

## True PID of the MC Events Reconstructed as Electrons/Pions



Meant to model remaining particle misidentification not caught by PID cuts

“Unidentified” Particles are those that had a reconstructed particle that could not be matched to a generated particle within the matching criteria used

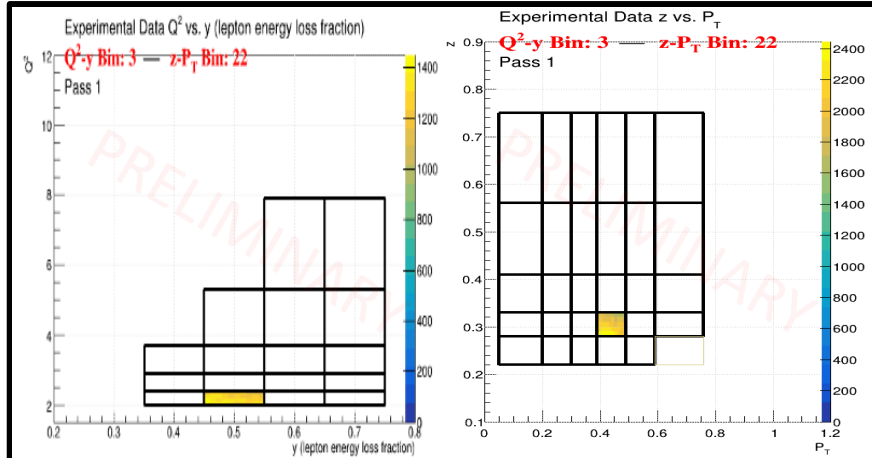
Integrating over z-P<sub>T</sub>: misidentification rate ranges from 1.5-2.5% (depending on Q<sup>2</sup>-y bin), the average is ~1.8%

(About 58% of this is from Unidentified Particles on average)

The misidentification rate within individual z-P<sub>T</sub> Bins ranges from 0.8-6.5%

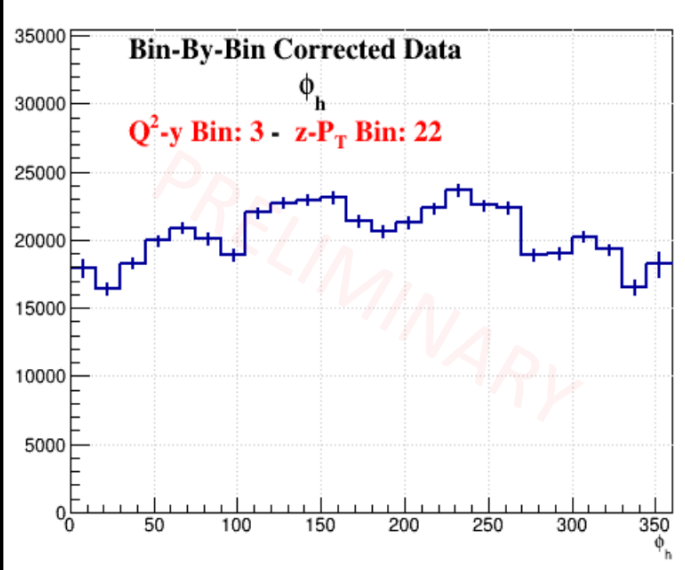
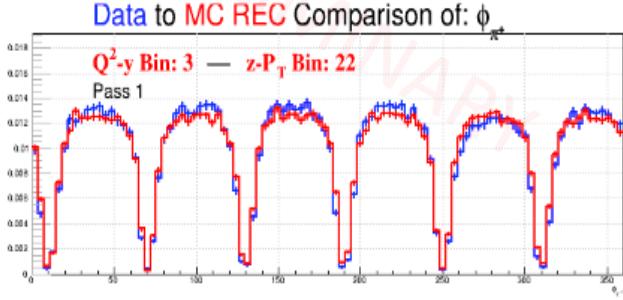
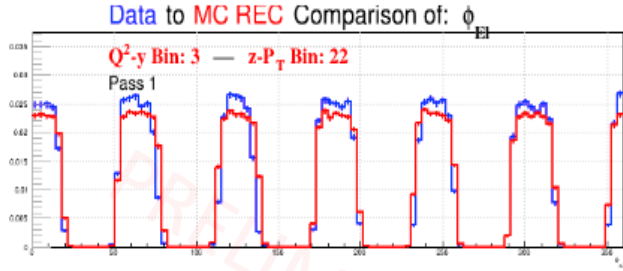
# Sector Dependence of $\phi_h$ Distributions

Comparison of Lab  $\phi$  angles of both particles for Data and MC

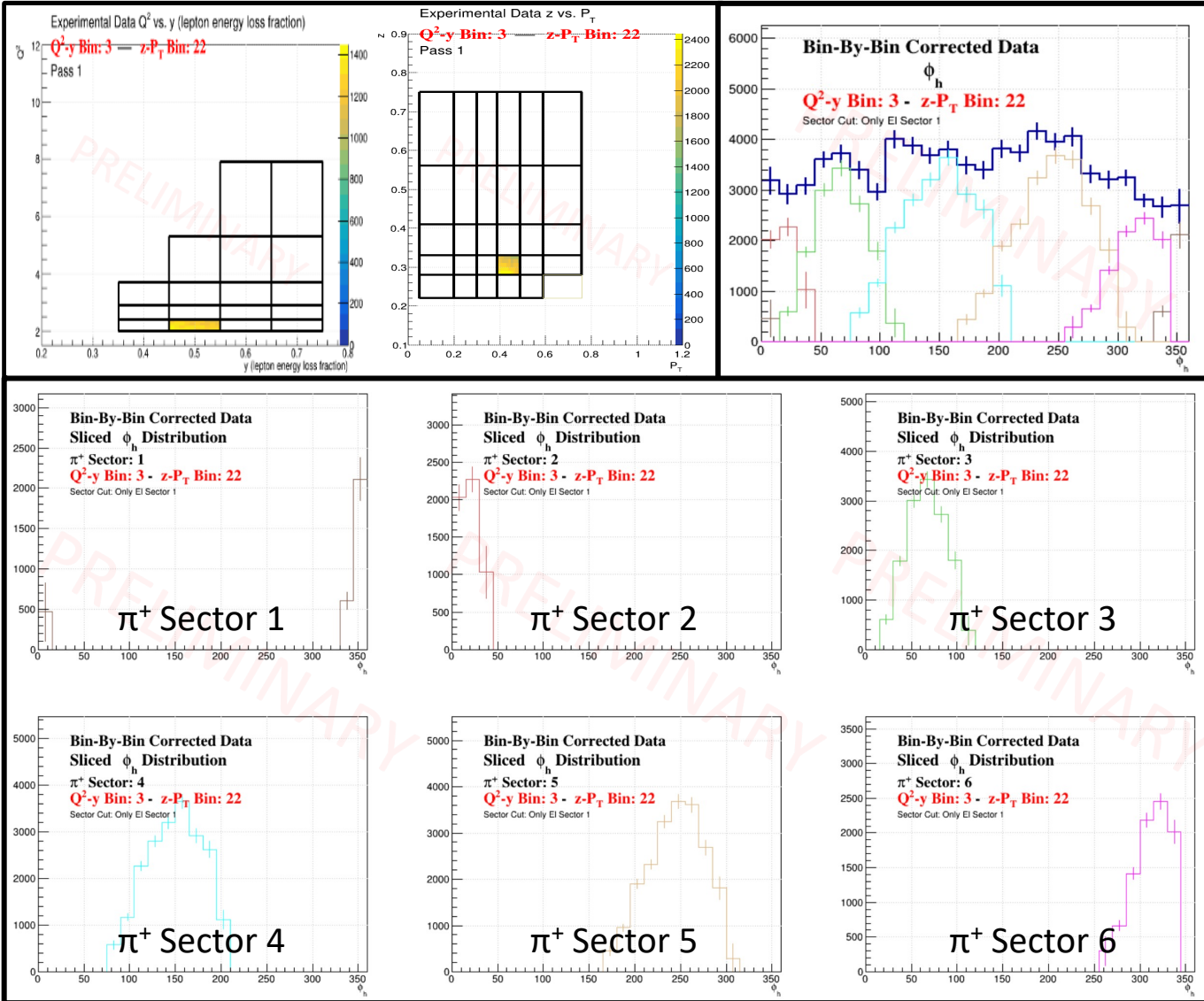


**Issue:** Some bins seem to have additional modulations AFTER Acceptance Corrections not explained by the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  moments

- The 6 peak structure is related to the forward detector sectors



# Sector Dependence of $\phi_h$ Distributions

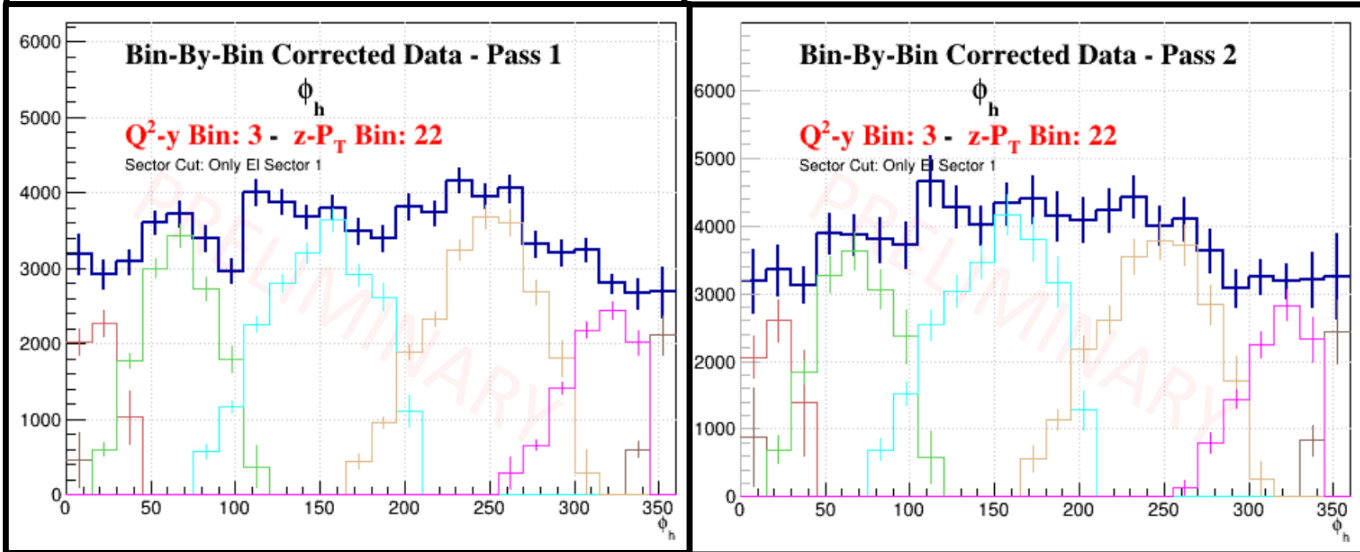
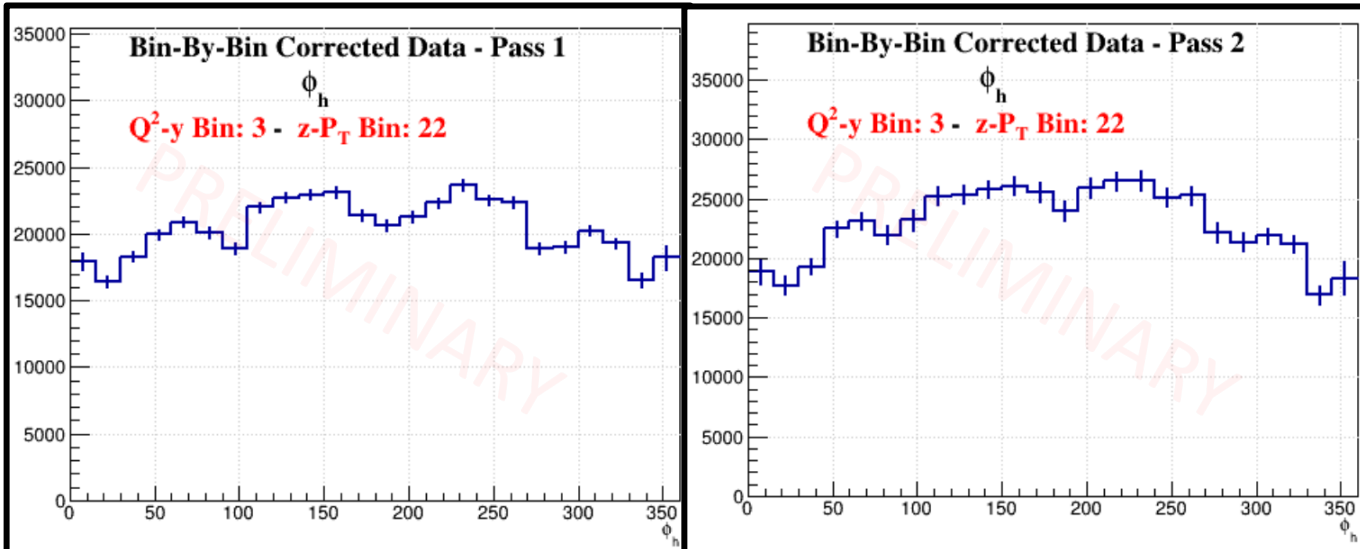


**Issue:** Some bins seem to have additional modulations AFTER Acceptance Corrections not explained by the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  moments

- The 6 peak structure is related to the forward detector sectors
- Plots show the  $\phi_h$  distributions separated based on which sector the  $\pi^+$  pion is detected
- Additional Requirement: Electron in Sector 1
- This suggests that the effect is related to mismatching in sector acceptance between Data and Monte Carlo



# Sector Dependence of $\phi_h$ Distributions – Pass 2 Comparison



Pass 1

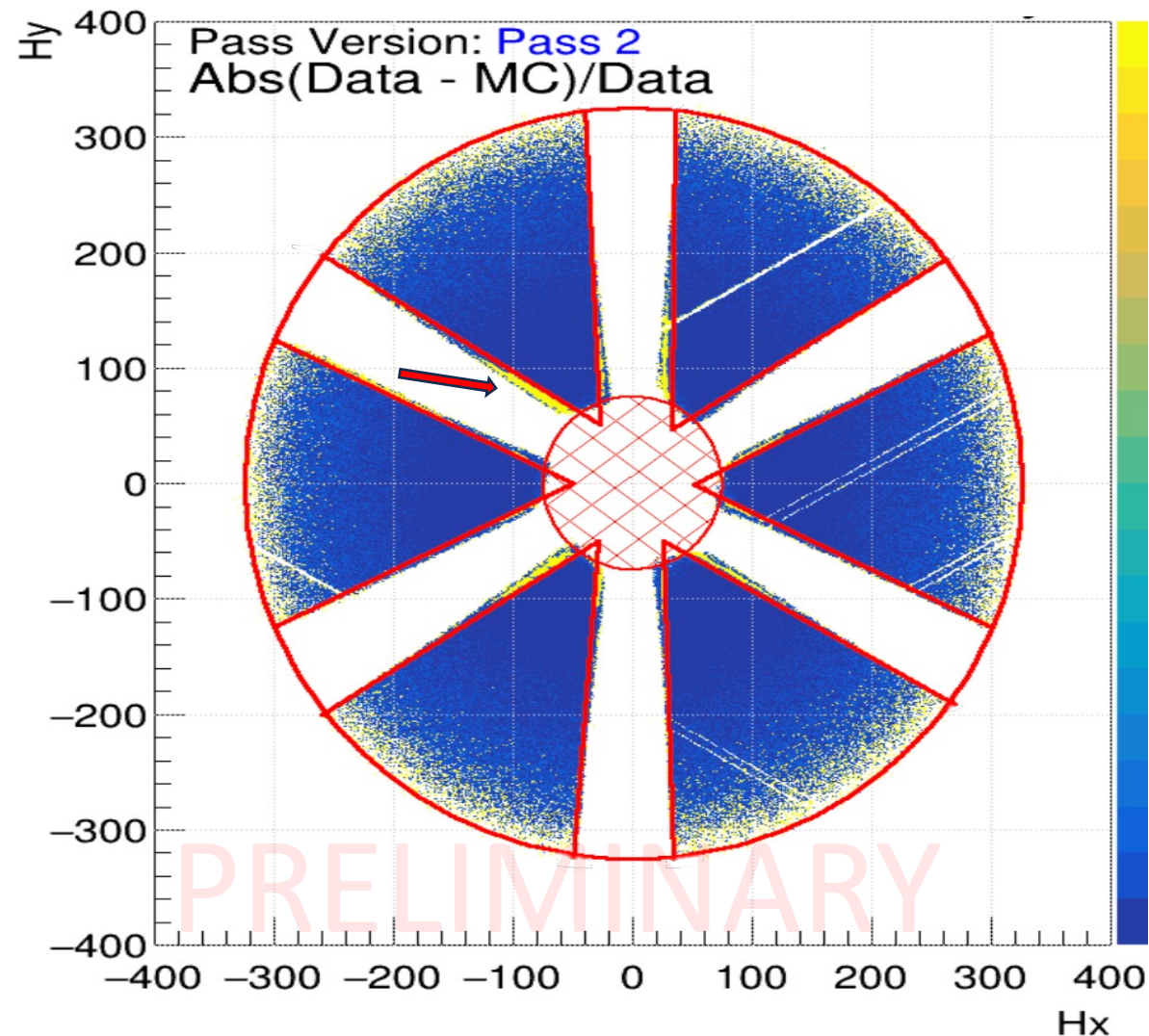
Pass 2

**Issue:** Some bins seem to have additional modulations AFTER Acceptance Corrections not explained by the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  moments

- The 6 peak structure is related to the forward detector sectors
- Plots show the  $\phi_h$  distributions separated based on which sector the  $\pi^+$  pion is detected
- Additional Requirement: Electron in Sector 1
- This suggests that the effect is related to mismatching in sector acceptance between Data and Monte Carlo
- Also present in Pass 2

# Refinement of Fiducial Cuts

## Electron Hit Position Comparison



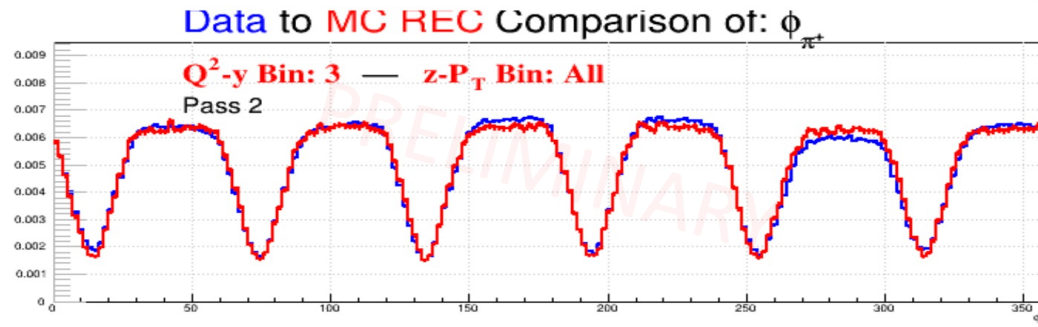
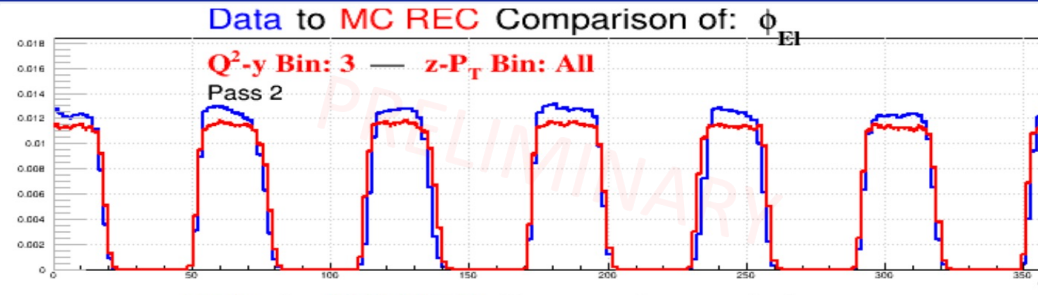
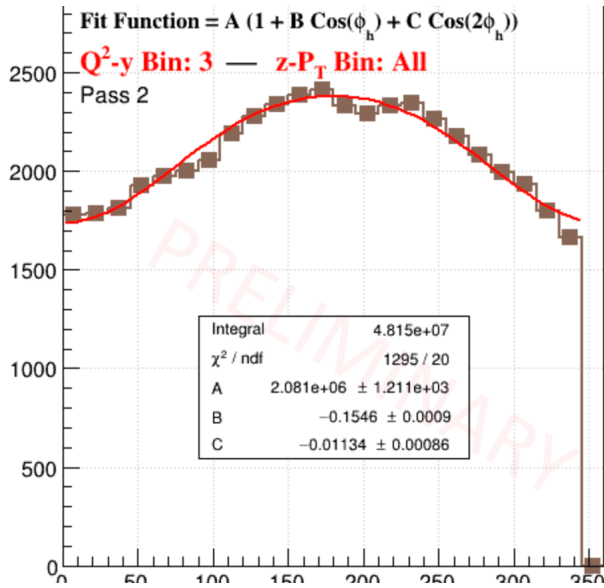
Shows the Percent Difference between the Normalized Data and Reconstructed MC For Electrons in the Particle Calorimeter

The highlighted regions show where the percent difference between Data and MC exceeds 100%

Red Lines show new (preliminary) fiducial cuts to be added

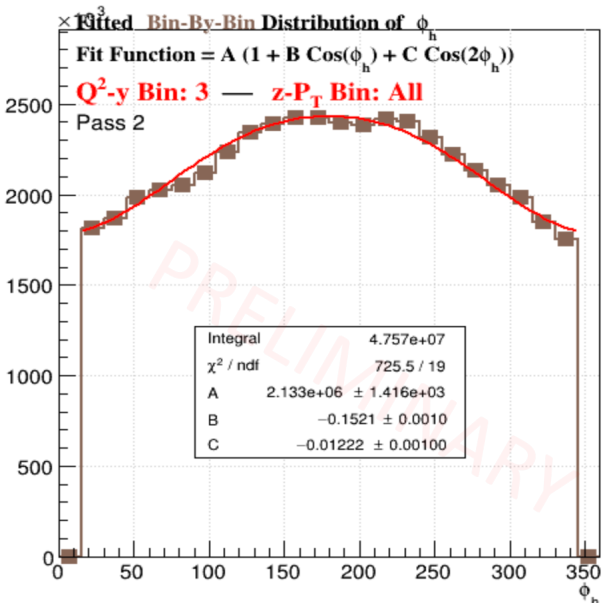
# Impact of New Fiducial Cuts – Integrated $z$ - $P_T$ Bin

Before  
New  
Cuts

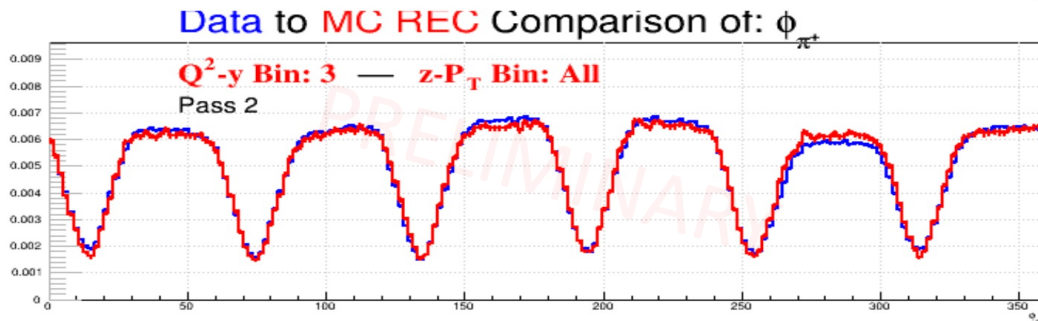
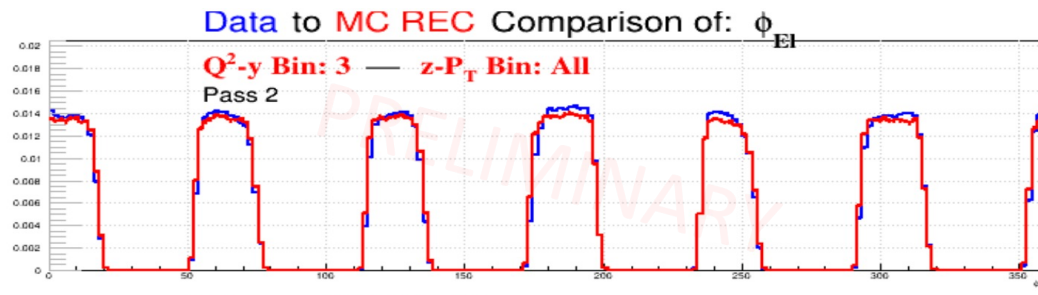


Discrepancies are more noticeable with integrated  $z$ - $P_T$  bins

After  
New  
Cuts



← Much  
Better  
 $\chi^2$

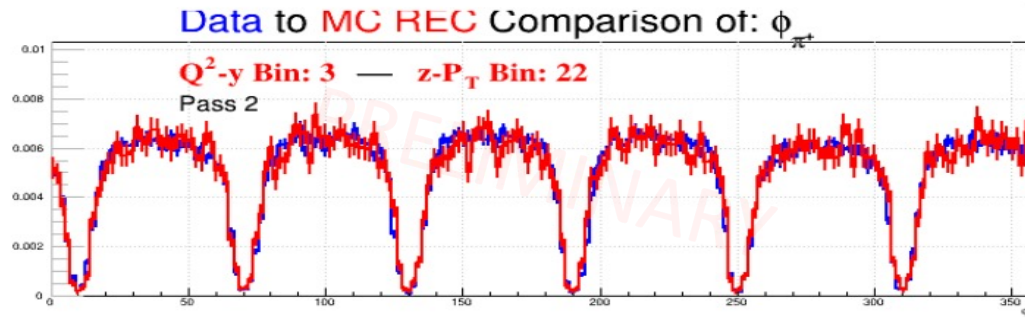
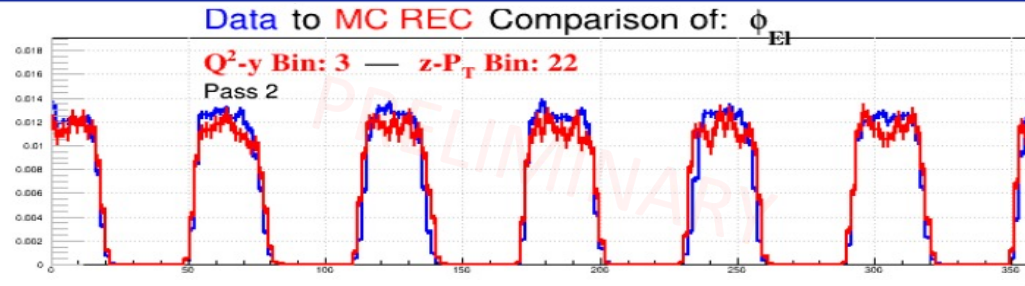
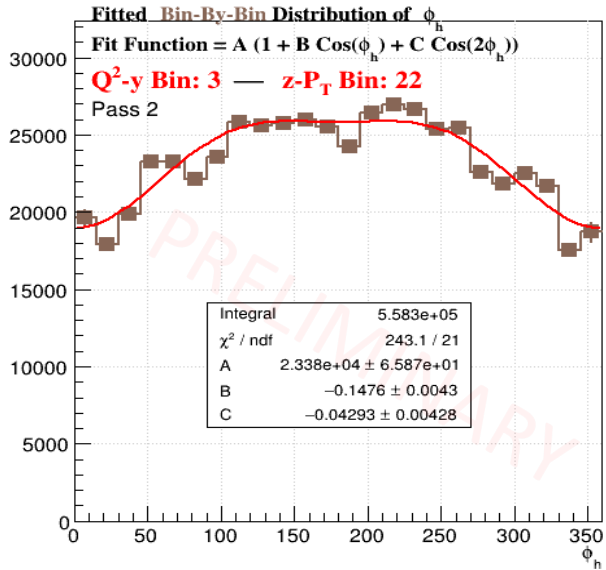


← Much better agreement between the lab angles of both particles

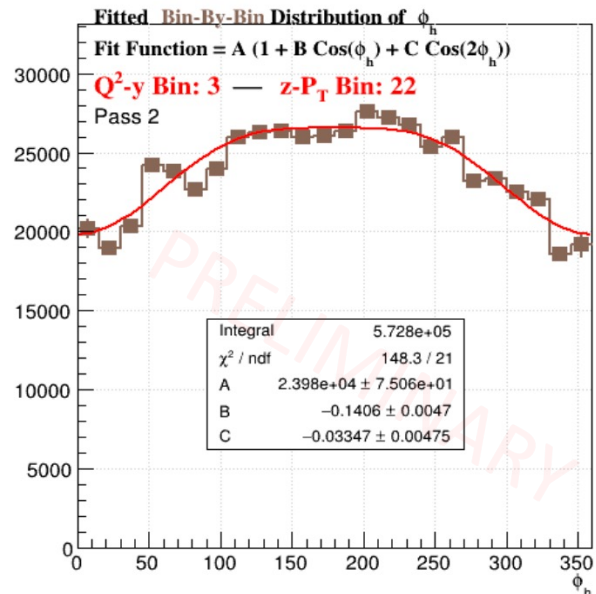
Cut starts to reduce (some) of the additional modulations for a smoother distribution of  $\phi_h$

# Impact of New Fiducial Cuts – Individual $z$ - $P_T$ Bin

Before  
New  
Cuts

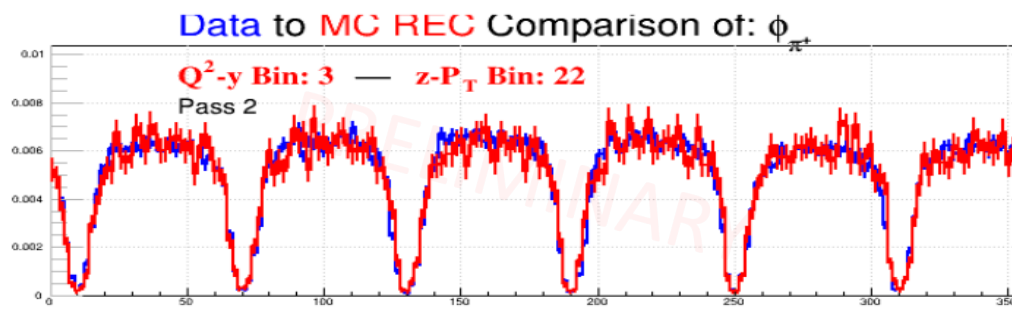
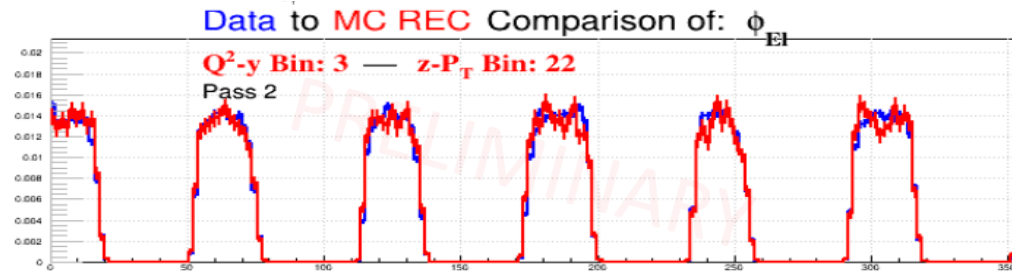


After  
New  
Cuts



← Much  
Better  
 $\chi^2$

20



← Much better agreement  
between the lab angles of  
both particles

Cut starts to reduce  
(some) of the  
additional modulations  
for a smoother  
distribution of  $\phi_h$

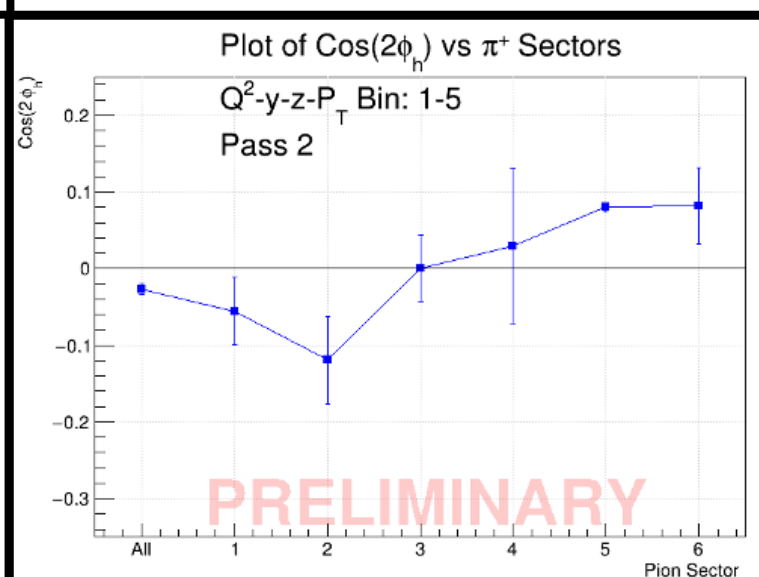
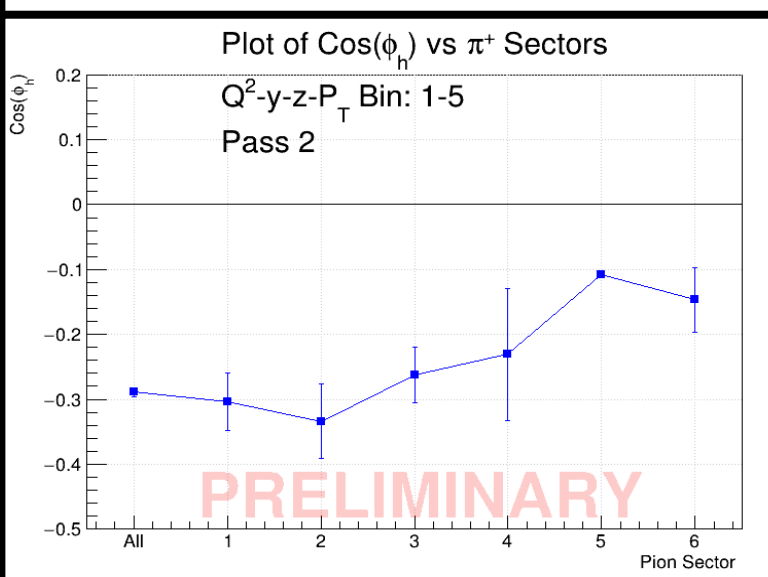
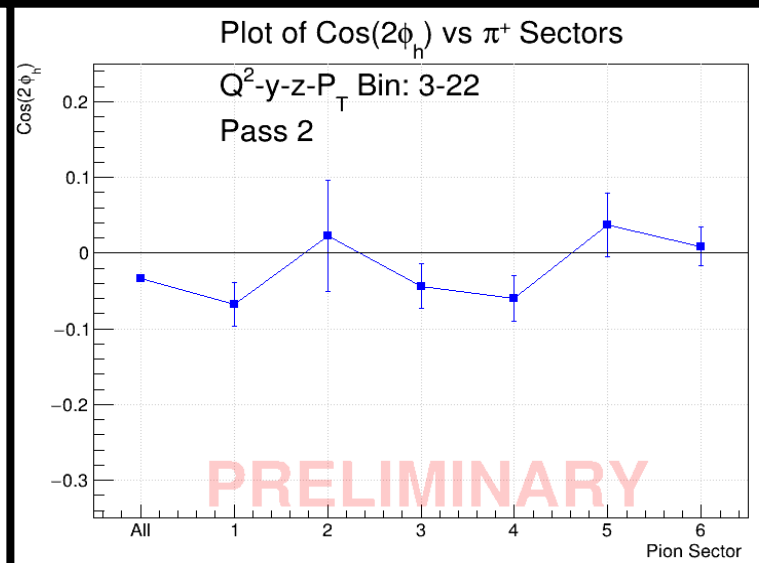
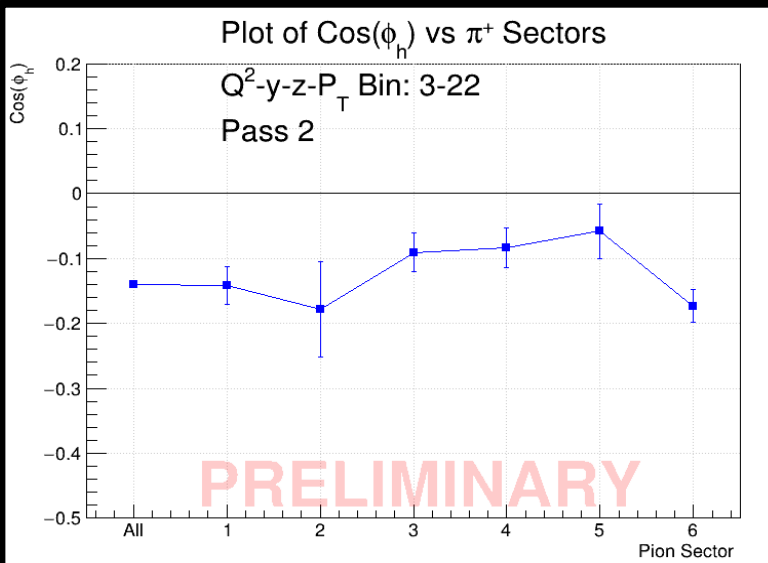
# (Pion) Sector Correlations with $\text{Cos}(\phi)$ and $\text{Cos}(2\phi)$ Measurements

Some sector dependence remains despite the new cuts

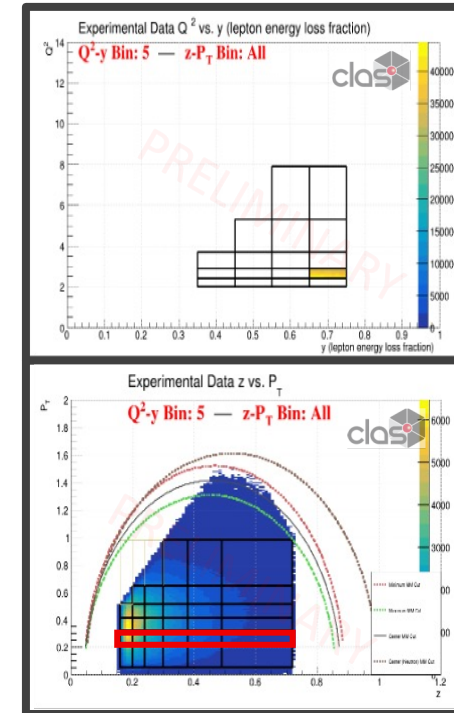
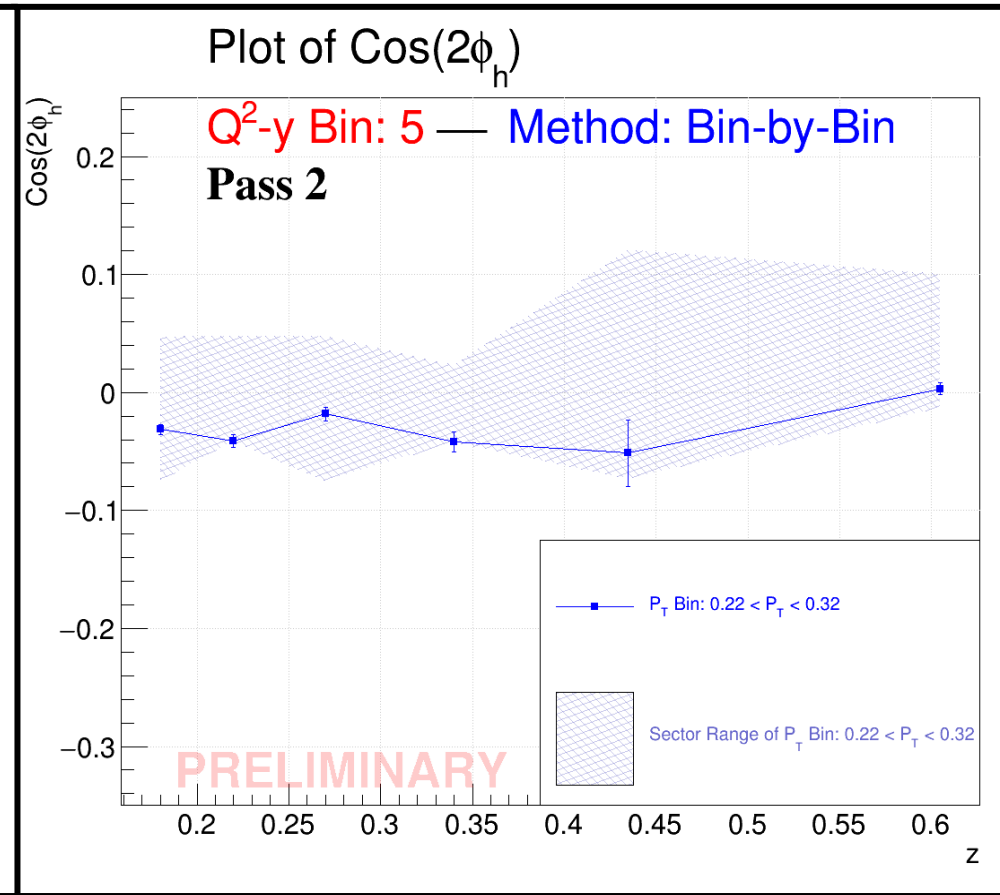
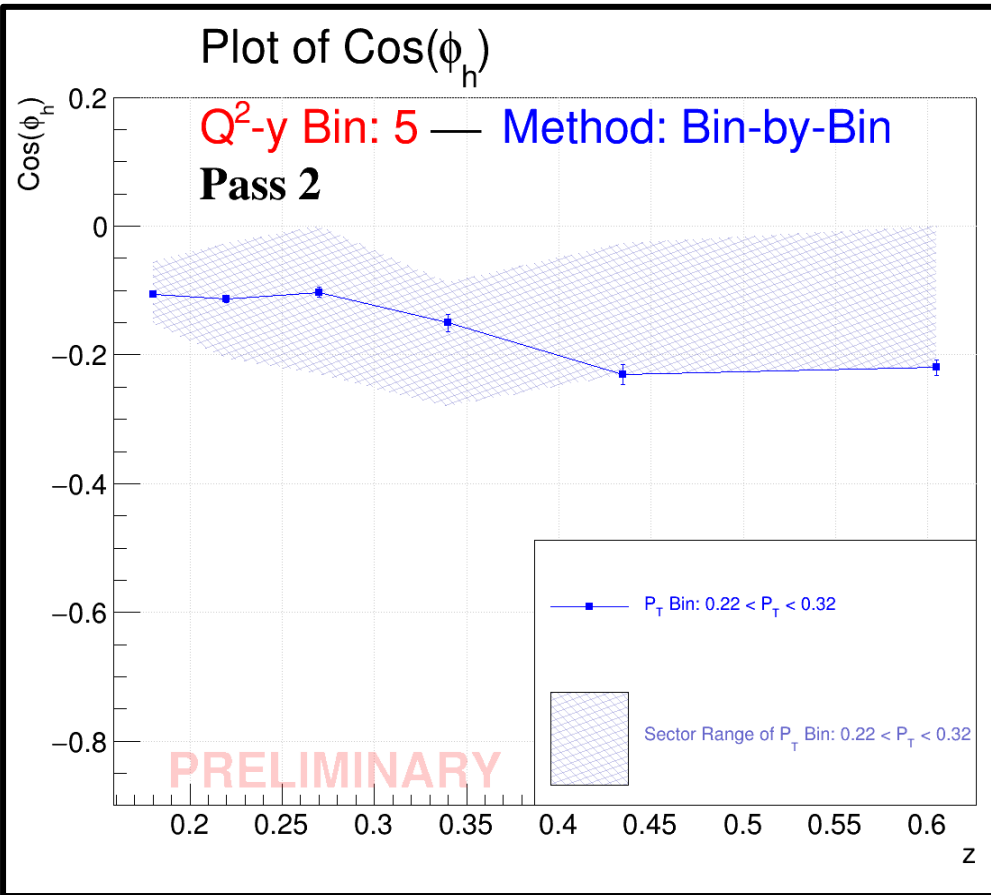
On average, the particle sector makes a noticeable difference about 50% of the time\* (i.e., the measurements of each sector do not agree with the measurement taken without sector dependence within the errors shown)

A sector dependence does seem to exist, but further investigation is still required

\*Some of these discrepancies can be blamed on individual fits failing due to even worse acceptances that have not yet been individually addressed

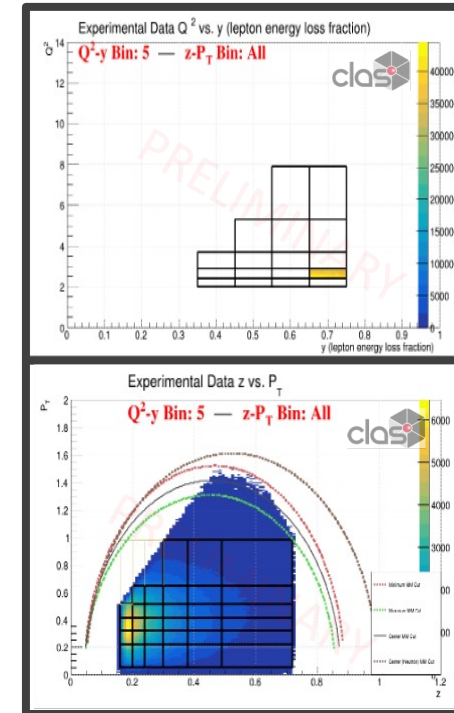
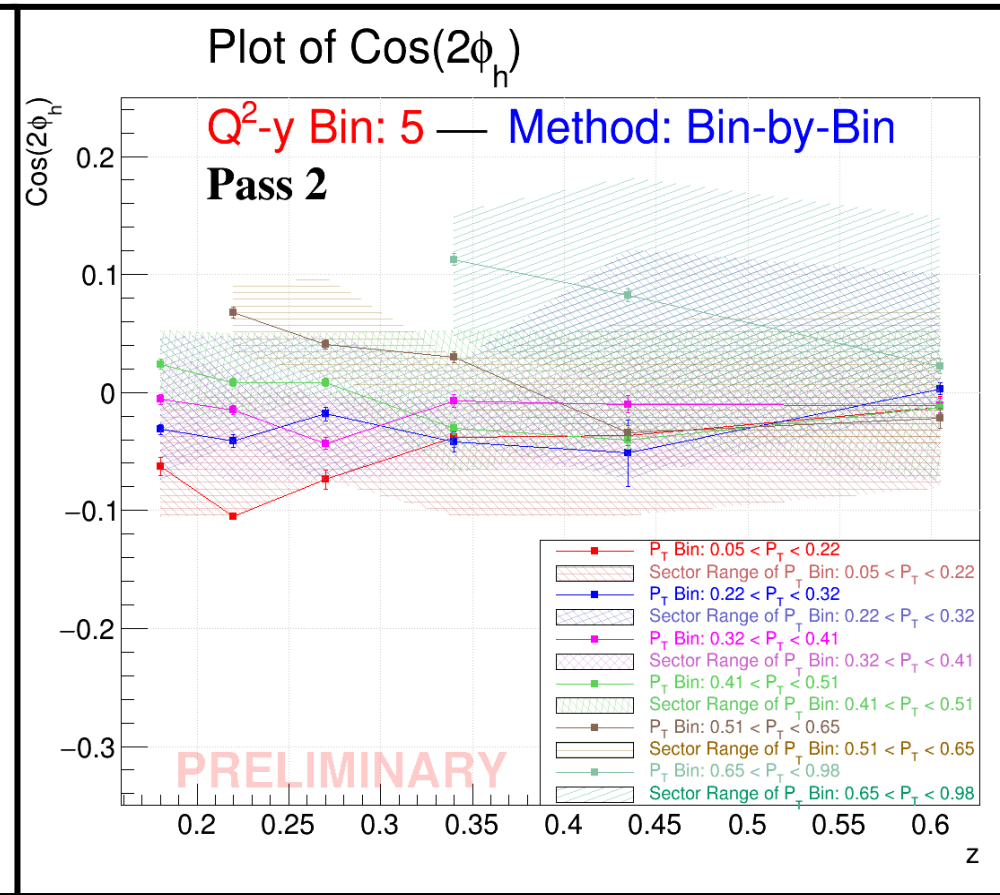
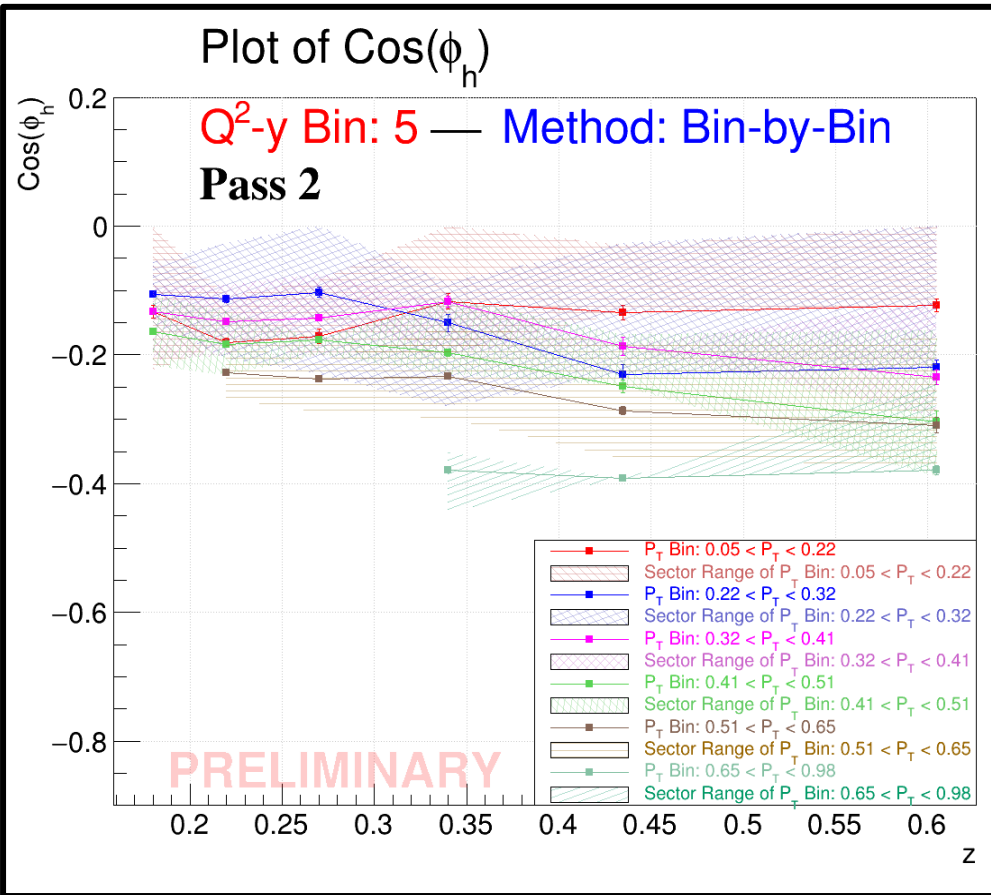


# (Pion) Sector Correlations with $\text{Cos}(\phi)$ and $\text{Cos}(2\phi)$ Measurements



The shaded regions show the ranges of sector dependence on these measurements  
Further refinements to limit this dependence are ongoing

# (Pion) Sector Correlations with $\text{Cos}(\phi_h)$ and $\text{Cos}(2\phi_h)$ Measurements



The shaded regions show the ranges of sector dependence on these measurements  
Further refinements to limit this dependence are ongoing

# Monte Carlo Smearing

- Momentum Smearing Corrections are designed to match the resolution effects between MC and Experimental data
- Uses exclusive reactions to compare the widths of distributions from the exclusive reactions in both data sets
  - The primary reaction used for the electron and  $\pi^+$  pion is  $e p \rightarrow e' \pi^+(N)$
  - Follows a similar process as was used for developing Momentum Corrections for the experimental data
    - i.e., use momentum conservation calculations to derive a  $\Delta P$  value between the predicted and measured momentums of a particle based on the kinematics of the other measured particle
    - Momentum smearing is focused on correcting the widths of the distributions instead of the peaks
  - Smearing functions are based on  $\Delta P/P$  vs  $\theta$  plots



# Data and Monte Carlo Comparison (Smearing)

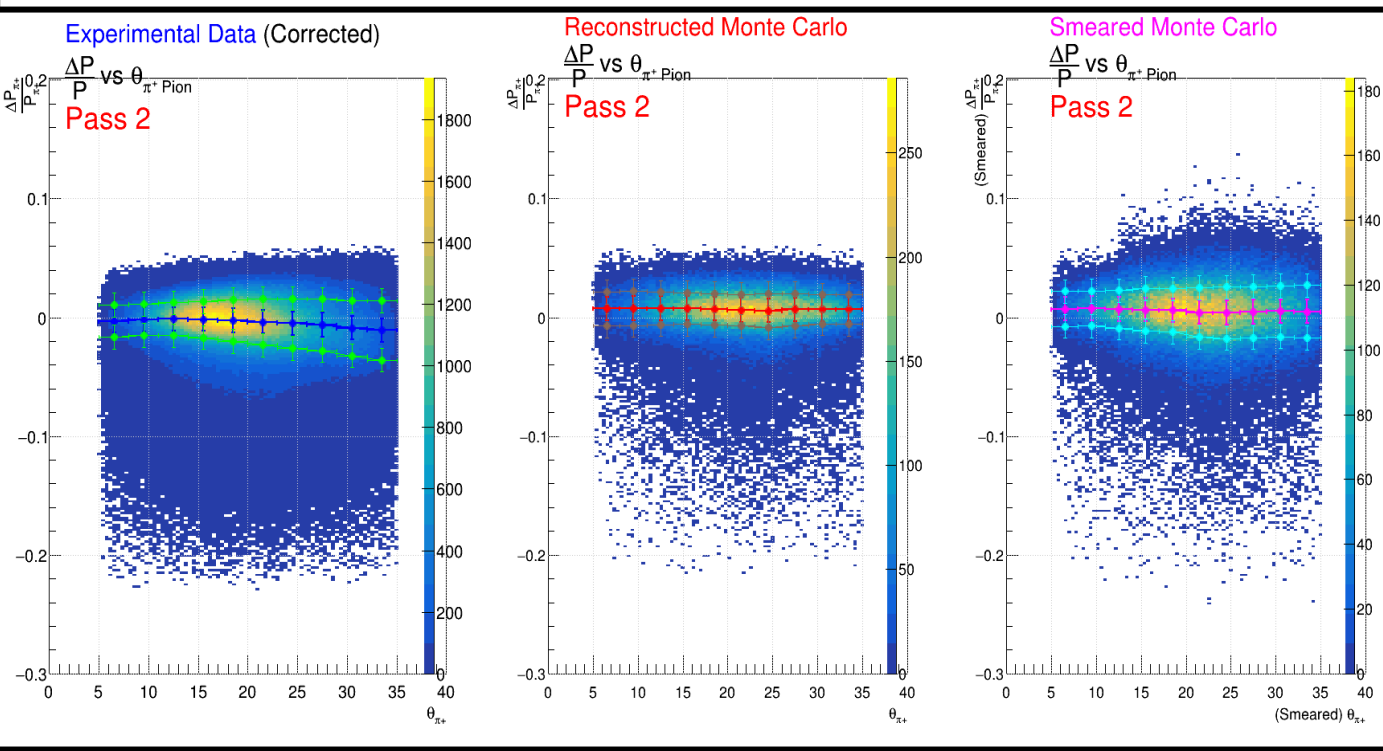
## Smearing for the $\pi^+$ Pion

Form of Smearing Function:

$$P_{Smearred} = P_{REC} + gRandom \rightarrow Gaus(0, P_{REC} * \sigma(\theta) * SF)$$

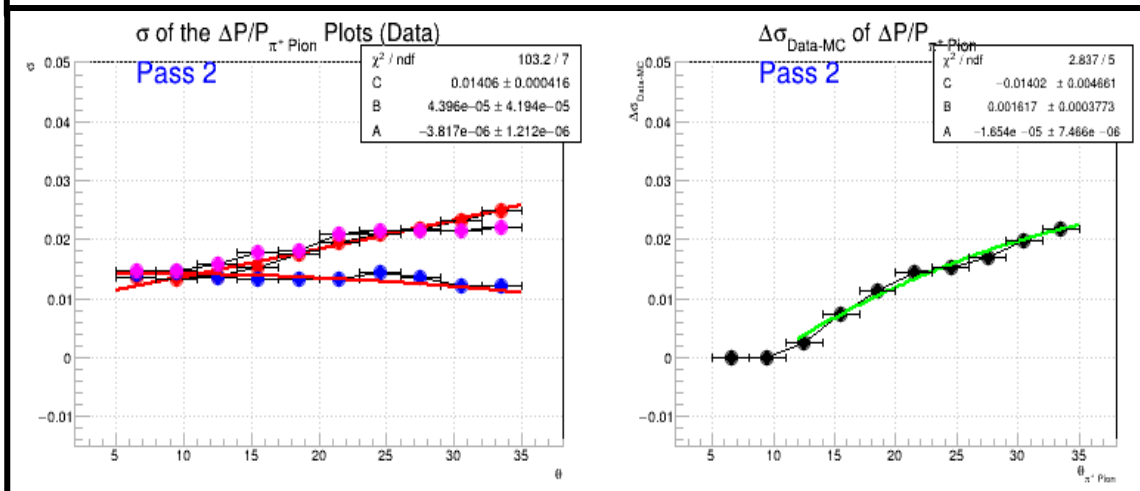
- $\sigma(\theta)$  is the difference in the widths of  $\Delta P/P$  for the Unsmearred MC and Data plots
- $SF$  is a constant factor that provides more control over the function's strength

Plots of  $\Delta P/P$  vs  $\theta$  for Data, Unsmearred MC, and Smearred MC



Shown with the peak positions and widths of the fitted distributions

Difference between widths of Smearred MC and Data



# Data and Monte Carlo Comparison (Smearing)

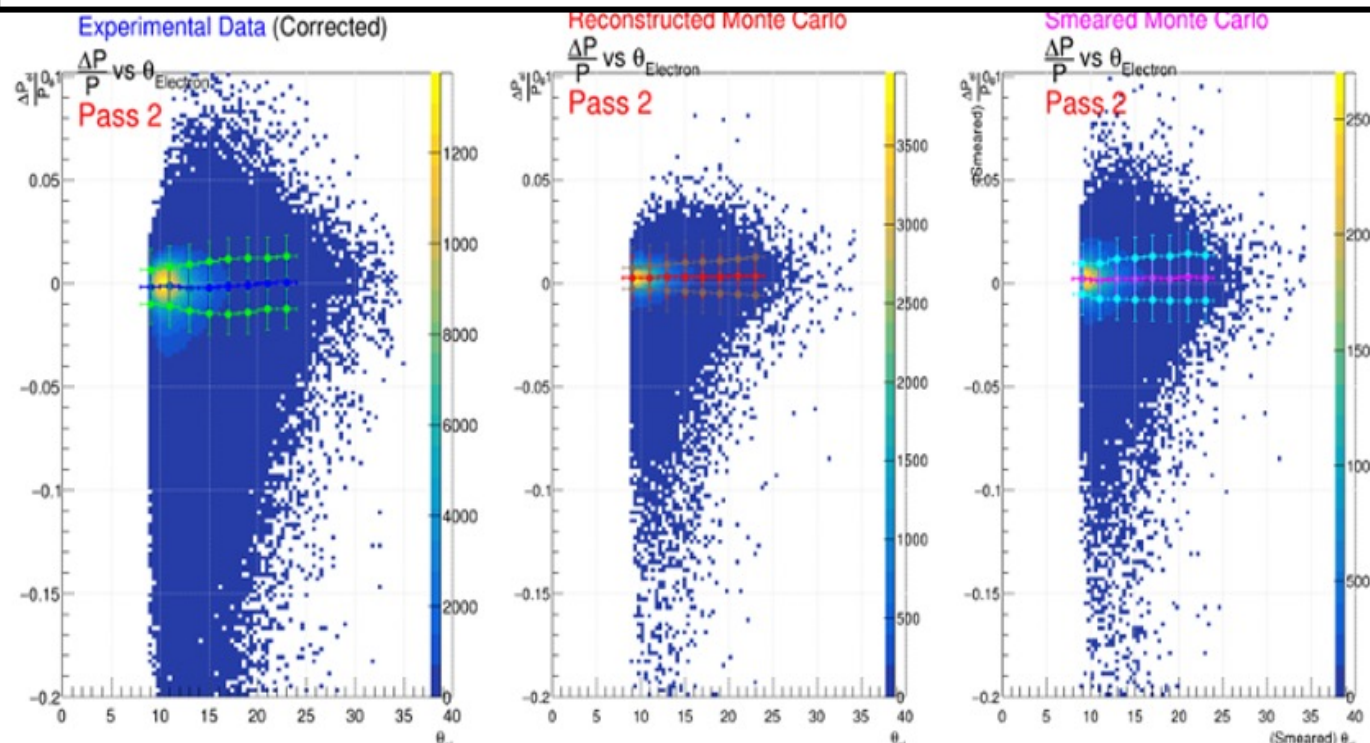
## Smearing for the Electron

Form of Smearing Function:

$$P_{Smearred} = P_{REC} + gRandom \rightarrow Gaus(0, P_{REC} * \sigma(\theta) * SF)$$

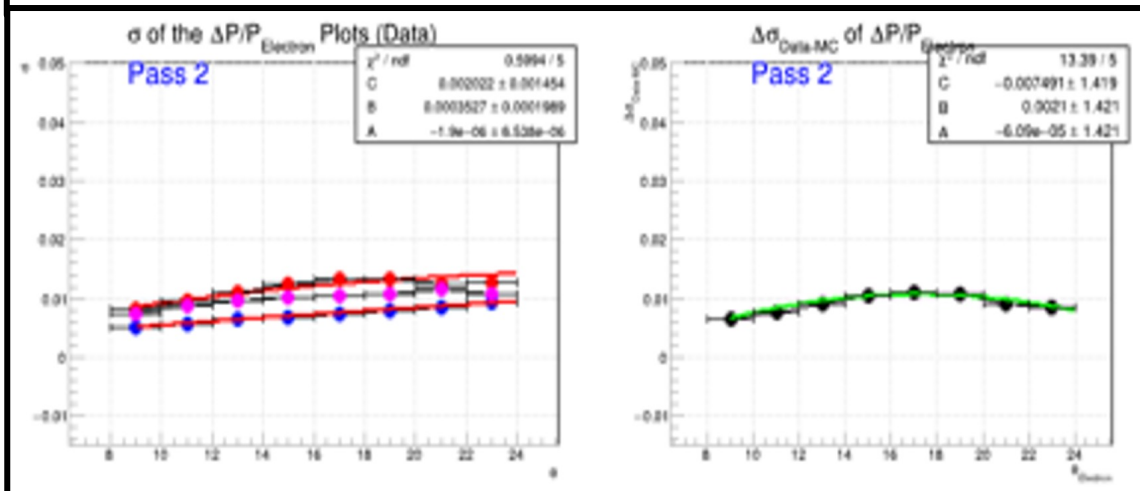
- $\sigma(\theta)$  is the difference in the widths of  $\Delta P/P$  for the Unsmearred MC and Data plots
- $SF$  is a constant factor that provides more control over the function's strength

Plots of  $\Delta P/P$  vs  $\theta$  for Data, Unsmearred MC, and Smearred MC



Shown with the peak positions and widths of the fitted distributions

Difference between widths of Smearred MC and Data



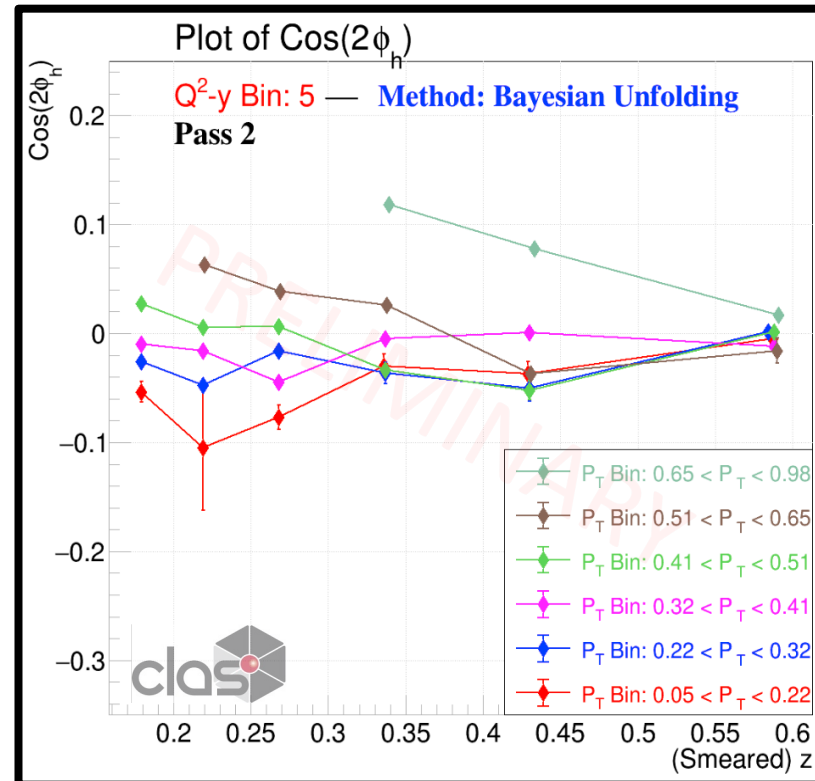
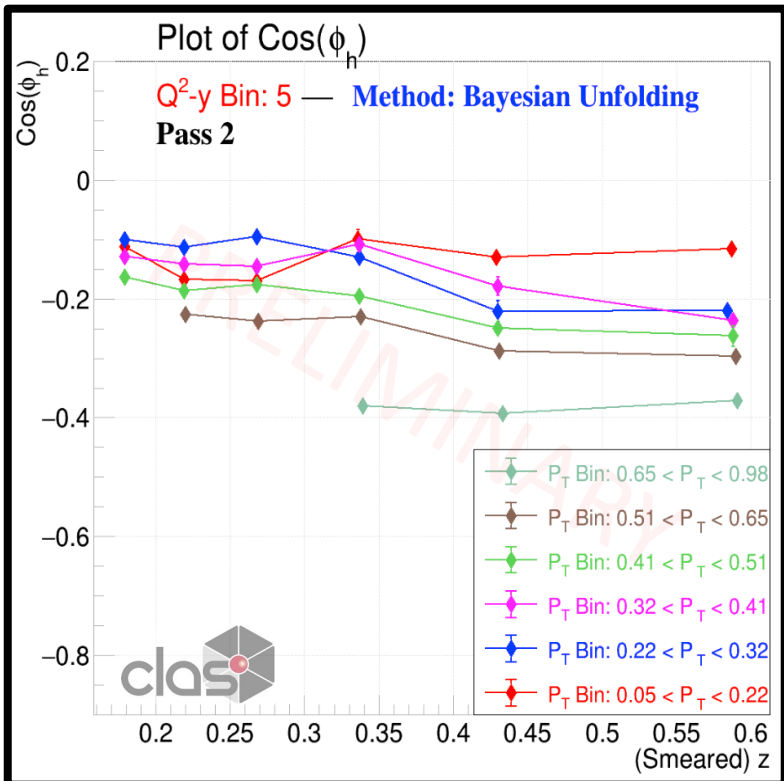
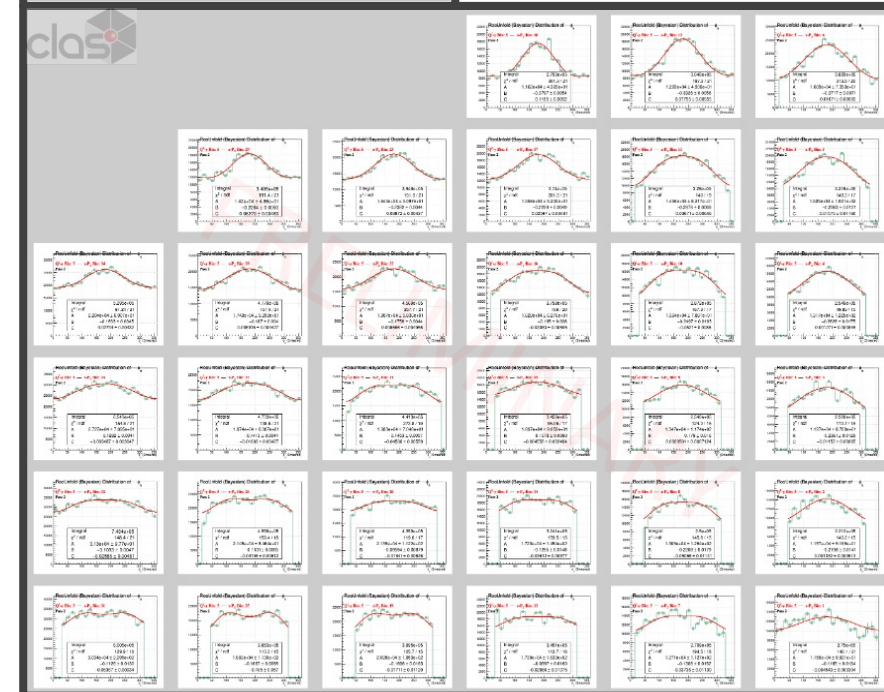
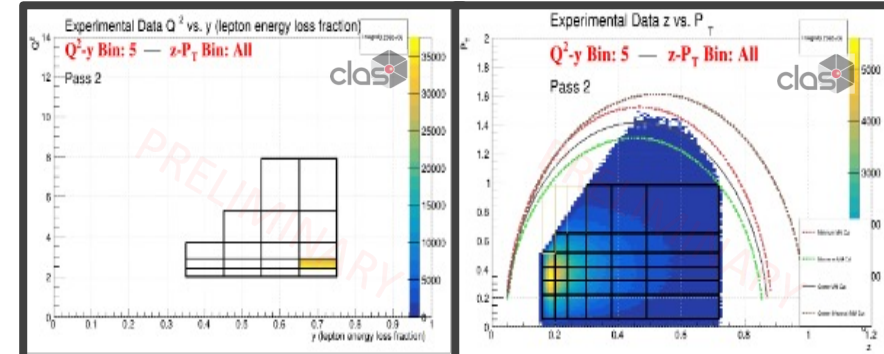
# Cosine Moments as Functions of z

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

Q<sup>2</sup>-y Bin 5



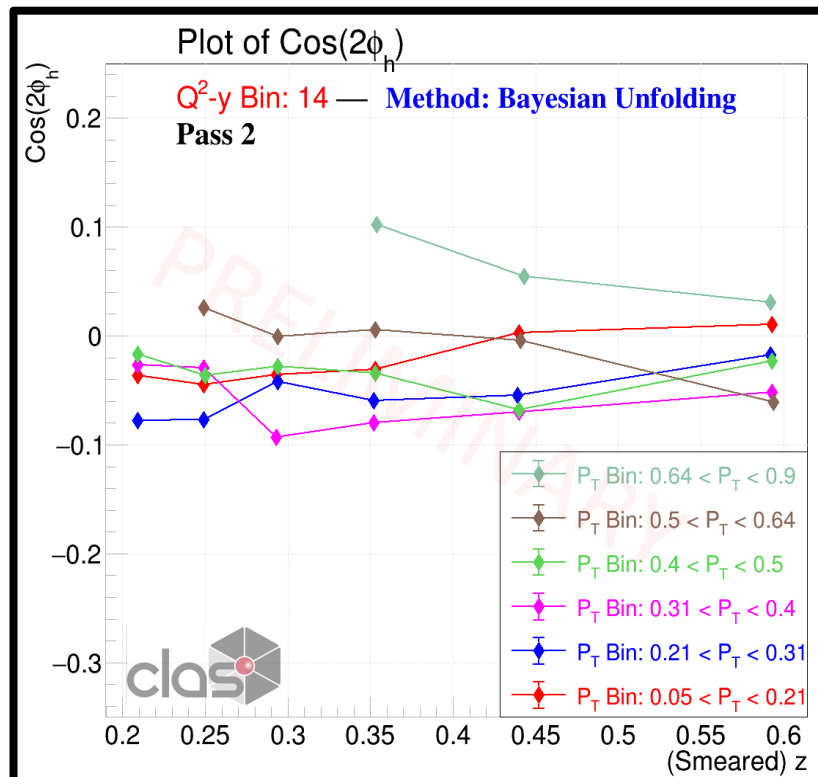
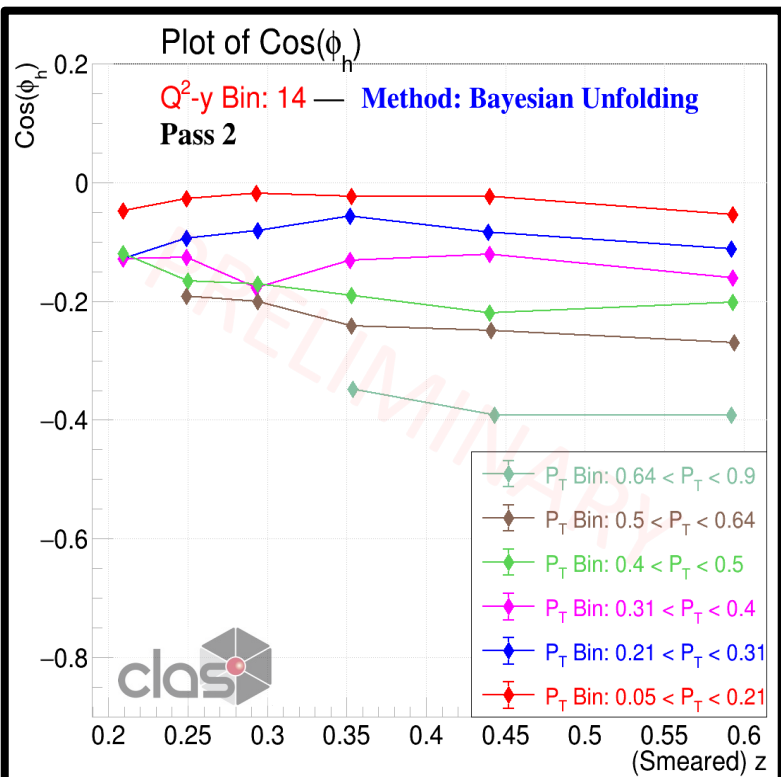
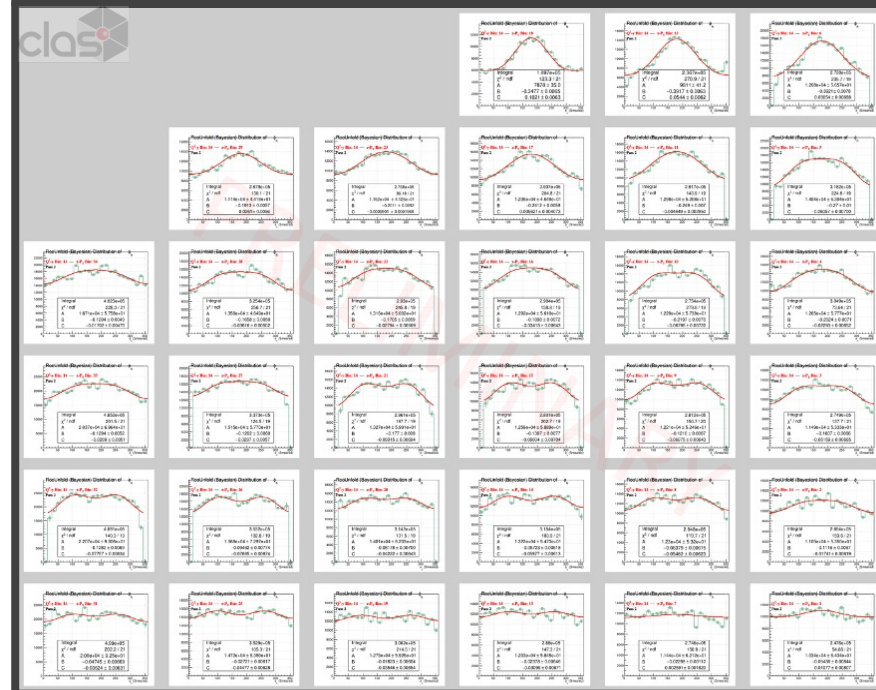
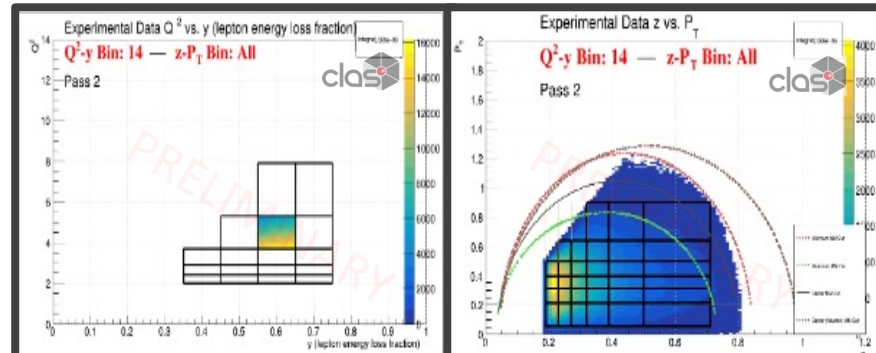
# Cosine Moments as Functions of z

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

Q<sup>2</sup>-y Bin 14



# Summary

- Analysis switched to Pass 2 Data
- Finalizing tests for applying the Multidimensional (5D) Acceptance Corrections for the simultaneous unfolding of  $Q^2$ ,  $\gamma$ ,  $z$ ,  $P_T$ , and  $\phi_h$  variables
  - Addressed migrations from outside the kinematic region
- Momentum Smearing Corrections applied to the Monte Carlo
- Began evaluation of systematic uncertainties related to sector dependence
- New Fiducial Cuts Added
  - Still optimizing

# Outlook

- Further Investigations regarding Sector Dependences
- Working on adding more Pass 2 simulations
- Working on including Radiative Corrections in this analysis
- Ongoing Investigations of Vector Meson Contributions

# Thank you

# Questions?

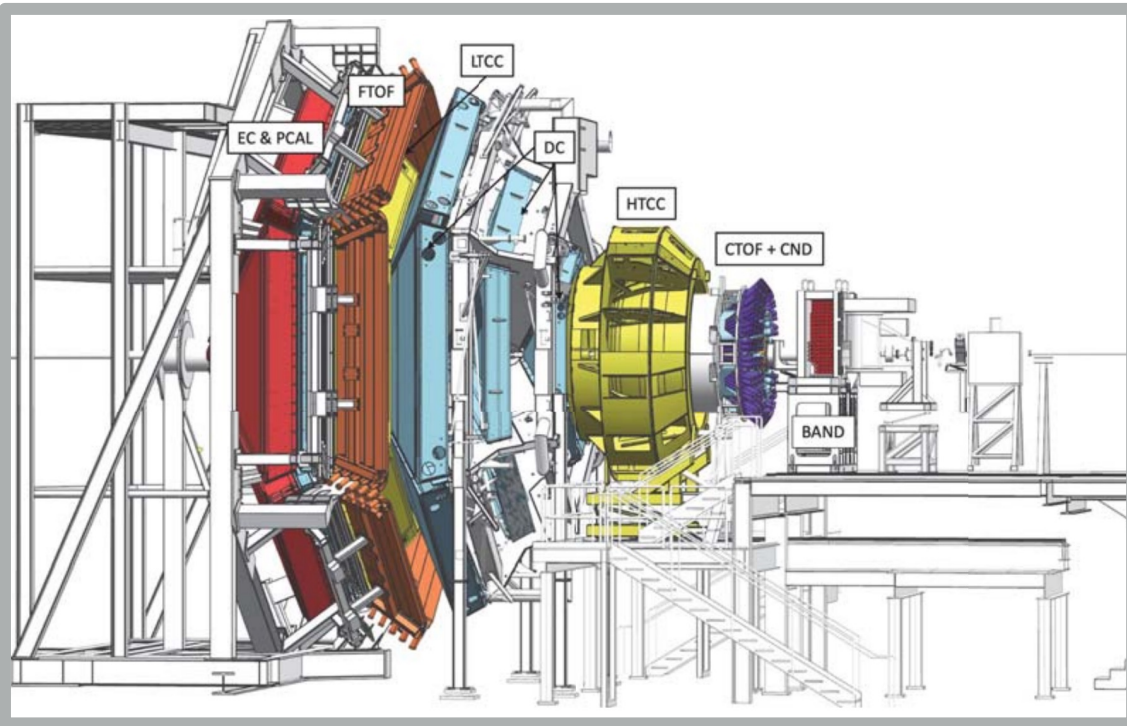
## Acknowledgments and Thanks

- Contributions made by other members of the CLAS Collaboration and researchers at Argonne National Lab
- This work is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under contract number DE-AC02-06CH11357

# Backup Slides



# Data Collection



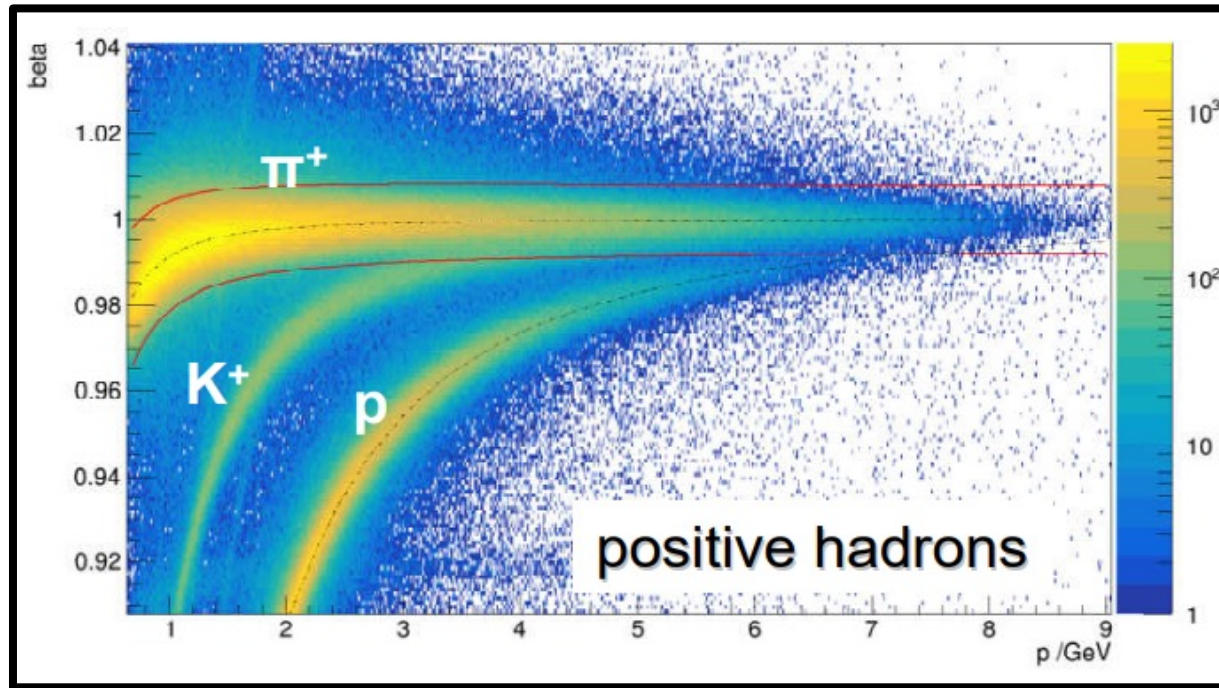
CLAS12 Detector

- CLAS12 detector in Hall B at Jefferson Lab
  - Upgrade from the CLAS detector
  - Enabled the higher energy and statistics for our experiments, not previously accessible
- Data from the Fall 2018 RG-A experiment
  - Used a 10.6 GeV polarized electron beam and unpolarized liquid hydrogen target
- Data presented uses forward tracking only

# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum



\*Image provided by Stefan Diehl

$\pi^+$  Pion PID –  $\beta$  vs  $p$

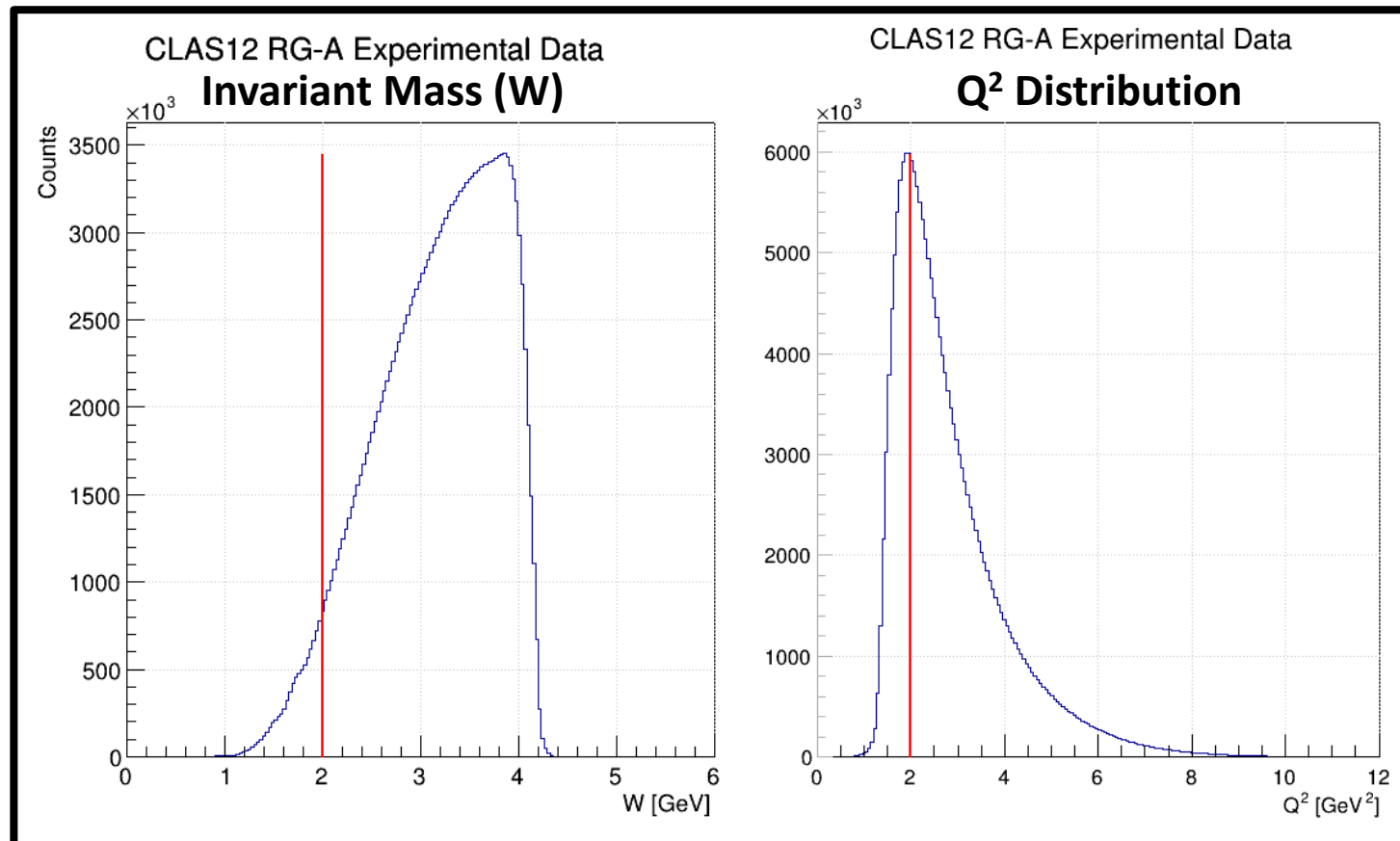
# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum

## Analysis Cuts:

- **SIDIS Cuts:**
  - $W > 2 \text{ GeV}$
  - $Q^2 > 2 \text{ GeV}^2$



# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum

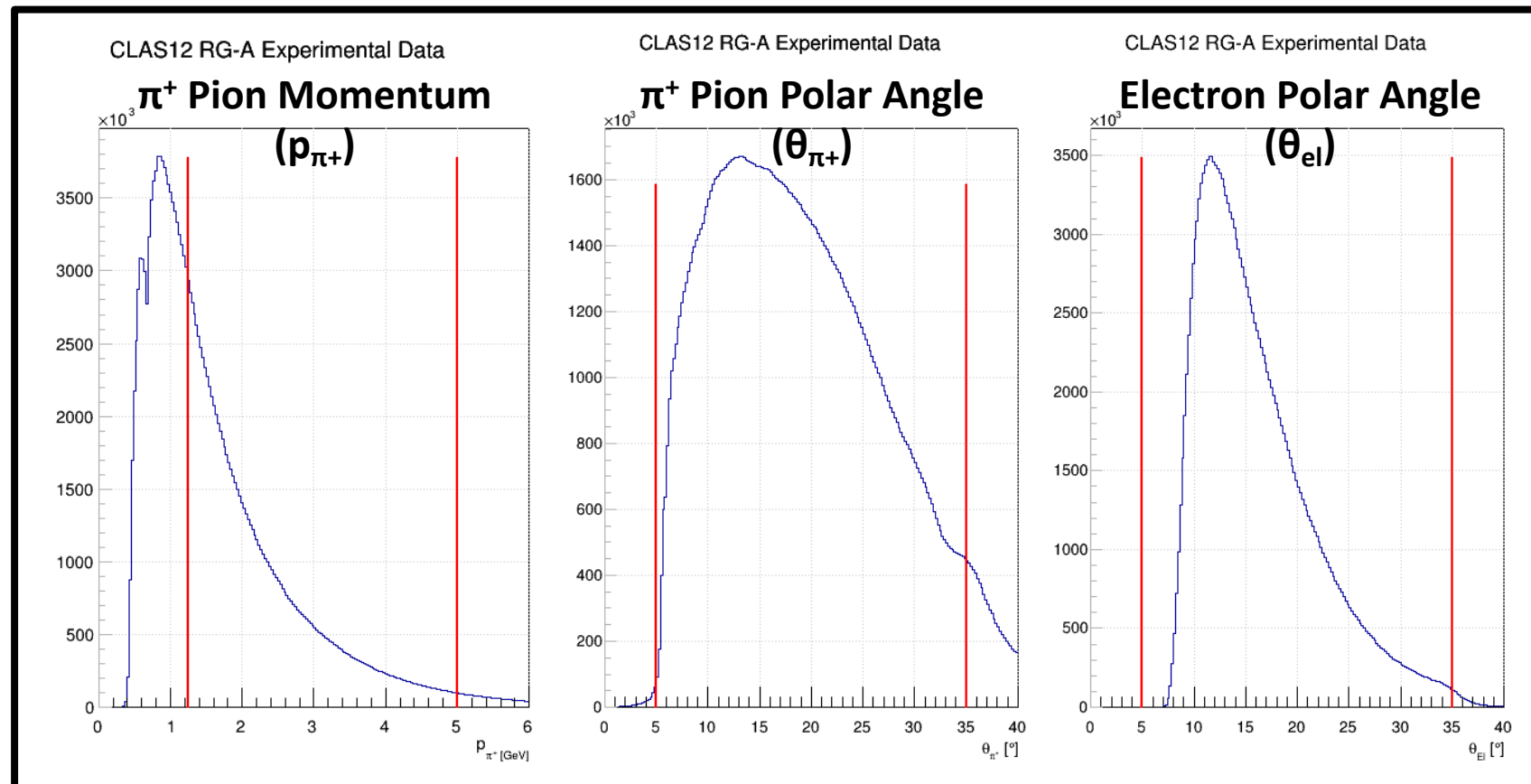
## Analysis Cuts:

- **SIDIS Cuts:**

- $W > 2 \text{ GeV}$
- $Q^2 > 2 \text{ GeV}^2$

- **Other Analysis Cuts:**

- $p_{\pi^+}$  Cut:  $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- $\theta$ -angle Cut:  $5^\circ < \theta_{\text{particle}} < 35^\circ$



# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum

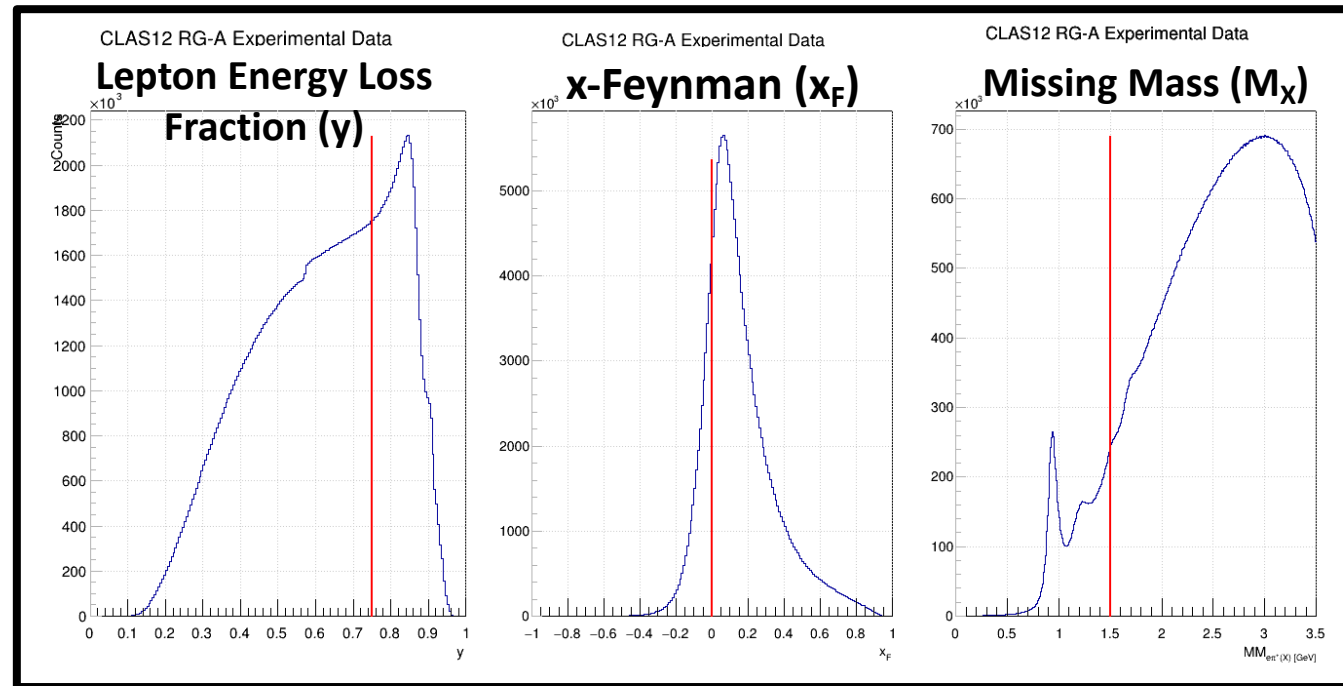
## Analysis Cuts:

- **SIDIS Cuts:**

- $W > 2 \text{ GeV}$
- $Q^2 > 2 \text{ GeV}^2$

- **Other Analysis Cuts:**

- $p_{\pi^+}$  Cut:  $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- $\theta$ -angle Cut:  $5^\circ < \theta_{\text{particle}} < 35^\circ$
- $y < 0.75$  (minimize other background processes)
- $x_F > 0$  (minimize contributions from target fragmentations)
- Missing Mass Cut:  $M_X > 1.5 \text{ GeV}$  (limits contributions from exclusive events)



# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum

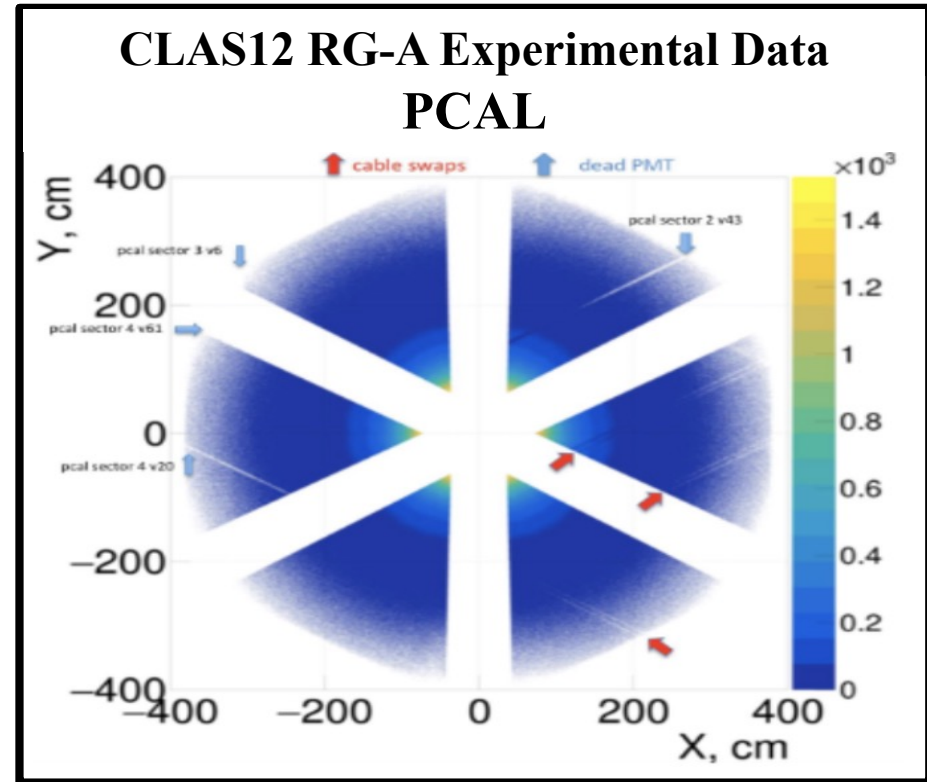
## Analysis Cuts:

- **SIDIS Cuts:**

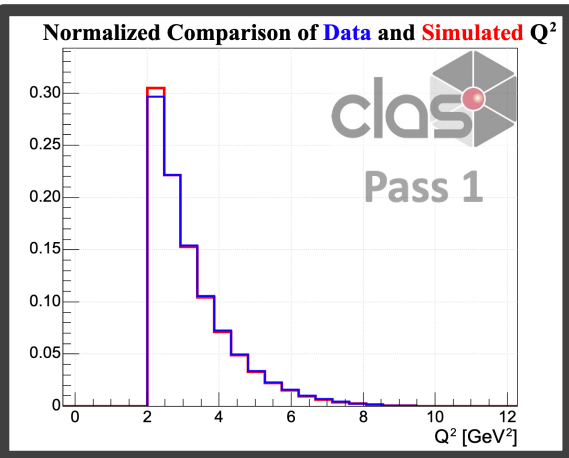
- $W > 2 \text{ GeV}$
- $Q^2 > 2 \text{ GeV}^2$

- **Other Analysis Cuts:**

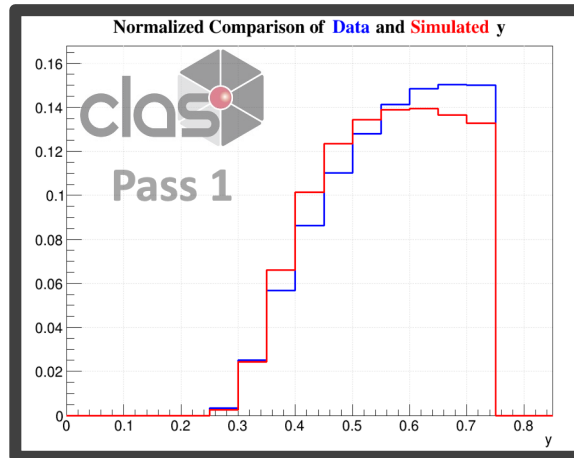
- $p_{\pi^+}$  Cut:  $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- $\theta$ -angle Cut:  $5^\circ < \theta_{\text{particle}} < 35^\circ$
- $y < 0.75$  (minimize other background processes)
- $x_F > 0$  (minimize contributions from target fragmentations)
- Missing Mass Cut:  $M_x > 1.5 \text{ GeV}$  (limits contributions from exclusive events)
- Fiducial Cuts (e.g., accounts for bad channels present in data)



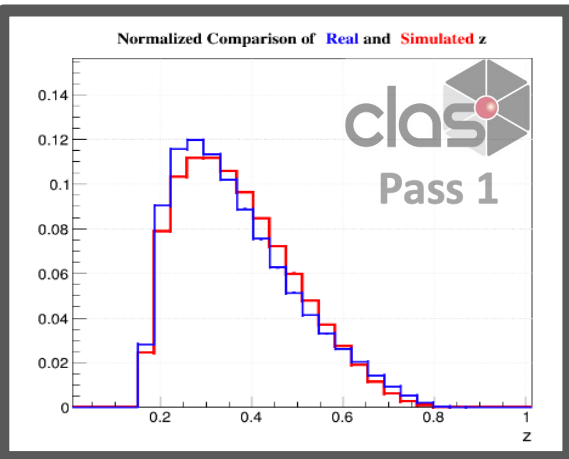
# Data and Monte Carlo Comparison



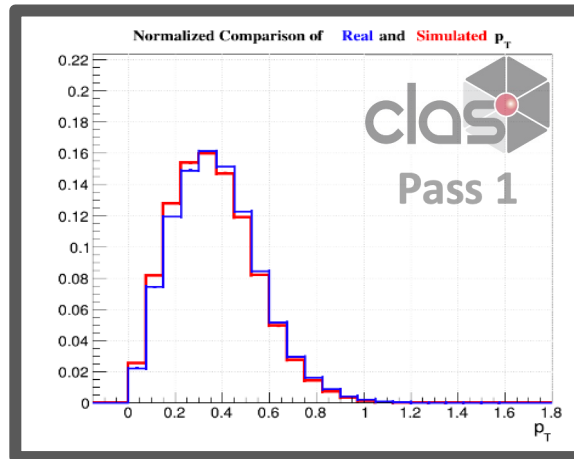
Q<sup>2</sup> Comparison



y Comparison

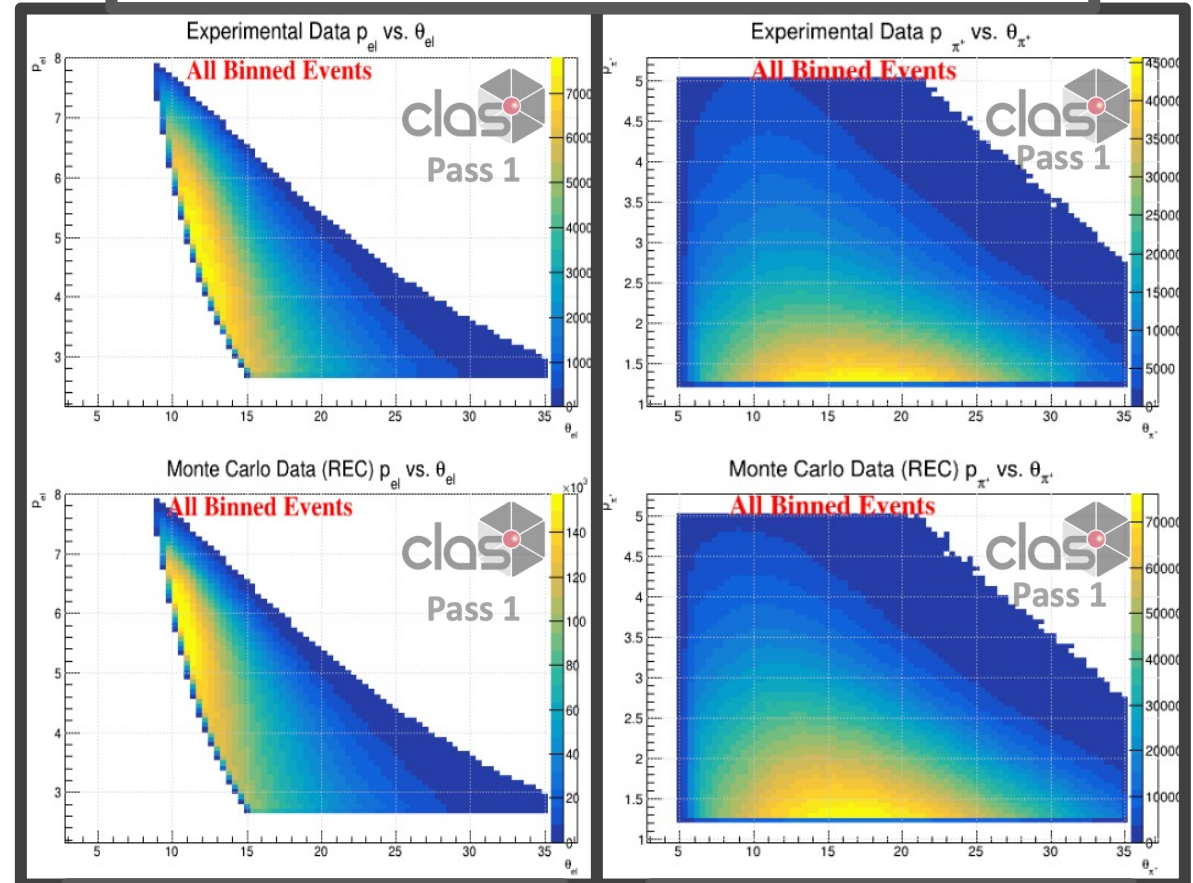


z Comparison



P<sub>T</sub> Comparison

## Momentum vs Polar Lab Angle Comparison



Electron Comparison

$\pi^+$  Pion Comparison

# Event Selection (Full PID)

The RG-A Analysis Overview and Procedures note goes into detail about the common particle identification scheme used for RG-A

(See: [https://clas12-docdb.jlab.org/DocDB/0009/000949/001/RGA\\_Analysis\\_Overview\\_and\\_Procedures-08172020.pdf](https://clas12-docdb.jlab.org/DocDB/0009/000949/001/RGA_Analysis_Overview_and_Procedures-08172020.pdf))

## Electron PID Criteria:

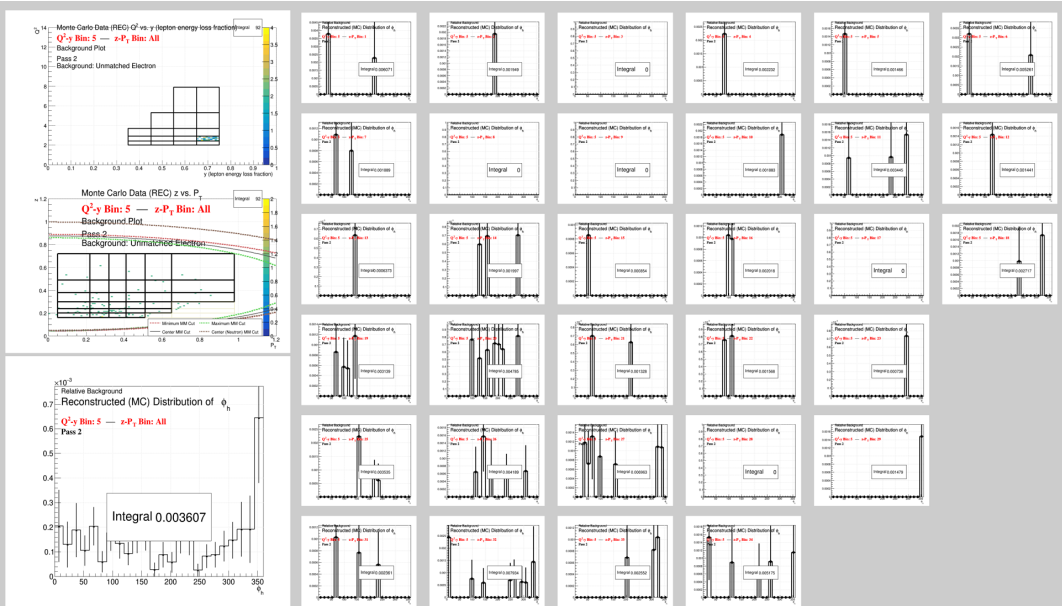
- Detected in Forward Detector
- > 2 photoelectrons detected in the HTCC
- > 0.07 GeV energy deposited in the PCAL
- Sector dependent sampling fraction cut
- “Diagonal cut” for electrons above 4.5 GeV (HTCC threshold)
- $y < 0.75$ , not strictly an “electron cut”, but sets the min electron energy approximately  $> 2.4$  GeV

## Pion PID Criteria:

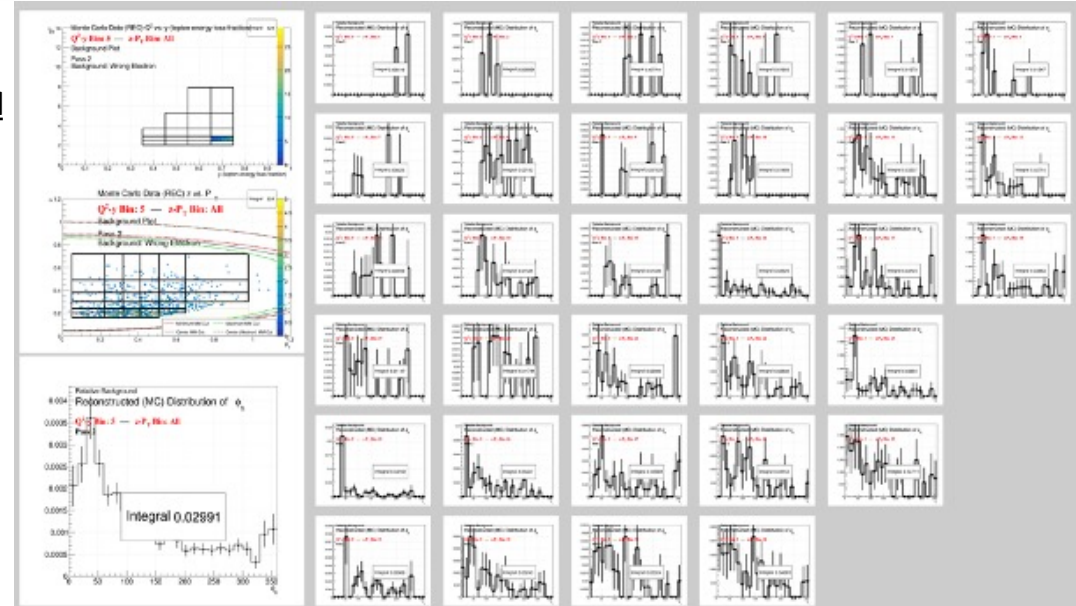
- Detected in Forward Detector
- $p > 1.25$  GeV
- Refined chi2pid cuts



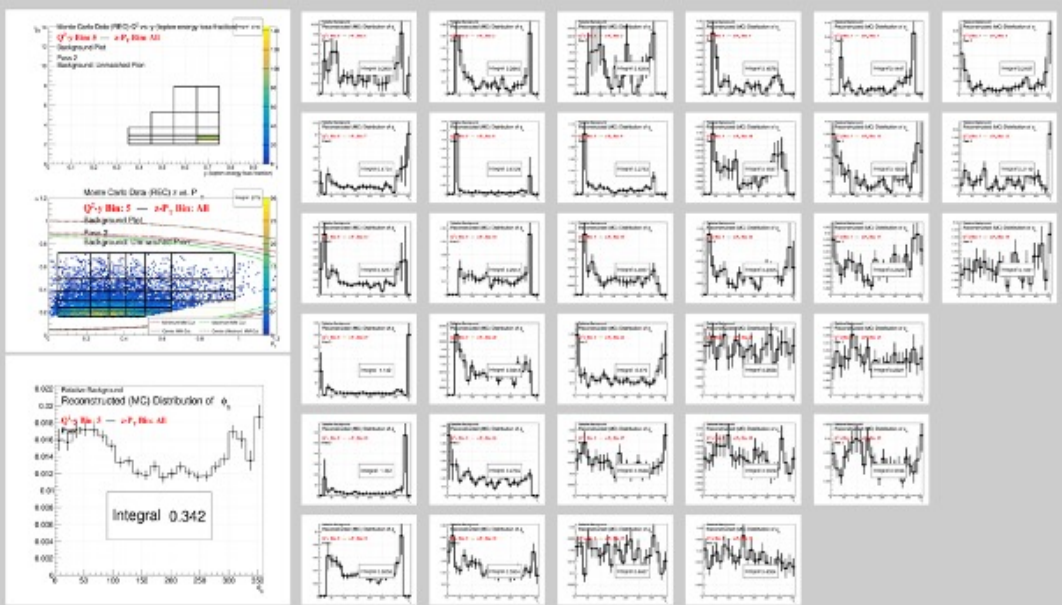
# Background ( $\beta$ ) Vector – Particle Mis-Identification (as functions of $\phi_h$ )



**Unmatched  
MC REC  
Electron**  
←

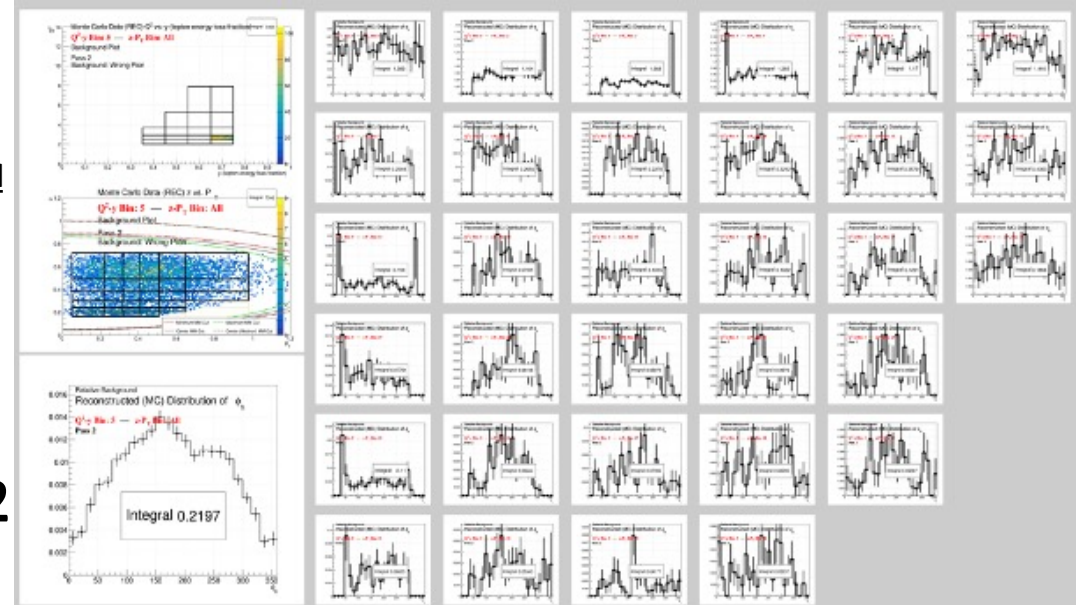


**Incorrect  
PID for  
MC REC  
Electron**  
←



**Unmatched  
MC REC  
 $\pi^+$  Pion**  
←

**PASS 2**

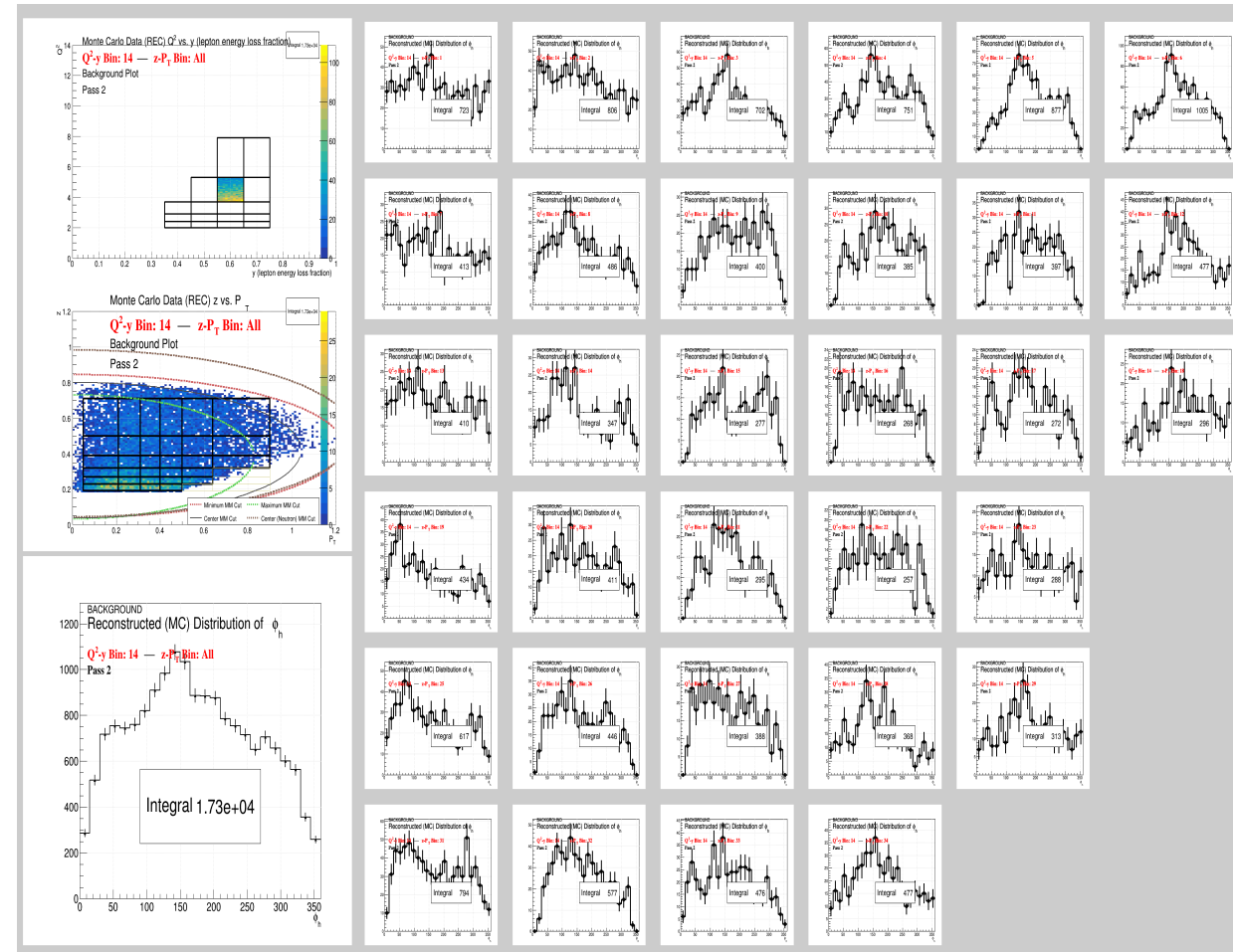
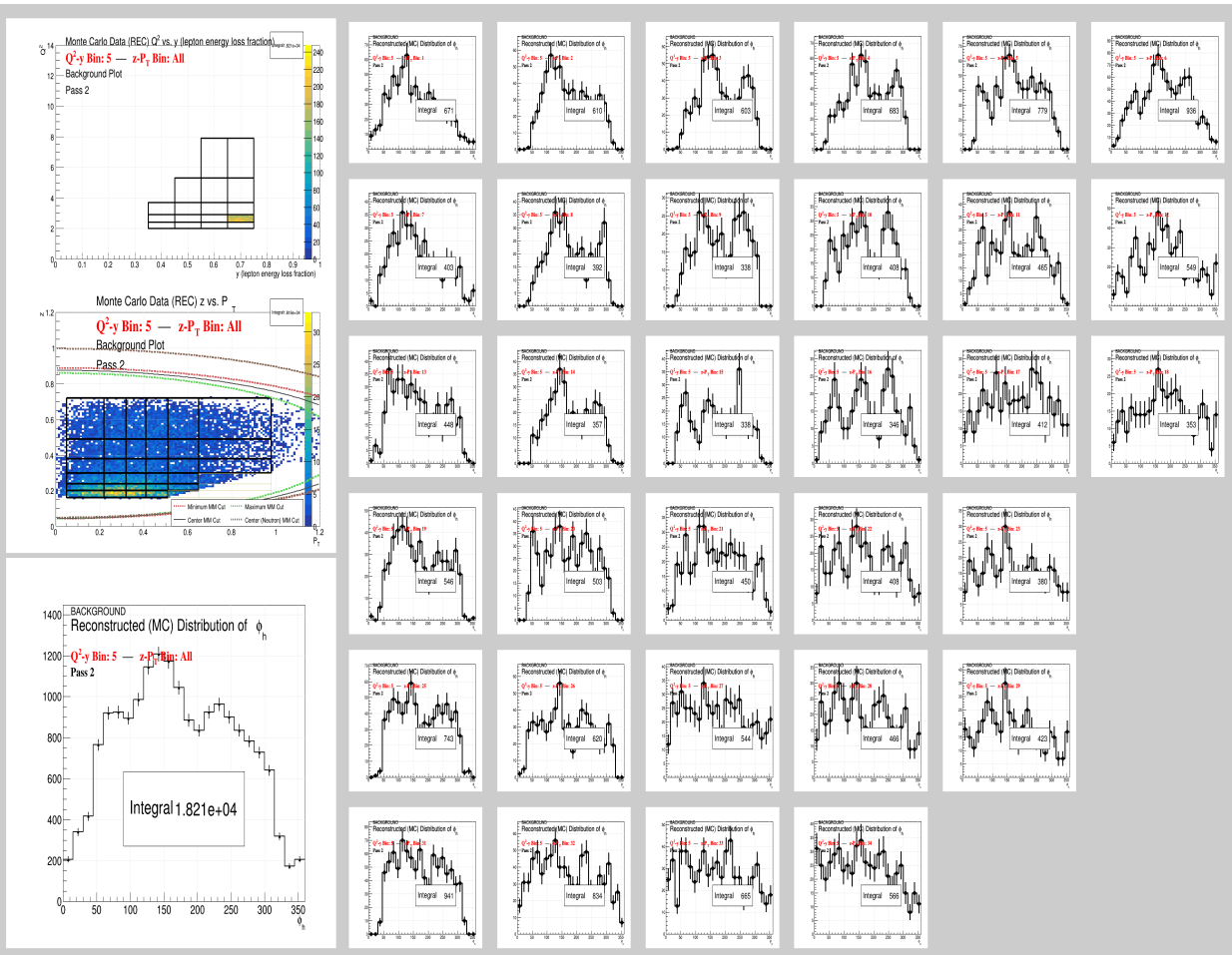


**Incorrect  
PID for  
MC REC  
 $\pi^+$  Pion**  
←

# $\beta$ Vector – All Contributions (Per $Q^2$ -y Bin)

**$Q^2$ -y Bin 5:** Events from Generated Missing Mass Cuts make up about 0.87% of the ‘Background’ shown below

**$Q^2$ -y Bin 14:** Events from Generated Missing Mass Cuts make up about 18.8% of the ‘Background’ shown below

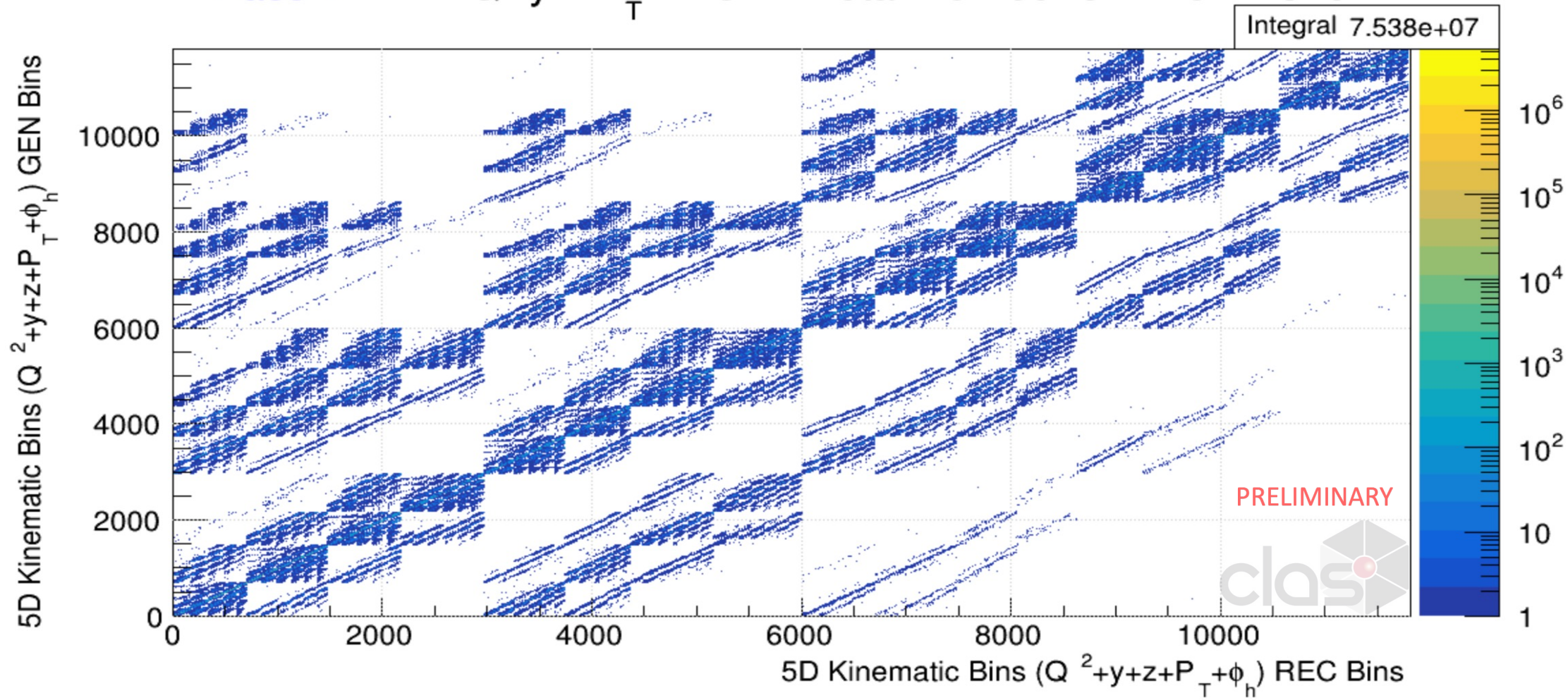


# Example of (5D) Unfolding Procedure

Using the Flattened  $Q^2$ - $y$ - $z$ - $P_T$ - $\phi_h$  Multidimensional Bins

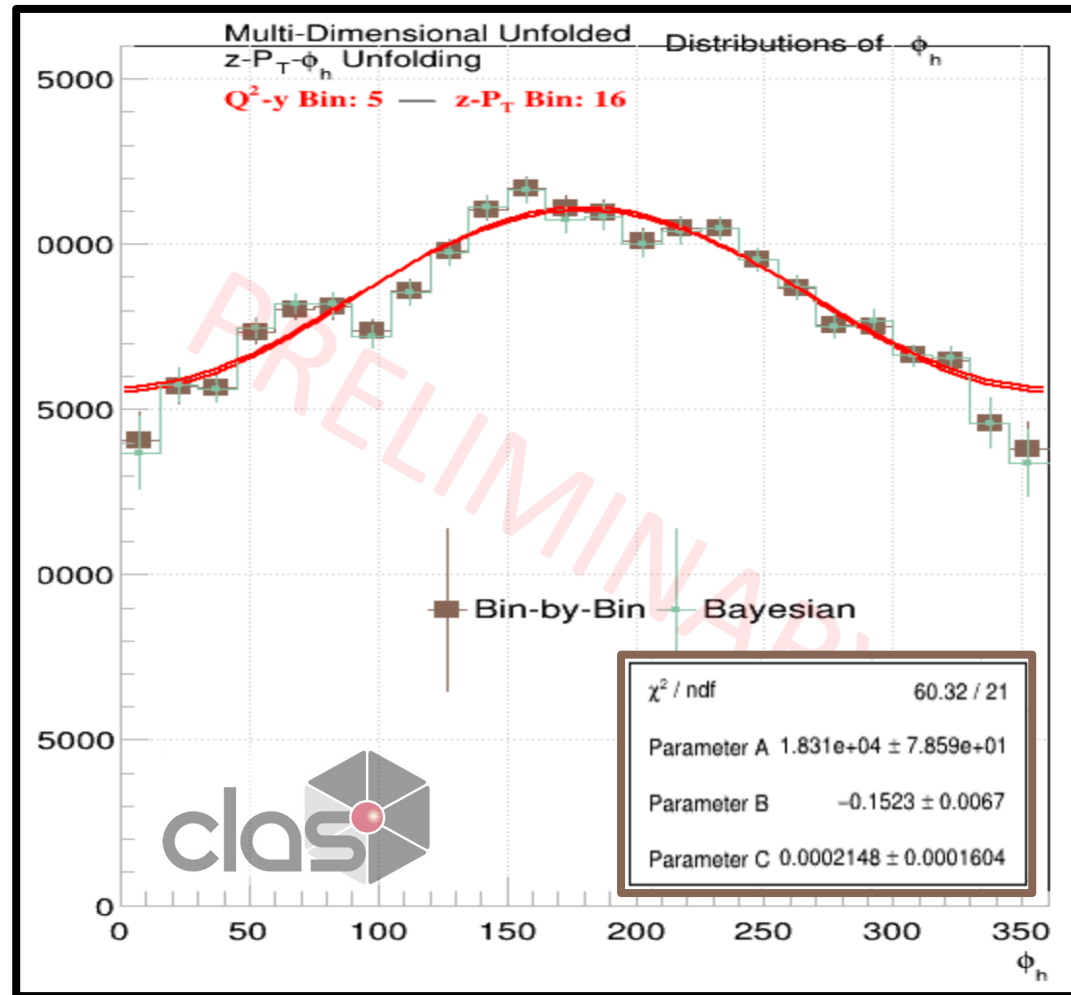
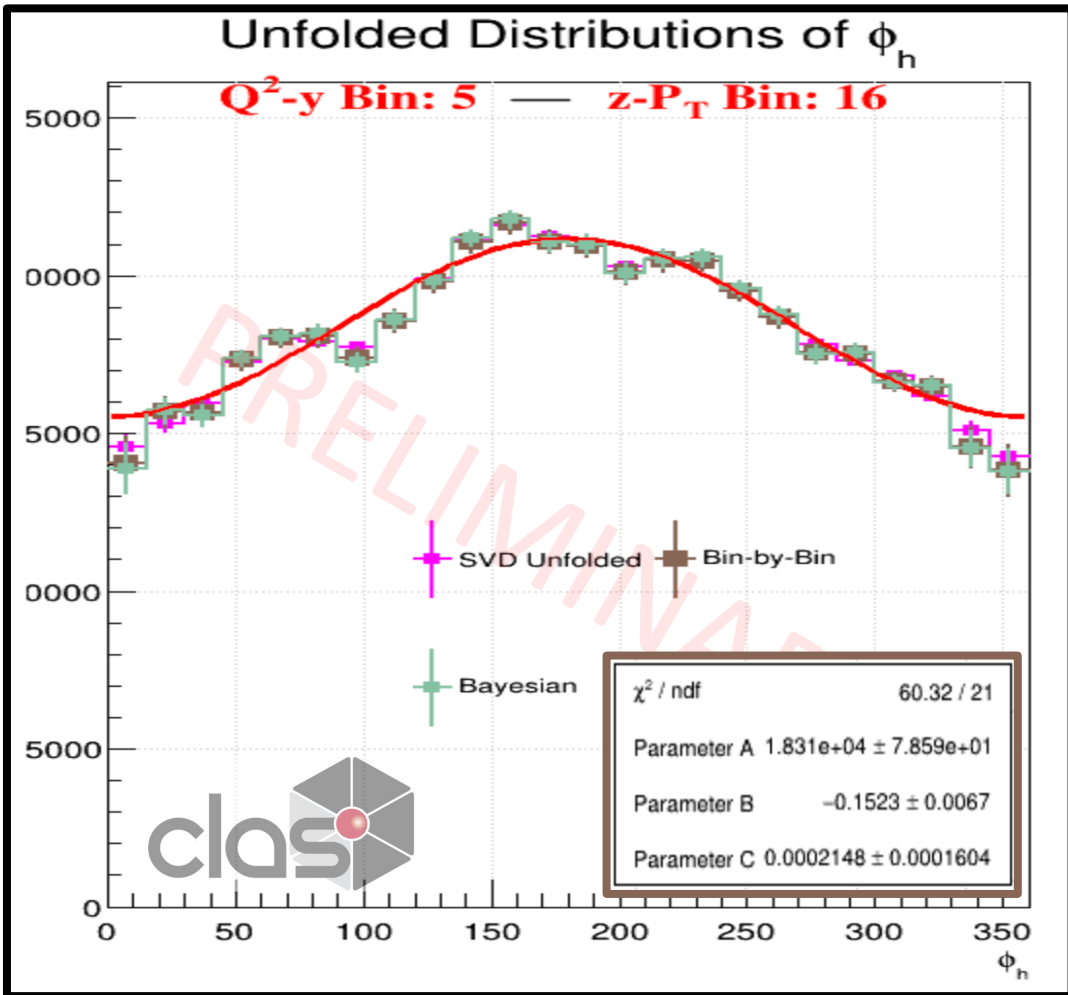
Response Matrix of 5D Kinematic Bins ( $Q^2$ - $y$ - $z$ - $P_T$ - $\phi_h$ )

Pass 1 — All  $Q^2$ - $y$ - $z$ - $P_T$  Bins — Total Number of Bins: 11816



# Comparisons of 1D and 3D Unfolding Procedure

Using the Multidimensional Kinematic Bin from the prior example for this comparison

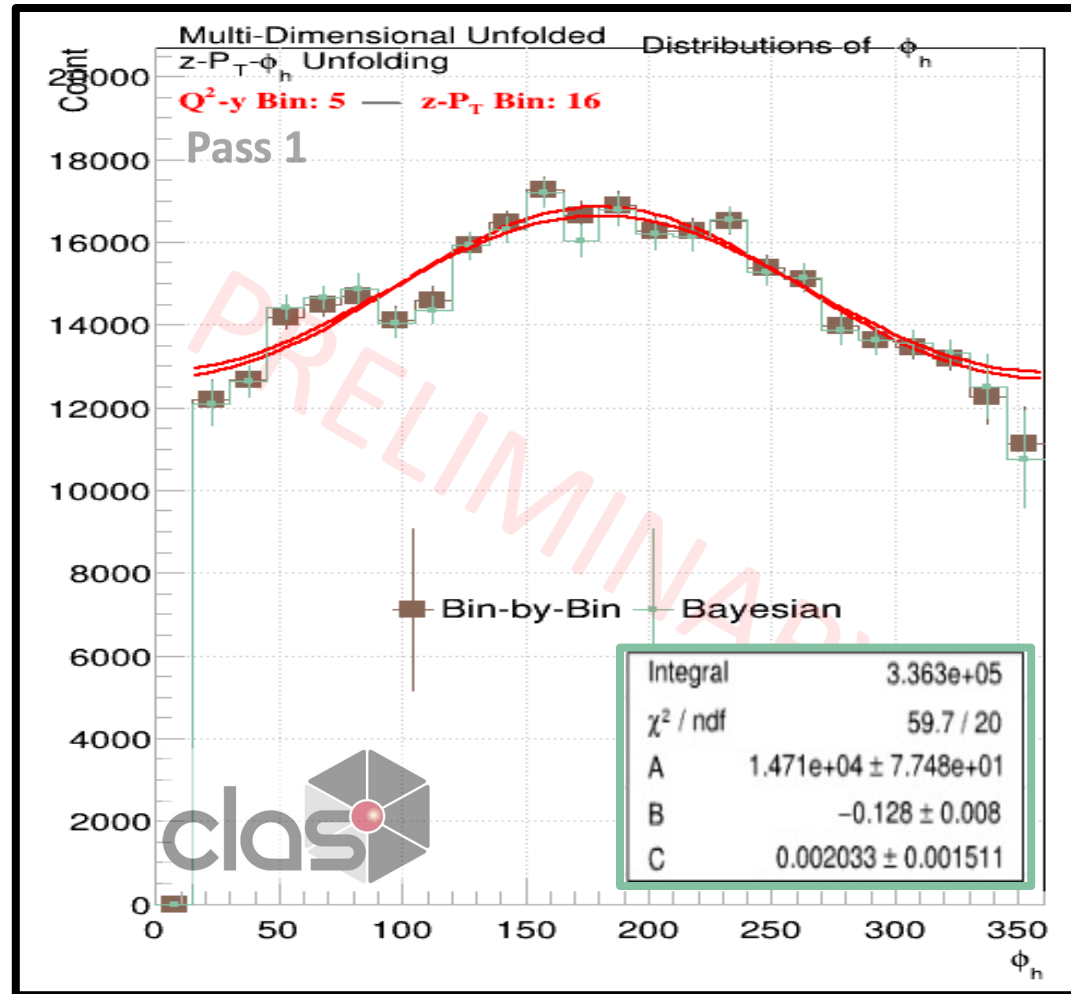
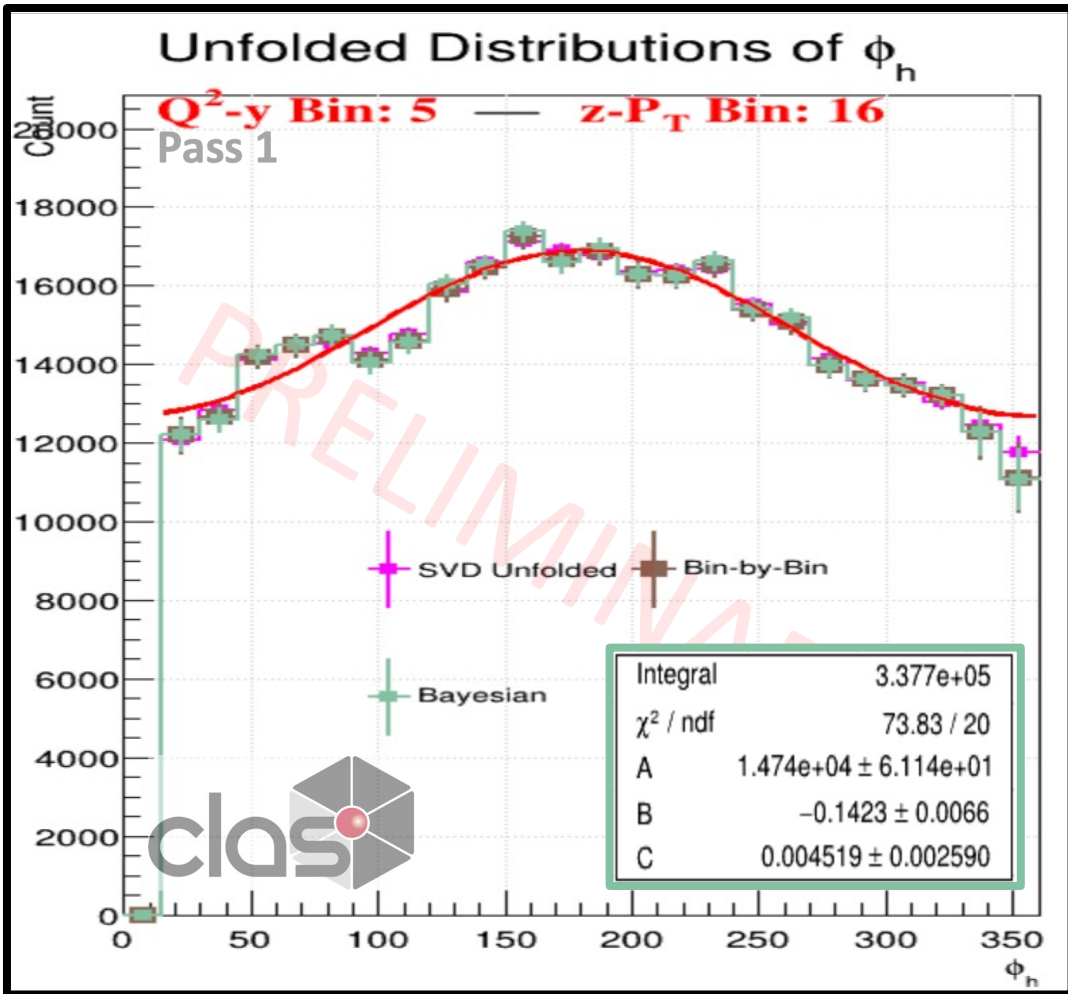


Bin-by-bin  
Acceptance  
Correction  
gives the exact  
same results

SVD Unfolding has not been able to work so far with the Multidimensional Unfolding procedures

# Comparisons of 1D and 3D Unfolding Procedure

Using the Multidimensional Kinematic Bin from the prior example for this comparison



Bin-by-bin  
 Acceptance  
 Correction  
 gives the exact  
 same results

Bayesian  
 Unfolding  
 gives similar  
 results

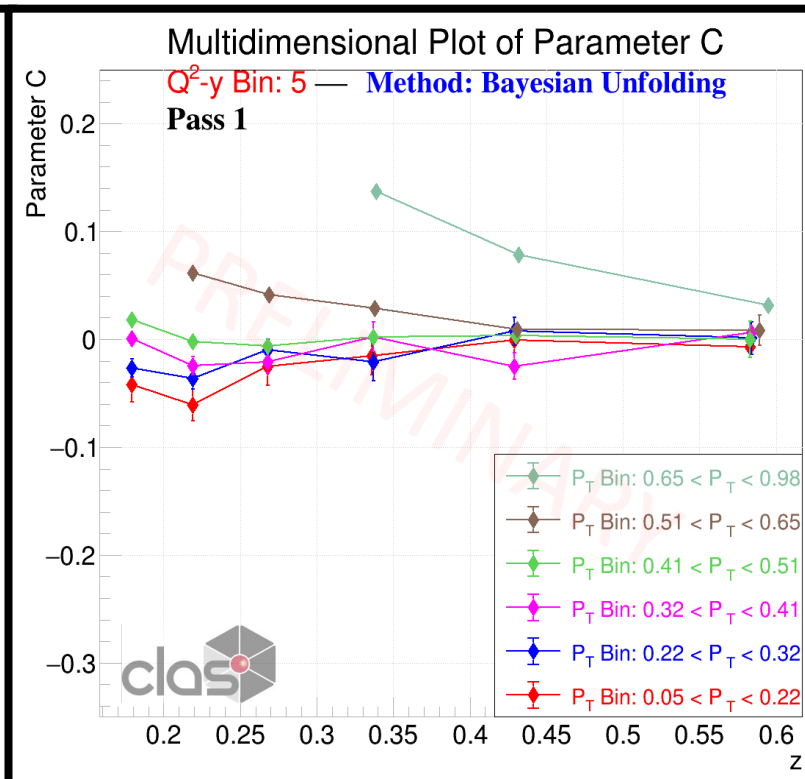
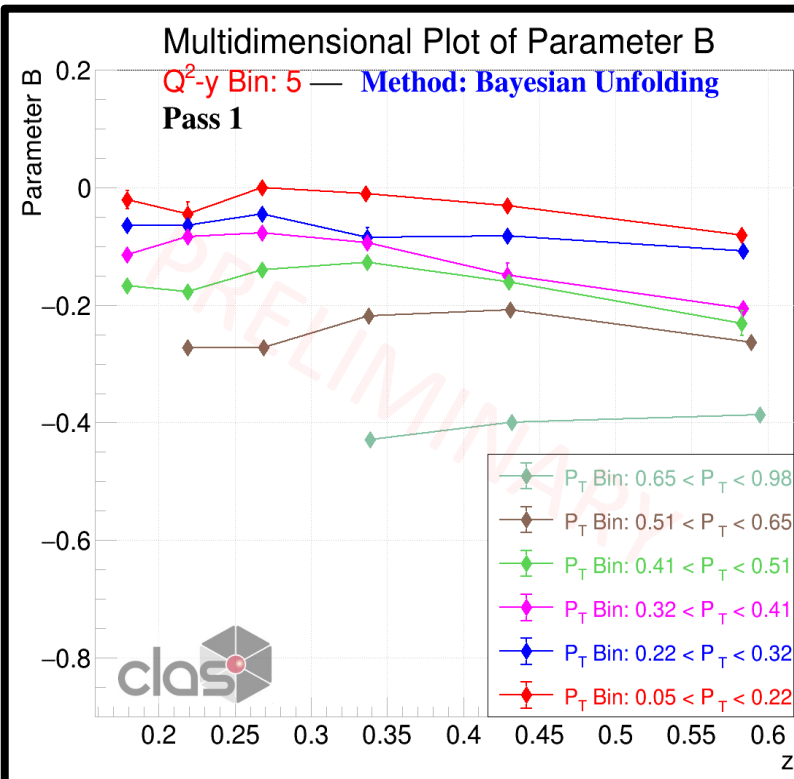
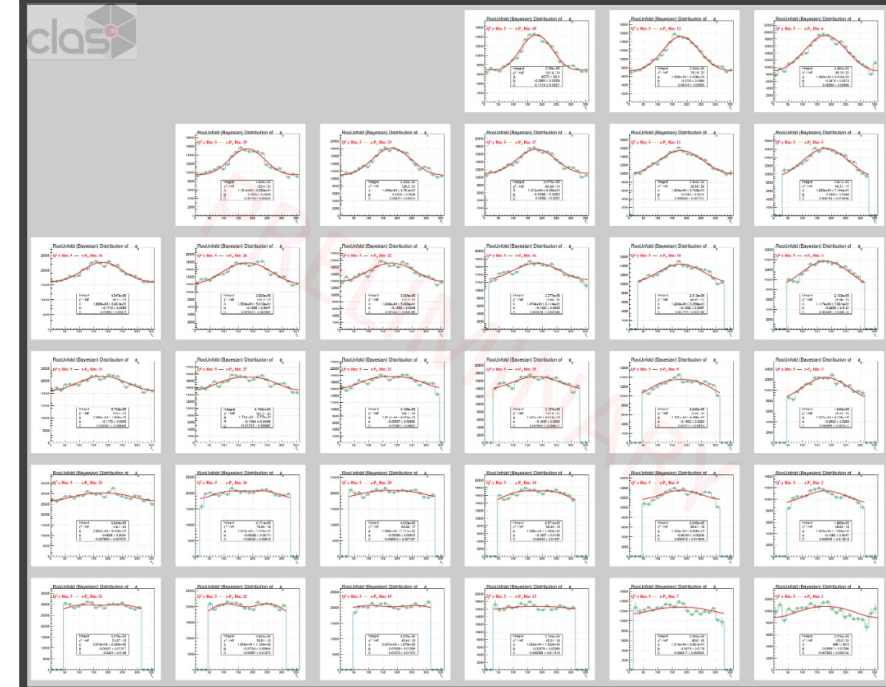
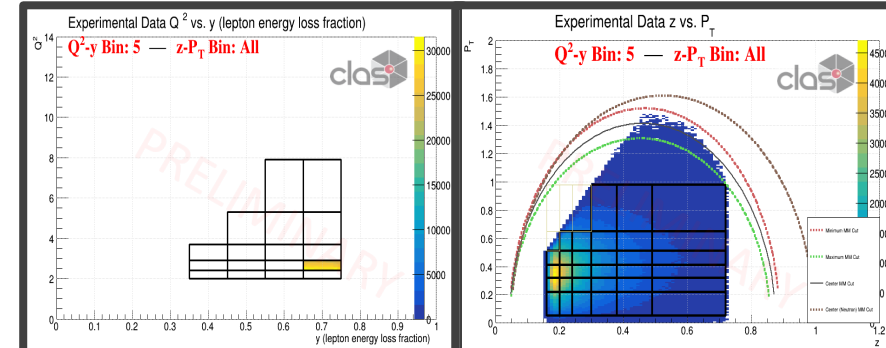
# Cosine Moments as Functions of z – Pass 1

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

$Q^2$ -y Bin 5



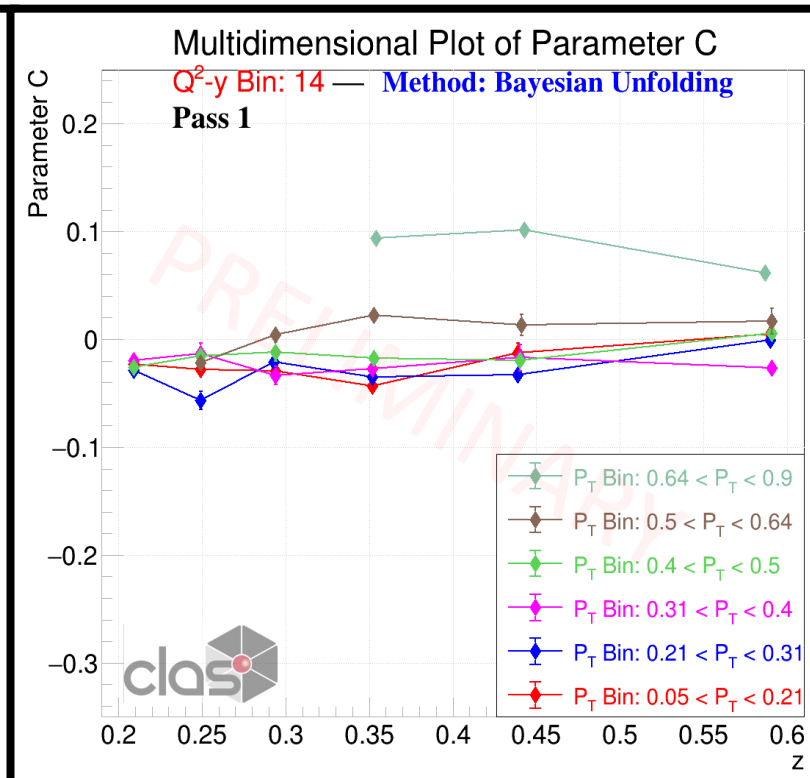
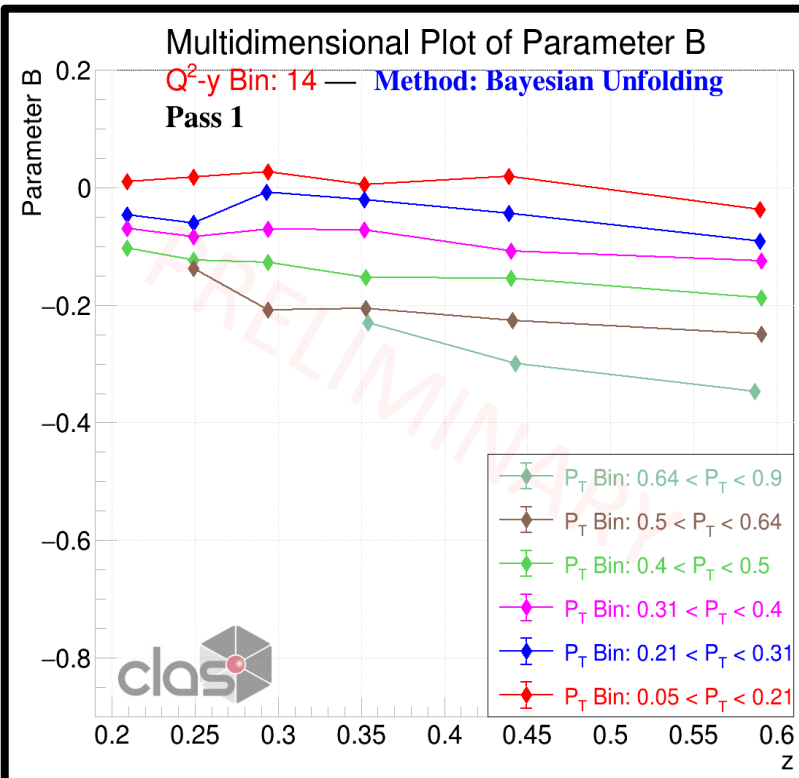
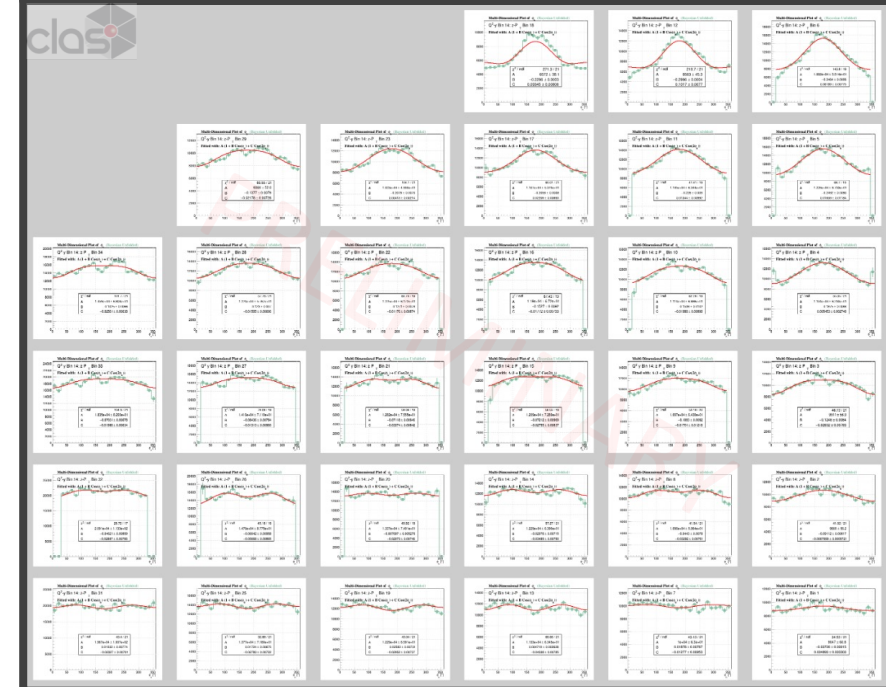
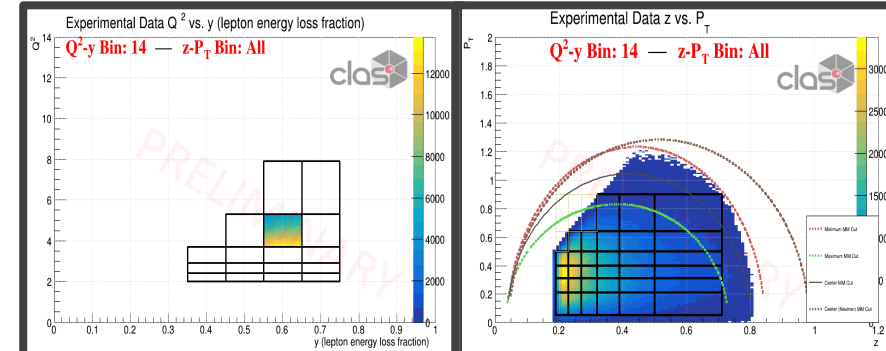
# Cosine Moments as Functions of z – Pass 1

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

Q<sup>2</sup>-y Bin 14



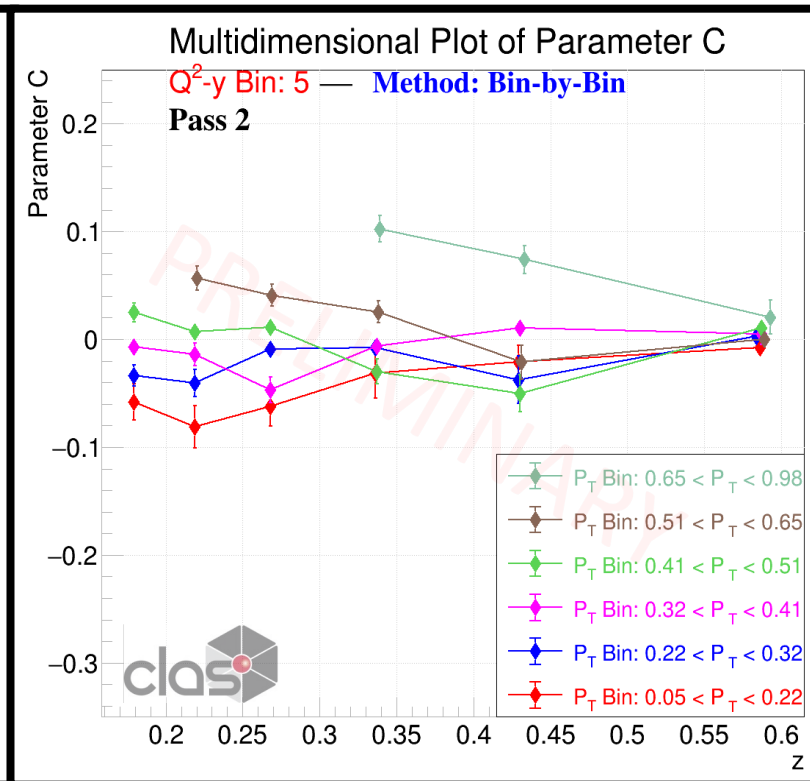
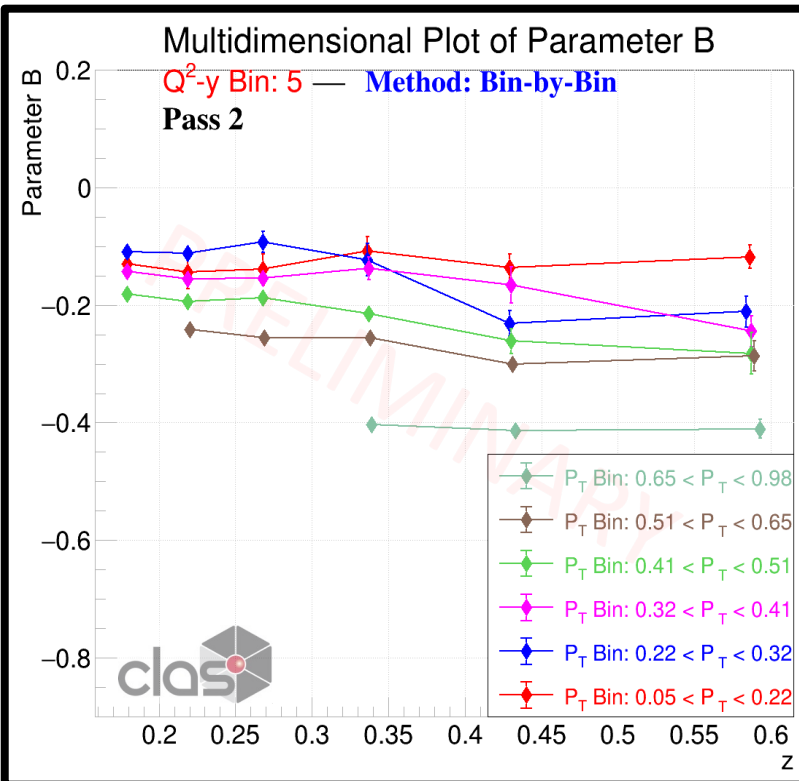
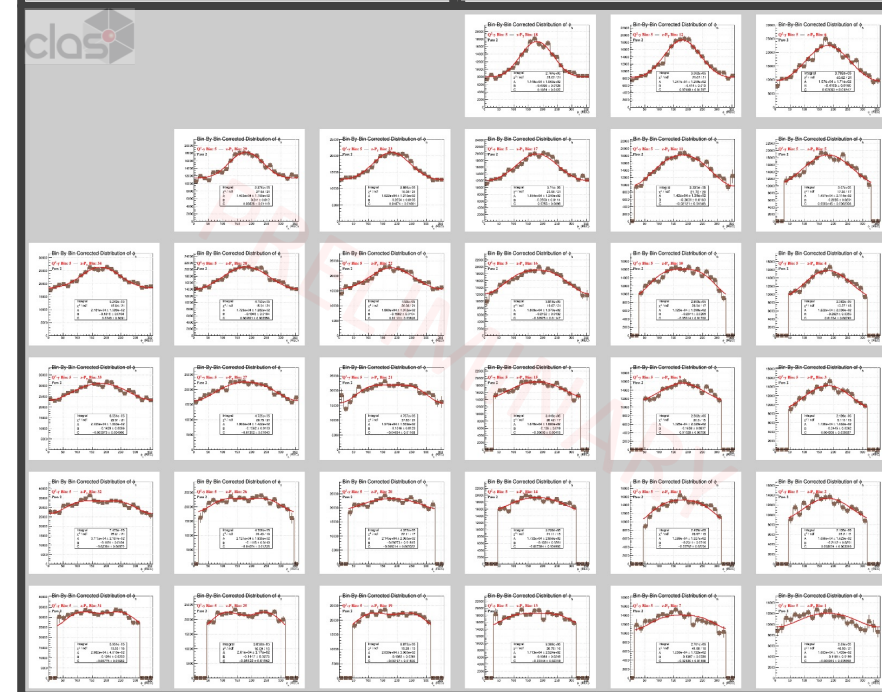
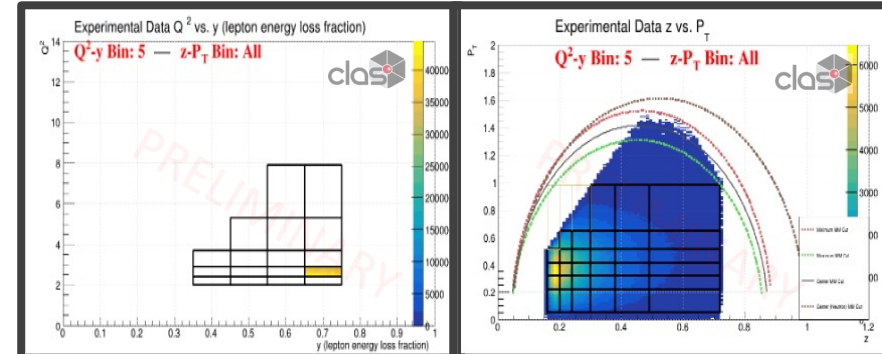
# Cosine Moments as Functions of z - with Pass 2

$$B = A_{UU}^{\cos \varphi_h} \quad C = A_{UU}^{\cos 2\varphi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Corrected with Bin-by-bin Method

$Q^2$ -y Bin 5





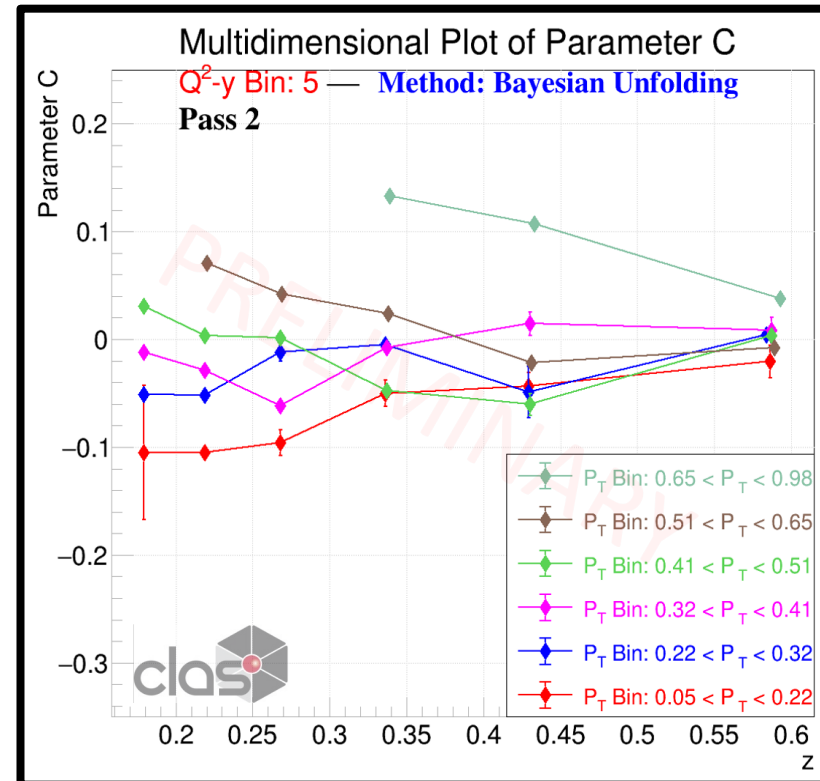
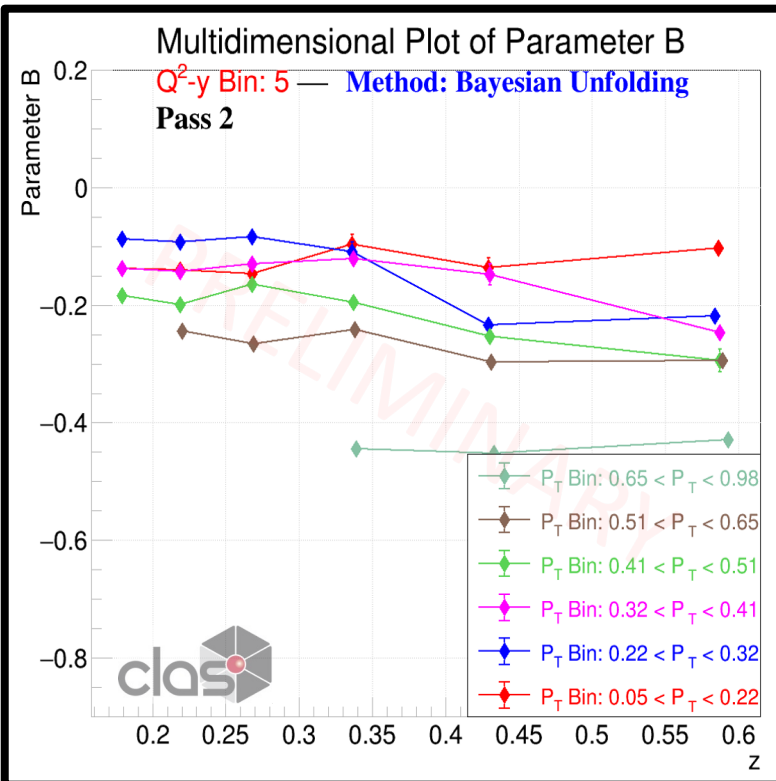
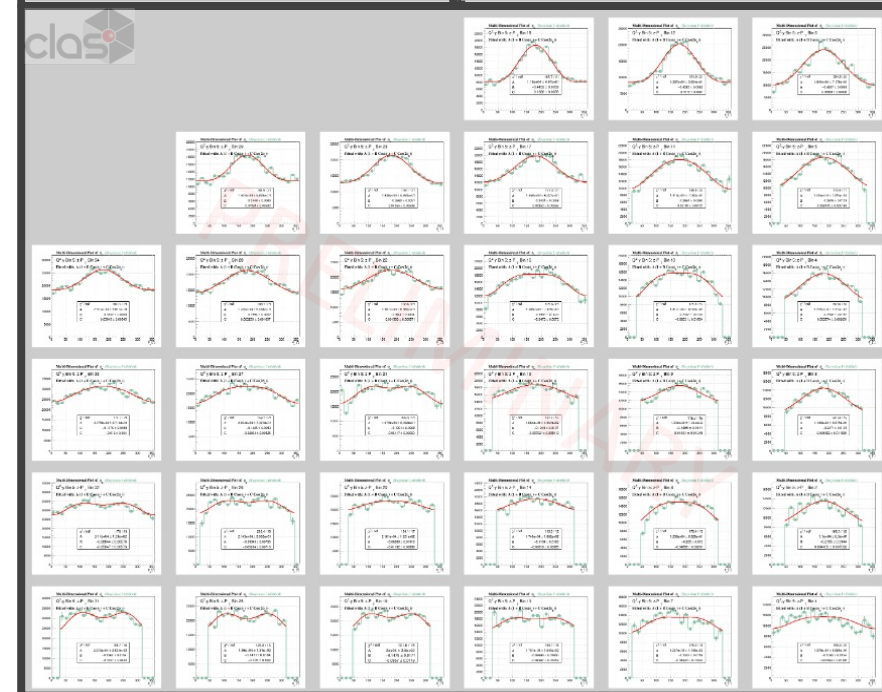
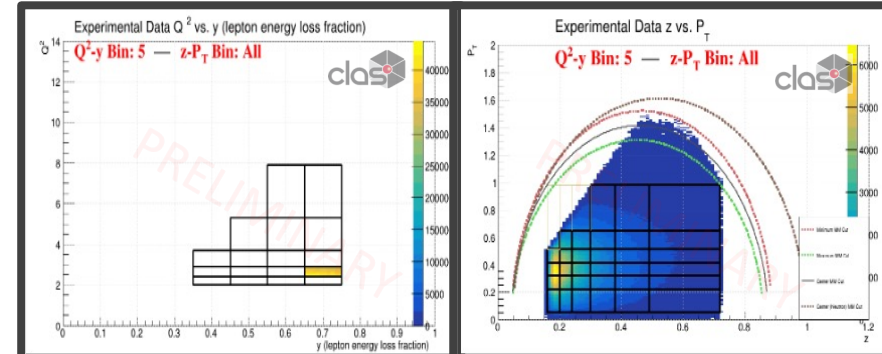
# Cosine Moments as Functions of z - with Pass 2

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

$Q^2$ -y Bin 5

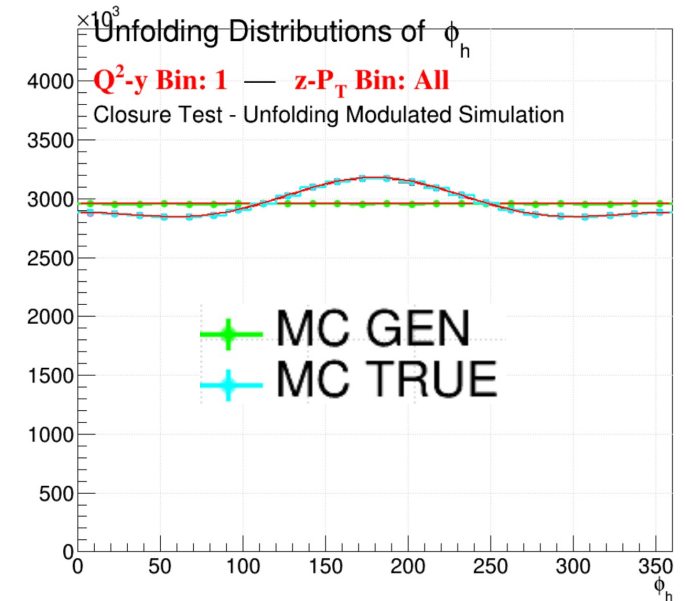


# Modulated Unfolding Closure Tests

- Modulated the MC distributions using the formula:

$$Weight = 1 + B \cos(\phi_h) + C \cos(2\phi_h)$$

- Gives the weight for each MC event based on generated  $\phi_h$
- Parameter values currently being used in this image:
  - $B = -0.05$  (Same for every  $z-P_T$  bin)
  - $C = 0.025$
- Modulated MC REC is then unfolded using the un-modulated response matrix (in 1D and Multi-Dim examples) and compared with 'MC TRUE'
  - MC TRUE is the modulated MC GEN distribution
  - Also performed a closure test of unfolding the un-modulated MC REC distribution with the un-modulated response matrix to ensure the method was applied properly

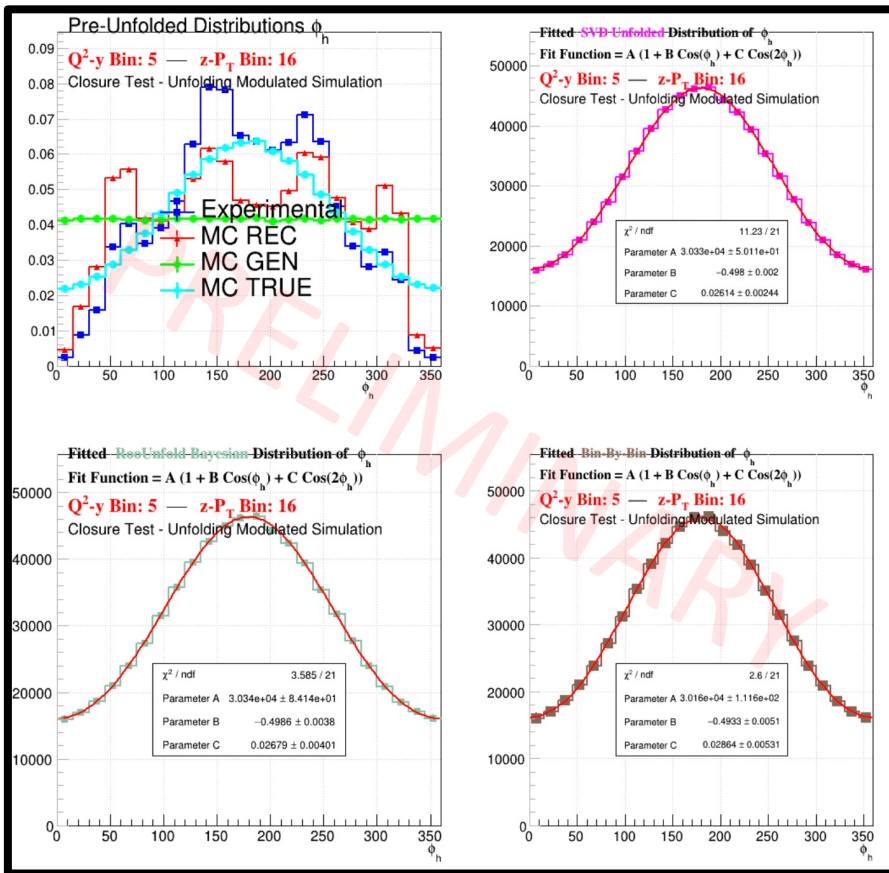


# Modulated Unfolding Closure Tests

The parameters used for weighing modulations below are:

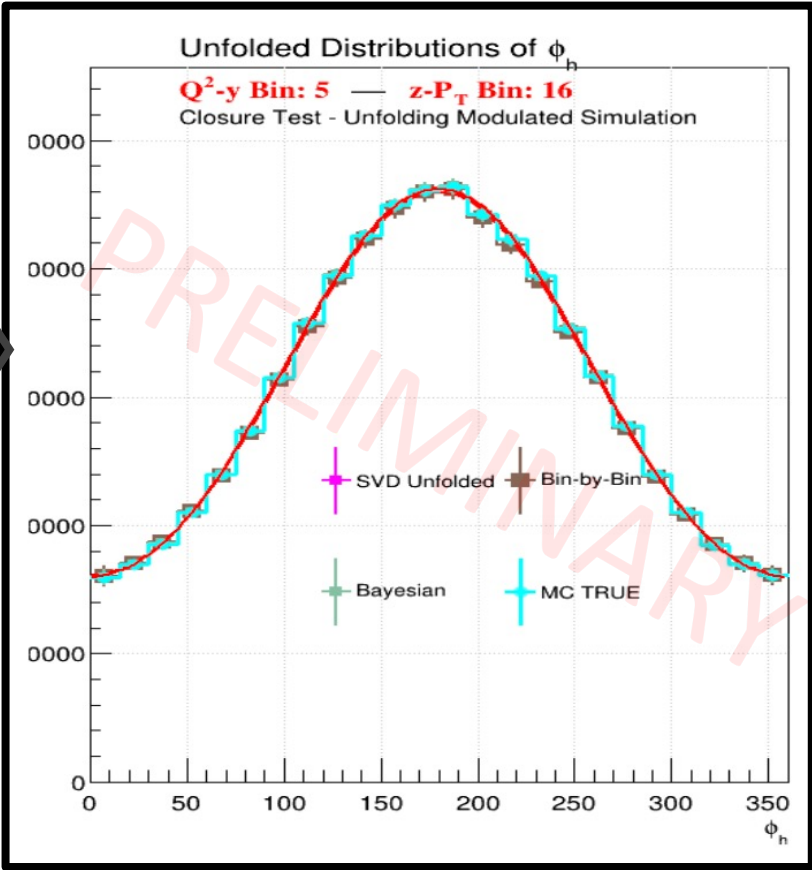
$$B = -0.5 \text{ and } C = 0.025$$

Results show that an **unmodulated** Simulation can correct distributions **with modulations**



Checking that the corrected distributions match MC TRUE

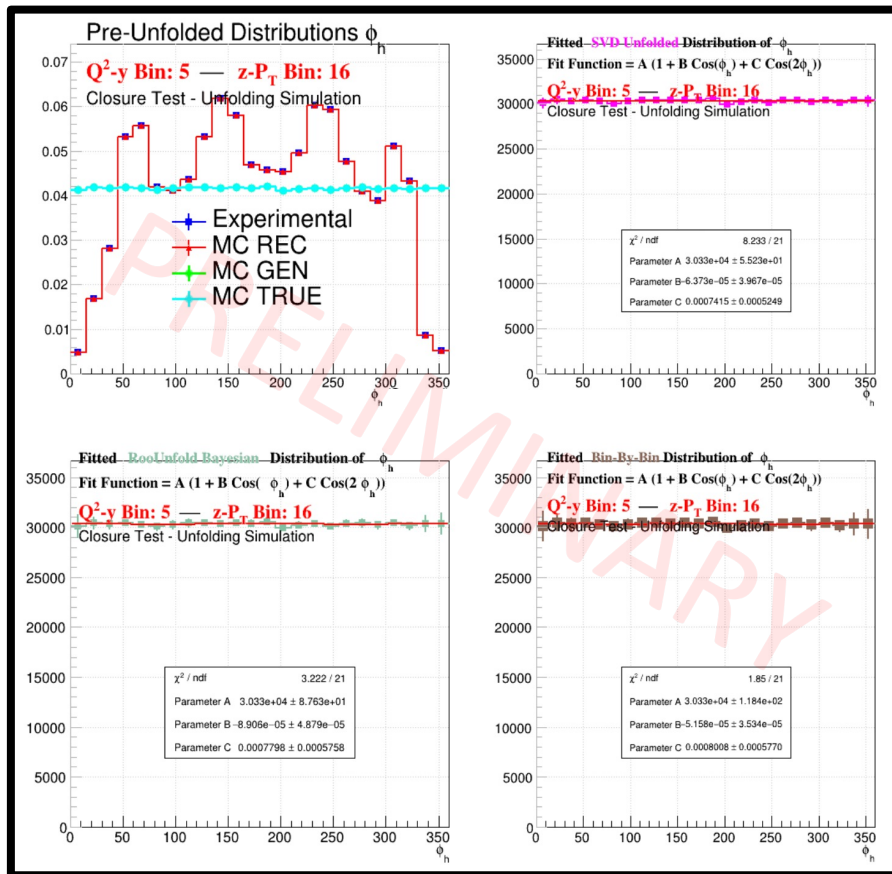
Fits are within the margin of error of the defined parameters



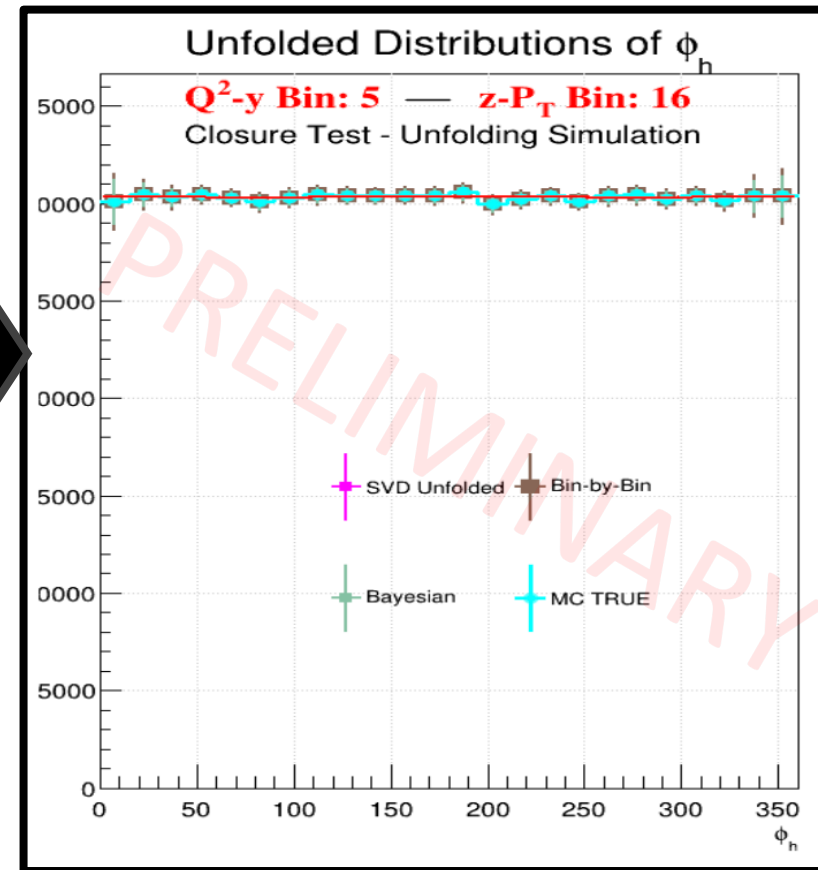
# Other Unfolding Closure Tests

Other closure tests being used to check that Unfolding is done properly:

- Replace the experimental data with the reconstructed Monte Carlo (no modulations)
  - Should return the generated (i.e., MC TRUE) distribution



Checking that the corrected distributions match MC TRUE

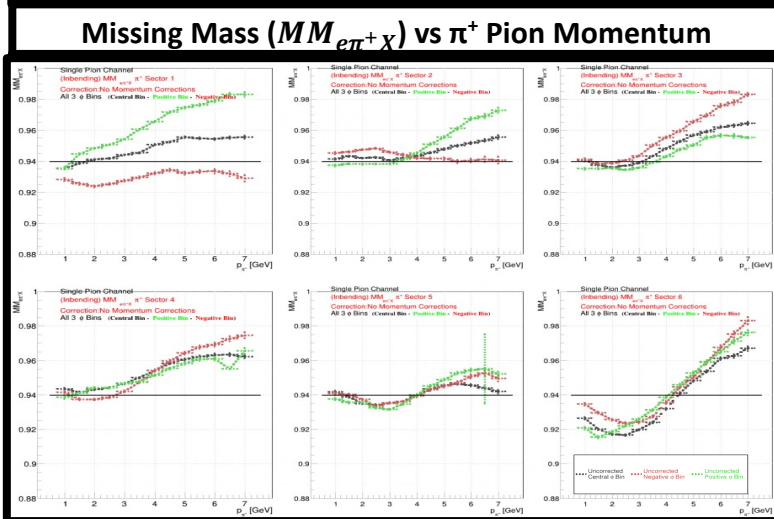
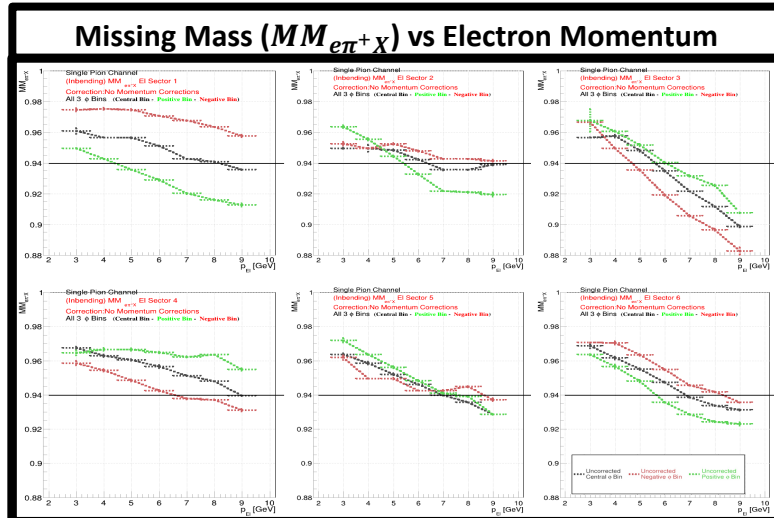


# Momentum Corrections from Exclusive Events

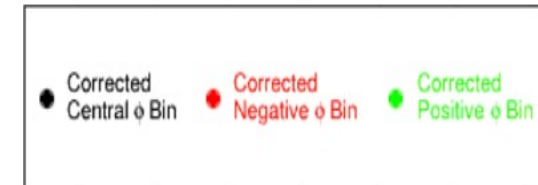
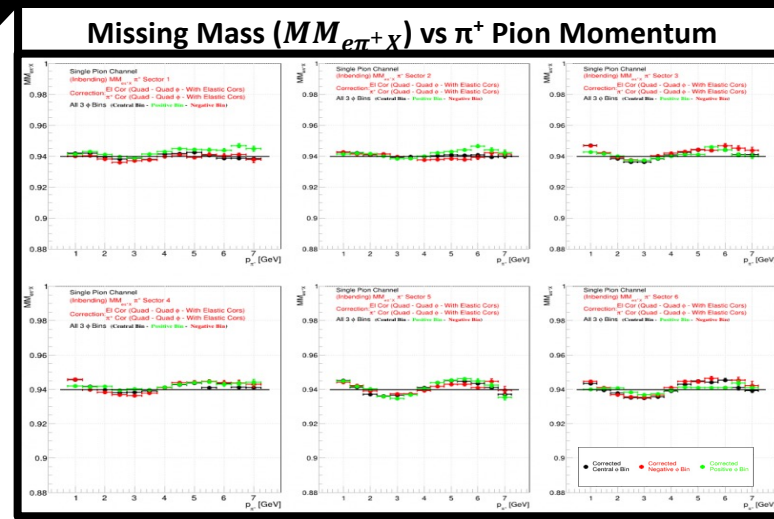
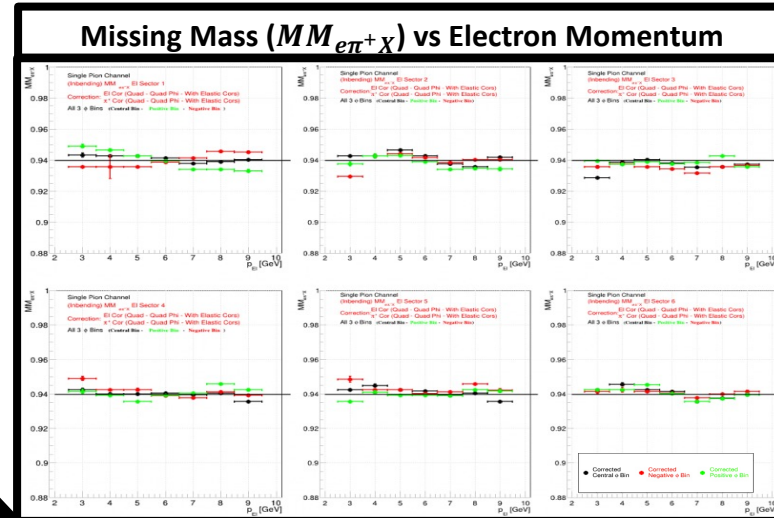
- Momentum corrections are developed for the RG-A data being used in this analysis
- Designed to correct for kinematic-dependent reconstruction issues in the experimental data using well-understood reactions
- Use exclusive reactions to correct the particles' momentum as sector-dependent functions of the particles' measured azimuthal angle ( $\phi_{\text{lab}}$ ) and momentum
  - The primary reaction used for the electron and  $\pi^+$  pion is  $\mathbf{ep} \rightarrow \mathbf{e}'\pi^+(\mathbf{N})$
  - Elastic scattering process also used to help correct the electron momentum
- Developed from momentum 4-vector conservation to calculate the ideal momentum of a particle from exclusive reactions based on the kinematics of the other particle(s)
  - Correction is taken by plotting the difference between this calculation and the measured momentum as functions of the measured momentum and  $\phi_{\text{lab}}$

# Momentum Corrections from Exclusive Events

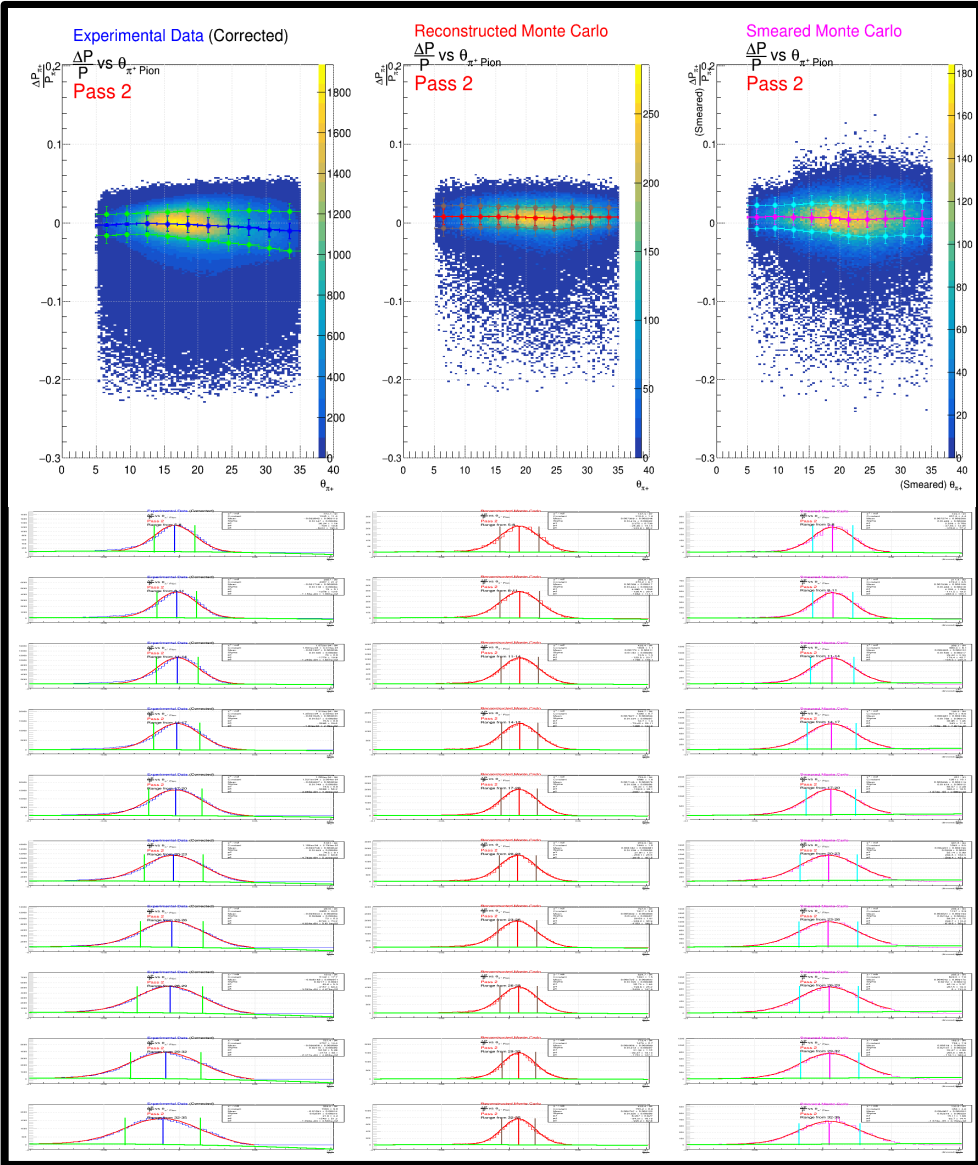
These plots show Missing Mass vs. particle momentum in 3  $\phi$  bins for all 6 sectors of the detector before/after momentum corrections – Corrections are quadratic functions of  $\phi$  and momentum



Apply Momentum Corrections



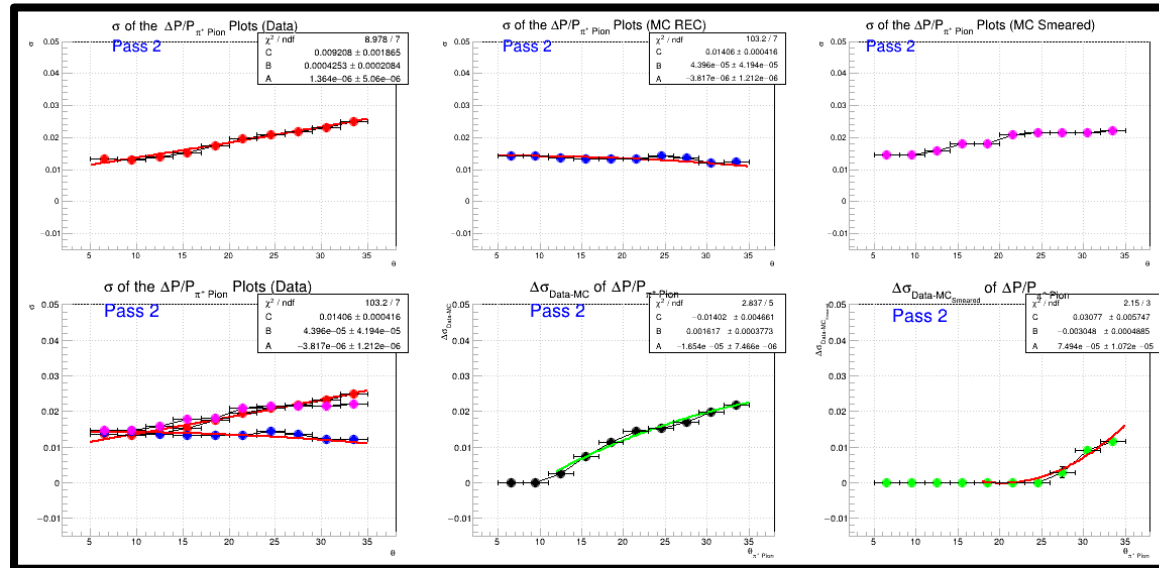
# Data and Monte Carlo Comparison (Smearing)



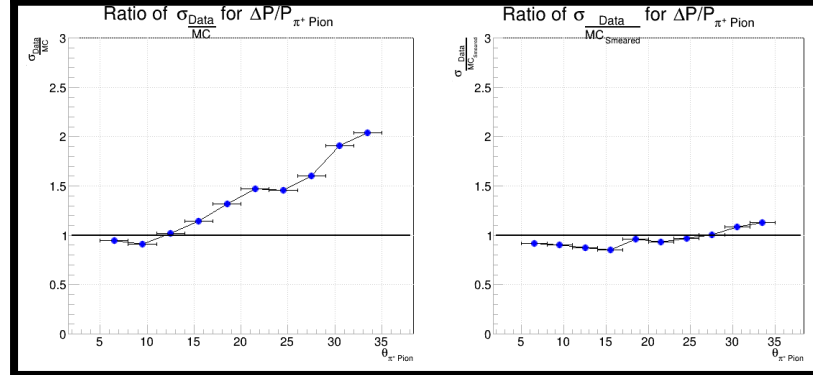
Form of Smearing Function:

$$P_{\text{smeared}} = P_{\text{REC}} + g\text{Random} \rightarrow \text{Gaus}(0, P_{\text{REC}} * \sigma(\theta) * SF)$$

Where  $\sigma(\theta)$  is the difference in the widths of  $\Delta P/P$  for the Unsmearred MC and Data plots  
 $SF$  is an additional constant smearing factor that gives me more control over the function



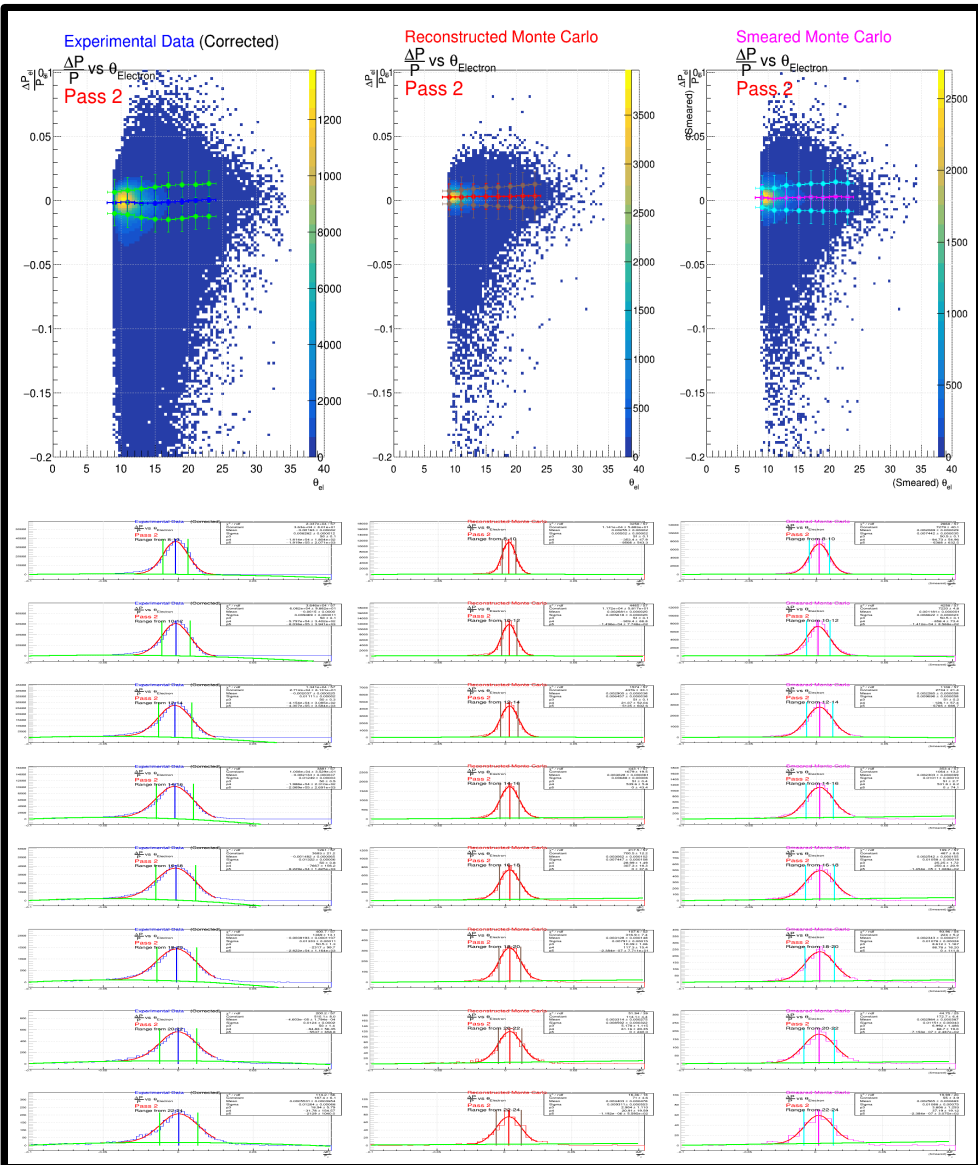
Difference between widths of Smeared MC and Data



Ratio of Peak Widths Before/After Smearing

Smearing for the **π<sup>+</sup> Pion**

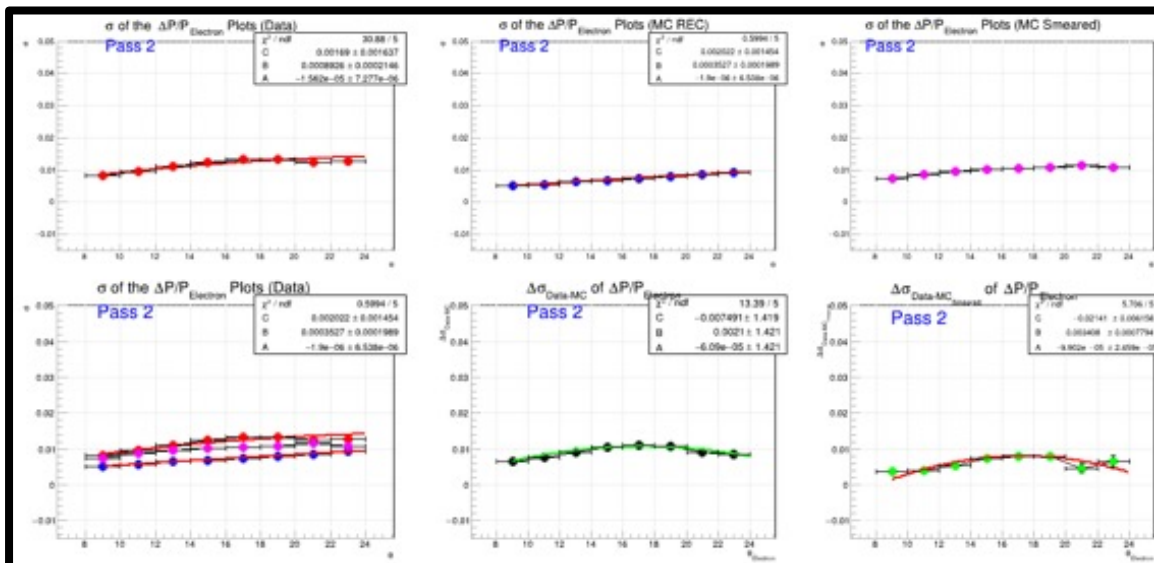
# Data and Monte Carlo Comparison (Smearing)



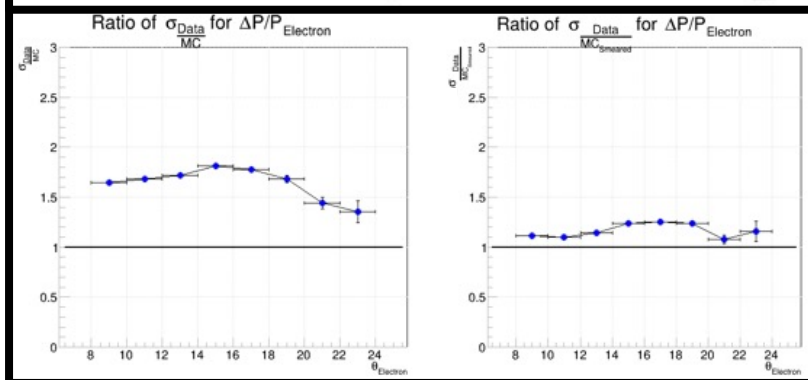
Form of Smearing Function:

$$P_{\text{smeared}} = P_{\text{REC}} + g\text{Random} \rightarrow \text{Gaus}(0, P_{\text{REC}} * \sigma(\theta) * SF)$$

Where  $\sigma(\theta)$  is the difference in the widths of  $\Delta P/P$  for the Unsmearred MC and Data plots  
 $SF$  is an additional constant smearing factor that gives me more control over the function



Difference between widths of Smeared MC and Data



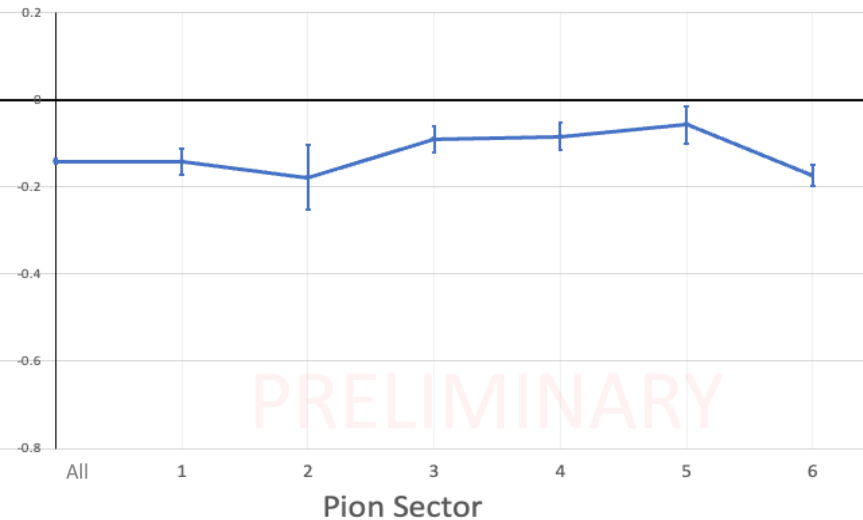
Ratio of Peak Widths Before/After Smearing

Smearing for the **Electron**

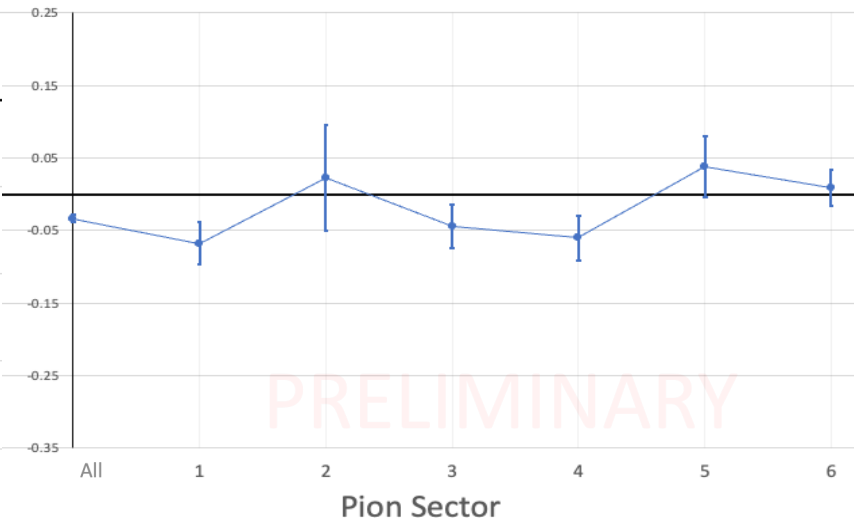


# (Pion) Sector Correlations with Cos( $\phi$ ) and Cos( $2\phi$ ) Measurements

Plot of Cos( $\phi$ ) vs Sector for Q2-y-z-PT Bin: 3-22



Plot of Cos(2 $\phi$ ) vs Sector for Q2-y-z-PT Bin: 3-22

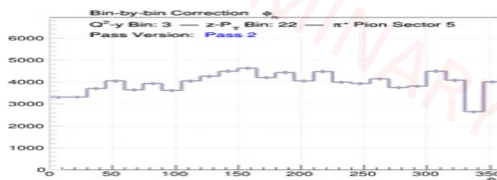
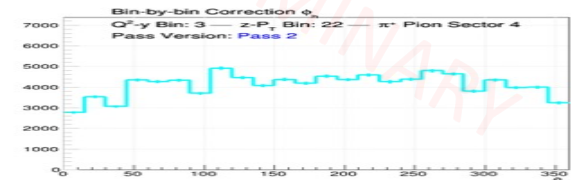
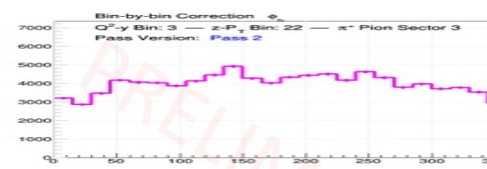
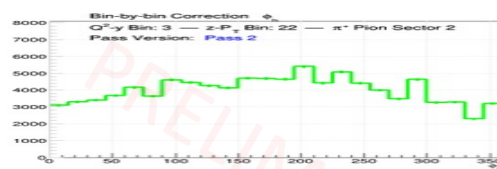
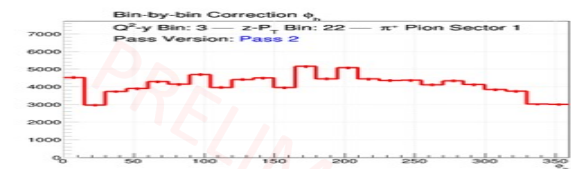
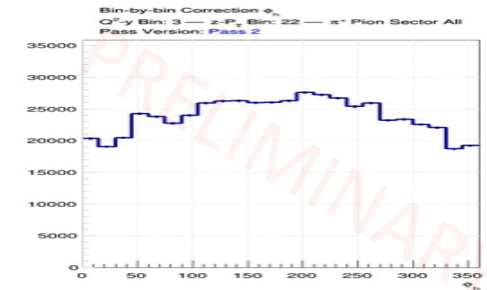
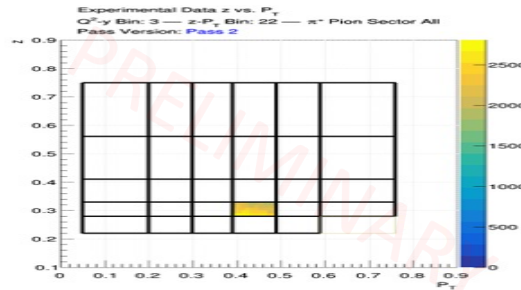
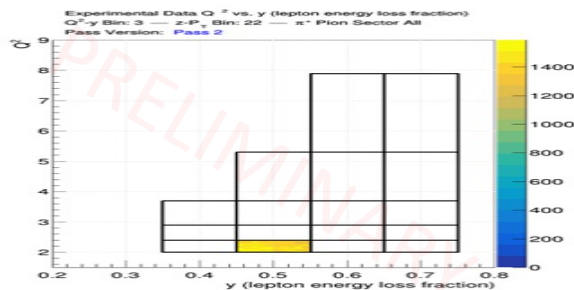


Some sector dependence remains despite the new cuts

On average, the particle sector makes a noticeable difference about 50% of the time\* (i.e., the measurements of each sector do not agree with the measurement taken without sector dependence to within the errors shown)

**A sector dependences does seem to exist, but further investigation is still required**

\*Some of these discrepancies can be blamed on individual fits failing due to even worse acceptances that have not yet been individually addressed



# More on Boer-Mulders...

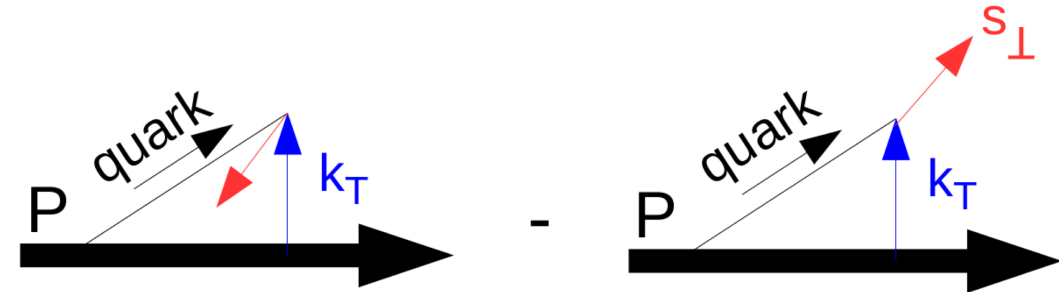
quark pol.

nucleon pol.

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}^\perp$	$h_1, h_{1T}^\perp$

Boer-Mulders

$$h_1^\perp =$$



- $\mathbf{P}$  is the momentum of the proton
- $\mathbf{k}_T$  is the transverse momentum of the quark
- $\mathbf{s}_\perp$  is the transverse spin of the quark

If the Boer-Mulders term is non-zero, then there is a net transverse quark polarization inside of unpolarized protons

# END

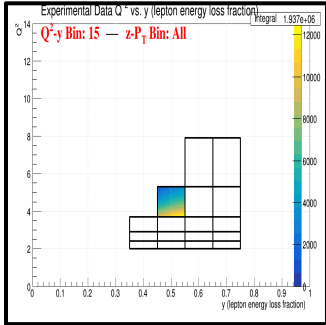
## Link to more Images:

[https://userweb.jlab.org/~richcap/Interactive\\_Webpage\\_SIDIS\\_richcap/Interactive\\_Unfolding\\_Page\\_Updated.html](https://userweb.jlab.org/~richcap/Interactive_Webpage_SIDIS_richcap/Interactive_Unfolding_Page_Updated.html)

# Pass 2 Condition

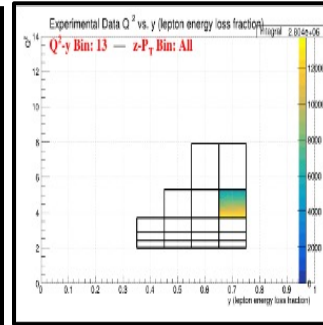
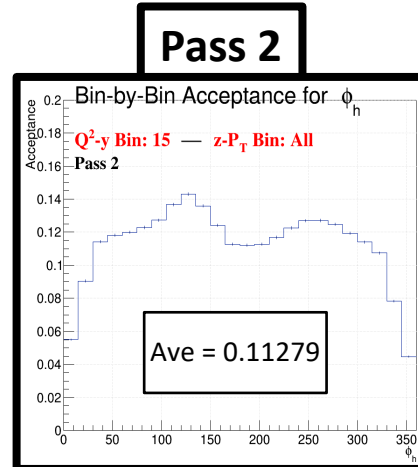
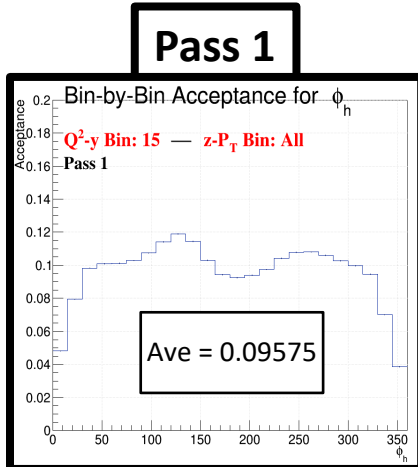
- Momentum/Energy Loss Corrections in Pass 2 have been implemented
- Monte Carlo statistics are still low (using test sample)
  - Planning to run more files soon
  - Also hope to run using RADGEN to start including radiative effects
  - Working side-by-side with Pass 1 in the meantime for better MC statistics

# Pass 2 Comparisons - Acceptances



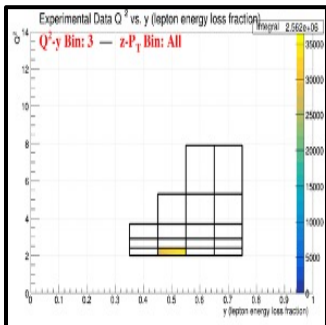
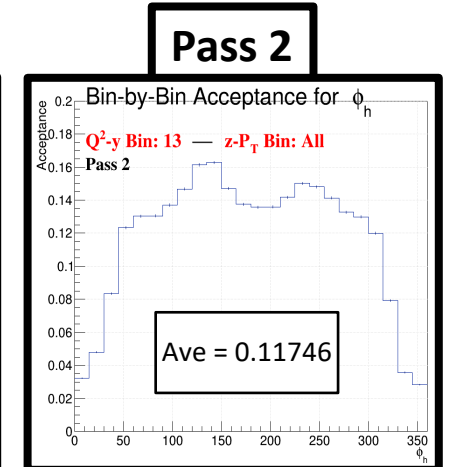
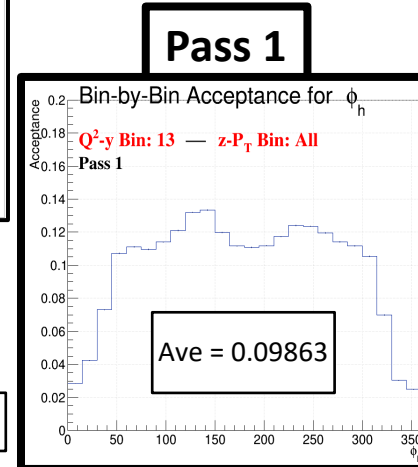
High  $Q^2$   
Low  $y$

$\Delta Ave = +0.01704$



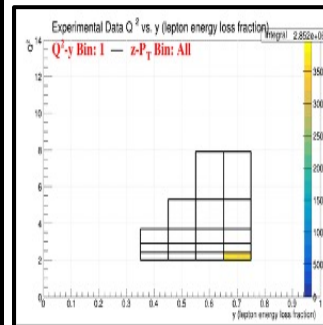
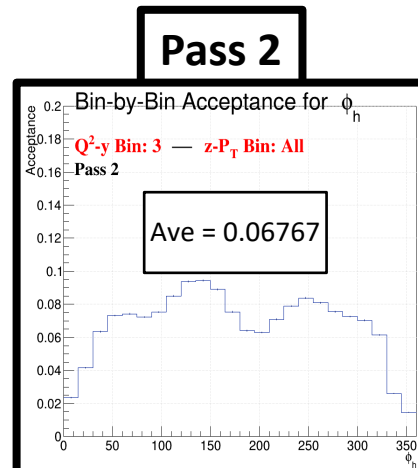
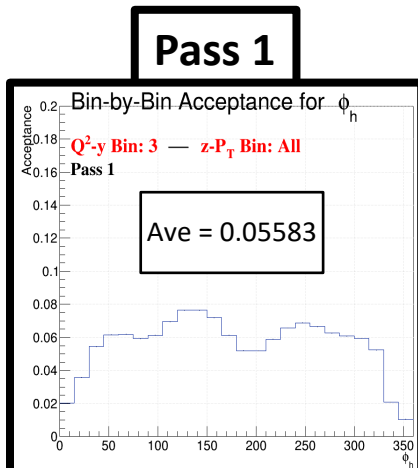
High  $Q^2$   
High  $y$

$\Delta Ave = +0.01883$



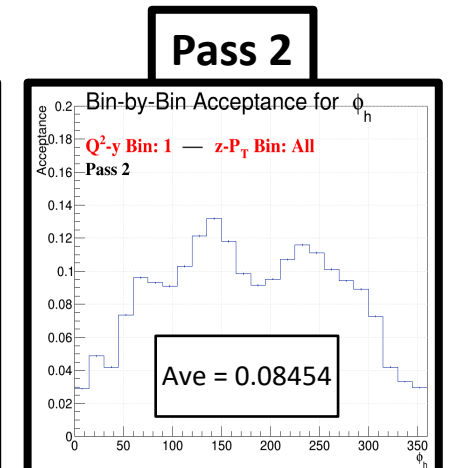
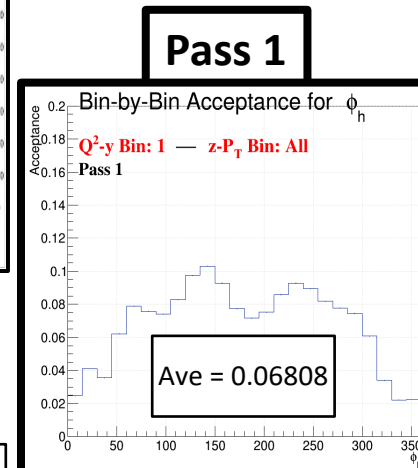
Low  $Q^2$   
Low  $y$

$\Delta Ave = +0.01184$



Low  $Q^2$   
High  $y$

$\Delta Ave = +0.01646$



# Cos( $\phi_h$ ) Moment as Functions of z - Pass 2 Comparison

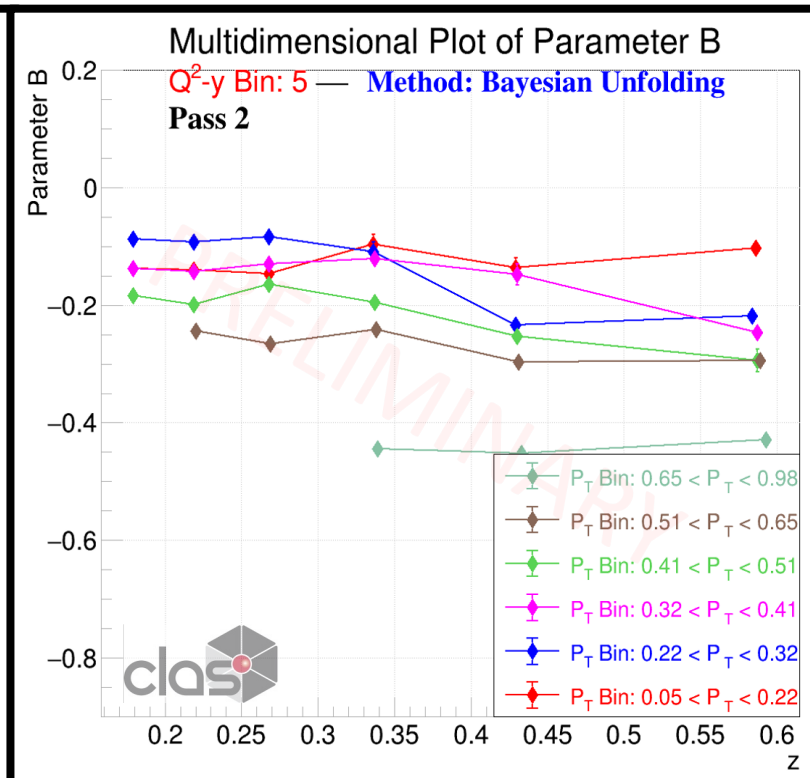
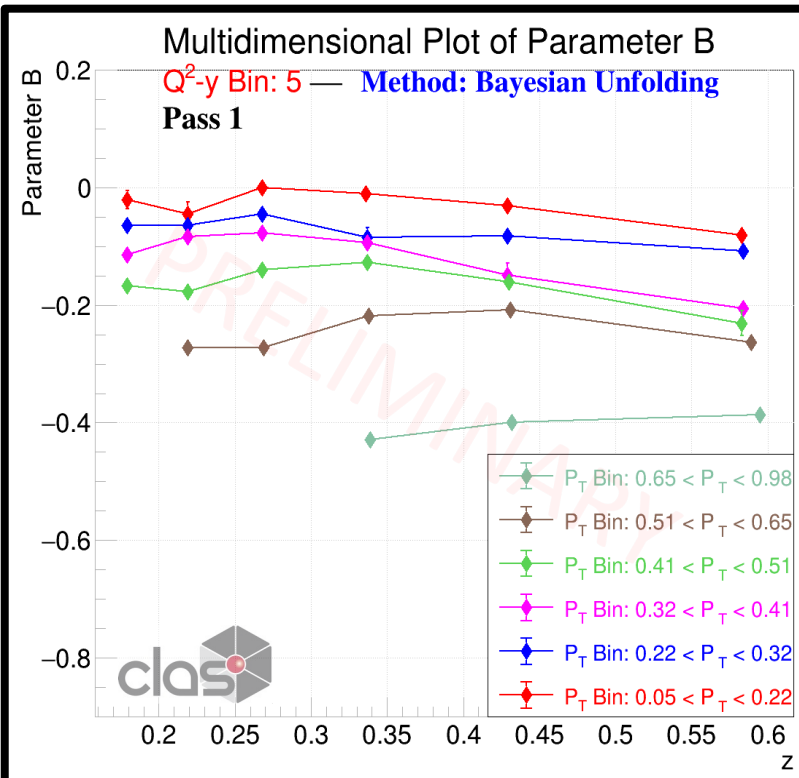
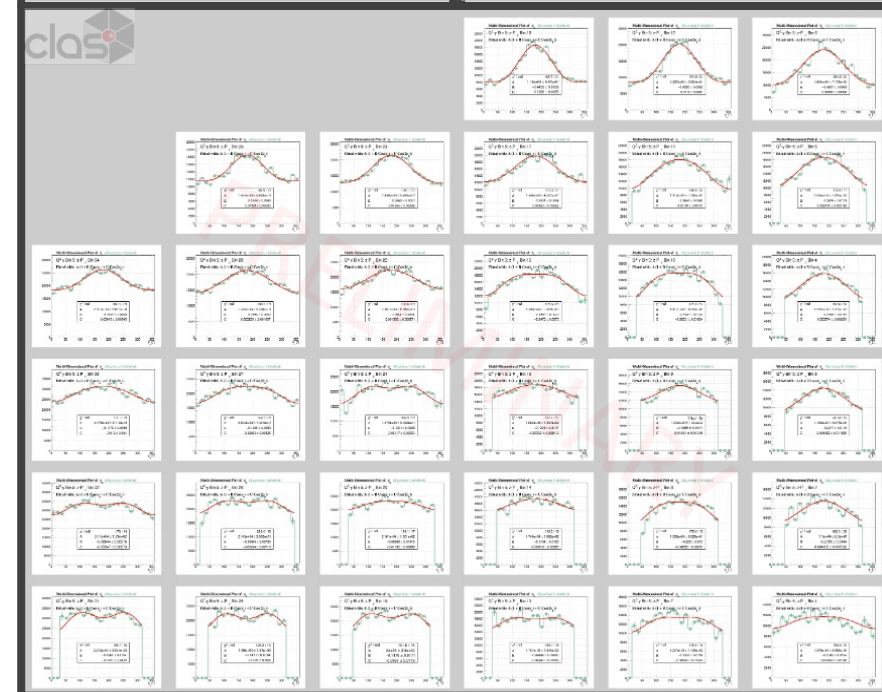
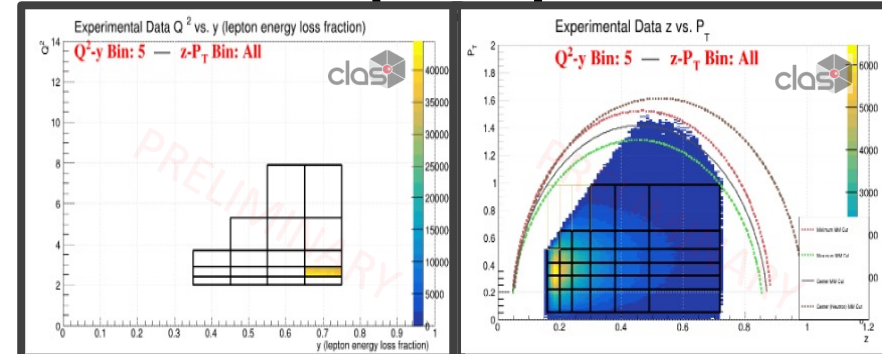
$$B = A_{UU}^{\cos \phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

$Q^2$ -y Bin 5

Pass 2



# Cos(2φ<sub>h</sub>) Moment as Functions of z - Pass 2 Comparison

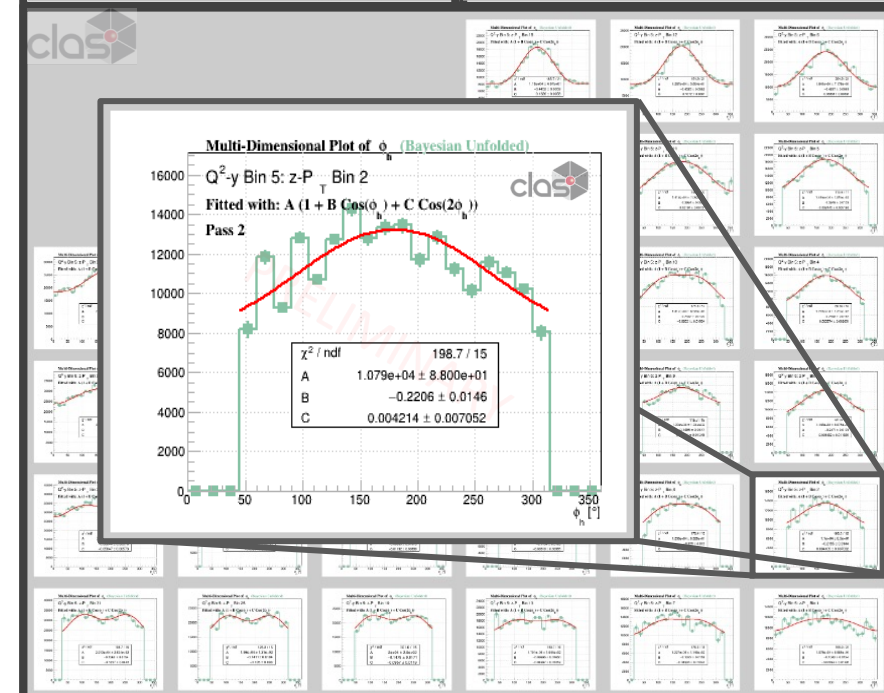
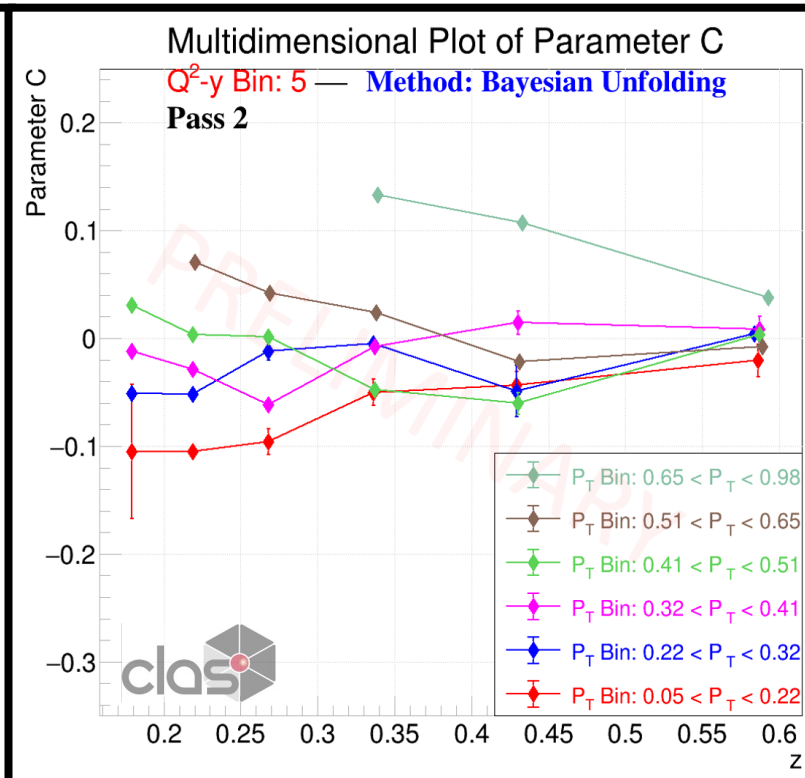
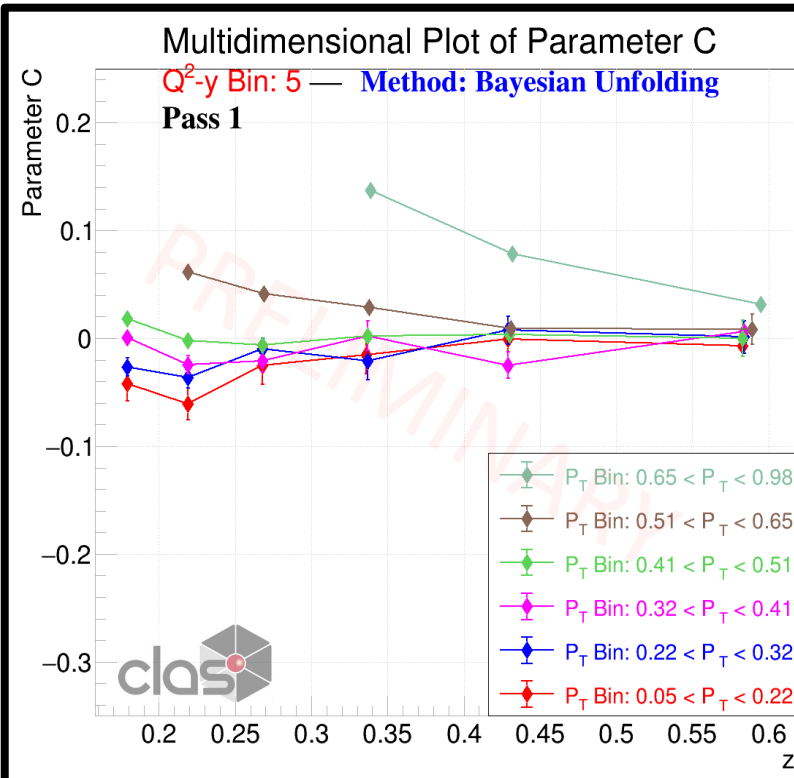
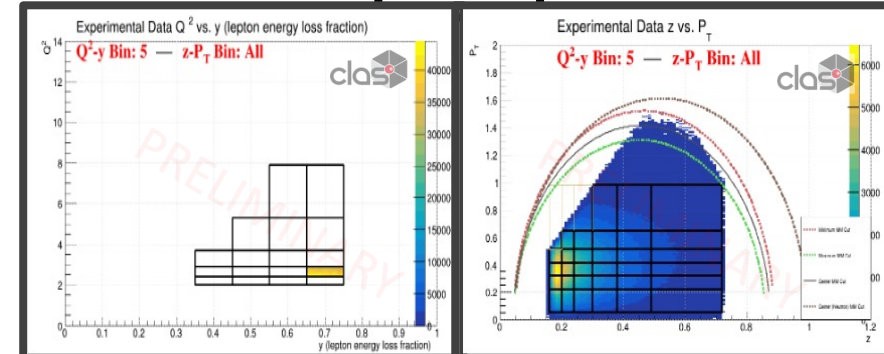
$$C = A_{UU}^{\cos 2\phi_h}$$

φ<sub>h</sub> Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

Q<sup>2</sup>-y Bin 5

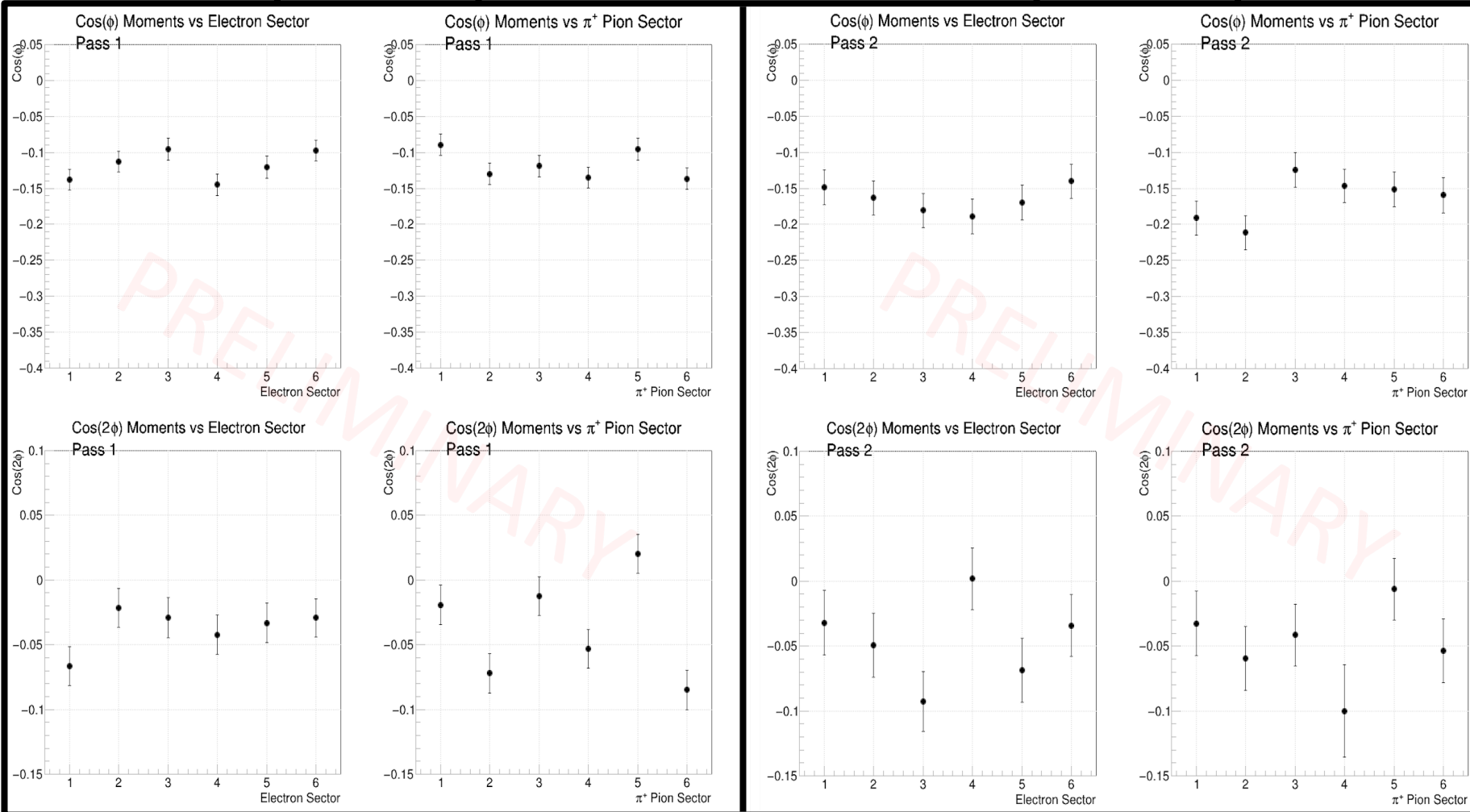
Pass 2



# Sector Correlations with $\text{Cos}(\phi)$ and $\text{Cos}(2\phi)$ Measurements

**PASS 1**

**PASS 2**



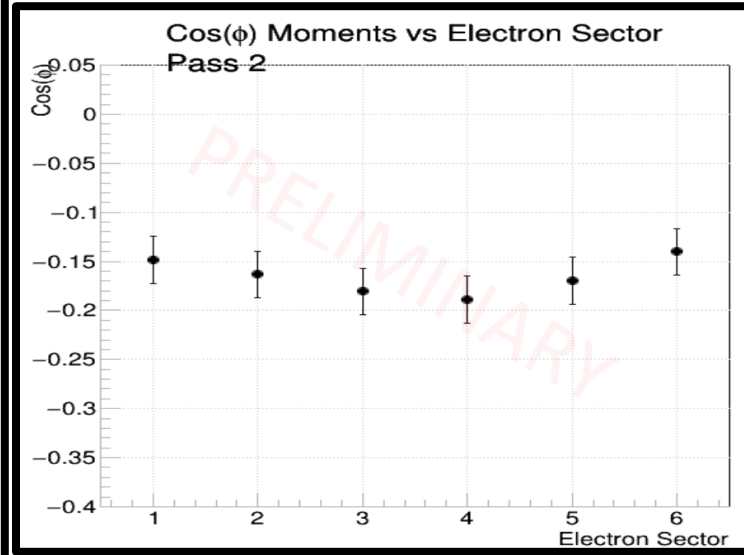
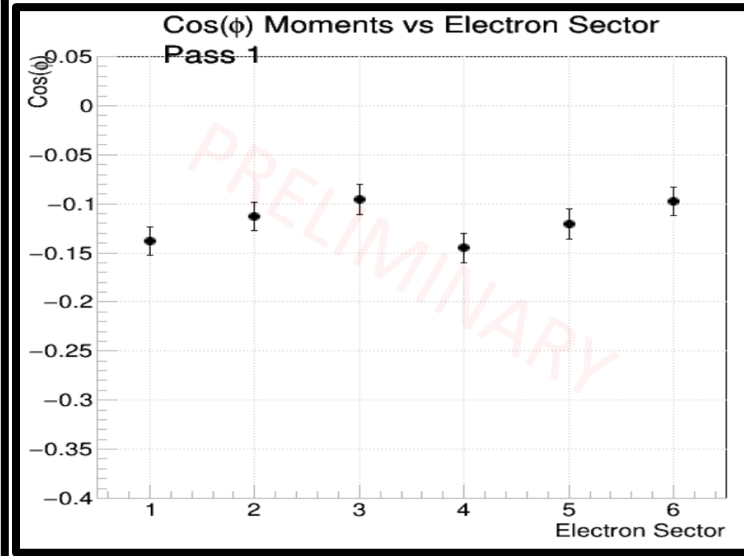
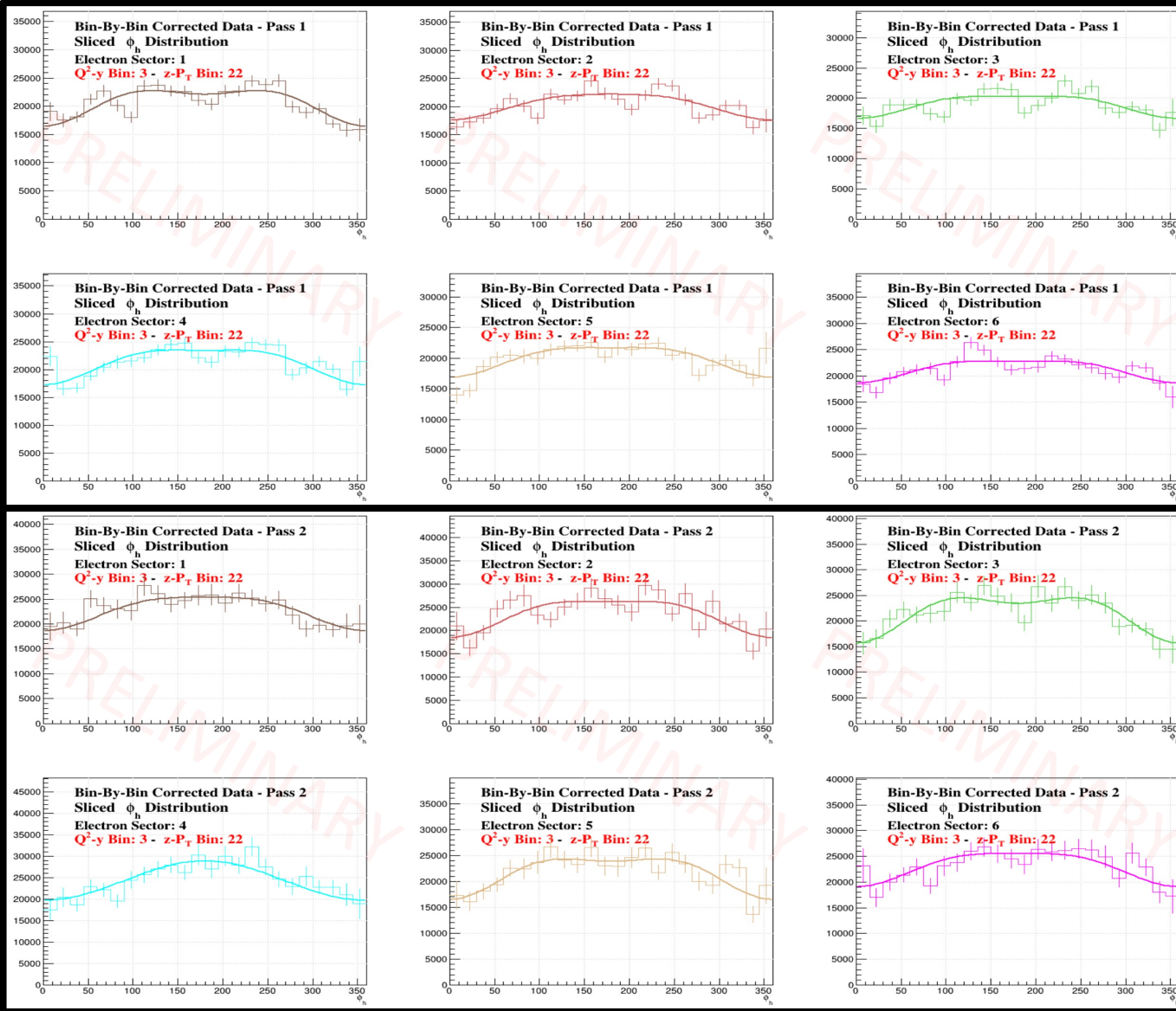
Showing the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  Moments as functions of the particle sector

These plots show those differences in Pass 1 and Pass 2 for when the Electron (left plots) or  $\pi^+$  pion (right plots) are restricted to being detected in a single sector

Images are grouped on the left and right based on Pass version of the data being used



# Sector Correlations with $\text{Cos}(\phi)$ Measurements – Pass 1 and 2



Sectors can cause different modulations within the kinematic bins

These plots show those differences in Pass 1 (top row) and Pass 2 (bottom row)

**Electron is restricted to being detected in a single sector**

Plotting  $\text{Cos}(\phi)$  Moments vs Electron Sector on the right