
A novel measurement of the neutron magnetic form factor from $A=3$ mirror nuclei

Nathaly Santiesteban

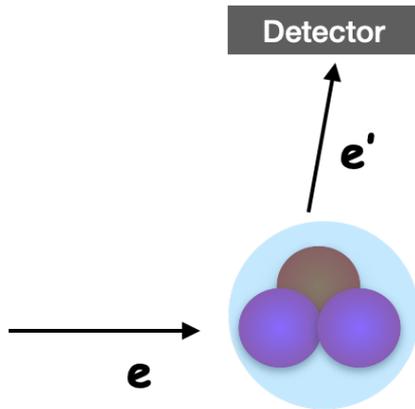
On behalf of the E12-11-112
collaboration

JLUO Annual Meeting
2024

[*Phys.Rev.Lett.* 132 \(2024\) 16, 162501](#)



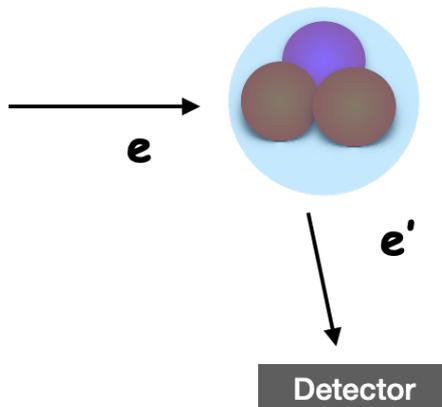
E12-11-112 Experiment



^3He and ^3H mirror nuclei:

^3He (protons) \leftrightarrow ^3H (neutrons)

- ◆ Few-body nuclei
- ◆ Benchmark data
- ◆ cancellation of experimental systematics, nuclear effects

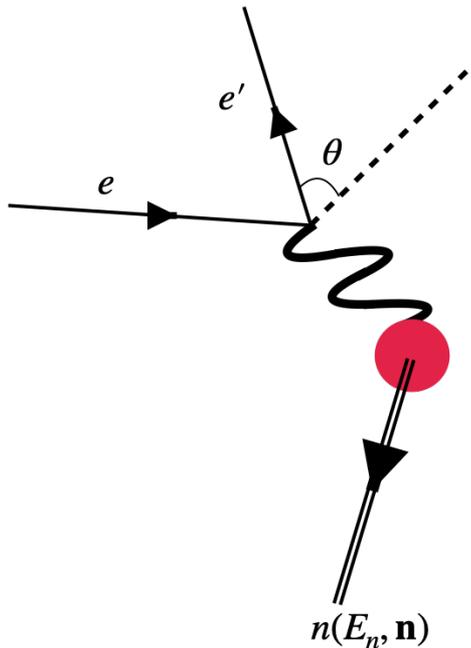


Inclusive Measurements

- ◆ Sum of Short-range correlations ([See Shujie's talk tomorrow](#))
 $^3\text{He}/^3\text{H}$ (2pn + pp)/(2pn + nn) ($x > 1$)
Ratio of pp to pn pairs assuming isospin symmetry
- ◆ Access G_M^n : Effective neutron target ($x=1$) (**This talk**)
- ◆ Charge radius of ^3H vs ^3He ($x=3$) (In progress)

Understanding neutron form factors

$$\left(\frac{d\sigma}{d\Omega}\right)_n = \left(\frac{d\sigma}{d\Omega}\right)_{Mott} \frac{1}{1 + \tau} \left((G_E^n(Q^2))^2 + \frac{\tau}{\varepsilon} (G_M^n(Q^2))^2 \right)$$



$G_E^n(Q^2)$: Electric form factor

$G_M^n(Q^2)$: Magnetic form factor

Encode information on the spatial distribution of charge and magnetization

In the center of mass of the electron-Nucleon system (Breit frame)
no energy transfer ($\omega_{CM} = 0 \rightarrow |q|^2 = |\mathbf{q}|^2$)

$\rho(\mathbf{r}) \rightarrow$ charge distribution $\mu(\mathbf{r}) \rightarrow$ Magnetization distribution

$$G_E = \int \rho(\mathbf{r}) e^{i\mathbf{q}\cdot\mathbf{r}} d^3\mathbf{r} \qquad G_M = \int \mu(\mathbf{r}) e^{i\mathbf{q}\cdot\mathbf{r}} d^3\mathbf{r}$$

Static limit: $Q^2 \rightarrow 0$

$$G_E^n(0) = 0 \qquad G_M^n(0) = \mu_n$$

No free neutron target

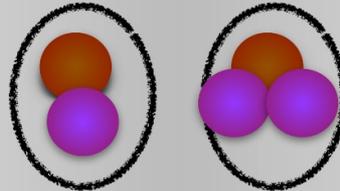
If measuring neutrons (no charge):

- Energy information from time of flight.
- Requires precise measurement of neutron detection efficiencies.

Measurement Corrections:

- Reaction mechanisms FSI and MEC.
- Nuclear structure.

Lightest nuclei are used for neutron measurements



${}^2\text{H}$

${}^3\text{He}$

Neutron measurements include:

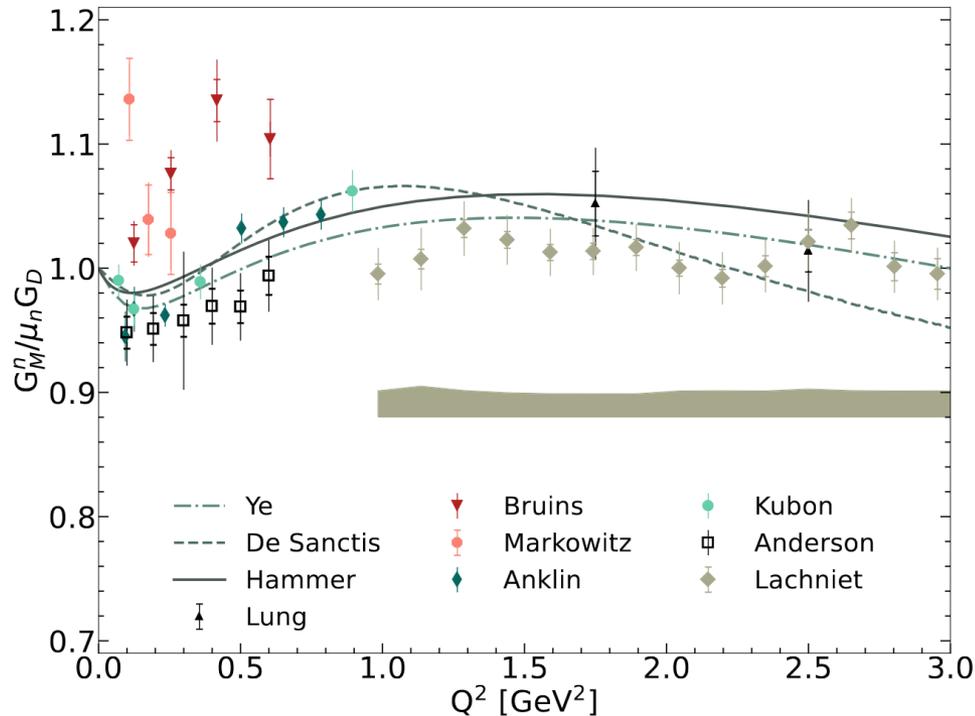
${}^3\overline{\text{He}}(\vec{e}, e')$ QE
polarization experiments

$\frac{{}^2\text{H}(e, e'p)}{{}^2\text{H}(e, e'n)}$ QE ratio

${}^2\overline{\text{H}}(\vec{e}, e')$ QE
Vector-polarized deuterium

${}^2\text{H}(e, e') - p(e, e')$
 ${}^2\text{H}(e, e'p), {}^2\text{H}(e, e'n)$

Previous measurements



Inclusive: $d(e,e')$

- Subtract proton, correct for Fermi motion
- Large subtraction enhances statistical, expt. systematic, and model uncertainties

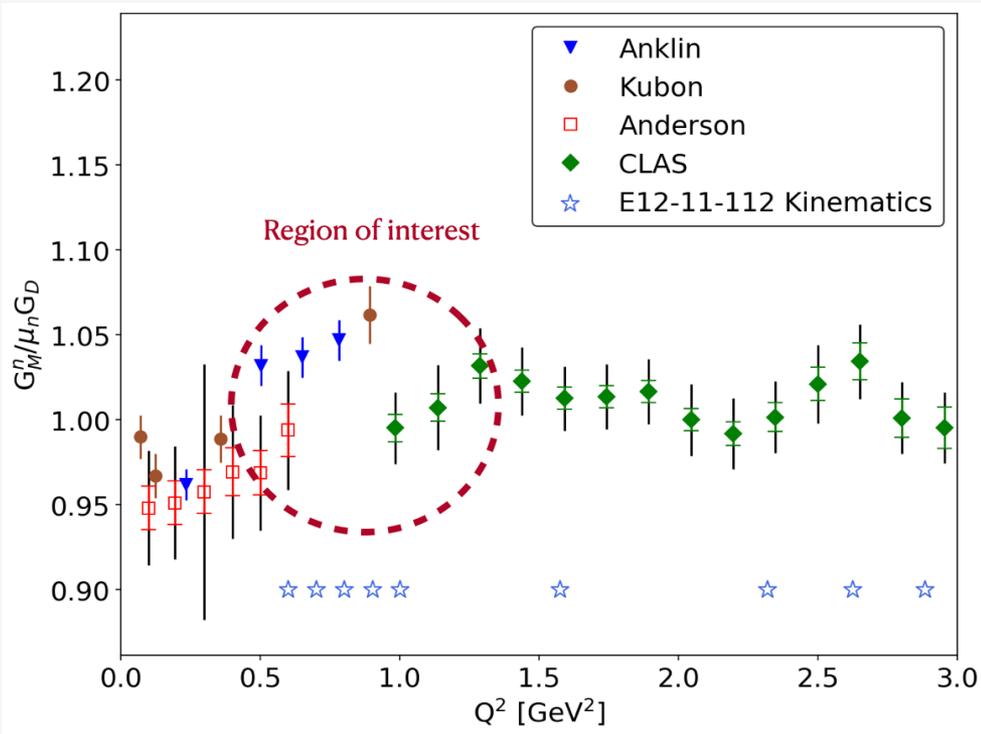
Exclusive: ratio of $d(e,e'n)/d(e,e'p)$

- No proton 'subtraction'
- Low (uncertain) neutron detection efficiency
- Smaller correction for motion in deuteron

Polarized ³He

- Corrections are well understood at low Q^2
- Larger overall uncertainties

Motivation



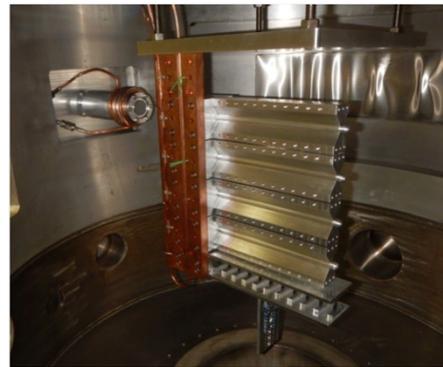
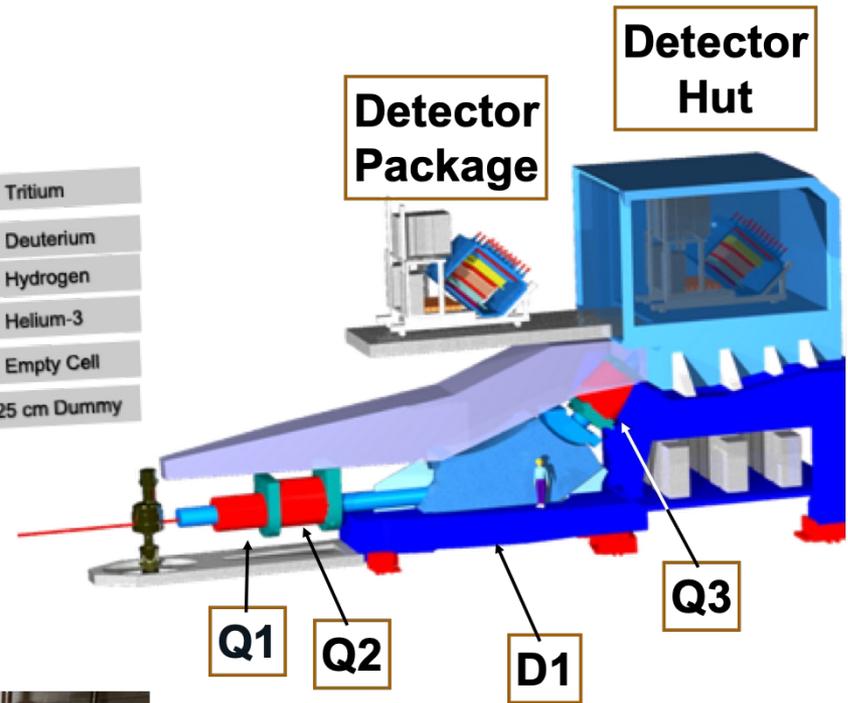
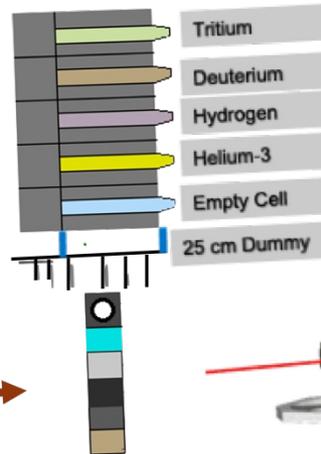
- Of particular interest is the region $0.5 < Q^2 < 1 \text{ GeV}^2$, where the differences are most pronounced
- E12-11-112 covered QE peak for $0.6 < Q^2 < 2.8$
- Goal of providing new data in this region to help understand the discrepancy using the A=3 targets – very different corrections, systematic uncertainties.

Experimental Setup

Hall A

$E = 2.2 \text{ GeV}$
 $E = 4.3 \text{ GeV}$

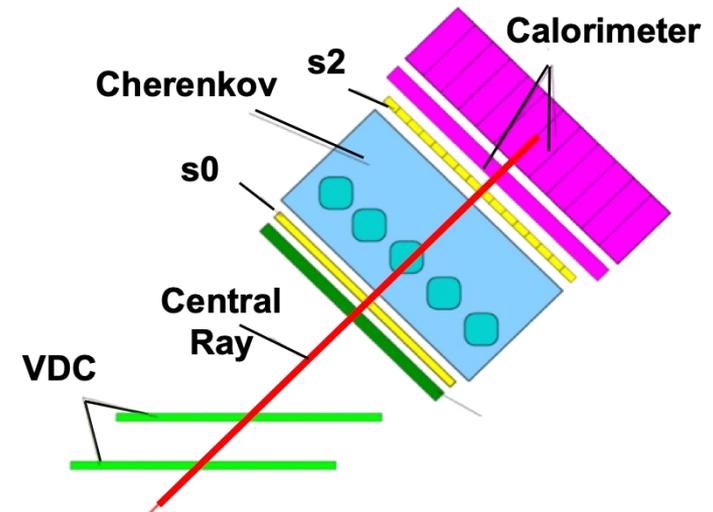
Electron Beam →



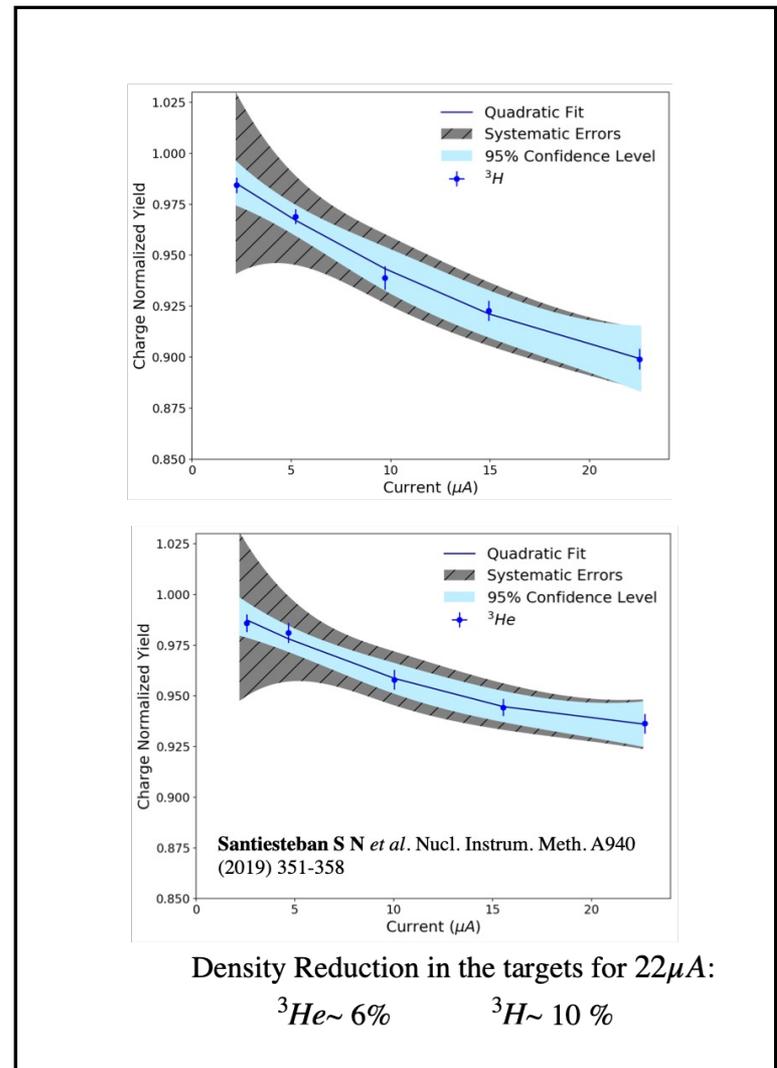
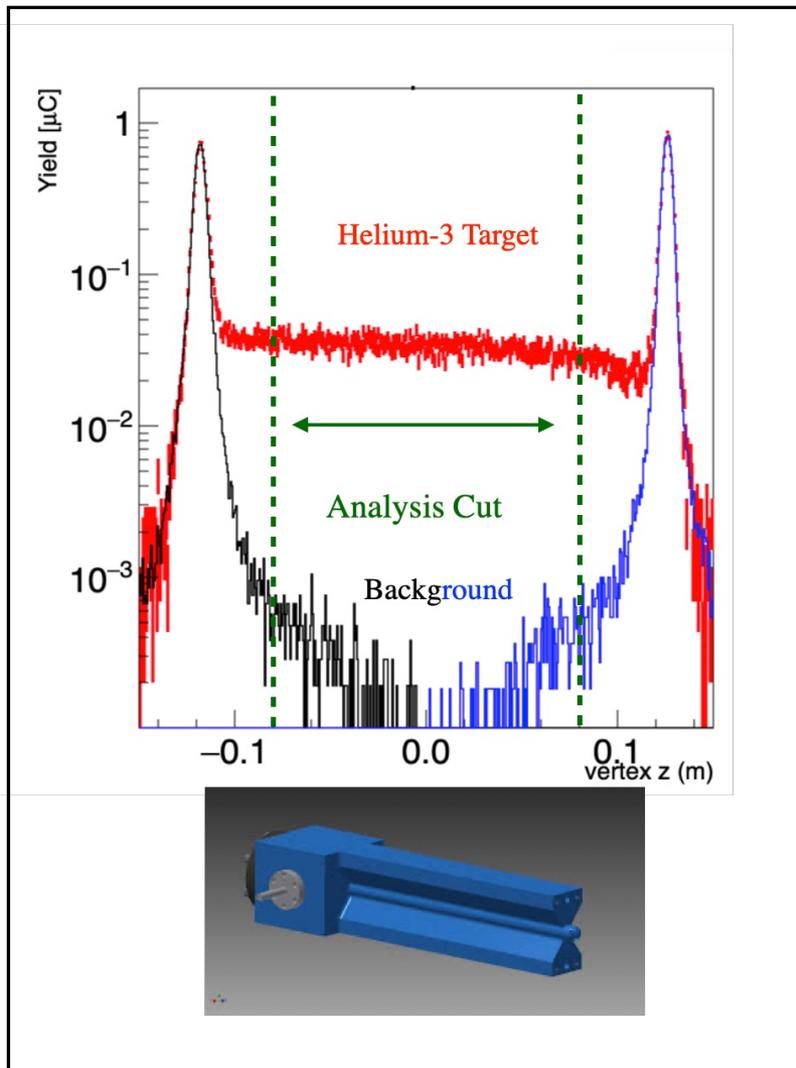
Target System

LHRS and RHRS

- *10 different Q^2 Points
- *2-3 Kinematics Settings per Q^2 point.
- *3 run periods.
- *2 Tritium Cells



A few analysis remarks



Helium contamination in the tritium cell

First Cell:



Second Cell:

Tritium ($\tau = 4500 \pm 8$ days): $n_{3H}(t) = n_0 e^{-t/\tau}$

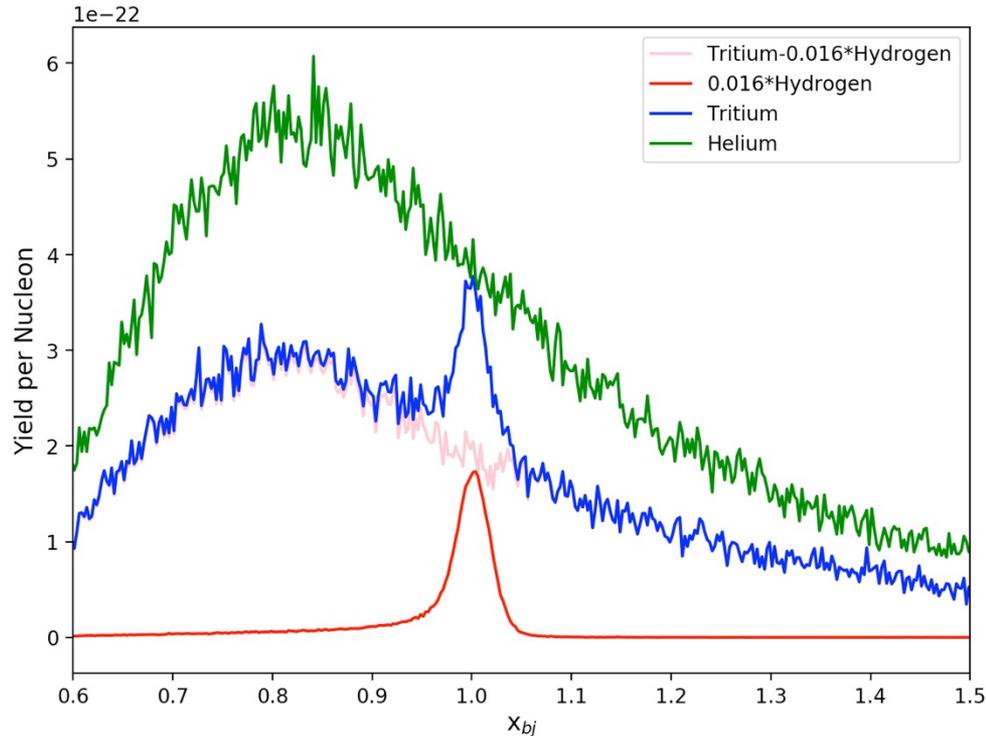
What is measured: $\sigma^{measured} = \sigma^{3H} e^{-t/\tau} + \sigma^{3He} (1 - e^{-t/\tau})$

What is wanted:
 if $f(t) = \frac{n_{3H}(t)}{n_0} = 1 - e^{-t/\tau}$ $Y^{3H} = \frac{Y^{measured}}{1 - f(t)} - Y^{3He} \frac{f(t)}{1 - f(t)}$

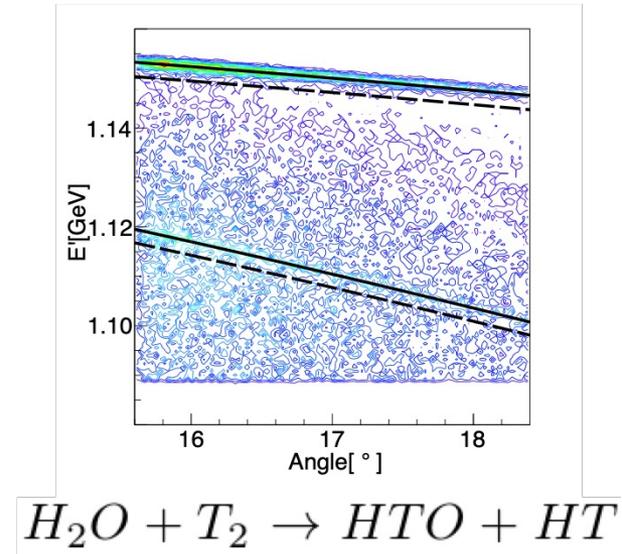
Filling Date
08/24/2018
100% Tritium



Hydrogen contamination in the second tritium cell

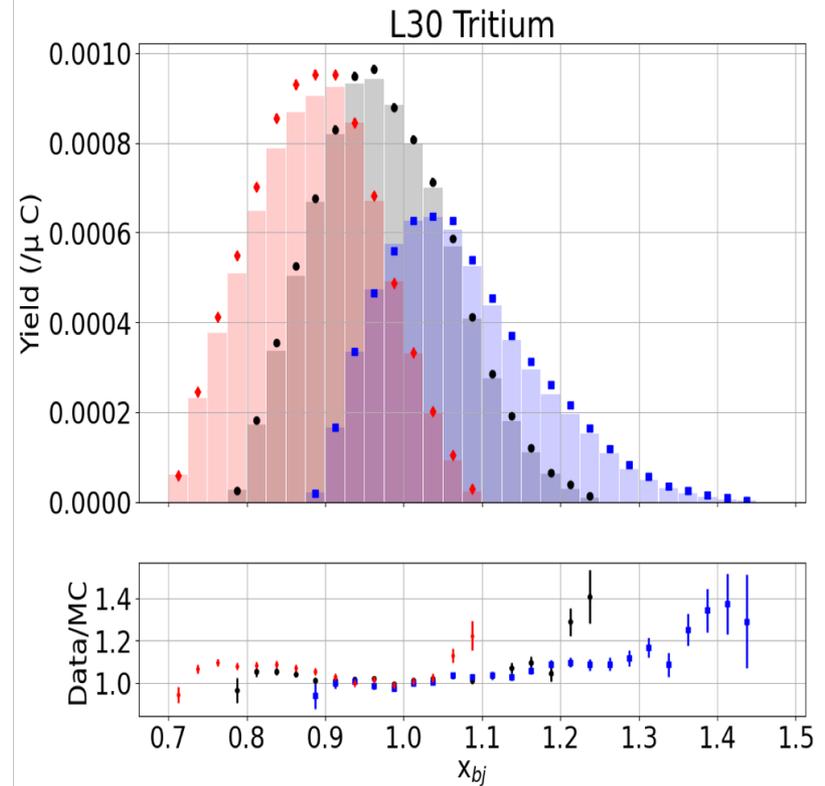
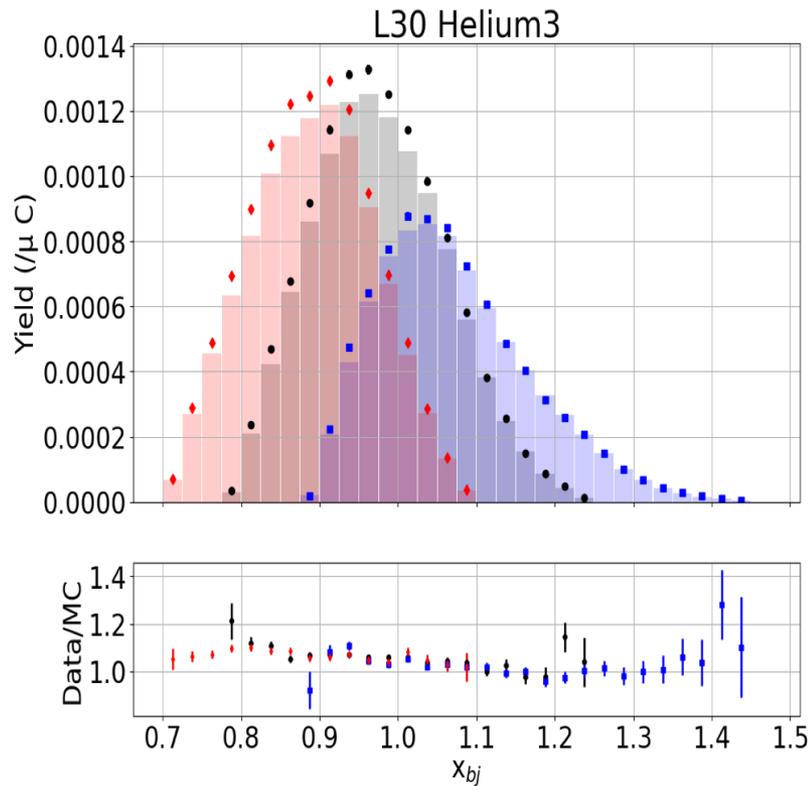


4.12% Hydrogen Contamination



The kinematics with hydrogen contamination were corrected with simulation or data when available.

Data/MC Sample

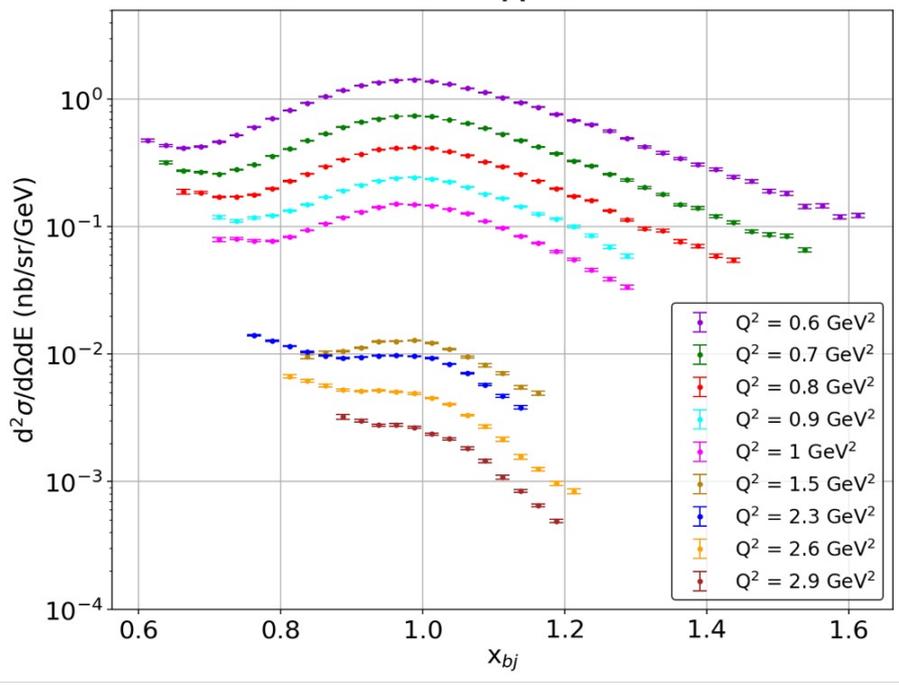


LS: Low Side of the QE peak
PK: Centered at the QE peak
HS: High side of the QE peak

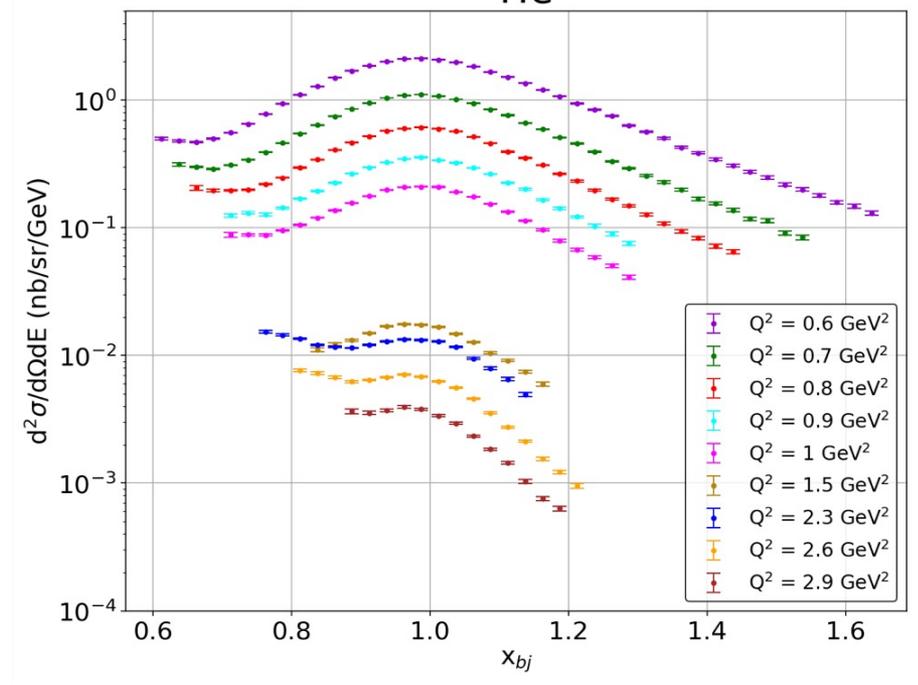
Cross-Sections

Preliminary Results

${}^3\text{H}$

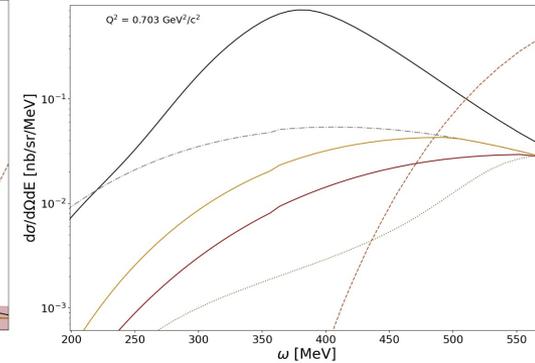
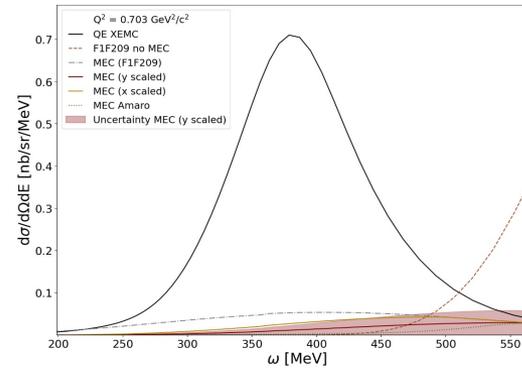
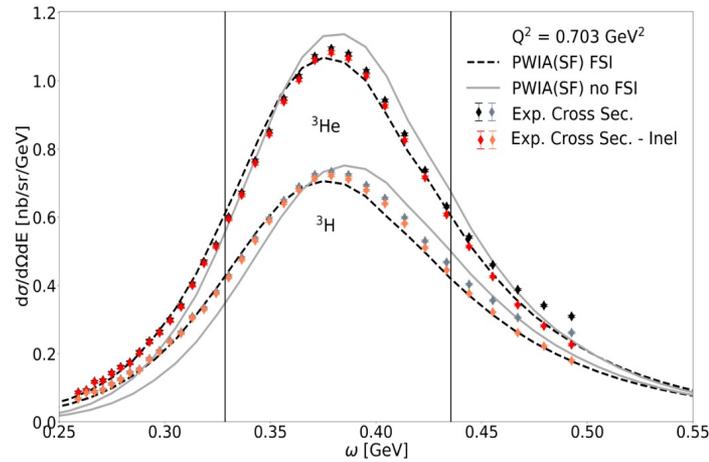


${}^3\text{He}$

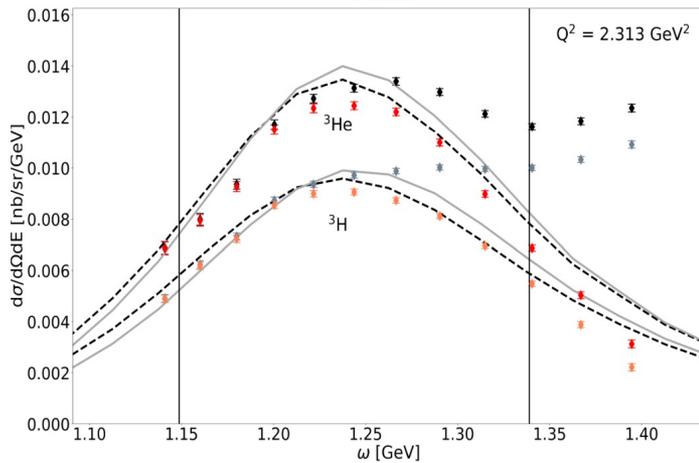


From Cross-Sections to G_M^n

1. Remove the inelastic distribution from the cross sections

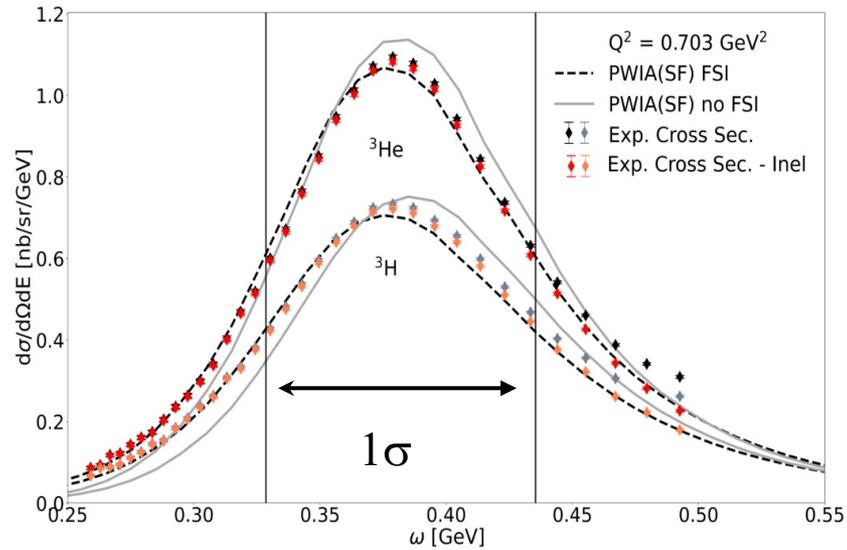


MEC100% uncertainty

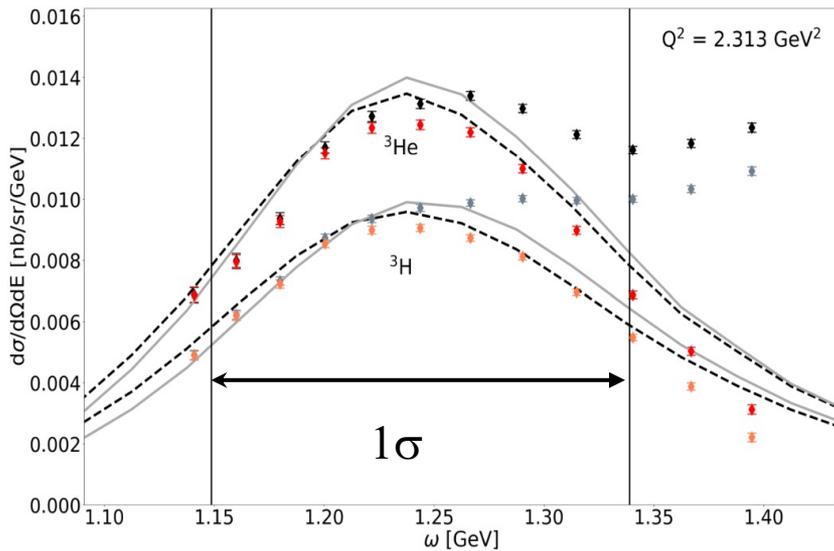


Calculations from Rocco and Lovatto
Phys. Rev. C 105, 014002 (2022)

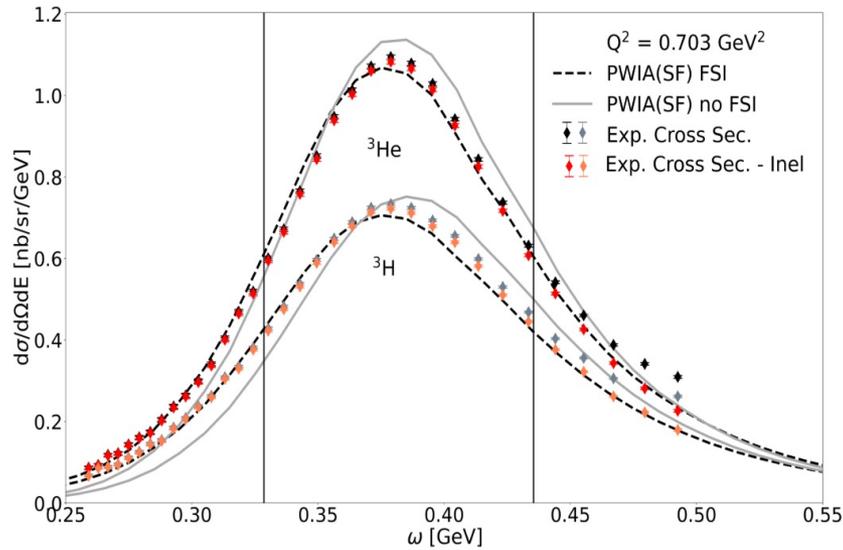
From Cross-Sections to G_M^n



1. Remove the inelastic distribution from the cross sections
2. Integrate the 1σ region (in both the model and the data) and calculate the ratio $R = ^3\text{H}/^3\text{He}$.

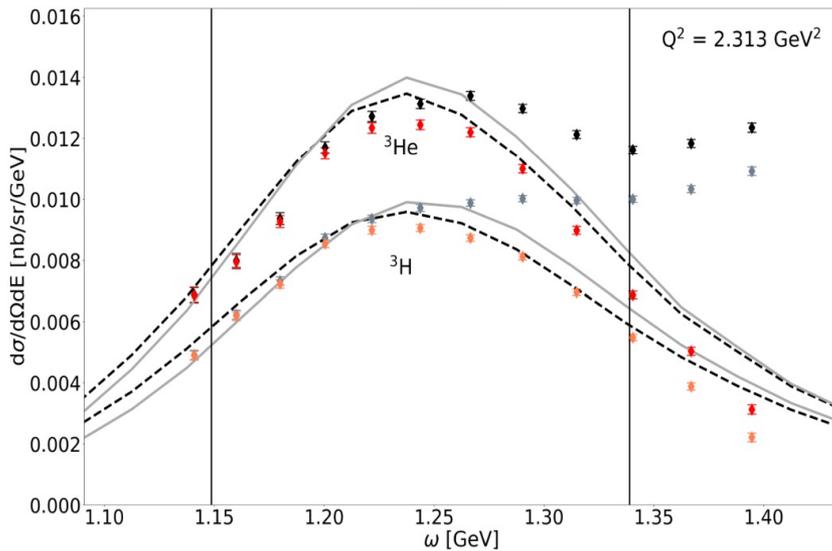


From Cross-Sections to G_M^n

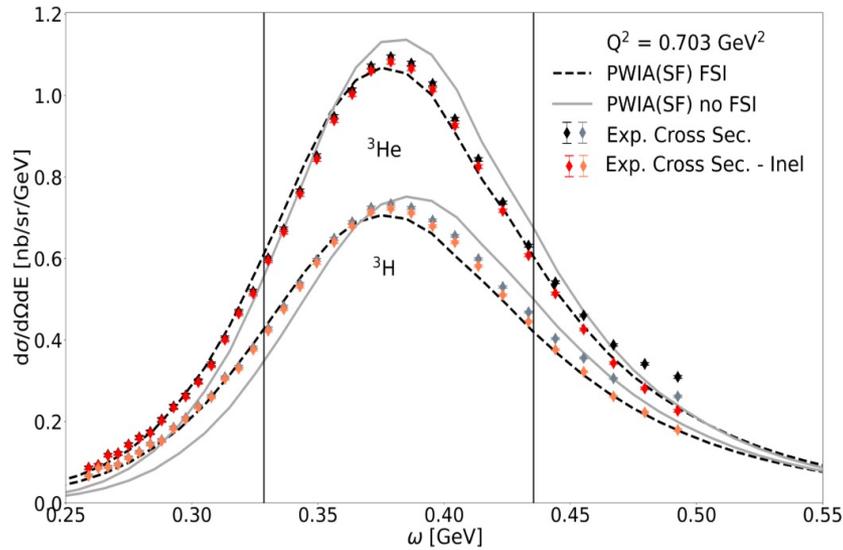


1. Remove the inelastic distribution from the cross sections
2. Integrate the 1σ region (in both the model and the data) and calculate the ratio $R = ^3\text{H}/^3\text{He}$.
3. Estimate the medium effects from the model (calculations).

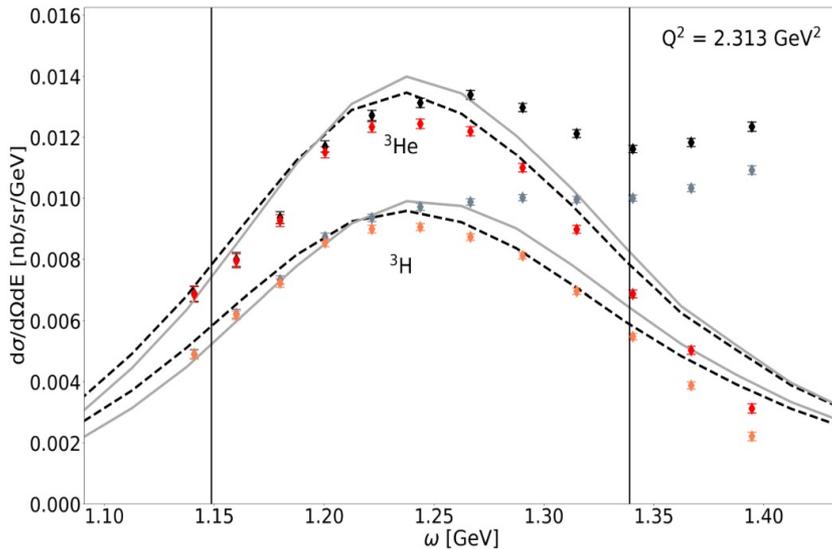
$$R^{Model} = \alpha \frac{2\sigma_n + \sigma_p}{\sigma_n + 2\sigma_p}$$



From Cross-Sections to G_M^n

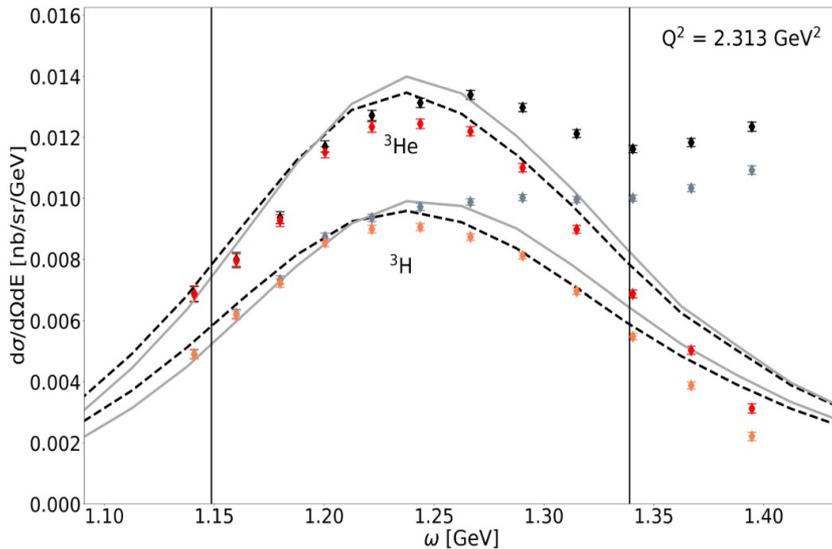
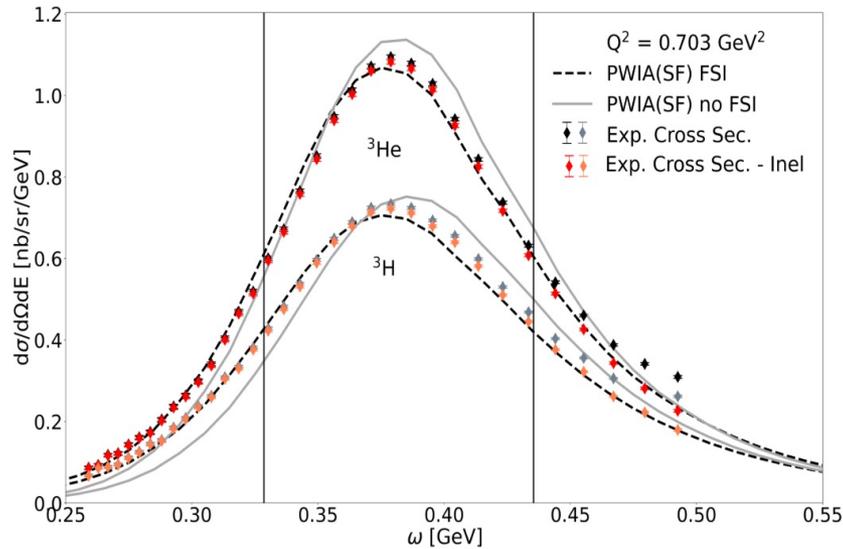


1. Remove the inelastic distribution from the cross sections
2. Integrate the 1σ region (in both the model and the data) and calculate the ratio $R = {}^3\text{H}/{}^3\text{He}$.
3. Estimate the medium effects from the model (calculations).
4. Calculate the σ_n/σ_p from the data ratio using the medium effects.



$$(\sigma_n/\sigma_p)^{Data} = \frac{\alpha - 2R^{Data}}{R^{Data} - 2\alpha}$$

From Cross-Sections to G_M^n

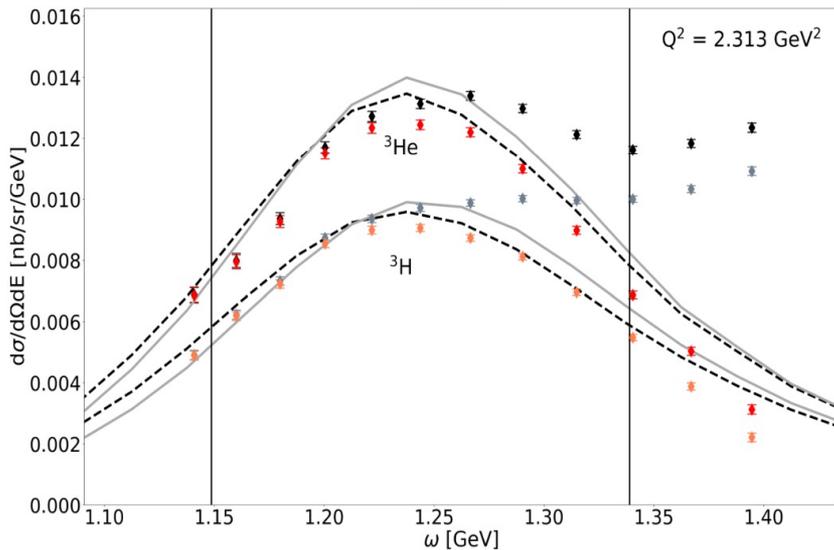
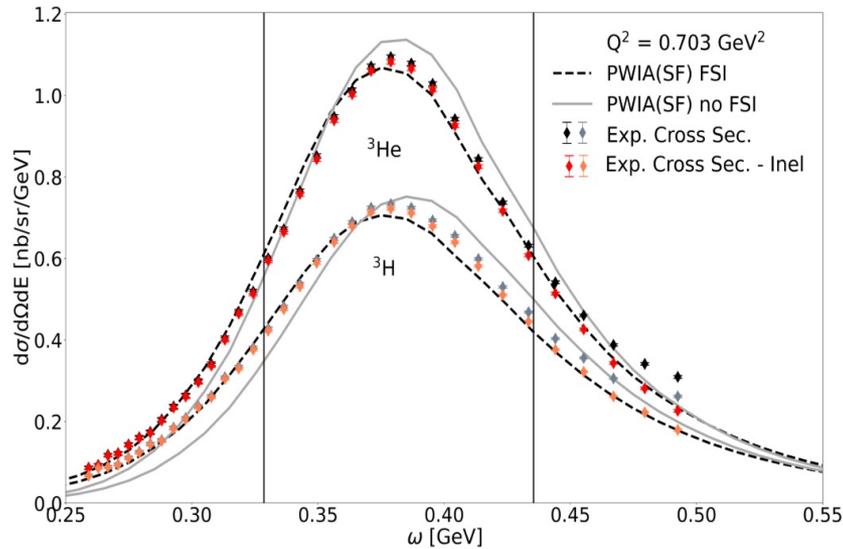


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4. Calculate the σ_n/σ_p from the data ratio using the medium effects.
5. Extract the born cross section, after correcting for the TPE.

$$\sigma_n^{Data-(Born+TPE)} = (\sigma_n/\sigma_p)^{Data} \sigma_p^{Fit-(Born+TPE)}$$

$\sigma_p^{Fit-(Born+TPE)}$ from direct fit to measured cross sections with no TPE correction J. Arrington, W. Melnitchouk, and J. A. Tjon, Phys. Rev. C 76, 035205 (2007).

From Cross-Sections to G_M^n



1. Remove the inelastic distribution from the cross sections
2. Integrate the 1σ region (in both the model and the data) and calculate the ratio $R = {}^3\text{H}/{}^3\text{He}$.
3. Estimate the medium effects from the model (calculations)..
4. Calculate the σ_n/σ_p from the data ratio using the medium effects.
5. Extract the born cross section, after correcting for the TPE.
6. Extract the form factor:

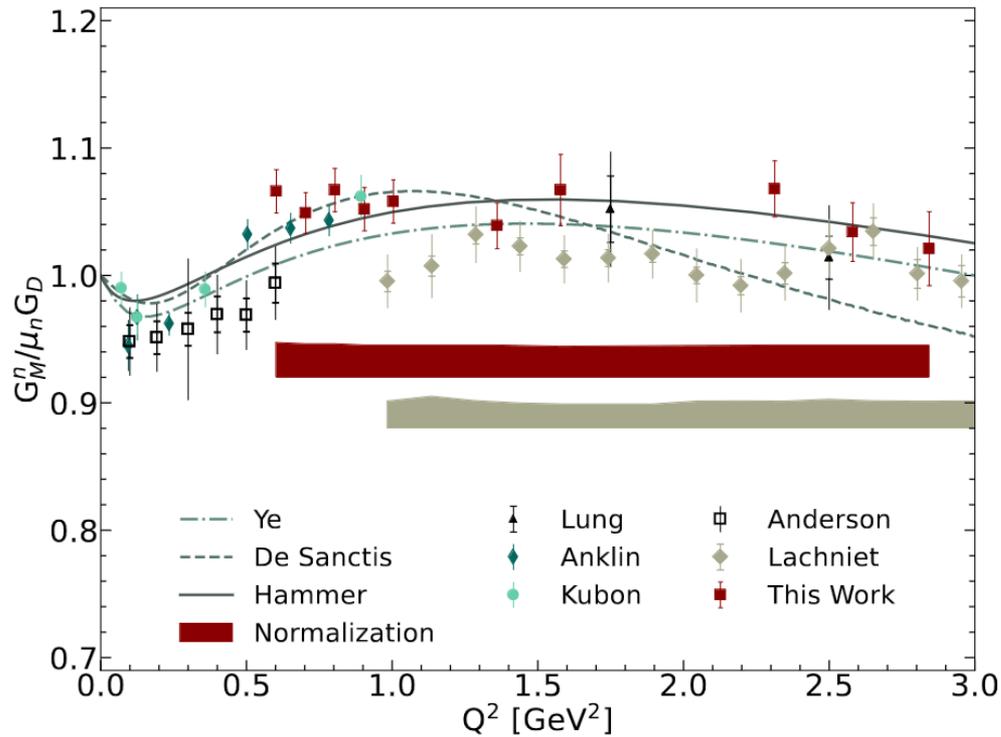
$$G_M^n = \left(\left[\sigma_n^{Born} - \frac{\epsilon}{\tau} (G_E^n)^2 \right] \right)^{1/2}$$

Subtract G_E^n contribution to get G_M^n from Z. Ye, J. Arrington, R. J. Hill, and G. Lee, Physics Letters B 777, 8 (2018).

Leading systematic contributions

Source	Normalization %	Point-to-Point for the Cross-sections %
Background Contamination (endcaps)	0.1	0.15 (QE)
Target Thickness	1.08	0
Charge	0	0.1
³ He contamination	0	0.35
Model Dependence	0.2	0.5
Radiative corrections	0.3	0.4
cut dependence/shape imperfections	0.3	0.3
MEC subtraction	L(0.4) and R(0.2)	L(0.3) and R(0.2)
FSI	0.3	0.2
SF vs nk estimate	0.2	0.2

This work



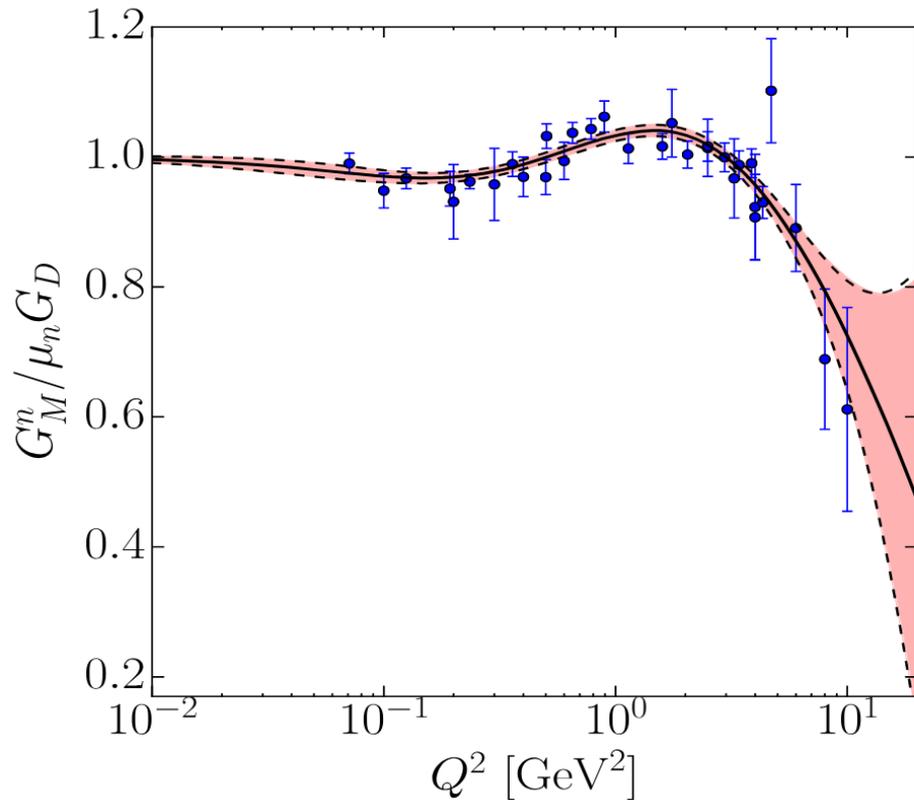
Some experiments did not separate out scale uncertainties from point-to-point systematics

Tritium results cover Q^2 range of multiple experiments – useful in constraining relative normalizations

Are the data consistent when accounting for scale uncertainties?

Our new results along with a subset of previous measurement

[Phys.Rev.Lett. 132 \(2024\) 16, 162501](#)



$$G(Q^2) = \sum_{k=0}^{k_{\max}} a_k z^k, \quad z = \frac{\sqrt{t_{\text{cut}} + Q^2} - \sqrt{t_{\text{cut}} - t_0}}{\sqrt{t_{\text{cut}} + Q^2} + \sqrt{t_{\text{cut}} - t_0}}$$

$$t_{\text{cut}} = 4m_{\pi}^2$$

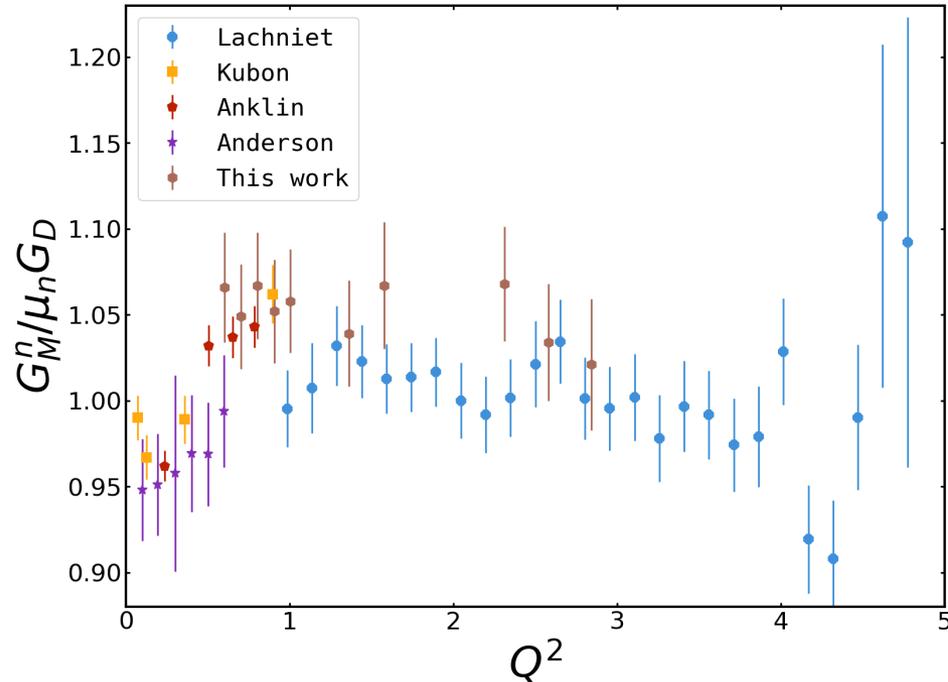
$$t_0 = -0.7 \text{ GeV}^2$$

Some additional steps

- Z. Ye *et al.* performed global fit. For GMn, increased uncertainties on data sets in region where results were inconsistent – all experiments given reduced weight
- Updating the global fit from this work using the exact same fit approach, but given more detailed estimate of scale uncertainty for each experiment (and reduced point-to-point uncertainties when something already included shifted to scale)
- Addl. Uncertainties associated with impact of TPE on previous measurements.

Global fit analysis

Examine each experimental paper individually:



- Add additional sources of uncertainties: e.g. TPE (not included in original work).

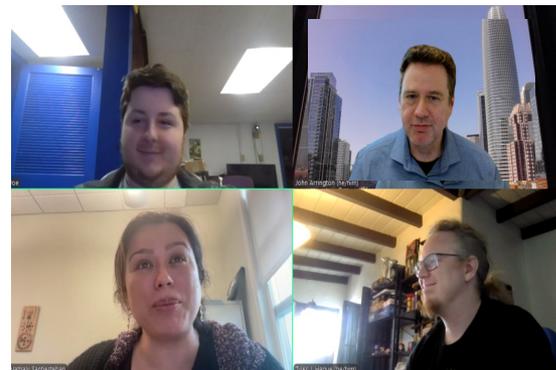
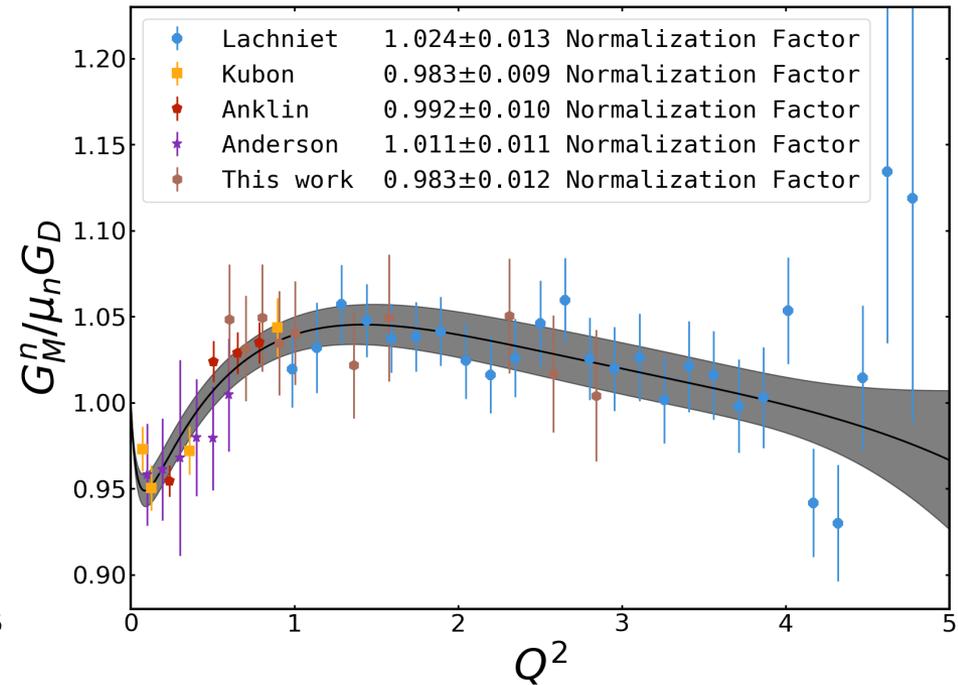
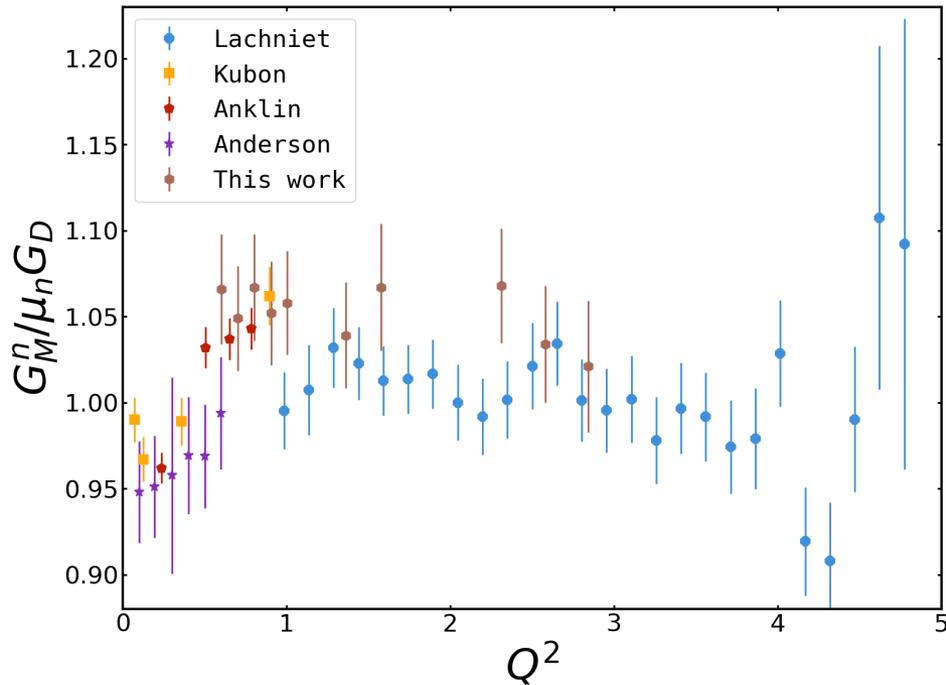
- In a few cases, enhance uncertainties (typically RC and proton FF uncertainty for older experiments).

- Identify highly-correlated uncertainties (neutron efficiency, nuclear models); add scale uncertainty and remove some/all of this uncorrelated uncertainty.

- 1-2% scale uncertainties for most experiments; larger for Rock, Lung (inclusive from proton and deuteron).

Courtesy of J. Jane (UNH) and T. Hague (LBNL)

Global fit analysis

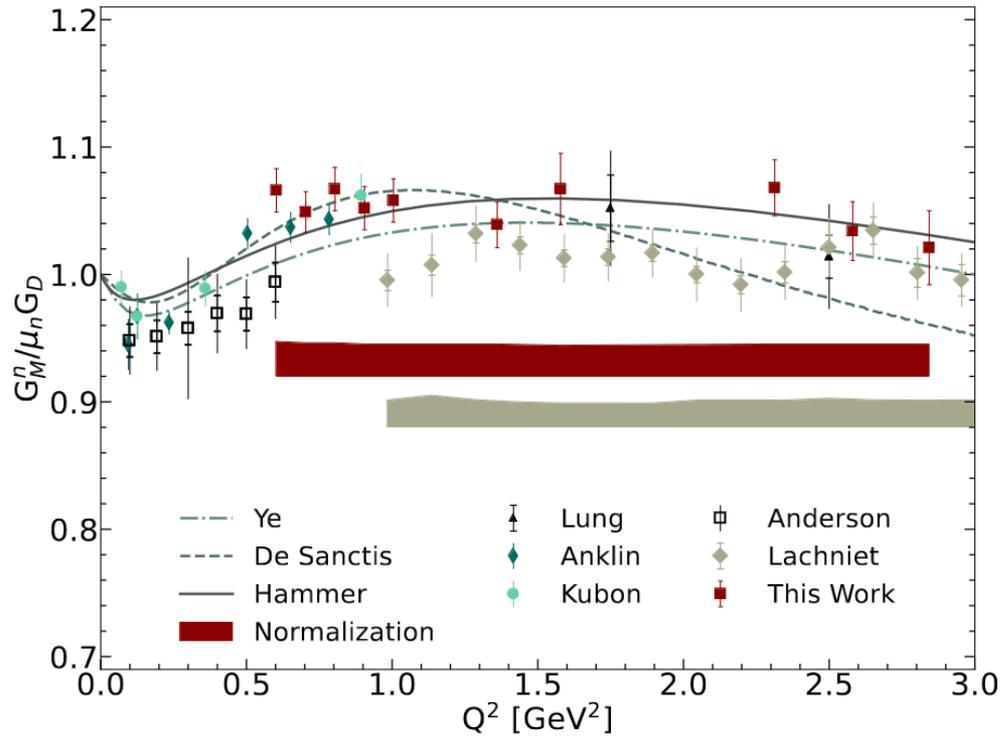


Global data in agreement...

Work in progress

Courtesy of J. Jane (UNH) and T. Hague (LBNL)

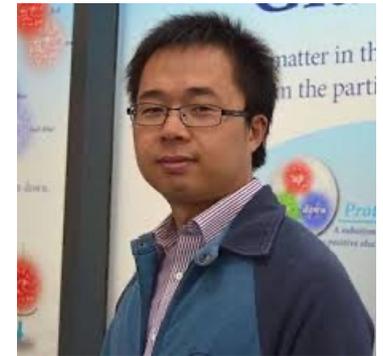
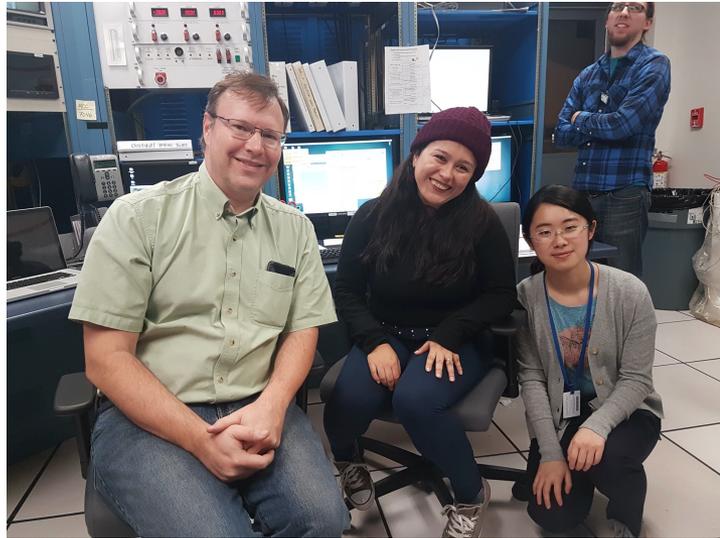
Summary



A deep study of the uncertainties could lead to reach consistency in the world's data.

This data help tie together normalizations of different data sets due to overlapping multiple measurements

Our new results along with a subset of previous measurement



Thank you!



Acknowledgment to everyone
who worked on the experiment