

FIRST INTERNATIONAL SCHOOL OF HADRON FEMTOGRAPHY

Jefferson Lab | September 16 - 25, 2024

Experimental Methods Sep 21st 2024

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with Charles Hyde

Diffraction and Imaging

Huygens-Kirchhoff-Fresnel principle



$$\vec{q} = \vec{k} - \vec{k'}$$

The interference pattern is given by the superposition of spherical wavelets

$$f(\Omega_{\vec{q}}) = \int \frac{\mathsf{d}^3 \vec{r}}{(2\pi)^3} F(\vec{r}) \mathsf{e}^{i \vec{q} \cdot \vec{r}}$$

Fourier imaging



Elastic scattering

Form Factors

Probing deeper using virtual photons







Hofstadter Nobel prize 1961

"The best fit in this figure indicates an rms radius close to $0.74\pm0.24\times10^{-13}$ cm."

Imaging in transverse impact parameter space



1-D distribution in longitudinal momentum space

Deep Exclusive Scattering

Generalized Parton Distributions



$$\begin{split} \gamma^* p &\to \gamma p', \ \gamma^* p \to \begin{cases} \rho p' \\ \omega p' \\ \phi p' \\ \phi p' \\ \end{bmatrix} \\ & \text{Bjorken regime :} \\ Q^2 \to \infty, \ x_B \text{ fixed} \\ t \text{ fixed } \ll Q^2, \ \xi \to \frac{x_B}{2 - x_B} \\ \end{cases} \\ \\ \frac{p^+}{2\pi} \int dy^- e^{igp^+ y^-} \langle p' | \bar{\psi}_q(0) \gamma^+(1 + \gamma^5) \psi(y) | p \rangle \\ &= \bar{N}(p') \left[H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) i \sigma^{+\nu} \frac{\Delta_{\nu}}{2M} \\ &+ \bar{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \bar{E}^q(x, \xi, t) \gamma^5 \frac{\Delta^+}{2M} \right] \\ &\text{spin} \qquad \boxed{\text{N no flip} \text{ N flip}} \end{split}$$

spin	N no flip	N flip
q no flip	Н	Е
q flip	Ĥ	Ê

N(p)

3-D Imaging conjointly in transverse impact parameter and longitudinal momentum

GPDs and Transverse Imaging

 (x_B, t) correlations

$$q_{\chi}(x,\vec{b}_{\perp}) = \int \frac{d^{2}\vec{\Delta}_{\perp}}{(2\pi)^{2}} \left[H(x,0,t) - \frac{E(x,0,t)}{2M} \frac{\partial}{\partial b_{y}} \right] e^{-i\vec{\Delta}_{\perp} \cdot \vec{b}_{\perp}}$$

M. Burkardt, Int. J. Mod. Phys. A 18 173 (2003)

QCDSF coll. PRL98 222001 (2007)



Lattice calculation



Energy Momentum Tensor

Gravitational Form Factors definition :

 $\langle p' | \hat{T}^{q}_{\mu\nu} | p \rangle = \bar{N}(p') \left[\frac{M_{2}^{q}(t)}{M} + J^{q}(t) \frac{v(P_{\mu}\sigma_{\nu\rho} + P_{\nu}\sigma_{\mu\rho})\Delta^{\rho}}{2M} + d_{1}^{q}(t) \frac{\Delta_{\mu}\Delta_{\nu} - g_{\mu\nu}\Delta^{2}}{5M} \right] N(p)$

Confinement forces from space-space components of EMT The graviton with spin 2 couples directly to EMT But gravity is too weak to produce count rates in the detector

We can construct a spin 2 operator using two spin 1 operators \rightarrow use a process with two photons to measure the EMT? X. Ji *PRL***78** 610 (1997); M. Polyakov *PLB***555** 57 (2003)



GPDs and Energy Momentum Tensor

(x,ξ) correlations

Form Factors accessed via second x-moments :

$$\langle p' | \hat{T}^{q}_{\mu\nu} | p \rangle = \bar{N}(p') \left[\frac{M_{2}^{q}(t)}{M} \frac{P_{\mu}P_{\nu}}{M} + J^{q}(t) \frac{i(P_{\mu}\sigma_{\nu\rho}+P_{\nu}\sigma_{\mu\rho})\Delta^{\rho}}{2M} + d_{1}^{q}(t) \frac{\Delta_{\mu}\Delta_{\nu}-g_{\mu\nu}\Delta^{2}}{5M} \right] N(p)$$

Angular momentum distribution

Deeply Virtual Compton Scattering

The cleanest GPD probe at low and medium energies



CLAS in Hall-B



Solenoid and Inner Calorimeter



CLAS proton Beam Spin Asymmetry





Finite Bin Size Corrections



Finite Bin Size Corrections



Finite Bin Size Corrections





Bin volume Average value (observable) in bin Bin center Bin average

$$V = \int_{\text{bin}} dx$$

 $< y >= y_a = \frac{1}{V} \int_{\text{bin}} y(x) dx$
 $x_c = \frac{1}{V} \int_{\text{bin}} x dx$
 $< x >= x_a = \frac{1}{Vy_a} \int_{\text{bin}} xy(x) dx$

CLAS proton cross-section





Radiative corrections (semiclassical)



Peskin & Schroeder chapter 6 (Introduction)

DVCS Radiative Corrections Fast MC



M. Vanderhaeghen *et al.*, Phys. Rev **C62** (2000) 025510 I. Akushevich & A. Ilyichev Phys. Rev **D98** (2018) 013005

Global Fits to extract the D-term



Beam Spin Asymmetries

$$Im \mathcal{H}(\xi, t) = \frac{N}{1+x} \left(\frac{2\xi}{1+\xi}\right)^{-\alpha_R(t)} \left(\frac{1-\xi}{1+\xi}\right)^b \left(\frac{1-\xi}{1+\xi}\frac{t}{M^2}\right)^{-1}$$

Unpolarized cross-sections Use dispersion relation:

$$\operatorname{Re}\mathcal{H}(\xi,t) = \Delta + \mathcal{P}\int \mathrm{d}x \left(\frac{1}{\xi-x} - \frac{1}{\xi+x}\right)\operatorname{Im}\mathcal{H}(\xi,t)$$

pure Bethe-Heitler local fit + uncertainty range resulting global fit

DVCS Dispersion: subtraction constant results



$$\operatorname{Im}\mathcal{H}(\xi,t) = \frac{N}{1+x} \left(\frac{2\xi}{1+\xi}\right)^{-\alpha_R(t)} \left(\frac{1-\xi}{1+\xi}\right)^b \left(\frac{1-\xi}{1+\xi}\frac{t}{M^2}\right)^{-1}$$

 α_R is fixed from small-x Regge phenomenology b is a free parameter for the large x behavior p is fixed to 1 for the valence M is a free parameter controlling the t dependence

$$\Delta(t) = \Delta(0) \left(1 - \frac{t}{M^2}\right)^{-\alpha} = 2 \int_{-1}^1 dz \frac{D(z,t)}{1-z}$$

$$D(z,t) = (1-z^2) \sum_{k=1}^{\infty} \left[e_u^2 \ d_{2k-1}^u(t) + e_d^2 \ d_{2k-1}^d(t) \right] \ C_{2k-1}^{3/2}(z)$$

Hereafter assume $d^u_{2k-1} \approx d^d_{2k-1}$

Separation of the GFF d_1



$$H(x, \xi, t) = \dots + \theta \left[1 - \frac{x^2}{\xi^2} \right] D(\frac{x}{\xi}, t)$$

$$D(z, t) = \left(1 - z^2 \right) \left[d_1(t) C_1^{3/2}(z) + d_3(t) C_3^{3/2}(z) + \dots \right]$$

$$C_1^{3/2}(z) = 3z$$

$$C_3^{3/2}(z) = \frac{5}{2} \left(7z^3 - 3z \right)$$

$$C_5^{3/2}(z) = \frac{21}{8} \left(33z^5 - 30z^3 + 5z \right)$$

To separate orthogonal Gegenbauer polynomials: requires measurement of (x, ξ) dependence (or at least $z = x/\xi$ dependence) different reaction such as DDVCS, will require higher luminosity

For now, to make progress it is necessary to make assumptions Use guidance from models such as χ QSM or lattice results Also implement constraints from theory into phenomenological fits

Separation of the GFF d_1

$$D^{q}(rac{x}{\xi},t) = \left(1 - rac{x^{2}}{\xi^{2}}
ight) \left[d_{1}^{q}(t)C_{1}^{3/2}(rac{x}{\xi}) + d_{3}^{q}(t)C_{3}^{3/2}(rac{x}{\xi}) + \cdots
ight]$$



t-dependence of the D-term :

Dipole gives singular pressure at r = 0Power law implied by counting rules? Exponential?

 $d_1(0) < 0$ dynamical stability of bound state $d_1(0) = -2.04 \pm 0.14 \pm 0.33$ First Measurement of new fundamental quantity

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D-term comparison with theory



Dispersion Relation Analysis Chiral quark soliton model Lattice results LHPC Global fit

M. V. Polyakov, P. Schweitzer Int.J.Mod.Phys. A33 (2018)

em:	$\partial_\mu J^\mu_{ m em}~=0$	$\langle N' J^{\mu}_{\mathbf{em}} N \rangle$	$\rightarrow Q =$	$1.602176487(40) \times 10^{-19}$ C
			$\mu =$	$2.792847356(23)\mu_N$
weak:	PCAC	$\langle N' J^{\mu}_{\rm weak} N\rangle$	$\rightarrow g_A =$	1.2694(28)
		Weak	$g_p =$	8.06(55)
gravity:	$\partial_{\mu}T^{\mu\nu}_{\mathbf{grav}} = 0$	$\langle N' T^{\mu\nu}_{\mathbf{grav}} N \rangle$	$\rightarrow m =$	$938.272013(23){ m MeV}/c^2$
			J =	$\frac{1}{2}$
			D =	?

Proton Pressure distribution results



Positive pressure in the core (repulsive force) Negative pressure at the periphery: pion cloud Pressure node around $r \approx 0.6$ fm

Stability condition :
$$\int_{0}^{\infty} dt r^2 p(r) = 0$$

Rooted into Chiral Symmetry Breaking

World data fit CLAS 6 GeV data Projected CLAS12 data E12-16-010B



DVCS with CLAS12 E12-16-010B

Experimental Configuration





Deep Process Kinematics at 6.6, 8.8, and 11 GeV

- ▶ $\mathcal{L} = 1 \times 10^{35} \text{ cm}^{-2} \text{s}^{-1}$
- Inclusive electron trigger (all calibration reactions will be analyzed in parallel)
- Electrons in the forward detector
- Protons in the central detector and forward detector
- Photons in the forward detector and forward tagger

DVCS with CLAS12 E12-16-010B

DVCS Projected Cross Section at 11GeV & 8.8GeV



DVCS with CLAS12 E12-16-010B



- Left : cross-sections at fixed kinematics for beam energies
 6.6 GeV and 8.8 GeV
- Right : corresponding Beam Spin Asymmetries
- Green : pure Bethe-Heitler

360

- Red : model fit on 6 GeV data
- Blue : simultaneous fit of the projected data
- Separation of : $\mathcal{I} \sim 1/y^3$ and $\left|\mathcal{T}^{\text{DVCS}}\right|^2 \sim 1/y^2$









Projection for the Nucleon transverse profile



Precision tomography in the valence region

Femtography simulations E12-16-010



Femtography simulations E12-16-010





High statistics CLAS12 simulations: sample of extracted Im and Re parts of CFF vs -t

Extraction of the D-term, and partonic pressure from amplitude dispersion global analysis



DVCS with a Polarized Positron beam

PEPPo production injecting 60 MeV 100 nA positron polarized at 60%

(PEPPo Collaboration) D. Abbott et al. , PRL116 (2016) 214801 ; L. Cardman et al. AIP CP 1970 (2018) 050001 Proposal 100 days (80+20) at $\mathcal{L}=0.6\times10^{35}~cm^{-2}s^{-1}$



Impact of the CLAS12 Positron data

Global analysis of CLAS12 program observables { $\sigma_{UU}, A_{LU}, A_{UL}, A_{UL}, A_{UU}^{C}, A_{LU}^{C}$ }

unpolarized beam charge asymmetry A_{UU}^{C} sensitive to the amplitude real part polarized beam charge asymmetry A_{UU}^{C} sensitive to the amplitude imaginary part



Improvement of the statistical and systematical uncertainties

Model independent separation of the Interference with BH and DVCS²

Science at the Luminosity Frontier: JLab at 22 GeV

First workshop January 23, 2023 to January 25, 2023



Second workshop

SCIENCE AT THE LUMINOSITY FRONTIER: JEFFERSON LAB AT 22 GE

LABORATORI NAZIONALI DI FRASCATI – INFN (ITALY) DECEMBER 9-13, 2024

CLAS12 at higher luminosities and energies

CLAS12 luminosity limited by accidental occupancy of DC R1.



Z. Meador, L. Elouadrhiri

DVCS with CLAS at 24 GeV



DVCS BSA with CLAS at 24 GeV



0.07 < x_B < 0.36

Summary - Outlook

- Dispersive analysis of the DVCS amplitude
- Access to the Gravitational Form Factors
- Global analysis with as few parameters as possible
- Questions about model dependance and systematic uncertainties
- Rosenbluth separation with several beam energies
- Direct access to the real part of the amplitude with a positron beam
- Future prospects: precision at the luminosity and energy frontiers

Next lecture: interplay between JLab and the future Electron Ion Collider



