

# Electromagnetic structure of light nuclei up to $Q^2 \sim 1 \text{ GeV}^2$

Hall A/C Summer Collaboration Meeting  
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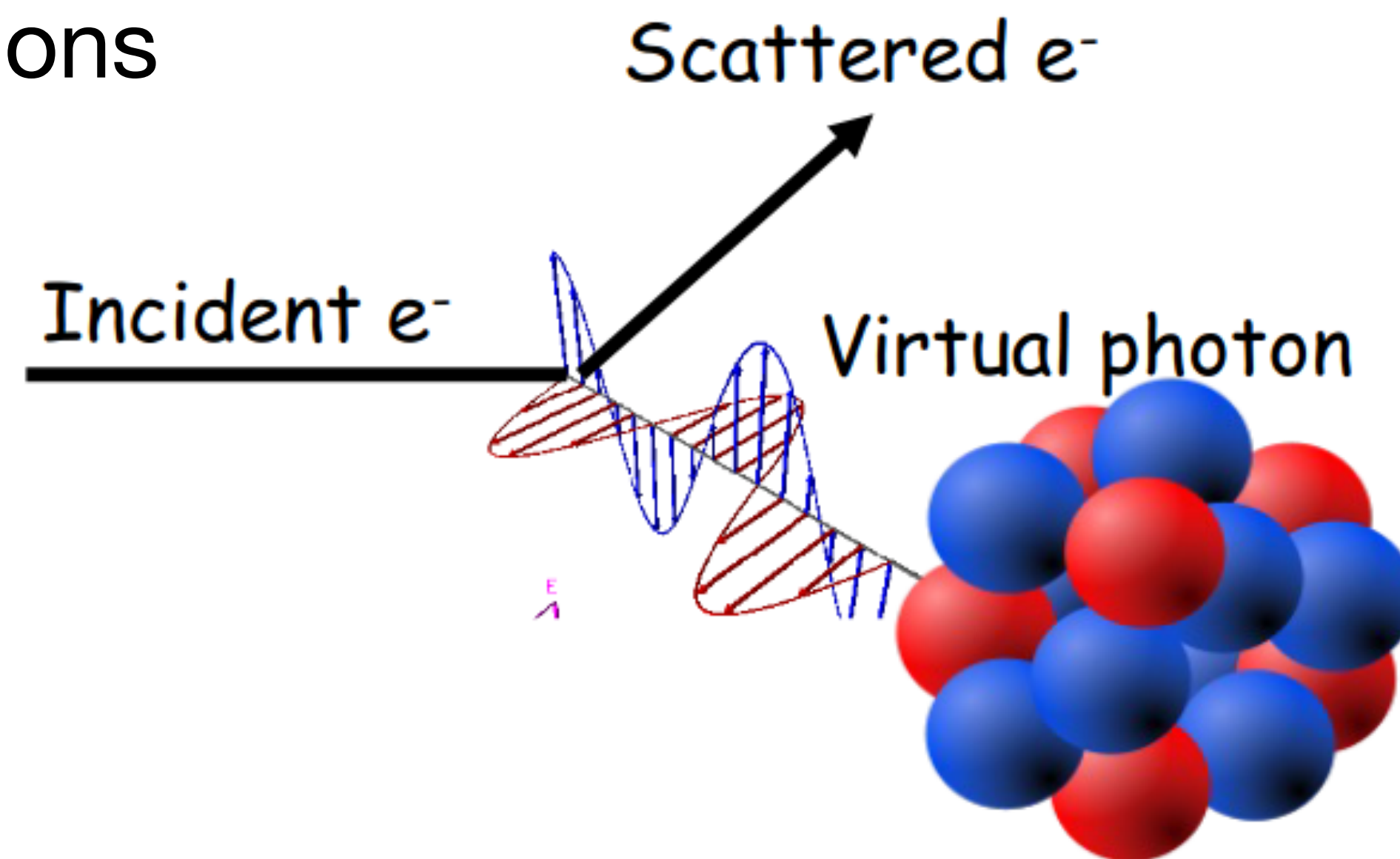
# Experimental motivation

## A low-energy prospective

Short Range Correlations  
(CaFe exp.,...)

SIDIS in nuclei  
(E12-06-014,...)

EMC effects  
(MARATHON,...)



Exclusive pion  
production

Neutrino physics  
(see L. Andreoli talk)

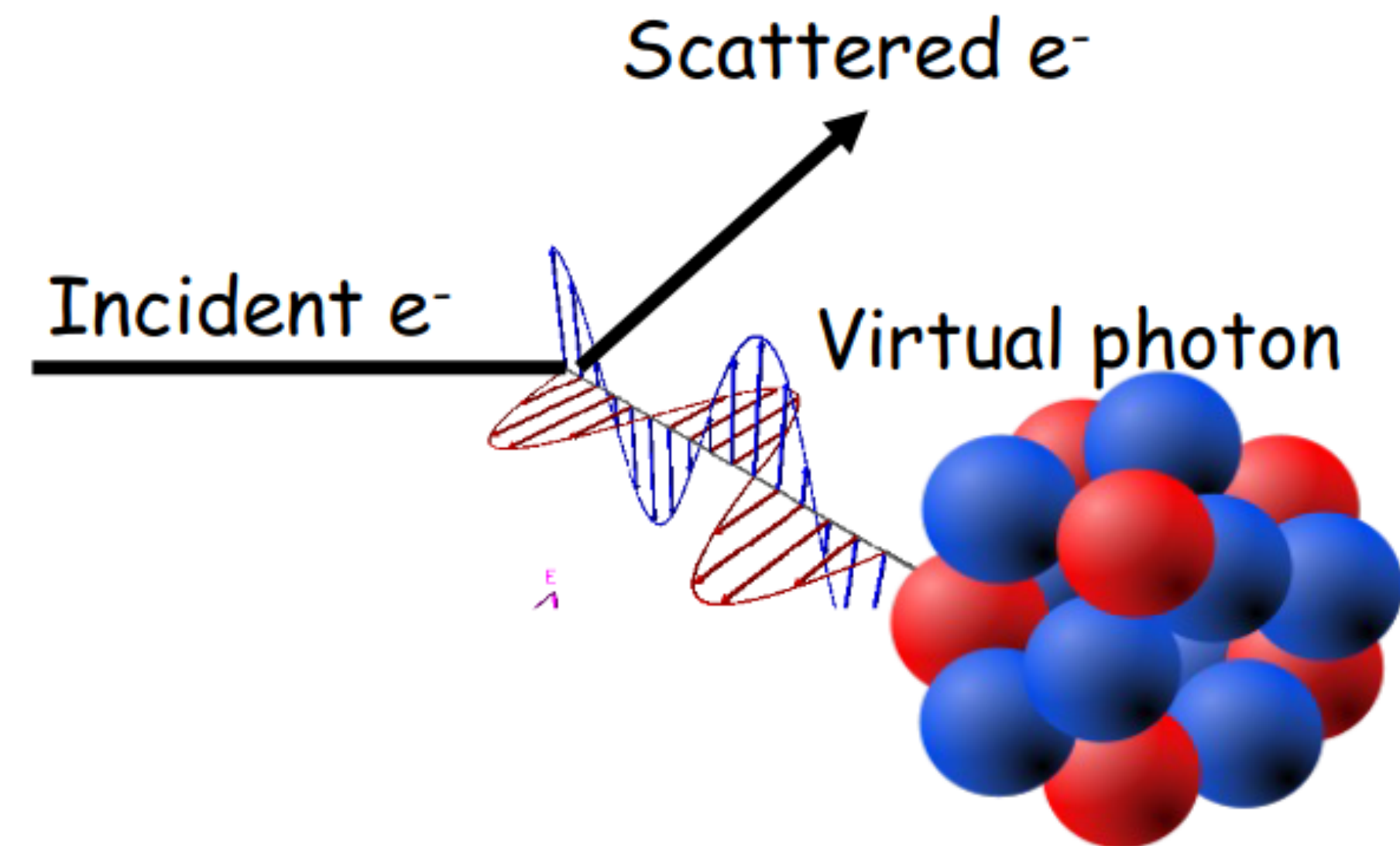
Hypernuclei

**Understanding and describing the nuclear correlations is crucial to disentangle the physics Hall A/C are looking for**

# Motivation of this talk

## The goal of the project

- Obtain nuclear currents reliable in a region of momentum transfer  $Q^2 \sim 0 - 3 \text{ GeV}^2$
- Perform calculation considering the full nuclear dynamics
- Introducing explicit emission of mesons (pions,...)
- Integrating the result with “medium” energy nuclear physics models (non perturbative region)



**In this talk:**

**test of the EM Currents on electrons elastic scattering**

**Magnetic form factors (MFF) using  $\chi$ EFT\***

# References

- Fit of the currents and test on few-body nuclei

[A.G. and R. Schiavilla, Phys. Rev. C 106, 044001 (2020)]

- Prediction of magnetic form factors of heavier systems

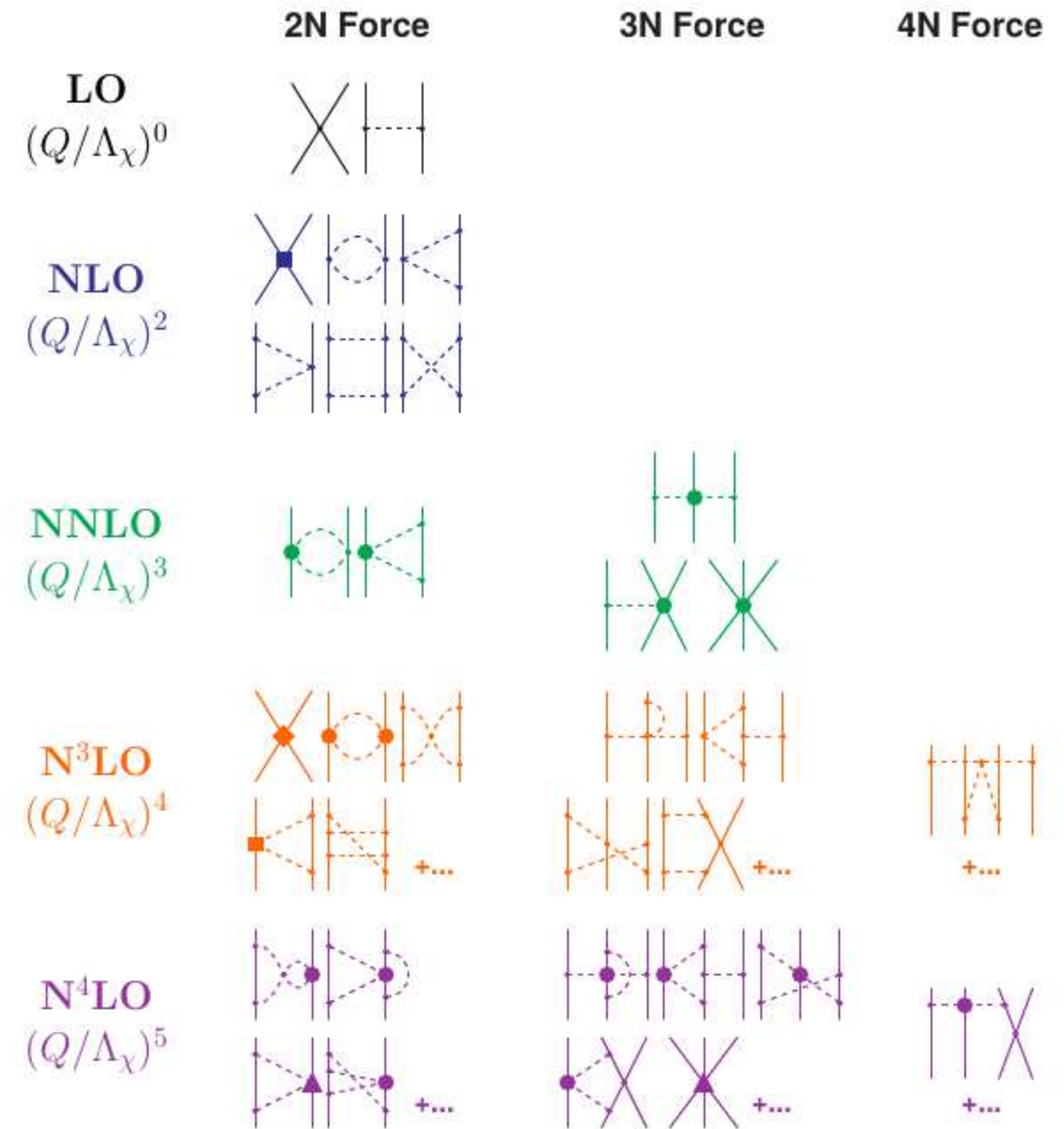
[[G. Chambers-Wall](#), A. G., [G. B. King](#), S. Pastore, M. Piarulli, R. Schiavilla, R. B. Wiringa, arXiv:2407.04744, arXiv:2407.03487]



# Chiral effective field theory

- Only Nucleons and Pions as degrees of freedom ( $M_{QCD} \sim 1 \text{ GeV}$ )
- Direct connection with QCD: **chiral symmetry** (+ discrete symmetries + Lorentz invariance)
- **Low Energy Constants (LECs)**: fitted on experimental data
- Organize the interaction as a power expansion  $Q/M_{QCD}$  (controlled errors)

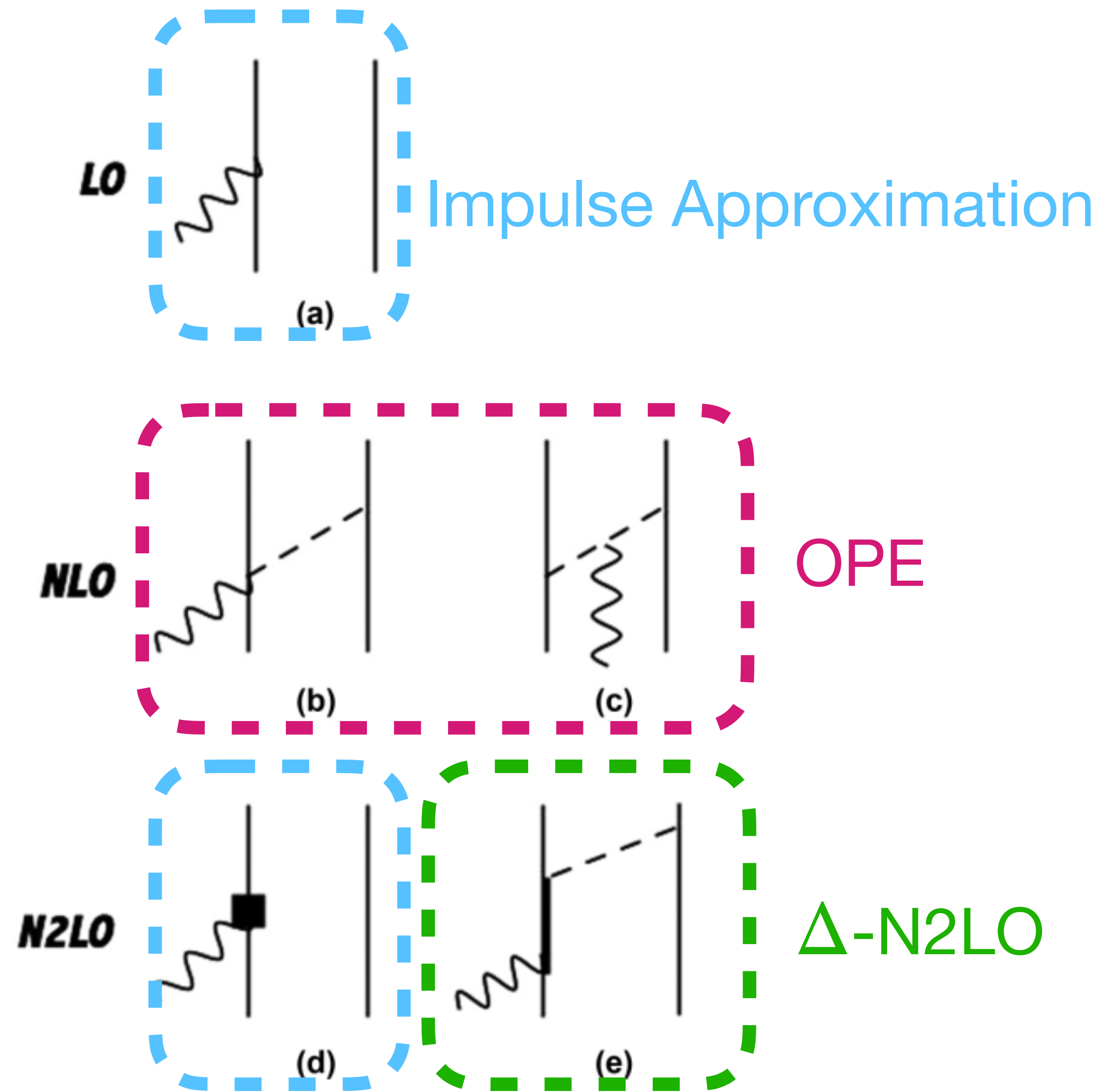
“Semi-phenomenological”  
 $\chi$ EFT approach to extend  
 theory to higher momenta



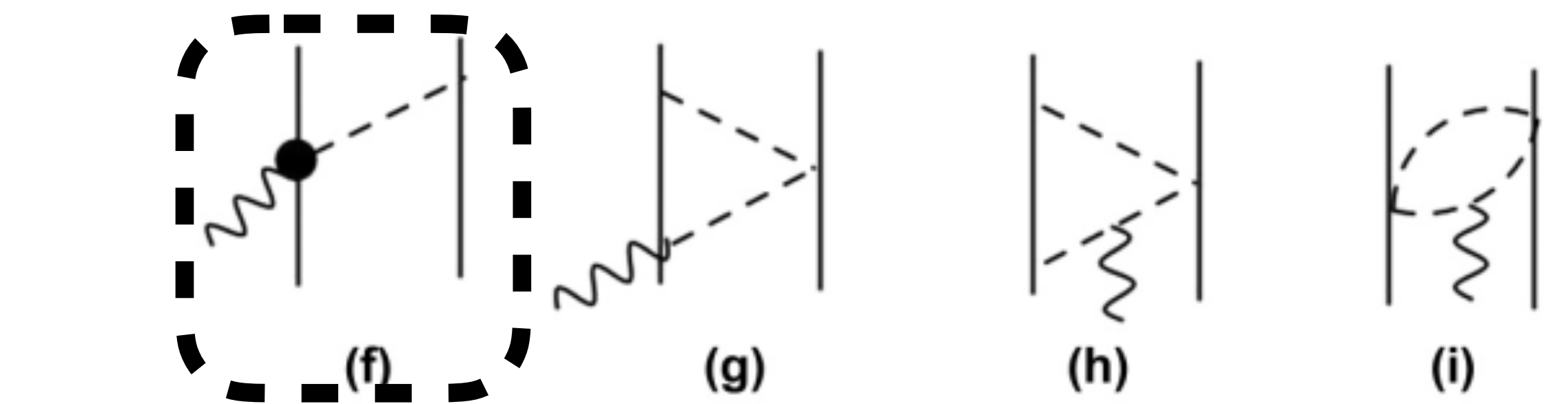
Phys. Rev. C **96**, 024004 (2017)

Phys. Rev. Lett. **115**, 122301 (2015)

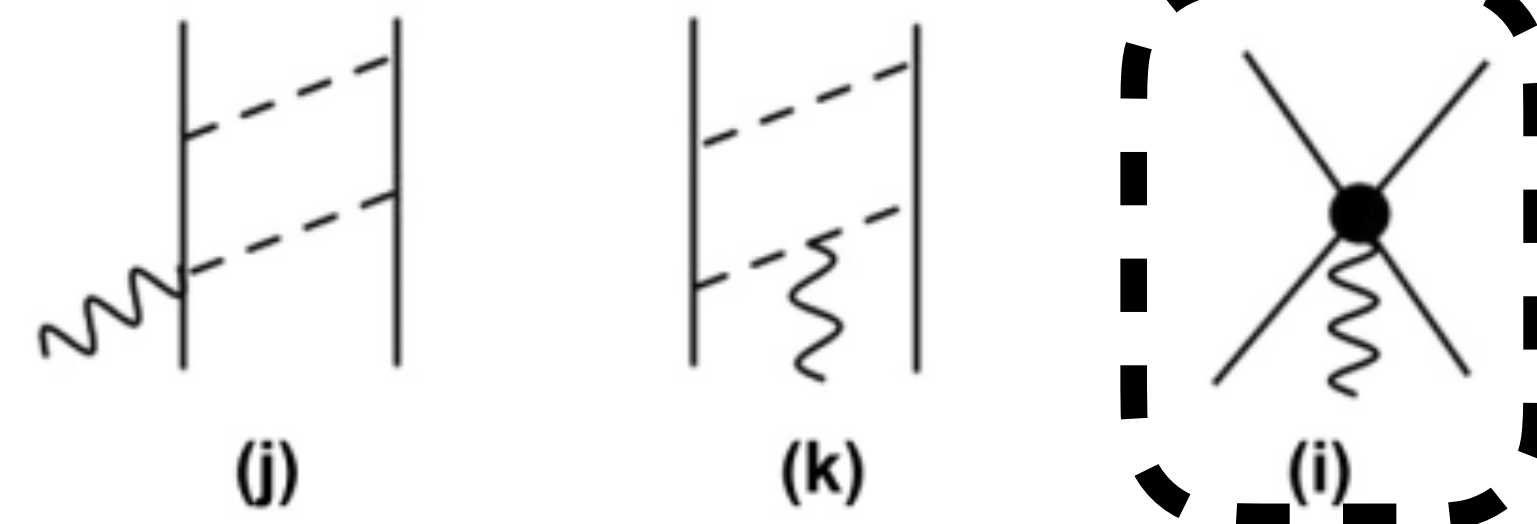
# The chiral currents



$d_2^V$   $d_3^V$   $d_2^S$  N3LO-OPE



N3LO



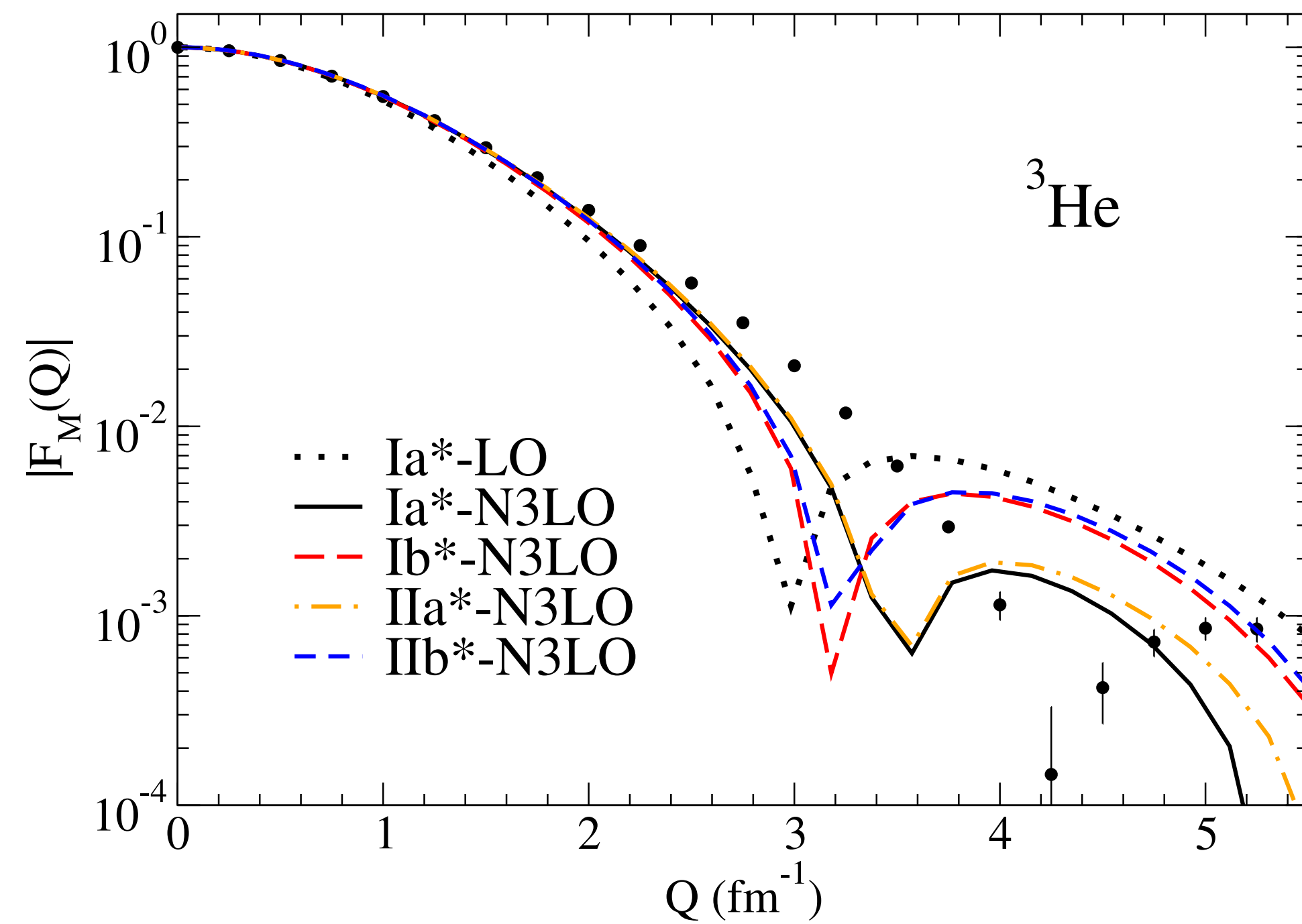
$d_1^V$   $d_1^S$  contact terms

Red: isoscalar Blue: isovector

# How to fix the LECs I

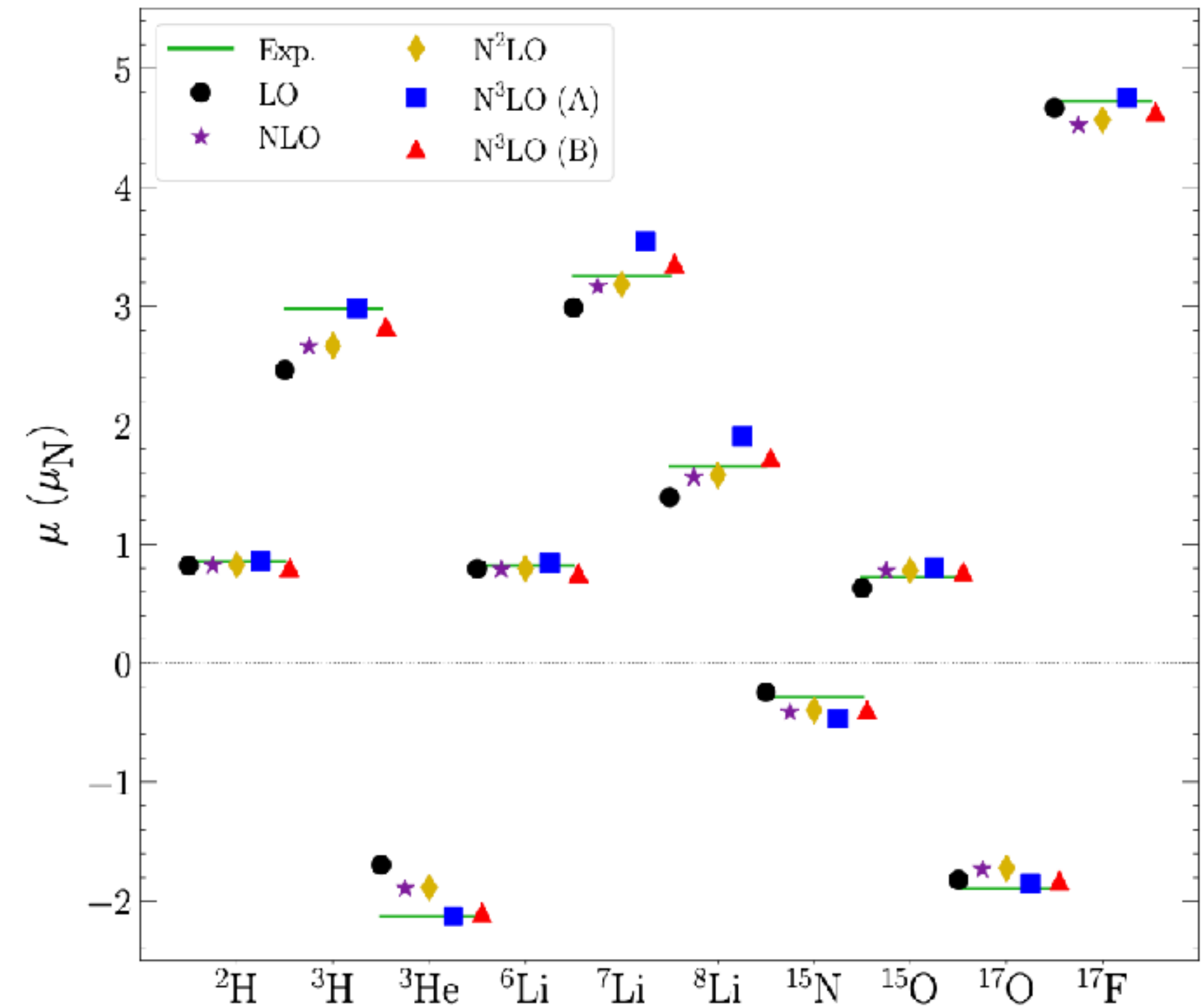
## Using the magnetic moments

$\Delta$  saturation (fix  $d_2^V$   $d_3^V$ )



[ R. Schiavilla et al., PRC 99, 034005 (2019)]

Not including ( $d_2^V$   $d_3^V$   $d_2^S$ )



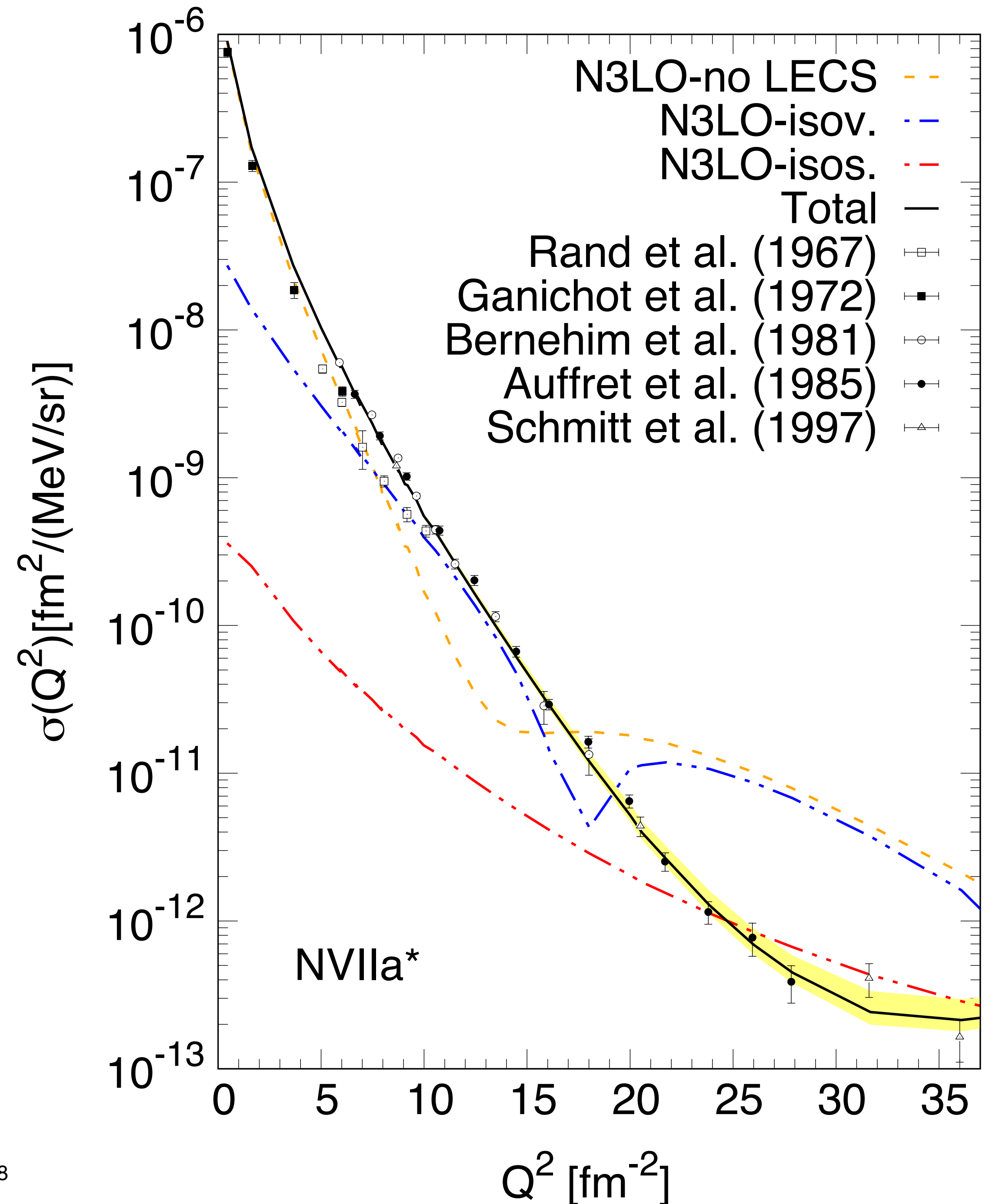
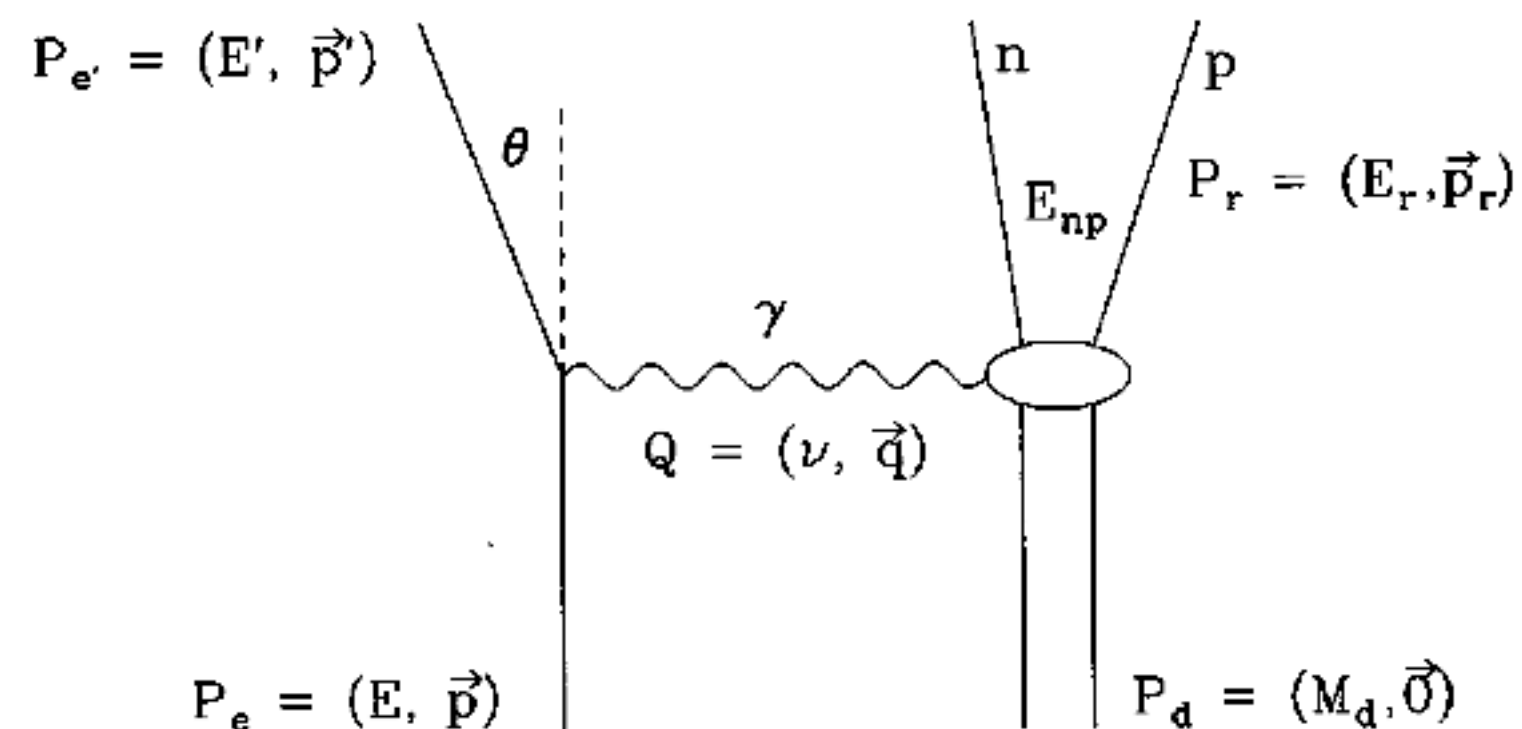
[ J.D. Martin et al., PRC 108, L031304 (2023)]

**Diffraction generated by tensor forces**

# How to fix the LECs II

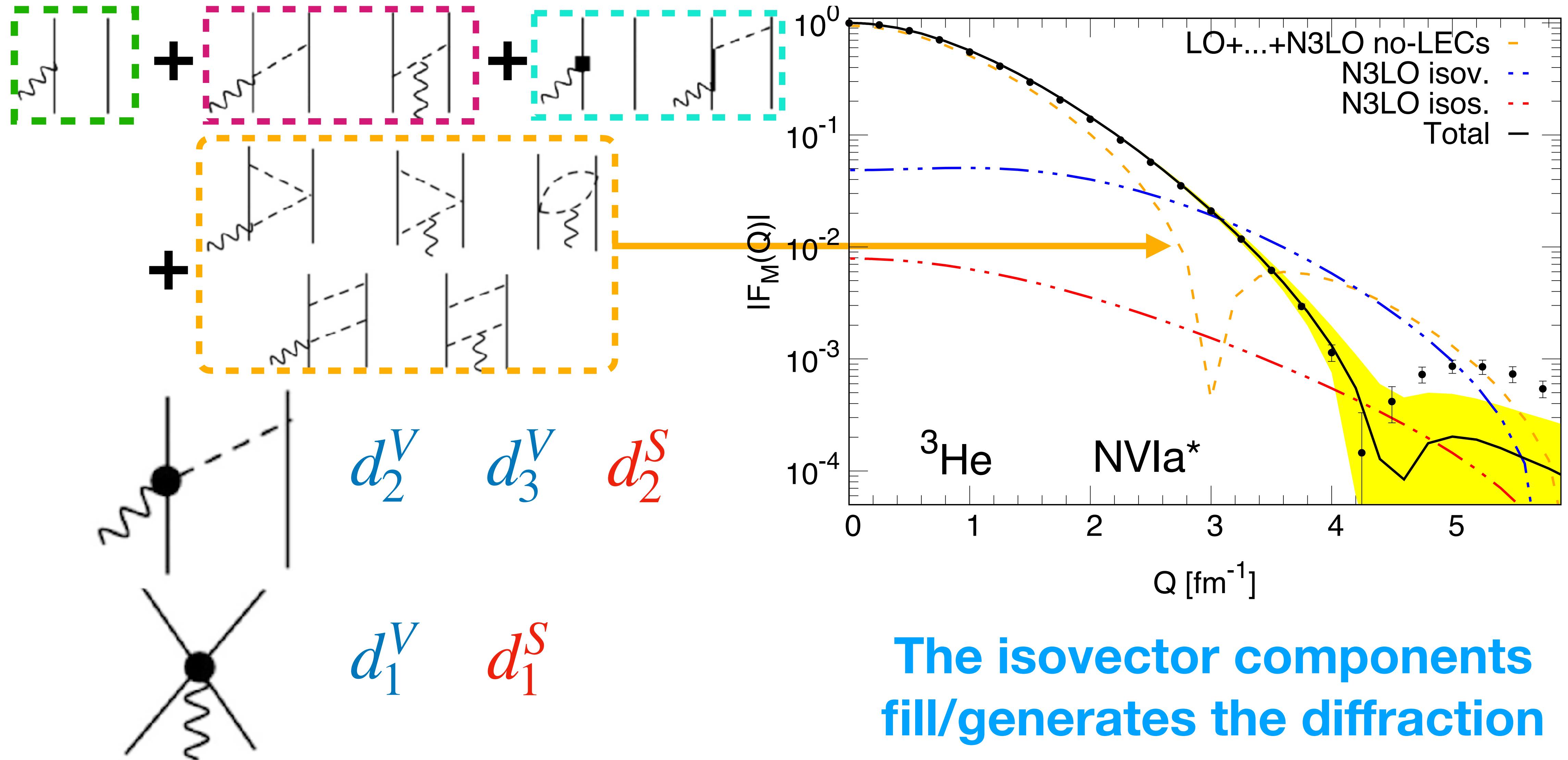
PRC 106, 04401 (2020)

- Magnetic moments of d,  $^3\text{He}$ ,  $^3\text{H}$  (fix normalization)
- Deuteron-threshold electrodisintegration at backward angles (fix dynamics)



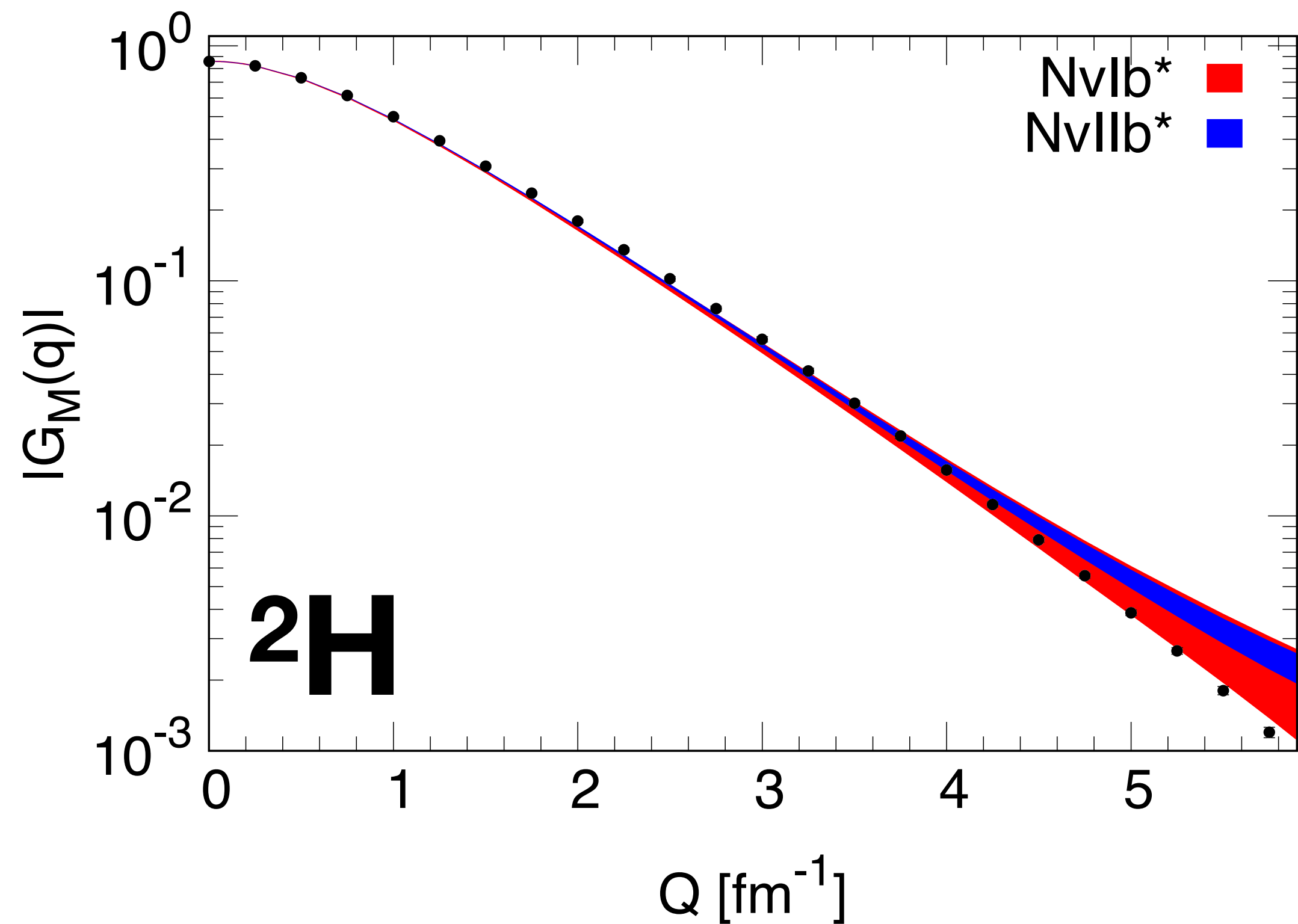


# Prediction of A=3 Magnetic Form Factor



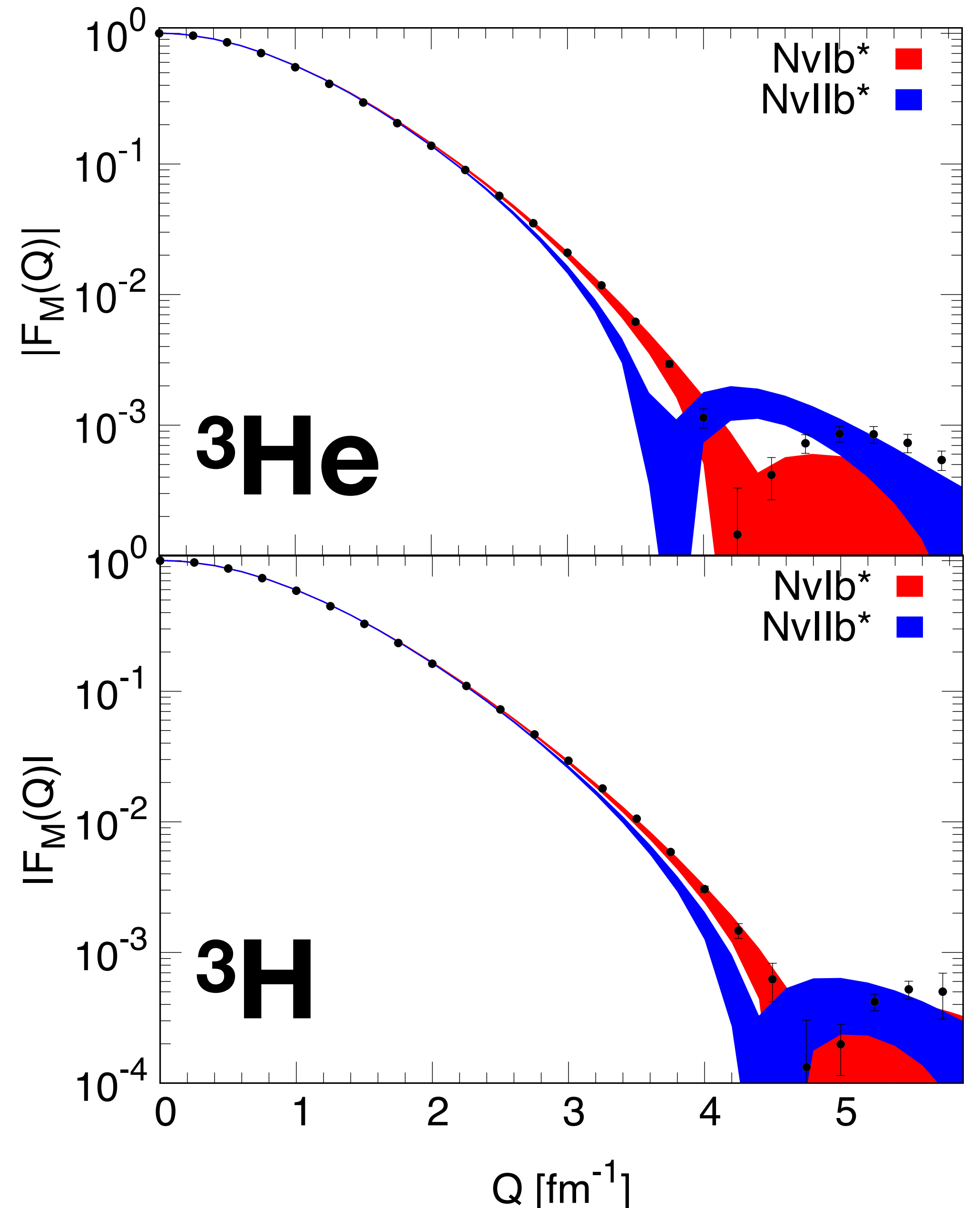
**The isovector components fill/generates the diffraction**

# Results for ${}^2\text{H}$ , ${}^3\text{H}$ , ${}^3\text{He}$



Norfolk interaction model

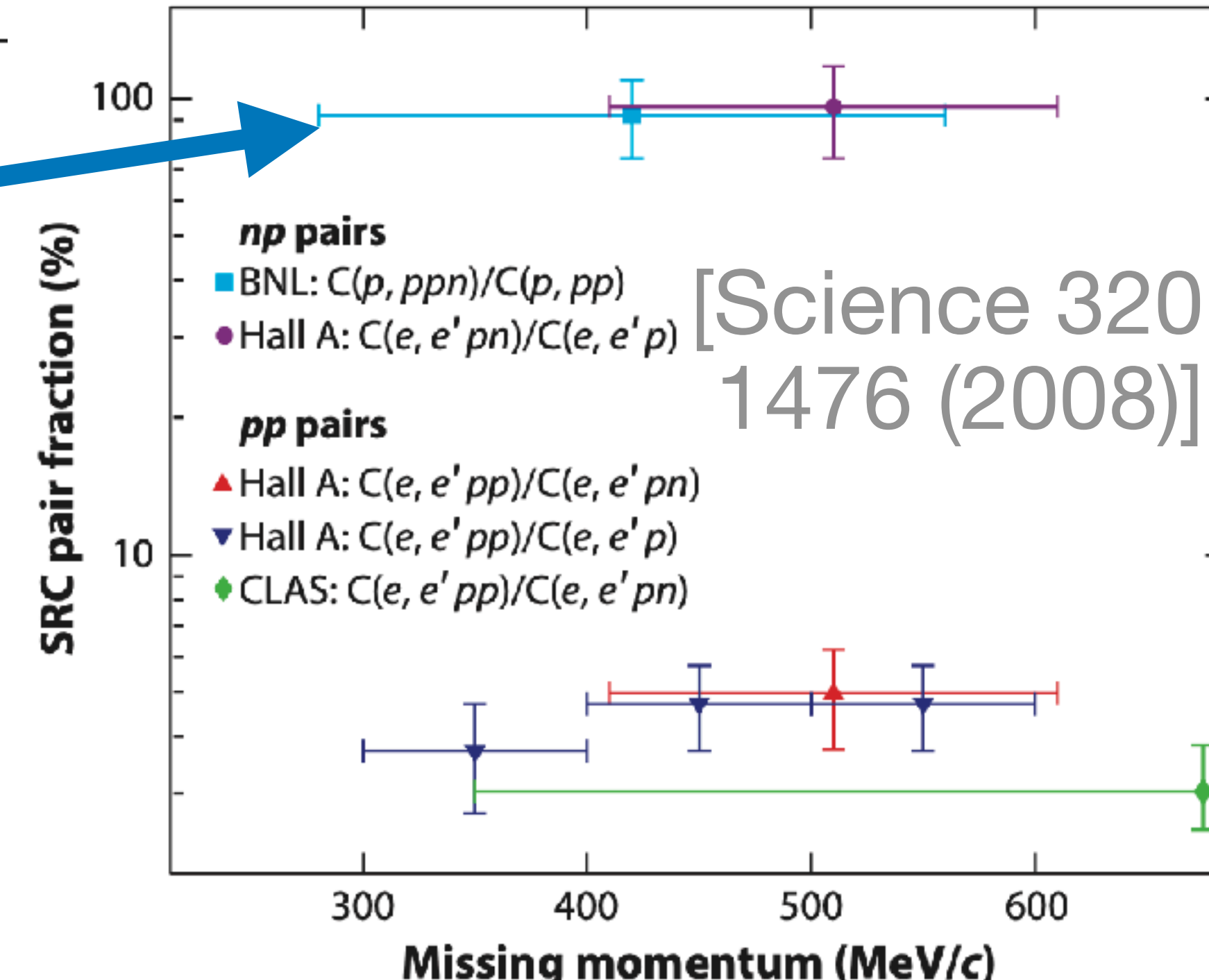
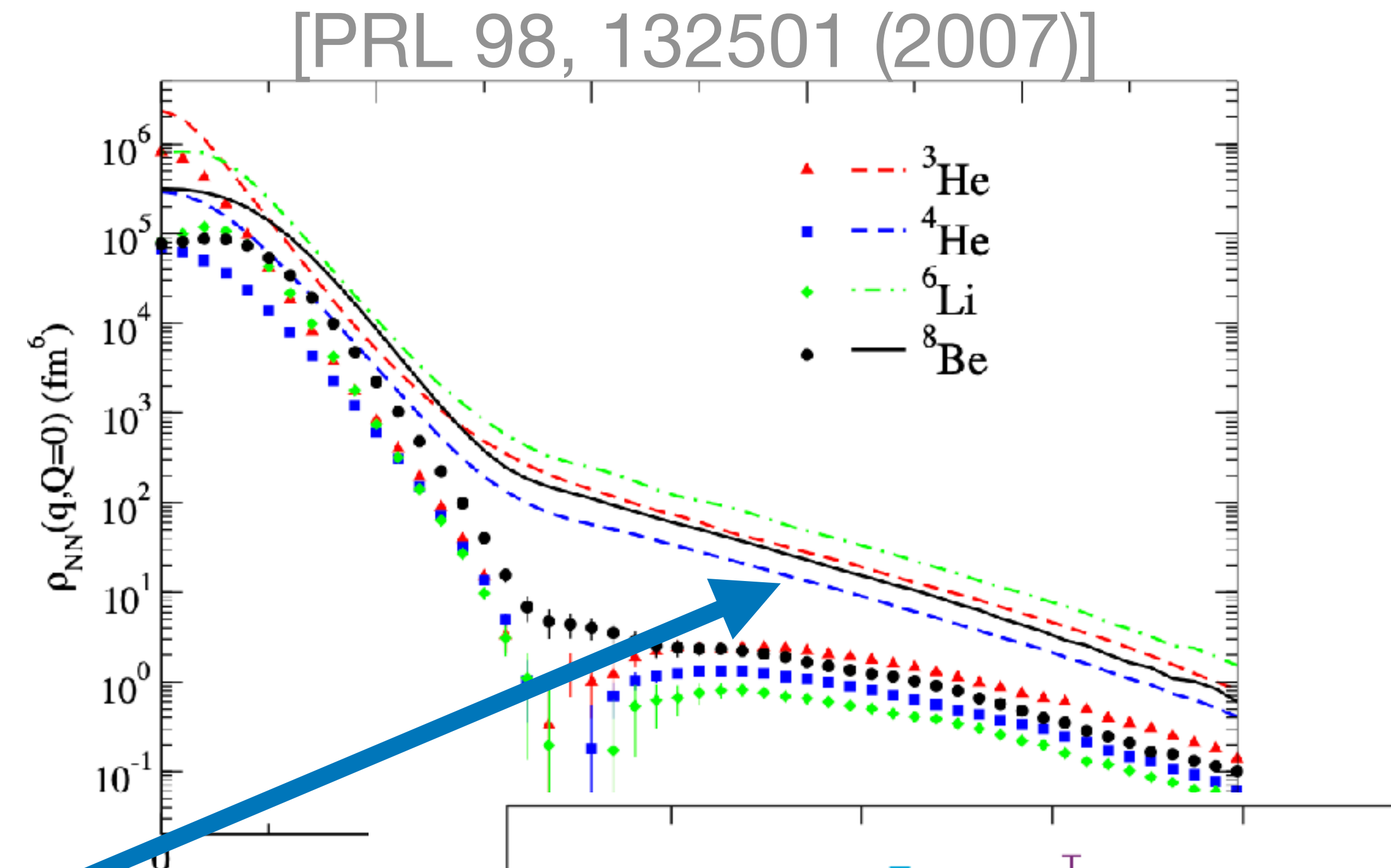
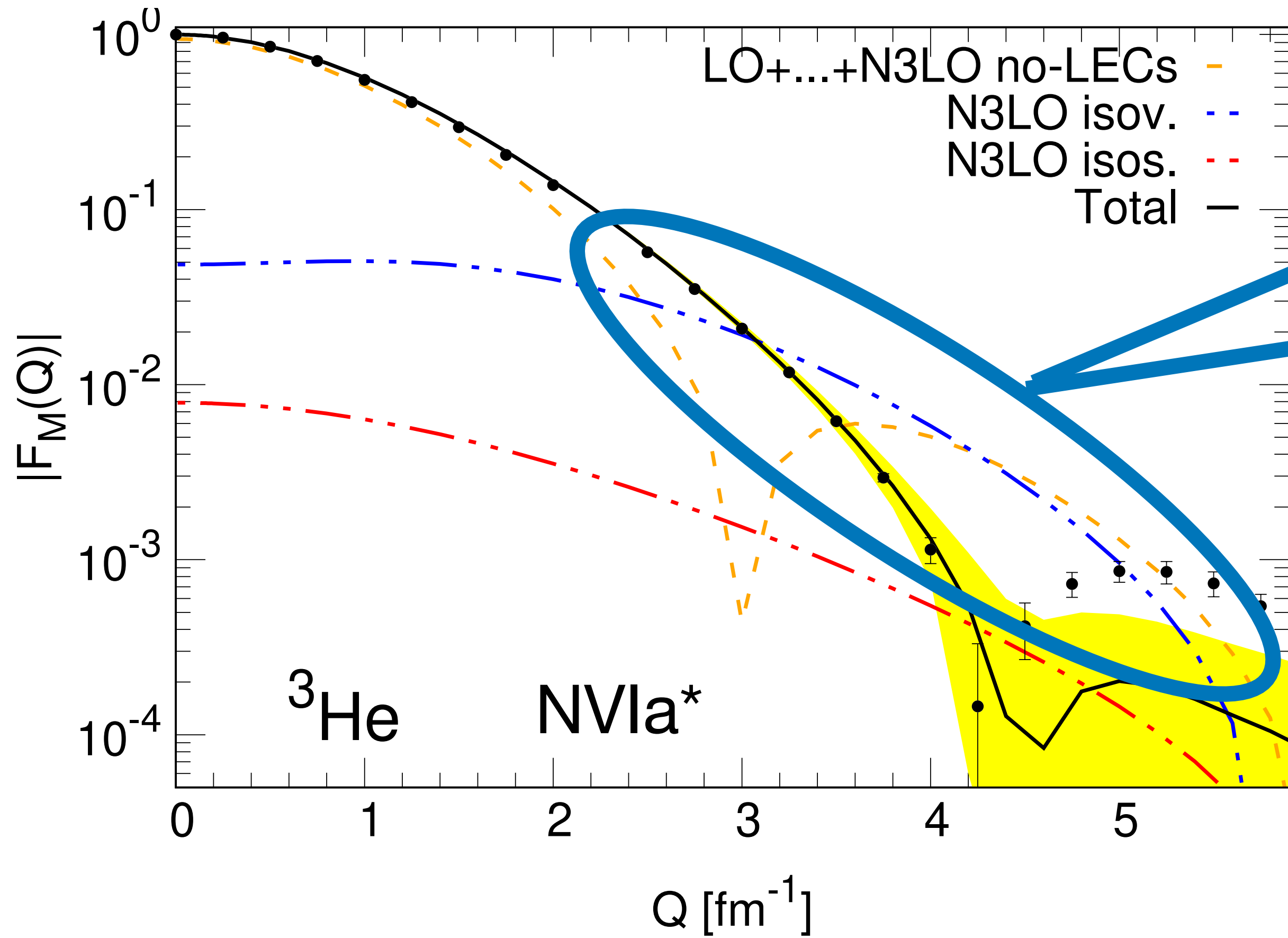
[M. Piarulli, et al., PRC 94, 054007 (2016)]



# Why does it work?

Isovector currents transform  
S/T=0/1 in S/T=1/0 pairs

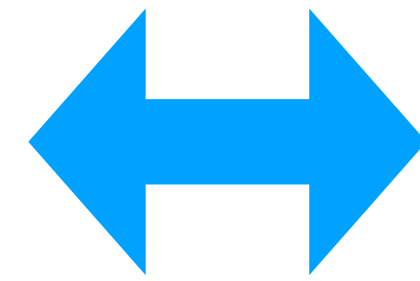
np dominance



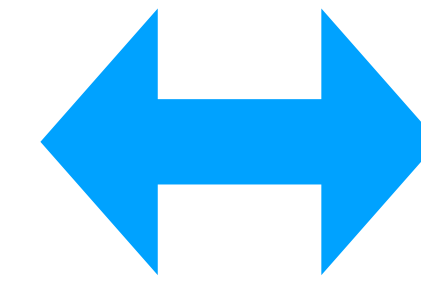
# Why does it work?

## Universal behavior of isovector transitions

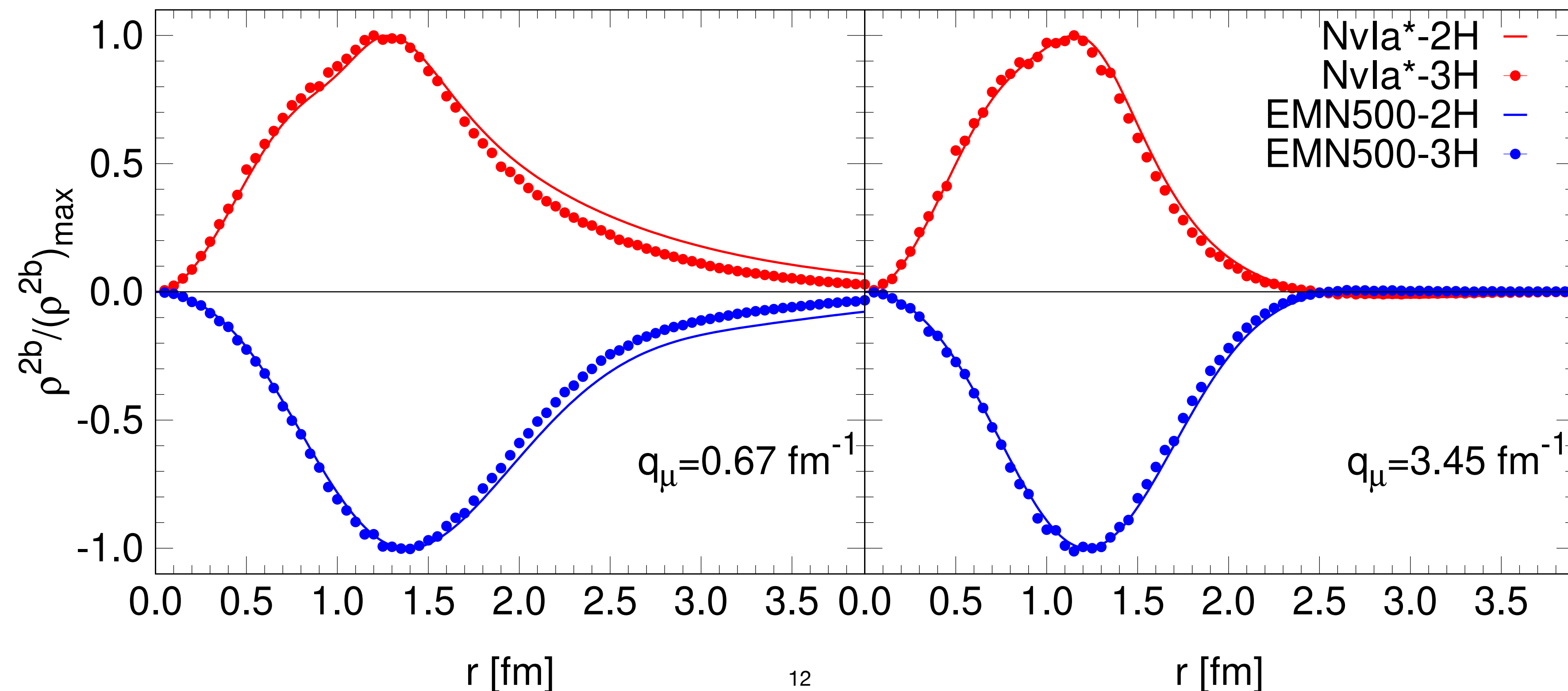
Correlated np  
pairs



Universal 2-body  
wave functions



Universal 2-body  
transition densities

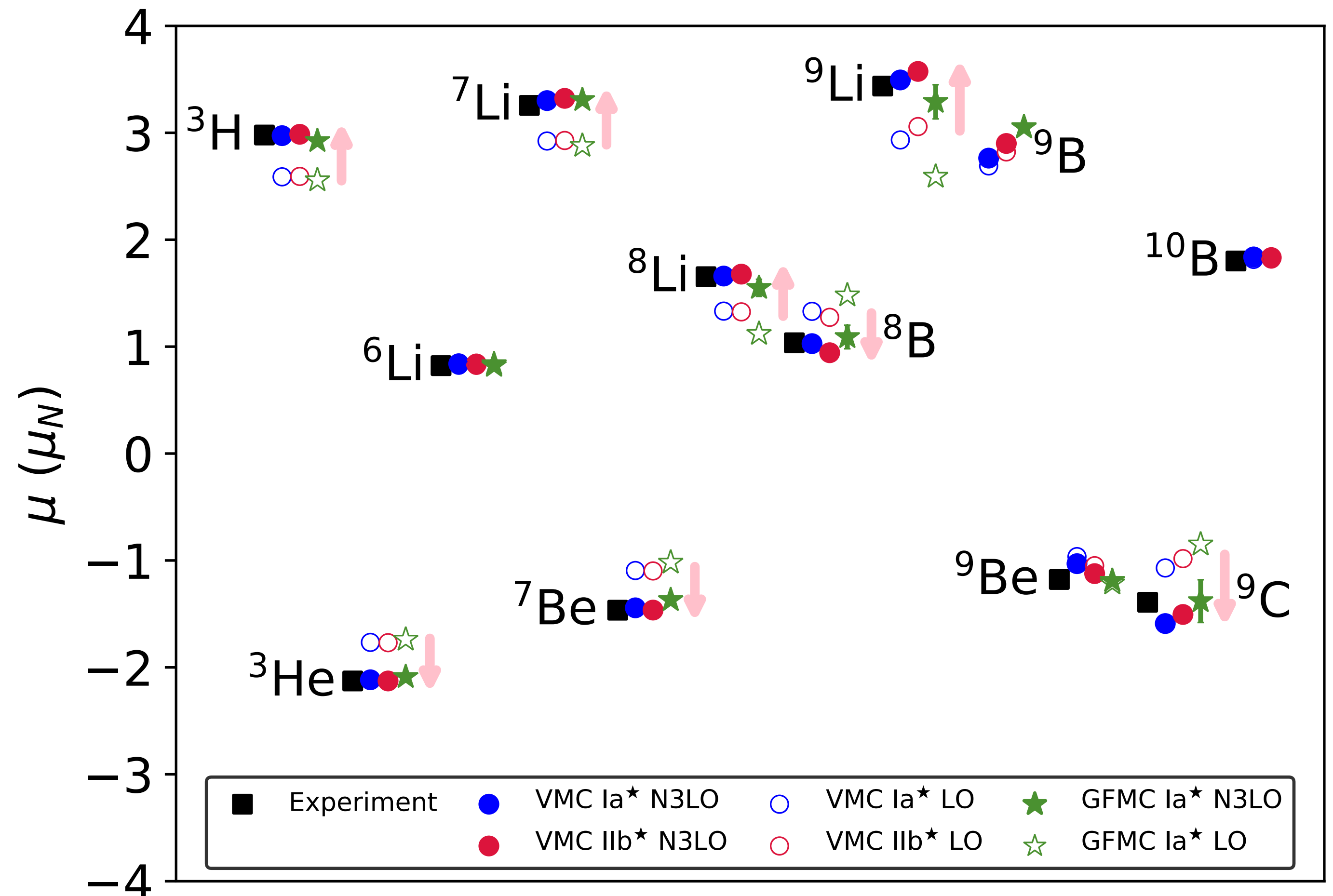




# Magnetic moments of light nuclei

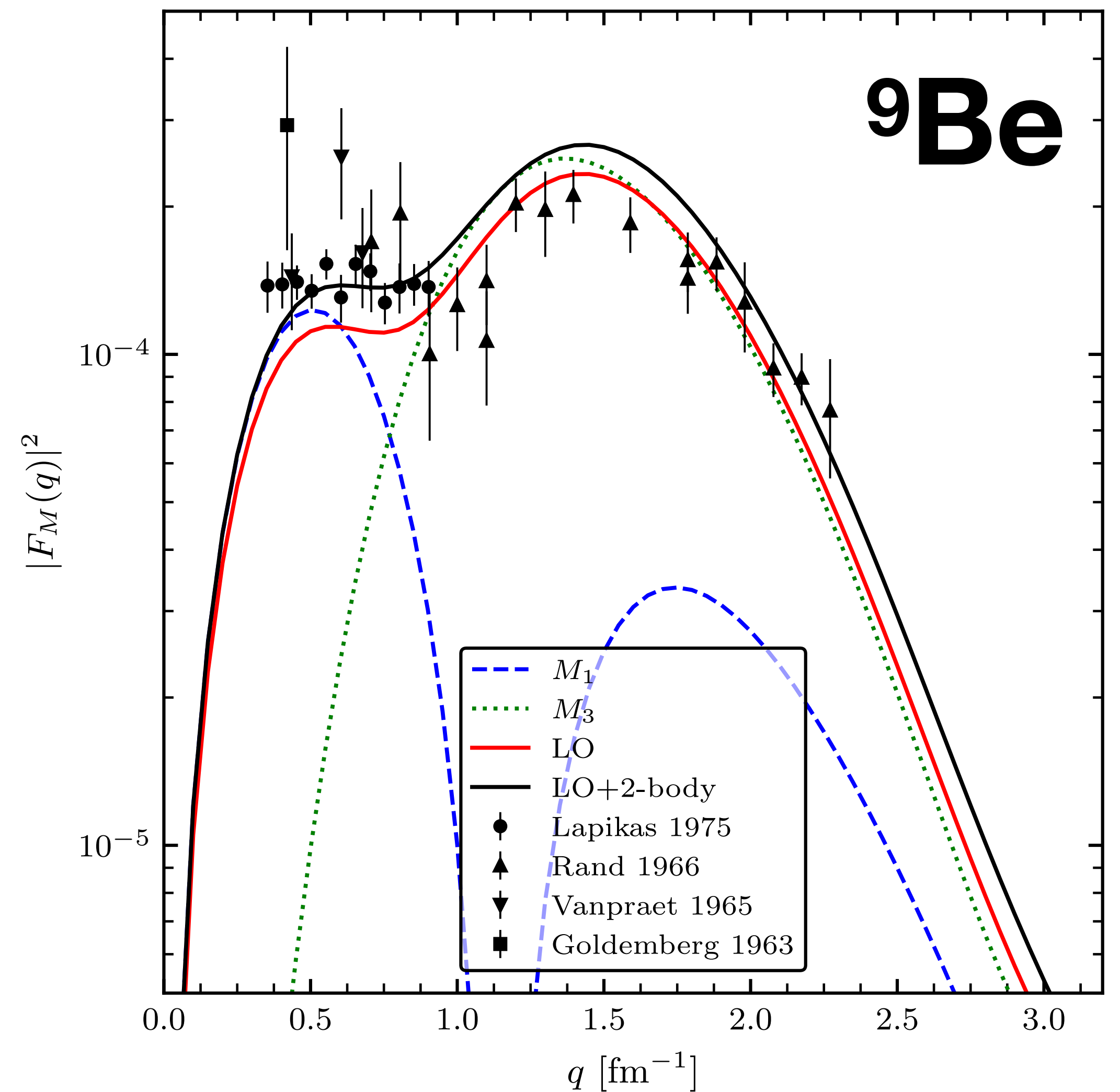
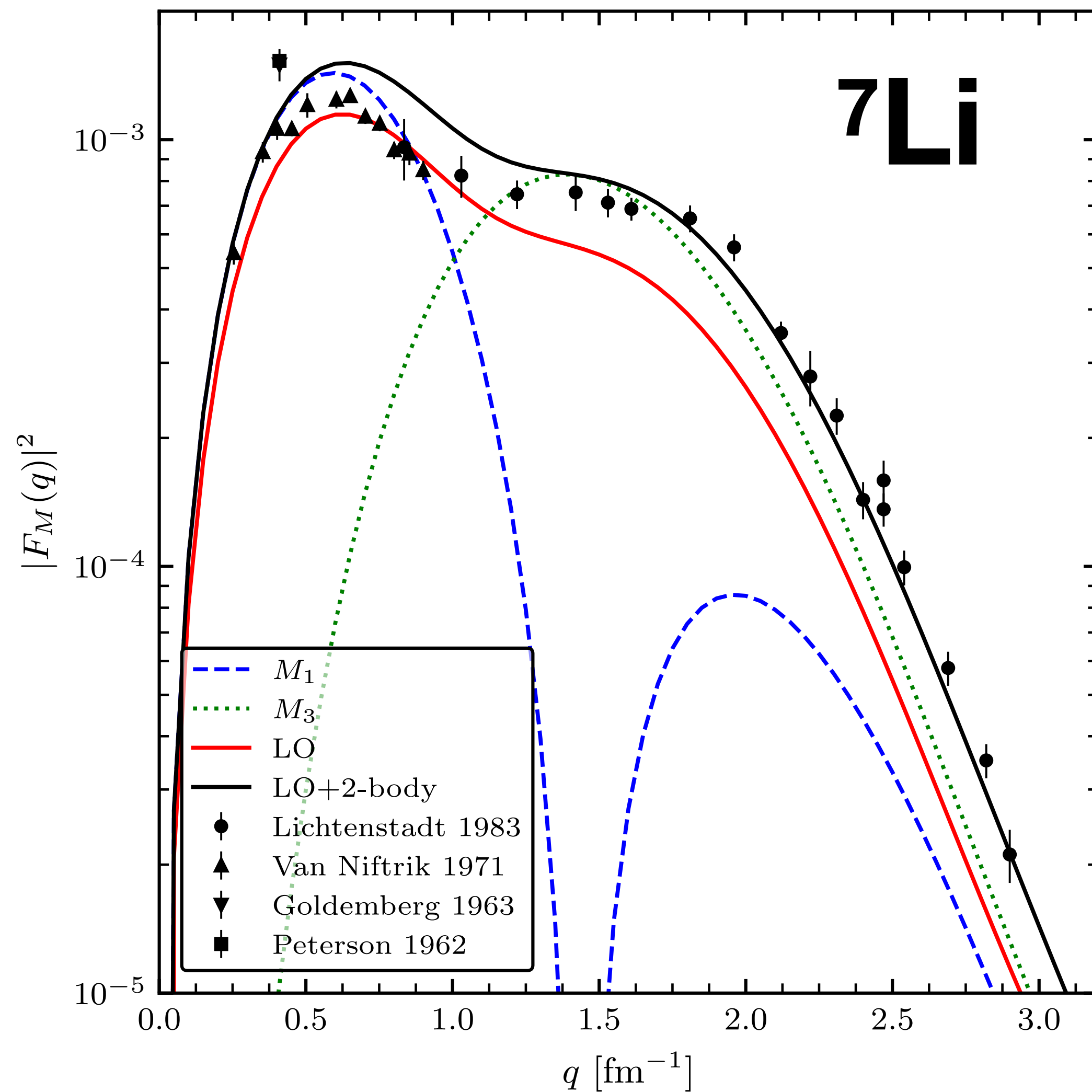
## Magnetic structure at $Q = 0$

- Calculation performed using Variational Monte Carlo and Green Function Monte Carlo methods (see L. Andreoli talk).
- The two-body currents bring the calculation in agreement with the experiments (pink arrows).



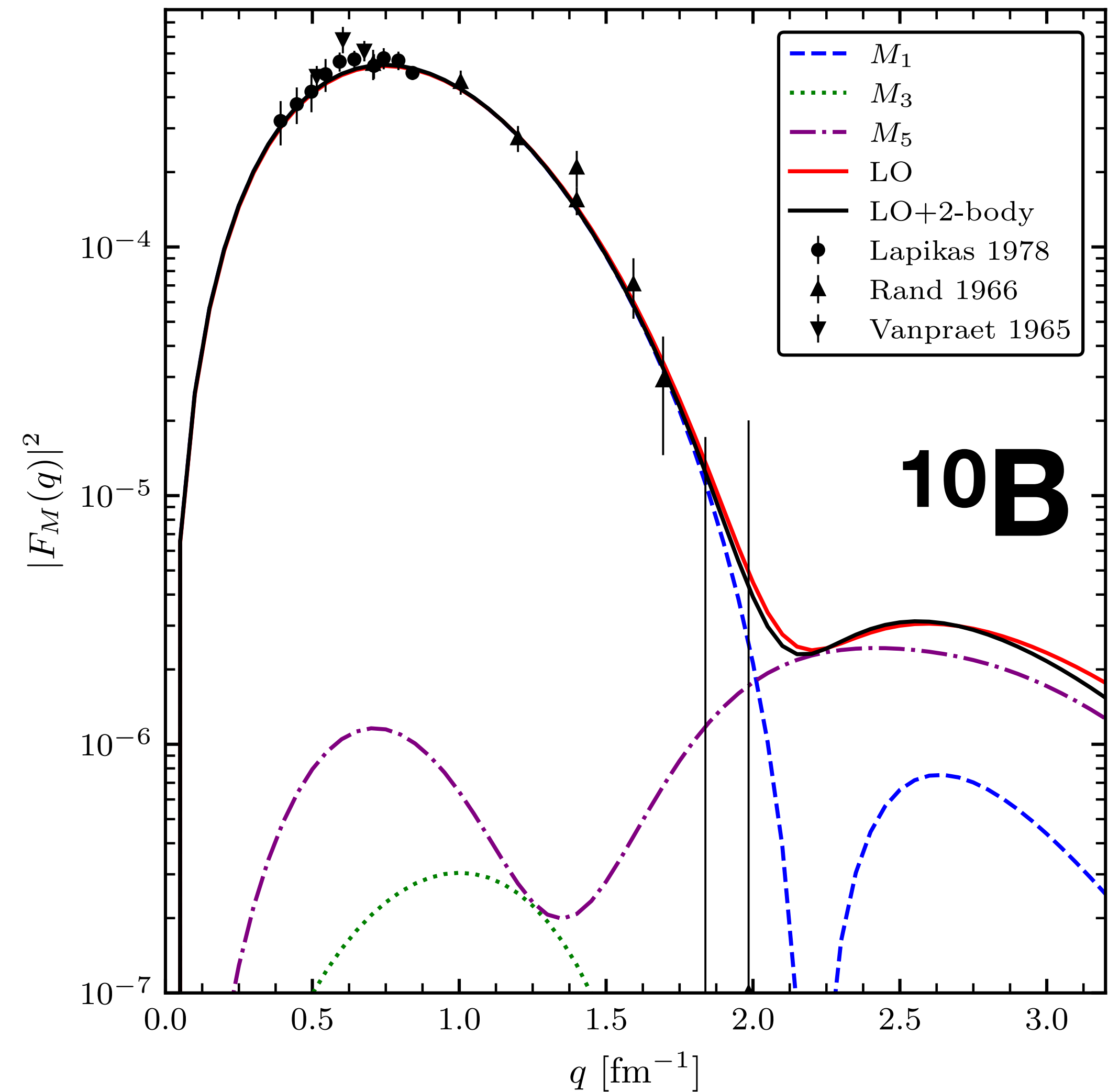
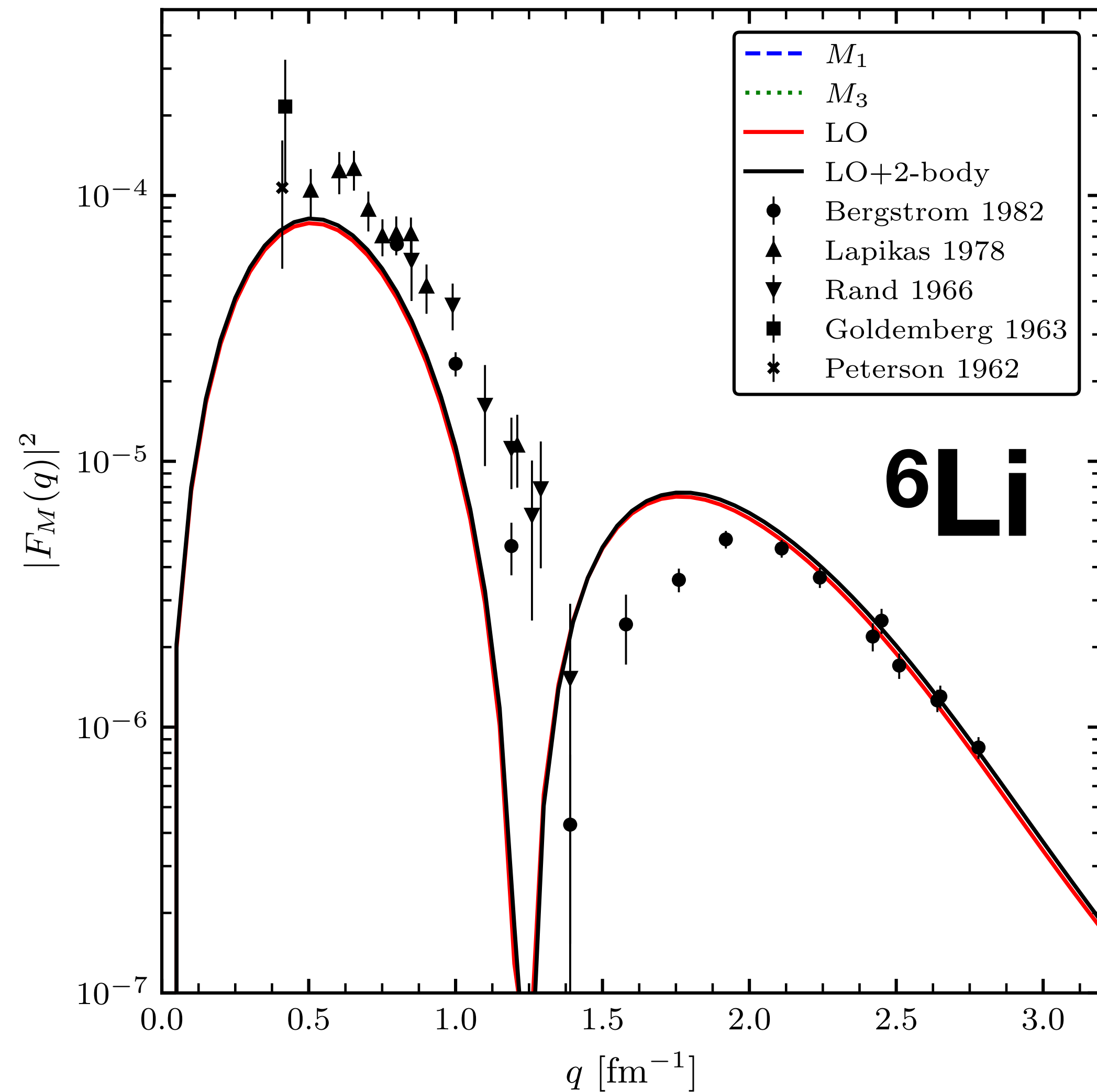
# Magnetic form factor predictions

## Lithium-7 and Berilium-9 (isovector dominated)



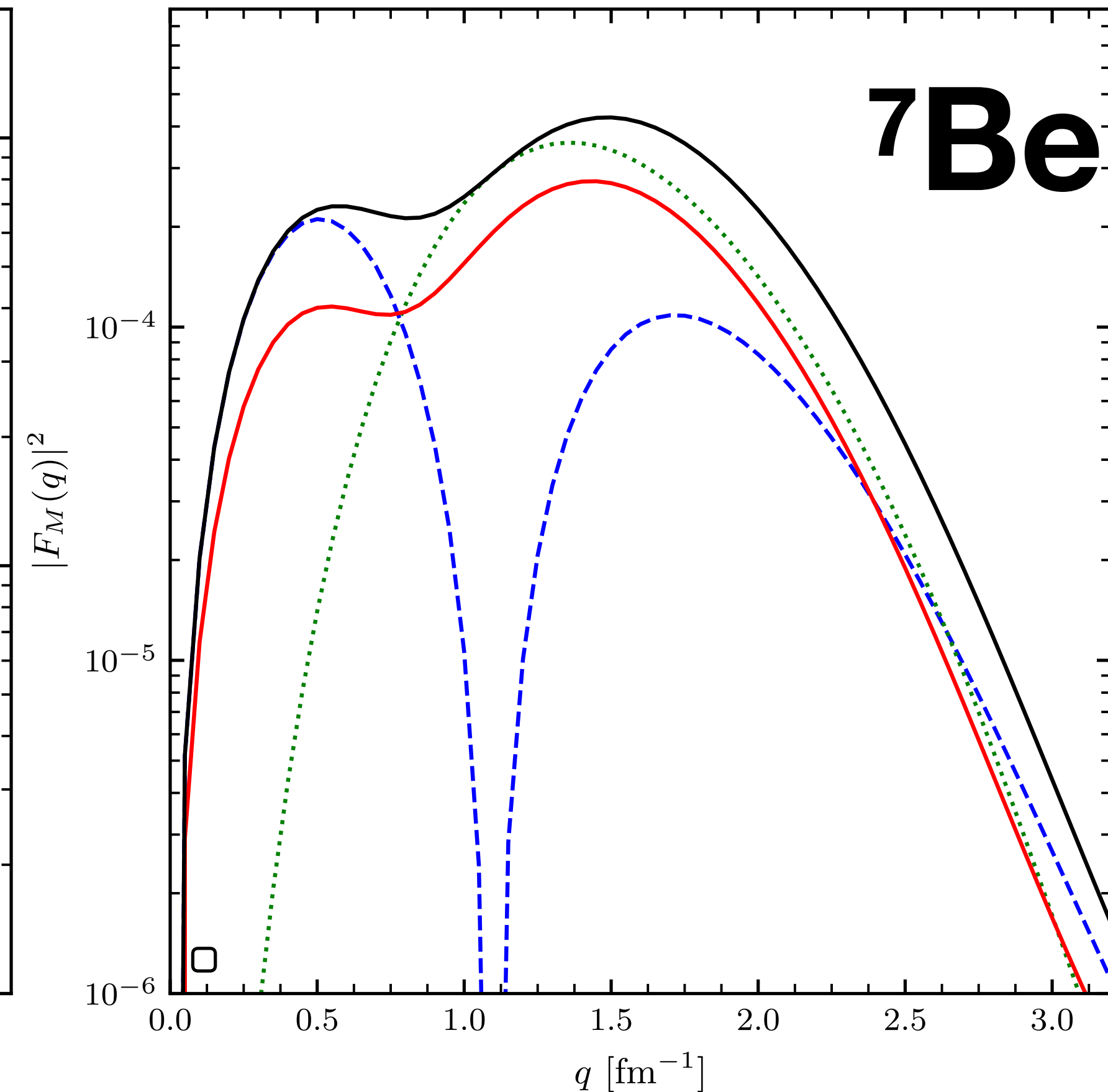
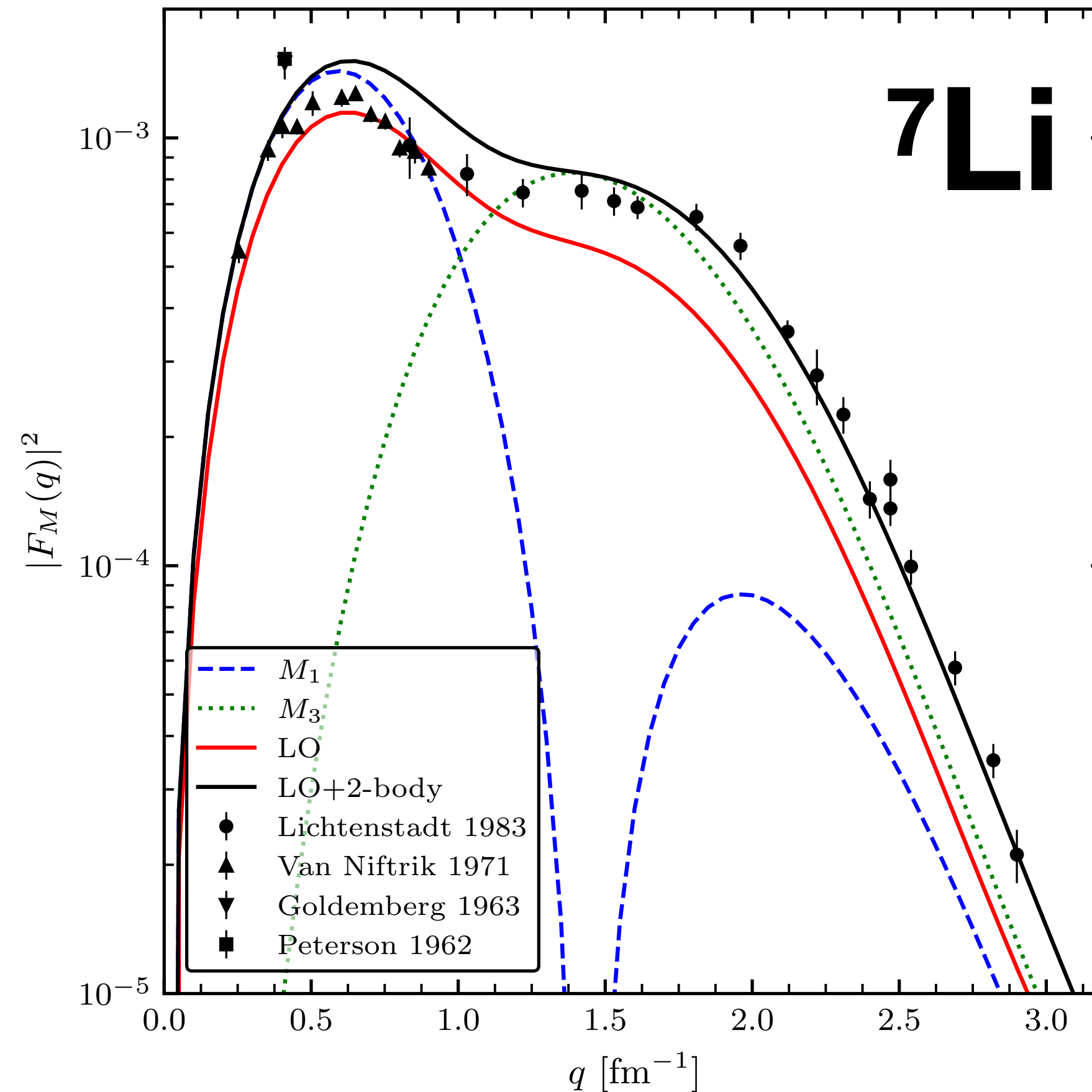
# Magnetic form factor predictions

## Lithium-6 and Boron-10 (isoscalar dominated)



# Mirror nuclei structure

- $M_1$  is enhanced respect to  $M_3$  for nuclei with an unpaired neutron in the p-shell.
- We observed a similar phenomenon for the mirror systems  ${}^9\text{Li}$ - ${}^9\text{C}$  and  ${}^9\text{Be}$ - ${}^9\text{B}$



**Pure prediction (no previous literature) + no experimental confirmation**



# Mirror nuclei structure

## The reason

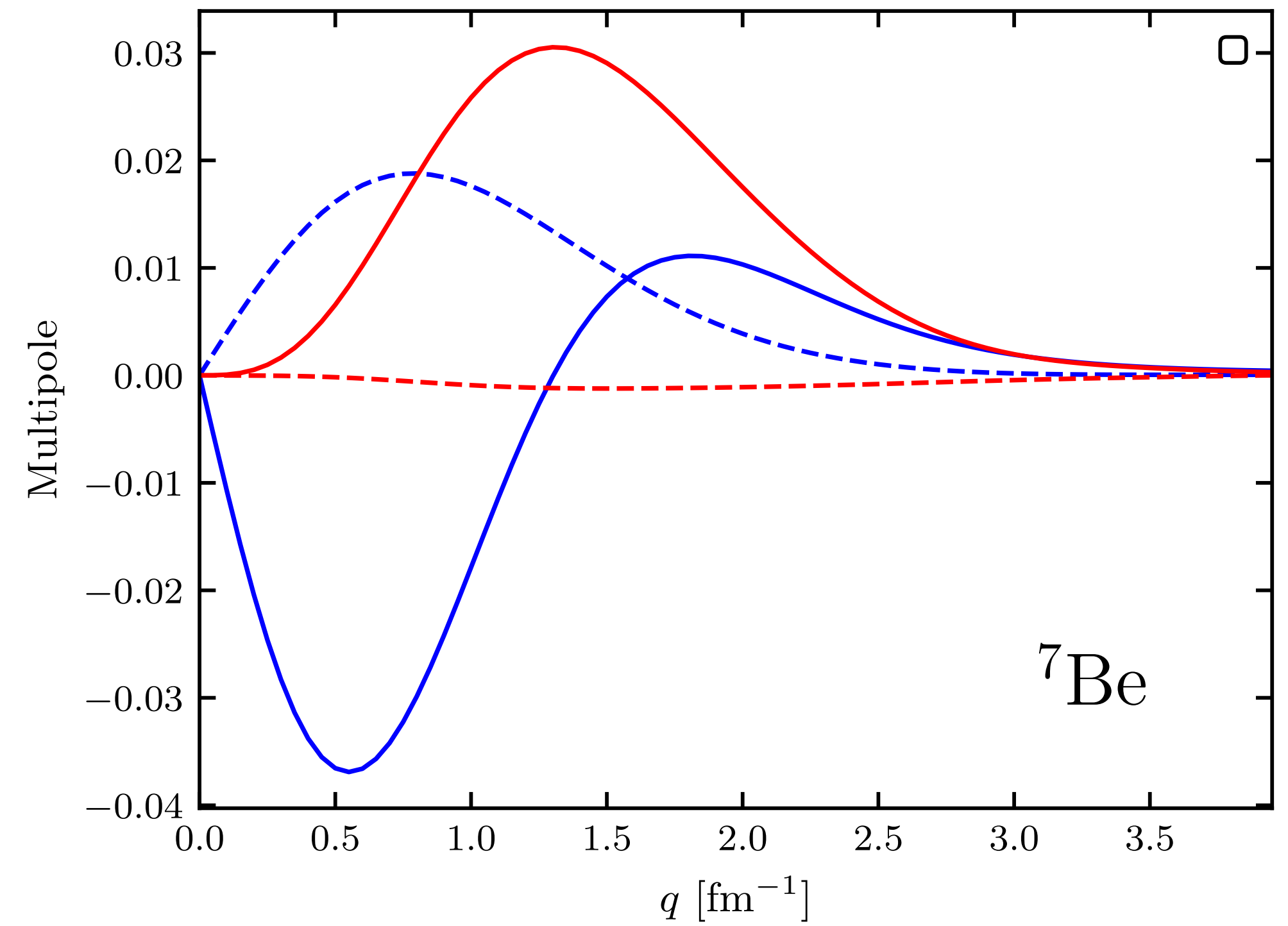
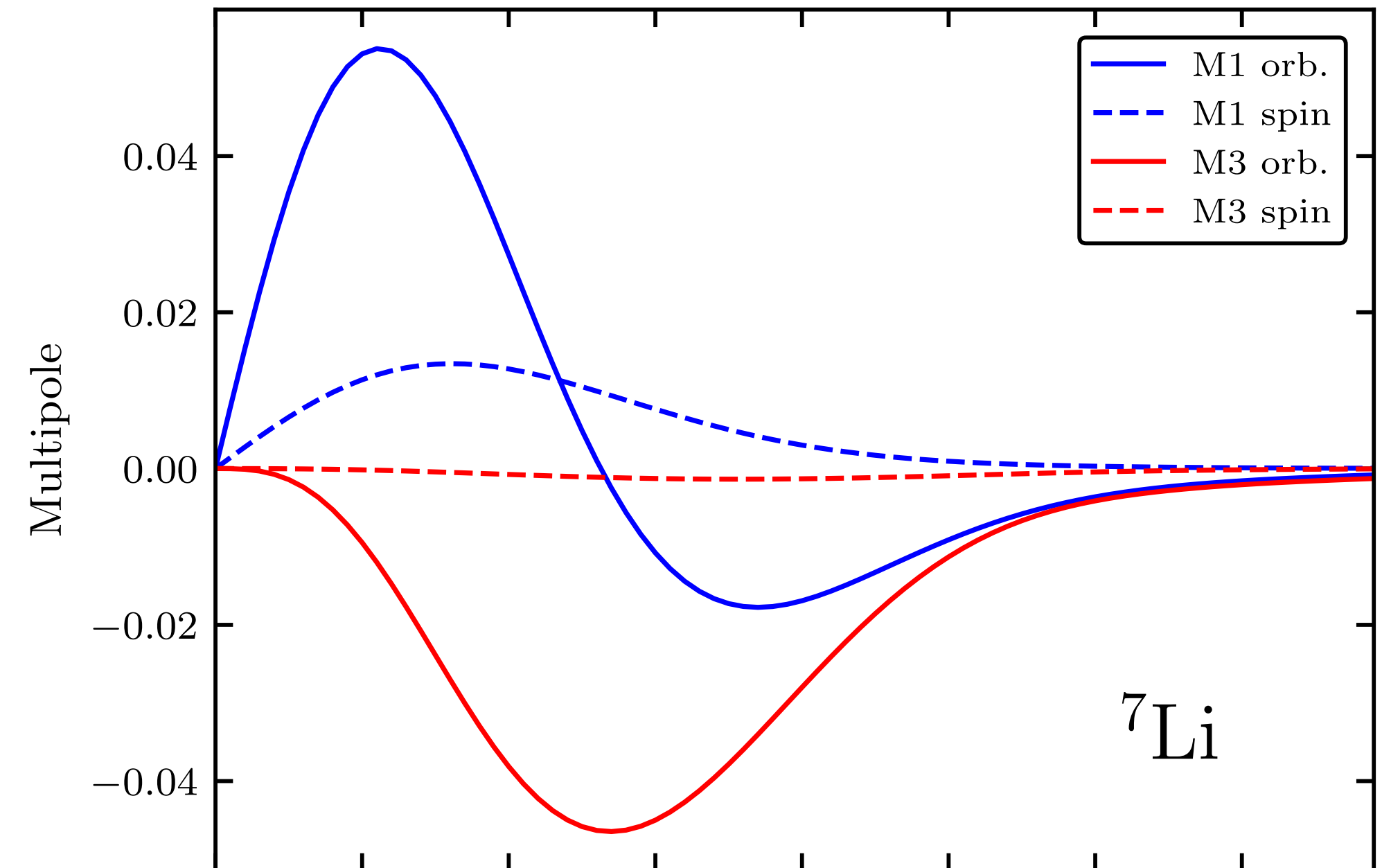
$$\mathbf{j}^{\text{LO}}(\mathbf{q}) = \frac{\epsilon_i(q_\mu^2)}{2m} [\mathbf{p}_i, e^{i\mathbf{q}\cdot\mathbf{r}_i}]_+ + i \frac{\mu_i(q_\mu^2)}{2m} e^{i\mathbf{q}\cdot\mathbf{r}_i} \boldsymbol{\sigma}_i \times \mathbf{q},$$

Convection current

Magnetic current

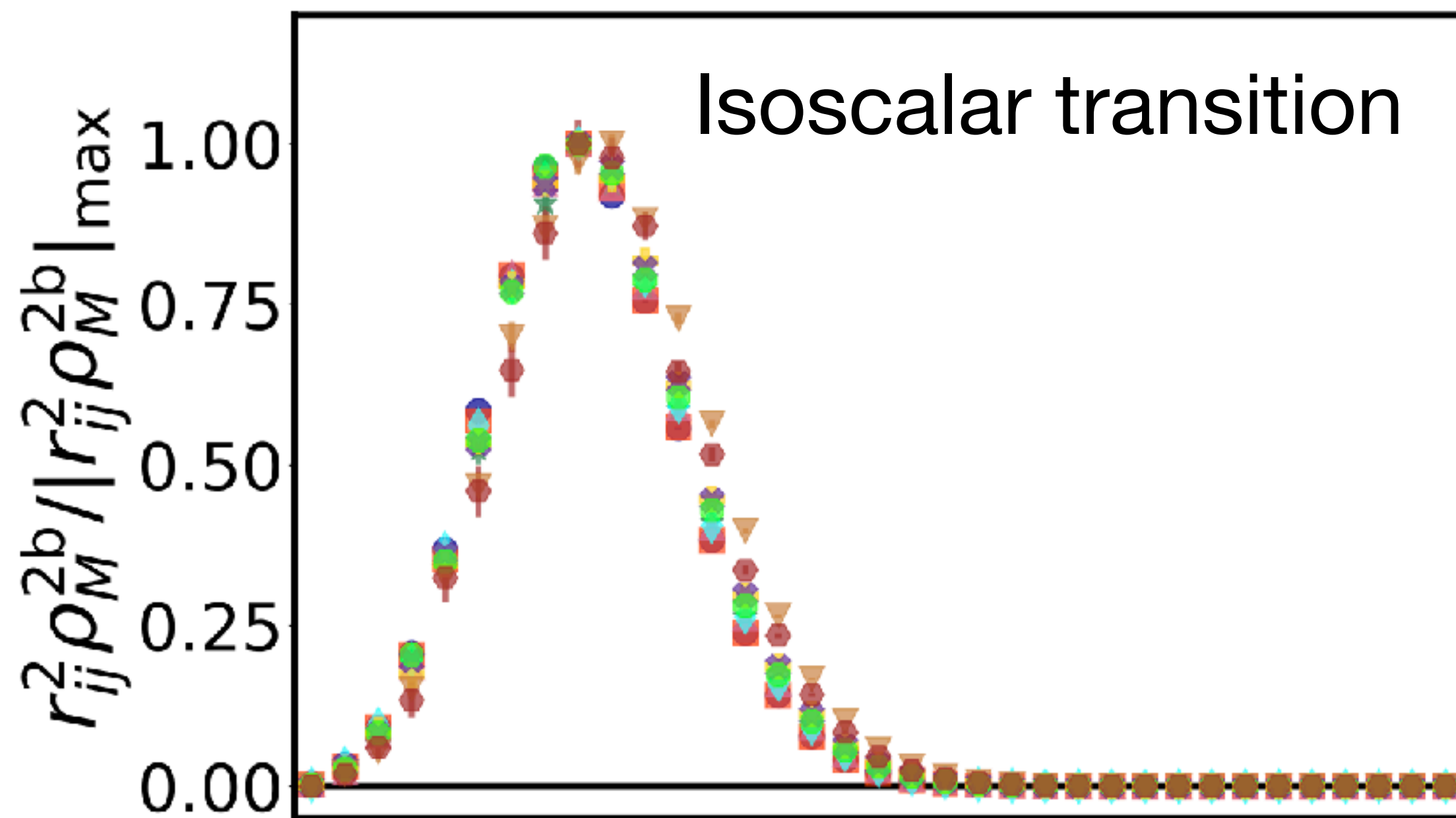
No contribution to  $M_3$

Change sign if there is an unpaired neutron/proton



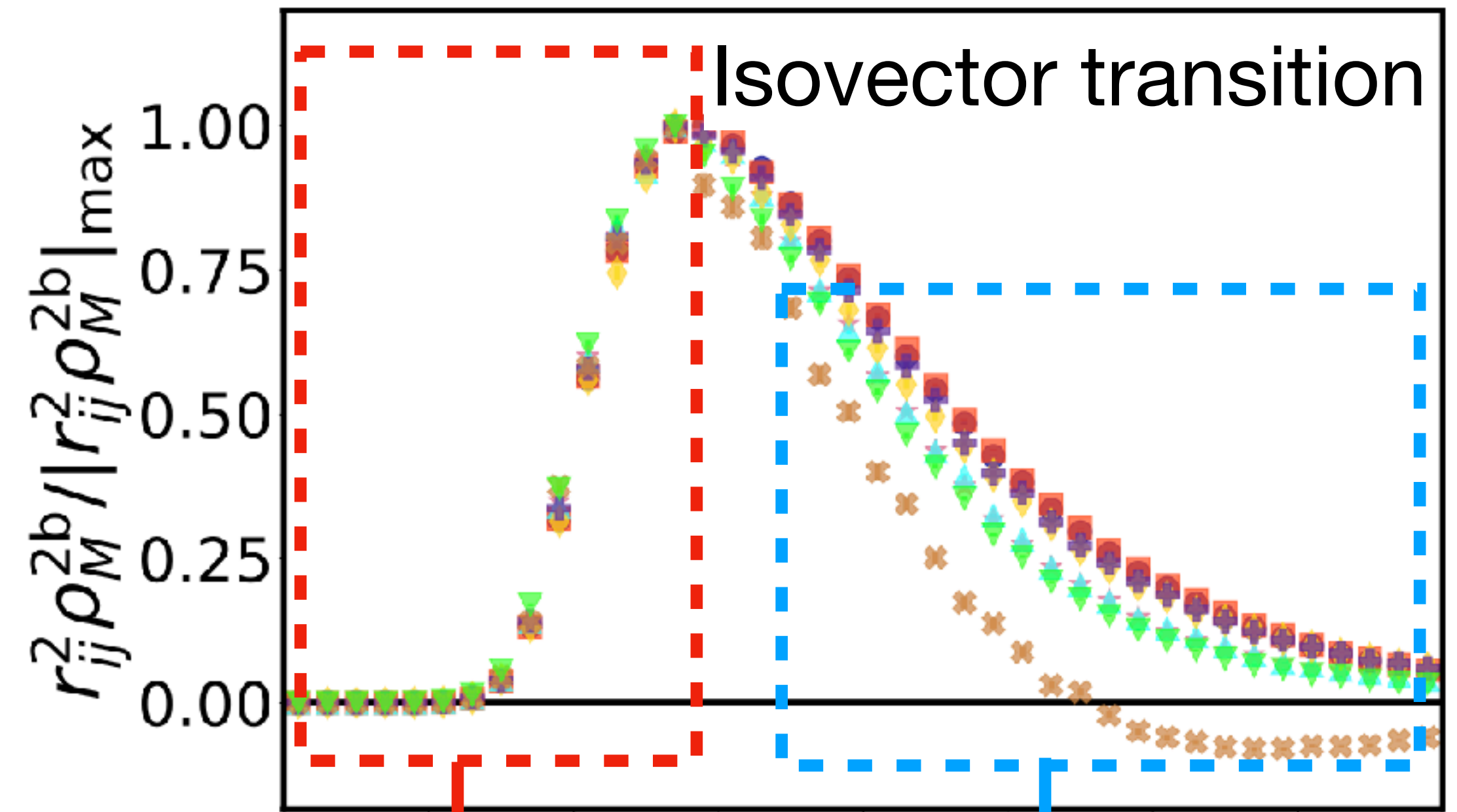
# More on 2-body transition densities

## Universality of isoscalar and isovector transitions



Transition  $^1S_0 \leftrightarrow ^1S_0$   $^3S_1 \leftrightarrow ^3S_1$

ST=00 isoscalar  
couples suppressed



SRC  $^1S_0 \leftrightarrow ^3S_1$

P-waves

+ ST=11 isovector couples

# Summary

## Magnetic form factors

- First ab-initio calculation of magnetic form factors of nuclei up to  $A=10$ .
- Good description of available magnetic form factor data.
- **Two-body currents account up to 40-50% of the total contribution to the magnetic form factors.**
- **First observation of  $M_1/M_3$  inversion in mirror p-shell nuclei (not observed experimentally yet).**

**More data at larger  $Q^2$  and on more nuclei would permit to validate our models**

# Conclusions

- Two-body currents are crucial for describing the EM structure of nuclei at  $Q^2 \sim 0 - 0.64 \text{ GeV}^2$
- The physics associated with the two body currents is determined by the correlations of nucleons in nuclei (SRC).
- The aim use the same currents and description of the nuclear dynamics to predict the effects in JLab experiments.
  - Increase the range of applicability (enlarge  $Q^2$ ).
  - Integrate our calculation with higher energies model.
- **Discriminate between nuclear structure effects and pure nucleon physics**



# Collaborators

L. Andreoli (JLab & ODU)

G. Chambers-Wall (WashU)

G. B. King (WashU)

S. Pastore (WashU)

M. Piarulli (WashU)

R. Schiavilla (JLab & ODU)

R. B. Wiringa (ANL)

# Acknowledgments

NTNP

DOE Topical Collaboration



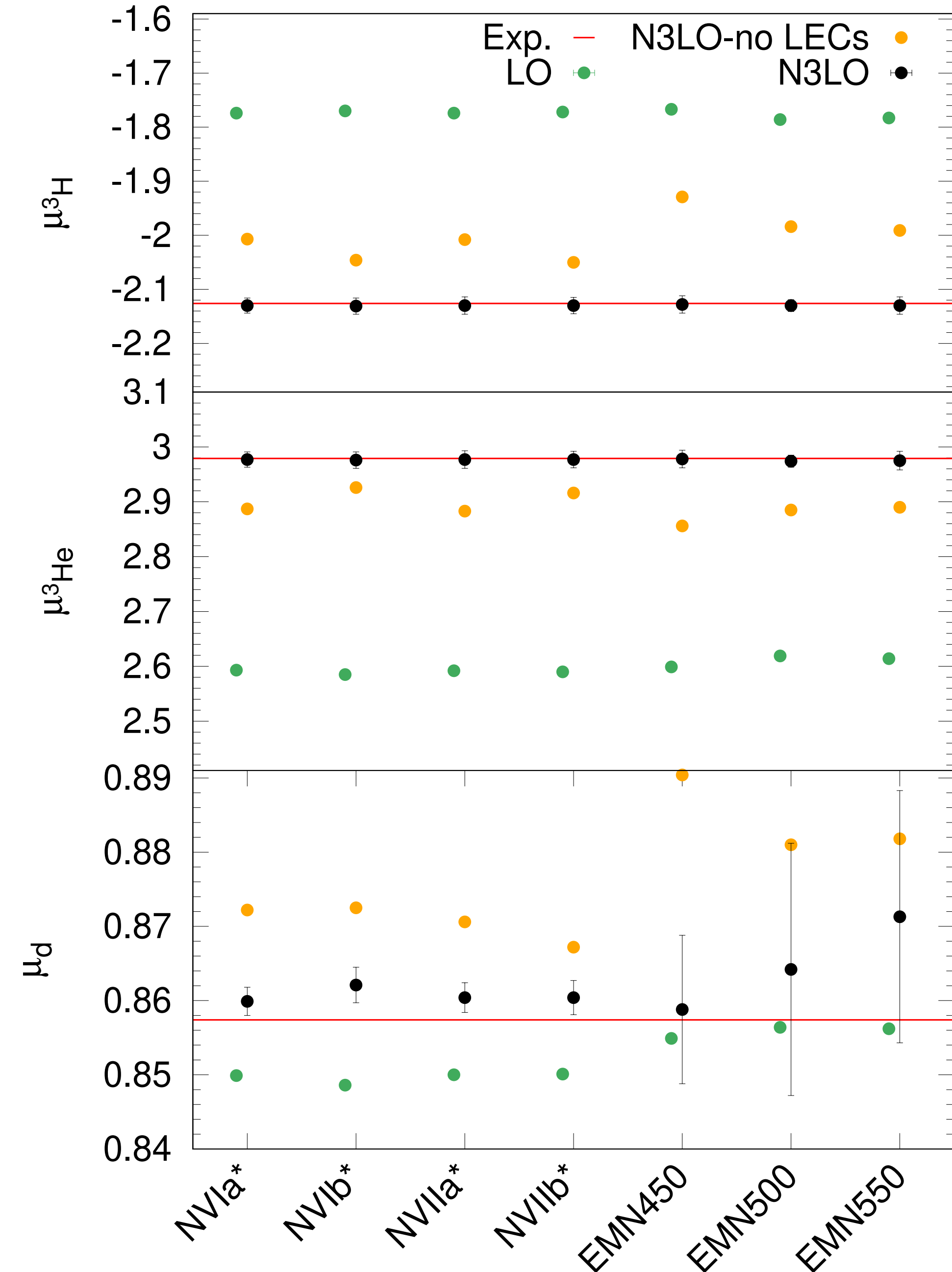
U.S. DEPARTMENT OF  
**ENERGY**

# Sparse

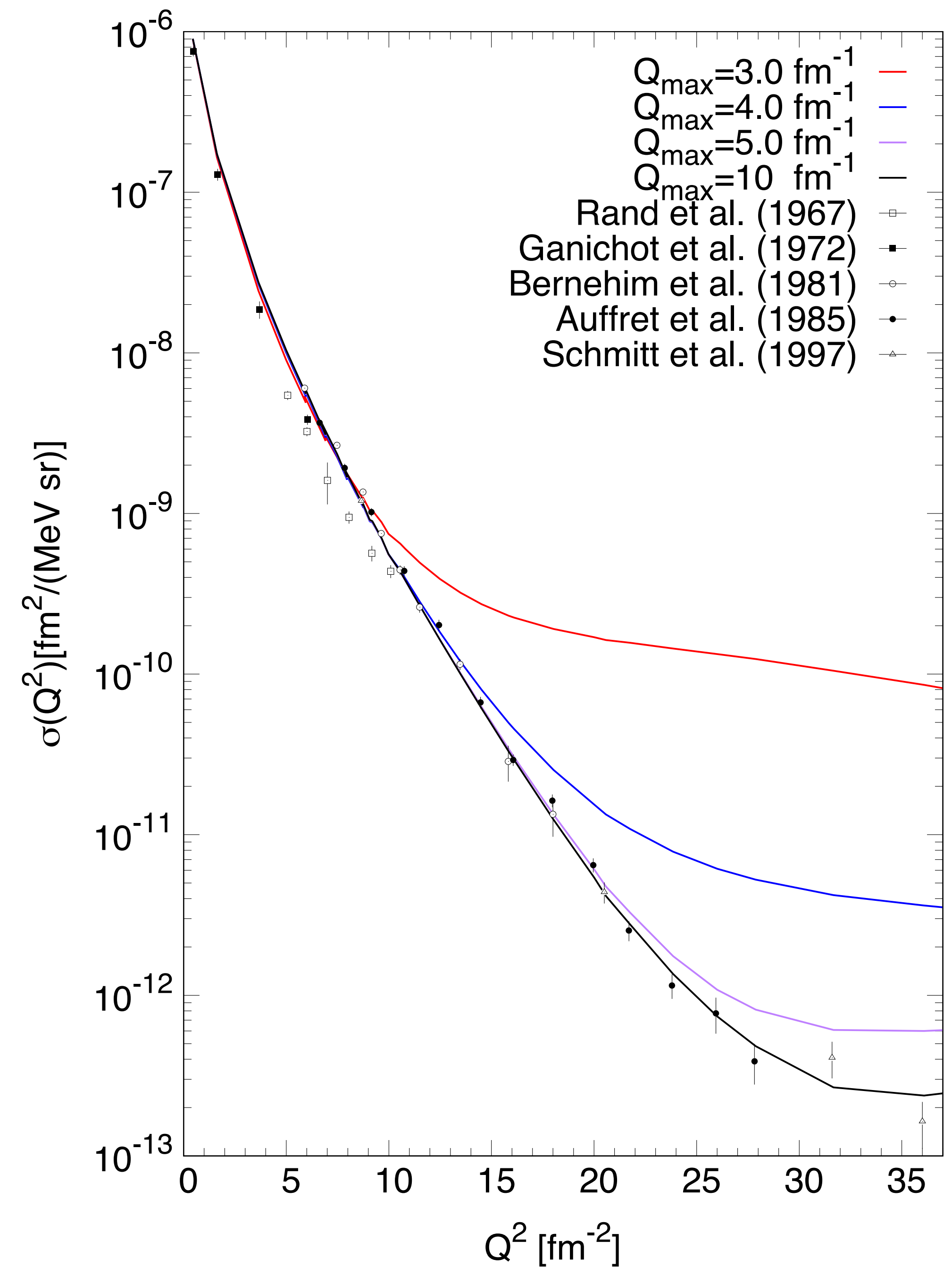
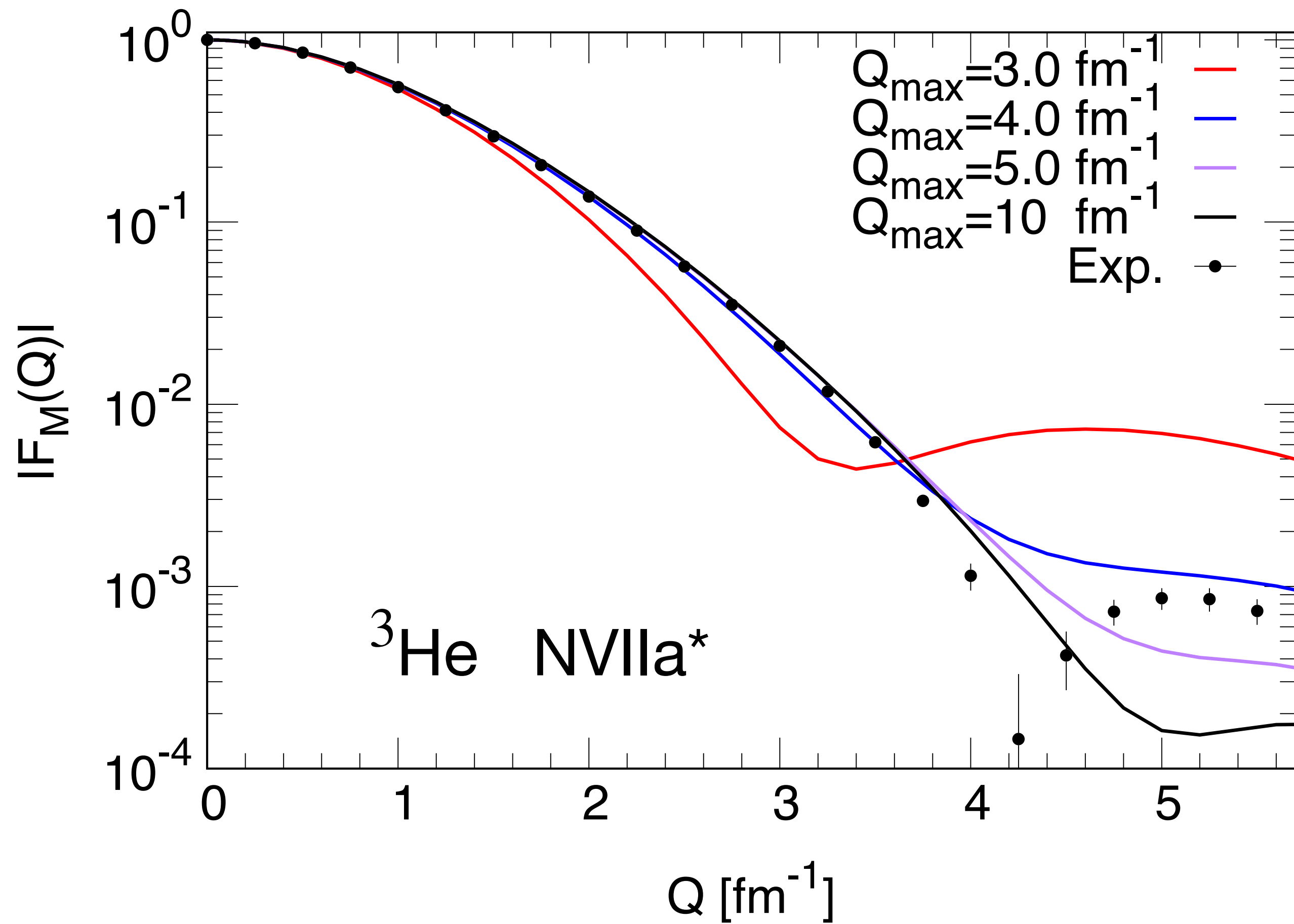
# Results of the fit

Pot.	$\chi^2/\text{ndf}$	$\chi^2/\text{ndf}$ (no Rand)
NVIa*	9.9	2.0
NVIb*	10.2	2.3
NVIIa*	11.6	2.5
NVIIb*	11.6	2.6
EMN450	11.3	2.8
EMN500	14.7	4.7
EMN550	17.7	7.9

- $\text{ndf} \sim 40$
- Removing Rand *et al.* data,  $\chi^2$  improves

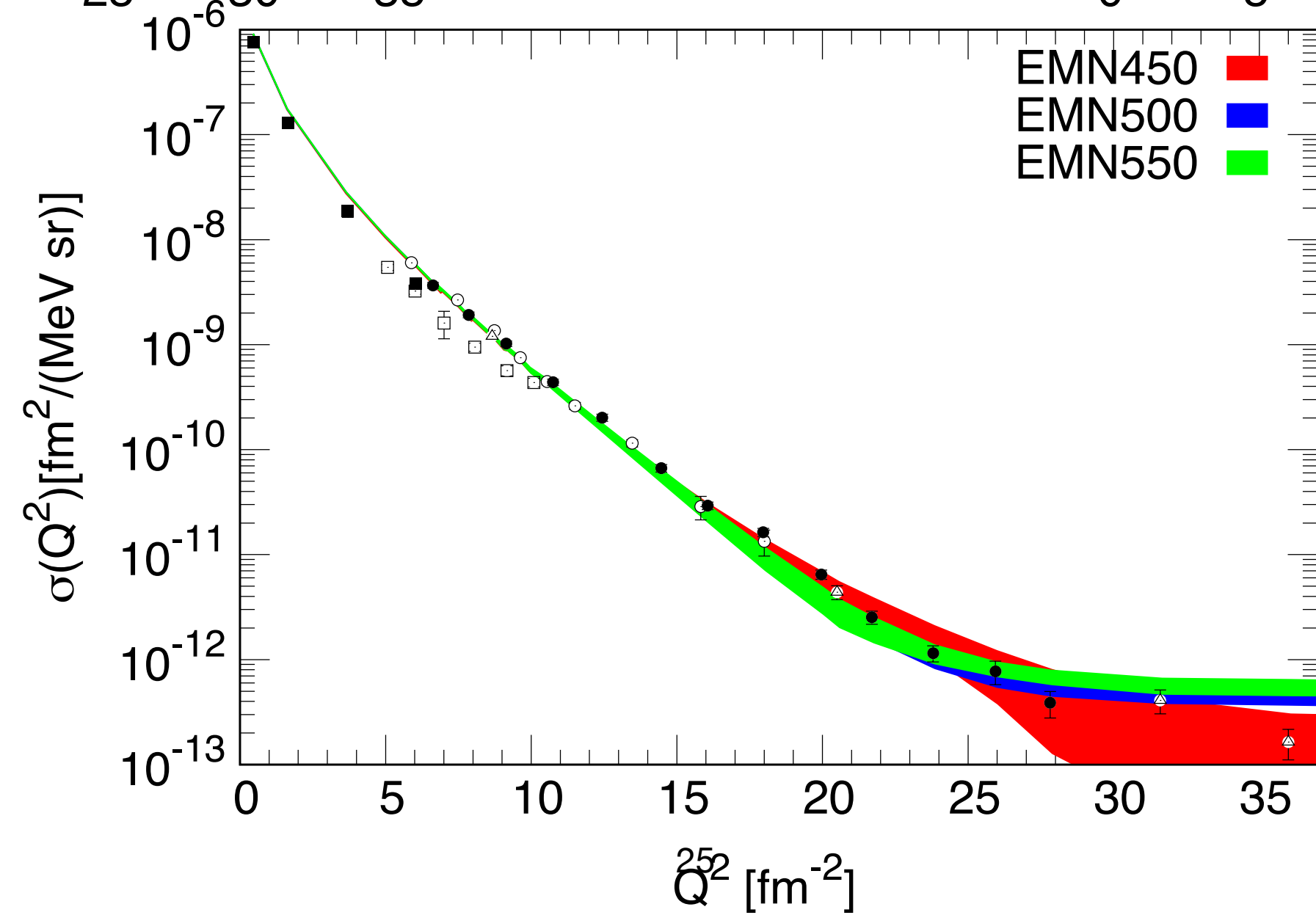
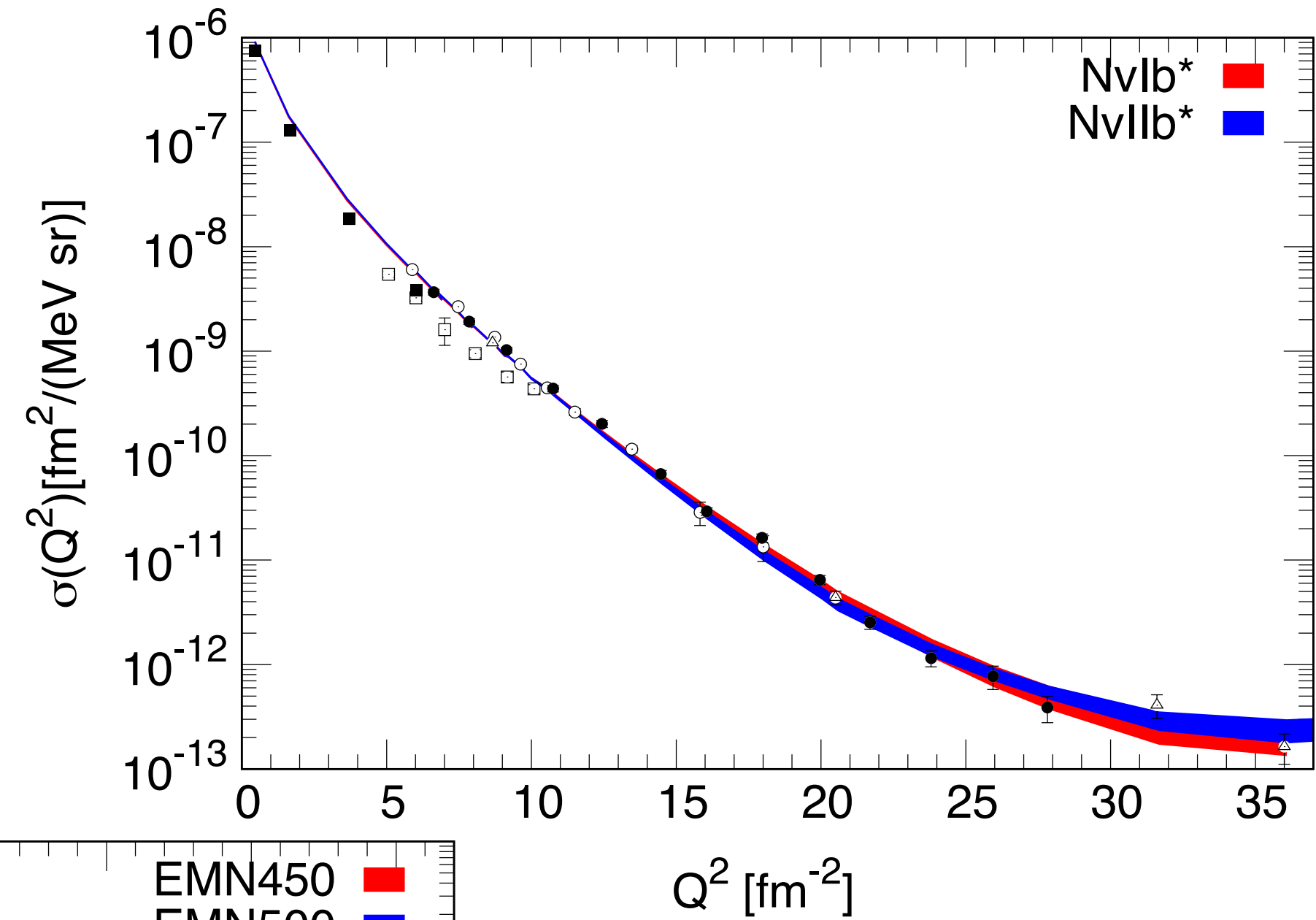
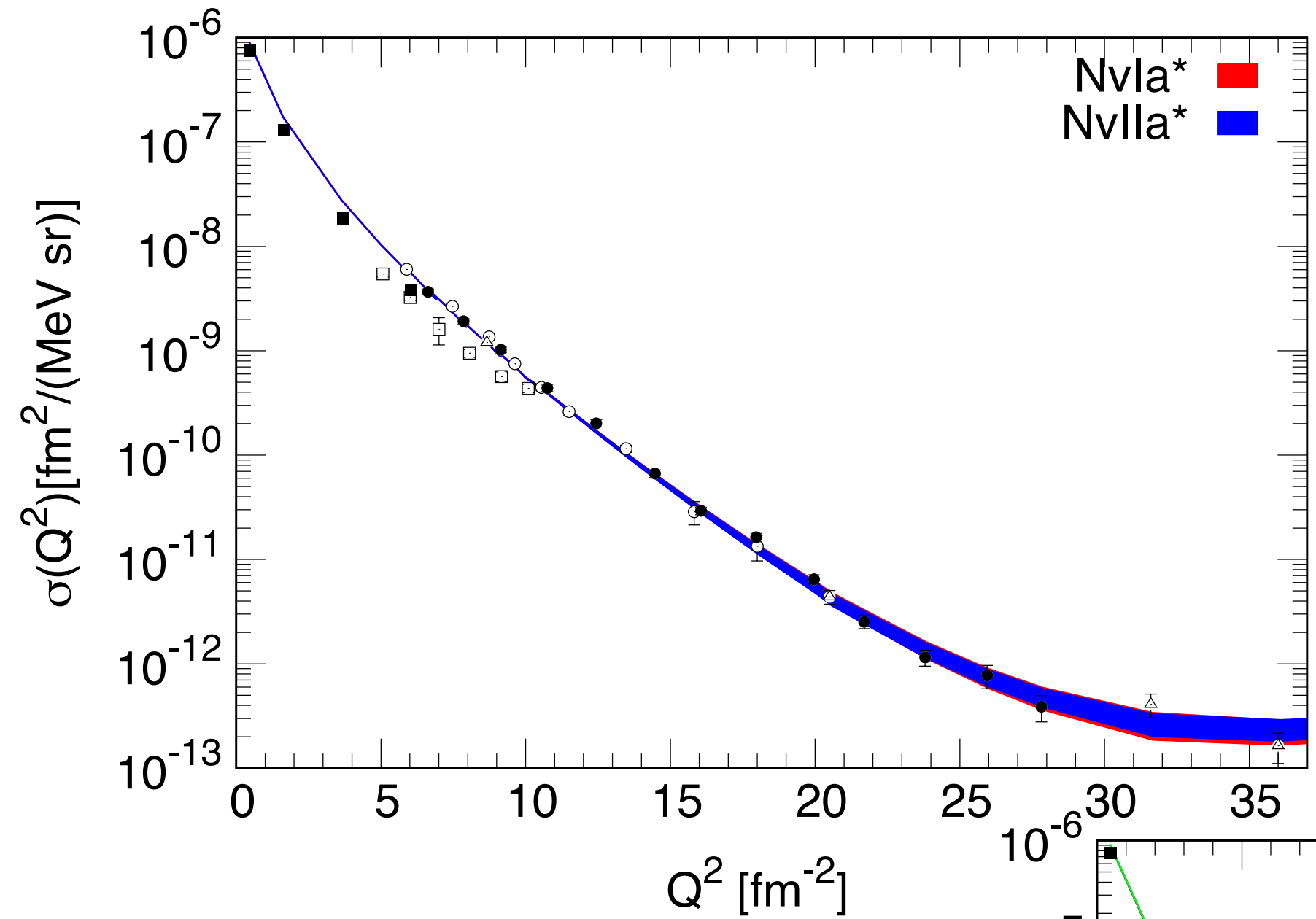


# Dependence on $Q_{\max}^2$

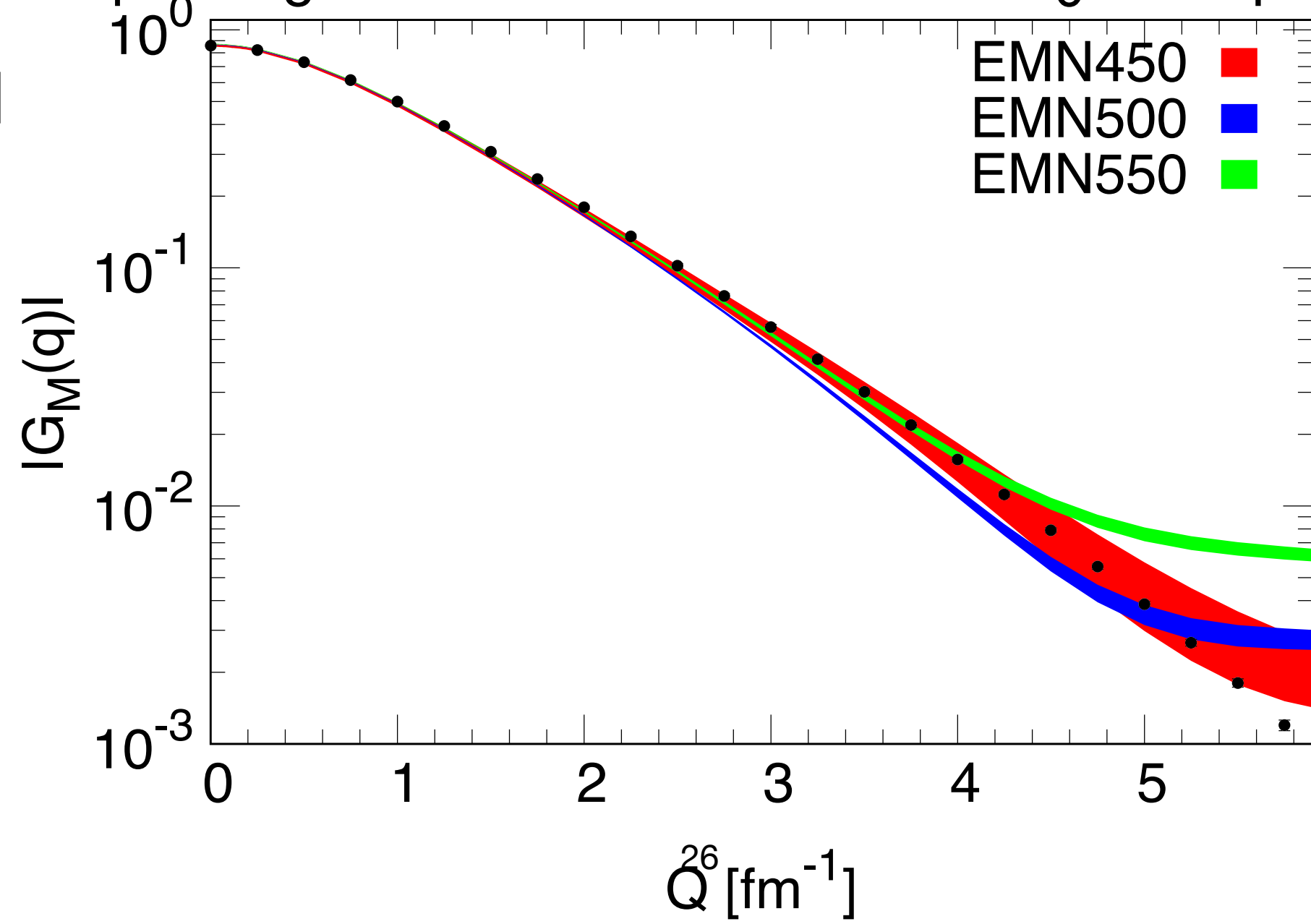
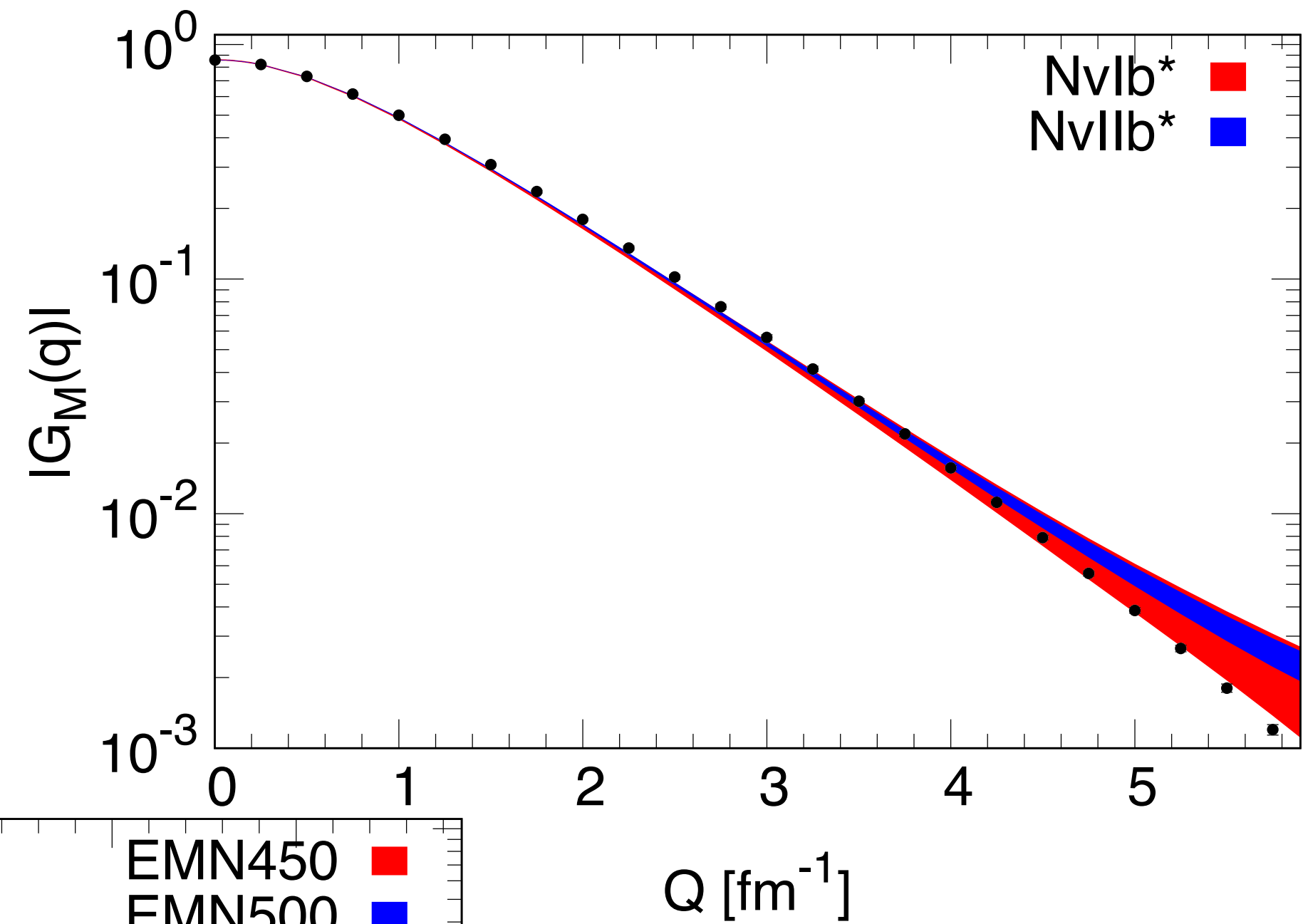
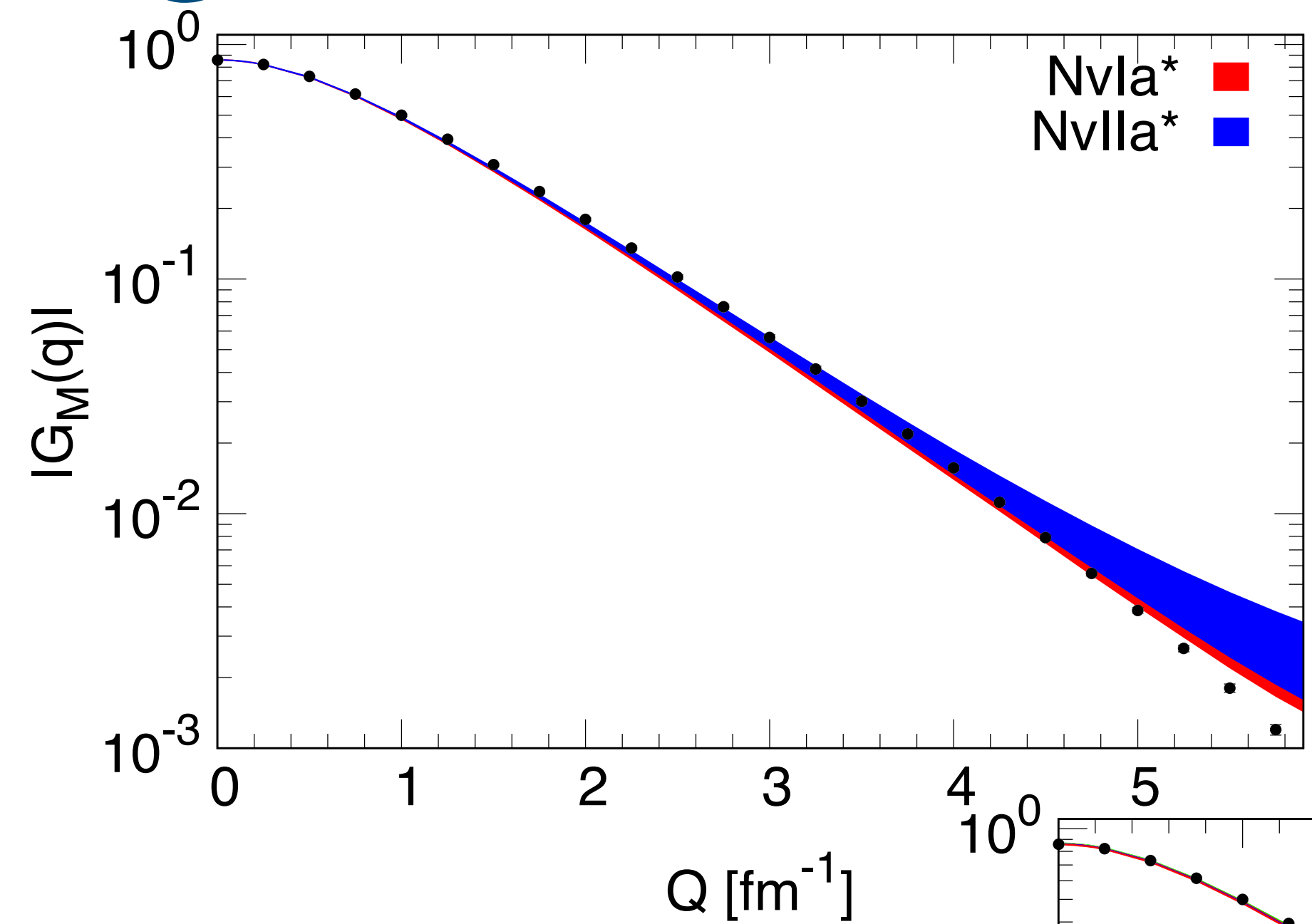




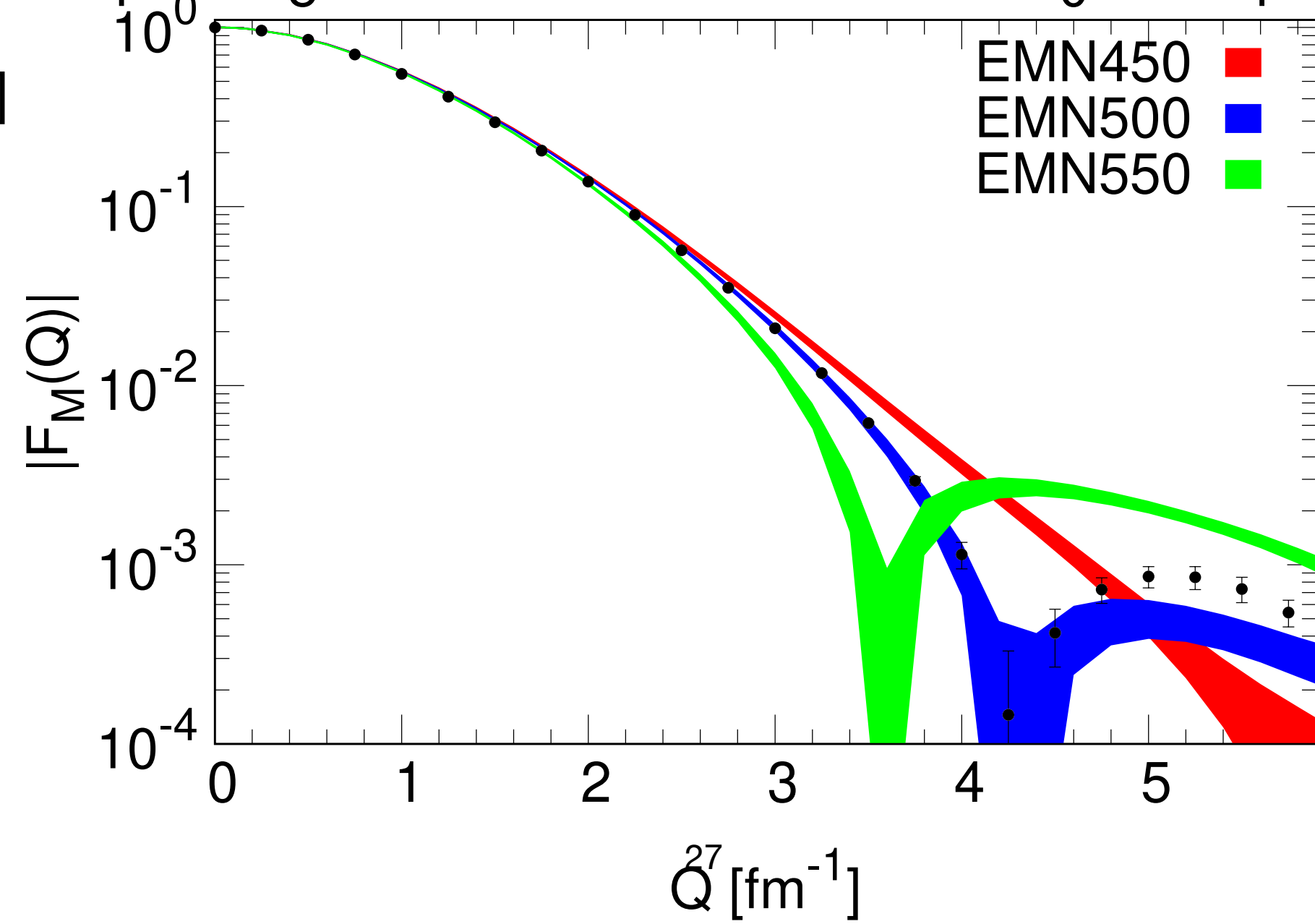
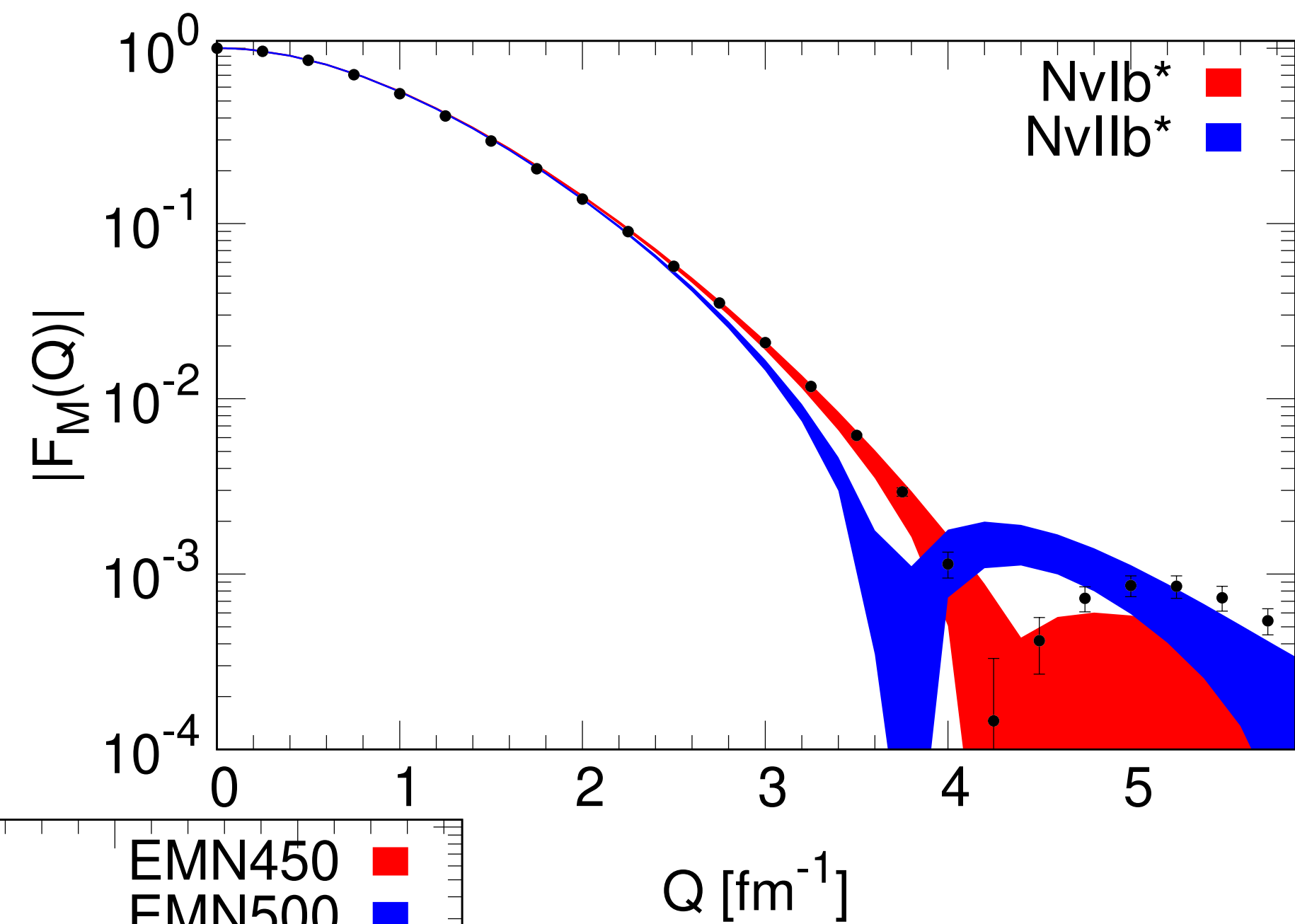
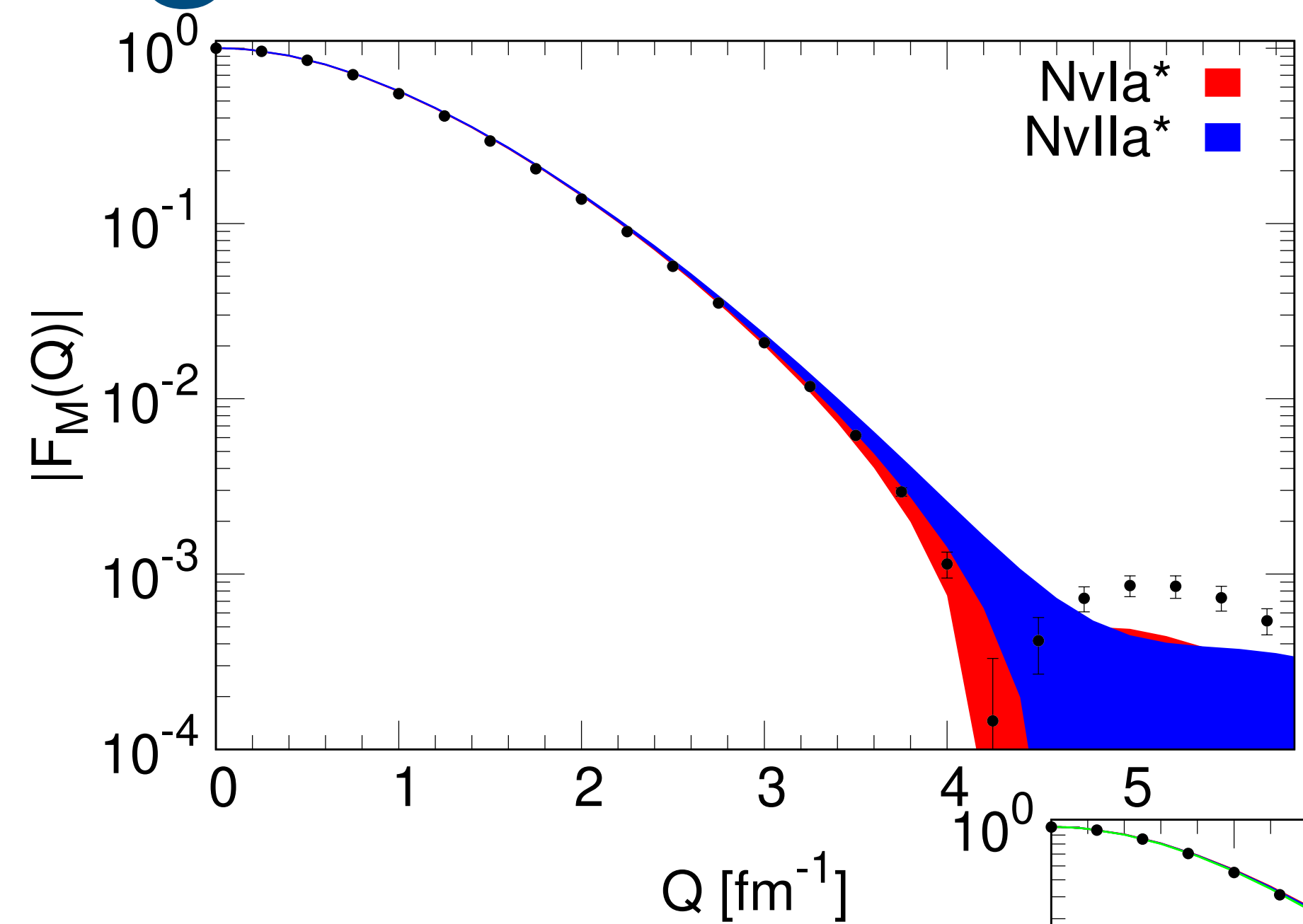
# d-threshold



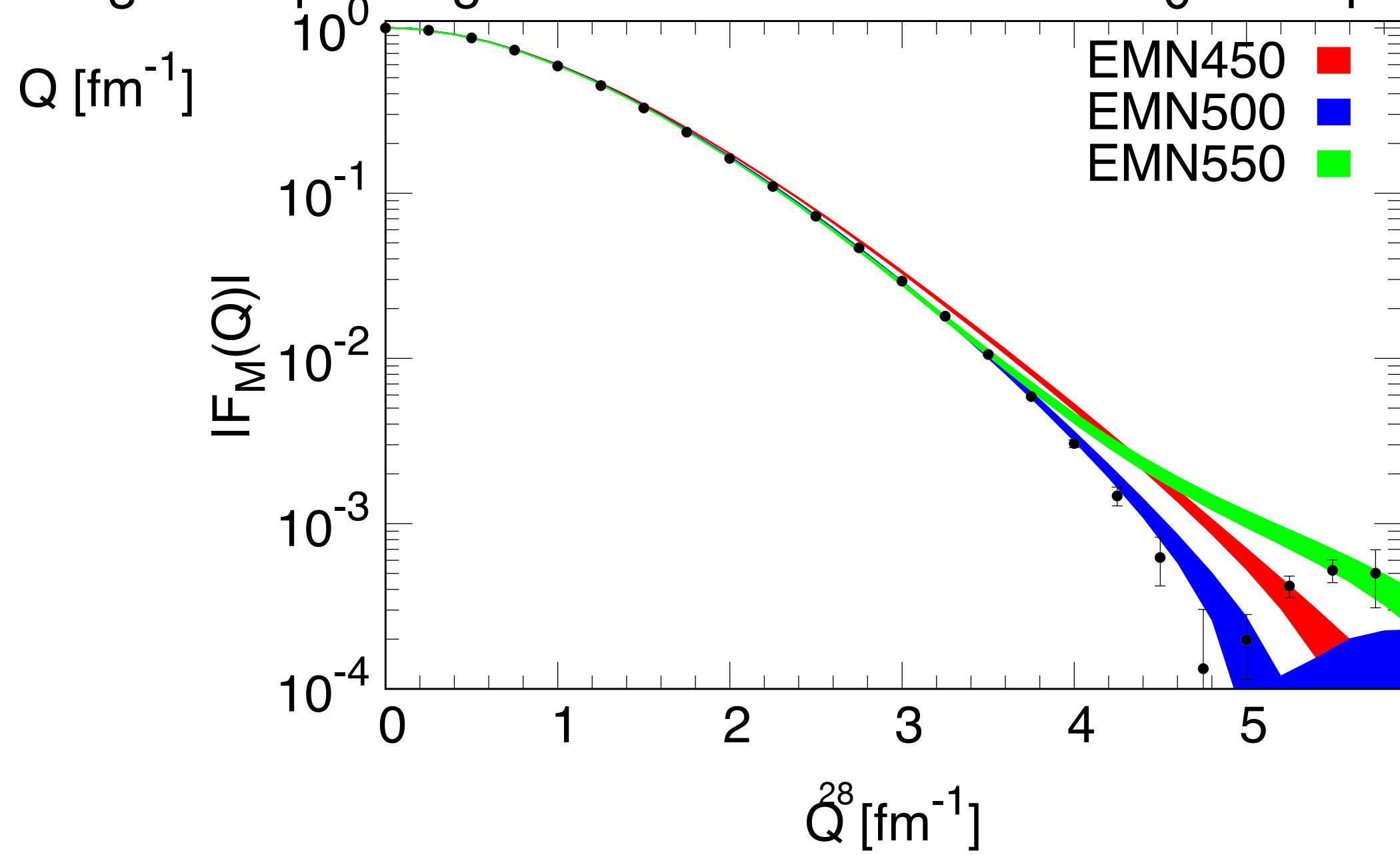
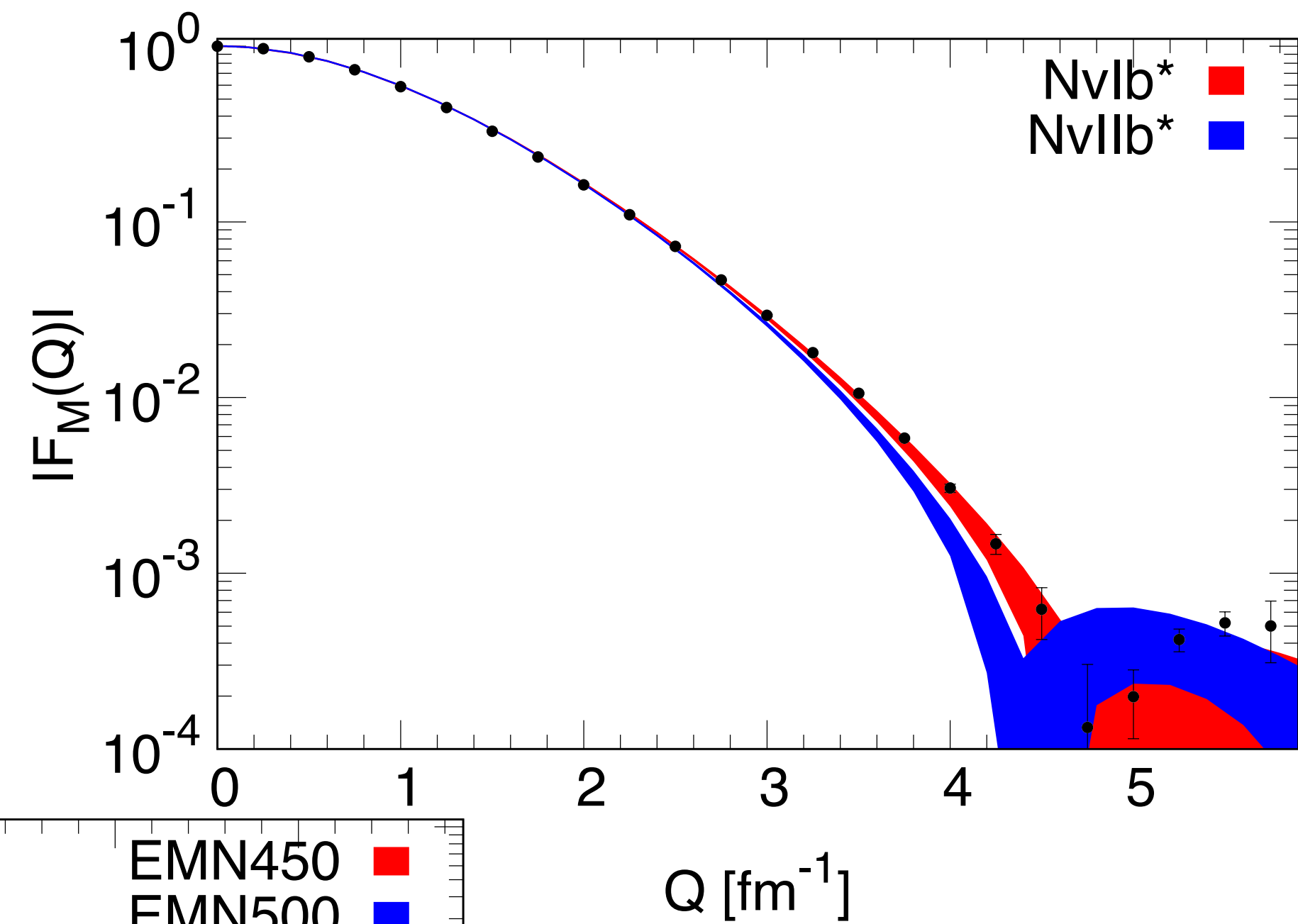
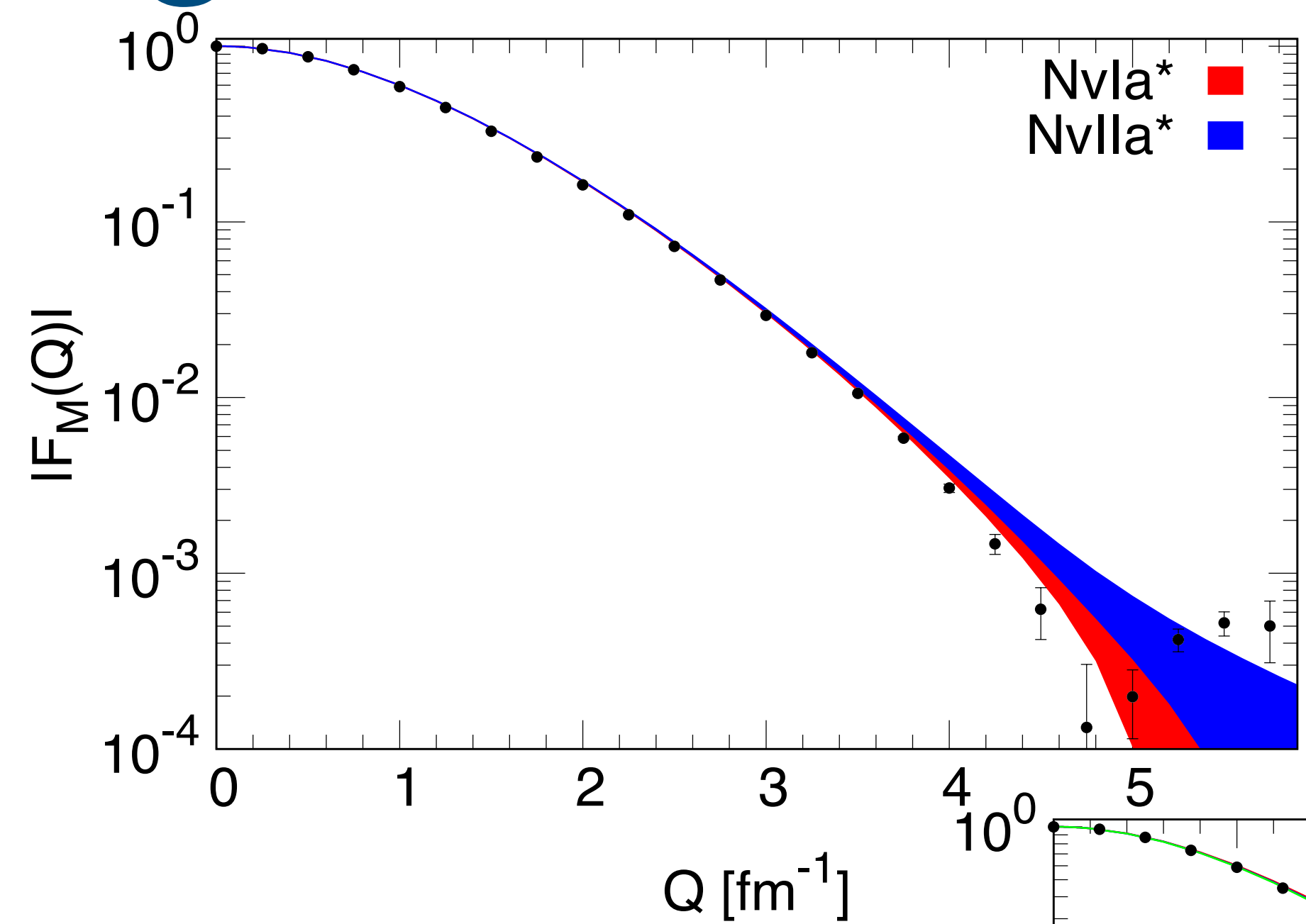
# Magnetic form factors of $^2\text{H}$



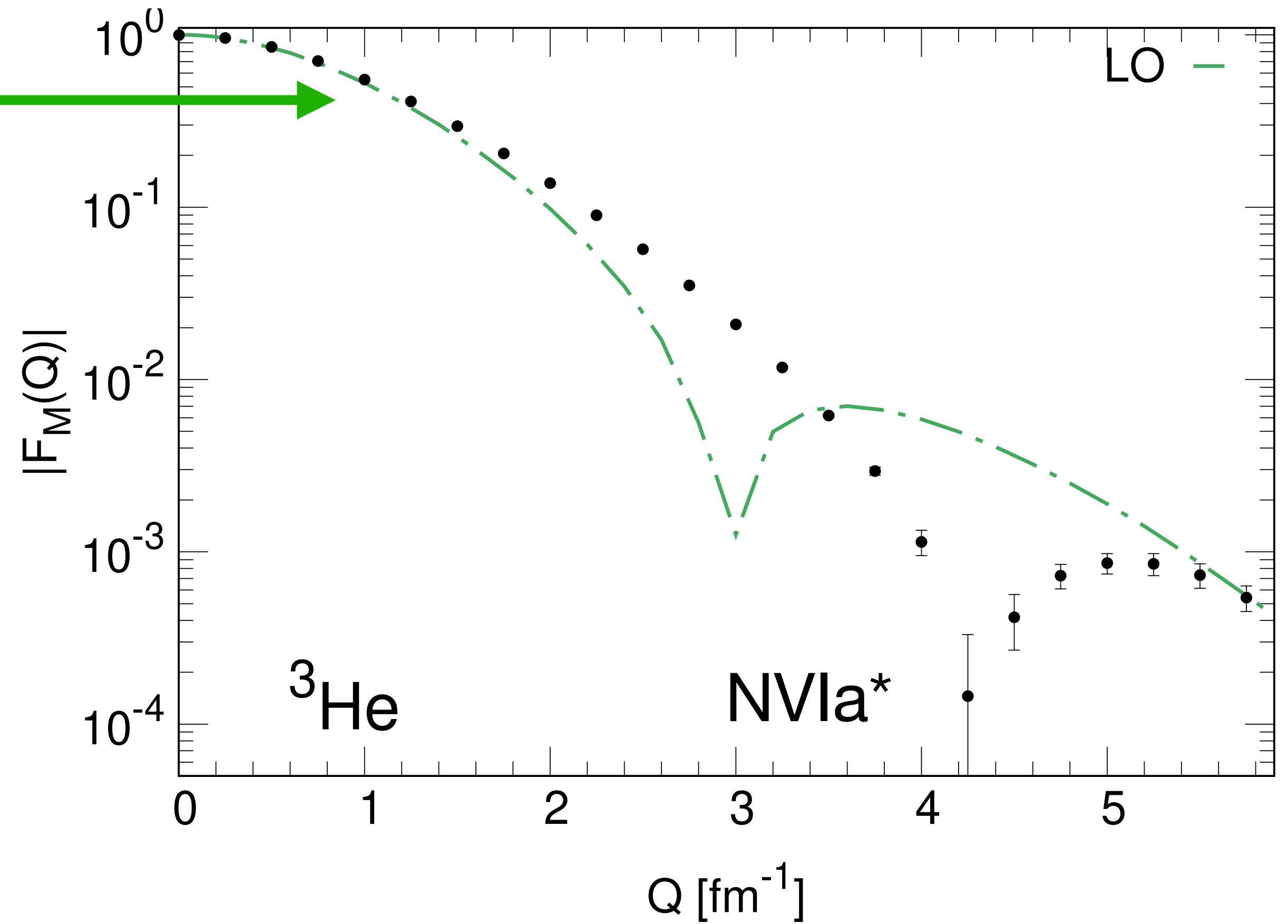
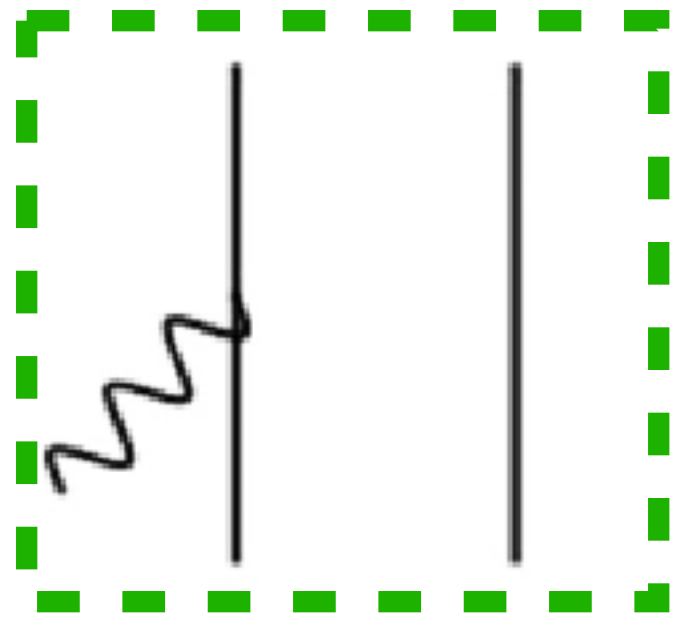
# Magnetic form factors of $^3\text{He}$



# Magnetic form factors of ${}^3\text{H}$

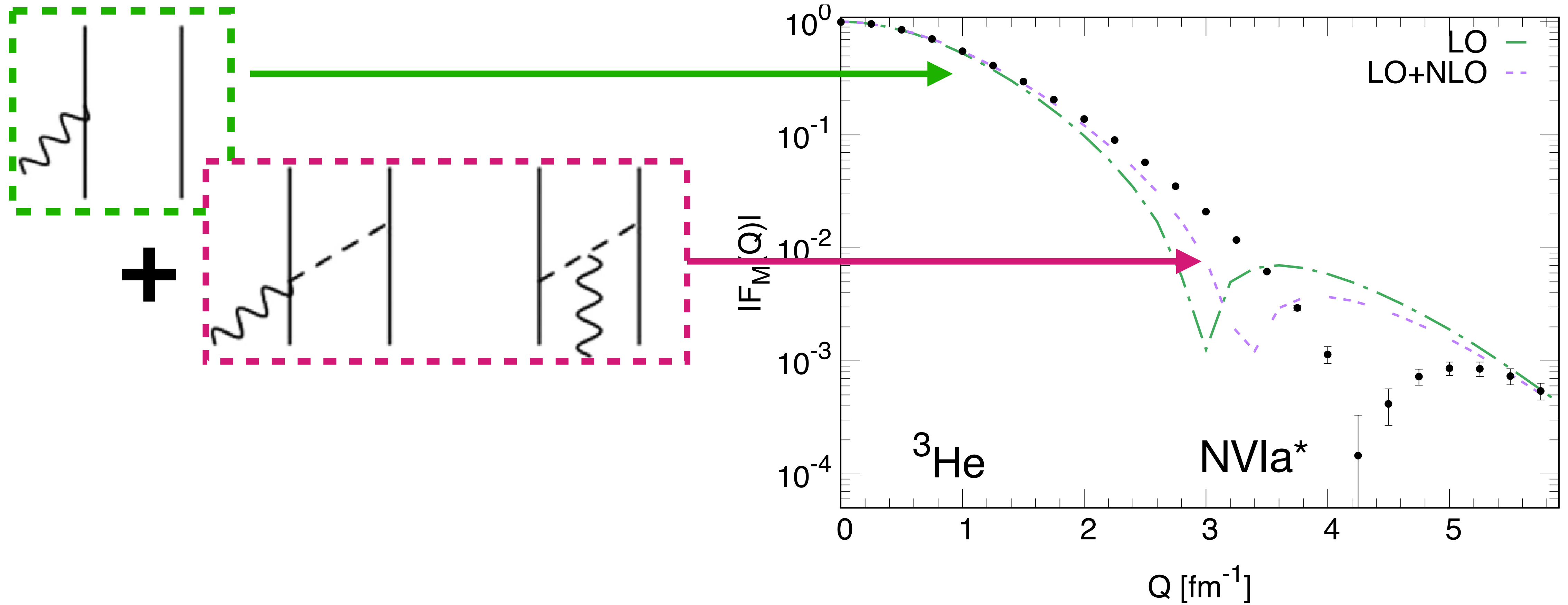


# Prediction of $A=3$ Magnetic Form Factors

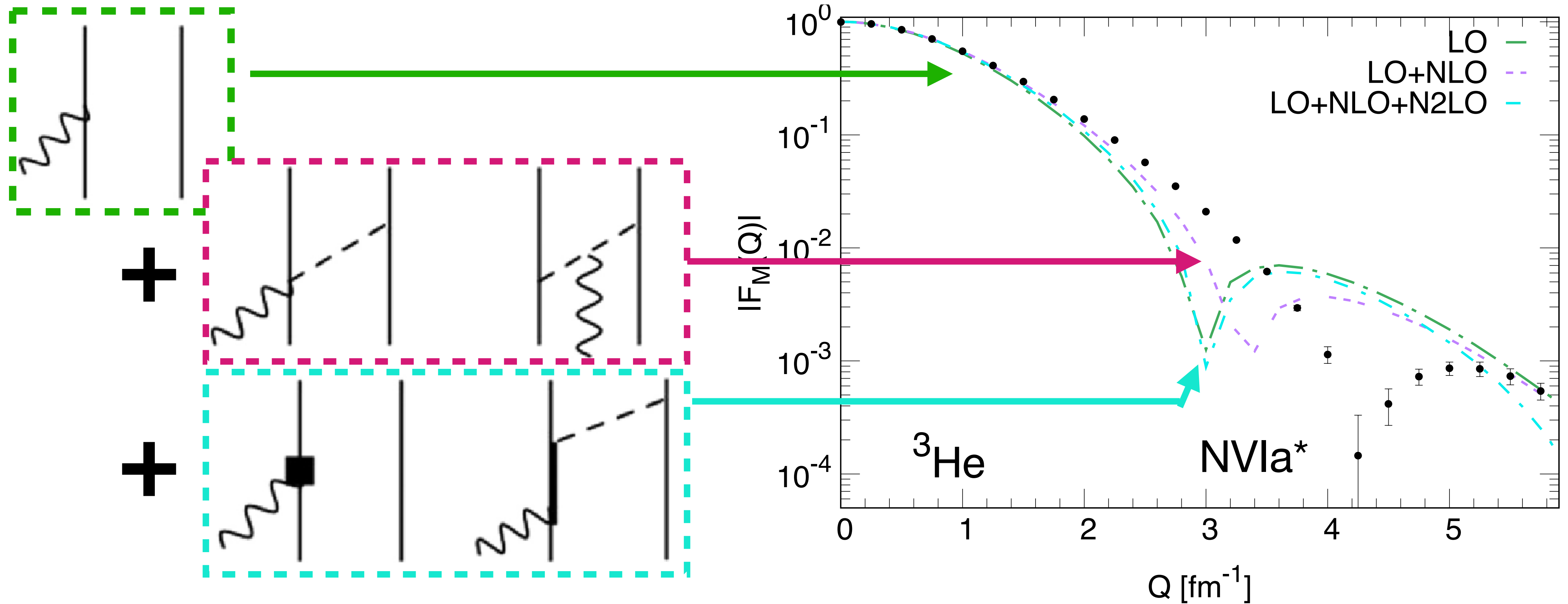




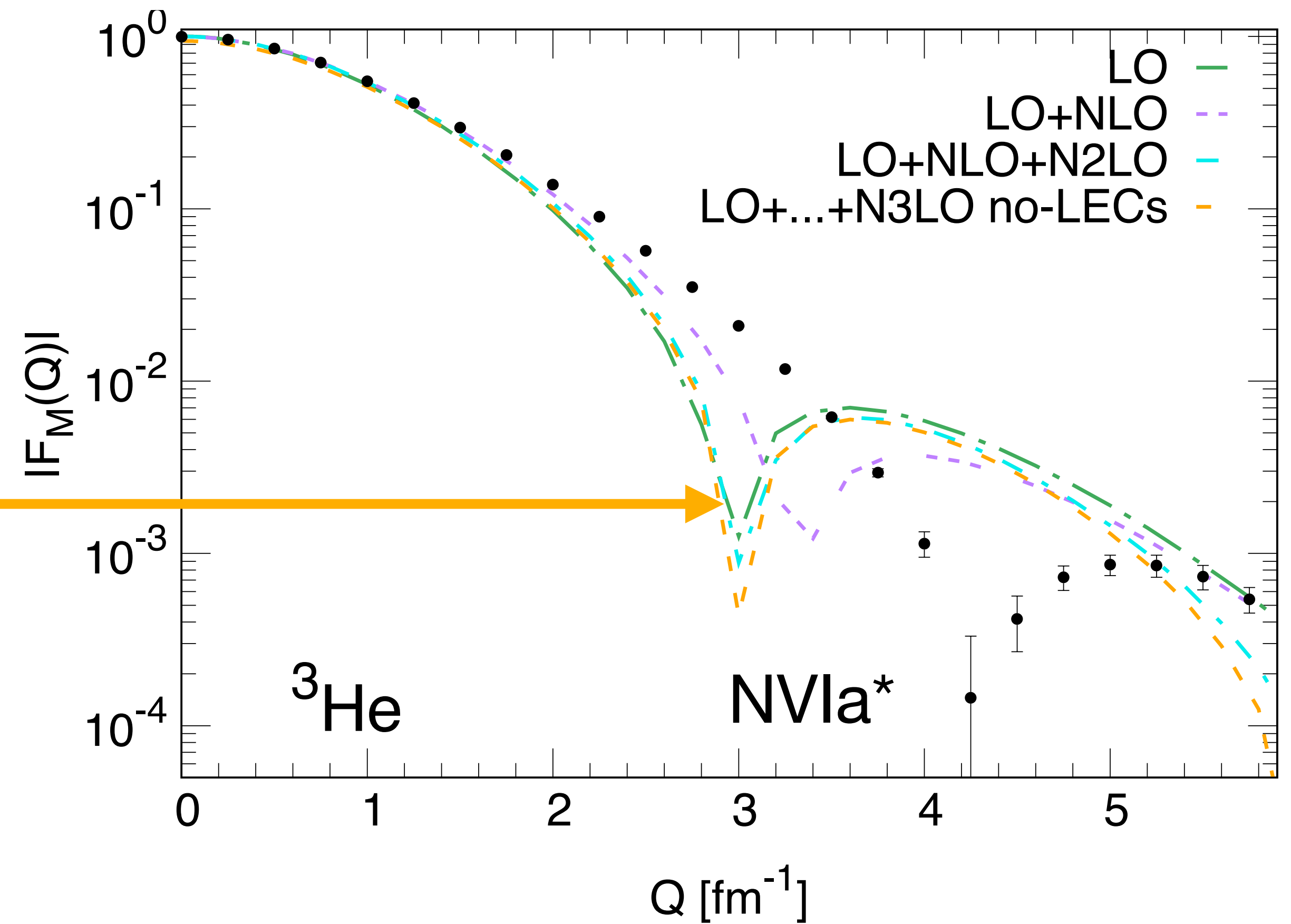
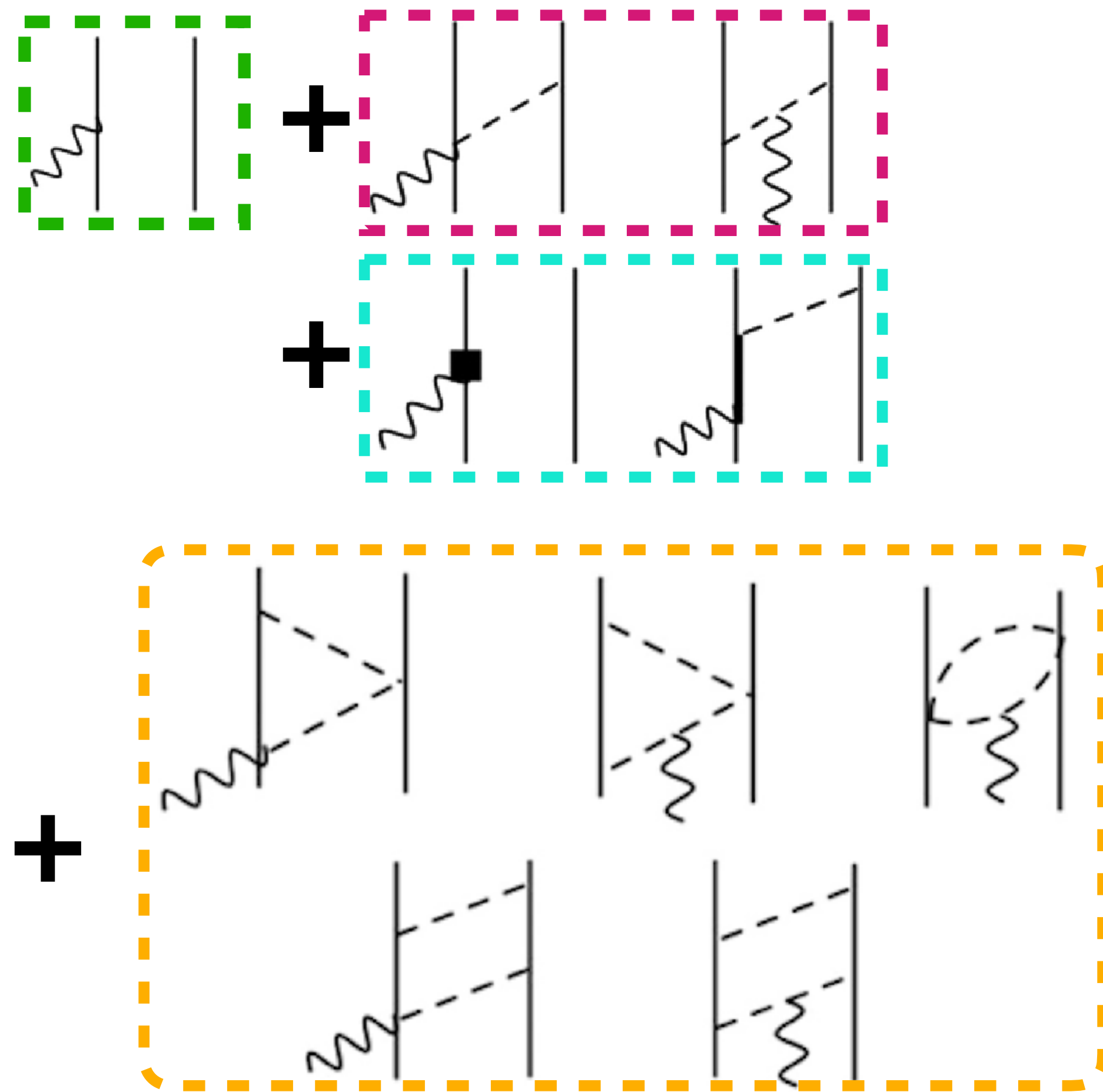
# Prediction of $A=3$ Magnetic Form Factor



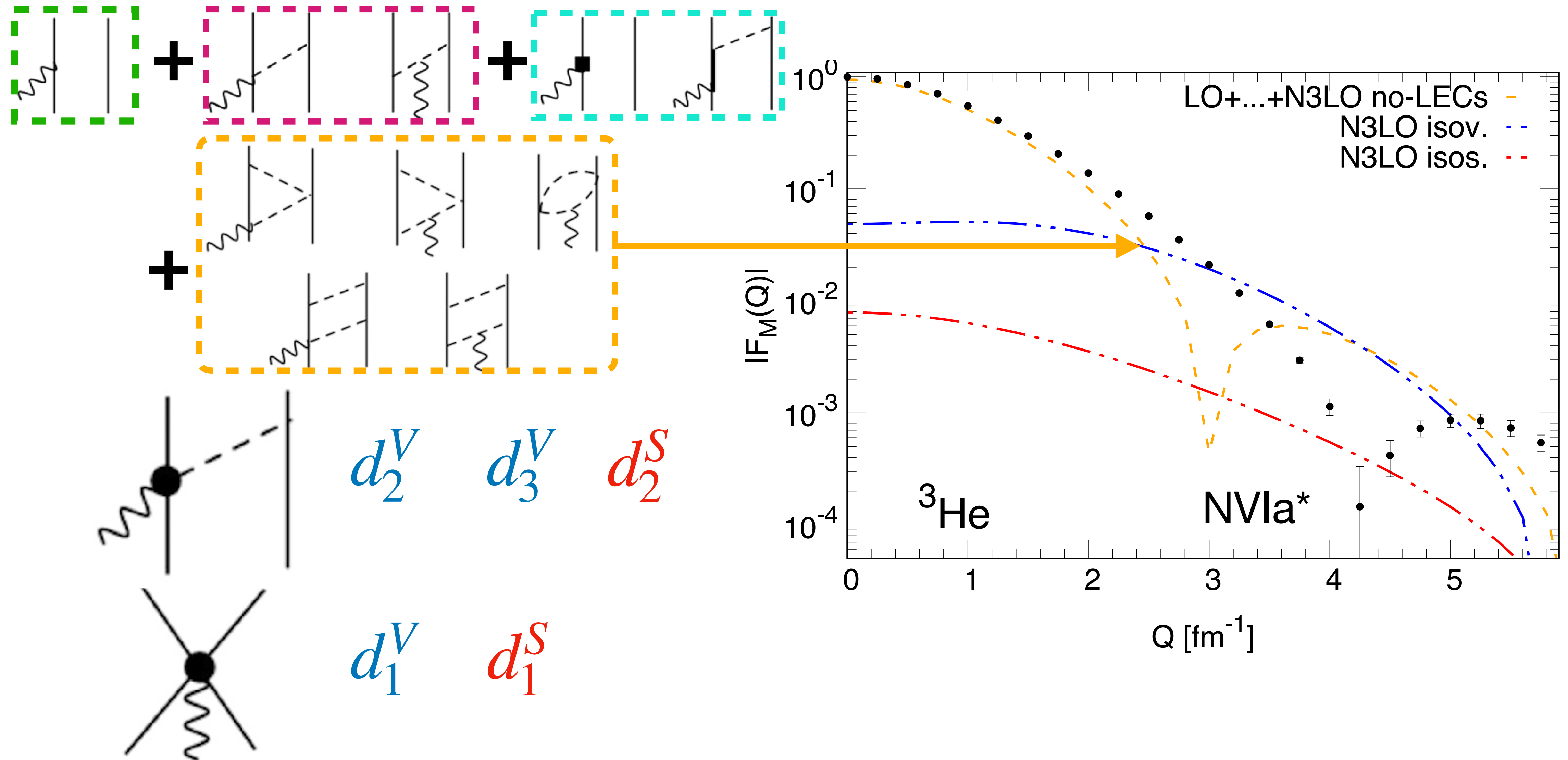
# Prediction of $A=3$ Magnetic Form Factor



# Prediction of $A=3$ Magnetic Form Factor



# Prediction of A=3 Magnetic Form Factor



# Reliability of the predictions

Is  $\chi$ EFT able to describe large  $Q$ ?

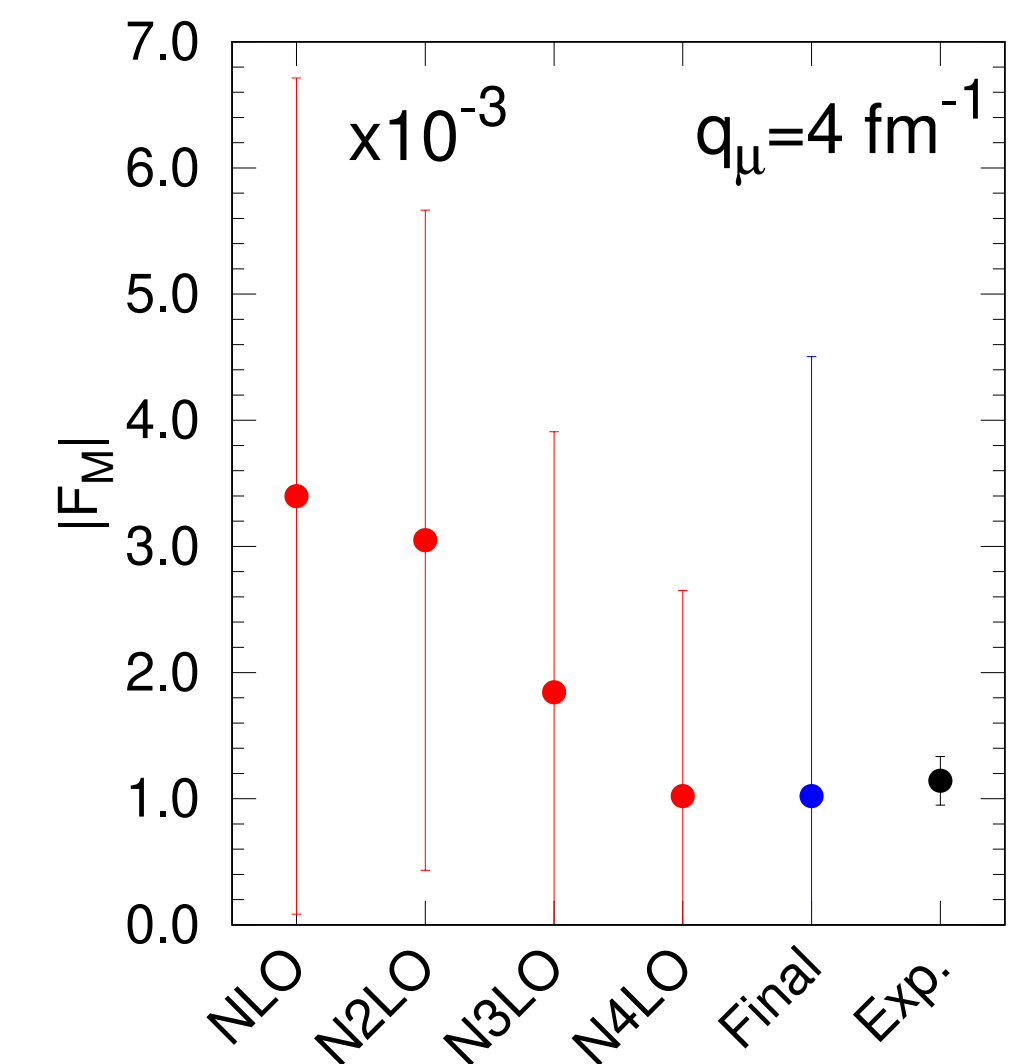
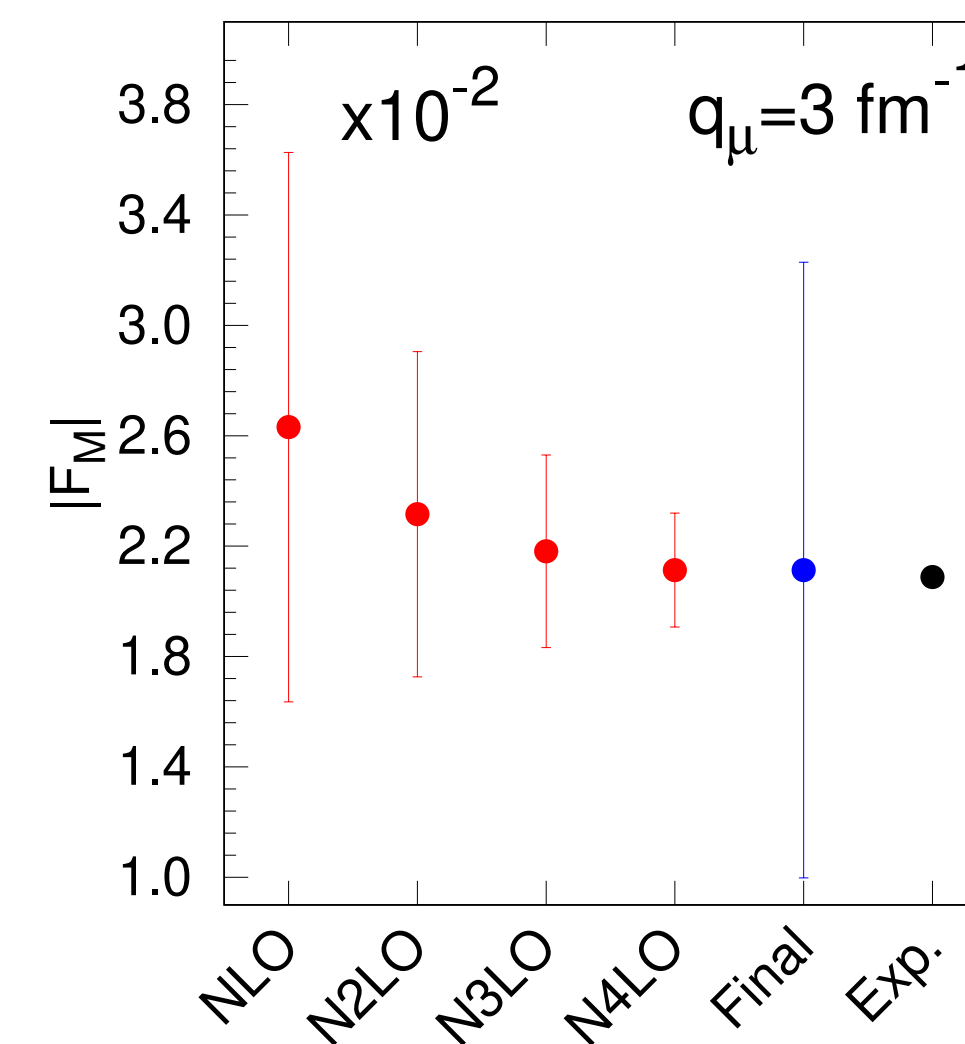
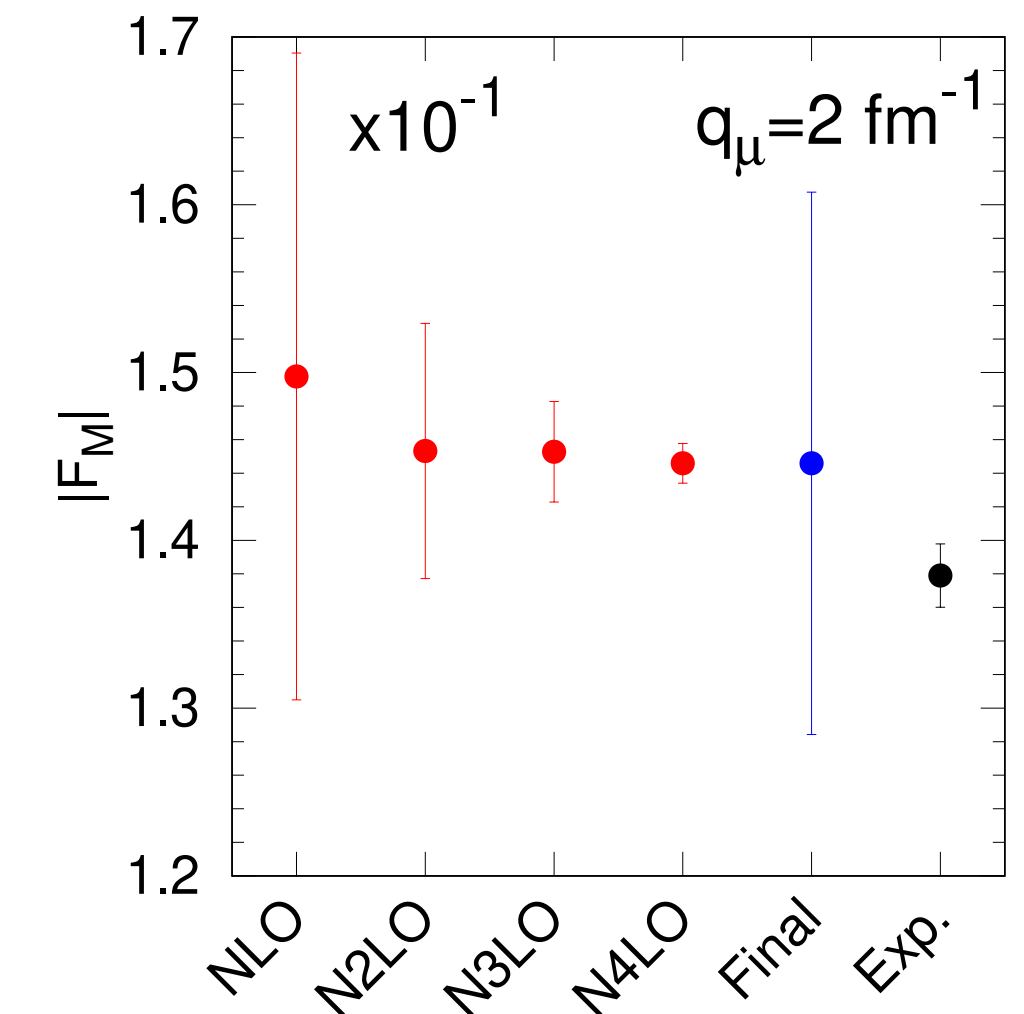
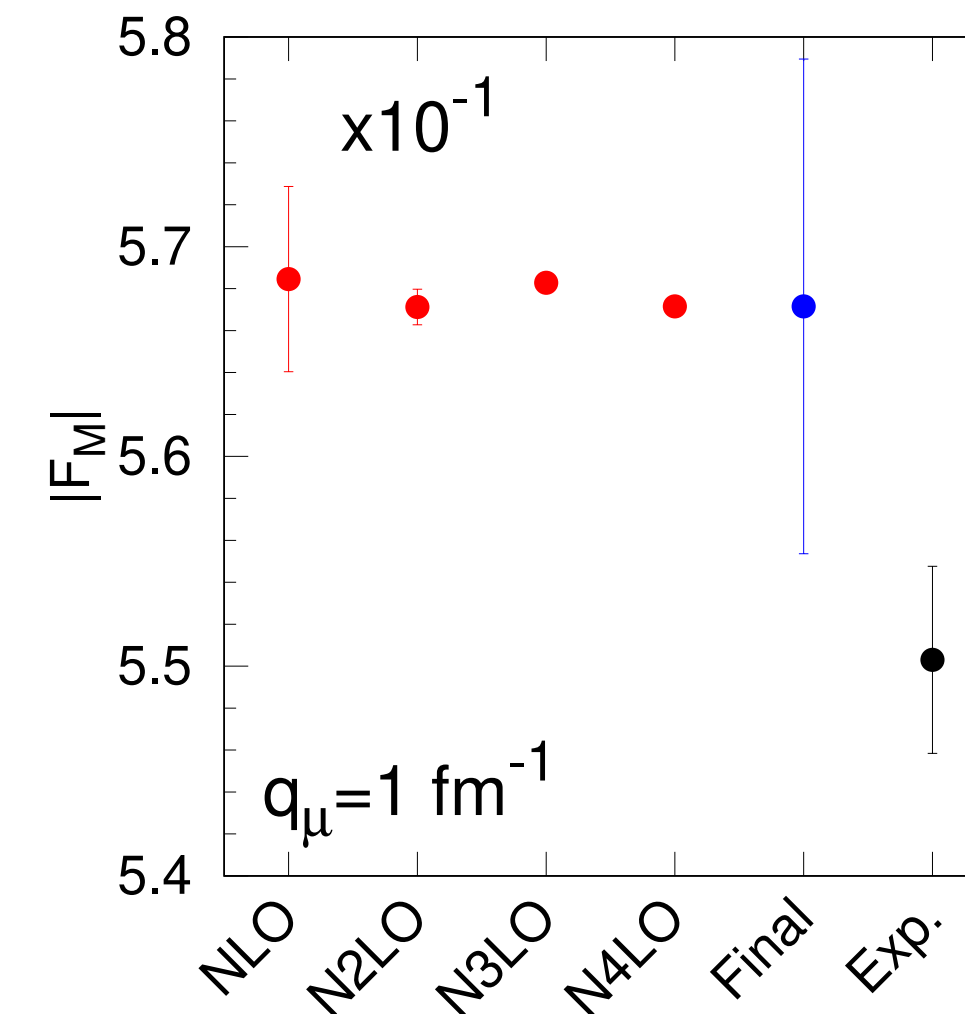
- Truncation errors (as [EPJA 51, 53 (2015)])

$$\alpha = \max \left\{ \frac{Q}{\Lambda_b}, \frac{m_\pi}{\Lambda_b} \right\} \Lambda_b = 1 \text{ GeV}$$

- Nuclear interaction + currents

- Systematic explodes after

$$Q^2 > 0.5 \text{ GeV}^2$$



$^3\text{He}$  EMN500



# Naive truncation error estimate

Is  $\chi$ EFT able to describe large  $Q^2$ ?

- Truncation errors (as [EPJA 51, 53 (2015)])

$$\alpha = \max \left\{ \frac{Q}{\Lambda_b}, \frac{m_\pi}{\Lambda_b} \right\} \Lambda_b = 1 \text{ GeV}$$

- Nuclear interaction + currents
- Systematic explodes after  $Q^2 > 0.5 \text{ GeV}^2$

