

[220-127

VI GHP Workshop, Baltimore

Apr, 201

# CUSPS AND EXOTIC CHARMONIA

Eric Swanson



Filling out the CKM matrix has been very good  
for spectroscopy!



# Focus on Charged & Heavy States [hence four-quark states(?)]

$\pi\pi J/\psi$   
 $\pi D\bar{D}^*$

$Z_c(3900)$



$\pi\pi h_c$   
 $\pi D^*\bar{D}^*$

$Z_c(4025)$



$K\pi\chi_{cJ}$

$Z_1(4050)$   
 $Z_2(4250)$



$K\pi J/\psi$

$Z_c(4200)$



$\pi K\psi'$

$Z_c(4475)$



$\pi\pi\Upsilon(nS)$   
 $\pi\pi h_b(nP)$   
 $\pi B\bar{B}^*$

$Z_b(10610)$   
 $Z_b(10650)$



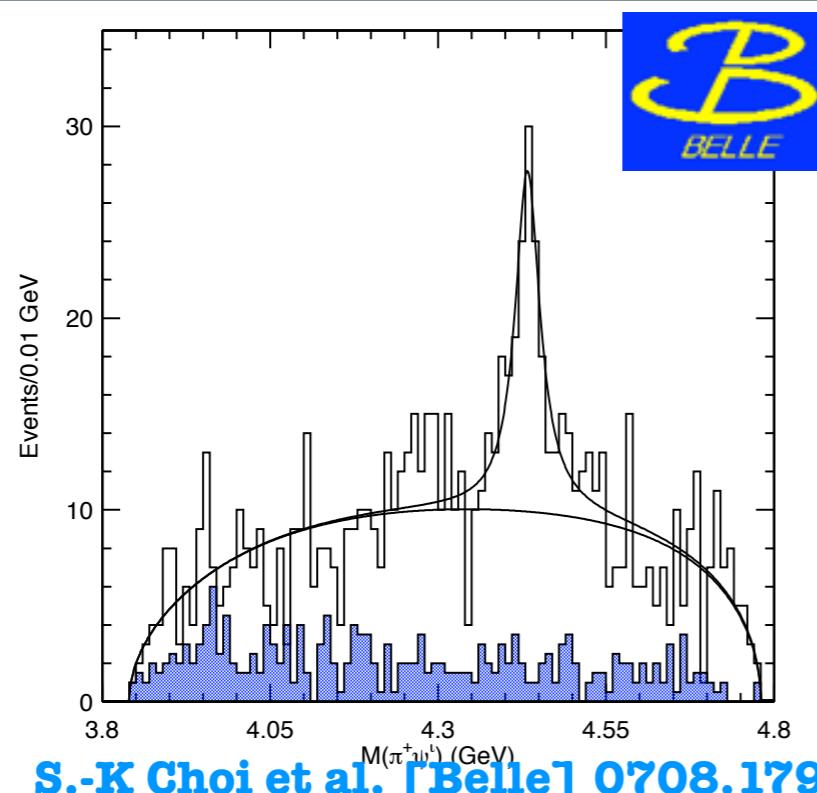
$Z(4430)|Z(4475)/$   
 $Z(4200)$

# $Z^+(4430)$

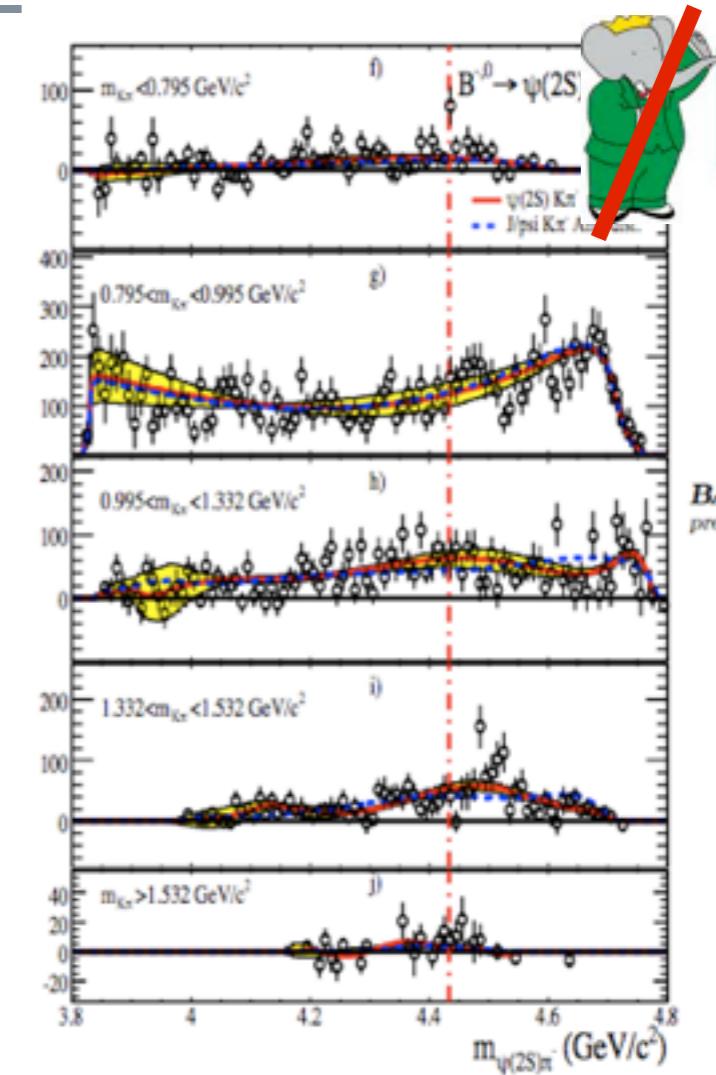
$$B \rightarrow K\pi^+\psi'$$

$$\begin{aligned} M &= 4443^{+24}_{-18} \\ \Gamma &= 107^{+113}_{-71} \\ J^{PC} &=? \end{aligned}$$

- .manifestly exotic
- .not confirmed by BaBar



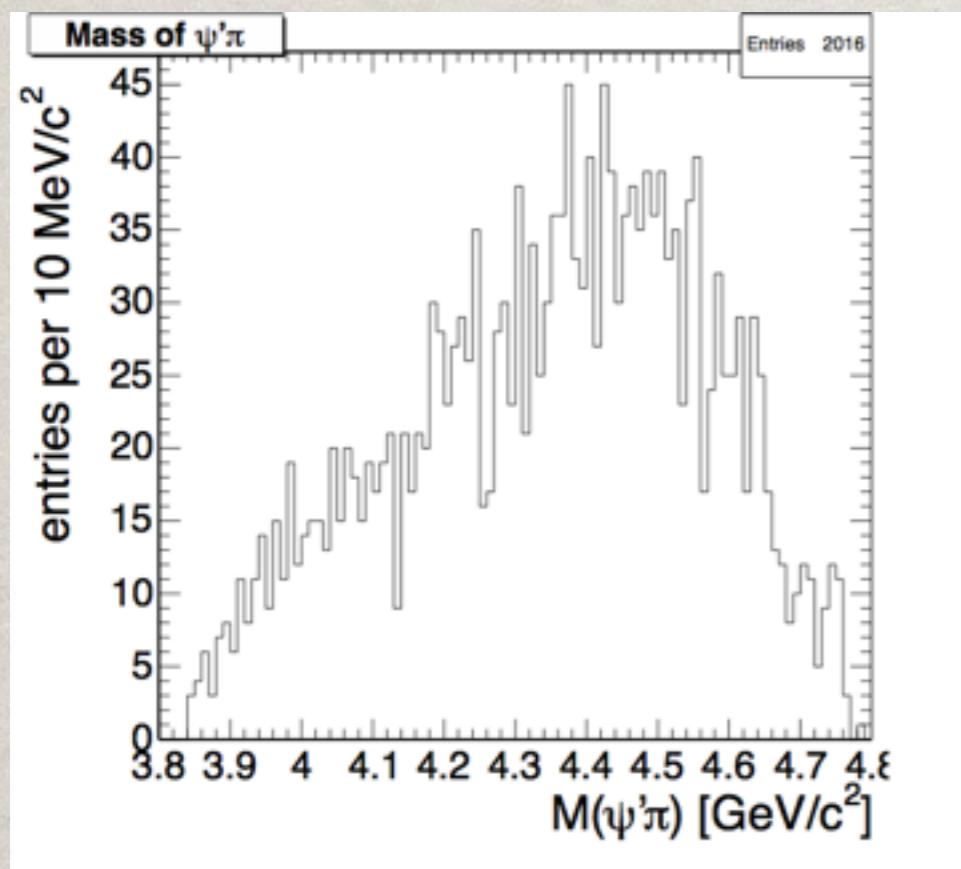
S.-K Choi et al. [Belle] 0708.1790



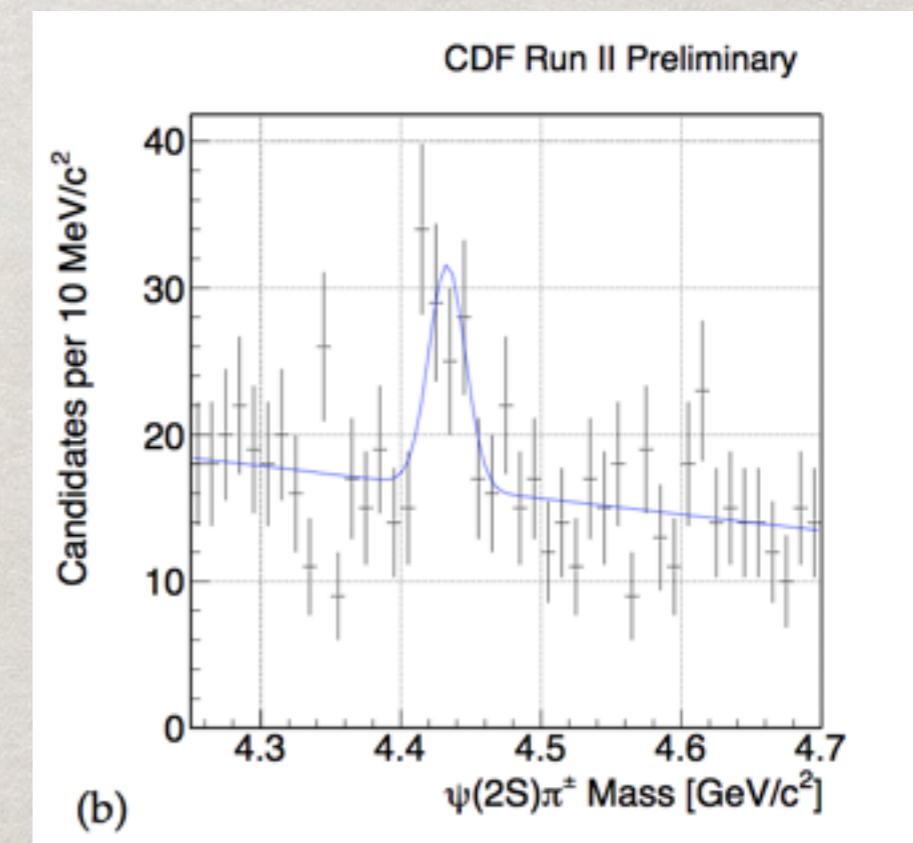
Mokhtar. 0810.1073

# $Z^+(4430)$

$pp \rightarrow B\bar{B}(\pi^- K^+ \psi')$



prompt production

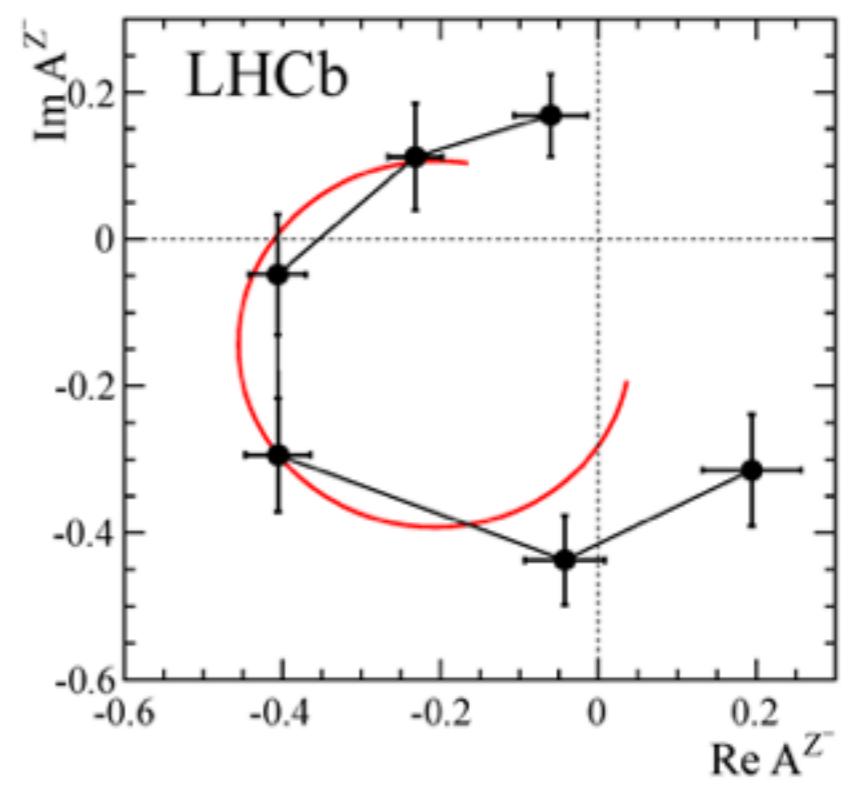
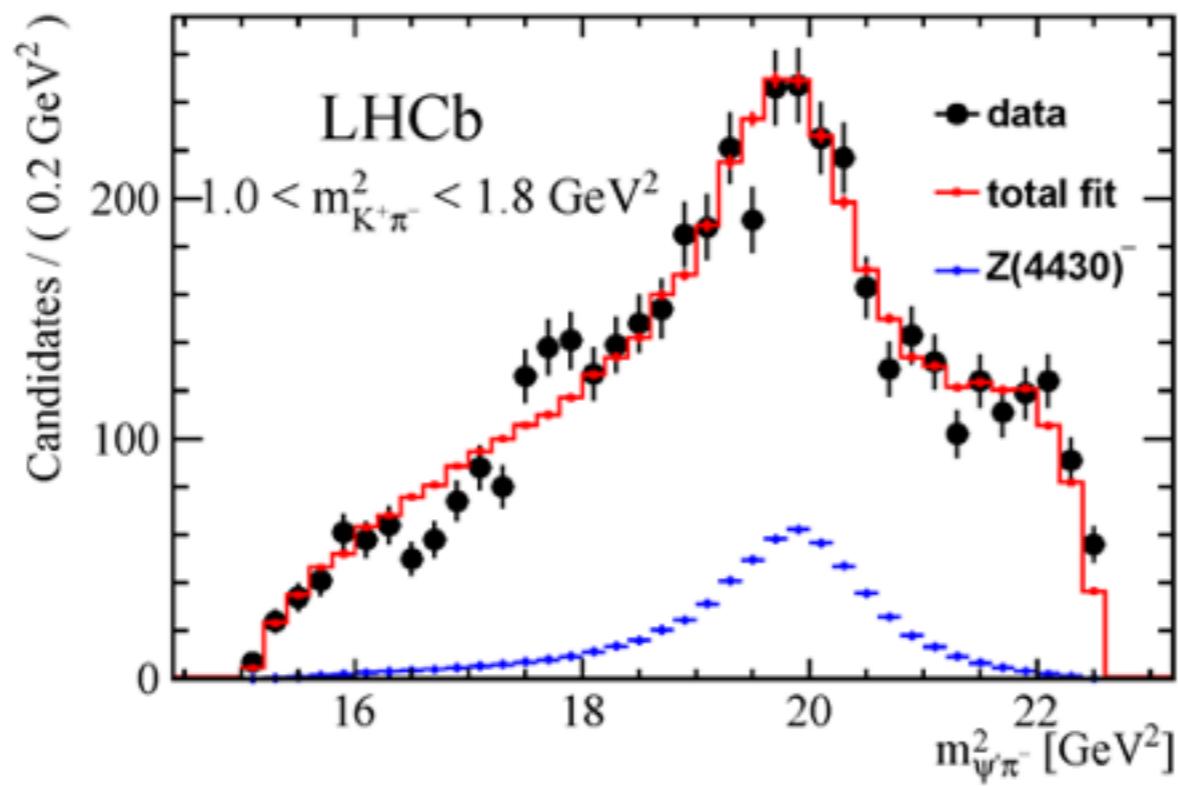


F. Rubbo, Torino thesis

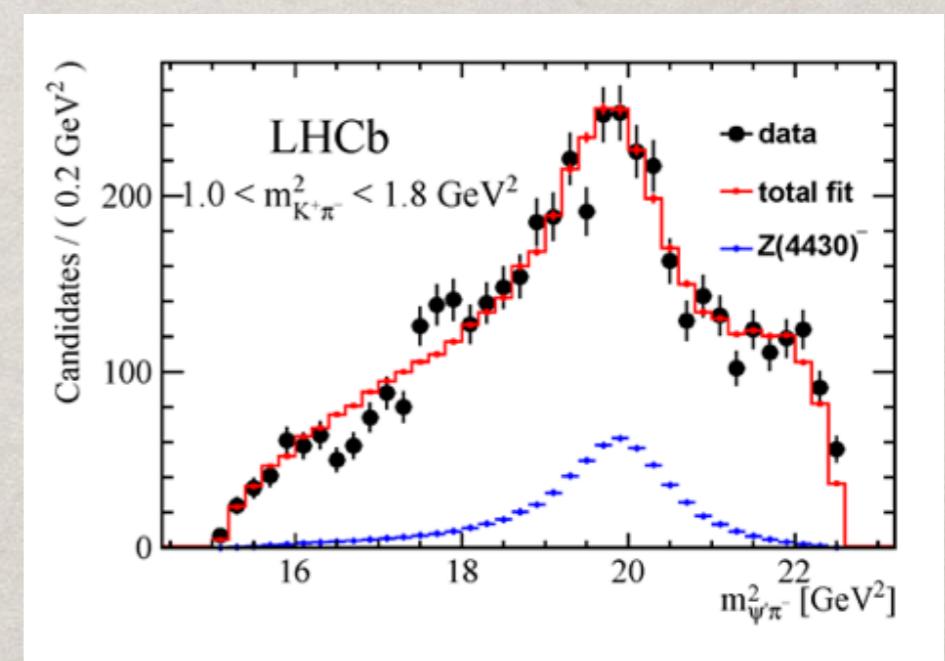
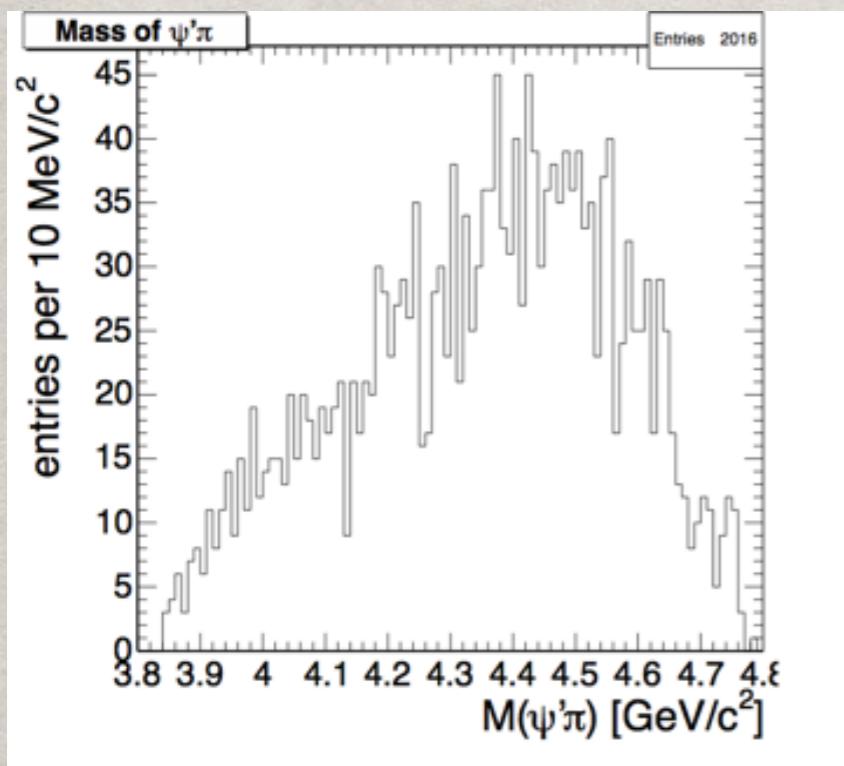
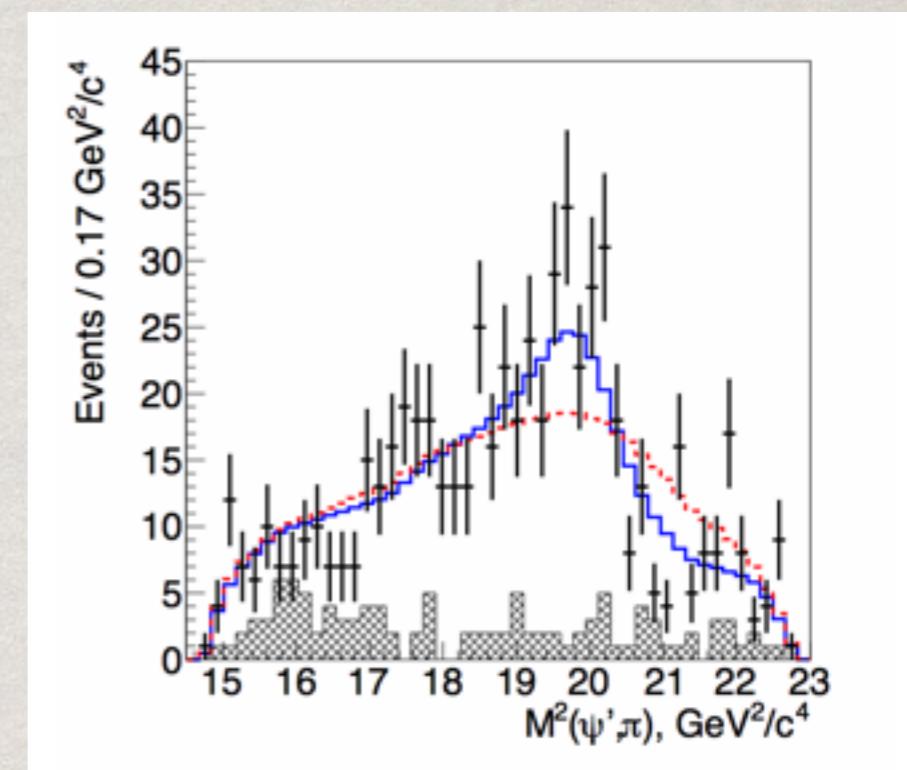
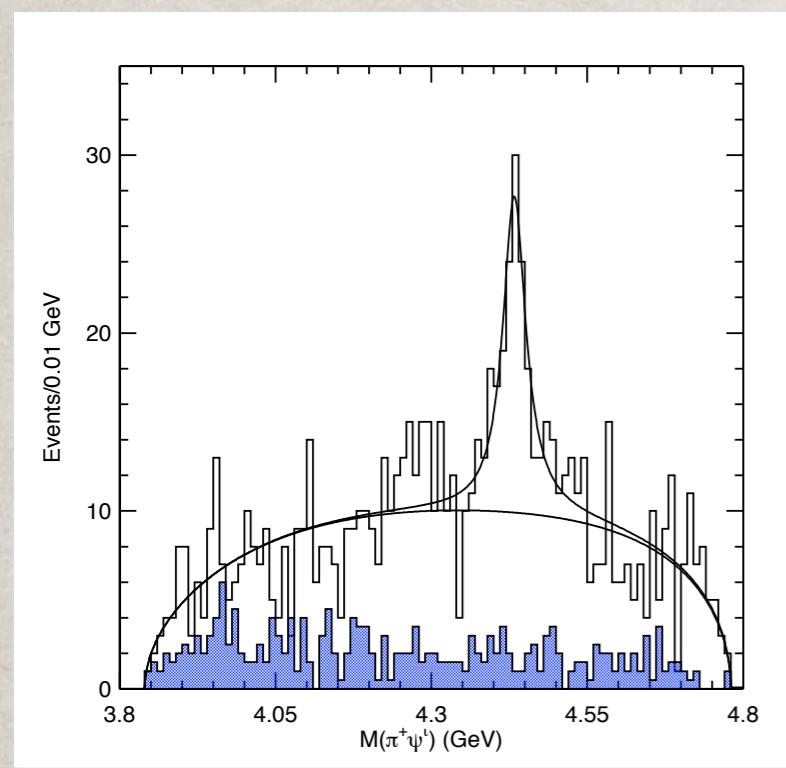
# $Z^+(4430)$

• confirmed by LHCb

$$J^P = 1^+$$



# $Z^+(4430)$



# Systematics: second exotic Z?

- Fit confidence level increases to 26% with a second exotic ( $J^P=0^-$ ) component, but...
  - No evidence for  $Z_0$  in model independent approach.
  - Argand diagram for  $Z_0$  is inconclusive.
- Need larger samples to characterise this state.

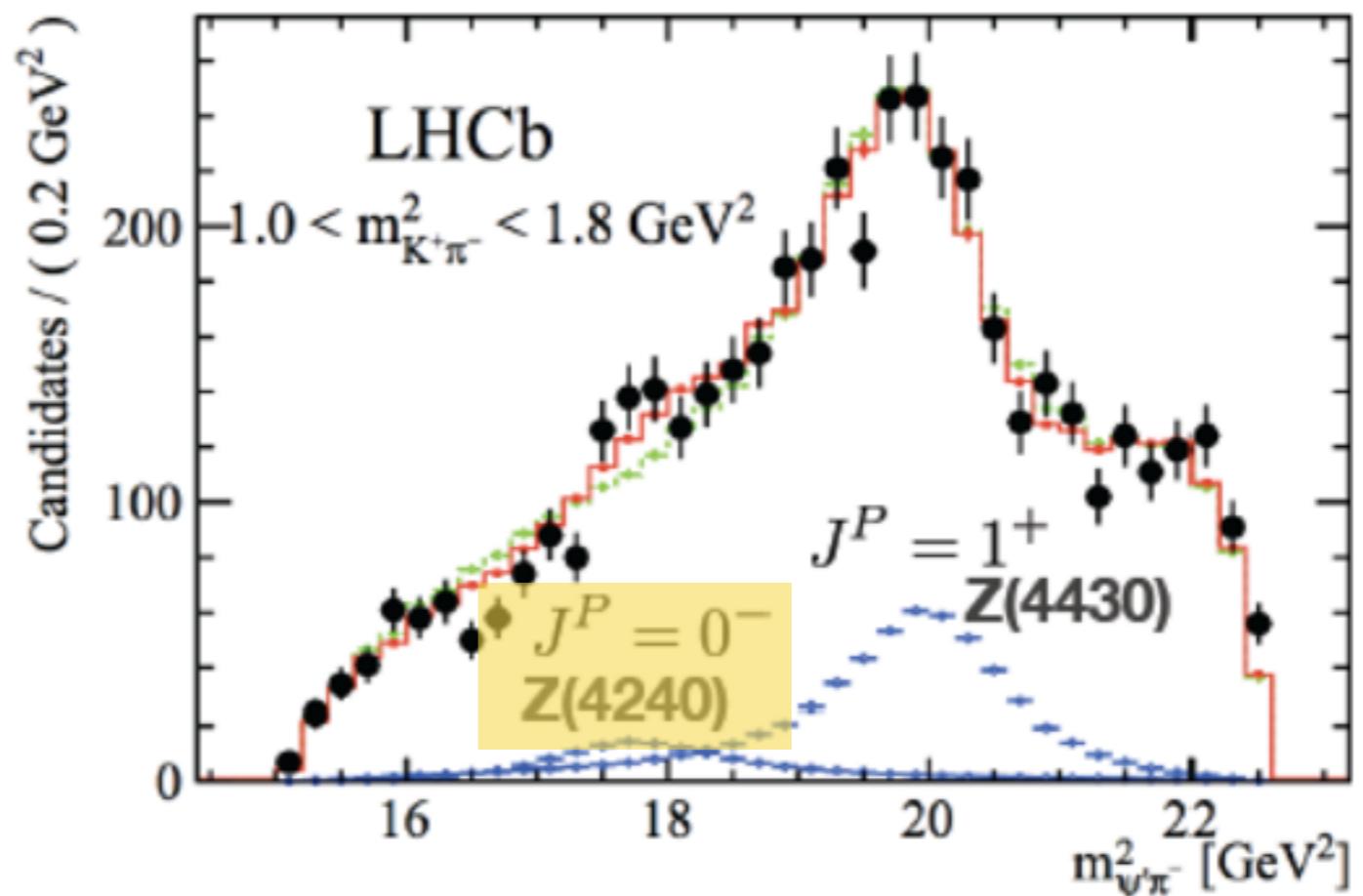
Significance from  
 $\Delta(-2 \ln L)$   
 $6\sigma$

Fitted parameters

$$M_{Z_0} = 4239 \pm 18^{+45}_{-10} \text{ MeV}$$
$$\Gamma_{Z_0} = 220 \pm 47^{+108}_{-74} \text{ MeV}$$
$$f_{Z_0} = (1.6 \pm 0.5^{+1.9}_{-0.4})\%$$

Same mass, width as  $Z^- \rightarrow \chi_{c1}\pi^-$  seen by Belle, but  $J^P=0^-$  can't decay strongly to  $\chi_{c1}\pi^-$

[PRD 78 (2008) 072004]



- Many checks performed to determine stability of the result and evaluate systematic errors on  $m_Z$ ,  $\Gamma_Z$ ,  $f_Z$ .
- Main systematics come from assumption on  $K^+\pi^-$  Isobar model, efficiency

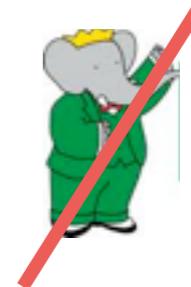
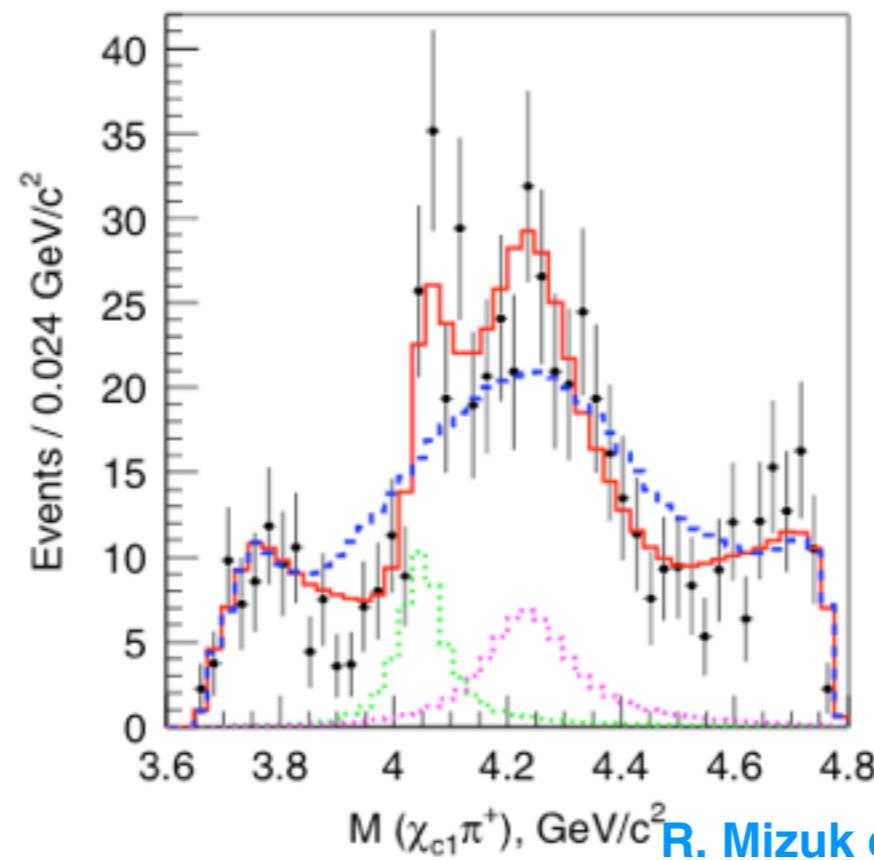
**Z<sub>1</sub> & Z<sub>2</sub>**

$Z_1(4050)$

$Z_2(4250)$

$$B \rightarrow ZK \rightarrow \chi_{c1}\pi K$$

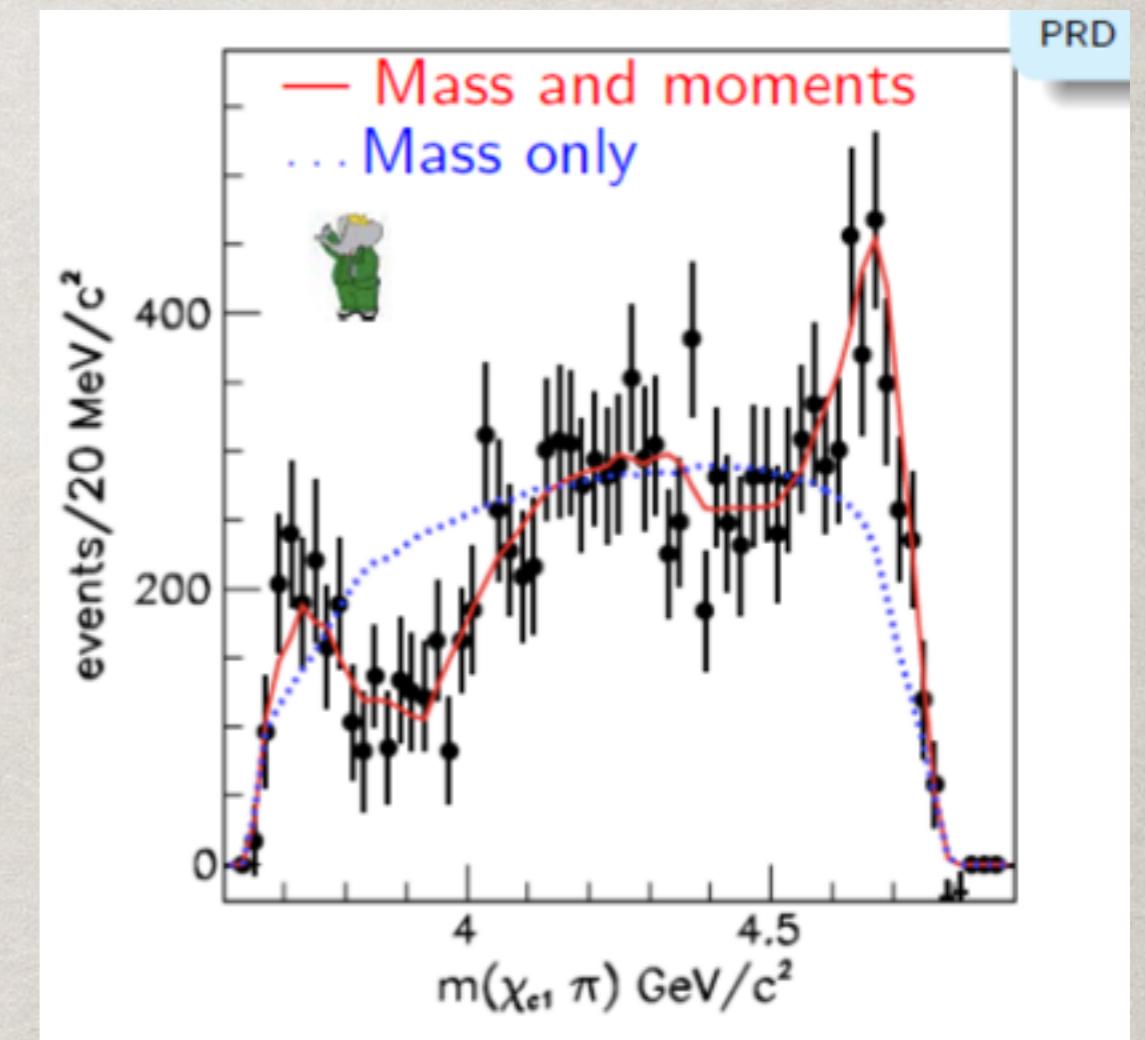
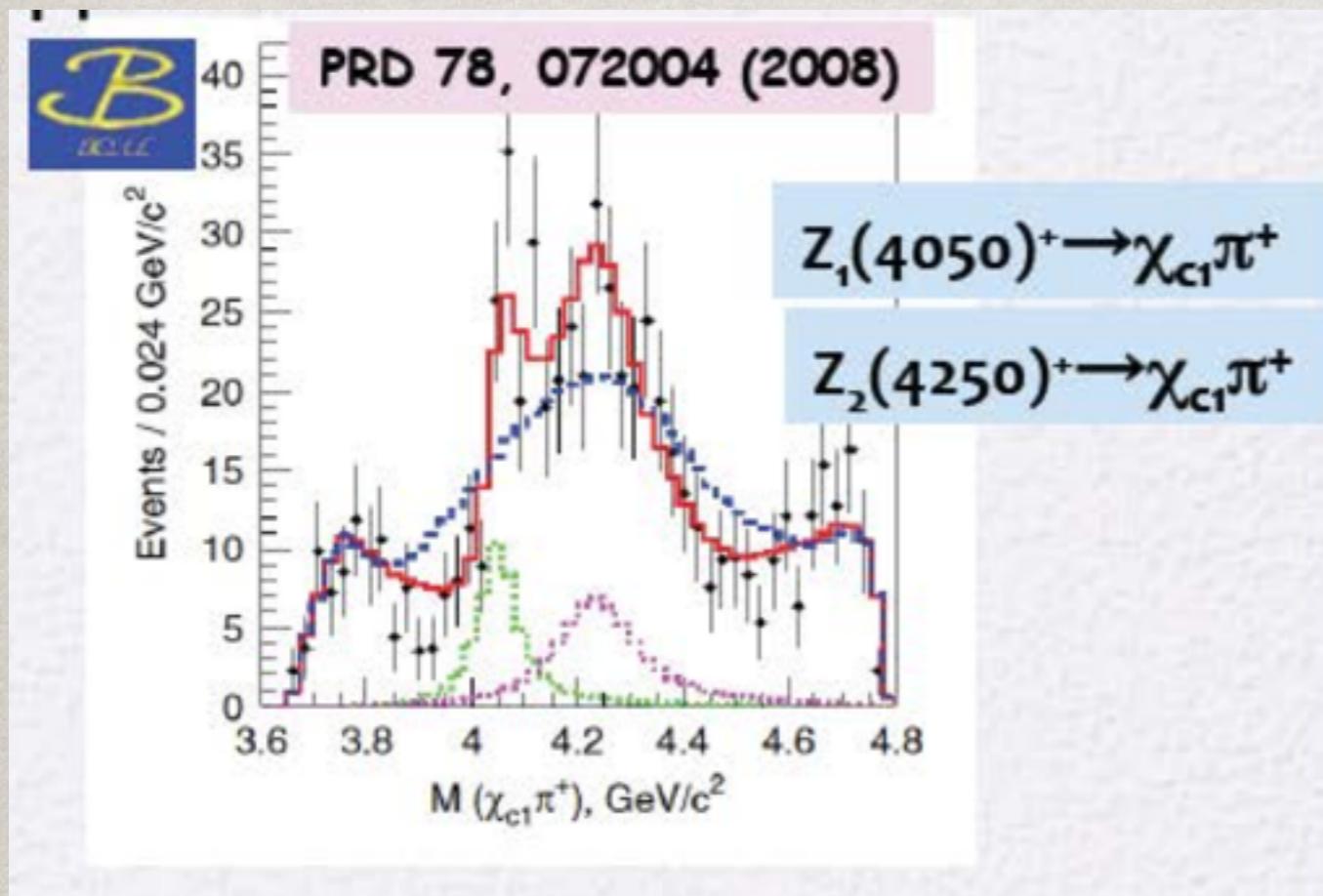
- manifestly exotic
- dubious



R. Mizuk et al. [Belle], PRD76, 072004 (08)

$Z_1(4050)$

$Z_2(4250)$

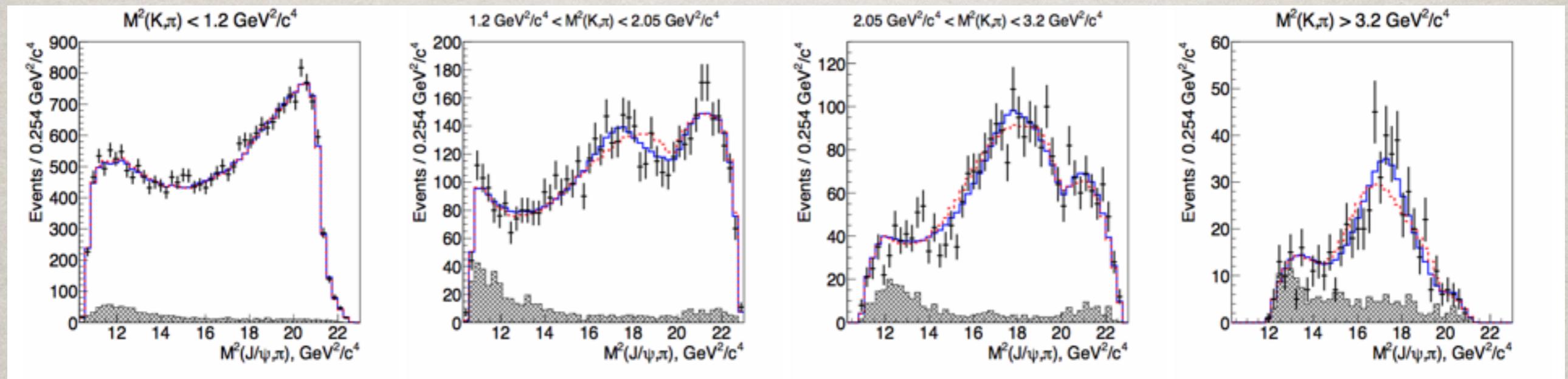


good fit with only K resonances!

ZC(4200)

# $Z_c(4200)$

$B \rightarrow K\pi J/\psi$



dotted: without  $Z_c(4200)$



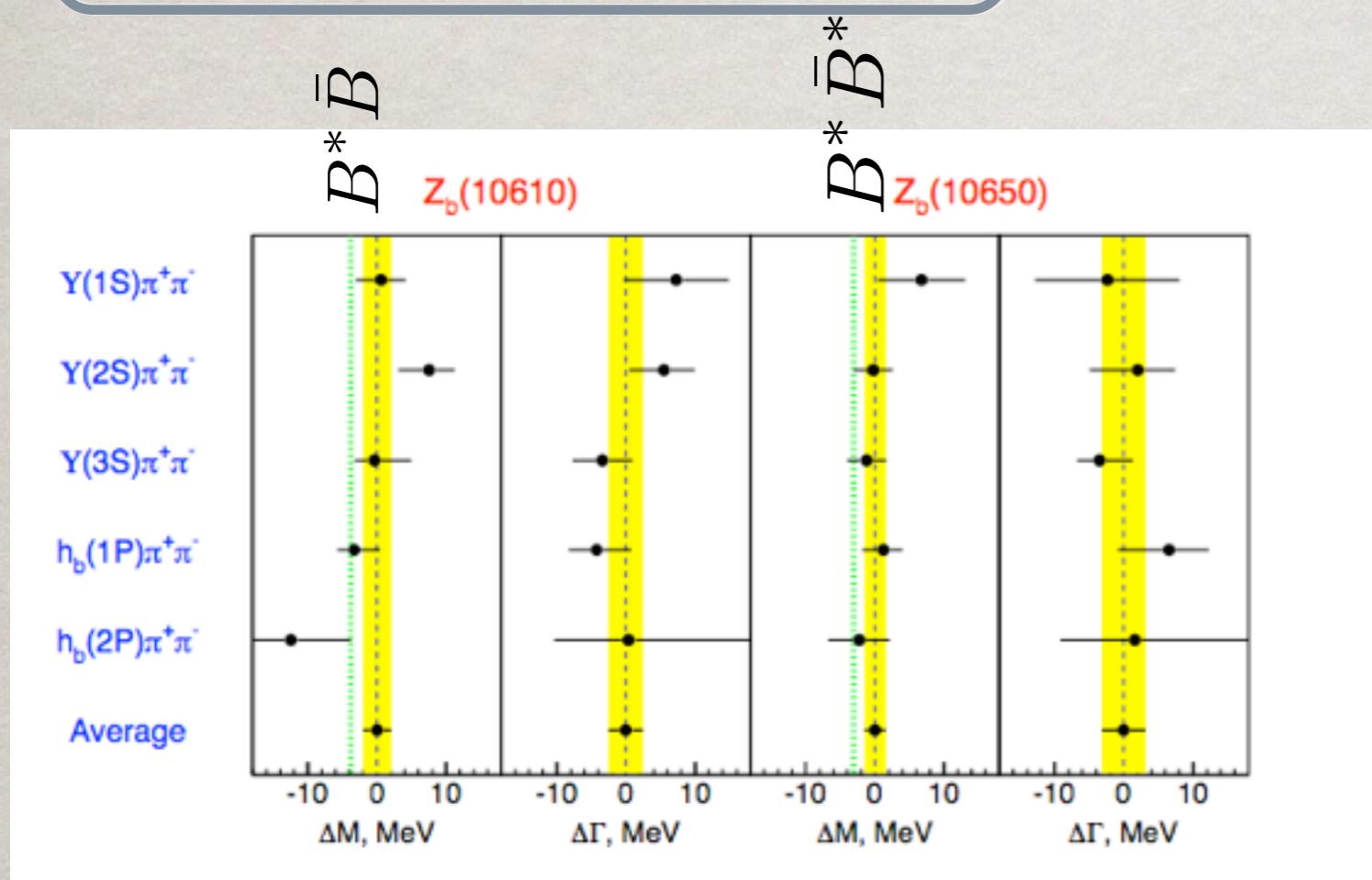
CUSP STATES

BOTTOM ZS

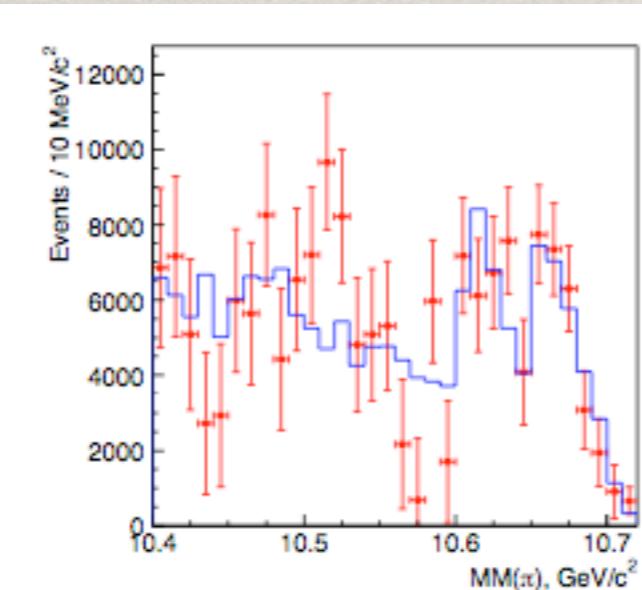
$Z_b^+(10610)$      $Z_b^+(10650)$

Adachi et al. [Belle] 1105.4583

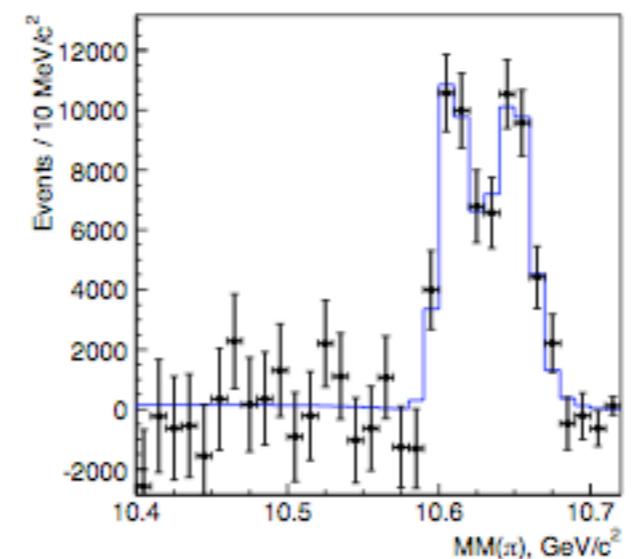
$I^G J^P = 1^+ 1^+$



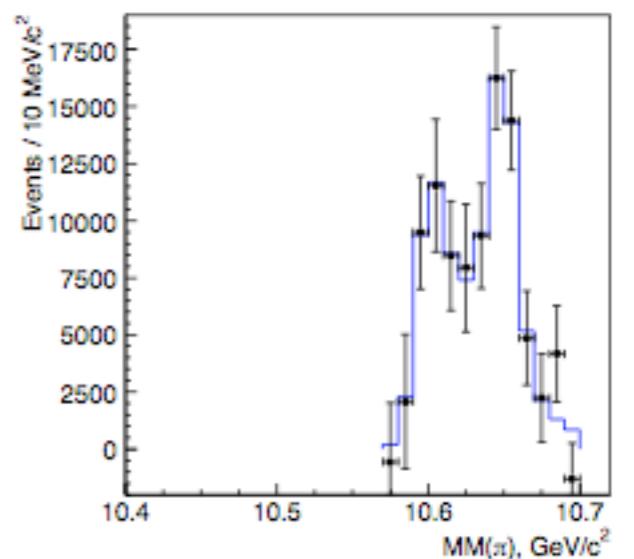
$\Upsilon(2S)$



$h_b(1P)$



$h_b(2P)$



CHARM ZS

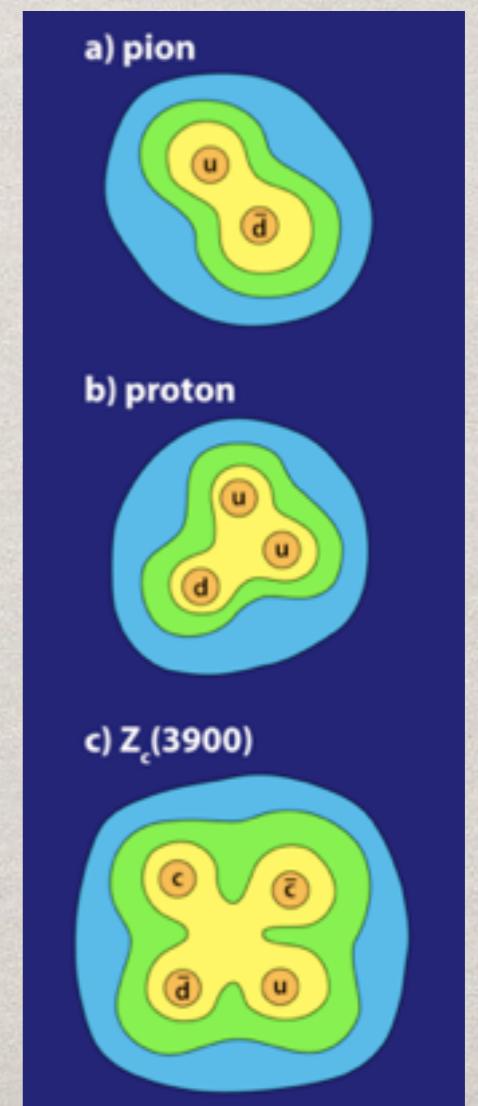
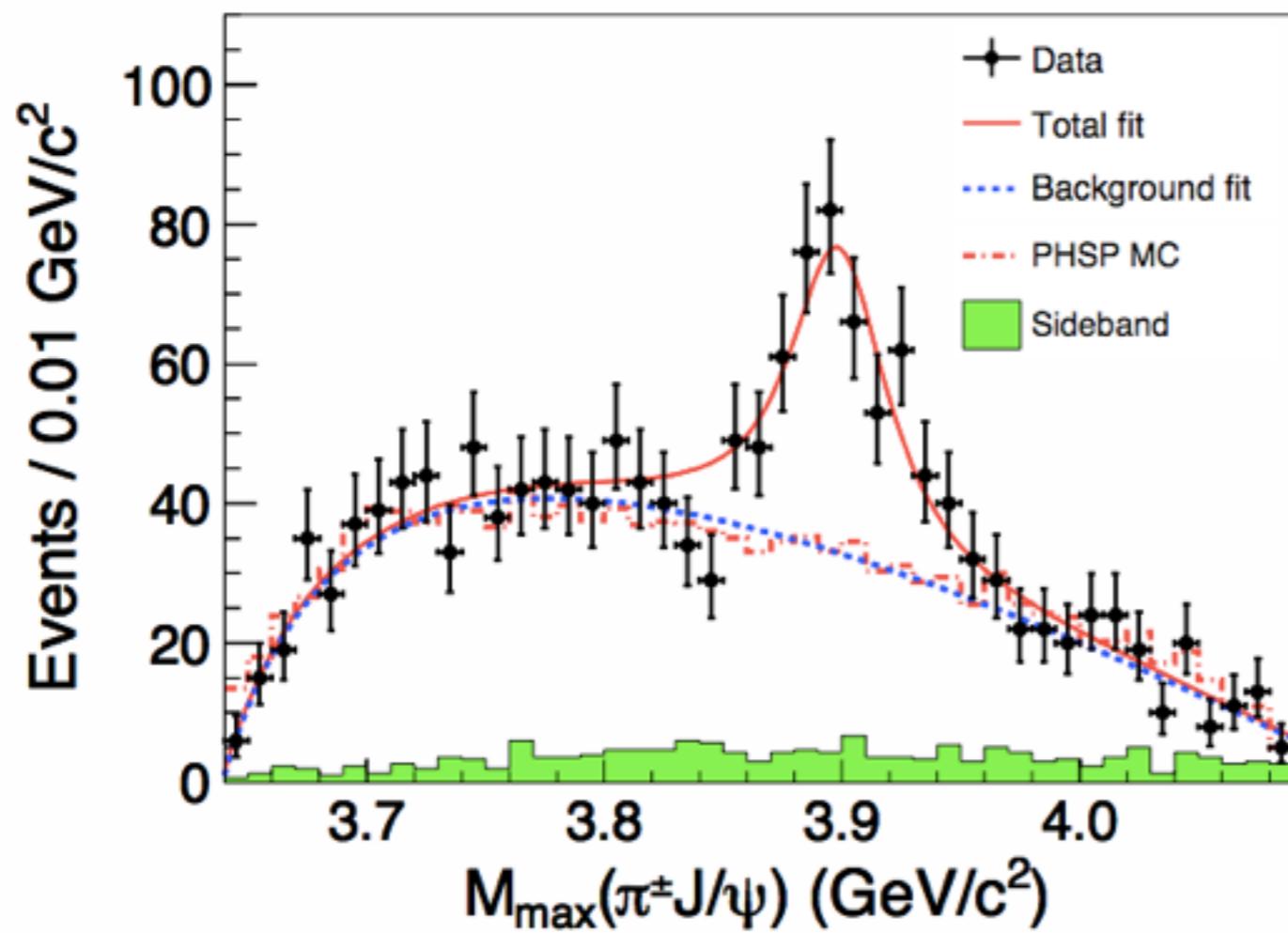
# Zc(3900)

$$e^+ e^- \rightarrow Y(4260) \rightarrow \pi\pi J/\psi$$

M. Ablikim et al. [BESIII], PRL (13)

A.Q. Lin et al. [Belle], PRL (13)

$$M = 3899 (3.6) (4.98) \quad \Gamma = 46(10)(20)$$

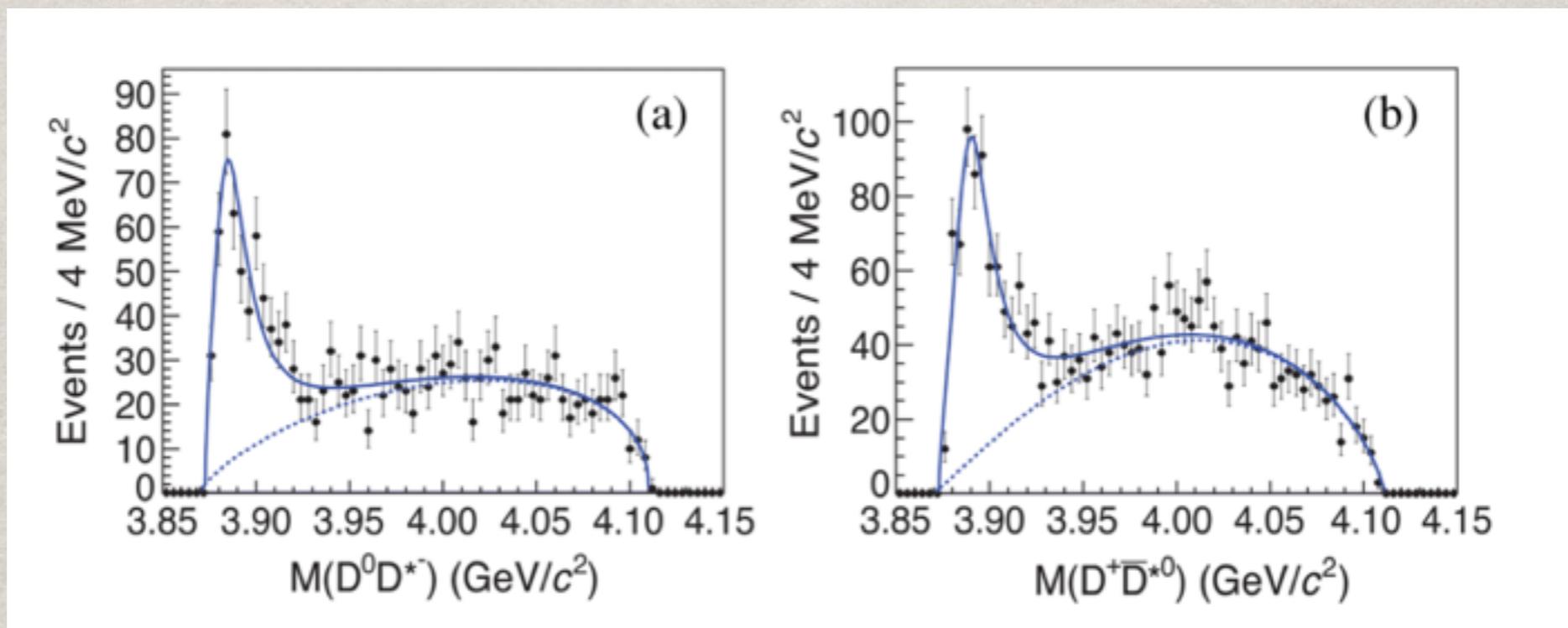


# Zc(3900)

$$e^+ e^- \rightarrow \pi D \bar{D}^* \quad \sqrt{s} = 4.26$$

$$M = 3883.9 \pm 1.5 \pm 4.2$$

$$\Gamma = 24.8 \pm 3.3 \pm 11.0$$



# $Z_c(4025)$

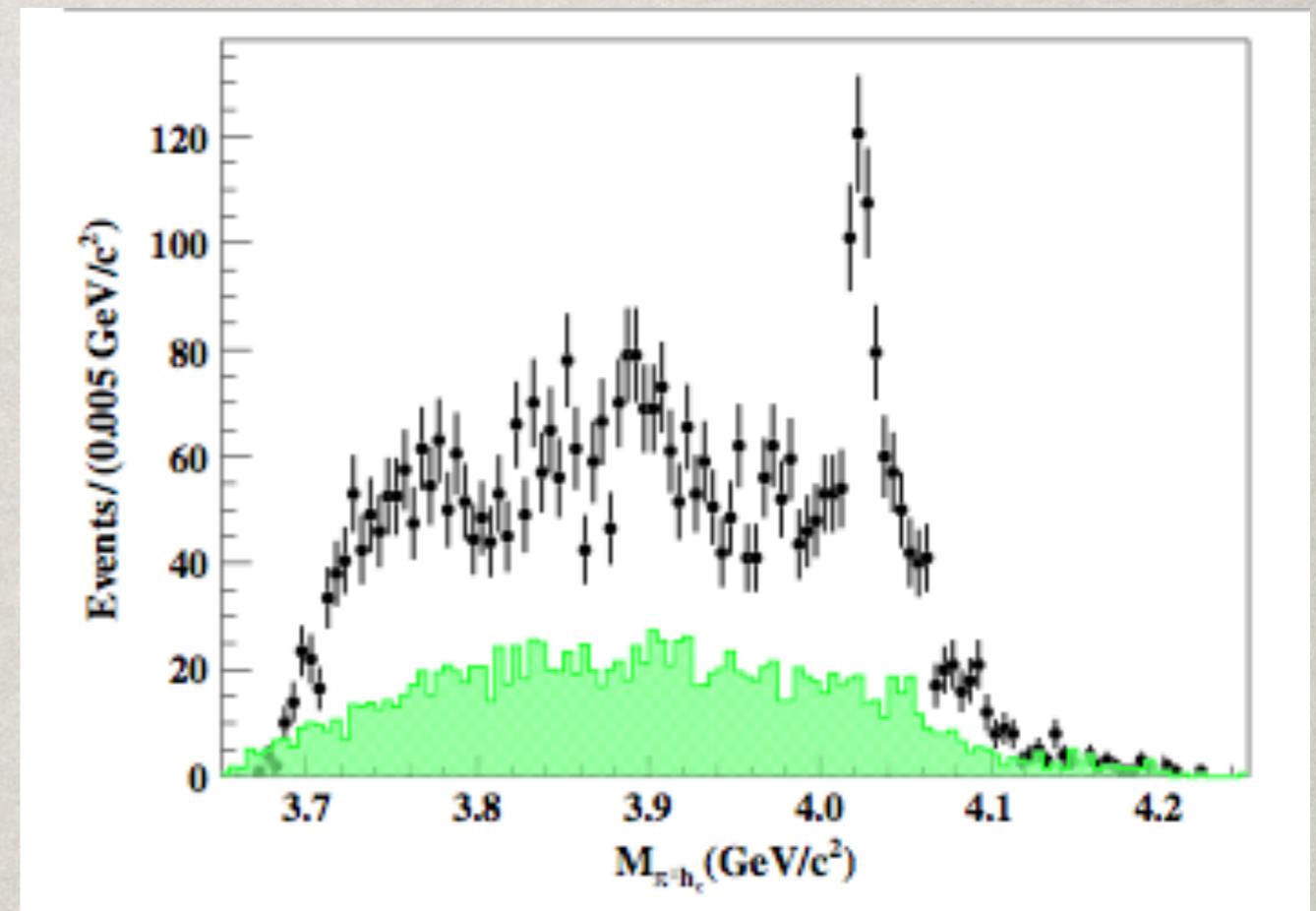
$$e^+ e^- \rightarrow \pi^+ \pi^- h_c$$

sums 13 different ee energy values

“no significant  $Z_c(3900)$  observed”

$$M = 4022.9 \pm 0.8 \pm 2.7$$

$$\Gamma = 7.9 \pm 2.7 \pm 2.6$$

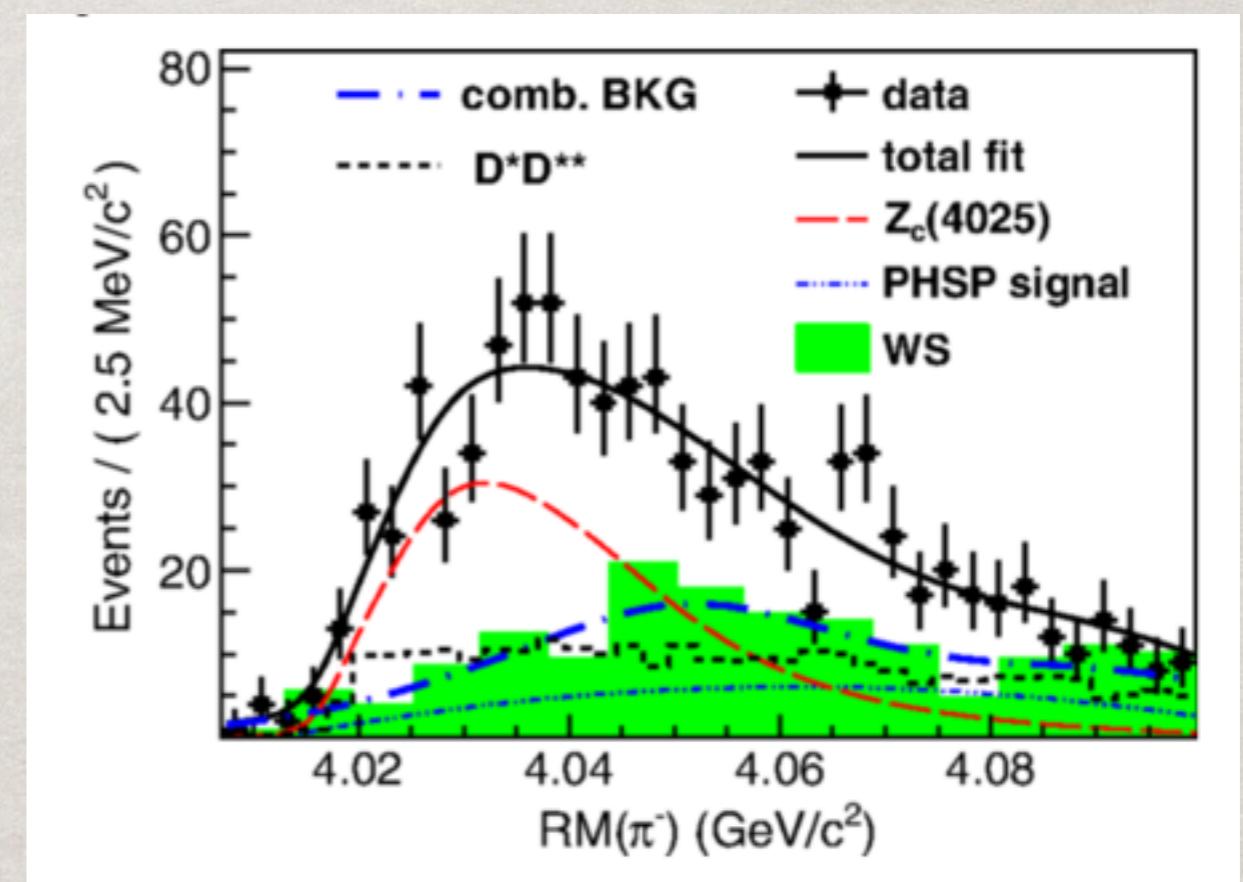


# $Z_c(4025)$

$$e^+ e^- \rightarrow (D^* \bar{D}^*)^\pm \pi^\mp$$

$$M = 4026.3 \pm 2.6 \pm 3.7$$

$$\Gamma = 24.8 \pm 5.6 \pm 7.7$$



BESIII Phys. Rev. Lett. 112, 132001 (2014)

Zc(3900)

Zc(4025)

# Theory

From SPIRE HEP Database (21st, Apr):

## 1. Tetraquarks

- arXiv:1110.1333, 1303.6857
- arXiv:1304.0345, 1304.1301

## 2. Hadronic molecules

- arXiv:1303.6608, 1304.2882, 1304.1850

## 3. Four quark state (1 or 2)

- arXiv:1304.0380

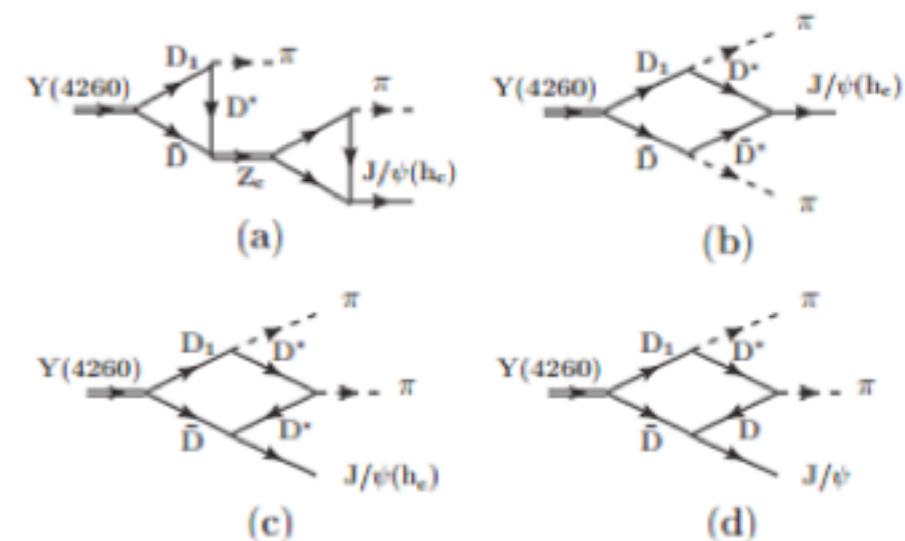
## 4. Meson loop

- arXiv:1303.6355
- arXiv:1304.4458

## 5. ISPE model

- arXiv:1303.6842

## 6. ...



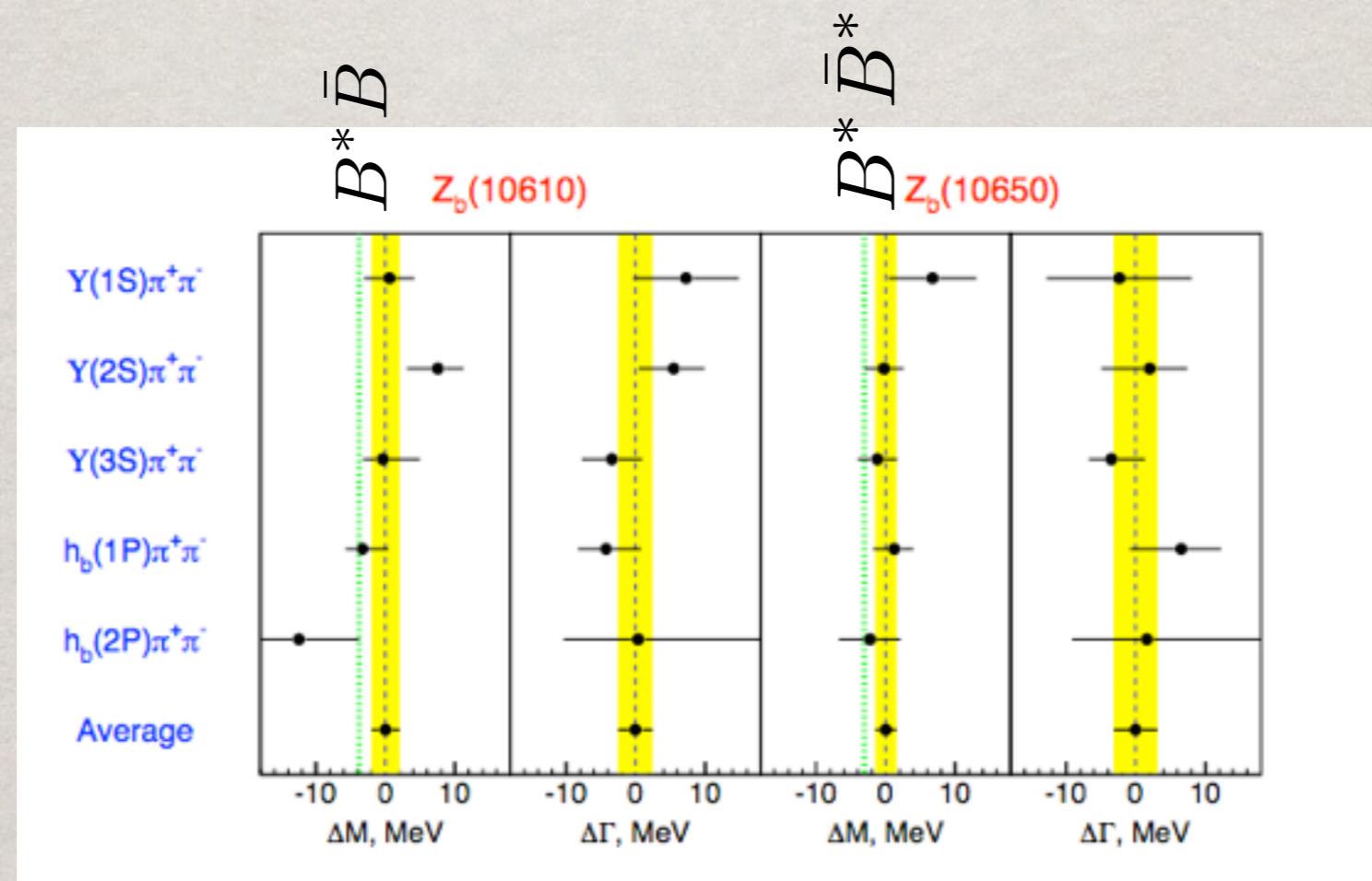
Meson loop

# A CUSP MODEL

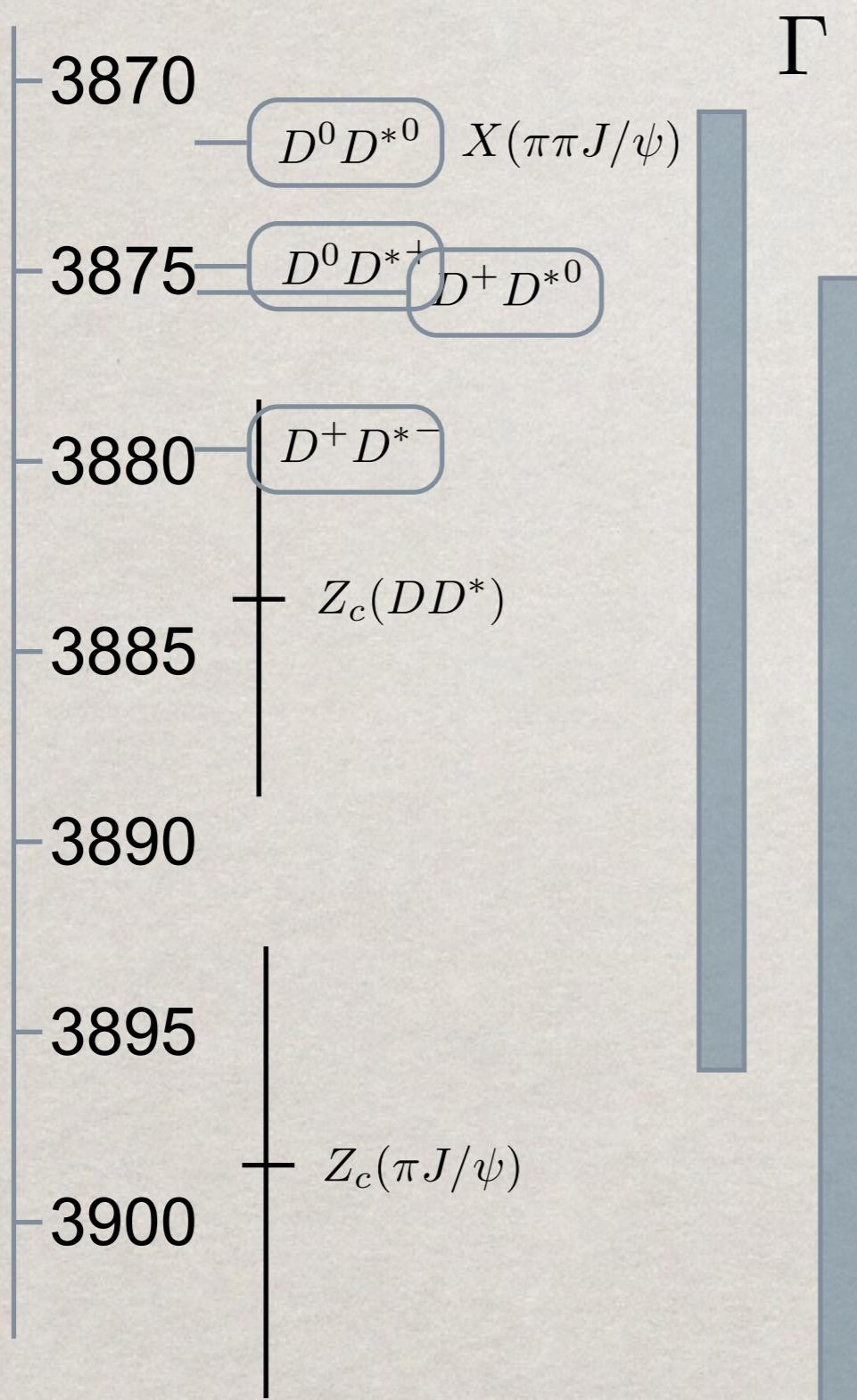
E.S. Swanson, arXiv:1409.3291; v2 to appear

# Charged Exotics as Threshold Cusps

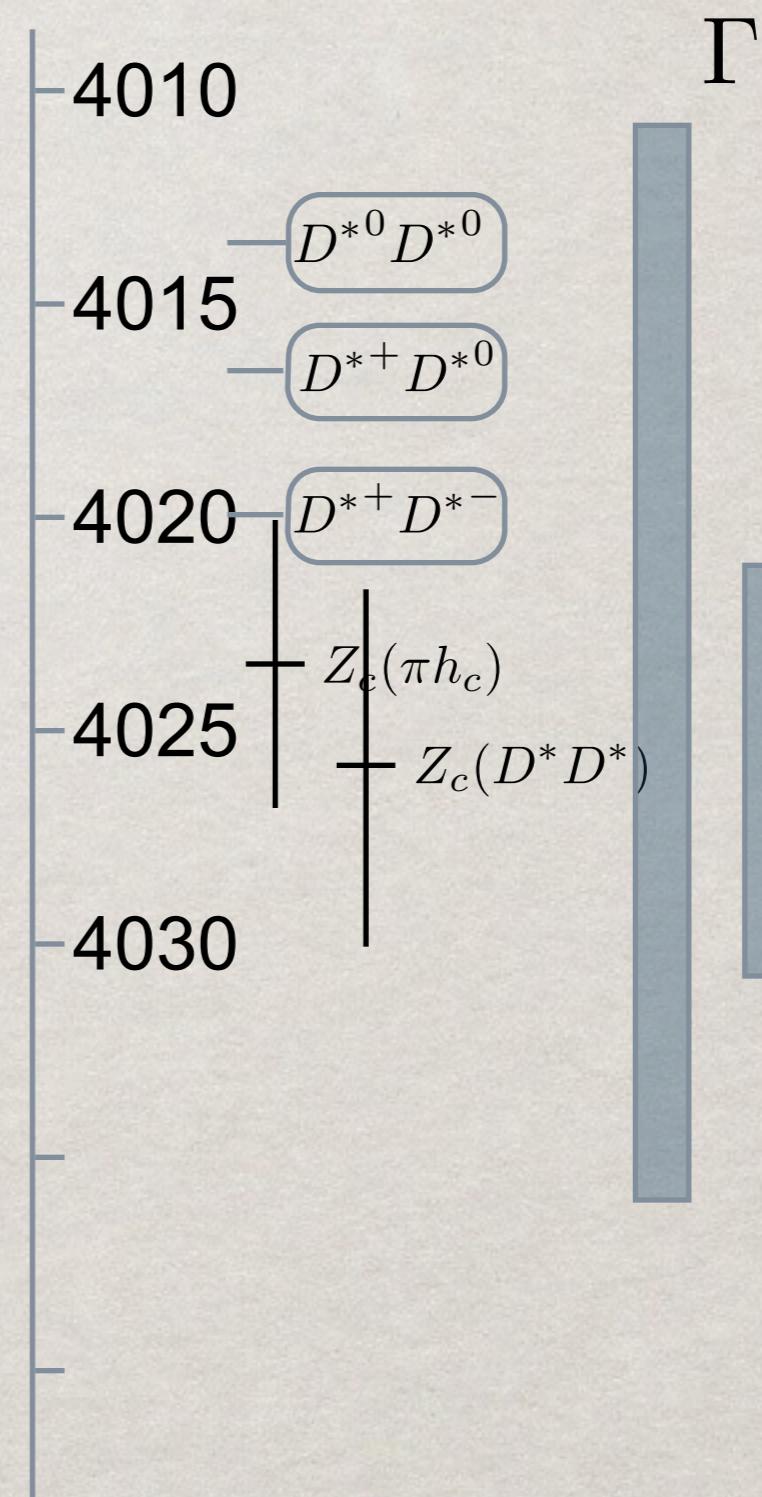
It seems foolish to ignore that many of these states are just above open charm/bottom thresholds.



# $Z_c(3900)$



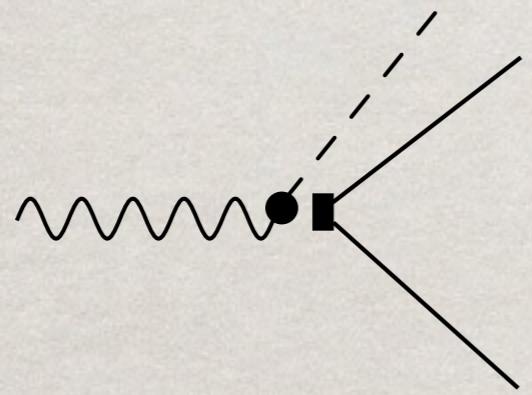
# $Z_c(4025)$



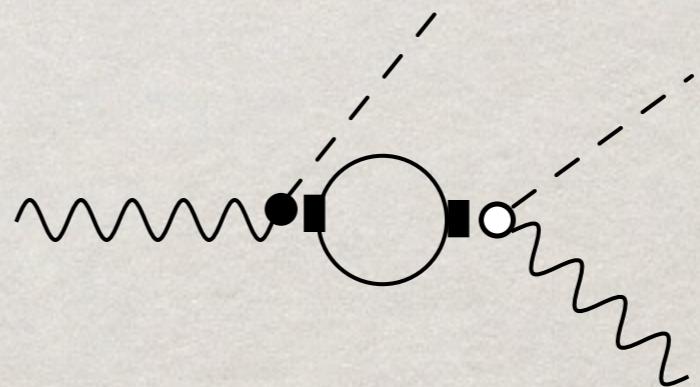
# Cusp Model

Attempt a “microscopic” cusp model.

[separable nonrelativistic model; solve exactly]



$$Y(4260) \rightarrow \pi D\bar{D}^*$$

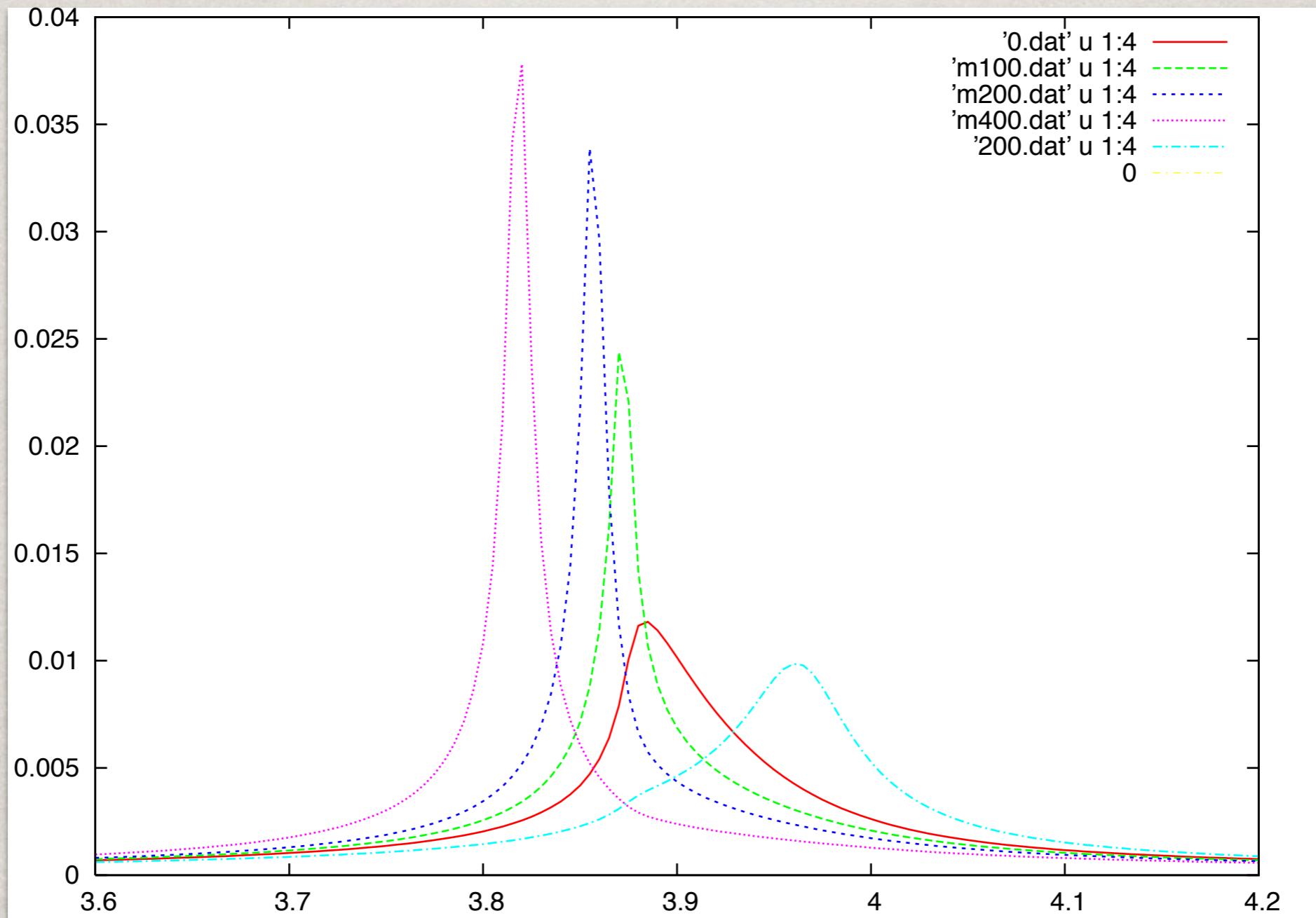


$$Y(4260) \rightarrow \pi\pi J/\psi$$

$$g_{DD^*} \cdot \exp(-\lambda(s_{\pi Y})/\beta_{\pi Y}^2) \exp(-\lambda(s_{D\bar{D}^*})/\beta_{D\bar{D}^*}^2)$$

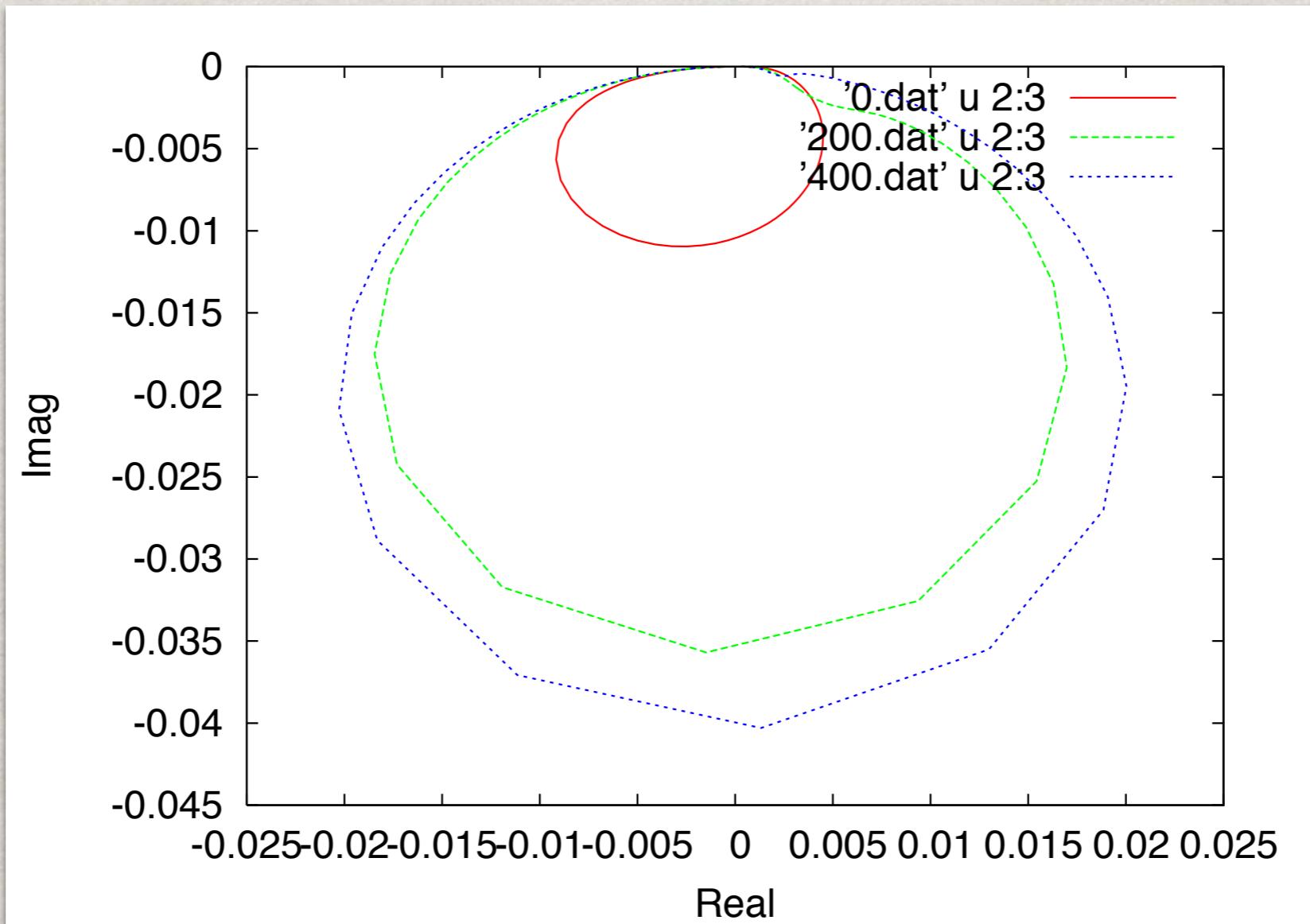
# Cusp Model

effect of the bubble sum



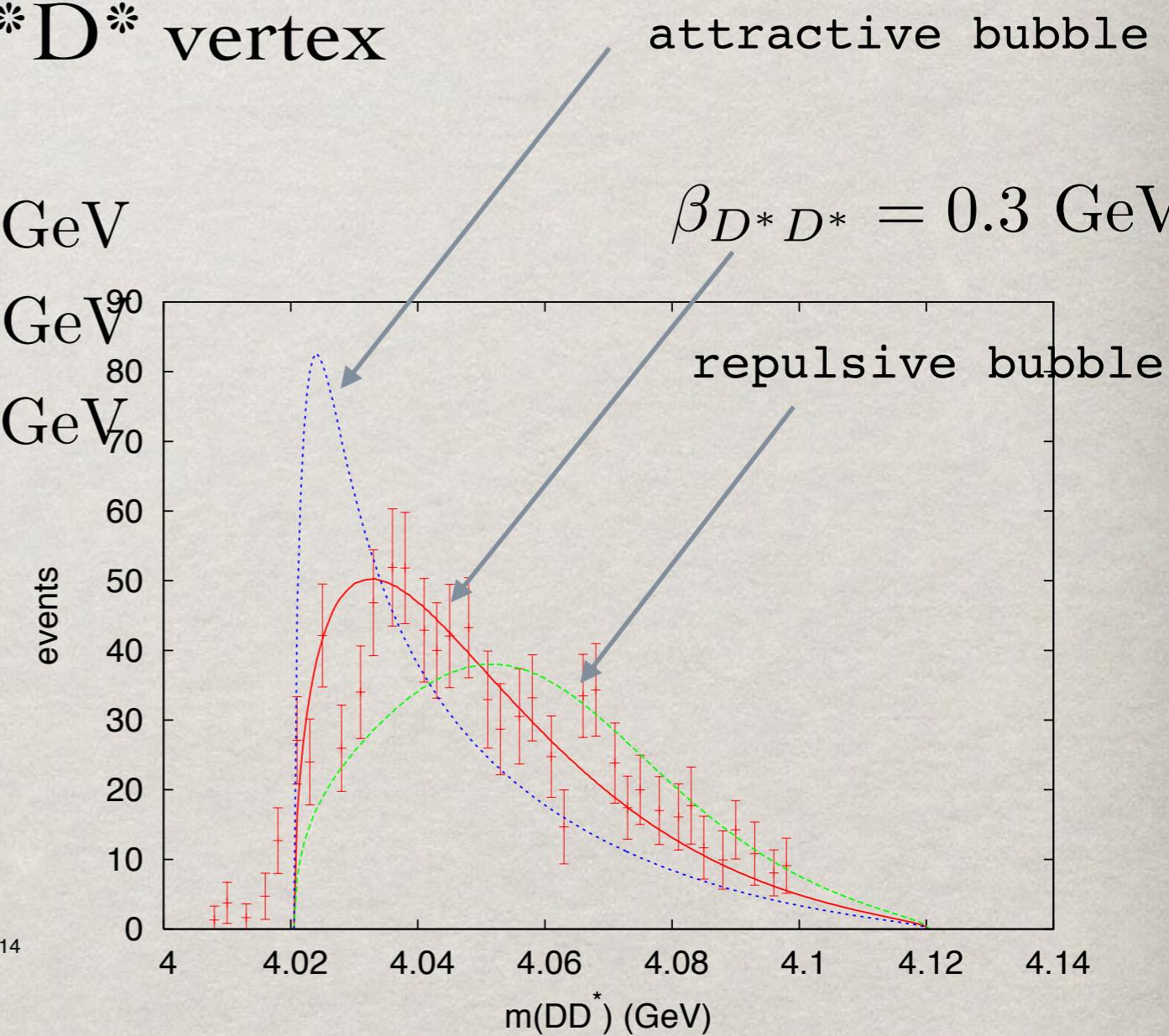
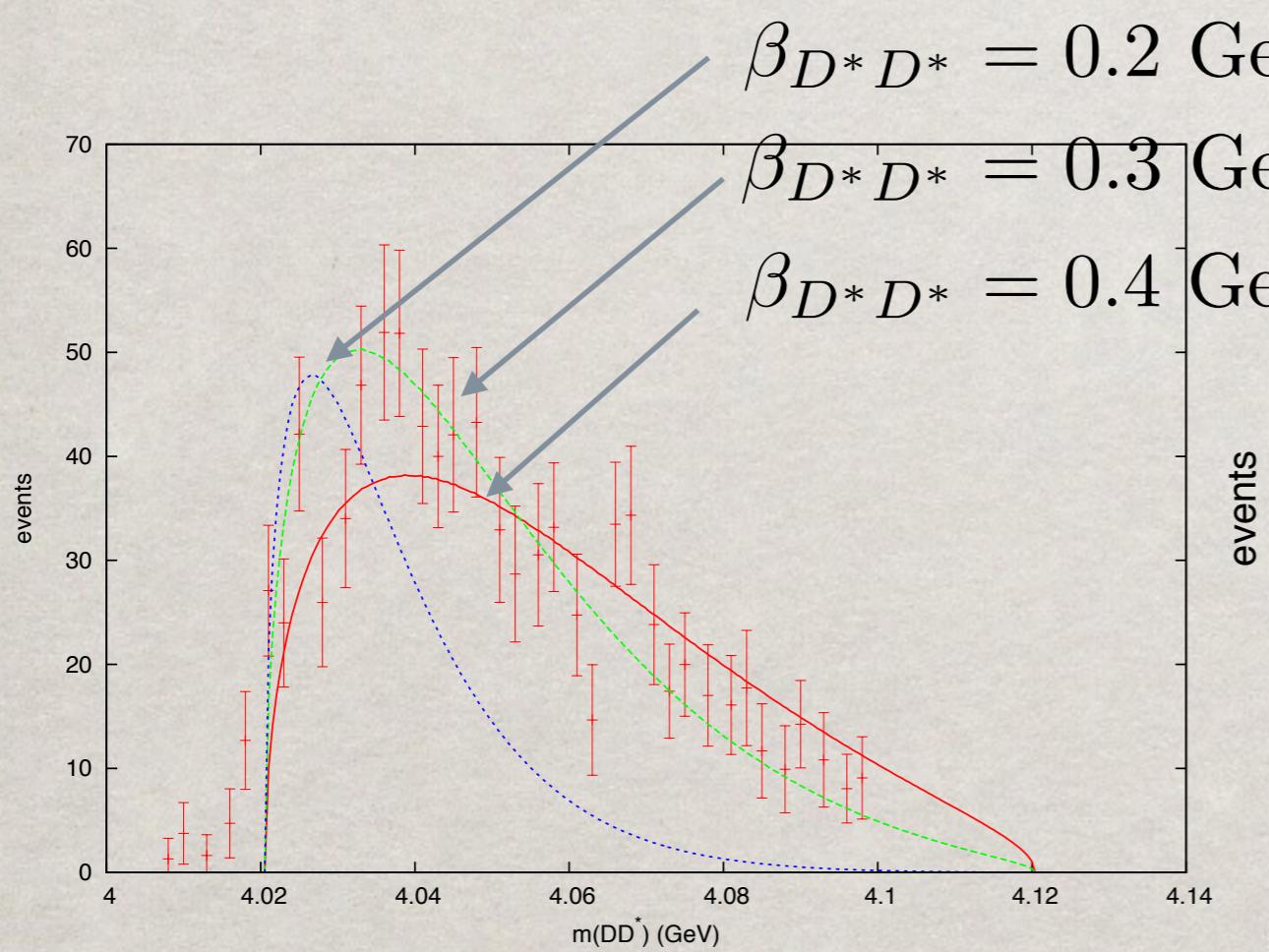
# Cusp Model

effect of the bubble sum



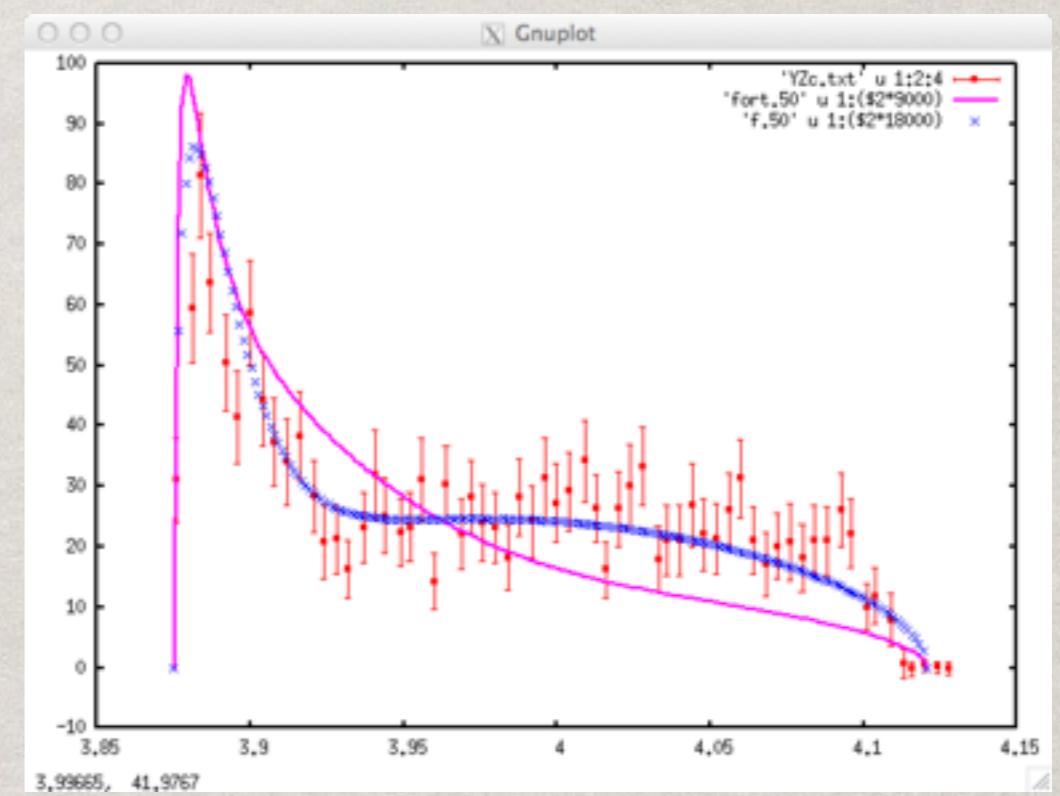
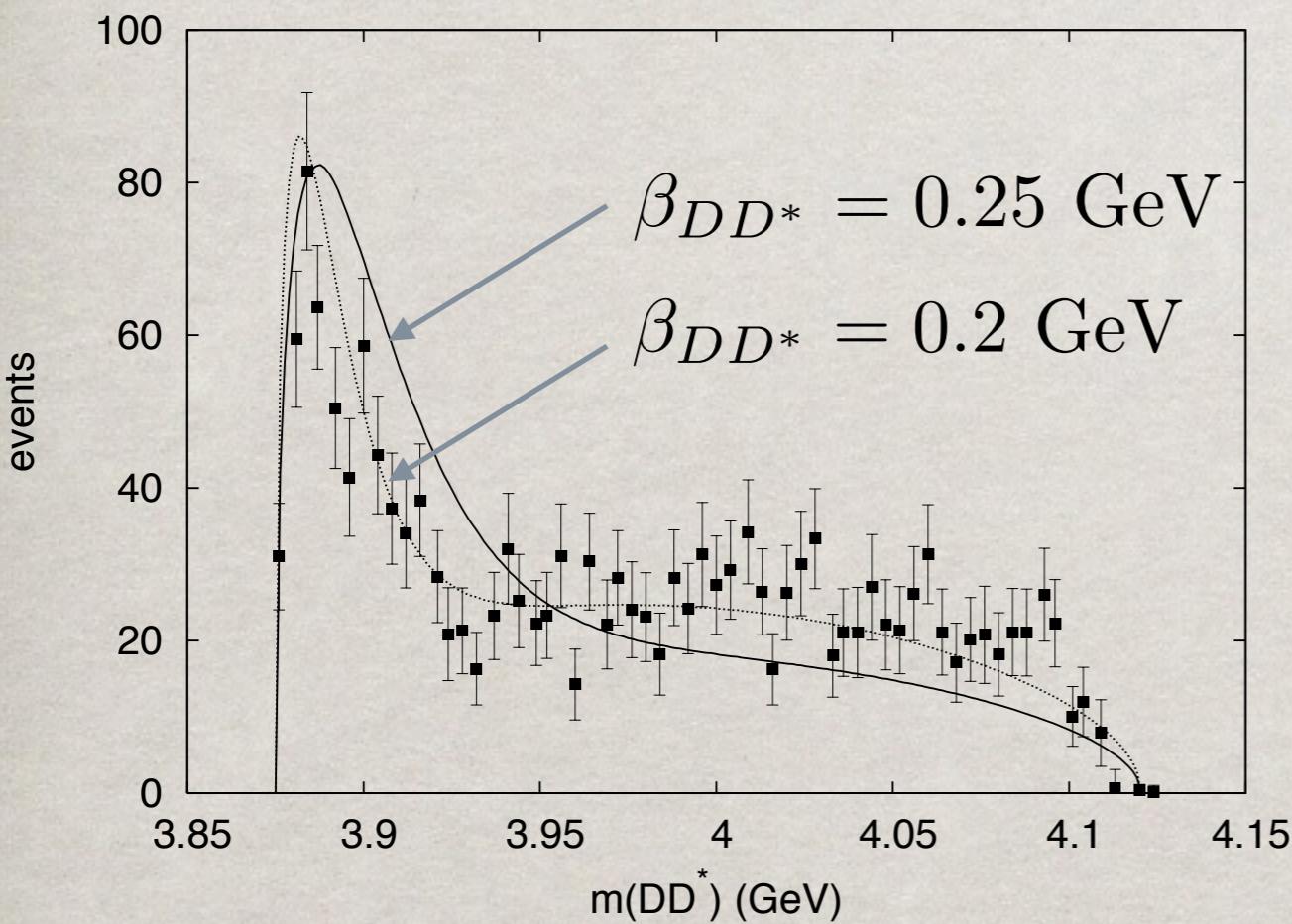
# Fit D\*D\* Vertex

fit the pi Y: D\*D\* vertex



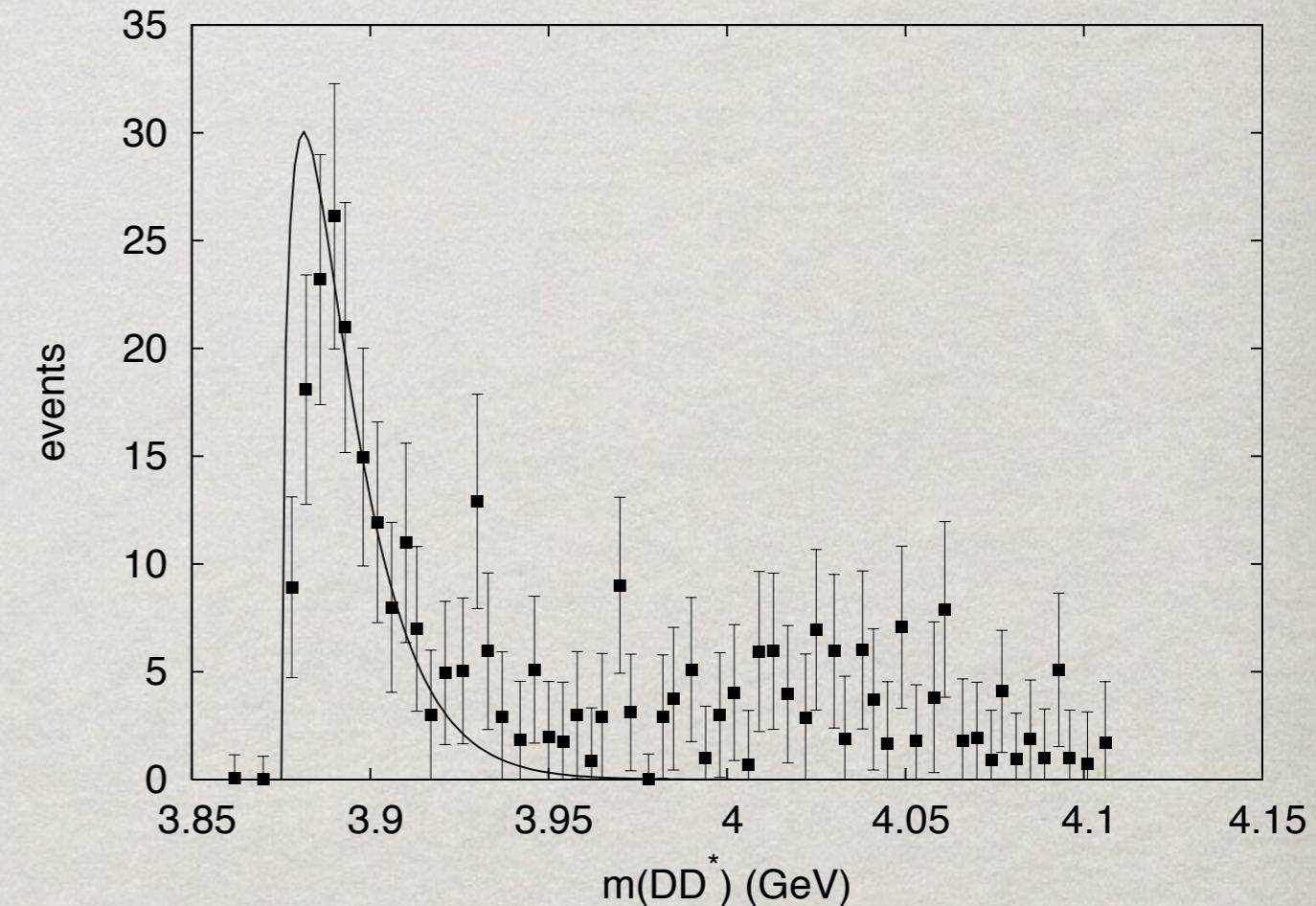
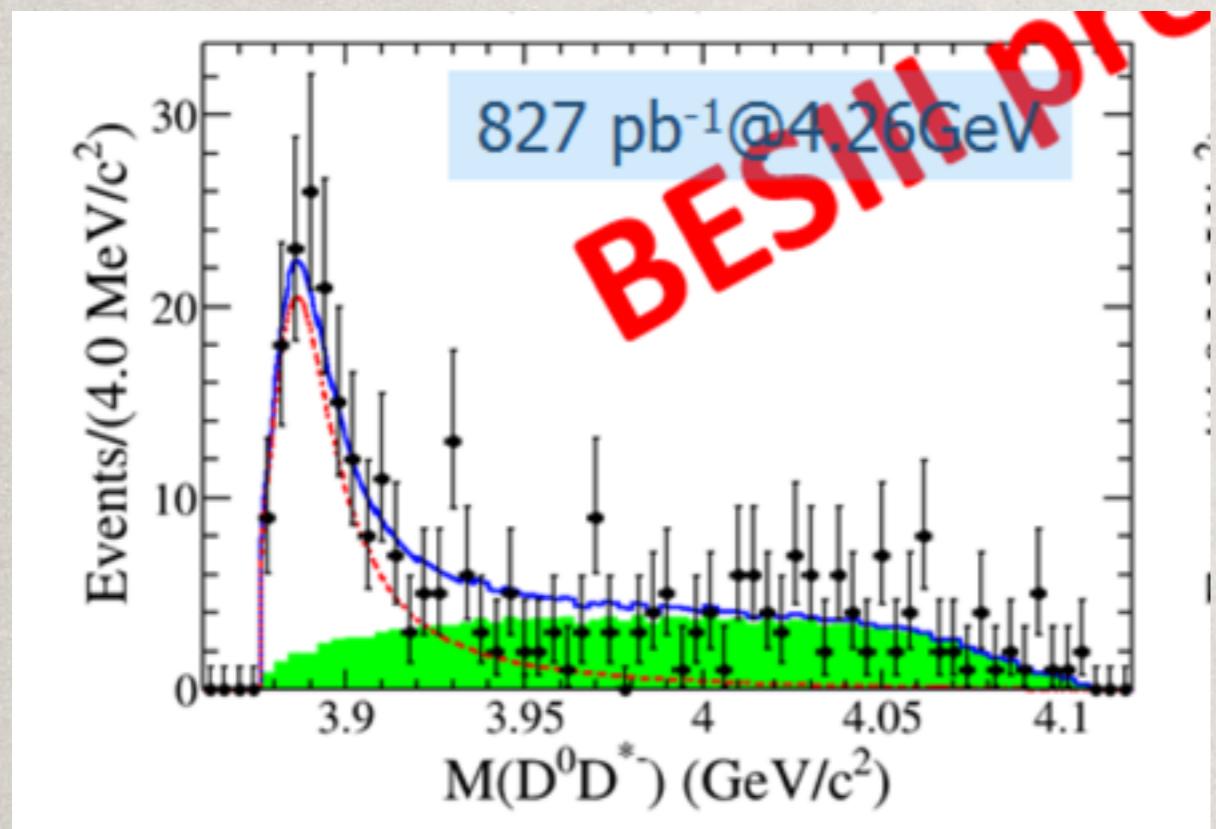
no evidence for  $\pi D^*$  dynamics, background, or bubble

# Fit DD\* Vertex



no evidence for bubble  
evidence for incoherent background

# Fit DD\* Vertex

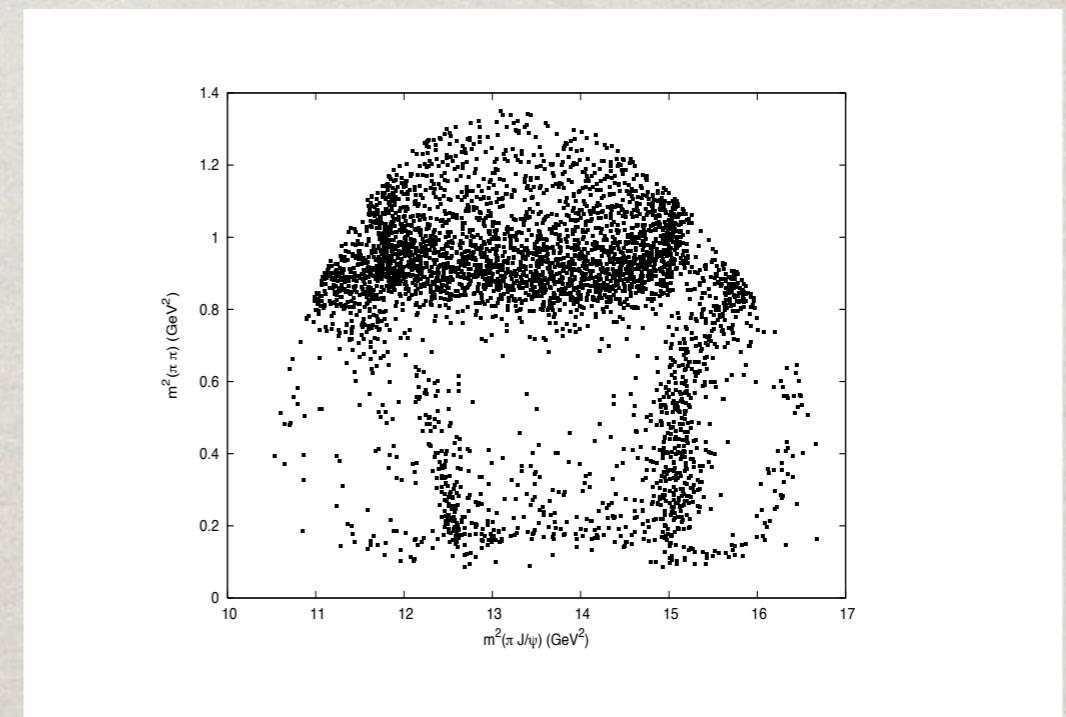
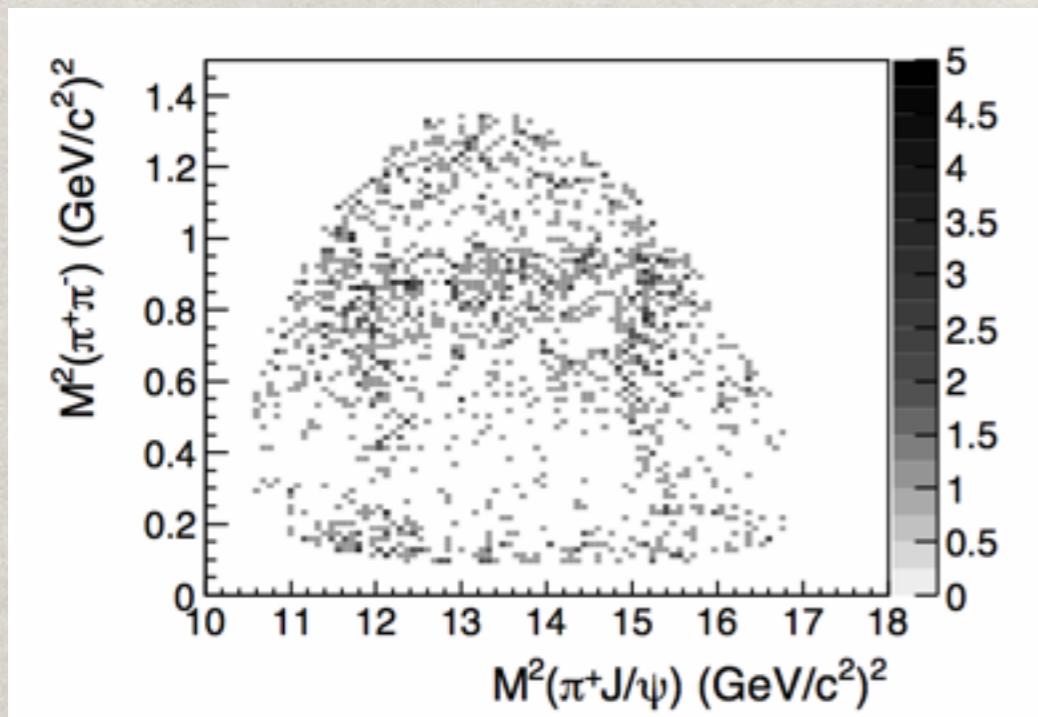


Wolfgang Gradl, "Bound States in QCD", St Goar, Mar 24-27, 2015

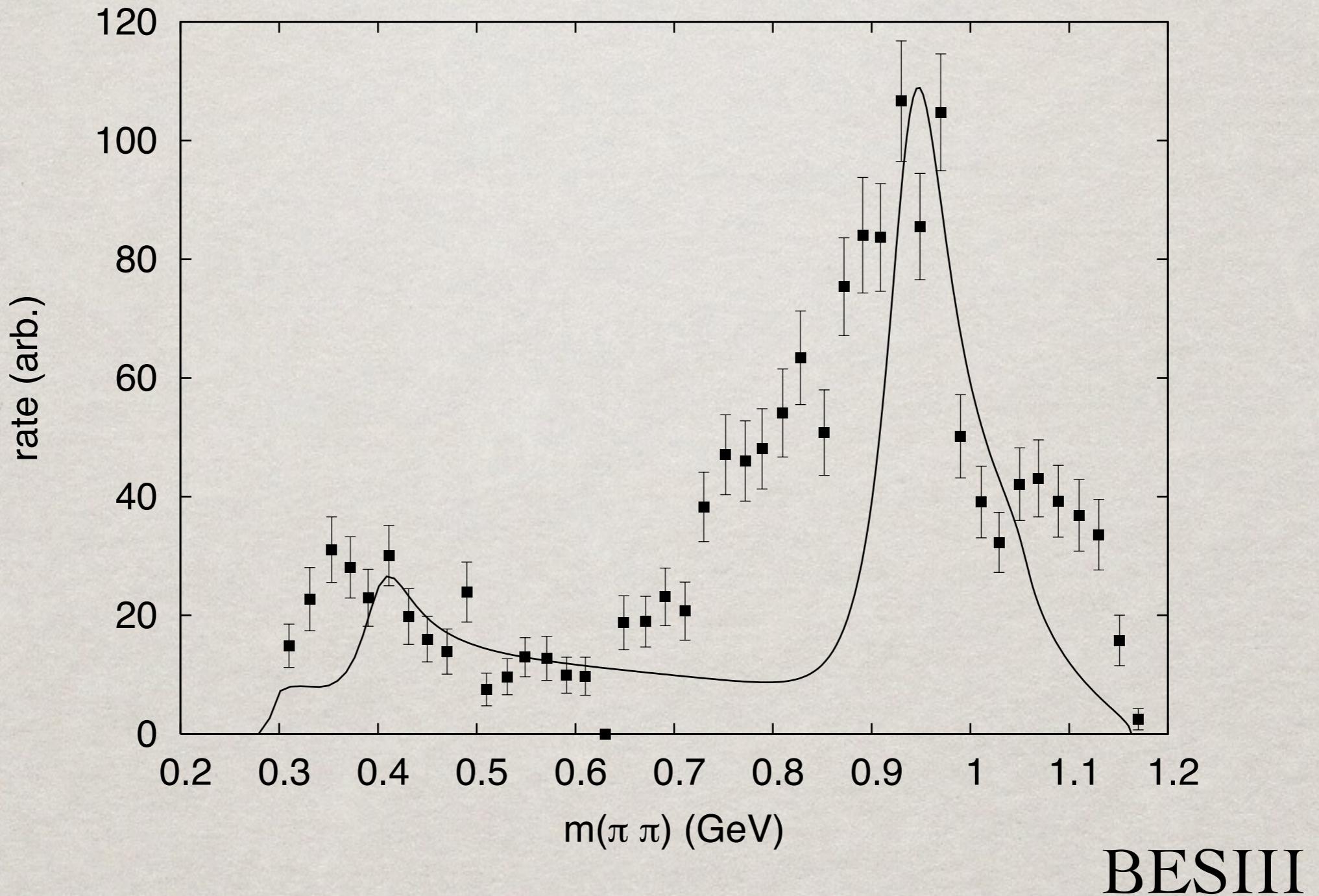
New BESIII result with all three particles identified.  
As hoped, background is diminished.

# Obtain $\pi \pi J/\psi$

Now  $\pi \pi$  dynamics is important

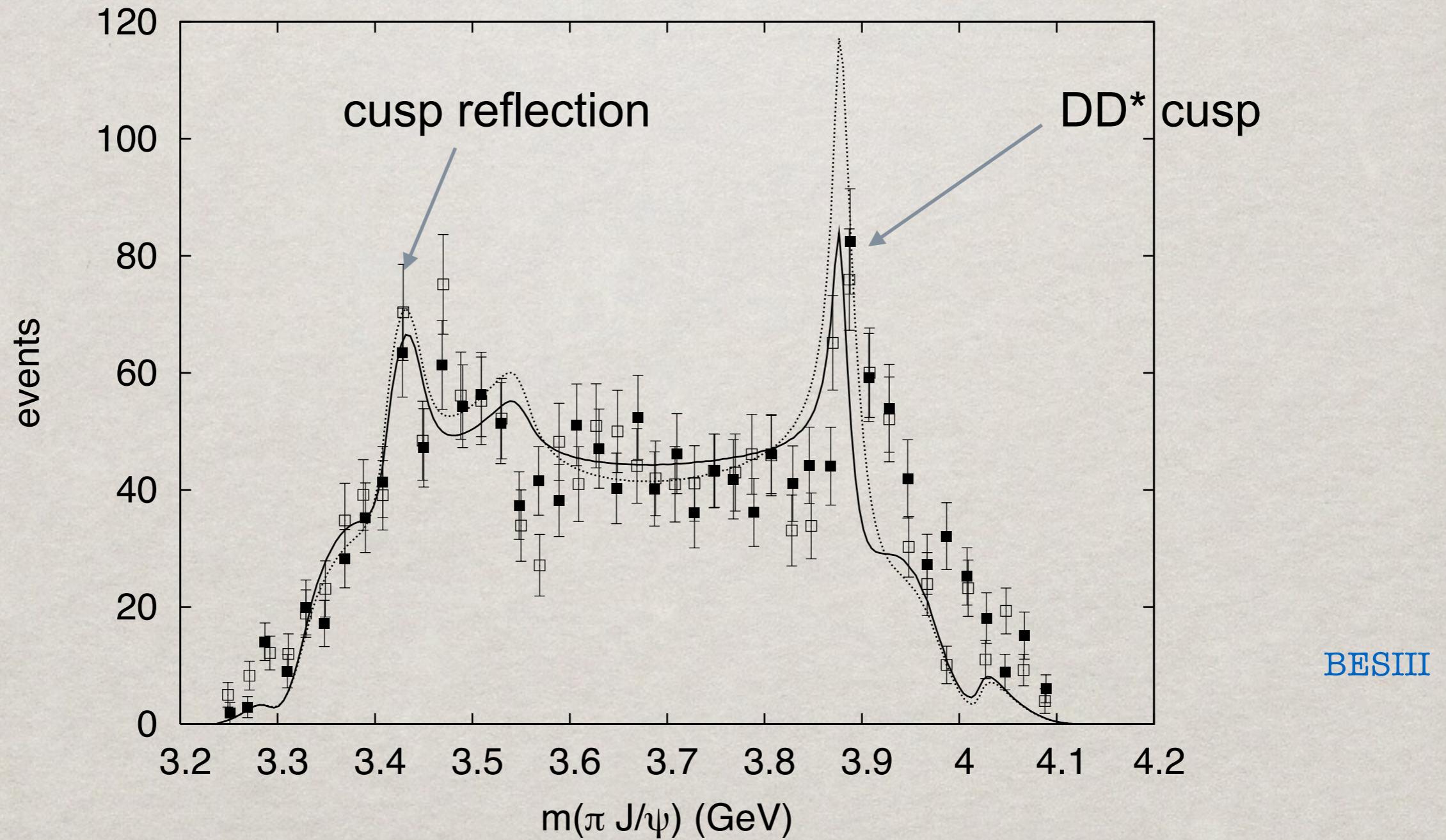


# Obtain pi pi J/psi



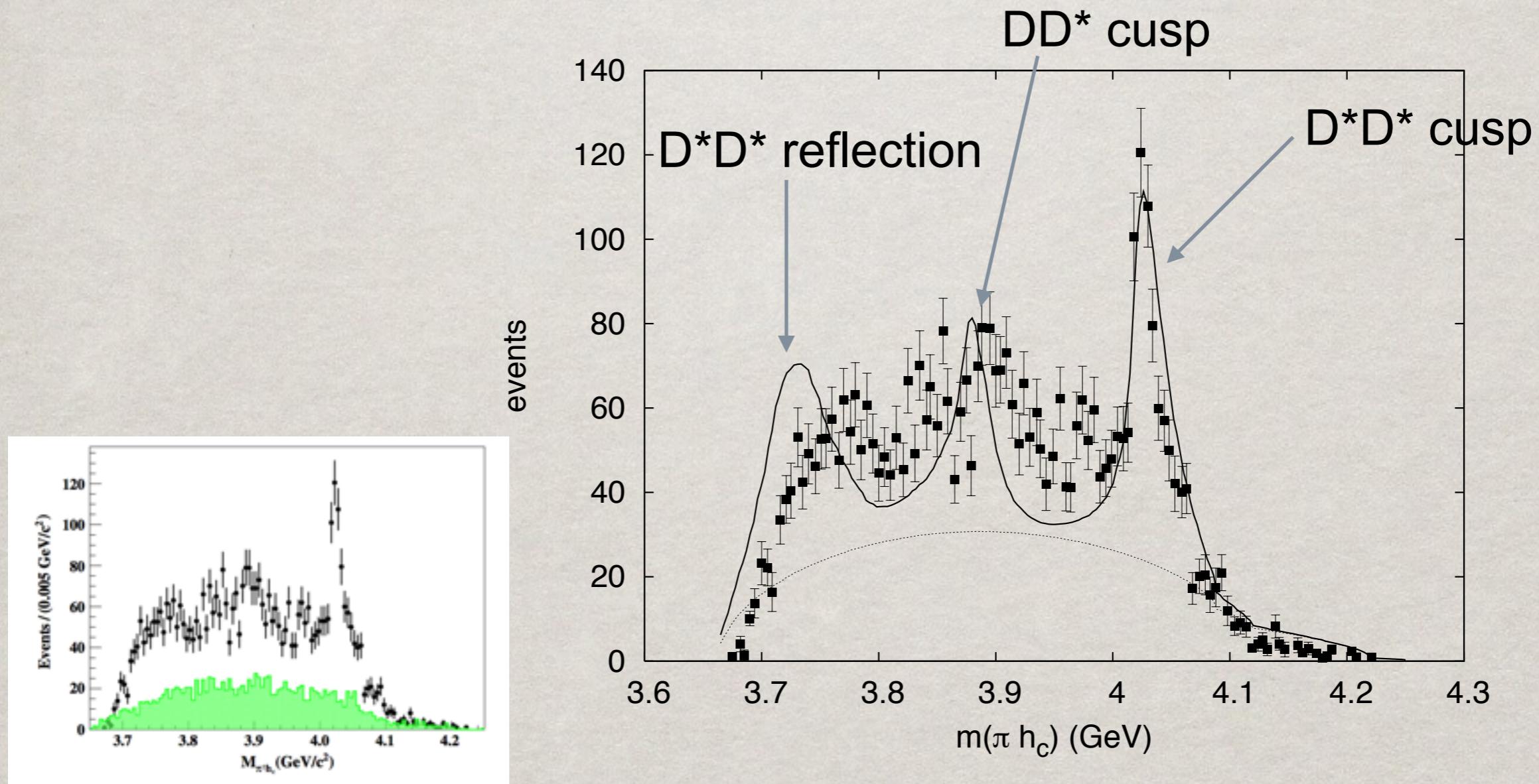
BW(0.4,60) + BW(0.94,80), betas=0.3, gamma=0

# Obtain pi pi J/psi

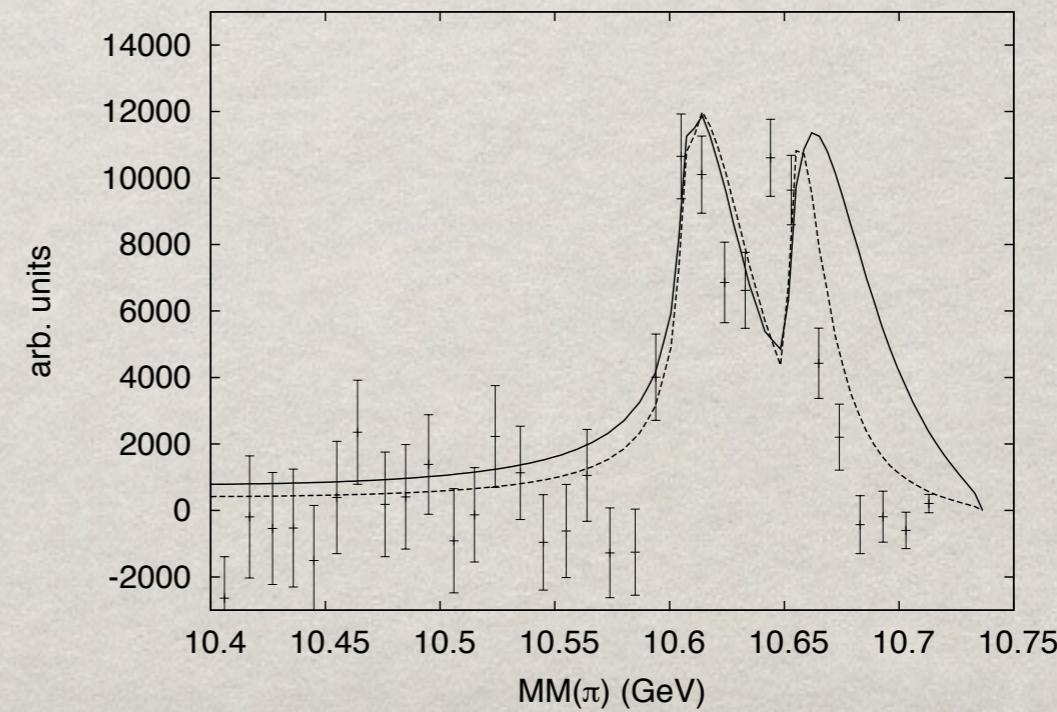
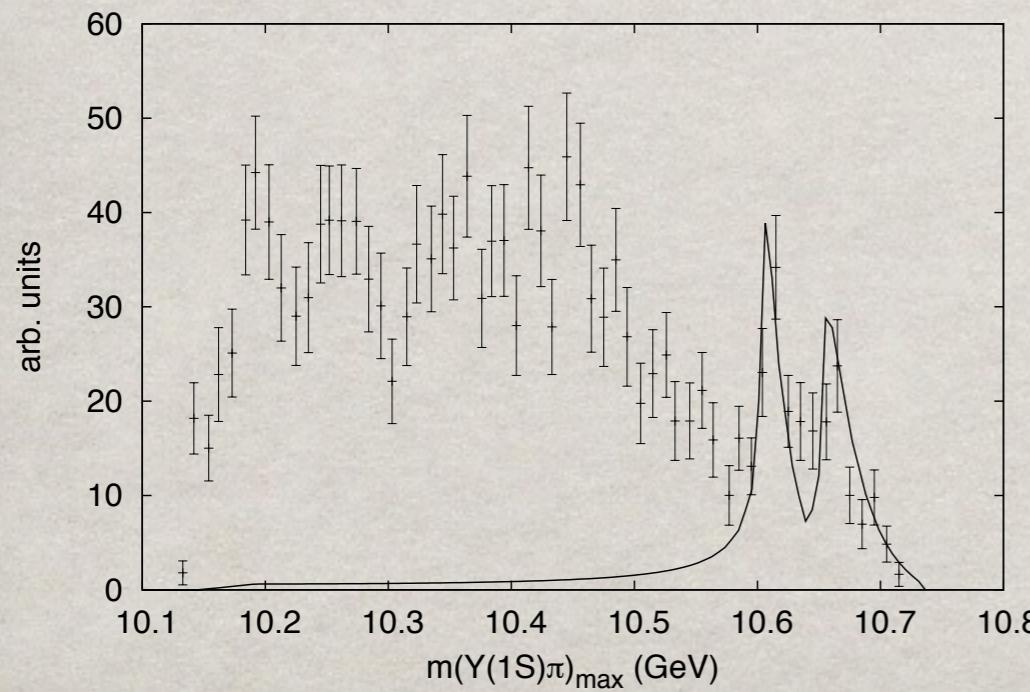
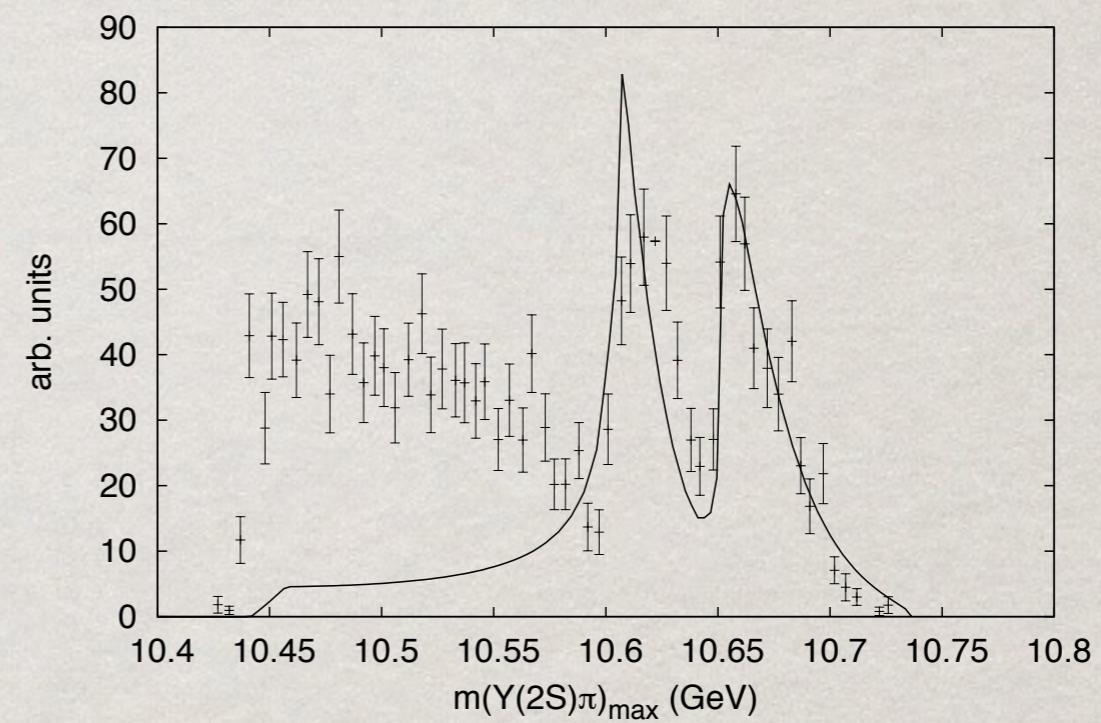
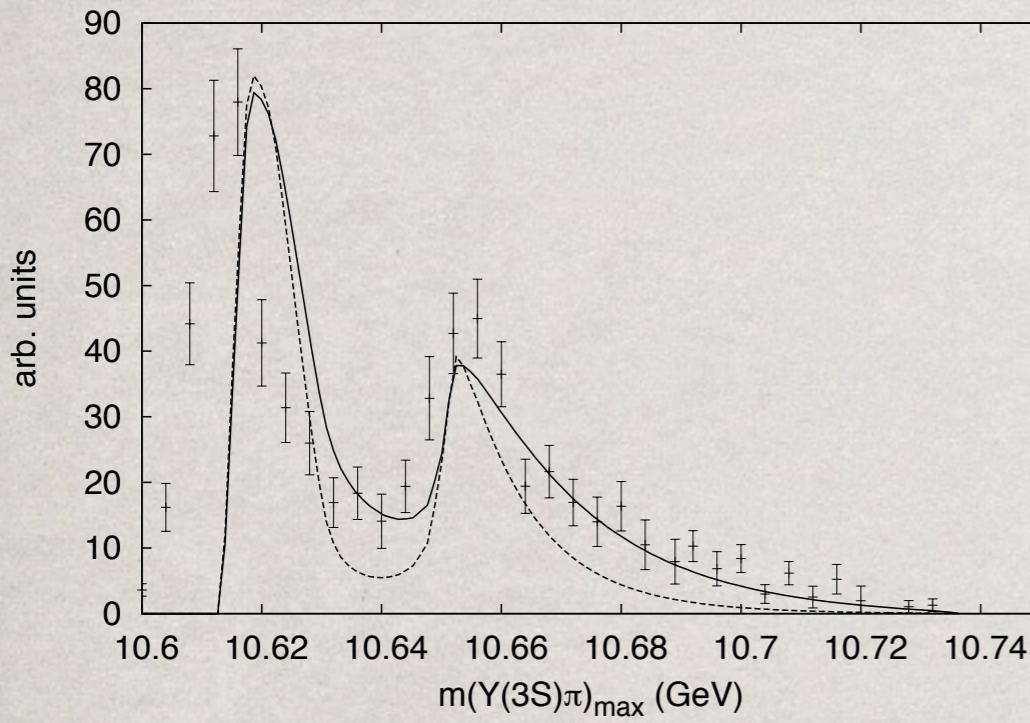


# Obtain $\pi \pi h_c$

[incoherent background only]

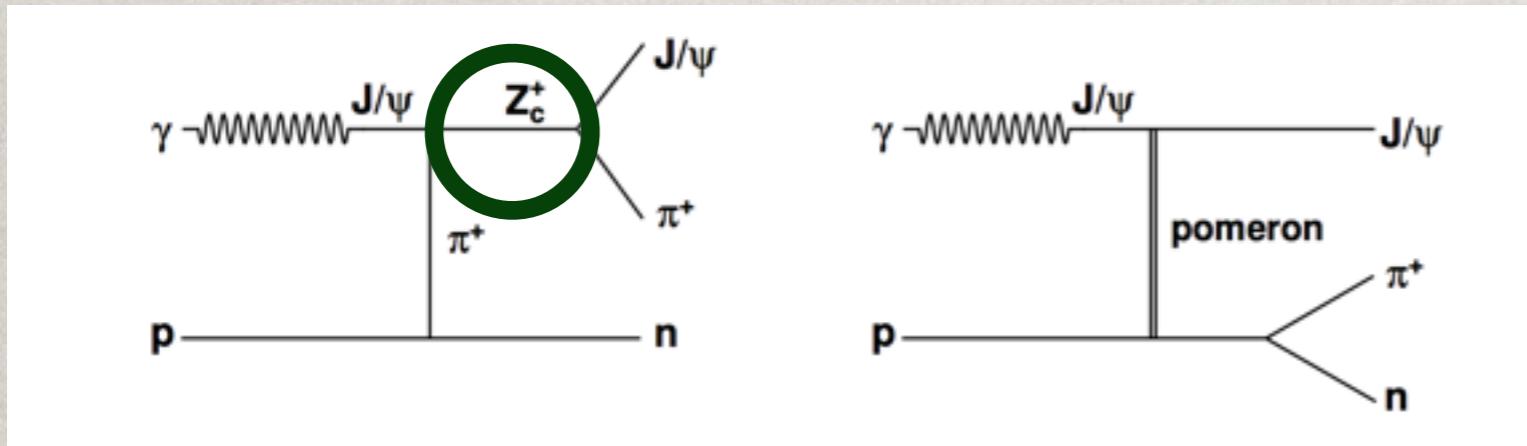


# $\Upsilon(5S) \rightarrow \Upsilon(nS)\pi\pi$



# Missing Exotics

COMPASS



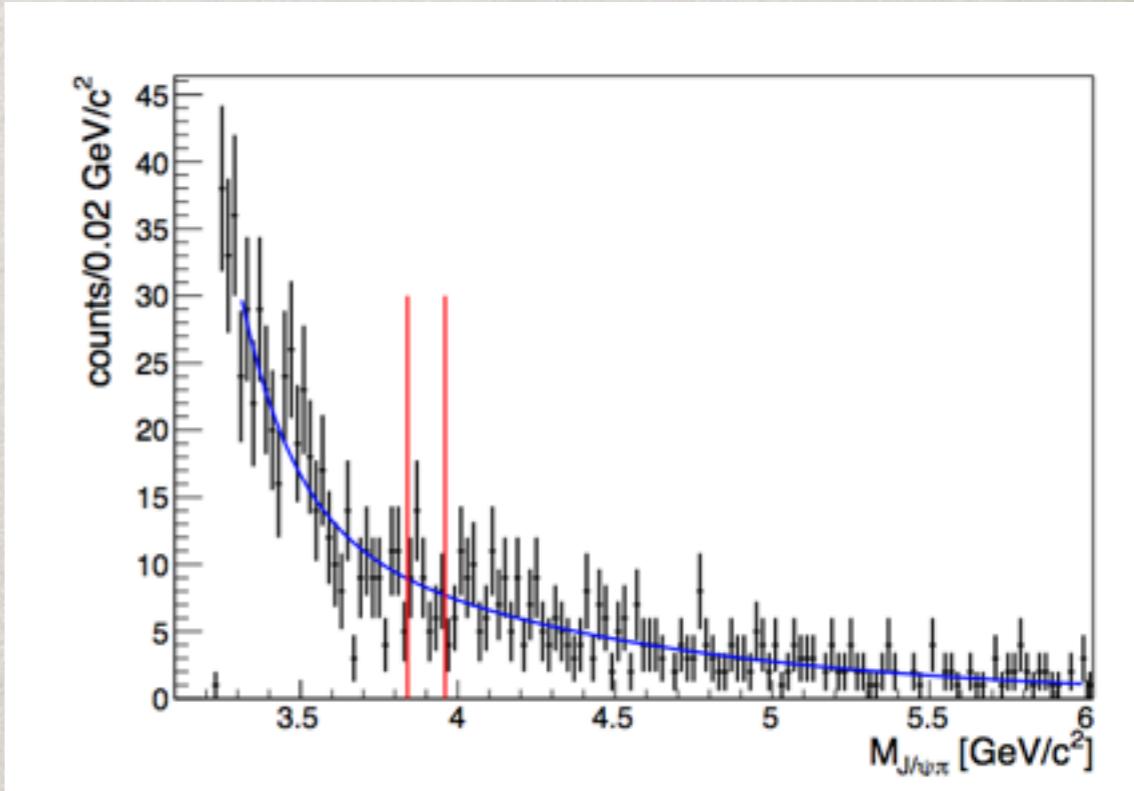
$$\exp(-\lambda(s_{\gamma N}, m_\psi^2, m_\pi^2)/(4s_{\gamma N}\beta^2)) \approx$$

$$\exp(-(s_{\gamma N} - m_\psi^2)^2/(4s_{\gamma N}\beta^2)) \approx$$

$$\exp(-88)$$

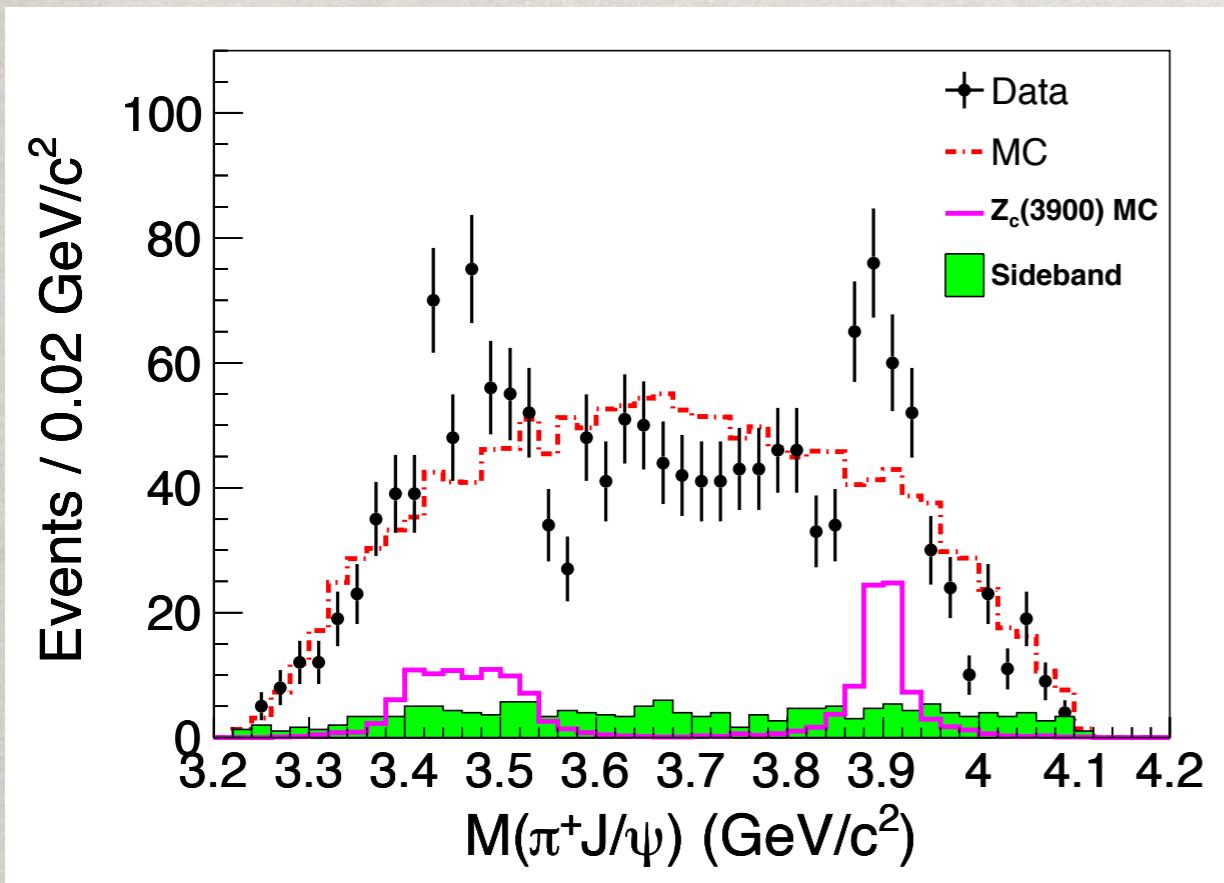
C. Adolph et al. [COMPASS] arXiv:1407.6186v1

$$\sqrt{s_{\gamma N}} = 7 \text{ GeV}$$



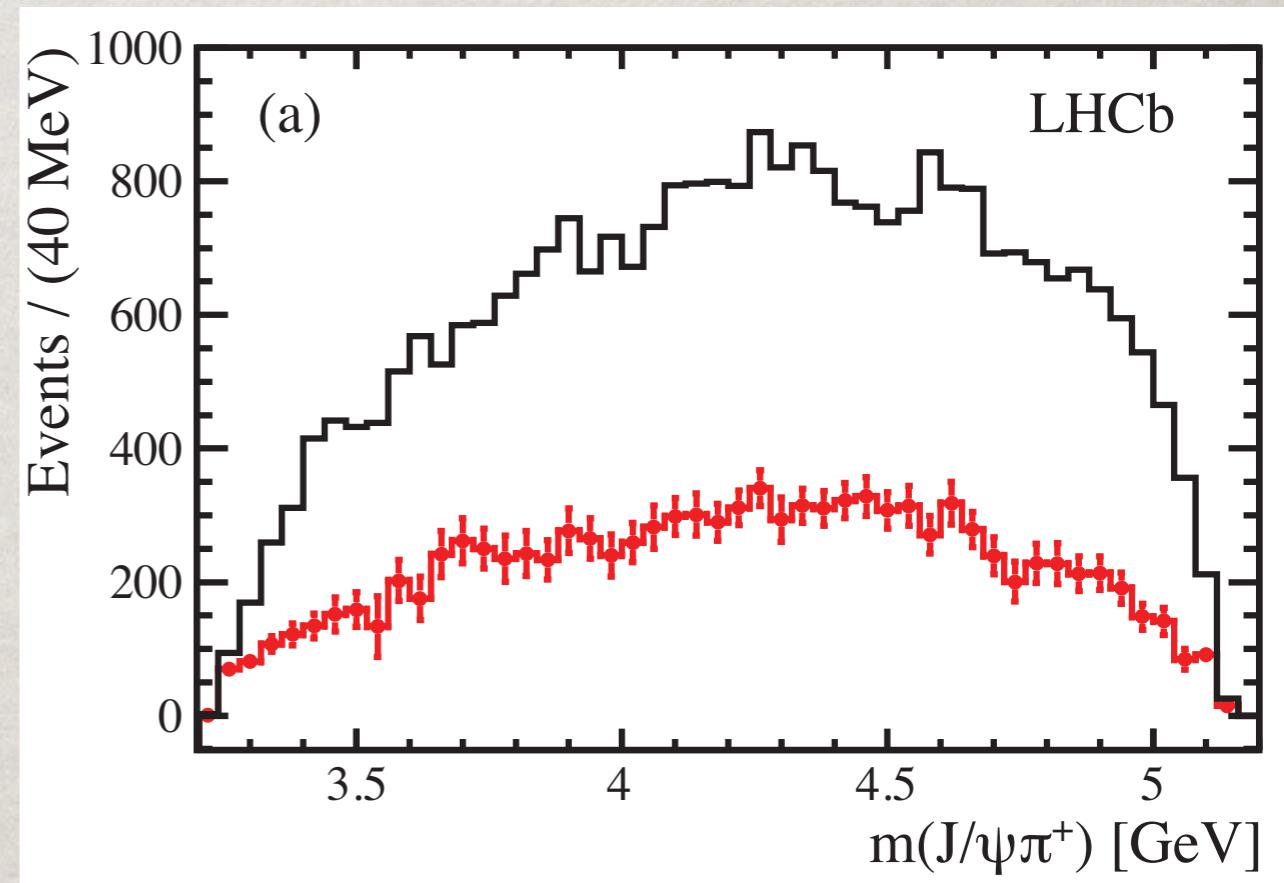
# Missing Exotics

$$Y(4260) \rightarrow \pi^+ \pi^- J/\psi$$



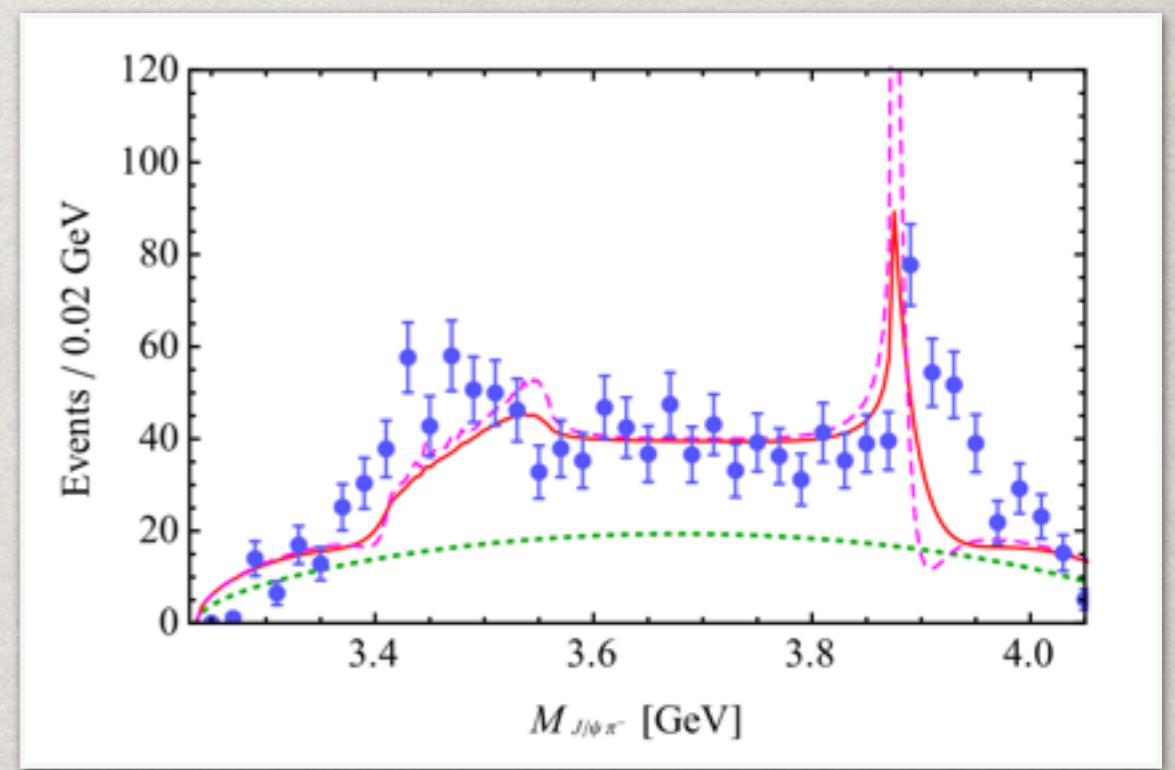
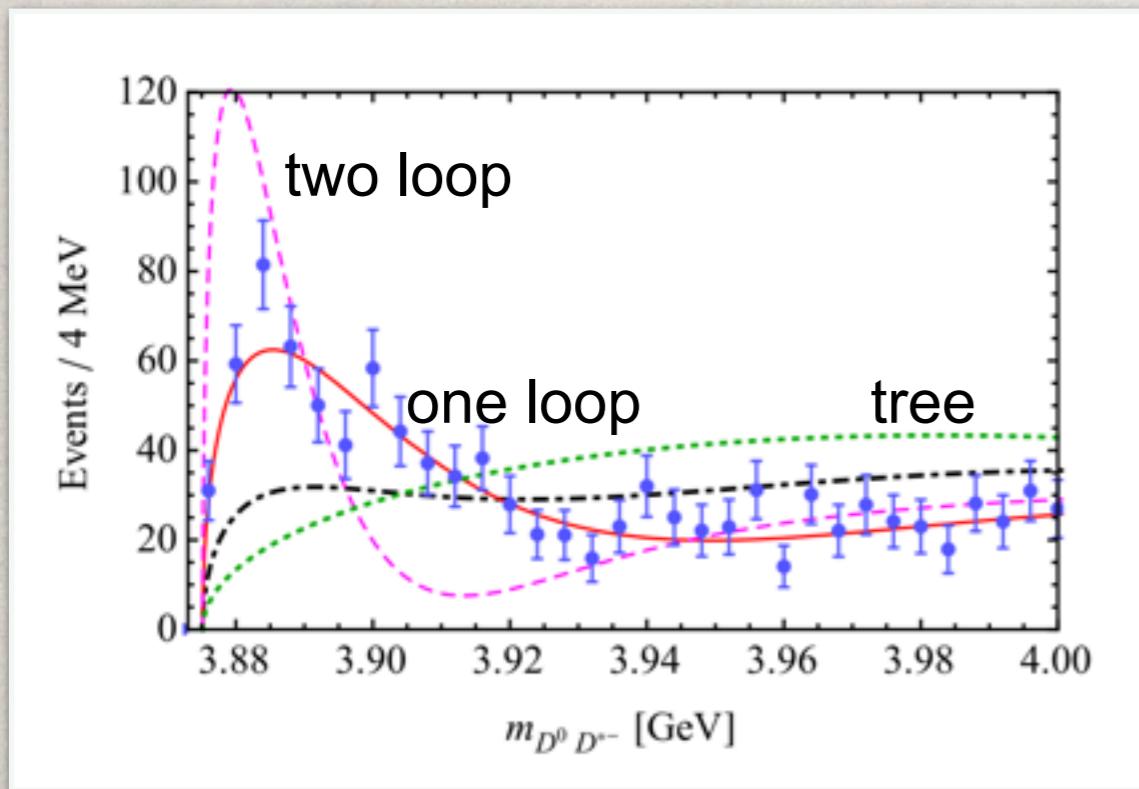
BESIII

$$B_0 \rightarrow \pi^+ \pi^- J/\psi$$



LHCb

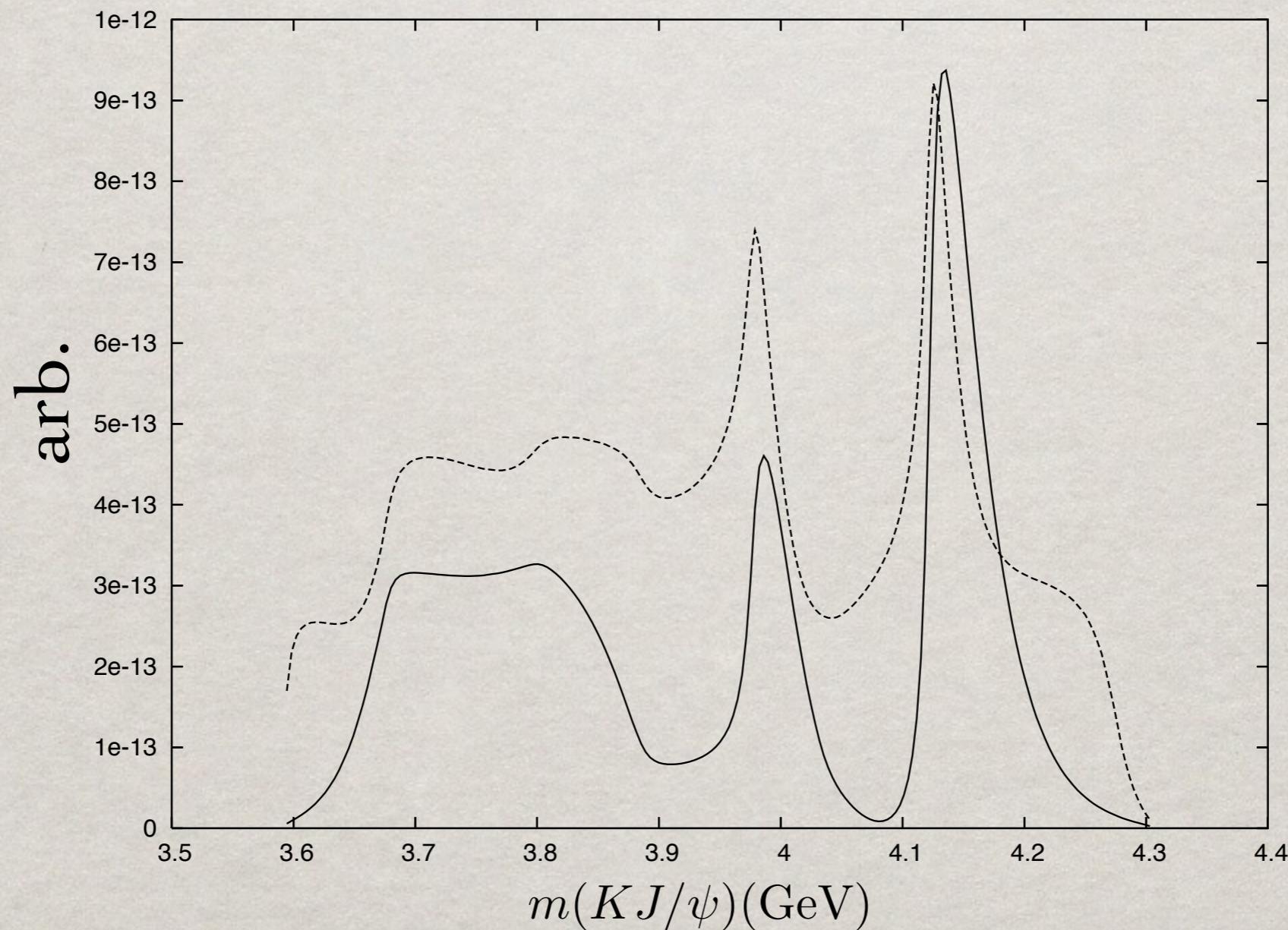
# Hanhart Model



Hanhart *et al.* claim that the strength of the vertex requires bubble summation, which generates a pole.

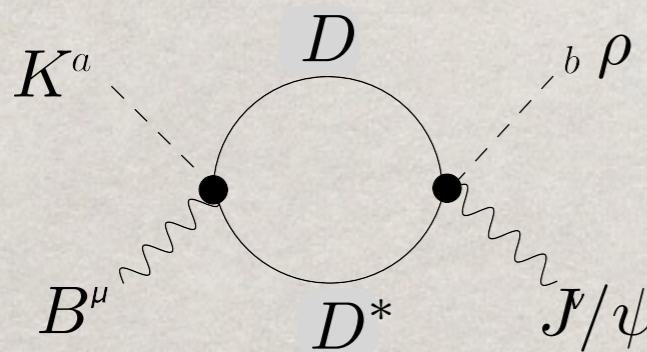
# Other Exotics?

$e^+e^- (\sqrt{s} = 4.8) \rightarrow K^+K^- J/\psi$



# Cusp Model — to do

- examine the X(3872): interplay of cusp, possible bound state dynamics, and mixing with cc states



$$-1 = -1 - \text{loop}$$

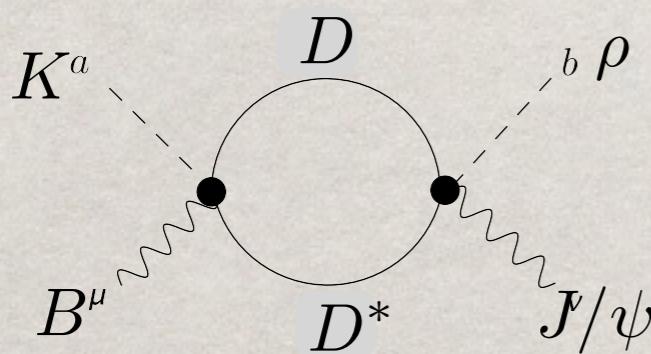
The equation shows a bare propagator (a line with a dot) minus a loop diagram (a circle with a dot).

$$\alpha \square \beta = \alpha \bullet \beta + \alpha \bullet \gamma \square \beta$$

The equation shows a bare vertex ( $\alpha$  connected to a square box, which is connected to  $\beta$ ) equal to the sum of a dressed vertex ( $\alpha$  connected to a black circle, which is connected to  $\beta$ ) and a loop correction ( $\alpha$  connected to a black circle, which is connected to a loop, which is connected to  $\beta$ ).

# Cusp Model — to do

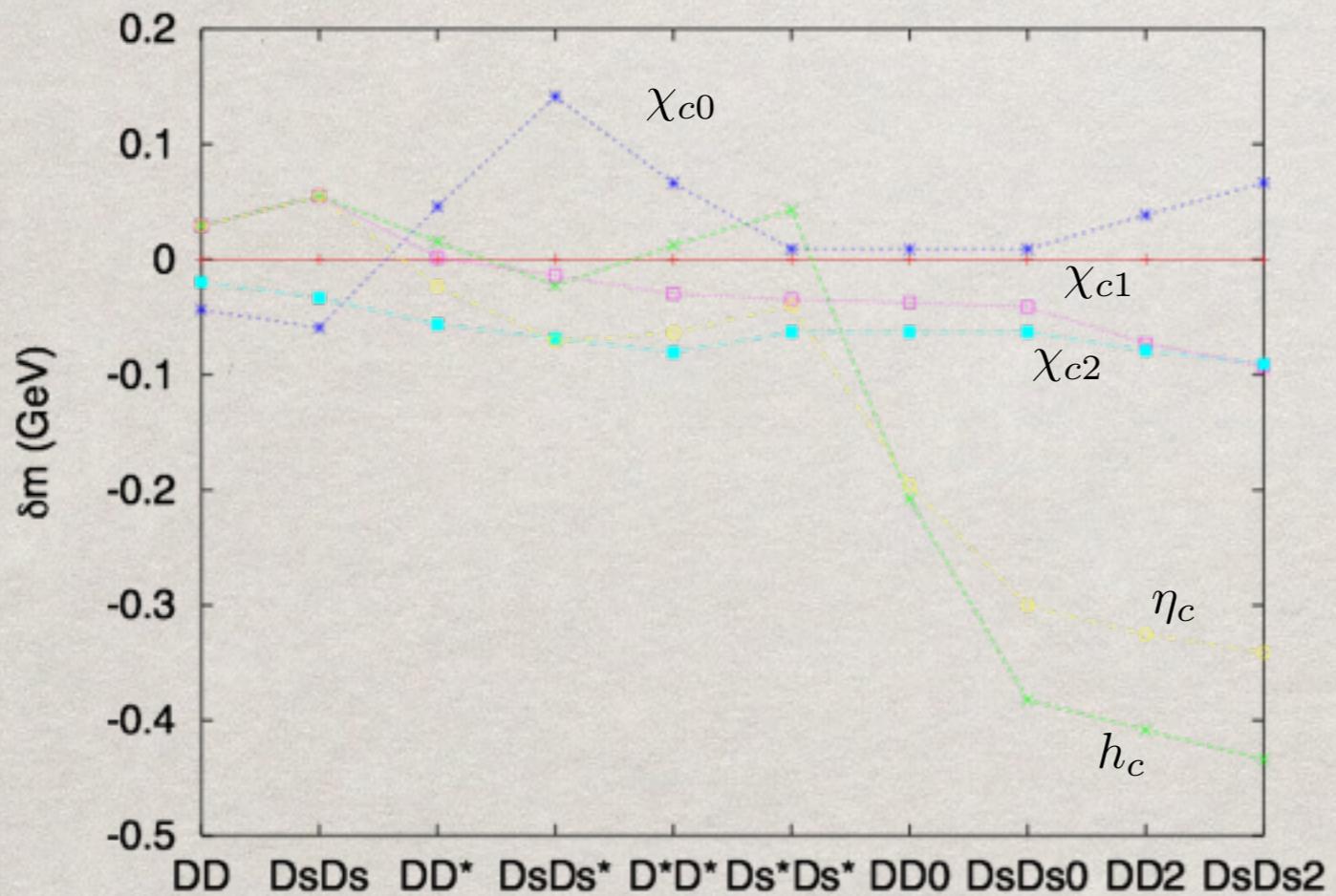
- model vertices in a reasonable way and perform bubble sums
- compare to D D\* pi and pi pi J/psi
- examine the X(3872): interplay of cusp, possible bound state dynamics, and mixing with cc states



$$-1 = -1 - \text{cusp loop}$$

$$\alpha \square \beta = \alpha \bullet \beta + \alpha \bullet \gamma \square \beta$$

# Cusp Model — to do



Need to correctly renormalise  
the bare model (in this case,  
the constituent quark model)

# Conclusions

- there are a lot of new states, not all of them are ‘real’!
- $X(3872)$  appears to be a likely cusp/molecule/charmonium mixture supernumerary state
- cusp effects can be important and should be accounted for when modelling
- it appears likely (?) that the  $Z_b$  and  $Z_c$  states are not associated with S-matrix poles
- analogue states will appear in many places, but must not be swamped in the production

+ ÆRIC MEC HEHT GEWYRCAN

