
Studying GPDs at Jefferson Lab

S. Stepanyan (JLAB)

6th Workshop of the APS Topical Group on Hadronic Physics
April 8-10, 2015, Baltimore, Maryland

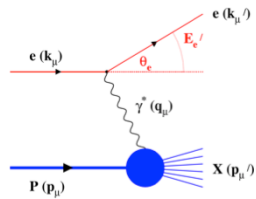


- 3-D picture of the nucleon and GPDs
- Extracting GPDs from experimental observables
- DVCS experiments with JLAB-6 GeV
- Future plans with upgraded JLAB-12 GeV
- Summary

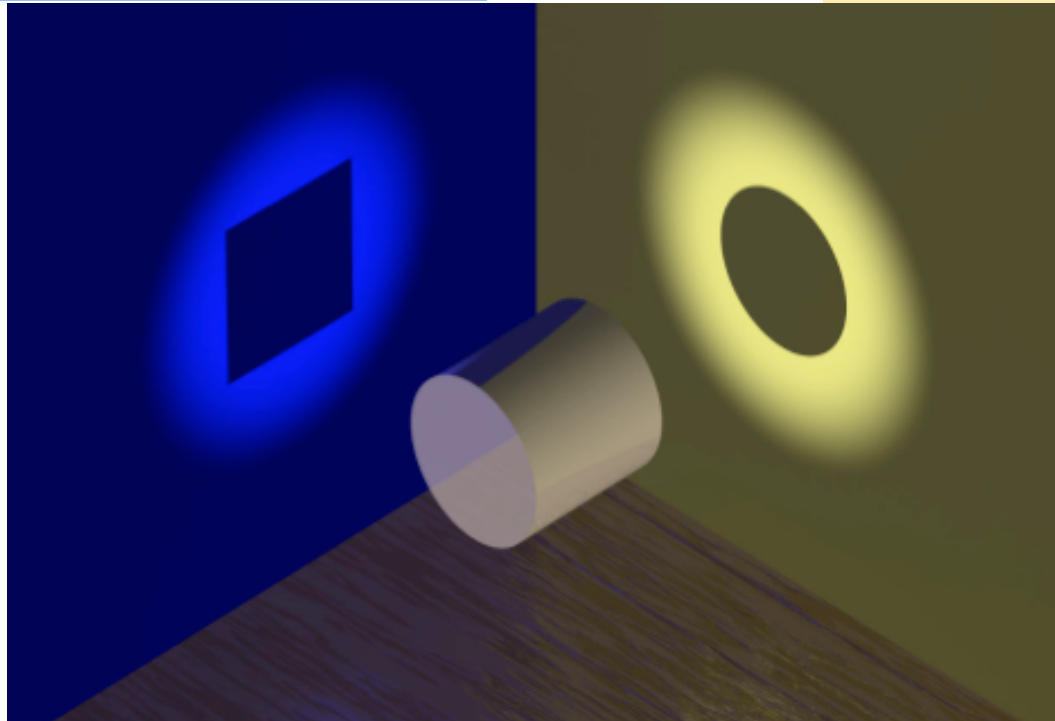


3-D Picture of the Nucleon

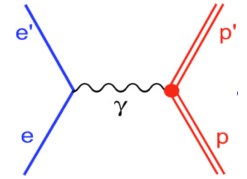
DIS Parton Distribution Functions



No information on the spatial location of the constituents



Elastic Form Factors



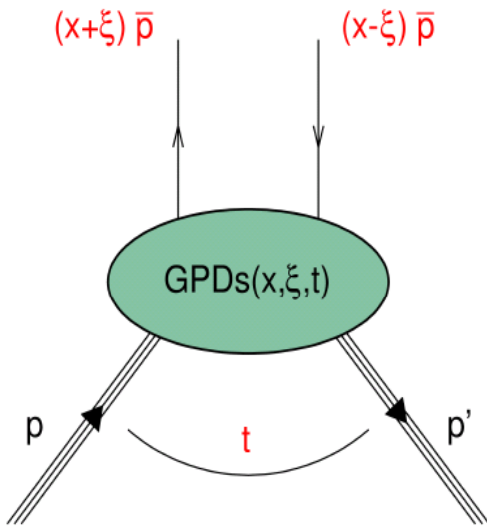
No information about the underlying dynamics of the system

Transverse Momentum Distributions & Generalized Parton Distributions

3-D imaging of the nucleon, the correlation of quark/antiquark transverse spatial and longitudinal momentum distributions, and on the quark angular momentum distribution



GPDs, PDFs, FFs



Four chiral-even GPDs:

$$H^q; E^q; \tilde{H}^q; \tilde{E}^q$$

- **GPDs** → PDFs (in the limite $t \rightarrow 0$)

$$H^q(x,0,0) = q(x), -\bar{q}(-x)$$

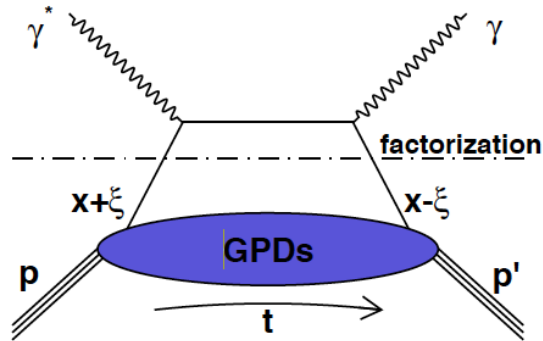
$$\tilde{H}^q(x,0,0) = \Delta q(x), \Delta \bar{q}(-x)$$

- **GPDs** → FFs (first moments of GPDs)

$$\int_{-1}^{+1} dx H^q(x, \xi, t) = F_1^q(t) \quad \int_{-1}^{+1} dx \tilde{H}^q(x, \xi, t) = g_A^q(t)$$

$$\int_{-1}^{+1} dx E^q(x, \xi, t) = F_2^q(t) \quad \int_{-1}^{+1} dx \tilde{E}^q(x, \xi, t) = h_A^q(t)$$

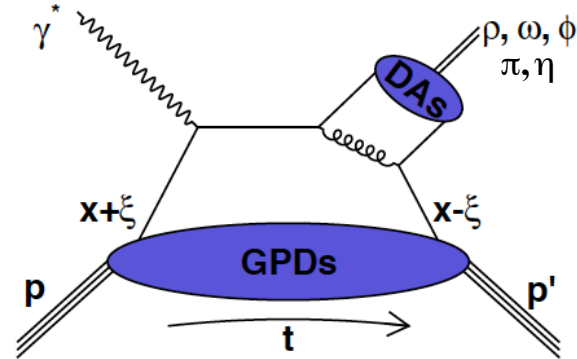
Deep-exclusive reactions and GPD



DVCS

	$\mathcal{I}m$	$\mathcal{R}e$
\mathcal{H}	A_{LU}	σ
$\tilde{\mathcal{H}}$	A_{UL}	
\mathcal{E}	A_{UT}	
		A_{LL}, A_{LT}

A global analysis is needed to fully disentangle GPDs



DVMP

	Meson	Flavor
$\mathcal{H}_{T, \mathcal{E}T}$	π^+	$\Delta u - \Delta d$
	π^0	$2\Delta u + \Delta d$
	η	$2\Delta u - \Delta d + 2\Delta s$
\mathcal{H}, \mathcal{E}	ρ^+	$u - d$
	ρ^0	$2u + d$
	ω	$2u - d$
	ϕ	g

Disentangling GPDs – model simulations

Global fit to the DVCS data, using models of GPDs - M. Guidal, Eur.Phys.J. **A37**, p319 (2008)

8 independent quantities to be fit -

$$\text{Im}(\mathbf{H}); \text{Im}(\mathbf{E}); \text{Im}(\tilde{\mathbf{H}}); \text{Im}(\tilde{\mathbf{E}})$$

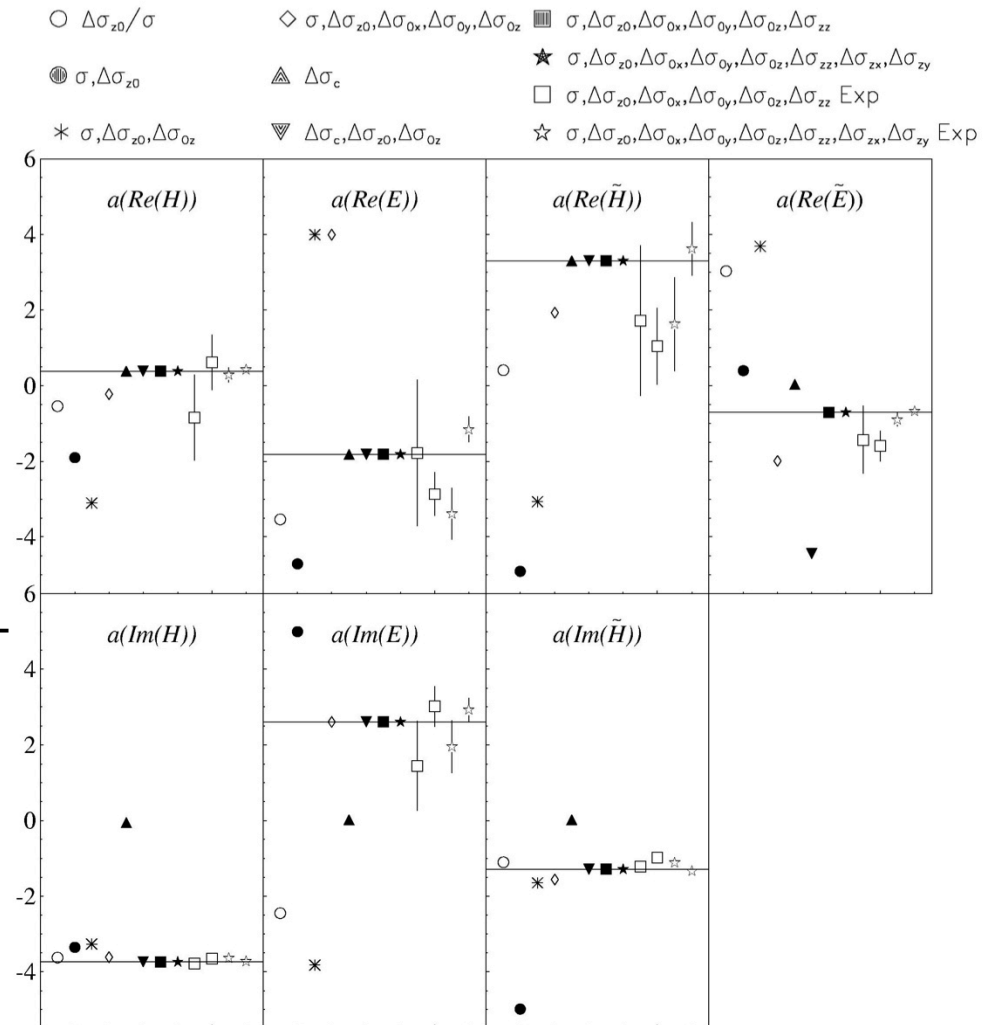
$$\text{Re}(\mathbf{H}); \text{Re}(\mathbf{E}); \text{Re}(\tilde{\mathbf{H}}); \text{Re}(\tilde{\mathbf{E}})$$

Using 9 independent observables -

$$\sigma; \Delta\sigma_{z0}; \Delta\sigma_{0x}; \Delta\sigma_{0y}; \Delta\sigma_{0z};$$

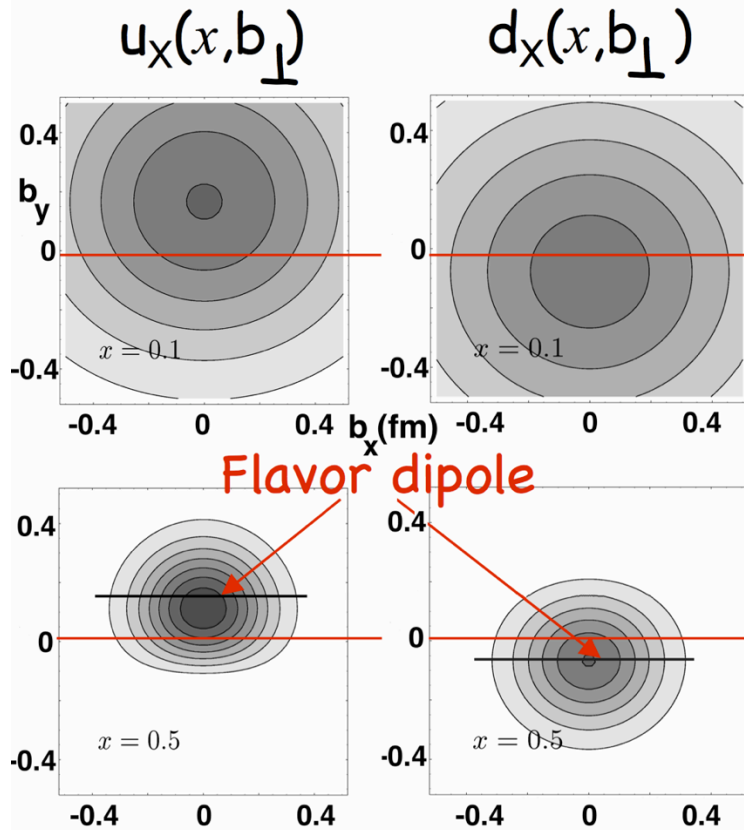
$$\Delta\sigma_{zx}; \Delta\sigma_{zy}; \Delta\sigma_{zz}; \Delta\sigma_c;$$

Assumption - $\text{Im}(\tilde{\mathbf{E}}) = 0$



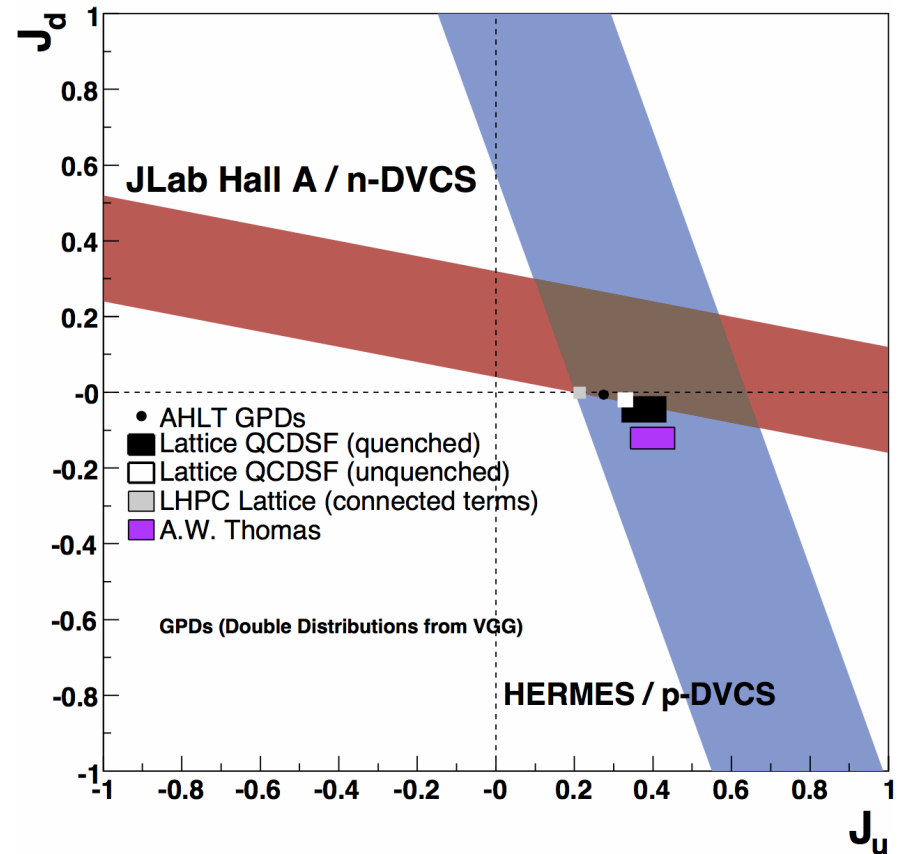
Angular momentum and Transverse Imaging

Target polarization



M. Burkardt, Int.J.Mod.Phys.A18:173-208,2003

$$J_q = \frac{1}{2} \Delta\Sigma + L_q = \lim_{t \rightarrow 0} \int_{-1}^{+1} dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

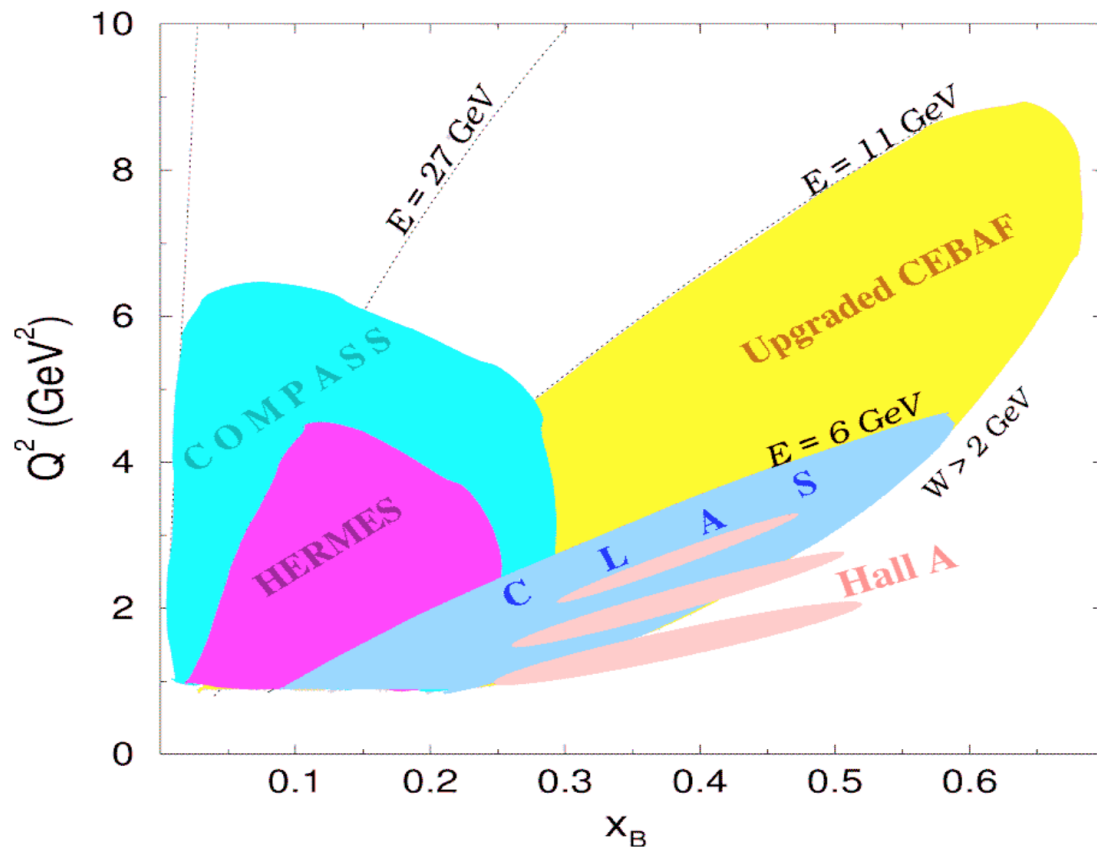


M. Mazouz et al., Phys.Rev.Lett.99:242501,2007

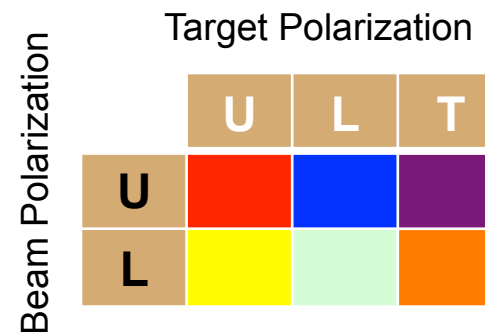


S. Stepanyan, GHP2015





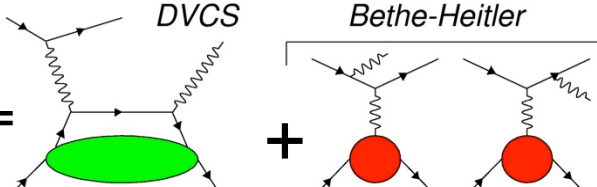
JLAB kinematic and experimental reach



Reaction	γ			$\pi^+/\pi^-/\pi^0$			η			$\rho/\omega/\phi$		
Deeply exclusive (GPDs)												



Accessing GPDs experimentally - DVCS

$ep \rightarrow e\gamma p =$


$$\mathcal{T}^2 = |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \mathcal{T}_{DVCS}^* \mathcal{T}_{BH} + \mathcal{T}_{BH}^* \mathcal{T}_{DVCS}$$

$$\mathcal{T}_{DVCS} \sim CFF \quad \mathcal{H}(\xi, t) = \underbrace{i\pi [H(\xi, \xi, t) - H(-\xi, \xi, t)]}_{Im} + P \underbrace{\int_{-1}^{+1} dx \left(\frac{1}{\xi - x} \pm \frac{1}{\xi + x} \right) [H(x, \xi, t) \mp H(-x, \xi, t)]}_{Re}$$

Spin asymmetries (Im, $x=\xi$)

HERMES, CLAS, Hall A, JLAB12, COMPASS

Charge asymmetry ($|\text{Re}|$)
HERMES, COMPASS

$H(x, \xi, 0)$

10
7.5
5
2.5
0
-2.5

0.5

x

0

-0.5

Cross sections ($|\text{Re}|^2$)
H1, Hall A, JLAB12, COMPASS

0.4
0.6
0.8
 ξ

DDVCS ($x \neq \xi$) - JLAB12



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GPDs and DVCS spin observables

Polarized **beam**, unpolarized **proton** target:

$$\Delta\sigma_{LU} \propto \sin\phi \cdot \text{Im}\{F_1^p H_p + \xi(F_1^p + F_2^p)\tilde{H}_p + kF_2^p E_p\}d\phi$$

Kinematically suppressed

Unpolarized beam, **longitudinal proton** target:

$$\Delta\sigma_{UL} \propto \sin\phi \cdot \text{Im}\{F_1^p \tilde{H}_p + \xi(F_1^p + F_2^p)(H_p + \dots)\}d\phi$$

Unpolarized beam, **transverse proton** target:

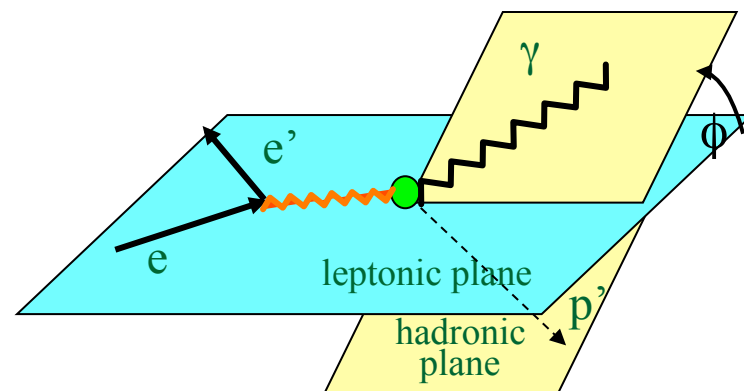
$$\Delta\sigma_{UT} \propto \sin\phi \cdot \text{Im}\{k(F_1^p H_p - F_1^p E_p) + \dots\}d\phi$$

Polarized **beam**, unpolarized **neutron** target:

$$\Delta\sigma_{LU} \propto \sin\phi \cdot \text{Im}\{F_1^n H_n + \xi(F_1^n + F_2^n)\tilde{H}_n + kF_2^n E_n\}d\phi$$

$$H_p(\xi, \xi, t) = 4/9 H_u(\xi, \xi, t) + 1/9 H_d(\xi, \xi, t)$$

$$H_n(\xi, \xi, t) = 1/9 H_u(\xi, \xi, t) + 4/9 H_d(\xi, \xi, t)$$



$$A = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma}{2\sigma}$$

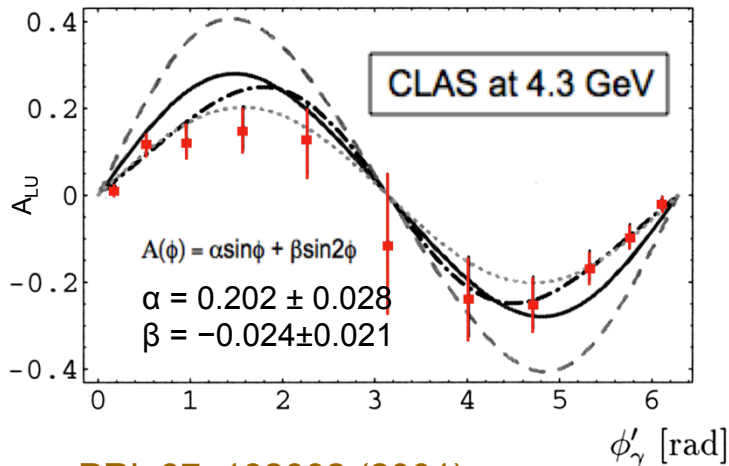
Experiments for all combinations of polarized and unpolarized beam and target have been approved by JLAB PAC

First DVCS measurements

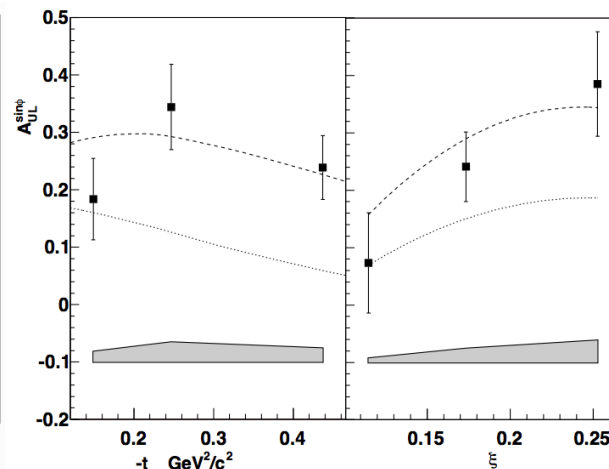
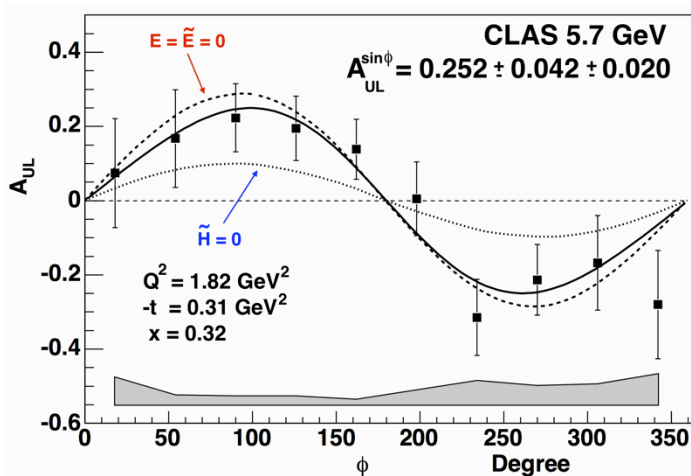
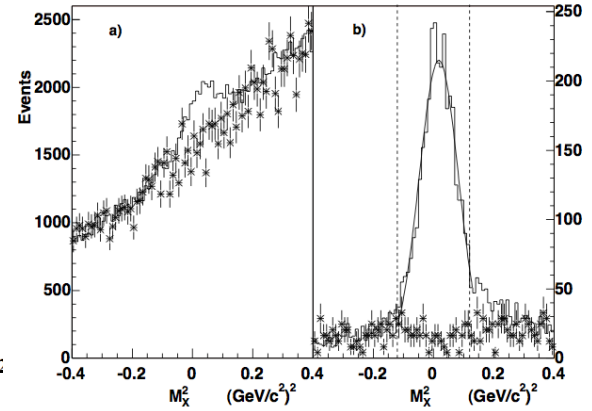
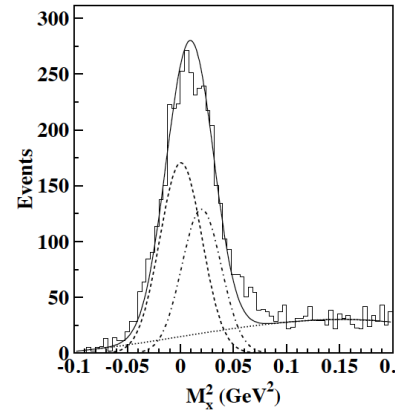
Analysis of existing CLAS data

Reaction: $ep \rightarrow e'p'X$

Missing momentum analysis $X \approx \gamma$



[PRL 87, 182002 \(2001\)](#)



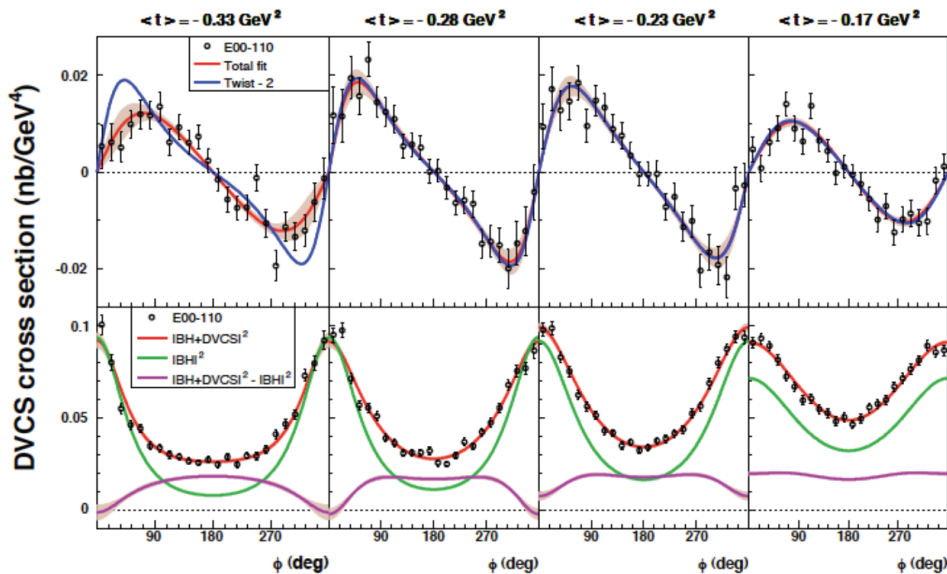
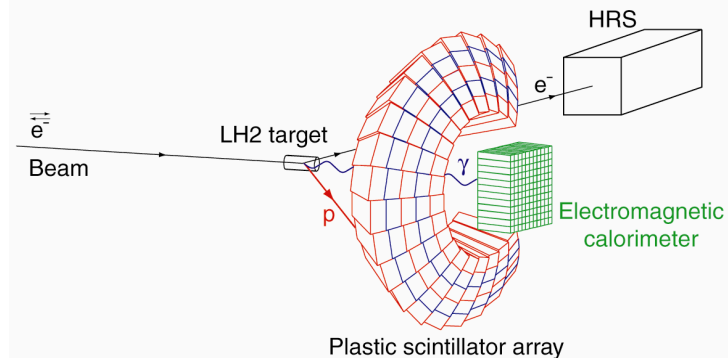
$$A_{UL}(\phi) = \frac{N^\uparrow(\phi) - N^\downarrow(\phi)}{f(P_t^\downarrow N^\uparrow(\phi) + P_t^\uparrow N^\downarrow(\phi))}$$

[PRL 97, 072002 \(2006\)](#)



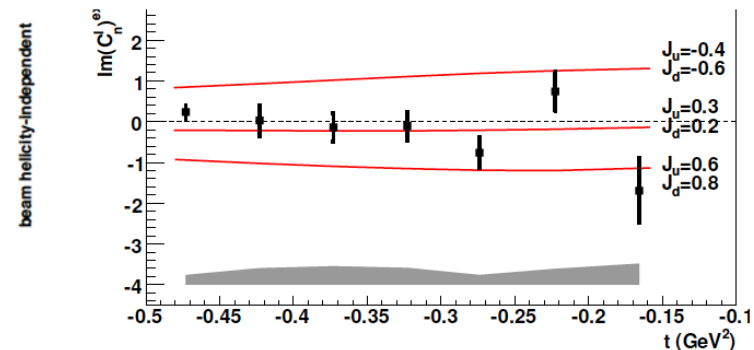
Hall-A DVCS measurements

- Helicity-dependent cross section ($\vec{\sigma} - \vec{\sigma}$) at $Q^2 = 1.5, 1.9$ and 2.3 GeV^2
- Helicity-independent cross section ($\vec{\sigma} + \vec{\sigma}$) at $Q^2=2.3 \text{ GeV}^2$
- Twist-2 dominance is observed



Phys. Rev. Lett. 97, 262002 (2006)

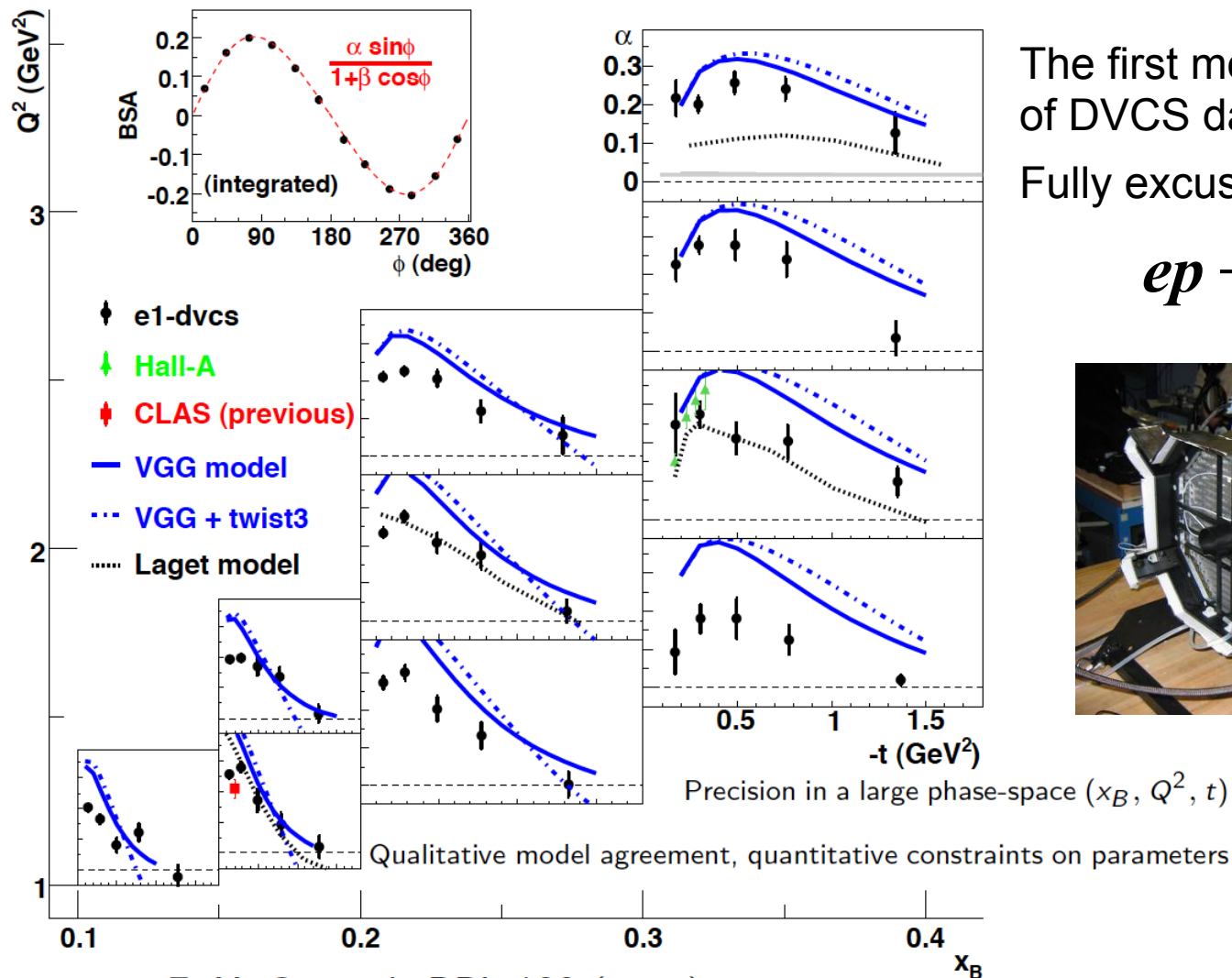
With an additional charged particle veto in front of the proton detector DVCS on neutron has been measured, where the main contribution is from GPD \mathcal{E}
 LD₂ target ($F_2^n(t) \gg F_1^n(t)$!)



$$\sigma^{\rightarrow} - \sigma^{\leftarrow} = \Gamma(A \sin \varphi + \dots)$$

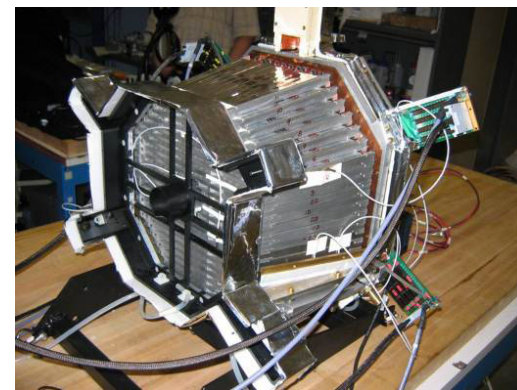


CLAS DVCS beam spin asymmetry



The first most extensive set of DVCS data with CLAS
Fully exclusive final state

$$ep \rightarrow e'p'\gamma$$



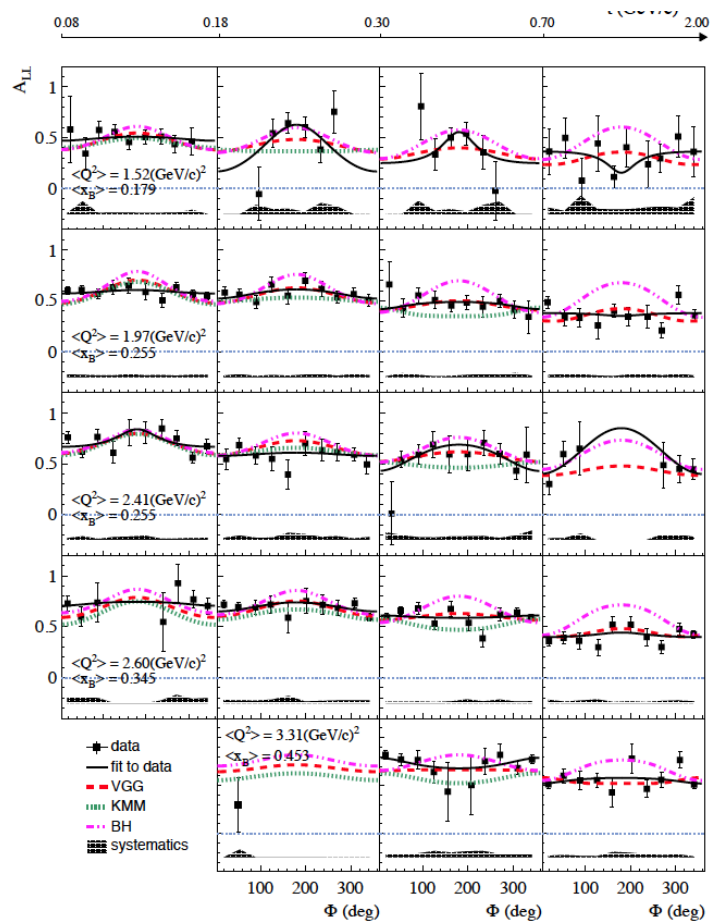
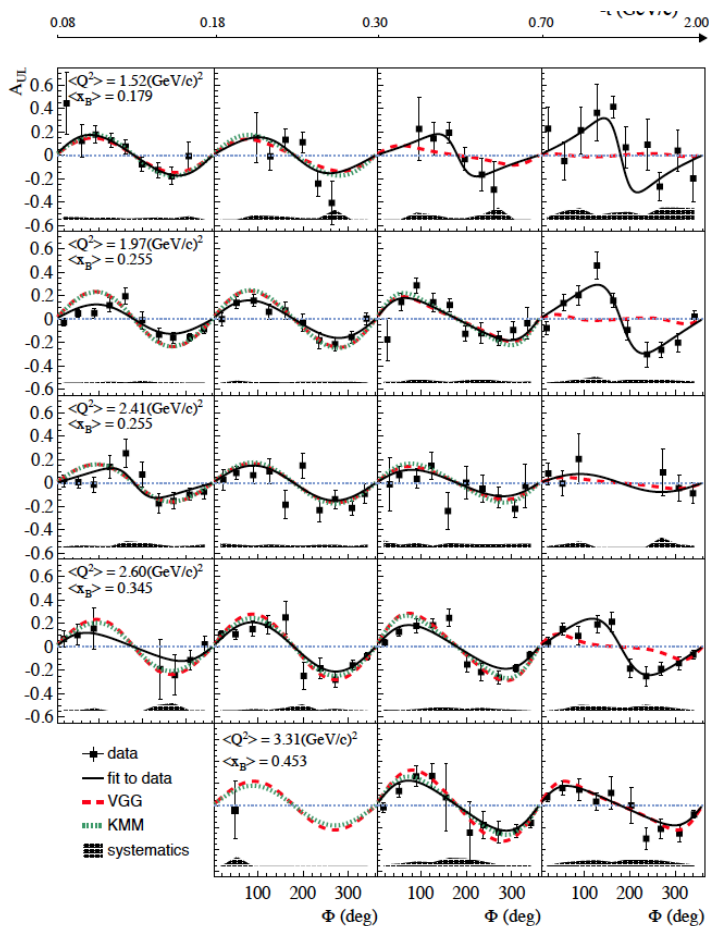
F.-X. G. *et al.*, PRL 100 (2008) 162002



CLAS target and double spin asymmetry

$$A_{UL} \propto F_1 \mathcal{I}m \tilde{H}$$

$$A_{LL} \propto F_1 \mathcal{R}e \tilde{H}$$

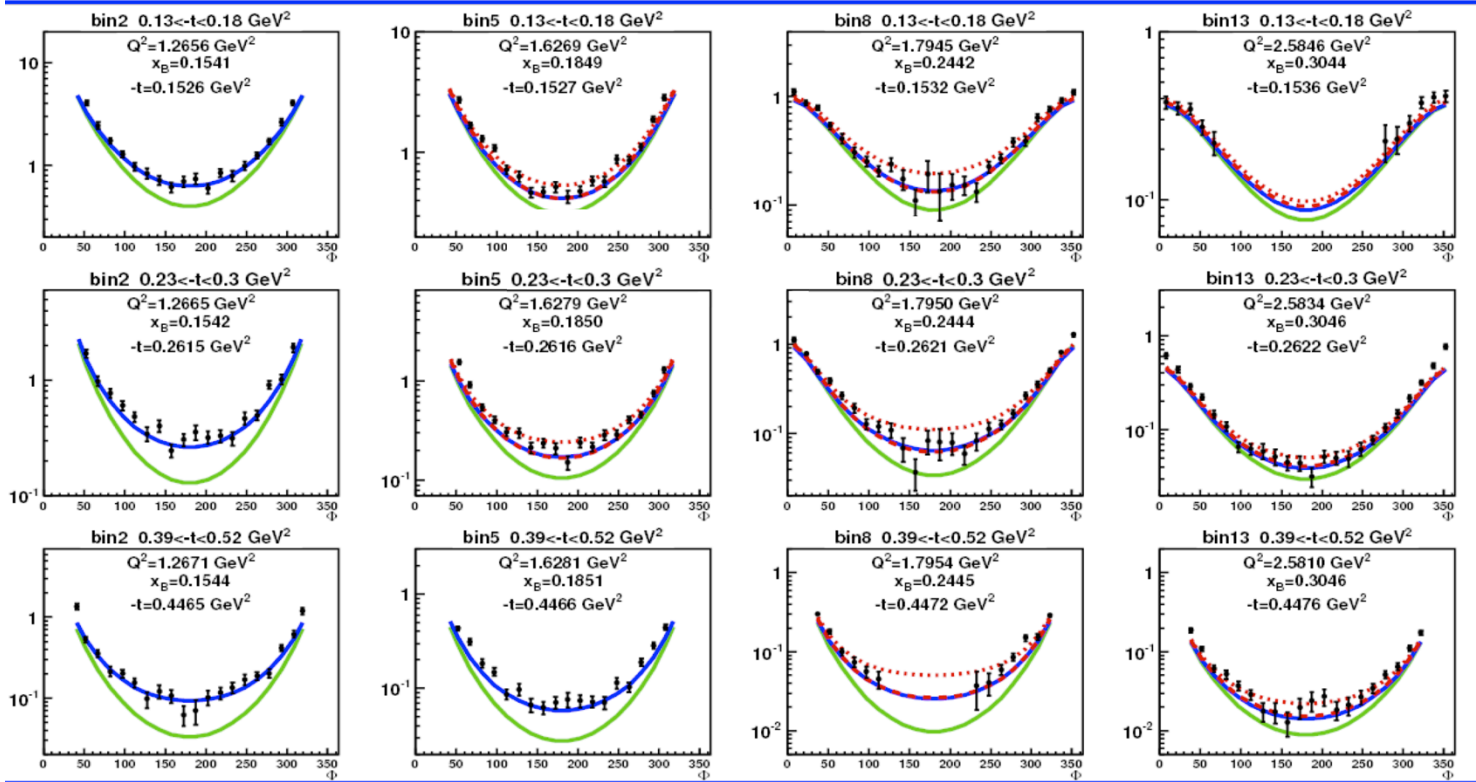


E. Seder et al., Phys. Rev. Lett. 114, 032001 (2015)

S. Pisano et al., Phys. Rev. D 91, 052014



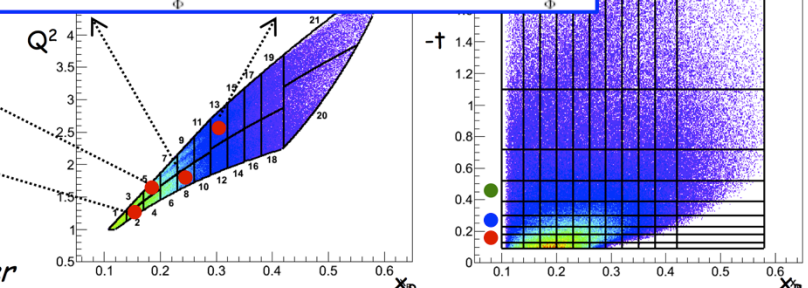
CLAS DVCS cross sections



●
●
●

$$\bullet \frac{d^4\sigma_{ep \rightarrow e\gamma}}{dQ^2 dx_B dt d\Phi} \text{ (nb/GeV}^4\text{)}$$

— BH — VGG (H only)
 KM10 - - - KM10a



VGG : Vanderhaeghen, Guichon, Guidal

KM : Kumericki, Mueller



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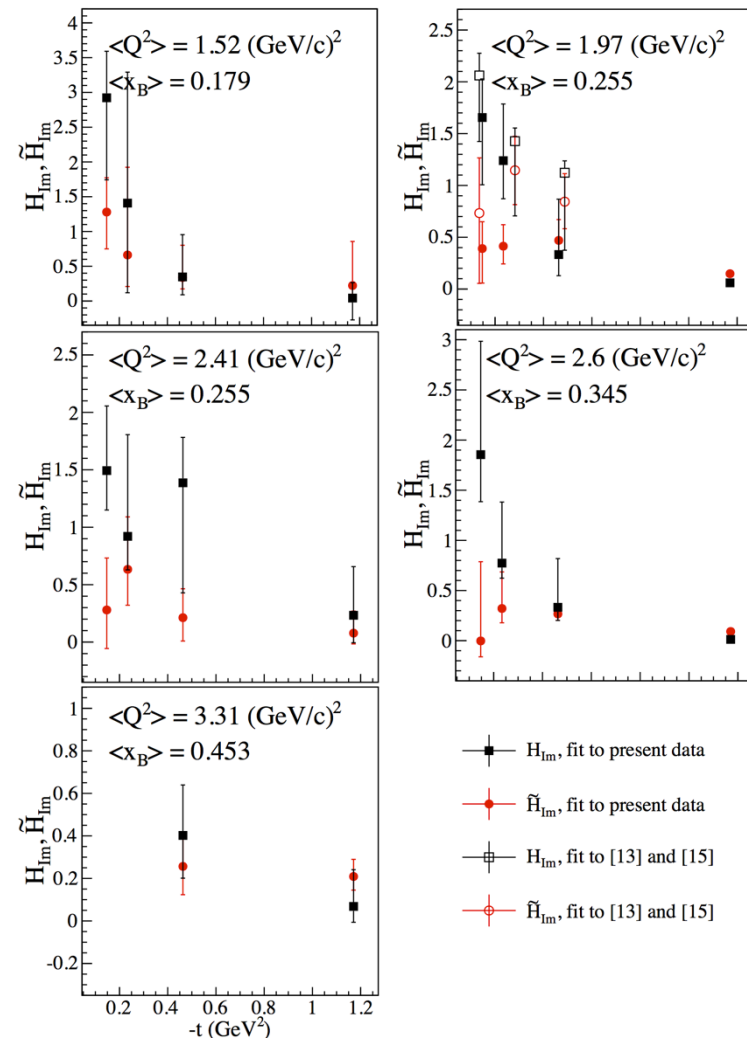
Extracting Compton form-factors

- The three sets of asymmetries (BSA, TSA and DSA) for all kinematic bins were processed using the local fitting procedure to extract the Compton FF
- In the fit \tilde{E}_{Im} is set to zero, as \tilde{E} is assumed to be purely real
- Thus seven out of the eight real and imaginary parts of the CFFs are left as free parameters in the fit

$$F_{\text{Re}}(\xi, t) = \Re e \mathcal{F}(\xi, t)$$

$$F_{\text{Im}}(\xi, t) = -\frac{1}{\pi} \Im m \mathcal{F}(\xi, t) = [F(\xi, \xi, t) \mp F(-\xi, \xi, t)]$$

- Two out of seven have been reasonably constrained by the fit



S. Pisano et al., Phys. Rev. D 91, 052014

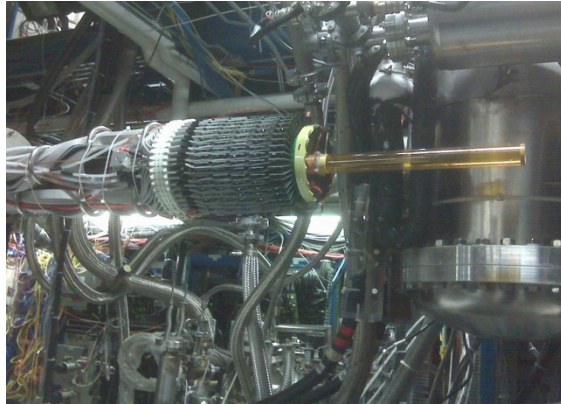


S. Stepanyan, GHP2015



Nuclear GPDs – ^4He (CLAS)

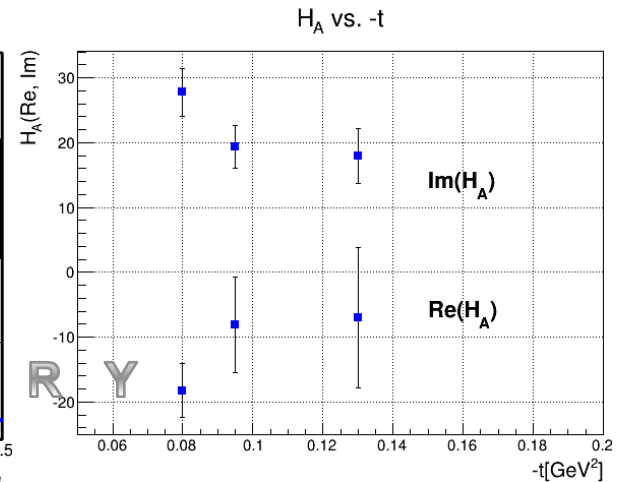
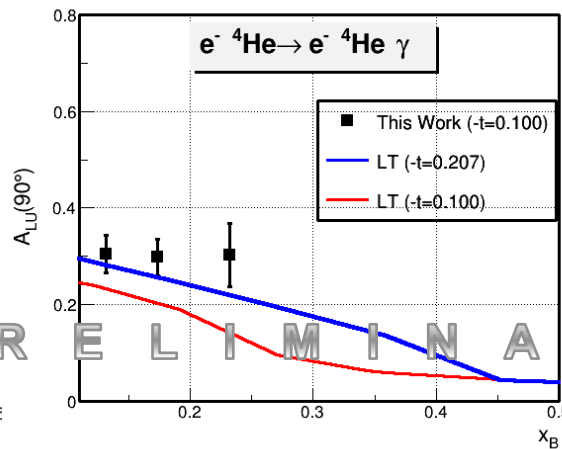
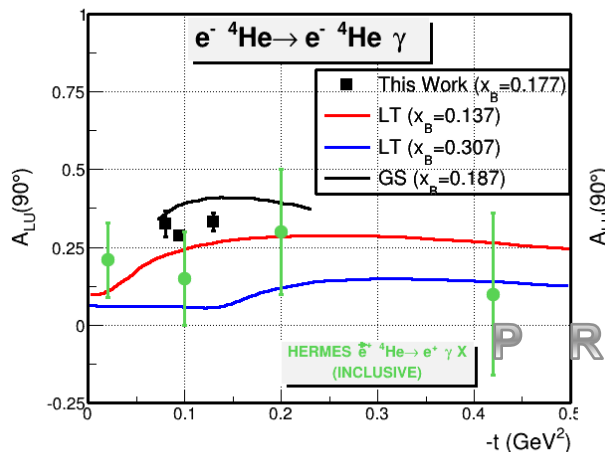
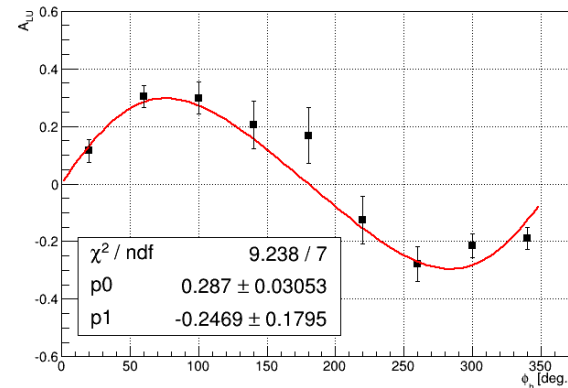
SPIN ZERO target \rightarrow ONE GPD IS NEEDED $H_A(x, \xi, t)$



GEM based low energy recoil detector
Gaseous target at 6 atm, cell 6 mm
ID, 27 μm wall thickness

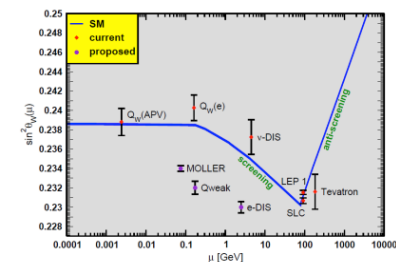
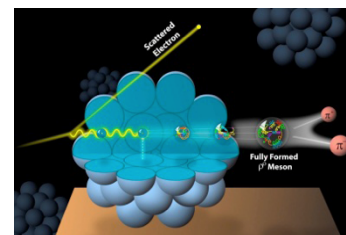
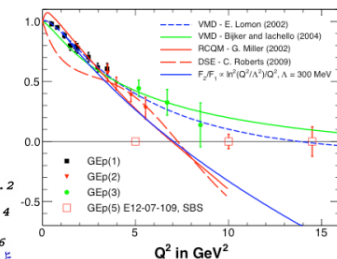
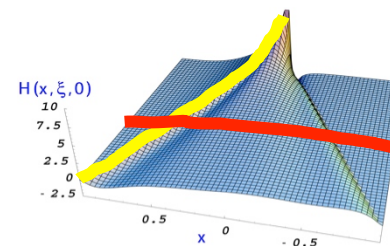
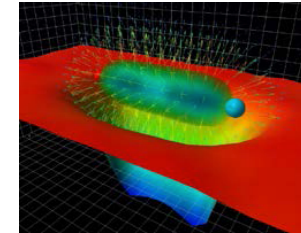
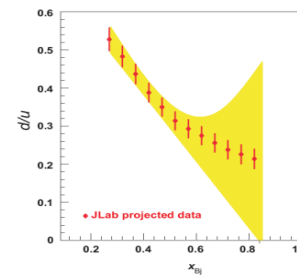
$$A_{LU} = \frac{\alpha_0(\phi) * \mathcal{H}_{Im}}{\alpha_1(\phi) + \alpha_2(\phi)\mathcal{H}_{Re} + \alpha_3(\phi)(\mathcal{H}_{Im}^2 + \mathcal{H}_{Re}^2)}$$

A_{LU} Coherent



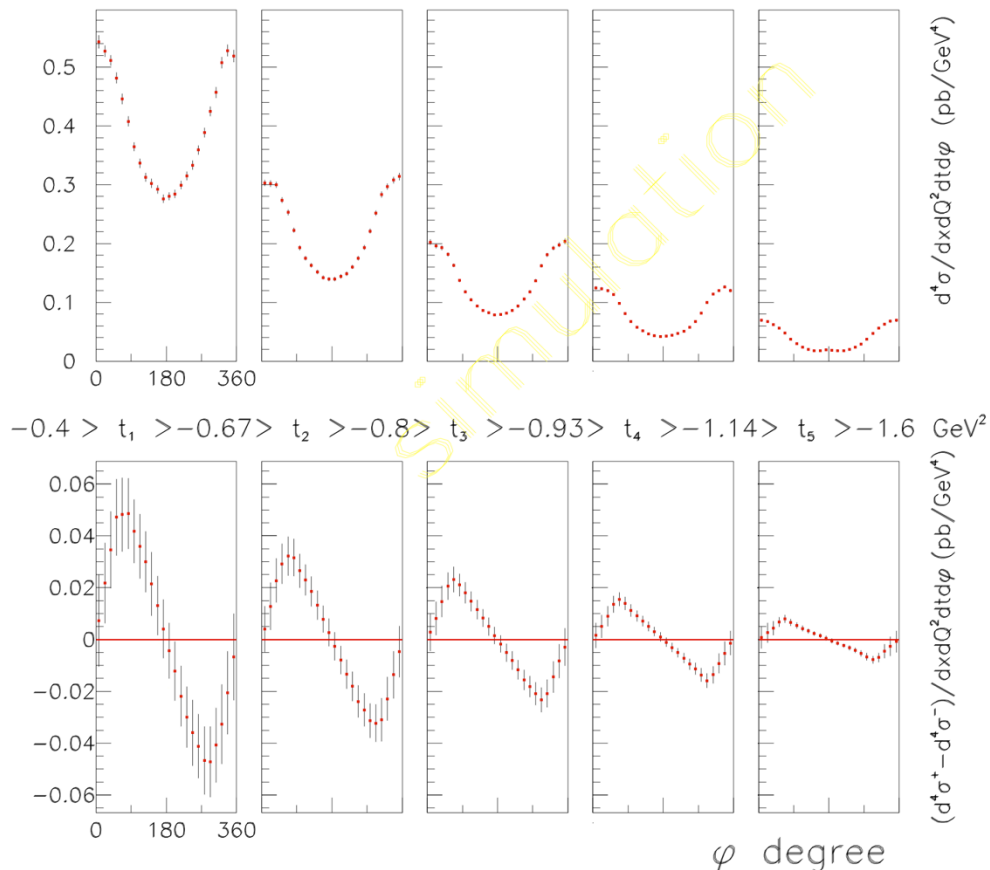
The JLab 12 GeV Upgrade - Major Programs in Six Areas

- The Hadron spectra as probes of QCD (GluEx and CLAS12, heavy baryon and meson spectroscopy)
- The transverse structure of hadrons (Elastic and transition Form Factors)
- The longitudinal structure of the hadrons (Unpolarized and polarized parton distribution functions)
- **The 3D structure of the hadrons (Generalized Parton Distributions and Transverse Momentum Distributions)**
- Hadrons and cold nuclear matter (Medium modification of the nucleons, quark hadronization, N-N correlations, few-body experiments)
- Low-energy tests of the Standard Model and Fundamental Symmetries (Møller, PVDIS, PRIMEX, Heavy Photons)



Hall-A DVCS

$K=11$ GeV, $Q^2=9$ GeV², $x_B=0.6$, $\theta_e=30.23^\circ$, $k=3$ GeV, $\theta_{\text{colo}}=-11^\circ$
 Calo 13x16 Blocks at 3 meters $\mathcal{L}=2.97 \times 10^{38}$ cm⁻²s⁻¹, 400 Hours



- Q^2 up to 9 GeV², only highest Q^2 shown, long lever arm
- Three Different beam energies for Rosenbluth separation of I and DVCS²
- High-precision scaling test on both Re and Im
- Combined with measurements in Hall-C at higher Q^2 and lower x_B will cover significant parameter space



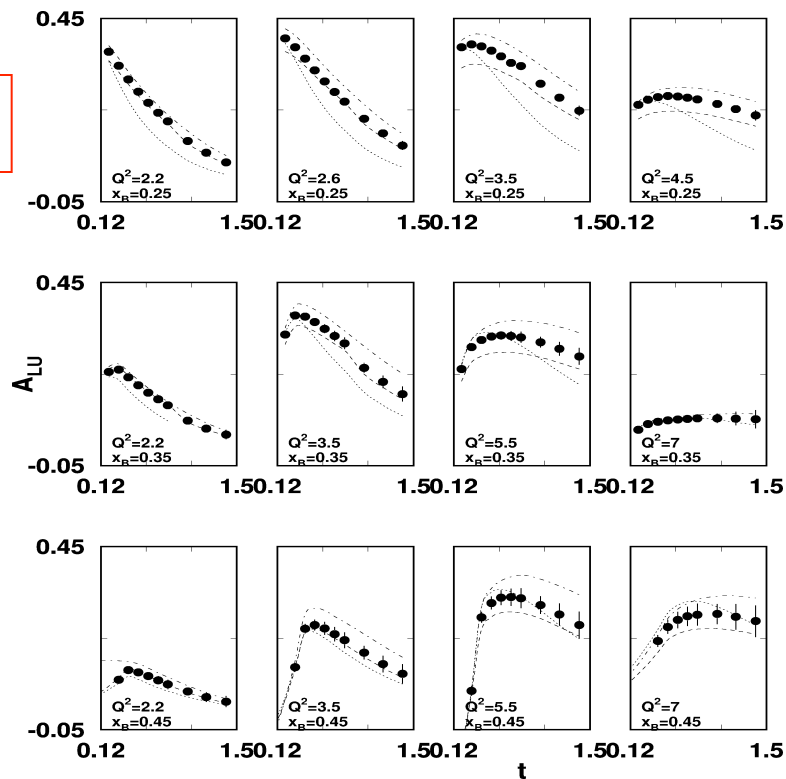
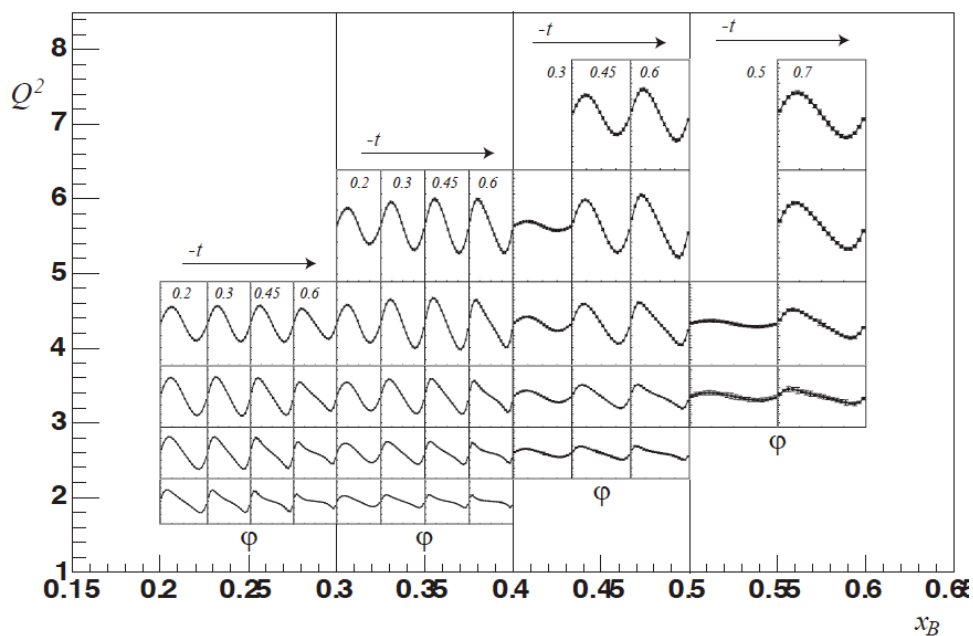
CLAS12 DVCS - longitudinally polarized beam

$$\vec{e} p \rightarrow ep\gamma$$

$$A = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-} = \frac{\Delta\sigma}{2\sigma}$$

Extract $H(\xi, t)$

$$\Delta\sigma_{LU} \sim \sin\phi \{F_1 H + \dots\} d\phi$$



Large coverage in x_B , Q^2 , and t
with high statistical precision



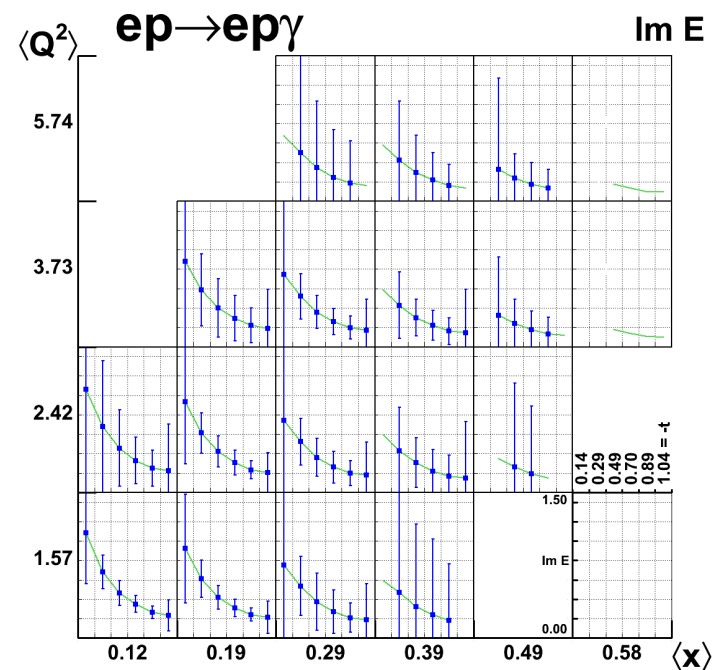
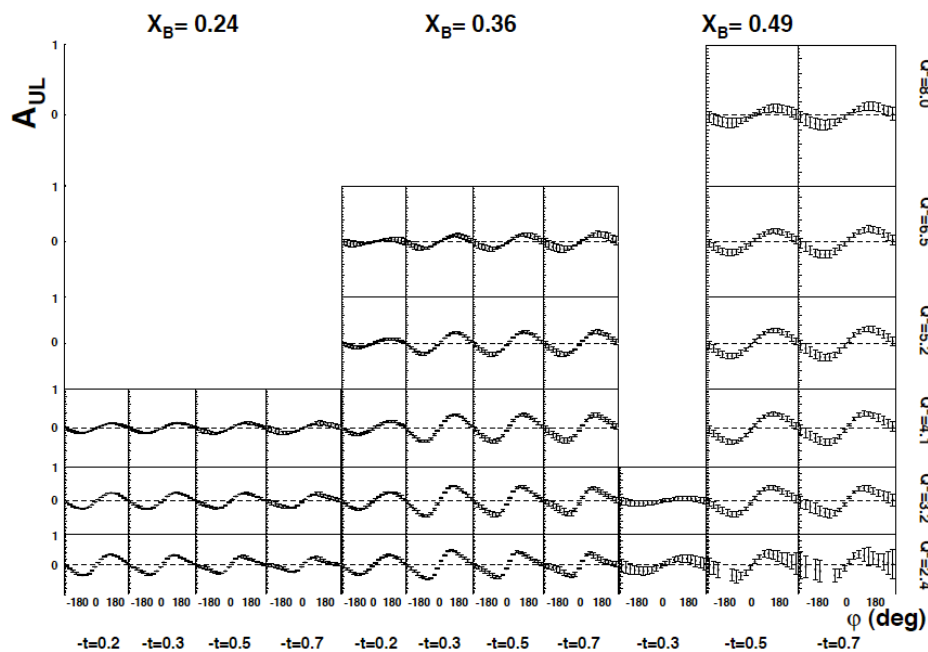
CLAS12 DVCS with polarized targets

$$A_{UL} = \frac{\sigma^{\Rightarrow} - \sigma^{\Leftarrow}}{\sigma^{\Rightarrow} + \sigma^{\Leftarrow}}$$

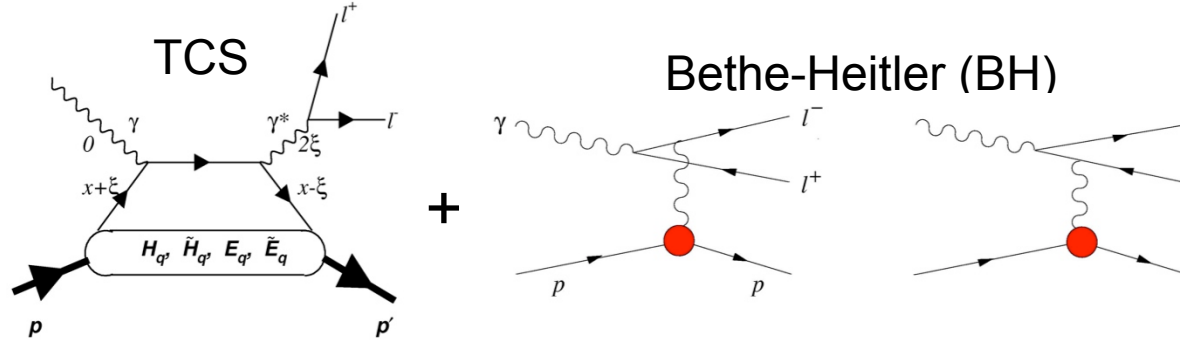
$$A_{UT} = \frac{\sigma^{\Downarrow} - \sigma^{\Uparrow}}{\sigma^{\Downarrow} + \sigma^{\Uparrow}}$$

$$\Delta\sigma_{UL} \sim \sin\phi \operatorname{Im}\{F_1 \tilde{H} + \xi(F_1 + F_2)(H + \dots)\} d\phi$$

$$\Delta\sigma_{UT} \sim \sin\phi \operatorname{Im}\{k(F_2 H - F_1 E) + \dots\} d\phi$$



Time-like Compton Scattering (TCS)



$$\frac{d^4\sigma}{dx_B dQ^2 dt d\phi} \propto |T^{BH}|^2 + T^{BH} \cdot \text{Re}(T^{VCS}) + \lambda T^{BH} \cdot \text{Im}(T^{VCS}) + |T^{VCS}|^2$$

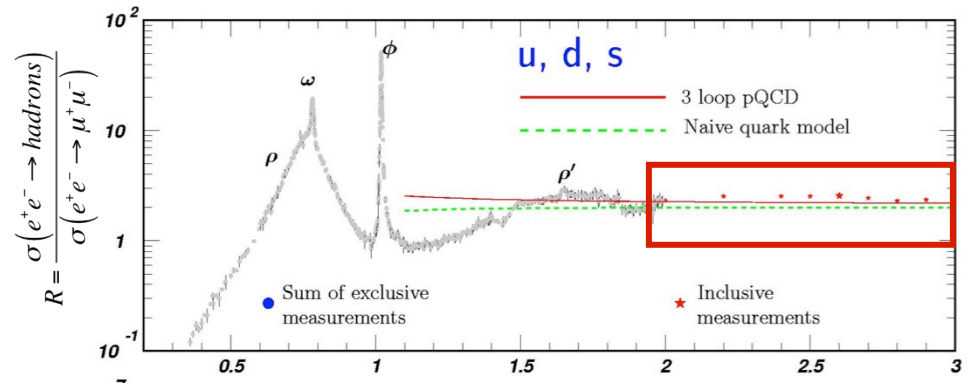
$$\begin{aligned} \frac{d\sigma_{INT}}{dQ'^2 dt d(\cos\theta) d\phi} = & -\frac{\alpha_{em}^3}{4\pi s^2} \frac{1}{-t} \frac{M}{Q'} \frac{1}{\tau\sqrt{1-\tau}} \frac{L_0}{L} \left[\cos\varphi \frac{1+\cos^2\theta}{\sin\theta} \text{Re}\tilde{M}^{--} \right. \\ & \left. - \cos 2\varphi \sqrt{2} \cos\theta \text{Re}\tilde{M}^{0-} + \cos 3\varphi \sin\theta \text{Re}\tilde{M}^{+-} + O\left(\frac{1}{Q'}\right) \right] \\ & - \lambda \frac{\alpha_{em}^3}{4\pi s^2} \frac{1}{-t} \frac{M}{Q'} \frac{1}{\tau\sqrt{1-\tau}} \frac{L_0}{L} \left[\sin\varphi \frac{1+\cos^2\theta}{\sin\theta} \text{Im}\tilde{M}^{--} \right. \\ & \left. - \sin 2\varphi \sqrt{2} \cos\theta \text{Im}\tilde{M}^{0-} + \sin 3\varphi \sin\theta \text{Im}\tilde{M}^{+-} + O\left(\frac{1}{Q'}\right) \right]. \end{aligned}$$

Universality of GPDs

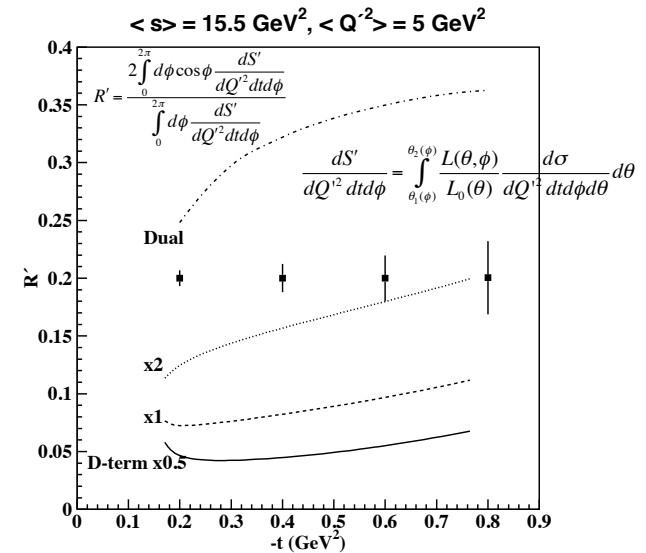
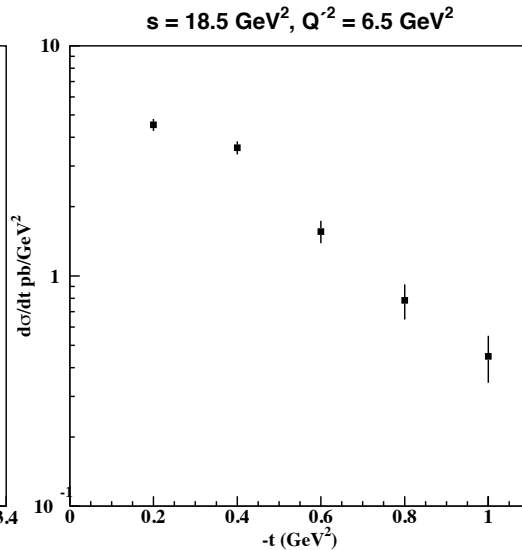
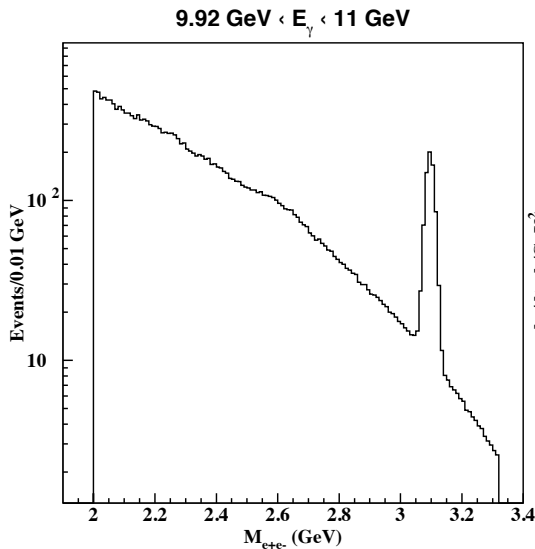
$$\tilde{M}^{--} = \frac{2\sqrt{t_0-t}}{m} \frac{1-\eta}{1+\eta} \left[F_1 \mathcal{H} - \eta(F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4m^2} F_2 \mathcal{E} \right]$$

TCS with 11 GeV electron beam

Lepton pair production will be studied in the range of outgoing photon virtualities $M_{ee}^2 \equiv Q'^2$ from 4 GeV^2 to 9 GeV^2 (above the light-quark meson resonances and below charm threshold)



100 days of running at luminosity of $10^{35} \text{ cm}^{-2} \text{ sec}^{-1}$



Summary

- DVCS clearly is the best channel to study GPDs
- After the first proof-of-principal BSA and TSA results in DVCS from CLAS data mining efforts, JLAB made significant investment in dedicated experiments where BSA and TSA on proton and neutron targets were explored
- The new set of data initiated new theoretical approaches for extracting GPDs from experimental observables
- The 12 GeV Upgrade will greatly enhance the scientific “reach” of JLAB facility
- Detectors in experimental halls are well suited to carry out vigorous program for studying the nucleon structure in terms of GPDs
- Experimental program includes DVCS measurements with polarized beams and targets on the proton and the neutron, as well as Deeply Virtual Meson Production, and Time-like Compton Scattering – not all approved experiment have been covered in this talk
- Solid and CLAS12 collaborations exploring possibilities of Double DVCS measurements with improved detector in near future

