

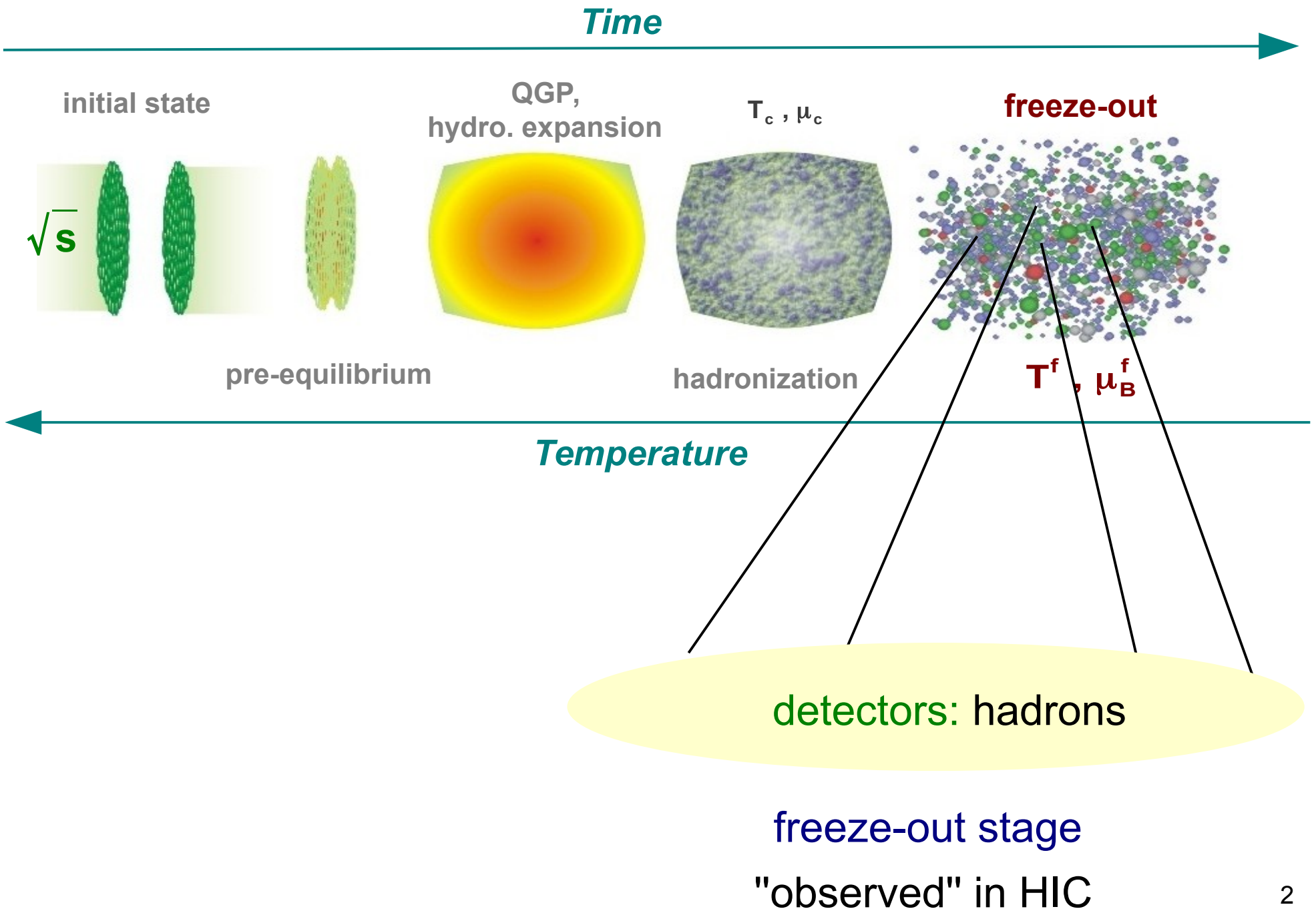
Thermodynamic Signatures of Additional Strange and Charm Baryons

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April 2015, GHP, Baltimore, MD

Heavy-ion collisions: a sketch



Hadrons yields at the freeze-out

well described by: **Hadron Resonance Gas (HRG)**

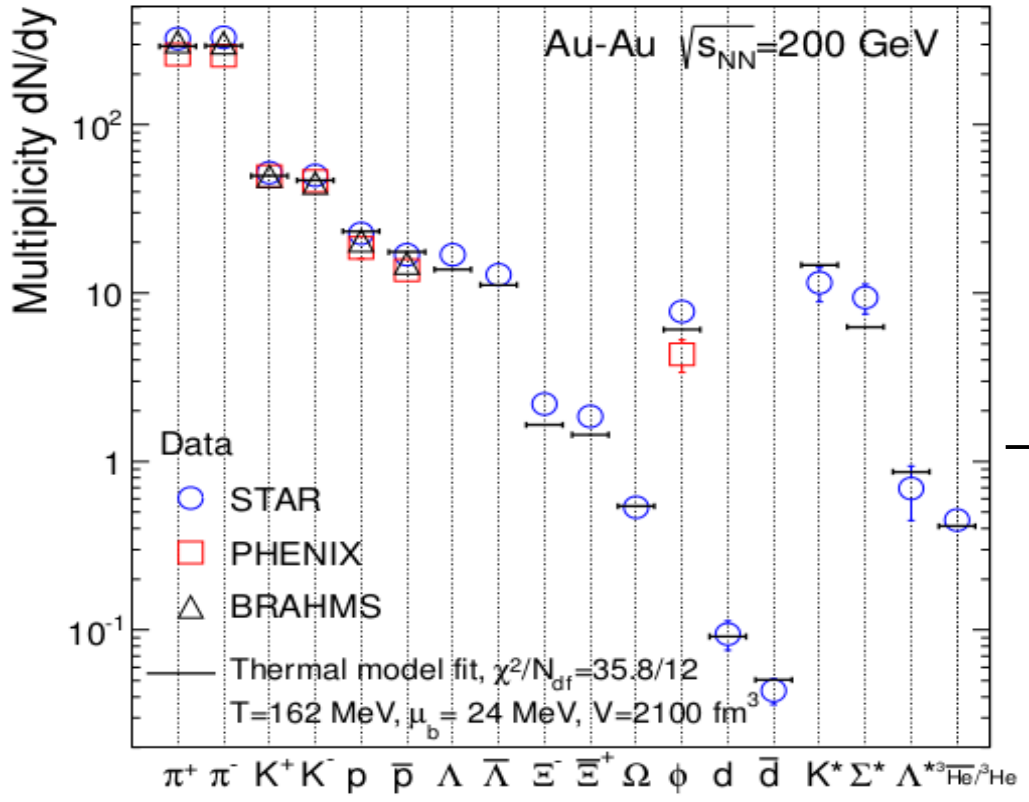
thermal gas of uncorrelated hadrons with vacuum masses

$$\hat{P}_h \sim f(\hat{m}_h) \cosh [B_h \hat{\mu}_B + Q_h \hat{\mu}_Q + S_h \hat{\mu}_S + C_h \hat{\mu}_C]$$

thermal abundance of hadrons
compare with expt. hadron yields

$$\hat{P}_{tot} = \sum_{\text{all hadrons}} \hat{P}_h$$

hat \rightarrow dimensionless in T units



freeze-out parameters

$$\left(T^f, \mu_B^f, \mu_Q^f, \mu_S^f \right)$$

thermal conditions
"observed" in HIC

LQCD: validity of hadronic description

baryon – charge/strangeness/charm correlations:

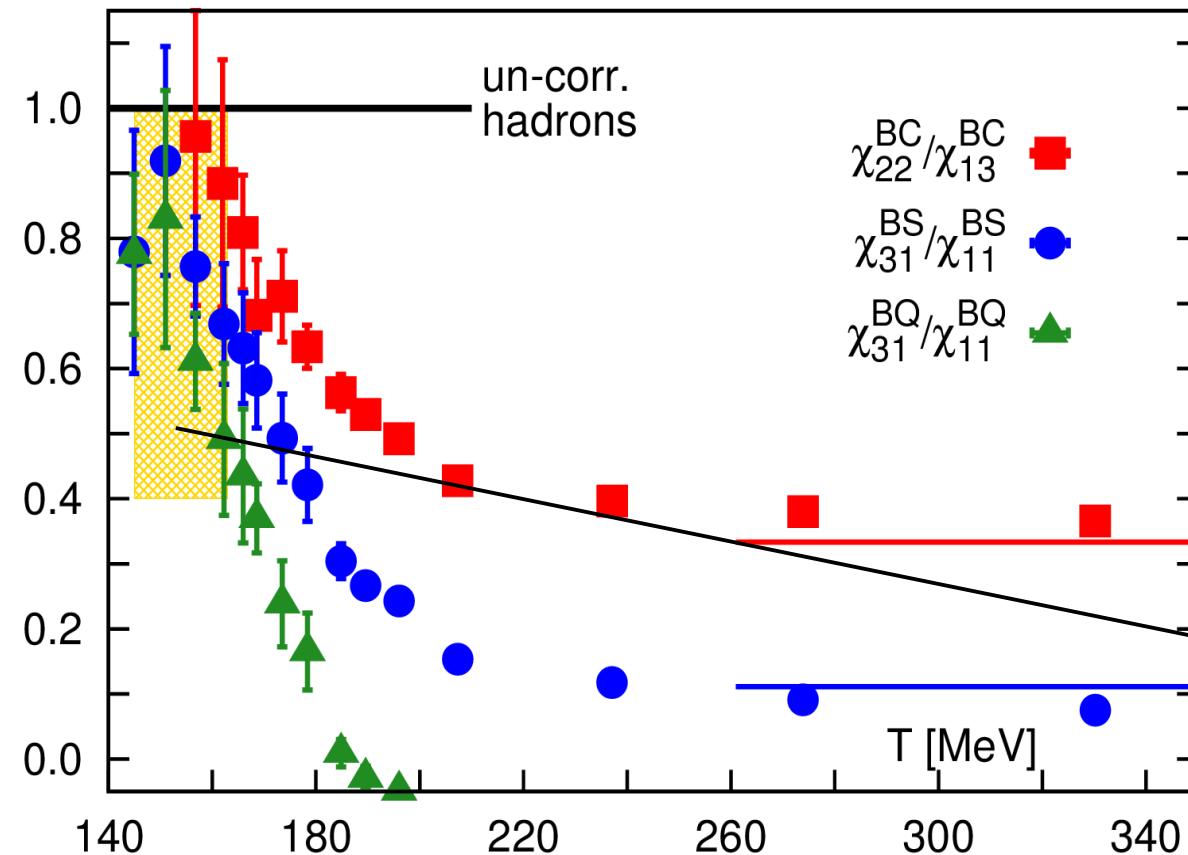
$$\chi_{BX}^{nm} = \left. \frac{\partial^{n+m} \hat{P}}{\partial^n \hat{\mu}_B \partial^m \hat{\mu}_X} \right|_{\hat{\mu}=0}$$

HRG: $\hat{P}_h \sim f(\hat{m}_h) \cosh[B_h \hat{\mu}_B + Q_h \hat{\mu}_Q + S_h \hat{\mu}_S + C_h \hat{\mu}_C]$

$$\chi_{BX}^{nm} = B^n \times F(\hat{m})$$

$\chi_{BX}^{nm} / \chi_{BX}^{km} = B^{n-k} = 1$, when dof are hadronic with $B=1$
 < 1 , when dof are quarks with $B=1/3$

independent of hadron mass spectrum, relies only on changing quantum number



uncorrelated hadron gas description is valid right till the QCD crossover region

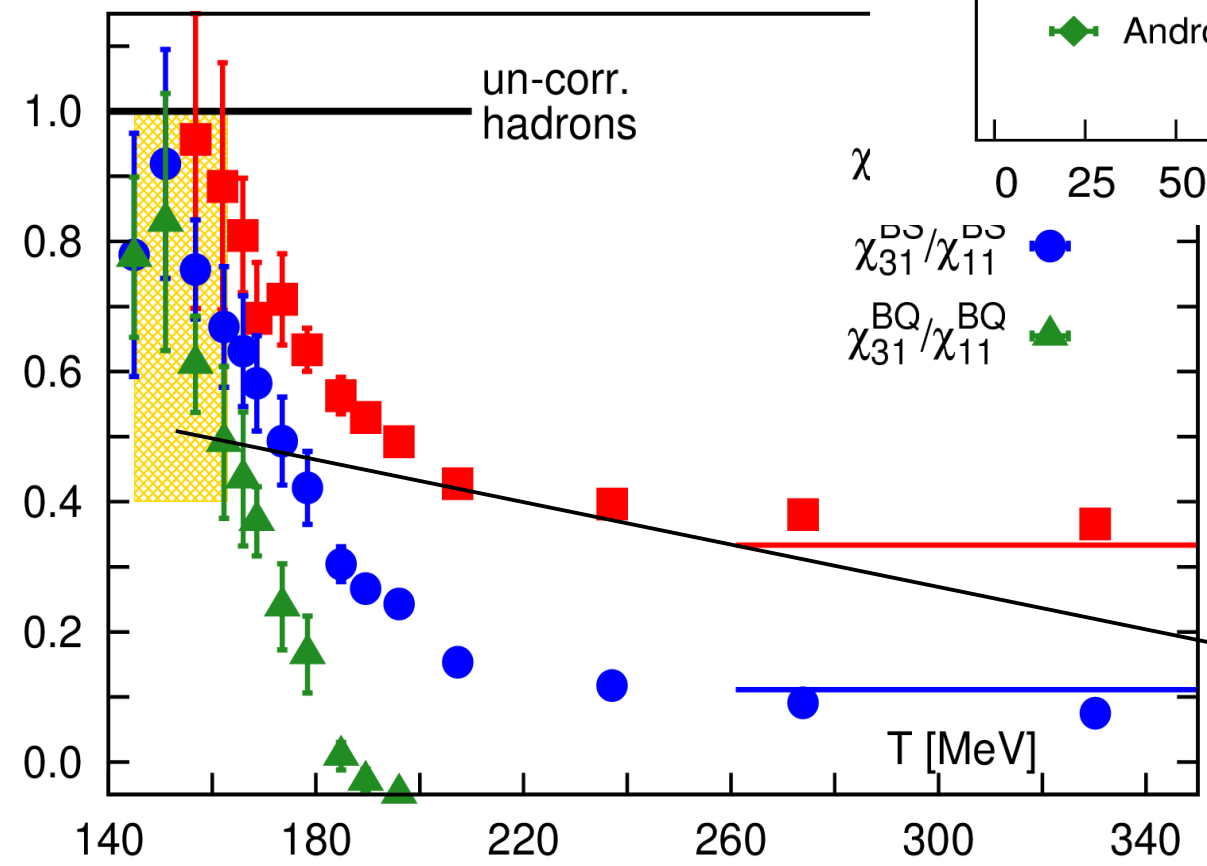
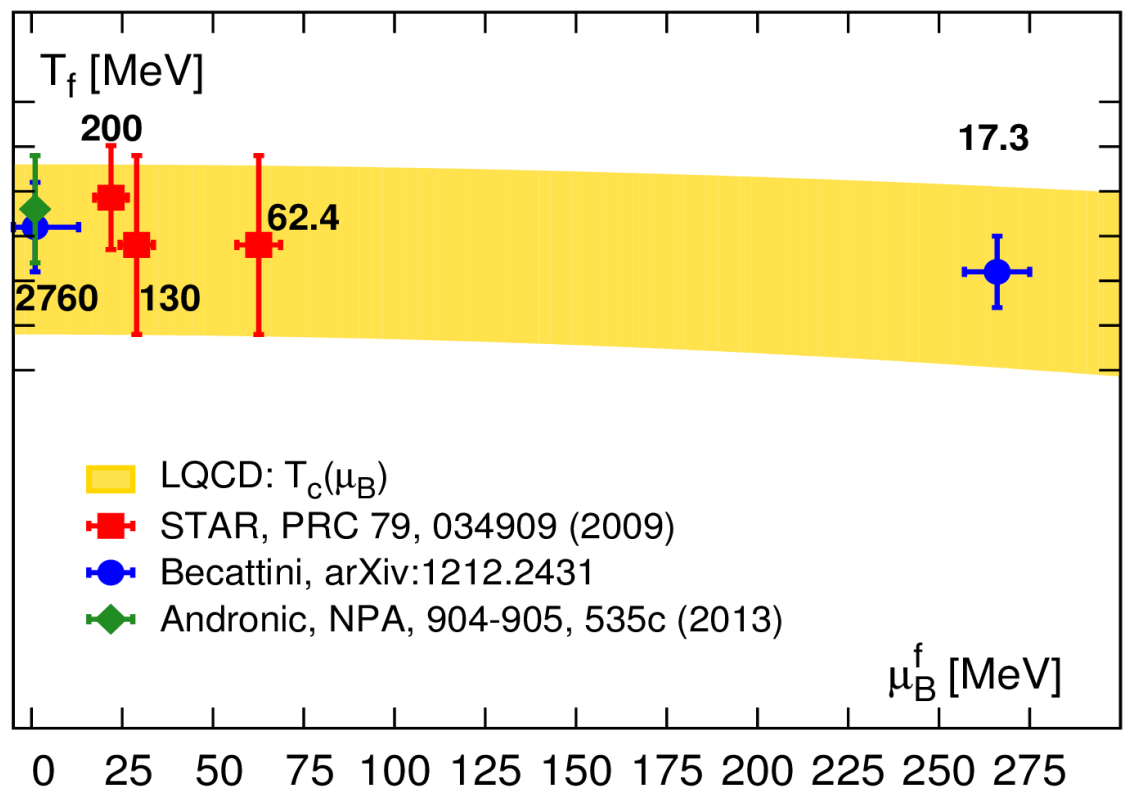
LQCD: validity of hadronic description

baryon – charge/strangeness

$$\text{HRG: } \hat{P}_h \sim f(\hat{m}_h) \cosh[B_h \hat{\mu}_B + C]$$

$$\chi_{\text{BX}}^{\text{nm}} / \chi_{\text{BX}}^{\text{km}} = B^{n-k} = 1, \text{ when } dc > 1$$

$$< 1, \text{ when } dc < 1$$



uncorrelated hadron gas description is valid right till the QCD crossover region

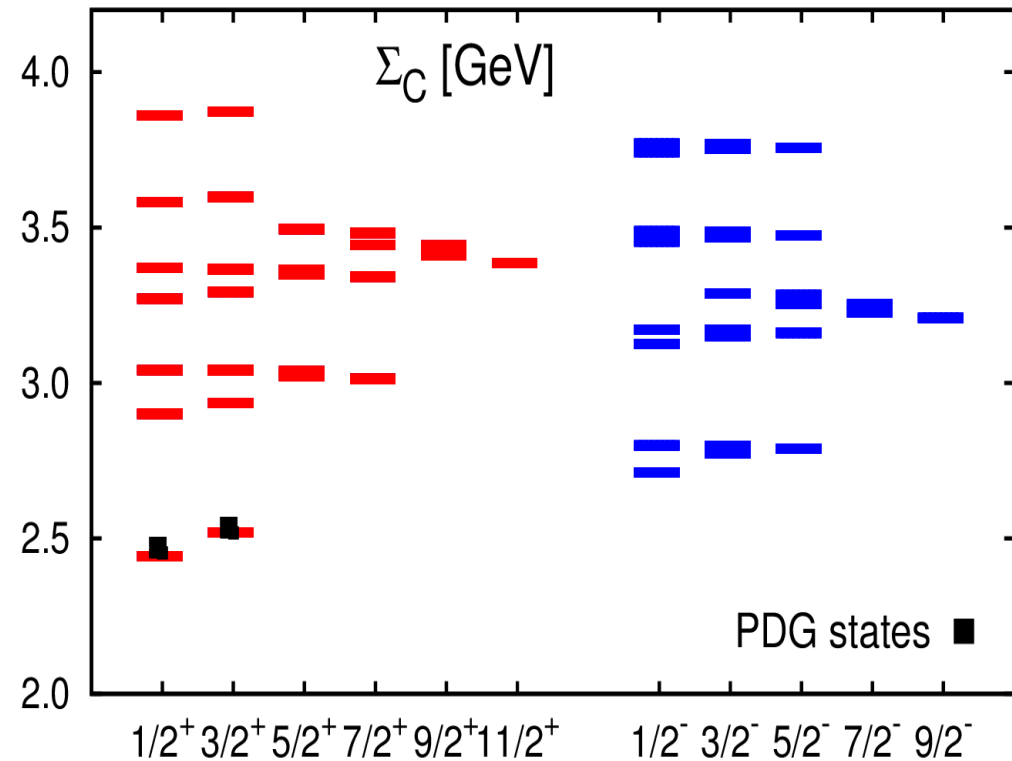
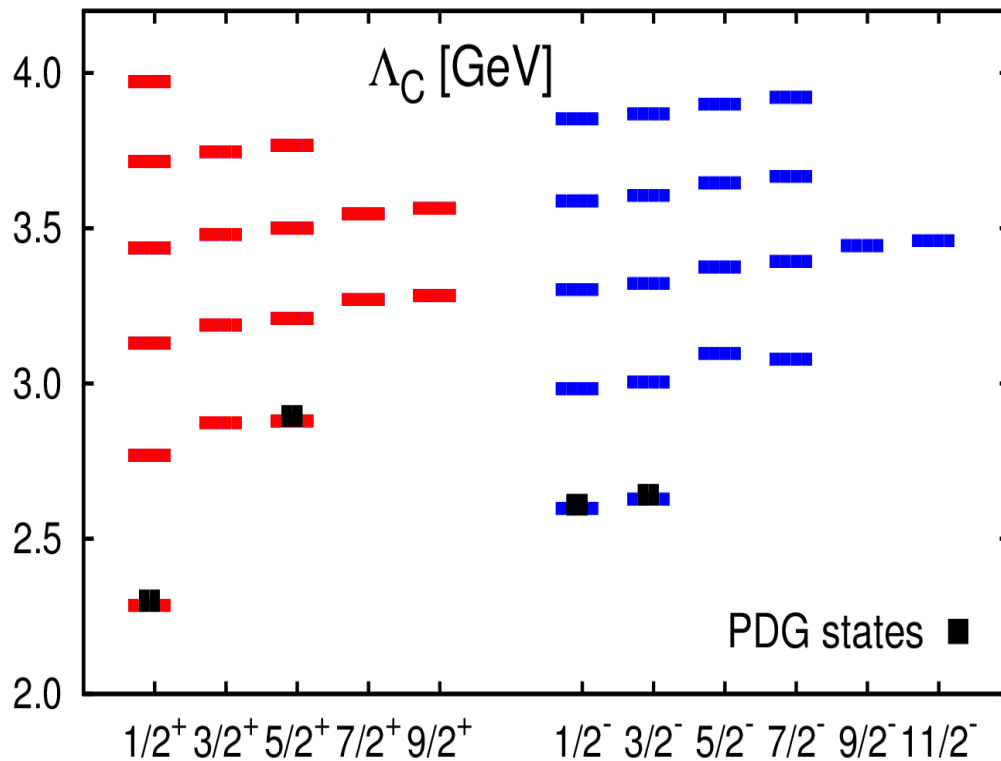
chiral crossover:
 $T_c = 154 \pm 9 \text{ MeV}$

Probing hadron spectrum using thermodynamics

hadronic pressure: $P^C = \sum_{h \in \text{all hadrons}} P_h$ ← expt. observed hadrons + unobserved ones


Quark Model

charm baryons



Ebert et. al.: Eur. Phys. J. C66, 197 (2010);
Phys. Rev. D84, 014025 (2011)

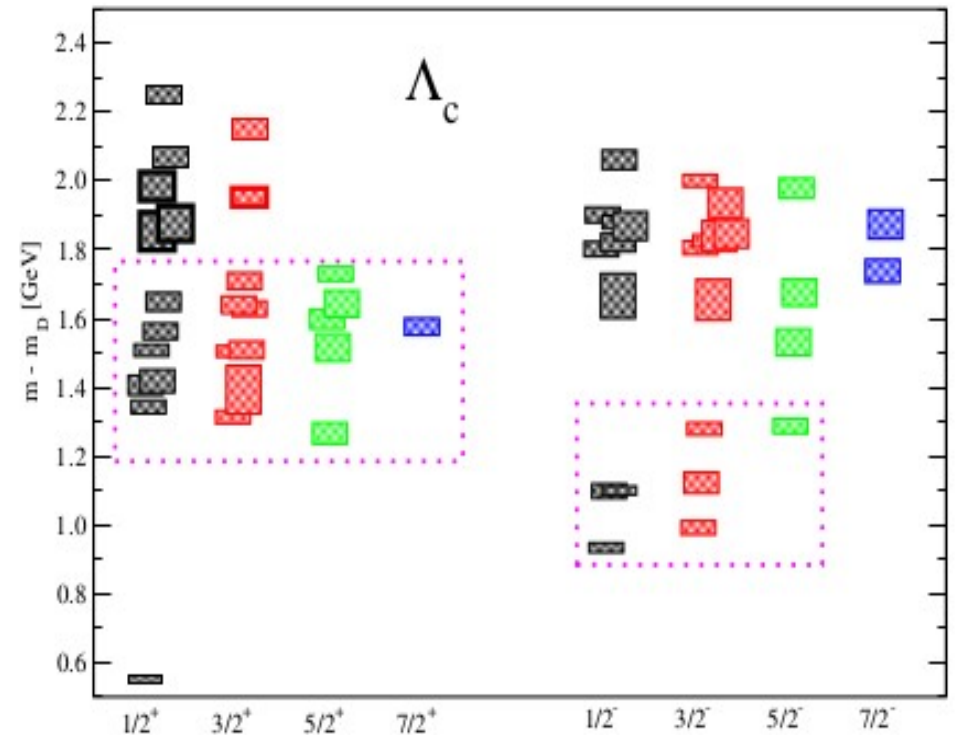
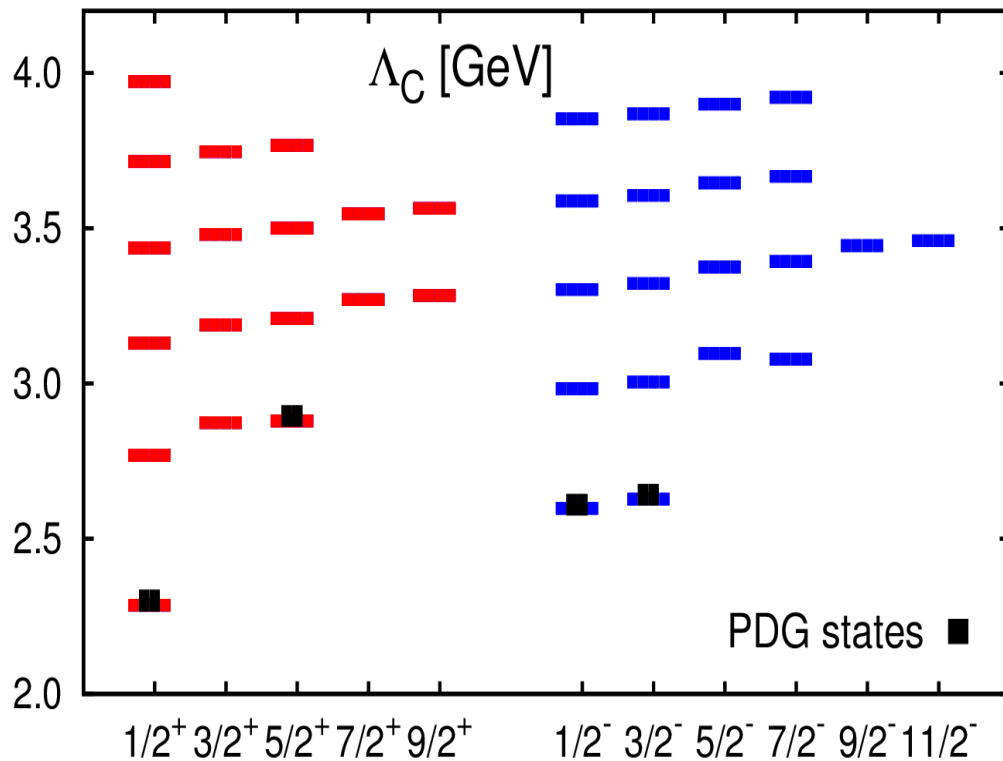
Probing hadron spectrum using thermodynamics

hadronic pressure: $P^C = \sum_{h \in \text{all hadrons}} P_h$  expt. observed hadrons + unobserved ones

Quark Model

charm baryons


LQCD



Padmanath et.al.:
arXiv:1311.4806 [hep-lat]

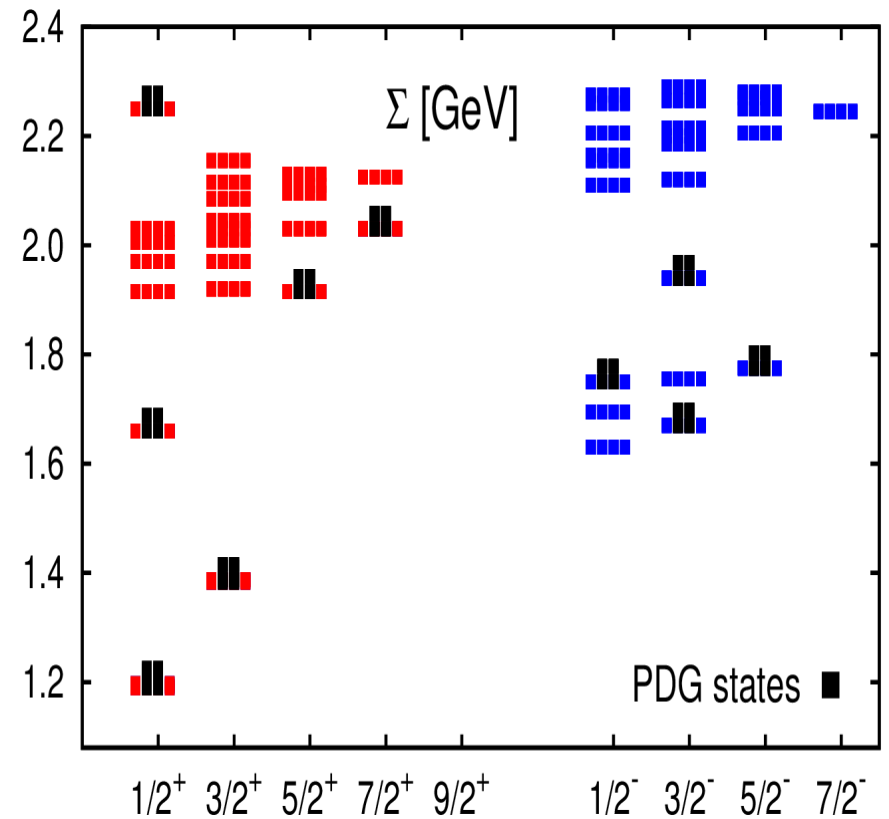
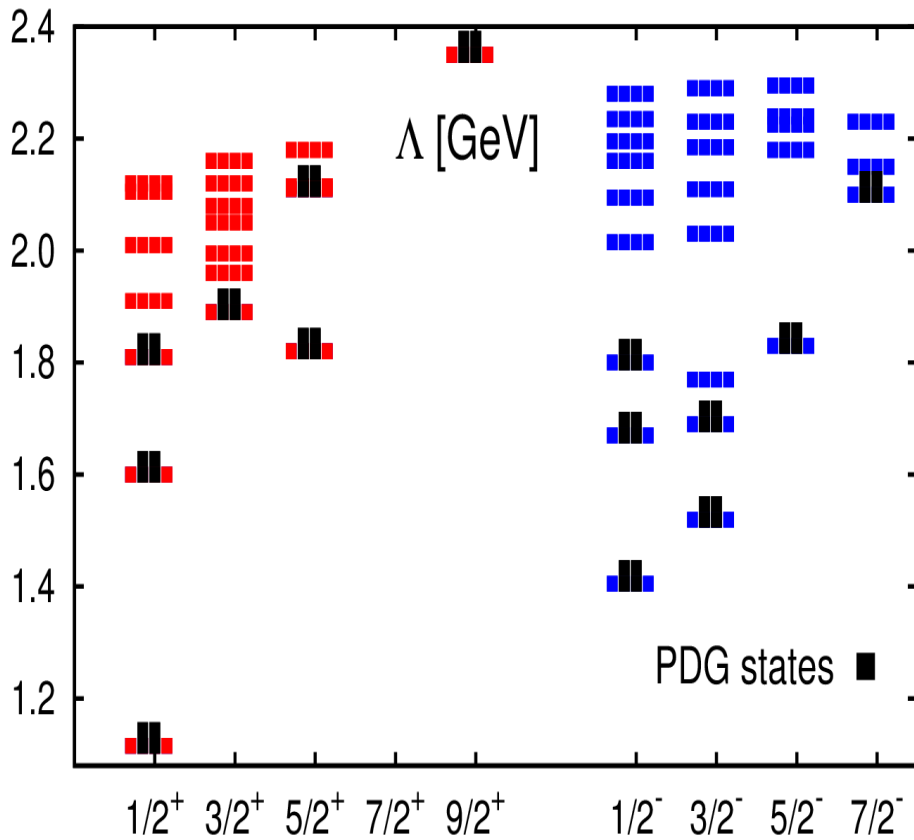
Ebert et. al.: Eur. Phys. J. C66, 197 (2010);
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Probing hadron spectrum using thermodynamics


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Quark Model

strange baryons



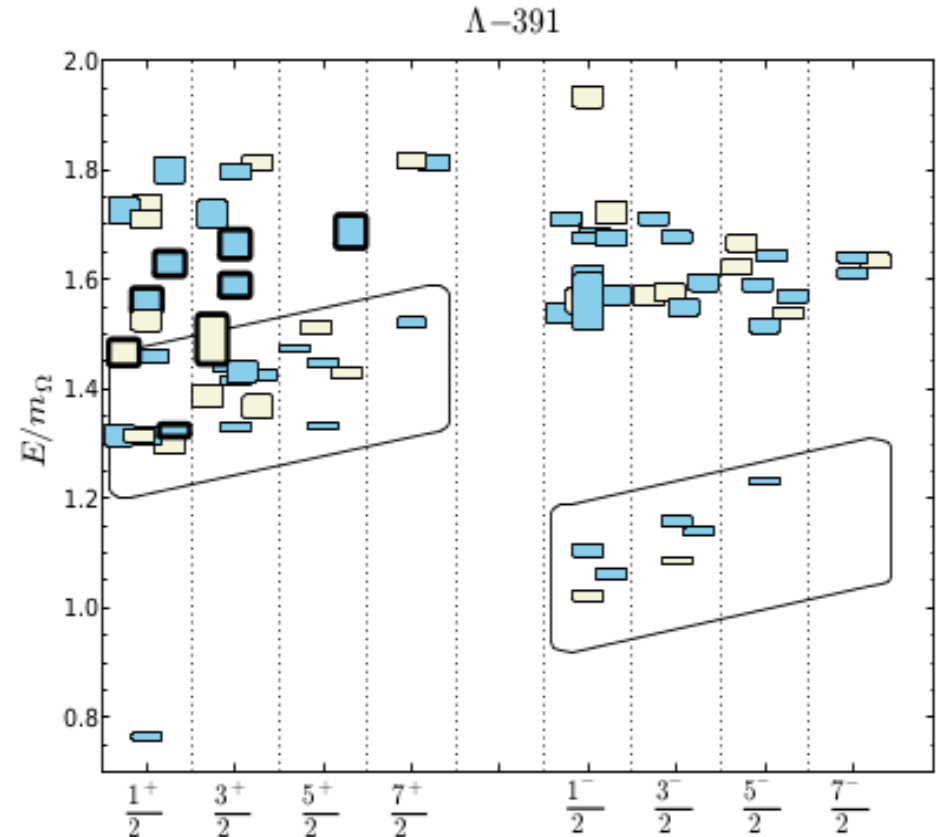
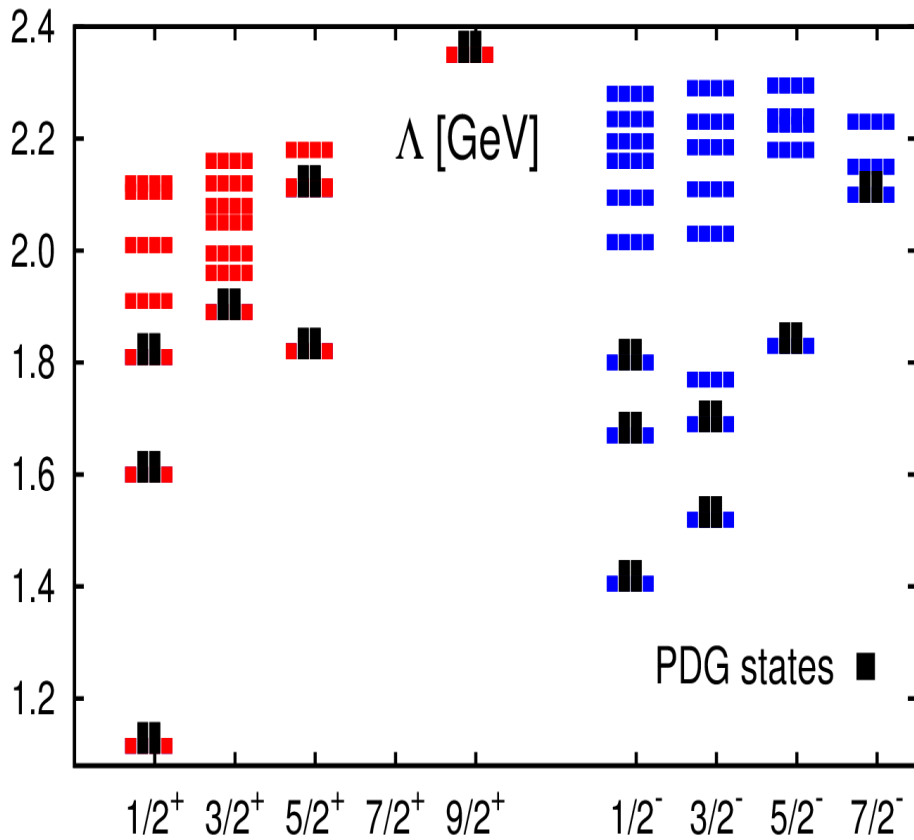
Probing hadron spectrum using thermodynamics

hadronic pressure: $P^S = \sum_{h \in \text{all hadrons}} P_h$  expt. observed hadrons + unobserved ones

Quark Model

strange baryons

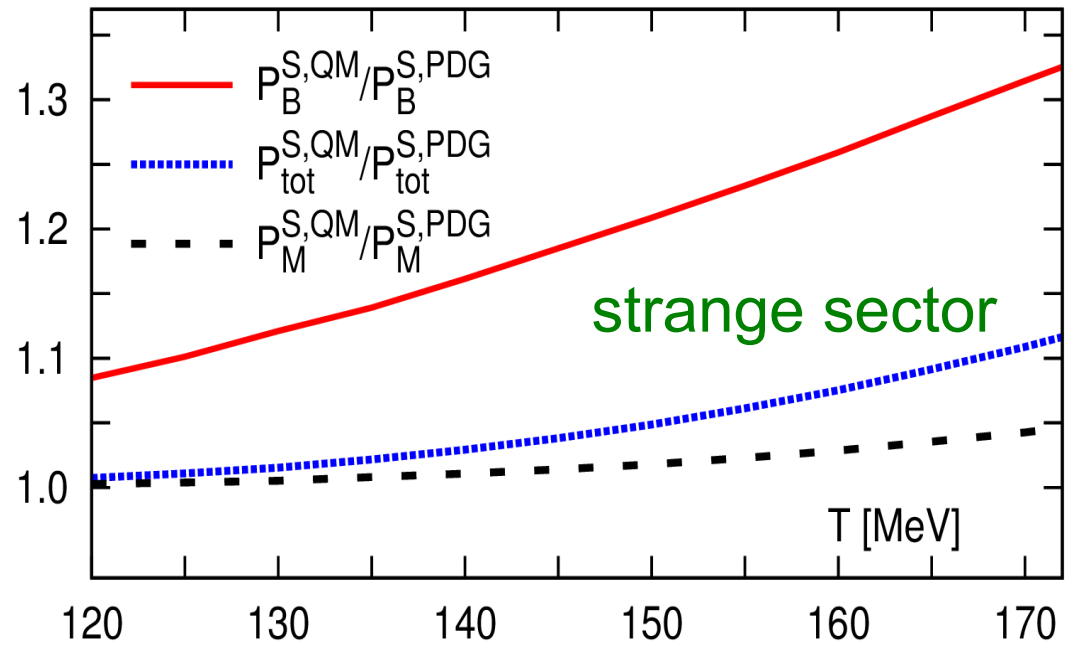
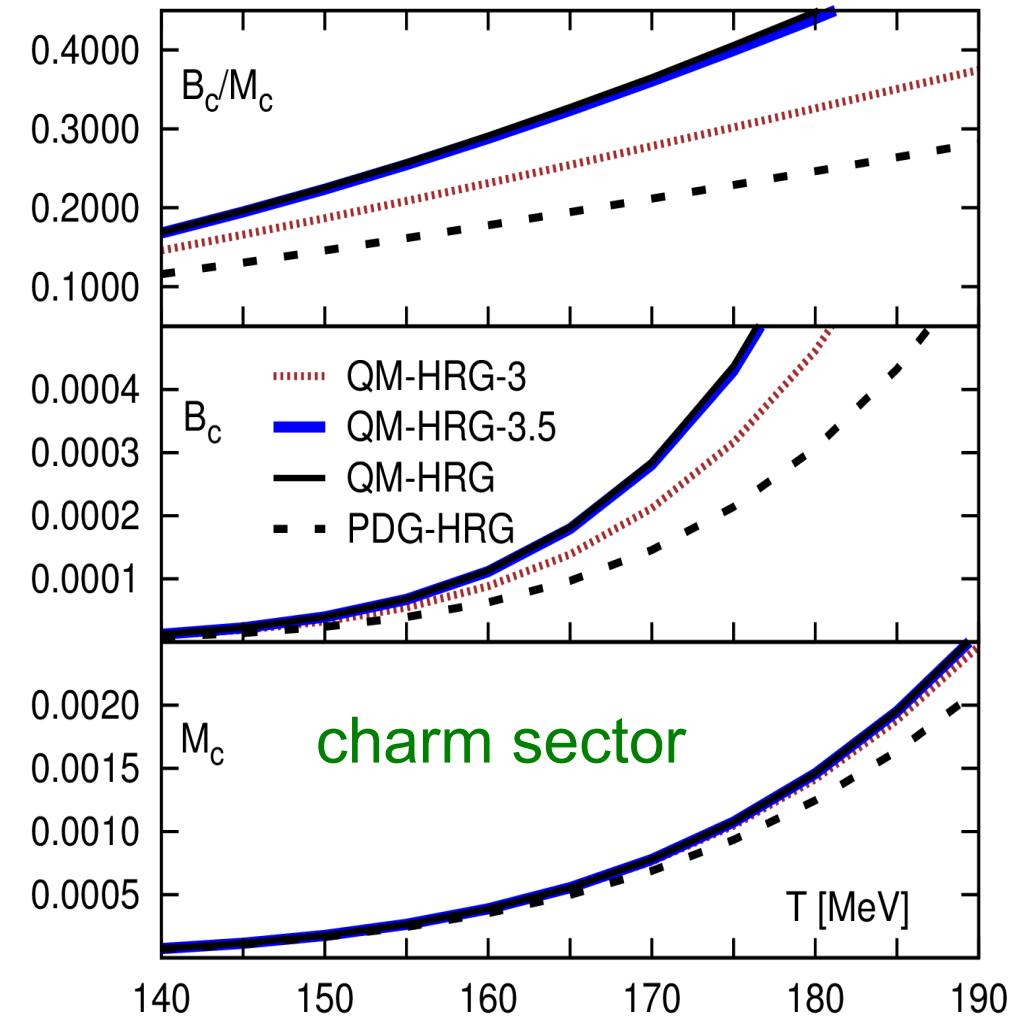
LQCD



JLab: Phys. Rev. D87, 054506 (2013)

Capstick-Isgur: Phys. Rev. D34, 2809 (1986)

Probing hadron spectrum using thermodynamics



significant contributions of these unseen states to the ratios of partial pressures of baryon to meson near the QCD crossover

partial pressure of baryon $\rightarrow B$; meson $\rightarrow M$

similar results with LQCD spectra

LQCD: operators to identify separate thermodynamic contributions of strange/charm baryons/mesons

Operators for partial pressures of baryons & mesons

suitable combinations of up to 4th order
baryon – charm/strangeness correlations

$$\chi_{BX}^{nm} = \left. \frac{\partial^{n+m} \hat{P}}{\partial^n \hat{\mu}_B \partial^m \hat{\mu}_X} \right|_{\vec{\mu}=0}$$

BNL-Bi: Phys. Lett. B737 (2014) 210; Phys. Rev. Lett. 111, 082301 (2013)

a simplified example:

hadron gas $\rightarrow \hat{P}^C \sim P_M^C \cosh[\hat{\mu}_C] + P_B^C \cosh[\hat{\mu}_B + \hat{\mu}_C]$

partial pressure
of $|C|=1$ mesons

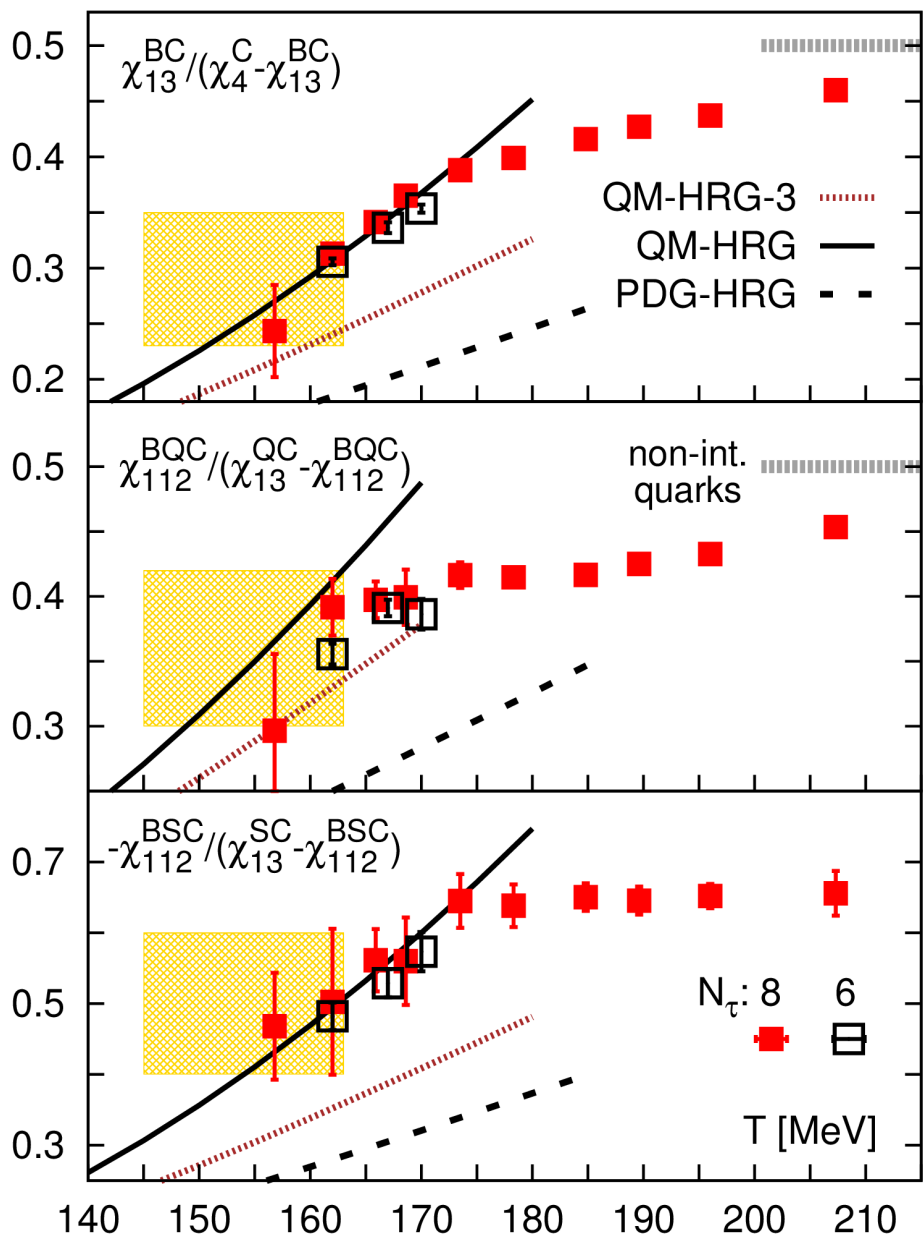
partial pressure
of $|C|=1$ baryons

neglect contributions of
heavier $|C|=2,3$ baryons,
x1000 suppressed

$$\chi_k^C \simeq P_M^C + P_B^C$$

$$\chi_{mn}^{BC} \simeq P_B^C$$

Signatures of additional charm baryons

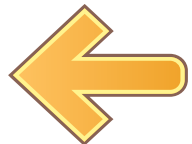


relative contributions:



charm baryons to charmed mesons

$$\chi_{13}^{BC} / (\chi_4^C - \chi_{13}^{BC}) = P_B^C / P_M^C$$



charged charm baryons to charged charmed mesons



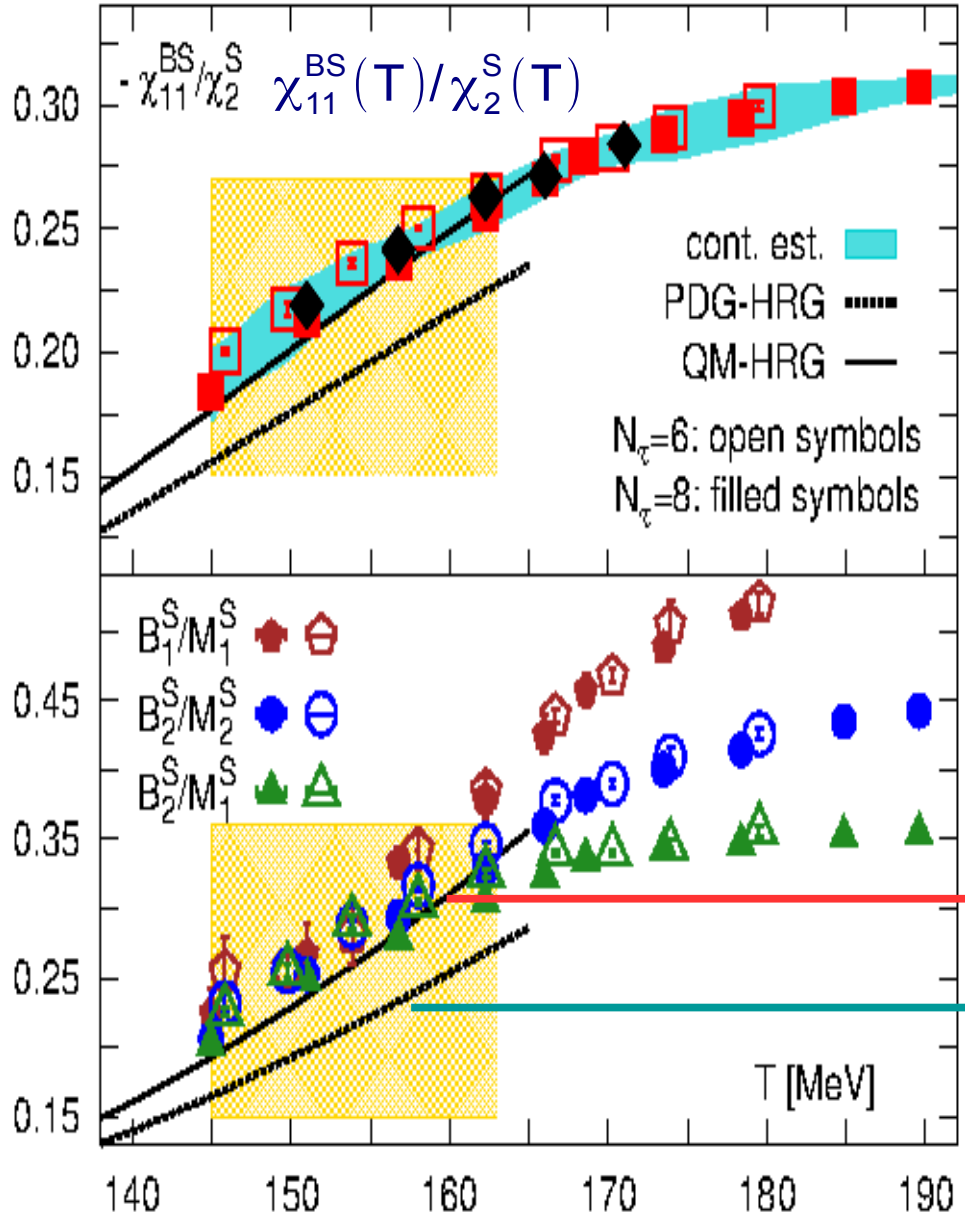
strange charm baryons to strange charmed mesons

signatures of additional, yet unobserved charm baryons from QCD thermodynamics

Thermodynamic contributions of additional strange baryons

relative contributions of strange baryons to strange mesons

BNL-Bi: Phys. Rev. Lett. 113 (2014) 072001



partial pressure of strange mesons:

$$M_1^S = \chi_2^S - \chi_{22}^{BS}$$

$$M_2^S = \frac{1}{12} (\chi_4^S + 11 \chi_2^S) + \frac{1}{2} (\chi_{22}^{BS} + \chi_{13}^{BS})$$

partial pressure of strange baryons:

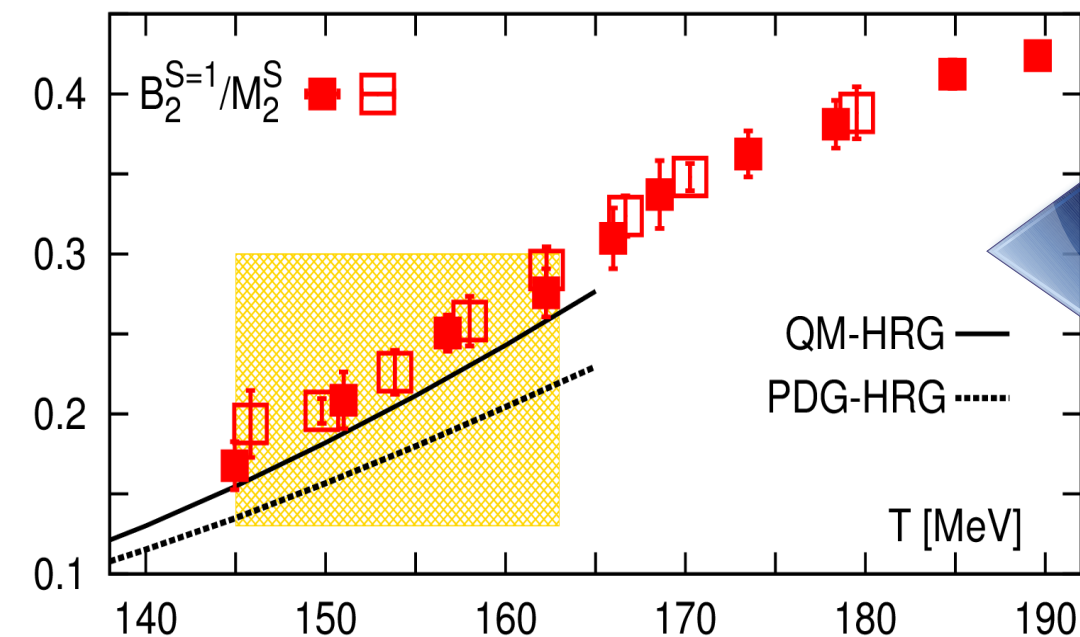
$$B_1^S = -\frac{1}{6} (11 \chi_{11}^{BS} + 6 \chi_{22}^{BS} + \chi_{13}^{BS})$$

$$B_2^S = \frac{1}{12} (\chi_4^S - \chi_2^S) + \frac{1}{3} (4 \chi_{11}^{BS} - \chi_{13}^{BS})$$

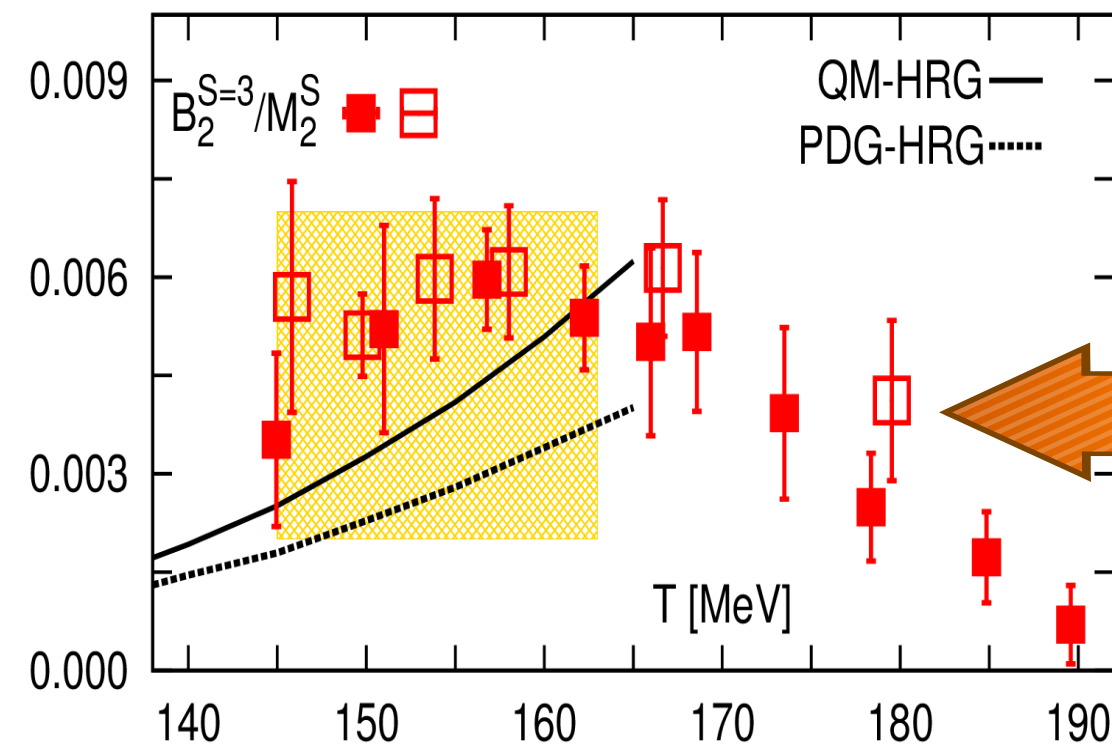
+ undiscovered strange baryons

contributions of all expt. observed strange hadrons

Thermodynamic contributions of additional strange baryons

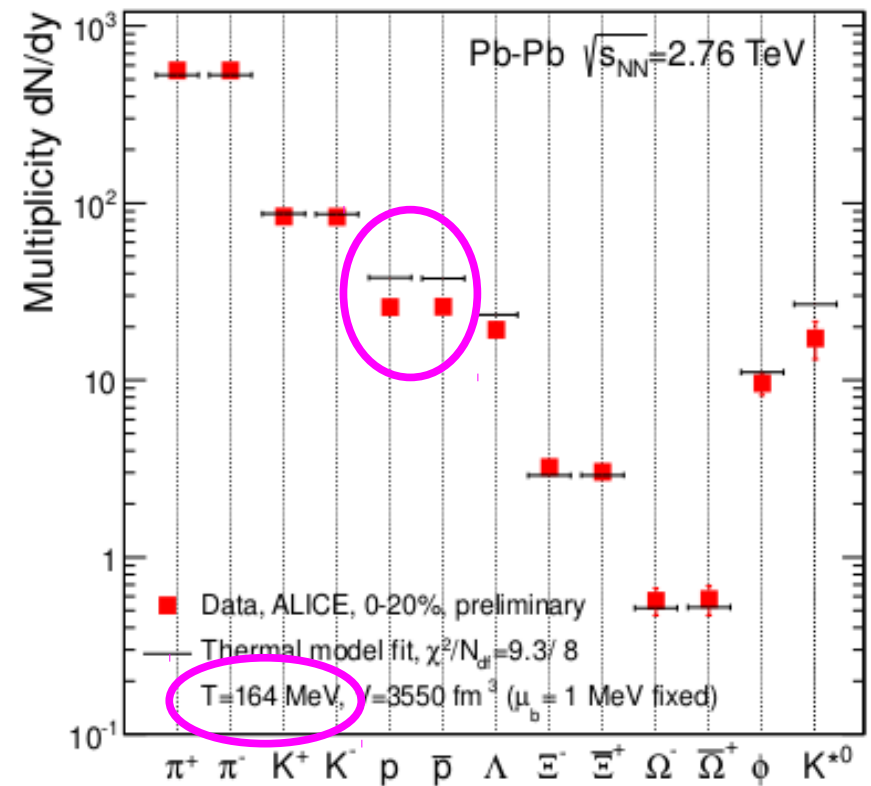
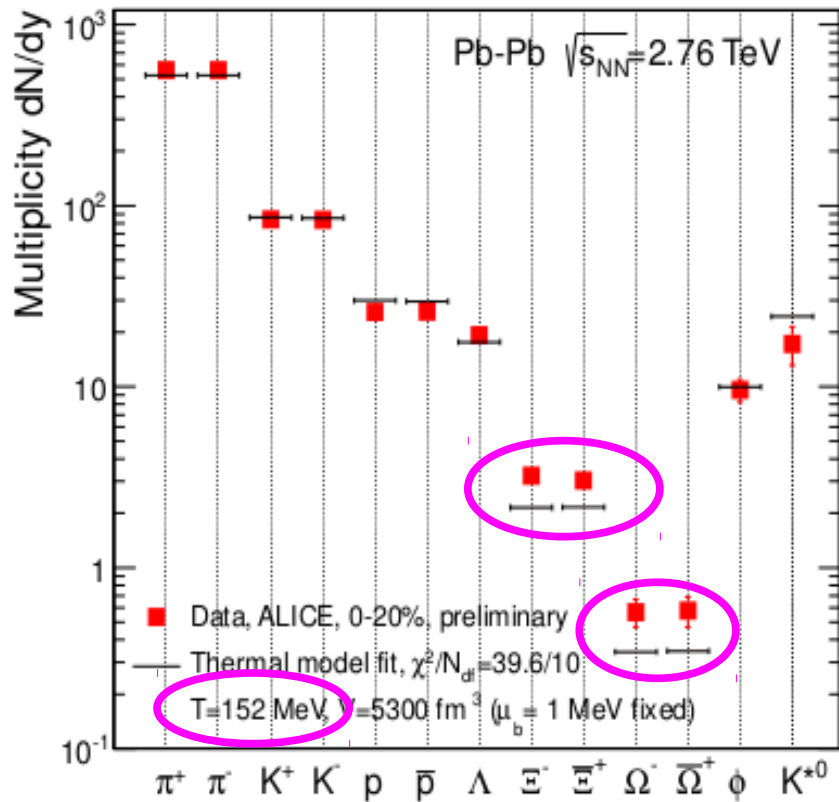


relative contributions of S=1 baryons to strange mesons



relative contributions of S=3 baryons to strange mesons

Hierarchical freeze-out of light & strange hadrons ?



Andronic et.al.: Nucl. Phys. A904, 535c (2013)

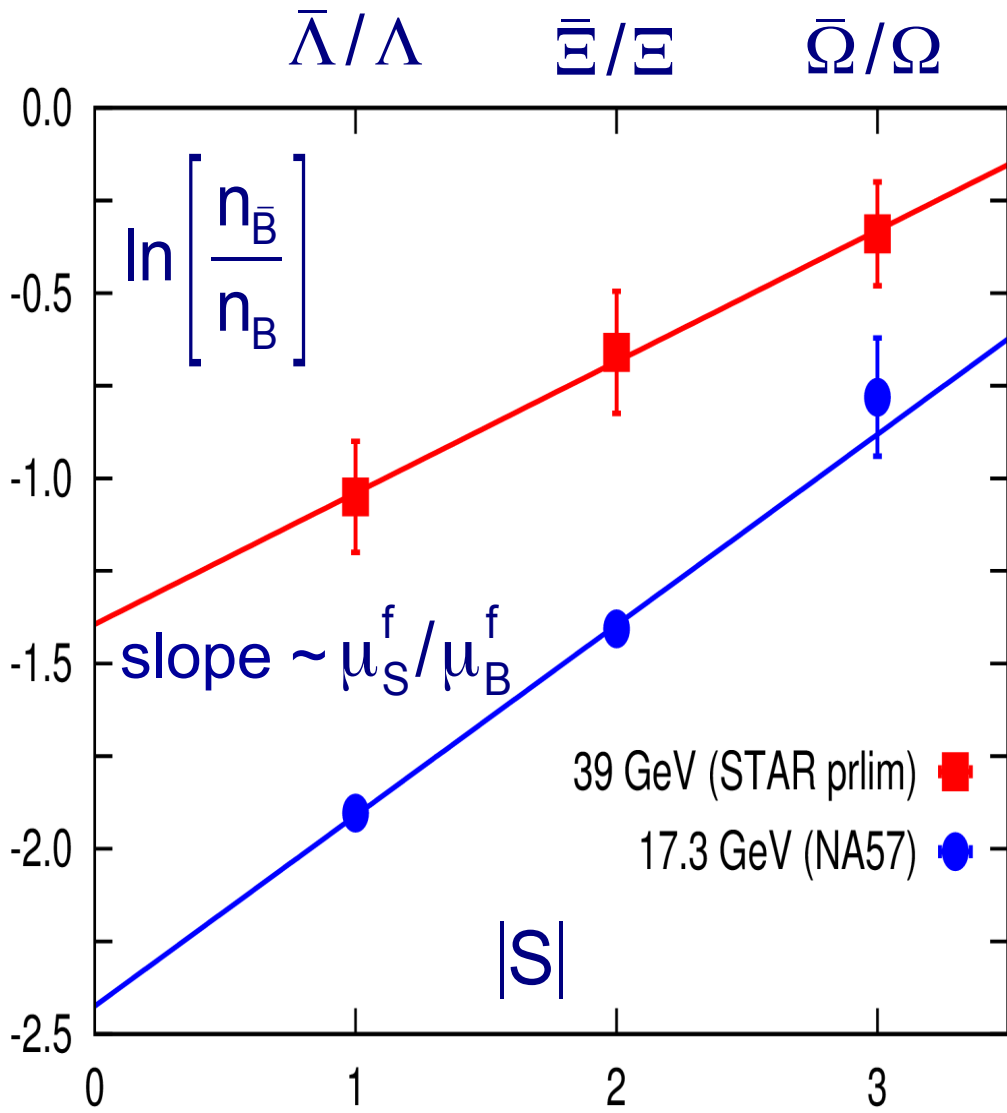
~10-5 MeV systematic difference in freeze-out T from separate fits to light and strange hadrons

two separate freeze-out stages for light and strange hadrons ?

Phys. Rev. Lett. 111, 202302 (2013); Phys. Lett. B727, 554 (2013);
 Europhys. Lett. 104, 22002 (2013) ...

Strange baryon yields in heavy-ion collisions

$$\frac{n_{\bar{\Lambda}}}{n_{\Lambda}}, \frac{n_{\bar{\Xi}}}{n_{\Xi}}, \frac{n_{\bar{\Omega}}}{n_{\Omega}} = \exp \left[- \frac{2\mu_B^f}{T^f} \left(1 - \frac{\mu_S^f}{\mu_B^f} |S| \right) \right]$$

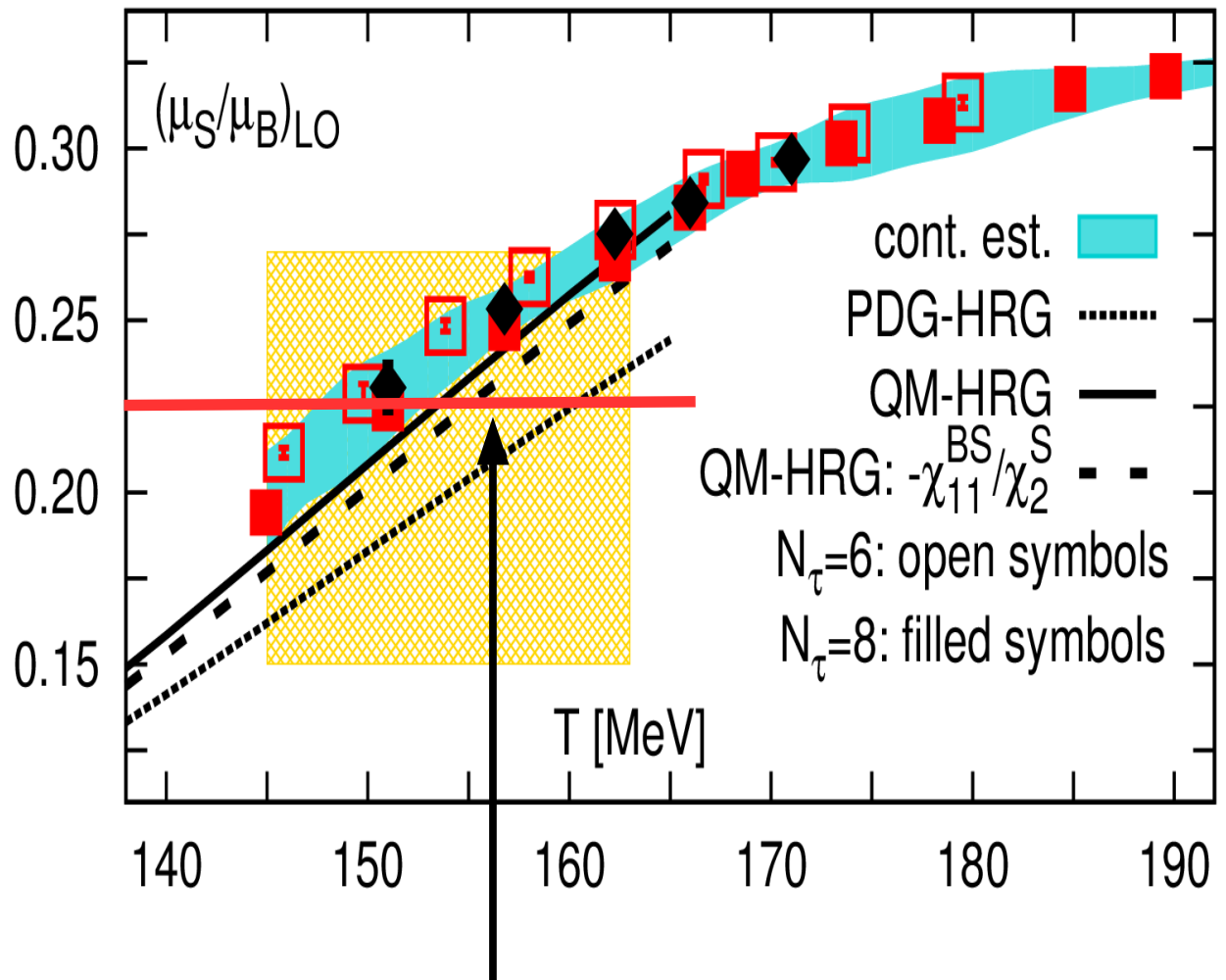


does not assume spectrum of hadron gas, only assumes hadron yields are thermal

Strangeness neutrality & strangeness chemical potential

medium formed in HIC is strangeness neutral:

$$\langle n_s \rangle = 0$$



$$\frac{\mu_S}{\mu_B}(T, \mu_B/T) \simeq \frac{\chi_{11}^{BS}(T)}{\chi_2^S(T)} + \dots$$

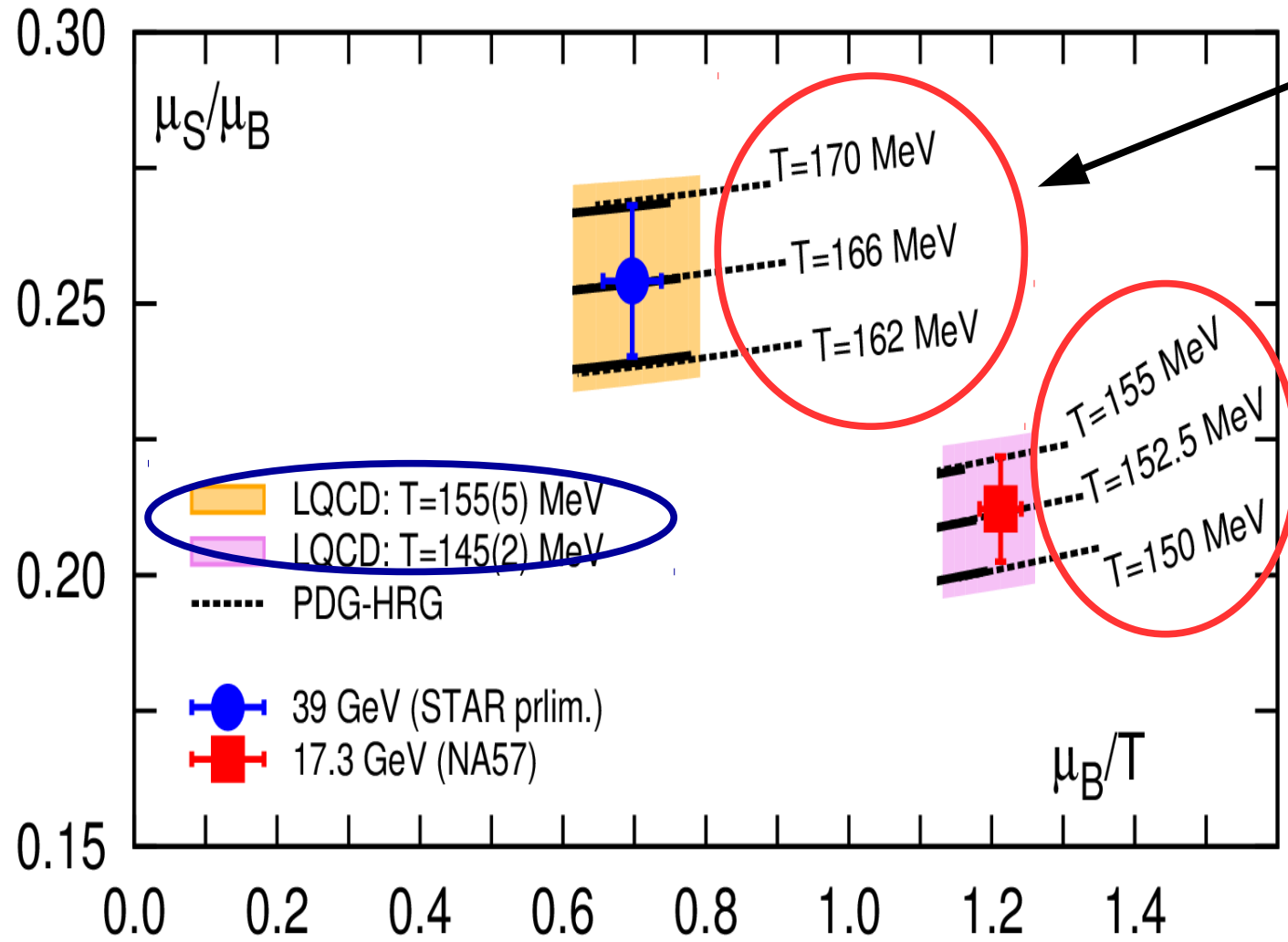
relative contribution of strange baryons to mesons

LQCD results are reproduced by including additional Quark Model states

a given value of μ_S/μ_B is realized at a lower temperature

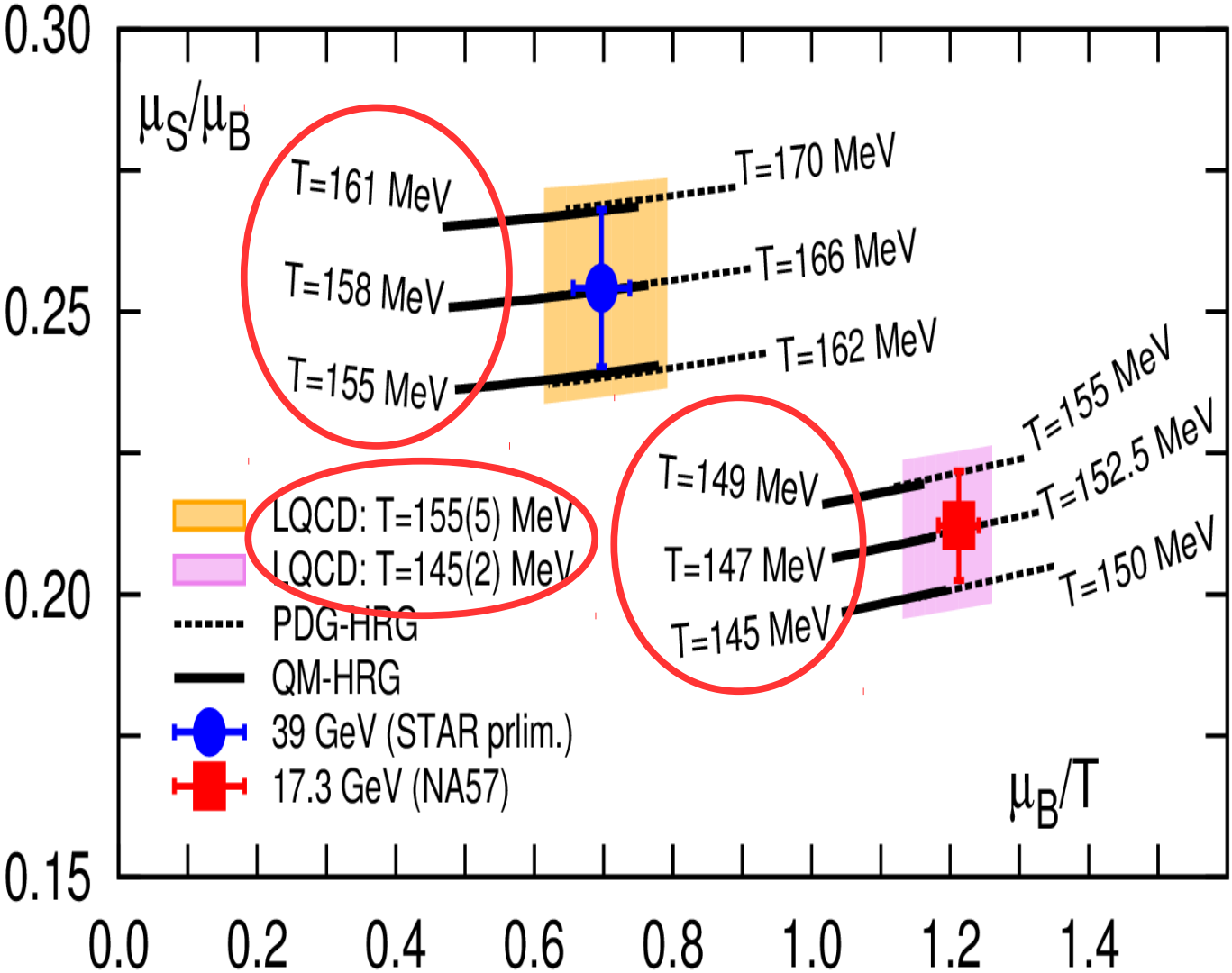
Strangeness, LQCD and freeze-out in HIC

freeze-out T by comparing μ_S/μ_B from LQCD and expt.



not reproduced by strangeness neutral hadrons gas with only PDG states

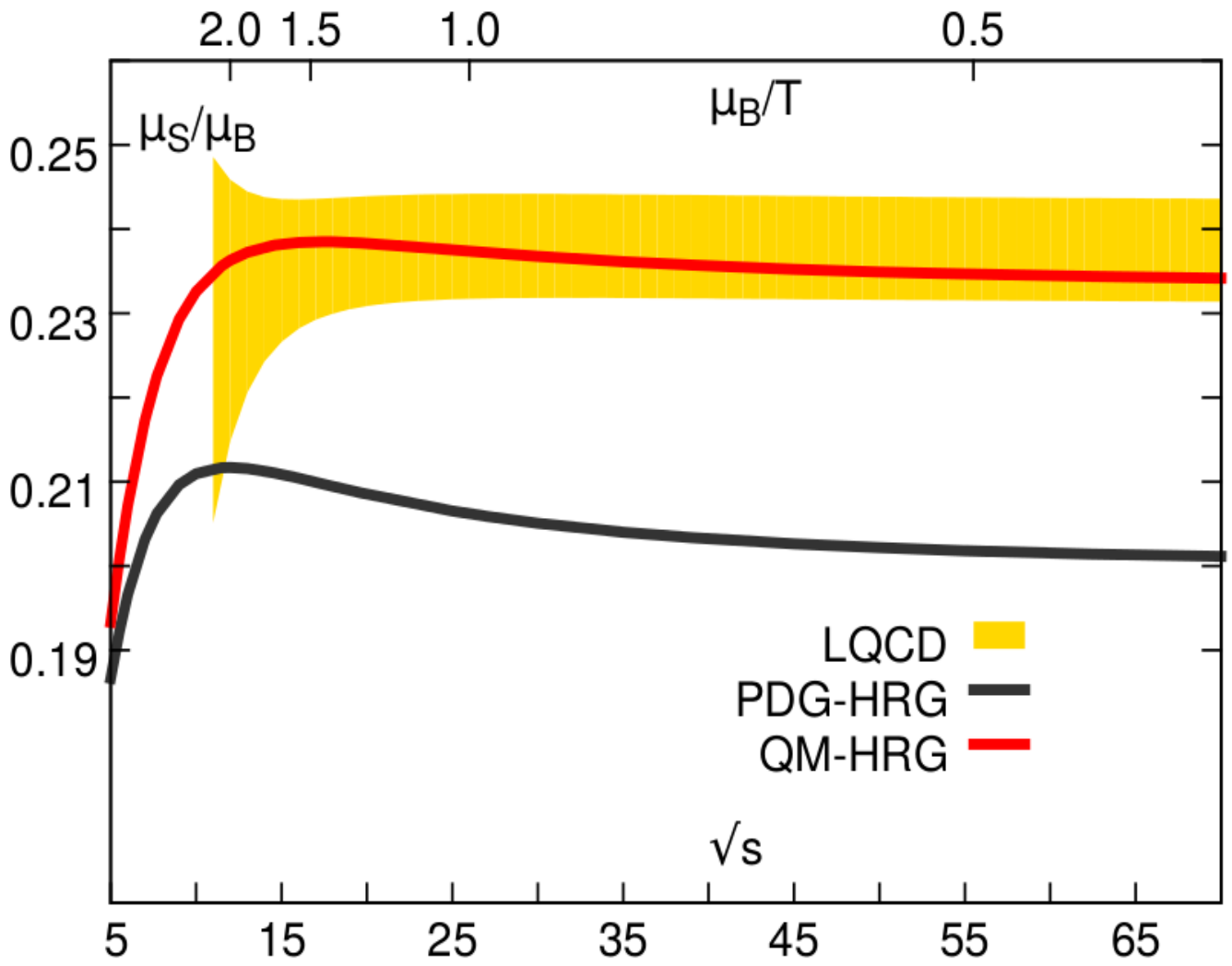
Additional strange hadrons & freeze-out in HIC



inclusion of additional strange hadrons reduces freeze-out T & agrees with LQCD+expt. determination

indirect evidence for so-far undiscovered strange baryons at RHIC ?

Additional strange hadrons & RHIC BES



signature for unobserved strange baryons persists for RHIC BES-II

can also be extracted from expt. measured

$$\frac{\ln[N_{K^-} / N_{K^+}]}{\ln[N_{\bar{p}} / N_p]} = \frac{\mu_S^f}{\mu_B^f}$$

need accurate expt. measurements & feed-down corrections

Summary

hot-dense LQCD:

additional, yet unobserved strange & charm baryons become thermodynamically relevant near the QCD crossover

these additional strange baryons are important for determining the `observed' freeze-out temperatures of heavy-ion collision experiments

freeze-out temperatures for strange hadrons obtained comparing LQCD and HIC expt. favors presence of these additional hadrons