

Quarkonium-Nucleus Interactions from Lattice QCD

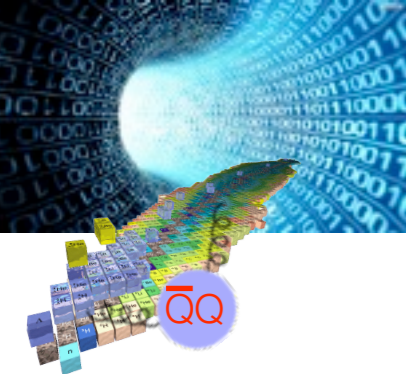
(APS, Baltimore, April 2015)

Martin J Savage



INSTITUTE for
NUCLEAR THEORY

Modeling Interactions with Nuclei

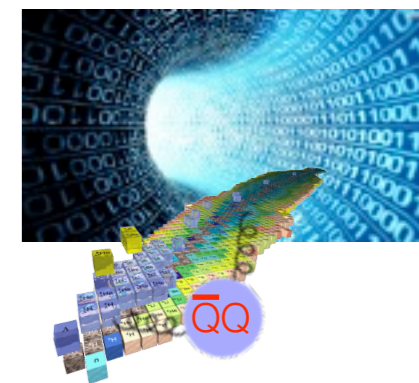
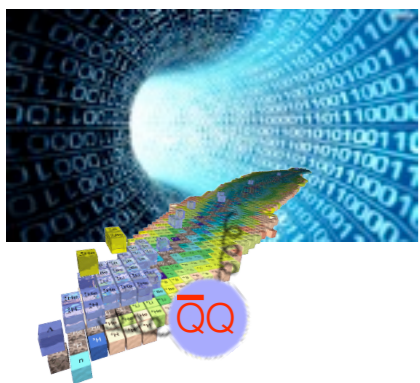


- Brodsky, Schmidt and deTeramond (1989)
 - multi-gluon exchange modeled by Pomerons
 - large binding energies, scaling with A
- Wasson (1991)
 - Saturation due to finite range interaction

Ref.	Binding Energy (MeV)			Binding Energy (MeV)	
	${}^3\text{He } \eta_c$	${}^4\text{He } \eta_c$	NM η_c	${}^4\text{He } J/\psi$	NM J/ψ
[1]	19	140			
[2]	0.8	5	27		
[3]			10		10
[5]	*	*	9		
[6]					5
[7]				5	18
[8]				15.7	

- [1] S. J. Brodsky, I. Schmidt, and G. de Teramond, Phys.Rev.Lett. **64**, 1011 (1990).
- [2] D. Wasson, Phys.Rev.Lett. **67**, 2237 (1991).
- [3] M. E. Luke, A. V. Manohar, and M. J. Savage, Phys.Lett. **B288**, 355 (1992), hep-ph/9204219.
- [4] S. J. Brodsky and G. A. Miller, Phys.Lett. **B412**, 125 (1997), hep-ph/9707382.
- [5] G. F. de Teramond, R. Espinoza, and M. Ortega-Rodriguez, Phys.Rev. **D58**, 034012 (1998), hep-ph/9708202.
- [6] S. H. Lee and C. Ko, Phys.Rev. **C67**, 038202 (2003), nucl-th/0208003.
- [7] K. Tsushima, D. Lu, G. Krein, and A. Thomas, Phys.Rev. **C83**, 065208 (2011), 1103.5516.
- [8] A. Yokota, E. Hiyama, and M. Oka, PTEP **2013**, 113D01 (2013), 1308.6102.

Quarkonium Structure and Scales

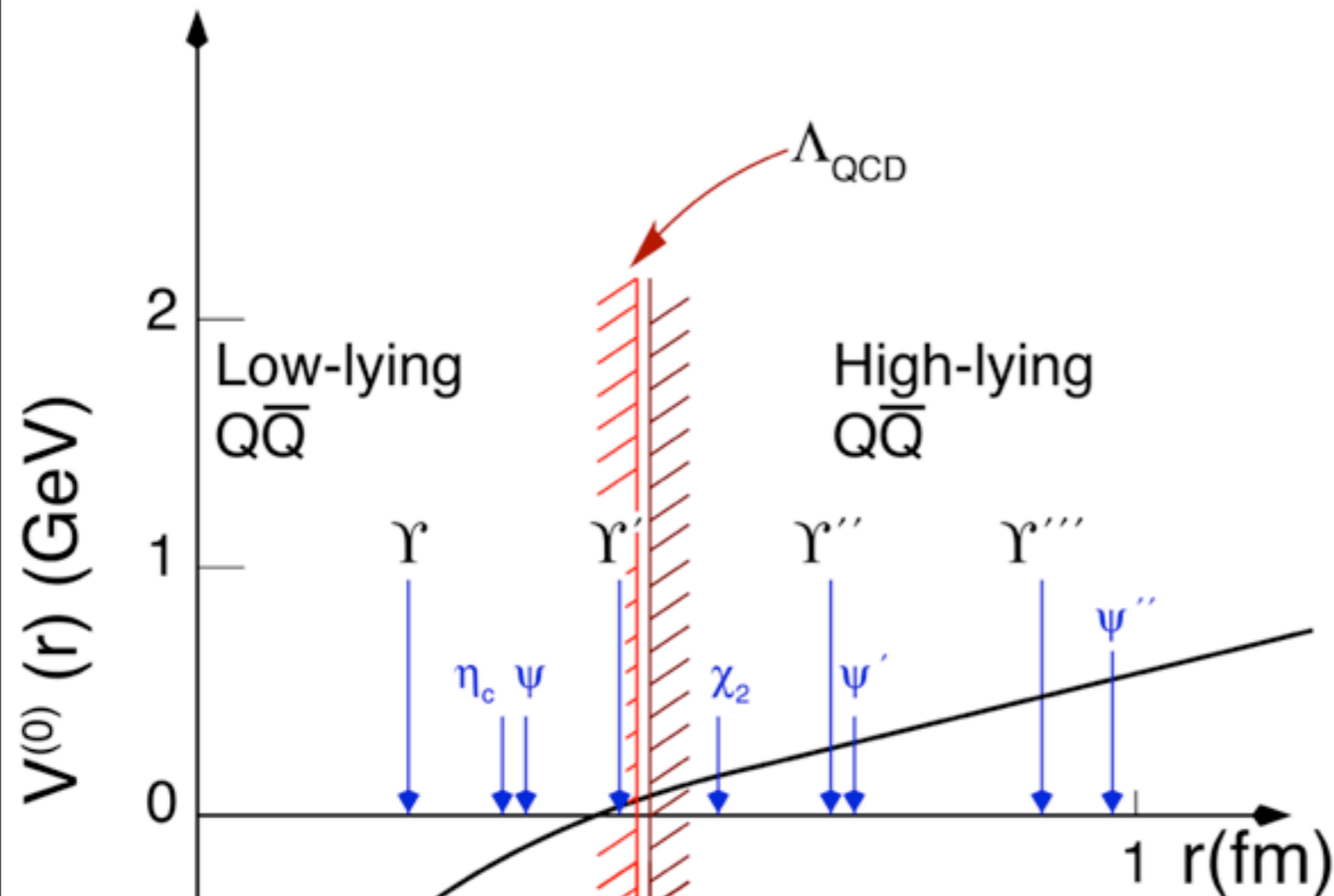


Small $r \rightarrow$ Coulomb

$$V \sim \alpha_s(r)/r$$

$$r \sim 1/(\alpha_s(r) M_Q)$$

$$B \sim (\alpha_s(r))^2 M_Q$$

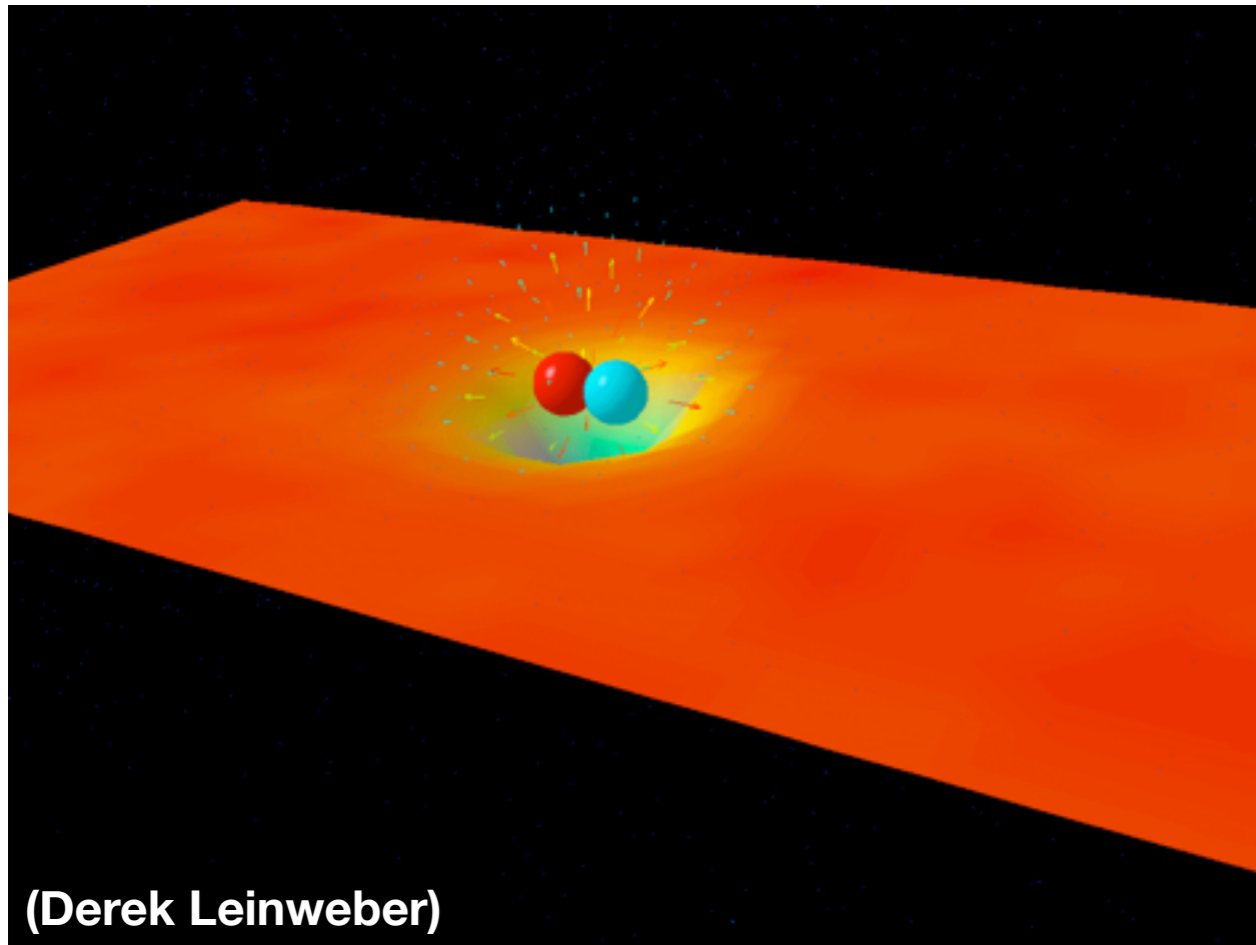


Brambilla *et al*, Eur.Phys.J. C71 (2011) 1534

System Factorizes
at small r

- color van der Waals

Quarkonium Symmetries and Interactions



(Derek Leinweber)

Gluon Energy Density

Heavy Quark Symmetry

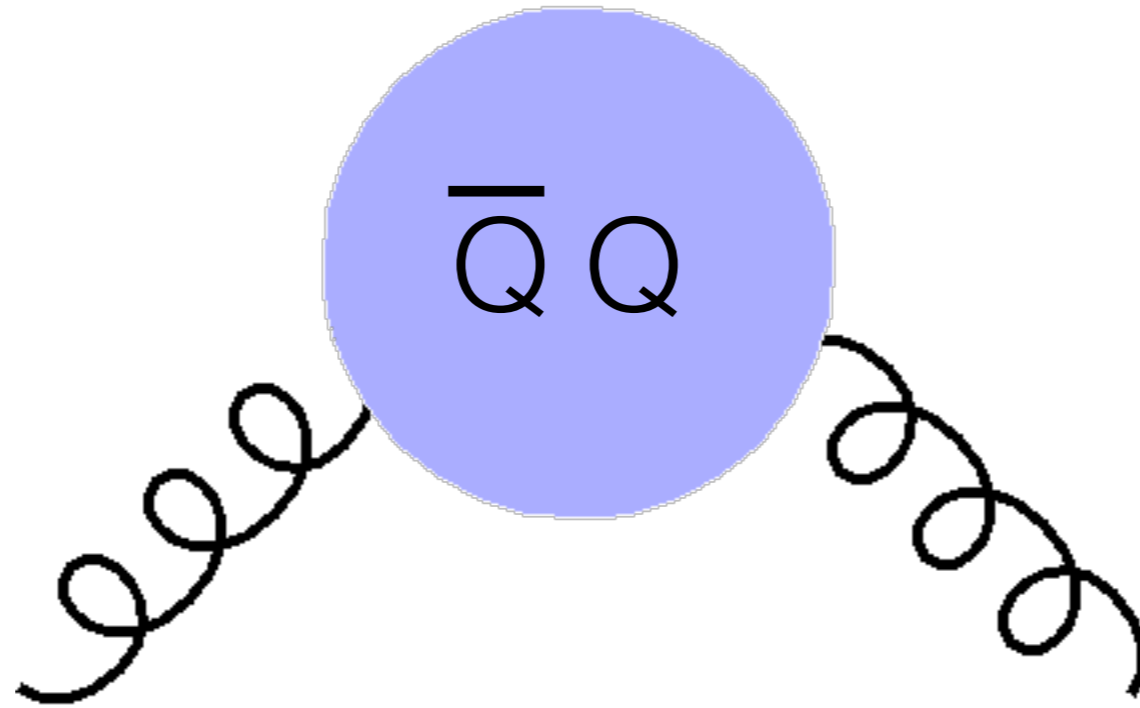
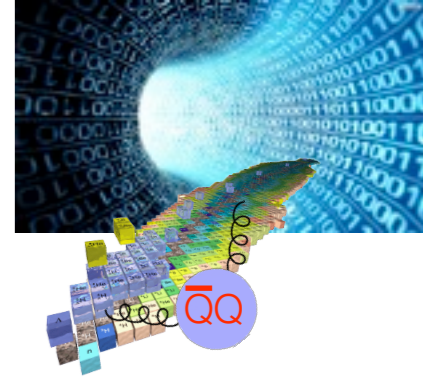
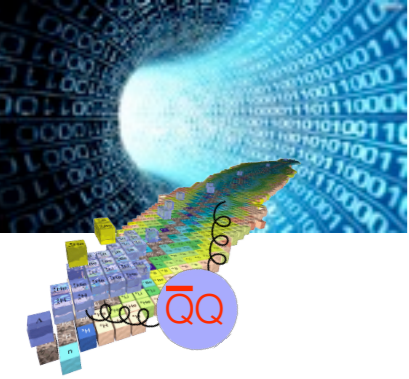
η_c and J/ψ have same
interactions in heavy-quark
limit

Multipole expansion of the
gluon interactions

Coefficients in Lagrangian
Density $\sim r^3, \dots$

Quarkonium

Symmetries and Interactions



Only spin-0 and spin-2 , no spin-1 (requires 3 gluons)

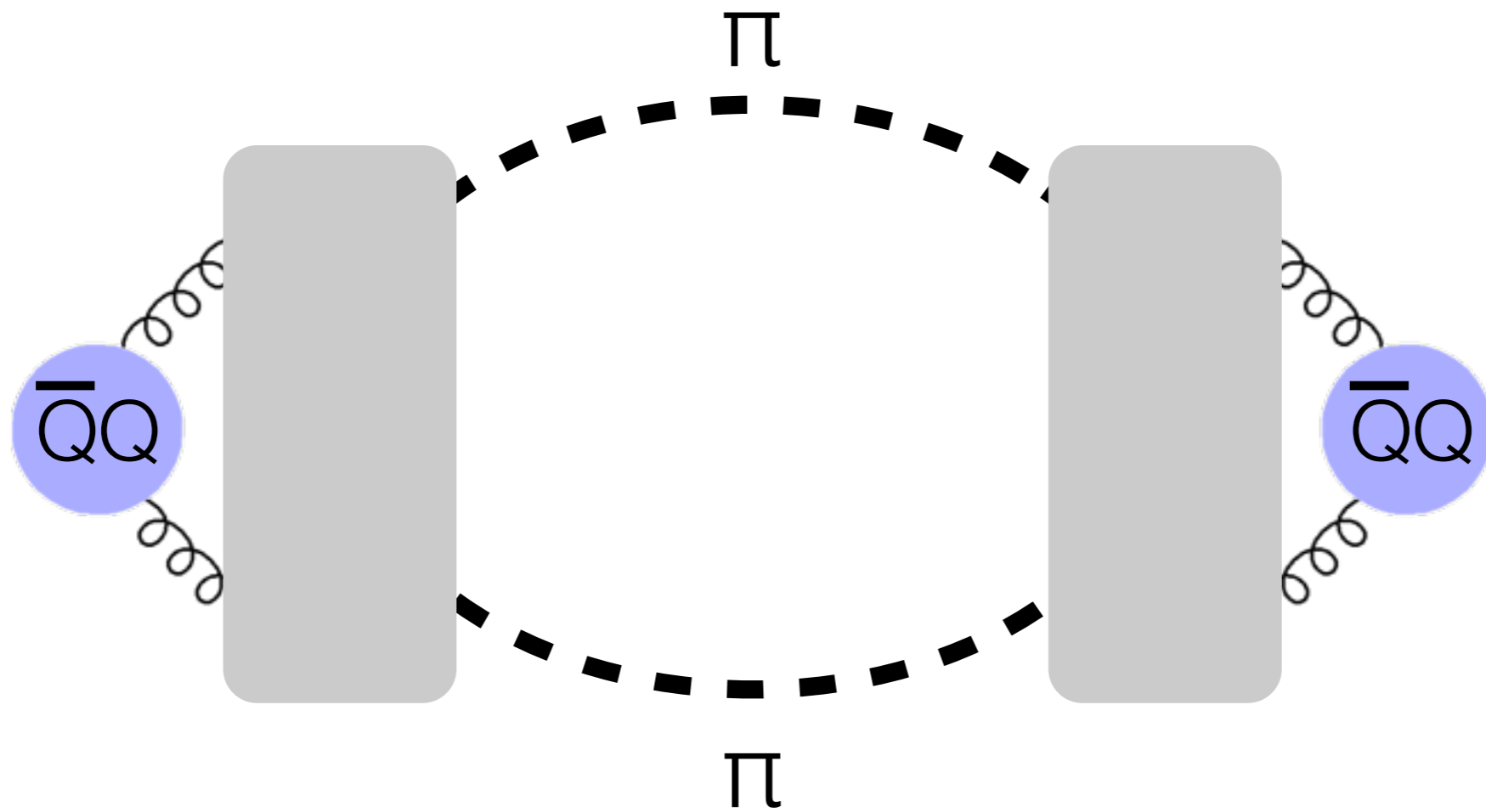
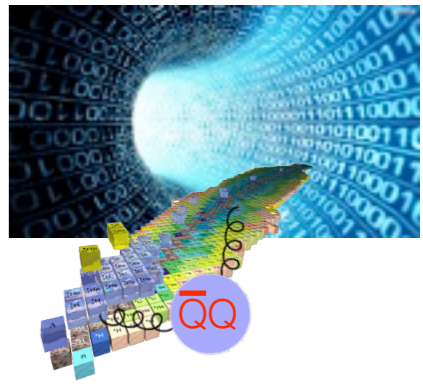
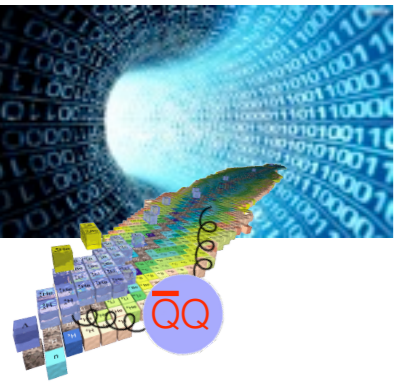
$$G_{\mu\nu} G^{\mu\nu}, G_{0\alpha} G_0^\alpha$$

$$O(1) \quad (\text{Luke, Manohar, MJS})$$

$$G_{i\alpha} G_j^\alpha \text{ symmetrized, traceless}$$

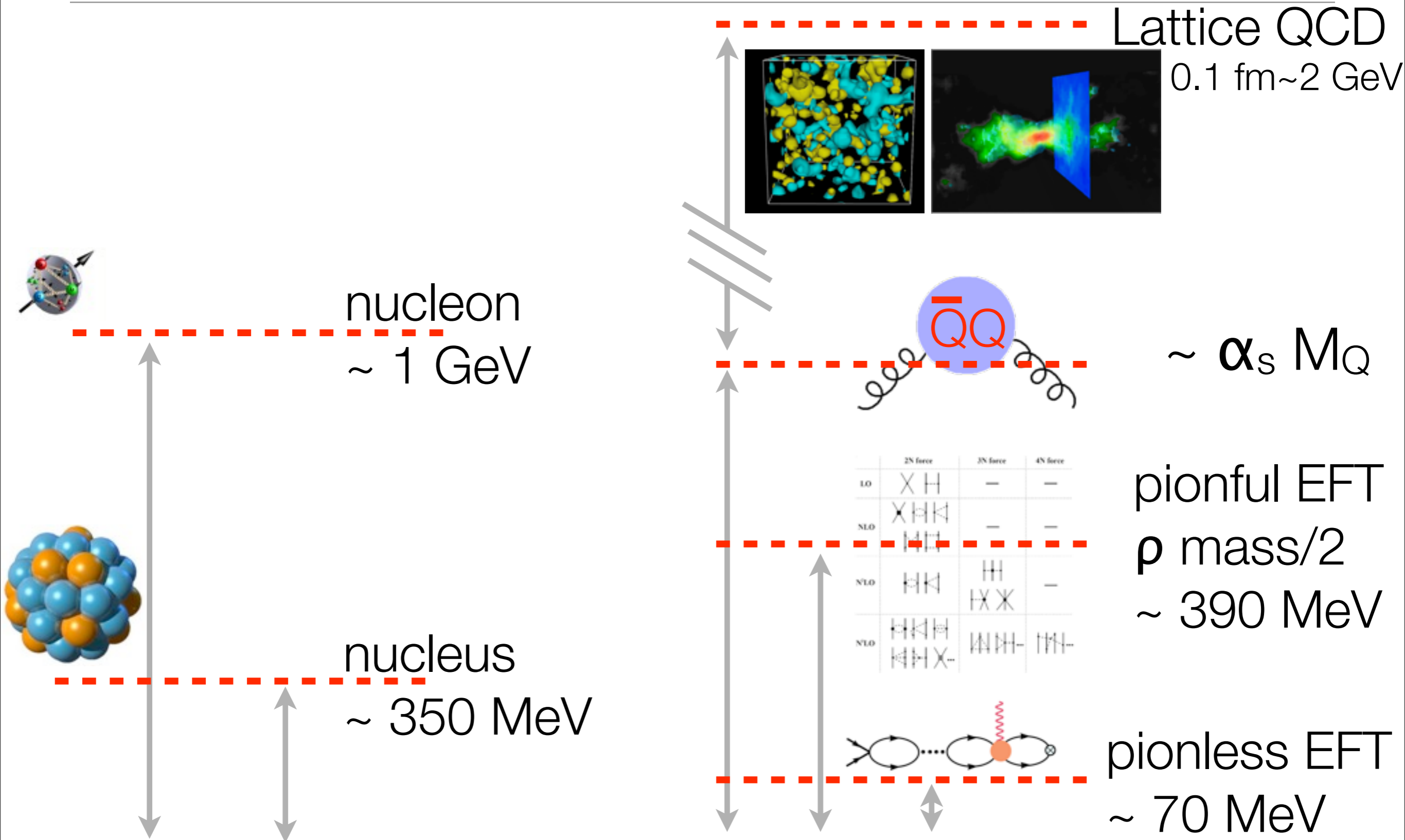
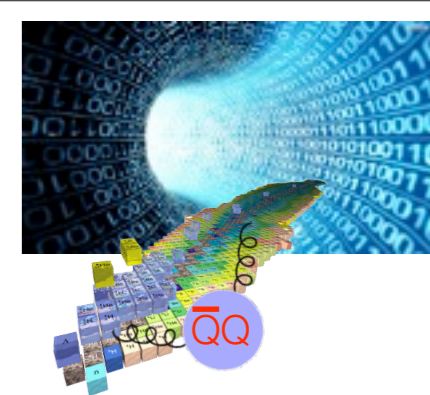
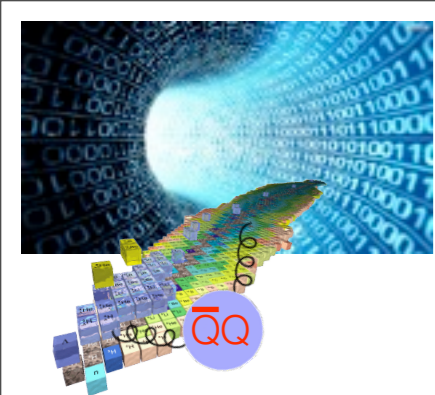
$$O(1/M_Q)$$

Leading Interactions

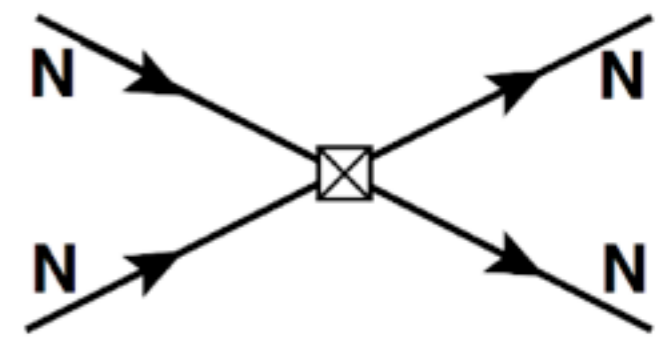
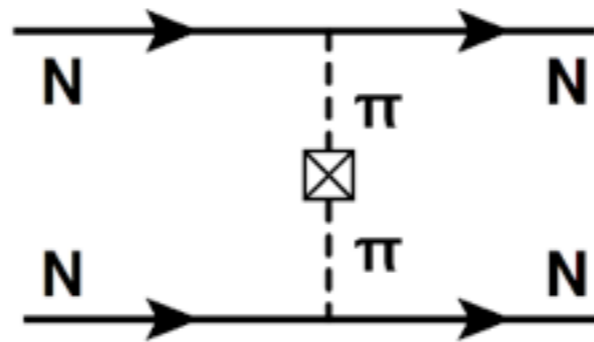
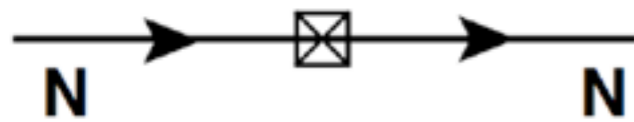
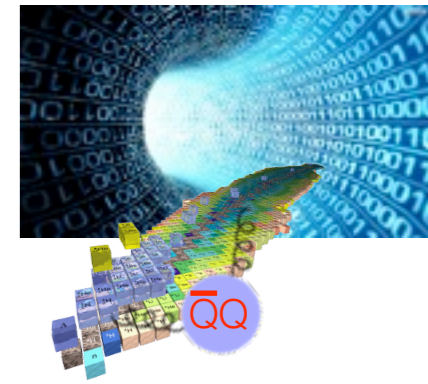
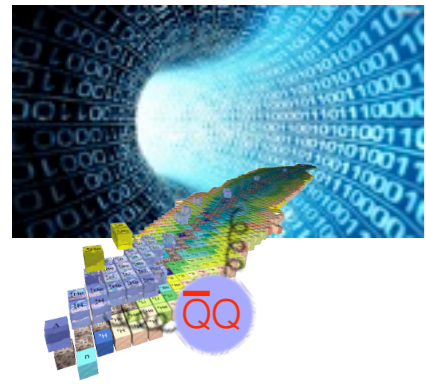


$$V \sim e^{-2mr} / r$$

Energy Scales



EFT Matching

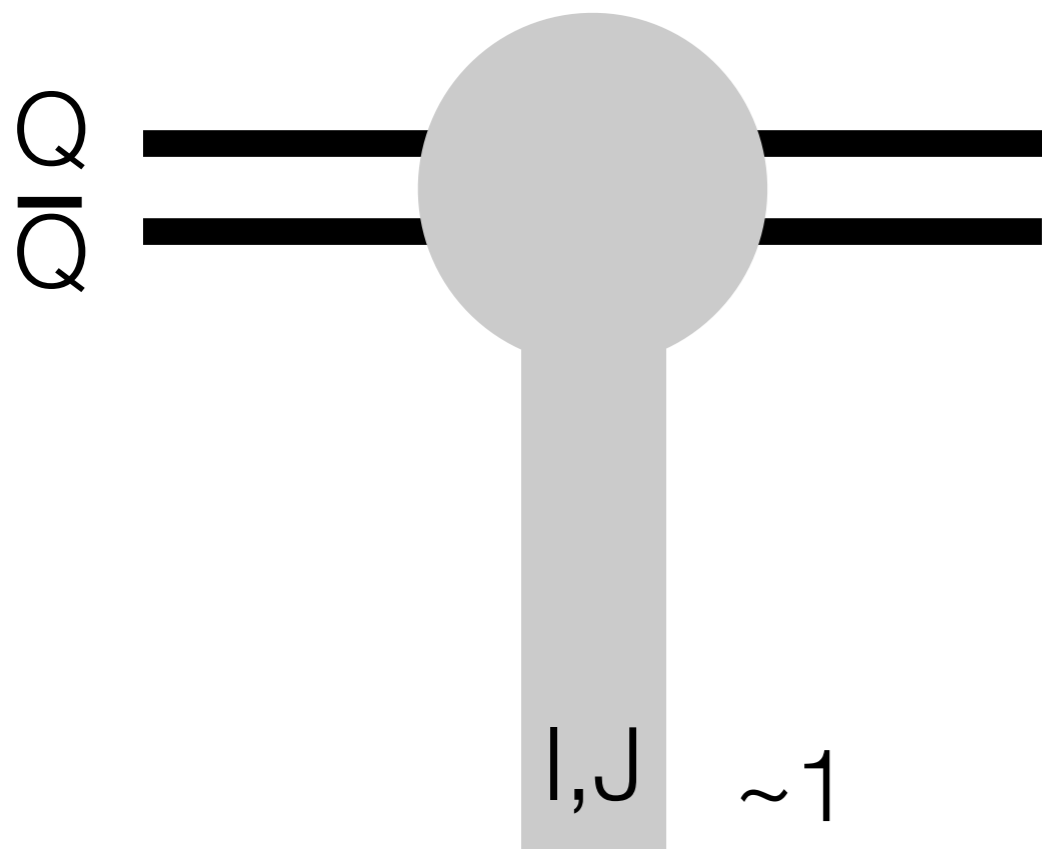
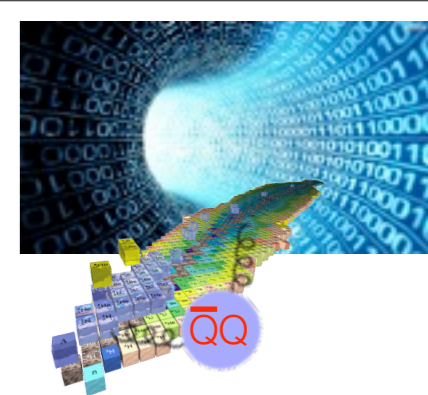
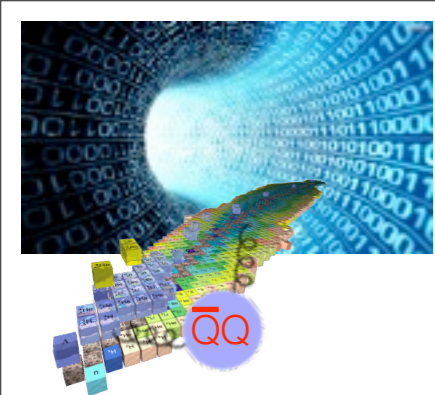


Single Nucleon

Required by QCD !
How big ??

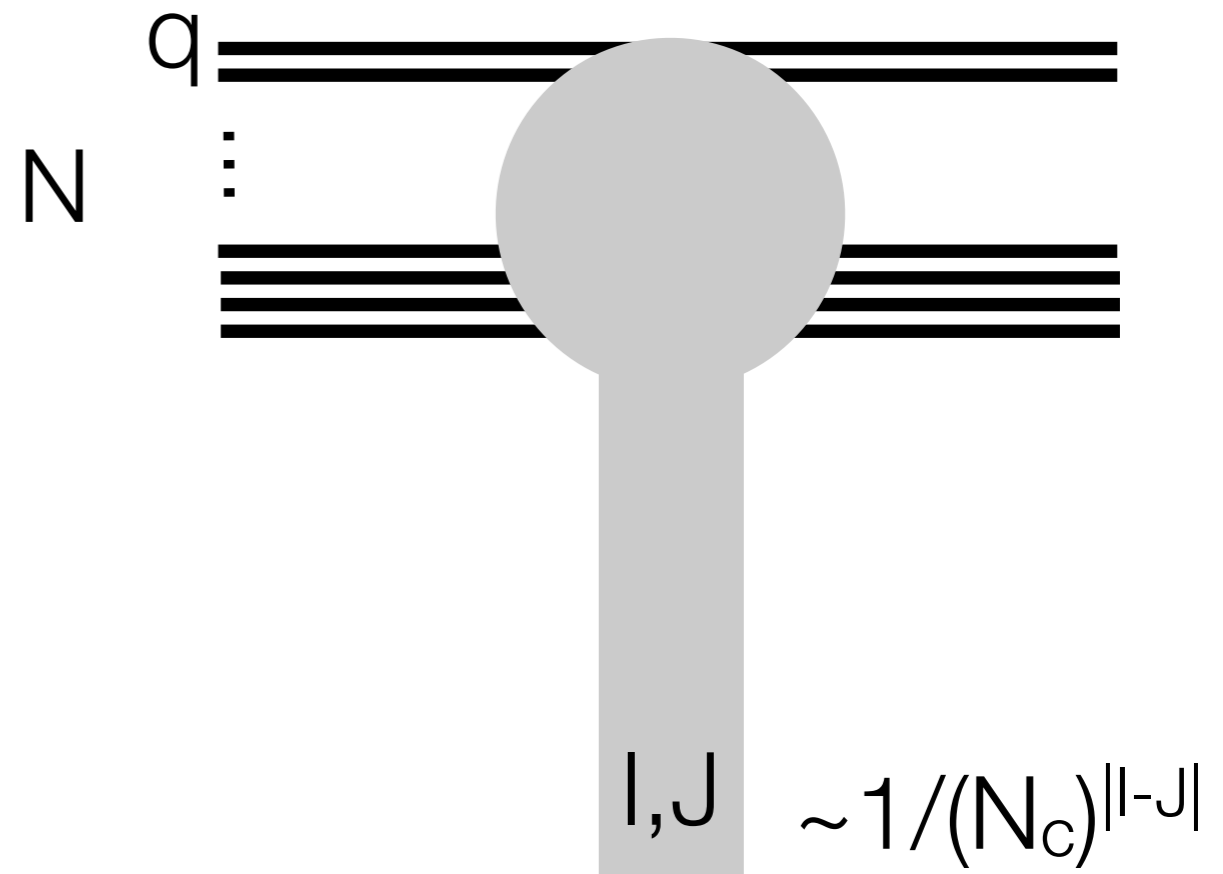
Quarkonium

Symmetries and Interactions



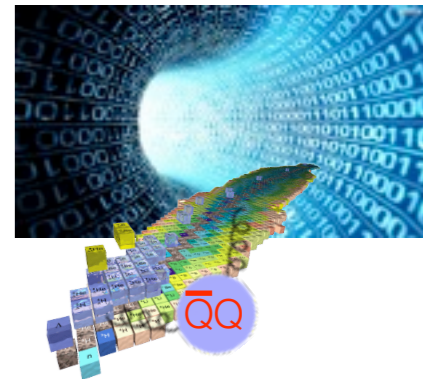
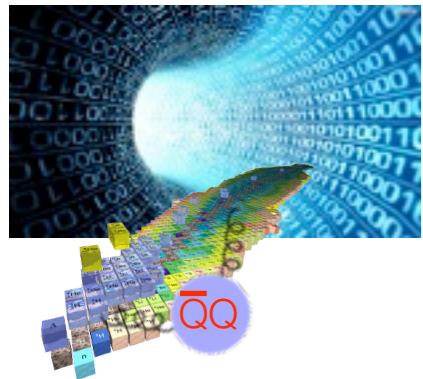
Large- N_c Limit

η_c and J/ψ have spin-independent interactions up to $1/M_Q$



Nuclei have $1/N_c$ suppressions that depend on t-channel quantum numbers

J/ψ - deuteron Interactions



e.g., structures of the effective interactions

$$\psi^{j\dagger} \psi_j d^{k\dagger} d_k$$

$$O(1)$$

$$J_t=0$$

$$\varepsilon^{ijk} \psi^{j\dagger} \psi_k \varepsilon^{ilm} d^{l\dagger} d_m$$

$$O(1/N_c, 1/M_Q, g_s)$$

$$J_t=1$$

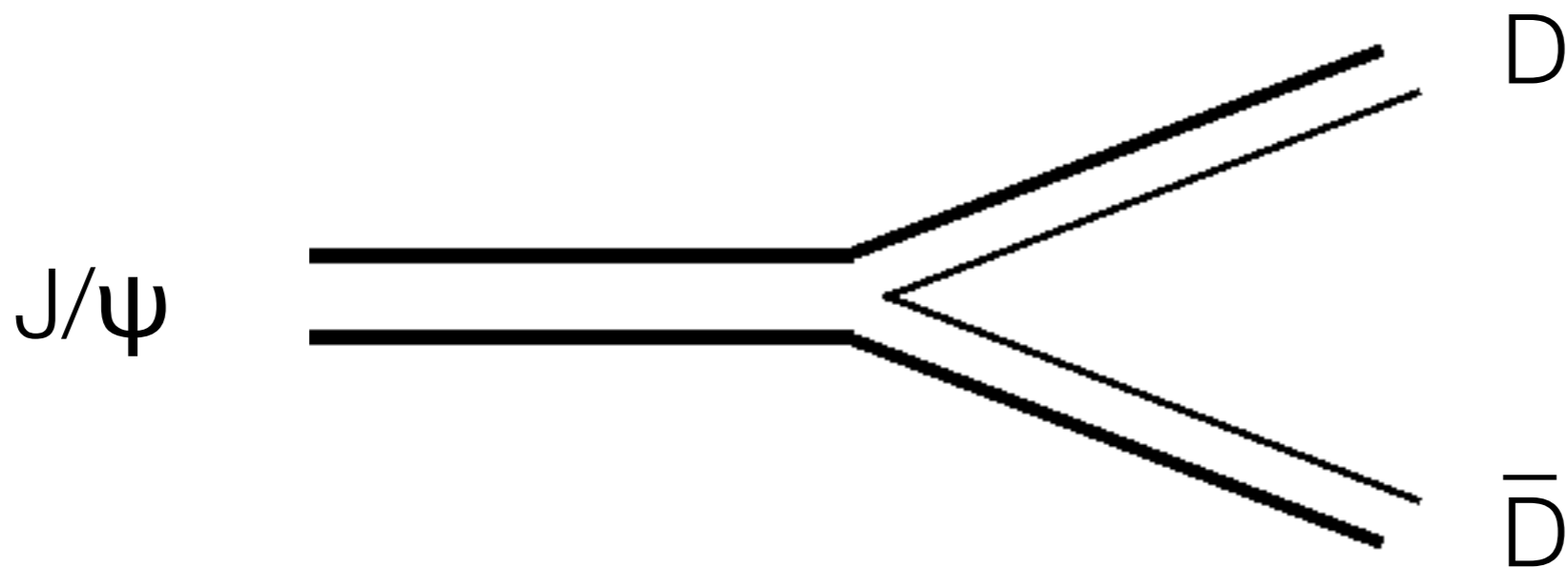
$$(\psi^{\{i\dagger} \psi_{j\}} - 2/3 \delta^{ij} \text{traces}) (d^{\{i\dagger} d_{j\}} - 2/3 \delta^{ij} \text{traces})$$

$$O(1/N_c^2, 1/M_Q)$$

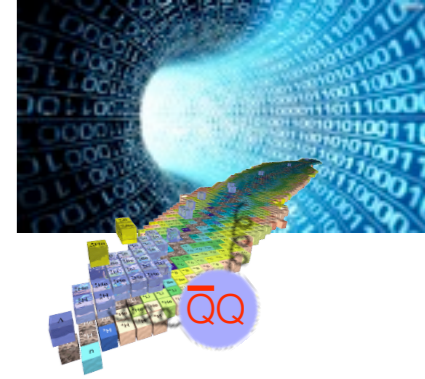
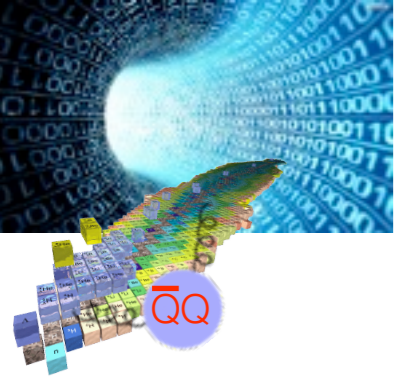
$$J_t=2$$

Charmonium Issues

- Is charmonium small enough ?
 - probably significant impact from charmed meson states
- Is strangeonium small enough ?
 - degenerate hadronic states, SU(3) symmetry

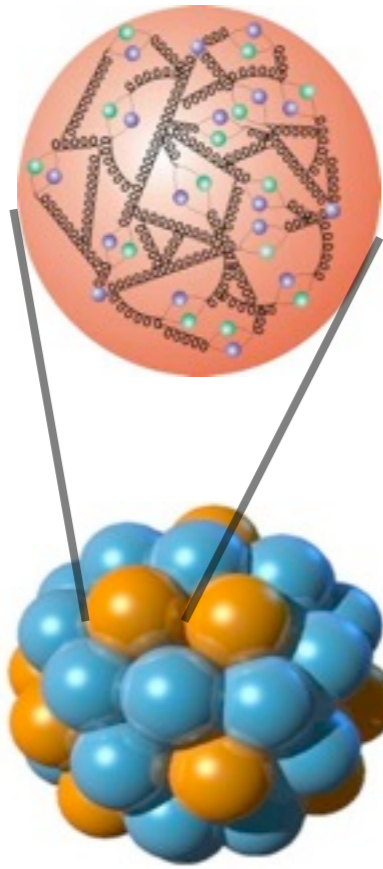


The Structure and Interactions of Matter from Quantum Chromodynamics



$p, n, \Lambda,$
 Σ, Ξ

(Hyper)
Nucleus



Quarks
and
Gluons

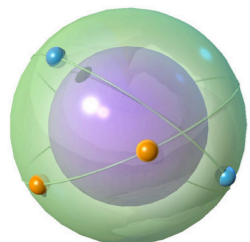
Λ_{QCD}

$$\frac{m_u}{\Lambda_{\text{QCD}}}$$

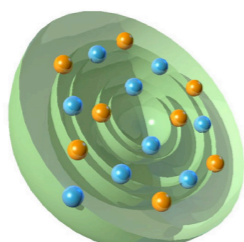
$$\frac{m_d}{\Lambda_{\text{QCD}}}$$

$$\frac{m_s}{\Lambda_{\text{QCD}}}$$

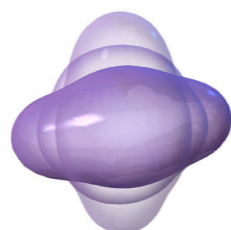
α_e



Spin-pairing



Shell-structure

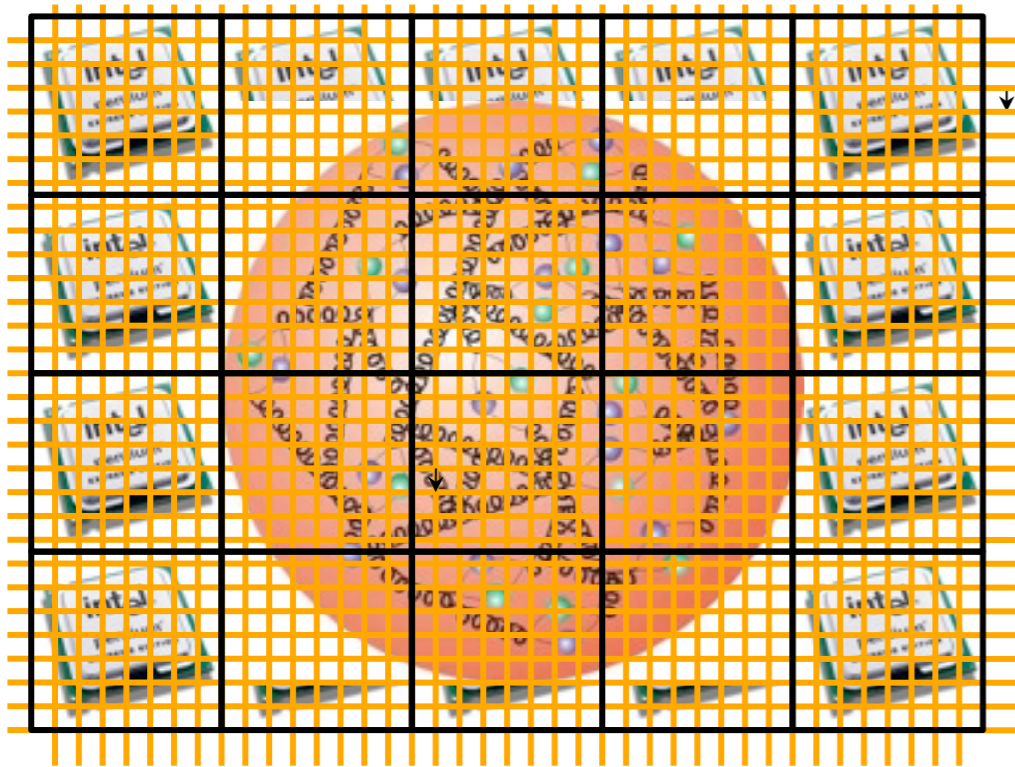


Vibrational and rotational
excitations

**Small number of input
parameters responsible for all
of strongly interacting matter**

Lattice QCD

Using a Discretized Spacetime



Lattice Spacing :
 $a \ll 1/\Lambda\chi$
(Nearly Continuum)

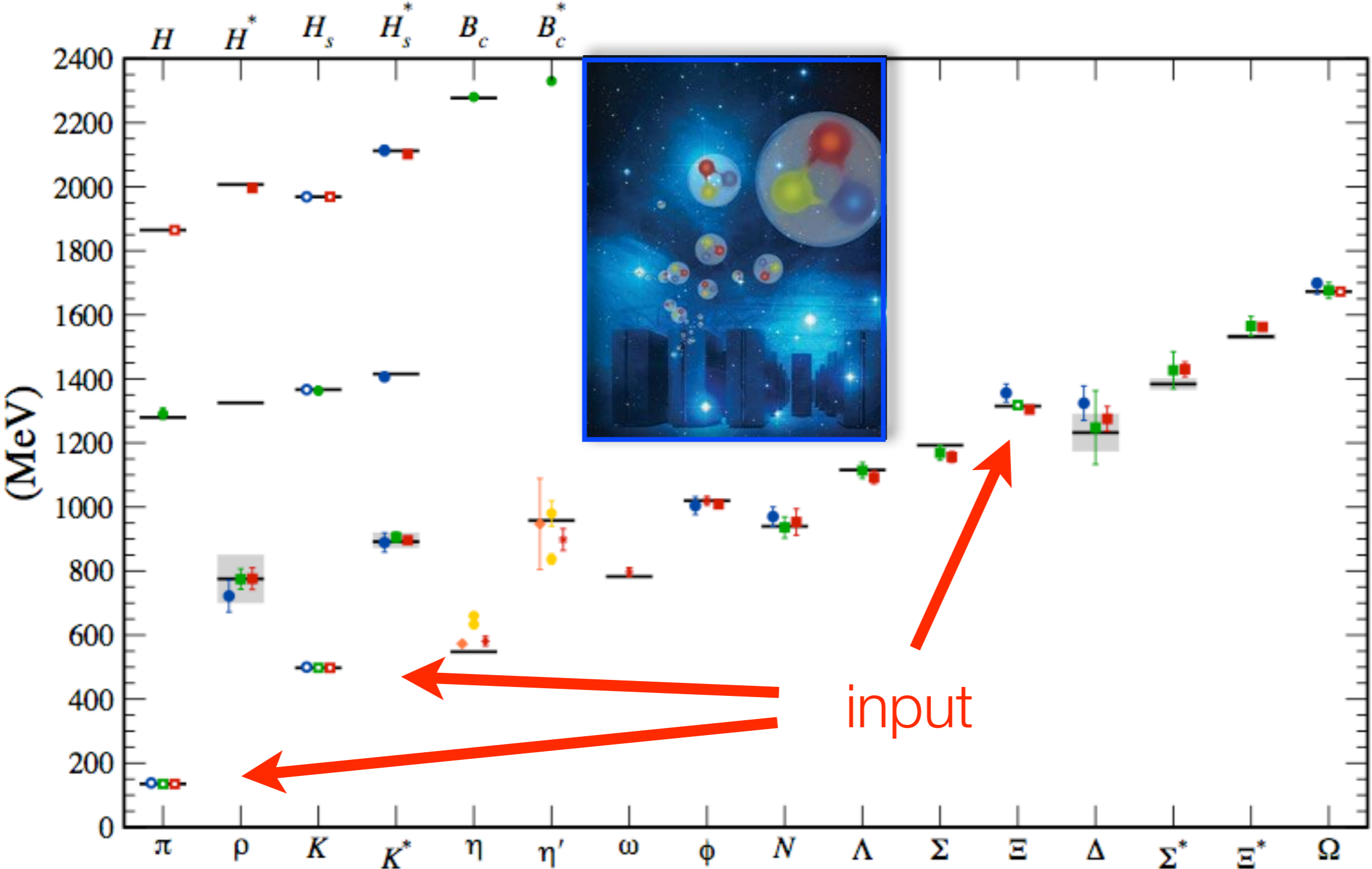
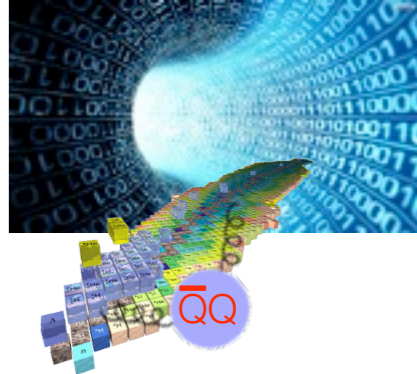
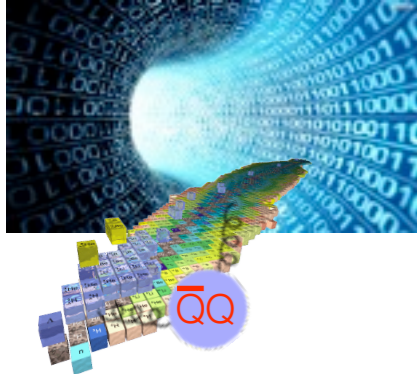
Lattice Volume :
 $m_\pi L \gg 2\pi$
(Nearly Infinite Volume)

Extrapolation to $a = 0$ and $L = \infty$

Systematically remove non-QCD parts of calculation

$$\langle \hat{\theta} \rangle \sim \int \mathcal{D}\mathcal{U}_\mu \hat{\theta}[\mathcal{U}_\mu] \det[\kappa[\mathcal{U}_\mu]] e^{-S_{YM}} \rightarrow \frac{1}{N} \sum_{\text{gluon cfgs}}^N \hat{\theta}[\mathcal{U}_\mu]$$

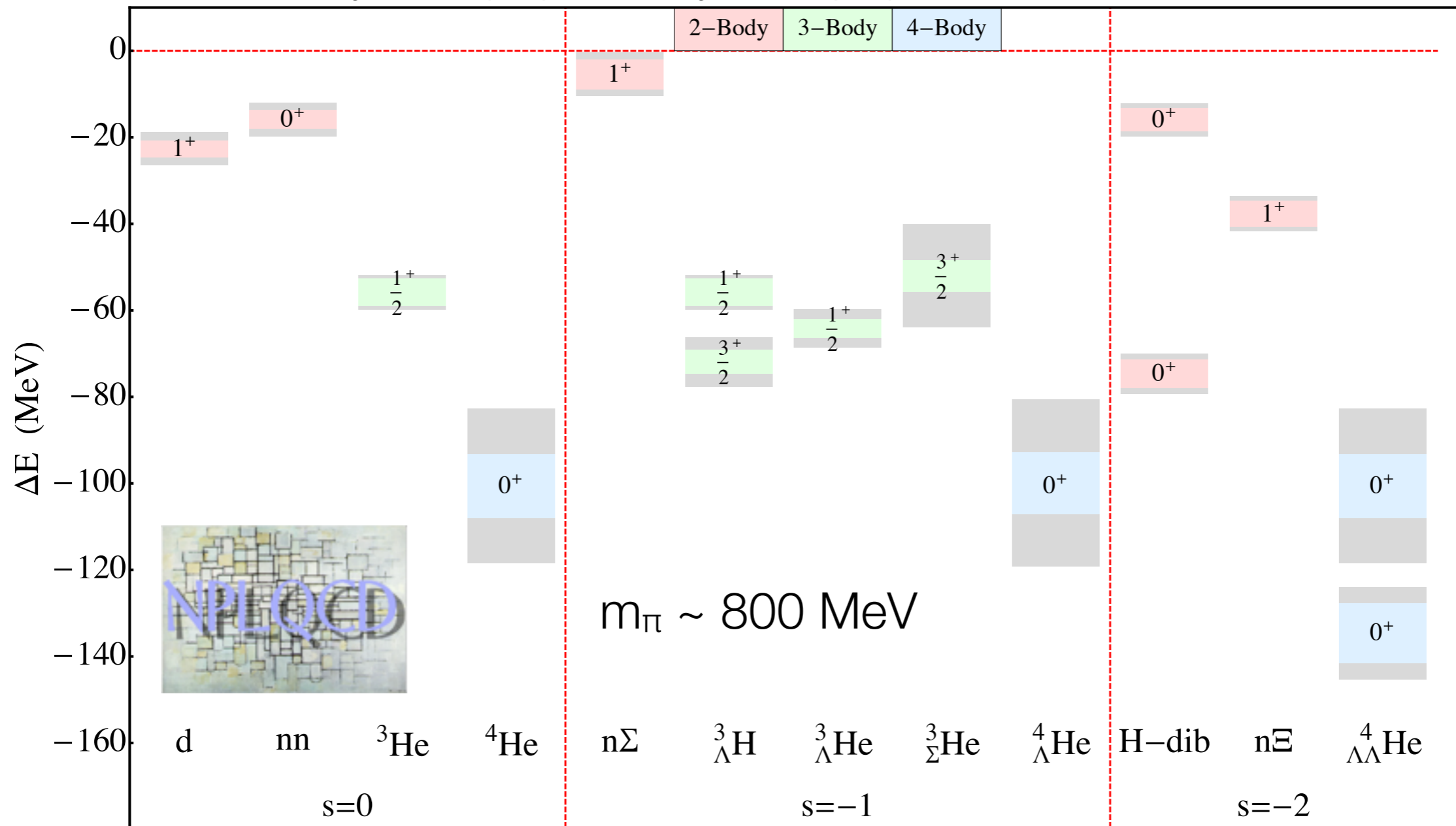
Hadron Masses



(Kronfeld)

(Hyper)Nuclei from QCD

Beane, Chang, Cohen, Detmold, Lin, Luu, Orginos, Parreno, MJS, Walker-Loud,
 Phys.Rev. D87 (2013) 3, 034506, Phys.Rev. C88 (2013) 2, 024003

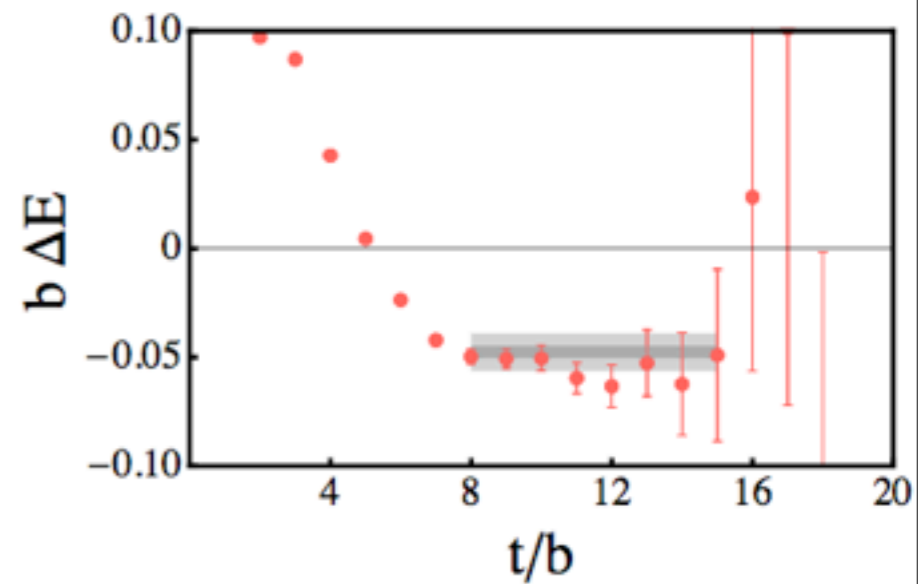
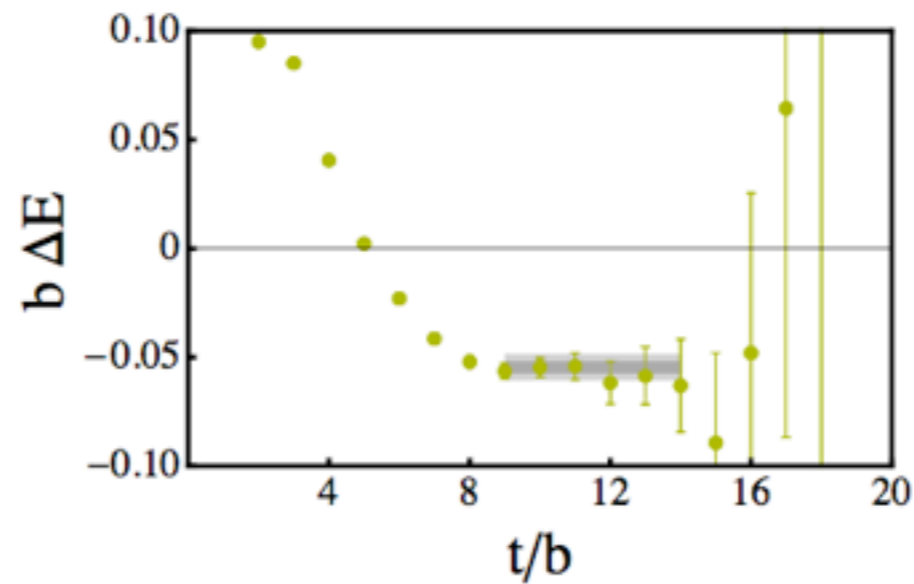
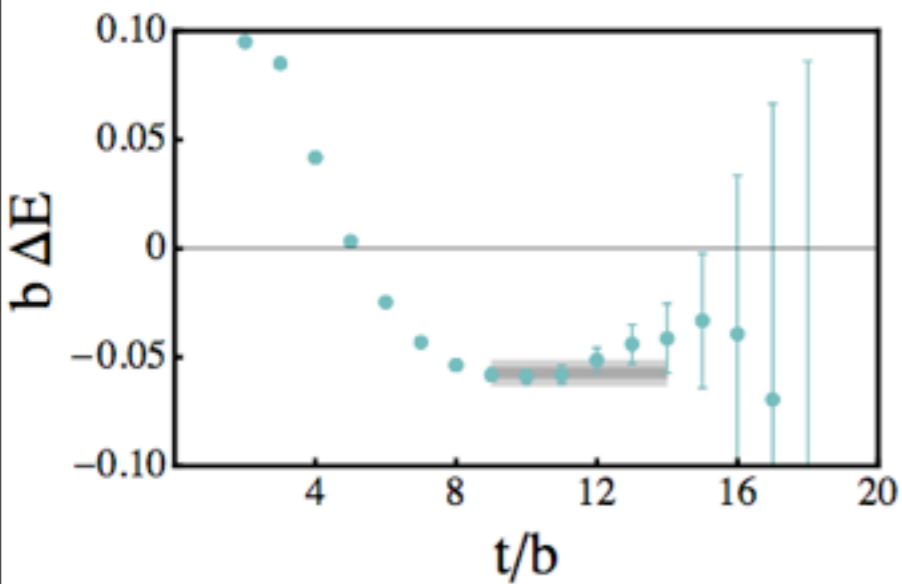


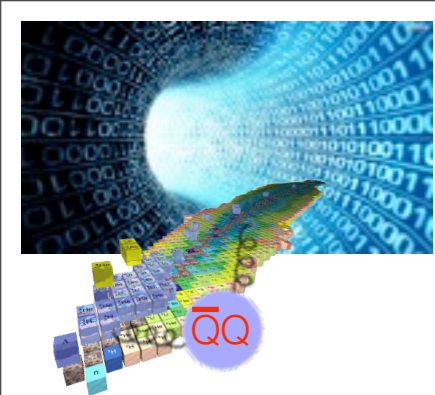
Extensive study of s-shell nuclei and hypernuclei, and baryon-baryon interactions at SU(3) symmetric point

(Hyper)Nuclei from QCD

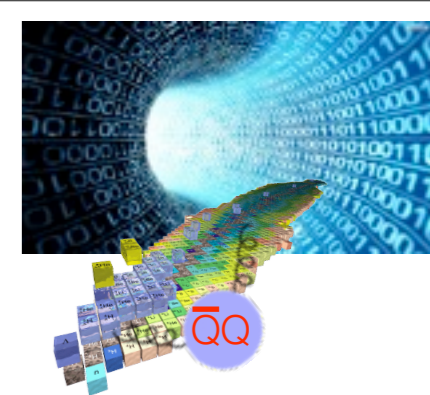
Beane, Chang, Cohen, Detmold, Lin, Luu, Orginos, Parreno, MJS, Walker-Loud,
Phys.Rev. D87 (2013) 3, 034506, Phys.Rev. C88 (2013) 2, 024003

e.g. 3-body correlator - $n\Lambda$, ${}^3_\Lambda\text{H}$





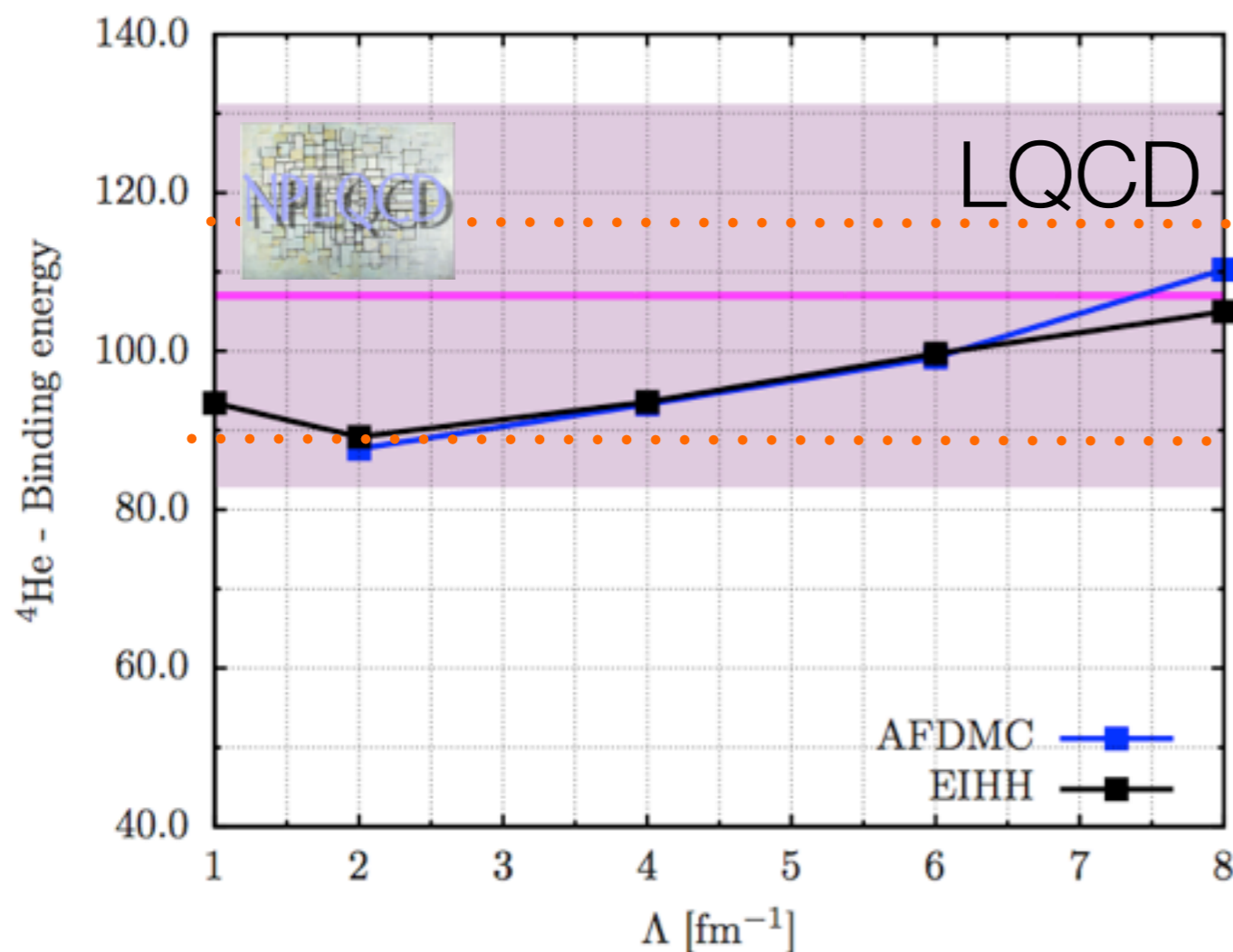
LQCD to Pionless EFT to Nuclei



LQCD Nuclei for 800 MeV pions

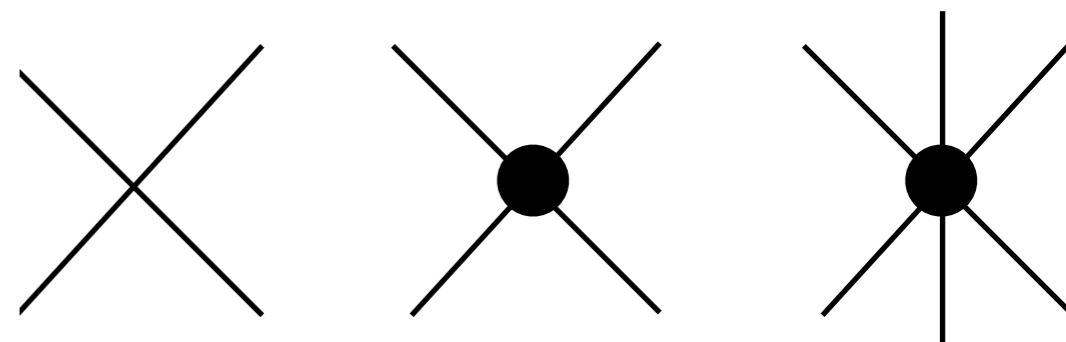
- Fit 2-body and 3-body LQCD bindings
- Predict 4-body, c/w LQCD prediction

Barnea, Conressi, Gazit,
Pederiva and van Kolck
arXiv:1311.4966



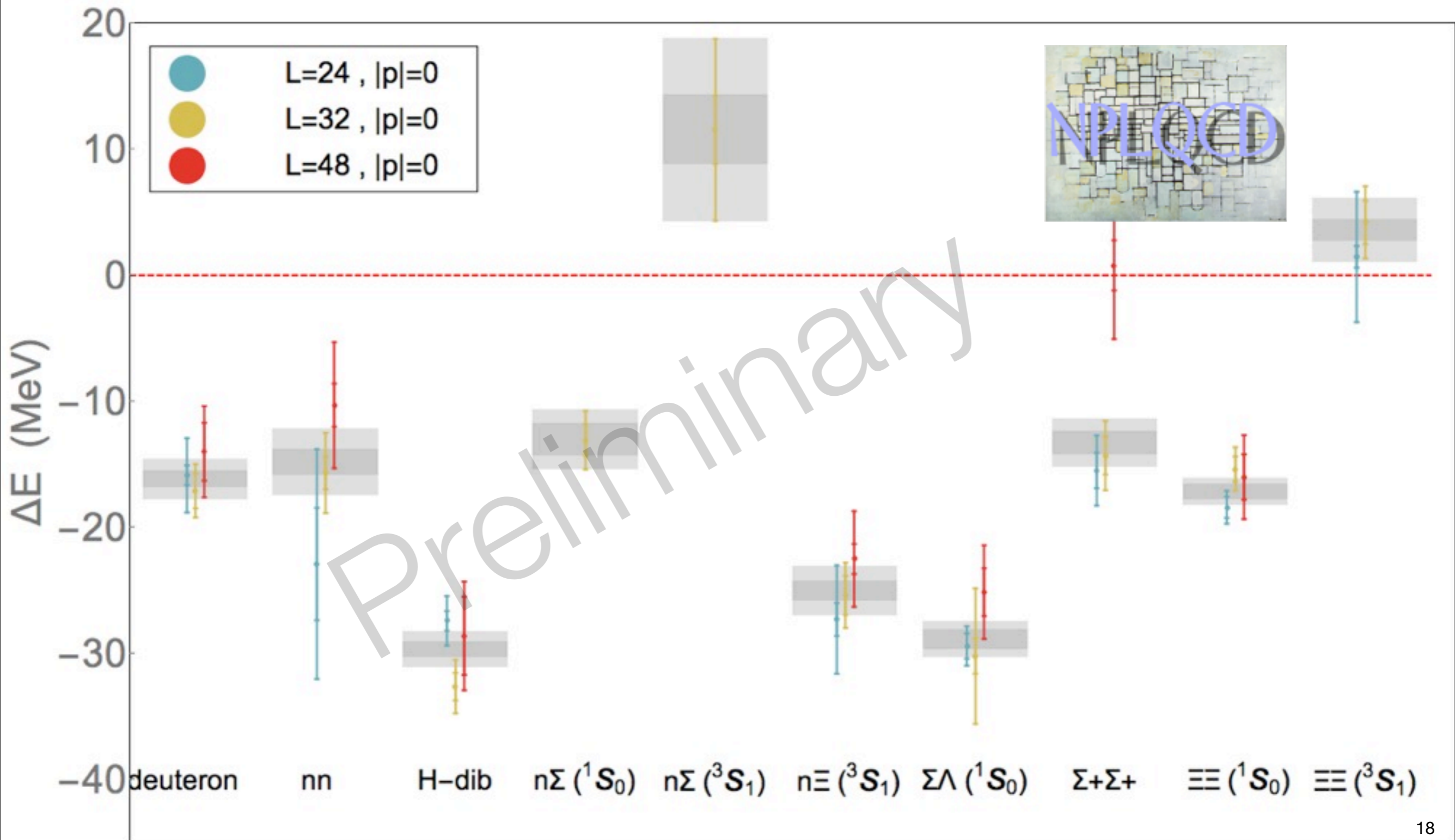
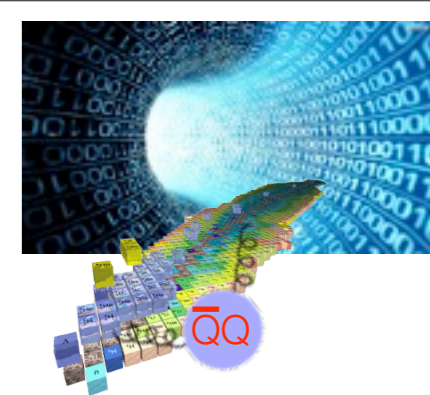
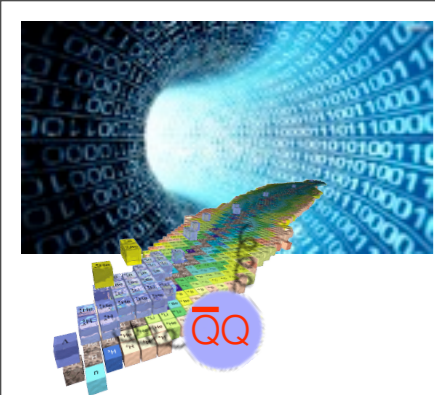
pionless EFT valid
for nuclei

“First Contact”

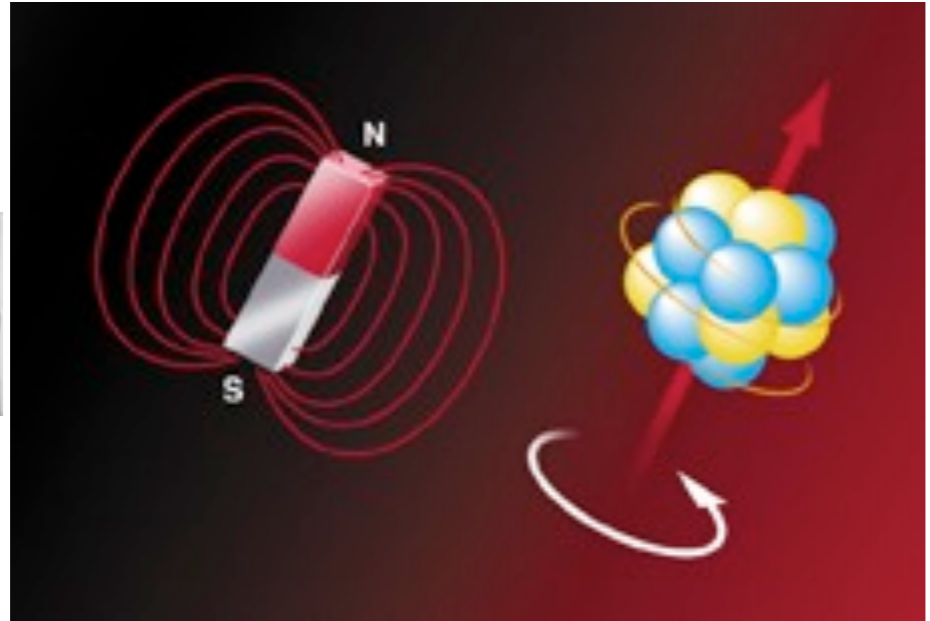


(Hyper)Nuclei from QCD

$$m_{\pi} \sim 430 \text{ MeV}$$

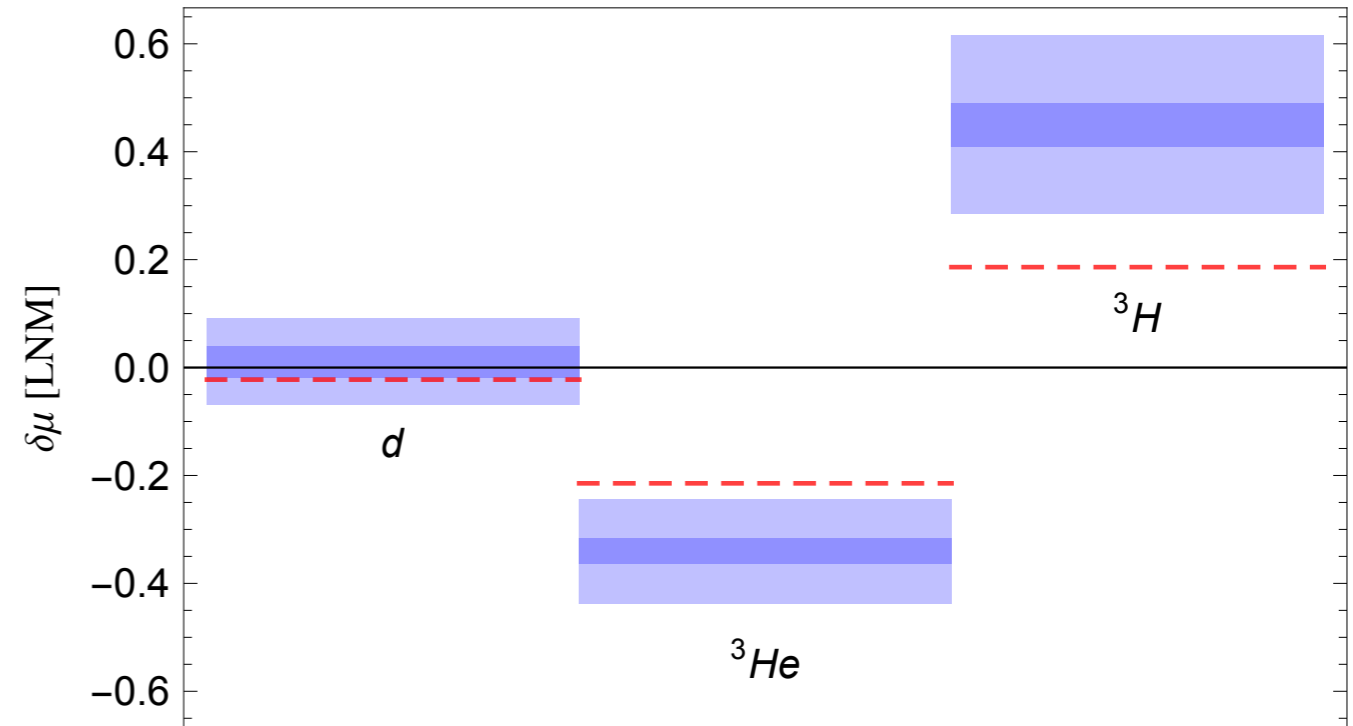
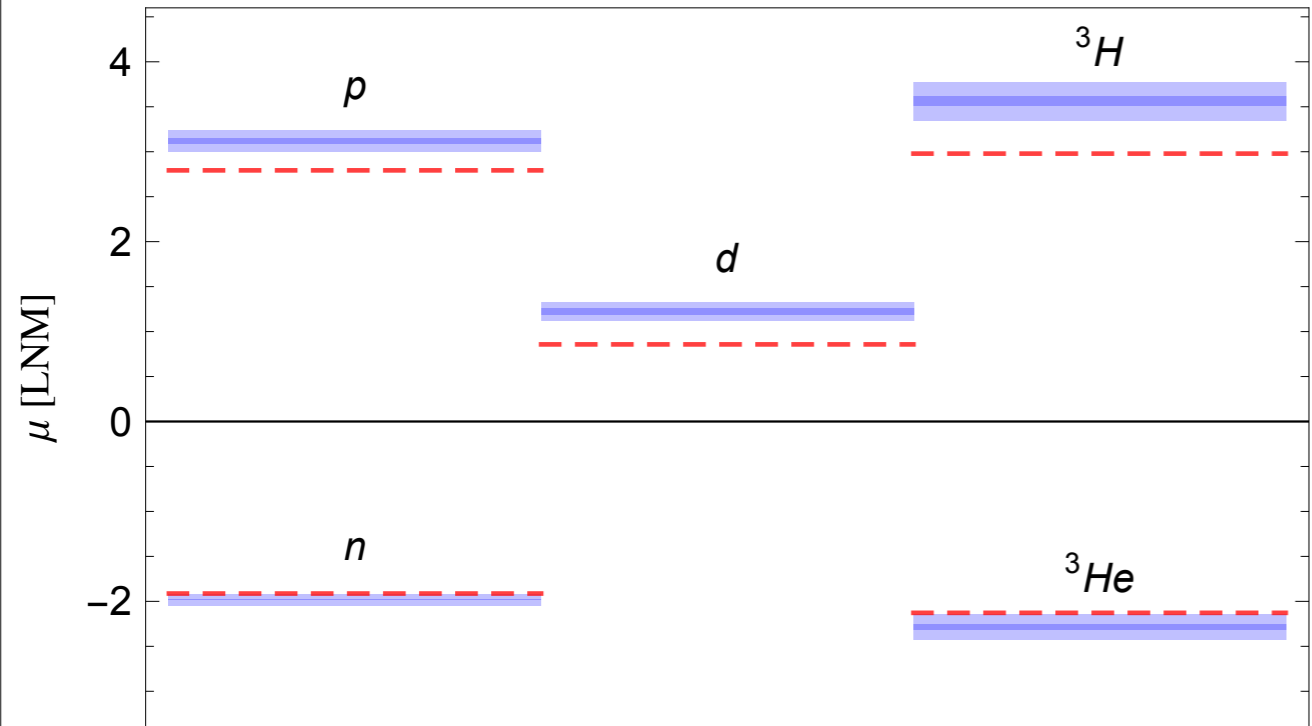


The Structure of Nuclei : Magnetic Moments



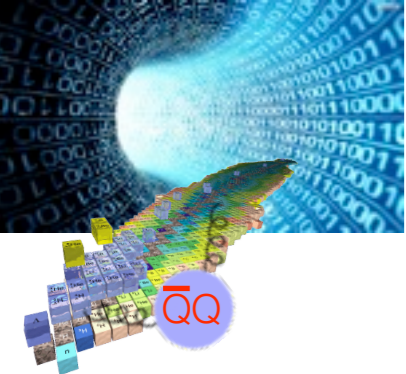
Beane, Chang, Cohen, Detmold, Lin, Luu, Orginos, Parreno, MJS, Tiburzi,
Phys.Rev. Lett. 113 (2014) 25, 252001

$m_\pi \sim 800 \text{ MeV}$ Vs Nature



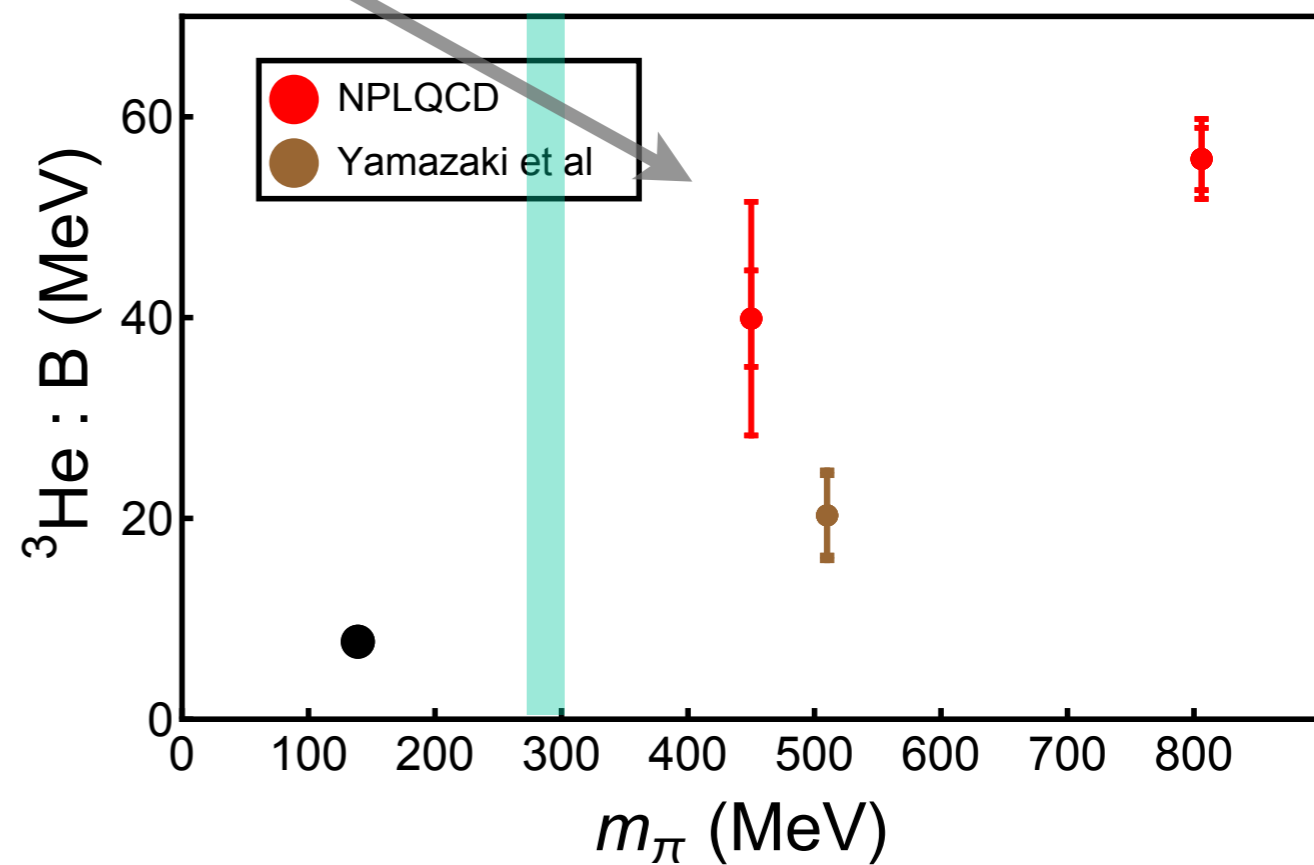
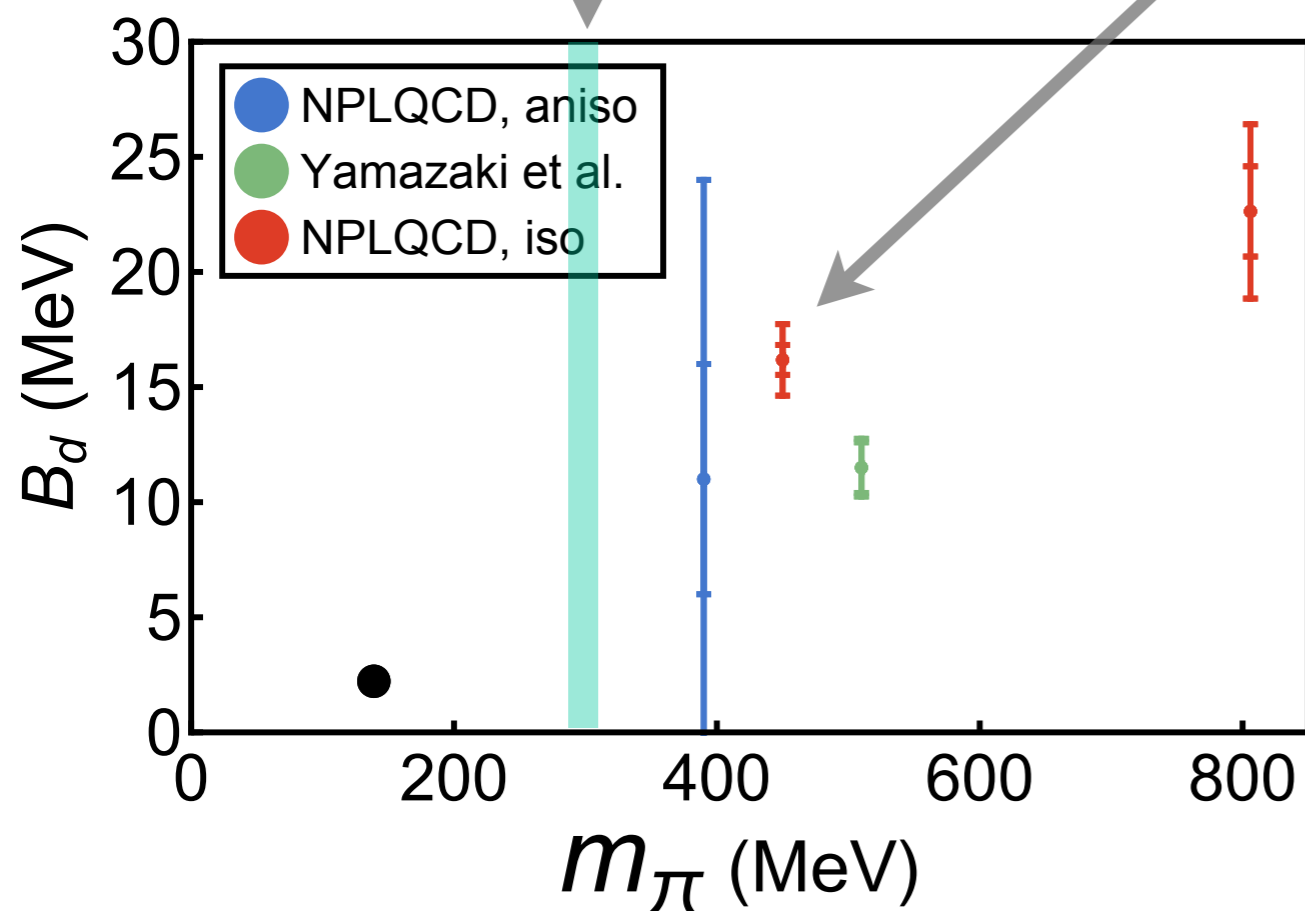
Nuclei are collections of nucleons
- shell model phenomenology!

Light Nuclei : Compilation



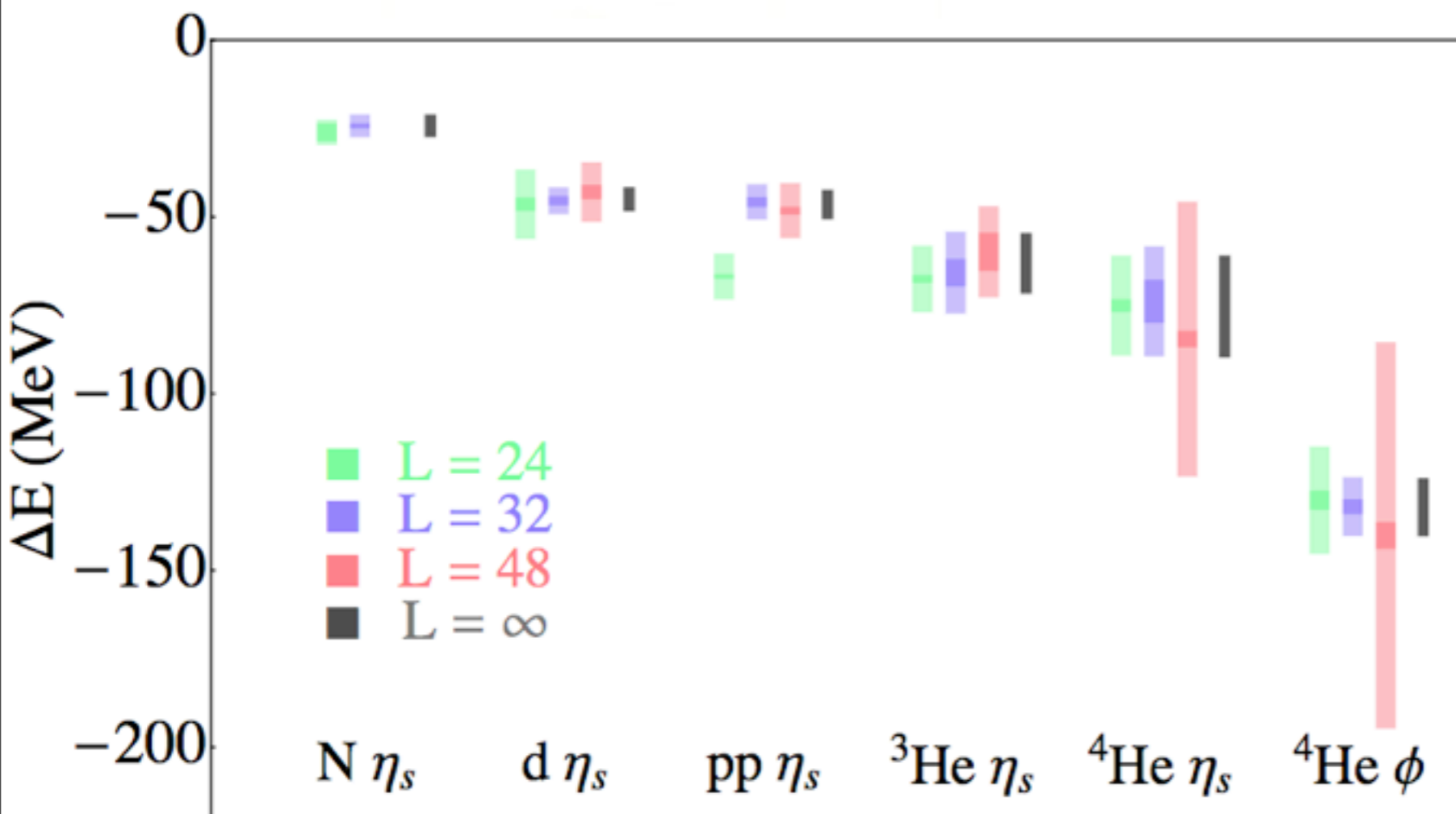
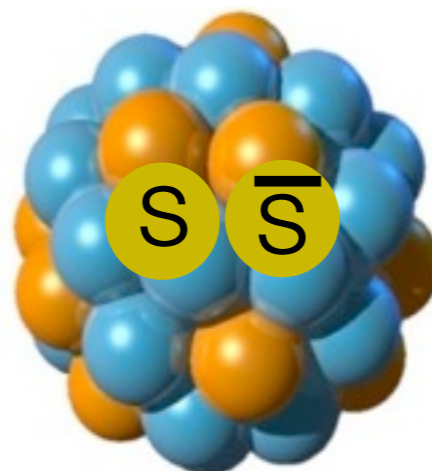
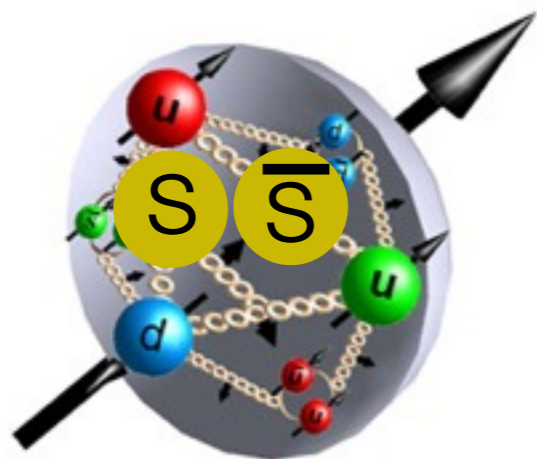
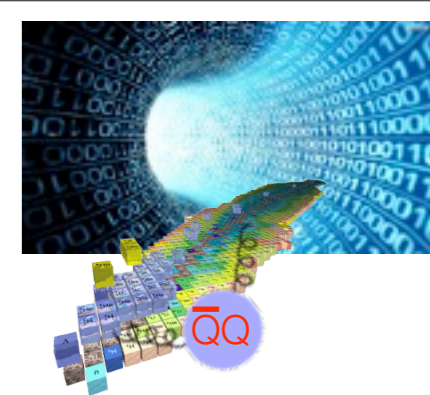
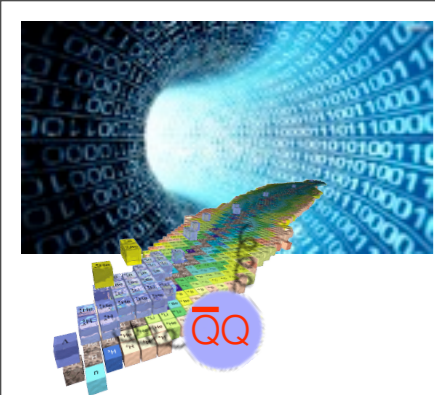
current production

preliminary



Strangeonium-Nuclei

$$m_{\pi} \sim 800 \text{ MeV}$$

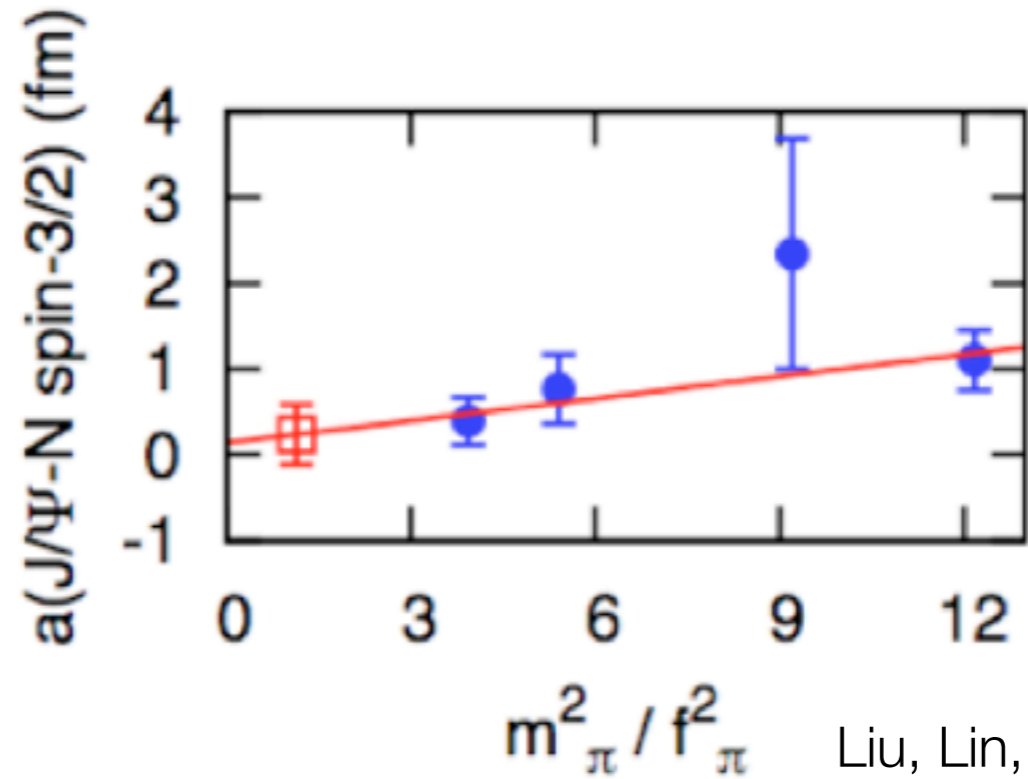
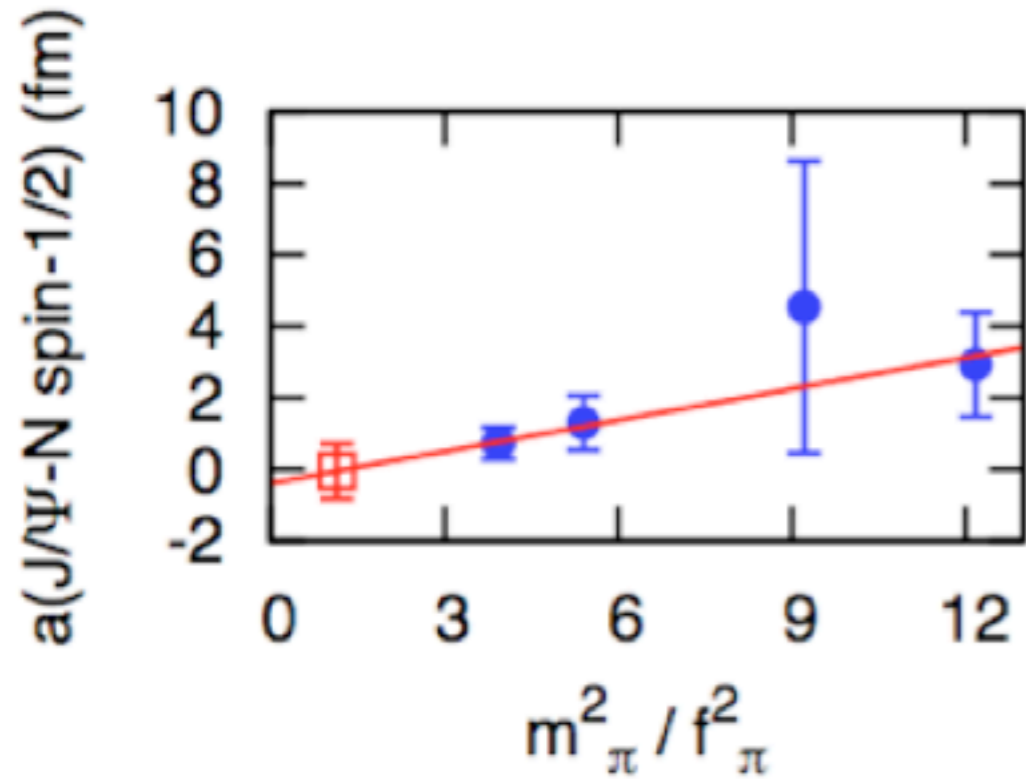


- coupled-channels
- challenging

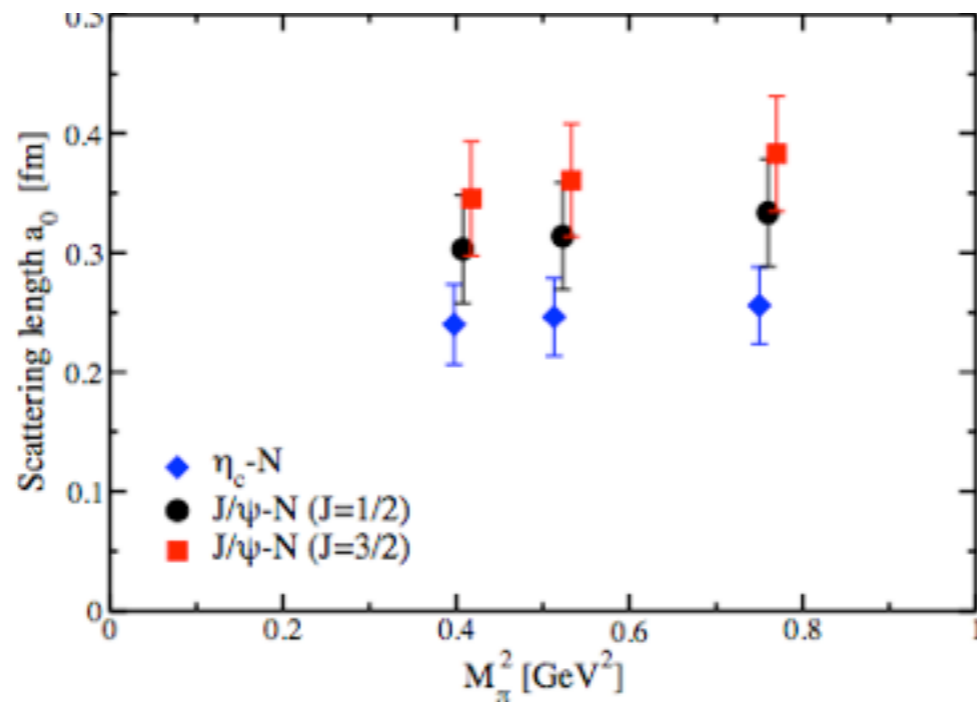
(Beane, Chang, Cohen, Detmold, Lin, Orginos, Parreno, MJS, [arXiv:1410.7069](https://arxiv.org/abs/1410.7069))

Charmonium-Nucleon

Previous Calculations



Liu, Lin, Orginos, (2008)

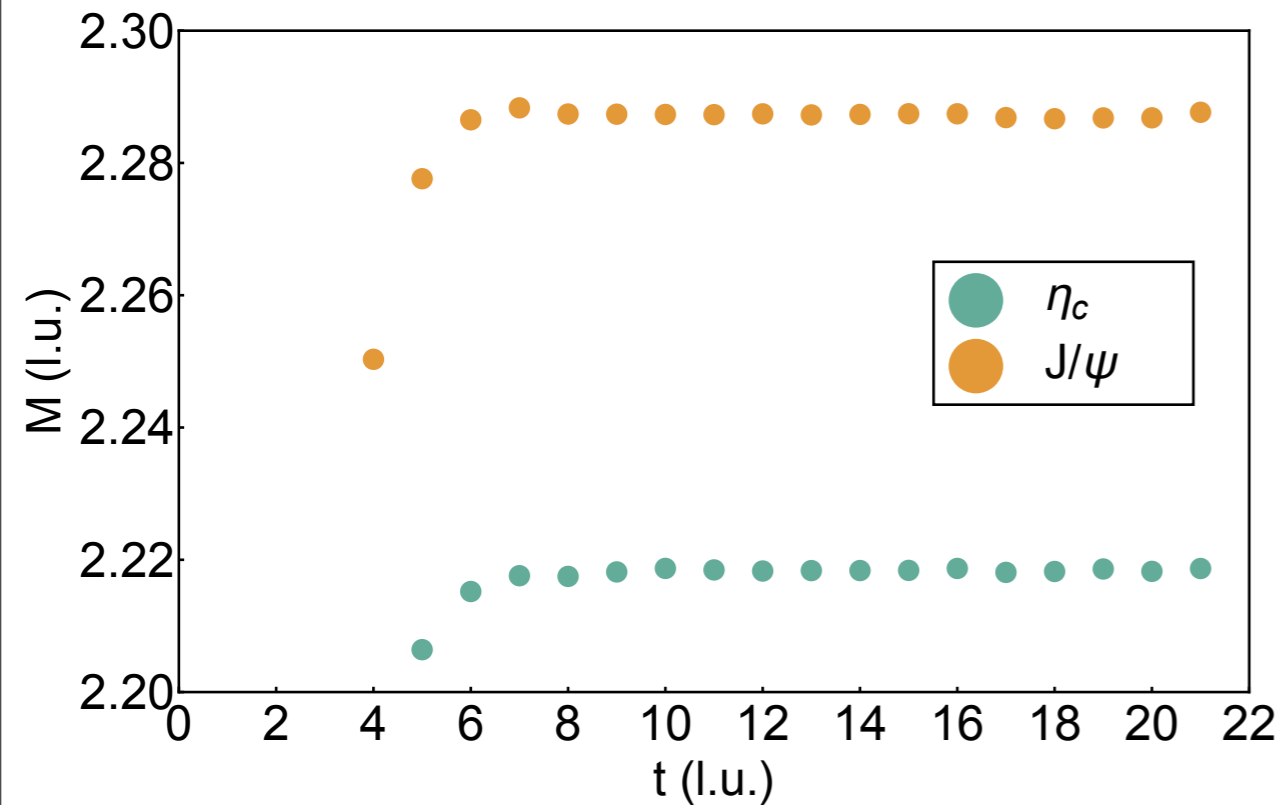


Kawanai, Sasaki, (2010)

Charmonium-Nuclei

$m_{\pi} \sim 800 \text{ MeV}$

$$S_Q = \sum_{x,x'} \bar{Q}_x \left(m_0 + \gamma_0 D_0 - \frac{a}{2} D_0^2 + \nu \left(\gamma_i D_i - \frac{a}{2} D_i^2 \right) - \frac{a}{4} c_B \sigma_{ij} G_{ij} - \frac{a}{2} c_E \sigma_{0i} G_{0i} \right)_{xx'} Q_{x'},$$

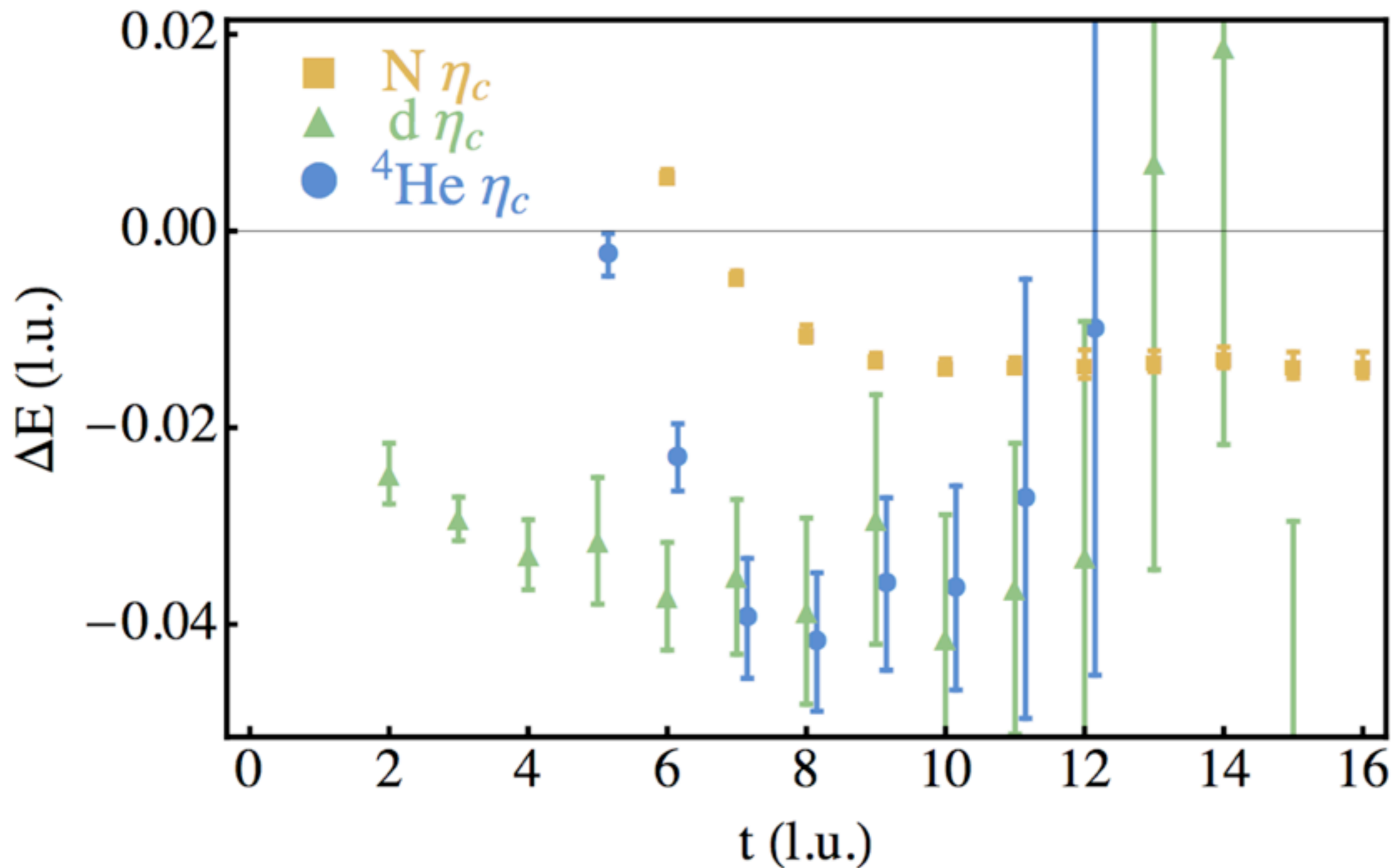
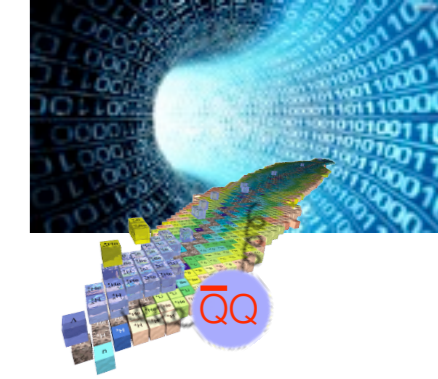
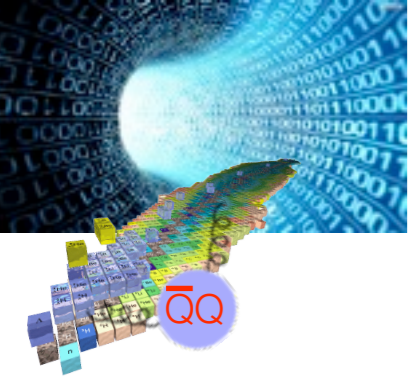


- tune to dispersion relations
- postmultiply nuclear correlators
 - src point by src point
 - shift in time to align plateaus

(Beane, Chang, Cohen, Detmold, Lin, Orginos, Parreno, MJS, [arXiv:1410.7069](https://arxiv.org/abs/1410.7069))

Charmonium-Nuclei

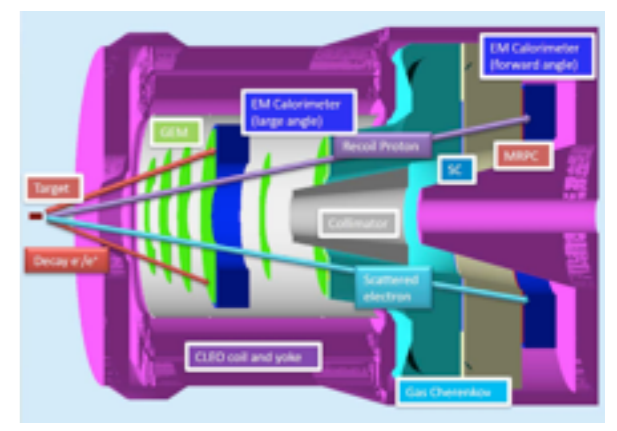
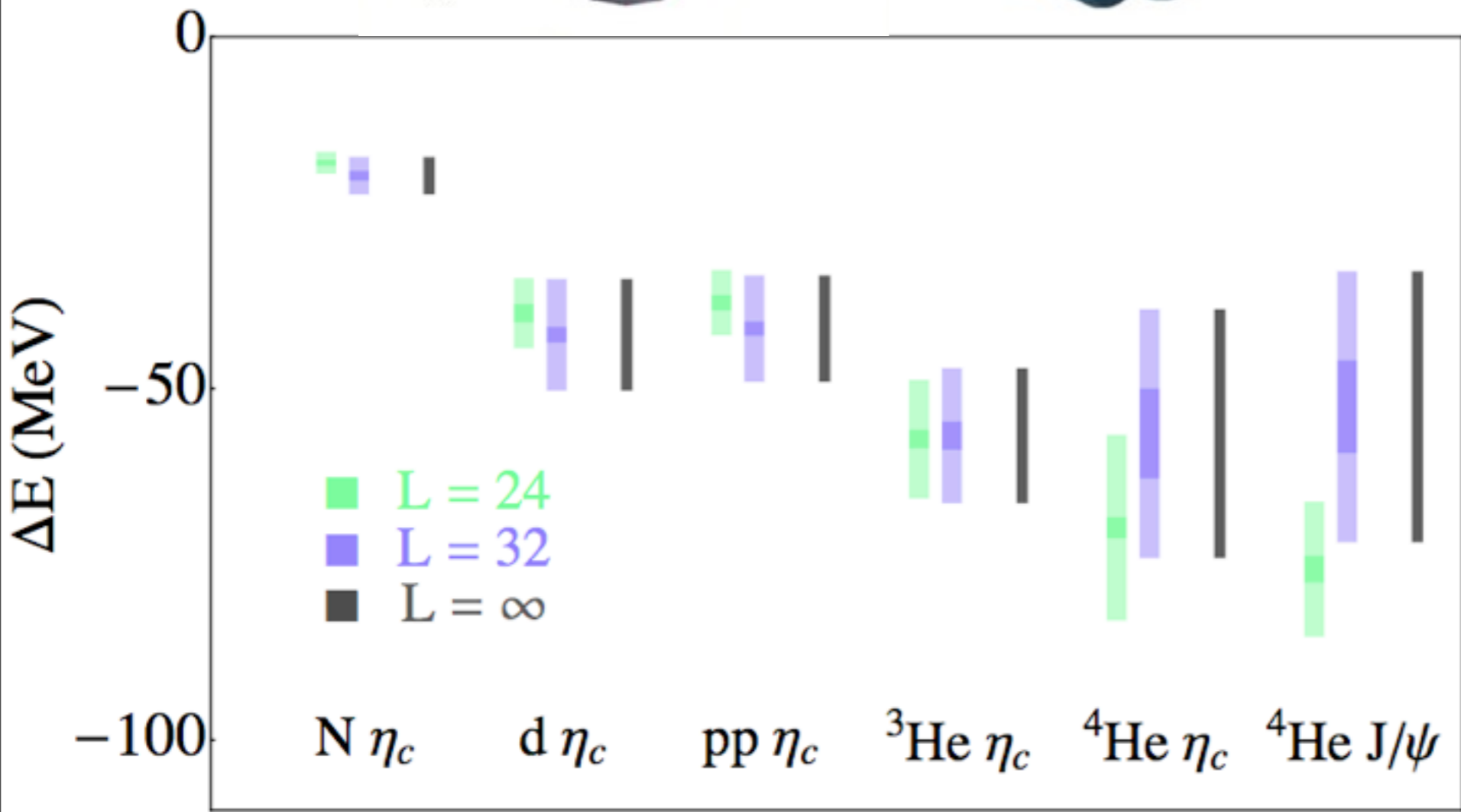
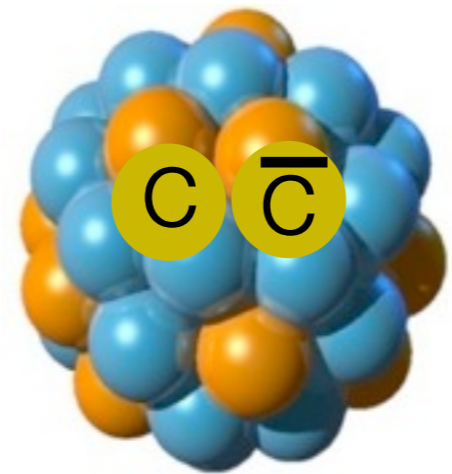
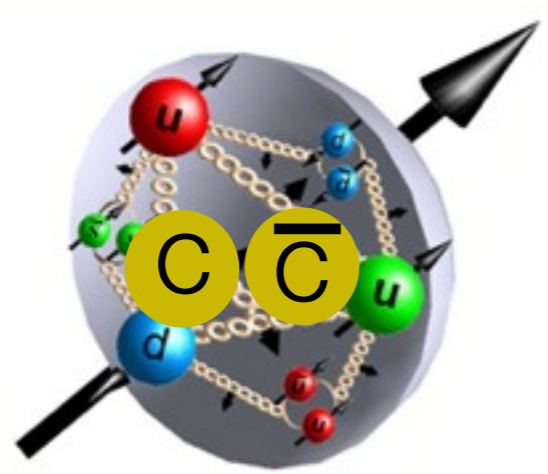
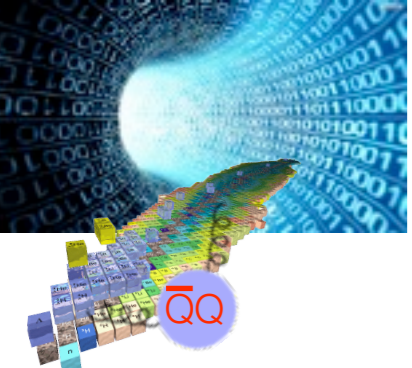
$m_{\pi} \sim 800 \text{ MeV}$



$32^3 \times 32^3 \times 32^3 \times 64$

Charmonium-Nuclei

$$m_{\pi} \sim 800 \text{ MeV}$$

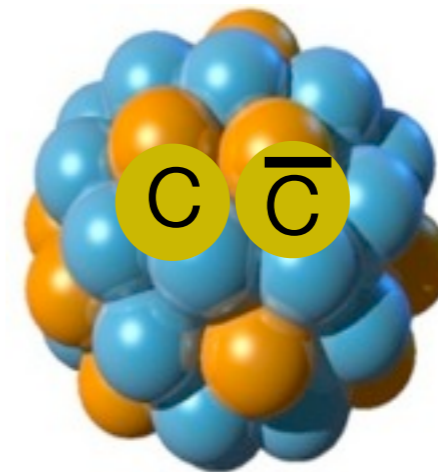
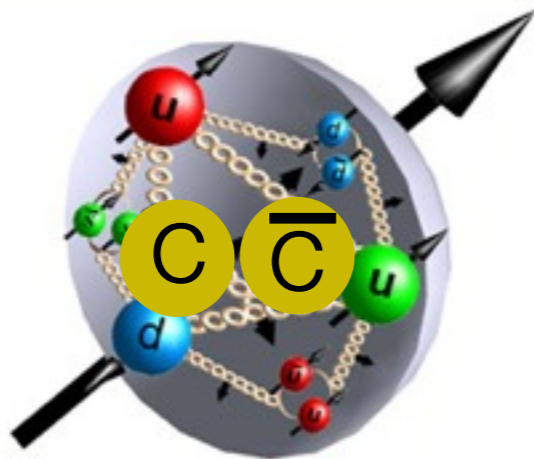


Athena



(Beane, Chang, Cohen, Detmold, Lin, Orginos, Parreno, MJS, [arXiv:1410.7069](https://arxiv.org/abs/1410.7069))

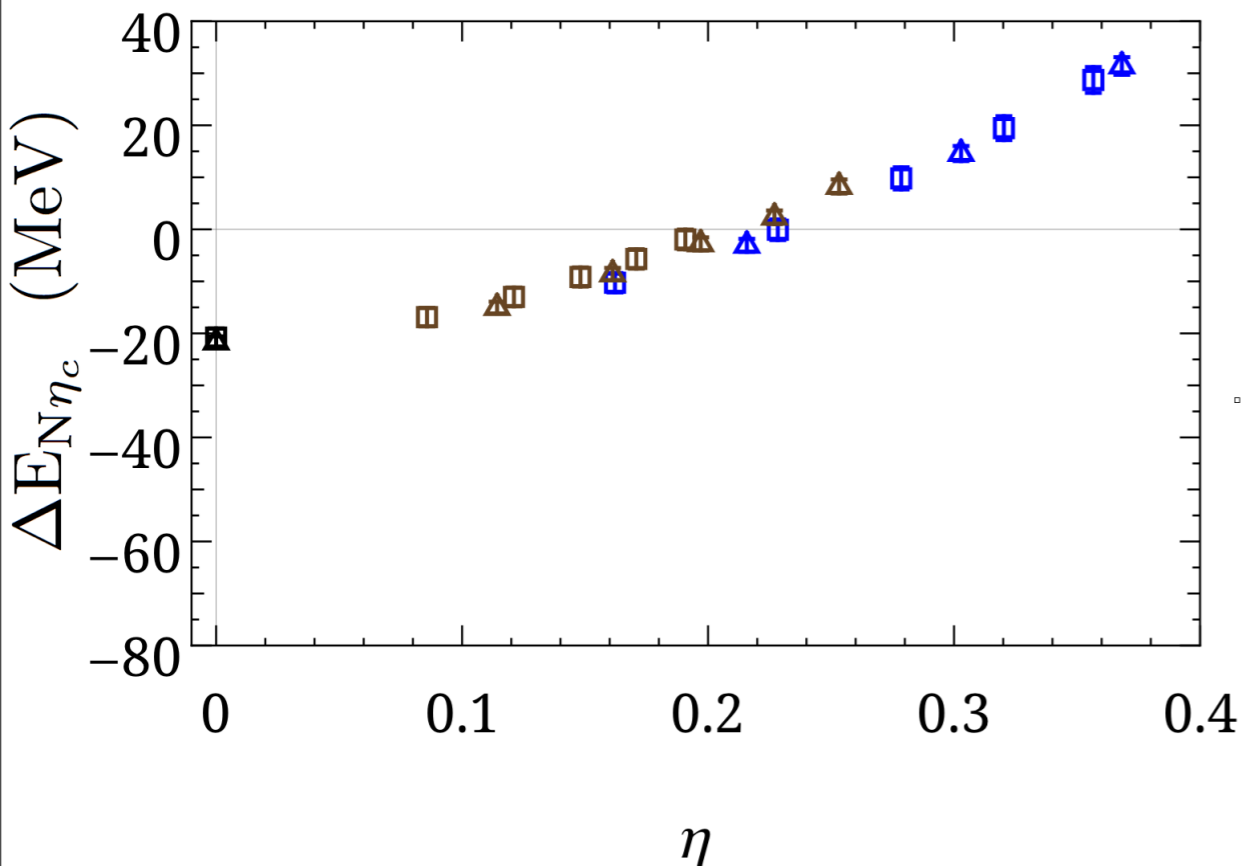
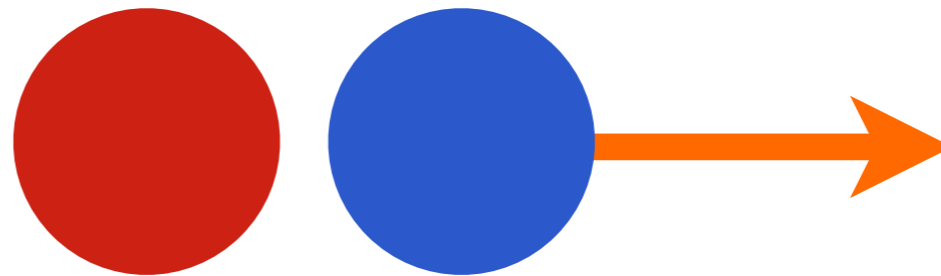
Charmonium-Nuclei Extrapolation to Nature



- Leading Gluonic Matrix Element $\sim M_N$
 - $B \sim 60 \text{ MeV}$ @ $m_\pi = 800 \text{ MeV}$ extrapolates to $B \sim 40 \text{ MeV}$ @ $m_\pi = 140 \text{ MeV}$
- Calculations at lighter masses underway

Charmonium-Nuclei Boosted Systems and Sources

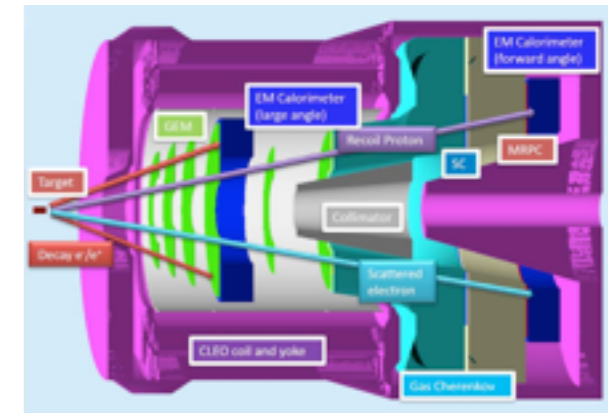
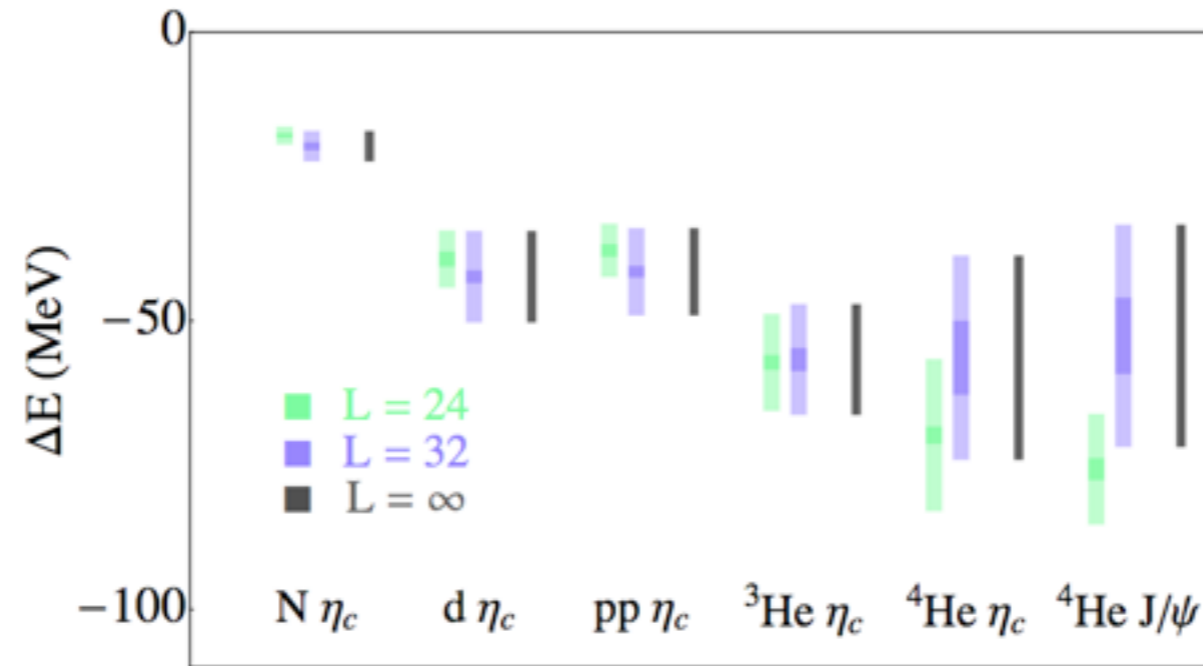
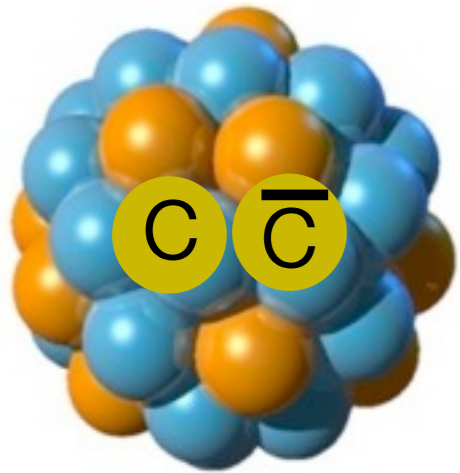
Boosted src structure
- one hadron is boosted



● Spectrum

- BS suppressed at higher relative P
- Continuum is independent of relative P
- Continuum contamination unresolved !

Summary



First calculations from Lattice QCD - multi-volume but one lattice spacing

Binding consistent with realistic hadronic models

Next generation LQCD will be higher precision and closer to physical quark masses

[Aside : Gluonic operators impact Techni-baryon Dark Matter signals]

END
