

# High-resolution spectroscopy of light hypernuclei with the decay-pion spectroscopy

Run Group Addition E12-20-013A/E12-15-008A

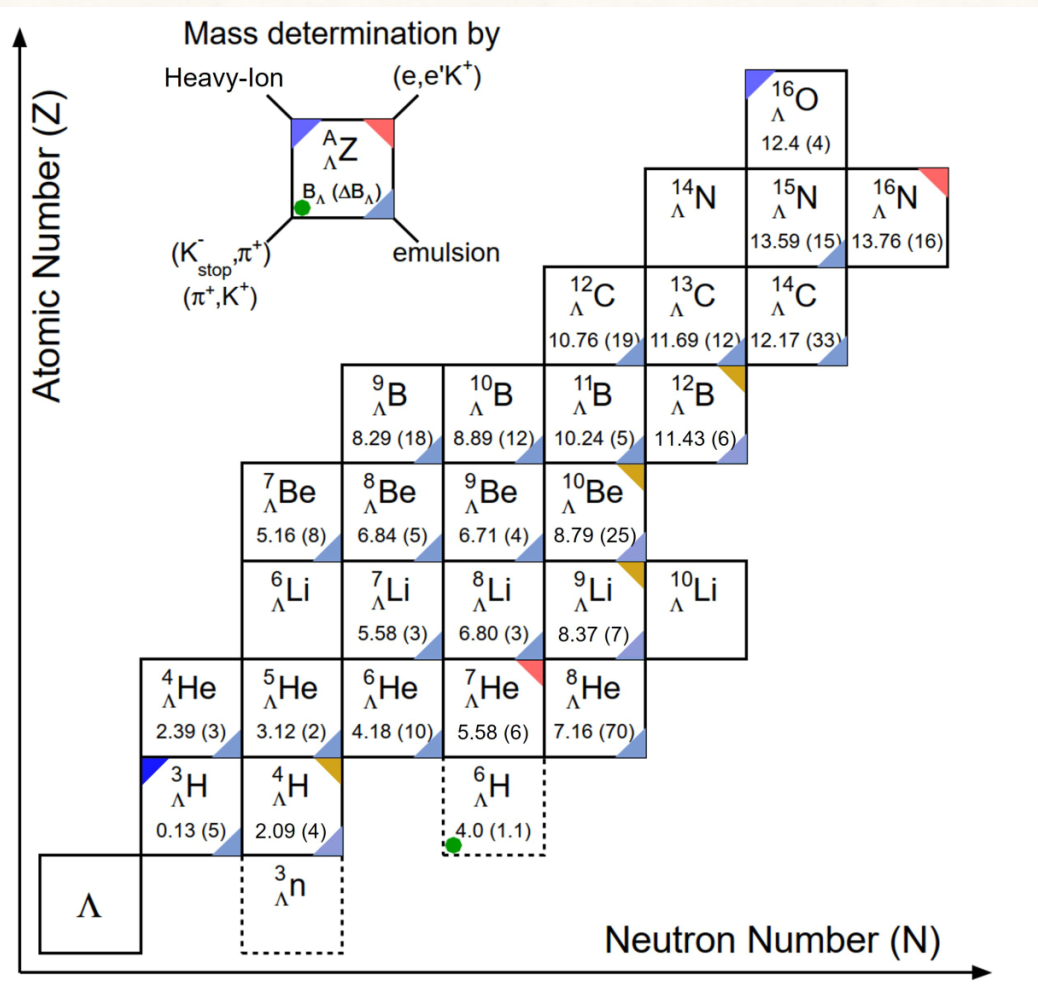
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on behalf of JLab hypernuclear collaboration

July 11, 2024

# Hypernuclear $\Lambda$ binding energies

## Hypernuclear Chart (up to p-shell)



## Precise Measurement of $\Lambda$ Binding Energy

Study of NN and BB interaction

$$B_\Lambda = M_{\text{core}} + M_\Lambda - M_{\text{HYP}}$$

*Core*
*Λ*
*Hypernucleus*  
*Mass*
*Mass*
*Mass*

### Good probe investigating $\Lambda\text{N}$ interaction

Mass, Isospin dependence etc...

Light hypernuclei as useful probes thanks to precise calculations.

### Precise $B_\Lambda(g.s \ \& \ e.x)$ with the $(e,e'K^+)$ experiment

Missing mass spectroscopy of

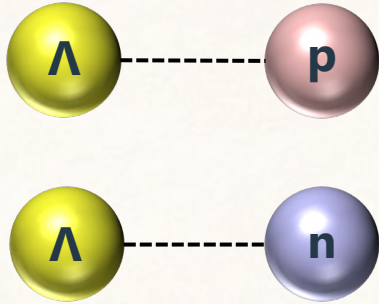
${}^{40,48}_\Lambda\text{K}$ ,  ${}^{208}_\Lambda\text{Pb}$   
 (E12-15-008 / E12-20-013)  
 (PR12-24-013 / PR12-24-003)

${}^6_\Lambda\text{He}$ ,  ${}^9_\Lambda\text{Li}$ ,  ${}^{11}_\Lambda\text{Be}$ ,  ${}^{12}_\Lambda\text{C}$ ,  ${}^{27}_\Lambda\text{Mg}$   
 (PR12-24-004 / PR12-24-011)

NOTE:  $B_\Lambda$  from hypernuclei database [<https://hypernuclei.kph.uni-mainz.de/>]

# High precision data provide

## Key information of $\Lambda N$ CSB effect

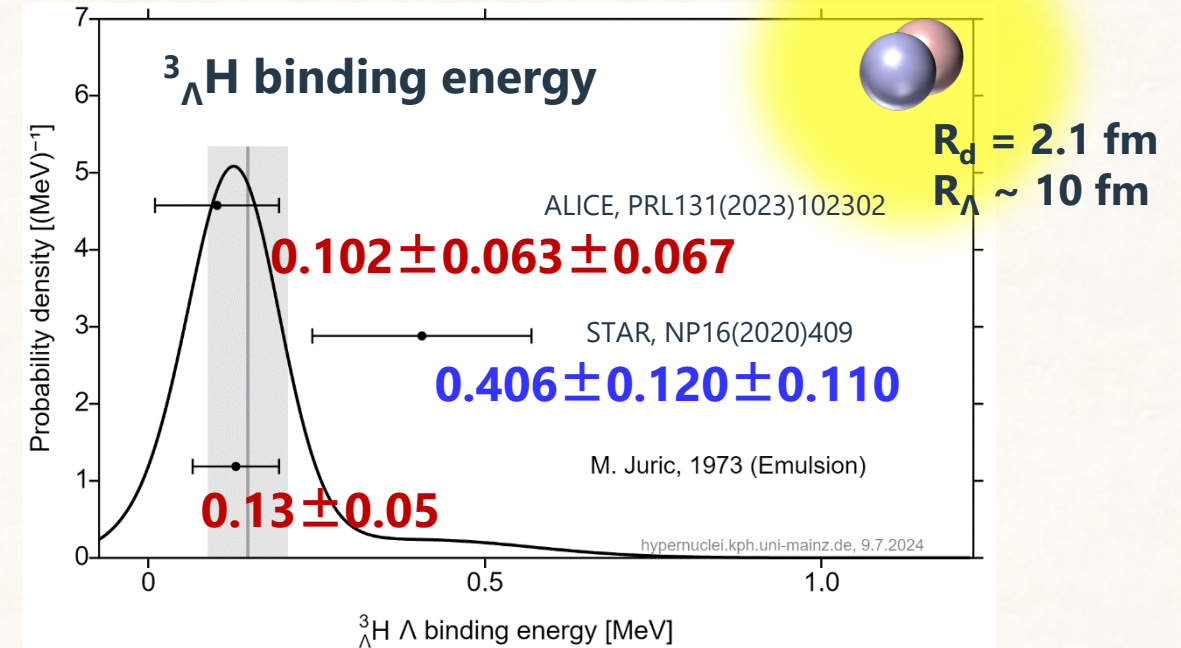


**Larger difference  
than  $pp$  &  $nn$**

Hypernuclides	$\Delta B_\Lambda$ (Exp) (keV)	Hiyama [PTP128(2012)105] [PLB744(2015)352]	Gal [PLB744(2015)352]	NLO13 [PRC107(2023)024002] [FBsyst.672(2021)105]	NLO19 [PRC107(2023)024002] [FBsyst.672(2021)105]
${}^4_\Lambda\text{He} - {}^4_\Lambda\text{H}$	$300 \pm 60$		226	252(43)	238(10)
${}^7_\Lambda\text{Li}^* - {}^7_\Lambda\text{He}$	$-320 \pm 140$	130(-60)	-17	-31(-5)	-16(-17)
${}^8_\Lambda\text{Be} - {}^8_\Lambda\text{Li}$	$40 \pm 80$		49	178(16)	146(-6)
${}^9_\Lambda\text{B} - {}^9_\Lambda\text{Li}$	$-160 \pm 210$		-54		
${}^{10}_\Lambda\text{B} - {}^{10}_\Lambda\text{Be}$	$100 \pm 300$	20(-180)	-136		
${}^{11}_\Lambda\text{B}^* - {}^{11}_\Lambda\text{Be}$	N/A				

- Large symmetry breaking of  $\Lambda p$ - $\Lambda n$
- Under discussion of its origin ( $\Sigma$  mixing?)
- Necessity of systematic studies

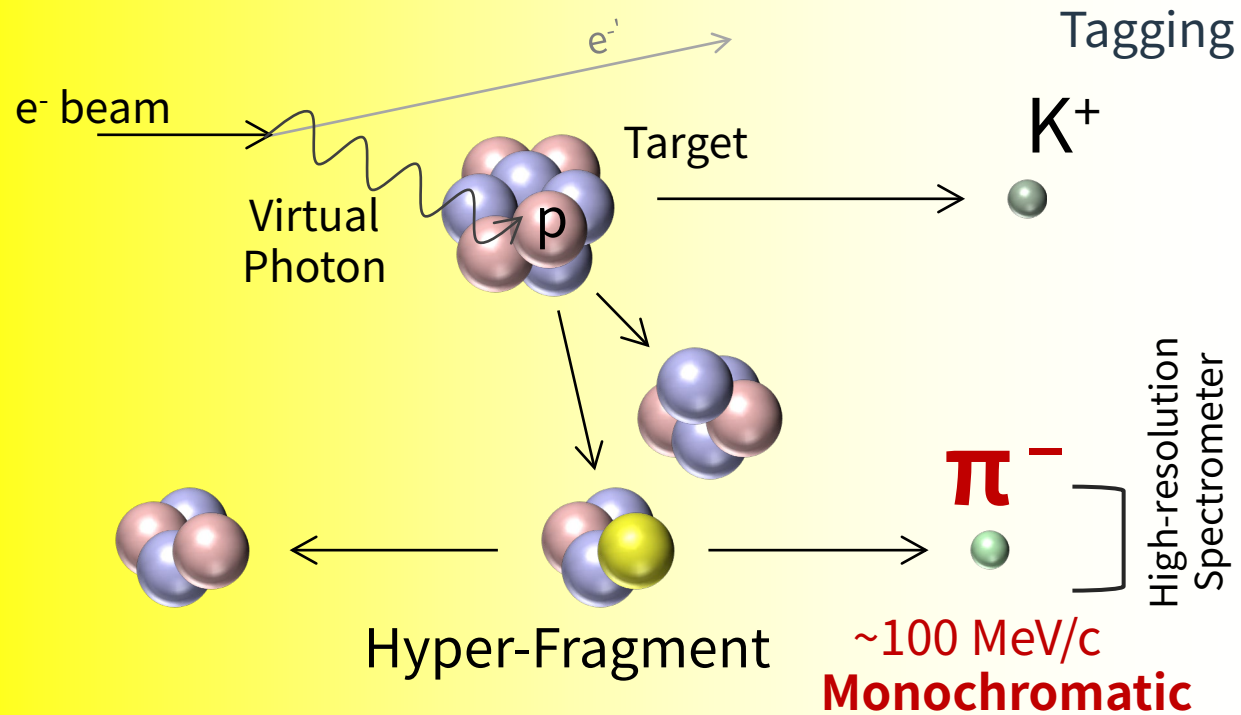
## Resolving the hypertriton puzzle



- Weakly  $\Lambda$  bound system in deuteron
- Deep/Shallow  $B_\Lambda$  and Long/Short life ??
- Most important input

# Decay Pion Spectroscopy (DPS)

## High-resolution, High-precision mass spectroscopy



$$M({}_{\Lambda}^AZ) = \sqrt{M({}^A(Z+1))^2 + p_{\pi}^2} + \sqrt{M_{\pi}^2 + p_{\pi}^2}$$

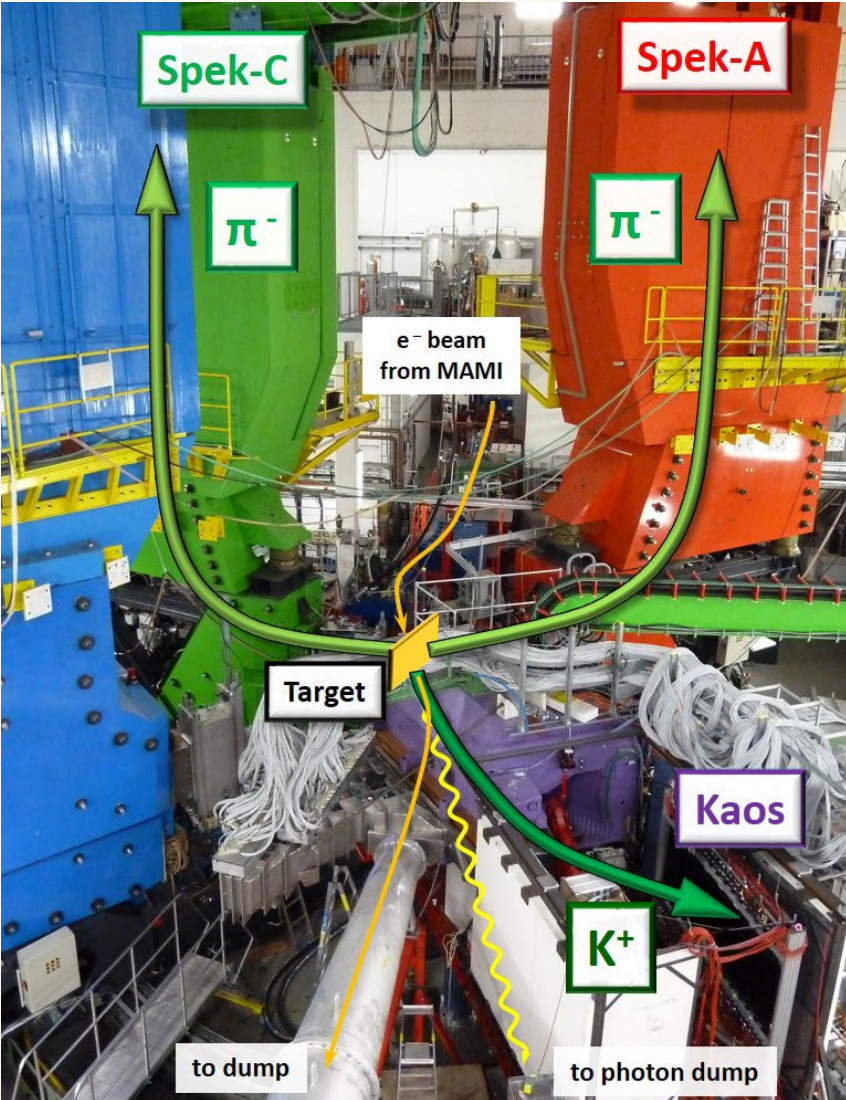
No effect from Beam energy spreading, stability etc.

### Principle

- Measurement of **monochromatic decay pion**
  - from hypernuclei **stopped** in the target
  - emitting pion in **two-body decay**  
(e.g.  ${}_{\Lambda}^4\text{H} \rightarrow {}^4\text{He} + \pi^-$ )
  - $B_{\Lambda}$  must be approximately known  
(hypernuclear ID is performed by the pion momentum)
- **Tagging  $K^+$**  for background suppression from non-strangeness production

# Previous Experiment at MAMI

## Proof of Principle at MAMI

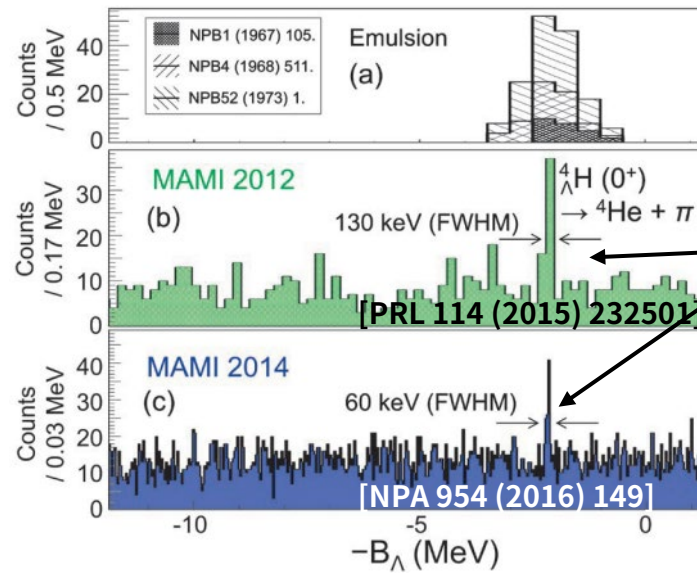


## Experimental Feasibility

**5 keV (stat.) & 77 keV (syst.) at MAMI exp.**

PRL 114 (2015) 232501  
 NPA 954 (2016) 149]

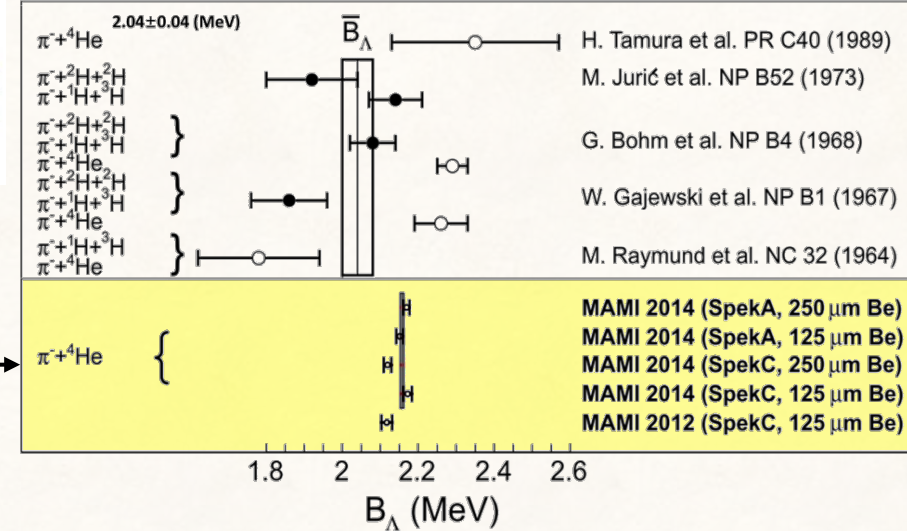
$^4_\Lambda\text{H}$  Spectrum



$^4_\Lambda\text{H}$  peak by Emulsion

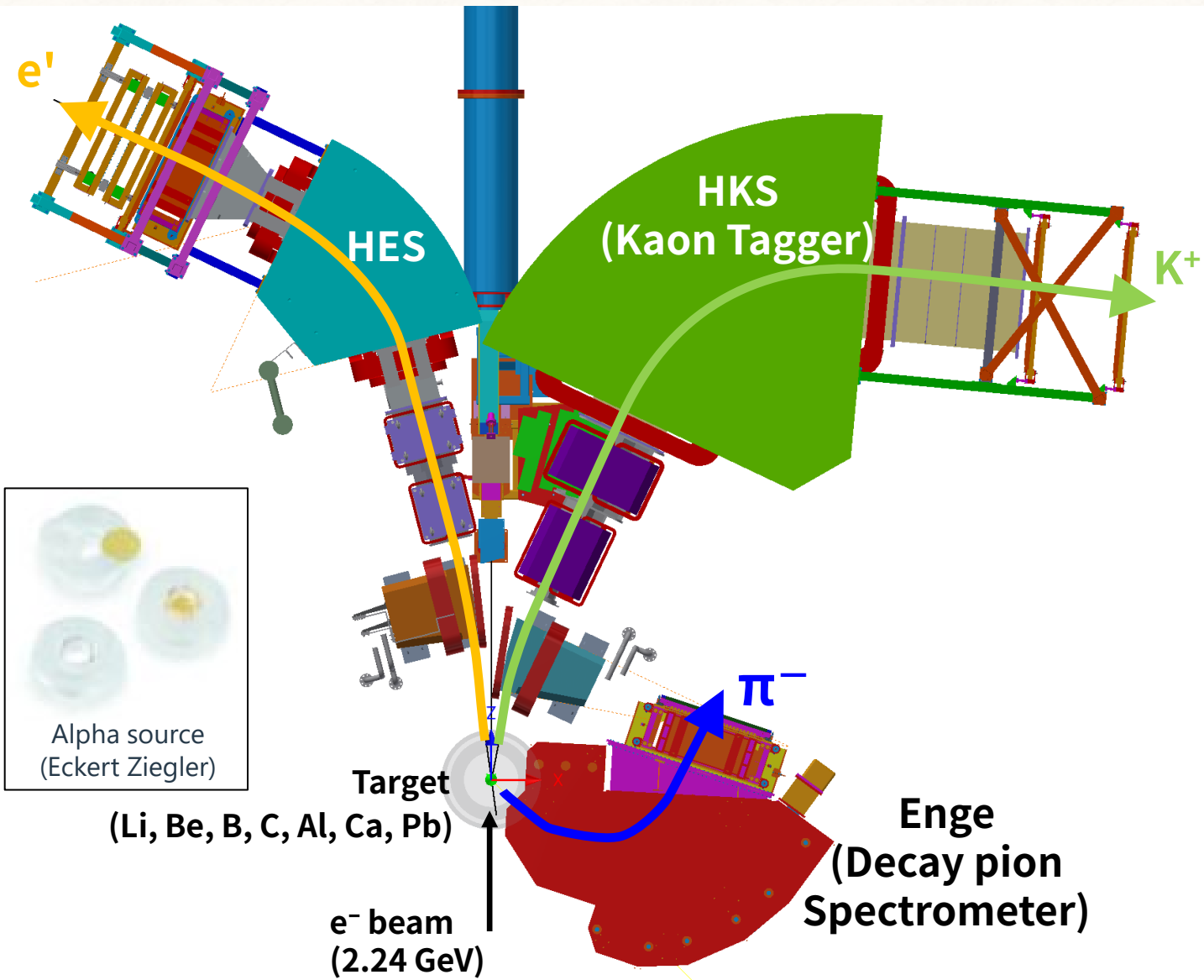
DPS at MAMI w/  $^9\text{Be}$  foil

Word Data of  $^4_\Lambda\text{H}$   $B_\Lambda$



MAMI results

# Proposed experiment



## Setup

- **Parallel exp.** with proposed  $(e,e'K^+)$  exp.
- "Enge" for decay pion measurement
- "HKS" for  $K^+$  tagger
- " $K^+$  &  $\pi^-$ " **coin. exp.** with HKS and Enge

## Advantage

- **30 times yield** per time thanks to higher CEBAF beam
- Background less thanks to better KID
- Another data **without additional beamtime**

## Others

- Compatible setup with the  $(e,e'K^+)$  target ladder for Enge@150deg.
- Possible installation plan by the engineering group
- Low radiation level & a few 10 kHz single rate
- Mixed nuclides (Eckert & Ziegler) through RadCon
- Calibration **w/o beams** (~10 keV systematic)

# Expectation

$$N_{HYP} = N_{\Lambda} R_{F.P} R_{stop} \Gamma_{\pi^-} \Delta\Omega_{\pi^-} \varepsilon_{\pi^-}^{decay} \varepsilon_{\pi^-}^{det}$$

**× 30**

AMD calc.

[Y.Nara, PLB346(1995)217.]

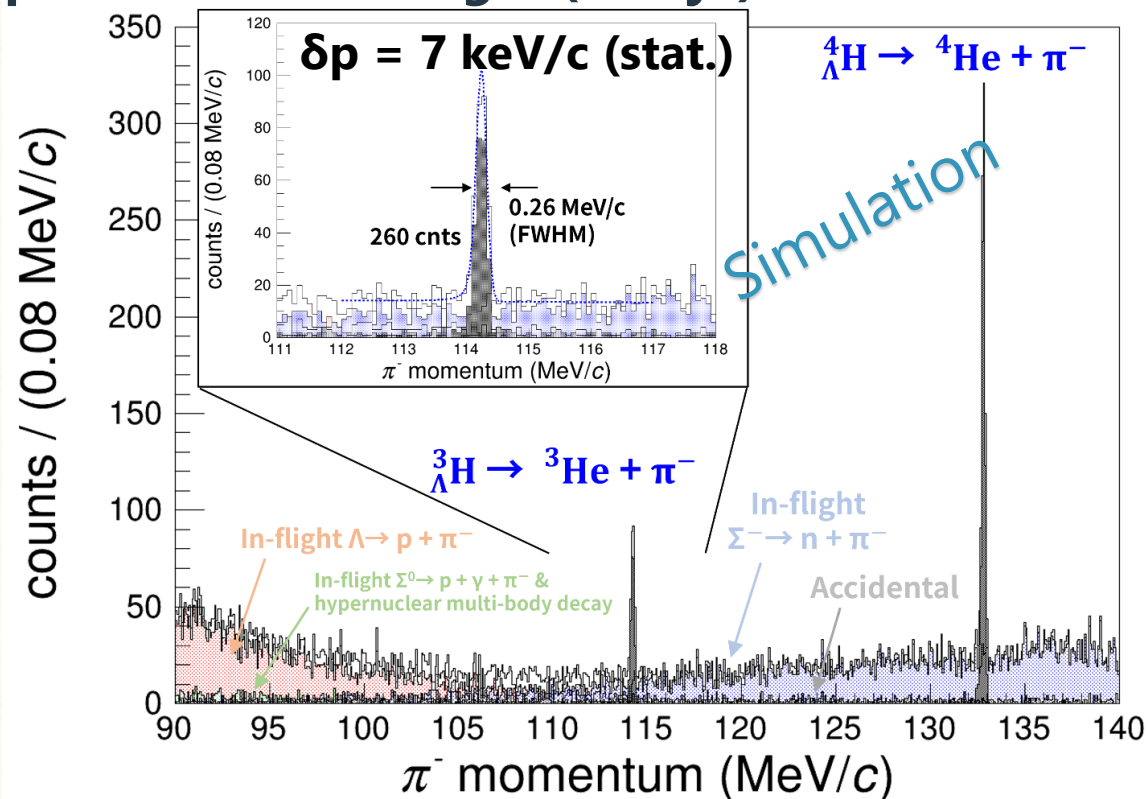
[A.Kawachi, Dthesis, U-Tokyo(1997)]

shell-model calc.

[T.Motoba, PTPS 117(1994)477]

Monte-Carlo

## Expected with ${}^6\text{Li}$ target (5 days)



- Low background from  $\Lambda/\Sigma$  & in-flight, multi-body hypernuclei
- Low accidental
- Clear peak from  ${}_{\Lambda}\text{H}$
- **$\delta B_{\Lambda} = 5 \text{ keV (stat.)}$**
- Pion from p-shell hypernuclei with  ${}^9\text{Be}$ ,  ${}^{12}\text{C}$  target

NOTE:  $\delta p \sim \sigma / \sqrt{N} = 0.26/2.35 / \sqrt{260} \sim 0.007 \text{ MeV/c}$

# Summary

## *Physics Motivation and Goals*

$\Lambda$ N interaction properties and hypernuclear structure have been discussed with the  $\Lambda$  binding energies of variety of hypernuclei.

**Hypertriton puzzle,  $\Lambda$ N Charge Symmetry Breaking, and  $\Sigma$  mixing effect** hypernuclear medium have been discussed, and are still open question.

**Precise measurements** of the  $\Lambda$  binding energies will resolve these problems.

The decay pion spectroscopy is possible to measure the  $B_\Lambda$  on **more various hypernuclei** via the fragmentation accurately.

## *Proposing Decay Pion Spectroscopy*

Pion momentum measurement in Enge together with  $K^+$  tagging in HKS will find peaks of **monochromatic two-body decay pions** from hyperfragments.

Targets, beamtime, and data taking will be shared with the  $(e,e'K^+)$  experiments.

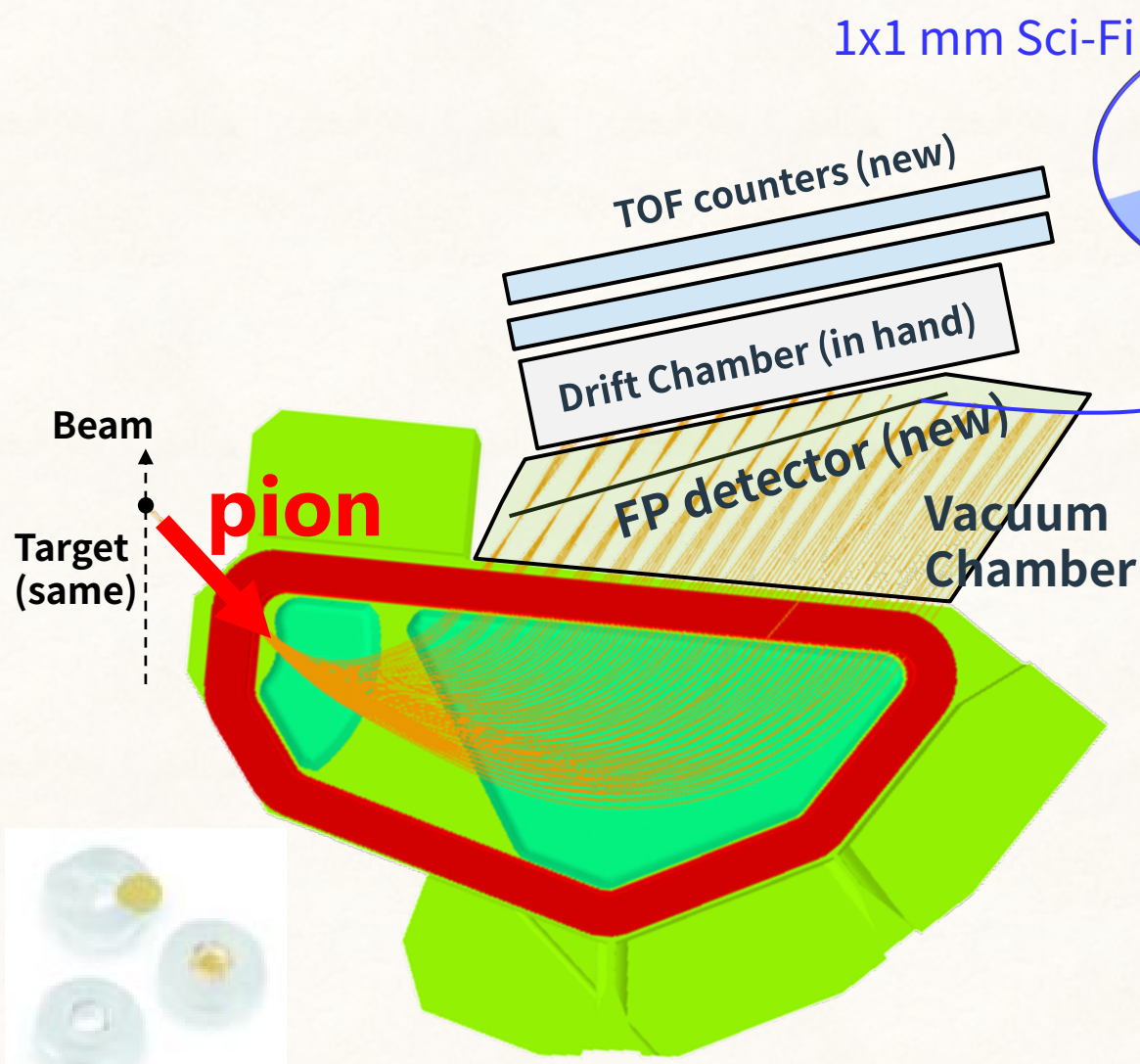
Once we successfully find a decay pion peak and identify the parent hypernucleus, new  $B_\Lambda$  determination will be possible with an **accuracy of  $\sim 10$  keV**.

**This excellent measurement will renovate the hypernuclear data from the 1960s.**



# Backup

# Pion Spectrometer "Enge"



## Hardware spectrometer Enge

- Particle momentum from Focal Plane position  
60 keV / mm Dispersion  
FP Position detector (Scinti+SiPM) in vacuum  
Full Mom. coverage from decay pions (70 ~150 MeV/c)
- Drift Chamber (spare KDC) for reconstruction to the target
- Timing & Trigger detector
- Low radiation level & a few 10 kHz single rate

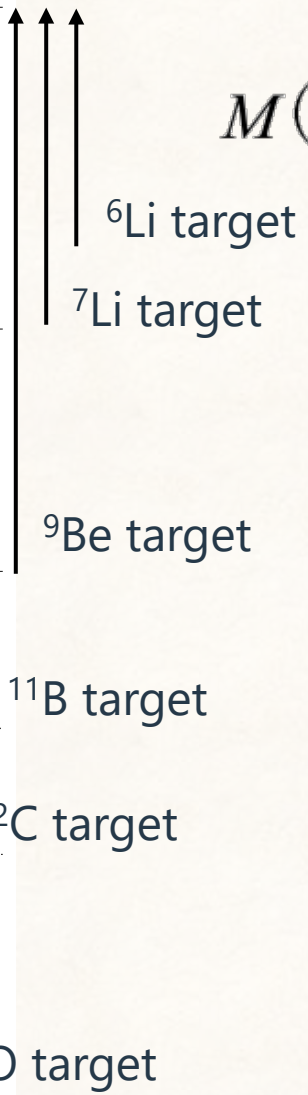
## Calibration with $\alpha$ -sources

- Mixed nuclides from Eckert & Ziegler through RadCon
- Possible calibration **without beams** (~10 keV systematic)

Alpha source PM-Type  
(Eckert & Ziegler)

# Possible hypernuclei & Decay pion momenta (up to A=16)

Hypernuclei	Decay mode	$p_{\pi^-}$ (MeV/c)	comments
${}^3_{\Lambda}\text{H}$	${}^3\text{He} + \pi^-$	114.37	
${}^4_{\Lambda}\text{H}$	${}^4\text{He} + \pi^-$	133.03	
<del><math>{}^4_{\Lambda}\text{He}</math></del>	<del><math>{}^4\text{Li} + \pi^-</math></del>	<del>98.17</del>	Impossible 2-body decay
<del><math>{}^5_{\Lambda}\text{He}</math></del>	<del><math>{}^5\text{Li} + \pi^-</math></del>	<del>99.26</del>	Impossible 2-body decay
${}^6_{\Lambda}\text{H}$	${}^6\text{He} + \pi^-$	135.27	
${}^6_{\Lambda}\text{He}$	${}^6\text{Li} + \pi^-$	108.48	
<del><math>{}^6_{\Lambda}\text{Li}</math></del>	<del><math>{}^6\text{Be} + \pi^-</math></del>	-	No $B_{\Lambda}$ data, above Sp
${}^7_{\Lambda}\text{He}$	${}^7\text{Li} + \pi^-$	115.10	
${}^7_{\Lambda}\text{Li}$	${}^7\text{Be} + \pi^-$	108.11	
<del><math>{}^7_{\Lambda}\text{Be}</math></del>	<del><math>{}^7\text{C} + \pi^-</math></del>	<del>95.90</del>	Impossible 2-body decay
${}^8_{\Lambda}\text{He}$	${}^8\text{Li} + \pi^-$	116.47	
${}^8_{\Lambda}\text{Li}$	${}^8\text{Be} + \pi^-$	124.20	
${}^8_{\Lambda}\text{Be}$	${}^8\text{B} + \pi^-$	97.19	No ${}^8\text{B}(\text{g.s.})$ decay
${}^9_{\Lambda}\text{Li}$	${}^9\text{Be} + \pi^-$	121.31	
${}^9_{\Lambda}\text{Be}$	${}^9\text{B} + \pi^-$	96.98	
${}^9_{\Lambda}\text{B}$	${}^9\text{C} + \pi^-$	96.82	
${}^{10}_{\Lambda}\text{Li}$	${}^{10}\text{Be} + \pi^-$	-	No $B_{\Lambda}$ data
${}^{10}_{\Lambda}\text{Be}$	${}^{10}\text{B} + \pi^-$	104.41	
${}^{10}_{\Lambda}\text{B}$	${}^{10}\text{C} + \pi^-$	100.49	
${}^{11}_{\Lambda}\text{B}$	${}^{11}\text{C} + \pi^-$	86.54	
${}^{12}_{\Lambda}\text{B}$	${}^{12}\text{C} + \pi^-$	115.87	
${}^{12}_{\Lambda}\text{C}$	${}^{12}\text{N} + \pi^-$	91.48	No ${}^{12}\text{N}(\text{g.s.})$ decay
${}^{13}_{\Lambda}\text{C}$	${}^{13}\text{N} + \pi^-$	92.27	
${}^{14}_{\Lambda}\text{C}$	${}^{14}\text{N} + \pi^-$	101.20	
${}^{14}_{\Lambda}\text{N}$	${}^{14}\text{O} + \pi^-$	-	No $B_{\Lambda}$ data
${}^{15}_{\Lambda}\text{N}$	${}^{15}\text{O} + \pi^-$	98.40	
${}^{16}_{\Lambda}\text{N}$	${}^{16}\text{O} + \pi^-$	106.23	
${}^{16}_{\Lambda}\text{O}$	${}^{16}\text{F} + \pi^-$	86.54	



$$M({}^A_{\Lambda}Z) = \sqrt{M({}^A(Z+1))^2 + p_{\pi}^2} + \sqrt{M_{\pi}^2 + p_{\pi}^2}$$

Example,  ${}^4_{\Lambda}\text{H} \rightarrow {}^4\text{He} + \pi^-$

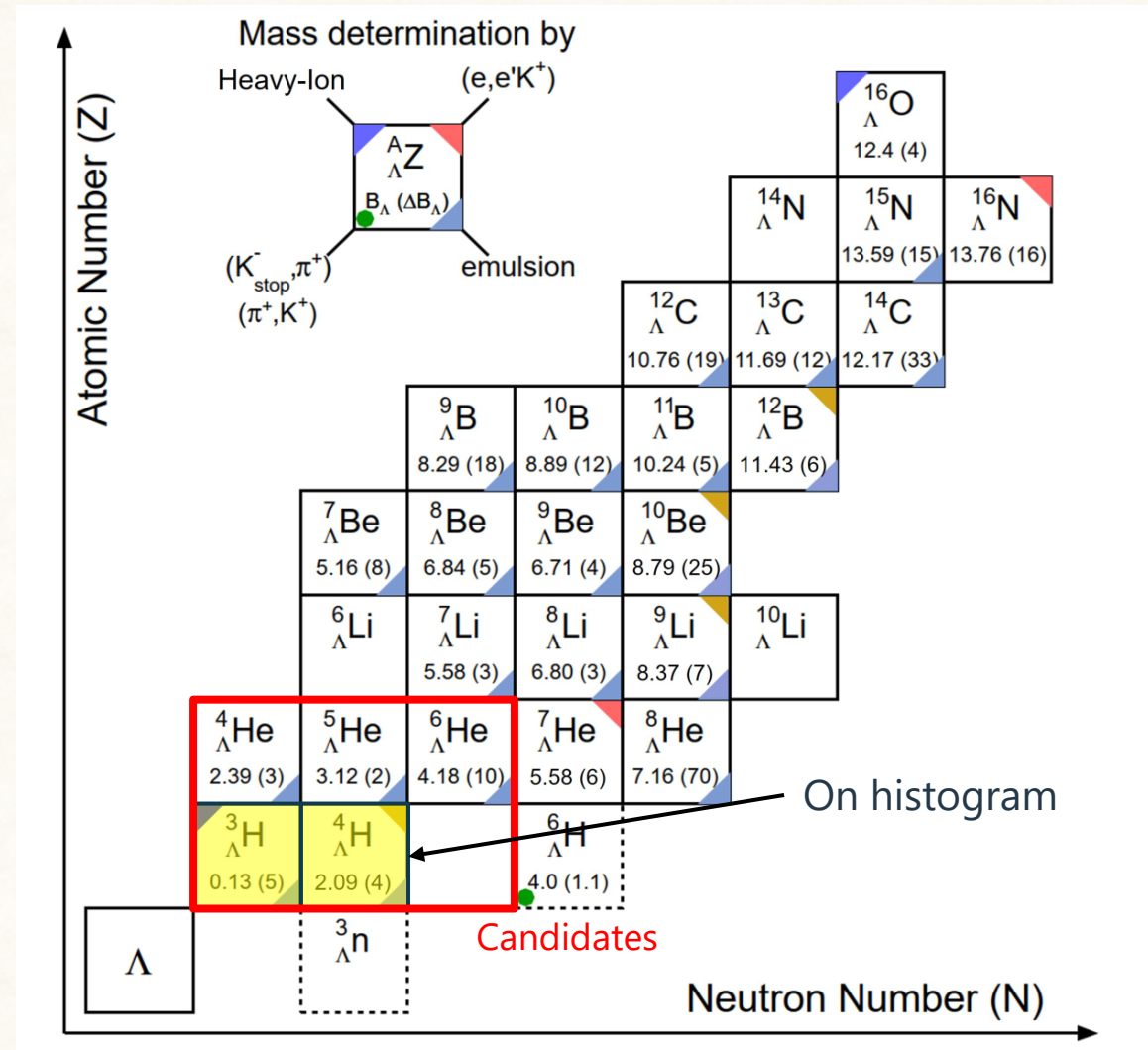
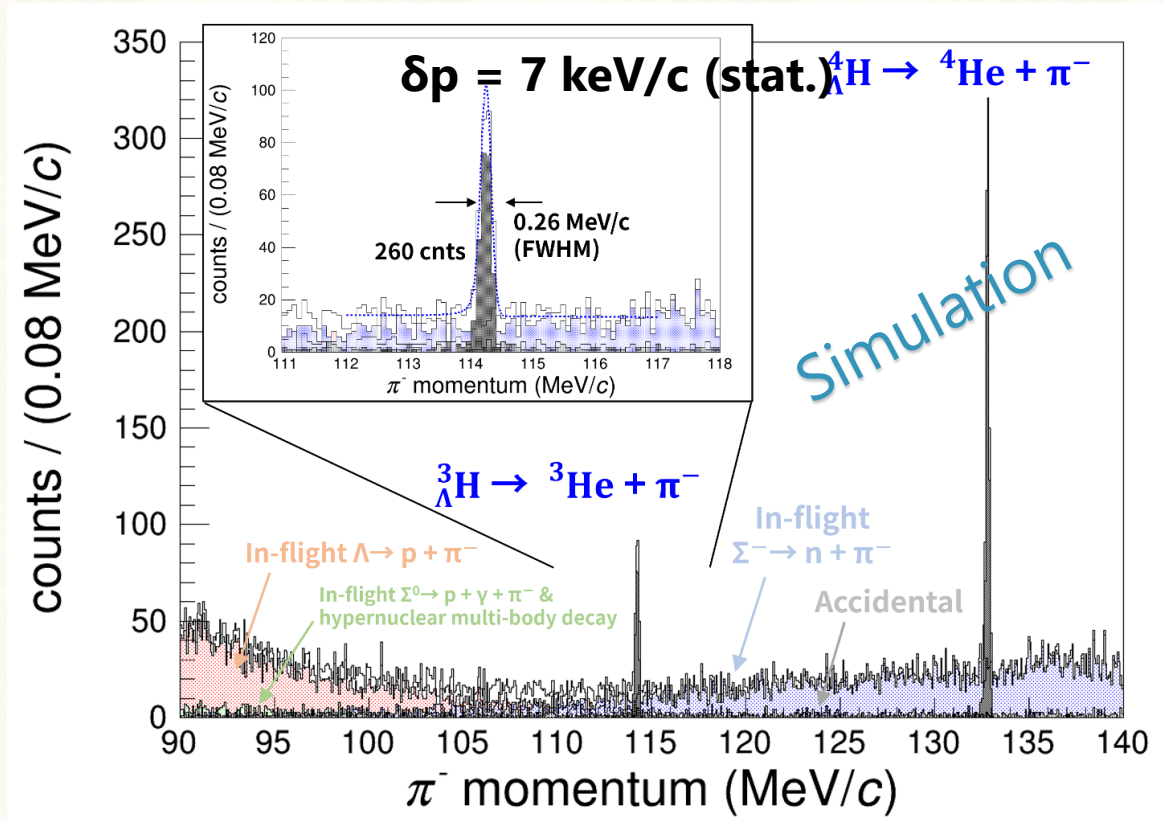
$$M(\alpha) = 3727.3794118(11) \text{ MeV}/c^2$$

$$M(\pi) = 139.57039(18) \text{ MeV}/c^2$$

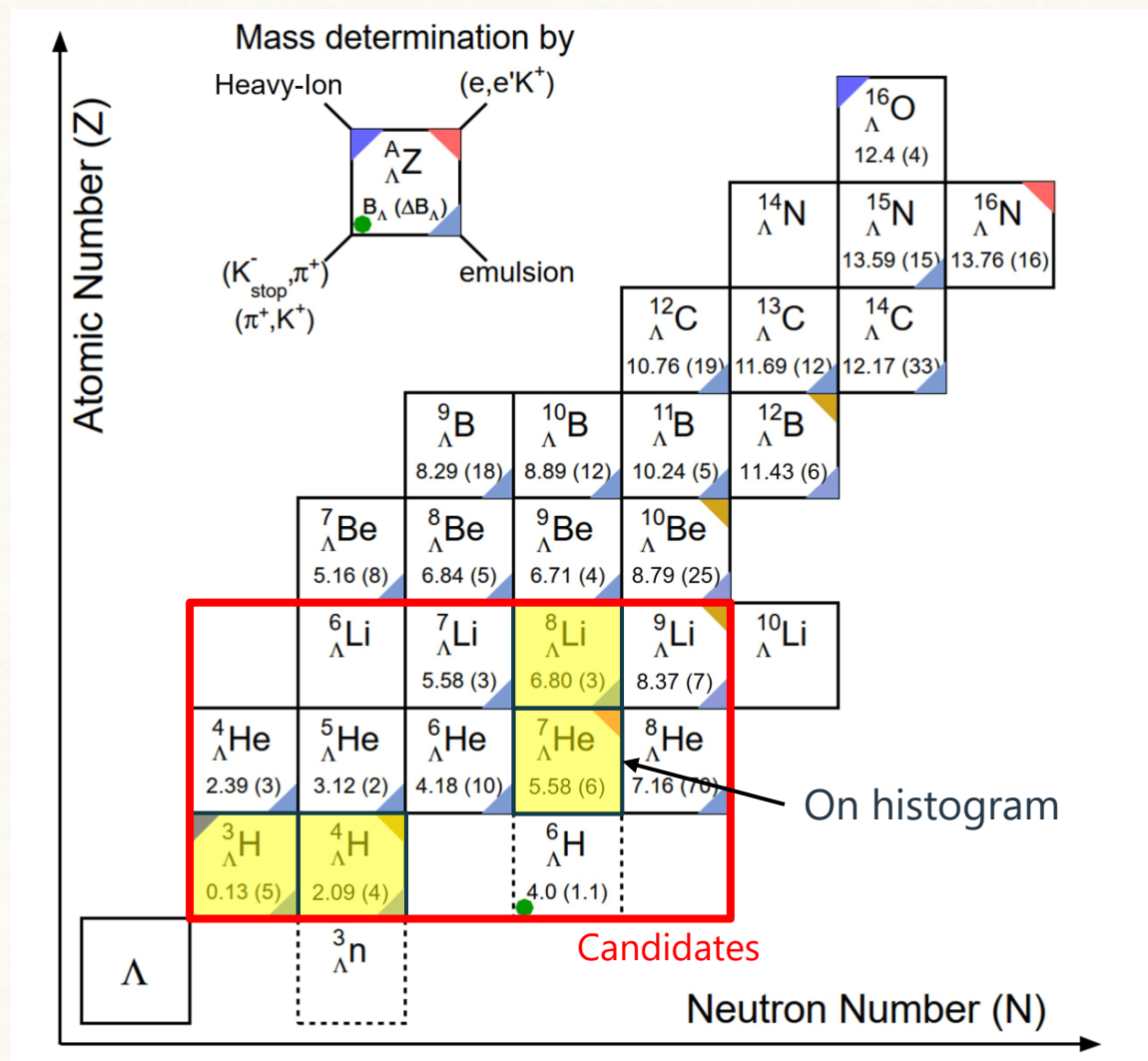
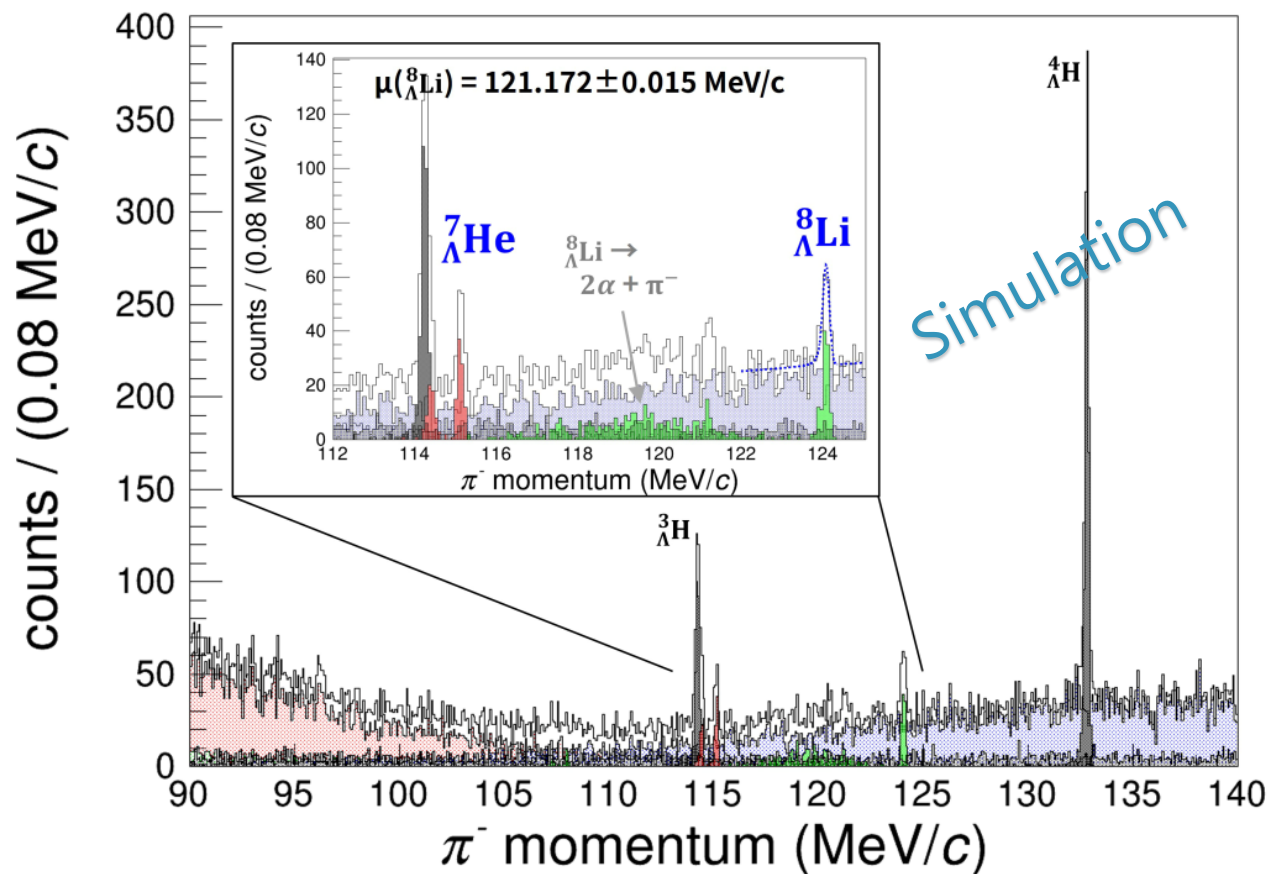
$$M({}^4_{\Lambda}\text{H}) = 3922.56(4) \text{ MeV}/c^2$$

$$p(\pi) = 133.03(6) \text{ MeV}/c$$

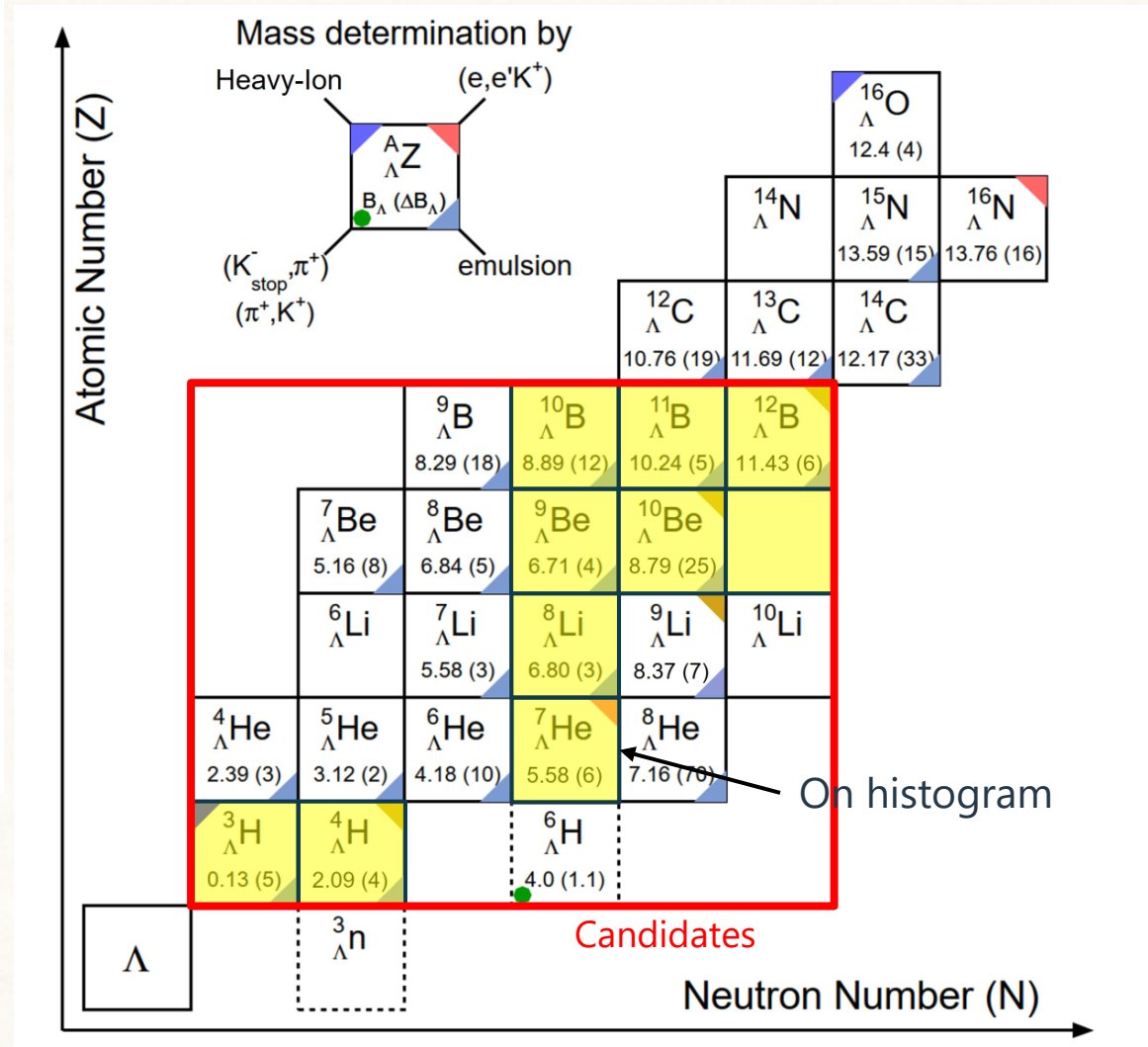
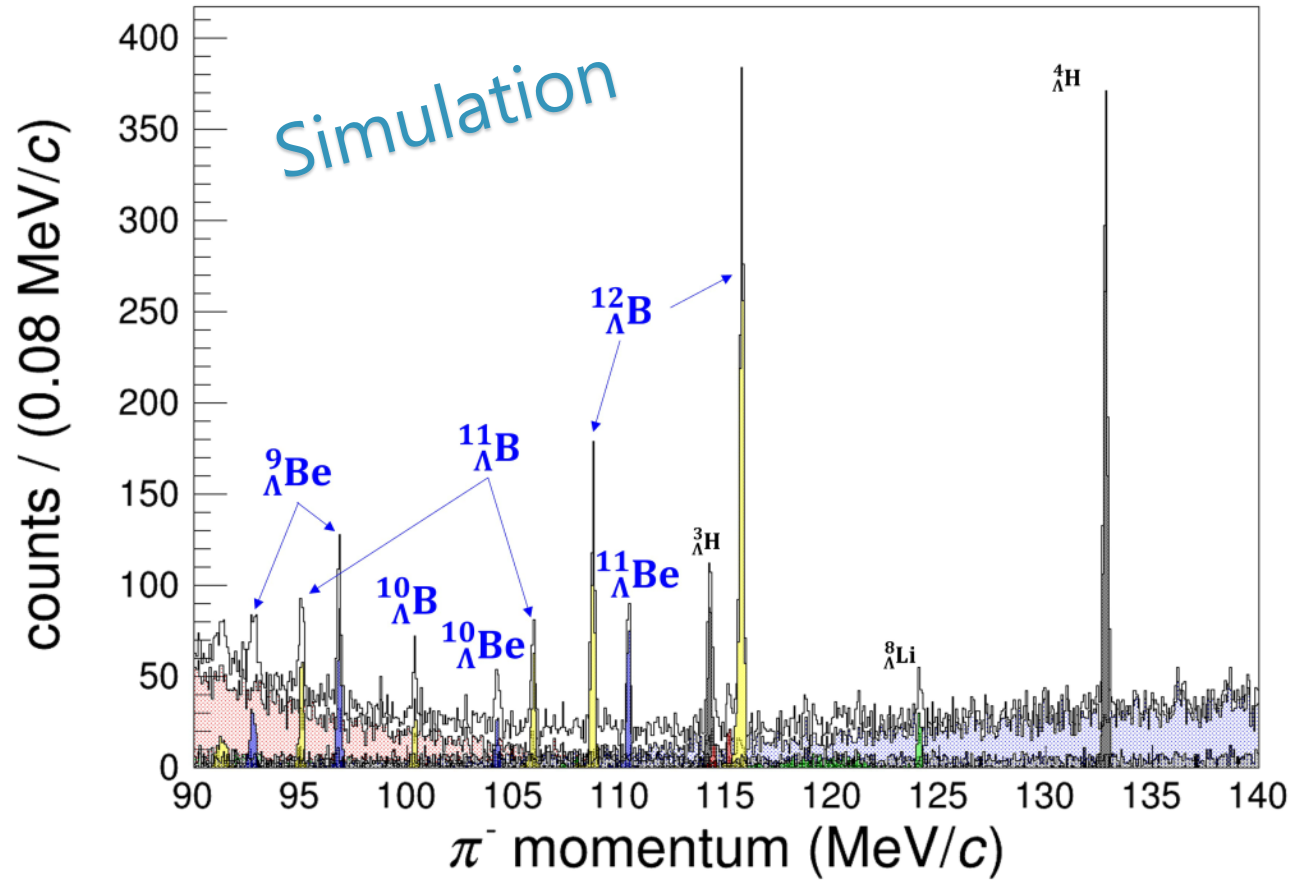
# Expectation ( ${}^7\text{Li}$ target)



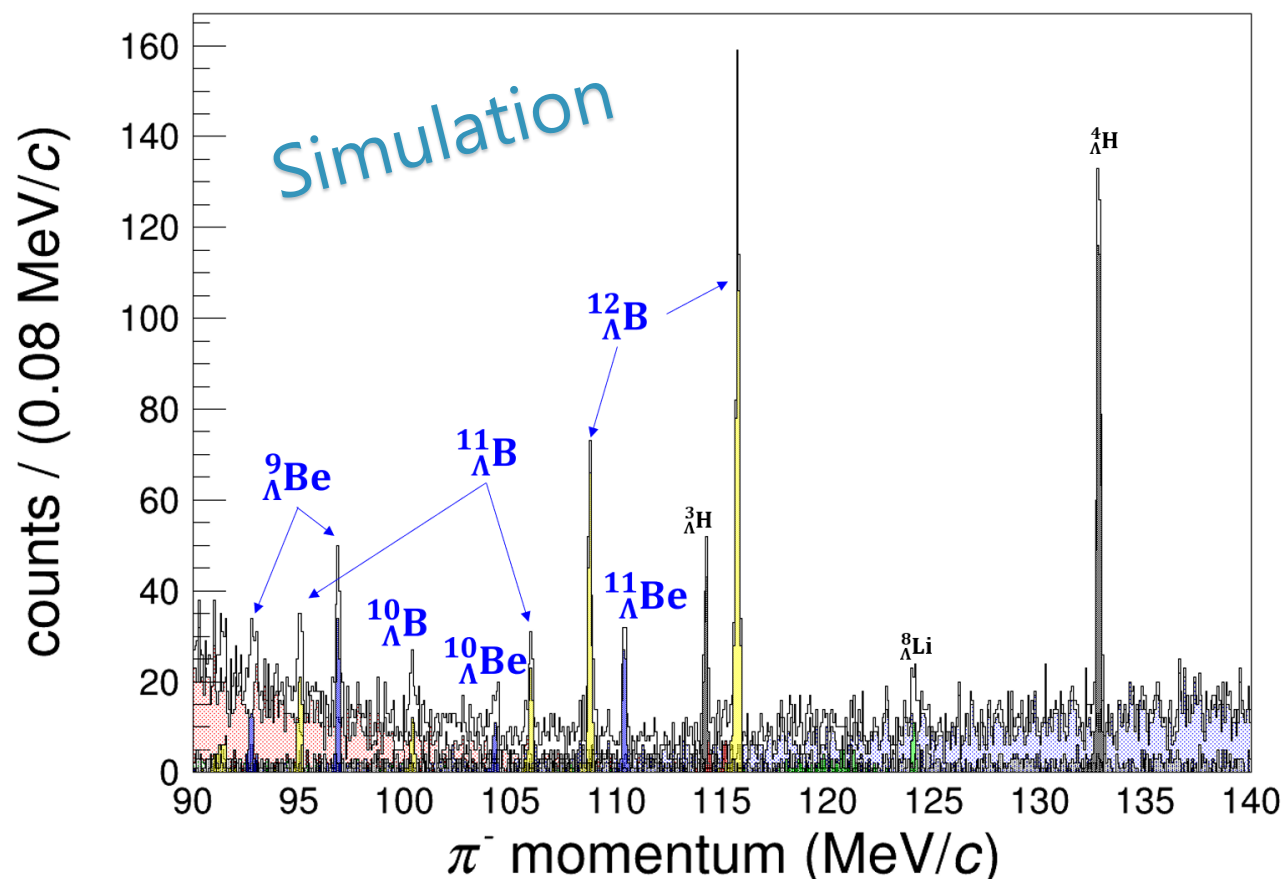
# Expectation ( ${}^9\text{Be}$ target)



# Expectation ( $^{12}\text{C}$ target)

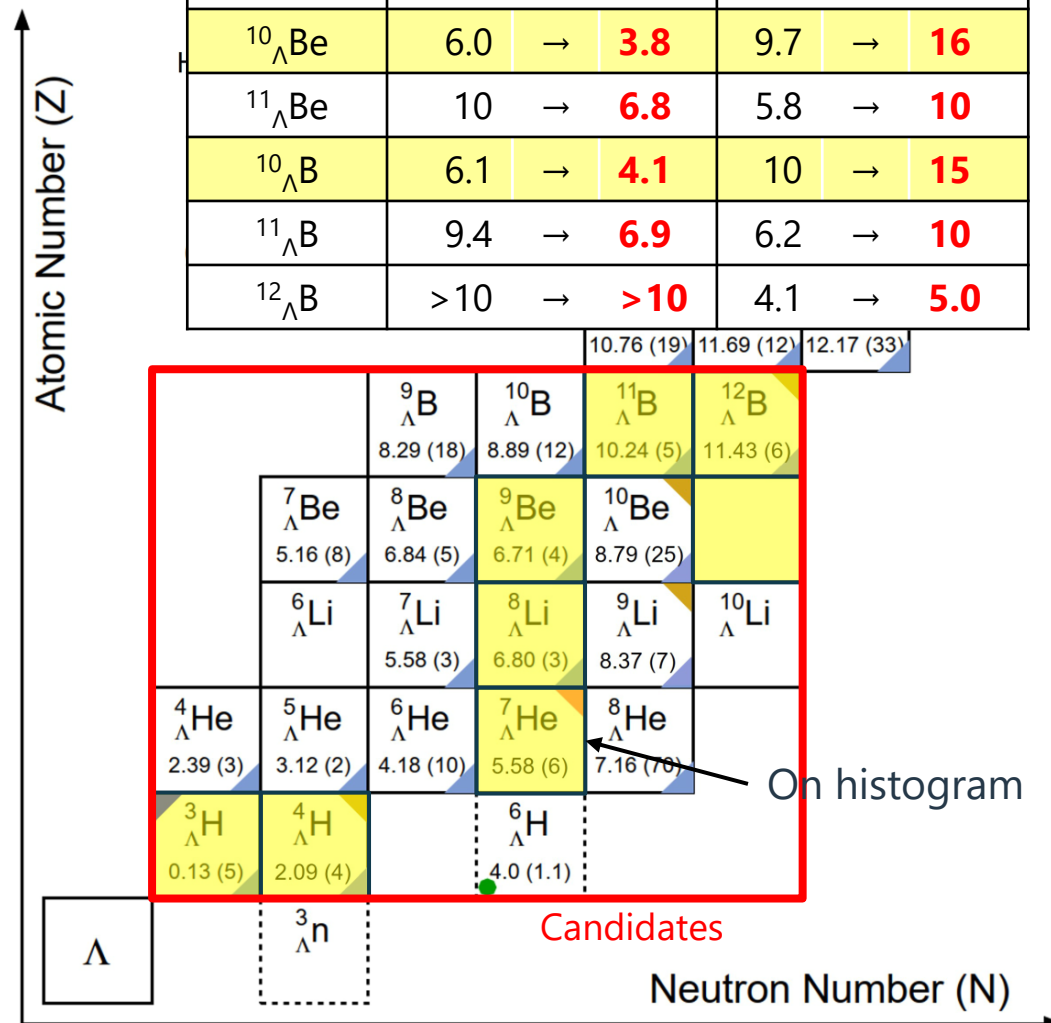


# Expected ( $^{12}\text{C}$ target, no-add beamtime)

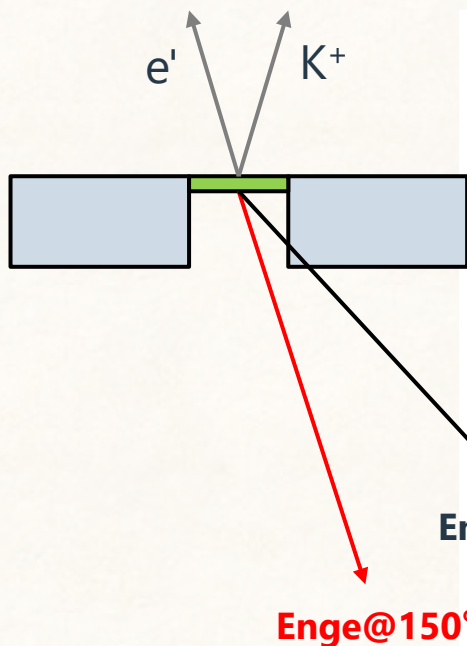


- Not enough statistics for A=10 hypernuclei
- No beam raster data on  $^{12}\text{C}$  for the  $^6\text{Li}$  run
- No thinner  $^{12}\text{C}$  runs for dE correction

Nuclides	Significance ( $\sigma$ )	Precision (keV)
$^3_\Lambda\text{H}$	>10 → <b>8.4</b>	4.9 → <b>8.2</b>
$^4_\Lambda\text{H}$	>10 → <b>&gt;10</b>	5.3 → <b>5.2</b>
$^9_\Lambda\text{Be}$	10 → <b>7.3</b>	5.2 → <b>9.1</b>
$^{10}_\Lambda\text{Be}$	6.0 → <b>3.8</b>	9.7 → <b>16</b>
$^{11}_\Lambda\text{Be}$	10 → <b>6.8</b>	5.8 → <b>10</b>
$^{10}_\Lambda\text{B}$	6.1 → <b>4.1</b>	10 → <b>15</b>
$^{11}_\Lambda\text{B}$	9.4 → <b>6.9</b>	6.2 → <b>10</b>
$^{12}_\Lambda\text{B}$	>10 → <b>&gt;10</b>	4.1 → <b>5.0</b>



# Target & Enge Geometry

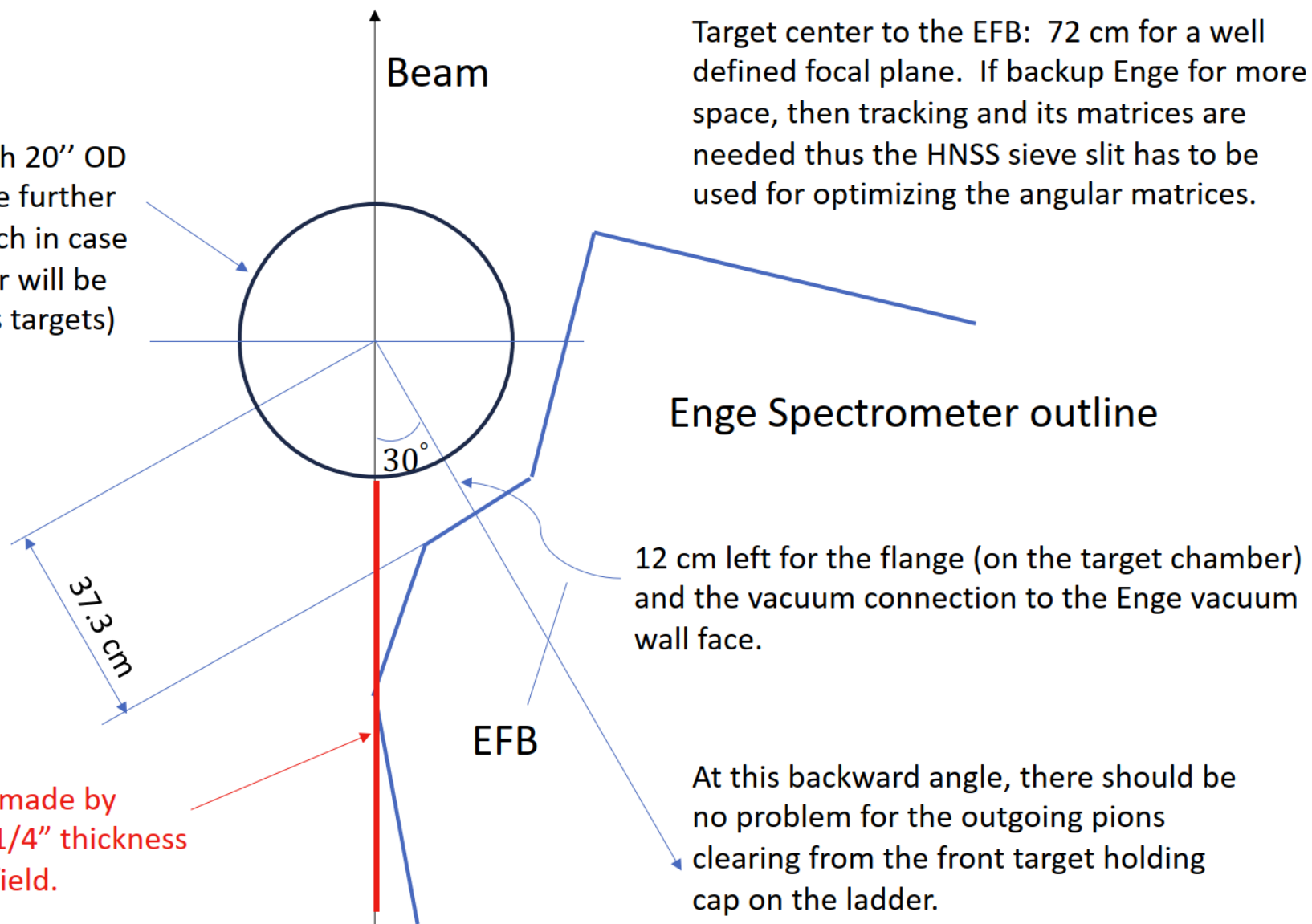


Target chamber with 20" OD  
(Dave said it can be further smaller but not much in case the same chamber will be used for future gas targets)

**Enge@135°**

**Enge@150°**

5' long beam pipe made by regular steel with 1/4" thickness to fully shield the field.



Target center to the EFB: 72 cm for a well defined focal plane. If backup Enge for more space, then tracking and its matrices are needed thus the HNSS sieve slit has to be used for optimizing the angular matrices.

**Enge Spectrometer outline**

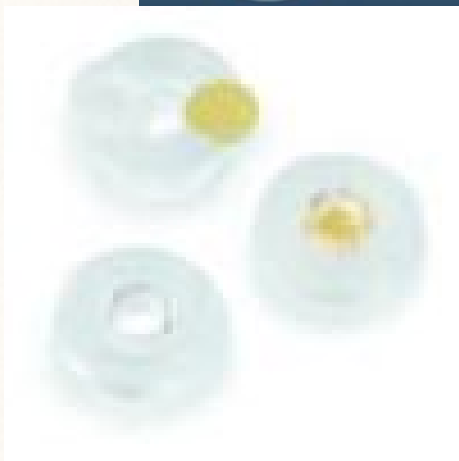
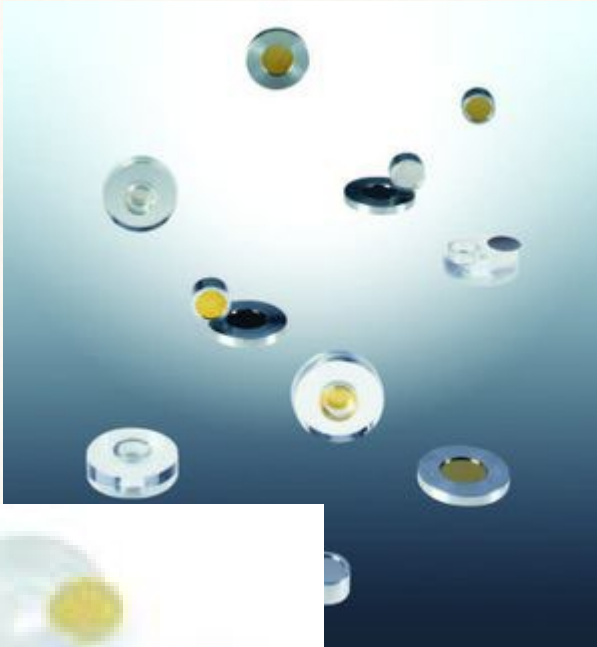
12 cm left for the flange (on the target chamber) and the vacuum connection to the Enge vacuum wall face.

At this backward angle, there should be no problem for the outgoing pions clearing from the front target holding cap on the ladder.



# alpha-source and calibration

Alpha source PM-Type  
(Eckert & Ziegler)



Plastic holder with removable alpha foil

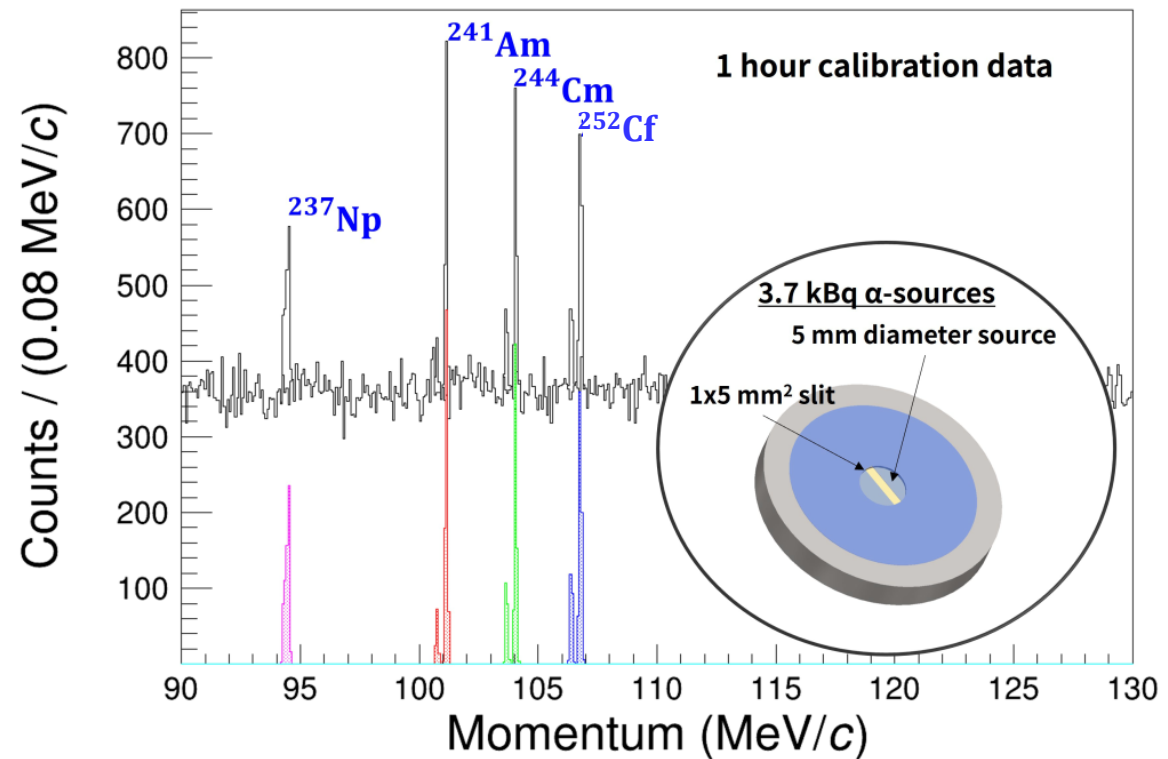
Holder: 1" diameter

Foil: 11.1 mm diameter

Active: 5.0 mm diameter

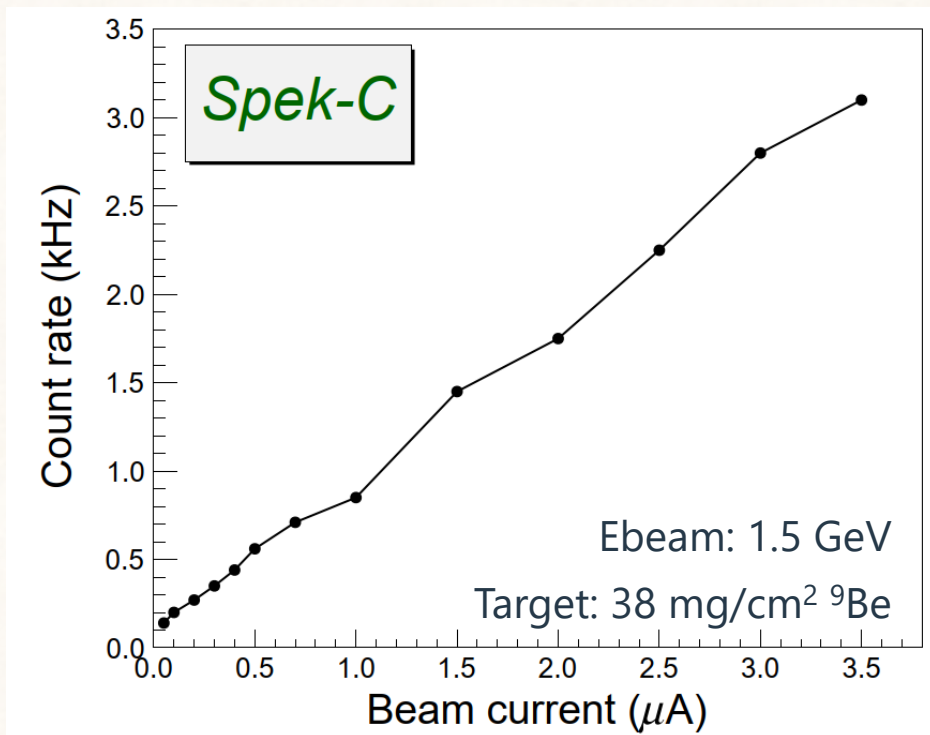
Mounting the foil into the custom designed target holder with 1x5 mm<sup>2</sup> slit

*3-mixed source  
241Am, 244Cm, and 252Cf (or 239Pu)  
is available*



# Expected Rate of Enge

## Single Rate of pion spectrometer



MAMI: 1 kHz /  $\mu\text{A}$  w/ Spek-C (28 msr, 120 deg)

JLab: x 3 thicker target, 50  $\mu\text{A}$

w/ Enge (4 msr, 150 deg)

→ a few tens kHz single rate

$$\mathcal{R}_{\text{Enge}} = 1 \text{ (kHz}/\mu\text{A}) \times I \frac{N_t}{2.6 \times 10^{21}} A^{0.86} \frac{\Delta\Omega_{\text{Enge}} \varepsilon_{\text{decay}}}{28 \text{ msr } 0.25},$$

$$\mathcal{R}_{\text{HKS}}^{\text{ana}} = \mathcal{R}_{\pi^+} \varepsilon_{\pi^+} + \mathcal{R}_{K^+} \varepsilon_{K^+} + \mathcal{R}_p \varepsilon_p,$$

$$\mathcal{R}_{\text{HKS}}^{\text{ana}} = \mathcal{R}_{\pi^-} \varepsilon_{\pi^-},$$

$$\mathcal{R}_{\text{Spectrum}} = \mathcal{R}_{\text{HKS}}^{\text{ana}} \times \mathcal{R}_{\text{Enge}}^{\text{ana}} \times T_{\text{window}},$$

Target	$\mathcal{R}_{\text{HKS}}$ (kHz)	$\mathcal{R}_{\text{Enge}}$ (kHz)	$\mathcal{R}_{\text{Trigger}}$ (Hz)	$\mathcal{R}_{\text{Spectrum}}$ (Hz/MeV)
<sup>6</sup> Li	45	20	90	$5.6 \times 10^{-6}$
<sup>9</sup> Be	25	21	50	$3.0 \times 10^{-6}$
<sup>12</sup> C (Graphite)	41	20	80	$5.2 \times 10^{-6}$
<sup>27</sup> Al	54	31	170	$1.0 \times 10^{-5}$
<sup>40</sup> Ca	52	31	160	$9.5 \times 10^{-6}$
<sup>208</sup> Pb	20	15	30	$1.9 \times 10^{-6}$

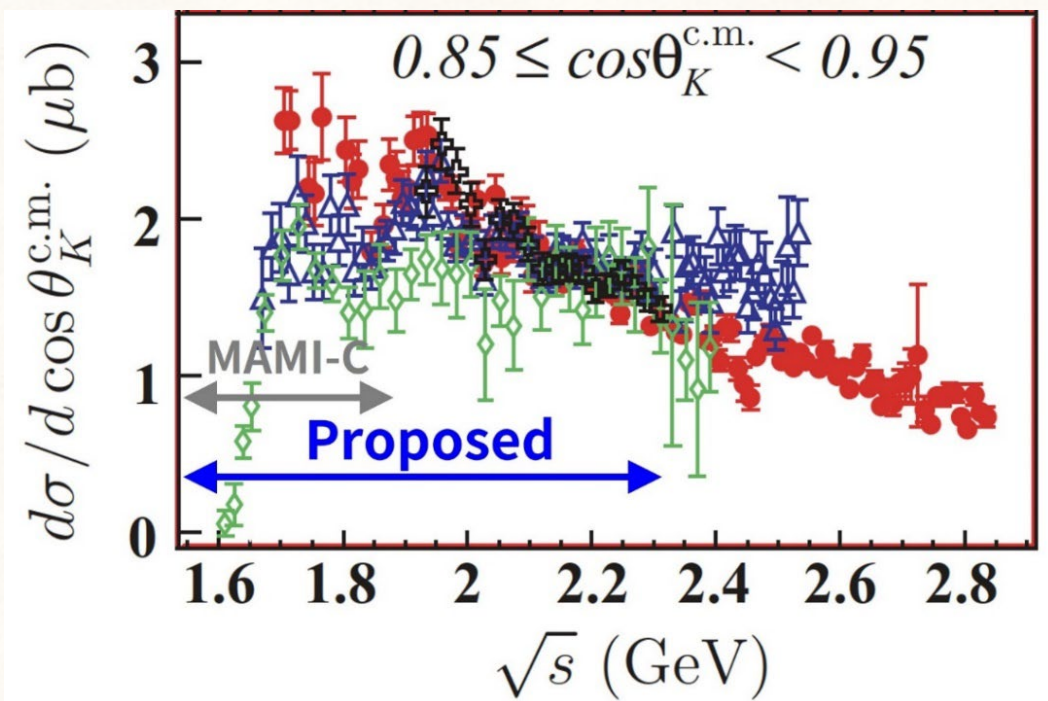
~30 times yield

$$N_{HYP} = \boxed{N_{\Lambda}} R_{F.P} \boxed{R_{stop}} \Gamma_{\pi^-} \boxed{\Delta\Omega_{\pi^-} \varepsilon_{\pi^-}^{decay} \varepsilon_{\pi^-}^{det}}$$

↑ × 30

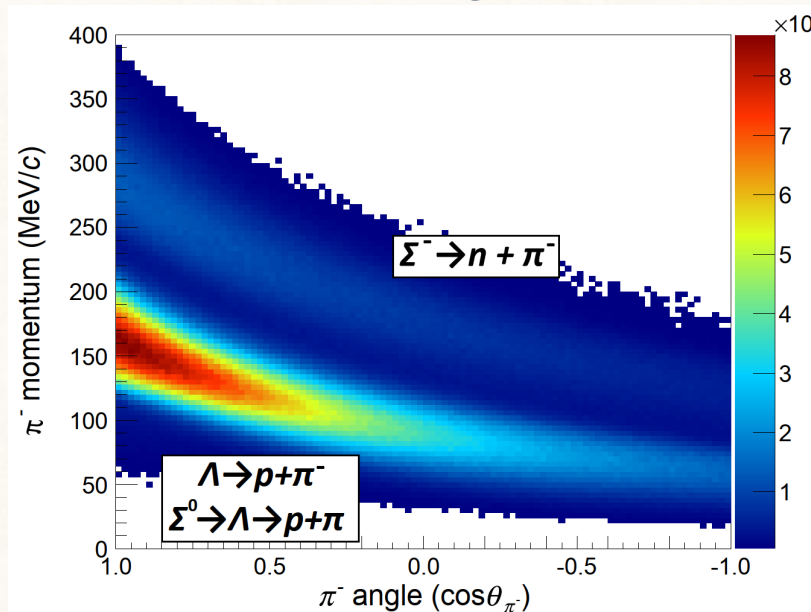
Monte-Carlo

$p(\gamma, K^+) \Lambda$  Cross Section

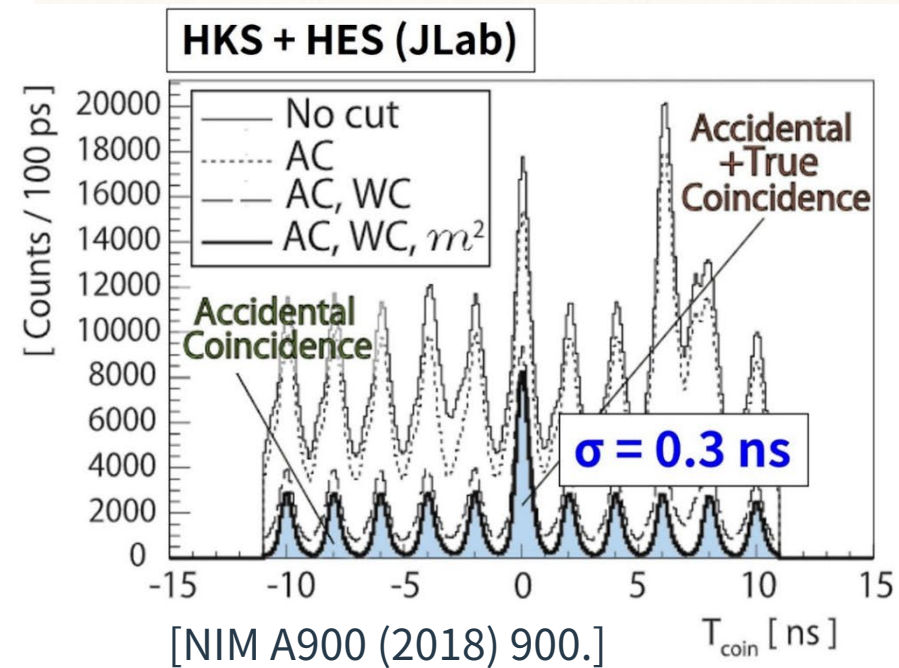
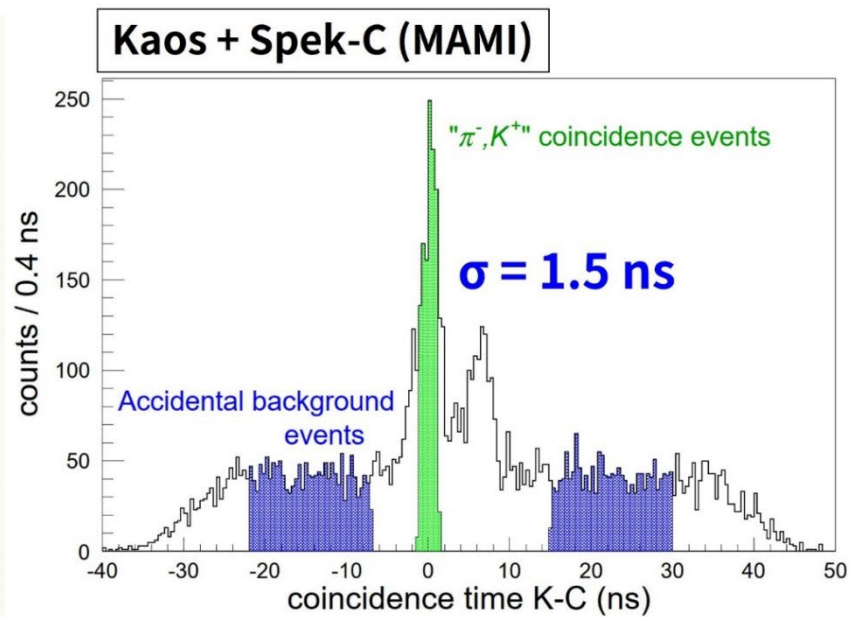
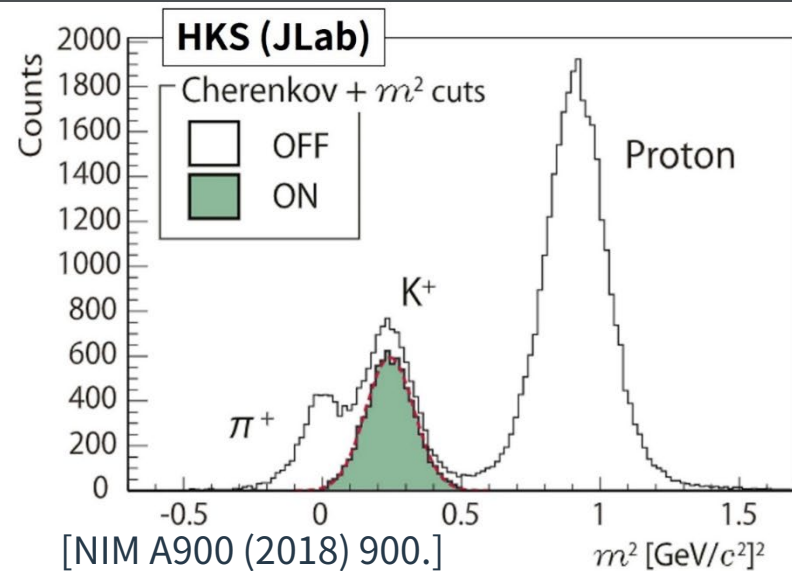
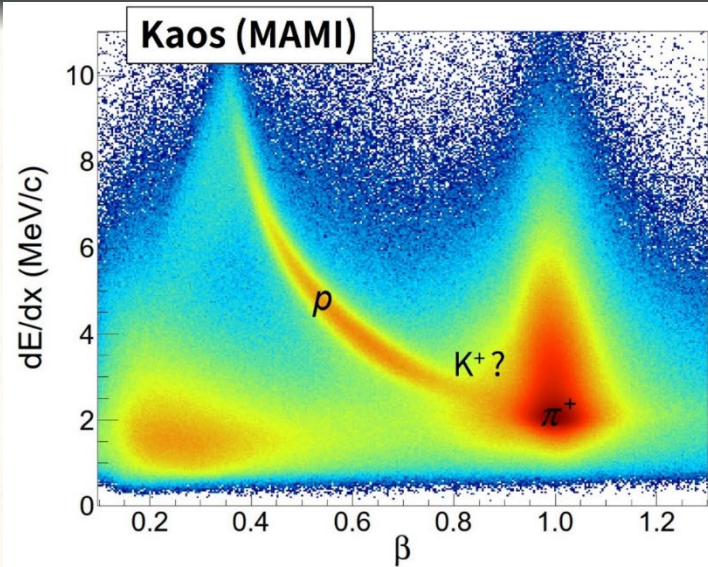


[CLAS, Phys. Rev. C 81 (2010) 025201.]

- Much better luminosity thanks to higher beam energy and intensity
- Background reduction from in-flight hyperons



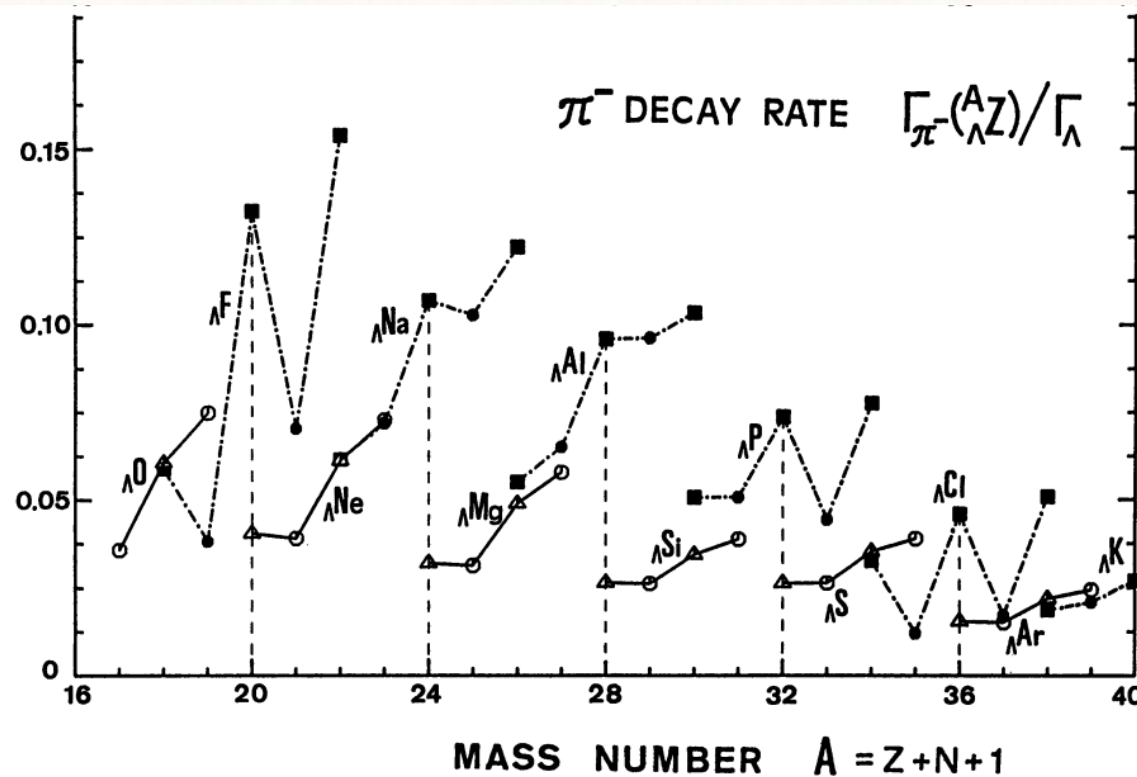
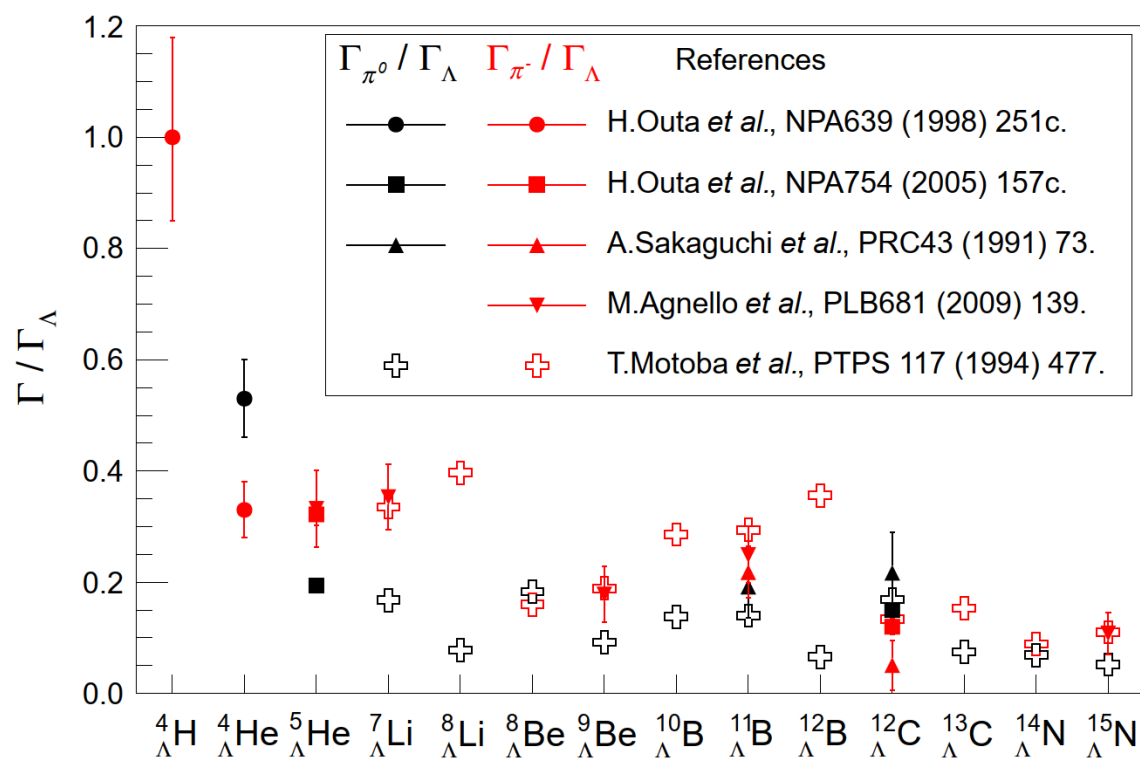
# PID performance



# Pion emission probability

$$N_{HYP} = N_{\Lambda} R_{F.P} R_{stop} \Gamma_{\pi^-} \Delta\Omega_{\pi^-} \varepsilon_{\pi^-}^{decay} \varepsilon_{\pi^-}^{det}$$

Monte-Carlo

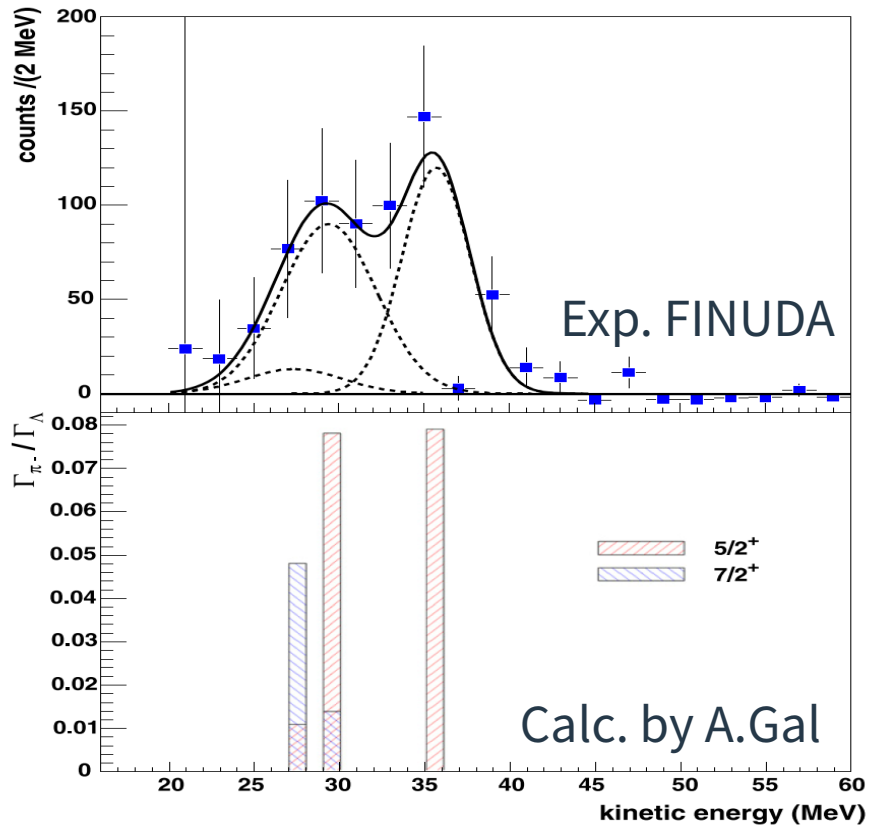


# Spin assignment from decay width

$$N_{HYP} = N_{\Lambda} R_{F.P} R_{stop} \Gamma_{\pi^-} \Delta\Omega_{\pi^-} \varepsilon_{\pi^-}^{decay} \varepsilon_{\pi^-}^{det}$$

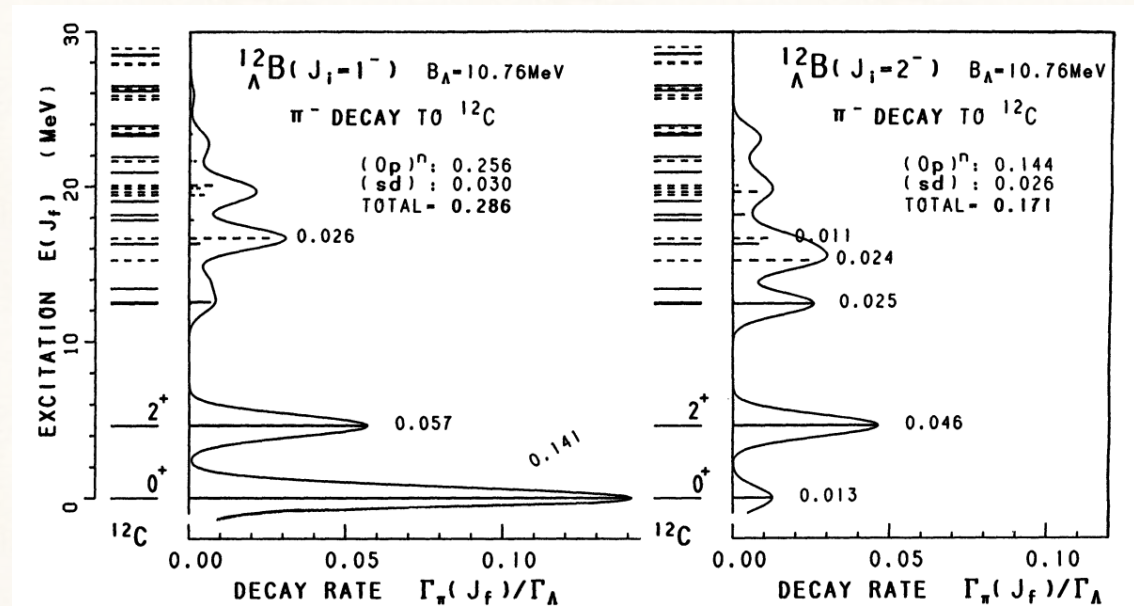
Monte-Carlo

$^{11}_{\Lambda}B \rightarrow ^{11}C + \pi^-$  decay pion energy



FINUDA, Phys. Lett. B681 (2009) 139

- Decay width calc. well reproduced exp. data (T. Motoba and K. Itonaga, PTPS117(1994)477.)
- Large  $\Gamma_{\pi}$  dependence on SPIN of parent hypernuclei

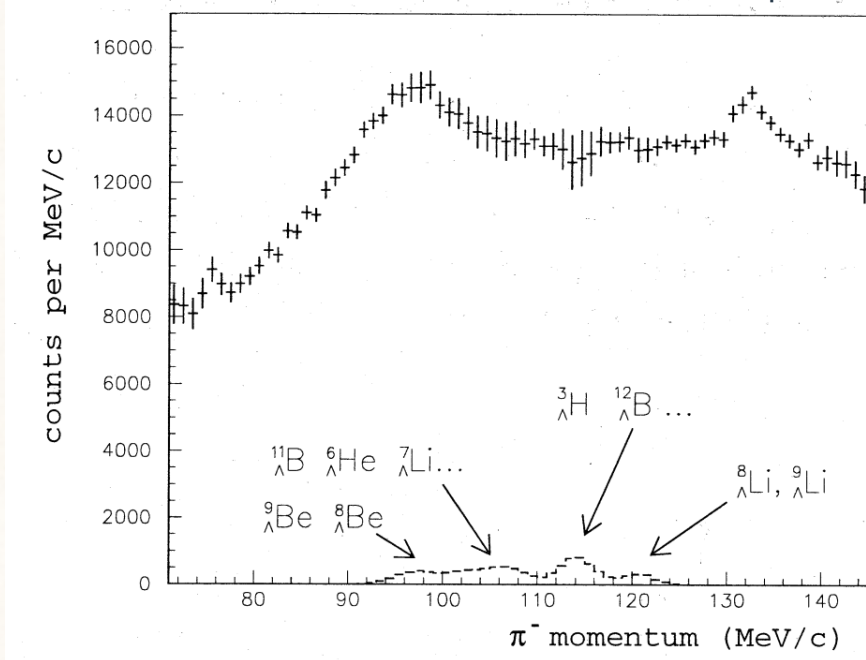


# Hypernuclear formation probability

$$N_{HYP} = N_{\Lambda} R_{F.P.} R_{stop} \Gamma_{\pi^-} \Delta\Omega_{\pi^-} \varepsilon_{\pi^-}^{decay} \varepsilon_{\pi^-}^{det}$$

Monte-Carlo

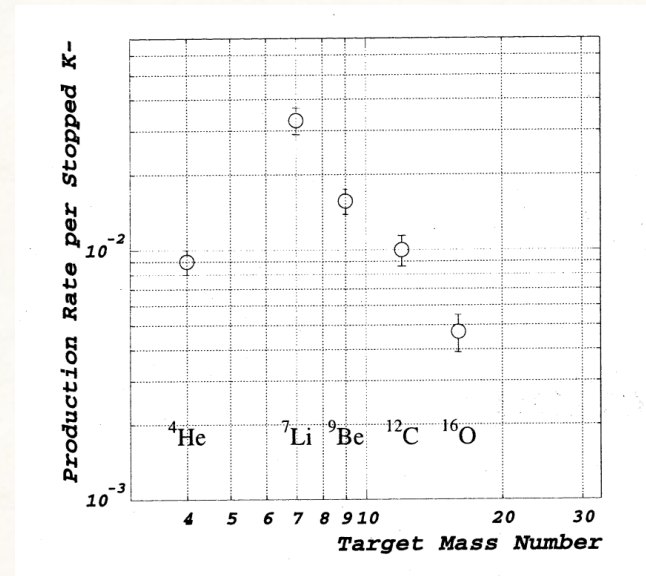
$\pi^-$  spectrum of  $^{12}\text{C}$  target @  $(\text{K}^-, \pi^-)_{stop}$



Hyp.	RFP(%)
$^4_{\Lambda}\text{H}$	1.1
$^9_{\Lambda}\text{Be}$	0.94
$^{10}_{\Lambda}\text{B}$	0.20
$^{11}_{\Lambda}\text{B}$	0.53

A. Kawachi (1992) Ph.D thesis, U-Tokyo

- $A^{-2}$  dependence of  $^4_{\Lambda}\text{H}$  Form. Prob. (H.Tamura, PRC40(1989)R479)
- 1.57% @  $(\text{K}^-, \pi^-)_{stop}$ , 1% @MAMI for  $^9\text{Be}$  target
- Prediction by AMD on  $^{12}\text{C}$  target



## Proposed (e,e'K<sup>+</sup>) experiments

Target	Period	Experiment
<sup>6</sup> Li	5	PR12-24-004
<sup>9</sup> Be	16	PR12-24-004
<sup>11</sup> B	3	PR12-24-004
<sup>12</sup> C	7	E12-15-008 / PR12-24-013
<sup>27</sup> Al	28	PR12-24-011 / PR12-24-013
<sup>40</sup> Ca	19	E12-15-008 / PR12-24-013
<sup>48</sup> Ca	23	E12-15-008 / PR12-24-013
<sup>208</sup> Pb	42	E12-20-013 / PR12-24-003