

Hyperon Recoil Polarization from Analysis of RG-K Data

Infinite Strangeness



Outline:

- KY Electroproduction Formalism
- Existing CLAS Recoil Polarization Data
- Analysis Details, Issues, Next Steps
- Summary/Conclusions



Pseudoscalar Meson Production Formalism

$$\frac{d\sigma_v}{d\Omega_K^{c.m.}} = \mathcal{K} \sum_{\alpha,\beta} S_\alpha S_\beta \left[R_T^{\beta\alpha} + \epsilon R_L^{\beta\alpha} + c_+ ({}^c R_{LT}^{\beta\alpha} \cos \Phi + {}^s R_{LT}^{\beta\alpha} \sin \Phi) \right. \\ \left. + \epsilon ({}^c R_{TT}^{\beta\alpha} \cos 2\Phi + {}^s R_{TT}^{\beta\alpha} \sin 2\Phi) + hc_- ({}^c R_{LT'}^{\beta\alpha} \cos \Phi + {}^s R_{LT'}^{\beta\alpha} \sin \Phi) + hc_0 R_{TT'}^{\beta\alpha} \right]$$

Photoproduction and electroproduction of eta mesons

G. Knochlein (Mainz U., Inst. Kernphys.), D. Drechsel (Mainz U., Inst. Kernphys.), L. Tiator (Mainz U., Inst. Kernphys.) (Jun, 1995)

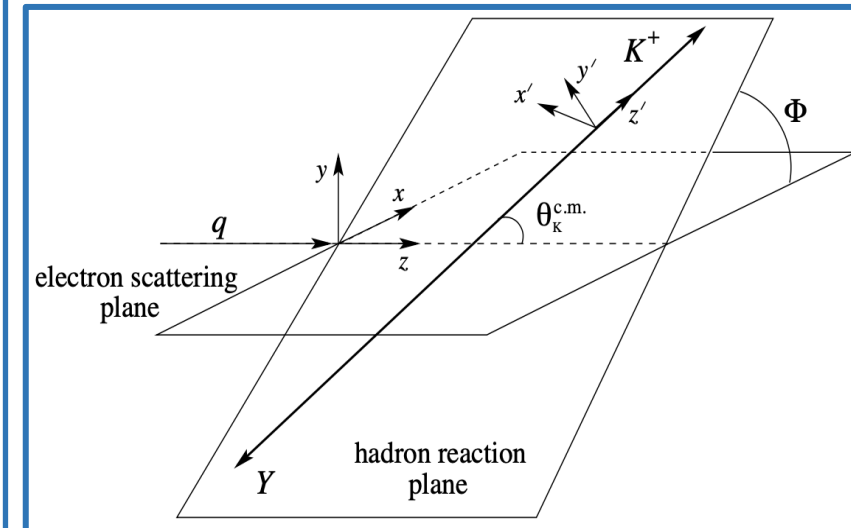
Published in: Z.Phys.A 352 (1995) 327-343 • e-Print: [nucl-th/9506029](https://arxiv.org/abs/nucl-th/9506029) [nucl-th]

TABLE I. Polarization observables in pseudoscalar meson electroproduction. A star denotes a response function which does not vanish but is identical to another response function via a relation in App. A.

	Target				Recoil			Target + Recoil								
	β	α	T	L	x'	y'	z'	x'	x'	x'	y'	y'	y'	z'	z'	z'
T	R_T^{00}	0	R_T^{0y}	0	0	$R_T^{y'0}$	0	$R_T^{x'x}$	0	$R_T^{x'z}$	0	*	0	$R_T^{z'x}$	0	$R_T^{z'z}$
L	R_L	0	R_L^{0y}	0	0	*	0	$R_L^{x'x}$	0	$R_L^{x'z}$	0	*	0	*	0	*
${}^c TL$	${}^c R_{TL}^{00}$	0	${}^c R_{TL}^{0y}$	0	0	*	0	${}^c R_{TL}^{x'x}$	0	*	0	*	0	${}^c R_{TL}^{z'x}$	0	*
${}^s TL$	0	${}^s R_{TL}^{0x}$	0	${}^s R_{TL}^{0z}$	${}^s R_{TL}^{x'0}$	0	${}^s R_{TL}^{z'0}$	0	*	0	*	0	*	0	*	0
${}^c TT$	${}^c R_{TT}^{00}$	0	*	0	0	*	0	*	0	*	0	*	0	*	0	*
${}^s TT$	0	${}^s R_{TT}^{0x}$	0	${}^s R_{TT}^{0z}$	${}^s R_{TT}^{x'0}$	0	${}^s R_{TT}^{z'0}$	0	*	0	*	0	*	0	*	0
${}^c TL'$	0	${}^c R_{TL'}^{0x}$	0	${}^c R_{TL'}^{0z}$	${}^c R_{TL'}^{x'0}$	0	${}^c R_{TL'}^{z'0}$	0	*	0	*	0	*	0	*	0
${}^s TL'$	${}^s R_{TL'}^{00}$	0	${}^s R_{TL'}^{0y}$	0	0	*	0	${}^s R_{TL'}^{x'x}$	0	*	0	*	0	${}^s R_{TL'}^{z'x}$	0	*
TT'	0	$R_{TT'}^{0x}$	0	$R_{TT'}^{0z}$	$R_{TT'}^{x'0}$	0	$R_{TT'}^{z'0}$	0	*	0	*	0	*	0	*	0

Response functions

$$R(Q^2, W, \cos \theta_K^{c.m.})$$

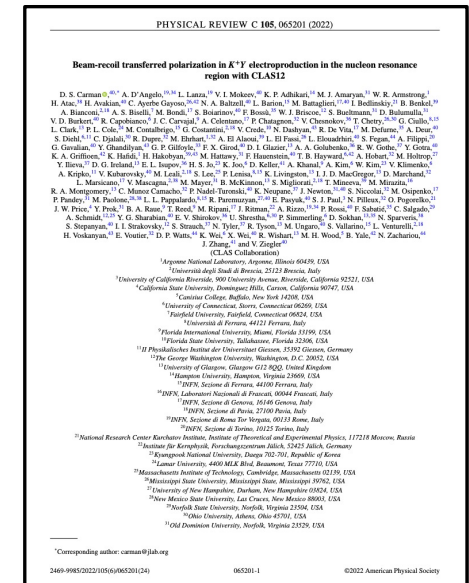


KY Polarization Formalism

	(x',y',z')	Φ -integrated	(x,y,z)	
\mathcal{P}^0 = recoil polarization	$\mathcal{P}_{x'}^0$	0	\mathcal{P}_x^0	0
	$\mathcal{P}_{y'}^0$	$K_I(R_T^{y'0} + \epsilon R_L^{y'0})$	\mathcal{P}_y^0	$\frac{1}{2}\sqrt{\epsilon(1+\epsilon)}K_I(R_{LT}^{x'0} \cos \theta_K^{c.m.} + R_{LT}^{y'0} + R_{LT}^{z'0} \sin \theta_K^{c.m.})$
	$\mathcal{P}_{z'}^0$	0	\mathcal{P}_z^0	0
\mathcal{P}' = transferred polarization	$\mathcal{P}_{x'}'$	$K_I\sqrt{1-\epsilon^2}R_{TT'}^{x'0}$	\mathcal{P}_x'	$\frac{1}{2}\sqrt{\epsilon(1-\epsilon)}K_I(R_{LT'}^{x'0} \cos \theta_K^{c.m.} - R_{LT'}^{y'0} + R_{LT'}^{z'0} \sin \theta_K^{c.m.})$
	$\mathcal{P}_{y'}'$	0	\mathcal{P}_y'	0
	$\mathcal{P}_{z'}'$	$K_I\sqrt{1-\epsilon^2}R_{TT'}^{z'0}$	\mathcal{P}_z'	$\sqrt{1-\epsilon^2}K_I(-R_{TT'}^{x'0} \sin \theta_K^{c.m.} + R_{TT'}^{z'0} \cos \theta_K^{c.m.})$

D.S. Carman et al., PRC 79, 065205 (2009)

- Polarization is a 3-vector whose components are defined in terms of response functions
- Polarization components extracted selecting hyperons from $MM(e'K^+)$ and measuring hyperon decay proton angular distribution
- Transferred polarization extracted from beam helicity asymmetry
- Recoil polarization extracted from forward-backward asymmetry in hyperon decay frame



KY Recoil Polarization Formalism

Λ Production

$$\frac{dN}{d \cos \theta_p^{\Lambda RF}} = N_0 (1 + \alpha P_\Lambda^0 \cos \theta_p^{\Lambda RF})$$

Weak decay parameter
 $\alpha = 0.732$

Self-analyzing weak decay

"forward"

$$N_F = \int_0^1 \frac{dN}{d \cos \theta_p^{\Lambda RF}} d \cos \theta_p^{\Lambda RF} = \int_0^1 N_0 (1 + \alpha P_\Lambda^0 \cos \theta_p^{\Lambda RF}) d \cos \theta_p^{\Lambda RF}$$
$$= N_0 + N_0 \frac{\alpha P_\Lambda^0}{2}$$

"backward"

$$N_B = \int_{-1}^0 \frac{dN}{d \cos \theta_p^{\Lambda RF}} d \cos \theta_p^{\Lambda RF} = \int_{-1}^0 N_0 (1 + \alpha P_\Lambda^0 \cos \theta_p^{\Lambda RF}) d \cos \theta_p^{\Lambda RF}$$
$$= N_0 - N_0 \frac{\alpha P_\Lambda^0}{2}$$

$$A = \frac{N_F - N_B}{N_F + N_B} = \frac{\alpha P_\Lambda^0}{2}$$

$$P_\Lambda^0 = \frac{2A}{\alpha} = 2.732 \cdot A$$

KY Recoil Polarization Formalism

Σ^0 Production

$$\frac{dN}{d \cos \theta_p^{\Sigma RF}} = N_0 (1 + \nu_\Sigma \alpha P_\Sigma^0 \cos \theta_p^{\Sigma RF})$$

"forward"

$$N_F = \int_0^1 \frac{dN}{d \cos \theta_p^{\Sigma RF}} d \cos \theta_p^{\Sigma RF} = \int_0^1 N_0 (1 + \nu_\Sigma \alpha P_\Sigma^0 \cos \theta_p^{\Sigma RF}) d \cos \theta_p^{\Sigma RF}$$

$$= N_0 + N_0 \frac{\nu_\Sigma \alpha P_\Sigma^0}{2}$$

"backward"

$$N_B = \int_{-1}^0 \frac{dN}{d \cos \theta_p^{\Sigma RF}} d \cos \theta_p^{\Sigma RF} = \int_{-1}^0 N_0 (1 + \nu_\Sigma \alpha P_\Sigma^0 \cos \theta_p^{\Sigma RF}) d \cos \theta_p^{\Sigma RF}$$

$$= N_0 - N_0 \frac{\nu_\Sigma \alpha P_\Sigma^0}{2}$$

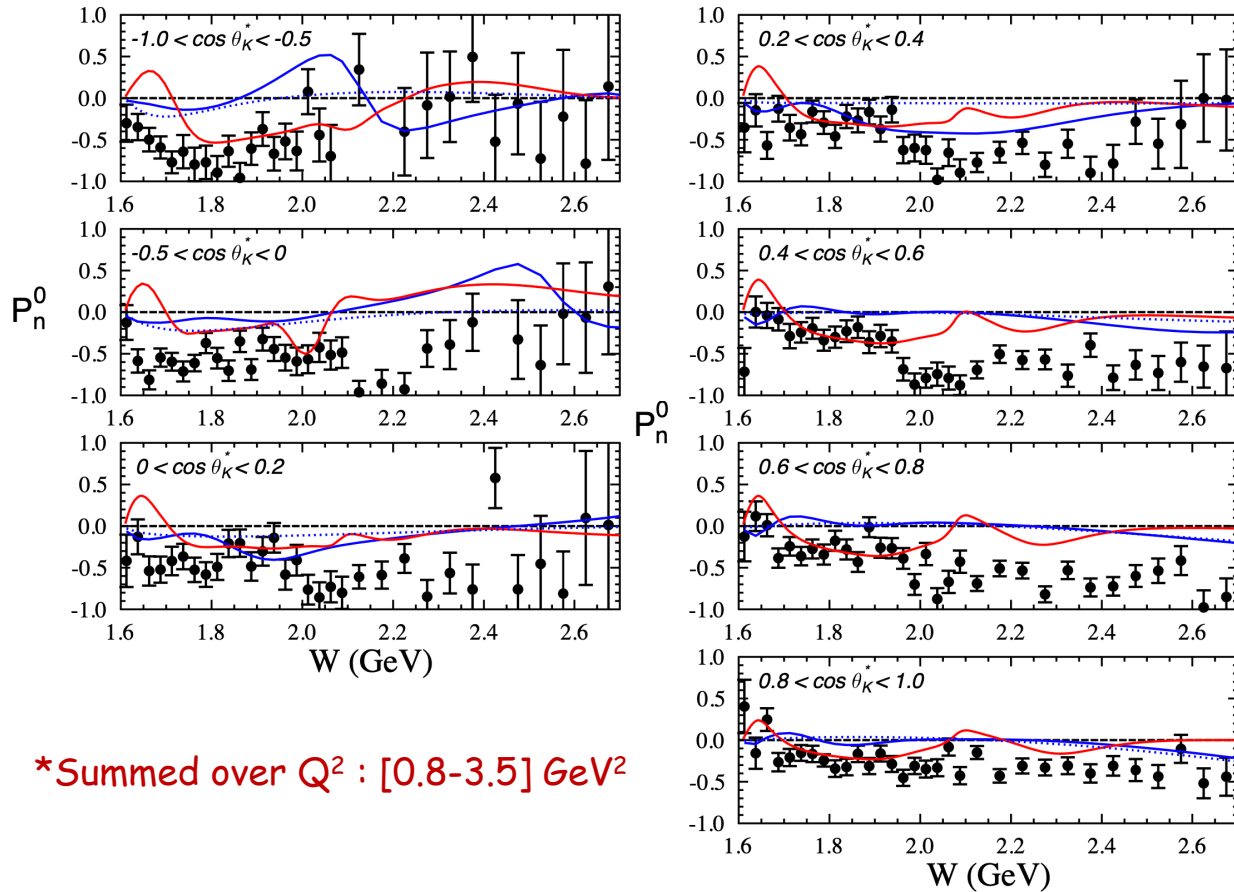
$$A = \frac{N_F - N_B}{N_F + N_B} = \frac{\nu_\Sigma \alpha P_\Sigma^0}{2}$$

$$P_\Sigma^0 = \frac{2A}{\nu_\Sigma \alpha} = -10.655 \cdot A$$

$\nu_\Sigma = -0.265$ includes depolarization for $\Sigma^0 \rightarrow \Lambda \gamma$ ($-1/3$) AND use of $\theta_p^{\Sigma RF}$ instead of $\theta_p^{\Lambda RF}$

KY Recoil Polarization

CLAS Data - Λ Polarization



M. Gabrielyan et al, PRC 90, 035202 (2014)

CLAS e1f

CLAS/CLAS12 Data - Λ and Σ^0 Polarization

Published

CLAS e1f run: Apr. - Jun. 2003

E_b (GeV)	W (GeV)	Q^2 (GeV^2)	Charge (mC)
5.479 GeV	1.6-3.0	0.8-3.5	15.7

Analysis in progress

CLAS12 RG-K run #1: Dec. 2018

6.535 GeV	1.6-2.4	0.3-3.5	18.2
7.546 GeV	1.6-2.4	0.4-4.5	10.8

Spr24

CLAS12 RG-K run #2: Jan. - Mar. 2024

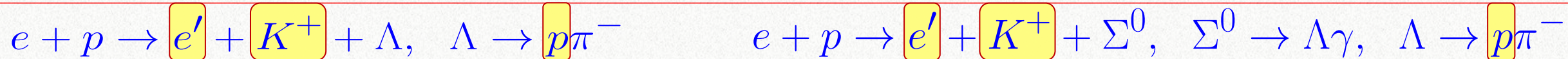
6.4 GeV	1.6-2.4	0.3-3.5	91.4
8.4 GeV	1.6-2.4	0.4-4.5	81.8

Upcoming

CLAS12 RG-K run #3: Planned fall 2025

6.6 GeV	1.6-2.4	0.3-3.5	200
8.8 GeV	1.6-2.4	0.4-4.5	200

Data Analysis



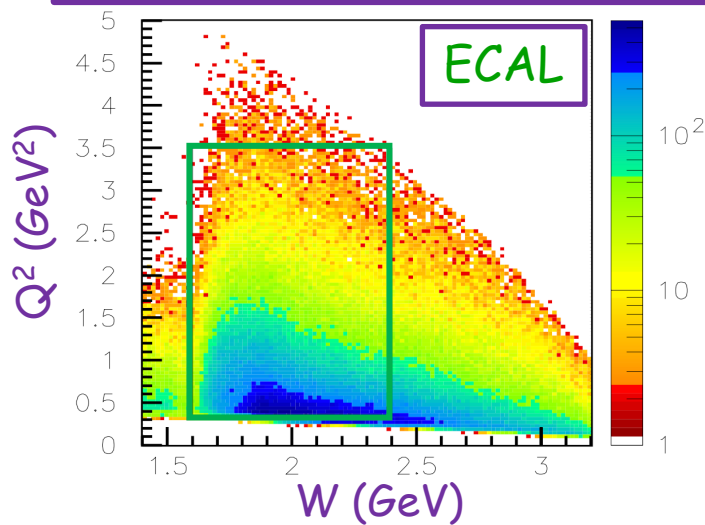
electrons	
Cut	Value
Track Status	$2000 \leq \text{abs}(\text{STATUS}) < 4000$
Event Builder PID	11
p_e	$[1.0:p_{beam}]$ GeV
TOF_e	[21:26] ns
v_z	[-10:2] cm
ECAL Sampling Fraction	$\pm 3.5\sigma$
ECAL Fiducial Cut	7 cm edge cut on U, V, W
π^- contamination	$E_{ECAL}/p_e < -0.84 * E_{PCAL}/p_e + 0.17$
DC Fiducial Cuts	on

Forward Detector

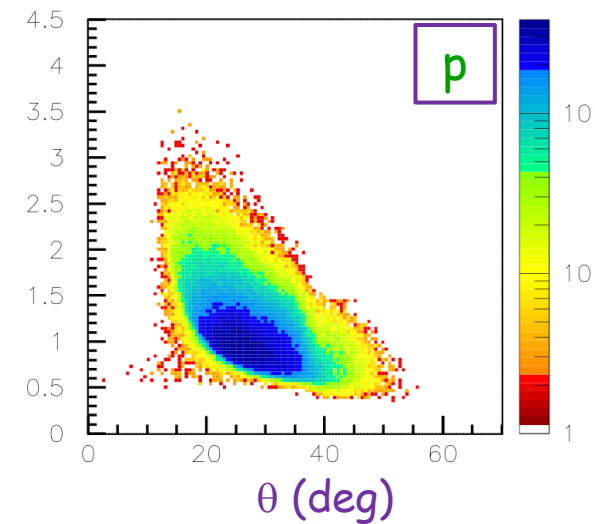
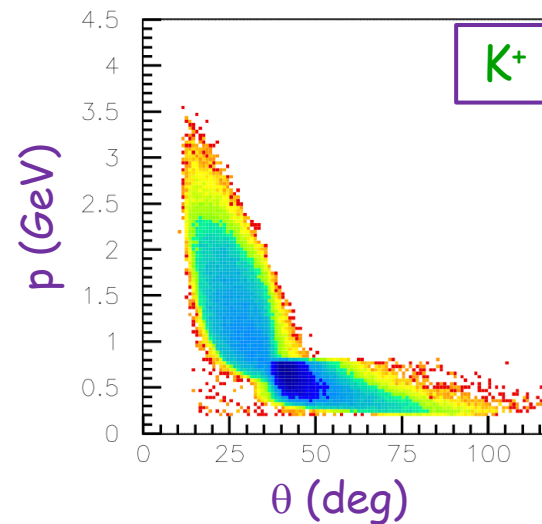
hadrons	
Cut	Value
Track status	$2000 \leq \text{STATUS} < 4000$
q	$\neq 0$
p_h	$[0.4:p_{beam}]$ GeV
β_h	[0.4:1.1]
Event Builder PID	$\pm 211, \pm 321, \text{ or } \pm 2212$
TOF_h	[20:55] ns ($q > 0$), [20:35] ns ($q < 0$)
v_z	[-10:2] cm (K^+ candidates)
DC Fiducial Cuts	on

Central Detector

hadrons	
Cut	Value
Track status	$ \text{STATUS} \geq 4000$
q	$\neq 0$
p_h	[0.2:1.5] GeV
β_h	[0.2:1.1]
Event Builder PID	$\pm 211, \pm 321, \text{ or } \pm 2212$
TOF_h	[0.5:4.0] ns
v_z	[-10:2] cm (K^+ candidates)
Duplicate FD/CD hadron	on

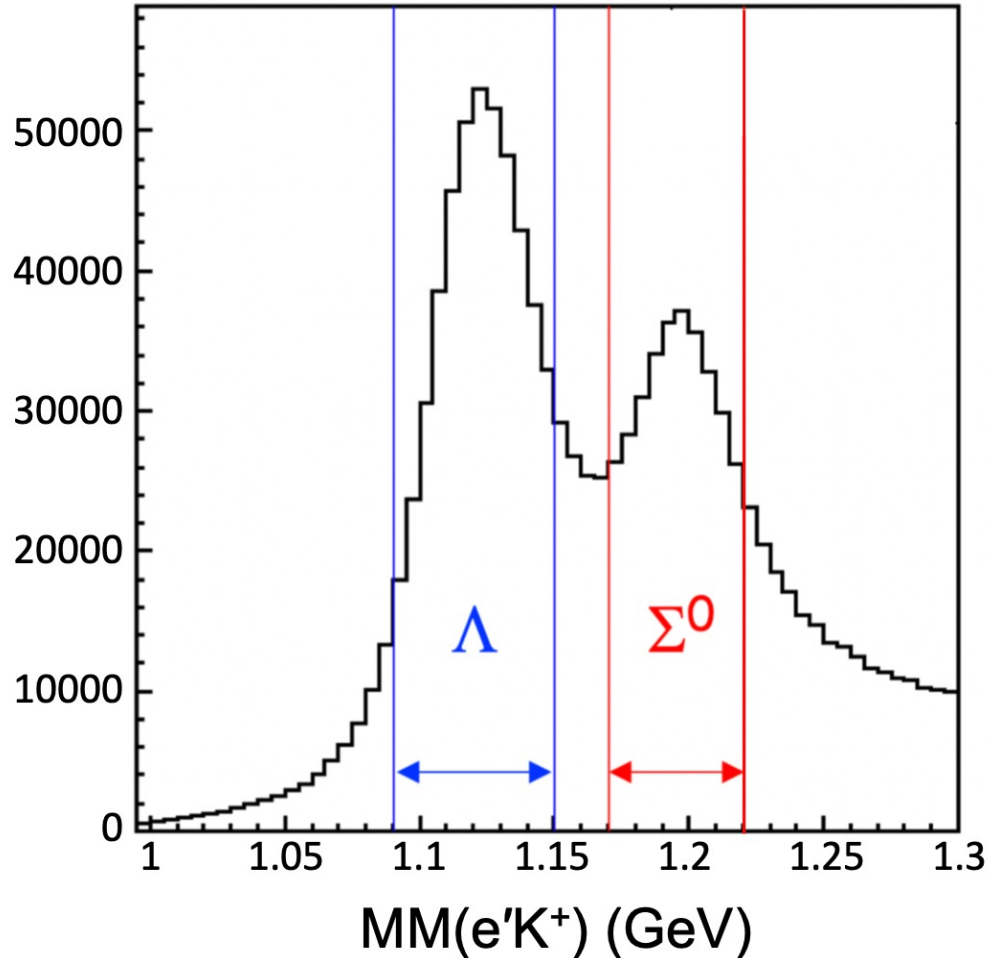


6.535 GeV



Data Binning

Hyperon Analysis Regions



1D Binning Sort

Dependence	Range	Bin Size
Q^2	$[Q_{min}^2:1.5]$ GeV^2	0.1 GeV^2
	$[1.5:2.5]$ GeV^2	0.2 GeV^2
	$[2.5:3.1]$ GeV^2	0.3 GeV^2
	$[3.1:3.5]$ GeV^2	0.4 GeV^2
W	$[W_{min}:2.4]$ GeV	25 MeV
$\cos \theta_K^{c.m.}$	$[-1:1]$	0.08

20 bins

31 bins

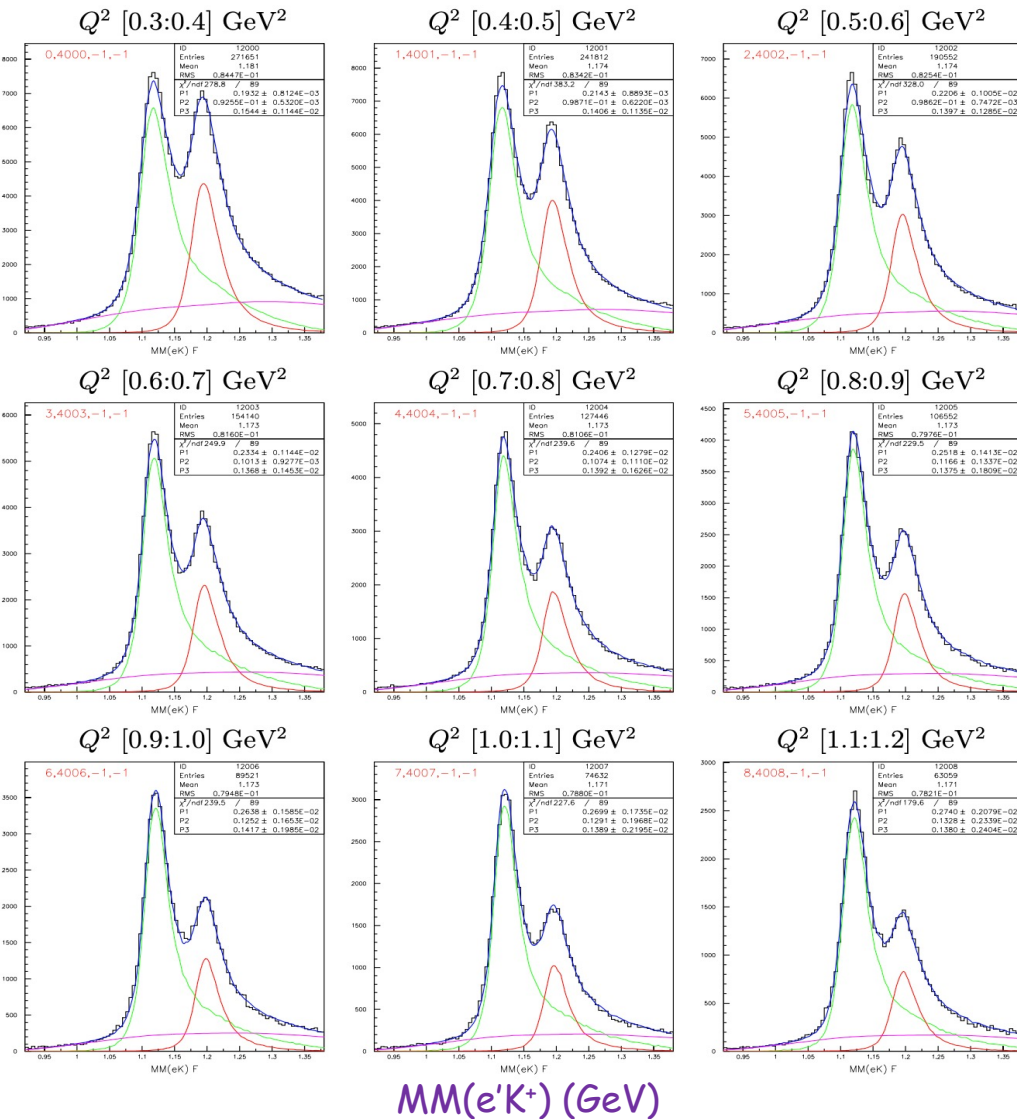
25 bins

- Sort vs. Q^2 - sum over W , $\cos \theta_K^{c.m.}$, Φ
- Sort vs. W - sum over Q^2 , $\cos \theta_K^{c.m.}$, Φ
- Sort vs. $\cos \theta_K^{c.m.}$ - sum over Q^2 , W , Φ

Analysis bounds: Q^2 $[0.3:3.5]$ GeV^2 , W $[\text{thr}:2.4]$ GeV

MM Spectrum Fits

6.535 GeV



Sum all FD/CD topologies together

Yield fitting approach:

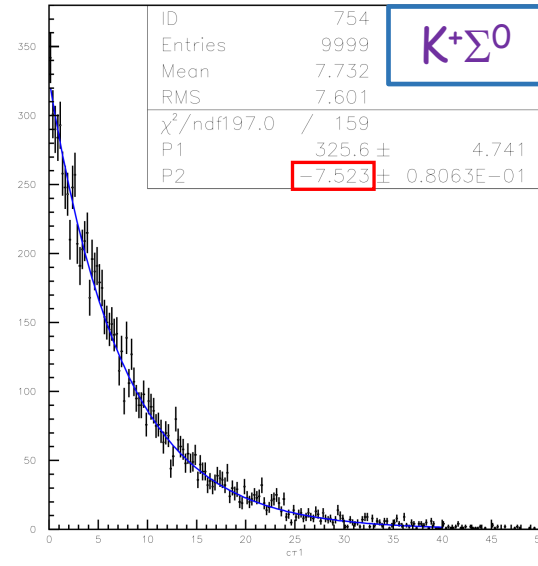
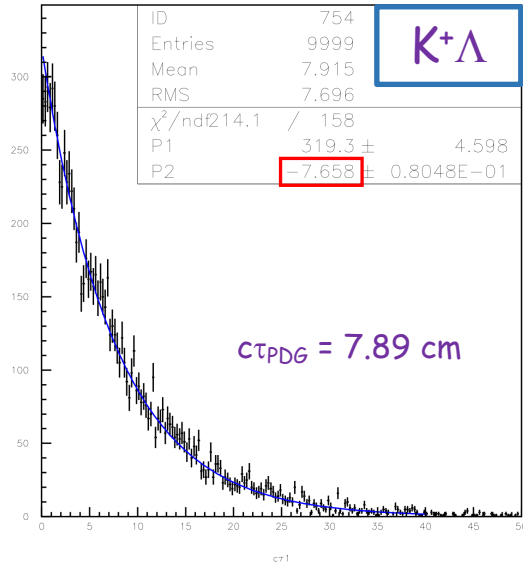
- Generate Monte Carlo $K^+\Lambda$ and $K^+\Sigma^0$ samples to use as fitting templates in bins matched to the data
- The background can be modeled with a polynomial or with the background channel
 - $e'\pi^+\pi^-p$ - with π^+ misidentified as a K^+
- Fit function:
 - Include resolution smearing on reconstructed electron and hadrons
 - Include simple-minded $1/E_\gamma$ model for internal electron radiation

$$MM = A*[TEMPLATE_\Lambda] + B*[TEMPLATE_\Sigma] + C*[bck]$$

Final MM(eK⁺) spectra fit only after e'/K⁺/p momentum and hadron energy loss corrections

Event Generator

$c\tau$ check



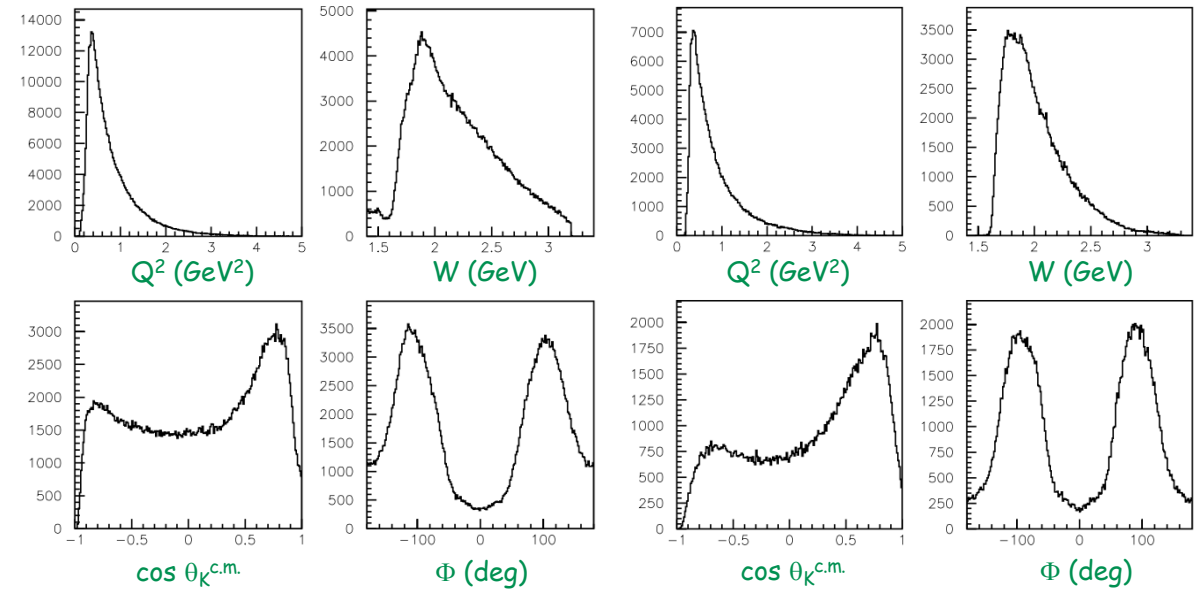
EG based on fit to CLAS KY ep data
CLAS12-Note 2021-003

V. Klimenko, D.S. Carman, V.I. Mokeev

genKYandOnePion

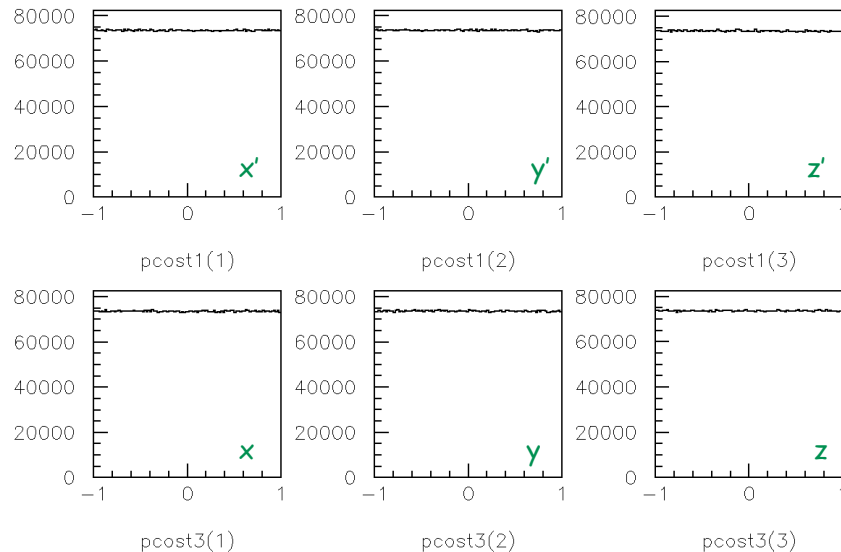
Data Plots

MC Plots



EG decays Λ and Σ^0 hyperons isotropically in their rest frames

Generated Distributions



MC Acceptance

$$ACC = \frac{N_{rec}(Q^2, W, \cos \theta_K^{c.m.}, \Phi, \cos \theta_p^{RF})}{N_{gen}(Q^2, W, \cos \theta_K^{c.m.}, \Phi, \cos \theta_p^{RF})}$$

N_{rec} and N_{gen} from MC sample

ACC2D:

- 1) Q^2 : 20 Q^2 bins, 2 $\cos \theta_p^{RF}$ bins
- 2) W : 31 W bins, 2 $\cos \theta_p^{RF}$ bins
- 3) $\cos \theta_K^{c.m.}$: 25 $\cos \theta_K^{c.m.}$ bins, 2 $\cos \theta_p^{RF}$ bins

$$ASM_{2D} = \frac{\frac{\sum_i N_{rec}^F}{ACC_{2D}} - \frac{\sum_i N_{rec}^B}{ACC_{2D}}}{\frac{\sum_i N_{rec}^F}{ACC_{2D}} + \frac{\sum_i N_{rec}^B}{ACC_{2D}}}$$

Apply ACC after sorting binned yields

ACC4D:

- Q^2 : 20 Q^2 bins, 8 W bins, 8 $\cos \theta_K^{c.m.}$ bins, 2 $\cos \theta_p^{RF}$ bins
- W : 31 W bins, 8 Q^2 bins, 8 $\cos \theta_K^{c.m.}$ bins, 2 $\cos \theta_p^{RF}$ bins
- $\cos \theta_K^{c.m.}$: 25 $\cos \theta_K^{c.m.}$ bins, 8 Q^2 bins, 8 W bins, 2 $\cos \theta_p^{RF}$ bins

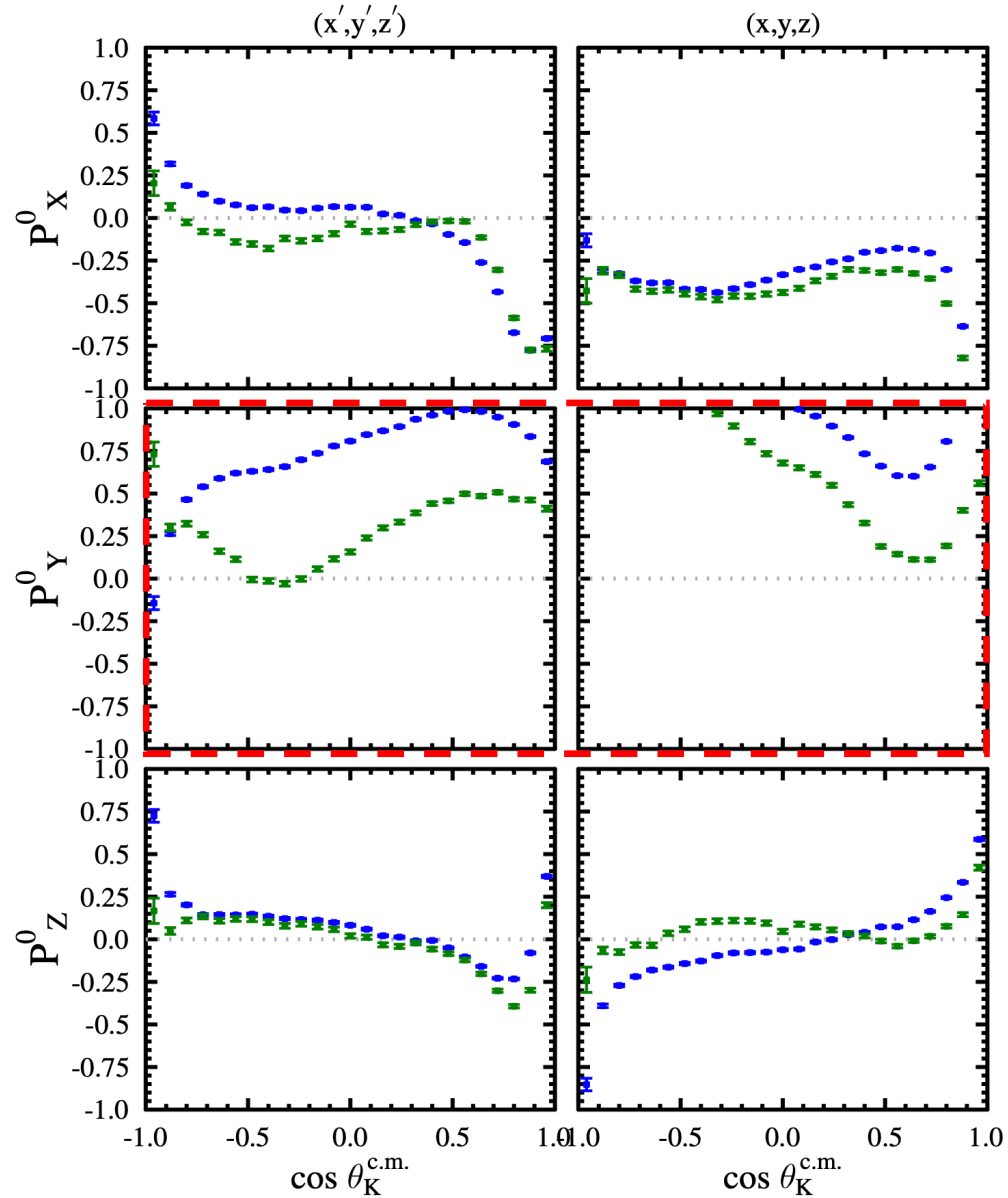
$$ASM_{4D} = \frac{\sum_i \left(\frac{N_{rec}^F}{ACC_{4D}} \right)_i - \sum_i \left(\frac{N_{rec}^B}{ACC_{4D}} \right)_i}{\sum_i \left(\frac{N_{rec}^F}{ACC_{4D}} \right)_i + \sum_i \left(\frac{N_{rec}^B}{ACC_{4D}} \right)_i}$$

Apply ACC event-by-event as event weight with $WGT = 1/ACC$

“Raw” Polarization Results – Data vs. MC

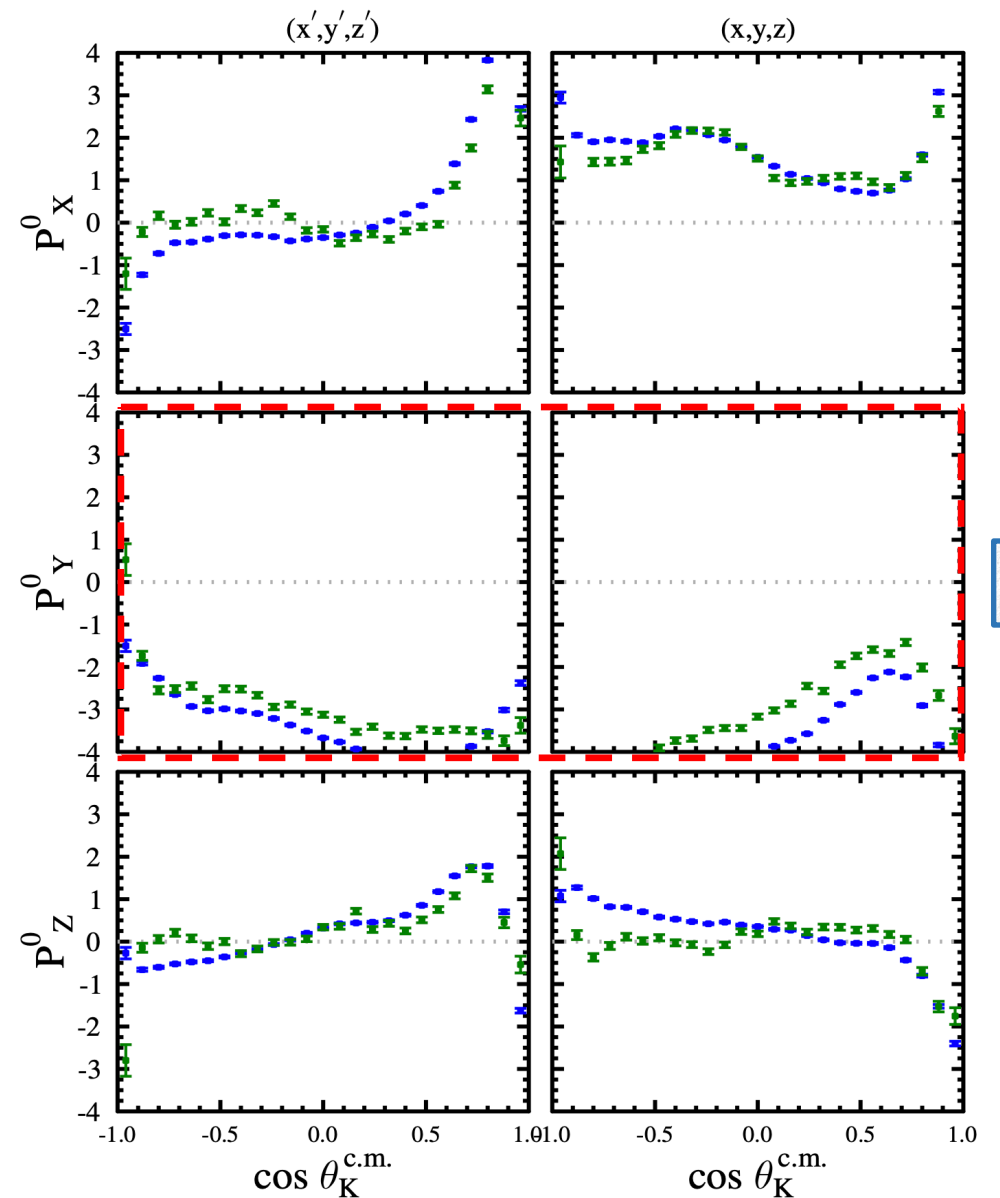
No ACC

$K^+\Lambda$



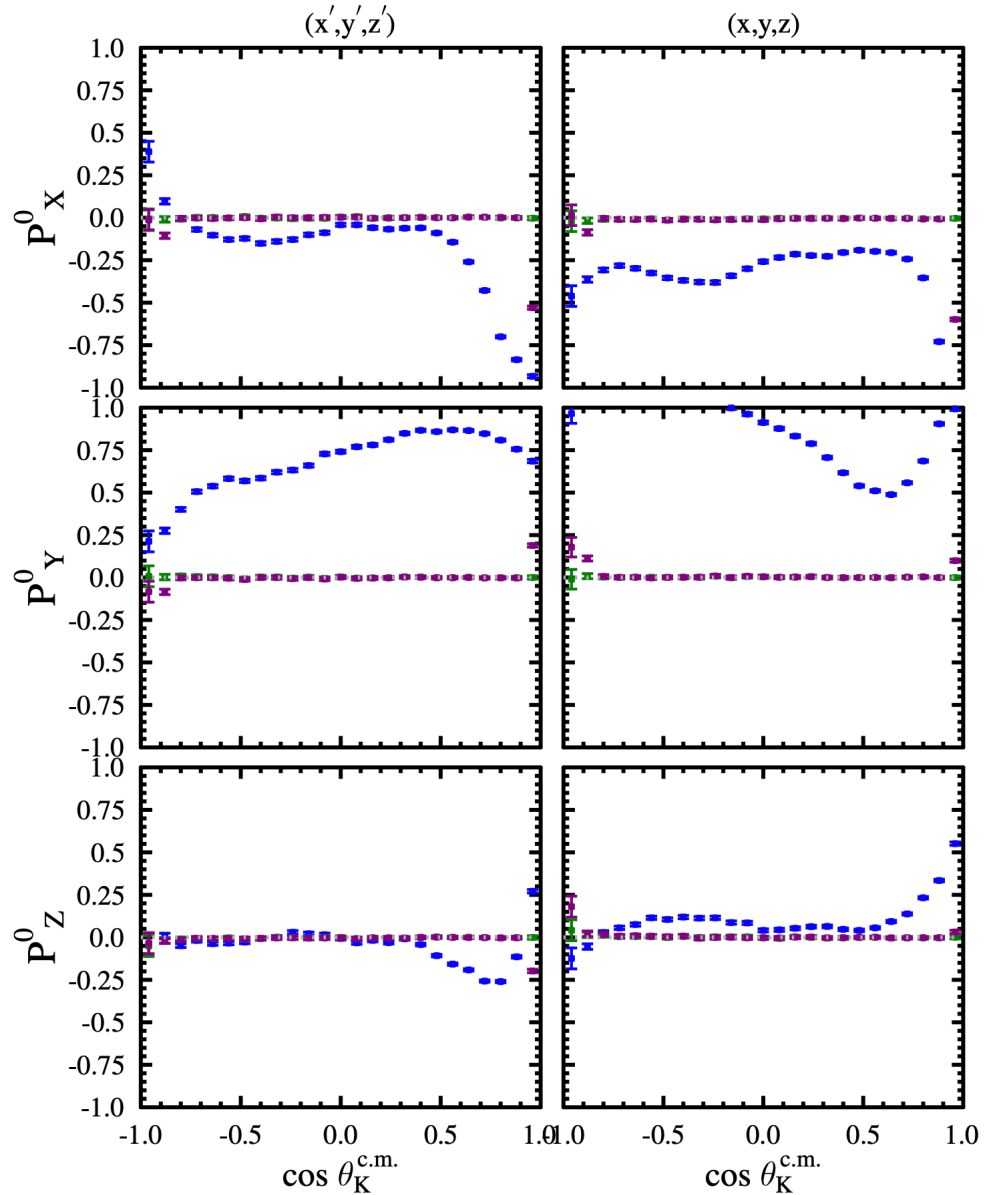
ipolc genKYn MC: raw MC raw data

$K^+\Sigma^0$

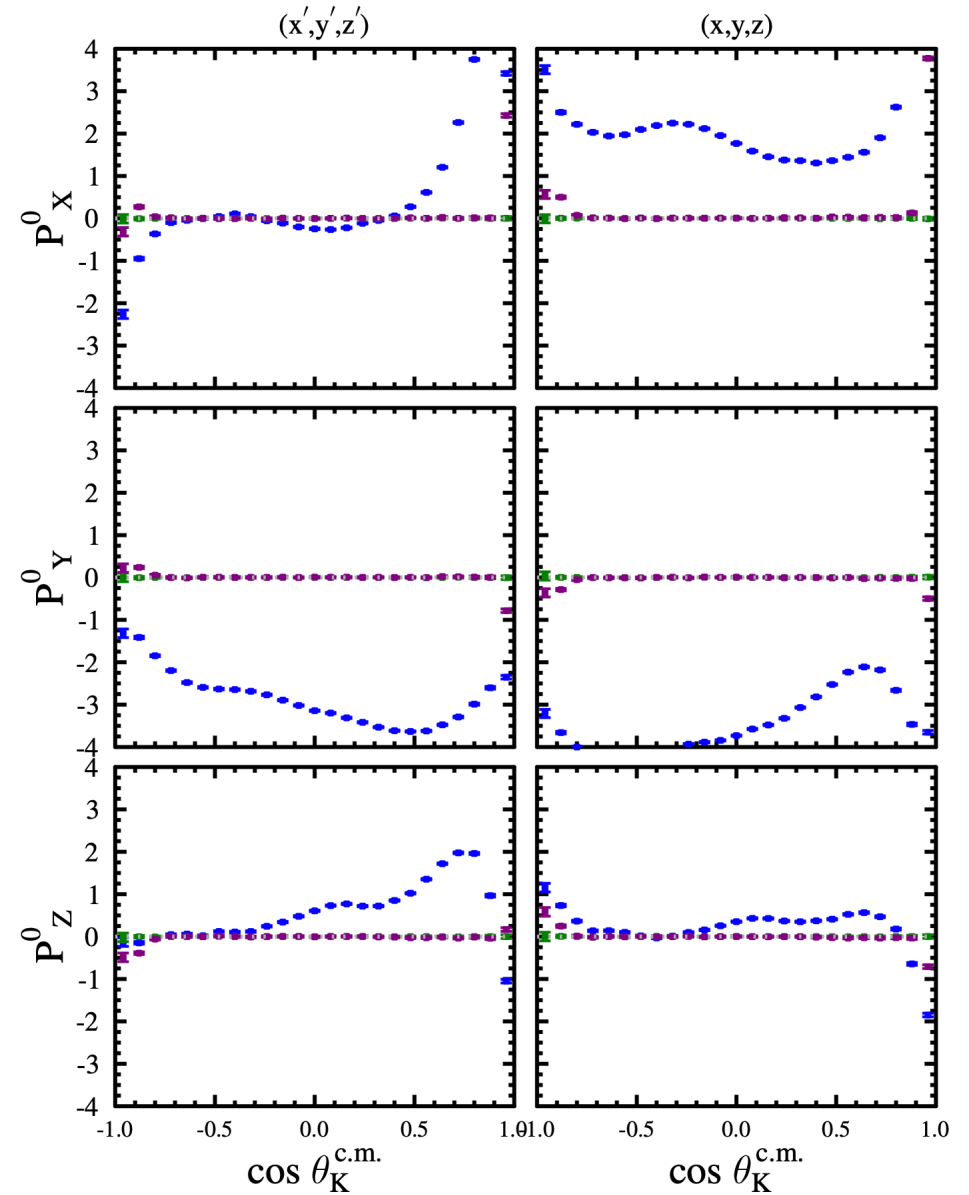


ipolc genKYn MC: raw MC raw data

MC Polarization Results



ipolc genKYn MC: raw ACC2D ACC4D

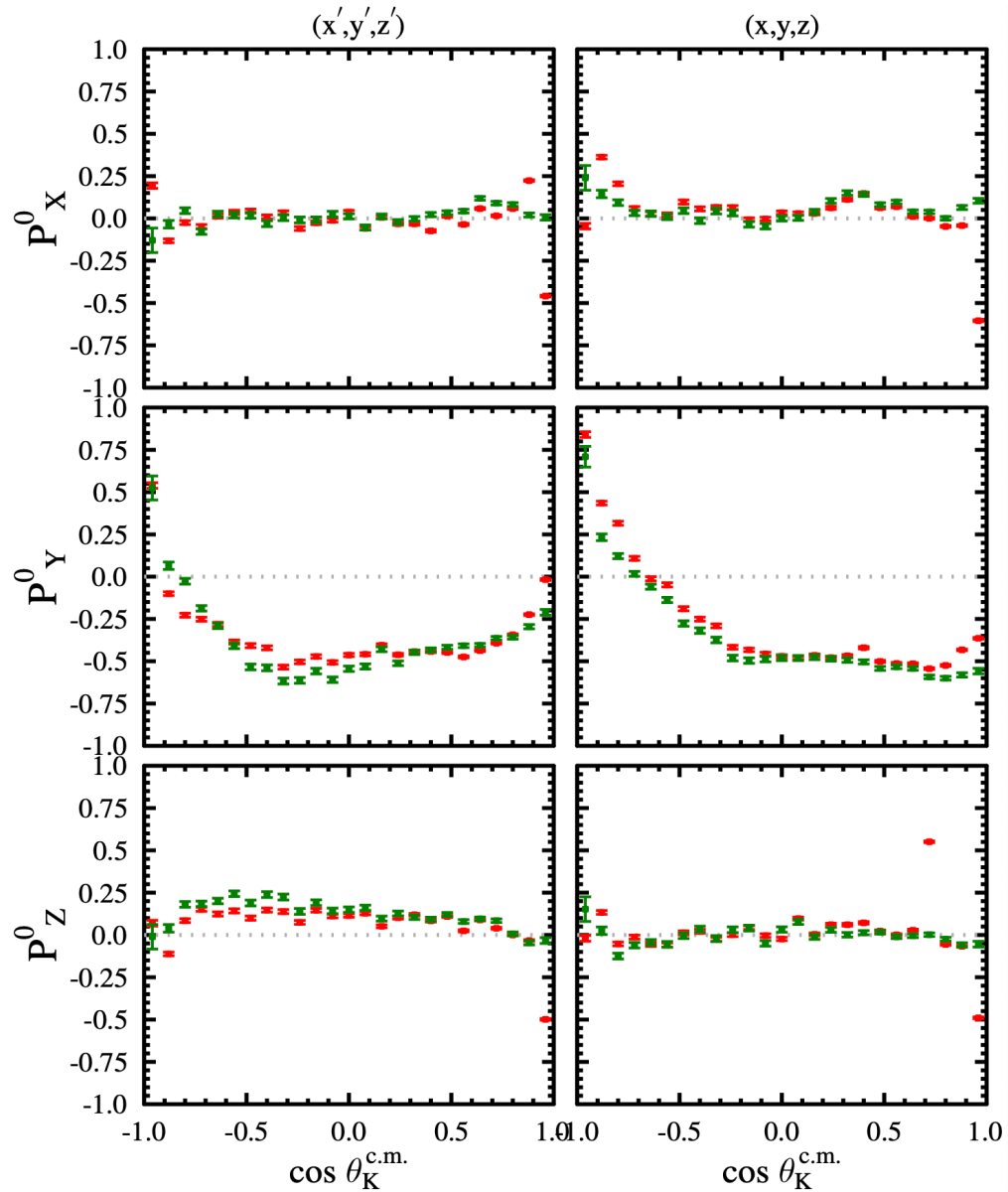


ipolc genKYn MC: raw ACC2D ACC4D

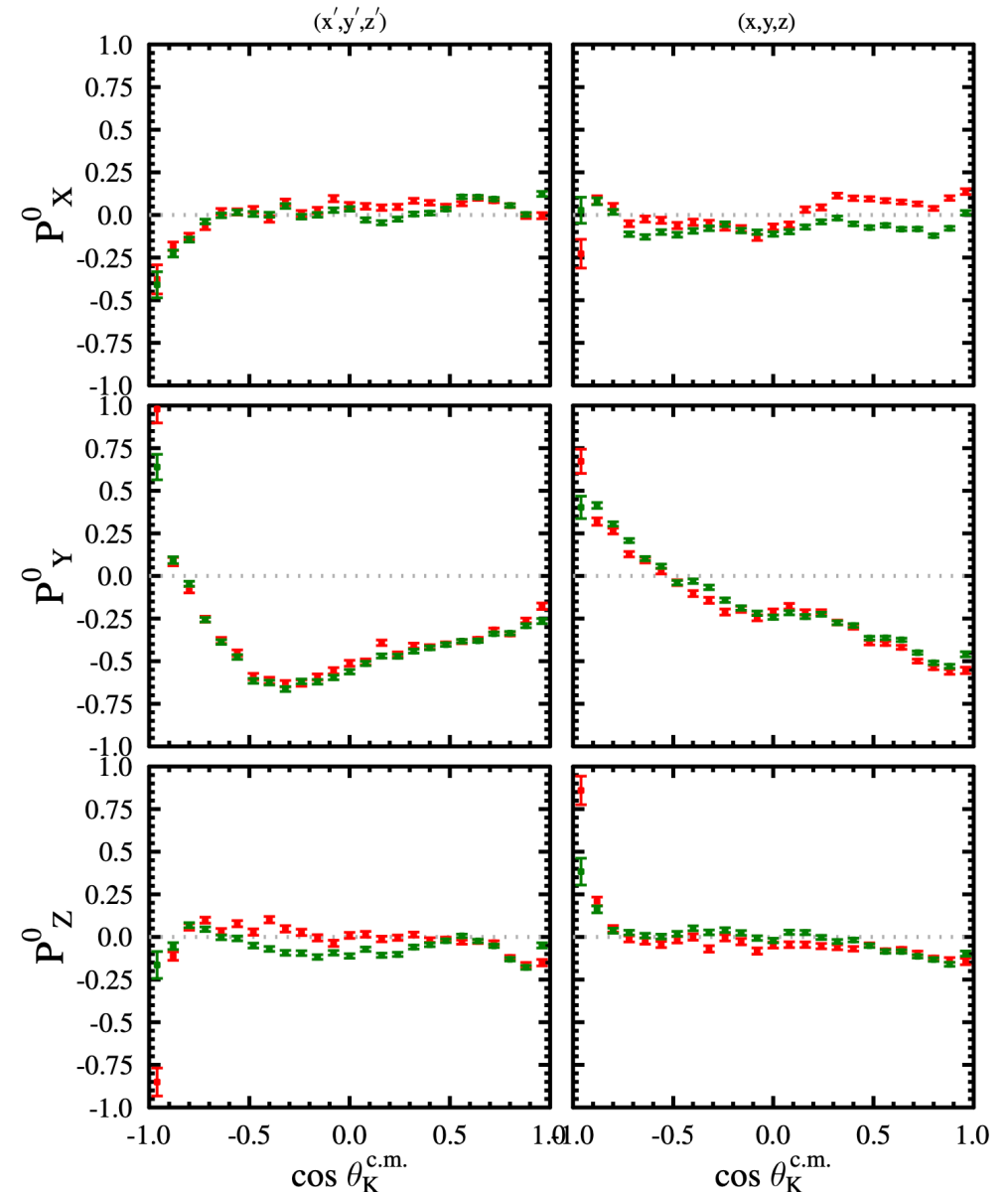
$K^+\Lambda$

$K^+\Sigma^0$

Data Polarization Results



ipolc genKYn: ACC2D ACC4D (0.05%)



ipolc genKYn: ACC2D (pass-1)

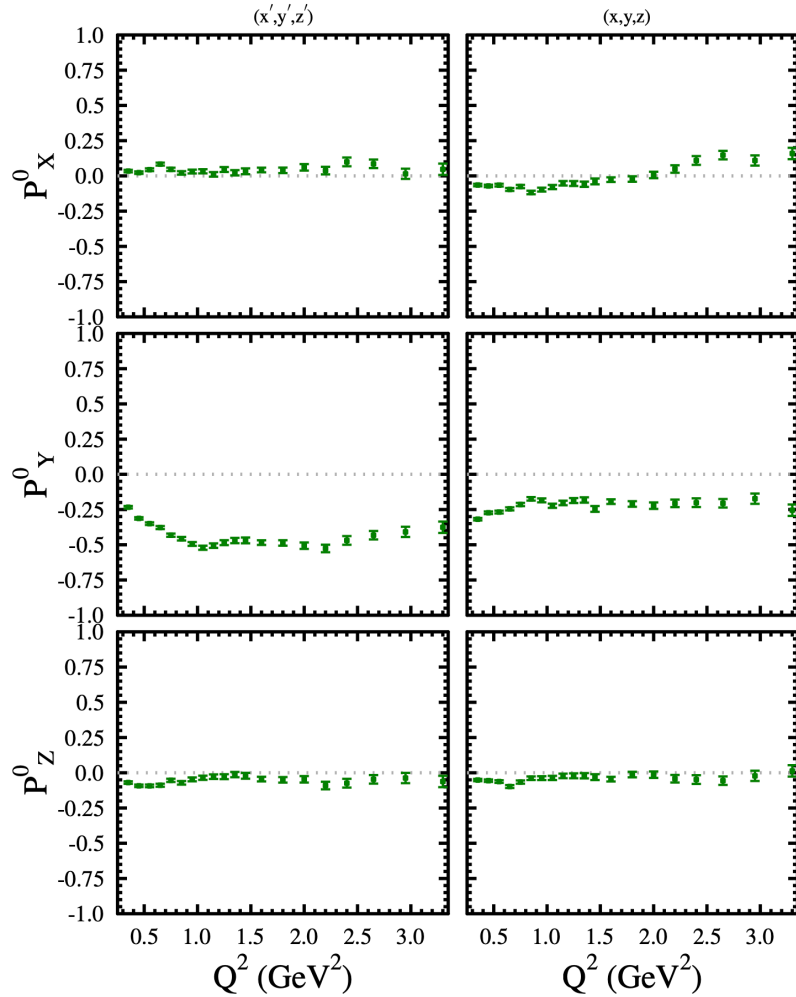
ACC2D (pass-2)

$K^+\Lambda$

$K^+\Lambda$

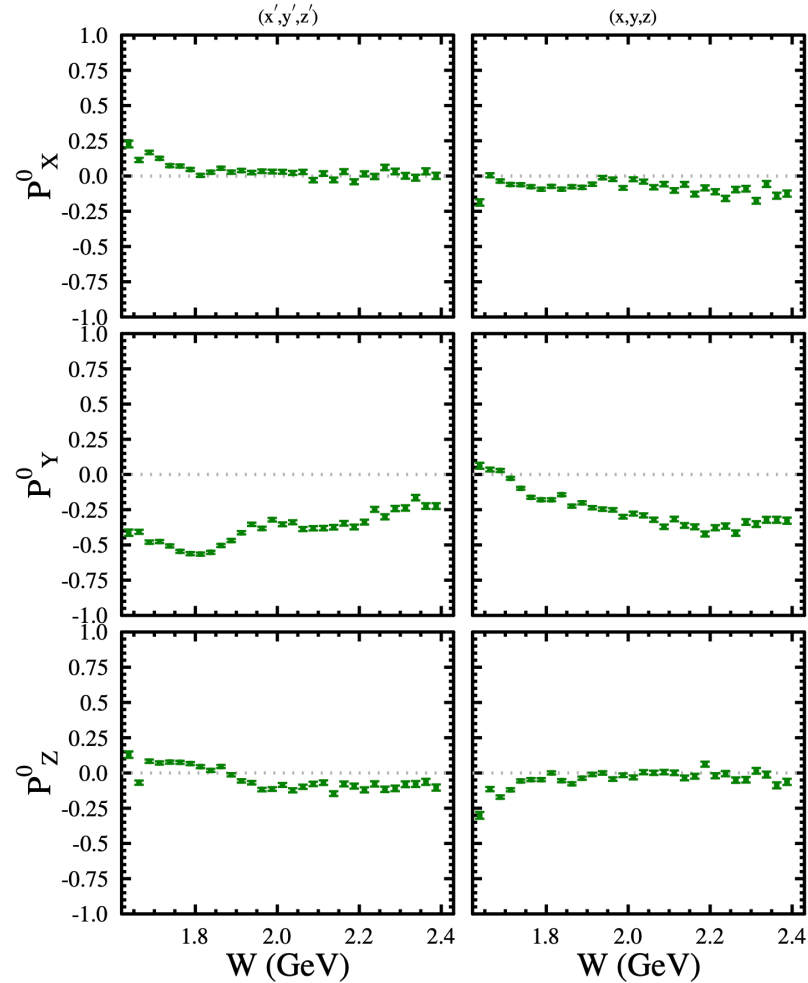
Data Polarization Results

$K^+\Lambda$



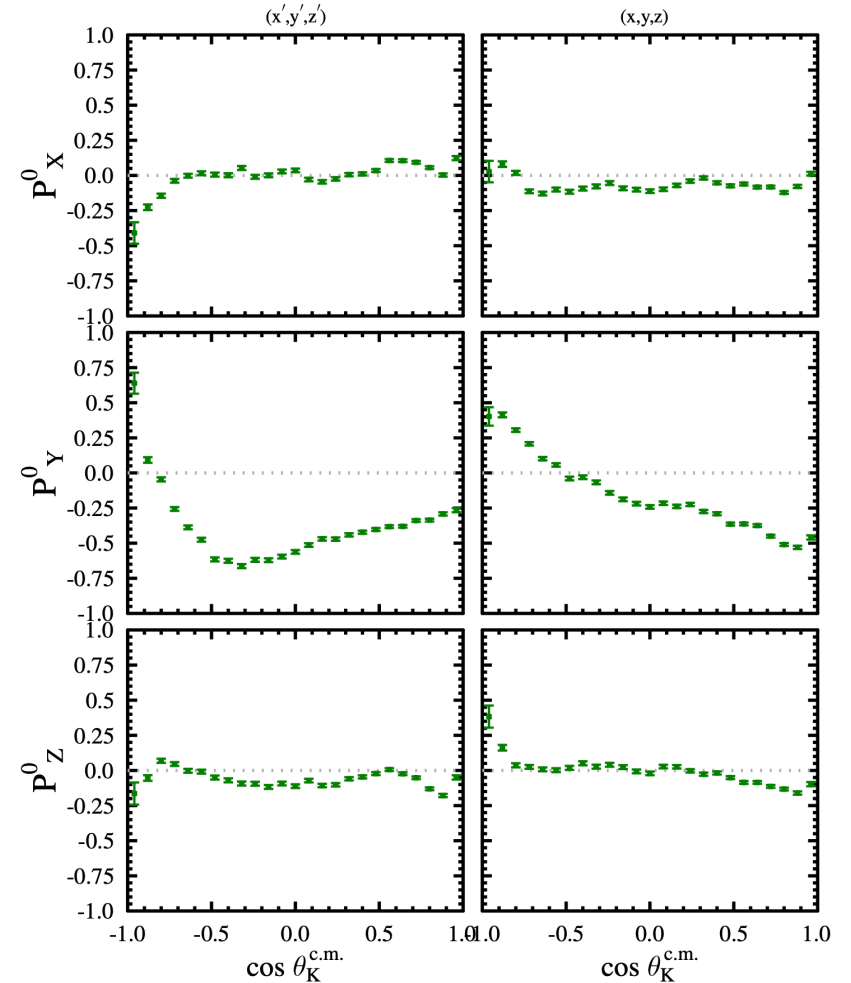
ipolq genKYn: p2v10

$K^+\Lambda$



ipolw genKYn: p2v10

$K^+\Lambda$



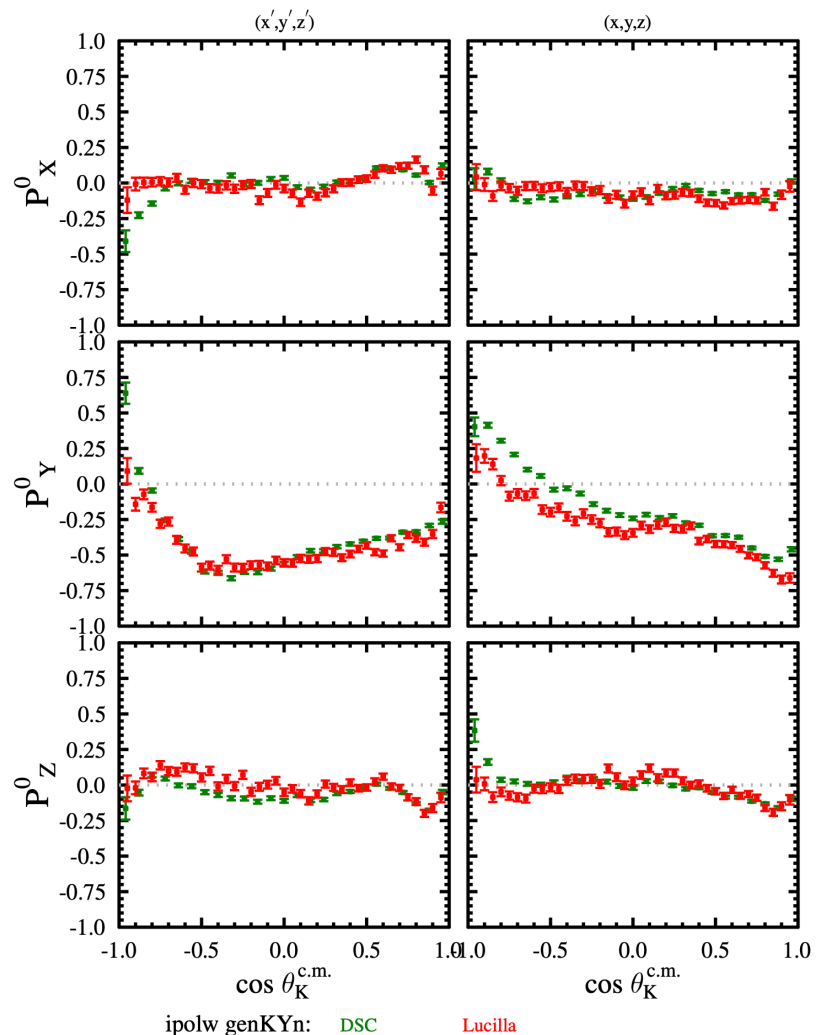
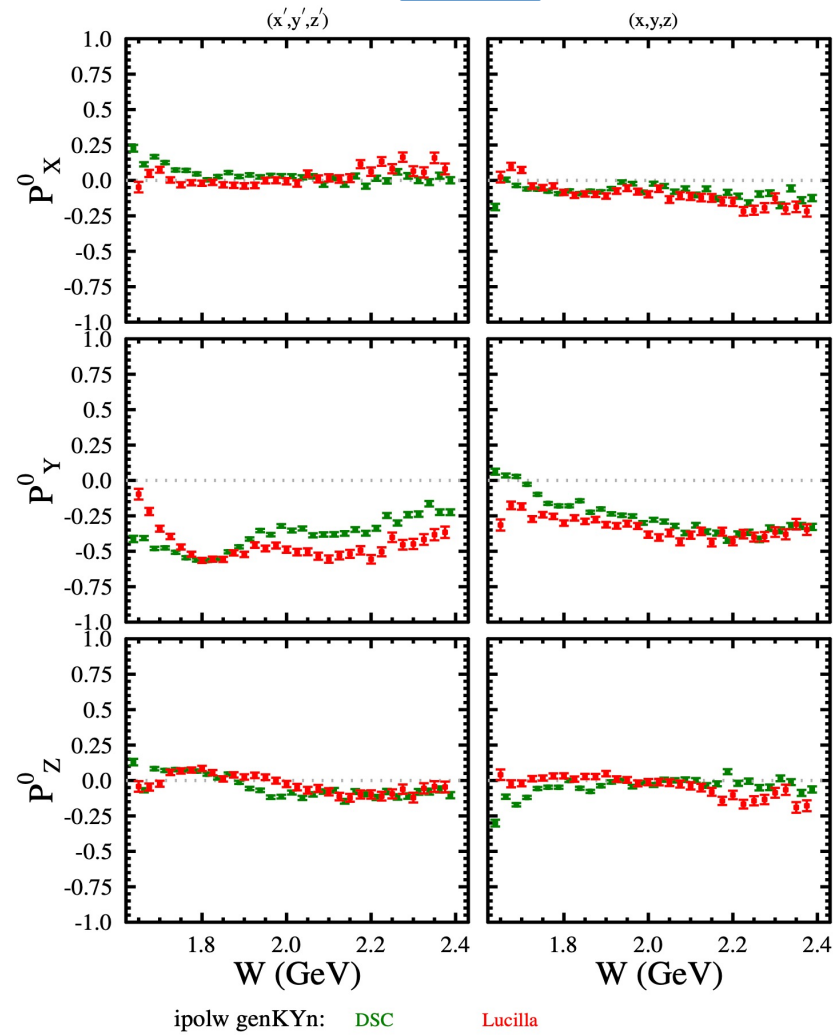
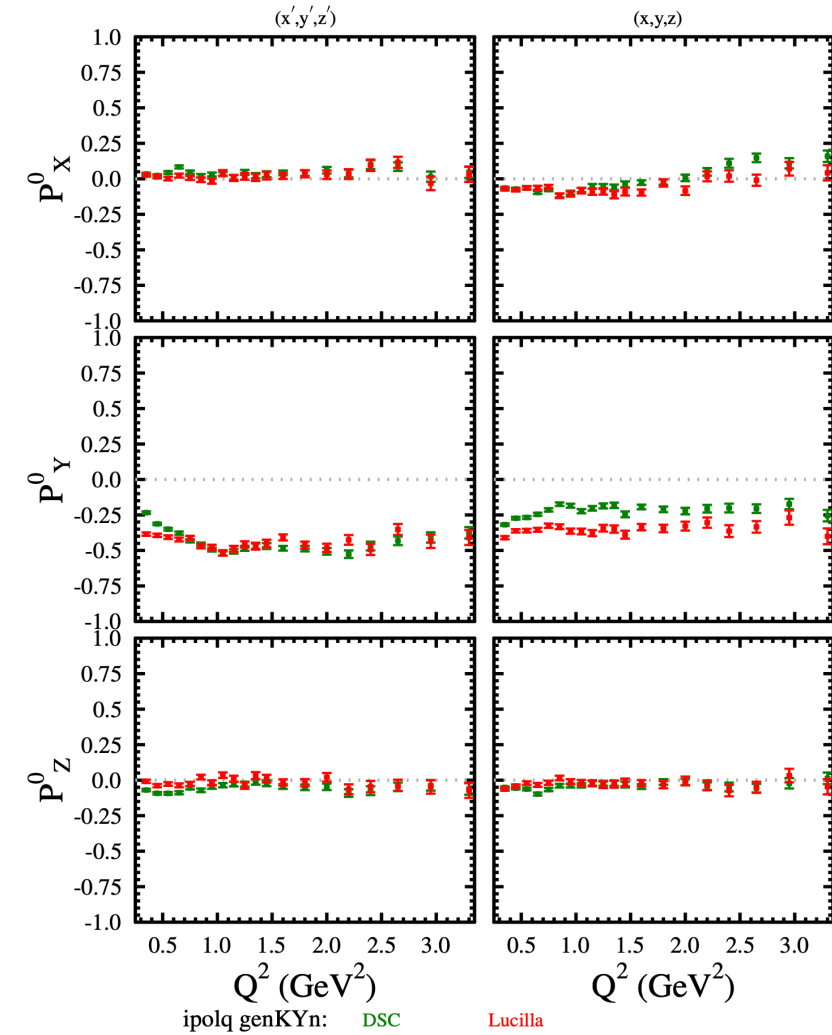
ipolw genKYn: p2v10

Data Polarization Results

$K^+\Lambda$

$K^+\Lambda$

$K^+\Lambda$

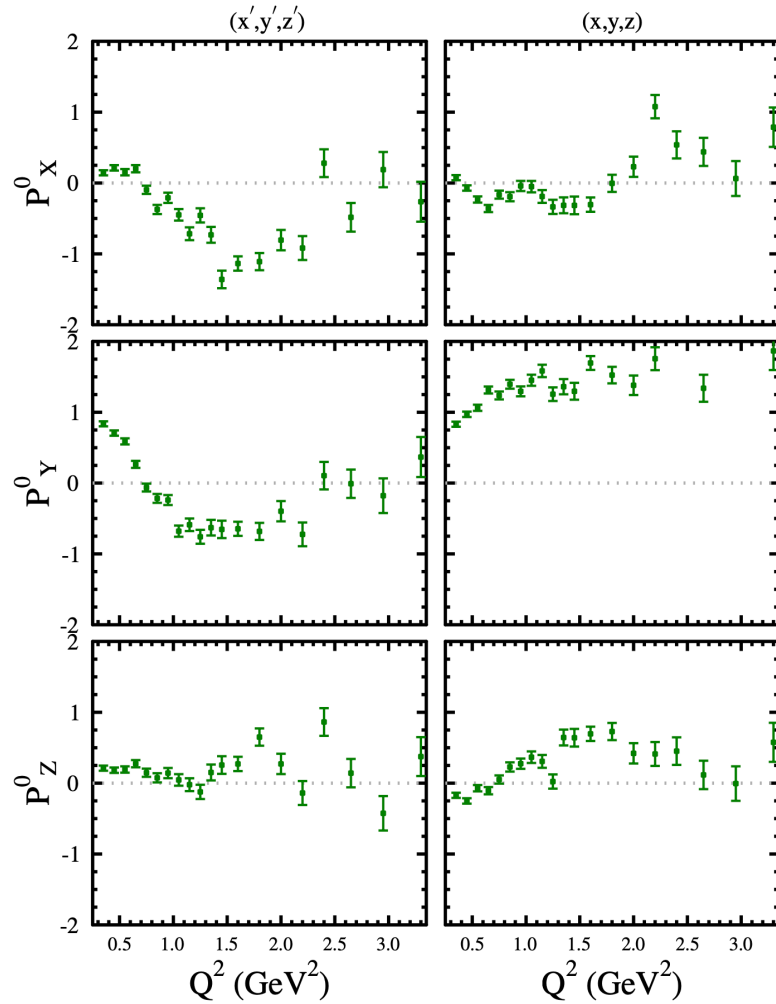


Comparison with parallel analysis by Lucilla Lanza

Data Polarization Results

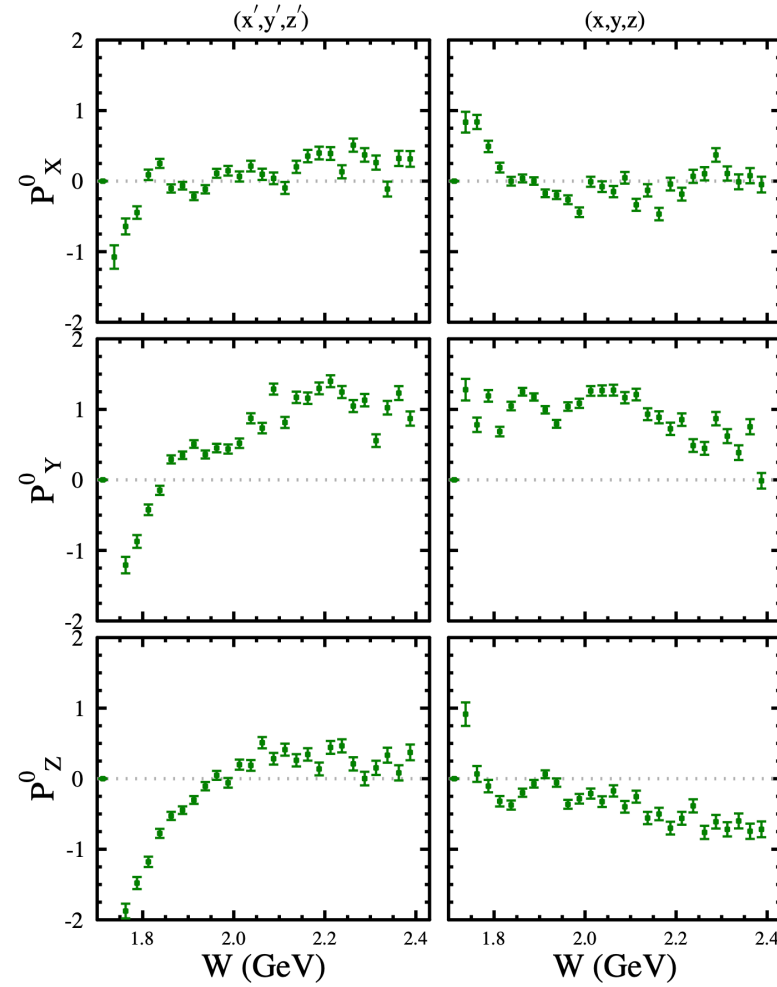
Issues are exposed here ...

$K^+\Sigma^0$



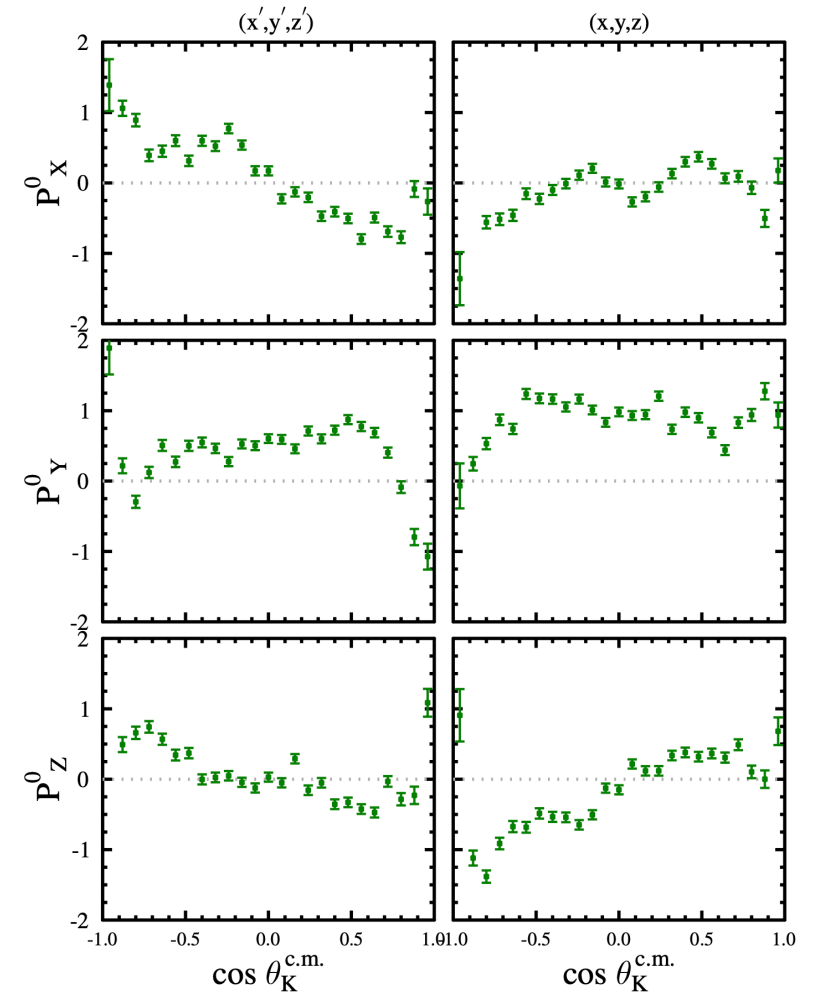
ipolc genKYn: ACC2D (p2v13g)

$K^+\Sigma^0$



ipolc genKYn: ACC2D (p2v13g)

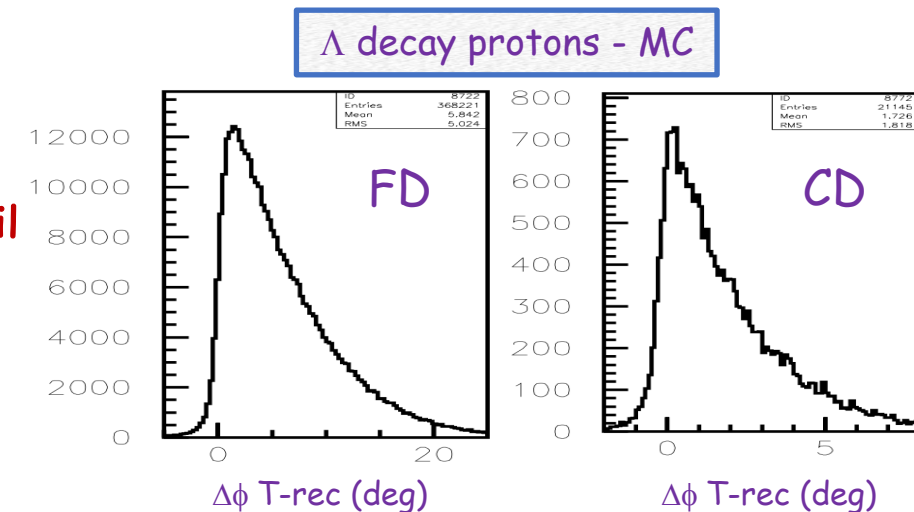
$K^+\Sigma^0$



ipolc genKYn: ACC2D (p2v13g)

Current Status of Analysis

- Significant advancement of the analysis has been made over the past year:
 - Updated event generator to include hyperon decays
 - Included resolution smearing of reconstructed Monte Carlo (significant time savings over old Gaussian convolution smearing)
 - Included model for electron radiation (necessary to account for full Λ radiative tail beneath Σ^0)
 - Developed improved momentum corrections for e' , K^+ , and p
 - A long list of systematic studies have been completed to understand effects on polarization components
- Still a number of hurdles to cross:
 - Model of radiation too crude; need proper theoretical approach
 - Model of resolution smearing too ad hoc and needs improvement
 - **Need to properly separate resolution smearing from radiative tail as polarization components are sensitive to these details**
 - Must account of reconstruction biases of detached vertex decays
 - U-Track bank removes bias of vertex constraint in CD
- I had hoped to bring the RG-K Win18 data to publication but understanding and reducing the systematics is taking time
 - Σ^0 results still non-physical (but have gotten much better with the recent work)
 - It likely makes sense to use Win18 to understand the issues and complete analysis on the Spr24 data with its much improved momentum resolution



Summary

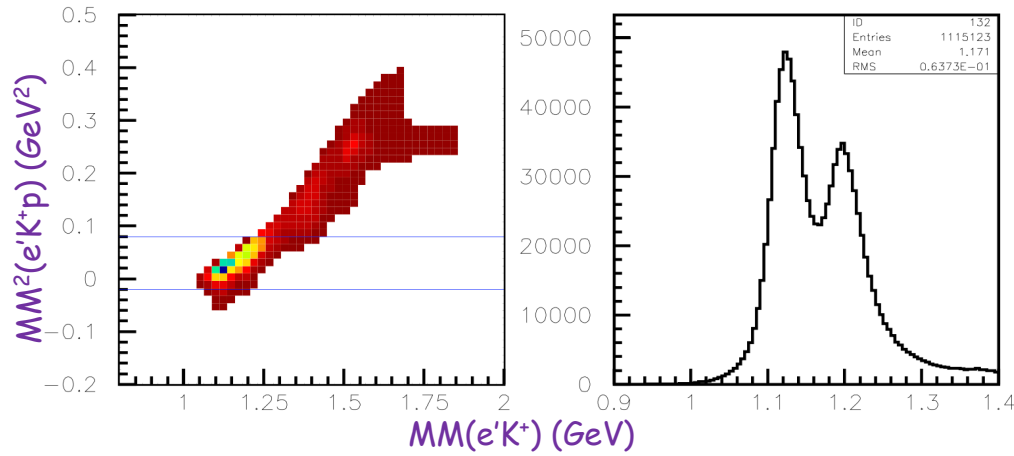
- As a companion analysis to the recent KY transferred polarization measurement, analysis of the KY recoil polarization is in progress.
 - Λ results are not so bad, but systematic uncertainties of ± 0.1 in P^0 are apparent, depending on Q^2 , W , $\cos \theta_K^{\text{c.m.}}$ and axis choice.
 - Σ^0 results have larger systematics - The scaling factor ($v_\Sigma = 1/0.256$) exposes the problems.
- The biggest remaining issue is the lack of proper radiative effects in the EG:
 - Need to properly separate radiative effects from resolution effects due to the sizable radiative tail from the Λ beneath the Σ^0 .
 - The improved resolution (expected) from the Spr24 data will be most welcome.
- The analysis of P^0 (and P') in a full multi-dimensional binning is important for the development of an accurate reaction model.
 - Extend the existing CLAS P^0 measurements for $K^+\Lambda$.
 - The measurements of P^0 for $K^+\Sigma^0$ are the new observable.

Backup

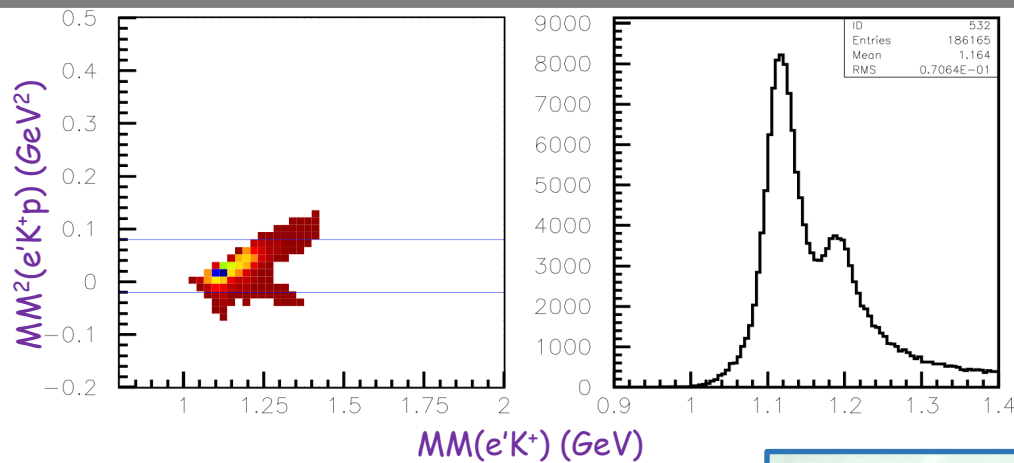
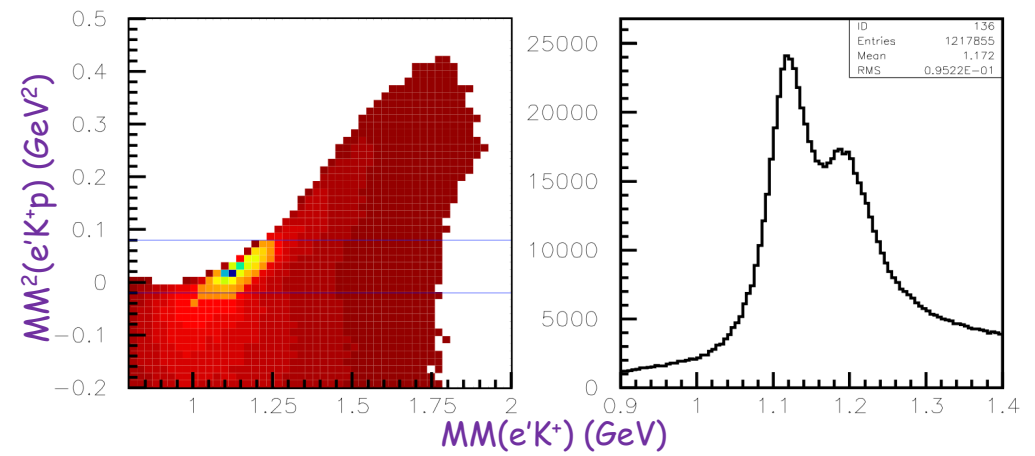
e'K⁺p Topologies

Favored Topologies

K⁺ forward, p forward

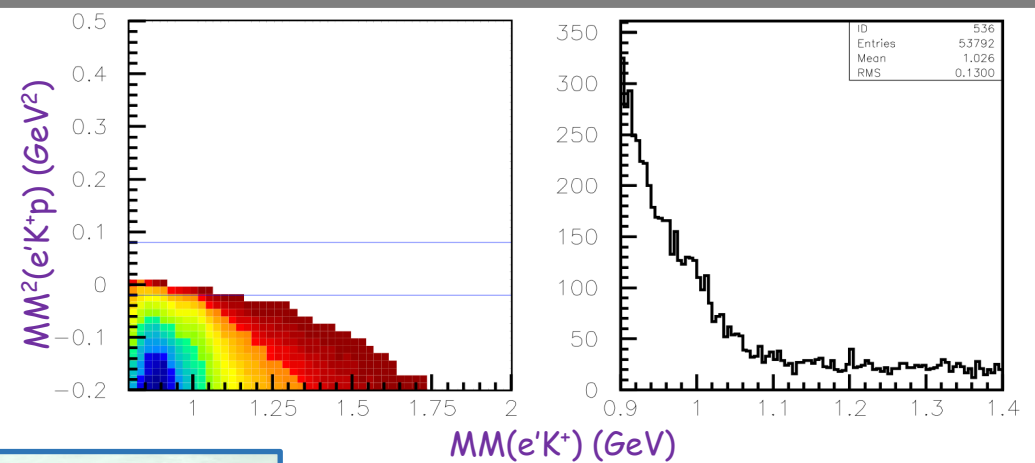


K⁺ central, p forward



K⁺ forward, p central

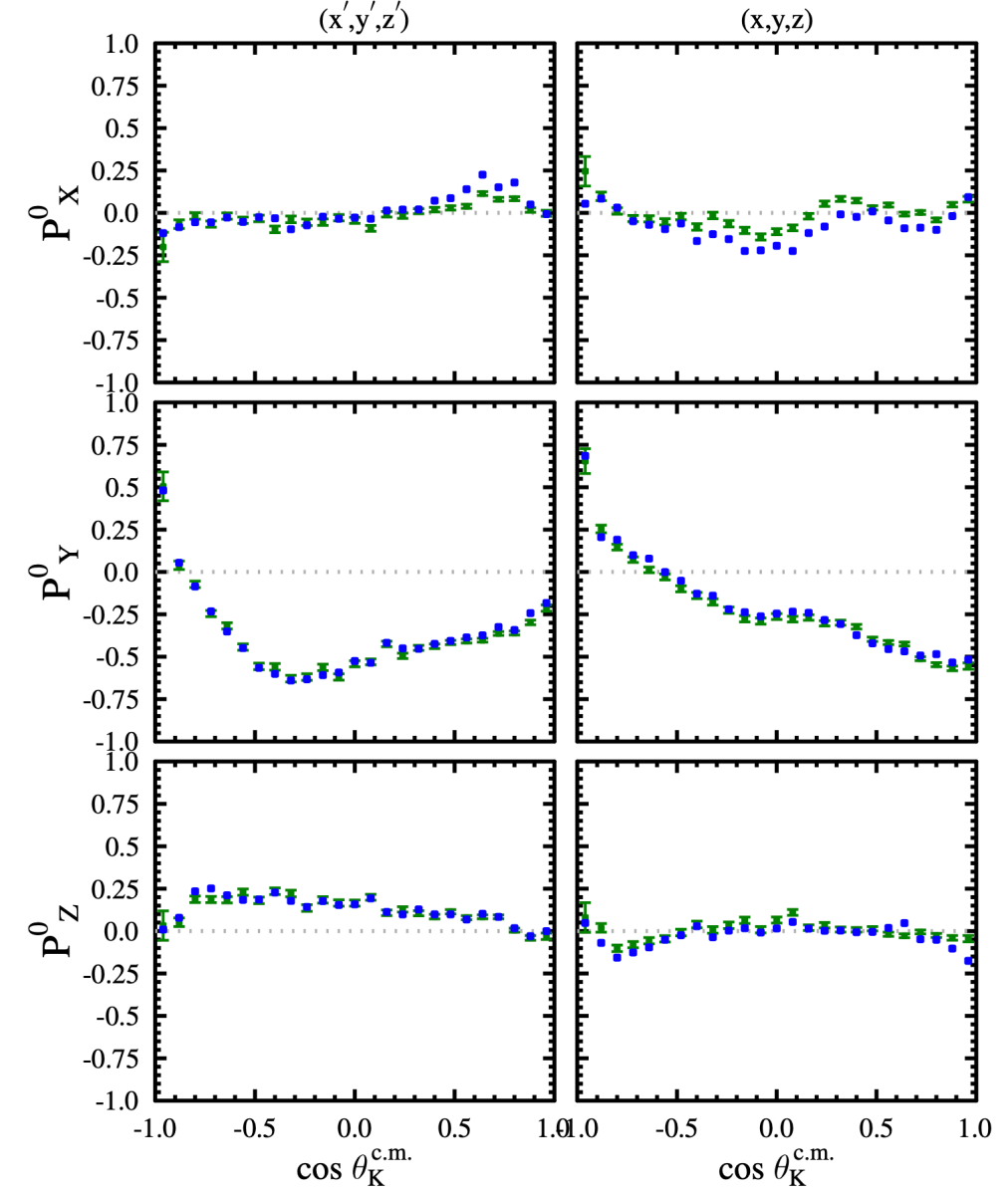
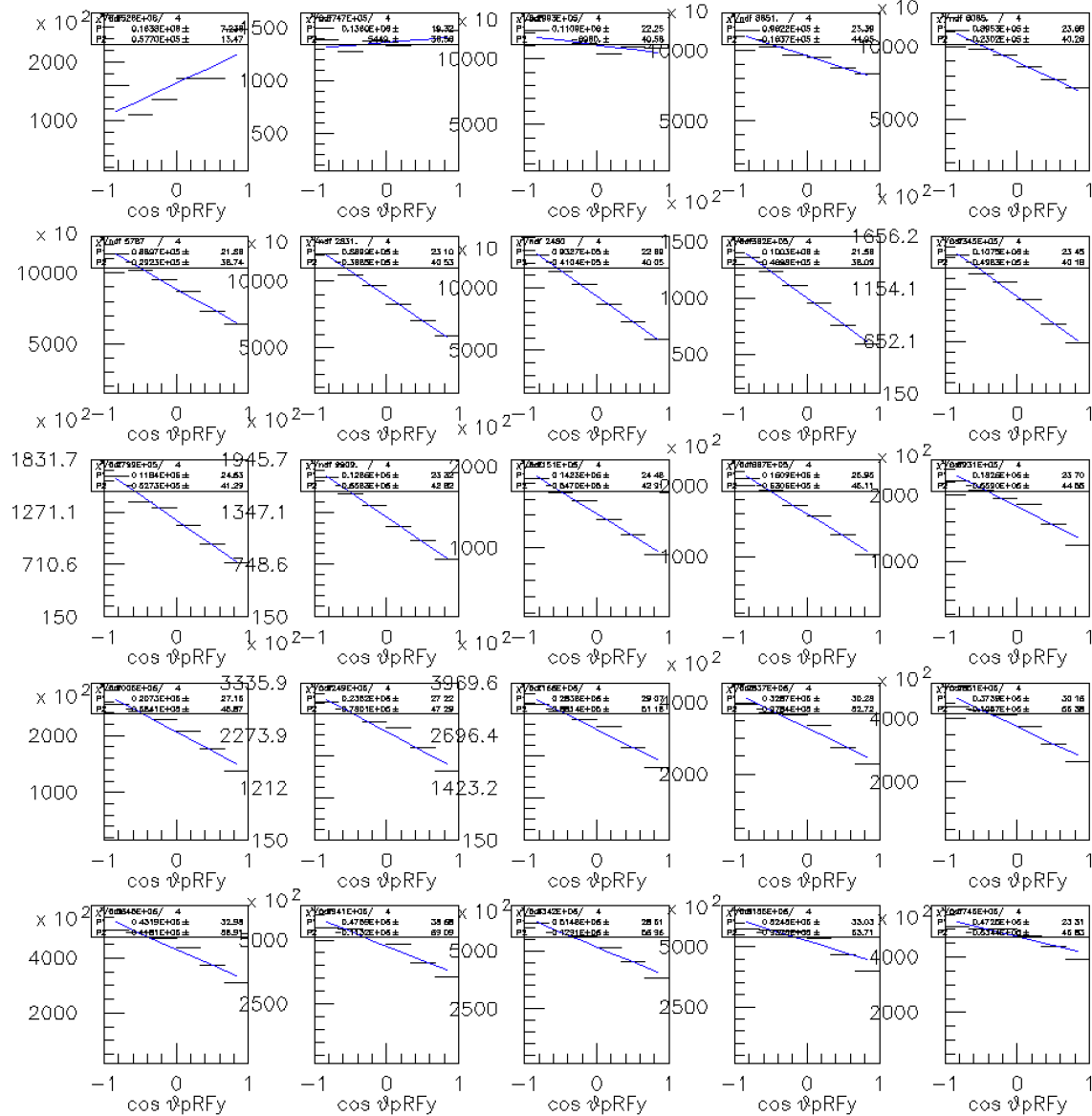
Unfavored Topologies



K⁺ central, p central

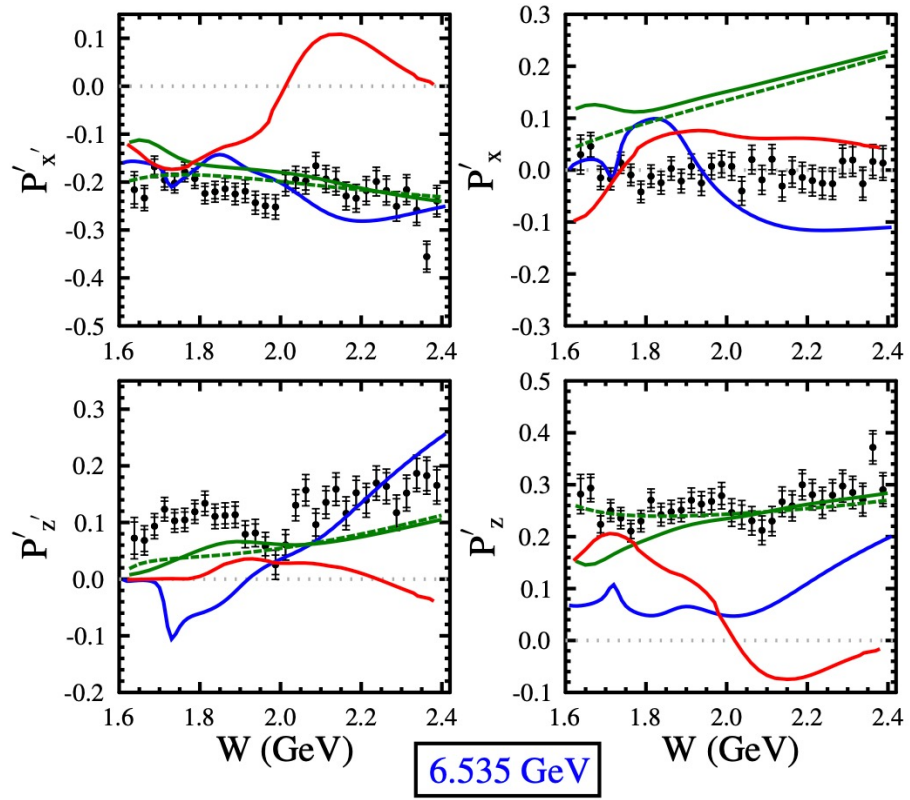
Data Polarization Results

Increasing N_{bins}

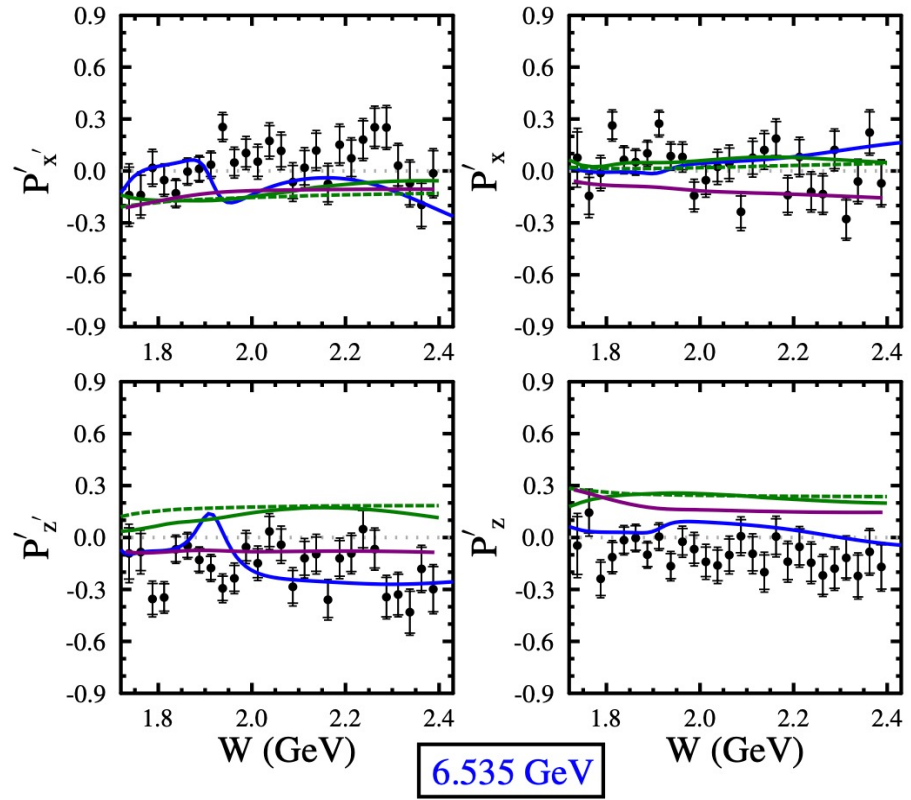


CLAS12 KY Beam-Recoil Transferred Polarization

$K^+\Lambda$



RG-K
Win18



$K^+\Sigma^0$

Model	Year	Type	Fit Data	N* States
Kaon-MAID	2000	Isobar	none	1/2, 3/2
RPR	2011	Isobar+Regge	CLAS γp	1/2, 3/2, 5/2
BS3	2018	Isobar	CLAS γp & ep	1/2, 3/2, 5/2

Model	Year	Type	Fit Data	N* States
SL	1996	Isobar	none	1/2, 3/2
Kaon-MAID	2000	Isobar	none	1/2, 3/2
RPR	2007	Isobar+Regge	CLAS γp	1/2, 3/2, 5/2

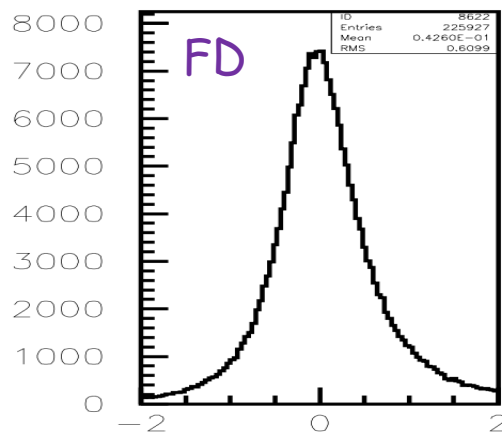
Extract KY P' vs. $Q^2, W, \cos \theta_K^{c.m.}$

Detached Vertex ϕ Bias

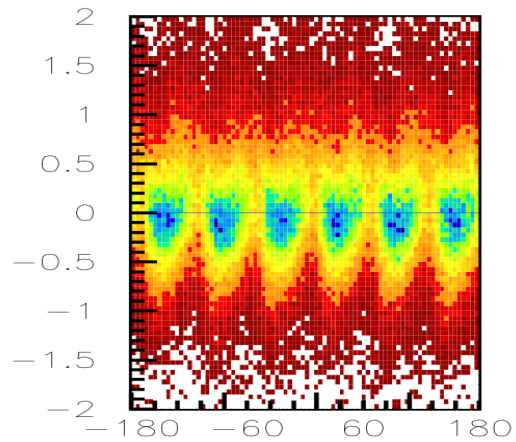
K⁺ reconstruction

Monte Carlo

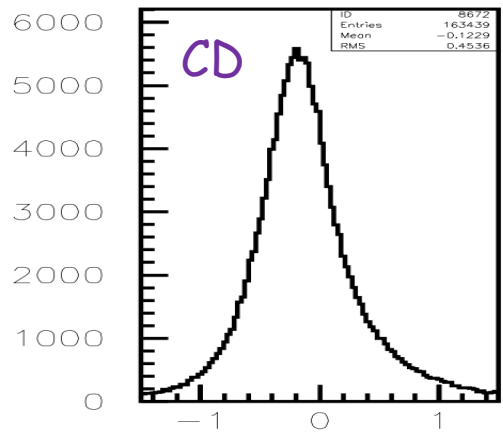
p reconstruction



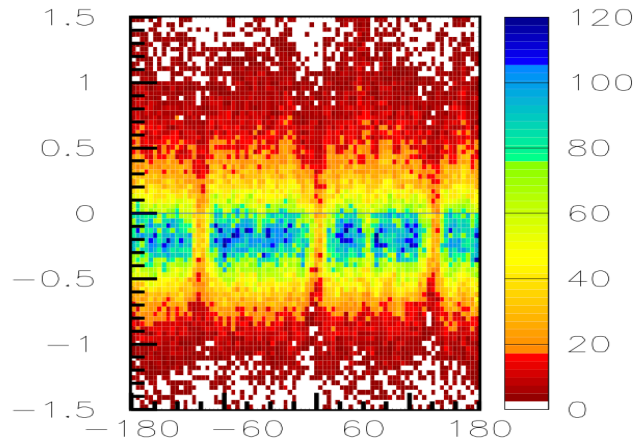
$\Delta\phi_{Kf}$ T-rec



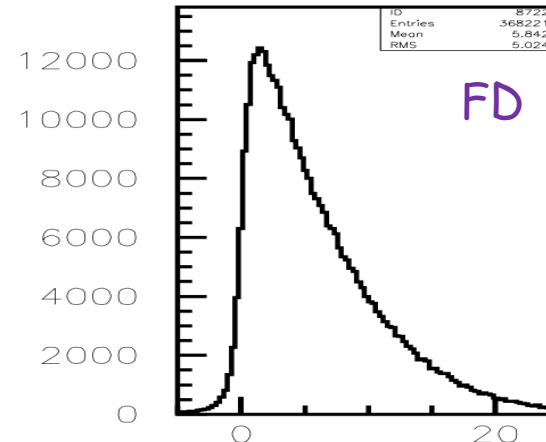
$\Delta\phi_{Kf}$ (T-rec) vs. ϕ_{Kf} rec



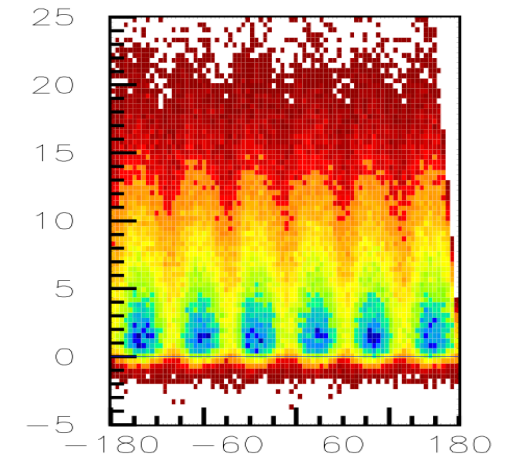
$\Delta\phi_{Kc}$ T-rec



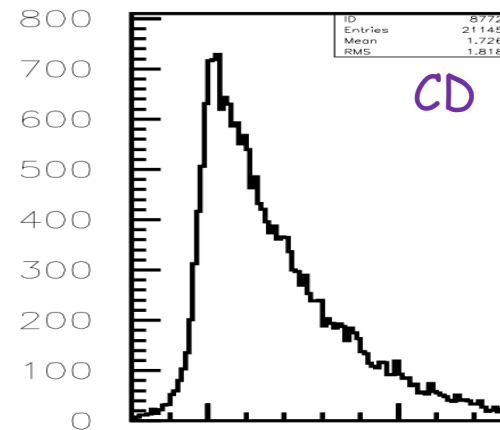
$\Delta\phi_{Kc}$ (T-rec) vs. ϕ_{Kc} rec



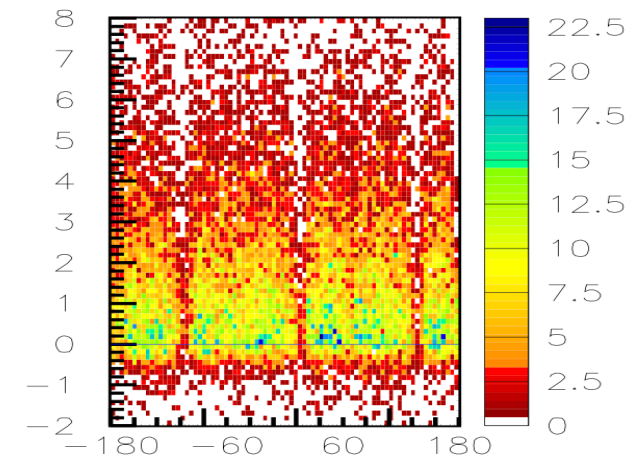
$\Delta\phi_{pf}$ T-rec



$\Delta\phi_{pf}$ (T-rec) vs. ϕ_{pf} rec



$\Delta\phi_{pc}$ T-rec



$\Delta\phi_{pc}$ (T-rec) vs. ϕ_{pc} rec