

# Measurements of the $\text{Cos}\phi$ and $\text{Cos}2\phi$ Moments of the Unpolarized SIDIS $\pi^+$ Cross-section at CLAS12

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CLAS Collaboration 2024

LinkedIn



# Motivation

- Semi-Inclusive Deep Inelastic Scattering (SIDIS) experiments allow us to address questions about the 3D structure of nucleons
- Azimuthal modulations in unpolarized SIDIS cross-section for charged pion electroproduction can give access to the Cahn and Boer-Mulders effects
  - **Boer-Mulders Effect:** Sensitive to the correlation between the quark's transverse momentum and intrinsic transverse spin in an unpolarized nucleon
  - **Cahn Effect:** Sensitive to the transverse motion of quarks inside the nucleon
- A non-zero Boer-Mulders requires quark orbital angular momentum contributions to the proton spin (aspect of the proton missing spin puzzle)

# SIDIS Cross-Section and Boer-Mulders

The lepton-hadron Unpolarized SIDIS Cross-Section:

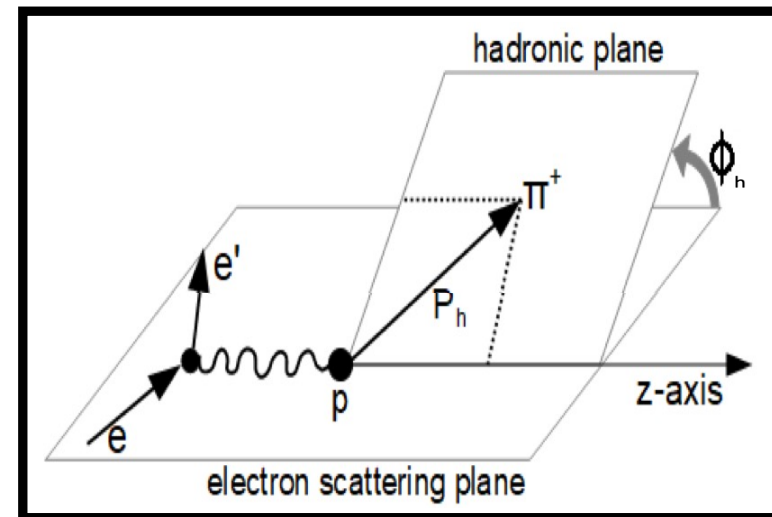
$$\frac{d^5\sigma}{dydQ^2dzd\phi_h dP_{h\perp}^2} = \underbrace{\frac{x_B}{y} \frac{2\pi\alpha^2}{x_B y Q^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x_B}\right) (F_{UU,T} + \epsilon F_{UU,L})}_{A_0} \left\{ 1 + \underbrace{\frac{\sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos\phi_h}} \cos\phi_h + \underbrace{\frac{\epsilon F_{UU}^{\cos 2\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos 2\phi_h}} \cos 2\phi_h \right\}$$

The Boer-Mulders and Cahn effects are present in the Structure Functions:

leading twist  $F_{UU}^{\cos 2\phi_h} \propto C \left[ \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{MM_h} h_1^\perp H_1^\perp + \dots \right]$  BOER-MULDERS EFFECT

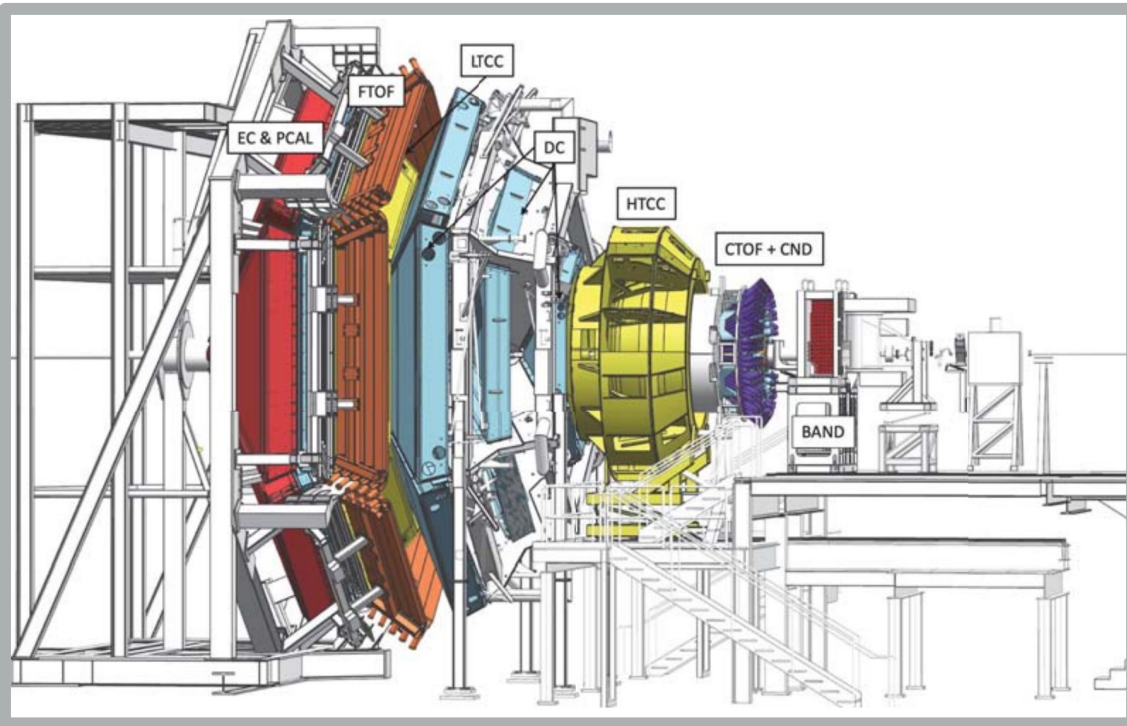
next to leading twist  $F_{UU}^{\cos\phi_h} \propto \frac{2M}{Q} C \left[ \frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} x h H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1 + \dots \right]$  CAHN EFFECT

Interaction dependent terms neglected



Reaction Studied:  $e p \rightarrow e \pi^+(X)$

# Data Collection



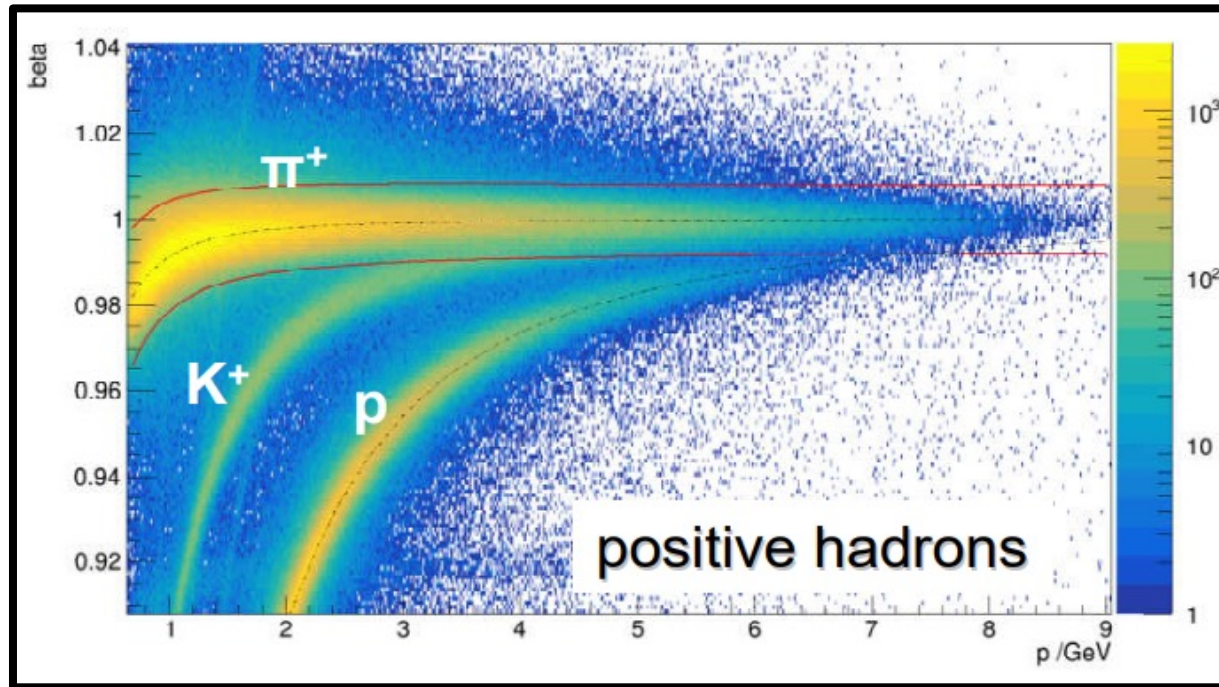
CLAS12 Detector

- CLAS12 detector in Hall B at Jefferson Lab
  - Upgrade from the CLAS detector
  - Enabled the higher energy and statistics for our experiments, not previously accessible
- Data from the Fall 2018 RG-A experiment
  - Used a 10.6 GeV polarized electron beam and unpolarized liquid hydrogen target
- Data presented uses forward tracking only

# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum



\*Image provided by Stefan Diehl

$\pi^+$  Pion PID –  $\beta$  vs  $p$

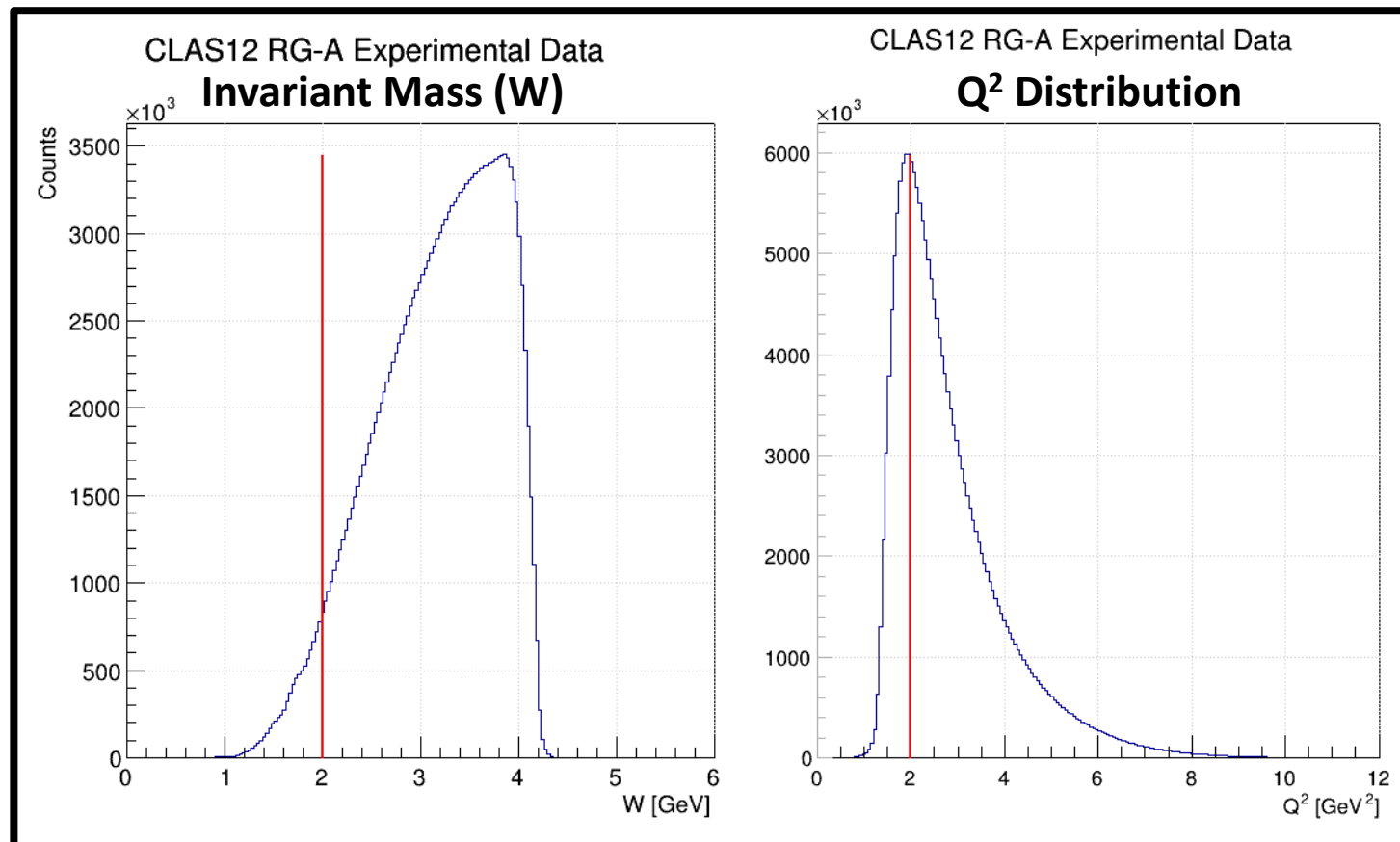
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## Analysis Cuts:

- **SIDIS Cuts:**
  - $W > 2 \text{ GeV}$
  - $Q^2 > 2 \text{ GeV}^2$



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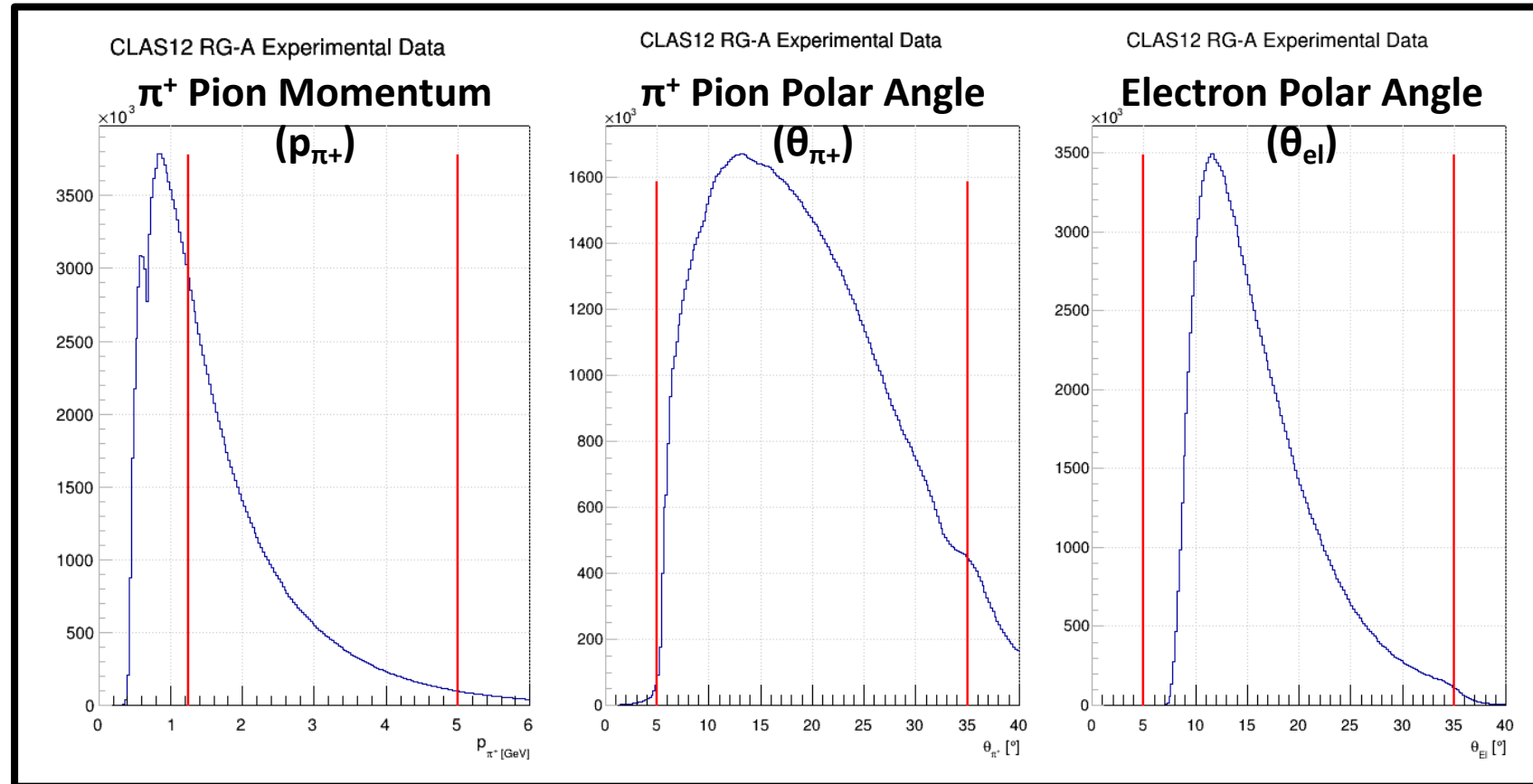
## Analysis Cuts:

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- **Other Analysis Cuts:**

- $p_{\pi^+}$  Cut:  $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- $\theta$ -angle Cut:  $5^\circ < \theta_{\text{particle}} < 35^\circ$



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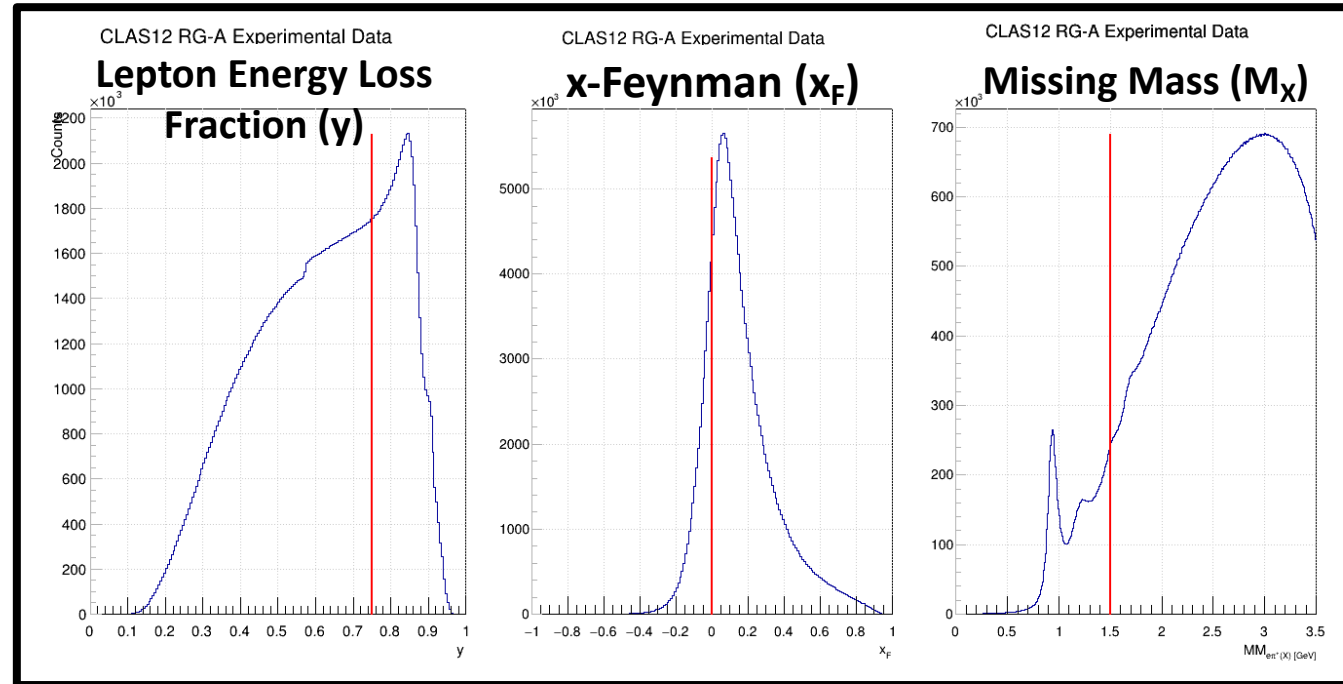
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- $\theta$ -angle Cut:  $5^\circ < \theta_{\text{particle}} < 35^\circ$
- $y < 0.75$  (minimize other background processes)
- $x_F > 0$  (minimize contributions from target fragmentations)
- Missing Mass Cut:  $M_X > 1.5 \text{ GeV}$  (limits contributions from exclusive events)





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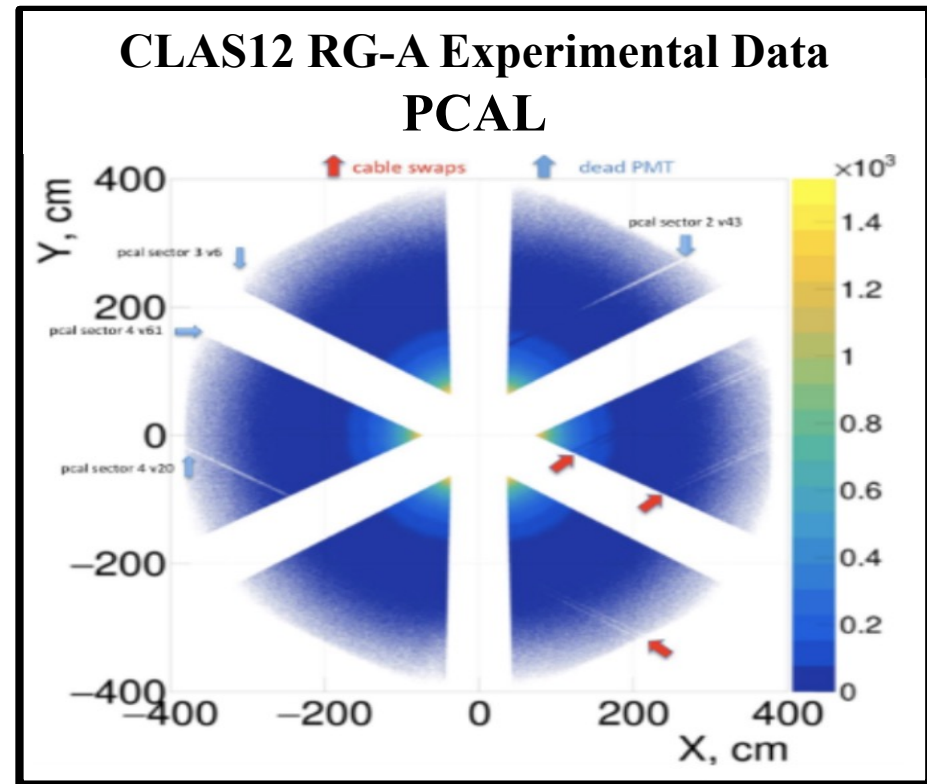
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- $x_F > 0$  (minimize contributions from target fragmentations)
- Missing Mass Cut:  $M_x > 1.5 \text{ GeV}$  (limits contributions from exclusive events)
- Fiducial Cuts (e.g., accounts for bad channels present in data)



# Analysis Procedure

## Experimental extraction of cross-section

$$\frac{d^5\sigma}{dQ^2 dy dP_T dz d\phi_h} = \frac{1}{\Gamma_\nu} \frac{1}{\Delta Q^2 \Delta y \Delta P_T \Delta z \Delta \phi_h} \frac{N}{R \cdot BC \cdot \eta \cdot N_0} \frac{1}{(N_A \cdot \rho \cdot t / A_w)}$$

Where:

Bin Volume

Target Number Density

- R = Radiative Correction
- $\eta$  = **Acceptance Correction** → Requires Monte Carlo (MC) Simulation
- N = Bin Yields
- $N_0$  = Life-time corrected incident electron flux
- BC = factor which evolves bin-averaged differential cross-section

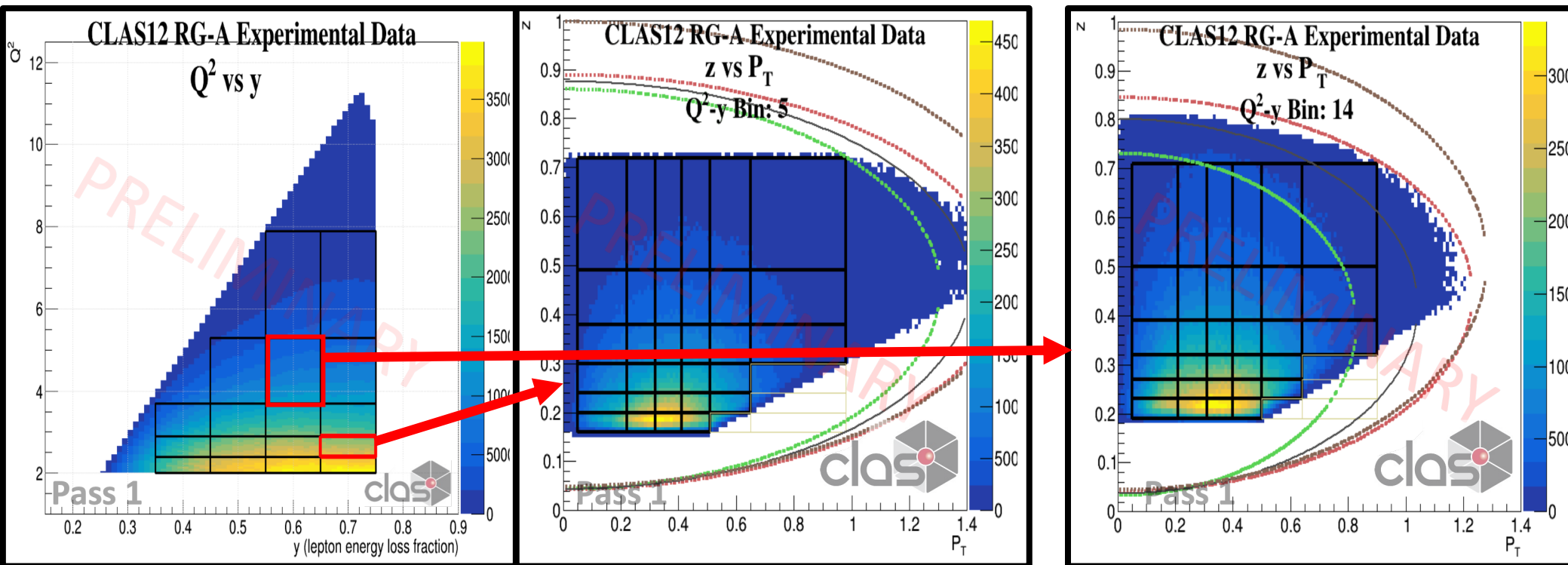
SIDIS MC are generated with LEPTO event generator

# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (4 Dimensions)

17  $Q^2$ - $y$  Bins Total – 25-36  $z$ - $P_T$  Bins (per  $Q^2$ - $y$  bin)

Examples of new binning scheme using  $Q^2$ ,  $y$ ,  $z$ , and  $P_T$



Lines drawn here show regions affected by the Missing Mass Cut

Missing Mass Cut Lines:

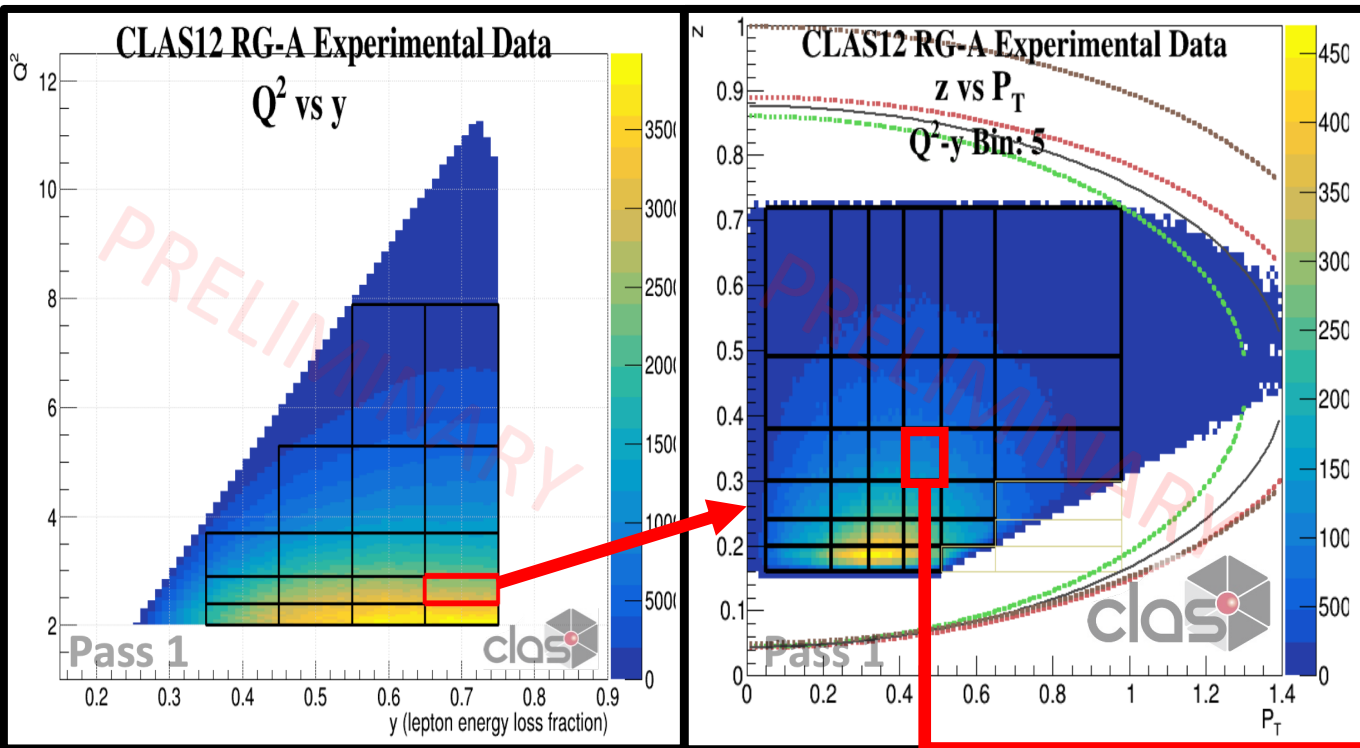
- ..... Minimum MM Cut
- ..... Maximum MM Cut
- Center MM Cut
- ..... Center (Neutron) MM Cut

# Multidimensional Analysis Procedures

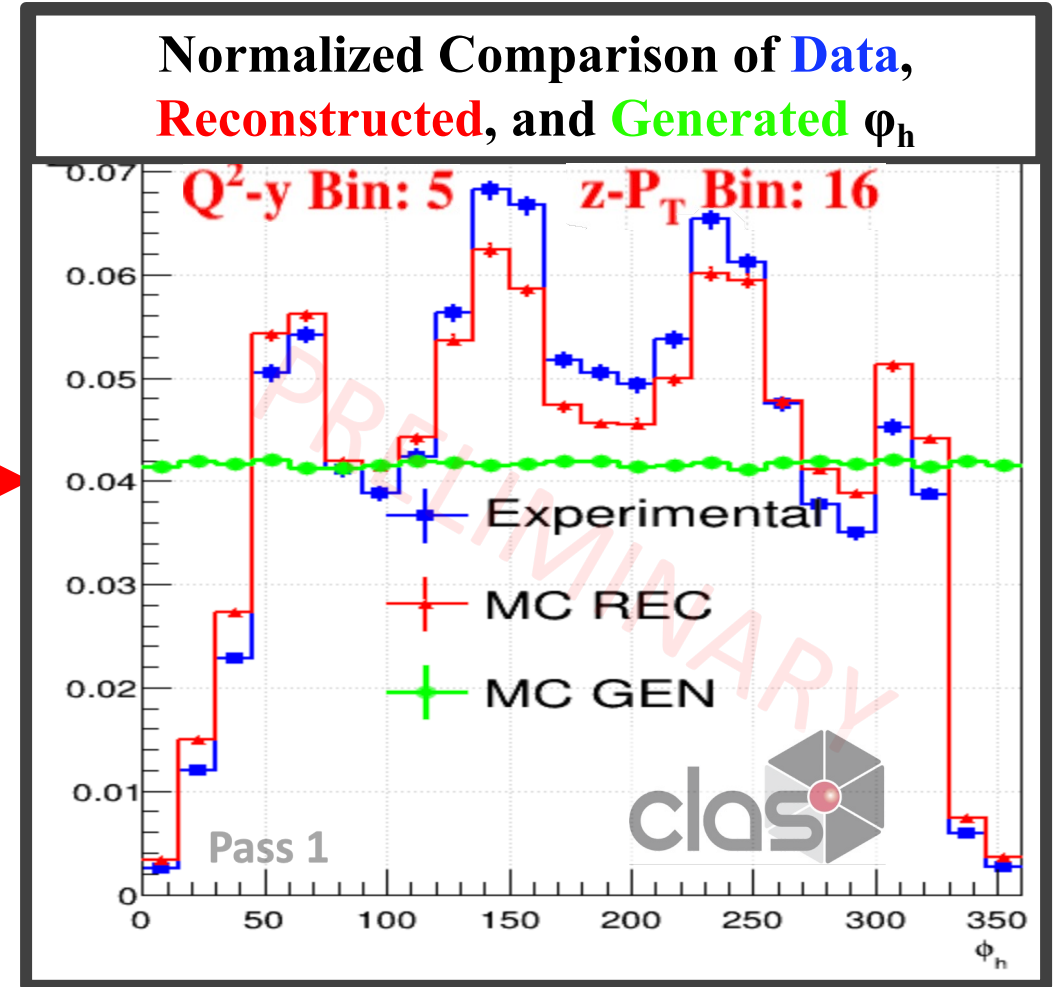
## Multidimensional Kinematic Binning (5 Dimensions)

17  $Q^2$ - $y$  Bins Total – 25-36  $z$ - $P_T$  Bins (per  $Q^2$ - $y$  bin)

$\phi_h$  distribution for the  $Q^2$ - $y$ - $z$ - $P_T$  bin shown in red



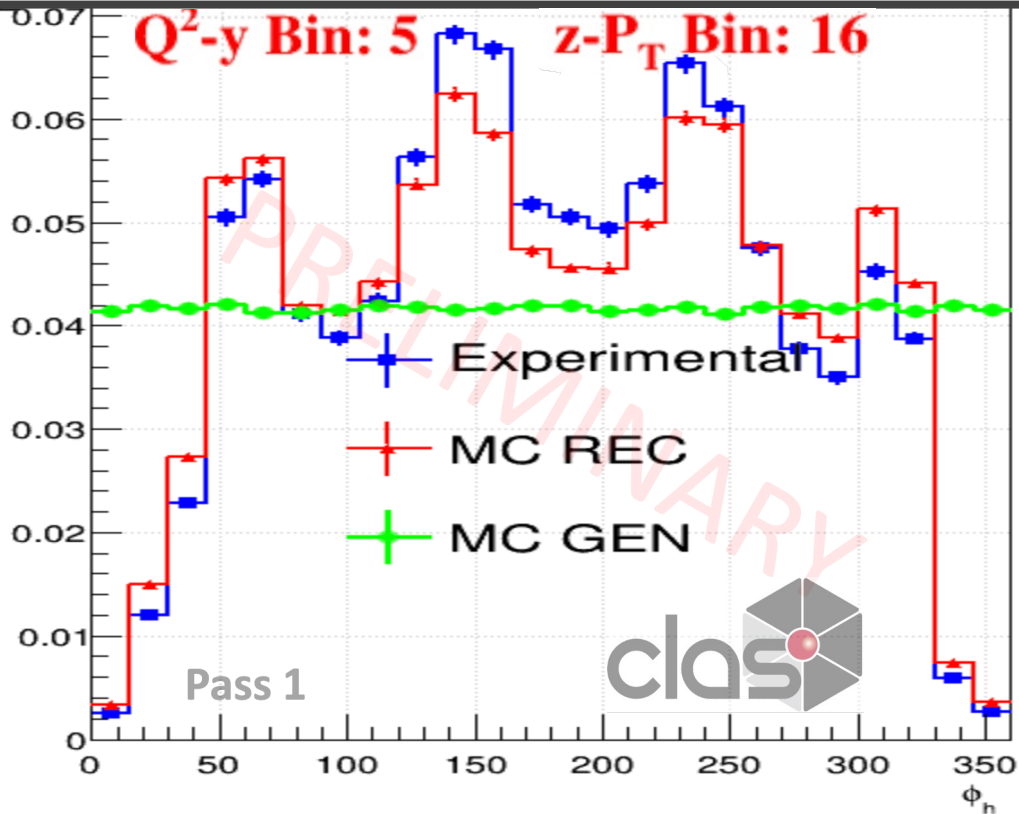
Missing Mass Cut Lines:



# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (5 Dimensions)

Normalized Comparison of **Data**,  
**Reconstructed**, and **Generated**  $\phi_h$



Apply  
Multidimensional  
Acceptance  
Corrections and  
convert to a  
cross-section  
measurement

$\phi_h$  fit for  
every bin

$A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$   
Where the parameters A, B, C  
give the cross-section moments

$$A_{UU}^{\cos \phi_h} = B \quad A_{UU}^{\cos 2\phi_h} = C$$

### Methods used for Acceptance Corrections:

- **Bin-by-bin Correction**
  - Simple method which just needs the 1D plots shown here
- **Bayesian Unfolding**
  - Bayesian Unfolding Method uses Acceptance Matrices to correct the data

# Acceptance Corrections and Bin Migration Study

- **Acceptance Matrix:**  $A_{(i,j)}$  describes both Acceptance (including geometric acceptance and detector efficiency) and Bin Migration
- $$A_{(i,j)} = \frac{\text{Number of Events Generated in bin } j \text{ but Reconstructed in bin } i}{\text{Total Number of Events Generated in the } j\text{th bin}}$$
- Acceptance Unfolding:  $Y_i = A_{(i,j)}X_j + \beta_i \Leftrightarrow X_j = A_{(i,j)}^{-1}(Y_i - \beta_i)$

where:

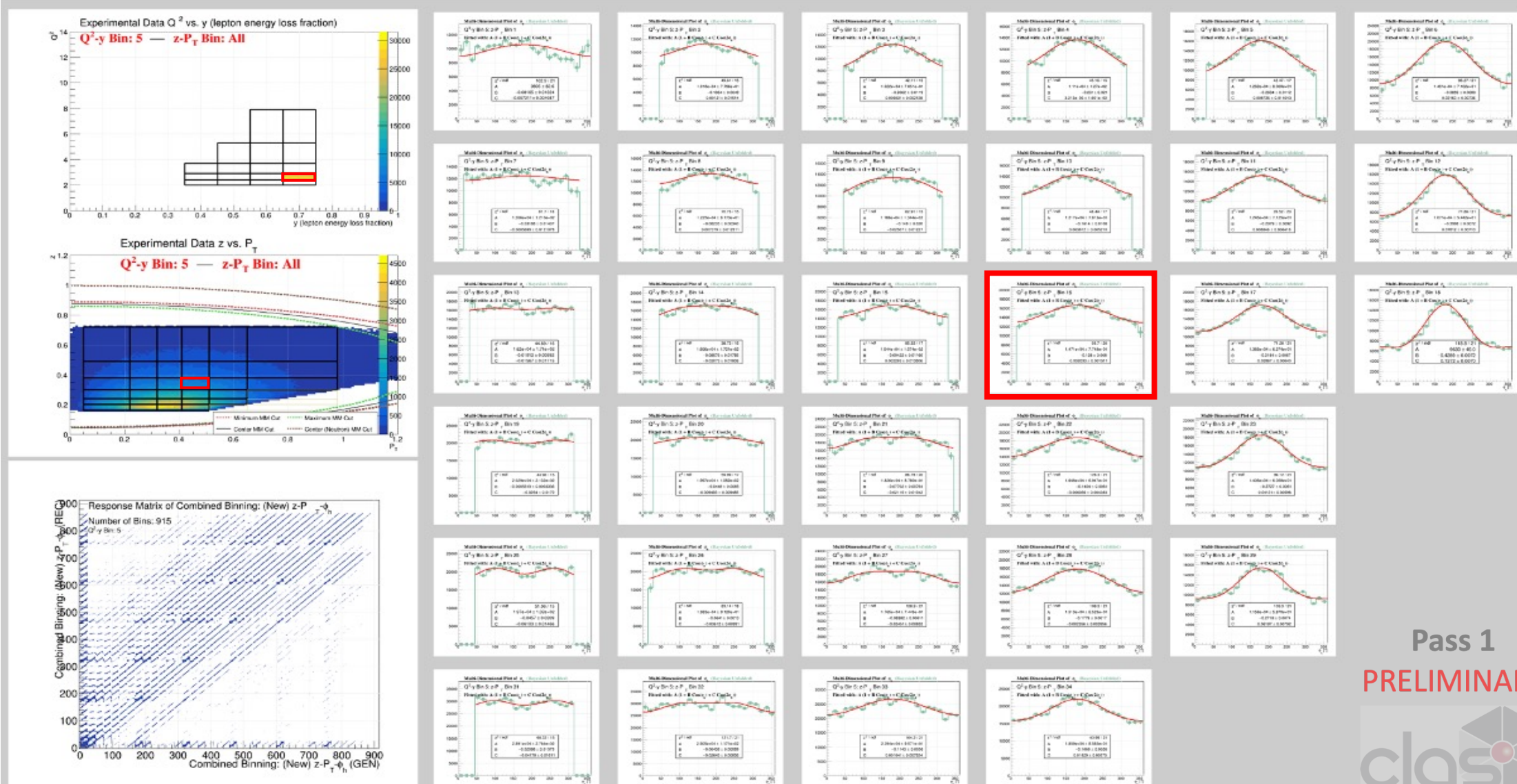
- $Y_i$  = Number of events experimentally measured in the  $i$ -th bin
- $X_j$  = Number of acceptance-corrected events in the  $j$ -th bin
- $\beta_i$  = Number of events from outside the signal region measured in the  $i$ -th bin

# Example of (3D) Unfolding Procedure

Using the Flattened  $z$ - $P_T$ - $\phi_h$  Multidimensional Bins

$Q^2$ -y Bin 5

Unfolded with Bayesian Method



Pass 1

PRELIMINARY



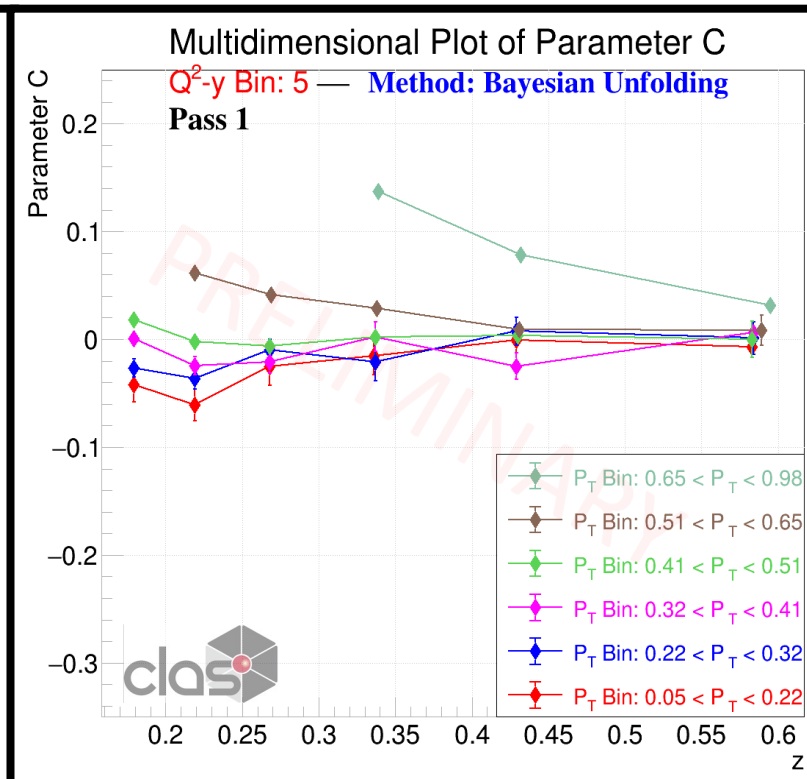
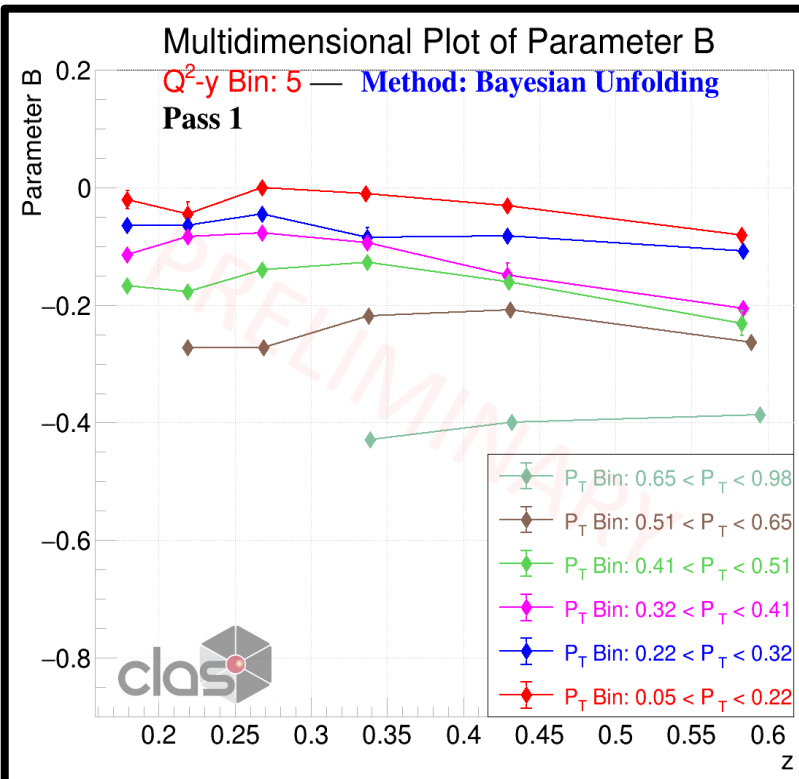
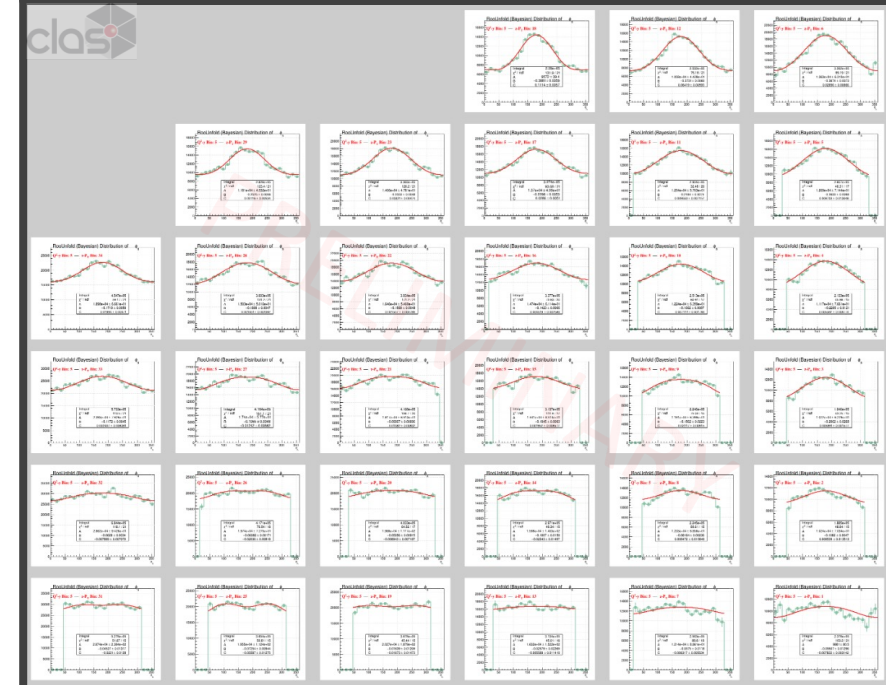
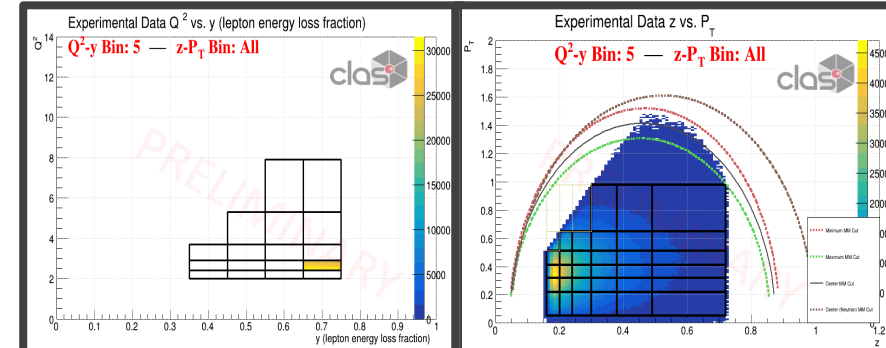
# Cosine Moments as Functions of z – Pass 1

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

$Q^2$ -y Bin 5





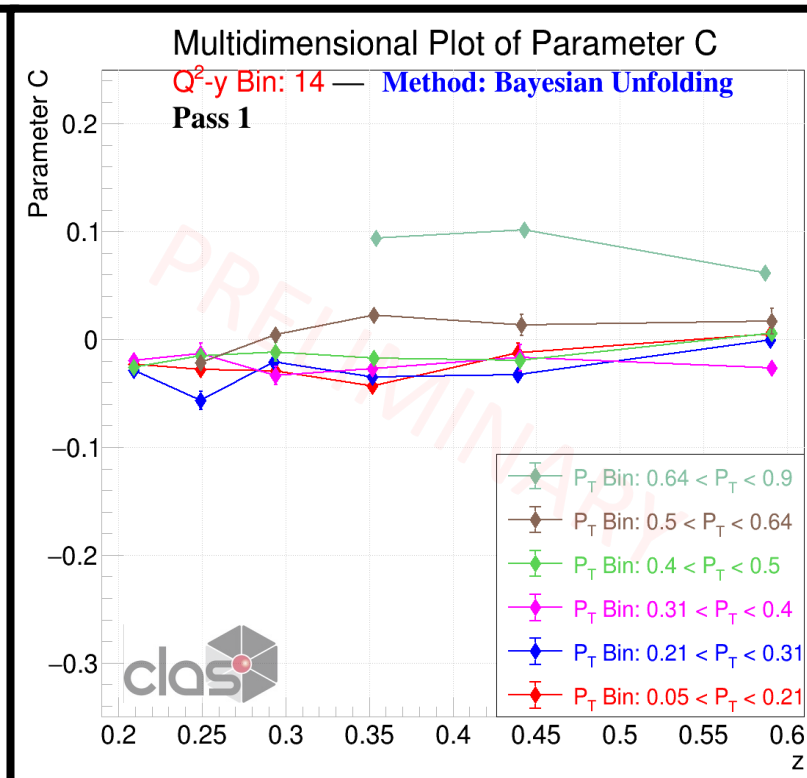
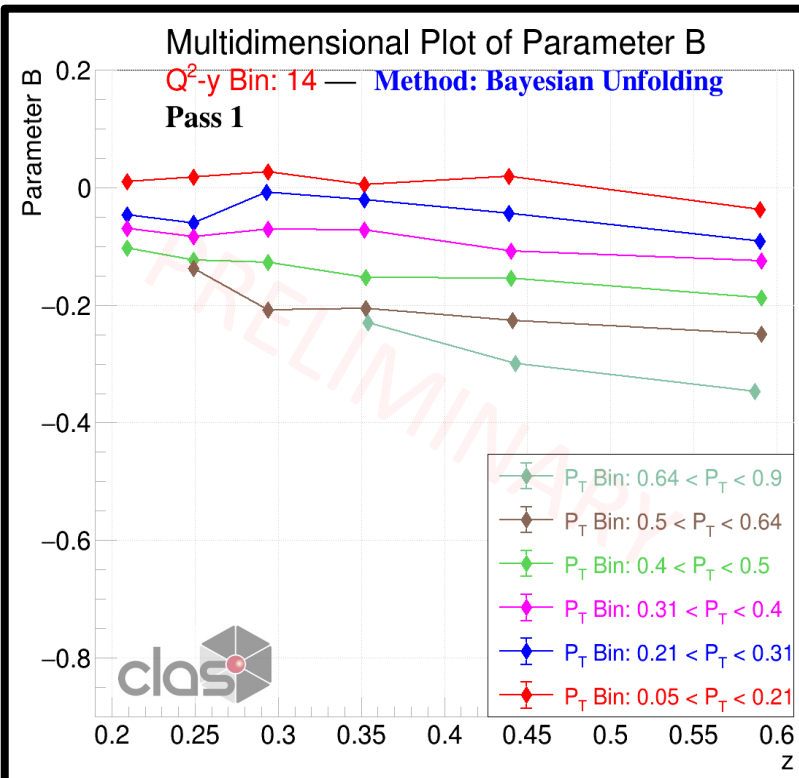
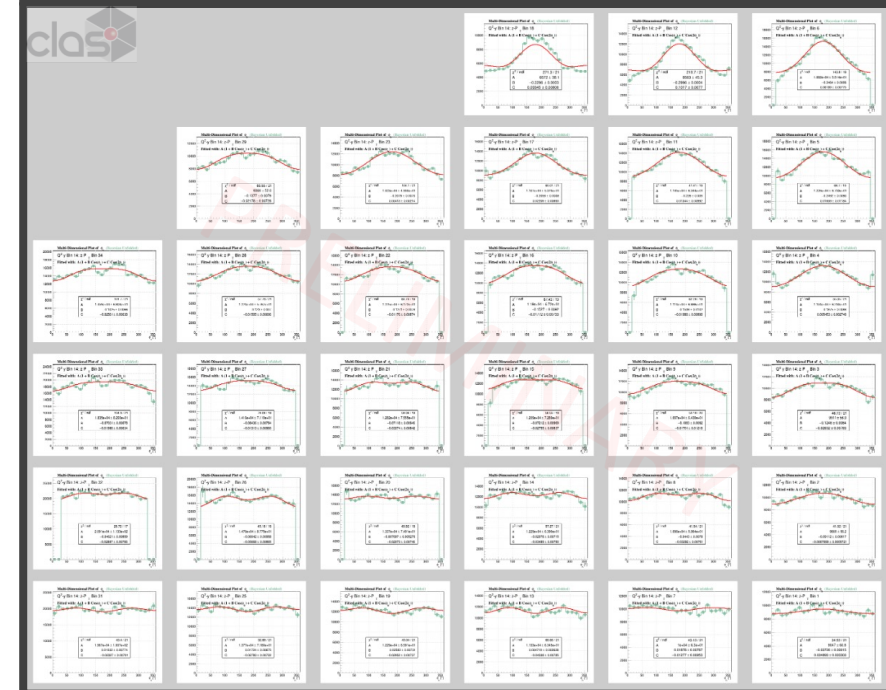
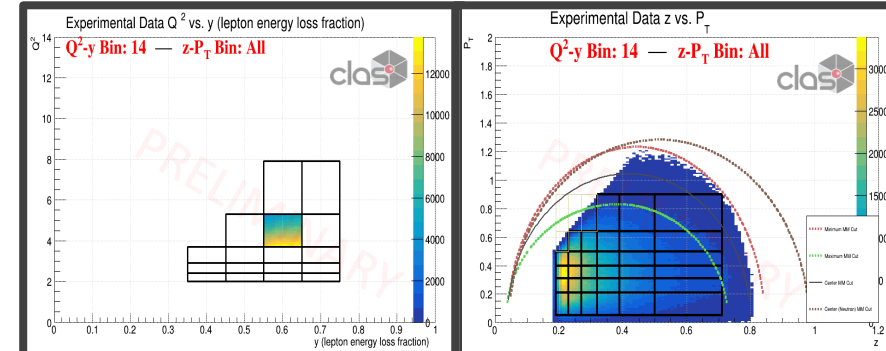
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Unfolded with Bayesian Method

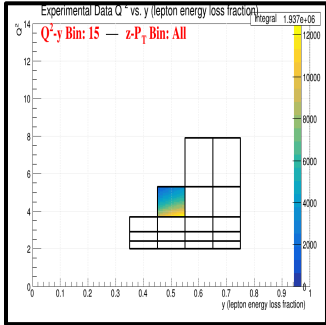
Q<sup>2</sup>-y Bin 14



# Pass 2 Conditions

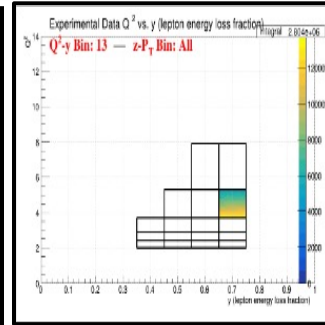
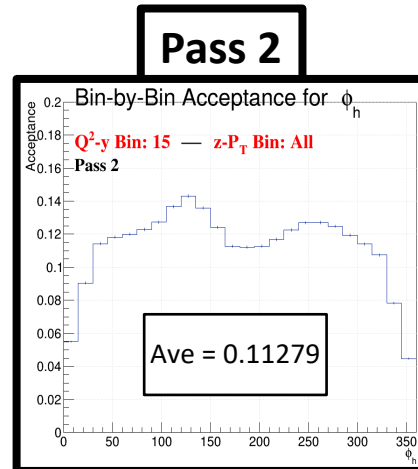
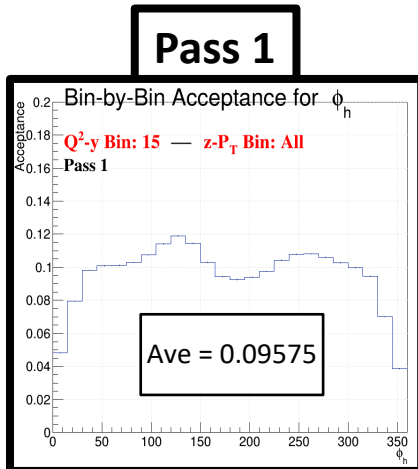
- Monte Carlo statistics are low (using test sample)
- Have not applied Momentum/Energy Loss Corrections in Pass 2
  - Momentum Corrections have been developed for Pass 1 Data but not for Pass 2 yet
  - Momentum Smearing Corrections are also needed for the Pass 2 Monte Carlo
- Need to check/develop new fiducial cuts optimized for Pass 2
  - Sector dependences in the  $\phi_h$  distributions may be improved by altering the cuts along the detector's edge

# Pass 2 Comparisons - Acceptances



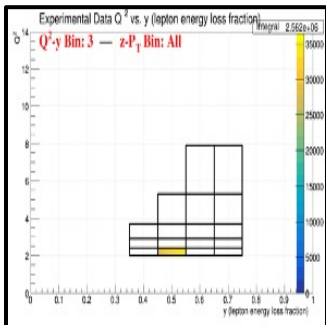
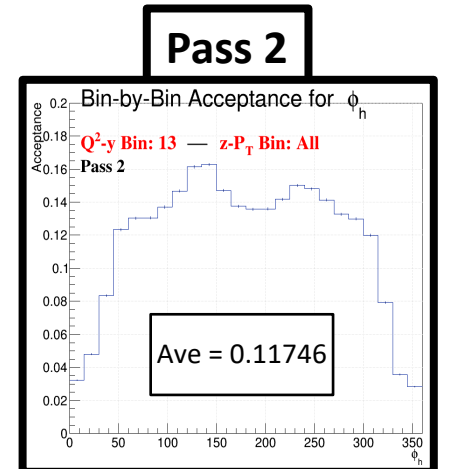
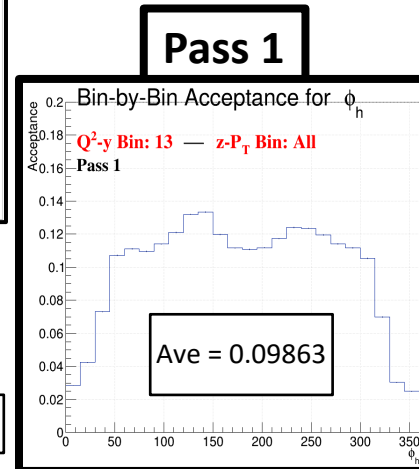
High  $Q^2$   
Low  $y$

$\Delta Ave = +0.01704$



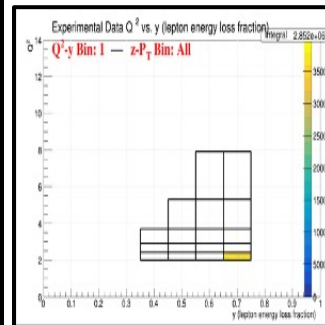
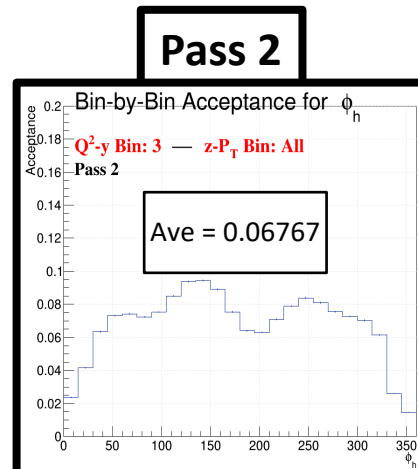
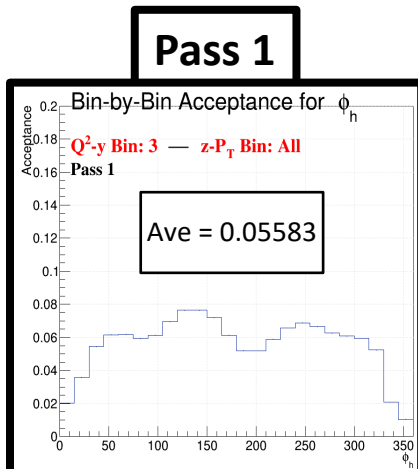
High  $Q^2$   
High  $y$

$\Delta Ave = +0.01883$



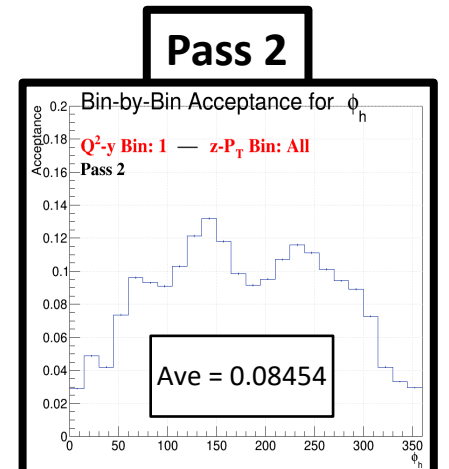
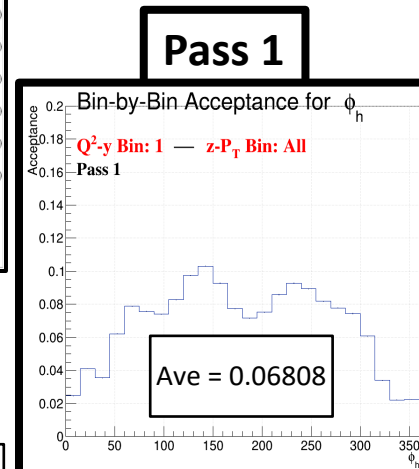
Low  $Q^2$   
Low  $y$

$\Delta Ave = +0.01184$



Low  $Q^2$   
High  $y$

$\Delta Ave = +0.01646$



# Cos( $\phi_h$ ) Moment as Functions of z - Pass 2 Comparison

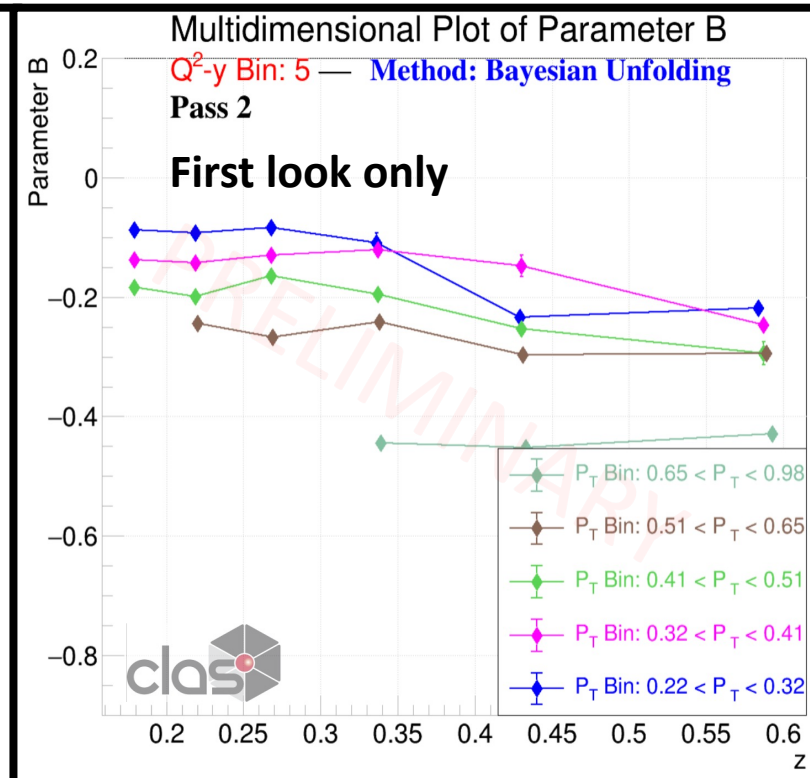
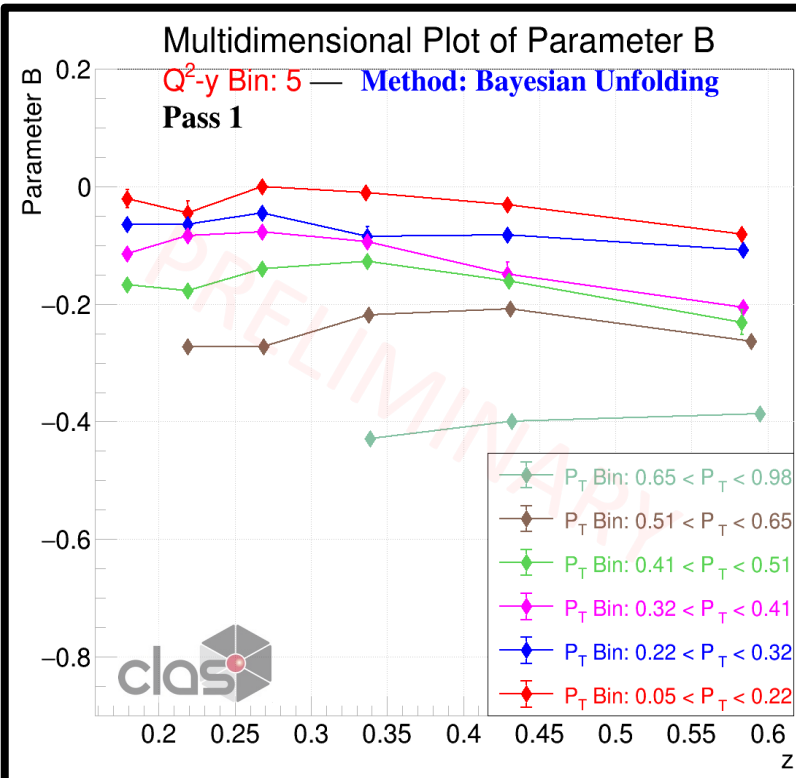
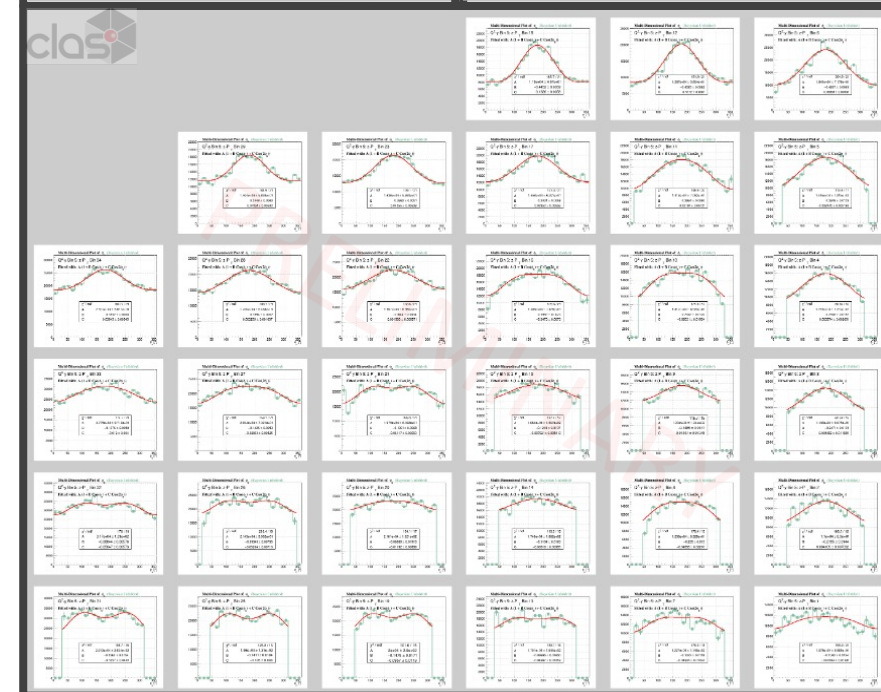
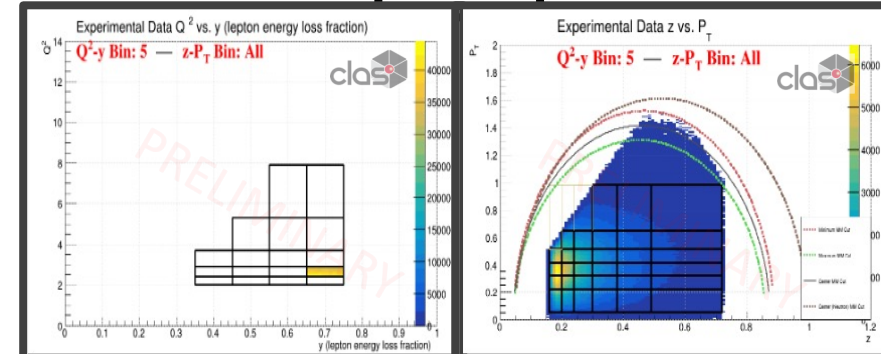
$$B = A_{UU}^{\cos \phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

$Q^2$ -y Bin 5

Pass 2



# Cos(2φ<sub>h</sub>) Moment as Functions of z - Pass 2 Comparison

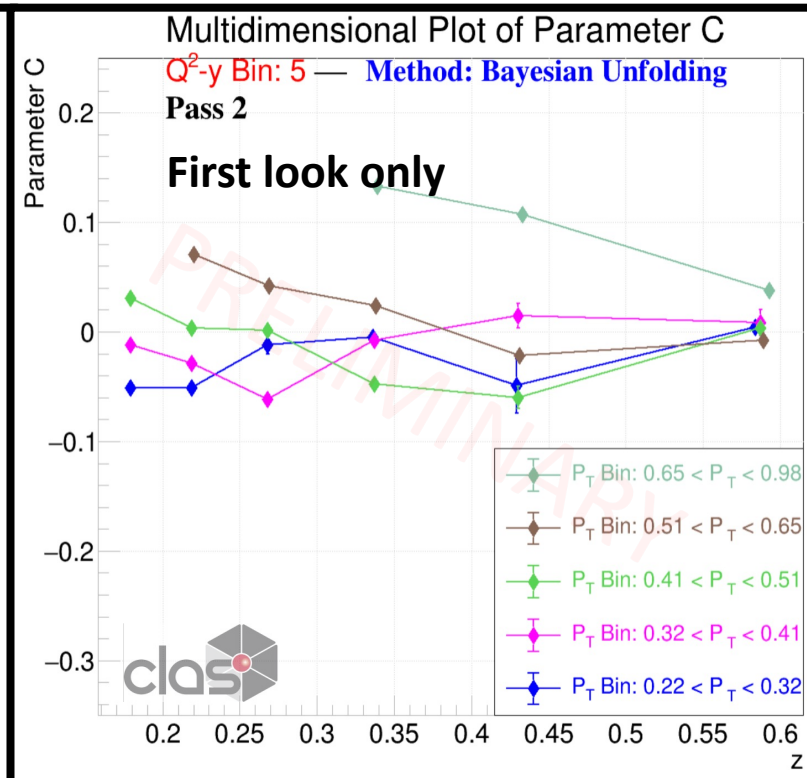
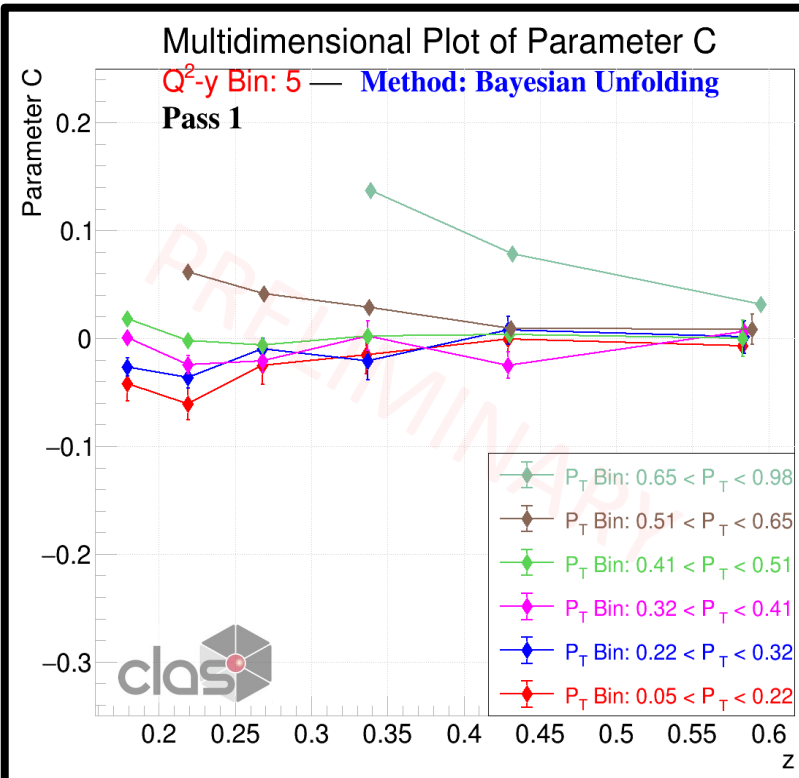
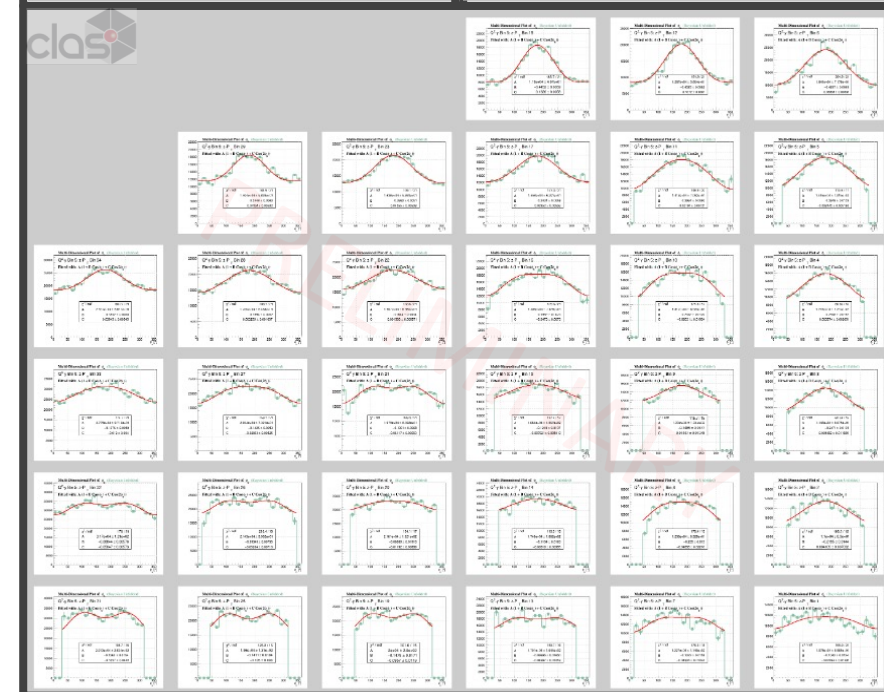
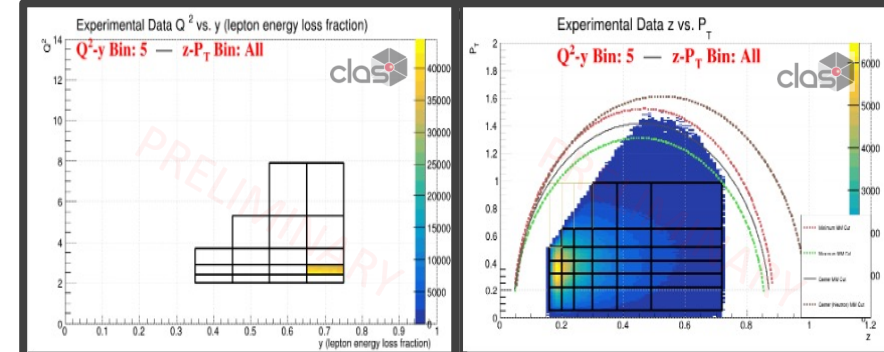
$$C = A_{UU}^{\cos 2\phi_h}$$

φ<sub>h</sub> Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

Q<sup>2</sup>-y Bin 5

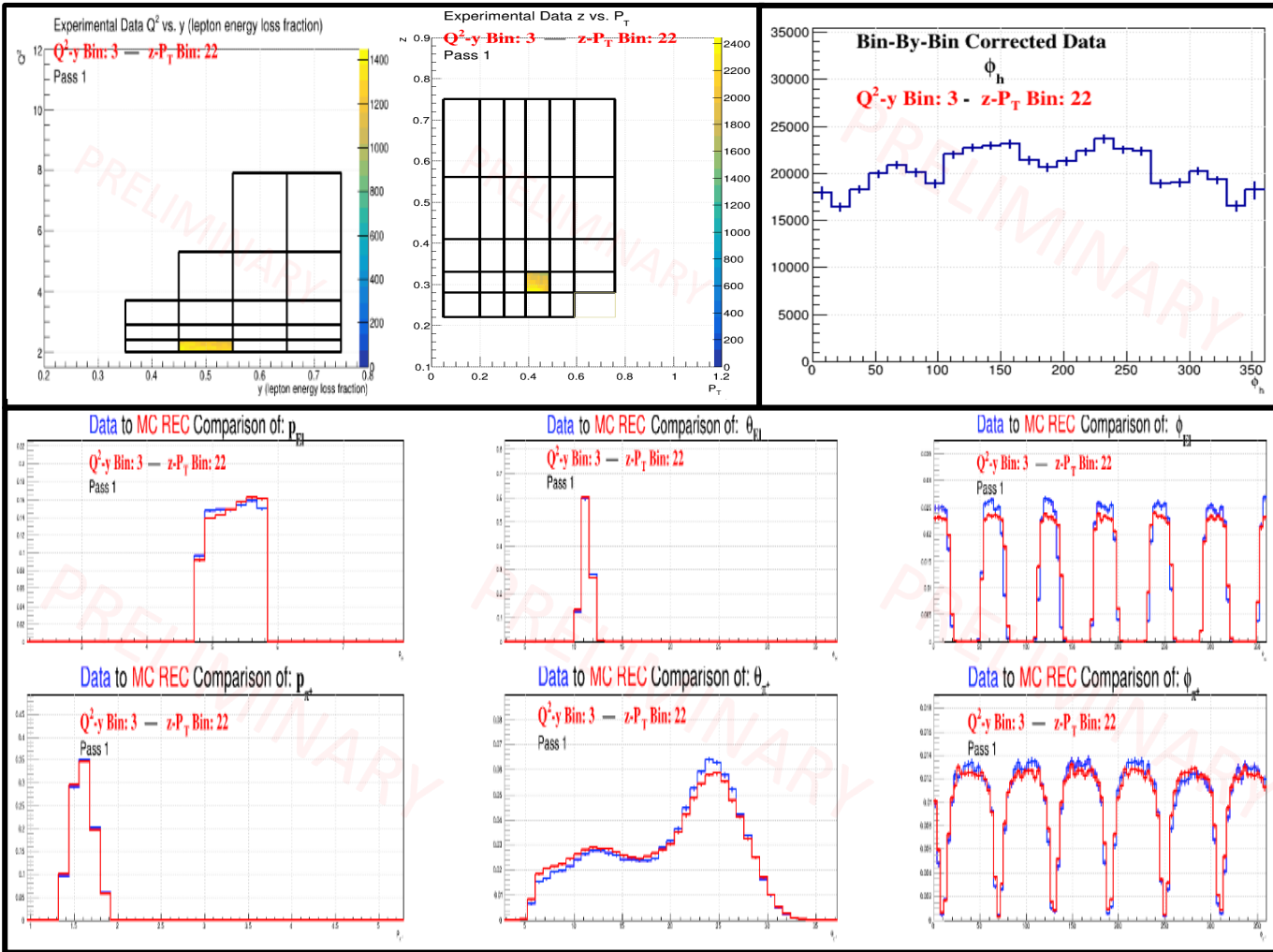
Pass 2



# Outlook

- Working on Multidimensional Acceptance Corrections for the simultaneous unfolding of  $Q^2$ ,  $y$ ,  $z$ ,  $P_T$ , and  $\phi_h$  variables
  - Includes additional efforts towards more realistic MC simulations, both on the detector response description and physics process
  - Investigating Sector Description/Sector Dependence related to Acceptance Corrections
- Working on fully including Pass 2 Data
- Still need to include Radiative and BC Corrections in this analysis
- Ongoing Investigations of Vector Meson Contributions
- Cross-checking Analysis with T. Hayward

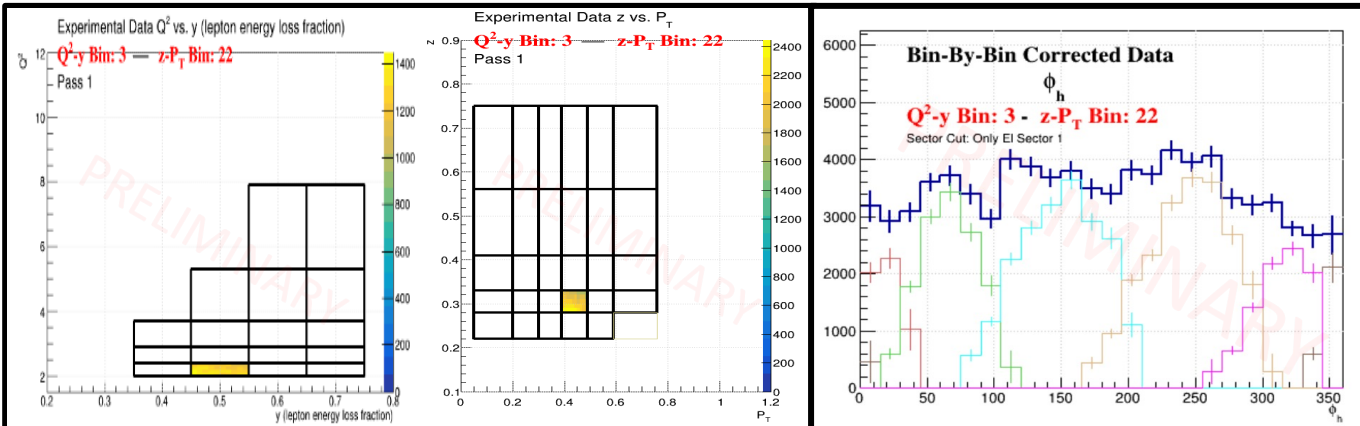
# Sector Correlations with $\phi_h$ Distributions – Pass 1



**Issue:** Some bins seem to have additional modulations not explained by the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  moments

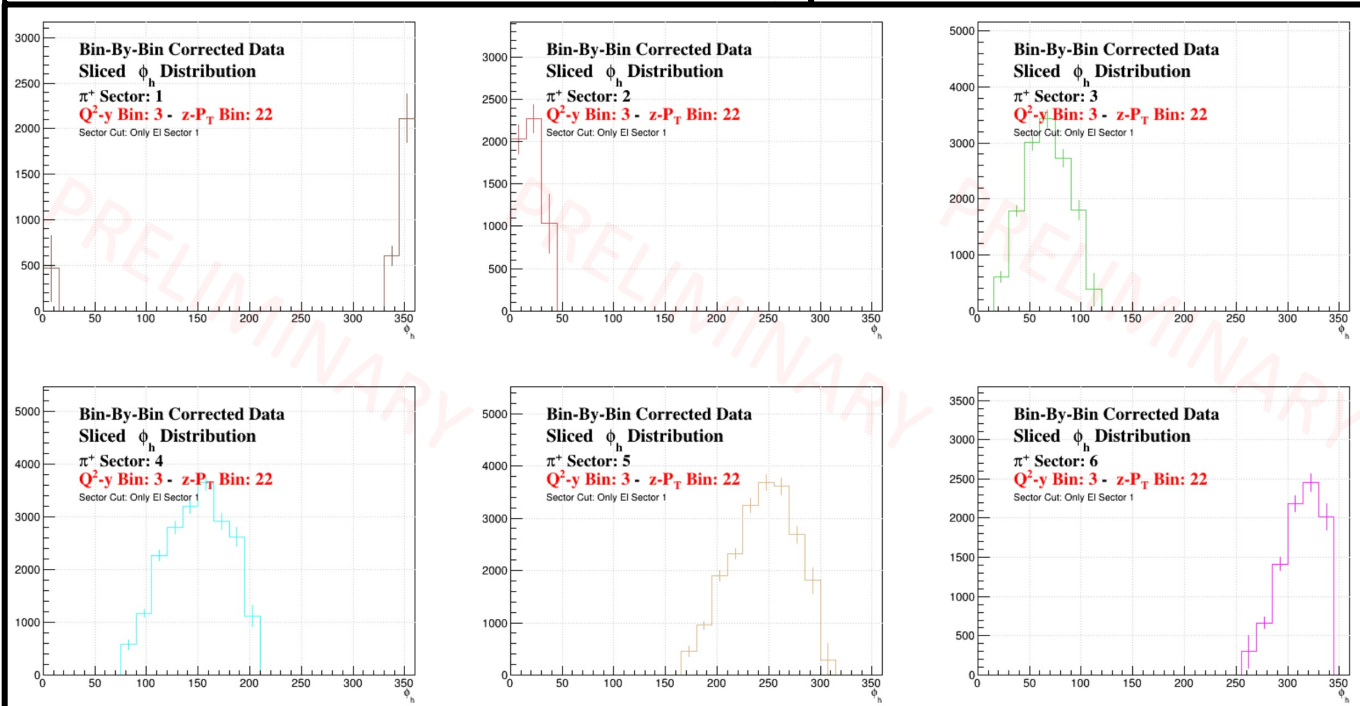
- The 6 peak structure could be related to the forward detector sectors
- Plots below show the lab angles and momentum of both particles within the given kinematic bin of  $Q^2$ ,  $y$ ,  $z$ , and  $P_T$

# Sector Correlations with $\phi_h$ Distributions – Pass 1



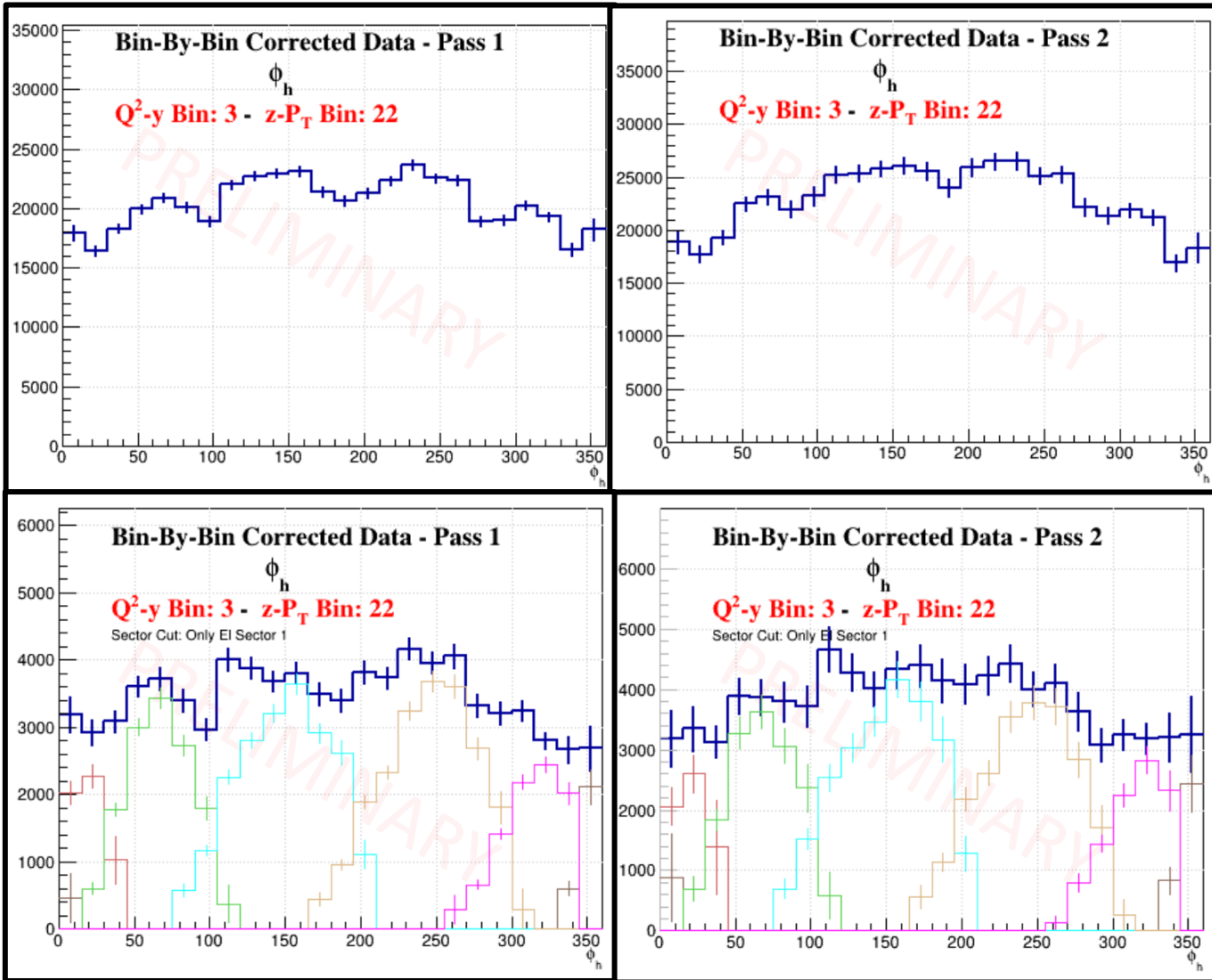
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- The 6 peak structure could be related to the forward detector sectors
- Plots show the  $\phi_h$  distributions separated based on which sector the  $\pi^+$  pion is detected
- **Additional Requirement: Electron in Sector 1**
- This suggests that the effect is related to mismatching in sector acceptance between Data and Monte Carlo





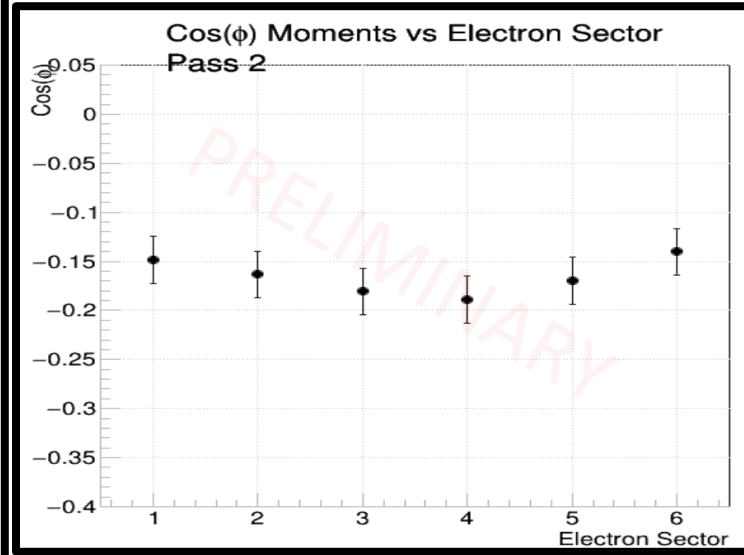
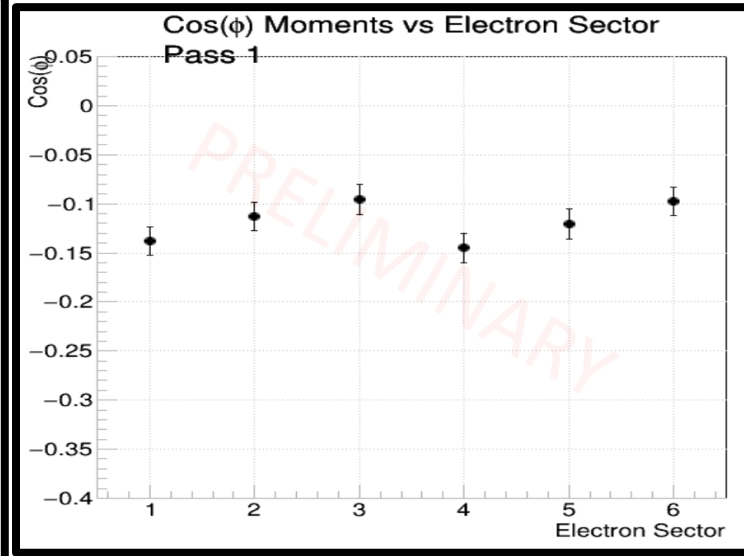
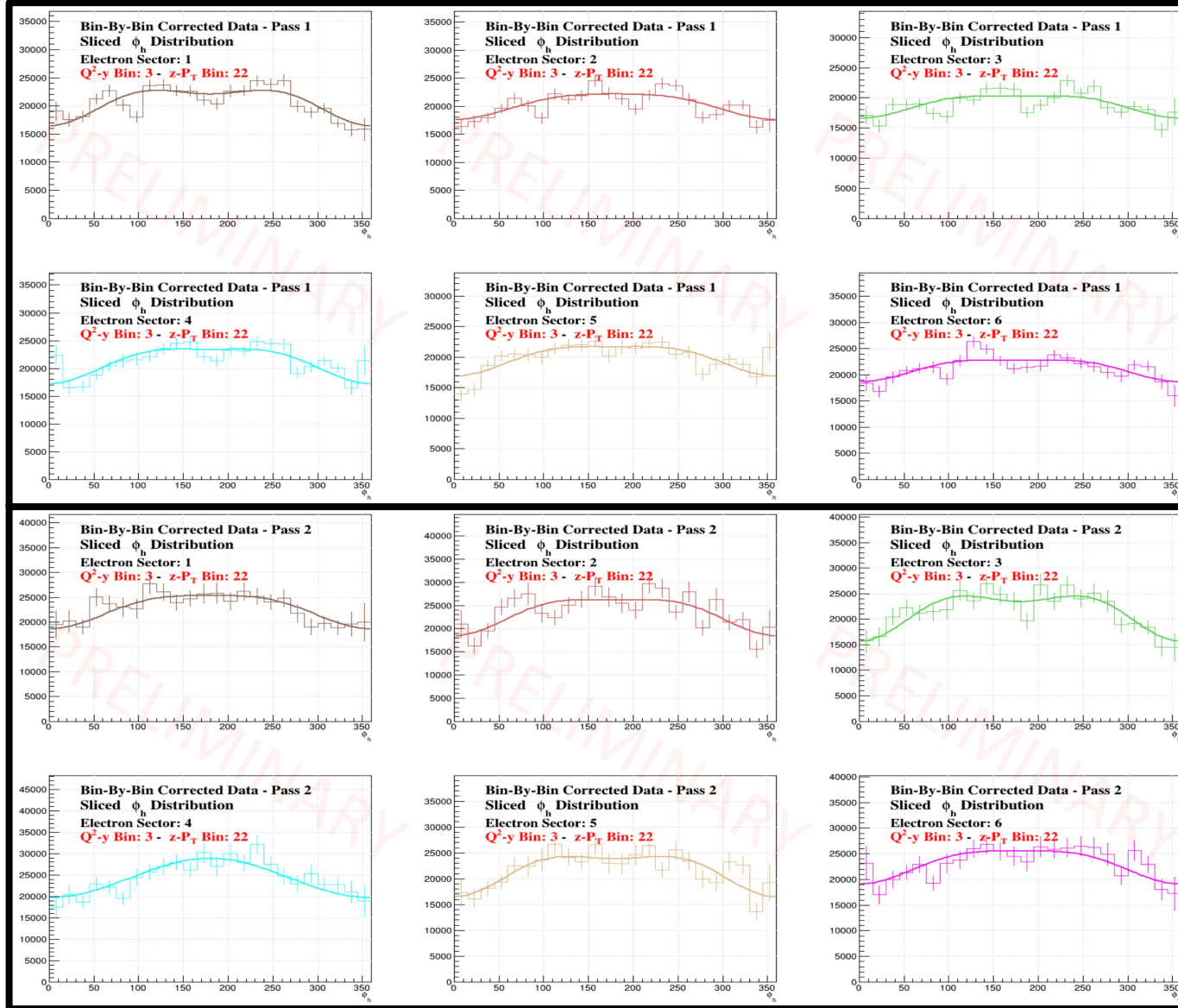
# Sector Correlations with $\phi_h$ Distributions – Pass 2 Comparison



**Issue:** Some bins seem to have additional modulations not explained by the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  moments

- The 6 peak structure could be related to the forward detector sectors
- Plots show the  $\phi_h$  distributions separated based on which sector the  $\pi^+$  pion is detected
- **Additional Requirement: Electron in Sector 1**
- This suggests that the effect is related to mismatching in sector acceptance between Data and Monte Carlo
- Also present in Pass 2

# Sector Correlations with $\text{Cos}(\phi)$ Measurements – Pass 1 and 2



Sectors can cause different modulations within the kinematic bins

These plots show those differences in Pass 1 (top row) and Pass 2 (bottom row)

**Electron is restricted to being detected in a single sector**

Plotting  $\text{Cos}(\phi)$  Moments vs Electron Sector on the right

# Thank you

# Questions?

## Acknowledgments and Thanks

- Contributions made by other members of the CLAS Collaboration and researchers at Argonne National Lab
- This work is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under contract number DE-AC02-06CH11357

# Backup Slides

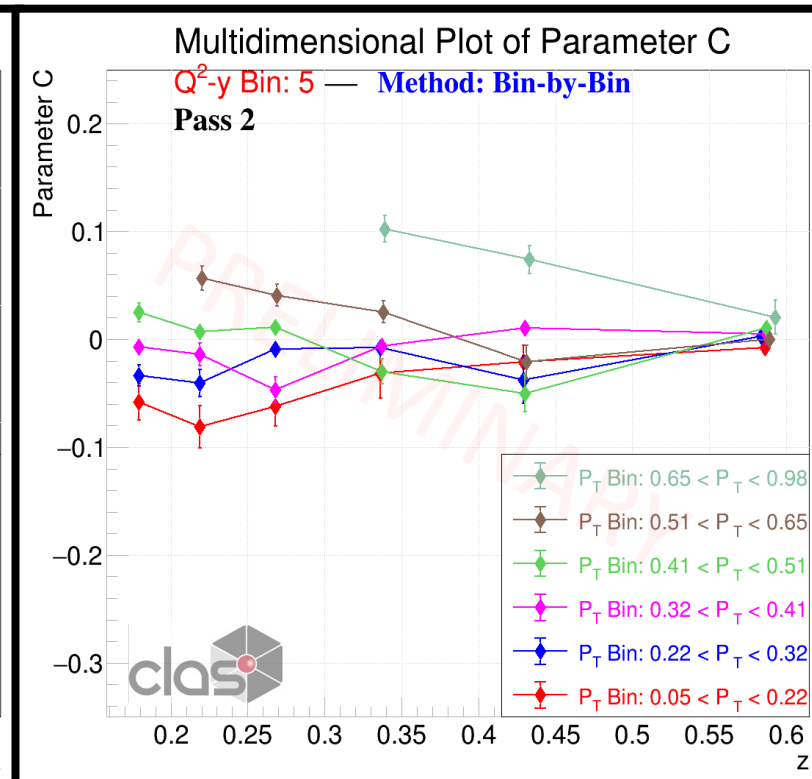
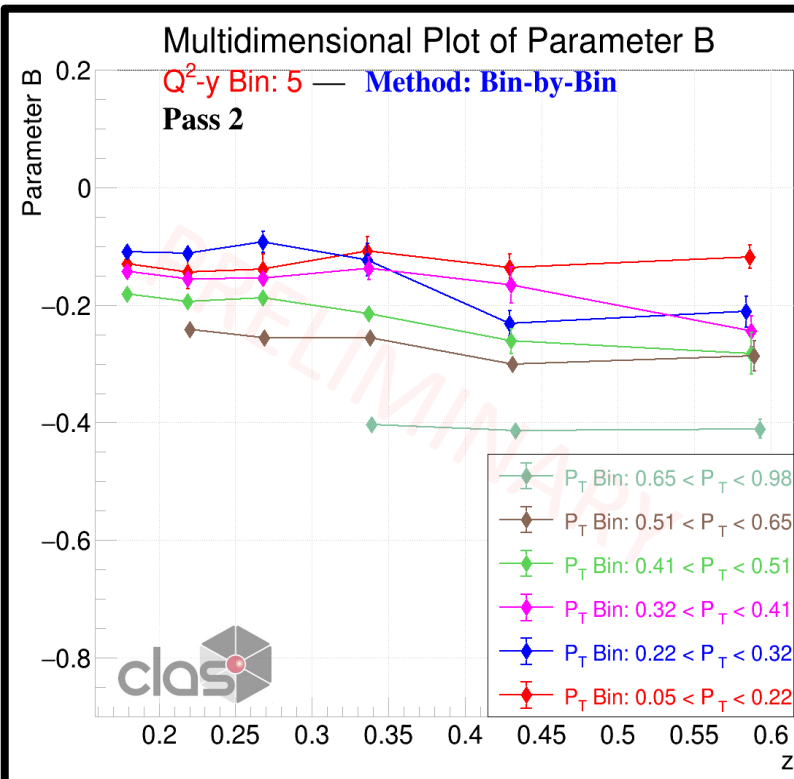
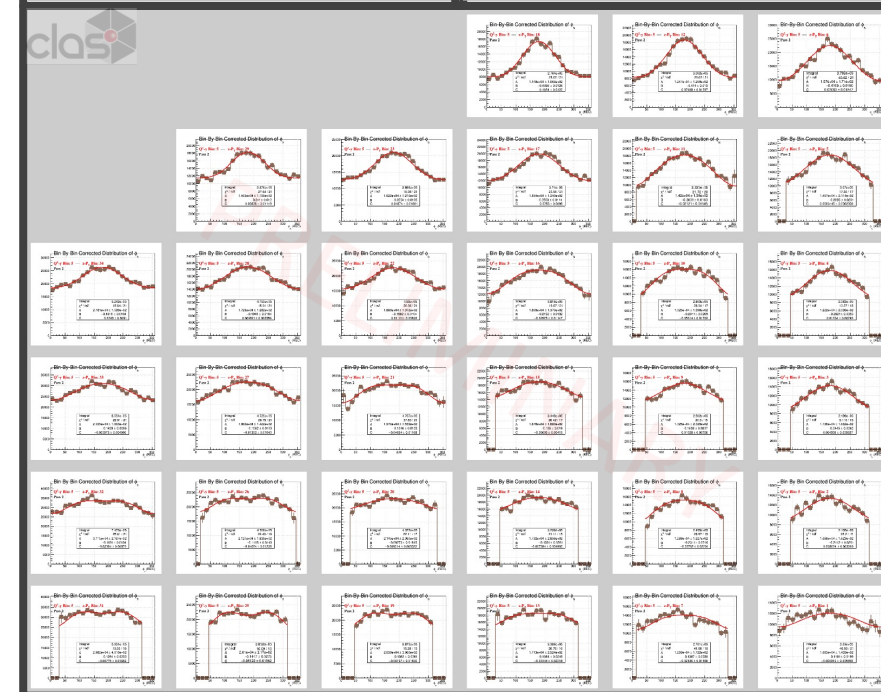
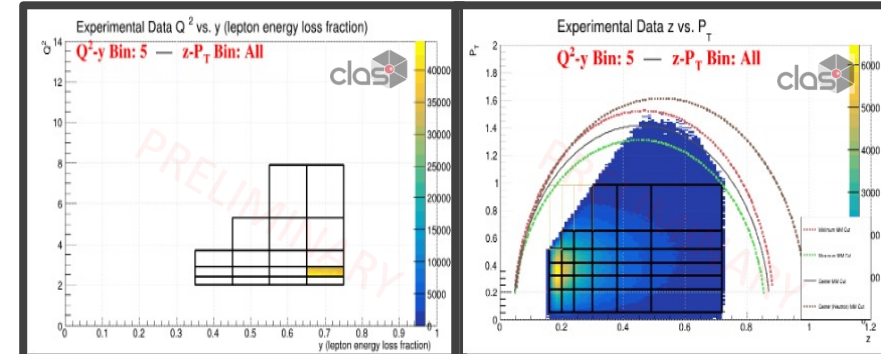
# Cosine Moments as Functions of z - with Pass 2

$$B = A_{UU}^{\cos \varphi_h} \quad C = A_{UU}^{\cos 2\varphi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Corrected with Bin-by-bin Method

$Q^2$ -y Bin 5



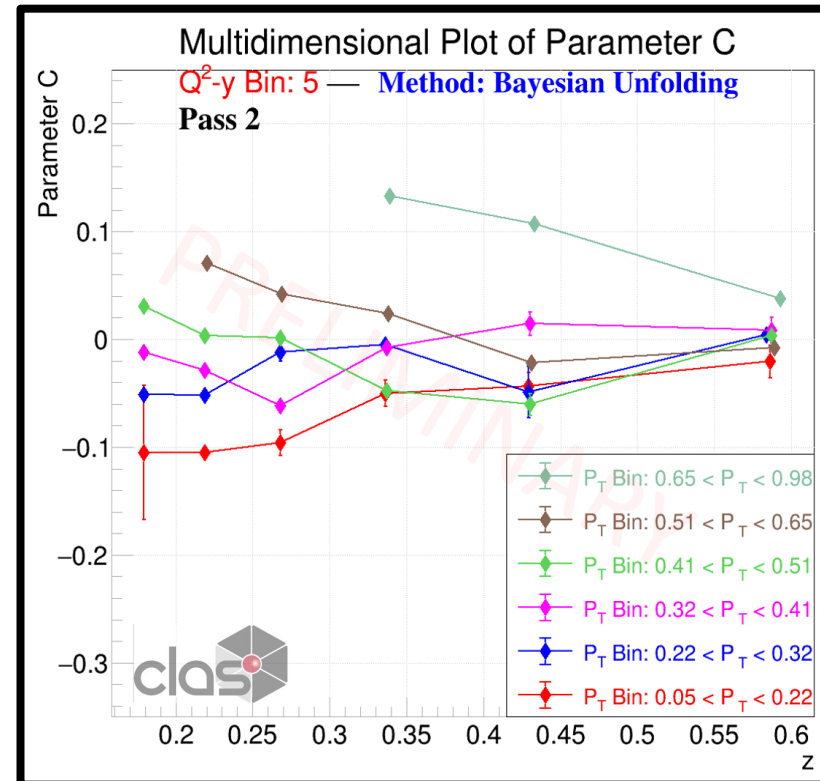
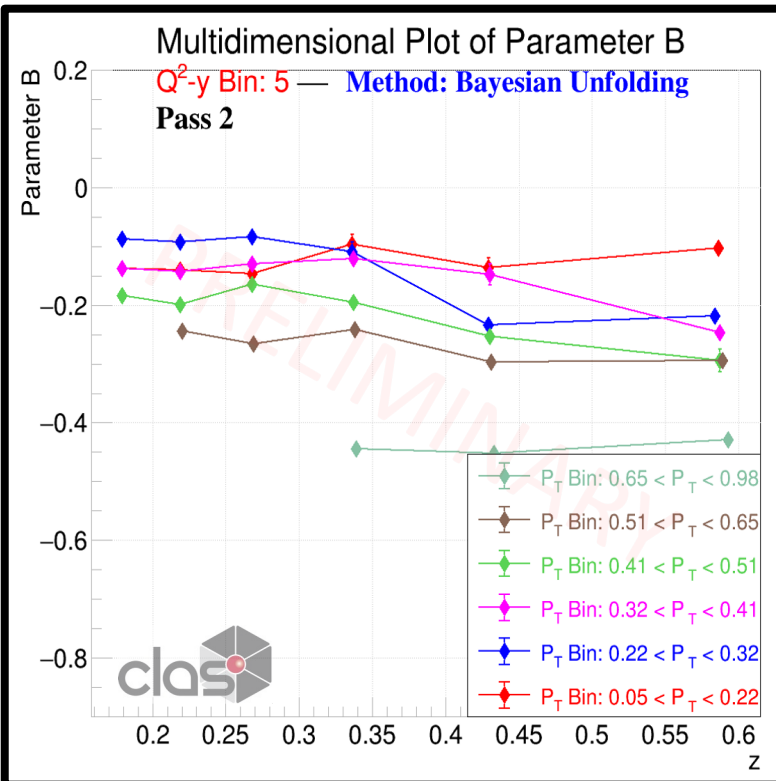
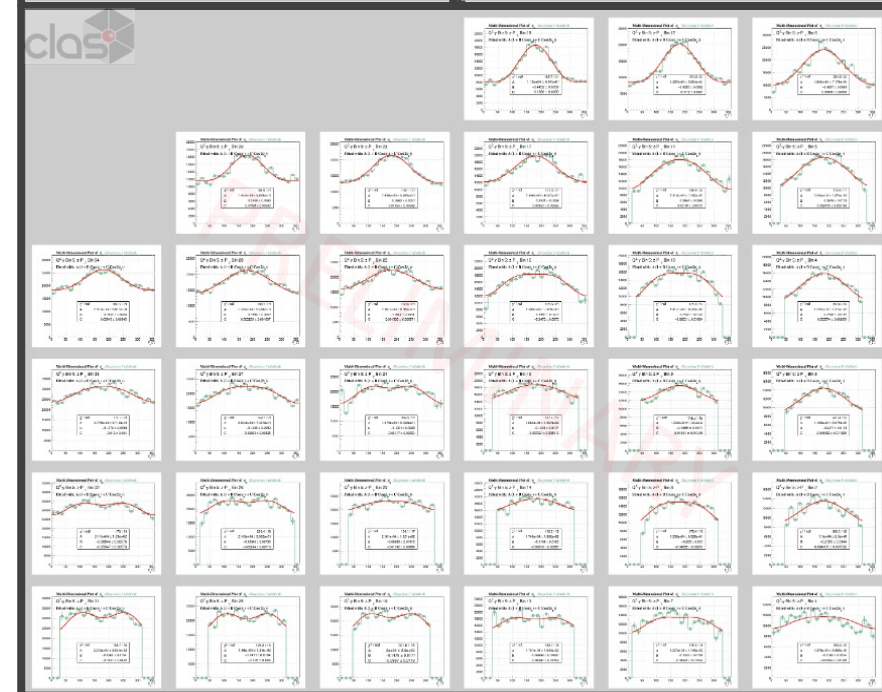
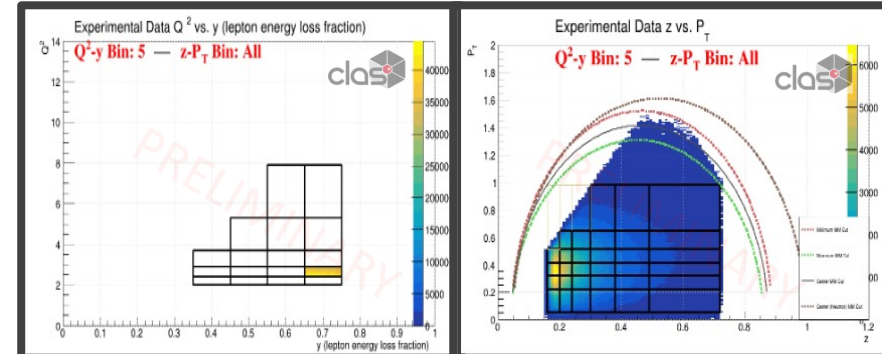
# Cosine Moments as Functions of z - with Pass 2

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

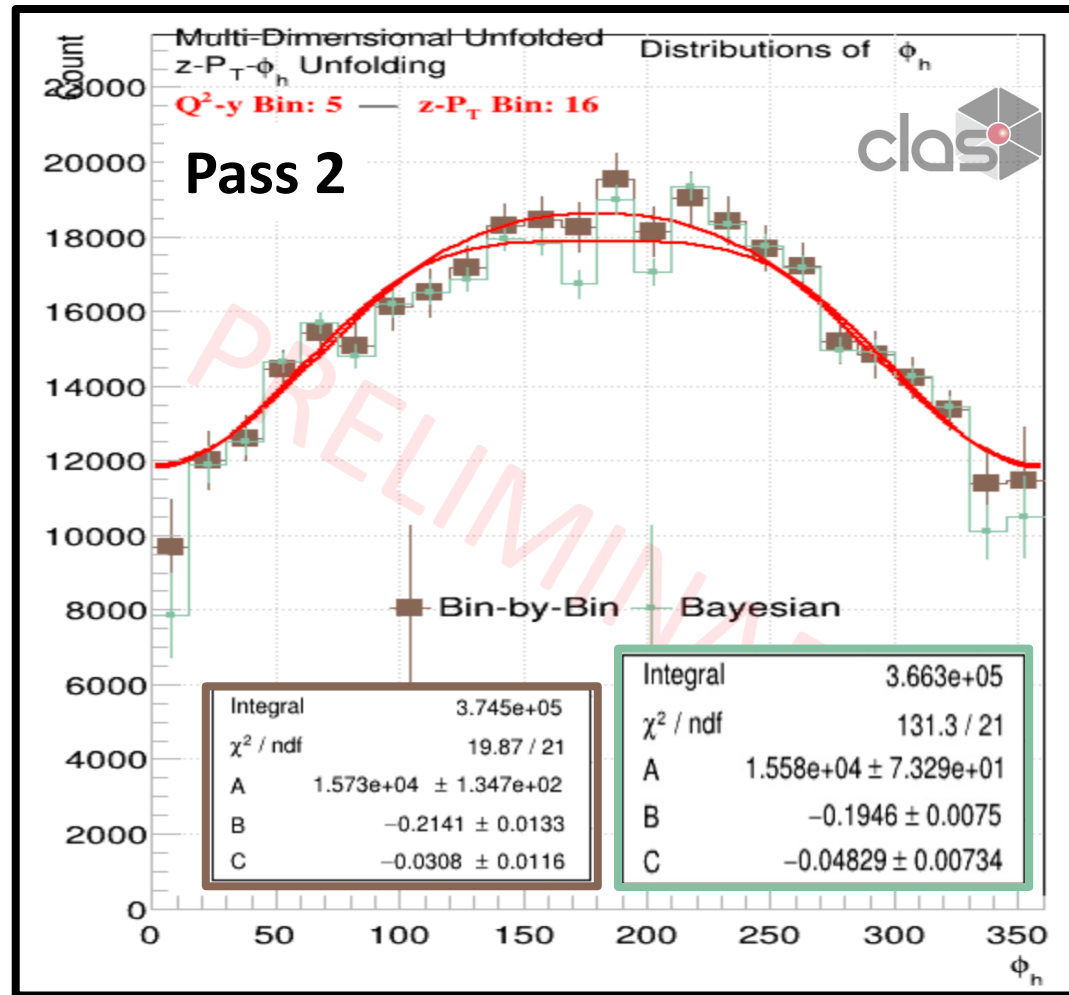
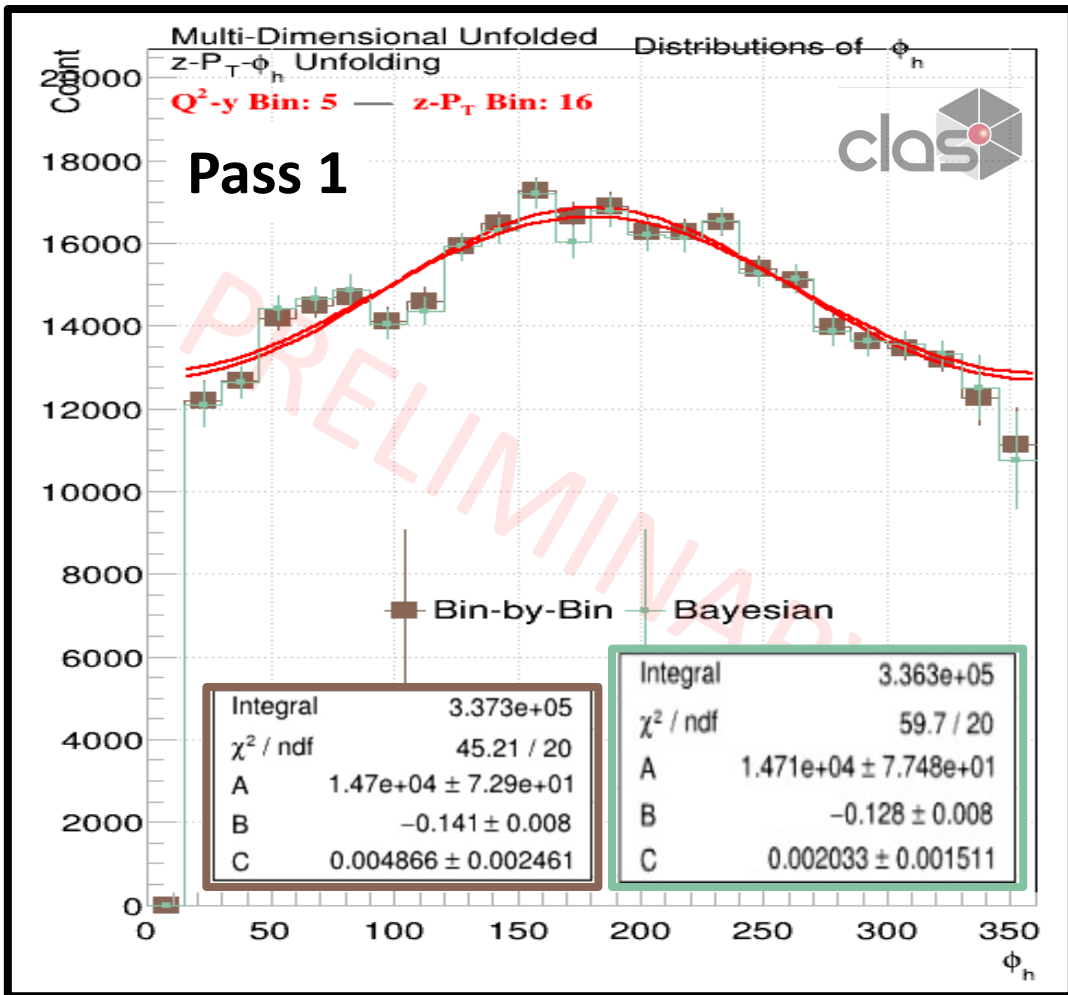
Unfolded with Bayesian Method

$Q^2$ -y Bin 5



# Comparisons of Pass 1 and Pass 2 Unfolding

Using the Multidimensional Kinematic Bin from the prior example for this comparison



# More on Boer-Mulders...

quark pol.

nucleon pol.

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_1$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}^\perp$	$h_1, h_{1T}^\perp$

Boer-Mulders

$$h_1^\perp =$$



- $\mathbf{P}$  is the momentum of the proton
- $\mathbf{k}_T$  is the transverse momentum of the quark
- $\mathbf{s}_\perp$  is the transverse spin of the quark

If the Boer-Mulders term is non-zero, then there is a net transverse quark polarization inside of unpolarized protons



# Event Selection (Full PID)

The RG-A Analysis Overview and Procedures note goes into detail about the common particle identification scheme used for RG-A

(See: [https://clas12-docdb.jlab.org/DocDB/0009/000949/001/RGA\\_Analysis\\_Overview\\_and\\_Procedures-08172020.pdf](https://clas12-docdb.jlab.org/DocDB/0009/000949/001/RGA_Analysis_Overview_and_Procedures-08172020.pdf))

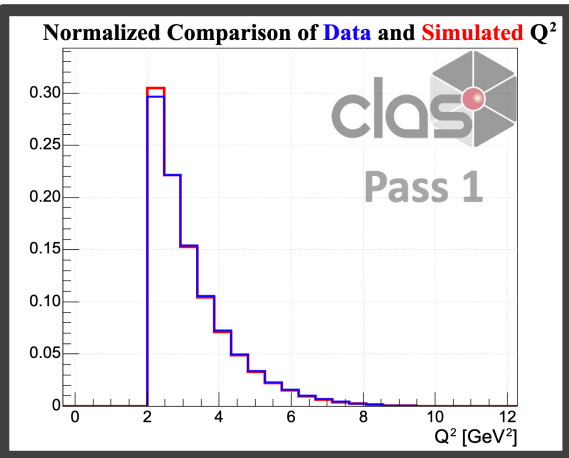
## Electron PID Criteria:

- Detected in Forward Detector
- > 2 photoelectrons detected in the HTCC
- > 0.07 GeV energy deposited in the PCAL
- Sector dependent sampling fraction cut
- “Diagonal cut” for electrons above 4.5 GeV (HTCC threshold)
- $y < 0.75$ , not strictly an “electron cut”, but sets the min electron energy approximately  $> 2.4$  GeV

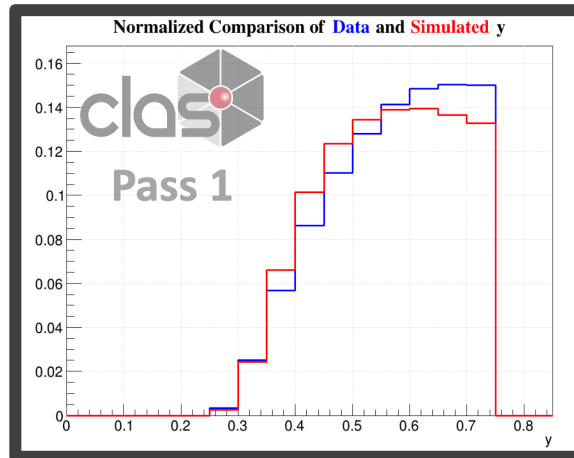
## Pion PID Criteria:

- Detected in Forward Detector
- $p > 1.25$  GeV
- Refined chi2pid cuts

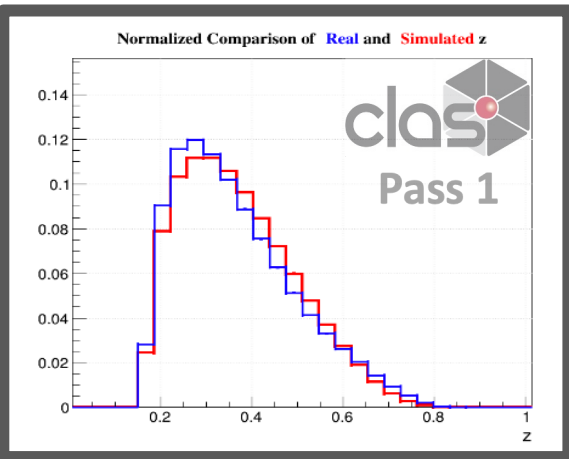
# Data and Monte Carlo Comparison



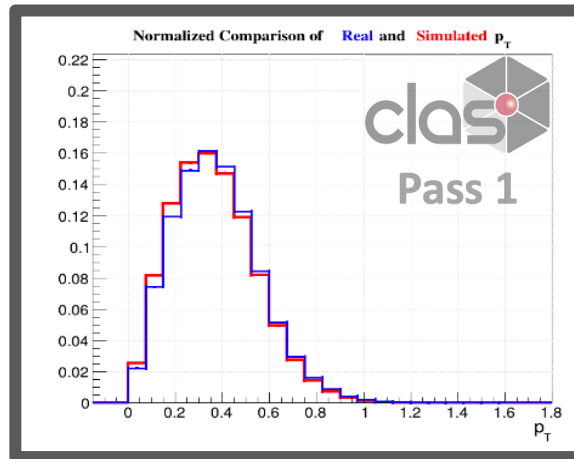
Q<sup>2</sup> Comparison



y Comparison

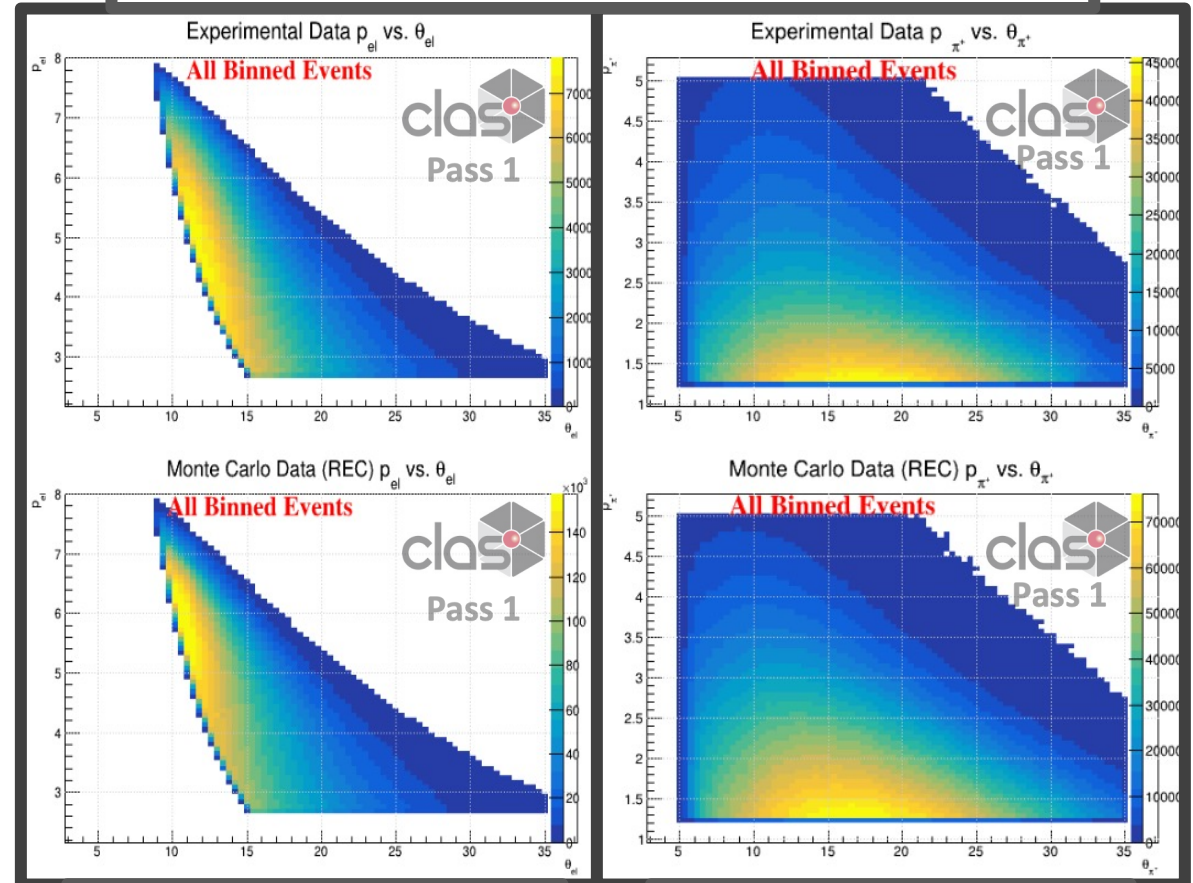


z Comparison



P<sub>T</sub> Comparison

## Momentum vs Polar Lab Angle Comparison



Electron Comparison

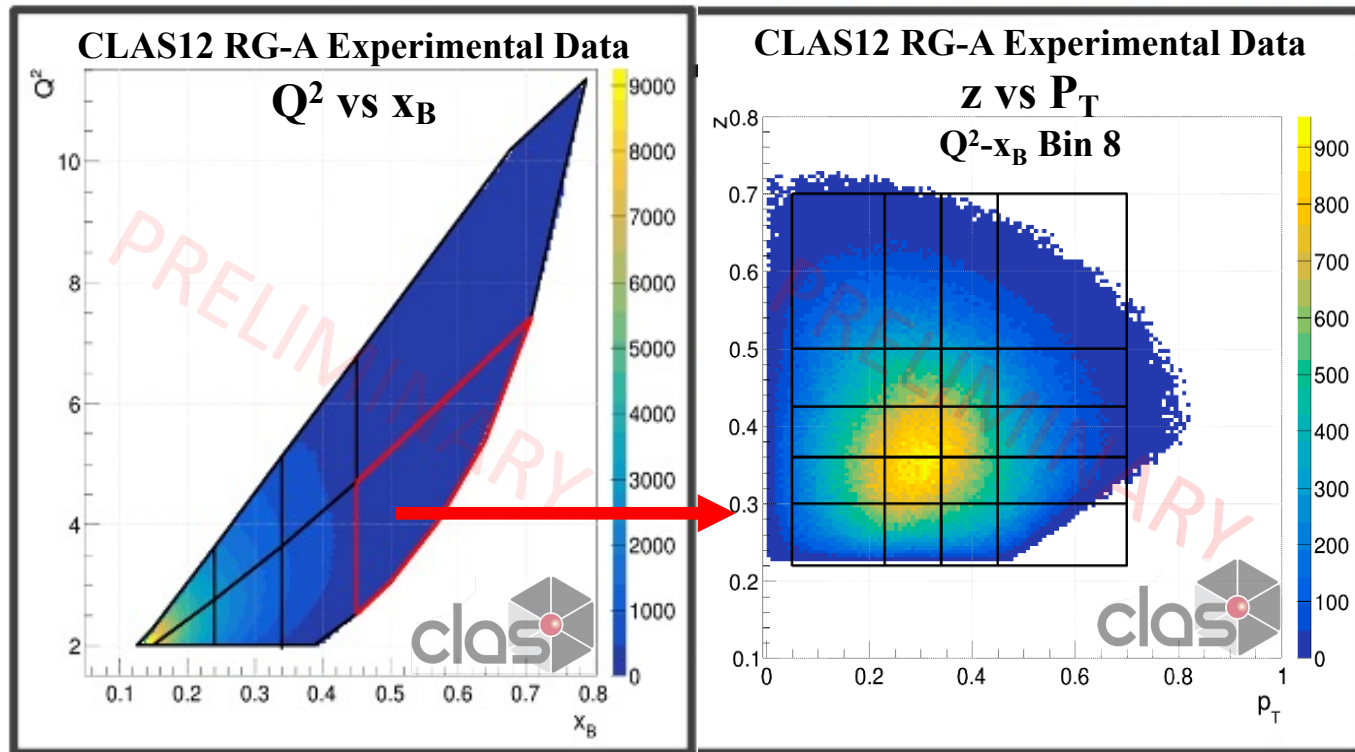
$\pi^+$  Pion Comparison

# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (4 Dimensions)

8  $Q^2$ - $x_B$  Bins Total – 20-49  $z$ - $P_T$  Bins (per  $Q^2$ - $x_B$  bin)

Example of old binning scheme  
using  $Q^2$ ,  $x_B$ ,  $z$ , and  $P_T$



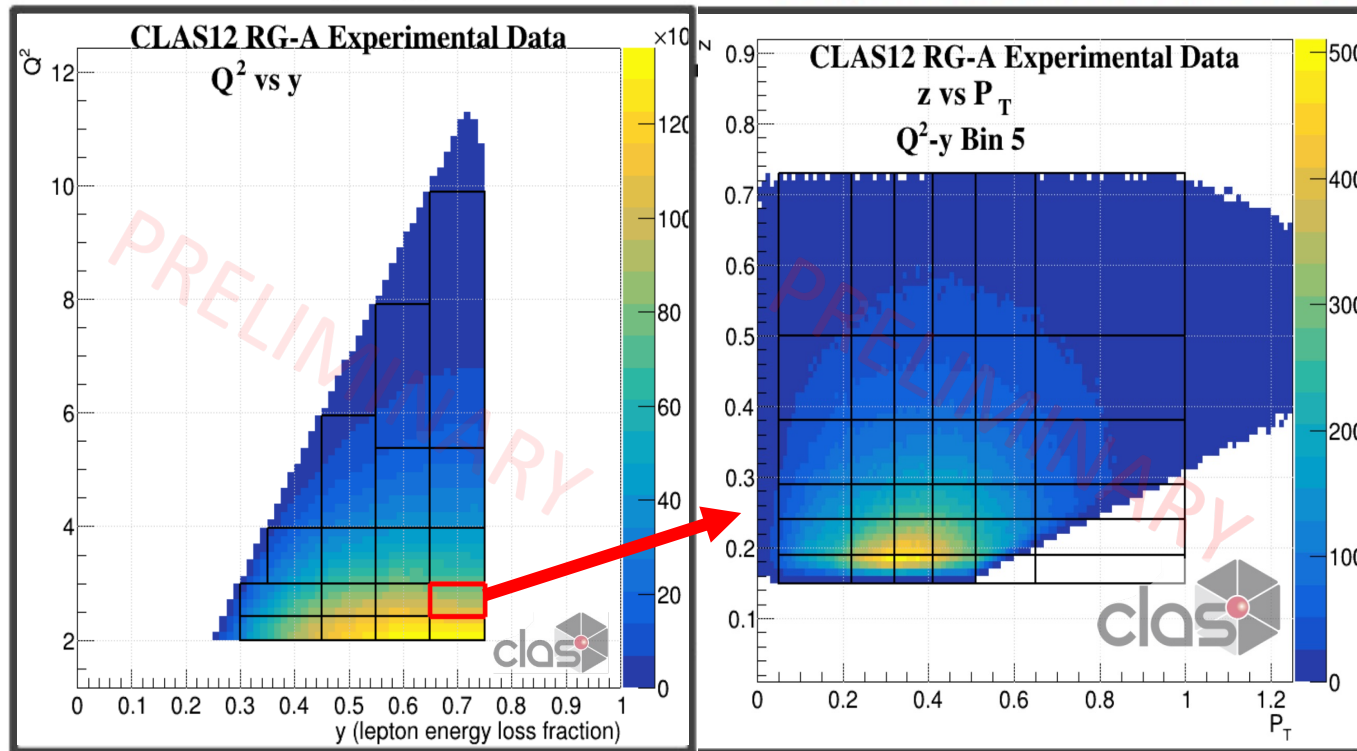
Main Issue was with the irregular  
shape of the  $Q^2$ - $x_B$  Bins

# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (4 Dimensions)

17  $Q^2$ - $y$  Bins Total – 20-42  $z$ - $P_T$  Bins (per  $Q^2$ - $y$  bin)

Example of prior binning scheme using  $Q^2$ ,  $y$ ,  $z$ , and  $P_T$



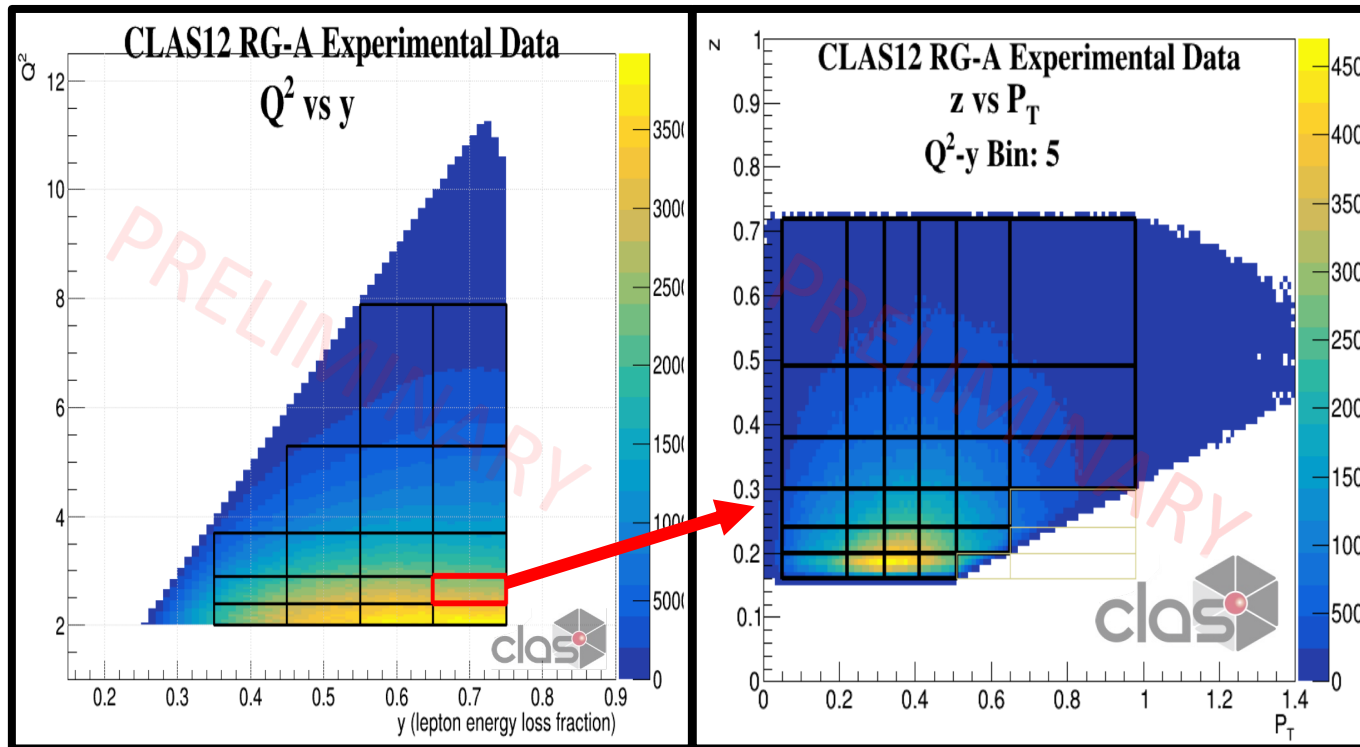
Both the  $Q^2$ - $y$  and  $z$ - $P_T$  bins are now rectangular, which makes the bins easier to work with

# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (4 Dimensions)

17  $Q^2$ - $y$  Bins Total – 25-36  $z$ - $P_T$  Bins (per  $Q^2$ - $y$  bin)

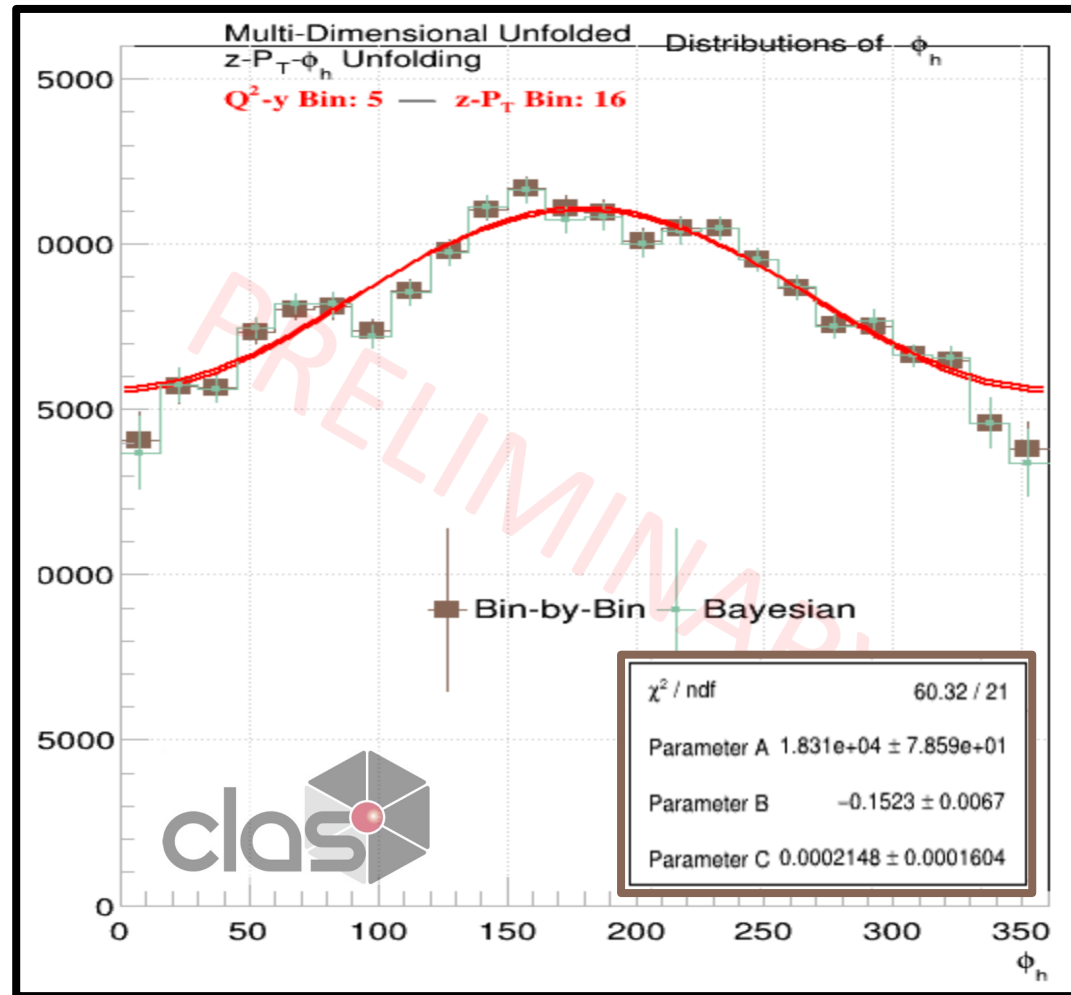
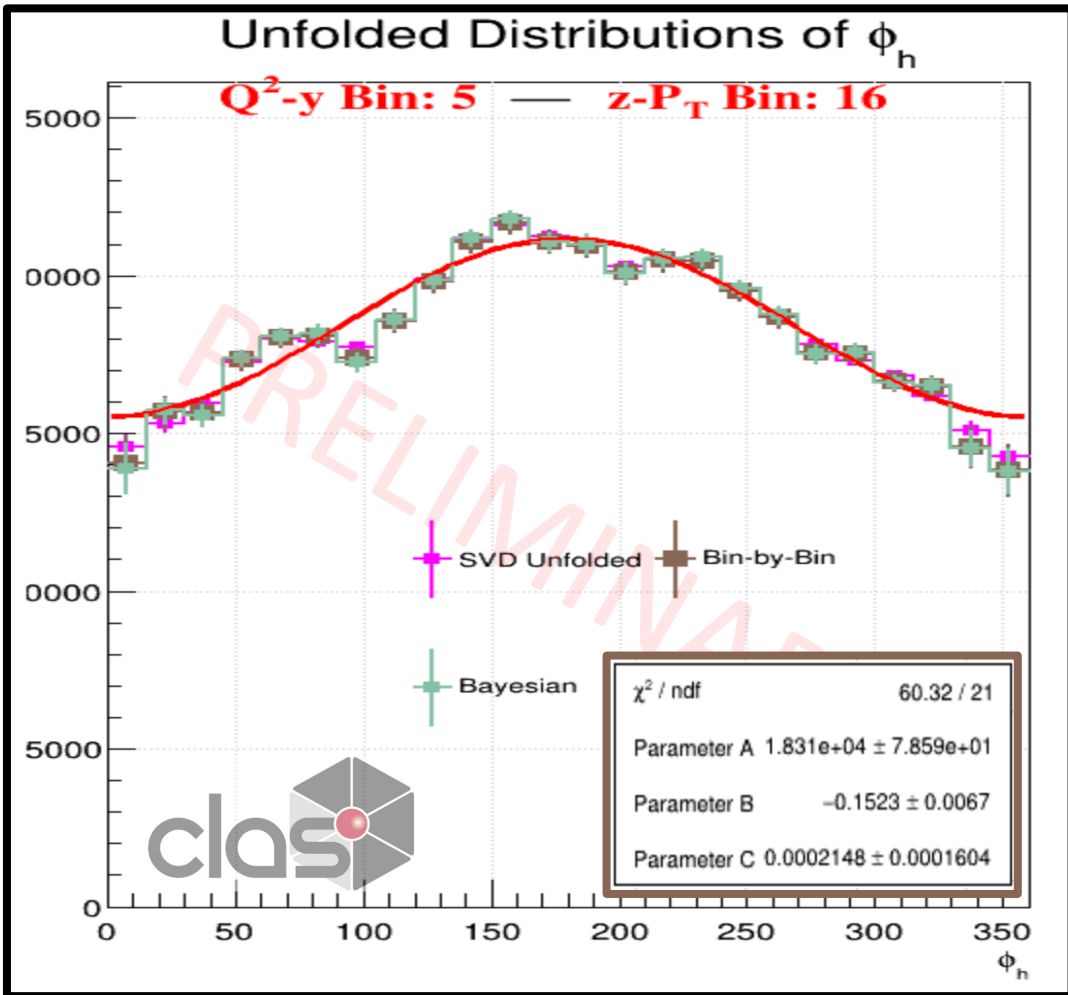
Example of the new binning scheme using  $Q^2$ ,  $y$ ,  $z$ , and  $P_T$



Optimized the binning for even distributions of event statistics and for consistent bin borders

# Comparisons of 1D and 3D Unfolding Procedure

Using the Multidimensional Kinematic Bin from the prior example for this comparison



Bin-by-bin  
 Acceptance  
 Correction  
 gives the exact  
 same results

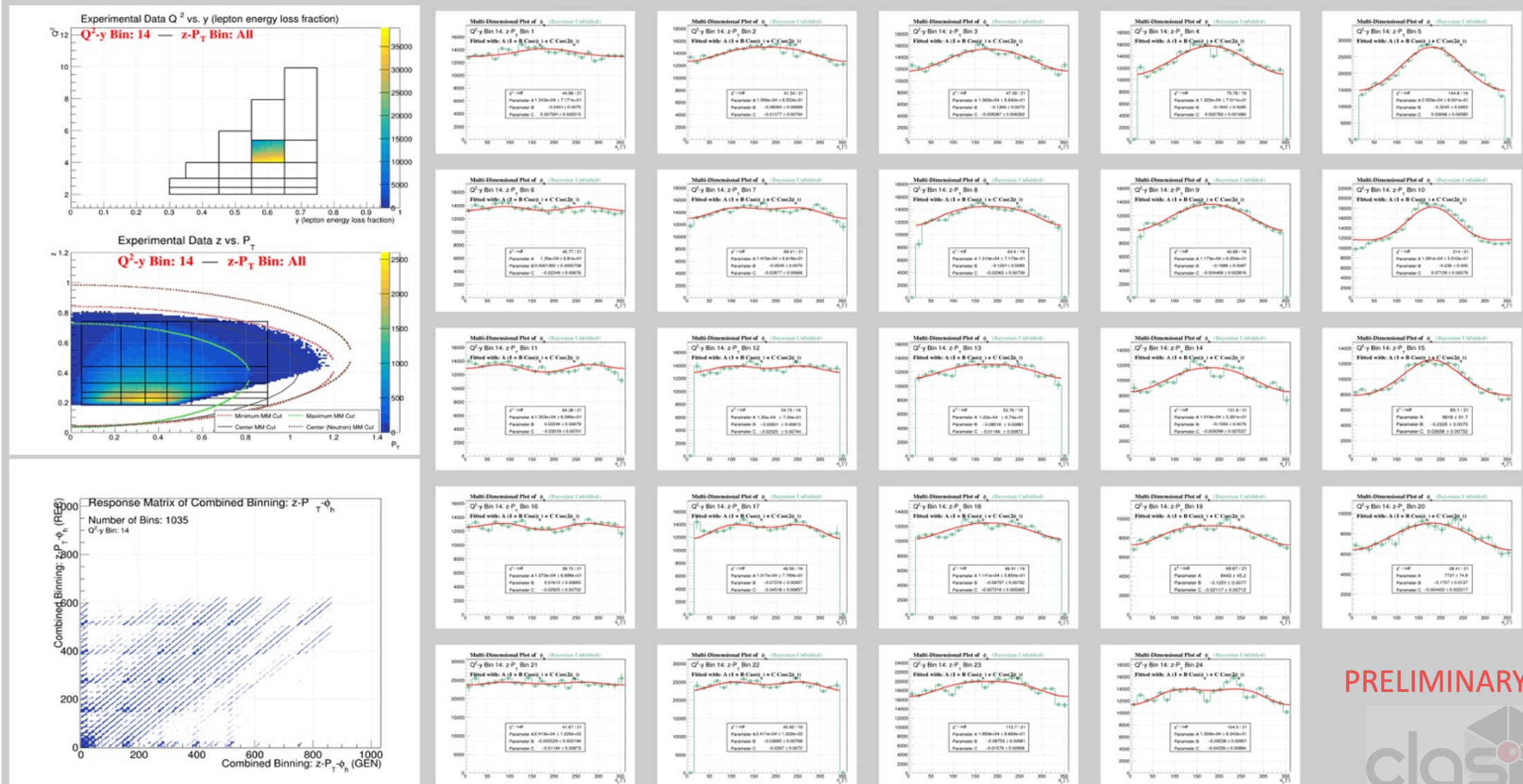
SVD Unfolding has not been able to work so far with the Multidimensional Unfolding procedures

# Extra Examples of (3D) Unfolding Procedure

Using the Flattened  $z$ - $P_T$ - $\phi_h$  Multidimensional Bins

Unfolded with Bayesian Method

$Q^2$ -y Bin 14



PRELIMINARY



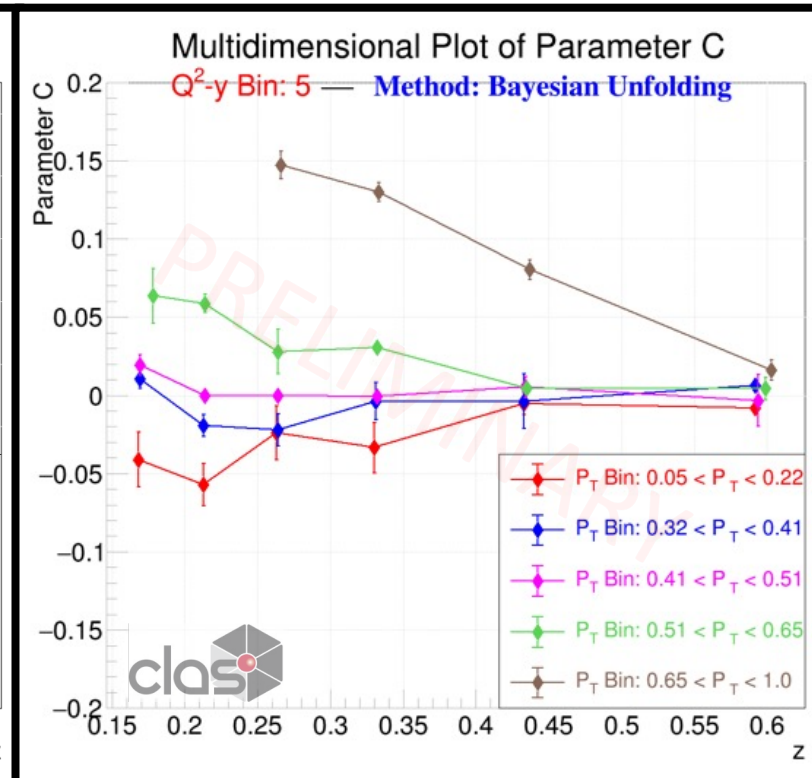
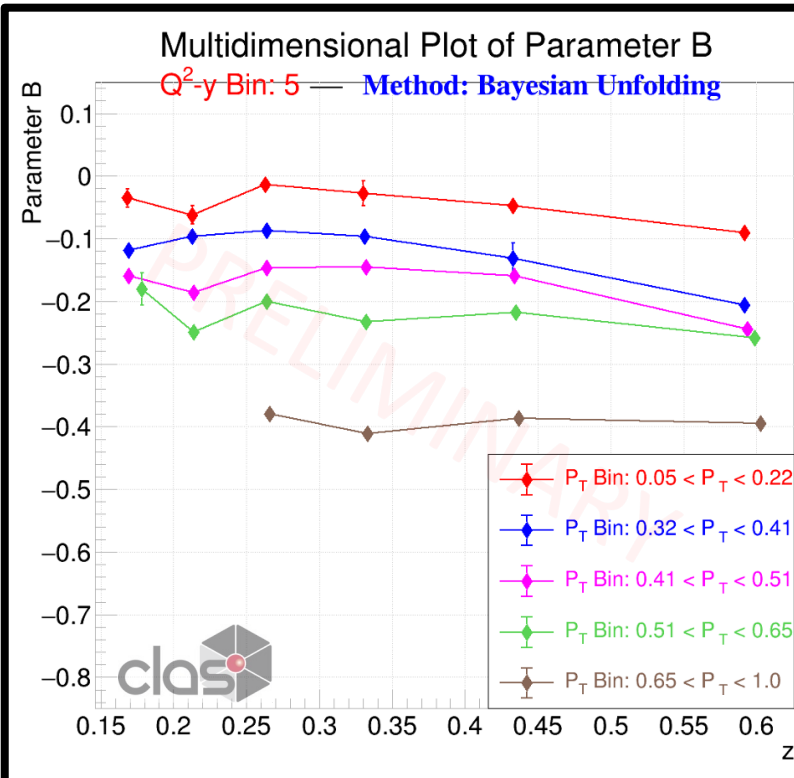
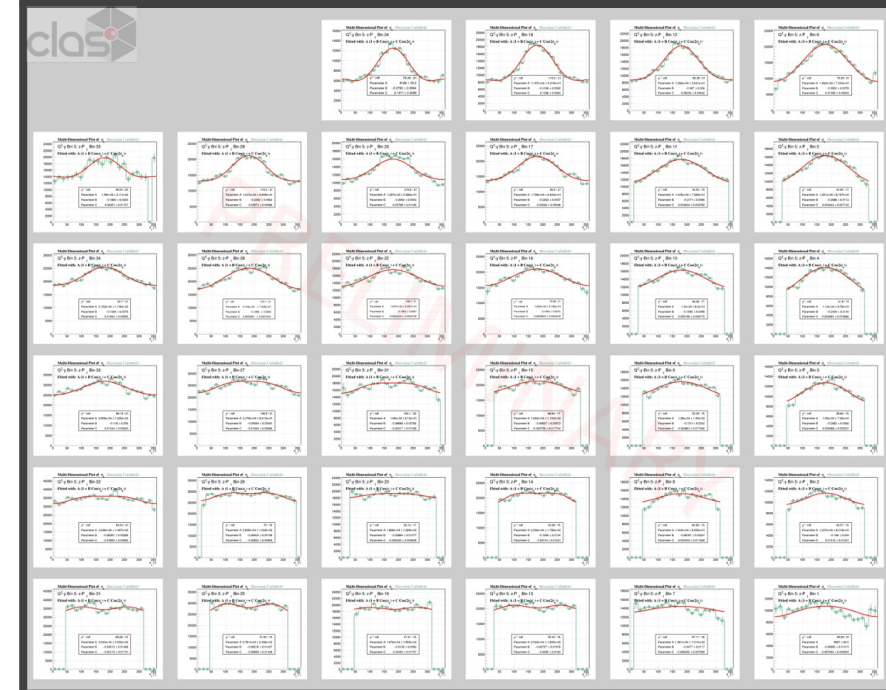
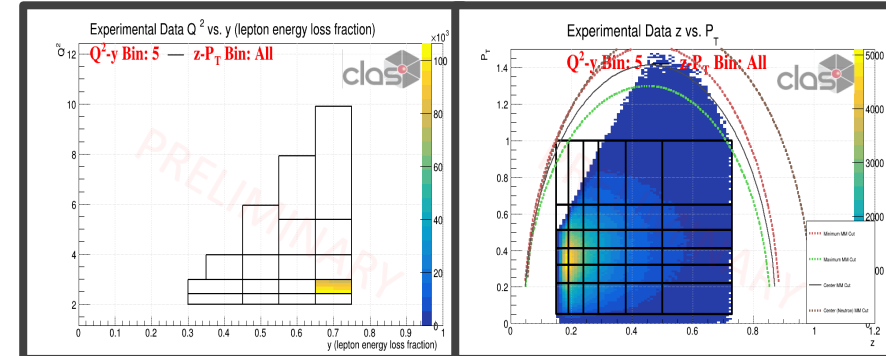
# Cosine Moments as Functions of z – Old Bins

$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Unfolded with Bayesian Method

$Q^2$ -y Bin 5





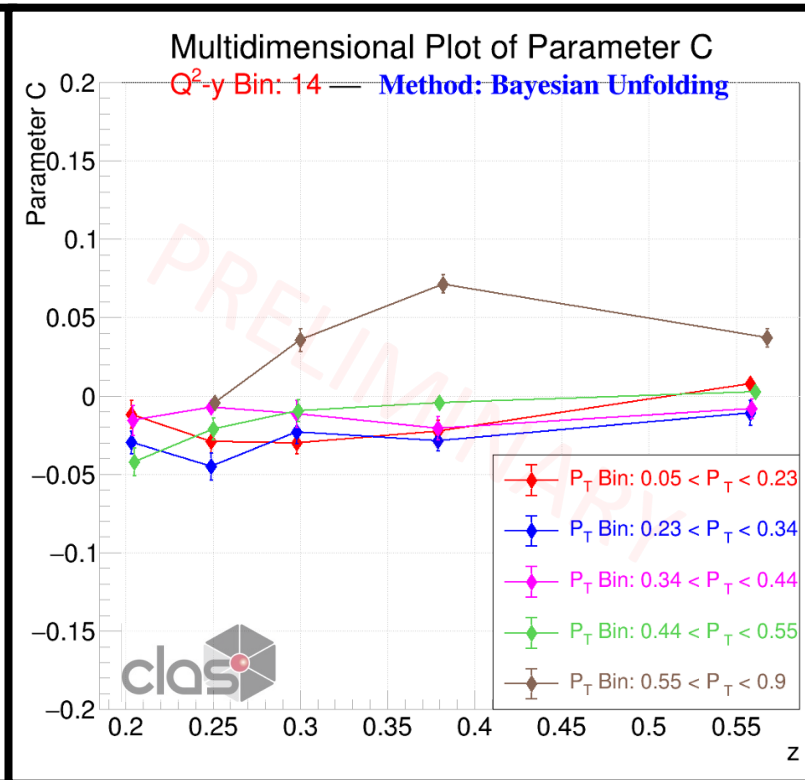
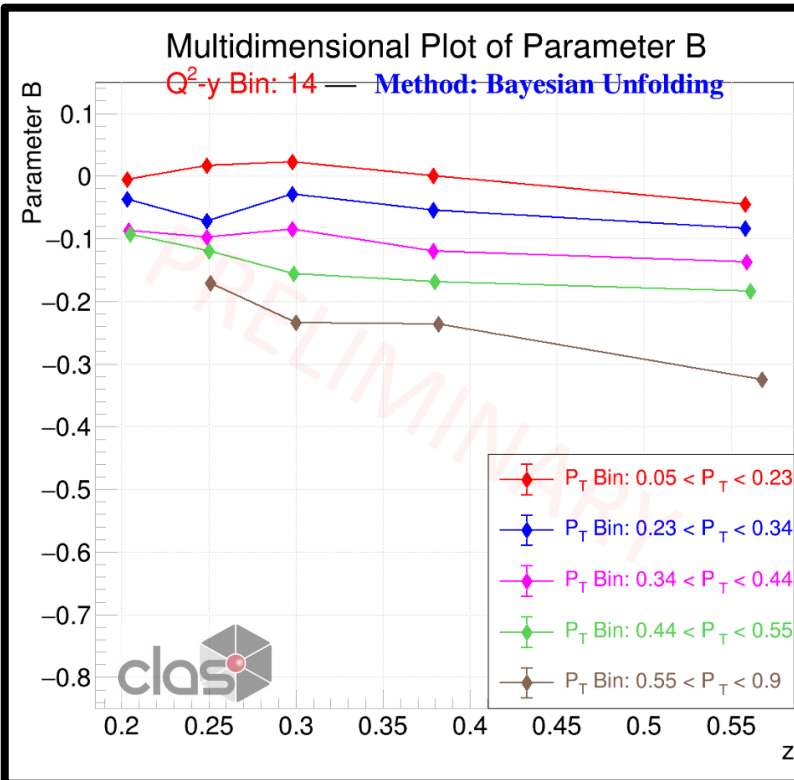
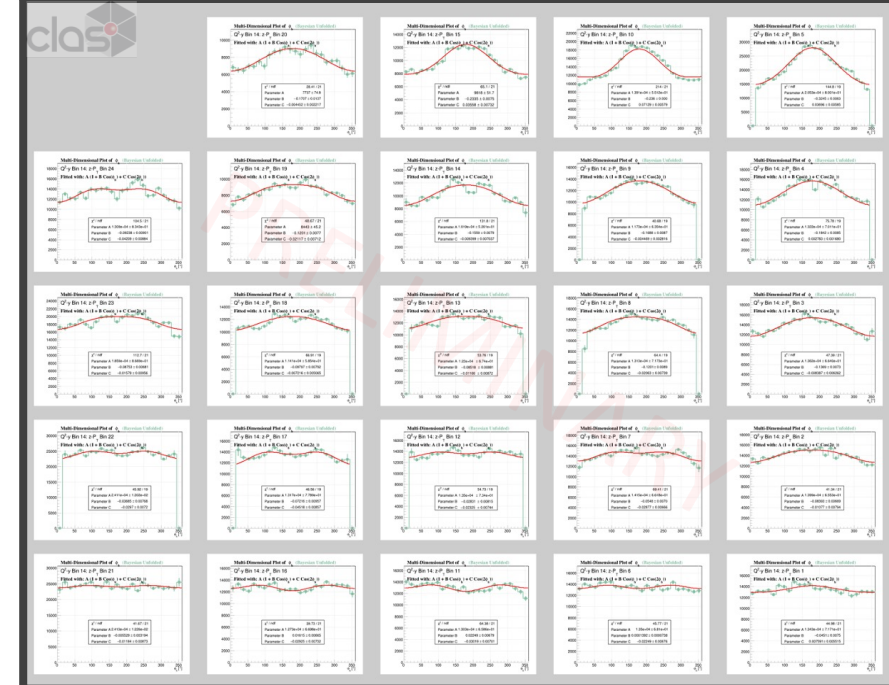
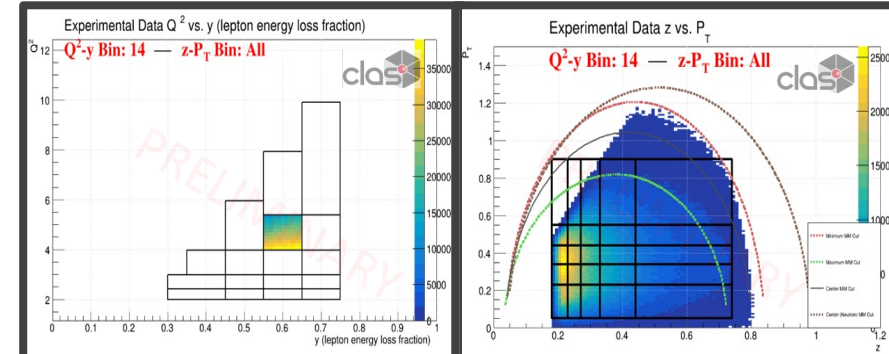
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Unfolded with Bayesian Method

Q<sup>2</sup>-y Bin 14



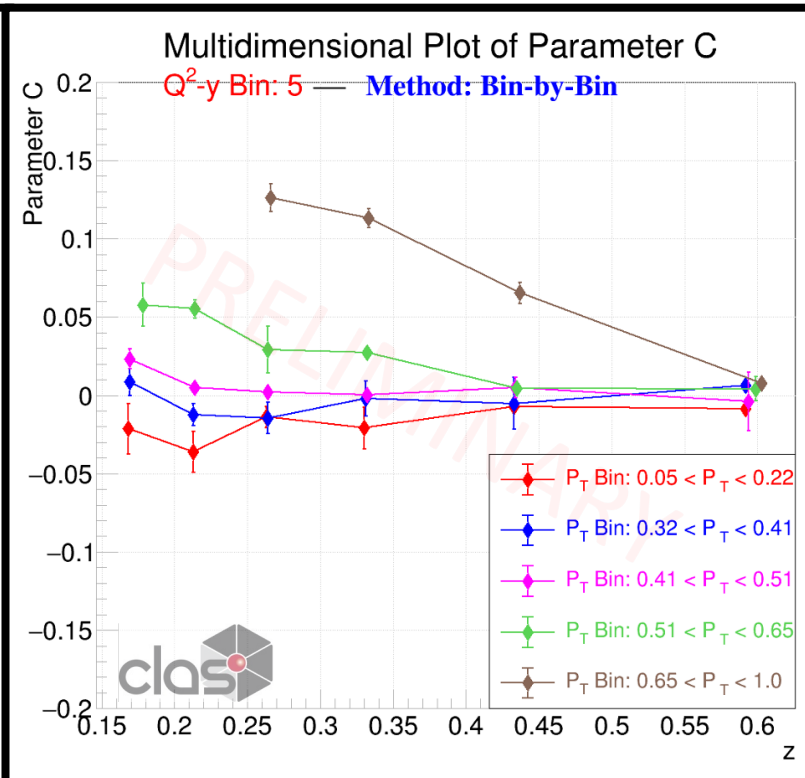
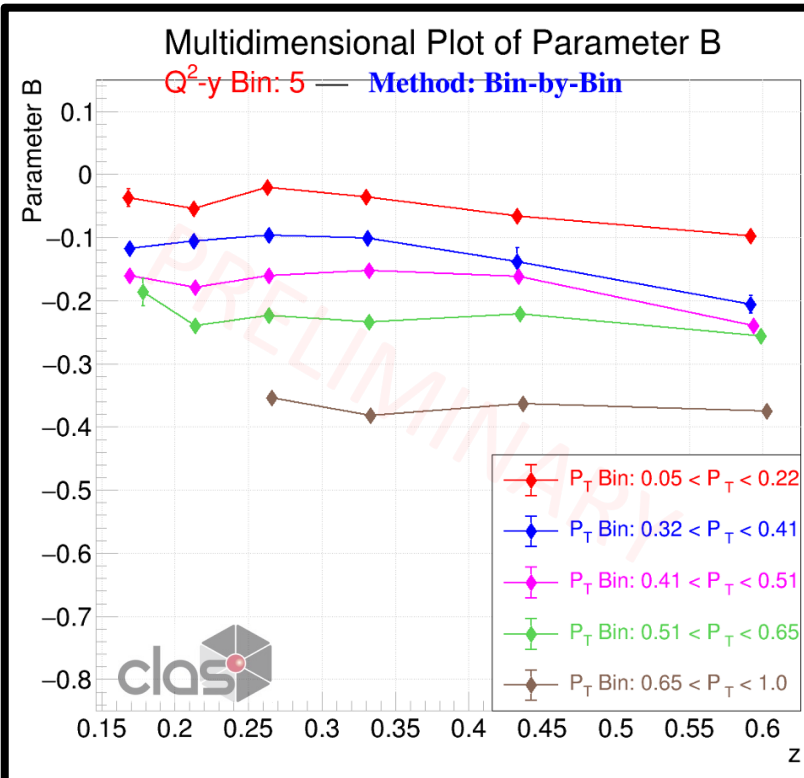
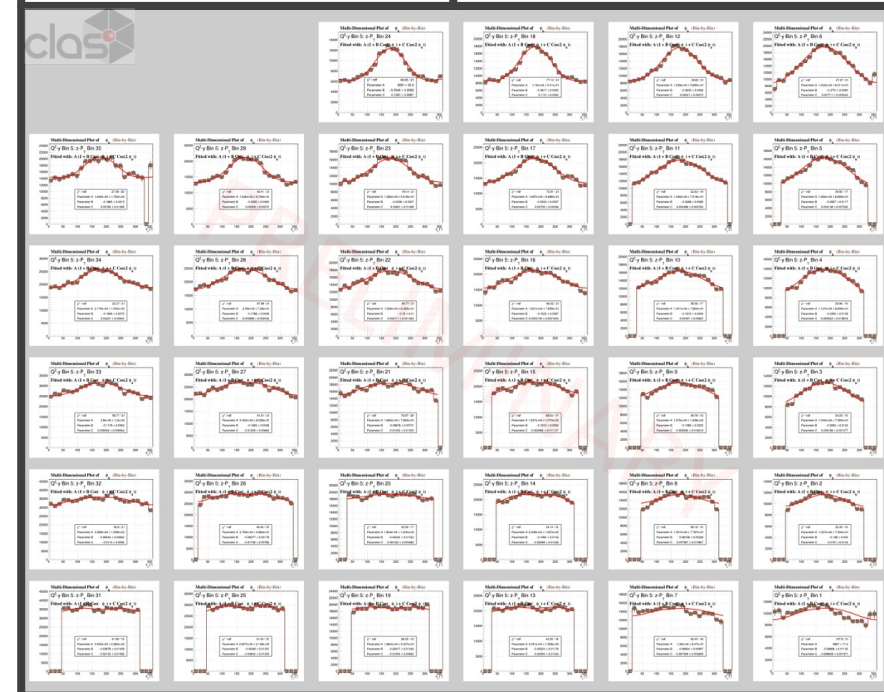
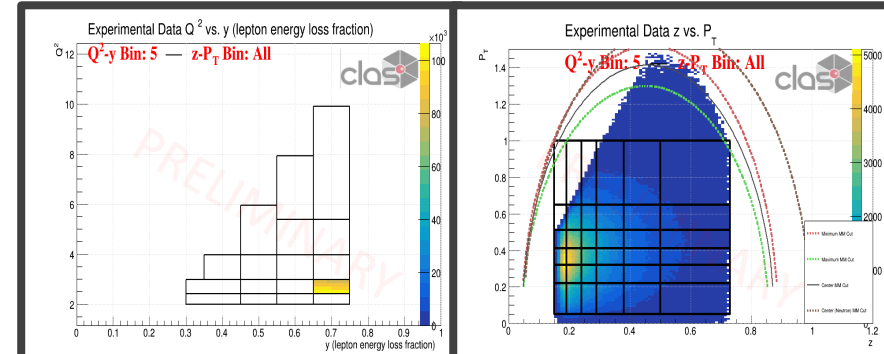
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$$B = A_{UU}^{\cos \phi_h} \quad C = A_{UU}^{\cos 2\phi_h}$$

$\phi_h$  Plots were fitted with:  
 $A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$

Corrected with Bin-by-bin Method

$Q^2$ -y Bin 5



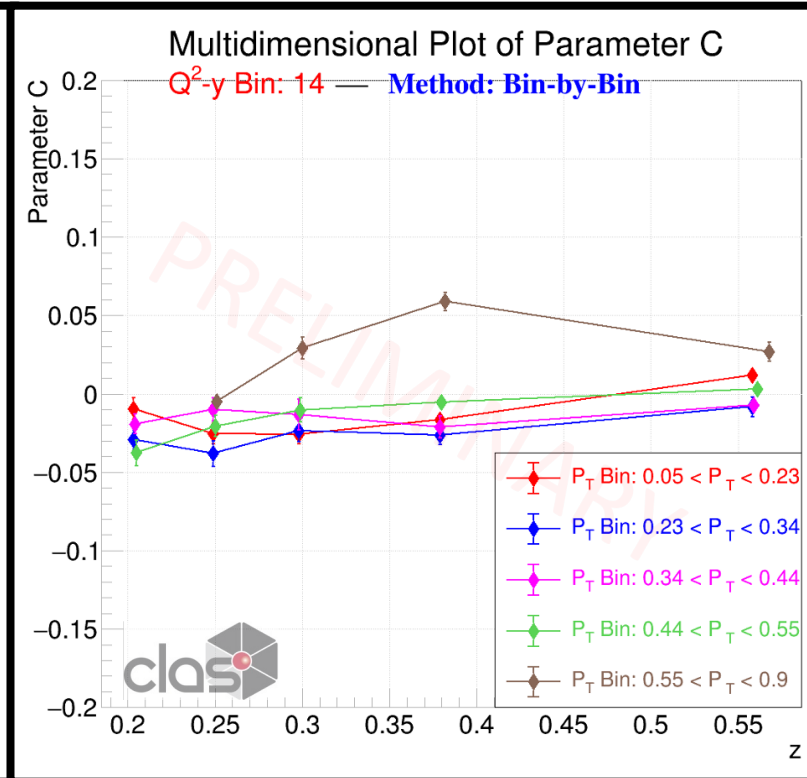
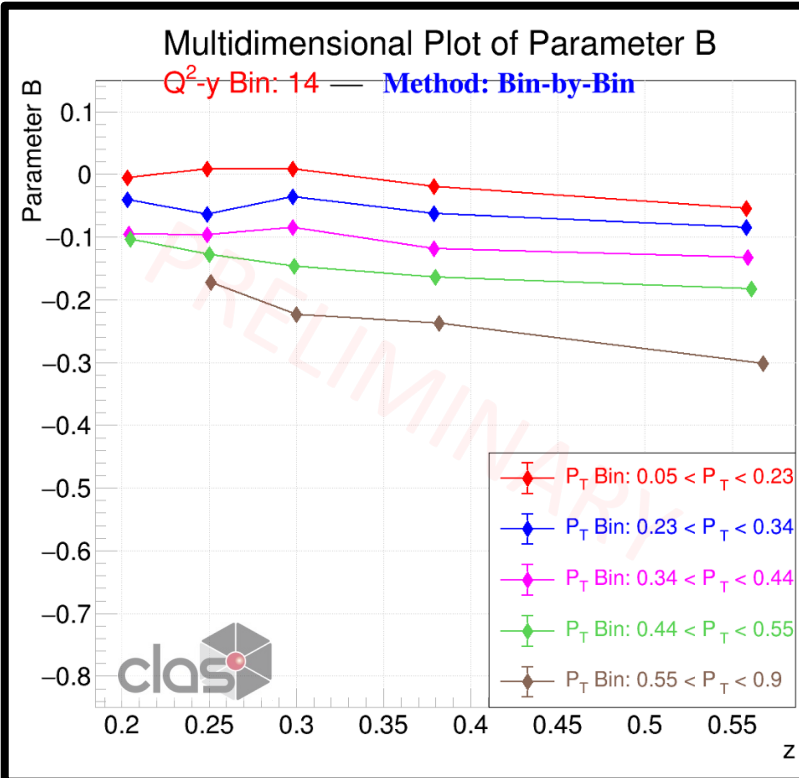
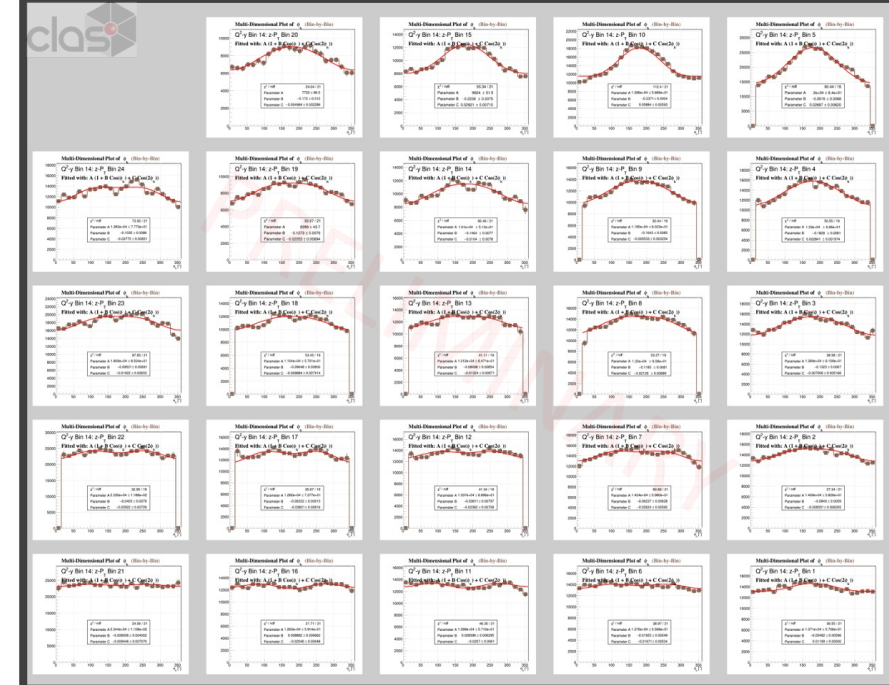
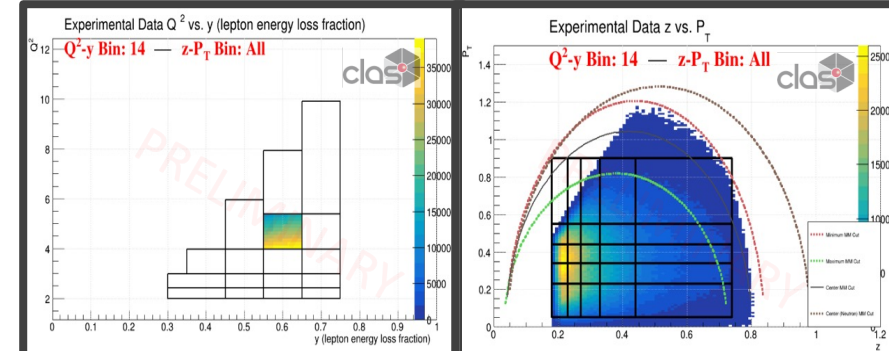
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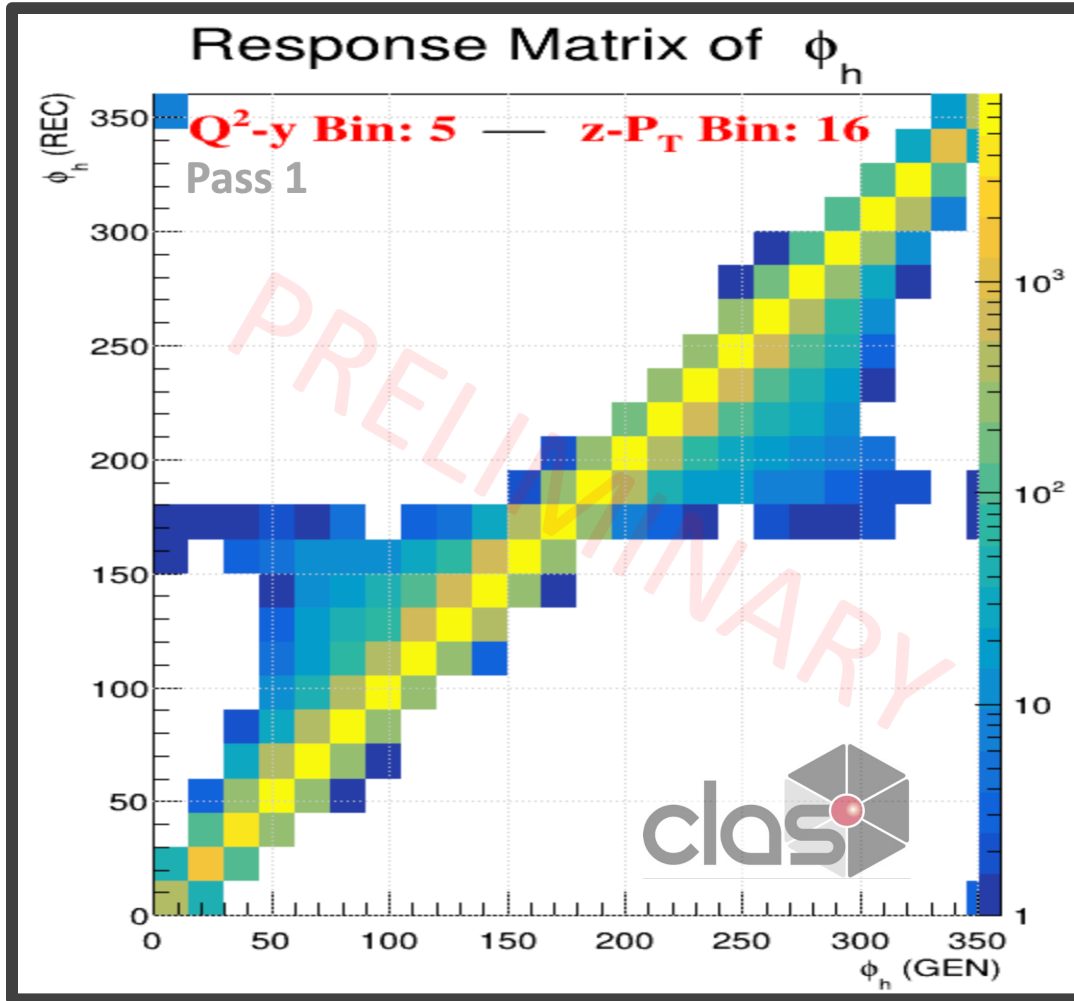
Corrected with Bin-by-bin Method

Q<sup>2</sup>-y Bin 14

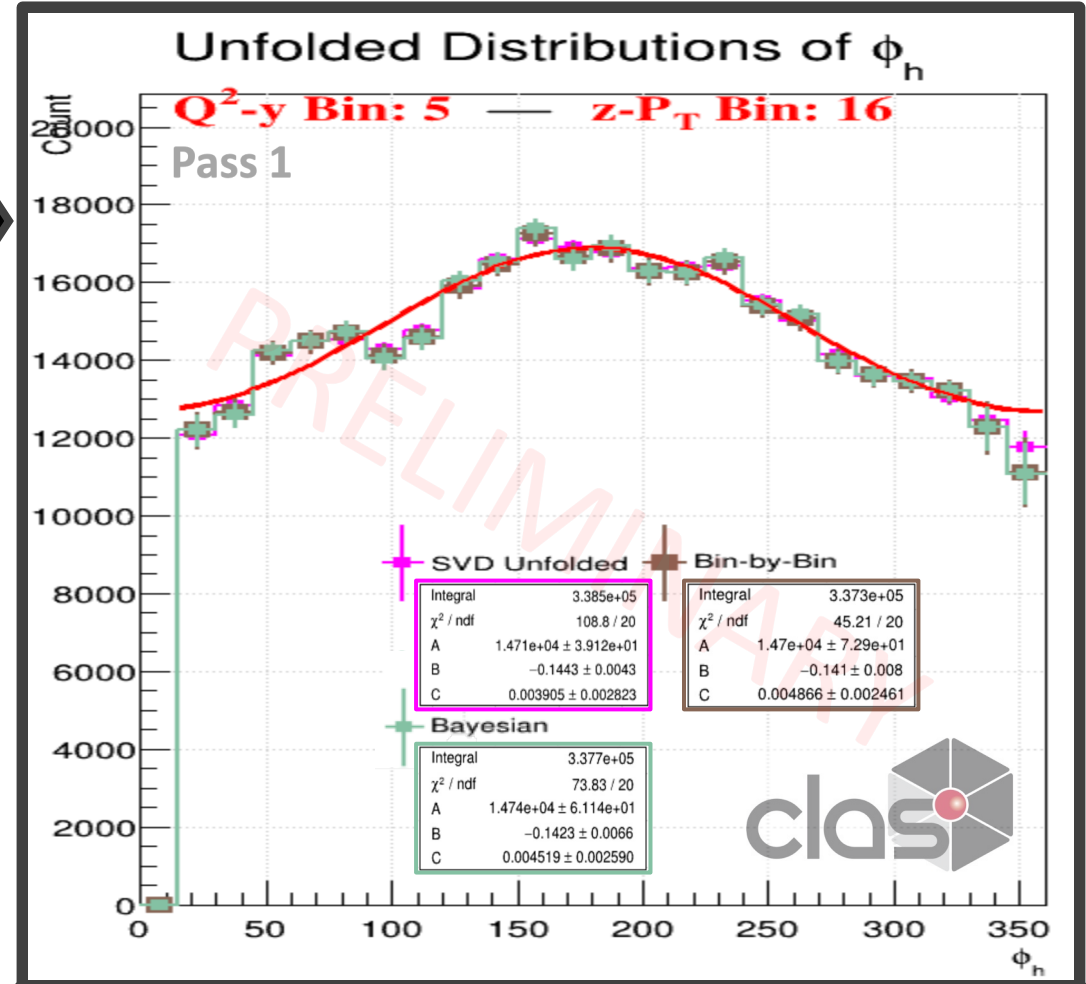


# Example of (1D) Unfolding Procedure

Using the Multidimensional Kinematic Bin from prior example



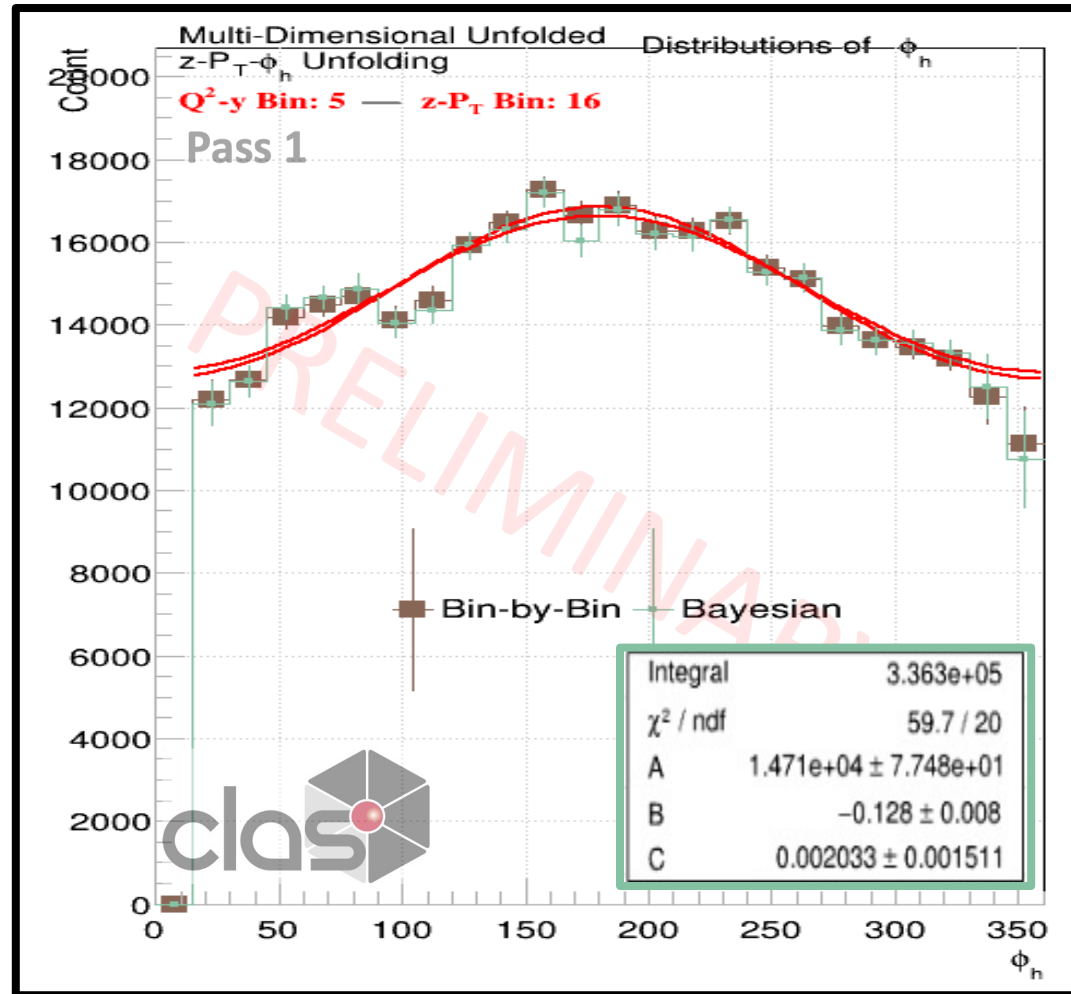
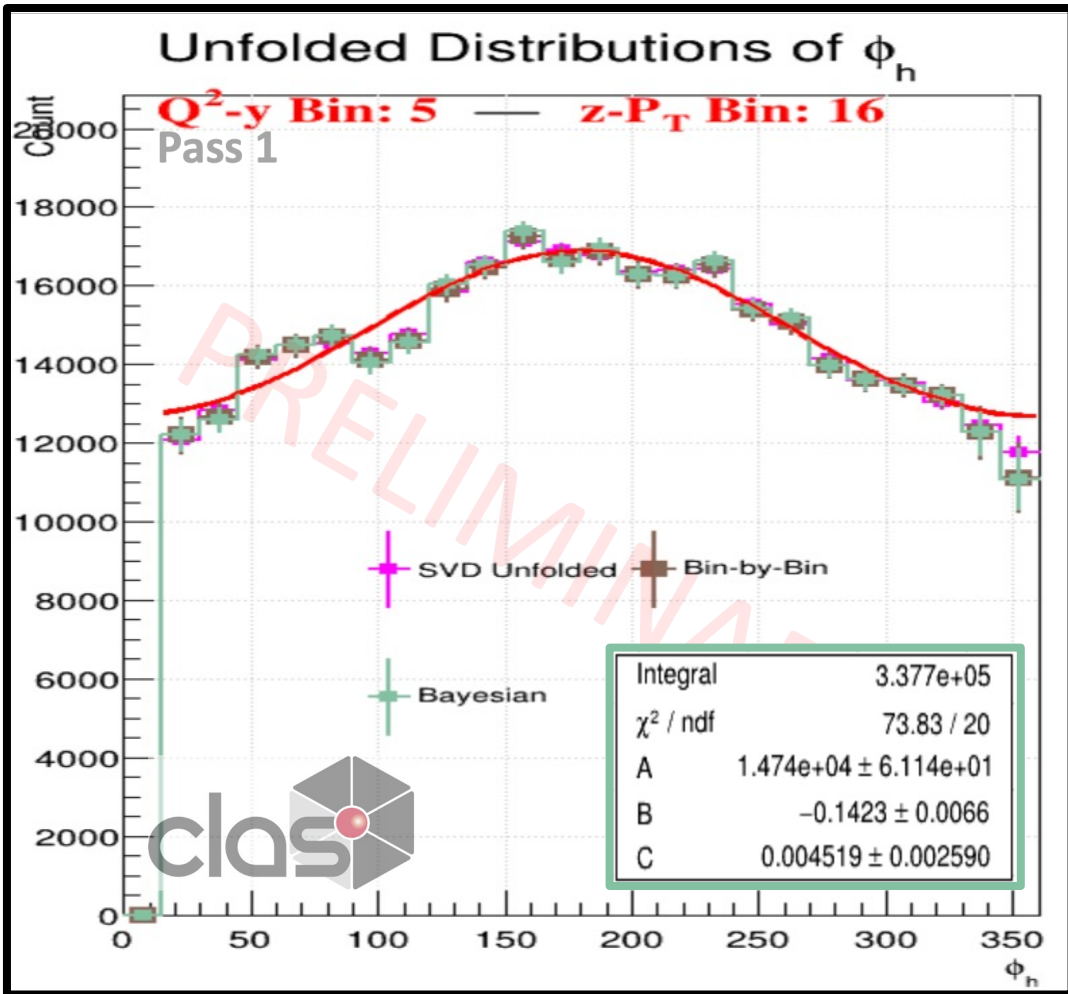
Unfolding Procedures



Parameters shown are from the fits previously described

# Comparisons of 1D and 3D Unfolding Procedure

Using the Multidimensional Kinematic Bin from the prior example for this comparison

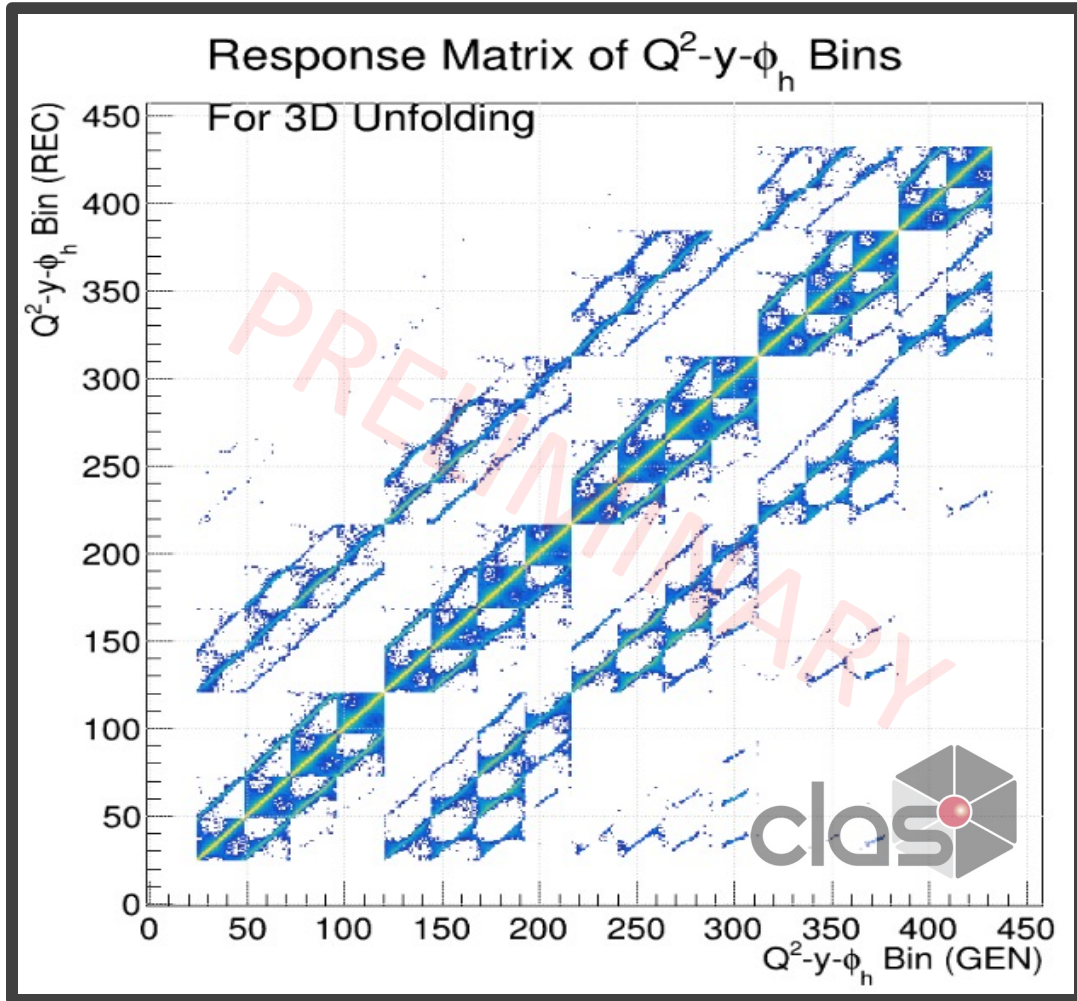


Bin-by-bin  
 Acceptance  
 Correction  
 gives the exact  
 same results

Bayesian  
 Unfolding  
 gives similar  
 results

# Example of (3D) Unfolding Procedure – Old Bins

Using  $Q^2$ - $y$ - $\phi_h$  Multidimensional Bins



Unfolding Procedure



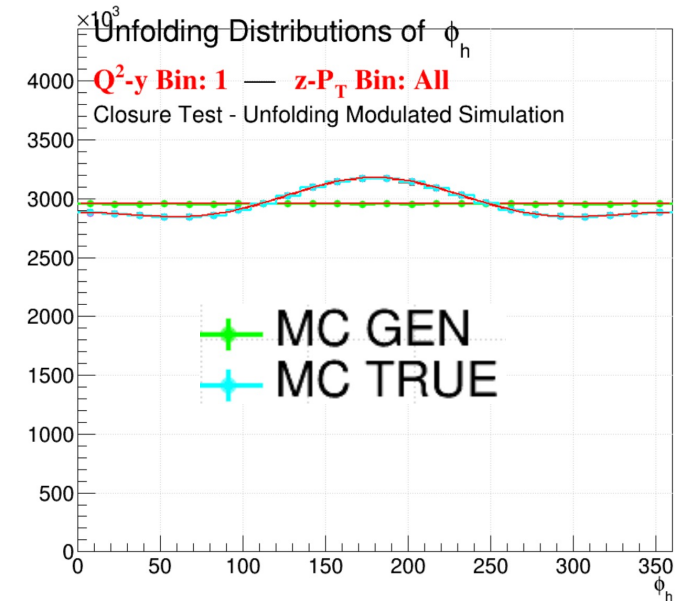
Unfolded with Bayesian Method

# Modulated Unfolding Closure Tests

- Modulated the MC distributions using the formula:

$$Weight = 1 + B \cos(\phi_h) + C \cos(2\phi_h)$$

- Gives the weight for each MC event based on generated  $\phi_h$
- Parameter values currently being used in this image:
  - $B = -0.05$  (Same for every  $z-P_T$  bin)
  - $C = 0.025$
- Modulated MC REC is then unfolded using the un-modulated response matrix (in 1D and Multi-Dim examples) and compared with 'MC TRUE'
  - MC TRUE is the modulated MC GEN distribution
  - Also performed a closure test of unfolding the un-modulated MC REC distribution with the un-modulated response matrix to ensure the method was applied properly

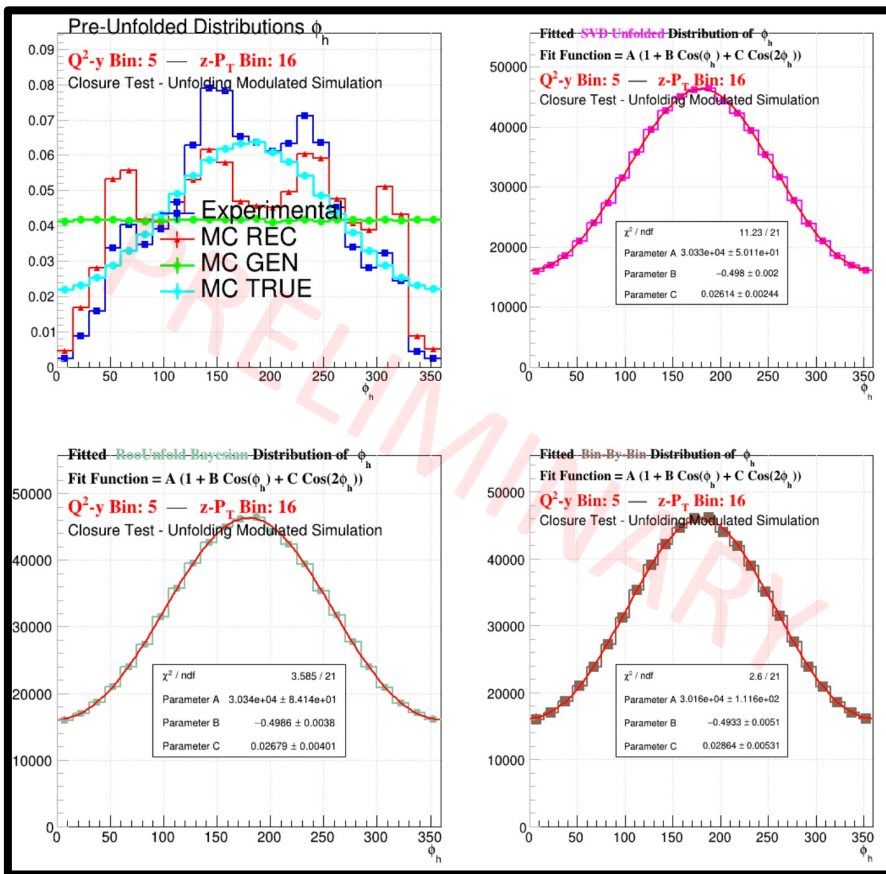


# Modulated Unfolding Closure Tests

The parameters used for weighing modulations below are:

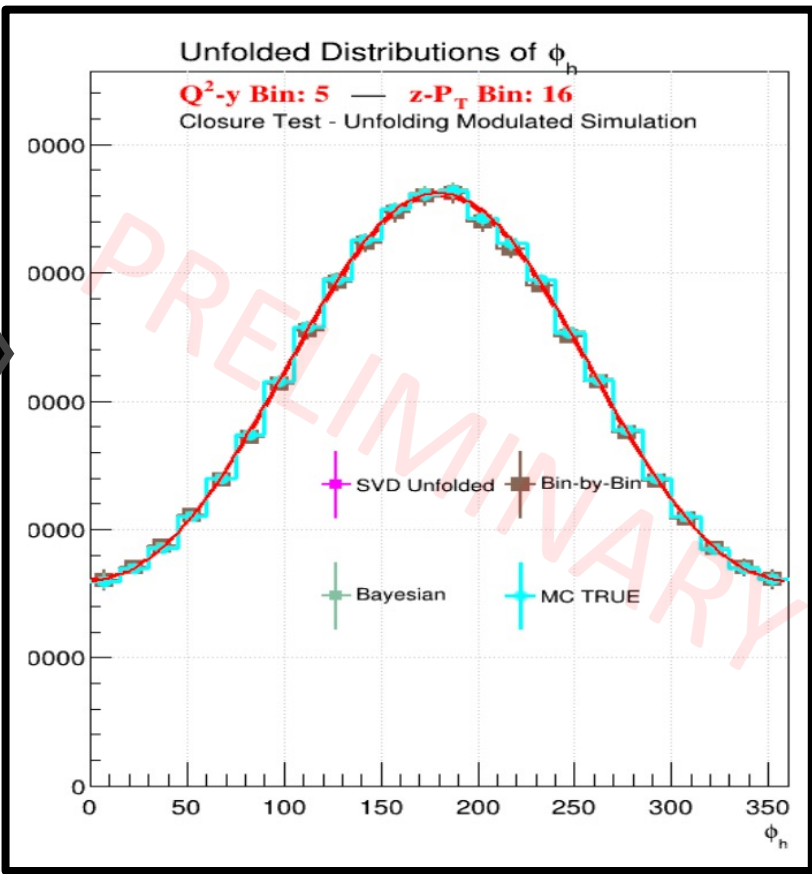
$$B = -0.5 \text{ and } C = 0.025$$

Results show that an **unmodulated** Simulation can correct distributions **with modulations**



Checking that the corrected distributions match MC TRUE

Fits are within the margin of error of the defined parameters

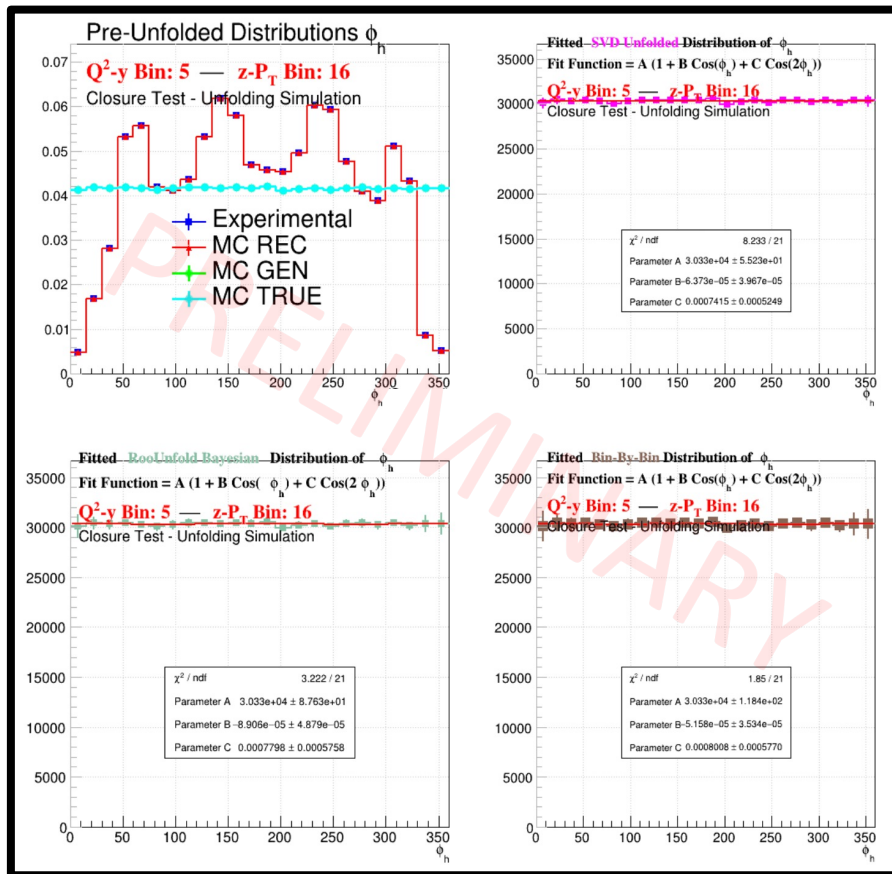




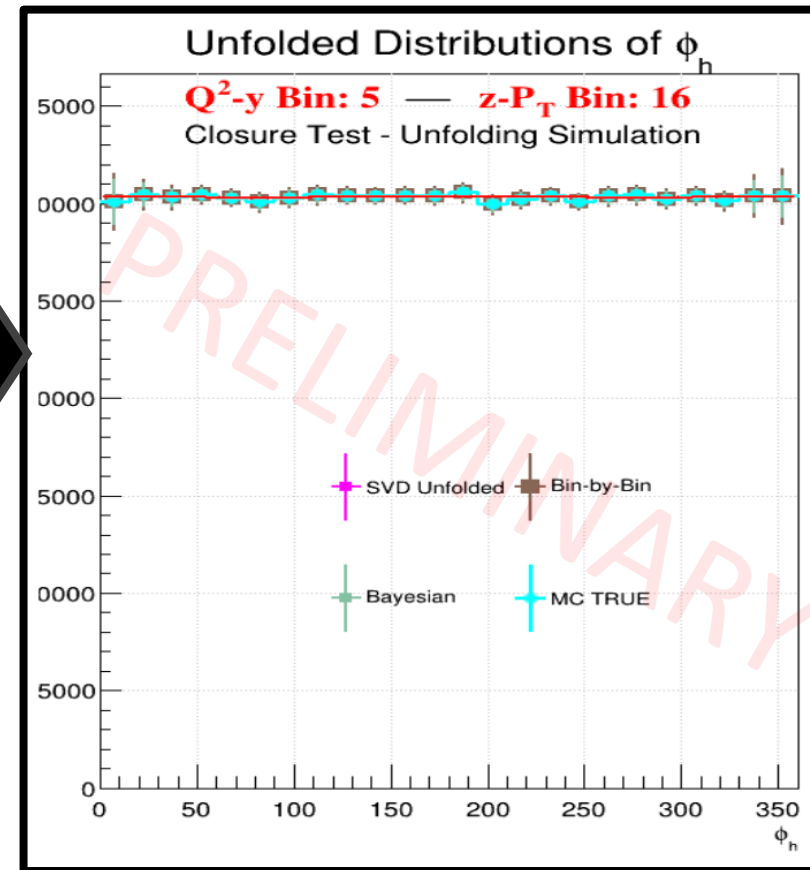
# Other Unfolding Closure Tests

Other closure tests being used to check that Unfolding is done properly:

- Replace the experimental data with the reconstructed Monte Carlo (no modulations)
  - Should return the generated (i.e., MC TRUE) distribution



Checking that the corrected distributions match MC TRUE

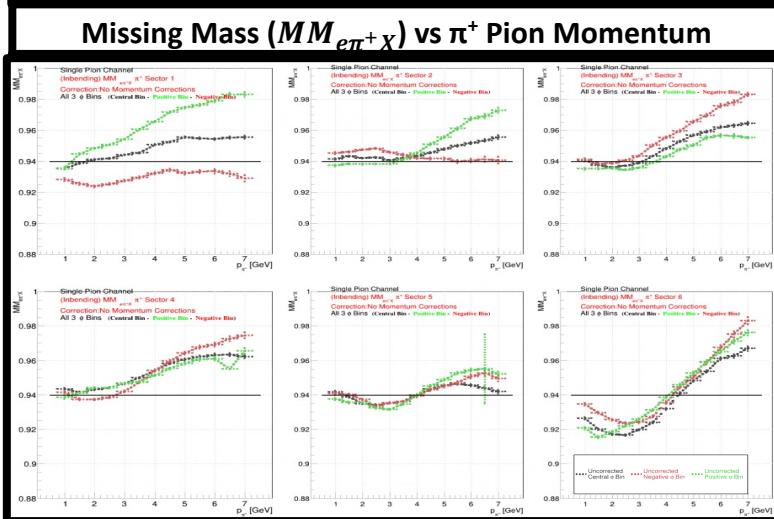
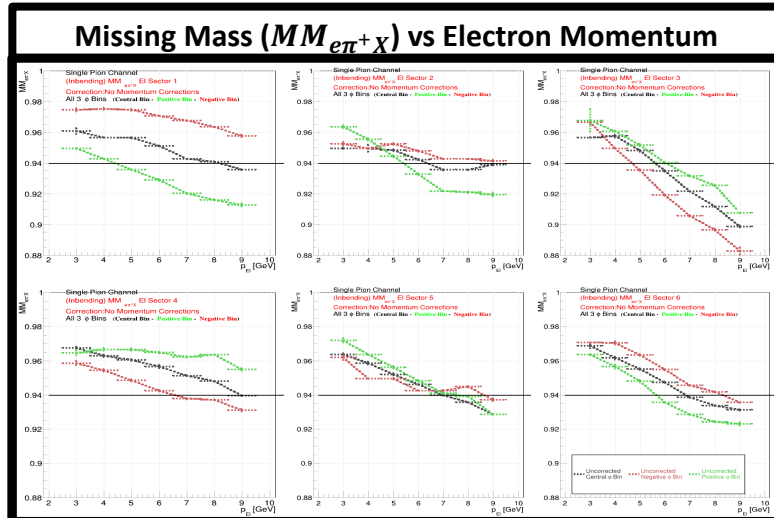


# Momentum Corrections from Exclusive Events

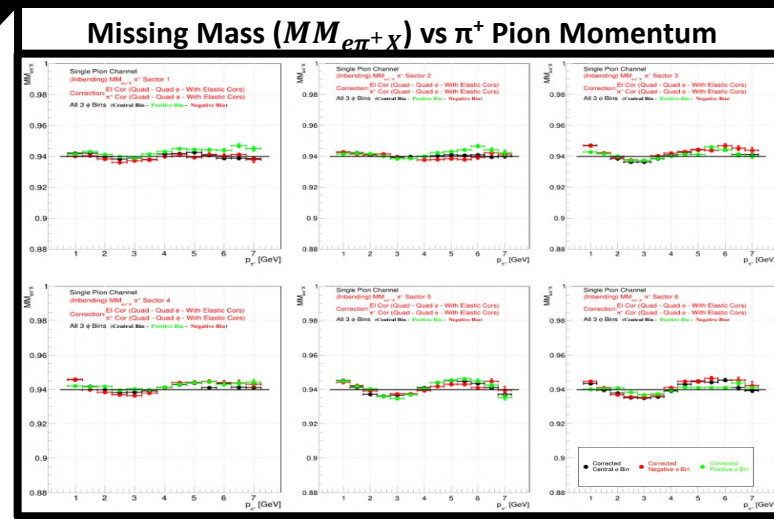
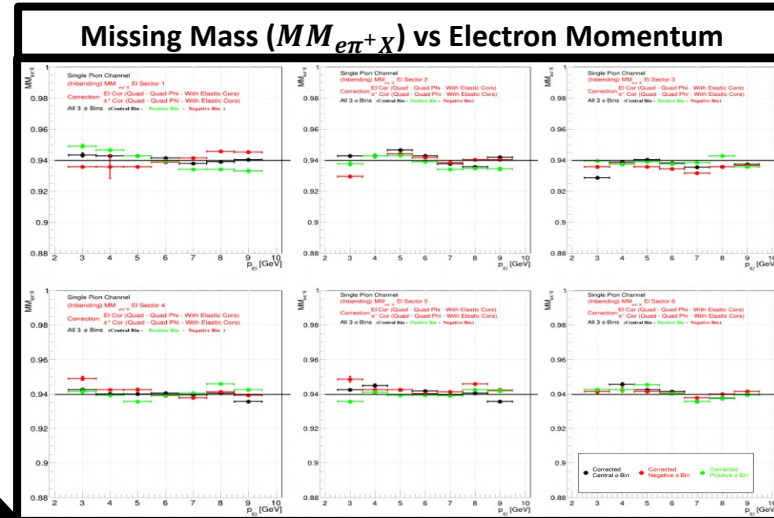
- Momentum corrections are developed for the RG-A data being used in this analysis
- Designed to correct for kinematic-dependent reconstruction issues in the experimental data using well-understood reactions
- Use exclusive reactions to correct the particles' momentum as sector-dependent functions of the particles' measured azimuthal angle ( $\phi_{\text{lab}}$ ) and momentum
  - The primary reaction used for the electron and  $\pi^+$  pion is  $ep \rightarrow e'\pi^+(N)$
  - Elastic scattering process also used to help correct the electron momentum
- Developed from momentum 4-vector conservation to calculate the ideal momentum of a particle from exclusive reactions based on the kinematics of the other particle(s)
  - Correction is taken by plotting the difference between this calculation and the measured momentum as functions of the measured momentum and  $\phi_{\text{lab}}$

# Momentum Corrections from Exclusive Events

These plots show Missing Mass vs. particle momentum in 3  $\phi$  bins for all 6 sectors of the detector before/after momentum corrections – Corrections are quadratic functions of  $\phi$  and momentum

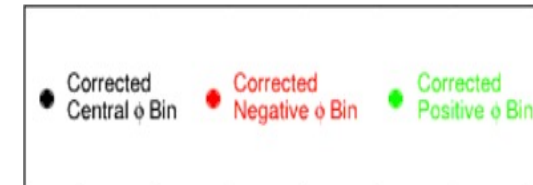
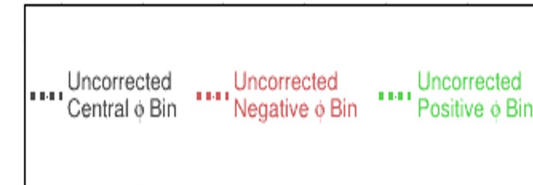


Apply Momentum Corrections



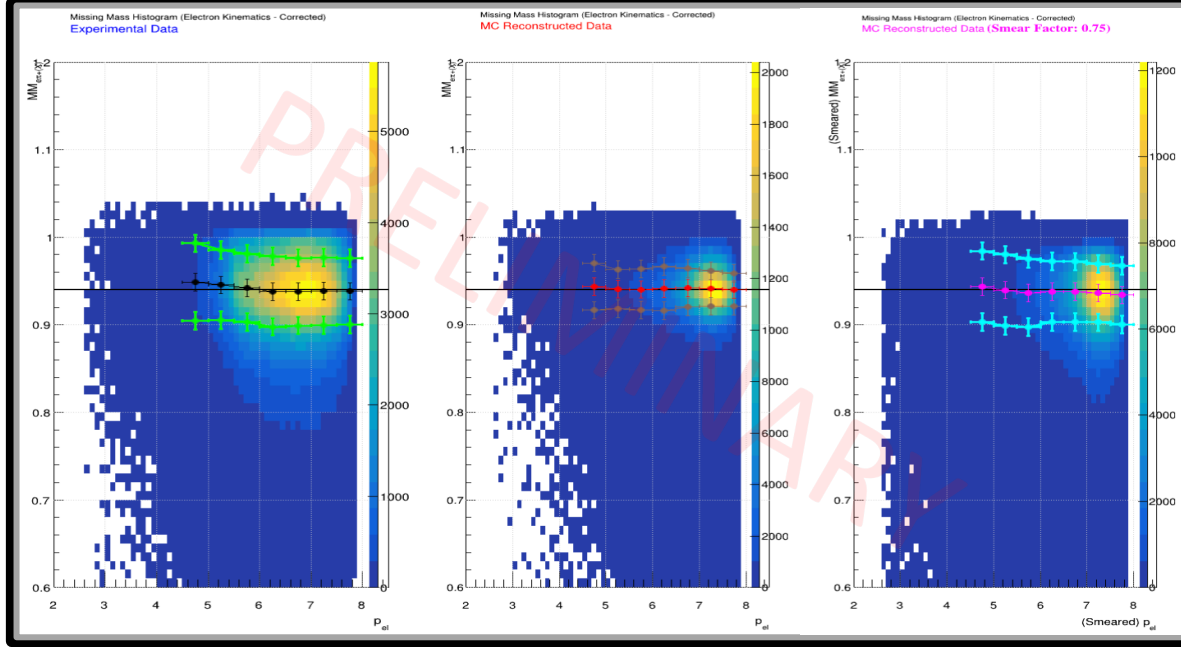
All Plots here are from Pass 1

(Pass 2 corrections are still in early development)

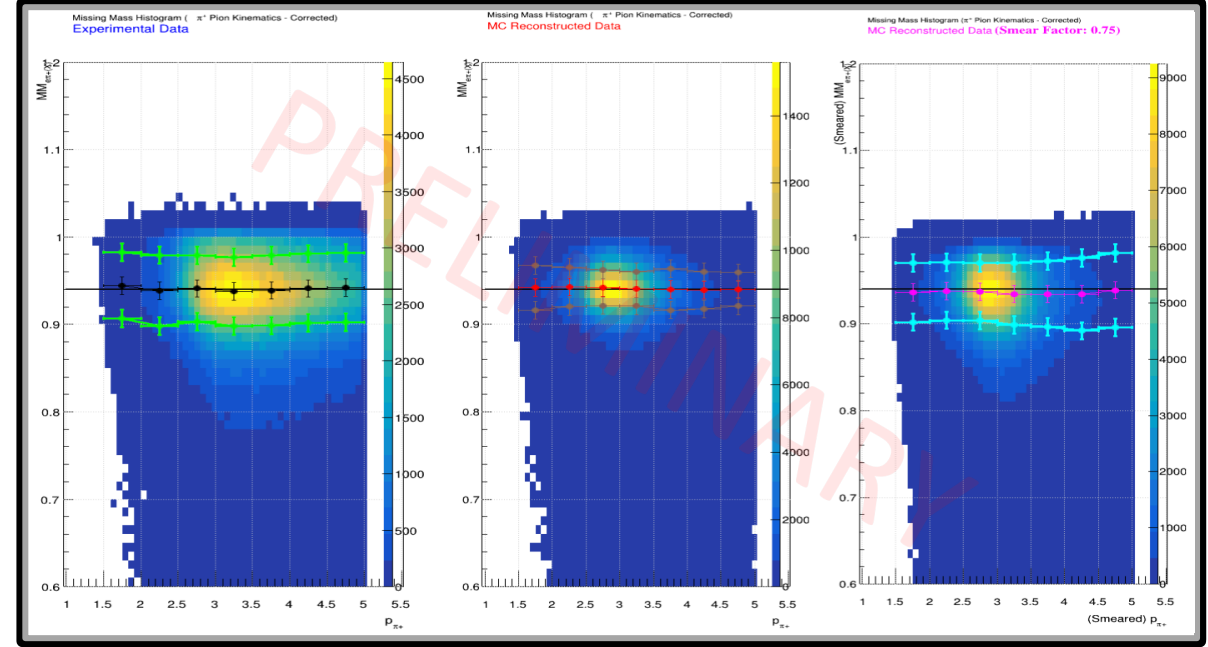


# Momentum Smearing – Pass 1

## Missing Mass vs Electron Momentum:



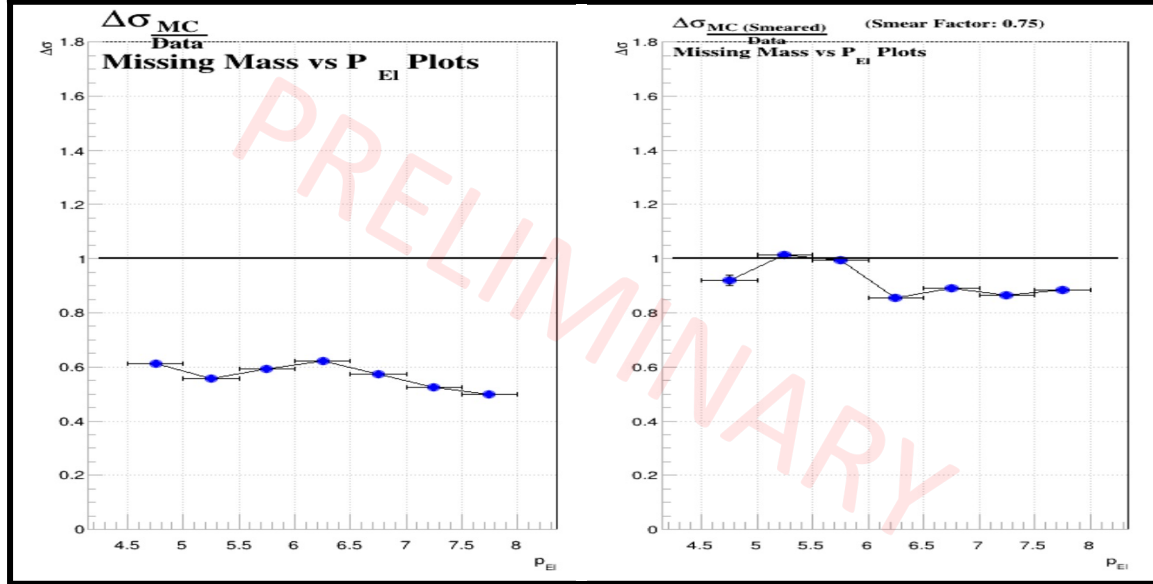
## Missing Mass vs $\pi^+$ Pion Momentum:



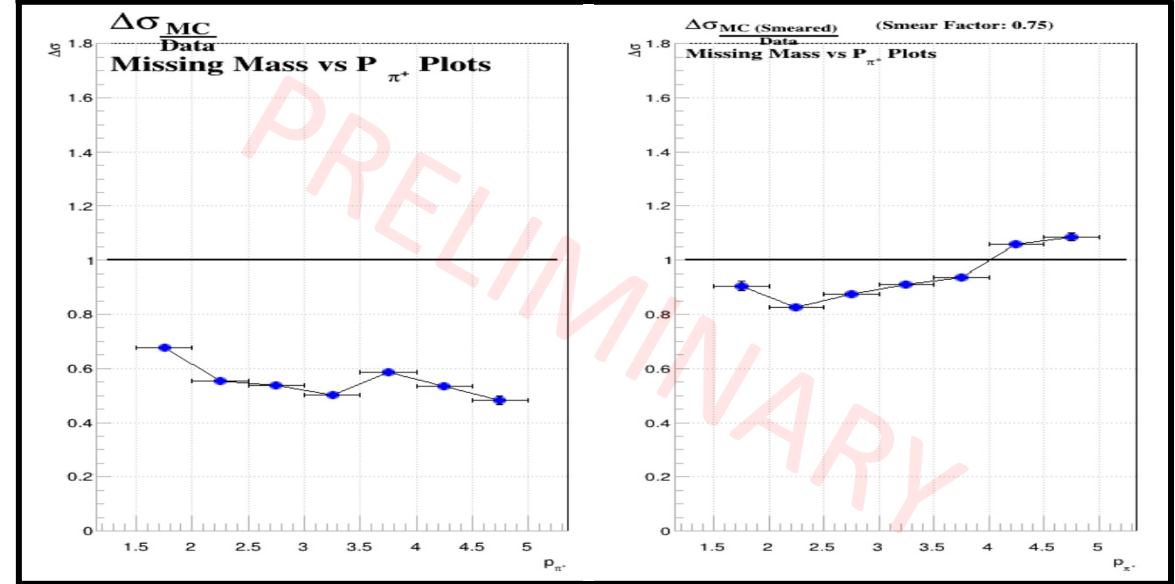
- The momentums of the particles in these plots are CORRECTED (see Momentum Corrections from Exclusive Events)
- Momentum Smearing is applied in addition to existing MC reconstruction processes
- The momentum smearing functions use 2D Missing Mass plots to check how it improves the MC
  - The widths of the peaks are shown in each plot above
- Momentum smearing is done with the equation:  $P_{\text{Smeared}} = P_{\text{Reconstructed}} + \text{SF} * (P_{\text{Reconstructed}} - P_{\text{Generated}})$ 
  - **SF** is the smear factor used to modify the simulated reconstructed momentum (currently equal to 0.75)
- A properly smeared MC distribution should have approximately the same width as the Experimental data

# Momentum Corrections/Smearing – Pass 1

Ratio of Missing Mass Width vs Electron Momentum:



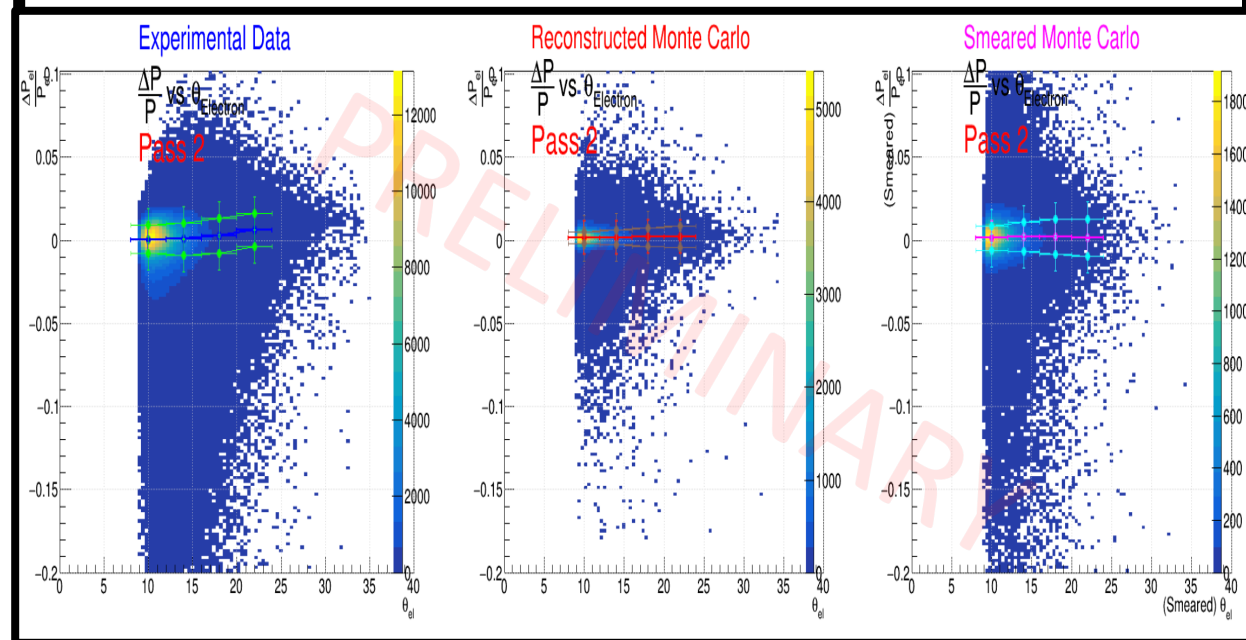
Ratio of Missing Mass Width vs  $\pi^+$  Pion Momentum:



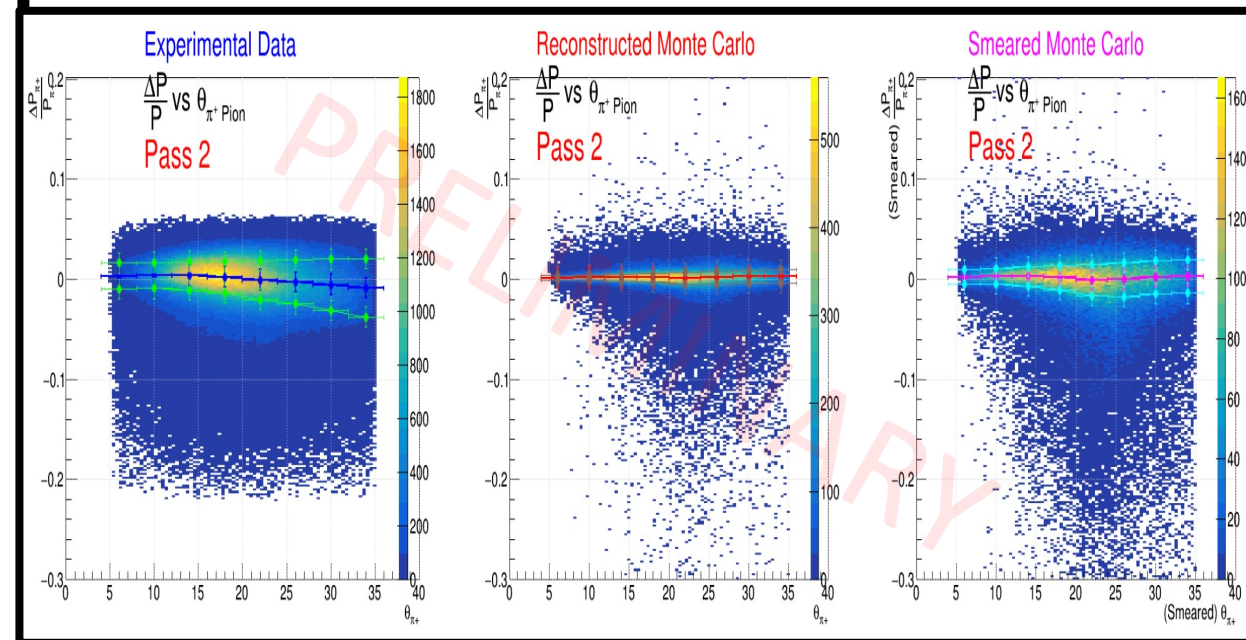
- The ratio of the Monte Carlo and Experimental data's widths should go to 1 as smearing improves
- Smearing the momentum also affects the widths of the Missing Mass vs azimuthal/polar angles of the particles
- Development of this correction calls for finding the best smearing parameter for all particle kinematics

# Momentum Smearing – Pass 2

$\Delta P/P$  vs  $\theta$  Plots for Electron Kinematics:



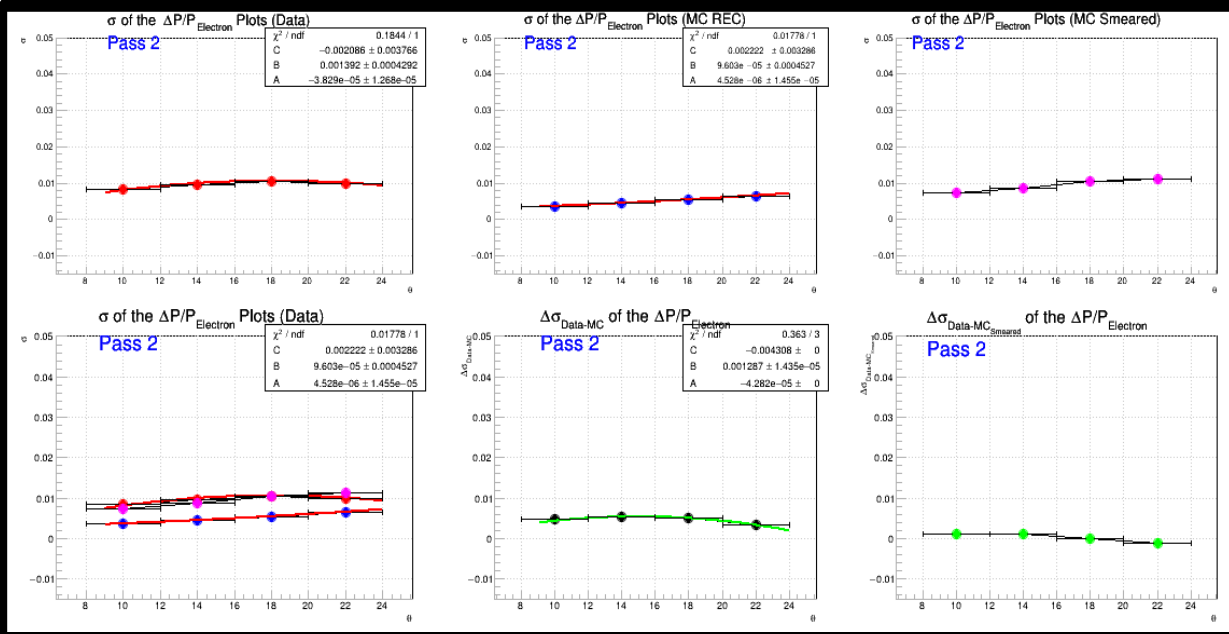
$\Delta P/P$  vs  $\theta$  Plots for  $\pi^+$  Pion Kinematics:



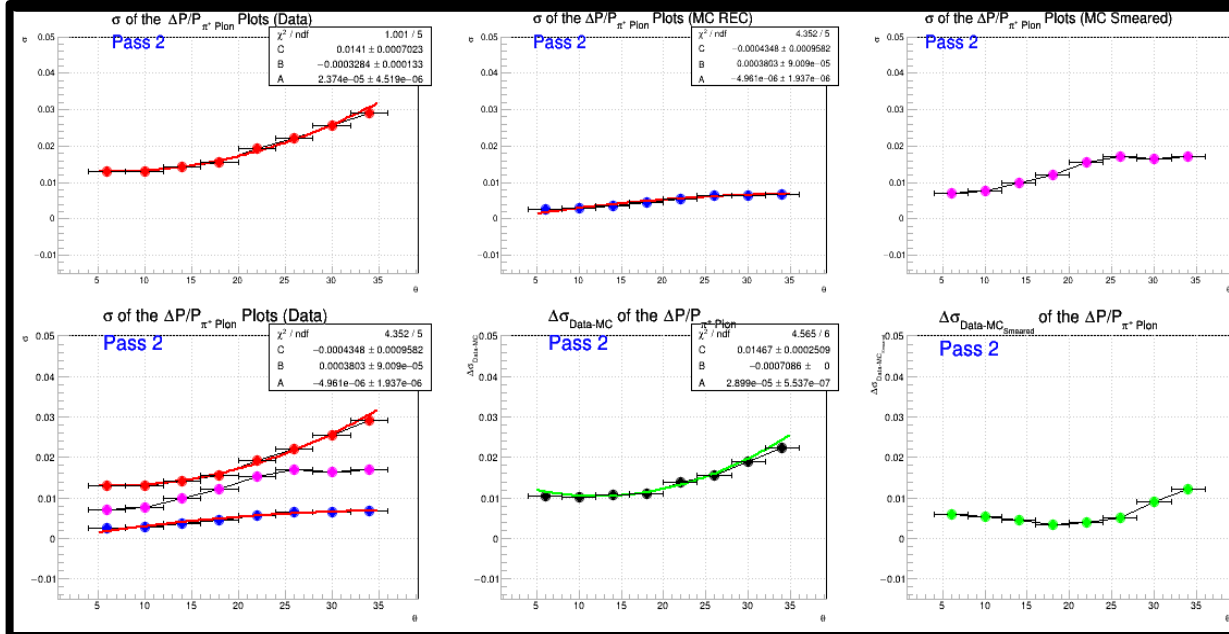
- The momentums of the particles in these plots do NOT include Momentum Corrections from Exclusive Events
- The momentum smearing procedure uses 2D  $\Delta P/P$  vs  $\theta$  plots to check the resolution matching between Data and MC
  - The resolution is defined as the widths of the peaks that are shown in each plot above
- Current Momentum smearing is done with the equation:  $\mathbf{P}_{\text{Smearred}} = \mathbf{P}_{\text{Reconstructed}} + \text{SF} * (\mathbf{P}_{\text{Reconstructed}} - \mathbf{P}_{\text{Generated}})$ 
  - SF is the smear factor used to modify the simulated reconstructed momentum (currently equal to 1.75)
- New (Ideal) form of Smearing Function (not yet applied) would be:  $\mathbf{P}_{\text{Smearred}} = \mathbf{P}_{\text{Reconstructed}} + (\mathbf{P}_{\text{Reconstructed}}) * \sigma_{\text{SF}}(\theta) * \text{SF} * (\text{gaus}(0,1))$ 
  - $\sigma_{\text{SF}}(\theta)$  is the main smearing factor (function of  $\theta$ ) based on the fits of the  $\Delta P/P$  vs  $\theta$  plots above
  - The **gaus(0,1)** adds some randomness to the smearing while SF is still a static smear factor meant to help control the amplitude of smearing
- A properly smeared MC distribution should have approximately the same width as the Experimental data

# Momentum Smearing – Comparison of Widths - Pass 2

Widths ( $\sigma$ ) vs  $\theta$  Plots for Electron Kinematics:



Widths ( $\sigma$ ) vs  $\theta$  Plots for  $\pi^+$  Pion Kinematics:

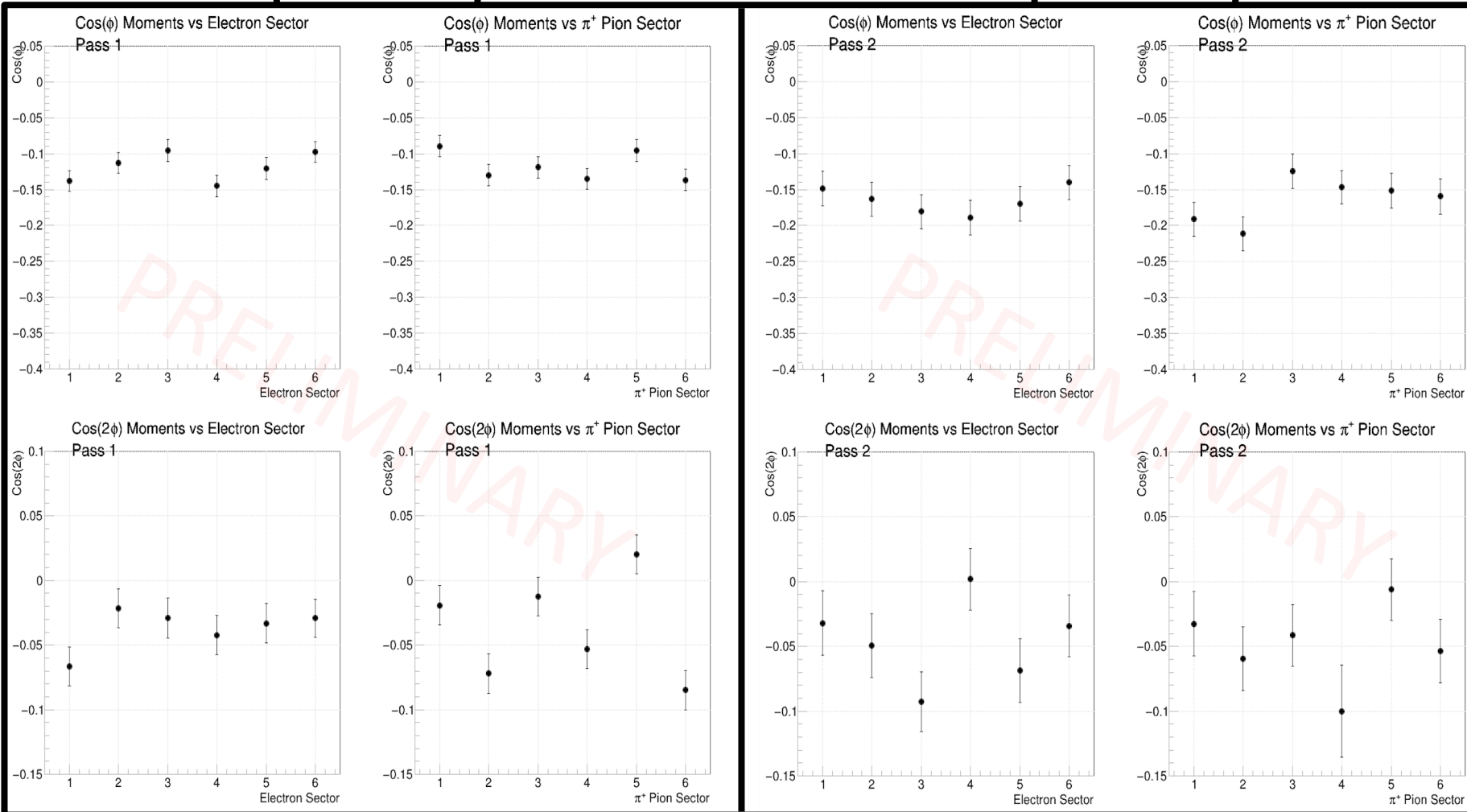


- The **Bottom Center** and **Bottom Right** plots show the differences between the widths of **Data** and **unsmearred/smearred MC**
  - The difference should go to 0 as resolution becomes a better match
- $\sigma_{\text{SF}}(\theta)$  can come from the **Bottom Center** plot to see how much more the MC Reconstructed momentum needs to be smeared to match the Experimental Data
  - Smeared plots here still use a static smearing factor instead of  $\sigma_{\text{SF}}(\theta)$

# Sector Correlations with $\text{Cos}(\phi)$ and $\text{Cos}(2\phi)$ Measurements

**PASS 1**

**PASS 2**



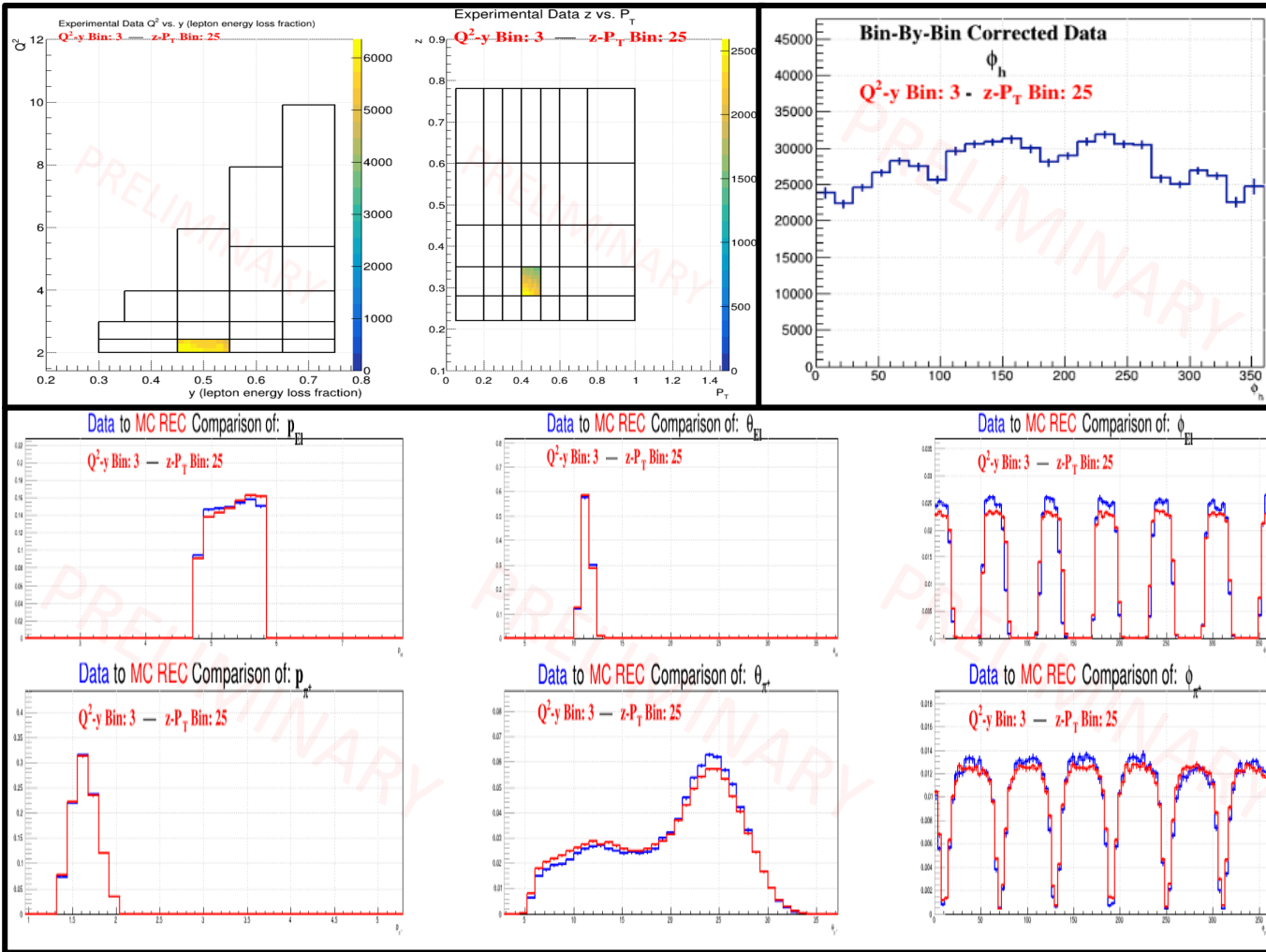
Showing the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  Moments as functions of the particle sector

These plots show those differences in Pass 1 and Pass 2 for when the Electron (left plots) or  $\pi^+$  pion (right plots) are restricted to being detected in a single sector

Images are grouped on the left and right based on Pass version of the data being used



# Sector Correlations with $\phi_h$ Distributions – Old Binning

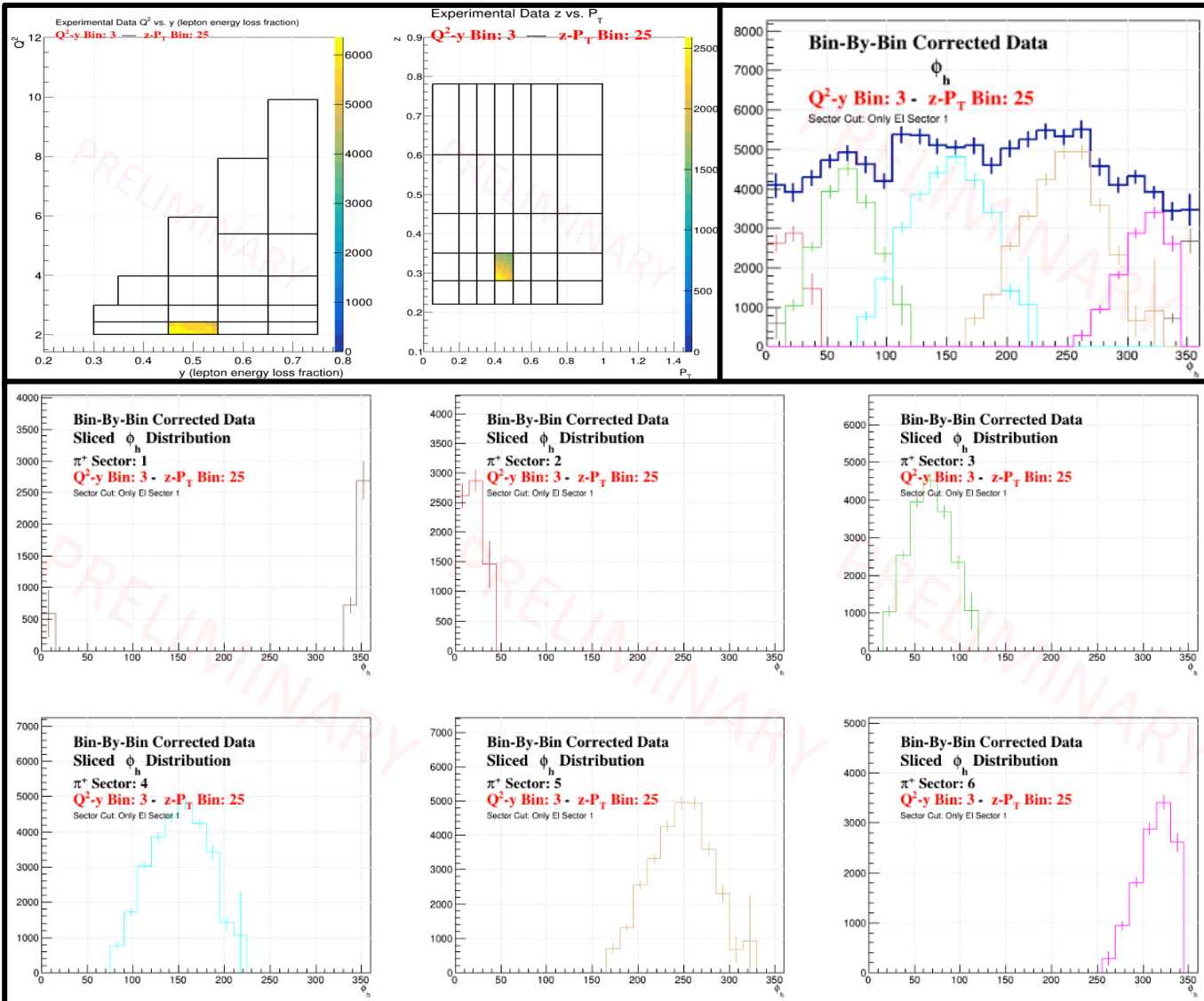


**Issue:** Some bins seem to have additional modulations not explained by the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  moments

- The 6 peak structure could be related to the forward detector sectors
- Plots below show the lab angles and momentum of both particles within the given kinematic bin of  $Q^2$ ,  $y$ ,  $z$ , and  $P_T$

\*Note: This example uses a slightly older version of the binning scheme and Pass 1 Data

# Sector Correlations with $\phi_h$ Distributions – Old Binning



**Issue:** Some bins seem to have additional modulations not explained by the  $\text{Cos}(\phi)$  and  $\text{Cos}(2\phi)$  moments

- The 6 peak structure could be related to the forward detector sectors
- Plots show the  $\phi_h$  distributions separated based on which sector the  $\pi^+$  pion is detected
- **Additional Requirement: Electron in Sector 1**
- This suggests that the effect is related to mismatching in sector acceptance between Data and Monte Carlo

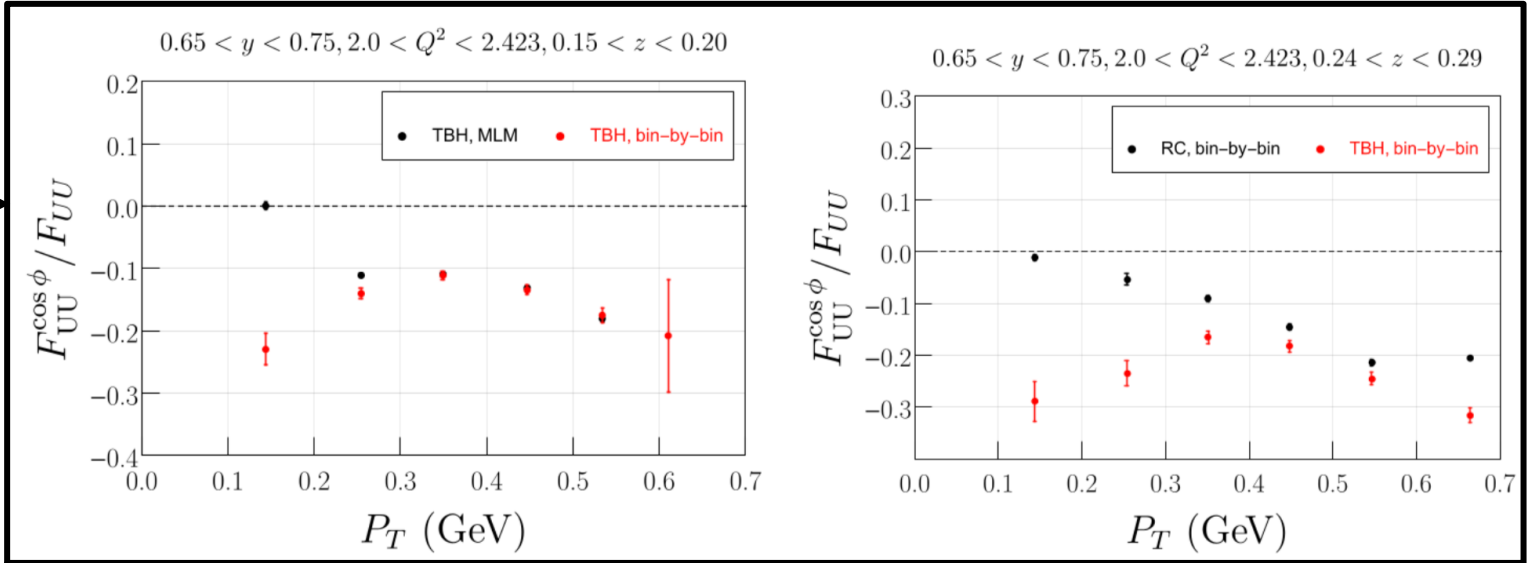
\*Note: This example uses a slightly older version of the binning scheme and Pass 1 Data

# Ongoing Cross-Checks with T. Hayward

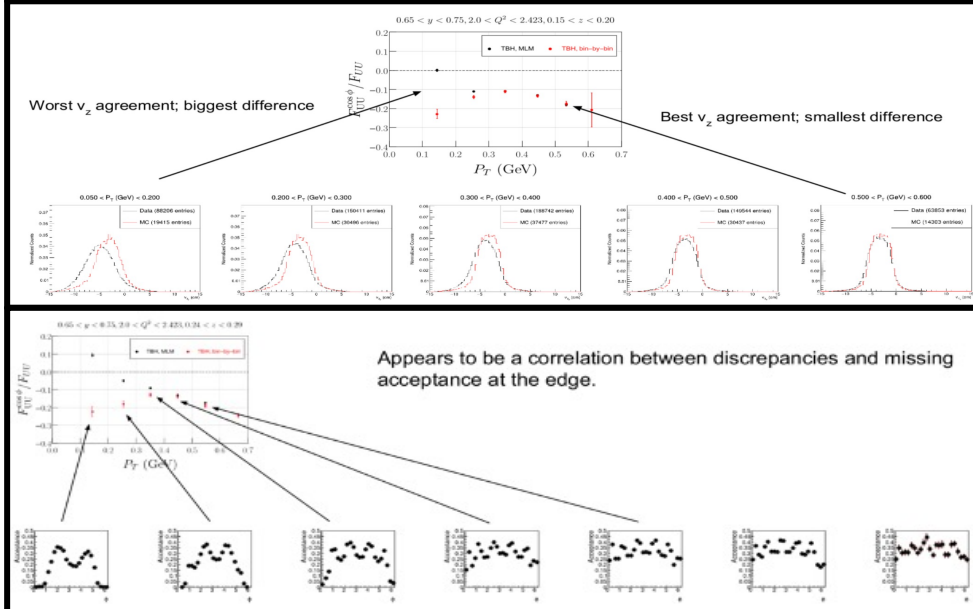
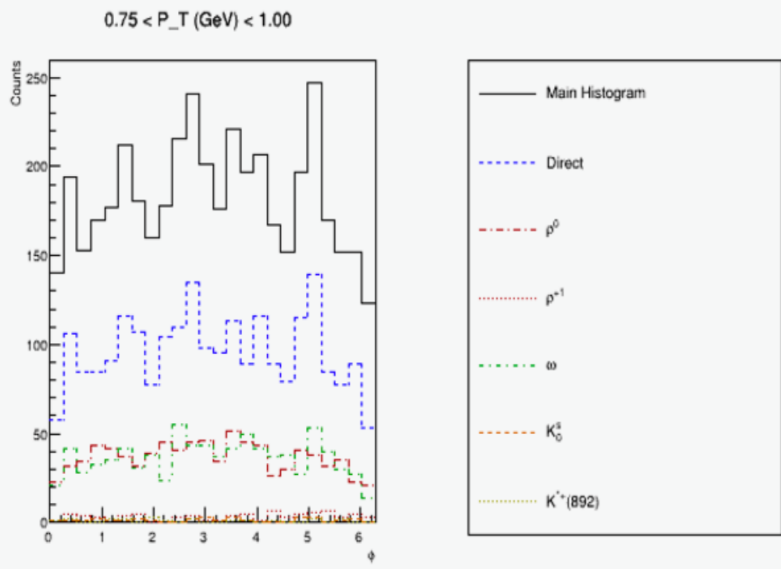
## Comparisons between T. Hayward's measurements (TBH) of the $\text{Cos}(\phi_h)$ Moments and mine (RC)

- Comparison is between different different fit methods
  - MLM  $\rightarrow$  Maximum Likelihood Method
- TBH  $\rightarrow$  Uses Pass 2 Data
- RC  $\rightarrow$  Uses Pass 1 Data

\*All images on this slide were created by T. Hayward\*



## Vector Meson Contributions to $\phi_h$ Distributions



## Investigations into discrepancies

### ← Suspicious Vertex Discrepancies between Data and MC

- Possibly coincidental based on other results in different kinematic regions

### ← Acceptance effects on the discrepancy

- Discrepancy is larger when acceptance vanishes along the edges of the  $\phi_h$  Distributions

# END

## Link to more Images:

[https://userweb.jlab.org/~richcap/Interactive\\_Webpage\\_SIDIS\\_richcap/Interactive\\_Unfolding\\_Page\\_Updated.html](https://userweb.jlab.org/~richcap/Interactive_Webpage_SIDIS_richcap/Interactive_Unfolding_Page_Updated.html)