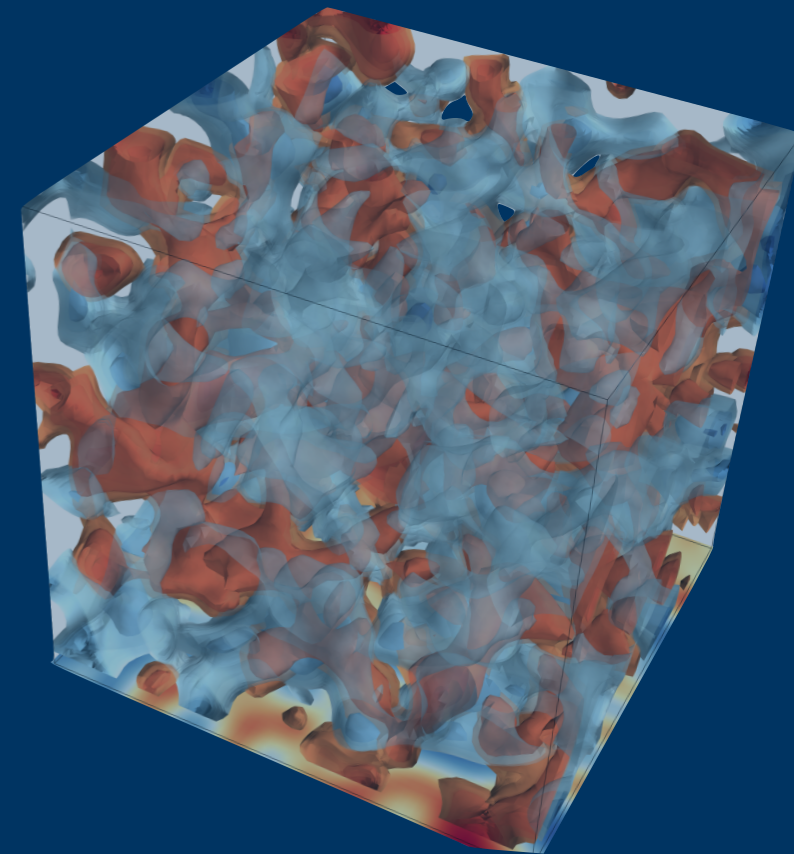
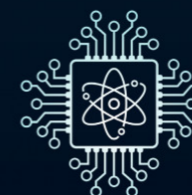


# Lattice Quantum Chromodynamics

Software Infrastructure and Computing



William Detmold, MIT

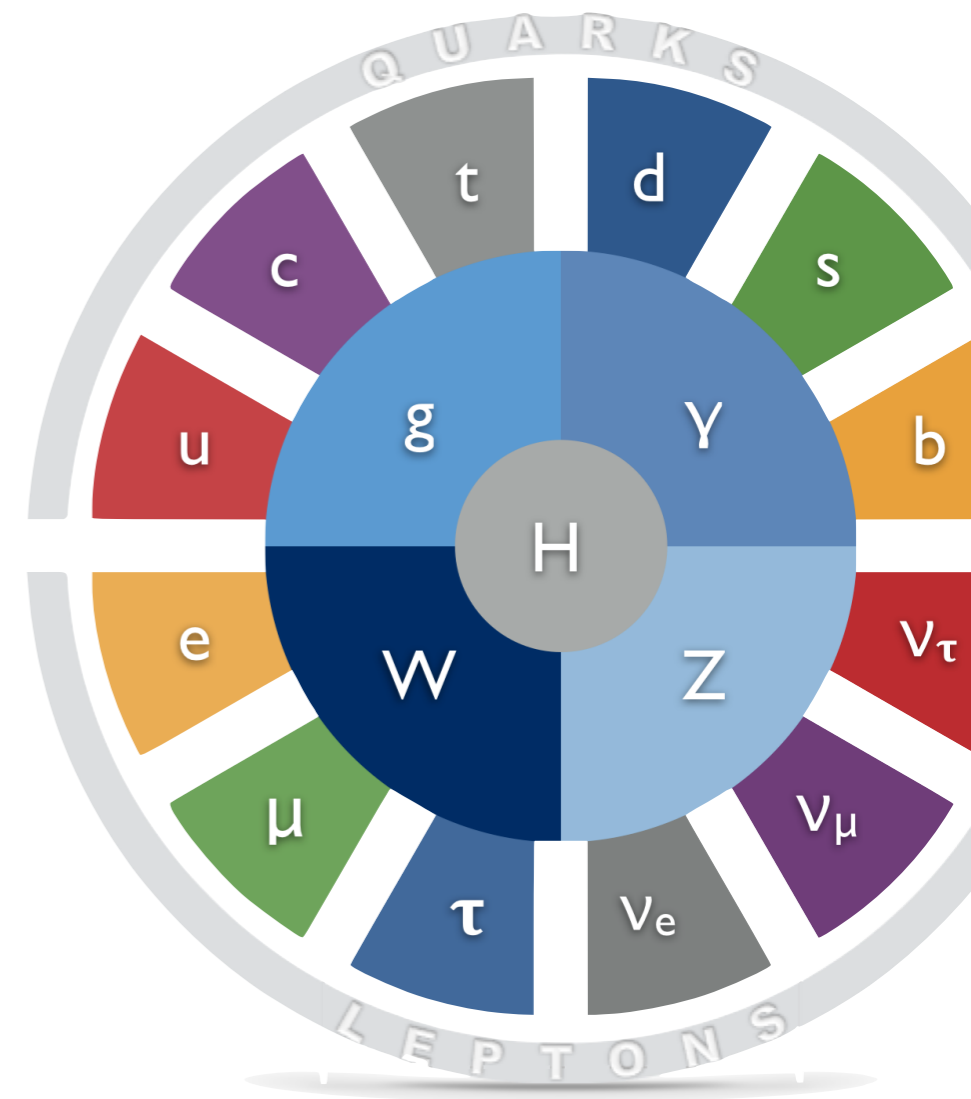


WORKSHOP ON  
**SOFTWARE INFRASTRUCTURE  
FOR ADVANCED  
NUCLEAR PHYSICS  
COMPUTING** JUNE 20-22, 2024

# The femtoscale universe

## The Standard Model

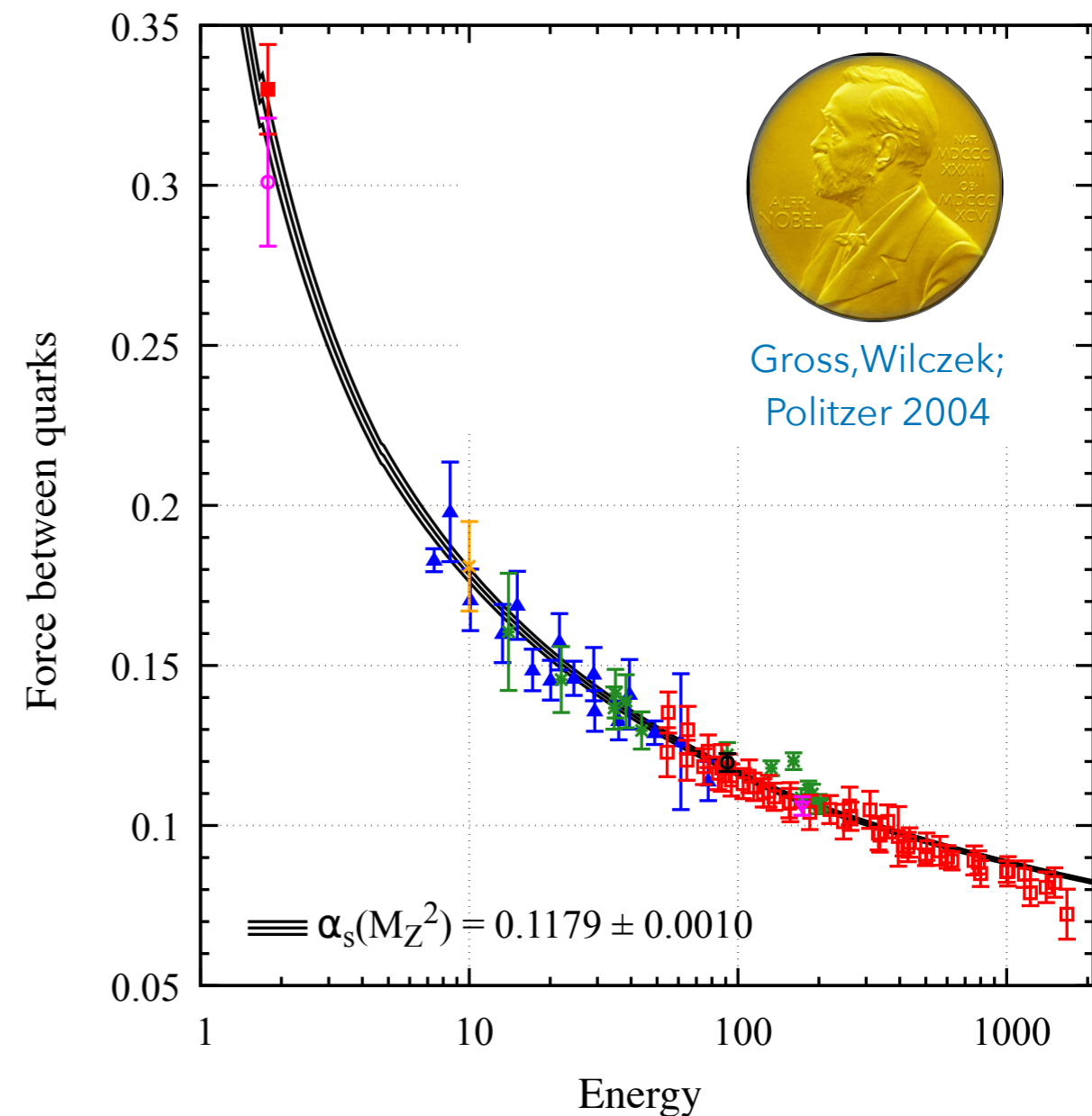
- Understand the world around us from first principles in the Standard Model (SM)
  - Quarks, leptons & bosons (17 fundamental fields)
- What is the structure of matter?
  - All the way from the proton to neutron stars and supernovae
- How does it depend on SM parameters?
- How do we constrain the SM in experiments?
- How do we search for new physics beyond the SM?
  - Dark matter, dark energy, origin of neutrino masses,...



# Quantum Chromodynamics (QCD)

## The strong interaction

- Standard Model = electromagnetism + weak + strong nuclear forces
- QCD is the strong force that binds protons together and into nuclei
- Interaction strength depends on energy
- At high energy: analytic small-coupling expansion
- At low energies/long distances: no analytic control
  - The regime of protons and nuclei
  - Numerical calculations through Lattice QCD



# Anatomy of lattice QCD

## In theory

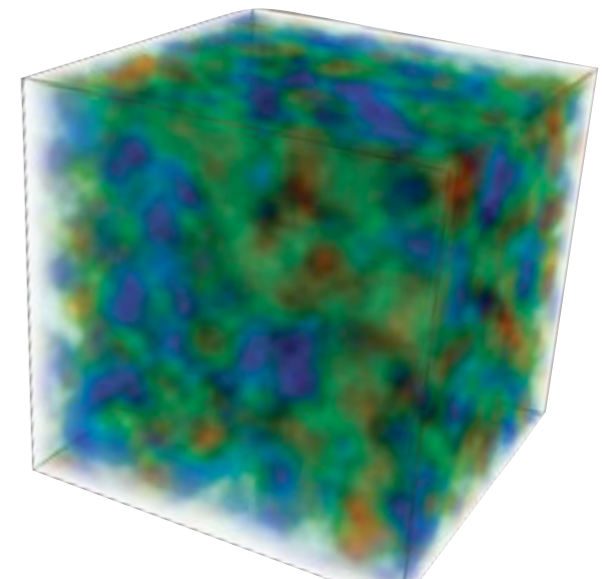
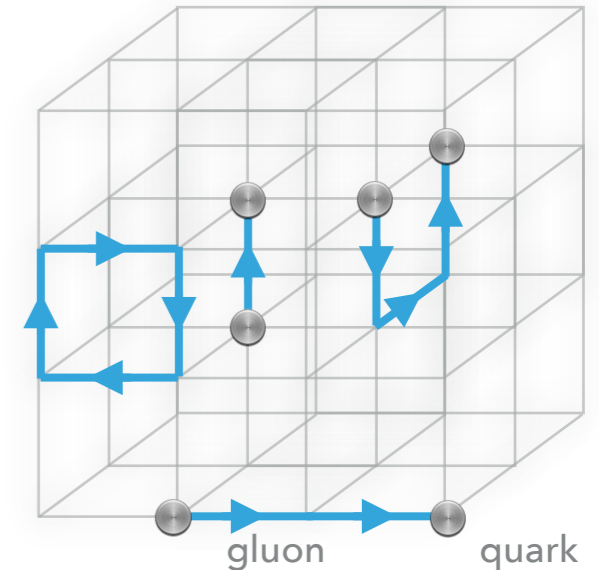
- Lattice QCD: tool to deal with quarks and gluons (also a rigorous definition of QCD)
- Formulate problem as functional integral over quark ( $q, \bar{q}$ ) and gluon ( $A$ ) d.o.f. in 3+1D spacetime

$$\langle \mathcal{O} \rangle = \int \mathcal{D}A \mathcal{D}q \mathcal{D}\bar{q} e^{-S_{\text{QCD}}[A, q, \bar{q}]} \mathcal{O}[A, q, \bar{q}]$$

- Discretise and compactify system
  - Finite but large number of d.o.f ( $\sim 10^8 - 10^{12}$ )
- Integrate via importance sampling according to probability measure

$$\langle \mathcal{O} \rangle = \int \mathcal{D}P(A) \mathcal{O}[A] \simeq \frac{1}{N_{\text{samp}}} \sum_i^{N_{\text{samp}}} \mathcal{O}[A_{(i)}]$$

- Undo the harm done in previous steps





# Anatomy of lattice QCD

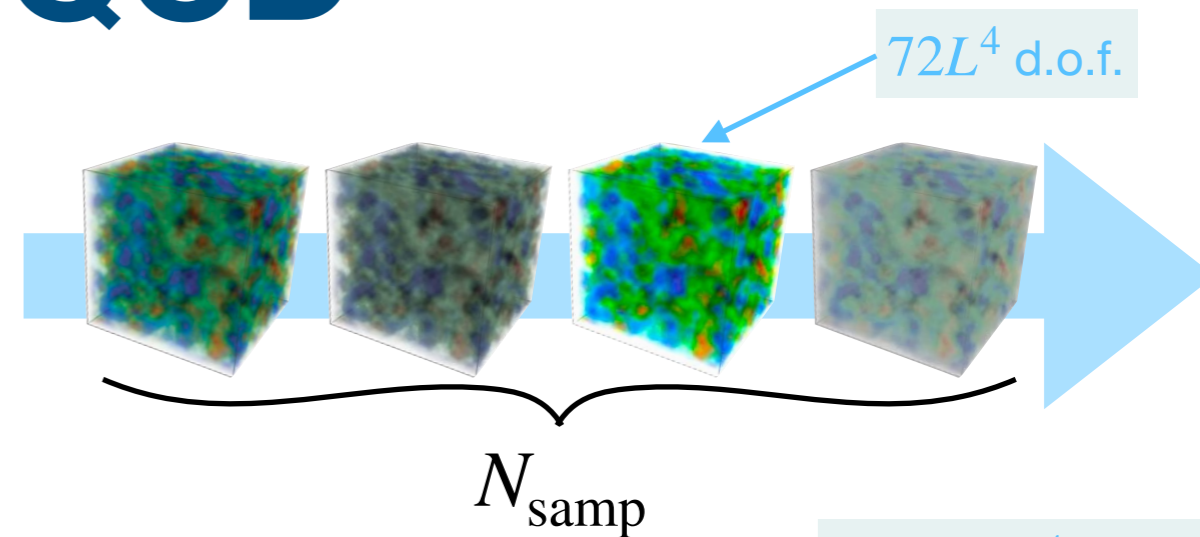
## In practice

1. Generate representative samples of gluon fields in a MC chain ( $N_{\text{samp}} \sim 1000$ )
2. On each gluon field calculate “quark propagators”  $\vec{S}$  by solving linear systems

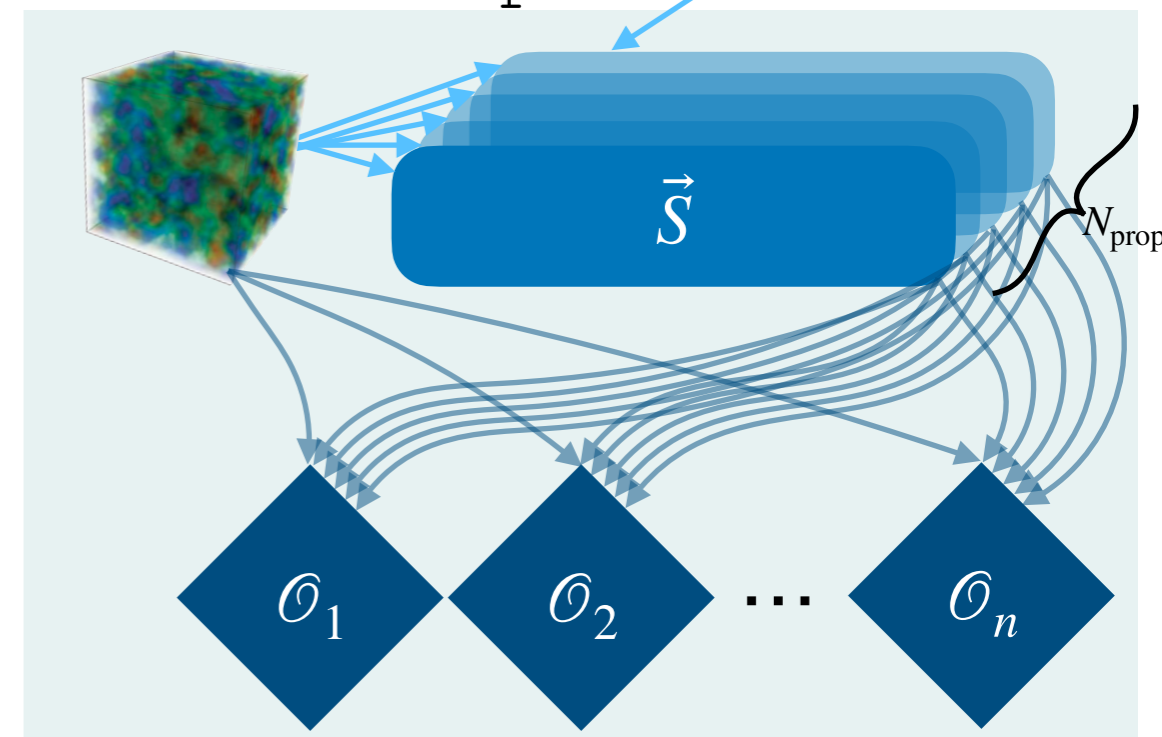
$$\mathbb{D}_{\text{Dirac}}[A_{(i)}]\vec{S} = \vec{\phi}$$

Dirac operator depends on the gluon field; typically  $N_{\text{prop}} \sim O(100s)$  RHSs used

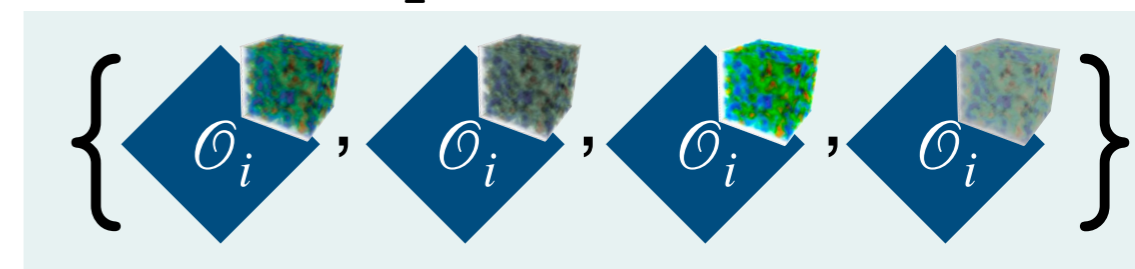
3. Construct operators  $\mathcal{O}_i$  for a particular physics goal from the gluon field and associated quark propagators
  - Tensor contractions
4. Analyse statistics of the resulting quantities to extract physics



foreach sample:  $12 \times 12L^4$  d.o.f.



foreach operator:



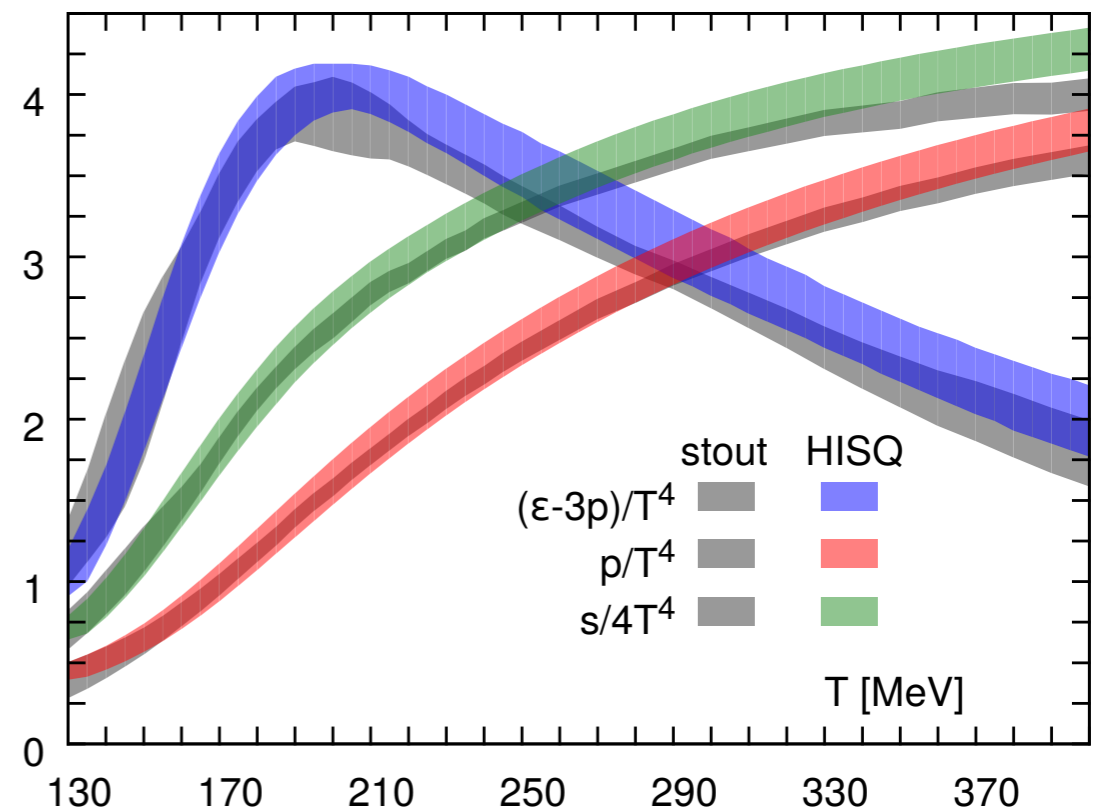
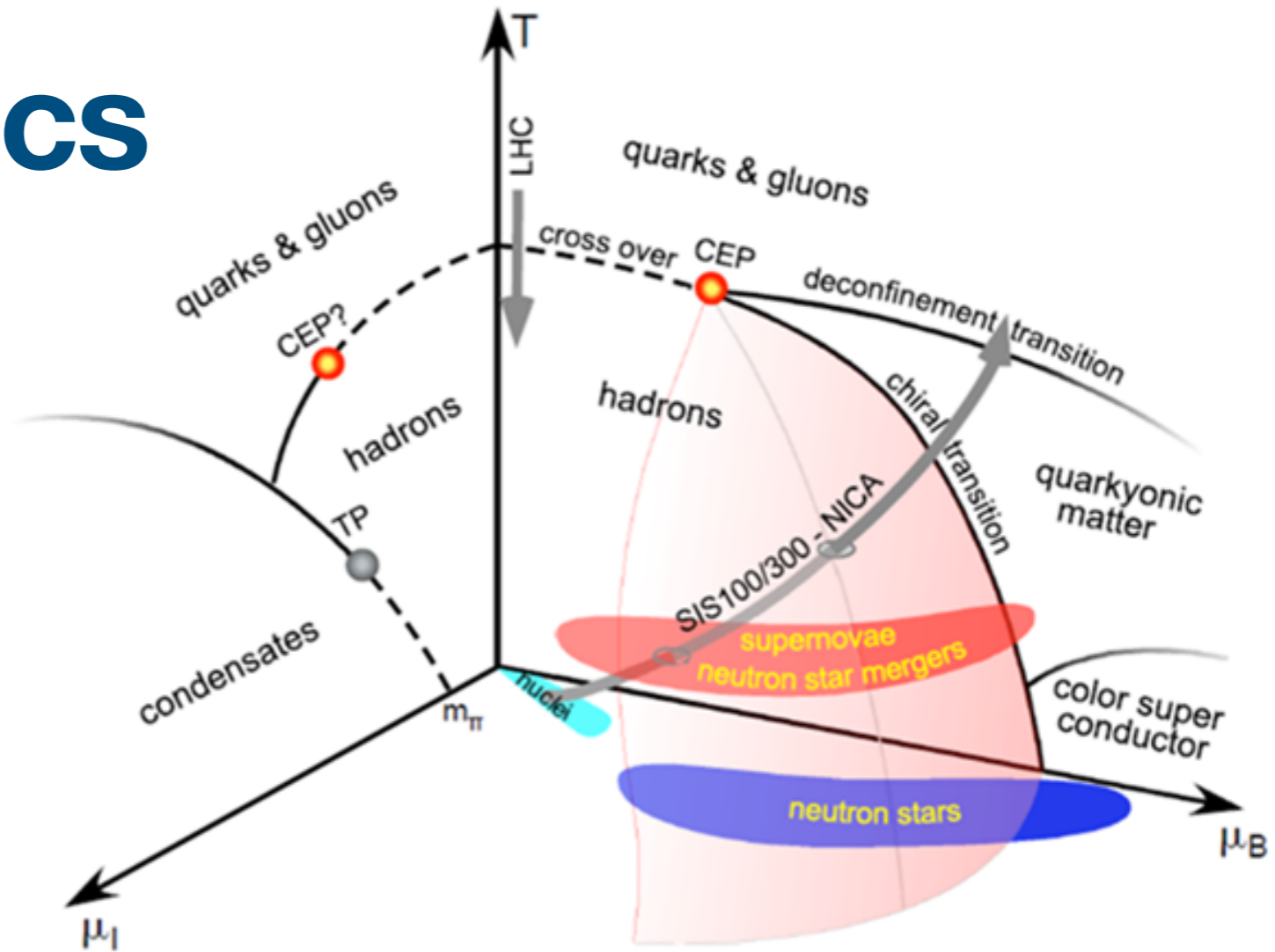
# LQCD Science

**Achievements and Goals in Nuclear Physics**

# Thermodynamics

## QCD Phase structure

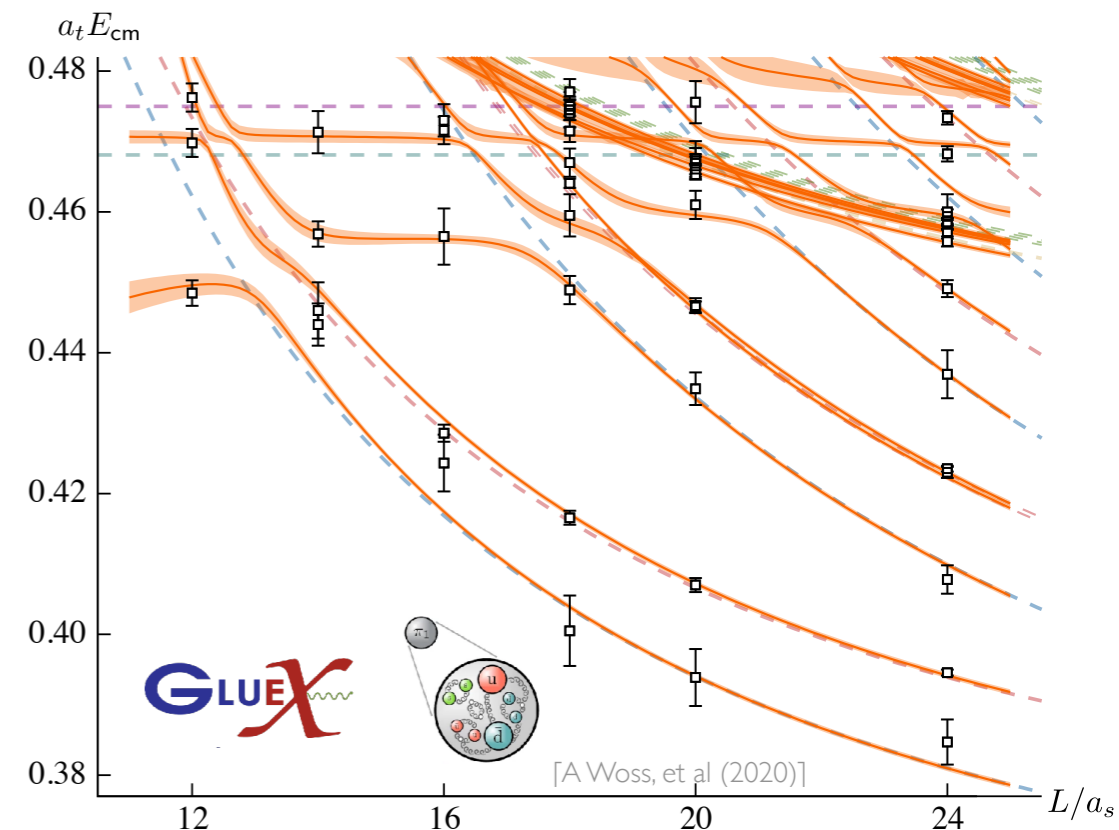
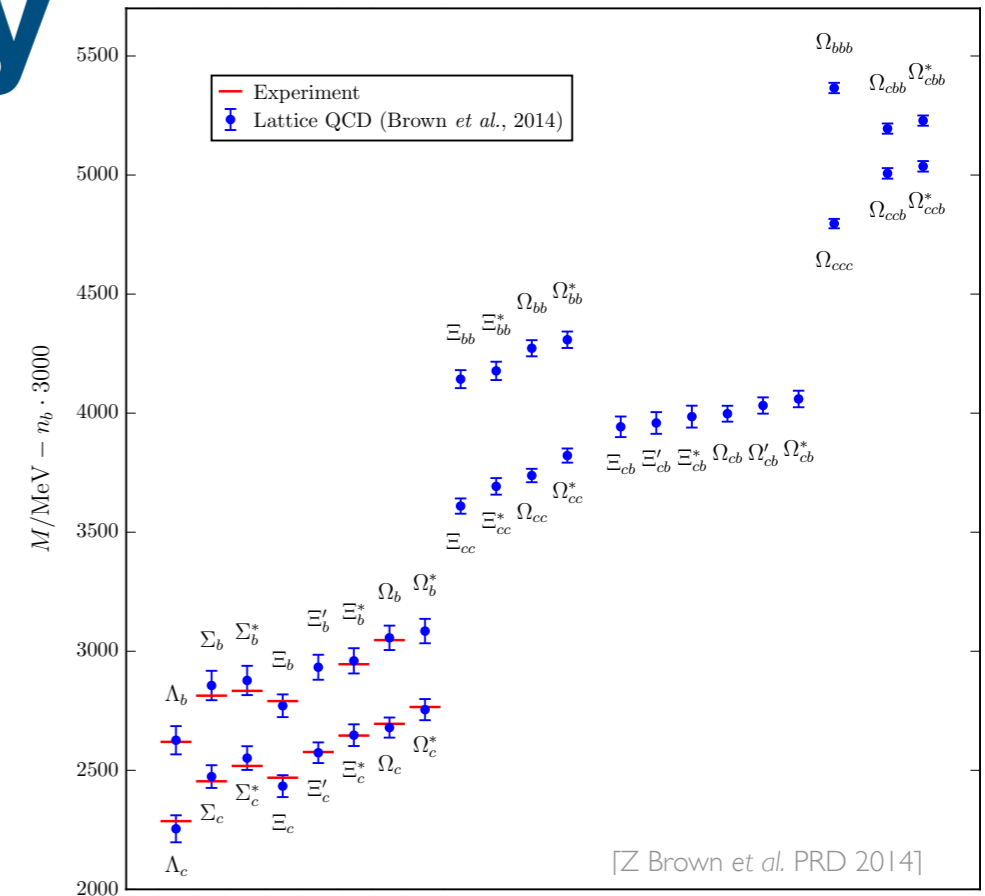
- Understand the phases of strongly interacting matter
- Deconfinement transition at  $\mu_B = \mu_I = 0, T \neq 0$ 
  - Crossover transition at  $T_c = 155$  MeV
- Nonzero isospin density
  - Superconductivity
- Baryon density
  - Hints for critical end point
  - “Sign problem” prevents direct Monte-Carlo calculations
- Many open problems: neutron star equation of state, transport in heavy-ion collisions,...



# Hadron Spectroscopy

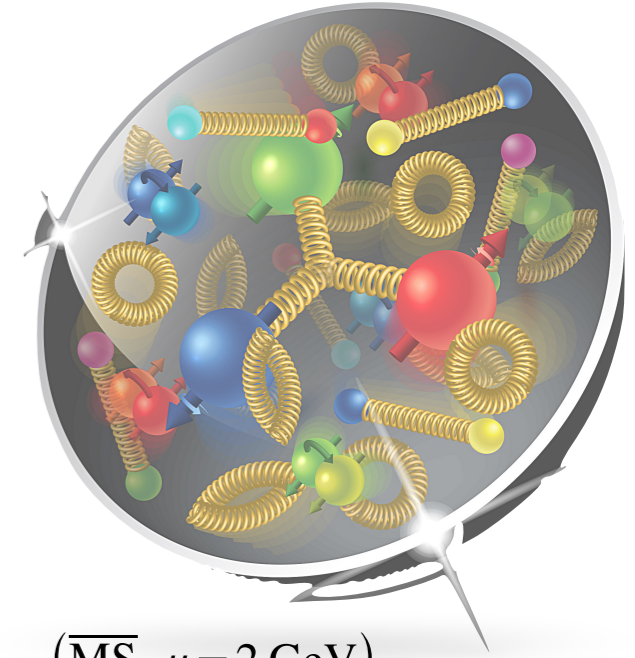
## Hadrons and resonances

- LQCD reproduces masses of stable hadrons
  - Demonstrates QCD describes nature at low energies
  - Go beyond experiment: separate QED & isospin contributions to  $M_n - M_p$
- Heavy hadrons
  - Predictions subsequently seen in experiment (eg  $\Omega_b, \Xi_{cc}$ )
- Predictions for exotic hadrons
  - Part of the motivation for the GlueX experiment
- Future:
  - More complicated decay channels
  - Branching fractions and structure of exotics



# Hadron Structure

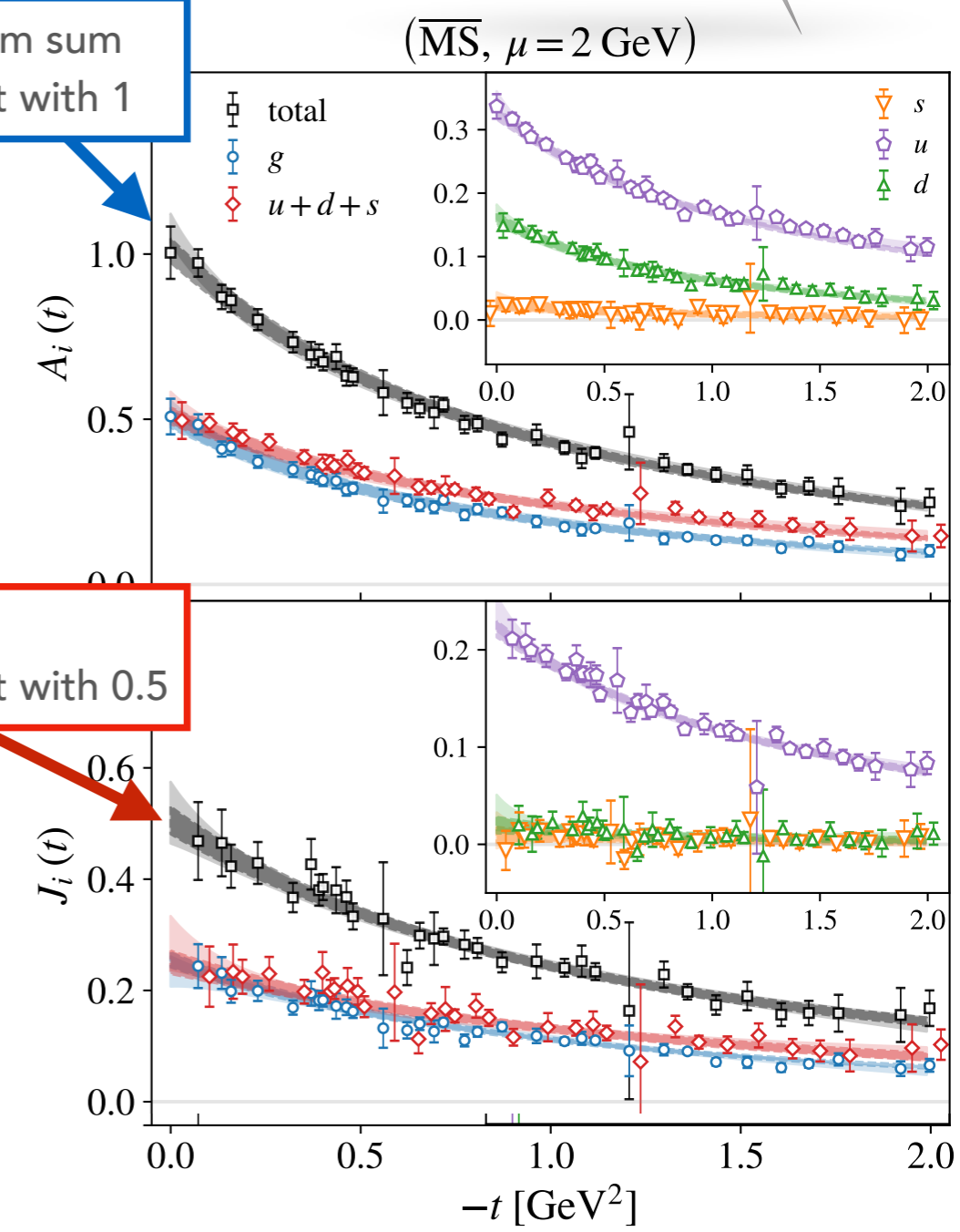
## The internal dynamics of the proton



- QCD studies of EM form factors
- Partonic structure: PDFs, GPDs, TMDs
  - Key inputs for EIC projections and predictions
- Gravitational form factors & the energy-momentum tensor
  - Origin of mass, spin and mechanical properties
  - Complementary to JLab DVCS experiments
- Future:
  - Increased precision as needed to match experiment for simple quantities
  - Predictions of harder-to-measure quantities

Momentum sum consistent with 1

Total spin consistent with 0.5



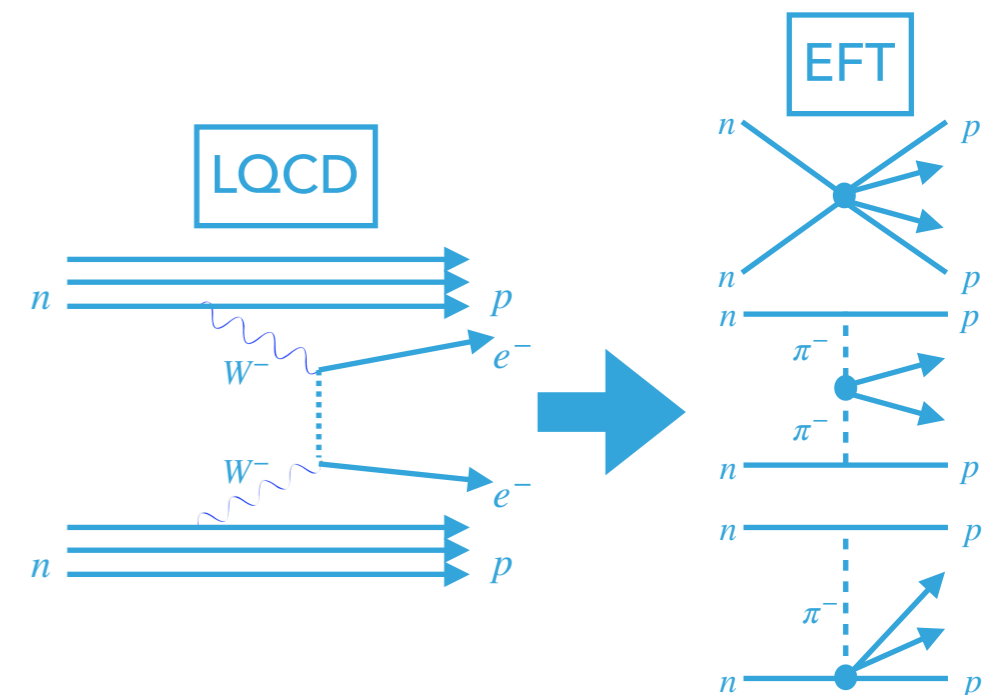
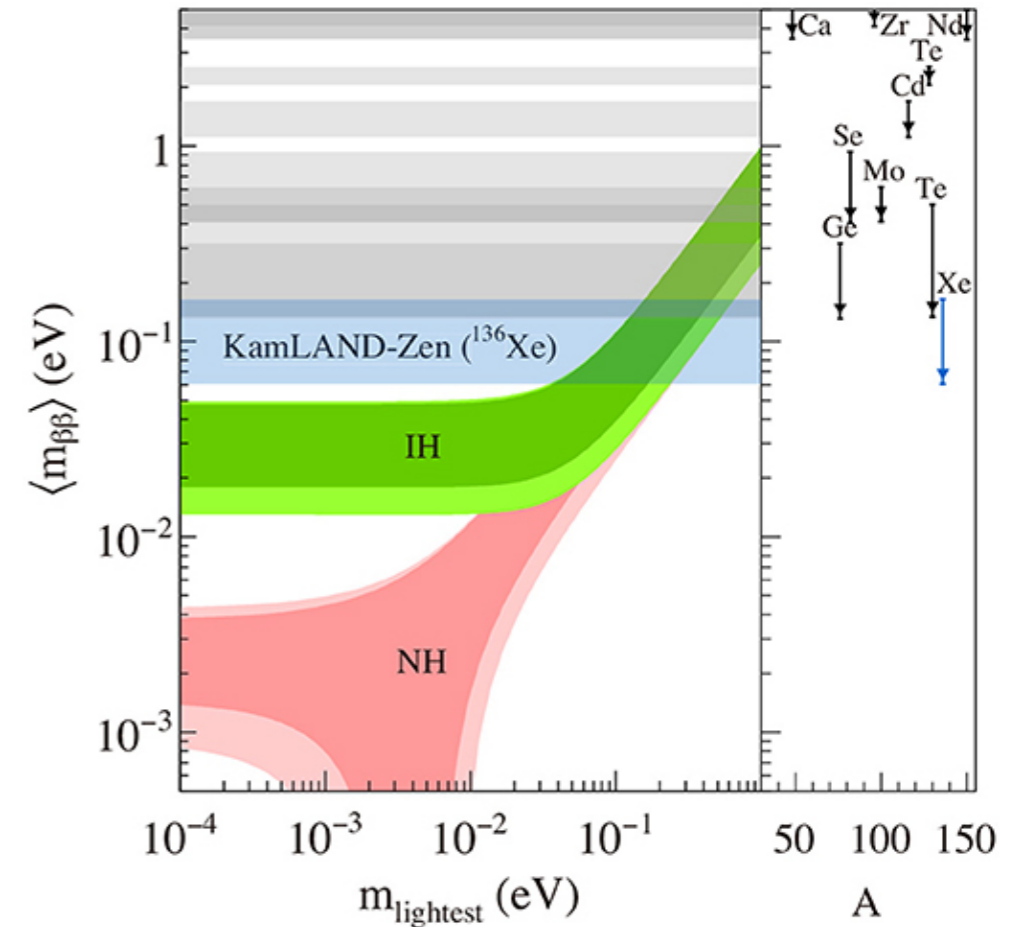
( $\overline{\text{MS}}$ ,  $\mu = 2 \text{ GeV}$ )



# Fundamental Symmetries

## Neutrinoless $\beta\beta$ decay

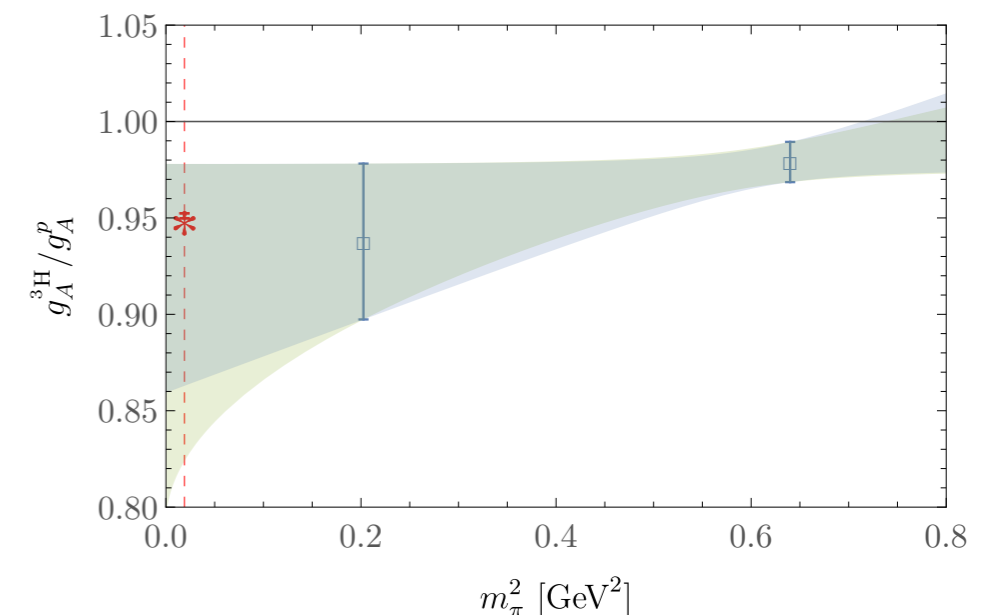
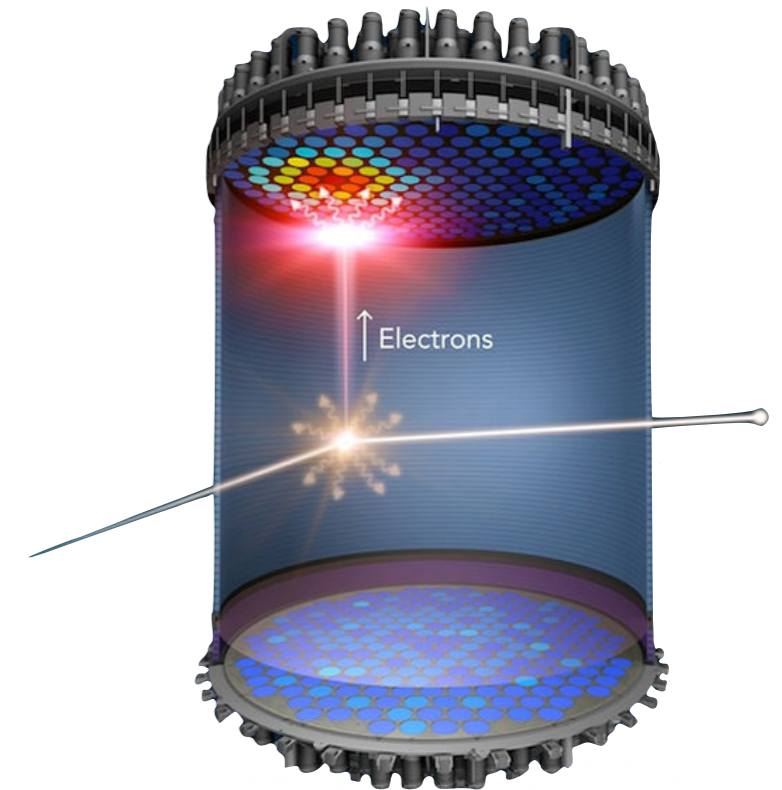
- ▶ Search for lepton number (L) violation/nature of neutrino [high priority in 2023 NSAC Long Range Plan]
- ▶ Uncontrolled nuclear model uncertainties cloud interpretation of experimental searches
- ▶ Ground nuclear physics in QCD: LQCD +EFT  $\rightarrow$  Many-body
- ▶ Calculations of subprocess  $\pi^- \rightarrow \pi^+ e^- e^-$ 
  - ▶ Light Majorana neutrino
  - ▶ Short distance L-violation from BSM
- ▶ First QCD calculations of  $nn \rightarrow ppe^- e^-$  for light Majorana neutrino
- ▶ Future: controlled inputs for future ton-scale  $0\nu\beta\beta$  experiments



# Beyond Standard Model physics

## QCD @ the intensity frontier

- Many Intensity Frontier (HEP) experiments use nuclear targets
  - Neutrino physics: DUNE, HyperK,...
  - Dark matter: LZ, XENON-nT, PANDAX-4T,...
  - Lepton flavour violation:  $\mu 2e$
- Must control QCD for rigorous BSM searches
- Current highlights:
  - Weak current nucleon form factors for DUNE
  - First calculations of nuclear effects
- Future: matrix elements for design and analysis of different detectors



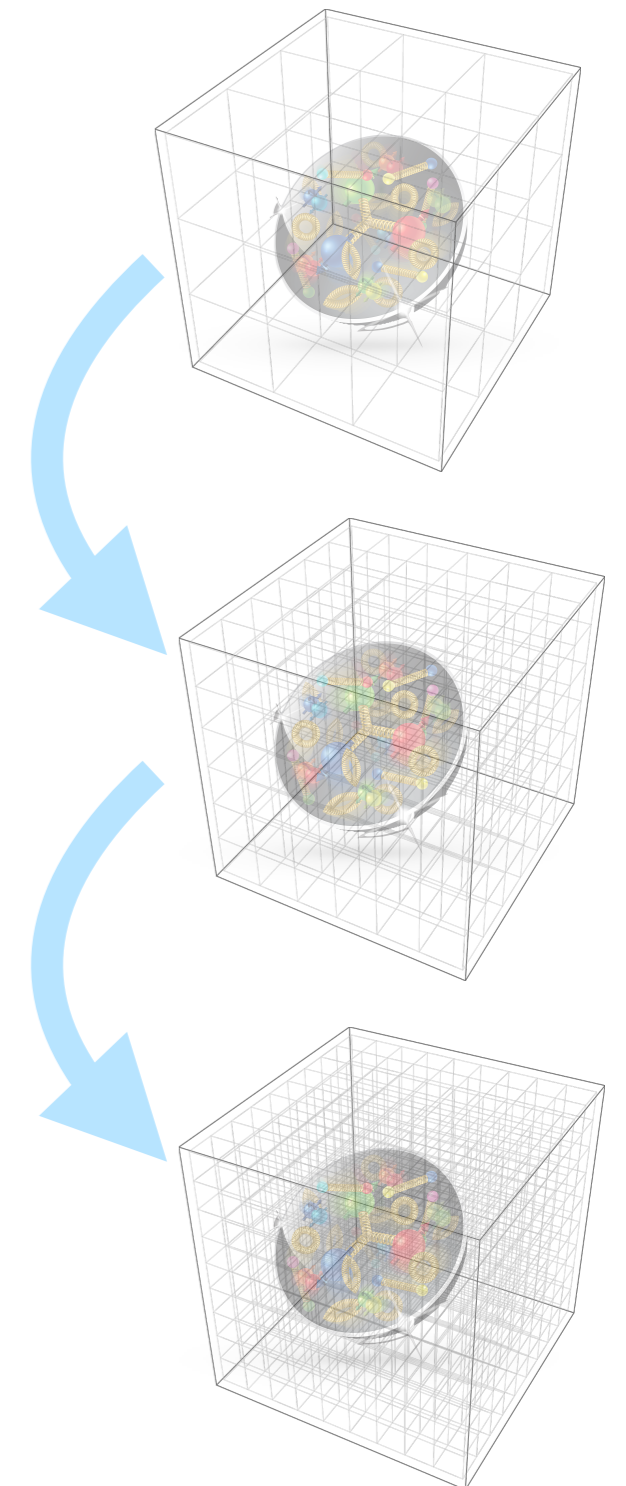
# LQCD Science

## **Challenges and Developments**

# Precision physics

## Continuum limit, QED, and isospin-breaking

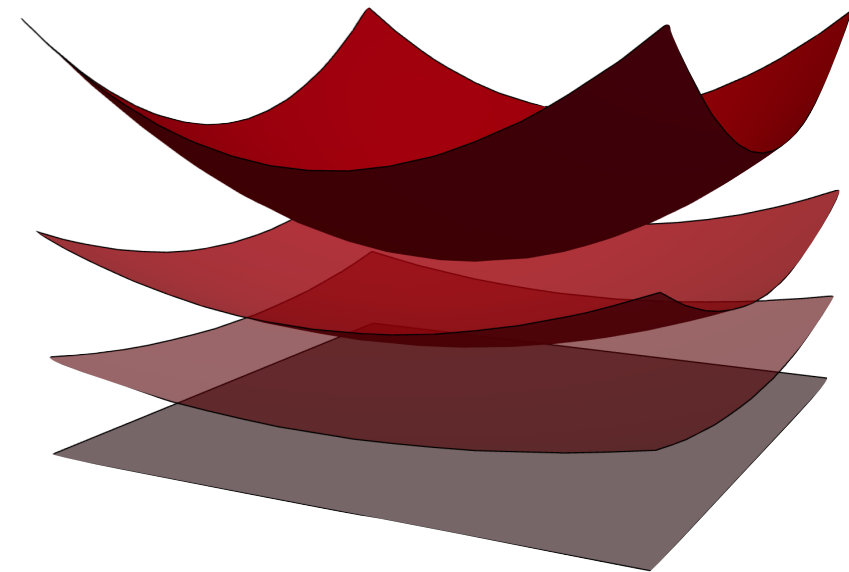
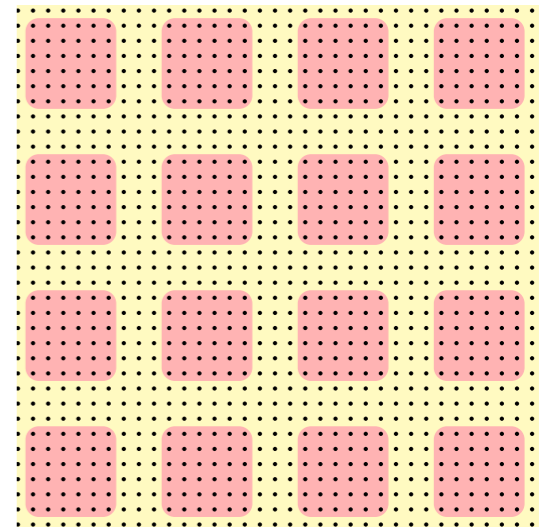
- Turning LQCD into physics requires continuum limit
  - Sampling becomes harder as update algorithms are quasi-local
  - New machine-learned normalising flow gauge generation algorithms seem promising
- $<1\%$  precision requires QED and effects of isospin breaking of quark masses ( $m_u \neq m_d$ )
  - Eg axial charge  $g_A$  precision limited by these effects
- New algorithmic requirements
  - Sampling with QED: complications of infinite volume limit
  - Sampling for  $m_u \neq m_d$ : Single fermion flavours



# Statistical limitations

## New sampling procedures

- LQCD is a Monte Carlo sampling method
  - High momentum structure of hadrons from LaMET/ short distance factorisation requires very boosted states: statistical noise grows
  - Multi-hadron systems (eg nuclei): exponential growth of noise
- Better statistical sampling approaches
  - Hierarchical integration
  - Machine learned changes of integration variables

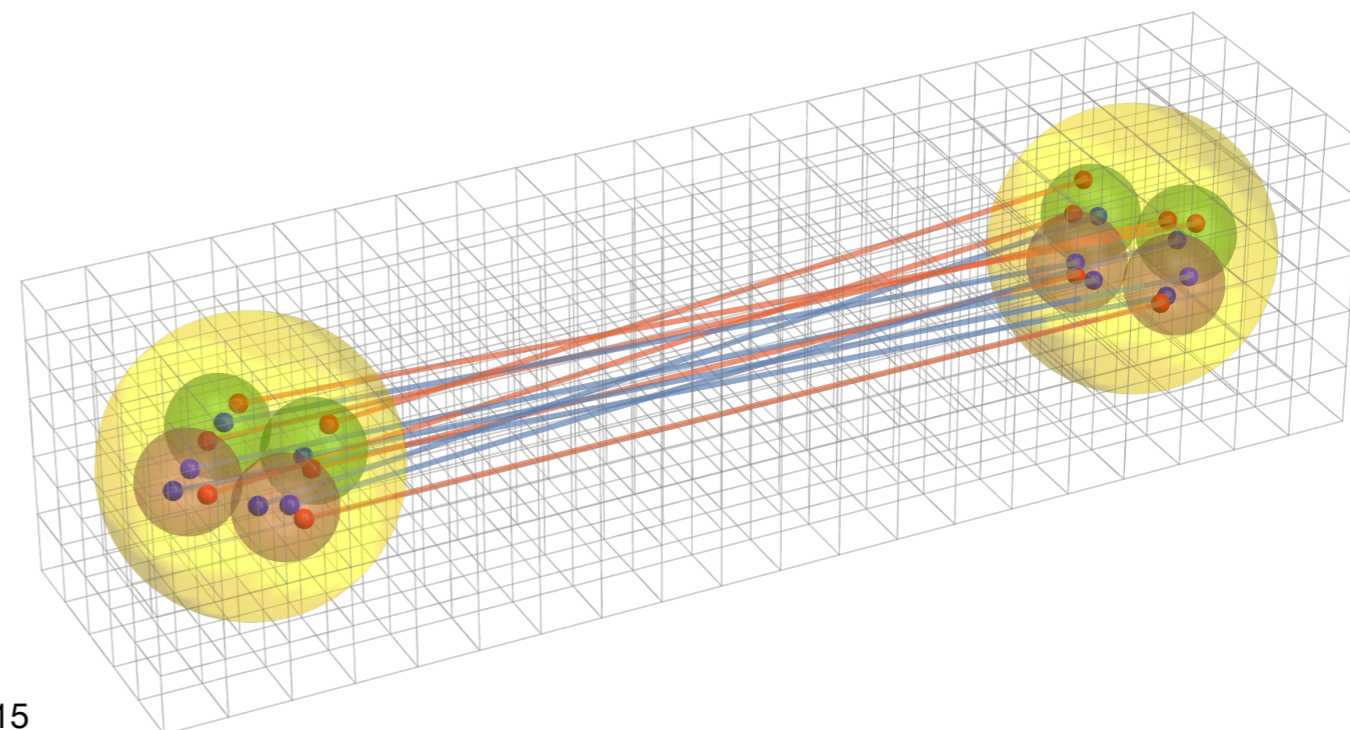
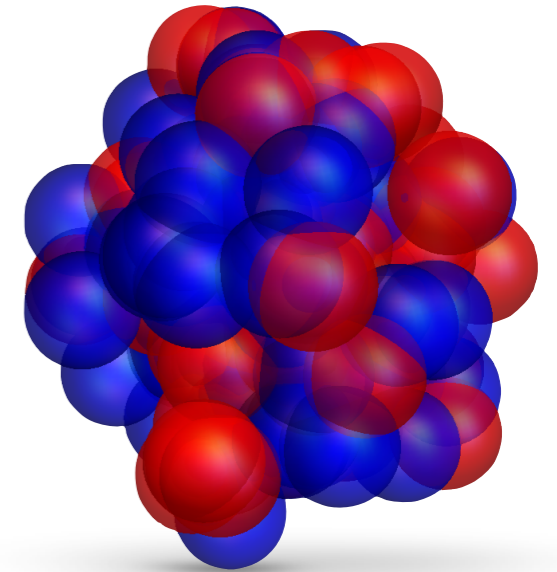




# Complexity

## Nuclear Contractions

- Physics of nuclei requires calculation of correlation functions with factorial number of Wick contractions:  $N_u!N_d!N_s!$ 
  - Wick contractions = tensor contractions
  - Costs grow dramatically with system size
  - Graph-theoretic methods minimise redundant work
- Efficient calculation requires many tricks
  - Common subexpression elimination
  - Tiling of partial sums
  - Code generators
- Current state-of-the-art:  $A = 5$  nuclei, but  $A \sim 250$  in nature ( a long way to go!)



# LQCD Ecosystem

## USQCD collaboration



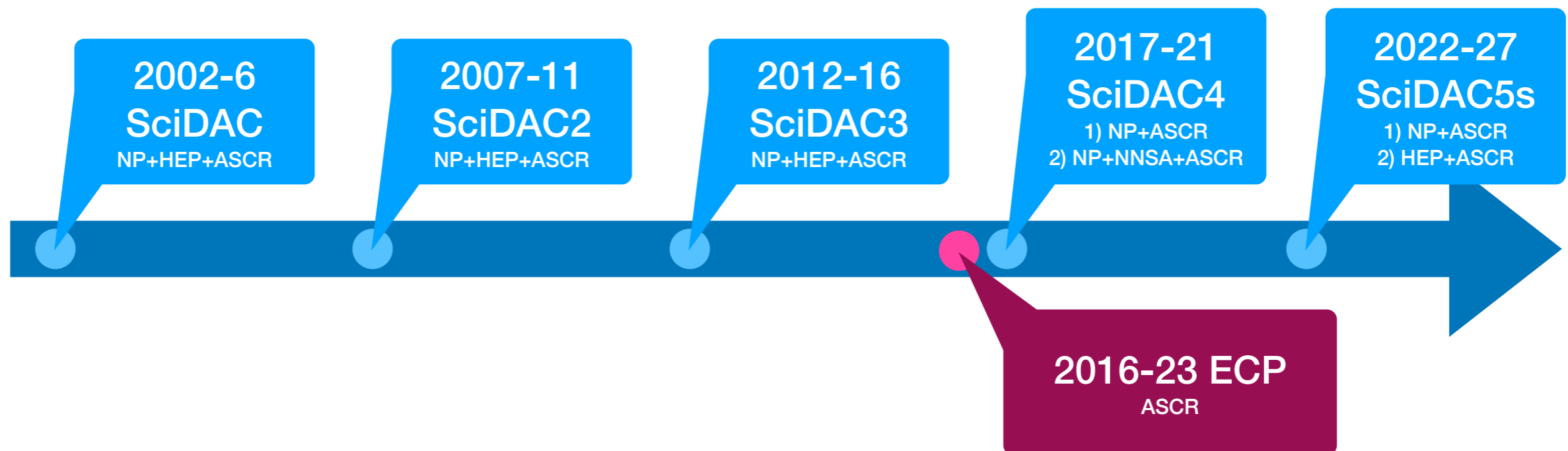
- Federation of scientific collaborations
  - 90+% of LQCD (NP+HEP) researchers in the US
  - 180+ members from grad students to permanent staff
- Collaborate on software development
  - Train students and postdocs in LQCD
- Seek funding for, deploy, and allocate mid-scale computing resources at JLab, BNL and FNAL
  - Allocations support development of new projects and research directions
  - Build community and support junior scientists



# LQCD Ecosystem

## Software Development under SciDAC and ECP

- Strong DoE support for software development through SciDAC and ECP

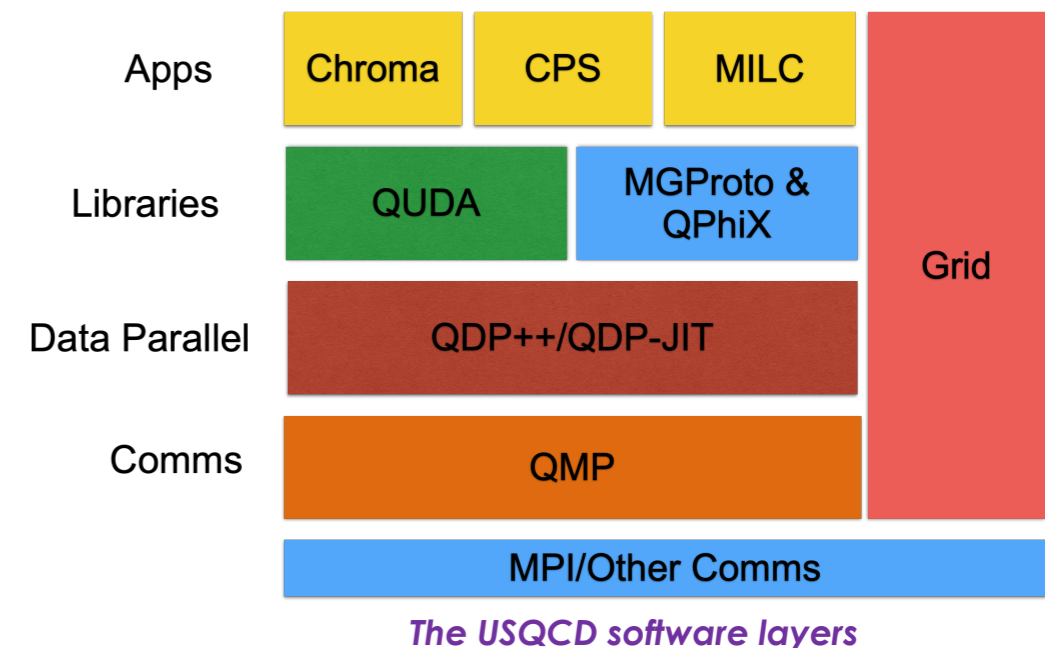


- Physics + Applied Math + Computer Science (SciDAC5 includes FastMath & RAPIDS SciDAC Institute collaborators)
- \$50M+ investment in LQCD software and algorithms

# LQCD Ecosystem

## Codes and Libraries

- Layered software infrastructure
  - QMP: QCD message passing (abstracts different MPI frameworks)
  - QDP/C, QDP++, QDP-JIT: QCD data parallel
  - Linear system solver libraries: QUDA, MDWF, QPhiX,...
  - General application frameworks
    - Chroma, QLua, CPS, Grid, Grid Python Toolkit, MILC, Redstar, ...
    - Most physicists work at this level
- Codes continue to evolve to address new physics problems

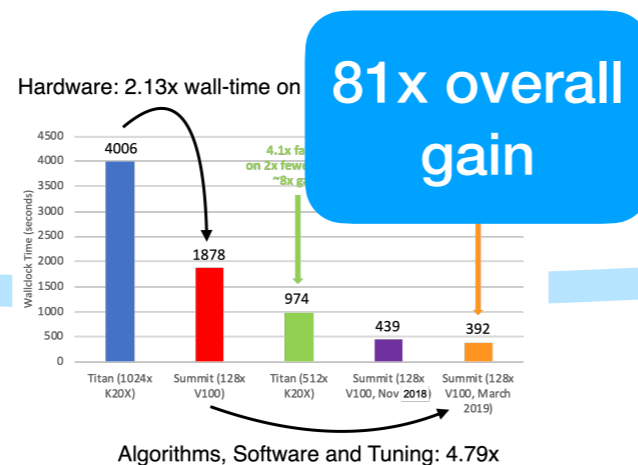




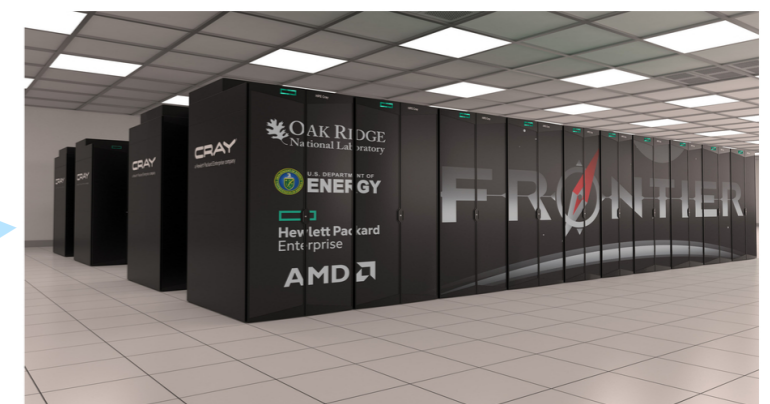
# LQCD Ecosystem

## Codes and Libraries

- Example: porting Chroma from Titan to Summit to Frontier
  - Major changes to low level layers: QDP-JIT, QUDA
  - Smaller tweaks to application level code: Chroma



**113x now, in progress**

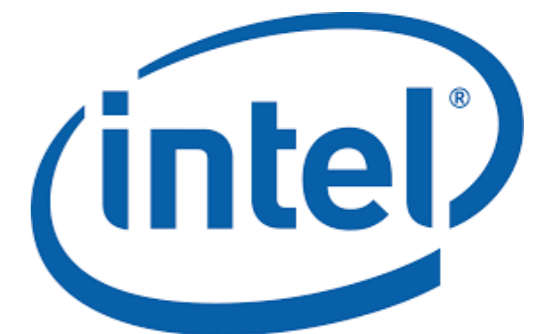




# LQCD Ecosystem

## Codes and Libraries

- Connections to industry
- QUDA GPU library development based at nVIDIA and critical for LQCD
  - Ported to AMD and Intel GPUs with significant vendor assistance
- Code generators for new hardware (LLVM, Halide etc) build upon industry efforts
- Flow of talent from academia to industry helps maintain this
  - SciDAC supports development of the necessary skills

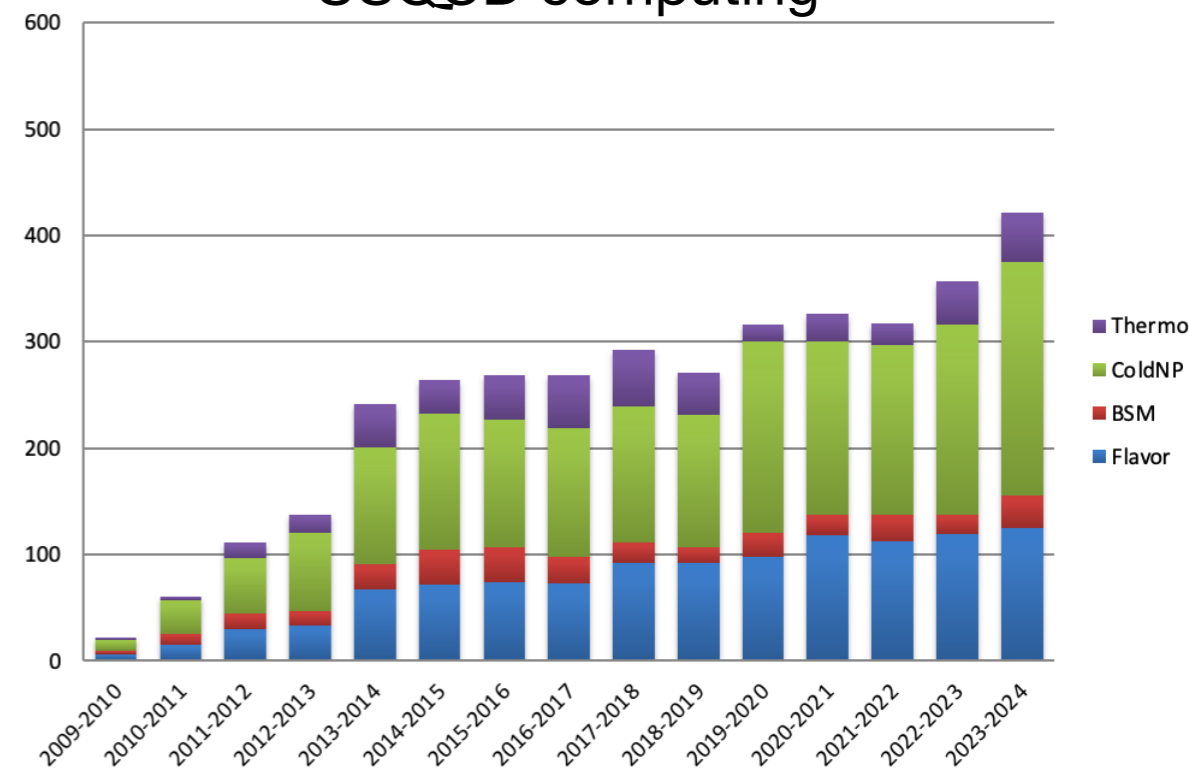


# LQCD computing

## Sources of computing

- INCITE 2020-4: 21 awards: 14.9M node hours
- ALCC 2019-23: 26 awards, 14.1M node hours
- NERSC (2023: 21 PIs, 1.4M/1.0M CPU/GPU node hours)
- NSF: O(5) Frontera LRAC awards per cycle
- LQCD(HEP) & NPLCC(NP) hardware projects
  - 1/10th of INCITE in 2024
  - 25-30 projects per year

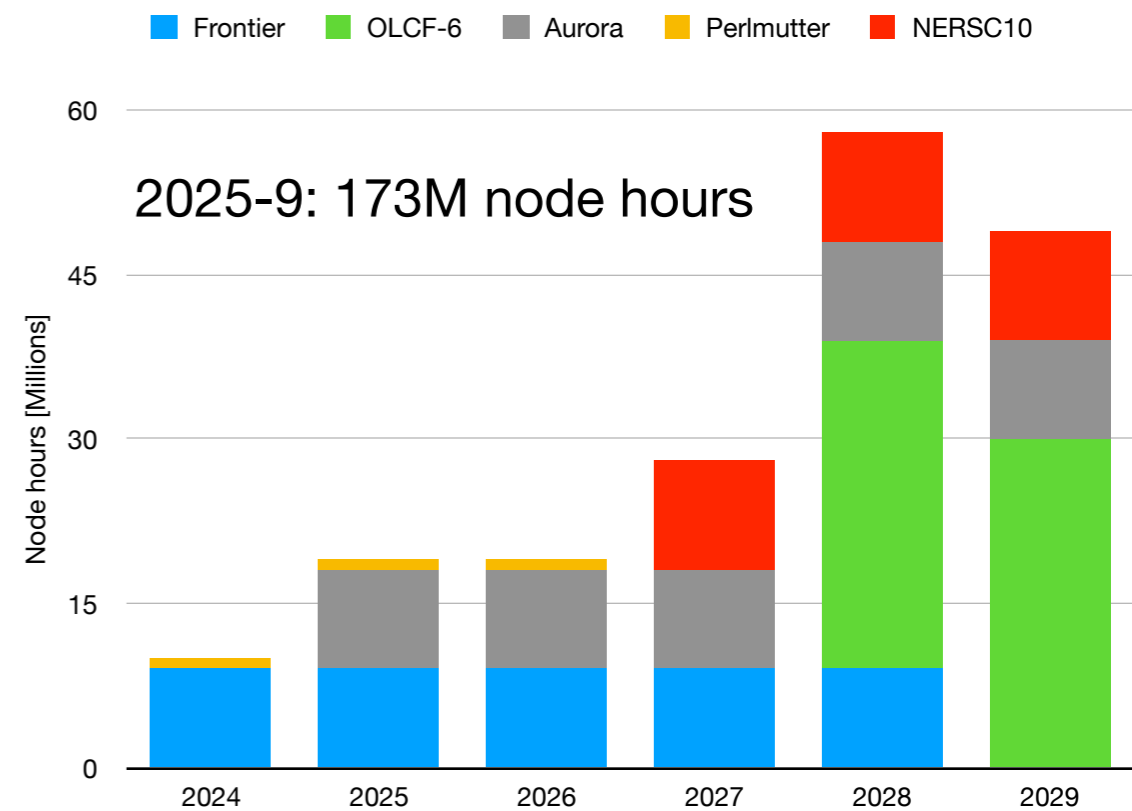
USQCD computing



# LQCD computing

## Computing 2025-30

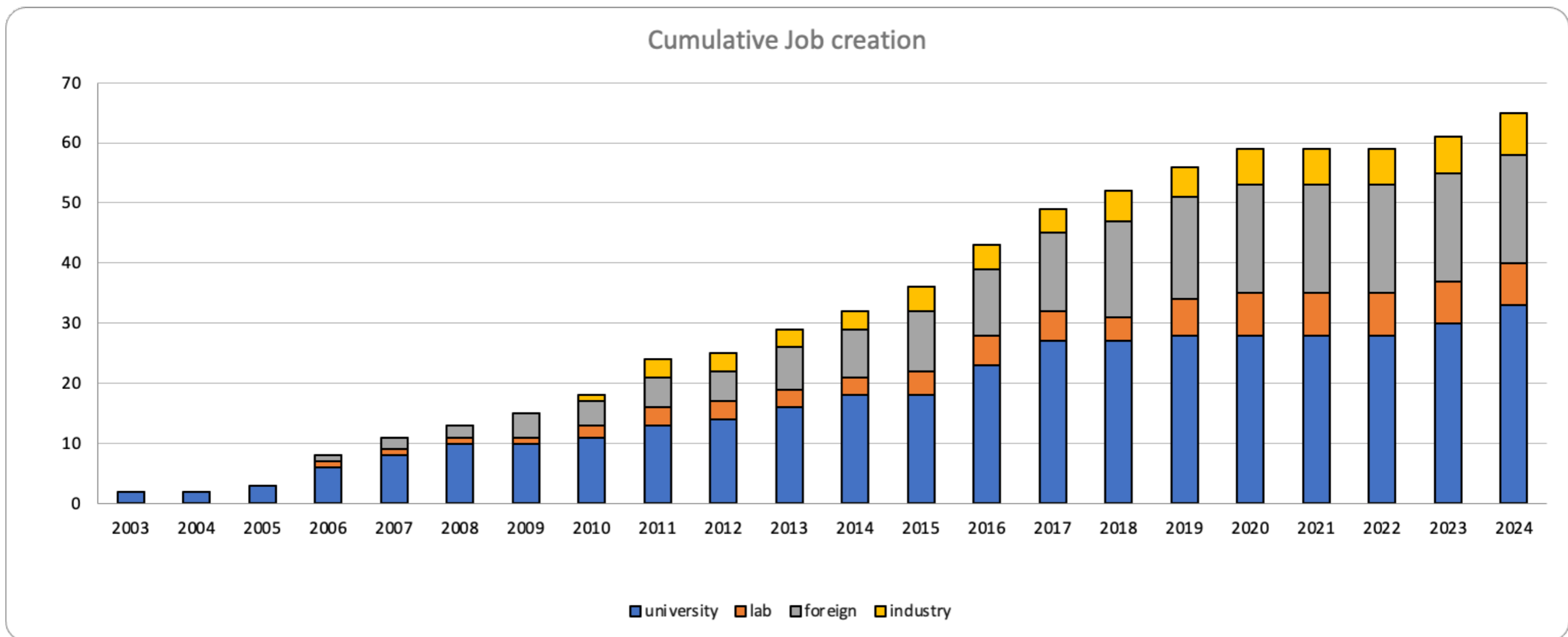
- Projections for INCITE/ALCC/NERSC computing for LQCD
  - 173M Frontier-equivalent node hours over 2025-9
- USQCD maintains detailed timelines for all major projects
  - Project goals align with anticipated growth of computing
  - Assume support for code development on new systems



# LQCD workforce

## Workforce development

- University/Lab/NPC industry LQCD hiring



# LQCD workforce

## Workforce development



### Early career awards



U.S. National  
Science  
Foundation

- Alexandru (GWU)
- Shanahan (MIT)
- Lin (MSU)
- Monahan (W&M)



U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

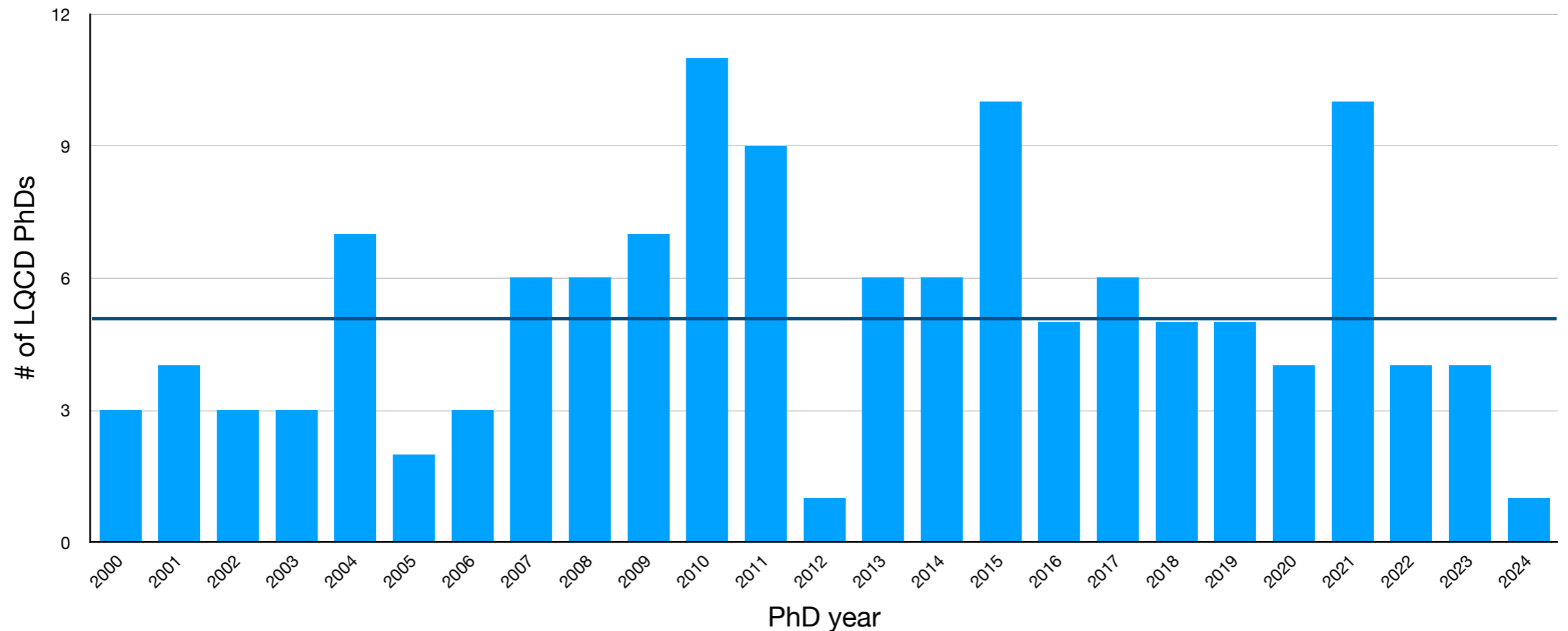
- Blum (UConn)
- Orginos (W&M)
- Dudek (W&M)
- Detmold (MIT, 2x)
- Walker-Loud (LBNL)
- Lehner (BNL)
- Davoudi (UMd)
- Jin (UConn)
- Constantinou (Temple)
- Briceño (Berkeley)
- Monahan (W&M)



# LQCD workforce

## Workforce development

- Training (average of 5.3) PhDs per year
- 35 current students



# LQCD outlook

## Some thoughts

- DOE SciDAC has been a successful pathway to support LQCD over the last 2+ decades: brings together a community and enables frontier scientific progress
  - Very much support its continuation
  - Broad scope for further innovation and abundant scientific goals
- ECP focus on code performance metrics and industry connections also very helpful
- Current framework (NP+ASCR) might not be necessary for smaller software projects, maybe just NP in some cases
- Storage of (and access to) community resources such as gauge fields is vital but lacking infrastructure
- Machine learning
  - Off the shelf ML tools will rarely solve the problems of the NP domain - interaction with data scientists needs to be two-way and we need to be prepared to develop problem-specific ML
  - Need for new allocation mechanisms to support ML applications where outcomes are not as predictable as with traditional modelling/simulation workloads
- Evaporating talent: flat budgets for many years and recent NT budget cuts do not provide an attractive recruiting environment
  - Students and postdocs leave the field for better-paying industry positions (8 LQCD researchers now @ nVIDIA)
  - Advocate for support for computational scientists at universities: very few mechanisms for scientific computing specialists at universities and technically minded postdocs who focus on software often leave the field