

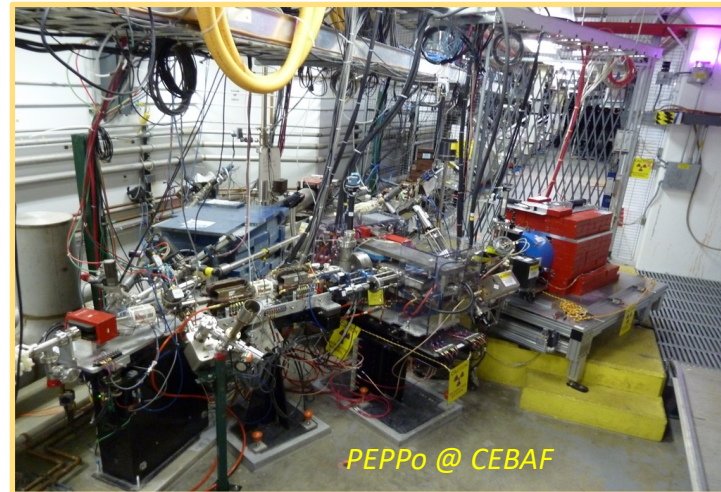
# *Positron Production, Polarization, and Polarimetry*

Eric Voutier

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**ijc** Lab  
Irène Joliot-Curie  
Laboratoire de Physique  
des 2 Infinis



- (i) Why ?
- (ii) How ?
- (iii) PEPPo
- (iv) Polarimetry
- (v) Summary

Why ?

## Positron Physics Opportunities

U = Unpolarized  
P = Polarized

*Interference Physics*

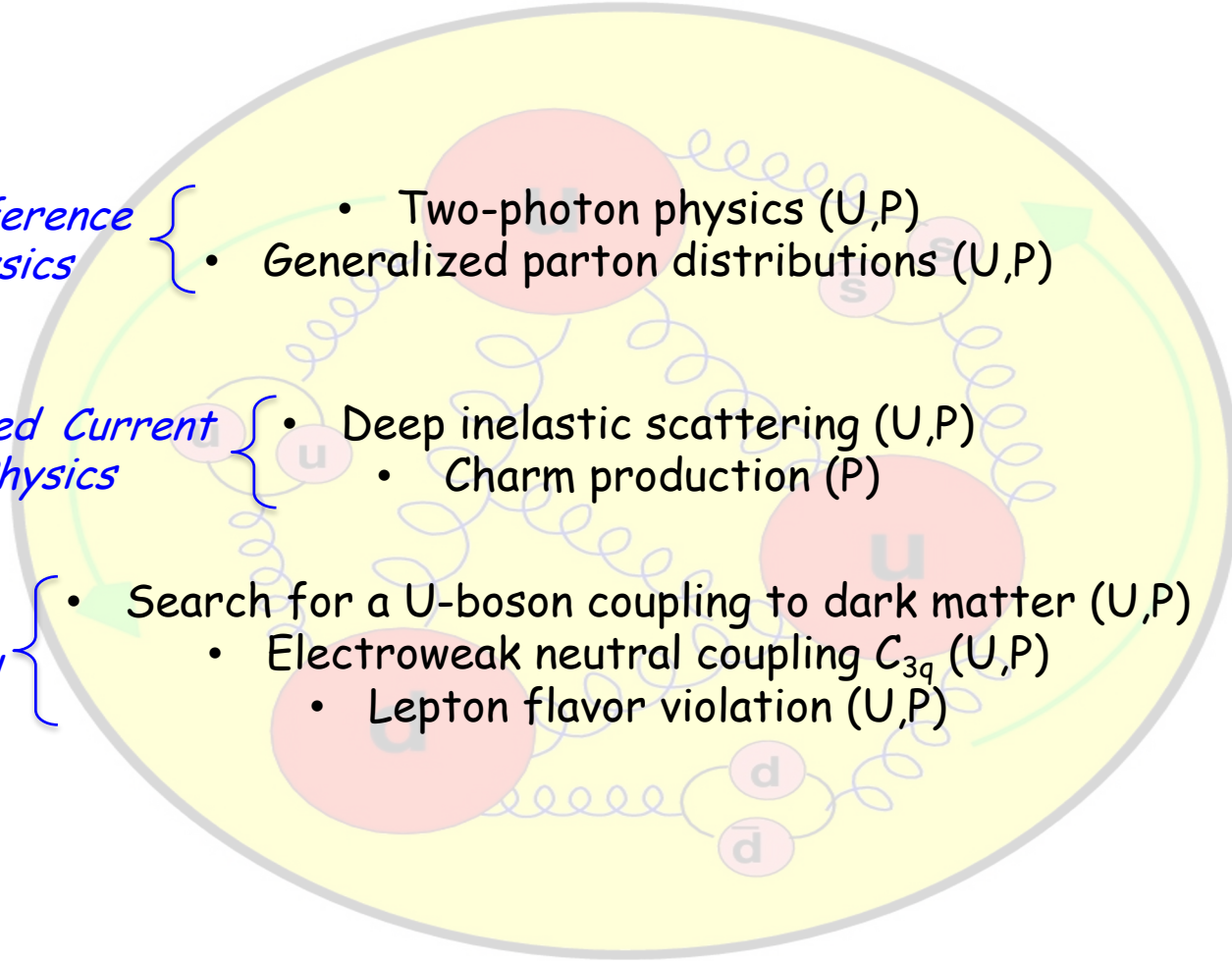
- Two-photon physics (U,P)
- Generalized parton distributions (U,P)

*Charged Current Physics*

- Deep inelastic scattering (U,P)
- Charm production (P)

*Test of the Standard Model*

- Search for a U-boson coupling to dark matter (U,P)
- Electroweak neutral coupling  $C_{3q}$  (U,P)
- Lepton flavor violation (U,P)



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- Positron annihilation spectroscopy (U,P)
- Spintronics (P)
- Positronium spectroscopy (U,P)
- Antimatter spectroscopy
- Antimatter gravity
- Energy production
- ...

Why ?

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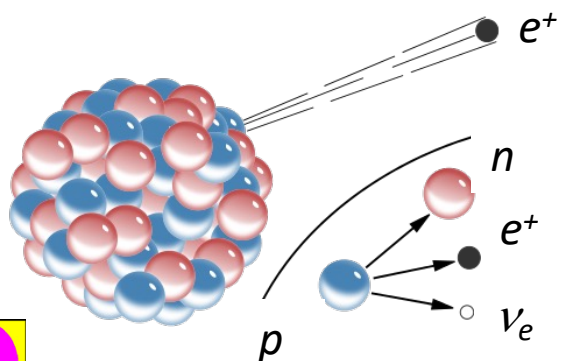
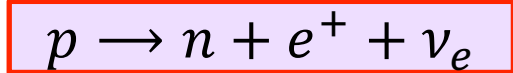
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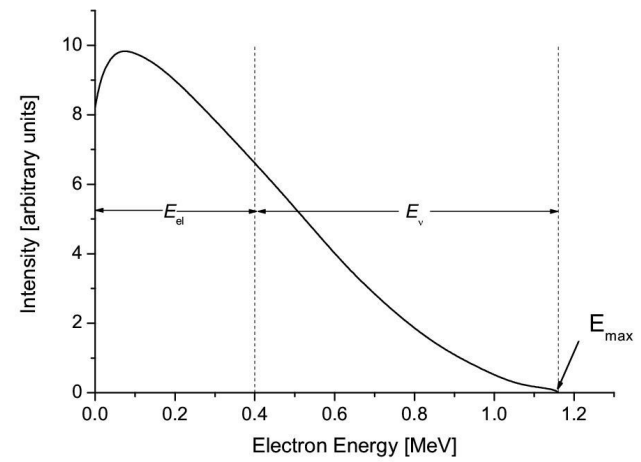
*e<sup>+</sup>e<sup>-</sup> Colliders Physics*

How ?

$\beta^+$  Decay

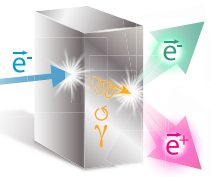


- **Positron emission** from a **radioactive source** is an electroweak process, non-conserving parity, and creating **right-handed positrons**.
- The magnitude of the **positron polarization increases with the positron energy**, however at the expense of the flux intensity.

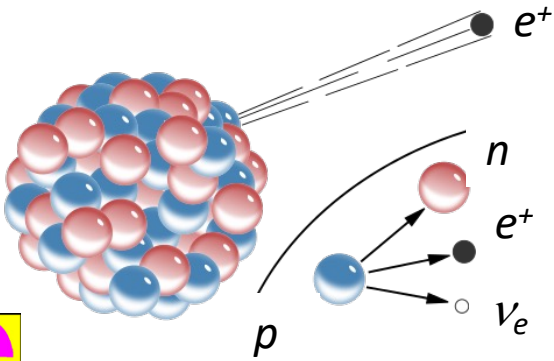
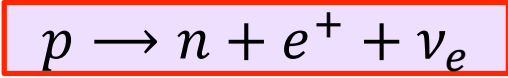


- The life-time of the source is limited (**months/years**)
- The flux intensity is limited (**10<sup>6</sup>-10<sup>8</sup> e<sup>+</sup>/s**)

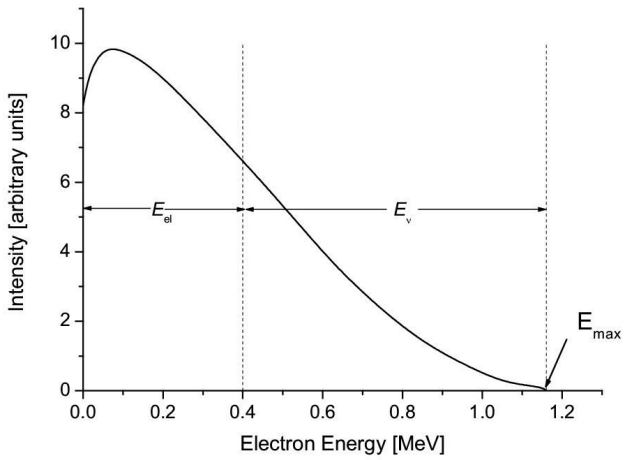
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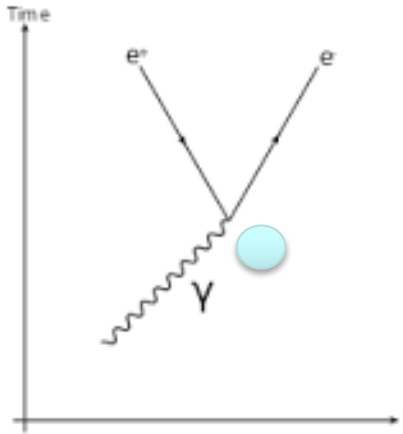
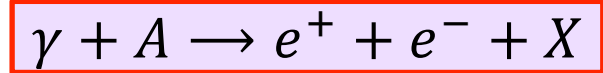
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- The flux intensity is limited ( $10^6$ - $10^8$  e<sup>+</sup>/s)

**Not performant enough for an accelerator source.**

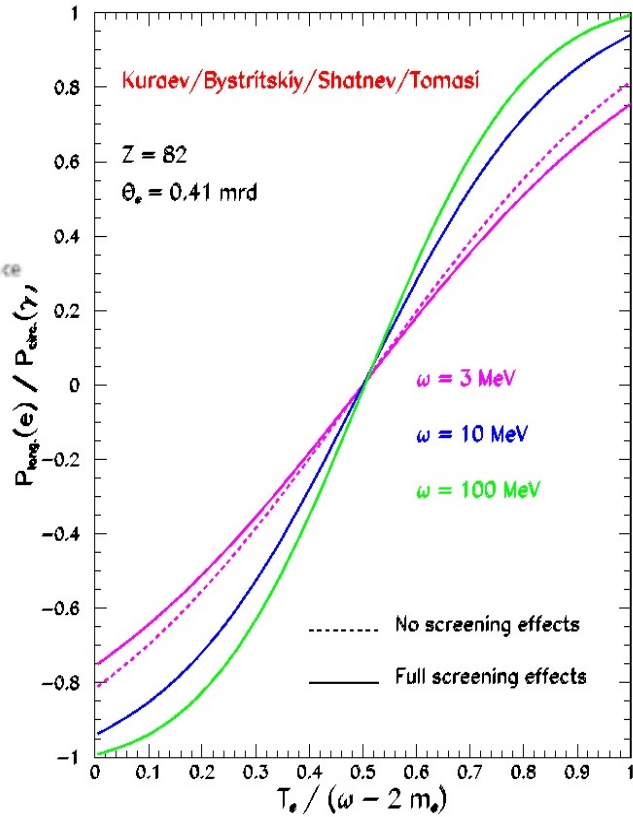
How ?

# Photon Materialisation

H. Olsen, L. Maximon PR 114 (1959) 887 E.A. Kuraev et al. PRC 81 (2010) 055208



## Polarization Transfer



- In the vicinity of the **electromagnetic field of a nucleus**, energetic enough photons ( $E_\gamma > 1.022 \text{ MeV}$ ) create  **$e^+e^-$  pairs**.
- The circular polarization of photons transfer to the pair into longitudinal polarization.
  - The life-time is intrinsically unlimited
  - High fluxes can be achieved ( $10^{10}$ - $10^{13} \text{ e}^+/\text{s}$ )

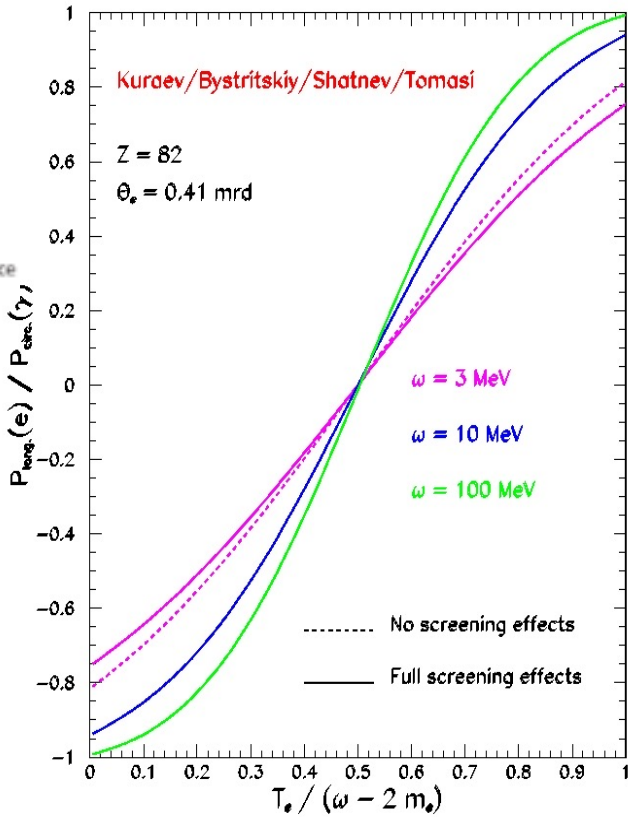
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$$\gamma + A \rightarrow e^+ + e^- + X$$

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**Ideally suited for an accelerator source.**

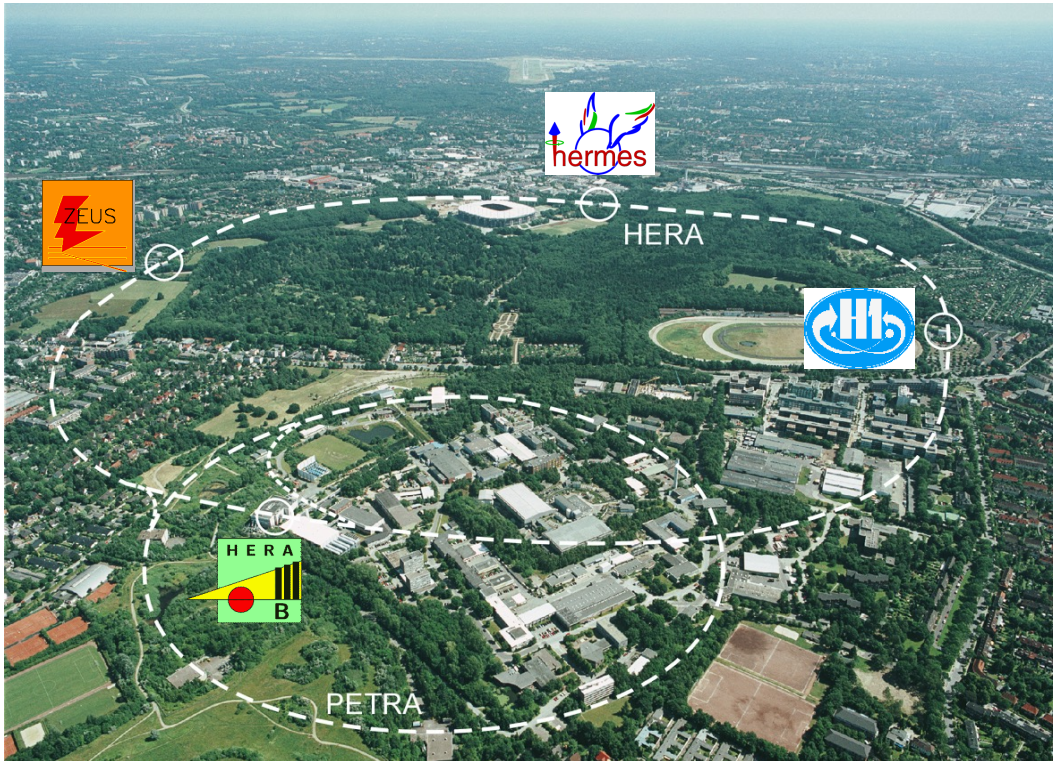


How ?

## Sokolov-Ternov Effect

A.A. Sokolov, I.M. Ternov Sov. Phys. Dokl. 8 (1964) 1203

- The **synchrotron radiation** of **unpolarized positrons** (electrons) in the magnetic field of a storage ring builds up **positron polarization** in the opposite direction to the magnetic field.



Polarization builds up exponentially with a time constant characteristic of the energy and the curvature of the positrons

$$\tau = \frac{8}{5\sqrt{3}} \frac{m_e^2 c^2}{\hbar e^2} \frac{\rho^3}{\gamma^5} \quad (\sim 20\text{mn}@HERA)$$

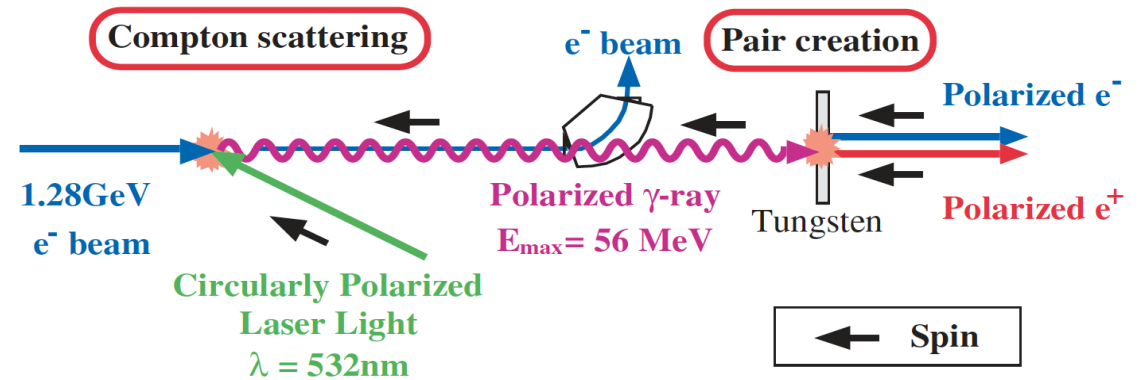
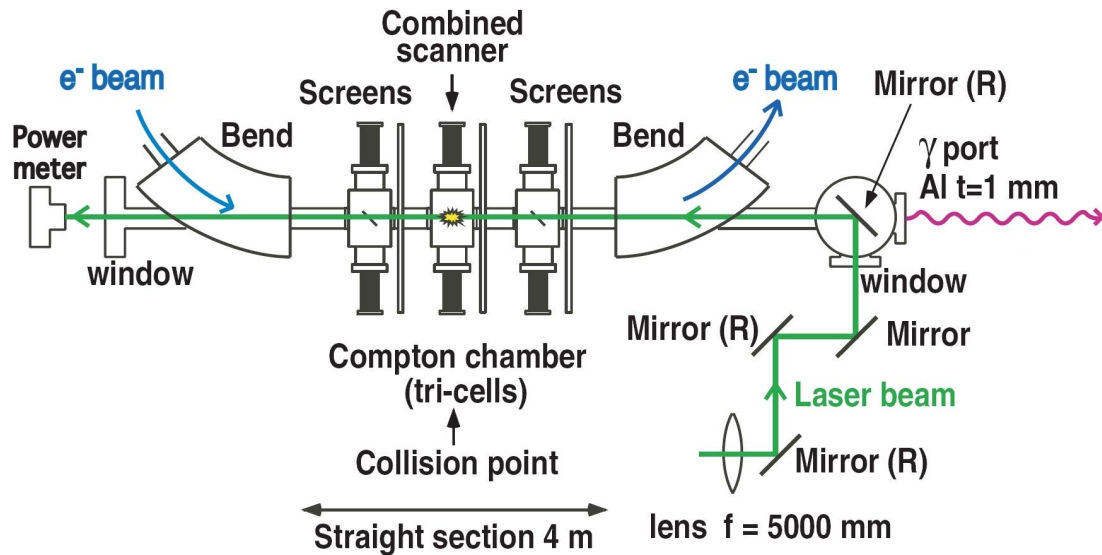
Requires a ring at **multi-GeV energies.**

How ?

# Compton Backscattering

T. Omori et al. PRL 96 (2006) 114801

- The **scattering** of a **polarized laser** light on a **GeV electron** beam generates high energy photons capable of **pair creation**, while the initial **laser polarization** transfers to the **photons**.



The **demonstration experiment** was performed at **KEK** and reported an **efficient propagation of the laser polarization** to the produced positron featuring a high longitudinal polarization degree.

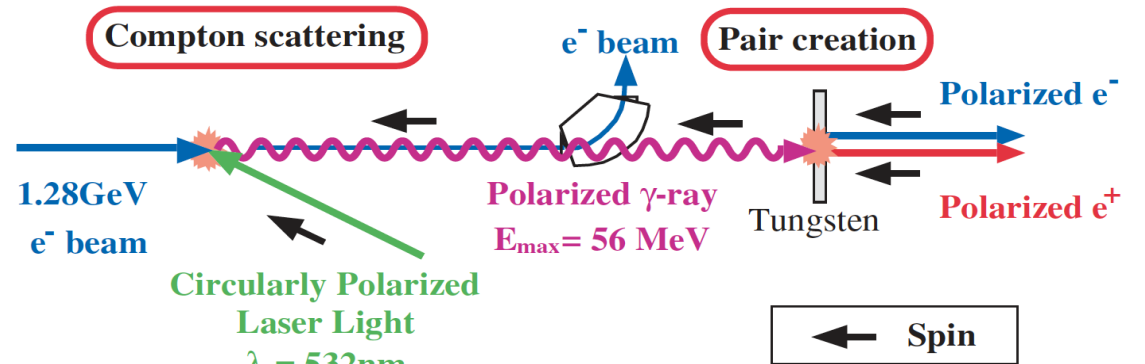
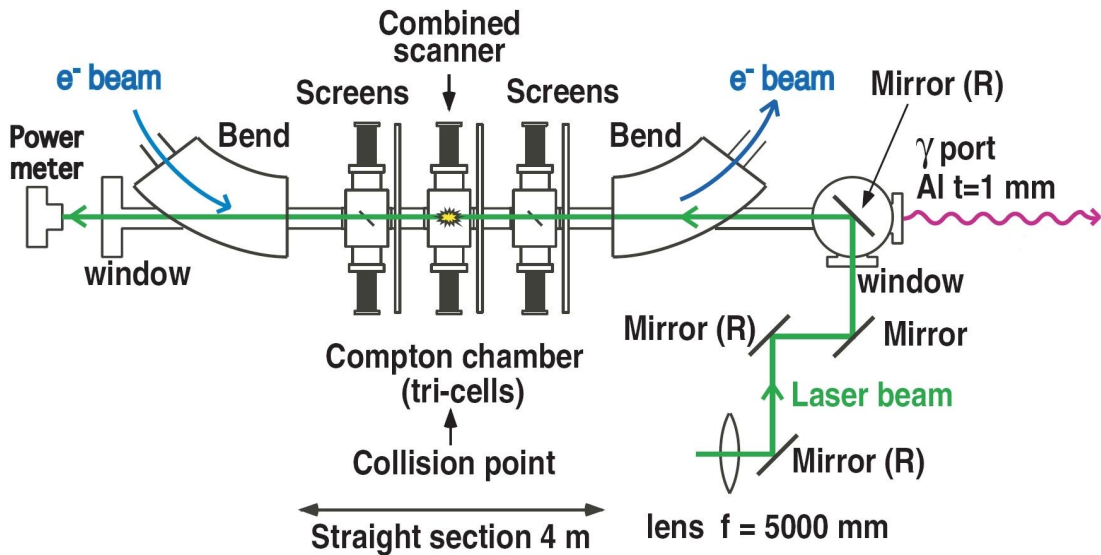
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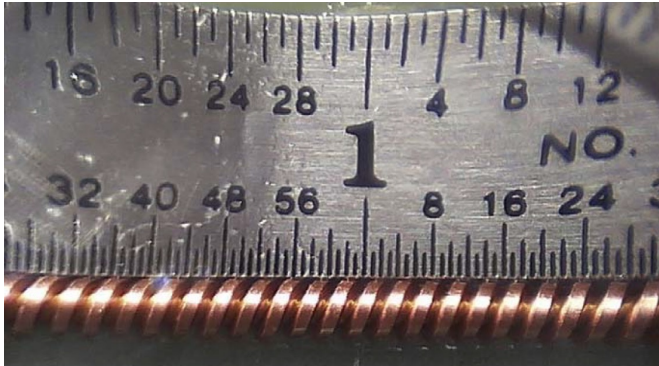
Requires few-GeV energies.

How ?

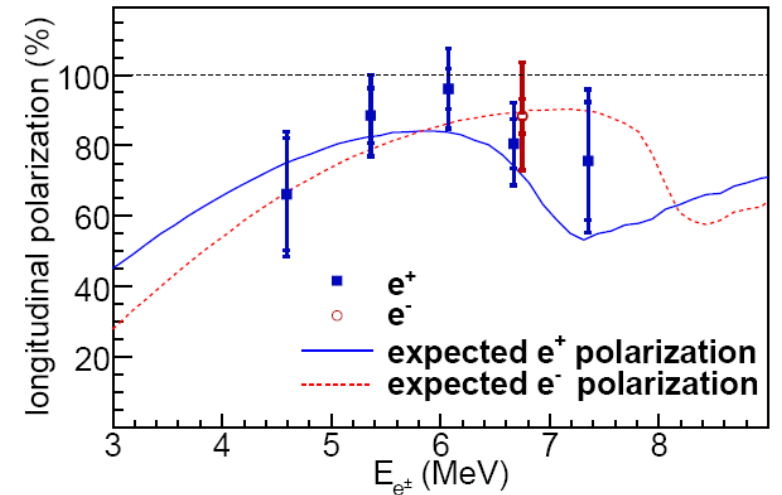
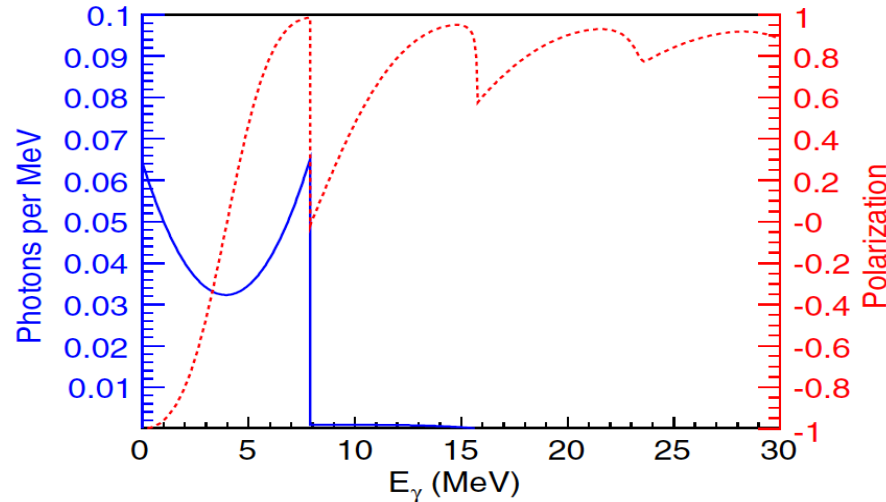
# Undulator Photons

G. Alexander et al. PRL 100 (2008) 210801 G. Alexander et al. NIMA 610 (2009) 451

- A **high energy electron** beam (multi tens of GeV) traveling through a **helical undulator** generates **circularly polarized photons** suitable for polarized positron production.

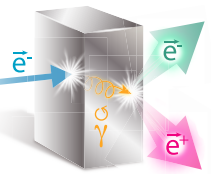


0.6x0.6 mm<sup>2</sup> wire with 2.54 mm period



The **demonstration experiment** was conducted at **SLAC** with a **46.6 GeV** electron beam and reported high longitudinal polarization degree.

The polarized positron source at the International Linear Collider involves a 150 GeV electron beam with a 231 m long undulator.

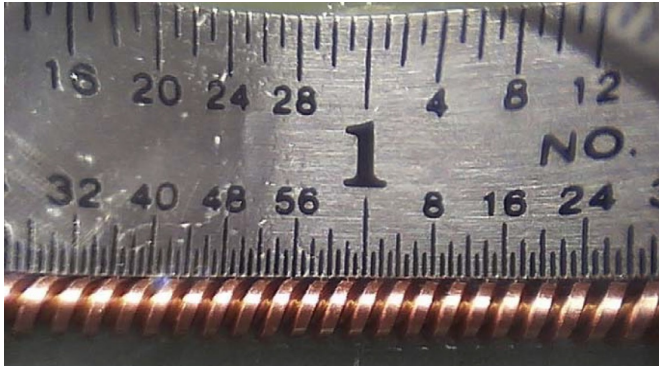


How ?

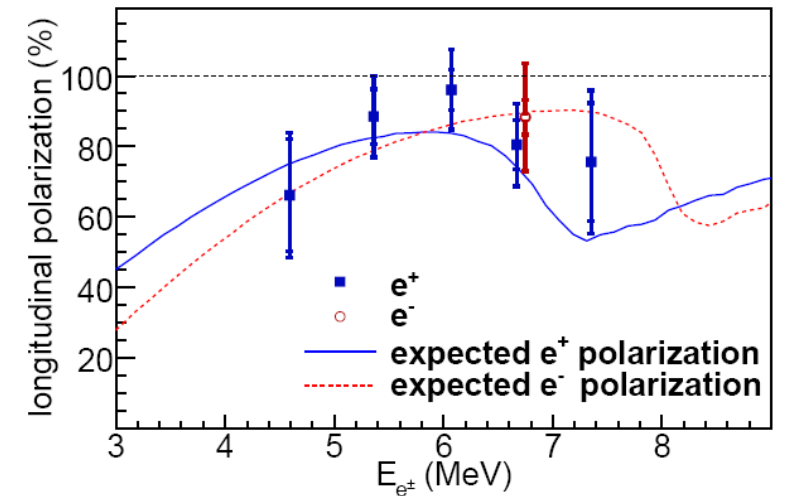
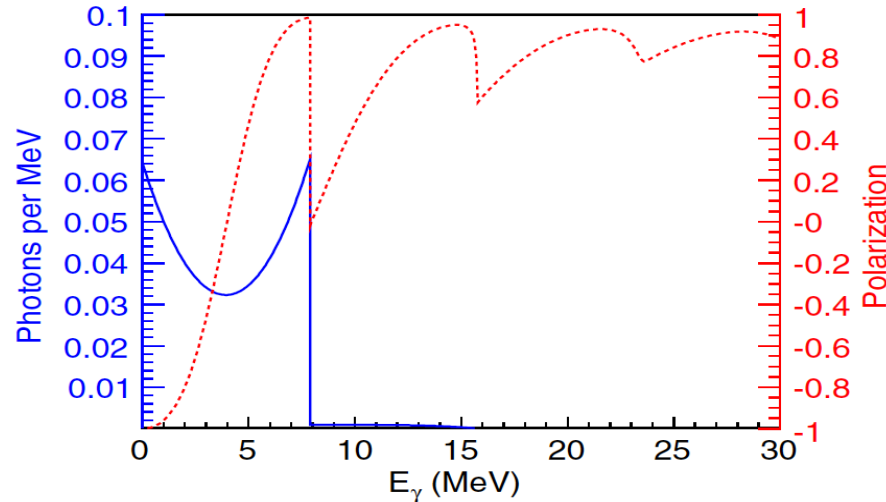
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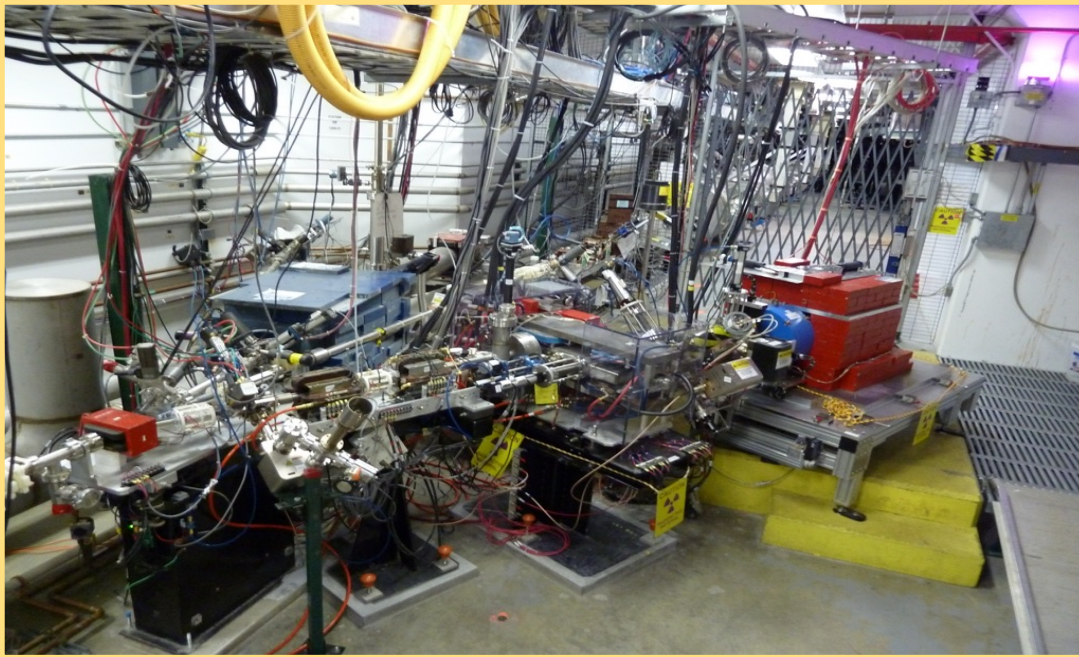
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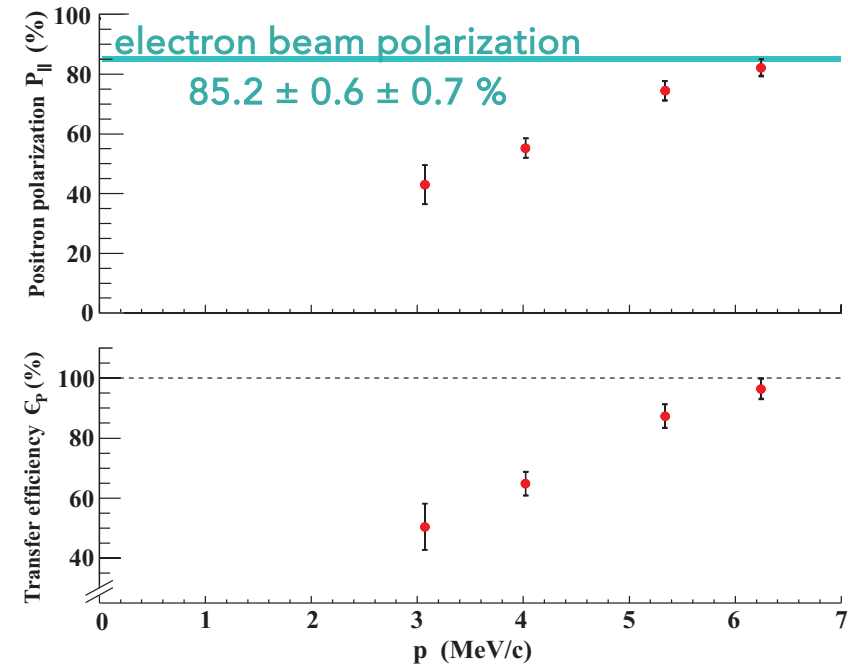
# Polarized Bremsstrahlung

(PEPPo Collaboration) D. Abbott et al. PRL 116 (2016) 214801

- A **longitudinally polarized electron** beam generates in the vicinity of a nuclear field **circularly polarized photons** which create within the same target **longitudinally polarized e<sup>+</sup>e<sup>-</sup>-pairs**.



J. Grames, E. Voutier et al. JLab Experiment E12-11-105 (2011)



The **demonstration experiment** was conducted at the **CEBAF** injector with a **8.2 MeV/c** electron beam reporting the **largest ever** achieved **polarization**.

How ?

# Polarized Bremsstrahlung

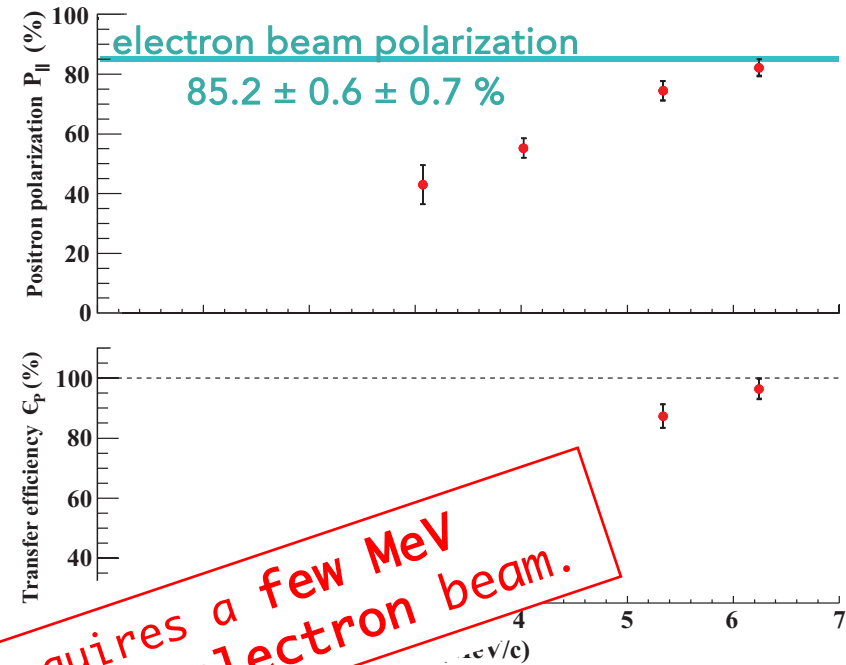
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Requires a few MeV polarized electron beam.

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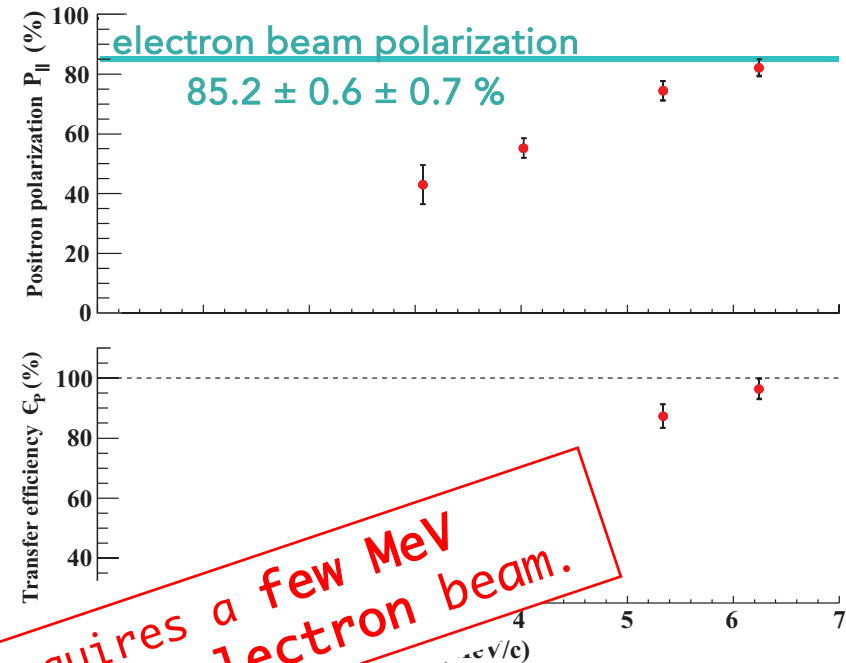
## Polarized Bremsstrahlung

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- ✓ The PEPPo technique has been selected for the **Ce<sup>+</sup>BAF** positron source.
- ✓ The Ce<sup>+</sup>BAF design involves a **120 MeV** highly polarized electron beam with a **1 mA** beam intensity.
- ✓ The **technique** is intrinsically **unlimited** in polarization and intensity.
- ✓ Practical/technological limitations apply in terms of the performances of the **polarized electron source** and the capabilities of the **positron production target**.

(Ce<sup>+</sup>BAF Working Group) J. Grames et al. JACoW IPAC (2023) MOPL152



Requires a few MeV polarized electron beam.

The **demonstration experiment** was conducted at the CEBAF accelerator with a **8.2 MeV/c** electron beam reporting the **largest ever achieved polarization**.



## Figure-of-Merit

- The **Figure-of-Merit** (FoM) quantifies the *polarized performance* of a **source** or a **polarimeter** from the statistical uncertainty of a measurement.

$\mathcal{A}_m$  is the measured asymmetry  
 $P$  is the beam polarization  
 $A_p$  is the physics asymmetry

$$\mathcal{A}_m = \frac{N^+ - N^-}{N^+ + N^-} \stackrel{N^\pm = N_0(1 \pm PA_p)}{=} PA_p$$

$$\delta \mathcal{A}_m = \frac{2}{N^+ + N^-} \sqrt{\frac{N^+ N^-}{N^+ + N^-}} \stackrel{PA_p \ll 1}{\approx} \sqrt{\frac{1}{2N_0}}$$

- $N_0$  is **proportionnal** to the **beam intensity**, the **cross section** of the process, the **detector efficiency**, and the **duration** of the **measurement**.

### Physics

$$A_p = \mathcal{A}_m / P$$

$$\delta A_p = \sqrt{\frac{1}{2N_0 P^2}} = \sqrt{\frac{1}{\text{FoM}}}$$

### Polarization

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Analyzing power

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The FoM is defined as the **convolution** of the **unpolarized yield** and the **squared polarization capabilities**.

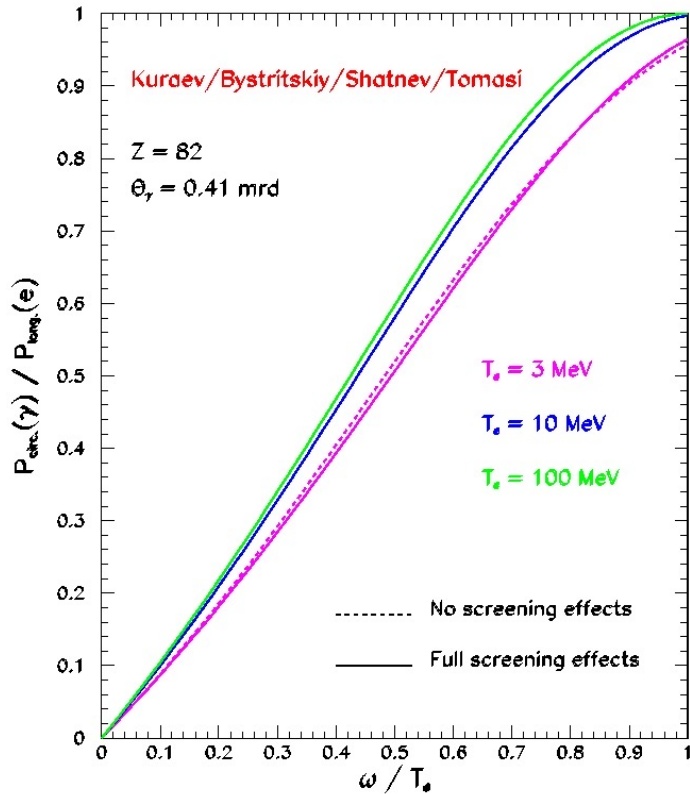
Analyzing power

# Polarized Yield

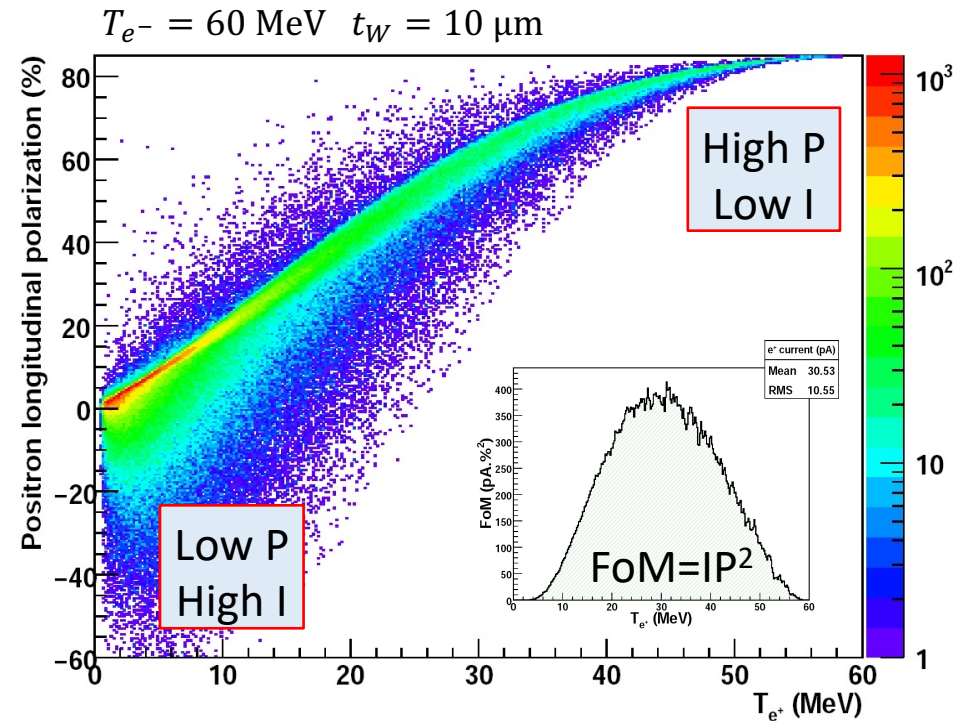
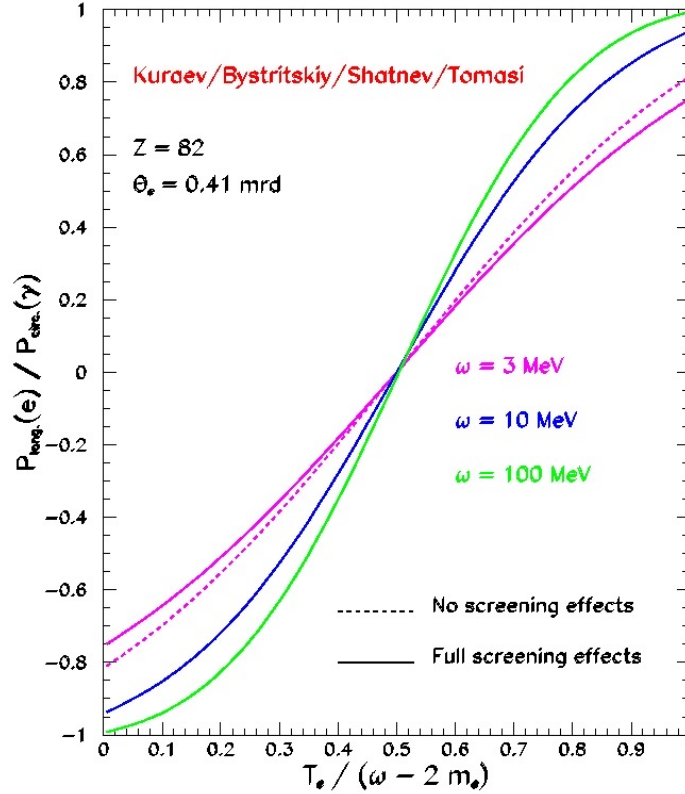
H. Olsen, L. Maximon PR 114 (1959) 887 E.A. Kuraev et al. PRC 81 (2010) 055208

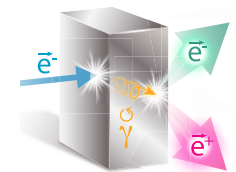
- The positron **yield** ( $e^+/e^-$ ) and **polarization** results from the convolution of two processes : the initial **polarized electron beam bremsstrahlung** and the **creation of  $e^+e^-$ -pairs** by the bremsstrahlung **polarized photons**.

BREMSSTRAHLUNG



PAIR CREATION

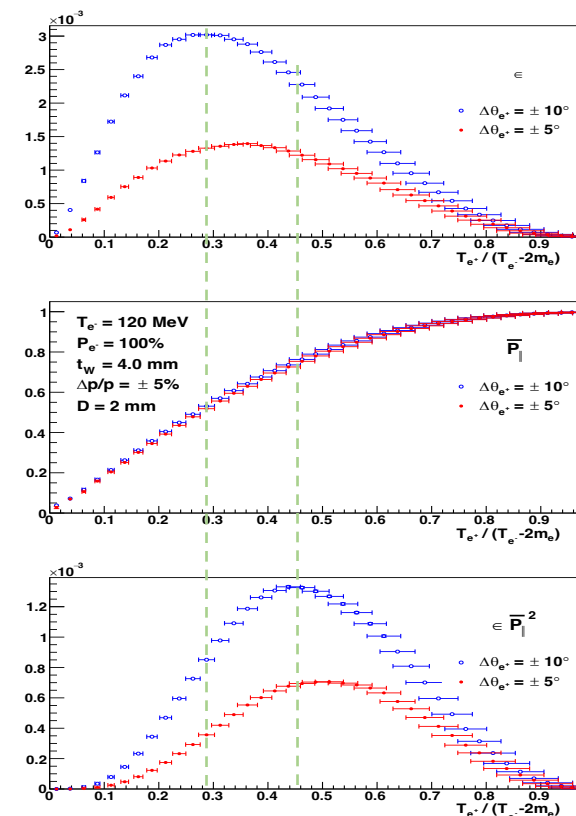
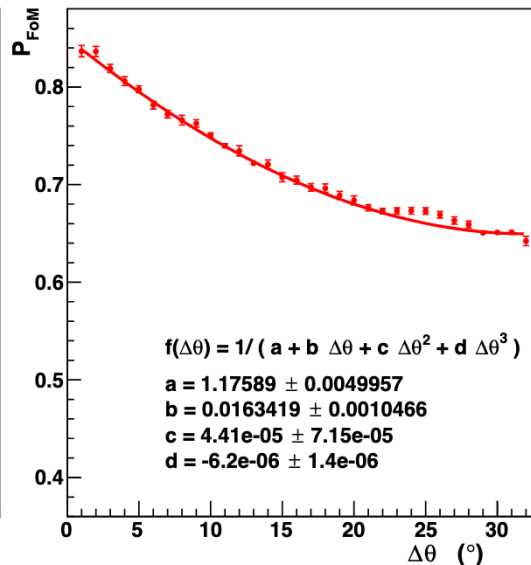
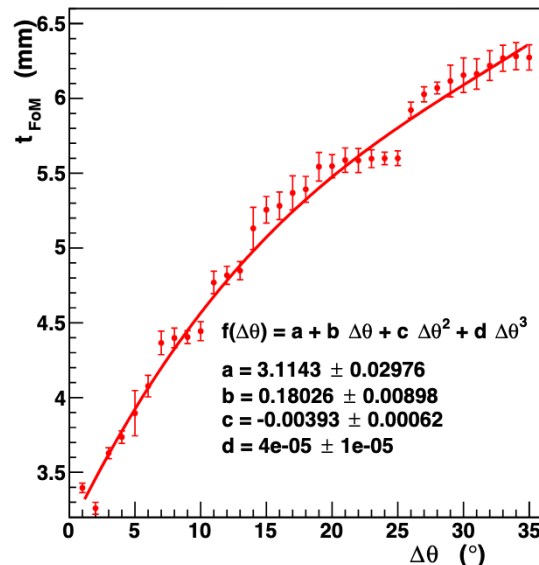
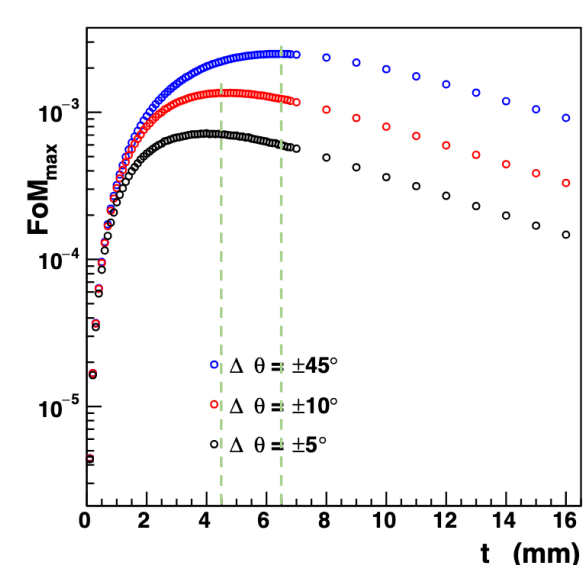




# ***e<sup>+</sup> Source Optimization***

S. Habet et al. JLAB-ACC-23-3794 (2023) arXiv:2401.04484

- The positron **yield** ( $e^+/e^-$ ) scales with the beam power (**Beam Energy × Beam Intensity**) and depends on the thickness of the production target.
- The **optimum target thickness** depends and the properties of the **positron collection system** which can mimic by angular ( $\Delta\theta_{e^+}$ ) and momentum ( $\Delta p/p$ ) acceptances.



- ✓ The **selection of the positron momentum** allows to operate either with **optimum FoM** (polarized mode) or **optimum efficiency** (unpolarized mode).

(Jefferson Lab Positron Working Group) A. Accardi et al. EPJ A 57 (2021) 261

# Polarimetry

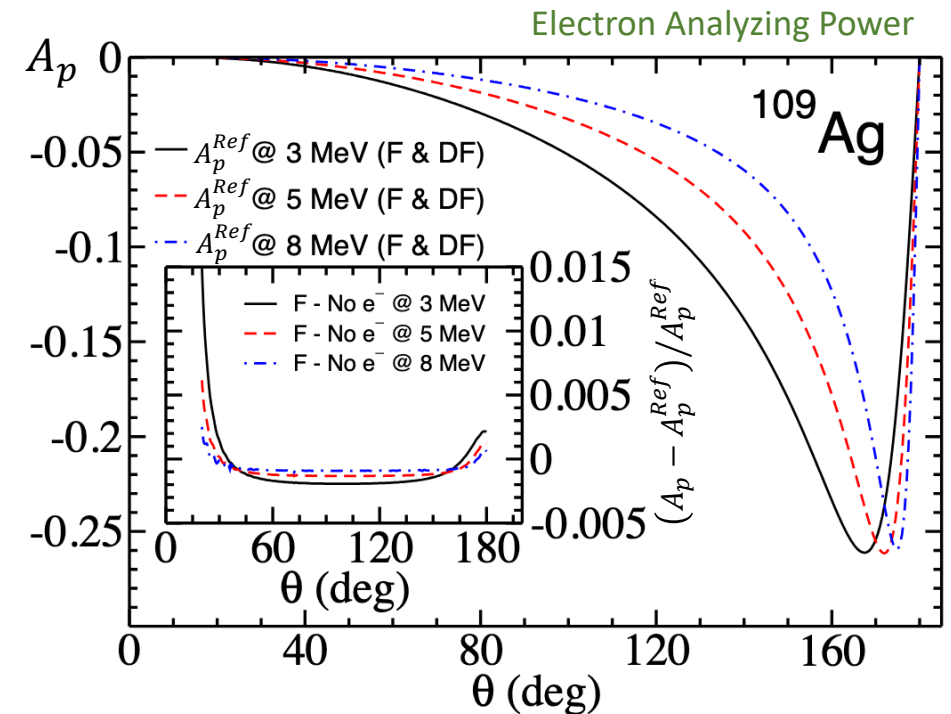
## Mott

J.M. Hoogduin PhD Thesis, Groningen University (1997) X. Roca-Maza EPL 120 (2017) 33002

- At low energies (up to a few MeV), the **Mott scattering** is a well-established method to measure the polarization of an electron beam.
- It involves the **elastic scattering** of electrons off a **heavy nucleus** and the interaction of the **electron spin** with the **Coulomb field** of the nucleus.
- The asymmetry is measured with respect to the **beam polarization orientation**.
- Mott polarimetry requires **transversely polarized** beams.

$$\frac{d\sigma}{d\Omega} = \frac{Z^2 e^4}{4m^2 c^4} \frac{(1 - \beta^2 \sin^2(\theta/2))(1 - \beta^2)}{\beta^4 \sin^2(\theta/2)} [1 \pm P_e A_p]$$

The **sensitivity** of the Mott process to positron polarisation is expected to be **strongly reduced** because of the **repulsive interaction** with the Coulomb field.



# Polarimetry

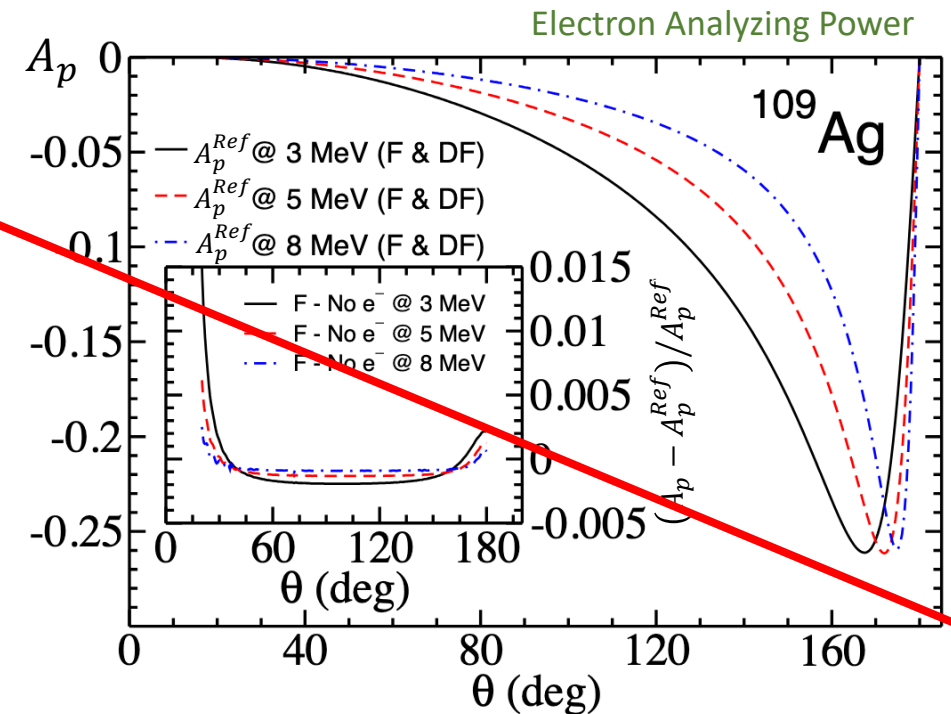
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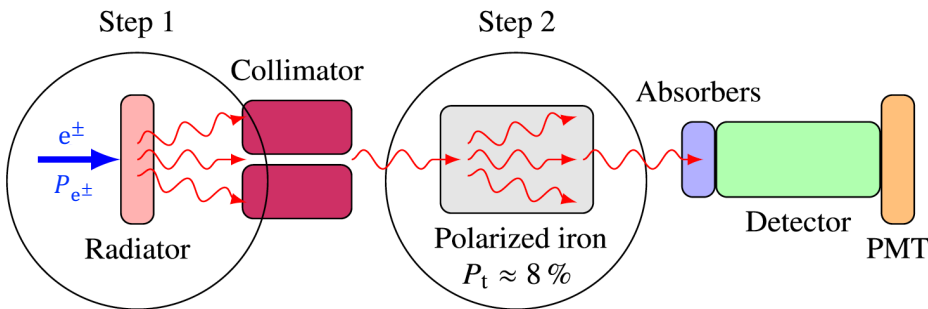


## Compton Transmission

G. Blume et al. NIMA 1062 (2024) 169224

Step 2

- The absorption of **circularly polarized photons** ( $P_\gamma$ ) inside a **polarized target** ( $P_t$ ) generates an asymmetry which is proportional to the photon polarization.
- The asymmetry is measured with respect to the **parallel/anti-parallel target polarization orientation**.



$$\varepsilon_T = \exp[-\rho_e L (\sigma_{\text{phot}} + \sigma_{\text{pair}})] \times \exp[-\rho_e L \sigma_C^0 (1 \pm \rho_e L P_t P_\gamma A_p)]$$

$$A_p = \int d\Omega \left[ \frac{\omega_0}{\omega} - \frac{\omega}{\omega_0} \right] \cos \theta$$

$(\omega, \omega_0)$  are the initial and scattered photon energies

Step 2  $\mathcal{A}_m \approx \rho_e L P_t P_\gamma A_p$

Step 1+2  $\mathcal{A}_m \approx \rho_e L P_t P_{e^\pm} \langle T_\gamma^e A_p \rangle$

- ✓ Compton transmission polarimeters can operate either with **electrons or positrons** for the measurement of the **longitudinal polarization** of a beam.
- ✓ The **optimum energy range** is up to a **few tens of MeV** where the cross section of the Compton process is significant.

## Positron Annihilation

W.H. McMaster RMP 33 (1961) 8 J.M. Hoogduin PhD Thesis, Groningen University (1997)

- The annihilation into  $\gamma$ -pairs of **polarized positrons** ( $P_x, P_y, P_z$ ) with electrons in a **polarized metallic target** ( $S_x, S_y, S_z$ ) generates an asymmetry suitable for the measurement of the beam polarization.
- The **sensitivity** of the annihilation process to the **3 different components** of the **positron polarization** is similar in magnitude.
- The asymmetry is measured with respect to the **parallel/anti-parallel target polarization orientation**.

$$\left. \frac{d\sigma}{d\Omega} \right|_{cm} = \frac{\alpha^2}{s} \frac{1}{\beta} \frac{A_0 (1 \pm P_x S_x A_x \pm P_y S_y A_y \pm P_z S_z A_z)}{(1 - \beta^2 \cos^2(\theta))^2}$$

$$A_0 = 1 + 2\beta^2 \sin^2(\theta) - \beta^4 [1 + \sin^4(\theta)]$$

$$A_x = \frac{(-1 + 2\beta^2 - \beta^4 [1 + \sin^4(\theta)])}{A_0}$$

$$A_y = \frac{(-1 + 2\beta^2 - \beta^4 [1 - \sin^4(\theta)])}{A_0}$$

$$A_z = \frac{(-1 + 2\beta^2 \sin^2(\theta)(1 - \sin^2(\theta)) + \beta^4 [1 + \sin^4(\theta)])}{A_0}$$

A possible solution  
for positron polarimetry  
of **few hundreds MeV**.



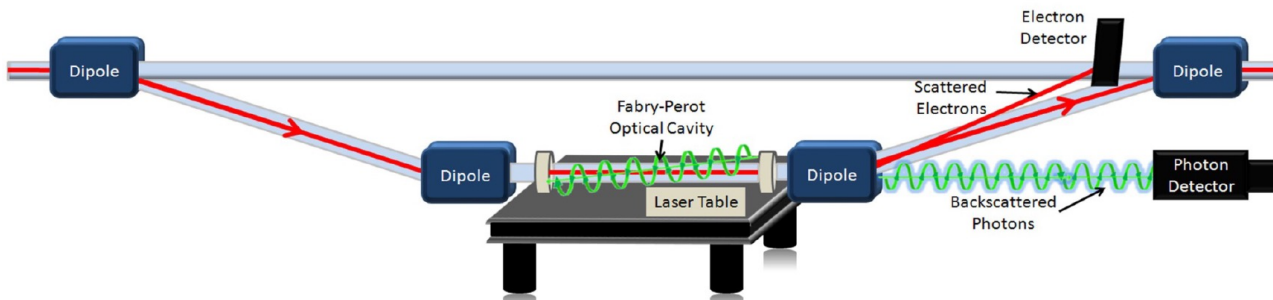
## Compton Backscattering

D. Gaskell, Positron Working Group Workshop, Charlottesville (2023)

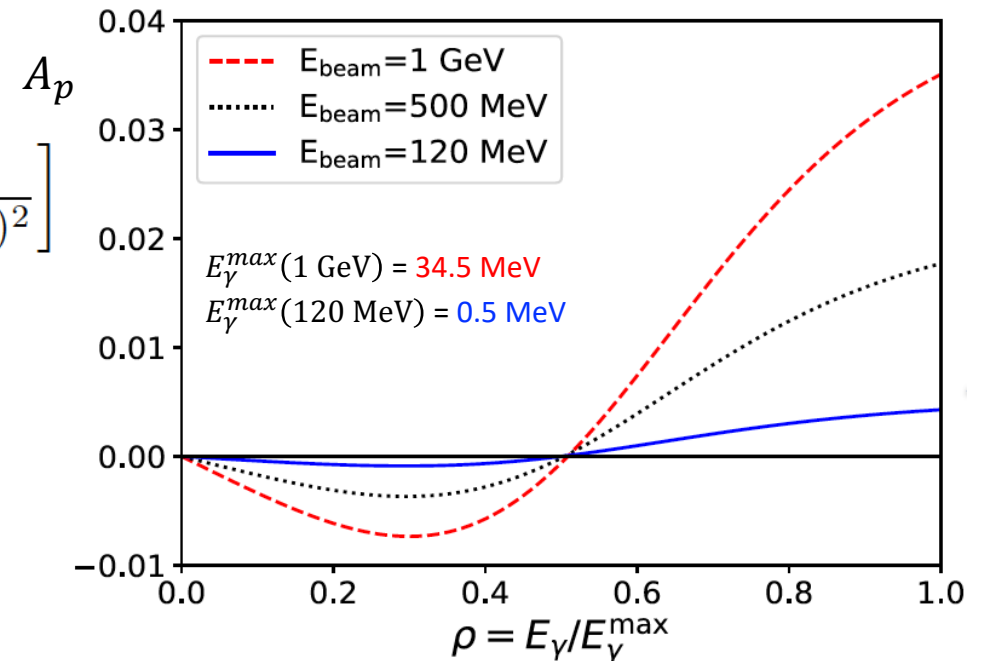
- The backscattering of a **circularly polarized laser** ( $P_\gamma$ ) onto a **longitudinally polarized** ( $P_{e^+}$ ) **positron beam** generates an asymmetry of the photon number.
- The asymmetry is measured with respect to the **left/right orientation** of the **laser polarization**.
- Compton backscattering requires **enough beam energy** (>1GeV) for sizeable analyzing power and energetic photon generation, as well as **reasonable beam intensity** for precise measurement.

$$\frac{d\sigma}{d\rho} = 2\pi r_o^2 a \left[ \frac{\rho^2(1-a)^2}{1-\rho(1-a)} + 1 + \left( \frac{1-\rho(1+a)}{1-\rho(1-a)} \right)^2 \right]$$

$$a = \frac{1}{1 + 4\gamma E_{\text{laser}}/m_e} \quad A_p = \frac{2\pi r_o^2 a}{(d\sigma/d\rho)} (1 - \rho(1+a)) \left[ 1 - \frac{1}{(1 - \rho(1-a))^2} \right]$$



Hall A & C Compton polarimeter



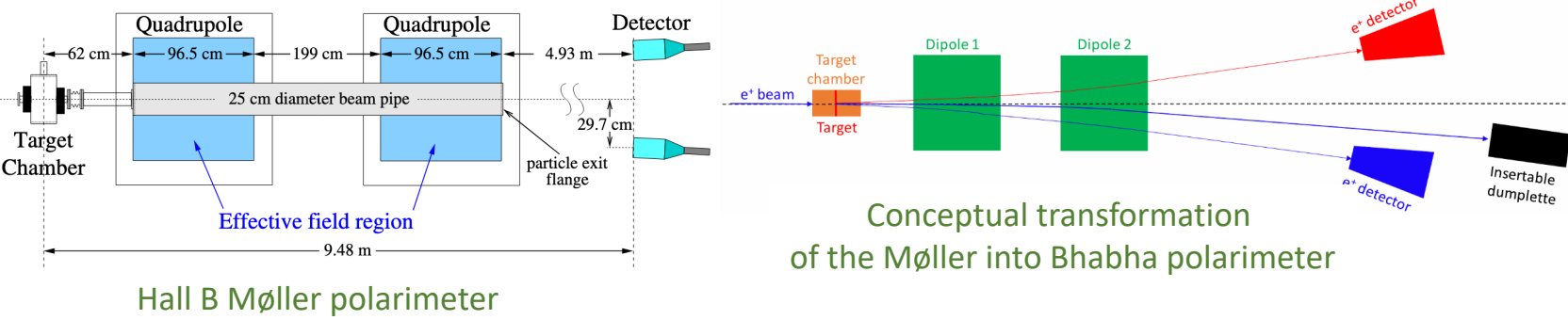
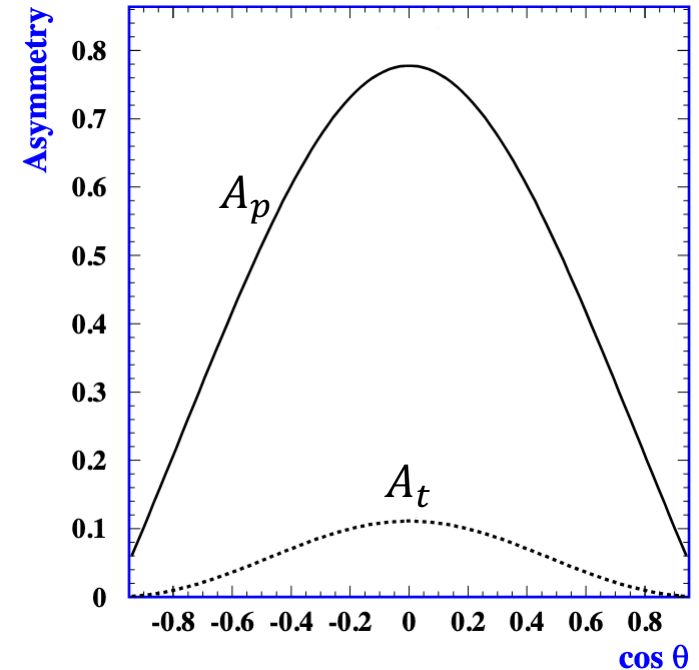
## Bhabha Scattering

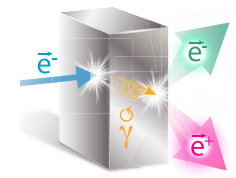
G. Alexander, I. Cohen NIMA 486 (2002) 552

- Similarly to the Møller scattering of polarized electrons, the scattering of **polarized positrons** off electrons (Bhabha) in a **polarized metallic target** can be used to measure the beam polarization.
- Bhabha scattering is sensitive to **longitudinal** and **transverse beam polarization**, however transverse sensitivity is much smaller.
- The asymmetry is measured with respect to the **parallel/anti-parallel target polarization orientation**.

$$\left. \frac{d\sigma}{d\Omega} \right|_{cm} = \frac{\alpha^2}{s} \frac{[3 + \cos^2(\theta)]^2}{\sin^4(\theta)} [1 \pm P_e^l + P_t A_p \pm P_e^t + P_t A_t \cos(2\phi - \phi_{e^+} - \phi_t)]$$

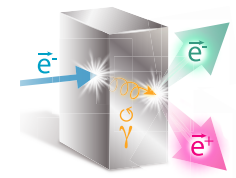
$$A_p = \frac{[7 + \cos^2(\theta)] \sin^2(\theta)}{(3 + \cos^2(\theta))^2} \quad A_t = \frac{\sin^4(\theta)}{(3 + \cos^2(\theta))^2}$$





# Summary

- ▶▶ **Positron beams** are **important tools** allowing us to investigate the many faces of physics.
- ▶▶ They are optimally produced by the **bremsstrahlung radiation** of an **electron beam** which **polarization transfers** efficiently to the produced **positrons**.
- ▶▶ The optimization of their production is a multi-dimensionnal problem which dominant parameter is the **angular acceptance** of the positron **collection system**.
- ▶▶ **Positron polarimetry** is **similar to electron polarimetry**, apart Mott scattering and positron annihilation.



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## Questions ?