

Application of novel computational techniques for the determination of the proton's gravitational form factors and mechanical properties:

A JLab LRDR project

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Outline

I **Motivations and scope of the project:**

Extraction of Gravitational Form Factors using Neural Networks, from experimental data with constraints from LQCD

II **Current state of the project:**

Test of the Gepard framework and extraction of Form Factors using LQCD

III **Future directions**

Motivation and scope of the project:

Extraction of Gravitational Form Factors from experimental data using Neural Networks, with constraints from LQCD

Gravitational Form Factors (GFFs)...

Matrix element from the QCD Energy-Momentum Tensor

$$\langle p', s' | \hat{T}_{\mu\nu}^a(x) | p, s \rangle = \bar{u}' \left[A^a(t) \frac{P_\mu P_\nu}{m} + J^a(t) \frac{iP_{\{\mu\sigma\nu\}\rho}\Delta^\rho}{2m} + D^a(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{4m} + m\bar{c}^a(t)g_{\mu\nu} \right] u e^{i(p'-p)x}$$

Properties of the proton

in unit of m_p

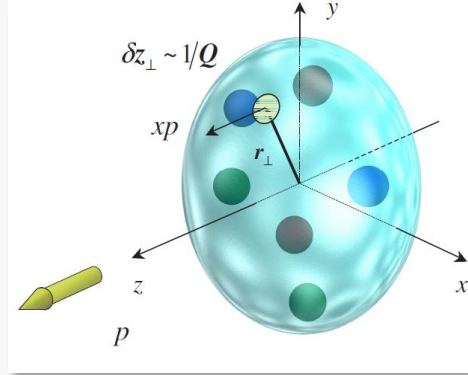
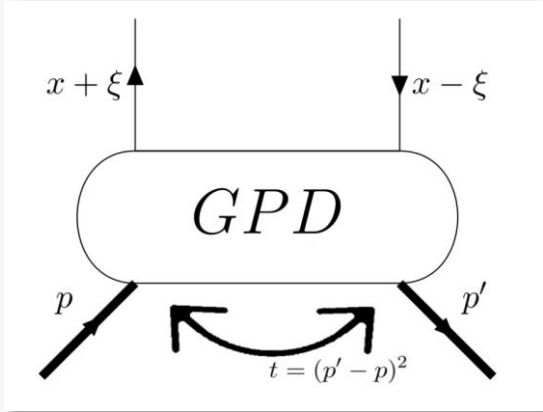
$$A(0) = \sum_a A^a(0) = 1 \quad \bar{c}(t) = \sum_a \bar{c}^a(t) = 0 \quad J(0) = \frac{1}{2}(A(0) + B(0)) = \frac{1}{2} \quad D(0) = ? < 0$$

$$\langle r^2 \rangle_{mech} = \frac{6D(0)}{\int_{-\infty}^0 dt D(t)} \quad p(r) = \frac{1}{6M_N} \frac{1}{r^2} \frac{d}{dr} r^2 \frac{d}{dr} \tilde{D}(r) \quad s(r) = \frac{1}{4M_N} r \frac{d}{dr} \frac{1}{r} \frac{d}{dr} \tilde{D}(r)$$

Full Review in Forces inside hadrons: pressure, surface tension, mechanical radius, and all that, Maxim V. Polyakov, Peter Schweitzer, Int.J.Mod.Phys. (2018)

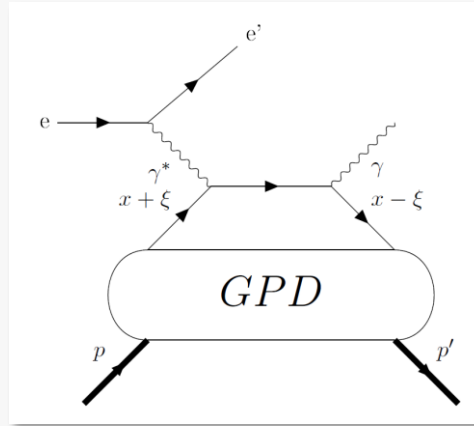
... and their link to GPDs

A “hand-wave” definition of GPDs:



Figures in A.V. Belitsky, A.V. Radyushkin, Unraveling hadron structure with generalized parton distributions, Physics Reports, Volume 418, Issues 1–6 2005

Deeply Virtual Compton Scattering



- DVCS amplitude depends on complex integral of GPDs, the Compton form factors:

$$\mathcal{H} = \int_{-1}^1 dx H(x, \xi, t) \left(\frac{1}{\xi - x - i\epsilon} - \frac{1}{\xi + x - i\epsilon} \right)$$

- Accessing Gravitational Form Factors, which appear in the nucleon EMT matrix elements:

$$\int_{-1}^1 dx x H^q(x, \xi, t) = A^q(t) + \xi^2 D^q(t)$$

$$\int_{-1}^1 dx x E^q(x, \xi, t) = B^q(t) - \xi^2 D^q(t)$$

→ $\text{Re}\mathcal{H}(\xi, t) = \mathcal{P} \int_{-1}^1 dx \left(\frac{1}{\xi - x} - \frac{1}{\xi + x} \right) \text{Im}\mathcal{H}(\xi, t) + \Delta(t)$ $\Delta(t) \propto D(t) \propto \int d^3\mathbf{r} p(r) \frac{j_0(r\sqrt{-t})}{t}$

DVCS beam charge asymmetry

- Understanding the spin composition of the nucleon (aka the “spin puzzle”) using the Ji’s sum rule:

$$J_Q = \sum_q \frac{1}{2} \int_{-1}^1 dx x (H^q(x, \xi, 0) + E^q(x, \xi, 0)) = \sum_q \frac{1}{2} (A^q(t) + B^q(t))$$

Existing tools



- C++ framework for the phenomenology of the 3D structure of the nucleon (TMDs & GPDs)
- [Partons Website](#)
- B. Berthou et al., PARTONS: PARtonic Tomography Of Nucleon Software: A computing platform for the phenomenology of Generalized Parton Distributions, Eur. Phys. J. C78 (2018), 478

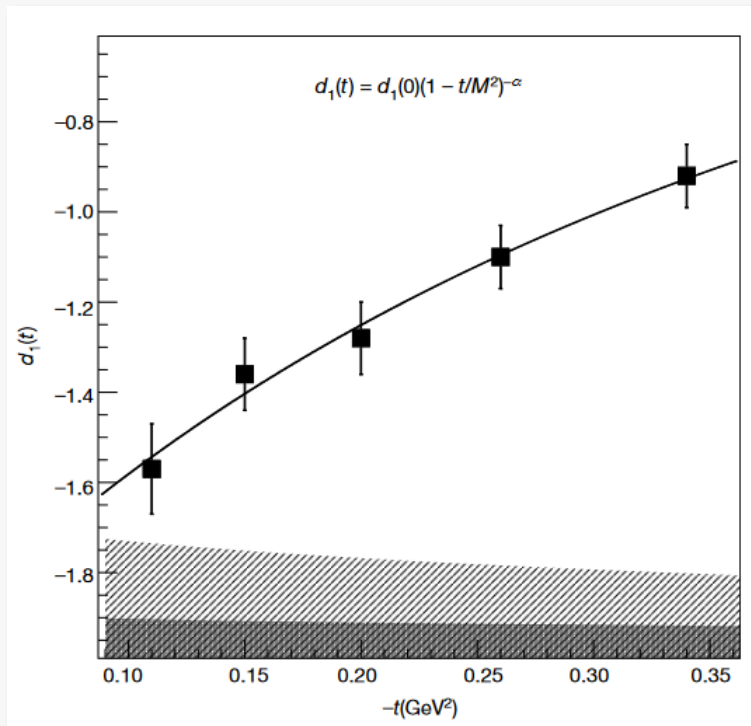


- Python framework for the study of GPDs
- [Gepard Website](#)
- K. Kumerički, D. Müller, K. Passek-Kumerički, Towards a fitting procedure for deeply virtual Compton scattering at next-to-leading order and beyond, Nuclear Physics B, Volume 794, Issues 1–2, 2008

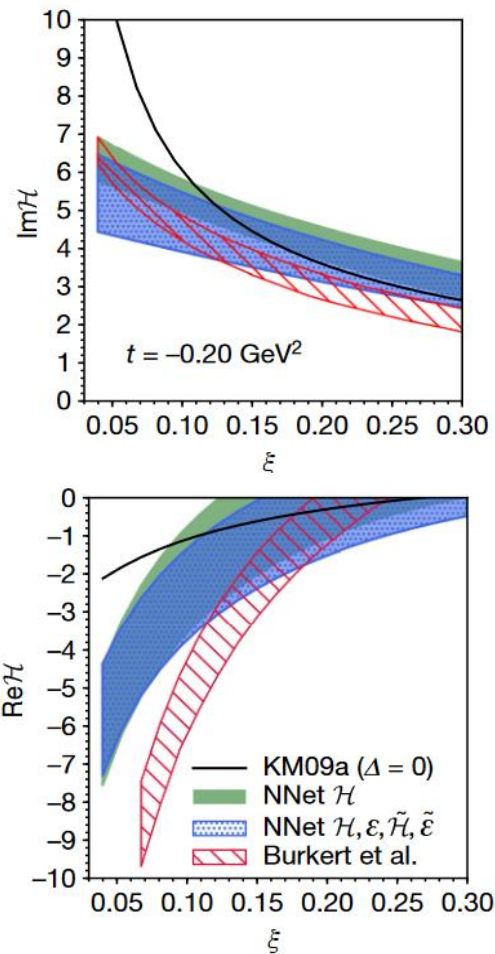
Limitations

- No dedicated methods to fit all GFFs
- Ad-hoc or outdated ML libraries

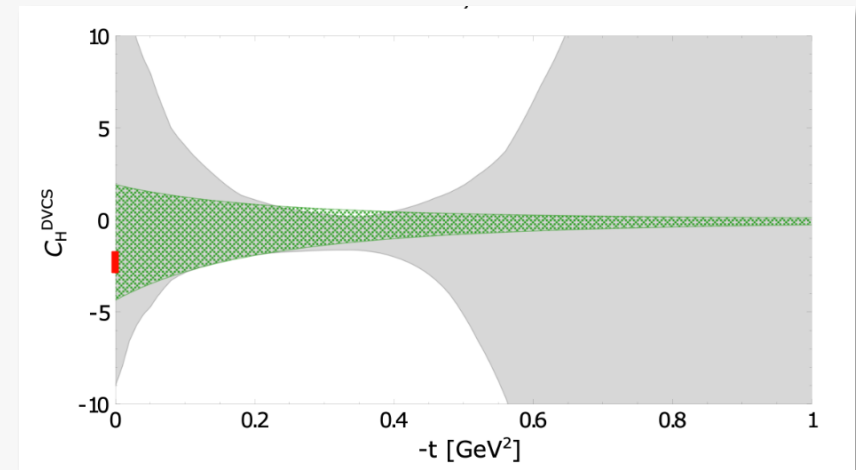
Previous works and results



Burkert, V.D., Elouadrhiri, L. & Girod, F.X. The pressure distribution inside the proton. *Nature* **557**, 396–399 (2018)





Kumerički, K. Measurability of pressure inside the proton. *Nature* **570**, E1–E2 (2019)



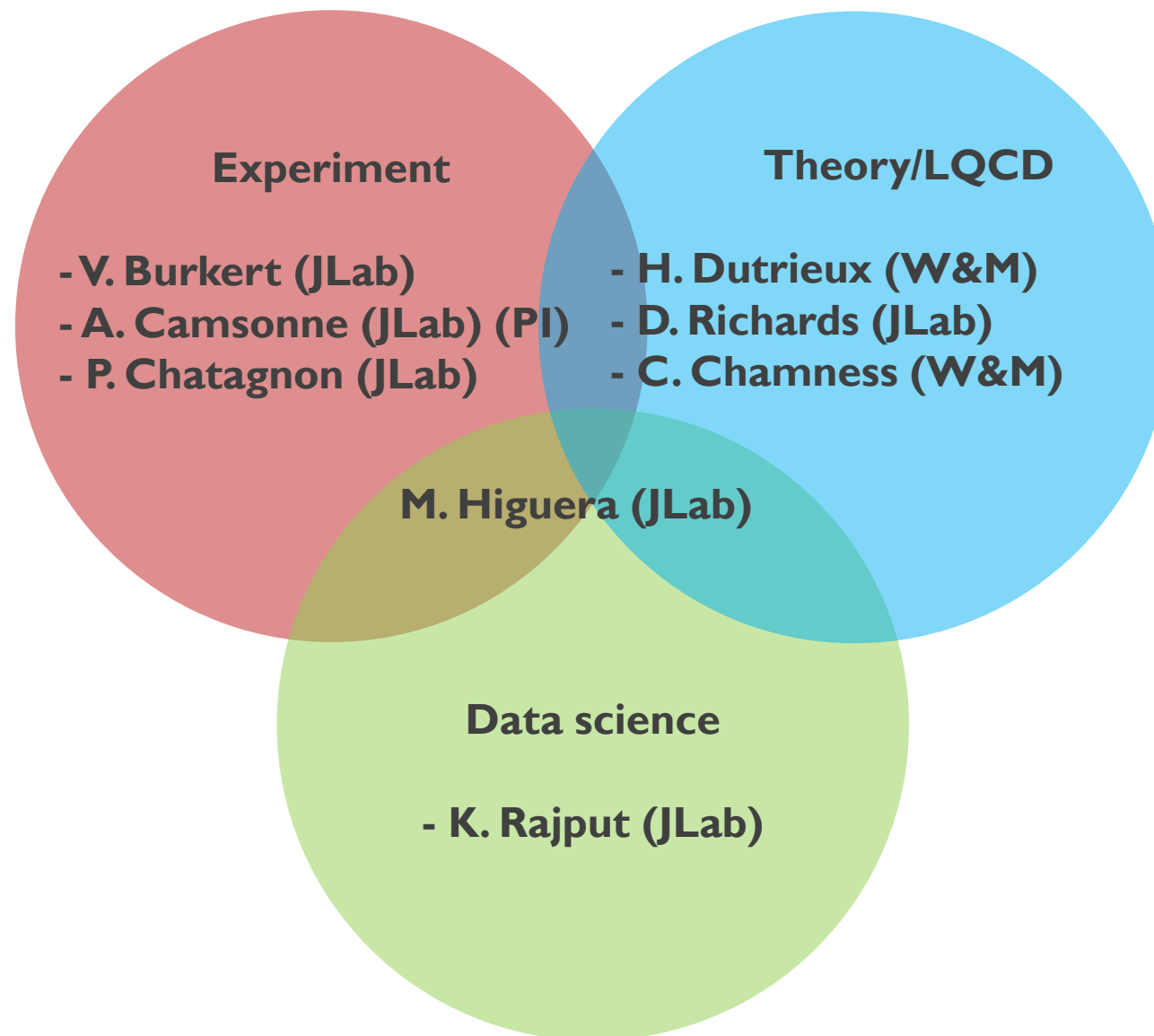
H. Dutrieux et al. Phenomenological assessment of proton mechanical properties from deeply virtual compton scattering. *The European Physical Journal C*, 81(4):300, Apr 2021

Deliverables

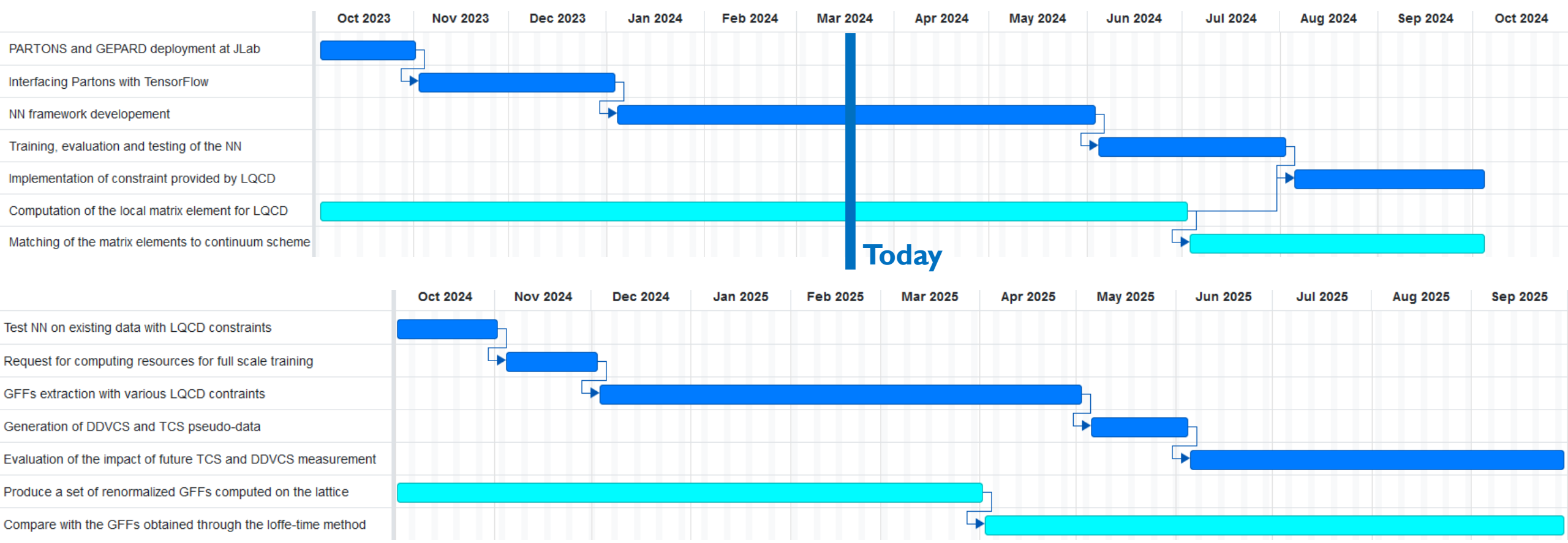
- A tools to fit all existing data using Neural Networks to extract GFFs
- Easy to use and interface with previous tools →  python™
- Use State-of-the-art standard ML libraries →  PyTorch
- Able to handle both experimental and LQCD data
- Able to test the impact of future experiments

Impact of the positron DVCS program

Personnel



Timeline



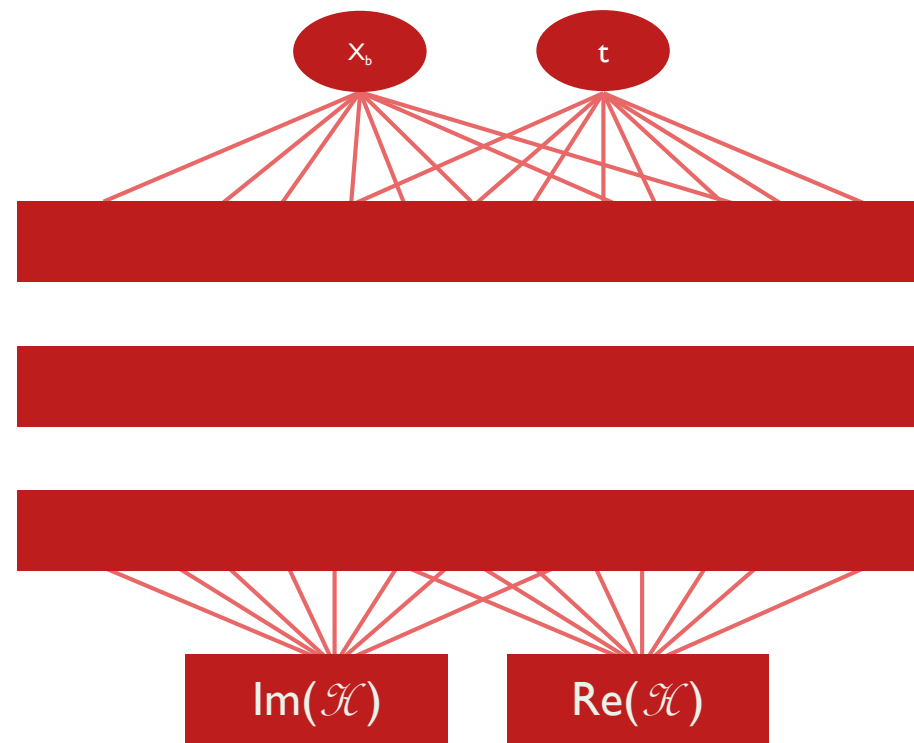
Current state of the project:

Test of the Gepard framework and
extraction of Form Factors using LQCD

Fitting DVCS data using a Neural Network

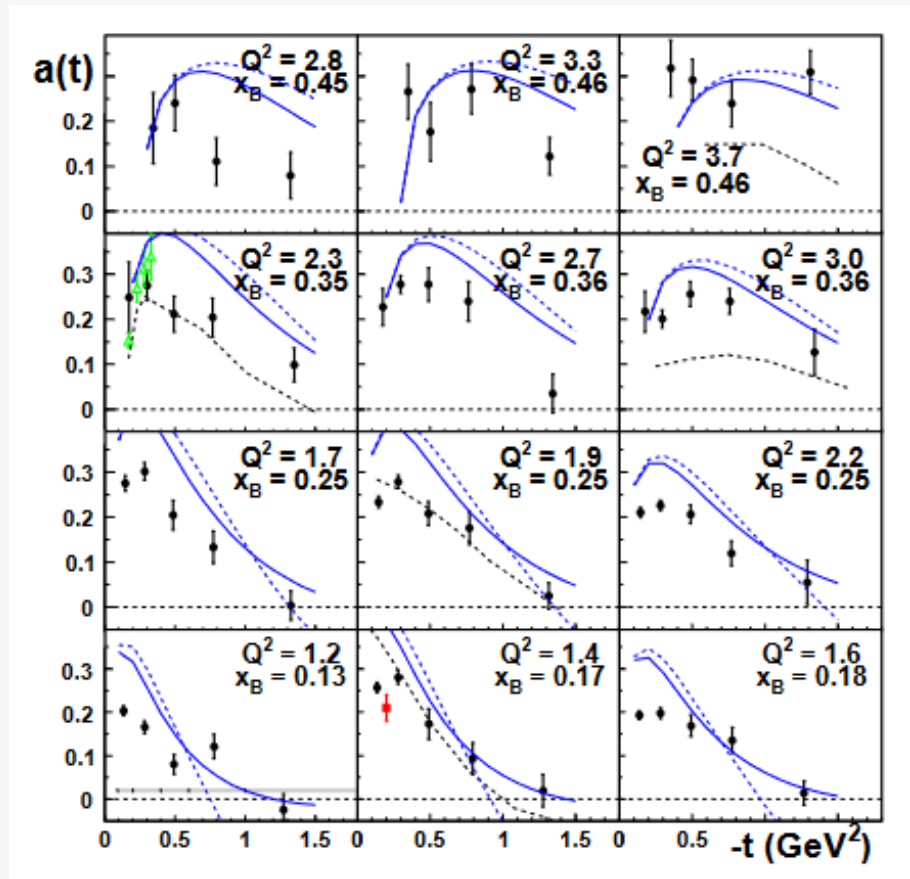
Test of the Gepard framework

- All results shown here are obtained based on the Gepard code available [here](#)
- Goal: test if one can reproduce *Kumerički, K. Measurability of pressure inside the proton. Nature 570, E1–E2 (2019)* results to build upon it
- **Approach:**
 - Fit CLAS results with a neural network and extract Compton Form Factors
 - Pytorch is used to build and train the Neural Network
 - No constraints on the NN (in particular no dispersion relation)

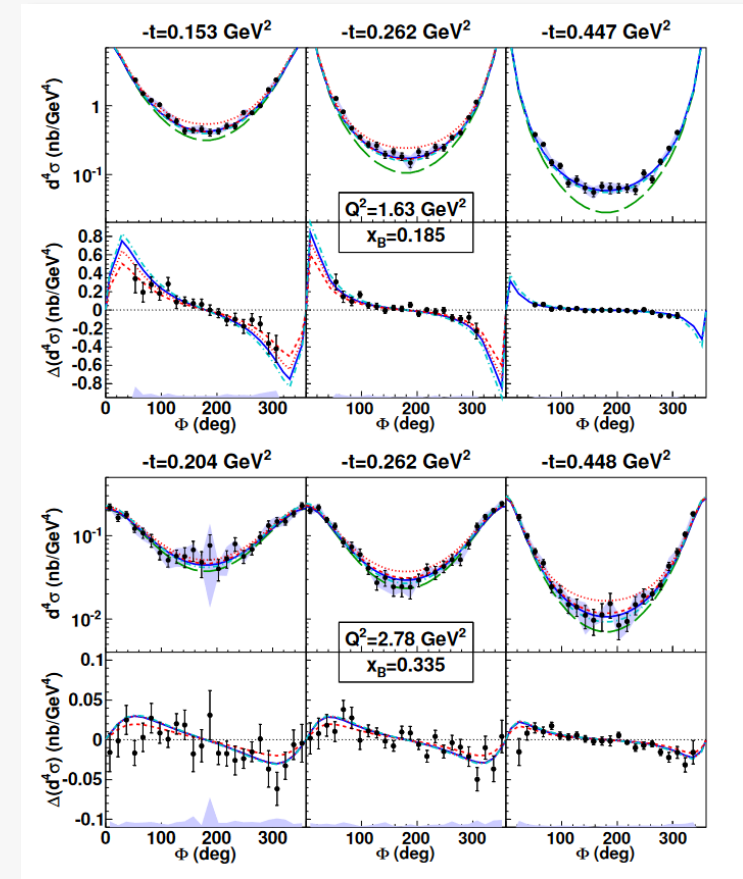


Data sets used for the fit

DVCS beam spin asymmetries measured by the CLAS experiment



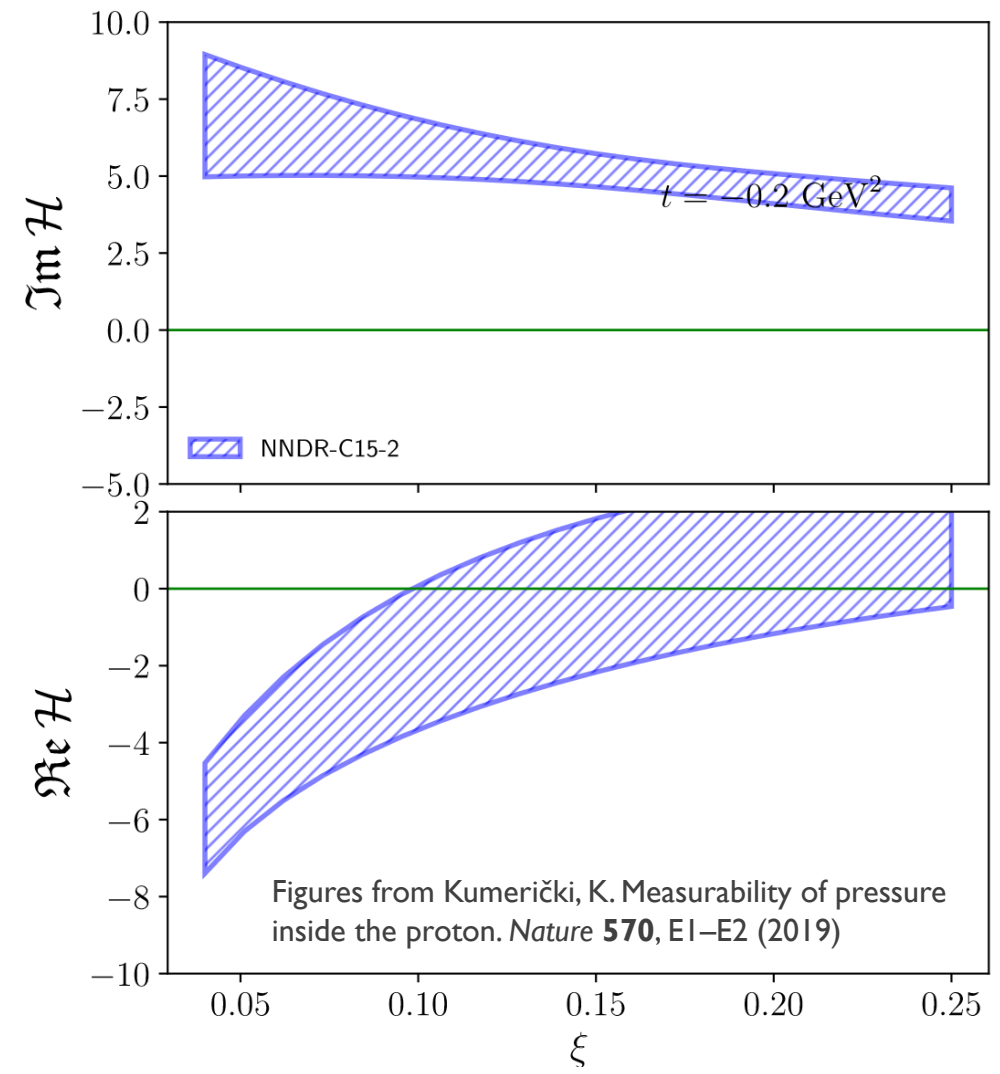
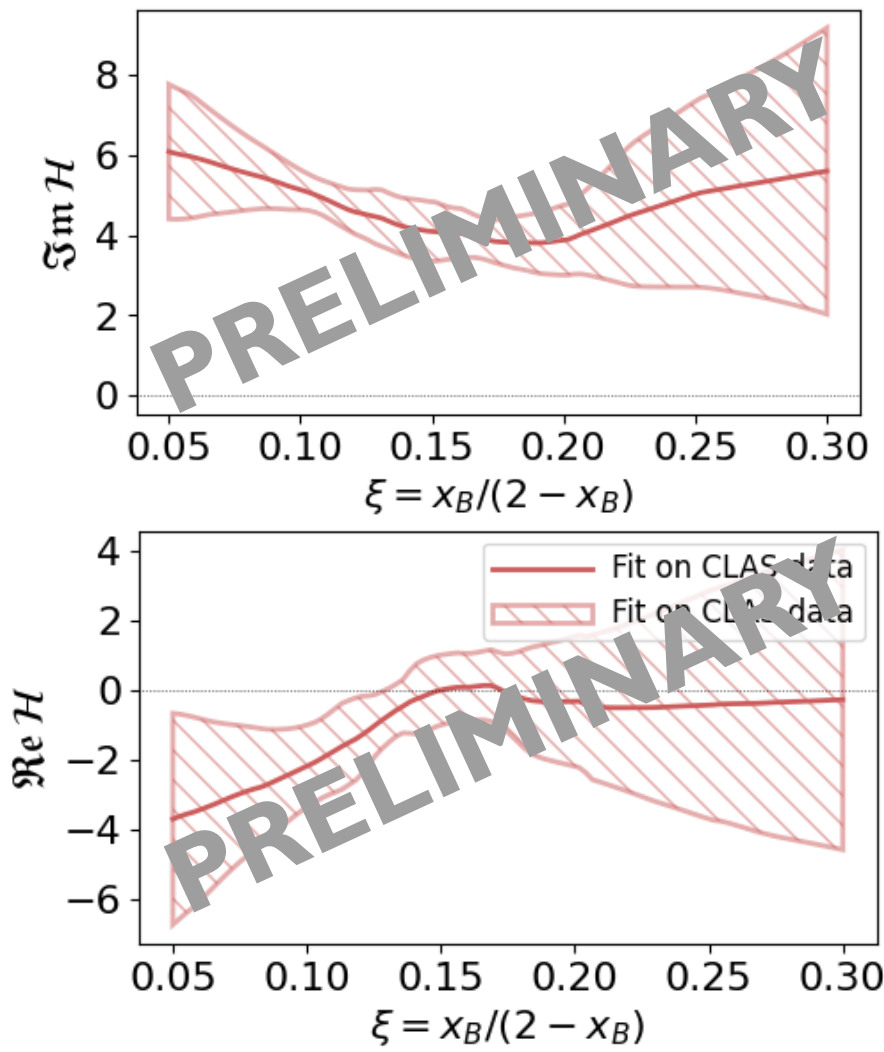
DVCS (un)polarized cross-section measured by the CLAS experiment



Measurement of Deeply Virtual Compton Scattering Beam-Spin Asymmetries
 F. X. Girod *et al.* (CLAS Collaboration)
 Phys. Rev. Lett. 100, 162002, 2008

Cross Sections for the Exclusive Photon Electroproduction on the Proton and Generalized Parton Distributions, H. S. Jo *et al.* (CLAS Collaboration) Phys. Rev. Lett. 115, 212003, 2015

Results of the fit



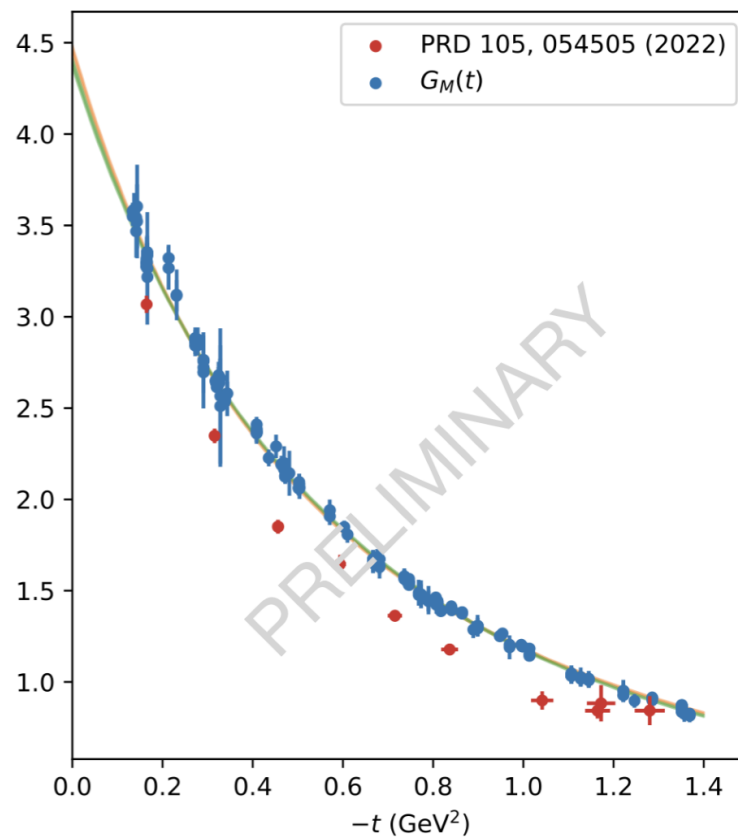
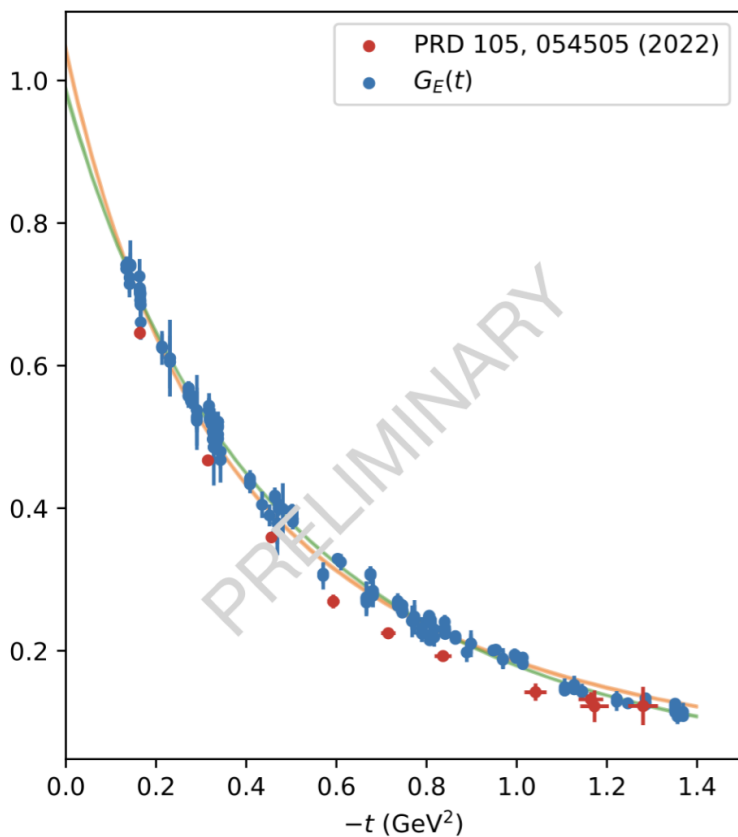
→ Qualitative good agreement, proof of concept to build upon

Input from LQCD

Material from H. Dutrieux – HadStruc Collaboration

- Extraction of EM FFs using the LQCD dataset which will be used for this work

$$\int_{-1}^1 dx H^q(x, \xi, t, \mu^2) = F_1^q(t) \quad \int_{-1}^1 dx E^q(x, \xi, t, \mu^2) = F_2^q(t)$$

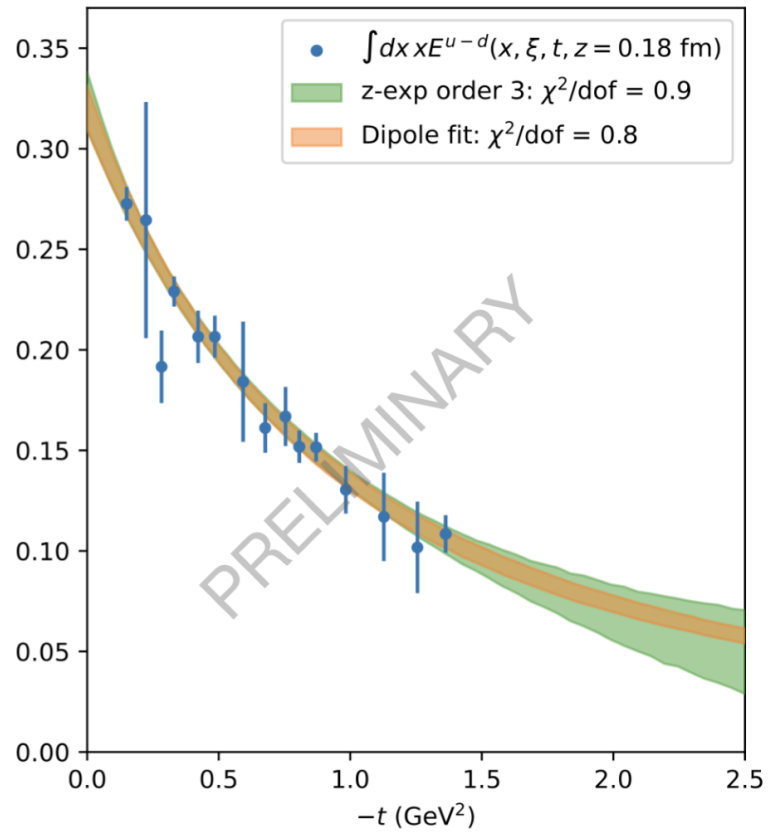
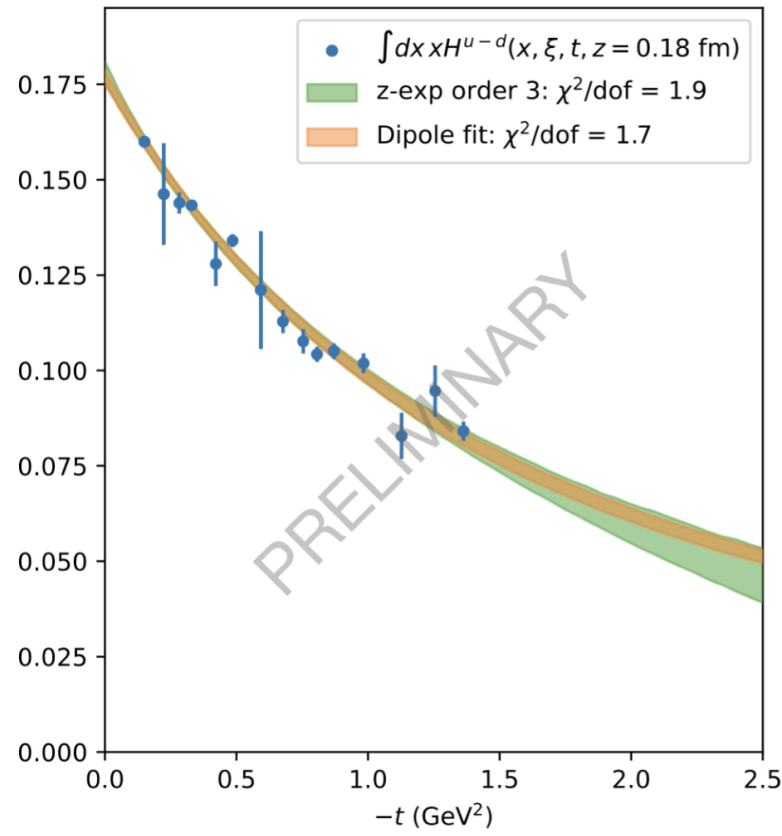


Input from LQCD

Material from H. Dutrieux – HadStruc Collaboration

- Using the same dataset, one can extract the integral of H
- So far only the “u-d” is extracted
- The obtained fit could be used as a constraint for the neural network

$$\int_{-1}^1 dx x H^q(x, \xi, t) = A^q(t) + \xi^2 D^q(t)$$



Future directions

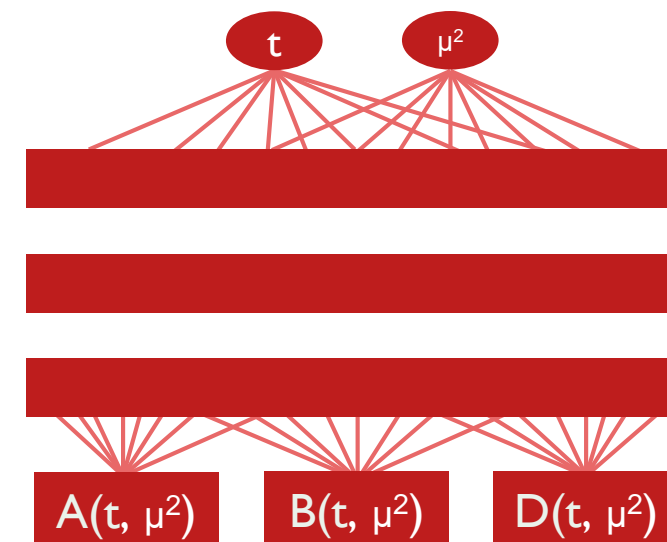
Next steps of the LDRD project

Lattice QCD computation of the GFFs

- Extract full GFFs A, B, D
- Provide parametrization for the NN approach (see below)

Fitting framework

- Implement NN architecture to extract GFFs
 - Adapt NN architecture
 - Test architecture dependence on extracted results
- Understand physical constraints (from LQCD, from EM FFs, from dispersion relation) and implement them (in the network architecture, in the loss function)



GPD database

- The goal is to fit all existing and future GPDs data.
- There is no unified common database storing these data (Partons and Gepard use ad-hoc DB).
- We have started implementing a DB format able to store both experimental data and LQCD data.
 - Involves many people across experiment and LQCD
- Based on JSON and planned to be hosted on Github.

Take-aways

- I Gravitational Form Factors, which describe mass and force distributions in the nucleon, are now at the center of the attention.
- II We are aiming at developing a versatile tool to extract these quantities. It will be based on Neural Networks and able to handle both experimental data points and input from LQCD.
- III We are building upon existing tools, aiming to use state-of-the-art widely available libraries.
- V We aim at providing a tool to test the impact of new data on the extraction of GFFs.**

DVCS observable with positrons