

Single-spin asymmetries in $e-p$ scattering with intermediate state resonances

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Positron Working Group Workshop

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Outline

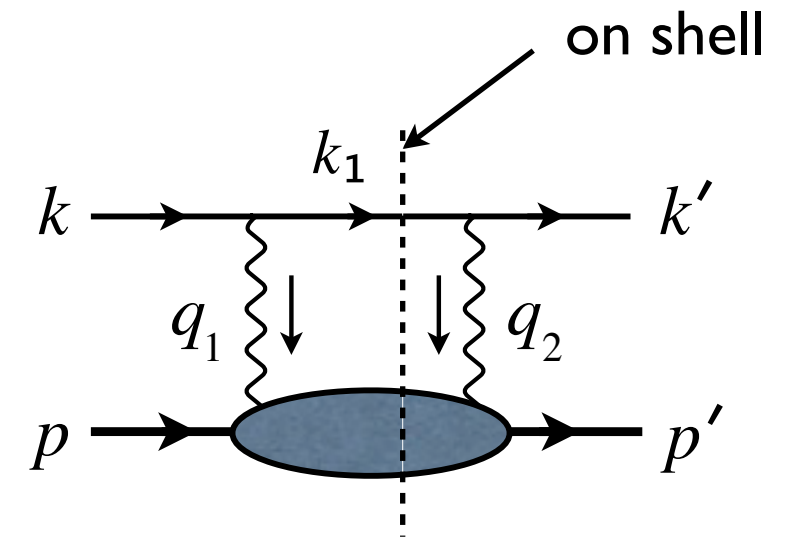
- Single spin asymmetries (SSA): beam normal B_n and target normal A_n cases: absorptive **imaginary** part of two-photon exchange (TPE)
 - What can we learn from B_n vs A_n ?
 - What are the prospects for measuring A_n at JLab?
- Relationship to TPE calculations for elastic $e-p$ scattering cross sections and the ratio G_E/G_M : dispersive **real** part of TPE
- Real and Imaginary parts connected by dispersion relations

Dispersive method

Unitarity \rightarrow

$$\text{Im}\langle f|\mathcal{M}|i\rangle \sim \sum_n \int dW_n dQ_1^2 dQ_2^2 \langle f|\mathcal{M}^*|n\rangle \langle n|\mathcal{M}|i\rangle$$

- Imaginary part determined by unitarity
- Uses only on-shell form factors (or helicity amplitudes), directly fit to data
- Real part determined from dispersion relations



- Resonance intermediate states:

$$\Delta(1232)3/2^+, N(1440)1/2^+, N(1520)3/2^-, N(1535)1/2^-, \\ \Delta(1620)1/2^-, N(1650)1/2^-, \Delta(1700)3/2^-, N(1710)1/2^+, N(1720)3/2^+$$

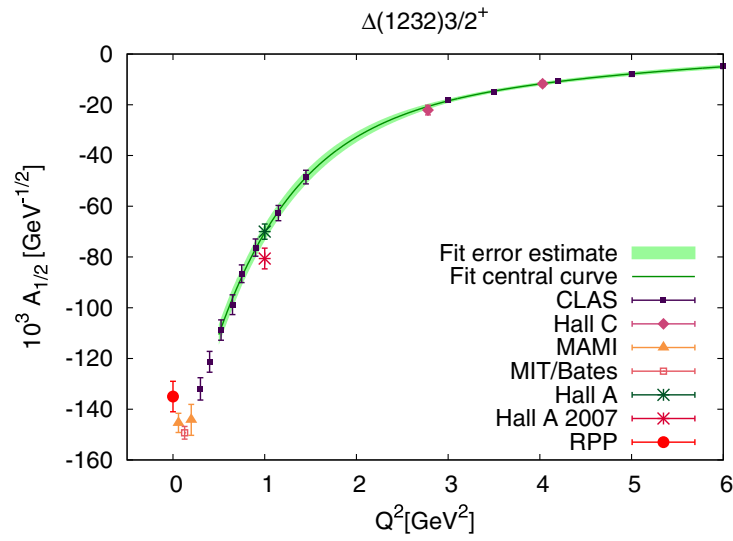
- Use CLAS exclusive meson electroproduction data for helicity amplitudes

$$A_{1/2}, A_{3/2}, S_{1/2}$$

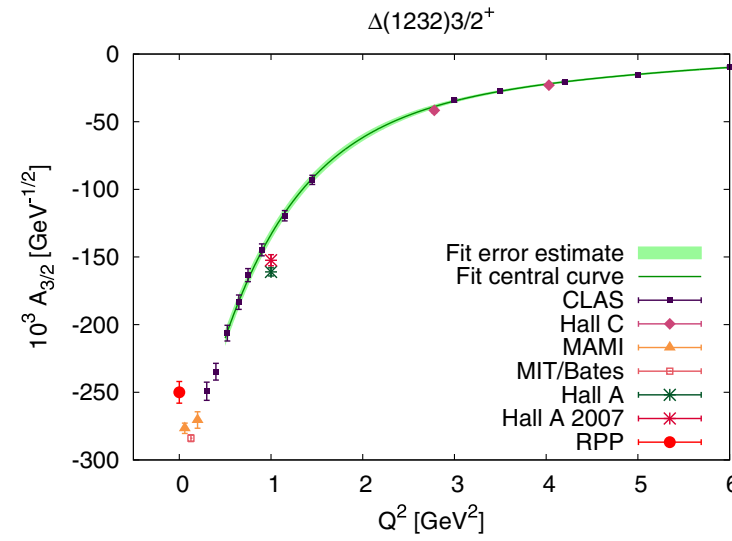
- Include Breit-Wigner lineshape

CLAS helicity amplitudes: examples of data

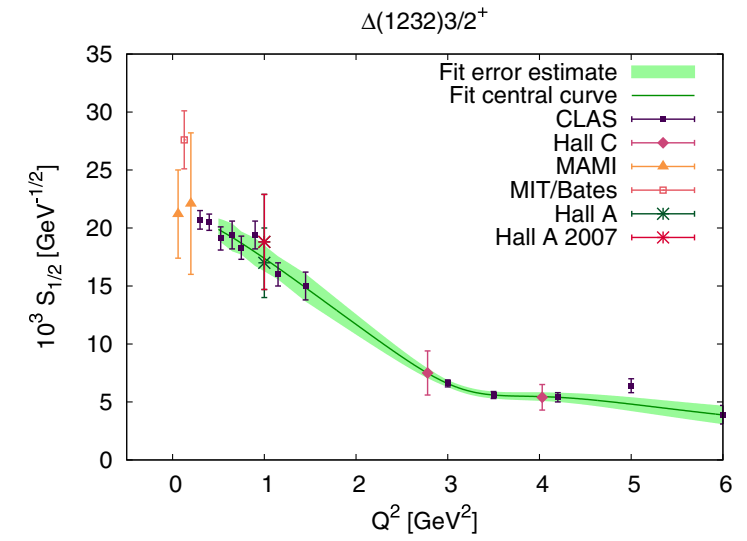
$\Delta(1232)$



(a)

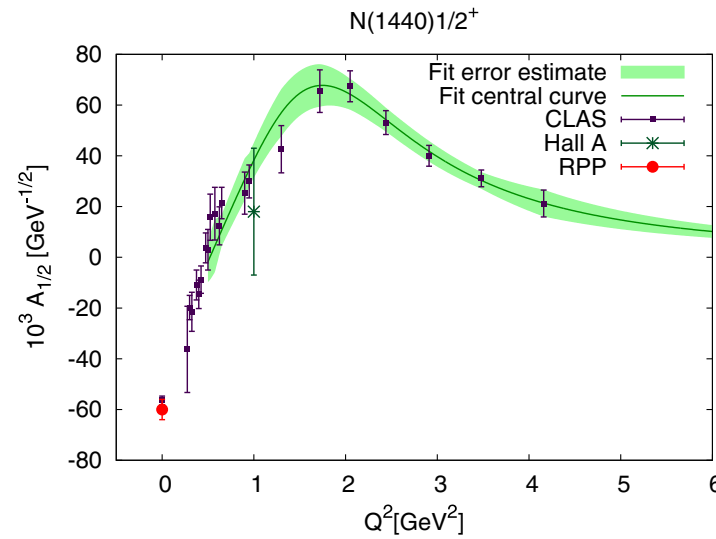


(b)

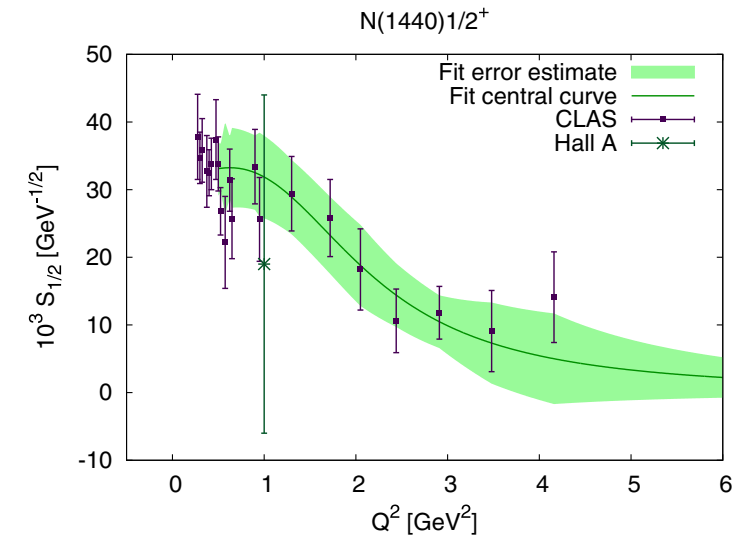


(c)

$N(1440)$



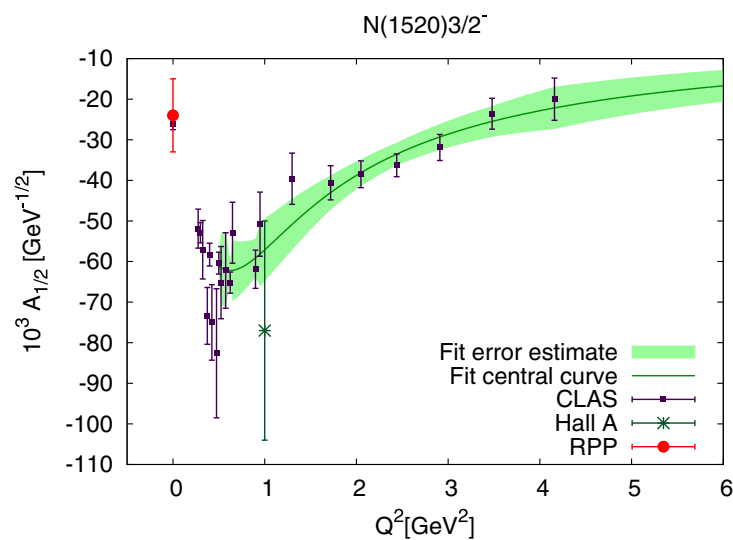
(d)



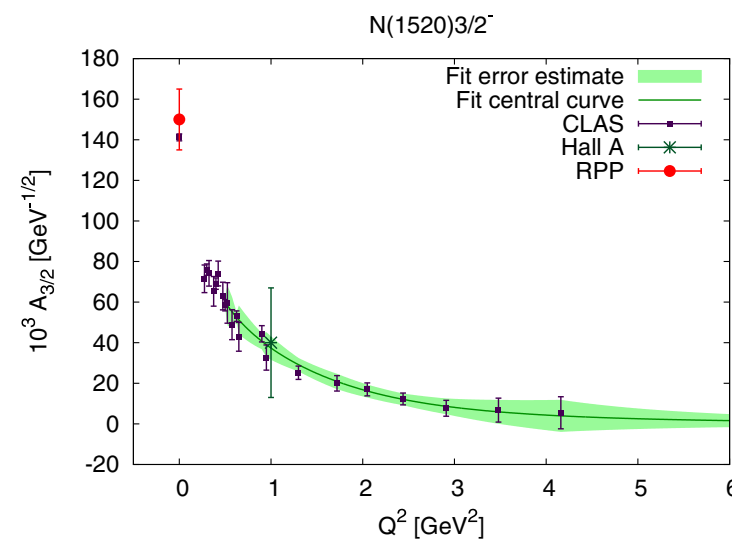
(e)

Hiller Blin *et al.*, PRC **100**, 035201 (2019)

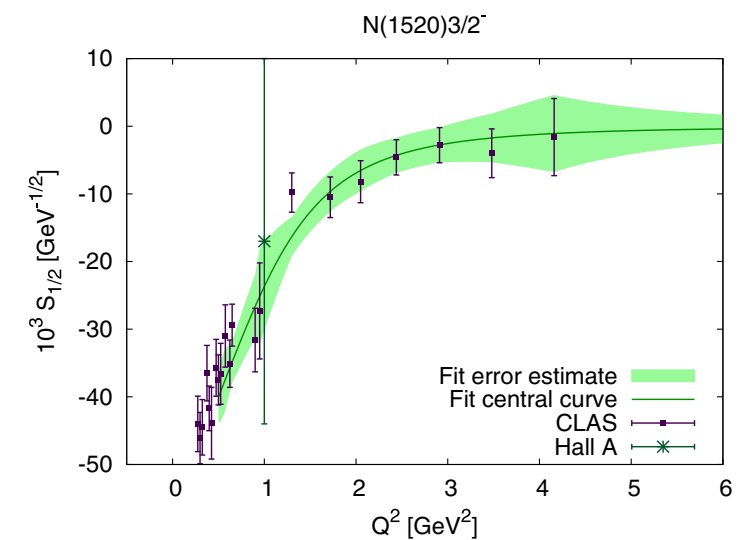
$N(1520)$



(f)

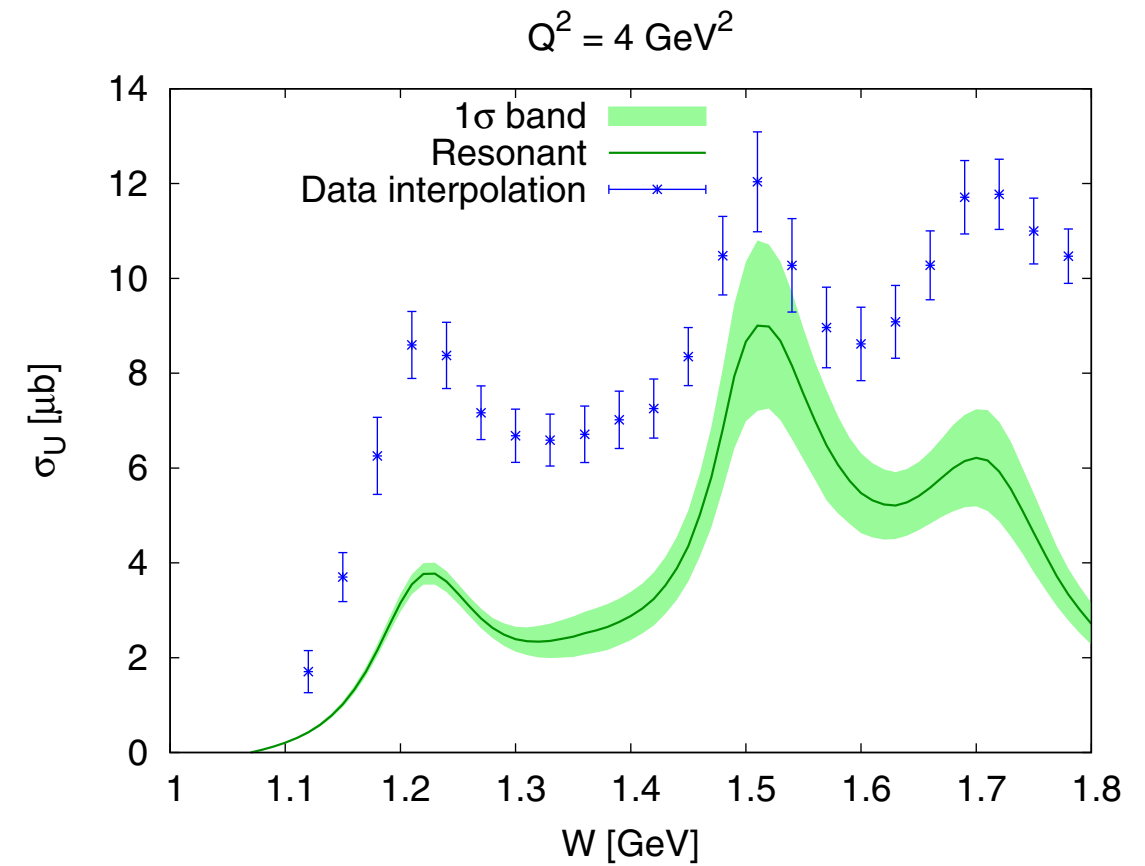
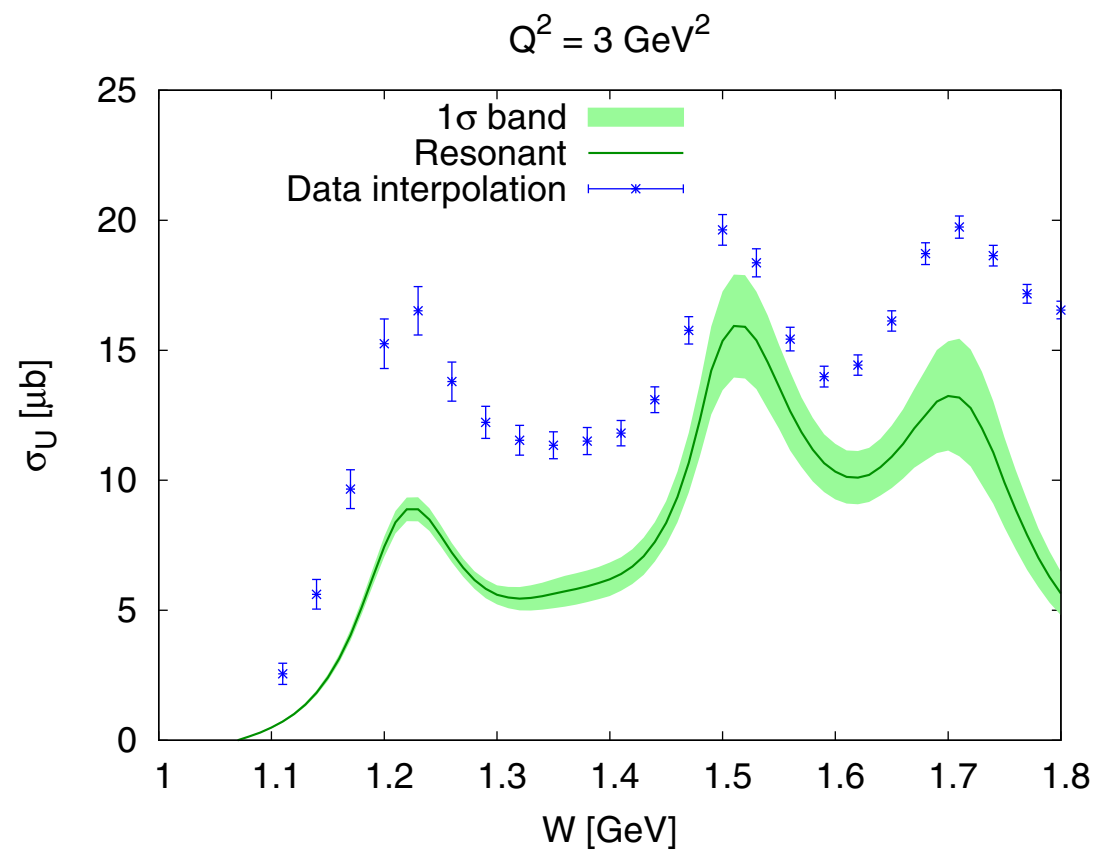
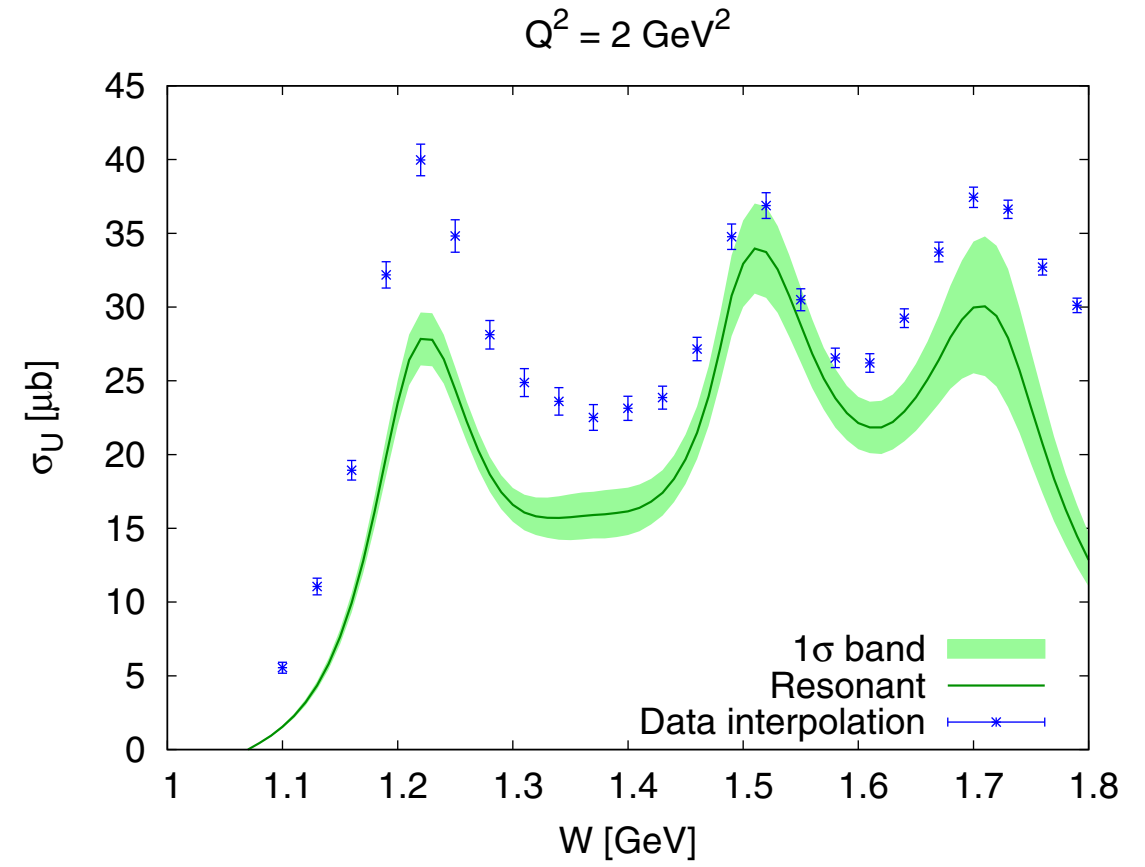
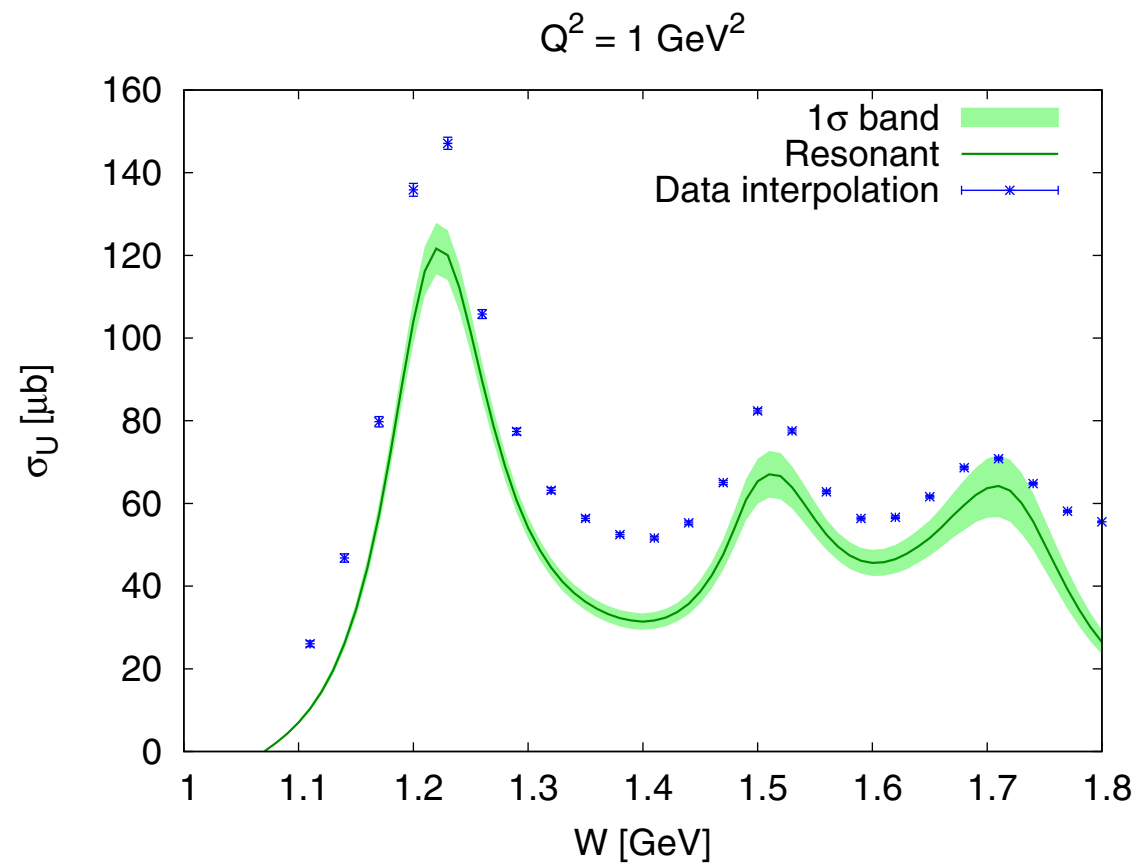


(g)



(h)

CLAS unpolarized cross sections vs W^2



- Resonant vs. Total cross section at increasing Q^2

TPE using dispersion relations

Generalized form factors

$$\mathcal{M}_{\gamma\gamma} \rightarrow (\gamma_\mu)^{(e)} \otimes \left(F'_1(Q^2, \nu) \gamma^\mu + F'_2(Q^2, \nu) \frac{i\sigma^{\mu\nu} q_\nu}{2M} \right)^{(p)} \\ + (\gamma_\mu \gamma_5)^{(e)} \otimes (G'_a(Q^2, \nu) \gamma^\mu \gamma_5)^{(p)}$$

Dispersion relations

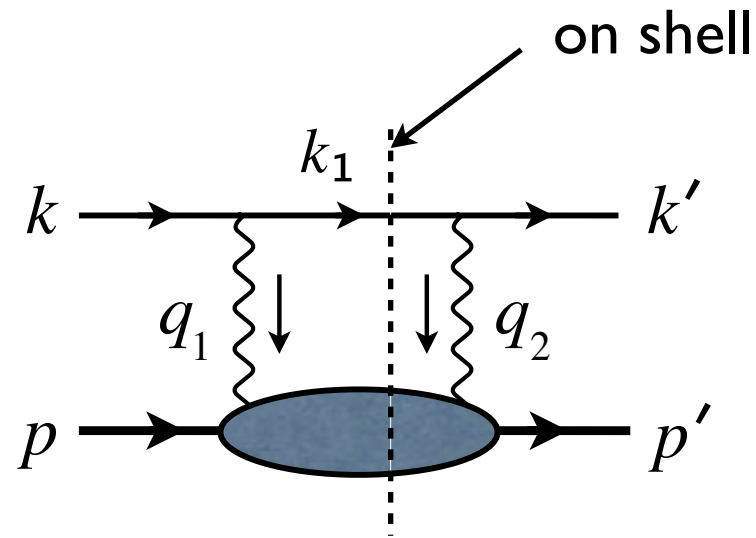
$$\text{Re } F'_1(Q^2, \nu) = \frac{2}{\pi} \mathcal{P} \int_{-\tau}^{\infty} d\nu' \frac{\nu}{\nu'^2 - \nu^2} \text{Im } F'_1(Q^2, \nu'),$$

$$\text{Re } F'_2(Q^2, \nu) = \frac{2}{\pi} \mathcal{P} \int_{-\tau}^{\infty} d\nu' \frac{\nu}{\nu'^2 - \nu^2} \text{Im } F'_2(Q^2, \nu'),$$

$$\text{Re } G'_a(Q^2, \nu) = \frac{2}{\pi} \mathcal{P} \int_{-\tau}^{\infty} d\nu' \frac{\nu'}{\nu'^2 - \nu^2} \text{Im } G'_a(Q^2, \nu').$$

Integral extends into “unphysical region” down to zero energy ($\cos \theta < -1$)

Direct measurements of Im part



This is all in the physical region.

Beam normal spin asymmetry: additional dependence on spin-flip FFs

$$B_n = -\frac{m_e}{M} \sqrt{2\epsilon(1-\epsilon)(1+\tau)} \frac{1}{\sigma_R} \text{Im} \{ -G_M G'_a + G_E F'_4 + \nu F_1 F'_5 \}$$

Target normal spin asymmetry: same generalized FFs as cross section

$$A_n = \sqrt{2\epsilon(1+\epsilon)\tau} \frac{1}{\sigma_R} \text{Im} \left\{ -G_M (F'_1 - \tau F'_2) + G_E \left(F'_1 + F'_2 + \frac{1+\tau}{\nu} G'_a \right) \right\}$$

Probe different aspects of TPE!

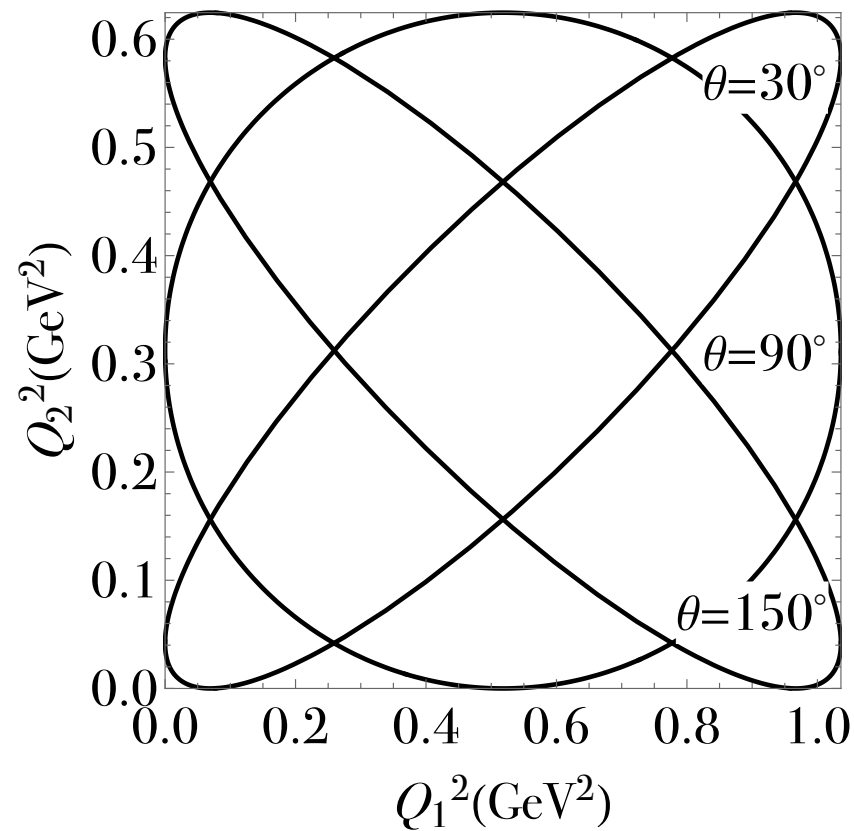
TPE correction to cross section:

$$\delta_{\gamma\gamma} = \frac{1}{\sigma_R} \text{Re} \{ \epsilon G_E (F'_1 - \tau F'_2) + G_M (\tau (F'_1 + F'_2) + \nu(1-\epsilon) G'_a) \}$$

Ingredients of the calculation

$$SSA = - \frac{\alpha Q^2}{\pi D(s, Q^2)} \int_{M^2}^{W_{\max}^2} dW^2 \frac{|\vec{k}_1|}{4\sqrt{s}} \int_{-1}^1 d\cos\theta_{k_1} \int_0^{2\pi} d\phi_{k_1} \frac{\text{Im } L_{\rho\mu\nu} H^{\rho\mu\nu}}{Q_1^2 Q_2^2}.$$

Kinematic bounds on Q_1^2 and Q_2^2



$$Q_1^2 \simeq 0, Q_2^2 \neq 0$$

$$\downarrow$$

$$k // k_1$$

$$Q_1^2 \neq 0, Q_2^2 \simeq 0$$

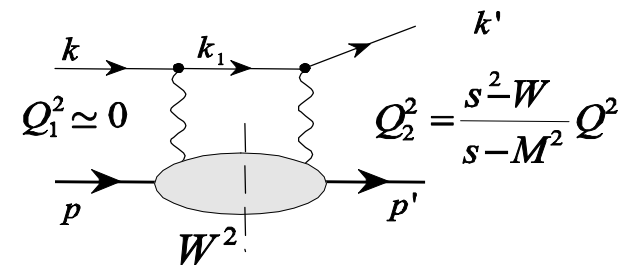
$$\downarrow$$

$$k_1 // k'$$

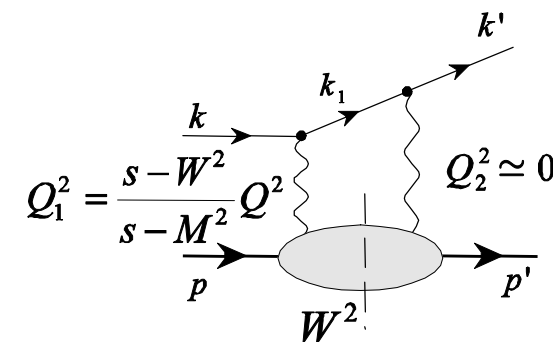
$$Q_1^2 \simeq 0, Q_2^2 \simeq 0$$

$$\downarrow$$

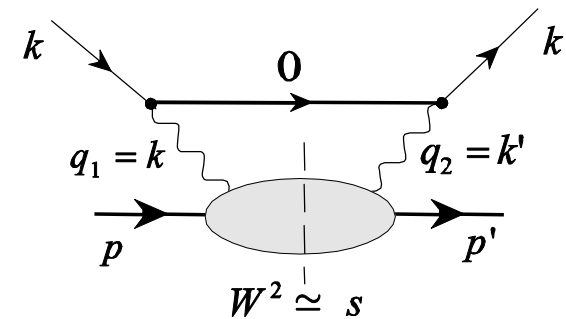
$$k_1 = 0, W = \sqrt{s} - m_e$$



Quasi - VCS



Quasi - VCS



Quasi - RCS

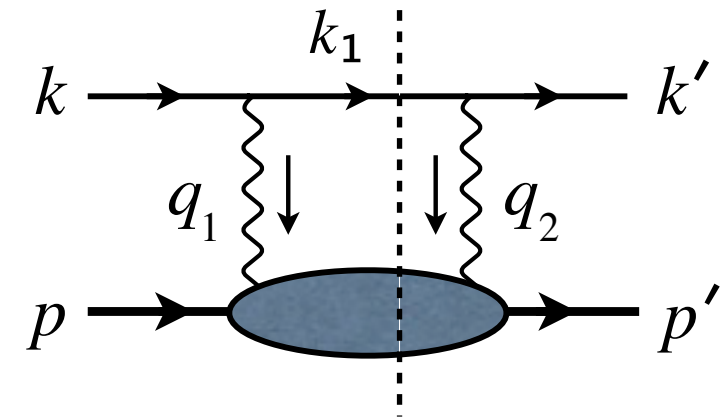
Kinematic enhancement for QRCS in B_n

- Pasquini & Vanderhaeghen (2004)
- Afanasev & Merenkov (2004)

Quasi-Real Compton Scattering (QRCS)

$$SSA = - \frac{\alpha Q^2}{\pi D(s, Q^2)} \int_{M^2}^{W_{\max}^2} dW^2 \frac{|\vec{k}_1|}{4\sqrt{s}} \int_{-1}^1 d\cos\theta_{k_1} \int_0^{2\pi} d\phi_{k_1} \frac{\text{Im} L_{\rho\mu\nu} H^{\rho\mu\nu}}{Q_1^2 Q_2^2}.$$

- Quasi-singular behaviour as $W \rightarrow W_{\max}$
- Two hard collinear photons
- Analogous to real Compton scattering



$$W_{\max} = \sqrt{s} - m_e, \quad E_{k_1} = m_e, \quad |\vec{k}_1| = 0$$

$$\text{At } W = W_{\max} : \quad Q_1^2 = Q_2^2 = m_e \frac{W_{\max}^2 - M^2}{\sqrt{s}}$$

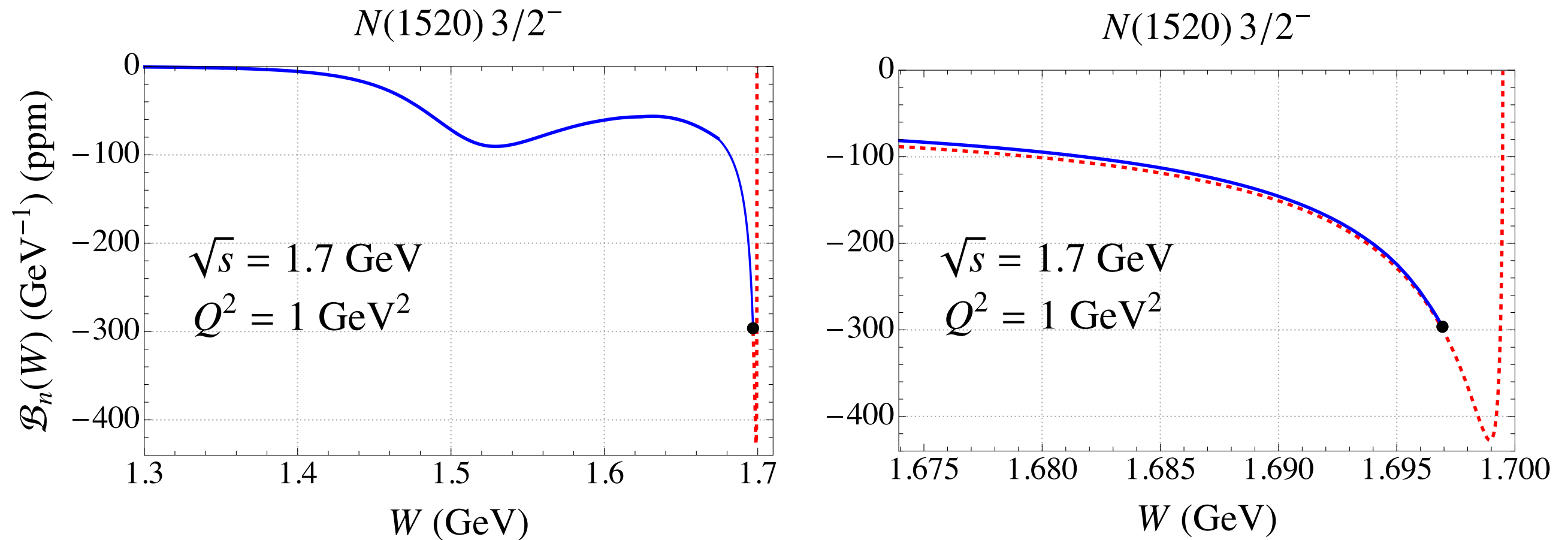
- Slowly varying numerator and rapidly varying denominator for $W \sim W_{\max}$
- **Strategy:** numerator evaluated at $Q_1^2 = Q_2^2 = 0$ times

$$\frac{|\vec{k}_1|}{4\sqrt{s}} \int d\Omega_{k_1} \frac{1}{Q_1^2 Q_2^2}$$

- This integral can be done analytically.
- Match to numerical solution for W below W_{\max}

Quasi-Real Compton Scattering (QRCS)

Example above nominal threshold for N(1520)

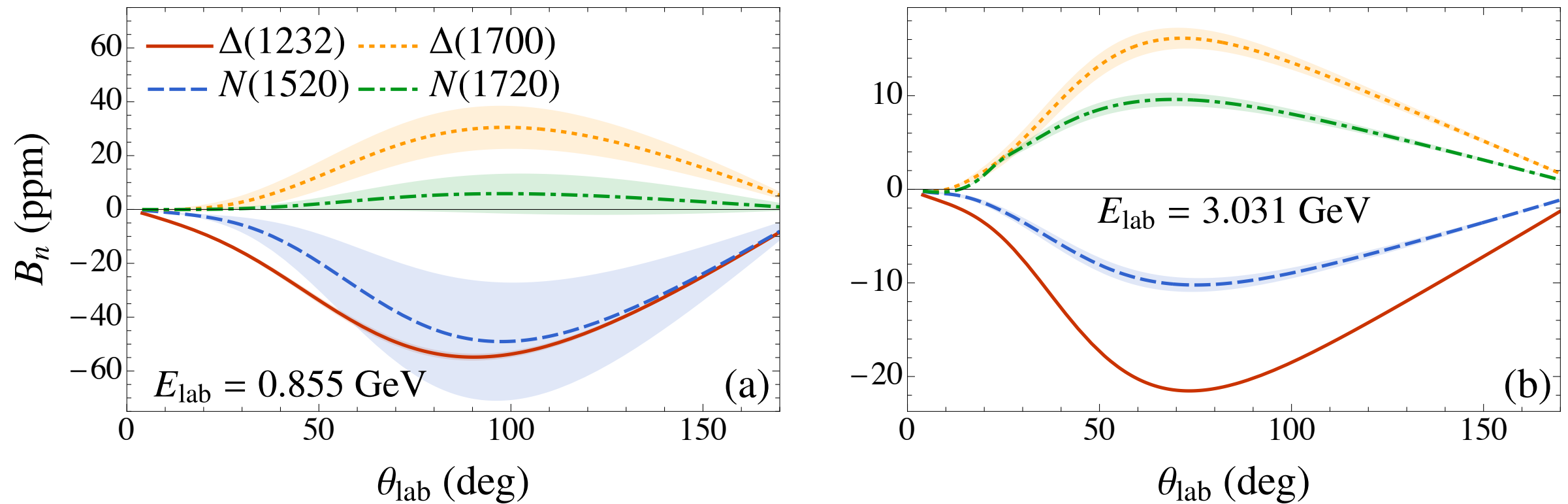


$$B_n = \int_{W_{\text{th}}}^{W_{\text{max}}} dW \mathcal{B}_n(W)$$

Match to numerical solution at $W^2 = \sqrt{s} - 5m_e$

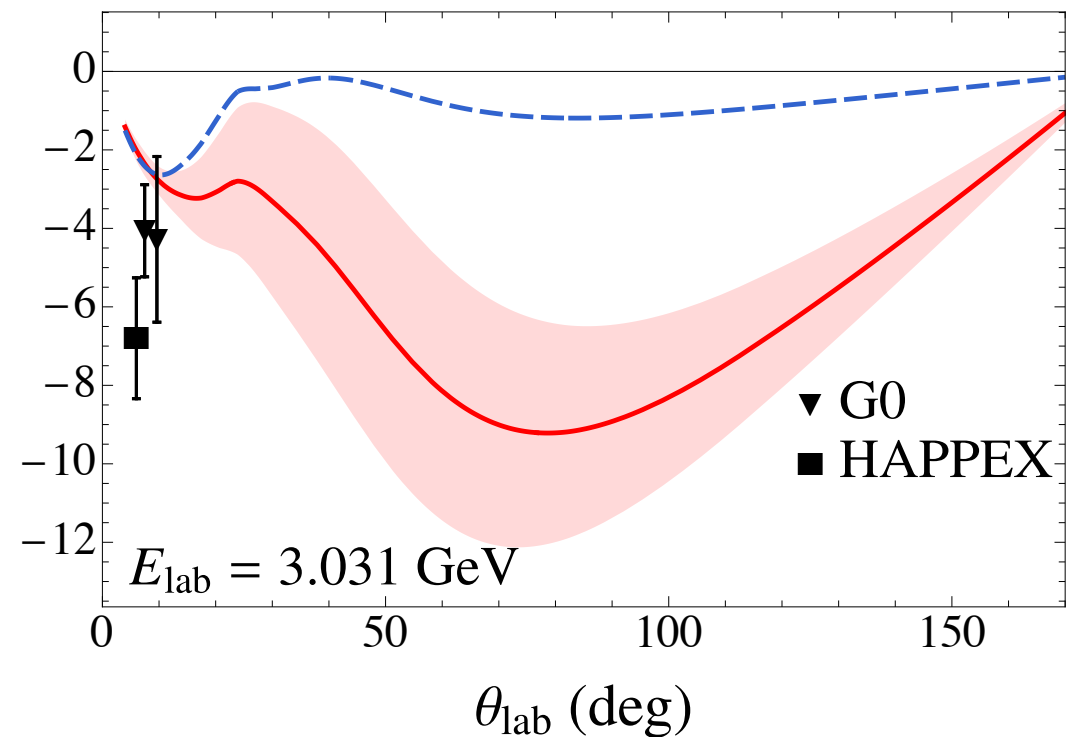
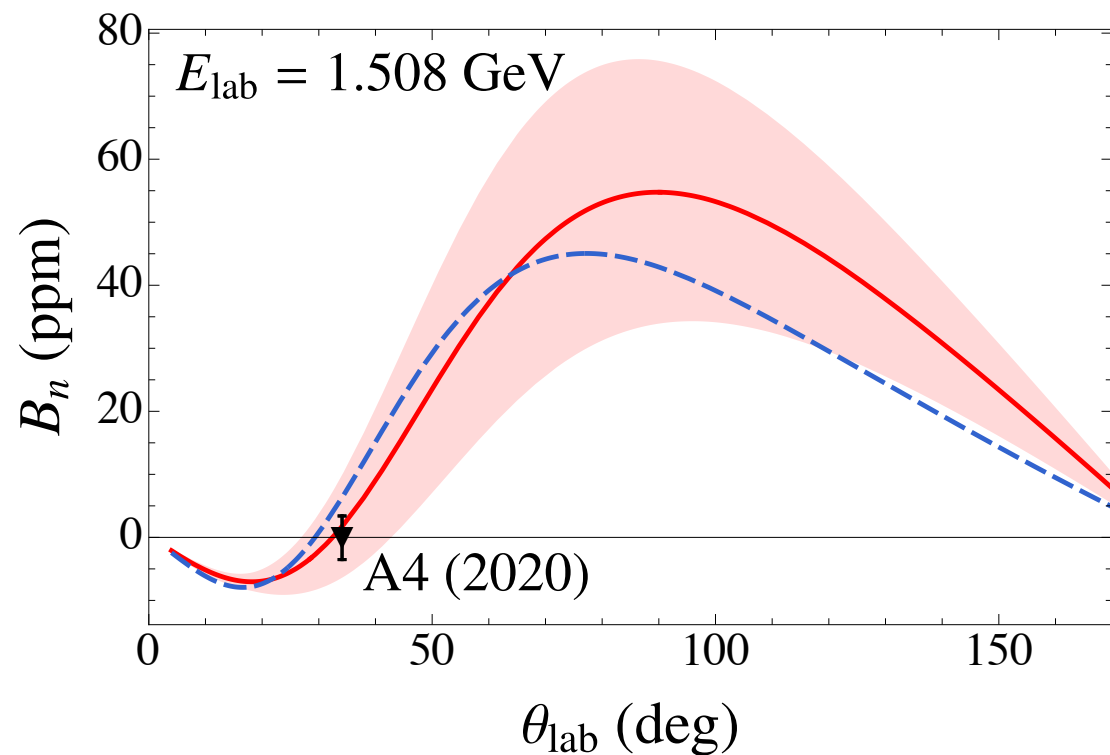
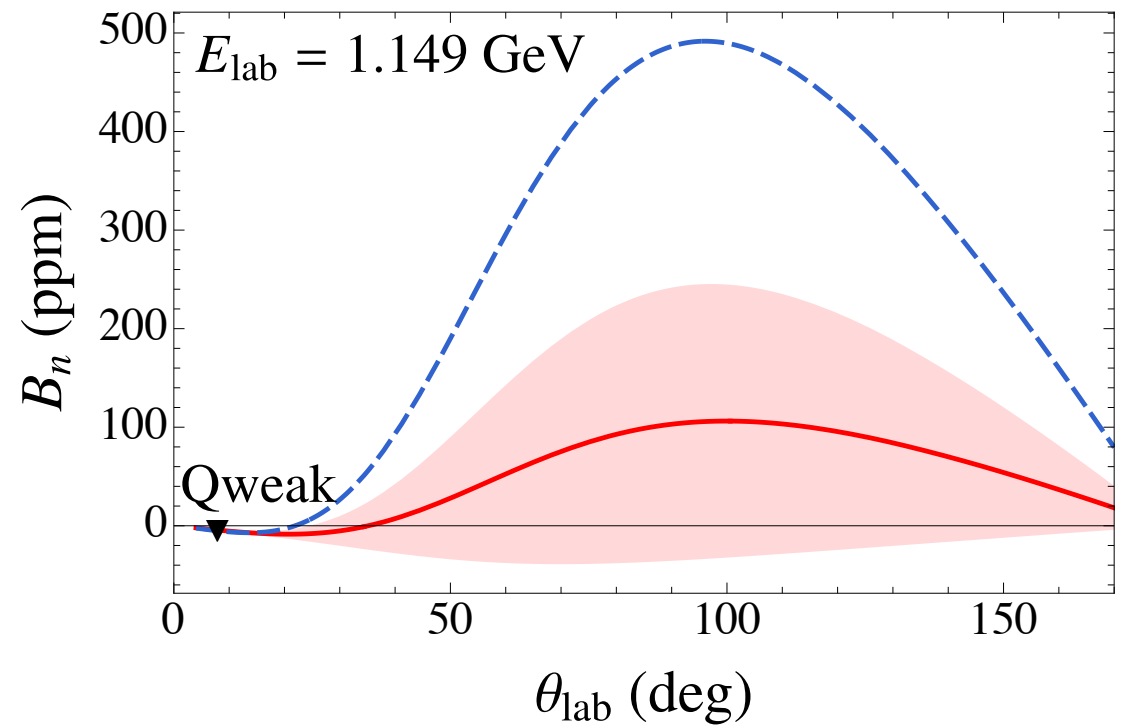
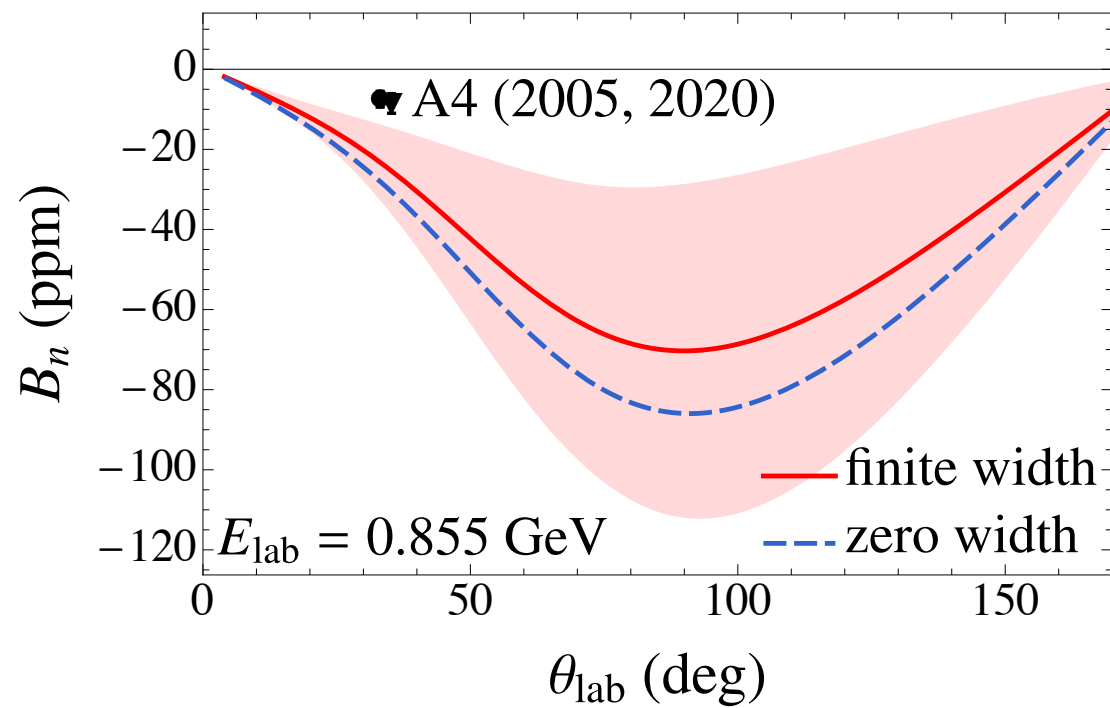
Beam normal SSA: fixed E vs θ

Ahmed, Blunden, Melnitchouk, PRC **108**, 055202, (2023)



- Individual contributions from four largest spin 3/2 resonances
- Decreases as E increases
- Spin 1/2 contributions suppressed by an order of magnitude
- Significant cancellation between positive parity ($\Delta(1232)$, $N(1520)$) and negative parity ($\Delta(1700)$, $N(1720)$) resonances

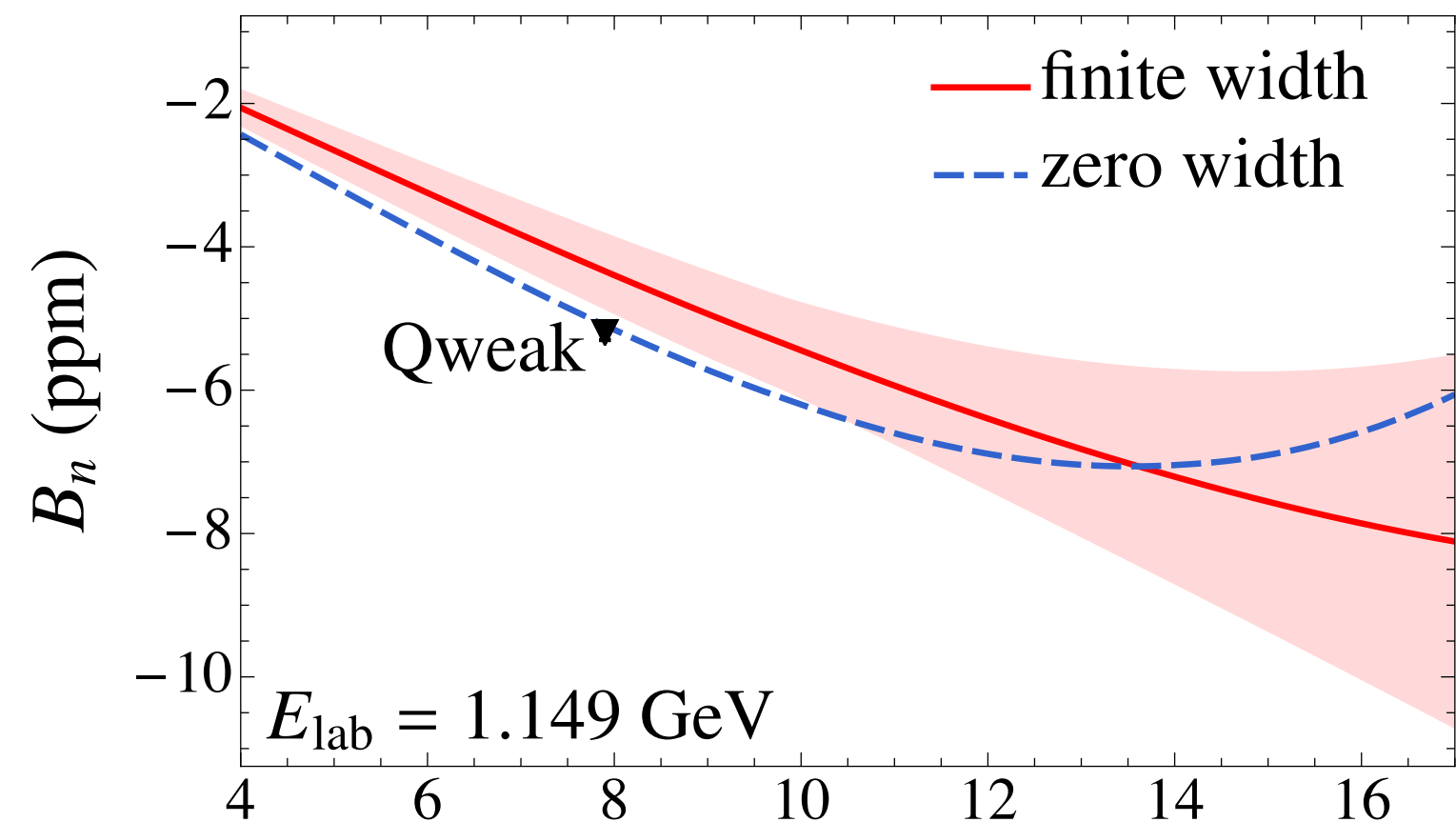
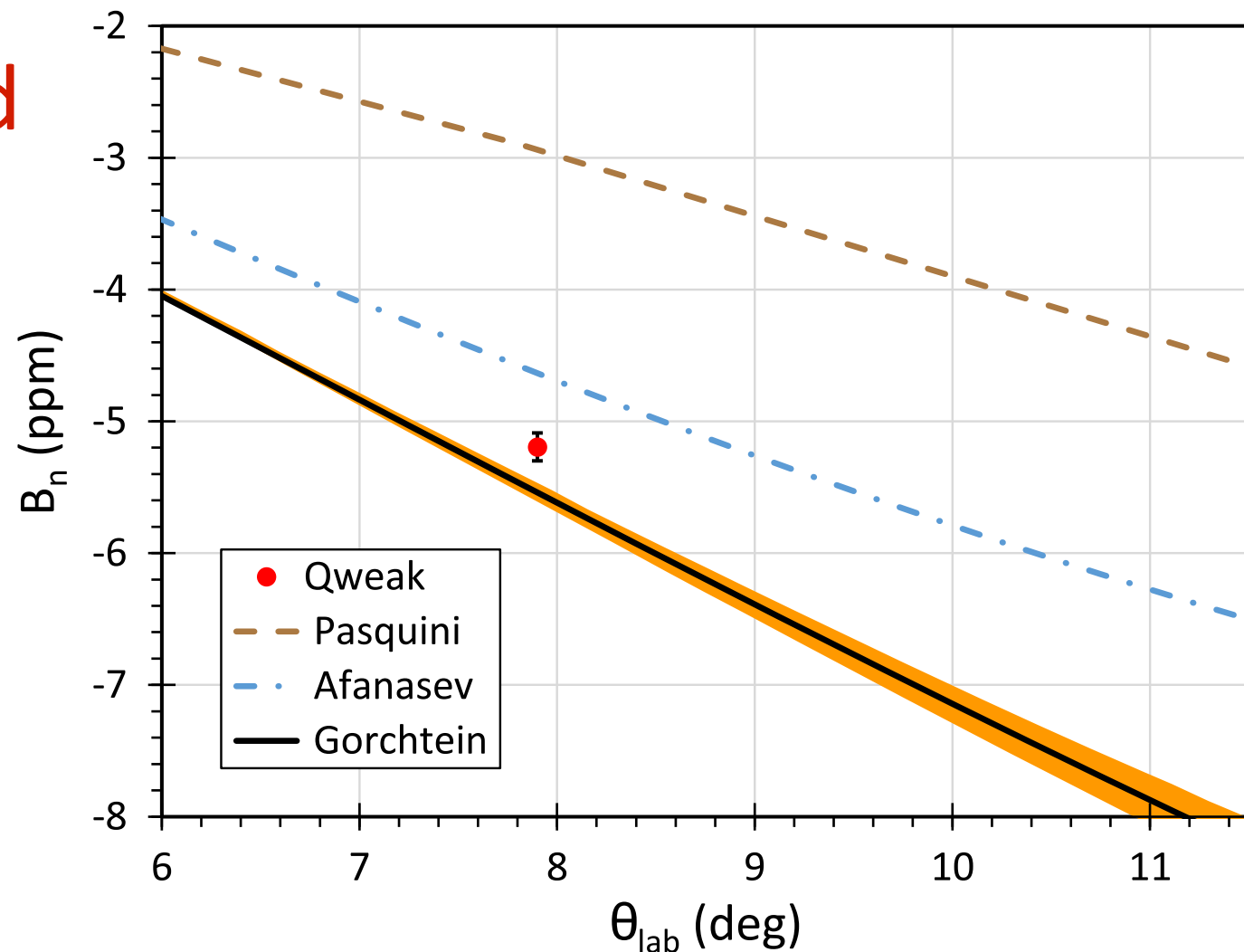
Beam normal SSA: fixed E vs θ



- Tends to overshoot data at low energies and forward angles
- Tends to undershoot data at high energies and forward angles

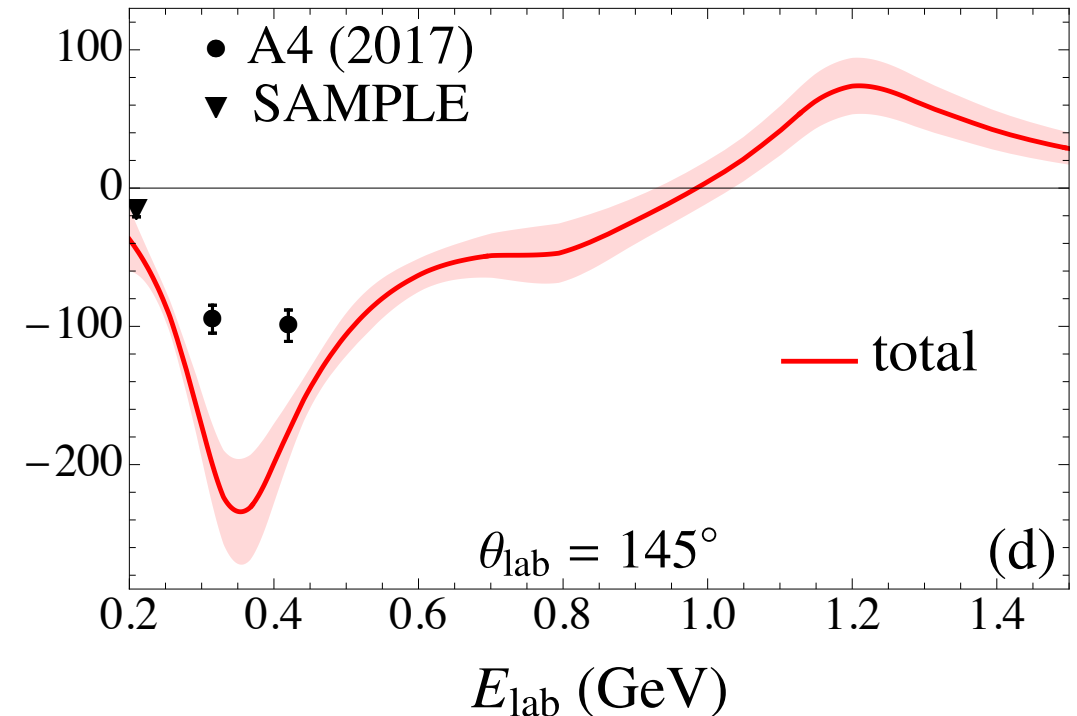
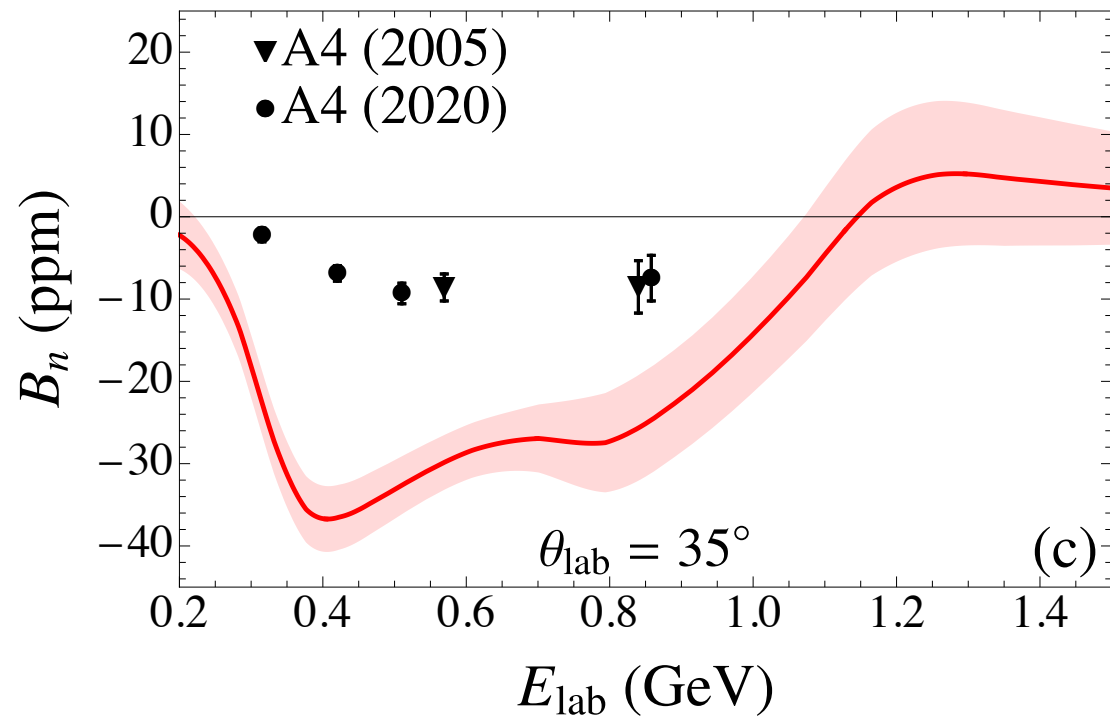
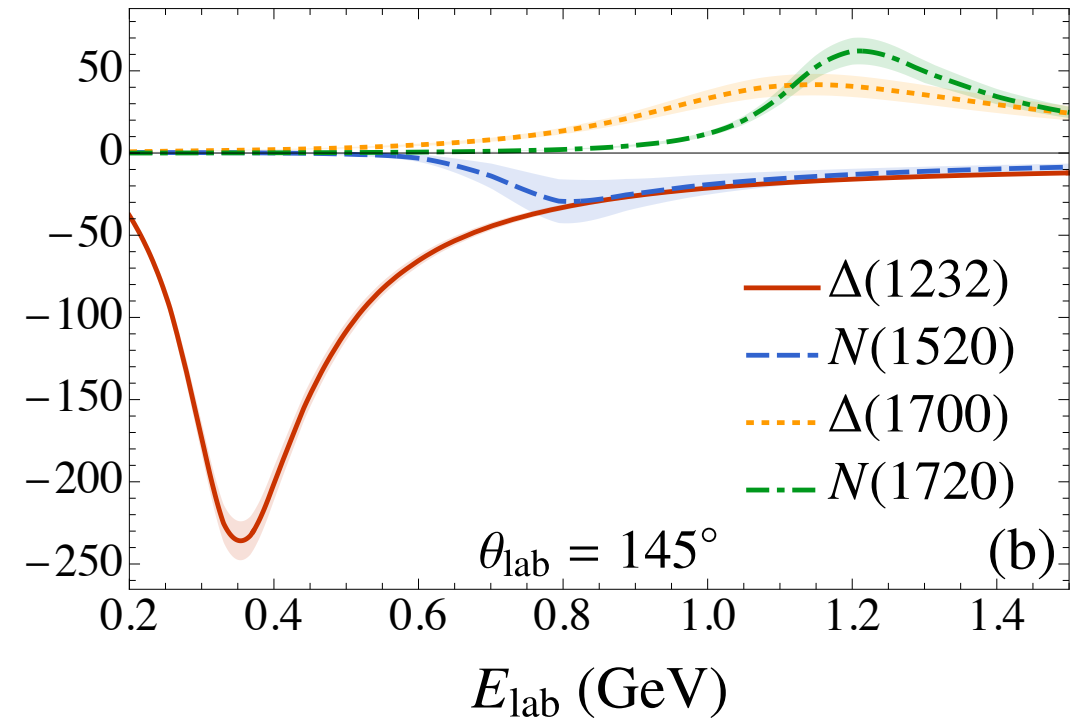
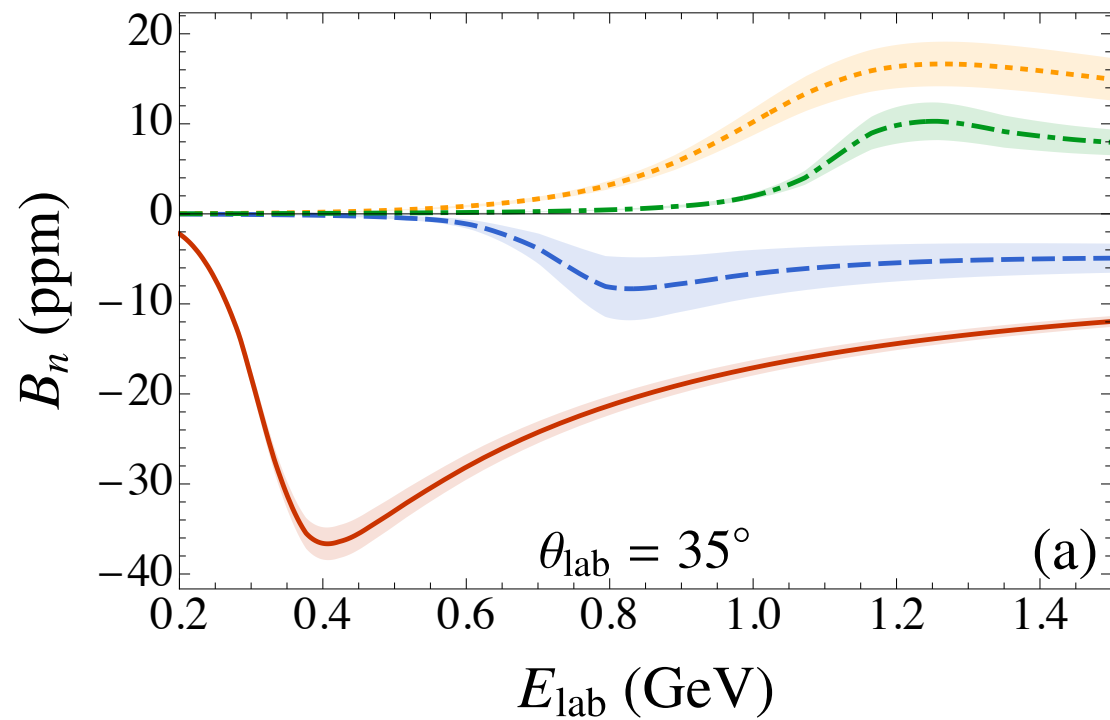
Qweak data point magnified

- Afanasev & Merenkov (2004)
- Pasquini & Vanderhaeghen (2004)
- Gorchtein (2006)

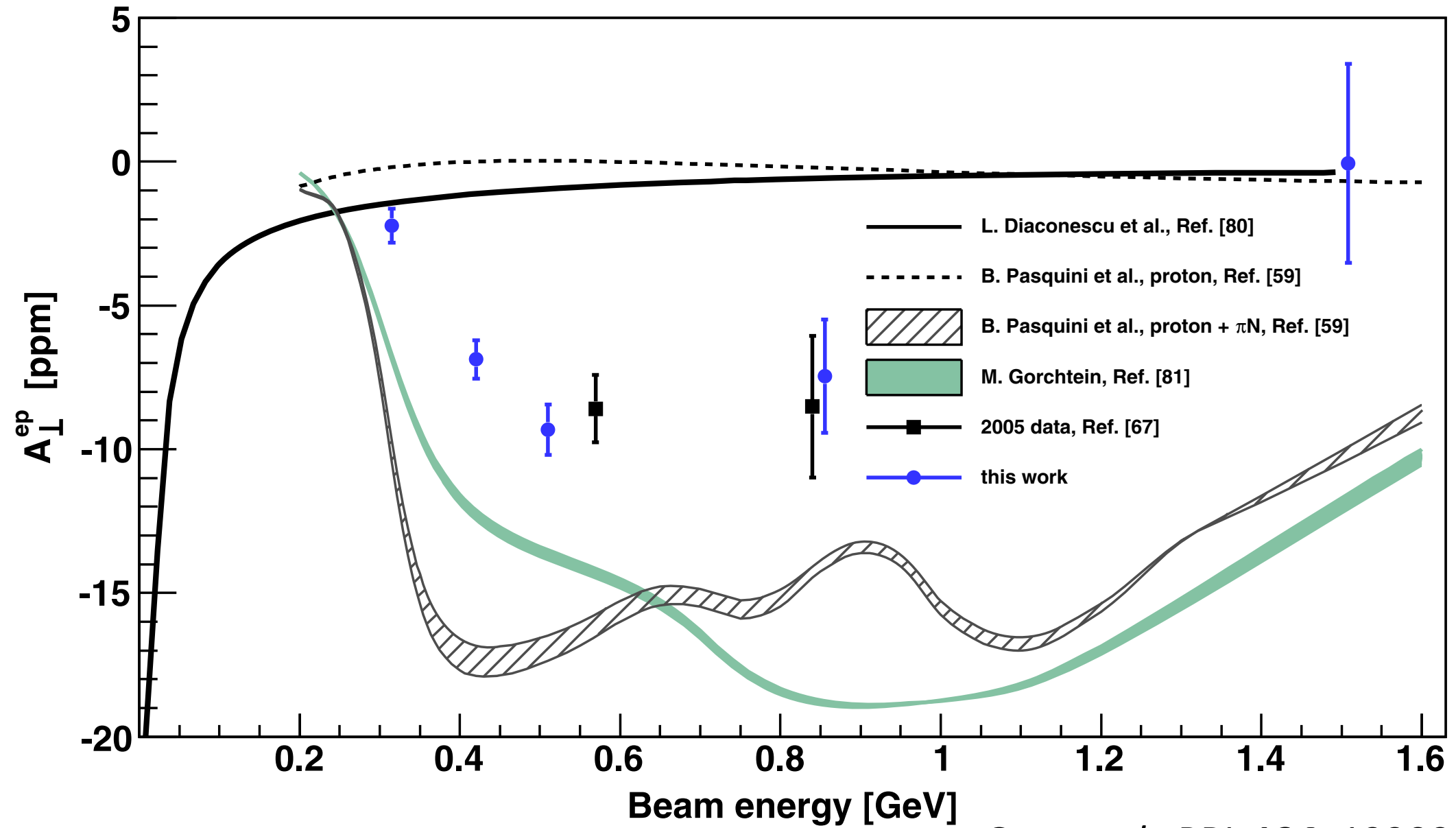


- Comparable with Afanasev and Gorchtein results
- Data point provides strong constraint on theory

Beam normal SSA: fixed θ vs E



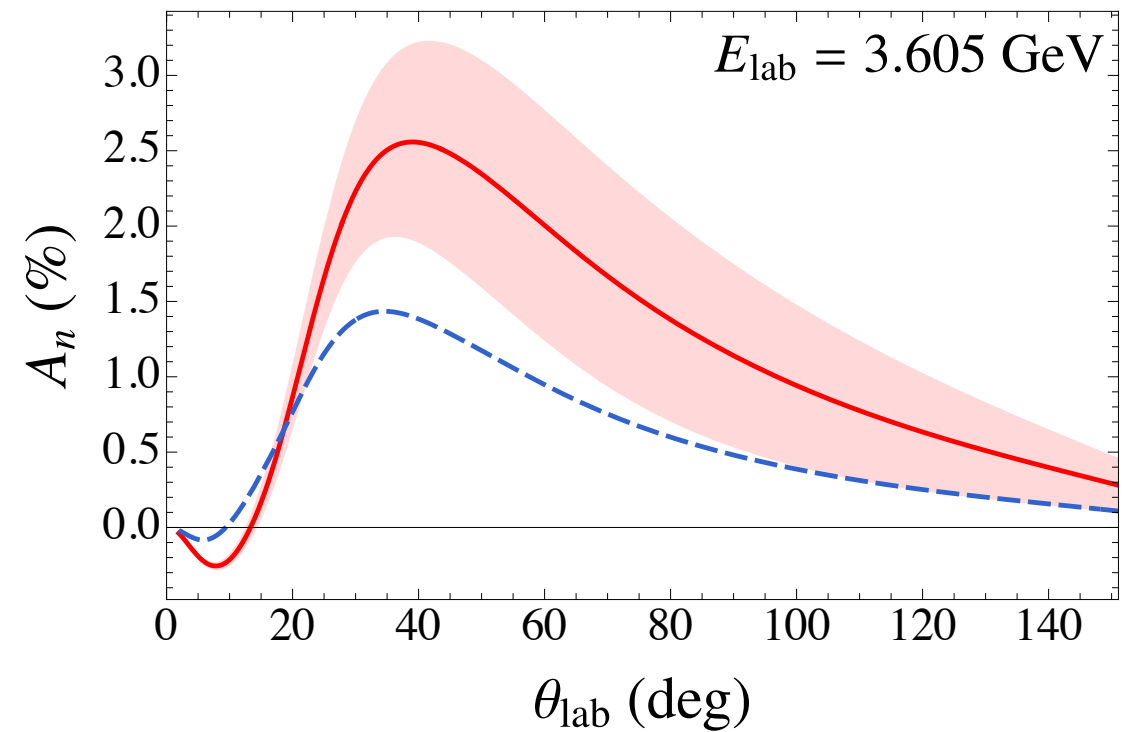
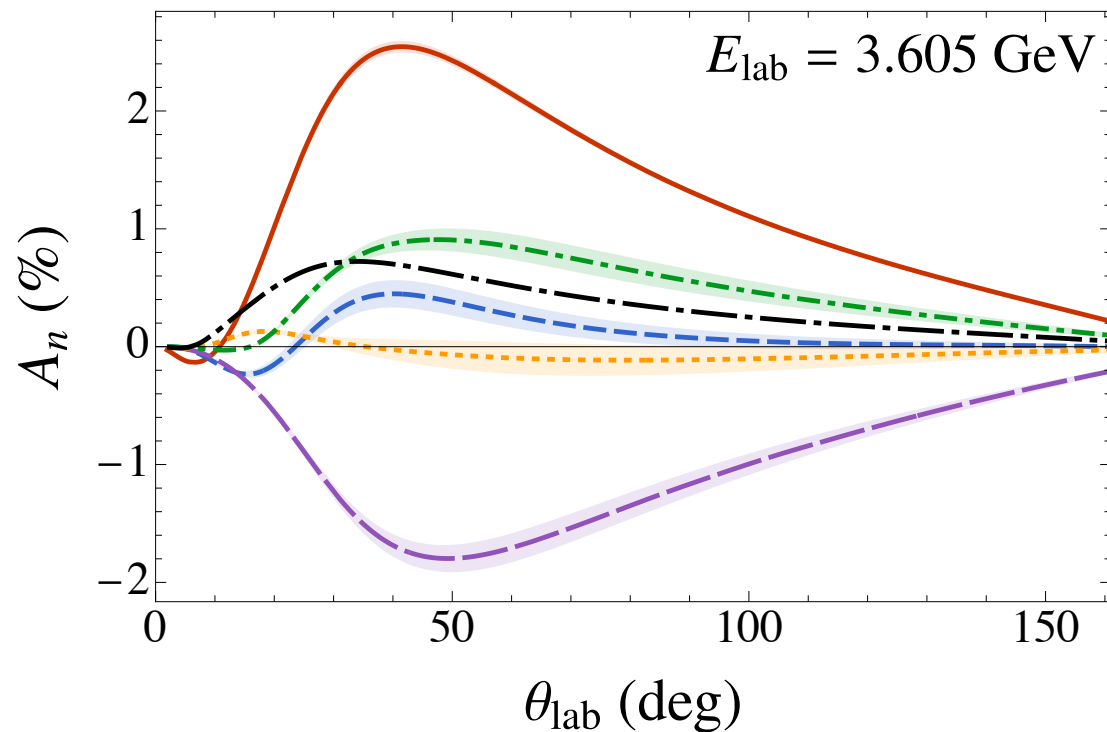
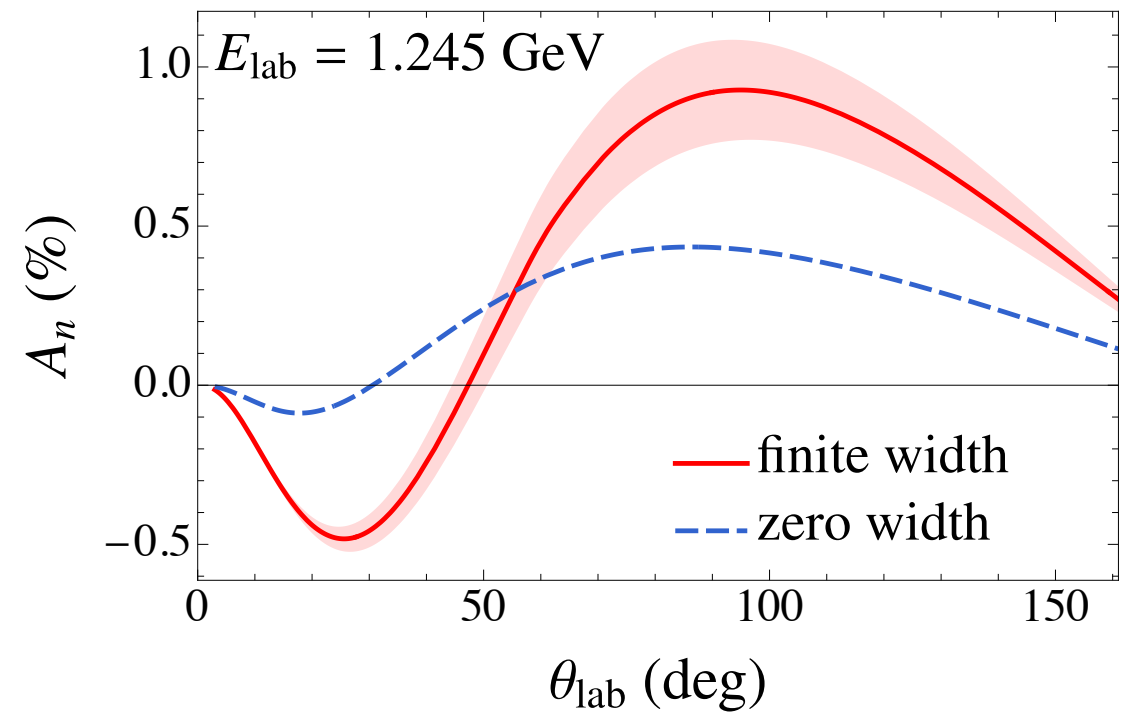
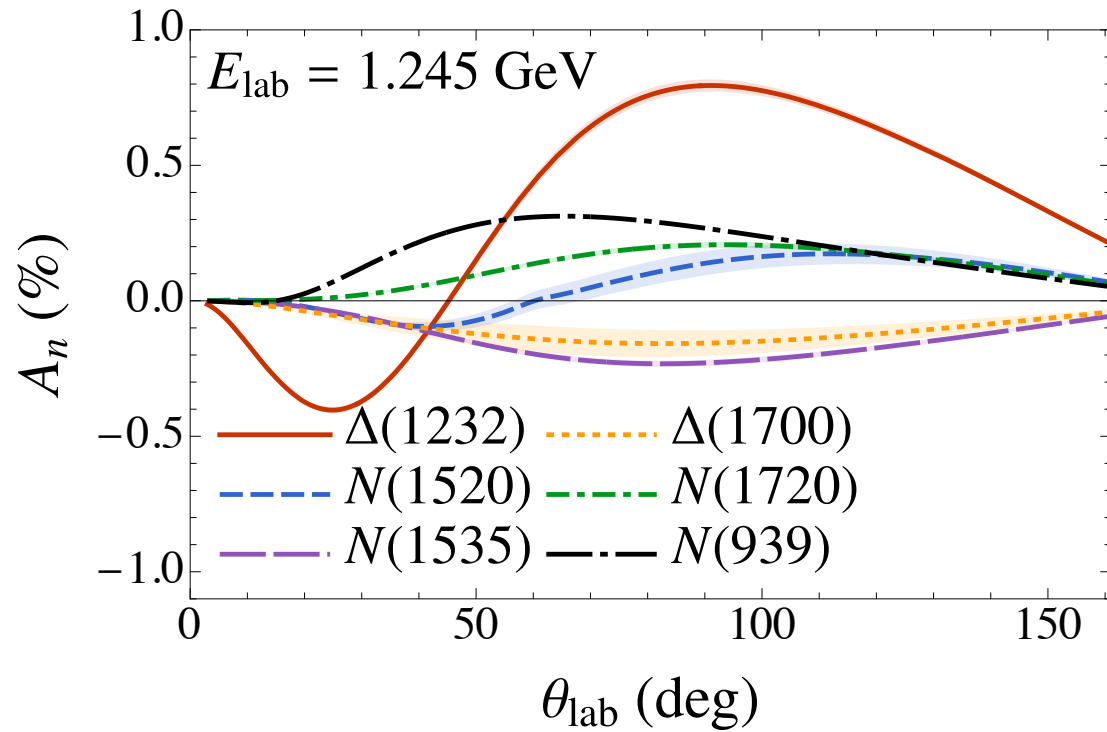
- Nominal threshold energy is at resonance peak in top row
- Tends to overshoot data in subthreshold region (low E)



Guo *et al.*, PRL **124**, 122003 (2020)

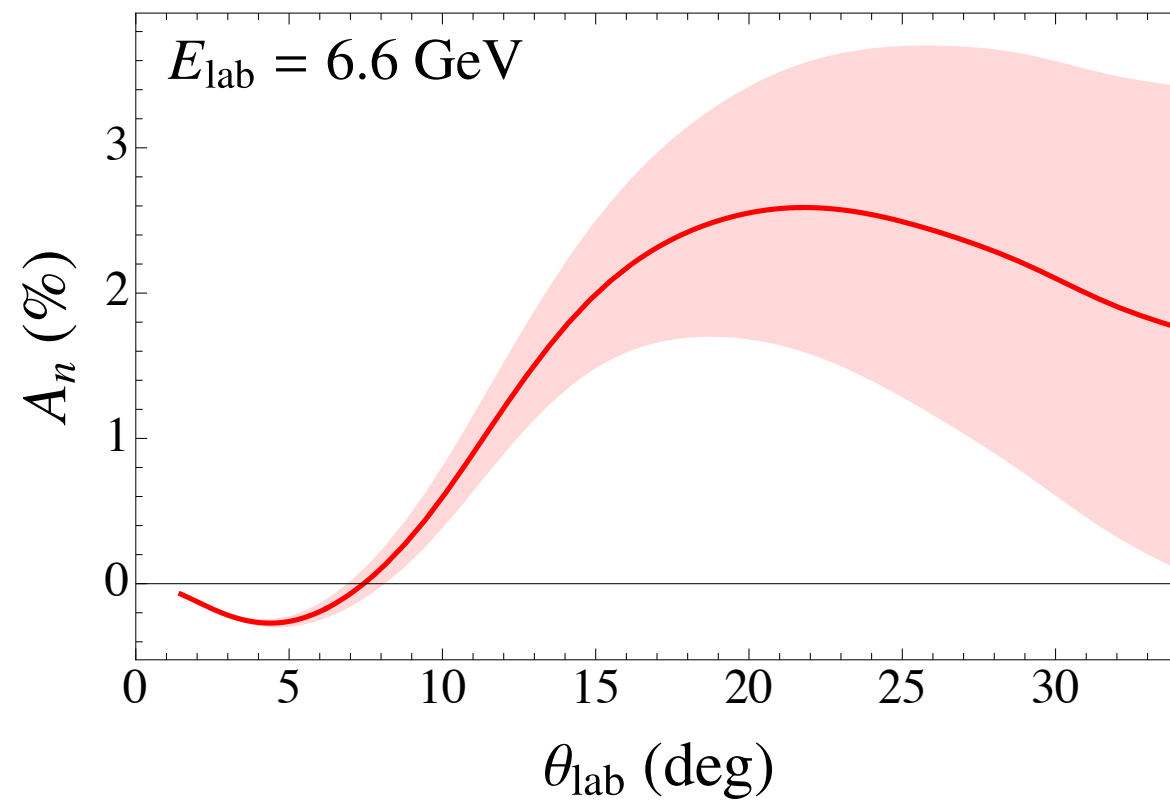
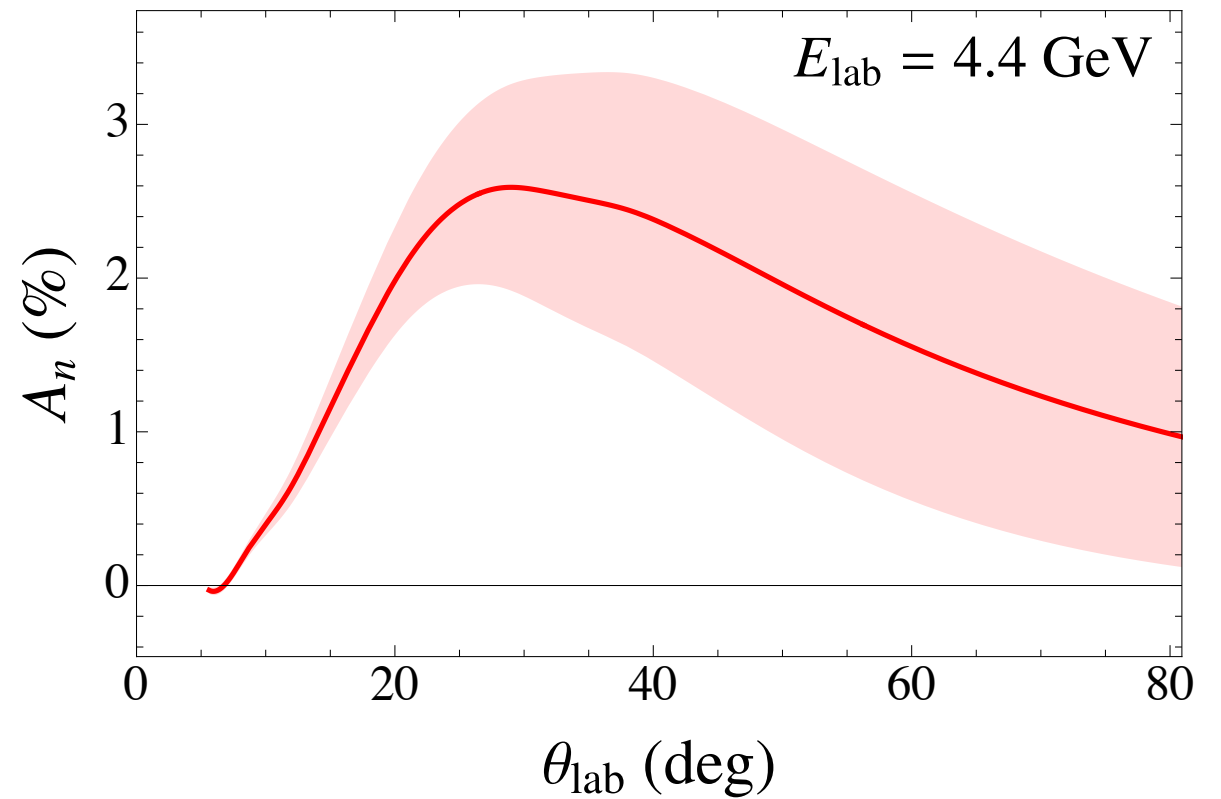
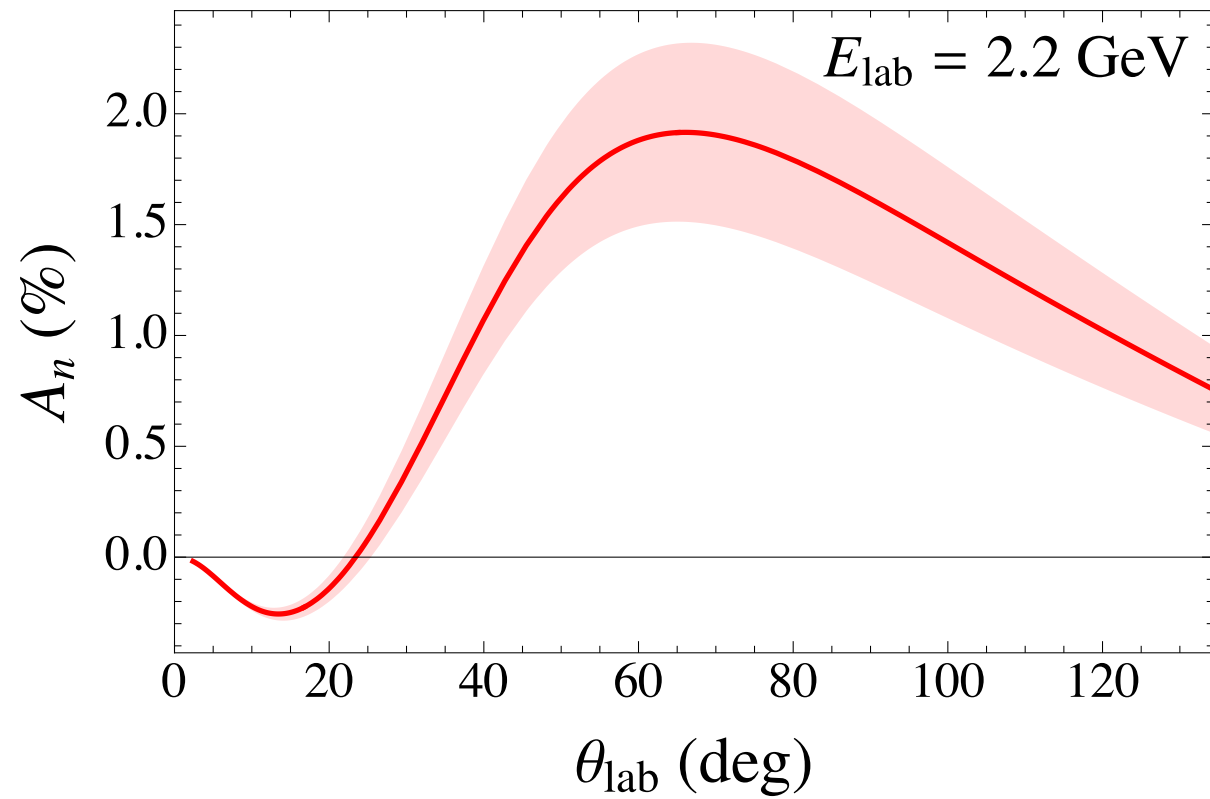
Similar overshoot of data at low energy is seen in other work

Target normal SSA



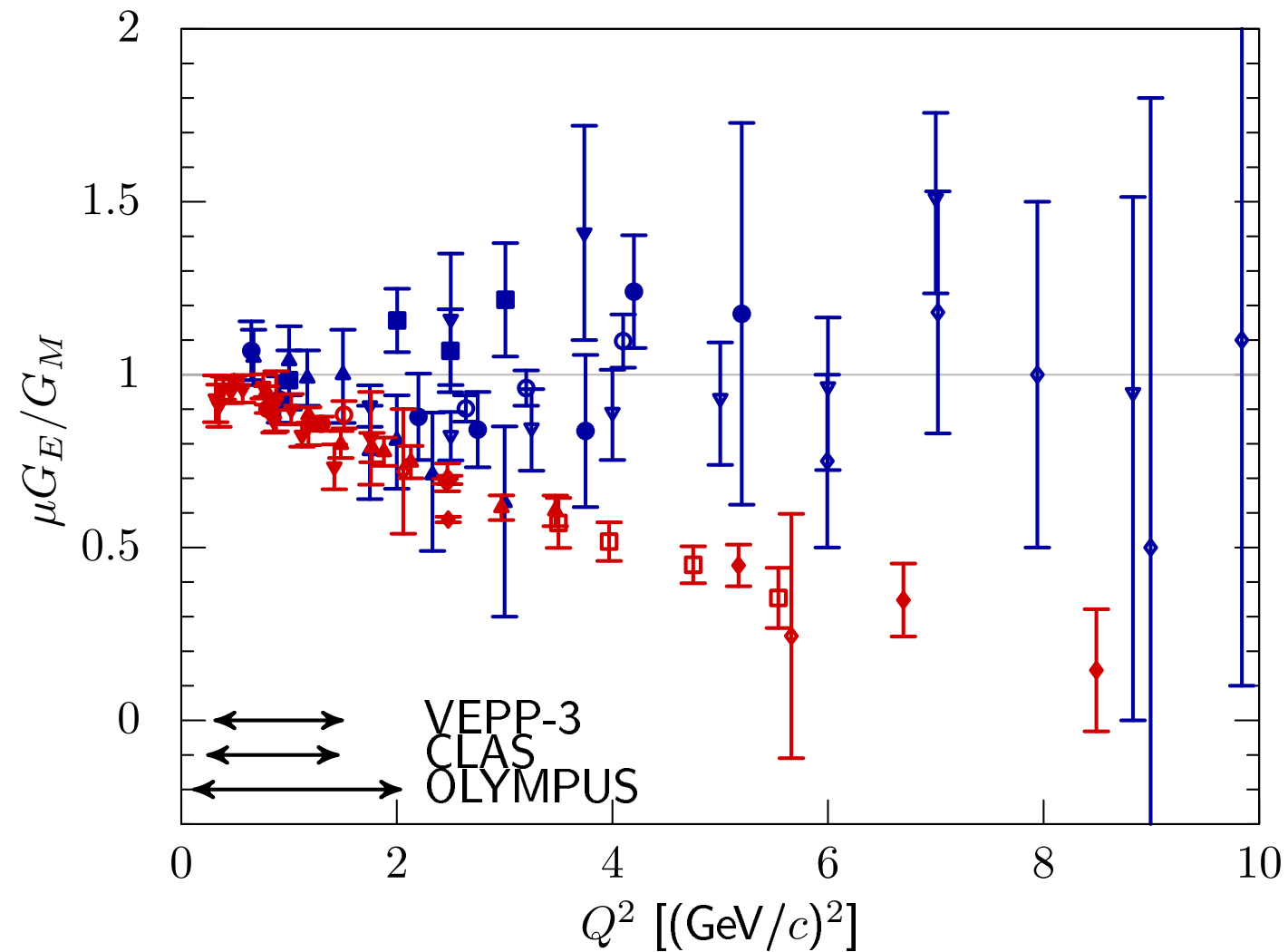
- Free of kinematics enhancements at thresholds (*i.e.* $W^2 \approx s$)
- Moderate dependence on width
- Increases as E increases (opposite of beam normal SSA)

Target normal SSA @ JLab energies



Potential 2% asymmetry in angular range 20-60° for $E_{\text{lab}} = 2.2, 4.4,$ and 6.6 GeV.

Form factors and the G_E/G_M ratio

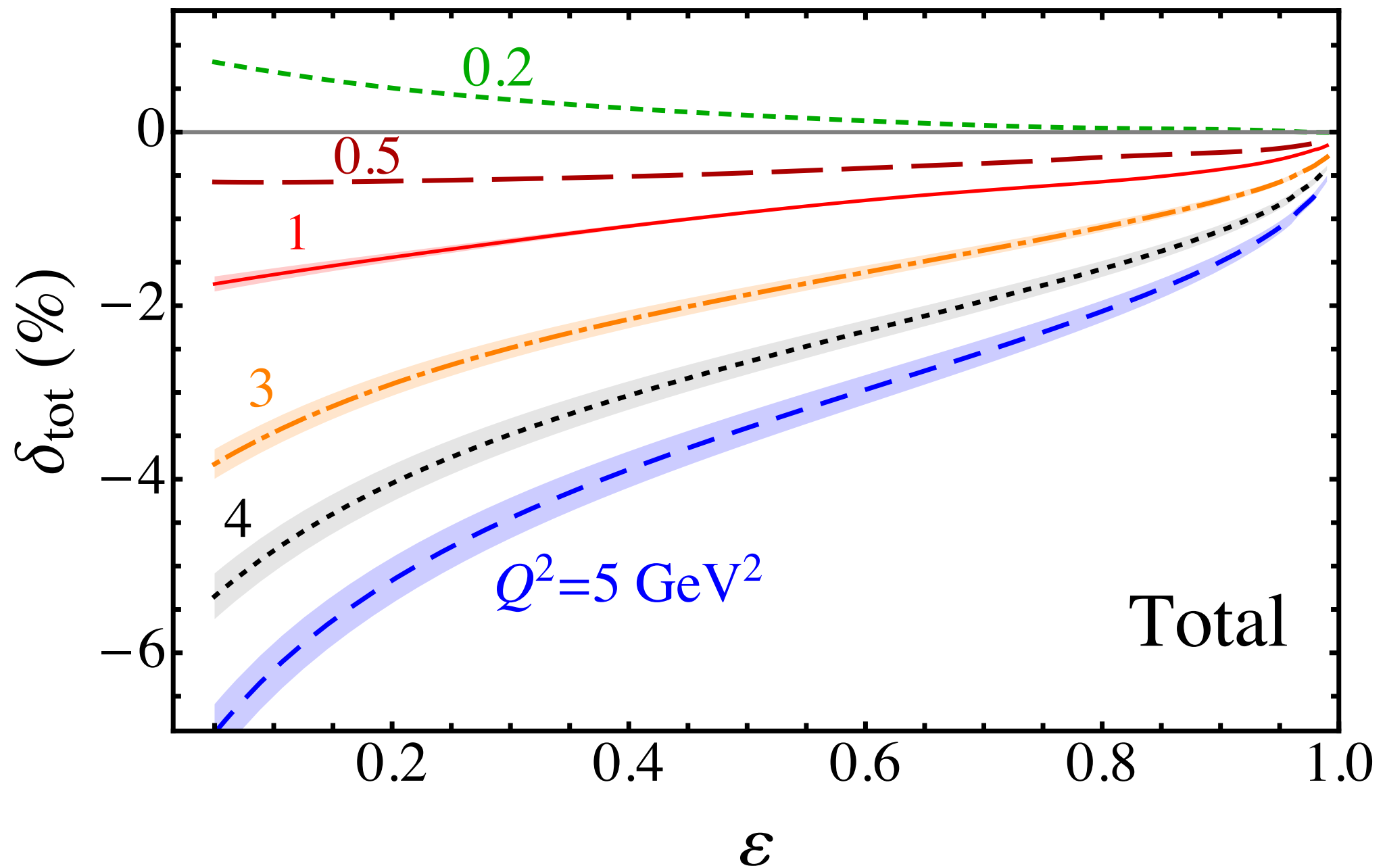


- | Rosenbluth | | Polarization | |
|-------------------|---------------|---------------------|--------------|
| ◄◄ | Litt '70 | ◄◄ | Gayou '01 |
| ◄◄ | Bartel '73 | ◄◄ | Punjabi '05 |
| ◄◄ | Andivahis '94 | ◄◄ | Jones '06 |
| ◄◄ | Walker '94 | ◄◄ | Paolone '10 |
| ◄◄ | Christy '04 | ◄◄ | Puckett '12 |
| ◄◄ | Qattan '05 | ◄◄ | Puckett '17 |
| ◄◄ | Christy '22 | ◄◄ | Liyanage '20 |

TPE leading candidate to explain discrepancy

TPE corrections to cross section (CLAS resonances)

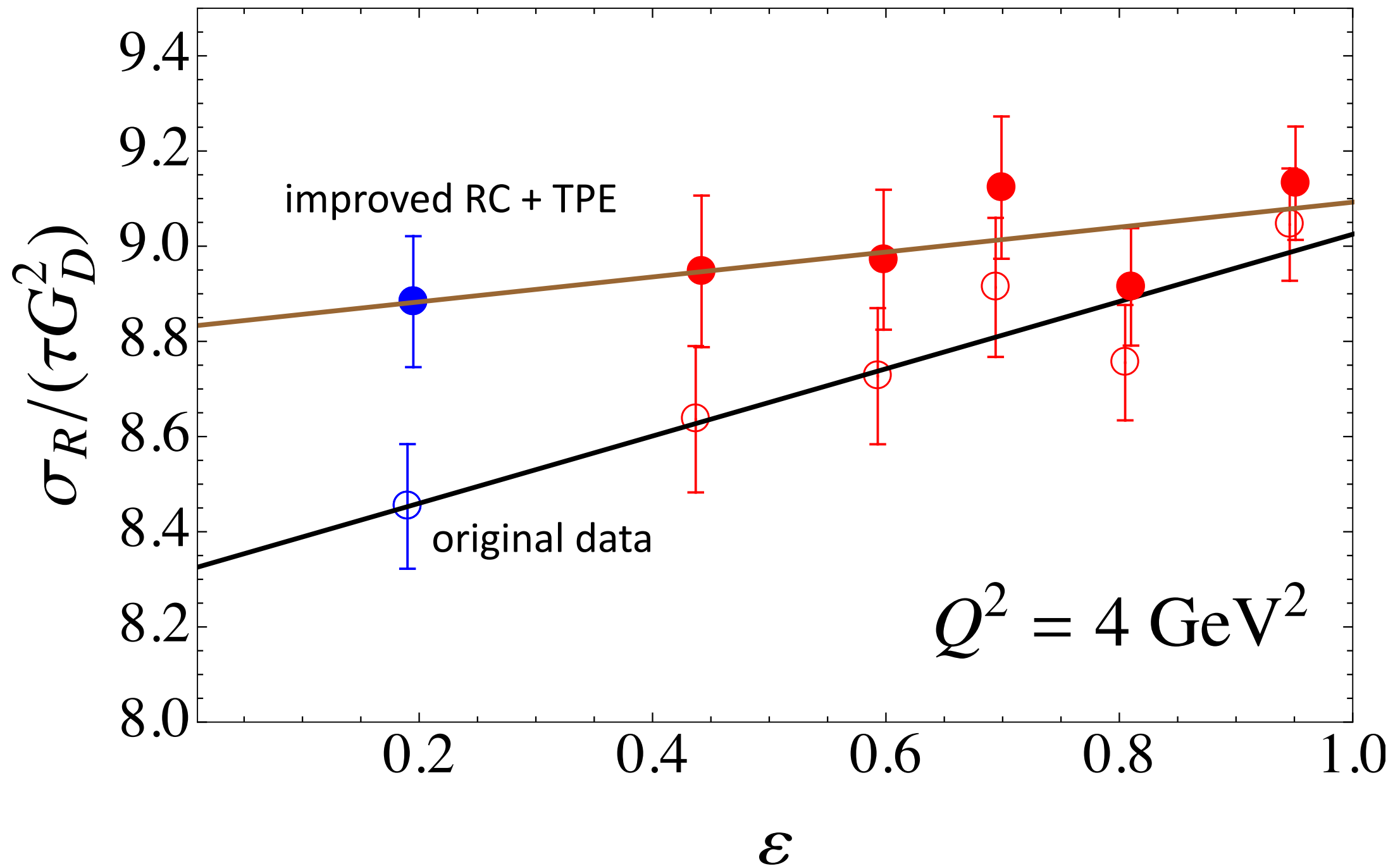
Ahmed, Blunden & Melnitchouk, PRC102, 045205 (2020)



- Linear over mid-range of ε values, but curves towards endpoints
- Presence of TPE allows for smaller contribution of G_E^2 to

$$\frac{1}{\tau} \sigma_{\text{red}} = G_M^2 + \frac{\varepsilon}{\tau} G_E^2$$

$$\frac{1}{\tau} \sigma_{\text{red}} = G_M^2 + \frac{\varepsilon}{\tau} G_E^2$$



- Example from Andivahis data set at $Q^2 = 4 \text{ GeV}^2$
- Uses improved RC + our TPE
- No evidence of non-linearity

Summary

- **Beam normal SSA:** interesting and challenging
 - dominated by spin $3/2$
 - mutual cancellation between opposite parities
 - seems to overestimate data at low energies (where $\Delta(1232)$ dominates) and underestimate data at high energies
- **Target normal SSA:** lack of data
 - Imaginary part of same generalized form factors as for cross section (real) — connected by dispersion relations
 - Potential 2% asymmetry at JLab energies 2.2 to 6.6 GeV and angles from 60° to 20°