

Lambda-D scattering from g10

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2023/11/09 (Thu) 16:25 – 16:50

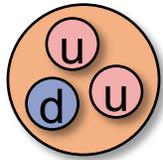
- Introduction (Physics motivation)
- 1st-level skimming (PID)
- Λ d event selection
- Efficiency
- Luminosity
- Cross-sections
- Summary

Introduction (Physics motivation)

From Quark to Neutron Star

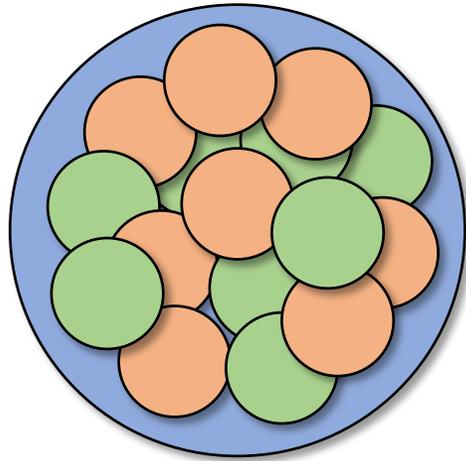
Bound systems, interacting by **strong interaction** with different scales

Hadron



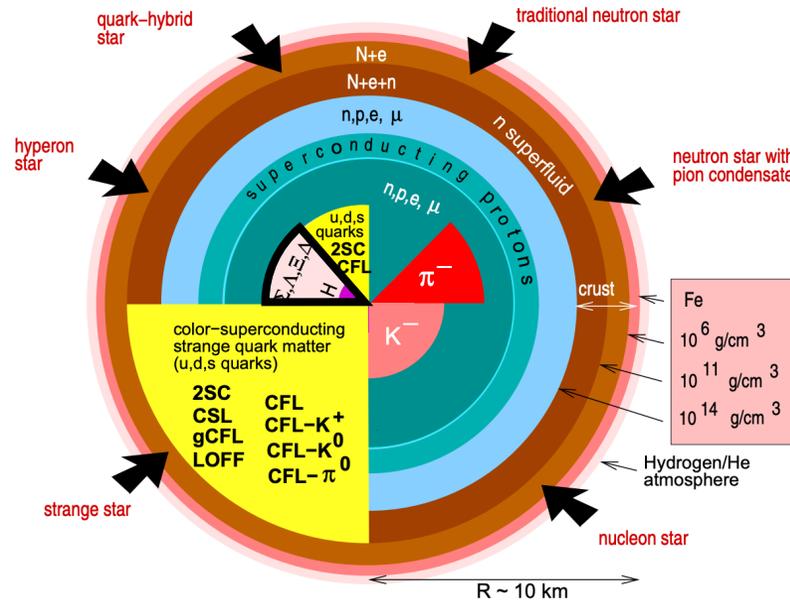
10^{-15} m

Nucleus, Hypernucleus

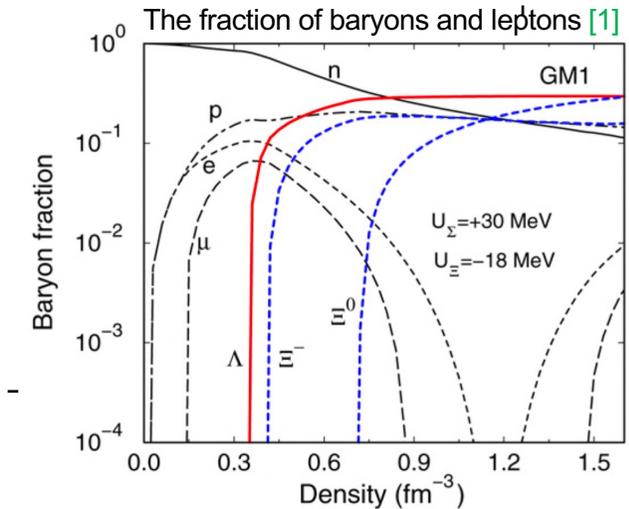
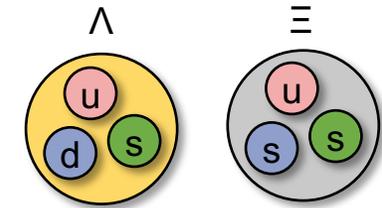


10^{-14} m

Neutron star [2]

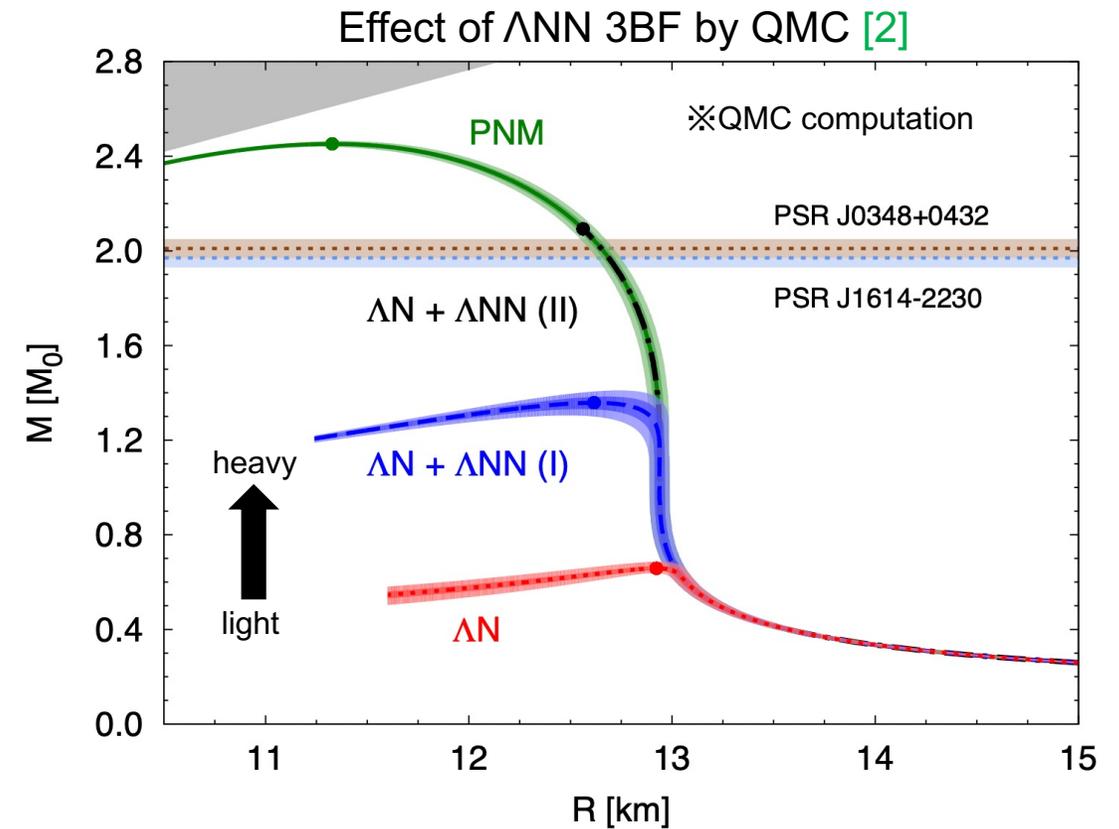
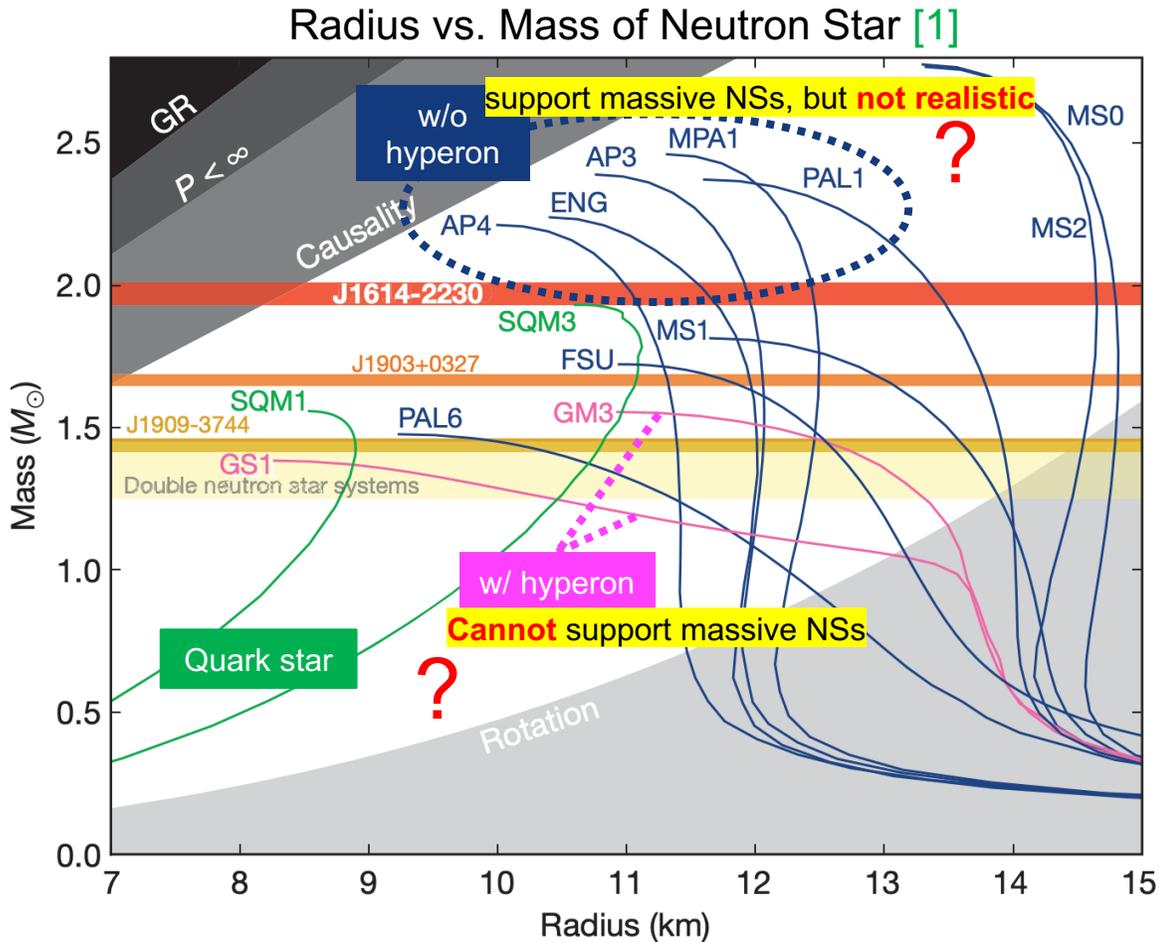


Strange hadronic matter?



- **They should be understood in the same framework** based on the microscopic picture.
- **Studying the mechanism of the Neutron Star would lead construction of realistic BB interactions.**

Hyperon Puzzle of Neutron Stars (NSs)

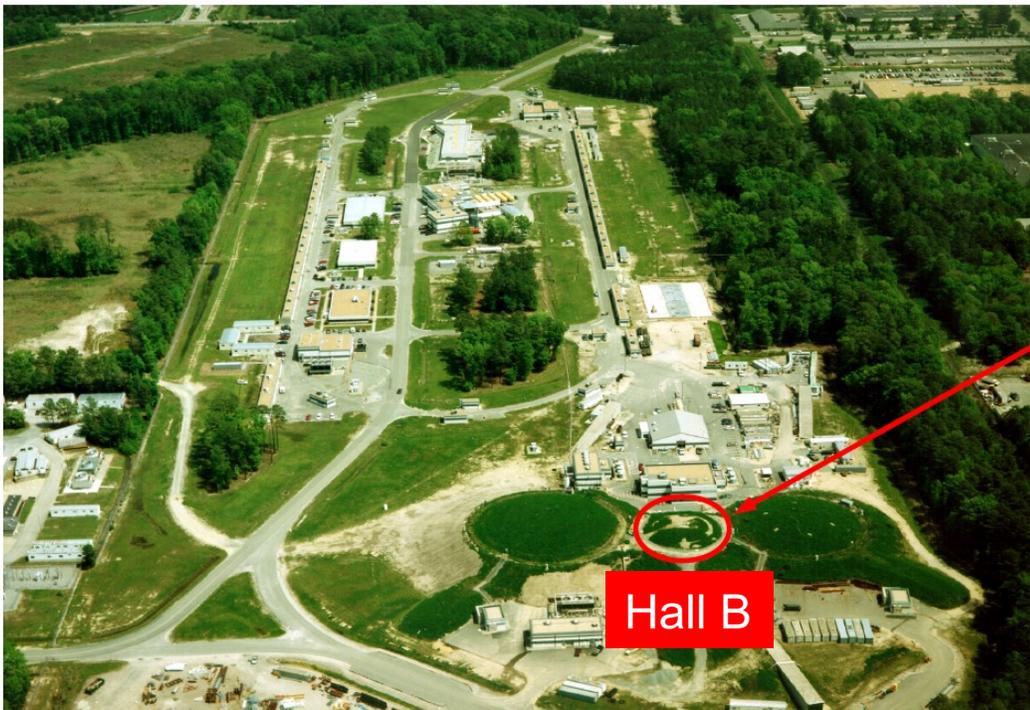


- **Hyperon-nucleon (YN) interaction is repulsive** in the short range (by the Quark Cluster Model).
 - **Λ is the first candidate** of the hyperon appearance in Neutron Stars.
- \rightarrow Λ NN three-body forces (3BF) could support massive NSs** by making the EoS stiffer.

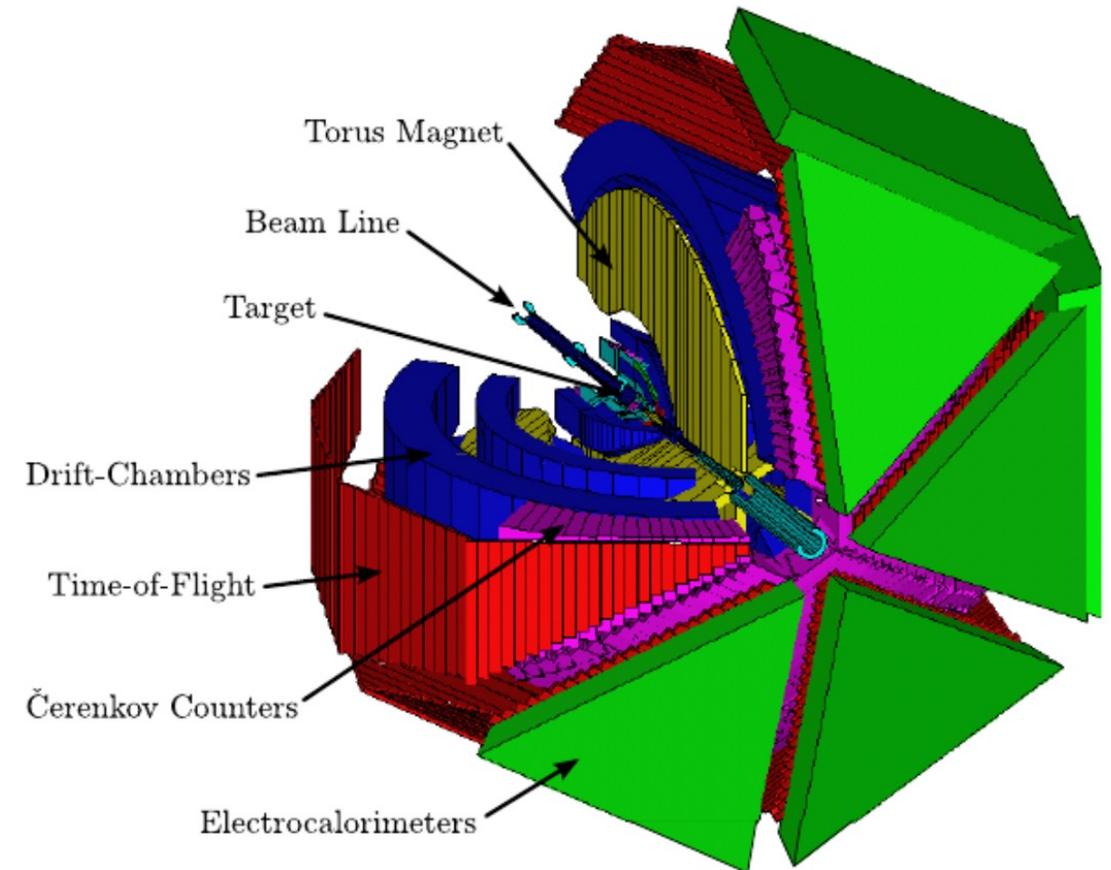
CLAS

- **Ad differential & integrated cross-sections** measurement by CLAS g10 dataset.
 - Analysis from Oct 2021 ~

J-Lab
Continuous Electron Beam Accelerator Facility (CEBAF)



CEBAF Large Acceptance Spectrometer (CLAS)



1st-level Skimming (PID)

Number of Photon

Photon selection

$$t_{track} = t_{ST} - \frac{d}{c\beta_{\gamma \text{ calc}}},$$

d: distance from the beam vertex to the SC

$$\beta_{\gamma \text{ calc}} = \sqrt{\frac{p_{DC}^2}{m^2c^2 + p_{DC}^2}},$$

t_{event} was obtained by averaging t_{track} for each track to select photon beam

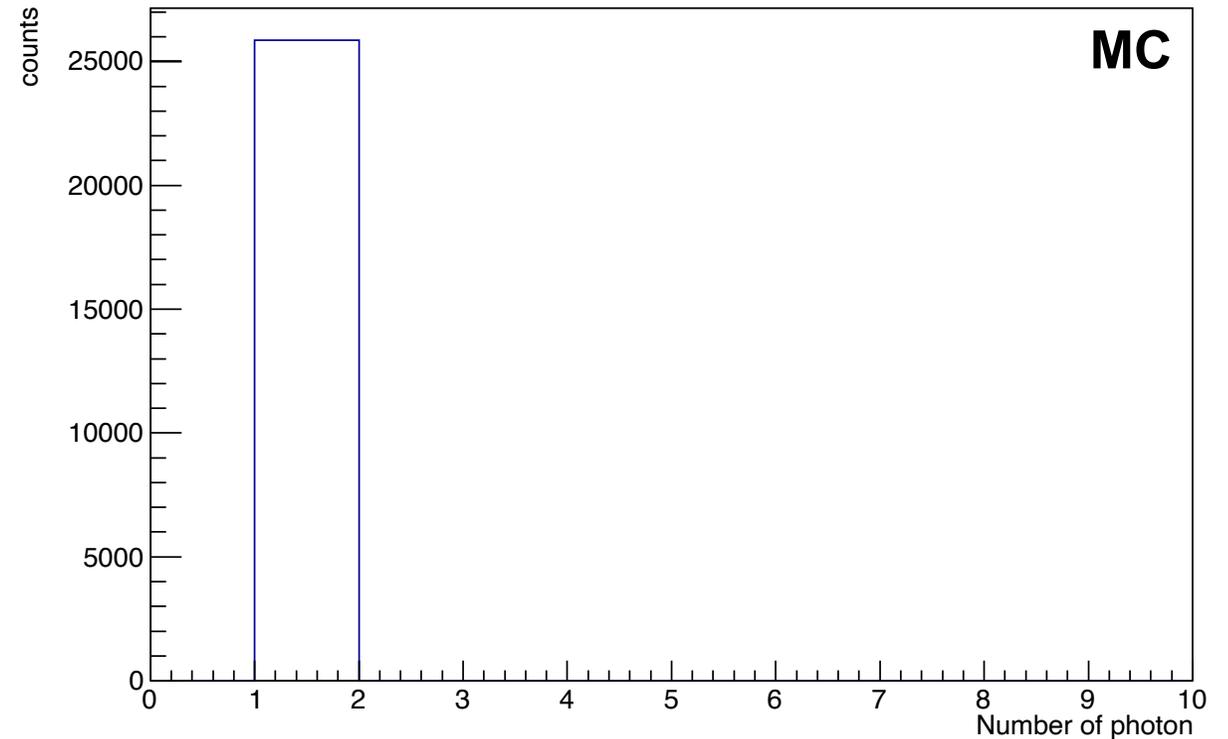
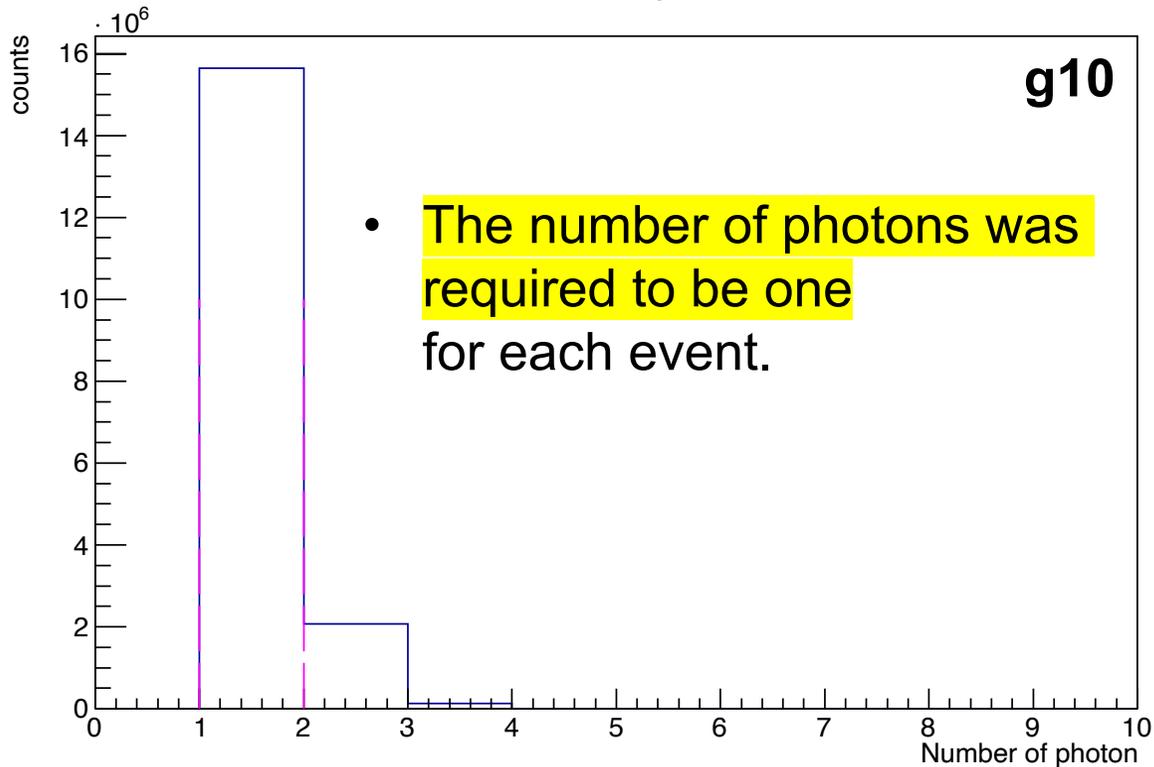
d': distance from the target center to event vertex

$$t_{\gamma} = t_{center} + \frac{d'}{c},$$

- Compare with trigger time (t_r)
 → $\Delta t = |t_{\gamma} - t_r| < 20 \text{ ns}$ (wide gate)

Number of photon

Number of photon



1st & 2nd PID

$$v = \frac{d}{t}$$



$$\beta_{meas}$$

- t : time the particle traveled from the event vertex to the TOF detector
- d : known path length the particle traveled in the Drift Chamber (DC)

← **Beta measurement**

$$m^2 = \frac{p^2(1 - \beta_{meas}^2)}{\beta_{meas}^2}$$

← **1st Particle ID**

The particle whose textbook reference value of the mass best matches the calculated mass value is identified as the detected particle

$$\delta t = t_{meas} - t_{calc}$$

← **2nd Particle ID (p vs. δt plot)**

A difference between measured & calculated timing is ideally should be 0.

$$t_{meas} = t_{SC} - t_{trig}$$

$$t_{calc} = d / (\beta_{calc} \cdot c)$$

$$\beta_{calc} = \sqrt{\frac{p^2}{m^2 c^2 + p^2}}$$

p: momentum by DC



$\Delta\beta$ measurement

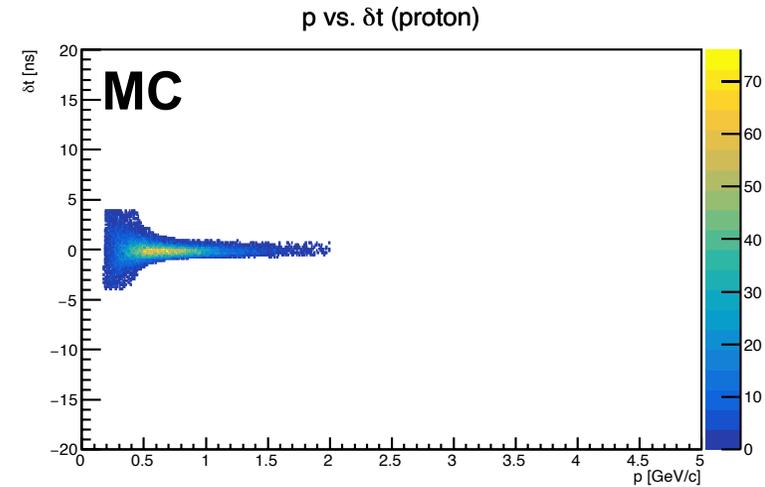
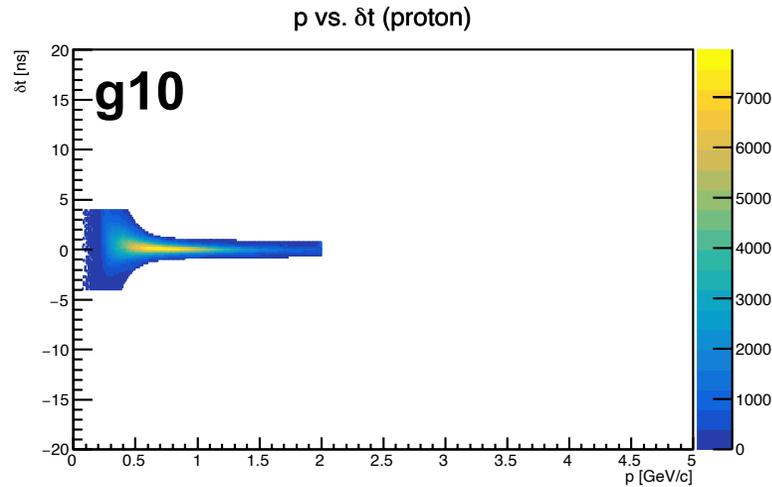
- To make PID better, a difference between measured & calculated β was obtained.

$$\Delta\beta = \beta_{calc} - \beta_{meas}$$

2nd PID (p vs. δt plot) & $\Delta\beta$ Measurement

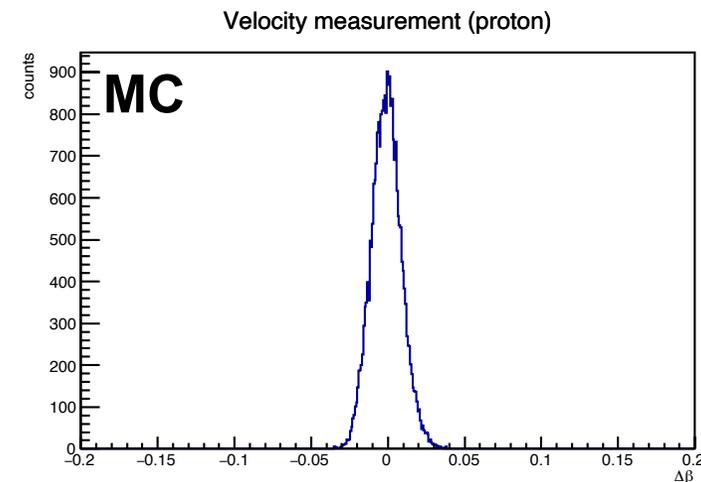
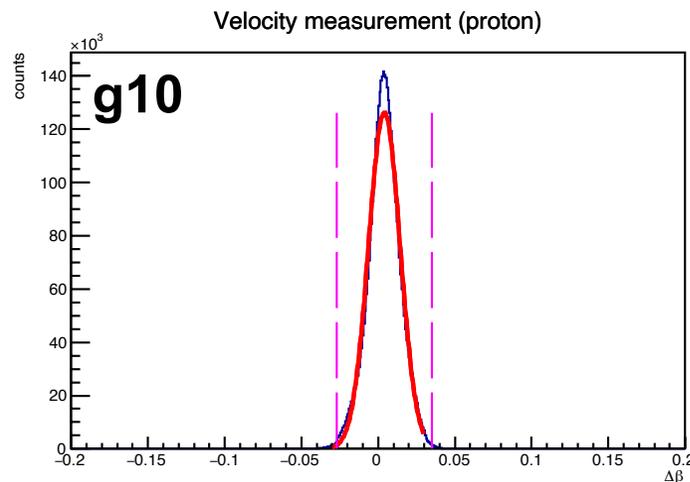
2nd PID (p vs. δt plot)

- Proper cut parameters were applied.



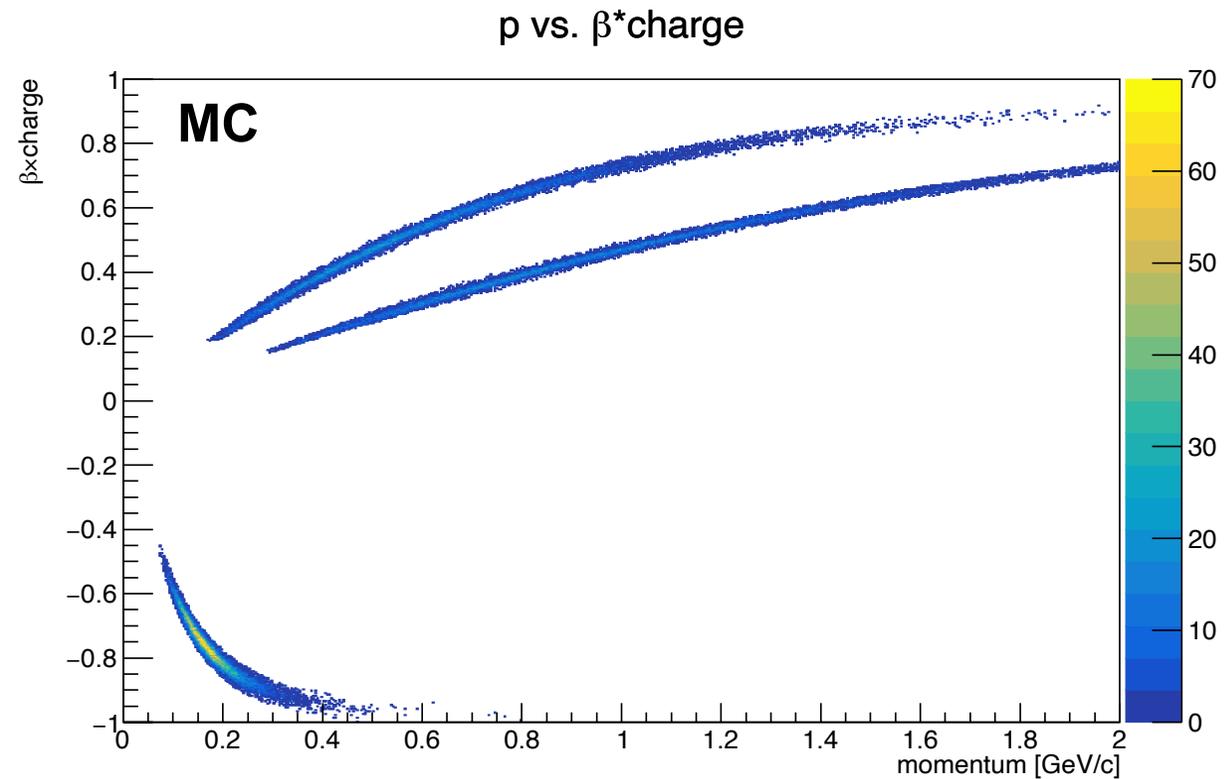
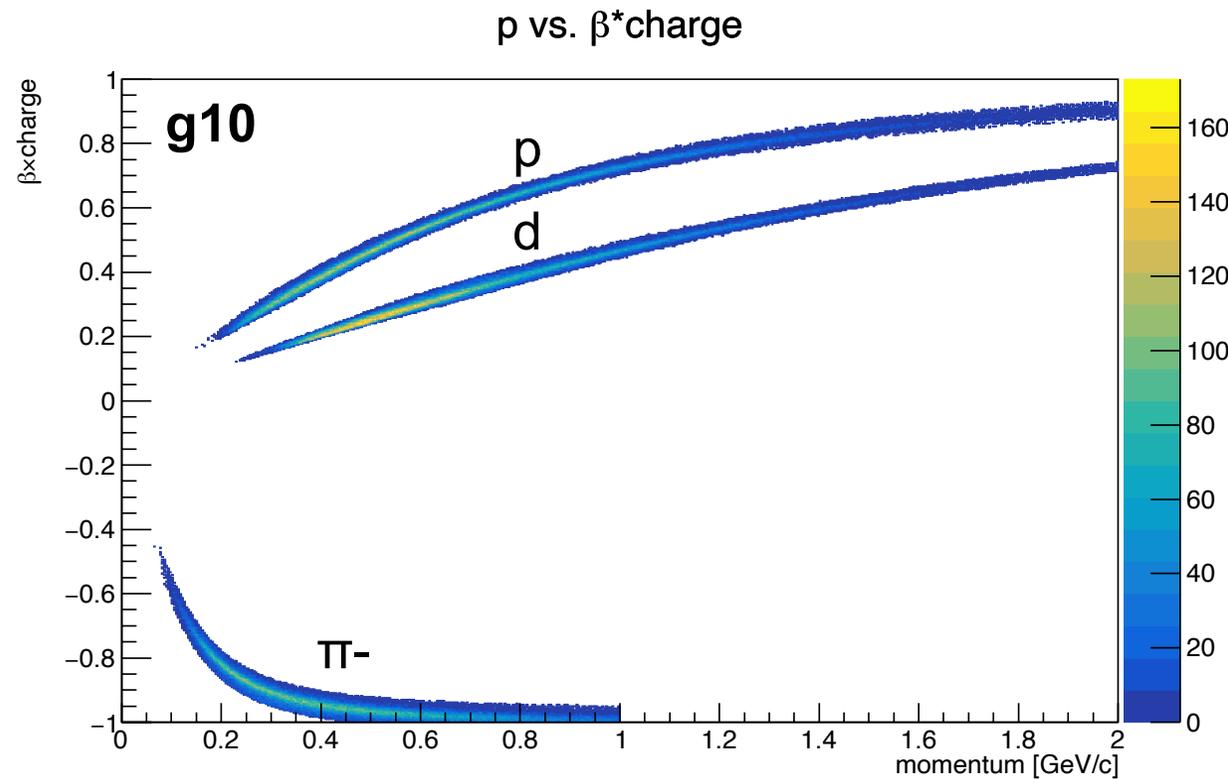
$\Delta\beta$ measurement

- The $\Delta\beta$ spectrum was fitted with **Gaussian**, and events **within $\pm 3\sigma$** were selected.



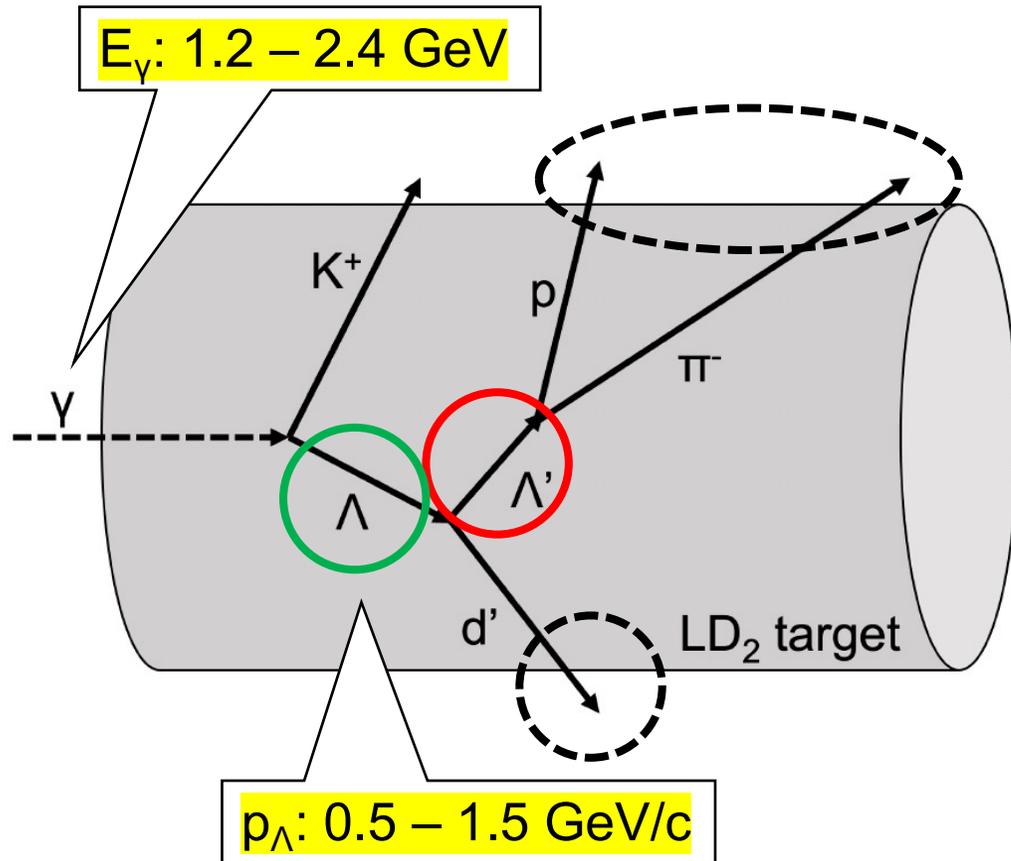
Final p vs. β^* charge Plot

- Through the above PID analysis, we could clearly identify protons, deuterons, and π^- .
- We used these particles for the physics analysis of Λd scattering.



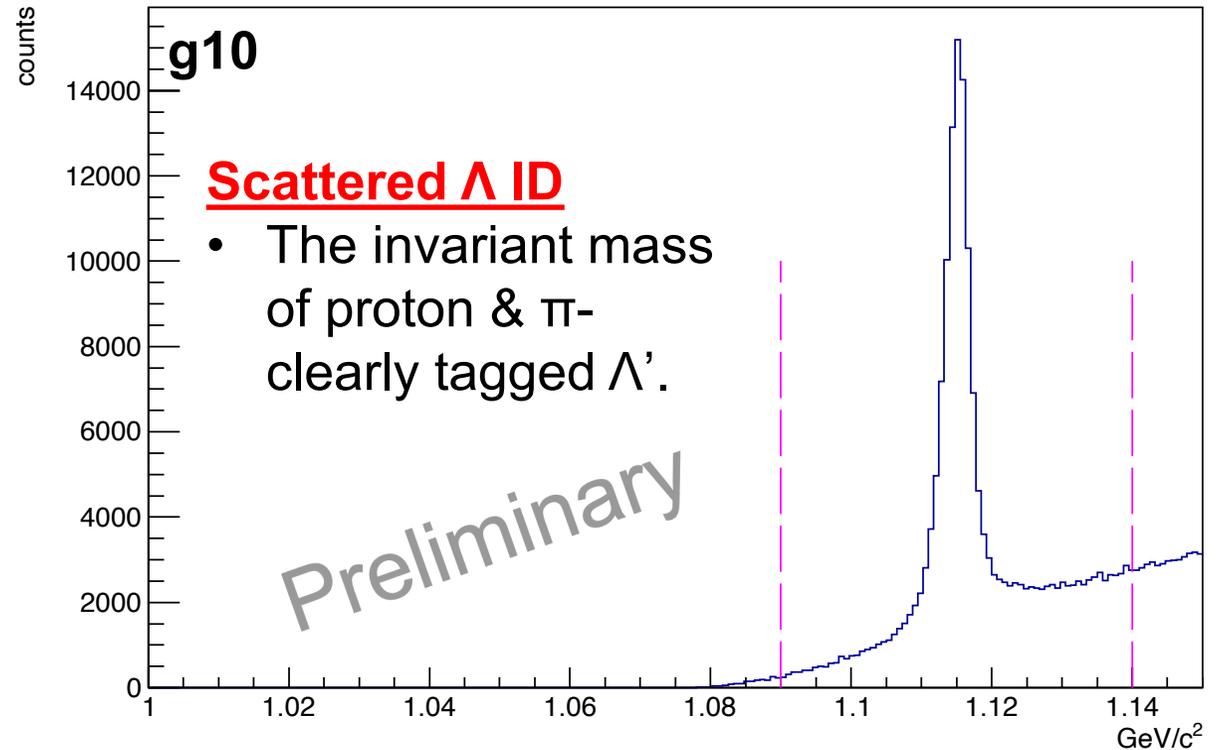
Ad Event Selection

Λ' & Λ Identification



$$M_{\Lambda'} = \sqrt{(E_p + E_{\pi^-})^2 - |\mathbf{p}_p + \mathbf{p}_{\pi^-}|^2}$$

Invariant mass (p & π^-)



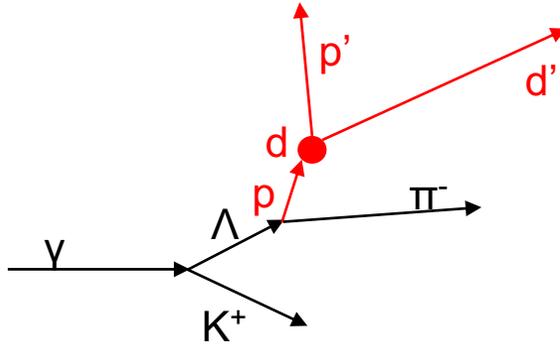
$$M_X = \sqrt{(m_d - E_{d'} - E_{\Lambda'})^2 - (p_{d'}^2 + p_{\Lambda'}^2 + 2p_{d'}p_{\Lambda'} \cos \theta_{d'\Lambda'})}$$

Beam Λ ID

- The missing mass of $Xd \rightarrow \Lambda d$ was required to be $>0 \text{ GeV}/c^2$.

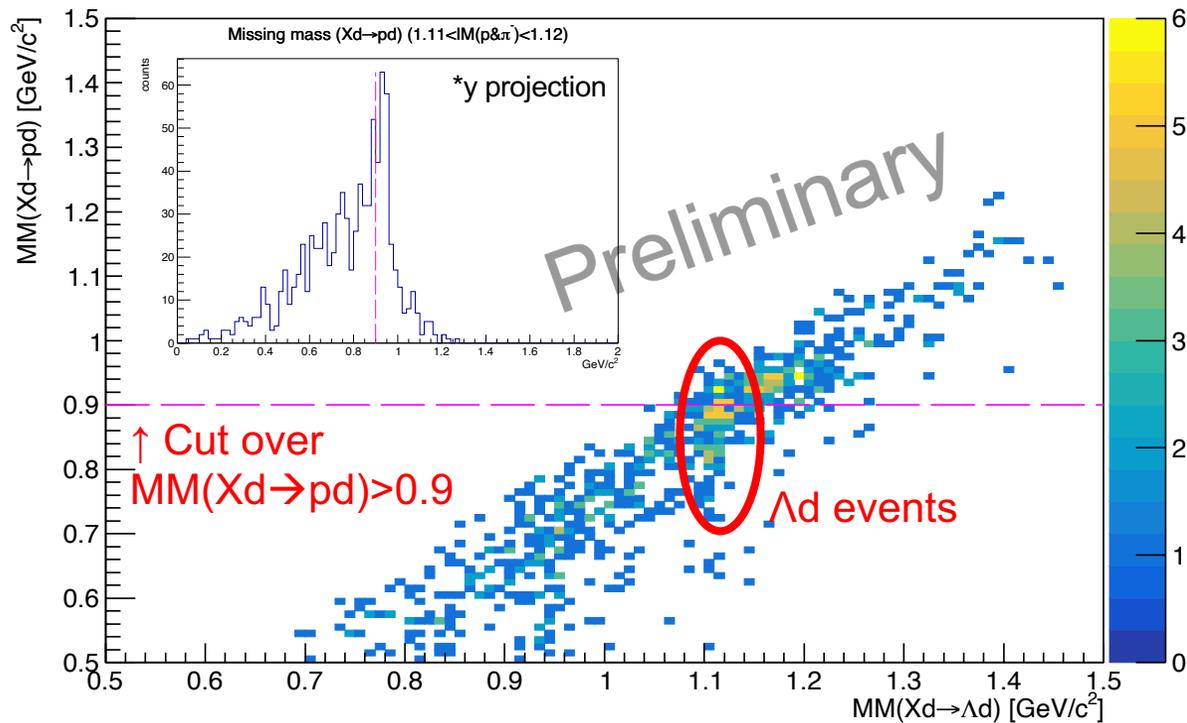
Main BG (pd scattering) Removal

$\Lambda \rightarrow \pi p$ decay & pd scattering

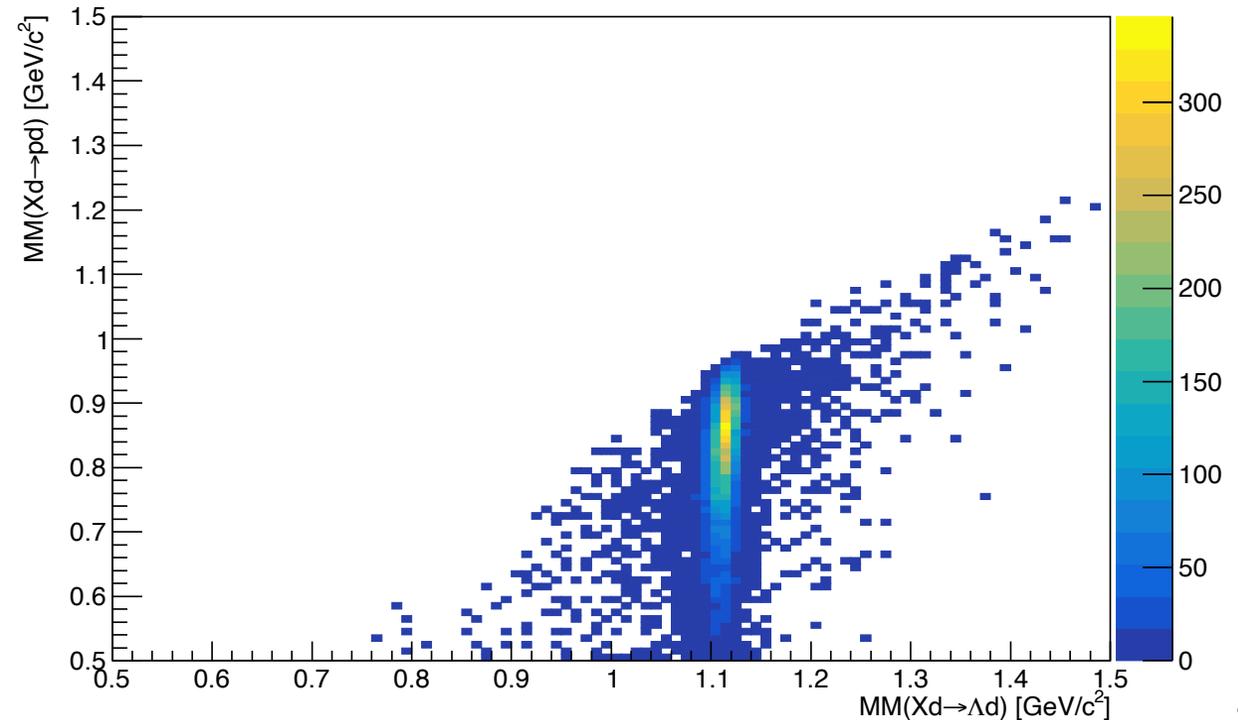


- The main background in Λd analysis is **pd scattering**
 - **Kinematically mixed in the $MM(Xd \rightarrow \Lambda d)$**
- Cut the events over $MM(Xd \rightarrow pd) > 0.9$
- although some Λd events were removed.

$MM(Xd \rightarrow \Lambda d)$ vs. $MM(Xd \rightarrow pd)$ ($1.11 < M(p\&\pi^-) < 1.12$)



$MM(Xd \rightarrow \Lambda d)$ vs. $MM(Xd \rightarrow pd)$

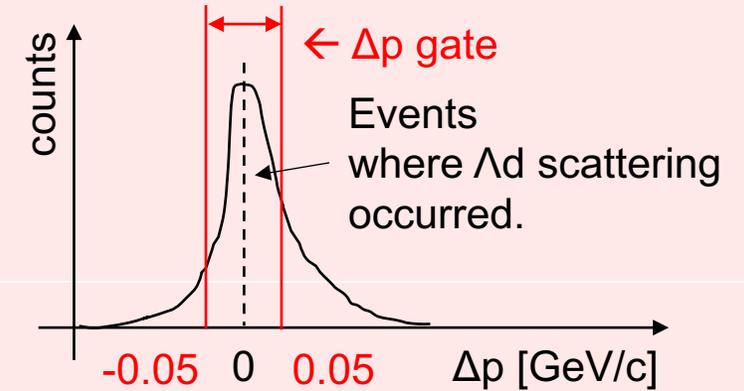


Yield of Λd Scattering Events

Scattered Λ momentum index (Δp)

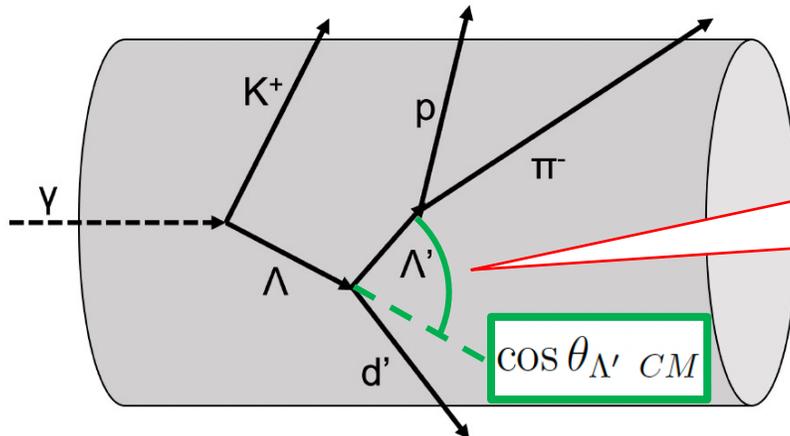
※ Equivalent to the missing mass method

- When calculating Λ' momentum ($p_{\Lambda' \text{ calc}}$), we assumed $\Lambda d \rightarrow \Lambda' d'$ kinematics.
- $p_{\Lambda' \text{ calc}}$ was compared to the measured momentum ($p_{\Lambda' \text{ meas}}$).
- The difference between $p_{\Lambda' \text{ meas}}$ & $p_{\Lambda' \text{ calc}}$ is “ Δp .”
- Events in the Δp gate ($|\Delta p| < 0.05 \text{ GeV}/c$) \rightarrow Integrated cross-section



Scattering angle distribution of Λ' ($\cos\theta_{CM}$)

- After applying the Δp gate, $\cos\theta_{CM}$ spectra were obtained.
 - Events where $|\cos\theta_{CM}| < 0.6 \rightarrow$ Differential cross-section



$$p_{\Lambda' \text{ calc}} = \frac{A p_{\Lambda} \cos \theta_{\Lambda'} + (E_{\Lambda} + m_d) \sqrt{B}}{2((E_{\Lambda} + m_d)^2 - p_{\Lambda}^2 \cos^2 \theta_{\Lambda'})}$$

$$A = m_{\Lambda}^2 + m_d^2 + m_{\Lambda'}^2 - m_{d'}^2 + 2E_{\Lambda} m_d$$

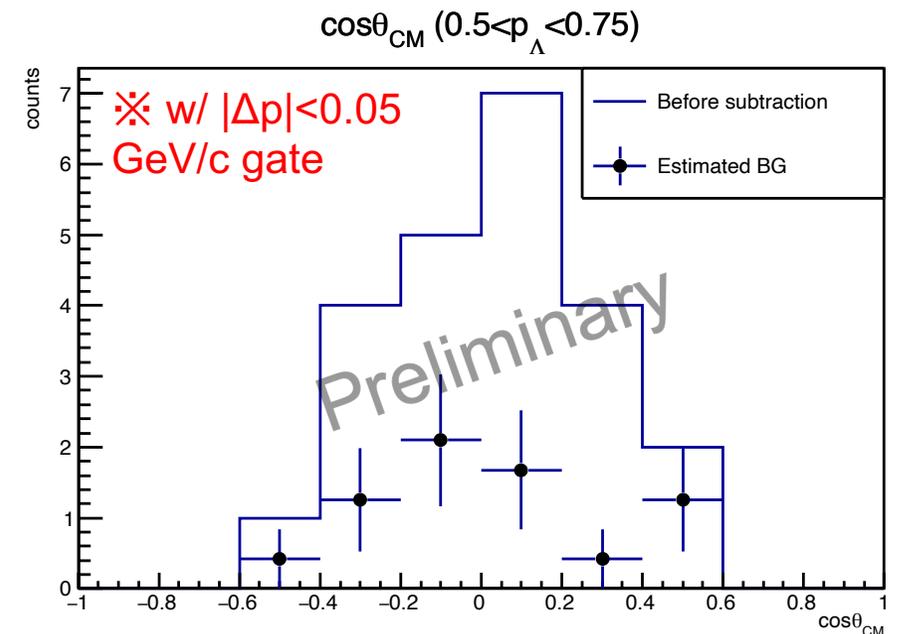
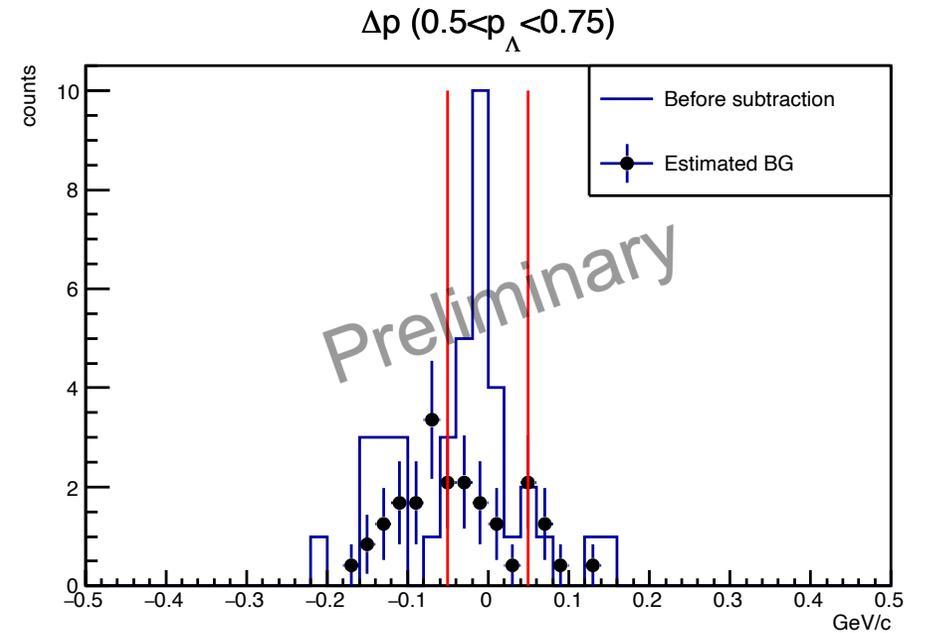
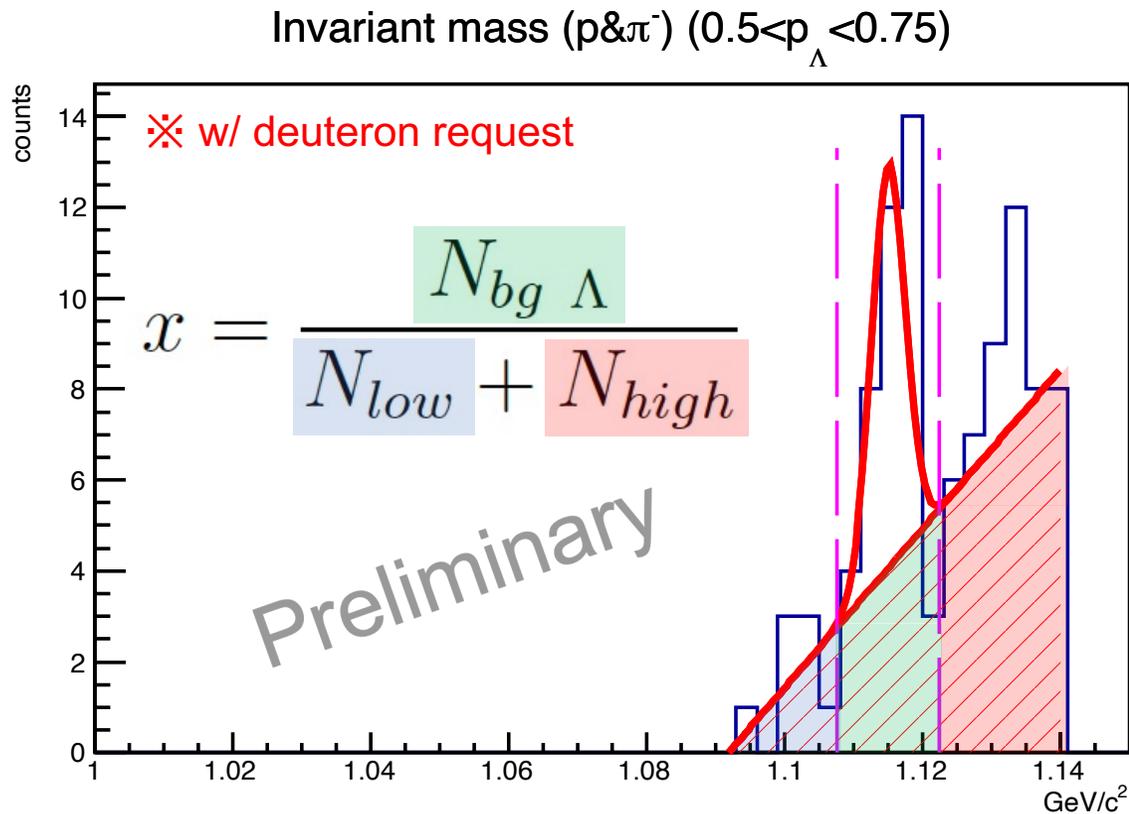
$$B = 4m_{\Lambda'}^2 (p_{\Lambda}^2 \cos^2 \theta_{\Lambda'} - (E_{\Lambda} + m_d)^2) + A^2.$$

$$\Delta p_{\Lambda'} = p_{\Lambda' \text{ meas}} - p_{\Lambda' \text{ calc}}$$

BG Subtraction before Cross-section Calculation

BG estimation

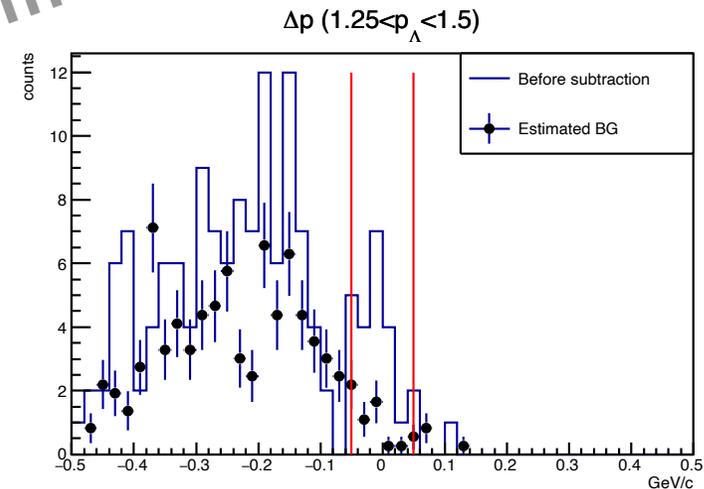
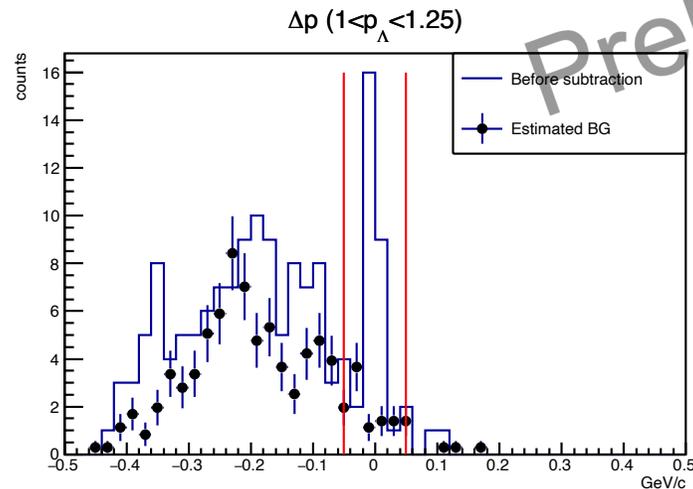
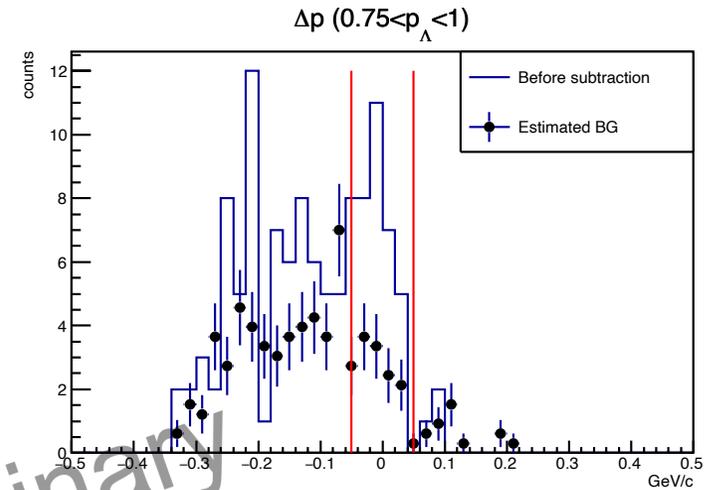
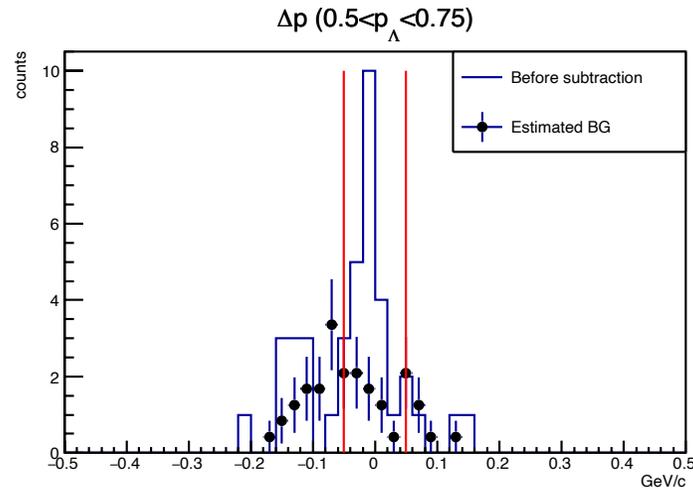
- Using the sidebands of the Λ peak in the invariant mass of proton and π^- .
- The scaling factor (x) to estimate the BG ratio under the Λ peak was calculated by fitting the invariant mass with linear and Gaussian functions.



Corrected Δp spectra

Final Λ events counting

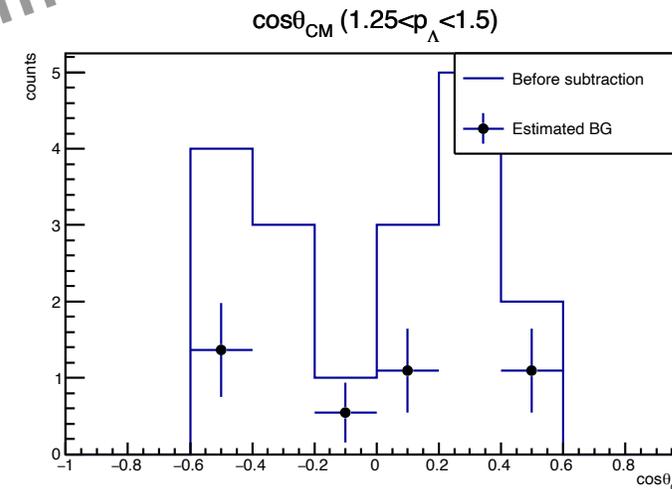
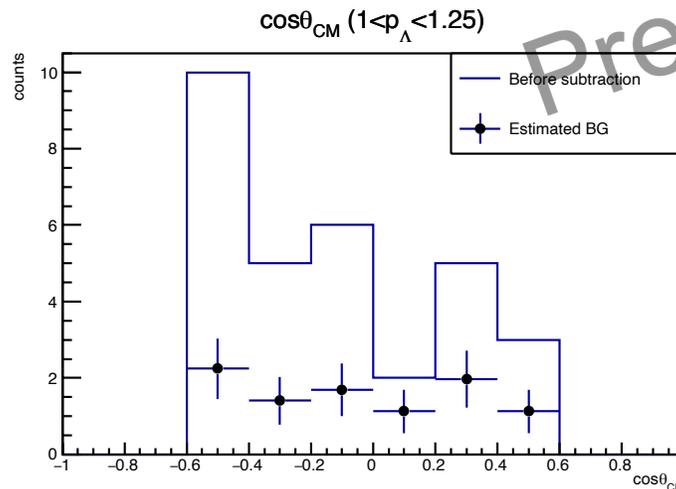
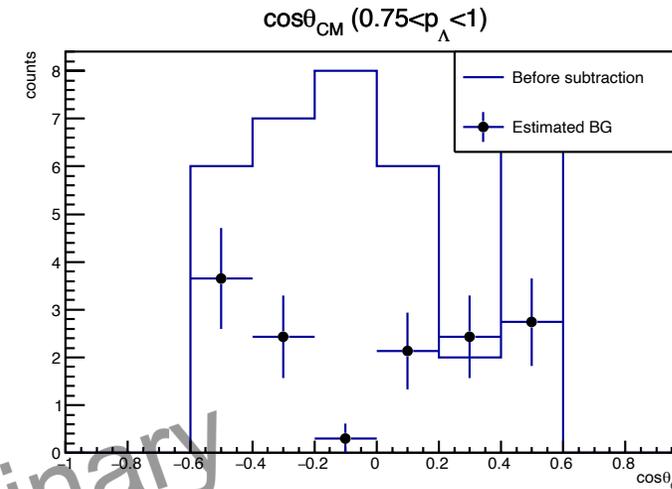
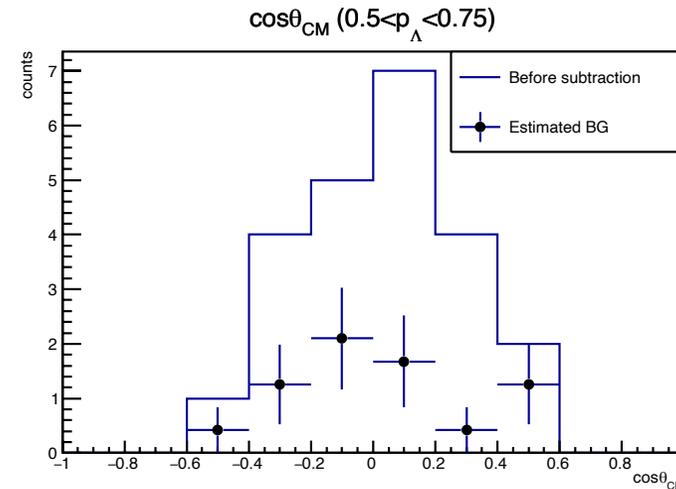
- The Δp spectra were calculated in each Λ beam momentum range ($dp_\Lambda = 0.25 \text{ GeV}/c$)
- Then, BG structures were subtracted. Events remaining in the range of $|\Delta p| < 0.05 \text{ GeV}/c$ were used to derive a integrated cross-section.



Corrected $\cos\theta_{\text{CM}}$ spectra

Final Ad events counting

- The $\cos\theta_{\text{CM}}$ spectra were calculated in each Λ beam momentum range ($dp_{\Lambda} = 0.25 \text{ GeV}/c$)
- Then, BG structures were subtracted. Events remaining in the range of $|\cos\theta_{\text{CM}}| < 0.6$ were used to derive a differential cross-section.



Efficiency

Efficiency for Cross-sections

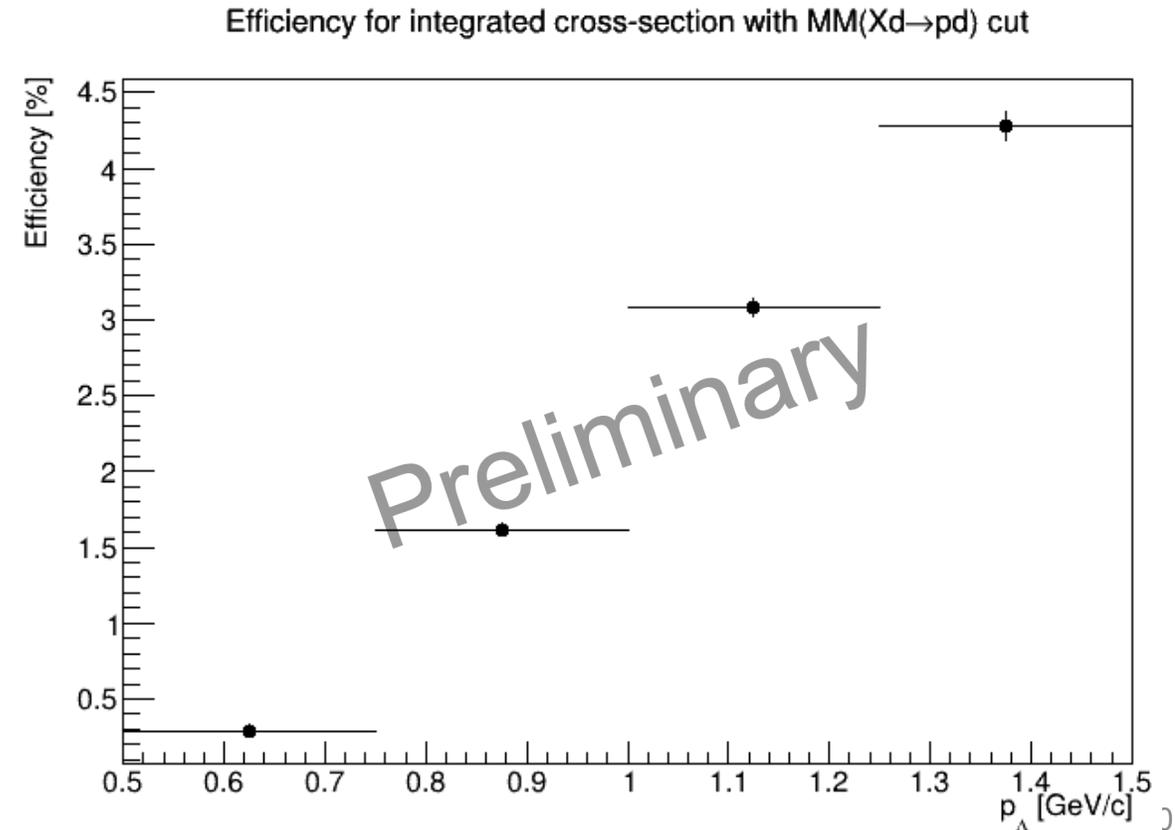
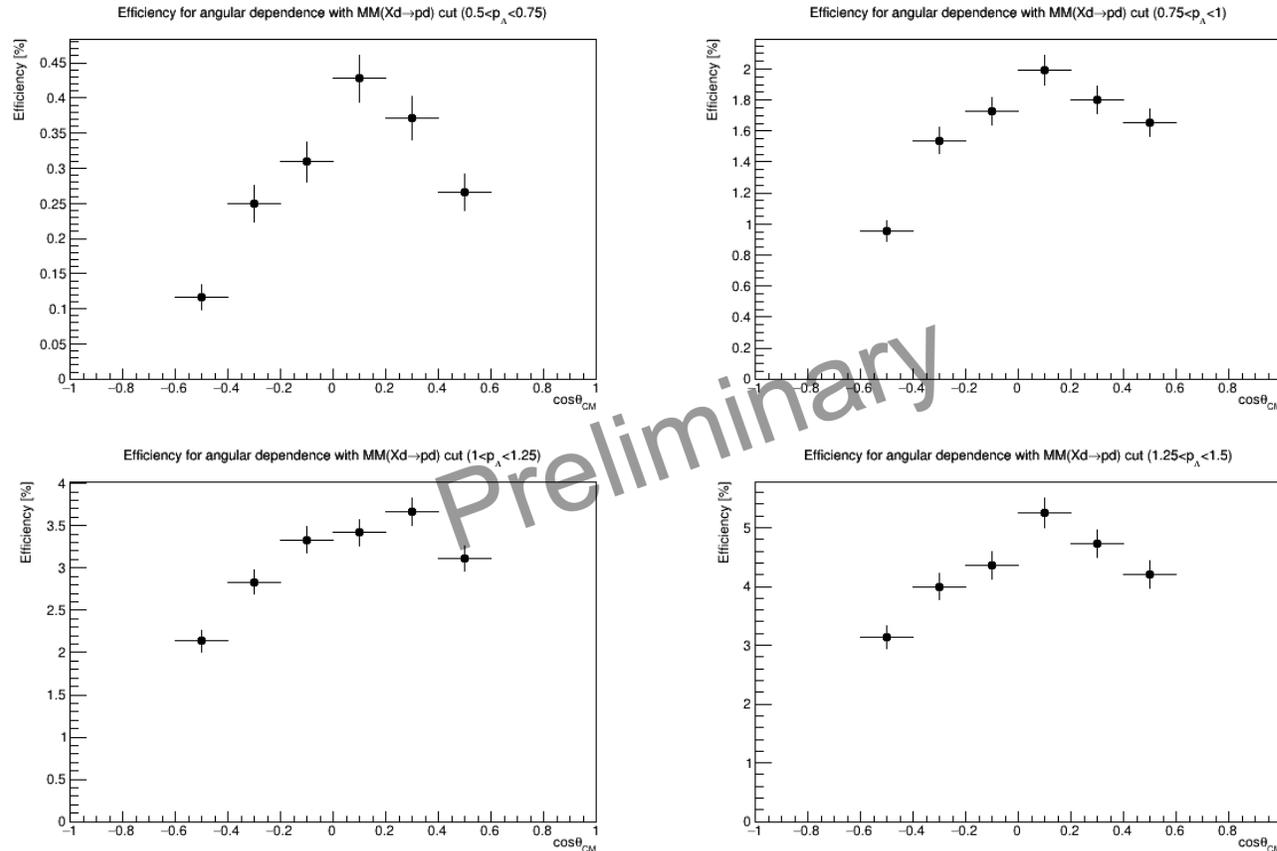
- The detection efficiency was estimated **independently** from CLAS Geant4 simulations.

$$E_{\cos\theta_{\Lambda'}, CM} = \left(\frac{N_{\Lambda d, skim}}{N_{\Lambda d, gen}} \right)_{\cos\theta_{\Lambda'}, CM}$$

$$\sigma(E_{\cos\theta_{\Lambda'}, CM}) = \frac{\sqrt{N_{\Lambda d, gen} E_{\cos\theta_{\Lambda'}, CM} (1 - E_{\cos\theta_{\Lambda'}, CM})}}{N_{\Lambda d, gen}}$$

$$E_{p_{\Lambda}} = \left(\frac{N_{all \Lambda d, skim}}{N_{all \Lambda d, gen}} \right)_{p_{\Lambda}} = \left(\frac{\sum_{i=n}^m (N_{\Lambda d, skim})_i}{\sum_{i=n}^m (N_{\Lambda d, gen})_i} \right)_{p_{\Lambda}}$$

$$\sigma(E_{p_{\Lambda}}) = \frac{\sqrt{N_{all \Lambda d, gen} E_{p_{\Lambda}} (1 - E_{p_{\Lambda}})}}{N_{all \Lambda d, gen}}$$

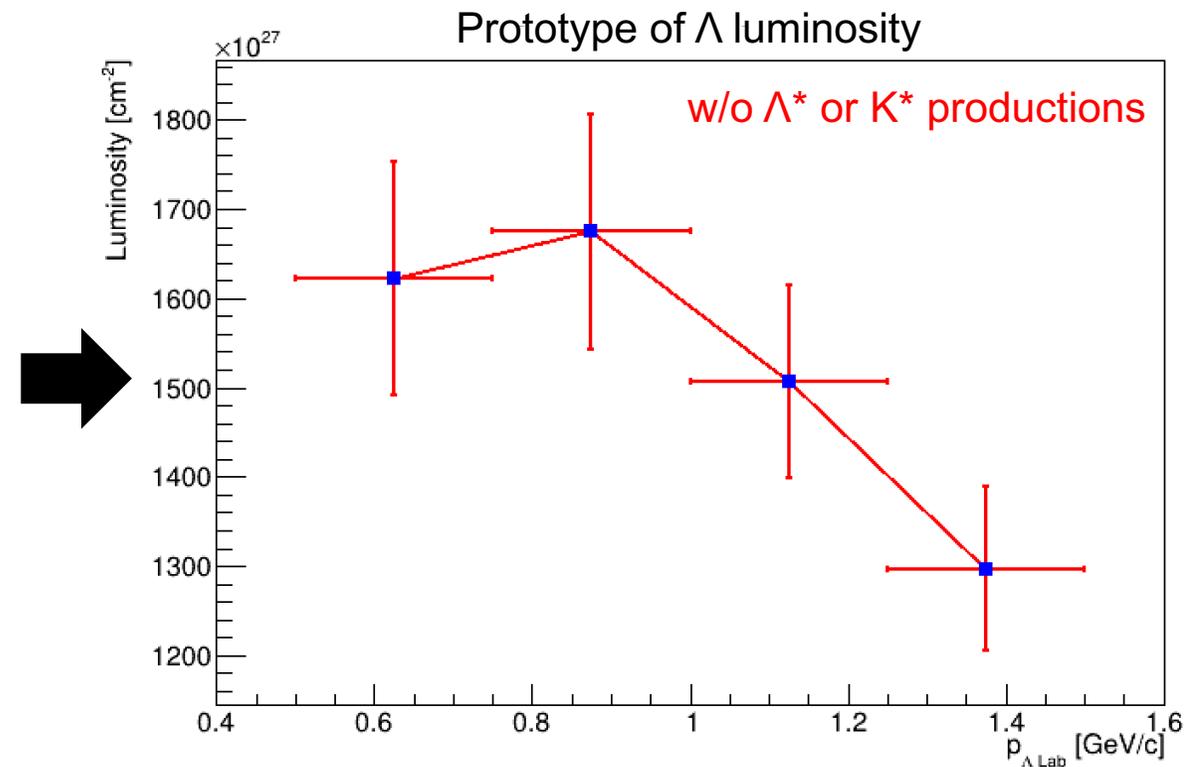
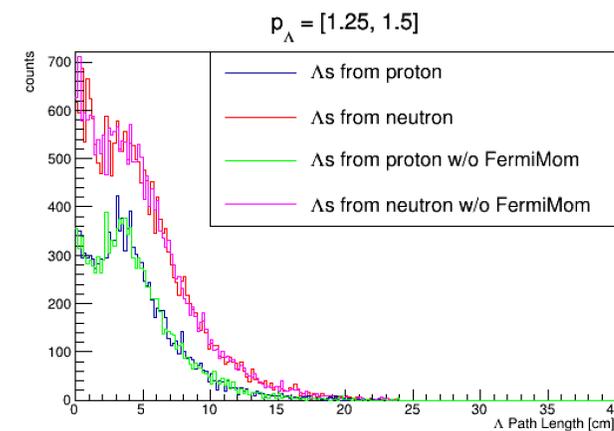
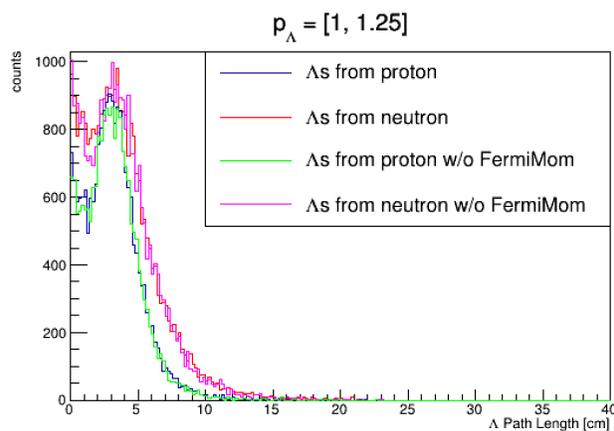
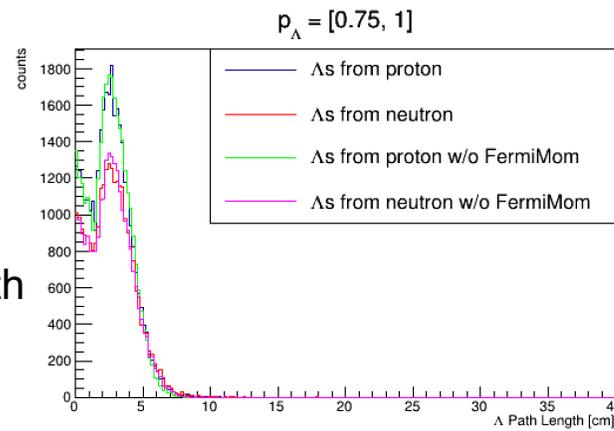
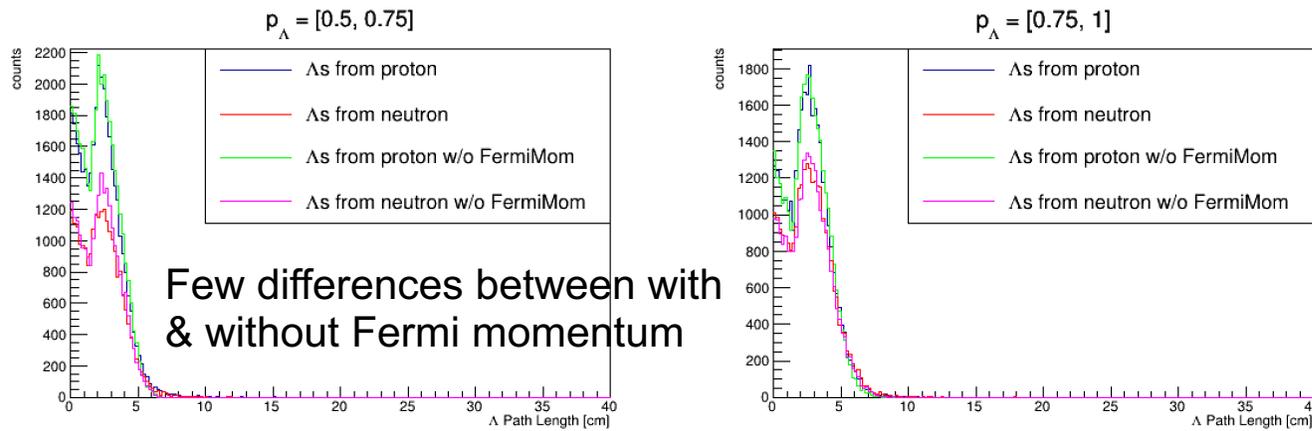


Luminosity

Λ path length (inside the LD₂ target)

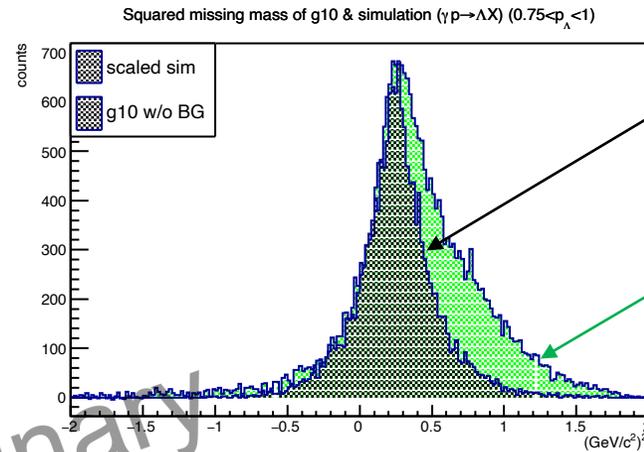
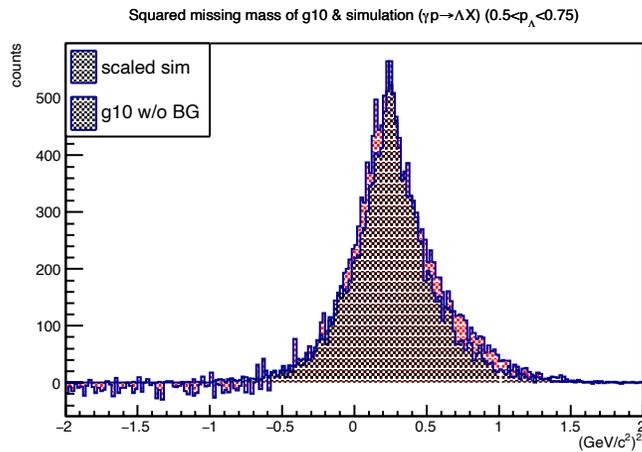
- Λ s derived from **both proton & neutron** should be considered.
- Path lengths were calculated with & without Fermi momentum in each p_Λ range.
- We calculated the luminosity **considering the Fermi momentum** of the target particle: proton or neutron.

→ **Problem:** The simulations handled by CLAS luminosity software did not include **resonance events such as Λ^* and K^* production.**



Estimation of resonance yield

- The number of resonance events included in the g10 data was estimated from the difference between the simulation result of only the elementary process ($\gamma p \rightarrow K^+ \Lambda$ or $\gamma n \rightarrow K^0 \Lambda$) and the g10 data result of the squared missing mass of $\gamma p \rightarrow \Lambda X$.
- Then, scaling factors for current luminosities were calculated.

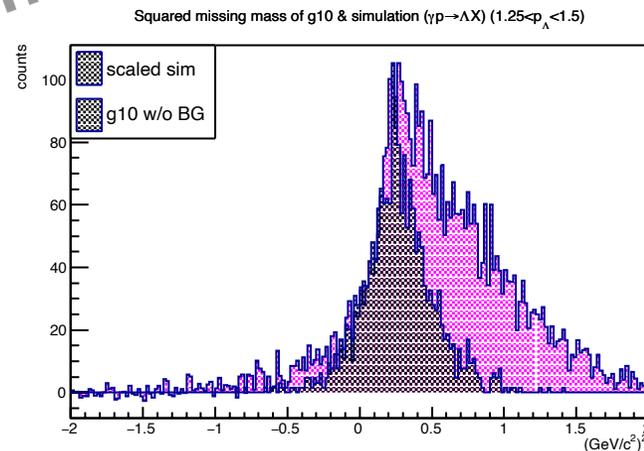
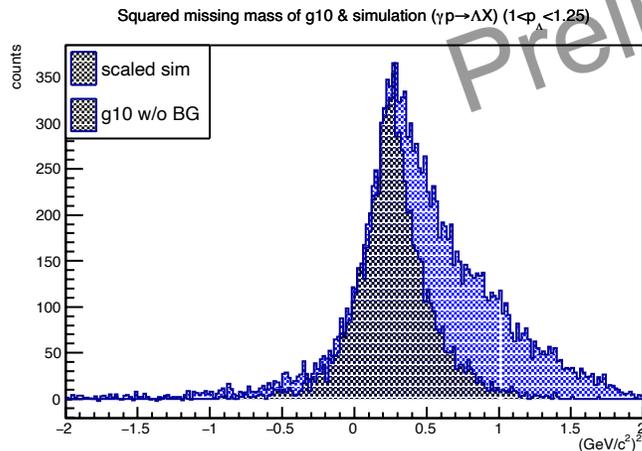


Simulation result of $\gamma p \rightarrow K^+ \Lambda$ or $\gamma n \rightarrow K^0 \Lambda$ reactions.

Original g10 spectrum (including Λ^* or K^* productions)

$$x_{lum} = \frac{N_{sim\ tot} + N_{reso}}{N_{sim\ tot}} + 1$$

Scaling factor for current Luminosity ↓

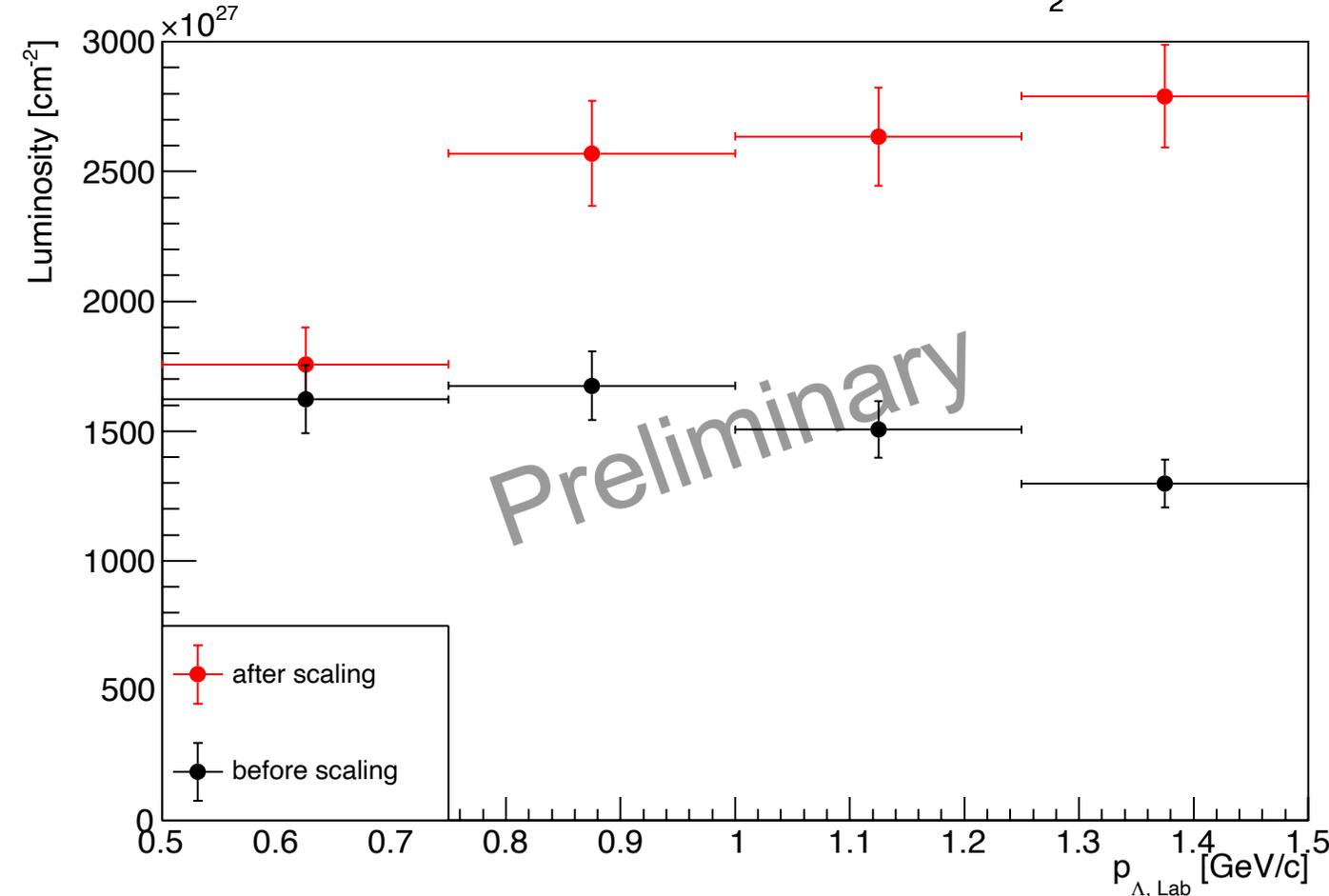


p_Λ bin (GeV/c)	$N_{sim\ tot}$	N_{reso}	x_{lum}
0.5 – 0.75	13705.6	1139.6	1.083
0.75 – 1.0	15210.0	8124.0	1.534
1.0 – 1.25	7538.4	5642.0	1.748
1.25 – 1.5	1898.9	2186.0	2.151

Estimation of resonance yield

- The luminosity of the Λ beam before and after correction is shown below.
- In this analysis, we used the corrected values represented by red dots to derive the cross-sections.

Luminosity for Λ s from proton & neutron (LD_2 target)



p_{Λ} bin (GeV/c)	L_{before} ($\times 10^{30} \text{ cm}^{-2}$)	Final Luminosity ↓ L_{after} ($\times 10^{30} \text{ cm}^{-2}$)
0.5 – 0.75	1.623 ± 0.131	1.758 ± 0.142
0.75 – 1.0	1.675 ± 0.132	2.570 ± 0.202
1.0 – 1.25	1.507 ± 0.108	2.634 ± 0.189
1.25 – 1.5	1.297 ± 0.921	2.790 ± 0.198

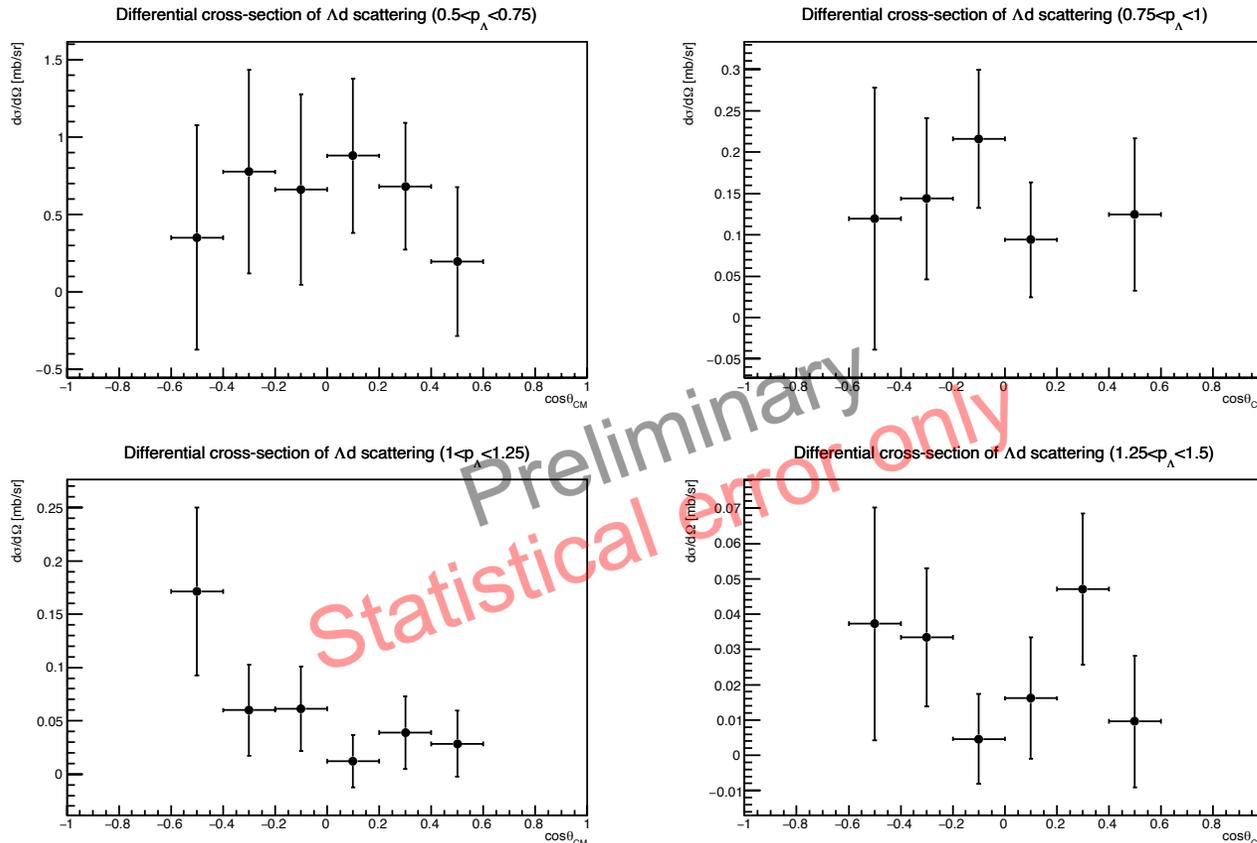
Cross-sections

Differential & Integrated cross-sections of Λd Scattering

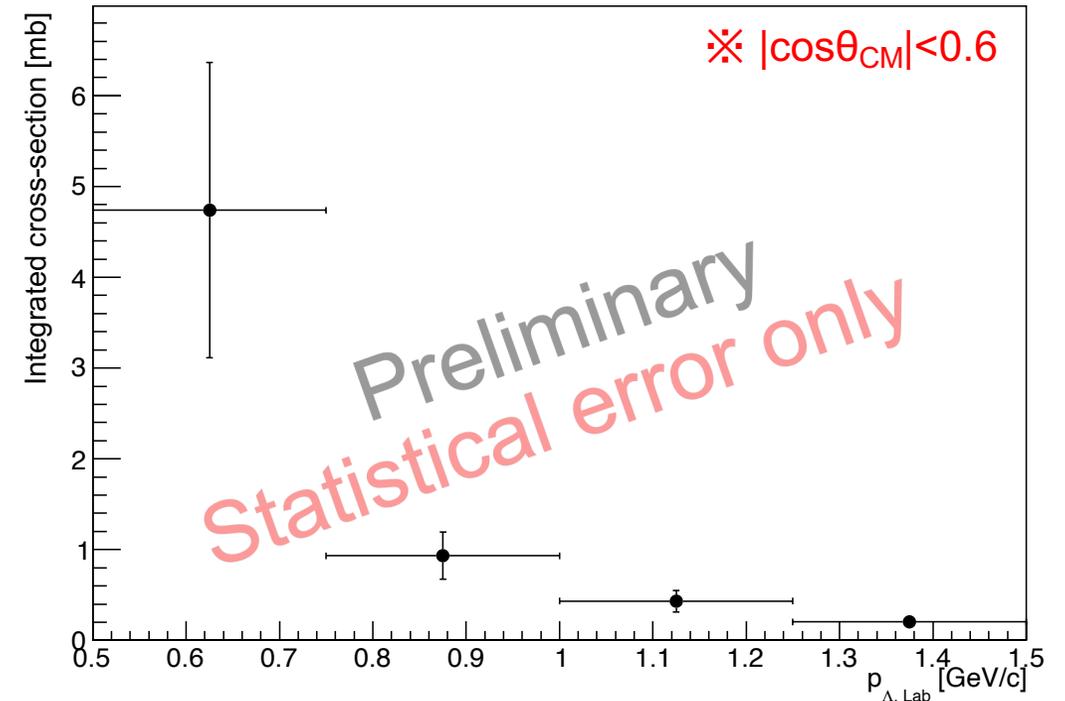
- Finally, the differential and integrated cross-sections in the $|\cos\theta_{CM}| < 0.6$ range were measured ($dp_{\Lambda} = 0.25 \text{ GeV}/c$, $d\cos\theta_{CM} = 0.2$).
- Systematic errors will be estimated by changing the angular distribution of Λd scattering in Geant4.
- The full analysis contents are currently summarized in a CLAS analysis note.

$$\left(\frac{d\sigma}{d\Omega}\right) = \frac{N_{\Lambda d} \cos\theta_{\Lambda' CM}}{\epsilon_{\cos\theta_{\Lambda' CM}} \cdot \tau \cdot L \cdot \Delta\Omega}$$

$$\sum_{\cos\theta_{CM}=-0.6}^{0.6} \frac{d\sigma}{d\Omega} = \frac{N_{\Lambda d} \Delta p}{\epsilon_{p_{\Lambda}} \cdot \tau \cdot L}$$



Integrated cross-section of Λd scattering



Preliminary
Statistical error only

Summary

- As a first step in knowing many-body BB interactions to solve the “Hyperon puzzle in Neutron Star, YNN data is essential. Therefore, we measured Λ d differential and integrated cross-sections.
- After 1st-level skimming (PID), Λ d events were selected
 - $|\Delta p| < 0.05$ GeV/c \rightarrow integrated cross-section
 - $|\cos\theta_{CM}| < 0.6 \rightarrow$ differential cross-section
- Efficiencies for differential & integrated cross-sections were estimated CLAS GSIM independently.
- Realistic Luminosity, which includes resonance events, was estimated using GSIM of elementary processes.
- The CLAS g10 dataset successfully measured Λ d differential and integrated cross-sections.
 - $E_\gamma : 1.2 - 2.4$ GeV, $p_\Lambda : 0.5 - 1.5$ GeV/c
 - $dp_\Lambda = 0.25$ GeV/c, $d\cos\theta_{CM} = 0.2$
 - Integrated cross-section = 0.1 ~ 5 mb in the scattering angular range of $|\cos\theta_{CM}| < 0.6$
 - Systematic errors will be estimated soon
 - The CLAS analysis note is almost ready.