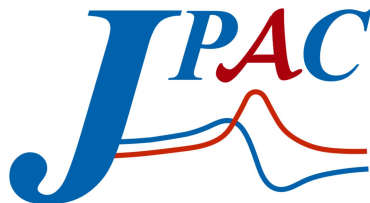


# Heavy meson spectroscopy in photoproduction



Daniel Winney  
Bonn University - HISKP

PWA 13 / ATHOS 8  
29 May 2024

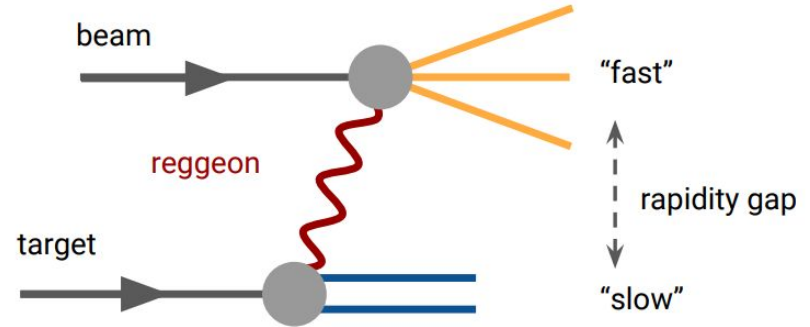


# Photoproduction

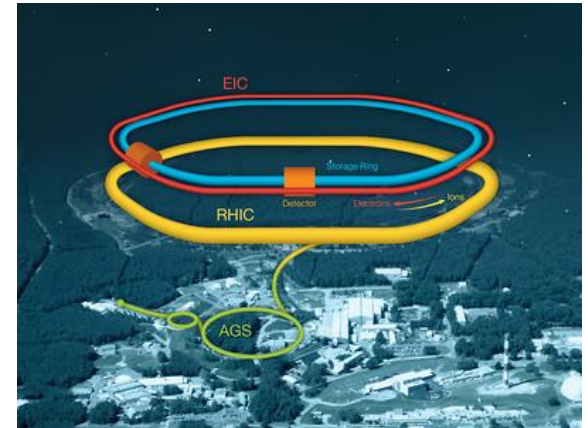
Powerful tool in spectroscopy

- Can produce any quantum-numbers
- Well understood in terms of diffractive production (**exchange physics**)
- Constrained kinematics means precise probe of production mechanism
- Polarization information gives useful insight into structure
- Minimizes role of rescattering

JPAC [Phys.Rev.D 98 (2018) 3, 034020]



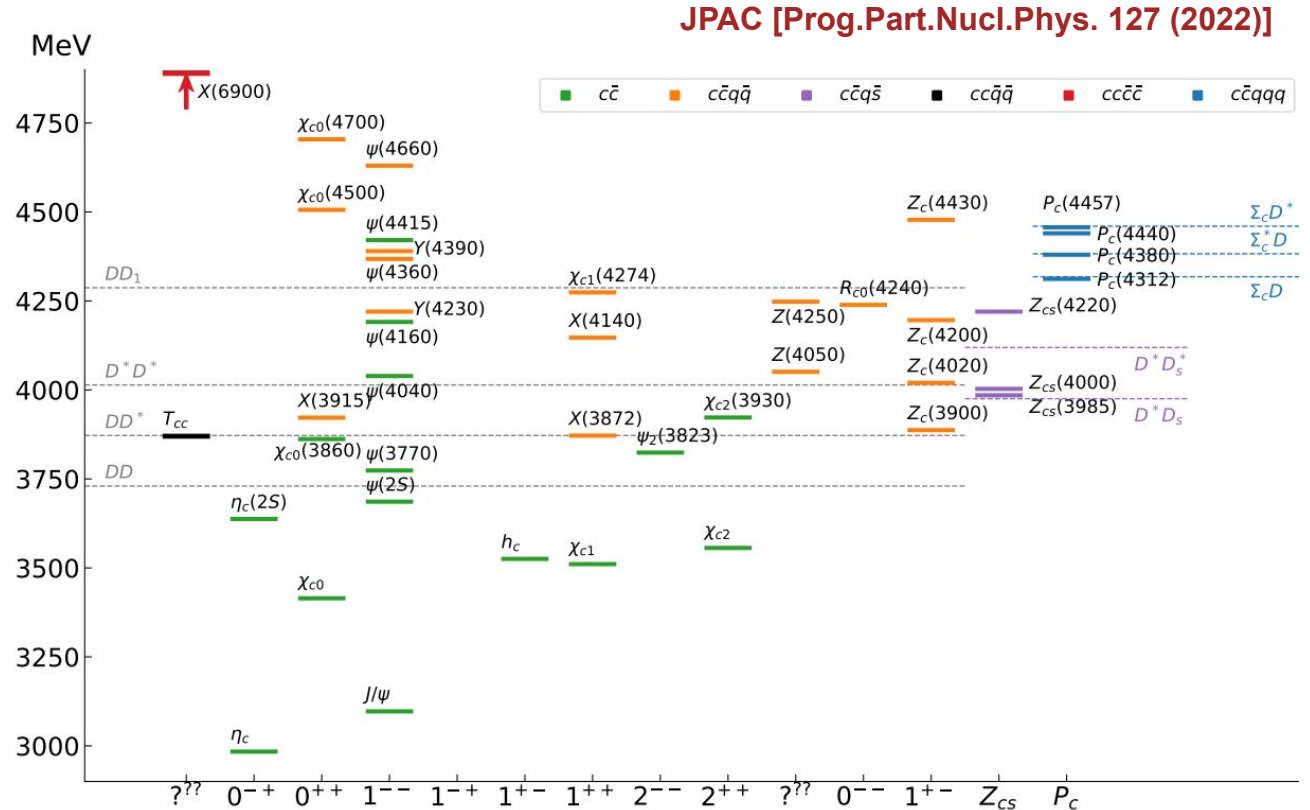
EIC Yellow Report [arXiv:2103.05419]



# Exotic XYZ states

Rich spectrum of resonance-like signals observed in heavy baryon decays and electron-positron collisions.

Seemingly consistent with structure **beyond  $Q\bar{Q}$** .



# Exotic XYZ states

Precise microscopic nature inconclusive, with multiple possible interpretations in terms of QCD degrees of freedom.

Coincidence of nearby multiparticle thresholds may suggest important **multi-channel dynamics**.

Understanding of many as shallow bound states with prominent molecular component from open-charm

$$a = -\frac{2X}{1+X}R + \mathcal{O}(m_\pi^{-1}) \quad r = -\frac{1-X}{X}R + \mathcal{O}(m_\pi^{-1})$$

Li et al [arXiv:2110.02766]

Albaladejo and Nieves [arXiv:2203.04864]

See reviews:

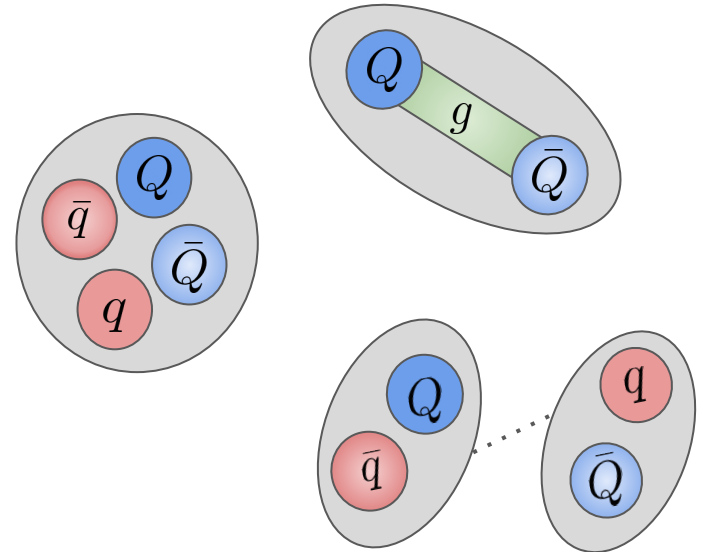
JPAC [Prog.Part.Nucl.Phys. 127 (2022)]

Chen et al [Rept. Prog. Phys. 86 (2023) no.2, 026201]

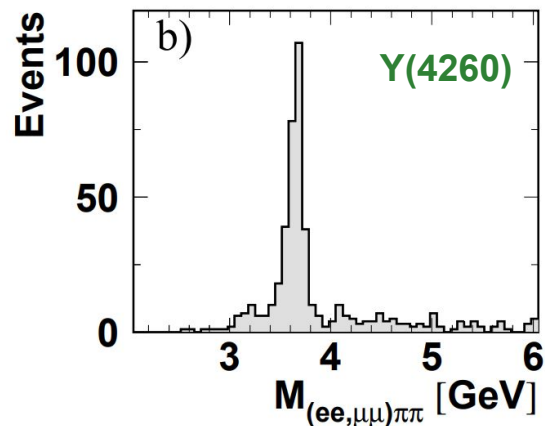
Brambilla et al [Phys.Rept. 873 (2020) 1-154]

Guo et al [Rev.Mod.Phys. 90 (2018) 1, 015004]

Esposito et al [Phys.Rept. 668 (2017) 1-97]



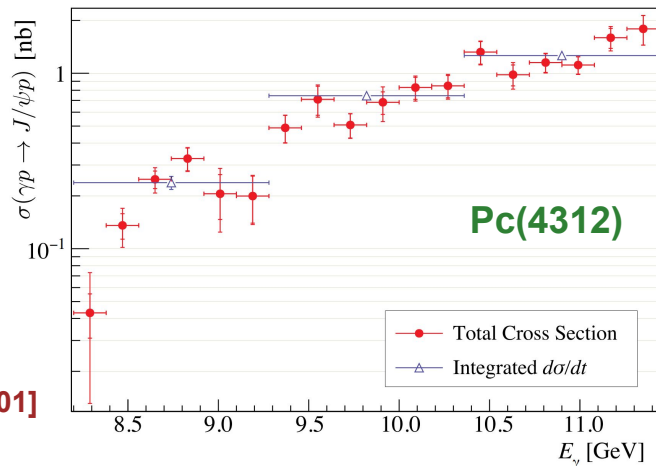
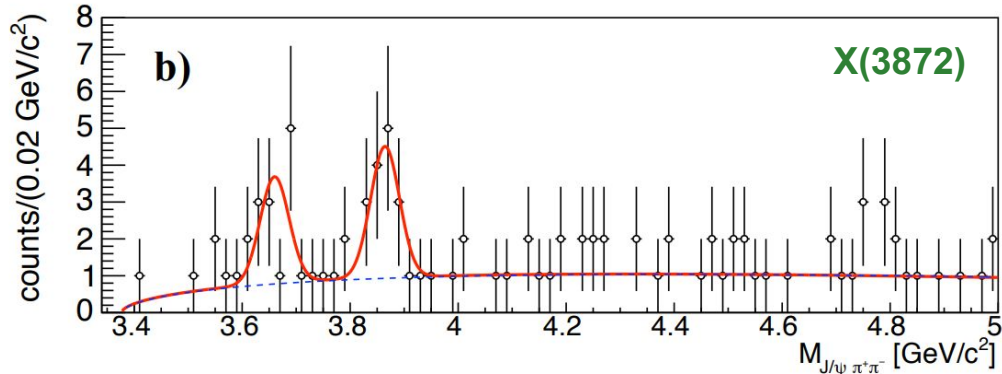
# Photoproduction searches



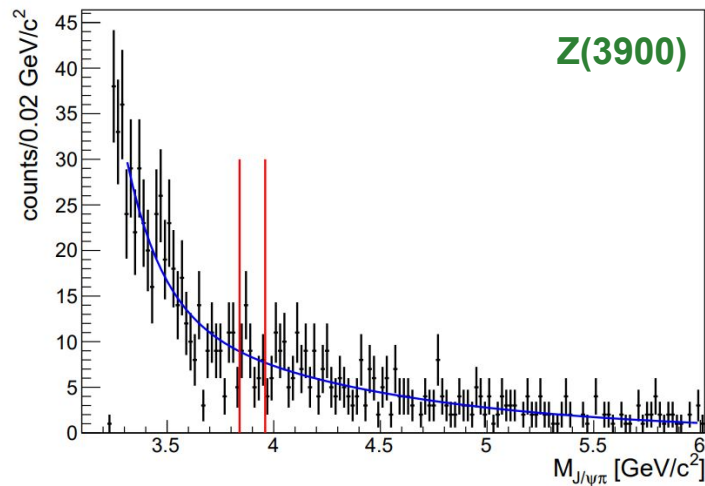
H1 [Phys.Lett.B 541 (2002) 251-264]

GlueX [Phys.Rev.C 108 (2023) 2, 025201]

COMPASS [Phys.Lett.B 783 (2018) 334-340]



COMPASS [Phys.Lett.B 742 (2015) 330-334]



# Proton structure

Potential probe of gluonic contributions to proton mass by mimicking spin-2 graviton current

- Gravitational form factors

Mamo & Zahed [Phys. Rev. D 101, 086003 (2020)]

Guo, Ji & Liu [Phys. Rev. D 103, 096010 (2021)]

- Mass radius

Kharzeev [Phys. Rev. D 104, 054015 (2021)]

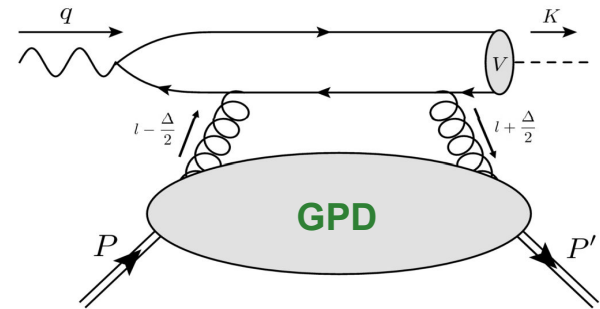
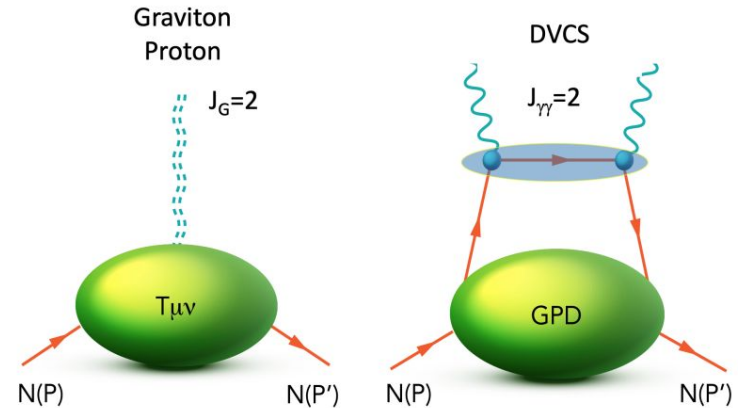
Mamo & Zahed [Phys. Rev. D 103, 094010 (2021)]

- Trace anomaly contribution to proton mass

Wang, Chen, & Evslin [Eur.Phys.J.C 80 (2020) 6, 507]

Hatta & Yang [Phys. Rev. D 98, 074003 (2018)]

V.D. Burkert, L. Elouadrhiri, F.X. Girod [arXiv:2310.11568]

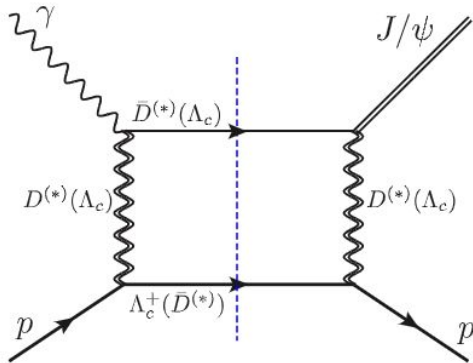


# Exclusive photoproduction

Expected dominant production modes relying on measured branching fractions. Minimal assumption on microscopic nature.

Can consider broad energy range. **Near-threshold** production dominated by meson exchanges while high-energy production proceeds through Reggeon exchanges.

Largest uncertainty comes from use of VMD.

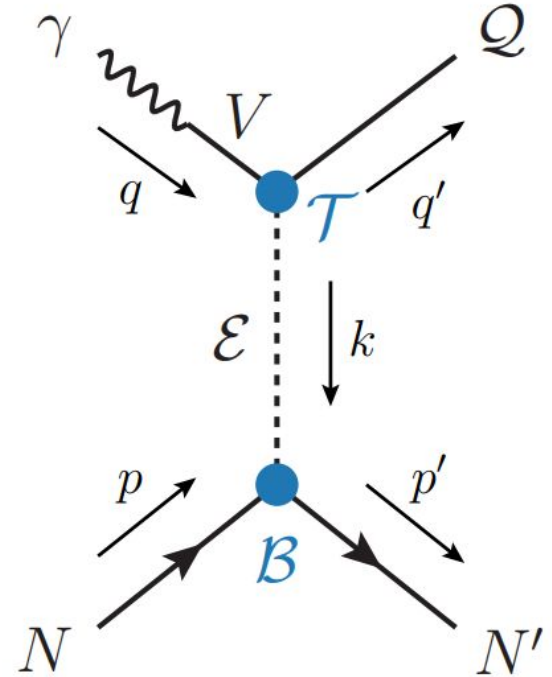


Xu et al [Eur.Phys.J.C 81 (2021) 10, 895]

Ignores possible more complicated production modes which may contribute

Du et al [Eur.Phys.J.C 80 (2020) 11, 1053]

JPAC [Phys. Rev. D 102, 114010 (2020)]



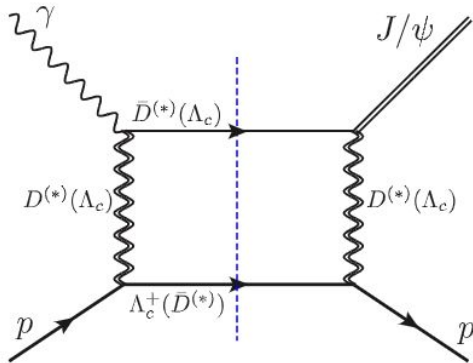
# Exclusive photoproduction

Expected dominant production modes relying on measured branching fractions. Minimal assumption on microscopic nature.

Can consider broad energy range. **Near-threshold** production dominated by meson exchanges while high-energy production proceeds through

Largest un

Baseline for production by assuming phenomenology the same as in light sectors.

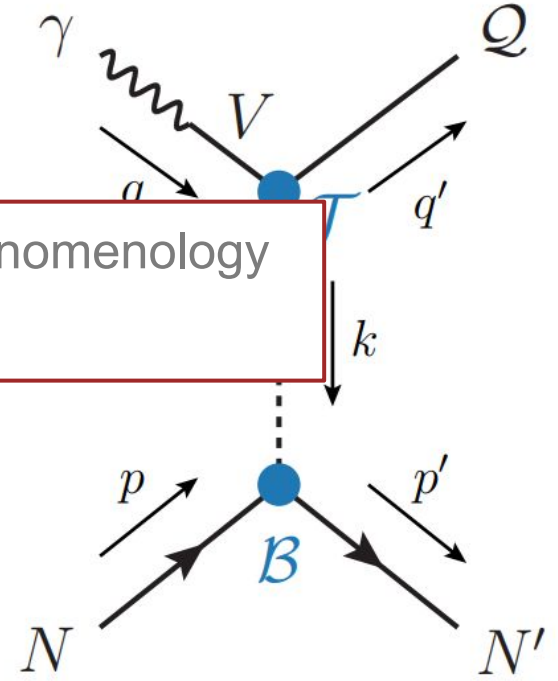


Xu et al [Eur.Phys.J.C 81 (2021) 10, 099]

Ignores possible more complicated production modes which may contribute

Du et al [Eur.Phys.J.C 80 (2020) 11, 1053]

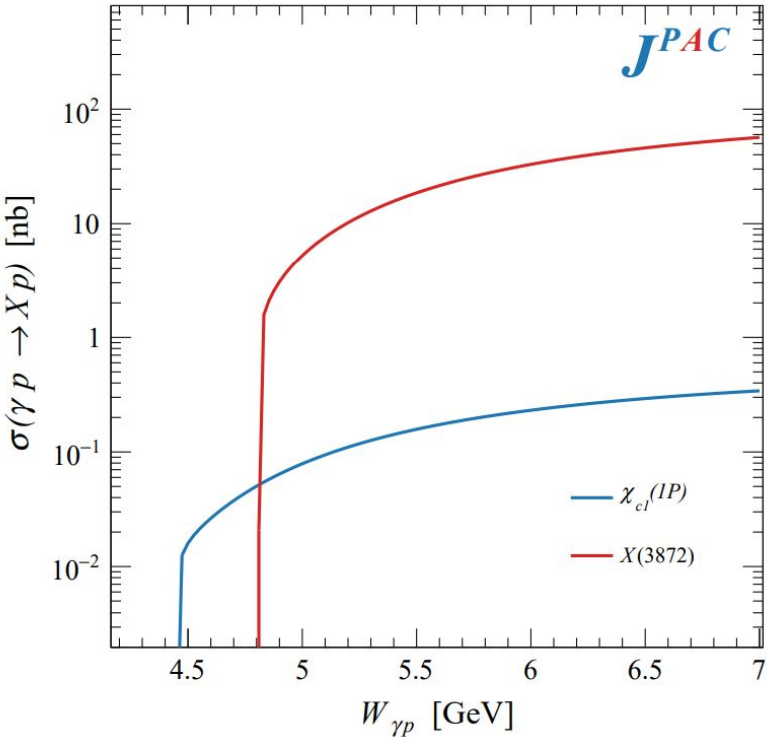
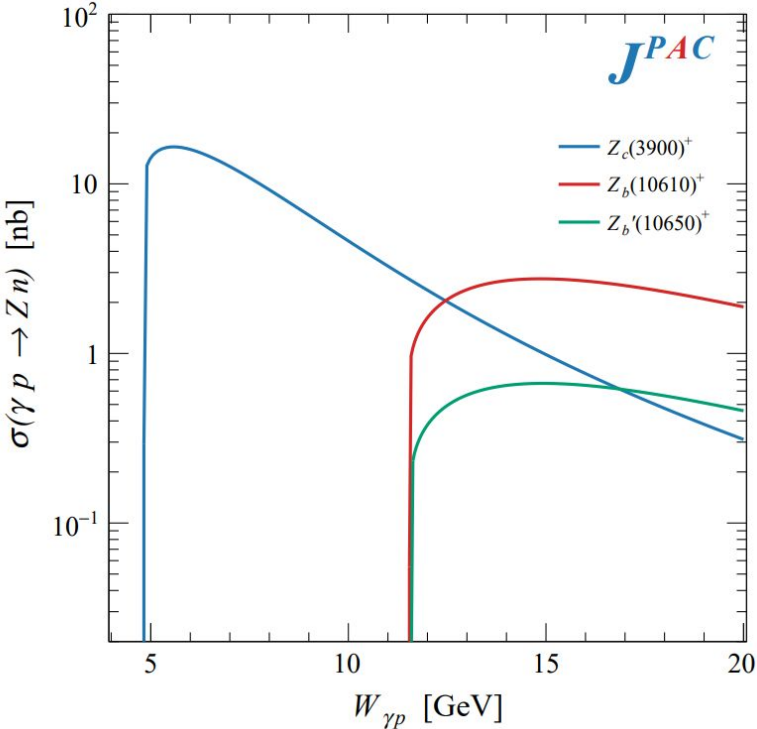
JPAC [Phys. Rev. D 102, 114010 (2020)]



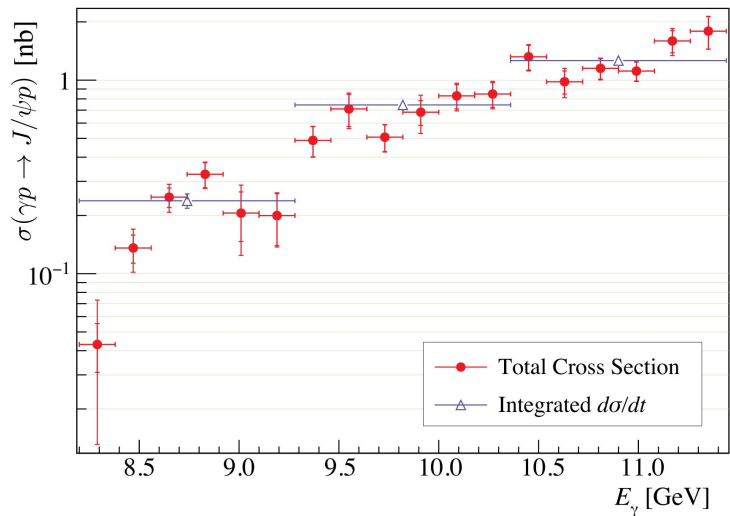


# Exclusive photoproduction

Near-threshold production seems very promising for X(3872) and Z states



# J/ψ at GlueX

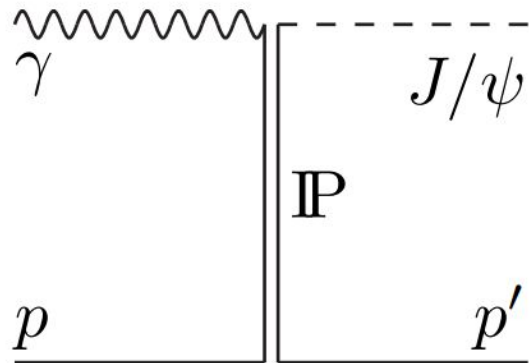
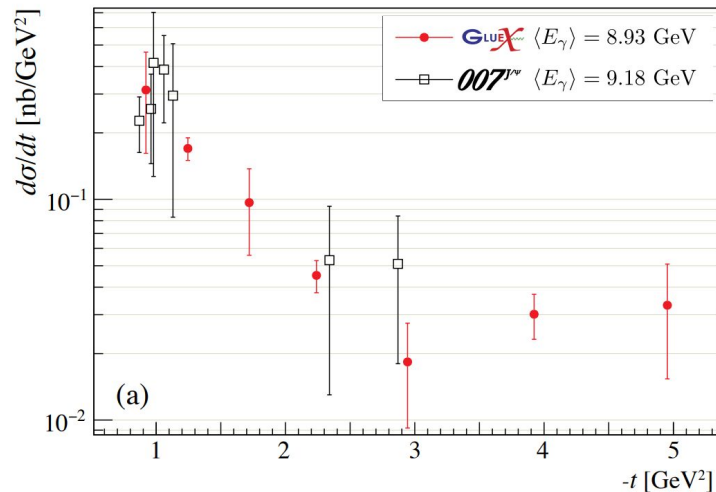


**007<sup>J/ψ</sup>**

[Nature 615 (2023) 7954, 813-816]

**GLUEX**

[Phys.Rev.C 108 (2023) 2, 025201]

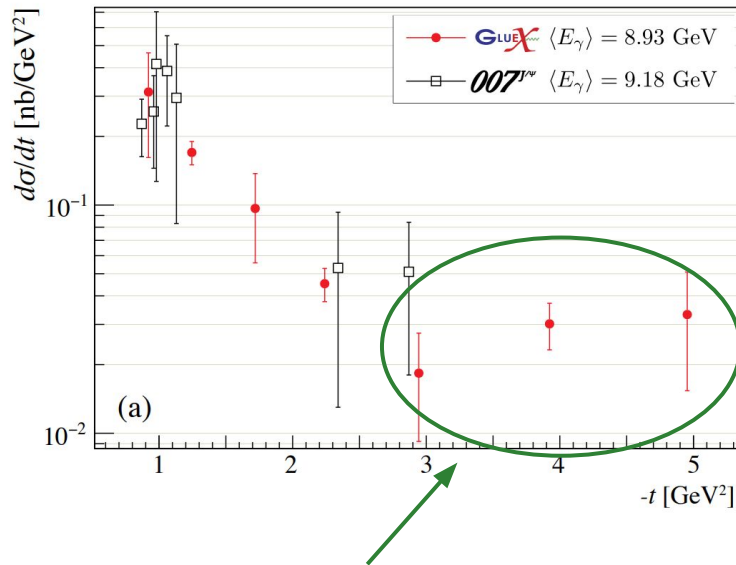
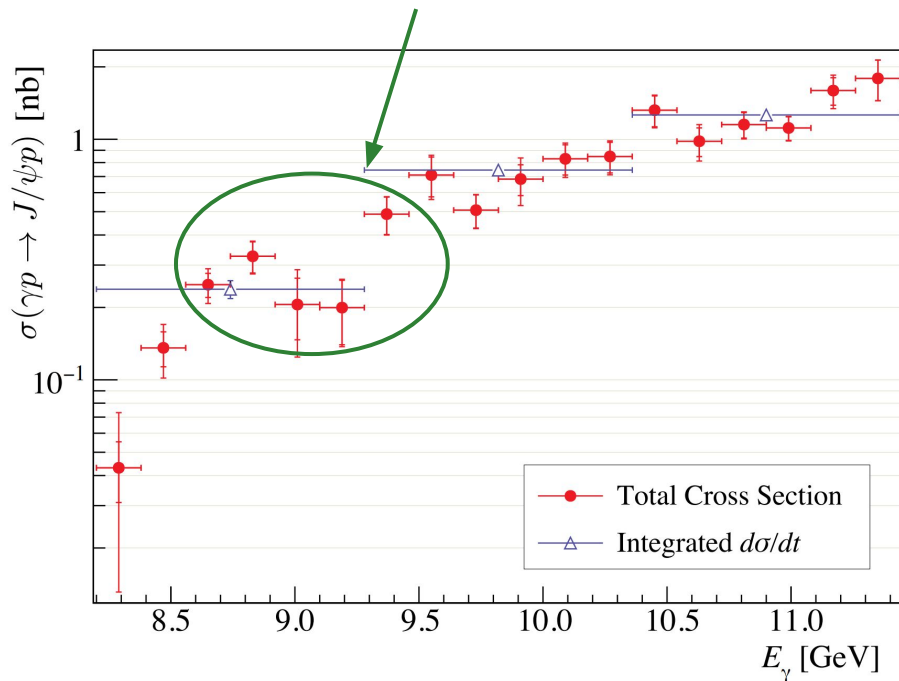


Much larger data set available, incorporating both integrated and differential cross sections.

The latter at from GlueX covers the **full kinematic range**

# J/ $\psi$ at GlueX

“Dip” now established at  $\sim 2.6\sigma$  compared to a smooth fit



Flattening of  $t$ -distribution at large momentum transfer also at  $\sim 2.3\sigma$  compared to a dipole

**Coupled-channels? Pentaquarks?**

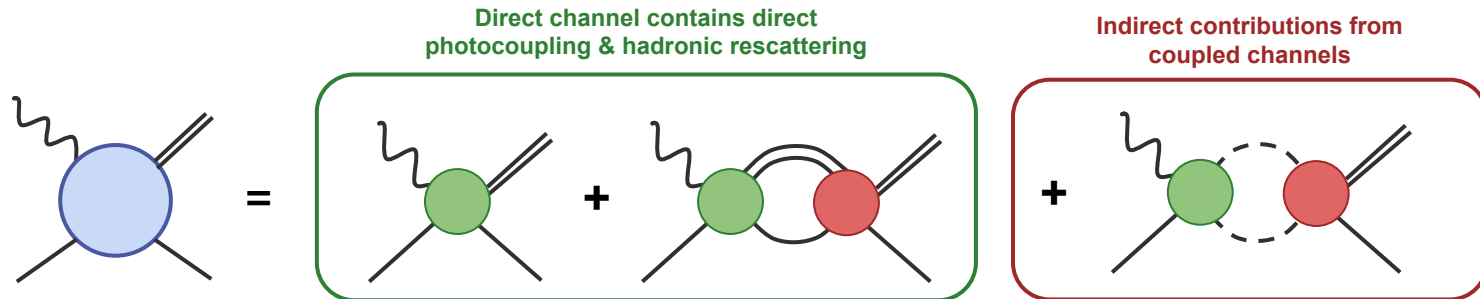
# K-matrix analysis

Larger data set allows more comprehensive analysis in terms of **s-channel partial waves**.

Expansion close to threshold, allows us to use finitely many partial waves, consistent with **coupled-channel unitarity**

$$F(s, t) = \sum_{\ell} (2\ell + 1) P_{\ell}(\cos \theta) F_{\ell}(s)$$

$$\left. \begin{array}{l} \text{Im } F_{\ell} = F_{\ell} \rho T_{\ell}^{\dagger} \\ \text{Im } T_{\ell} = T_{\ell} \rho T_{\ell}^{\dagger} \end{array} \right\} \longrightarrow F_{\ell} = f_{\ell} (1 - G T_{\ell}) \quad \text{with} \quad T_{\ell} = \frac{1}{K_{\ell}^{-1} + G}$$



# K-matrix analysis

## ~~Limitations:~~ Advantages:

- **Not a microscopic model**

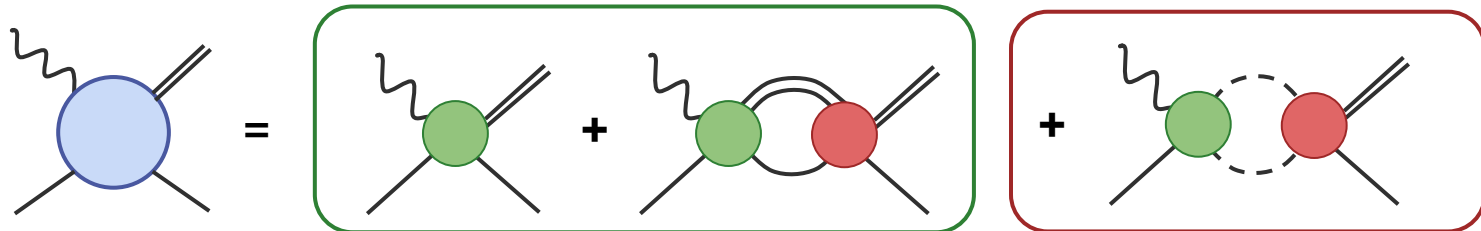
We don't incur model uncertainty from having to assume dynamics. Model fully analytic and describes entire kinematic range. Depends only on # of terms in PWE and in NTE.

**Systematics testable a posteriori.  $L \leq 3$  and effective range work well**

- **Each partial wave must be parameterized independently**

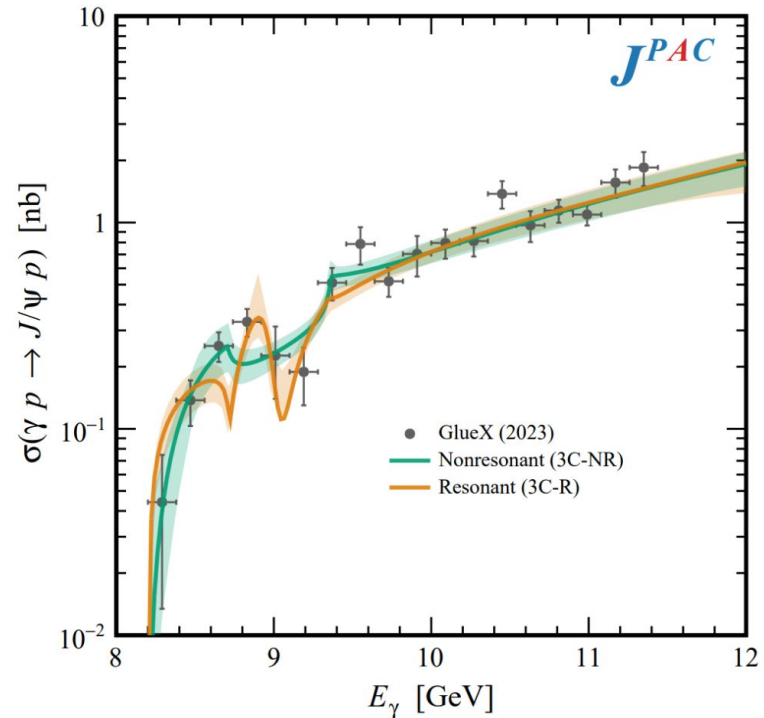
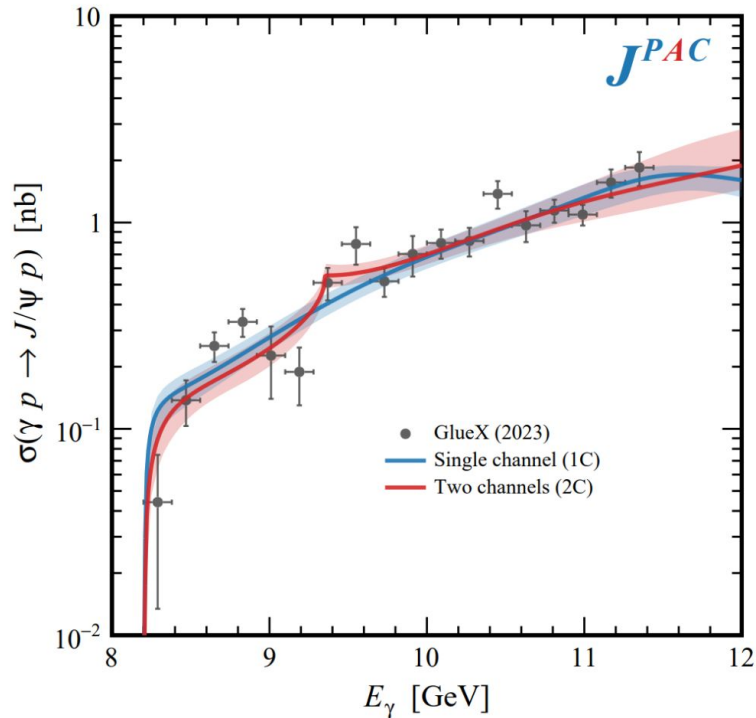
**Production and rescattering entirely unconstrained except by unitarity.**

$$K_S^{ij} = \alpha_S^{ij} + \beta_S^i q_i^2 \delta_{ij} \quad f_\ell = (pq)^\ell n_\ell$$



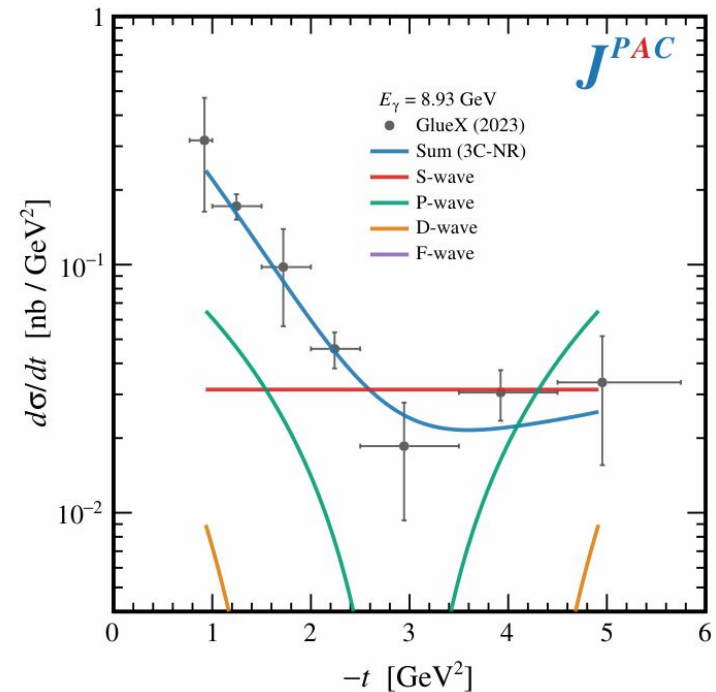
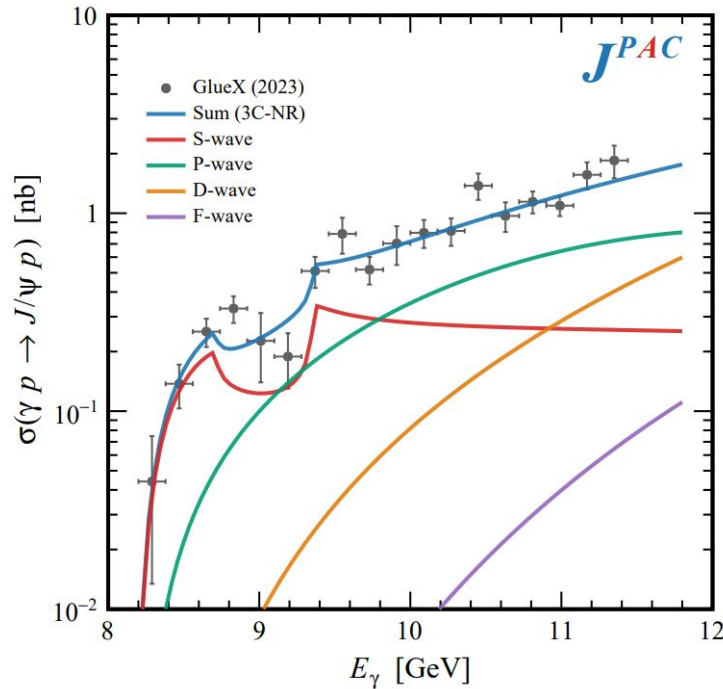
# Integrated cross section

**Four solutions** with different dynamical pictures found to be consistent with full data with similar statistical significance.



# Differential cross section

Exponential  $t$  behavior captured with only a **few partial waves** (completely analytic in  $t$ )



# Extract dynamics

Unitary amplitude allows us to extract quantities that characterize the interaction with minimal assumption

**Elastic scattering length:** 
$$T_S^{\psi p, \psi p} = \frac{8\pi \sqrt{s_{\text{th}}}}{-a_{\psi p}^{-1} - i q} + O(q^2) \quad \sim O(1 \text{ fm})$$

**Inelasticity:** 
$$\zeta_{\text{th}} = \frac{|F_{\text{direct}}^{\psi p}(s_{\text{th}})|}{|F_{\text{direct}}^{\psi p}(s_{\text{th}})| + |F_{\text{indirect}}^{\psi p}(s_{\text{th}})|} > 25\%$$

**Pentaquark poles:**

One (3C) solution found with a narrow S-wave pole

$$M = 4211 \text{ MeV} \quad \Gamma = 48 \text{ MeV}$$



# Extract dynamics

Unitary amplitude allows us to extract quantities that characterize the interaction with minimal assumption

**Elastic scattering:**  $\sigma_{\text{th}} = 8\pi \sqrt{s_{\text{th}}} |F_{\text{direct}}^{\psi p}(s_{\text{th}})|^2$

Need predictions and measurements of polarized observables!

**Inelasticity:**  $\zeta_{\text{th}} = \frac{|F_{\text{direct}}^{\psi p}(s_{\text{th}})|^2}{|F_{\text{direct}}^{\psi p}(s_{\text{th}})|^2 + |F_{\text{indirect}}^{\psi p}(s_{\text{th}})|^2} > 25\%$

**Pentaquark poles:**

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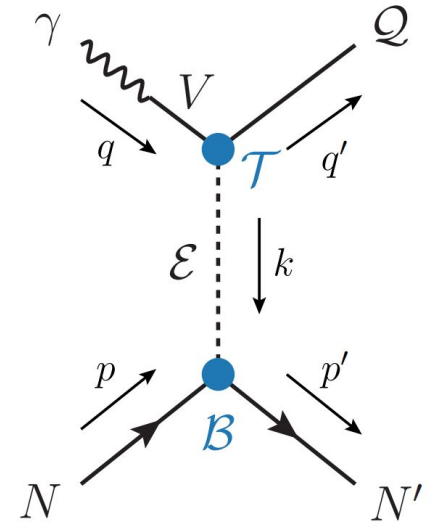
$$M = 4211\text{MeV} \quad \Gamma = 48\text{MeV}$$

# Vector meson dominance

K-matrix formalism allows us to extract the **elastic  $J/\psi p$  amplitude** directly (obeying unitarity). Define test ratio to check the validity of the VMD assumption:

$$R_{\text{VMD}}(x) = \left| \frac{F^{\psi p}(s_{\text{th}}, x) / g_{\gamma\psi}}{T^{\psi p, \psi p}(s_{\text{th}}, x)} \right|$$

VMD found to underestimate elastic scattering by **2 orders of magnitude** in all cases except those containing a nearby pole!



<b>1C</b>	$[0.45, 0.73] \times 10^{-2}$	$[1.3, 2.0] \times 10^{-2}$
<b>2C</b>	$[0.39, 1.69] \times 10^{-2}$	$[1.3, 5.1] \times 10^{-2}$
<b>3C-NR</b>	$[0.03, 1.74] \times 10^{-2}$	$[0.08, 8.9] \times 10^{-2}$
<b>3C-R</b>	$[1.4 \times 10^{-2}, 0.58]$	$[5.4 \times 10^{-2}, 1.8]$

# In defense of VMD

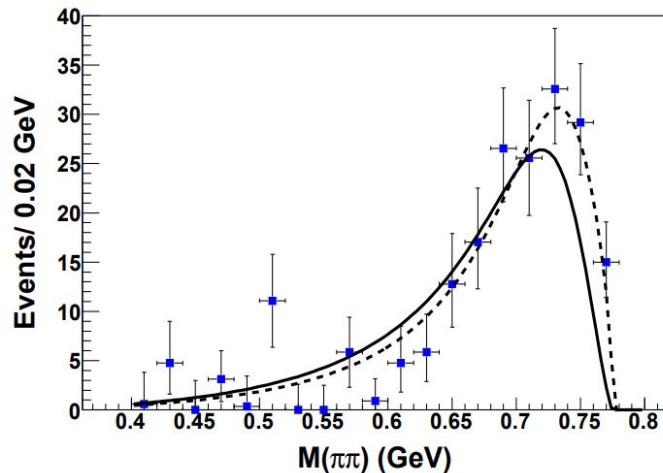
The X(3872) observed in purely hadronic and photonic modes gives us unique clue to efficacy of VMD.

Model both by same Lagrangian (compare apples to apples)

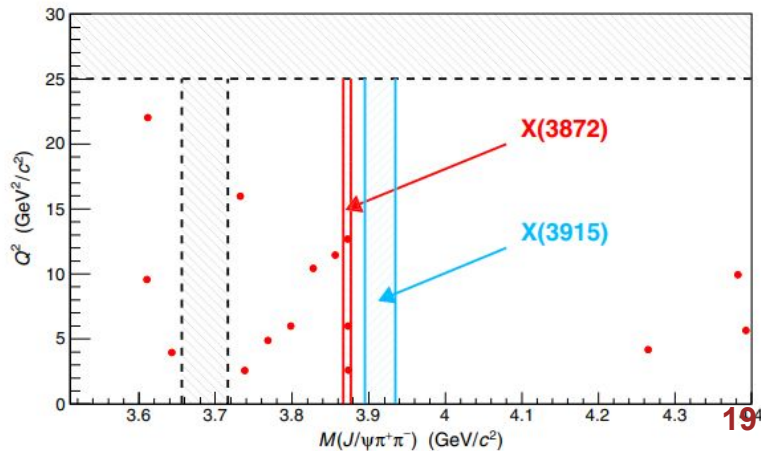
$$\mathcal{L}_{Q\gamma\gamma^*} = \frac{1}{2} \frac{g_{Q\gamma\gamma^*}}{m_Q^2} \epsilon_{\alpha\beta\mu\nu} F^{\alpha\beta} \partial_\sigma F^{\sigma\mu} Q^{*\nu}$$

VMD predicts relations between two-photon, radiative, and hadronic couplings

$g_{Q\gamma\gamma} = \sum_i \frac{g_{Q\gamma i\gamma}}{\gamma_i}$			
$g_{Q\gamma\mathcal{E}} = \sum_V \frac{g_{QV\mathcal{E}}}{\gamma_V}$	VMD 1	$ g_{X\gamma\rho} $	$ g_{X\gamma\omega} $
	VMD 2	0.088	0.199
	VMD 3	0.058	0.199
$g_{\gamma NN} = \sum_{\mathcal{E}} \frac{g_{\mathcal{E}NN}}{\gamma_{\mathcal{E}}}$		0.088	0.303



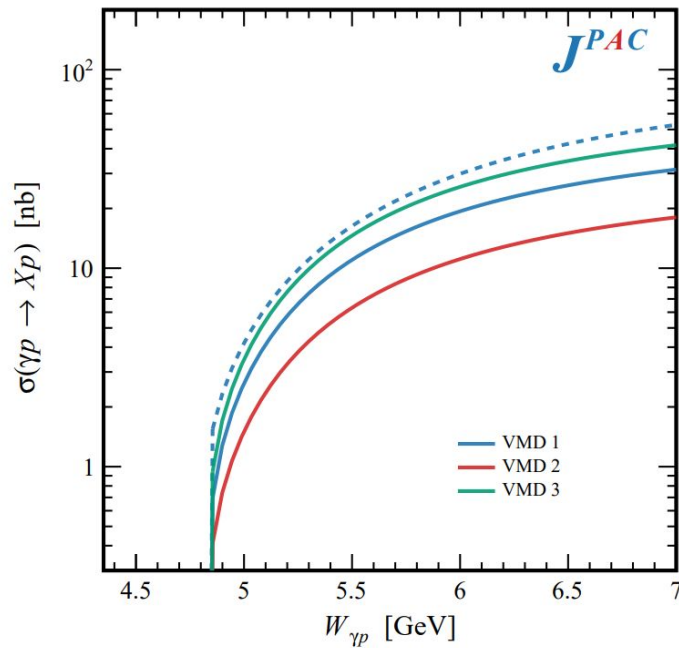
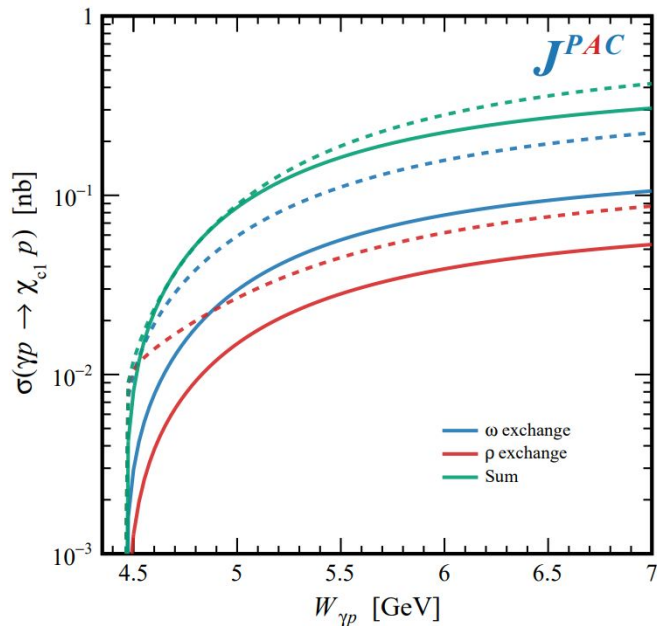
Belle [Phys.Rev.D 84 (2011) 052004,  
Phys.Rev.Lett. 126 (2021) 12, 122001]



# In defense of VMD

Alternatively go the other way, use the fully determined photon exchange amplitude to re-predict the hadronic exchange.

$$\langle \lambda_\gamma, \lambda_N | T \mathcal{E} | \lambda_Q, \lambda_{N'} \rangle = T_{\lambda_\gamma, \lambda_{\gamma^*} = \lambda_Q}^\mu \eta \mathcal{E} \left[ \frac{-g_{\mu\nu}}{t - m_\mathcal{E}^2} \right] \eta \mathcal{E} \beta_\mathcal{E}(t') \mathcal{B}_{\lambda_N, \lambda_{N'}}^\nu$$



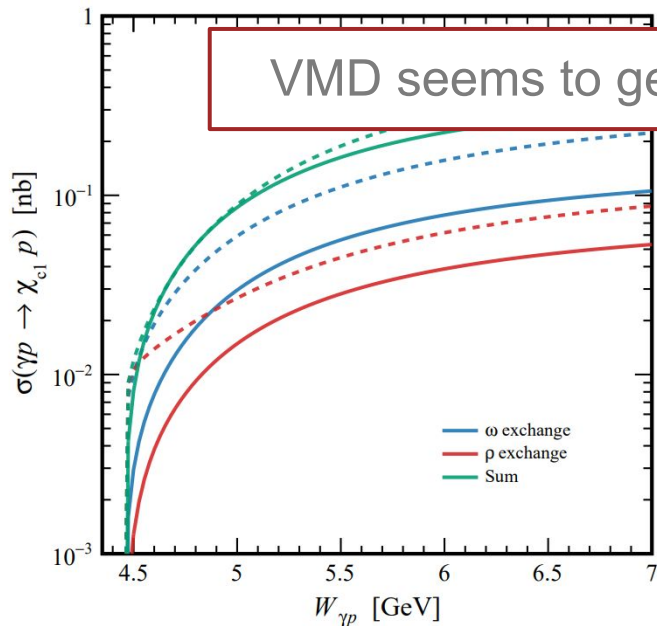
Rescaling electromagnetic form factors of the with VMD consistent with our original prediction without any knowledge of the X(3872) hadronic coupling

Why does VMD seem to work okay in some sectors but not others? Are there other processes we can look at to test VMD in charm?

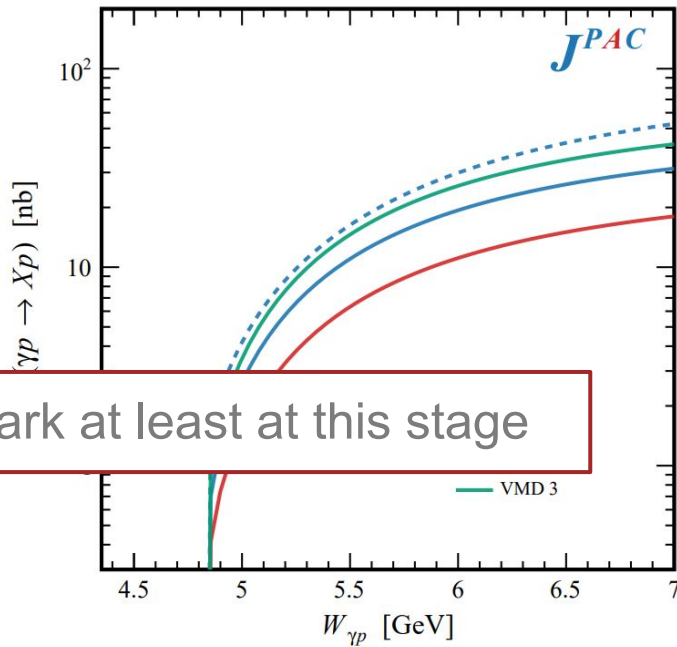
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$$\langle \lambda_\gamma, \lambda_N | T \mathcal{E} | \lambda_Q, \lambda_{N'} \rangle = \mathcal{T}_{\lambda_\gamma, \lambda_{\gamma^*} = \lambda_Q}^\mu \eta_\varepsilon \left[ \frac{-g_{\mu\nu}}{t - m_\varepsilon^2} \right] \eta_\varepsilon \beta_\varepsilon(t') \mathcal{B}_{\lambda_N, \lambda_{N'}}^\nu$$



VMD seems to get us in the ballpark at least at this stage



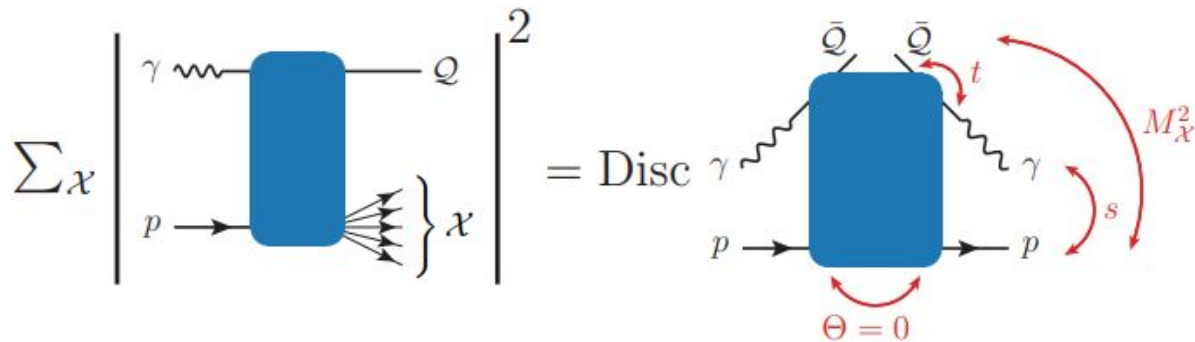
Rescaling electromagnetic form factors of the with VMD consistent with our original prediction without any knowledge of the X(3872) hadronic coupling

Why does VMD seem to work okay in some sectors but not others? Are there other processes we can look at to test VMD in charm?

# Semi-inclusive production

Expected larger cross-sections, potentially useful for **first observation**.

Exclusive exchange reactions extendable to semi-inclusive final states via generalized optical theorem.



$$E_Q \frac{d^3\sigma}{d^3q_f} = \frac{K}{16\pi^3} \frac{1}{2} \sum_{\lambda_\gamma \lambda_Q} |\mathcal{T}_{\lambda_\gamma \lambda_Q}|^2 \mathcal{P}_\pi^2 \sigma_{\text{tot}}^{\pi^* N}$$

phase-space factors  $\rightarrow$   $\frac{K}{16\pi^3} \frac{1}{2}$   
 pion propagator  $\rightarrow$   $\mathcal{P}_\pi^2$   
 total hadronic cross-section  $\rightarrow$   $\sigma_{\text{tot}}^{\pi^* N}$   
 $\pi\gamma Q$  coupling  $\rightarrow$   $|\mathcal{T}_{\lambda_\gamma \lambda_Q}|^2$

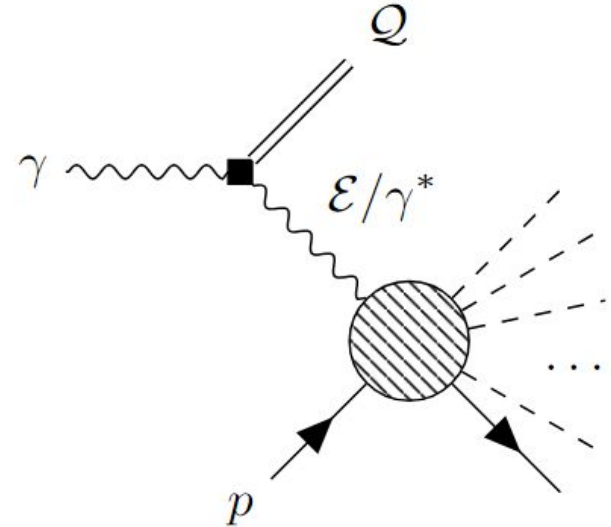
Spineless  $\pi$  exchange factorizes to very simple form in terms of  $\pi N$  total cross section!

# Semi-inclusive production (with spin)

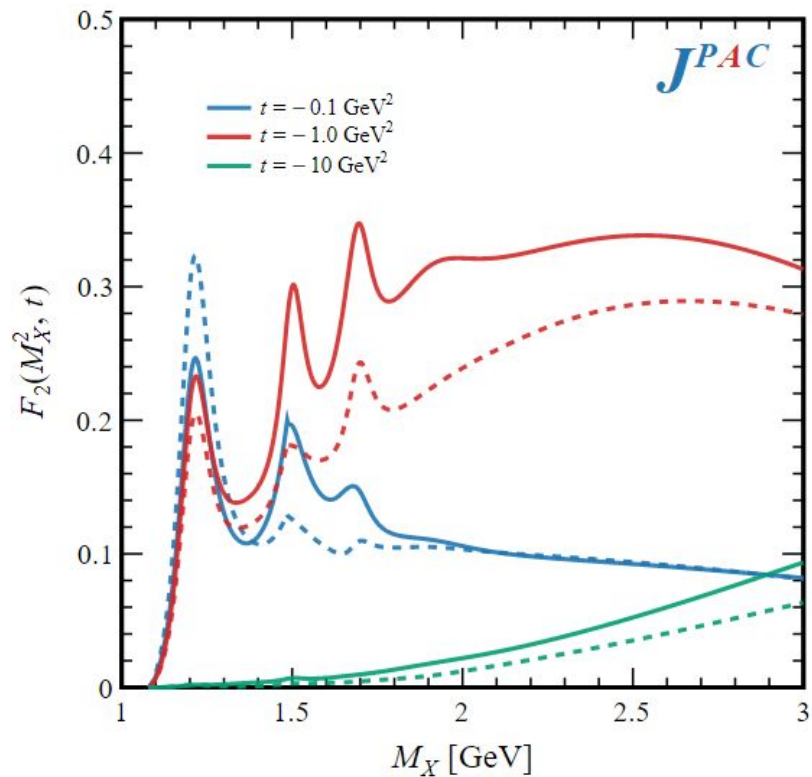
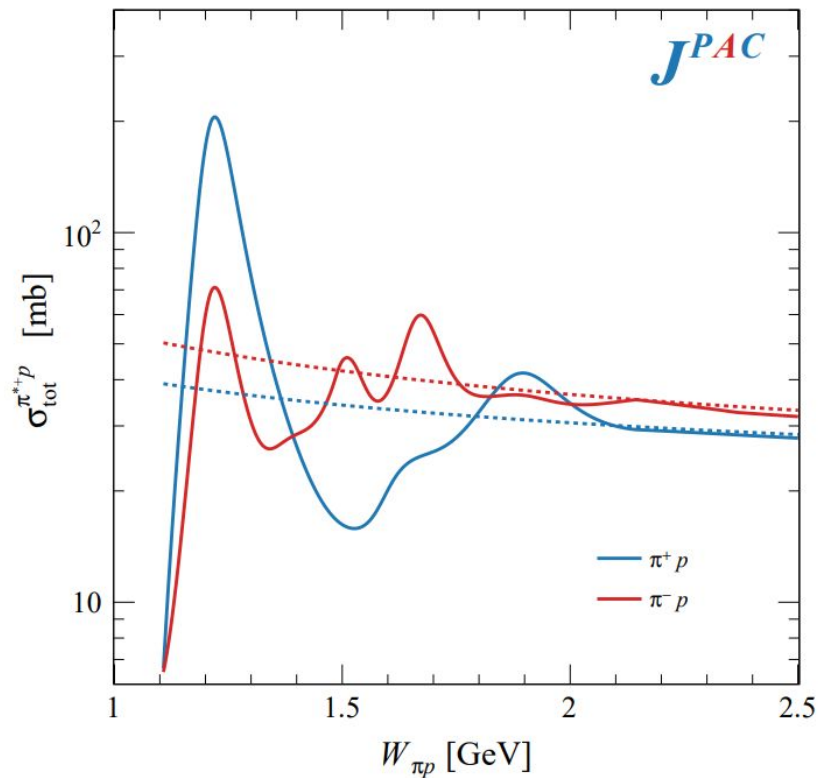
Spin-exchange processes like  $\omega$  exchange require knowledge of **polarized  $\omega$ N cross sections**...

Potential solution is using the apparent success of rescaling electromagnetic form factors to relate to semi-inclusive structure functions!

$$\frac{d^2\sigma}{dt dM_X^2} = \sum_{\varepsilon} \frac{\overset{\text{VMD}}{\alpha \eta \varepsilon^4}}{2 (2\sqrt{s} E_{\gamma})^2} \underset{\text{V}\gamma\text{X coupling}}{\mathcal{T}_{\gamma Q}^{\mu\nu}} \overset{\text{scalar propagator}}{|\beta_{\varepsilon} \mathcal{P}_{\varepsilon}|^2} \underset{\text{Inclusive structure functions}}{W_{\mu\nu}}$$

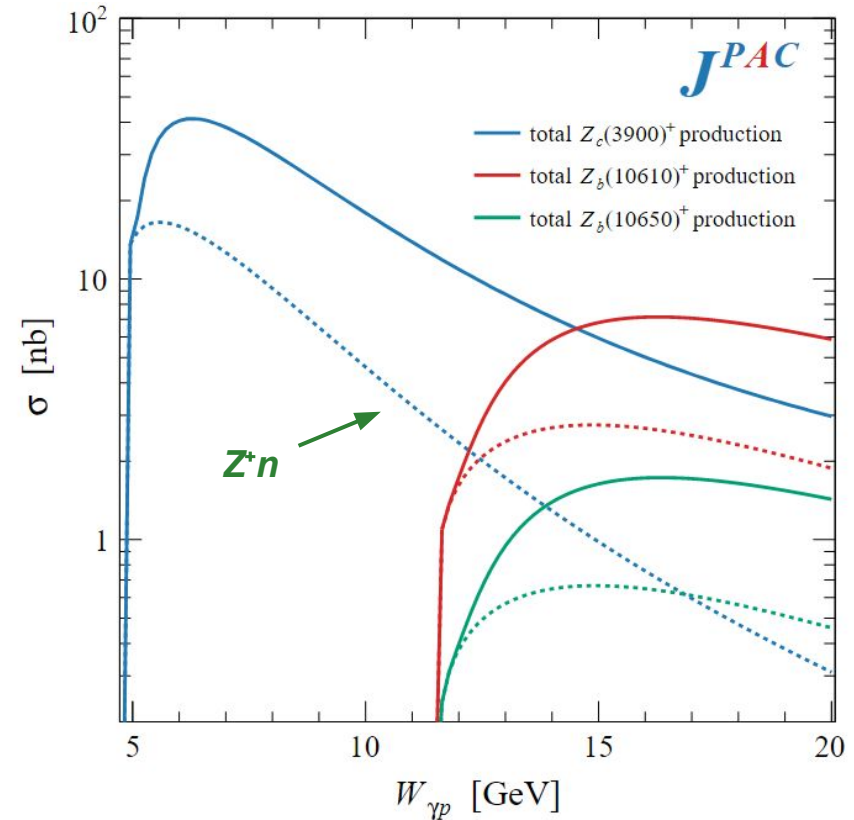
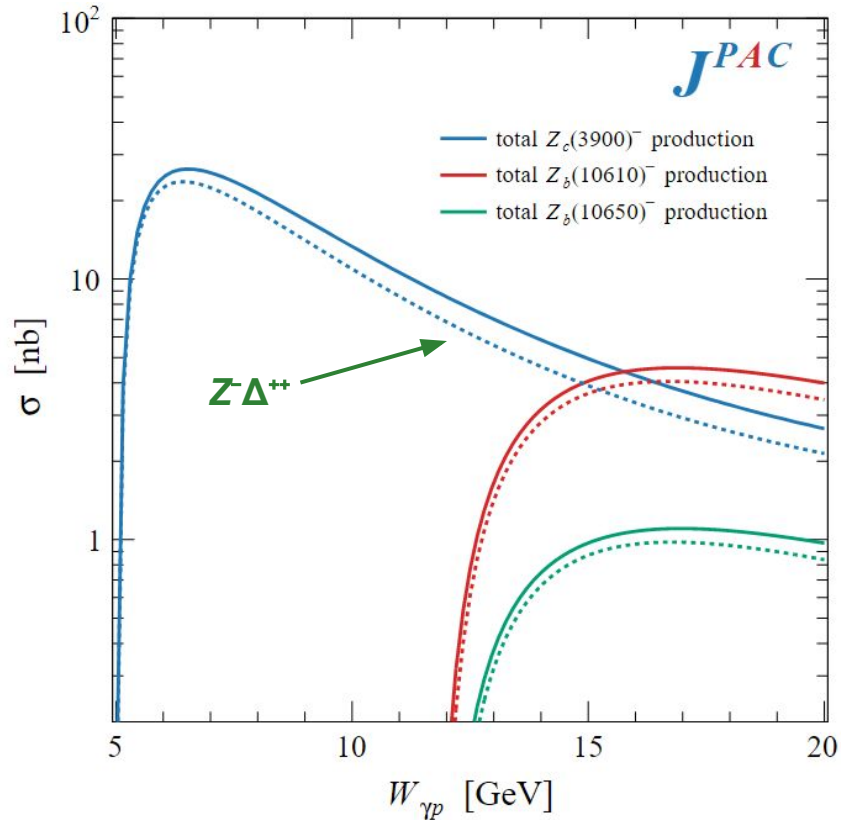


# Missing mass in resonance region

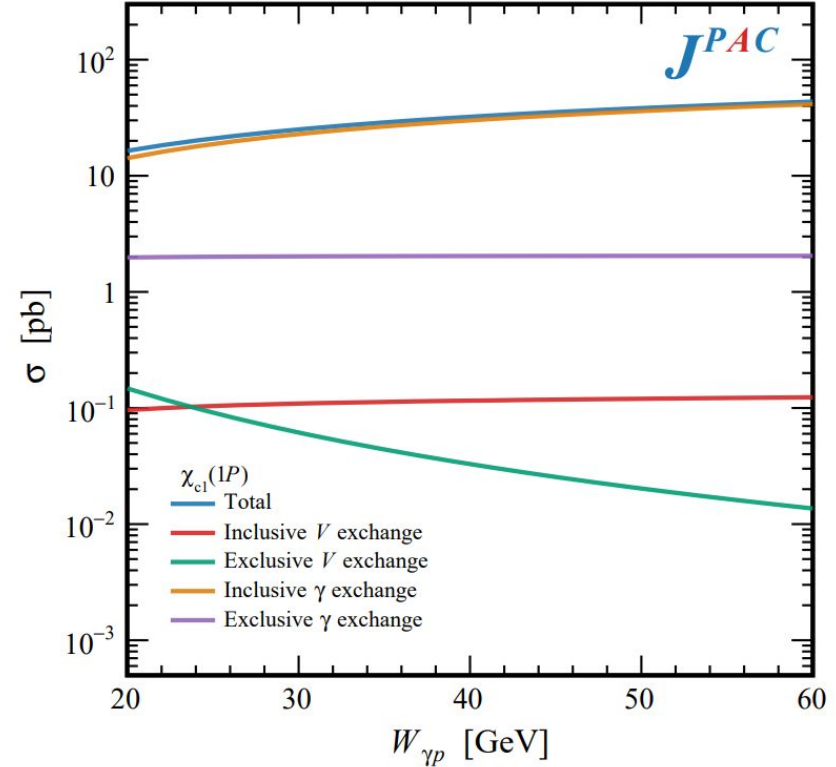
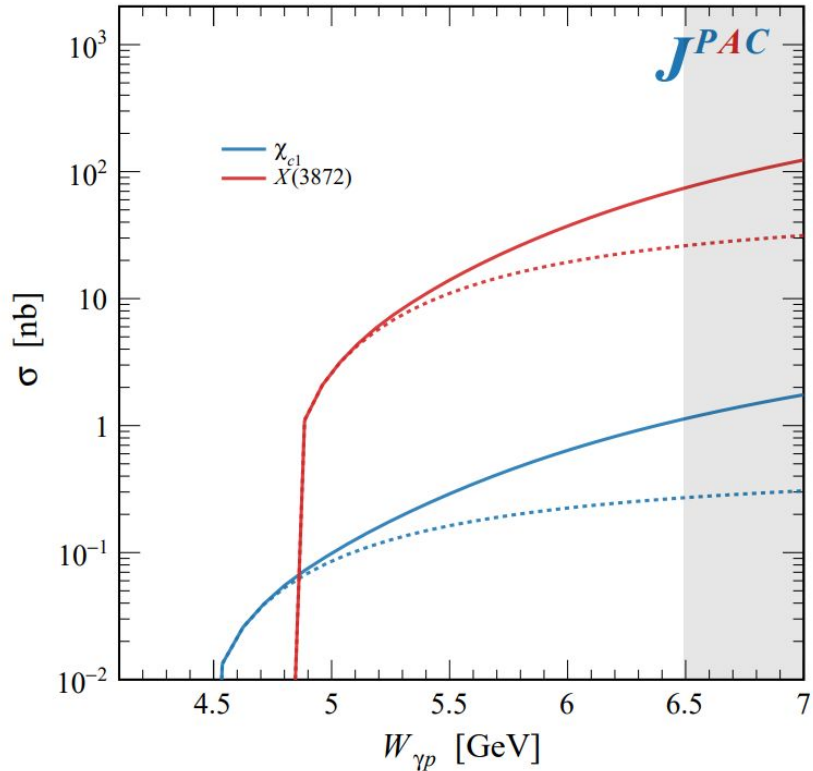




# Charged Z production



# X(3872) production



# jpacPhoto

Unified code bank for all JPAC photoproduction models.

- |   |                                      |
|---|--------------------------------------|
| [1] <a href="#">Double Polarization Observables in Pentaquark Photoproduction</a>       | [Phys. Rev. D 100, 034019 (2019)]    |
| [2] <a href="#">XYZ spectroscopy at electron-hadron facilities: Exclusive processes</a> | [Phys. Rev. D 102, 114010 (2020)]    |
| [3] <a href="#">XYZ spectroscopy at electron-hadron facilities II:</a>                  | [Phys. Rev. D 106 (2022) 09, 094009] |
| [4] <a href="#">XYZ spectroscopy at electron-hadron facilities III</a>                  | [arXiv:2404.05326]                   |
| [5] <a href="#">Dynamics in near-threshold J/ψ photoproduction</a>                      | [Phys. Rev. D 108 (2023) 5, 054018]  |
| [6] <a href="#">Features of πΔ Photoproduction at High Energies</a>                     | [Phys.Lett.B 779 (2018) 77-81]       |
| [7] <a href="#">Vector Meson Photoproduction with a Linearly Polarized Beam</a>         | [Phys. Rev. D 97, 094003 (2018)]     |
| [8] <a href="#">Exclusive Tensor Meson Photoproduction</a>                              | [Phys. Rev. D 102, 014003 (2020)]    |

**For experimentalists:** easier integration of theory models into existing workflows

Broad range of (polarized) observables calculable.

**Incorporated into eISpectro  
Interfaceable with AmpTools**

**For theorists:** suite of tools for effective model testing, data analysis, reproducibility, etc.

**To extend to two meson  
photoproduction reactions**

$$\gamma^5 \left[ (\not{q} + \not{p} + m) \right] \epsilon^\mu(q, \lambda)$$

```
lorentz_tensor<dirac_matrix, 1> projector = gamma_5() * (slash(q + p) + M_PROTON) * eps;
```

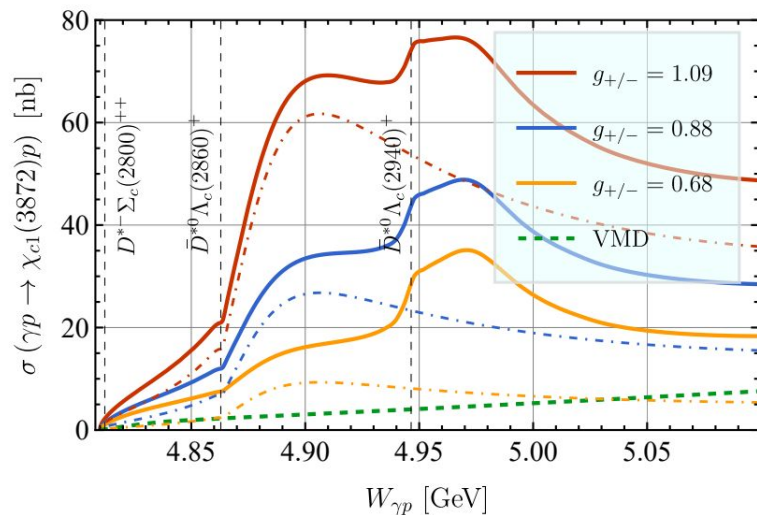
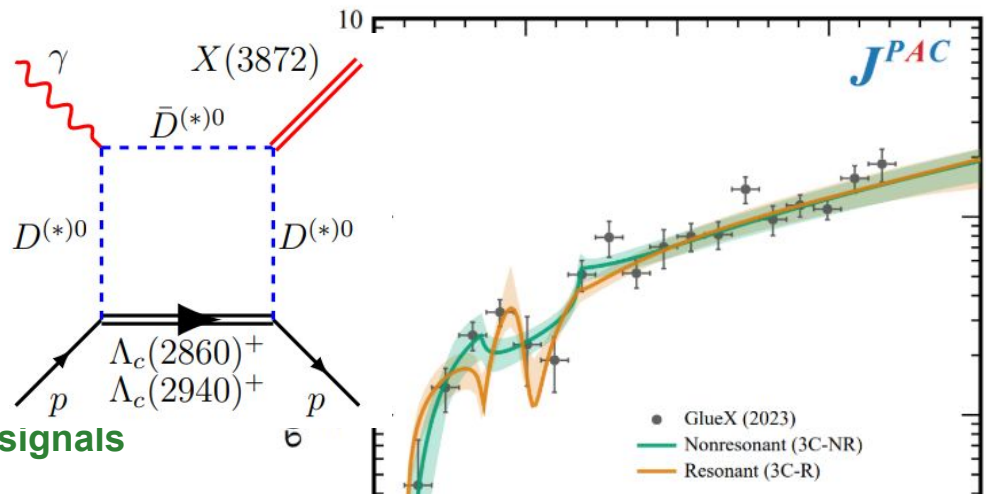
# Summary

Next generation experiments will extend photoproduction programs to heavy sectors.

Lot of work needed to motivate potential **exotic signals** and interesting processes to look at.

Aim to use established phenomenology and measured quantities to estimate production rates.

Once data is available, amplitude analysis can extract meaningful quantities to surmise the underlying dynamics.



**Thank you :)**

# BACKUPS

# Production mechanisms

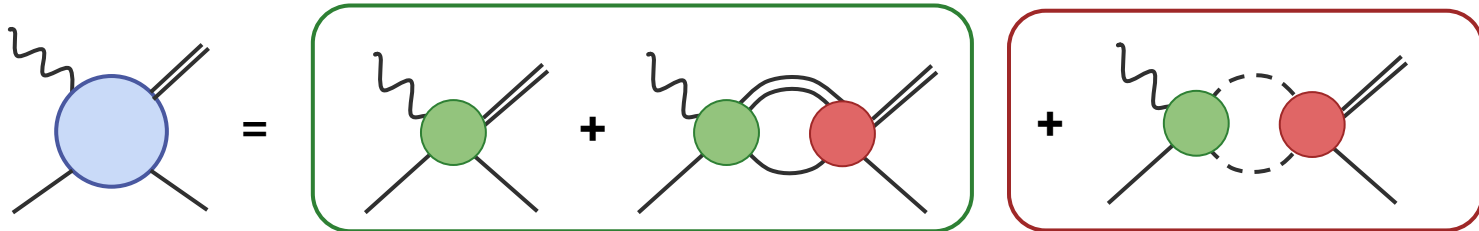
Define the ratio of direct  $J/\psi$  photocoupling to all other intermediate channels. Figure of merit measuring the “**directness**” the total production occurs at threshold.

$$\zeta_{\text{th}} = \frac{|F_{\text{direct}}^{\psi p}(s_{\text{th}})|}{|F_{\text{direct}}^{\psi p}(s_{\text{th}})| + |F_{\text{indirect}}^{\psi p}(s_{\text{th}})|}$$

90% CL

<b>1C</b>	1
<b>2C</b>	[0.56, 0.74]
<b>3C-NR</b>	[0.36, 0.63]
<b>3C-R</b>	[0.03, 0.62]

When included, “**factorization violating**” contributions make up > 25% at 90% CL!



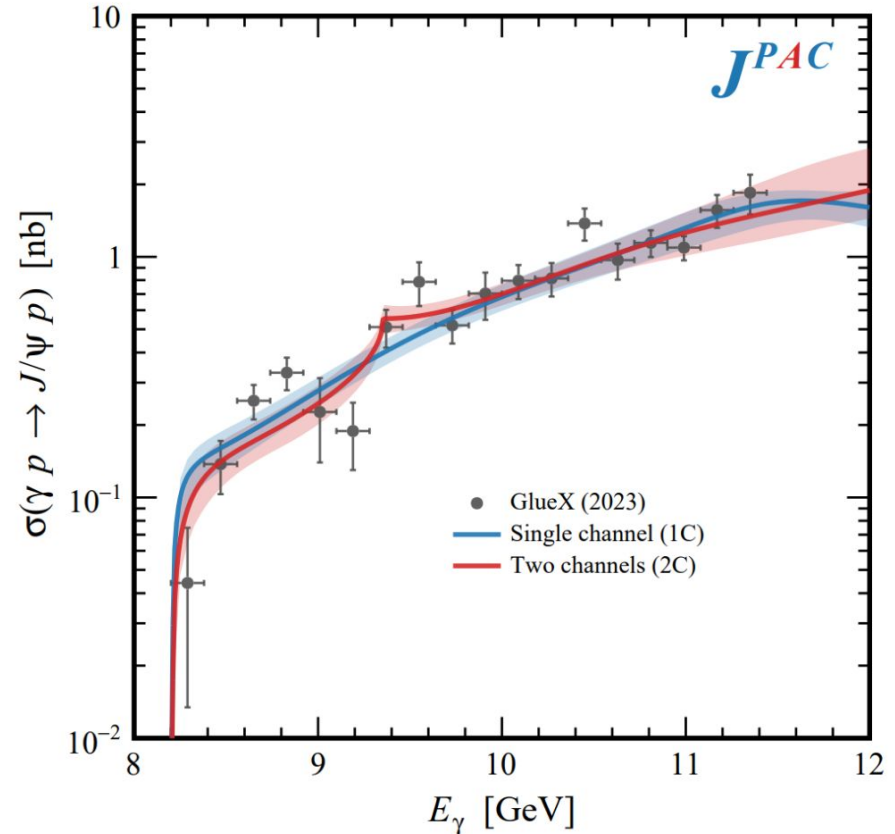
# Production mechanisms

Presence of cusps may indicate large contributions from open charm channels (i.e. **charm exchange processes**) which may complicate the connection to proton structure quantities.

**90% CL**

<b>1C</b>	1
<b>2C</b>	[0.56, 0.74]
<b>3C-NR</b>	[0.36, 0.63]
<b>3C-R</b>	[0.03, 0.62]

Solution with nearby pentaquark pole even consistent with entirely charm exchange dominated production!

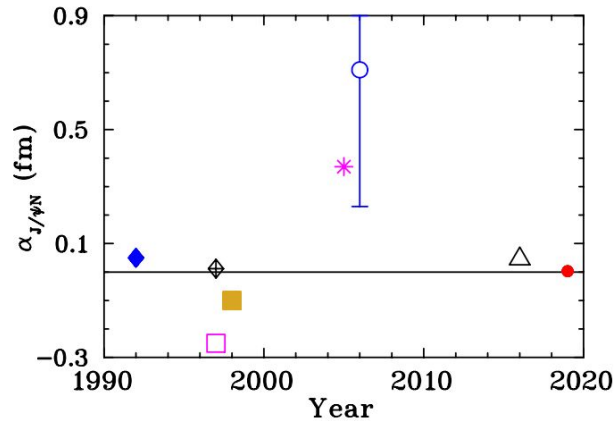




# Elastic scattering length

First extraction of the elastic  $J/\psi p$  scattering length without the use of VMD.

Analysis favors large values on the **order of Fermi!**



Strakovsky et al [Phys. Rev. C 101, 042201 (2020)]

## Scattering length [fm]

<b>1C</b>	[0.56 1.00]
<b>2C</b>	[0.11, 0.76]
<b>3C-NR</b>	[-2.77, 0.35]
<b>3C-R</b>	[-0.04, 0.19]

$$T_S^{\psi p, \psi p} = \frac{8\pi \sqrt{s_{\text{th}}}}{-a_{\psi p}^{-1} - i q} + O(q^2)$$

Possibly indicated **typical hadronic interaction** between nucleon and charmonia but poorly constrained 3C results still consistent with zero!

# Pentaquark poles

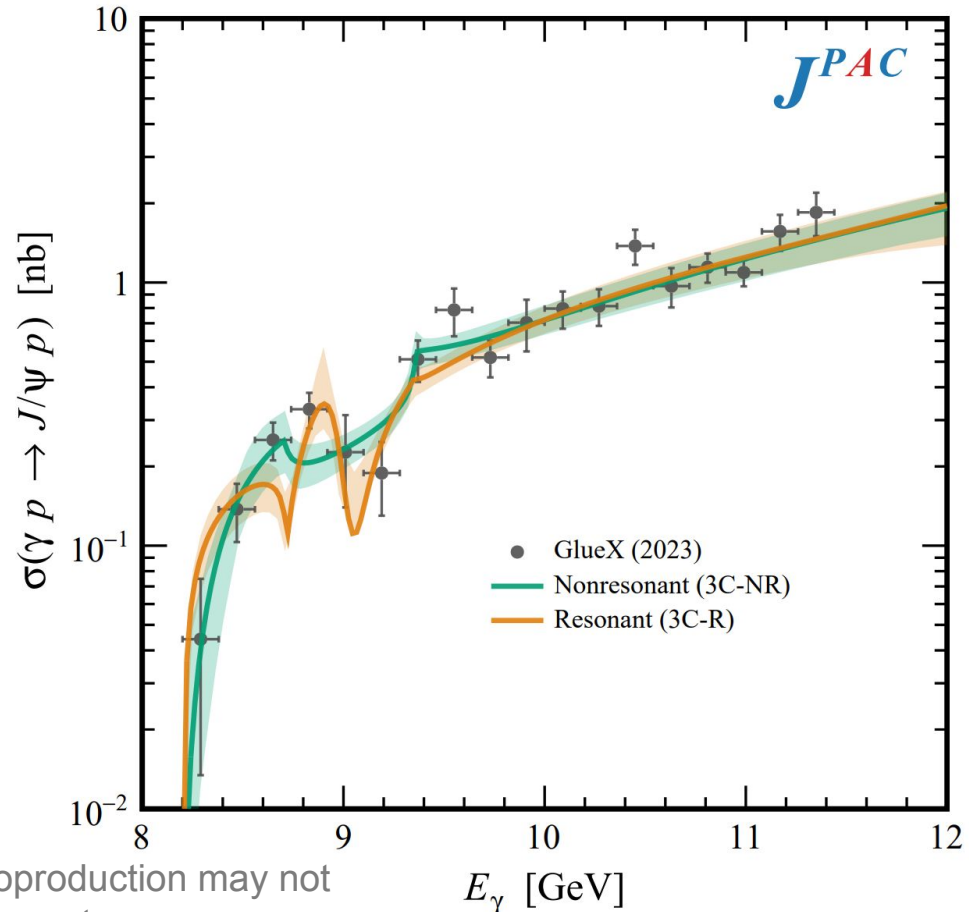
Pronounced dip in 3C-R found to correspond to a narrow pole on  $RS = (- - +)$  making it consistent with an **S-wave pentaquark state**.

$$M = 4211\text{MeV} \quad \Gamma = 48\text{MeV}$$

Two other poles also found but on more remote Reimann sheets.

When considering all uncertainties pole **very unconstrained** but leaves room for solutions with poles in **strongly coupled channel scenarios!**

VMD result also indicates nonobservation in photoproduction may not immediately kill possibility of pentaquarks in  $J/\psi p$  spectrum

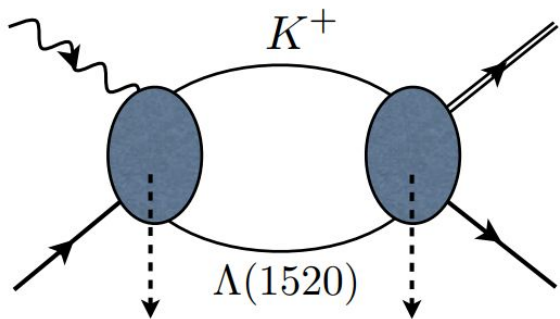


# $\phi$ Photoproduction

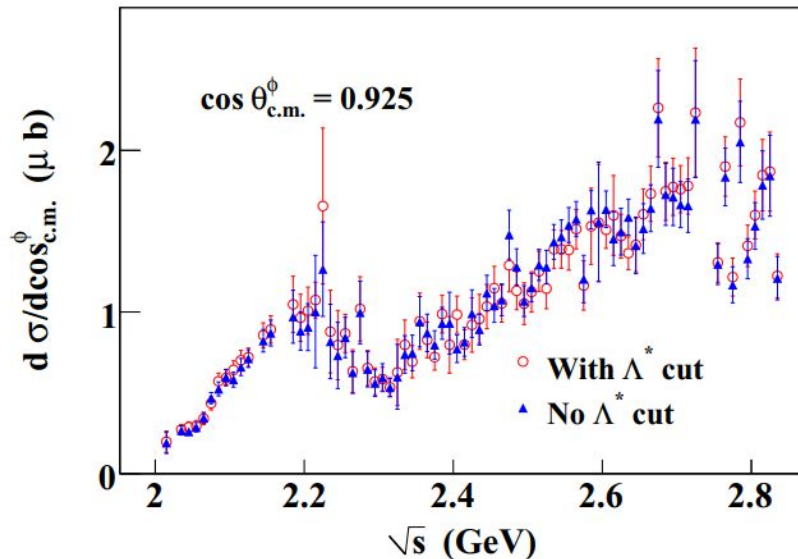
Completely analogous system to charmonium.

Significant structures seen within 1-2 GeV of threshold. Coincides with **open flavor thresholds**.

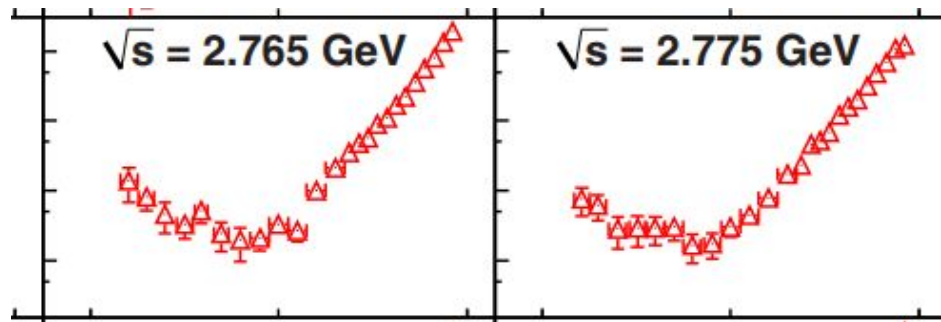
Possibility of hidden strange bound states



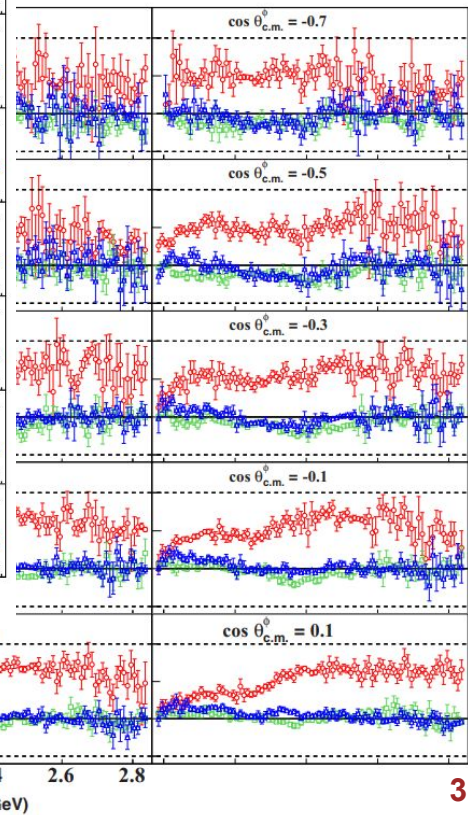
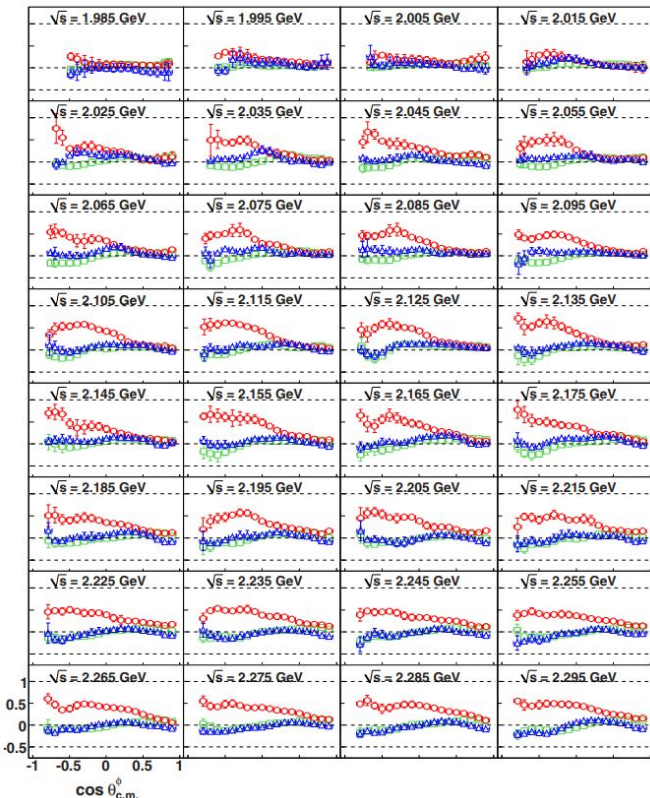
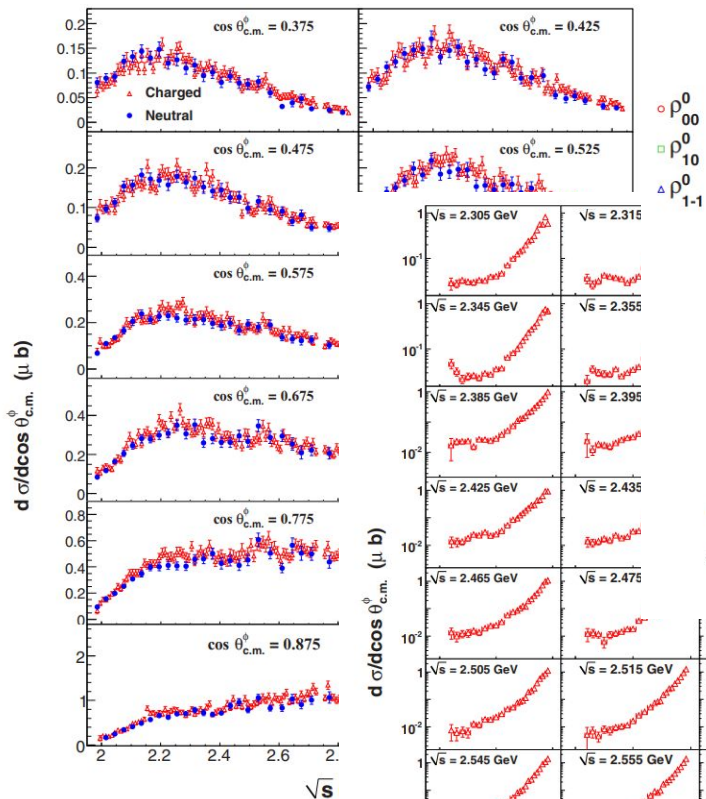
H-Y Rui et al [PTEP 2014 (2014) 023D03]



CLAS [Phys.Rev.C 89 (2014) 5, 055208]



# A TON OF DATA



# Full K-matrix analysis

Possibility to study coupled channels, nearby bound states, etc in considering all spins and helicity dependence.

On going but very preliminary, still trying to understand gauge-invariance structure...

$$\begin{aligned}l_1^{\mu\nu} &= P^\mu [(P \cdot q) k^\nu - (k \cdot q) P^\nu] \quad , & l_7^{\mu\nu} &= q^\mu \gamma^\nu \not{q} \quad , \\l_2^{\mu\nu} &= (k \cdot q) g^{\mu\nu} - q^\mu k^\nu \quad , & l_8^{\mu\nu} &= P^\mu \gamma^\nu \not{q} \quad , \\l_3^{\mu\nu} &= (P \cdot q) g^{\mu\nu} - q^\mu P^\nu \quad , & l_9^{\mu\nu} &= \gamma^\mu [(P \cdot q) k^\nu - (k \cdot q) P^\nu] \\l_4^{\mu\nu} &= g^{\mu\nu} \not{q} - q^\mu \gamma^\nu \quad , & l_{10}^{\mu\nu} &= \gamma^\mu [(k \cdot q) \gamma^\nu - k^\nu \not{q}] \quad , \\l_5^{\mu\nu} &= [(q \cdot P) g^{\mu\nu} - q^\mu P^\nu] \not{q} \quad , & l_{11}^{\mu\nu} &= \gamma^\mu [(P \cdot q) \gamma^\nu - P^\nu \not{q}] \\l_6^{\mu\nu} &= P^\mu [P^\nu \not{q} - (q \cdot P) \gamma^\nu] & l_{12}^{\mu\nu} &= \gamma^\mu \gamma^\nu \not{q} \quad ,\end{aligned}$$

Hope to have some cool results in the coming months

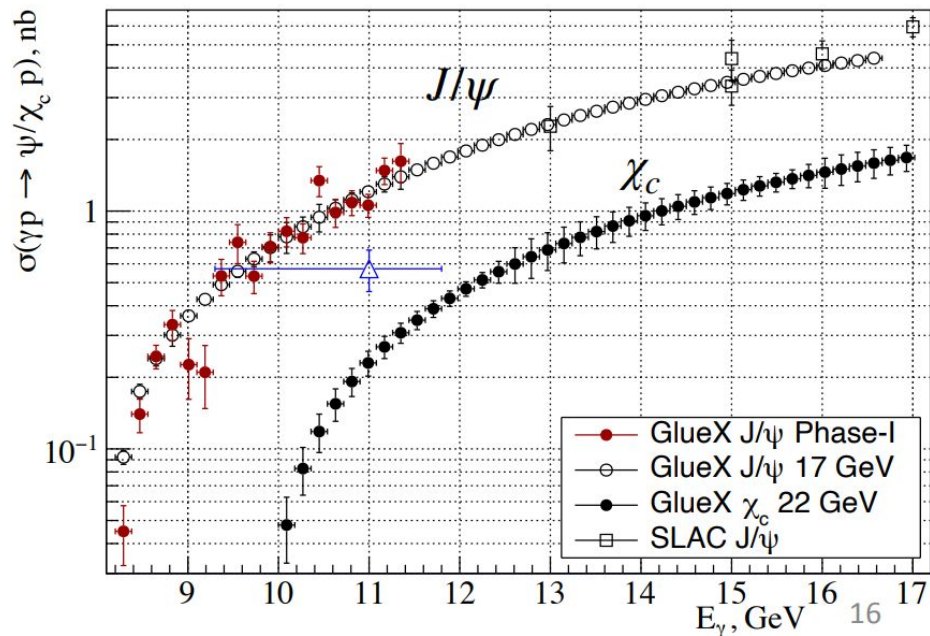
# $\chi_{c1}$ at GlueX?

Radiative couplings measured (no need for VMD) so vector exchange is in principle a known amplitude.

**Observation in GlueX about a factor 10 enhanced compared to prediction (~0.02 nb at 11 GeV)**

Other production mechanism? C-odd glue exchange, open charm box? Something else?

From Lubomir's talk at "J/psi and Beyond" Workshop at JLab Aug 2022



- We have used the measured  $\chi_c$  yields and MC simulations (efficiency  $\sim 10\%$ ) to scale the JPAC calculations for  $\chi_{c1}$  photoproduction cross section and make projections for GlueX with 22 GeV beam: