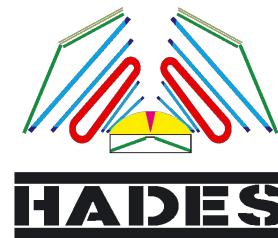


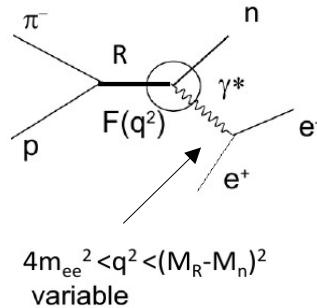
Studies of Time-like Baryon Transition Form Factors with HADES



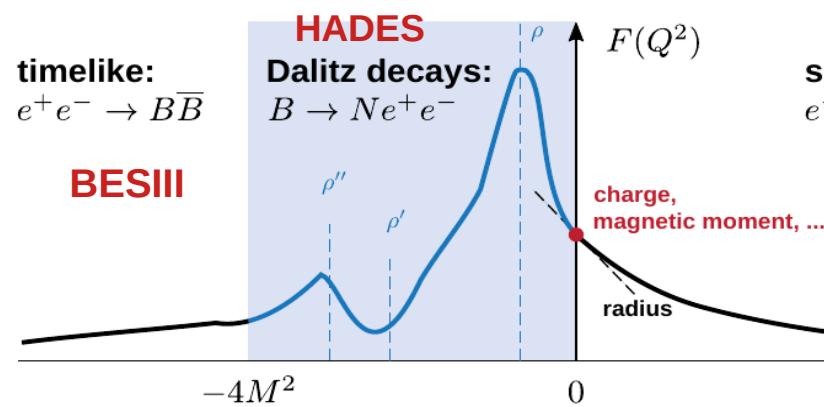
Izabela Ciepał



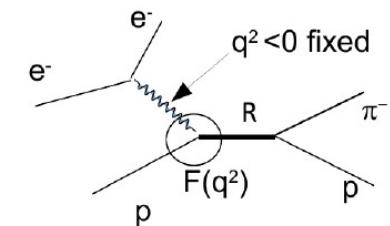
Electromagnetic structure of baryons



timelike:
 $e^+ e^- \rightarrow B\bar{B}$
BESIII



spacelike:
 $e^- N \rightarrow e^- N$



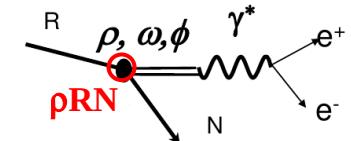
CLAS/JLab,
MAMI, ELSA,
JLab-Hall A, ...

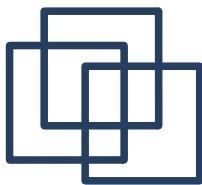
$R \rightarrow N$ Transition
Form Factor

$$\frac{d\Gamma(\Delta \rightarrow N e^+ e^-)}{dq^2} = f(m_\Delta, q^2) \left(|G_M^2(q^2)| + 3|G_E^2(q^2)| + \frac{q^2}{2m_\Delta^2} |G_C^2(q^2)| \right)$$

QED
transition
of point-like
particles

G_{M/E/C}: Form-Factors ($A_{1/2}, A_{3/2}, S_{1/2}$)
internal structure of hadrons





Combined Partial Wave Analysis of hadronic 2-pion channels and Dalitz decays

Bn-Ga PWA: pwa.hisp.uni-bonn.de

2 π data included in the fit

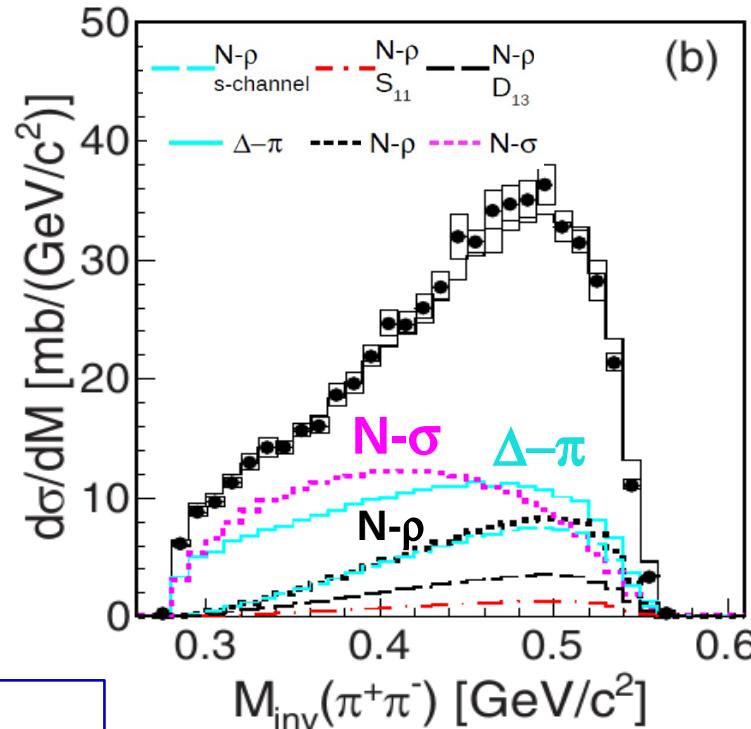
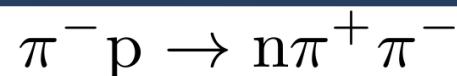
Reaction	Observable	W (GeV)	
$\gamma p \rightarrow \pi^0 \pi^0 p$	DCS, Tot	1.2-1.9	MAMI
$\gamma p \rightarrow \pi^0 \pi^0 p$	E	1.2-1.9	MAMI
$\gamma p \rightarrow \pi^0 \pi^0 p$	DCS, Tot	1.4-2.38	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	P, H	1.45-1.65	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	T, P_x, P_y	1.45-2.28	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	P_x, P_x^c, P_x^s (4D)	1.45-1.8	CB-ELSA
$\gamma p \rightarrow \pi^0 \pi^0 p$	P_y, P_y^c, P_y^s (4D)	1.45-1.8	CB-ELSA
$\gamma p \rightarrow \pi^+ \pi^- p$	DCS	1.7-2.3	CLAS
$\gamma p \rightarrow \pi^+ \pi^- p$	I^c, I^s	1.74-2.08	CLAS
$\pi^- p \rightarrow \pi^0 \pi^0 n$	DCS	1.29-1.55	Crystal Ball
$\pi^- p \rightarrow \pi^+ \pi^- n$	DCS	1.45-1.55	HADES
$\pi^- p \rightarrow \pi^0 \pi^- p$	DCS	1.45-1.55	HADES

ρ meson production:

- s-channel D_{13} ($N(1520)$ $3/2^-$) **dominant contribution**
- $N(1520) \rightarrow N\rho$ BR=12.2 \pm 2 %
- $N(1535) \rightarrow N\rho$ BR=3.2 \pm 0.6 %

8 new entries:

- branching ratios of
 $N(1440)$
 $N(1535)$
 $N(1520)$
to 2 π channels ($\Delta\pi$, $N\rho$, $N\sigma$)



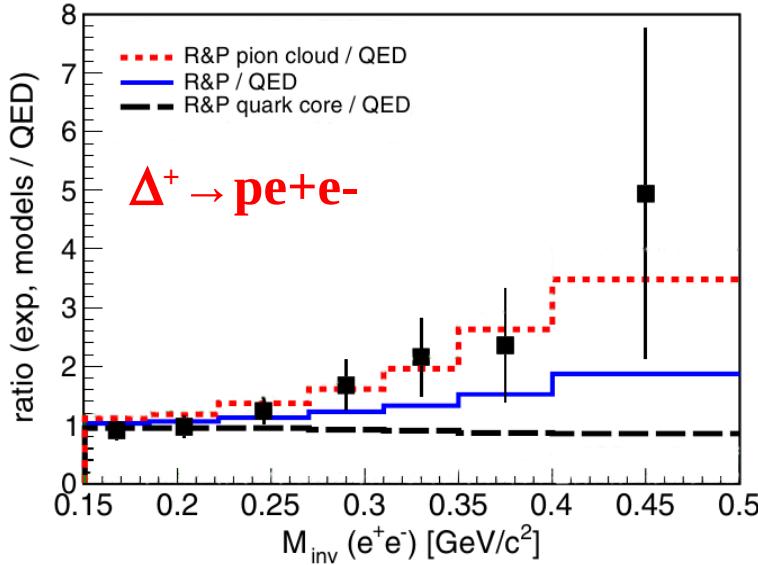
**reference ρ mass spectrum
for e⁺e⁻ analysis**



Time-like transition form factors for nucleon resonances

$pp \rightarrow ppe^+e^-$ @ 1.25 GeV

calculations T. Pena & G. Ramalho

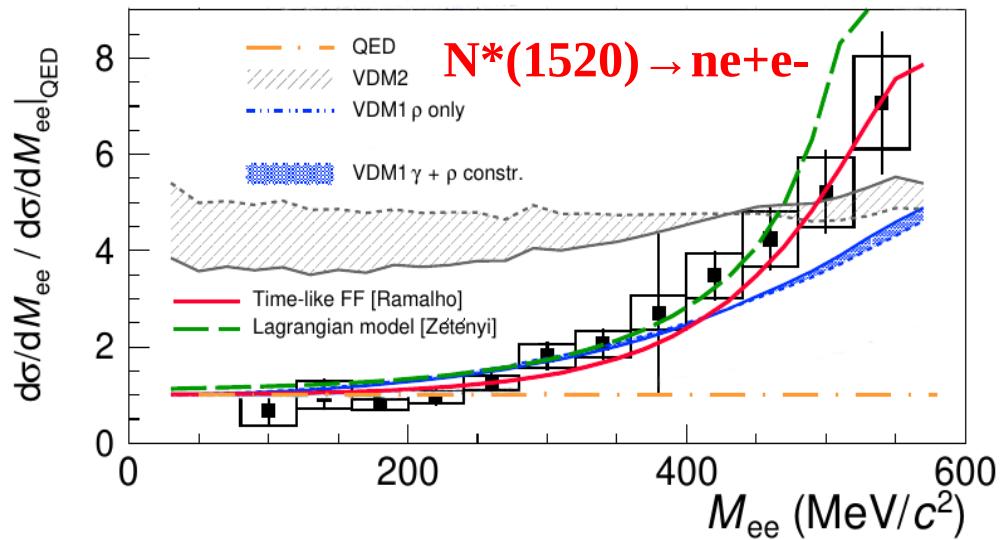


effective eTFF

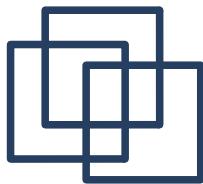
$$\frac{d\Gamma(\Delta \rightarrow Ne^+e^-)}{dq^2} = f(m_\Delta, q^2) \left(|G_M(q^2)| + 3|G_E(q^2)| + \frac{q^2}{2m_\Delta^2}|G_C(q^2)| \right)$$

QED

$\pi p \rightarrow ne^+e^-$ @ 0.7 GeV/c



- VMD2 (*strict VMD*) overestimates data below 400 MeV
- 2-component VMD (VMD1) gives reasonable description
- Z&W: Lagrangian model – very promising
- R&P: Time-like FF - dominant pion cloud contribution (pion emFF)
- S. Leupold: FF based on dispersive framework



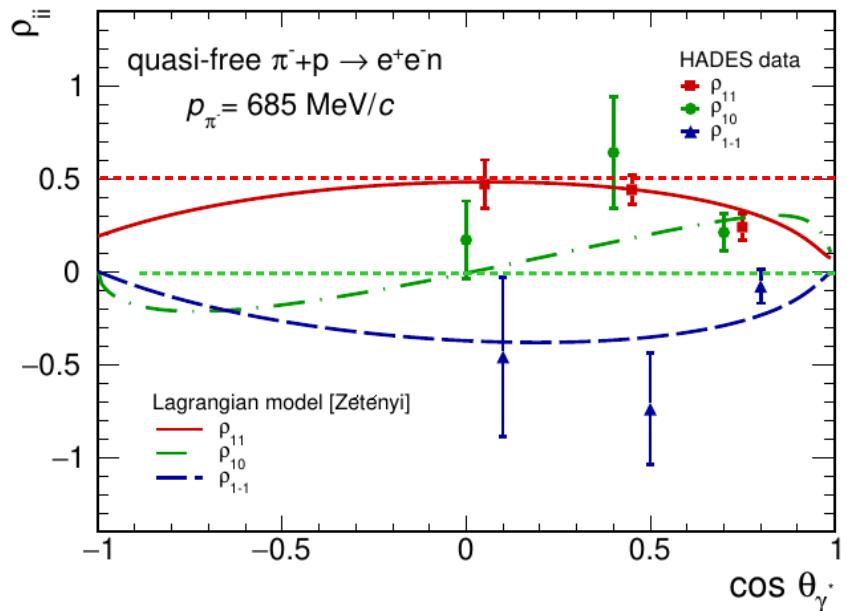
Virtual photon polarization

HADES Coll. arXiv:2205.15914 [nucl-ex]

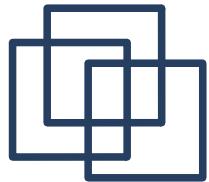
$$\frac{d^3\sigma}{dM_{ee} d\Omega_{\gamma_*} d\Omega_e} \sim |\mathbf{A}|^2 = \frac{e^2}{Q^4} \sum_{\Lambda\Lambda'} \rho_{\Lambda\Lambda'}^{(H)} \rho_{\Lambda\Lambda'}^{(dec)} \quad \text{QED: } \gamma^* \rightarrow e^+e^- \\ \mathbf{R} \rightarrow \mathbf{N} + \gamma^*$$

$$|A|^2 \propto 8k^2 [1 - \rho_{11} + (3\rho_{11} - 1) \cos^2 \Theta + \sqrt{2} R e \rho_{10} \sin 2\Theta \cos \phi + R e \rho_{1-1} \sin^2 \Theta \cos 2\phi]$$

- SDME ρ_{11} , ρ_{10} , ρ_{1-1} extracted from experiment taking into account acceptance and efficiency (A. Sarantsev) in 3 bins in $\cos\theta_{\gamma^*}$



- $\rho_{11} = 0.5$, $\rho_{10} = 0$ for transverse polarization
- (real photon)
- we see angular dependence
 \Rightarrow contribution from a virtual photon
- \Rightarrow contributions of spins larger than $1/2$: N(1520) resonance
- more precise data needed !



Backup

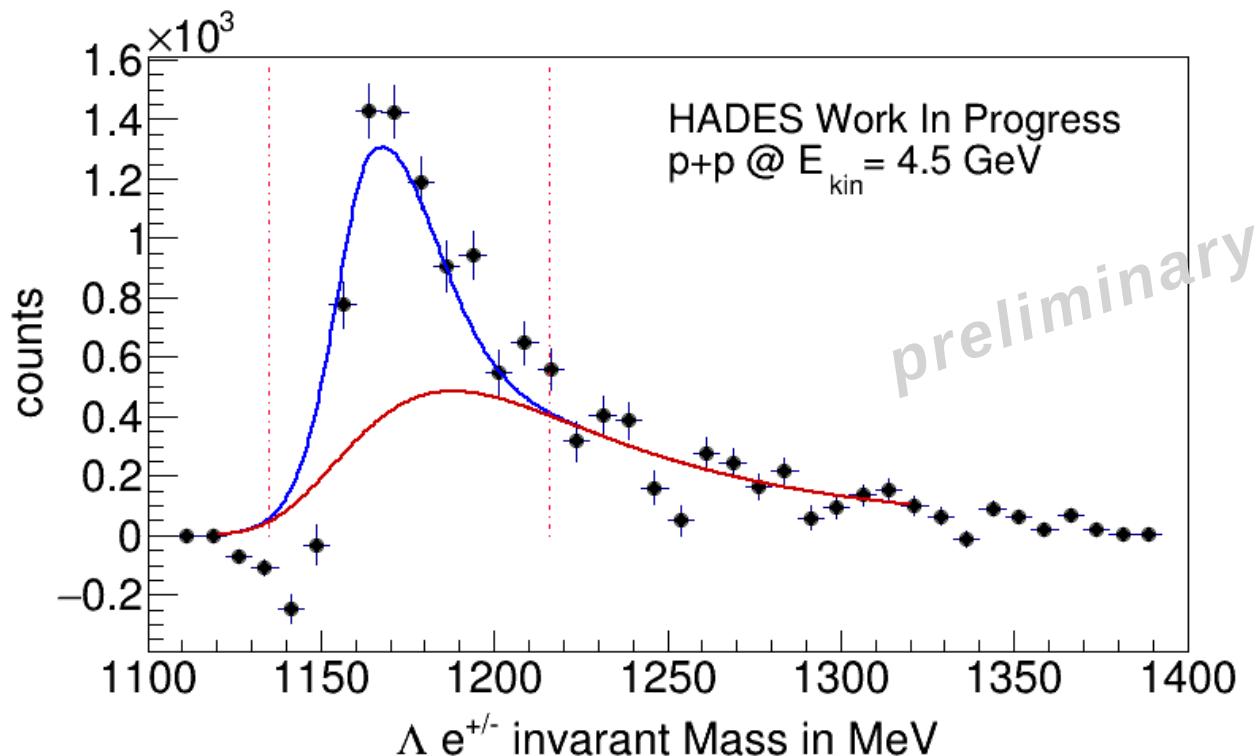


Time-like transition form factors for hyperons

pp → pp π^- e⁺e⁻ @4.5 GeV

Jana Rieger (PhD)

$\Sigma^0(1192) \rightarrow \Lambda e^+e^-$ Dalitz decay





Dalitz decays of baryon resonances

Vector Meson Dominance Models (VMD)

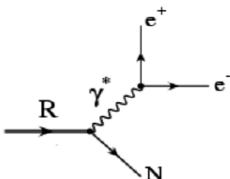
hadrons \longleftrightarrow photons

Meson Dalitz decays: (Crystal Ball/TAPS, A2, Na60 data), many theoretical studies

Baryons Dalitz decays: (Hades), most of the calculations of eTFF are based on VMD

→ QED “point-like”

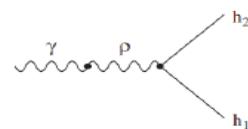
$R\gamma^*$ vertex



*M. Zetenyi et al.,
PRC 67, 044002 (2003)*

→ strict VMD (VMD2)

- $N\rho$ coupling
- used in HI transport models

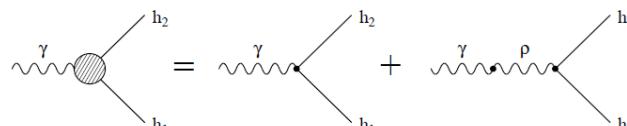


$$\Gamma_{\rho}^{VDM2} = \left(\frac{M_0}{M}\right)^3 \Gamma_{\rho}^0$$

*Sakurai, Phys. Rev 22 (1969) 981
M. I. Krivoruchenko et al.,
Ann. Phys. 296, 299 (2002)*

→ 2-component VMD (VMD1)

- $N\rho$ and $N\gamma$ couplings
- used in calculations of in-medium spectral functions



*Kroll, Lee & Zuminio
Phys. Rev. 157, 1376 (1967)*

$$\Gamma_{\rho}^{VDM1} = \left(\frac{M}{M_0}\right) \Gamma_{\rho}^0$$



etFF of baryons: models

Covariant quark model +VMD

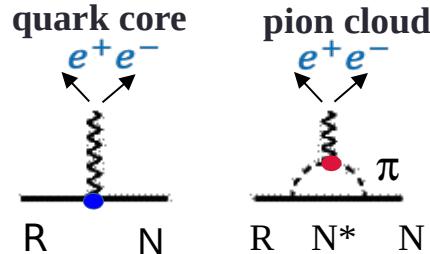
T. Pena & G. Ramalho

N- $\Delta(1232)$: *Phys. Rev. D* 93, 033004 (2016)

N-N(1520): *Phys. Rev. D* 95, 014003 (2017)

N-N(1535): *Phys. Rev. D* 101, 114008 (2020)

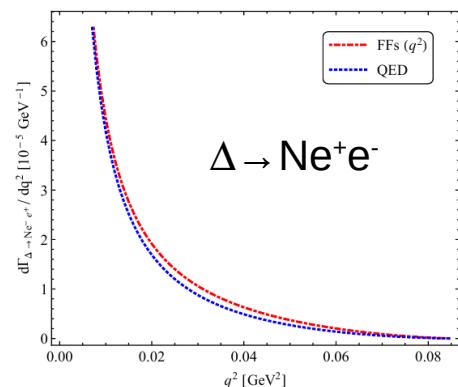
VMD:
quark FF
pion FF



Dispersion theory

S. Leupold et al.

S. Leupold
arXiv:2401.17756 (2024)



Two-component Lagrangian model

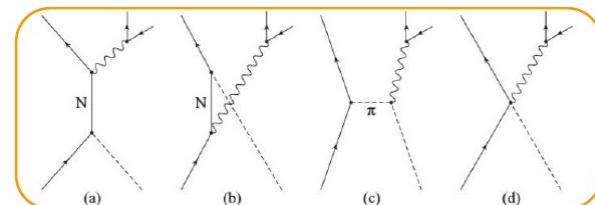
M. Zetenyi & G. Wolf

PRC 86, 065209 (2012)

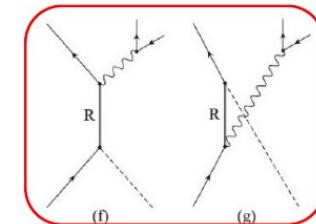
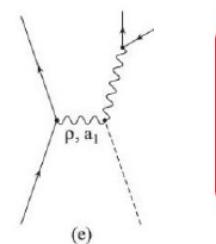
PRC 104, 015201 (2021)

microscopic calculations of $\pi N \rightarrow Ne + e^-$

Born terms

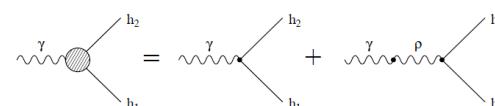


baryon resonances



$N^*(1440)$
 $N^*(1520)$
 $N^*(1535)$

2-component VMD:



interference
between
 γ and ρ
contributions



Virtual photon polarization

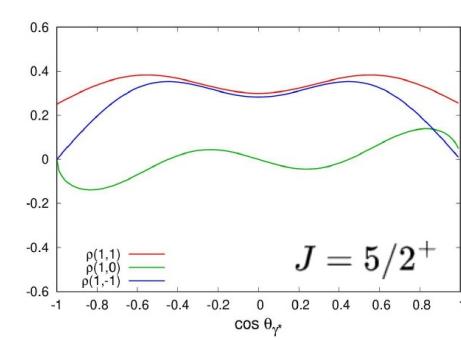
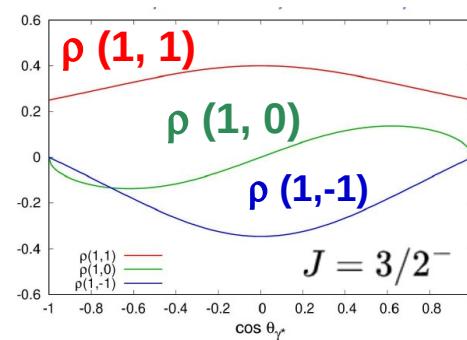
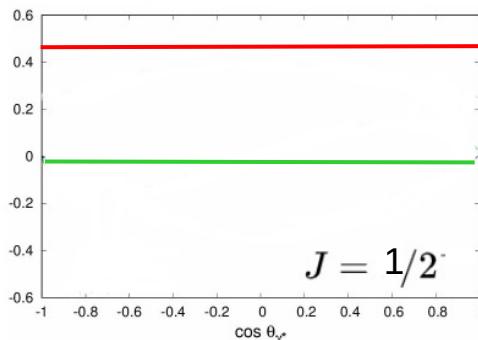
E. Speranza et al. Phys. Lett. B764, 282 (2017)

angular distribution of $e^+e^- \rightarrow$ polarization of $\gamma^* \rightarrow$ spin density matrix elements ($\rho_{\Lambda\Lambda'}$)

$$\pi N \rightarrow N \gamma^* \rightarrow Ne + e^- \quad \frac{d^3\sigma}{dM_{ee} d\Omega_{\gamma^*} d\Omega_e} \sim |A|^2 = \frac{e^2}{Q^4} \sum_{\Lambda\Lambda'} \rho_{\Lambda\Lambda'}^{(H)} \rho_{\Lambda\Lambda'}^{(dec)} \quad \text{QED: } \gamma^* \rightarrow e^+e^- \\ R \rightarrow N + \gamma^*$$

Angular distribution of the lepton pair:

$$|A|^2 \propto 8k^2 [1 - \rho_{11} + (3\rho_{11} - 1) \cos^2 \Theta + \sqrt{2} Re \rho_{10} \sin 2\Theta \cos \phi + Re \rho_{1-1} \sin^2 \Theta \cos 2\phi]$$



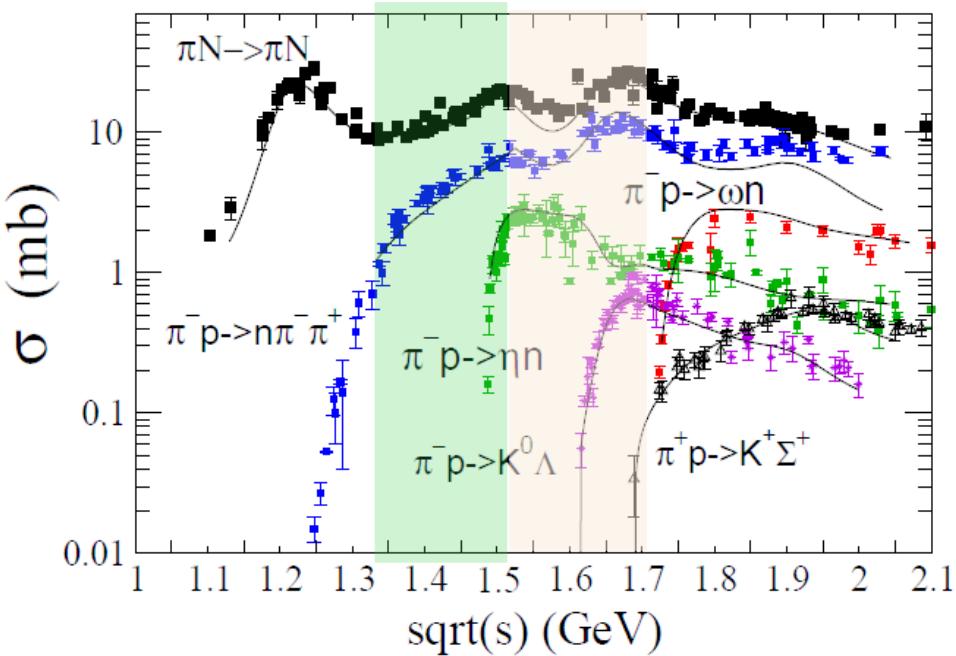
- $\rho_{\Lambda\Lambda'}$ depends on γ^* polarization
- $\rho_{\Lambda\Lambda'}$ are combination of G_E , G_M , G_C
- **the angular distribution is sensitive to J^P of the resonance**
- can be obtain from fit to the experimental angular distribution



OUTLOOK

HADES Physics Program with Pion Beams explore the 3rd resonance region $\sqrt{s} = 1.7 \text{ GeV}/c^2$

2014 2025



CBM@ SIS100 pp @ 30 GeV

- prod. cross sec. higher than at SIS18:
 $\sigma(\Sigma^*, \Lambda^*) \sim 1 \text{ mb}$
- much higher luminosity

Beam energy scan 2025:
continuation and extension
to 3rd resonance region

- 1) Baryon-meson couplings:
- 2) $\rightarrow \pi\pi N, \omega n, \eta n, K^0 \Lambda, K^0 \Sigma, \dots$
- 3) including neutral mesons (ECAL),
 $\rightarrow \rho R$ couplings $S31(1620)$,
- 4) $D33(1700), P13(1720), \dots$
- 5) Hyperon polarization: Λ, Σ
- 6) Exotic states:
 - \rightarrow the lowest glueballs, 4q systems,
hybrids , bound states of mesons:
 $f_0(500), f_0(980), a_0(980), f_0(1370), \dots$
 - \rightarrow unknown region of $\text{inv}M(\pi\pi) \sim 1 \text{ GeV}$
very precise data needed !