

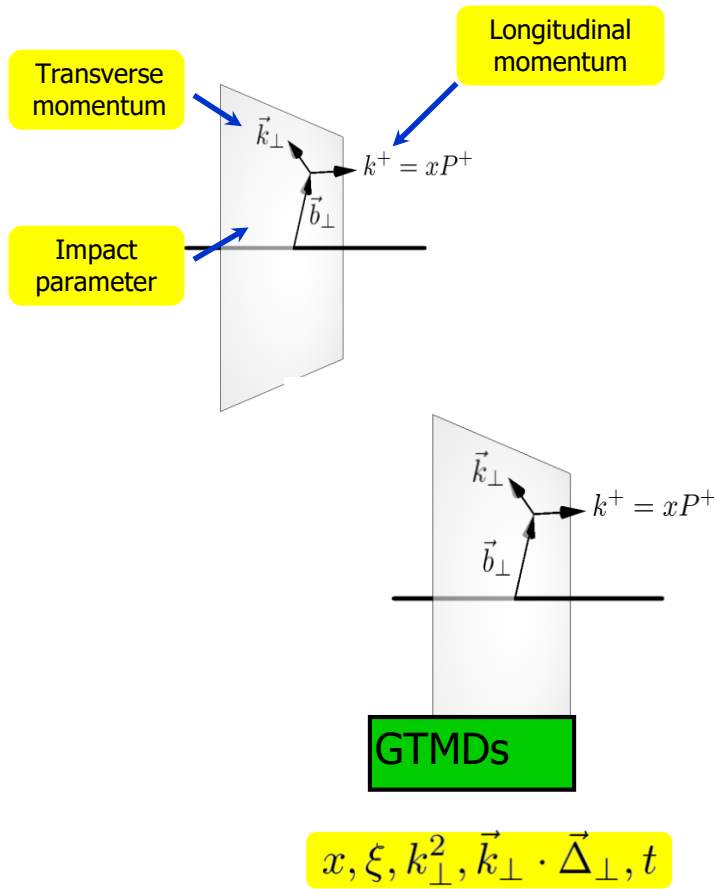


**Deeply Virtual Compton Scattering
on the neutron with CLAS12 at Jefferson Lab**

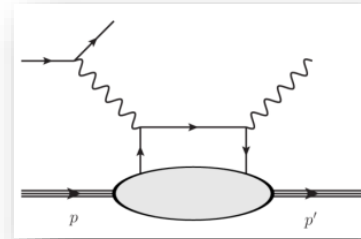
Silvia Niccolai (IJCLab Orsay), for the CLAS Collaboration
NSTAR 2024, York (UK), 17/6/2024
Analysis done by Adam Hobart (IJCLab)



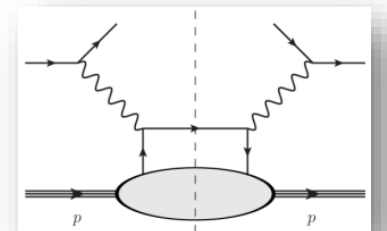
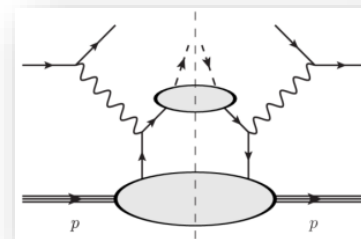
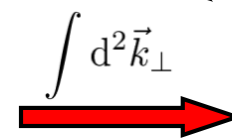
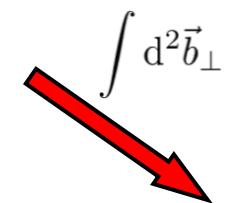
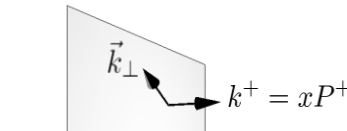
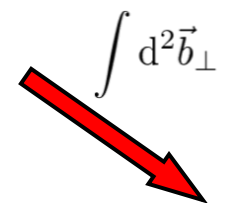
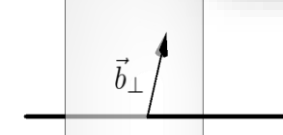
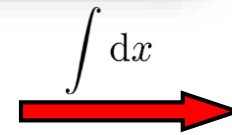
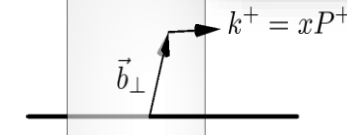
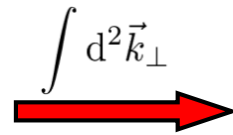
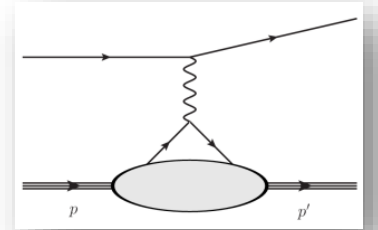
Multi-dimensional mapping of the nucleon



DVCS et al.

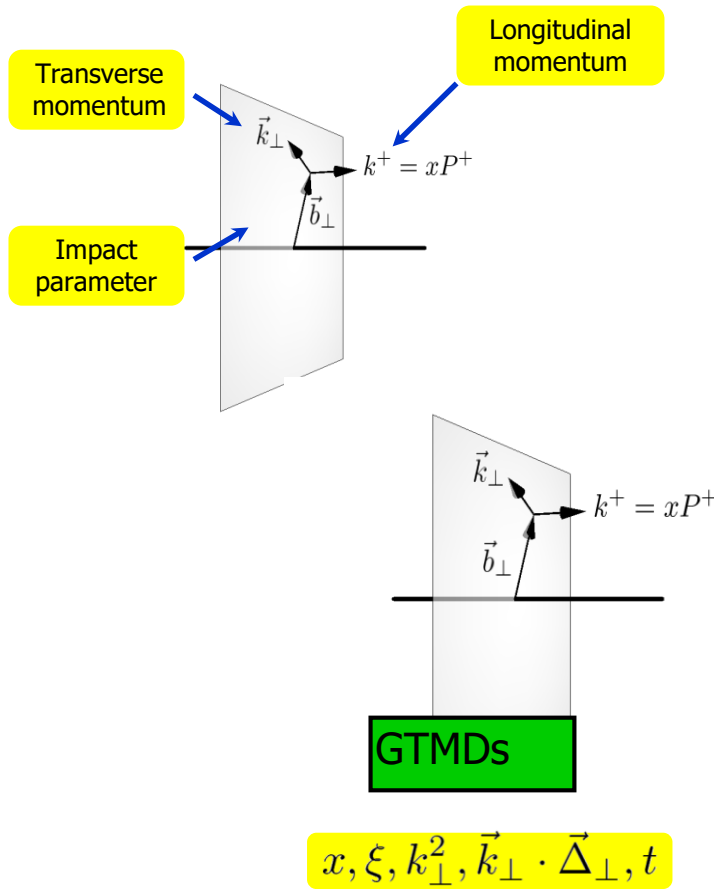


Elastic Scattering

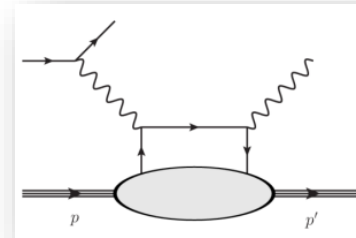


A complete picture of nucleon structure requires the measurement of all these distributions

Multi-dimensional mapping of the nucleon



DVCS et al.



Nucleon tomography

$$q(x, \mathbf{b}_\perp) = \int_0^\infty \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{i\Delta_\perp \mathbf{b}_\perp} H(x, 0, -\Delta_\perp^2)$$

$$\Delta q(x, \mathbf{b}_\perp) = \int_0^\infty \frac{d^2 \Delta_\perp}{(2\pi)^2} e^{i\Delta_\perp \mathbf{b}_\perp} \tilde{H}(x, 0, -\Delta_\perp^2)$$

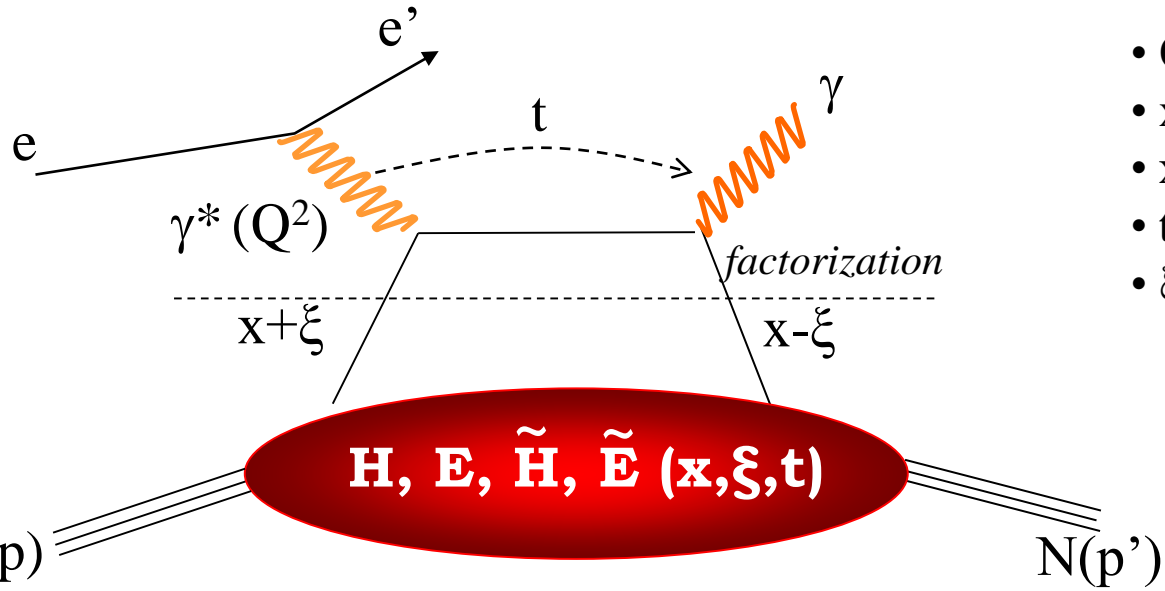
Generalized Parton Distributions:

- ✓ fully correlated parton distributions in both **coordinate** and **longitudinal momentum** space
 - ✓ linked to **FFs** and **PDFs**
- ✓ **Accessible in exclusive reactions**

Quark angular momentum (Ji's sum rule)

$$\frac{1}{2} \int_{-1}^1 x dx (H(x, \xi, t=0) + E(x, \xi, t=0)) = J = \frac{1}{2} \Delta \Sigma + \Delta L$$

Deeply Virtual Compton Scattering and GPDs



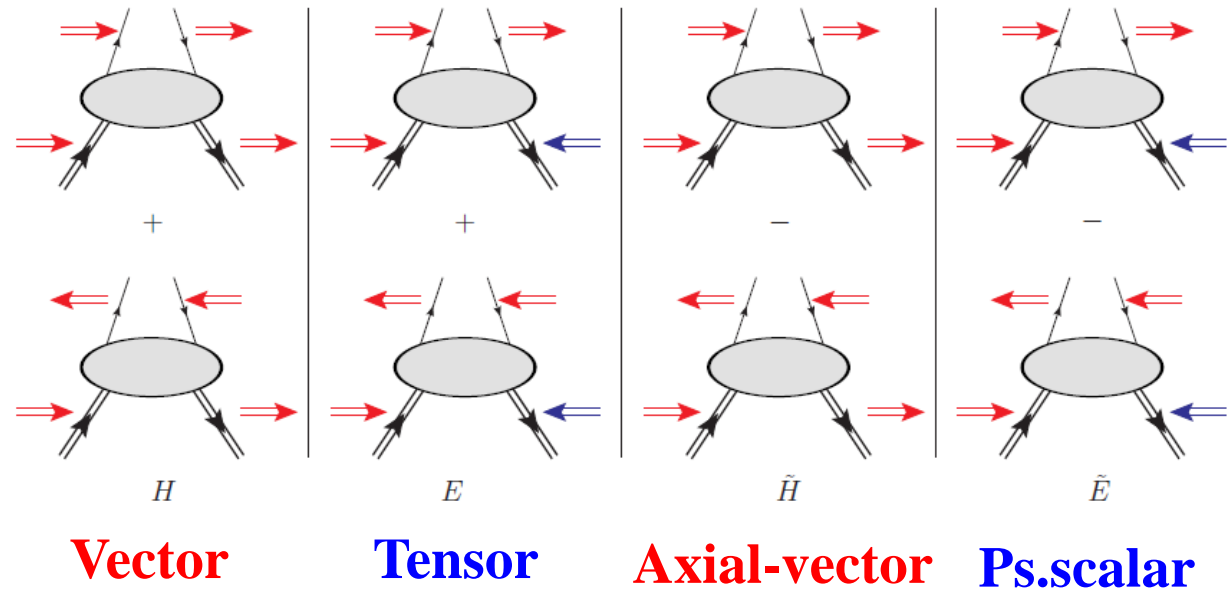
- $Q^2 = -(e-e')^2$
- $x_B = Q^2/2Mv$ $v = E_e - E_{e'}$
- $x+\xi, x-\xi$ longitudinal momentum fractions
- $t = \Delta^2 = (p-p')^2$
- $\xi \cong x_B/(2-x_B)$

« Handbag » factorization, valid in the **Bjorken regime** (high Q^2 and v , fixed x_B), $t \ll Q^2$

GPDs: Fourier transforms of *non-local, non-diagonal* QCD operators

4 GPDs for each quark flavor (leading-order, leading twist, quark-helicity conservation)

conserve nucleon spin
flip nucleon spin

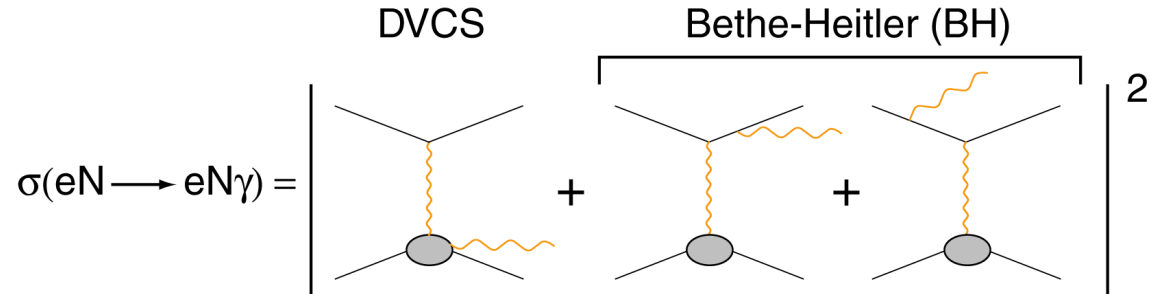


Accessing GPDs through DVCS

$$T^{DVCS} \sim P \int_{-1}^{+1} \frac{GPDs(x, \xi, t)}{x \pm \xi} dx \pm i\pi GPDs(\pm\xi, \xi, t) + \dots$$

$$Re\mathcal{H}_q = e_q^2 P \int_0^{+1} \left(H^q(x, \xi, t) - H^q(-x, \xi, t) \right) \left[\frac{1}{\xi - x} + \frac{1}{\xi + x} \right] dx$$

$$Im\mathcal{H}_q = \pi e_q^2 \left[H^q(\xi, \xi, t) - H^q(-\xi, \xi, t) \right]$$



$$\sigma(eN \rightarrow eN\gamma) =$$

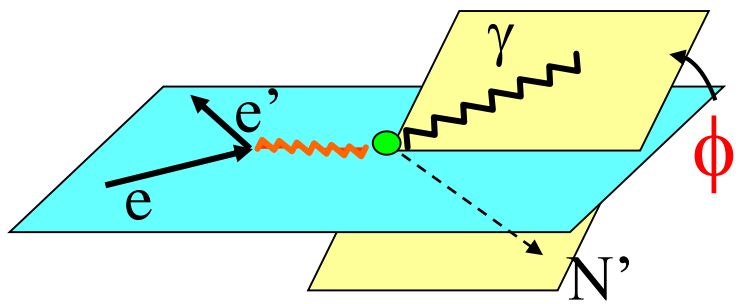
Proton Neutron

$$Im\{\mathcal{H}_p, \tilde{\mathcal{H}}_p, \mathcal{E}_p\}$$

$$Im\{\mathcal{H}_n, \tilde{\mathcal{H}}_n, \mathcal{E}_n\}$$

$$\sigma \sim |T^{DVCS} + T^{BH}|^2$$

$$\Delta\sigma = \sigma^+ - \sigma^- \propto I(DVCS \cdot BH)$$



Polarized beam, unpolarized target:

$$\Delta\sigma_{LU} \sim \sin\phi \text{Im}\{F_1\mathcal{H} + \xi(F_1+F_2)\tilde{\mathcal{H}} - kF_2\mathcal{E} + \dots\}$$

Unpolarized beam, longitudinal target:

$$\Delta\sigma_{UL} \sim \sin\phi \text{Im}\{F_1\tilde{\mathcal{H}} + \xi(F_1+F_2)(\mathcal{H} + x_B/2\mathcal{E}) - \xi kF_2\tilde{\mathcal{E}}\}$$

Polarized beam, longitudinal target:

$$\Delta\sigma_{LL} \sim (A+B\cos\phi) \text{Re}\{F_1\tilde{\mathcal{H}} + \xi(F_1+F_2)(\mathcal{H} + x_B/2\mathcal{E}) + \dots\}$$

Unpolarized beam, transverse target:

$$\Delta\sigma_{UT} \sim \cos\phi \sin(\phi_s - \phi) \text{Im}\{k(F_2\mathcal{H} - F_1\mathcal{E}) + \dots\}$$

Unpolarized beam and target, different lepton charges:

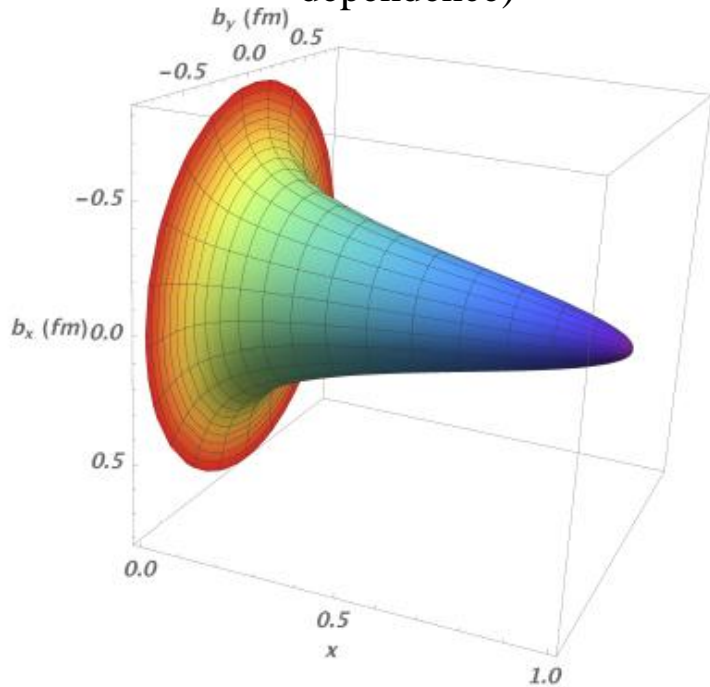
$$\Delta\sigma_C \sim \cos\phi \text{Re}\{F_1\mathcal{H} + \xi(F_1+F_2)\tilde{\mathcal{H}} - kF_2\mathcal{E} + \dots\}$$

$$Re\{\mathcal{H}_p, \tilde{\mathcal{H}}_p, \mathcal{E}_p\}$$

$$Re\{\mathcal{H}_n, \tilde{\mathcal{H}}_n, \mathcal{E}_n\}$$

What have we learned from the first generation of proton-DVCS results?

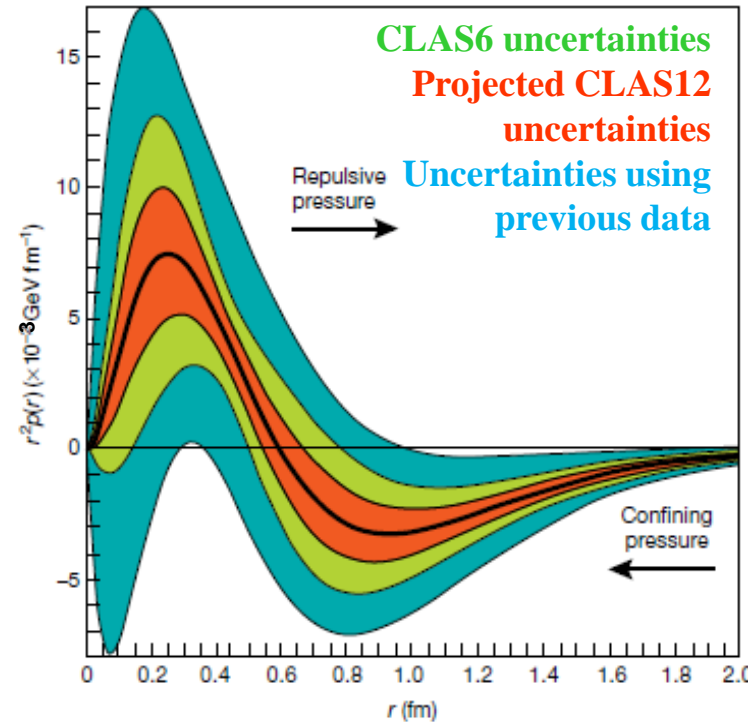
Proton tomography from *local fits* to HERMES, CLAS, and Hall-A data (**Im \mathcal{H}** + **model dependent** assumptions for x dependence)



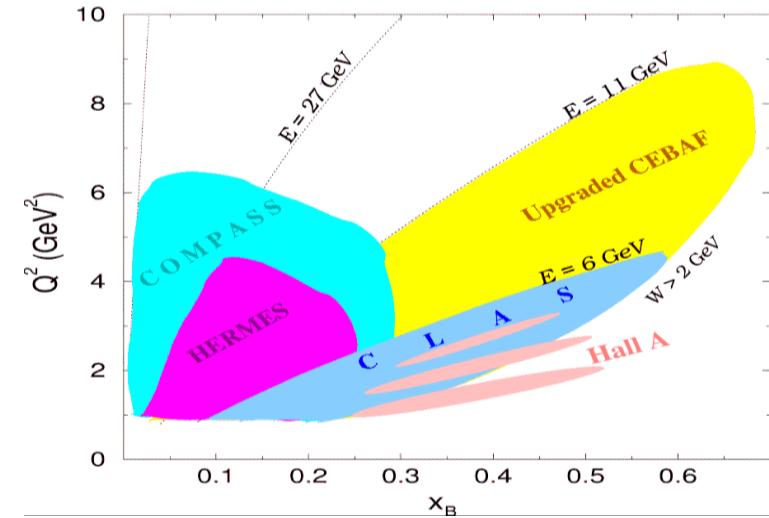
High-momentum quarks (valence) are at the core of the nucleon, low-momentum quarks (sea) spread to its periphery

R. Dupré, M. Guidal, M. Vanderhaeghen, PRD95 (2017)

From **\mathcal{H} -only fit** of DVCS BSA and cross section from CLAS@6 GeV (**model dependent**): an insight in the pressure distribution in the proton



V. Burkert, L. Elouadrhiri, F.X. Girod, Nature 557, 396-399 (2018)



An extensive experimental program is underway for proton DVCS at JLab@12 GeV

Observable (target)	12-GeV experiments
$\Delta\sigma_{\text{beam}}(p)$	Hall A, CLAS12, Hall C
BSA(p)	CLAS12
TSA(p)	CLAS12
DSA(p)	CLAS12
t TSA(p)	CLAS12

Interest of DVCS on the neutron

A combined analysis of DVCS observables for **proton and neutron** targets is necessary for the **flavor separation** of GPDs

$$(H, E)_u(\xi, \xi, t) = \frac{9}{15} [4(H, E)_p(\xi, \xi, t) - (H, E)_n(\xi, \xi, t)]$$

$$(H, E)_d(\xi, \xi, t) = \frac{9}{15} [4(H, E)_n(\xi, \xi, t) - (H, E)_p(\xi, \xi, t)]$$

Moreover, the beam-spin asymmetry for nDVCS is the most sensitive observable to the GPD E
 → Ji's sum rule for Quarks Angular Momentum

Polarized beam, unpolarized target:

$$\Delta\sigma_{LU} \sim \sin\phi \operatorname{Im}\{F_1\mathcal{H} + \xi(F_1 + F_2)\tilde{\mathcal{H}} + kF_2\mathcal{E}\}d\phi$$

$$\Longrightarrow \operatorname{Im}\{\mathcal{H}_n, \tilde{\mathcal{H}}_n, \mathcal{E}_n\}$$

Unpolarized beam, transversely polarized target:

$$\Delta\sigma_{UT} \sim \cos\phi \operatorname{Im}\{k(F_2\mathcal{H} - F_1\mathcal{E}) + \dots\}d\phi$$

$$\Longrightarrow \operatorname{Im}\{\mathcal{H}_p, \mathcal{E}_p\}$$

Neutron
Proton

The BSA for nDVCS:

- is complementary to the **TSA for pDVCS** on transverse target, aiming at **E**
- depends strongly on the **kinematics** → **wide coverage needed**
- is smaller than for pDVCS → more **beam time** needed to achieve reasonable statistics

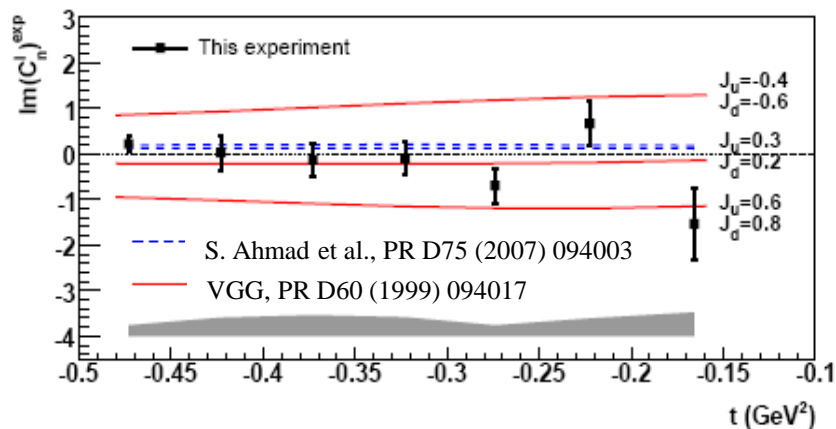
DVCS on the neutron in Hall A at 6 GeV

$\vec{e}d \rightarrow e\gamma(np)$

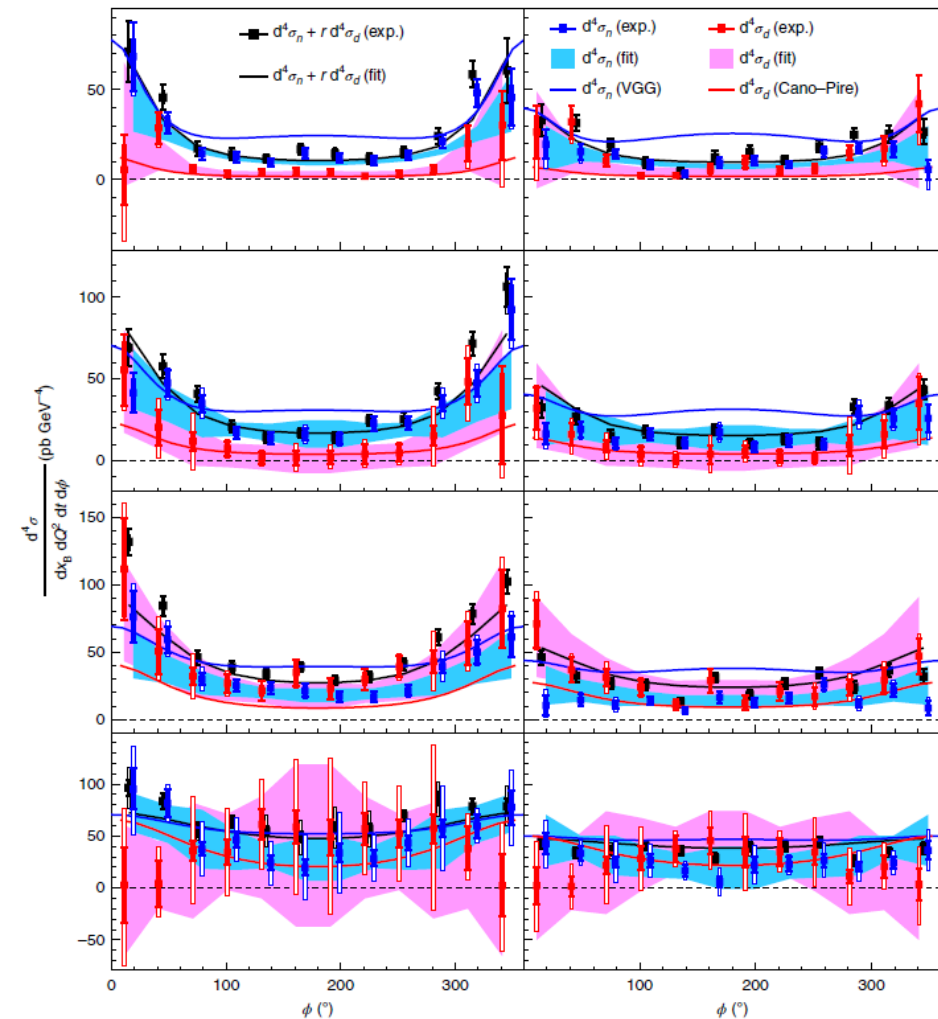
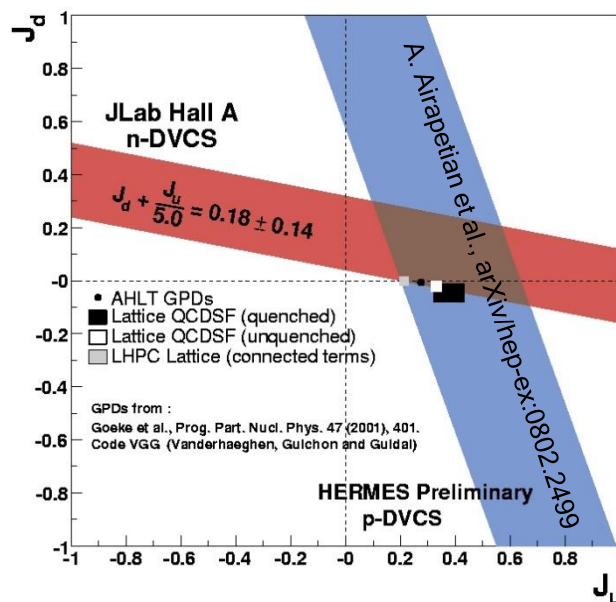
$$D(e, e'\gamma)X - H(e, e'\gamma)X = n(e, e'\gamma)n + d(e, e'\gamma)d + \dots$$

$$\Delta\sigma_{LU} \sim \sin\phi \operatorname{Im}\{F_1\mathcal{H} + \xi(F_1 + F_2)\tilde{\mathcal{H}} - kF_2\mathcal{E}\}$$

M. Mazouz et al., PRL 99 (2007) 242501



$Q^2=1.9 \text{ GeV}^2$ and $x_B=0.36$



• E03-106: First-time measurement of $\Delta\sigma_{LU}$ for nDVCS, model-dependent extraction of J_u, J_d

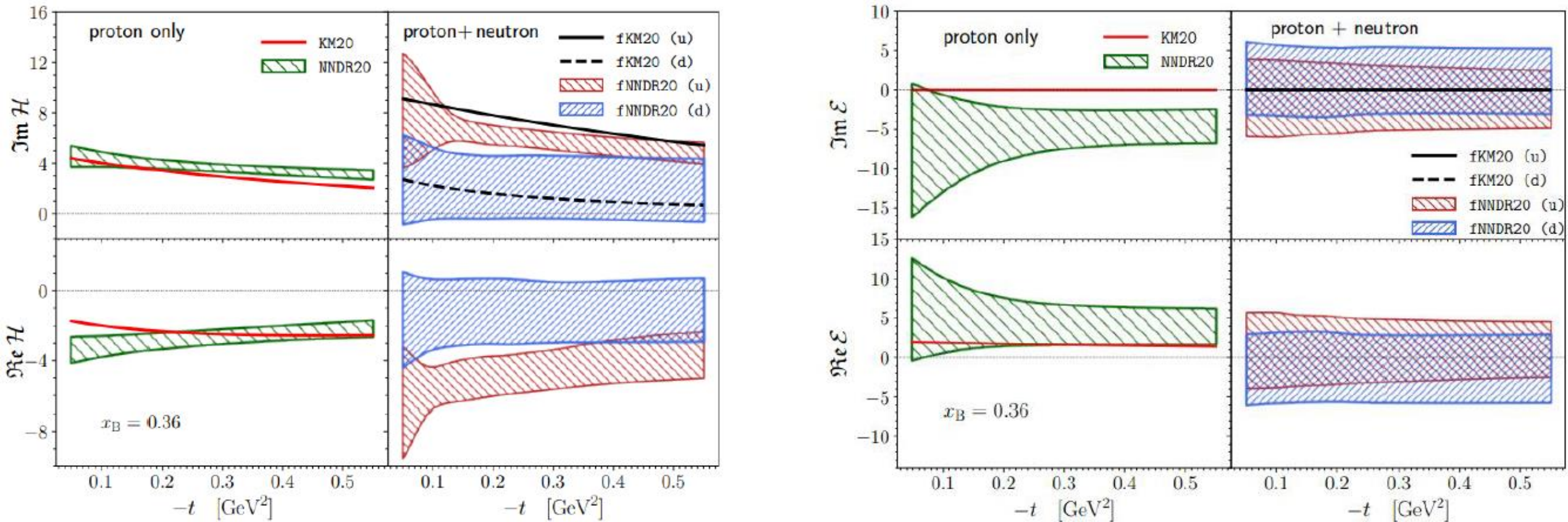
$$\frac{1}{2} \int_{-1}^1 x dx (H(x, \xi, t=0) + E(x, \xi, t=0)) = J$$

Hall-A experiment E08-025 (2010)

- Beam-energy « Rosenbluth » separation of nDVCS CS using an LD2 target and two different beam energies
- First observation of non-zero nDVCS CS
- M. Benali et al., Nature 16 (2020)

Extraction of CFFs and flavor separation using 6-GeV JLab data

M. Čuić, K. Kumericki et al. Phys. Rev. Lett.125.232005 (2020) and Arxiv 2007.00029 (2020)



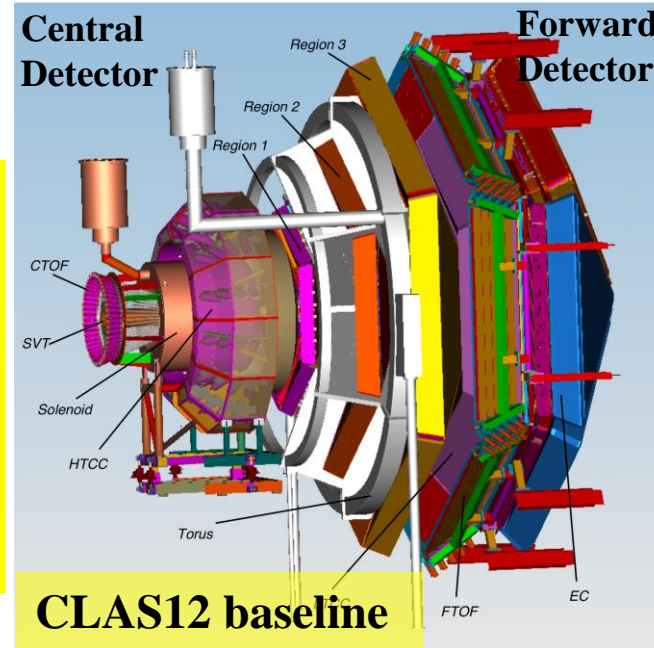
- Proton- and neutron-DVCS data from JLab (CLAS6 and Hall A)
 - Up and down contributions to the CFFs of H are separated
- The CFFs of E are not separated, a significant sign ambiguity remains

CLAS12 Run Group B at Jefferson Lab

Electroproduction on deuterium with CLAS12

Run infos:

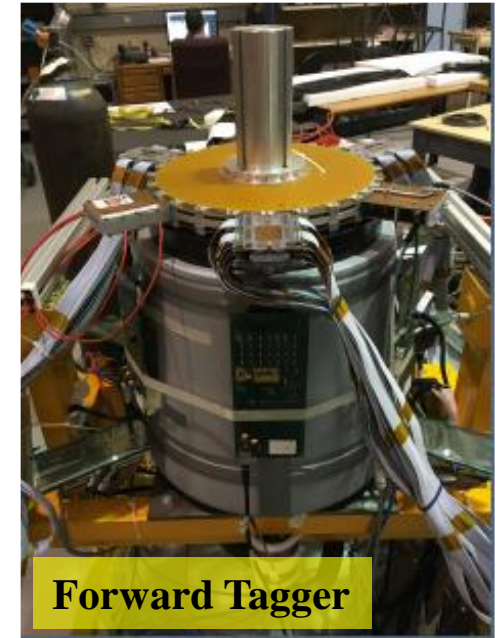
- Feb. 6th – Mar. 25th 2019 + Dec. 3 –20 2019 + Jan. 6 – 30 2020 → ~39 PAC days (~43% of the approved run time)
- 3 beam energies: 10.6, 10.2, 10.4 GeV
- Average beam polarization ~86%
- Liquid deuterium target, 5 cm long
- $L = \sim 1.3 \cdot 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ per nucleon



CLAS12 baseline



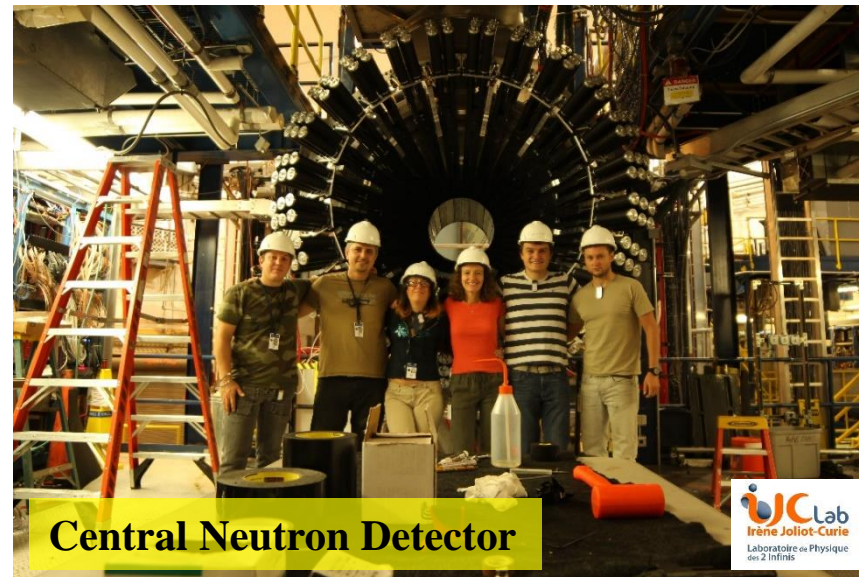
RICH



Forward Tagger

Physics goals:

- Form factors
- DIS
- SIDIS
- DVCS
- J/psi photoproduction
- Short-Range Correlations



Central Neutron Detector



BAND

Central Neutron Detector: performances with CLAS12 data

Purpose: detect the **recoiling neutron in nDVCS**

Requirements/performances:

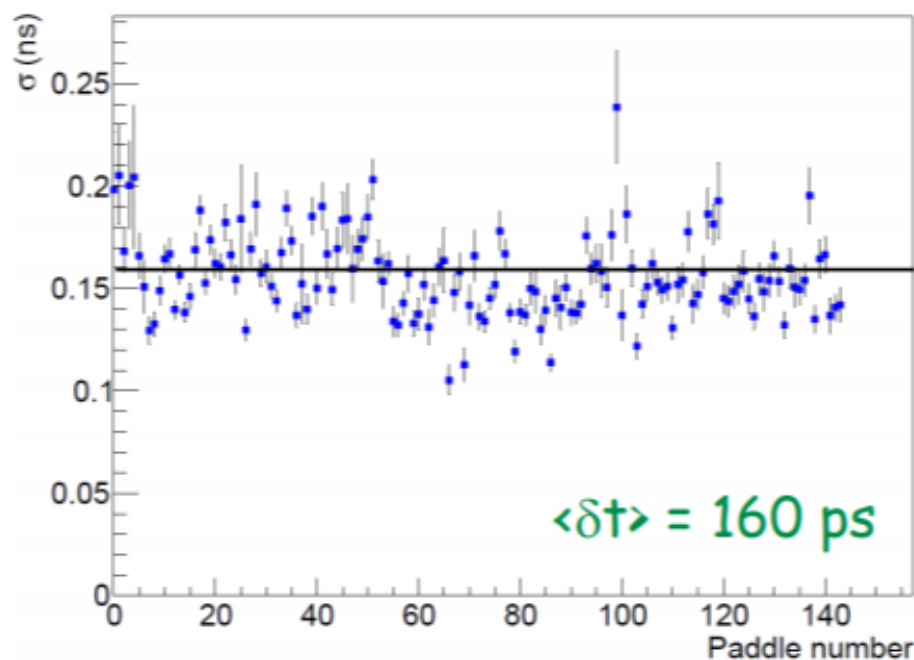
- good neutron/photon separation for $0.2 < p_n < 1$ GeV/c
→ ~ 150 ps time resolution ✓ (~ 160 ps)
- momentum resolution $\delta p/p < 10\%$ ✓
- neutron detection efficiency $\sim 10\%$ ✓

CND design: **scintillator barrel** - 3 radial layers, 48 bars per layer **coupled two-by-two** downstream by a **“u-turn” lightguide**, 144 long light guides with **PMTs** upstream

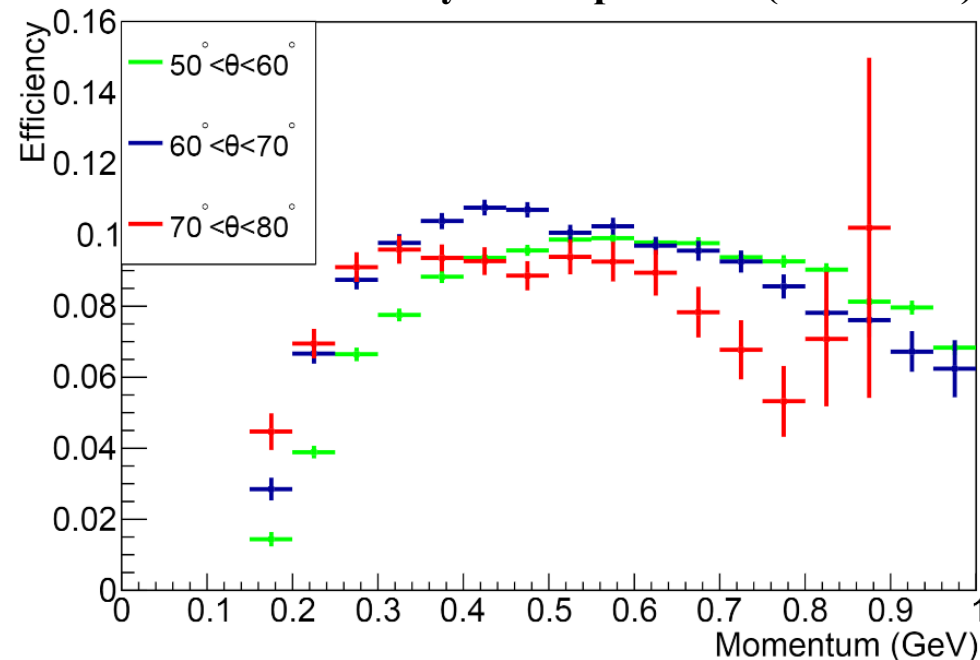
S.N. *et al.*, NIM A 904, 81 (2018)

P. Chatagnon *et al.*, NIM A 959 (2020) 163441

Timing resolution per paddle (RGB data)

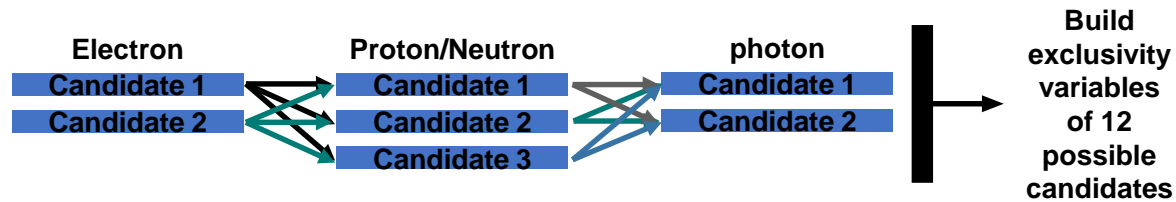


Neutron efficiency from $ep \rightarrow e' n \pi^+$ (RGA data)



Channel selection for nDVCS

- Select events with **at least one electron, one neutron, one photon**
- Final state reconstructed using **CLAS12 PID + a dedicated proton veto**, based on Machine Learning, for neutron selection optimization
 - Best candidate in event is selected based on best exclusivity criteria (a multi-dimensional χ^2 with all exclusivity variables)



- **Fiducial cuts** included for: electrons in PCAL and DC, photons in PCAL and protons in DC
- The nDVCS final state is selected using:
 - **Missing masses:** $ed \rightarrow en\gamma X$, $en \rightarrow en\gamma X$, $en \rightarrow enX$
 - **Missing momentum** (spectator proton) in $ed \rightarrow en\gamma X$
 - $\Delta\phi$, Δt : Difference between two ways of calculating ϕ and t
 - $\theta(\gamma, X)$: Cone angle between measured and reconstructed photon
- Cuts informed by **Monte Carlo simulations**:
 - GPD-based event generator for DVCS/ π^0 on deuterium
 - DVCS amplitude calculated according to the BMK formalism
 - Fermi-motion distribution evaluated according to Paris potential

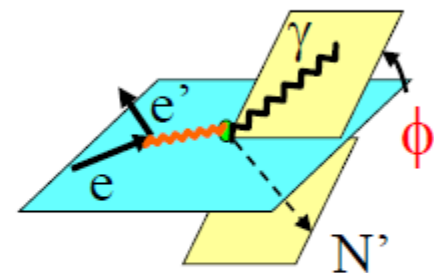
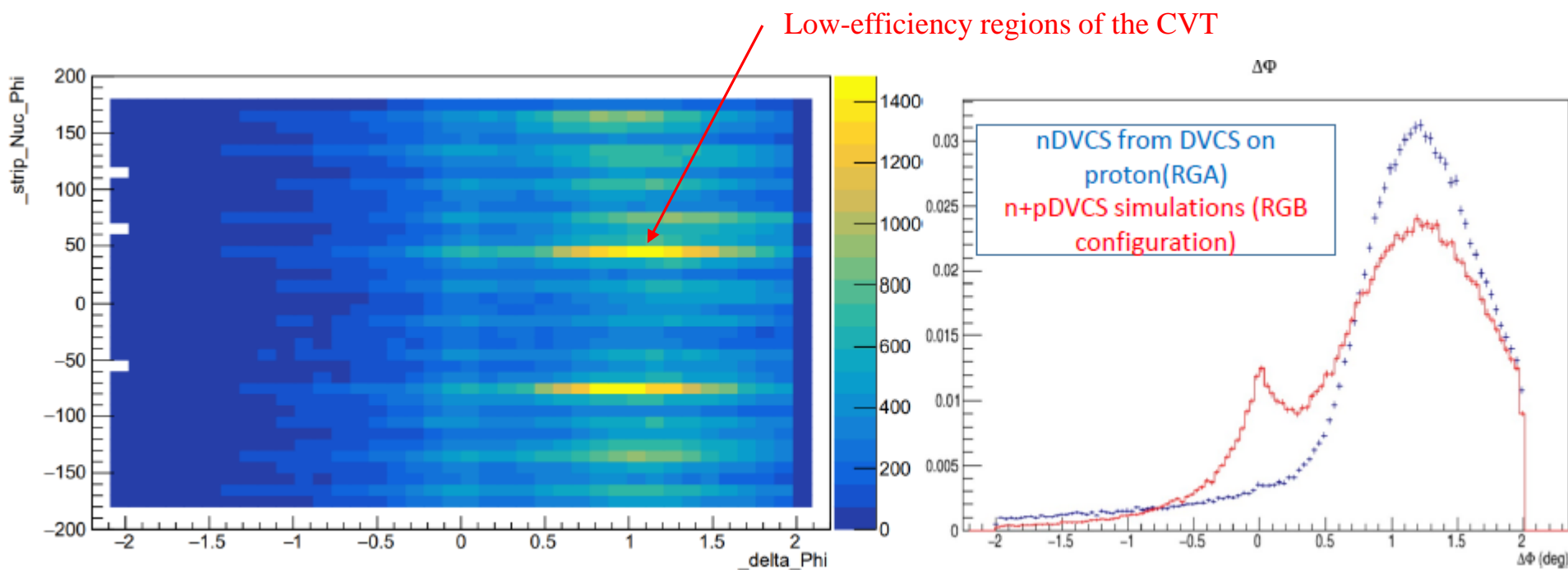
	Proton	Electron	Photon	Neutron
Momentum (GeV)	0.3	1	2	0.35
	Q ² > 1 GeV ²		W > 2 GeV ²	
$\theta(e, \gamma) > 5^\circ$	Remove radiative photons			

Proton contamination removal from CND neutrons

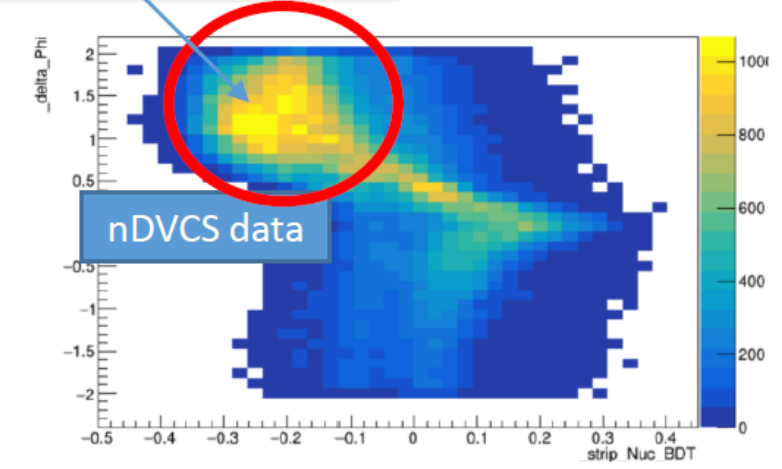
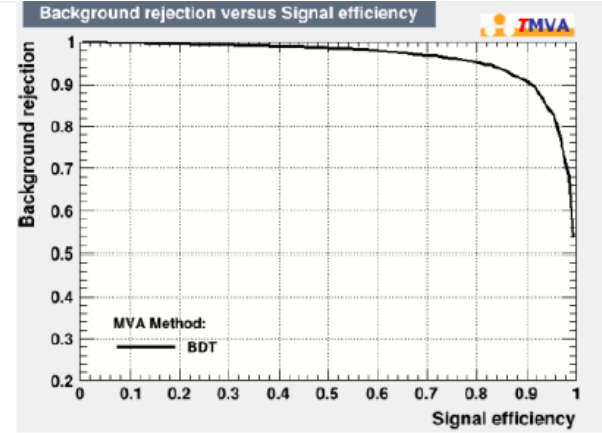
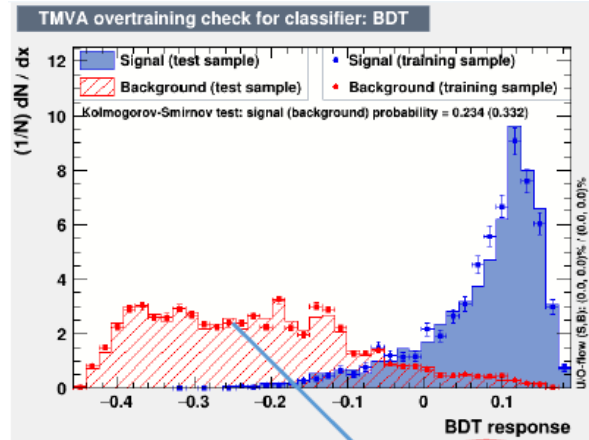
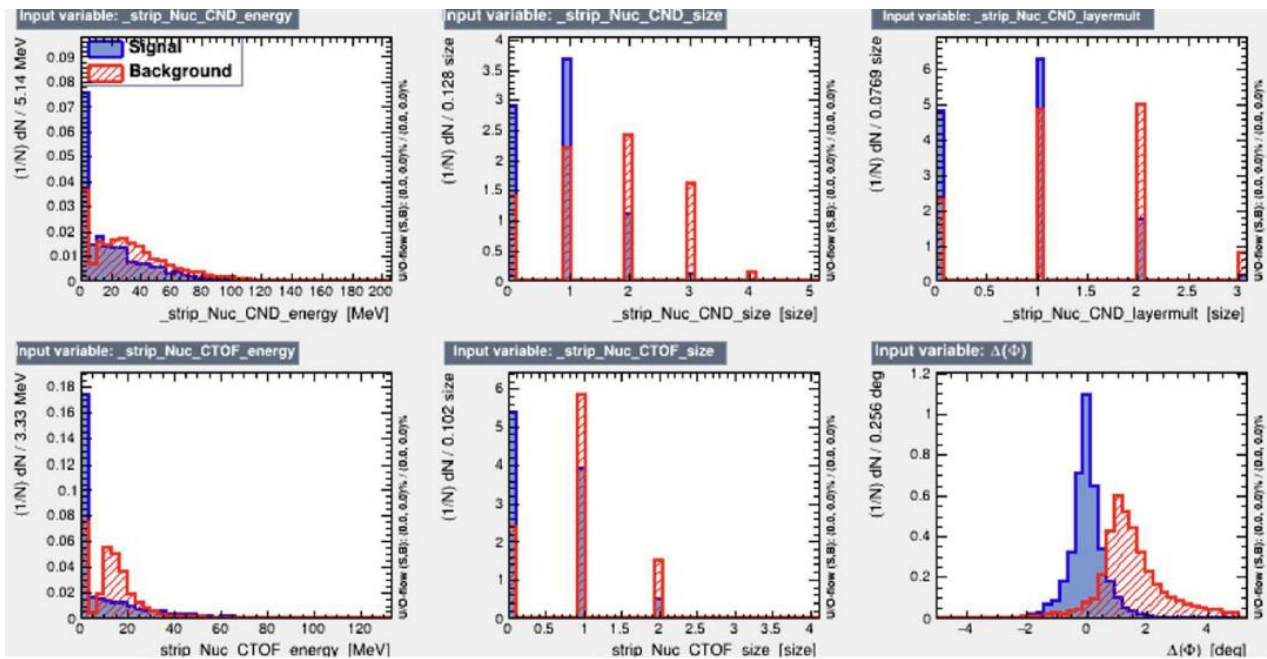
- Tracking in the CVT is not 100% efficient: in the dead regions of the Central Vertex Tracker protons can be identified as neutrons
- Protons roughly account for **more than 40% contamination** in the signal sample

Approach based on Machine Learning & Multi-Variate Algorithms:

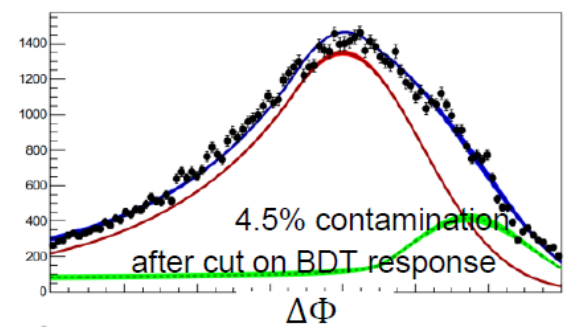
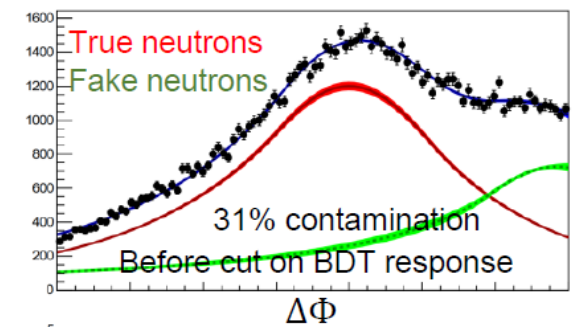
- Reconstruct nDVCS from DVCS experiment on proton (RG-A) requiring neutron PID: selected neutrons are misidentified protons
- Use this sample to determine the characteristics of fake neutrons in low and high level reconstructed variables
- Based on those characteristics, subtract the fake neutrons contamination from nDVCS
- « Signal » sample in the training of the ML: $ep \rightarrow en\pi^+$ events from RG-A



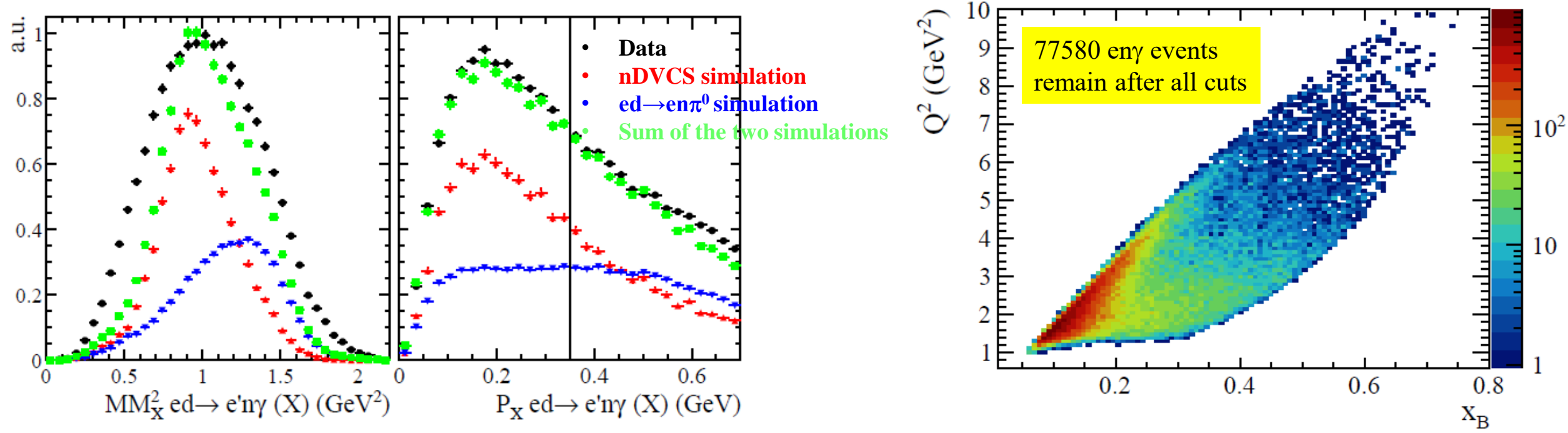
Proton contamination removal from CND neutrons



- Using detector variables (CTOF and CND) and one exclusivity variable ($\Delta\phi$)
- Directly trained on data
- Better optimization of signal to background ratio than straight cuts
- Few percent irreducible contamination corrected for in the final BSA



Selected nDVCS events sample and background subtraction



- Subtraction of the π^0 background from **simulation** and reconstructed exclusive π^0 events from **data**
 - Estimate the ratio R of partially reconstructed $\text{en}\pi^0$ (1 photon) decay to fully reconstructed $\text{en}\pi^0$ events in simulation
 - Multiply this ratio by the number of **reconstructed $\text{en}\pi^0$ in data** to get the number of $\text{en}\pi^0$ (1 photon) in data
 - Subtract this number from DVCS reconstructed decays in data **per each kinematical bin and beam helicity**

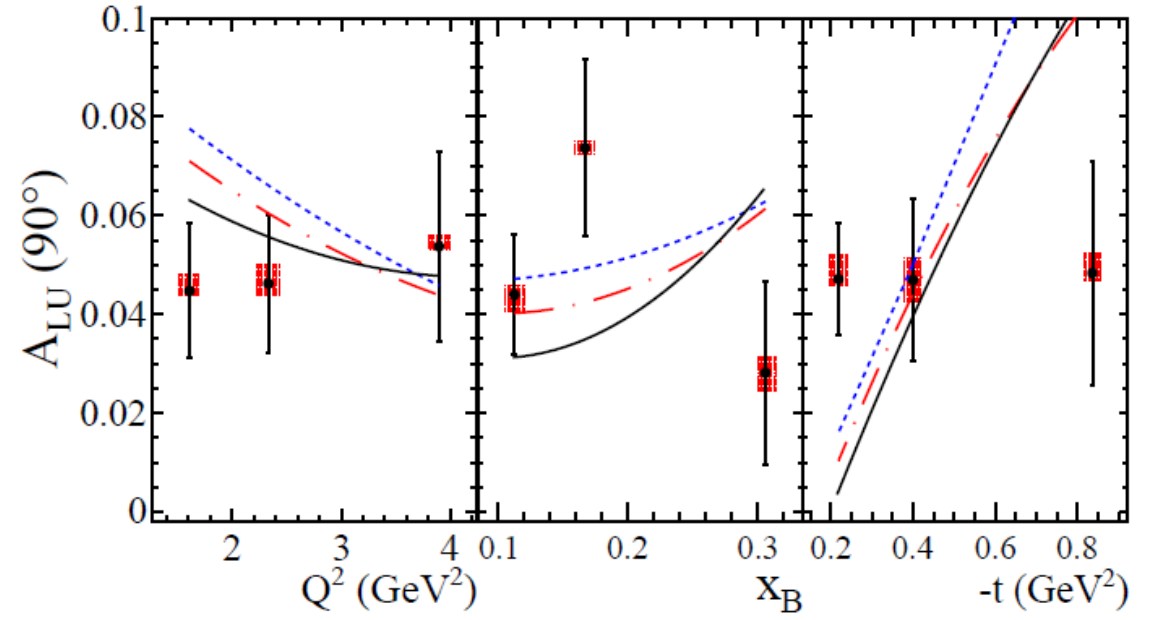
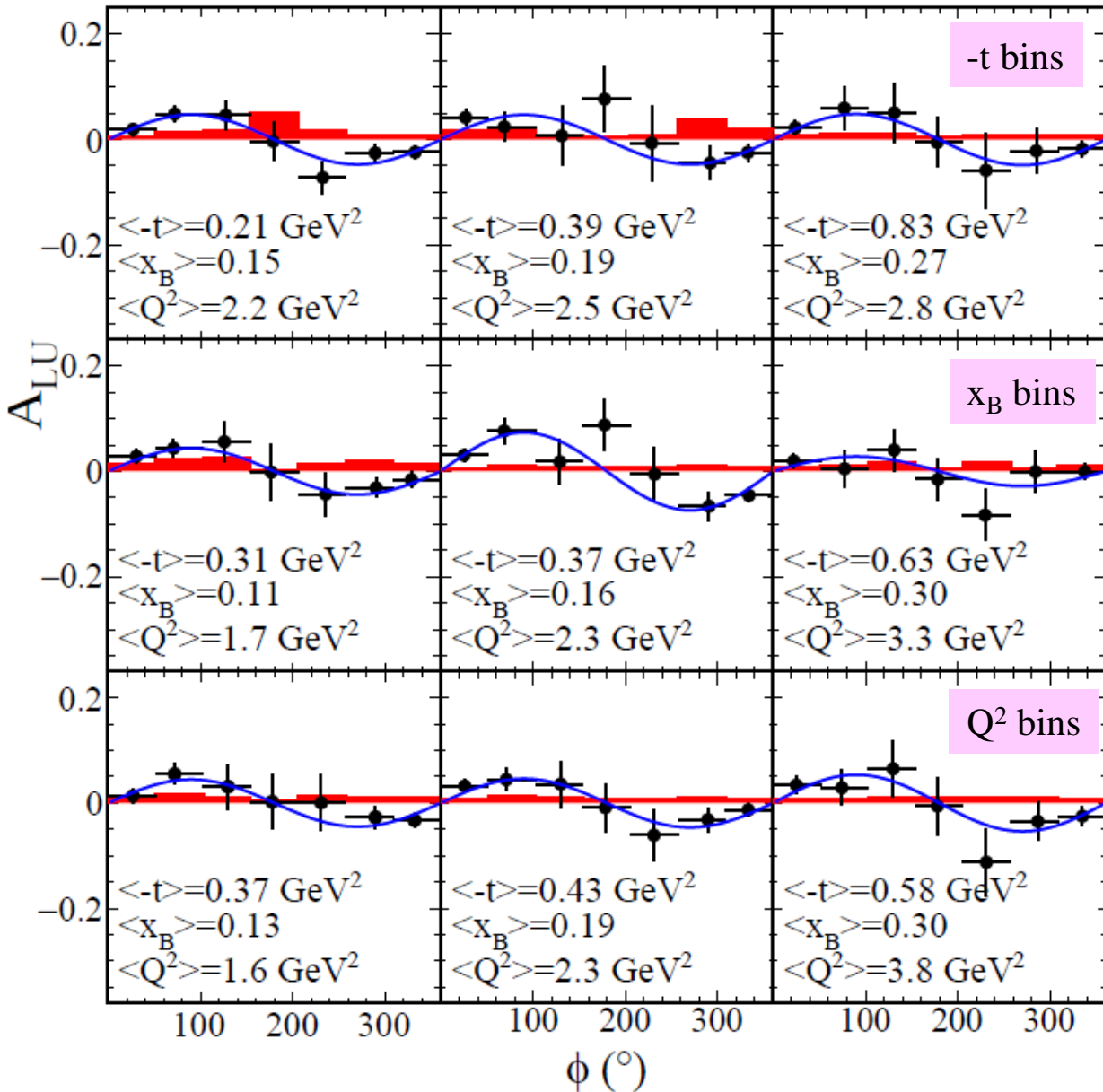
$$R = \frac{N(\text{en}\pi_{1\gamma}^0)}{N(\text{en}\pi^0)}$$

$$N(\text{en}\pi_{1\gamma}^0) = R * N(\text{en}\pi^0)$$

$$N(\text{DVCS}) = N(\text{DVCS}_{recon}) - N(\text{en}\pi_{1\gamma}^0)$$

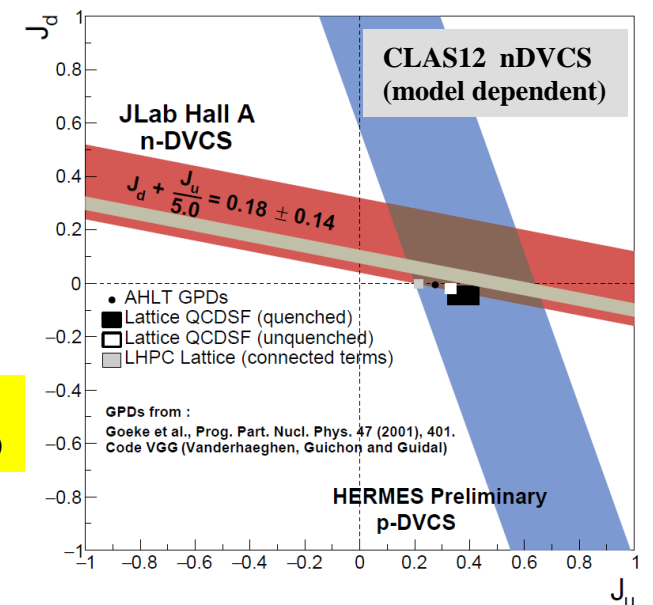
First-time measurement of BSA for nDVCS with detection of the active neutron

$$\vec{e}d \rightarrow e n \gamma (p)$$



$J_u = 0.35$ $J_d = 0.05$
 $J_u = -0.2$ $J_d = 0.15$
 $J_u = -0.45$ $J_d = 0.2$
 VGG model predictions
 giving the smallest χ^2

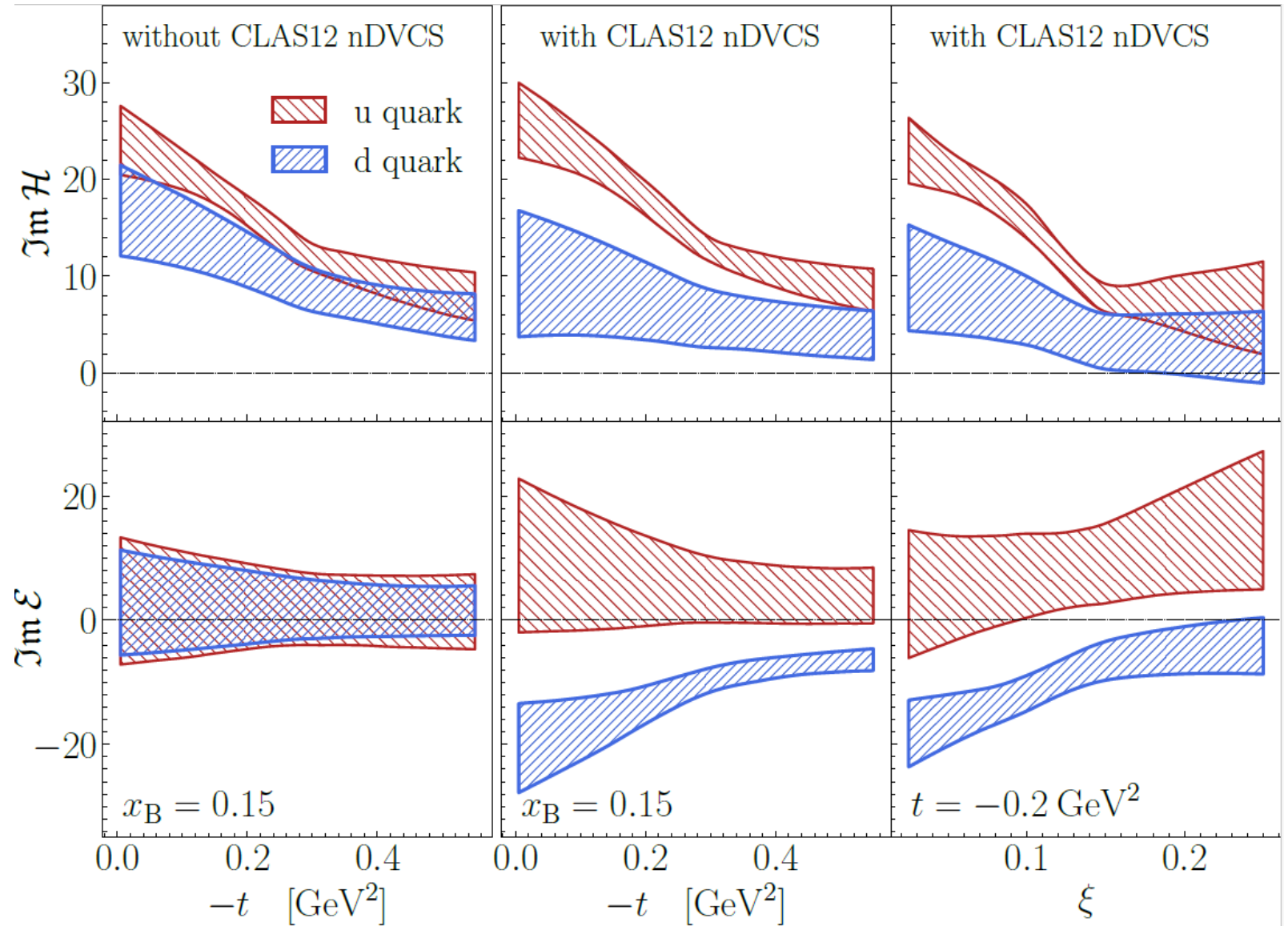
**M. Vanderhaeghen, P.A.M. Guichon,
 and M. Guidal, PRD 60, 094017 (1999)**



Flavor separation of CFFs with Hall A pDVCS and CLAS12 p,n DVCS data

- Global fits of CFF using neural networks (K. Kumericki et al., JHEP 07, 073531 (2011); M. Cuic, K. Kumericki, et al., Phys. Rev. Lett. 533 125, 232005 (2020)).
- Data used: CLAS6 and HERMES pDVCS observables, CLAS12 pDVCS BSA and nDVCS BSA
- Same extraction method applied to nDVCS Hall-A data, only separation for $\text{Im}\mathcal{H}$

The CLAS12 nDVCS data allow the quark-flavor separation of both $\text{Im}\mathcal{H}$ and $\text{Im}\mathcal{E}$



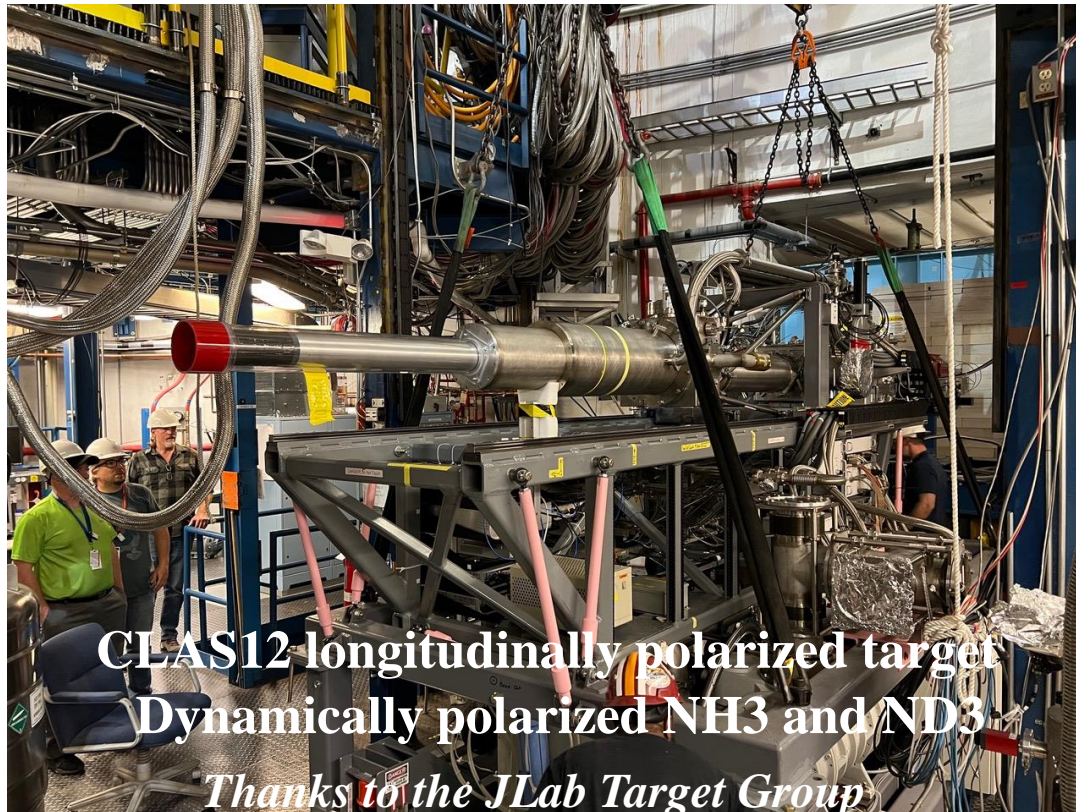
Recently run with CLAS12: DVCS (p, n) on longitudinally polarized target

First-time measurement of longitudinal target-spin asymmetry and double (beam-target) spin asymmetry for nDVCS

$$\Delta\sigma_{UL} \sim \sin\phi \operatorname{Im}\{F_1\tilde{\mathcal{H}} + \xi(F_1 + F_2)(\mathcal{H} + x_B/2\mathcal{E}) - \xi kF_2\tilde{\mathcal{E}} + \dots\}$$

$$\Delta\sigma_{LL} \sim (\mathbf{A} + \mathbf{B}\cos\phi) \operatorname{Re}\{F_1\tilde{\mathcal{H}} + \xi(F_1 + F_2)(\mathcal{H} + x_B/2\mathcal{E}) - \xi kF_2\tilde{\mathcal{E}} + \dots\}$$

→ 3 observables (including BSA), constraints on real and imaginary CFFs of various **neutron GPDs**



$$\vec{e}\vec{p} \rightarrow ep\gamma$$
$$\vec{e}\vec{d} \rightarrow e(p)n\gamma$$

CLAS12 + Longitudinally polarized target + CND

Ran from June 2022 to March 2023

Ultimate goals: flavor separation of CFFs & Ji's sum rule

See Noémie Pilleux's talk

Summary and outlook

- The **beam-spin asymmetry for nDVCS** is a precious tool to constrain the GPD E and for quark-flavor separation of GPDs
- **CLAS12** measured the **BSA for nDVCS with detected neutron for the first time**
- The first **~43%** of the experiment ran in 2019-2020 at JLab
- The **Central Neutron Detector** performed according to specifications
- A small but clear **BSA was extracted**
- Comparison with a model allows to put **model-dependent constraints on J_d**
- The data, together with the proton DVCS data, allow the **quark-flavor separation of ImH and ImE**
- An article is **ready for submission to PRL**
- A first-time measurement of **BSA for incoherent pDVCS** on deuterium is in progress
- Another nDVCS experiment on **polarized deuterium target** was carried out in 2022-2023 with CLAS12
- The second half of Run Group B will run with **double luminosity** following the CLAS12 high-lumi upgrade
- A **transversely polarized target pDVCS experiment** is foreseen for ~2028 with CLAS12
- The combination of all neutron and proton DVCS data will allow **quark-flavor separation of all CFFs** in the valence regime
- The **J_i 's sum rule** is the ultimate, ambitious goal of this program

First Measurement of Deeply Virtual Compton Scattering on the Neutron with Detection of the Active Neutron

A. Hobart,¹ S. Niccolai,¹ M. Čuić,² K. Kumerički,² P. Achenbach,³ J.S. Alvarado,¹ W.R. Armstrong,⁴ H. Atac,⁵ H. Avakian,³ N.A. Baltzell,³ L. Barion,⁶ M. Bashkanov,⁷ M. Battaglieri,^{3,8,*} B. Benkel,⁹ F. Benmokhtar,¹⁰ A. Bianconi,^{11,12} A.S. Biselli,¹³ S. Boiarinov,³ M. Bondi,¹⁴ W.A. Booth,⁷ F. Bossi,¹⁵ K.-Th. Brinkmann,¹⁶ W.J. Briscoe,¹⁷ W.K. Brooks,¹⁸ S. Bueltmann,¹⁹ V.D. Burkert,³ T. Cao,³ R. Capobianco,²⁰ D.S. Carman,³ P. Chatagnon,^{3,1} G. Ciullo,^{6,21} P.L. Cole,²² M. Contalbrigo,⁶ A. D'Angelo,^{9,23} N. Dashyan,²⁴ R. De Vita,^{8,†} M. Defurne,¹⁵ A. Deur,³ S. Diehl,^{16,20} C. Dilks,^{3,25} C. Djalali,²⁶ R. Dupre,¹ H. Egiyan,³ A. El Alaoui,¹⁸ L. El Fassi,²⁷ L. Elouadrhiri,²⁸ S. Fegan,⁷ A. Filippi,²⁹ C. Fogler,¹⁹ K. Gates,³⁰ G. Cavalian,^{3,31} G.P. Gilfoyle,³² D. Glazier,³⁰ R.W. Gothe,³³ Y. Gotra,³ M. Guidal,¹ K. Hafidi,⁴ H. Hakobyan,¹⁸ M. Hattawy,¹⁹ F. Hauenstein,^{3,19} D. Heddle,^{28,3} M. Holtrop,³¹ Y. Ilieva,^{33,17} D.G. Ireland,³⁰ E.L. Isupov,³⁴ H. Jiang,³⁰ H.S. Jo,³⁵ K. Joo,²⁰ T. Kageya,³ A. Kim,²⁰ W. Kim,³⁵ V. Klimenko,²⁰ V. Kubarovsky,^{3,36} S.E. Kuhn,¹⁹ L. Lanza,^{9,23} M. Lesli,^{11,12} S. Lee,^{4,37} P. Lenisa,^{6,21} X. Li,³⁷ I.J.D. MacGregor,³⁰ D. Marchand,¹ V. Mascagna,^{11,38,12} B. McKinnon,³⁰ Z.E. Meziani,⁴ S. Migliorati,^{11,12} R.G. Milner,³⁷ T. Mineeva,¹⁸ M. Mirazita,³⁹ V. Mokeev,^{3,34} C. Muñoz Camacho,¹ P. Nadel-Turonski,³ P. Naidoo,³⁰ K. Neupane,³³ G. Niculescu,⁴⁰ M. Osipenko,⁵ P. Pandey,³⁷ M. Paolone,^{41,5} L.L. Pappalardo,^{6,21} R. Paremuzyan,^{3,31} E. Pasyuk,³ S.J. Paul,⁴² W. Phelps,²⁸ N. Pilleux,¹ M. Pohlrel,¹⁹ S. Polcher Rafael,¹⁵ J. Poudel,³ J.W. Price,⁴³ Y. Prok,¹⁹ T. Reed,⁴⁴ J. Richards,²⁰ M. Ripani,⁸ J. Ritman,^{45,46} P. Rossi,³ A.A. Golubenko,³⁴ C. Salgado,⁴⁷ S. Schadmand,^{45,46} A. Schmidt,¹⁷ E.M. Seroka,¹⁷ Y.G. Sharabian,³ E.V. Shirokov,³⁴ U. Shrestha,^{20,26} N. Sparveris,⁵ M. Spreafico,⁸ S. Stepanyan,³ I.I. Strakovsky,¹⁷ S. Strauch,^{39,17} J.A. Tan,³⁵ N. Trotta,²⁰ R. Tyson,³ M. Ungaro,³ S. Vallarino,⁸ L. Venturini,^{11,12} V. Tommaso,⁸ E. Voutier,¹ D.P. Watts,⁷ X. Wei,³ R. Williams,⁷ M.H. Wood,^{48,33} L. Xu,¹ N. Zachariou,⁷ J. Zhang,⁴⁹ Z.W. Zhao,²⁵ and M. Zurek⁴

(The CLAS Collaboration)

¹ Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France

² Department of Physics, Faculty of Science, University of Zagreb, 10000 Zagreb, Croatia

³ Thomas Jefferson National Accelerator Facility, Newport News, Virginia 23606

⁴ Argonne National Laboratory, Argonne, Illinois 60439

⁵ Temple University, Philadelphia, Pennsylvania 19122

⁶ INFN, Sezione di Ferrara, 44100 Ferrara, Italy

⁷ University of York, York YO10 5DD, United Kingdom

⁸ INFN, Sezione di Genova, 16146 Genova, Italy

⁹ INFN, Sezione di Roma Tor Vergata, 00133 Rome, Italy

¹⁰ Duquesne University, 600 Forbes Avenue, Pittsburgh, Pennsylvania 15282

¹¹ Università degli Studi di Brescia, 25123 Brescia, Italy

¹² INFN, Sezione di Pavia, 27100 Pavia, Italy

¹³ Fairfield University, Fairfield, Connecticut 06824

¹⁴ INFN - Sezione di Catania, 95123 Catania, Italy

¹⁵ IRFU, CEA, Université Paris-Saclay, F-91191 Gif-sur-Yvette, France

¹⁶ II Physikalisches Institut der Universität Gießen, 35392 Gießen, Germany

¹⁷ The George Washington University, Washington, DC 20052

¹⁸ Universidad Técnica Federico Santa María, Castilla 110-V Valparaíso, Chile

¹⁹ Old Dominion University, Norfolk, Virginia 23529

²⁰ University of Connecticut, Storrs, Connecticut 06269

²¹ Università di Ferrara, 44121 Ferrara, Italy

²² Lamar University, 4400 MLK Blvd, PO Box 10046, Beaumont, Texas 77710

²³ Università di Roma Tor Vergata, 00133 Rome, Italy

²⁴ Yerevan Physics Institute, 375036 Yerevan, Armenia

²⁵ Duke University, Durham, North Carolina 27708-0305

²⁶ Ohio University, Athens, Ohio 45701

²⁷ Mississippi State University, Mississippi State, Mississippi 39762-5167

²⁸ Christopher Newport University, Newport News, Virginia 23606

²⁹ INFN, Sezione di Torino, 10125 Torino, Italy

³⁰ University of Glasgow, Glasgow G12 8QQ, United Kingdom

³¹ University of New Hampshire, Durham, New Hampshire 03824-3568

³² University of Richmond, Richmond, Virginia 23173

³³ University of South Carolina, Columbia, South Carolina 29208

³⁴ Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, 119234 Moscow, Russia

³⁵ Kyungpook National University, Daegu 41566, Republic of Korea