

Peter Hurck for the GlueX collaboration

Hadron spectroscopy at GlueX



University
of Glasgow

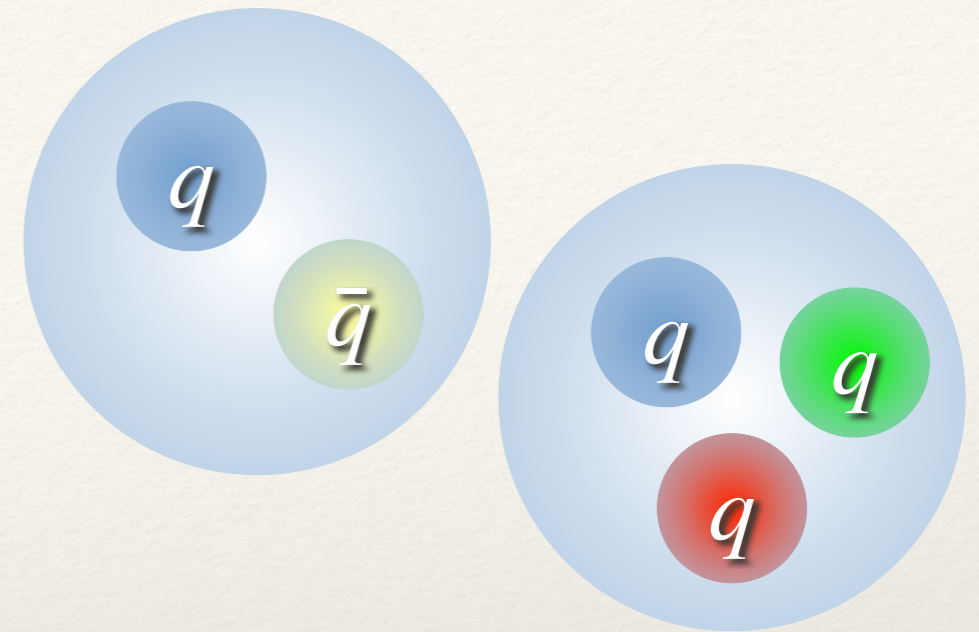
NSTAR 2024

Hilton Hotel York



Introduction

- ❖ QCD gives rise to spectrum of hadrons
- ❖ Many $q\bar{q}$ and qqq states have been observed
- ❖ $q\bar{q}q\bar{q}$, $qqqq\bar{q}$, ... are not forbidden!



A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN

California Institute of Technology, Pasadena, California

Received 4 January 1964

... Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. ...

Phys. Lett. 8 (1964) 214

- ❖ $q\bar{q}g$ are also allowed!
- ❖ so are g -only states

Introduction

- ❖ QCD gives rise to spectrum of hadrons
- ❖ Many $q\bar{q}$ and qqq states have been observed
- ❖ $q\bar{q}q\bar{q}$, $qqqq\bar{q}$, ... are not forbidden!

A SCHEMATIC MODEL OF BARYONS AND MESONS *

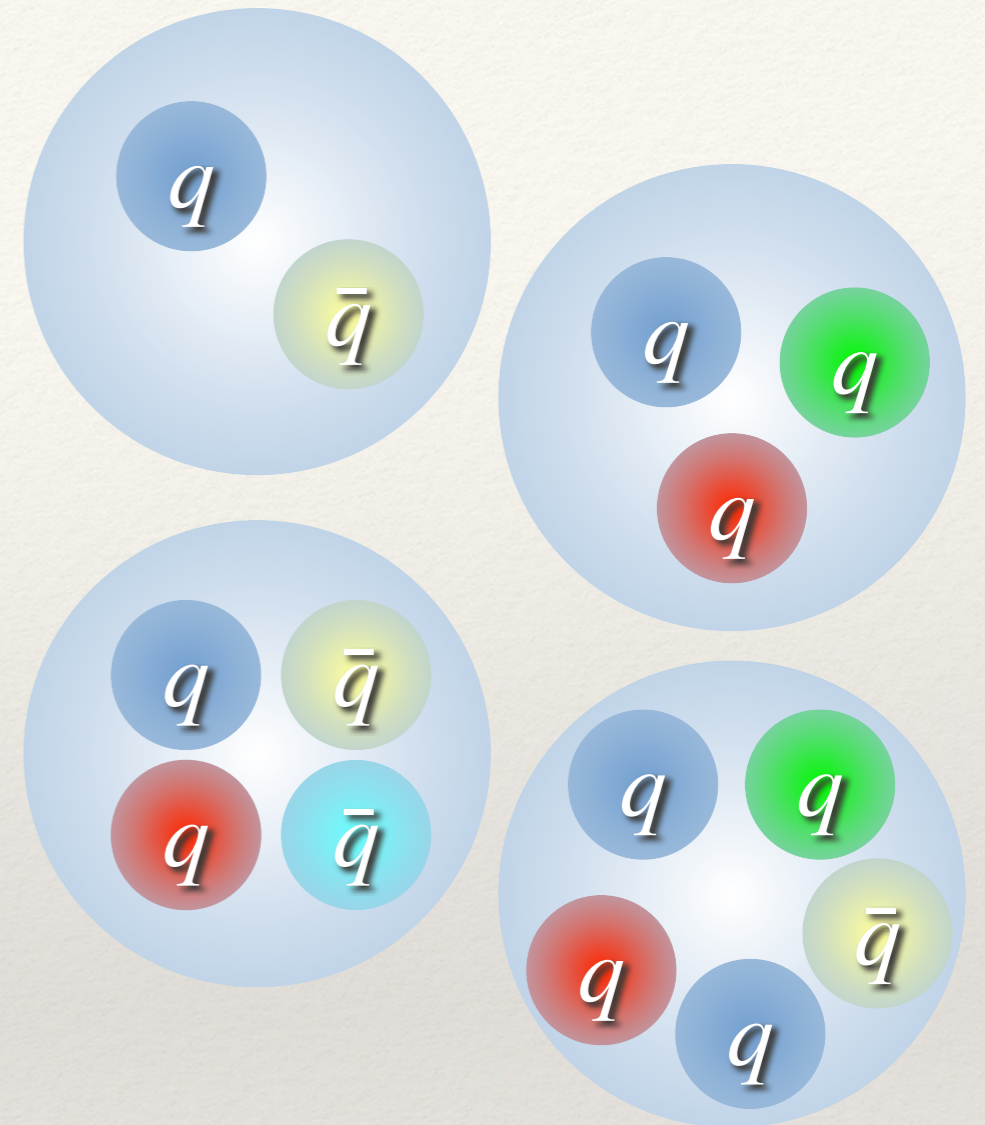
M. GELL-MANN

California Institute of Technology, Pasadena, California

Received 4 January 1964

... Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. ...

Phys. Lett. 8 (1964) 214



- ❖ $q\bar{q}g$ are also allowed!
- ❖ so are g -only states

Introduction

- ❖ QCD gives rise to spectrum of hadrons
- ❖ Many $q\bar{q}$ and qqq states have been observed
- ❖ $q\bar{q}q\bar{q}$, $qqqq\bar{q}$, ... are not forbidden!

A SCHEMATIC MODEL OF BARYONS AND MESONS *

M. GELL-MANN

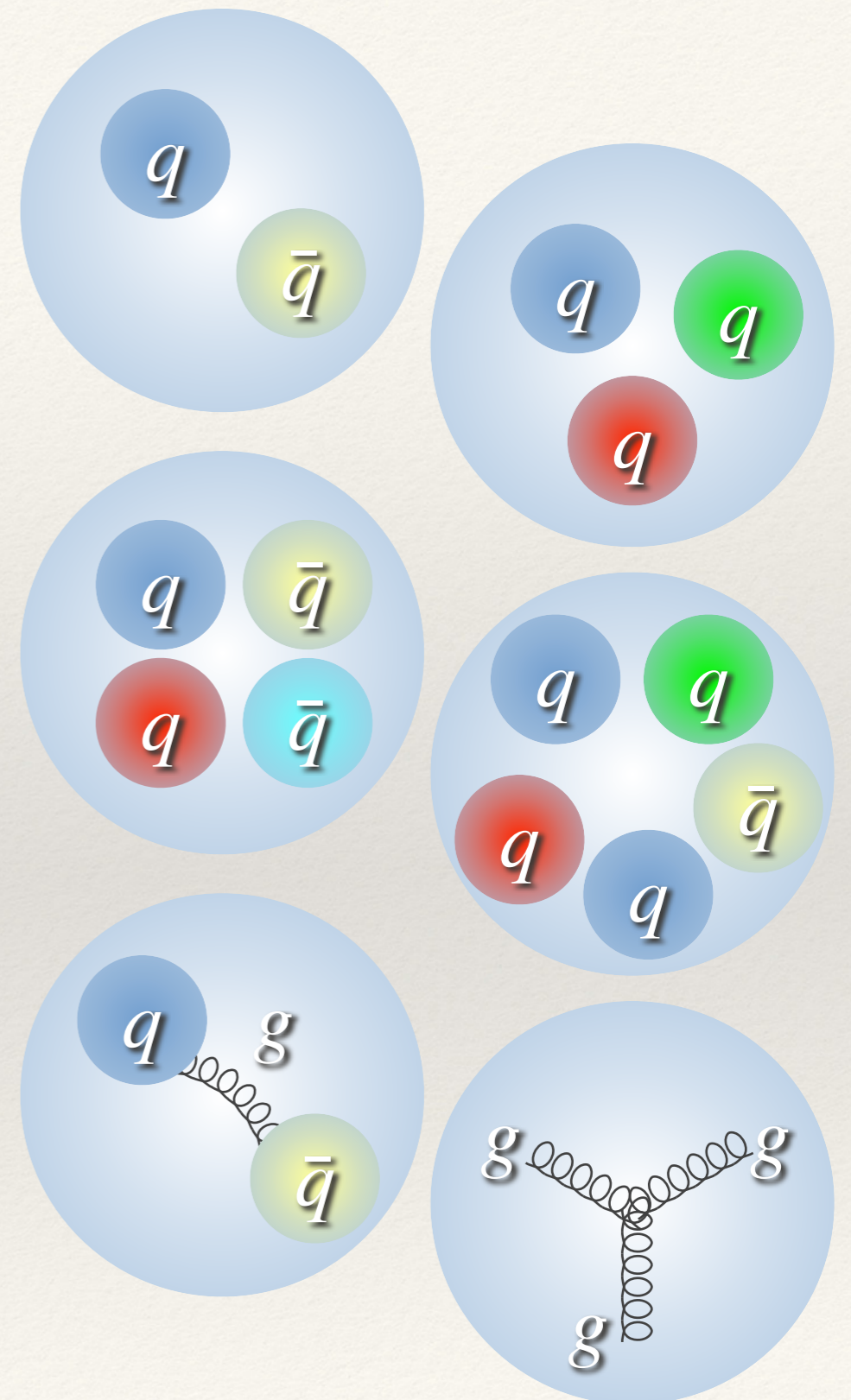
California Institute of Technology, Pasadena, California

Received 4 January 1964

... Baryons can now be constructed from quarks by using the combinations (qqq) , $(qqqq\bar{q})$, etc., while mesons are made out of $(q\bar{q})$, $(qq\bar{q}\bar{q})$, etc. ...

Phys. Lett. 8 (1964) 214

- ❖ $q\bar{q}g$ are also allowed!
- ❖ so are g -only states



Hybrid mesons

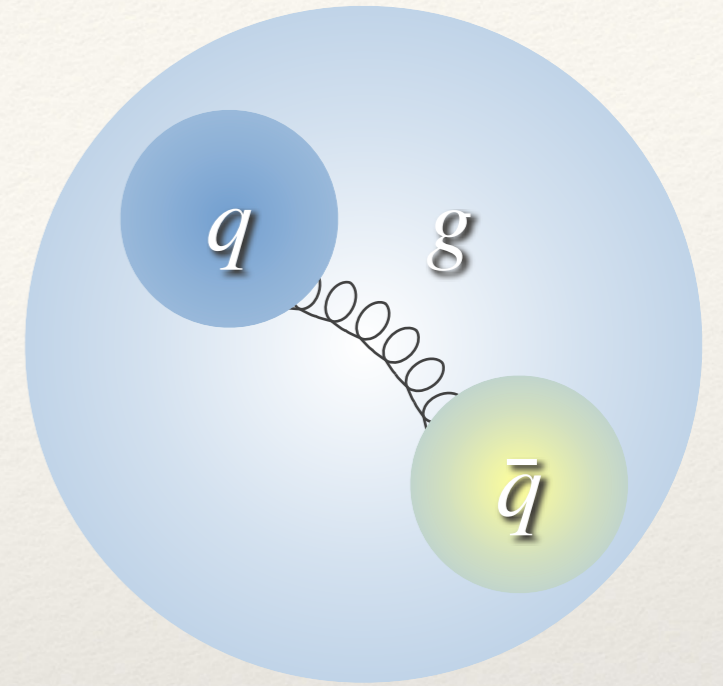
- ❖ main objective for GlueX:
Search and study of hybrid mesons

- ❖ In quark model:
 $\vec{J} = \vec{L} + \vec{S}$, $P = (-1)^{L+1}$, $C = (-1)^{L+S}$

→ not allowed:

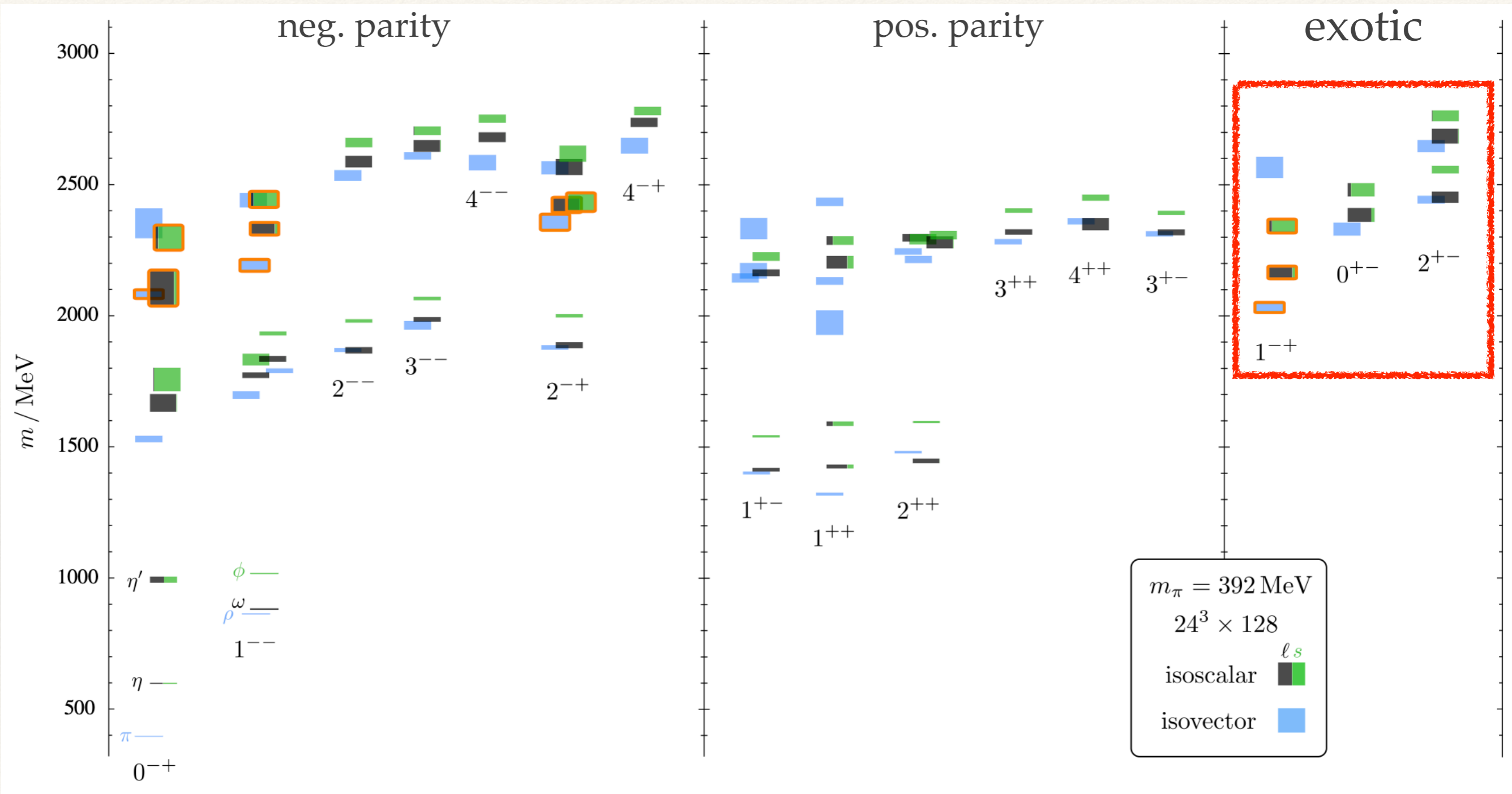
$$J^{PC} = 0^{--}, 0^{+-}, 1^{-+}, 2^{+-}, \dots$$

- ❖ “Exotic” quantum numbers are “smoking gun” for something not being pure $q\bar{q}$



Light quark mesons from lattice QCD

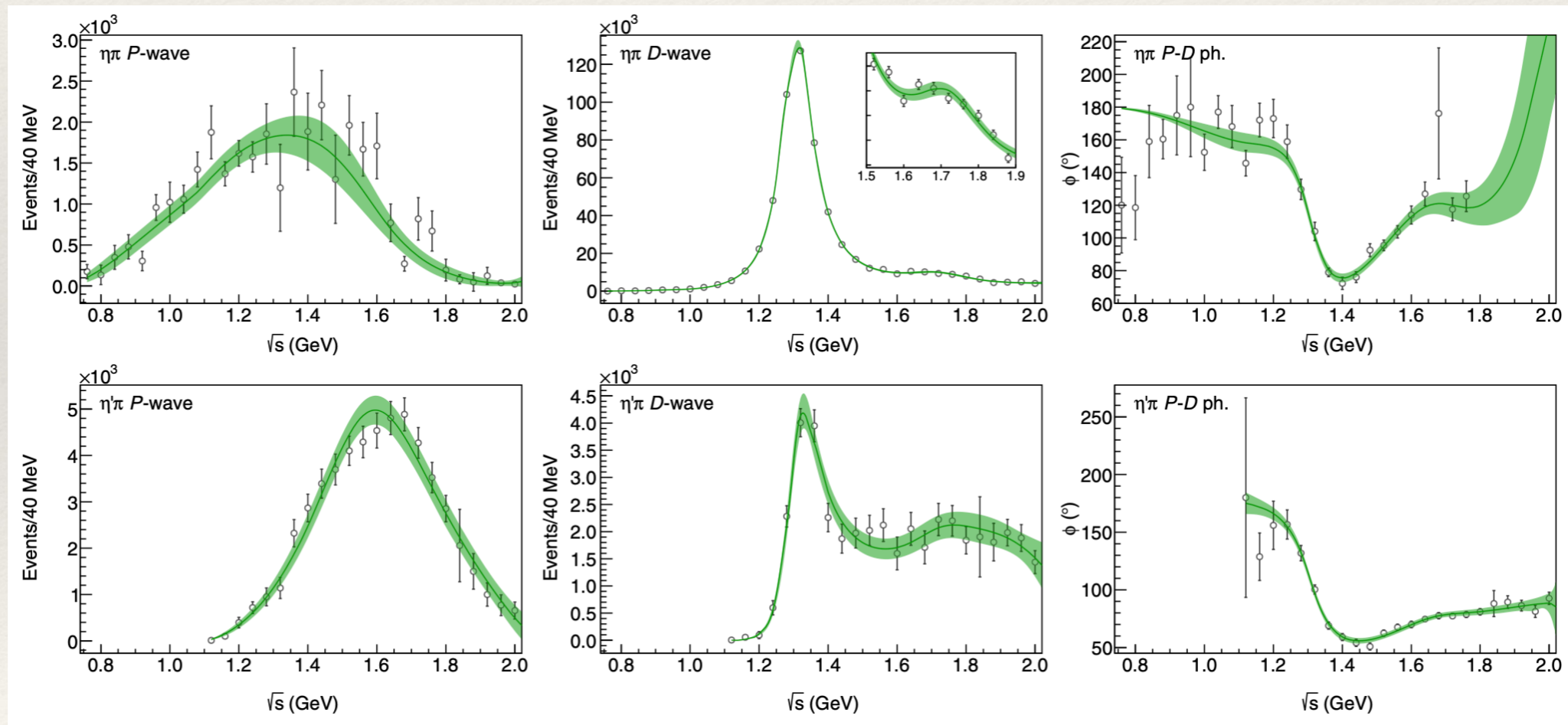
hadspec collaboration



hadspec, Phys. Rev. D 88, 094505

Hybrid mesons - evidence

- ❖ Experimental evidence for a 1^{-+} :
 - ❖ $\pi_1(1400)$: GAMS, VES, E852, CBAR, COMPASS
 - ❖ $\pi_1(1600)$: VES, E852, COMPASS
- ❖ JPAC coupled channel fit to $\eta\pi$ and $\eta'\pi$ data from COMPASS

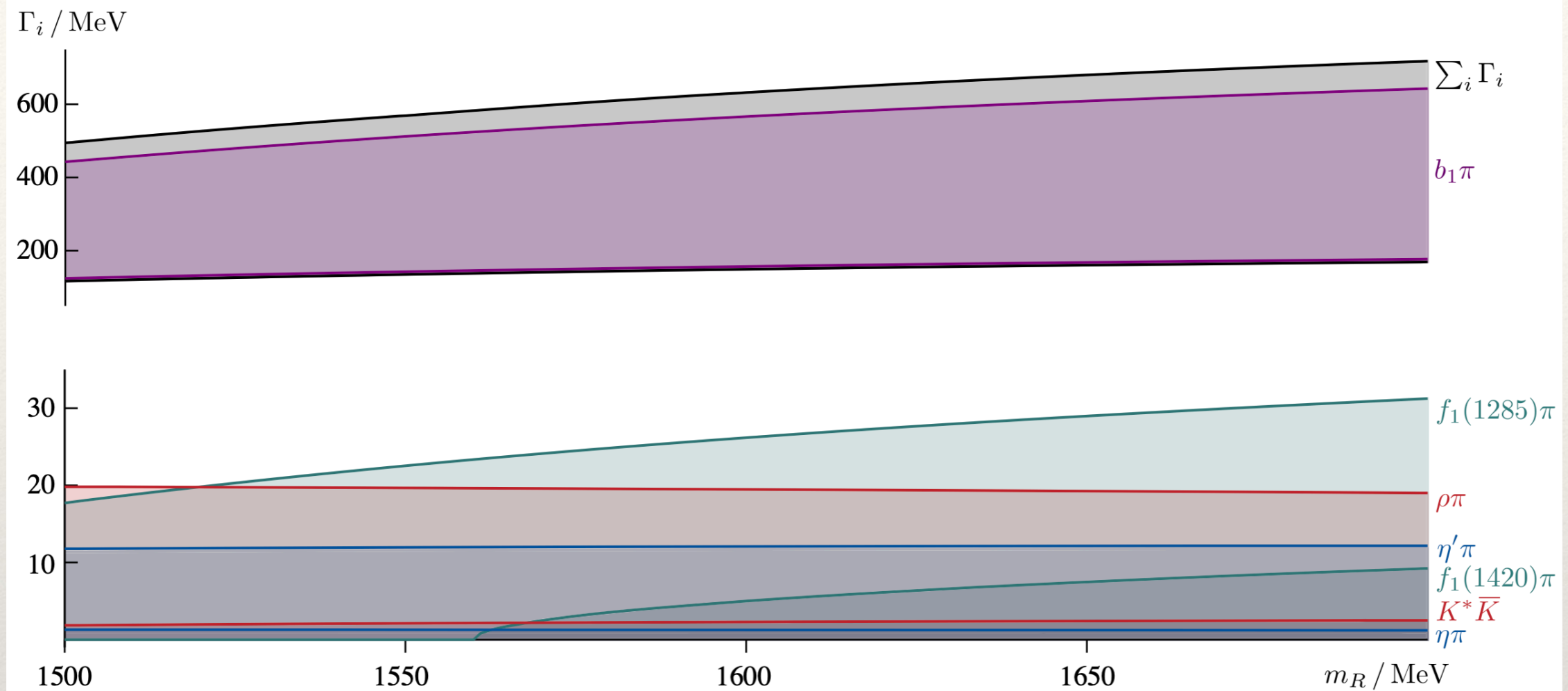


mass = $1564 \pm 24 \pm 86$ MeV width = $492 \pm 54 \pm 102$ MeV

1^{-+} hybrid from lattice QCD

hadspec collaboration

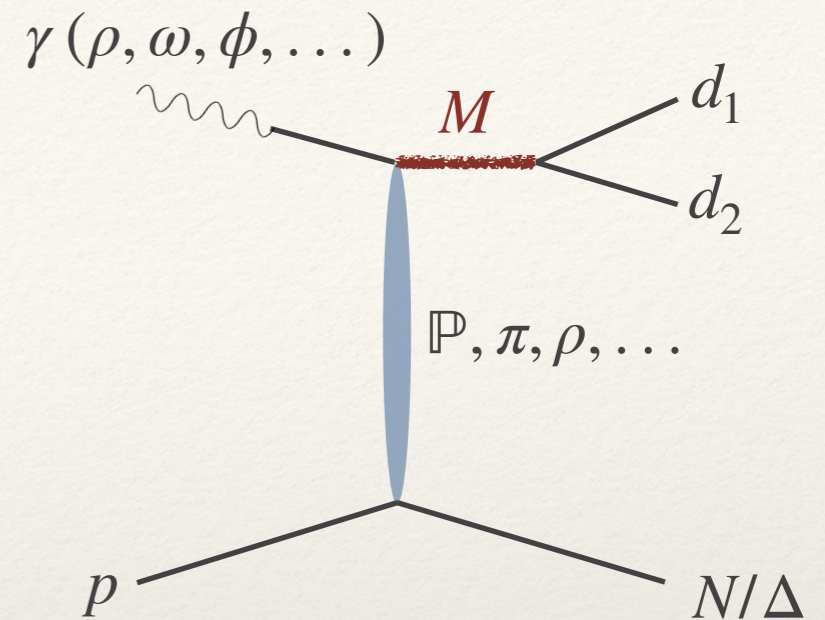
hadspec, Phys. Rev. D 103, 054502



- ❖ LQCD indicates that $b_1\pi$ is the dominant decay mode
- ❖ Experimentally challenging
- ❖ Start with $\eta\pi, \eta'\pi$
- ❖ Smaller expected branching ratio but large statistics
- ❖ Narrow peaks and pseudo scalars

Towards hybrids at GlueX

- ❖ Photoproduction complementary to pion production
- ❖ Utilize polarization to understand production mechanisms
- ❖ Study production mechanisms to inform choice of wave sets for PWA (beam asymmetries, spin density matrix elements)
- ❖ Focus on $\eta\pi$ and $\eta'\pi$
 - ❖ Look at different production and decay mechanisms
- ❖ Work closely with theory colleagues to tackle model complexity

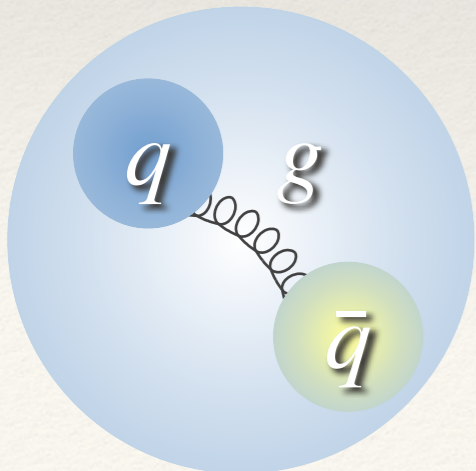
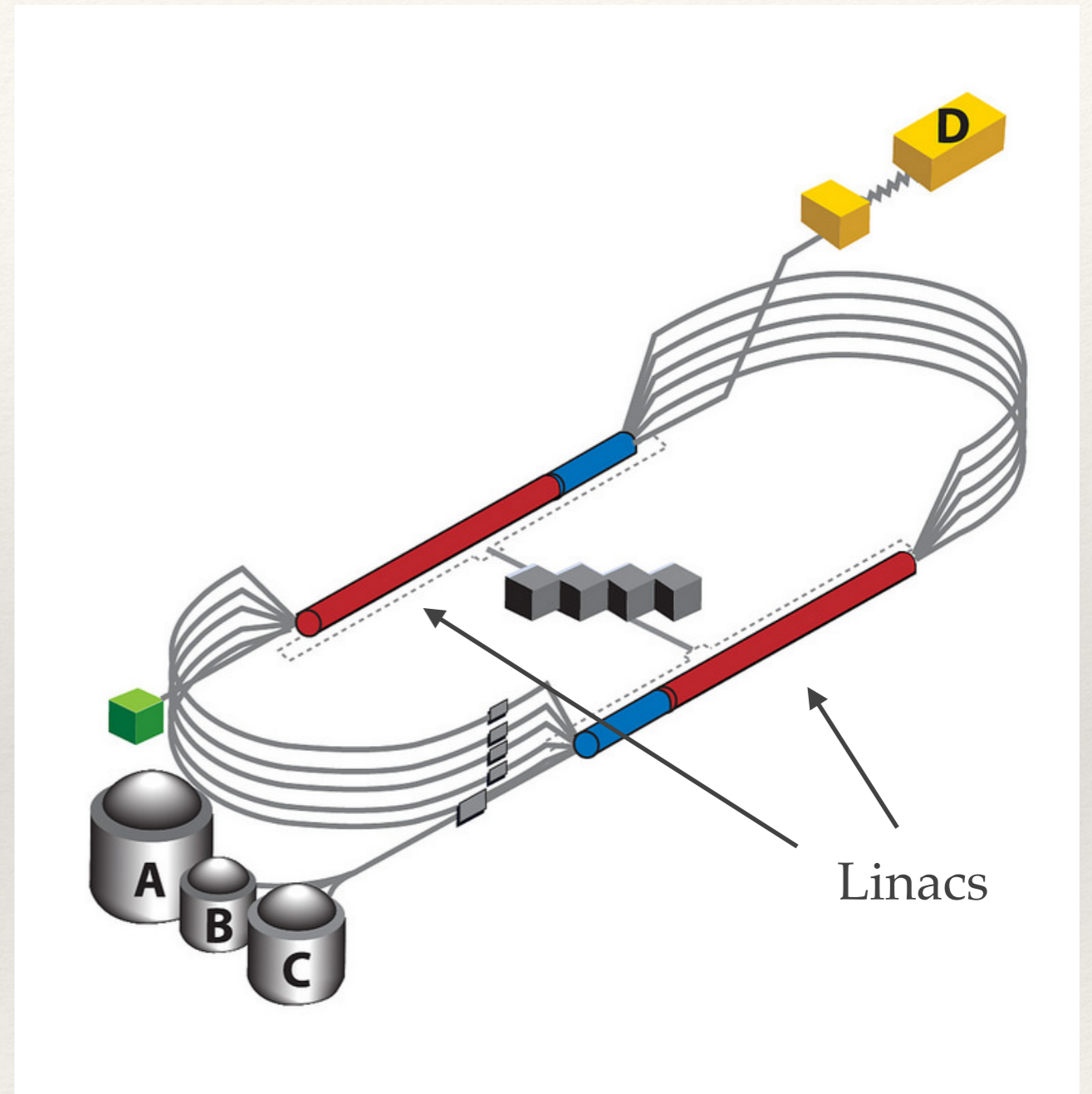


CEBAF at Jefferson Lab

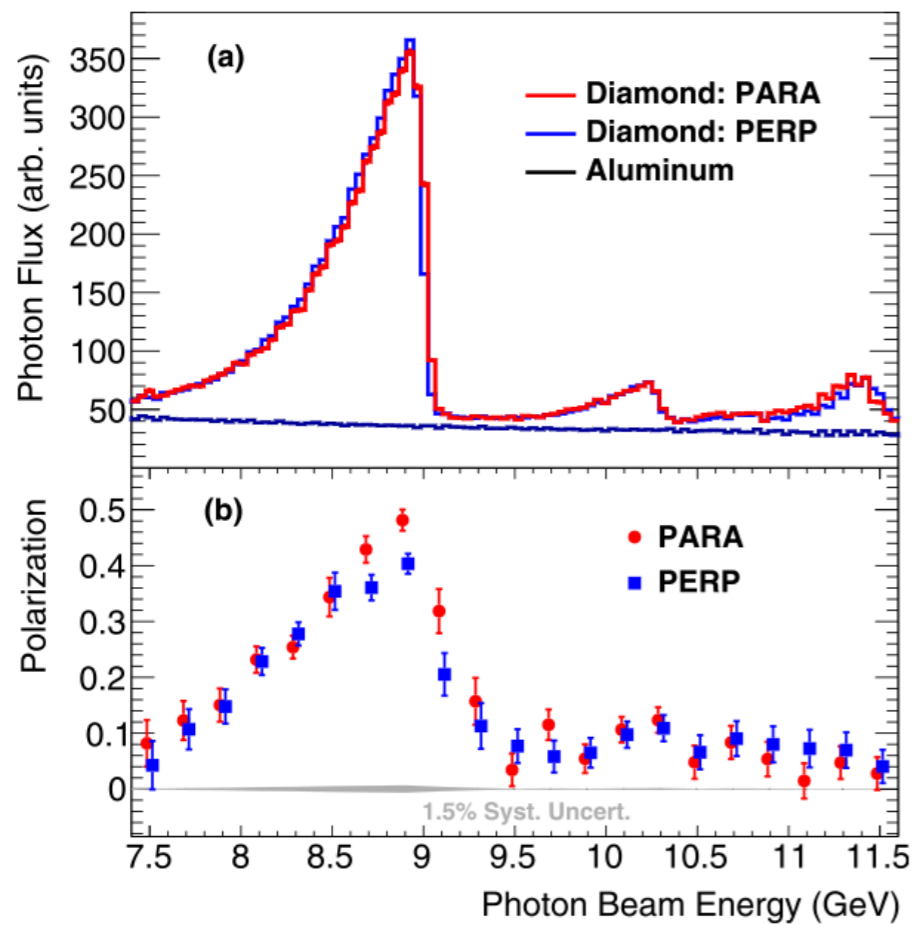


CEBAF at Jefferson Lab

- ❖ up to 12 GeV electron beam
- ❖ high luminosities for Hall A/C (high resolution spectrometer)
- ❖ CLAS12 in Hall B
- ❖ GlueX in Hall D
- ❖ Focus on exotic hybrid mesons
BUT:
Large data set available to study wide range of reactions

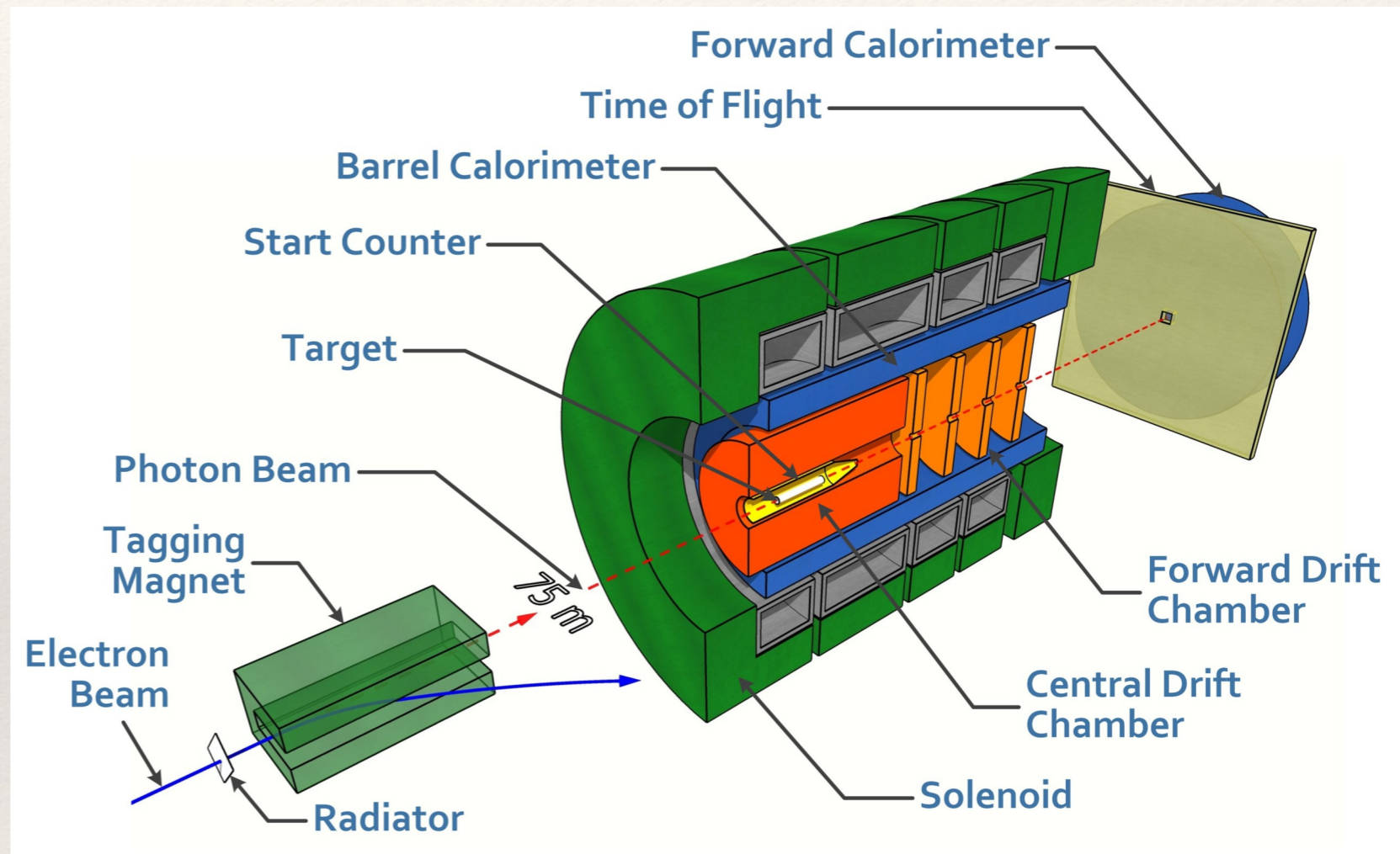


GlueX experiment in Hall D



GlueX, Nucl. Instrum. Meth. A 987 (2021) 164807

- ❖ produce linearly polarized photon beam via coherent bremsstrahlung on thin diamond

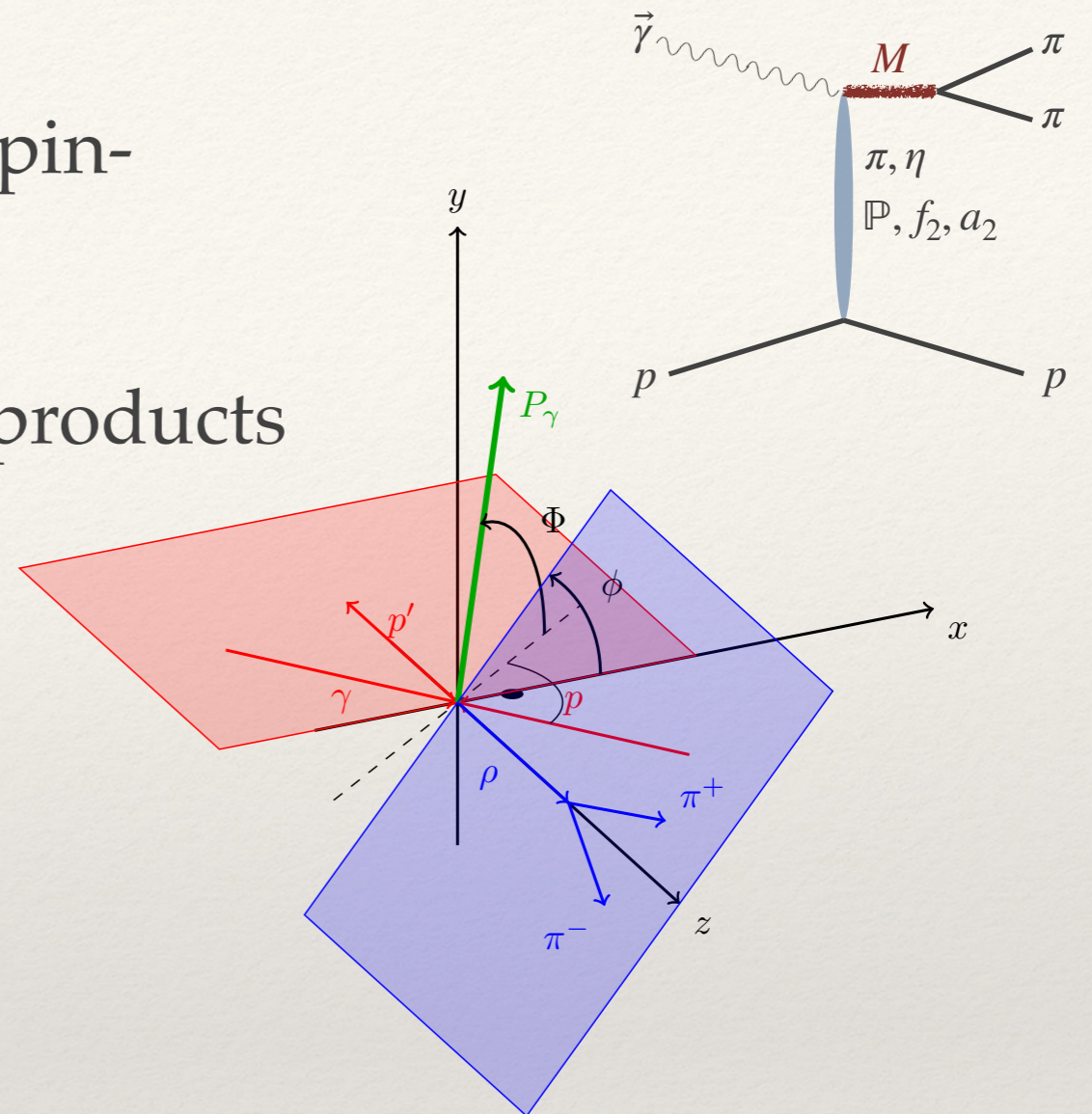


- ❖ tag electrons to determine photon energy

- ❖ Acceptance: $\theta_{lab} \approx 1^\circ - 120^\circ$
- ❖ Charged particles: $\sigma_p/p \approx 1\% - 3\%$ (8% - 9% very-forward high-momentum tracks)
- ❖ Photons: $\sigma_E/E = 6\%/\sqrt{E} \oplus 2\%$

Spin density matrix elements

- ❖ SDMEs ρ_{jk}^i contain information on the spin-polarization of the produced state
- ❖ Measure angular distribution of decay products
- ❖ Learn about production mechanism
 - ❖ Study the naturality $\eta = P(-1)^J$ of the exchanged particle X



For vector meson to pseudo-scalar decays:

$$W(\cos \theta, \phi, \Phi) = W^0(\cos \theta, \phi, \Phi) + P_\gamma \cos(2\Phi)W^1(\cos \theta, \phi, \Phi) + P_\gamma \sin(2\Phi)W^2(\cos \theta, \phi, \Phi)$$

$$W^0(\cos \theta, \phi) = \frac{3}{4\pi} \left(\frac{1}{2}(1 - \rho_{00}^0) + \frac{1}{2}(3\rho_{00}^0 - 1) \cos^2 \theta - \sqrt{2}\text{Re}\rho_{10}^0 \sin 2\theta \cos \phi - \rho_{1-1}^0 \sin^2 \theta \cos 2\phi \right)$$

$$W^1(\cos \theta, \phi) = \frac{3}{4\pi} \left(\rho_{11}^1 \sin^2 \theta + \rho_{00}^1 \cos^2 \theta - \sqrt{2}\text{Re}\rho_{10}^1 \sin 2\theta \cos \phi - \rho_{1-1}^1 \sin^2 \theta \cos 2\phi \right)$$

$$W^2(\cos \theta, \phi) = \frac{3}{4\pi} \left(\sqrt{2}\text{Im}\rho_{10}^2 \sin 2\theta \sin \phi + \rho_{1-1}^2 \sin^2 \theta \sin 2\phi \right)$$

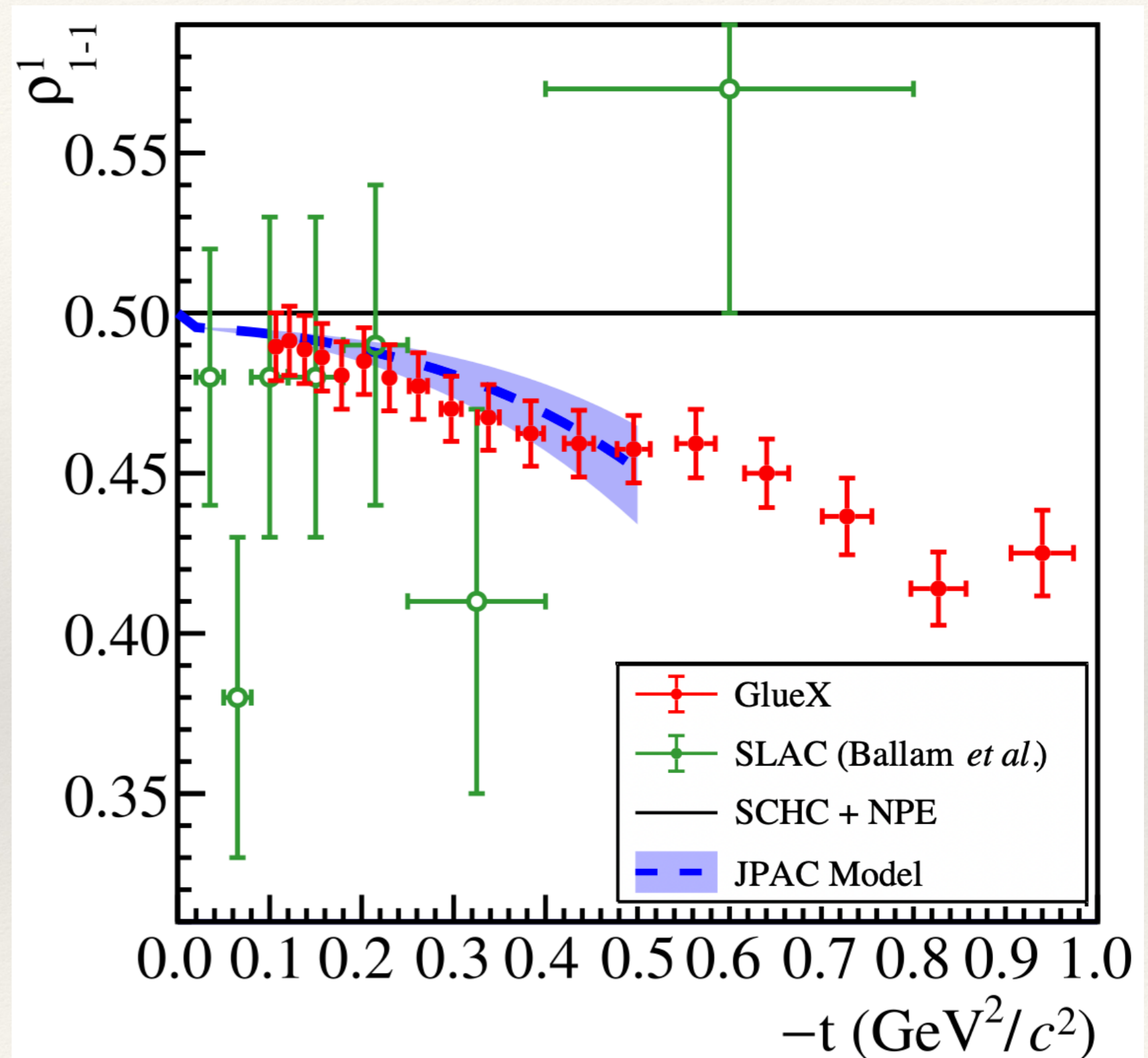
$\rho(770)$ SDMEs

Phys. Rev. C 108, 055204 (2023)

$$\gamma p \rightarrow \rho(770) p \rightarrow \pi^+ \pi^- p$$

- ❖ Uncertainties dominated by systematics
- ❖ s-channel helicity conservation:
 $\rho_{1-1}^1 = 0.5$
valid for very small $-t$
- ❖ JPAC: Regge model (fit to SLAC data)
→ good agreement at low $-t$

JPAC, *Phys. Rev. D* **97**, 094003 (2018)



$\rho(770)$ SDMEs

Phys. Rev. C 108, 055204 (2023)

- Study combinations of SDMEs which are purely natural or unnatural

$$\rho_{jk}^{N,U} = \frac{1}{2} \left(\rho_{jk}^0 \mp (-1)^i \rho_{-jk}^1 \right)$$

Schilling et al., Nucl. Phys. B 15 (1970) 397-412

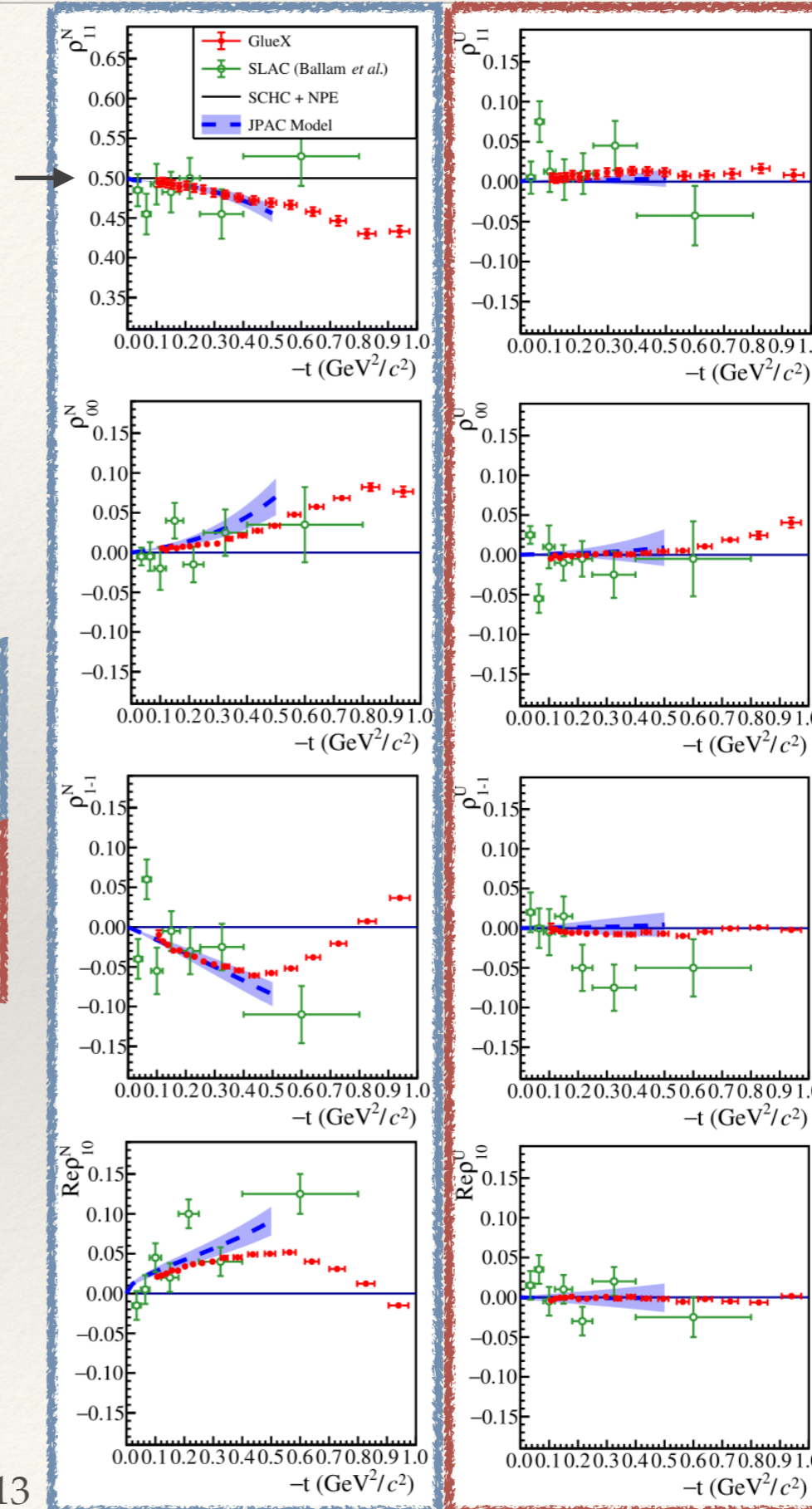
pos. parity exchange / natural:

e.g. f_2, a_2

neg. parity exchange / unnatural:

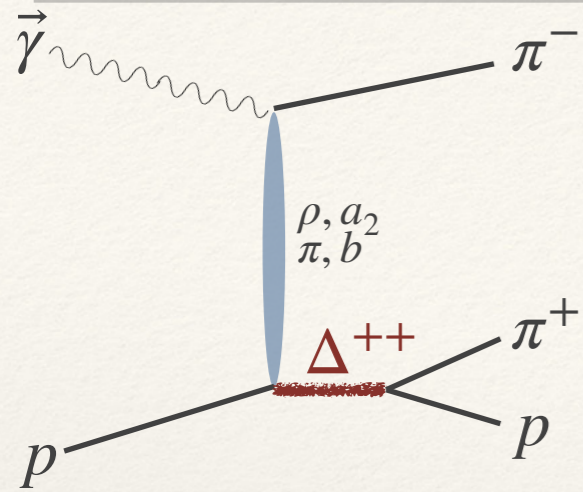
e.g. π, η

- Dominance of natural amplitudes
- In the pipeline: ϕ, ω



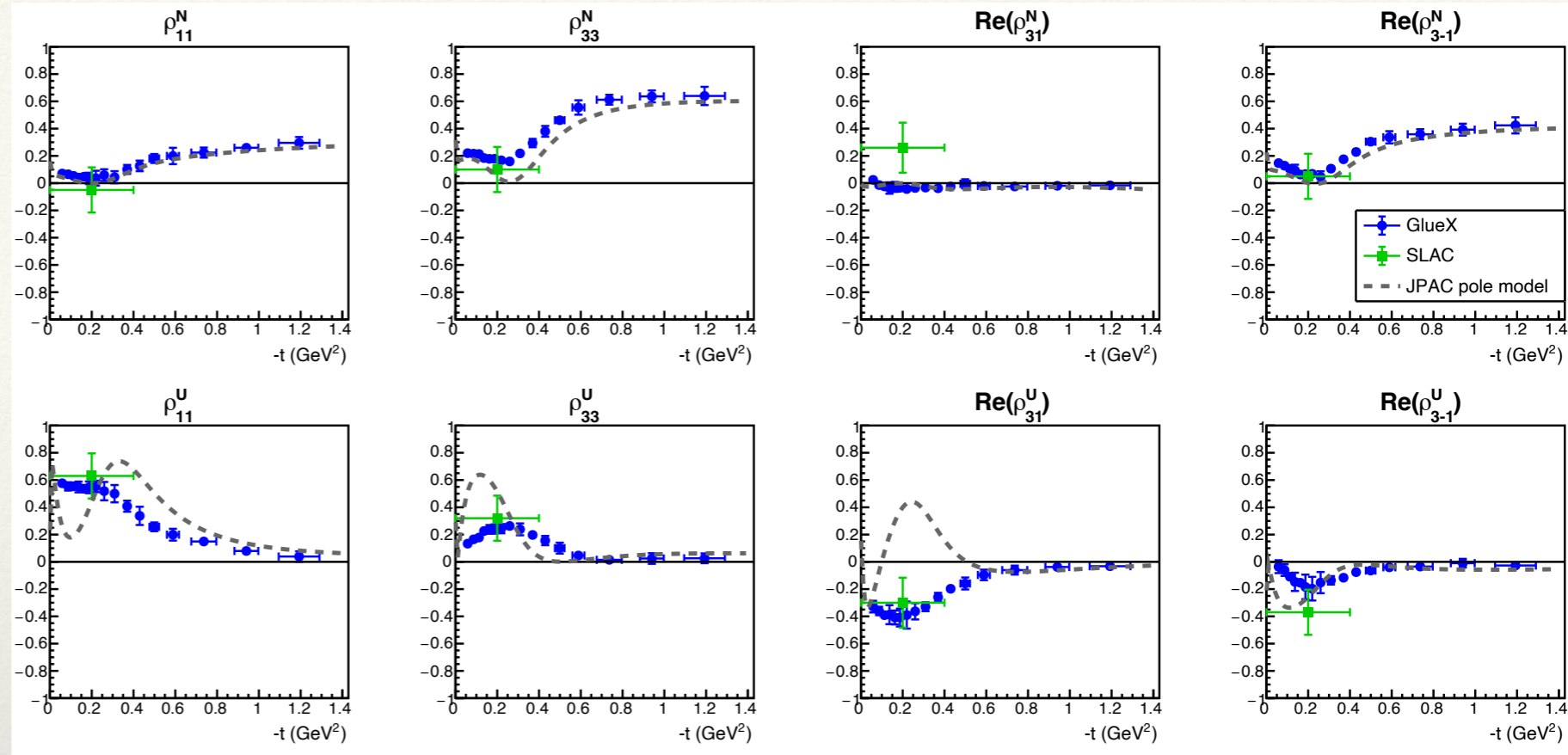
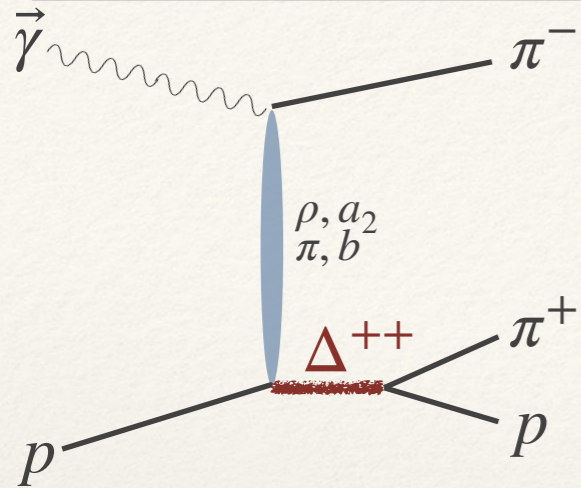
$\Delta^{++}(1232)$ SDMEs

F. Afzal



$\Delta^{++}(1232)$ SDMEs

F. Afzal

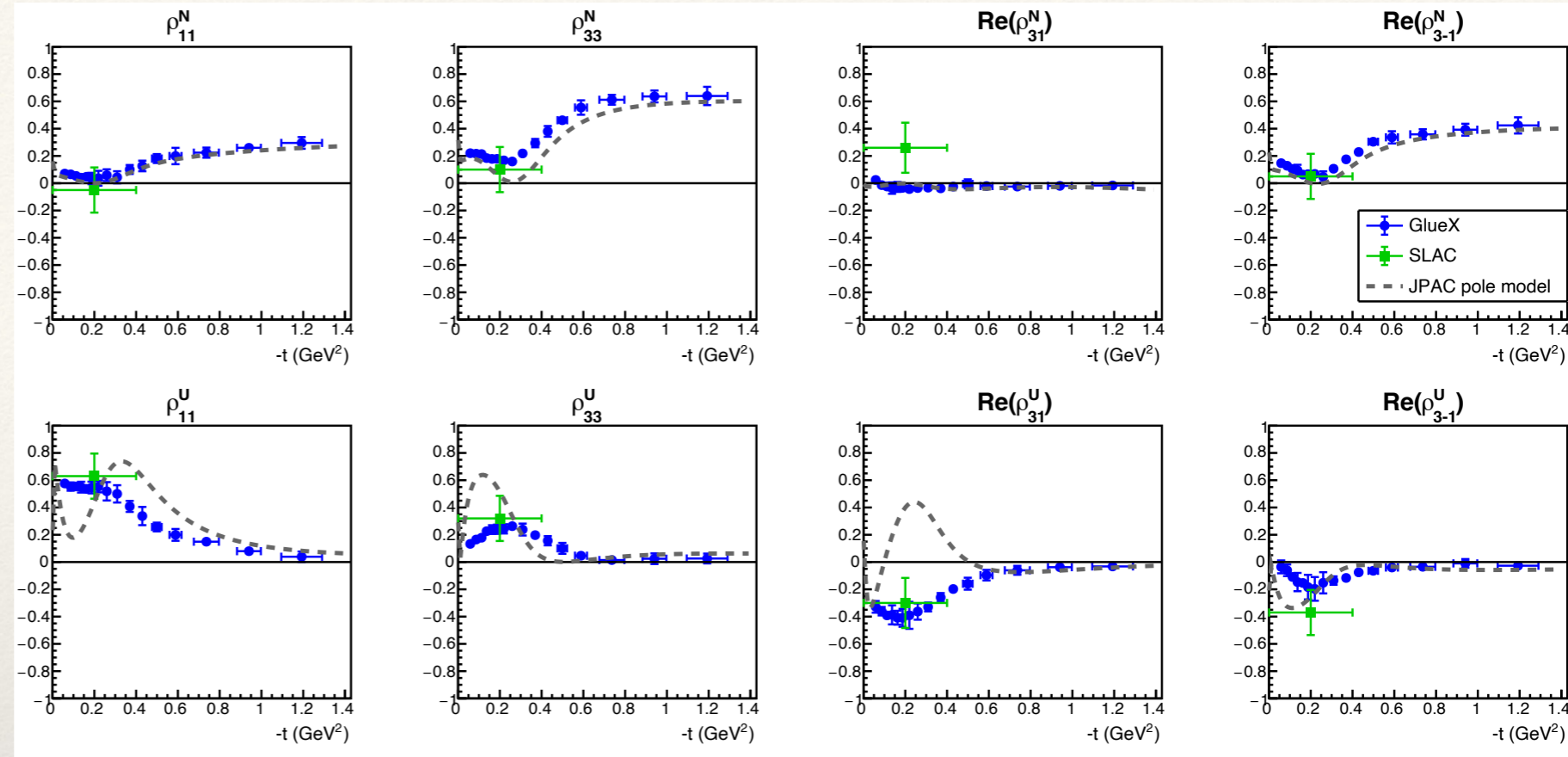
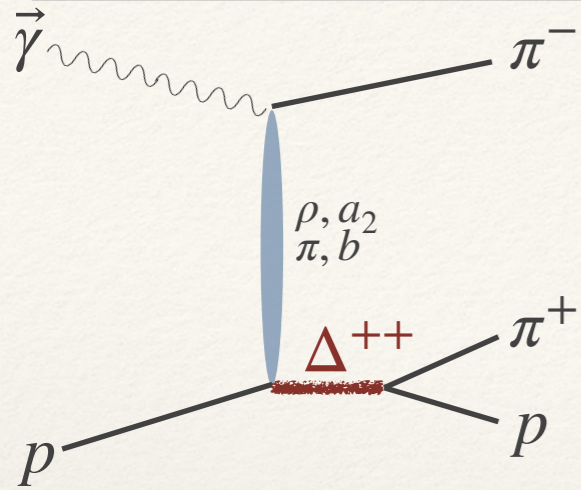


JPAC, Physics Letters B 779 (2018) 77–81

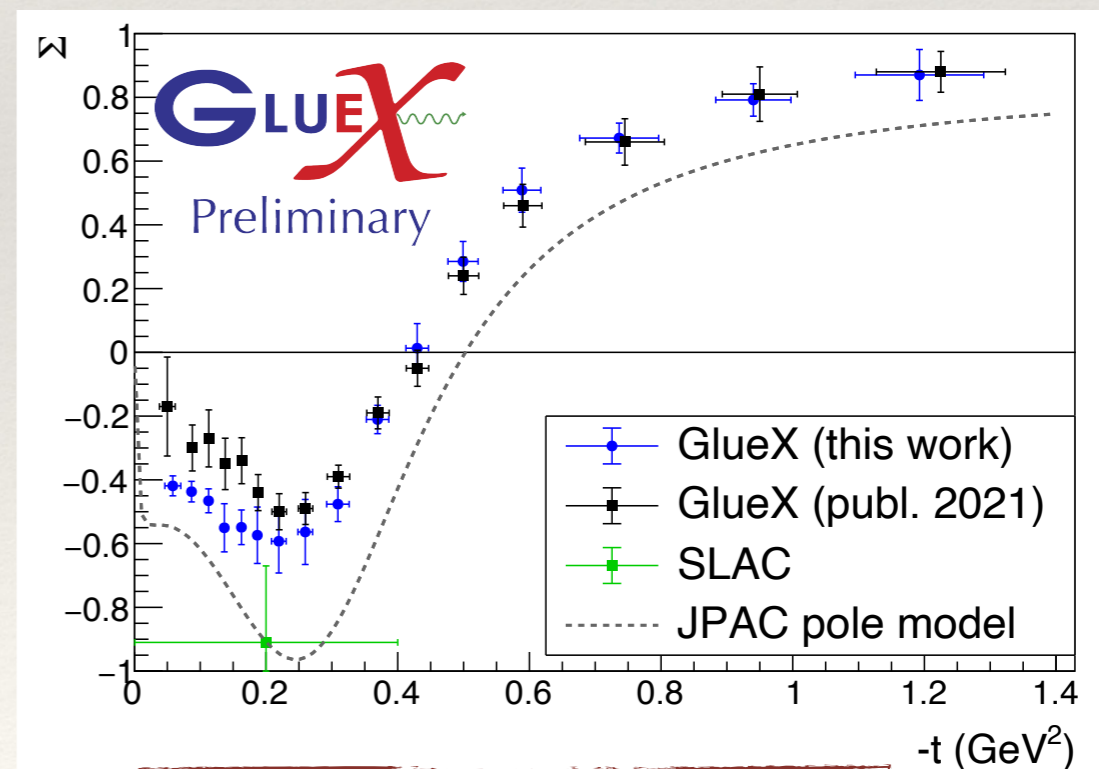
- ❖ Orders of magnitude improvement over previous data
- ❖ Data will be used to describe bottom vertex of reaction (couplings)
 - ❖ Important for hybrid search
- ❖ Good description of natural exchange by JPAC model

$\Delta^{++}(1232)$ SDMEs

F. Afzal



JPAC, Physics Letters B 779 (2018) 77–81

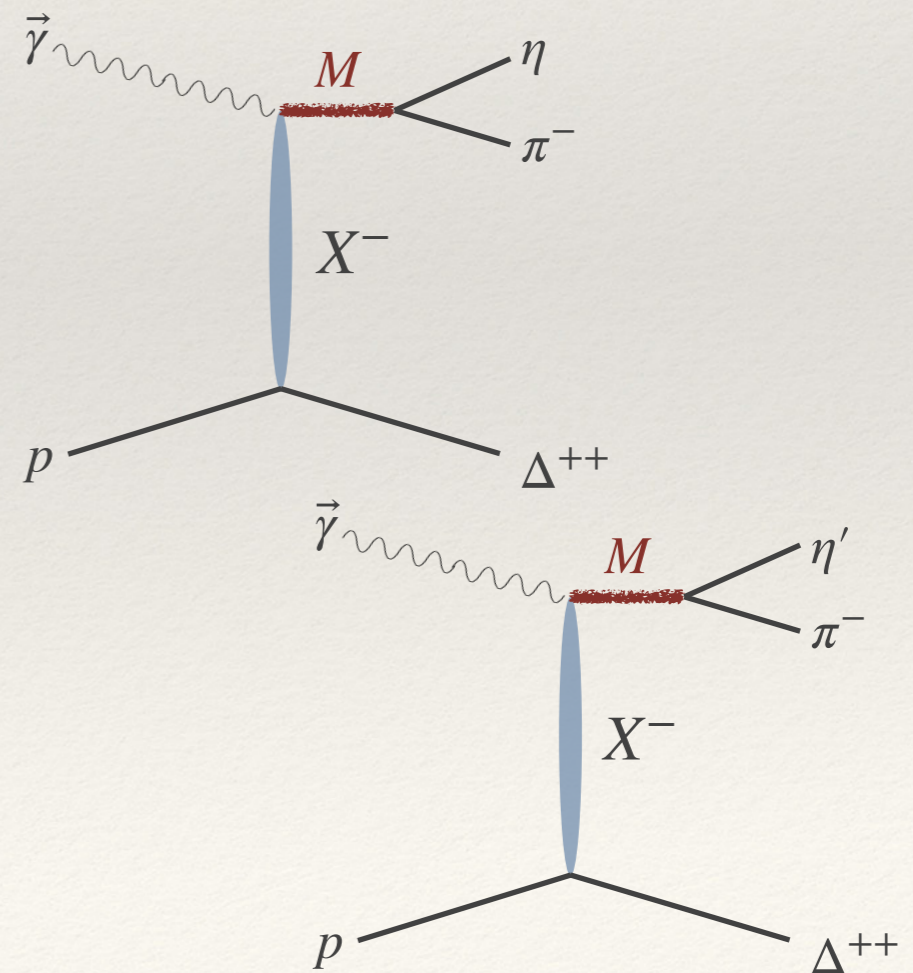
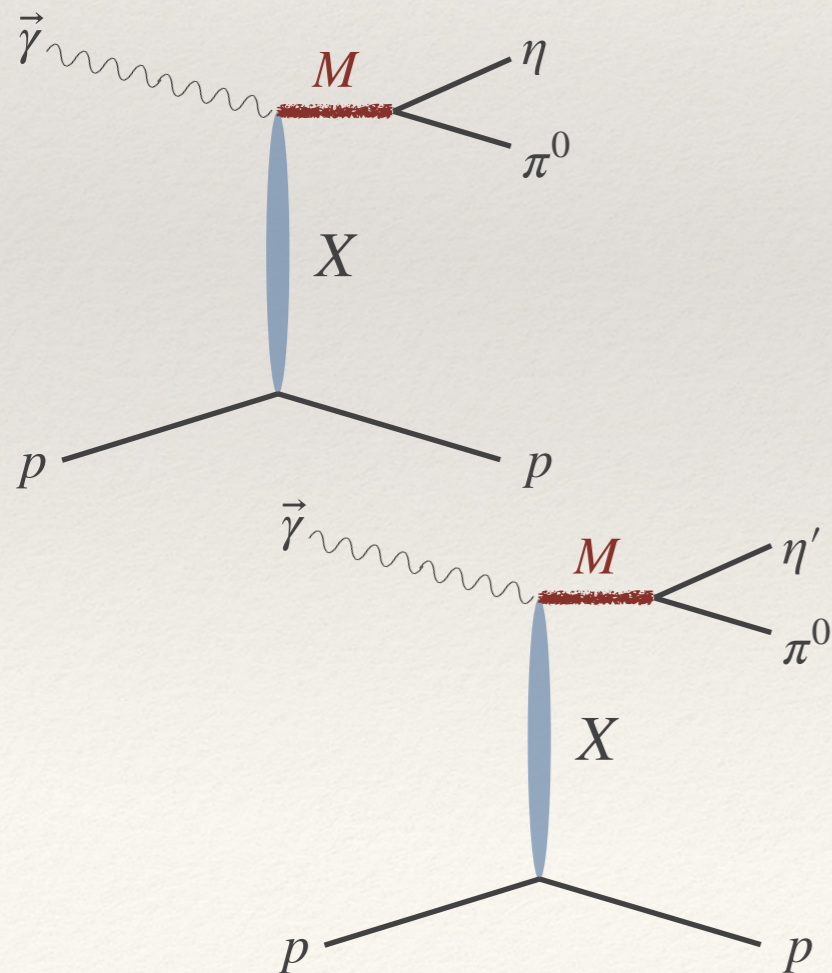


Publication in preparation

- ❖ Orders of magnitude improvement over previous data
- ❖ Data will be used to describe bottom vertex of reaction (couplings)
 - ❖ Important for hybrid search
- ❖ Good description of natural exchange by JPAC model
- ❖ More reliable than “simple” beam asymmetry

Hybrid search in $\eta\pi$

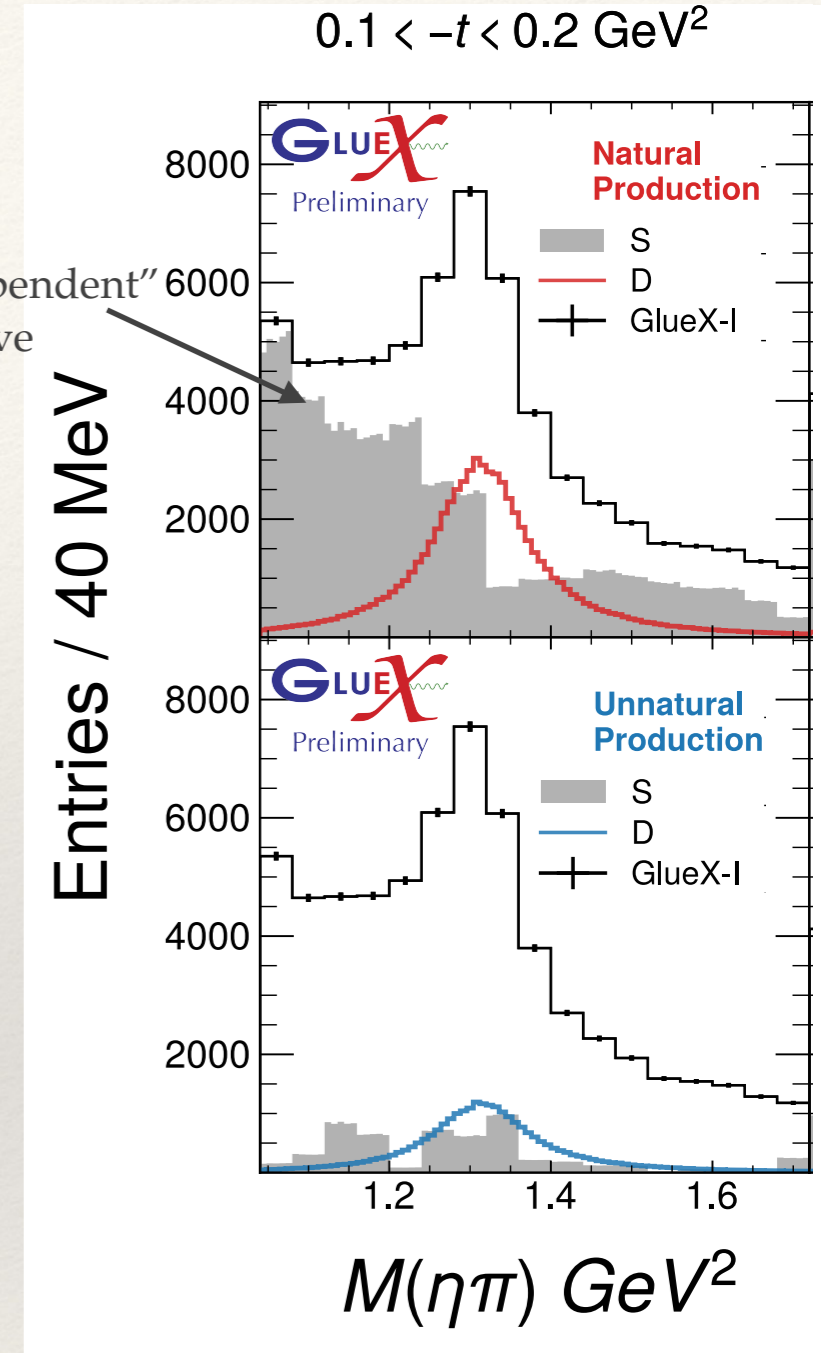
- ❖ JPAC coupled channel fit to $\eta\pi$ and $\eta'\pi$ data from COMPASS
- ❖ GlueX has access to different decay modes in multiple final states
- ❖ $\gamma p \rightarrow \eta\pi^0 p, \eta \rightarrow \gamma\gamma$
- ❖ $\gamma p \rightarrow \eta\pi^0 p, \eta \rightarrow \pi^+\pi^-\pi^0$
- ❖ $\gamma p \rightarrow \eta'\pi^0 p, \eta' \rightarrow \pi^+\pi^-\eta, \eta \rightarrow \gamma\gamma$
- ❖ $\gamma p \rightarrow \eta\pi^-\Delta^{++}, \eta \rightarrow \pi^+\pi^-\pi^0$
- ❖ $\gamma p \rightarrow \eta\pi^-\Delta^{++}, \eta \rightarrow \gamma\gamma$
- ❖ $\gamma p \rightarrow \eta'\pi^-\Delta^{++}, \eta' \rightarrow \pi^+\pi^-\eta, \eta \rightarrow \gamma\gamma$



Towards a PWA in $\eta\pi^0 - a_2(1320)$ cross-section

L. Ng, M. Albrecht

- ❖ First look at PWA in $\gamma p \rightarrow \eta\pi^0 p$
- ❖ Study $a_2(1320)$ cross-section
- ❖ Positive helicity (natural exchange, e.g. ρ) dominates
- ❖ a_2 predominantly D_2 wave, consistent with helicity=2 dominance at Belle ($\gamma\gamma \rightarrow \eta\pi^0$)
Belle, Phys. Rev. D 80, 032001



Mixed method: imposing BW shape on a_2 improves fit

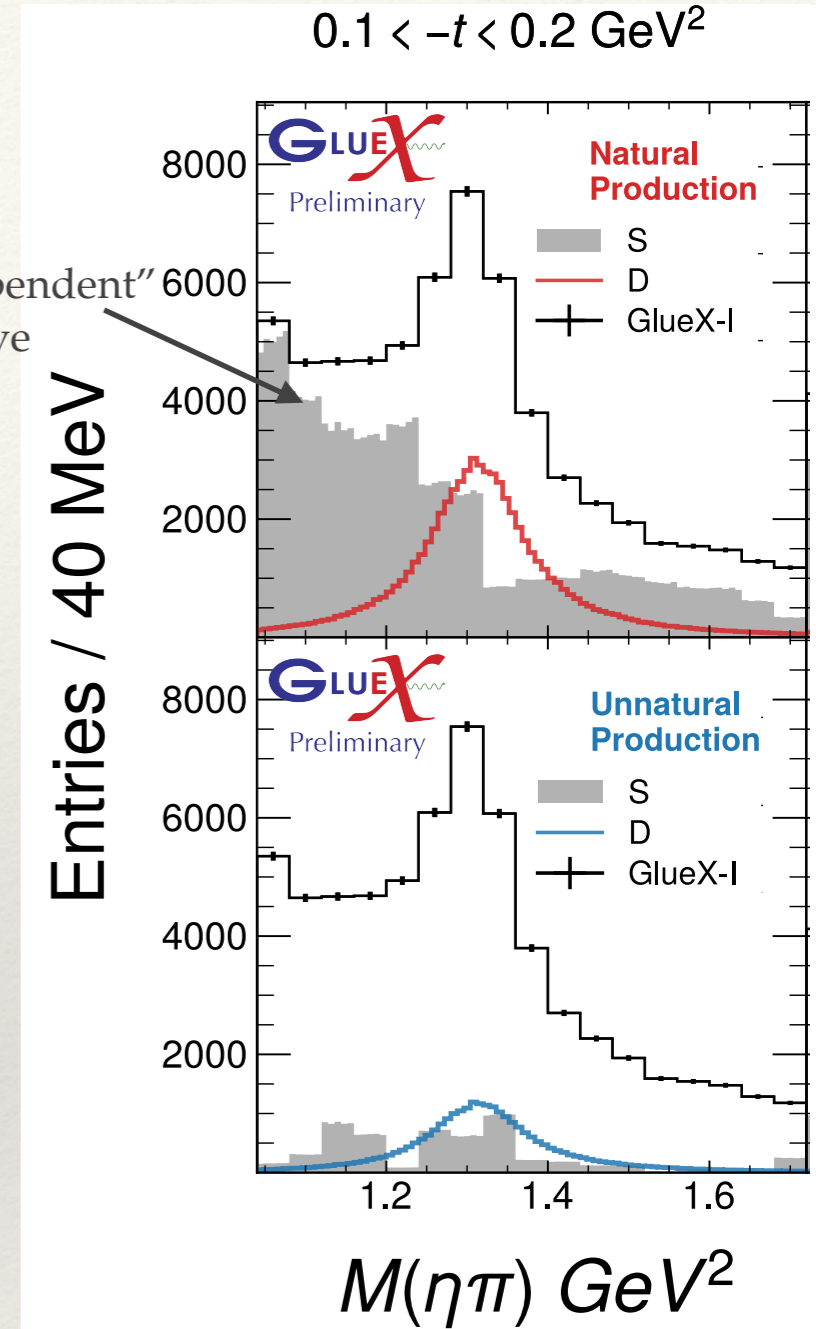
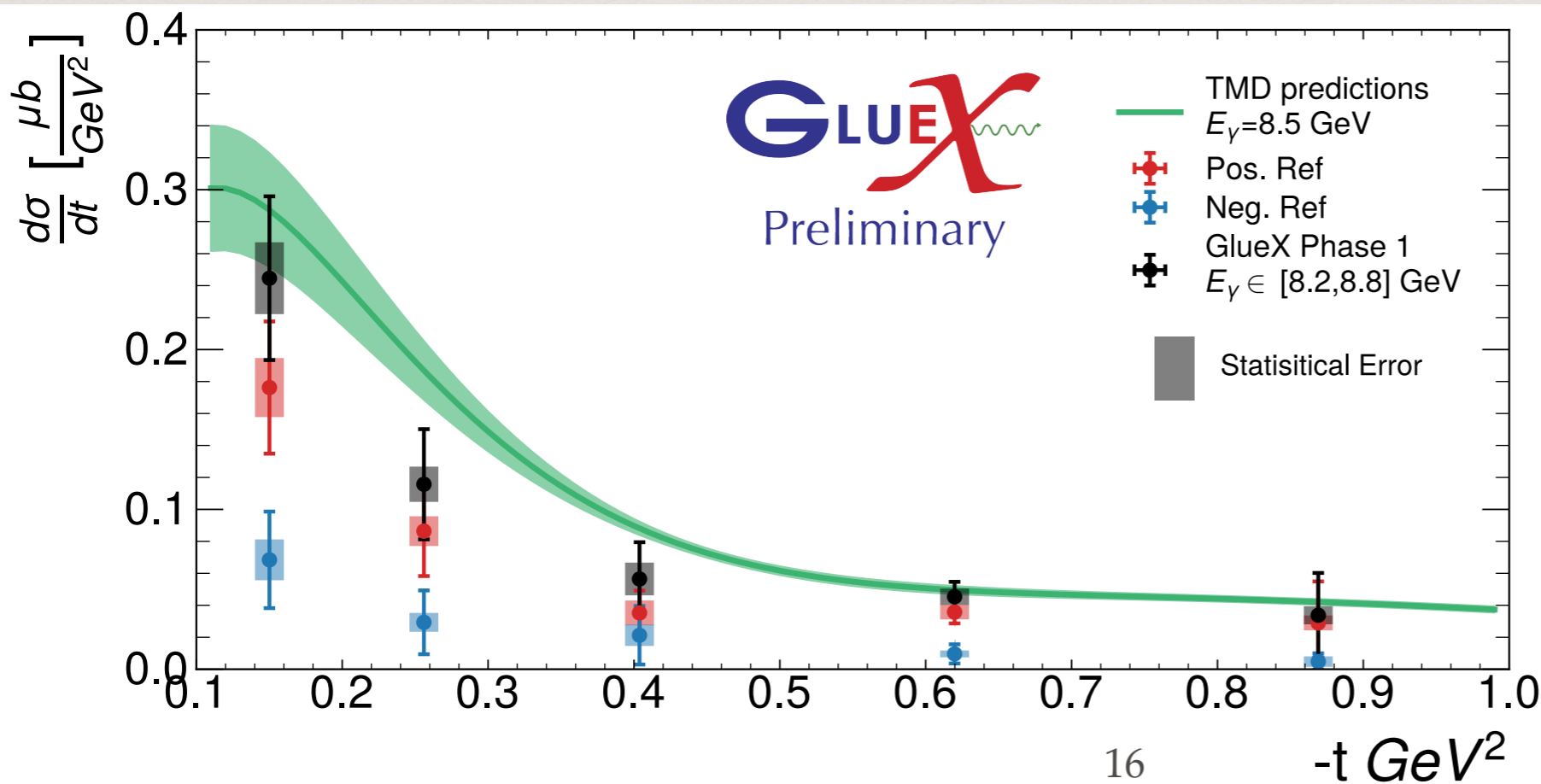
Publication in preparation

Towards a PWA in $\eta\pi^0 - a_2(1320)$ cross-section

L. Ng, M. Albrecht

- ❖ First look at PWA in $\gamma p \rightarrow \eta\pi^0 p$
- ❖ Study $a_2(1320)$ cross-section
- ❖ Positive helicity (natural exchange, e.g. ρ) dominates
- ❖ a_2 predominantly D_2 wave, consistent with helicity=2 dominance at Belle ($\gamma\gamma \rightarrow \eta\pi^0$)

Belle, Phys. Rev. D 80, 032001

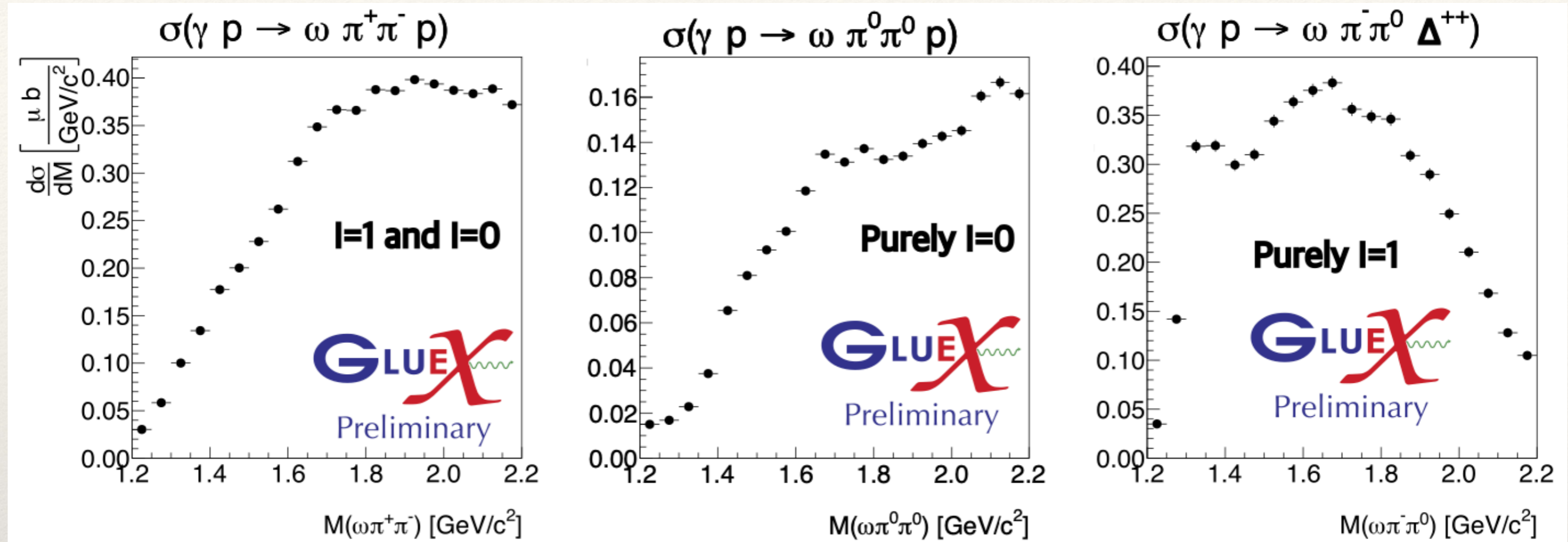


Mixed method: imposing BW shape on a_2 improves fit

Publication in preparation

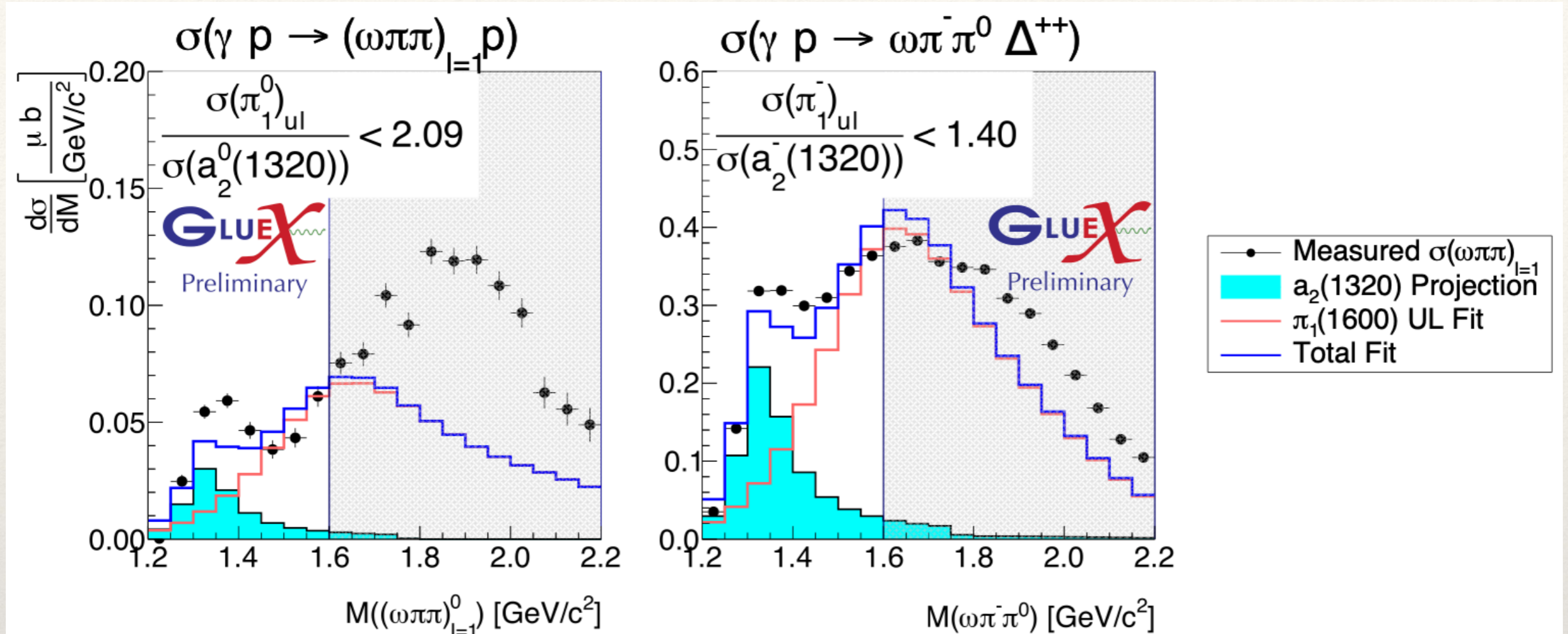
$\pi_1(1600)$ upper limits

W. Imoehl



- ❖ Set upper limit on $\pi_1(1600)$ using isospin separation, assume no $I = 2$
 - ❖ $\sigma((\omega\pi\pi)^0)_{I=1} = \sigma(\omega\pi^+\pi^-) - 2\sigma(\omega\pi^0\pi^0)$
 - ❖ $\sigma((\omega\pi\pi)^-)_{I=1} = \sigma(\omega\pi^-\pi^0)$
- ❖ Fit $\sigma(\omega\pi\pi)_{I=1}$ using known shapes for a_2 (PDG) and π_1 (JPAC)

$\pi_1(1600)$ upper limits

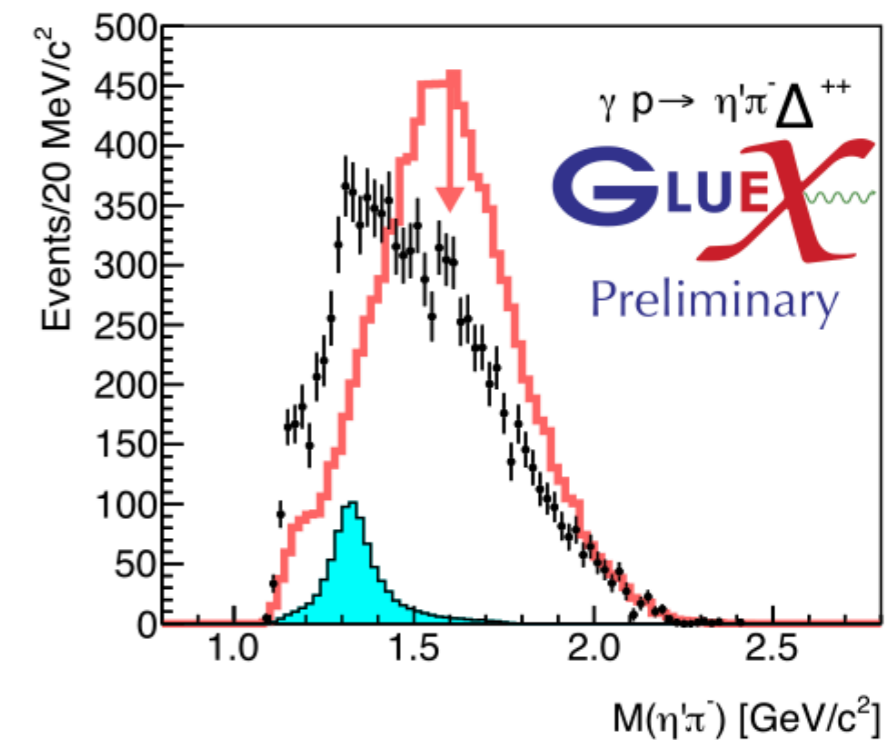
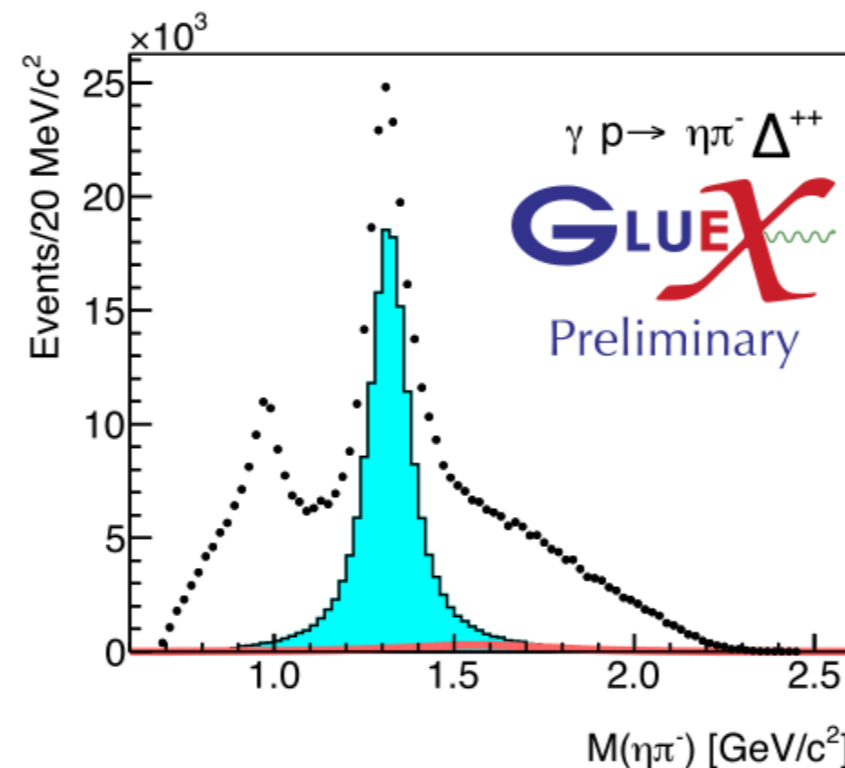
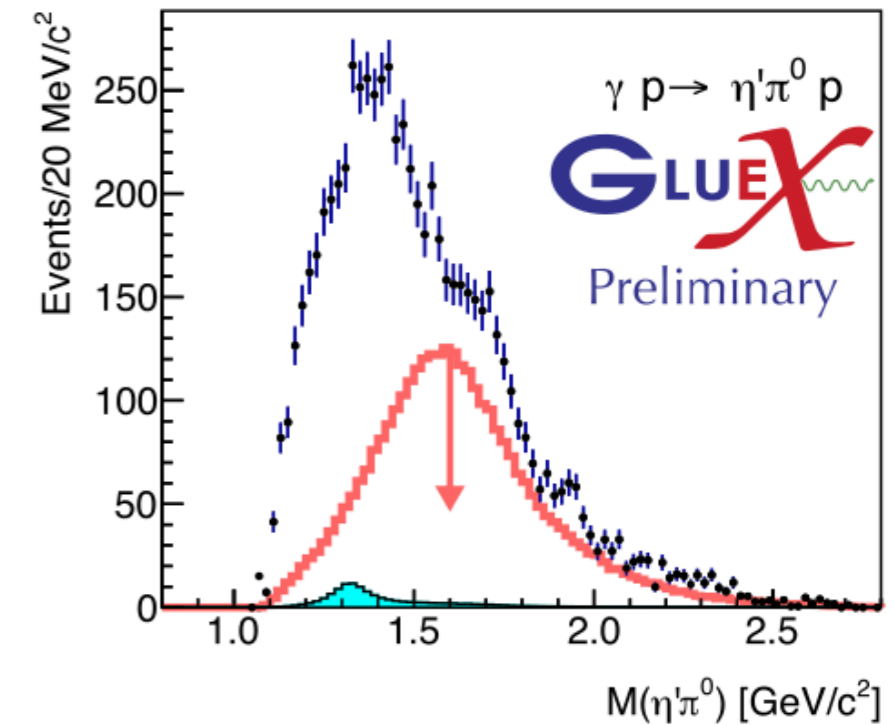
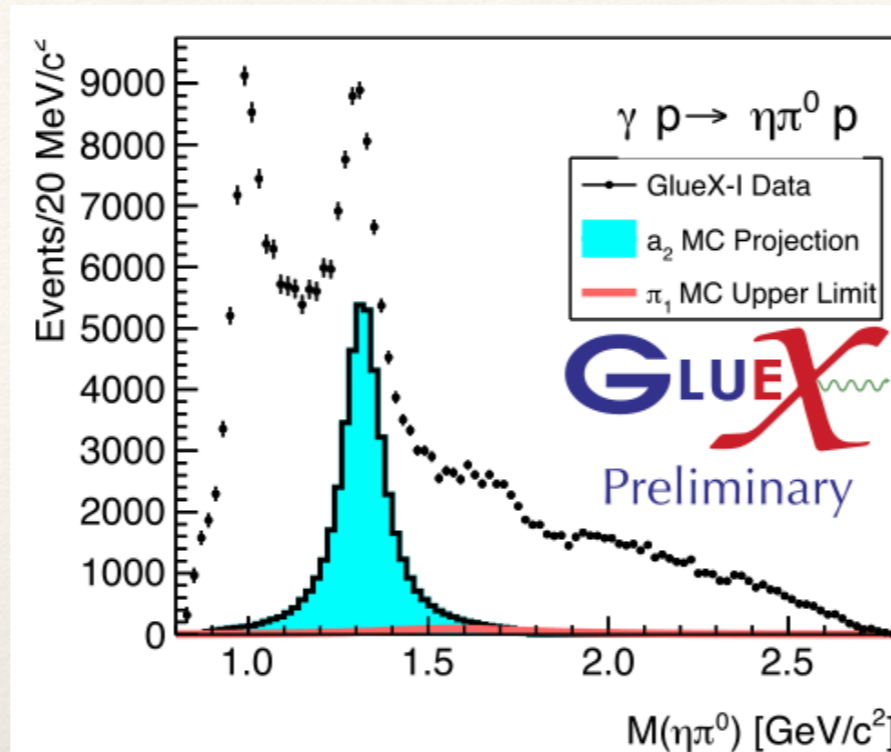


- ❖ Fit $M(\omega\pi\pi)_{I=1} < 1.6 \text{ GeV}/c^2$
- ❖ Fix a_2 size to measured cross-section adjusted with known BR
- ❖ π_1 BR from lattice
- ❖ Only free parameter is π_1 normalisation!
- ❖ π_1 upper limits similar in size to a_2 cross-sections

π_1 projections to $\eta\pi$ and $\eta'\pi$

W. Imoehl

- ❖ $\pi_1 \rightarrow \eta\pi$ expected to be very small
- ❖ $\pi_1 \rightarrow \eta'\pi$ potentially dominating the spectrum
- ❖ First limit on size of photoproduction cross-sections
- ❖ Guidance for amplitude analysis



Hyperons at GlueX

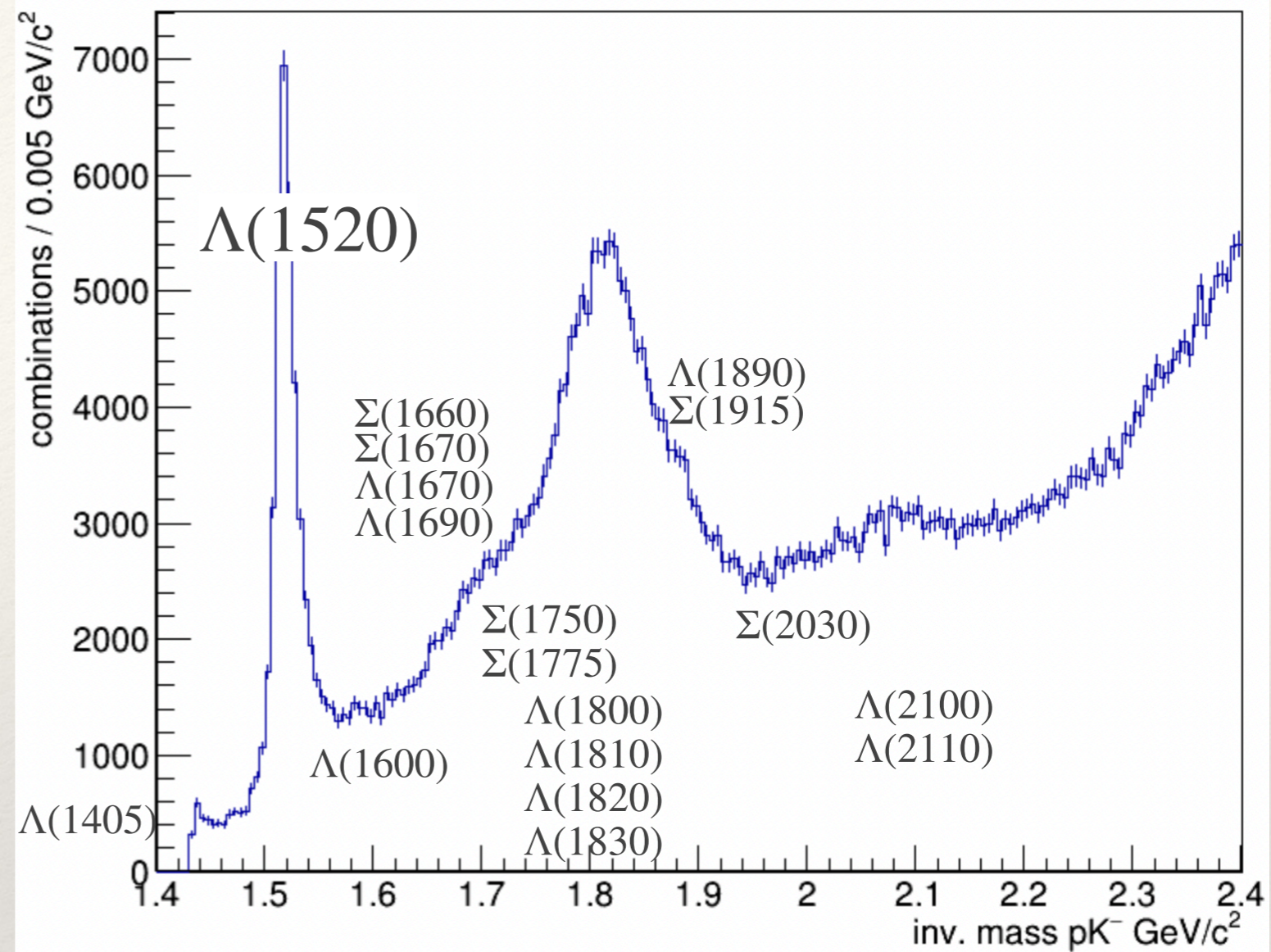
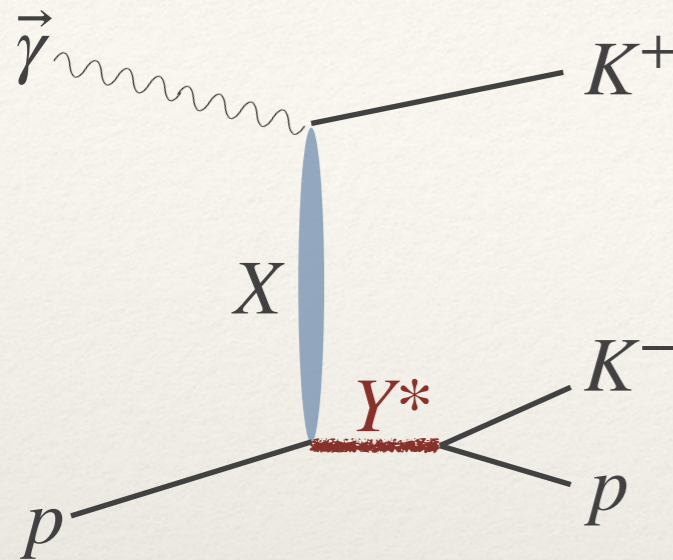
*“For several decades, there has been very little new experimental data bearing on the properties of Λ and Σ resonances. [...] the **field is starved for data**. Recent analyses (see below) have improved what we know about the properties of the known Λ and Σ resonances, but the **established resonances are the same ones that were listed in our 1984 edition [...]**”*

— Λ and Σ resonances, PDG (2021)

Excited hyperons

Phys. Rev. C 105, 035201

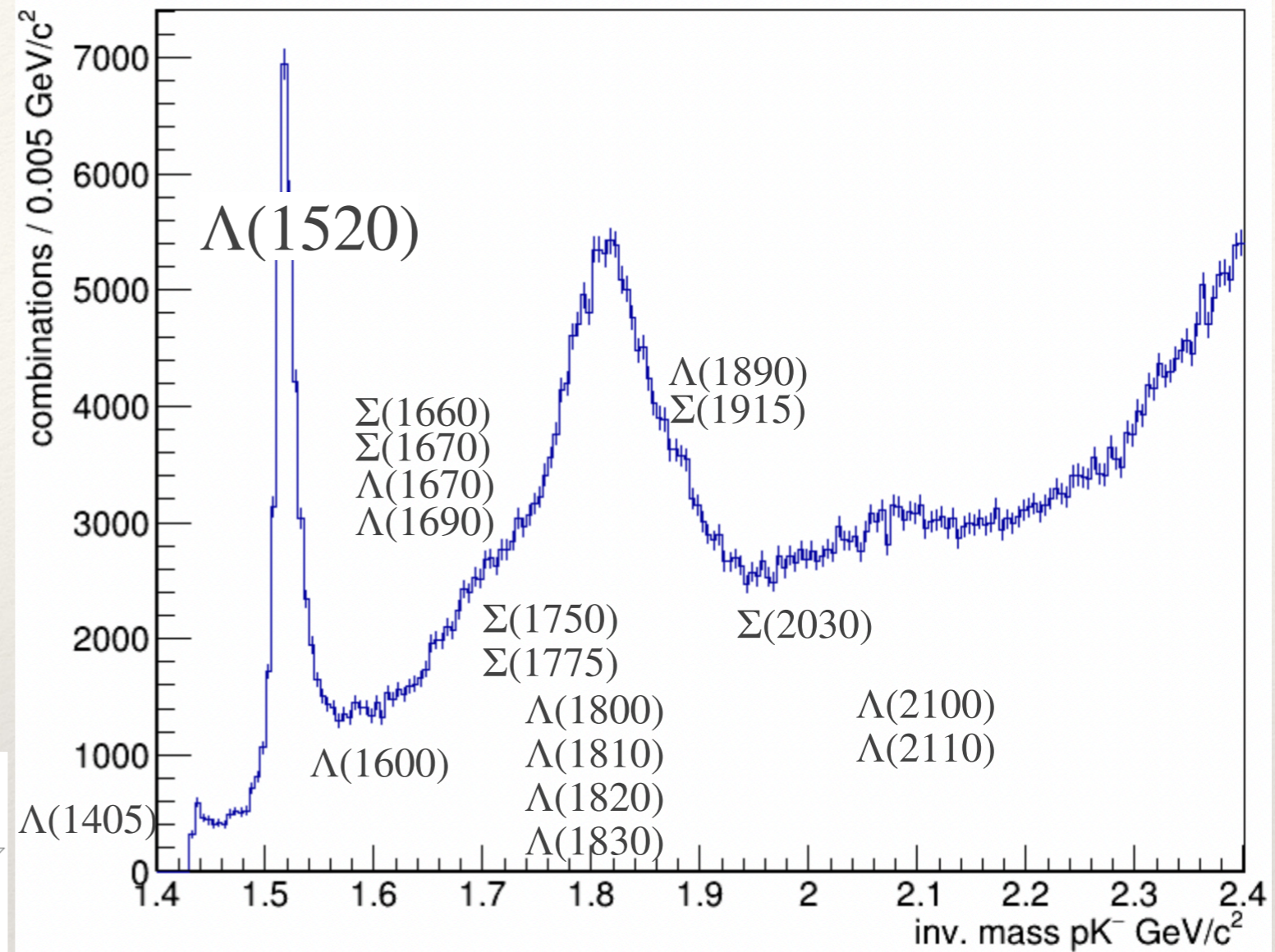
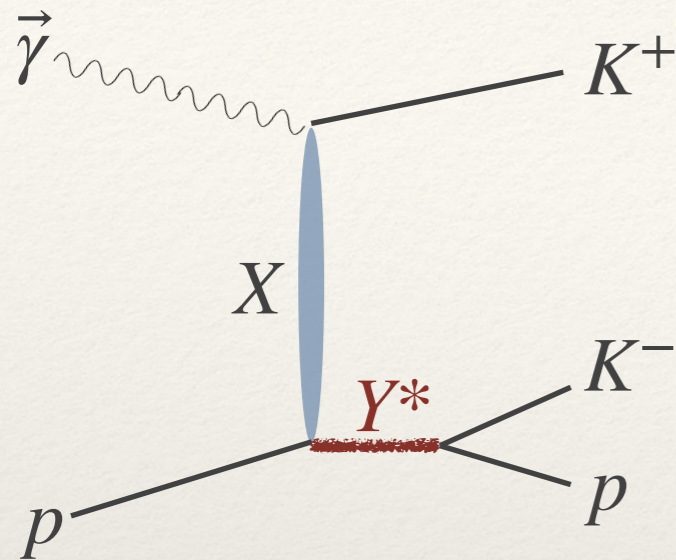
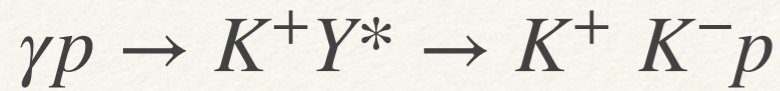
$$\gamma p \rightarrow K^+ Y^* \rightarrow K^+ K^- p$$



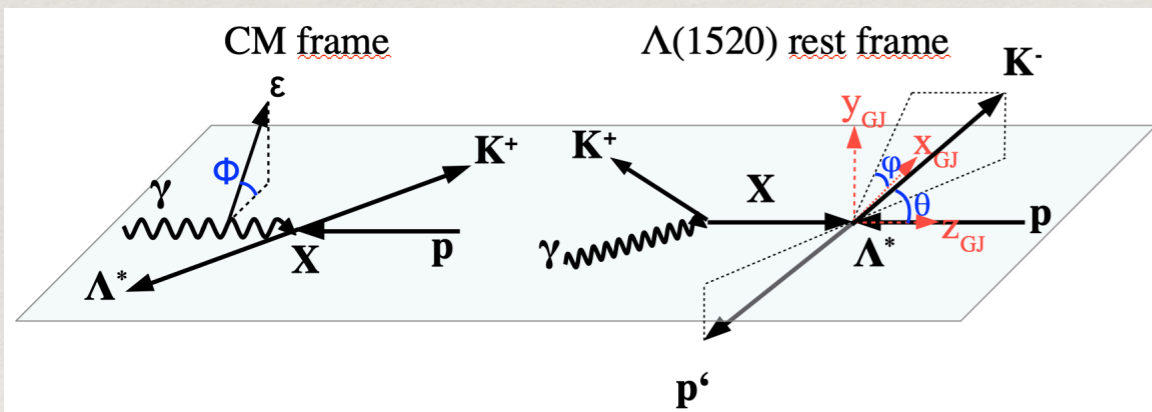
- ❖ Many excited Λ^* and Σ^* expected in spectrum
- ❖ Most prominent: $\Lambda(1520)$ hyperon with $J^P = 3/2^-$

Excited hyperons

Phys. Rev. C 105, 035201



$\Lambda(1520)$ SDMEs



$$W_0 = \frac{1}{4\pi} \left[3 \left(\frac{1}{2} - \rho_{11}^0 \right) \sin^2(\theta) + \rho_{11}^0 (1 + 3 \cos^2(\theta)) - 2\sqrt{3} \left(\text{Re}(\rho_{31}^0) \cos(\varphi) \sin(2\theta) + \text{Re}(\rho_{3-1}^0) \cos(2\varphi) \sin^2(\theta) \right) \right]$$

$$W_1 = \frac{1}{4\pi} \left[3 \rho_{33}^1 \sin^2(\theta) + \rho_{11}^1 (1 + 3 \cos^2(\theta)) - 2\sqrt{3} \left(\text{Re}(\rho_{31}^1) \cos(\varphi) \sin(2\theta) + \text{Re}(\rho_{3-1}^1) \cos(2\varphi) \sin^2(\theta) \right) \right]$$

$$W_2 = \frac{1}{4\pi} \left[2\sqrt{3} \left(\text{Im}(\rho_{31}^2) \sin(\varphi) \sin(2\theta) + \text{Im}(\rho_{3-1}^2) \sin(2\varphi) \sin^2(\theta) \right) \right]$$

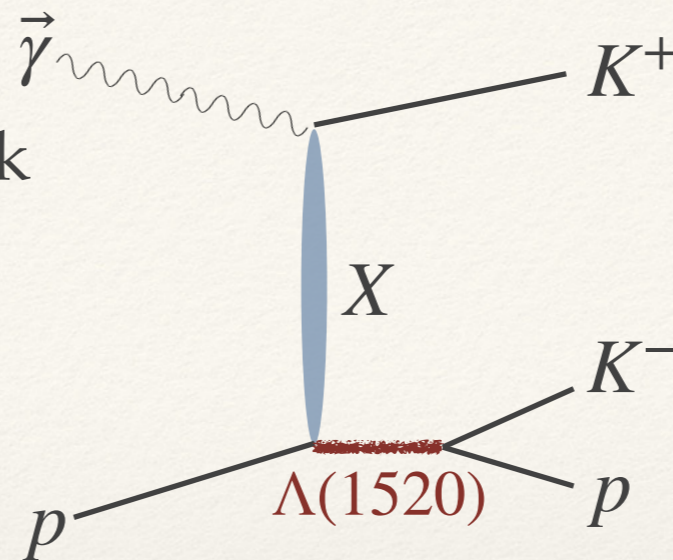
$$W = W_0 - P_\gamma \cos(2\Phi) W_1 - P_\gamma \sin(2\Phi) W_2$$

- ❖ Many excited Λ^* and Σ^* expected in spectrum
- ❖ Most prominent: $\Lambda(1520)$ hyperon with $J^P = 3/2^-$

$\Lambda(1520)$ SDME combinations

Phys. Rev. C **105**, 035201

- ❖ red and blue show model predictions in Reggeized framework (priv. comm. based on [1])
- ❖ natural amplitudes dominate
- ❖ More work needed to model the reaction accurately



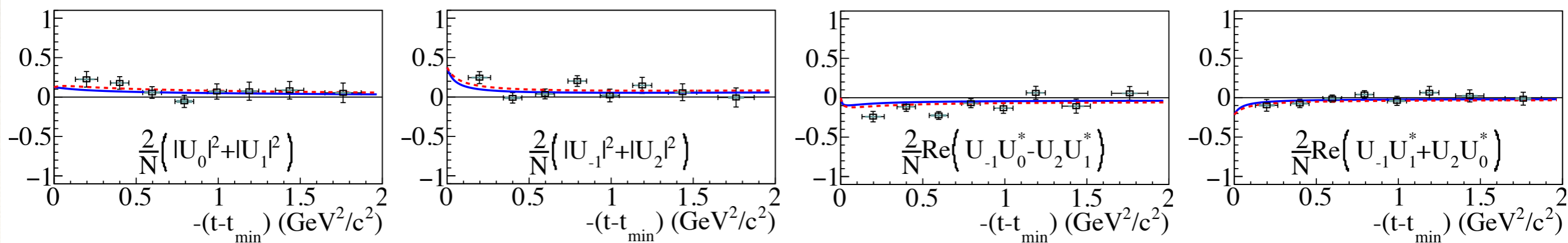
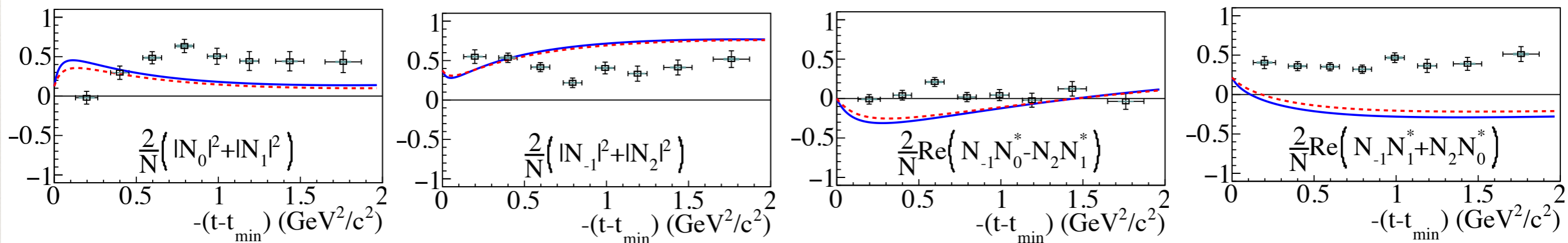
X is exchange particle with spin-parity quantum number J^P and naturality $\eta = P(-1)^J$

Natural: e.g. $K^*(892)$, $K_2^*(1430)$

Unnatural: e.g. $K(492)$, $K_1(1270)$

Natural

Unnatural



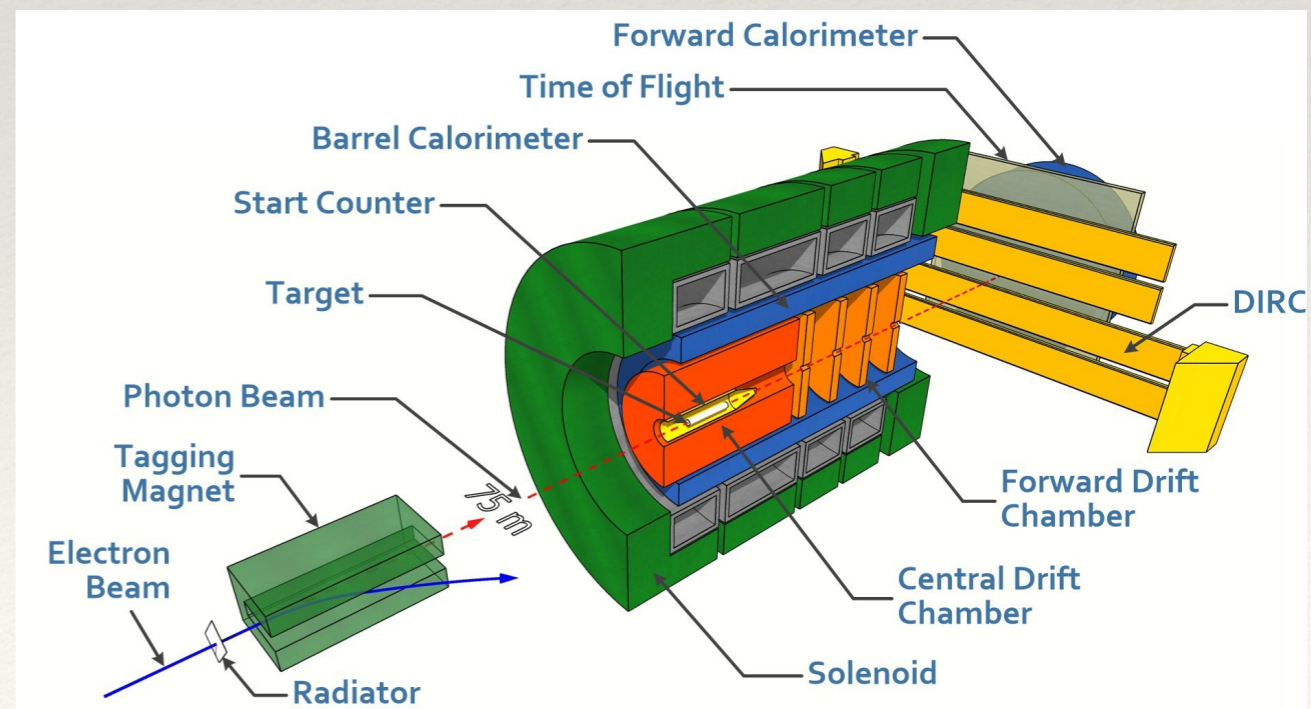
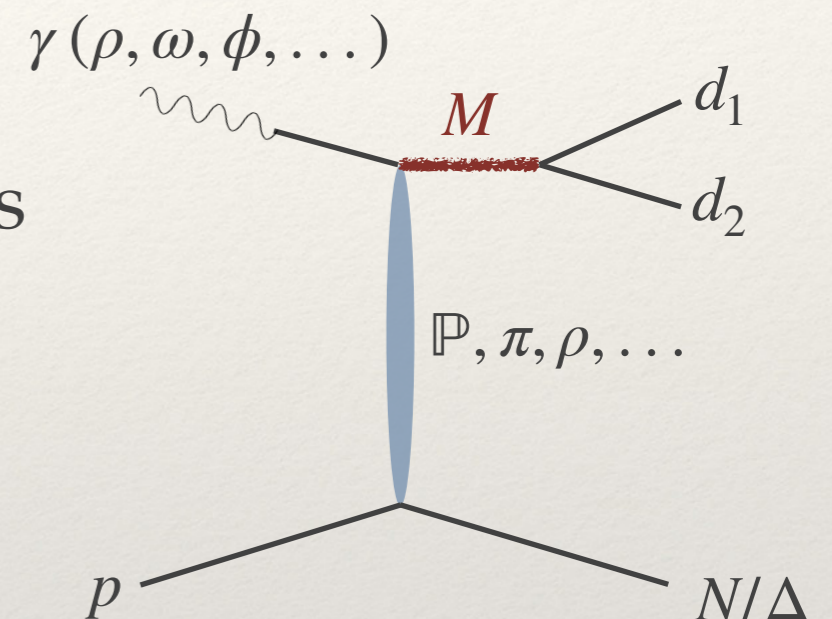
Summary

Acknowledgments:



gluex.org/thanks

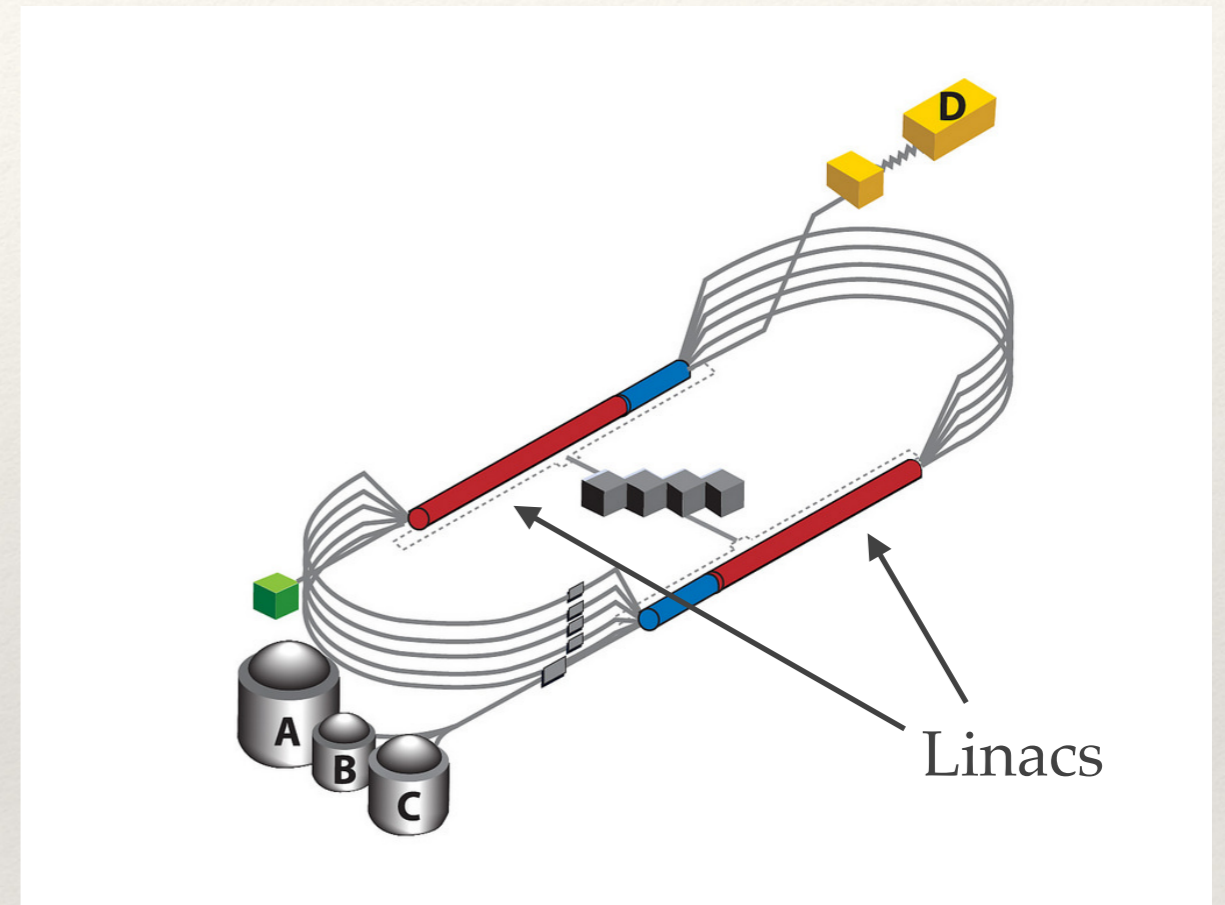
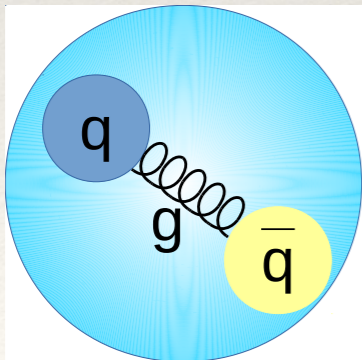
- ❖ GlueX has a unique data set with unprecedented statistical precision in its energy range
- ❖ Start with studying production mechanisms (SDMEs) and develop PWA in parallel
- ❖ $\pi_1(1600)$ upper limits, guide for future searches
- ❖ Many more interesting analyses in the pipeline and room for other physics
- ❖ Rich hyperon spectrum visible in photoproduction
- ❖ $\Lambda(1405)$ (R. Schumacher, Tue 14.00h, parallel III B)
- ❖ Cascades and charmonium (S. Dobbs, Fri 11.15h, plenary X)



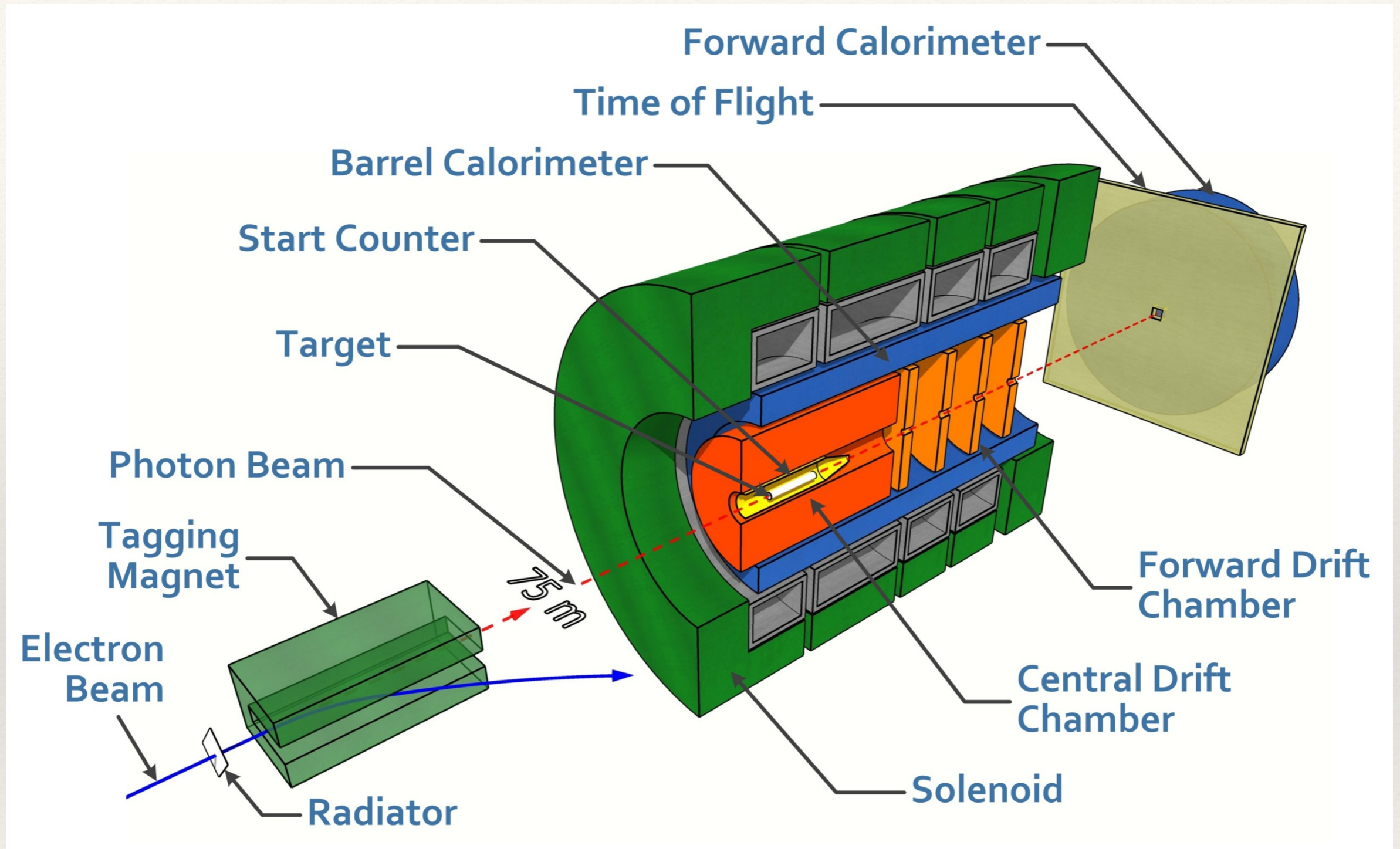
Backup

CEBAF at Jefferson Lab

- ❖ up to 12 GeV electron beam
- ❖ high luminosities for Hall A/C
- ❖ CLAS12 in Hall B
- ❖ GlueX in Hall D
main objective:
Search and study of hybrid mesons



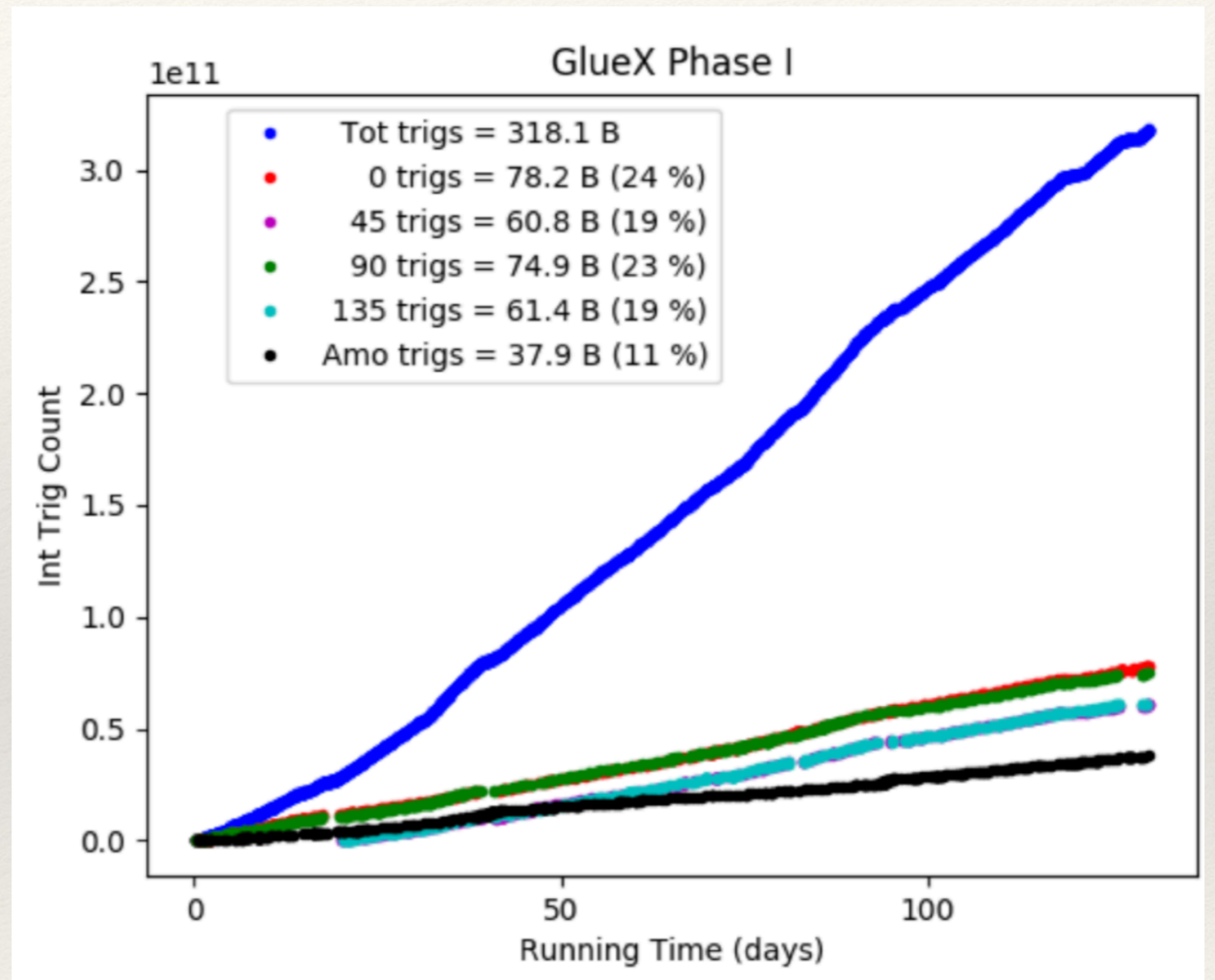
GlueX experiment in Hall D



- ❖ Acceptance: $\theta_{lab} \approx 1^\circ - 120^\circ$
- ❖ Charged particles: $\sigma_p/p \approx 1\% - 3\%$ (8% - 9% very-forward high-momentum tracks)
- ❖ Photons: $\sigma_E/E = 6\%/\sqrt{E} \oplus 2\%$

GlueX experiment

- ❖ Spring 2016
 - ❖ Engineering run
- ❖ Spring 2017
 - ❖ 20% of GlueX-I
- ❖ Spring 2018
 - ❖ 50% of GlueX-I
- ❖ Fall 2018
 - ❖ 30% of GlueX-I

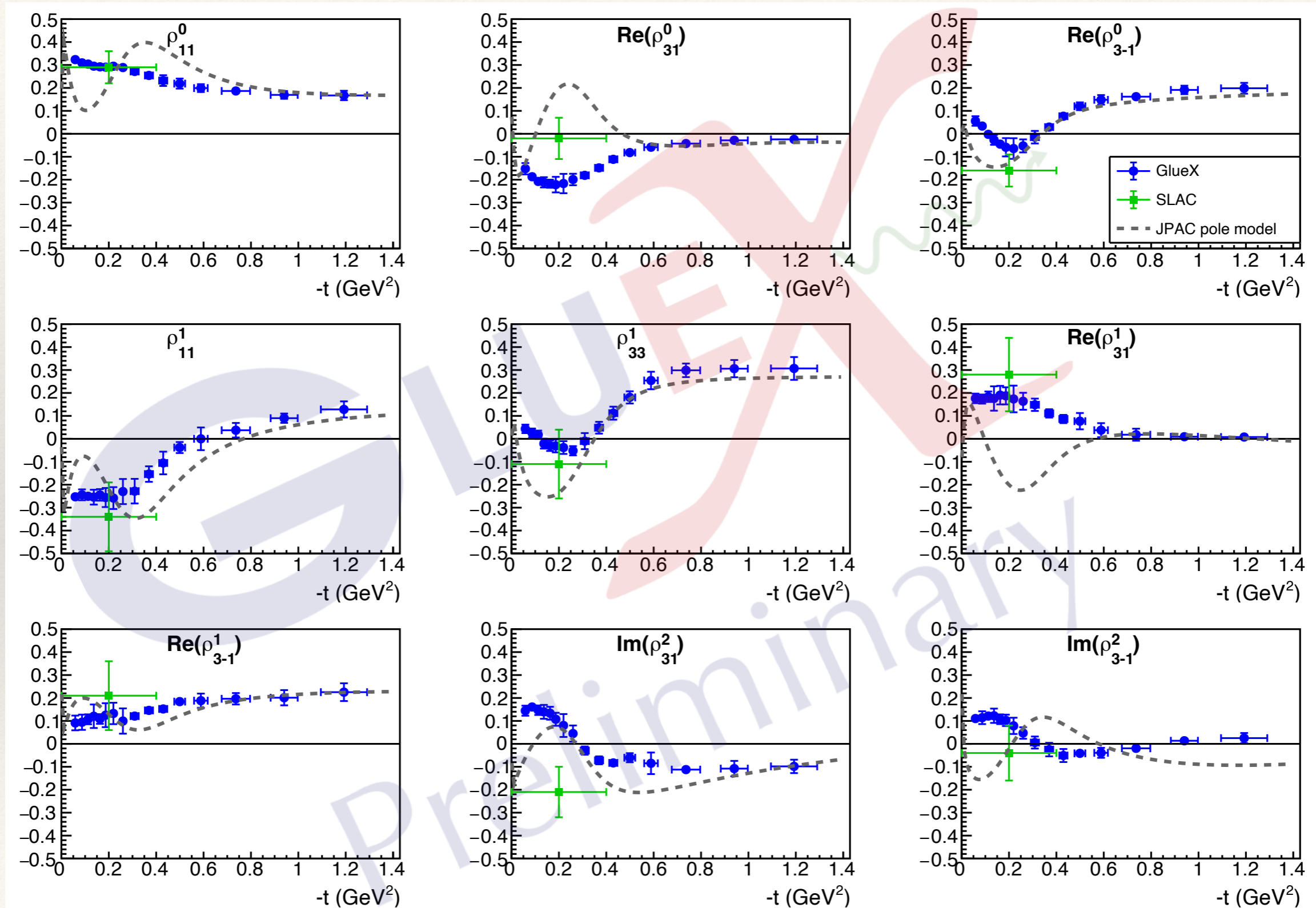


From 2019 onwards:
GlueX-II incl. DIRC

121 pb^{-1} in coherent peak

$\Delta^{++}(1232)$ SDMEs

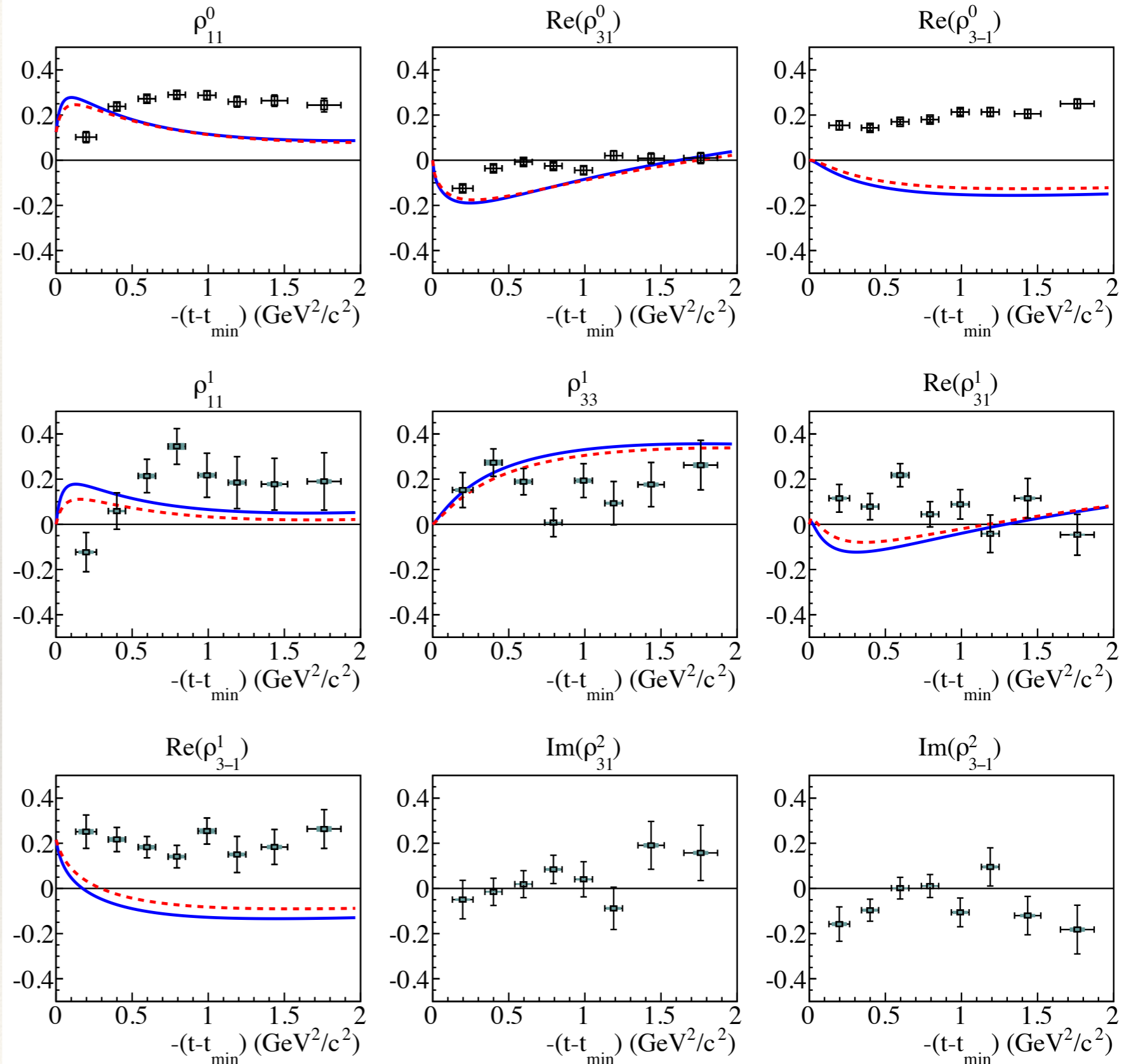
$$\gamma p \rightarrow \pi^- \Delta^{++}(1232) \rightarrow \pi^- \pi^+ p$$



$\Lambda(1520)$ SDMEs

PH (Phys. Rev. C **105**, 035201)

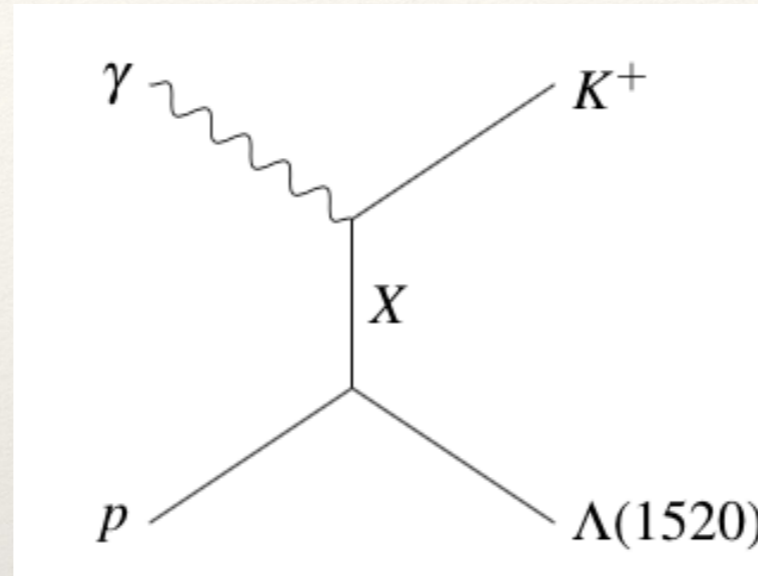
- ❖ So far, sparse data at high energies
- ❖ red and blue show model predictions in Reggeized framework (priv. comm. based on [1])
- ❖ these measurements constrain models in the future



$\Lambda(1520)$ SDME Interpretation

PH (Phys. Rev. C **105**, 035201)

- ❖ to help with interpretation form combinations of SDMEs which correspond to purely natural (N) and purely unnatural (U) exchange amplitudes



X is exchange particle with spin-parity quantum number J^P and naturality $\eta = P(-1)^J$

Natural: e.g. $K^*(892)$, $K_2^*(1430)$

Unnatural: e.g. $K(492)$, $K_1(1270)$

$$\rho_{11}^0 + \rho_{11}^1 = \frac{2}{N} (|N_0|^2 + |N_1|^2)$$

$$\text{Re}(\rho_{31}^0 + \rho_{31}^1) = \frac{2}{N} (N_{-1}N_0^* - N_2N_1^*)$$

$$\rho_{11}^0 - \rho_{11}^1 = \frac{2}{N} (|U_0|^2 + |U_1|^2)$$

$$\text{Re}(\rho_{31}^0 - \rho_{31}^1) = \frac{2}{N} (U_{-1}U_0^* - U_2U_1^*)$$

$$\rho_{33}^0 + \rho_{33}^1 = \frac{2}{N} (|N_{-1}|^2 + |N_2|^2)$$

$$\text{Re}(\rho_{3-1}^0 + \rho_{3-1}^1) = \frac{2}{N} (N_{-1}N_1^* + N_2N_0^*)$$

$$\rho_{33}^0 - \rho_{33}^1 = \frac{2}{N} (|U_{-1}|^2 + |U_2|^2)$$

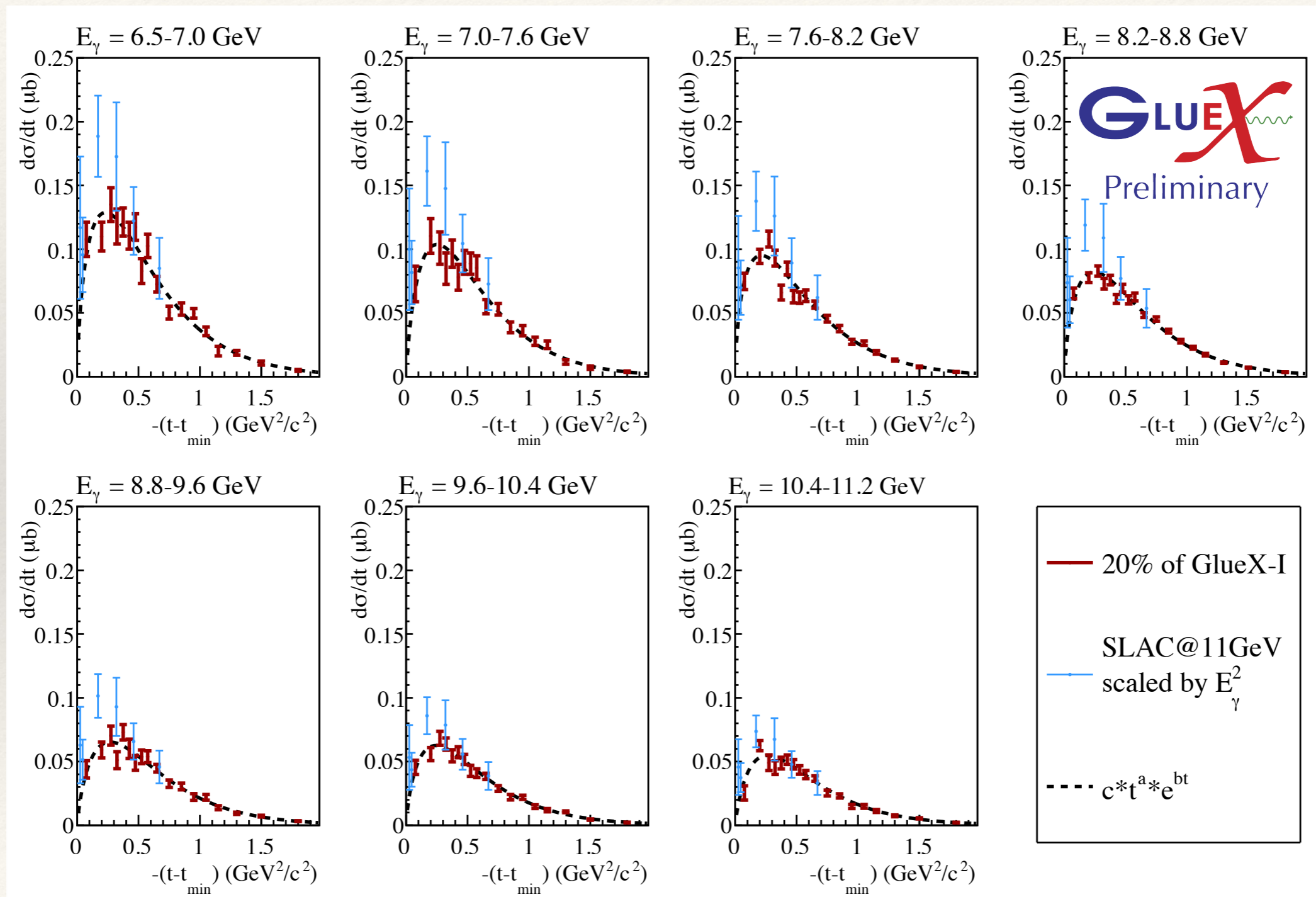
$$\text{Re}(\rho_{3-1}^0 - \rho_{3-1}^1) = \frac{2}{N} (U_{-1}U_1^* + U_2U_0^*)$$

$$N = 2(|N_{-1}|^2 + |N_0|^2 + |N_1|^2 + |N_2|^2 + |U_{-1}|^2 + |U_0|^2 + |U_1|^2 + |U_2|^2)$$

$\Lambda(1520)$ cross-sections

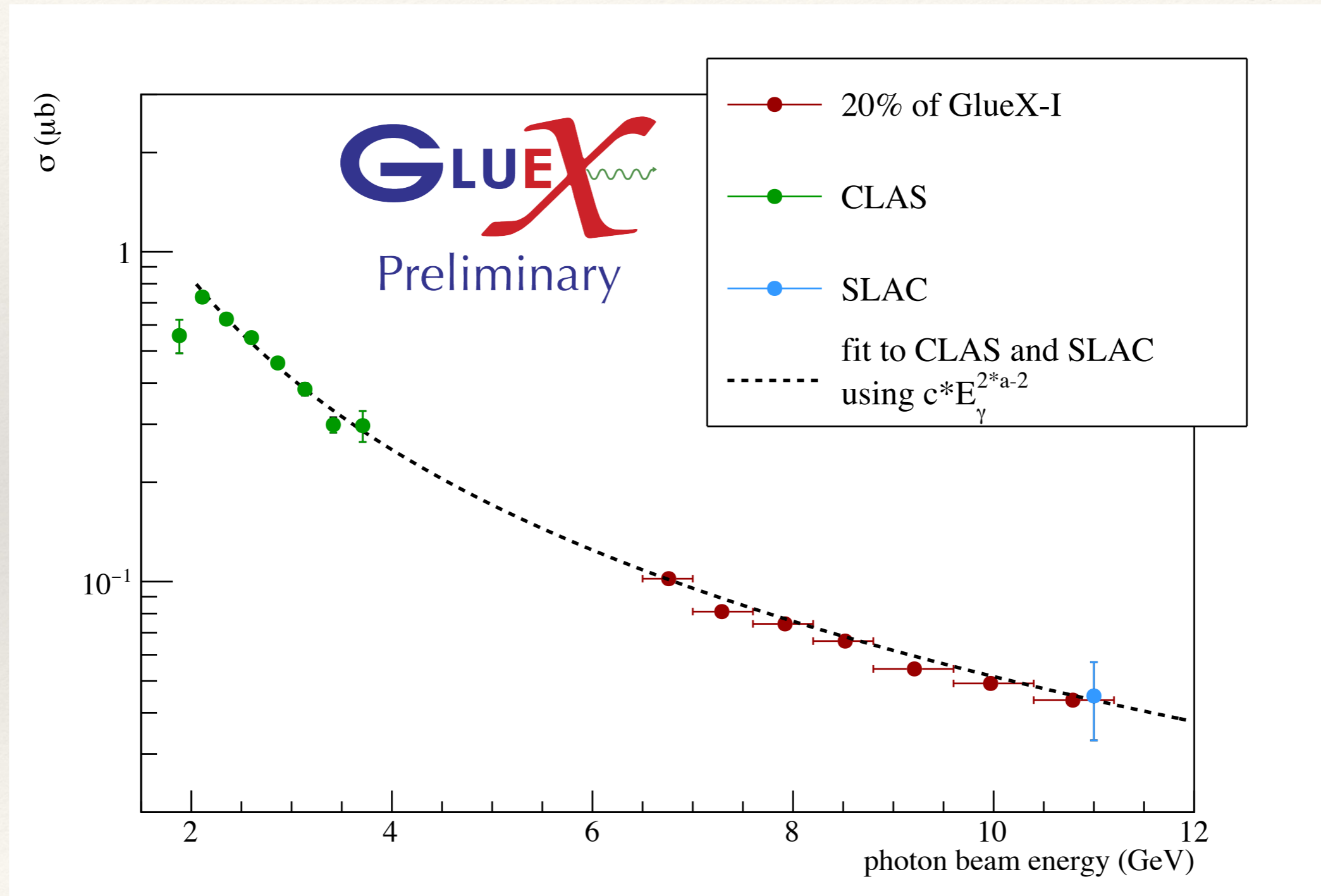
PH (HYP2022)

- ❖ To get full picture of production we need couplings: measure cross-sections
- ❖ Fit t -distribution and integrate to get “total cross-section”



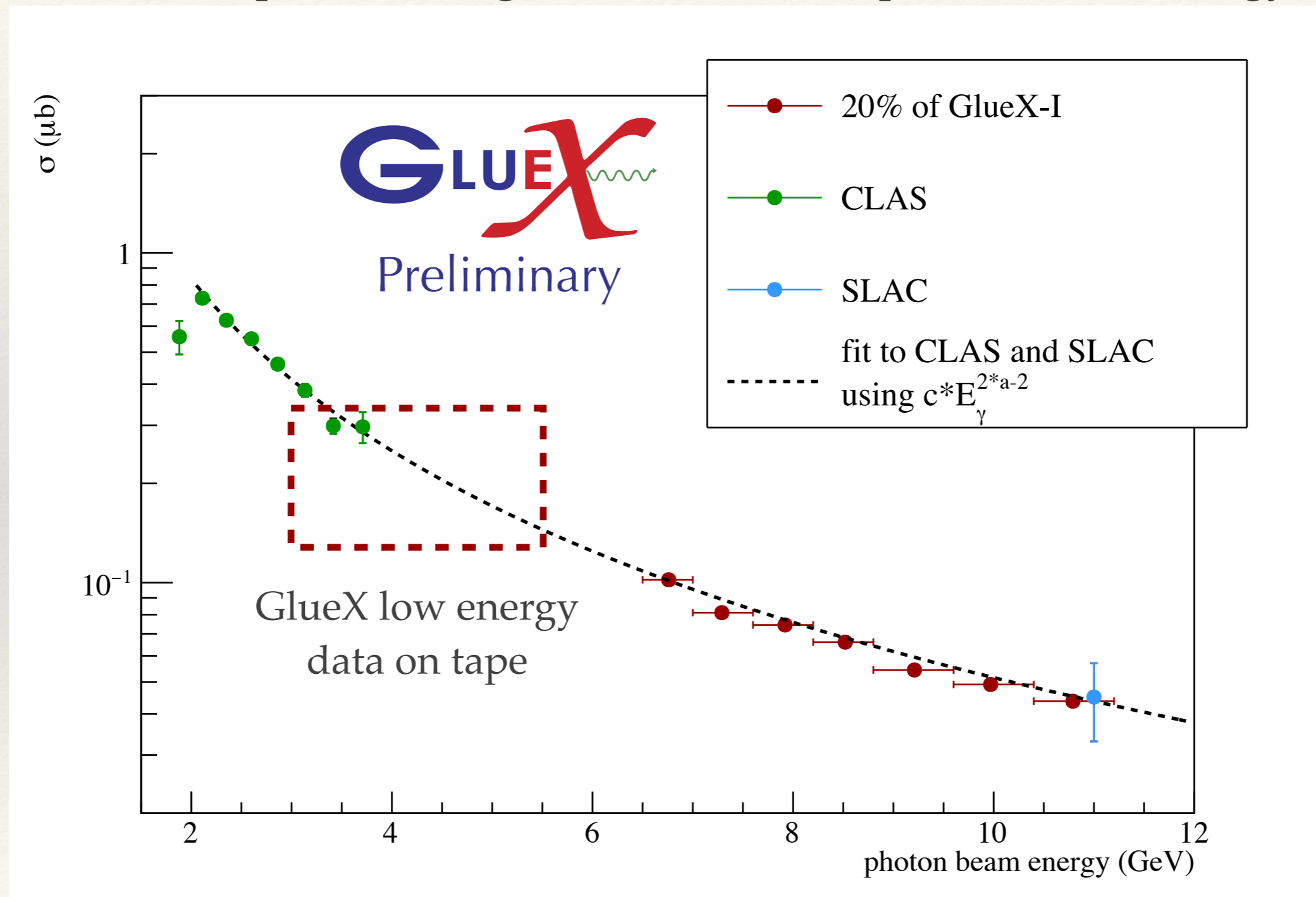
$\Lambda(1520)$ cross-sections

- ❖ Good agreement with previous data by SLAC
- ❖ More data on tape, including some with lower photon beam energy



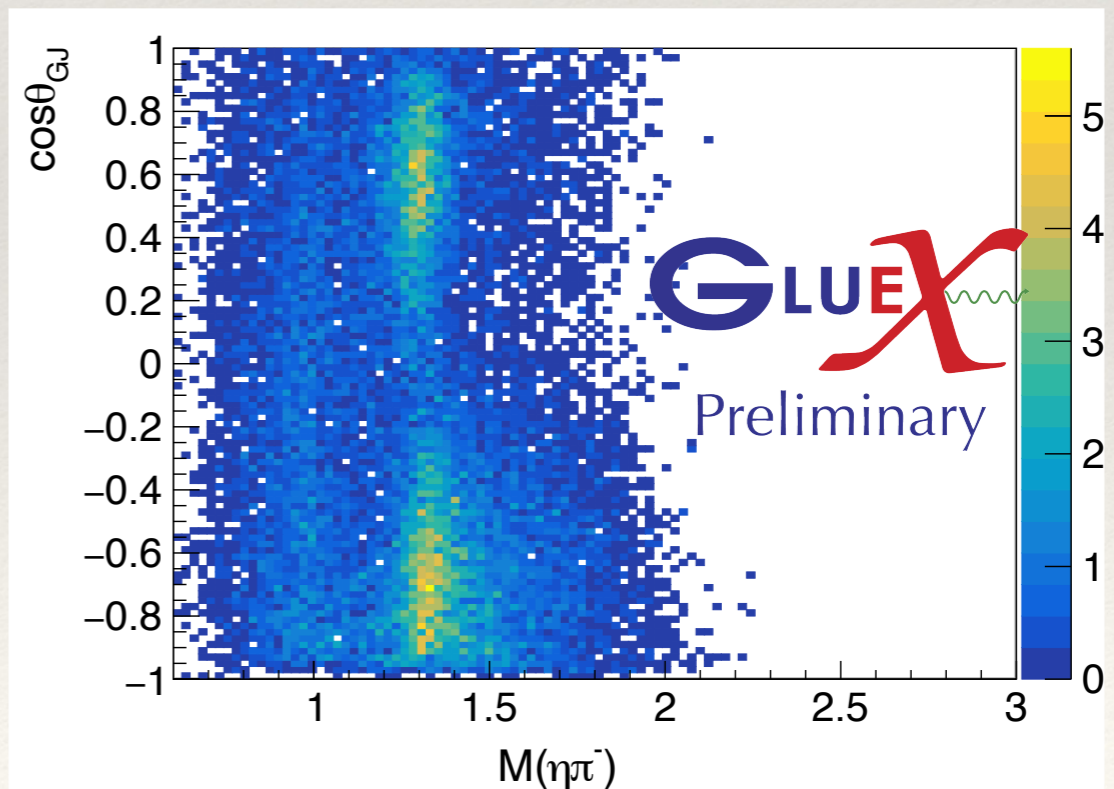
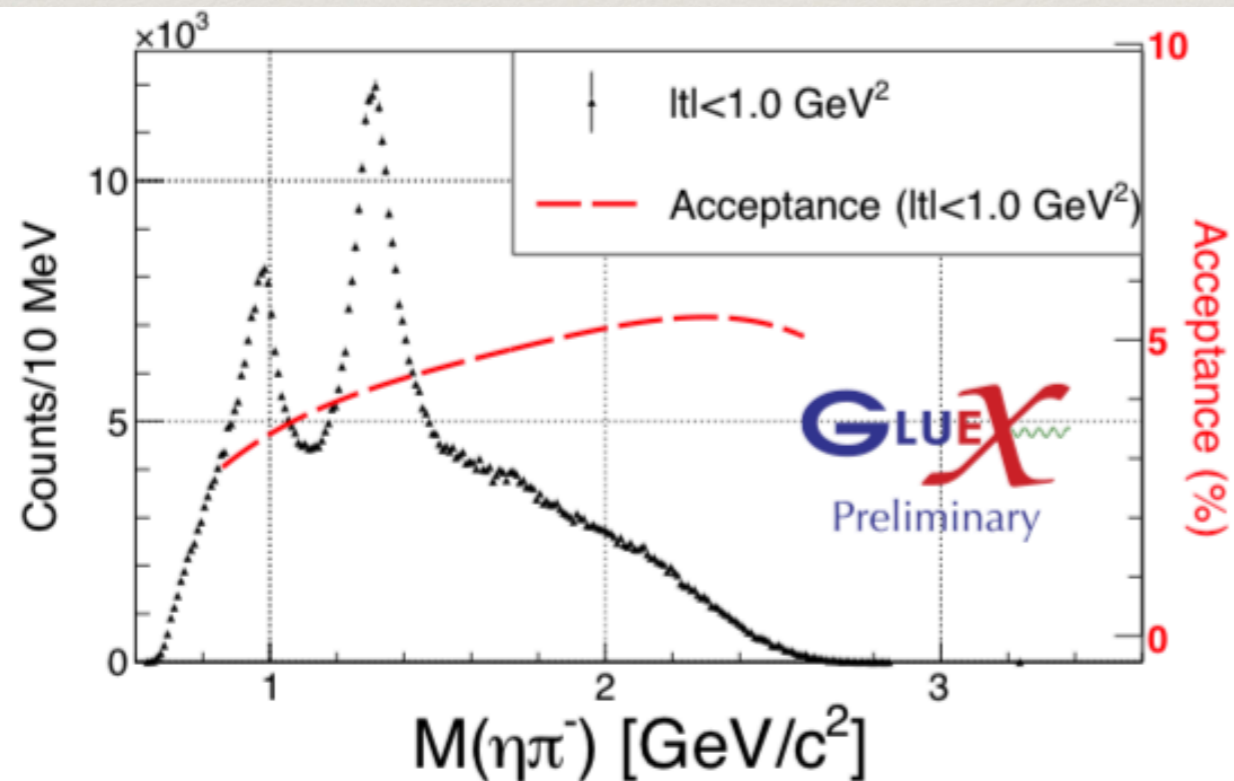
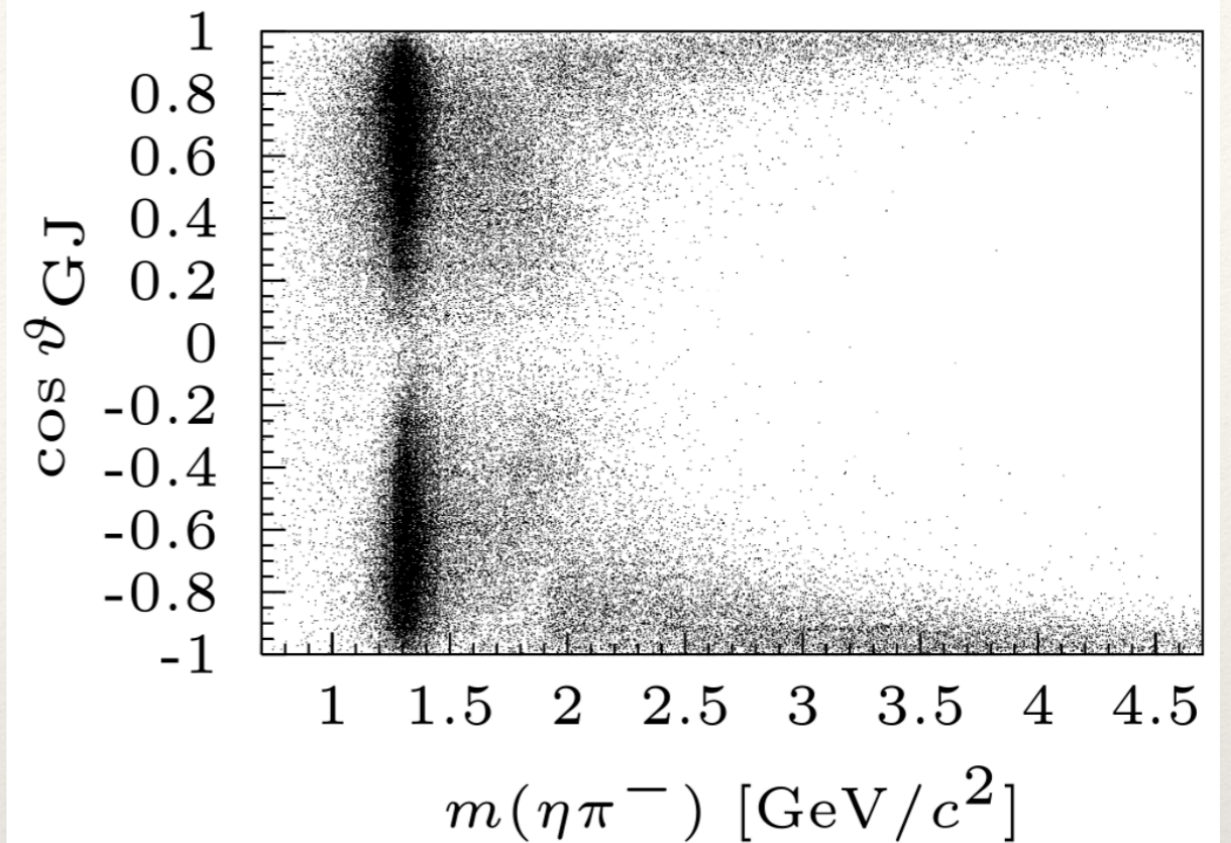
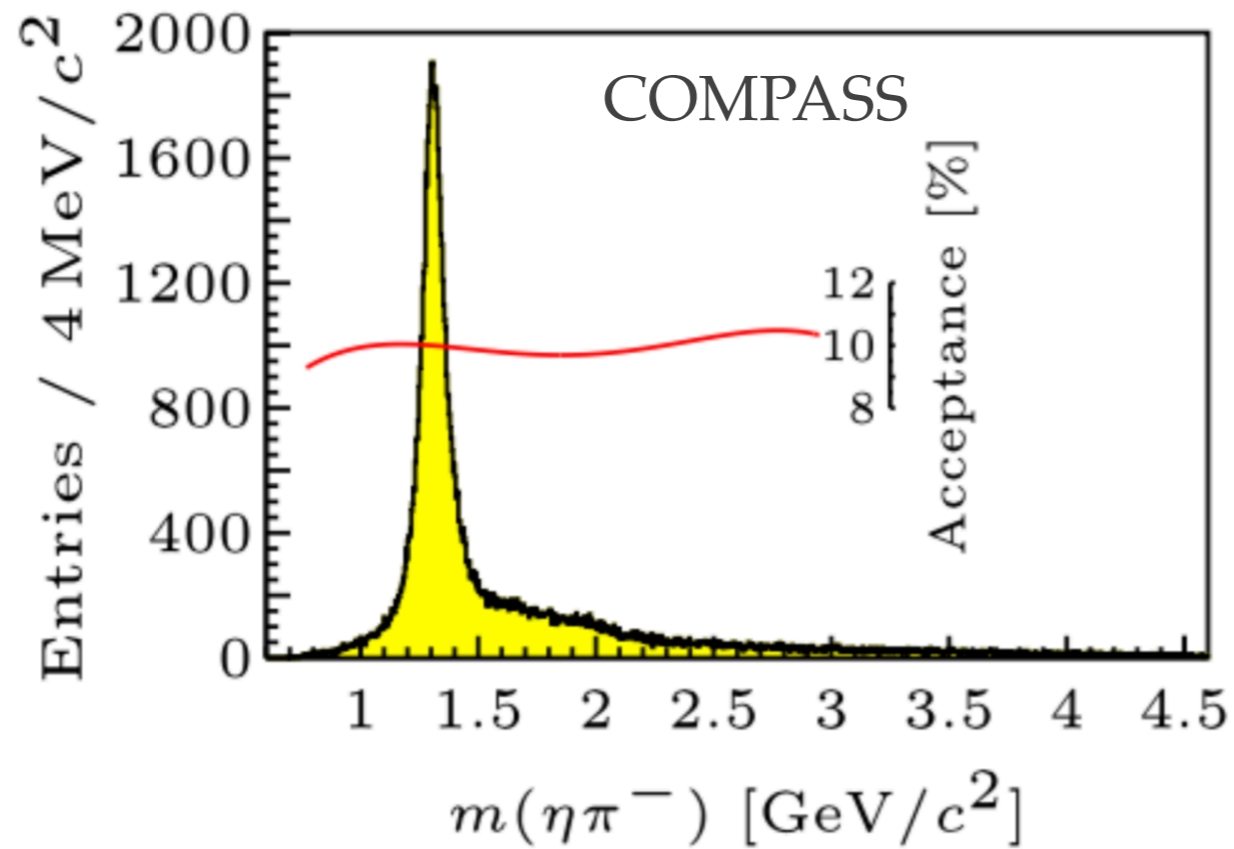
$\Lambda(1520)$ cross-sections

- ❖ Good agreement with previous data by SLAC
- ❖ More data on tape, including some with lower photon beam energy



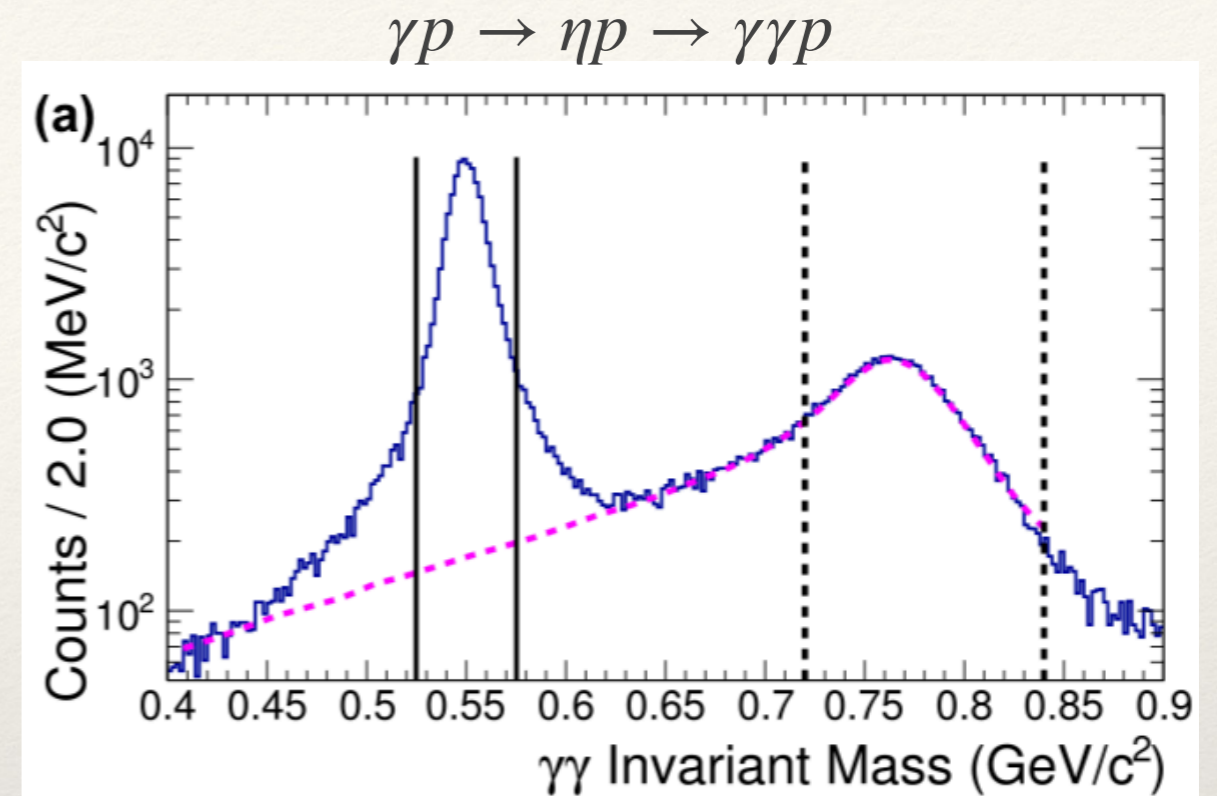
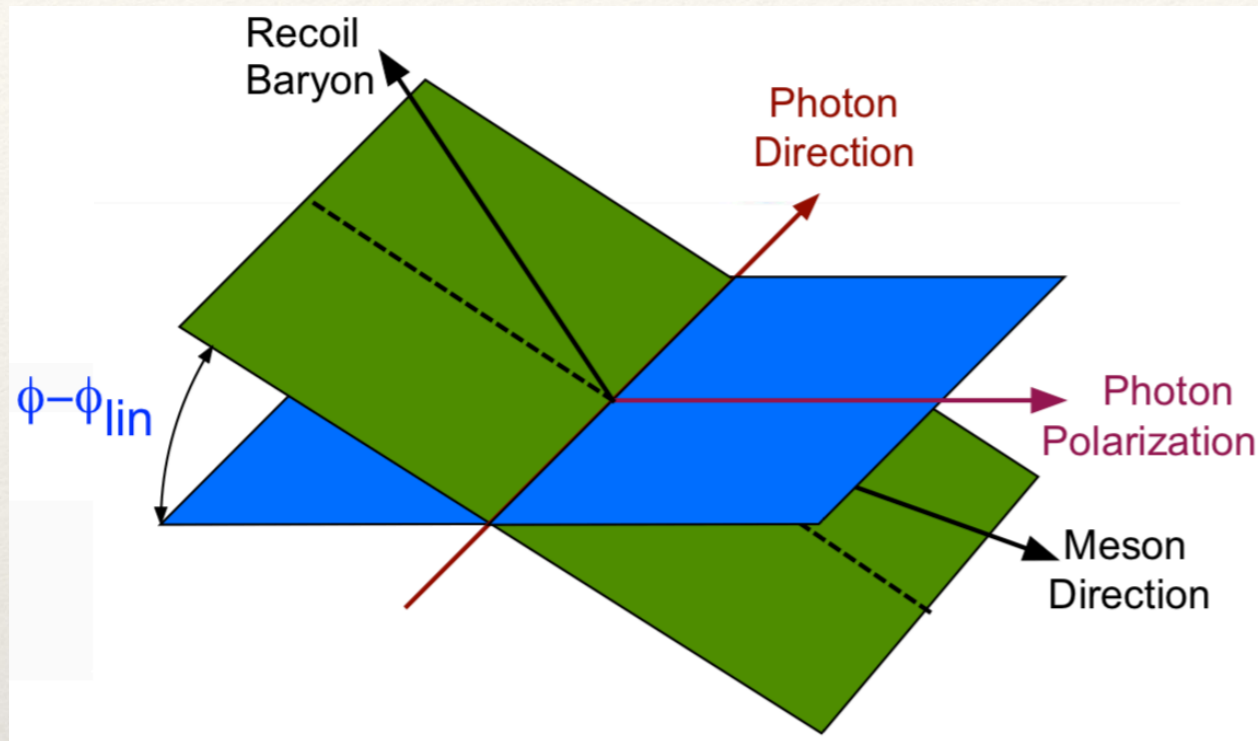
Hybrid search in $\eta\pi^-$

COMPASS, *Phys. Lett. B* 740 (2015) 303–311

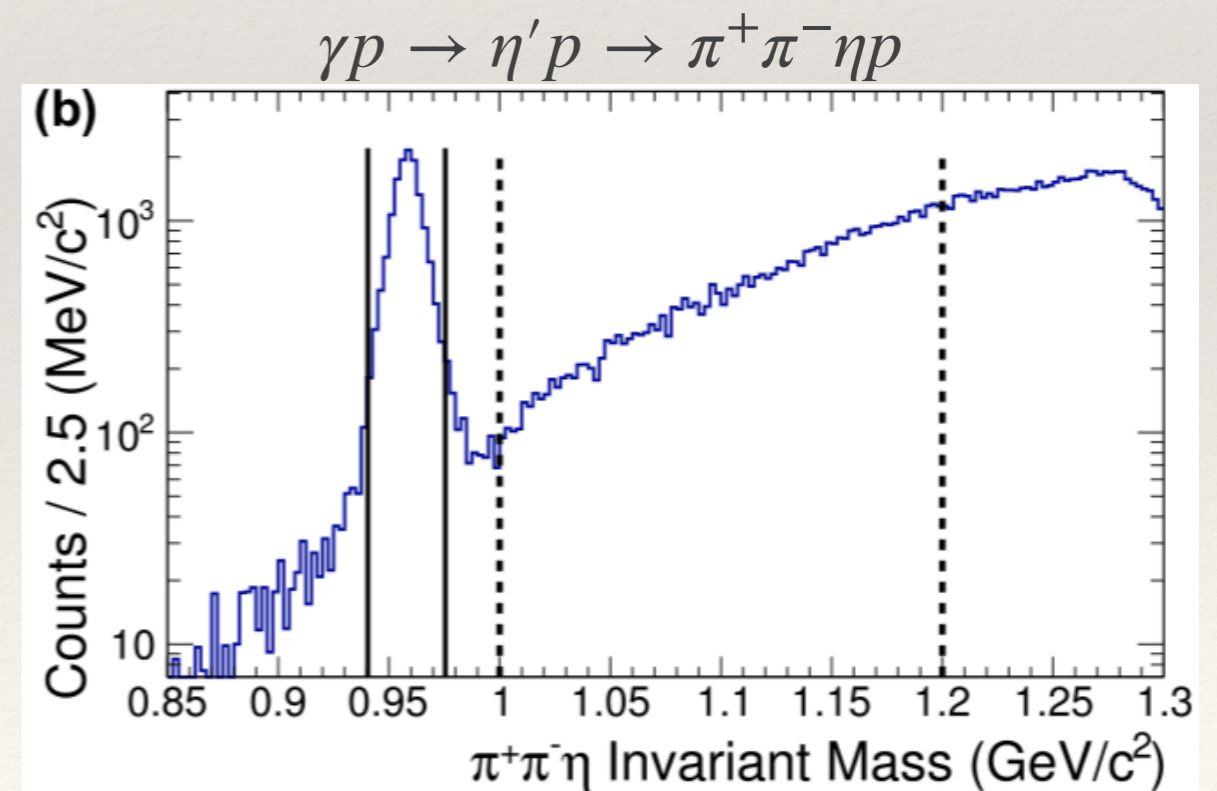


η/η' beam asymmetry

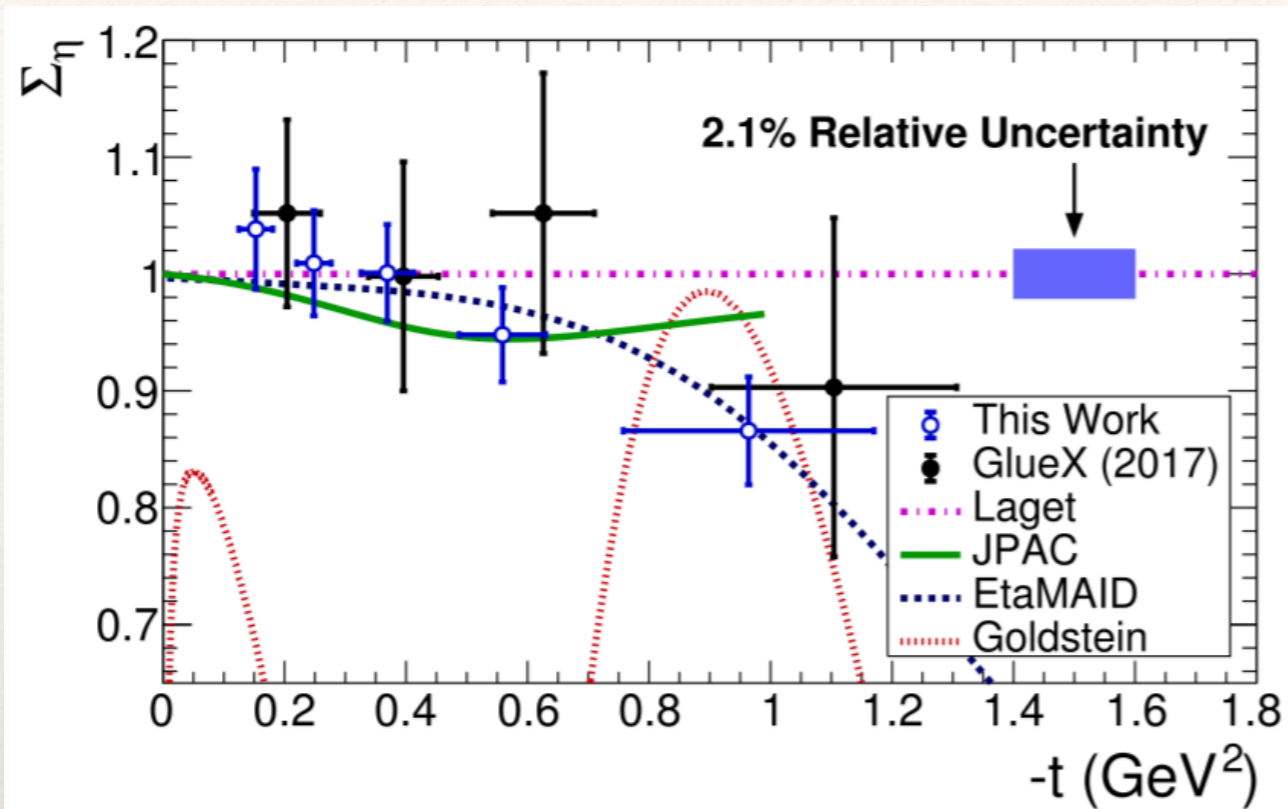
$$\sigma(\phi) \sim 1 - P_\gamma \Sigma \cos 2(\phi - \phi_{lin})$$



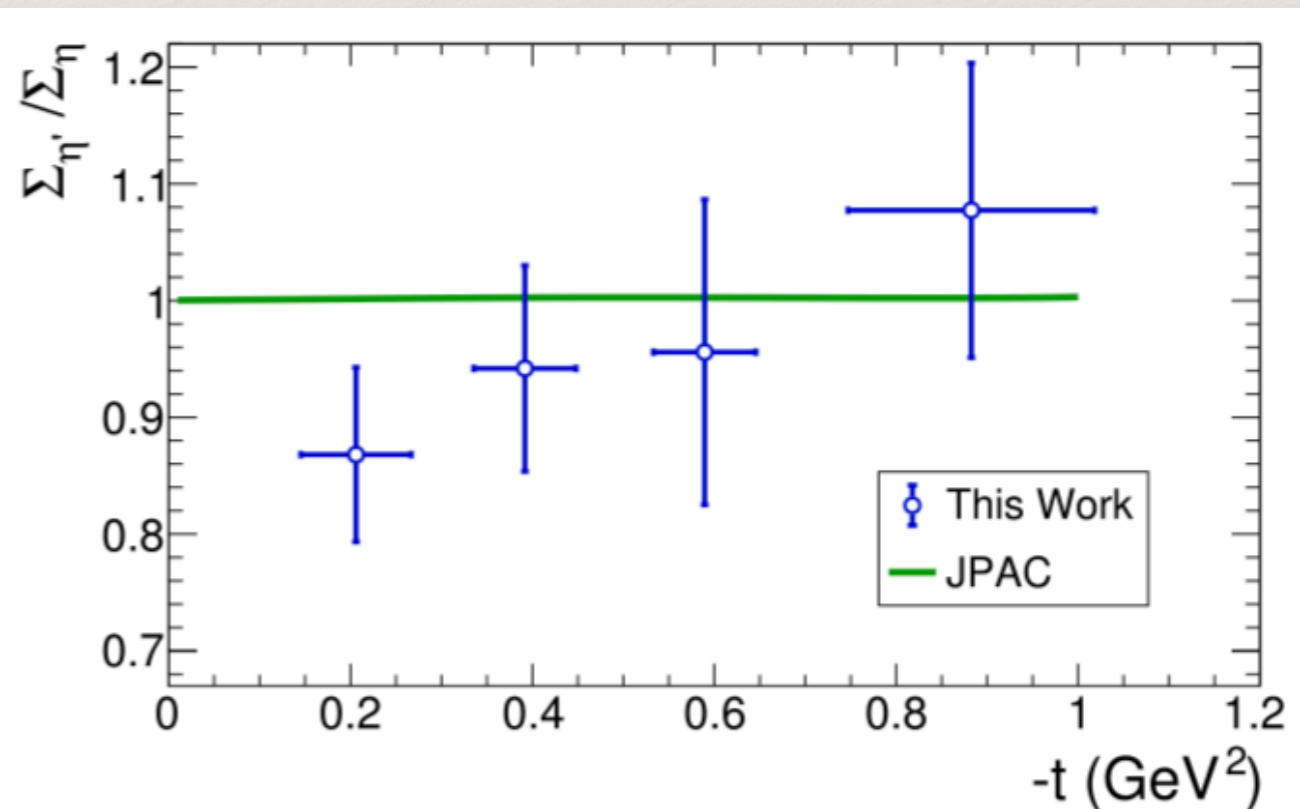
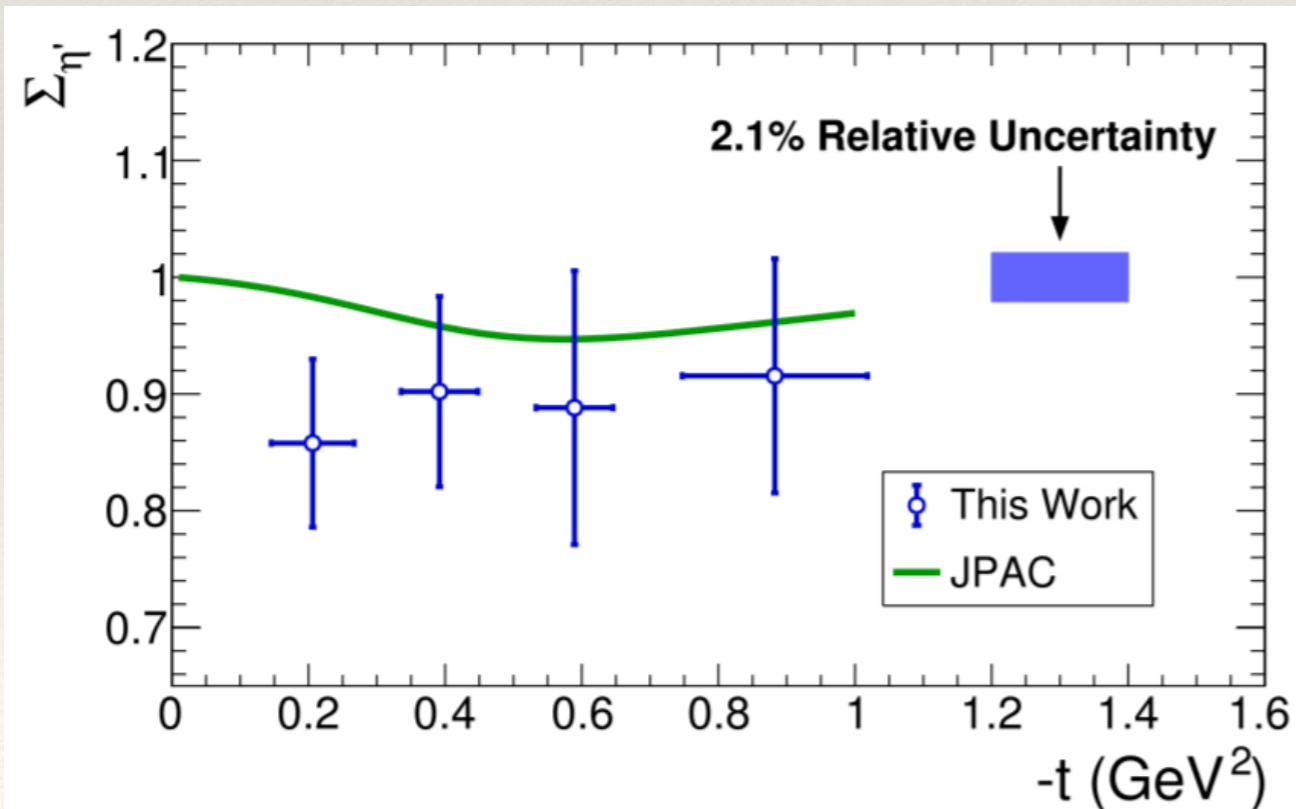
- ❖ measure photon beam asymmetry Σ to learn about t-channel Reggeon exchange
- ❖ ratio of $\Sigma_{\eta'}/\Sigma_{\eta}$ provides information on $s\bar{s}$ exchange



η/η' beam asymmetry

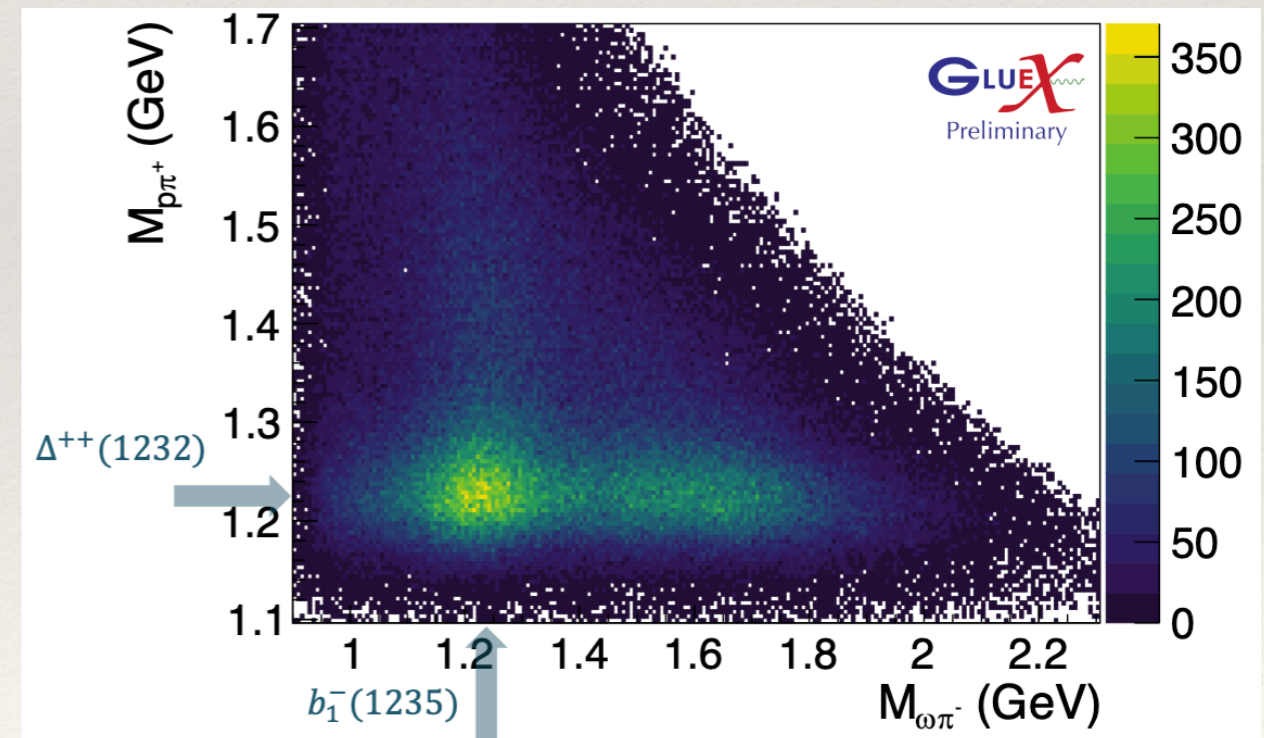
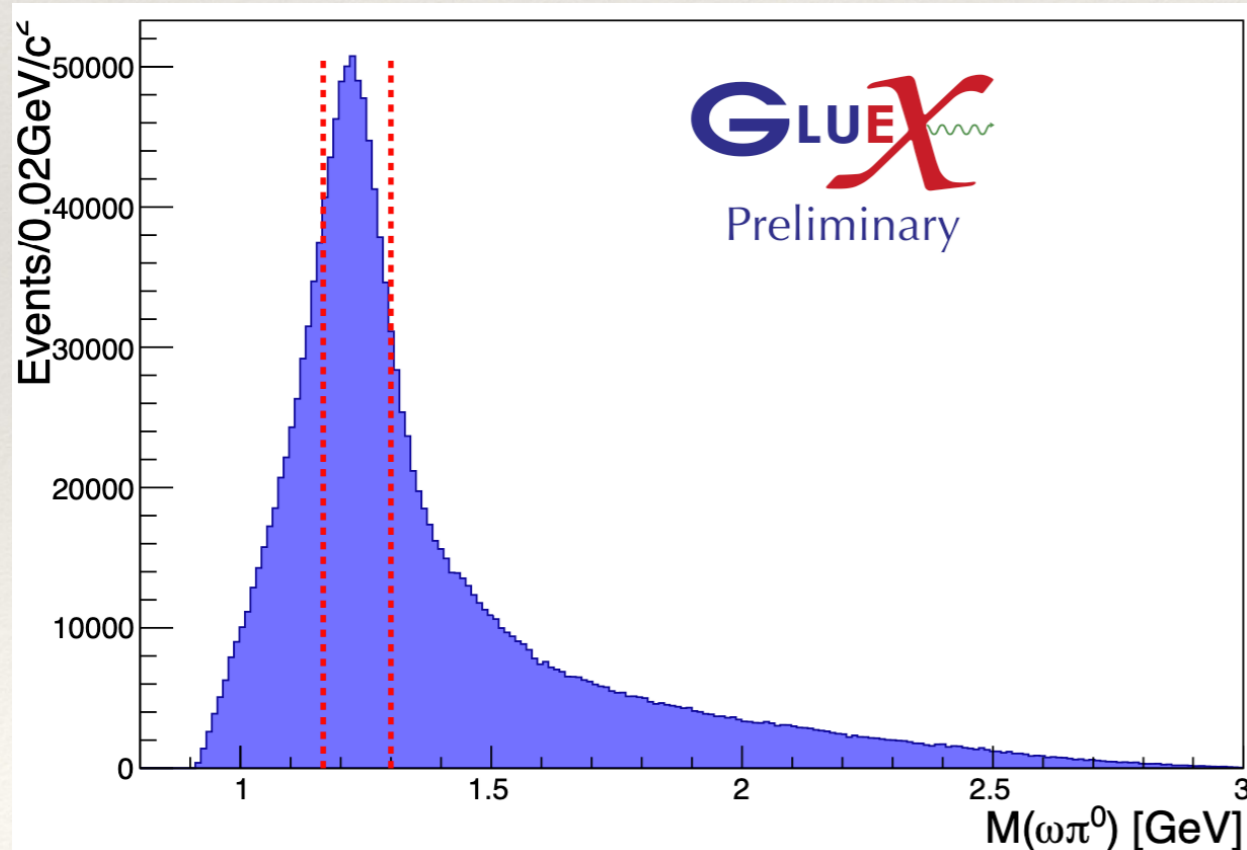


- ❖ vector exchange dominating
- ❖ ratio indicates no substantial $s\bar{s}$ component in exchange



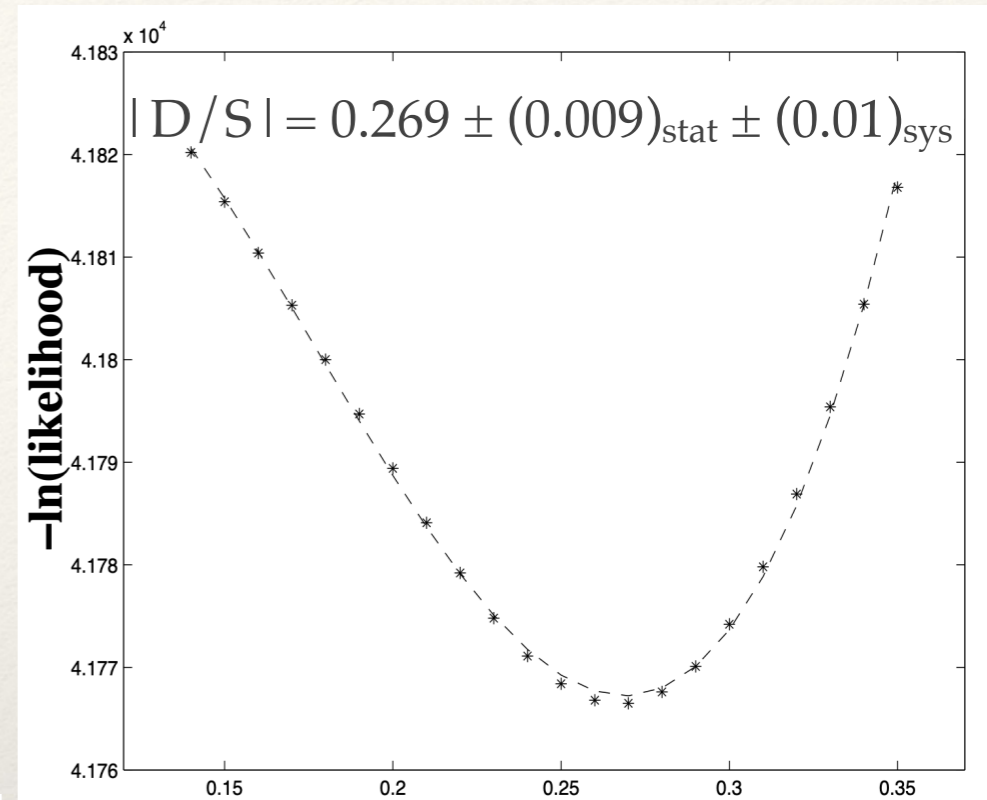
b_1 decay

- ❖ LQCD: $b_1\pi$ is dominating decay mode of 1^{-+} exotic
- ❖ First step: study b_1
 - ❖ $\gamma p \rightarrow b_1 p \rightarrow \omega\pi^0 p \rightarrow \pi^+\pi^-\pi^0\pi^0 p$
 - ❖ $\gamma p \rightarrow b_1^-\Delta^{++} \rightarrow \omega\pi^-\Delta^{++} \rightarrow \pi^+\pi^-\pi^0\pi^-\pi^+ p$

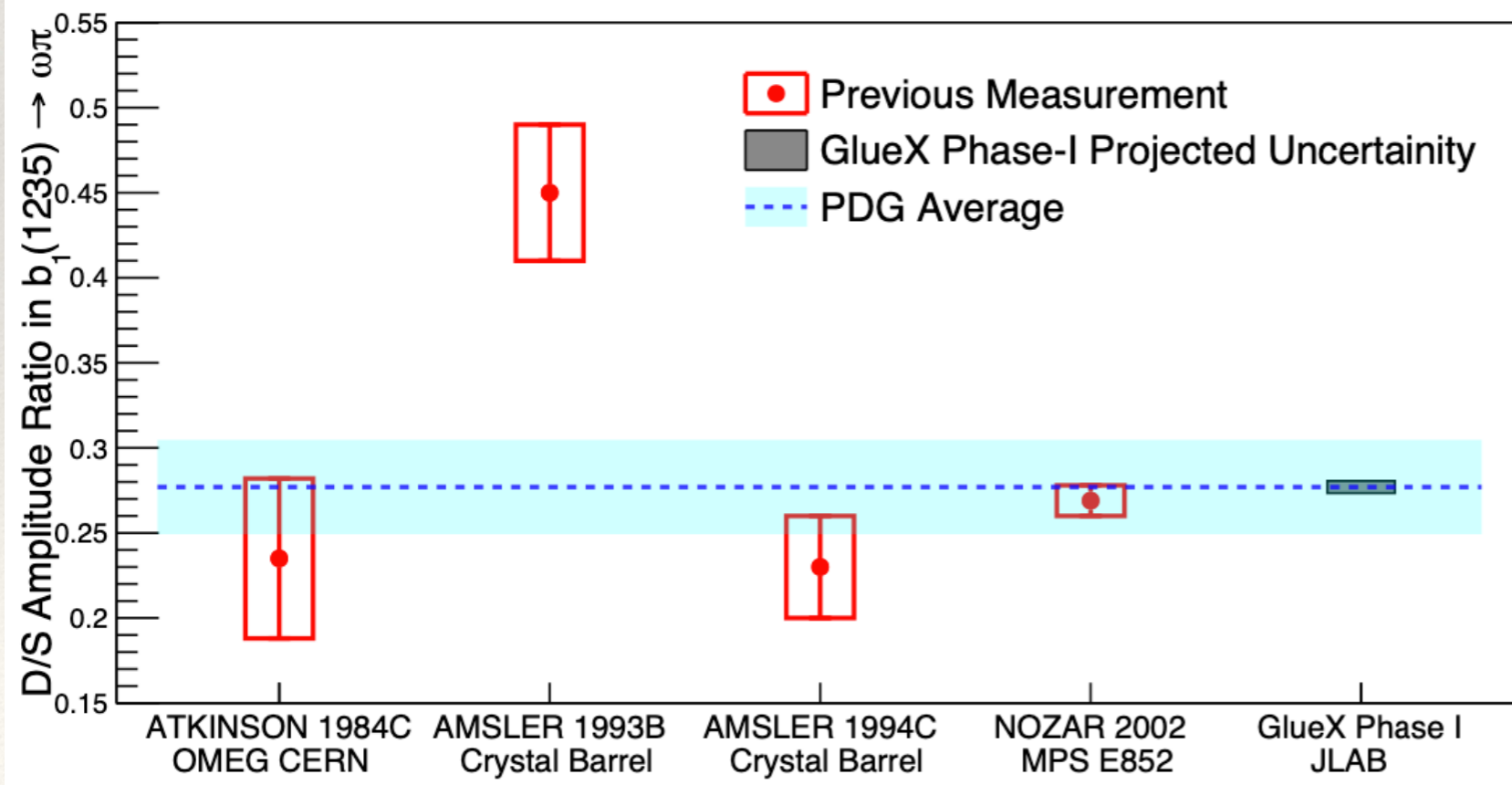


b_1 decay

- ❖ Start by measuring D/S amplitude ratio
- ❖ LQCD prediction by hadspec of $|D/S| = 0.27(20)$
hadspec, Phys. Rev. D 100, 054506 (2019)



E852, Phys. Lett. B 541, 35 (2002)



- ❖ Good first test of amplitude model
- ❖ Can be expanded to all vector-pseudoscalar systems ($\omega\eta, \phi\pi, \phi\eta, \dots$)