

SBS- G_M^n Experiment



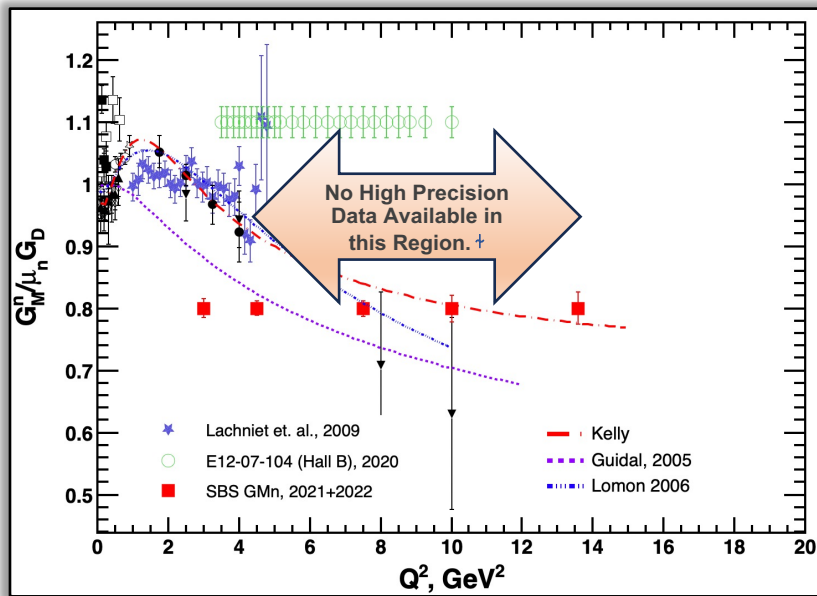
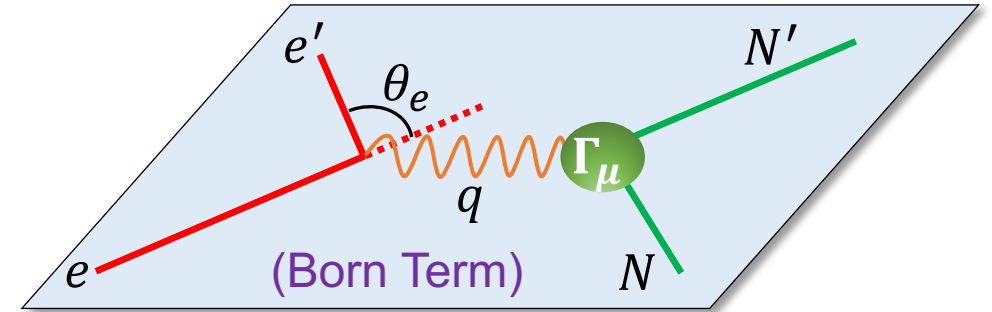
Provakar Datta

(Supervisor: Prof. Andrew Puckett)

Thesis Topic: SBS- G_M^n Experiment

- Ran in Jefferson Lab's Experimental Hall A from Fall 2021 to February 2022.
- ❖ **Goal:** High precision measurement of G_M^n at $Q^2 = 3, 4.5, 7.5, 10$ & 13.6 (GeV/c)².
- Nucleon vertex (elastic e - N scattering):

$$\Gamma_\mu(q) = \gamma_\mu \underbrace{F_1(-q^2)}_{\text{Dirac FF}} + \frac{i\sigma_{\mu\nu}q^\nu}{2M_N} \underbrace{F_2(-q^2)}_{\text{Pauli FF}}$$



- Defining Sachs Form Factors (FFs): $\begin{cases} G_E(Q^2) \equiv F_1(Q^2) - \tau F_2(Q^2) \\ G_M(Q^2) \equiv F_1(Q^2) + F_2(Q^2) \end{cases}$
- G_E, G_M : Sachs Electric and Magnetic FFs, respectively.
- Differential Cross Section:

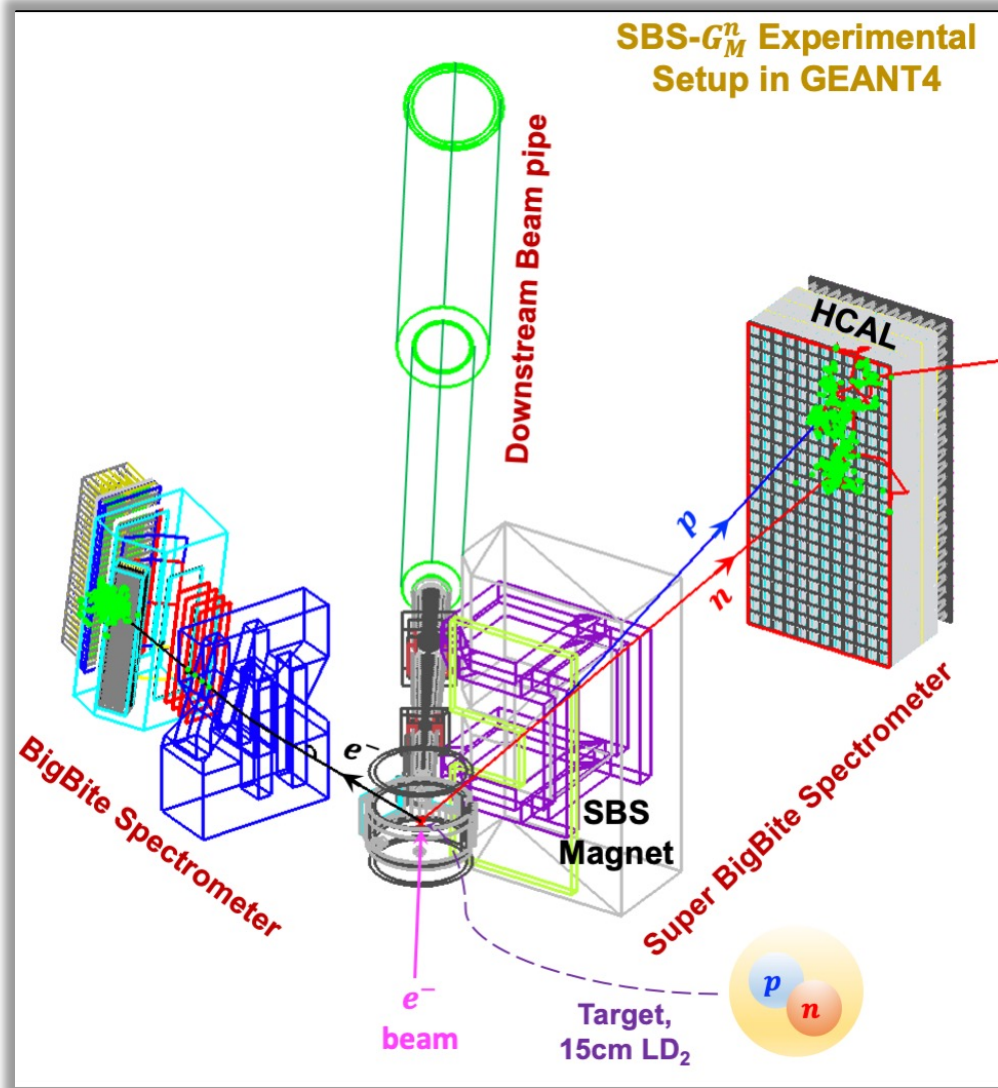
$$\frac{d\sigma}{d\Omega} = \frac{\sigma_{Mott}}{1 + \tau} \left(G_E^2(Q^2) + \frac{\tau}{\epsilon} G_M^2(Q^2) \right)$$

$$\begin{cases} \bullet Q^2 = -q^2 \\ \bullet \tau = Q^2/4M_N^2 \\ \bullet \epsilon = (1 + 2(1 + \tau)\tan^2(\theta_e/2))^{-1} \end{cases}$$

- ❖ Q^2 evolution of Sachs FFs reveal nucleon's internal structure.

† CLAS12 measured G_M^n up to $Q^2 = 10$ GeV^2 , results are yet to be published.

Apparatus & Measurement Technique



- Simultaneous detection of elastically scattered electrons and nucleons lets us use “ratio method”.^[1]
- 3 major steps to get G_M^n :

- 1 Extracting QE cross section ratio, R'' , directly from the experiment:

$$R'' = \frac{\frac{d\sigma}{d\Omega} | d(e, e' n)}{\frac{d\sigma}{d\Omega} | d(e, e' p)}$$

- 2 Apply nuclear corrections to obtain:

$$R' = \frac{\frac{d\sigma}{d\Omega} | n(e, e')}{\frac{d\sigma}{d\Omega} | p(e, e')} \equiv \frac{\frac{\sigma_{Mott}}{1+\tau} (G_E^{n,2} + \frac{\tau}{\epsilon} G_M^{n,2})}{\frac{d\sigma}{d\Omega} | p(e, e')}$$

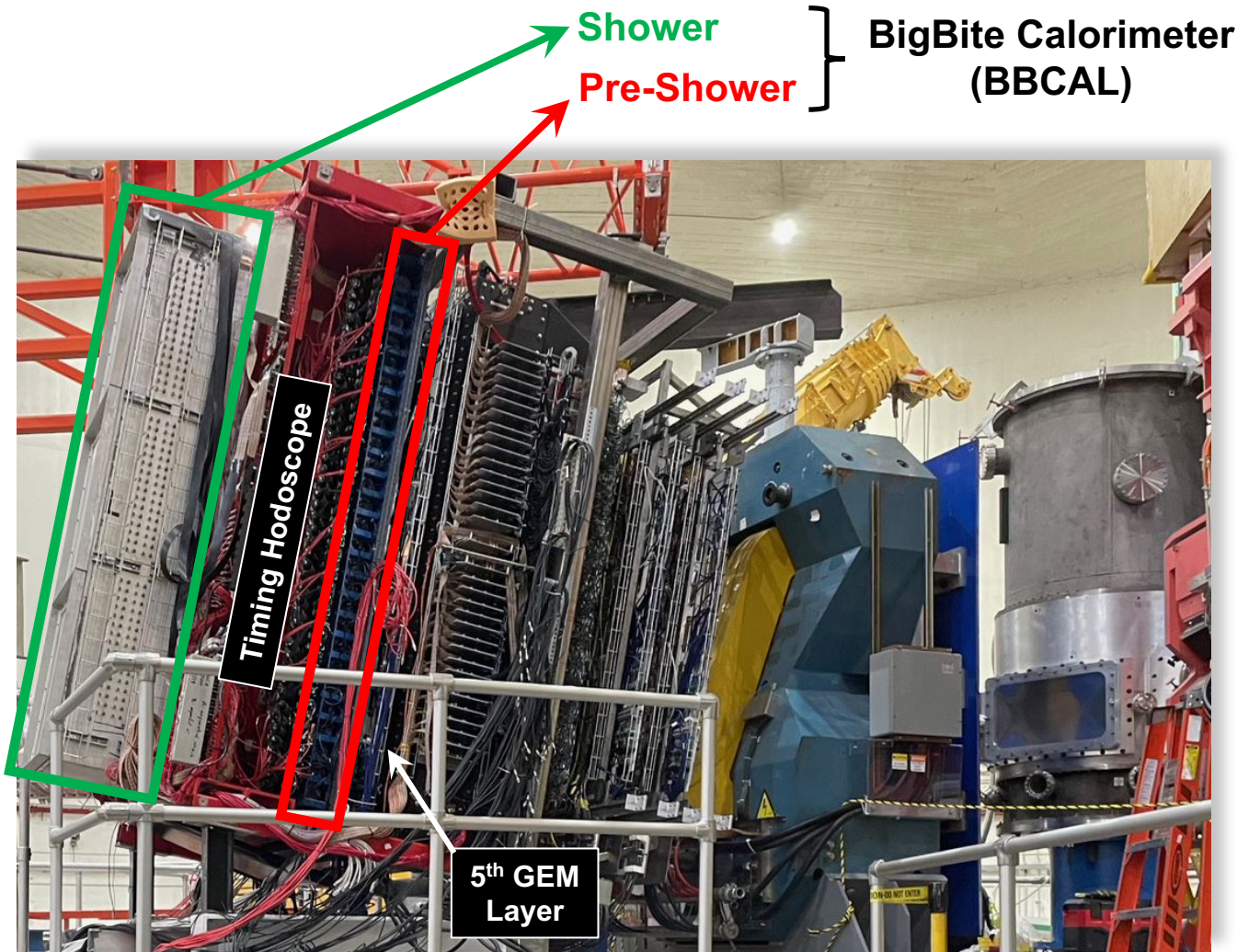
- 3 Finally,

$$G_M^n = - \left[\frac{1}{\tau} \frac{d\sigma}{d\Omega} | p(e, e') R' - \frac{\epsilon}{\tau} G_E^{n,2} \right]^{\frac{1}{2}}$$

- ❖ “Ratio method” is way less sensitive to systematic errors than other measurement techniques.^[1]

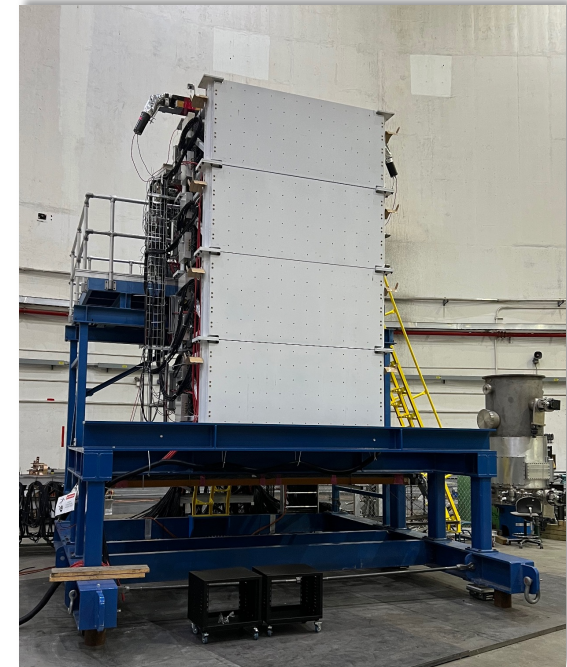
^[1] L. Durand, Phys. Rev. 115 1020 (1959).

Hardware Focus: SBS Calorimeters (BBCAL & HCAL)



The BigBite Spectrometer in Hall A (Side View)

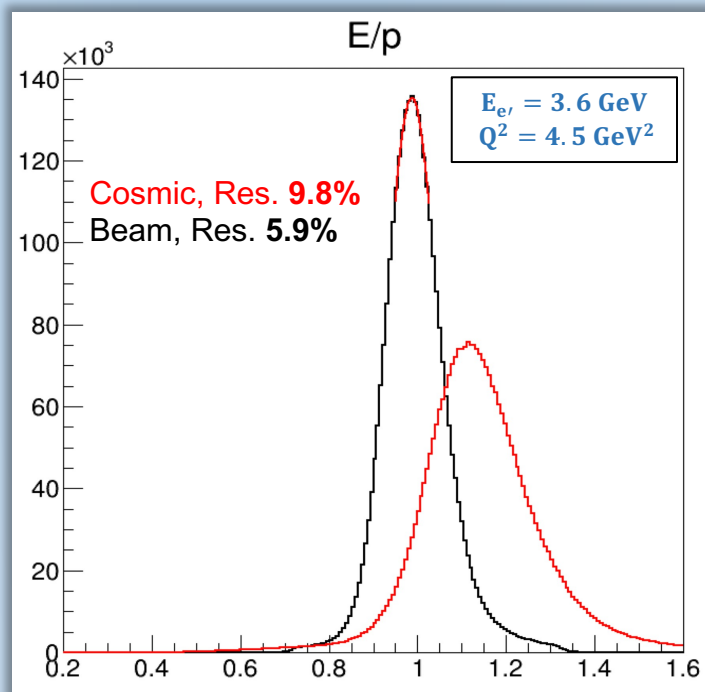
Hadron Calorimeter (HCAL)



- I am a part of the SBS calorimeter group.
- Primarily worked on the testing, commissioning, and calibration of the BigBite calorimeter (BBCAL). Offline fine tuning of the calibration for G_M^n is still ongoing.
- Provided expert support during G_M^n experiment and doing the same during G_E^n -II.

Analysis Status

- We finished 1st pass cooking of the entire SBS- G_M^n experiment in January this year. **Now, we are almost ready to start 2nd pass cooking.**
- Realistic MC event generator including nuclear and radiative effects is now available for $G_M^n/nTPE$ analysis.
- Sophisticated physics analysis machineries for quasi-elastic event selection, yield extraction, data/MC comparison, nucleon detection efficiency estimation are in place. A huge effort is ongoing to optimize them.



- Highlights of Detector Performance using pass 0/1 data:

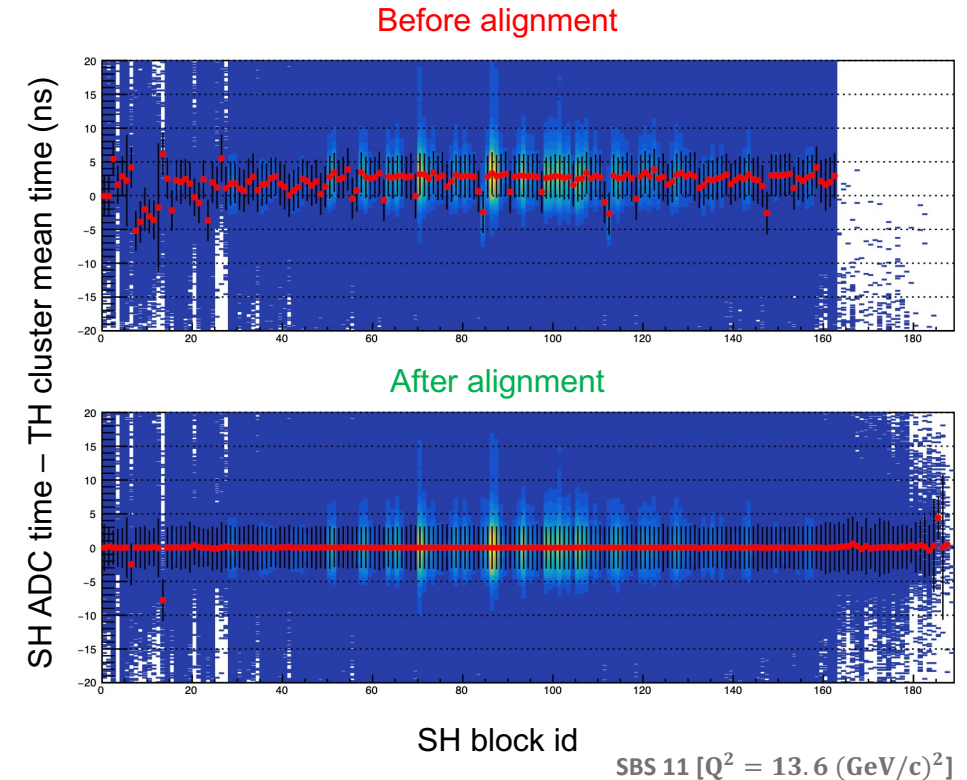
- BigBite Spectrometer:
 - Momentum resolution: $\frac{\sigma_p}{p} \approx 1 - 1.5\%$
 - Angular resolution (in-plane & out-of-plane): **1 – 2 mrad**
 - Vertex resolution: $\sigma_z \leq 1 \text{ cm}$
 - BigBite Calorimeter(BBCAL) energy resolution: **5.9% at 3.6 GeV** scattered e^- energy.
- Super BigBite Spectrometer:
 - Hadron Calorimeter (HCAL):
 - Time Resolution: $\sigma_t \approx 1.7 \text{ ns}$
 - Angular Resolution: **~2 mrad**

BBCAL Calibration Highlights

Energy calibration

Configuration	E_{beam} (GeV)	$E_{e'}$ (GeV)	Magnet current (A)		E/p peak position		BBCAL resolution (%)	
			BB	SBS	Before calib.	After calib.	Before calib.	After calib.
SBS-4	3.728	2.11	750	0	0.97	0.99	6.4	6.2
			750	630	0.97	0.99	6.4	6.3
			750	1050	0.98	0.99	6.6	6.3
SBS-7	7.906	2.67	750	1785	0.97	0.99	6.4	6.2
SBS-11	9.91	2.67	750	0	1.01	1.00	8.0	7.7
			750	2100	1.02	0.99	7.0	6.2
SBS-14	5.965	2.00	750	0	0.98	0.99	7.5	7.4
			750	1470	0.99	0.99	6.9	6.4
SBS-8	5.965	3.59	750	0	0.96	0.99	5.6	5.7
			750	1050	0.95	0.99	5.6	5.6
			750	1470	0.99	0.99	6.8	6.2
			750	2100	0.96	0.99	5.6	5.6
SBS-9	4.015	1.63	750	1470	0.99	0.99	7.4	7.0

ADC time alignment

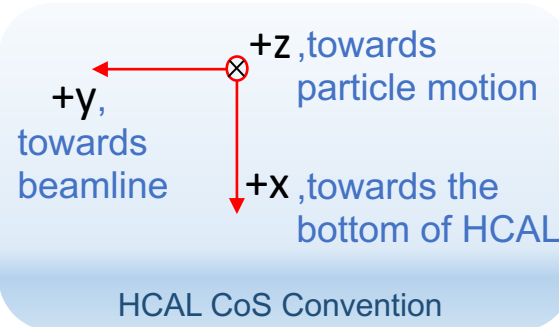
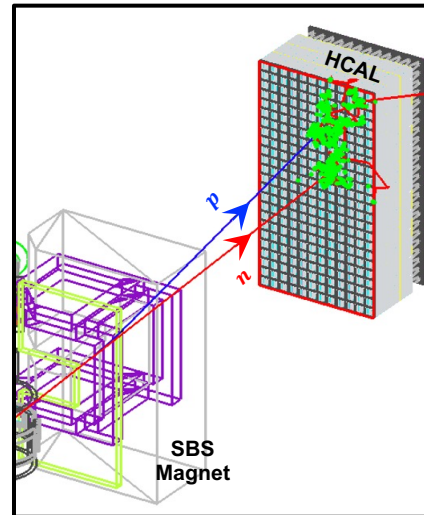
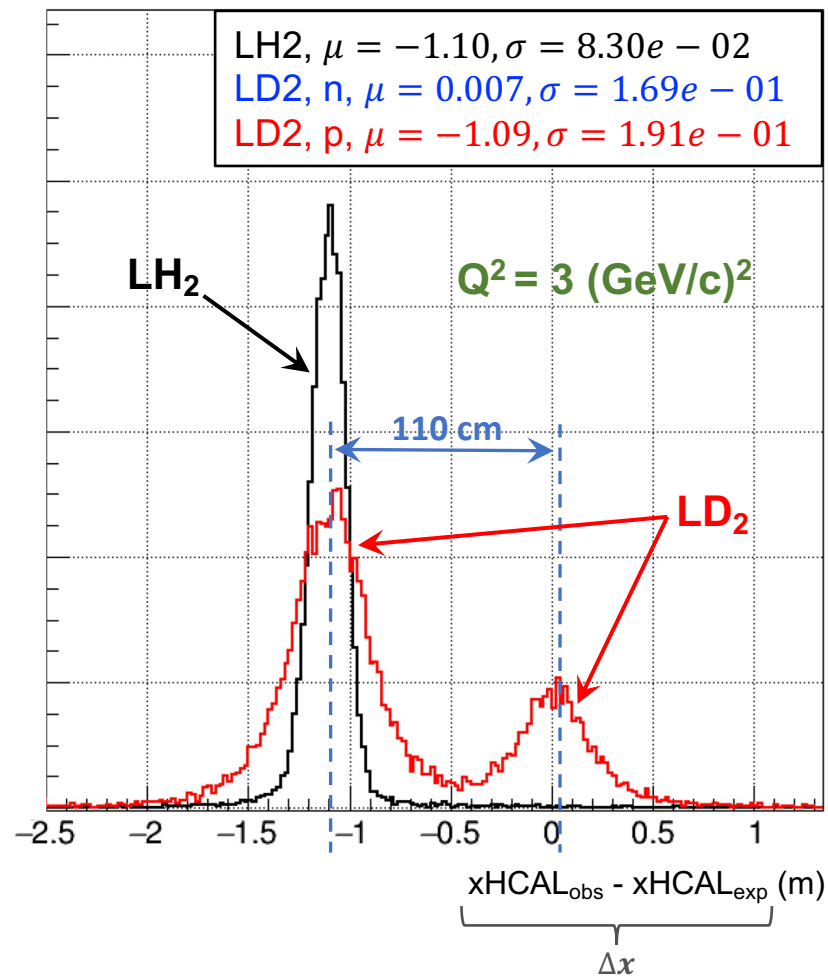


- Fine tuning of BBCAL energy calibration for all 13 different settings is done for pass 2 readiness. **5.6%** energy resolution at **3.6 GeV** elastic e^- energy.
- ADC time alignment is done as well for both SH and PS for all the $G_M^n/n\text{TPE}$ configurations. Achieved **1.6 ns** time resolution from BBCAL-HCAL coincidence ADC time for $Q^2 = 3 \text{ (GeV/c)}^2$.

BBCAL is ready for 2nd pass cooking!

Physics Analysis Highlights: Quasi-Elastic (QE) Event Selection

❖ Introducing HCAL Δx plot:



■ Primary Cuts:

1. Presence of a track
2. $|(\text{vertex})_z| < 0.08 \text{ m}$
3. PS cluster energy $> 0.2 \text{ GeV}$
4. Cut on reconstructed track momentum (kinematics dependent)

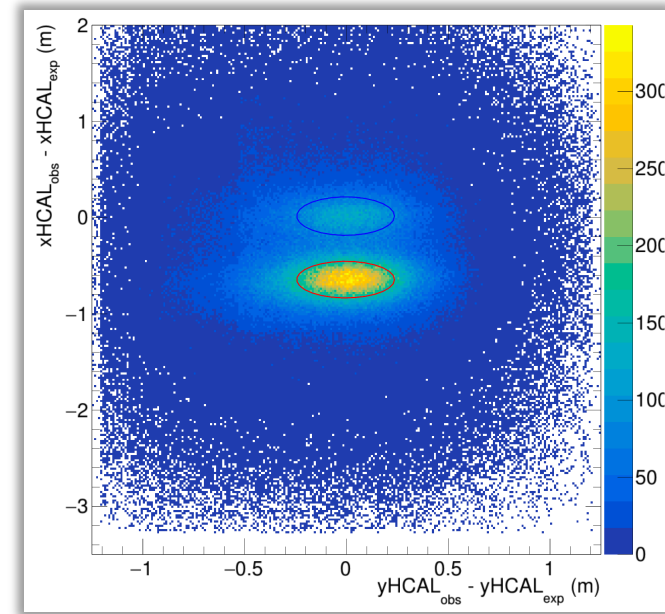
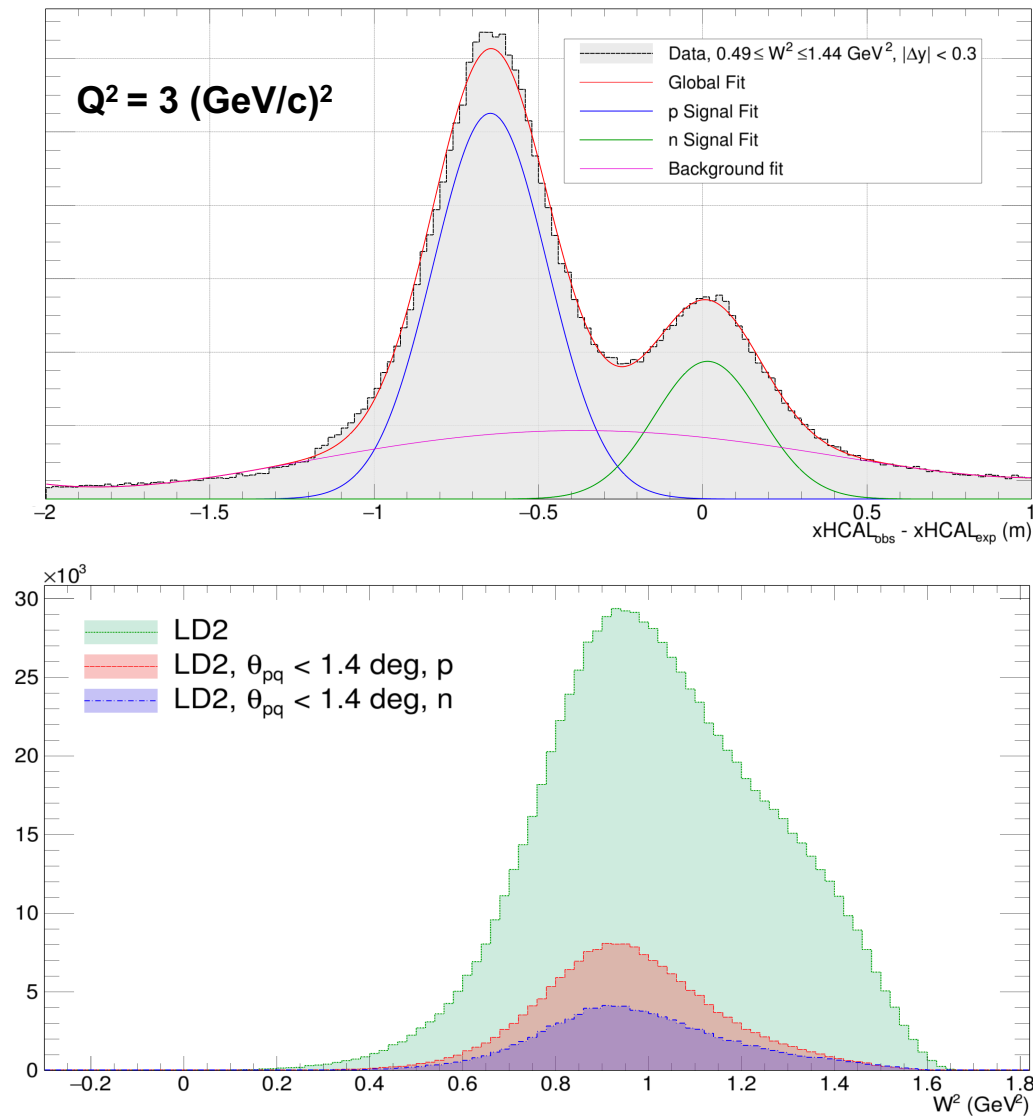
■ QE Event Selection Cuts: (Q^2 dep.)

1. Cut on W^2
2. Cut on Δy
3. Cut on θ_{pq} (angle between reconstructed nucleon momentum (\vec{p}) and the momentum transfer vector (\vec{q}))
4. Fiducial/Acceptance Cuts

❖ Fitting Δx plot we can extract $d(ee'n)p$ & $d(ee'p)n$ yields and then form the ratio:

$$R'' = \frac{\frac{d\sigma}{d\Omega} |_{d(e,e'n)}}{\frac{d\sigma}{d\Omega} |_{d(e,e'p)}}$$

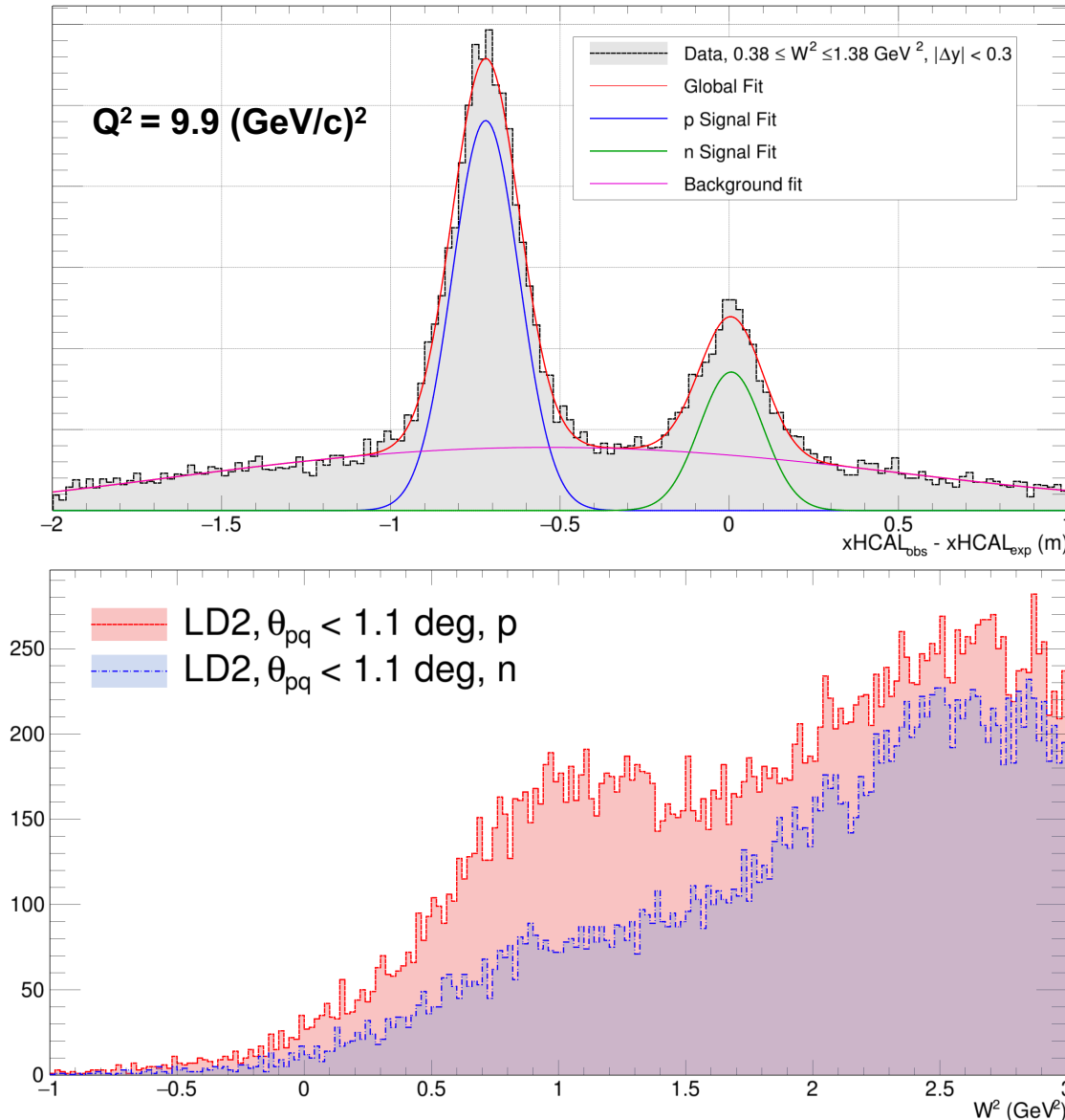
QE Event Selection: $Q^2 = 3 \text{ (GeV/c)}^2$ [SBS-4]



Figures: HCAL Δx (Top Left), HCAL Δx vs Δy (Top Right), W^2 (Bottom Left)

- All primary cuts listed on page 5.
 - Fiducial Cuts
 - $0.49 \leq W^2 \leq 1.44 \text{ GeV}^2$ (Δx & Δx vs Δy plots)
 - $|\Delta y| < 0.3 \text{ m}$ (Δx & Δx vs Δy plots)
 - $\theta_{\text{pq}} < 1.4^\circ$ with p hypothesis (W^2 plot)
 - $\theta_{\text{pq}} < 1.4^\circ$ with n hypothesis (W^2 plot)
- We fit the Δx distribution to sum of two Gaussian signals (p & n) along with a 4th degree polynomial background to extract raw $d(e, e'(p, n))$ yields.

QE Event Selection: $Q^2 = 9.9 \text{ (GeV/c)}^2$ [SBS-7]



Figures: HCAL Δx (Top Left), HCAL Δx vs Δy (Top Right), W^2 (Bottom Left)

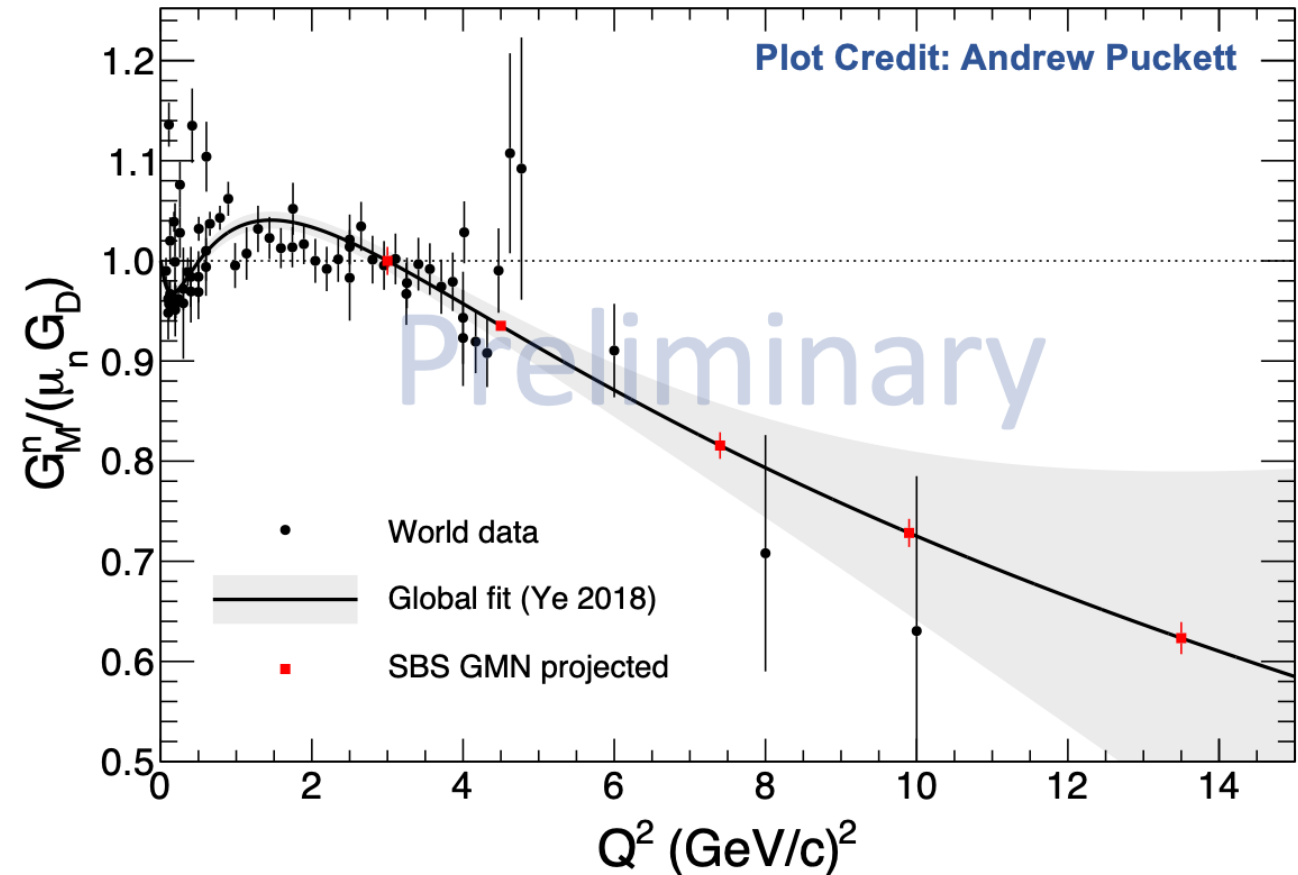
- All primary cuts listed on page 5.
 - Fiducial Cuts
 - $0.38 \leq W^2 \leq 1.38 \text{ GeV}^2$ (Δx & Δx vs Δy plots)
 - $|\Delta y| < 0.3 \text{ m}$ (Δx & Δx vs Δy plots)
 - $\theta_{\text{pq}} < 1.1^\circ$ with **p** hypothesis (W^2 plot)
 - $\theta_{\text{pq}} < 1.1^\circ$ with **n** hypothesis (W^2 plot)
- We fit the Δx distribution to sum of two Gaussian signals (p & n) along with a 4th degree polynomial background to extract raw $d(e, e'(p, n))$ yields.

Raw Yields & Preliminary Uncertainty Projections

Table I: Estimated Raw QE Yields from SBS- G_M^n dataset

Q^2 (GeV/c) ²	E_{beam} (GeV)	Raw QE Yields	Projected $\Delta_{\text{stat}}(G_M^n/G_M^p)$	Projected $\Delta_{\text{syst}}(G_M^n/G_M^p)$
3.0	3.73	471,000	0.12%	1.4%
4.5	5.97	1,092,000	0.07%	0.6%
7.4	5.97	76,700	0.30%	1.6%
9.9	7.91	13,100	0.70%	1.8%
13.5	9.86	19,200	0.60%	2.5%

- Relative statistical uncertainties in G_M^n/G_M^p is estimated from the raw yields we got using the analysis shown in the previous slides.
- Projected systematic uncertainties have been taken from experiment proposal.
- ❖ Things we **haven't** considered:
 - HCAL p/n detection efficiency corrections
 - Radiative corrections
 - Nuclear corrections
 - Nucleon misidentification probabilities and many more

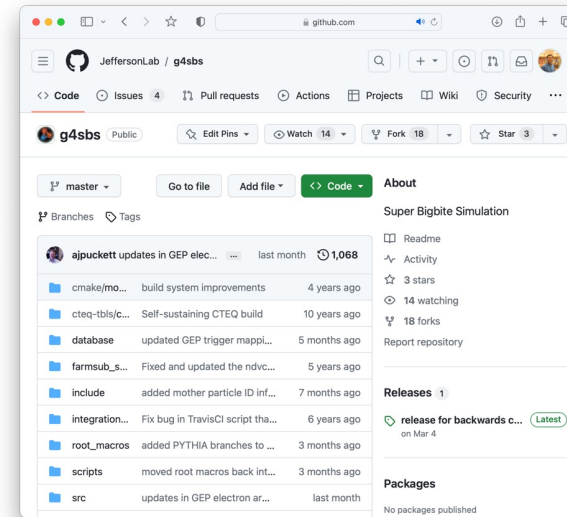
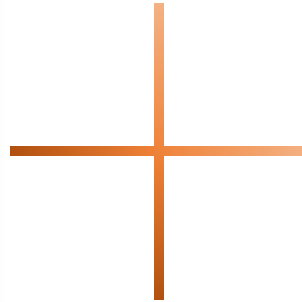
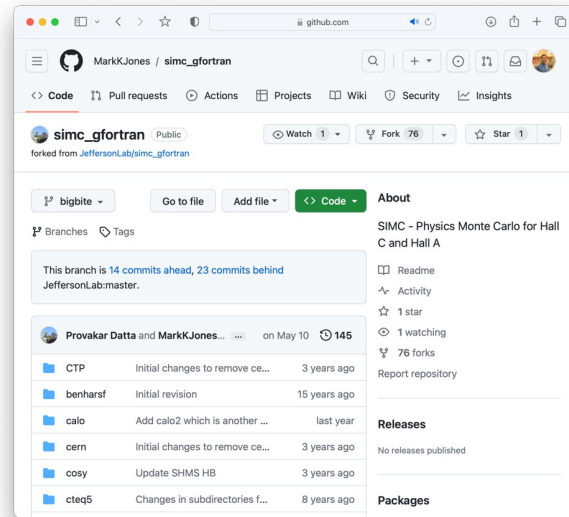


Realistic MC Event Generator for $G_M^n/nTPE$ Analysis

SIMC (simc_gfortran)
Standard Hall C MC framework for
coincidence experiments

G4SBS
Standard MC framework for SBS
experiments

- Realistic deuteron model.
- Radiative corrections for $(ee'p)$ reaction at energies suitable for $G_M^n/nTPE$. [2]
- MC event generation machinery for $H(ee'p)$ and $D(ee'p)$ processes.



- Realistic detector geometry built using GENAT4 for SBS spectrometers.

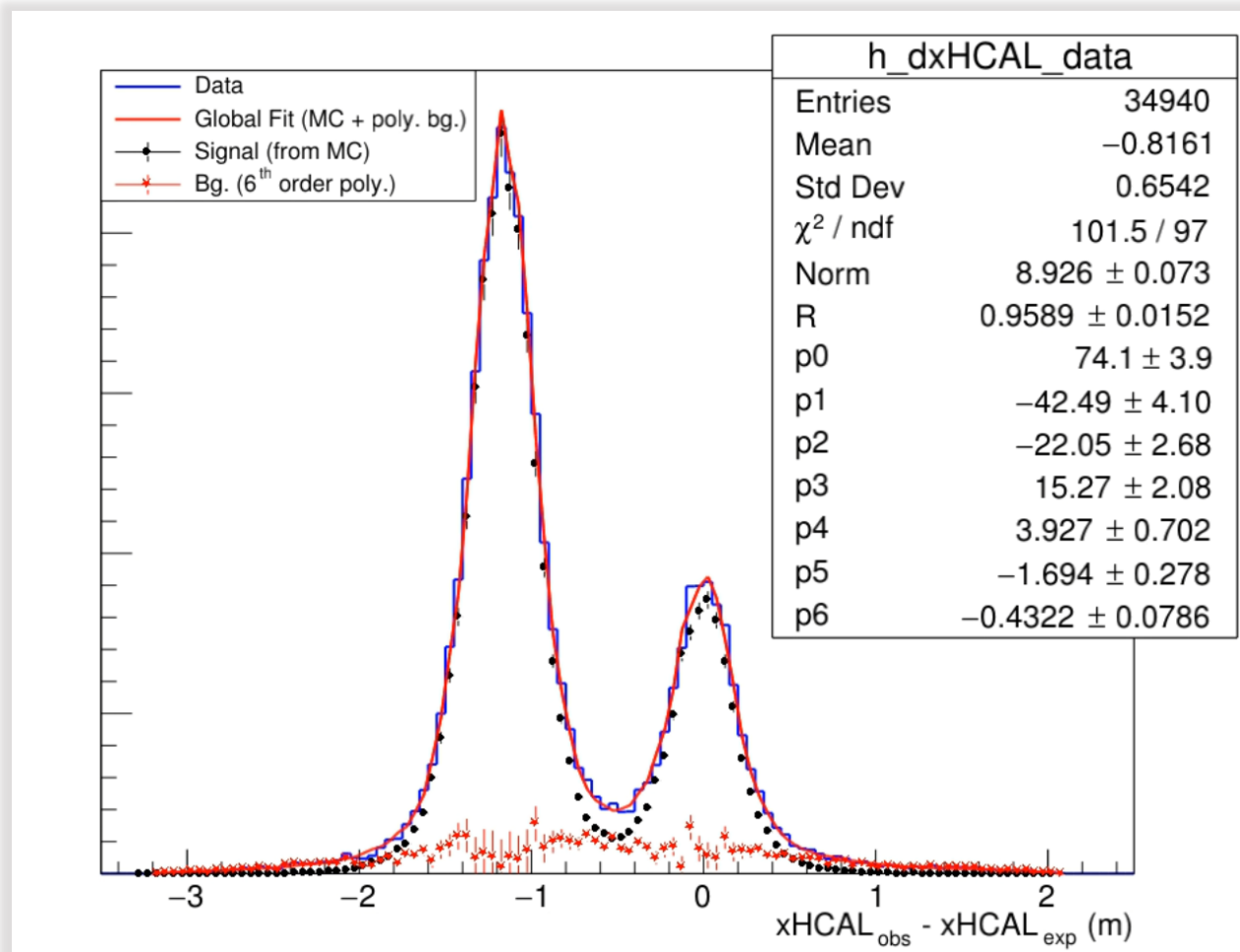
- ✓ Build box detectors in SIMC to mimic the acceptance of SBS spectrometers. (Mark Jones)
- ✓ Write an interface for G4SBS which enables is to interpret SIMC generated events. (Eric Fuchey)
- ✓ Upgrade SIMC to generate $D(ee'n)$ events. Generation of both $D(ee'p)$ and $D(ee'n)$ events are required for our analysis.
- ✓ Finally, upgrade and optimize the existing digitization and reconstruction machinery for realistic data/MC comparisons.

We now have realistic MC event generator available for $G_M^n/nTPE$ analysis!

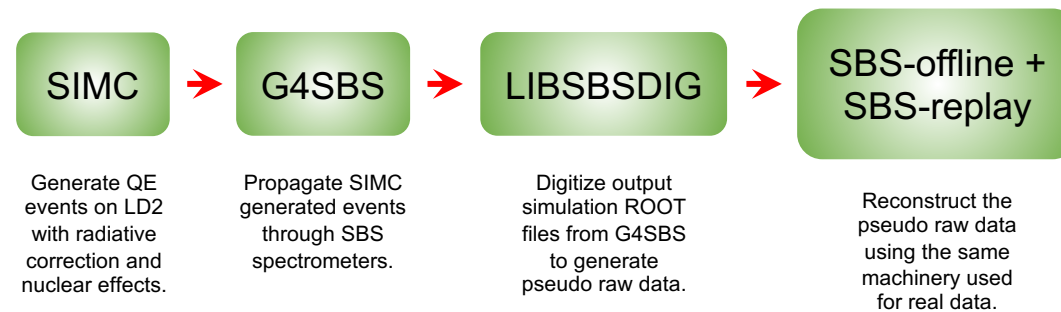
[2] R. Ent et al, Phys. Rev. C 64, 054610 (2001).

Preliminary Data vs MC for Δx Dist.: $Q^2 = 3 \text{ (GeV/c)}^2$ [SBS-4]

$Q^2 = 3 \text{ GeV}^2$, $0.49 \leq W^2 \leq 1.44 \text{ GeV}^2$, Fiducial Cuts



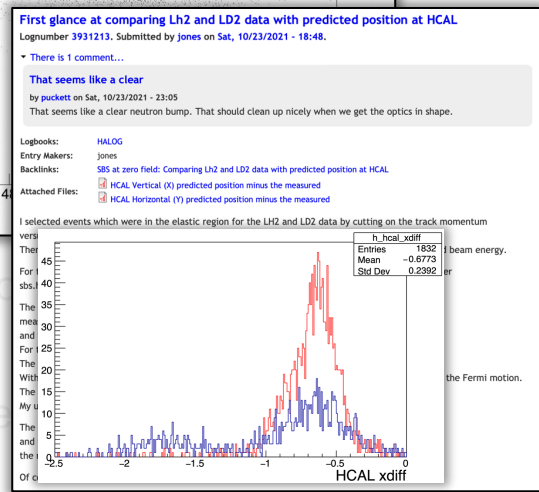
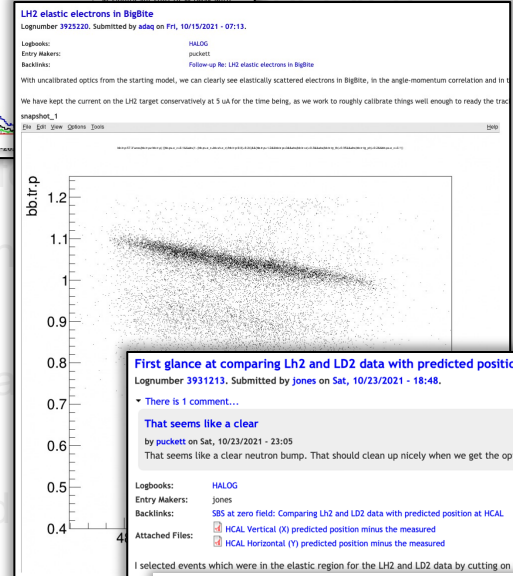
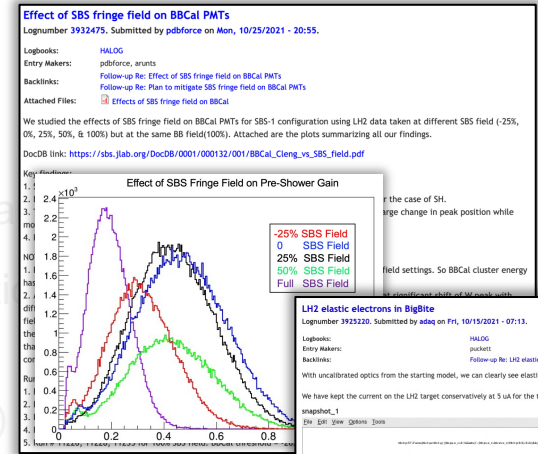
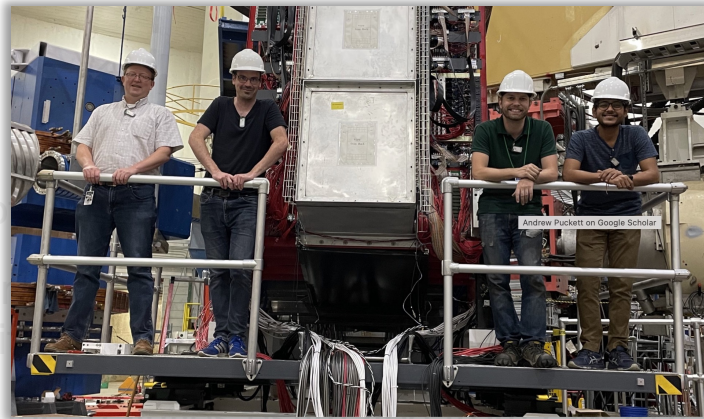
- Steps to generate realistic MC events:



- All the same cuts have been used for data and simulation analysis.
- Agreement of fit looks very promising with preliminary analysis. Further optimization and systematic studies are ongoing.

Summary and Acknowledgements

- The 1st pass cooking of entire SBS- G_M^n dataset was finished in January this year!
- A huge effort of data analysis is ongoing. Quasi-elastic event selection seems reasonably clean for even the highest Q^2 point with very basic cuts.
- Preliminary projected uncertainties estimated from raw $d(e, e'(p, n))$ counts show promising results. Precision of the highest Q^2 data point (13.5 GeV²) is expected to stay unmatched for years to come.
- Realistic MC event generator including radiative correction and nuclear effects is in place. Data/MC comparison looks very encouraging with preliminary analysis. Further optimization is ongoing.
- We are aiming to finish 2nd pass cooking within a month. Sophisticated physics analysis machinery is already in place, so will try to get preliminary results out soon after that.
- In parallel with analysis work, I have started writing my thesis. My plan is to defend by the end of this year.
- ❖ I would like to thank the entire Hall A collaboration and of course the SBS collaboration for letting me be a part of this program and write my thesis on the SBS- G_M^n experiment.
- ❖ I would also like to thank the US Department of Energy Office of Science, Office of Nuclear Physics, for supporting this work (Award ID DE-SC0021200).



Thank You for Your Attention!
 Questions? Comments?

- ❖ The 1st pass cooking of the beam was completed in January.
- ❖ A huge effort of data analysis is ongoing to select the highest Q² point with the highest Q² data point (13.5 GeV²) is expected to stay unmatched.
- ❖ Preliminary projected uncertainties estimated from raw $\alpha(e, e', p, n)$ event generator including radiative correction and nuclear effects is impressive. It is very encouraging with preliminary analysis. Further optimization to finish 2nd pass preliminary analysis in physics analysis so will try to get preliminary results earlier that.
- ❖ In my analysis work, I have started writing my thesis. My plan is to defend it in the next few months.
- ❖ I would like to thank the entire Hall A collaboration and of course the SBS collaboration for their part of this program.
- ❖ I would also like to thank the support staff for supporting this work.

Backup Slides

Kinematic of $SBS-G_M^n$

Table I: Kinematics of $SBS-G_M^n$

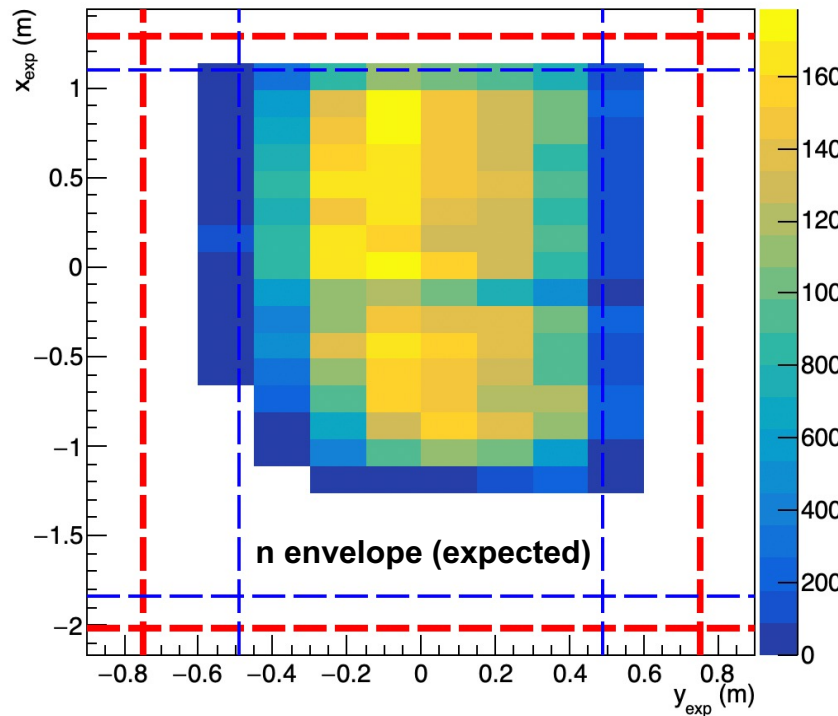
SBS Config.	Q^2 (GeV/c) ²	E_{beam} (GeV)	θ_{BB} (deg)	d_{BB} (m)	θ_{SBS} (deg)	d_{SBS} (m)	d_{HCAL} (m)
SBS-4	3.0	3.73	36.0	1.79	31.9	2.25	11.0
SBS-9	4.5	5.97	49.0	1.55	22.5	2.25	11.0
SBS-14	7.4	5.97	46.5	1.85	17.3	2.25	14.0
SBS-7	9.9	7.91	40.0	1.85	16.1	2.25	14.0
SBS-11	13.5	9.86	42.0	1.55	13.3	2.25	14.5

- Apart from G_M^n extraction, **SBS-9** data will also be used for Rosenbluth separation to shed some light on the TPE contribution in the elastic $e-n$ scattering.

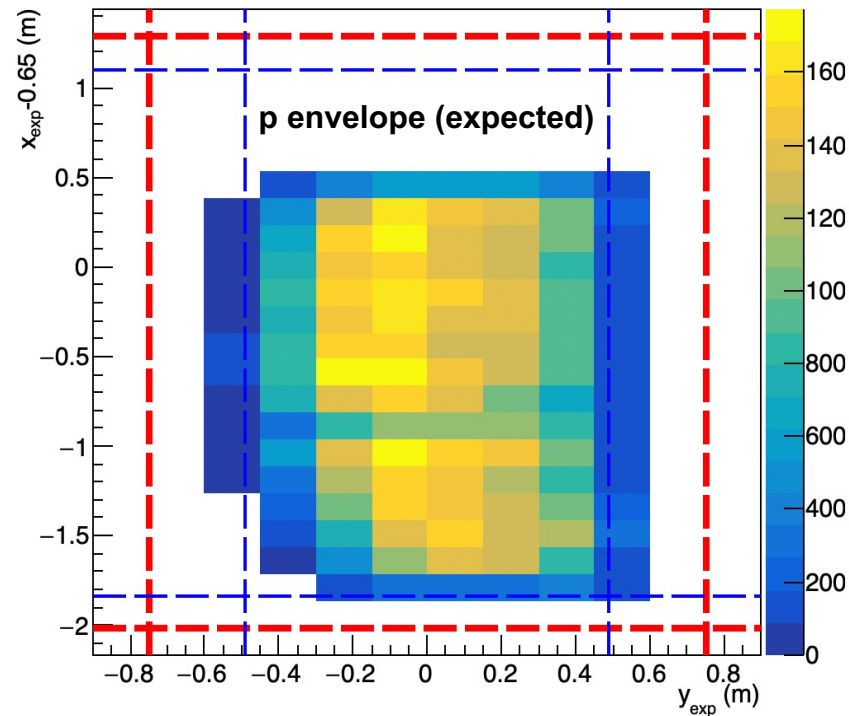
Implementation of Fiducial Cut on \vec{q}

$$Q^2 = 3 \text{ (GeV/c)}^2$$

$|W^2 - 0.88| < 0.5$ & Fiducial Cuts



$|W^2 - 0.88| < 0.5$ & Fiducial Cuts

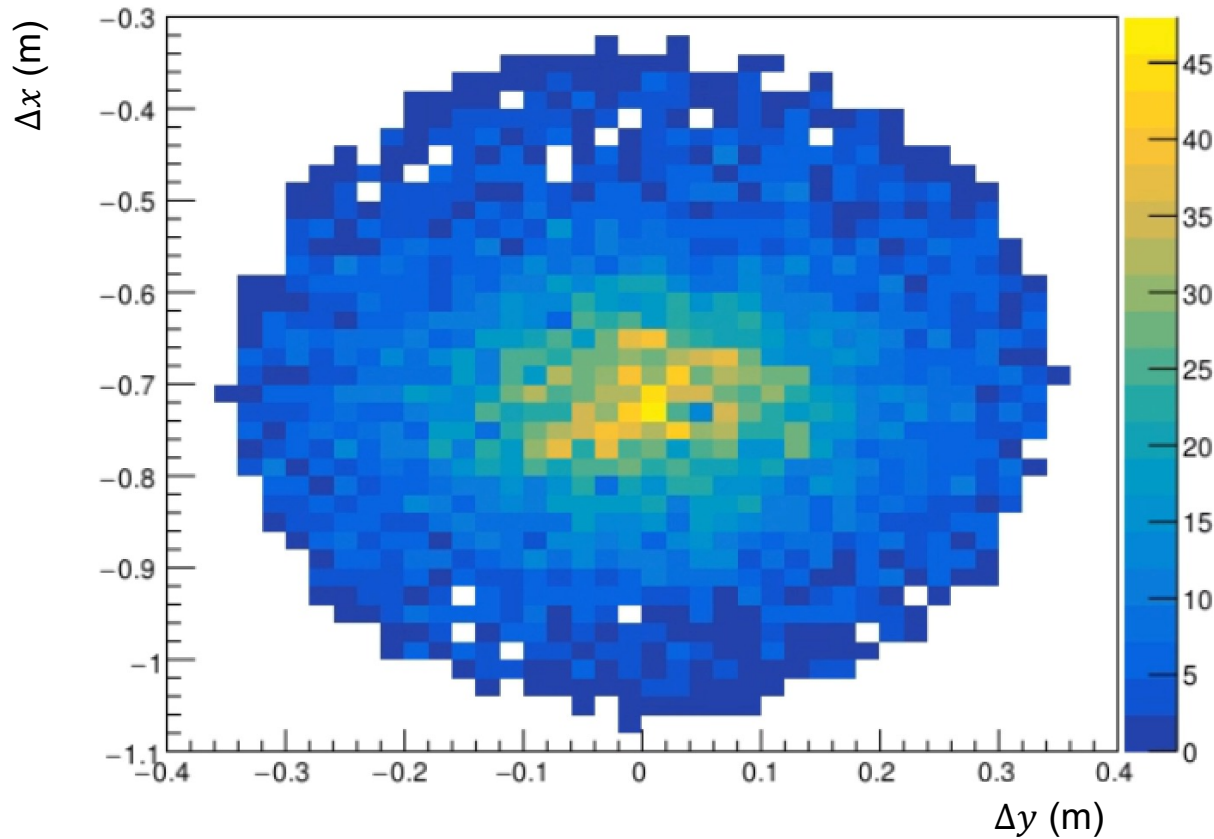


--- Top of HCAL ---

- The idea is to accept a n (p) event only if a p (n) event with equivalent kinematics would also be guaranteed to hit the active area of HCAL.
- The fiducial cut is only based on the scattered-electron angle and momentum measured by BigBite.
- As “active area” (red dashed lines) we consider entire HCAL excluding the outermost rows and columns.
- We also use an additional “safety margin” (blue dashed lines) based on the widths of the Δx & Δy distributions for p & n to encounter the effects of Fermi motion to some extent.

Visualizing θ_{pq} Cuts: $Q^2 = 9.9 \text{ (GeV/c)}^2$ [SBS-7]

p coincidence



n coincidence

