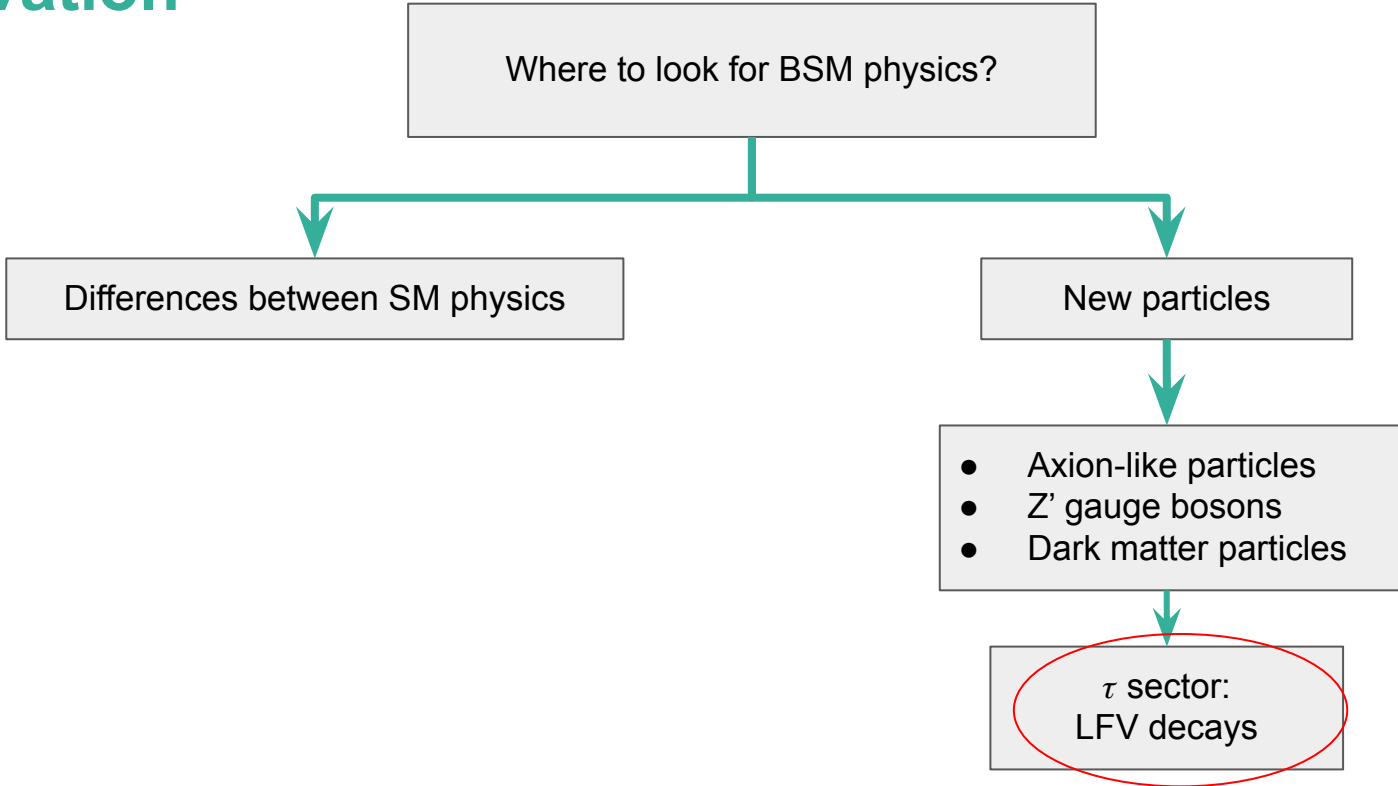


# Exploring invisible particles: In a search of “Beyond Standard Model” in $\tau$ decays

Johan A. Colorado Caicedo  
In collaboration with  
Eduard De La Cruz Burelo

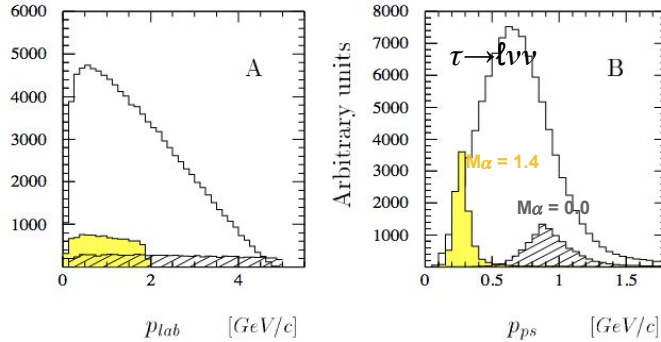


# Motivation



# How to look for BSM physics?

## ARGUS



[Z. Phys. C 68, 25-28 \(1995\)](#)

as signal (1 prong):  $\tau \rightarrow l \alpha$     as tag (3 prong):  $\tau \rightarrow (3h)\nu$  or  $\tau \rightarrow (3h)\pi^0\nu$

- pseudo-rest frame distribution.

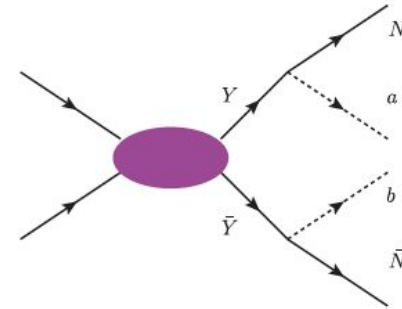
Issue:

Overlap in the kinematic region with background distribution: **low discriminant power**

Approximate the boost direction: **smearing effect**

[Phys. Rev. D 90, 114029](#)

[Phys. Rev. D 95, 075037](#)



$$Y\tilde{Y} \rightarrow (a+N)(b+\tilde{N})$$

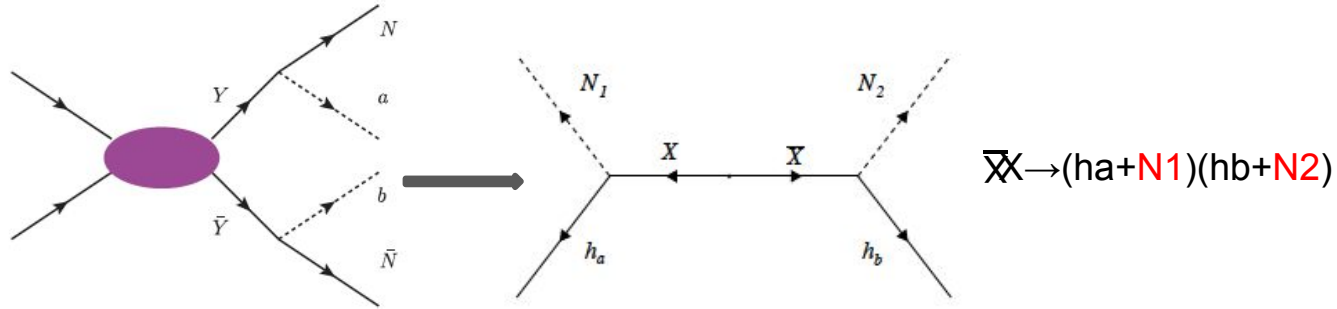
Suitable for leptonic colliders

Issue:

It is necessary  $Y\tilde{Y}$  pairs, only one detectable particle in each side and one invisible particle also: **a large data sample to be able to perform a sensitivity study**

[johan.colorado@cinvestav.mx](mailto:johan.colorado@cinvestav.mx)

# Our method



$h_a, h_b$ : could be a bunch of detectable particles

$N_1, N_2$ : couple of particles that evade the detector

[Phys. Rev. D 102, 115001](#)

This generalization allows to study  $XX$  pair decays with BSM processes in one decay, and SM processes with missing particle in the complementary decay (such as the  $\tau$  lepton decays).

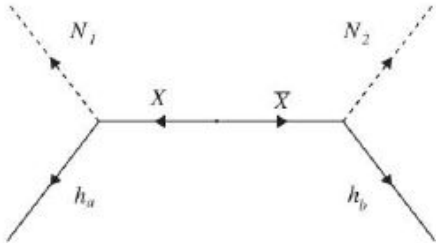
This could be to increase the possibility of a BSM particle production compared with the requirement of a double creation of the unknown particle.

[johan.colorado@cinvestav.mx](mailto:johan.colorado@cinvestav.mx)



# Kinematic constraints

$$X \bar{X} \rightarrow (h_a + N_1)(h_b + N_2)$$



At CMS energy  $\sqrt{s}$

$$p_a = (E_a, \vec{p}_a)$$

$$p_b = (E_b, \vec{p}_b)$$

$$p_1 = (E_1, \vec{p}_1)$$

$$p_2 = (E_2, \vec{p}_2)$$

The kinematic equations:

$$q^\mu = p_a^\mu + p_b^\mu + p_1^\mu + p_2^\mu, \quad \mu = 0, 1, 2, 3$$

$$p_{1,2}^2 = m_{1,2}^2$$

$$(p_a + p_1)^2 = (p_b + p_2)^2 = m_X^2$$

After some algebra:

$$\begin{aligned} & A_1(\mu_X^2 - \mu_1^2)^2 + A_2(\mu_X^2 - \mu_2^2)^2 \\ & + A_3(\mu_X^2 - \mu_1^2)(\mu_X^2 - \mu_2^2) \\ & + B_1(\mu_X^2 - \mu_1^2) + B_2(\mu_X^2 - \mu_2^2) \\ & + C_1\mu_1^2 + D_1 \leq 0 \end{aligned}$$

$\mu_i$  is the normalized mass of the  $i$ -th particle.

$$A_1 = |\mathbf{b}|^2,$$

$$A_2 = |\mathbf{a}|^2,$$

$$A_3 = 2(\mathbf{a} \cdot \mathbf{b}),$$

$$B_1 = 2(\mathbf{b} \cdot \mathbf{H}),$$

$$B_2 = 2(\mathbf{a} \cdot \mathbf{H}),$$

$$C_1 = 4|\mathbf{a} \times \mathbf{b}|^2,$$

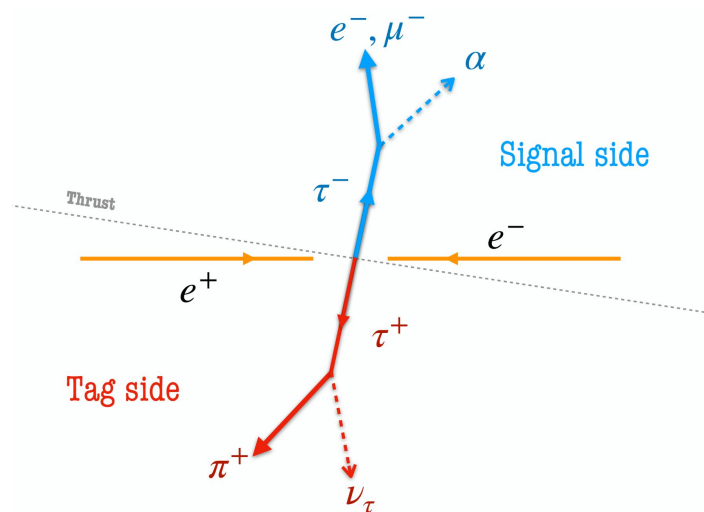
$$D_1 = \mathbf{H} \cdot \mathbf{H} - 4|\mathbf{a} \times \mathbf{b}|^2 \left( \frac{1}{2} - z_a \right)^2.$$

$$\mathbf{H} \equiv (z_b^2 - z_b - |\mathbf{b}|^2 - 2\mathbf{a} \cdot \mathbf{b})\mathbf{a} + (z_a^2 - z_a + |\mathbf{a}|^2)\mathbf{b}.$$

We summarized all the available kinematic information of the process

# Our case

- **Signal side:**  $\tau$  decay into  $\ell$ +invisible
  - **Tag side:**  $\tau$  decay into  $\pi$ +invisible
- The Branching of 1x1-prong is significant  
→ ( $\mathcal{B}(\tau \rightarrow \pi\nu) \sim 10.8$  and  $\mathcal{B}(\tau \rightarrow e\nu\nu) \sim 17.8$ )



# Mmin and Mmax variables

Discriminant variables

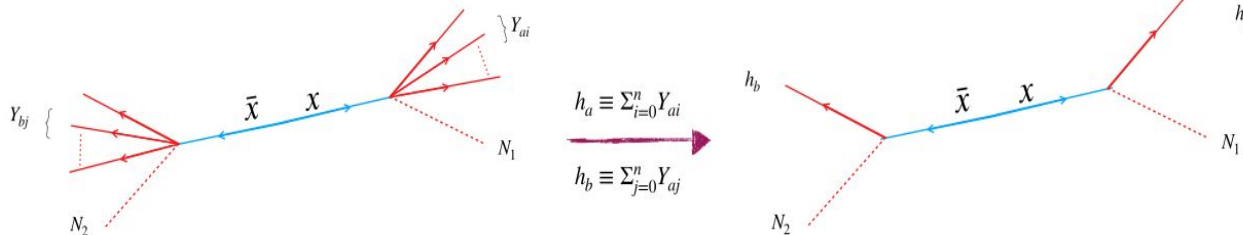
$$M_{min}^2 = (\sqrt{s})^2 \left( \frac{-B_0 - \sqrt{B_0^2 - 4A_0D_0}}{2A_0} \right),$$

$$M_{max}^2 = (\sqrt{s})^2 \left( \frac{-B_0 + \sqrt{B_0^2 - 4A_0D_0}}{2A_0} \right).$$

$$A_0 = A_1,$$

$$B_0 = -B_1 + C_1 - (2A_1 + A_3)\mu_\tau^2,$$

$$C_0 = (A_1 + A_2 + A_3)\mu_\tau^4 + (B_1 + B_2)\mu_\tau^2 + D_1.$$



“Measuring masses in semi-invisible final states at electron-positron colliders”

Qian-Fei Xiang, Xiao-Jun Bi, Qi-Shu Yan, Peng-Fei Yin, and Zhao-Huan Yu

[PhysRevD.95.075037](https://arxiv.org/abs/hep-th/0505187)

“New method for beyond the Standard Model invisible particle searches in tau lepton decays”

E. De La Cruz-Burelo, A. De Yta-Hernandez, and M. Hernandez-Villanueva

[Phys. Rev. D 102, 115001](https://arxiv.org/abs/1905.07501)

“Measurement of the mass of the tau lepton in semi-invisible final states in the Belle II collaboration”

J. A. Colorado-Caicedo

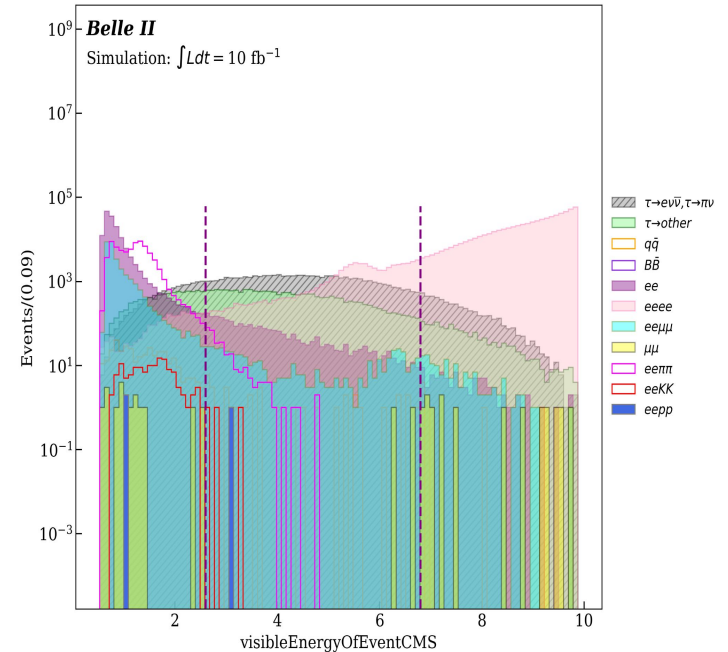
[BELLE2-MTHESIS-2023-007](https://arxiv.org/abs/2303.007)

johan.colorado@cinvestav.mx

# Cleaning the signal zone

Optimizing with the SM irreducible background ( $\tau \rightarrow \ell \nu \mathbf{v}$ ) using a purity FOM in a simulated annealing algorithm.

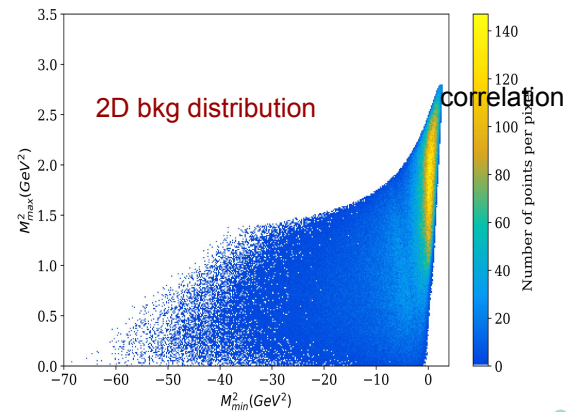
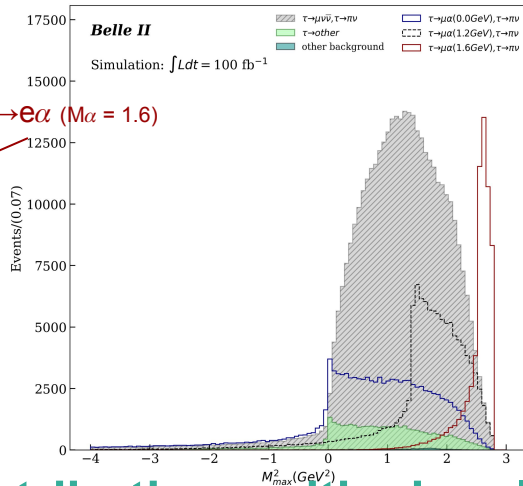
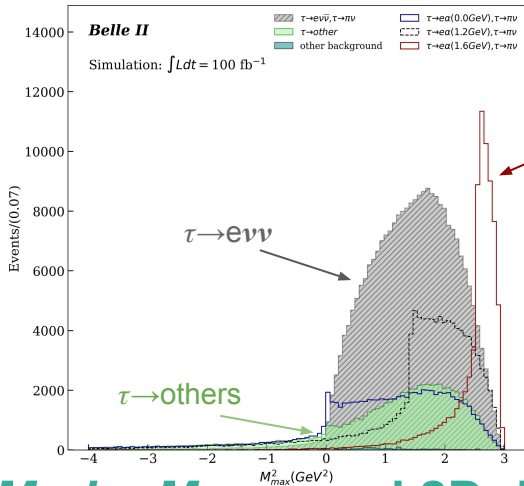
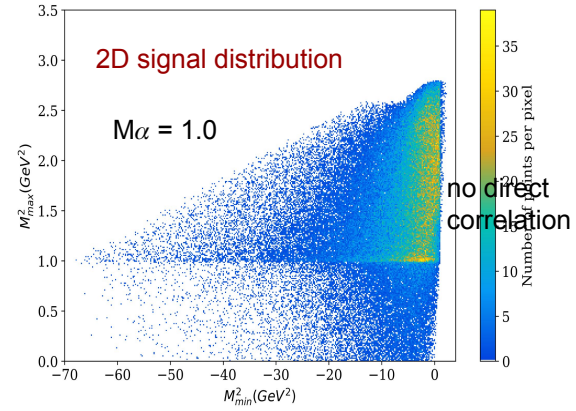
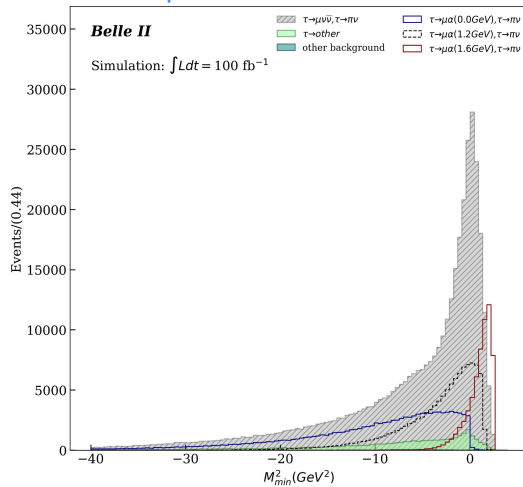
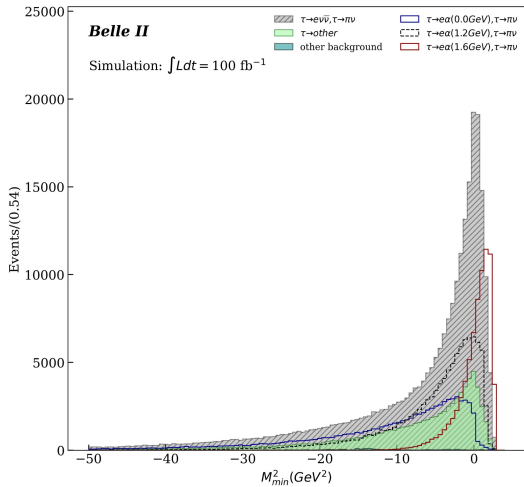
$$\frac{N_{sig}}{\sqrt{N_{sig} + 100(N_{bkg})}} \longrightarrow \text{Purity-focused optimization}^*$$



\* Another optimization with FOM =  $S/(S+B)^{(1/2)}$  was made, we stayed with the better performance

e-channel

$\mu$ -channel



# Mmin, Mmax and 2D distributions with signal component

joan.colorado@cinvestav.mx



# Upper Limit Estimation

We used the following PDF

$$F(x) = \frac{\epsilon_\alpha}{\epsilon_{l\nu\nu}} \times R \times f_\alpha(x) + N_{SM} \times f_{SM}(x) + N_{bkg} \times f_{bkg}(x)$$

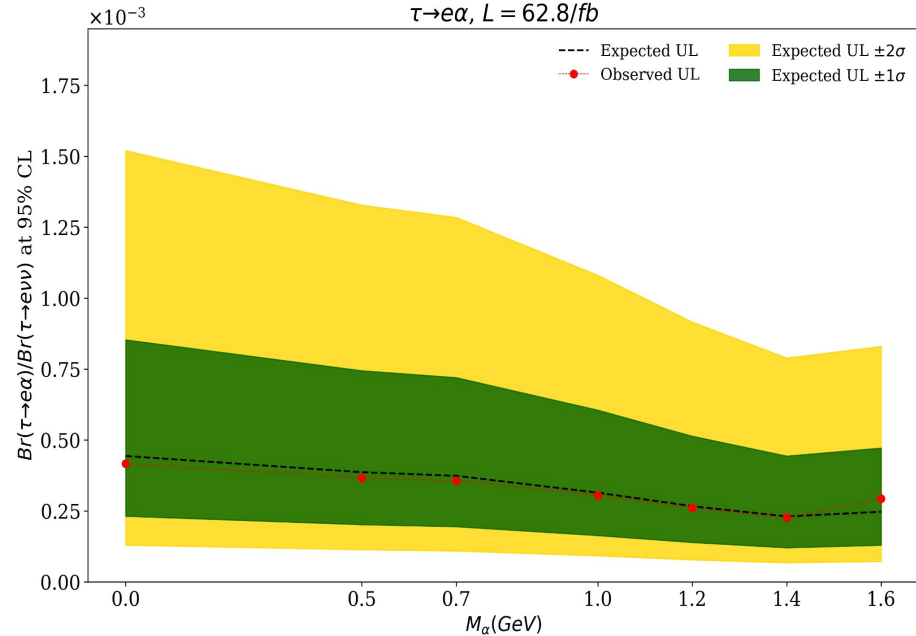
where  $R \equiv \frac{Br(\tau \rightarrow l\alpha)}{Br(\tau \rightarrow l\nu\nu)} = \frac{\epsilon_{SM}}{\epsilon_\alpha} \frac{N_\alpha}{N_{SM}}$ ,  $N_{bkg} = N_{\tau bkg} + N_{other}$  and  $f_{bkg}(x)$  is constructed with the histogram of the remaining tau decays and the background remaining (qqbar, lowmulti, etc.). And we determined upper limits with the asymptotic CLs technique, implemented in the RooStats package.

# UL estimation with the purity cuts

UL with 2D method to different  $\alpha$  masses - 62.8/fb

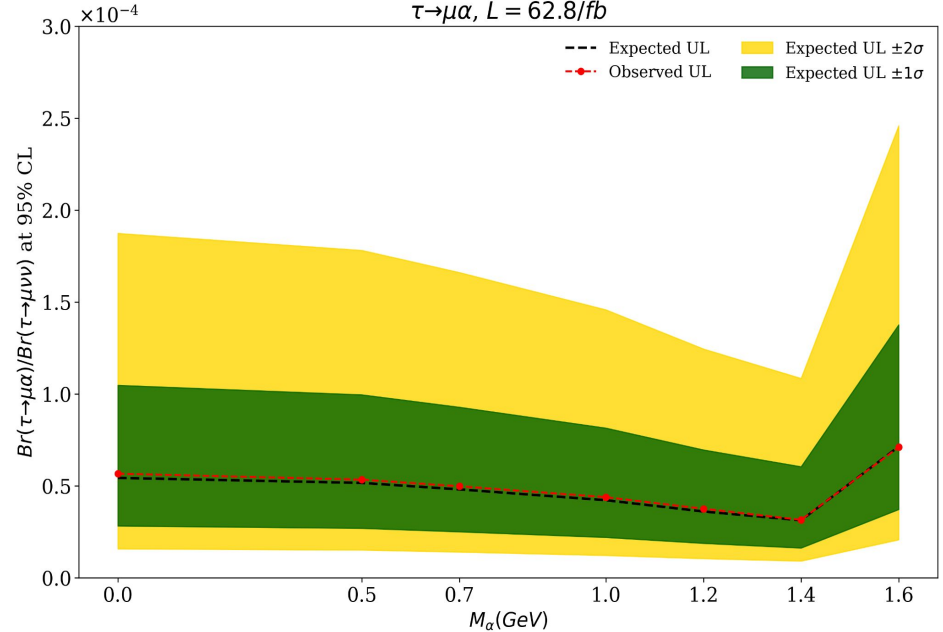
*e-channel*

$\tau \rightarrow e\alpha$ ,  $L = 62.8/\text{fb}$



*$\mu$ -channel*

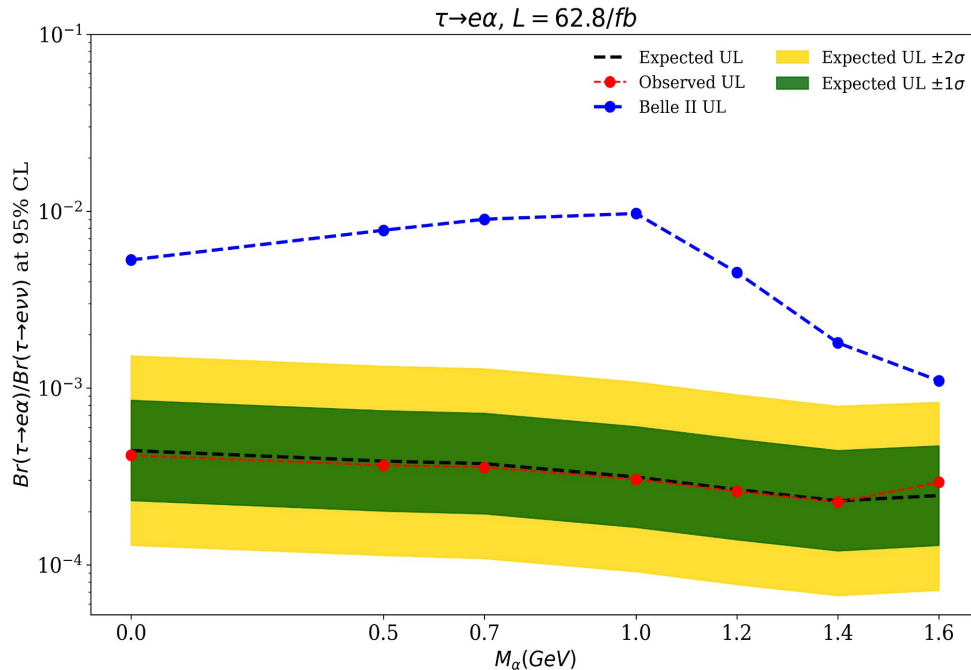
$\tau \rightarrow \mu\alpha$ ,  $L = 62.8/\text{fb}$



johan.colorado@cinvestav.mx

# UL estimation with the purity cuts (e-channel)

## Comparison with previous study - 62.8/fb



Central values at 95% CL, upper limits for the branching-fraction ratios  $\mathcal{B}_{e\alpha}/\mathcal{B}_{e\nu\nu}$  for various masses of  $\alpha$  boson

$M_\alpha$ [GeV/ $c^2$ ]	UL at 95% CL* ( $\times 10^{-3}$ )	UL at 95% CL* ( $\times 10^{-3}$ )
0.0	5.30	0.416
0.5	7.80	0.366
0.7	9.00	0.356
1.0	9.70	0.305
1.2	4.50	0.260
1.4	1.80	0.226
1.6	1.10	0.293

\*[Phys. Rev. Lett. 130, 181803](#)

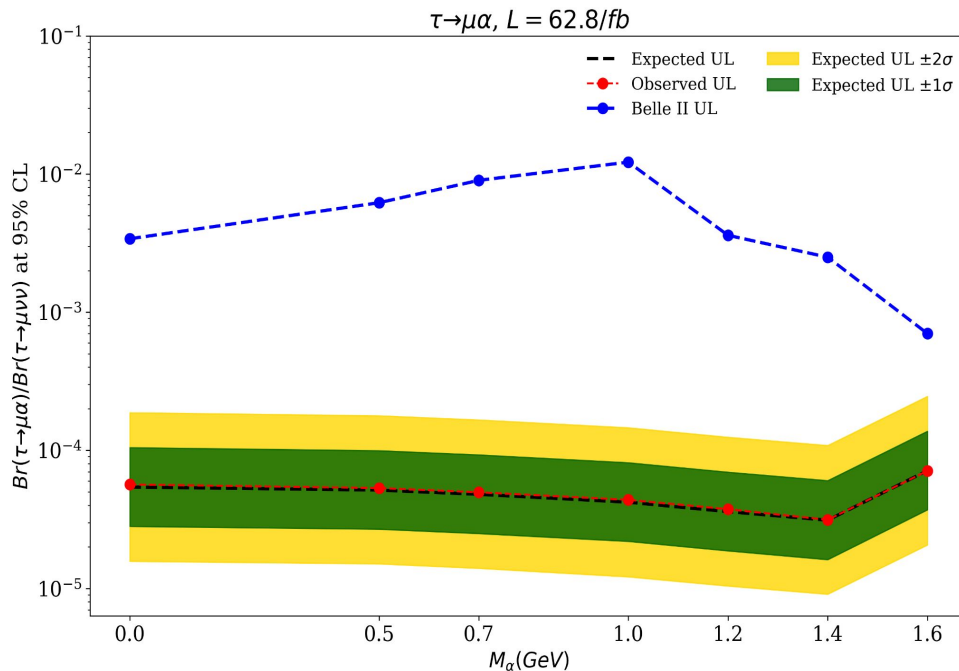
\*UL's found by us using 2D method

[johan.colorado@cinvestav.mx](mailto:johan.colorado@cinvestav.mx)



# UL estimation with the purity cuts ( $\mu$ -channel)

## Comparison with previous study - 62.8/fb



Central values at 95% CL, upper limits for the branching-fraction ratios  $\mathcal{B}_{\mu\alpha} / \mathcal{B}_{\mu\nu\nu}$  for various masses of  $\alpha$  boson

$M_\alpha$ [GeV/ $c^2$ ]	UL at 95% CL ( $\times 10^{-3}$ )	UL at 95% CL* ( $\times 10^{-3}$ )
0.0	3.40	0.057
0.5	6.20	0.053
0.7	9.00	0.050
1.0	1.22	0.044
1.2	3.60	0.037
1.4	2.50	0.031
1.6	0.70	0.071

\*[Phys. Rev. Lett. 130, 181803](#)

\*UL's found by us using 2D method

johan.colorado@cinvestav.mx



# In summary

- In the recent Belle II paper for 3x1-prong topology it was achieved upper limits on the branching-ratio fraction  $\mathcal{B}(\tau \rightarrow e\alpha)/\mathcal{B}(\tau \rightarrow e\nu\bar{\nu})$  ranging in  $(1.1 - 9.7) \times 10^{-3}$  and on  $\mathcal{B}(\tau \rightarrow \mu\alpha)/\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})$  in the range  $(0.7 - 12.2) \times 10^{-3}$  at 95% CL. CLs limits are 2.2 to 14 times more stringent than ARGUS collaboration
- Our MC estimations (without systematics) in the 1x1-prong topology for 62.8/fb are  $(2.26 - 4.16) \times 10^{-4}$  and  $(3.1 - 7.1) \times 10^{-5}$  for the electron and the muon channel respectively. Our limits are **4.9 to 23.3** and **22.6 to 171.8** times more stringent than the previous Belle II study.
- At this level these two different estimations could be in the worst worst case (including systematics) at least comparables and they could be combined to estimate a better upper limit.

**¡Muchas gracias!**

*johan.colorado@cinvestav.mx*

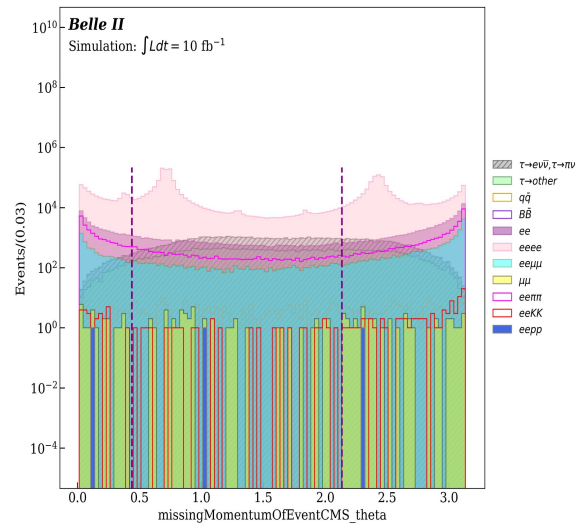
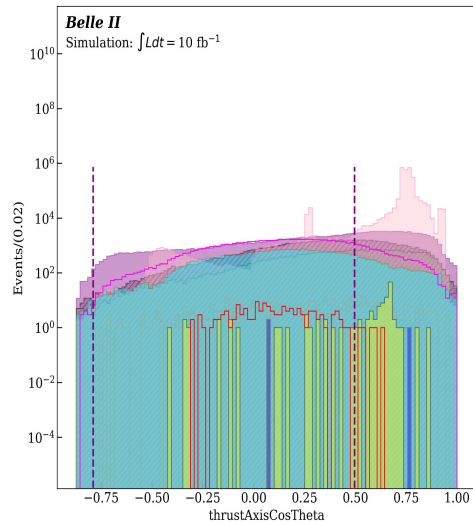
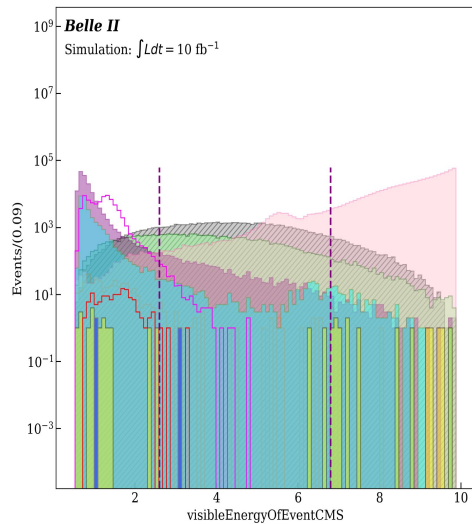


# Back up

*johan.colorado@cinvestav.mx*



# Selection cuts (e-channel)



Luminosity: 10/fb:100/fb

(Sample  $\rightarrow$  Events)

SM  $\rightarrow$  66818

tau  $\rightarrow$  28932

qqbar  $\rightarrow$  403

mixed+charged  $\rightarrow$  1

ee  $\rightarrow$  2745305

eeee  $\rightarrow$  148972

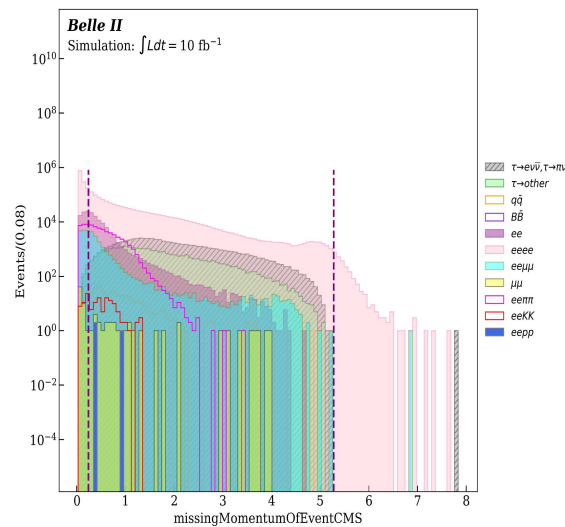
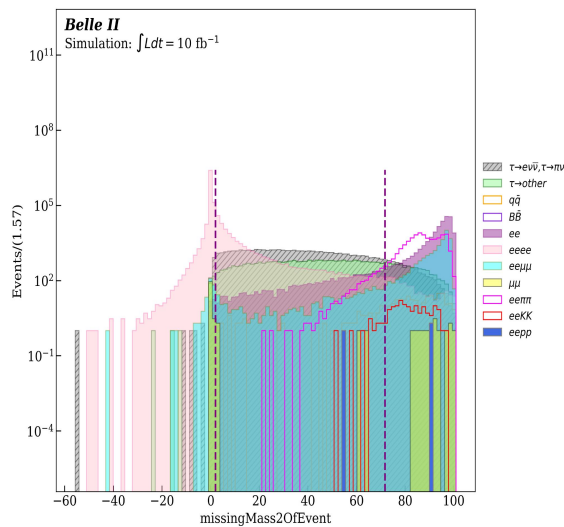
eemumu  $\rightarrow$  29429

mumu  $\rightarrow$  114

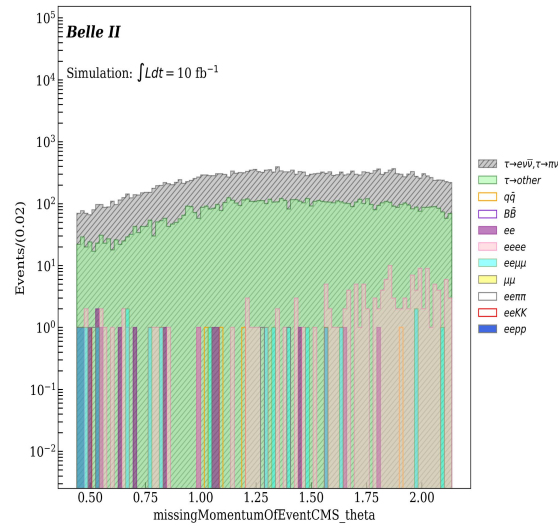
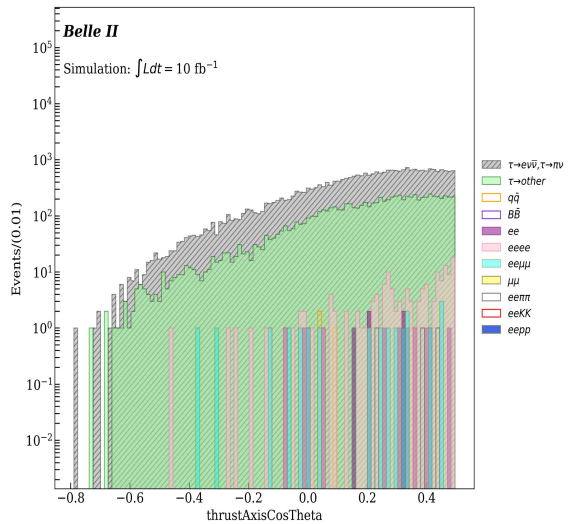
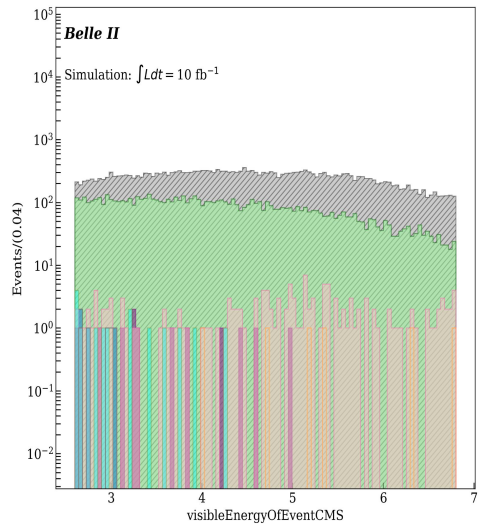
eeppi  $\rightarrow$  73360

eeKK  $\rightarrow$  134

eepp  $\rightarrow$  3



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Luminosity: 10/fb:100/fb

(Sample  $\rightarrow$  Remaining Events)

SM  $\rightarrow$  25186

tau  $\rightarrow$  7418

qqbar  $\rightarrow$  8

mixed+charged  $\rightarrow$  0

ee  $\rightarrow$  99

eeee  $\rightarrow$  26

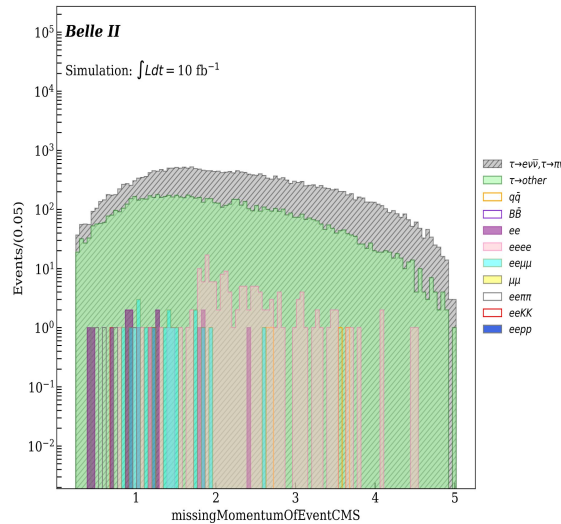
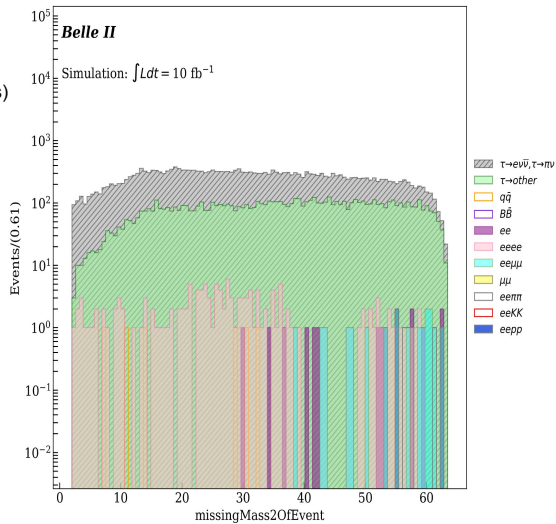
eemumu  $\rightarrow$  26

mumu  $\rightarrow$  0

eeppi  $\rightarrow$  4

eeKK  $\rightarrow$  0

eepp  $\rightarrow$  0

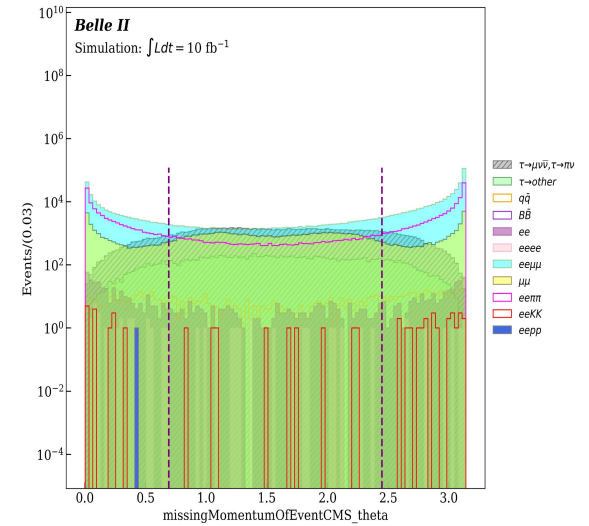
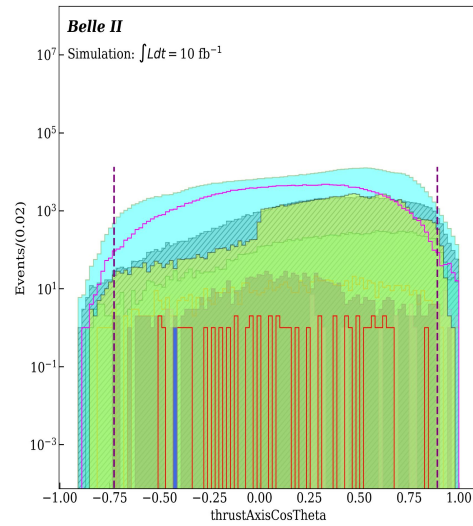
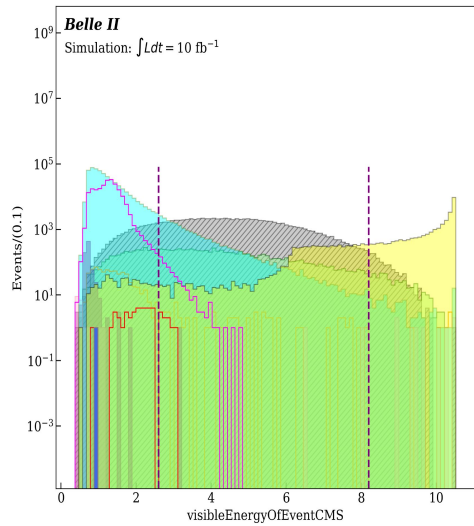


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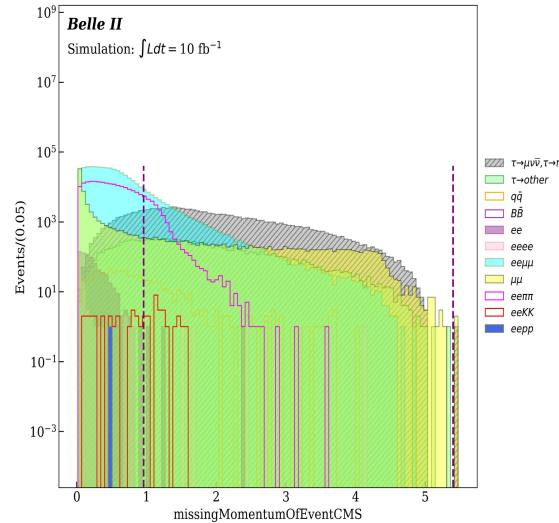
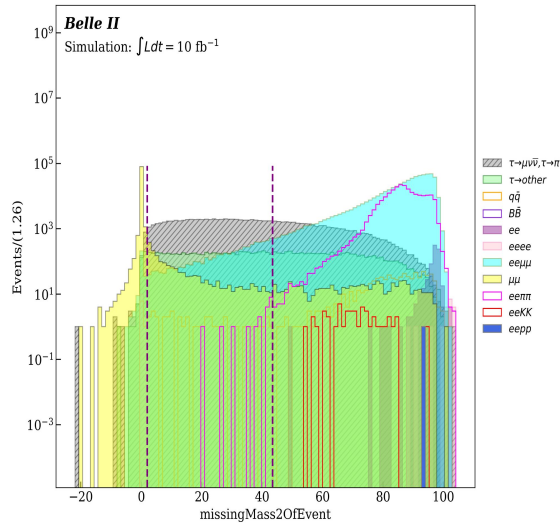
# Selection cuts ( $\mu$ -channel)



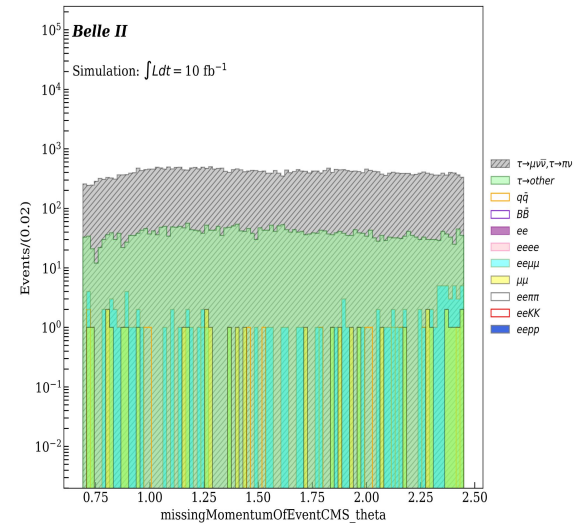
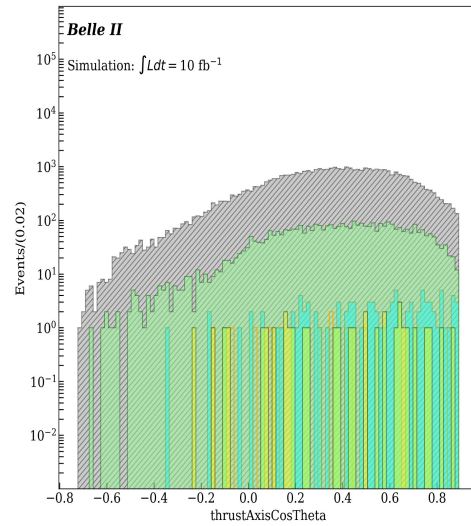
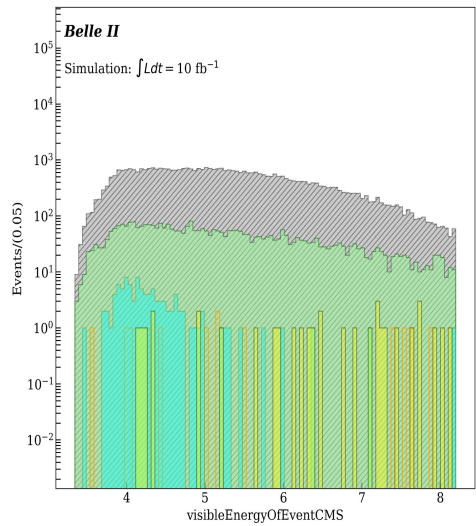


Luminosity: 10/fb:100/fb

(Sample  $\rightarrow$  Events)  
 SM  $\rightarrow$  95772  
 tau  $\rightarrow$  12012  
 qqbar  $\rightarrow$  761  
 mixed+charged  $\rightarrow$  0  
 ee  $\rightarrow$  49  
 eeee  $\rightarrow$  734  
 eemumu  $\rightarrow$  556163  
 mumu  $\rightarrow$  84246  
 eepipi  $\rightarrow$  217331  
 eeKK  $\rightarrow$  47  
 eepp  $\rightarrow$  1



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Luminosity: 10/fb:100/fb

(Sample  $\rightarrow$  Remaining Events)

SM  $\rightarrow$  38380

tau  $\rightarrow$  3269

qqbar  $\rightarrow$  14

mixed+charged  $\rightarrow$  0

ee  $\rightarrow$  0

eeee  $\rightarrow$  0

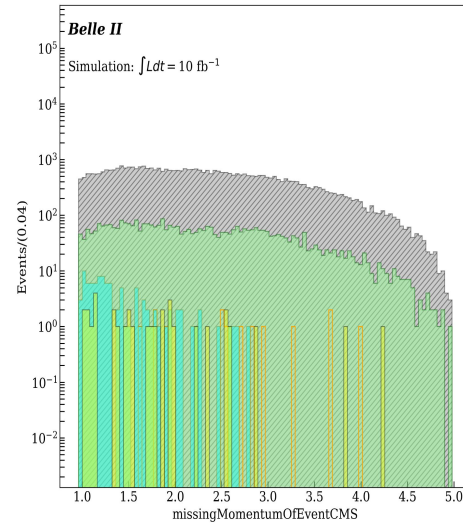
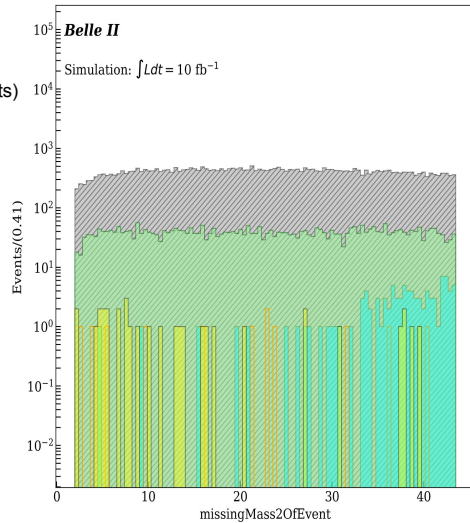
eemumu  $\rightarrow$  82

mumu  $\rightarrow$  27

eeppi  $\rightarrow$  4

eeKK  $\rightarrow$  0

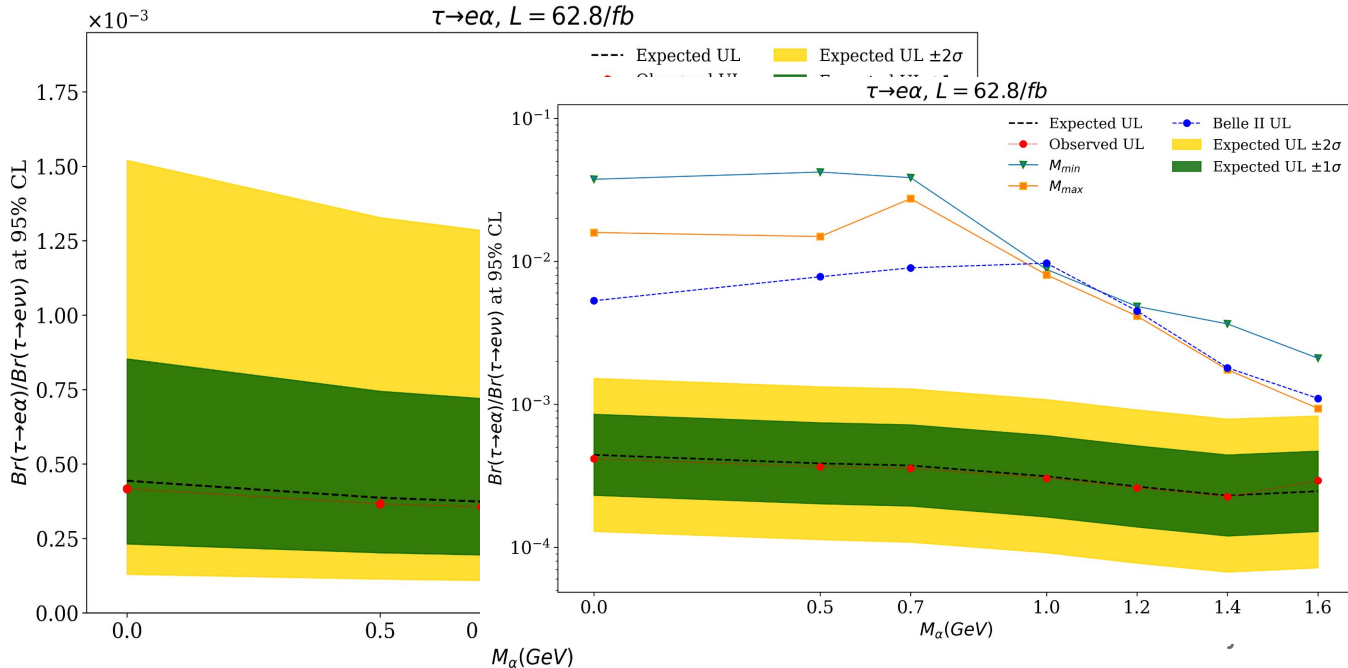
eepp  $\rightarrow$  0



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# UL estimation with the purity cuts (e-channel)

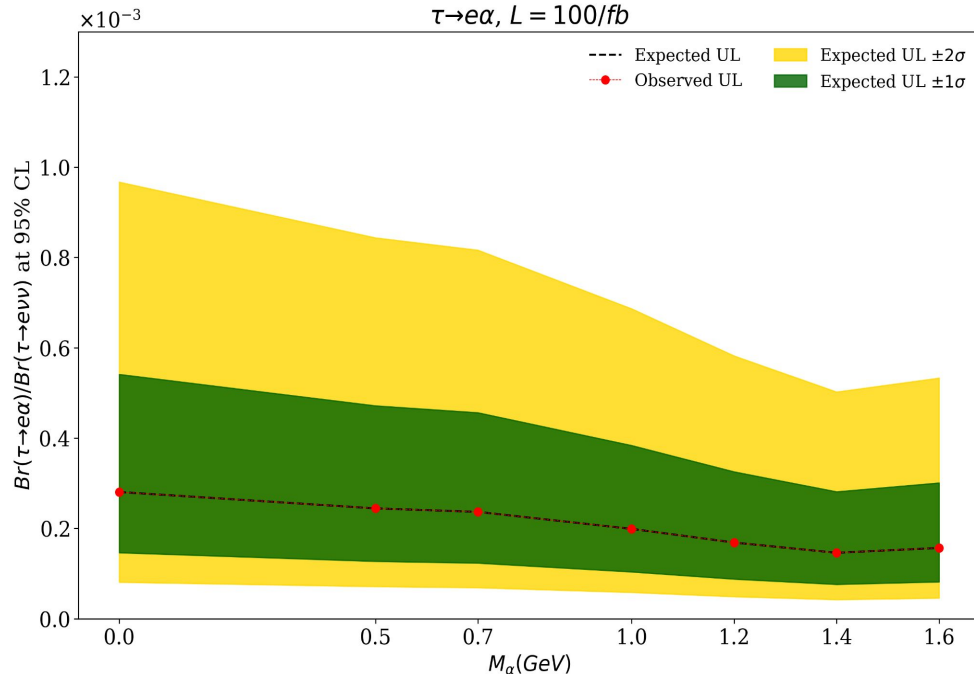
## UL with 2D method to different $\alpha$ masses - 62.8/fb



1D methods comparison, we can see a better agreement in large masses

# UL estimation with the purity cuts (e-channel)

## UL with 2D method to different $\alpha$ masses - 100/fb



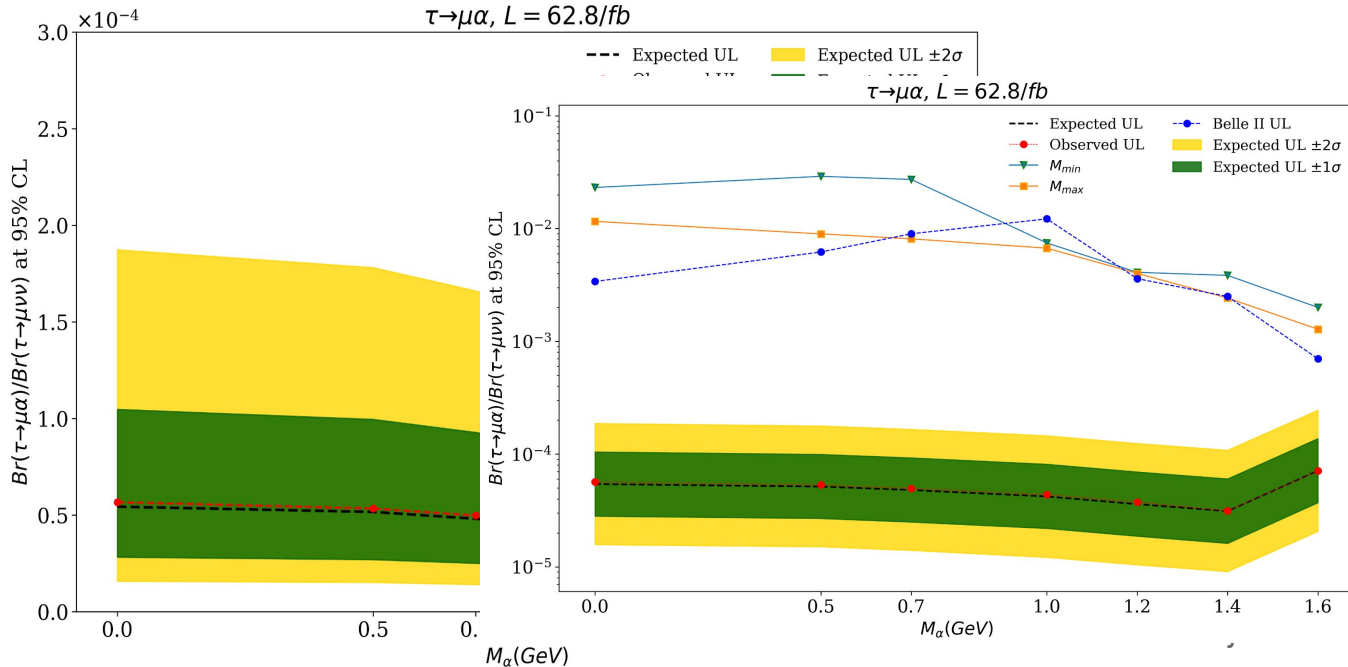
$M_\alpha$ [GeV/ $c^2$ ]	UL at 95% CL ( $\times 10^{-4}$ )
0.0	2.80
0.5	2.44
0.7	2.36
1.0	1.99
1.2	1.69
1.4	1.46
1.6	1.57

UL's found by us using 2D  
method

[johan.colorado@cinvestav.mx](mailto:johan.colorado@cinvestav.mx)

# UL estimation with the purity cuts ( $\mu$ -channel)

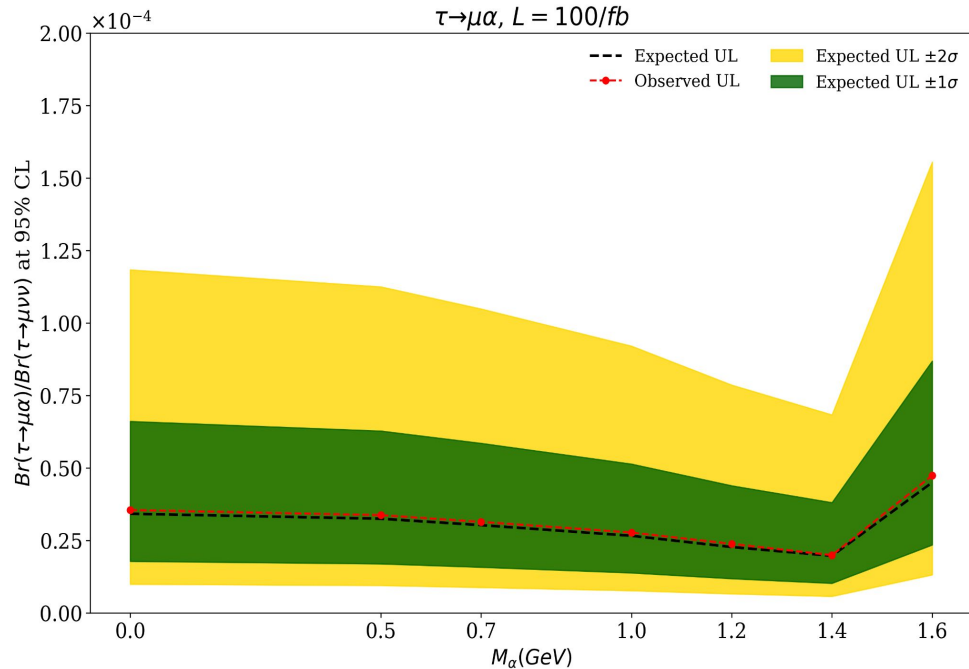
## UL with 2D method to different $\alpha$ masses - 62.8/fb



1D methods comparison, we can see a better agreement in large masses

# UL estimation with the purity cuts ( $\mu$ -channel)

## UL with 2D method to different $\alpha$ masses - 100/fb

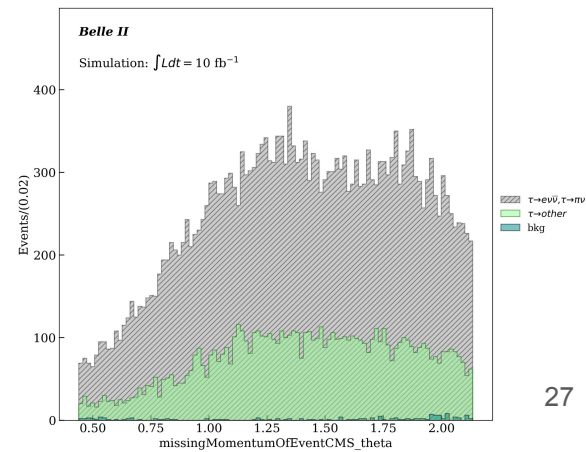
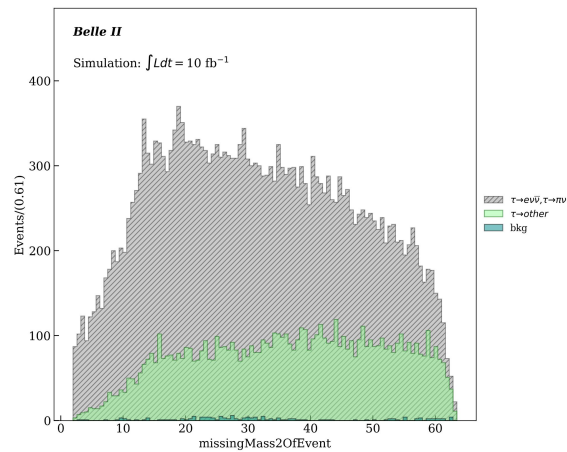
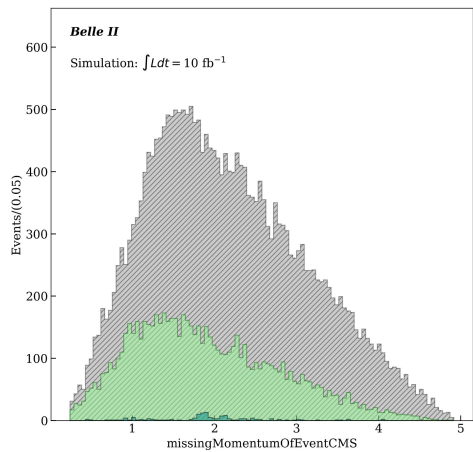
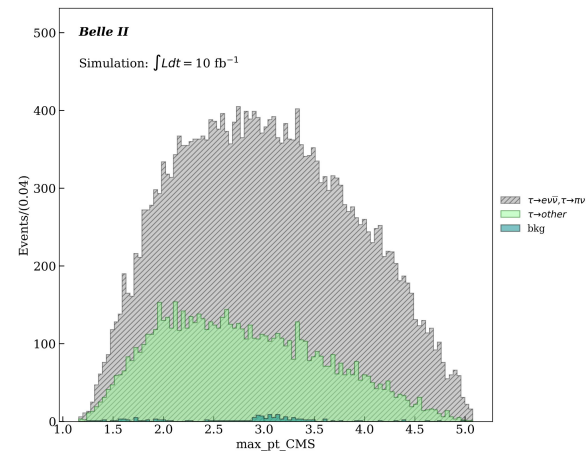
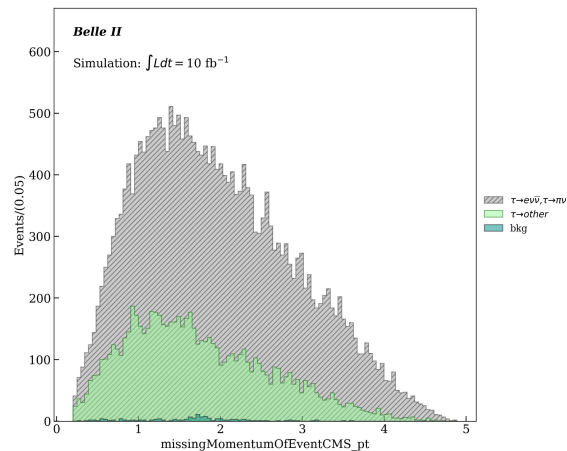
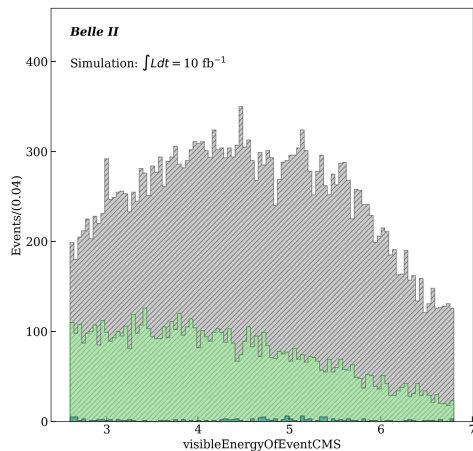


$M_\alpha$ [GeV/ $c^2$ ]	UL at 95% CL ( $\times 10^{-5}$ )
0.0	3.50
0.5	3.40
0.7	3.10
1.0	2.80
1.2	2.40
1.4	2.00
1.6	4.70

UL's found by us using 2D method

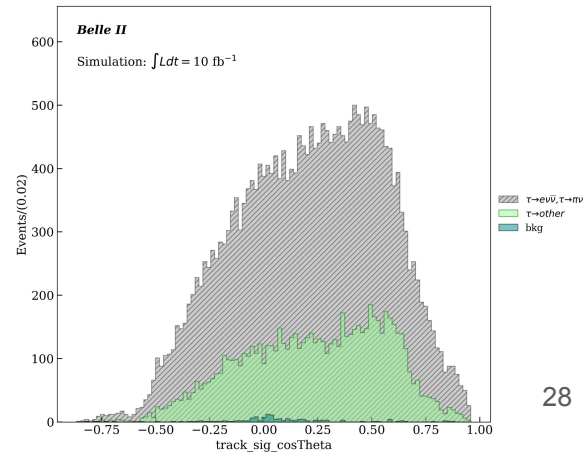
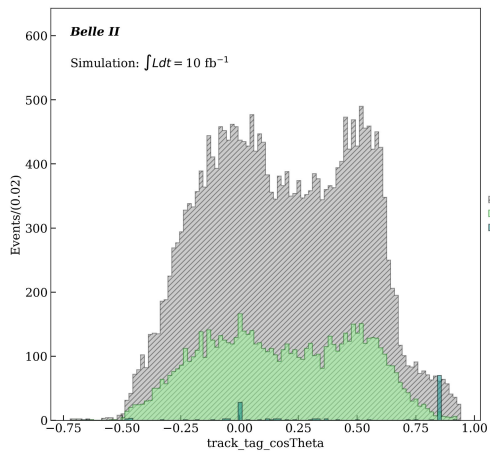
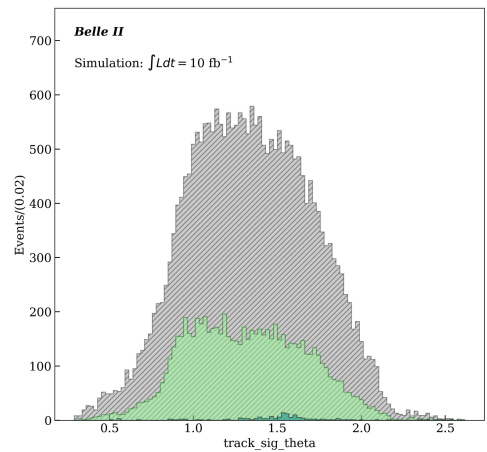
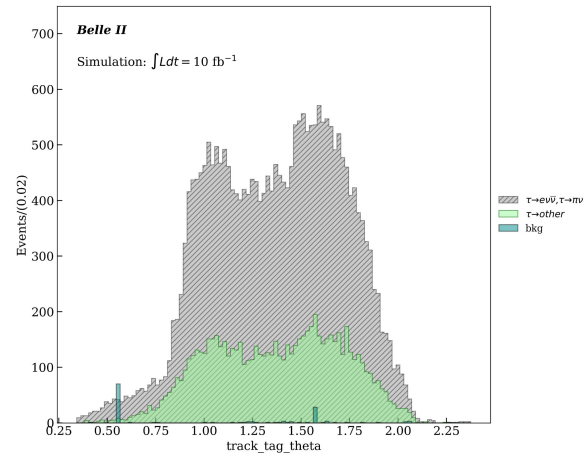
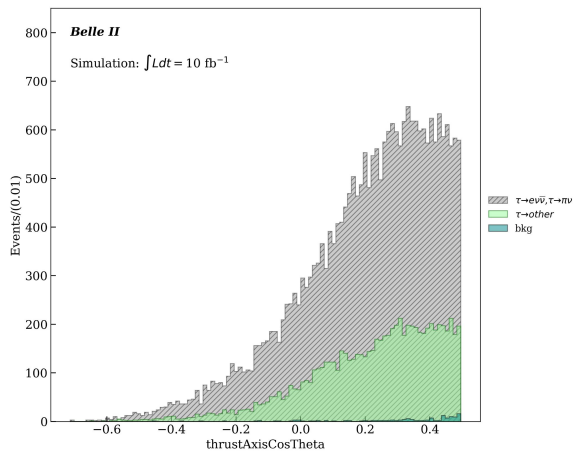
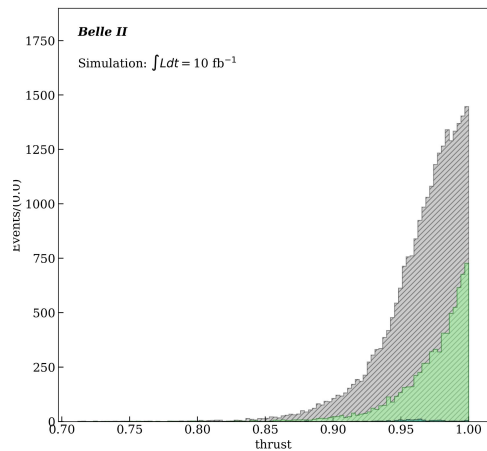
[johan.colorado@cinvestav.mx](mailto:johan.colorado@cinvestav.mx)

# MC study background rejection - $\tau \rightarrow e\nu$

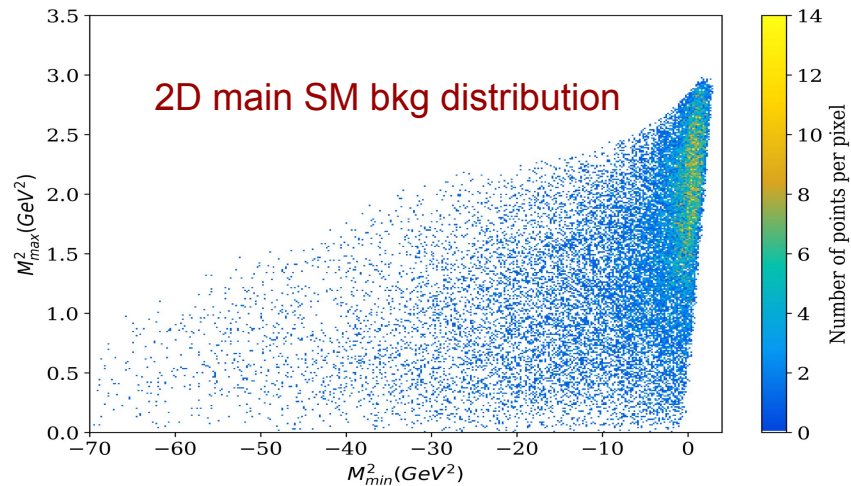
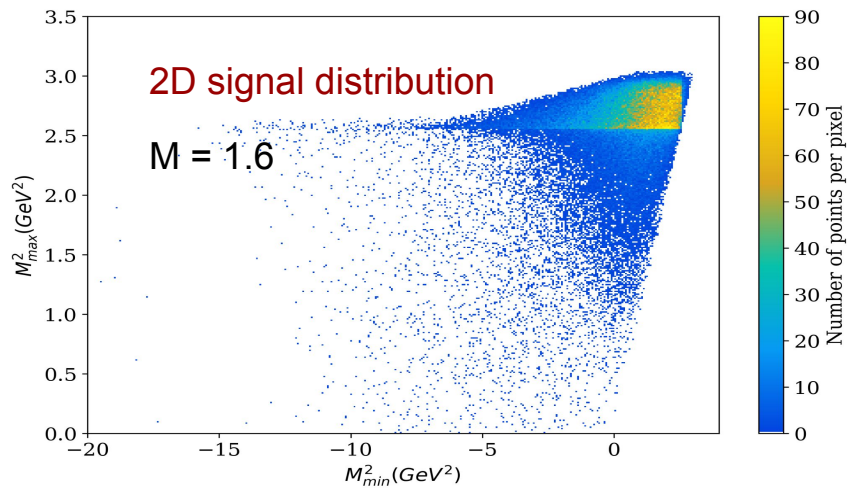
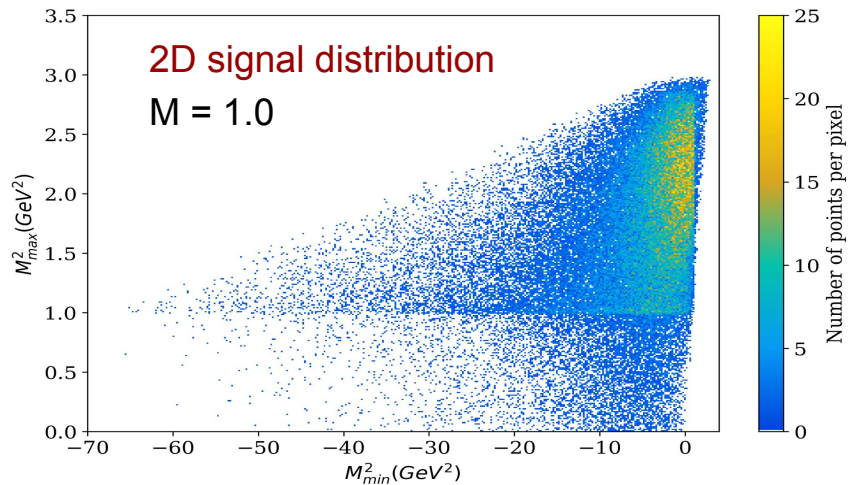




# MC study background rejection - $\tau \rightarrow e\nu$

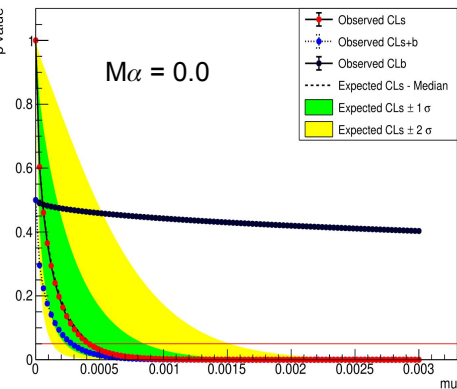




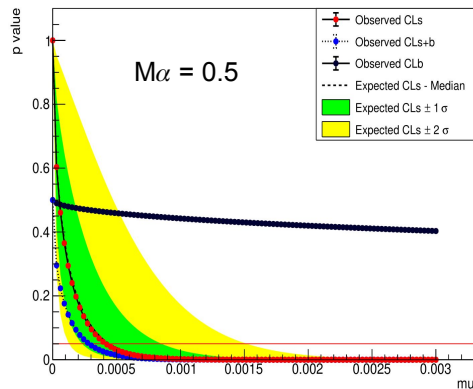


# CLs upper limit (Brazilian plots) using 2D method to 62.8/fb (e-channel)

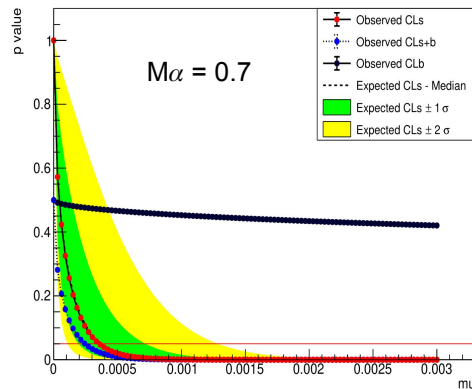
CLs upper limit



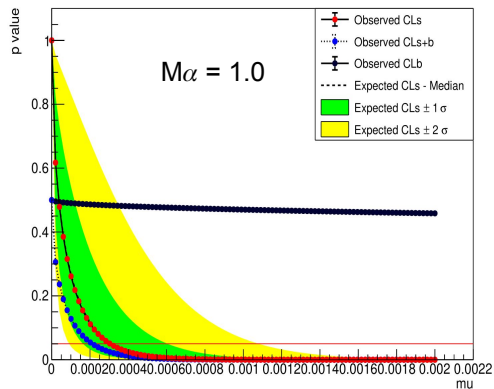
CLs upper limit



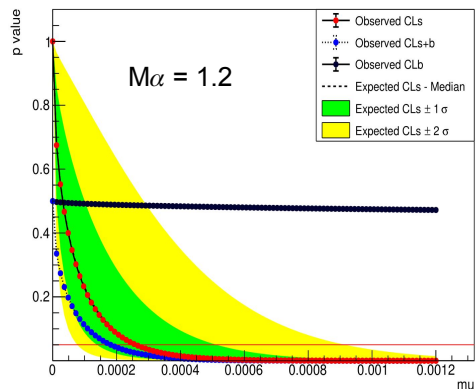
CLs upper limit



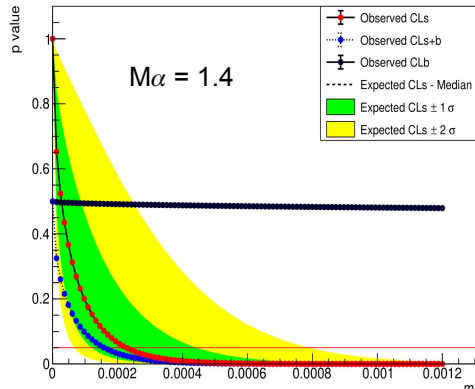
CLs upper limit



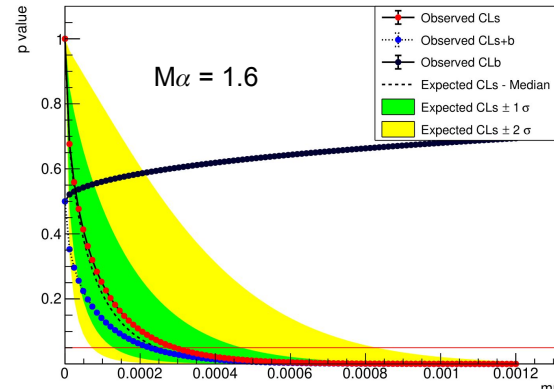
CLs upper limit



CLs upper limit



CLs upper limit



johan.colorado@cinvestav.mx