

# Electron Ion Collider: (a limited personal view on the) Science Case

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# Outline

Presentation

General Introduction

EIC Science Case

CLAS12 CFF Impact Projections

Selected EIC Science Projections

Summary

# Presentation

# Presentation

François-Xavier Girod

- ▶ 12/2006 PhD (Saclay)  
*Deeply Virtual Compton Scattering Beam Spin Asymetries at CLAS for a study of Generalized Parton Distributions*
- ▶ Feb. 2007 - Oct. 2011 : Post-doc in Hall-B at JLab
- ▶ 2011 Staff scientist in Hall-B
- ▶ Continued program support on DVCS, DVMP, and SIDIS studies
- ▶ Focus on Exclusive Reaction program on (polarized) Hydrogen and Nuclei (He)
- ▶ Polarized Positron Beam proposal
- ▶ Detector operation: CLAS12 beamline, calorimeters
- ▶ Heavy Photon Search
- ▶ 2020 switch to Electron Collider Science



# Suggested Reading

## Electron Ion Collider specific references

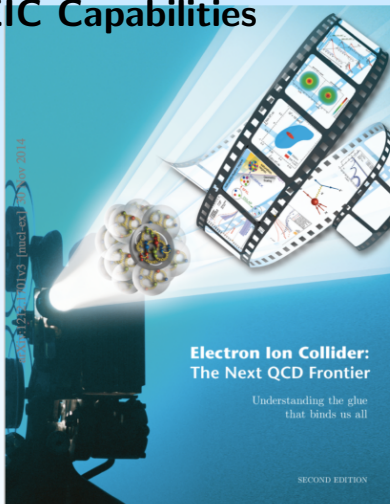
- ▶ “Yellow Report” EIC community, Nucl. Phys. A 1026 (2022) 122447
- ▶ “An Assessment of U.S.-Based Electron-Ion Collider Science” National Academies of Science (2018)
- ▶ “White Paper” Eur. Phys. J. A52 (2016) 268
- ▶ “HERA Physics” G. Wolf, DESY-94-22 (1994)

## Some **personal** recommendations

- ▶ “The Quark Structure of Hadrons” C. Amsler Springer Lecture Notes in Physics Vol 949 (2018)
- ▶ “High-Energy Particle Diffraction” V. Barone E. Predazzi Springer Texts and Monographs in Physics (2002)
- ▶ “The Structure of the Nucleon” A.W. Thomas W. Weise Wiley VCH (2001)
- ▶ “Deep Inelastic Positron-Proton Scattering at High- $p$  Transfer at HERA” U.F. Katz Springer Tracts in Modern Physics (2000)
- ▶ “QCD at HERA” M. Kuhlen Springer Tracts in Modern Physics (1999)

# **General Introduction**

# EIC Capabilities



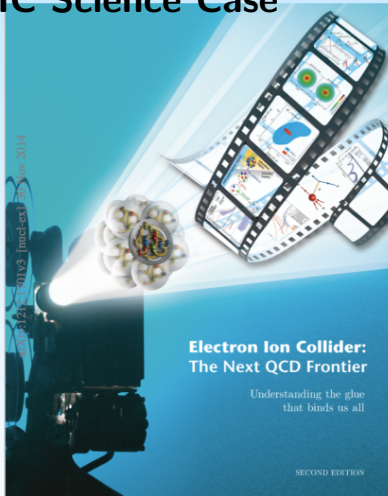
Eur. Phys. J. A52 (2016) no.9, 268

See also Rept.Prog.Phys. 82 (2019) 024301

- *A collider to provide kinematic reach well into the gluon dominated regime,*
- *Electron beams provide the unmatched precision of the electromagnetic interaction as a probe,*
- *Polarized nucleon beams to determine the correlations of sea quark and gluon distributions with the nucleon spin,*
- *Heavy Ion beams to access the gluon-saturated regime and as a precise dial to study propagation of color charges in nuclear matter.*
- *Facility concepts at BNL and at JLab, re-use of existing, significant investment (BNL has since been site-selected).*

E. Sichtermann (LBNL) CNFS-CTEQ23

# EIC Science Case



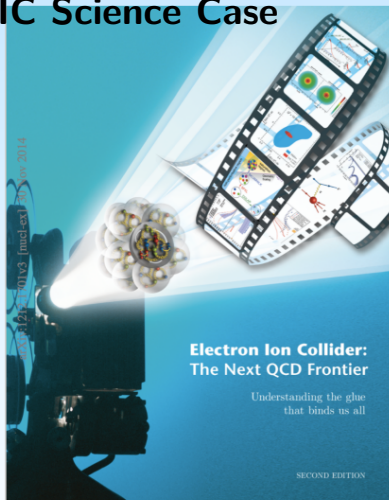
Eur. Phys. J. A52 (2016) no.9, 268

See also Rept.Prog.Phys. 82 (2019) 024301

- *How are the sea quarks and gluons, and their spins, distributed in space and momentum inside the nucleus?*
- *Where does the saturation of gluon densities set in?*
- *How does the nuclear environment affect the distribution of quarks and gluons and their interactions in nuclei?*

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# EIC Science Case



Eur. Phys. J. A52 (2016) no.9, 268

See also Rept.Prog.Phys. 82 (2019) 024301

*Organized around four themes:*

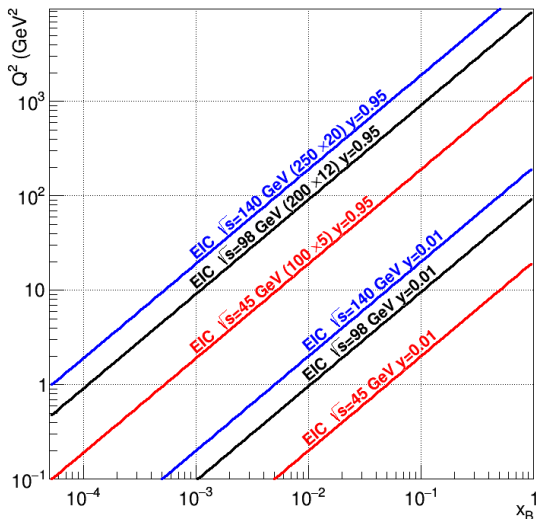
- *Proton spin, quark and gluon helicity distributions, orbital motion*
- *Imaging of nucleons and nuclei TMDs, GPDs, Wigner functions*
- *Saturation Non-linear evolution, Color-glass condensate,*
- *Hadronization and fragmentation, in-medium propagation, attenuation*

*Identified measurements and impact.*

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# Collider Energy Scenarios

## $Q^2$ vs $x_B$ landscape



Build on knowledge from

other colliders  
HERA, RHIC, LHC

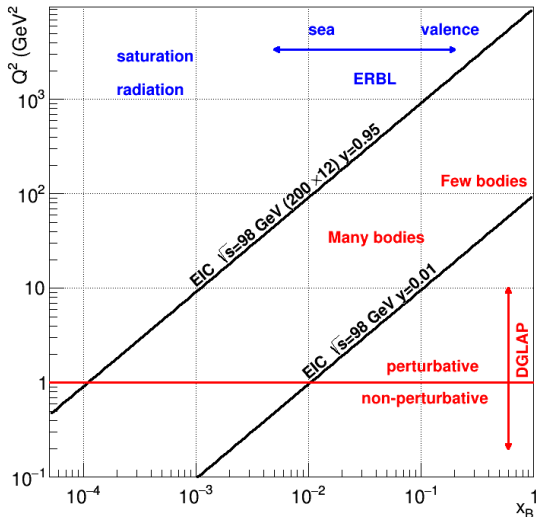
Fixed targets  
SLAC, HERMES, COMPASS, JLab

Crucial ingredients:  
**polarizations**  
**luminosity**

Complementarity of energy runs

# Kinematic reach and QCD Landscape

## $Q^2$ vs $x_B$ landscape



### Rich physics program

Position, Spin, Energy, Momentum distributions of quarks and gluons

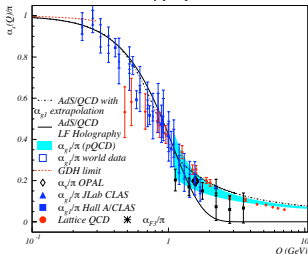
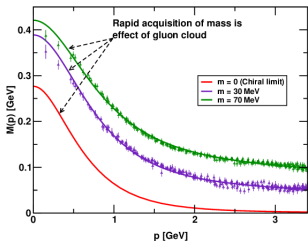
Origin Mass, Confinement,  $\chi$ SM  
QCD and Gravity

Gluon saturation, jet radiophysics  
QCD Bremsstrahlung

Nuclear Modifications  
EMC Effect, SRC

# Confinement Mechanism(s?)

Hadrons are singlets under  $SU(3)_{\text{color}}$  : No net color charge in asymptotic particle states



- ▶ **Linear growth of the static quark-antiquark pair**  
Area-law falloff for the Wilson loop
- ▶ **Gribov Confinement for light quarks**  
Analytical properties of the propagators in the infrared  
Instability of the vacuum above a supercritical charge

$$\alpha_{\text{QED}}^{\text{crit}} = 137 \text{ for a point-like nucleus}$$

$$\approx 180 \text{ for a finite size nucleus}$$

$$\frac{\alpha_{\text{QCD}}^{\text{crit}}}{\pi} = C_F^{-1} \left[ 1 - \sqrt{\frac{2}{3}} \right] \approx 0.137$$

- ▶ **Light-Front AdS/QCD**  
quark and gluon chiral condensates confined!  
→ condensates contribution to the cosmological constant  
already included in hadron mass
- ▶ **Mass-Gap Millennium problem and Yang-Mills existence**  
\$1M from the Clay Mathematical Institute



# Gravity and QCD

In some fundamental sense a *graviton* can be thought of as a *pair of vector bosons*: Gravity amplitudes appear as squared Yang-Mills amplitudes in the *Color-Kinematics Duality*

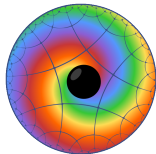
Understanding the deeper origin of these dualities is at the heart of string theory. Here a graviton (closed string) happens naturally as a pair of vector bosons (open strings). The **duality** between Gravity in the bulk and QCD on the boundary of AdS space, also called **holographic principle** is the currently the all time most cited high energy physics publication

Gravitational Form Factors from QCD bound states are observables of choice to test these dualities. Most promising avenue to understand the non-perturbative structure of gauge theories.

Z. Bern *et al.*  
Gravity as the Square of Gauge Theory  
*Phys. Rev. D* **82** 065003 (2010)



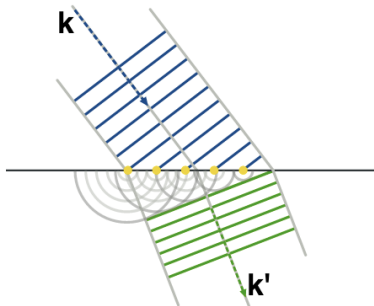
J. Maldacena  
The Large N limit of superconformal field theories and supergravity  
*Int. J. Theor. Phys.* **38** 1113 (1999)  
(13k citations as of June 2018)



# **EIC Science Case**

# Diffraction and Imaging

Huygens-Kirchhoff-Fresnel principle



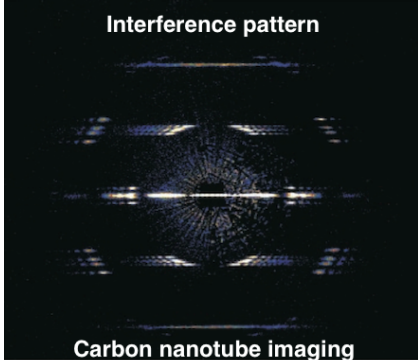
$$\vec{q} = \vec{k} - \vec{k}'$$

The interference pattern is given by the superposition of spherical wavelets

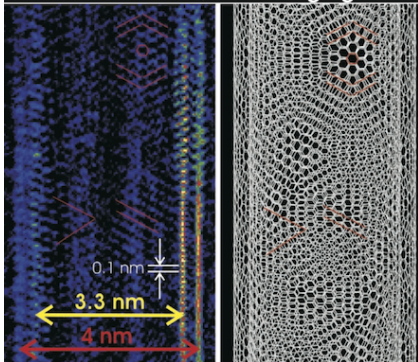
$$f(\Omega_{\vec{q}}) = \int \frac{d^3\vec{r}}{(2\pi)^3} F(\vec{r}) e^{i\vec{q}\cdot\vec{r}}$$

Fourier imaging

Interference pattern

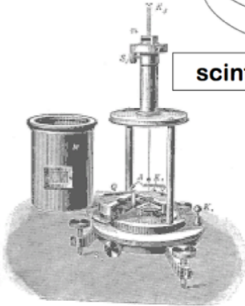
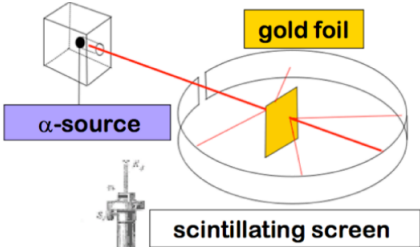


Carbon nanotube imaging

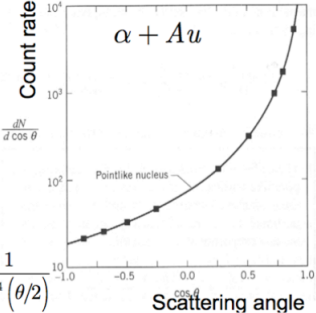


# Rutherford Scattering

~5 MeV



Ernest Rutherford,  
Nobel Prize 1908



$$\frac{d\sigma}{d\Omega} = (zZ\alpha)^2 \left( \frac{\hbar c}{4E_{kin}} \right)^2 \frac{1}{\sin^4(\theta/2)}$$

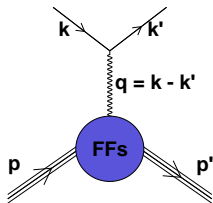
Scattering off a hard sphere;  $r_{nucleus} \sim (10^{-4} \cdot r_{atom}) \sim 10^{-14} \text{ m}$

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# Elastic scattering

## Form Factors

Probing deeper using virtual photons



$$J_{EM}^{\mu} = F_1 \gamma^{\mu} + \frac{\kappa}{2M} F_2 i \sigma^{\mu\nu} q_{\nu}$$

$$\frac{d\sigma}{d\Omega} = \frac{\sigma_{Mott}}{\epsilon(1+\tau)} [\tau G_M^2 + \epsilon G_E^2]$$

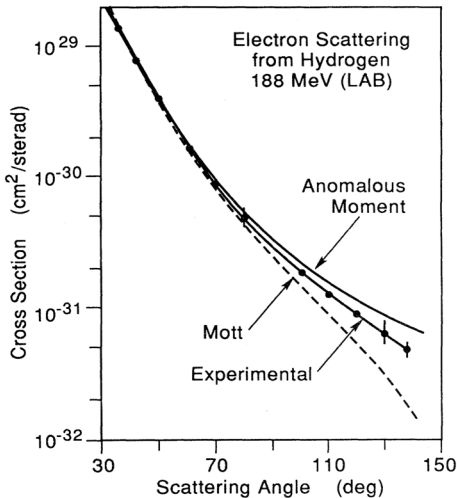
$$\tau = \frac{Q^2}{4M^2}$$

$$Q^2 = -(k - k')^2 = -m_{\gamma^*}^2$$

$$\frac{1}{\epsilon} = 1 + 2(1 + \tau) \tan^2 \frac{\theta_e}{2}$$

$$G_E = F_1 - \tau F_2$$

$$G_M = F_1 + F_2$$



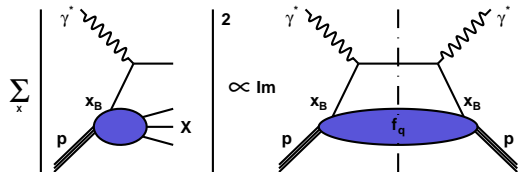
Hofstadter Nobel prize 1961

"The best fit in this figure indicates  
an rms radius close to  $0.74 \pm 0.24 \times 10^{-13}$  cm."

Imaging in transverse impact parameter space

# Deeply Inelastic Scattering

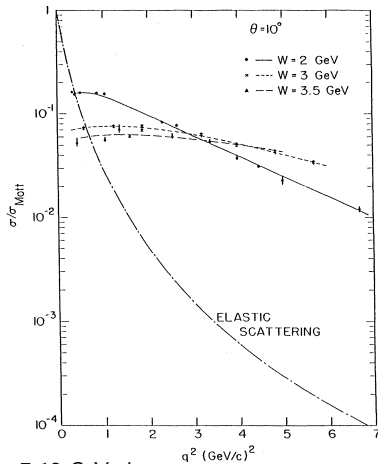
## Parton Distributions



The total cross section is given by the imaginary part of the forward amplitude

$$\nu = E_{\gamma^*} \quad , \quad x_B = \frac{Q^2}{2M\nu}$$

$\sigma_{\text{DIS}}(x_B, Q^2) \rightarrow$  scaling, point-like constituents



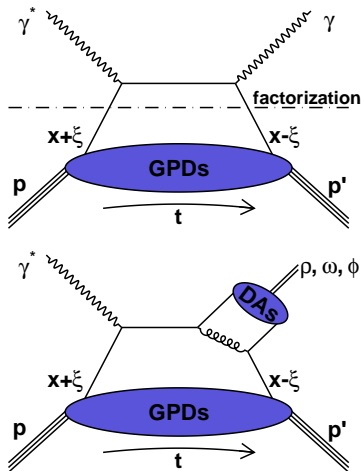
**Discovery of quarks**, SLAC-MIT group, 7-18 GeV electron  
Friedman, Kendall, Taylor, Nobel prize 1990

$$\lim_{Q^2 \rightarrow \infty} \sigma_{\text{DIS}}(x_B) = \int_{x_B}^1 \frac{d\xi}{\xi} \sum_a f_a(\xi, \mu) \hat{\sigma}^a \left( \frac{x_B}{\xi}, \frac{Q}{\mu} \right)$$

1-D distribution in longitudinal momentum space

# Deep Exclusive Scattering

## Generalized Parton Distributions



$$\gamma^* p \rightarrow \gamma p', \quad \gamma^* p \rightarrow \begin{cases} \rho p' \\ \omega p' \\ \phi p' \end{cases}$$

Bjorken regime :  
 $Q^2 \rightarrow \infty, x_B \text{ fixed}$

$$t \text{ fixed} \ll Q^2, \quad \xi \rightarrow \frac{x_B}{2-x_B}$$

$$\frac{P^+}{2\pi} \int dy^- e^{ixP^+y^-} \langle p' | \bar{\psi}_q(0) \gamma^+ (1 + \gamma^5) \psi(y) | p \rangle$$

$$= \bar{N}(p') \left[ H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) i\sigma^{+\nu} \frac{\Delta_\nu}{2M} \right. \\ \left. + \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \gamma^5 \frac{\Delta^+}{2M} \right] N(p)$$

spin	N no flip	N flip
q no flip	$H$	$E$
q flip	$\tilde{H}$	$\tilde{E}$

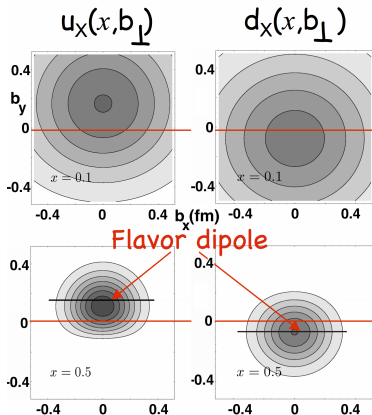
3-D Imaging conjointly in transverse impact parameter **and** longitudinal momentum

# GPDs and Transverse Imaging

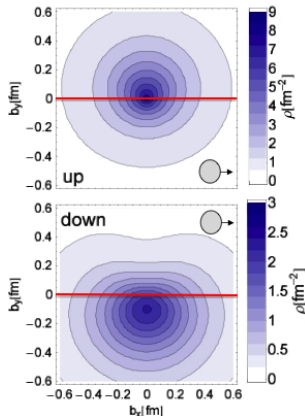
$(x_B, t)$  correlations

$$q_X(x, \vec{b}_\perp) = \int \frac{d^2 \vec{\Delta}_\perp}{(2\pi)^2} \left[ H(x, 0, t) - \frac{E(x, 0, t)}{2M} \frac{\partial}{\partial b_y} \right] e^{-i\vec{\Delta}_\perp \cdot \vec{b}_\perp}$$

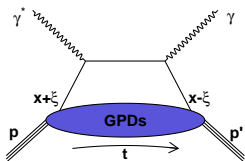
Target polarization



Lattice calculation

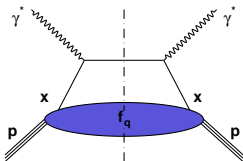






### Generalized Parton Distributions

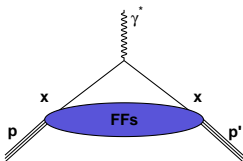
$$\begin{aligned} & \frac{P^+}{2\pi} \int dy^- e^{ixP^+y^-} \langle p' | \bar{\psi}_q(0) \gamma^+ (1 + \gamma^5) \psi(y) | p \rangle \\ &= \bar{N}(p') \left[ H^q(x, \xi, t) \gamma^+ + E^q(x, \xi, t) i\sigma^{+\nu} \frac{\Delta_\nu}{2M} \right. \\ & \quad \left. + \tilde{H}^q(x, \xi, t) \gamma^+ \gamma^5 + \tilde{E}^q(x, \xi, t) \gamma^5 \frac{\Delta^+}{2M} \right] N(p) \end{aligned}$$



### Parton longitudinal momentum fraction distributions

$$\begin{aligned} & \frac{1}{4\pi} \int dy^- e^{ixp^+y^-} \langle p | \bar{\psi}_q(0) \gamma^+ \psi(y) | p \rangle = f_q(x) \\ & H^q(x, \xi = 0, t = 0) = f_q(x) \end{aligned}$$

### Form Factors - Fourier transform of transverse spatial distributions



$$\langle p' | \bar{\psi}_q(0) \gamma^+ \psi(0) | p \rangle = \bar{N}(p') \left[ F_1^q(t) \gamma^+ + F_2^q(t) i\sigma^{+\nu} \frac{\Delta_\nu}{2M} \right] N(p)$$

$$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t) \quad \text{First } x\text{-moment}$$

$$\int_{-1}^1 dx E^q(x, \xi, t) = F_2^q(t)$$

# GPDs and Energy Momentum Tensor

$(x, \xi)$  correlations

**Form Factors** accessed *via* second x-moments :

$$\langle p' | \hat{T}_{\mu\nu}^q | p \rangle = \bar{N}(p') \left[ M_2^q(t) \frac{P_\mu P_\nu}{M} + J^q(t) \frac{i(P_\mu \sigma_{\nu\rho} + P_\nu \sigma_{\mu\rho}) \Delta^\rho}{2M} + d_1^q(t) \frac{\Delta_\mu \Delta_\nu - g_{\mu\nu} \Delta^2}{5M} \right] N(p)$$

Angular momentum distribution

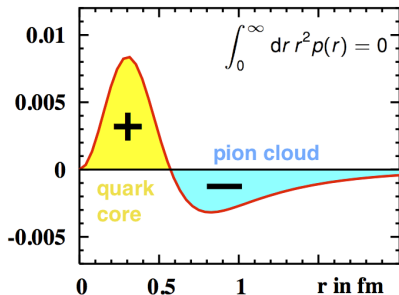
$$J^q(t) = \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

Mass and force/pressure distributions

$$M_2^q(t) + \frac{4}{5} d_1^q(t) \xi^2 = \frac{1}{2} \int_{-1}^1 dx x H^q(x, \xi, t)$$

$$d_1(t) = 15M \int d^3\vec{r} \frac{j_0(r\sqrt{-t})}{2t} \rho(r)$$

Distribution of pressure  
 $r^2 p(r)$  in  $\text{GeV fm}^{-1}$



# Deeply Virtual Compton Scattering

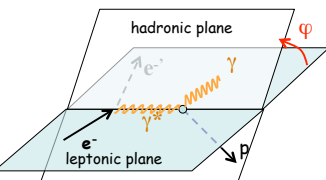
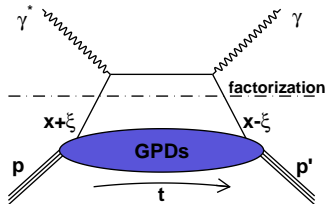
The cleanest GPD probe at low and medium energies

$$\gamma^* p \rightarrow \gamma p'$$

Bjorken regime :

$$Q^2 \rightarrow \infty, \nu \rightarrow \infty, x_B \text{ fixed}$$

$$\xi \rightarrow \frac{x_B}{2-x_B}$$



$$ep \rightarrow ep\gamma$$

$$\sigma(ep \rightarrow ep\gamma) \propto \left| \begin{array}{c} \text{DVCS} \\ \text{BH} \end{array} \right|^2$$

Diagram showing the DVCS and BH contributions to the DVCS cross-section. The DVCS contribution is shown as a single diagram (a). The BH contribution is shown as two diagrams (b) and (c).

Diehl, Gousset, Pire, Ralston (1997)

Belitsky, Müller, Kirchner (2002, 2010)

$$A_{LU} = \frac{d^4\sigma \rightarrow -d^4\sigma \leftarrow}{d^4\sigma \rightarrow + d^4\sigma \leftarrow} \stackrel{\text{twist-2}}{\approx} \frac{\alpha \sin \phi}{1 + \beta \cos \phi}$$

$$\alpha \propto \text{Im} \left( F_1 \mathcal{H} + \xi G_M \tilde{\mathcal{H}} - \frac{t}{4M^2} F_2 \mathcal{E} \right)$$

$$\mathcal{H}(\xi, t) = i\pi H(\xi, \xi, t) + \mathcal{P} \int_{-1}^1 dx \frac{H(x, \xi, t)}{x - \xi}$$

$$A_{UL} \propto \text{Im} \left( F_1 \tilde{\mathcal{H}} + \xi G_M \mathcal{H} + G_M \frac{\xi}{1 + \xi} \mathcal{E} + \dots \right) \sin \phi$$

# Deeply Virtual Compton Scattering

The cleanest GPD probe at low and medium energies

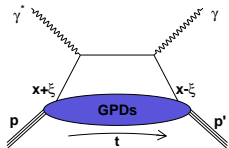
$$\begin{aligned} A_{\text{UT}} &= \frac{d^4\sigma^{U\uparrow}(\phi_S - \phi) - d^4\sigma^{U\downarrow}(\phi_S - \phi + \pi)}{d^4\sigma^{U\uparrow}(\phi_S - \phi) + d^4\sigma^{U\downarrow}(\phi_S - \phi + \pi)} \\ &\stackrel{\text{twist-2}}{\propto} A_{\text{UT}}^{\sin(\phi_S - \phi)\cos\phi} \sin(\phi_S - \phi)\cos\phi \\ &\quad + A_{\text{UT}}^{\cos(\phi_S - \phi)\sin\phi} \cos(\phi_S - \phi)\sin\phi \\ A_{\text{UT}}^{\sin(\phi_S - \phi)\cos\phi} &= \frac{1}{\pi} \int_0^{2\pi} d\phi \cos(\phi) A_{\text{UT}}^{\sin(\phi_S - \phi)} \\ A_{\text{UT}}^{\sin(\phi_S - \phi)} &\propto \frac{1-x}{2-x} \frac{t}{Q^2} F_2 \mathcal{H} + \frac{t}{4M^2} (2-x) F_1 \mathcal{E} \end{aligned}$$

# Deeply Virtual Compton Scattering

The cleanest GPD probe at low and medium energies

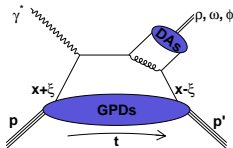
$$\begin{aligned}A_{\text{LT}} &= \frac{(d^4\sigma_{\rightarrow\uparrow} + d^4\sigma_{\leftarrow\downarrow}) - (d^4\sigma_{\rightarrow\downarrow} + d^4\sigma_{\leftarrow\uparrow})}{(d^4\sigma_{\rightarrow\uparrow} + d^4\sigma_{\leftarrow\downarrow}) + (d^4\sigma_{\rightarrow\downarrow} + d^4\sigma_{\leftarrow\uparrow})} \\A_{\text{LT}}^{\sin(\phi_S - \phi)\sin\phi} &= \frac{1}{\pi} \int_0^{2\pi} d\phi \sin(\phi) A_{\text{LT}}^{\sin(\phi_S - \phi)} \\A_{\text{LT}}^{\sin(\phi_S - \phi)} &\propto A_{\text{LT,BH}}^{\sin(\phi_S - \phi)} + \frac{1}{2-x} \left( x^2 F_1 - (1-x) \frac{t}{M^2} F_2 \right) \mathcal{H} \\&\quad + \left\{ \frac{t}{4M^2} \left( \frac{x}{\xi} F_1 + x\xi F_2 \right) + x\xi F_1 \right\} \mathcal{E}\end{aligned}$$

# Observables sensitivities to GPD



DVCS

	$\mathcal{I}m$	$\mathcal{R}e$
$\mathcal{H}$	$A_{LU}$	$\sigma$ $A_{LL}, A_{LT}$
$\tilde{\mathcal{H}}$	$A_{UL}$	
$\mathcal{E}$	$A_{UT}$	



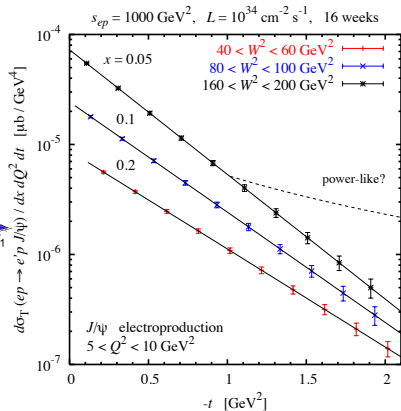
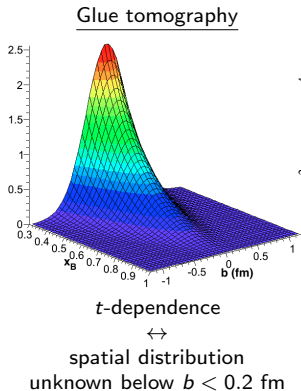
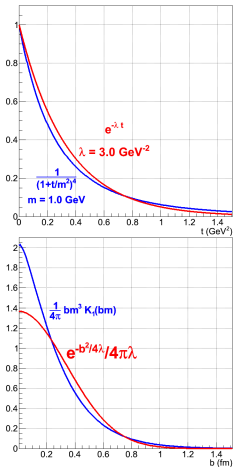
DVMP

	Meson	Flavor
$\tilde{\mathcal{H}}, \tilde{\mathcal{E}}$	$\pi^+$	$\Delta u - \Delta d$
	$\pi^0$	$2\Delta u + \Delta d$
	$\eta$	$2\Delta u - \Delta d + 2\Delta s$
$\mathcal{H}, \mathcal{E}$	$\rho^+$	$u - d$
	$\rho^0$	$2u + d$
	$\omega$	$2u - d$
	$\phi$	$s$

*A global analysis is needed to fully disentangle GPDs*

# Electron-Ion Collider

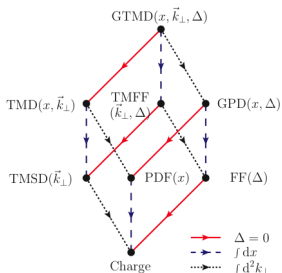
## J/ψ electroproduction as a probe of the glue distribution



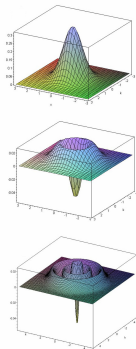
# Unified view of hadron structure

## Wigner Distributions

FFs, PDFs, GPDs, TMDs, inflation of acronyms all related to the same Wigner distribution



- ▶ Most general one-parton density matrix
- ▶ Not known how to measure
- ▶ Provides a unifying description
- ▶ Constraints for model building



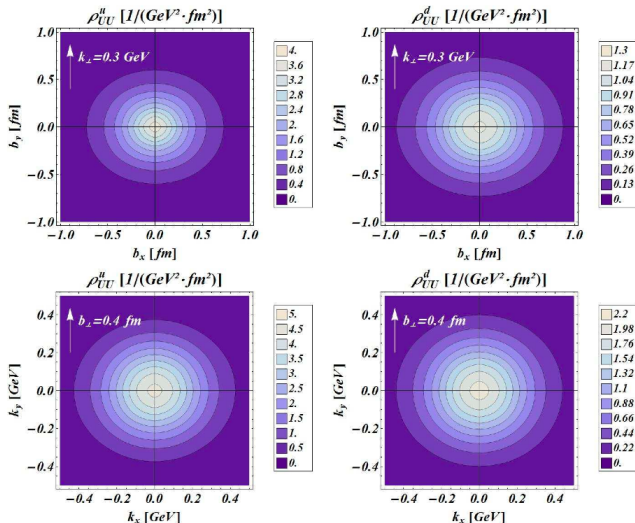
Unified framework for GPDs and TMDs within a 3Q LC picture of the nucleon

C. Lorcé *et al*, arXiv:1102.4704, JHEP 1105:041,2011



# Overview of the nucleon structure

## Unpolarized quark in unpolarized nucleon

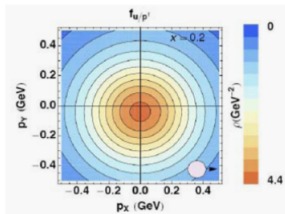


Quadrupole deformation of transverse position for quarks at large transverse momentum  
Intuitive from a semi-classical picture of confinement

# Two Approaches to Imaging

## TMDs

2+1 D picture in **momentum space**

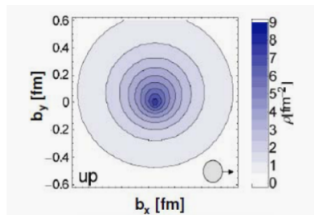


Bacchetta, Conti, Radici

- intrinsic transverse motion
- spin-orbit correlations = indicator of OAM
- non-trivial factorization
- accessible in SIDIS, DY (and at RHIC)

## GPDs

2+1 D picture in **impact-parameter space**



QCDSF collaboration

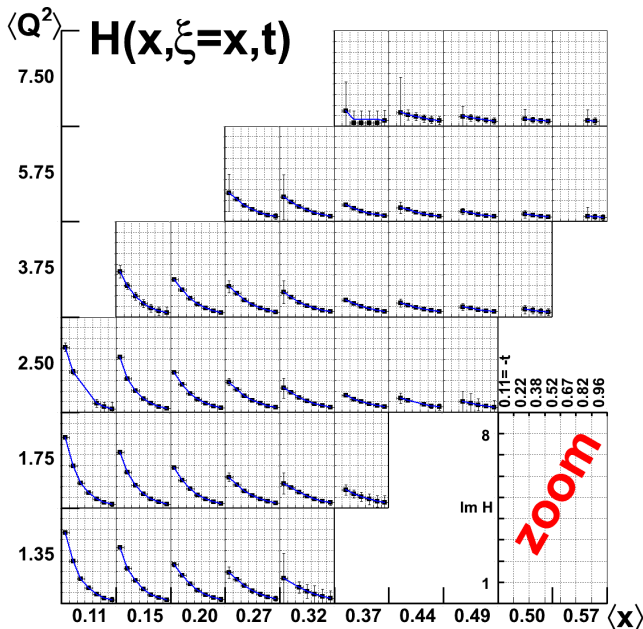
- collinear but long. momentum transfer
- indicator of OAM; access to Ji's total  $J_{q,g}$
- existing factorization proofs
- DVCS, exclusive vector-meson production

currently no direct, model-independent relation known between TMDs and GPDs

E. Sichtermann (LBNL) CNFS-CTEQ23

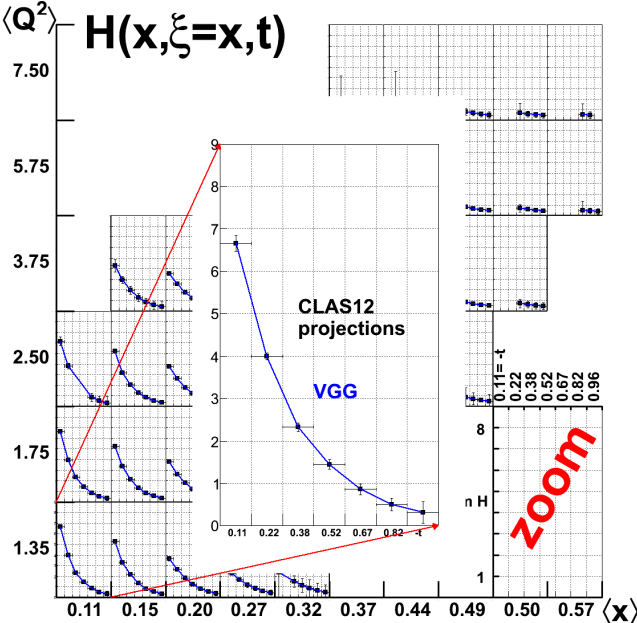
## **CLAS12 CFF Impact Projections**

# Projected CLAS12 impact on CFFs



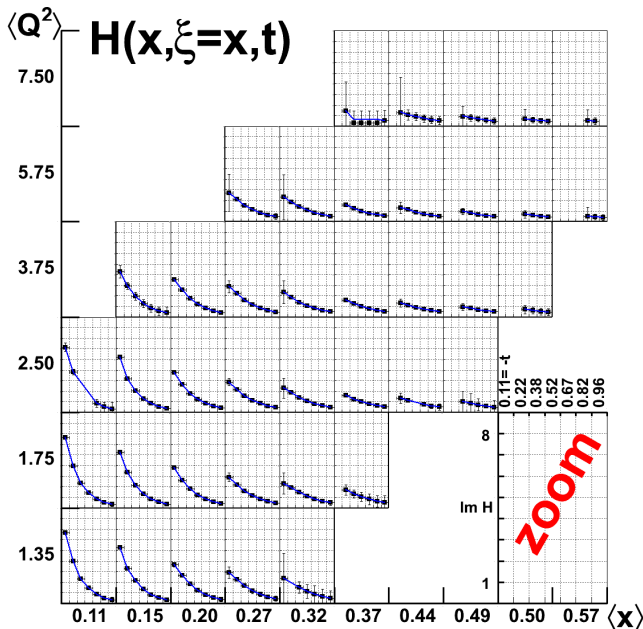
Using simulated data based on VGG model.  
Input GPD H extracted with good accuracy

# Projected CLAS12 impact on CFFs

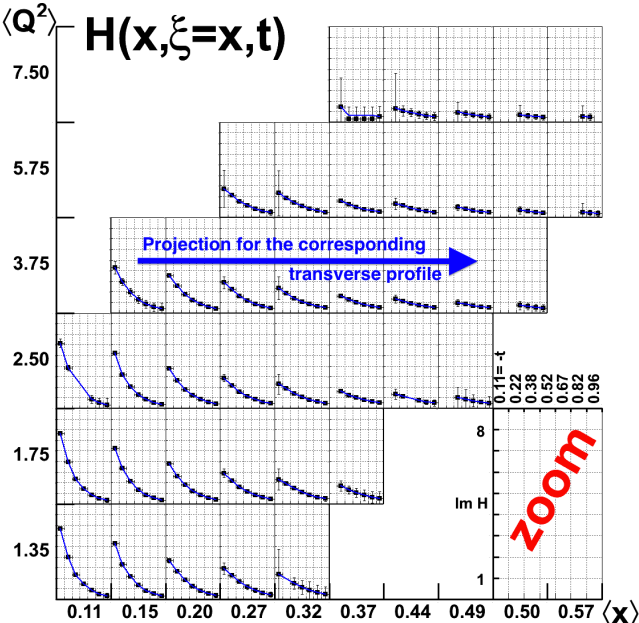


Using simulated data based on VGG model. Input GPD H extracted with good accuracy

# Projected CLAS12 impact on CFFs



# Projected CLAS12 impact on CFFs



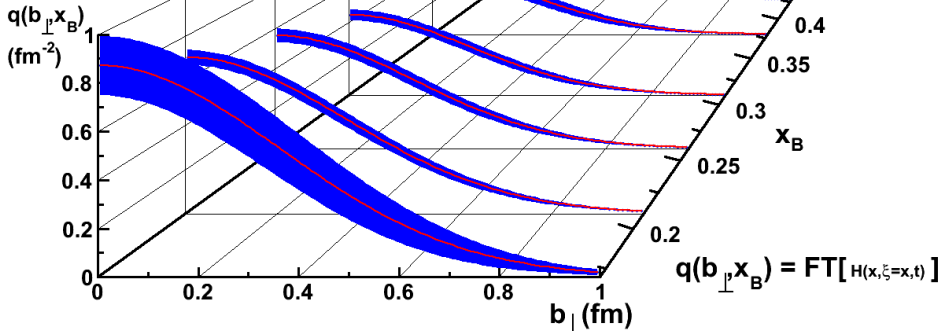
Using simulated data based on VGG model. Input GPD H extracted with good accuracy

# Projection for the Nucleon transverse profile

Model profile

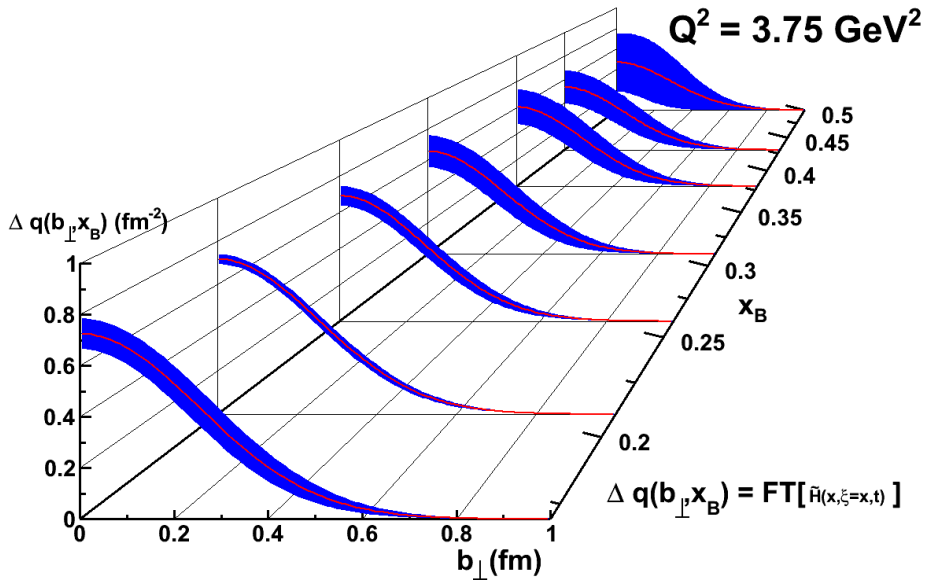
Projected error band

$$Q^2 = 3.75 \text{ GeV}^2$$



Precision tomography in the valence region

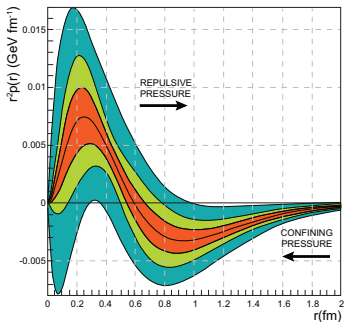




Precision tomography in the valence region

# Proton Pressure distribution results

The pressure at the core of the proton is  $\sim 10^{35}$  Pa  
About 10 times the pressure at the core of a neutron star



Positive pressure in the core (repulsive force)  
Negative pressure at the periphery: pion cloud  
Pressure node around  $r \approx 0.6$  fm

$$\text{Stability condition : } \int_0^{\infty} dt r^2 p(r) = 0$$

Rooted into Chiral Symmetry Breaking

World data fit

CLAS 6 GeV data

Projected CLAS12 data E12-16-010B

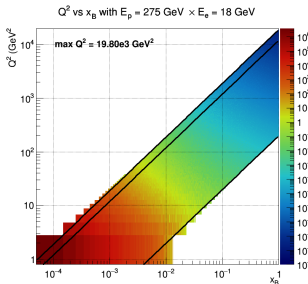
## **CFF local Fits at EIC**

# EIC proton DVCS Observables

	$\int \mathcal{L}$	Observables	$A_{e,p}$
unpolarized	200 fb <sup>-1</sup>	$\sigma$	$A_{LU}$
L polarized	100 fb <sup>-1</sup>	$A_{UL}$	$A_{LL}$
T polarized	100 fb <sup>-1</sup>	$A_{UTx}$	$A_{UTy}$ $A_{LTx}$ $A_{LTy}$
$e^+$	100 fb <sup>-1</sup>	$A^C$	$A_{LU}^C$

$$N_{\text{events}} = \int \mathcal{L} \times \sigma \times \text{KPS}$$

$$\text{KPS} = \Delta x_B \Delta Q^2 \Delta t \Delta \phi$$



$$\frac{\Delta\sigma}{\sigma} = \frac{1}{\sqrt{N_{\text{events}}}} \oplus 5\%$$

$$\Delta A_{LU} = \frac{1}{P_e} \sqrt{\frac{1 - P_e^2 A_{LU}^2}{N}} \oplus 3\%_{\text{relative}} \quad P_e = 70\%$$

$$\Delta A_{UL} = \frac{1}{P_p} \sqrt{\frac{1 - P_p^2 A_{UL}^2}{N}} \oplus 3\%_{\text{relative}} \quad P_p = 70\%$$

$$\Delta A_{LL} = \frac{1}{P_e P_p} \sqrt{\frac{1 - P_e^2 P_p^2 A_{LL}^2}{N}} \oplus 3\%_{\text{relative}} \oplus 3\%_{\text{relative}}$$

$$\Delta A_C = \sqrt{\frac{1 - A_C^2}{N}} \oplus 3\%_{\text{relative}}$$

$$\Delta A_{LC} = \frac{1}{P_{e^+}} \sqrt{\frac{1 - P_{e^+}^2 A_{LC}^2}{N}} \oplus 3\%_{\text{relative}} \quad P_{e^+} = 70\%$$

## N.B. assumption on the luminosity

$$1 \text{ year} = 365 \text{ days} \times 24 \text{ hours/day} \times 3600 \text{ s/hour} = 3.15 \times 10^7 \text{ s} \approx \frac{1}{3} \times 10^8 \text{ s}$$

$$\mathcal{L} = 10^{34} \text{ cm}^{-2}\text{s}^{-1} = 10^{38} \text{ m}^{-2}\text{s}^{-1}$$

$$\int \mathcal{L} = 10^{34} \text{ cm}^{-2}\text{s}^{-1} \times 1 \text{ year} \approx \frac{1}{3} \times 10^{46} \text{ m}^{-2}$$

$$1 \text{ barn} = 10^{-28} \text{ m}^2$$

$$1 \text{ fb} = 10^{-43} \text{ m}^2$$

$$1 \text{ fb}^{-1} = 10^{43} \text{ m}^{-2}$$

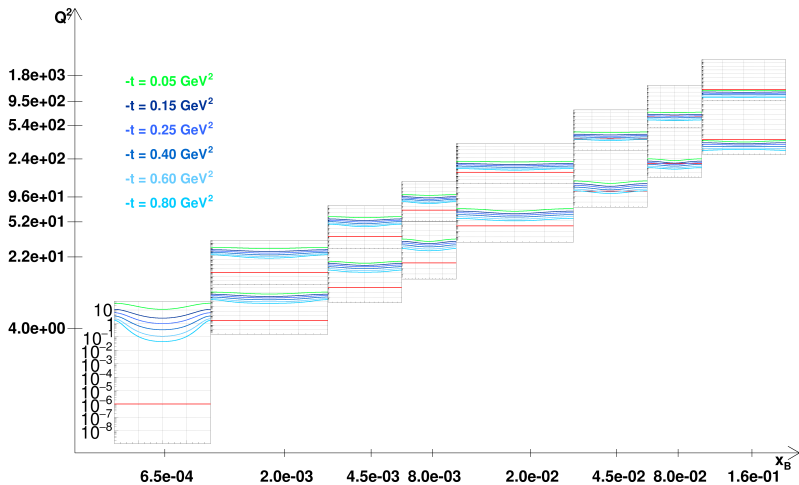
$$100 \text{ fb}^{-1} = 10^{45} \text{ m}^{-2}$$

$$\begin{aligned} 100 \text{ fb}^{-1} &\iff 1 \text{ year at } 10^{34} \text{ cm}^{-2}\text{s}^{-1} \text{ with contingency } (\approx 3) \\ &\iff 10 \text{ years at } 10^{33} \text{ cm}^{-2}\text{s}^{-1} \end{aligned}$$

Luminosity is a potential challenge for exclusive reactions

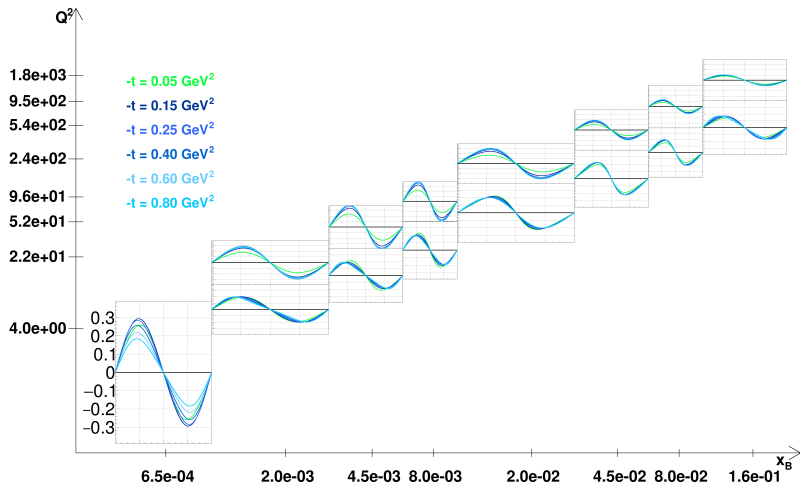
275 GeV  $\times$  18 GeV

$\sigma$



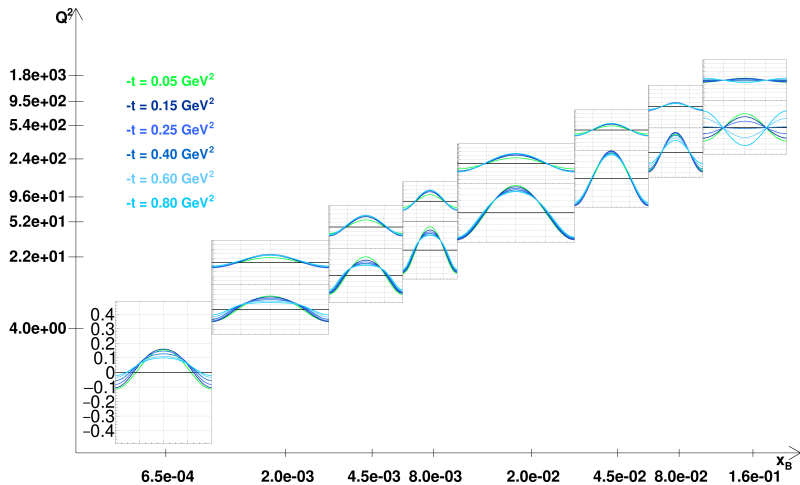
275 GeV  $\times$  18 GeV

$A_{LU}$



275 GeV  $\times$  18 GeV

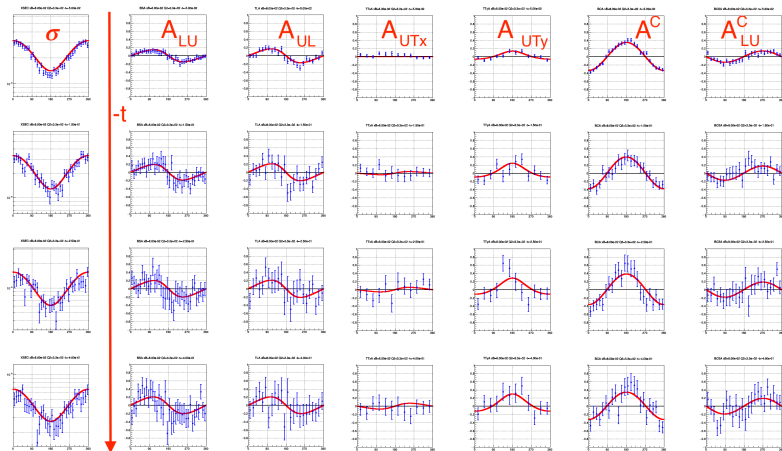
$A^C$





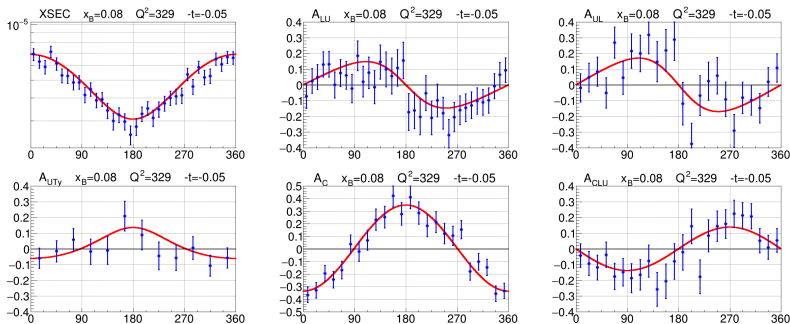
275 GeV  $\times$  18 GeV  $x_B = 0.08 \pm 0.02$

$Q^2 = 329 \pm 175 \text{ GeV}^2$



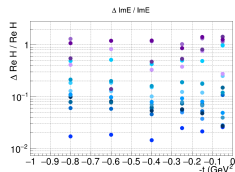
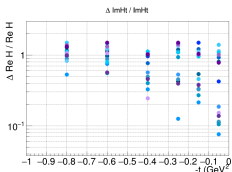
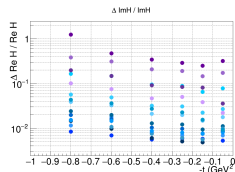
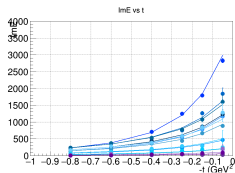
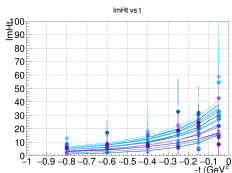
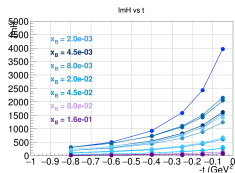
Not shown here:  $A_{LL}$   $A_{LTx}$   $A_{LTy}$  are small

275 GeV  $\times$  18 GeV  $x_B = 0.08 \pm 0.02$   $Q^2 = 329 \pm 175 \text{ GeV}^2$   $-t = 0.05 \pm 0.05 \text{ GeV}^2$

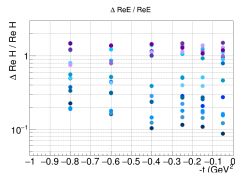
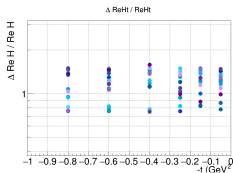
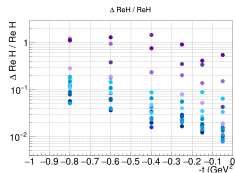
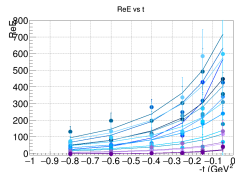
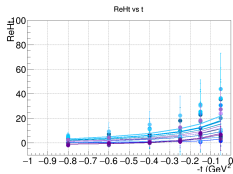
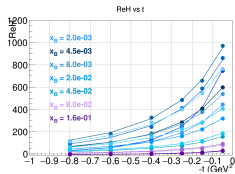


note: statistics and systematics included

# Locally extracted Im CFF $275 \times 18 \text{ GeV}^2$



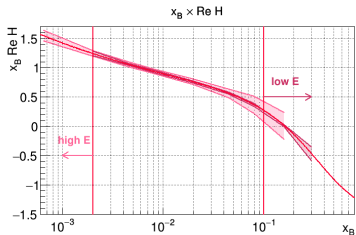
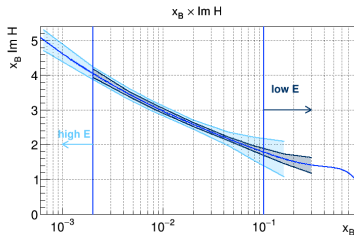
# Locally extracted Re CFF $275 \times 18 \text{ GeV}^2$



# High and Low energies runs

## Kinematical coverage complementarity

Local extraction results:



### Better Strategy:

global fit using DR and parameterizations for  $\text{Im}H$  and  $D(t)$   
note: subtraction constant: same for  $H$  and  $\mathcal{E}$ , none for  $\tilde{H}$  and  $\tilde{\mathcal{E}}$

# Towards Ji's sum rule

$$J^q(t) = \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

independent of  $\xi$  but at fixed  $\xi$

DVCS measures

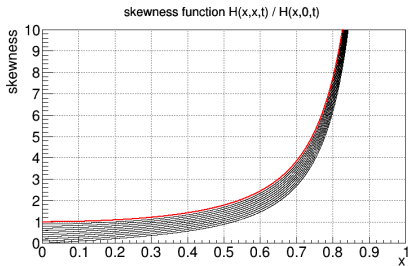
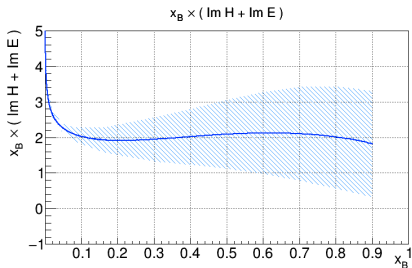
$$\mathcal{I}m\mathcal{H}(\xi, t) = \pi H(\xi, \xi, t)$$

need another process to access the skewness

→ especially crucial at large  $x_B$

DDVCS?

JLab 12 luminosity upgrade?

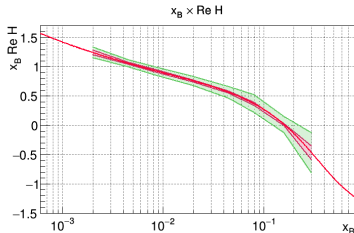
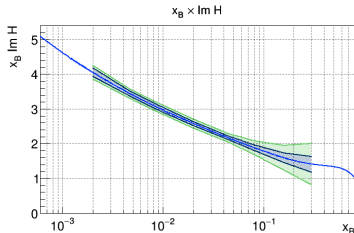


# Impact of the positron beam

Enhanced sensitivity to the Real part of the amplitude

Local extraction results:

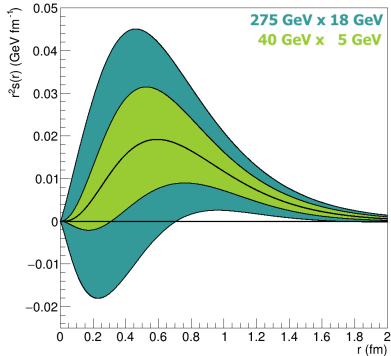
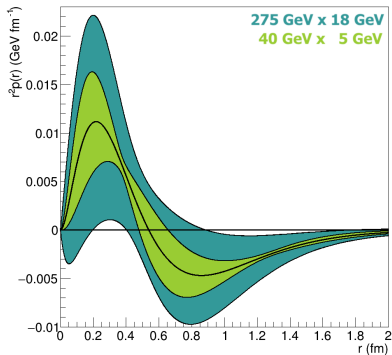
low E: 40 GeV  $\times$  5 GeV



**Improved sensitivity, and systematic checks**  
**Also, in general opens up access to new physics ( $\dots$ )**

# Pressure and Shear Sensitivities

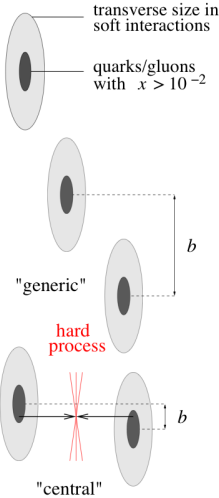
Propagate uncertainties estimated with local fits using dispersion relation



Relevance of the large  $x_B$  region to the dispersion analysis



# Nucleon structure for hadron-hadron colliders



- ▶ MultiParton Interaction first suggested in 1975 (Landshoff & Polkinghorne)
- ▶ Evidence in :
  - ▶ high  $p_T$  at the CERN/ISR and Tevatron
  - ▶ intermediate  $p_T$  : underlying event in Dijet and Drell-Yann at CFD Run I and II, and at CMS
  - ▶ Found to be necessary to tune low  $p_T$  Pythia and Herwig
- ▶ MPI more important at LHC is expected to challenge many new physics search
- ▶ MPI can also be better studied at LHC for itself !

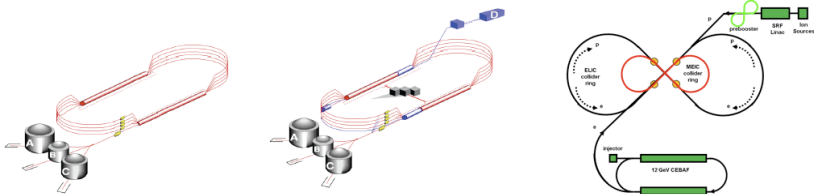
$$\left| \begin{array}{c} x_1 \\ \uparrow y_1 \\ x_2 \end{array} \right|^2 \approx \int d^2b \left| \begin{array}{c} \downarrow b \\ x_2 \end{array} \right|^2 \times \left| \begin{array}{c} x_1 \\ \uparrow b + y_1 \end{array} \right|^2$$

C. Weiss, L. Frankfurt, M. Strikman, Ann.Rev.Nucl.Part.Sci. 55 (2005) 403-465  
 Diehl, Ostermeier, Schäfer, "Elements of MPI in QCD", DESY 11-196

# Summary

# Summary

- ▶ A unified framework for nucleon tomography
- ▶ The first 6 GeV results suggested precocious dominance of small configurations
- ▶ Accuracy of 12 GeV era in the valence region at moderate momentum transfer
- ▶ Long range plan extends naturally to EIC
- ▶ Interplay between spin and flavor decompositions requires all reactions
- ▶ The EIC will expand the reach and probe the sea and gluons
- ▶ Other future measurements planned at CERN/Compass and DESY/Panda
- ▶ EIC will be essential for QCD backgrounds at LHC and beyond
- ▶ Complementarity



**Outlook**  
**Supplementary slides**

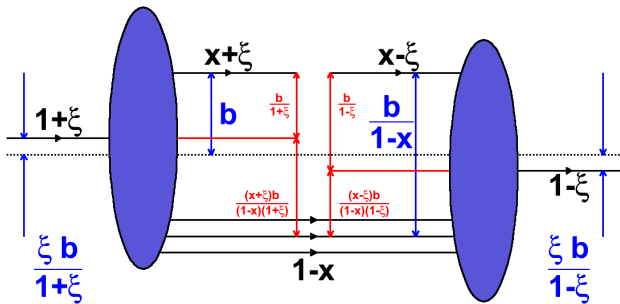
# Impact parameter space

$$\text{GPD} \propto e^{Bt}$$

$$-t = \frac{x_B^2 M^2 + \Delta_{\perp}^2}{1 - x_B}$$

$$\text{GPD} \propto e^{-B_{\perp} \Delta_{\perp}^2}$$

$$B_{\perp} = \frac{1}{1 - x_B} B$$



# GPD modelling and Dispersion relations

$$\text{CFF}(x_B, Q^2, t) = \int_{-1}^1 dx \frac{2x}{\xi^2 - x^2 - i\epsilon} \text{GPD}(x, \xi, t, Q^2)$$

$$\text{Im CFF}(x_B, Q^2, t) = \pi \text{GPD}(\xi, \xi, t, Q^2)$$

$$\text{Re CFF}(x_B, Q^2, t) = \int_0^1 dx \frac{2x}{\xi^2 - x^2} \text{GPD}(x, x, t, Q^2) \pm \mathcal{D}(t, Q^2)$$

“Holographical” models for global fitting strategies  
Parameters are direct observables

# Model dependent extraction of $J_u$ and $J_d$

