

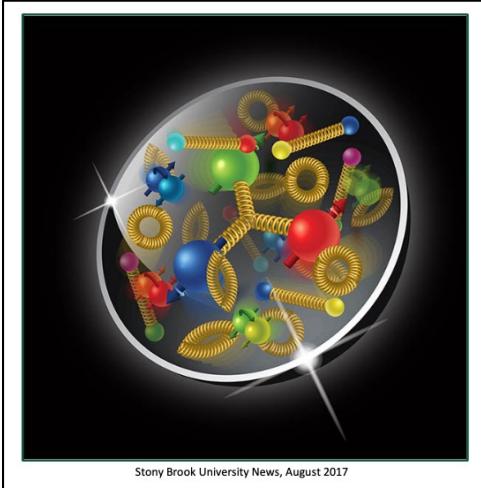
# (Very) Selected SIDIS Results from Hall-B

Timothy B. Hayward



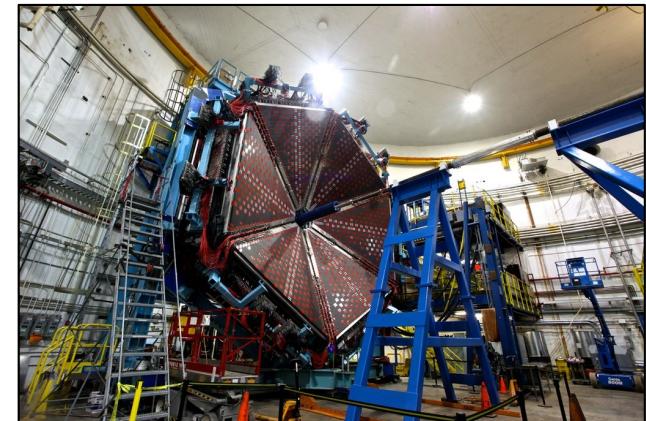
June 26, 2023

# CLAS12 (Hall B) Physics Program

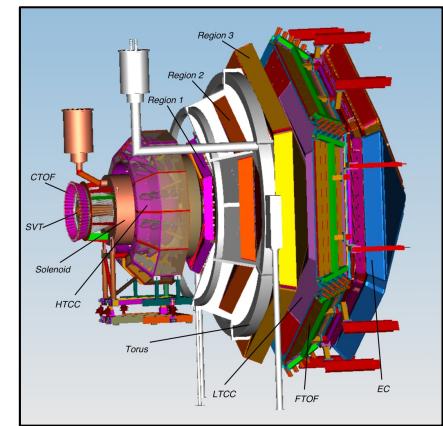


Stony Brook University News, August 2017

- International collaboration with more than 40 member institutions and 200 full members.
- CLAS(12) is the world's only large acceptance and high luminosity spectrometer for fixed target lepton scattering experiments.



1. Study of the nucleon resonance structure at photon virtualities from 2.0 to 12  $\text{GeV}^2$
2. Study of Generalized Parton Distributions (GPDs), (2 +1) D imaging of the proton and the study of its gravitational and mechanical structure.
3. Study of the Transverse Momentum Dependence (TMDs) and the of 3D structure in momentum space.
4. Study of J/ $\psi$  Photoproduction, LHCb Pentaquarks and Timelike Compton Scattering.
5. Study of meson spectroscopy in search of hybrid mesons
6. Much more!



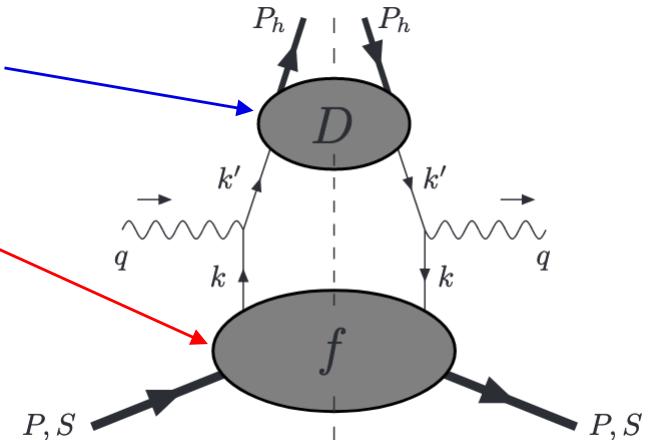
# SIDIS measurements

- Decades of study have led to detailed mappings of the momentum distribution of partons in the nucleon in terms of 1-D and 3-D (TMD) parton distribution functions (PDFs).
- SIDIS measurements rely on the assumption that measured hadrons are produced in the CFR.
- Cross section factorized as a convolution of PDFs and Fragmentation Functions (FFs)<sup>1</sup>.

A. Bacchetta et al., JHEP 02 (2007) 093 [hep-ph] 0611265,

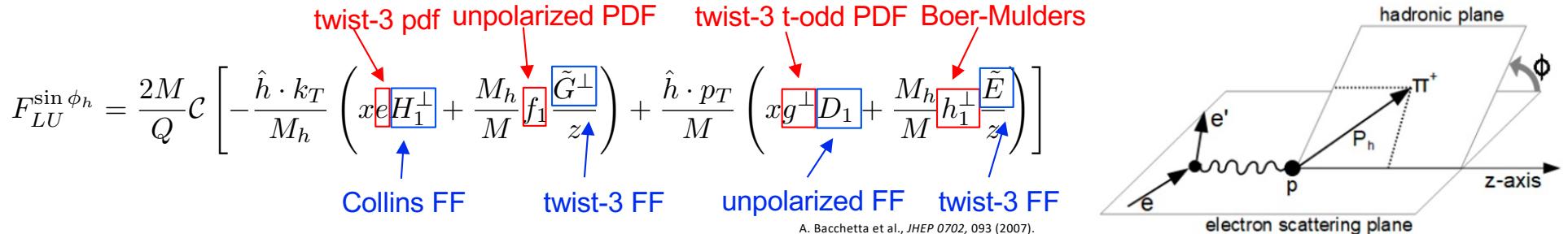
$$\frac{d\sigma^{\text{CFR}}}{dx_B dy dz_h} = \sum_a e_a^2 f_a(x_B) \frac{d\hat{\sigma}}{dy} D_a(z_h)$$

- PDFs
  - Confined motion of quarks and gluons inside the nucleus
  - Orbital motion of quarks, correlations between quarks and gluons
- Fragmentation Functions
  - Probability for a quark to form particular final state particles
  - Insight into transverse momenta and polarization

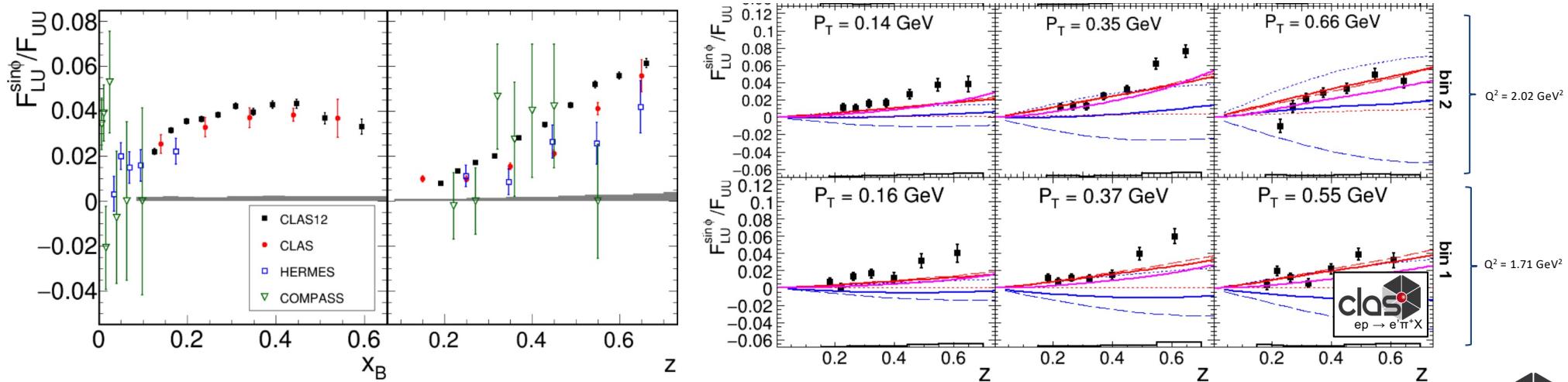


M. Anselmino et al., Phys. Lett. B. 706 (2011), 46-52, [hep-ph] 1109.1132

# Single Hadron Production



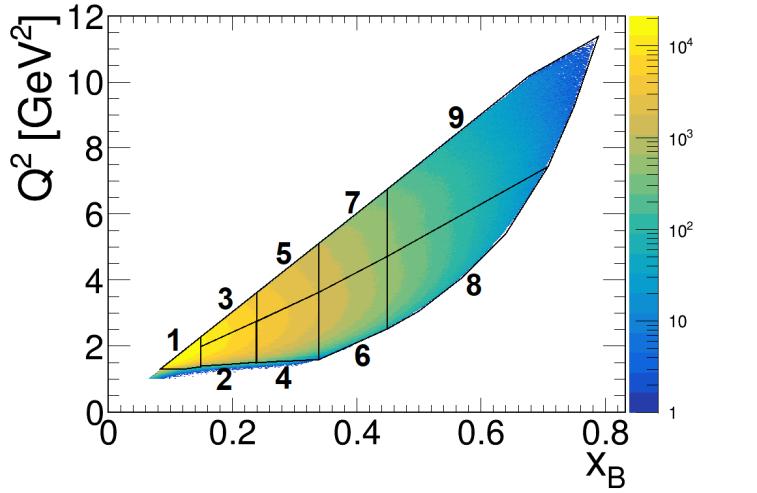
First high-precision multidimensional study: important for constraints of PDFs.



S. Diehl et al., Phys. Rev. Lett., 128, 062005, (2022), [hep:ex] 2101.03544

# Flavor Decomposition

→ Measurement of all 3 pions allows a flavor decomposition of TMDs and FFs

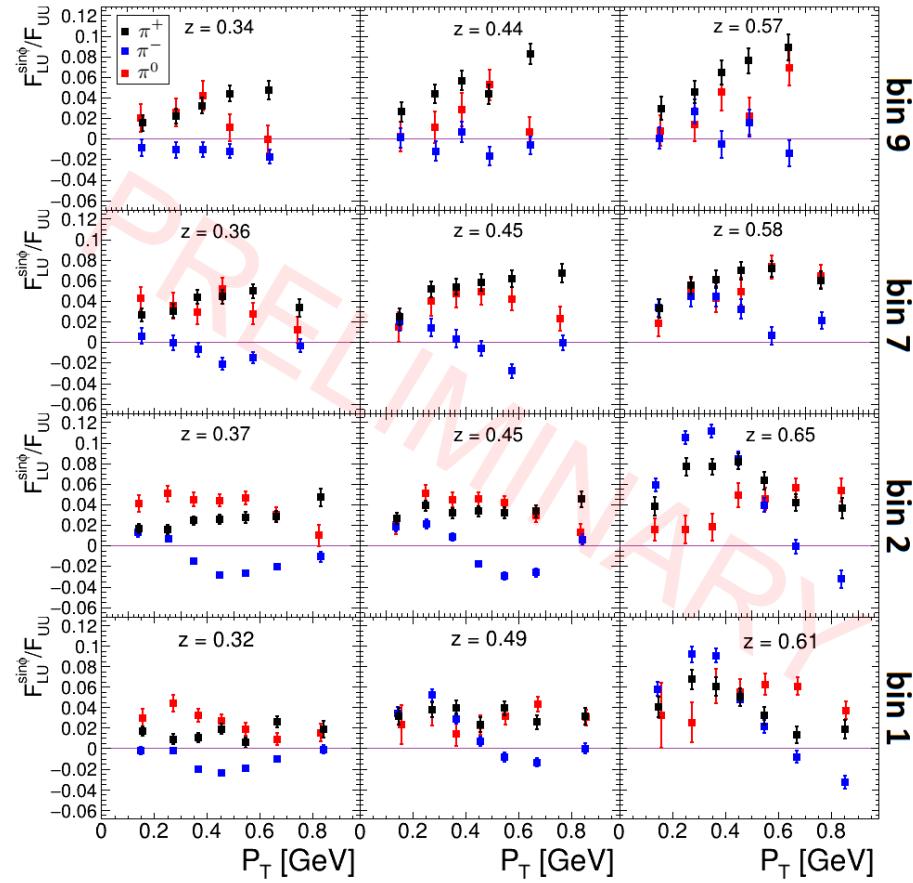


$\blacksquare \pi^+$   $\blacksquare \pi^0$   $\blacksquare \pi^-$

preliminary

S. Diehl

UCONN



# Moments of the Unpolarized SIDIS $\pi^+$ Cross-section

- Boer-Mulders Effect:** Sensitive to the correlation between the quark's transverse momentum and intrinsic transverse spin in an unpolarized nucleon; requires quark orbital angular momentum contributions to the proton spin
- Cahn Effect:** Sensitive to the transverse motion of quarks inside the nucleon

$$\frac{d^5\sigma}{dx dQ^2 dz d\phi_h dP_{h\perp}^2} = \frac{2\pi\alpha^2 y^2}{xyQ^2 2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) (F_{UU,T} + \epsilon F_{UU,L}) \left\{ 1 + \frac{\sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})} \cos\phi_h + \frac{\epsilon F_{UU}^{\cos 2\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})} \cos 2\phi_h \right\}$$

$A_0$        $A_{UU}^{\cos\phi_h}$        $A_{UU}^{\cos 2\phi_h}$

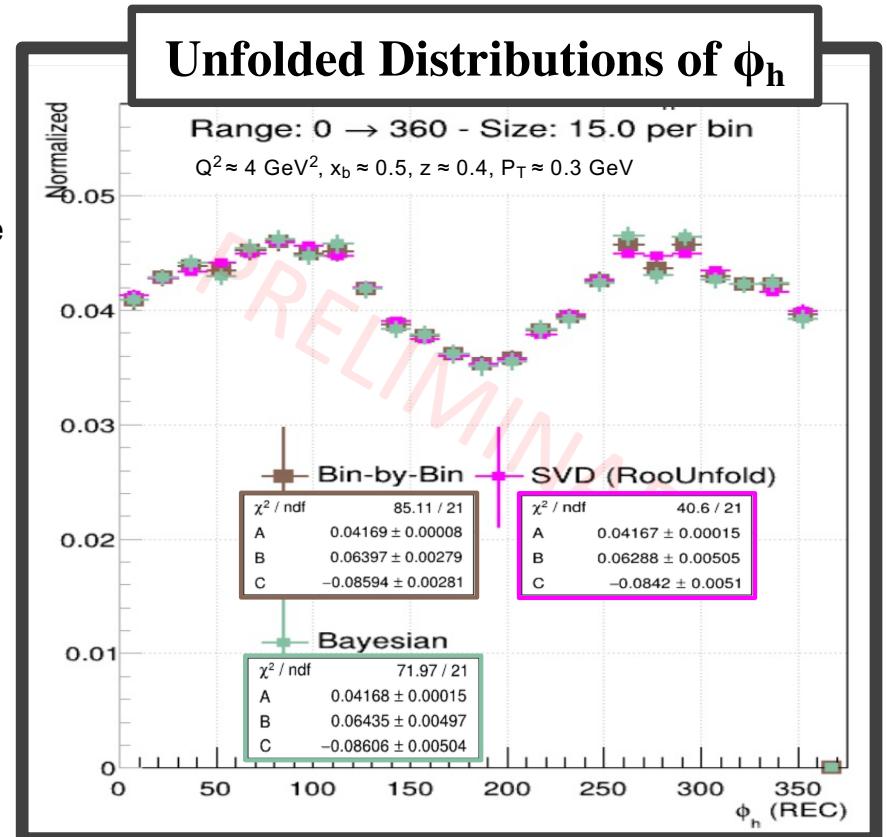
$$F_{UU}^{\cos 2\phi_h} \propto C \left[ -\frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T h_1^\perp H_1^\perp}{MM_h} + \dots \right]$$

BOER-MULDERS EFFECT

$$F_{UU}^{\cos\phi_h} \propto \frac{2M}{Q} C \left[ -\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} x h H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1 + \dots \right]$$

CAHN EFFECT

Interaction dependent terms neglected



R. Capobianco



# Neutral Pion Multiplicities

- Goal

- Measure neutral pion multiplicities

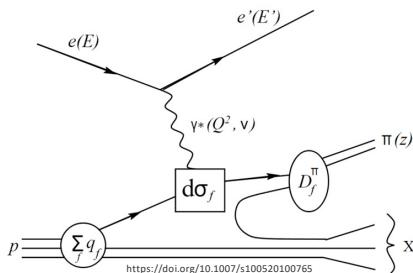
$$M_h = \frac{d\sigma^h}{dx dQ^2 dz dp_T^2} / \frac{d\sigma^{DIS}}{dx dQ^2}$$

- Related to the non-perturbative proton structure, i.e., PDFs and FFs

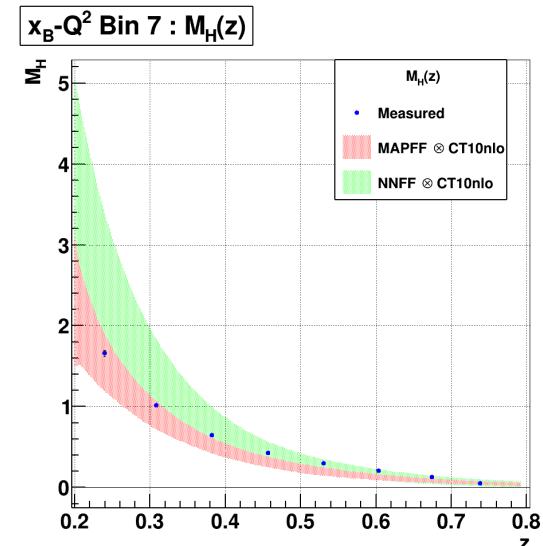
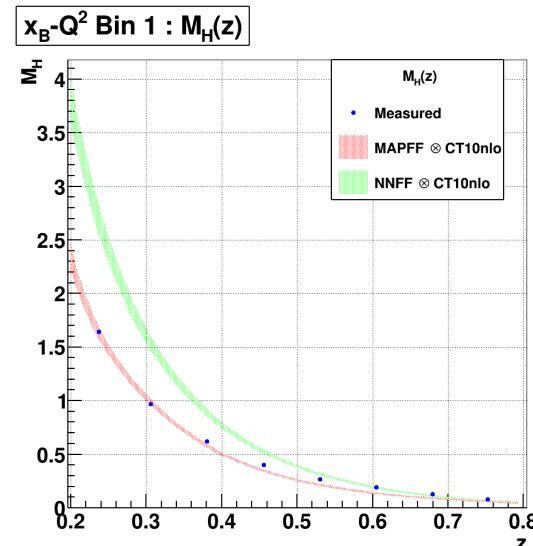
$$\sigma^{\pi^0} \approx \sigma^{DIS} \otimes f^p(x, Q^2) \otimes D^{p \rightarrow \pi^0}(z, Q^2)$$

- Connected to charged pion multiplicities

$$D_1^{\pi^0/q} = \frac{1}{2} \left( D_1^{\pi^+/q} + D_1^{\pi^-/q} \right)$$



The  $p_T^2$  integrated multiplicities have been extracted and shown to be inline with the MAPFF  $\otimes$  CT10nlo leading order predictions.

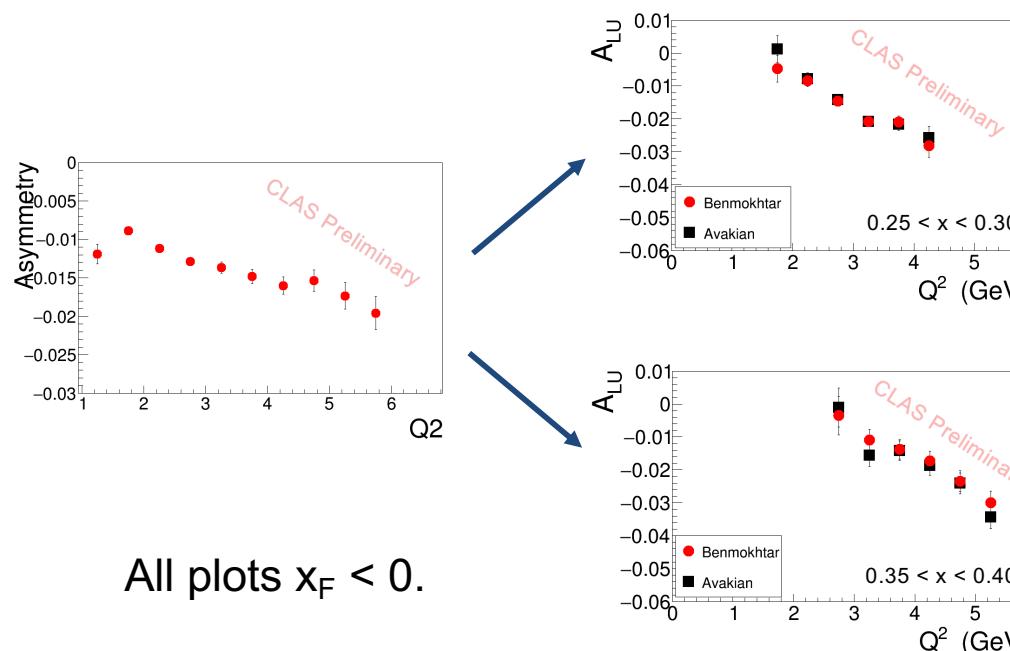


M. B. C. Scott

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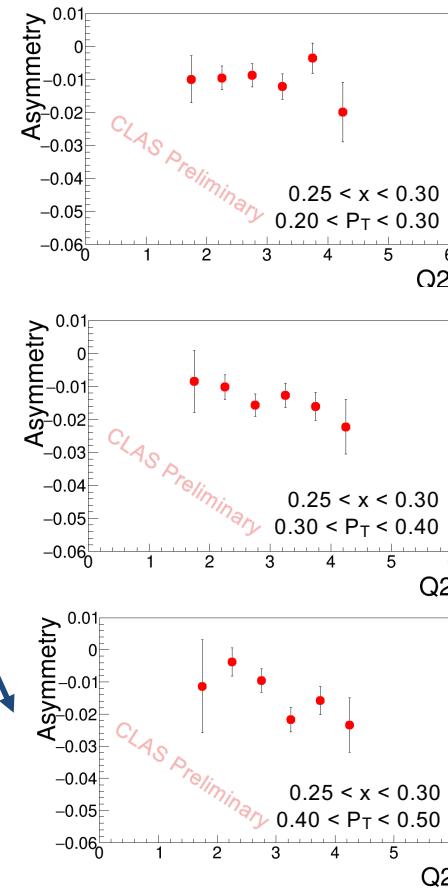
# Mapping the $Q^2$ dependence

- SSAs in single hadron production are twist-3 (M/Q suppression).
- "Twist 3" asymmetries not behaving as expected (EMC, COMPASS, CLAS12 etc!)
- Proper interpretation of the  $Q^2$  dependence is crucial for our understanding of the underlying dynamics.



Only about 1/3(1/6) of statistics collected(approved) on  $H_2$  with CLAS12!

**UCONN**



Onward to 4D

Observing the expected  $Q^2$  behavior for subleading twist objects may require high precision multidimensional bins... or maybe our theory is wrong.

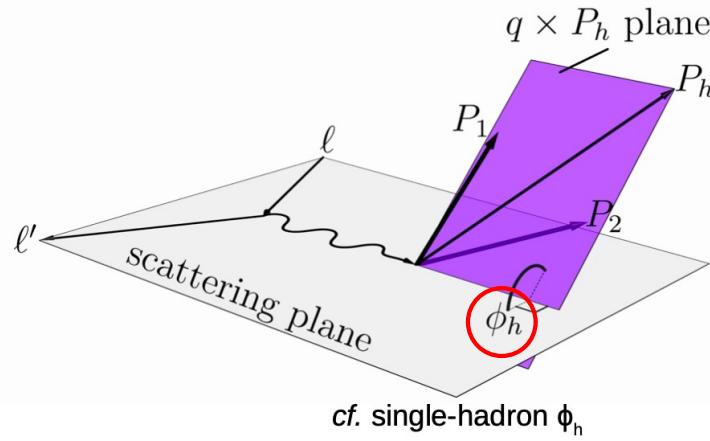


# Dihadron Kinematics

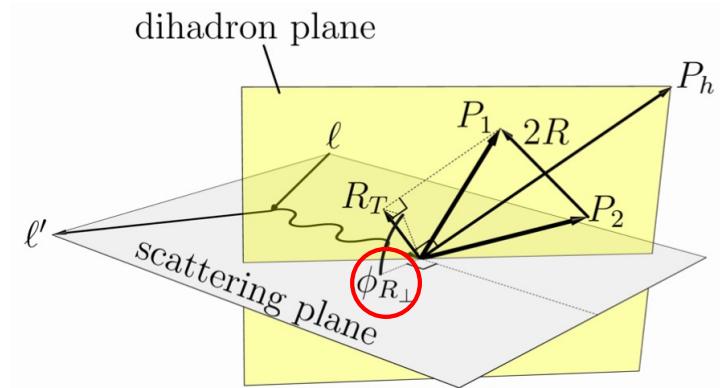
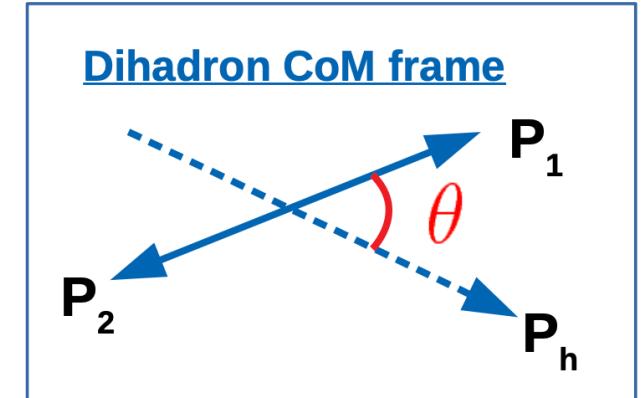
$$P_h = P_1 + P_2 \quad \text{or} \quad R = \frac{1}{2} (P_1 - P_2)$$

$$\phi_h = \frac{(\mathbf{q} \times \mathbf{l}) \cdot \mathbf{P}_h}{|(\mathbf{q} \times \mathbf{l}) \cdot \mathbf{P}_h|} \arccos \left( \frac{(\mathbf{q} \times \mathbf{l}) \cdot (\mathbf{q} \times \mathbf{P}_h)}{|\mathbf{q} \times \mathbf{l}| \cdot |\mathbf{q} \times \mathbf{P}_h|} \right)$$

$$\phi_R = \frac{(\mathbf{q} \times \mathbf{l}) \cdot \mathbf{R}_\perp}{|(\mathbf{q} \times \mathbf{l}) \cdot \mathbf{R}_\perp|} \arccos \left( \frac{(\mathbf{q} \times \mathbf{l}) \cdot (\mathbf{q} \times \mathbf{R}_\perp)}{|\mathbf{q} \times \mathbf{l}| \cdot |\mathbf{q} \times \mathbf{R}_\perp|} \right)$$

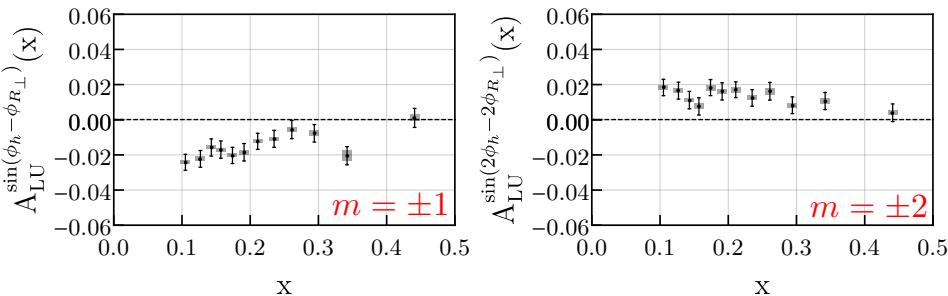


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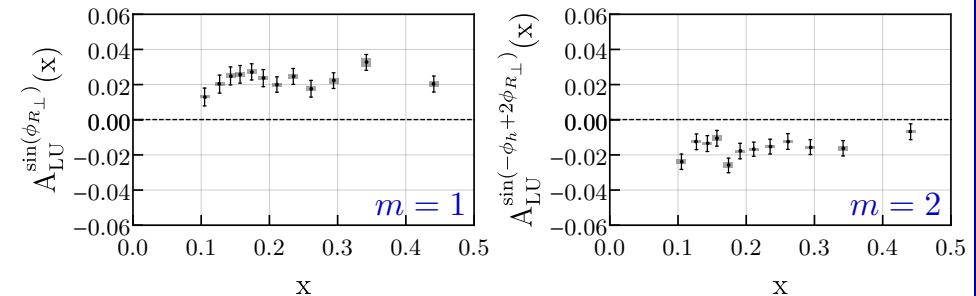


# $A_{LU}(x)$ Amplitudes

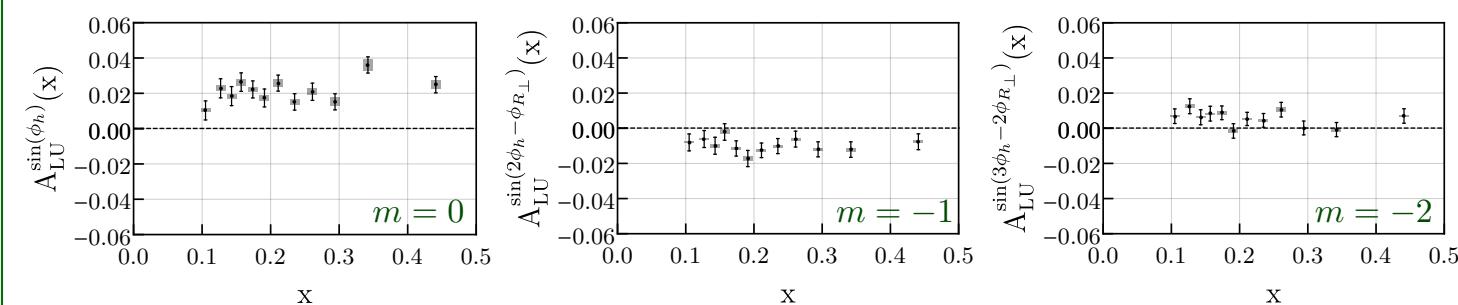
Twist 2,  $f_1(x) \otimes G_1^{\perp|\ell,m\rangle}$



Twist 3,  $e(x) \otimes H_1^{\triangleleft|\ell,m\rangle}$



Twist 3,  $e(x) \otimes H_1^{\perp|\ell,m\rangle}$



T. B. Hayward et al., *Phys. Rev. Lett.*, 126, 152501, (2021), hep-ex/2101.04842

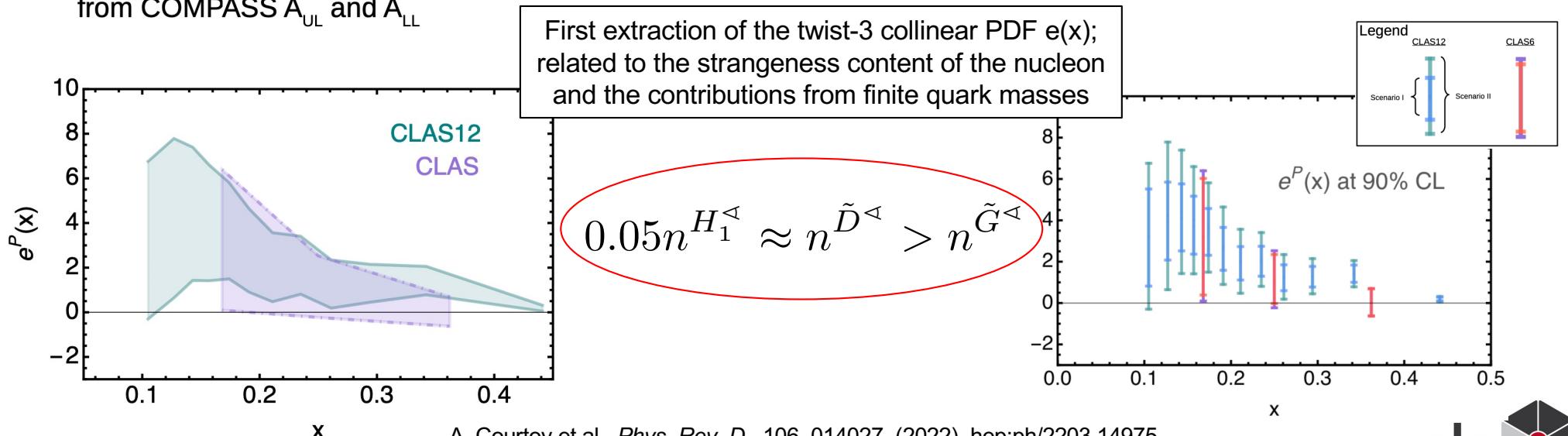
# Extraction of $e^p(x)$ , beyond WW

$$A_{LU}^{\sin \phi_R} \propto \frac{M}{Q} \frac{\sum_q e_q^2}{\sum_q e_q^2 f_1^q(x)} \left[ xe^q(x) H_{1,sp}^{\triangleleft,q}(z, m_{\pi\pi}) + \frac{m_{\pi\pi}}{z M} f_1^q(x) \tilde{G}_{sp}^{\triangleleft,q}(z, m_{\pi\pi}) \right]$$

twist-3 DiFF

## Scenario II: Beyond WW approximation

- Estimate max integrated twist-3 DiFF from COMPASS  $A_{UL}$  and  $A_{LL}$



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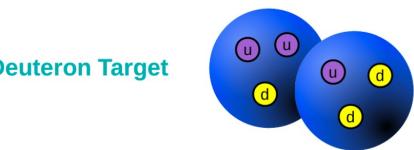
A. Courtoy et al., *Phys. Rev. D.*, 106, 014027, (2022), hep-ph/2203.14975  
also [A. Courtoy at CPHI2022](#)

clas

# Twist-3 PDF Flavor Dependence

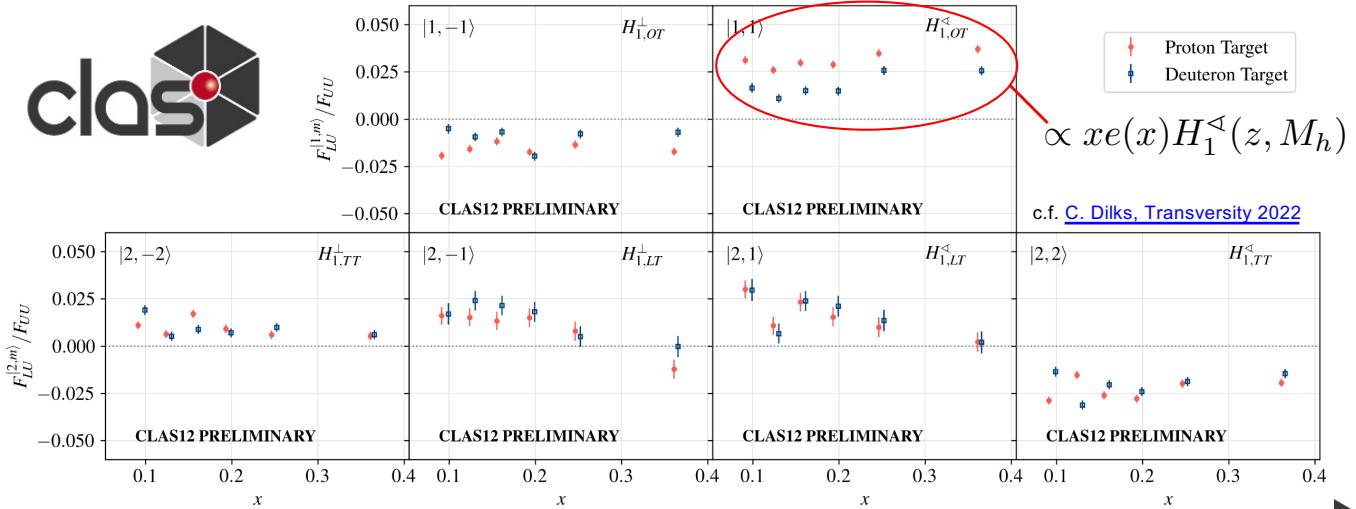
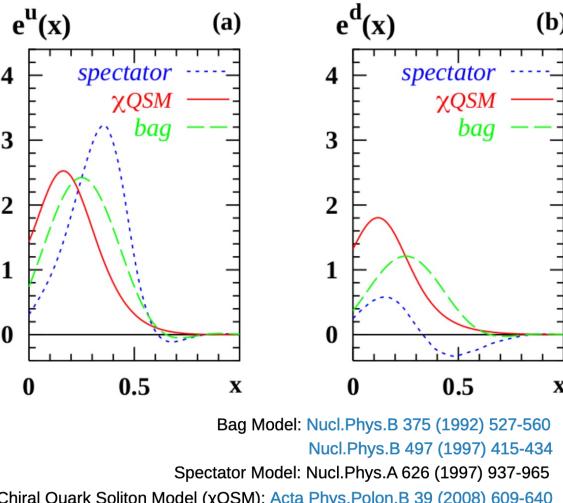


$$A_{LU,p}^{\text{twist } 3} \propto 4xe^{u_V}(x) - xe^{d_V}(x)$$



$$A_{LU,d}^{\text{twist } 3} \propto xe^{u_V}(x) + xe^{d_V}(x)$$

Ongoing full partial wave analysis and comparison between proton and deuteron targets could lead to the flavor decomposition of the scalar PDF.



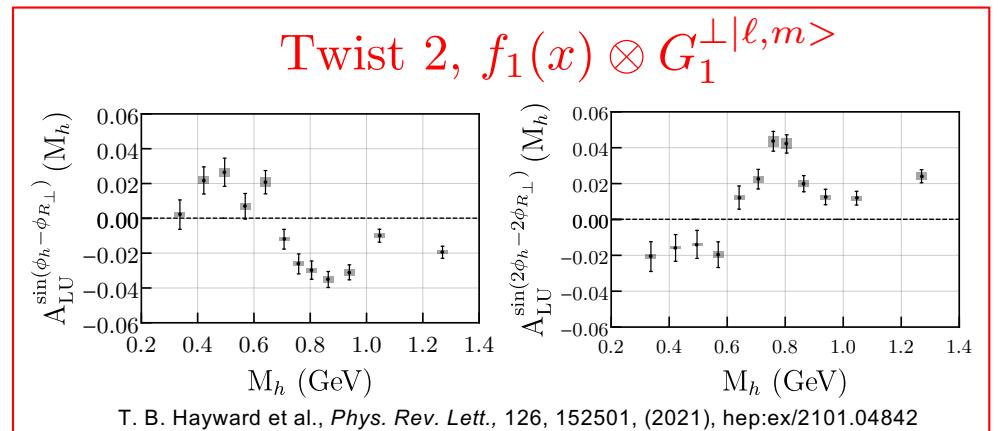
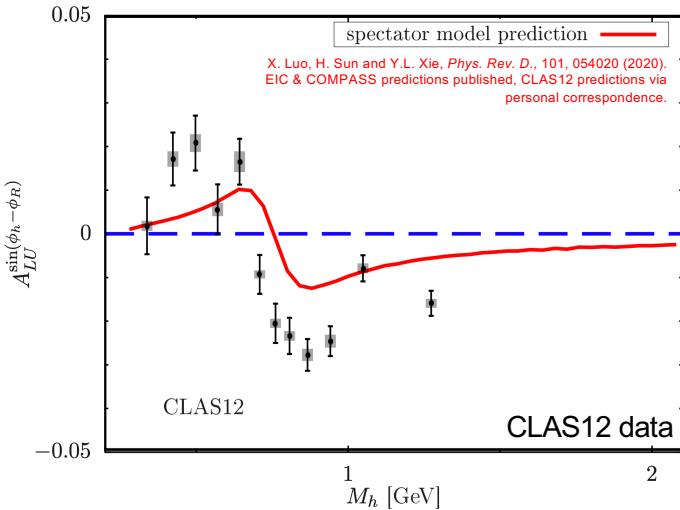
C. Dilks & T.B. Hayward

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# First Observation of TMD DiFF $G_1^{\perp}$

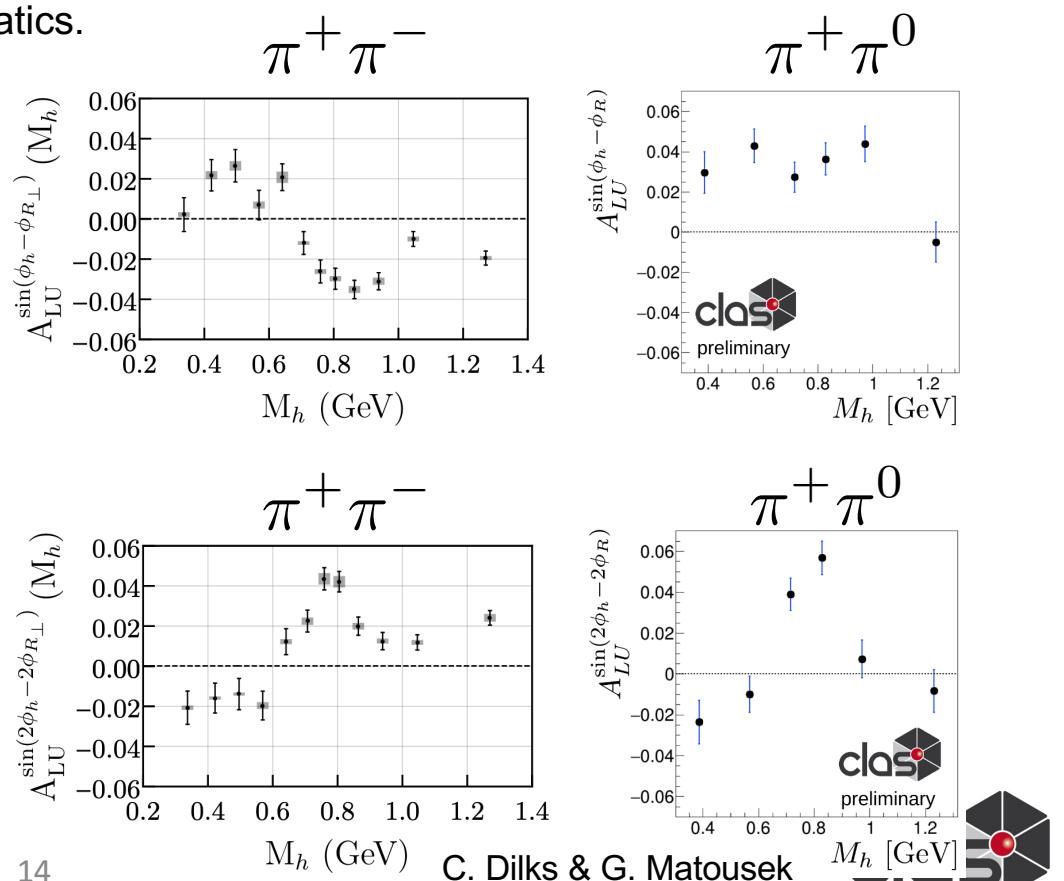
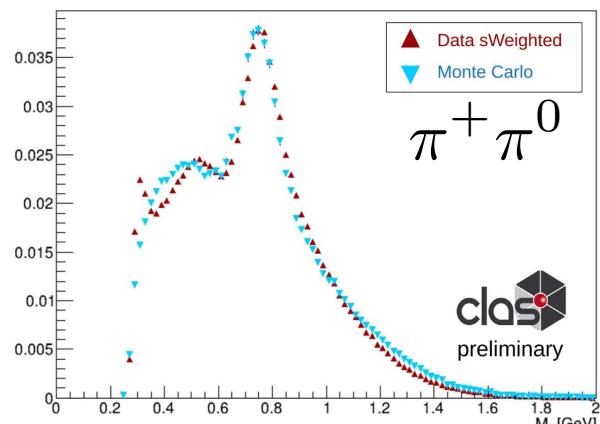
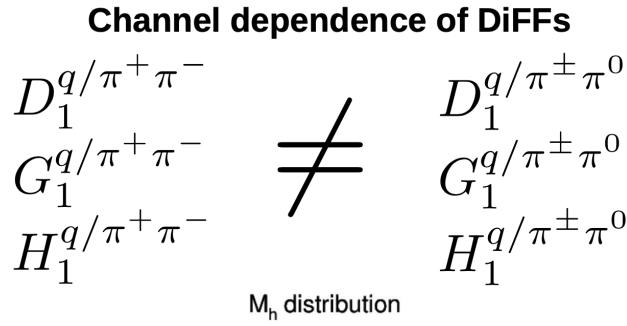
- Results correspond to the first ever experimental signal sensitive to the helicity dependent DiFF.
- Confirmation that the produced pions depend on the helicity of the fragmenting quark.



- Results are consistent with model predictions for a sign change around the  $\rho$ -meson mass.
- This corresponds to an interference term between s- and p- wave dihadron production.

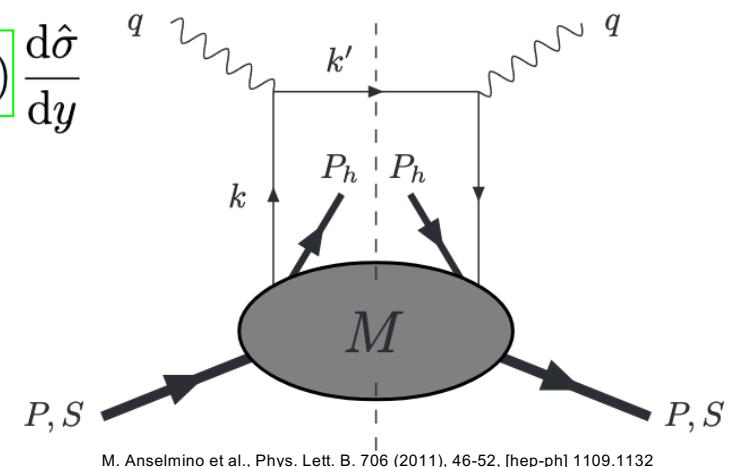
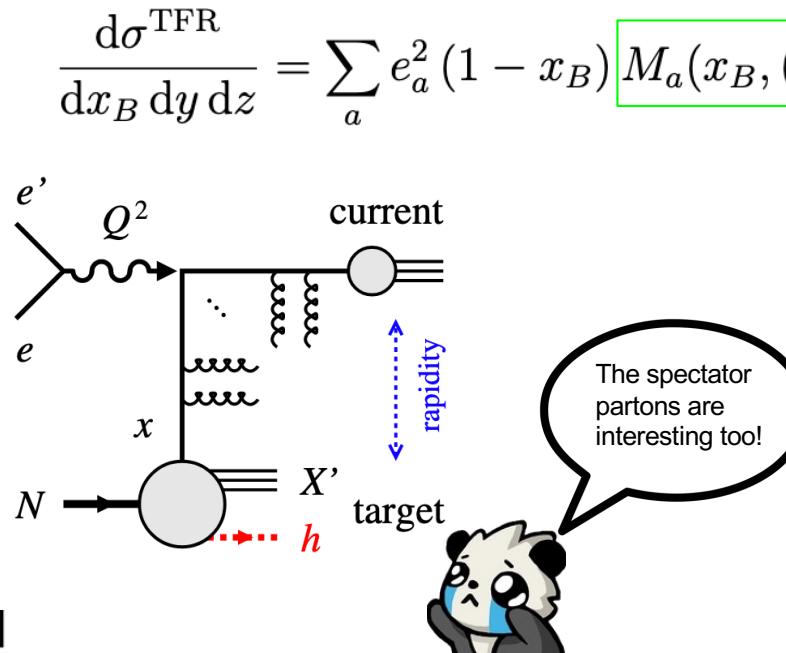
# Channel Dependence of DiFFs

The study of other pion flavor combinations gives access to the flavor dependence of DiFFs while testing the effects of different systematics.



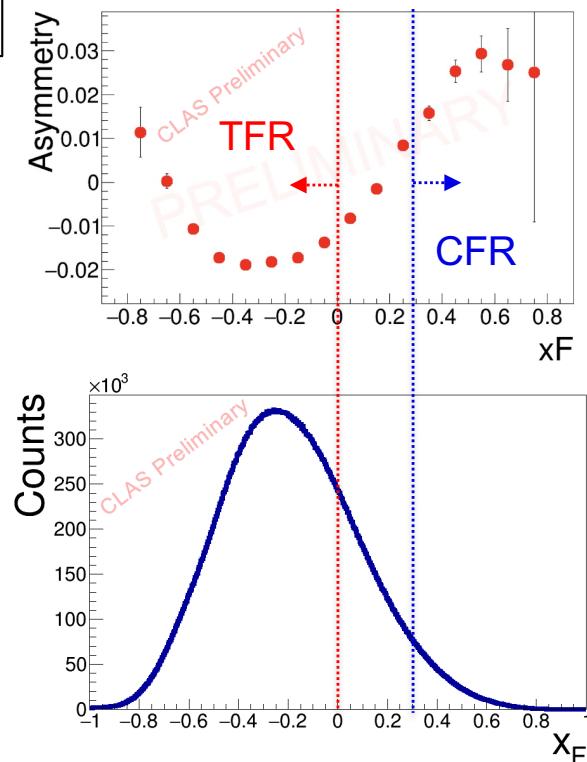
# The Neglected Hemisphere – Target Fragmentation

- Final state hadrons also form from the left-over target remnant (TFR) whose partonic structure is defined by “fracture functions”<sup>1,2</sup>: the probability for the target remnant to form a certain hadron given a particular ejected quark.
- In the TFR, factorization into  $x$  and  $z$  does not hold because it is not possible to separate quark emission from hadron production.



1. L. Trentadue and G. Veneziano, Phys. Lett. B323 (1994) 201,
2. M. Anselmino et al., Phys. Lett. B. 699 (2011), 108-118, [hep-ph] 1102.4214
3. TFR/CFR Fig. from EIC Yellow Report, (2021) [physics.ins-det] 2103.05419

# Can We Separate Target and Current?



F. Benmokhtar, H. Avakian, T.B. Hayward

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**Feynman variable**

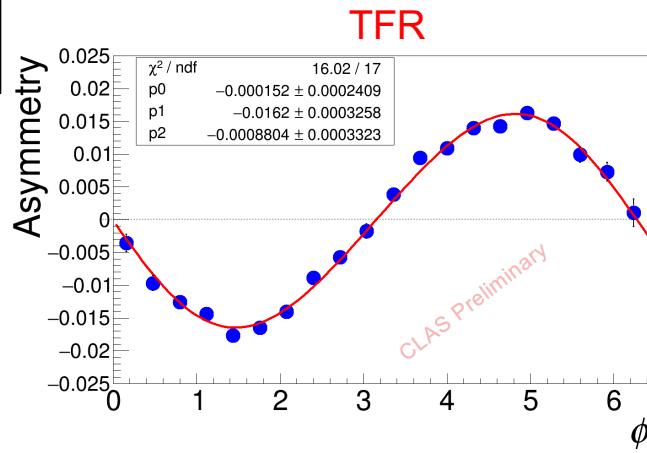
$$x_F = \frac{p_h^z}{p_h^z(\max)} \text{ in CM frame } \mathbf{p} = -\mathbf{q}, \quad -1 < x_F < 1$$

**Rapidity**

$$y = \frac{1}{2} \log \frac{p_h^+}{p_h^-} = \frac{1}{2} \log \frac{E_h + p_h^z}{E_h - p_h^z}$$

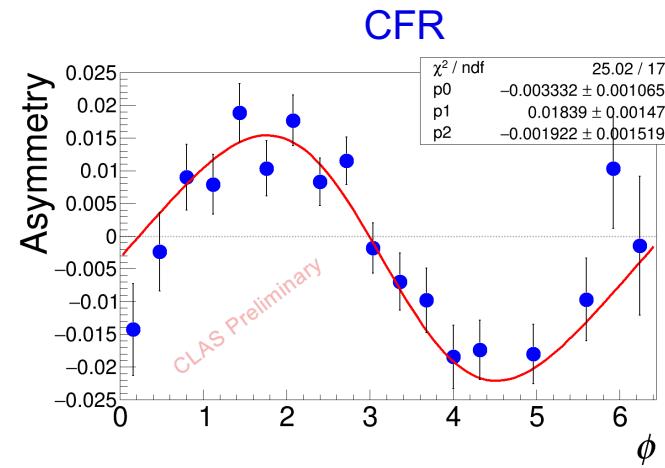
- No clear *experimental* definition of what constitutes current production versus target production.
- Structure functions, with different production mechanisms in both regions, give a possible clue.
- Protons (as opposed to mesons) at CLAS12 kinematics give a unique opportunity because they have extensive coverage in both regions.

# Separate Signals



$$F_{LU}^{\sin \phi} \propto \frac{2M}{Q} \left[ \tilde{l}_2^\perp h + \dots \right]$$

Need more theory calculations!



$$F_{LU}^{\sin \phi} \propto \frac{2M}{Q} C \left[ -\frac{\hat{h} \cdot k_T}{M_h} \left( xeH_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot p_T}{M} \left( xg^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right]$$

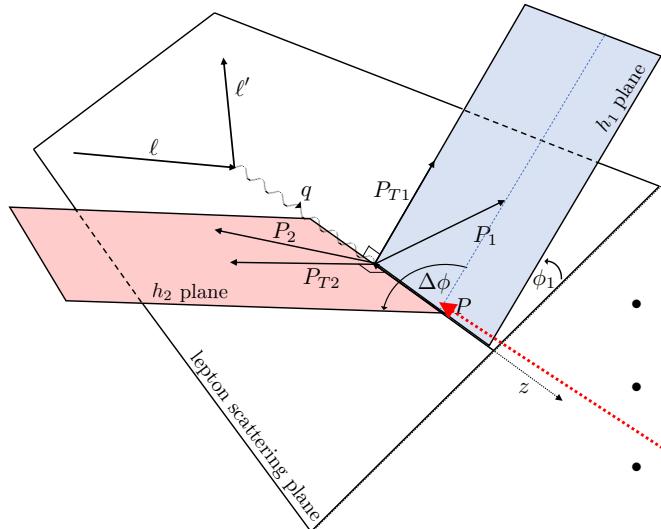
F. Benmokhtar, H. Avakian, T.B. Hayward

- Sinusoidal modulations (that are probably) coming from the struck quark and the spectator partons appear with roughly equal amplitudes but opposite signs.

# Back-to-back (dSIDIS) Formalism

- When two hadrons are produced “back-to-back”<sup>1,2</sup> with one in the CFR and one in the TFR the structure function contains a convolution of a **fracture function** and a **fragmentation function**.
- Leading twist beam(target)-spin asymmetry.

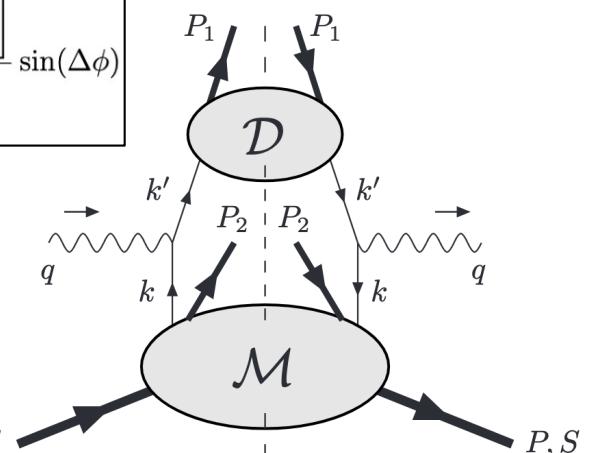
$\hat{l}_1^{\perp h}$  Unique access to longitudinally polarized quarks in unpolarized nucleon... no corresponding PDF!



Kinematic plane for b2b dihadron production.

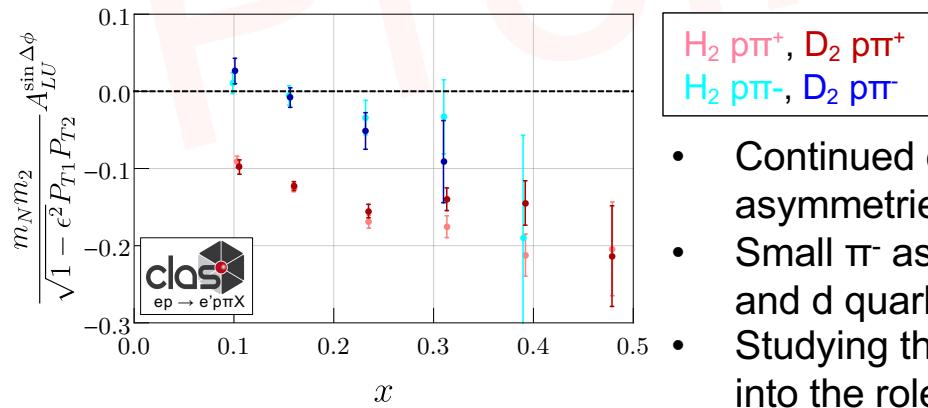
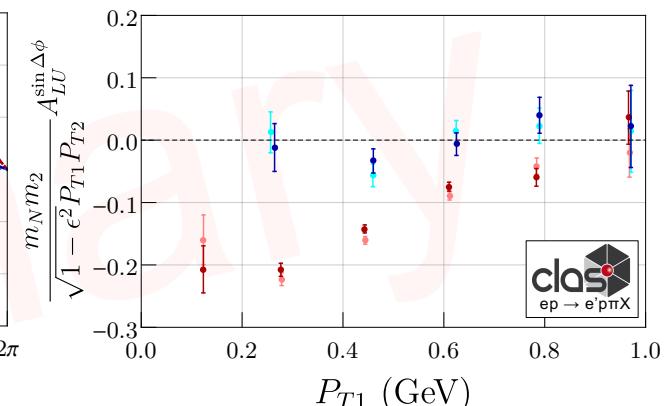
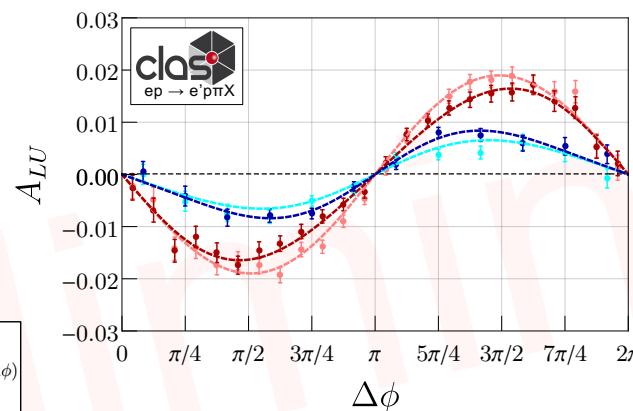
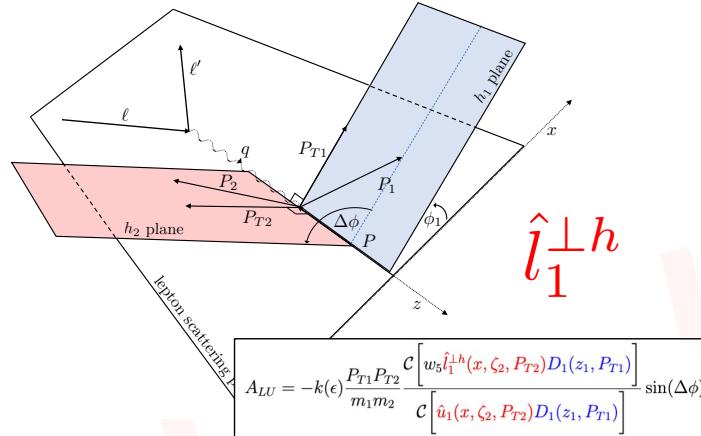
$$A_{LU} = -k(\epsilon) \frac{P_{T1}P_{T2}}{m_1m_2} \frac{\mathcal{C} \left[ w_5 \hat{l}_1^{\perp h}(x, \zeta_2, P_{T2}) D_1(z_1, P_{T1}) \right]}{\mathcal{C} \left[ \hat{u}_1(x, \zeta_2, P_{T2}) D_1(z_1, P_{T1}) \right]} \sin(\Delta\phi)$$

- $h_1$  in the CFR with production dictated by the **fragmentation function**
- $h_2$  in the TFR with production dictated by the **fracture function**
- Long range correlation depends on the difference in azimuthal angles of both hadrons



Handbag diagram for dihadron production; lower blob contains FrFs and upper blob contains the FFs.

# Back-to-back (dSIDIS) Measurements



- Unique access to longitudinally polarized quarks in unpolarized nucleon... no corresponding PDF!

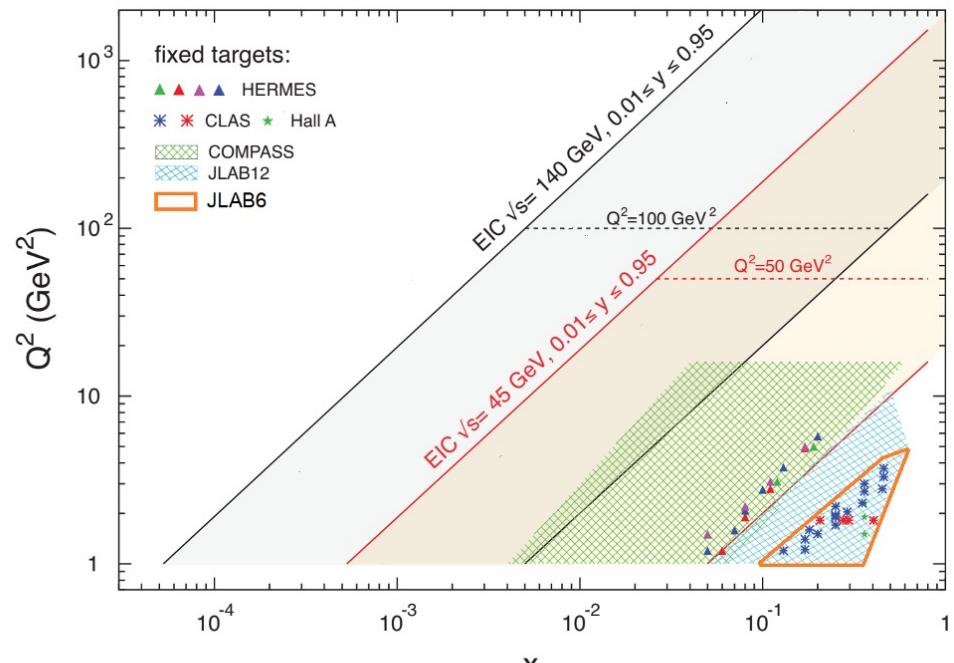
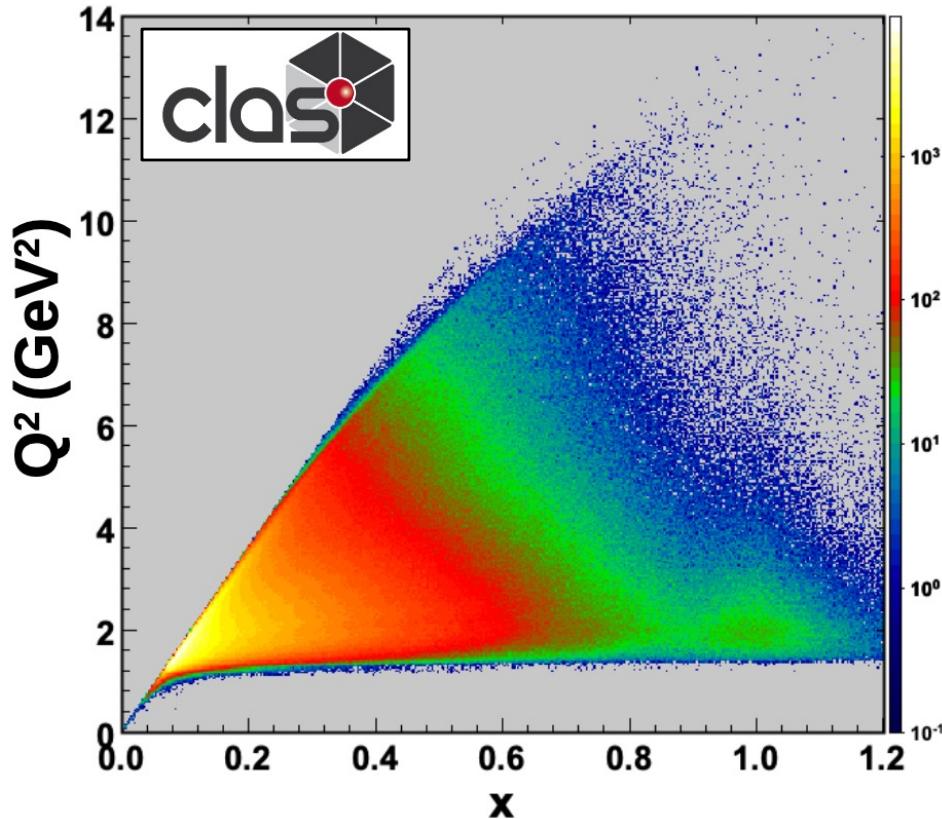
- Continued evidence that the driving force behind SIDIS asymmetries is determined by the struck quark.
- Small π- asymmetries are consistent with cancellation between u and d quark.
- Studying the transverse momentum dependence can give insight into the role played by vector mesons.

# Conclusions

- CLAS12 is an ideal place to study the multiparticle final state processes that are critical to SIDIS.
- The Hall-B and CLAS12 physics program features a diverse set of analyses covering many different target types and final state observables.
- Several high-quality publications already with many more in progress including upcoming polarized target measurements.

# Back up

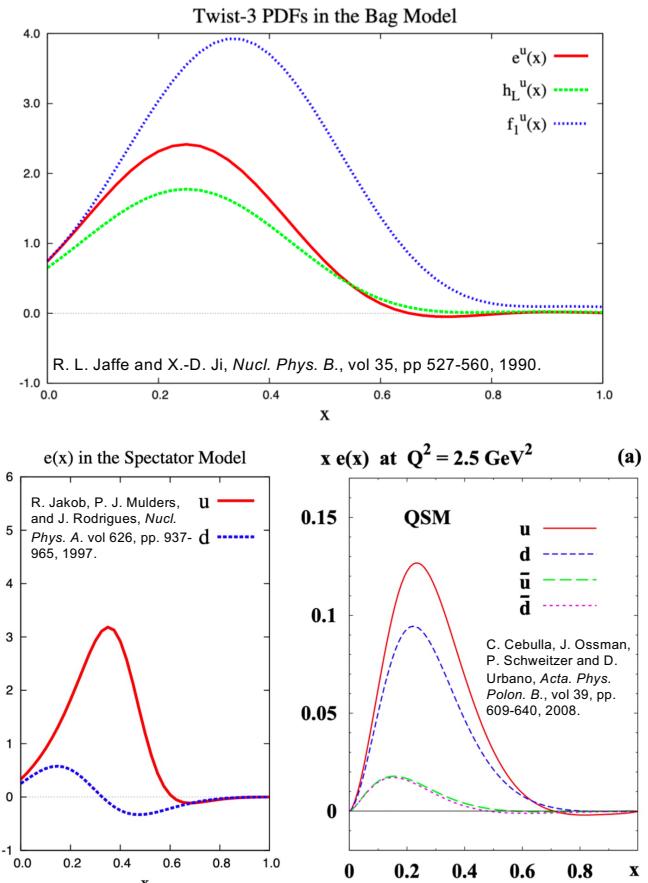
# CLAS12 Kinematic Reach



JLab: Valence quark distribution  
Compass: Sea quark distribution  
EIC: Gluon distribution

# The twist-3 TMD/PDF $e(x)$

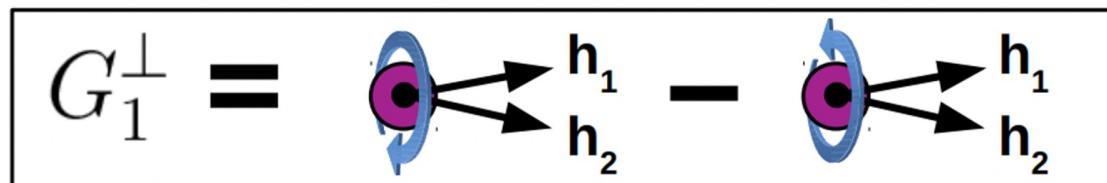
- One of the six collinear PDFs; offers insight into largely unexplored quark-gluon correlations.
- $\int e(x)dx \rightarrow$  related to the strangeness content of the nucleon and the contributions from finite quark masses; arises in chiral perturbation theory to measure explicit symmetry breaking due to nonzero masses of the light quarks. (Also appears in dark matter studies!)
- $\int x e(x)dx \rightarrow$  proportional to the number of valence quarks in the nucleus.
- $\int x^2 e(x)dx \rightarrow \perp$  force on  $\perp$  polarized quarks in a unpolarized nucleon, related to the “Boer-Mulders”
- Although the PDF  $e(x)$  has been studied extensively in models, direct experimental access has remained relatively scarce



# Helicity Dependent DiFF

- Dihadron studies allow for the existence of FFs with no single hadron analog.
- The TMD DiFF  $G_1^\perp$  describes the azimuthal dependence of an unpolarized hadron pair on the helicity of the struck quark, “jet handedness”.<sup>1</sup>
- **Completely unmeasured;** exciting opportunity to study spin-momentum dynamics in hadronization.

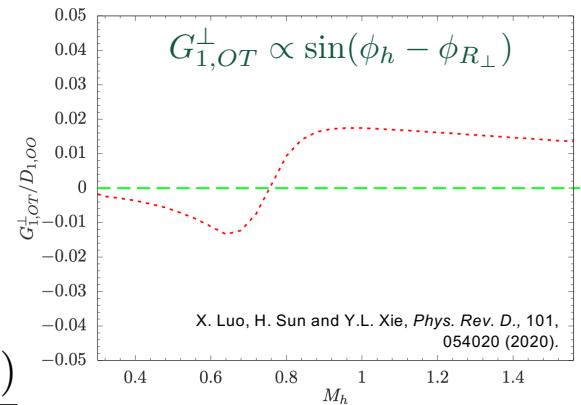
<sup>1</sup> D. Boer, R. Jakob, and M. Radici, Phys. Rev. D67 (2003) 094003, hep-ph/0302232



$$A_{LU}^{\sin(\phi_h - \phi_{R\perp})} = \frac{\int d_{LU} (P_h^\perp/M_h) \sin(\phi_h - \phi_{R\perp})}{\int d_{UU}} \propto \frac{\sum z f_1(x) G_1^\perp(z, M_h)}{\sum f_1(x) D_1(z, M_h)}$$

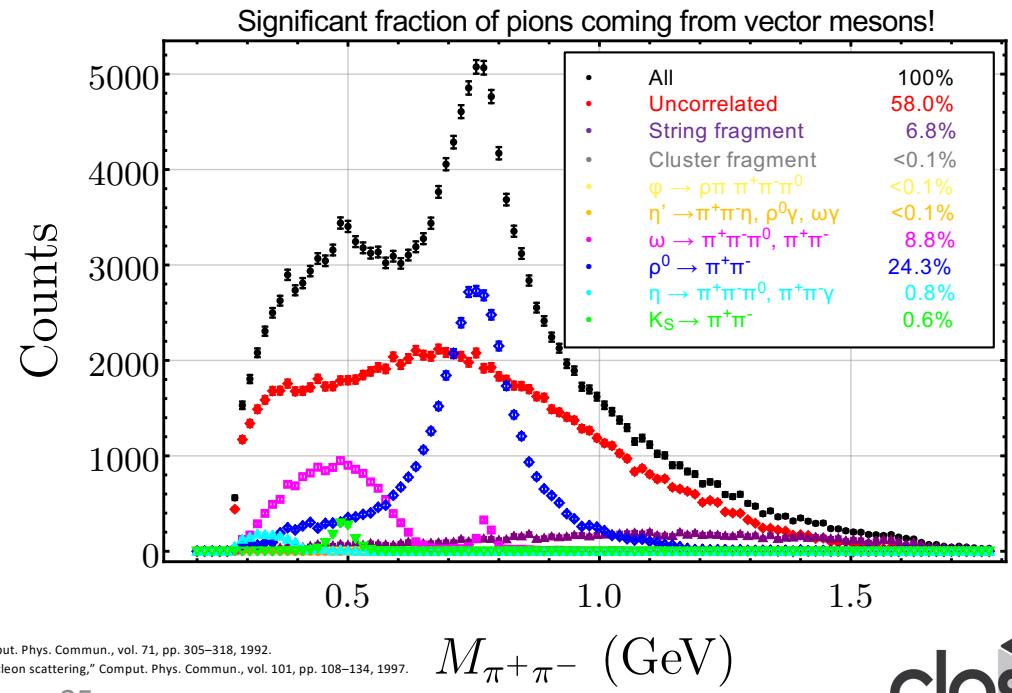
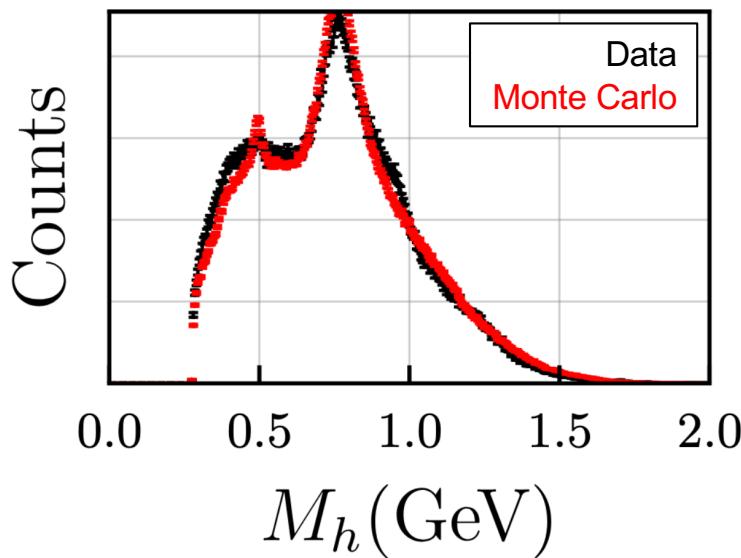
H. H. Matevosyan, A. Kotzinian, and A. W. Thomas, Phys. Rev. Lett., 120, 252001 (2018)

unpolarized PDF  
unpolarized FF



# Monte Carlo and Vector Mesons

- SIDIS MC “clasdis”<sup>1</sup> based on PEPSI<sup>2</sup> generator, the polarized version of the well-known LEPTO<sup>3</sup> generator.
- Parameters changed to reproduce observed distributions include average transverse momentum, fraction of spin-1 light mesons and fraction of spin-1 strange mesons.
- CLAS12 detector system described in “GEMC”<sup>4</sup>, a detailed GEANT4 simulation package.

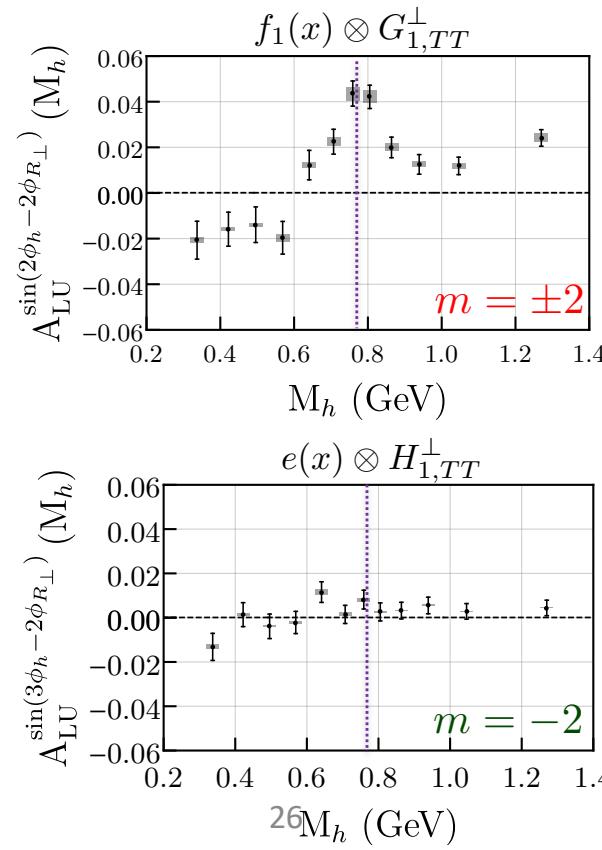
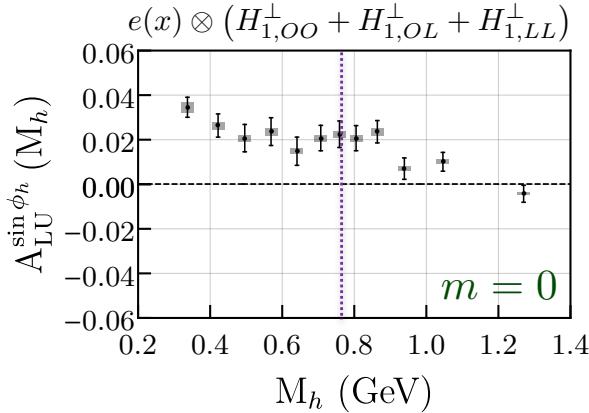


1. H. Avakian, “clasdis,” <https://github.com/JeffersonLab/clasdis>, 2020.
2. L. Mankiewicz, A. Schafer, and M. Veltri, “Pepsi: A monte carlo generator for polarized leptoproduction,” *Comput. Phys. Commun.*, vol. 71, pp. 305–318, 1992.
3. G. Ingelman, A. Edin, and J. Rathsman, “LEPTO 6.5: A Monte Carlo generator for deep inelastic 912 lepton - nucleon scattering,” *Comput. Phys. Commun.*, vol. 101, pp. 108–134, 1997.
4. M. Ungaro et al., “The CLAS12 Geant4 simulation,” *Nucl. Instrum. Meth. A*, vol. 959, p. 163422, 2020.

# Significant Effects From Vector Mesons

Recall that  $l = 0, 1$  and  $2$  terms correspond to ss, sp and pp wave dihadron interference. Enhancement is seen around the  $\rho$ -meson mass for several modulations.

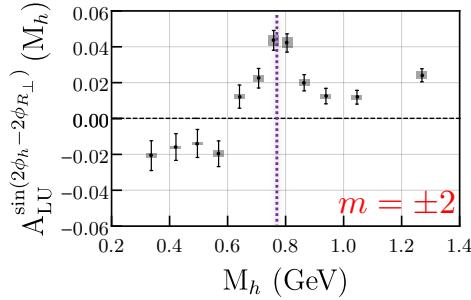
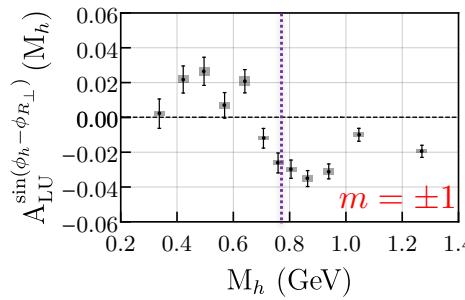
- $m=0$ , ss term is relatively flat.



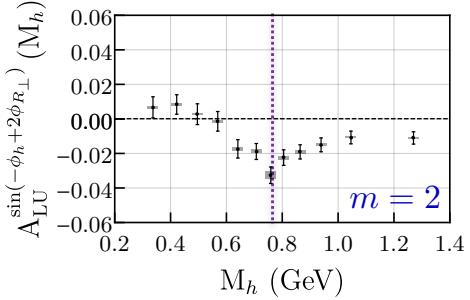
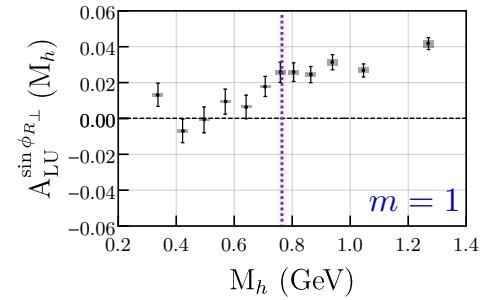
- $m = 2$  amplitudes increasing rapidly around the  $\rho$  mass
- twist-3,  $m = -2$  amplitude is relatively small  $H_{1,TT}^\perp \approx 0$ ?

# $A_{LU}(M_h)$ Amplitudes

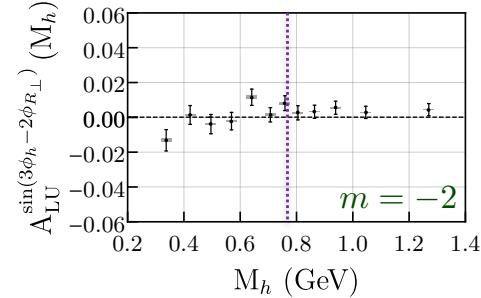
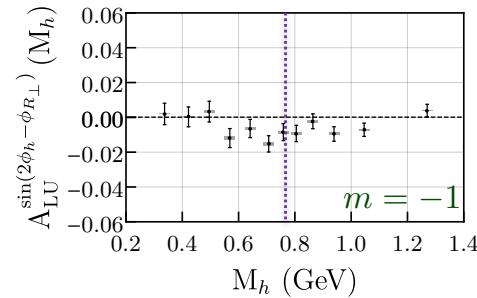
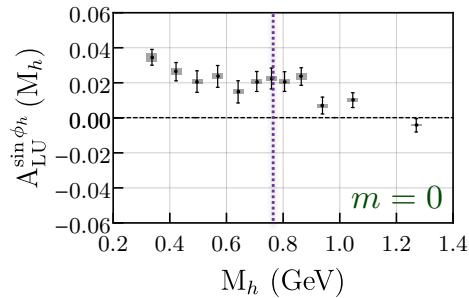
Twist 2,  $f_1(x) \otimes G_1^{\perp|\ell,m\rangle}$



Twist 3,  $e(x) \otimes H_1^{\triangleleft|\ell,m\rangle}$



Twist 3,  $e(x) \otimes H_1^{\perp|\ell,m\rangle}$

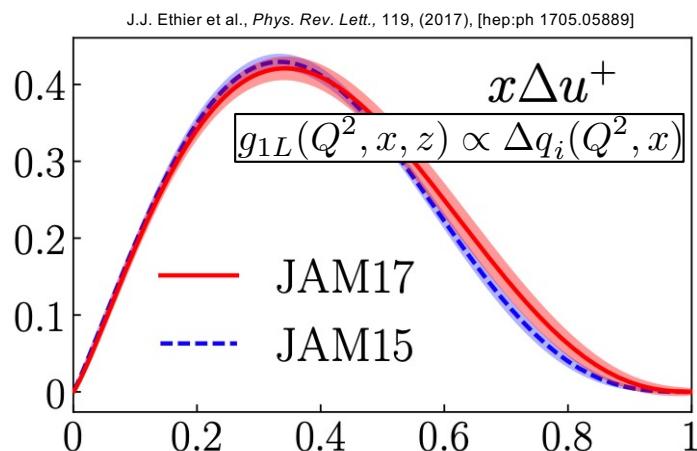


# A<sub>LL</sub> – The Best of Both Worlds

$$\frac{d\sigma}{dxdydzdP_T^2} = 2\pi\hat{\sigma}_U \sum_q e_q^2 \left[ F_{UU,T} + \lambda S_L \sqrt{1-\varepsilon^2} F_{LL} \right]$$

M. Anselmino et al., Phys. Lett. B. 699 (2011), 108, [hep-ph] 1102.4214

At leading twist for the case of a longitudinally polarized target and a single hadron produced in the TFR, only two terms appear:



J.J. Ethier et al., Phys. Rev. Lett., 119, (2017), [hep-ph 1705.05889]

$$F_{UU,T} \propto \tilde{u}_1(x, \zeta, P_T^2) = \int d^2 k_T \hat{u}_1$$

$$F_{LL} \propto \tilde{l}_{1L}(x, \zeta, P_T^2) = \int d^2 k_T \hat{l}_{1L}$$

**Double Spin Asymmetry:**  $A_{LL} = \lambda_\ell S_L \frac{\sqrt{1-\varepsilon^2} F_{LL}}{F_{UU,T}}$

1. Single hadron → Highest statistics
2. Leading twist → Simple interpretation
3. Linked to  $g_1$  → easiest test of FrF prediction

$$\sum_h \int \zeta d\zeta \int d^2 P_T \hat{l}_{1L} = (1-x) g_{1L}(x, k_T^2)$$

# Collinear twist-3 PDF $h_L(x)$

## $h_L(x)$

- Average longitudinal gradient of the transverse force on a transversely polarized struck quark in a longitudinally polarized nucleon

$$\mathcal{L}_{JM}^q - L_{Ji}^q = \Delta L_{FSI}^q$$

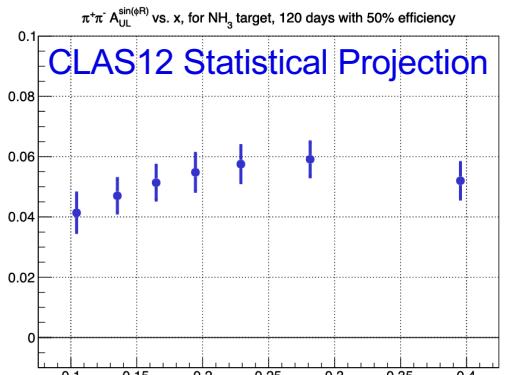
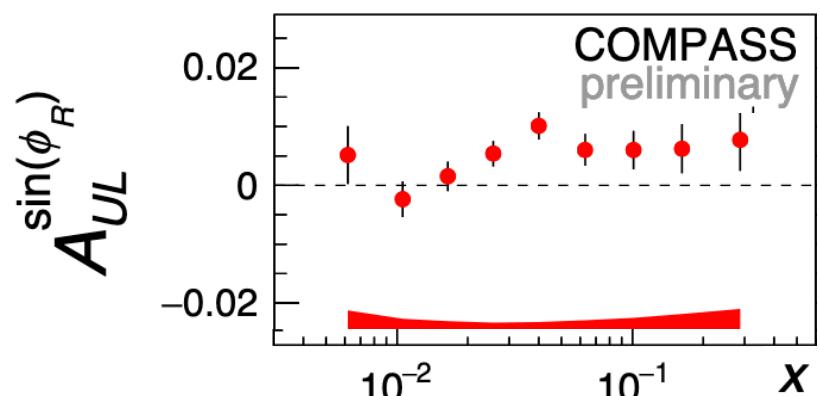
Expressible in terms of the change in quark OAM as it leaves the target

- Phys.Rev.D 94 (2016) 9, 094040
- Phys.Rev.D 66 (2002) 114005
- Nucl.Phys.B 461 (1996) 197-237

$$A_{UL}^{\sin(\phi_R)}(x, M_h, z; Q, y) = -\frac{W(y)}{A(y)} \frac{M}{Q} \frac{|\mathbf{R}|}{M_h} \frac{\sum_q e_q^2 \left( x h_L^q(x) H_1^{\triangleleft, q}(z, M_h) + \frac{M_h}{z M} g_1^q(x) \tilde{G}_{sp}^{\triangleleft, q}(z, M_h) \right)}{\sum_q e_q^2 f_1^q(x) D_{1,ss+pp}^q(z, M_h)}$$

A. Bacchetta and M. Radici, Phys.Rev. D69, 074026 (2004), arXiv:hep-ph/0311173 [hep-ph]

- CLAS12 began taking data on a longitudinally polarized target last year.
- Will access additional twist-3 collinear PDF with similar or better statistical precision as COMPASS but at higher x.



# Why fracture functions?

- Sometimes possible to kinematically separate CFR and TFR (some jets, high energy DY, etc) ... but not always clear (fixed target experiments).
- Without an understanding of the signals we expect from target fragmentation we may misinterpret results that we expect are from the current.
- Studying the TFR tests our complete understanding of the SIDIS production mechanism while also providing access to information not available in the CFR.
- Access to more familiar TMD/PDFs through momentum sum rules, but with different systematics.