DVCS with CLAS and CLAS12 and the mechanical properties of the proton

Hadron Physics
Beyond Tomography

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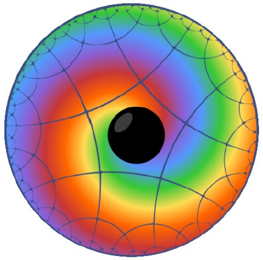
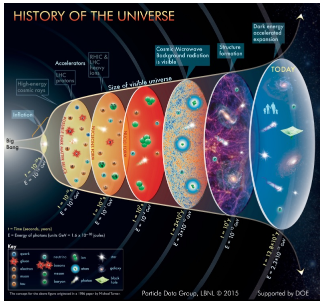
CENTER *for* NUCLEAR FEMTOGRAPHY

Basic questions about the proton

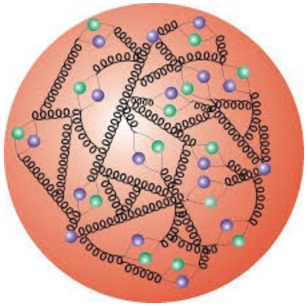
- Proton's make up nearly 90% of the (normal) matter in the universe. Elementary valence quarks contribute only few percent to the proton mass. What is the origin of its mass?



- How did quarks hadronize and form protons as the universe cooled below the Hagedorn temperature? What is the origin of confinement ?



- How are the strong forces distributed in space to keep quarks confined and make protons stable particles.



Fundamental global properties of the proton

The structure of strongly interacting particles can be probed by means of the other fundamental forces: *electromagnetic*, *weak*, and (in principle) *gravity*.

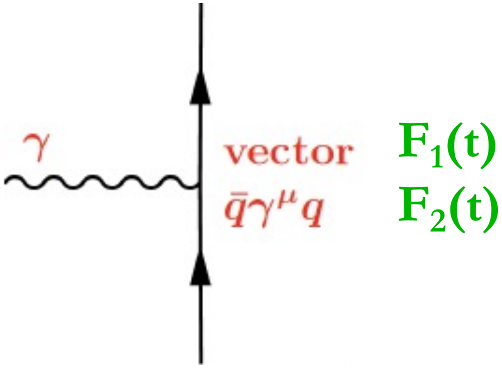
em:	$\partial_\mu J^\mu_{\text{em}} = 0$	$\langle N' \vert J^\mu_{\text{em}} \vert N \rangle$	$\longrightarrow$	Q_{prot}	$=$	$1.602176487(40) \times 10^{-19}\text{C}$
	vector			μ_{prot}	$=$	$2.792847356(23)\mu_N$
weak:	PCAC	$\langle N' \vert J^\mu_{\text{weak}} \vert N \rangle$	$\longrightarrow$	g_A	$=$	$1.2694(28)$
	axial			g_p	$=$	$8.06(0.55)$
gravity:	$\partial_\mu T^{\mu\nu}_{\text{grav}} = 0$	$\langle N' \vert T^{\mu\nu}_{\text{grav}} \vert N \rangle$	$\longrightarrow$	M_{prot}	$=$	$938.272013(23)\,\text{MeV}/c^2$
				J	$=$	$\frac{1}{2}$
	tensor			D	$=$	**?**

P. Schweitzer et al., arXiv:1612.0672, 2016.

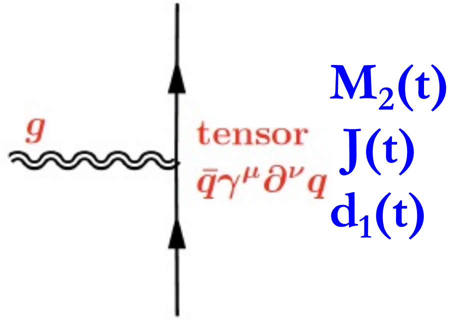
The D-term is the "last unknown global property" of the nucleon

Probing basic properties of the proton

- **Electromagnetic properties:** probed with photons
  - **Charge** - electromagnetic form factors, inelastic structure functions, proton charge radius, charge densities and current densities for N & N*
  - **Magnetic moment** - helicity densities



- **Gravitational properties:** probed with gravitons
  - **Mass:** energy and mass densities
  - **Spin:** angular momentum distribution
  - **D-term:** dynamical stability, normal and shear forces, pressure distribution



2018 Review of Particle Physics.
M. Tanabashi *et al.* (Particle Data Group), Phys. Rev. D **98**, 030001 (2018)

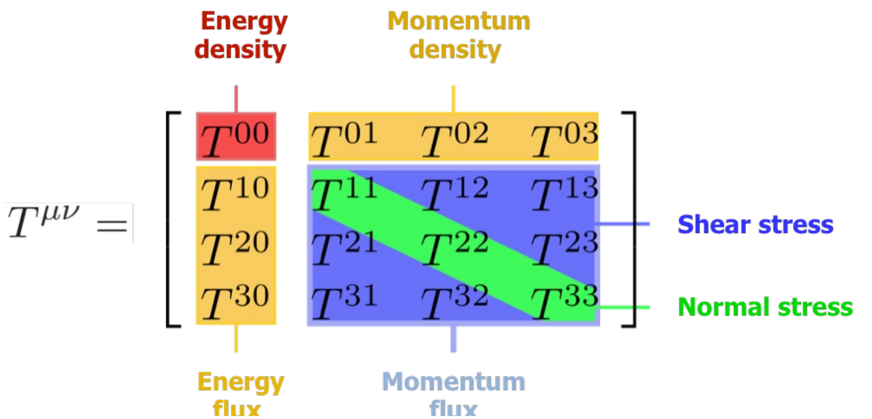
GAUGE AND HIGGS BOSONS

graviton $J = 2$

graviton MASS	$< 6 \times 10^{-32}$ eV

Probing mechanical properties of the proton?

Gravitational Interaction of Fermions
Yu. Kobzarev and L.B. Okun, JETP 16, 5 (1963)
Energy-Momentum Structure Form Factors of Particles *Heinz Pagels, Phys. Rev. 144 (1966) 1250-1260*

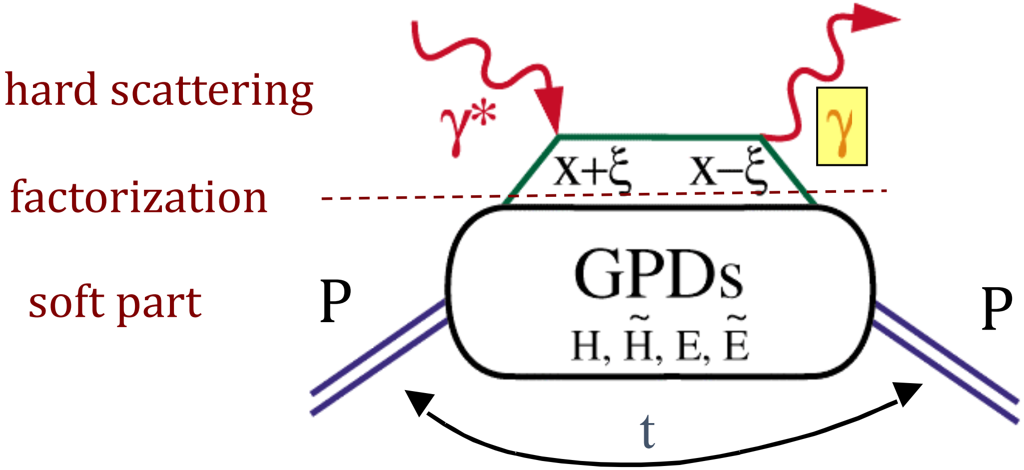


$$T_{ij}(\vec{r}\,) = s(r)\left(\frac{r_i r_j}{r^2} - \frac{1}{3}\delta_{ij}\right) + p(r)\delta_{ij}$$

"….. , there is very little hope of learning anything about the detailed mechanical structure of a particle, because of the extreme weakness of the gravitational interaction"
(*H. Pagels)*

Generalized Parton Distributions (GPDs)

Deeply virtual Compton scattering (DVCS)



$$\xi = \frac{x_B}{2 - x_B}$$

(in the Bjorken regime)

GPD: *H(x,ξ, t)*, …

Proton stays intact

D. Müller (1994) *X. Ji (1996)* *A.Radyushkin (1996)*

D. Müller et al., F.Phys. 42,1994
X. Ji, PRL 78, 610, 1997
A. Radyushkin, PLB 380, 1996

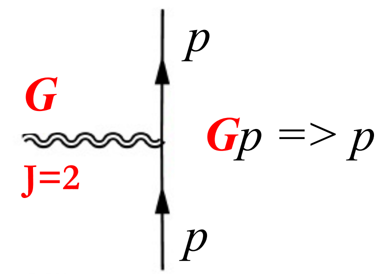
GPDs – GFFs Relations

Nucleon matrix element of the Energy-Momentum Tensor contains three scalar form factors and can be written as:

$$\langle p_2|\hat{T}^q_{\mu\nu}|p_1\rangle = \bar{U}(p_2)\left[M_2^q(t)\frac{P_\mu P_\nu}{M} + J^q(t)\frac{\imath(P_\mu\sigma_{\nu\rho} + P_\nu\sigma_{\mu\rho})\Delta^\rho}{2M} + d_1^q(t)\frac{\Delta_\mu\Delta_\nu - g_{\mu\nu}\Delta^2}{5M}\right]U(p_1)$$

$M_2(t)$: Mass/energy distribution inside the nucleon
$J(t)$: Angular momentum distribution
$d_1(t)$: Forces and pressure distribution

Graviton – proton scattering

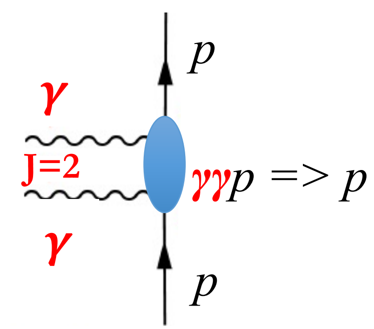


<u>GPDs</u> ⟺ <u>GFFs</u>

$$\int dx\, x\,[H(x,\xi,t) + E(x,\xi,t)] = 2J(t)$$

$$\int dx\, x H(x,\xi,t) = M_2(t) + \frac{4}{5}\xi^2 d_1(t),$$

DVCS



X. Ji, Phys. Rev. D55, 7114 (1997)

GPDs & Compton Form Factors

- GPDs cannot directly be determined from current DVCS measurements alone.
- We can determine the Compton Form Factor $\mathcal{H}(\xi, t)$
- $\mathcal{H}(\xi, t)$ is related to the corresponding GPD $H(x,\xi,t)$ through an integral over the quark longitudinal momentum fraction *x*.

$$\mathcal{H}(\xi,t) = \int_{-1}^{+1} dx H(x,\xi,t) \left(\frac{1}{\xi - x - i\epsilon} - \frac{1}{\xi + x - i\epsilon} \right)$$

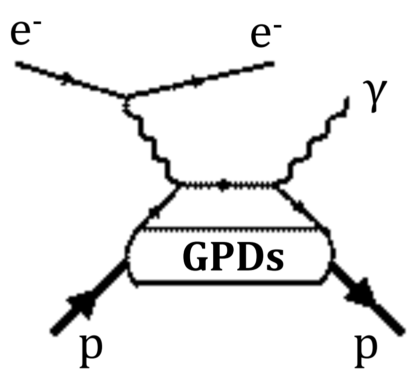
M. Polyakov (2003)

To determine the complex CFF $\mathcal{H}(\xi, t)$ we exploit the interference of the DVCS amplitude with the Bethe-Heitler amplitude that results in a polarized beam spin asymmetry.

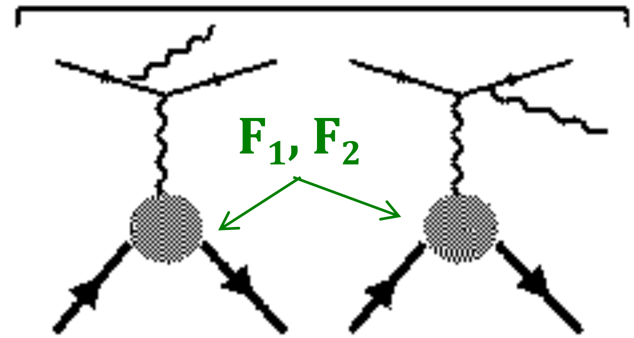
M. Polyakov, Phys. Lett. B555 (2003) 57

From GPD to GFF $d_1(t)$ to $s(r)$ and $p(r)$

DVCS



BH



F_1: Dirac FF; F_2: Pauli FF

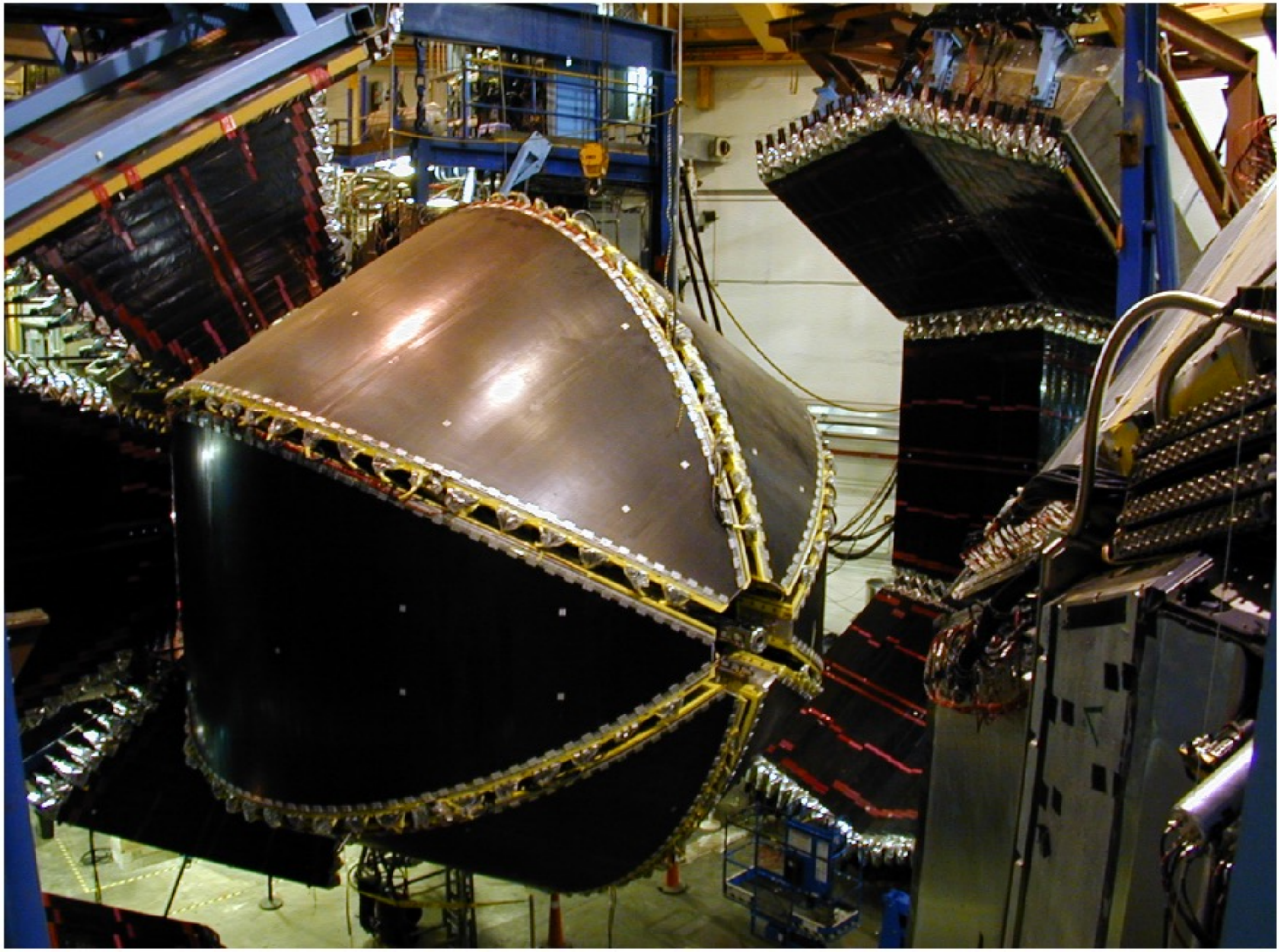
Polarized beam, unpolarized target:

$$\Delta\sigma_{LU} \sim \sin\phi \,\mathrm{Im}\{F_1 \mathcal{H} + ..\} \;\Rightarrow\; \mathcal{H}(\xi,t) \;\Rightarrow\; d_1(t)$$

Bessel Integral relates $d_1(t)$ to the pressure distribution

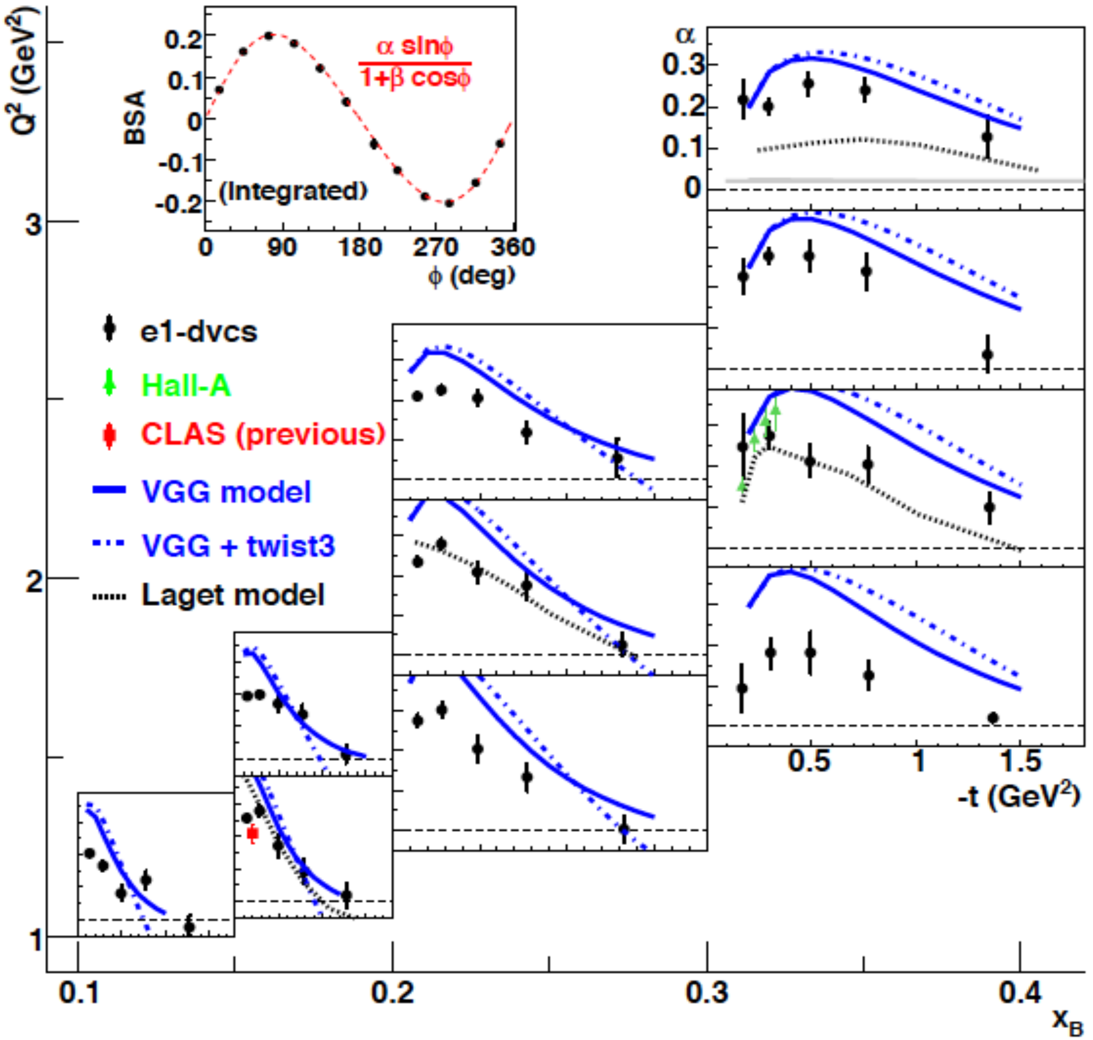
$$d_1(t) \propto \int \mathrm{d}^3\mathbf{r}\, \frac{j_0(r\sqrt{-t})}{2t}\, p(r)$$

CLAS Experiment



In operation 1997 – 2012

DVCS Beam Spin Asymmetry

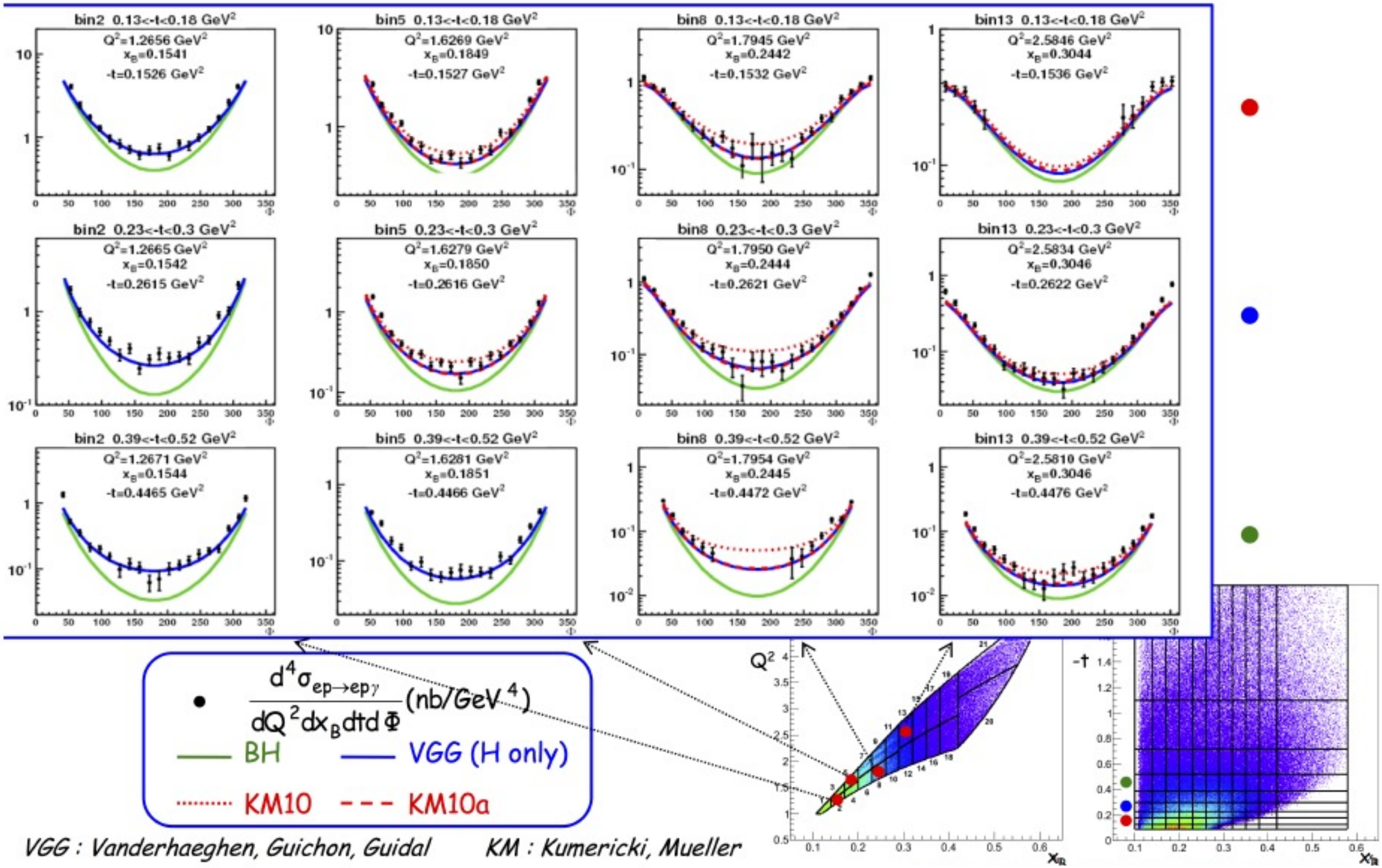


$$F_1\mathcal{H} + \xi G_M\tilde{\mathcal{H}} - \frac{t}{4M^2}F_2\mathcal{E}$$

Precision in a large phase space Q^2, x_B, t

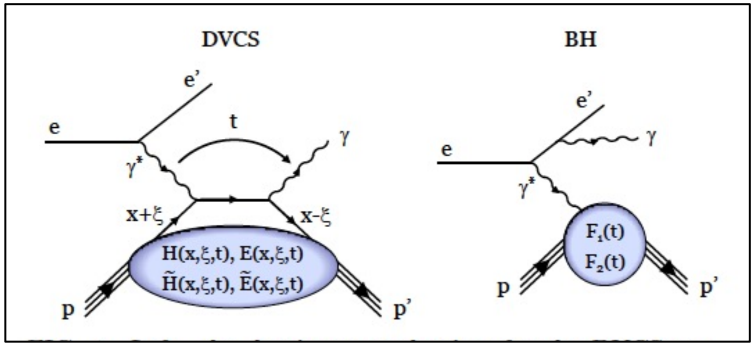
F.X. Girod et al. Phys.Rev.Lett. 100 162002 (2008)

DVCS Unpolarized Cross-Sections

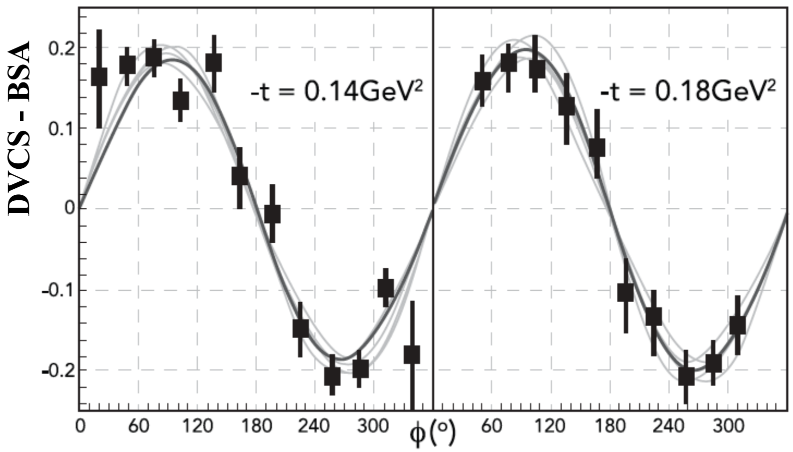


H.S. Jo et al., Phys.Rev.Lett. 115 (2015)

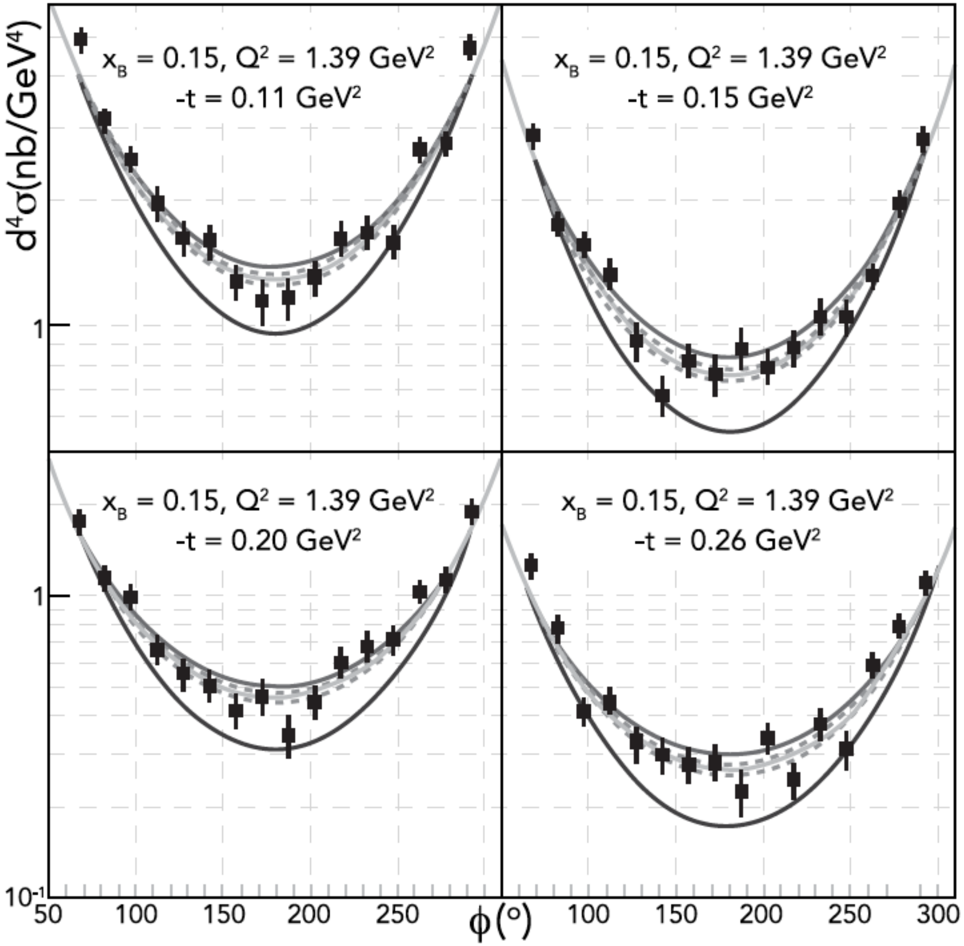
Fit to DVCS data to determine *D*-Term



Samples of Beam Spin Asymmetry



Samples of differential cross sections with fits



F.X. Girod et al., Phys.Rev.Lett. 100 (2008) 162002 ; H.S. Jo et al., Phys.Rev.Lett. 115 (2015) 212003,

Dispersion Relation Analysis and Global Fits

Compton Form Factor $\mathcal{H}$

$$\mathrm{Re}\mathcal{H}(\xi,t) + i\mathrm{Im}\mathcal{H}(\xi,t) = \int_{-1}^{1} dx \left[\frac{1}{\xi - x - i\epsilon} - \frac{1}{\xi + x - i\epsilon}\right] H(x,\xi,t)$$

Beam Spin Asymmetries

$$\mathrm{Im}\mathcal{H}(\xi,t) = \frac{r}{1+\xi}\left(\frac{2\xi}{1+\xi}\right)^{-\alpha(t)}\left(\frac{1-\xi}{1+\xi}\right)^{b}\left(\frac{1-\xi}{1+\xi}\frac{t}{M^2}\right)^{-1}$$

*K. Kumericki, D. Müller, Nucl. Phys. B **841,** 1-58, 2010*
D. Müller, T. Lautenschlager, K, Passek-Kumericki, G. Schaefer, Nucl.B. 884, 438, 2014

Unpolarized cross sections

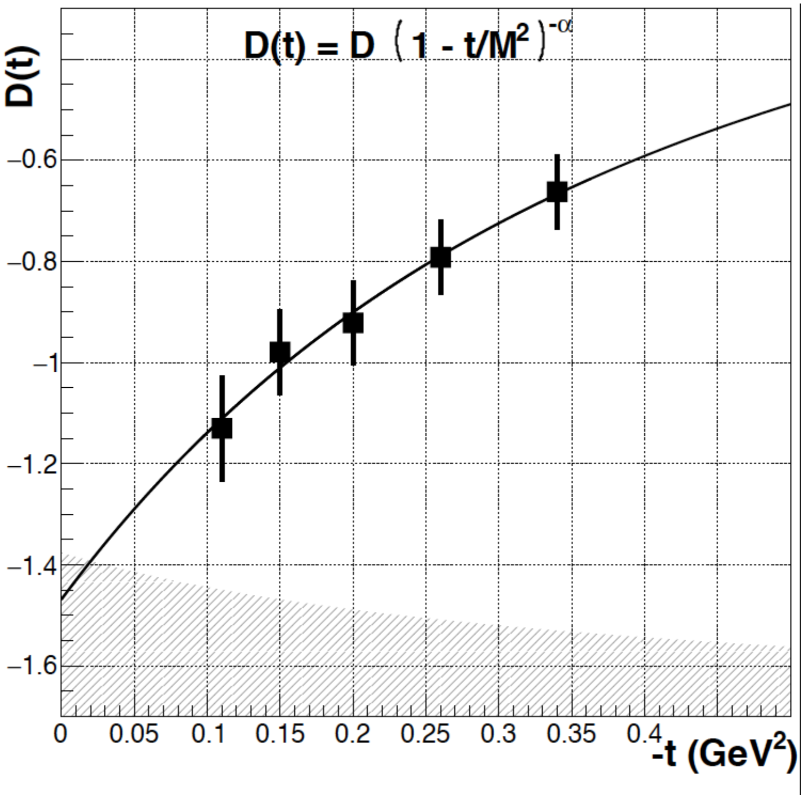
Use Dispersion Relations:

$$\mathrm{Re}\mathcal{H}(\xi,t) \stackrel{\mathrm{LO}}{=} D(t) + \mathcal{P}\int_{-1}^{1} dx \left(\frac{1}{\xi - x} - \frac{1}{\xi + x}\right)\mathrm{Im}\mathcal{H}(x,t)$$

M. Polyakov , C. Weiss, Phys.Rev. D60 (1999) 114017

Extraction of D^q (t) for quark distribution

D(t) from CLAS 6 GeV data



$D^Q(0) = -1.47 \pm 0.10 \pm 0.24$

$M^2 = 1.06 \pm 0.10 \pm 0.15$

$\alpha = 2.76 \pm 0.25 \pm 0.50$

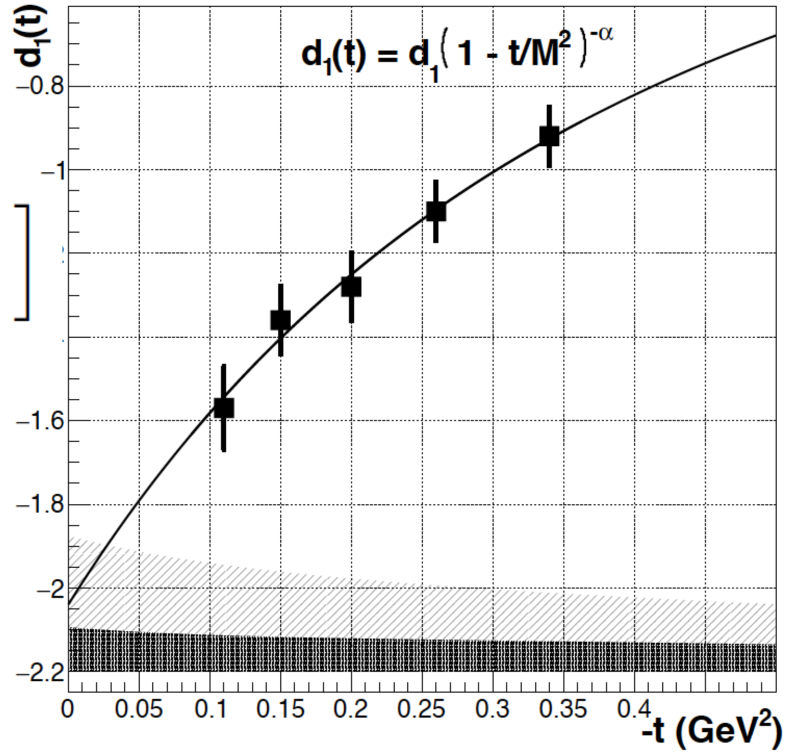
$d^Q_1(t)$ - Gravitational Form Factor

Expansion in Gegenbauer polynomials

$$D(t) = \frac{1}{2}\int_{-1}^{1} \mathrm{d}z \frac{D(z,t)}{1-z} \quad \text{with}$$

$$D(z,t) = (1-z^2)\left[d_1(t) C_1^{3/2}(z) + \cdots\right]$$

$$-1 < z = \frac{x}{\xi} < 1$$



$d_1(0) < 0$ dynamical **stability** of bound state

$d^Q_1(0) = -2.04 \pm 0.14 \pm 0.33$

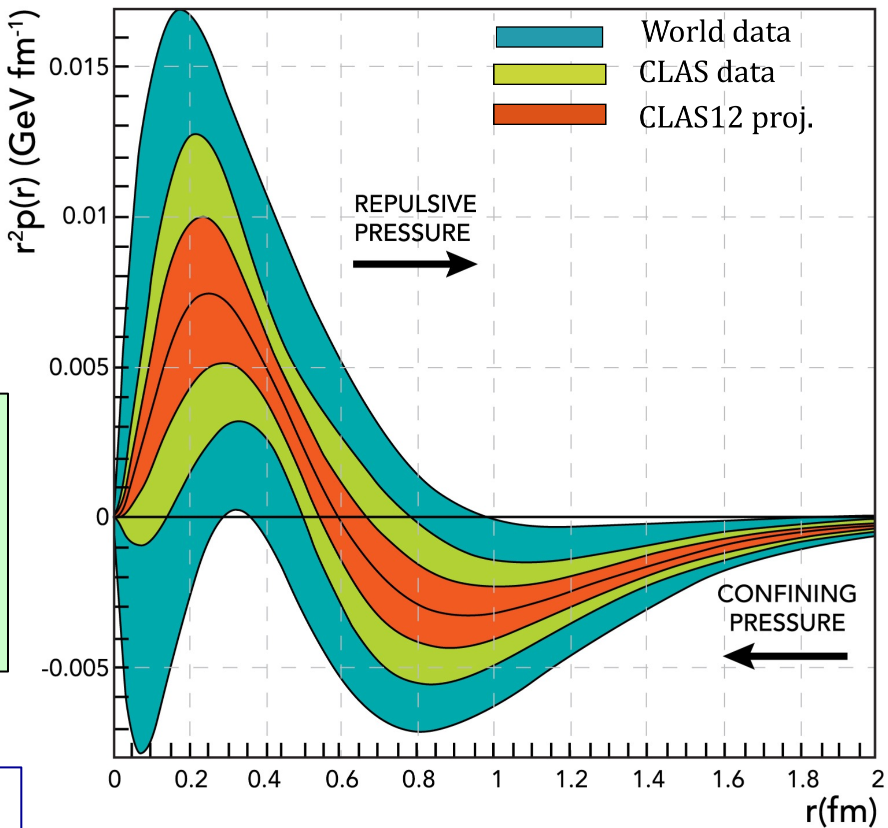
First determination of new fundamental quantity.

The pressure distribution inside the proton

$$d_1(t) \propto \int d^3\mathbf{r}\, \frac{j_0(r\sqrt{-t})}{2t}\, p(r)$$

Repulsive pressure near center
$p(r=0) = 10^{35}$ Pa
Confining pressure at r > 0.6 fm
(in χQSM due to the pion field)

Atmospheric pressure: 10^5 Pa
Pressure in the center of neutron stars ≤ 10^{34} Pa



V.B., L. Elouadrhiri, F.X. Girod
Nature 557 (2018) no.7705, 396-399

A new direction in experimental nuclear/hadronic physics.

Distribution of forces in the proton

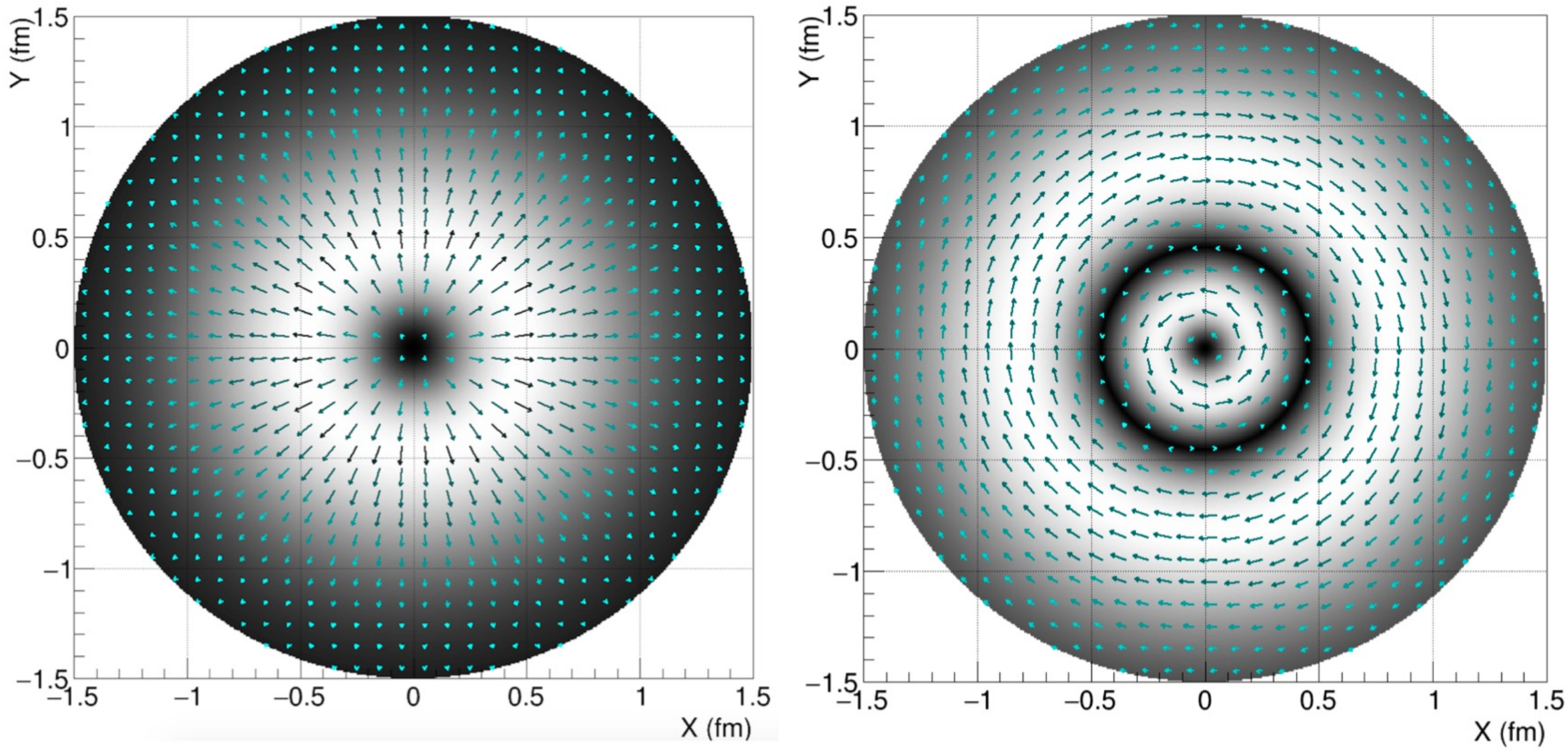
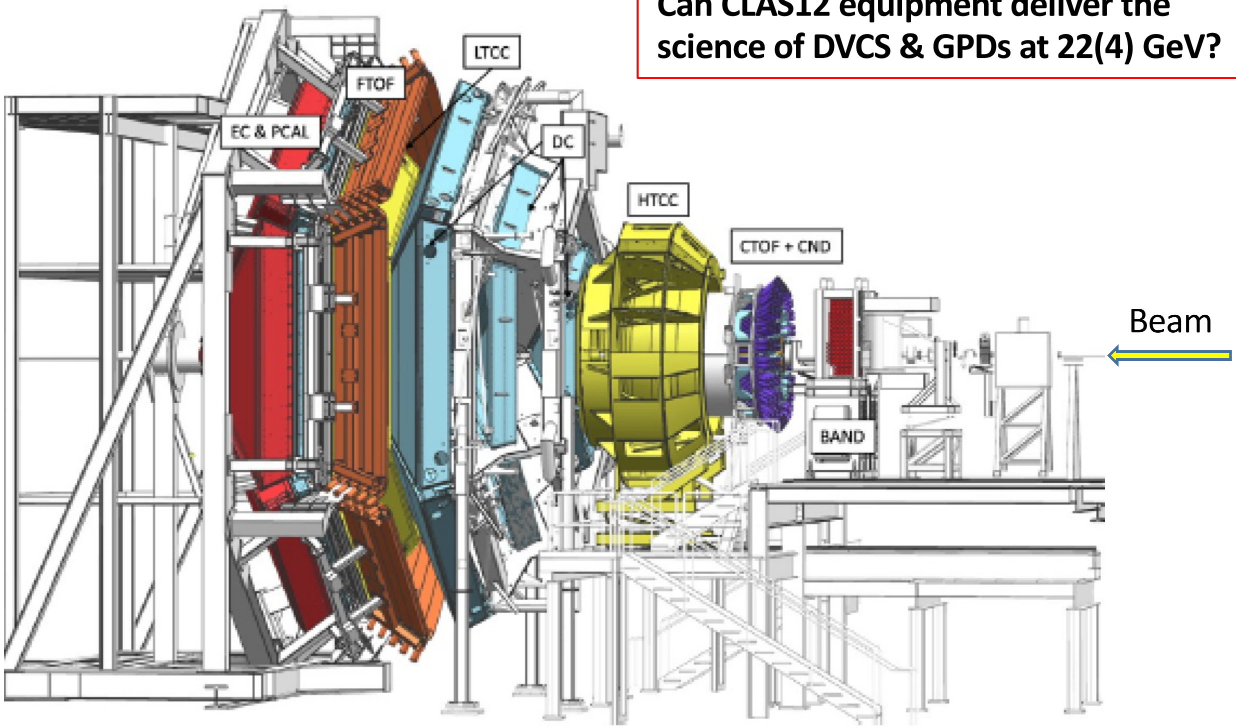


FIG. 14 2D display of the quark contribution to the distribution of forces in the proton as a function of the distance from the proton's center (Burkert et al., 2021b). The light gray shading and longer arrows indicate areas of stronger forces, the dark shading and shorter arrows indicate areas of weaker forces. Left panel: Normal forces as a function of distance from the center. The arrows change magnitude and point always radially outwards. Right panel: Tangential forces as a function of distance from the center. The forces change direction and magnitude as indicated by the direction and lengths of the arrows. They change sign near 0.4 fm from the proton center.

Gravitational Form Factors of the Proton (submitted to RMP)
V. D. Burkert, L. Elouadrhiri, F. X. Girod,1 C. Lorc ́e, P. Schweitzer, and P. E. Shanahan

The CLAS12 Spectrometer at Jefferson Lab



Can CLAS12 equipment deliver the science of DVCS & GPDs at 22(4) GeV?

Baseline equipment

Forward Detector (FD)

- TORUS magnet (6 coils)
- HT Cherenkov Counter
- Drift Chamber System
- LT Cherenkov Counter
- Forward ToF System
- Pre-Shower Calorimeter
- E.M. Calorimeter

Central Detector (CD)

- SOLENOID magnet (5T)
- Central Tracker (SVT, MM)
- Central Time-of-Flight
- Central Neutron Detector

Beamline

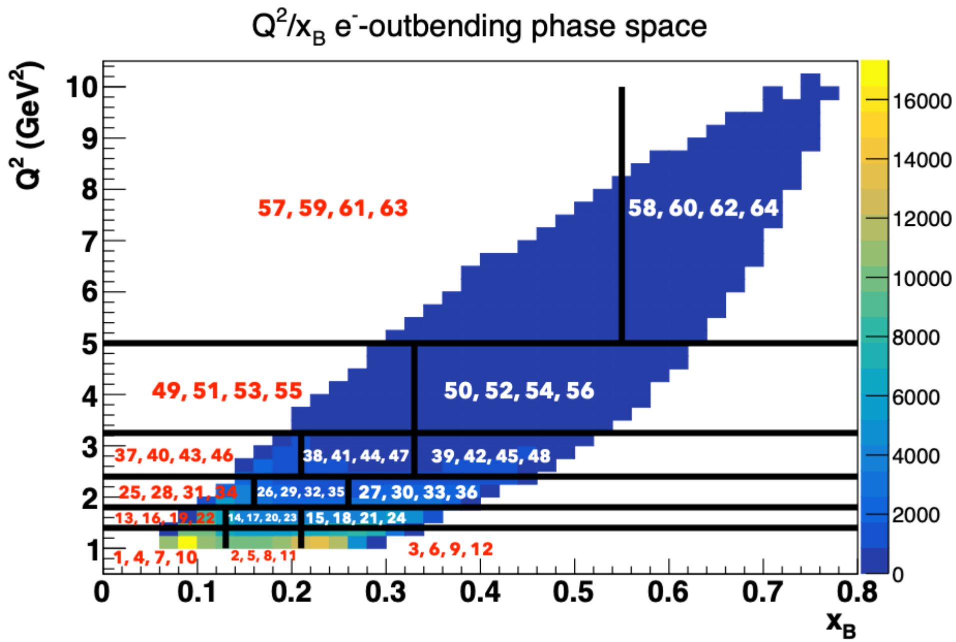
- Liquid & solid targets
- Moller Polarimeter

Ancillary equipment

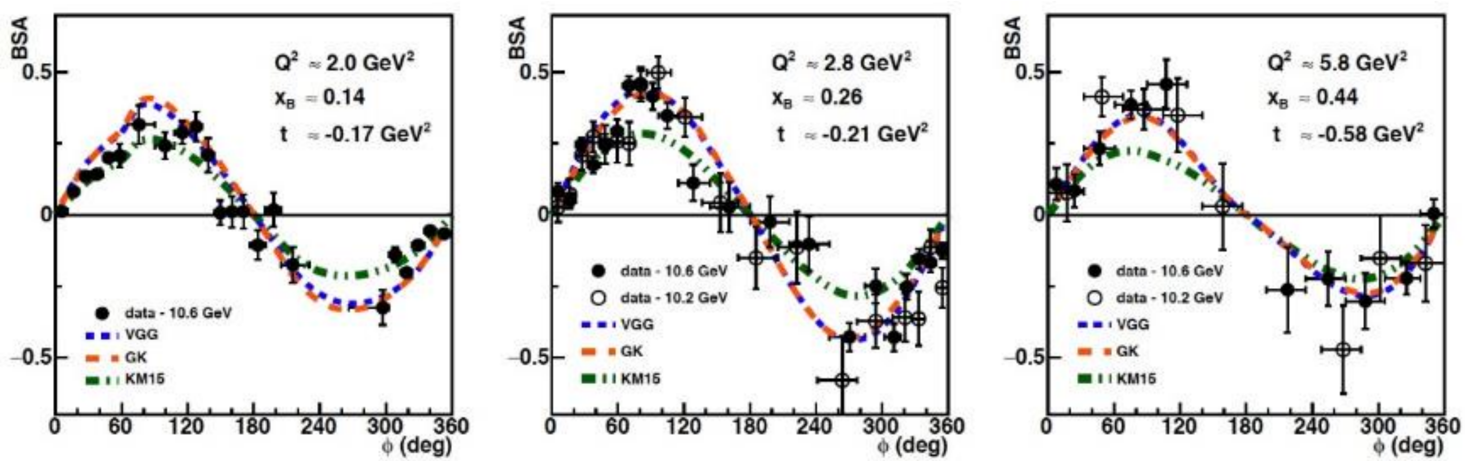
- RICH Detector 2 sectors
- Polarized Target (long.)

Nuclear Inst. and Methods in Physics Research, A 959 (2020) 163419 + 17 articles on all subsystems.

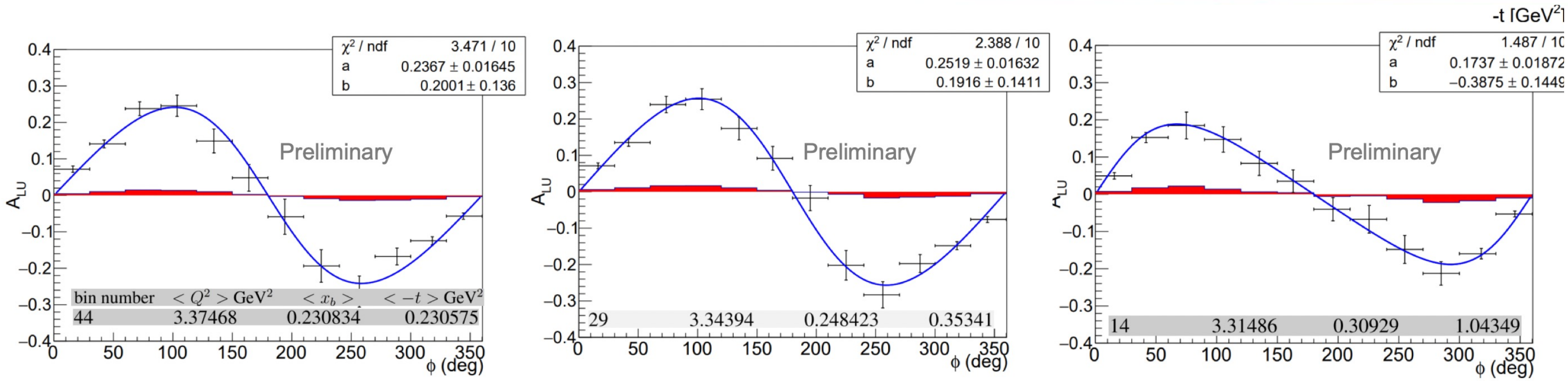
DVCS Beam-Spin Asymmetries in Extended Valence Region with CLAS12



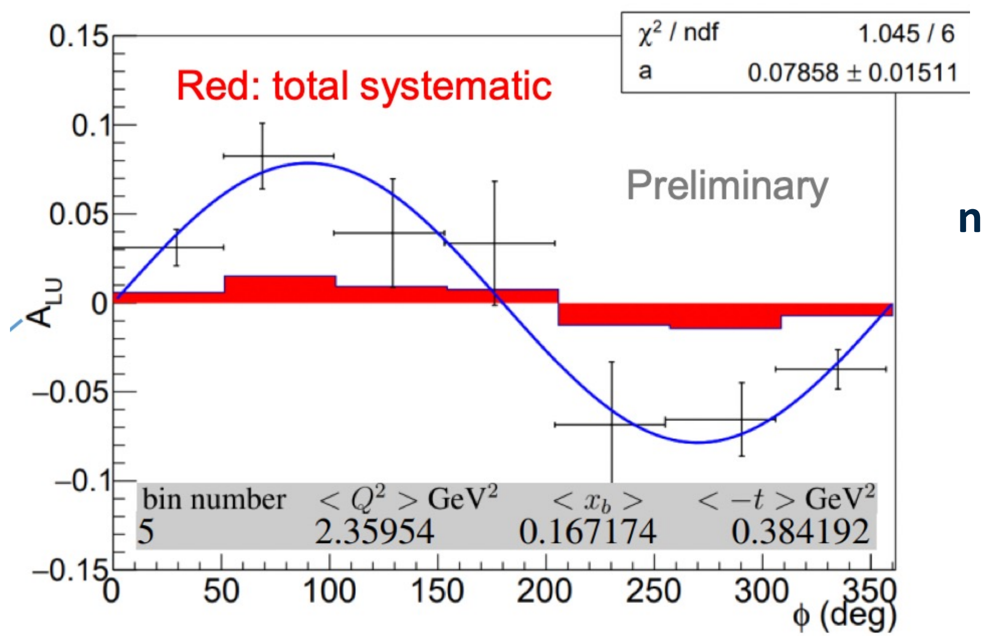
G. Christiaens *et al.* (CLAS Collaboration)
Phys. Rev. Lett. **130**, 211902 – Published 25 May 2023



CLAS12: DVCS with an unpolarized deuterium target



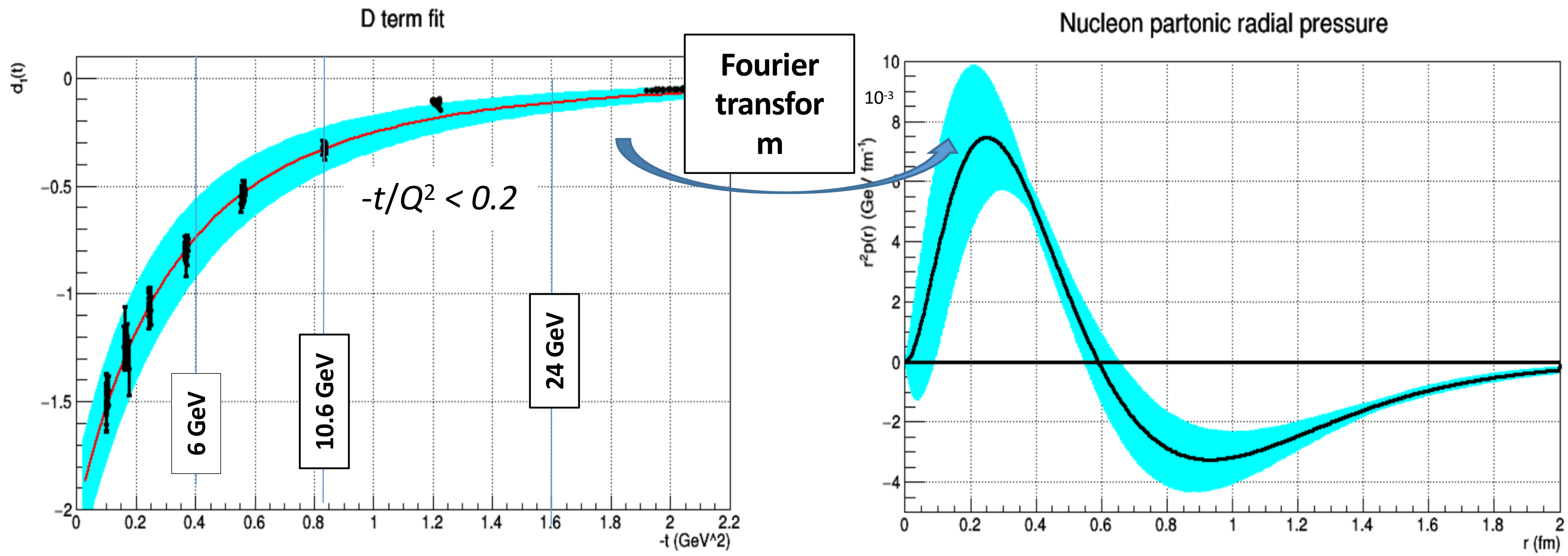
pDVCS



nDVCS

From GFF $D_q(t)$ to distribution of forces (pressure)

Fitting the dispersion relation to $\mathrm{Im}\mathcal{H}(\xi,t)$, $\mathrm{Re}\mathcal{H}(\xi,t)$



22 GeV required to cover sufficient range in t for extraction of mechanical properties.

Summary and Outlook

- First determination of the proton Gravitational Form Factor $D^Q(t)$.
- Opens a new avenue in hadron physics.
- New CLAS12 DVCS data increase kinematical range and allow measurement with different beam energies, target and beam polarizations.
- Program essential part of the Jefferson Lab 22 GeV and positron beam.