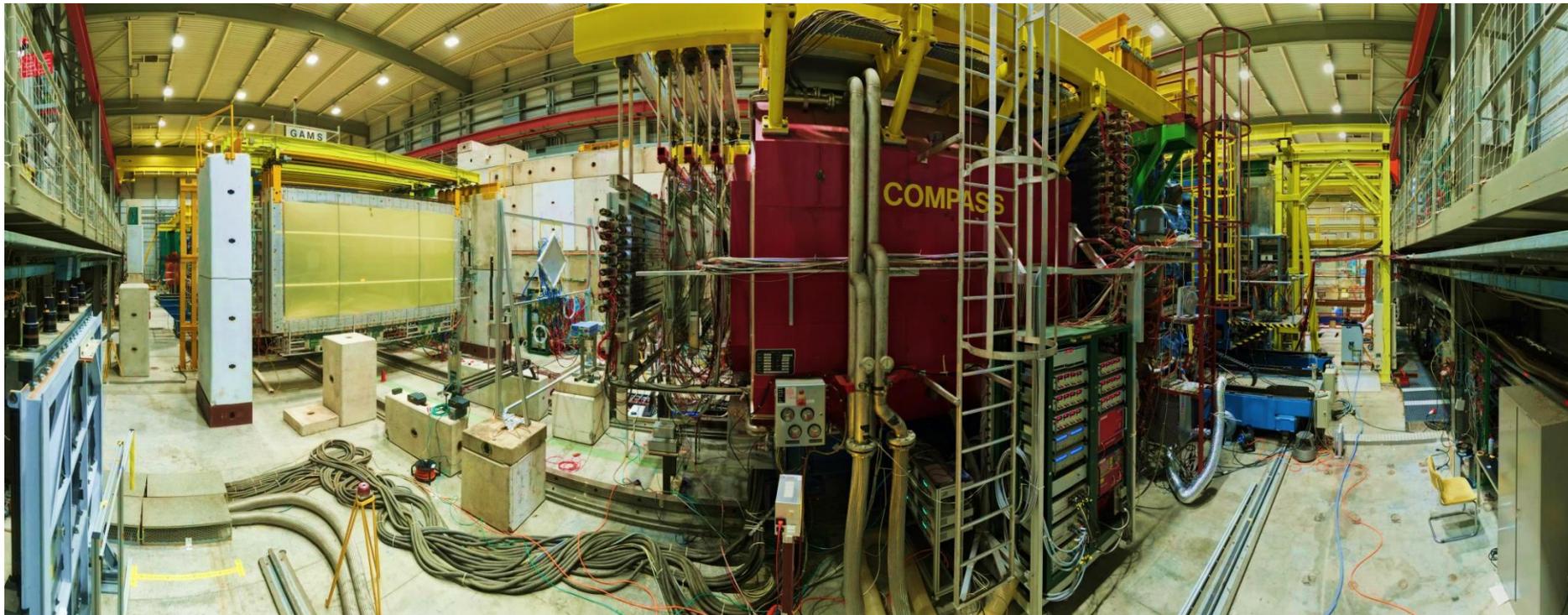


# The relevance of multidimensional binning in SIDIS measurements: COMPASS experience



**BAKUR PARSAMYAN**

AANL, INFN section of Turin and CERN  
*on behalf of the COMPASS Collaboration*



“Science at the Luminosity Frontier: Jefferson Lab at 22 GeV workshop”  
23-26 January 2022, JLab, US

24 January 2023

B. Parsamyan

# Introductory message



- For a better and more complex understanding of the TMD-spin-phenomena, it is important to carry out the extractions, analyses and various corrections in a multi-D approach
- It is also important to carefully confront experimental data from different experiments
- Different complex analysis techniques, Monte-Carlo simulations and various corrections (acceptance, VMs, radiative corrections) are being employed by different experimental collaborations
  - Closer collaboration between different experimental groups would be very beneficial for the field in general
  - Sharing the tools (MC, generators, analysis techniques), preliminary results, doing cross-analyses, etc.
- Close collaboration between experimentalists on one side and phenomenologists and theorists on the other would also be very beneficial
  - Flexibility in adapting on the analysis side (in a timely manner) the choice of the observables, phase-space limitations, etc.
  - Ideally a close collaborative work can be organized

# COMPASS collaboration



## Common Muon and Proton Apparatus for Structure and Spectroscopy

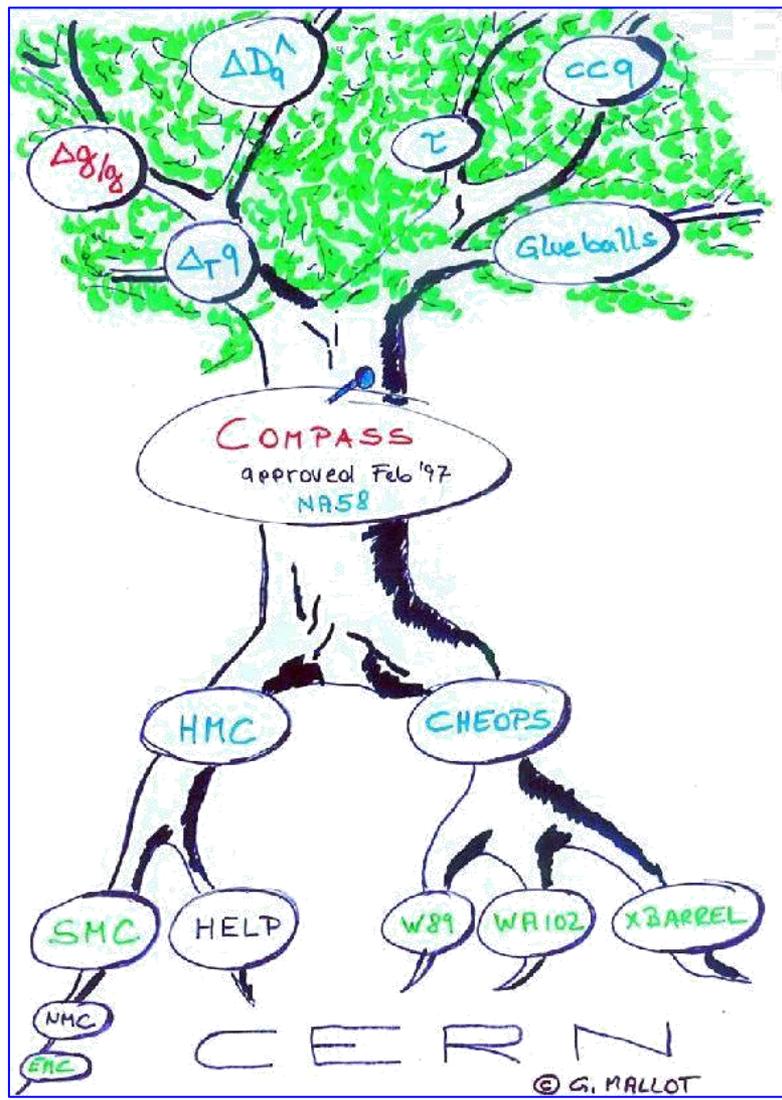


25 institutions from 13 countries  
 – nearly 200 physicists

- CERN SPS north area
- Fixed target experiment
- Approved in 1997 (**25 years**)
- Taking data since 2002 (**20 years**)

International Workshop on Hadron Structure and Spectroscopy  
 IWHSS-2022 workshop (**anniversary edition**)

CERN Globe, August 29-31, 2022



<https://indico.cern.ch/e/IWHSS-2022>



# COMPASS collaboration



## Common Muon and Proton Apparatus for Structure and Spectroscopy



25 institutions from 13 countries  
– nearly 200 physicists

- CERN SPS north area
- Fixed target experiment
- Approved in 1997 (**25 years**)
- Taking data since 2002 (**20 years**)

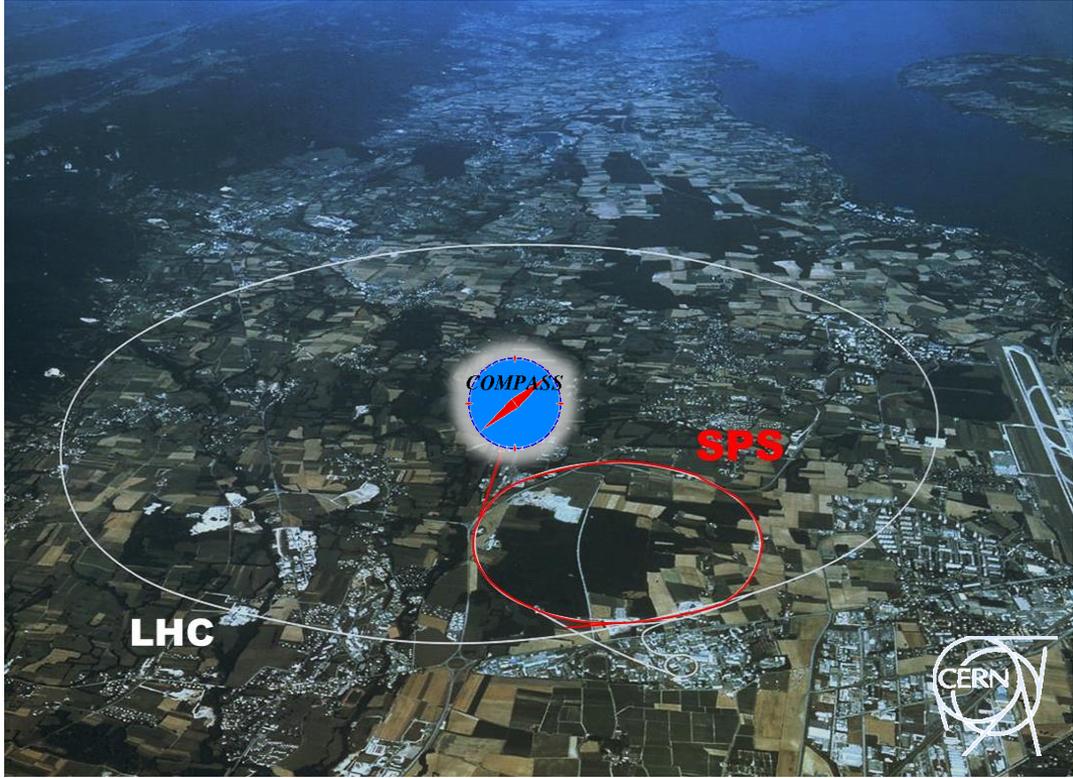
### Wide physics program

#### COMPASS-I

- Data taking 2002-2011
- Muon and hadron beams
- Nucleon spin structure
- Spectroscopy

#### COMPASS-II

- Data taking 2012-2022
- Primakoff
- DVCS (GPD+SIDIS)
- Polarized Drell-Yan
- **Transverse deuteron SIDIS 2022**



COMPASS web page: <http://wwwcompass.cern.ch>

# COMPASS data taking campaigns

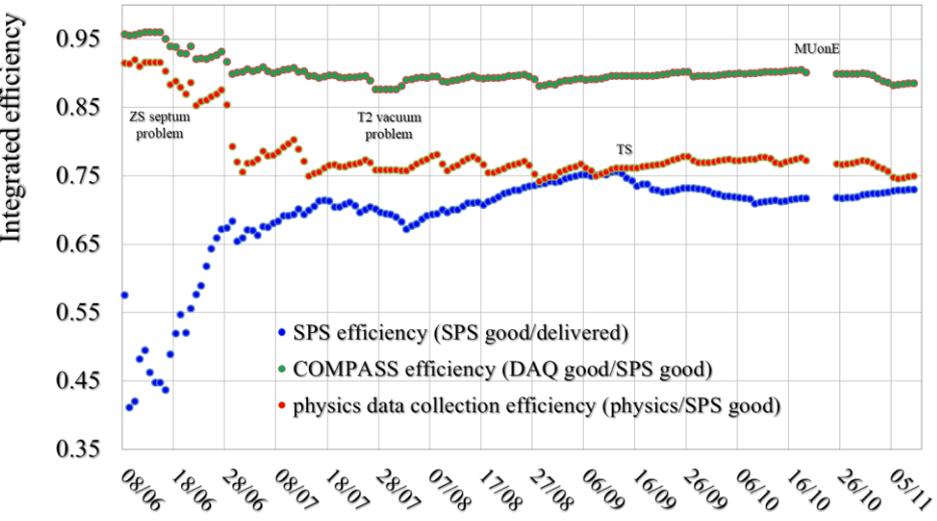
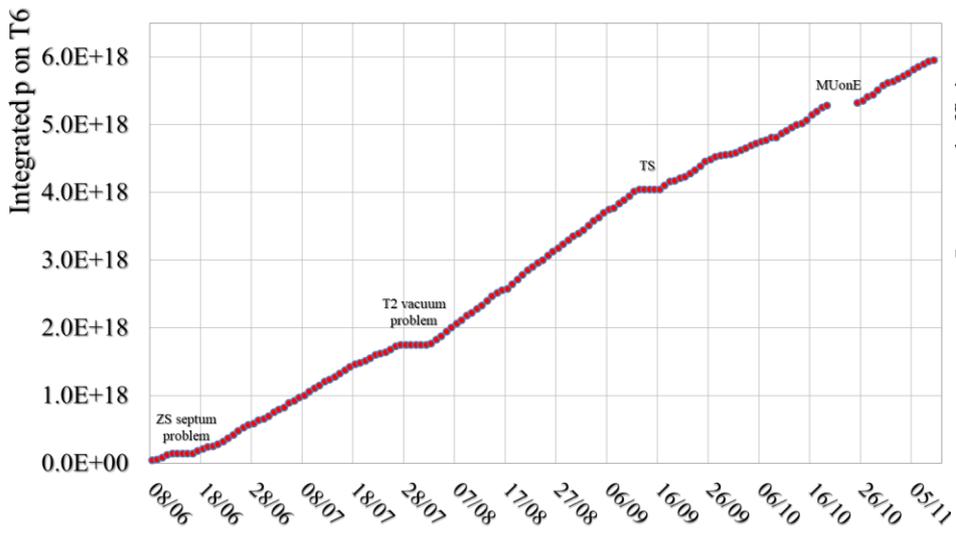
Beam	Target	year	Physics programme
$\mu^+$	Polarized deuteron ( ${}^6\text{LiD}$ )	2002 2003 2004	80% Longitudinal   20% Transverse SIDIS
		2006	Longitudinal SIDIS
	Polarized proton ( $\text{NH}_3$ )	2007	50% Longitudinal   50% Transverse SIDIS
$\pi$   K   p	$\text{LH}_2$ , Ni, Pb, W	2008 2009	Spectroscopy
$\mu^+$	Polarized proton ( $\text{NH}_3$ )	2010	Transverse SIDIS
		2011	Longitudinal SIDIS
$\pi$   K   p	Ni	2012	Primakoff
$\mu^\pm$	$\text{LH}_2$	2012	Pilot DVCS & HEMP & unpolarized SIDIS
$\pi^-$	Polarized proton ( $\text{NH}_3$ )	2014	Pilot Drell-Yan
		2015 2018	Transverse Drell-Yan
$\mu^\pm$	$\text{LH}_2$	2016 2017	DVCS & HEMP & unpolarized SIDIS
$\mu^+$	Polarized deuteron ( ${}^6\text{LiD}$ )	2021 2022	Transverse SIDIS

# COMPASS data taking campaigns

Beam	Target	year	Physics programme
$\mu^+$	Polarized deuteron ( $^6\text{LiD}$ )	2002	80% Longitudinal   20% Transverse SIDIS
		2003	
		2004	

- Total number of protons delivered on T6:  
 $\sim 5.95 \times 10^{18}$  (98%) in about 150 days

SPS efficiency:  $\sim 73\%$   
 Spectrometer efficiency:  $\sim 90\%$   
 Physics data collection efficiency:  $\sim 75\%$



$\mu^+$	Polarized deuteron ( $^6\text{LiD}$ )	2021 2022	Transverse SIDIS
---------	---------------------------------------	--------------	------------------

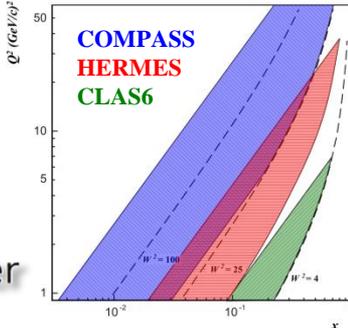
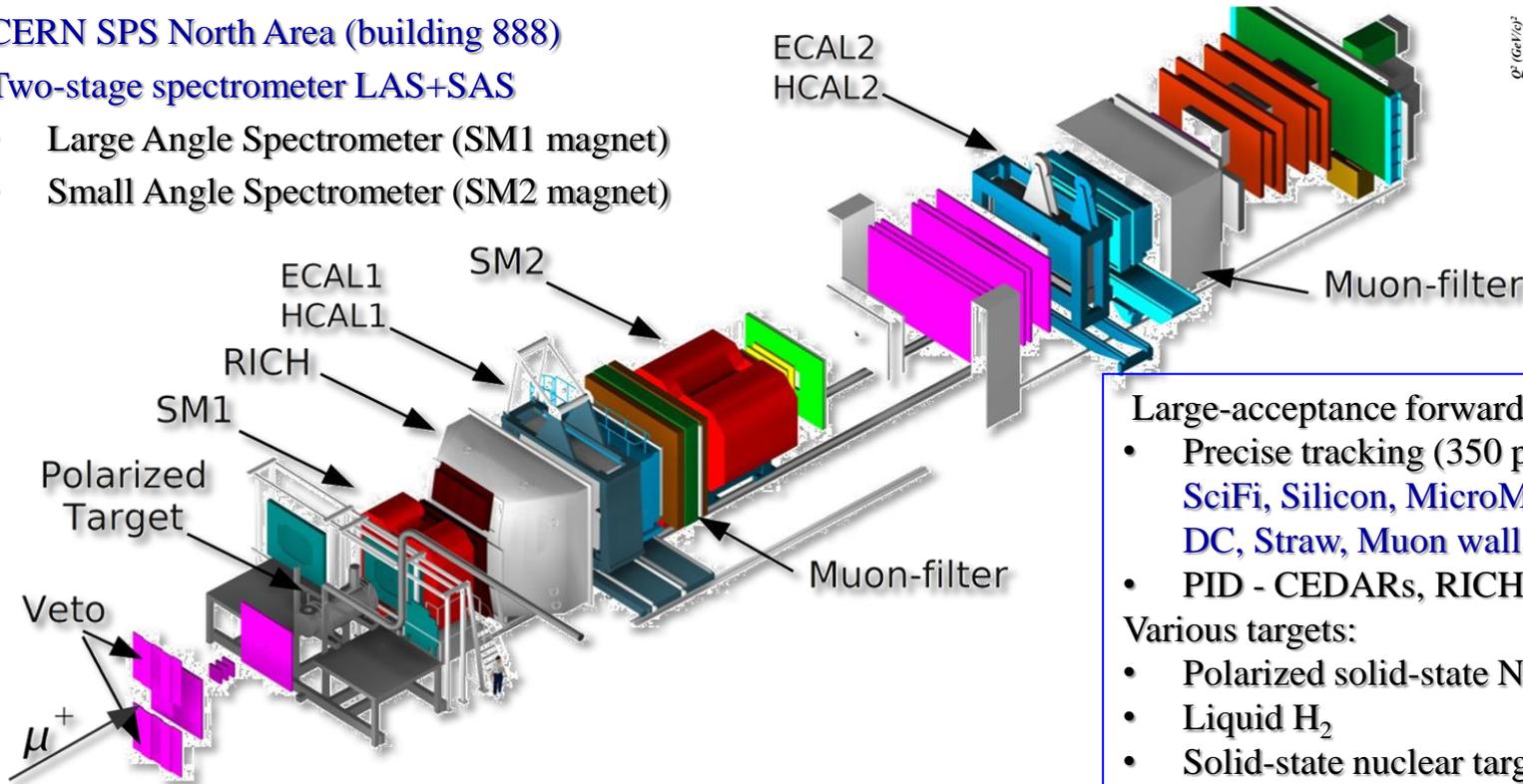
# COMPASS experimental setup

## COmmon MUon Proton Apparatus for Structure and Spectroscopy

CERN SPS North Area (building 888)

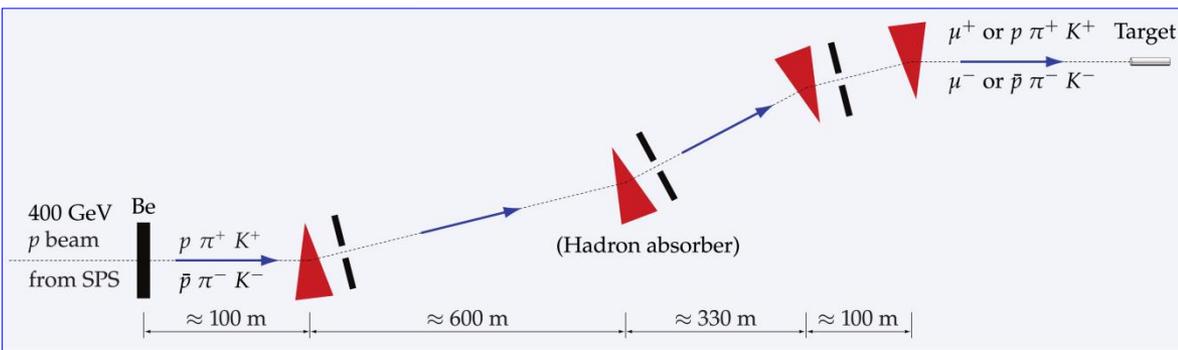
Two-stage spectrometer LAS+SAS

- Large Angle Spectrometer (SM1 magnet)
- Small Angle Spectrometer (SM2 magnet)



- Large-acceptance forward spectrometer
- Precise tracking (350 planes)  
SciFi, Silicon, MicroMegas, GEM, MWPC, DC, Straw, Muon walls
  - PID - CEDARs, RICH, calorimeters, MWs
- Various targets:
- Polarized solid-state NH<sub>3</sub> or <sup>6</sup>LiD
  - Liquid H<sub>2</sub>
  - Solid-state nuclear targets (e.g. Ni, W, Pb)

- Primary beam - 400 GeV *p* from SPS
  - impinging on Be production target (T6)
- 190 GeV secondary hadron beams
  - h<sup>-</sup> beam: 97% π<sup>-</sup>, 2% K<sup>-</sup>, 1% *p*
  - h<sup>+</sup> beam: 75% *p*, 24% π<sup>+</sup>, 1% K<sup>+</sup>
- 160 GeV tertiary muon beams
  - μ<sup>±</sup> longitudinally polarized



# COMPASS experimental setup: Phase II (SIDIS programme)

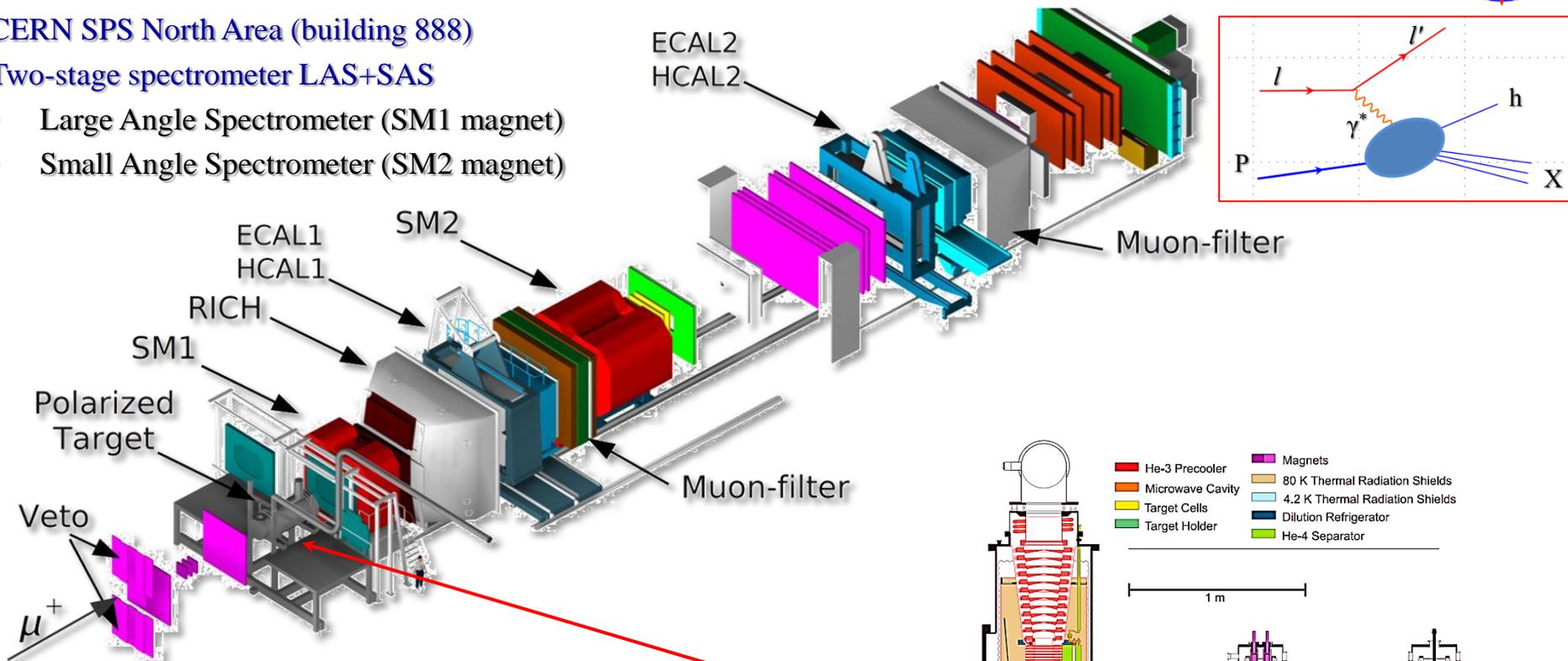


## Common Muon Proton Apparatus for Structure and Spectroscopy

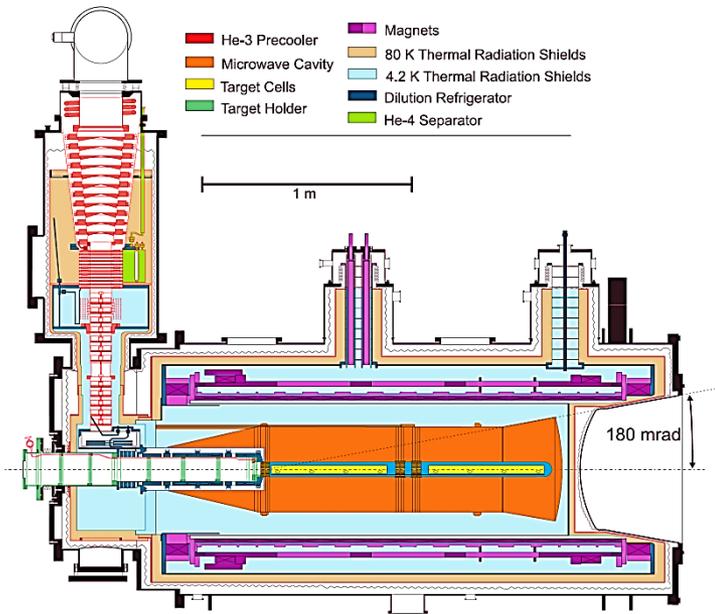
CERN SPS North Area (building 888)

Two-stage spectrometer LAS+SAS

- Large Angle Spectrometer (SM1 magnet)
- Small Angle Spectrometer (SM2 magnet)



- Primary beam - 400 GeV  $p$  from SPS
  - impinging on Be production target (T6)
- 190 GeV secondary hadron beams
  - $h^-$  beam: 97%  $\pi^-$ , 2%  $K^-$ , 1%  $p$
  - $h^+$  beam: 75%  $p$ , 24%  $\pi^+$ , 1%  $K^+$
- 160 GeV tertiary muon beams
  - $\mu^+$  longitudinally polarized



# COMPASS experimental setup: Phase II (DY programme)

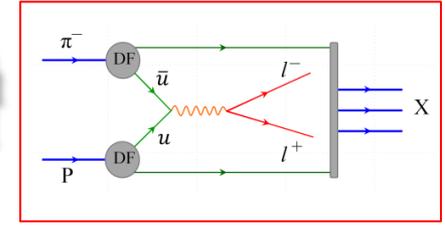
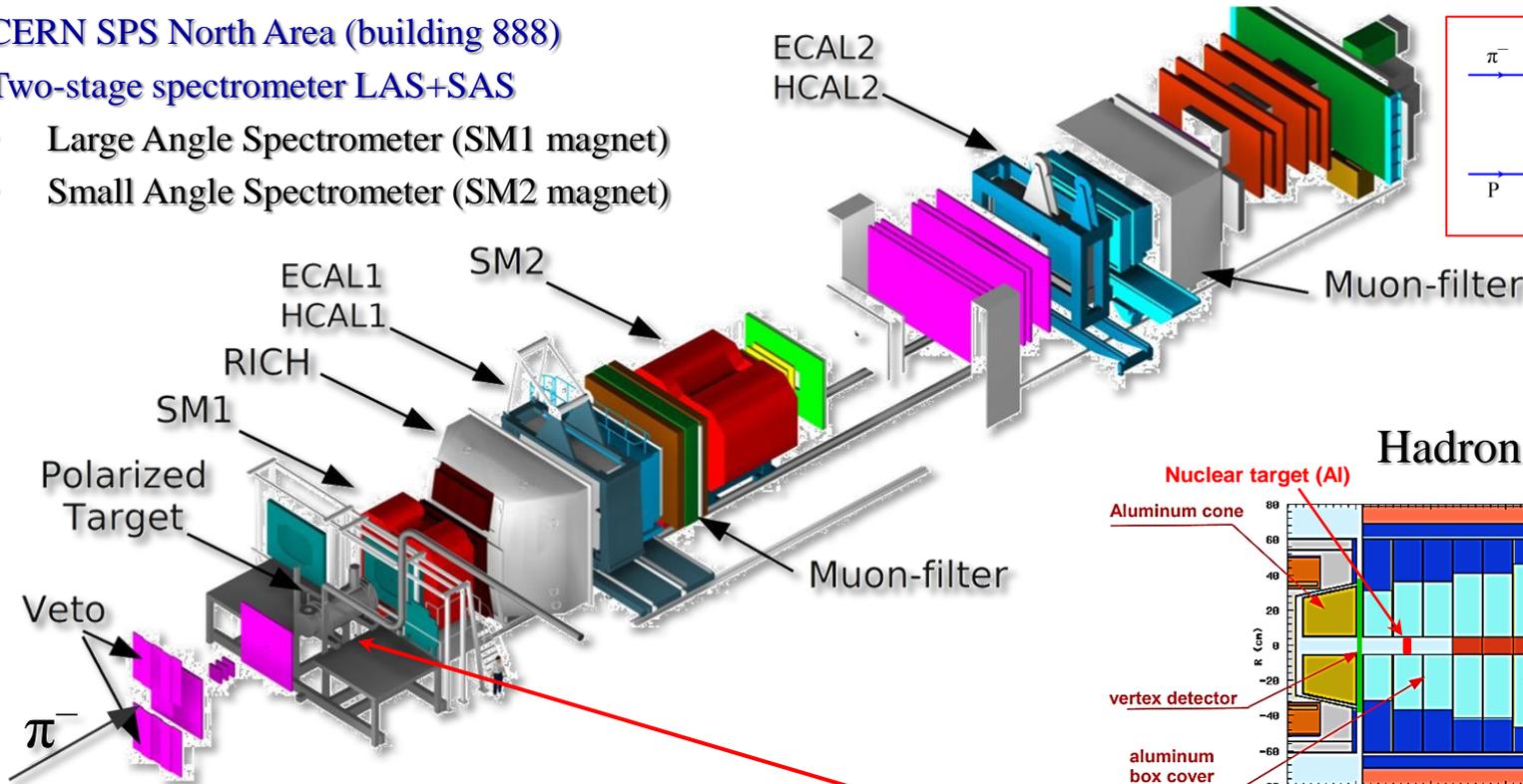


## COmmon MUon Proton Apparatus for Structure and Spectroscopy

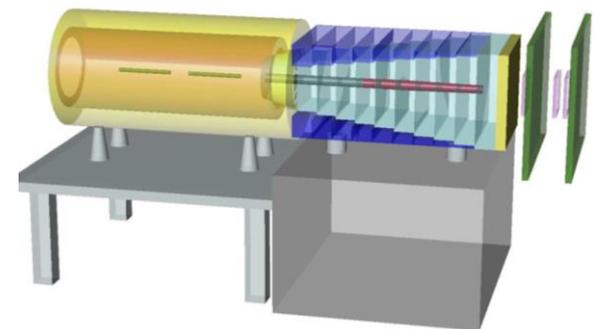
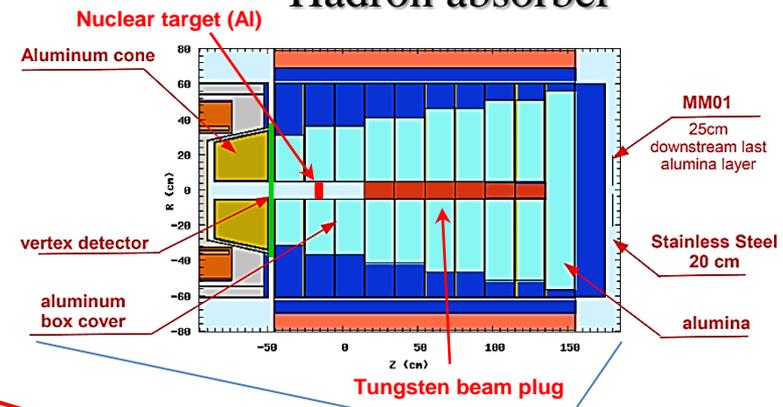
CERN SPS North Area (building 888)

Two-stage spectrometer LAS+SAS

- Large Angle Spectrometer (SM1 magnet)
- Small Angle Spectrometer (SM2 magnet)



### Hadron absorber



- Primary beam - 400 GeV  $p$  from SPS
  - impinging on Be production target (T6)
- 190 GeV secondary hadron beams
  - $h^-$  beam: 97%  $\pi^-$ , 2%  $K^-$ , 1%  $p$
  - $h^+$  beam: 75%  $p$ , 24%  $\pi^+$ , 1%  $K^+$
- 160 GeV tertiary muon beams
  - $\mu^\pm$  longitudinally polarized

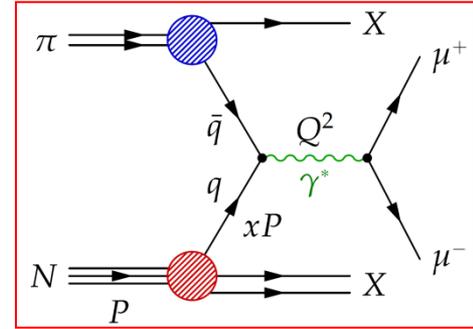
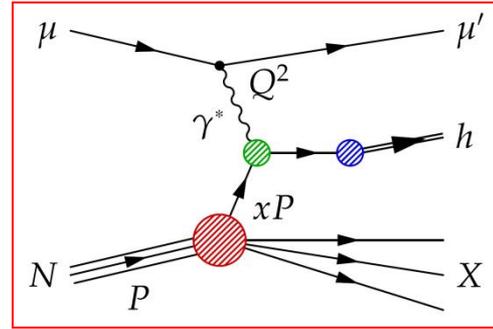
# The COMPASS Experiment at the CERN SPS

Broad Physics Program to study Structure and Excitation Spectrum of Hadrons

Increasing resolution scale  
(momentum transfer)

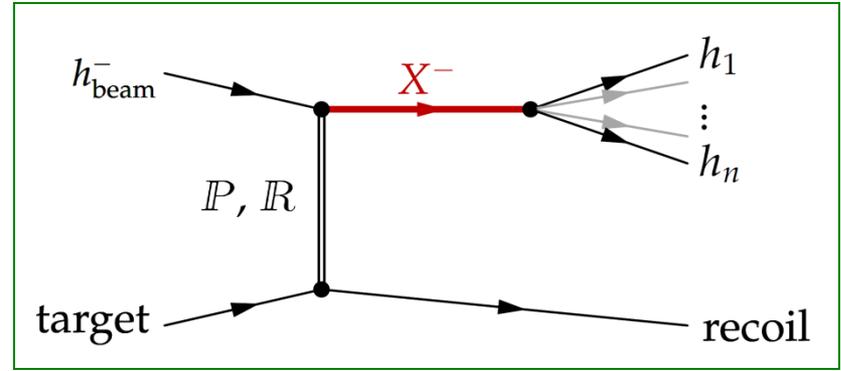
## Nucleon structure

- Hard scattering of  $\mu^\pm$  and  $\pi^-$  off (un)polarized P/D targets
- Study of nucleon spin structure
- Parton distribution functions and fragmentation functions



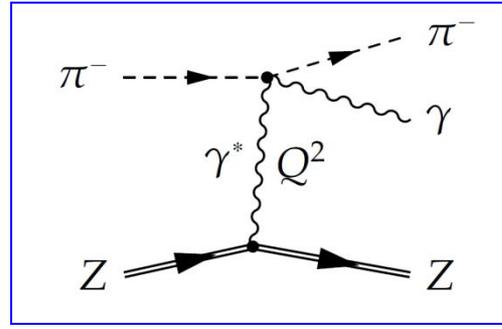
## Hadron spectroscopy

- Diffractive  $\pi(K)$  dissociation reaction with proton target
- PWA technique employed
- High-precision measurement of light-meson excitation spectrum
- Search for exotic states



## Chiral dynamics

- Test chiral perturbation theory in  $\pi(K) \gamma$  reactions
- $\pi^\pm$  and  $K^\pm$  polarizabilities
- Chiral anomaly  $F_{3\pi}$

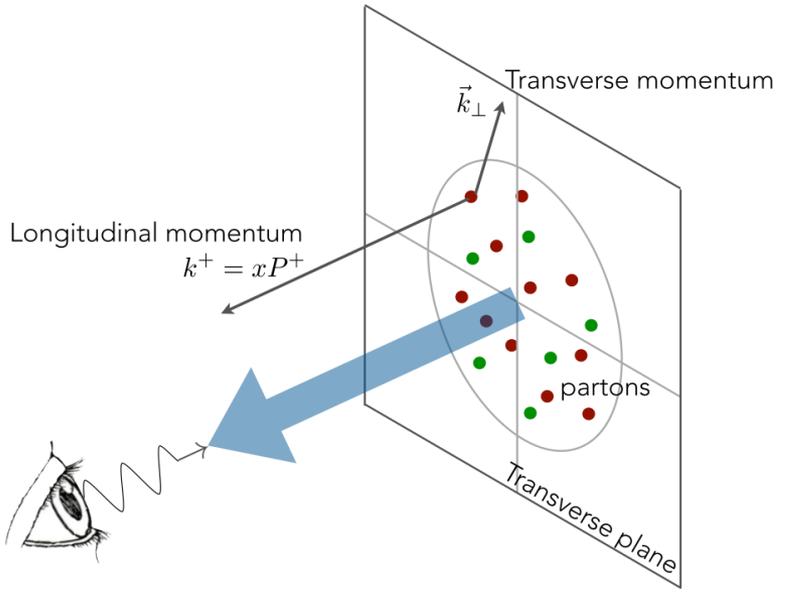
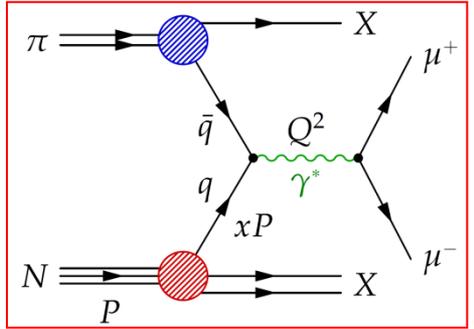
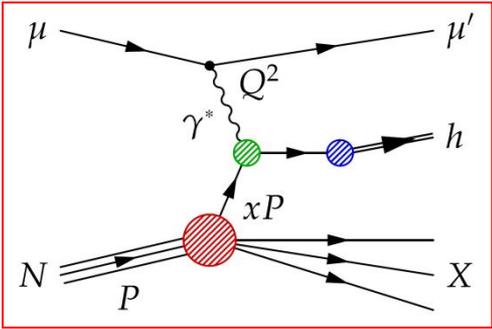


# The COMPASS Experiment at the CERN SPS

Broad Physics Program to study Structure and Excitation Spectrum of Hadrons

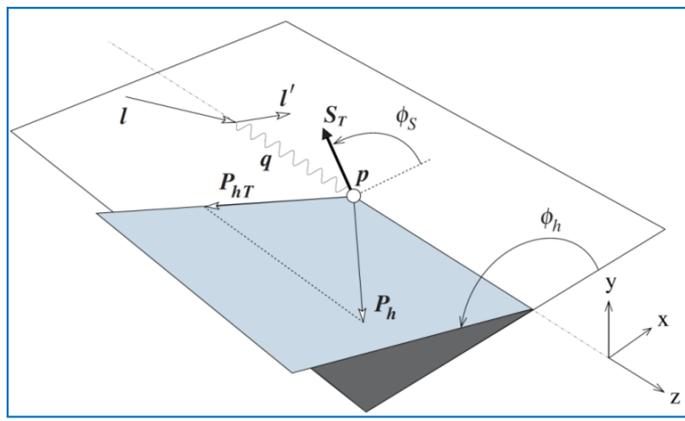
Increasing resolution scale  
(momentum transfer)

- Nucleon structure**
  - Hard scattering of  $\mu^\pm$  and  $\pi^-$  off (un)polarized P/D targets
  - Study of nucleon spin structure
  - Parton distribution functions and fragmentation functions
- Hadron spectroscopy**
  - Diffractive  $\pi(K)$  dissociation reaction with proton target
  - PWA technique employed
  - High-precision measurement of light-meson excitation spectrum
  - Search for exotic states
- Chiral dynamics**
  - Test chiral perturbation theory in  $\pi(K) \gamma$  reactions
  - $\pi^\pm$  and  $K^\pm$  polarizabilities
  - Chiral anomaly  $F_{3\pi}$



# Cahn effect in SIDIS

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} = \left[ \frac{\alpha}{xy Q^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L}) \times \left( 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \dots \right)$$



## Cahn effect

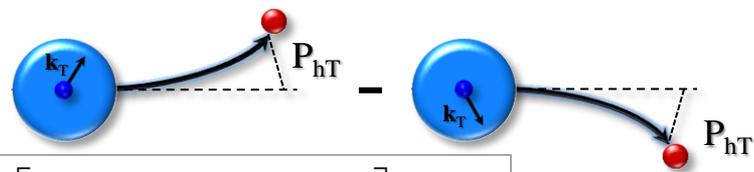
R.N. Cahn, **PLB 78 (1978)**



The point that there are azimuthal dependences, which arise from the transverse momenta of the partons was clearly stated in this papers:

- T.P. Cheng and A. Zee, **Phys. Rev. D6 (1972)** 885;
- F. Ravndal, **Phys. Lett. 43B (1973)** 301.
- R.L. Kingsley, **Phys. Rev. D10 (1974)** 1580;
- A.M. Kotsinyan, **Teor. Mat. Fiz. 24 (1975)** 206;

$$k_T \rightarrow \cos\phi_q \rightarrow \cos\phi_h$$

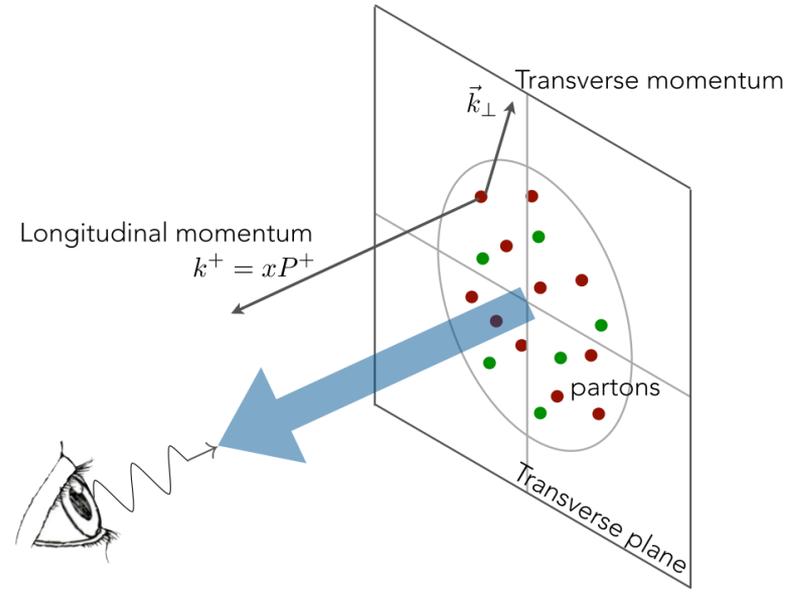


$$\hat{s} \approx xs \left[ 1 - 2\sqrt{1-y} \frac{k_T}{Q} \cdot \cos\phi_q \right]$$

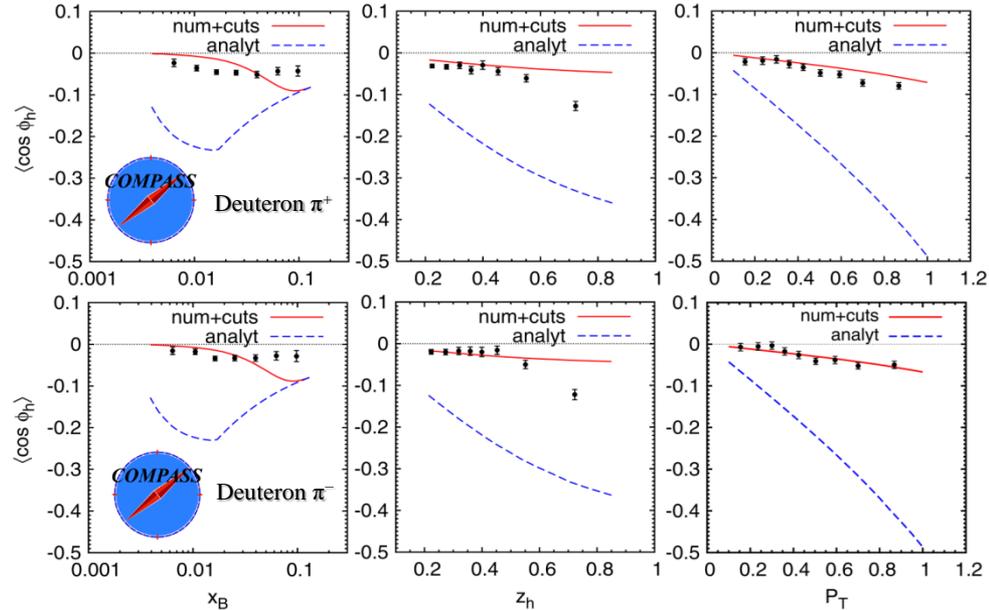
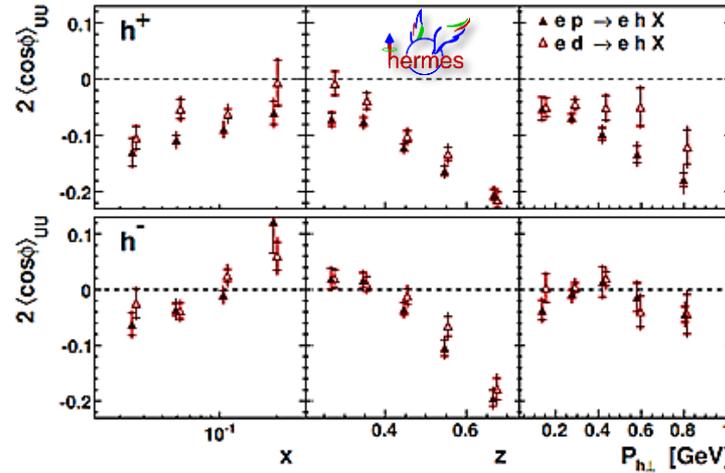
$$\hat{u} \approx -xs(1-y) \left[ 1 - \frac{2k_T}{Q\sqrt{1-y}} \cdot \cos\phi_q \right]$$

$$\hat{t} = -Q^2 = -xys, \quad \text{where } s = (l + P)^2$$

$$d\sigma^{lp \rightarrow l'hX} \propto d\sigma^{lq \rightarrow lq} \propto \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2}$$



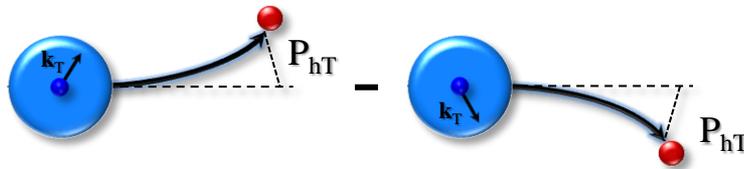
Significant non-zero effect observed by a number of experiments



# Cahn effect in SIDIS

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L}) \times (1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \dots)$$

Quark	U
Nucleon	$f_1^q(x, k_T^2)$ number density



As of 1978 – simplistic kinematic effect:

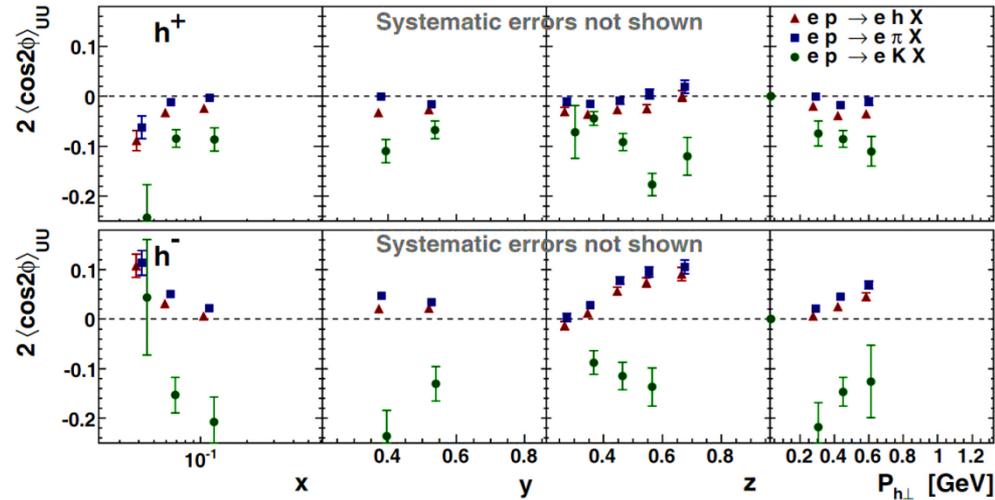
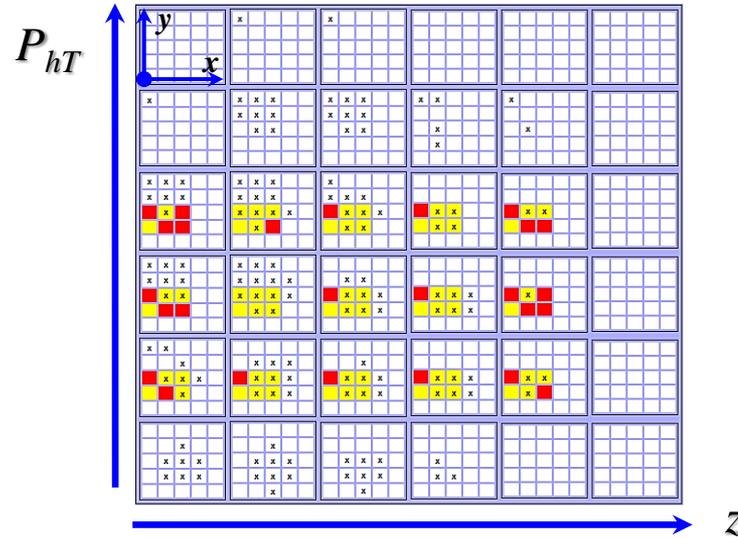
- non-zero  $k_T$  induces an azimuthal modulation

As of 2022 – complex SF (twist-2/3 functions)

- Measurements by different experiments

$$F_{UU}^{\cos\phi_h} = \frac{2M}{Q} C \left\{ -\frac{\hat{h} \cdot p_T}{M_h} \left( xhH_{1q}^{\perp h} + \frac{M_h}{M} f_1^q \frac{\tilde{D}_q^{\perp h}}{z} \right) - \frac{\hat{h} \cdot k_T}{M} \left( xf^{\perp q} D_{1q}^h + \frac{M_h}{M} h_1^{\perp q} \frac{\tilde{H}_q^h}{z} \right) \right\}$$

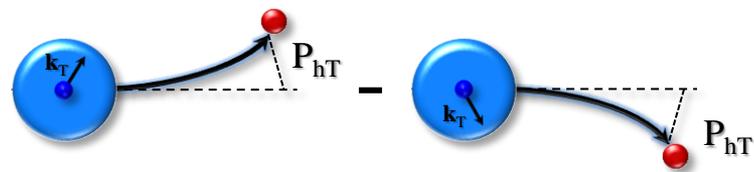
Significant non-zero effect observed by a number of experiments



# Cahn effect in SIDIS

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_s} = \left[ \frac{\alpha}{xy Q^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L}) \times (1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \dots)$$

Quark	U
Nucleon	
U	$f_1^q(x, k_T^2)$ number density 



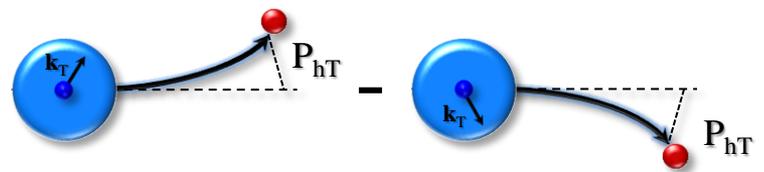
- As of 1978 – simplistic kinematic effect:
- non-zero  $k_T$  induces an azimuthal modulation
- As of 2022 – complex SF (twist-2/3 functions)
- Measurements by different experiments

$$F_{UU}^{\cos\phi_h} = \frac{2M}{Q} C \left\{ -\frac{\hat{h} \cdot p_T}{M_h} \left( xhH_{1q}^{\perp h} + \frac{M_h}{M} f_1^q \frac{\tilde{D}_q^{\perp h}}{z} \right) - \frac{\hat{h} \cdot k_T}{M} \left( xf^{\perp q} D_{1q}^h + \frac{M_h}{M} h_1^{\perp q} \frac{\tilde{H}_q^h}{z} \right) \right\}$$

# Cahn effect in SIDIS

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L}) \times ( 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \dots )$$

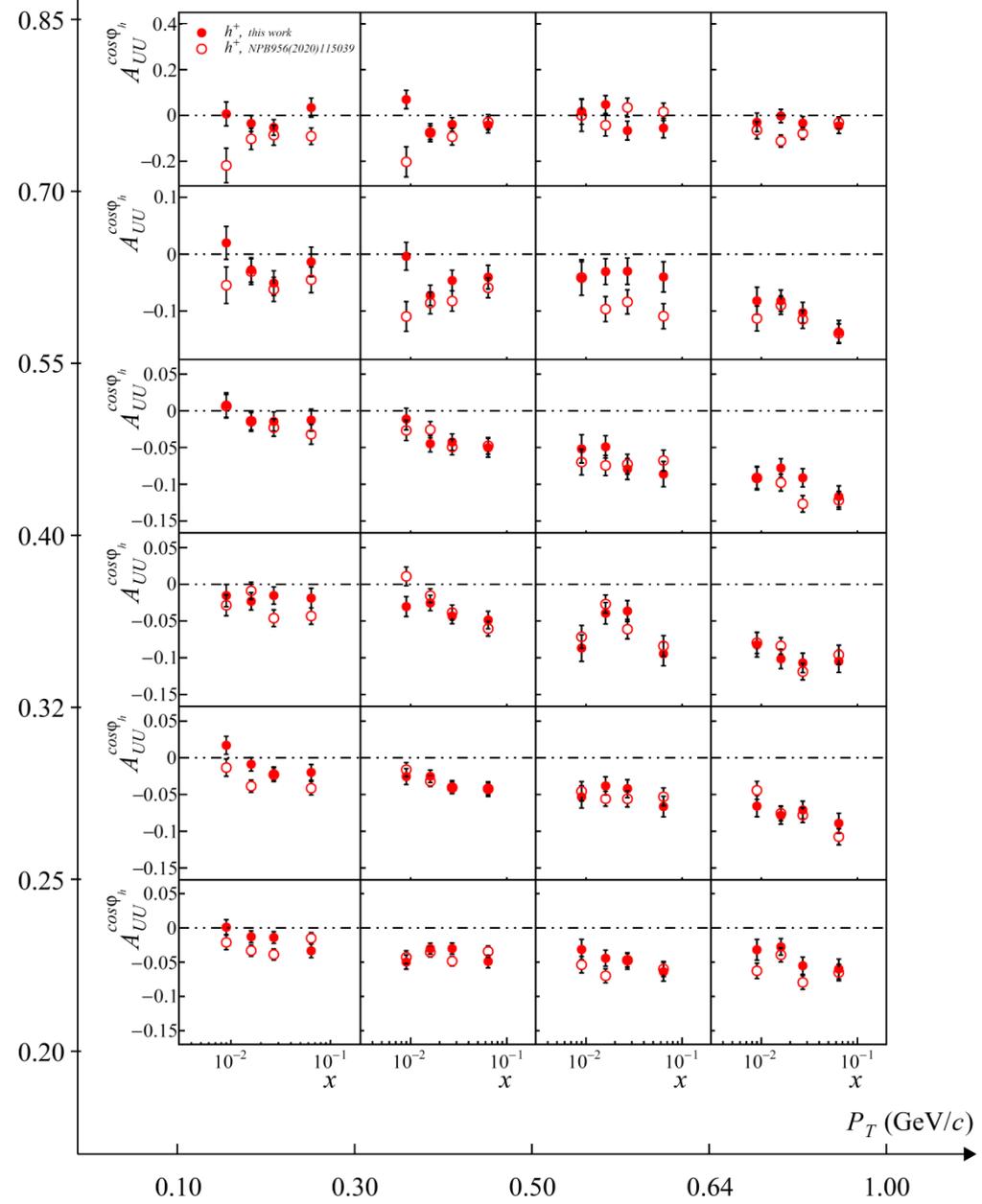
Quark	U
Nucleon	$f_1^q(x, k_T^2)$ number density 
U	



- As of 1978 – simplistic kinematic effect:
- non-zero  $k_T$  induces an azimuthal modulation
- As of 2022 – complex SF (twist-2/3 functions)
- Measurements by different experiments
  - Complex multi-D kinematic dependences
    - So far, no clear interpretation

## Recent COMPASS results (see A. Moretti's talk)

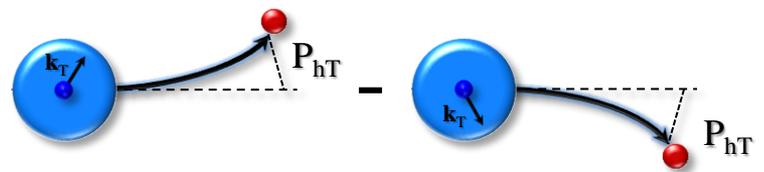
COMPASS preliminary



# Cahn effect in SIDIS

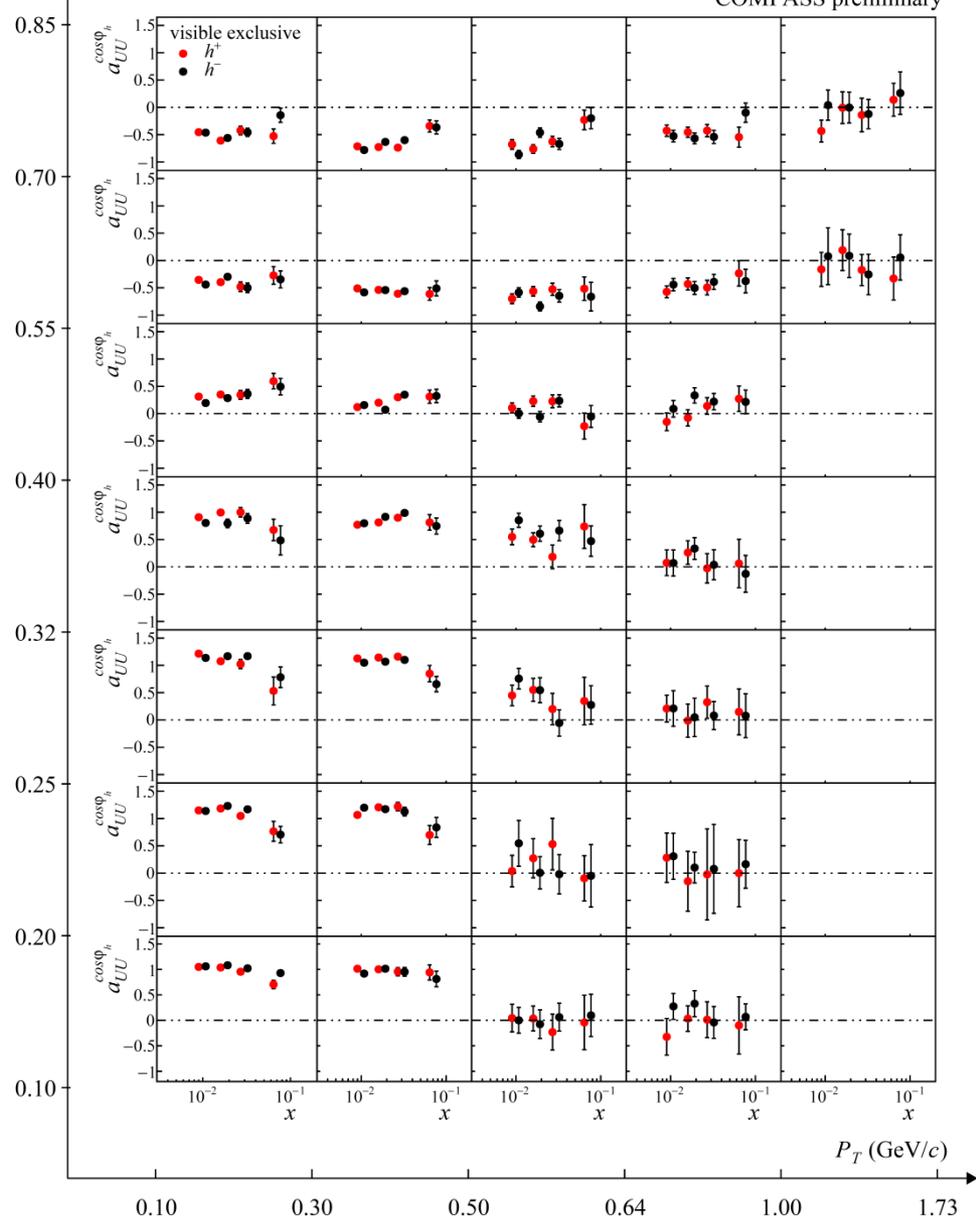
$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L}) \times ( 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \dots )$$

Quark	U
Nucleon	$f_1^q(x, k_T^2)$ number density 
U	



- As of 1978 – simplistic kinematic effect:
- non-zero  $k_T$  induces an azimuthal modulation
- As of 2022 – complex SF (twist-2/3 functions)
- Measurements by different experiments
  - Complex multi-D kinematic dependences
    - So far, no clear interpretation

## Recent COMPASS results (see A. Moretti's talk)

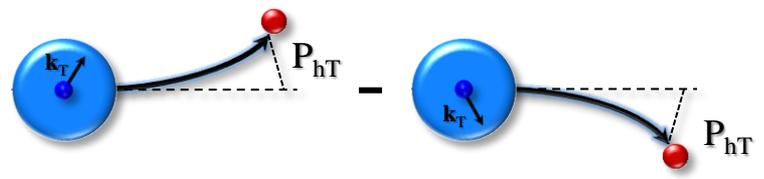


- A set of complex corrections: Acceptance, diffractively produced VMs, radiative corrections, etc.

# Cahn effect in SIDIS

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L}) \times ( 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \dots )$$

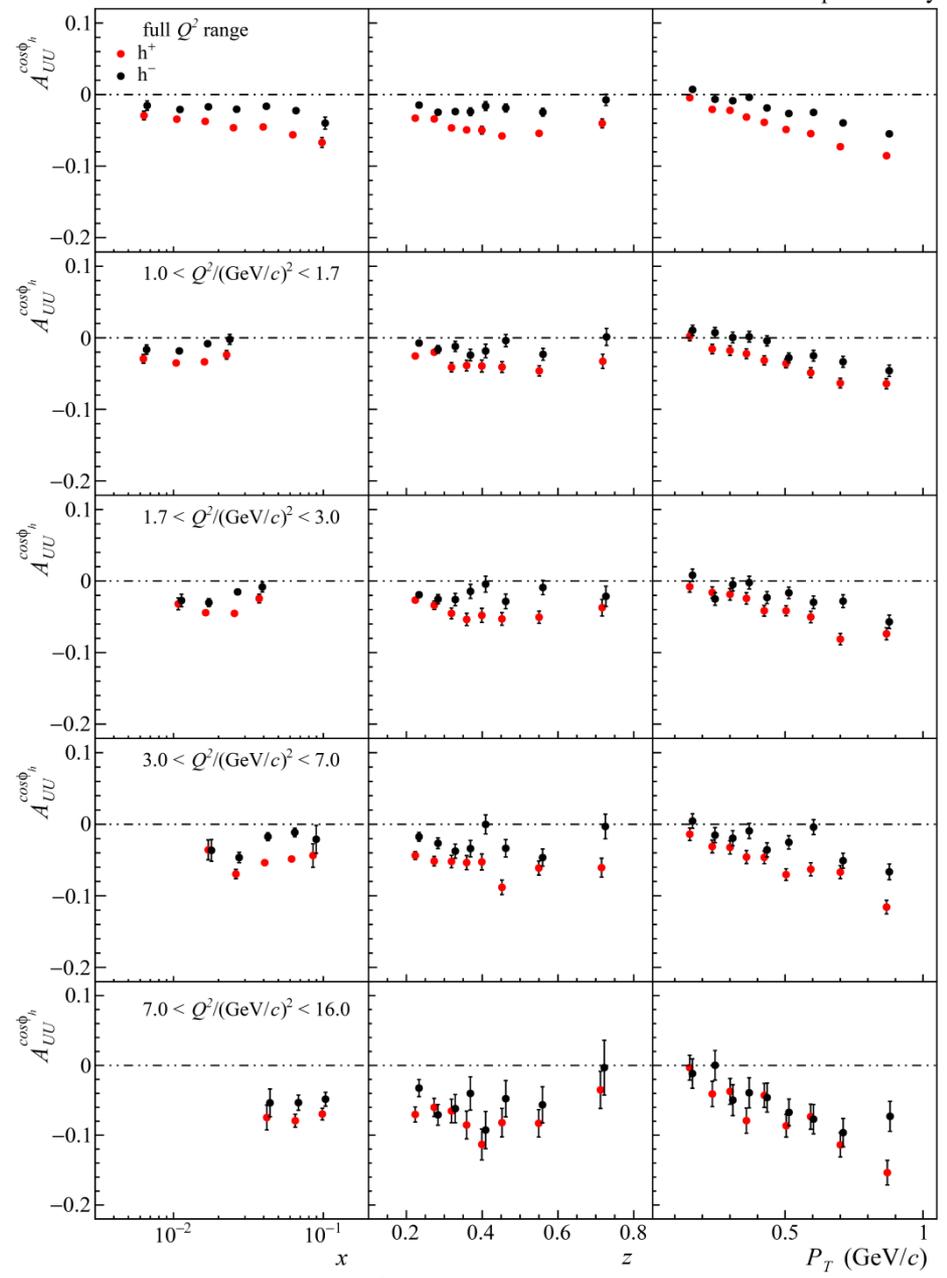
Quark	U
Nucleon	$f_1^q(x, k_T^2)$ number density 
U	



- As of 1978 – simplistic kinematic effect:
- non-zero  $k_T$  induces an azimuthal modulation
- As of 2022 – complex SF (twist-2/3 functions)
- Measurements by different experiments
  - Complex multi-D kinematic dependences
    - So far, no clear interpretation

## Recent COMPASS results (see A. Moretti's talk)

COMPASS preliminary



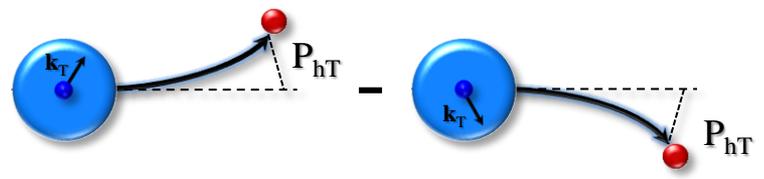
B. Parsamyan

- Strong  $Q^2$  dependence

# Cahn effect in SIDIS

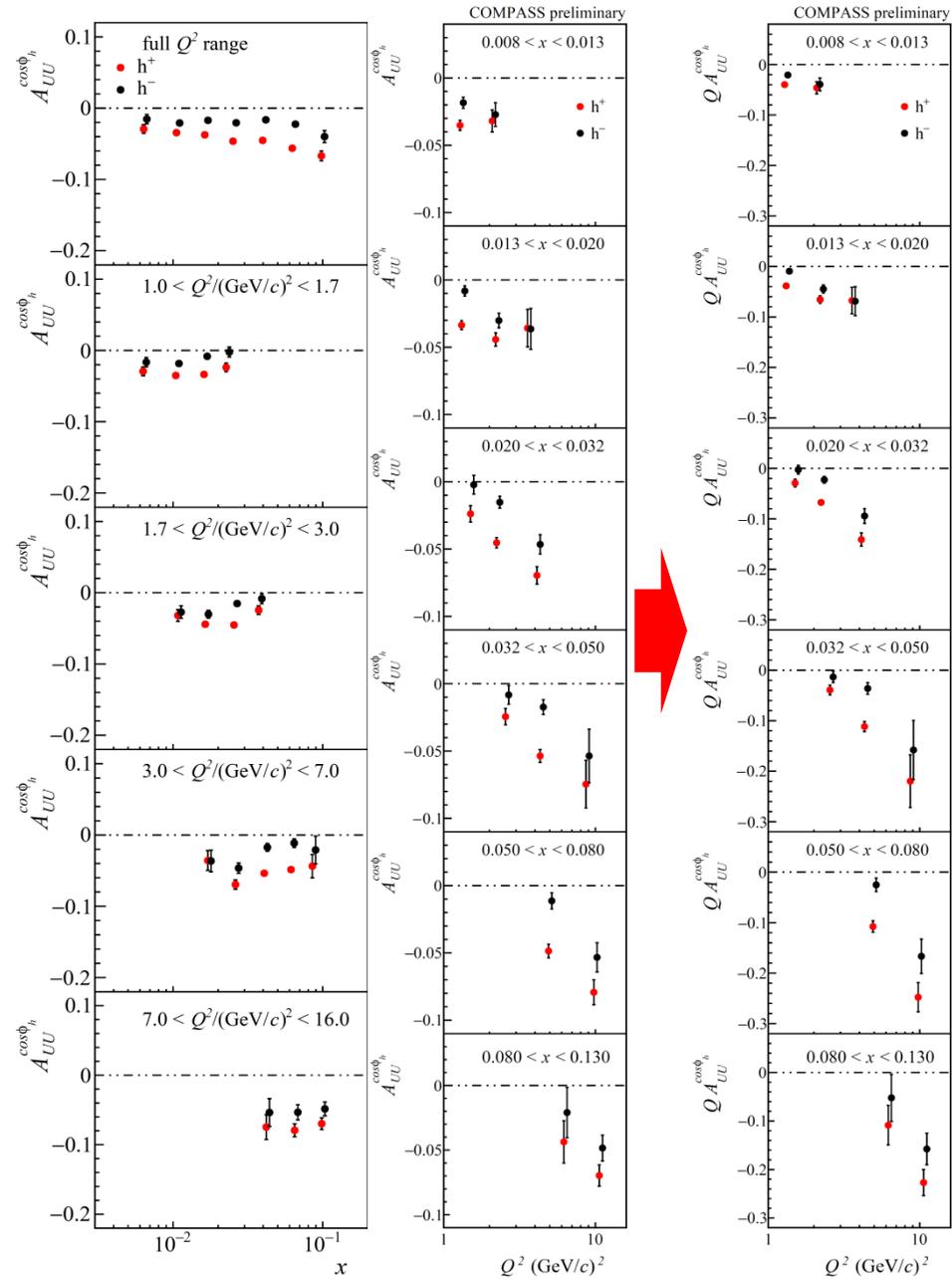
$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} = \left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L}) \times ( 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \dots )$$

Quark	U
Nucleon	$f_1^q(x, k_T^2)$ number density 
U	



- As of 1978 – simplistic kinematic effect:
- non-zero  $k_T$  induces an azimuthal modulation
- As of 2022 – complex SF (twist-2/3 functions)
- Measurements by different experiments
  - Complex multi-D kinematic dependences
    - So far, no clear interpretation

# Recent COMPASS results (see A. Moretti's talk)



B. Parsamyan

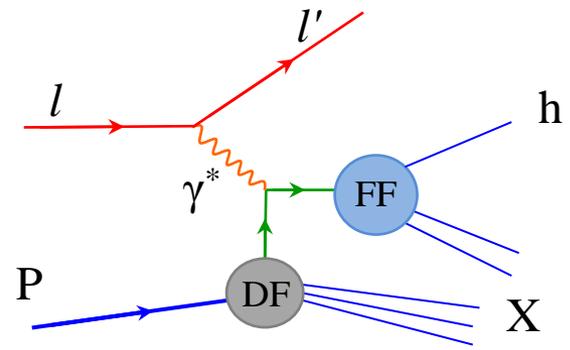
• Strong  $Q^2$  dependence

# SIDIS x-section and TMDs at twist-2

**All measured by COMPASS**

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} =$$

$$\left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L})$$



$$\times \left\{ \begin{array}{l} \left[ \begin{array}{l} 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ + \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \sin\phi_h \end{array} \right] \\ + S_L \left[ \begin{array}{l} \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \\ + S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right] \end{array} \right] \\ + S_T \left[ \begin{array}{l} A_{UT}^{\sin(\phi_h-\phi_S)} \sin(\phi_h-\phi_S) \\ + \varepsilon A_{UT}^{\sin(\phi_h+\phi_S)} \sin(\phi_h+\phi_S) \\ + \varepsilon A_{UT}^{\sin(3\phi_h-\phi_S)} \sin(3\phi_h-\phi_S) \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_S} \sin\phi_S \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h-\phi_S)} \sin(2\phi_h-\phi_S) \end{array} \right] \\ + S_T \lambda \left[ \begin{array}{l} \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_S)} \cos(\phi_h-\phi_S) \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_S} \cos\phi_S \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h-\phi_S)} \cos(2\phi_h-\phi_S) \end{array} \right] \end{array} \right.$$

Quark \ Nucleon	U	L	T
U	number density		Boer-Mulders
L		helicity	worm-gear L
T	Sivers	Kotzinian-Mulders worm-gear T	transversity pretzelosity

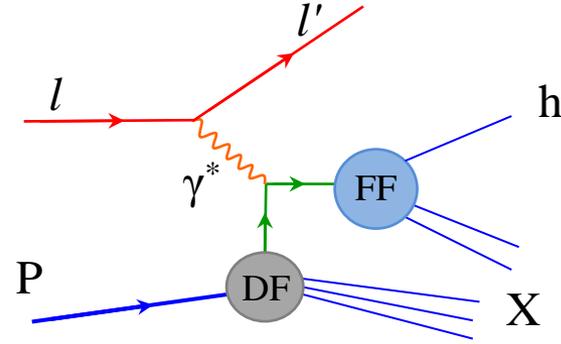
spin of the nucleon    
 spin of the quark    
  $k_T$

# SIDIS x-section and TMDs at twist-2

**All measured by COMPASS**

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_s} =$$

$$\left[ \frac{\alpha}{xyQ^2} \frac{y^2}{2(1-\varepsilon)} \left( 1 + \frac{\gamma^2}{2x} \right) \right] (F_{UU,T} + \varepsilon F_{UU,L})$$



$$\times \left\{ \begin{array}{l} \left[ \begin{array}{l} 1 + \sqrt{2\varepsilon(1+\varepsilon)} A_{UU}^{\cos\phi_h} \cos\phi_h + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ + \lambda \sqrt{2\varepsilon(1-\varepsilon)} A_{LU}^{\sin\phi_h} \sin\phi_h \end{array} \right] \\ \left[ \begin{array}{l} + S_L \left[ \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h \right] \\ + S_L \lambda \left[ \sqrt{1-\varepsilon^2} A_{LL} + \sqrt{2\varepsilon(1-\varepsilon)} A_{LL}^{\cos\phi_h} \cos\phi_h \right] \end{array} \right] \\ \left[ \begin{array}{l} A_{UT}^{\sin(\phi_h-\phi_s)} \sin(\phi_h-\phi_s) \\ + \varepsilon A_{UT}^{\sin(\phi_h+\phi_s)} \sin(\phi_h+\phi_s) \\ + \varepsilon A_{UT}^{\sin(3\phi_h-\phi_s)} \sin(3\phi_h-\phi_s) \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin\phi_s} \sin\phi_s \\ + \sqrt{2\varepsilon(1+\varepsilon)} A_{UT}^{\sin(2\phi_h-\phi_s)} \sin(2\phi_h-\phi_s) \end{array} \right] \\ \left[ \begin{array}{l} \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h-\phi_s)} \cos(\phi_h-\phi_s) \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos\phi_s} \cos\phi_s \\ + \sqrt{2\varepsilon(1-\varepsilon)} A_{LT}^{\cos(2\phi_h-\phi_s)} \cos(2\phi_h-\phi_s) \end{array} \right] \end{array} \right.$$

$$A_{UT}^{\sin(\phi_h-\phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

$$A_{UT}^{\sin(\phi_h+\phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(3\phi_h-\phi_s)} \propto h_{1T}^{\perp q} \otimes H_{1q}^{\perp h}$$

$$A_{UT}^{\sin(\phi_s)} \overset{WW}{\propto} Q^{-1} \left( h_1^q \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{UT}^{\sin(2\phi_h-\phi_s)} \overset{WW}{\propto} Q^{-1} \left( h_{1T}^{\perp q} \otimes H_{1q}^{\perp h} + f_{1T}^{\perp q} \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(\phi_h-\phi_s)} \propto g_{1T}^q \otimes D_{1q}^h$$

$$A_{LT}^{\cos(\phi_s)} \overset{WW}{\propto} Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

$$A_{LT}^{\cos(2\phi_h-\phi_s)} \overset{WW}{\propto} Q^{-1} \left( g_{1T}^q \otimes D_{1q}^h + \dots \right)$$

Twist-2

Twist-3

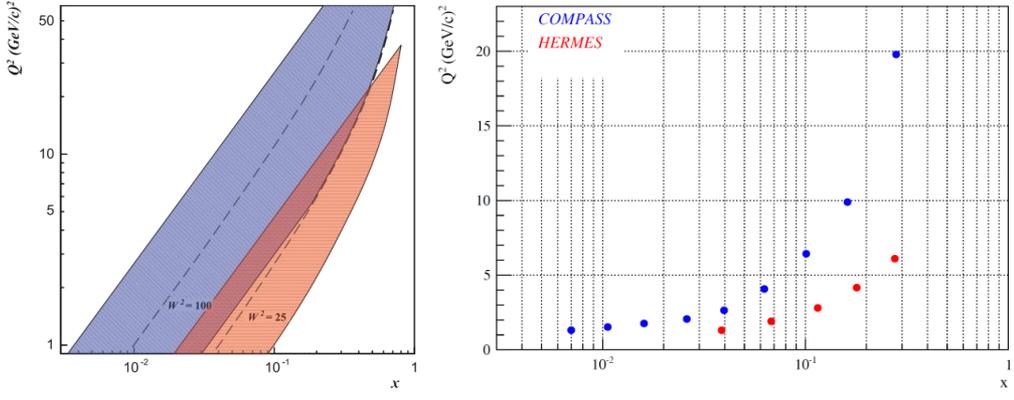
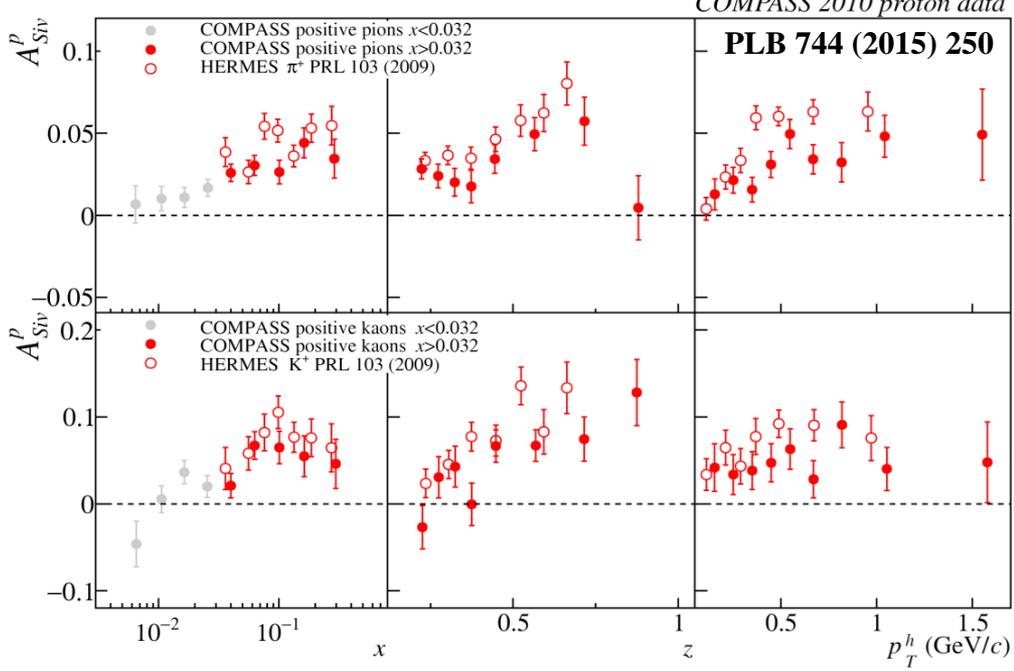
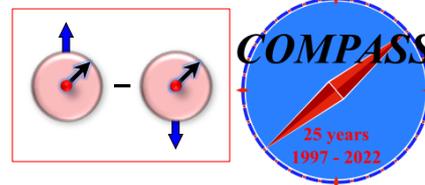
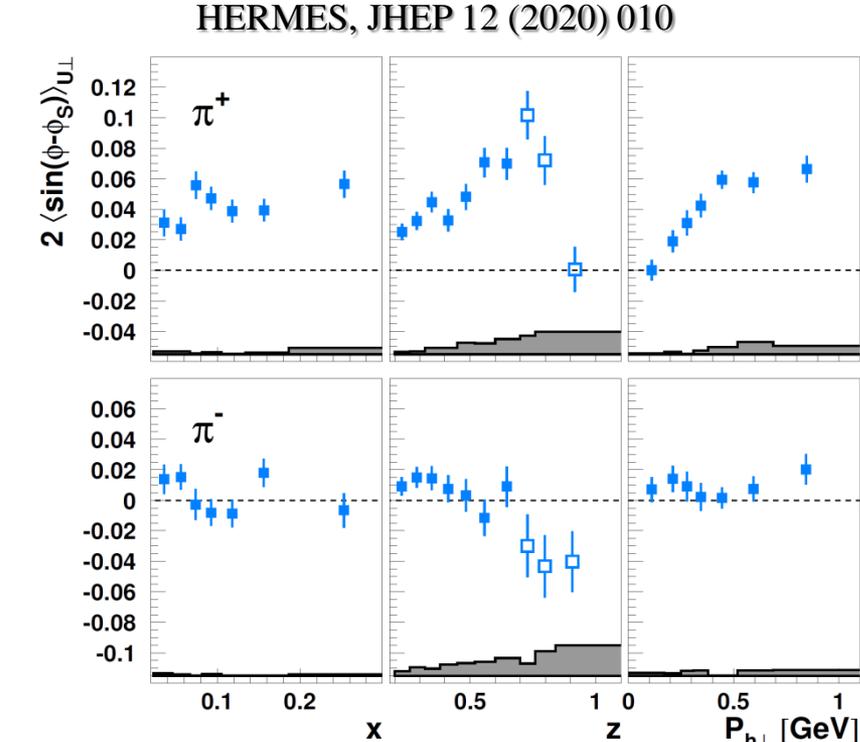
# SIDIS TSAs: Sivers effect

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_T A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) + \dots \right\}$$

$$F_{UT,T}^{\sin(\phi_h - \phi_S)} = C \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M} f_{1T}^{\perp q} D_{1q}^h \right], F_{UT,L}^{\sin(\phi_h - \phi_S)} = 0$$



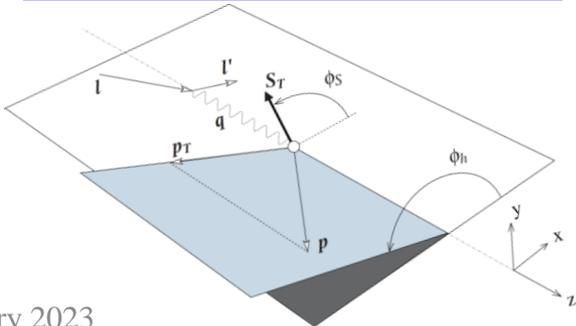
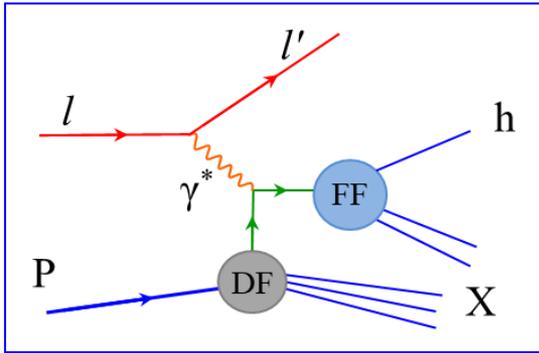
- Measured on proton and deuteron
- Expected to change sign between SIDIS and Drell-Yan



# SIDIS and single-polarized DY x-sections at twist-2 (LO)

$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \quad \text{SIDIS}$$

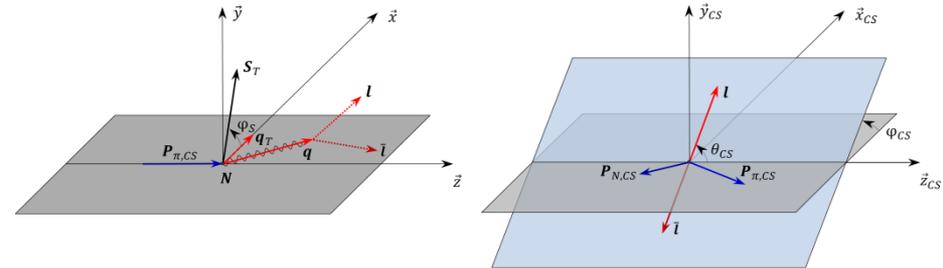
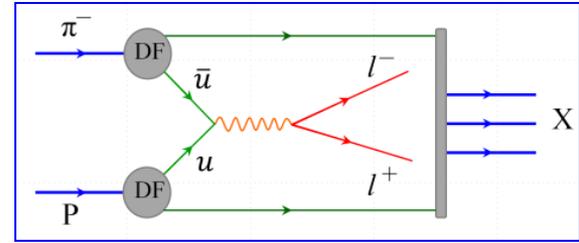
$$\left\{ \begin{aligned} & 1 + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ & + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \end{aligned} \right\} \times \left\{ \begin{aligned} & S_T \begin{bmatrix} A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} \sin(3\phi_h - \phi_S) \end{bmatrix} \\ & + S_T \lambda \left[ \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) \right] \end{aligned} \right\}$$



$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS}) \quad \text{DY}$$

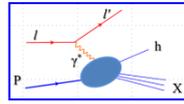
$$\left\{ \begin{aligned} & 1 + D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} \\ & + S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \end{aligned} \right\} \times \left\{ \begin{aligned} & S_T \begin{bmatrix} A_T^{\sin \varphi_S} \sin \varphi_S \\ + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\varphi_{CS} - \varphi_S)} \sin(2\varphi_{CS} - \varphi_S) \right. \right. \\ \left. \left. + A_T^{\sin(2\varphi_{CS} + \varphi_S)} \sin(2\varphi_{CS} + \varphi_S) \right) \end{bmatrix} \end{aligned} \right\}$$

where  $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$

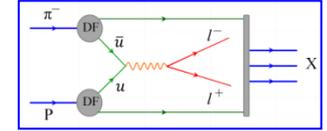


# SIDIS and single-polarized DY x-sections at twist-2 (LO)

$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$



$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$$



$$\left\{ \begin{aligned} & 1 + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ & + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1 - \varepsilon^2} A_{LL} \\ & + S_T \begin{bmatrix} A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} \sin(3\phi_h - \phi_S) \end{bmatrix} \\ & + S_T \lambda \left[ \sqrt{(1 - \varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) \right] \end{aligned} \right\} \times \left\{ \begin{aligned} & 1 + D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} \\ & + S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \\ & + S_T \begin{bmatrix} A_T^{\sin \varphi_S} \sin \varphi_S \\ + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\varphi_{CS} - \varphi_S)} \sin(2\varphi_{CS} - \varphi_S) \right. \\ \left. + A_T^{\sin(2\varphi_{CS} + \varphi_S)} \sin(2\varphi_{CS} + \varphi_S) \right) \end{bmatrix} \end{aligned} \right\}$$

**SIDIS-DY bridge**

where  $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$

$A_{UU}^{\cos 2\phi_h} \propto \underline{h_1^{\perp q}} \otimes \underline{H_{1q}^{\perp h}} + \dots$	Boer-Mulders	$A_U^{\cos 2\varphi_{CS}} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1,p}^{\perp q}}$
$A_{UT}^{\sin(\phi_h - \phi_S)} \propto \underline{f_{1T}^{\perp q}} \otimes \underline{D_{1q}^h}$	Sivers	$A_T^{\sin \varphi_S} \propto \underline{f_{1,\pi}^q} \otimes \underline{f_{1T,p}^{\perp q}}$
$A_{UT}^{\sin(\phi_h + \phi_S)} \propto \underline{h_1^q} \otimes \underline{H_{1q}^{\perp h}}$	Transversity	$A_T^{\sin(2\varphi_{CS} - \varphi_S)} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1,p}^q}$
$A_{UT}^{\sin(3\phi_h - \phi_S)} \propto \underline{h_{1T}^{\perp q}} \otimes \underline{H_{1q}^{\perp h}}$	Pretzelosity	$A_T^{\sin(2\varphi_{CS} + \varphi_S)} \propto \underline{h_{1,\pi}^{\perp q}} \otimes \underline{h_{1T,p}^{\perp q}}$

Complementary information from two different channels :

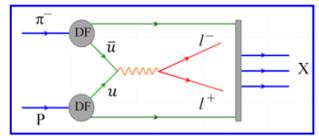
- SIDIS-DY bridging of nucleon TMD PDFs; Universality studies;
- **Sign-change of T-odd Sivers and Boer-Mulders TMD PDFs;**
- Multiple access to Collins FF  $H_{1q}^{\perp h}$  and pion Boer-Mulders PDF  $h_{1,\pi}^{\perp q}$

# Single-polarized DY measurements at COMPASS

- $1.0 < M/(GeV/c^2) < 2.0$  “Low mass”
  - Large background contamination, combinatorial, Open-charm (B)  $D\bar{D}$ ,  $B\bar{B}$ ,  $\pi$ , K decays
- $2.0 < M/(GeV/c^2) < 2.5$  “Intermediate mass”
  - High DY-cross section
  - Still low DY-signal/background ratio
- $2.5 < M/(GeV/c^2) < 4.3$  “Charmonia mass”
  - Strong  $J/\psi$ -signal  $\rightarrow$  study of  $J/\psi$  physics
  - Good signal/background
- $4.3 < M/(GeV/c^2) < 8.5$  “High mass”
  - Low DY cross-section
  - Beyond charmonium region, background  $< 3\%$
  - Valence region  $\rightarrow$  largest asymmetries

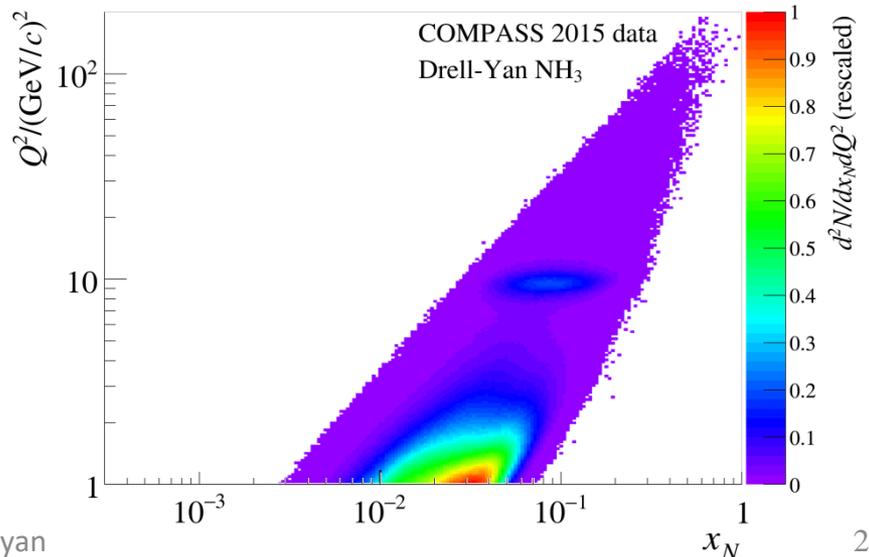
$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$$

$$\left\{ 1 + D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} + S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \right\} \times \left\{ S_T \left[ A_T^{\sin \varphi_S} \sin \varphi_S + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\varphi_{CS} - \varphi_S)} \sin(2\varphi_{CS} - \varphi_S) + A_T^{\sin(2\varphi_{CS} + \varphi_S)} \sin(2\varphi_{CS} + \varphi_S) \right) \right] \right\}$$

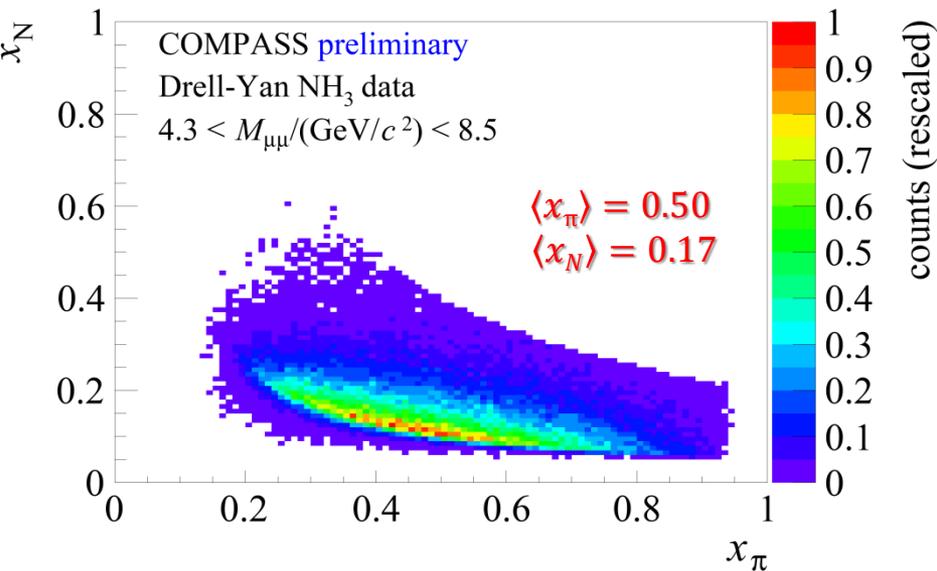


$$D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$$

COMPASS x:Q<sup>2</sup> phase space



# Single-polarized DY measurements at COMPASS

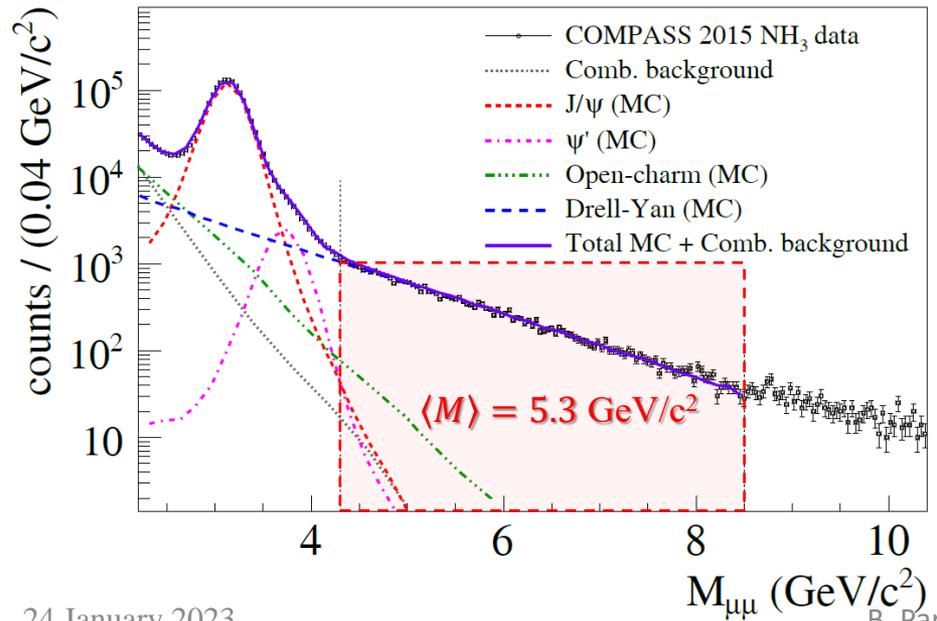


$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$$

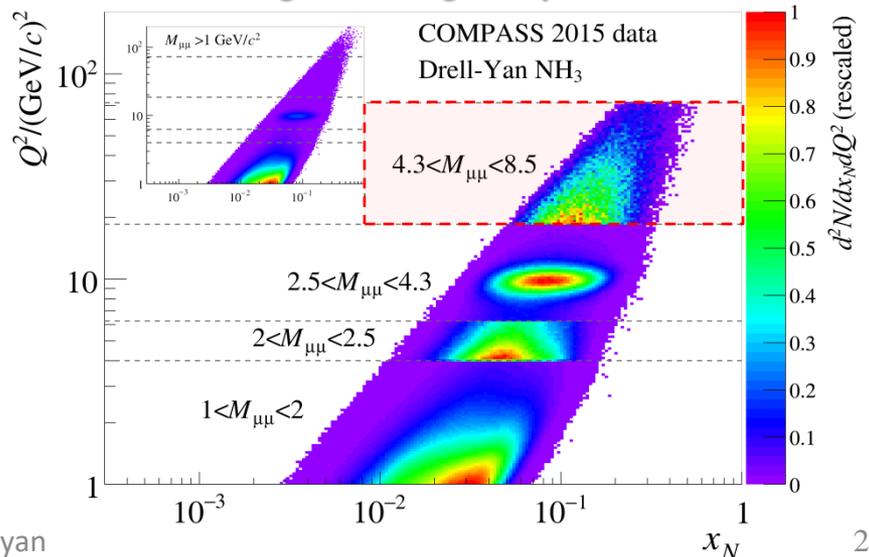
$$\left\{ 1 + D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} + S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \right\} \times \left\{ S_T \left[ A_T^{\sin \varphi_S} \sin \varphi_S + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\varphi_{CS} - \varphi_S)} \sin(2\varphi_{CS} - \varphi_S) + A_T^{\sin(2\varphi_{CS} + \varphi_S)} \sin(2\varphi_{CS} + \varphi_S) \right) \right] \right\}$$

$$D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$$

## HM events are in the valence quark range



**4.3 < M / (GeV/c<sup>2</sup>) < 8.5 “High mass” range**  
**Beyond charmonium region, background < 3%**  
**Valence region → largest asymmetries**





# SIDIS and single-polarized DY x-sections at twist-2 (LO)

**SIDIS**

$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$

$$\left\{ \begin{aligned} & 1 + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ & + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \end{aligned} \right.$$

$$\times \left\{ \begin{aligned} & S_T \begin{bmatrix} A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) \\ + \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \\ + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} \sin(3\phi_h - \phi_S) \end{bmatrix} \\ & + S_T \lambda \left[ \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) \right] \end{aligned} \right.$$

**DY**

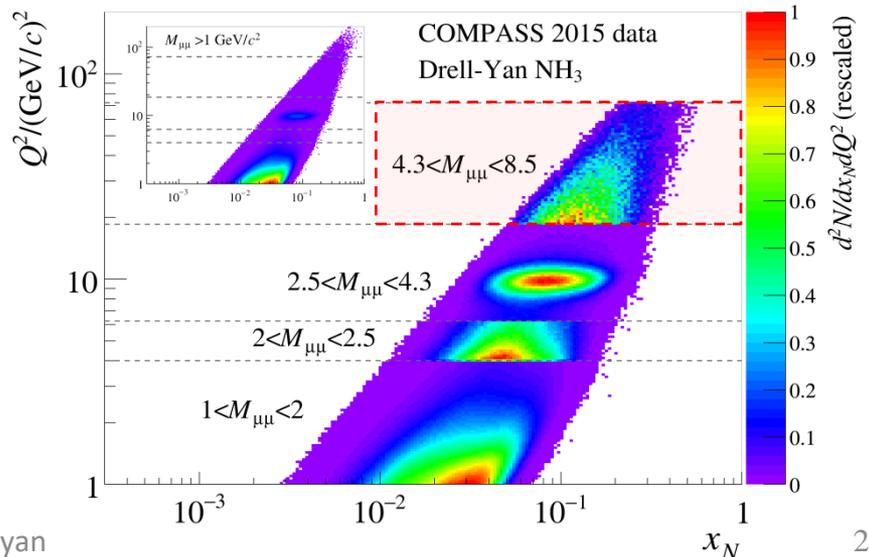
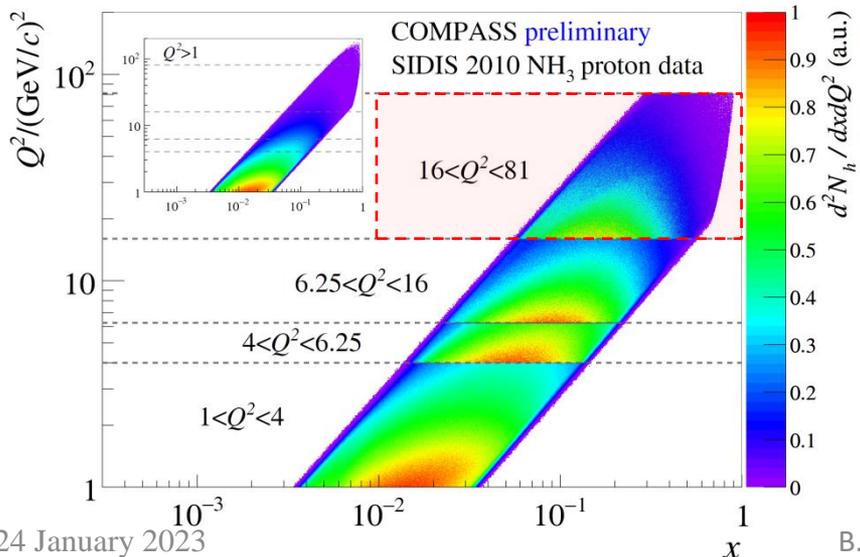
$$\frac{d\sigma^{LO}}{dq^4 d\Omega} \propto F_U^1 (1 + \cos^2 \theta_{CS})$$

$$\left\{ \begin{aligned} & 1 + D_{[\sin^2 \theta_{CS}]} A_U^{\cos 2\varphi_{CS}} \cos 2\varphi_{CS} \\ & + S_L \sin^2 \theta_{CS} A_L^{\sin 2\varphi_{CS}} \sin 2\varphi_{CS} \end{aligned} \right.$$

$$\times \left\{ \begin{aligned} & S_T \begin{bmatrix} A_T^{\sin \varphi_S} \sin \varphi_S \\ + D_{[\sin^2 \theta_{CS}]} \left( A_T^{\sin(2\varphi_{CS} - \varphi_S)} \sin(2\varphi_{CS} - \varphi_S) \right. \\ \left. + A_T^{\sin(2\varphi_{CS} + \varphi_S)} \sin(2\varphi_{CS} + \varphi_S) \right) \end{bmatrix} \end{aligned} \right.$$

where  $D_{[\sin^2 \theta_{CS}]} = \sin^2 \theta_{CS} / (1 + \cos^2 \theta_{CS})$

Comparable x:Q<sup>2</sup> coverage – minimization of possible Q<sup>2</sup>-evolution effects

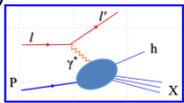


# SIDIS and single-polarized DY x-sections at twist-2 (LO)

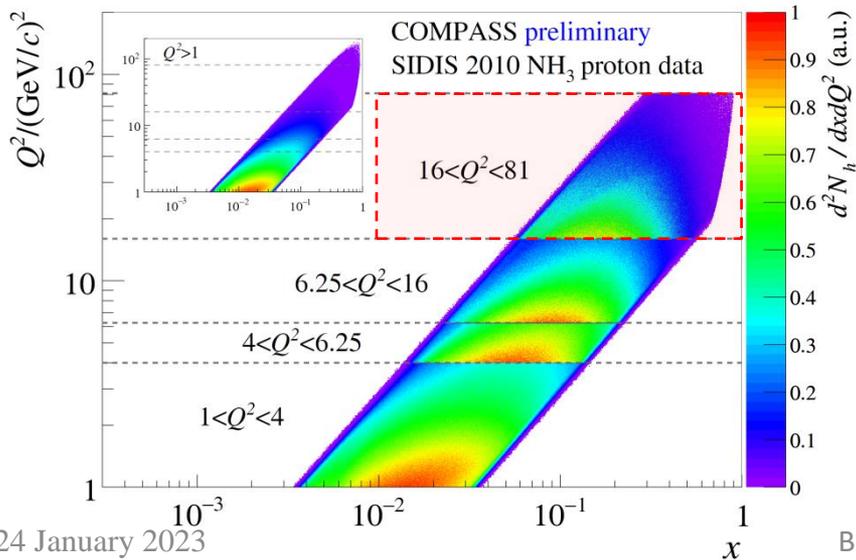


**SIDIS**

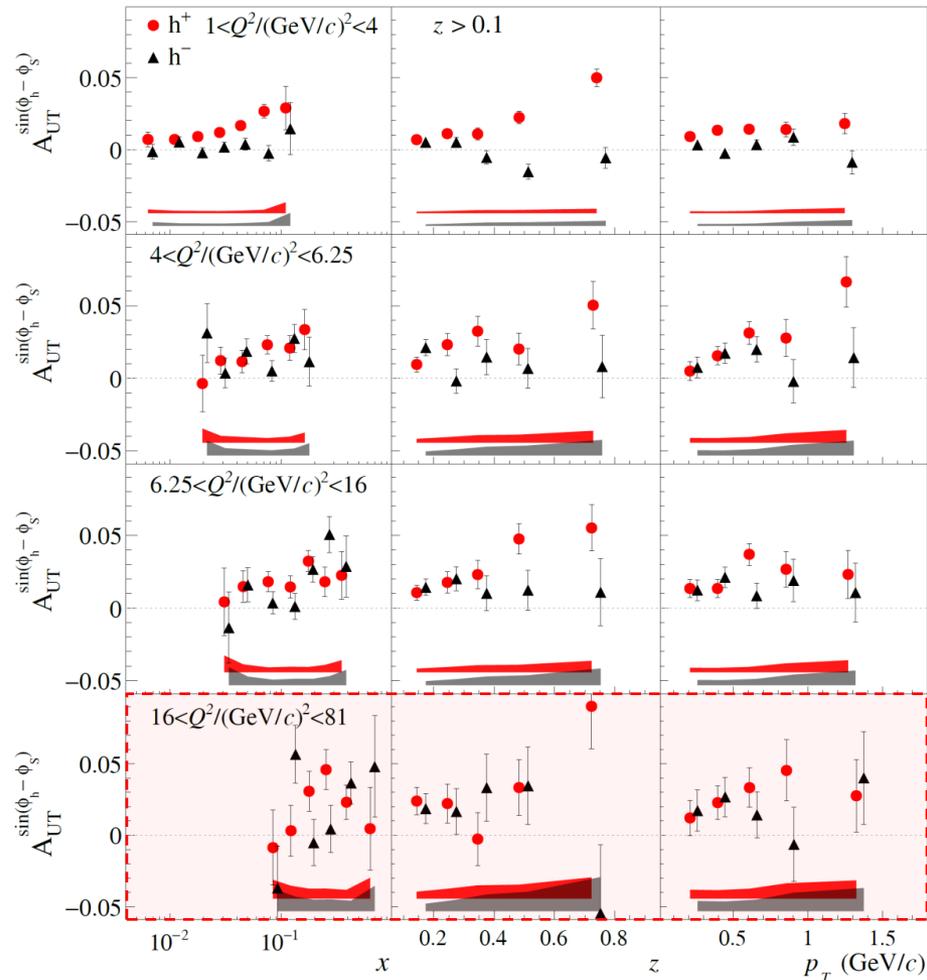
$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$



$$\left\{ \begin{aligned} & 1 + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ & + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1-\varepsilon^2} A_{LL} \\ & \times \left\{ \begin{aligned} & + S_T \left[ \begin{aligned} & A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) \\ & + \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \\ & + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} \sin(3\phi_h - \phi_S) \end{aligned} \right] \\ & + S_T \lambda \left[ \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) \right] \end{aligned} \right. \end{aligned} \right.$$



COMPASS PLB 770 (2017) 138



1<sup>st</sup> COMPASS multi-D fit done for all eight TSAs

# SIDIS and single-polarized DY $\chi$ -sections at twist-2 (LO)

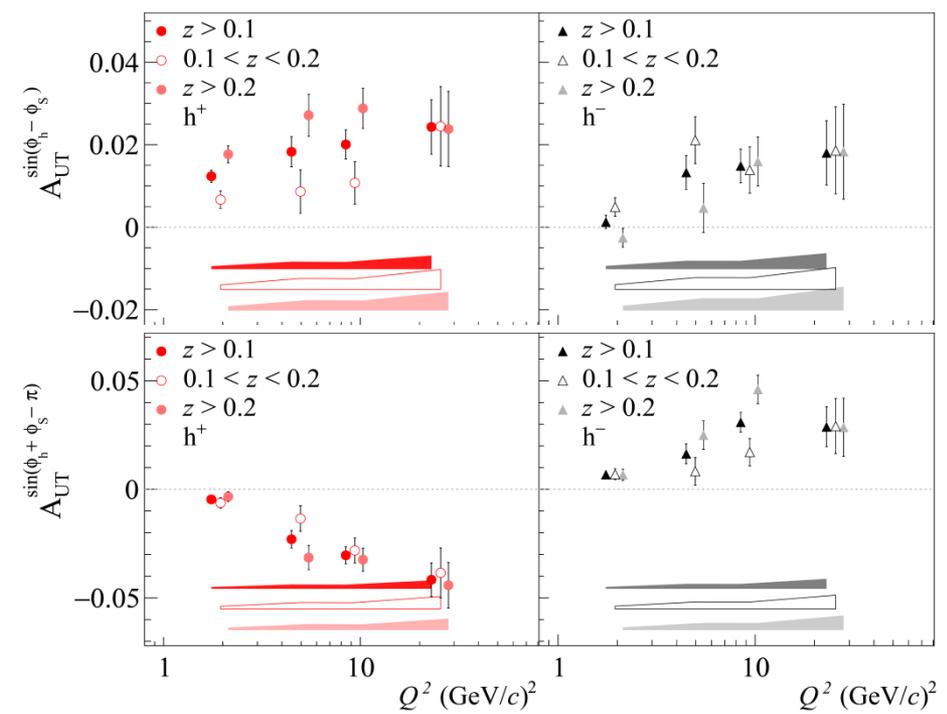
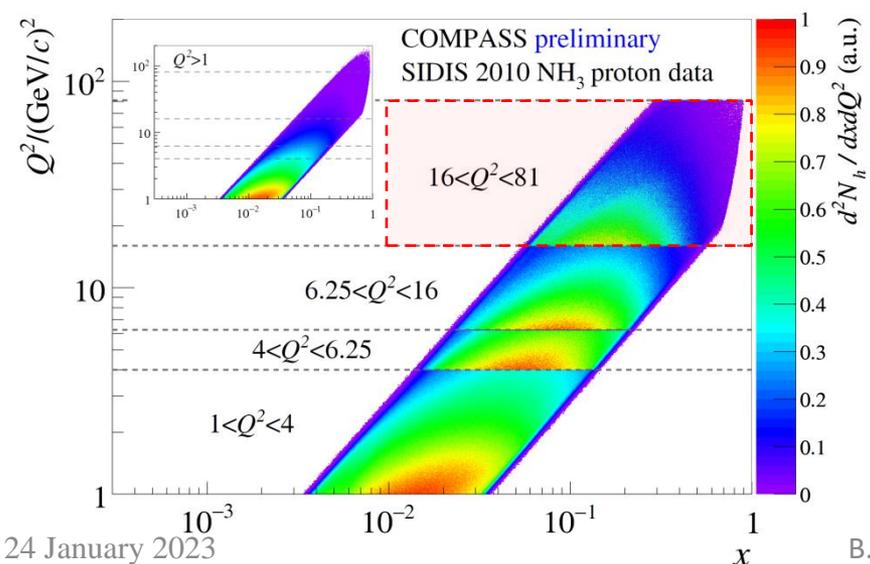
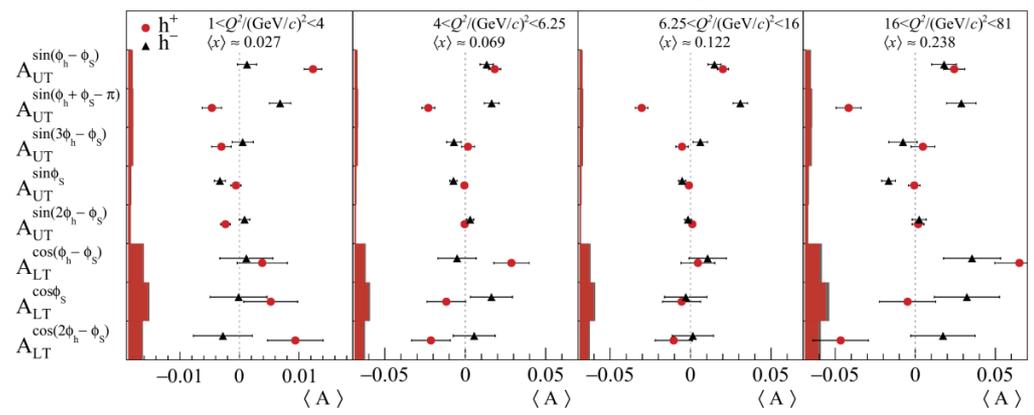


COMPASS PLB 770 (2017) 138  
1<sup>st</sup> COMPASS multi-D fit done for all eight TSAs

$$\frac{d\sigma^{LO}}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L})$$

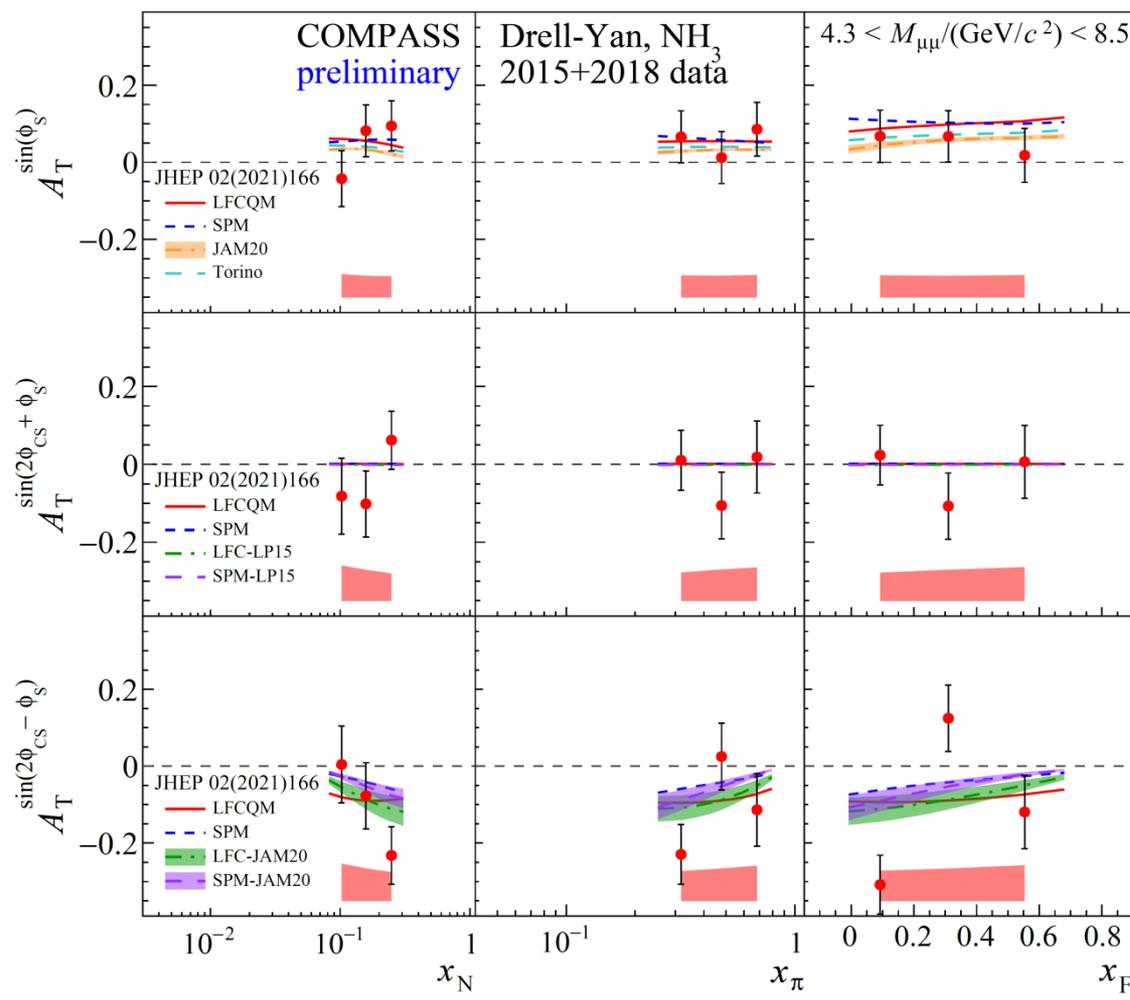
**SIDIS**

$$\left\{ \begin{aligned} & 1 + \varepsilon A_{UU}^{\cos 2\phi_h} \cos 2\phi_h \\ & + S_L \varepsilon A_{UL}^{\sin 2\phi_h} \sin 2\phi_h + S_L \lambda \sqrt{1 - \varepsilon^2} A_{LL} \\ & + S_T \left[ \begin{aligned} & A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) \\ & + \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \\ & + \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} \sin(3\phi_h - \phi_S) \end{aligned} \right] \\ & + S_T \lambda \left[ \sqrt{1 - \varepsilon^2} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) \right] \end{aligned} \right\}$$

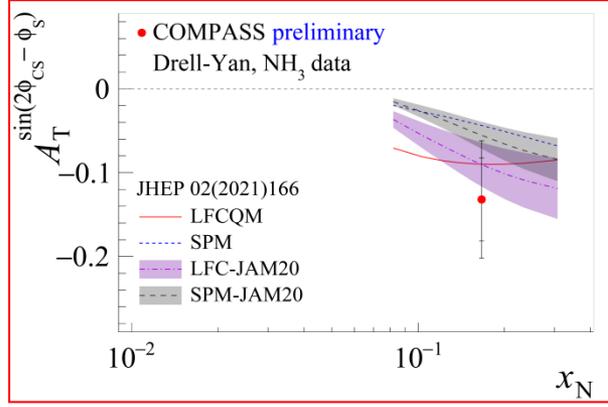
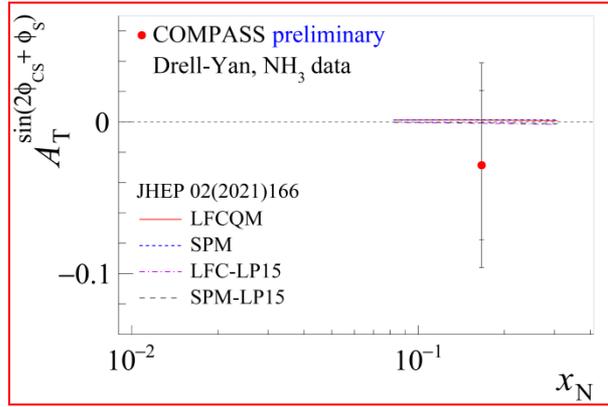
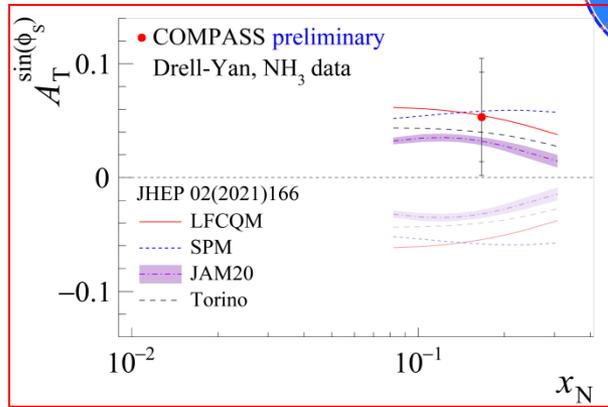


# DY TSAs at COMPASS (high-mass range)

Theory curves based on S. Bastami et al. JHEP 02, (2021),166



- General agreement with available theory predictions



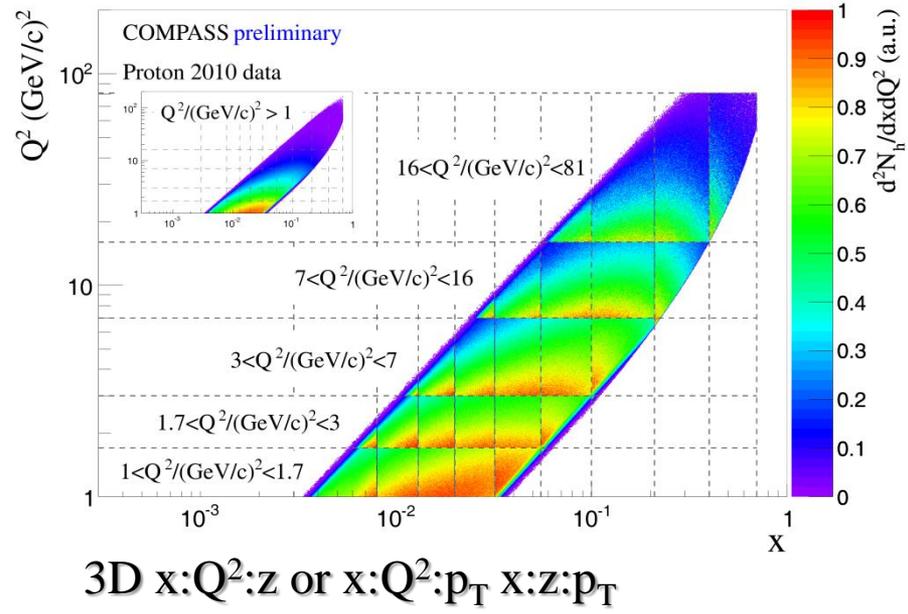
# COMPASS Multi-D TSA analyses

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_T A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) + S_T \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) \dots \right\}$$

$$F_{UT,T}^{\sin(\phi_h - \phi_S)} = C \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M} f_{1T}^{\perp q} D_{1q}^h \right], F_{UT,L}^{\sin(\phi_h - \phi_S)} = 0$$

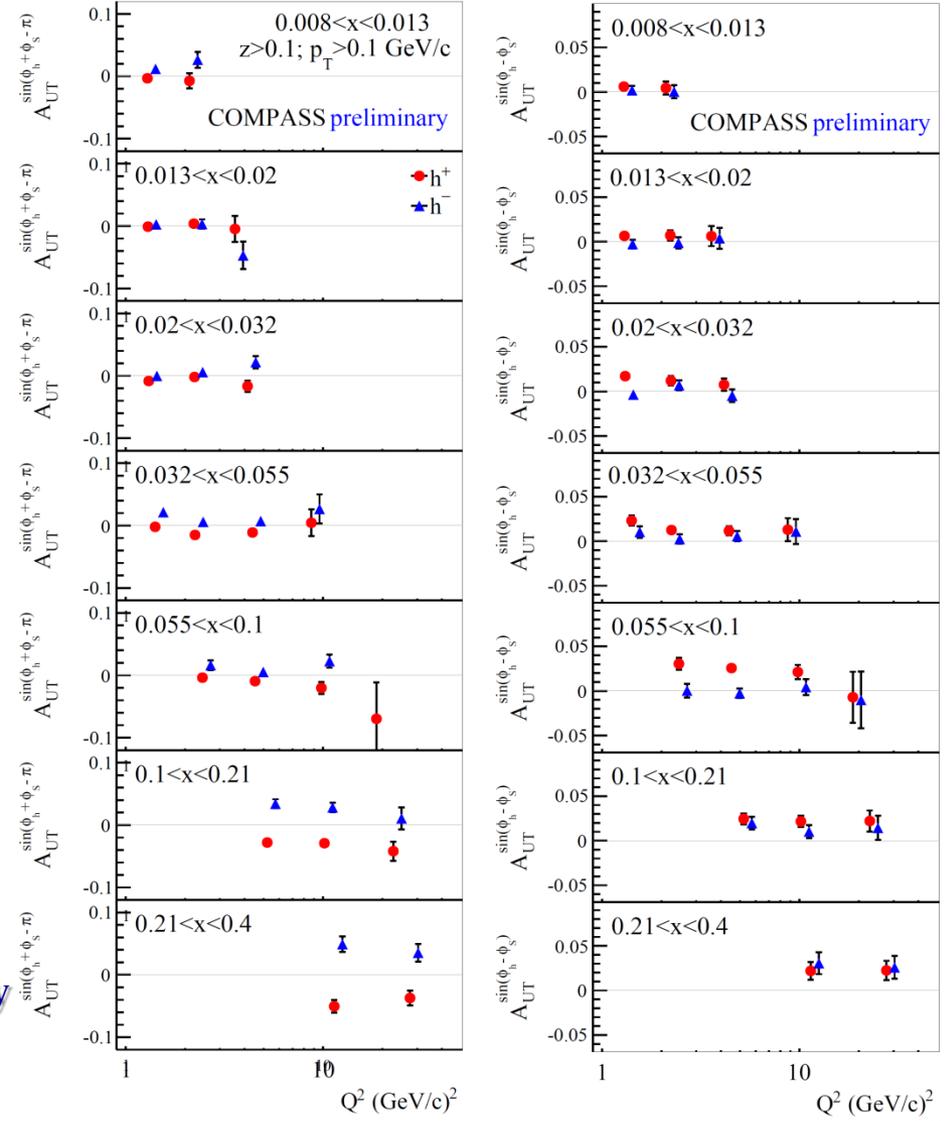


$$F_{UT}^{\sin(\phi_h + \phi_S)} = C \left[ -\frac{\hat{h} \cdot \mathbf{p}_T}{M_h} h_1^q H_{1q}^{\perp h} \right]$$



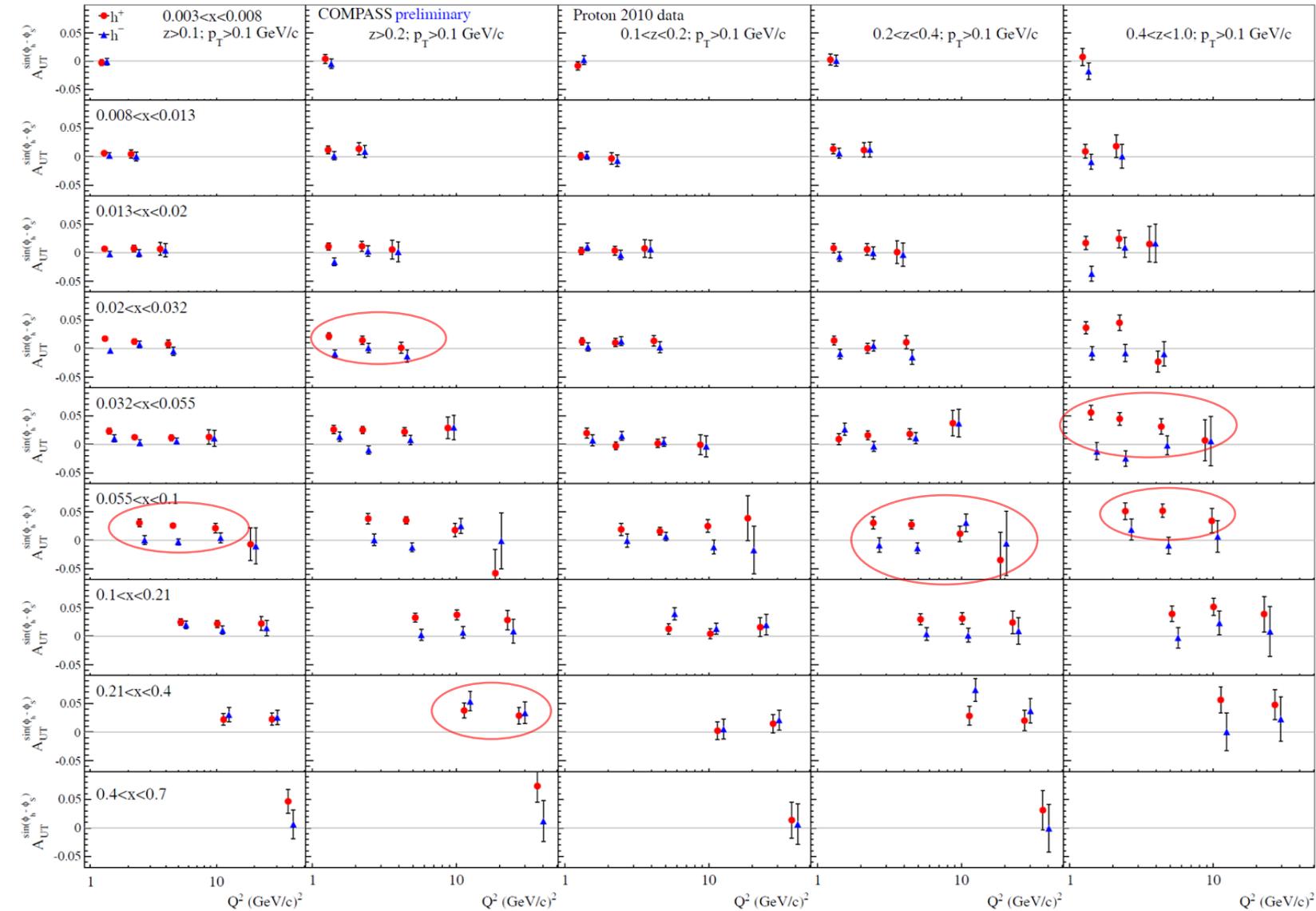
- No clear  $Q^2$ -dependence within statistical accuracy
- Possible decreasing trend for Sivers TSA?

B. Parsamyan (for COMPASS) [arXiv:1504.01599](https://arxiv.org/abs/1504.01599) [hep-ex] (SPIN-2014)



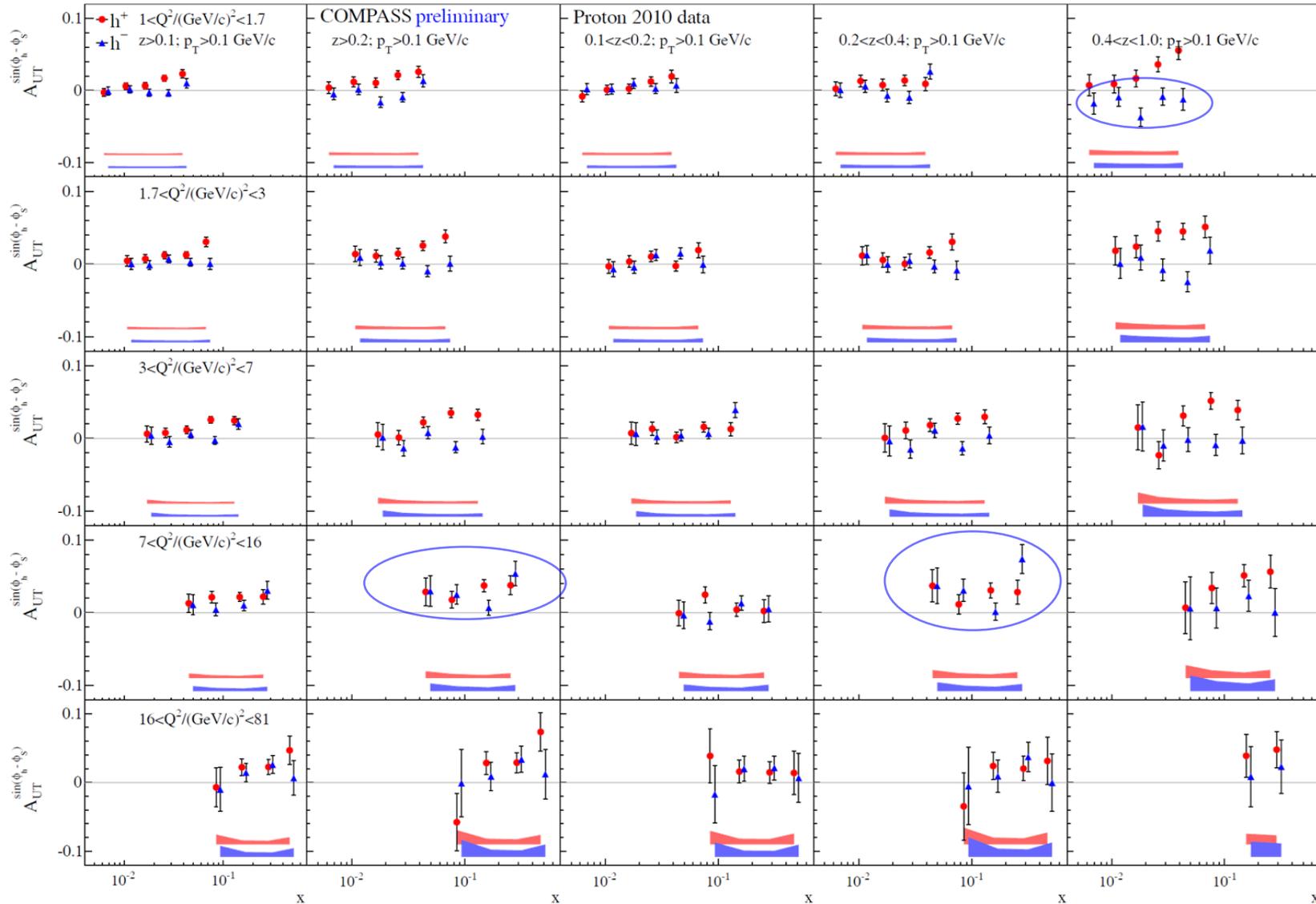
3D

# Sivers asymmetry: 3D x-z-Q<sup>2</sup> dependence



- In several x-bins some hints for possible Q<sup>2</sup>-dependence for positive hadrons (decrease) **more evident at large z**
- At **low z** effect for h<sup>+</sup> is smaller in general
- No clear picture for negative hadrons

# Sivers asymmetry: 3D $Q^2$ - $z$ - $x$ dependence



- Positive amplitude for  $h^+$  (increasing with  $x$  and  $z$ )
- Positive  $h^-$  amplitude at relatively large  $x$  ( $>0.032$ ) and  $Q^2$  ( $>7$ ) at **intermediate and large  $z$**
- Some hint for a possible negative  $h^-$  amplitude at low  $x$  ( $<0.032$ ) and  $Q^2$  ( $<7$ ) ) at **intermediate and large  $z$**

# COMPASS Multi-D TSA analyses

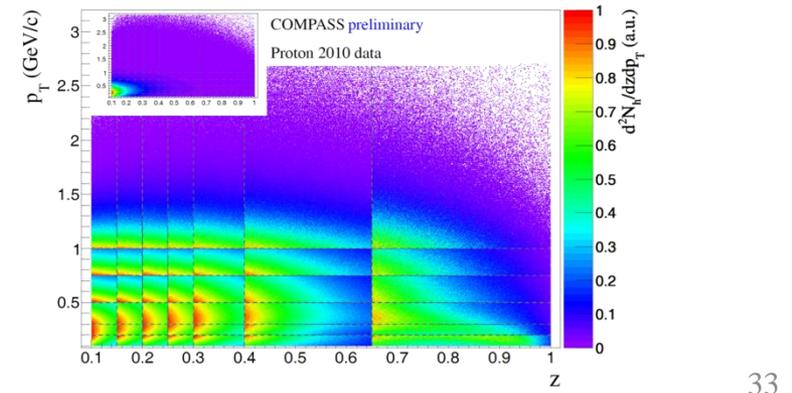
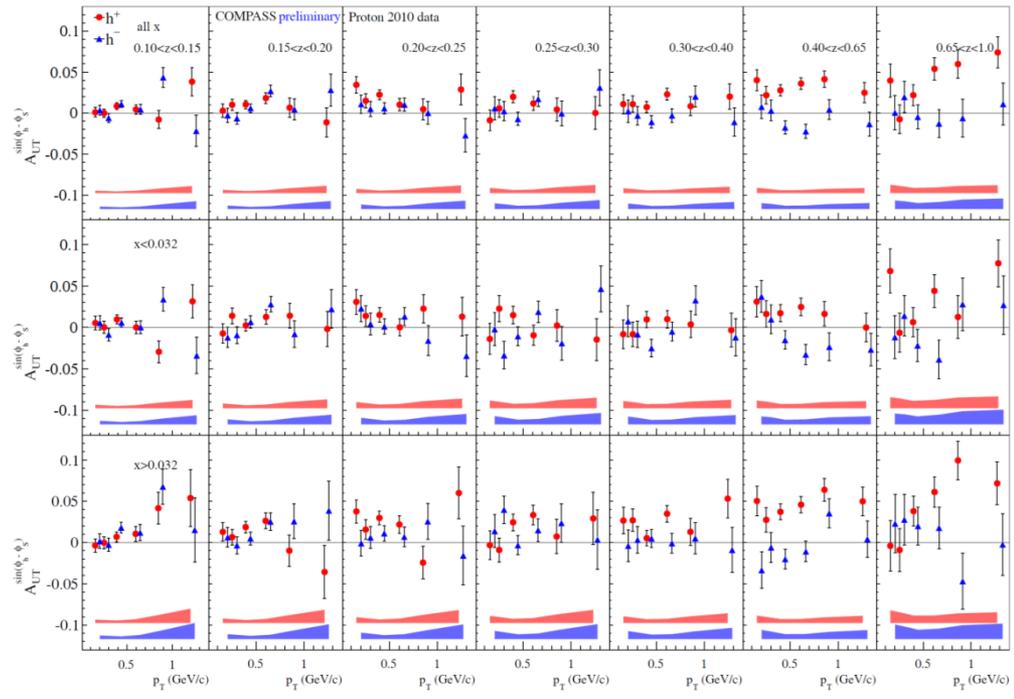
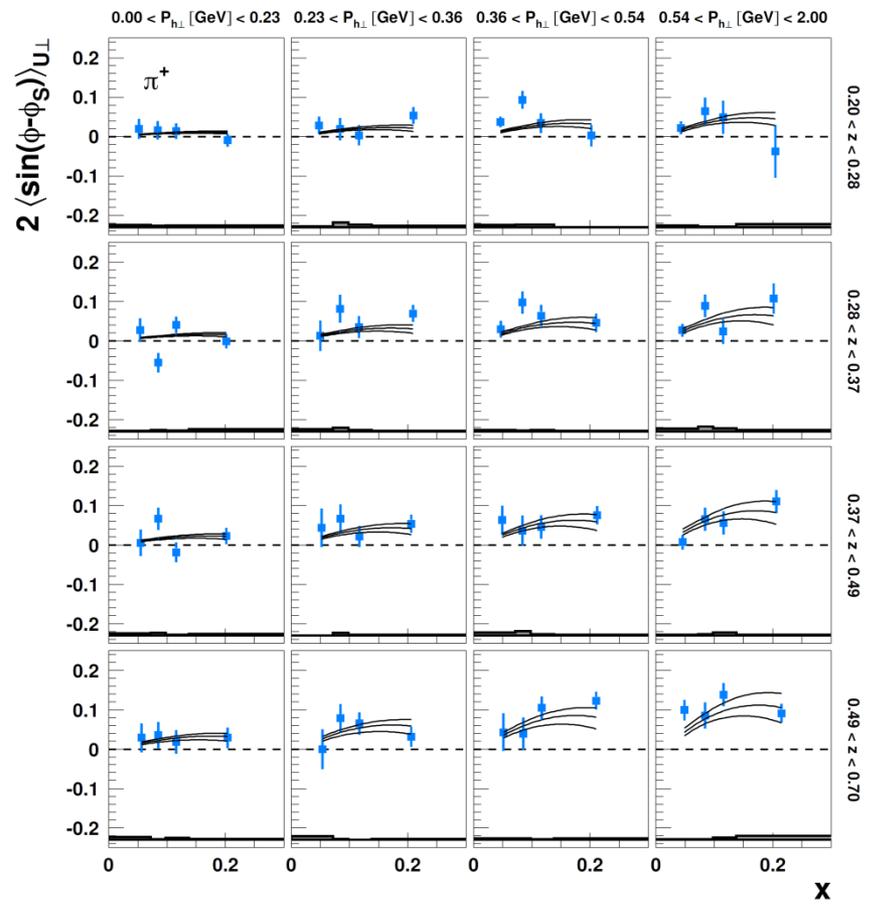
$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_T A_{UT}^{\sin(\phi_h - \phi_S)} \sin(\phi_h - \phi_S) + \dots \right\}$$

$$F_{UT,T}^{\sin(\phi_h - \phi_S)} = C \left[ -\frac{\hat{h} \cdot \mathbf{k}_T}{M} f_{1T}^{\perp q} D_{1q}^h \right], F_{UT,L}^{\sin(\phi_h - \phi_S)} = 0$$

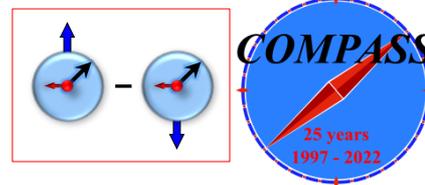


B. Parsamyan (for COMPASS) [arXiv:1504.01599](https://arxiv.org/abs/1504.01599) [hep-ex] (SPIN-2014)

HERMES, JHEP 12 (2020) 010



# SIDIS TSAs: Kotzinian-Mulders asymmetry



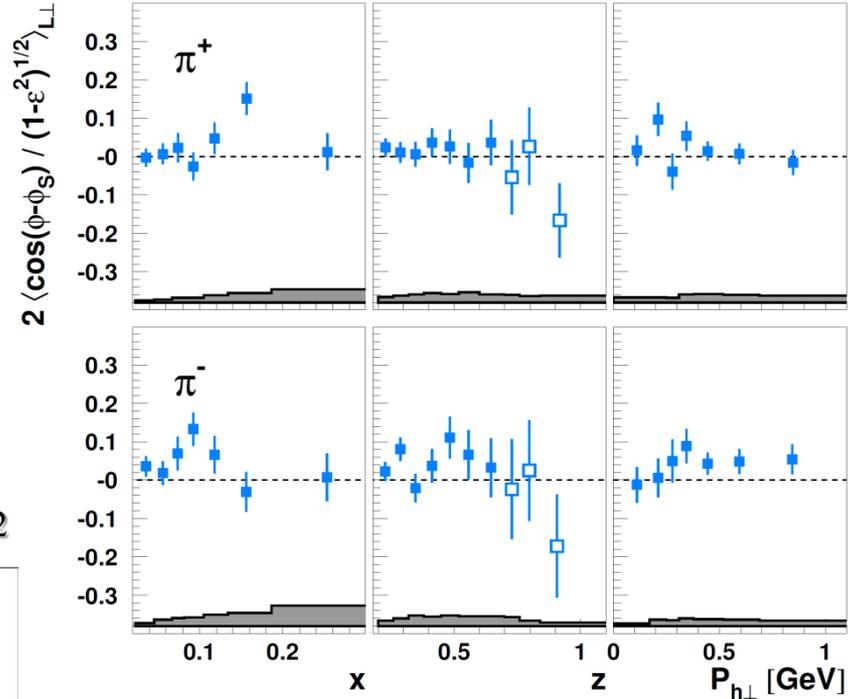
$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + \lambda S_T \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) + \dots \right\}$$

$$F_{LT}^{\cos(\phi_h - \phi_S)} = C \left[ \frac{\hat{h} \cdot \mathbf{k}_T}{M} g_{1T}^q D_{1q}^h \right]$$

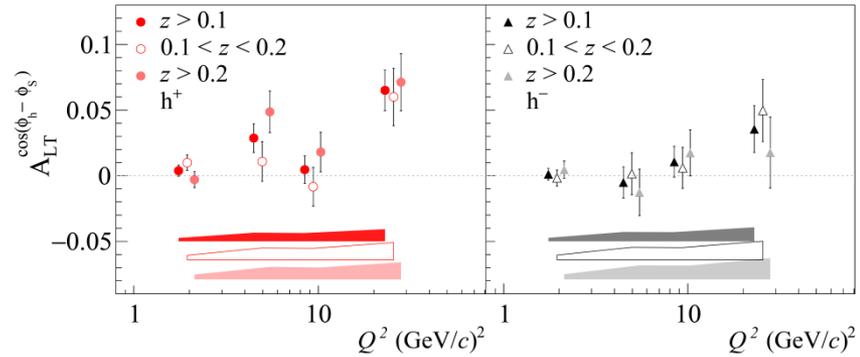
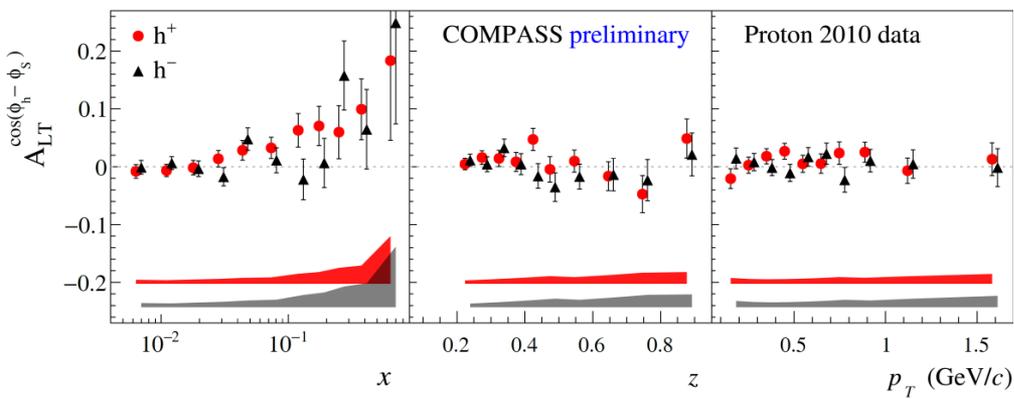


- COMPASS/HERMES/CLAS6 results
- $A_{LT}^{\cos(\phi_h - \phi_S)}$
- Only “twist-2” ingredients
  - **Sizable non-zero effect for  $h^+$  !**
  - **Similar effect at HERMES**

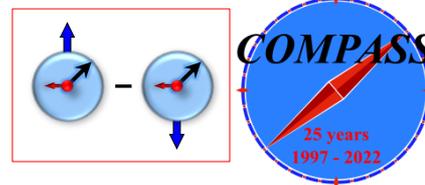
HERMES, JHEP 12 (2020) 010



COMPASS, PBL 770 (2017) 138; PoS QCDEV2017 (2018) 042



# SIDIS TSAs: Kotzinian-Mulders asymmetry

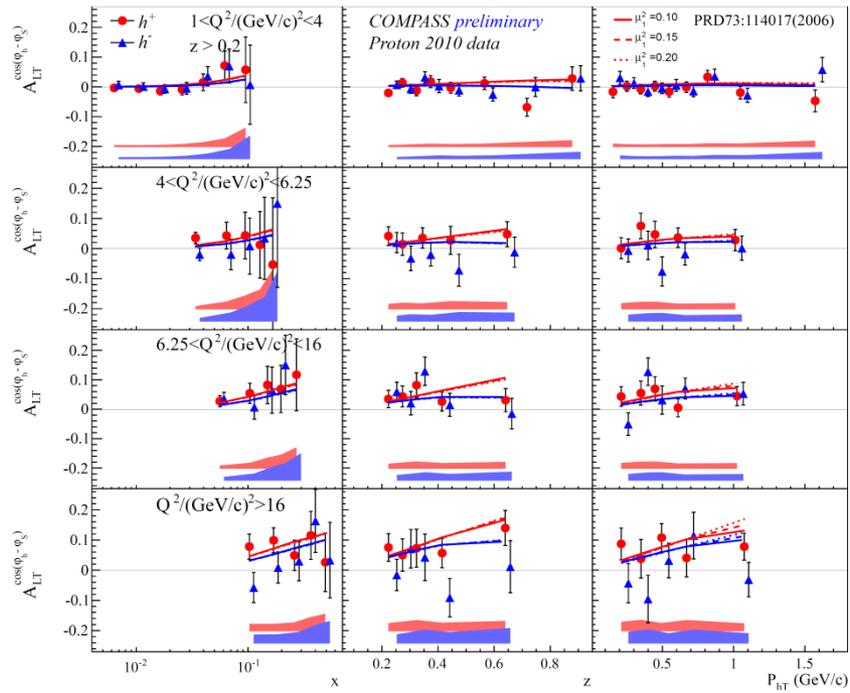
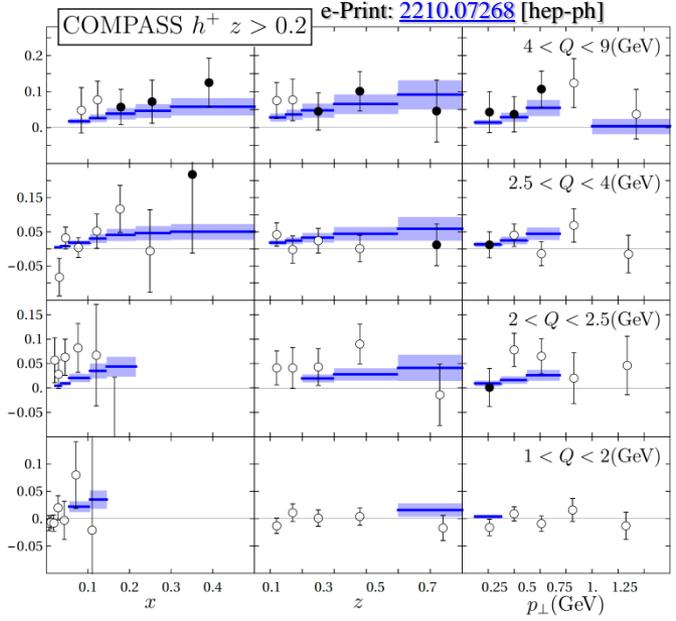


$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + \lambda S_T \sqrt{(1-\varepsilon^2)} A_{LT}^{\cos(\phi_h - \phi_S)} \cos(\phi_h - \phi_S) + \dots \right\}$$

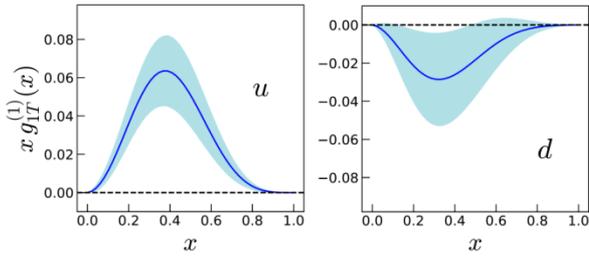
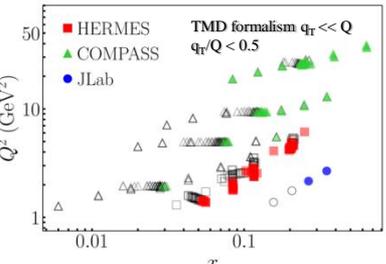
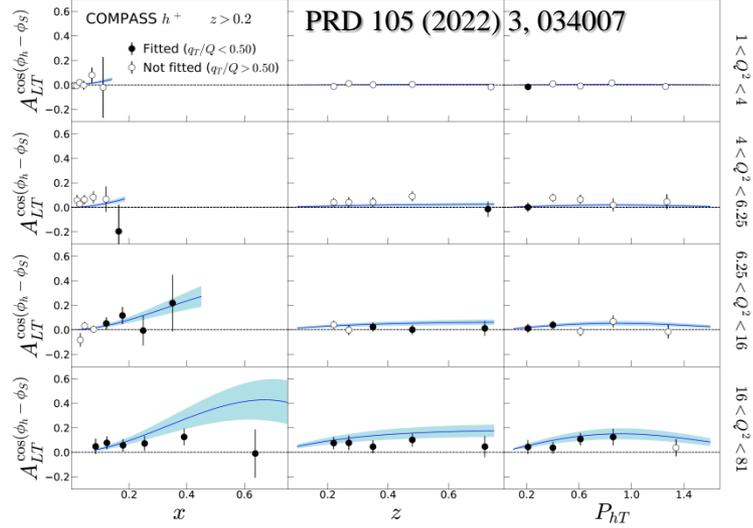
$$F_{LT}^{\cos(\phi_h - \phi_S)} = C \left[ \frac{\hat{h} \cdot k_T}{M} g_{1T}^q D_{1q}^h \right]$$



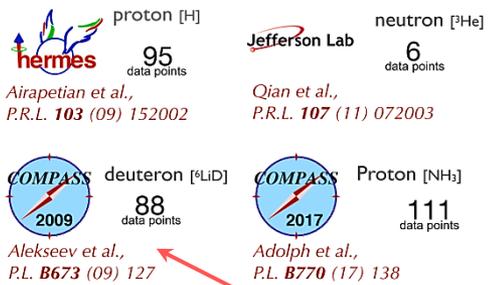
M. Horstmann, A. Schafer and A. Vladimirov



First global QCD analysis of the  $g_{1T}$  TMD PDF using SIDIS data



# COMPASS 2022 run: new unique deuteron data to come



## Pavia group fits

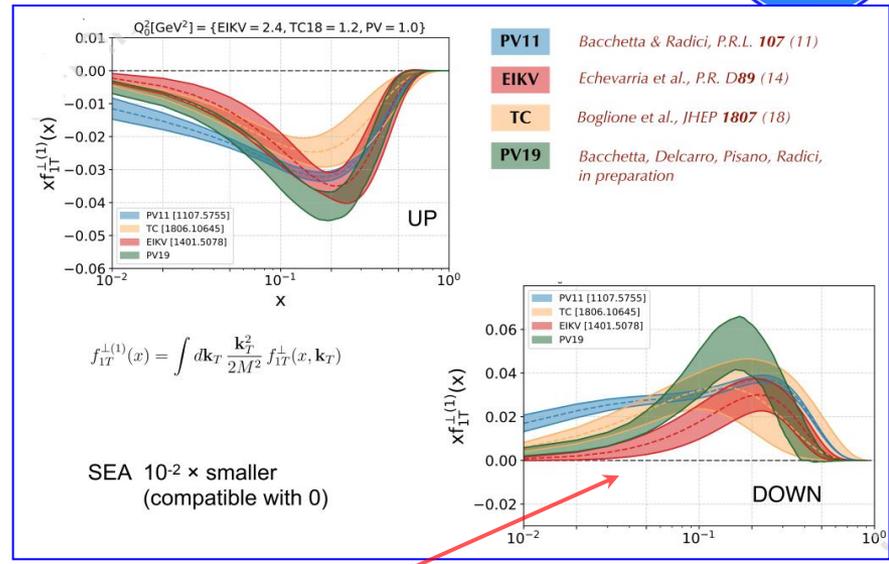
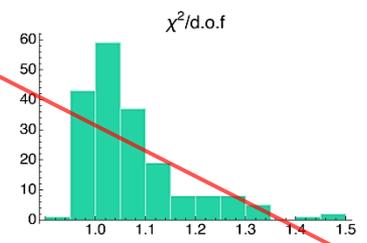
Bacchetta, Delcarro, Pisano, Radici, in preparation  
 analysis of statistical error with replica method (200)  
 68% confidence level

Same kinematic cuts applied to unpolarized  $x, z, P_{1T}$  data projections

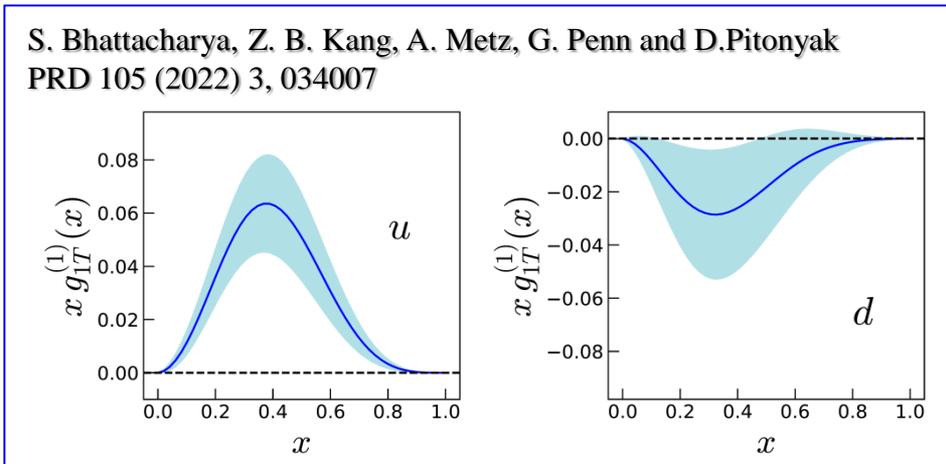
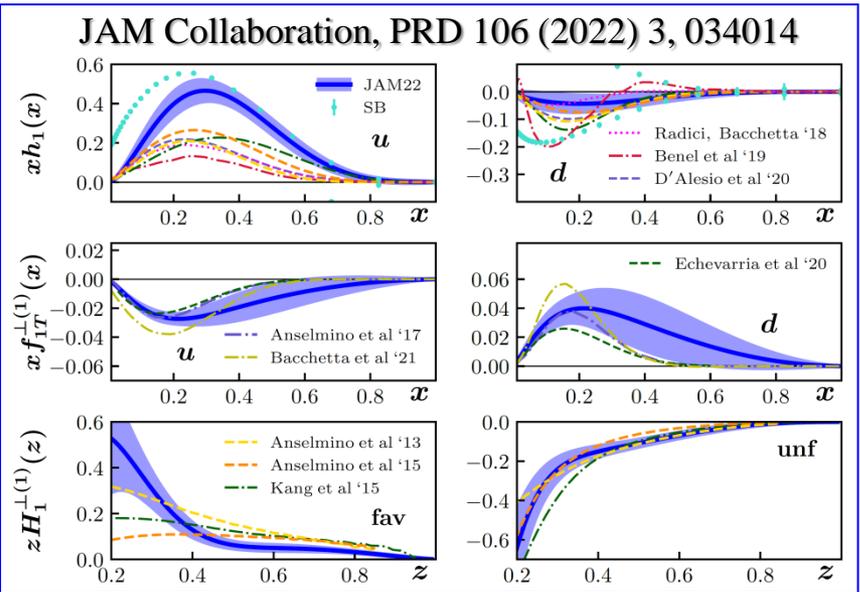
$$Q^2 \geq 1.4 \text{ GeV}^2 \quad 0.2 \leq z \leq 0.7$$

$$P_{1T} < \min[0.2Q, 0.7Qz] + 0.5 \text{ GeV}$$

300 data points  $\rightarrow$  118 data fitted  
 14 free parameters  
 $\chi^2/\text{d.o.f.} = 1.06 \pm 0.10$



## COMPASS 2022 deuteron run



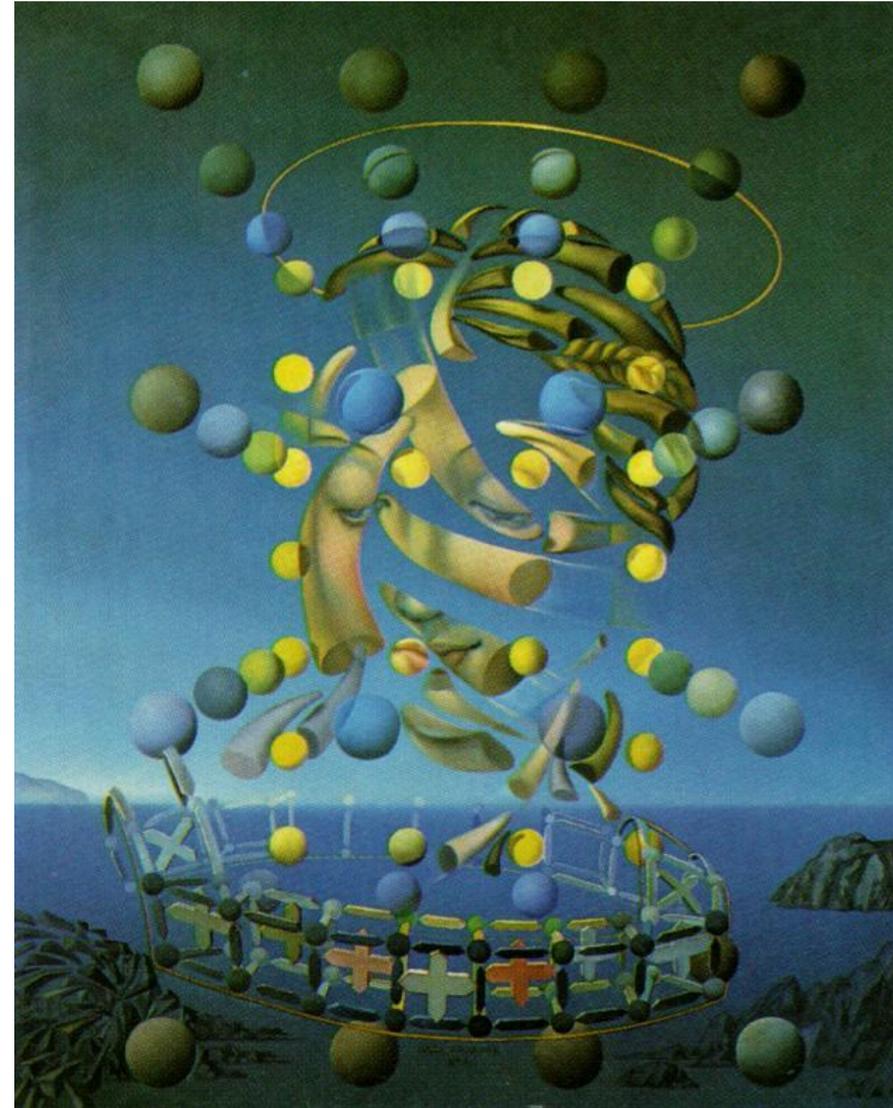
“Nature”



Raphael “Madonna del Prato”

24 January 2023

“1D”



Salvador Dalí “Maximum Speed of Raphael's Madonna”

B. Parsamyan

37

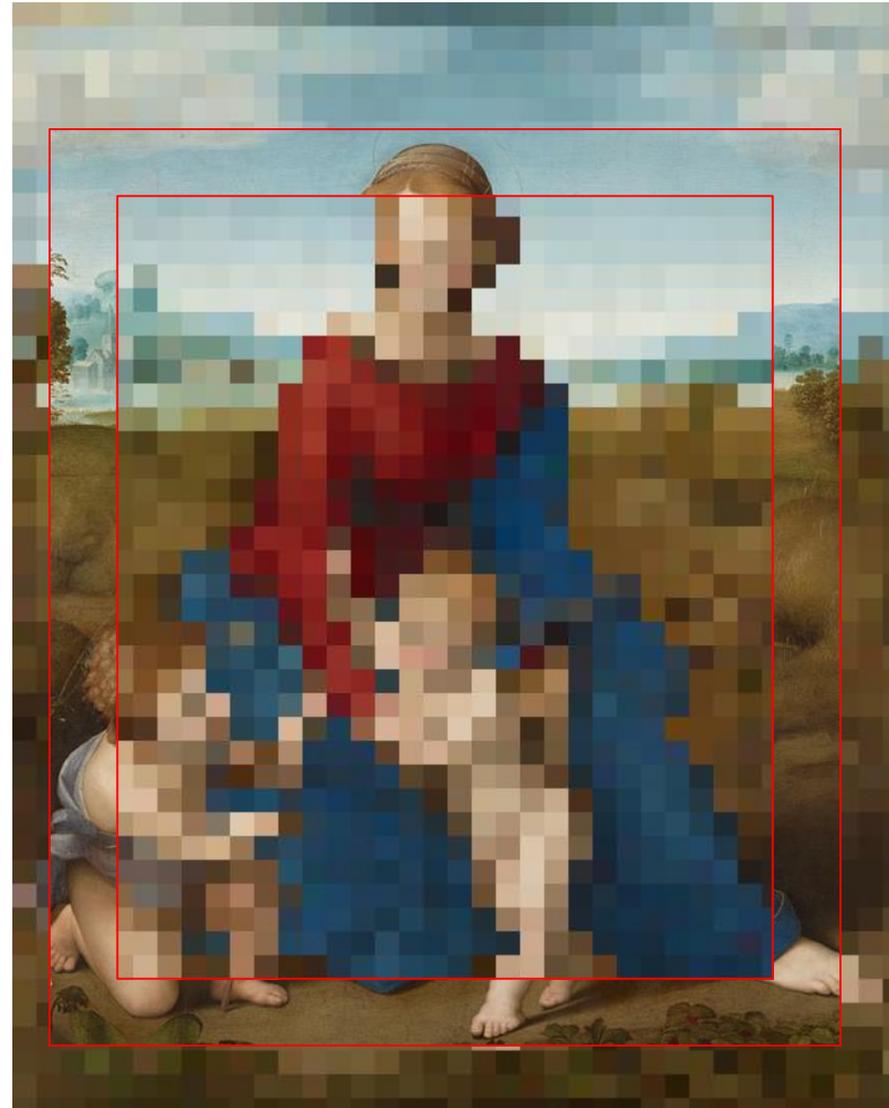
“Nature”



Raphael “Madonna del Prato”

24 January 2023

“multi-D” with available statistics



Raphael “Madonna del Prato” (poor resolution)

B. Parsamyan

38

# Conclusions

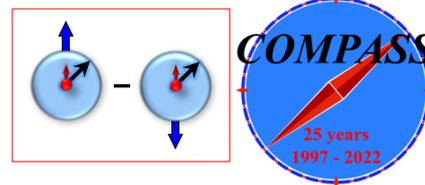
- For a better and more complex understanding of the TMD-spin-phenomena, it is important to carry out the extractions, analyses and various corrections in a multi-D approach
- It is also important to carefully confront experimental data from different experiments
- Different complex analysis techniques, Monte-Carlo simulations and various corrections (acceptance, VMs, radiative corrections) are being employed by different experimental collaborations
  - Closer collaboration between different experimental groups would be very beneficial for the field in general
  - Sharing the tools (MC, generators, analysis techniques), preliminary results, doing cross-analyses, etc.
- Close collaboration between experimentalists on one side and phenomenologists and theorists on the other would also be very beneficial
  - Flexibility in adapting on the analysis side (in a timely manner) the choice of the observables, phase-space limitations, etc.
  - Ideally a close collaborative work can be organized

**Thank You!**



- Spare slides

# SIDIS TSAs: Collins effect and Transversity



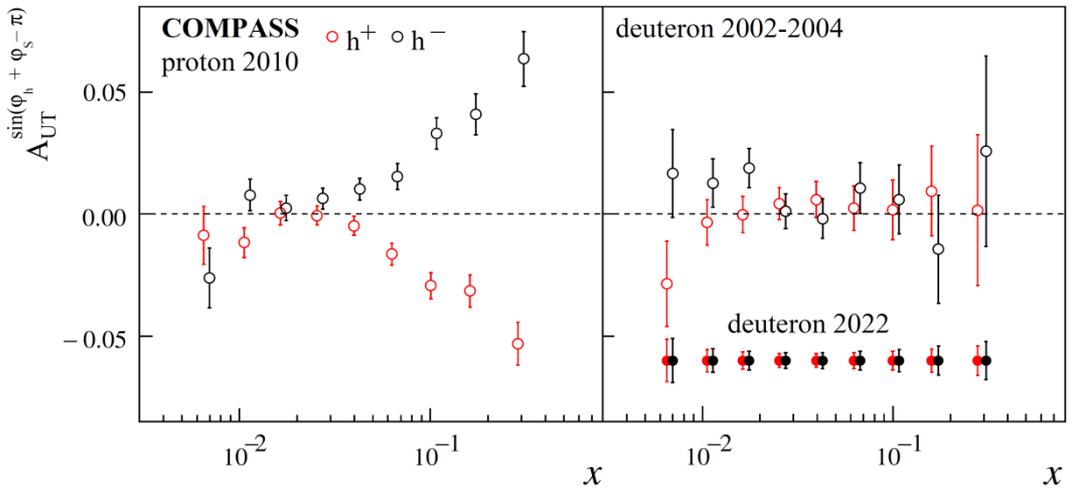
$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_T \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} \sin(\phi_h + \phi_S) + \dots \right\}$$

$$F_{UT}^{\sin(\phi_h + \phi_S)} = C \left[ -\frac{\hat{h} \cdot p_T}{M_h} h_1^q H_{1q}^{\perp h} \right]$$

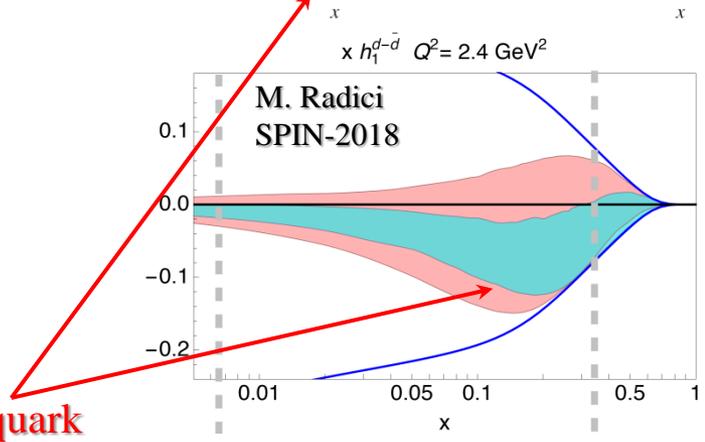
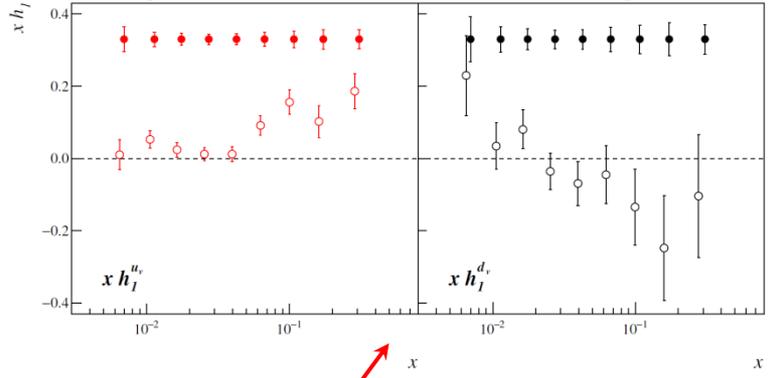


- Measured on P/D in SIDIS and in dihadron SIDIS
- Compatible results COMPASS/HERMES (Q<sup>2</sup> is different by a factor of ~2-3)
- **No impact from Q<sup>2</sup>-evolution?**
- Extensive phenomenological studies and various global fits by different groups

[Addendum to the COMPASS-II Proposal]  
Projected uncertainties for Collins asymmetry



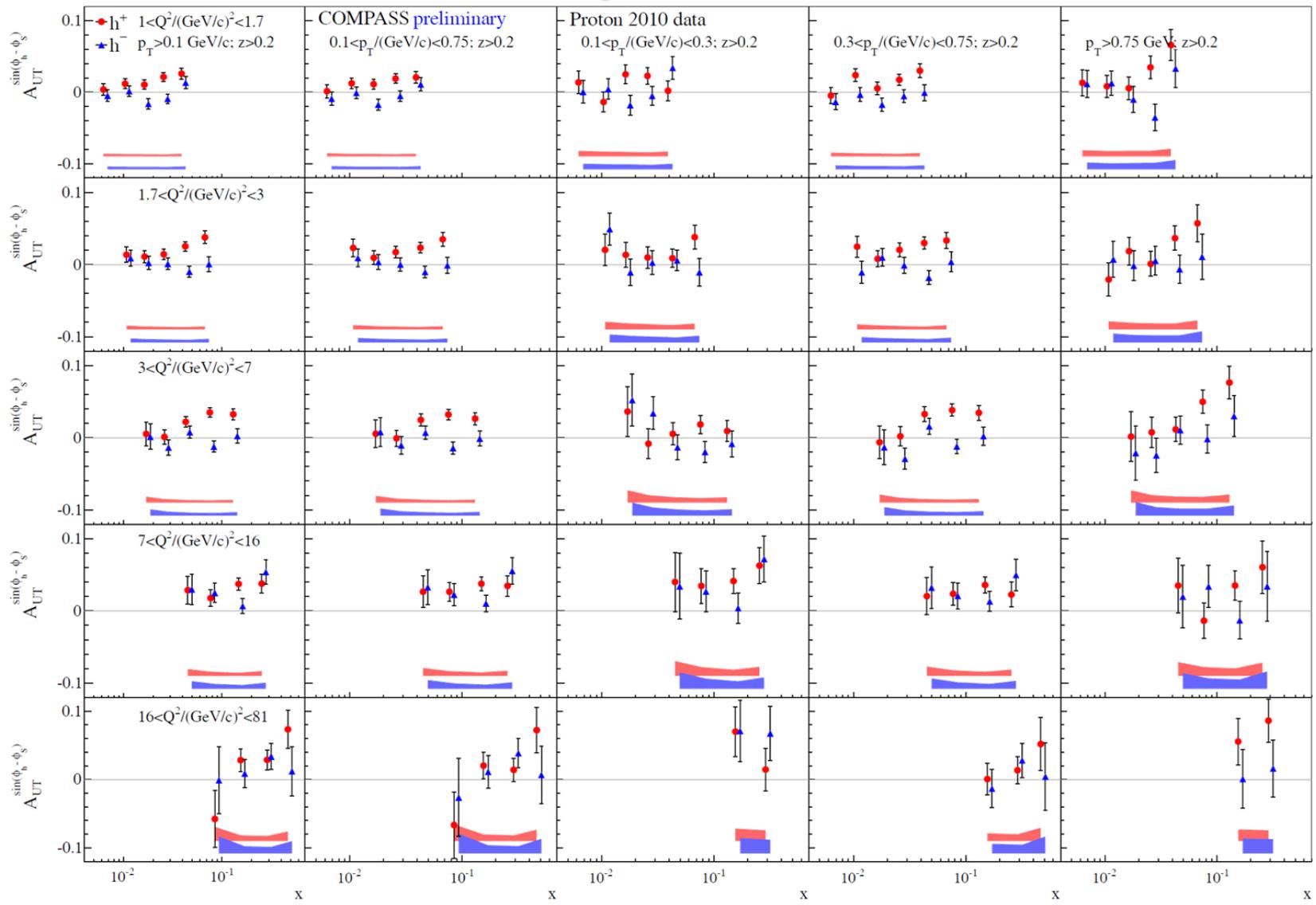
Projected uncertainties for transversity PDF



**COMPASS-II (2022)**

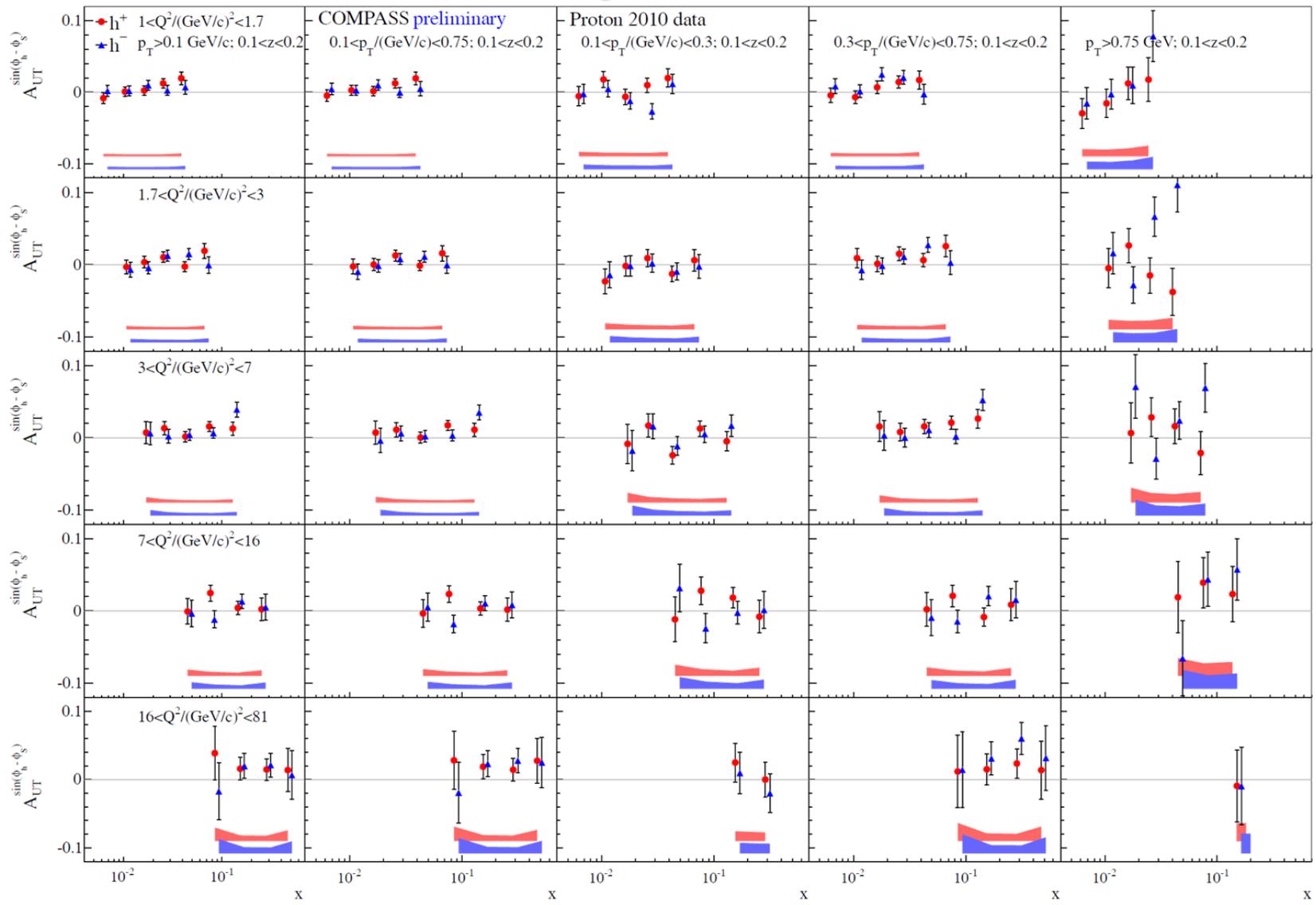
- Deuteron measurement being repeated
- Will be crucial to constrain the transversity TMD PDF for the d-quark

# Sivers asymmetry: 4D $Q^2$ - $p_T$ - $x$ dependence at $z>0.2$



- Positive amplitude for  $h^+$  (increasing with  $x$  and  $z$  and  $p_T$ )
- Positive  $h^-$  amplitude at relatively large  $x$  ( $>0.032$ ) and  $Q^2$  ( $>7$ ) at intermediate and large  $z$  (all  $p_T$ )
- Some hint for a possible negative  $h^-$  amplitude at low  $x$  ( $<0.032$ ) and  $Q^2$  ( $<7$ ) at intermediate and large  $z$  (all  $p_T$ )

# Sivers asymmetry: 4D $Q^2$ - $p_T$ - $x$ dependence at $0.1 < z < 0.2$



- Positive amplitude for  $h^+$  (increasing with  $x$  and  $z$  and  $p_T$ )
- Positive  $h^-$  amplitude at relatively large  $x$  ( $>0.032$ ) and  $Q^2$  ( $>7$ ) at intermediate and large  $z$  (all  $p_T$ )
- Some hint for a possible negative  $h^-$  amplitude at low  $x$  ( $<0.032$ ) and  $Q^2$  ( $<7$ ) at intermediate and large  $z$  (all  $p_T$ )

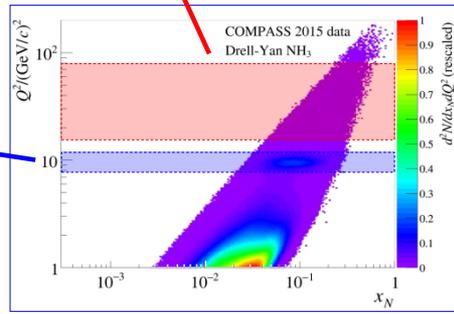
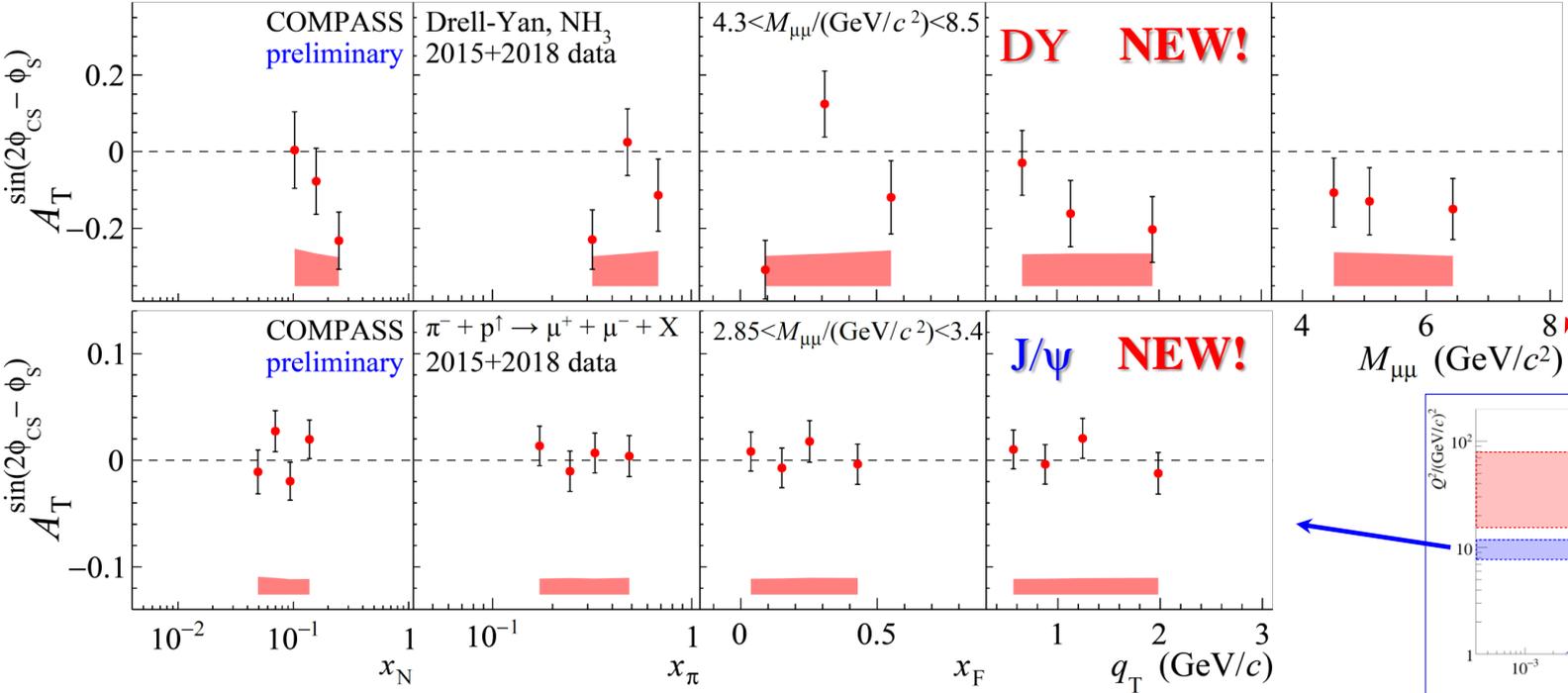
# Drell-Yan TSAs – Transversity

Transversity DY TSA

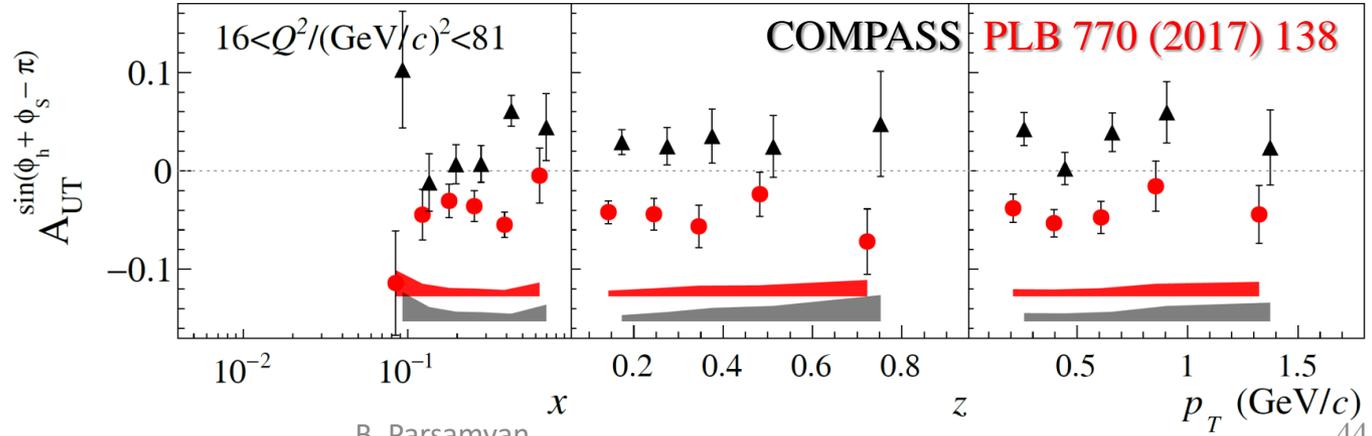
$$A_T^{\sin(2\varphi_{CS}-\varphi_S)} \propto h_{1,\pi}^{\perp q} \otimes h_{1,p}^q$$



$$\frac{d\sigma}{dq^4 d\Omega} \propto 1 + \dots + S_T \left[ D_{[\sin^2\theta_{CS}]} A_T^{\sin(2\varphi_{CS}-\varphi_S)} \sin(2\varphi_{CS}-\varphi_S) + \dots \right]$$



Collins SIDIS TSA

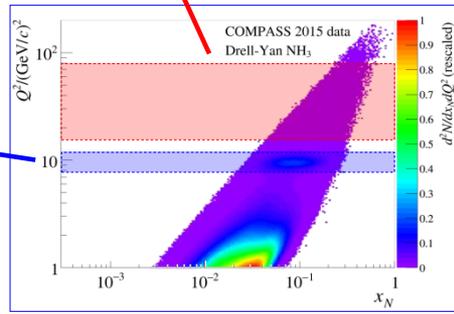
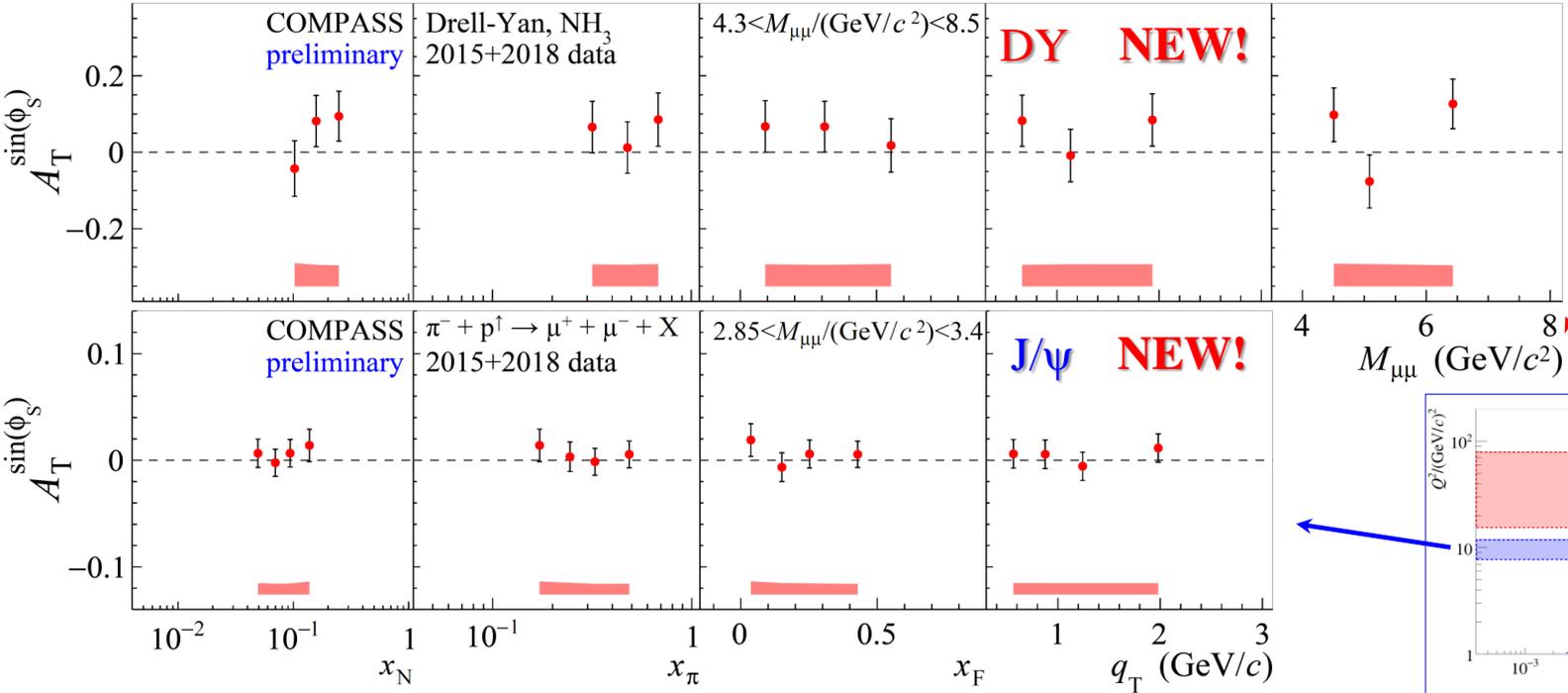
$$A_{UT}^{\sin(\phi_h + \phi_s)} \propto h_1^q \otimes H_{1q}^{\perp h}$$


# Drell-Yan TSAs – Sivers

**Sivers DY TSA**

$$A_T^{\sin\phi_S} \propto f_{1,\pi}^q \otimes f_{1T,p}^{\perp q}$$

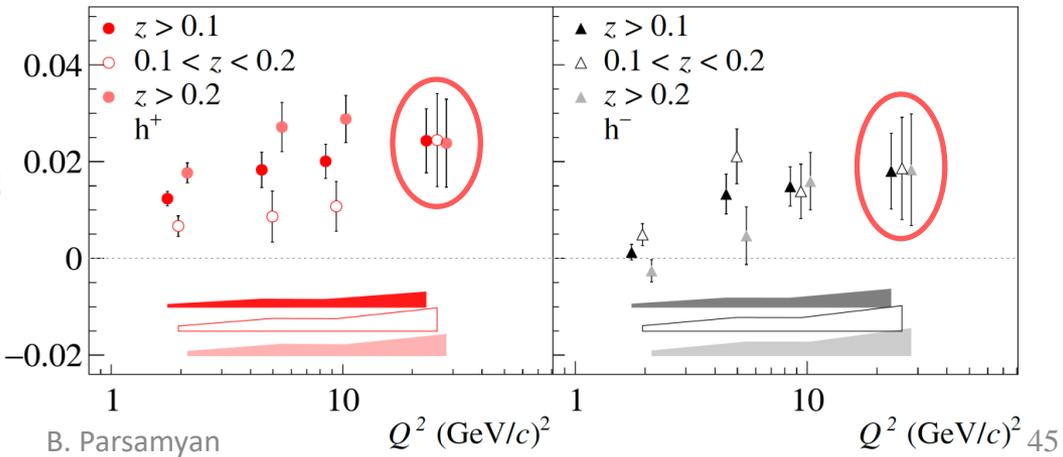
$$\frac{d\sigma}{dq^4 d\Omega} \propto 1 + \dots + S_T \left[ A_T^{\sin\phi_S} \sin\phi_S + \dots \right]$$



**Sivers SIDIS TSA**

$$A_{UT}^{\sin(\phi_h - \phi_s)} \propto f_{1T}^{\perp q} \otimes D_{1q}^h$$

**COMPASS  
PLB 770 (2017) 138**



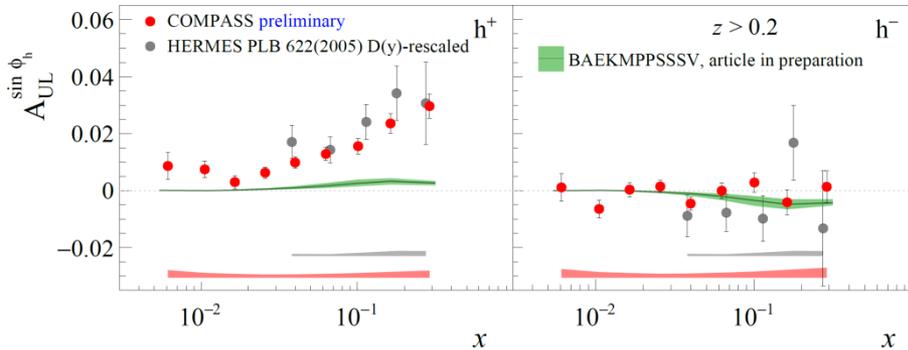
# SIDIS: target longitudinal spin dependent asymmetries

$$\frac{d\sigma}{dx dy dz dp_T^2 d\phi_h d\phi_S} \propto (F_{UU,T} + \varepsilon F_{UU,L}) \left\{ 1 + \dots + S_L \sqrt{2\varepsilon(1+\varepsilon)} A_{UL}^{\sin\phi_h} \sin\phi_h + \dots \right\}$$

$$F_{UL}^{\sin\phi_h} = \frac{2M}{Q} \mathcal{C} \left\{ -\frac{\hat{h} \cdot \mathbf{p}_T}{M_h} \left( x h_L^q H_{1q}^{\perp h} + \frac{M_h}{M} g_{1L}^q \frac{\tilde{G}_q^{\perp h}}{z} \right) + \frac{\hat{h} \cdot \mathbf{k}_T}{M} \left( x f_L^{\perp q} D_{1q}^h - \frac{M_h}{M} h_{1L}^{\perp q} \frac{\tilde{H}_q^h}{z} \right) \right\}$$

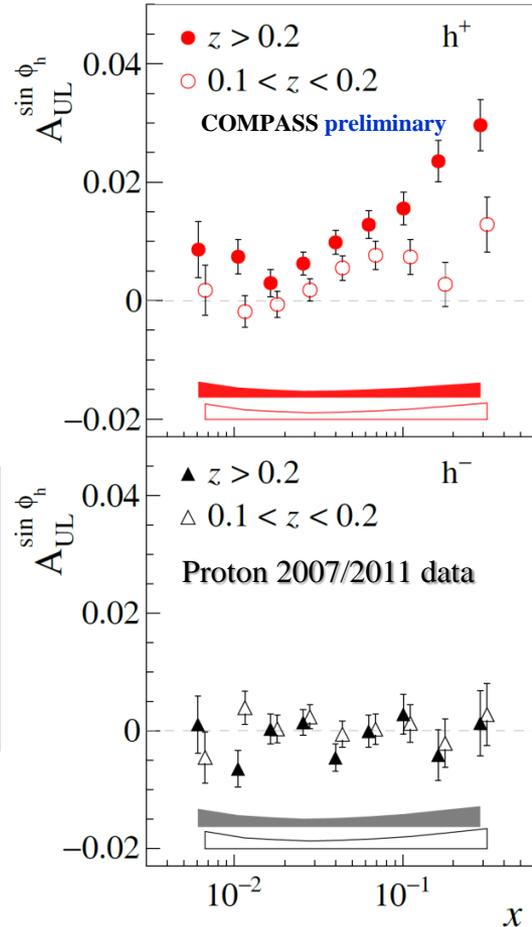
S. Bastami et al. JHEP 1906 (2019) 007:

“SIDIS in Wandzura-Wilczek-type approximation”



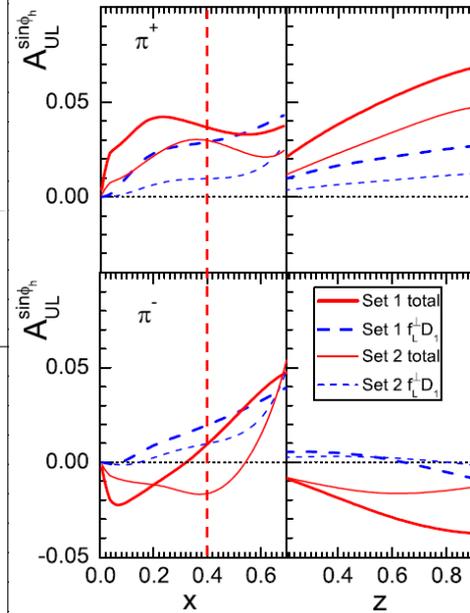
B. Parsamyan (for COMPASS)

[arXiv:1801.01488](https://arxiv.org/abs/1801.01488) [hep-ex]



Zhun Lu

Phys. Rev. D 90, 014037(2014)



- Q-suppression, TSA-mixing
- Various different “twist” ingredients
- **Strong non-zero effect for  $h^+$ ,  $h^-$  compatible with zero, clear  $z$ -dependence**