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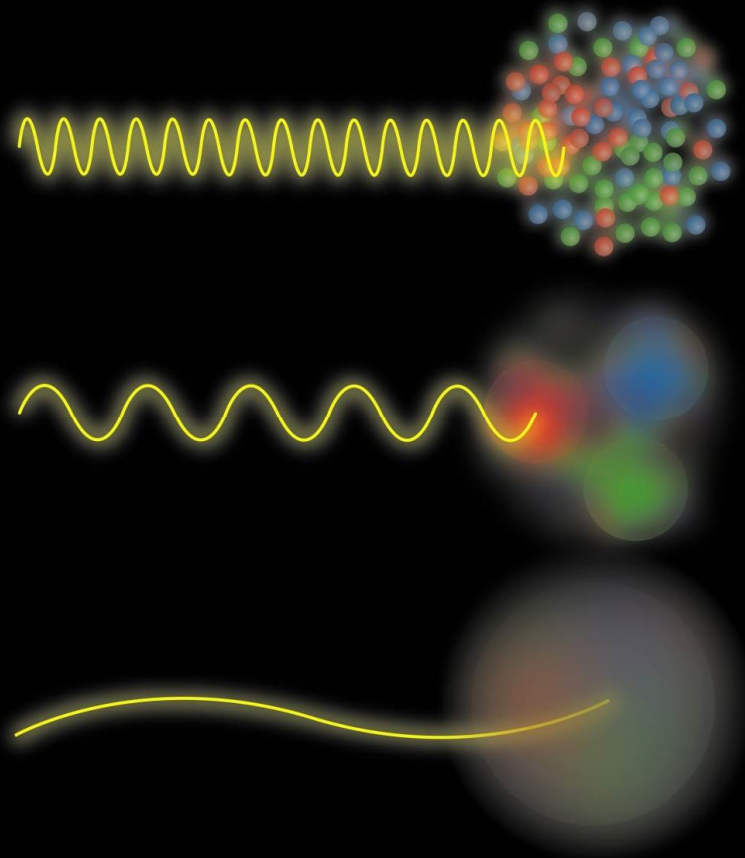
Bringing Science Solutions to the World



## Two-photon exchange from positron Super-Rosenbluth measurements

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Berkeley National Laboratory*

*Mikhail Yurov - Mississippi State  
University*



# Form factors: unpolarized elastic scattering

Unpolarized elastic cross section depends on charge and magnetic form factors:  $G_E(Q^2)$   $G_M(Q^2)$

$$\sigma_R = d\sigma/d\Omega [\varepsilon(1+\tau)/\sigma_{\text{Mott}}] = \tau G_M^2(Q^2) + \varepsilon G_E^2(Q^2)$$

$$\tau = Q^2/4M^2$$

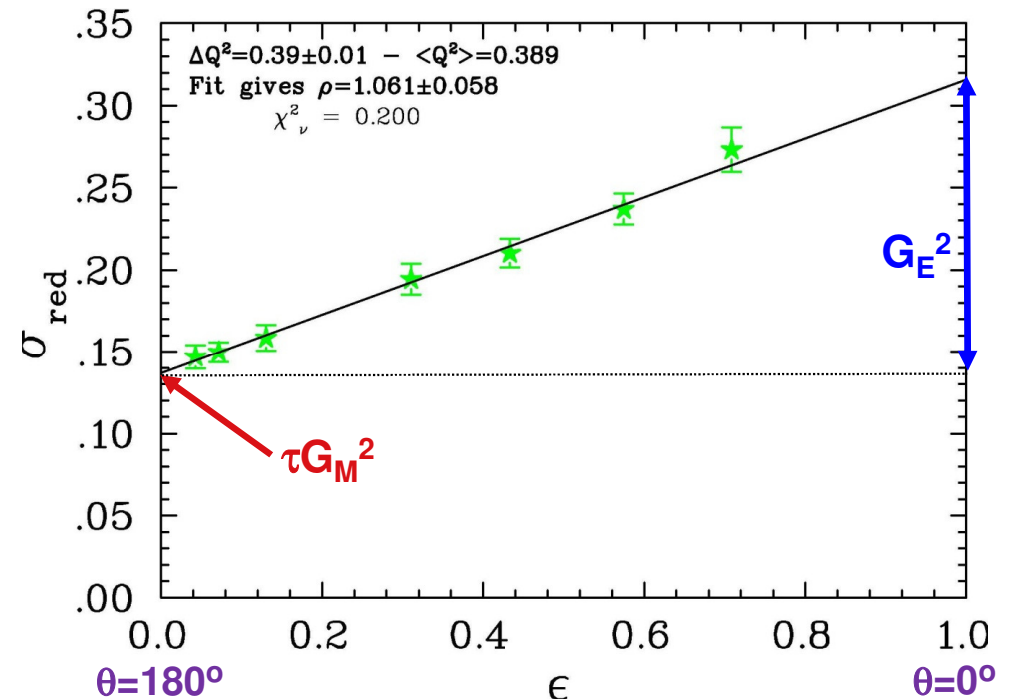
$$\varepsilon = [1 + 2(1+\tau)\tan^2(\theta/2)]^{-1}$$

Reduced sensitivity when one term dominates:

- $G_M$  if  $\tau \ll 1$
- $G_E$  if  $\tau \gg 1$
- $G_E$  if  $G_E^2 \ll G_M^2$  (e.g. neutron)

Worlds data give  $G_M$  and  $G_E$  proportional to dipole form:  $(1+Q^2/[0.71 \text{ GeV}^2])^{-2}$

$$\rightarrow \mu_p G_E(Q^2) / G_M(Q^2) \approx 1$$



# Form factors: Recoil polarization, pol targets

Mid '90s brought measurements using polarization degrees of freedom

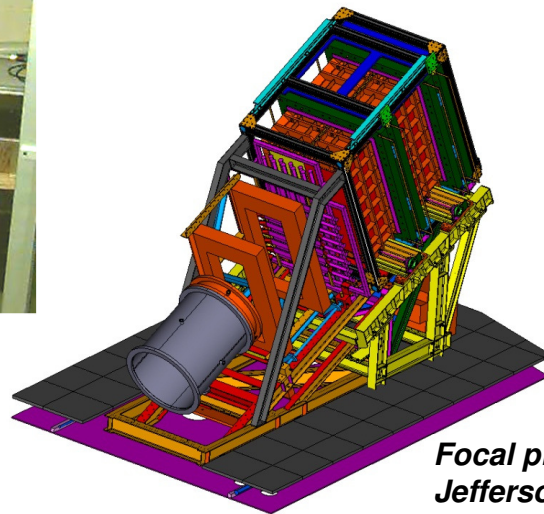
- High luminosity, highly polarized electron beams
- Polarized targets ( $^1\text{H}$ ,  $^2\text{H}$ ,  $^3\text{He}$ ) or recoil polarimeters



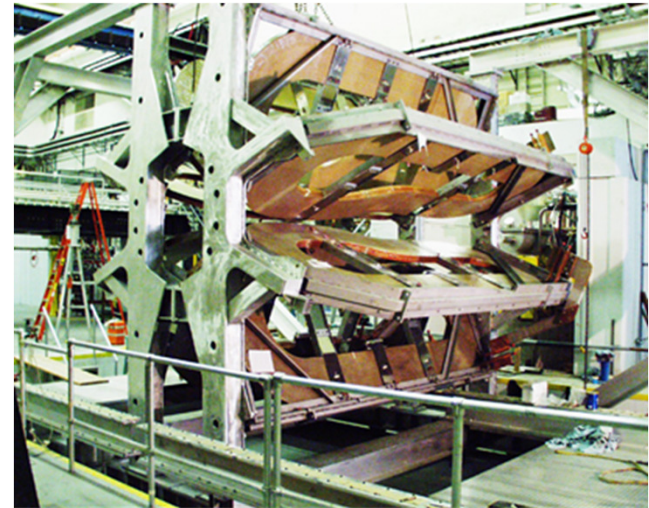
*Polarized  $^3\text{He}$  target*

$$\text{Unpol: } \tau G_M^2 + \epsilon G_E^2$$

$$\text{Pol: } G_E / G_M$$



*Focal plane polarimeter – Jefferson Lab*



*BLAST at MIT-Bates*

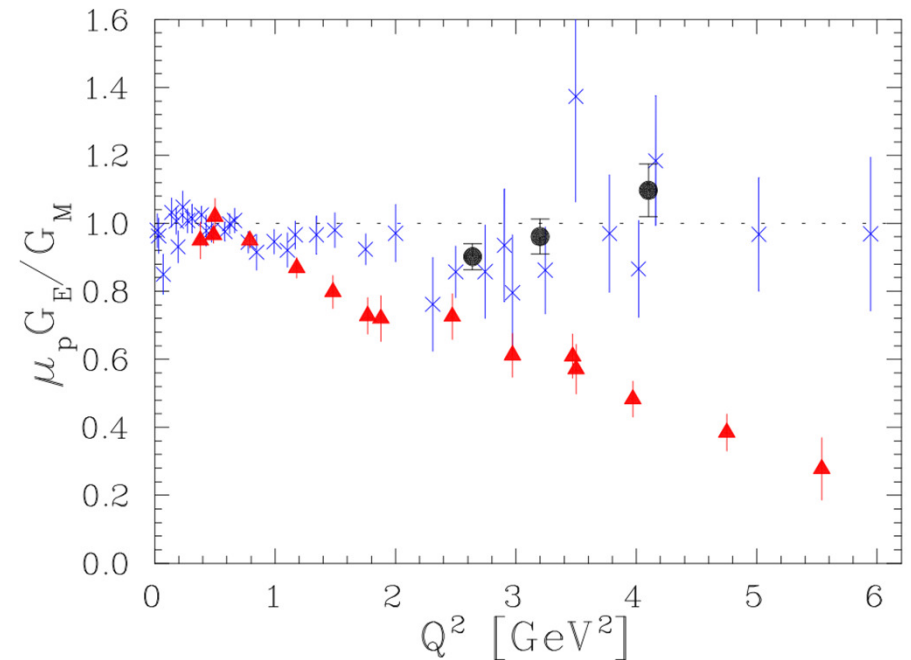
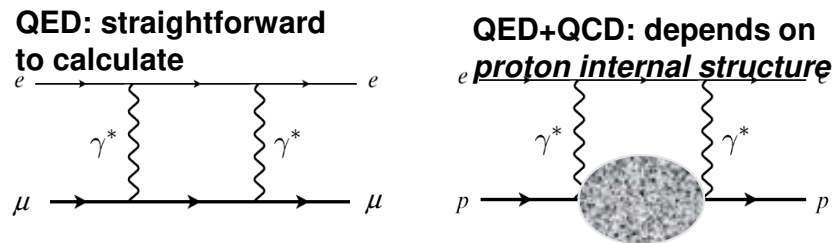
# Form factors: Rosenbluth vs Polarization

Blue points are global Rosenbluth extractions

Red points are polarization measurements

- Significant difference at high  $Q^2$ , where Rosenbluth have large errors, typically limited by systematics

Difference assumed to be caused by two-photon exchange (TPE) corrections



Black points – “Super-Rosenbluth” measurement:

Modified technique that gives significantly smaller uncertainty on the RATIO  $G_E/G_M$

I. A. Qattan, et al, PRL 94, 142301 (2005)

# Super-Rosenbluth technique

Rosenbluth (L/T) measurement: vary  $\epsilon$  ( $\theta$ ) at fixed  $Q^2$

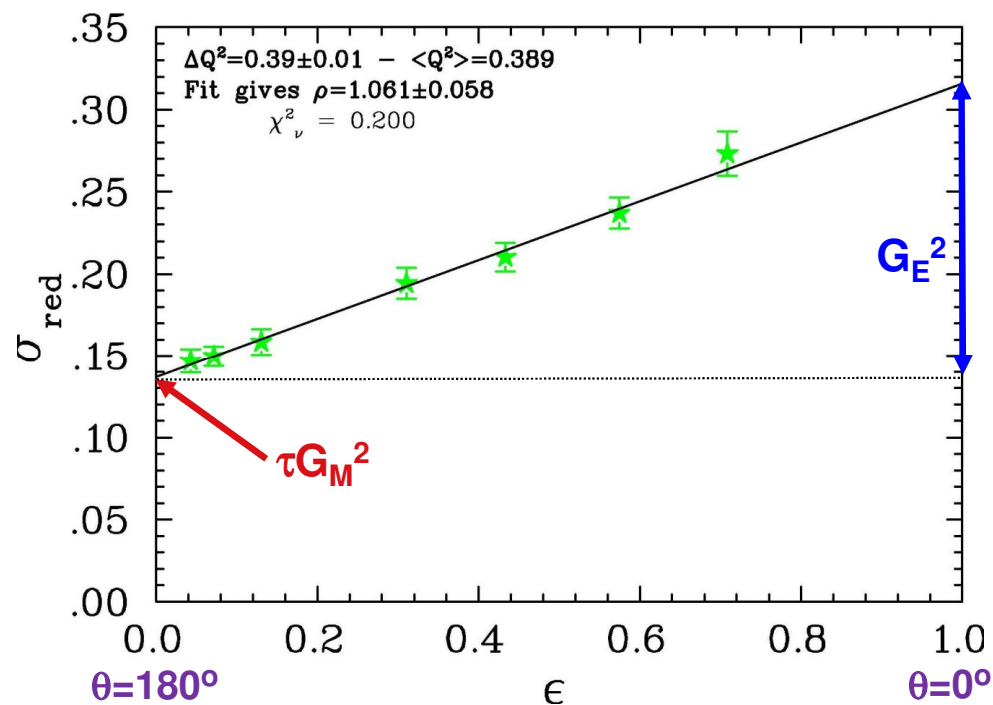
Conventional measurement: electron detection

- $\epsilon \approx 1$ : large beam energy, small scattering angle, large electron momentum, high rates
- $\epsilon \approx 0$ : small beam energy, large angle, small electron momentum, low rates
- Extraction of  $\epsilon$  dependence sensitive to momentum- and rate-dependent corrections (including rad corr)
- Limited by low cross sections at large scattering angle

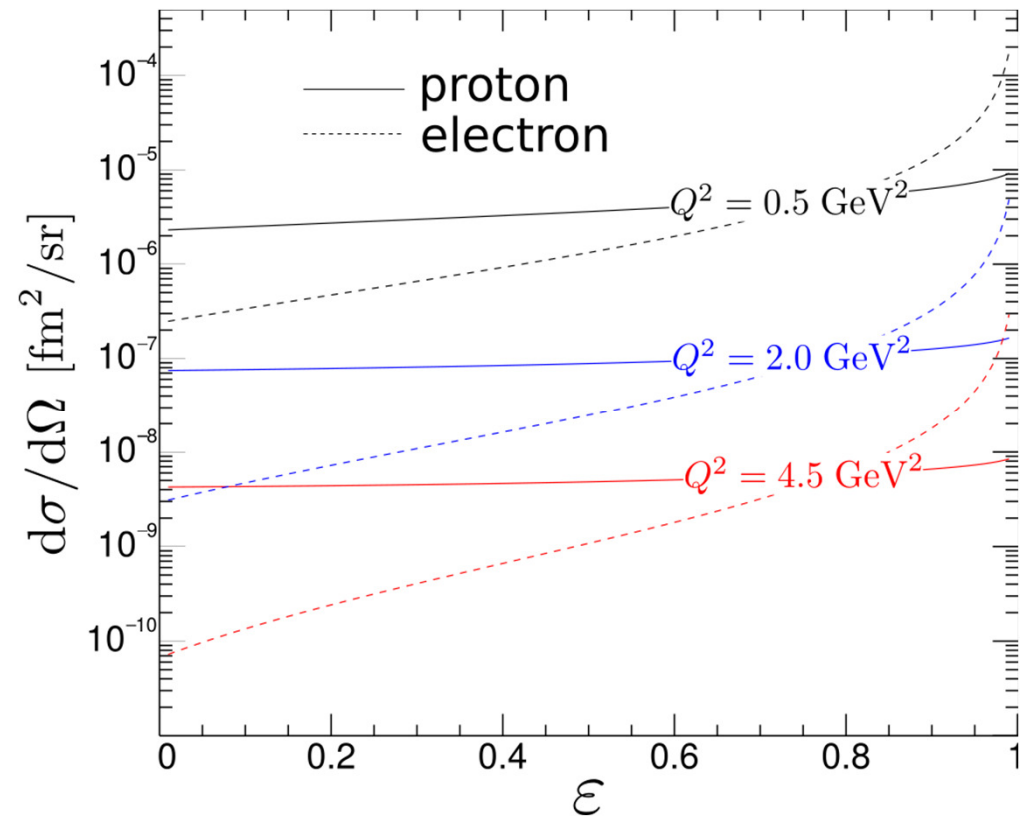
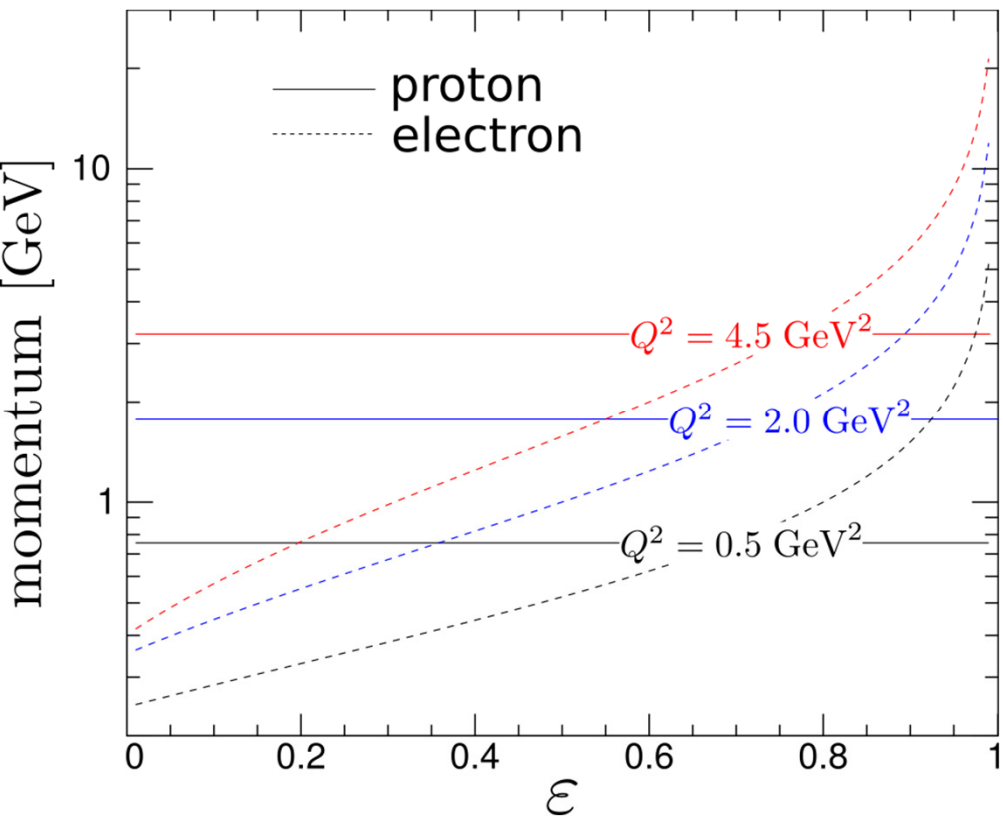
## Super-Rosenbluth: Proton detection

- Fixed proton momentum at fixed  $Q^2$
- Cross section, radiative correction have much smaller  $\epsilon$  dependence
- Higher cross section for small  $\epsilon$
- Less sensitive to kinematic uncertainties

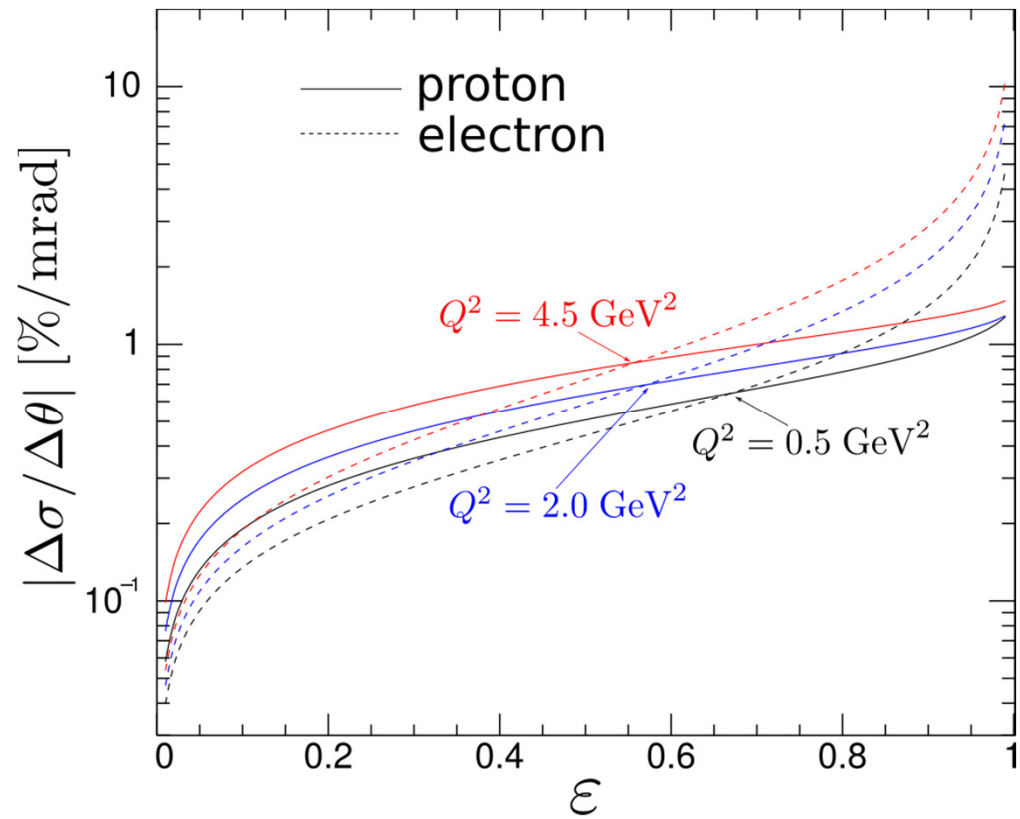
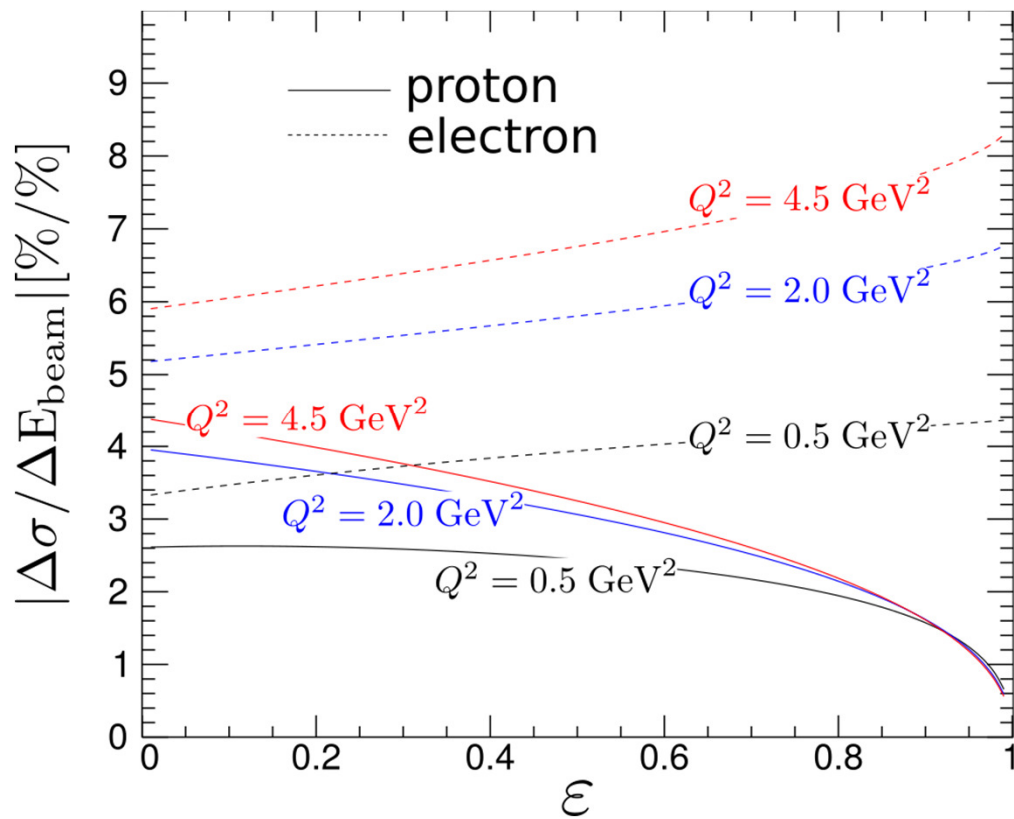
**While some uncertainties (e.g. acceptance, proton absorption) have larger absolute uncertainties, they are independent of  $\epsilon$  and cancel completely in extraction of  $G_E/G_M$**



# Proton vs electron detection: kinematics and rate



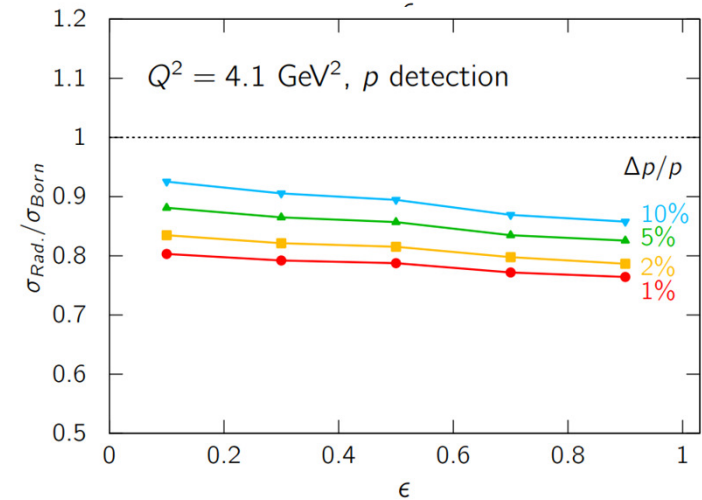
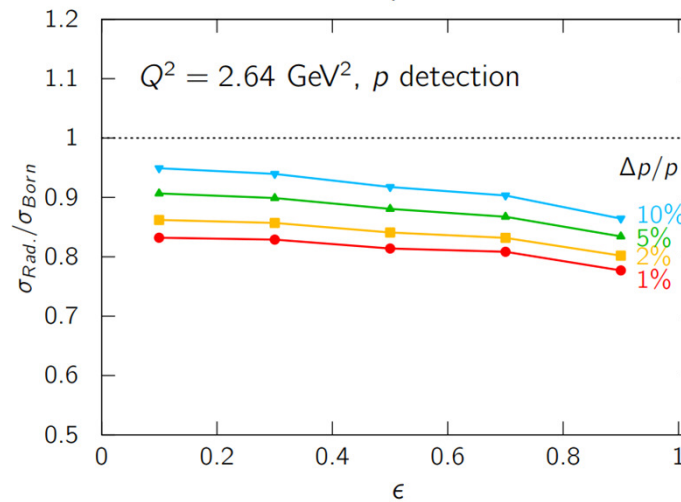
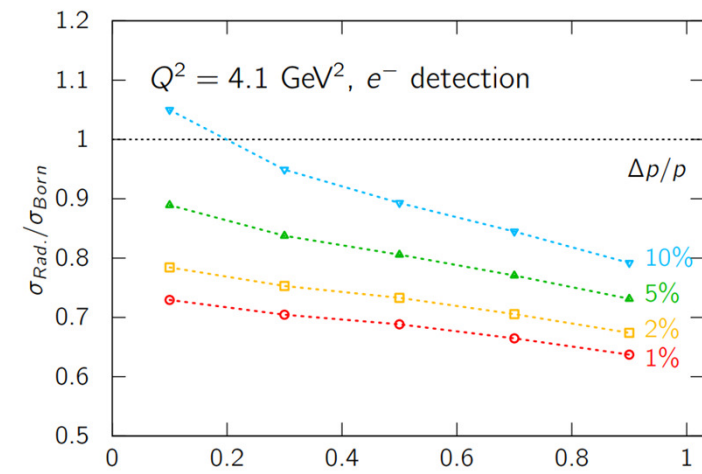
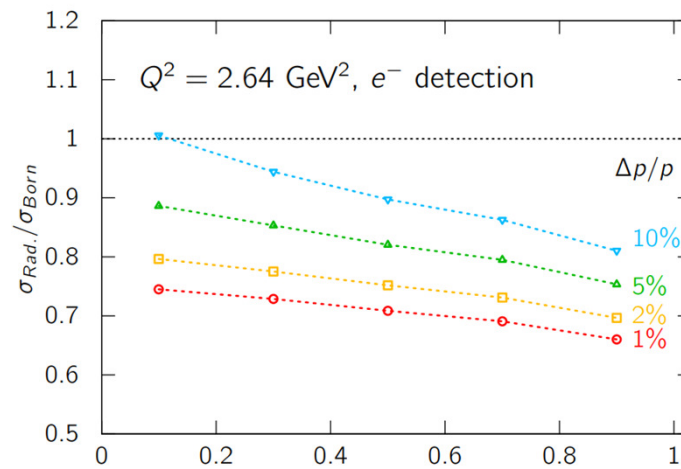
# Proton vs electron detection: kinematic sensitivity



# Proton vs electron detection – radiative corrections

Radiative corrections for electron and proton detection are similar in size, but proton detection has significantly smaller  $\epsilon$  dependence (and less sensitive to cutoff)

Results pilfered from Axel Schmidt – reference?





# Super-Rosenbluth with positrons

Conventional positron-electron comparisons **limited by positron luminosity** (especially at low  $\epsilon$ , where TPE are larger) and **requirement of significant cancellation between e- and e+ systematics**

- Cross section limit most significant at kinematics where TPE are large
- Require frequent changes between e+ and e- beams; similar beam properties

S-R technique **enhances cross section at low  $\epsilon$** , relies on **cancellation between points at different scattering angles (and fixed  $Q^2$ )**

- Allows precise e+ to e- comparison on the Rosenbluth slope, even for separate e+, e- experiments
- Does not allow direct e+/e- ratio at individual  $\epsilon$ ,  $Q^2$  points (without normalization at  $\epsilon=1$ )

Can perform precise S-R extraction with positrons and S-R with electrons independently.

Does not require rapid beam changes or identical beam characteristics.

# Two Photon Exchange Corrections

Two-photon exchange effects can explain discrepancy in  $G_E$

Guichon and Vanderhaeghen, PRL 91, 142303 (2003)

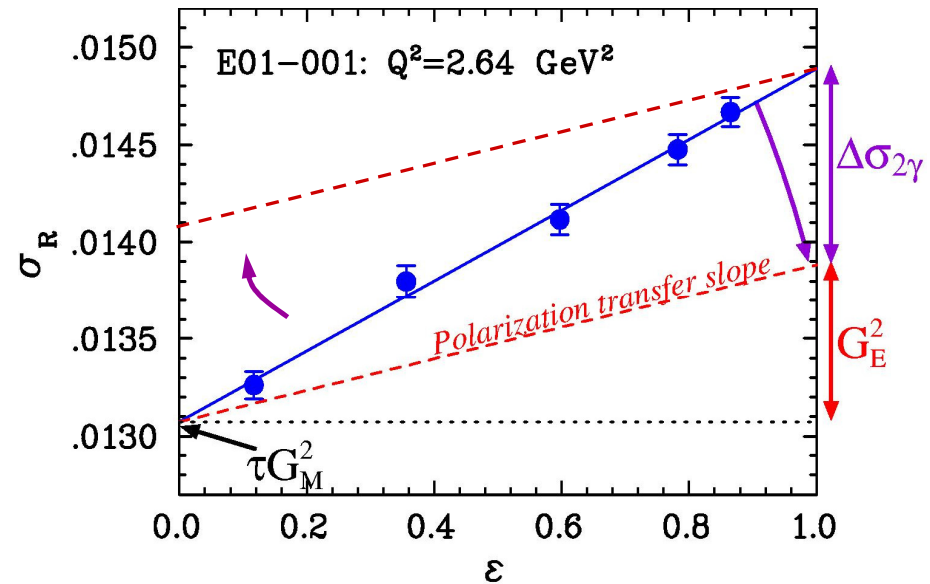
Requires  $\sim 6\%$   $\varepsilon$ -dependence, weakly dependent on  $Q^2$ , roughly linear in  $\varepsilon$

JA, PRC 69, 022201 (2004)

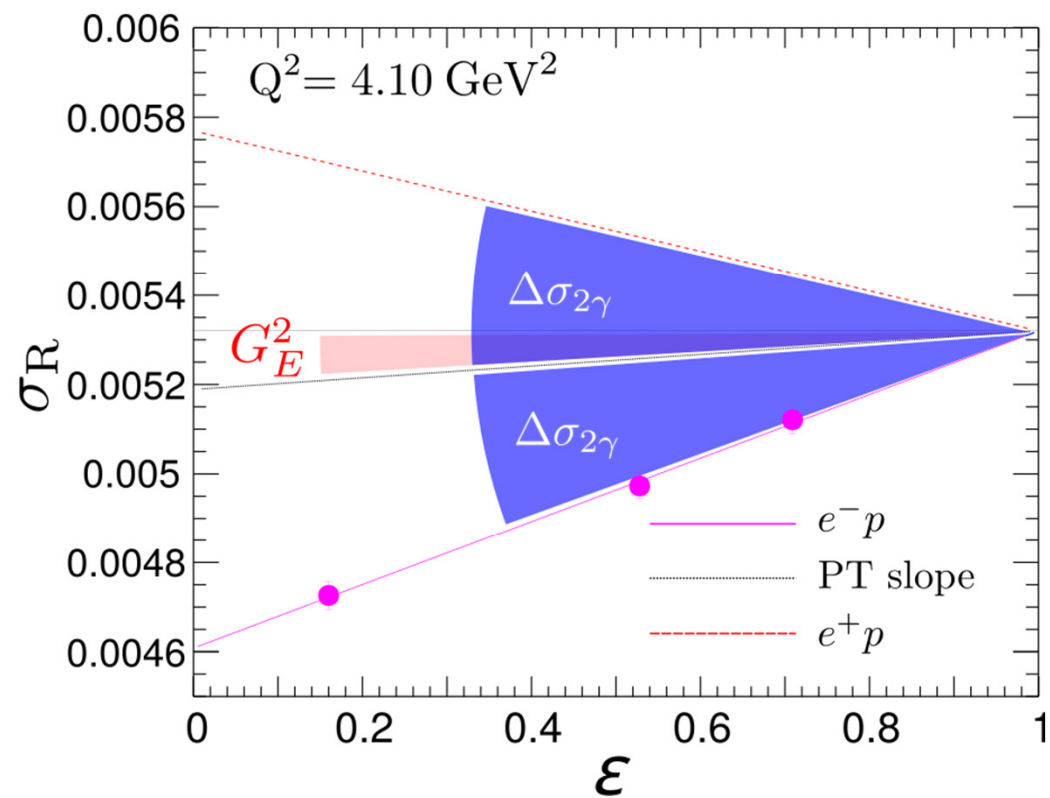
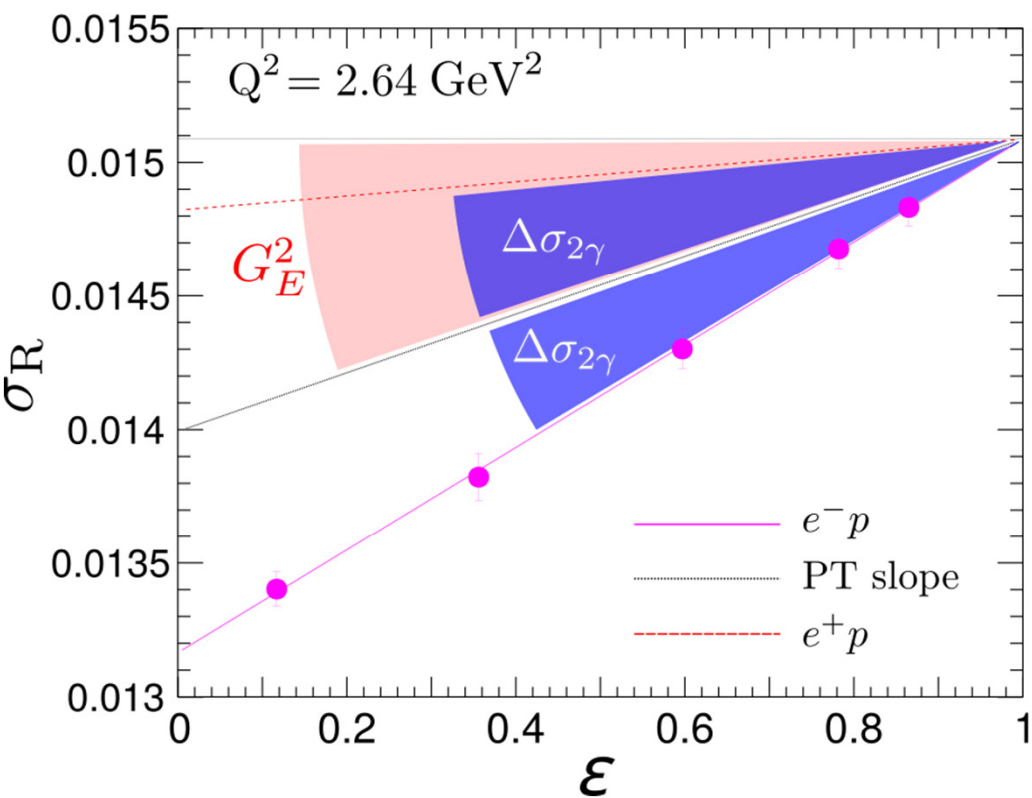
If this were the whole story, LT would give  $G_M$ , PT gives  $G_E/G_M$

There are other issues to be addressed

Constraints ( $\sim 1\%$ ) from positron-electron comparisons  
TPE effects on *polarization transfer*?



# Rosenbluth separations: $e^+$ vs $e^-$



# Kinematics

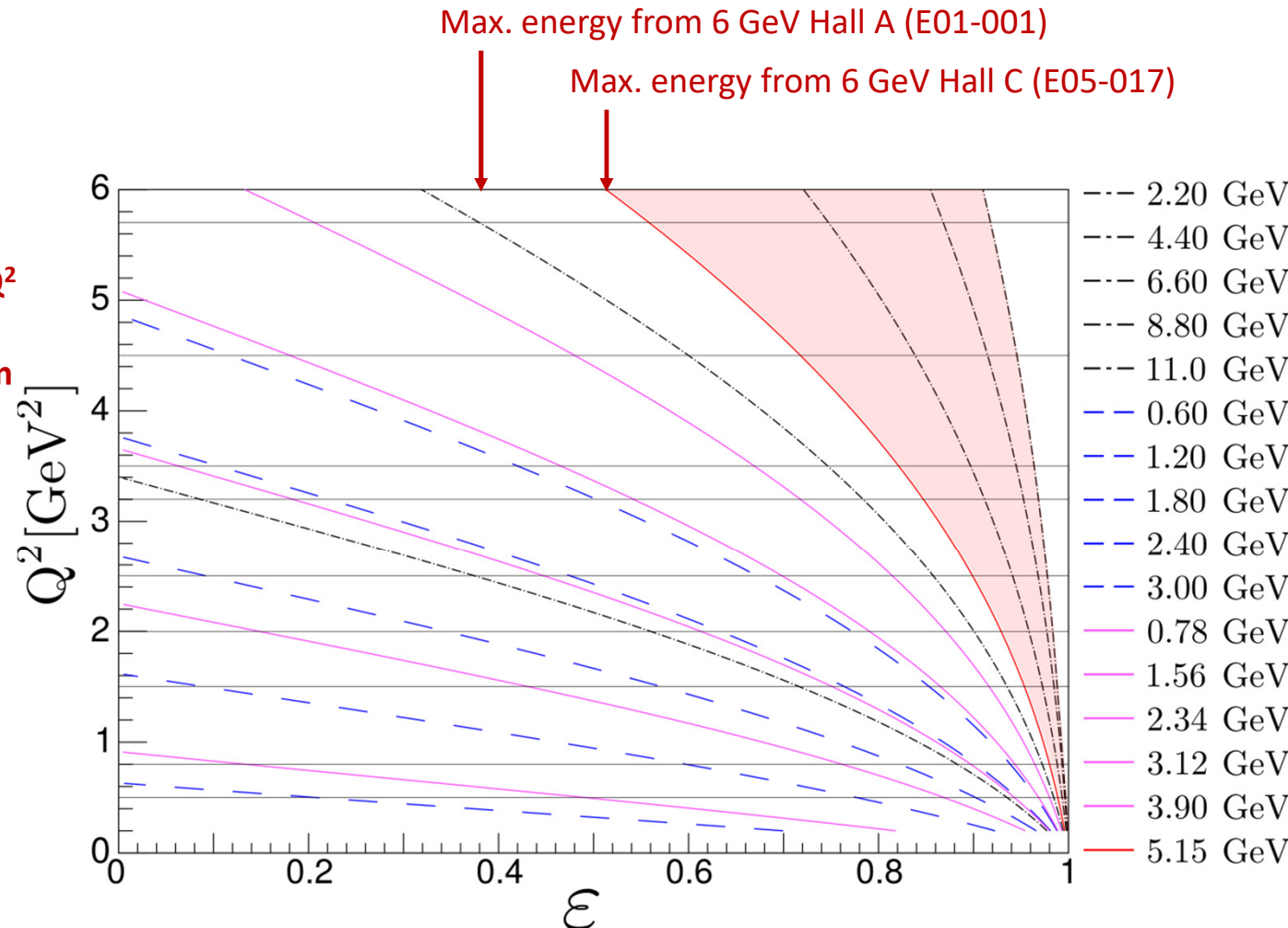
**Black: 2.2 GeV/pass**

- 2-3 high-epsilon points at each  $Q^2$
- Larger  $\epsilon$  range for higher  $Q^2$  points

**Blue or magenta: 0.6 or 0.78 GeV/pass**

- Each linac setting gives five different  $Q^2$  values with large lever arm in epsilon
- Intermediate  $Q^2$  with smaller lever arm

Can run with positrons only, compare to polarization  $\rightarrow$  should see opposite discrepancy than electrons



# Projected uncertainties

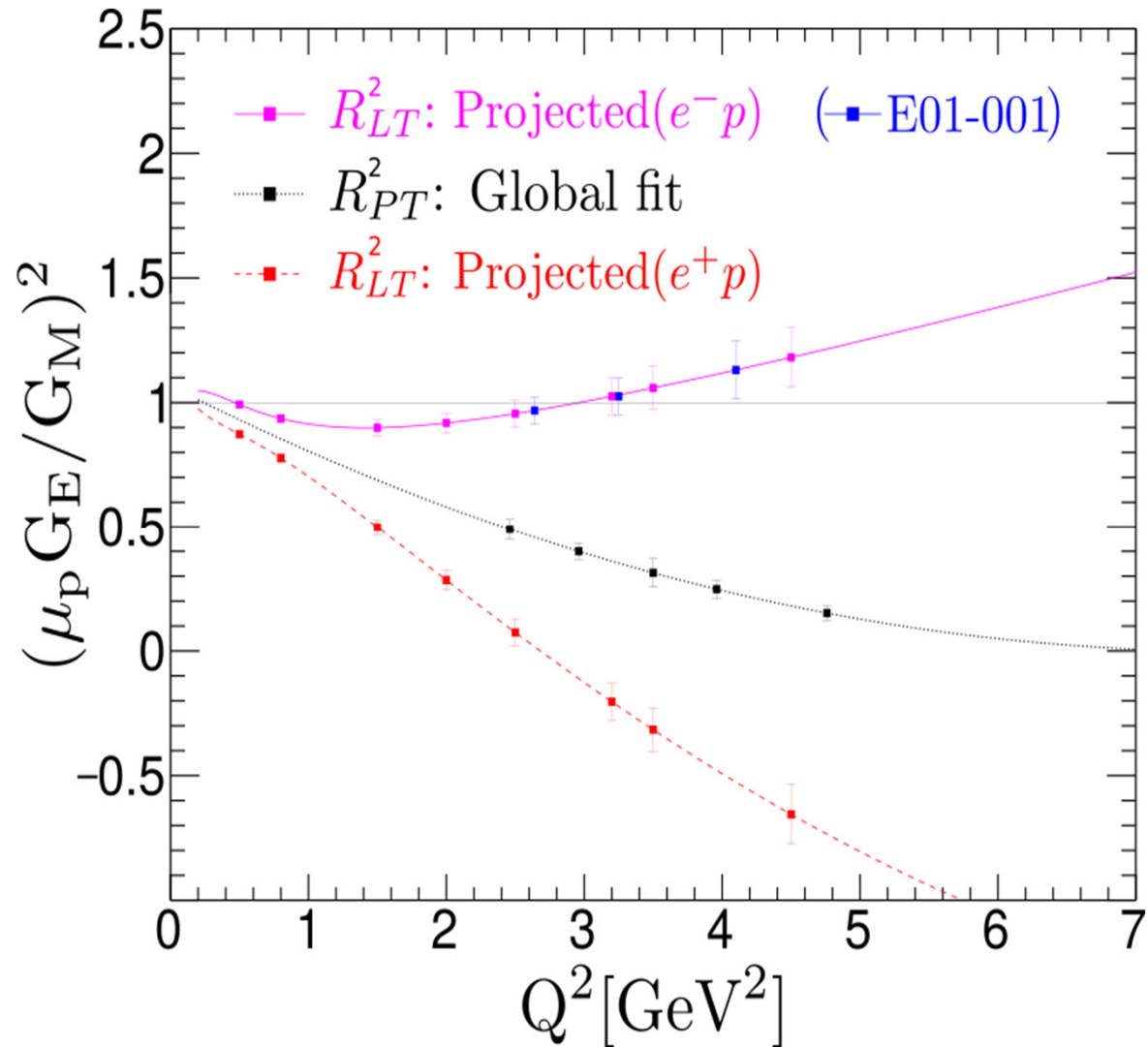
Uses all 3 linac settings from previous plot

Assumes 2 uA for positrons, 10cm LH2 target

Electron data in separate run: 20-50uA

→ 35-40 days using 2 HRSs in Hall A OR using the HMS in Hall C (twice the solid angle)

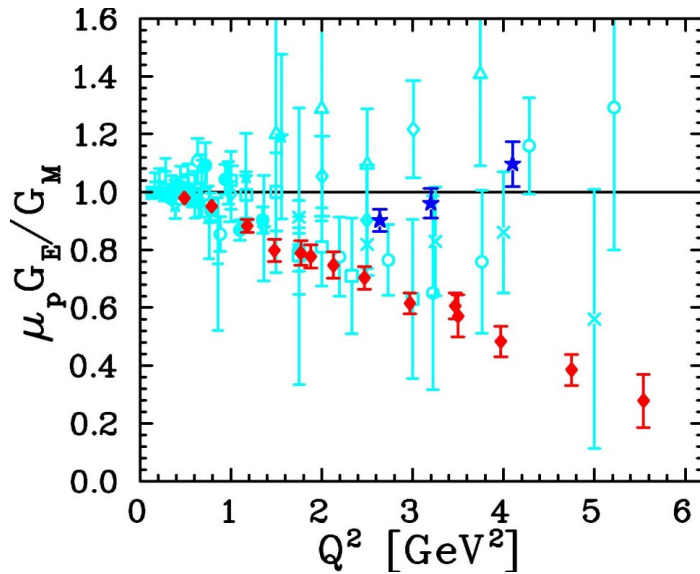
Comparison doubles size of observed TPE contributions, is independent of potential TPE to polarization measurements





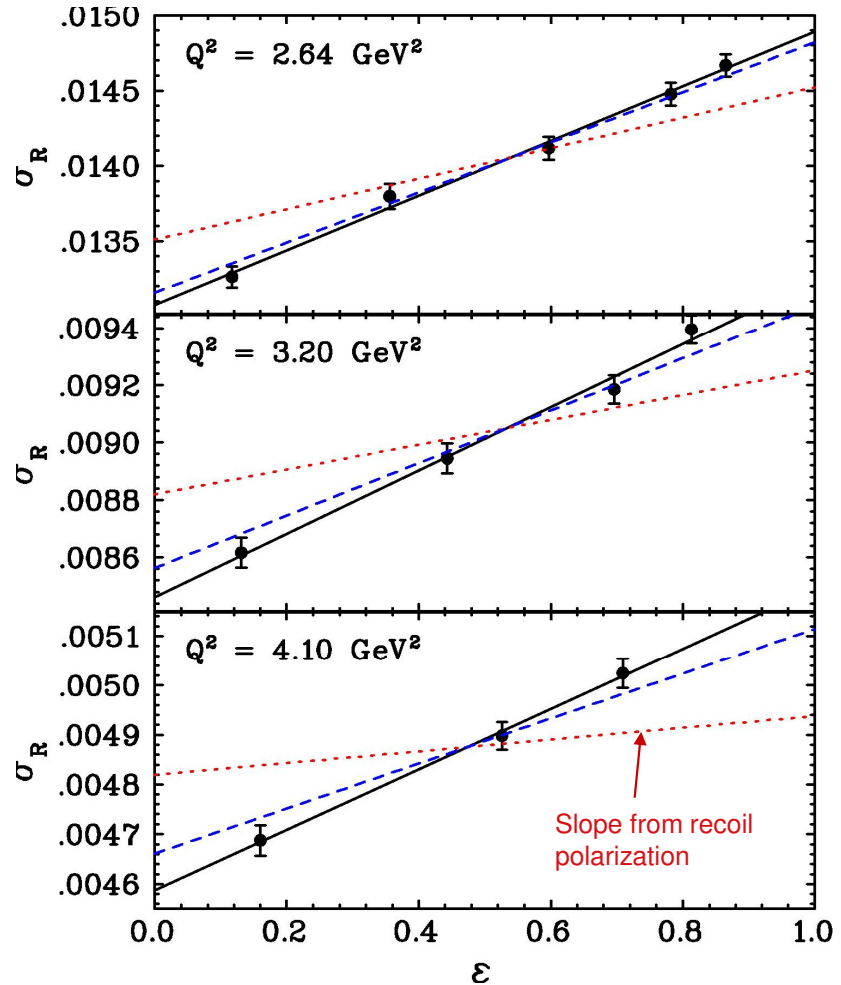
# Polarization vs. Rosenbluth: $G_E/G_M$

$\mu_p G_{Ep}/G_{Mp}$  from Rosenbluth measurements



New data: **Recoil polarization**  
and **p(e,p) "Super-Rosenbluth"**

JLab Hall A: *M. Jones, et al.; O. Gayou, et al.*  
*I. A. Qattan, et al, PRL 94, 142301 (2005)*



# Two Photon Exchange

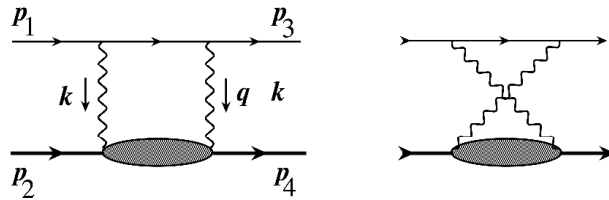
## Proton form factor measurements

- Comparison of precise Rosenbluth and Polarization measurements of  $G_{Ep}/G_{Mp}$  show clear discrepancy at high  $Q^2$

*I.A.Qattan, et al., PRL 94 (2005) 142301*

## Two-photon exchange corrections believed to explain the discrepancy

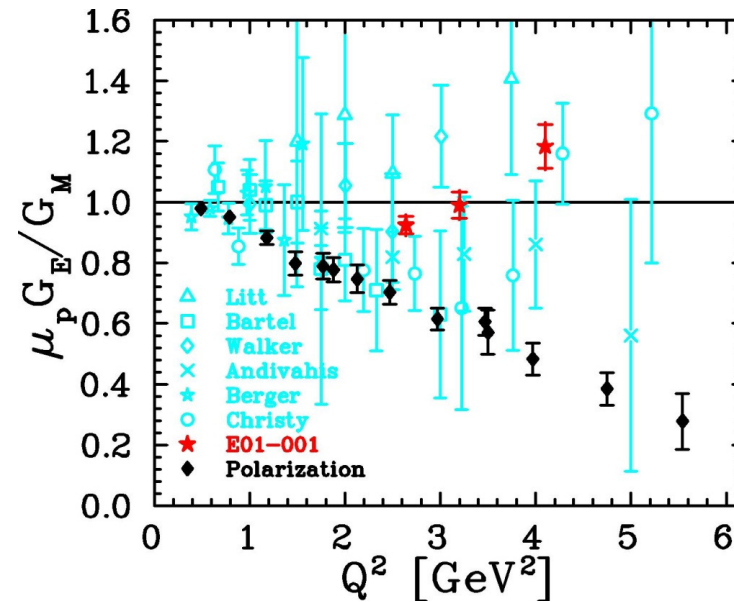
- Minimal impact on polarization data



- Active program to confirm, calculate, and understand TPE

*P. G. Blunden et al, PRC 72 (2005) 034612*  
*A.V. Afanasev et al, PRD 72 (2005) 013008*  
*D. Borisyuk, A. Kobushkin, PRC 78 (2008) 025208*  
*C. Carlson, M. Vanderhaeghen,*  
*Ann. Rev. Nucl. Part. Sci. 57 (2007) 171*  
*JA, P. Blunden, W. Melnitchouk, PPNP 66 (2011) 782*  
 + several completed or ongoing experiments

*P.A.M.Guichon and M.Vanderhaeghen, PRL 91, 142303 (2003)*



*M.K.Jones, et al., PRL 84, 1398 (2000)*  
*O.Gayou, et al., PRL 88, 092301 (2003)*  
*I.A.Qattan, et al., PRL 94, 142301 (2005)*



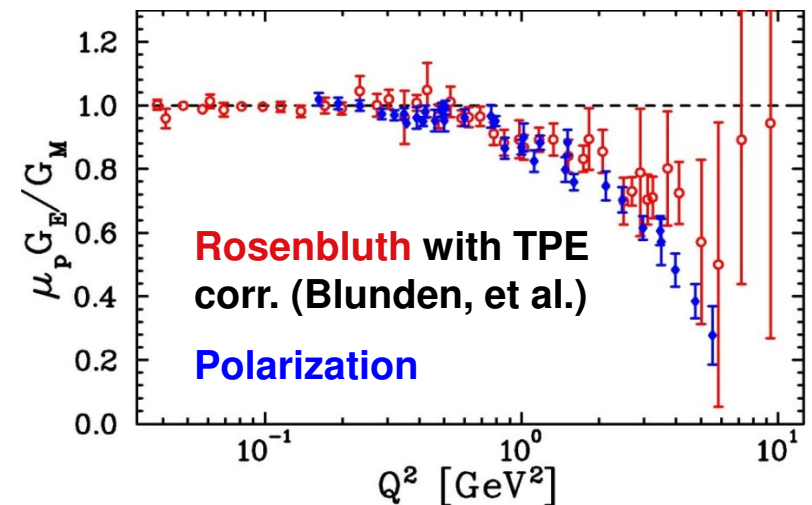
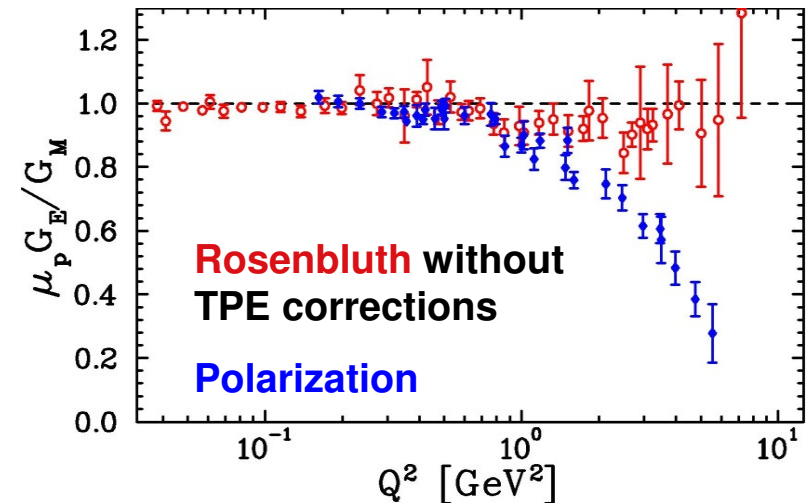
# Two Photon Exchange?

Limits set for non-linear (non-Born) contributions: *V. Tvaskis, et al., PRC 73 (2006) 025206*

Limits set for  $\theta$ -dependent (non-Born) PT contributions: *M. Meziane, PRL 106 (2011) 132501*

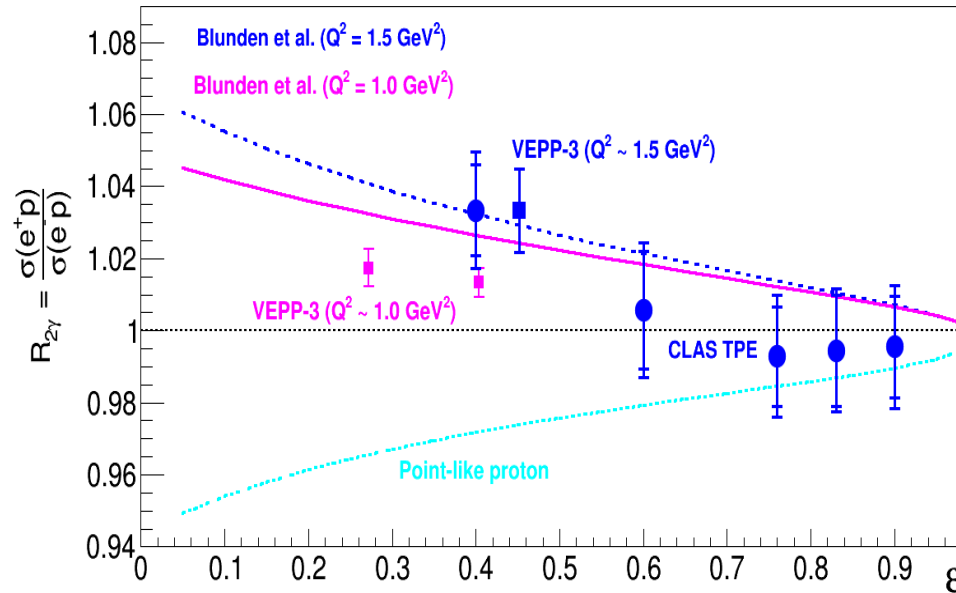
Evidence ( $3\sigma$ ) for TPE in existing  $e^+/e^-$  comparisons (TPE changes sign with lepton charge): *JA, PRC 69 (2004) 032201*

Many model-dependent TPE calculations - generally good qualitative agreement with observed discrepancy: *[Afanasev, et al.; Blunden, et al.; Borisyuk and Kobushkin; Chen, et al.; etc.....]*



*JA, W. Melnitchouk, J. Tjon, PRC 76, 035205 (2007)*

# Snapshot of new $e^+e^-$ comparisons



JLab: D. Adikaram, et al., PRL 114 (2015) 062003  
D. Rimal, et al., arXiv:1603.00315

VEPP-3: I.A.Rachek, et al., PRL 114 (2015) 062005

**Good agreement with hadronic TPE**

**Point proton ( $\sim Q^2=0$  limit) has opposite sign from data at  $Q^2 = 1-1.5 \text{ GeV}^2$**

**OLYMPUS: up to  $Q^2 \sim 2 \text{ GeV}^2$ ,  $\sim 1\%$  uncertainties [talk by J. Bernauer]**

- If Olympus also agrees with calculations, very strong overall case for TPE as culprit
  - Hadronic calculations appear to be reliable at low  $Q^2$ , where they should be most reliable, and where many of the extremely high-precision data are taken
  - Other improvements to radiative corrections still being investigated  
e.g., Gramolin and Nikolenko, PRC 93 (2016) 055201 [arXiv:1603.06920]

# Issues in extracting the radius: TPE corrections

**Blunden, Melnitchouk, Tjon, hadronic calculation** [PRC 72, 034612 (2005)]

**Borisyuk & Kobushkin:** Low- $Q^2$  expansion, valid up to  $0.1 \text{ GeV}^2$  [PRC 75, 038202 (2007)]

**B&K: Dispersion analysis (proton only)**

[PRC 78, 025208 (2008)]

**B&K: proton +  $\Delta$**  [arXiv:1206.0155]

**B&K proton only: (same as Blunden)**

