

# **Isovector EMC Effect from JAM Global QCD Analysis with MARATHON Data**

**Hanjie Liu  
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## Isovector EMC Effect from Global QCD Analysis with MARATHON Data

C. Cocuzza, C. E. Keppel, H. Liu, W. Melnitchouk, A. Metz, N. Sato, and A. W. Thomas (Jefferson Lab Angular Momentum (JAM) Collaboration)

Phys. Rev. Lett. **127**, 242001 – Published 6 December 2021

### **Outline – – from an experimentalist point of view:**

- Motivations and backgrounds
- Analysis details
- Results

### **From a theorist point of view:**

Christopher Cocuzza (Temple University)

[https://www.jlab.org/intralab/calendar/phys\\_seminar/2021/MARATHON%20Marathon%202021.pdf](https://www.jlab.org/intralab/calendar/phys_seminar/2021/MARATHON%20Marathon%202021.pdf)



# MARATHON Experiment

- Electron Deep Inelastic Scattering on p, D, H3, He3 fixed target @ JLab 11 GeV
- Goal is to measure  $F_2^n/F_2^p$  to put constraints on d/u quark distribution ratio at large x

## Some Backgrounds about MARATHON

1960 ~ 1990

### The Nobel Prize in Physics 1990

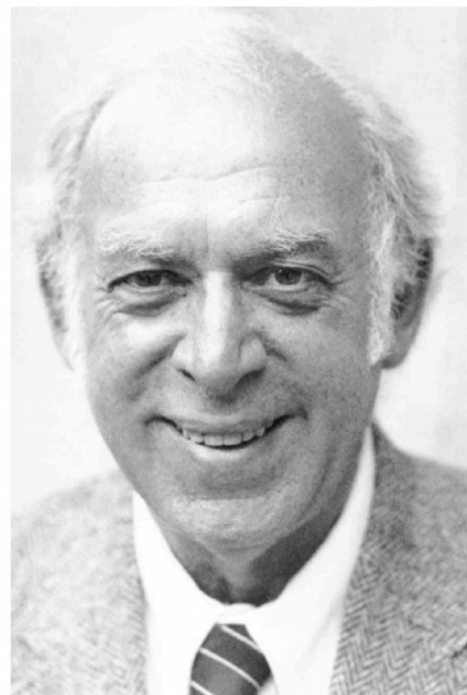


Photo from the Nobel Foundation archive.  
Jerome I. Friedman  
Prize share: 1/3

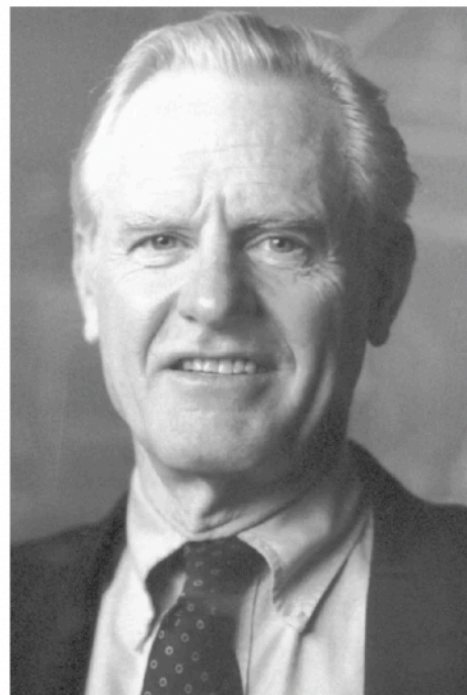


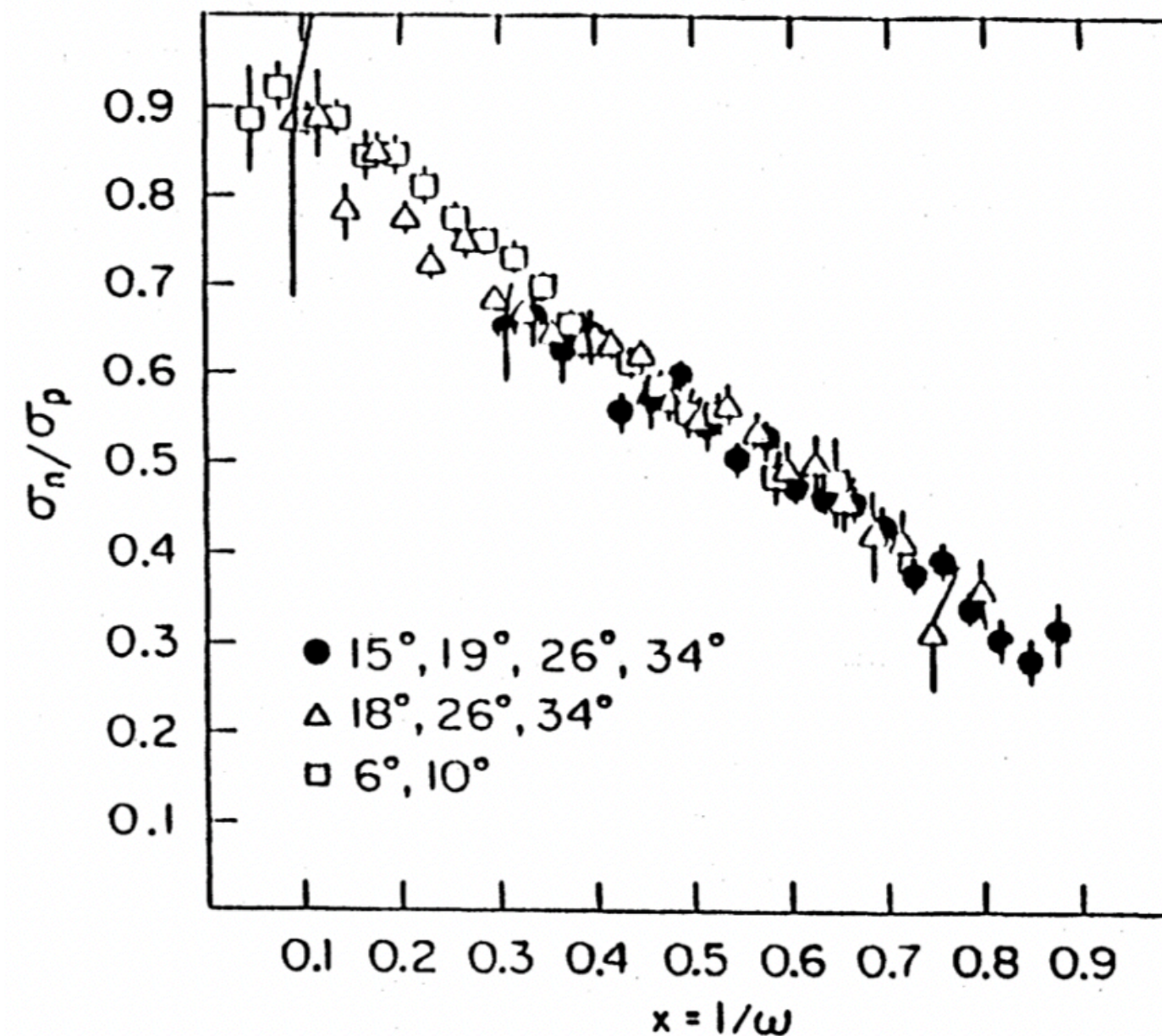
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Henry W. Kendall  
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Photo: T. Nakashima  
Richard E. Taylor  
Prize share: 1/3

“SLAC-MIT experiment”

Electron DIS leads to the discovery of quarks



Bodek et al. Phys.Rev. D20 (1979)

Only Fermi motion is considered in the extraction

$$\frac{\sigma_n}{\sigma_p} = U\left(\frac{\sigma_{ns}}{\sigma_{ps}}\right) = U\left(S_p \frac{\sigma_d}{\sigma_p} - 1\right).$$

~ 50 years history of measuring  $F_2^n/F_2^p$



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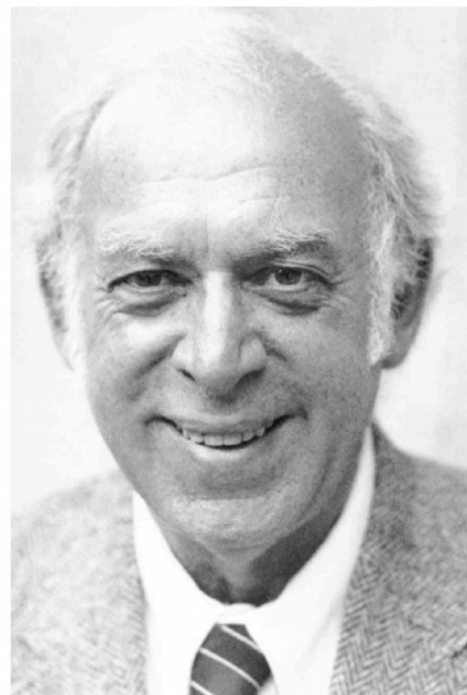


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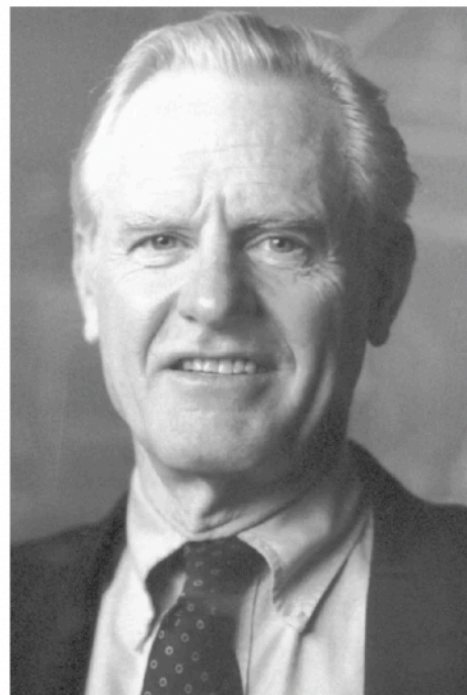


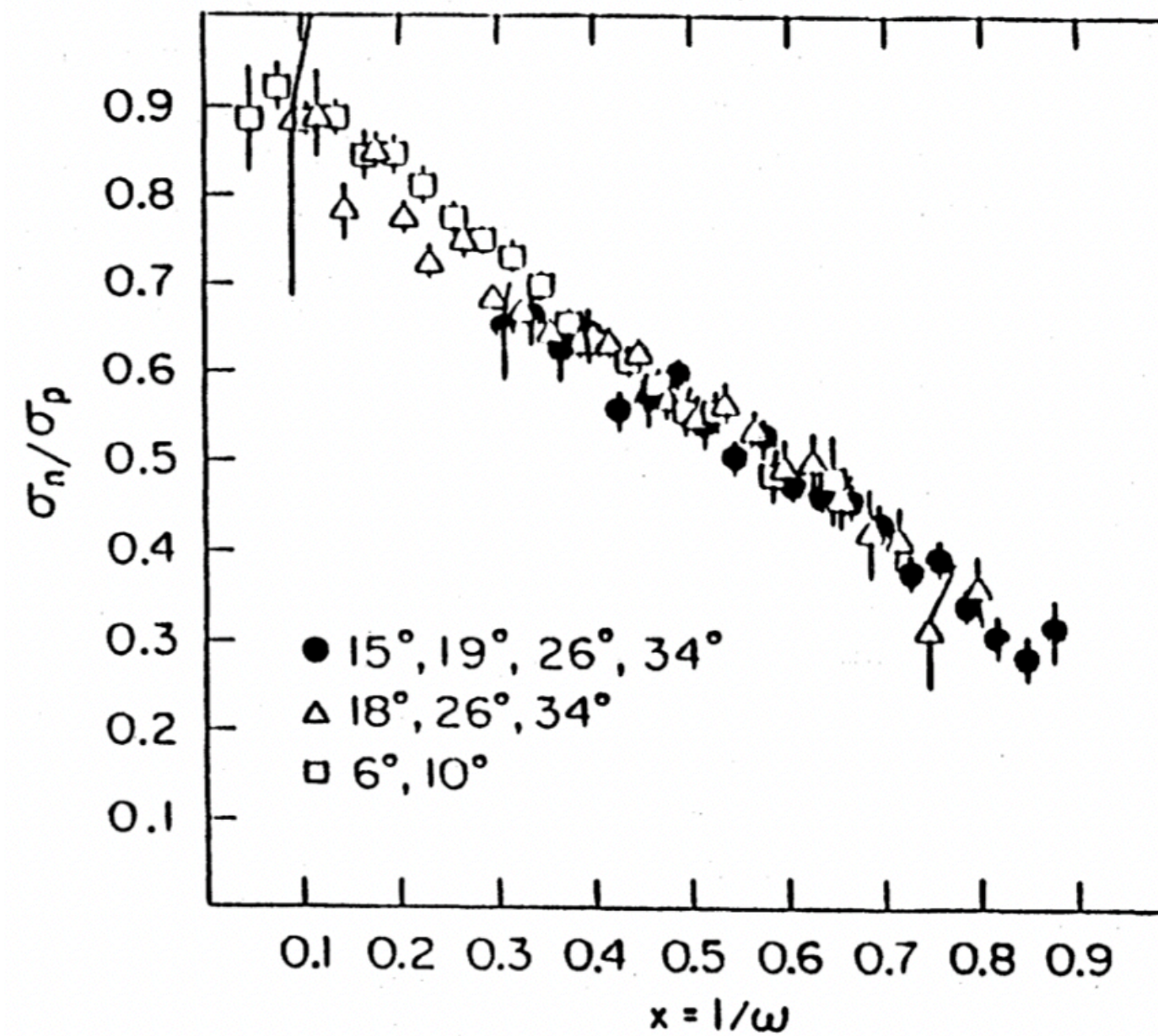
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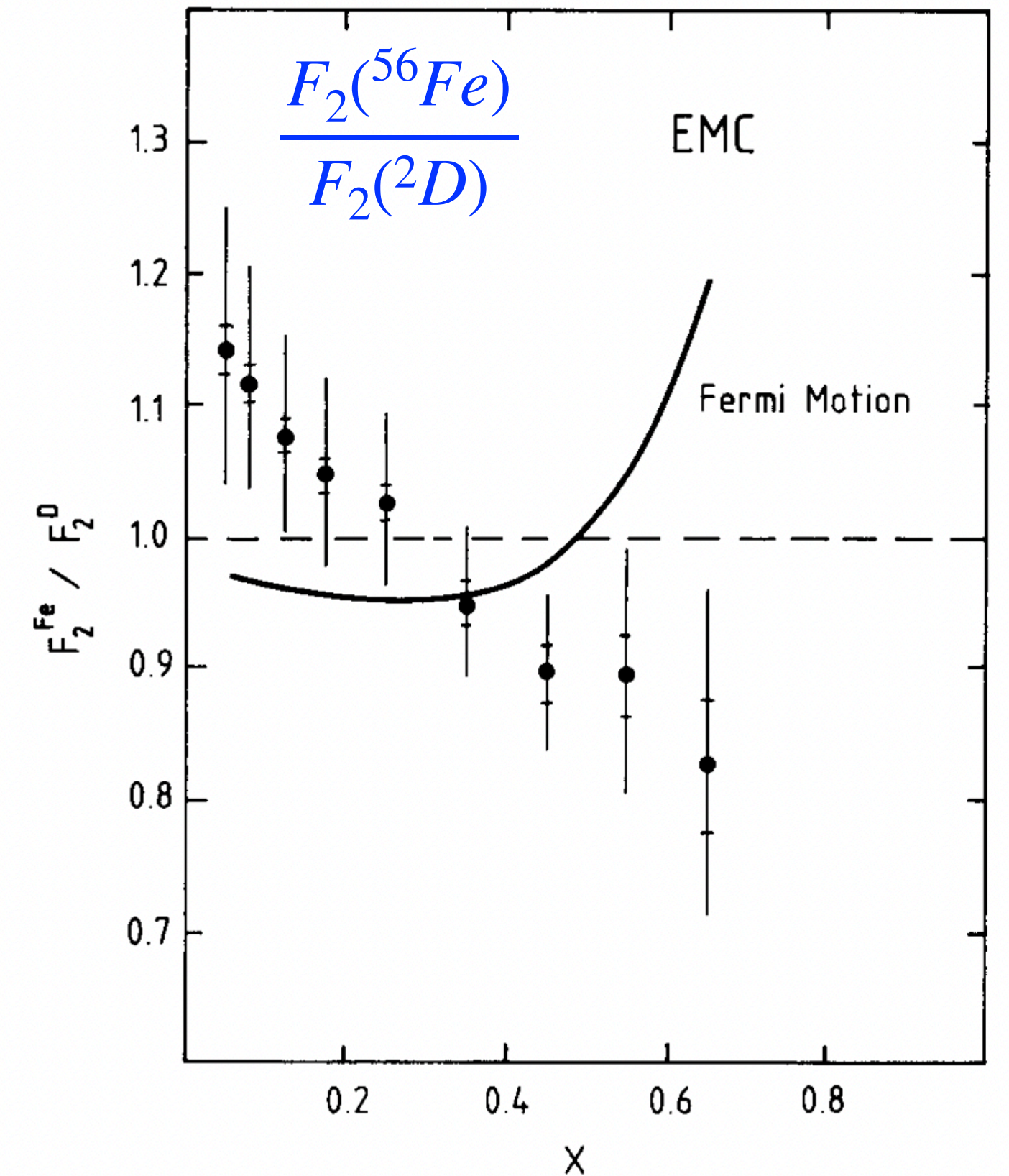
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Aubert J J et al. Nucl. Phys. B 293 740 (1987)

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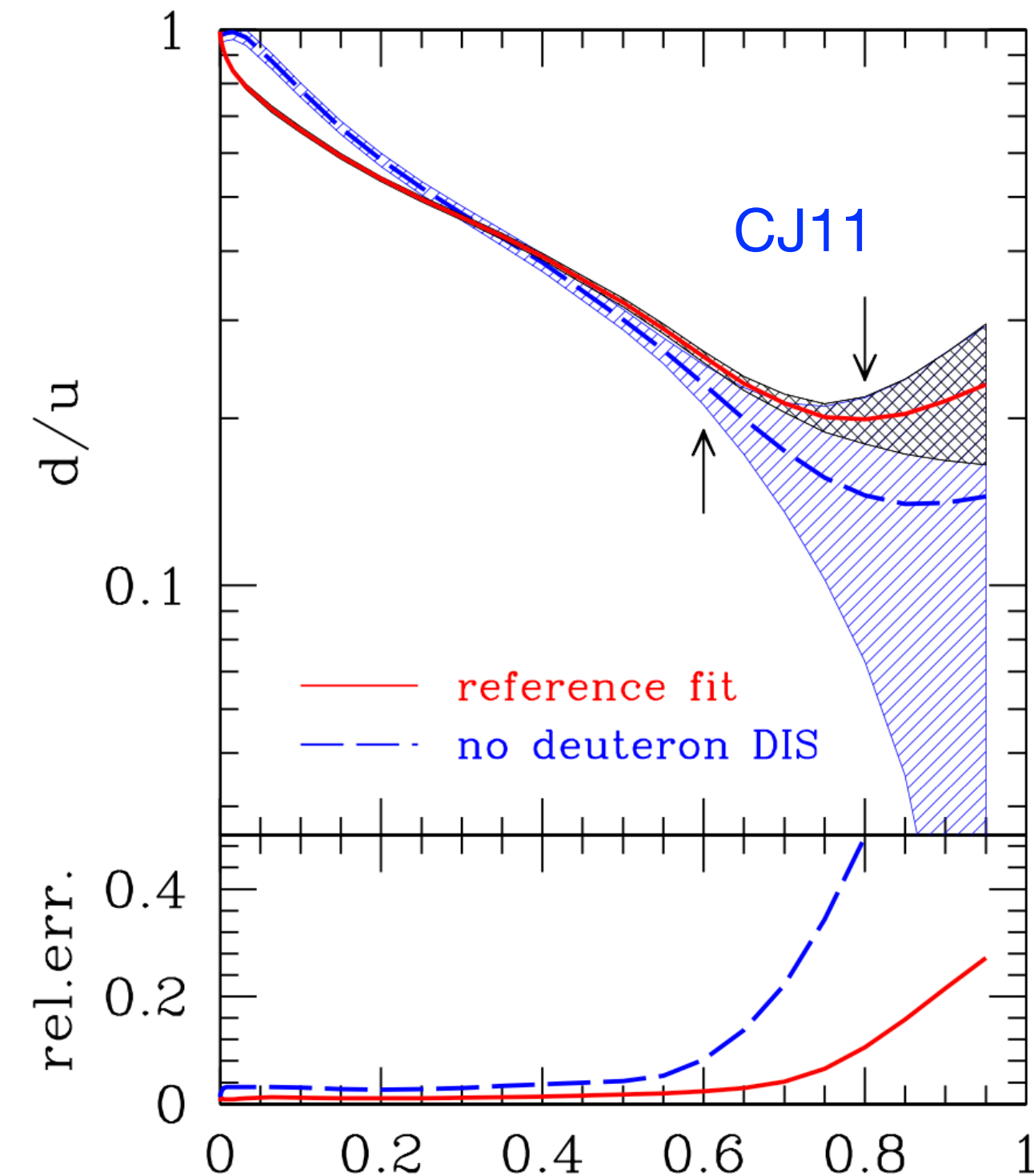
## Some Backgrounds about MARATHON

### Over the next 20 years

- Deep inelastic scattering is one of the primary way for PDFs parameterizations
- Lots of experiments are performed to understand the nuclear effects

			total		deuterium		CTEQ6.1
			cut0	cut3	cut0	cut3	
DIS	JLab	[58]	-	272	-	136	
	SLAC	[59]	206	1147	104	582	
	NMC	[60]	324	464	123	189	✓
	BCDMS	[61]	590	605	251	254	✓
	H1	[62]	230	251	-	-	✓
	ZEUS	[63]	229	240	-	-	✓
$\nu$ A DIS	CCFR	[64, 65]	-	-	-	-	✓
DY	E605	[66]	119	-	-	-	✓
	E866	[67]	375	-	191	-	
W asymmetry	CDF '98 ( $\ell$ )	[68]	11	-	-	-	✓
	CDF '05 ( $\ell$ )	[69]	11	-	-	-	
	D0 '08 ( $\ell$ )	[70]	10	-	-	-	
	D0 '08 ( $e$ )	[71]	12	-	-	-	
	CDF '09 (W)	[72]	13	-	-	-	
jet	CDF	[73]	33	-	-	-	✓
	D0	[74]	90	-	-	-	✓
$\gamma$ +jet	D0	[75]	56	-	-	-	
TOTAL			2408	3709	569	1161	

A. Accardi et al. Phys. Rev. D81 (2010)



A. Accardi et al. Phys. Rev. D84 (2011)

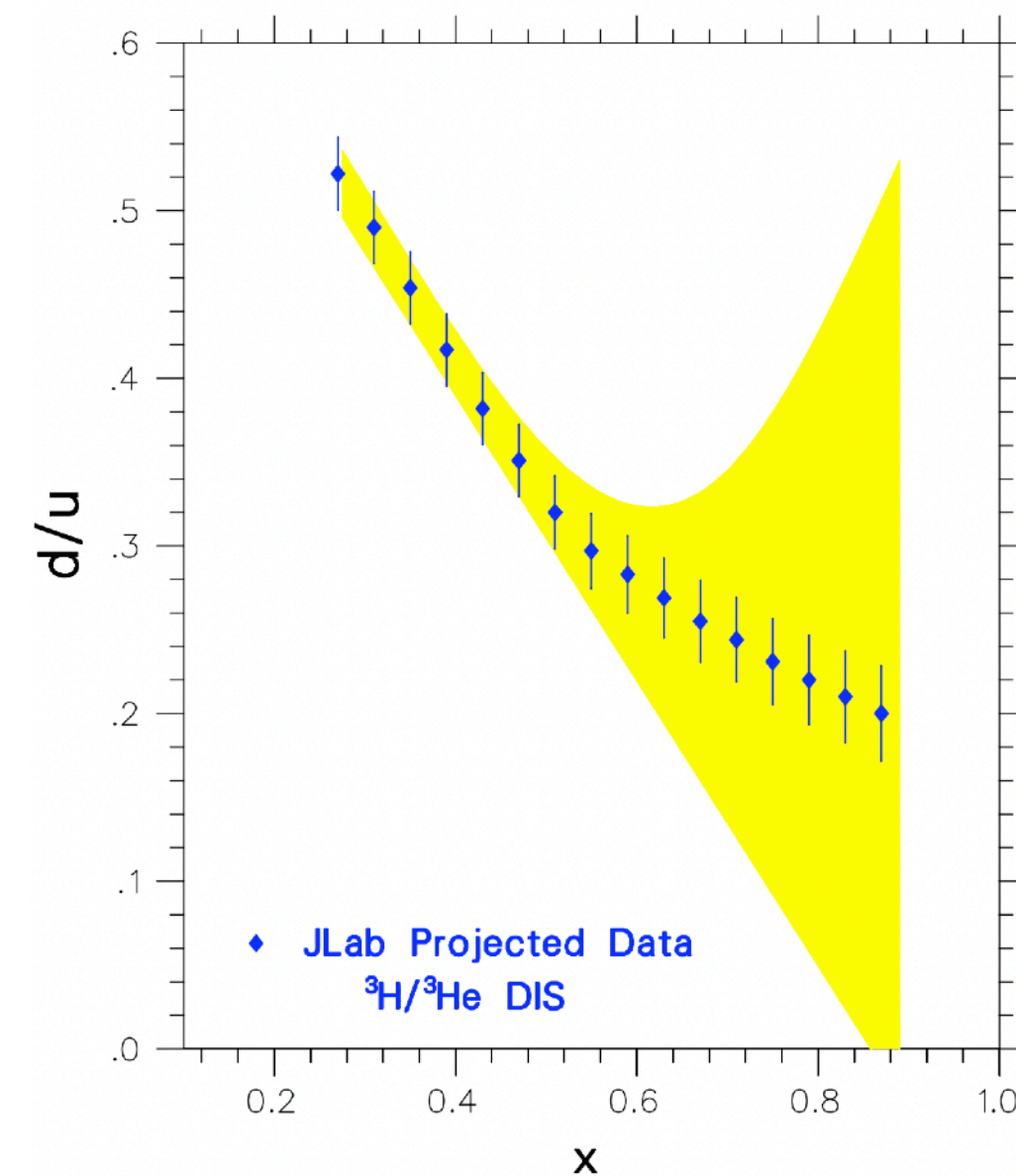
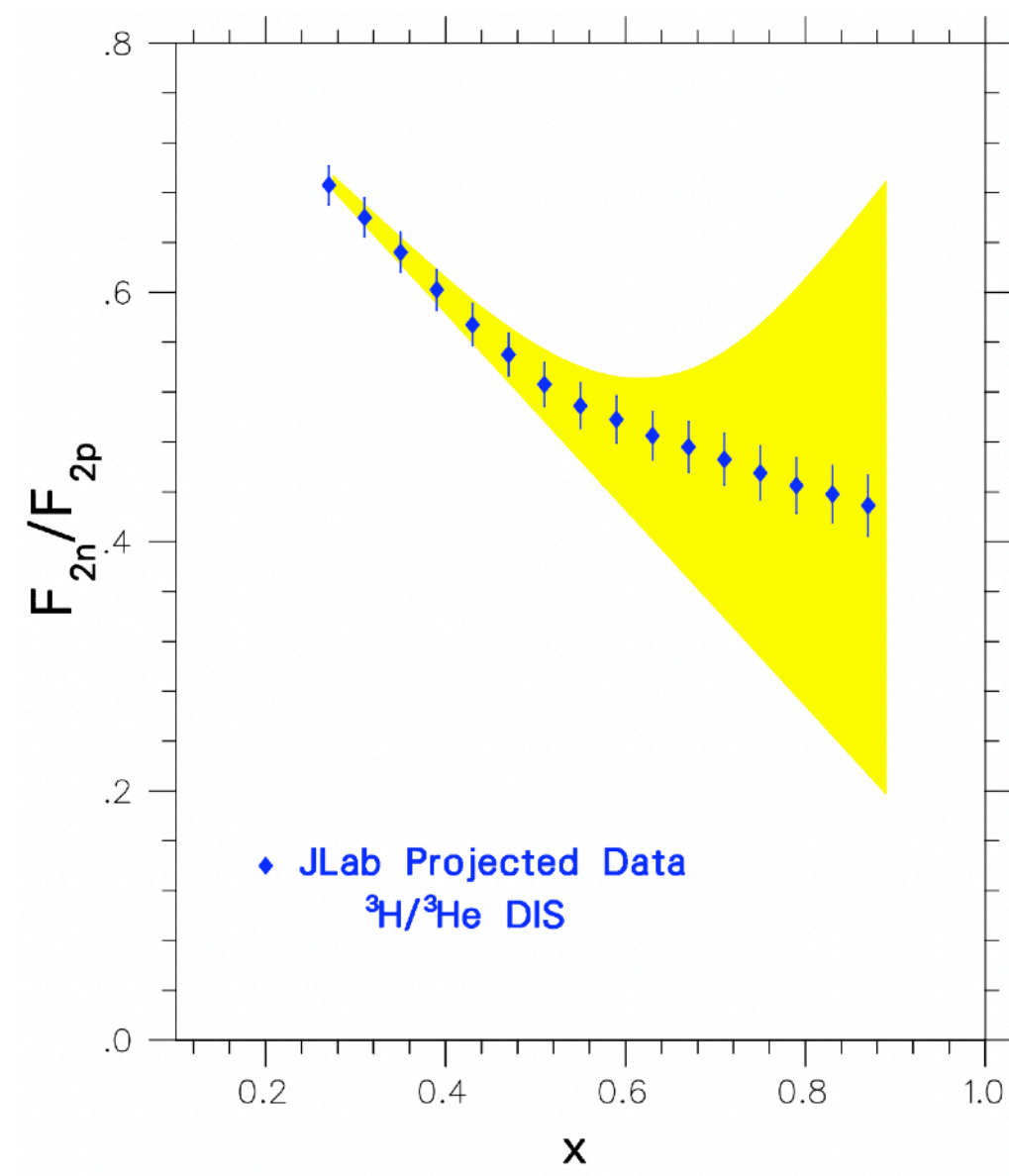


# MARATHON Experiment

- Electron Deep Inelastic Scattering on p, D, H3, He3 fixed target @ JLab 11 GeV
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## Some Backgrounds about MARATHON

- The idea of using H3 and He3 to extract  $F_2^n/F_2^p$  to avoid nuclear model dependence started @ 1999
- The proposal is approved at PAC36 @ 2010



MARATHON proposal 2010

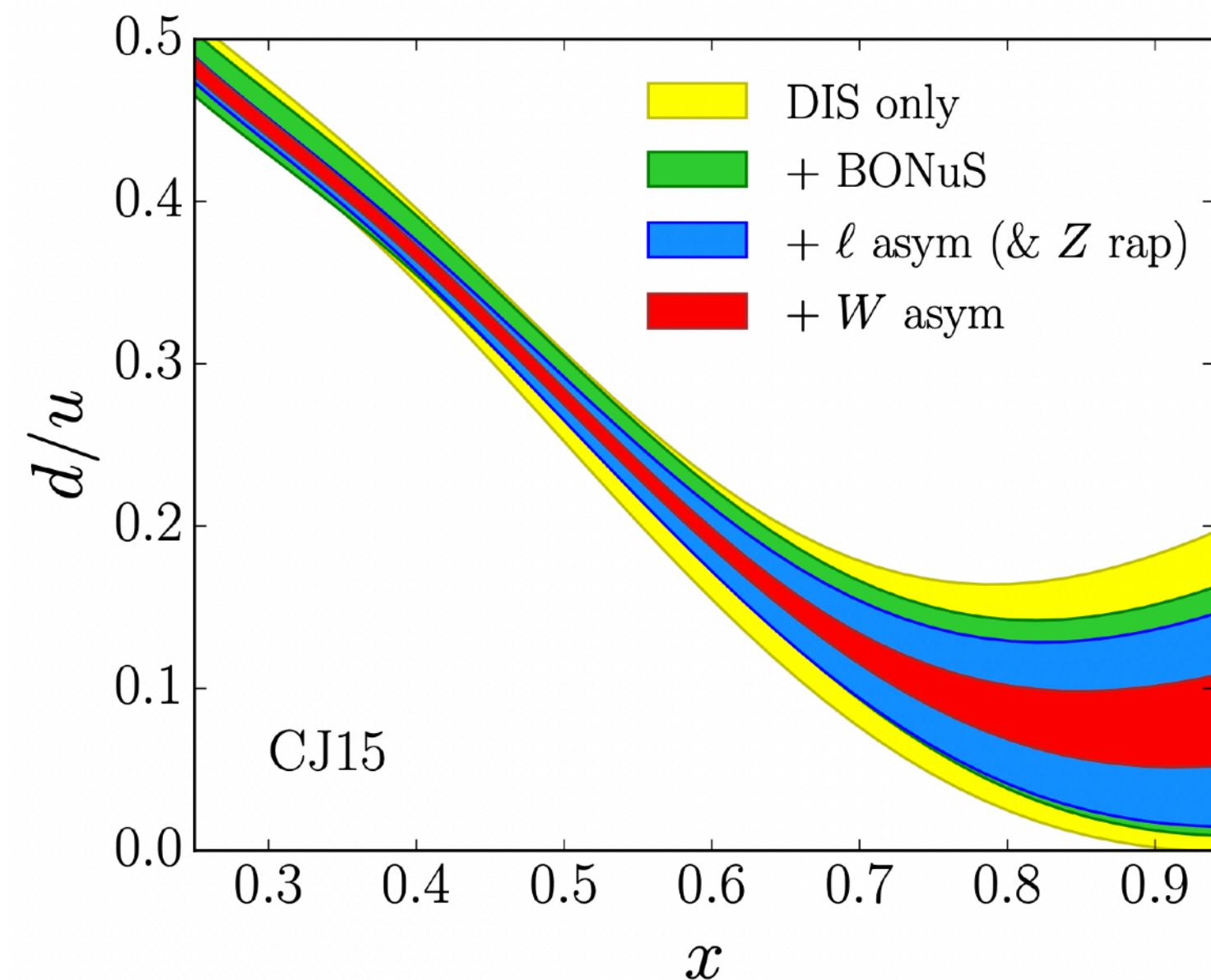


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- Electron Deep Inelastic Scattering on p, D, H3, He3 fixed target @ JLab 11 GeV
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## Some Backgrounds about MARATHON

- The idea of using H3 and He3 to extract  $F_2^n/F_2^p$  to avoid nuclear model dependence started @ 1999
- The proposal is approved at PAC36 @ 2010
- Large improvement on  $d/u$  with improved nuclear corrections and new high precision HEP data @ 2016



A. Accardi et al. Phys. Rev. D 93 (2016)

- MARATHON took data @ 2018 Spring



# MARATHON Experiment

Experimental way of extracting  $F_2^n / F_2^p$

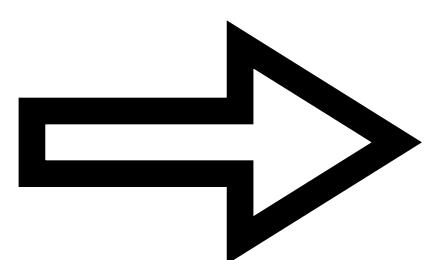
$$\frac{F_2^{3H}}{F_2^{3He}} = \frac{\sigma(^3H)}{\sigma(^3He)}$$

- EMC type of ratio

$$R(^3H) = \frac{F_2^{3H}}{F_2^p + 2F_2^n} \quad R(^3He) = \frac{F_2^{3He}}{2F_2^p + F_2^n}$$

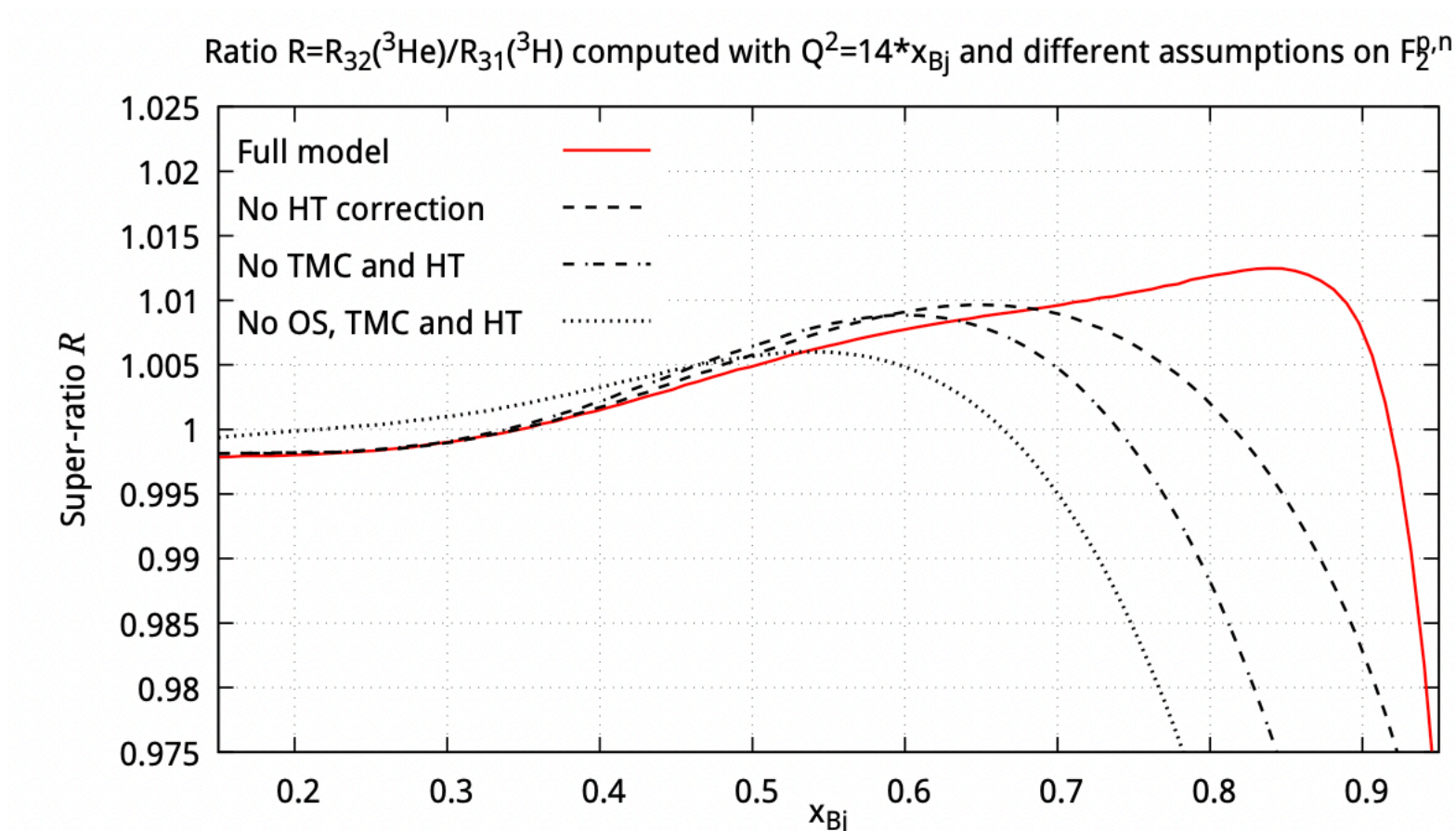
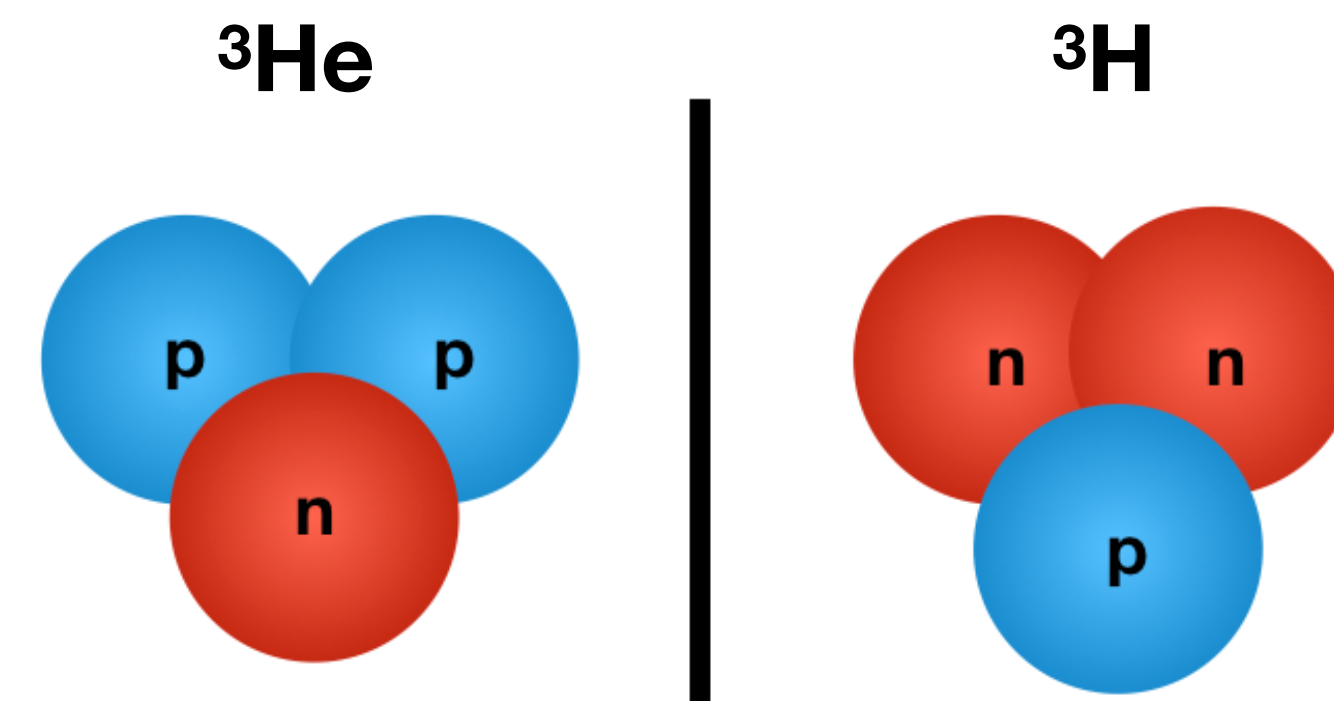
- Super ratio:

$$\mathcal{R} = \frac{R(^3He)}{R(^3H)}$$



$$\frac{F_2^n}{F_2^p} = \frac{2\mathcal{R} - F_2^{3He} / F_2^{3H}}{2F_2^{3He} / F_2^{3H} - \mathcal{R}}$$

- measure  $F_2^{3He} / F_2^{3H}$
- $\mathcal{R}$  is determined by theory



Super-ratio  $\mathcal{R}$  calculated by S. Kulagin and R. Petti

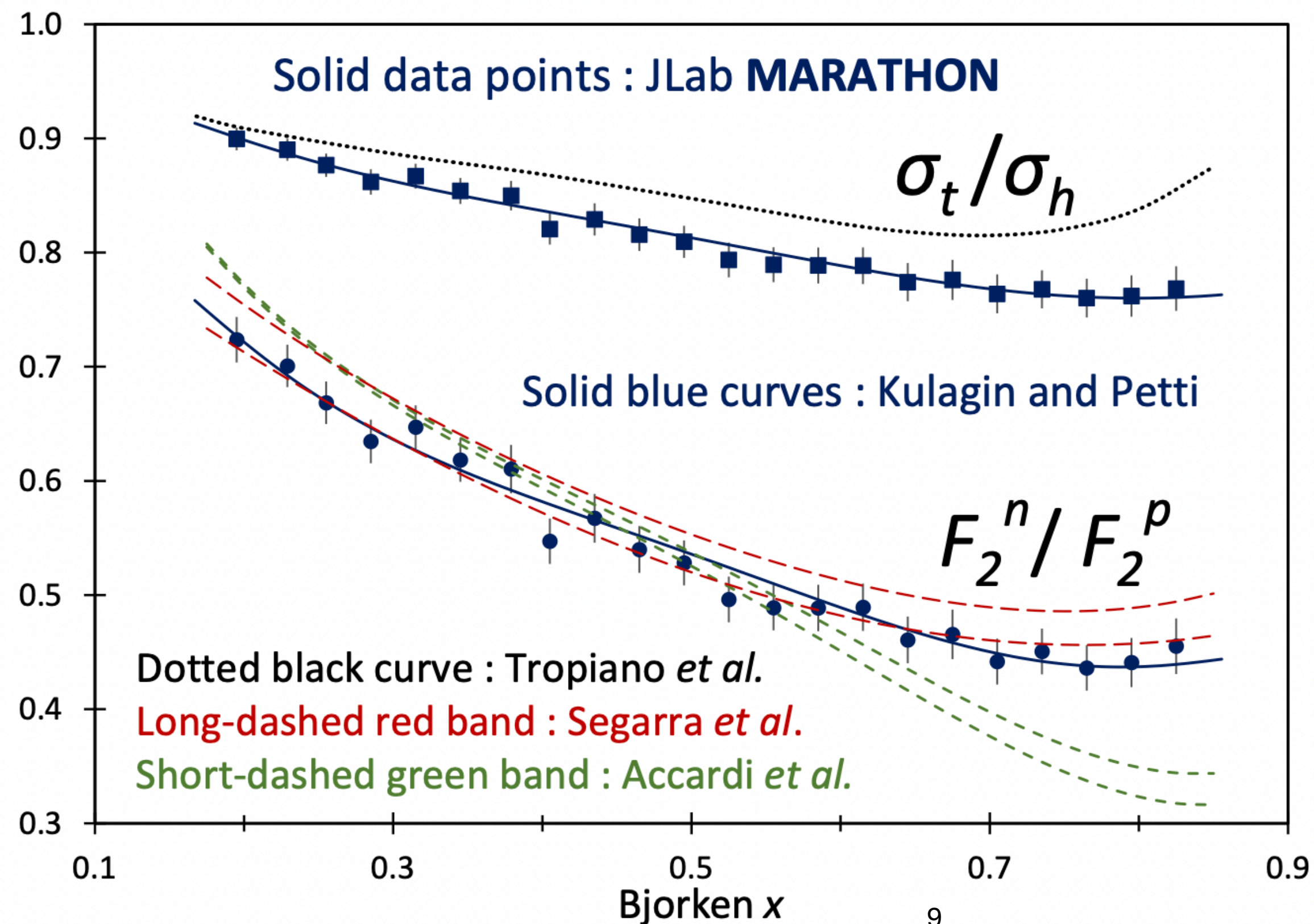
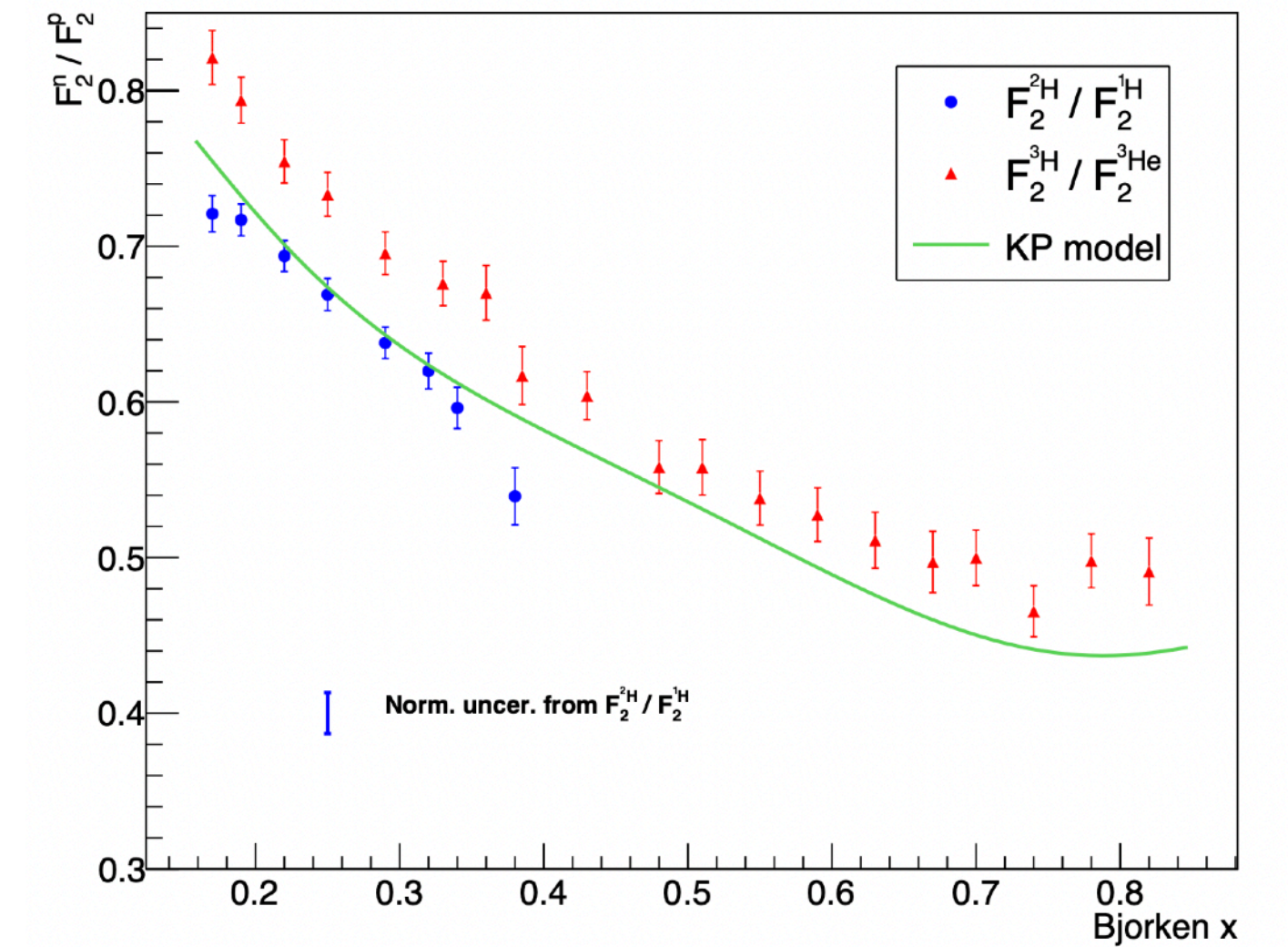
$^3He$  and  $^3H$  are mirror nuclei, the nuclear effect should be similar and have small model dependence



# MARATHON Experiment

Experimental way of extracting  $F_2^n / F_2^p$

In order to match the  $F_2^n / F_2^p$  extracted from  $\sigma(^3\text{He})/\sigma(^3\text{H})$  to that from  $\sigma(\text{D})/\sigma(\text{p})$  at  $x = 0.31$ ,  $\sigma(^3\text{He})/\sigma(^3\text{H})$  ratio at  $x = 0.31$  had to be normalized by a multiplicative factor of  $1.025 \pm 0.007$



**Final results**

**Phys. Rev. L 128, 132003 (2022)**

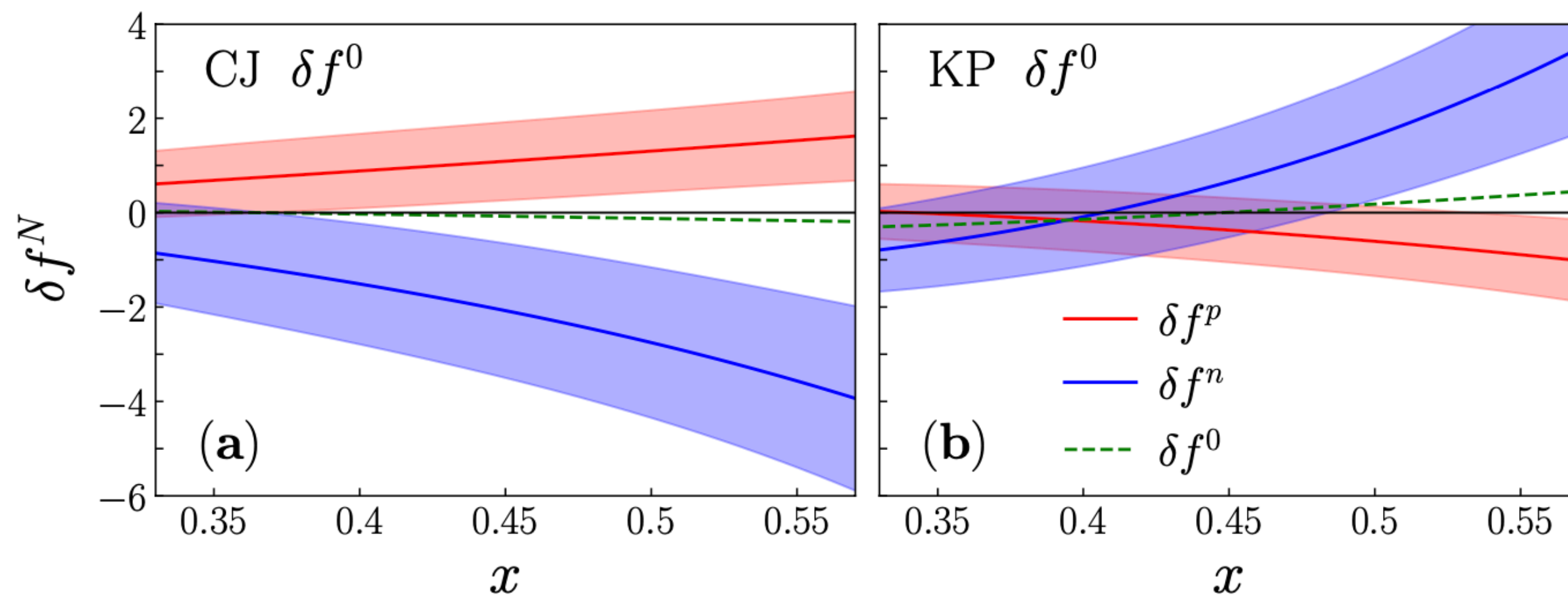


# MARATHON Experiment

## Theoretical way of thinking about MARATHON data

Cross section ratios:  $\sigma(^3\text{He})/\sigma(^3\text{H})$ ,  $\sigma(\text{D})/\sigma(\text{p})$

- How much impact is MARATHON data on PDFs and nucleon structure functions
- MARATHON data may help study the isovector effect
- Is the normalization on  $\sigma(^3\text{He})/\sigma(^3\text{H})$  necessary?



A. J. Tropiano, J. J. Ethier, W. Melnitchouk, N. Sato  
Phys. Rev. C 99, 035201 (2019)

- Hall C E03-103 He3/D data needs 3% normalization if using KP model to match n/p from other datasets
- Possible isospin dependence of the nuclear effect is indicated in the fitting of He3/D data
- $^3\text{He}$  and  $^3\text{H}$  are light nuclei, and n/p ratio are very different: 2 and 1/2

# Jefferson Lab Angular Momentum (JAM) Collaboration

A Powerful framework utilizing the development from multiple areas

Inclusive DIS:

$$l + N \rightarrow l + X$$

$$\frac{d\sigma_{\text{DIS}}}{dQ^2 dx_{\text{Bj}}} = \sum_i \mathcal{H}_i^{\text{DIS}} \otimes f_i$$

Semi-inclusive DIS:

$$l + N \rightarrow l + h^\pm + X$$

$$\frac{d\sigma_{\text{SIDIS}}}{dQ^2 dx_{\text{Bj}} dz_h} = \sum_{ij} \mathcal{H}_{ij}^{\text{SIDIS}} \otimes f_i \otimes D_j^h$$

Drell-Yan lepton-pair production:

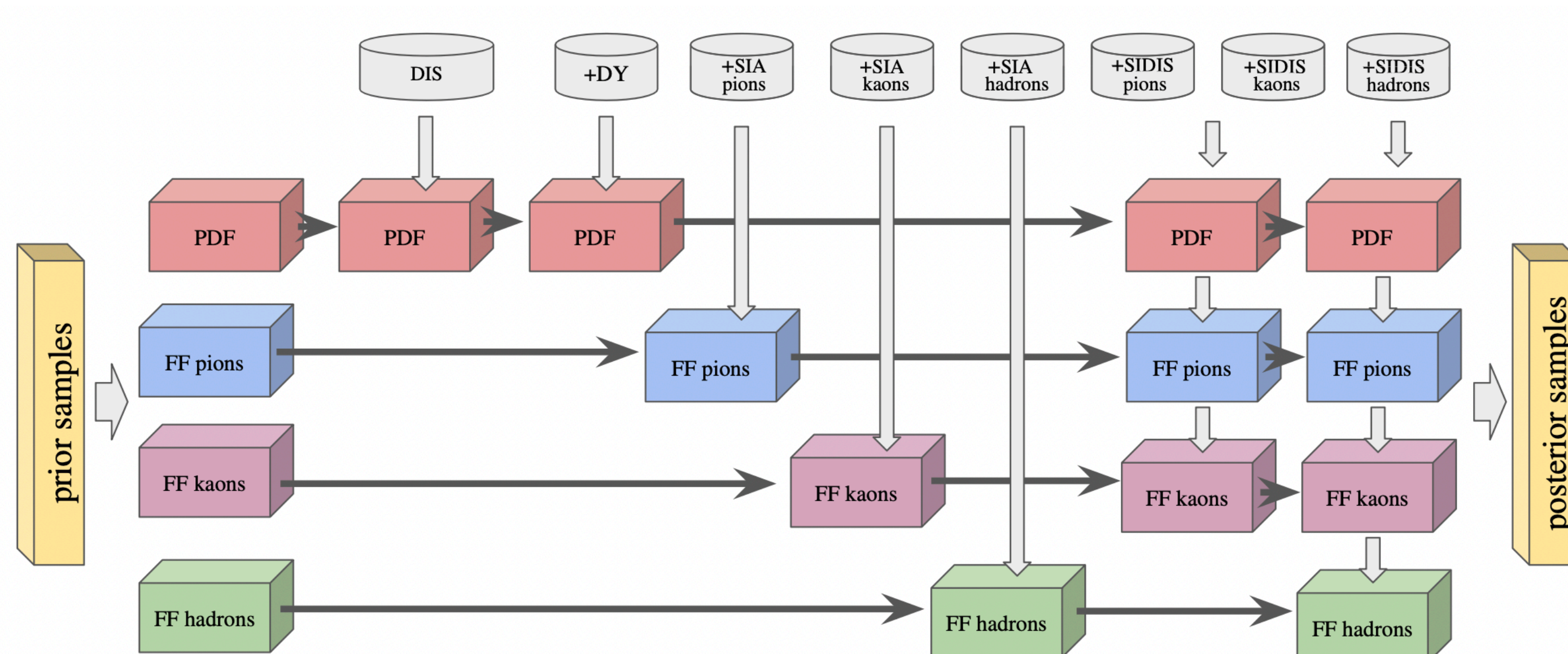
$$N_1 + N_2 \rightarrow l^+ + l^- + X$$

$$\frac{d\sigma_{\text{DY}}}{dQ^2 dx_{\text{F}}} = \sum_{ij} \mathcal{H}_{ij}^{\text{DY}} \otimes f_i \otimes f_j$$

Single-inclusive annihilation:

$$l^+ + l^- \rightarrow h^\pm + X$$

$$\frac{d\sigma_{\text{SIA}}}{dQ^2 dz_h} = \sum_j \mathcal{H}_j^{\text{SIA}} \otimes D_j^h$$



Fit simultaneously:

- PDFs
- FFs
- Nuclear effect

using a multistep Bayesian inference procedure



# JAM and A=3 nuclei

$$F_2^A(x, Q^2) = F_2^{A(on)} + F_2^{A(off)}$$

$$F_2^{A(on)}(x, Q^2) = \sum_N [ f^{N/A} \otimes F_2^{N(on)} ] \quad , \quad N = n, p$$

on-shell smearing function

$$F_2^{A(off)}(x, Q^2) = \sum_N [ \tilde{f}^{N/A} \otimes F_2^{N/A(off)} ]$$

off-shell smearing function

computed from the nuclear wave functions or spectral functions.

$$F_2^{N(on)}(x, Q^2) = \left( \sum_q [C_q \otimes q_N^+] + [C_g \otimes g_N] \right) \times \left( 1 + \frac{C_N^{HT}(x)}{Q^2} \right)$$

$$F_2^{N/A(off)}(x, Q^2) = \left( \sum_q [C_q \otimes \delta q_{N/A}] \right) \times \left( 1 + \frac{C_N^{HT}(x)}{Q^2} \right)$$

off-shell corrections

2 × 2 × 3 = 12 functions  
(u, d) × (p, n) × (3He, 3H, D)

Parameterize PDFs at input scale  $Q_0^2 = m_c^2$

$$f_i(x) = Nx^\alpha(1-x)^\beta(1 + \gamma\sqrt{x} + \eta x)$$

Evolve PDFs using DGLAP

$$\frac{d}{d \ln(\mu^2)} f_i(x, \mu) = \sum_j \int_x^1 \frac{dz}{z} P_{ij}(z, \mu) f_j\left(\frac{x}{z}, \mu\right)$$

# Offshell corrections

$$\delta u_{p/D}$$

$$\delta u_{n/D}$$

$$\delta u_{p/^3\text{He}}$$

$$\delta u_{n/^3\text{He}}$$

$$\delta u_{p/^3\text{H}}$$

$$\delta u_{n/^3\text{H}}$$

$$\delta d_{p/D}$$

$$\delta d_{n/D}$$

$$\delta d_{p/^3\text{He}}$$

$$\delta d_{n/^3\text{He}}$$

$$\delta d_{p/^3\text{H}}$$

$$\delta d_{n/^3\text{H}}$$



# Offshell corrections

$$\delta u_{p/D} \quad \delta u_{n/D} \quad \delta u_{p/{}^3\text{He}} \quad \delta u_{n/{}^3\text{He}} \quad \delta u_{p/{}^3\text{H}} \quad \delta u_{n/{}^3\text{H}}$$

$$\delta d_{p/D} \quad \delta d_{n/D} \quad \delta d_{p/{}^3\text{He}} \quad \delta d_{n/{}^3\text{He}} \quad \delta d_{p/{}^3\text{H}} \quad \delta d_{n/{}^3\text{H}}$$

## Charge symmetry

$$\delta u_{p/D} = \delta d_{n/D} \quad \delta u_{n/D} = \delta d_{p/D}$$

$$\delta u_{p/{}^3\text{He}} = \delta d_{n/{}^3\text{H}} \quad \delta u_{n/{}^3\text{He}} = \delta d_{p/{}^3\text{H}}$$

$$\delta d_{p/{}^3\text{He}} = \delta u_{n/{}^3\text{H}} \quad \delta d_{n/{}^3\text{He}} = \delta u_{p/{}^3\text{H}}$$

# Offshell corrections

$$\begin{array}{cccccc} \delta u_{p/D} & \cancel{\delta u_{n/D}} & \delta u_{p/^3\text{He}} & \cancel{\delta u_{n/^3\text{He}}} & \delta u_{p/^3\text{H}} & \cancel{\delta u_{n/^3\text{H}}} \\ \delta d_{p/D} & \cancel{\delta d_{n/D}} & \delta d_{p/^3\text{He}} & \cancel{\delta d_{n/^3\text{He}}} & \delta d_{p/^3\text{H}} & \cancel{\delta d_{n/^3\text{H}}} \end{array}$$

## Charge symmetry

$$\delta u_{p/D} = \delta d_{n/D} \quad \delta u_{n/D} = \delta d_{p/D}$$

$$\delta u_{p/^3\text{He}} = \delta d_{n/^3\text{H}} \quad \delta u_{n/^3\text{He}} = \delta d_{p/^3\text{H}}$$

$$\delta d_{p/^3\text{He}} = \delta u_{n/^3\text{H}} \quad \delta d_{n/^3\text{He}} = \delta u_{p/^3\text{H}}$$



# Offshell corrections

$\delta u_{p/D}^{\delta_u}$	<del><math>\delta u_{n/D}</math></del>	$\delta u_{p/^3He}^{\frac{1}{2}(\delta_u + 2\delta_d)}$	<del><math>\delta u_{n/^3He}</math></del>	$\delta u_{p/^3H}^{\delta_u}$	<del><math>\delta u_{n/^3H}</math></del>
$\delta d_{p/D}^{\delta_d}$	<del><math>\delta d_{n/D}</math></del>	$\delta d_{p/^3He}^{\frac{1}{4}(\delta_u + 2\delta_d)}$	<del><math>\delta d_{n/^3He}</math></del>	$\delta d_{p/^3H}^{\delta_d}$	<del><math>\delta d_{n/^3H}</math></del>

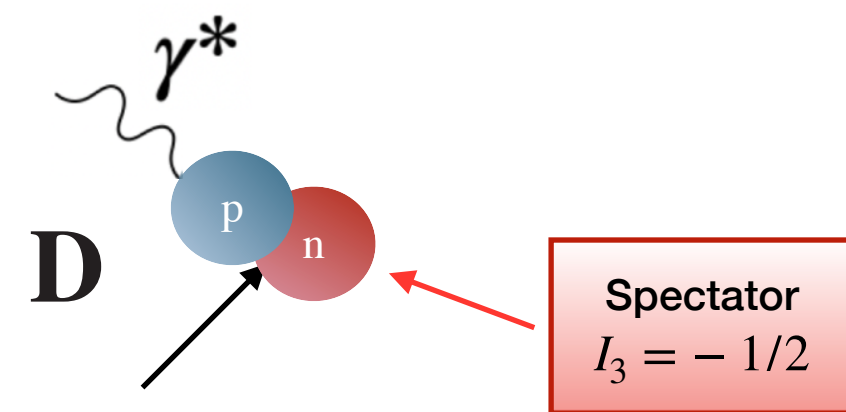
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$$\delta d_{p/^3He} = \delta u_{n/^3H} \quad \delta d_{n/^3He} = \delta u_{p/^3H}$$

Assume a spectator system for the DIS on proton inside of a nucleus:



- Assume same off-shell function for D and  $^3H$

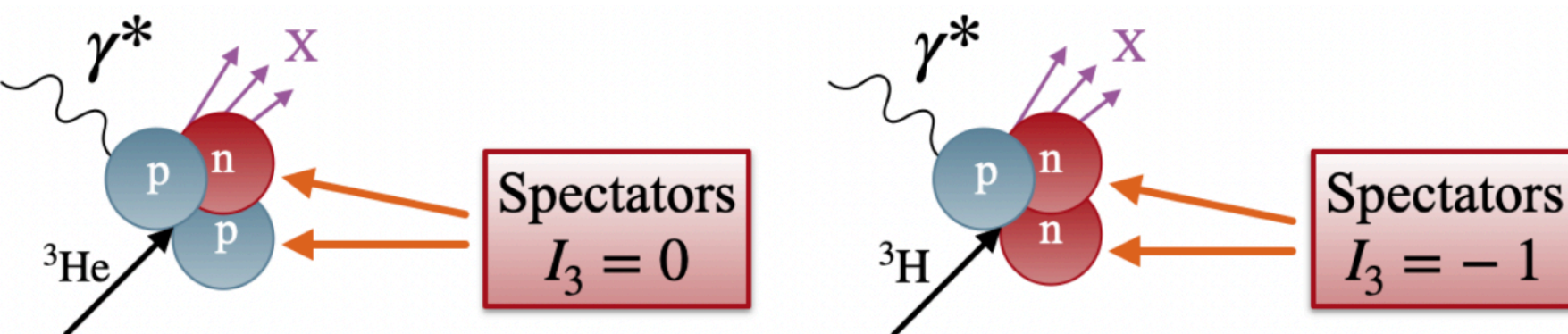
$$\delta d_{p/D} = \delta d_{p/^3H} \equiv \delta_d \quad \delta u_{p/D} = \delta u_{p/^3H} \equiv \delta_u$$

- The isospin of  $^3He$  spectators are 0, assume no isovector contribution

$$\delta u_{p/^3He} \approx 2\delta d_{p/^3He} = \frac{1}{2}(\delta u + 2\delta d).$$

$$\int_0^1 dx \delta u(x) = \int_0^1 dx \delta d(x) = 0.$$

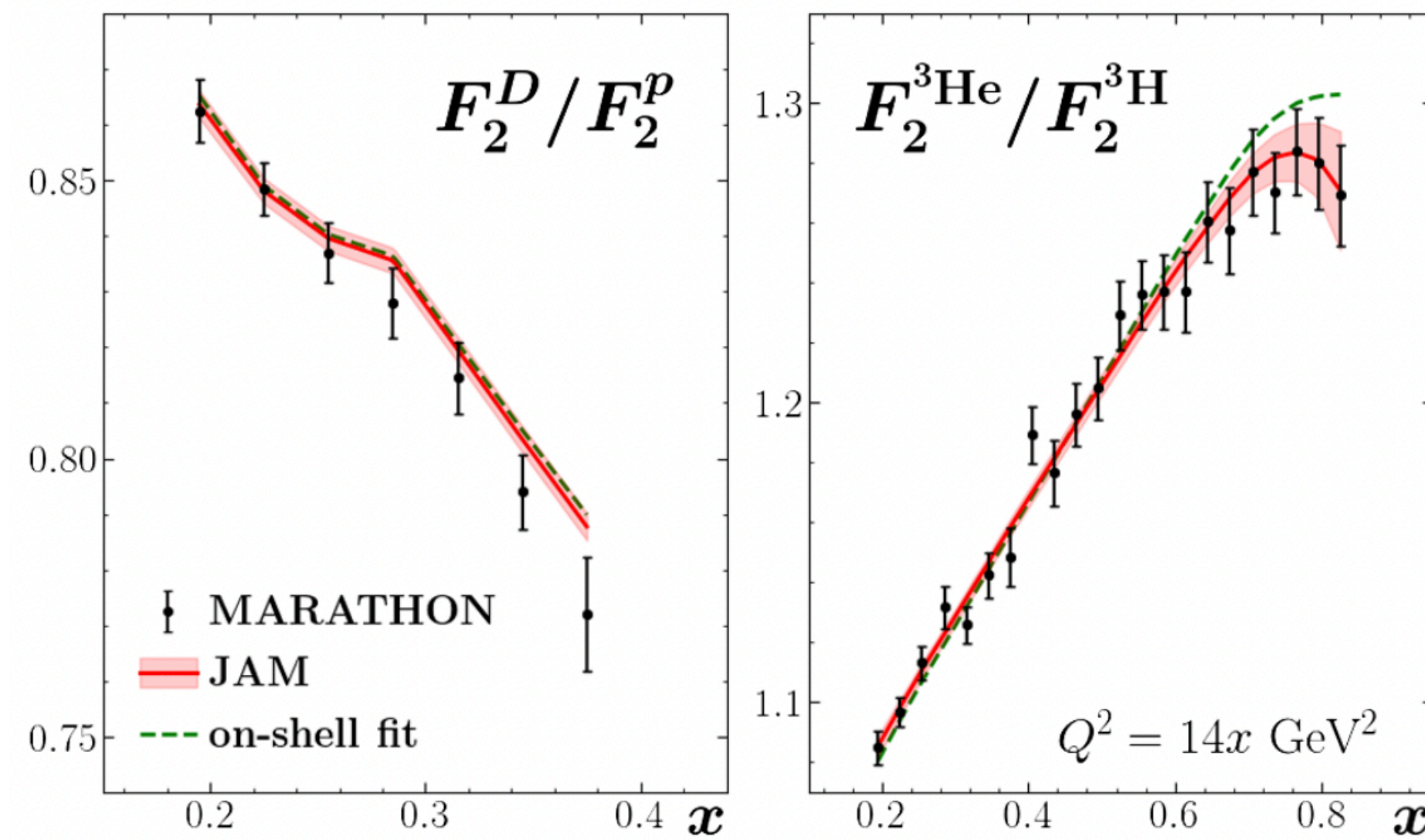
$$f_i(x) = Nx^\alpha(1-x)^\beta(1+\gamma\sqrt{x}+\eta x), \quad \gamma = 0$$



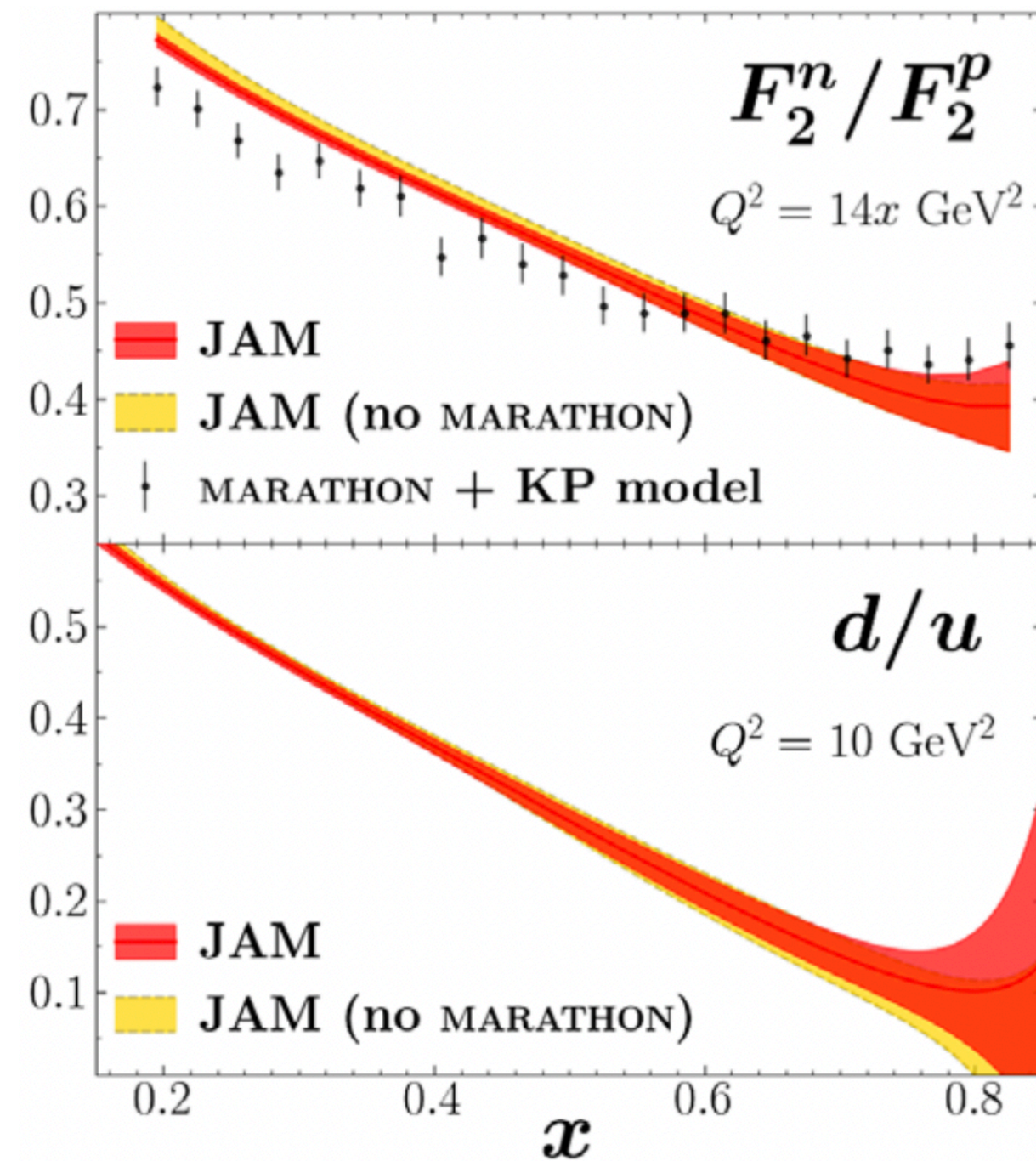


# Results

- It describes the data well



- MARATHON data on PDFs and nucleon structure functions constraints are limited
- 2.5% normalization on  $\sigma(^3\text{He})/\sigma(^3\text{H})$  is transferred to  $\sigma(D)/\sigma(p)$  and absorbed by nuclear effect

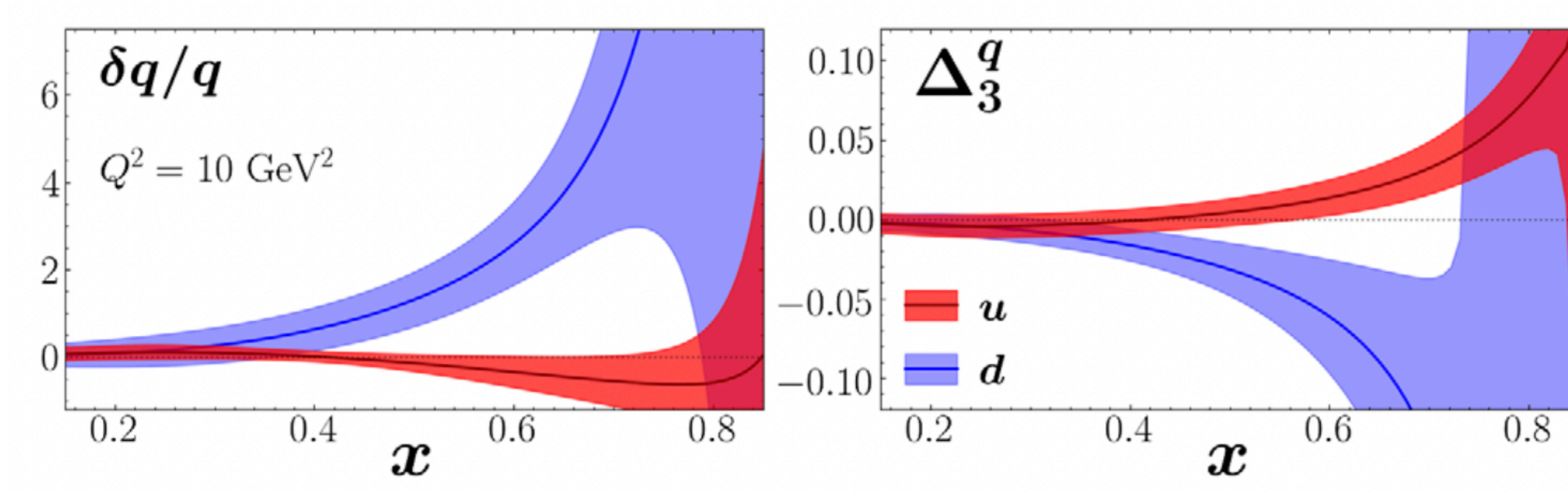


Process	$N_{\text{dat}}$	$\chi^2/N_{\text{dat}}$	Fitted normalization
DIS			
MARATHON $^3\text{He}/^3\text{H}$	22	0.63	1.007(6)
MARATHON $D/p$	7	0.95	1.019(4)
JLab E03-103 $^3\text{He}/D$	16	0.25	1.006(10)



# Off shell corrections results

- It indicates an isovector nuclear effect



$$\Delta_3^q \equiv \frac{q_{p/{}^3\text{H}} - q_{p/{}^3\text{He}}}{q_{p/{}^3\text{H}} + q_{p/{}^3\text{He}}}$$

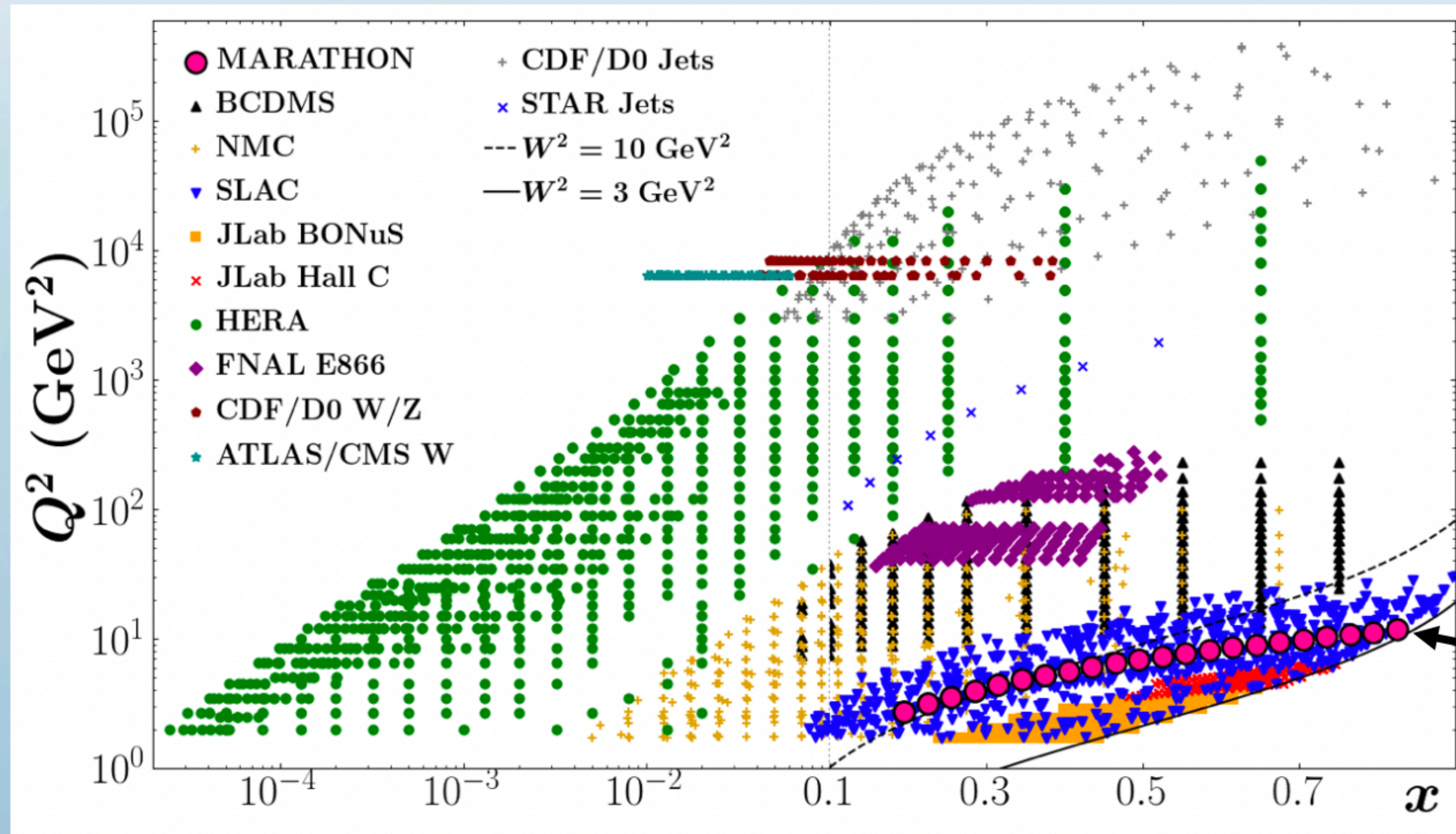
# Conclusions

- A global QC analysis with MARATHON data indicates an isovector EMC effect
- Multiple assumptions are made in the analysis, more experimental data inputs are required to improve the results confidence
- Experimentalists should pay more attention to the normalization factors: normalization factor is at 1% level, while theoretical predictions are at few percent level as well. In order to pin down small effect, we would want to determine the normalization factor better
- Communication between theorists and experimentalists are important, so we can know the underlying tricks we did in each other's analysis...



## Kinematic Coverage

<b>Deep Inelastic Scattering</b>	BCDMS, NMC, SLAC, HERA, Jefferson Lab	3863 points
<b>Drell-Yan</b>	Fermilab E866	250 points
<b>W/Z Boson Production</b>	Tevatron CDF/D0, LHC ATLAS/CMS	239 points
<b>Jets</b>	Tevatron CDF/D0, RHIC STAR	196 points



New MARATHON data