

Near-threshold quarkonium production and the nucleon gravitational form factors

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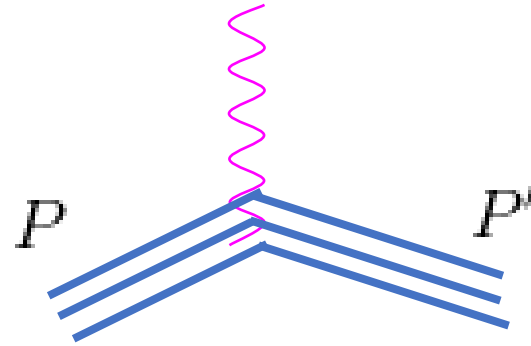
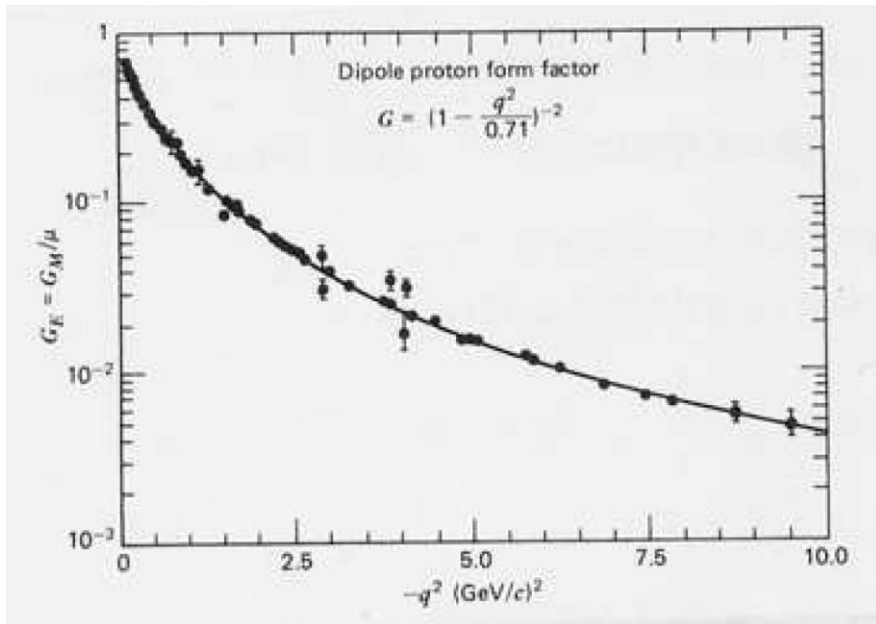
BNL/RIKEN BNL

Contents

- Gravitational form factors
- Quark GFF from DVCS
- Gluon GFF from near-threshold quarkonium production

Proton electromagnetic form factors

$$\langle p', \sigma' | J^\mu | p, \sigma \rangle = \bar{u}_{p', \sigma'} \left[F_1(Q^2) \gamma^\mu + F_2(Q^2) \frac{i\sigma^{\mu\nu} q_\nu}{2m_N} - F_3(Q^2) \frac{\gamma_5 \sigma^{\mu\nu} q_\nu}{2m_N} \right] u_{p, \sigma}$$



PRad (2019)

$$r_p = 0.831 \pm 0.007_{\text{stat}} \pm 0.012_{\text{syst}}$$

Over 70 years of experimental study.
 Charge radius known to percent-level accuracy!



Nucleon gravitational form factors

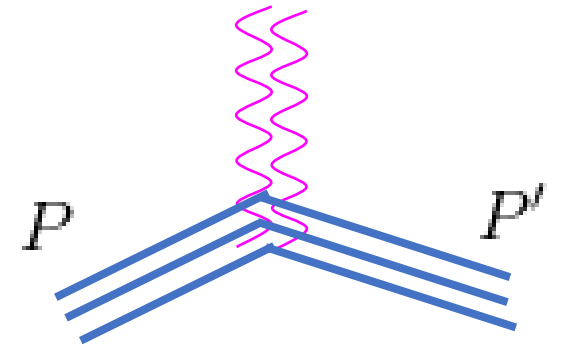
Off-forward matrix element of the QCD energy momentum tensor

$$T^{\mu\nu} = -F^{\mu\alpha} F^{\nu}_{\alpha} + \frac{\eta^{\mu\nu}}{4} F^{\alpha\beta} F_{\alpha\beta} + \bar{\psi} i \gamma^{(\mu} D^{\nu)} \psi$$

$$\langle P' | T^{\mu\nu} | P \rangle = \bar{u}(P') \left[A(t) \gamma^{(\mu} \bar{P}^{\nu)} + B(t) \frac{\bar{P}^{(\mu} i \sigma^{\nu)\alpha} \Delta_{\alpha}}{2M} + D(t) \frac{\Delta^{\mu} \Delta^{\nu} - g^{\mu\nu} \Delta^2}{4M} \right] u(P)$$

Form factors associated with scattering off a **graviton**

Width of GFF \rightarrow **mass radius** of proton



Can we measure these form factors in experiments?

D-term: the last global unknown

$D(t=0)$ is a fundamental conserved charge of the proton

The value, even the sign, is unknown at the moment. No entry in the Particle Data Group.

Spatial components of the energy momentum tensor

→ May be interpreted as radial 'pressure' exerted by quarks and gluons

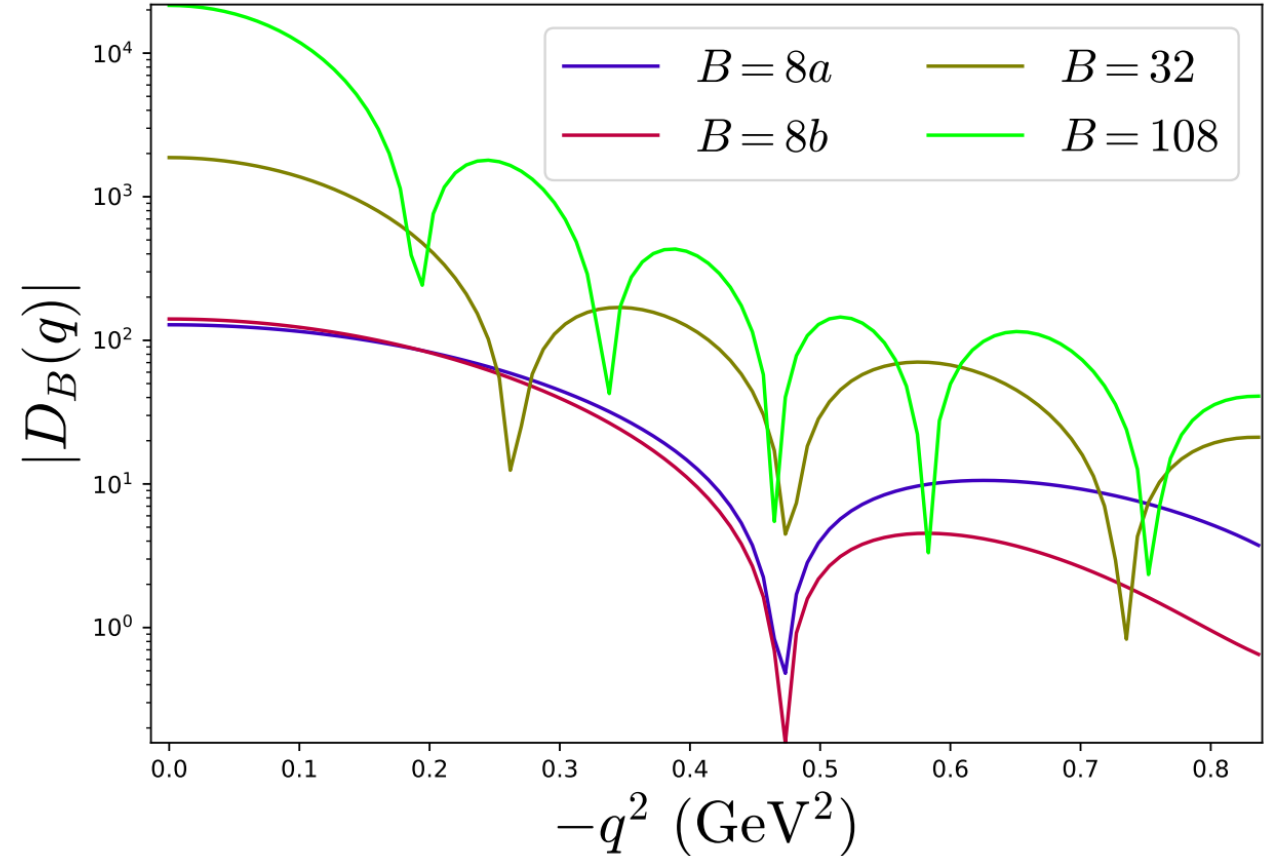
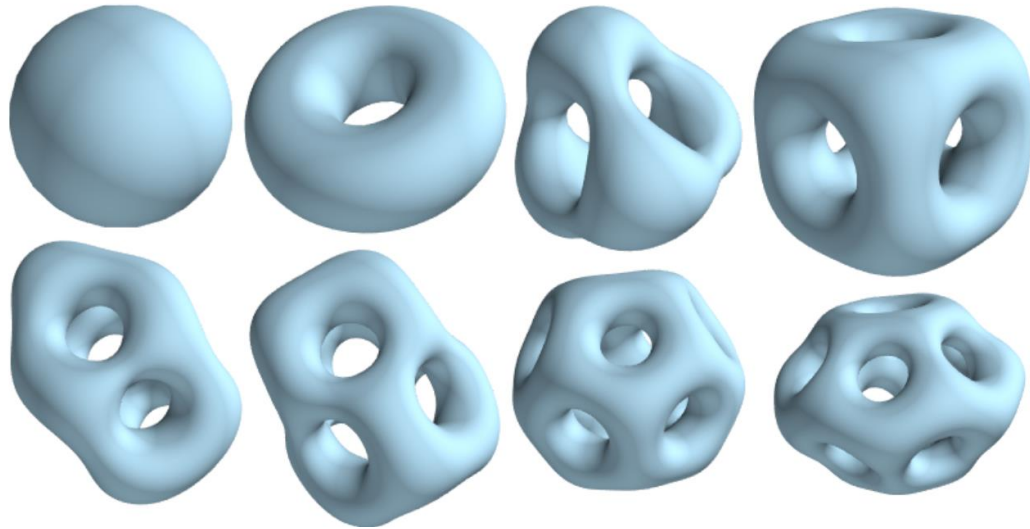
$$T^{ij}(\mathbf{r}) = \left(\frac{r^i r^j}{r^2} - \frac{1}{3} \delta^{ij} \right) s(r) + \delta^{ij} p(r) \quad D = M \int d^3r r^2 p(r)$$

Conjecture: Stable hadrons must have a **negative** D-term $D(t=0) < 0$

D-term of nuclei in the Skyrme model

Martin-Caro, Huidobro, YH, 2304.05994 (preprint today)

Skyrmion solutions known up to $B=108$



Giant D-term for massive nuclei

Form factor resembles the diffractive pattern in elastic scattering

Deeply Virtual Compton Scattering (DVCS)

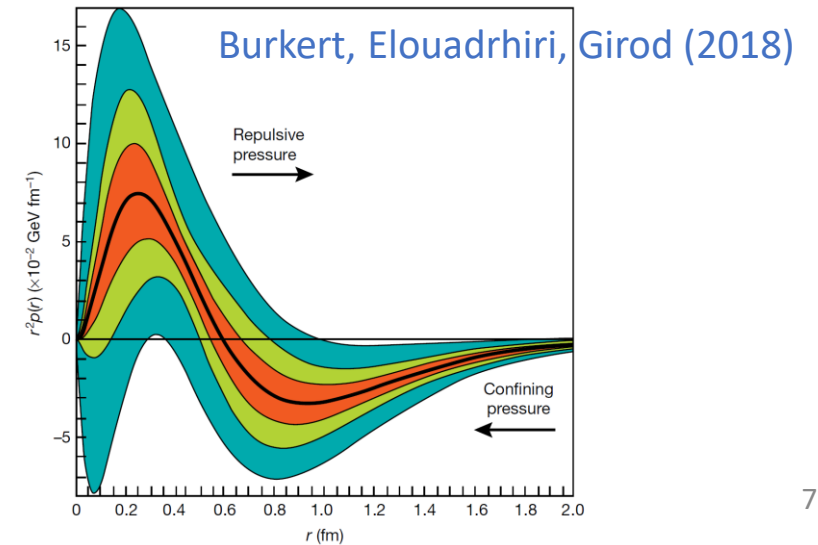
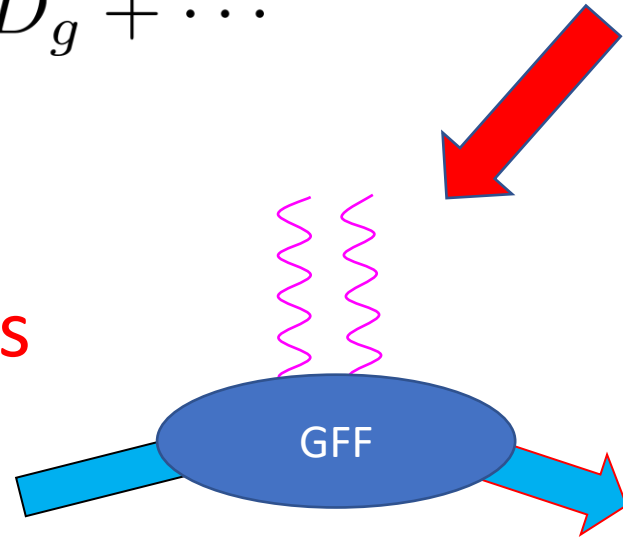
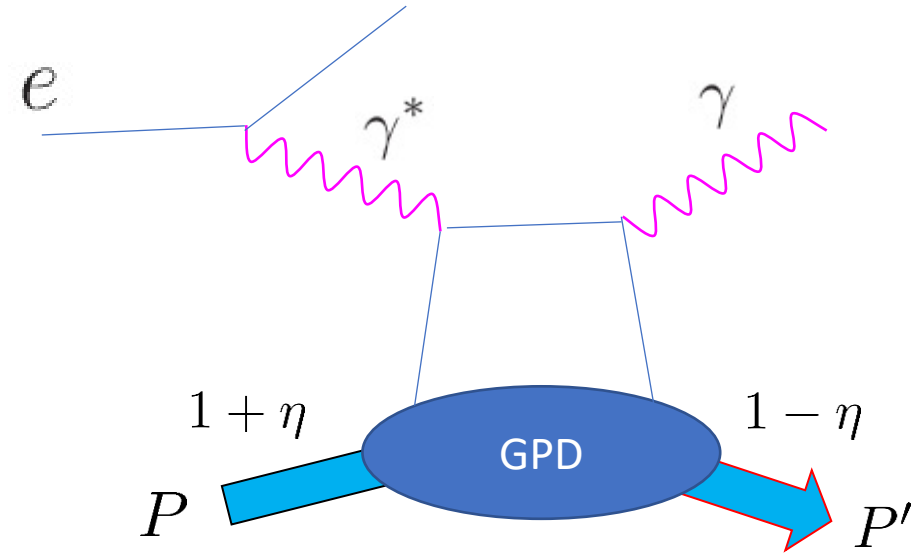
Experimental access to GPDs

Moments of GPDs \rightarrow GFFs

Can access the **quark D-term**?

$$D = D_u + D_d + D_s + D_g + \dots$$

1 graviton \approx 2 photons



Extraction of quark D-term from DVCS

$D_{u,d}$ related to the **subtraction constant** in the dispersion relation for the Compton form factor

Teryaev (2005)

$$\text{Re}\mathcal{H}_q(\xi, t) = \frac{1}{\pi} \int_{-1}^1 dx \text{P} \frac{\text{Im}\mathcal{H}_q(x, t)}{\xi - x} + 2 \int_{-1}^1 dz \frac{D_q(z, t)}{1 - z}$$

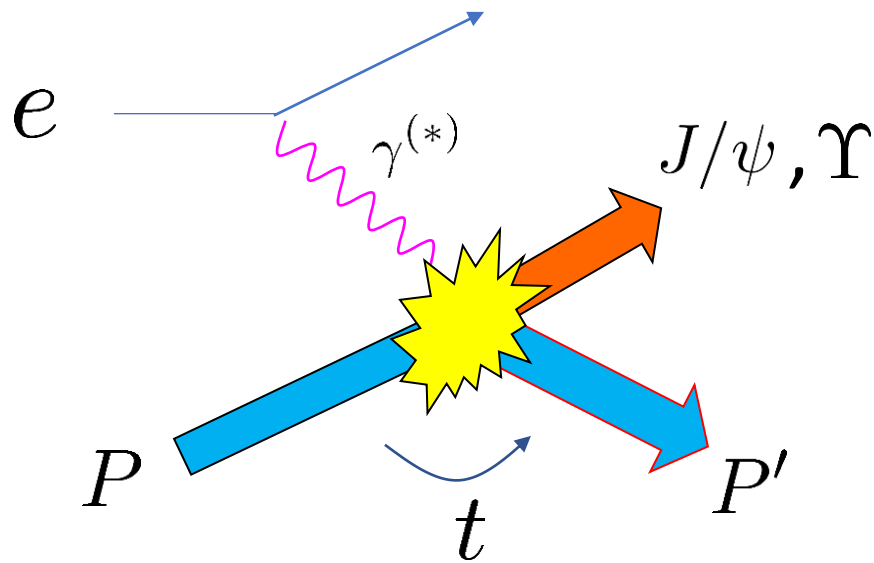
HOWEVER, this is not directly proportional to what we want $\int_{-1}^1 dz z D_q(z, t) = D_q(t)$

The difference is due to twist-2, higher-spin ($j > 2$) operators $\bar{q}\gamma^+(\overleftrightarrow{D}^{\dagger})^{j-1}q$

Two-photon state couples to not just the energy momentum tensor, but infinitely many higher spin operators.

There is no controlled parameter to suppress higher spin contributions.

Quarkonium photo-production near threshold



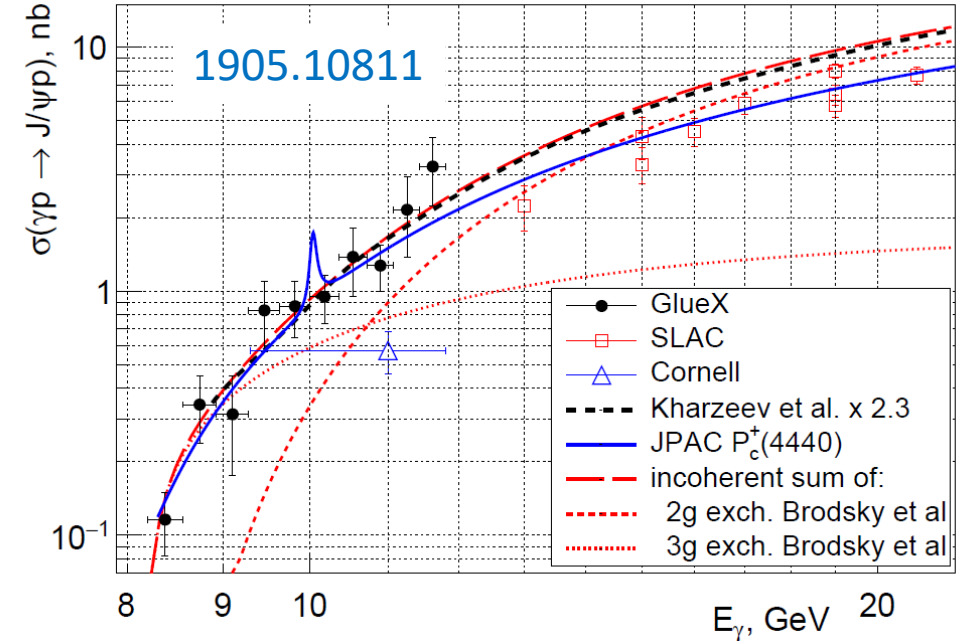
Ongoing experiments at Jlab,
future measurement at EIC, RHIC?

Original motivation:

Insight into the origin of proton mass

Khazzev, et al.(1997)

The process is also sensitive to GFFs, in particular,
the gluon D-term YH, Yang (2018)



Article

Determining the gluonic gravitational form factors of the proton

<https://doi.org/10.1038/s41586-023-05730-4>

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Check for updates

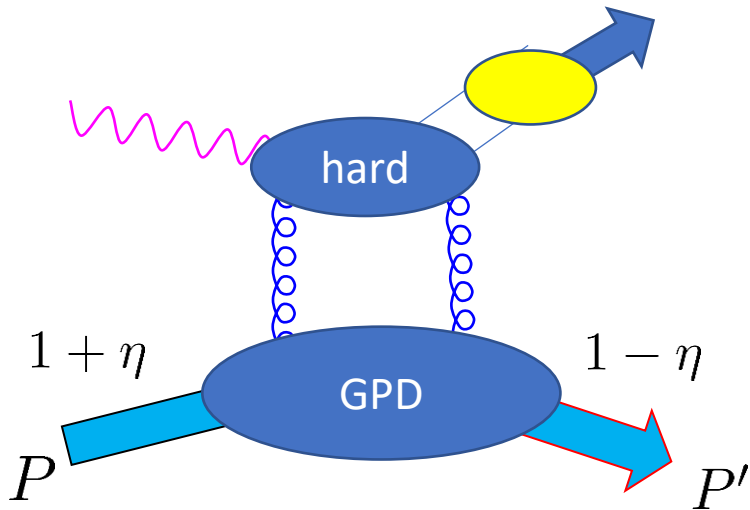
B. Duran^{1,2}, Z.-E. Meziani^{1,2,3}, S. Joosten¹, M. K. Jones³, S. Prasad¹, C. Peng¹, W. Armstrong¹, H. Atac², E. Chudakov³, H. Bhatt⁴, D. Bhetuwal⁴, M. Boer⁵, A. Camsonne³, J.-P. Chen³, M. M. Dalton³, N. Deokar², M. Diefenthaler³, J. Dunne⁴, L. El Fassi⁴, E. Fuchey⁶, H. Gao⁷, D. Gaskell³, O. Hansen², F. Hauenstein⁸, D. Higinbotham³, S. Jia², A. Karki⁴, C. Keppel³, P. King⁹, H. S. Ko¹⁰, X. Li⁷, R. Li², D. Mack³, S. Malace³, M. McCaughan³, R. E. McClellan¹¹, R. Michaels³, D. Meekins³, Michael Paolone², L. Pentchev³, E. Poeser³, A. Puckett⁶, R. Radloff³, M. Rehfuss², P. E. Reimer¹, S. Riordan¹, B. Sawatzky³, A. Smith⁷, N. Sparveris², H. Szumila-Vance³, S. Wood³, J. Xie¹, Z. Ye¹, C. Yero⁸ & Z. Zhao¹

GPD factorization

Light-cone dominance when $Q^2 \rightarrow \infty$ or $M_{QQ} \rightarrow \infty$

GPD factorization at high energy [Collins, Frankfurt, Strikman \(1996\)](#)
[Ivanov, Schafer, Szymanowski, Krasnikov \(2004\)](#)

Assume factorization is valid near the threshold (OK to leading order [Guo, Ji, Liu \(2021\)](#))



Amplitude proportional to **Compton form factor**

$$\int_{-1}^1 \frac{dx}{x} \left(\frac{1}{\eta - x - i\epsilon} - \frac{1}{\eta + x - i\epsilon} \right) H_g(x, \eta, t)$$

Skewness $\eta = \frac{P^+ - P'^+}{P'^+ + P^+}$

Gluon GPD

Connection to GFF?

GPD factorization allows us to study this reaction from first principles.

But it also means that we are dealing with infinitely many twist-2 operators.

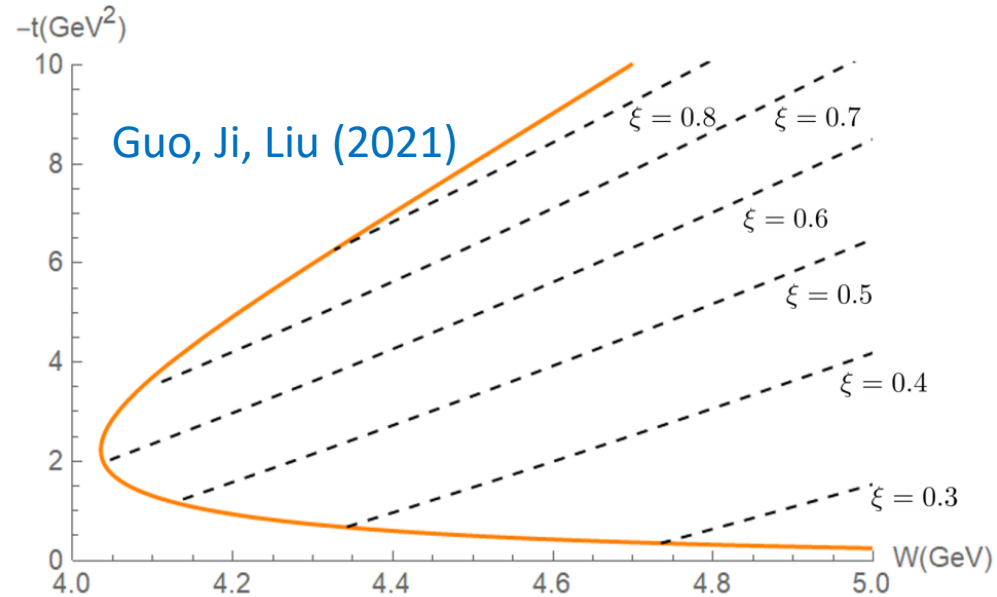
Connection to GFFs unclear. Cogent criticism by [Sun, Tong, Yuan \(2021\)](#)

Clearly, from the above GPD formalism, one can only link to the gluonic gravitational form factors by making approximations of no x -dependence in the pre-factor $\frac{1}{(x+\xi-i\varepsilon)(x-\xi+i\varepsilon)}$ [26, 29]. This is the same as we discussed

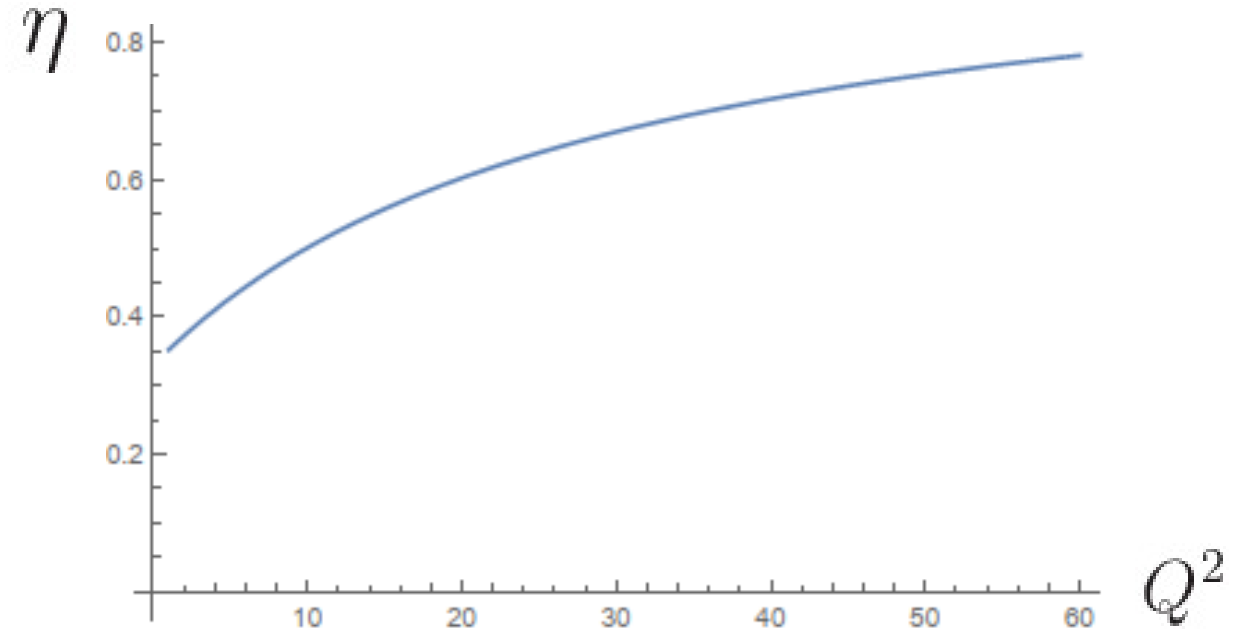
Essentially the same criticism applies to the extraction of the quark D-term in DVCS.

Skewness

J/ψ Photoproduction



Electro-production $|t| \ll Q^2$ $W = 4.5 \text{ GeV}$



Threshold production is characterized by large values of skewness

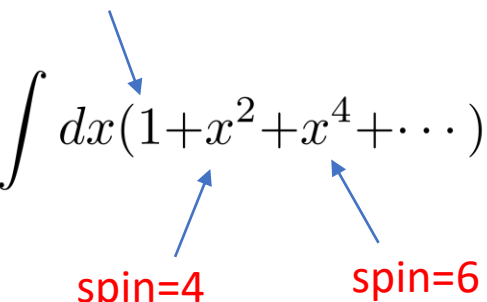
In the ideal limits $Q^2 \rightarrow \infty$ or $m_V \rightarrow \infty$, $\eta \approx 1$

Energy momentum tensor strikes back

If (and only if) $\eta \approx 1$, one can Taylor expand.

$$\frac{1}{1-x} = 1 + x + x^2 + \dots$$

$$\int_{-1}^1 \frac{dx}{x} \left(\frac{1}{\eta - x - i\epsilon} - \frac{1}{\eta + x - i\epsilon} \right) H_g(x, \eta, t) \approx 2 \int dx (1 + x^2 + x^4 + \dots) H_g(x, \eta, t)$$

spin=2 (energy momentum tensor)


Asymptotic form $H_g(x, \eta = 1) \approx (1 - x^2)^2$

all spins $\int dx \frac{H_g(x, \eta = 1, t)}{1 - x^2} \sim \int_0^1 dx \frac{(1 - x^2)^2}{1 - x^2} = \frac{2}{3}$

spin-2 only $\int_0^1 dx (1 - x^2)^2 = \frac{8}{15} \quad \leftarrow \text{80\% of the total}$

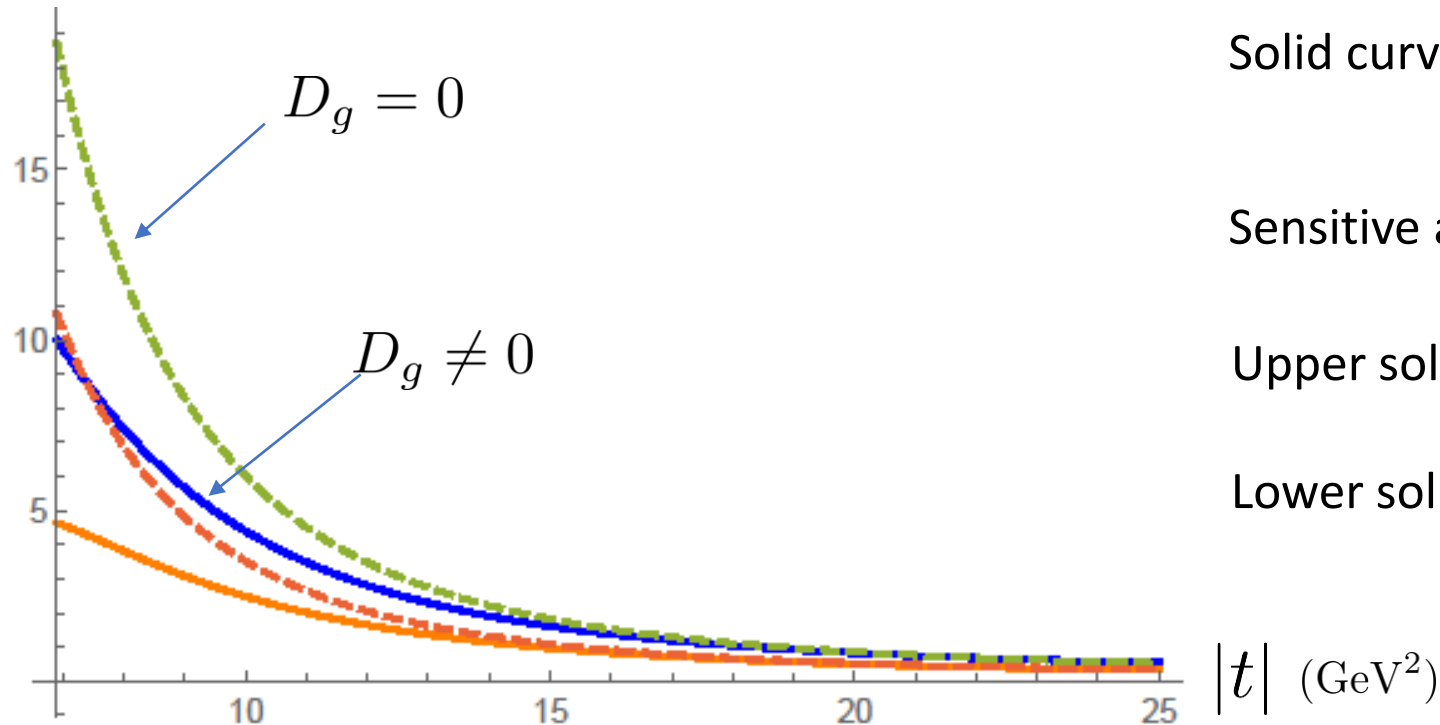
Energy momentum tensor dominates over all the other twist-2 operators combined!

Prediction for the Electron-Ion Collider (EIC)

Boussarie, YH (2020)

$$J/\psi \quad Q^2 = 64 \text{ GeV}^2 \quad \sqrt{S_{ep}} = 20 \text{ GeV} \quad W = 4.4 \text{ GeV}$$

$$\frac{d\sigma}{dt} \text{ (fb/GeV}^2\text{)}$$



Dashed curves: without gluon D-term

Solid curves: with gluon D-term

Sensitive also to the **gluon condensate**

Upper solid $b = 1$

Lower solid $b = 0$

$$\langle P | \frac{\beta}{2g} F^2 | P \rangle = 2M^2(1 - b)$$

Summary

Gravitational form factors and mechanical properties of the proton

→ One of the largely unexplored frontiers of nucleon science,
fits perfectly with the scope of EIC

Quarkonium threshold production at large Q or M_{QQ} is characterized by

1. gluon dominance
2. large skewness

This unique combination allows us to access the gluon gravitational form factors.

Make skewness larger by measuring

{ Υ photo-production,
 J/ψ (maybe ϕ) electro-production at high Q^2