

# Measurements of the $\text{Cos}\phi$ and $\text{Cos}2\phi$ Moments of the Unpolarized SIDIS $\pi^+$ Cross-section at CLAS12

Richard Capobianco

University of Connecticut

Presentation for the APS meetings

LinkedIn



# Motivation

- Semi-Inclusive Deep Inelastic Scattering (SIDIS) experiments allow us to address questions about the 3D structure of nucleons
- Azimuthal modulations in unpolarized SIDIS cross-section for charged pion electroproduction can give access to the Cahn and Boer-Mulders effects
  - **Boer-Mulders Effect:** Sensitive to the correlation between the quark's transverse momentum and intrinsic transverse spin in an unpolarized nucleon
  - **Cahn Effect:** Sensitive to the transverse motion of quarks inside the nucleon
- A non-zero Boer-Mulders requires quark orbital angular momentum contributions to the proton spin (aspect of the proton missing spin puzzle)

# SIDIS Cross-Section and Boer-Mulders

The lepton-hadron Unpolarized SIDIS Cross-Section:

$$\frac{d^5\sigma}{dx dQ^2 dz d\phi_h dP_{h\perp}^2} = \underbrace{\frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) (F_{UU,T} + \epsilon F_{UU,L})}_{A_0} \left\{ 1 + \underbrace{\frac{\sqrt{2\epsilon(1+\epsilon)} F_{UU}^{\cos\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos\phi_h}} \cos\phi_h + \underbrace{\frac{\epsilon F_{UU}^{\cos 2\phi_h}}{(F_{UU,T} + \epsilon F_{UU,L})}}_{A_{UU}^{\cos 2\phi_h}} \cos 2\phi_h \right\}$$

The Boer-Mulders and Cahn effects are present in the Structure Functions:

leading twist

$$F_{UU}^{\cos 2\phi_h} \propto C \left[ \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{M M_h} h_1^\perp H_1^\perp + \dots \right]$$

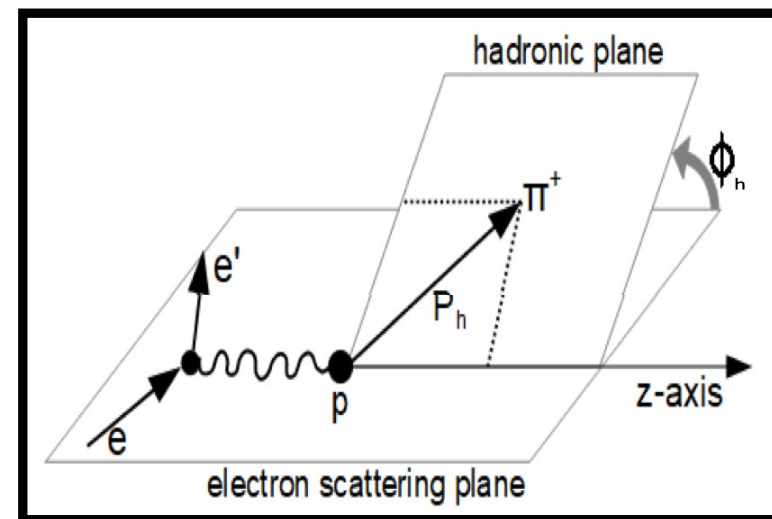
BOER-MULDERS EFFECT

CAHN EFFECT

Interaction dependent terms neglected

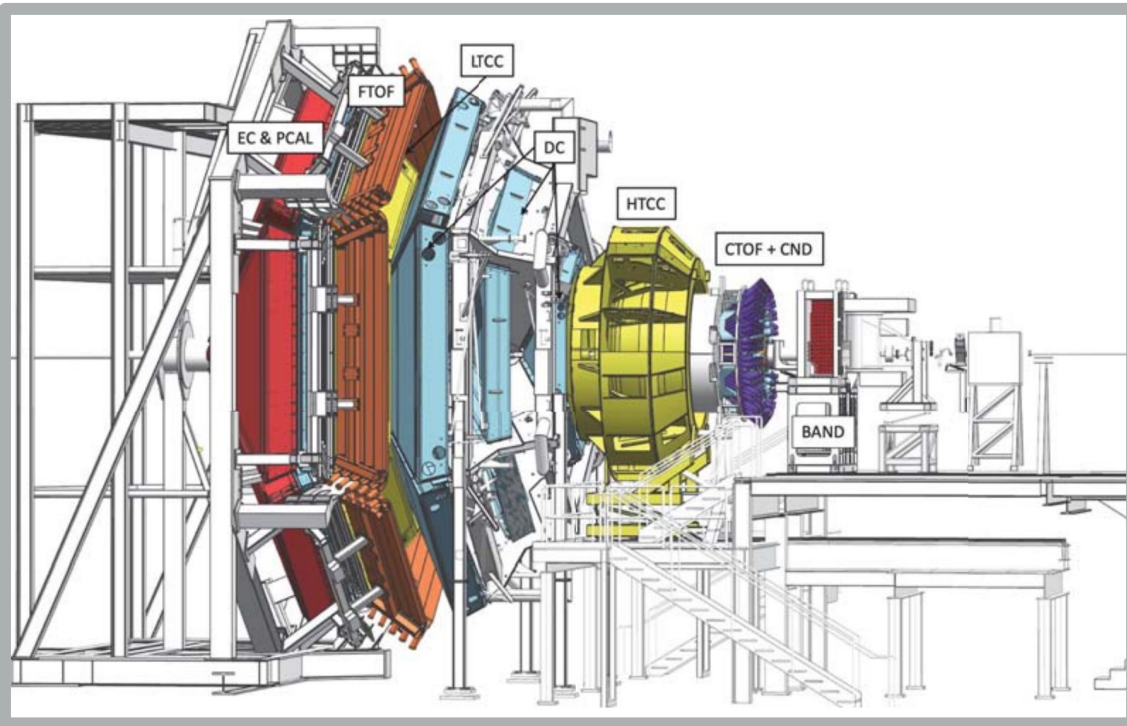
next to leading twist

$$F_{UU}^{\cos\phi_h} \propto \frac{2M}{Q} C \left[ \frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} x h H_1^\perp - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1 + \dots \right]$$



Reaction Studied:  $e p \rightarrow e \pi^+(X)$

# Data Collection



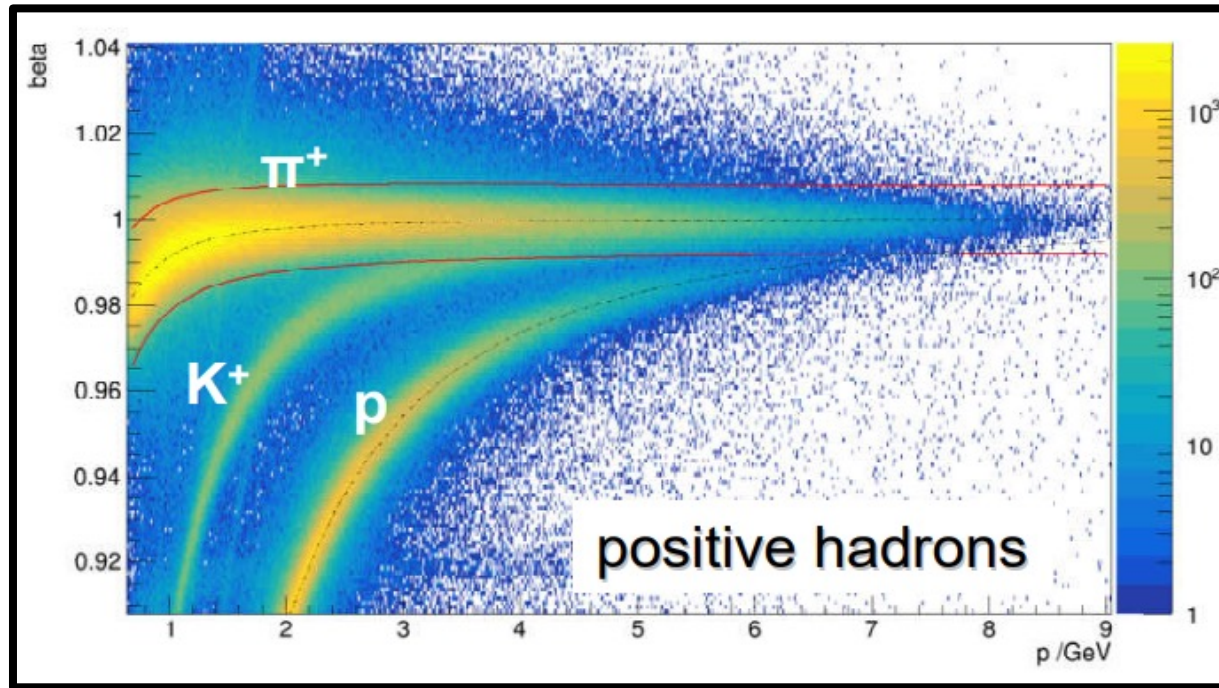
CLAS12 Detector

- CLAS12 detector in Hall B at Jefferson Lab
  - Upgrade from the CLAS detector
  - Enabled the higher energy and statistics for our experiments, not previously accessible
- Data from the Fall 2018 RG-A experiment
  - Used a 10.6 GeV polarized electron beam and unpolarized liquid hydrogen target
- Data presented uses forward tracking only

# Event Selection

## Particle ID (PID):

- **Electron ID:** Based on Electromagnetic Calorimeter (PCAL) and Cherenkov Counters (HTCC)
- **Hadron ( $\pi^+$ ) ID:** Based on Time-Of-Flight Counters (TOF) and the correlation of velocity ( $\beta$ ) and momentum



\*Image provided by Stefan Diehl

$\pi^+$  Pion PID –  $\beta$  vs  $p$

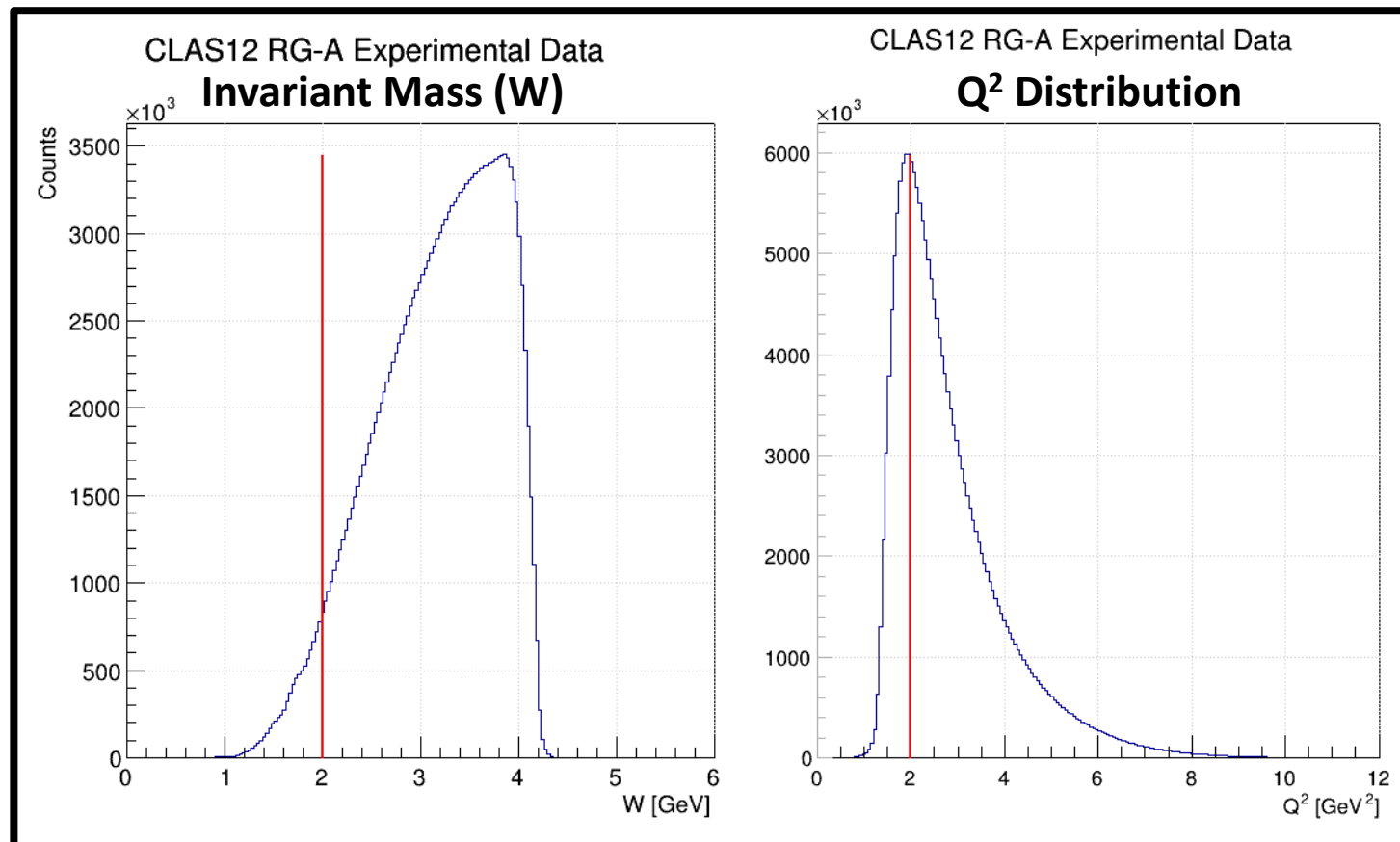
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## Analysis Cuts:

- **SIDIS Cuts:**
  - $W > 2 \text{ GeV}$
  - $Q^2 > 2 \text{ GeV}^2$



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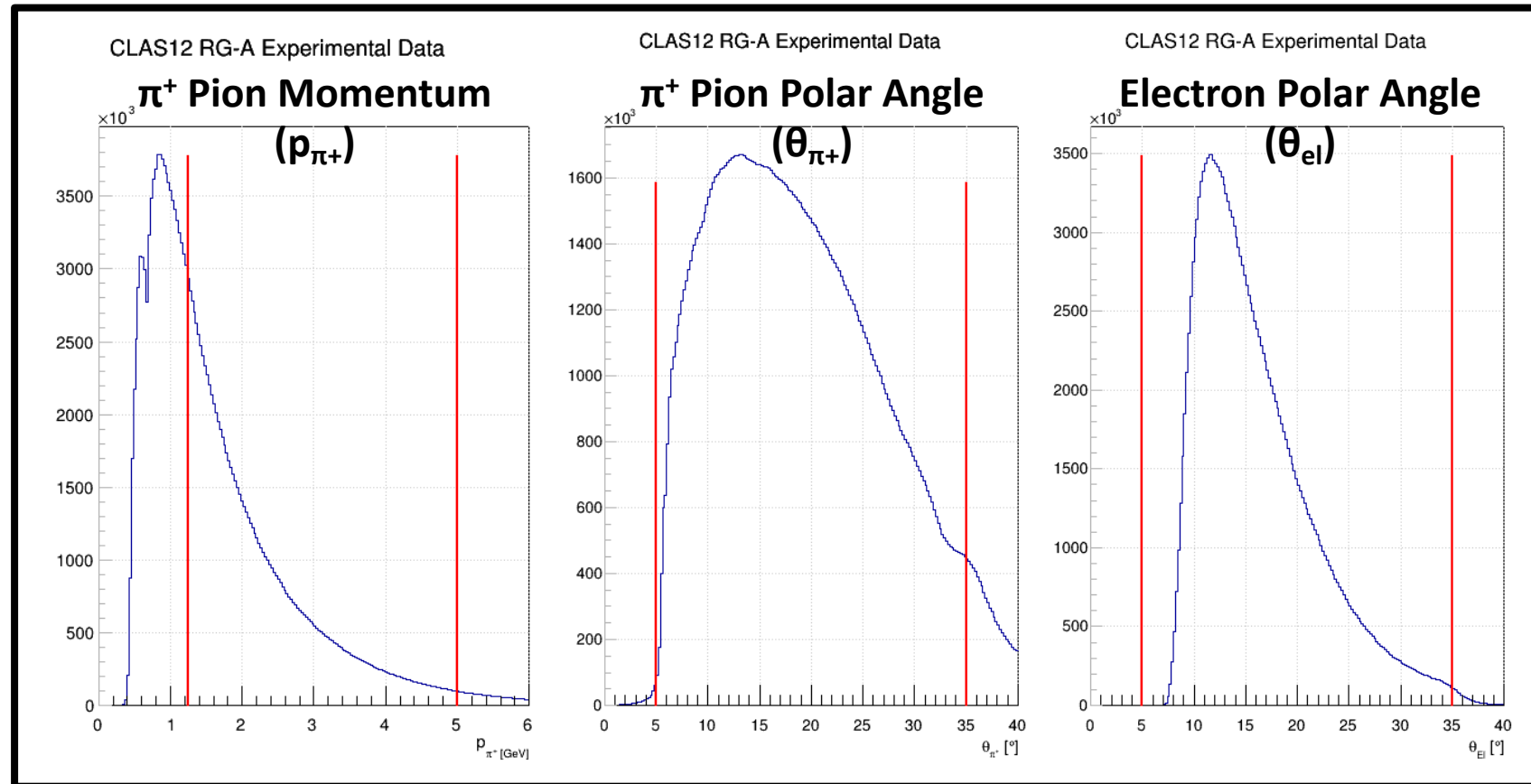
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- **Other Analysis Cuts:**

- $p_{\pi^+}$  Cut:  $1.25 \text{ GeV} < p_{\pi^+} < 5 \text{ GeV}$
- $\theta$ -angle Cut:  $5^\circ < \theta_{\text{particle}} < 35^\circ$



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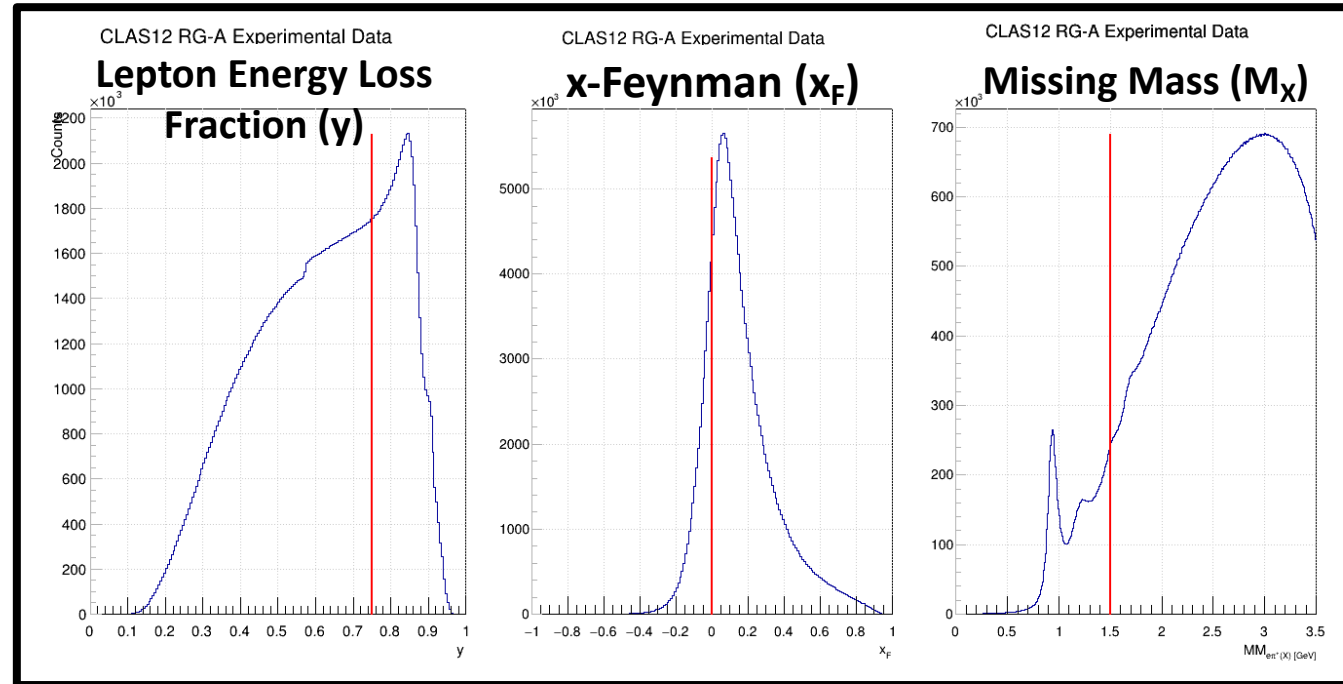
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- $y < 0.75$  (minimize other background processes)
- $x_F > 0$  (minimize contributions from target fragmentations)
- Missing Mass Cut:  $M_X > 1.5 \text{ GeV}$  (limits contributions from exclusive events)





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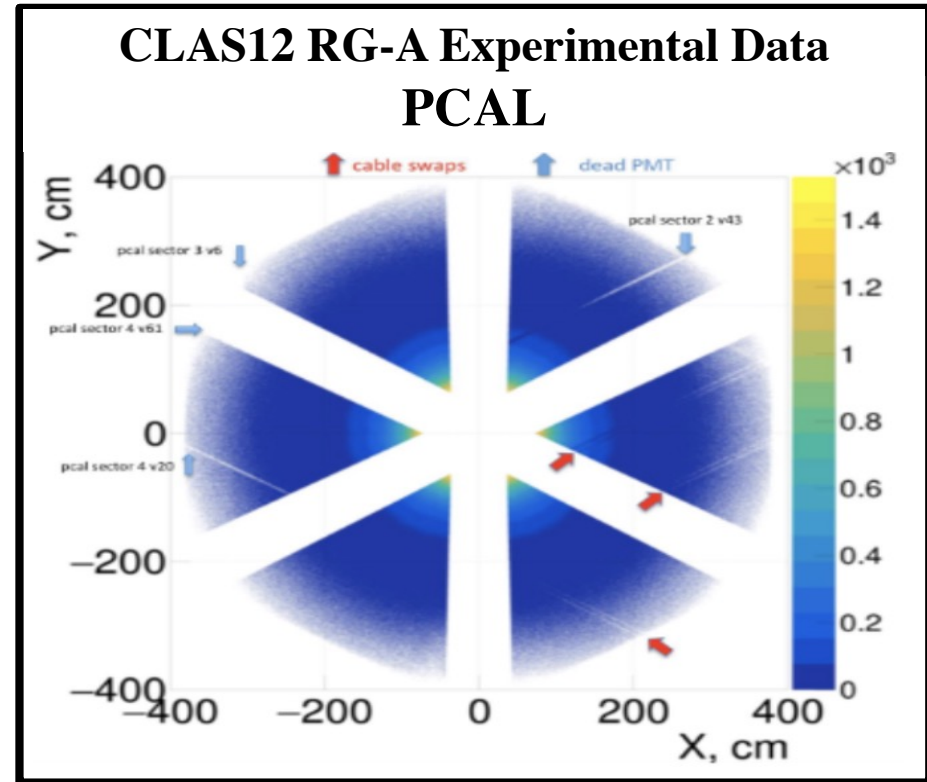
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- Missing Mass Cut:  $M_x > 1.5 \text{ GeV}$  (limits contributions from exclusive events)
- Fiducial Cuts (e.g., accounts for bad channels present in data)



# Analysis Procedure

## Experimental extraction of cross-section

$$\frac{d^5\sigma}{dQ^2 dx_B dP_T dz d\varphi_h} = \frac{1}{(\Delta Q^2 \Delta x_B \Delta P_T \Delta z \Delta \varphi_h)} \frac{N}{R \cdot BC \cdot \eta \cdot N_0} \frac{1}{(N_A \cdot \rho \cdot t / A_w)}$$

Where:

Bin Volume

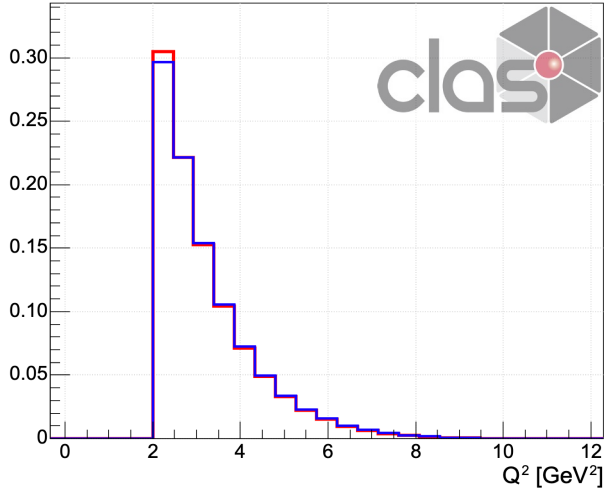
Target Number Density

- R = Radiative Correction
- $\eta$  = **Acceptance Correction** → Requires Monte Carlo (MC) Simulation
- N = Bin Yields
- $N_0$  = Life-time corrected incident electron flux
- BC = factor which evolves bin-averaged differential cross-section

SIDIS MC are generated with LEPTO event generator

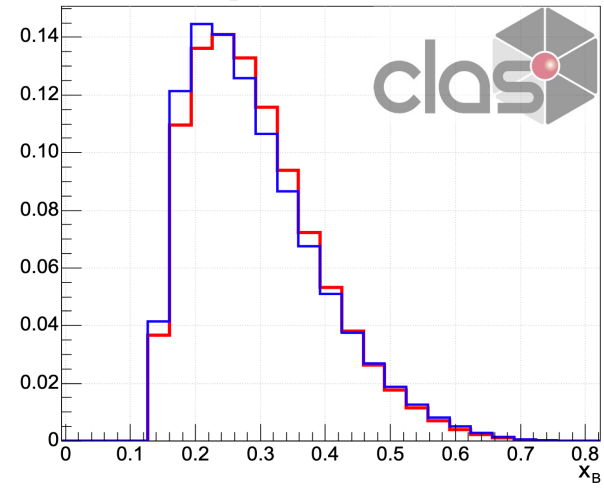
# Data and Monte Carlo Comparison

Normalized Comparison of **Data** and **Simulated**  $Q^2$



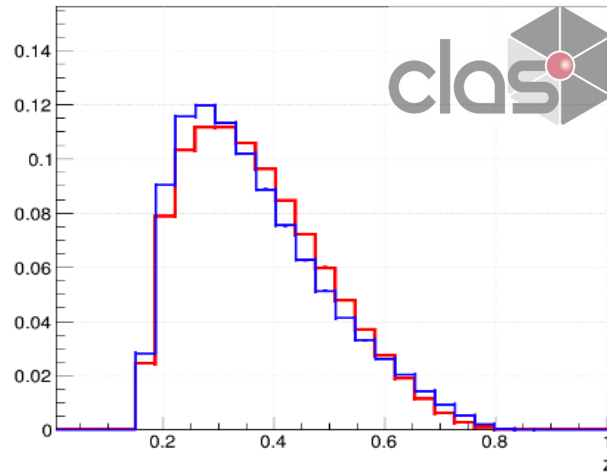
$Q^2$  Comparison

Normalized Comparison of **Data** and **Simulated**  $x_B$



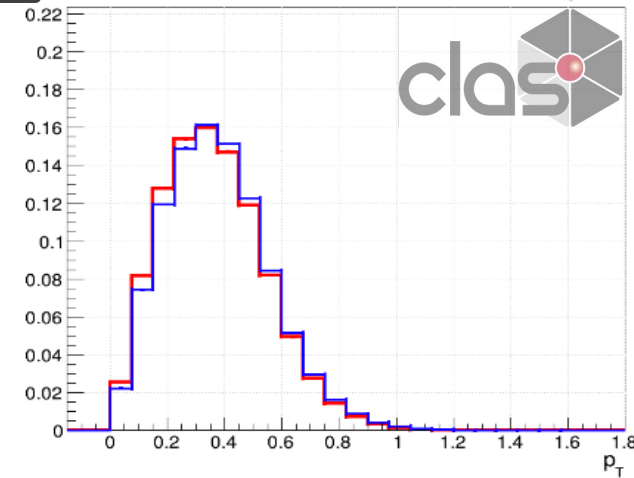
$x_B$  Comparison

Normalized Comparison of **Real** and **Simulated**  $z$



$z$  Comparison

Normalized Comparison of **Real** and **Simulated**  $p_T$



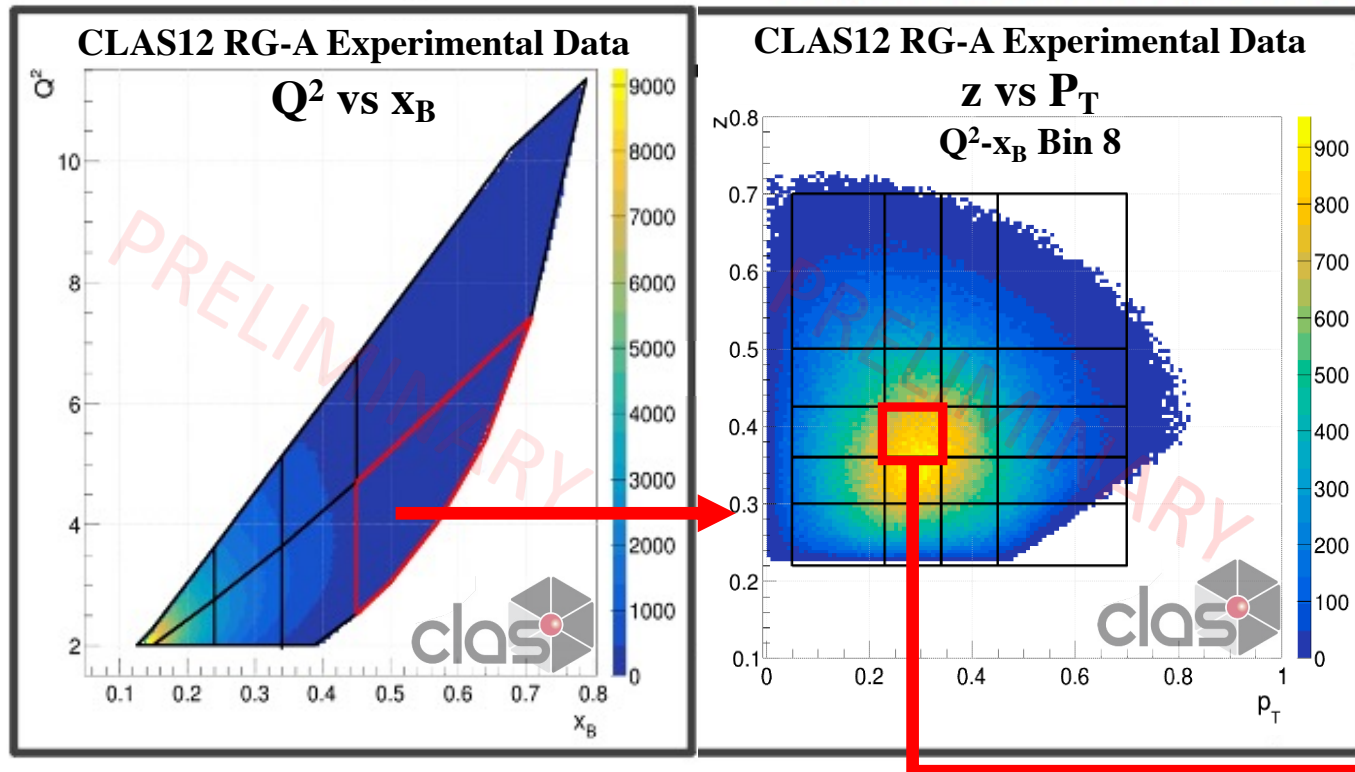
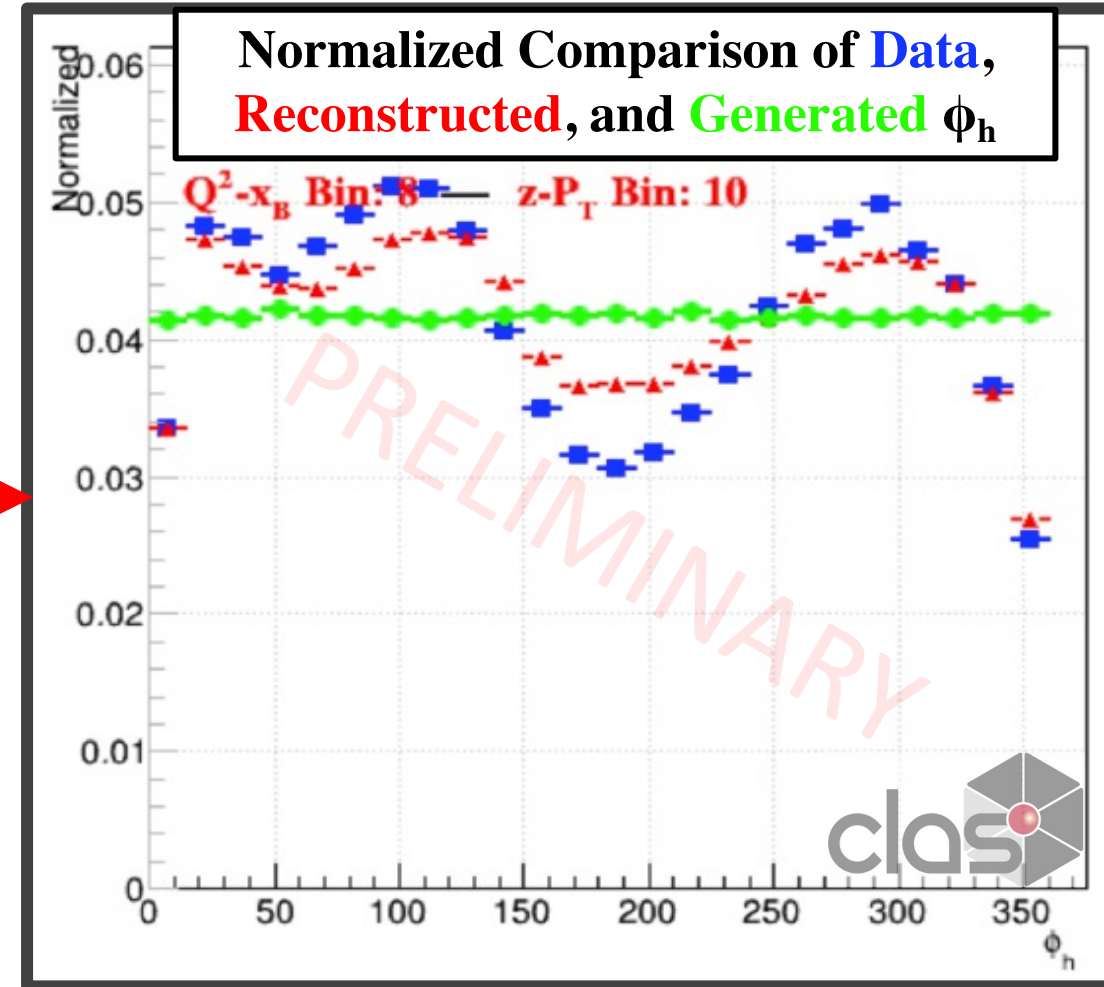
$p_T$  Comparison

# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (5 Dimensions)

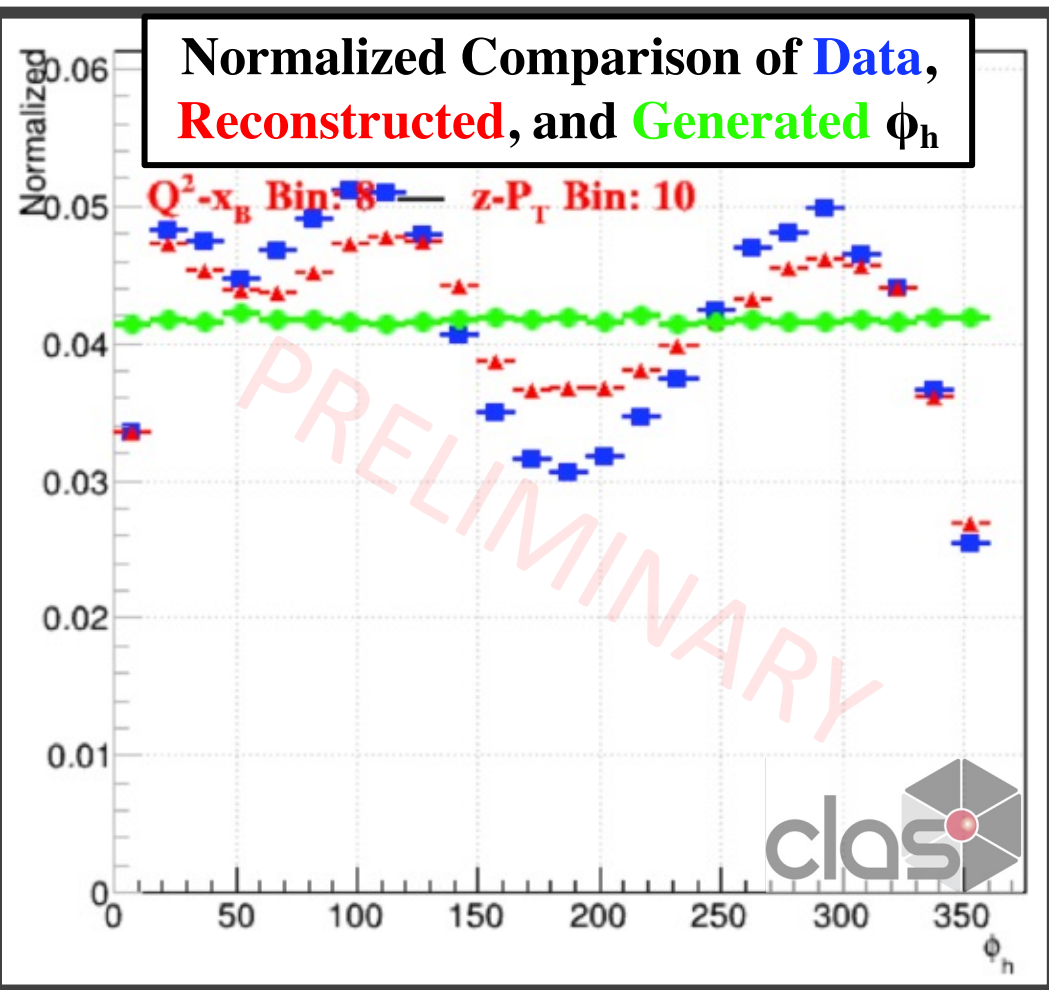
8  $Q^2-x_B$  Bins Total – 20-49  $z-P_T$  Bins (per  $Q^2-x_B$  bin)

$\phi_h$  distribution for the  $Q^2-x_B-z-P_T$  bin shown in red



# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (5 Dimensions)



Apply  
Multidimensional  
Acceptance  
Corrections and  
convert to a  
cross-section  
measurement

$\phi_h$  fit for  
every bin

$A(1 + B \cos(\phi_h) + C \cos(2\phi_h))$   
Where the parameters A, B, C  
give the cross-section moments

$$A_{UU}^{\cos \phi_h} = B \quad A_{UU}^{\cos 2\phi_h} = C$$

### Methods used for Acceptance Corrections:

- **Bin-by-bin Correction**
  - Simple method which just needs the 1D plots shown here
- **(SVD) Singular Value Decomposition**
- **Bayesian Unfolding**
  - Both the SVD and Bayesian Unfolding Methods use Acceptance Matrices to correct the data

# Acceptance Corrections and Bin Migration Study

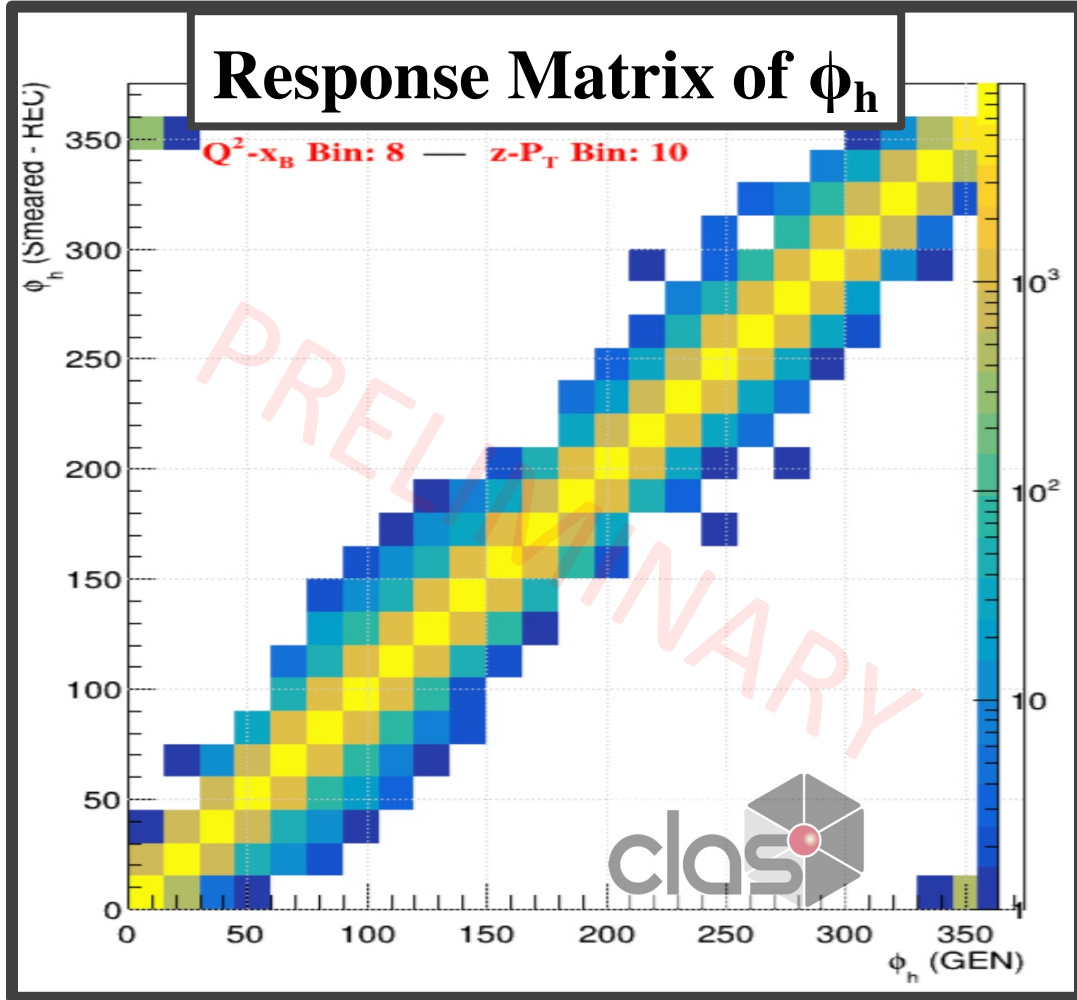
- **Acceptance Matrix:**  $A_{(i,j)}$  describes both Acceptance (including geometric acceptance and detector efficiency) and Bin Migration
- $A_{(i,j)} = \frac{\text{Number of Events Generated in bin } j \text{ but Reconstructed in bin } i}{\text{Total Number of Events Generated in the } j\text{th bin}}$
- Acceptance Unfolding:  $Y_i = A_{(i,j)}X_j \Leftrightarrow X_j = A_{(i,j)}^{-1}Y_i$

where:

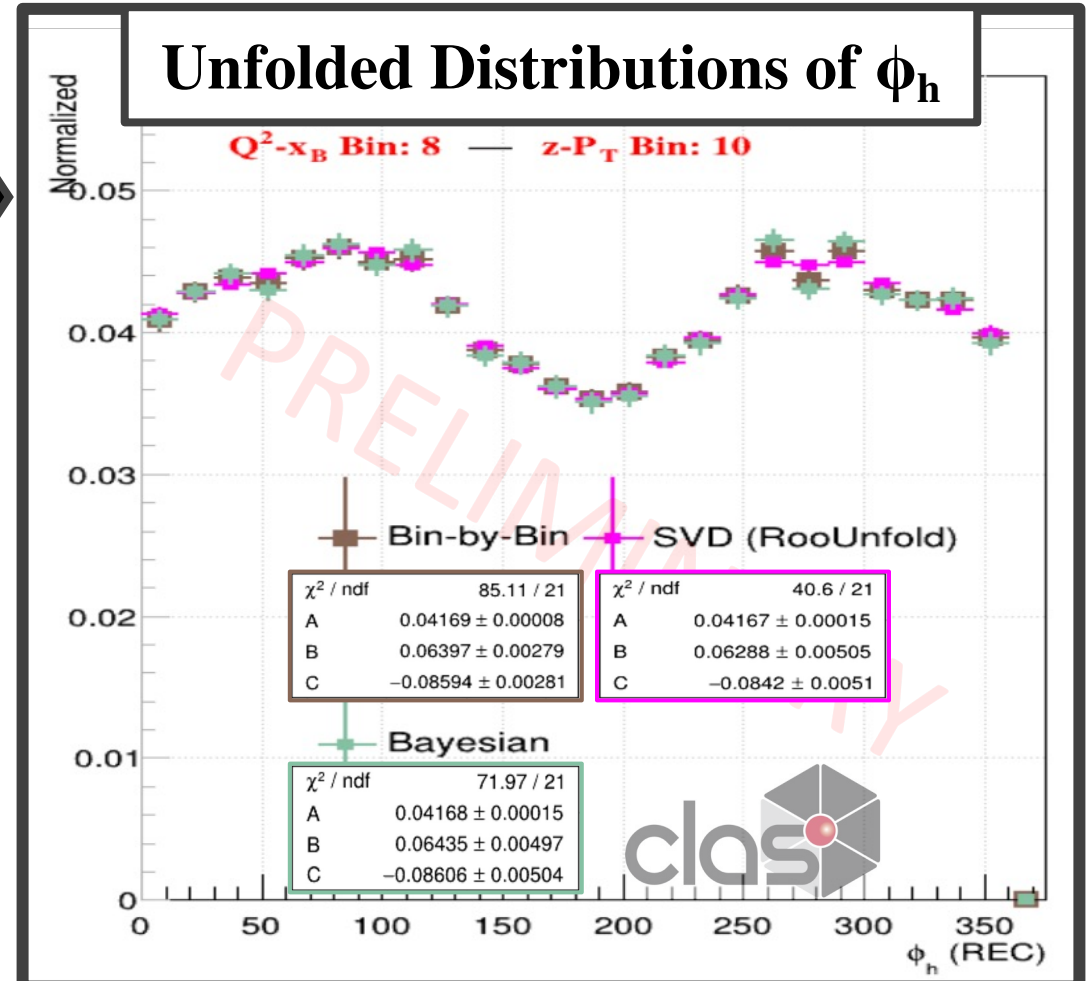
- $Y_i$  = Number of events experimentally measured in the  $i$ -th bin
- $X_j$  = Number of acceptance-corrected events in the  $j$ -th bin

# Example of Unfolding Procedure

Using the Multidimensional Kinematic Bin from prior example



Unfolding Procedures



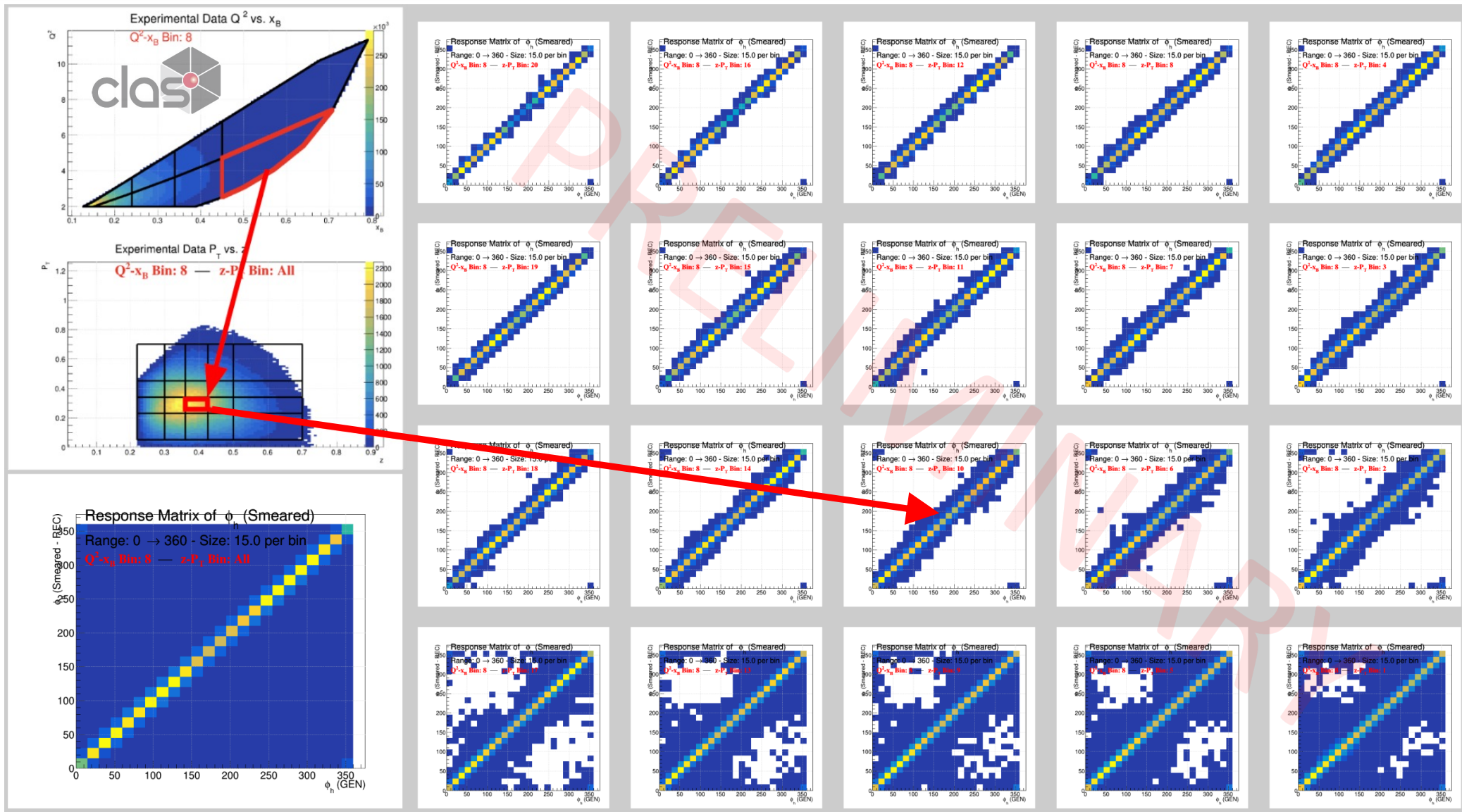
Parameters shown are from the fits previously described

# Multiple Examples of the Unfolding Procedure

## Response Matrices

in each  $z$ - $P_T$  bin for the highlighted  $Q^2$ - $x_B$  bin

Arrows point to the distribution used in prior examples

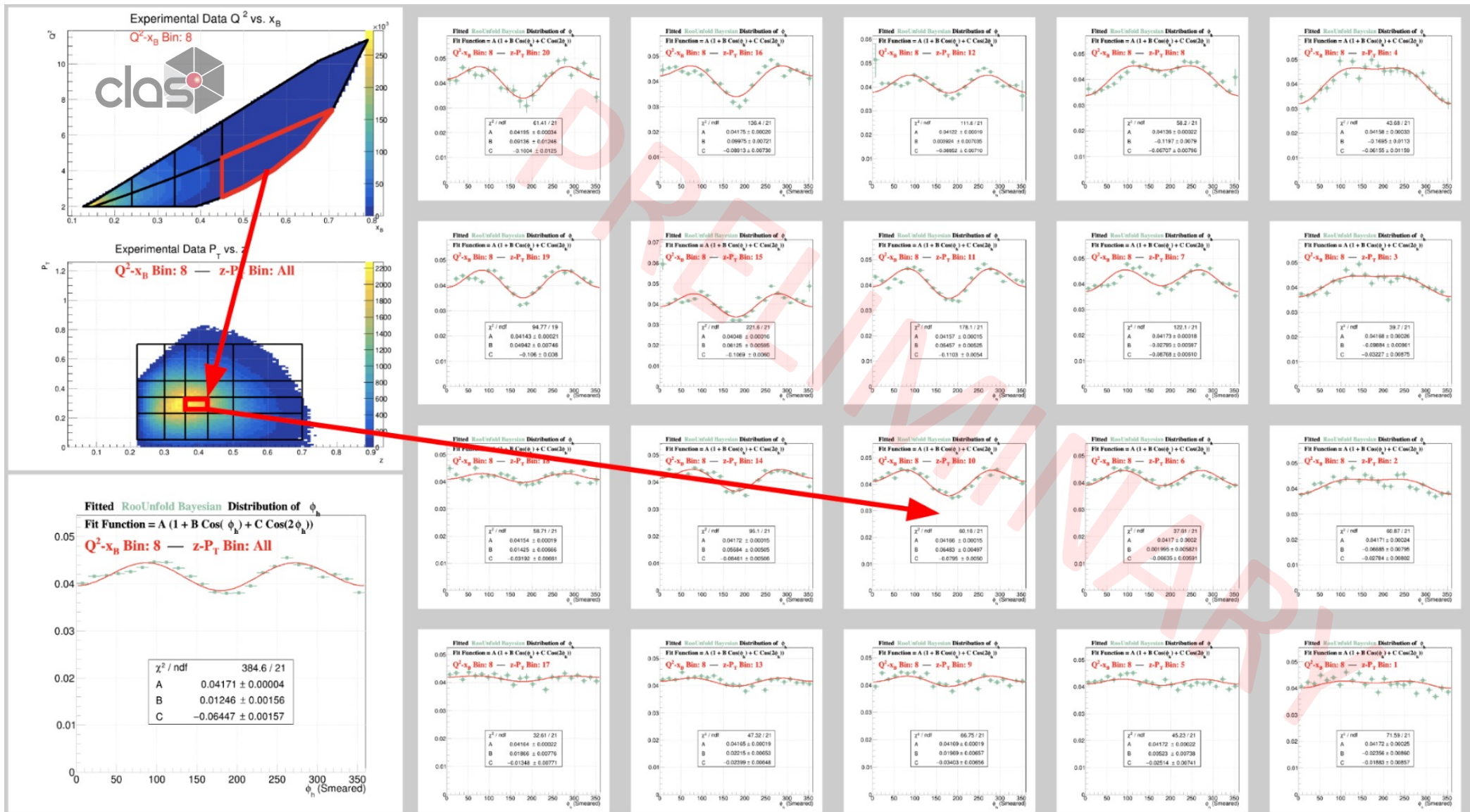




# Multiple Examples of the Unfolding Procedure

**Bayesian Unfolding**  
in each  $z$ - $P_T$  bin for  
the highlighted  
 $Q^2$ - $x_B$  bin

Arrows point to the  
distribution used in  
prior examples



# Outlook

- Working on Multidimensional Acceptance Corrections for the simultaneous unfolding of  $Q^2$ ,  $x_B$ ,  $z$ ,  $P_T$ , and  $\phi_h$  variables
- Efforts towards more realistic MC simulations, both on the detector response description and physics process
- Include Radiative and BC Corrections to analysis
- Long-term goals:
  - Extraction of multiplicity ( $F_{UU,T} + \epsilon F_{UU,L}$ ),  $F_{UU}^{\cos \phi_h}$ , and  $F_{UU}^{\cos 2\phi_h}$  in terms of in  $Q^2$ ,  $x_B$ ,  $z$ , and  $P_T$  for the  $\pi^+$  for all CLAS12 RG-A data

# Thank you

## Questions?

### Acknowledgements

- Financial support from The Gordon and Betty Moore Foundation and the American Physical Society to present this work at the GHP 2023 workshop
- Contributions made by other members of the CLAS Collaboration
- This work is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics under contract number DE-AC02-06CH11357

# Backup Slides

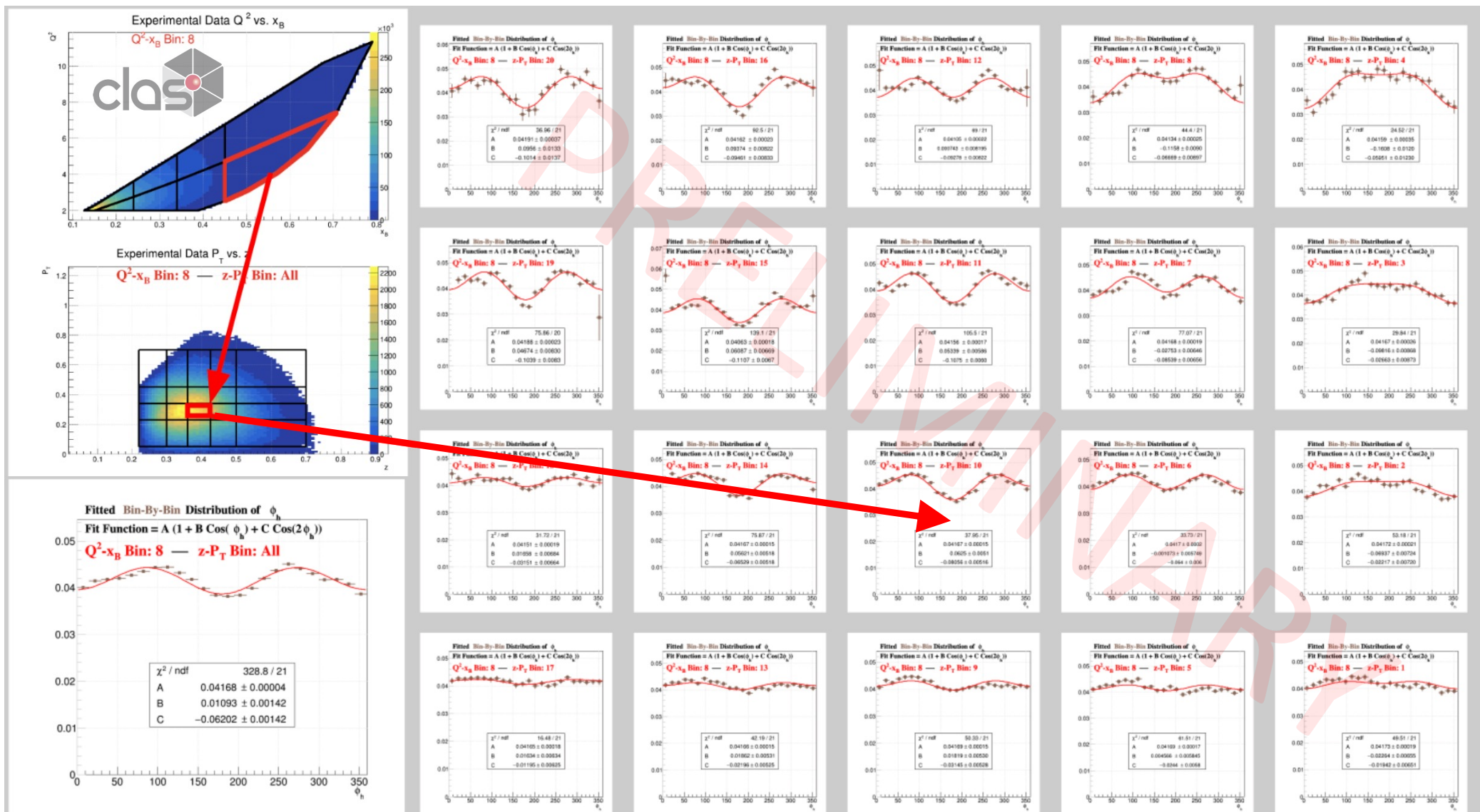
# Multiple Examples of the Unfolding Procedure

[https://userweb.jlab.org/~richcap/Interactive Webpage SIDIS richcap/Interactive Unfolding Page.html](https://userweb.jlab.org/~richcap/Interactive%20Webpage%20SIDIS%20richcap/Interactive%20Unfolding%20Page.html)

## Bin-by-bin Correction

in each  $z$ - $P_T$  bin for the highlighted  $Q^2$ - $x_B$  bin

Arrows point to the distribution used in prior examples



These images are also available at the web address linked above

# Multiple Examples of the Unfolding Procedure

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## SVD Unfolding

in each  $z$ - $P_T$  bin for the highlighted  $Q^2$ - $x_B$  bin

Arrows point to the distribution used in prior examples

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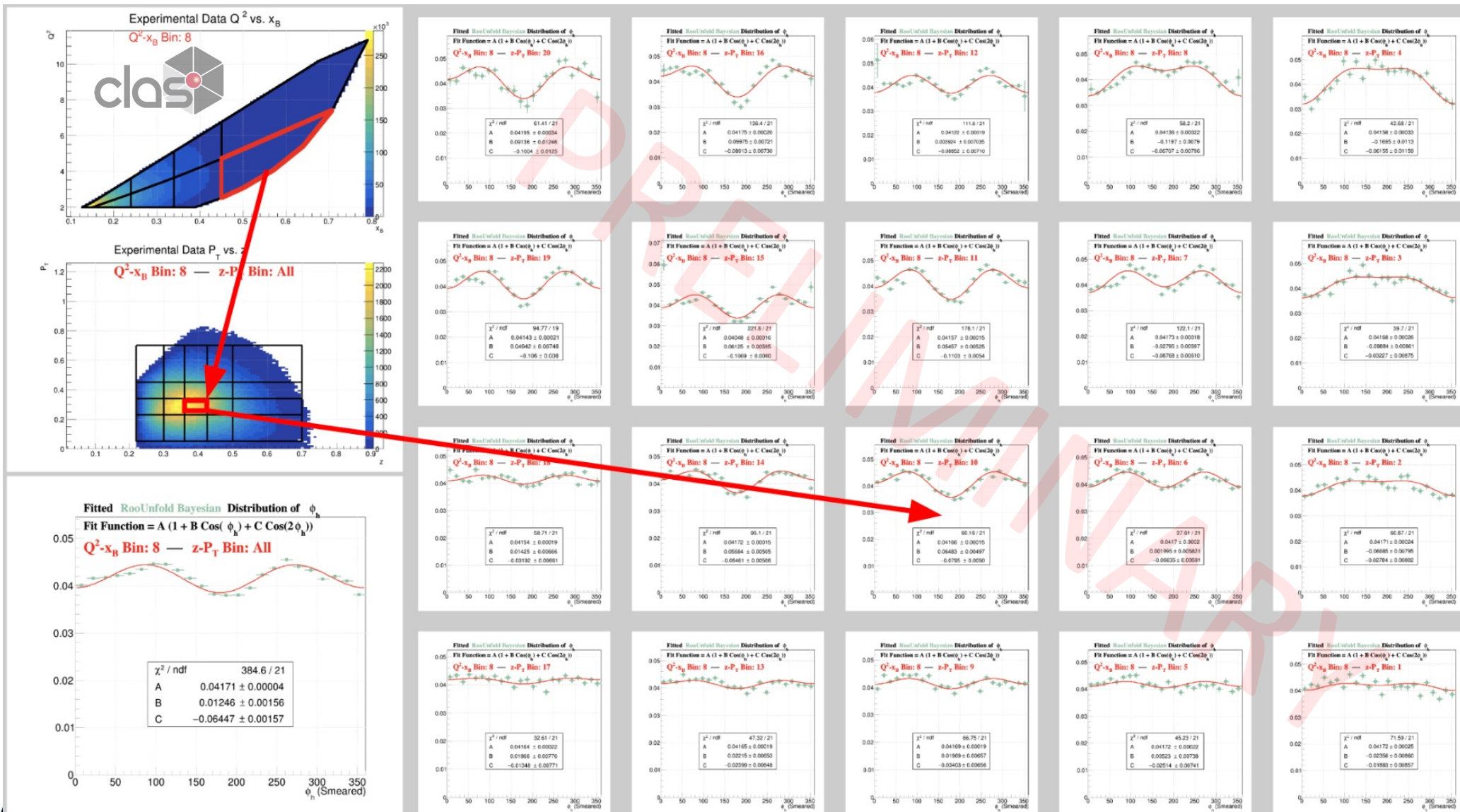
## Bayesian Unfolding

in each  $z$ - $P_T$  bin for the highlighted  $Q^2$ - $x_B$  bin

Arrows point to the distribution used in prior examples

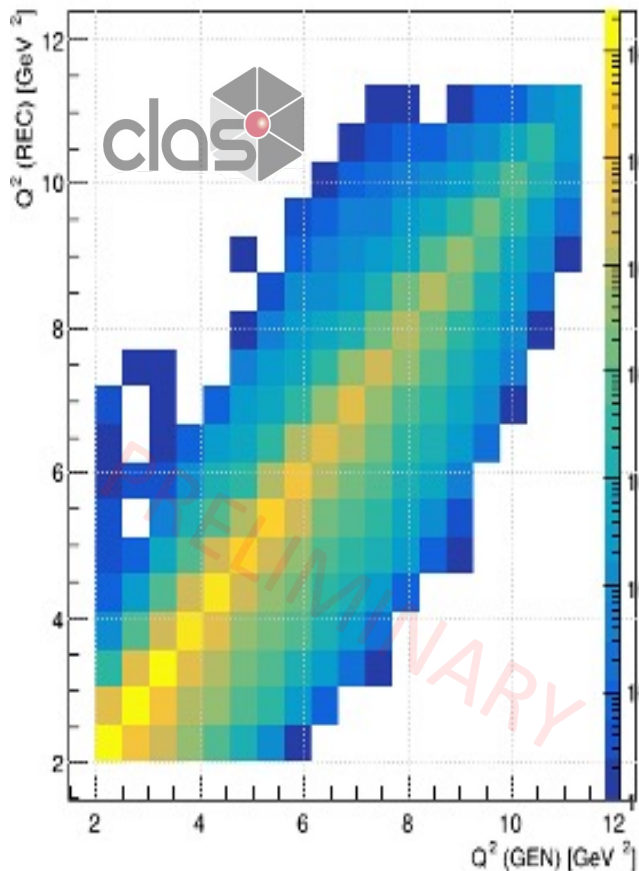
**DUPLICATE SLIDE**

These images are also available at the web address linked above

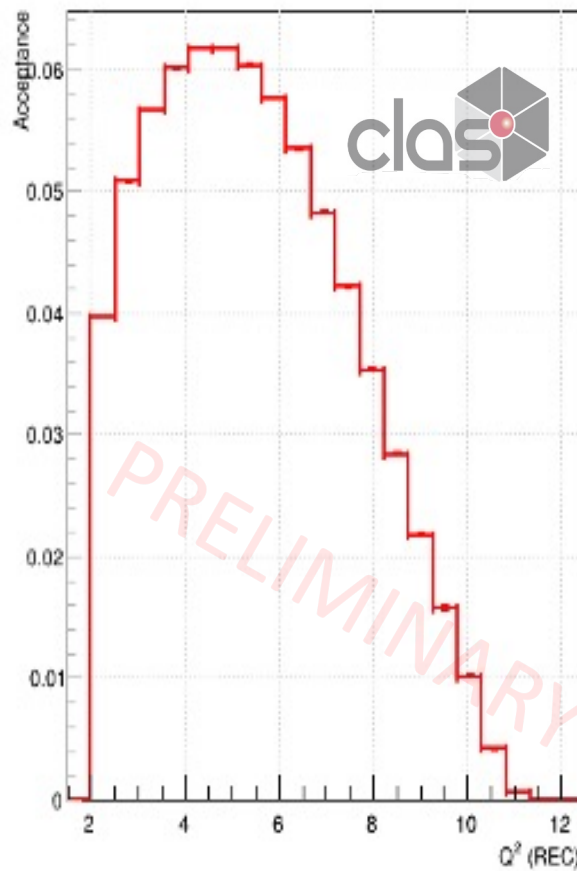


# Example of Unfolding ( $Q^2$ )

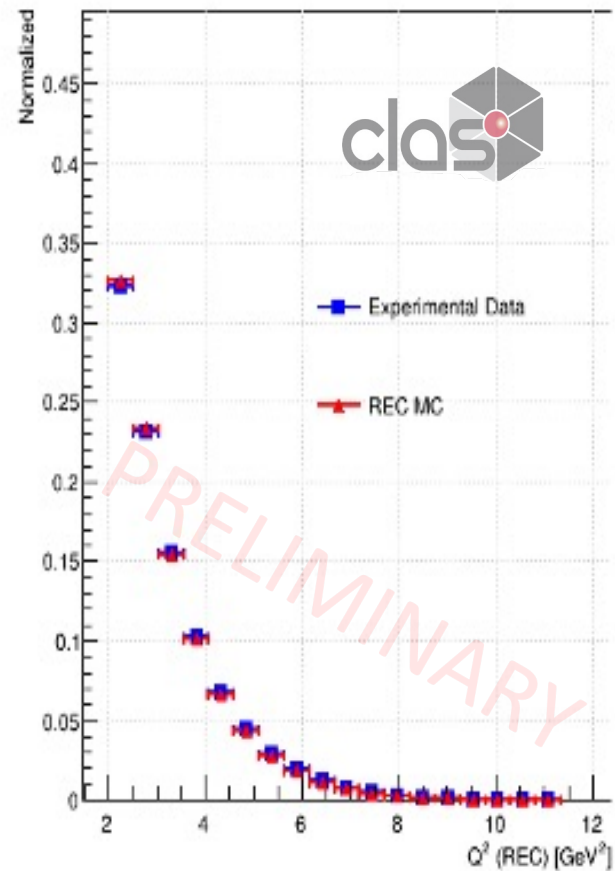
Response Matrix of  $Q^2$



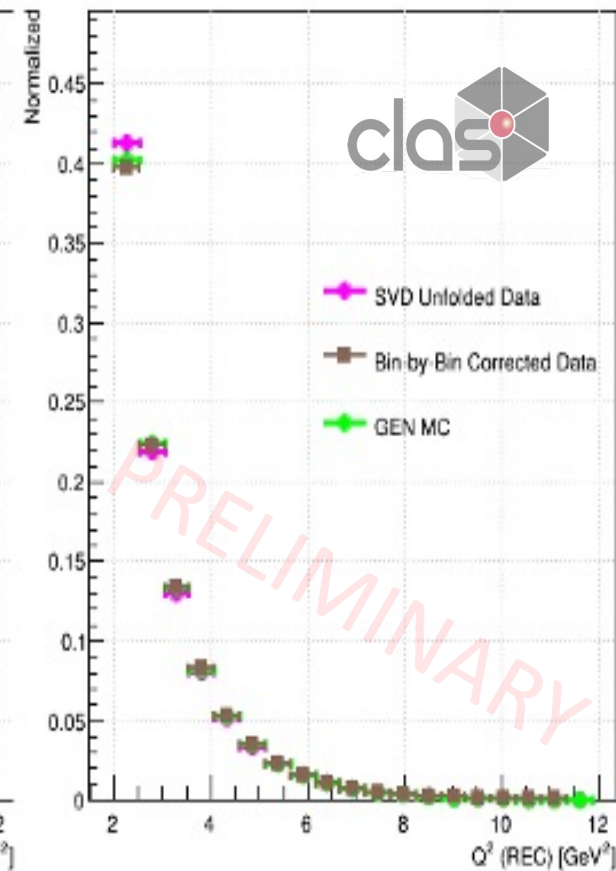
Acceptance Correction of  $Q^2$



Reconstructed Distribution of  $Q^2$



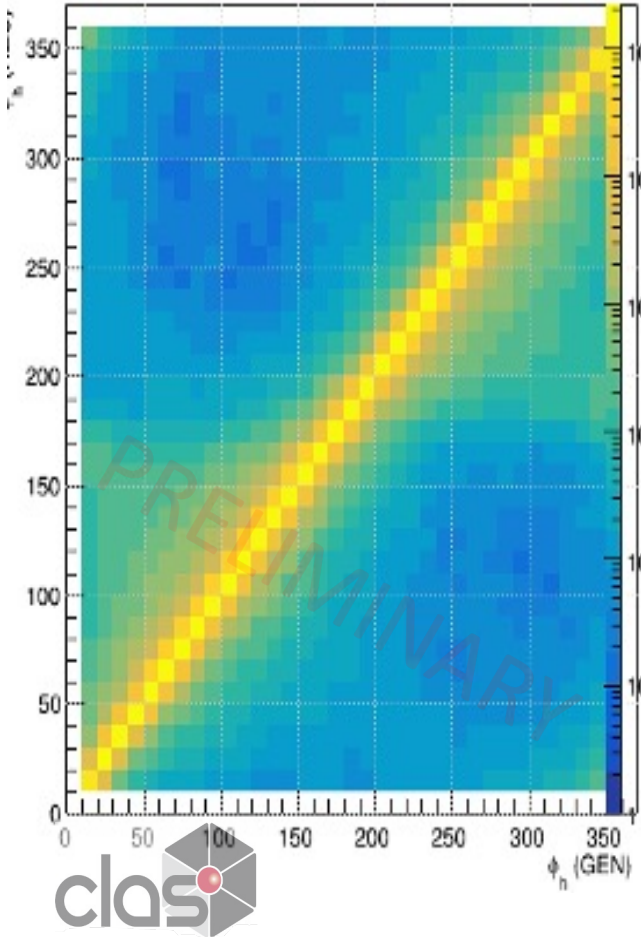
Unfolded Distribution of  $Q^2$



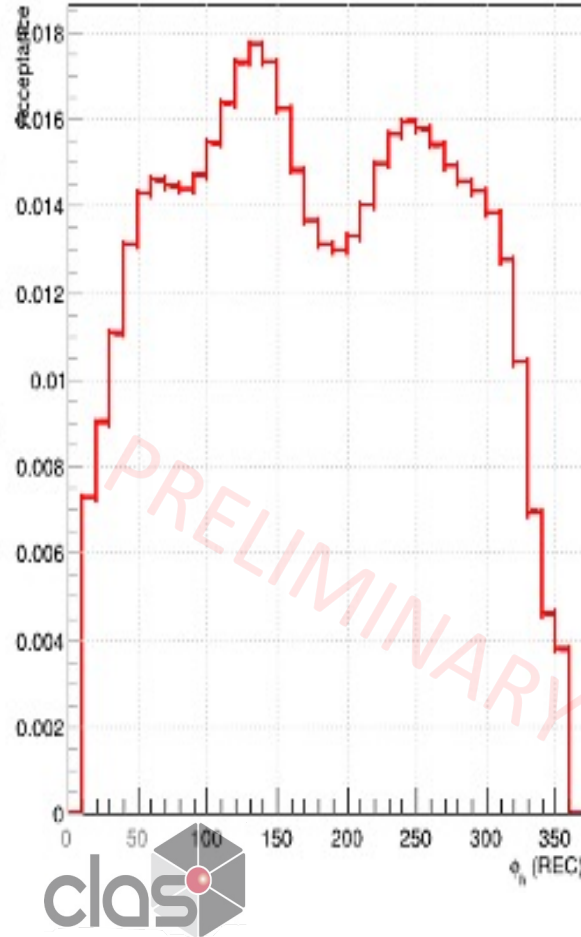


# Example of Unfolding ( $\phi_h$ )

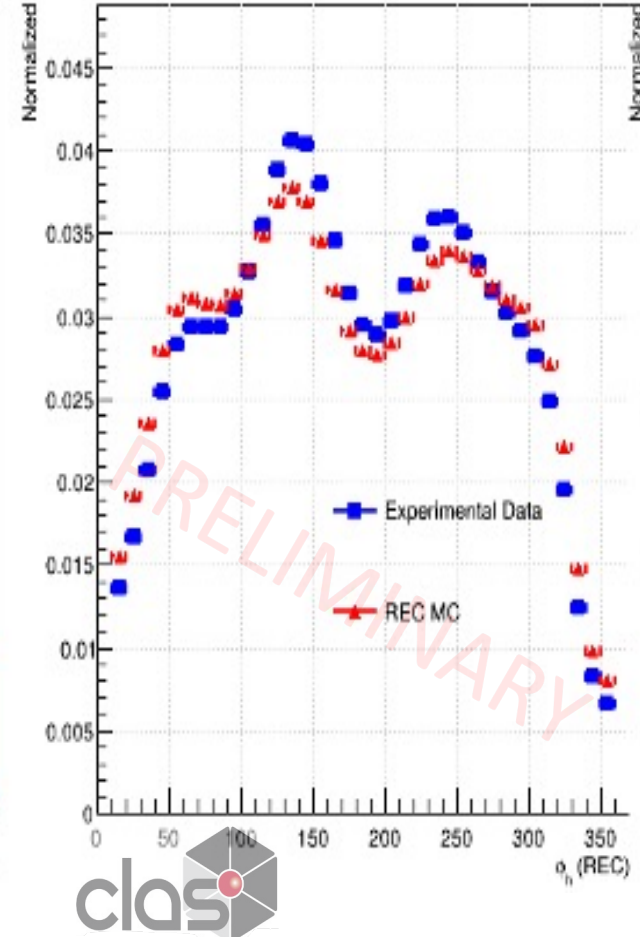
Response Matrix of  $\phi_h$



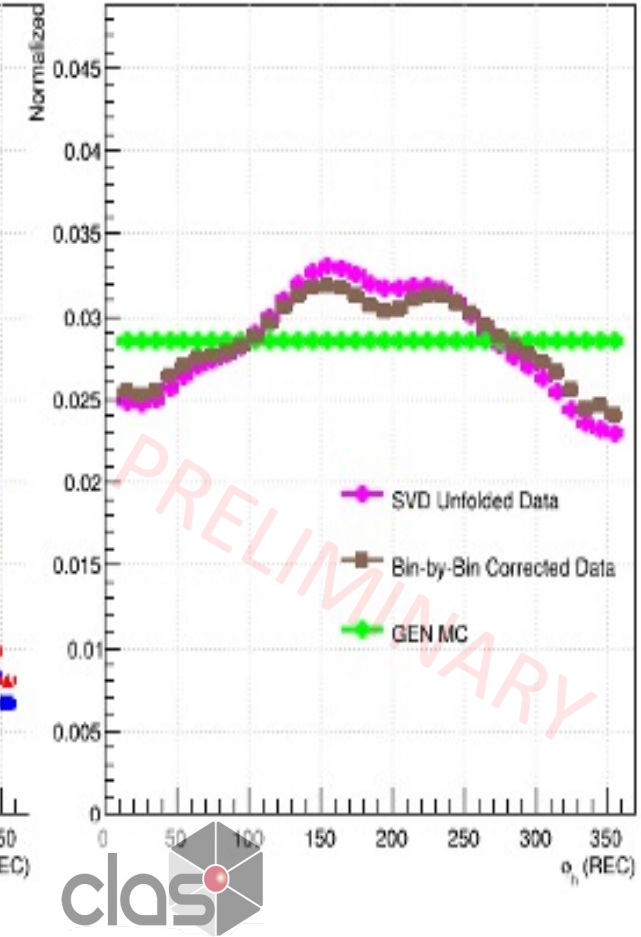
Acceptance Correction of  $\phi_h$



Reconstructed Distribution of  $\phi_h$



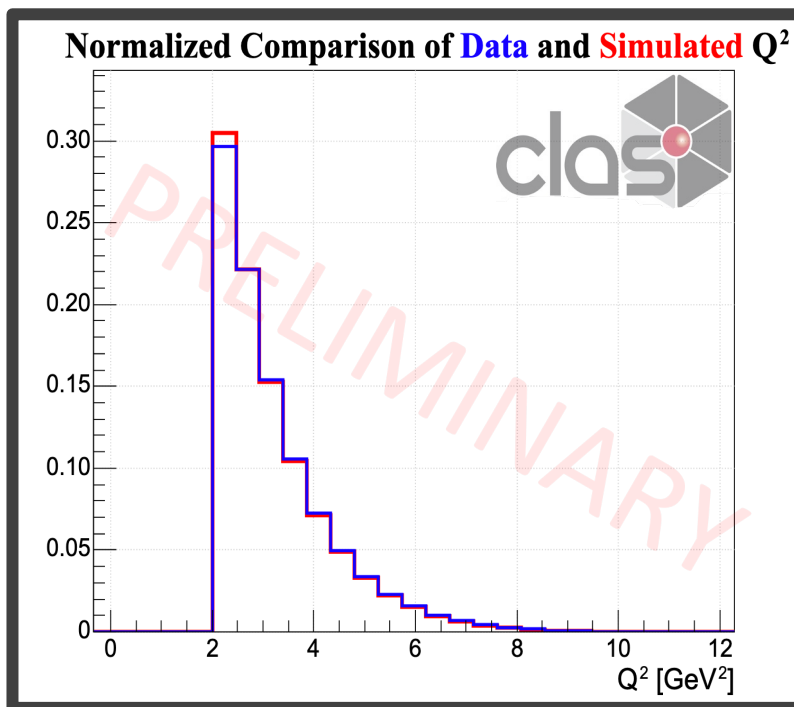
Unfolded Distribution of  $\phi_h$



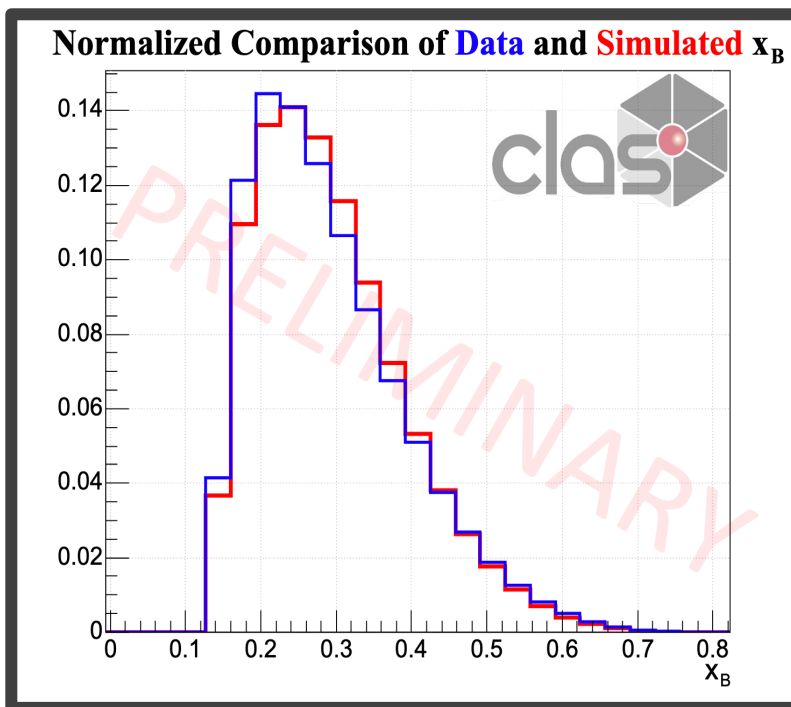
# Kinematic Binning and Data-MC Comparison

## Other Comparisons

### All Events



$Q^2$  Comparison



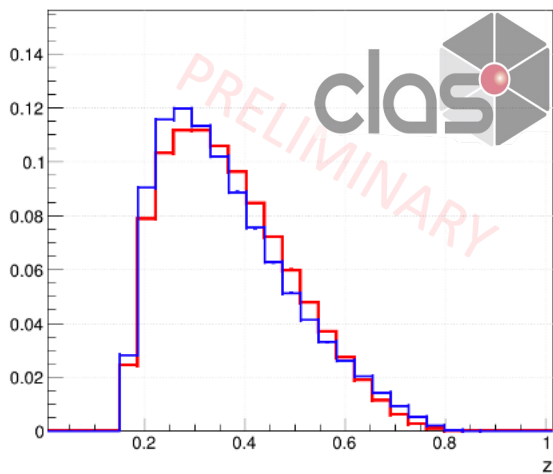
$x_B$  Comparison

# Kinematic Binning and Data-MC Comparison

## Other Comparisons

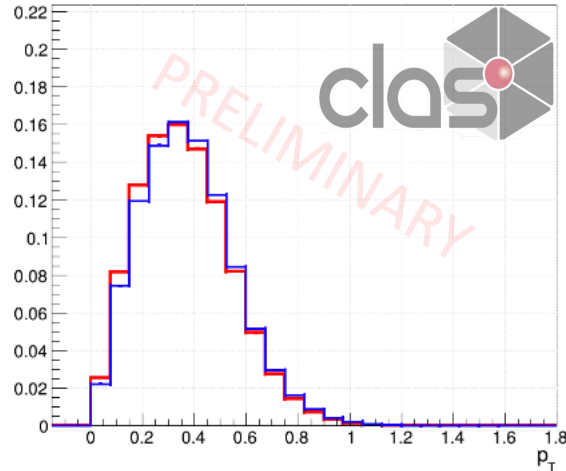
### All Events

Normalized Comparison of Real and Simulated  $z$



$z$  Comparison

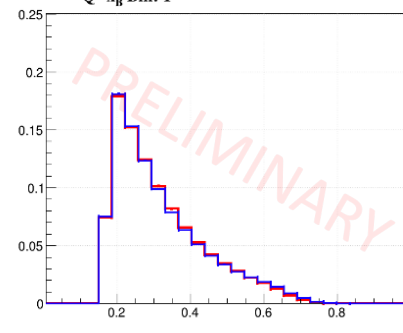
Normalized Comparison of Real and Simulated  $p_T$



$p_T$  Comparison

### $z$ Comparison

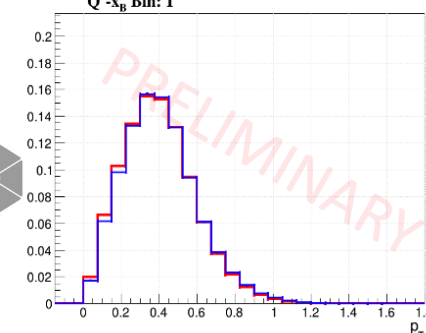
Normalized Comparison of Real and Simulated  $z$   
 $Q^2-x_B$  Bin: 1



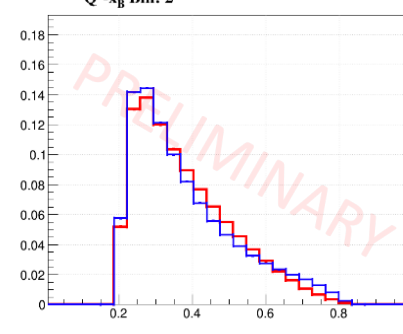
$Q^2-x_B$   
Bin 1

### $p_T$ Comparison

Normalized Comparison of Real and Simulated  $p_T$   
 $Q^2-x_B$  Bin: 1

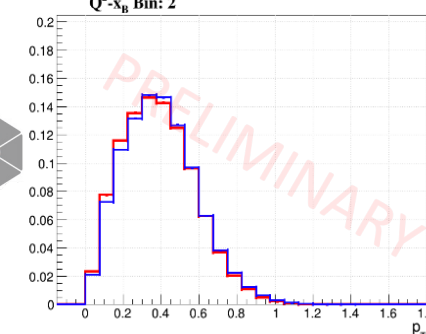


Normalized Comparison of Real and Simulated  $z$   
 $Q^2-x_B$  Bin: 2



$Q^2-x_B$   
Bin 2

Normalized Comparison of Real and Simulated  $p_T$   
 $Q^2-x_B$  Bin: 2



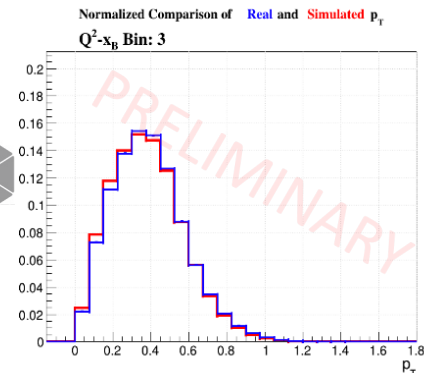
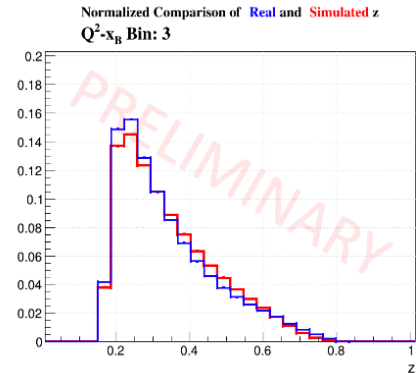
# Kinematic Binning and Data-MC Comparison

## Other Comparisons

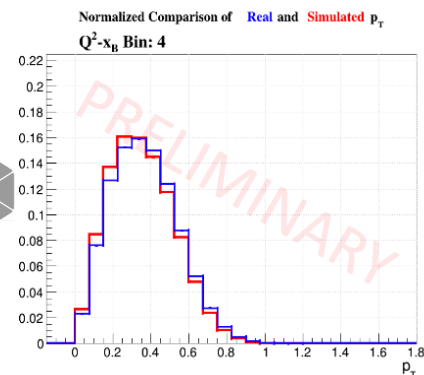
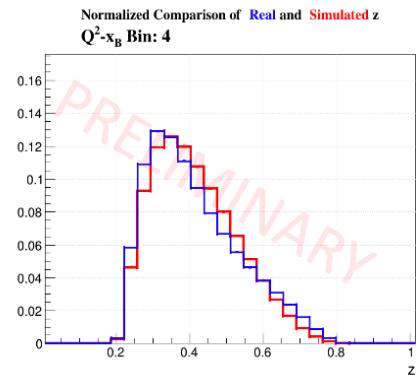
z Comparison

$P_T$  Comparison

$Q^2-x_B$   
Bin 3



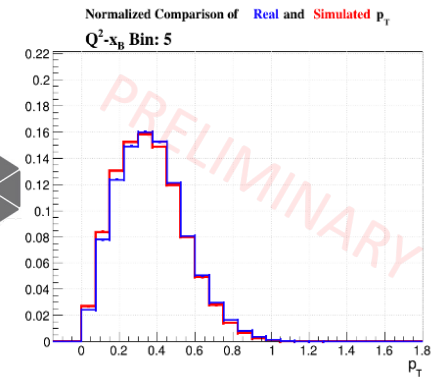
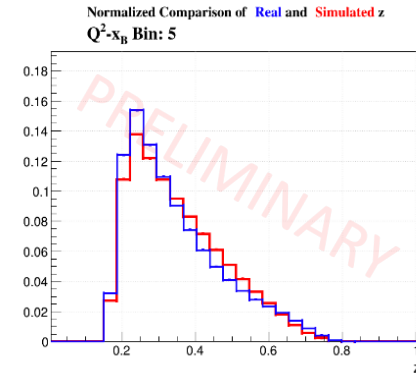
$Q^2-x_B$   
Bin 4



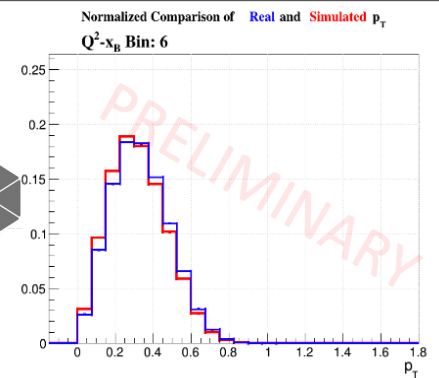
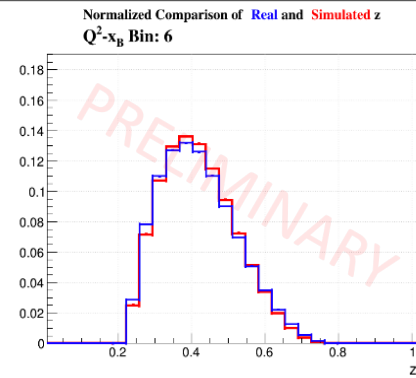
z Comparison

$P_T$  Comparison

$Q^2-x_B$   
Bin 5



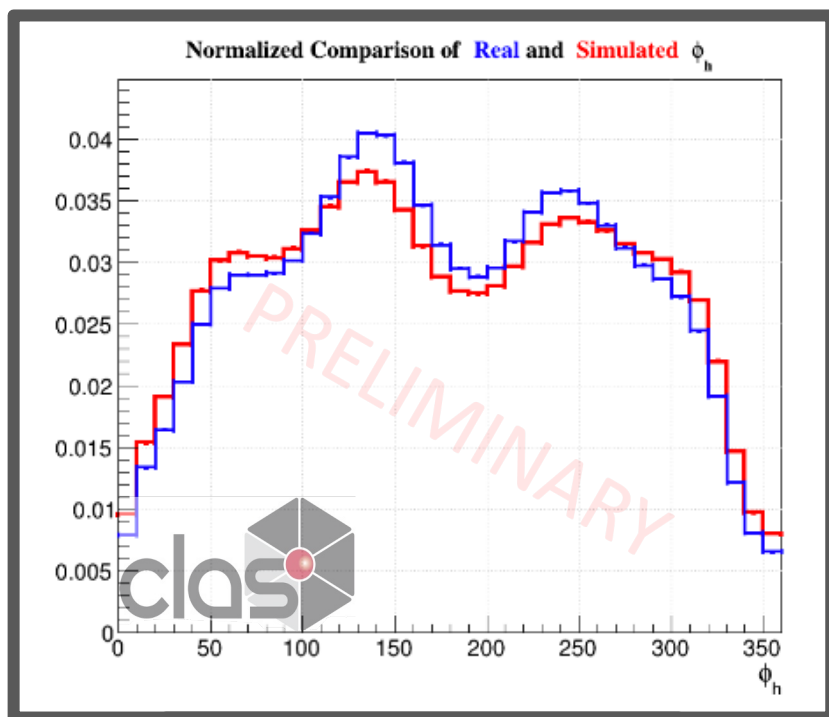
$Q^2-x_B$   
Bin 6



# Kinematic Binning and Data-MC Comparison

## Other Comparisons

### All Events

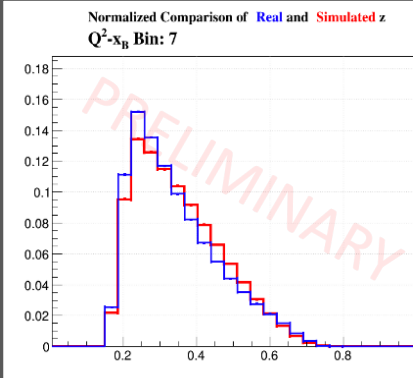


$\phi_h$  Comparison

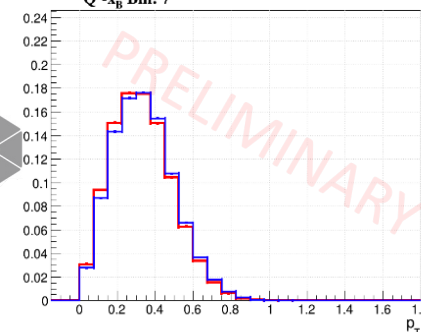
### z Comparison

### $P_T$ Comparison

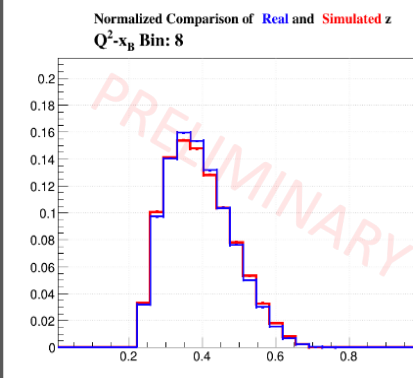
$Q^2-x_B$   
Bin 7



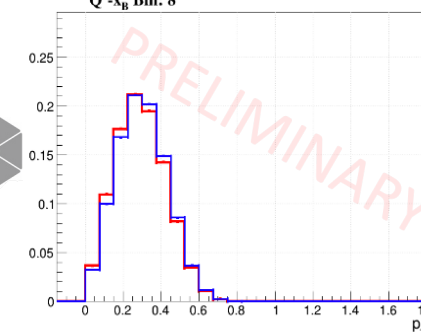
Normalized Comparison of Real and Simulated  $p_T$   
 $Q^2-x_B$  Bin: 7



$Q^2-x_B$   
Bin 8



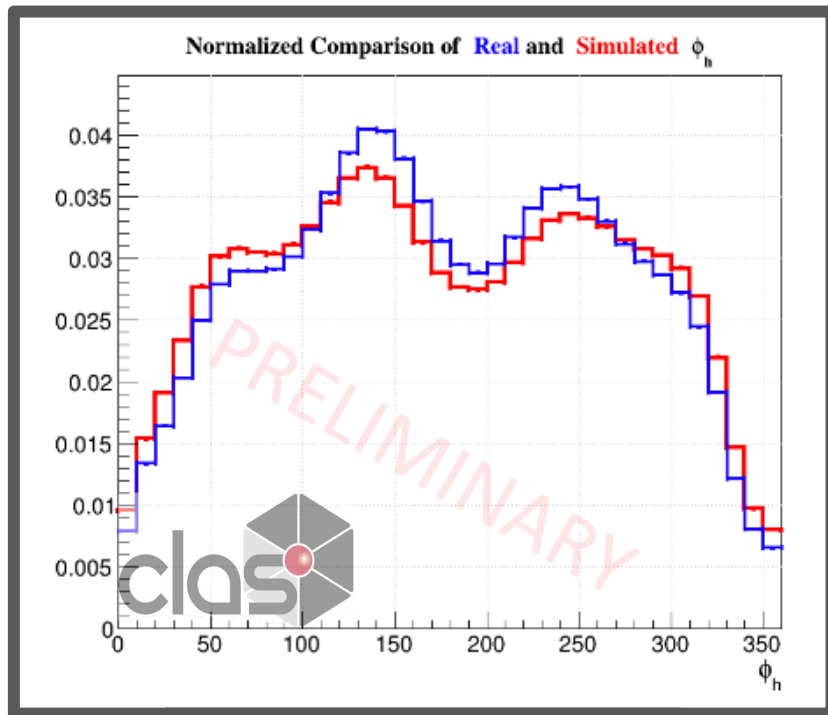
Normalized Comparison of Real and Simulated  $p_T$   
 $Q^2-x_B$  Bin: 8



# Kinematic Binning and Data-MC Comparison

## Other Comparison

### All Events



$\phi_h$  Comparison

- Some differences between the  $\phi_h$  distributions are expected
- **Reason:** The Monte Carlo Simulation is not initialized with any  $\phi_h$  modulations yet
  - i.e., the  $\phi_h$  distribution is completely flat before reconstruction
- Initial calculations of the  $\cos\phi$  and  $\cos 2\phi$  moments will be used to 'update' the simulation in an iterative fashion

# Event Selection (Full PID)

The RG-A Analysis Overview and Procedures note goes into detail about the common particle identification scheme used for RG-A

(See: [https://clas12-docdb.jlab.org/DocDB/0009/000949/001/RGA\\_Analysis\\_Overview\\_and\\_Procedures-08172020.pdf](https://clas12-docdb.jlab.org/DocDB/0009/000949/001/RGA_Analysis_Overview_and_Procedures-08172020.pdf))

## Electron PID Criteria:

- Detected in Forward Detector
- > 2 photoelectrons detected in the HTCC
- > 0.07 GeV energy deposited in the PCAL
- Sector dependent sampling fraction cut
- “Diagonal cut” for electrons above 4.5 GeV (HTCC threshold)
- $y < 0.75$ , not strictly an “electron cut”, but sets the min electron energy approximately  $> 2.4$  GeV

## Pion PID Criteria:

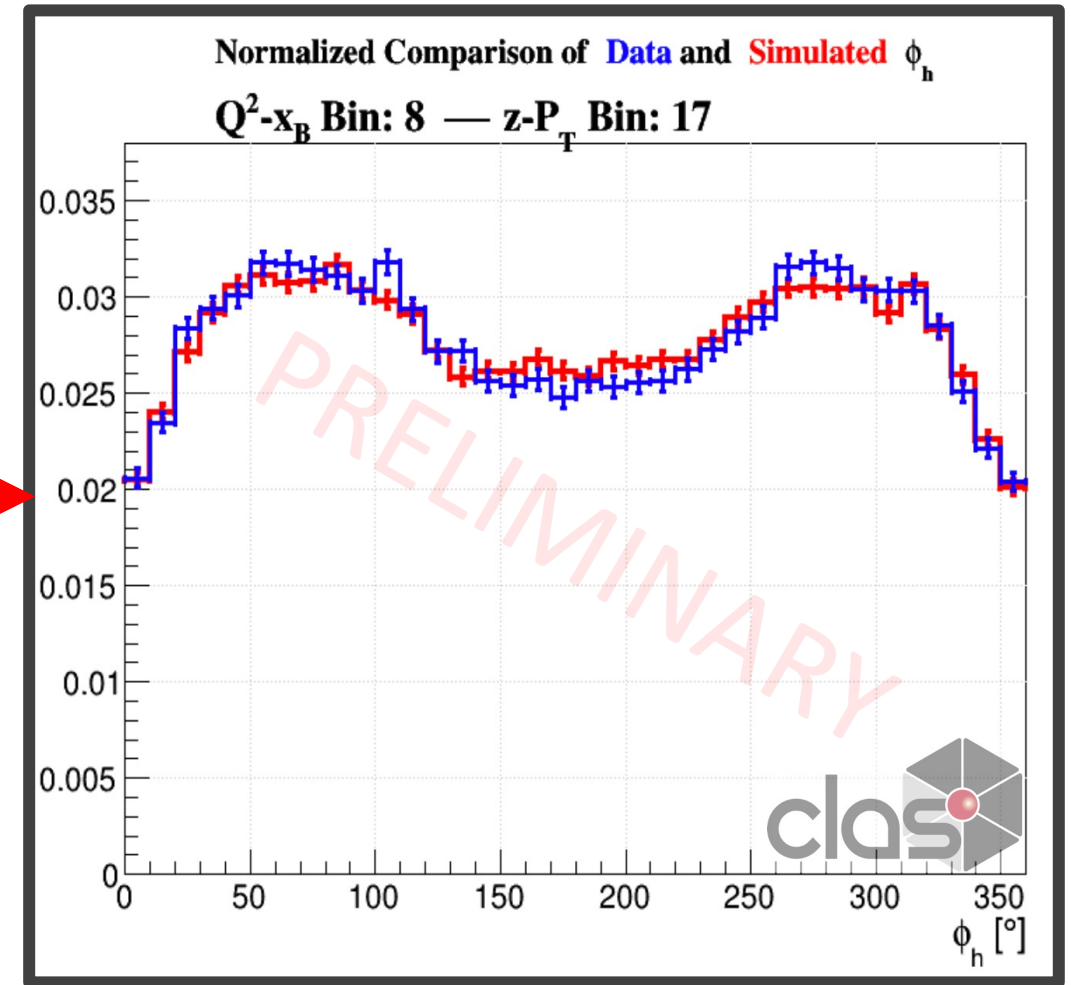
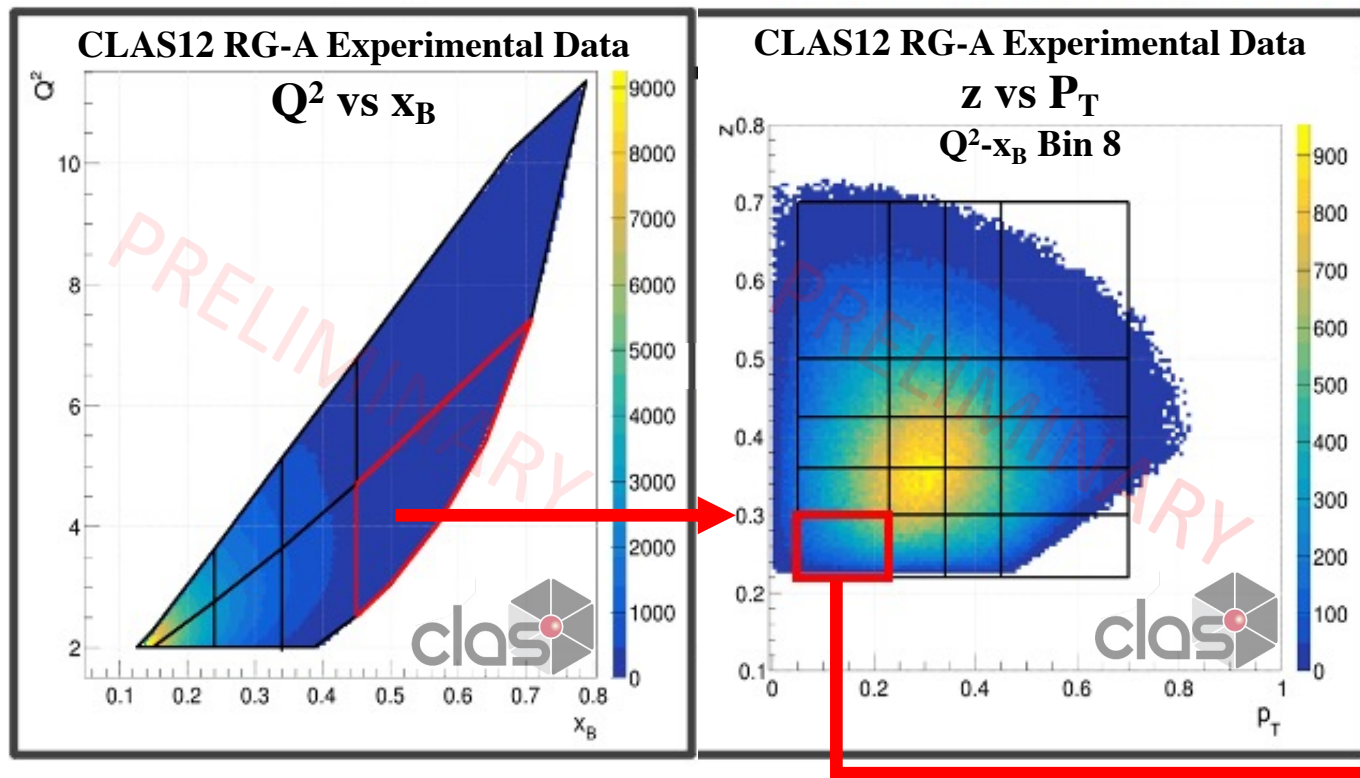
- Detected in Forward Detector
- $p > 1.25$  GeV
- Refined chi2pid cuts

# Multidimensional Analysis Procedures

## Multidimensional Kinematic Binning (5 Dimensions)

8  $Q^2$ - $x_B$  Bins Total – 20-49  $z$ - $P_T$  Bins (per  $Q^2$ - $x_B$  bin)

$\phi_h$  distribution for the  $Q^2$ - $x_B$ - $z$ - $P_T$  bin shown in red



EXTRA EXAMPLE