# The Search for Hybrid Mesons at GlueX 

Will Imoehl
Carnegie Mellon University on behalf of the GlueX collaboration

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## The Quark Model

## Want to know which types of hadrons exist in QCD

Conventional light mesons are $q \bar{q}$ states

- Allowed $J^{P C}$ for conventional light mesons $(n=0,1,2, \ldots)$ :

| $J^{P C}$ | $(2 n)^{-+}$ | $(2 n+1)^{+-}$ | $(n+1)^{--}$ | $n^{++}$ |
| :---: | :---: | :---: | :---: | :---: |
| Minimal Quark Content |  |  |  |  |
| $u \bar{d}, u \bar{u}-d \bar{d}, d \bar{u}(I=1)$ | $\pi$ | $b$ | $\rho$ | $a$ |
| $d \bar{d}+u \bar{u}$ and /or $s \bar{s}$ | $\eta, \eta^{\prime}$ | $h, h^{\prime}$ | $\omega, \phi$ | $f, f^{\prime}$ |



Hybrid mesons have gluonic excitations

- Hybrids can mix with conventional mesons
- Some hybrids have "exotic" $J^{P C}$ not allowed for $q \bar{q}$ mesons


## Lattice QCD Spectrum



- Lightest hybrid meson predicted to be $I=1 J^{P C}=1^{-+}$state - Likely the $\pi_{1}(1600)$, seen by multiple experiments
- BESIII observes $\eta_{1}(1855)$, candidate for either $\eta_{1}$ or $\eta_{1}^{\prime}$


## Recent Experimental Results on Lightest Hybrid Meson

- Previous experiments find $\pi_{1}(1400)$ in $\eta \pi$ and $\pi_{1}(1600)$ in $\eta^{\prime} \pi$
- Joint Physics Analysis Center (JPAC) analysis of the COMPASS data only requires one resonance
- $M=1564 \pm 24 \pm 86 \mathrm{MeV}$ and $\Gamma=492 \pm 54 \pm 102 \mathrm{MeV}$



Analysis: A. Rodas et al. PRL 122042002 (2019)
Data: C. Adolph et al. (COMPASS) PLB 740 303-311 (2015)

## The GlueX Experiment

Photoproduction experiment located at Jefferson Lab

- Photoproduction has been predicted to copiously produce hybrid mesons in some models
- GlueX uses polarized photon beam - allows us to differentiate production mechanisms
Steps to studying the hybrid meson spectrum:

1. Demonstrate photoproduction produces hybrid mesons by confirming COMPASS result
2. Search for undiscovered hybrid mesons


## $\pi_{1}$ Branching Fractions from Lattice QCD

- Lattice QCD provides predictions for $\pi_{1}$ branching fractions

| PRD 103054502 (2021) |  |  |
| :---: | :---: | :---: |
| Decay | Width (MeV) | Branching Fraction |
| $\eta \pi$ | $0 \rightarrow 1$ | $0 \rightarrow 0.7 \%$ |
| $\eta^{\prime} \pi$ | $0 \rightarrow 12$ | $0 \rightarrow 7.9 \%$ |
| $b_{1} \pi$ | $139 \rightarrow 529$ | $69.5 \rightarrow 100 \%$ |
| All others | $0 \rightarrow 48$ | $0 \rightarrow 25.7 \%$ |
| Total | $139 \rightarrow 590$ | - |



## GlueX Search Strategy for $\pi_{1}(1600)$

Two main goals:

1. Set upper limit on photoproduction cross section of $\pi_{1}(1600)$

- Never done before - use recent lattice calculations
- Can be used to test discovery potential in different final states
- Expect signals in $\pi_{1}^{0} \rightarrow \omega \pi^{+} \pi^{-}$and $\pi_{1}^{-} \rightarrow \omega \pi^{-} \pi^{0}$


2. Confirm state found in COMPASS data:

- Perform partial wave analyses on $\eta \pi$ and $\eta^{\prime} \pi$
- $\pi_{1}(1600)$ would appear in $P$-wave
- $\eta \pi$ has stronger coupling to $a_{2}(1320)$
- $\eta^{\prime} \pi$ has stronger coupling to $\pi_{1}(1600)$


## $\pi_{1}(1600) \rightarrow \omega \pi \pi$ Search

- Measure $d \sigma / d M$ in $50 \mathrm{MeV} / c^{2}$ bins of $M(\omega \pi \pi)$


No obvious $\pi_{1}(1600)$ signal - set upper limit Isolate $\sigma(\omega \pi \pi)_{I=1}$ using Clebsch-Gordan coefficients:

- Assume no $I=2$ contributions to $\sigma(\omega \pi \pi)$
- $\sigma\left((\omega \pi \pi)^{0}\right)_{l=1}=\sigma\left(\omega \pi^{+} \pi^{-}\right)-2 \sigma\left(\omega \pi^{0} \pi^{0}\right)$
- $\sigma\left((\omega \pi \pi)^{-}\right)_{I=1}=\sigma\left(\omega \pi^{-} \pi^{0}\right)$

Know $a_{2}(1320)$ shape from PDG, $\pi_{1}$ shape from JPAC
Fit $I=1$ cross sections with sum of these shapes

## $\pi_{1}$ Upper Limit - Upper Limit Results

Measure ratio $\frac{\sigma_{u l}\left(\pi_{1}\right)}{\sigma\left(a_{2}(1320)\right)}$



Analysis for $0.1<-t<0.5 \mathrm{GeV}^{2}$ and $8<E_{\gamma}<10 \mathrm{GeV}$ using $28 \%$ of GlueX-I data
$\rightarrow a_{2}(1320)$ size fixed to $\sigma_{\eta \pi}\left(a_{2}\right) \mathcal{B}_{P D G}\left(a_{2} \rightarrow \omega \pi \pi\right)$

- Fit $M(\omega \pi \pi)_{I=1}<1.6 \mathrm{GeV} / c^{2}$ using $\pi_{1}(1600)$ (pink) shape
- Only free parameter in fit is the $\pi_{1}$ normalization
$\pi_{1}(1600)$ upper limit is of similar size to the $a_{2}(1320)$ cross section


## $\pi_{1}$ Upper Limit - Projections to $\eta \pi$ and $\eta^{\prime} \pi$





Do not expect large $\pi_{1}(1600)$ in $\eta \pi$
$\pi_{1}(1600)$ could be the dominant contribution in $\eta^{\prime} \pi^{-}$

Projections for $0.1<-t<0.5 \mathrm{GeV}^{2}$ and $8.2<E_{\gamma}<8.8 \mathrm{GeV}$ using full GlueX-I data First limit on size of hybrid photoproduction cross sections
These projections guide the next steps of the search

## Partial Wave Analysis of $\eta \pi$

- Beam polarization allows us to separate production mechanisms
- Natural parity exchange for $J^{P}=0^{+}, 1^{-}, 2^{+}, .$.
- Unnatural parity exchange for $J^{P}=0^{-}, 1^{+}, 2^{-}, .$.


Natural exchange


Unnatural exchange

- $\eta \pi$ is system of two pseudoscalars $\left(J^{P C}=0^{-+}\right)$

|  | $S$-wave $(\ell=0)$ | $P$-wave $(\ell=1)$ | $D$-wave $(\ell=2)$ |
| :---: | :---: | :---: | :---: |
| $J^{P C}$ | $0^{++}$ | $1^{-+}($exotic $)$ | $2^{++}$ |

Amplitudes function of production angle $\Phi$ and decay angles $(\phi, \theta)$

## Semi-Mass Independent PWA on $\eta \pi^{0}$

Signal process: $\gamma p \rightarrow a_{2}^{0}(1320) p$

- Ultimately want mass independent PWA to $\eta \pi$ and $\eta^{\prime} \pi$
- Mass independent PWA has many parameters
- To stabilize fits, we add in physical constraints: model $a_{2}(1320)$ and $a_{2}(1700)$ as Breit-Wigner
- Use these results to measure $\frac{d \sigma\left(a_{2}\right)}{d t}$



## $a_{2}^{0}(1320)$ Cross Section from $\eta \pi^{0}$



- First separation of natural and unnatural exchanges
- Comes from polarized photon beam - unique to GlueX
- $\sigma\left(a_{2}(1320)\right)$ measured here can be used as reference for $\eta^{\prime} \pi$
- Results agree reasonably well with theory prediction
- Publication being prepared


## Semi-mass Independent PWA on $\eta \pi^{-}$

Process: $\gamma p \rightarrow \eta \pi^{-} \Delta^{++}$

- Use same method as $\eta \pi^{0}$
- $a_{2}(1320)$ appears in $D_{1}^{-}$ wave $\Longrightarrow$ pion exchange with direct polarization transfer from $\gamma$ to $a_{2}$
$S_{0}^{-}$
$\mathbf{a}_{2}(1320)$
Gluef
Preliminary


$$
M\left(\eta \pi^{-}\right)\left[G e V / c^{2}\right]
$$

Complication: background from $\gamma p \rightarrow\left(a_{2}^{-} \pi^{+}\right) p \rightarrow \pi^{+} \pi^{-} \eta p$

$\Delta^{++}$

## Prospects for $\eta^{\prime} \pi$

Analysis on $\eta^{\prime} \pi$ being performed in parallel

- Expect best sensitivity to $\pi_{1}(1600)$ in $\eta^{\prime} \pi$
- Less pronounced $a_{2}(1320) \Longrightarrow$ use $\eta \pi$ measurement as reference


- GlueX-I Data
$a_{2}$ MC Projection
$=\pi_{1}$ MC Upper Limit


## Summary

- GlueX provides a unique place to look for hybrid mesons
- Beam polarization gives info on production mechanisms
- Some models predict hybrids copiously produced in photoproduction
- We set first upper limit on $\pi_{1}$ photoproduction cross sections
- $\eta^{\prime} \pi$ final states have largest discovery potential
- $\eta \pi$ PWA is being used to extract $\sigma\left(a_{2}(1320)\right)$
- Agrees well with theory predictions
- Can be used as reference for $\eta^{\prime} \pi$ analysis
- Publication being prepared
- $\eta^{\prime} \pi$ is most sensitive channel to $\pi_{1}(1600)$ at GlueX
- PWA framework from $\eta \pi$ analysis can be used

Acknowledgements: gluex.org/thanks


## Hall D at Jefferson Lab

- Hall D is one of four experimental halls at Jefferson Lab
- CEBAF accelerates electrons up to 12 GeV
- Electrons impinge on diamond wafer, creating linearly polarized photons via coherent bremsstrahlung
- Photon beam incident on liquid hydrogen target



## CLAS $\pi_{1} \rightarrow 3 \pi$ Upper Limit

CLAS sets an upper limit of $\sigma\left(\gamma p \rightarrow \pi_{1}^{+} n\right)<13.5 \mathrm{nb}$.

- Lower photon beam energy: $4.8<E_{\gamma}<5.4 \mathrm{GeV}$
- Different reaction - produced against a neutron

- Upper limit is really on $\sigma\left(\gamma p \rightarrow \pi_{1}^{+} n\right) \mathcal{B}\left(\pi_{1}^{+} \rightarrow \pi^{+} \pi^{-} \pi^{+}\right)$
- They used a model dependent central value for $\mathcal{B}\left(\pi_{1}\right)$
- Upper limit needs to include systematic uncertainty in $\mathcal{B}\left(\pi_{1}^{+}\right)$
- LQCD allowed values are $0<\mathcal{B}\left(\pi_{1} \rightarrow 3 \pi\right)<12.6 \%$.

