

---

# Measurement of the $N \rightarrow \Delta$ Transition Form Factors at low $Q^2$

Hamza Atac  
Temple University

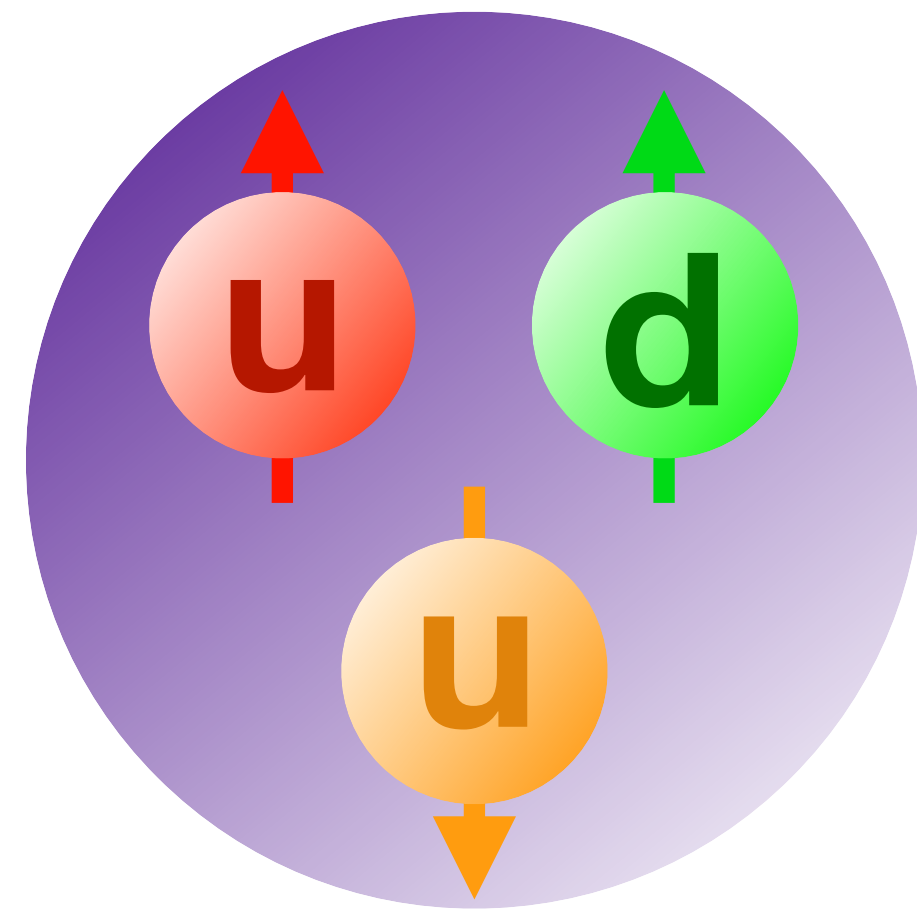
Supported by the US DOE / NP award DE-SC0016577

 Jefferson Lab



# The N- $\Delta$ transition

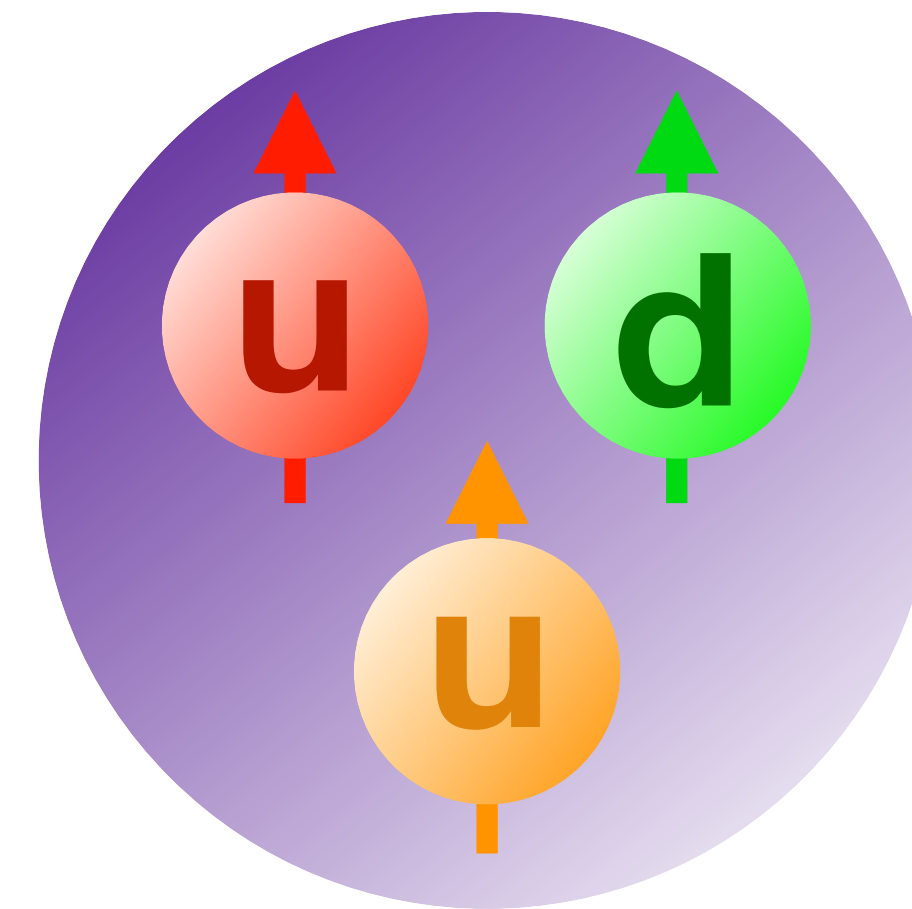
Proton (938 MeV)



Dominant transition



Delta (1232 MeV)

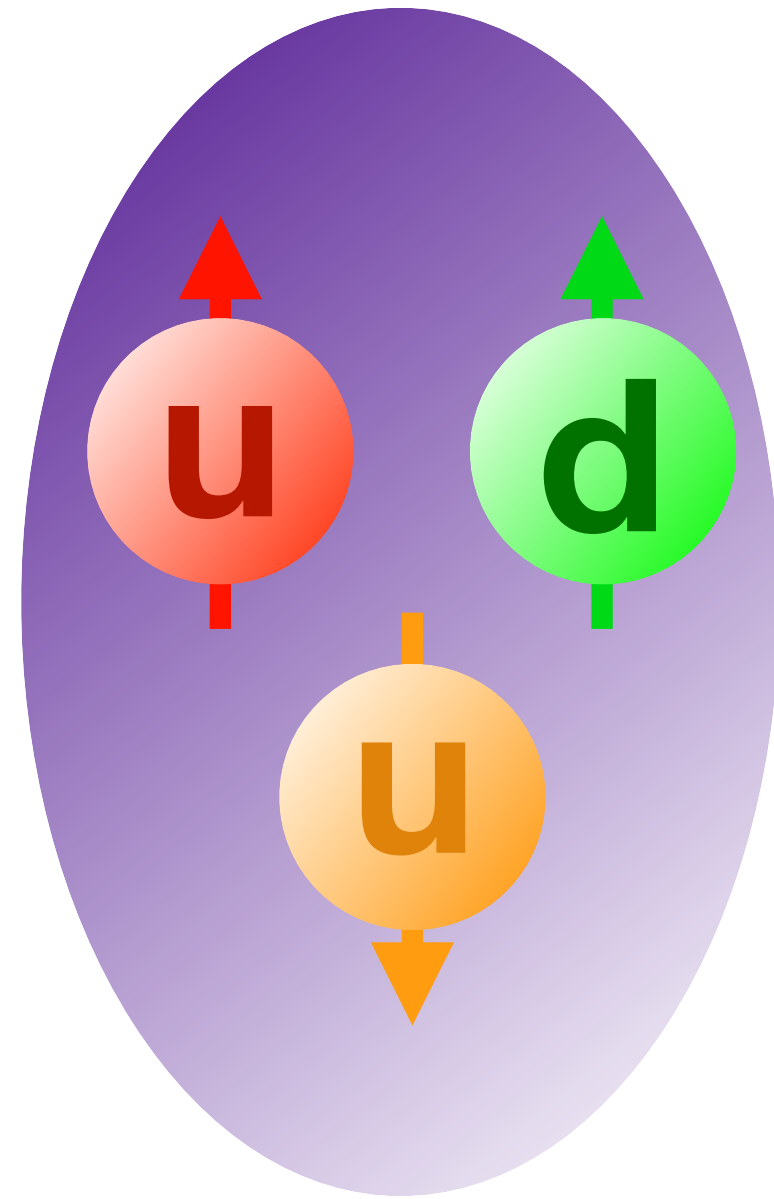


The first excited state of the proton, the Delta, can be reached through a magnetic spin flip of one of the quarks (M1).

(spherical S-wave proton WF  $\rightarrow$  spherical S-wave Delta WF)

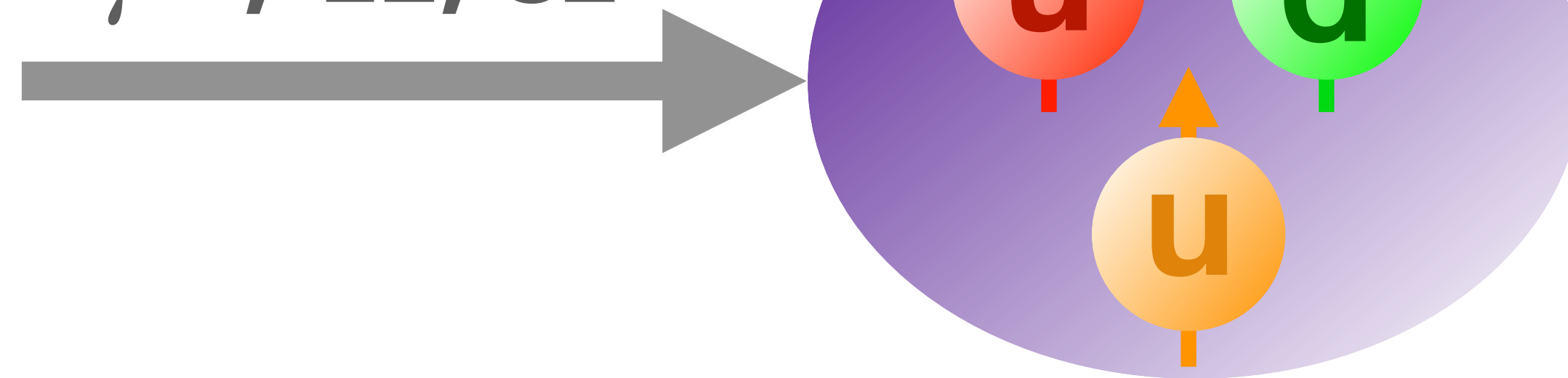
# The N- $\Delta$ transition

Proton (938 MeV)



Delta (1232 MeV)

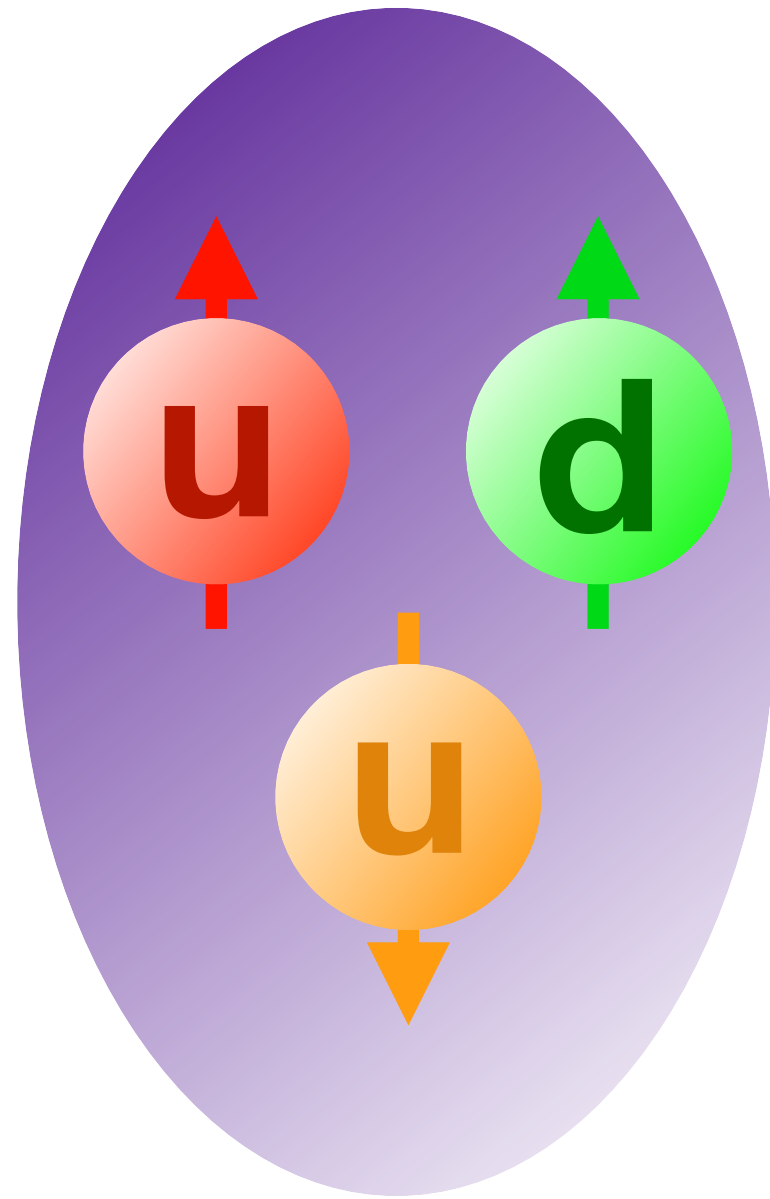
$\gamma^*$ , E2, C2



It can also be reached through a quadrupole (E2 or C2) transition from proton to delta.  
(The quadrupole amplitudes are associated with the existence of non-spherical components in the proton and Delta WF)

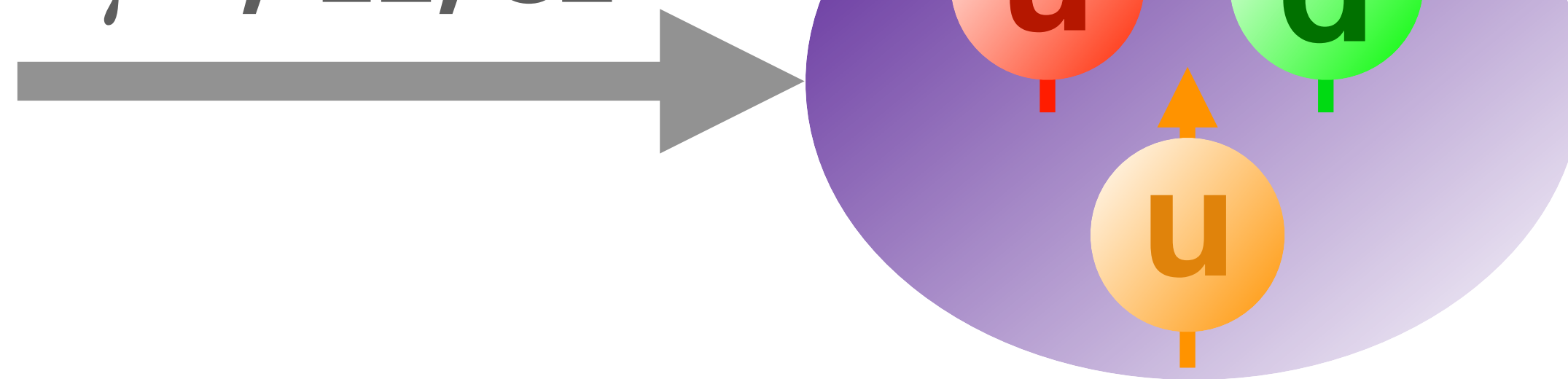
# The N- $\Delta$ transition

Proton (938 MeV)



Delta (1232 MeV)

$\gamma^*$ , E2, C2



It can also be reached through a quadrupole (E2 or C2) transition from proton to delta.  
(The quadrupole amplitudes are associated with the existence of non-spherical components in the proton and Delta WF)

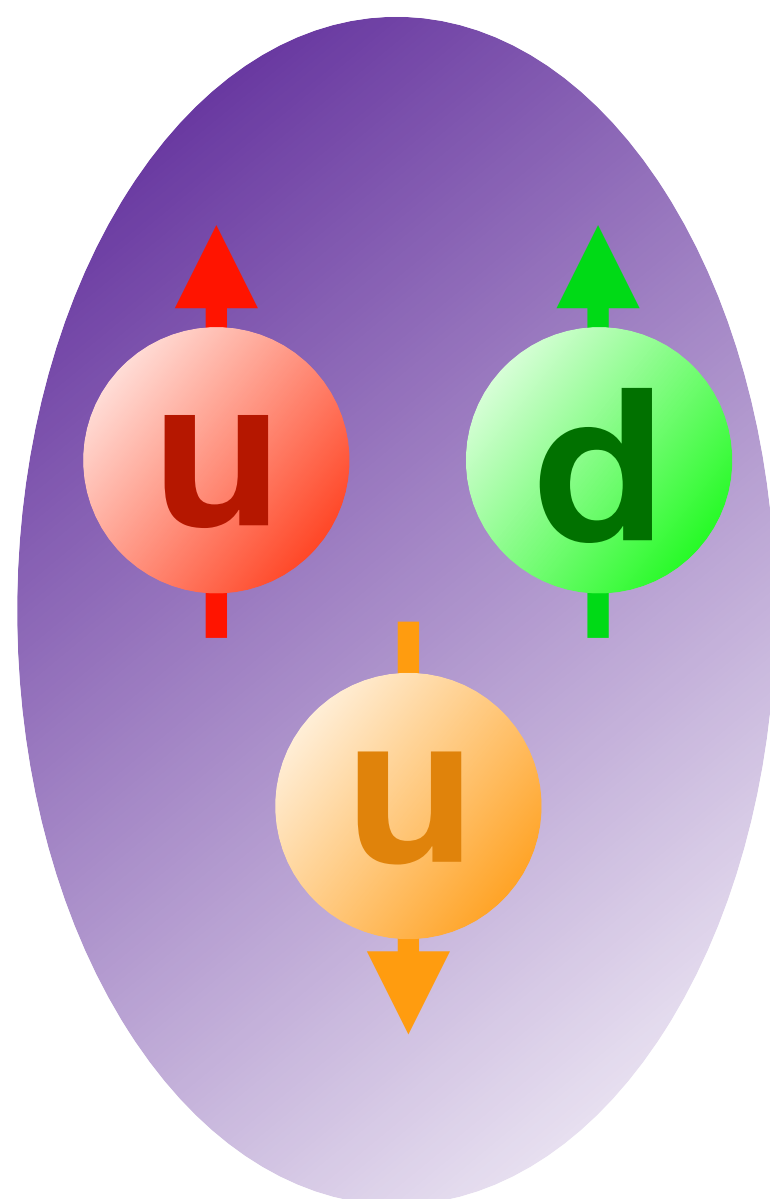
The quadrupole to dipole ratio (E2/M1 or C2/M1) is non-zero... Why?

Electric-Quadrupole to Magnetic-Dipole Ratio = EMR = E2/M1

Coulomb-Quadrupole to Magnetic-Dipole Ratio = CMR = C2/M1

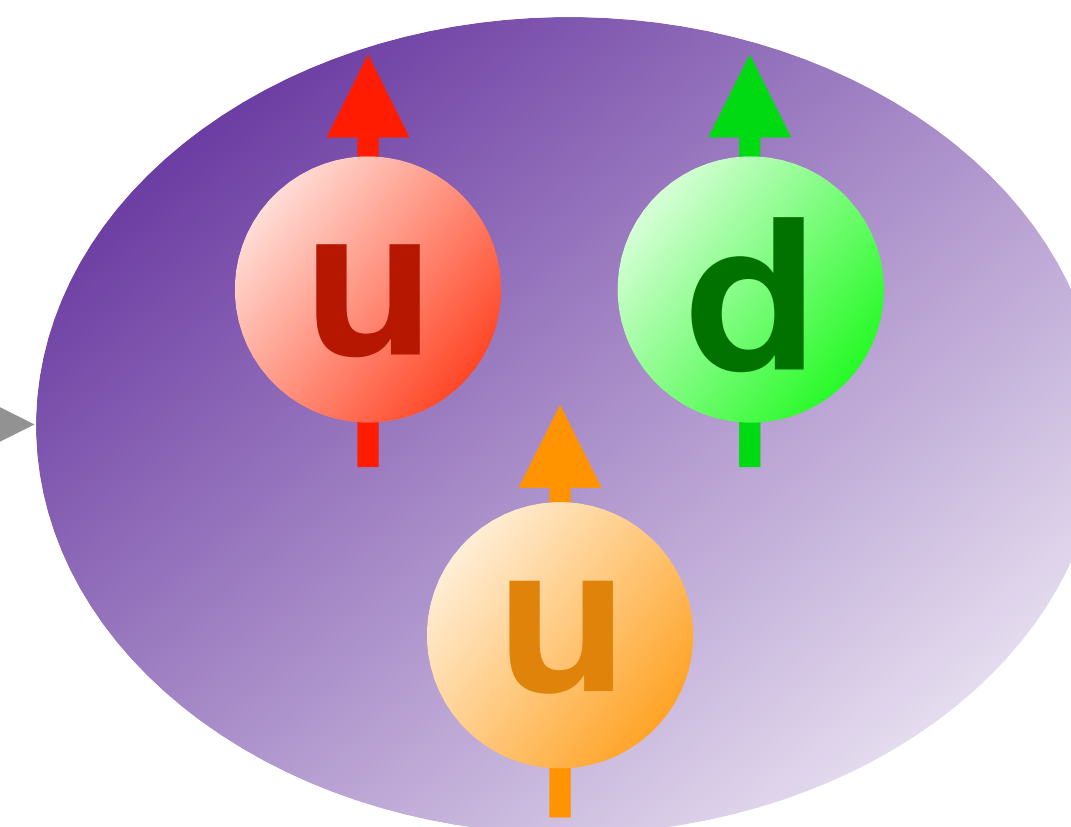
# The N- $\Delta$ transition

Proton (938 MeV)



Delta (1232 MeV)

$\gamma^*$ , E2, C2

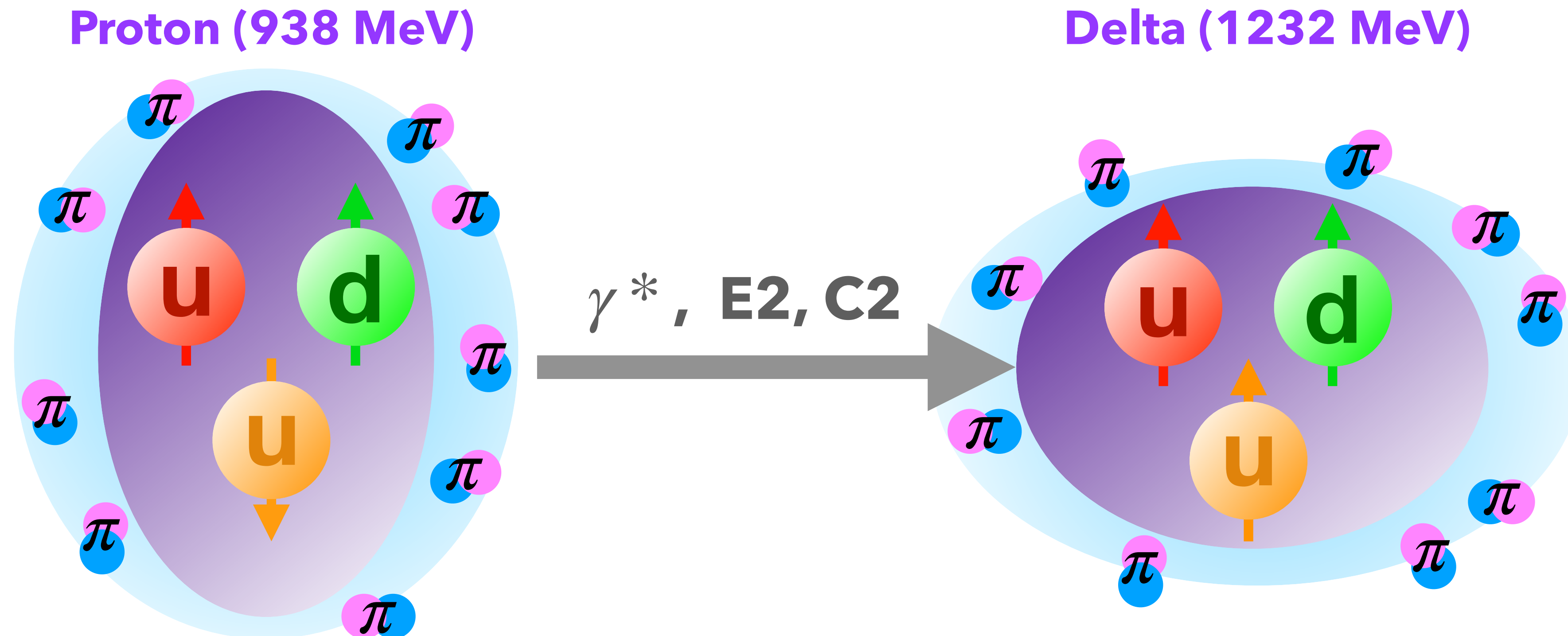


It can also be reached through a quadrupole (E2 or C2) transition from proton to delta.  
(The quadrupole amplitudes are associated with the existence of non-spherical components in the proton and Delta WF)

The quadrupole to dipole ratio (E2/M1 or C2/M1) is non-zero... Why?

Non-central (tensor) interactions between quarks can account for some of the spherical deviation, but not all...

# The N- $\Delta$ transition



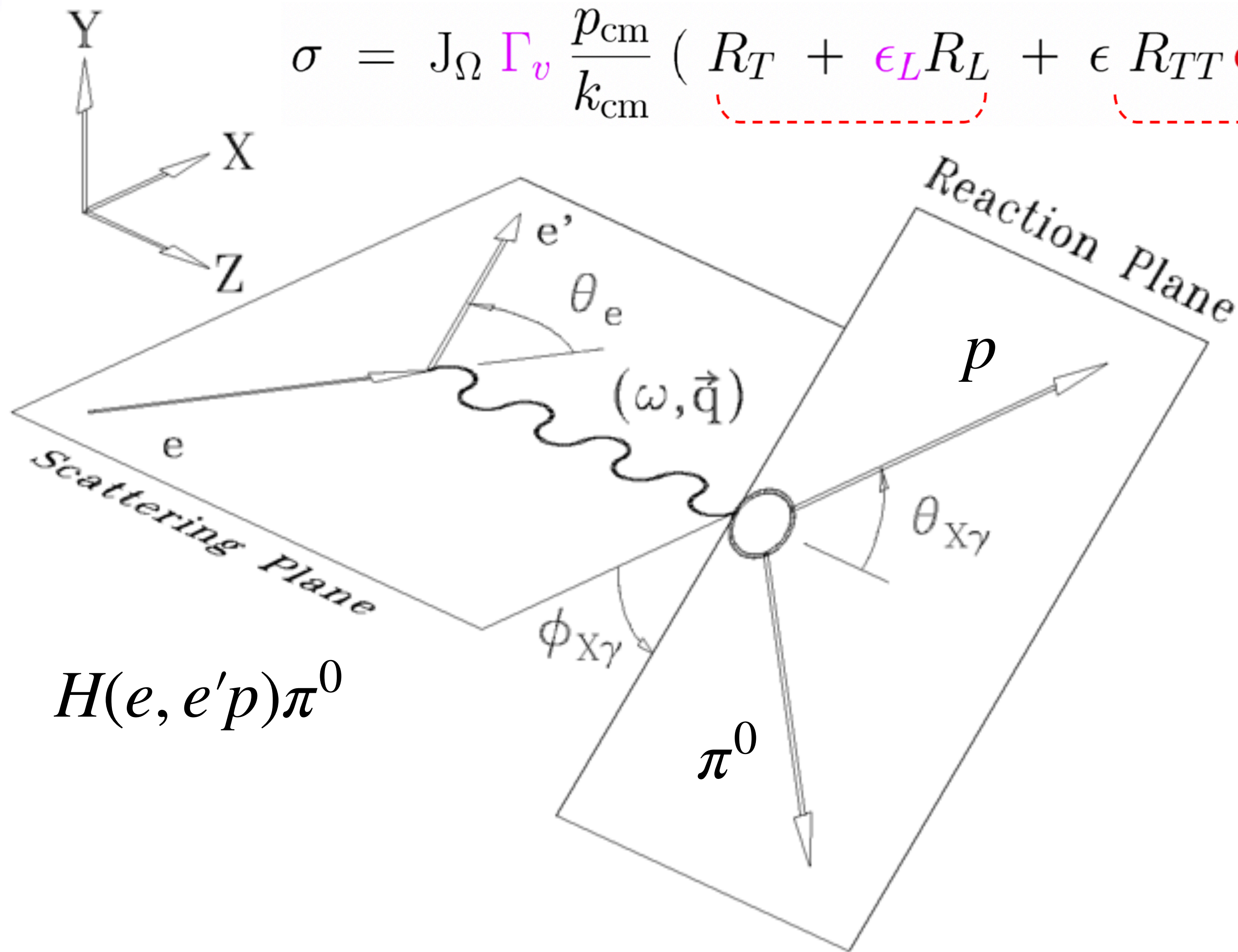
It can also be reached through a quadrupole (E2 or C2) transition from proton to delta. (The quadrupole amplitudes are associated with the existence of non-spherical components in the proton and Delta WF)

The quadrupole to dipole ratio (E2/M1 or C2/M1) is non-zero... Why?

The dynamics of a meson cloud are important to describe the structure of the nucleon.

# Experimental Methodology

$$\sigma = J_{\Omega} \Gamma_v \frac{p_{\text{cm}}}{k_{\text{cm}}} \left( \underbrace{R_T + \epsilon_L R_L}_{\text{M1}} + \underbrace{\epsilon R_{TT} \cos 2\phi_{X\gamma}}_{\text{EMR}} - \underbrace{\nu_{LT} R_{LT} \cos \phi_{X\gamma}}_{\text{CMR}} \right)$$

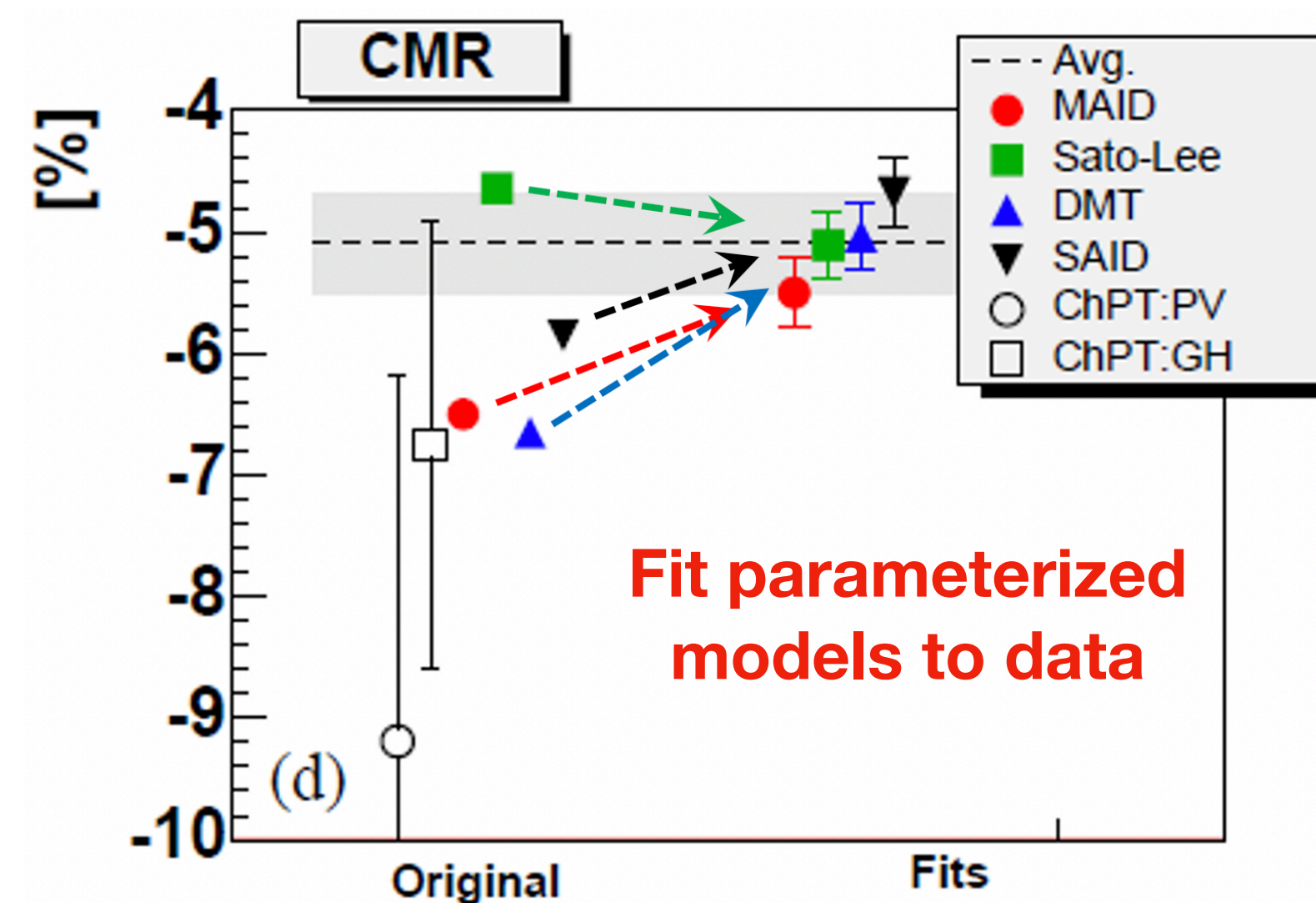


For a given  $\theta_{X\gamma}$ , one can measure at least 3  $\phi_{X\gamma}$  to simultaneously extract  $R_T + R_L, R_{TT}$  and  $R_{LT}$ .

$R_{TT}$  → sensitive to the **EMR**

$R_{LT}$  → sensitive to the **CMR**

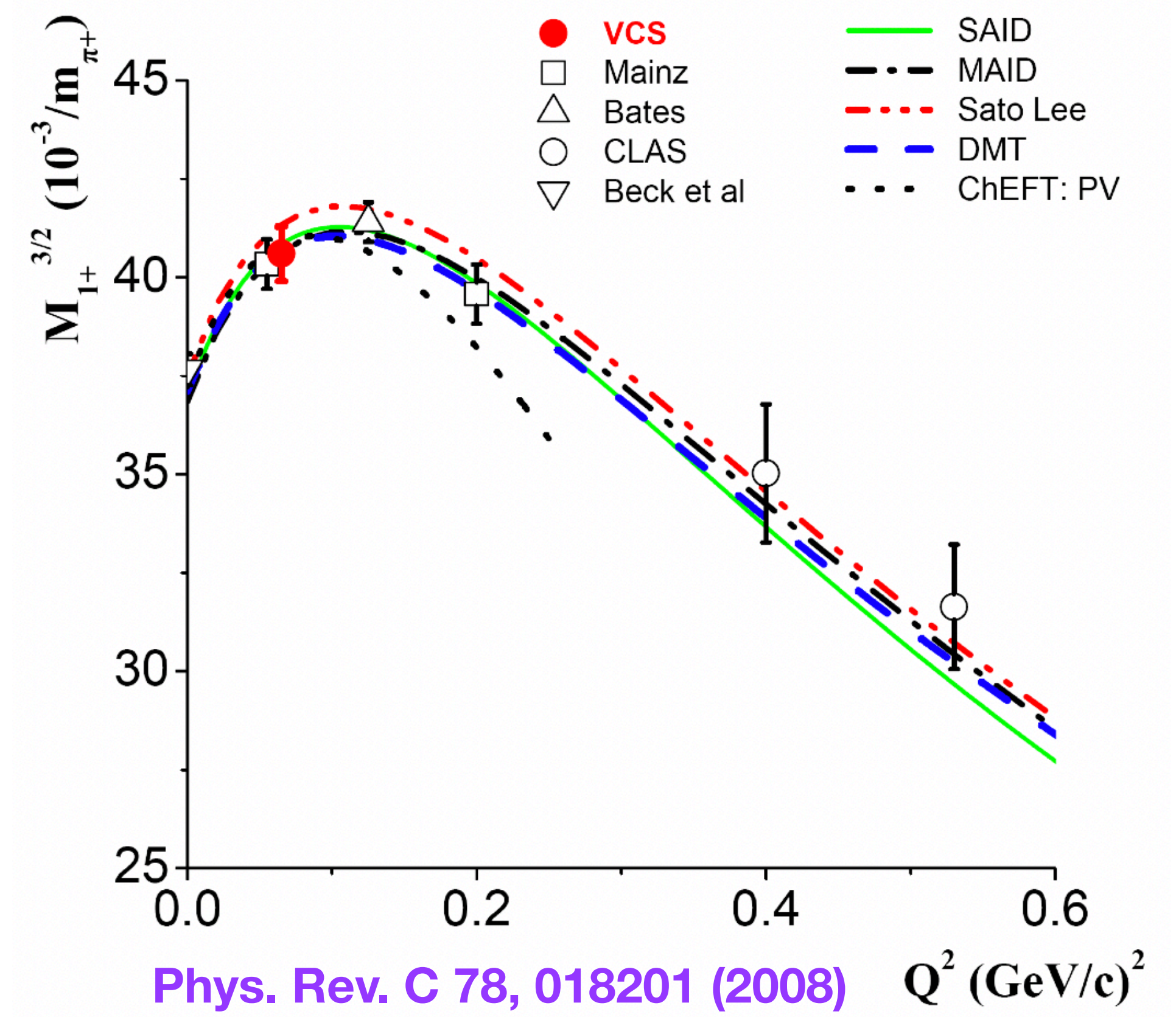
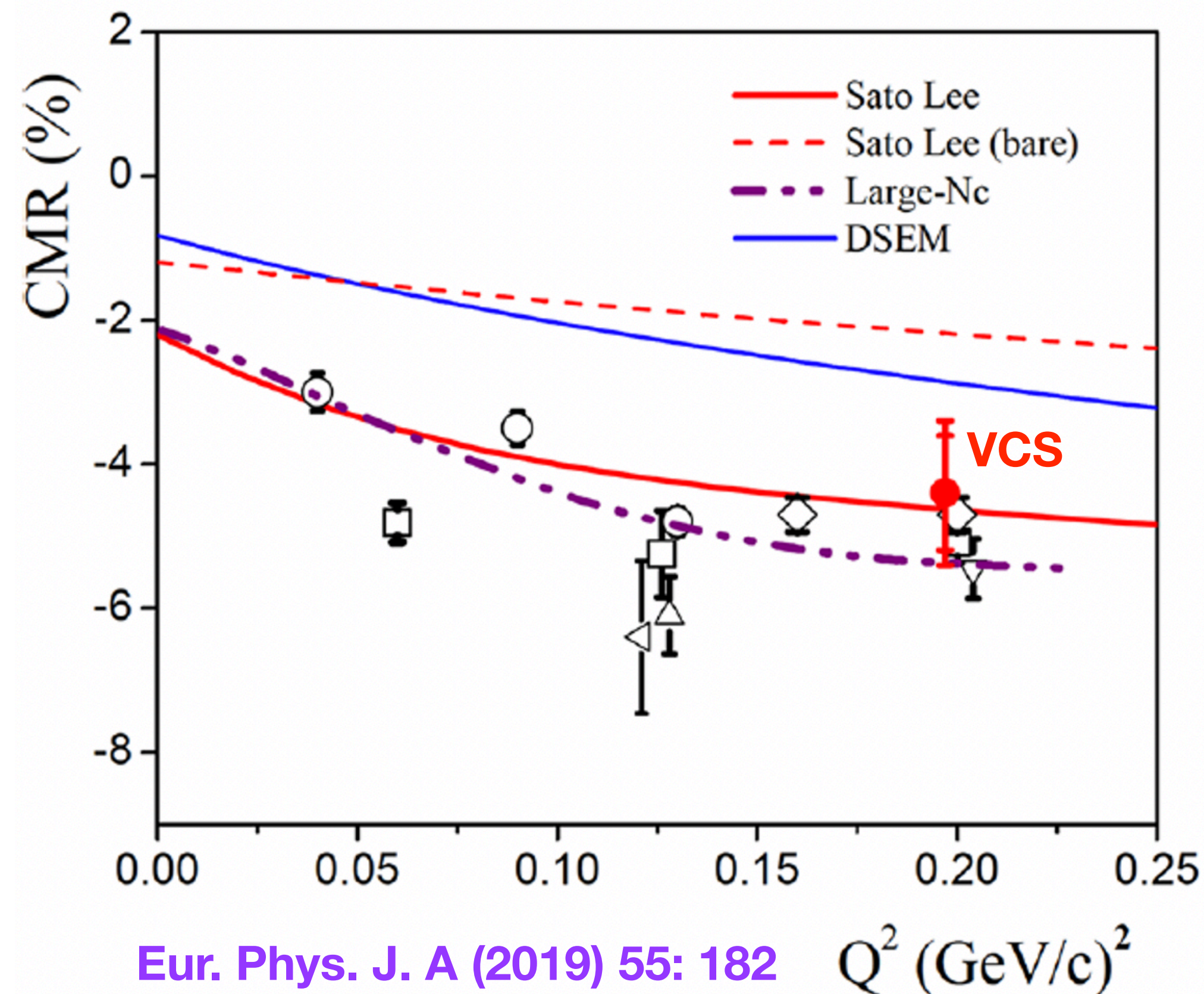
$R_T + R_L$  → sensitive to **M1**



# Cross-checks on Extraction Methods: VCS

$$\begin{aligned} \Delta^+ &\rightarrow N\pi && \sim 99\% && \text{H(e,e'p)\pi}^0, \text{H(e,e'\pi}^+)\text{n} \\ \Delta^+ &\rightarrow p\gamma && < 1\% && \text{VCS: H(e,e' p)\gamma} \end{aligned}$$

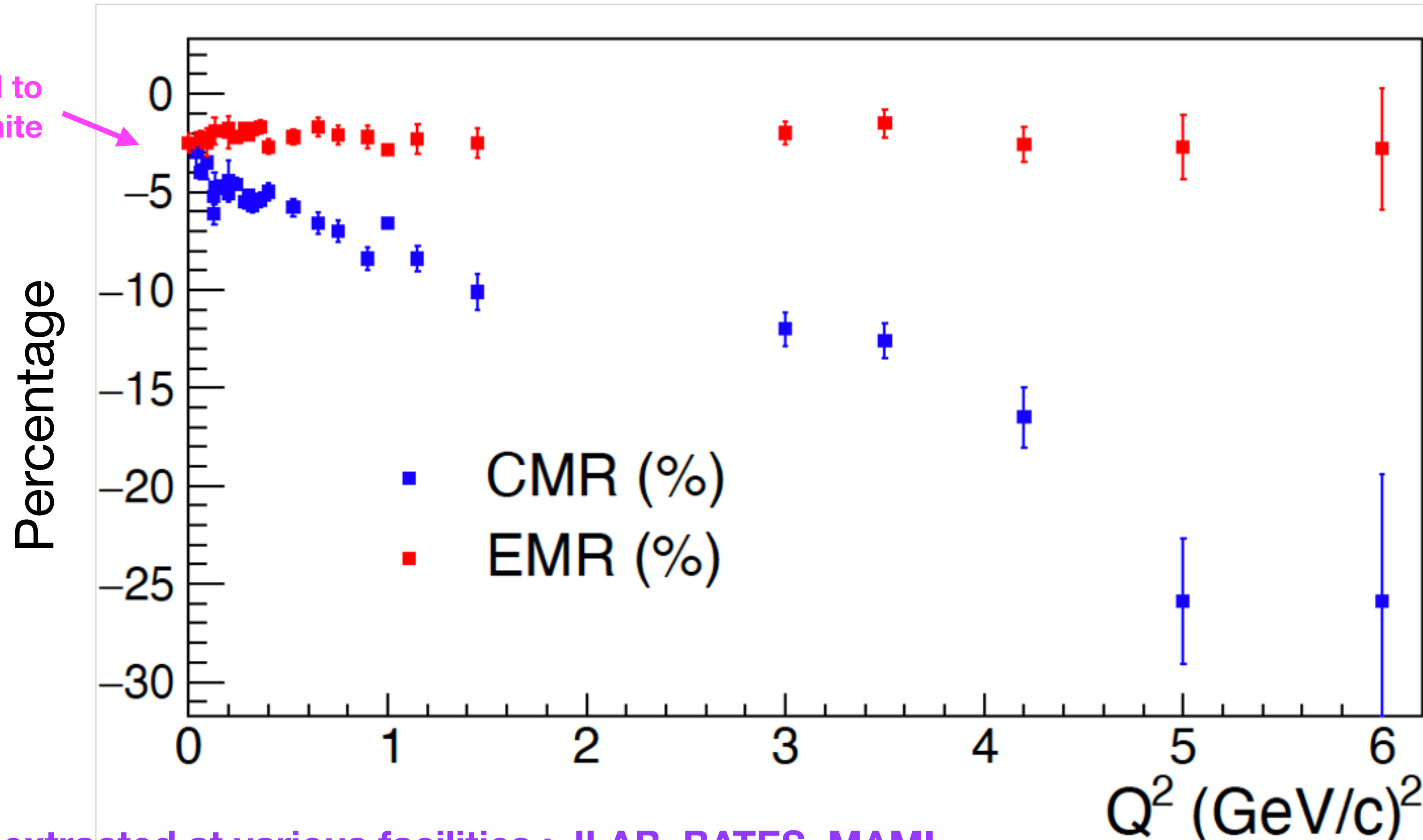
The excitation process is the same, but the backgrounds are very different:  
Stringent test of the theoretical framework & control of theoretical model uncertainties





# World data and status of TFFs

CMR & EMR predicted to converge at a small finite value as  $Q^2 \rightarrow 0$

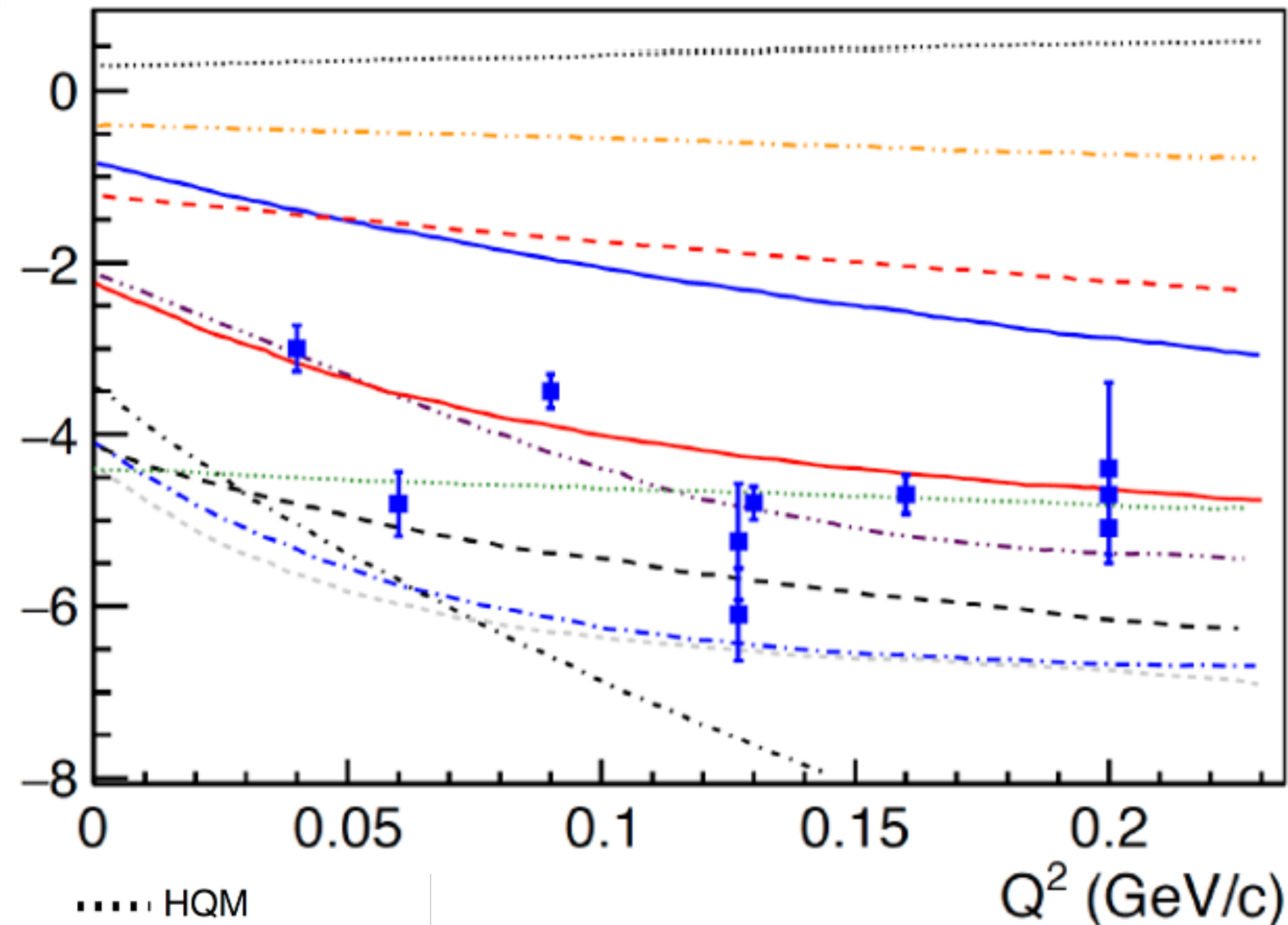


TFFs has been extracted at various facilities : JLAB, BATES, MAMI

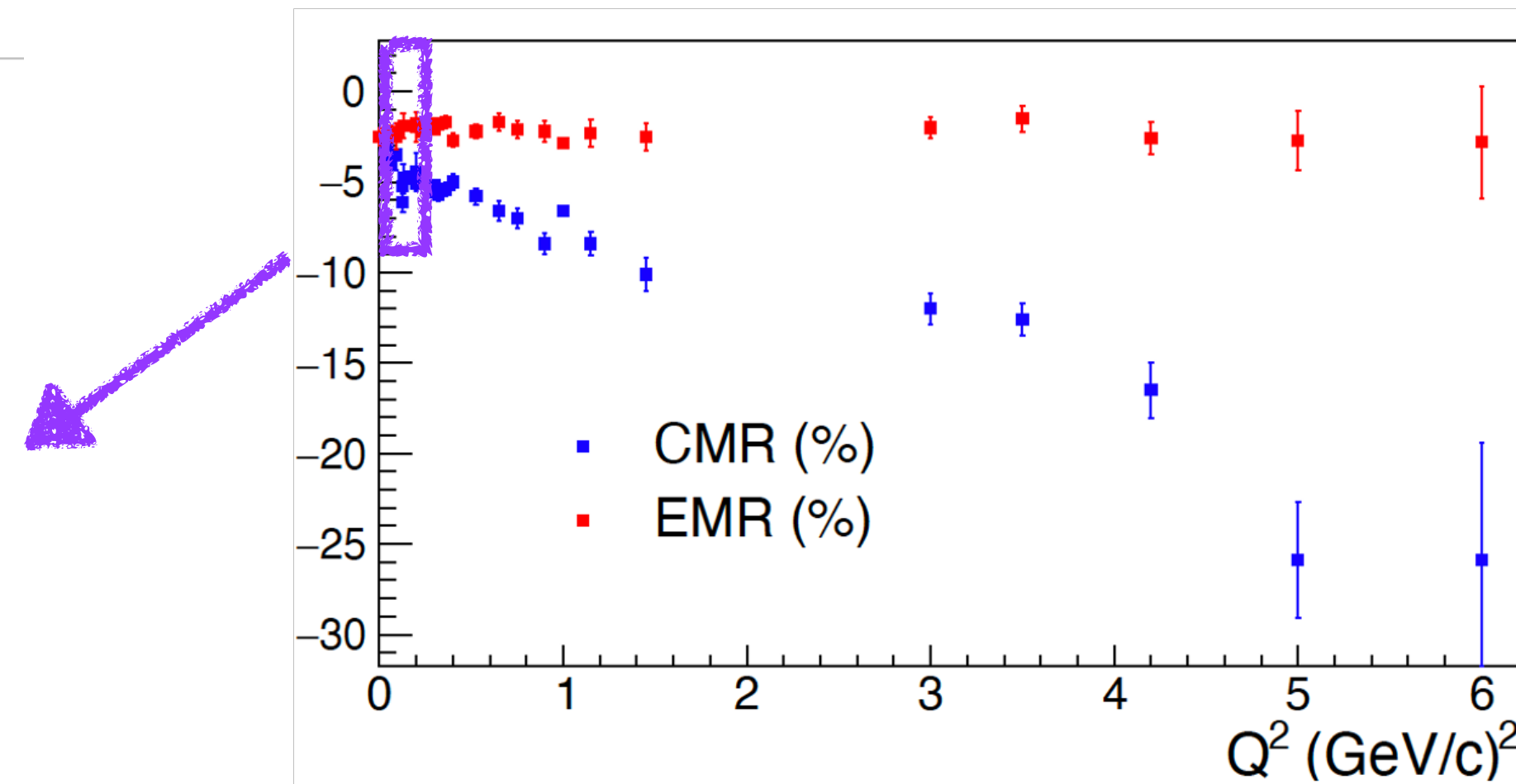
At large  $Q^2$ , no direct indication of EMR  $\rightarrow$  100% and CMR  $\rightarrow$  constant (predicted in pQCD regime)

# Low $Q^2$ $N$ - $\Delta$ transition form factors

CMR (%)



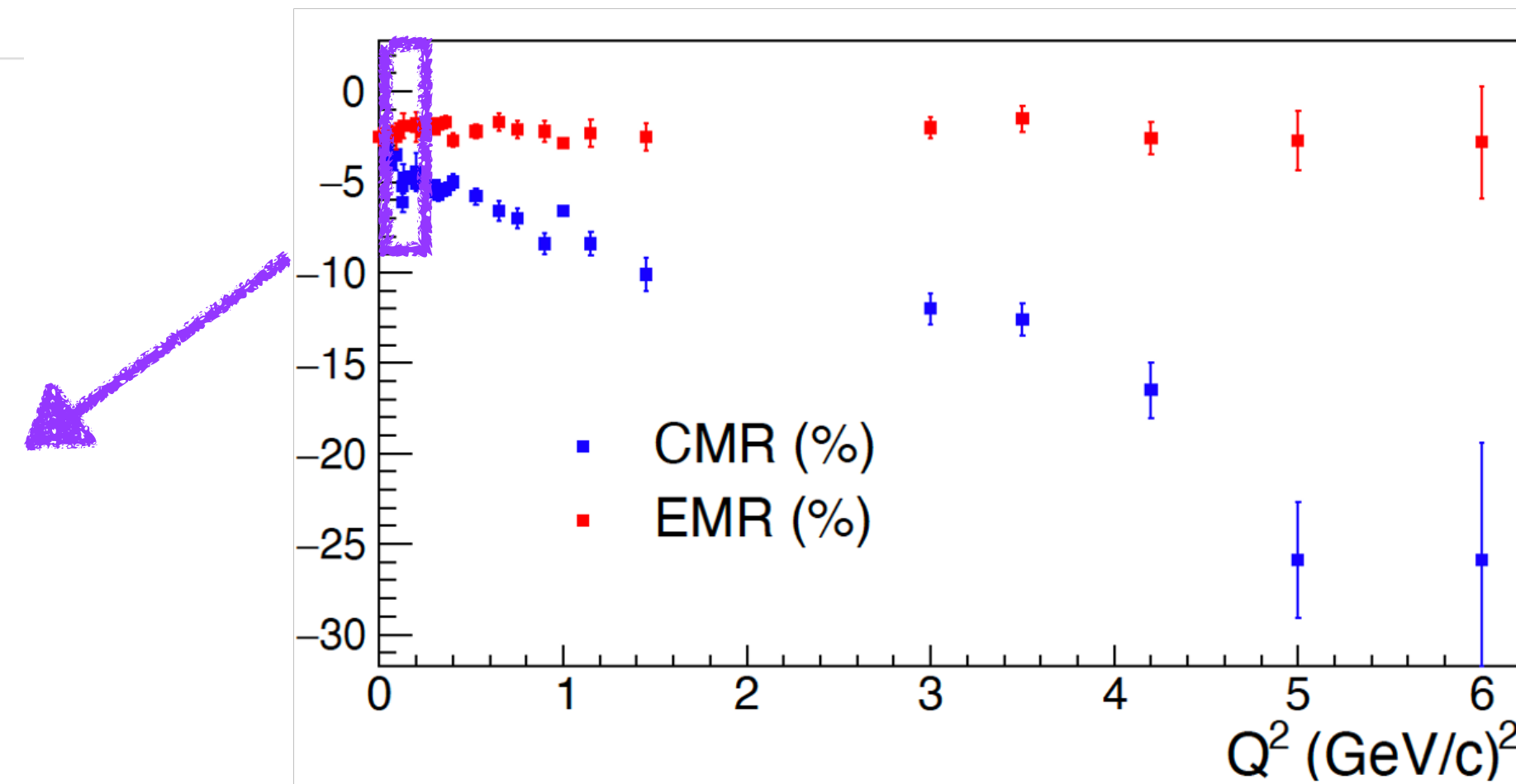
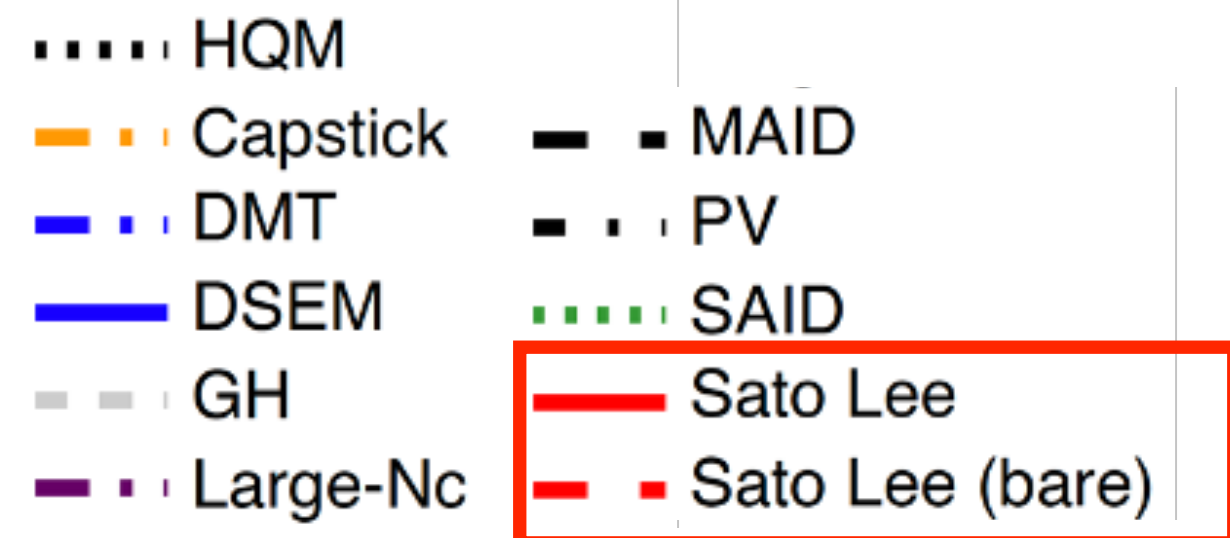
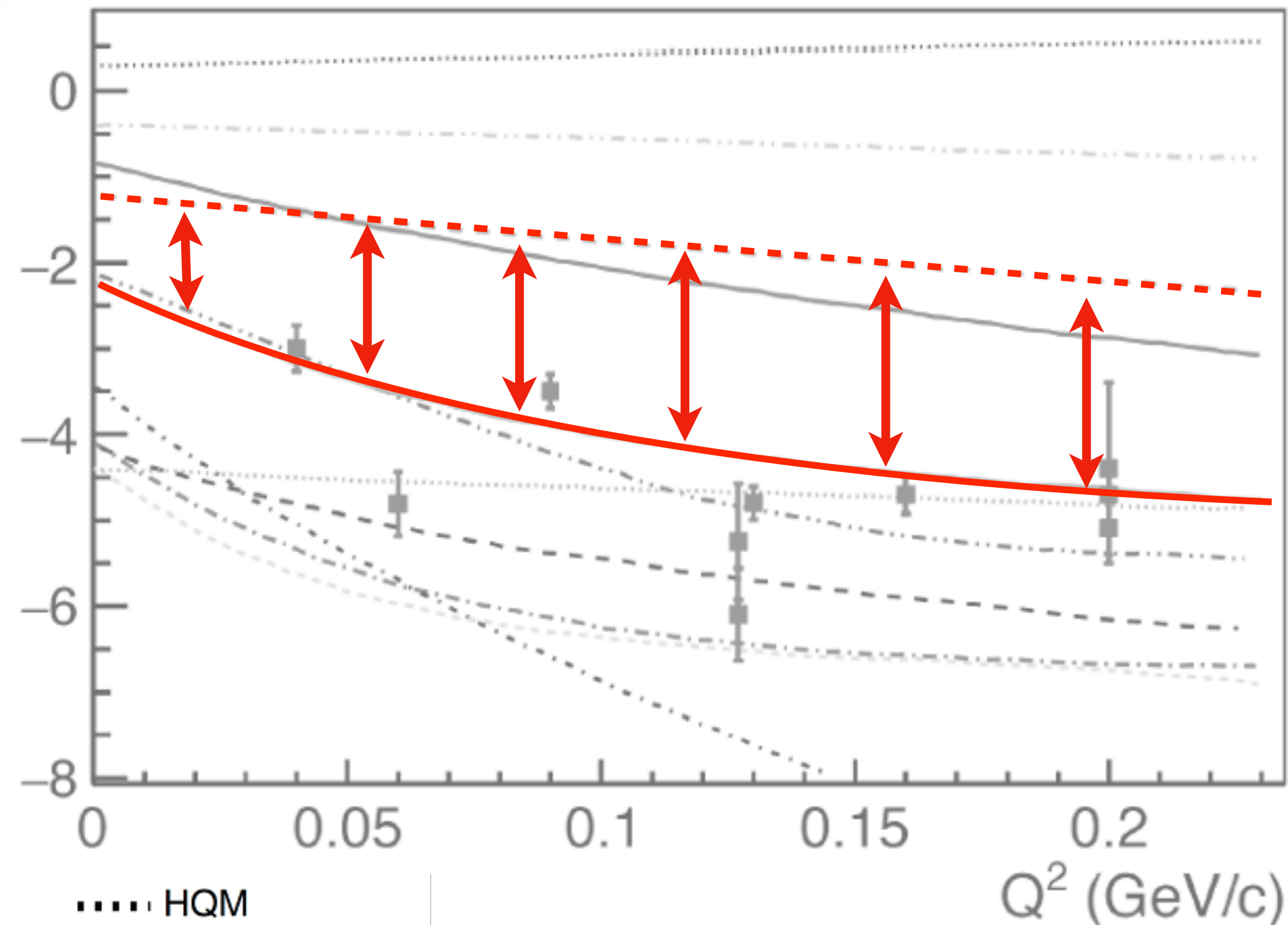
..... HQM  
 - - - Capstick  
 - · - DMT  
 — DSEM  
 - - - GH  
 - · - Large-Nc  
 - - - MAID  
 - · - PV  
 ..... SAID  
 — Sato Lee  
 - - - Sato Lee (bare)



- Low  $Q^2$  landscape is an important region to measure:
  - Mesonic cloud effects are predicted to be:
    - changing most rapidly over all  $Q^2$
  - Provides an excellent test bed for ChEFT and LQCD calculations
  - Tests the predicted convergence of EMR and CMR as  $Q^2 \rightarrow 0$ .
  - Sparsely measured region.

# Low $Q^2$ $N$ - $\Delta$ transition form factors

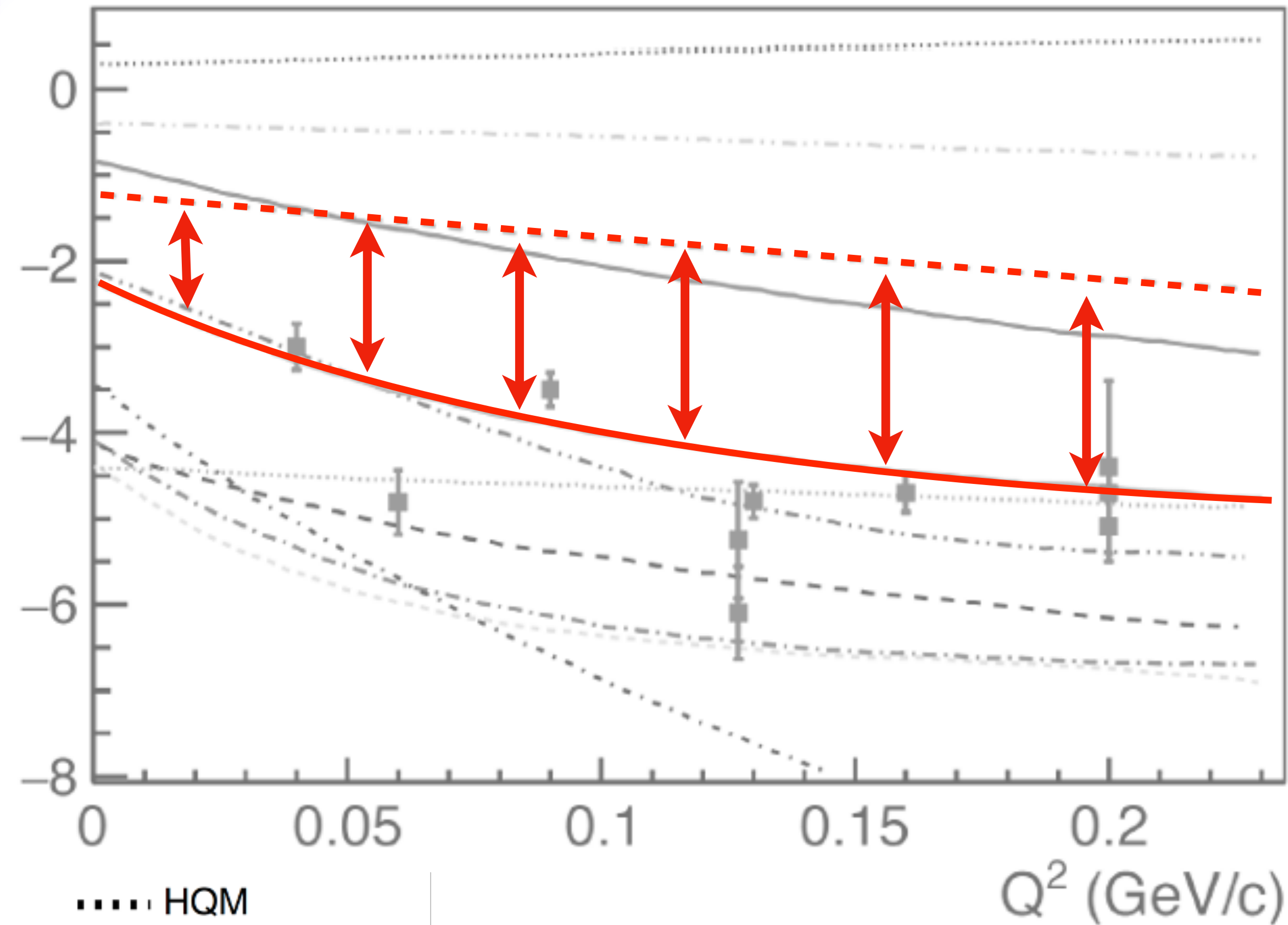
CMR (%)



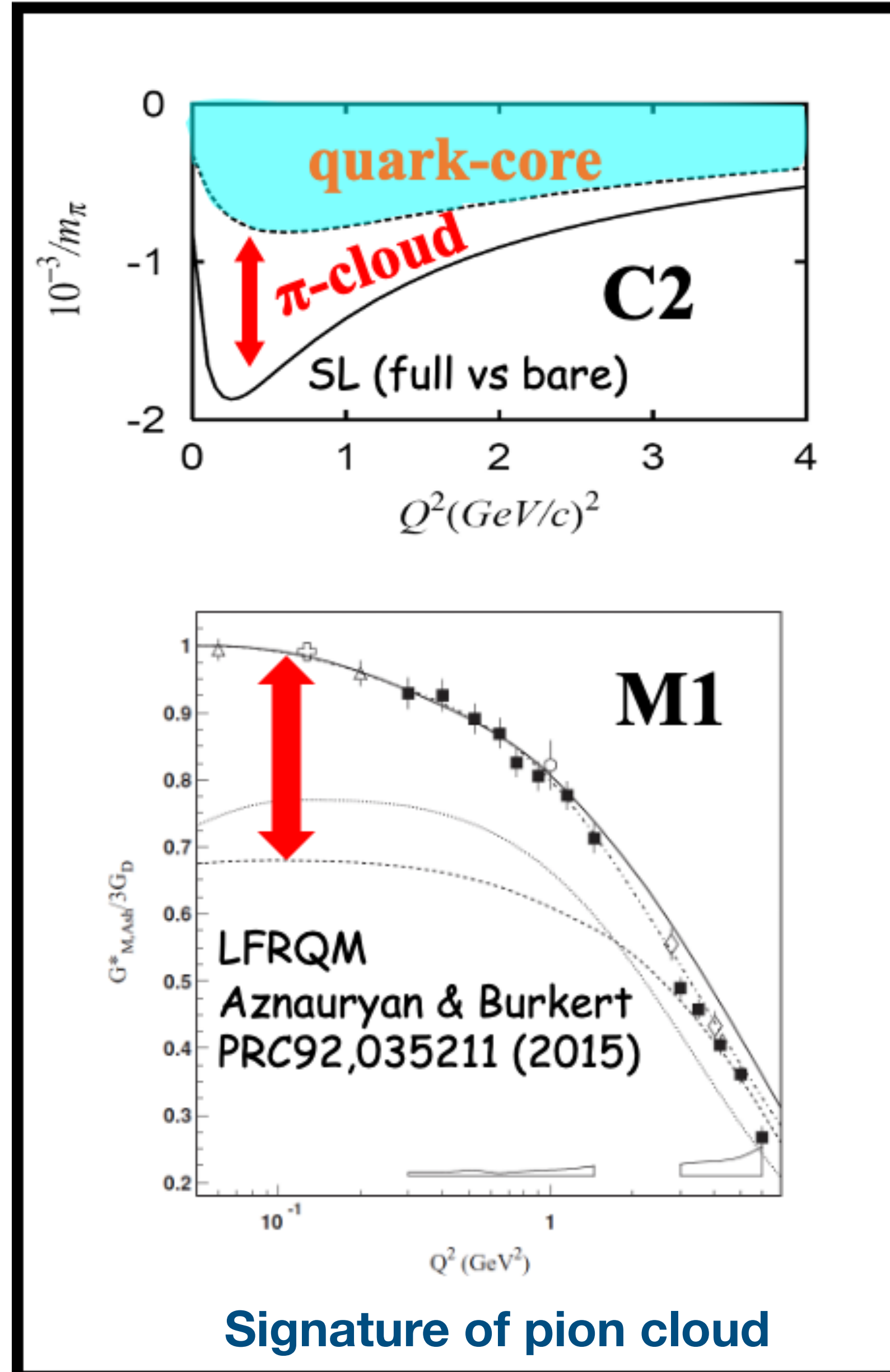
- Low  $Q^2$  landscape is an important region to measure:
  - Mesonic cloud effects are predicted to be:
    - changing most rapidly over all  $Q^2$
  - Provides an excellent test bed for ChEFT and LQCD calculations
  - Tests the predicted convergence of EMR and CMR as  $Q^2 \rightarrow 0$ .
  - Sparsely measured region.

# Low $Q^2$ $N$ - $\Delta$ transition form factors

CMR (%)



- ..... HQM
- Capstick
- DMT
- DSEM
- GH
- Large-Nc
- MAID
- PV
- SAID
- Sato Lee**
- - Sato Lee (bare)**



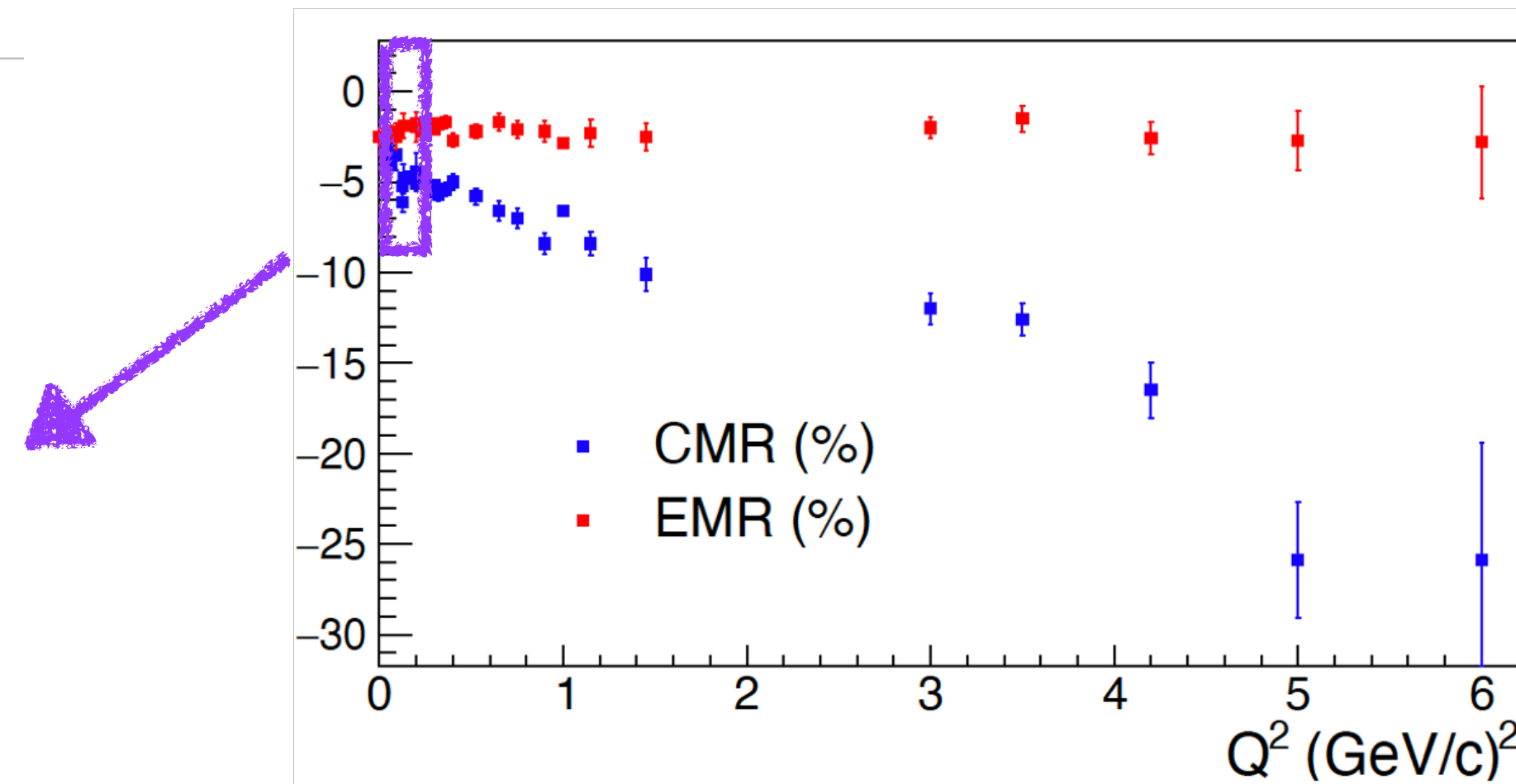
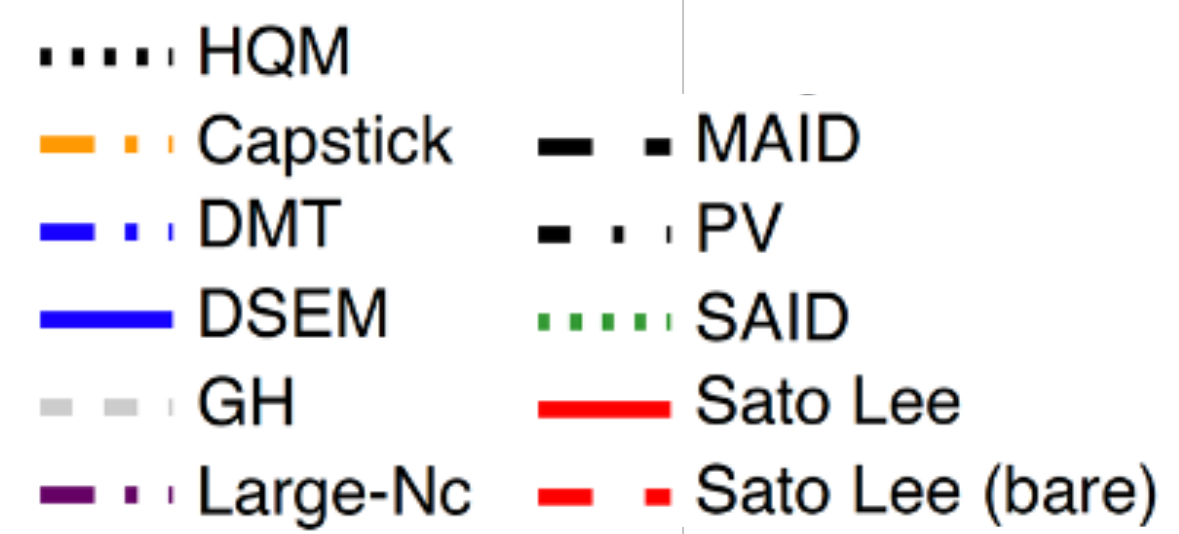
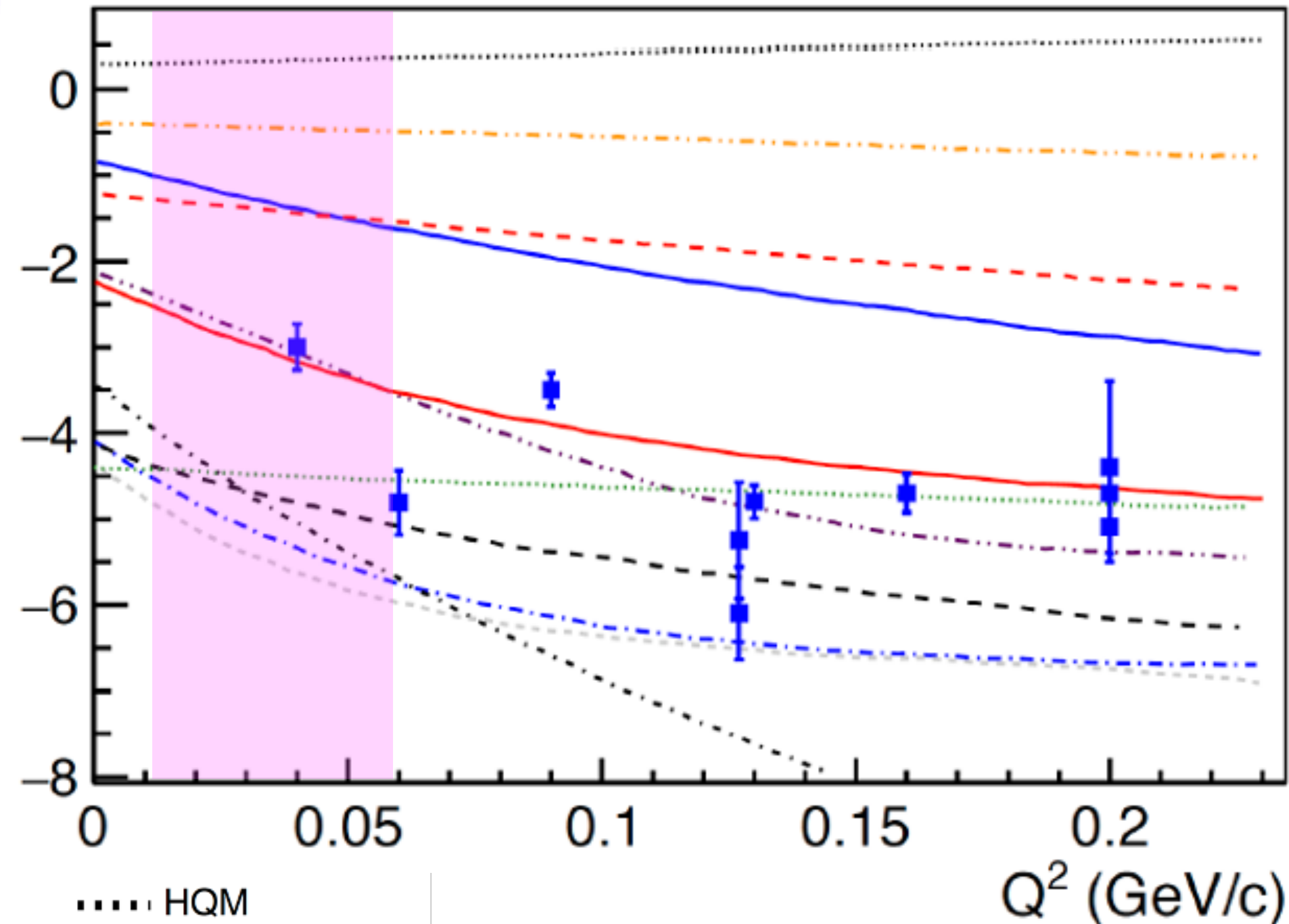
Dominant role of mesonic d.o.f. at large distance scale:

Mesonic cloud ~ 50% of the quadrupole amplitude magnitude & 1/3 of the magnetic dipole strength

Signature of pion cloud

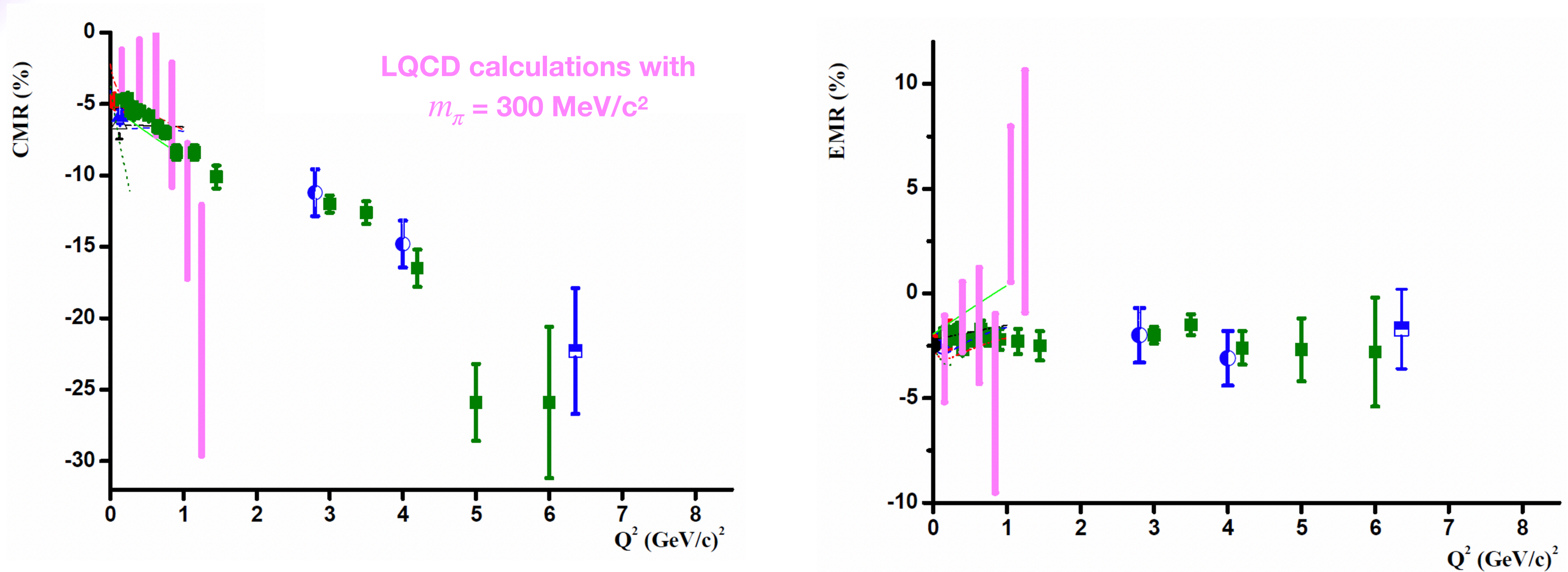
# Low $Q^2$ $N$ - $\Delta$ transition form factors

CMR (%) Region that new experiment will cover.



- **Low  $Q^2$  landscape is an important region to measure:**
  - Mesonic cloud effects are predicted to be:
    - changing most rapidly over all  $Q^2$
  - Provides an excellent test bed for ChEFT and LQCD calculations
  - Tests the predicted convergence of EMR and CMR as  $Q^2 \rightarrow 0$ .
  - **Sparsely measured region.**

# Lattice Calculations



- Updated LQCD calculations are in progress → new calculations will have a physical pion mass and uncertainties comparable to experiment.
- Low  $Q^2$  data will provide a precision benchmark for LQCD calculations.

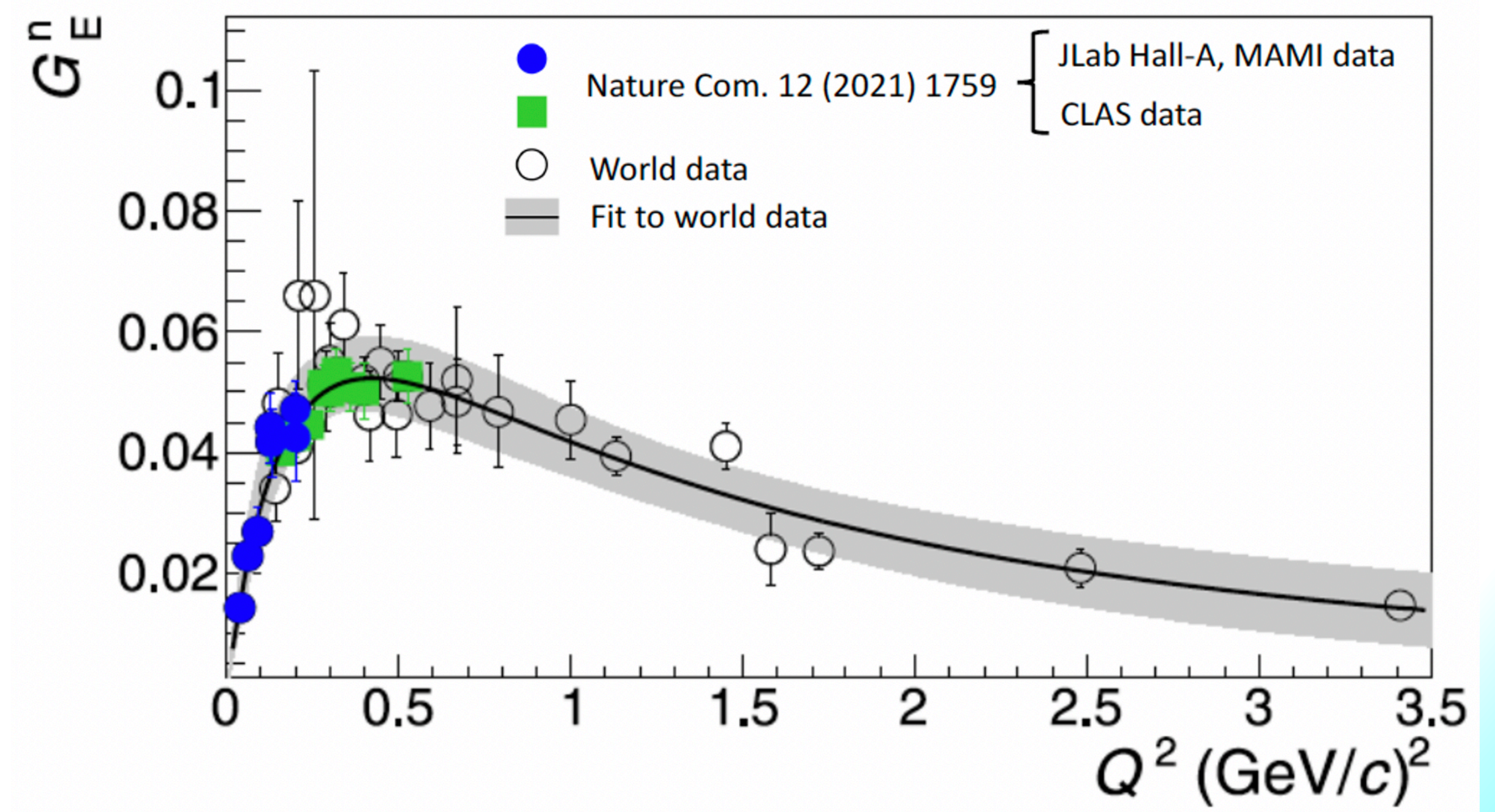
# Connections to the neutron structure

There are long-known relations between the TFFs and the neutron FFs.

- Pascalutsa, V. & Vanderhaeghen, M. : Phys. Rev. D 76 (2007) [Large-Nc]
- Grabmayr, P. & Buchmann, A. J. : Phys. Rev. Lett. 86 (2001) [SU(6)]

$G_E^n$  extraction from TFFs show strong agreement with world data.

- Allows access to low- $Q^2$  region where direct measurement of  $G_E^n$  is difficult.



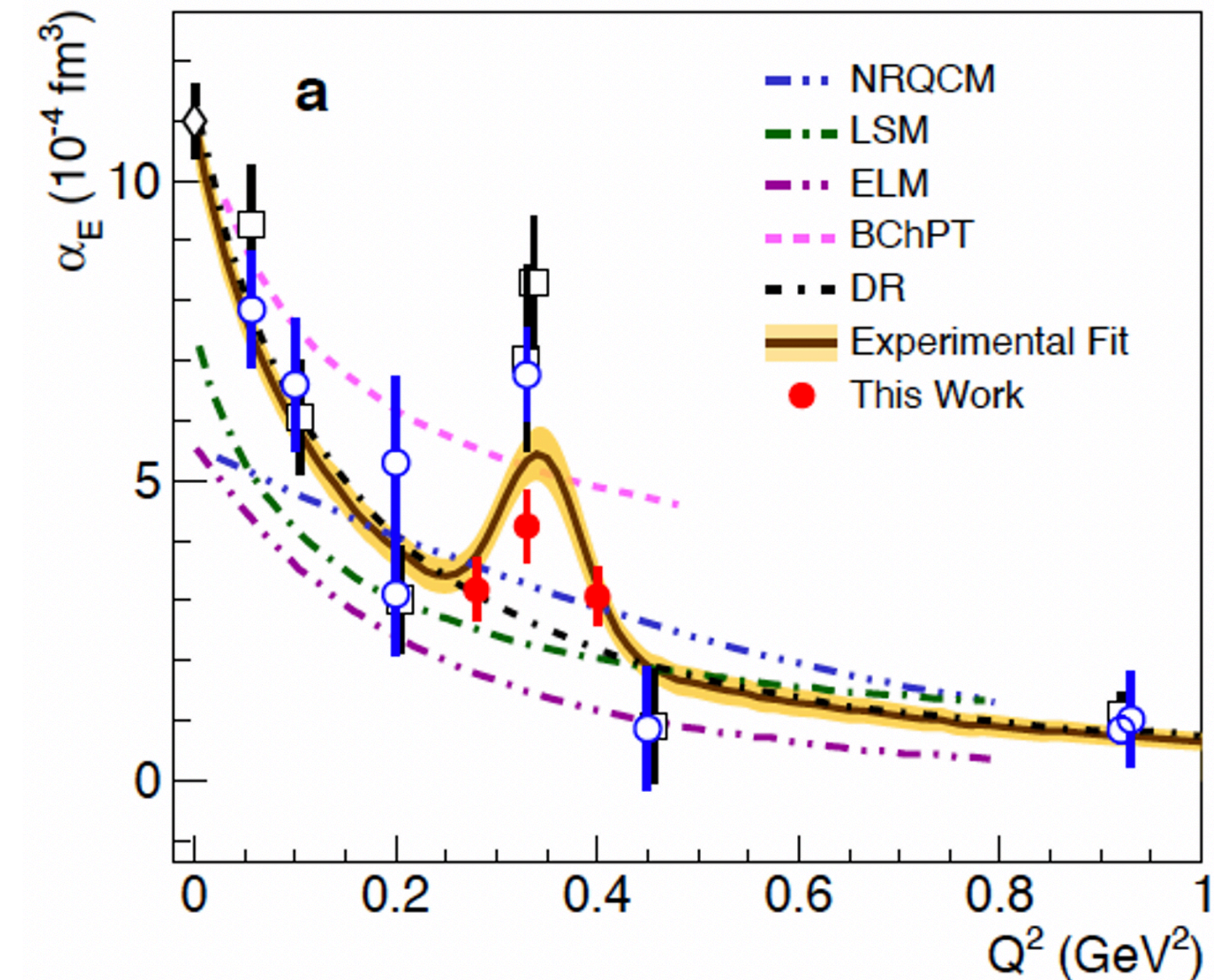
# Impact on other domains of nuclear physics

- Generalized polarizabilities (GPs) of the proton:

- The TFFs enter as an input in the VCS cross section over the  $\Delta$  resonance region - their precise knowledge is necessary for the precise extraction of the GPs from the measured cross sections

- Physics of interest:

- Electric polarizability puzzle
- Interplay of paramagnetism & diamagnetism in the proton
- Extraction of the polarizability radii and imaging of the induced polarization density.



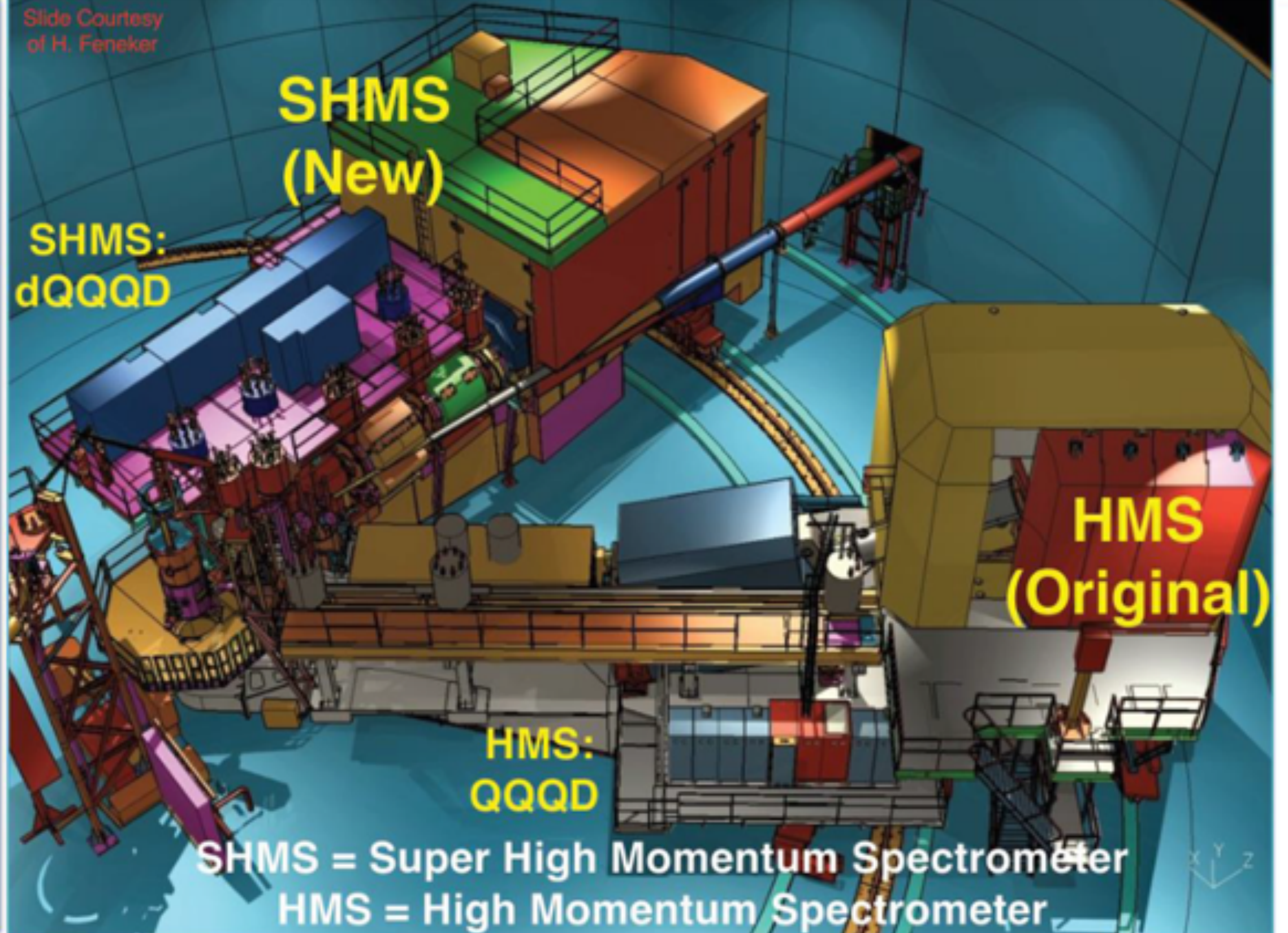


# New Experiment

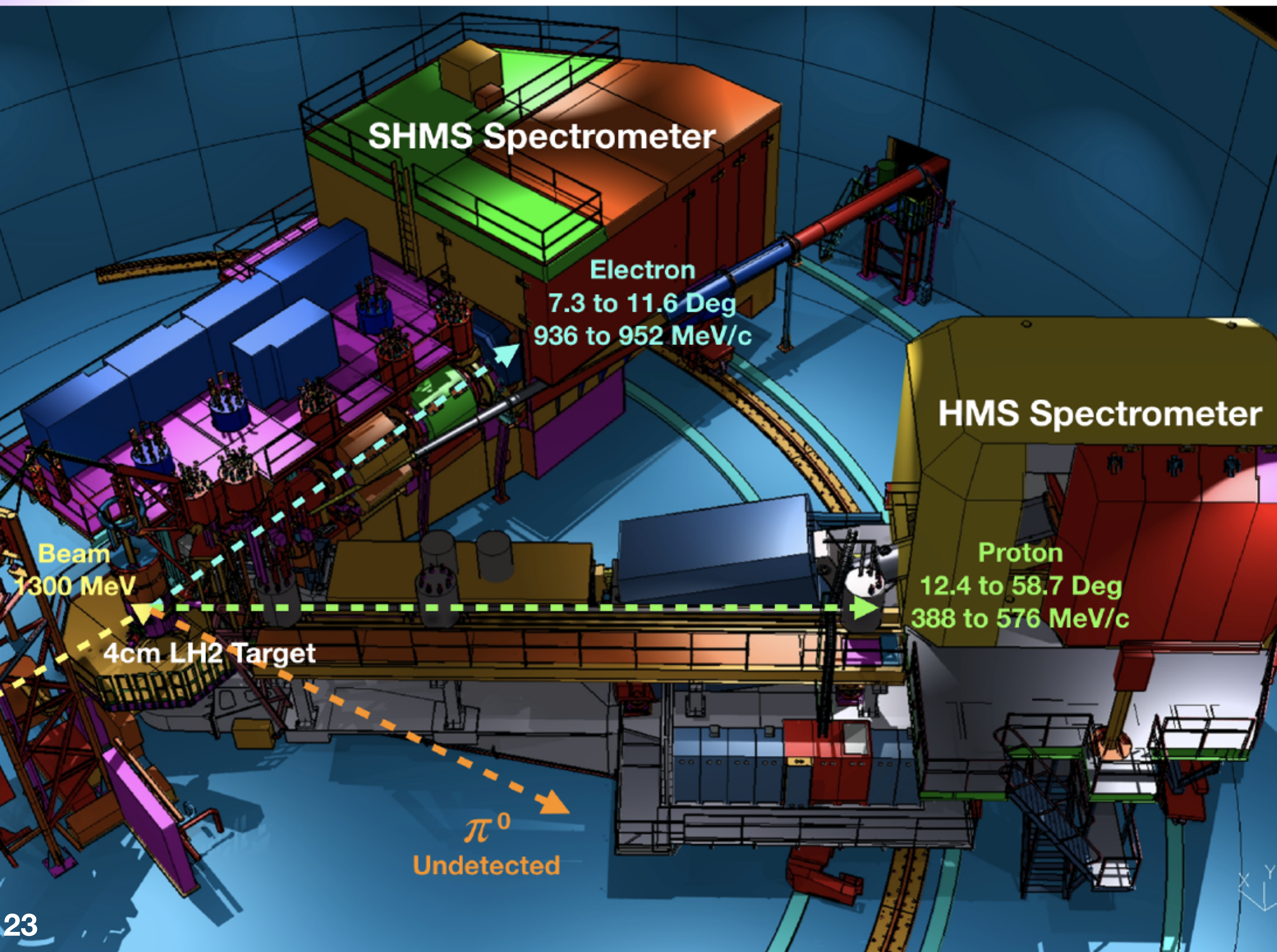
## Hall C HMS and SHMS



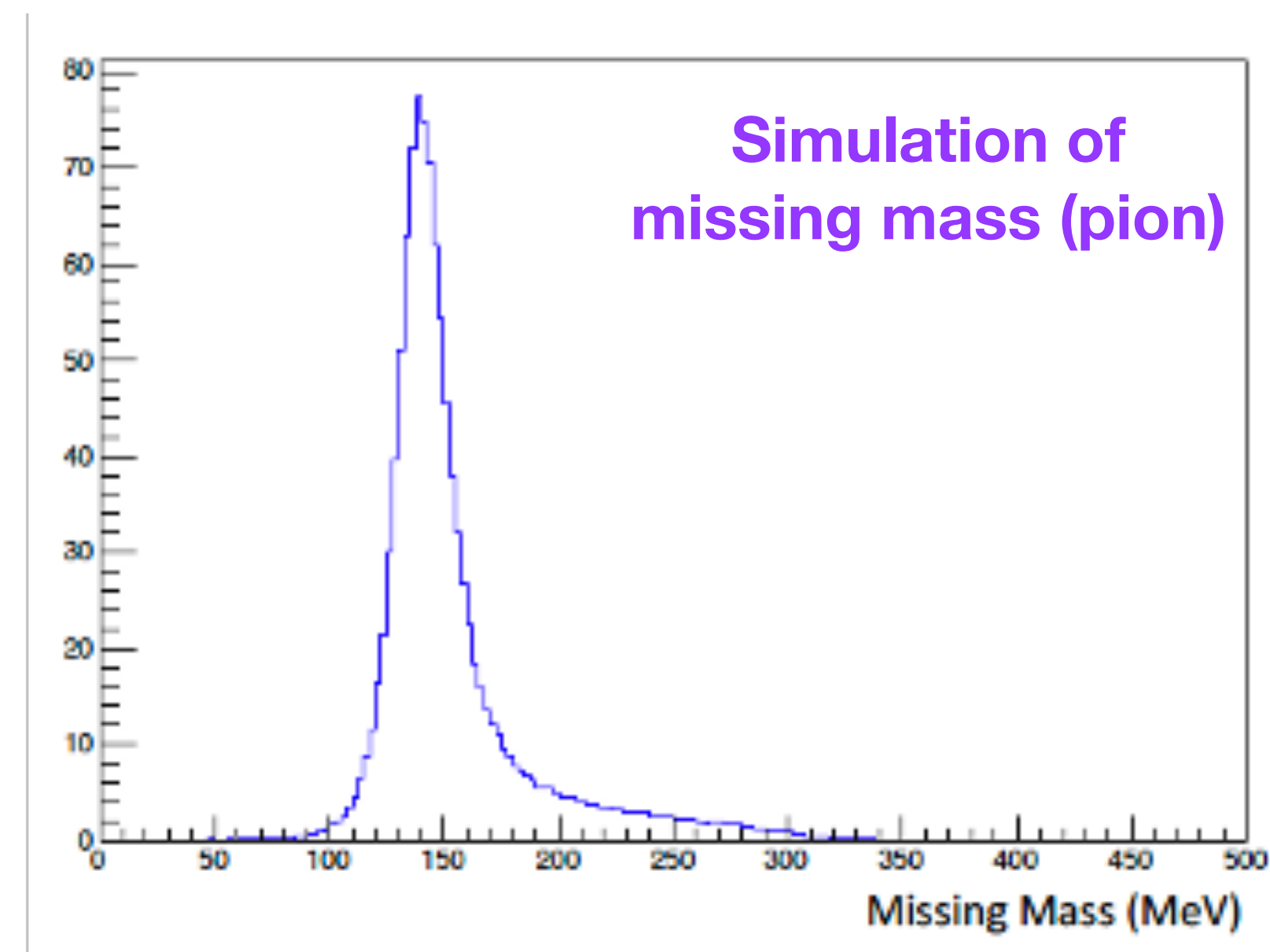
- SHMS:**
  - 11-GeV Spectrometer
  - Partner of existing 6-GeV HMS
- MAGNETIC OPTICS:**
  - Point-to Point QQD for easy calibration and wide acceptance.
  - Horizontal bend magnet allows acceptance at forward angles ( $5.5^\circ$ )
- Detector Package:**
  - Drift Chambers
  - Hodoscopes
  - Cerenkovs
  - Calorimeter
  - All derived from existing HMS/SOS detector designs
- Well-Shielded Detector Enclosure**
- Rigid Support Structure**
  - Rapid & Remote Rotation
  - Provides Pointing Accuracy & Reproducibility demonstrated in HMS



# Experimental Setup



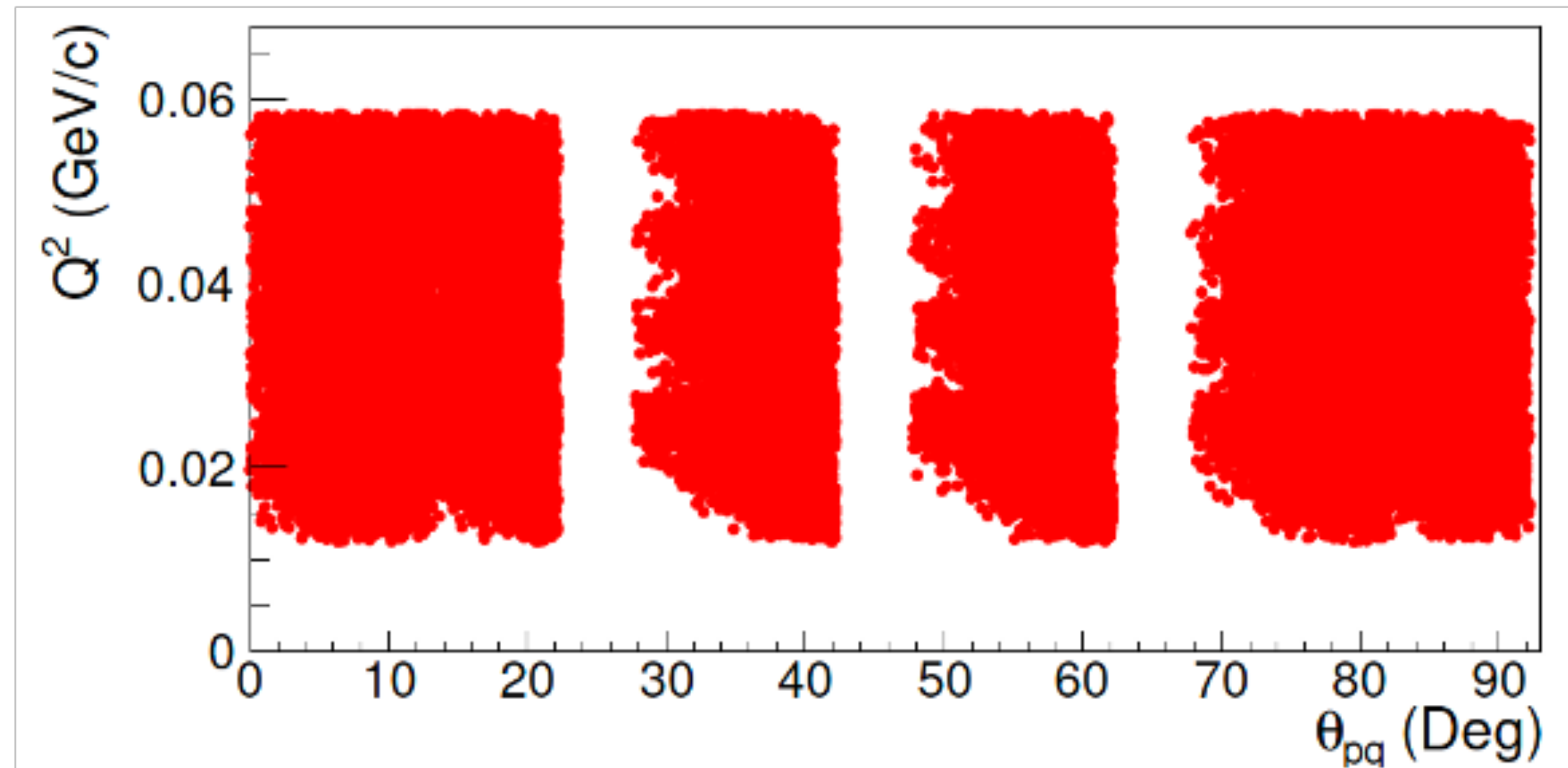
- Standard Hall-C equipment
  - 1300 MeV electron beam
  - Detect proton and electron in coincidence
  - Reconstruct pion from missing mass.



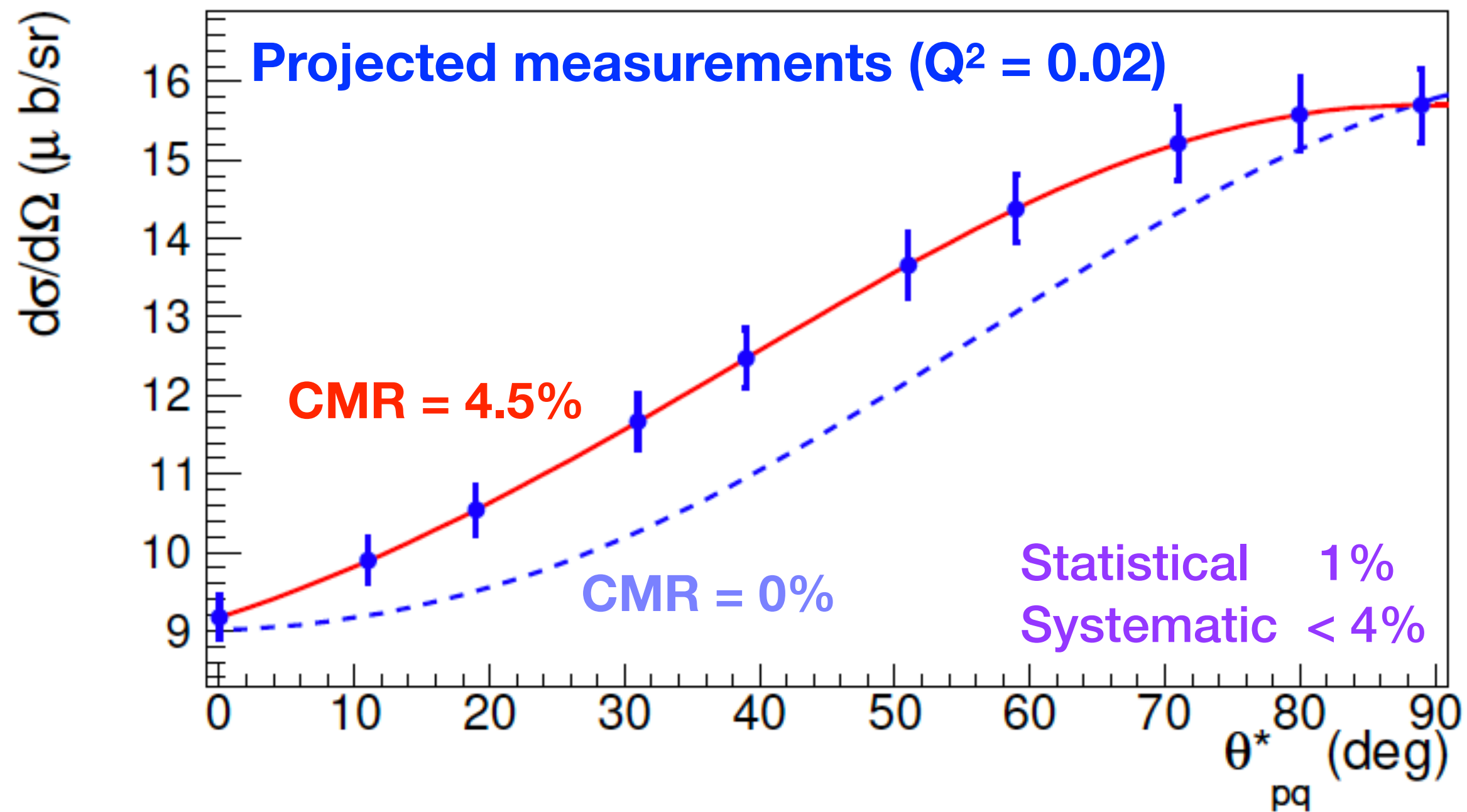
# Measurement Settings

Setting	SHMS $\theta$ (deg)	SHMS P (MeV/c)	HMS $\theta$ (deg)	HMS P (MeV/c)	S/N	Time (hrs)
1a	7.29	952.26	18.77	532.53	2	7
2a			25.17	527.72	2	7
3a			33.7	506.61	3.2	6
4a			42.15	469.66	4.3	5
5a			50.44	418.56	4.9	5
6a			54.47	388.38	4.9	5
7a			12.37	527.72	2.7	6
1b	8.95	946.93	22.01	547.54	1.2	6
2b			28.24	542.61	1.4	6
3b			36.52	520.95	2.5	5
4b			44.64	483.08	3.4	4
5b			52.68	430.78	3.7	4
6b			56.53	399.92	3.5	4
7b			12.46	535.98	1.6	5
1c	10.37	941.61	24.40	562.00	1.5	9
2c			30.47	556.95	1.9	9
3c			38.52	534.79	3.5	6
4c			46.47	496.06	4.4	6
5c			54.17	442.64	4.8	6
6c			57.85	411.16	4.8	6
7c			12.69	543.24	2	6
1d	11.63	936.28	26.24	575.96	1.8	12
2d			32.16	570.80	2.5	11
3d			40.01	548.17	4.5	8
4d			47.73	508.64	5.5	8
5d			55.18	454.17	6.9	7
6d			58.71	422.13	6	8
7d			12.47	548.17	2.1	10

- Cover a  $Q^2$  range of 0.015 to 0.055 (GeV/c)<sup>2</sup>
  - 28 arm configurations
  - Coverage for 9  $Q^2$  bins.
  - 8 days production
  - 3 days other (dummy, calibration, etc..)

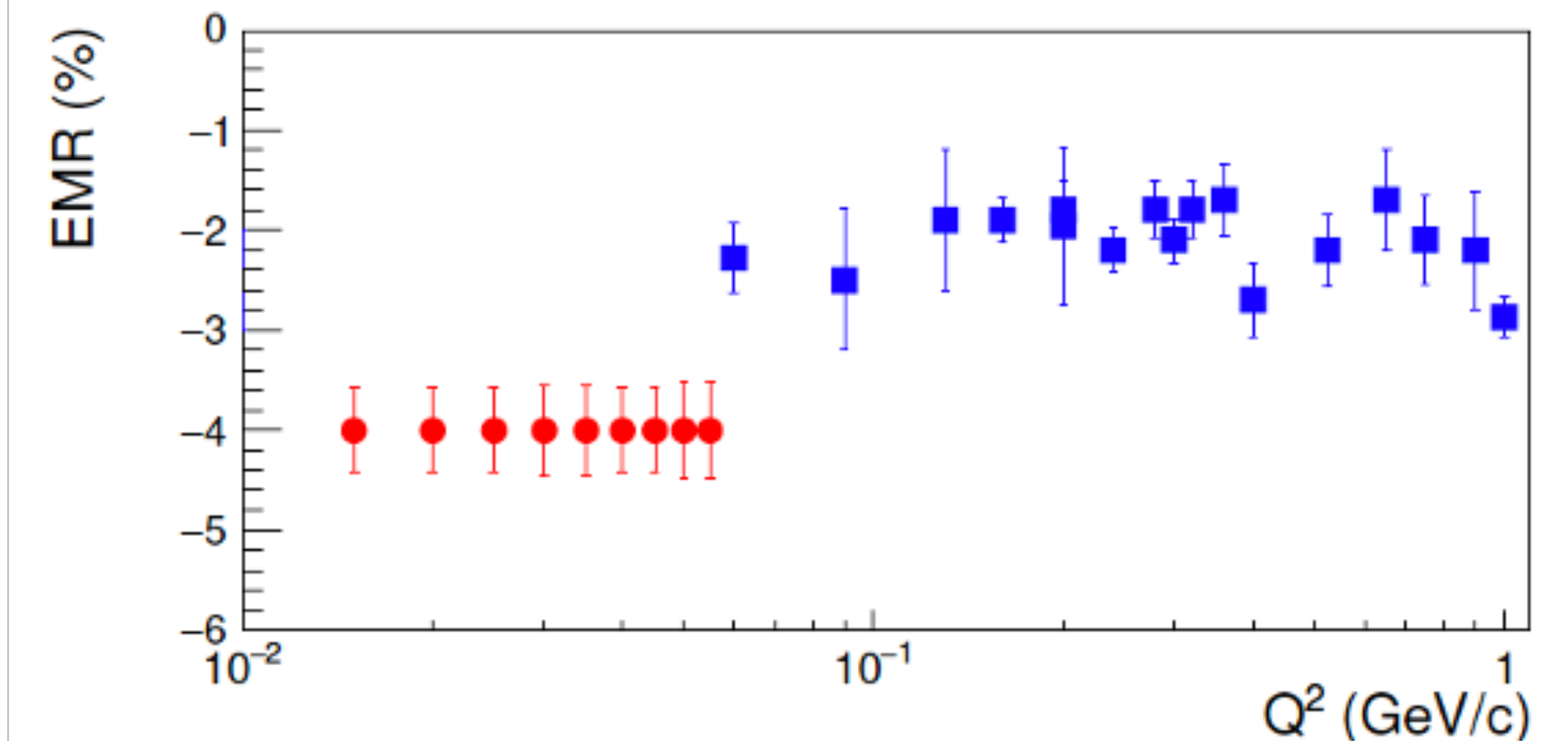
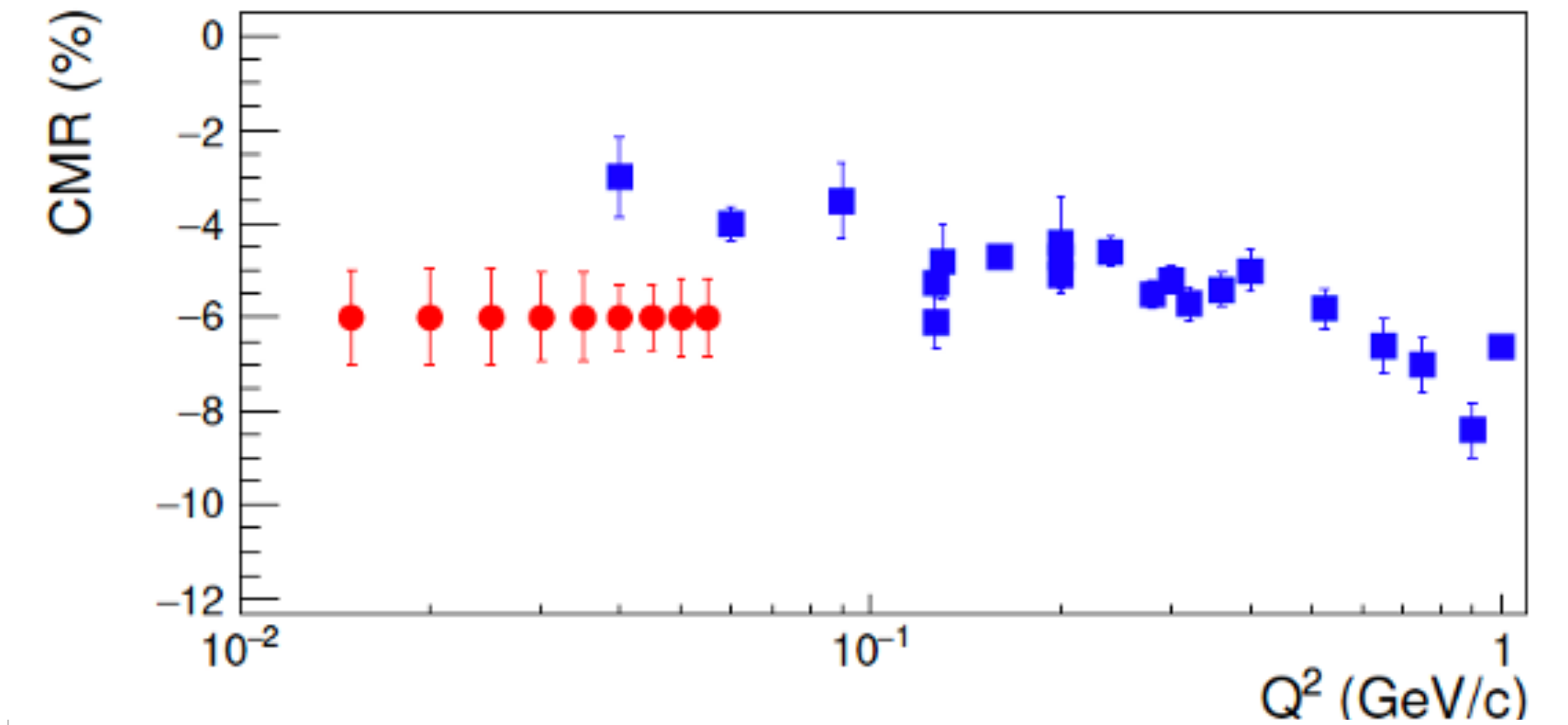


# Projected CMR and EMR measurements

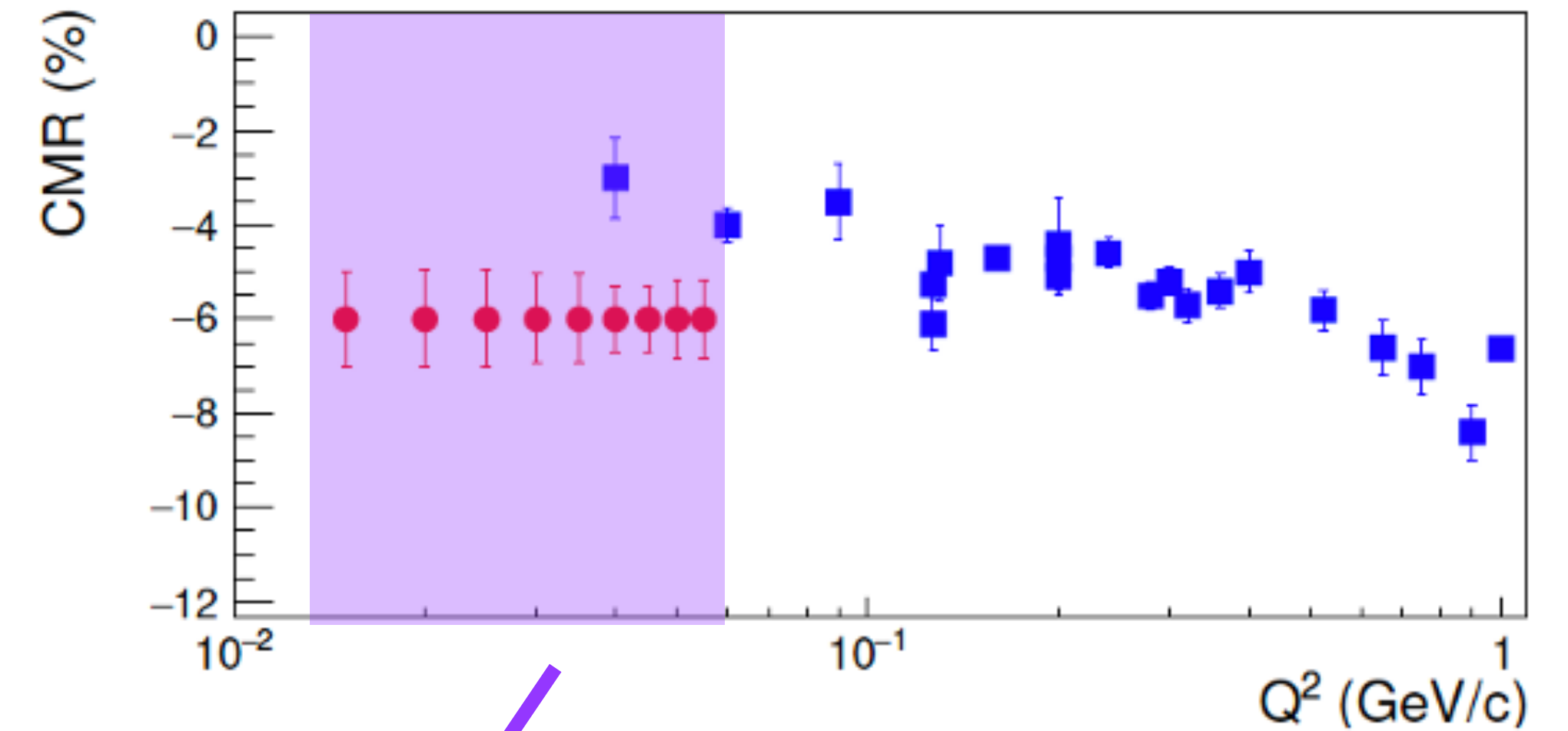
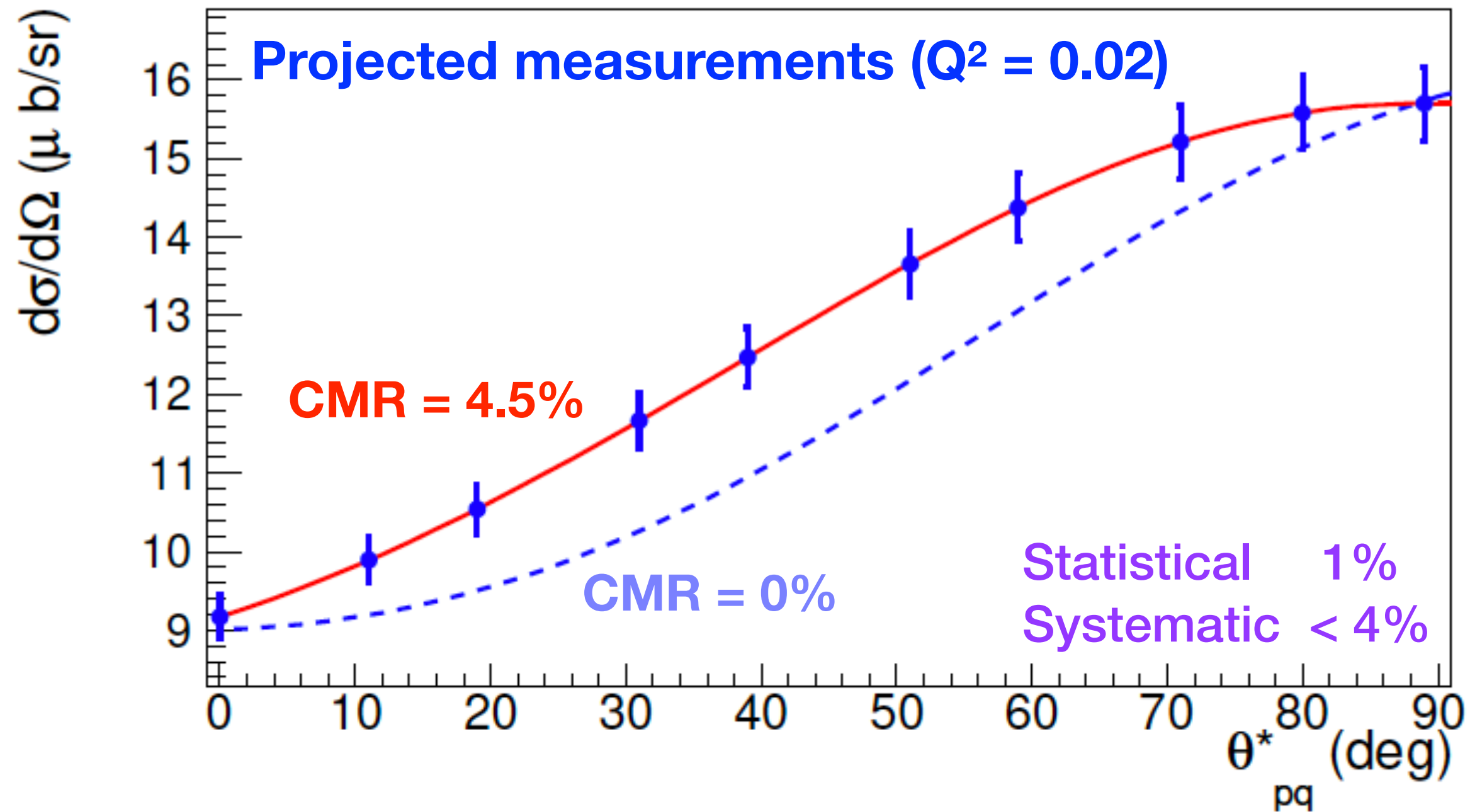


Resolution	2% - 3%
Acceptance	1%
Scattering angle	0.4% - 0.6%
Beam energy	0.7% - 1.2%
Beam charge	1%
Target density	0.5%
Detector efficiencies	0.5%
Target cell background	0.5%
Target length	0.5%
Dead-time corrections	0.5%
<b>Total</b>	<b>2.8% - 3.8%</b>

- High precision in very low  $Q^2$  region that is sparsely populated
- Region where pion-cloud effects are expected to be prominent

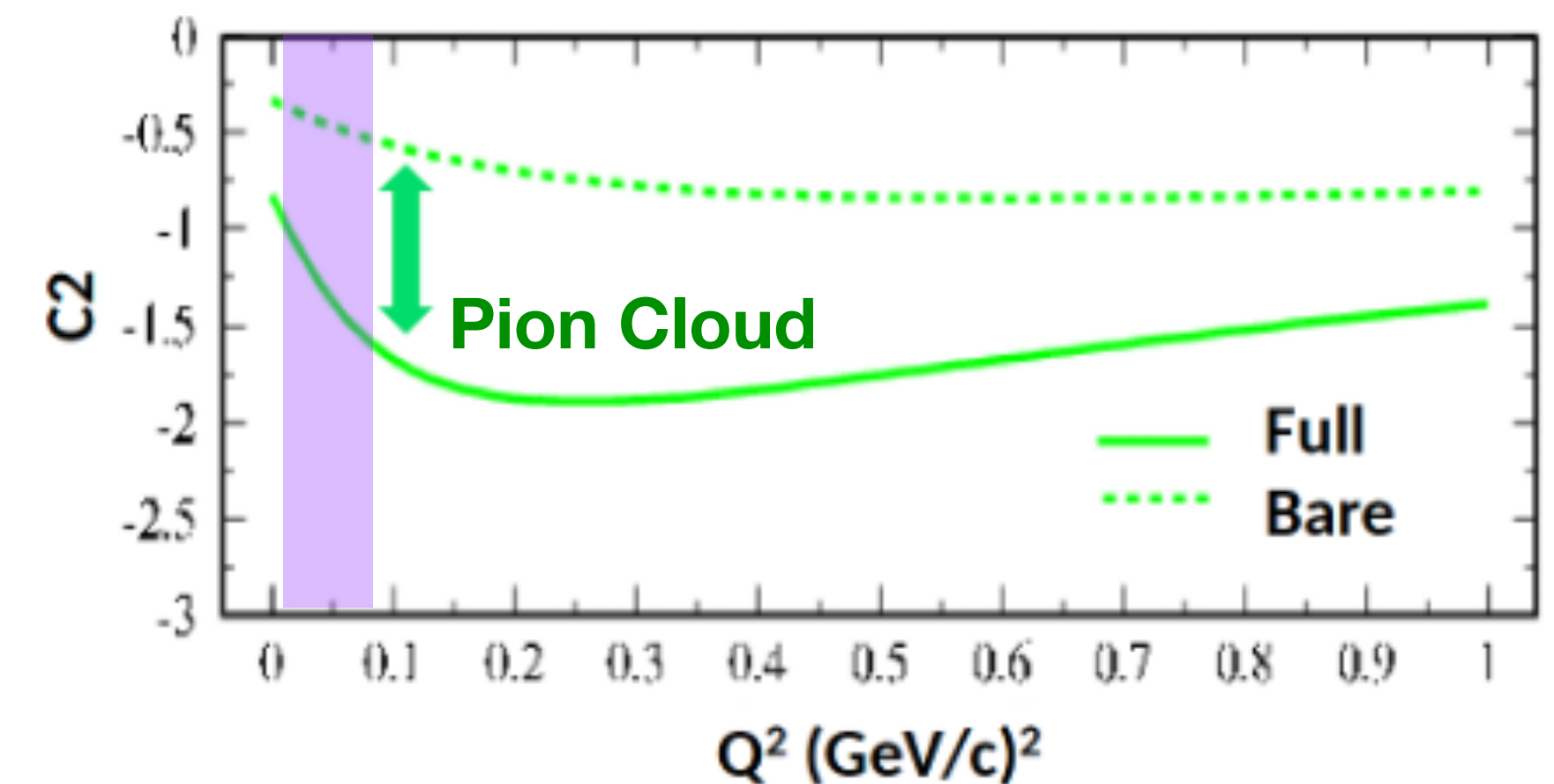


# Projected CMR and EMR measurements



Resolution	2% - 3%
Acceptance	1%
Scattering angle	0.4% - 0.6%
Beam energy	0.7% - 1.2%
Beam charge	1%
Target density	0.5%
Detector efficiencies	0.5%
Target cell background	0.5%
Target length	0.5%
Dead-time corrections	0.5%
<b>Total</b>	<b>2.8% - 3.8%</b>

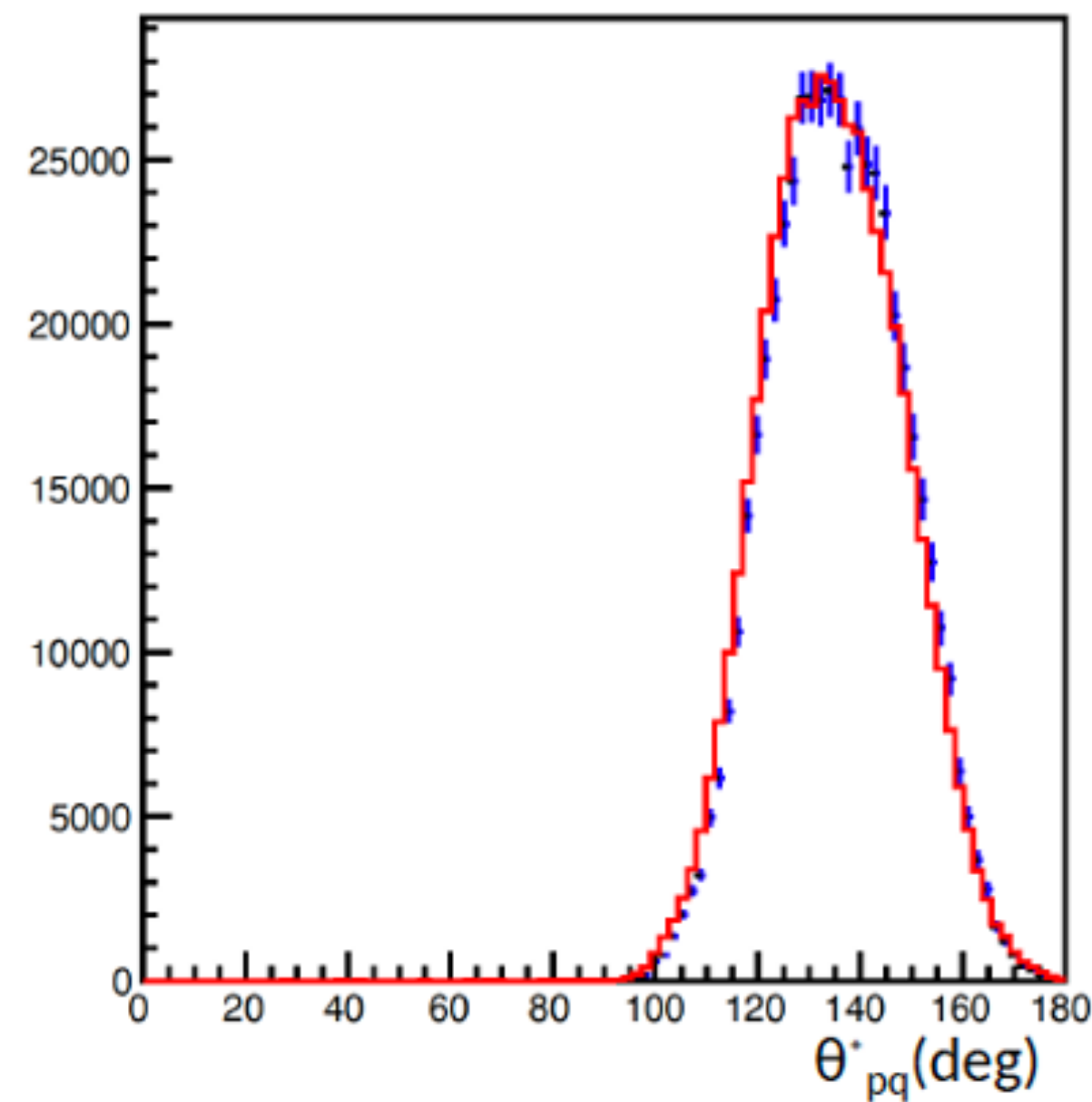
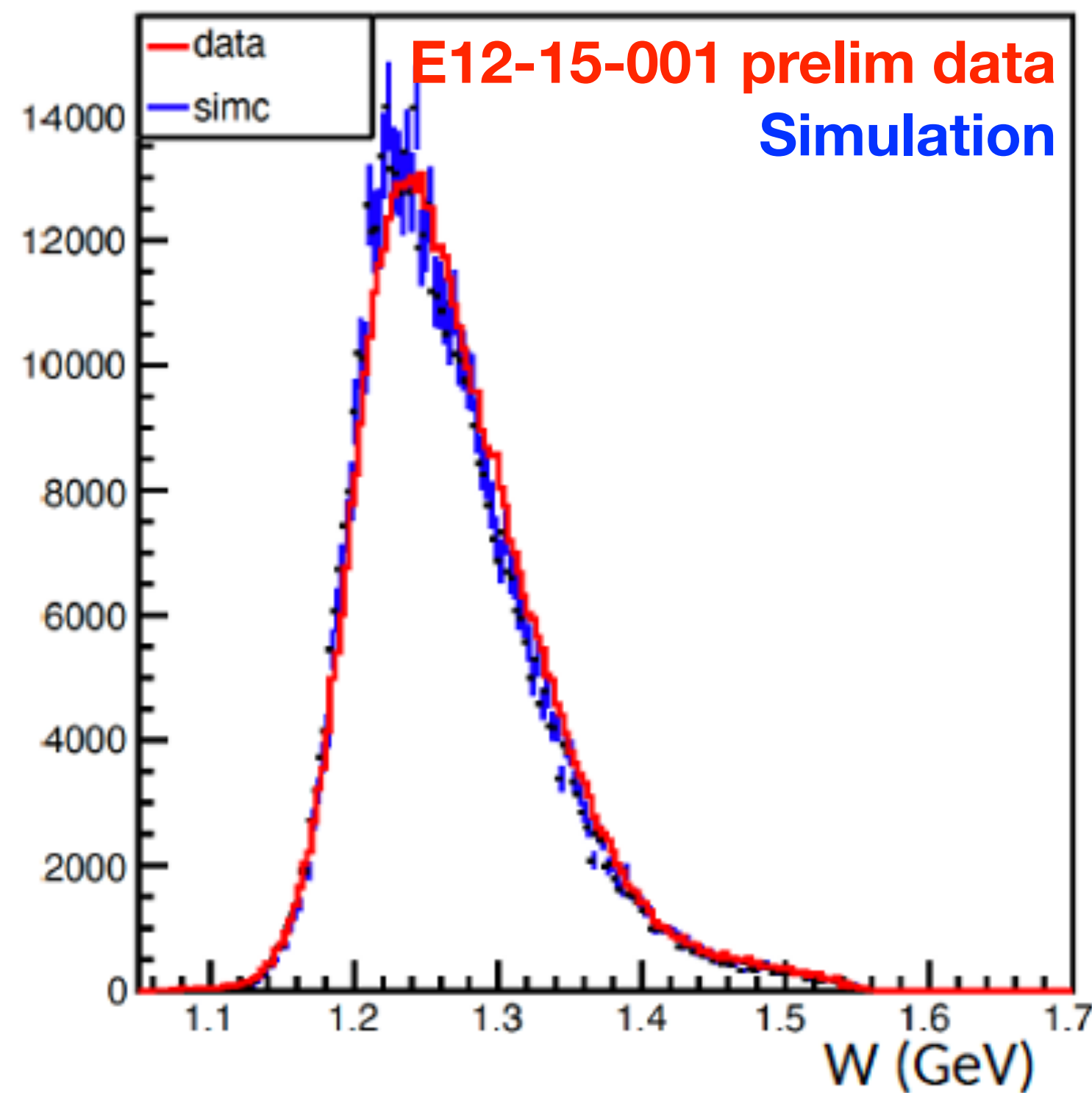
- High precision in very low  $Q^2$  region that is sparsely populated
- Region where pion-cloud effects are expected to be prominent
- Experiment was approved with A- rating by PAC50



# Readiness in experimental & theoretical methodology/tools

VCS Experiment E12-15-001 ran in Hall-C (2019) with a similar set-up at  $Q^2 = 0.33 \text{ (GeV/c)}^2$

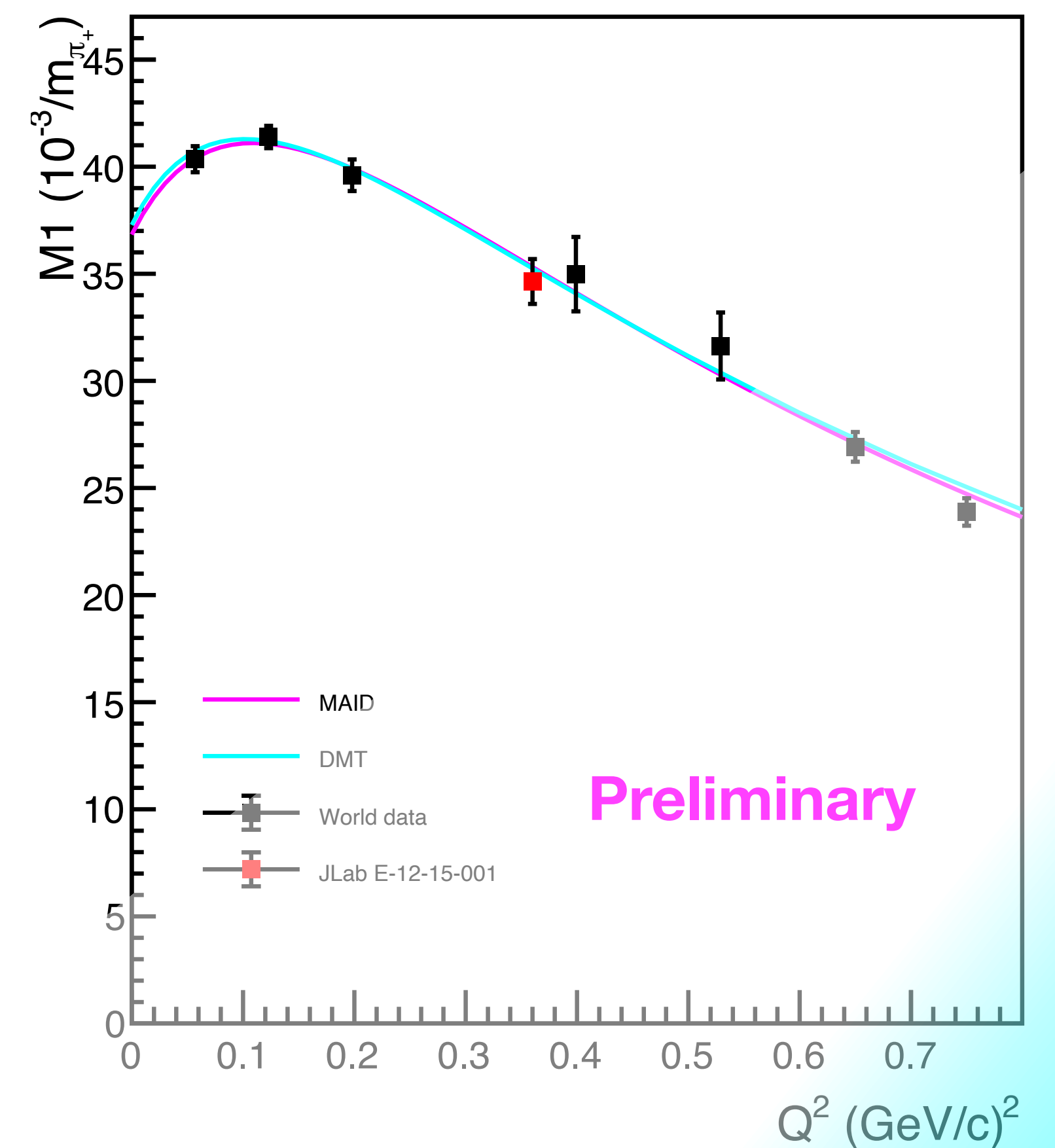
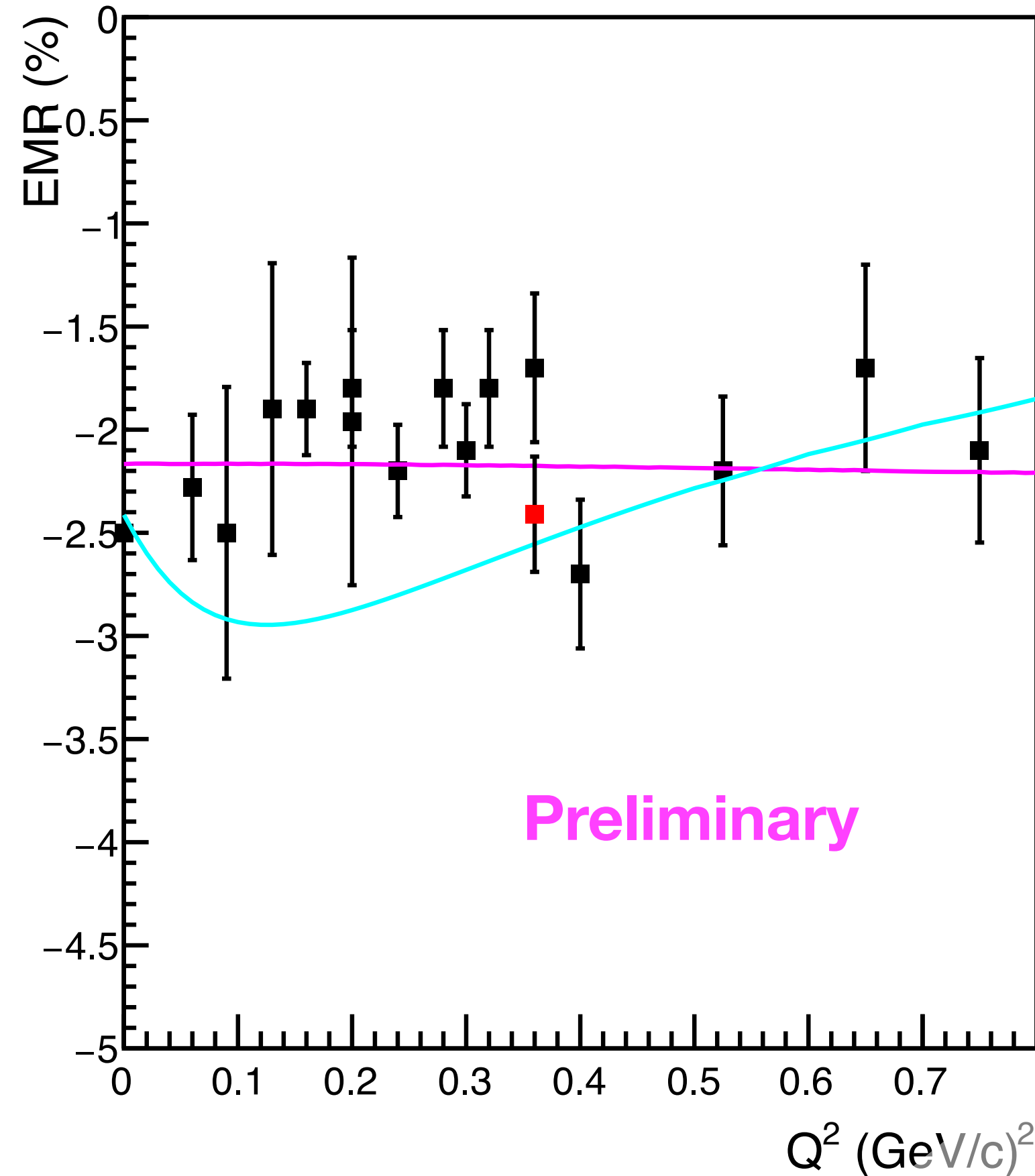
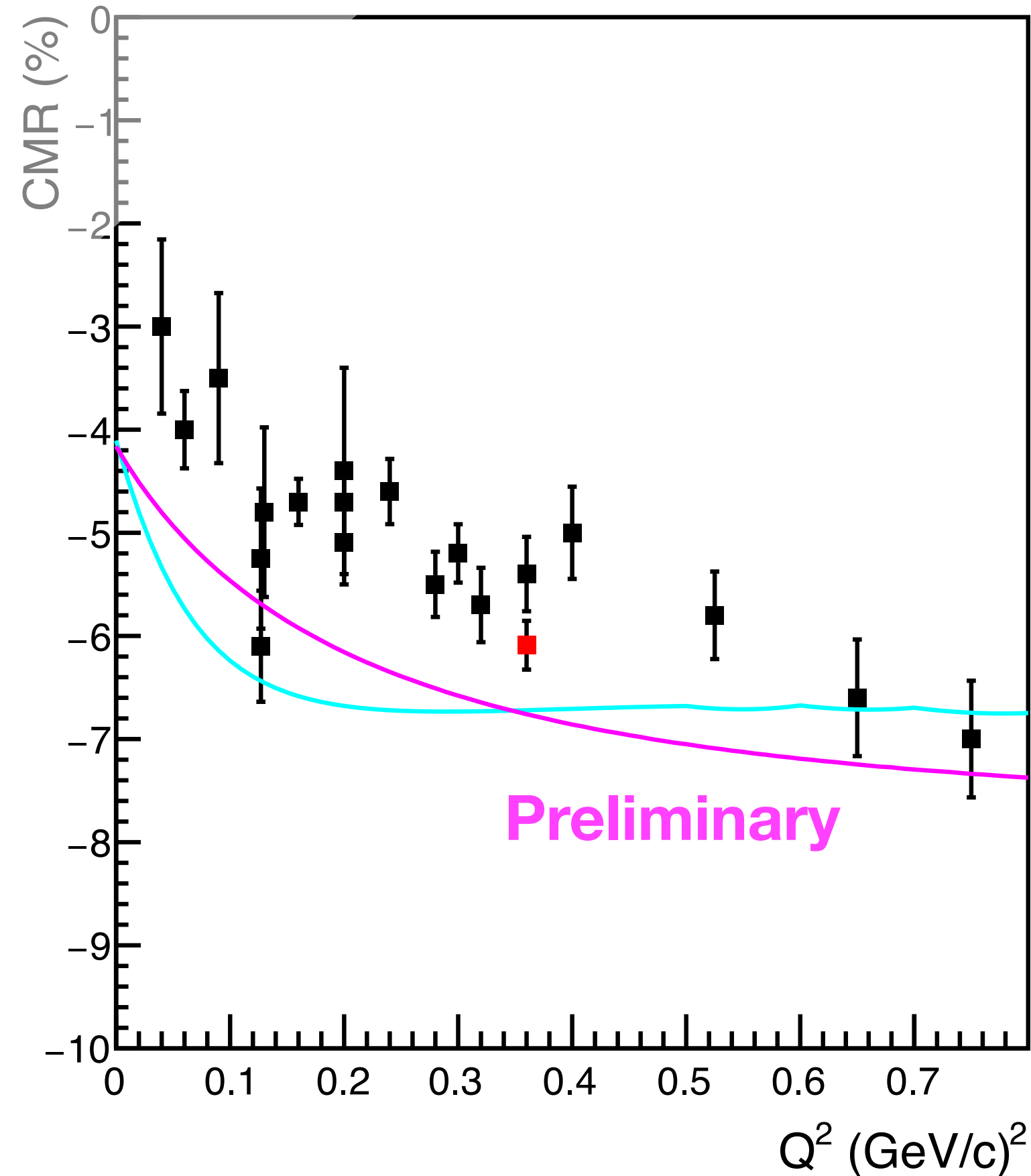
Main difference with proposed experiment: Lower  $Q^2 \rightarrow$  lower beam energy and lower central momentum settings



# Readiness in experimental & theoretical methodology/tools

VCS Experiment E12-15-001 ran in Hall-C (2019) with a similar set-up at  $Q^2 = 0.33$  (GeV/c)<sup>2</sup>

Main difference with proposed experiment: Lower  $Q^2$   $\rightarrow$  lower beam energy and lower central momentum settings



# Summary

- **The  $N \rightarrow \Delta$  TFFs represent a central element of the nucleon dynamics**
  - We will extend these measurements in the low  $Q^2$  region:
    - Test bed for ChEFT calculations
    - High precision benchmark data for the Lattice QCD calculations
    - New constraints and input to the theoretical models
    - Insight to the mesonic-cloud dynamics within a region where they are dominant and rapidly changing
    - Insight to the origin of non-spherical components in the nucleon wave-function
    - Will test if the QCD prediction that CMR & EMR converge as  $Q^2 \rightarrow 0$
- **Experiment was approved with A- rating by PAC50**
  - 11 days (8 production, 3 calibration)
  - Beam energy: 1.3 GeV (flexible within +/- 0.1 GeV)
  - Hall C standard SHMS and HMS setup with a 4 cm LH2 target

**Thank you!**

