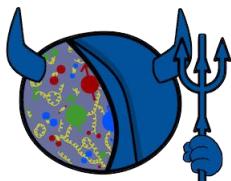


Global Analyses of Polarized DIS & SIDIS from Small-x Evolution



SPIN 2023



Matthew D. Sievert



9/29/2023

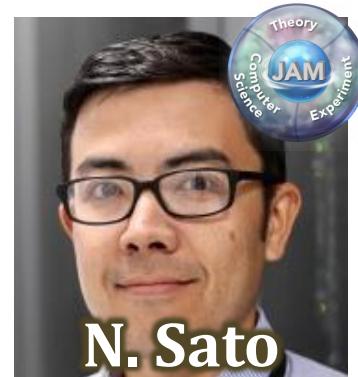
This work is supported by the U.S. Department of Energy, Office of Science, Office of Nuclear Physics within the framework of the Saturated Glue (SURGE) Topical Theory Collaboration.



Collaborators



W. Melnitchouk



N. Sato



Y. Kovchegov



D. Pitonyak



M. Sievert



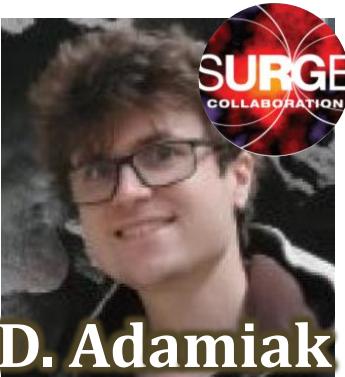
A. Tarasov



Y. Tawabutr



N. Baldonado



D. Adamiak

- Wally Melnitchouk (JAM)
- Nobuo Sato (JAM)
- Yuri Kovchegov (SURGE)
- Dan Pitonyak (SURGE)

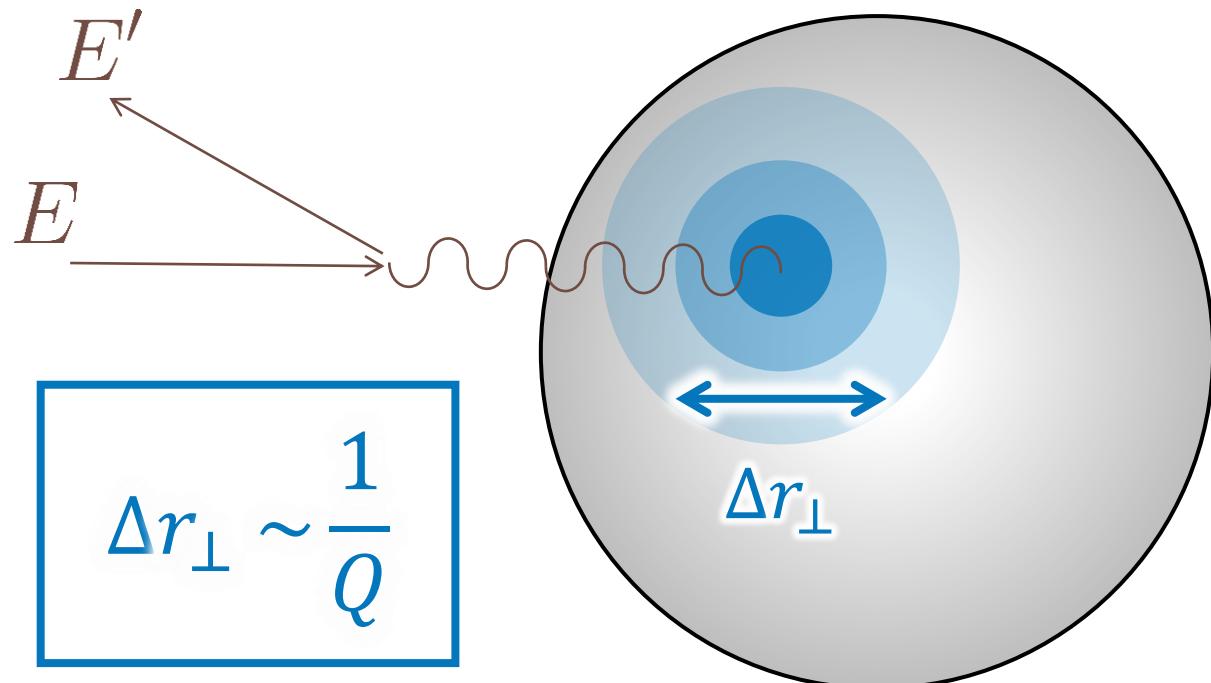
- **Andrey Tarasov (SURGE: PD)**
- **Yossathorn Tawabur (SURGE: PD)**
- **Daniel Adamiak (SURGE: PD)**

- **Nick Baldonado (SURGE: GA)**

DIS: A Relativistic Femtoscope in Two Scales

Image Resolution:

$$Q^2 = 4 E E' \sin^2 \frac{\theta}{2}$$

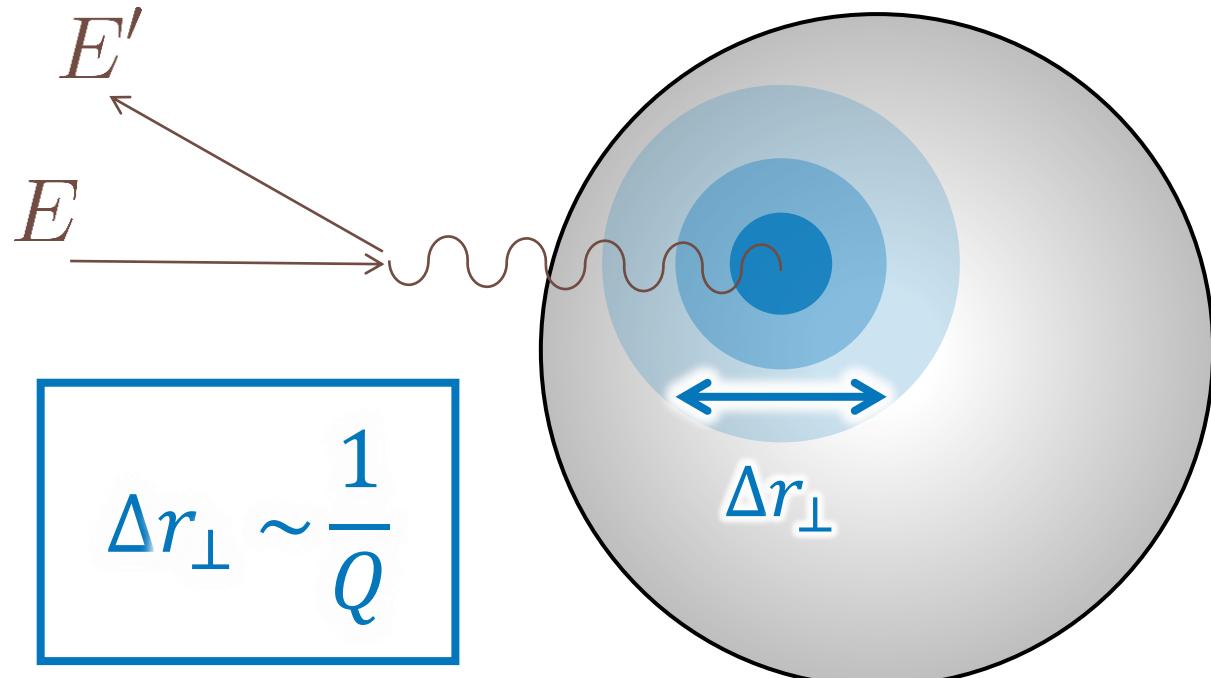


$$\Delta r_\perp \sim \frac{1}{Q}$$

DIS: A Relativistic Femtoscope in Two Scales

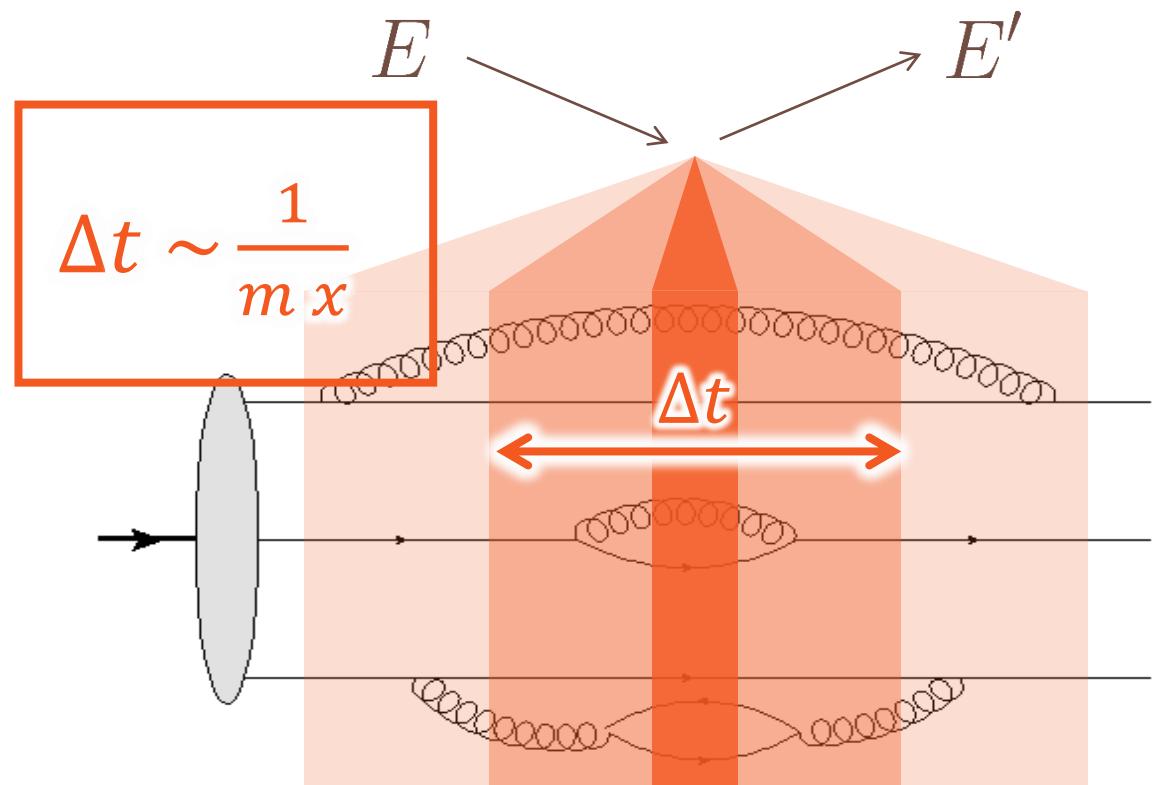
Image Resolution:

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Exposure Time:

$$x = \frac{Q^2}{2m(E - E')}$$

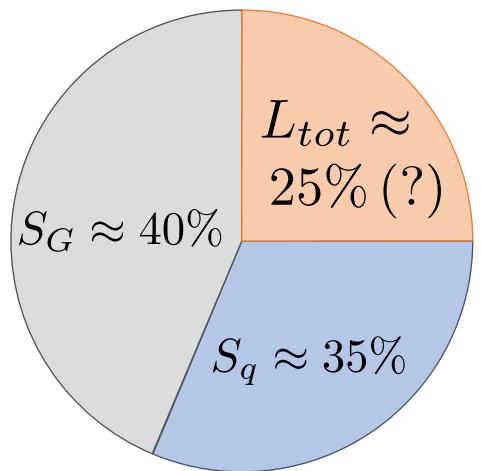


The Proton Spin Budget

Jaffe-Manohar Spin Sum Rule:

Jaffe and Manohar, Nucl. Phys. B337 509 (1990)

$$\frac{1}{2} = S_q + S_G + L_q + L_G$$



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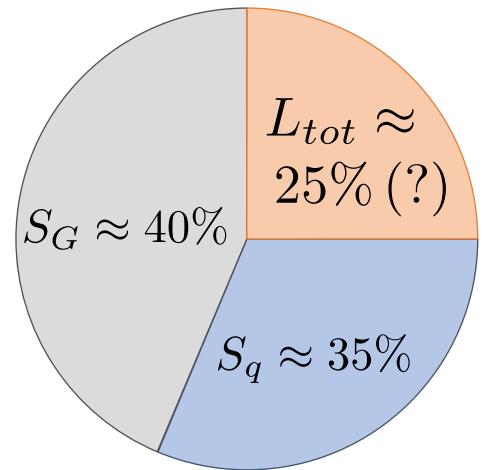
$$\frac{1}{2} = S_q + S_G + L_q + L_G$$

- Quark Polarization:

$$S_q(Q^2) = \frac{1}{2} \sum_{f,\bar{f}} \int_0^1 dx \Delta q_f(x, Q^2)$$

$$\Delta q(x, Q^2) = \int \frac{dr^-}{2\pi} e^{ixp^+r^-} \left\langle pS_L \left| \bar{\psi}(0) \mathcal{U}[0, r] \frac{\gamma^+ \gamma^5}{2} \psi(r) \right| pS_L \right\rangle$$

➤ Nonlocal generalization of the **axial vector current** $j_5^\mu = \bar{\psi} \gamma^\mu \gamma^5 \psi$



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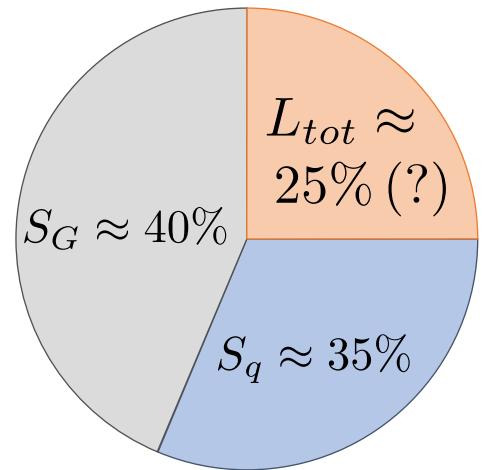
➤ Nonlocal generalization of the **axial vector current** $j_5^\mu = \bar{\psi} \gamma^\mu \gamma^5 \psi$

- Gluon Polarization:

$$S_G(Q^2) = \int_0^1 dx \Delta G(x, Q^2)$$

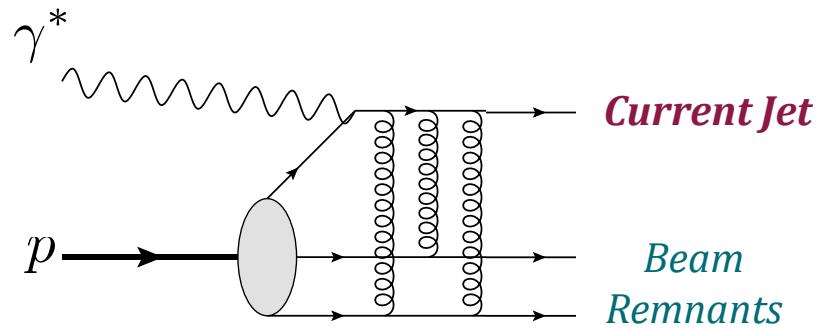
$$\Delta G(x, Q^2) = \frac{-2i}{xp^+} \int \frac{dr^-}{2\pi} e^{ixp^+r^-} \left\langle pS_L \left| \epsilon_T^{ij} \text{tr} \left[F^{+i}(0) \mathcal{U}[0, r] F^{+j}(r) \mathcal{U}'[r, 0] \right] \right| pS_L \right\rangle$$

➤ Circular azimuthal correlation of gluon field strengths



Dipole Degrees of Freedom at Small x

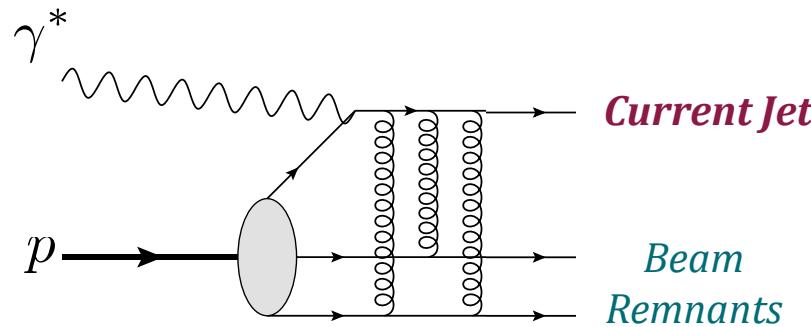
“Knockout” DIS at Large x:



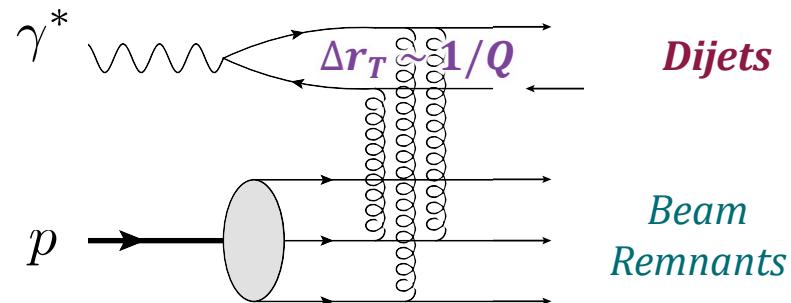
- At **large x**, DIS resembles a **knockout** process in which a quark is ejected from the proton.

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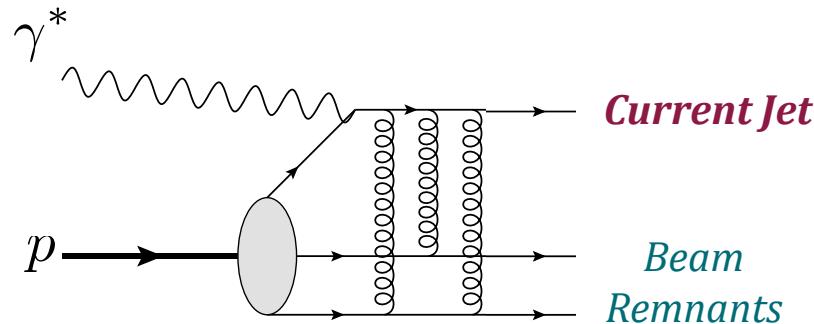
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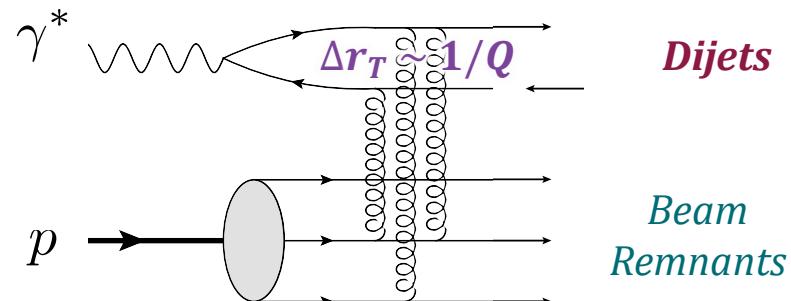
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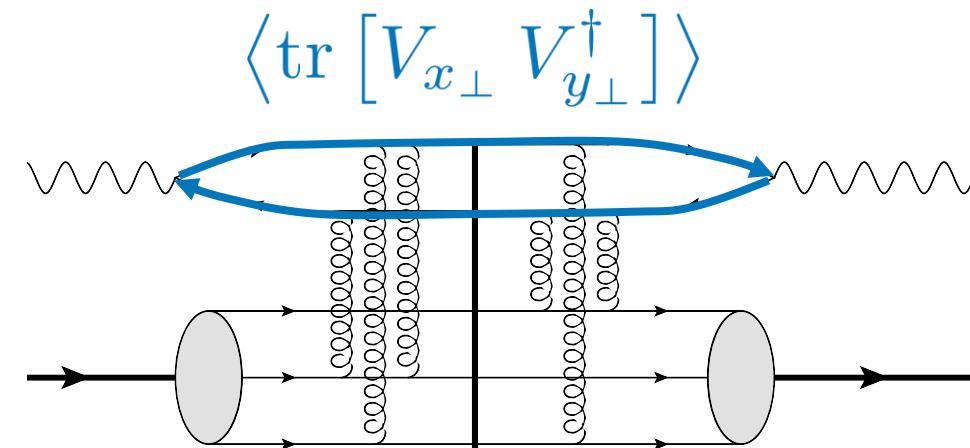


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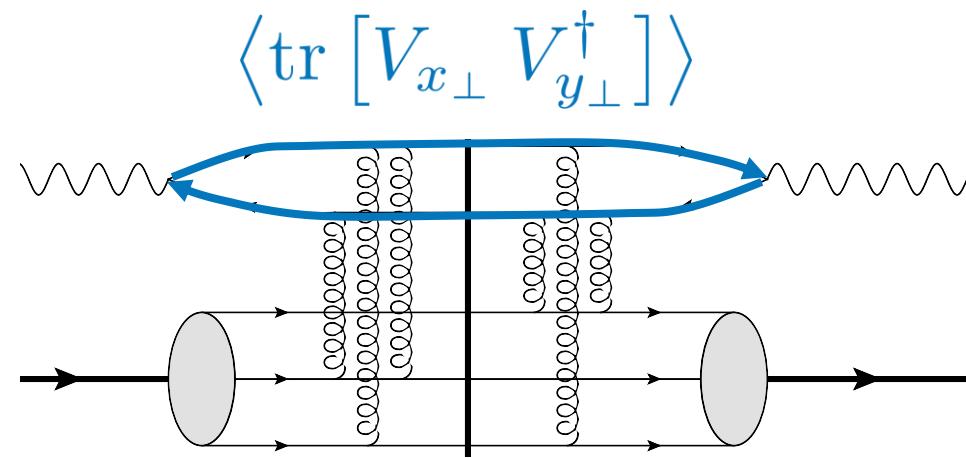
- At **large x**, DIS resembles a **knockout** process in which a quark is ejected from the proton.
 - At **small x**, DIS resembles a **hadronic scattering** process of a $q\bar{q}$ dipole on the target
- **Wilson lines: Boosted, coherent** scattering in a background field

$$V = \mathcal{P} \exp \left[ig \int dz_\mu A^\mu(z) \right]$$



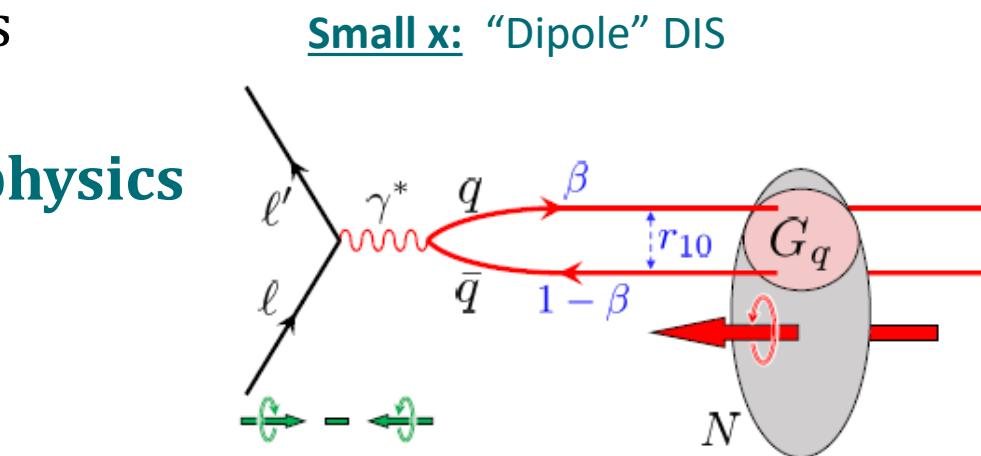
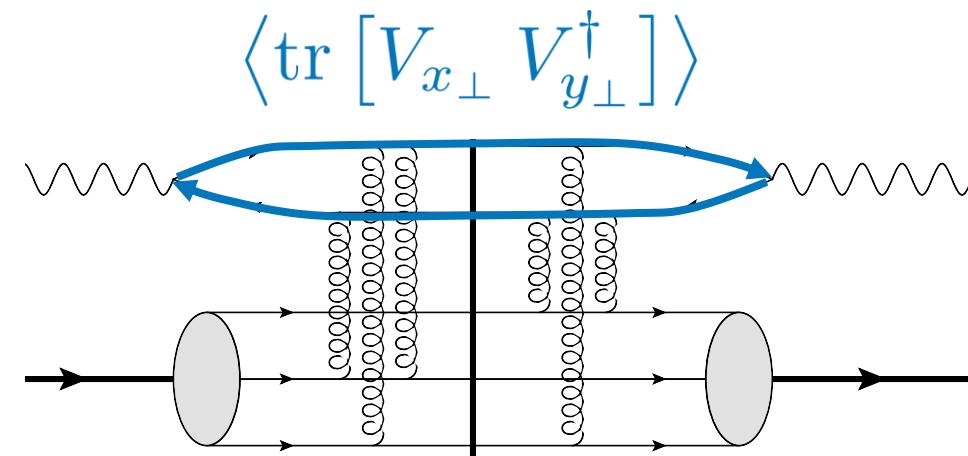
Spin at Small x versus Large x

- The **leading-power** dipole scattering is **spin-independent**
 - It is **not the ordinary eikonal Wilson lines** that describe polarized physics at small x!

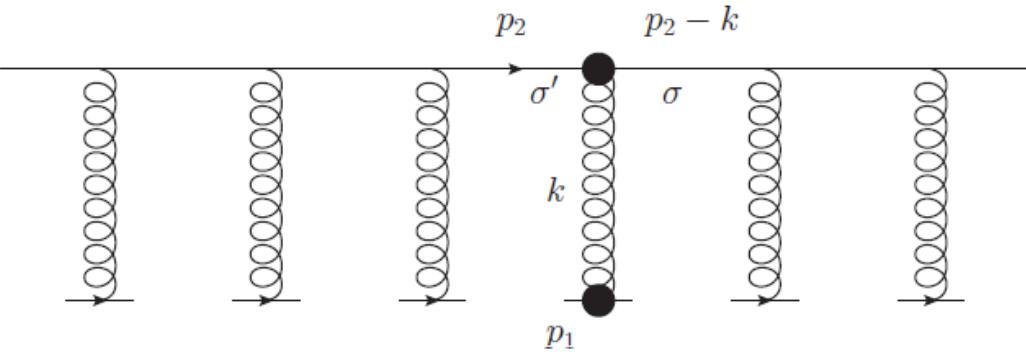


Spin at Small x versus Large x

- The **leading-power** dipole scattering is **spin-independent**
 - It is **not the ordinary eikonal Wilson lines** that describe polarized physics at small x!
- **Spin at small x** selects on **different, sub-eikonal** dynamics than unpolarized observables
 - Spin observables are sensitive to **novel small-x physics**
 - **Useful for gluon saturation**, but **broader** than saturation alone



Building Blocks: Polarized Wilson Lines

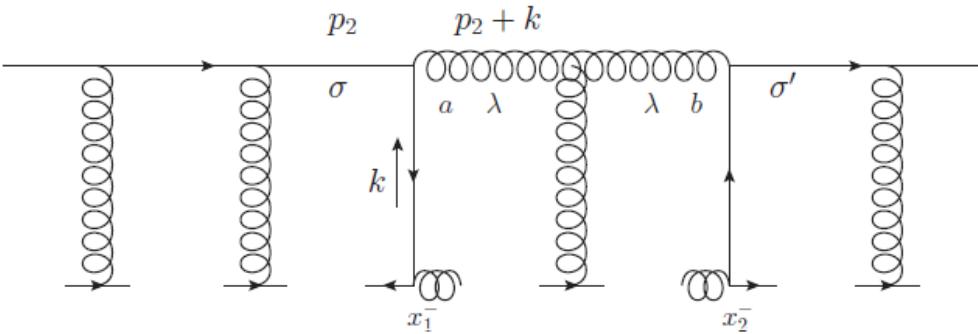
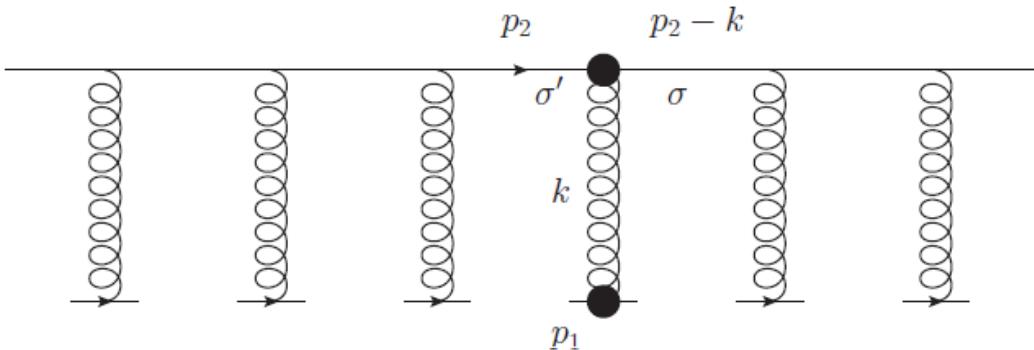


QCD Stern-Gerlach: $\gamma \vec{S} \cdot \vec{B}$

See, e.g., Kovchegov, Pitonyak, MS: JHEP **01** (2016),
Phys. Rev. **D95** (2017), Phys.Rev.Lett. **118** (2017)

$$V_{\underline{x}}^{pol} = \frac{igp_1^+}{s} \int_{-\infty}^{\infty} dx^- V_{\underline{x}}[+\infty, x^-] F^{12}(x^-, \underline{x}) V_{\underline{x}}[x^-, -\infty]$$

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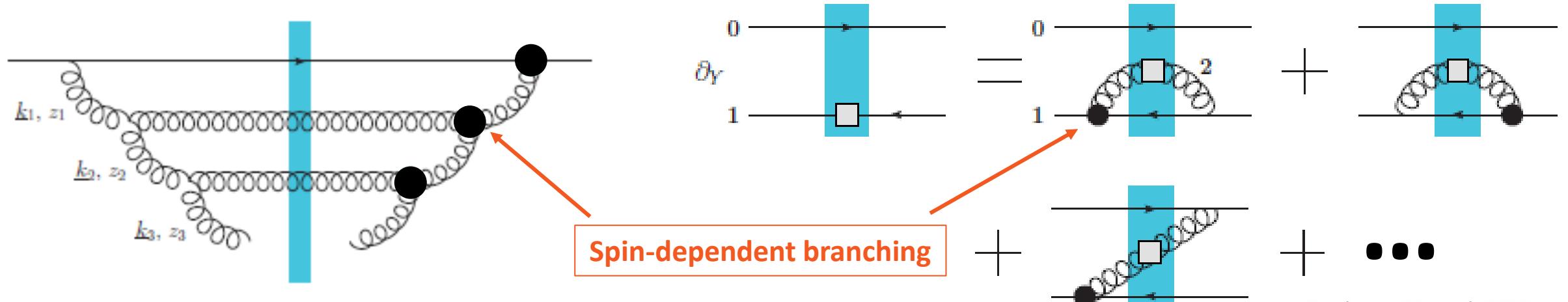
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$$- \frac{g^2 p_1^+}{s} \int \limits_{-\infty}^{\infty} dx_1^- \int \limits_{x_1^-}^{\infty} dx_2^- V_{\underline{x}}[+\infty, x_2^-] t^b \psi_{\beta}(x_2^-, \underline{x}) U_{\underline{x}}^{ba}[x_2^-, x_1^-] \left[\frac{1}{2} \gamma^+ \gamma^5 \right]_{\alpha\beta} \bar{\psi}_{\alpha}(x_1^-, \underline{x}) t^a V_{\underline{x}}[x_1^-, -\infty].$$

Flavor-changing Wilson line

Since m=0 in Bjorken kinematics: Quark helicity conservation

Cascading Polarized Dipoles at Small x

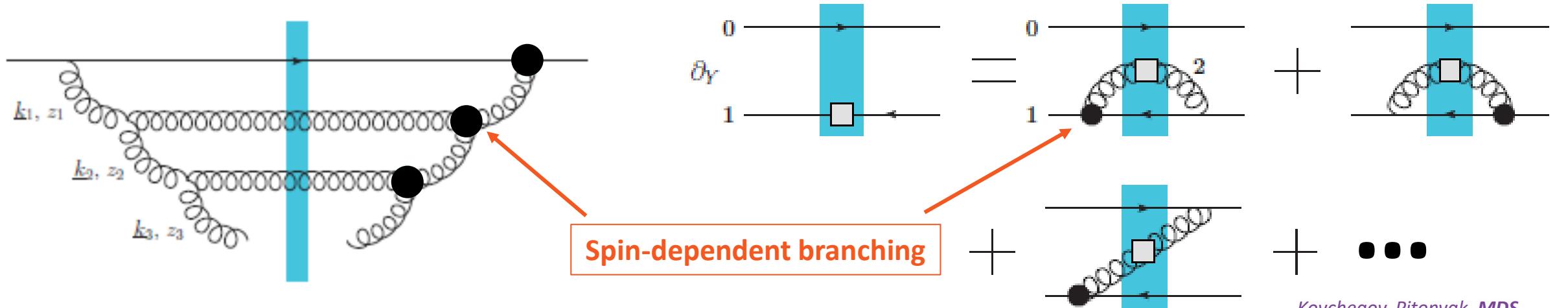


Kovchegov, Pitonyak, **MDS**,
JHEP 1601 (2016), Phys. Rev. D95 (2017)

- **Spin information** from the valence sector (large x) is **transmitted to small x** by **spin-dependent branching**

Also G. Chirilli, JHEP 1901 (2019)

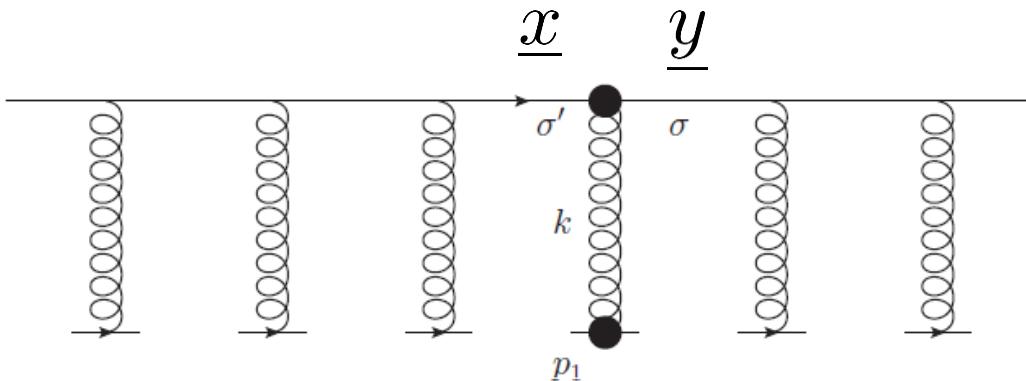
Cascading Polarized Dipoles at Small x



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- **Spin information** from the valence sector (large x) is **transmitted to small x** by **spin-dependent branching**
Also G. Chirilli, JHEP 1901 (2019)
- **Suppressed** by the **coupling** α_s but **enhanced** by the **phase space** $\ln \frac{1}{x}$
 - Resummation leads to **quantum evolution of spin at small x**
 - Analogous to **BFKL evolution** for unpolarized gluons (*leading log accuracy*)

The Missing Link: Transverse Recoil



- **Spin-independent** sub-eikonal operator contributes to evolution
- **New contribution** not previously included in dipole helicity evolution

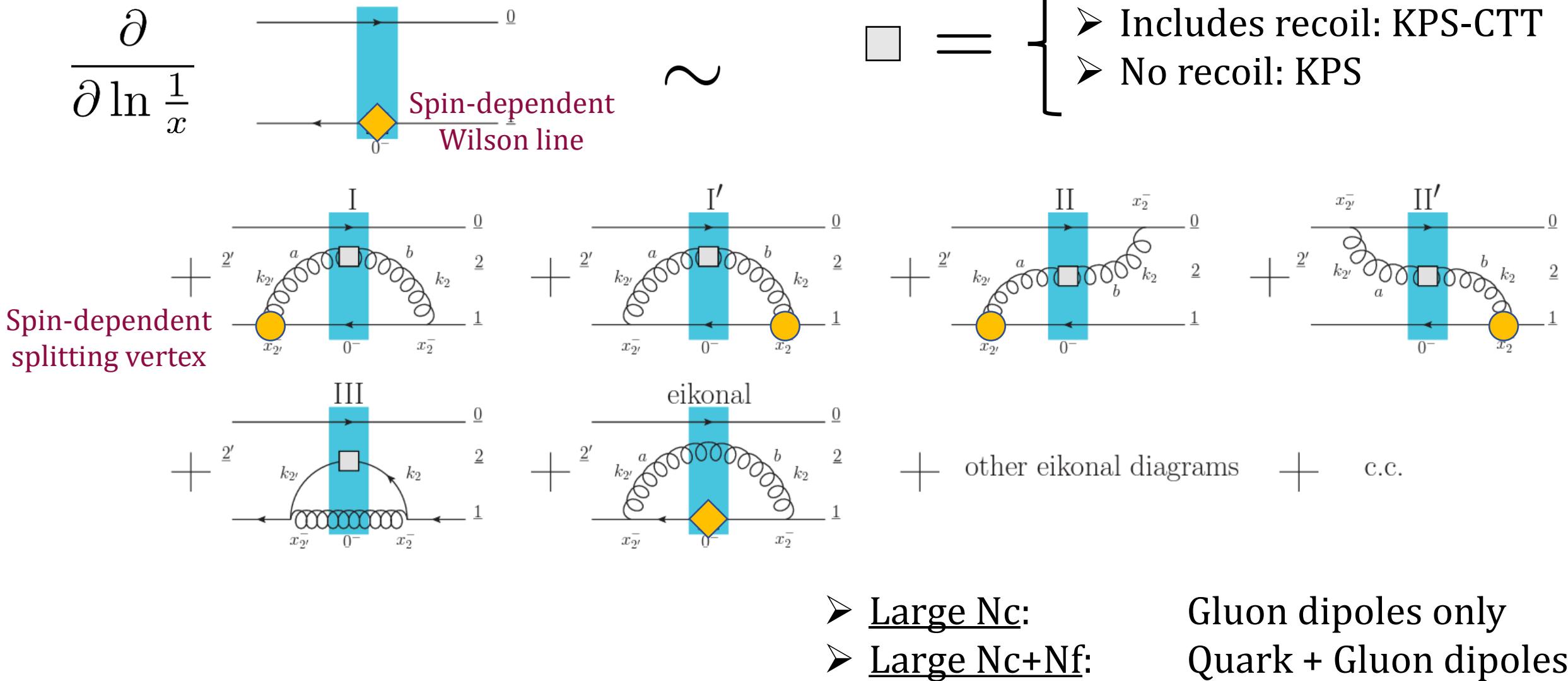
F. Cougoulic, Y. Kovchegov, A. Tarasov, Y. Tawabutr, JHEP 07 (2022)

Jump displacement in transverse position: $\nabla \delta^2(\underline{x} - \underline{y})$

$$V_{\underline{x}, \underline{y}}^{G[2]} = -\frac{i P^+}{s} \int_{-\infty}^{\infty} dz^- d^2 z V_{\underline{x}}[\infty, z^-] \delta^2(\underline{x} - \underline{z}) \bar{D}^i(z^-, \underline{z}) D^i(z^-, \underline{z}) V_{\underline{y}}[z^-, -\infty] \delta^2(\underline{y} - \underline{z}),$$



Small-x Helicity Evolution (KPS-CTT)



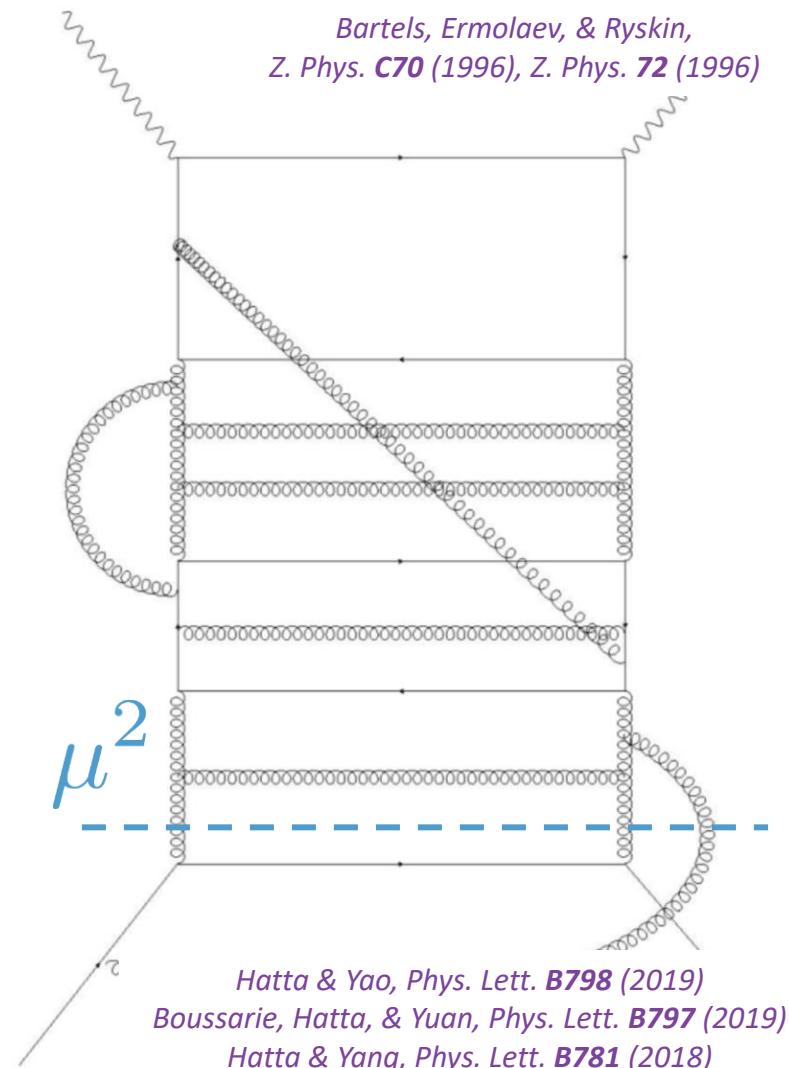
Method of Infrared Evolution Equations

- Missing recoil term **brings small-x asymptotics into agreement** with other calculations using infrared evolution equations (beyond 2 loops)
- Based on identifying and resuming **double logarithms of the infrared cutoff**, capturing both types of logs

$$\ln \frac{Q^2}{\mu^2} \text{ and } \ln \frac{1}{x}.$$

$$\left. \begin{array}{l} \Delta\Sigma(x, Q^2) \\ \Delta G(x, Q^2) \\ g_1(x, Q^2) \end{array} \right\} \sim \left(\frac{1}{x} \right)^{3.66} \sqrt{\frac{\alpha_s N_c}{2\pi}}$$

Asymptotically as $x \rightarrow 0$

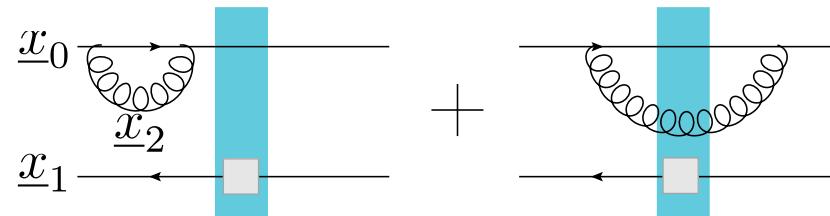


Beyond Color Transparency and Into the UV

- Ladder emissions from the **unpolarized Wilson line** possess **color transparency** at short distances

$$\frac{\alpha_s N_c}{2\pi^2} \int_{\frac{\Lambda^2}{s}}^z \frac{dz'}{z'} \int \frac{d^2x_2}{x_{20}^2} \times \left[\frac{1}{N_c^2} \left\langle \text{tr} \left[V_2 V_1^{pol\dagger} \right] \text{tr} \left[V_0 V_2^\dagger \right] \right\rangle_{(z's)} - \frac{1}{N_c} \left\langle \text{tr} \left[V_0 V_1^{pol\dagger} \right] \right\rangle_{(z's)} \right]$$

Cancels when $\underline{x}_2 \rightarrow \underline{x}_0$

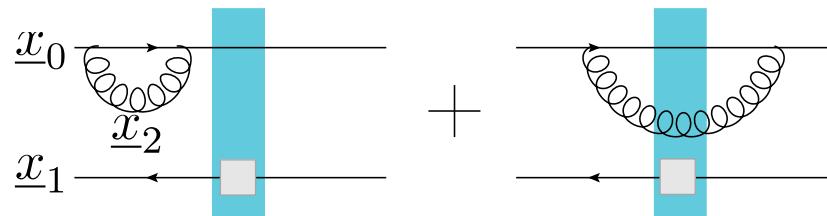


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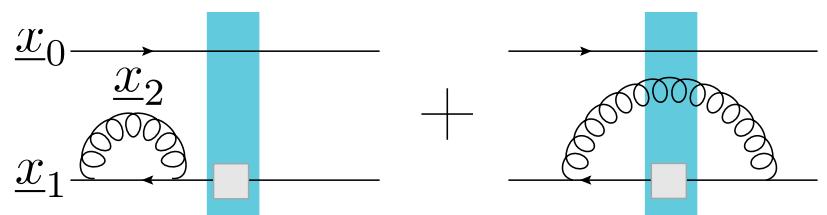
Cancels when $\underline{x}_2 \rightarrow \underline{x}_0$



- But for ladder emissions from the **polarized Wilson line**, color transparency is **violated by spin**

$$\frac{\alpha_s N_c}{2\pi^2} \int_{\frac{\Lambda^2}{s}}^z \frac{dz'}{z'} \int \frac{d^2x_2}{x_{21}^2} \times \left[\frac{1}{N_c^2} \left\langle \text{tr} \left[V_2 V_1^{pol\dagger} \right] \text{tr} \left[V_0 V_2^\dagger \right] \right\rangle_{(z's)} - \frac{1}{N_c} \left\langle \text{tr} \left[V_0 V_1^{pol\dagger} \right] \right\rangle_{(z's)} \right]$$

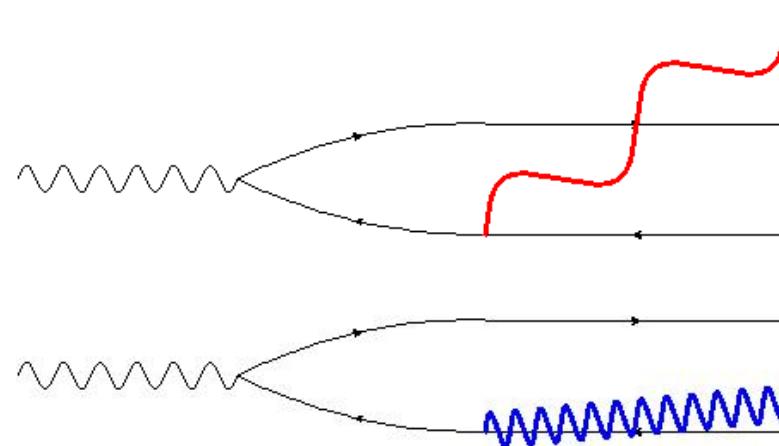
Does NOT cancel when $\underline{x}_2 \rightarrow \underline{x}_1$



Double-Logarithmic Evolution at Small x

Longitudinal + transverse
logarithmic phase space

$$dP \sim \alpha_s \frac{dx}{x} \frac{d^2 k}{k_T^2}$$



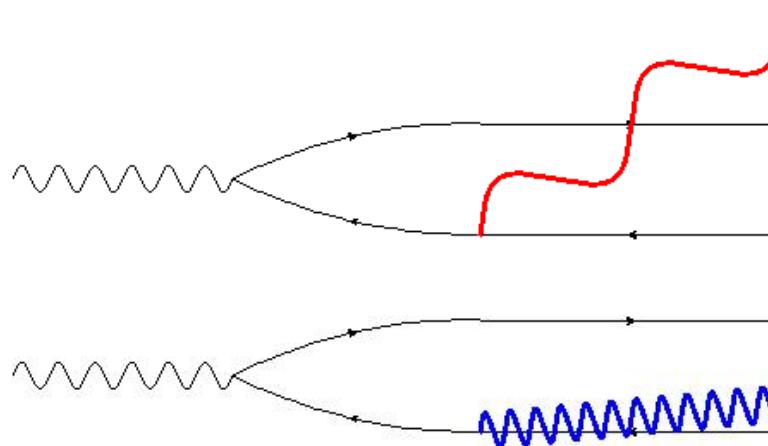
Long wavelength/IR

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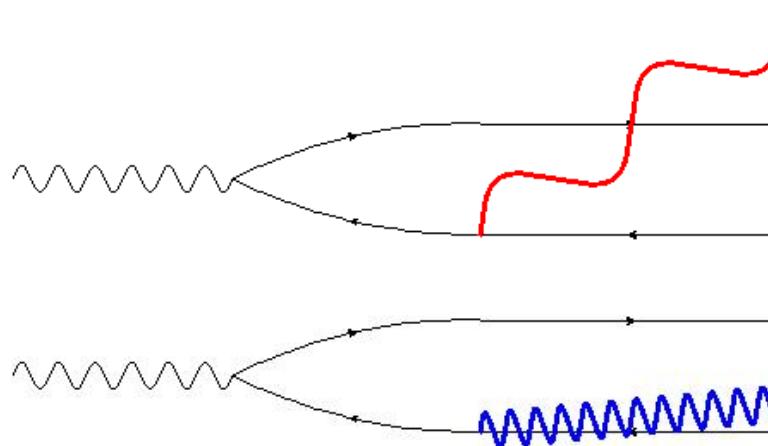
- **Unpolarized (BFKL) evolution:**

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- Only **longitudinal** phase space is logarithmic: $\alpha_s \ln \frac{1}{x} \sim O(1)$

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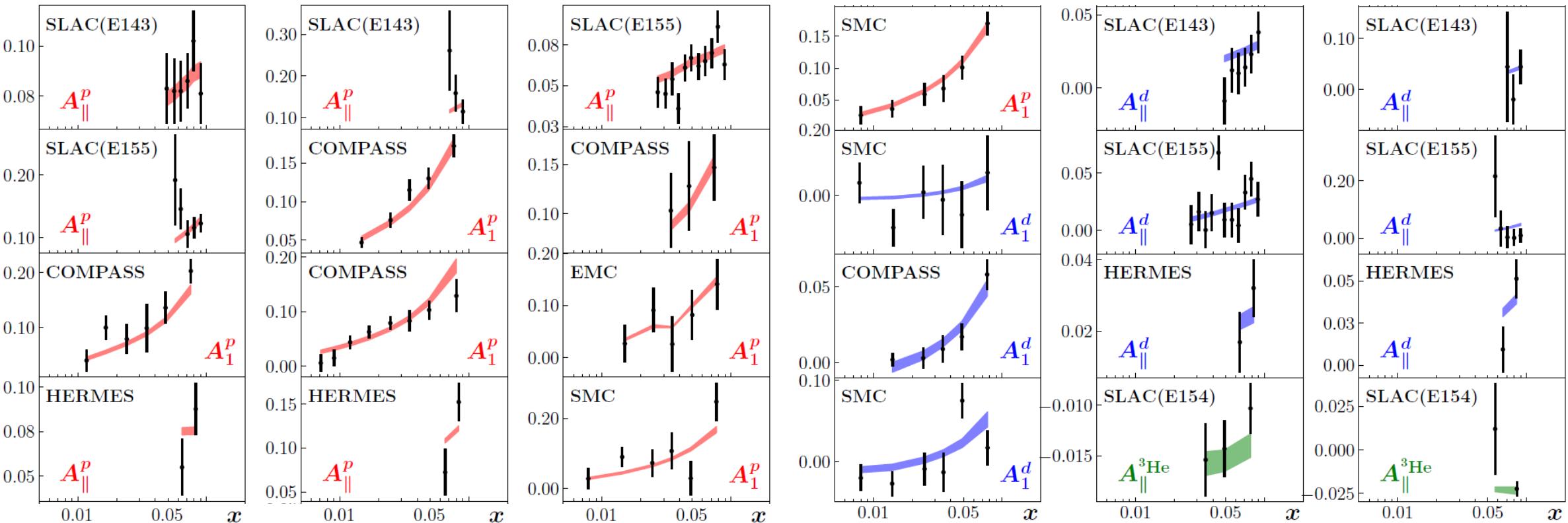
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- Only longitudinal phase space is logarithmic: $\alpha_s \ln \frac{1}{x} \sim O(1)$

- **Polarized (KPS) evolution:**

- No transparency of spin: dominance of collinear transverse logs
- Double-logarithmic evolution: $\alpha_s \ln^2 \frac{1}{x} \sim O(1)$
- Sensitive to lifetime ordering (c.f. NLO BFKL), less sensitive to saturation

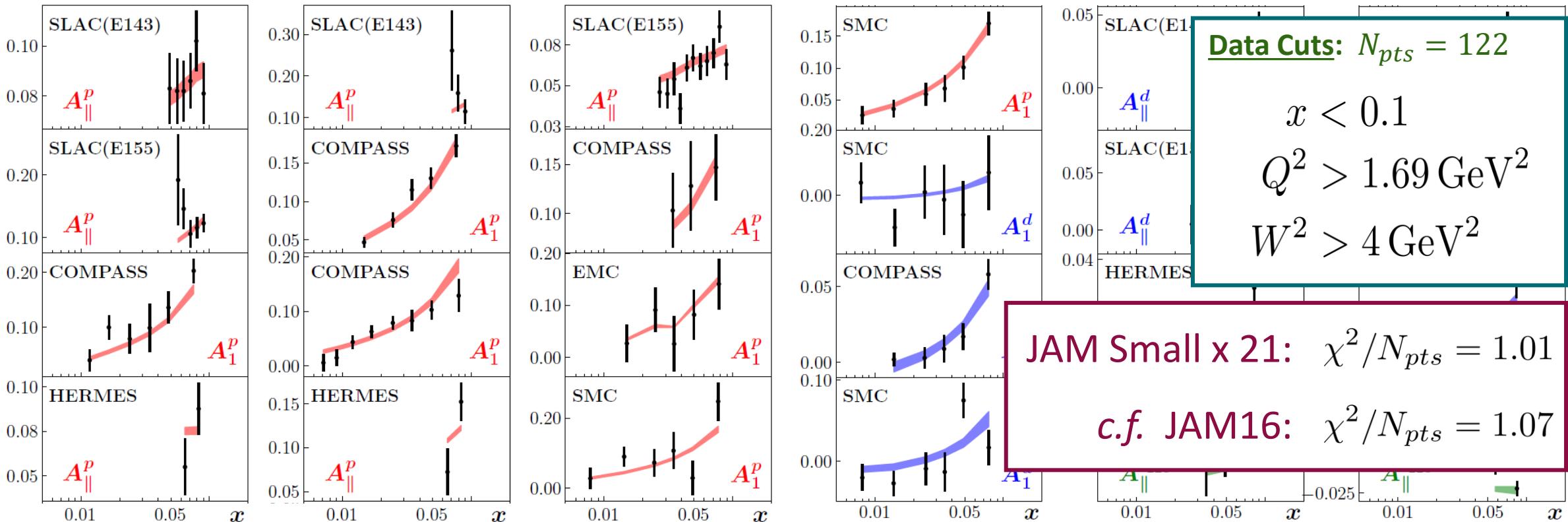
First Global Analysis Using KPS Evolution



- **Global analysis of polarized DIS at small x using KPS formalism**

D. Adamiak et al., Phys. Rev. D104 (2021)

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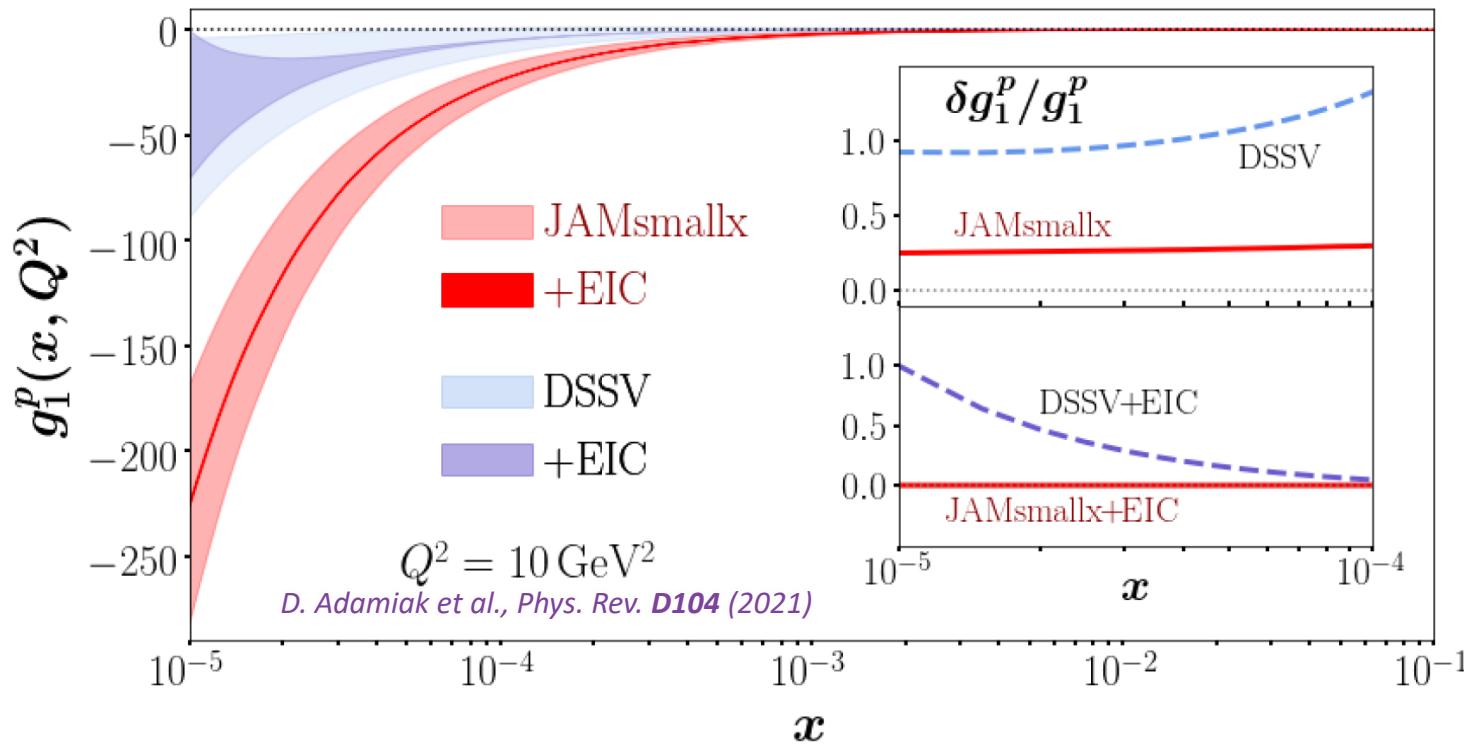
- **Bayesian analysis** performed using JAM architecture

N. Sato et al., Phys. Rev. D93 (2016)



First Global Analysis Using KPS Evolution

- Structure function g_1 determined down to low x
- Analysis prefers **large, negative g_1** at small x
- **Predictive power** at small x : controlled error in extrapolation
- The procedure **cannot describe everything**
 - Fails for **too-large x** (as expected)
 - Equally good $\frac{\chi^2}{N_{pts}} \sim 1$ for $0.05 \leq x \leq 0.20$

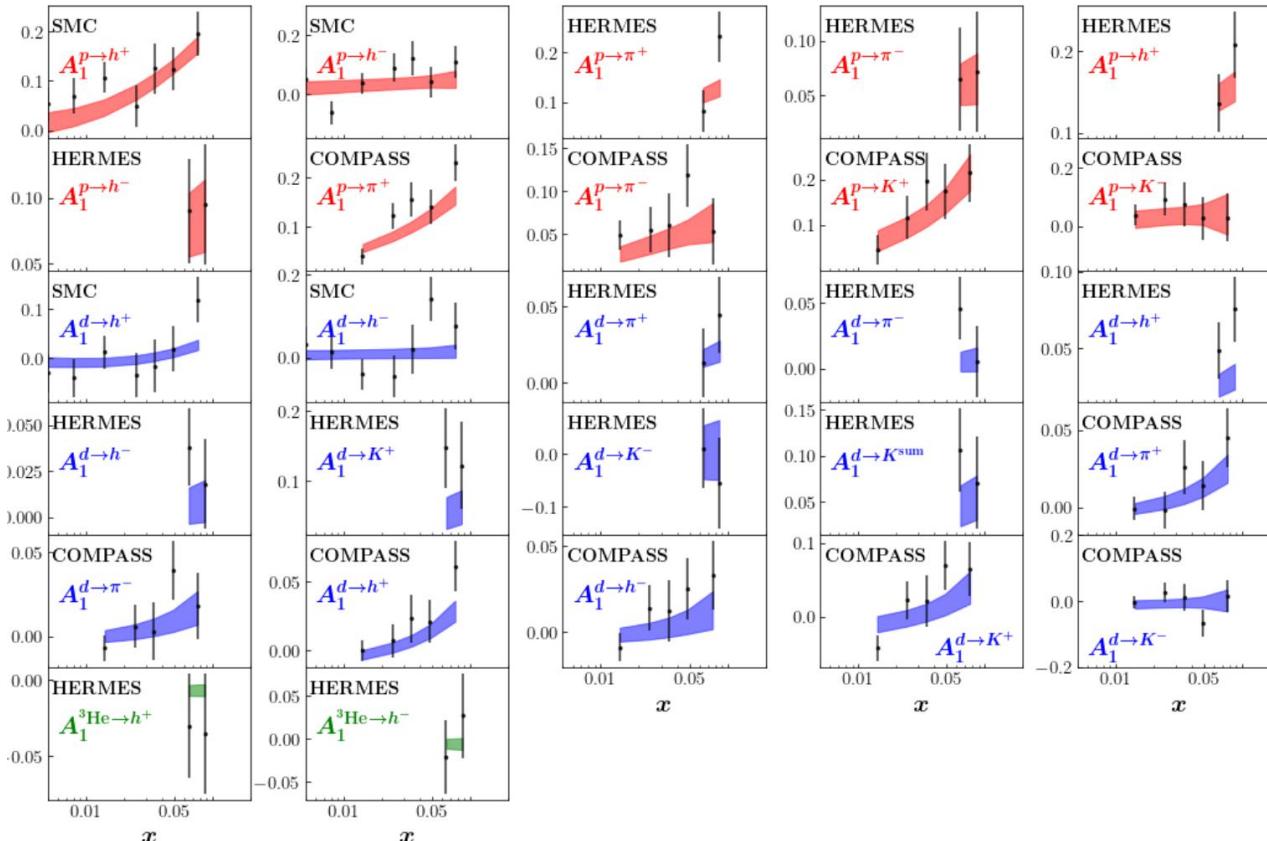


Error band: Bayesian 1σ confidence level
Statistical impact of EIC data (thin red band)

DSSV: de Florian et al., Phys. Rev. Lett. 113 (2014), Phys. Rev. D100 (2019)

New Global Analysis

D. Adamiak et al., arXiv: 2308.07461



- ❖ New evolution + large N_f = several new dipole functions included in fit

- New, updated JAM Small x fit:
 - DIS + SIDIS data
 - Improved KPS-CTT evolution
 - Large $N_c + N_f$ limit

Data Cuts: $N_{pts} = 226$

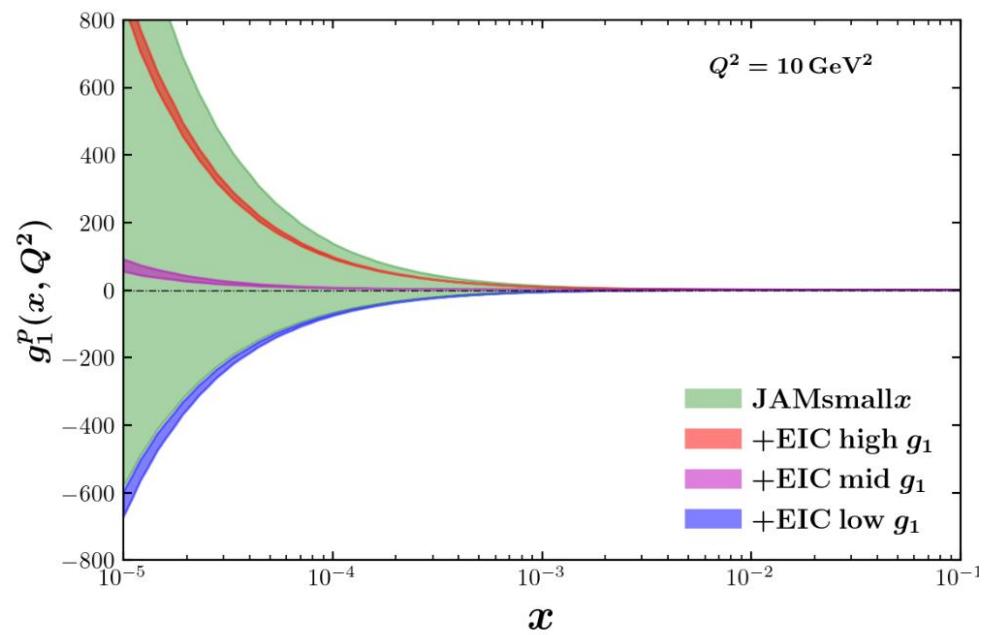
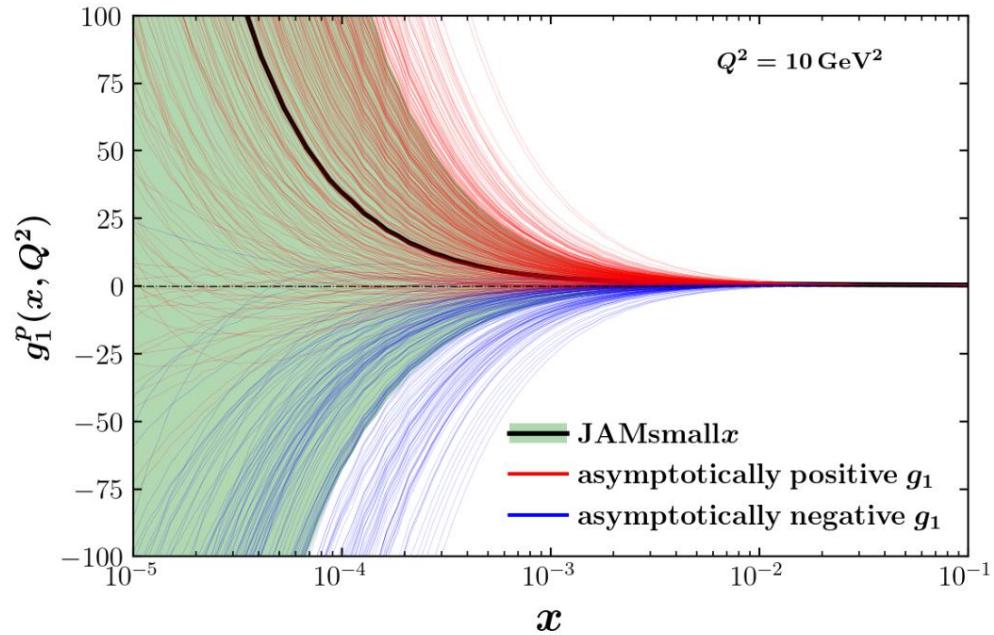
$$x < 0.1$$

$$Q^2 > 1.69 \text{ GeV}^2$$

$$0.4 \lesssim z \lesssim 0.6$$

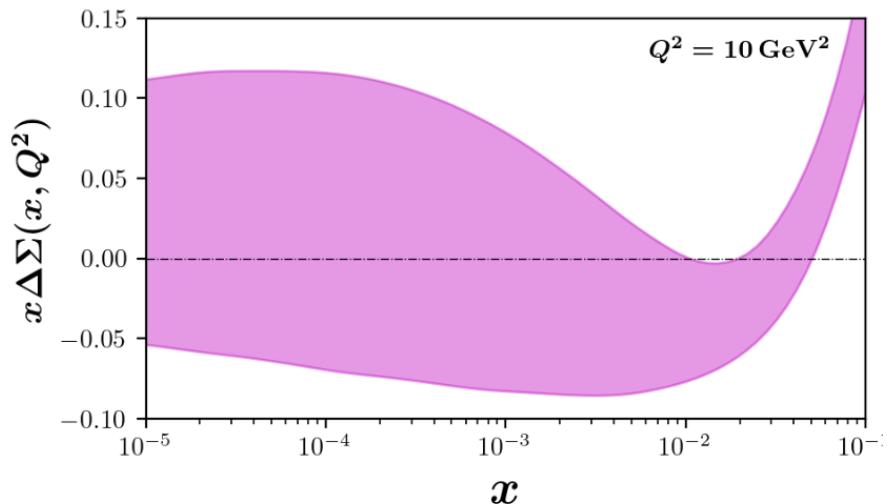
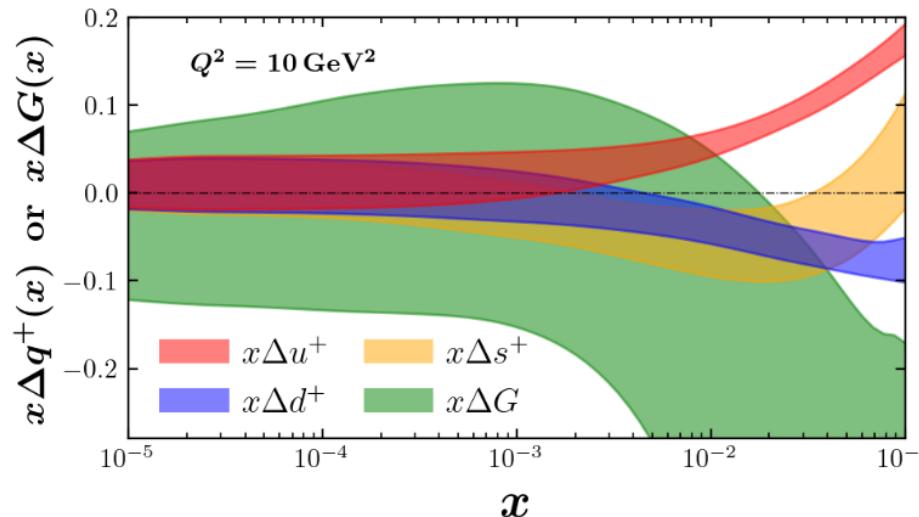
JAM Small x 23: $\chi^2/N_{pts} = 1.03$

New Global Analysis

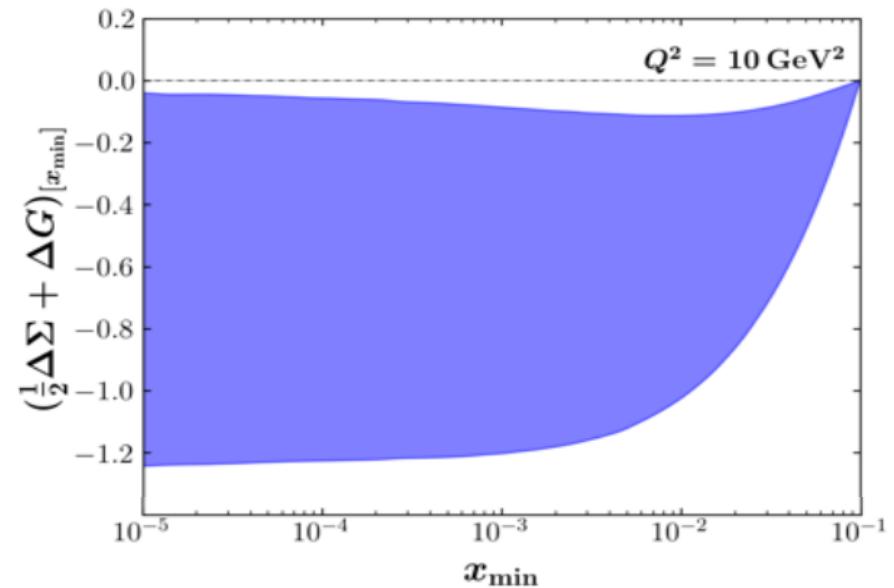


- Small-x evolution drives a definite **curvature of $g_1(x)$** -- but the **sign is unconstrained** from current data for a few new amplitudes
- **Need some kind of additional input:** smaller-x data, theory of small-x hadron production in polarized pp, or controlled matching to large x

New Global Analysis



- Small-x signs of most distributions span zero due to a few poorly-constrained amplitudes
- Preference for negative spin contribution from small x ?
- **Stay tuned!**



Parting Comment: The Roots of Spin are Chiral

- **Helicity** shares an intimate connection with the **axial vector current**

Jaffe and Manohar, *Nucl. Phys.* **B337** 509 (1990)

A. Tarasov, R. Venugopalan,
Phys. Rev. **D100** (2019), **D102** (2020), **D105** (2022)

$$\Delta q(x, Q^2) = \int \frac{dr^-}{2\pi} e^{ixp^+ r^-} \left\langle pS_L \left| \bar{\psi}(0) \mathcal{U}[0, r] \frac{\gamma^+ \gamma^5}{2} \psi(r) \right| pS_L \right\rangle$$

- The **total quark helicity** leads to a **local matrix element** of the **axial vector current**.

$$\Delta\Sigma(Q^2) = \sum_q \int_0^1 dx (\Delta q + \Delta \bar{q})(x, Q^2) = \frac{1}{p^+} \sum_q \langle pS_L | \bar{\psi}(0) \frac{\gamma^+ \gamma^5}{2} \psi(0) | pS_L \rangle \sim \frac{\langle j_5^+ \rangle}{p^+}$$

- Opens the door to nonperturbative contributions from the **axial anomaly**

$$\partial_\mu j_5^\mu = \frac{\alpha_s N_f}{2\pi} \text{tr} \left(F_{\mu\nu} \tilde{F}^{\mu\nu} \right)$$

Parting Comment: The Roots of Spin are Chiral

$$\langle p' S_L | j_5^\mu | p S_L \rangle = \frac{1}{4\pi^2} \frac{\ell^\mu}{\ell^2} \int \frac{d^4 k}{(2\pi)^4} \text{tr} F_{\alpha\beta}(k) \tilde{F}^{\alpha\beta}(-k - \ell)$$

$$\ell^\mu = p'^\mu - p^\mu$$

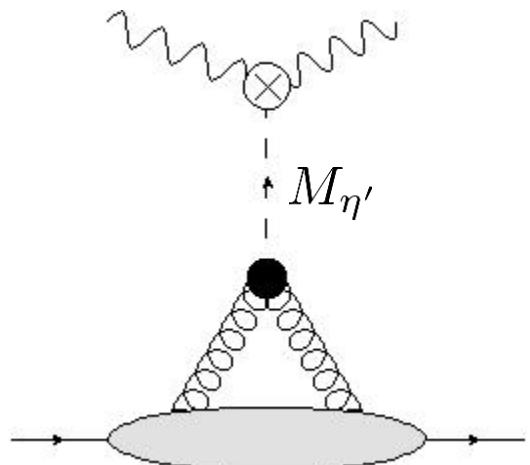
- Singularities in $\frac{1}{t}$ appear in the forward limit, **beyond those captured by collinear factorization**

*S. Bhattacharya, Y. Hatta, W. Vogelsang,
Phys. Rev. D107 (2023), arxiv: 2305.09431*

- This pole can be interpreted as the **exchange of a scalar η' meson**, coupled to gluon helicity: $g \phi_{\eta'} F \tilde{F}$.

*A. Tarasov, R. Venugopalan,
Phys. Rev. D100 (2019), D102 (2020), D105 (2022)*

- Does collinear factorization capture **all** the contributions to g_1^p ?



Conclusions

- Spin at small x lies at the intersection of multiple frontiers in hadronic structure:
 - Longitudinal coherence
 - Sub-eikonal degrees of freedom (spin)
 - High density / saturation
- Theory and phenomenology of spin at small x is developing rapidly!

