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## The Polarized Hydrogen Gas Jet Target. From RHIC to EIC.

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#### Hadronic polarimetry at the EIC



High energy, 41-275 GeV polarized proton and helion (<sup>3</sup>He<sup>↑</sup>) beams are planned at the future Electron Ion Collider.

The requirement for the EIC beam polarimetry:

 $\sigma_P^{\rm syst}/P \lesssim 1\%$ 

Compared to RHIC, there are new challenges for the hadronic beam polarimetry at EIC

- Much shorter, 10 ns bunch spacing (107 ns at RHIC)
- <sup>3</sup>He↑ beam

- A complete analysis of the beam polarization includes measurement of the polarization profile, polarization decay time, ...
- The main goal of this presentation is to discuss the RHIC Hydrogen Jet Target (HJET) feasibility to provide absolute calibration of the p<sup>↑</sup> and <sup>3</sup>He<sup>↑</sup> beam polarization at EIC.

#### The Atomic Polarized Hydrogen Gas Jet Target (HJET)

- HJET was designed to measure absolute polarization of the proton beams with accuracy <5% in RHIC Spin Program.
- It was commissioned in 2005.
- The actual performance of HJET significantly surpassed the design requirements.
- The jet target polarization is  $P_{jet} \approx 96 \pm 0.1$  %.
- The hydrogen gas target allows us to measure spin asymmetry in CNI region  $0.0013 < -t < 0.018 \text{ GeV}^2$  (where analyzing power is well predictable) with low background and low systematic uncertainties.
- During RHIC Runs, HJET can operate continuously in parasitic mode (i.e., without disturbing RHIC beams).
- In numerous measurements (for 20 years) with proton p<sup>↑</sup> and ion (d, 0, Al, Ru, Zr, Au) beams
  - transverse analyzing powers  $A_N(t)$  for  $p^{\uparrow}p$  and  $p^{\uparrow}A$ scattering was measured
  - HJET performance was well studied





#### The HJET recoil spectrometer



AP et al., Nucl. Instrum. Meth. A 976, 164261 (2020)

- The vertically polarized proton beams are scattered from the vertically polarized gas jet target.
- The recoil protons are detected in the vertically oriented Si strip detectors.
- For elastic events  $\frac{Z_R Z_{jet}}{L} \approx \sqrt{\frac{Z_R Z_{jet}}{L}}$

$$\frac{\overline{T_R}}{2m_n} \times \left(1 + \frac{m_p}{E_{\text{heam}}}\right)$$

 $T_R = -t/2m_p$  is (measured) kinetic energy of the recoil proton

The beam polarization can be precisely determined ailed knowledge of the analyzing power

$$a_{\text{beam}}(T_R) = \frac{N_R^{\uparrow} - N_R^{\downarrow}}{N_R^{\uparrow} + N_R^{\downarrow}} = A_N(t)P_{\text{beam}}$$

$$P_{\text{beam}} = \frac{\langle a_{\text{beam}}(T_R) \rangle}{\langle a_{\text{jet}}(T_R) \rangle} = \frac{N_R^{+} - N_R^{-}}{N_R^{+} + N_R^{-}} = A_N(t)P_{\text{jet}}$$

$$_{\text{eam}} = \frac{\langle a_{\text{beam}}(T_R) \rangle}{\langle a_{\text{jet}}(T_R) \rangle} P_{\text{jet}}$$

Typical results for an 8-hour store in RHIC Run 17 (255 GeV)

$$P_{beam} \approx (56 \pm 2.0_{stat} \pm 0.3_{syst})\%$$
  
 $\sigma_P^{syst}/P_{beam} \lesssim 0.5\%$ 

#### Isolation of the elastic pp events



- Only few percent of all detected events are elastic recoil protons.
- Nonetheless, for 107 ns bunch spacing at RHIC, the elastic events can be easily isolated, and background can be properly subtracted.
- However, to validate the method **10** ns bunch spacing at **EIC**, a special study is needed.

#### Reconstruction of the punch-through proton kinetic energy



Signal parametrization:  $W(t) = p + A (t - t_i)^n \exp\left(-\frac{t - t_i}{\tau_s}\right)$ 

- The signal wave form shape depends on the recoil proton energy.
- It allows us to reconstruct kinetic energy of the punch-through recoil protons.



[us]

Time

100

80

60

40

20

0

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Kinetic Energy [MeV]

Time [ns]

10<sup>3</sup>

10<sup>2</sup>

10

10

12

8

Detected Energy [MeV]

100

80

60

40

20

0

2

#### Isolation of the elastic pp events



- To isolate elastic events:
  - The measured time-of-flight is compared with ToF corresponding measured  $T_R$  (the detected particle is proton)
  - The measured  $\sqrt{T_R}$  is compared with  $\sqrt{T_R}$  corresponding to the Si strip
  - (the scattered particle is proton)
- Since, for fixed  $T_R$ , the background rate is <u>about</u> the same in all strips of the Si detector, background events can be subtracted (separately for each combination of the beam and jet spins) from the elastic data. However, the results of the background suppression may be affected by
  - Inelastic events
  - Tracking of the recoil protons in the Holding Field magnet.

#### Inelastic scattering in HJET

At the HJET, the elastic and inelastic events can be separated by comparing recoil proton energy and z coordinate (i.e. the Si strip location). For  $A + p \rightarrow X + p$  scattering:

$$\frac{Z_R - Z_{jet}}{L} = \sqrt{\frac{T_R}{2m_p}} \times \left[1 + \frac{m_p}{E_{beam}} + \frac{m_p \Delta}{T_R E_{beam}}\right]$$

 $\Delta = M_X - M_A$ E<sub>beam</sub> is the beam energy per nucleon

- The inelastic events occupy the area above the elastic line.
- For the 100 GeV beam, the inelastic event detection in HJET is strongly suppressed.
- For 255 GeV elastic events are well detected (but not overlapped with the elastic ones)



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#### Recoil proton tracking in the magnetic field



Currents in the Helmholtz coils are adjusted to minimize alteration of the recoil proton z-coordinate in the Si detector

 $_{R}$  = 1 MeV

MeV

- field may result in incorrect background subtraction.
- For  $T_R < 2$  MeV, the corresponding systematic error i value of the polarization may be  $1 \div 3\%$ .
- In the data analysis, the residual background was simulated.

-5

-10

0

Z<sub>jet</sub>

cm

10

#### The anticipated "bunch spacing" problem at EIC.

Significant decreasing of the bunch spacing,  $107 \text{ ns} \rightarrow 10 \text{ ns}$ , at EIC may be an issue due to mixing prompts and elastic pp signals from different bunches.



HJET performance at EIC can be easily emulated by using RHIC experimental data and shifting the measured time with 8.9 ns (107/12) step.

Usage of the reconstructed kinetic energy results in a significant improvement.



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#### Proton Beam Polarization measurements. EIC vs RHIC.

The emulated (8.9 ns bunch spacing) data was processed using regular HJET software.



- Since the same events are used in two (107 and 8.9 ns bunch spacing) determination of the beam polarization, only bunch spacing related systematic errors can contribute to the discrepancy in the two distributions.
- For  $T_R > 2$  MeV, the corresponding errors are small,  $|\delta P/P \leq 0.2\%|$ .
- In the RHIC measurements, the following kinetic energy cuts were used,

 $T_R > 0.7 \text{ MeV} (100 \text{ GeV})$  and  $T_R > 2.0 \text{ MeV} (255 \text{ GeV})$ 

## Prototype of a double-layer detector for HJET

- The prompts **are usually considered** as fast charged particles, which penetrate the Si detectors.
- To veto prompts, a prototype of a double layer detector was assembled and tested
- Although the prototype design was not optimized, a reliable vetoing of the prompts was foreseen.



#### The prototype did not work as expected.

For the non-vetoed events (about 30-40% of all prompts):

- Time of flight is consistent with speed of light.
- The wave form shape is like that of stopped particles in the Si strip.

My best **guess** is that non-vetoed prompt events are due to the Si nuclear breakup by a  $\gamma$  (from a  $\pi^0$  decay) or ultra-fast minimum ionizing charged particles (which are not detected in the Si strip due to low dE/dx). In this case there may be no correlation between signals in two detector layers. However, I have no realistic model for such a process and, consequently, **have no proves that the guess is correct.** 

### Elastic single spin proton-proton analyzing power $A_{\rm N}(s, t)$



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## How to measure the EIC <sup>3</sup>He beam polarization with HJET?

$$P_{\text{meas}}^{h}(T_{R}) = P_{\text{jet}} \frac{a_{\text{beam}}(T_{R})}{a_{\text{jet}}(T_{R})} \times \frac{A_{N}^{p^{\uparrow}h}(T_{R})}{A_{N}^{h^{\uparrow}p}(T_{R})}$$
$$= \frac{a_{\text{beam}}}{a_{\text{jet}}} P_{\text{jet}} \times \frac{\kappa_{p} - 2I_{5}^{ph} - 2R_{5}^{ph}T_{R}/T_{c}}{\kappa_{h} - 2I_{5}^{hp} - 2R_{5}^{hp}T_{R}/T_{c}}$$
$$\approx P_{\text{beam}}^{h} \times (1 + \xi_{0} + \xi_{1}T_{R}/T_{c})$$

AP, Phys. Rev. C 106, 065202 (2022)

$$\kappa_p = \mu_p - 1 = 1.793$$
  
 $\kappa_h = \mu_h / Z_h - m_p / m_h = -1.398$   
 $T_c \approx 0.7 \text{ MeV}$ 

$$\kappa_p/\kappa_h = -1.283$$

The systematic uncertainties in value of  $P_{\text{beam}}^{h}$  are defined by  $\xi_{0}$ ,  $\xi_{0} = 2\delta I_{5}^{hp}/\kappa_{h} - 2\delta I_{5}^{ph}/\kappa_{p}$ ,  $\xi_{1}$  - can be determined in the measurements

Since  $r_5^{pA} = r_5^{pp} \frac{i+\rho^{pA}}{i+\rho^{pp}} \approx r_5^{pp}$  [B. Kopeliovich and T. Trueman, Phys. Rev. D 64, 034004 (2001)],  $r_5^{ph} \approx r_5^{pp}$  $r_5^{hp} \approx r_5^{pp} \langle P_N \rangle \approx r_5^{pp}/3$ 

Systematic error in the  ${}^{3}$ He beam polarization measurement:  $\sigma_{P}^{\rm syst}/P = 0.5\%_{r_{5}^{pp}} \oplus 0.2\%_{
m theor}$ 

## <sup>3</sup>He breakup

#### AP, Phys. Rev. C 106, 065203 (2022)

A counter-intuitive observation in the HJET measurements with 3.8-100 GeV/n Au beams: no evidence (<0.5% of elastic rate)of Au breakup were found in the data analysis

For incoherent proton-nucleus scattering, a simple kinematical consideration gives:

$$\Delta = \left(1 - \frac{m^*}{M_A}\right)T_R + p_x \sqrt{\frac{2T_R}{m_p}},$$

where  $\Delta = M_X - M_A$  is missing mass excess,  $m^* = m_p$  and  $p_x$  is the target nucleon transverse momentum.

Since  $T_R$  and, consequently,  $\Delta$  are small at HJET, the breakup is strongly suppressed by the phase space factor.

Assuming the following  $p_x$  distribution,

$$f_{\rm BW}(p_x,\sigma_p) = \frac{\pi^{-1}\sqrt{2}\sigma_p}{p_x^2 + 2\sigma_p^2}, \qquad \int f_{\rm BW}(p_x,\sigma_p)dp_x = 1,$$

one finds for a two-body breakup (for given  $T_R$ )

$$dN/d\Delta \propto f_{\rm BW}(\Delta - \Delta_0, \sigma_\Delta) \Phi_2(\Delta), \qquad \Delta_0 = (1 - m^*/M_A)T_R, \ \sigma_\Delta = \sigma_p \sqrt{2T_R/m_p}$$

If the elastic and breakup events cannot be separated in the data:

$$\frac{d\sigma_{el}(T_R) \to d\sigma_{el}(T_R) + \int d\Delta \ \frac{d\sigma_{brk}(T_R,\Delta)}{d\Delta} \varepsilon_{acc.}(T_R,\Delta) = \frac{d\sigma_{el}(T_R) \times [1 + \omega(T_R)]}{\omega(T_R) \to 0 \text{ if } T_R \to 0}$$



#### Experimental evaluation of $\omega(T_R)$

#### AP, Phys. Rev. C 108, 025202 (2023)

- In the deuteron measurements at HJET, it was found  $\omega_d(T_R = 3.5 \text{ MeV}) = 5.0 \pm 1.4\%$ , and an extrapolation to the <sup>3</sup>He breakup,  $\langle \omega_h \rangle_{1-10 \text{ MeV}} = 2.4 \pm 0.4\%$ , had been done.
- The estimates were found to be in reasonable agreement with the hydrogen bubble chamber measurements in Dubna.



J. Stepaniak , Acta Phys. Polon. B 27, 2971 (1996)



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## **Breakup corrections to the** <sup>3</sup>He beam polarization

AP, Phys. Rev. C 108, 025202 (2023)

The breakup corrections,

 $1 + \omega_{\text{int}}(T_R), \qquad \omega_{\text{int}} \in \left\{\omega_{\kappa}^p, \omega_I^p, \omega_R^p, \omega_{\kappa}^h, \omega_I^h, \omega_R^h\right\}$ can also modify the interference terms in the analyzing power ratio  $\frac{\kappa_p - 2I_5^{ph} - 2R_5^{ph}T_R/T_c}{\kappa_h - 2I_5^{hp} - 2R_5^{hp}T_R/T_c} \implies \frac{\kappa_p [1 + \omega_{\kappa}^p] - 2I_5^{ph} [1 + \omega_I^p] - 2R_5^{ph} [1 + \omega_R^p]T_R/T_c}{\kappa_h [1 + \omega_{\kappa}^h] - 2I_5^{hp} [1 + \omega_I^h] - 2R_5^{hp} [1 + \omega_R^h]T_R/T_c}$ 

An incoherent scattering of proton from <sup>3</sup>He can be approximated by scattering off a nucleon  $(m^* = m_p)$ or di-nucleon  $(m^* = 2m_p)$ . Thus, the breakup corrections (to the interference terms) are limited by:  $\omega_{2m}(T_R) \leq \omega_{int}(T_R) \leq \omega_m(T_R)$  $\Delta = (1 - \frac{m^*}{M_A})T_R + p_x \sqrt{\frac{2T_R}{m_p}}$ 

Assuming **linear fit** of the measured polarization  $P_{\text{meas}}^{h}(T_{R})$ ,  $T_{R} > 2$  MeV, the following estimate can be done :

$$\left|P_{\text{meas}}^{h}(T_{R})/P_{\text{beam}}^{h}-1\right| < \left|\omega_{m}(T_{R})-\omega_{2m}(T_{R})\right|/2 \approx -0.11\% + 0.13\% \frac{T_{R}}{T_{c}}$$

In a more accurate fit, the breakup correction can be reduced to a negligible level

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#### Summary

- Systematic uncertainties  $\sigma_P^{\text{syst}}/P$  in the absolute calibration of the proton and <sup>3</sup>He beam polarization at EIC were estimated (predicted) as
  - p: 0.6% meas <sup>3</sup>He: 0.6% meas ⊕ 0.5%  $r_r^{pp}$
- For the helion beams with energy <100 GeV/n , proton-proton  $r_5^{pp}$  may be needed to be pre-determined before the <sup>3</sup>He beam polarization measurement
- To improve the data analysis (*including the development of the calibration methods*), the following can (should) be considered:
  - Optimization of the reconstruction of the punch-through recoil proton kinetic energy
  - More accurate analysis of the recoil proton tracking in the magnetic field.
  - Optimization of the detector geometry for better evaluation of the background.
  - Understanding of the prompts.
  - More accurate theoretical analysis of the breakup corrections to the <sup>3</sup>He beam polarization measurements

#### From the analysis done, it follows that

HJET, as it was designed for RHIC Spin Program, has a capability to precisely,  $\sigma_P^{\text{syst}}/P \leq 1\%$ , measure absolute polarization of the proton and helion beams at EIC.

# Backup

#### **Calibration Using Alpha-sources**



All Si detectors are exposed by 2  $\alpha$ -sources:  $^{148}Gd$  (3.183 MeV) <sup>241</sup>*Am* (5.486 *MeV*) Gain ( $\alpha \sim 2.5 \ keV/cnt$ ) and dead-layer thickness ( $x_{DL} \sim 0.37 mg/cm^2$ ) were measured for every Si strip.

Energy resolution  $\sigma_E \approx 20 \ keV$  is dominated by electronic noise. (For CAMAC DAQ  $\sigma_E \sim 30 \ keV$ )



#### **Event Selection Cuts.**

- 1. Recoil proton kinetic energy  $T_R$ . The measured kinetic energy range  $(0.5 \div 11 \text{ MeV})$  is limited by the detector geometry and the trigger threshold )
- 2. "Recoil mass cut":  $\delta t = t_m t_p(A)$

 $t_p(A)$  is the expected proton signal time for the measured amplitude A. It depends on gain, dead-layer and time offset which are found in calibrations.

The  $\delta t$  distribution is defined by the beam bunch longitudinal profile.

"Missing mass cut":  $\delta \sqrt{T_R} = \sqrt{T_R} - \sqrt{T_{strip}}$ 3.

 $T_{\rm strip}$  is the energy corresponding to the strip center. It is determined in the geometry alignment. The  $\delta \sqrt{T_R}$  distribution is defined by the jet density profile.

r elastic scattering, the 
$$\left(\frac{d\sigma}{dt}\sqrt{T_R}\right)^{-1} \frac{d^2N}{d\delta t \, d\delta \sqrt{T_R}}$$
 distribution

is the same for all Si strips.

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**Minimum systematic error cuts**  $3.2 < T_R < 7.6 \text{ MeV}$  $-7 < \delta t < 7$  ns  $-0.18 < \delta \sqrt{T_R} < 0.3 \text{ MeV}^{1/2}$ PSTP 2017. HJET in RHIC Run17.



#### **Background subtraction**



- The background subtraction is based on the assumption that background  $dN/d\sqrt{T_R}$  distribution is the same for all Si strips.
- In the data analysis, the background is determined/subtracted independently for
  - every detector
  - > every  $\sqrt{T_R}$  bin
  - every combination of beam/jet spins (to properly account background analyzing power if any)



## Measurements of $A_N(t)$ in Runs 15 (100 GeV) & 17 (255 GeV)



AP et al., Phys. Rev. Lett. 123, 162001 (2019)

- The filled areas specify  $1\sigma$ experimental uncertainties, stat.+syst., scaled by x50.
- Hadronic spin-flip amplitude parameter  $r_5 = \frac{m_p \phi_5^{had}(s, t)}{\sqrt{-t} \operatorname{Im} \phi_+^{had}(s, t)} = R_5 + iI_5$

#### The measured hadronic spin flip amplitudes:

 $\sqrt{s} = 13.76 \text{ GeV} \quad R_5 = (-12.5 \pm 0.8_{\text{stat}} \pm 1.5_{\text{syst}}) \times 10^{-3}$   $I_5 = (-5.3 \pm 2.9_{\text{stat}} \pm 4.7_{\text{syst}}) \times 10^{-3}$   $\sqrt{s} = 21.92 \text{ GeV} \quad R_5 = (-3.9 \pm 0.5_{\text{stat}} \pm 0.8_{\text{syst}}) \times 10^{-3}$   $I_5 = (19.4 \pm 2.5_{\text{stat}} \pm 2.5_{\text{syst}}) \times 10^{-3}$ The corrections due to absorption and the updated value of the proton charge radius  $r_p = 0.841$  fm were applied  $R_5 = R_5^{\text{PRL}} + (3.1_{\text{abs.}} + 0.8_{r_n}) \times 10^{-3}$ 



On the possibility of measuring the polarization of the <sup>3</sup>He beam at EIC by the HJET

#### Double spin-flip analyzing power $A_{NN}(s, t)$

A.A. Poblaguev et al., Phys. Rev. Lett. 123, 162001 (2019)

 $\frac{d^2\sigma}{dtd\varphi} \propto \left[1 + A_{\rm N}(t)\sin\varphi\left(P_b + P_j\right) + A_{\rm NN}(t)\sin^2\varphi P_b P_j\right] \text{ (at HJET, } \sin\varphi = \pm 1)$ Double spin-flip amplitude parameter  $r_2 = \frac{\phi_2^{had}(s,t)}{2 \operatorname{Im} \phi_{\perp}^{had}(s,t)} = R_2 + iI_2$  $0.004 \models A_{\rm NN}(T_p)$ 0.003  $\sqrt{s} = 13.76 \text{ GeV}$   $R_2 = (-3.65 \pm 0.28_{\text{stat}}) \times 10^{-3}$  $I_2 = (-0.10 \pm 0.12_{\text{stat}}) \times 10^{-3}$ 0.002  $E_{\text{beam}} = 100 \text{ GeV}$  $\sqrt{s} = 21.92 \text{ GeV}$   $R_2 = (-2.15 \pm 0.20_{\text{stat}}) \times 10^{-3}$ 0.001 =255 GeV  $I_2 = (-0.35 \pm 0.07_{\text{stat}}) \times 10^{-3}$ 0.000  $\times 10^3$ 0.0  $T_{R}$ [GeV]  $r_{r}^{2}$ -0.2 100 GeV -0.4255 GeV -0.6-2 Re  $r_2 \times 10^3$ On the possibility of measuring the polarization of the <sup>3</sup>He beam at 24 HEP23 2023.01.12 EIC by the HJET

 $p_{\text{beam}}^{\uparrow} + p_{\text{jet}}^{\uparrow} \rightarrow X_{\text{beam}} + p_{\text{jet}}^{\uparrow}$ 



On the possibility of measuring the polarization of the <sup>3</sup>He beam at EIC by the HJET

#### **Proton-nucleus Scattering at HJET**



In the Au beam measurements at HJET ( $\Delta \gtrsim 4$  MeV,  $3.8 < E_{\text{beam}} < 100$  GeV/n), no evidence of the breakup fraction in the elastic data was found.

$$\begin{pmatrix} \frac{d\sigma_{\text{brk}}^{p\text{Au}}(T_R,\Delta)}{d\sigma_{\text{el}}^{p\text{Au}}(T_R)} \end{pmatrix}_{1.7 < T_R < 4.4 \text{ MeV}}$$

$$3.85 \text{ GeV/n:} \quad 0.20 \pm 0.12\% \quad [3.6 < \Delta < 8.5 \text{ MeV}]$$

$$26.5 \text{ GeV/n:} \quad -0.08 \pm 0.06\% \quad [20 < \Delta < 60 \text{ MeV}]$$

#### A model used to search for the d ightarrow pn breakup events at HJET



- In the HJET measurements,  $\Delta < 50$  MeV is small.
- The breakup to elastic amplitude ratio,  $\psi(T_R, \Delta)$ , is about independent of the  $T_R$  and  $\Delta$ .
- The  $h \to pd$  breakup is strongly suppressed by the phase space factor  $\omega(T_R, \Delta) \propto \sqrt{\Delta \Delta_{\text{thr}}^h}$ .
- For the  $h \to ppn$  breakup the suppression is much stronger  $\omega(T_R, \Delta) \propto (\Delta \Delta_{thr}^h)^2$ .
- The electromagnetic *ph* amplitudes are nearly the same for elastic and breakup scattering.

#### **Deuteron beam measurements at HJET**

- In RHIC Run 16, deuteron-gold scattering was studied at beam energies 10, 20, 31, and 100 GeV/n.
- In the HJET analysis, the breakup events  $d \rightarrow p + n$  $(\Delta_{\text{thr}}^d = 2.2 \text{ MeV})$  were isolated for 10, 20, and 31 GeV data.
- The breakup was evaluated for  $2.8 < T_R < 4.2 \text{ MeV}$
- In the data fit, the  $d \rightarrow pd$  breakup fraction  $\omega(T_R, \Delta)$  was parameterized,

 $|\psi| \approx 5.6$ ,  $\sigma_p \approx 35 \text{ MeV}$ 

• For  $T_R \sim 3.5$  MeV, the breakup fraction was evaluated to be  $\frac{d\sigma_{d \to pn}(T_R)}{d\sigma_{d \to d}(T_R)} = \omega_{d \to pn}(T_R)$ 

$$= |\psi|^2 \int d\Delta \,\omega_{d \to pn}(T_R, \Delta) \approx 5.0 \pm 1.4\%$$

• The result obtained strongly depends on the used parametrization and, thus, a verification is needed.

AP, Phys. Rev. 106, 065203 (2022)



