

# Polarization Observables with a Photon Probe

Spin physics in Nuclear Reactions and Nuclei  
SPIN 2023

Mark Dalton



# Outline

Introduction to Polarized Target Program in Hall D

GDH sum rule on a nuclear target

Exclusive SRC Measurements with Polarization Observables

# GDH Sum Rule

Spin-dependent photoproduction cross-sections

$$\int_{\nu_0}^{\infty} (\sigma^{3/2} - \sigma^{1/2}) \frac{d\nu}{\nu} = \frac{4\pi^2 S \alpha \kappa^2}{M^2}$$

↑ Photon energy      ↑ Mass

↓ spin      ← anomalous magnetic moment

Fundamental Quantum Field Theory prediction. Applicable to any type of target.

Links the anomalous magnetic moment  $\kappa$  of a particle to its helicity-dependent photoproduction cross-sections

Conditions for the sum rule to be valid:

Spin-dependent forward Compton amplitude  $f_2(\nu)$  must vanish at large  $\nu$  (no-subtraction hypothesis).

Imaginary part of  $f_2$ ,  $(\sigma^{3/2} - \sigma^{1/2})$  must decrease with  $\nu$  faster than  $\sim 1/\ln(\nu)$  (for the integral to converge).

Experimentally verified on the proton to  $\sim 10\%$  but not yet for the neutron.

JLab Experiment  
E12-20-011

Measure the high energy behavior of  $\Delta\sigma(\nu)$

Verify **convergence** of integral

$\Delta\sigma(\nu)$  must decrease faster than  $1/\log \nu$

[arXiv.2008.11059](https://arxiv.org/abs/2008.11059)

Test **validity** of sum rule for  
neutron (first time)

proton improve by 25% relative

$$\int_{\nu_0}^{\infty} \frac{\Delta\sigma(\nu)}{\nu} d\nu = \frac{4\pi^2 S\alpha\kappa^2}{M^2}$$

Improve sensitivity to physics that would cause a real (or apparent  $\nu \neq \infty$ ) violation

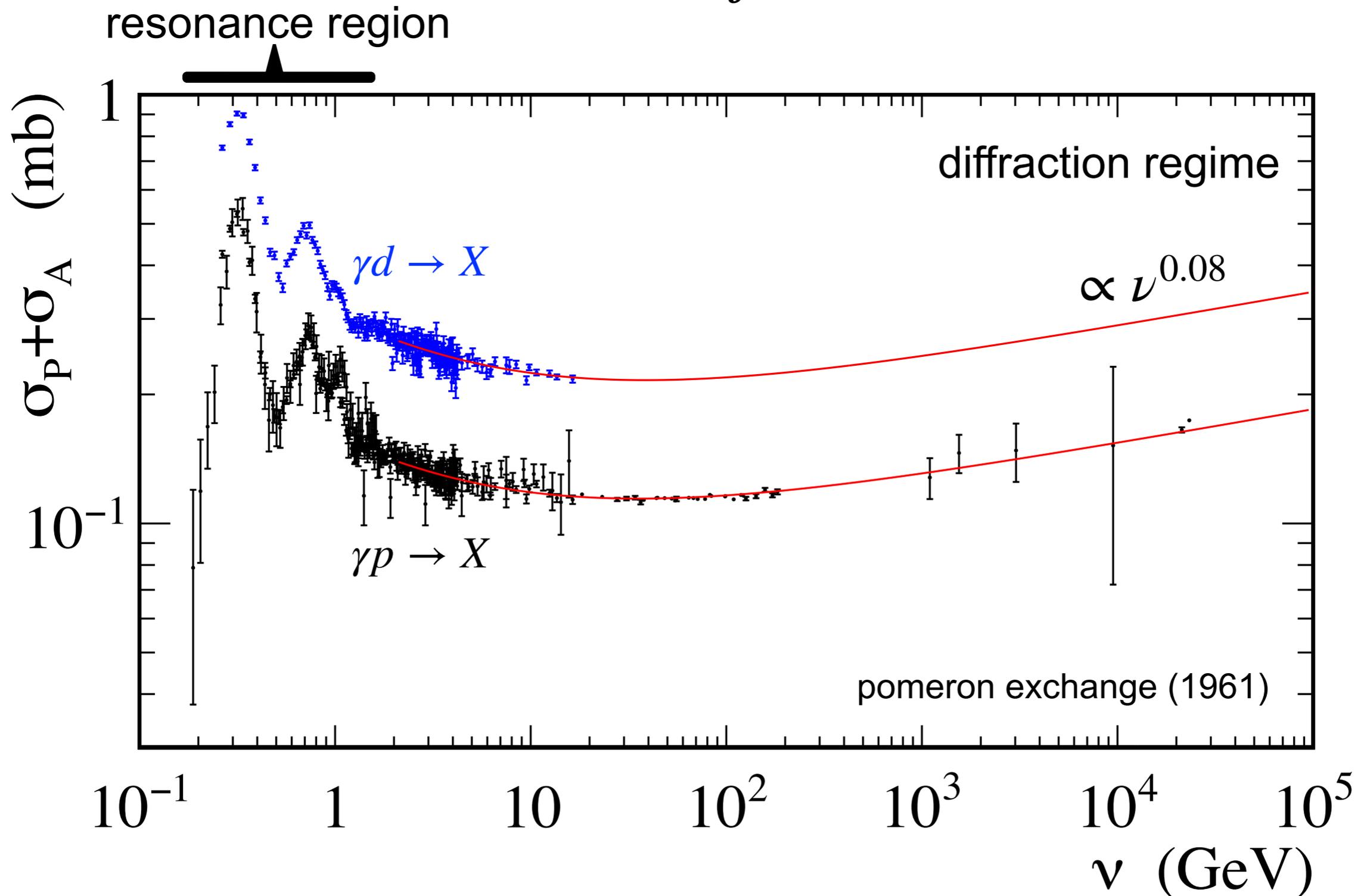
Failure of sum rule would occur at high energy

Stringent test of Regge theory. Resolve discrepancy in Regge parameter determination

Proton and neutron will allow isospin decomposition

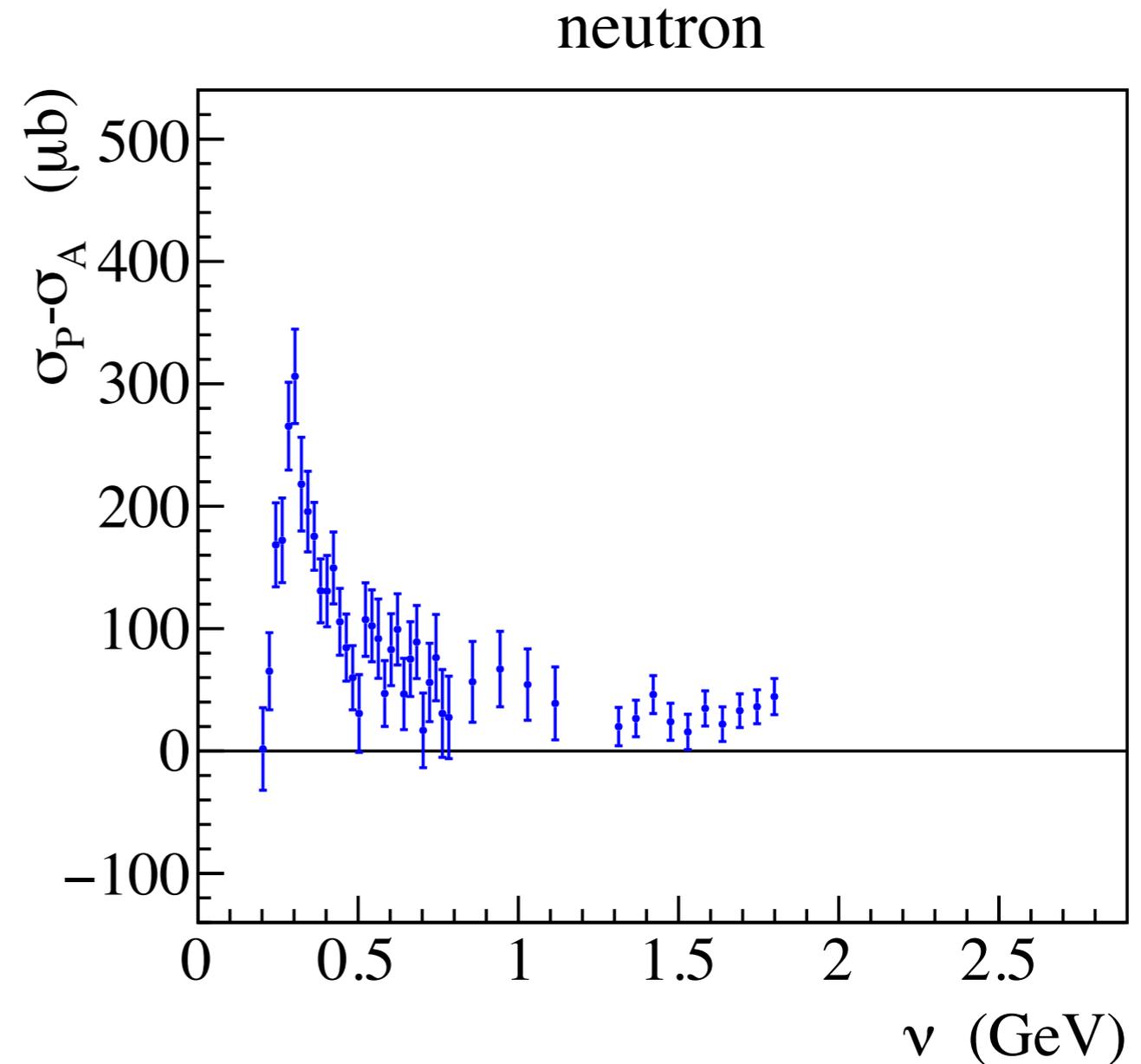
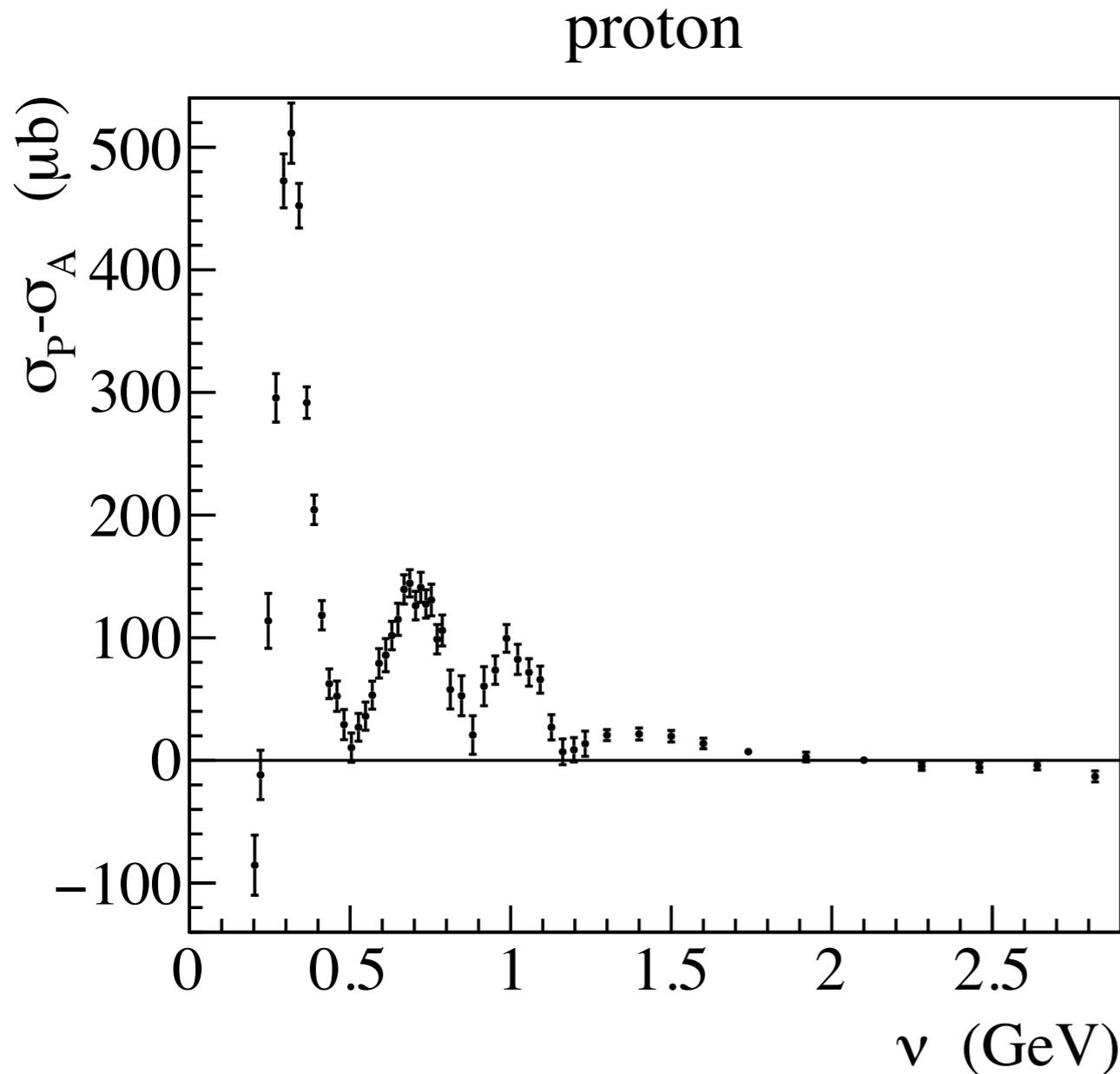
# Photoproduction

Unpolarized version of GDH integral  $\int (\sigma^{3/2} + \sigma^{1/2}) d\nu$  does not converge.



# Helicity dependent photoabsorption

Existing data from MAMI and ELSA. Partial contributions from LEGS and CLAS.



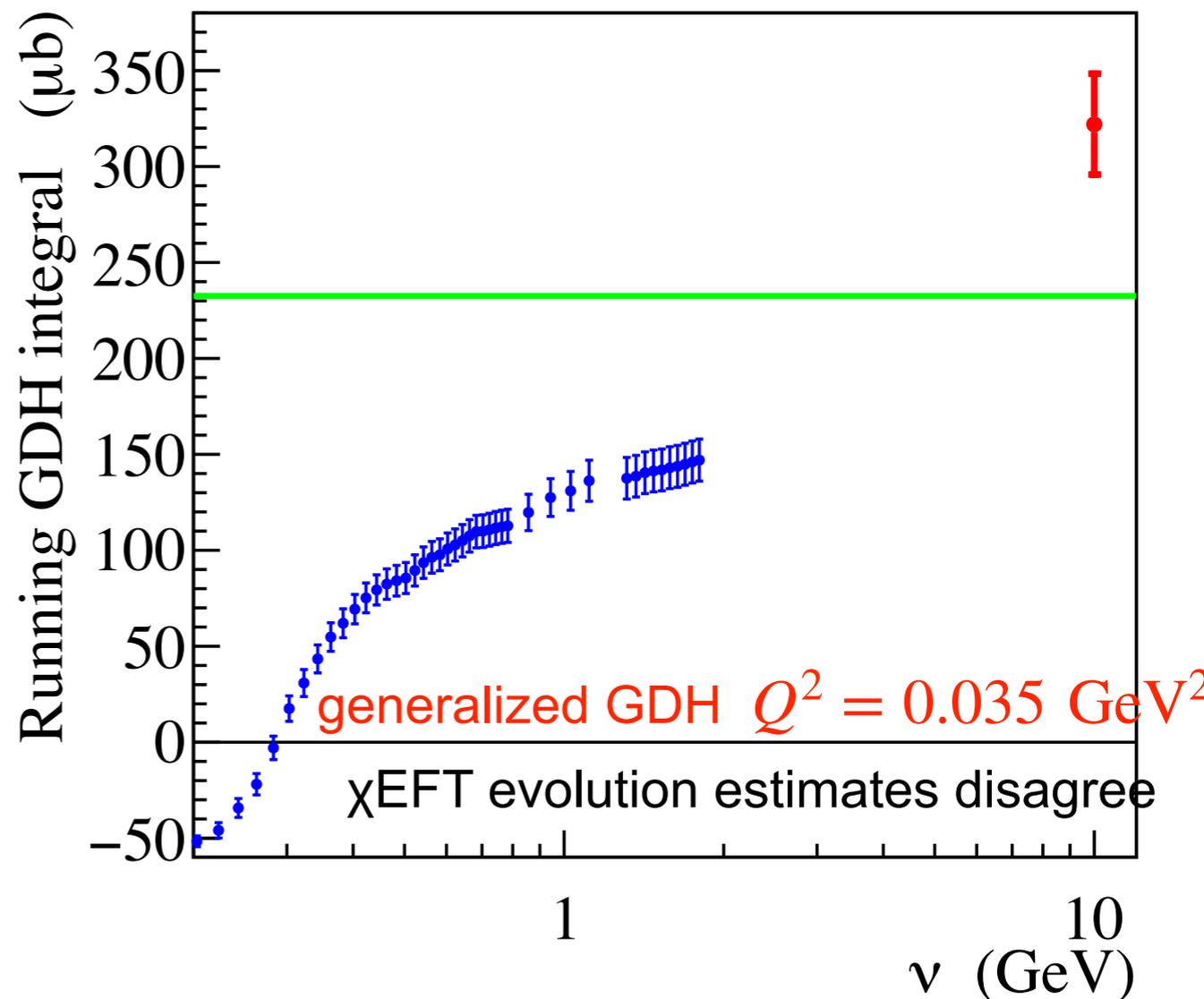
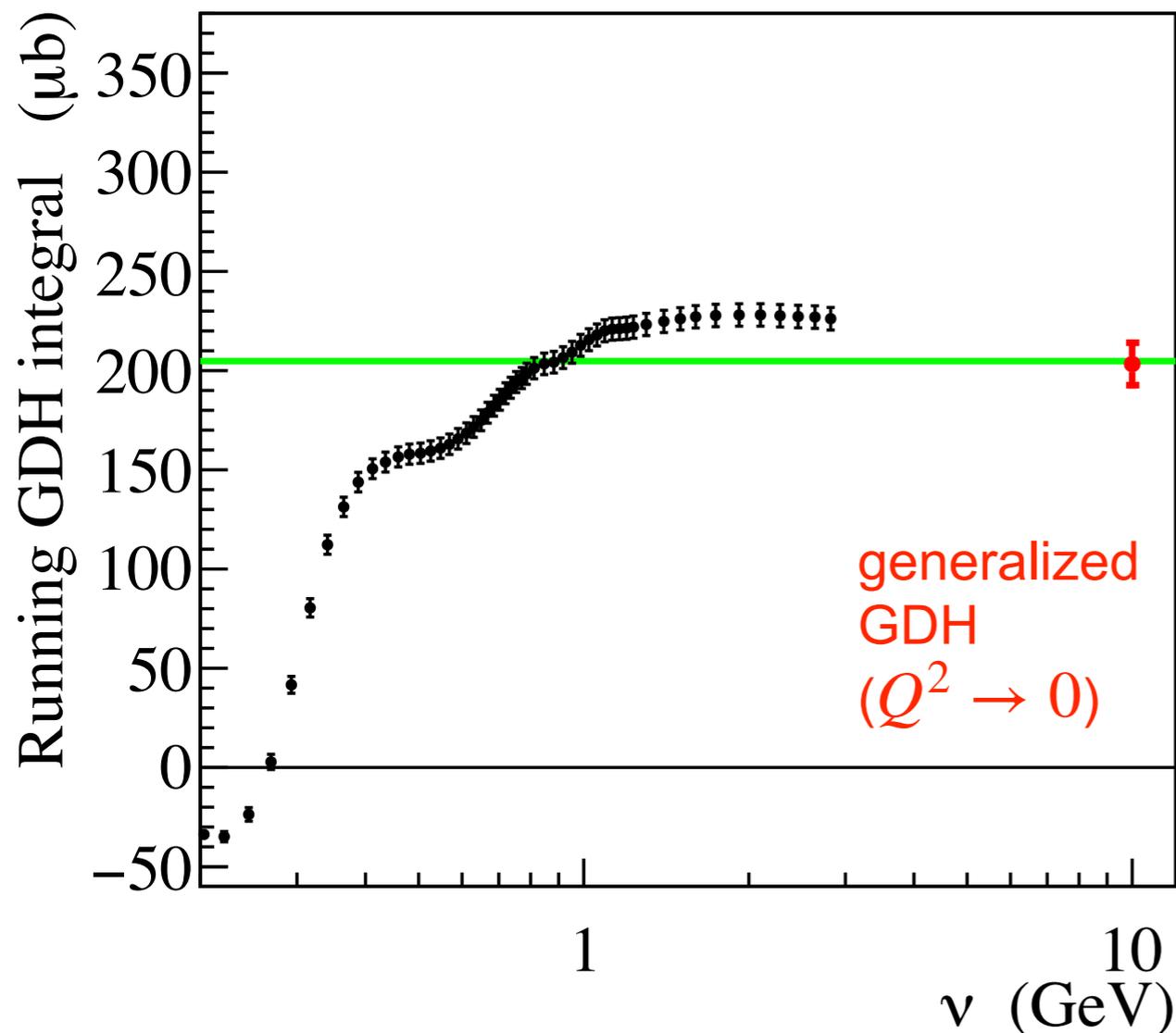
Threshold and high energy regions cannot be measured, need models like MAID/SAID and Regge phenomenology.

# GDH Integral

$$\int_{\nu_0}^{\infty} \frac{\Delta\sigma(\nu)}{\nu} d\nu = \frac{4\pi^2 S\alpha\kappa^2}{M^2}$$

proton

neutron



Unmeasured part estimated using Regge model. Dominates uncertainty.

Has not converged yet

Contributions below 0.2 GeV:  $\approx -28 \mu\text{b}$  (proton),  $\approx -41 \mu\text{b}$  (neutron)

# From Nucleons to Nuclei

## Inclusive Measurements

# Modification of bound nucleons

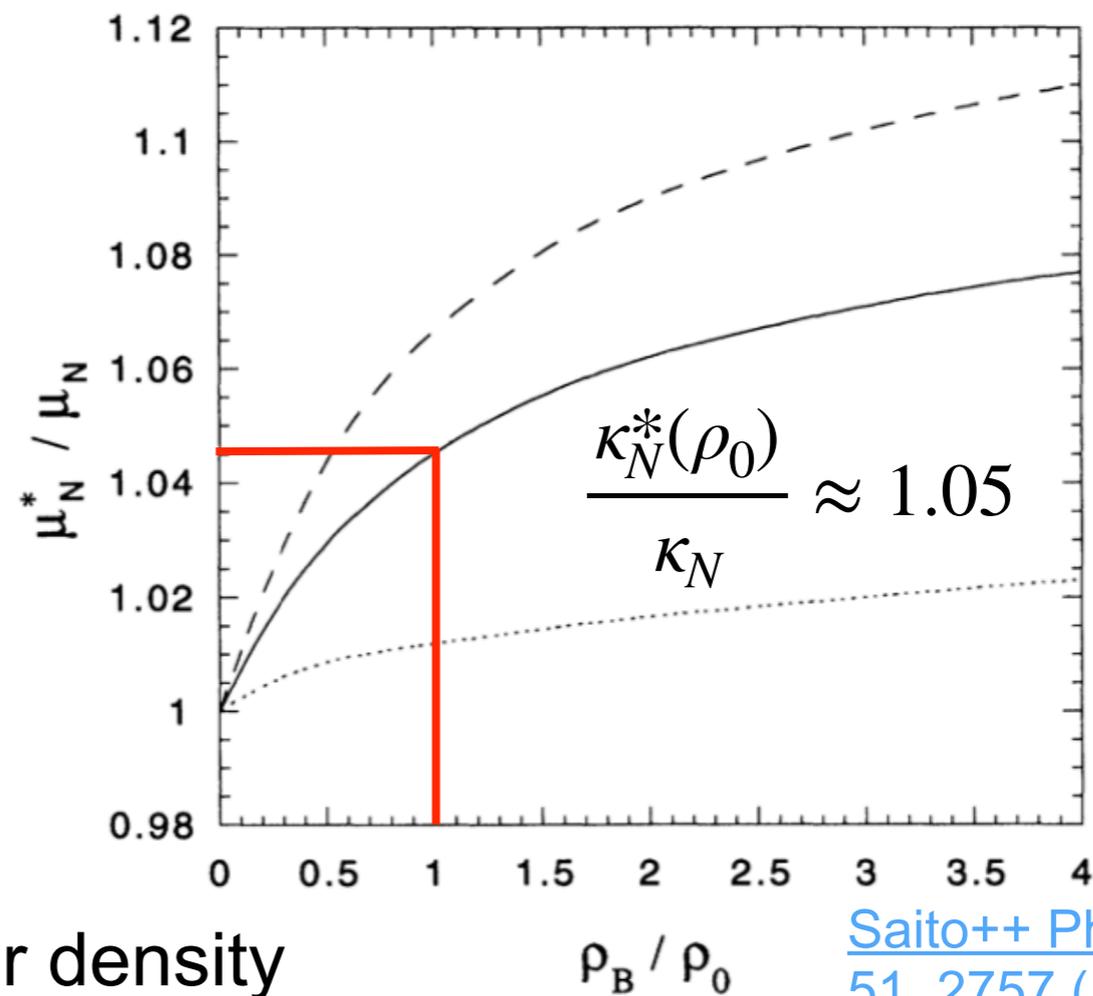
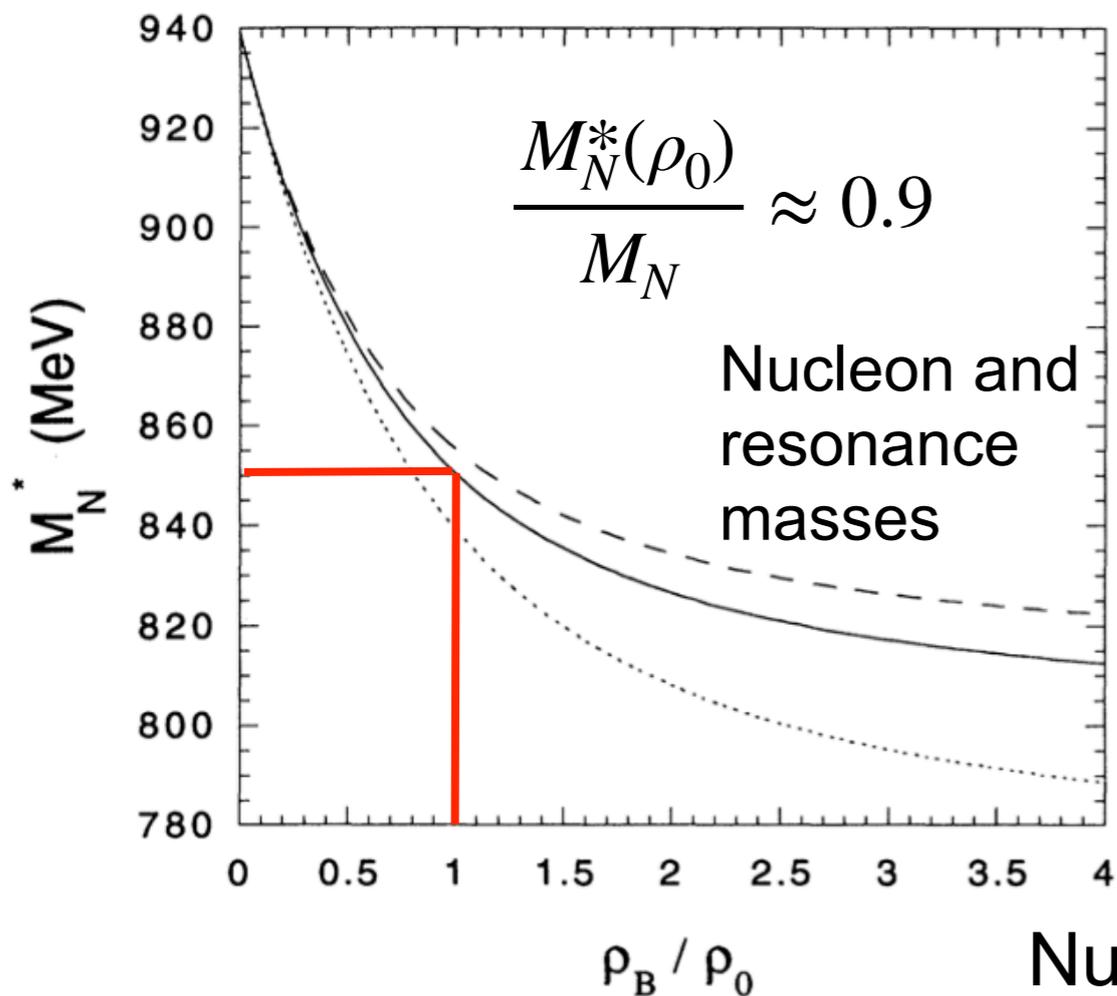
A nucleon in the nuclear medium will be modified  
modification of both sides of the GDH sum rule  
for the nucleon in the nucleus

Bass, Acta Phys. Pol. B 52, 42 (2021)  
Bass++, arXiv:2212.04795 [nucl-th]

Quark Meson Coupling (QMC) model  
predicts modification of mass and  
anomalous magnetic moment.

## Static Side

$$\left( \frac{\kappa_N^*(\rho_0)}{M_N^*(\rho_0)} \right)^2 / \left( \frac{\kappa_N}{M_N} \right)^2 \approx 1.3$$



Saito++ Phys. Rev. C  
51, 2757 (1995)

# The GDH Sum on Nuclei

REGGEON: REGGE on Nuclei

Magnetic moment of a particle with charge  $Qe$ , mass  $M$  and spin  $\vec{S}$ :

$$\vec{\mu} = \frac{e}{M}(Q + \kappa)\vec{S}$$

For a nucleus of mass  $M \approx AM_p$  and charge  $Ze$

$$\vec{\mu} = \frac{e}{AM_p}(Z + \kappa)\vec{S} \implies \kappa = \frac{A}{2|\vec{S}|} \frac{\mu}{\mu_N} - Z$$

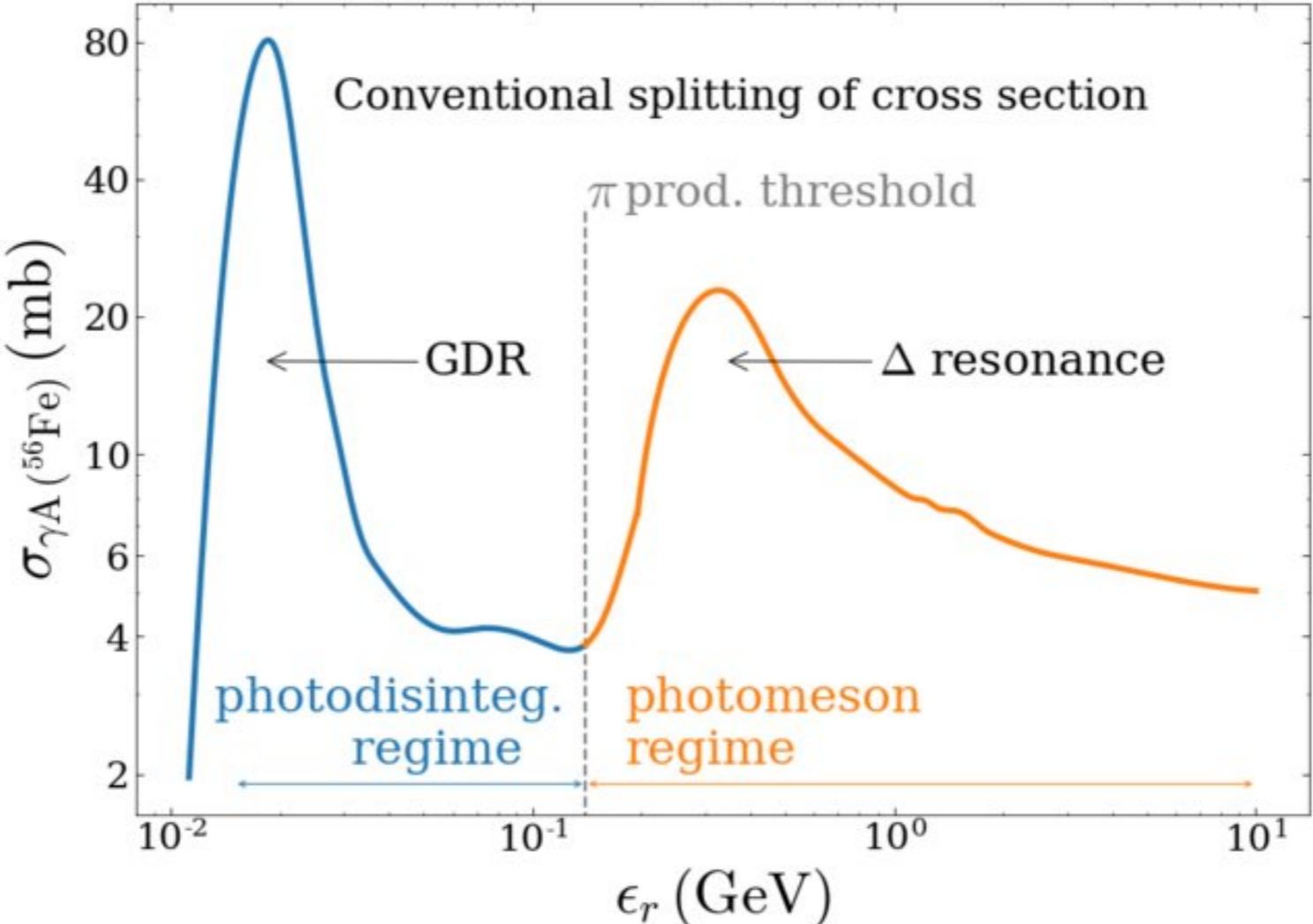
This allows us to calculate  $\kappa$  for all stable nuclei with spin and compute the static part of the GDH sum rule.

# Nuclear spectrum

No data on  $\Delta\sigma$  exists for  $A>3$

photo excitation of nucleus  
properties of nucleus

photoproduction of hadrons  
properties of nucleon



negative

$$I_{\text{GDH}}^* \approx 270 \mu\text{b}$$

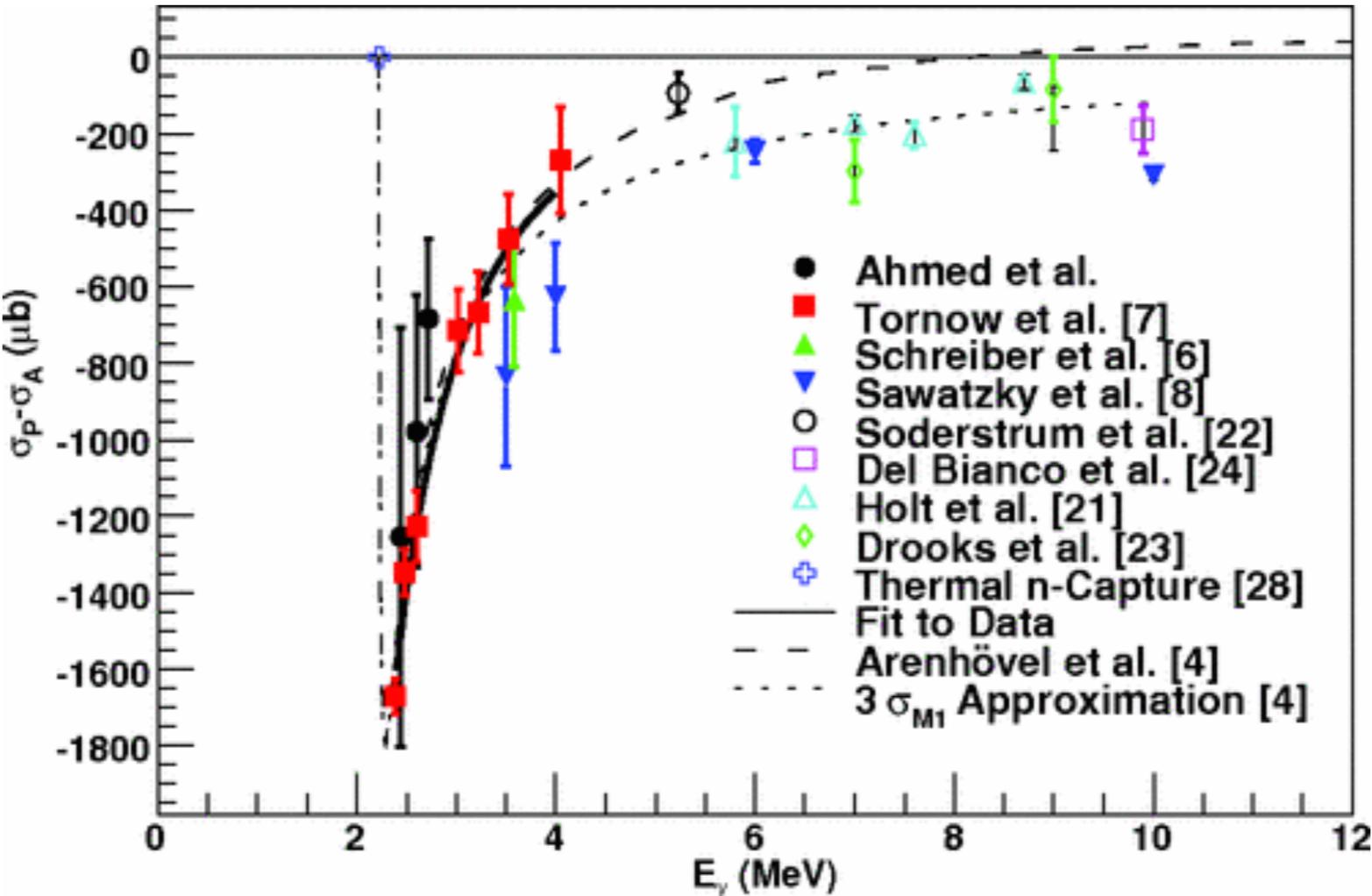
example for  ${}^7\text{Li}$

$$I_{\text{GDH}}^{{}^7\text{Li}} \approx 83 \mu\text{b}$$

Morejon++ JCAP 11, 007 (2019)

# Deuteron

Large negative GDH integrand at low energy.

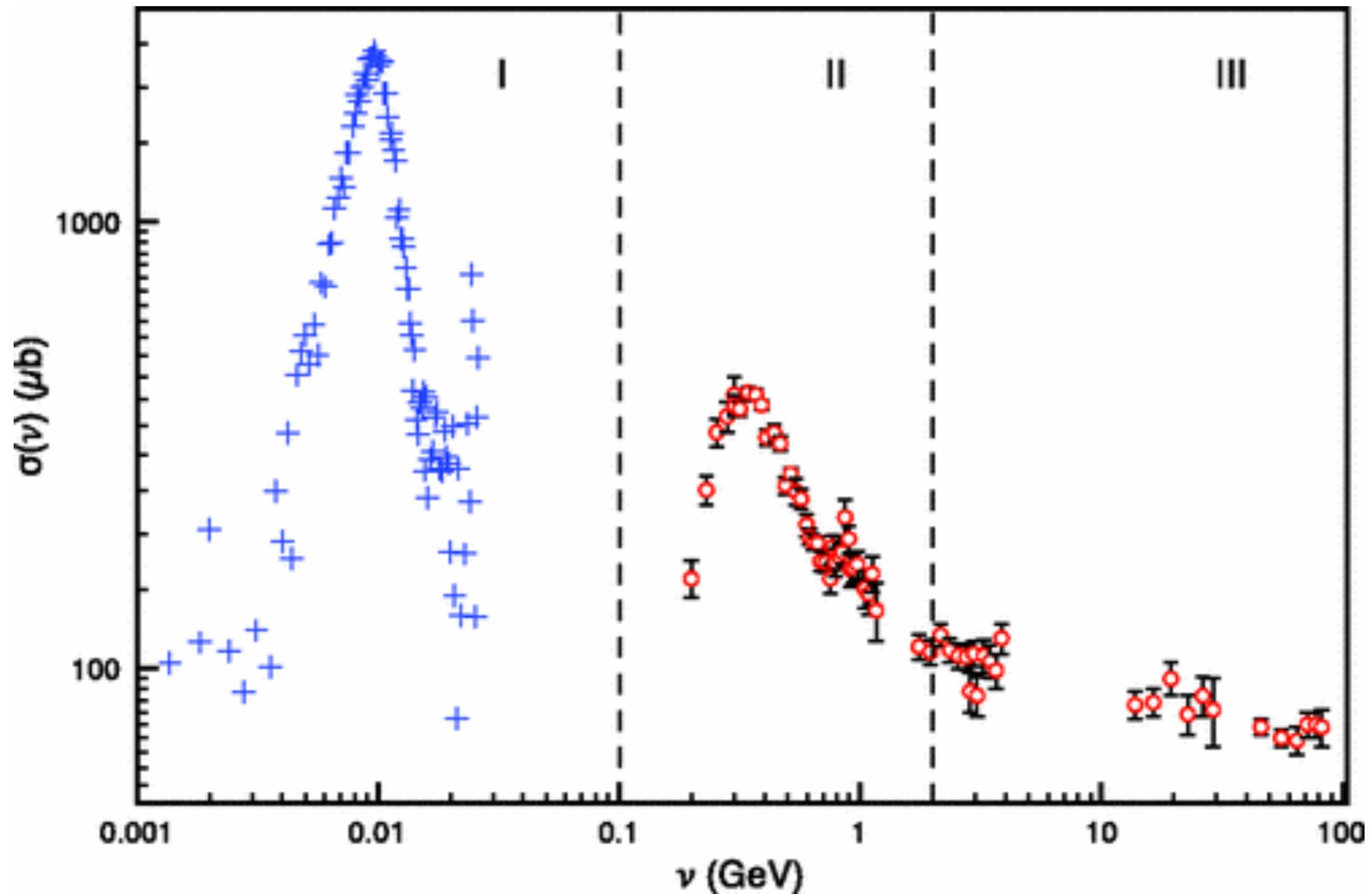


Deuteron GDH indirect

Ahmed++, PRC 77, 044005 (2008)

# Nuclear spectrum

Photoabsorption cross-section data for a  $^{207}\text{Pb}$  target



Gorchtein++ Phys. Rev. C 84 (2011)

# Modification of bound nucleons

## Dynamic (integral) Side

$$\int_{\nu_0}^{\infty} \frac{\Delta\sigma(\nu)}{\nu} d\nu = \frac{4\pi^2 S\alpha\kappa^2}{M^2}$$

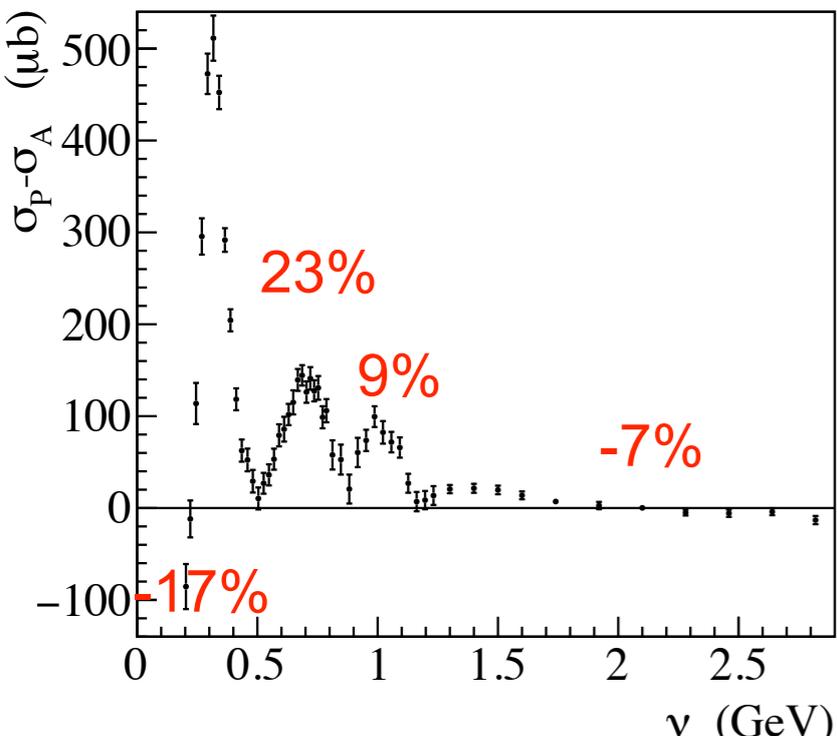
In-medium shift of resonance mass,  $1/\nu$  dependence (slower than  $1/M^2$ )

$\Delta(1232)$

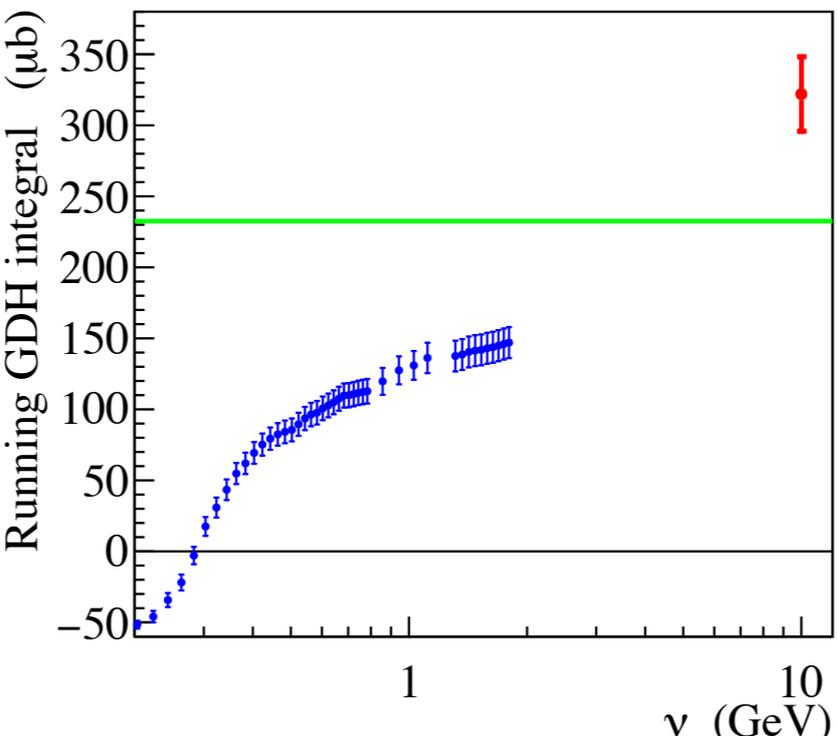
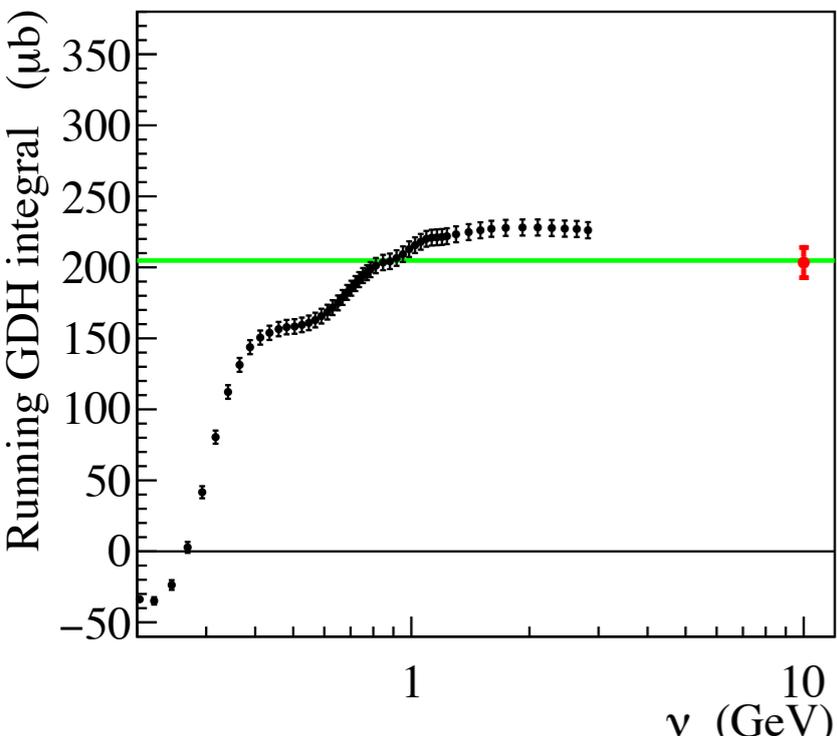
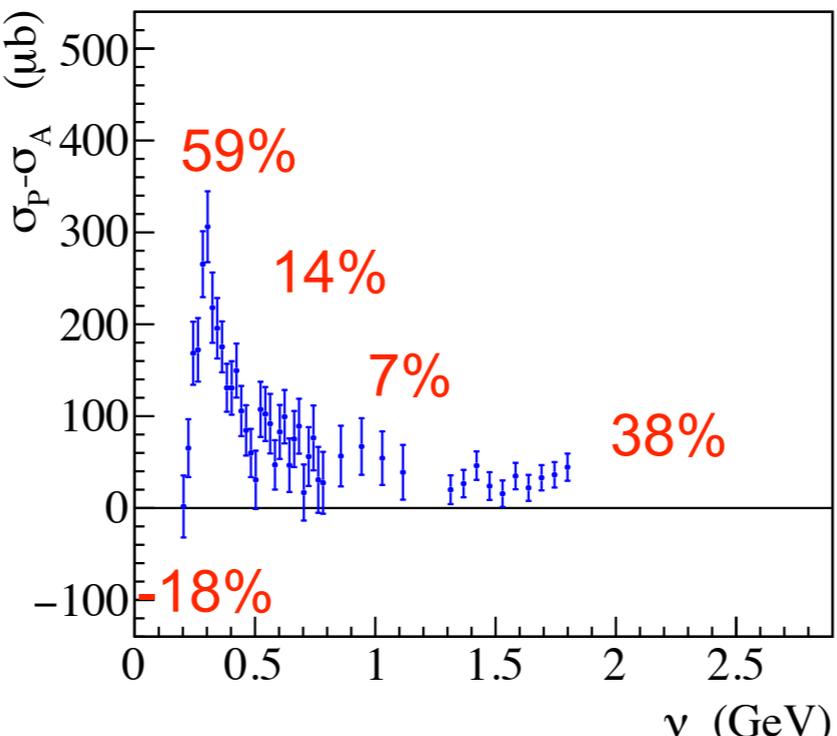
$D_{13}(1520)$ ,  $S_{11}(1535)$   
expected to be small

3rd resonance and Regge modification

93% proton



neutron



# Candidate Nuclei

Choice will depend on target feasibility and FOM

The strongest candidate is  ${}^7\text{Li}$ :

- Also the subject of unpolarized (E12–10–008) and polarized (E12–14–001:  $Q^2 > 1 \text{ GeV}^2$ ) EMC experiments at JLab
- A GDH measurement will provide the  $Q^2 \rightarrow 0$  limit

	$J^\pi$	$\mu$	$\kappa$	$M$	$I_{\text{GDH}}$
${}^1\text{H}$	$1/2^+$	2.793	1.793	0.9383	204.8
${}^2\text{H}$	$1^+$	0.857	-0.1426	1.875	0.6484
${}^3\text{He}$	$1/2^+$	-2.128	-8.383	2.808	499.9
${}^7\text{Li}$	$3/2^-$	3.256	4.598	6.532	83.39
${}^{13}\text{C}$	$1/2^-$	0.702	3.131	12.11	3.753
${}^{17}\text{O}$	$5/2^+$	-1.894	-14.44	15.83	233.4
${}^{19}\text{F}$	$1/2^+$	2.628	40.94	17.69	300.5

# Target FOM

	$J^\pi$	$P$	species	molecule	dilution $F$	FOM $P^2F$ ( $\times 10^{-3}$ )	days	
							12 GeV	4 GeV
$^1\text{H}$	$1/2^+$	90%	$\vec{p}$	$\text{C}_4\text{H}_9\text{OH}$	$10/74 = 0.135$	110	7	4
$^2\text{H}$	$1^+$	80%	$\vec{n}, \vec{p}$	$\text{C}_4\text{D}_9\text{OD}$	$10/84 = 0.119$	76	10	6
$^7\text{Li}$	$3/2^-$	80%	$\vec{p}$	$^7\text{Li}^2\text{H}$	$1/9 = 0.111$	71	11	6
$^{13}\text{C}$	$1/2^-$	60%	$\vec{n}$	$\text{C}_4\text{D}_9\text{OD}$	$4/78 = 0.051$	4.6	42	24
$^{17}\text{O}$	$5/2^+$	80%	$\vec{n}$	$\text{C}_4\text{D}_9^{17}\text{OD}$	$1/75 = 0.013$	8.5	90	51
		80%	$\vec{n}$	$\text{H}_2^{17}\text{O}$	$1/19 = 0.053$	34	23	13
$^{19}\text{F}$	$1/2^+$	90%	$\vec{p}$	$^6\text{Li}^{19}\text{F}$	$1/25 = 0.040$	32	24	14
		80%	$\vec{p}$	$\text{C}_3\text{H}_2^{19}\text{F}_6\text{O}$	$6/168 = 0.036$	23	34	19

Continuous polarization using dynamic nuclear polarization (DNP)

Temperature 200-300 mK.

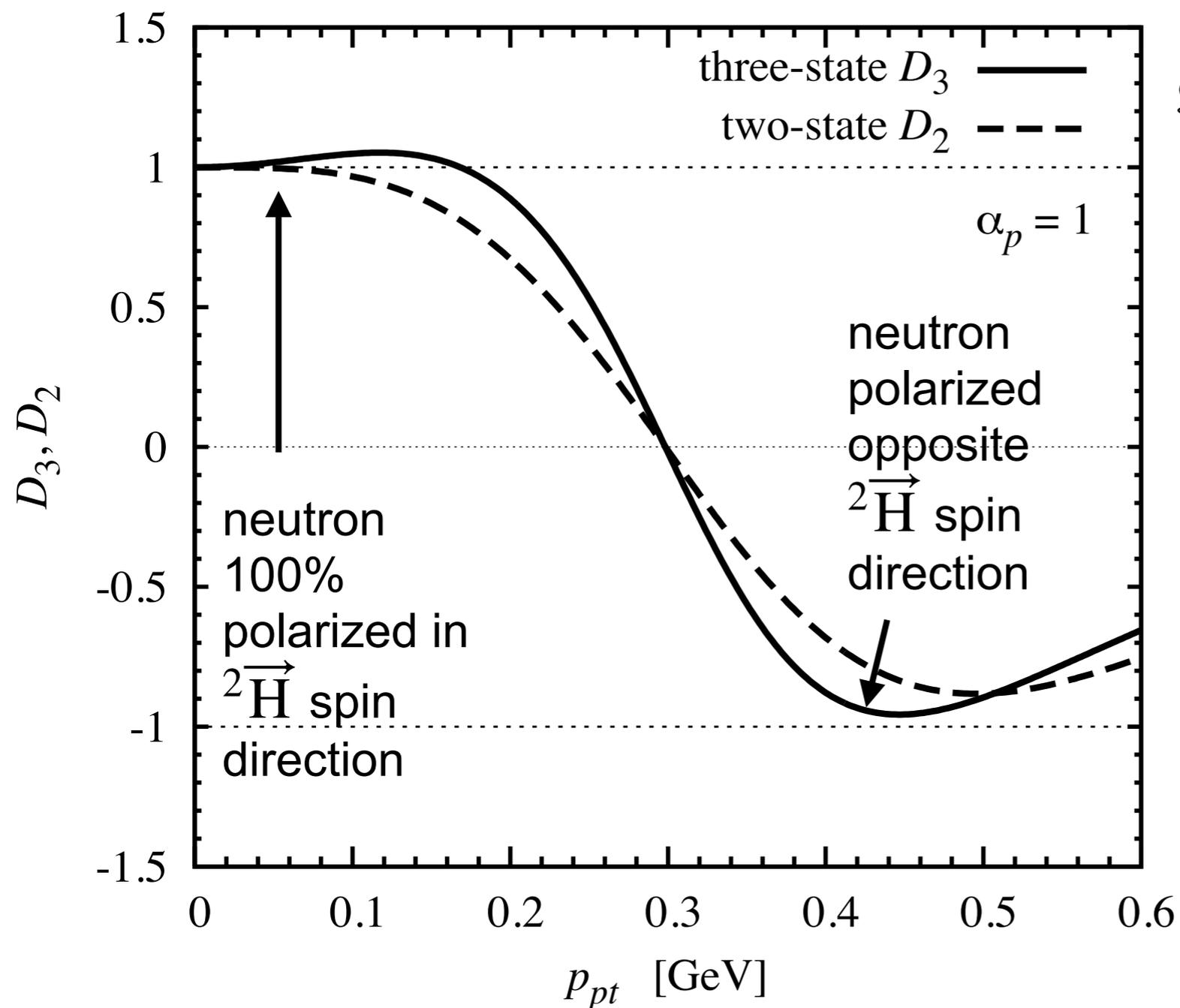
Internal superconducting coils, increase field to 2.5 T, improve homogeneity.

# SRC Measurements with Photon Probe

## Exclusive Measurements

# Deuteron Spin Structure

Required for using the deuteron as a polarized neutron target.



$$\mathcal{D}_2(\alpha_P, |p_{pT}|) \equiv \frac{\Delta\mathcal{S}_S(\alpha_P, |p_{pT}|)}{[\mathcal{S}_U + \mathcal{S}_T](\alpha_P, |p_{pT}|)}$$

$$\mathcal{D}_3(\alpha_P, |p_{pT}|) \equiv \frac{\Delta\mathcal{S}_S(\alpha_P, |p_{pT}|)}{\mathcal{S}_U(\alpha_P, |p_{pT}|)}$$

$\mathcal{S}_U$ ,  $\Delta\mathcal{S}_S$ ,  $\mathcal{S}_T$  are three distinct LF helicity projections of the spectral function

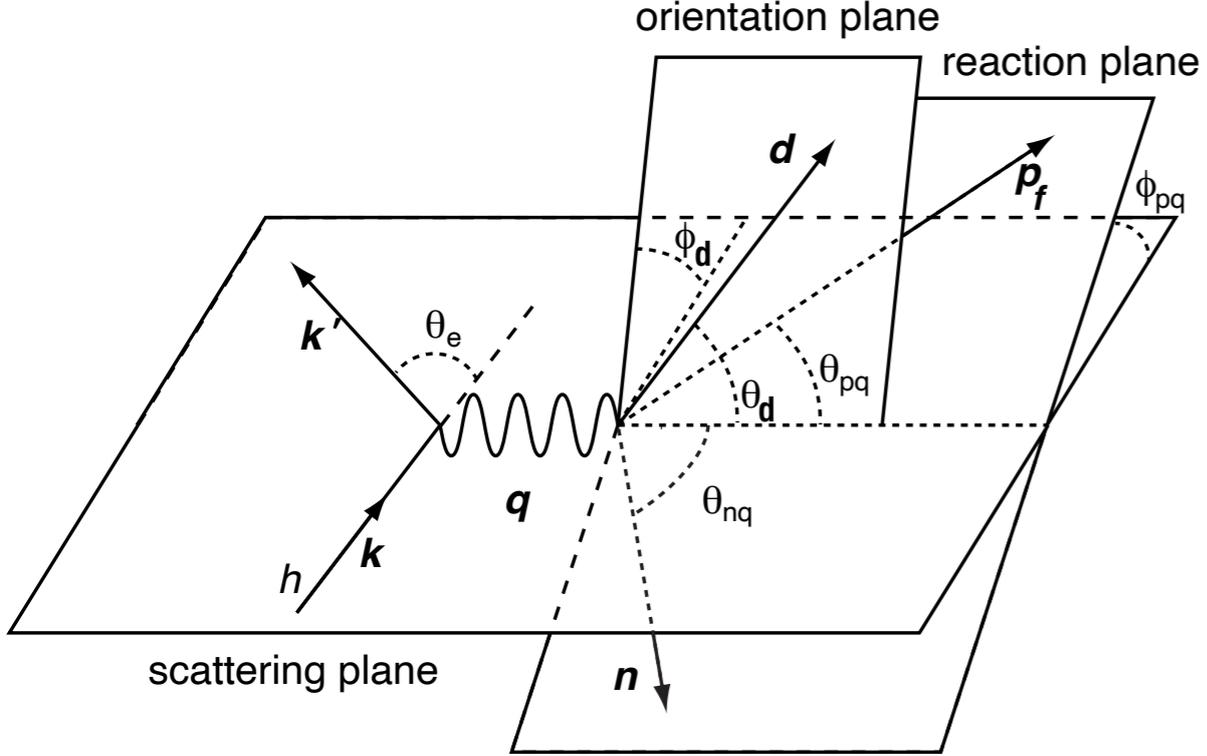
describing an unpolarized, vector-polarized, and tensor-polarized ensemble quantized along the z-axis,

W. Cosyn, C. Weiss / PLB 799 (2019) 135035

# Deuteron Spin Structure

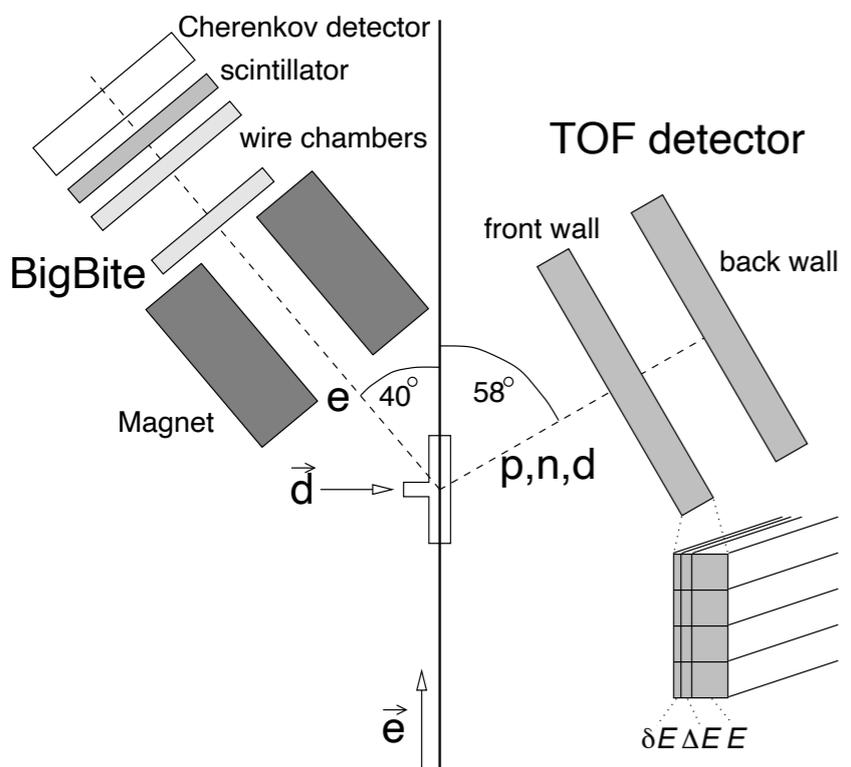
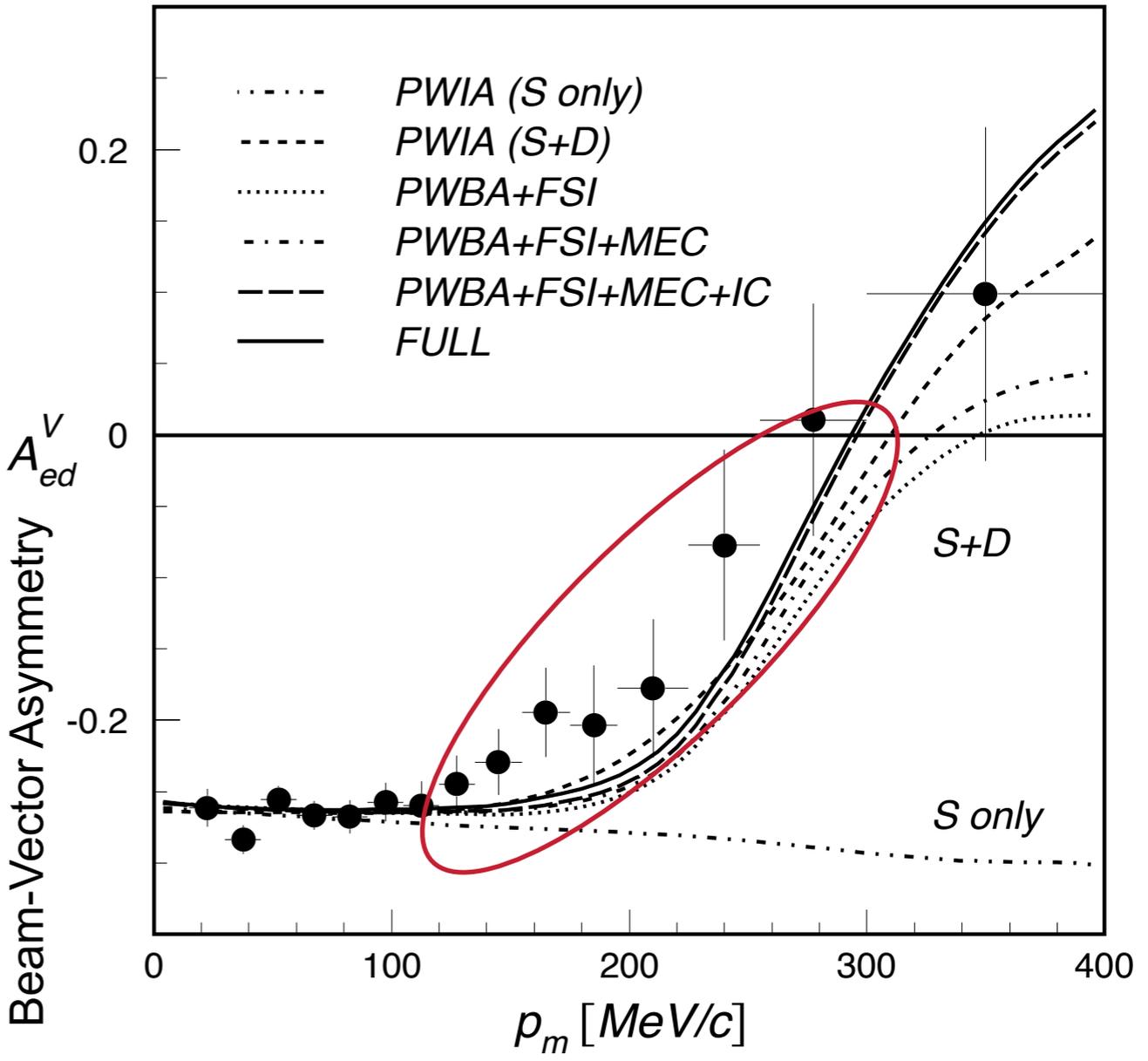
$$\sigma = \sigma_0(1 + P_1^d A_d^V + P_2^d A_d^T + h(A_e + P_1^d A_{ed}^V + P_2^d A_{ed}^T))$$

Arenhövel PhysRevC.46.455



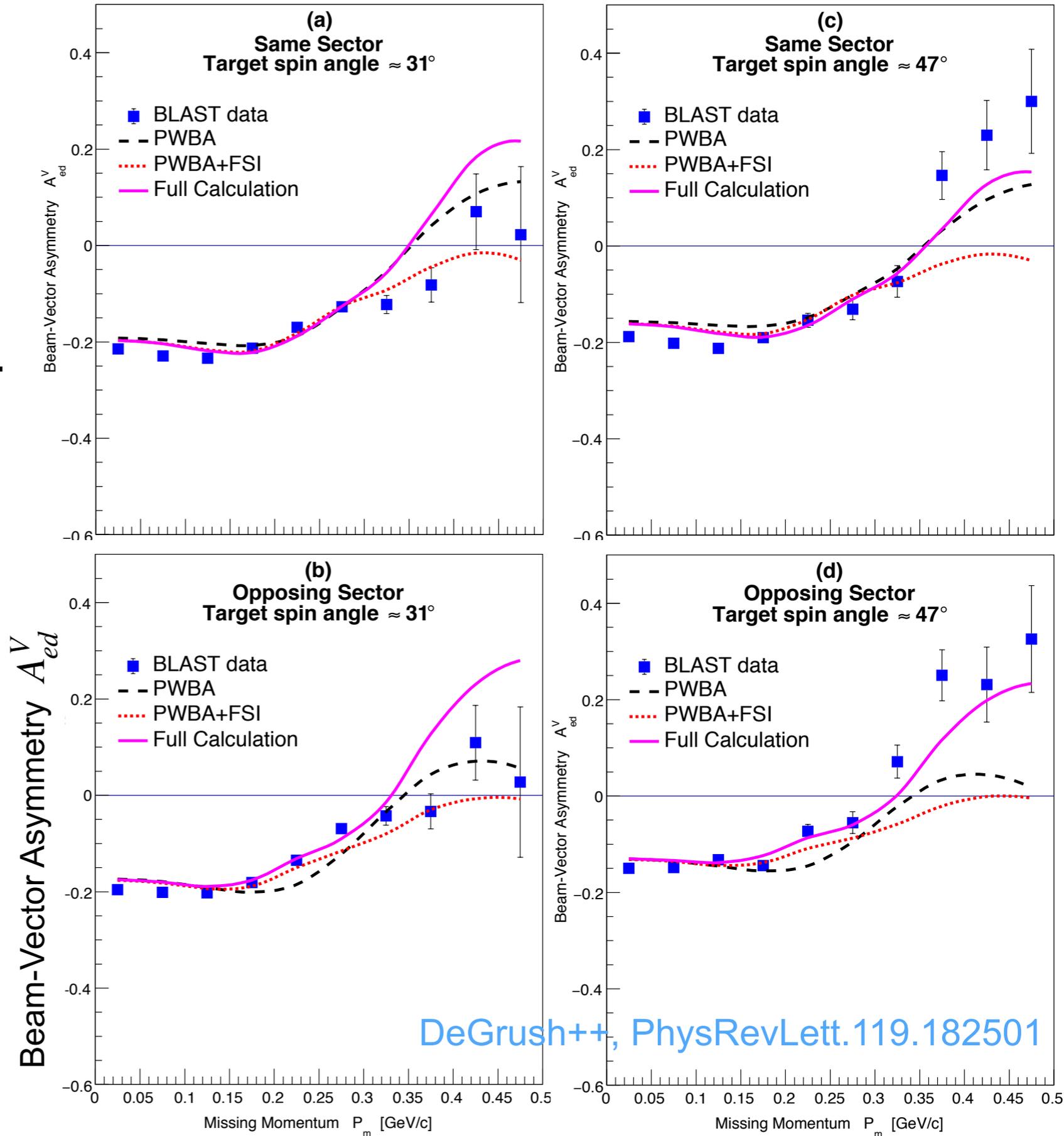
$^2\vec{H}(\vec{e}, e'p)n$  at Nikhef

Paschier++ PhysRevLett.88.102302



# $^2\vec{H}(\vec{e}, e'p)n$ at Bates

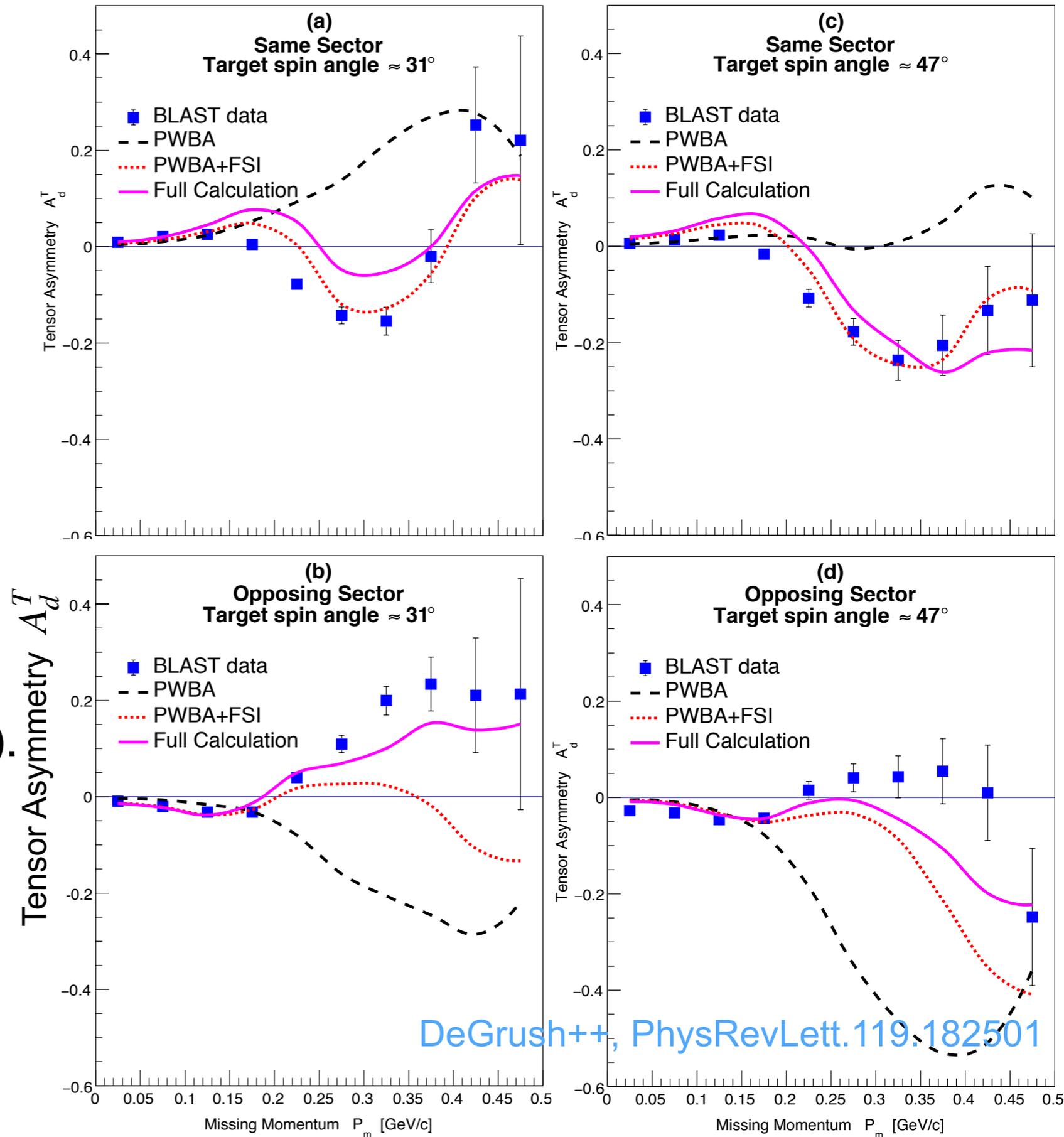
Blast measurements reached to higher  $P_m$  and tended to agree with calculations better.



# $^2\overline{H}(\vec{e}, e'p)n$ at Bates

Tensor asymmetries significantly affected by FSI  
Full calculations disagree with data

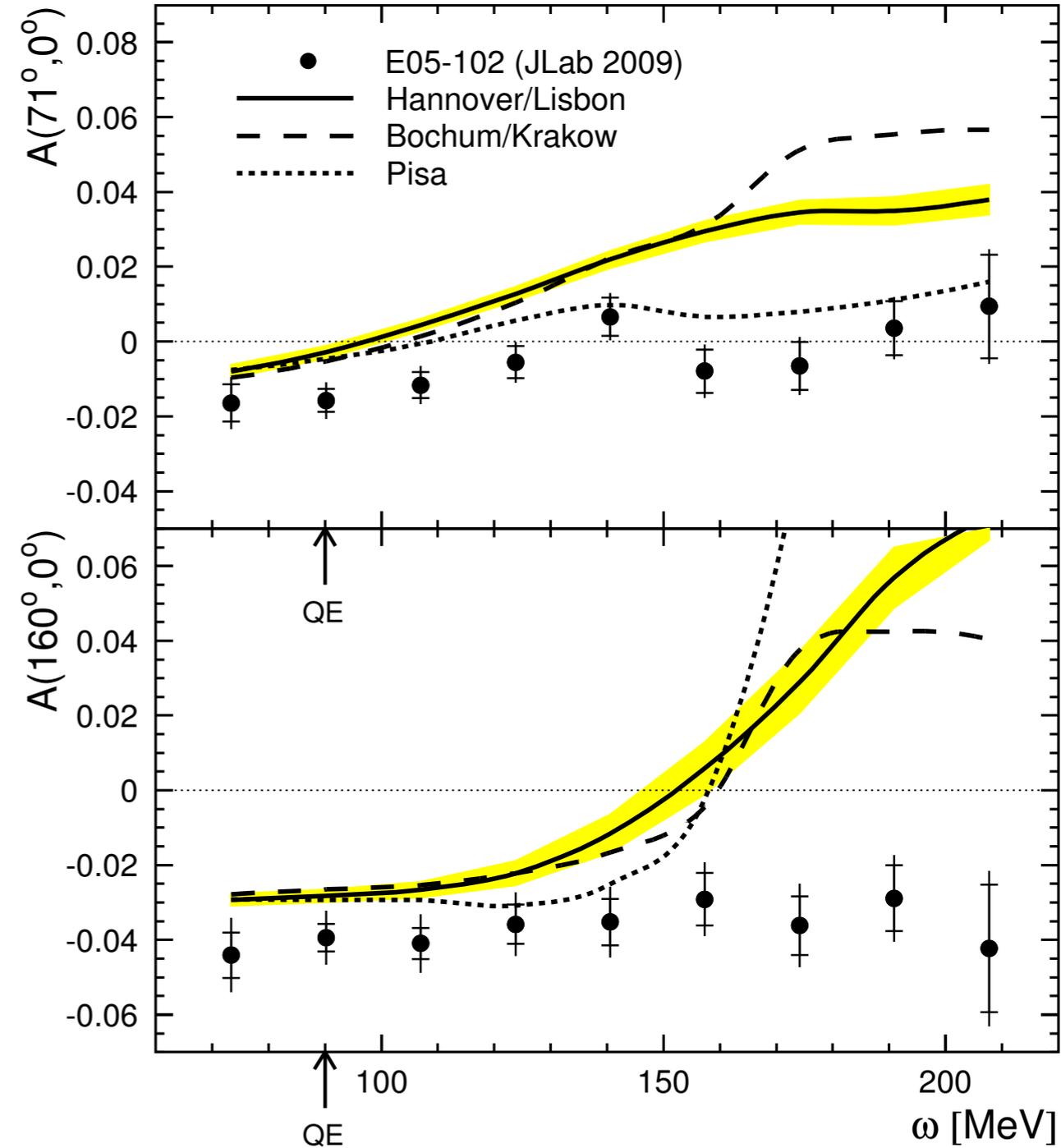
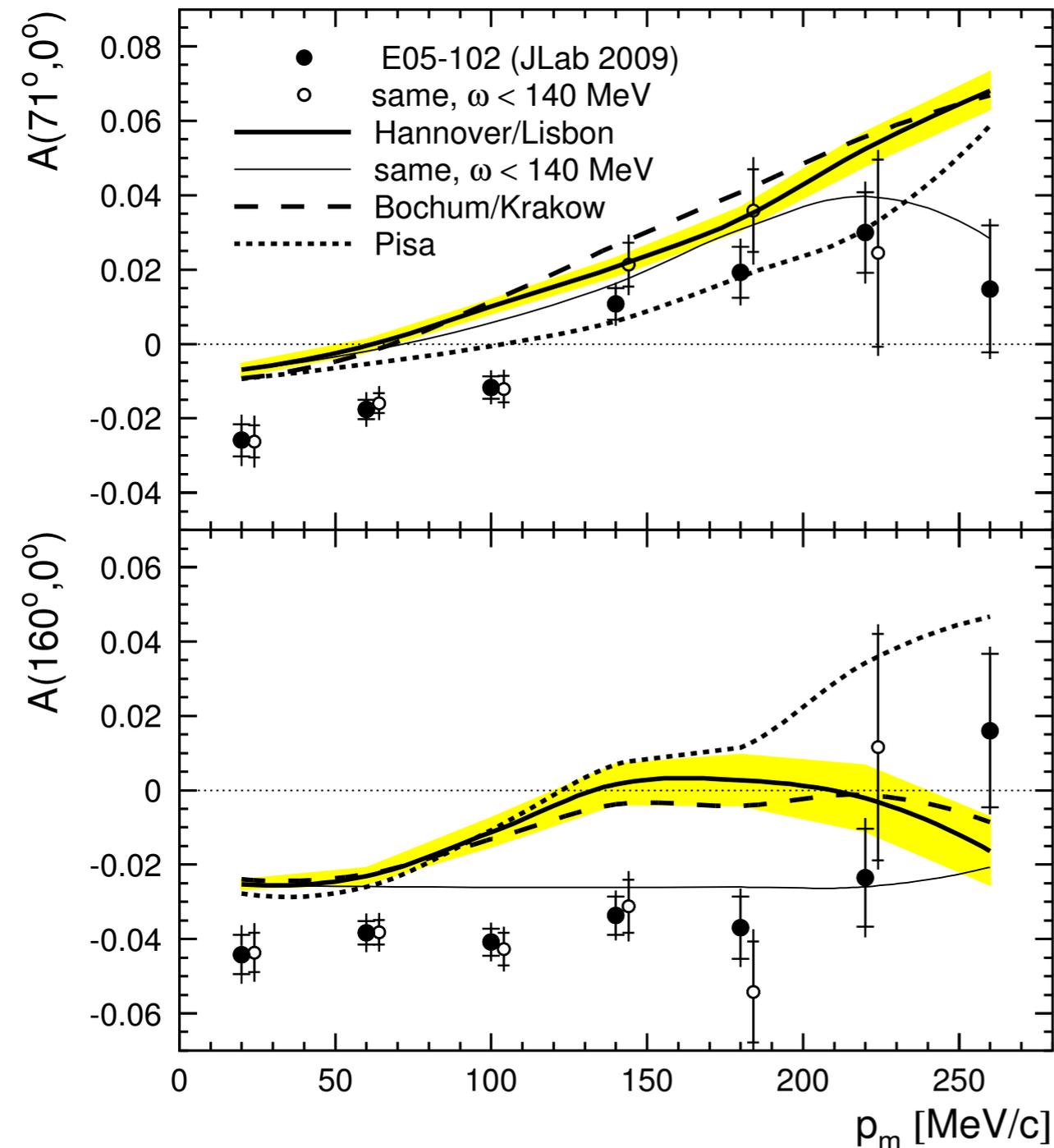
meson-exchange currents (MECs),  
isobar configurations (ICs),  
relativistic corrections (RCs).  
insensitive to the choice of different realistic potentials



# Helium-3 Spin Structure

${}^3\text{He}(\vec{e}, e'd)$  study a polarized deuteron in the nucleus

Mihovilovic++ PhysRevLett.113.232505



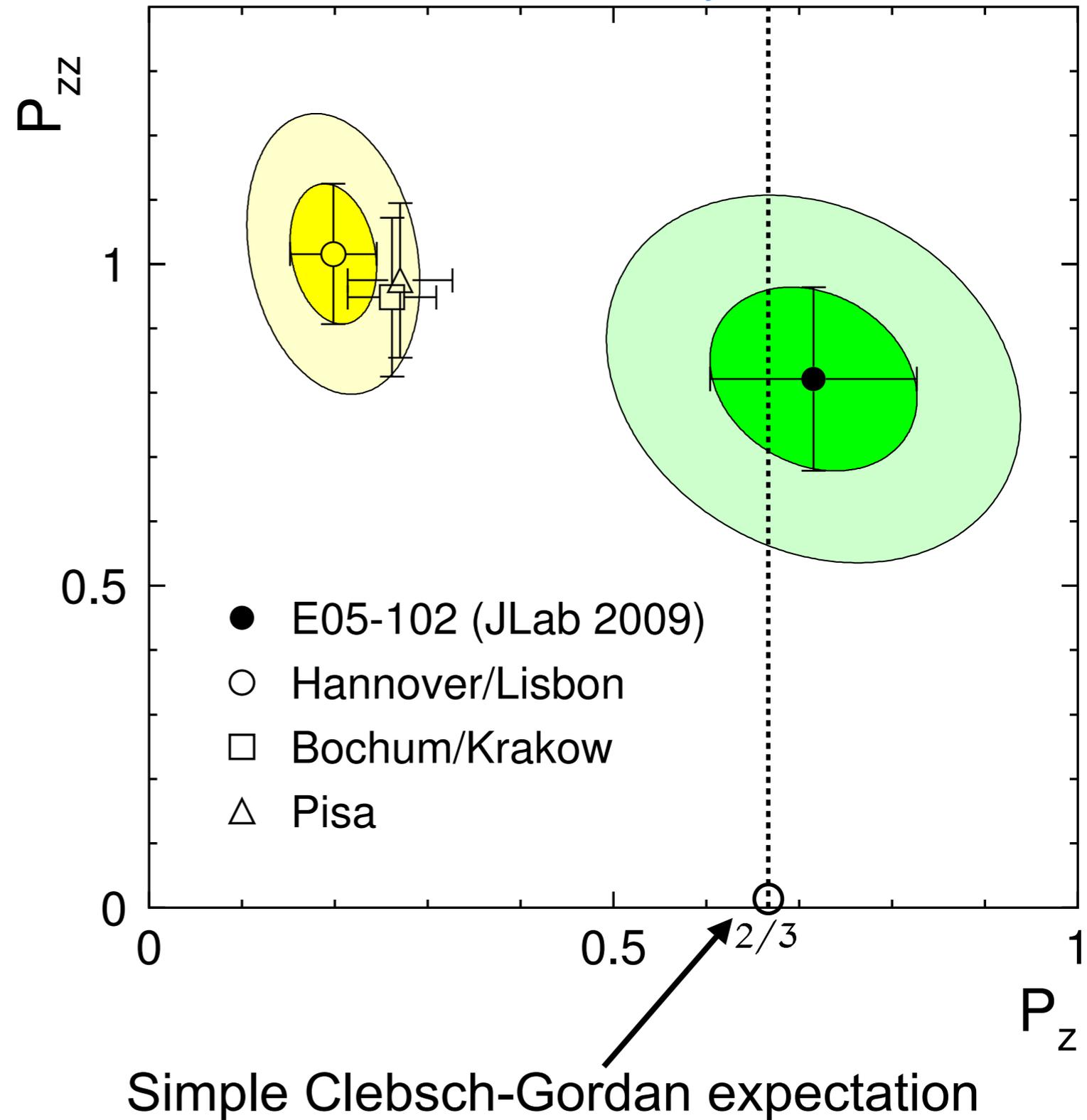
$p_m = |\mathbf{q} - \mathbf{p}_d|$  is momentum of recoil proton

# Helium-3 Spin Structure

Mihovilovic++ PhysRevLett.113.232505

Effective polarizations from asymmetries as  $p_m \rightarrow 0$

Theoretical calculations of the vector polarization of the deuteron in  $^3\text{He}$  appear underestimated.



# Short Range Correlated np pairs

Experiment E12-14-001 approved to study polarized EMC effect using DIS on  ${}^7\text{Li}$  in Hall B.

mean field model predict a significant polarized EMC effect  
SRC pairs might produce no effect if they are depolarized

Assume 100% polarized valence nucleon in S-wave with another nucleon

pair in nucleus are not required to be spin oriented same direction  
could be a  $J_z = 0$  or  $J_z = 1$  combination

SRC interacts through tensor interaction which preserves  $J_z$   
Clebsch-Gordan coefficients for orbital angular momentum  $L = 2$

Valence nucleon polarization changes sign but is only about -10 to -15%.

Thomas IJMP E27 (2018)

# Expansion to Heavier Nuclei

SRC/CT Experiment in Hall D

$^2\text{H}$  4 days 350 per day

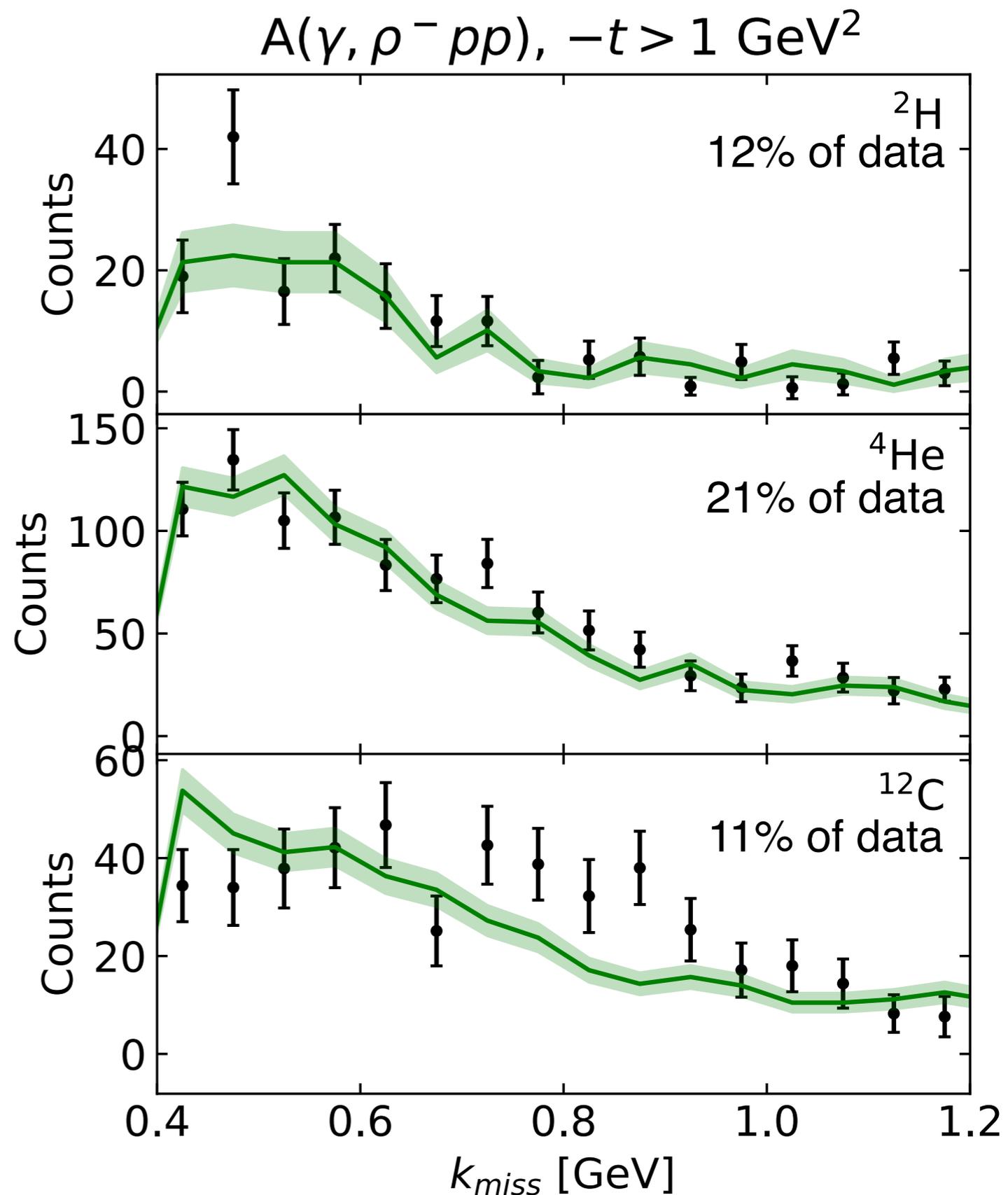
$^4\text{He}$  10 days 520 per day

$^{12}\text{C}$  14 days 340 per day

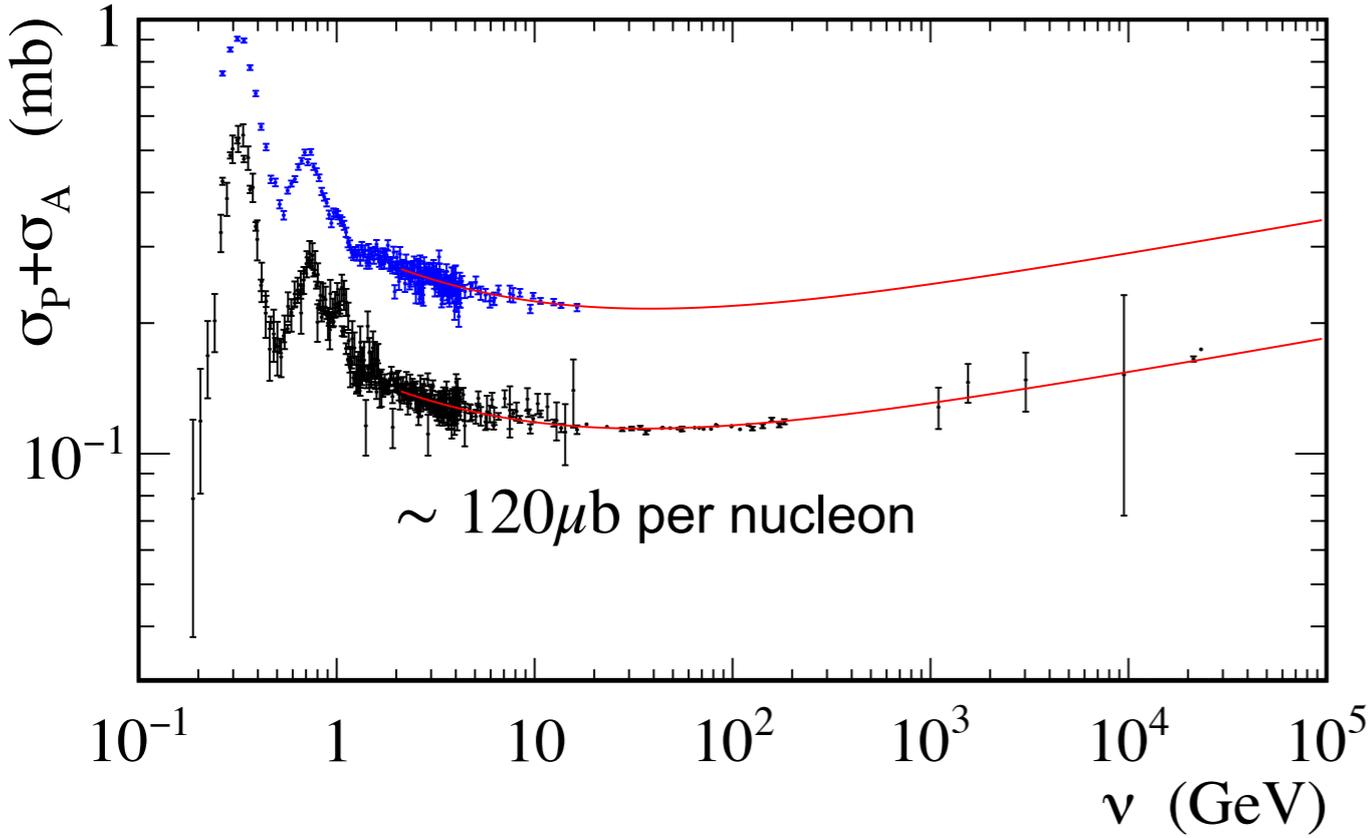
events above  $k_{\text{miss}} > 0.4 \text{ GeV}$

$-t > 1 \text{ GeV}^2, -u > 1 \text{ GeV}^2,$

$E_\gamma > 7 \text{ GeV}$

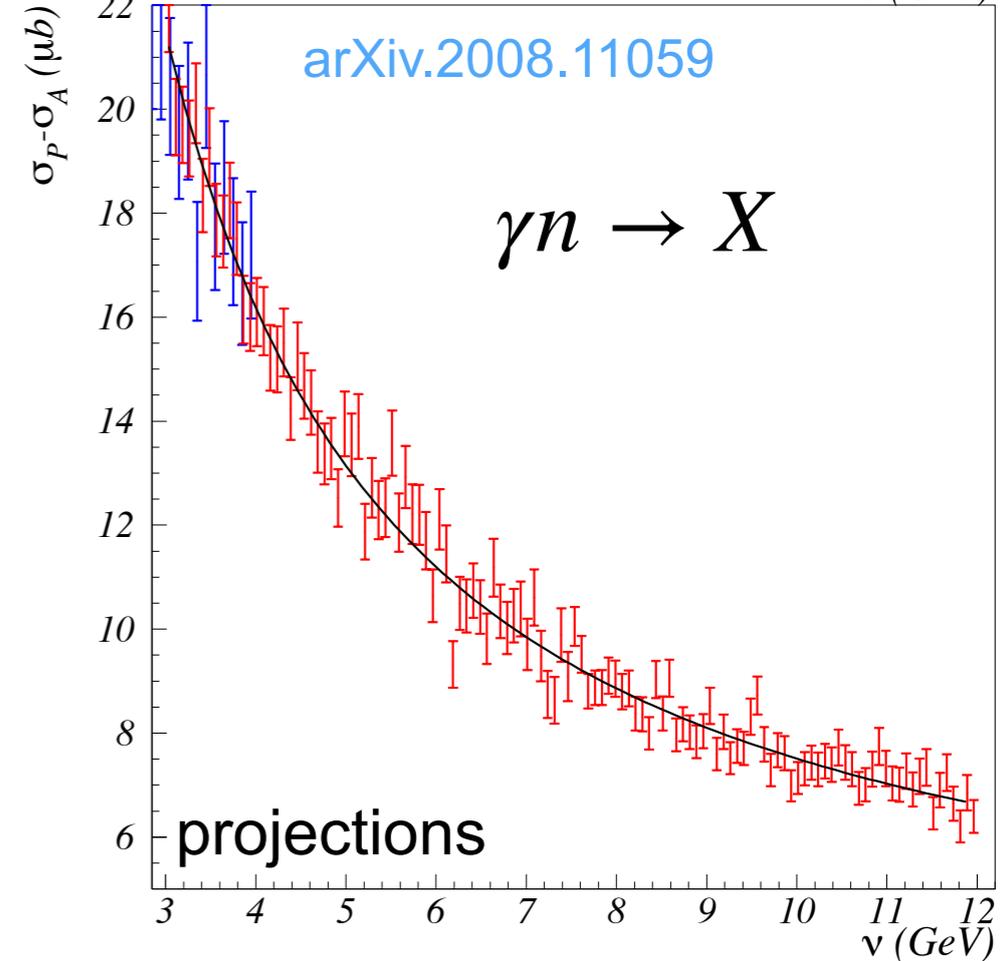
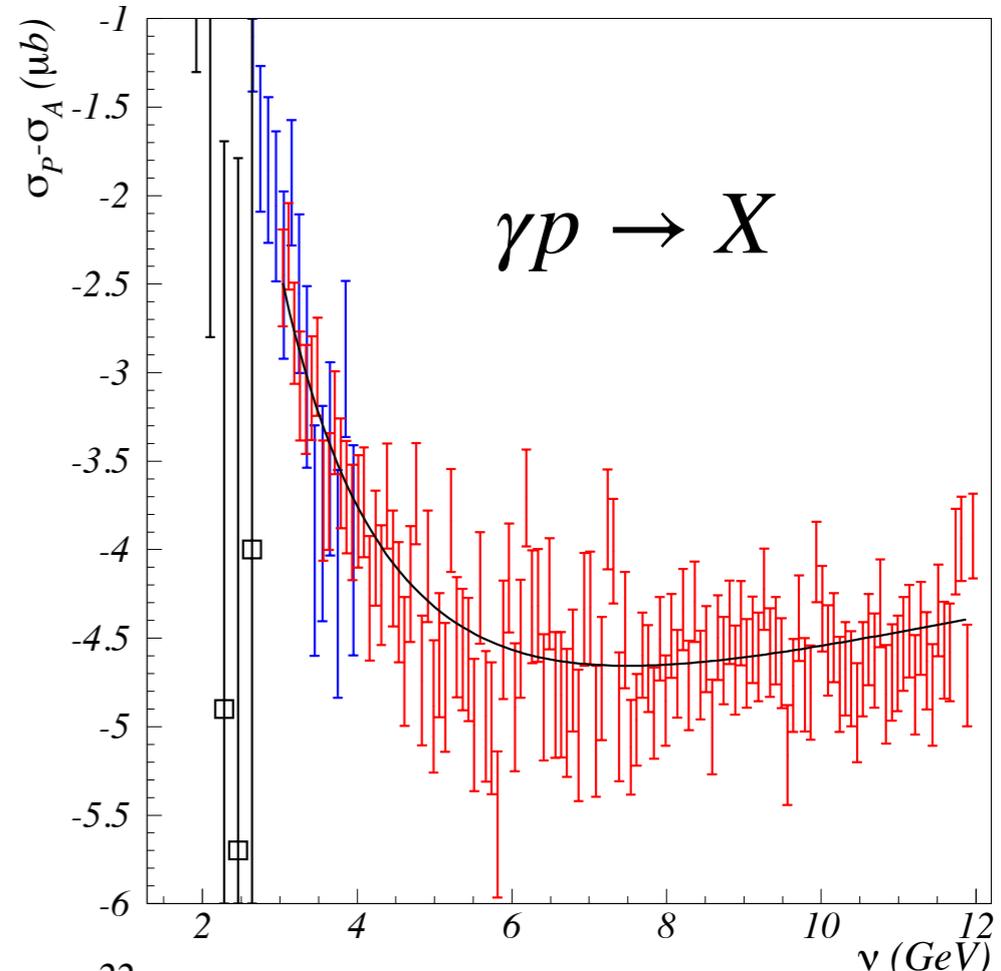


# Inclusive Asymmetries



Regge phenomenology predicts inclusive asymmetries:  
 proton  $-4\%$   
 neutron  $5\%$  to  $10\%$

Will be measured by REGGE

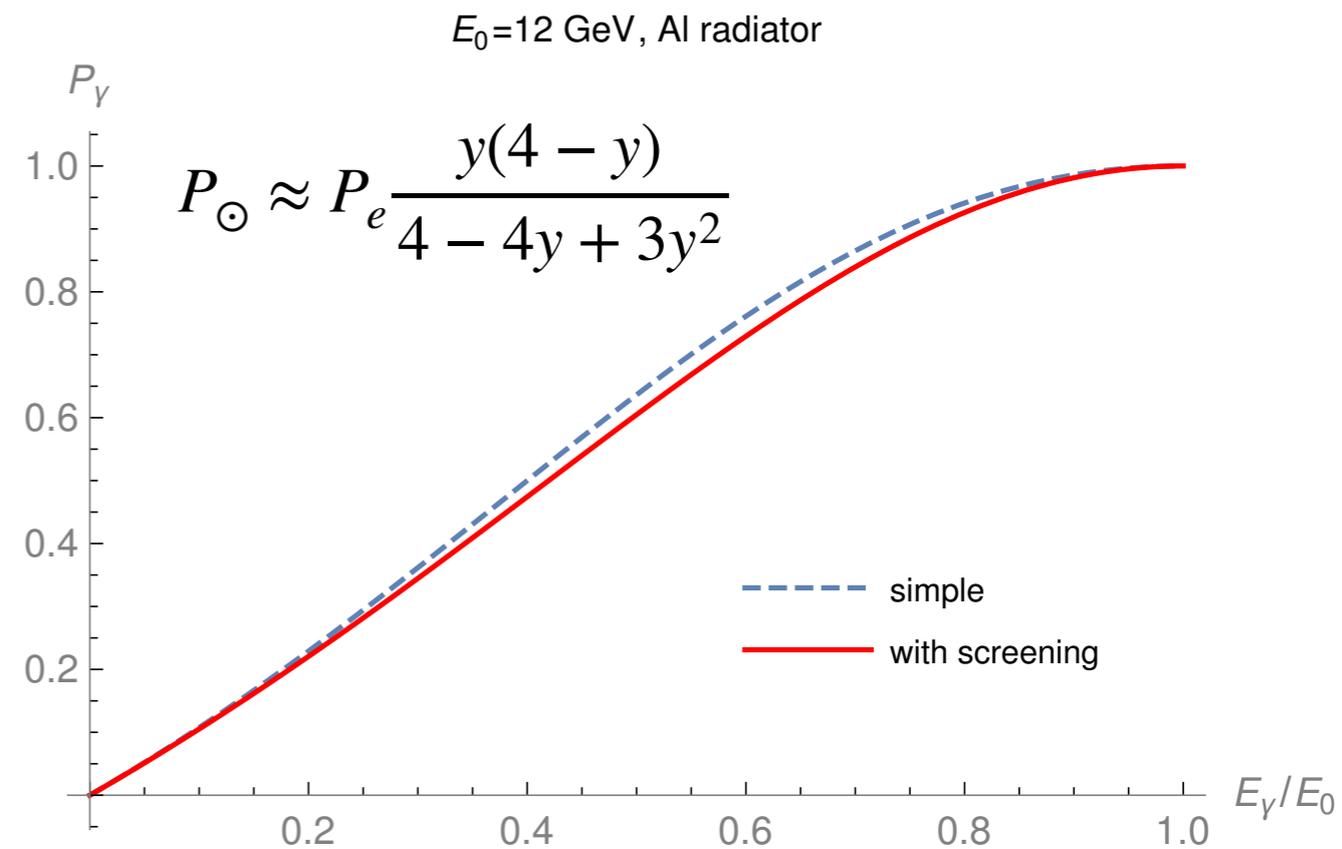
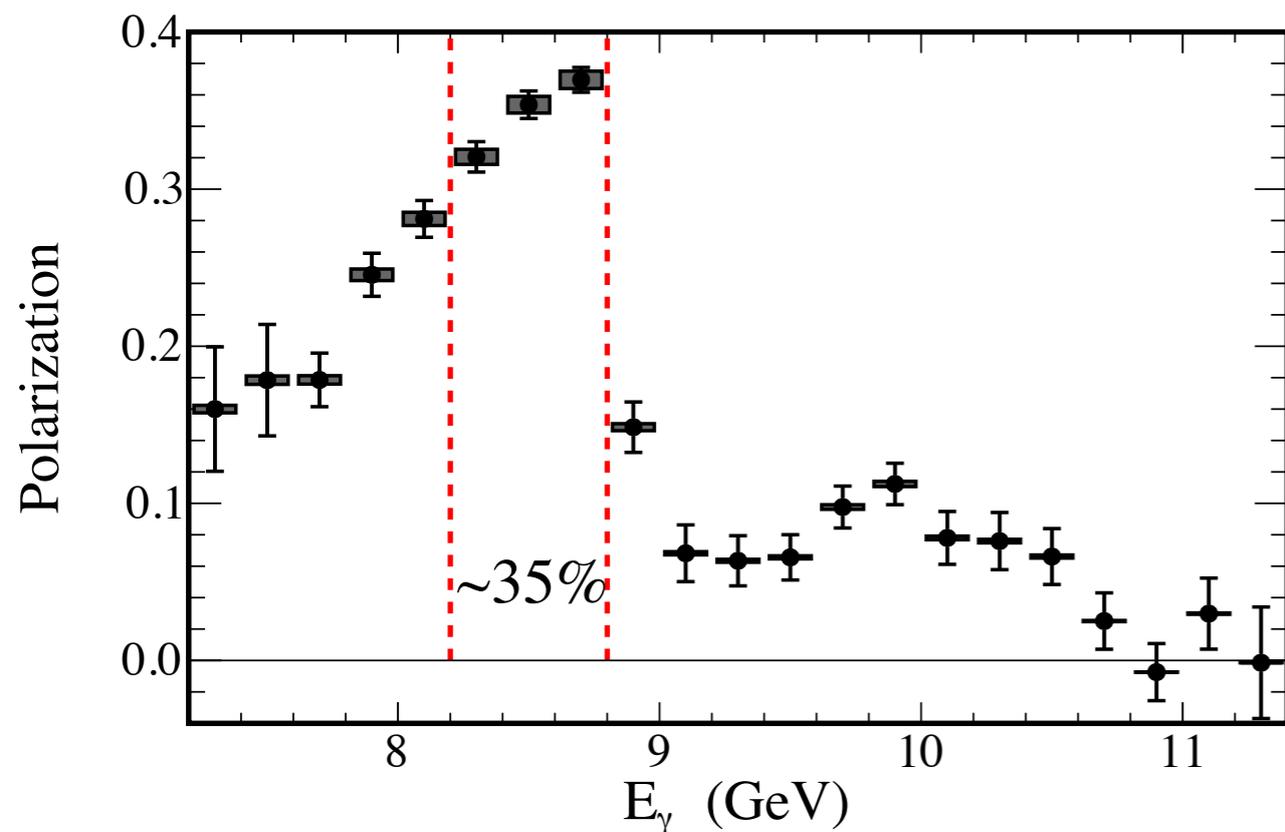


# Exclusive Asymmetries

$$\vec{P}_\gamma = (-P_T \cos 2\Phi, -P_T \sin 2\Phi, P_\odot)$$

$$\vec{P} = (0, 0, P_z)$$

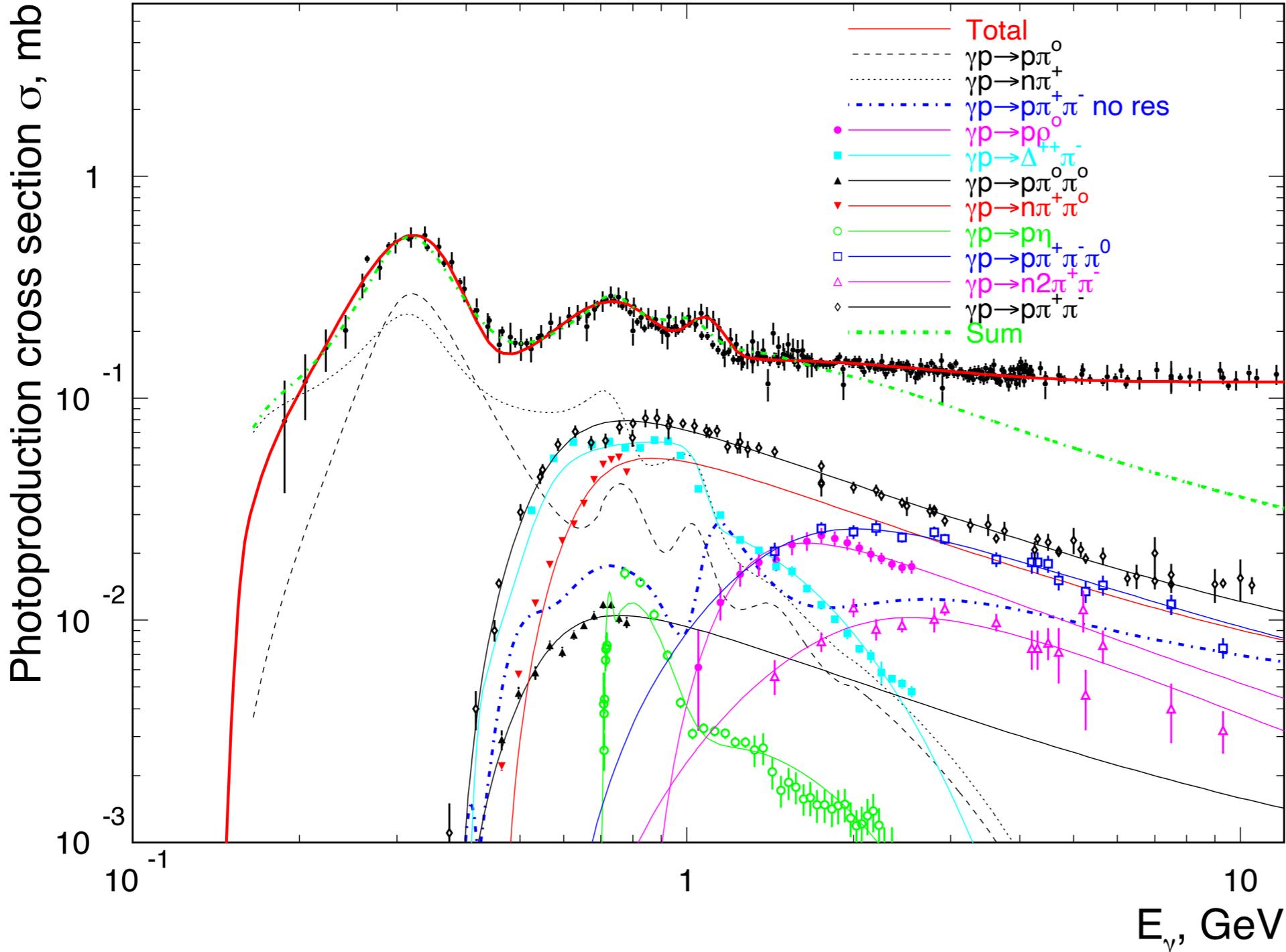
$$I(\Phi) = \frac{d\sigma}{dt} \left[ 1 + P_T \Sigma \cos 2\Phi + P_T P_z G \sin 2\Phi - P_\odot P_z E \right]$$



Working with Vincent Matthieu from JPAC to predict asymmetries for vector and pseudo-scalar meson production.

# Final States

Vector meson production has highest cross section.



initial	final
$np$	$pp \rho^-$
$np$	$np \omega$
$np$	$pp \pi^-$
$pp$	$pp \rho^0$
$pp$	$pp \omega$
$pp$	$pp \pi^0$

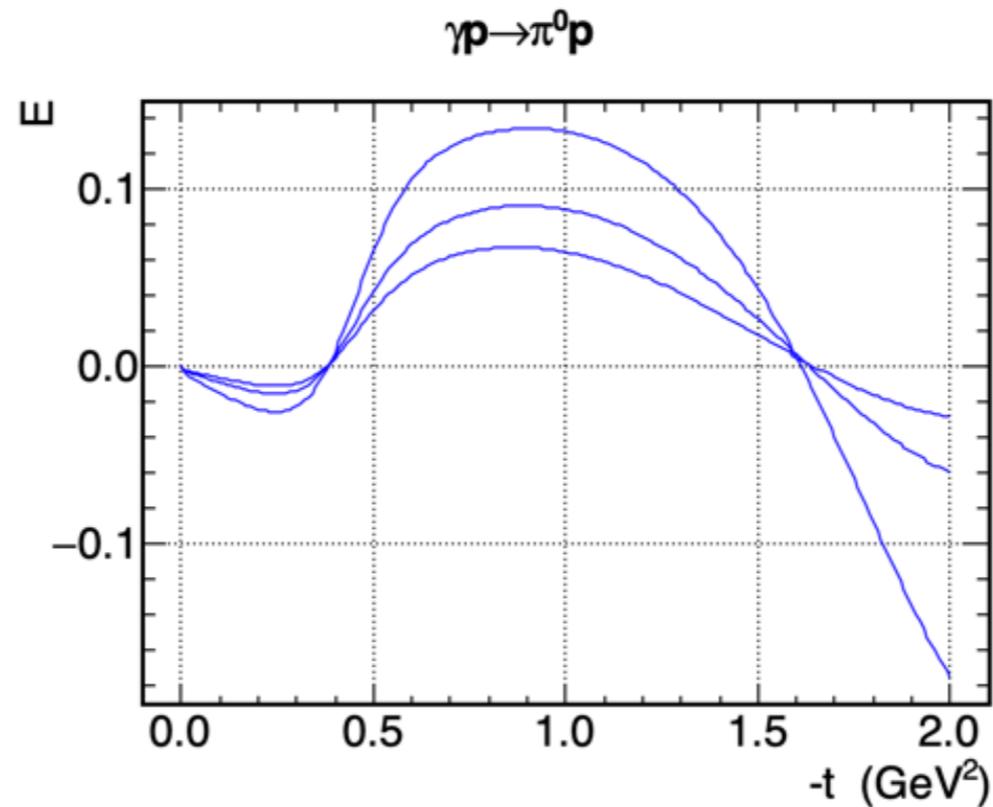
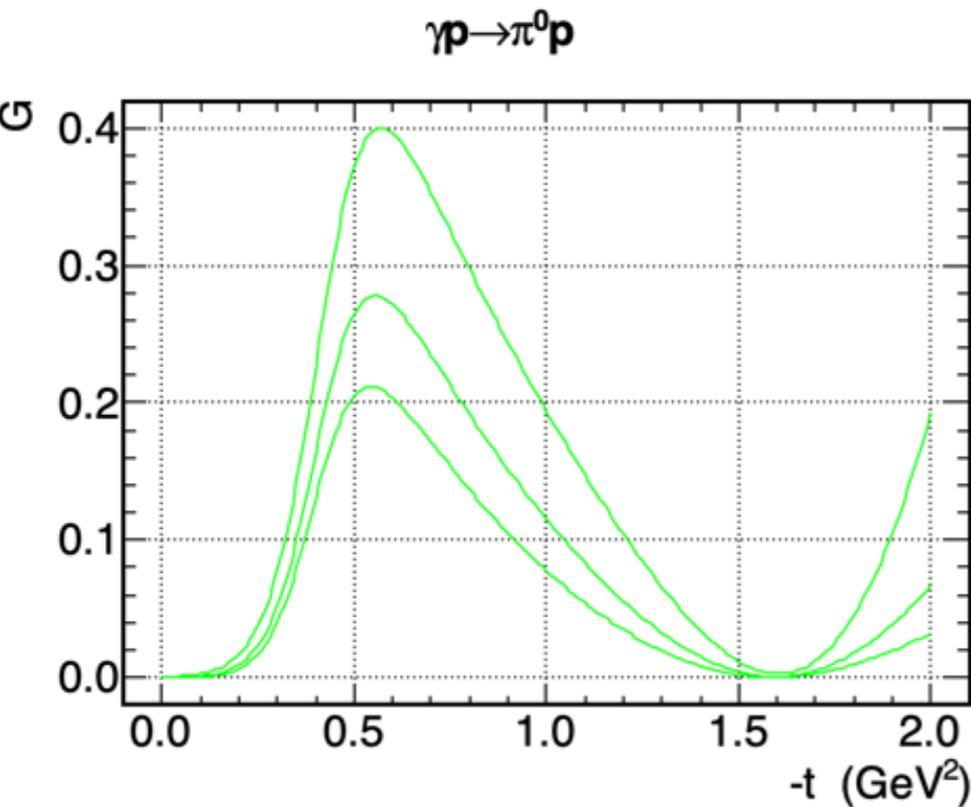
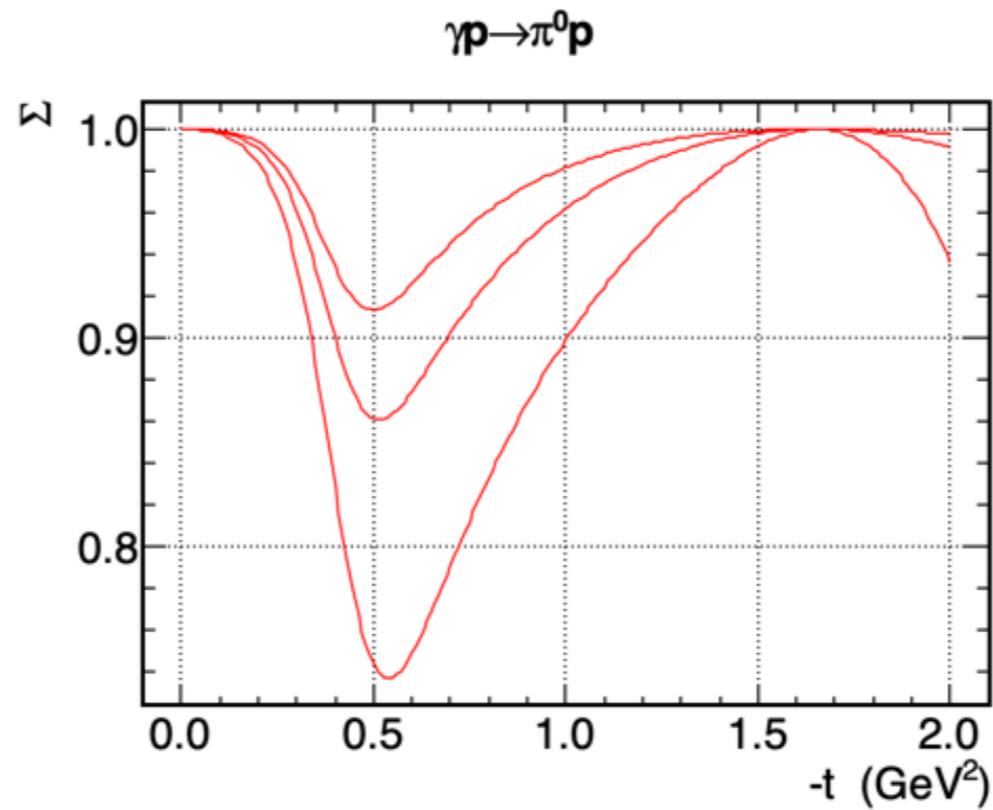
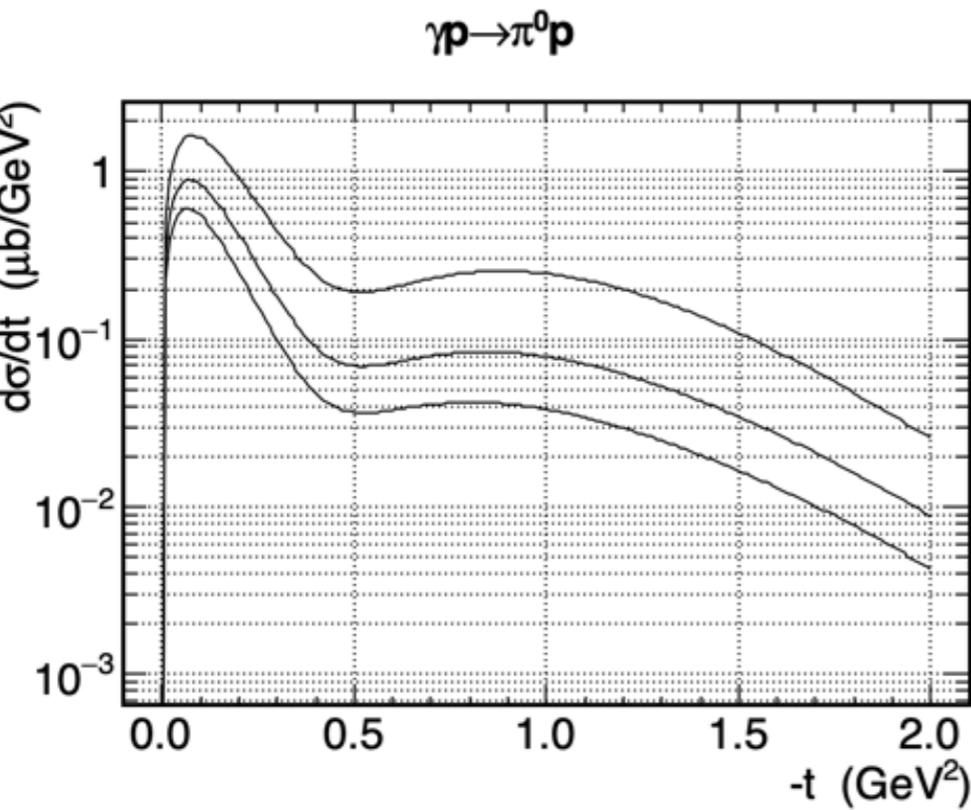
# Example: $\gamma p \rightarrow p\pi^0$

Regge calculation

Curves at  
4.5, 7.5, 10.5 GeV

$\Sigma$  asymmetry  
matches data well

G and E  
asymmetries  
completely  
untested



Mathieu++, PHYSICAL REVIEW D 92, 074013 (2015)

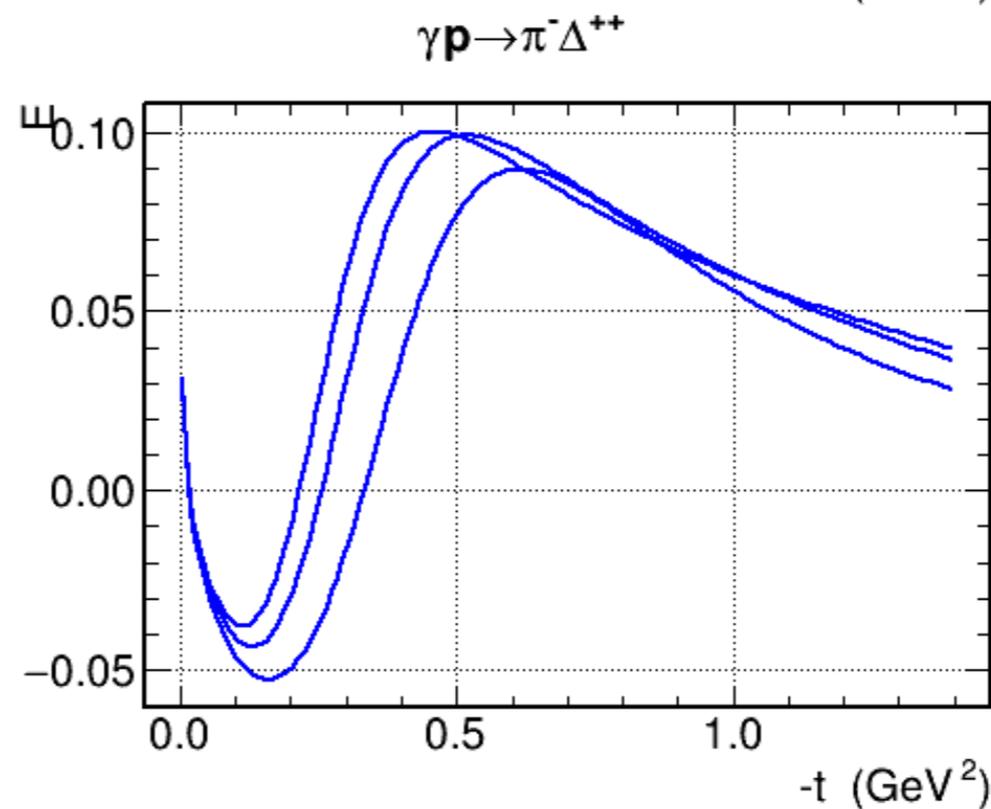
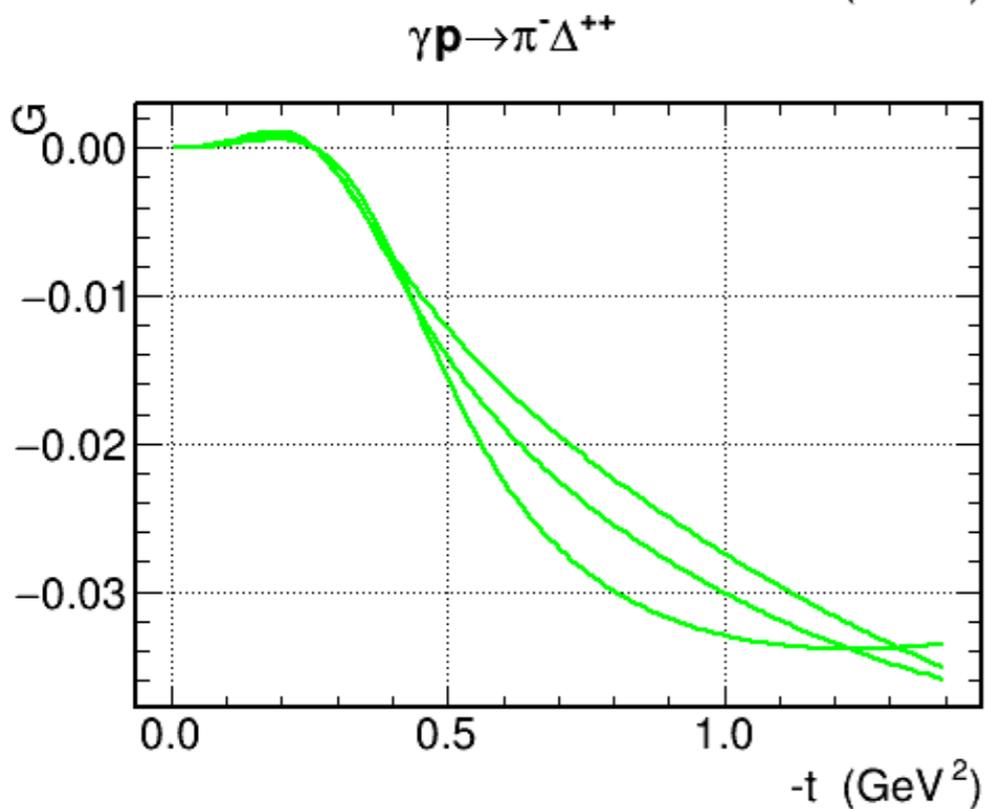
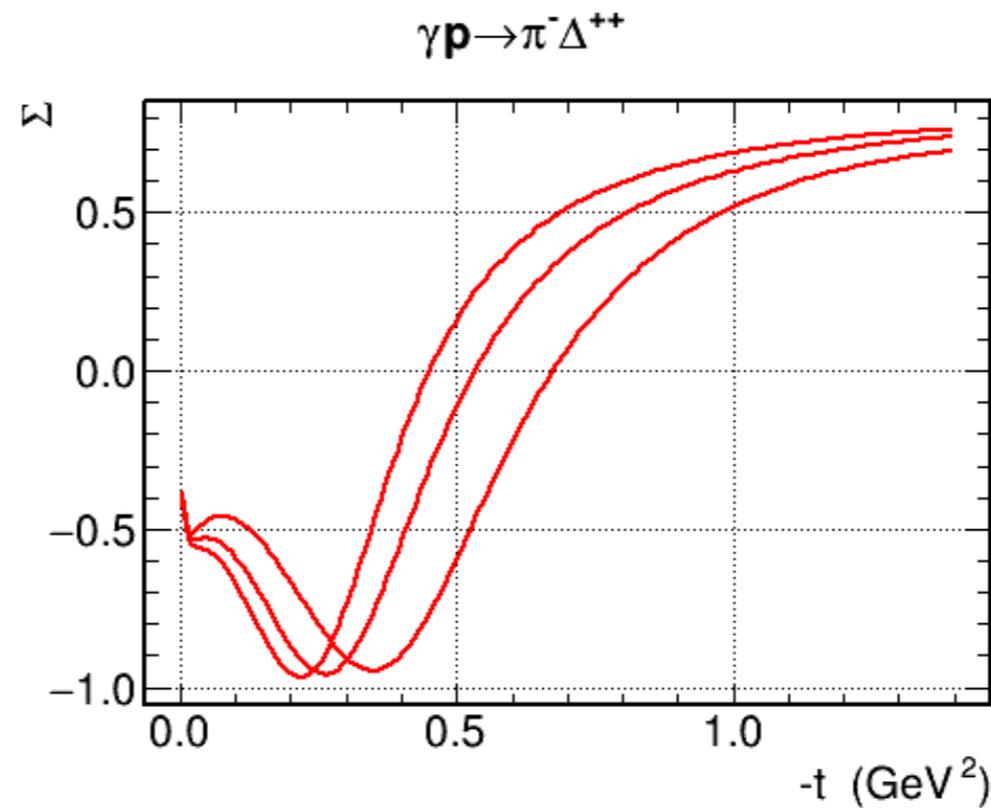
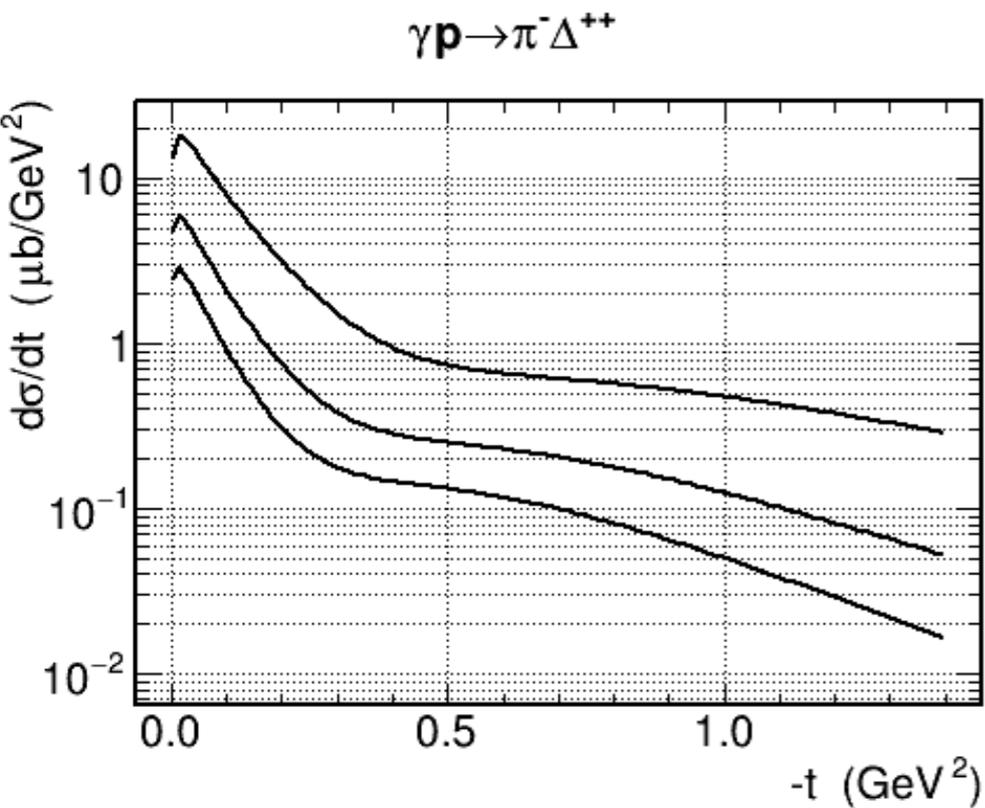
# Example: $\gamma p \rightarrow \pi^- \Delta^{++}$

Regge calculation

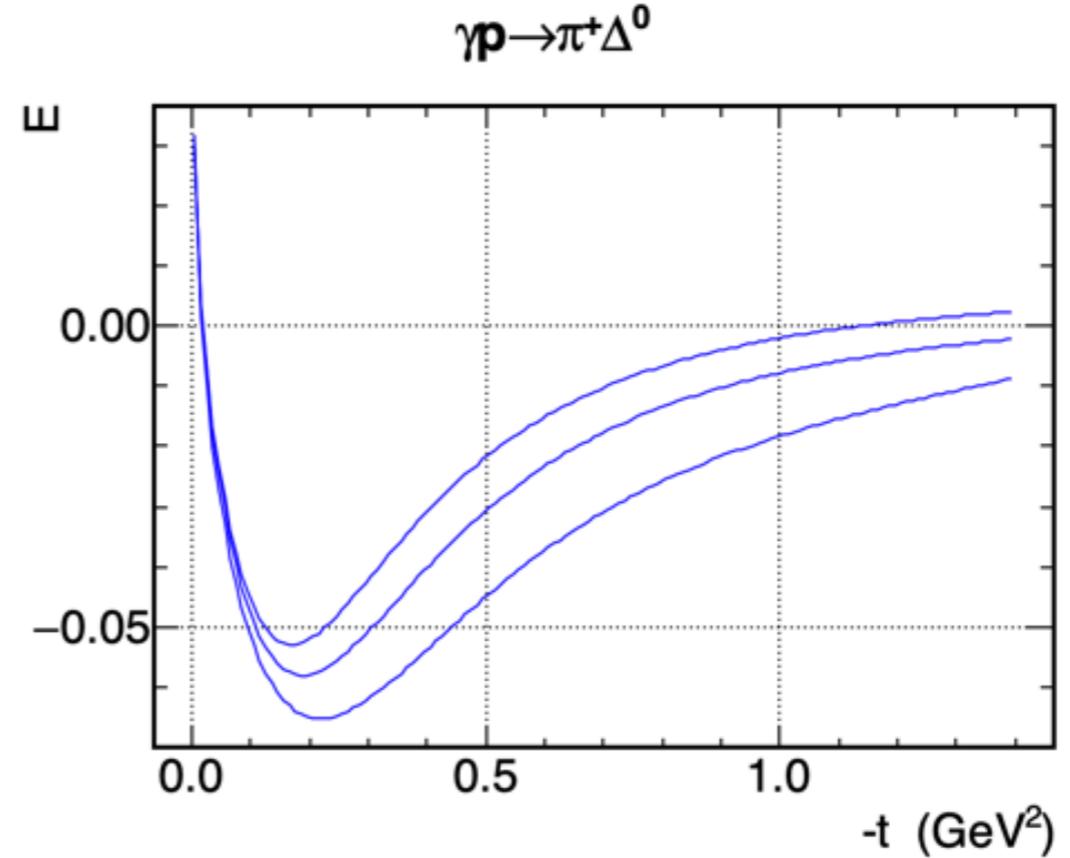
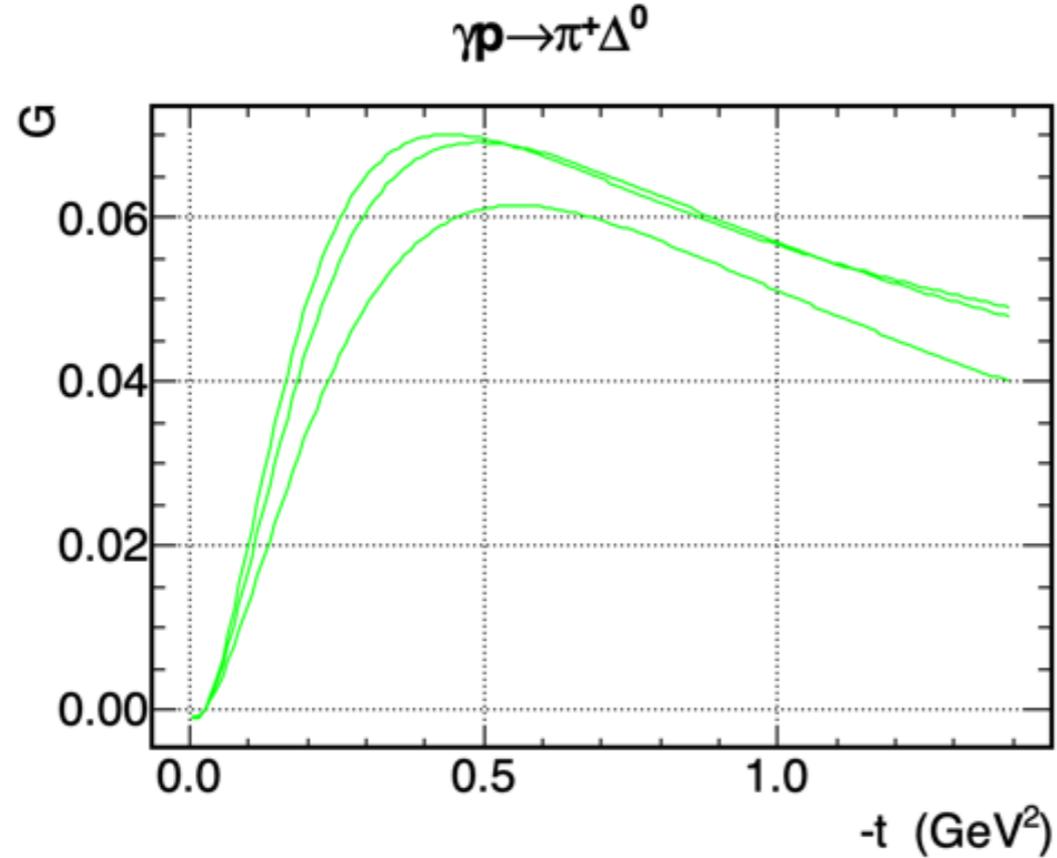
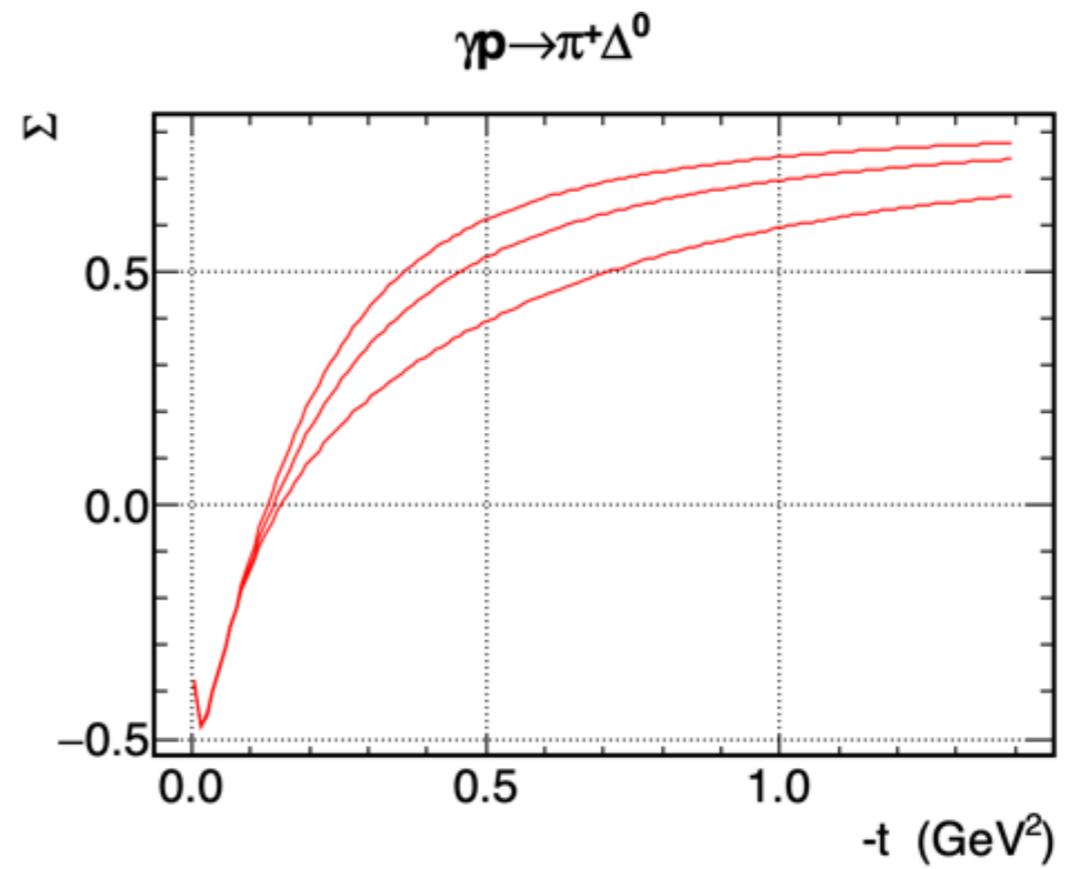
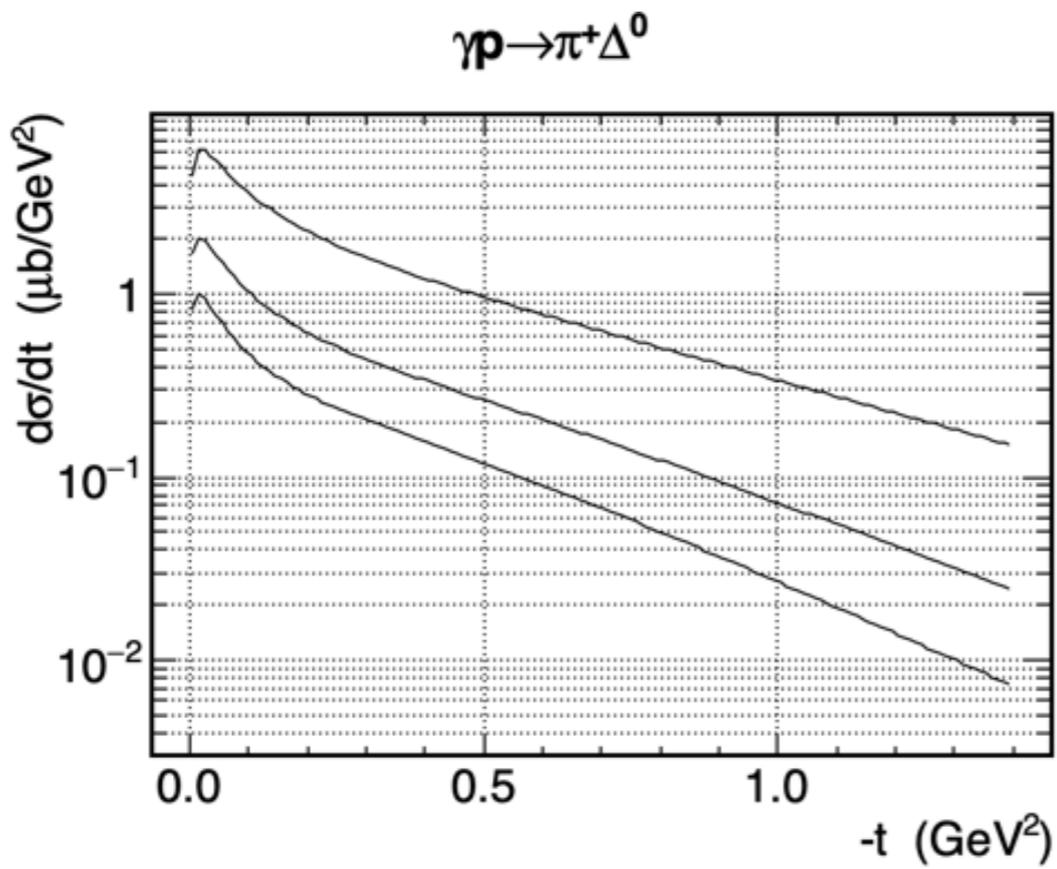
Curves at 4.5, 7.5, 10.5 GeV

$\Sigma$  asymmetry matches data well

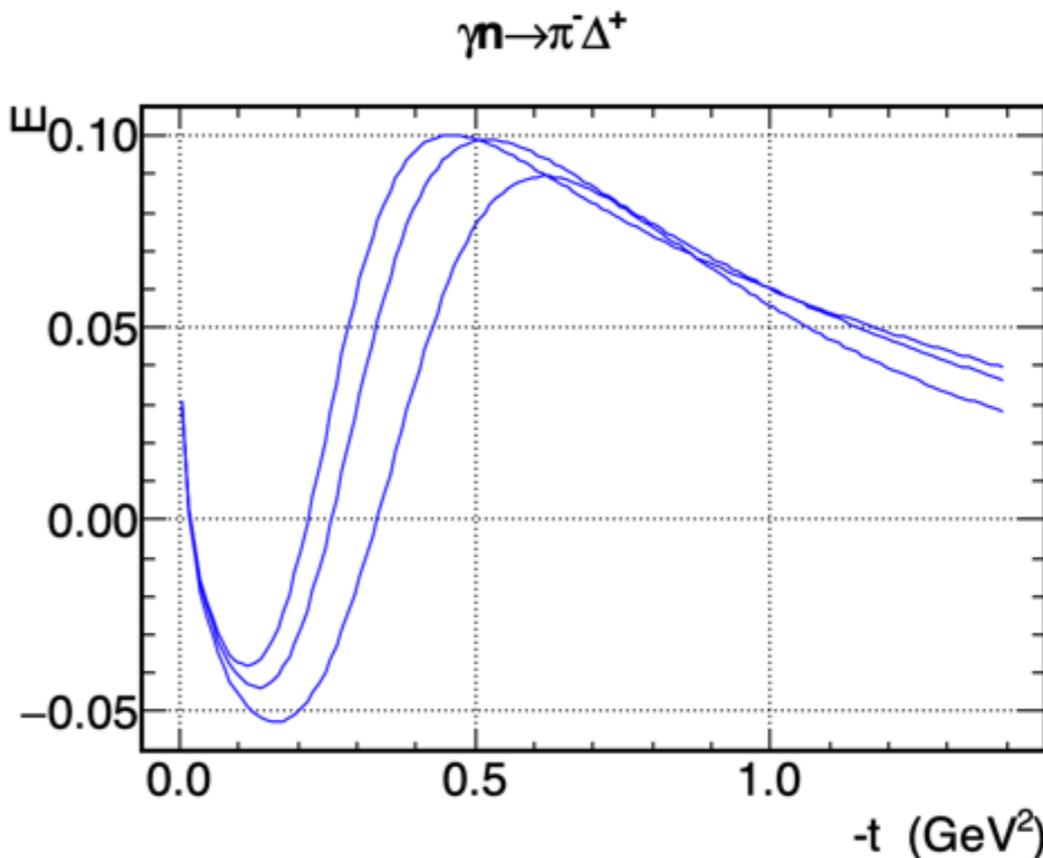
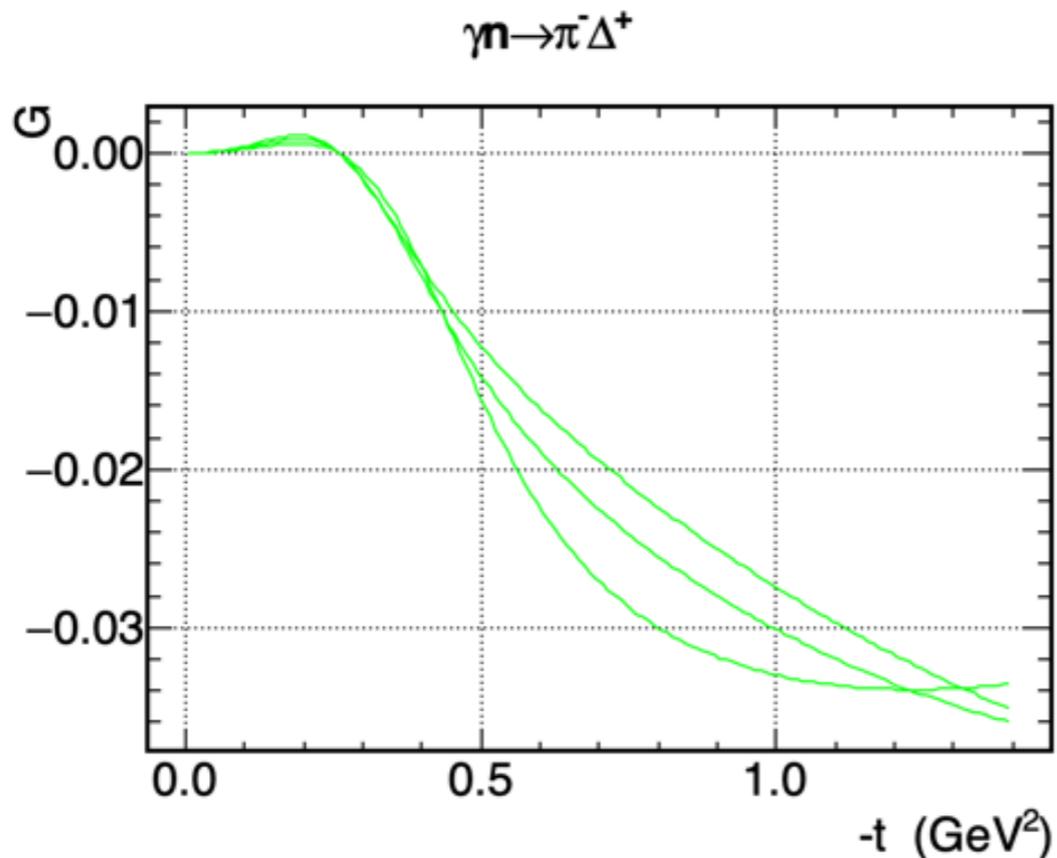
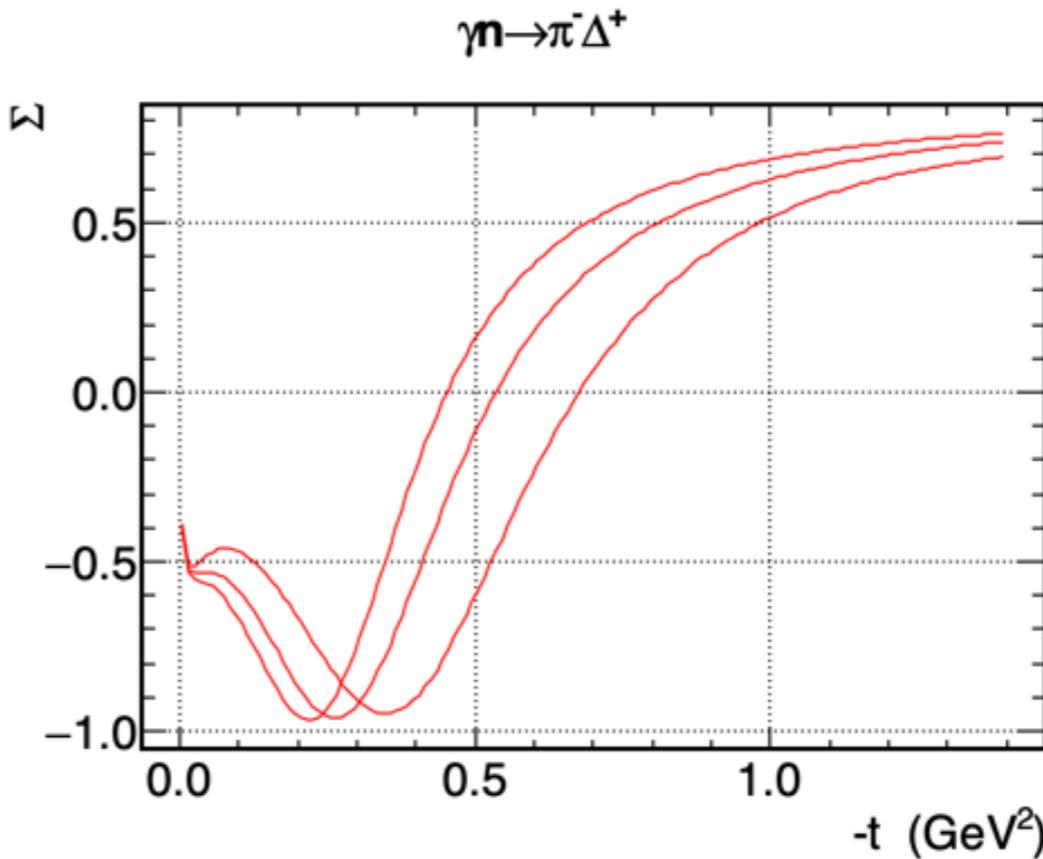
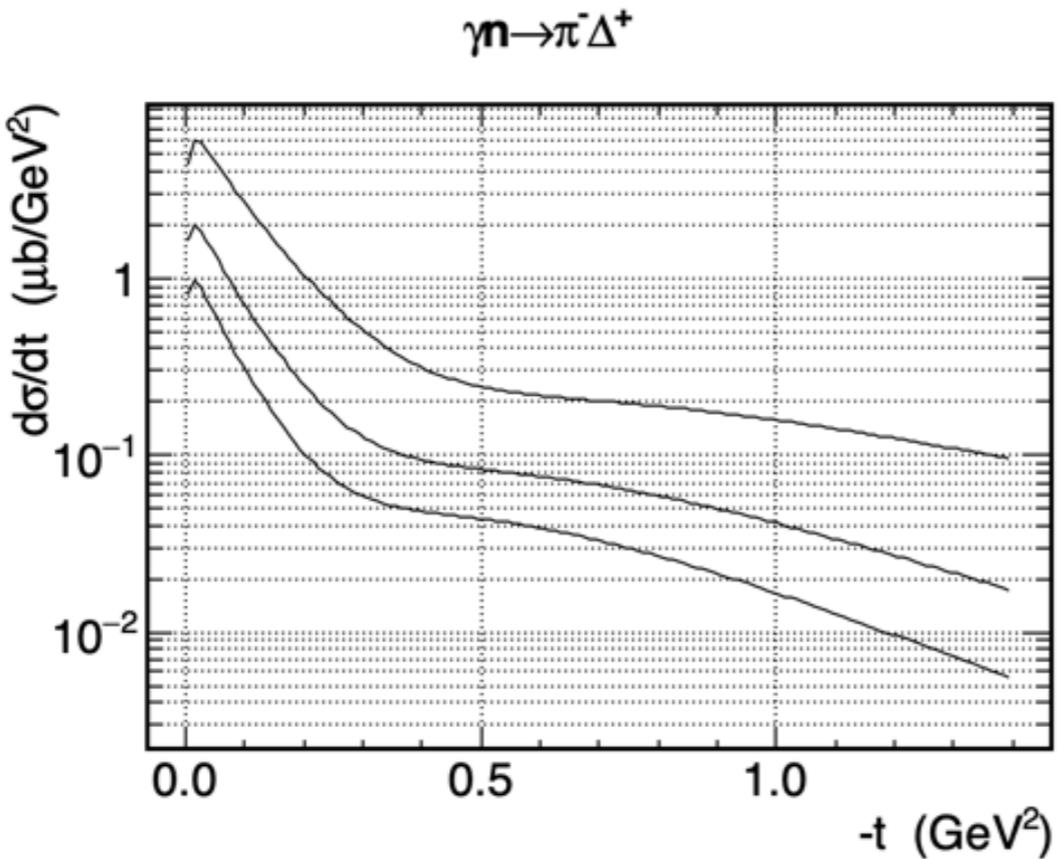
G and E asymmetries completely untested



# Example: $\gamma p \rightarrow \pi^+ \Delta^0$



# Example: $\gamma n \rightarrow \pi^- \Delta^+$

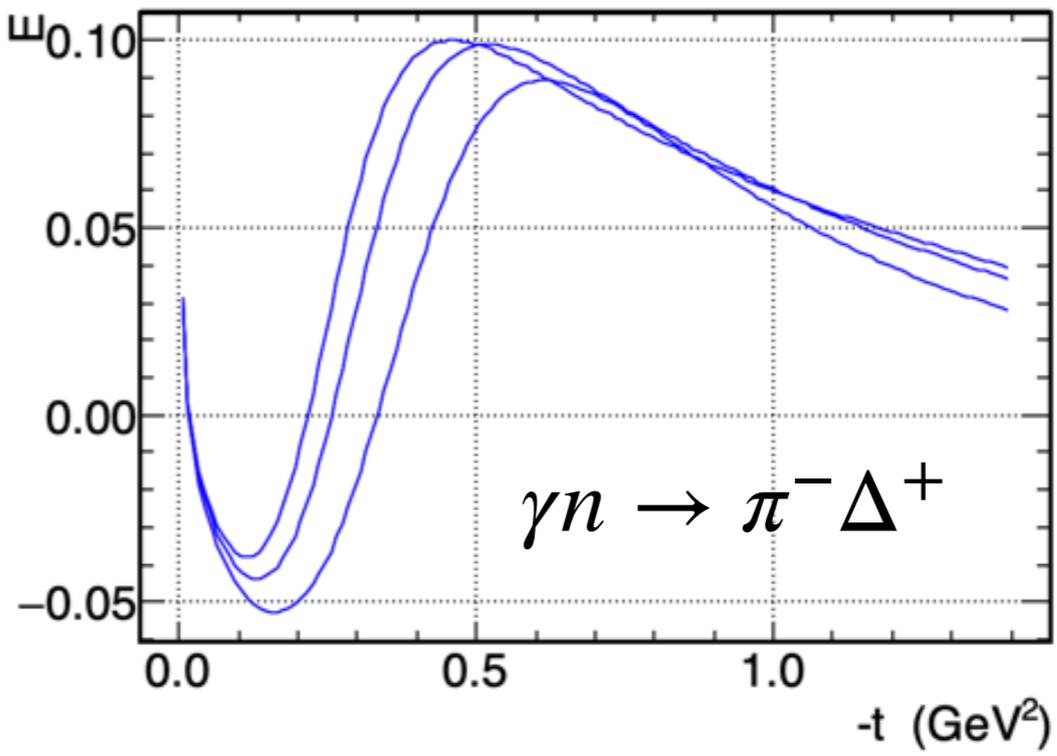
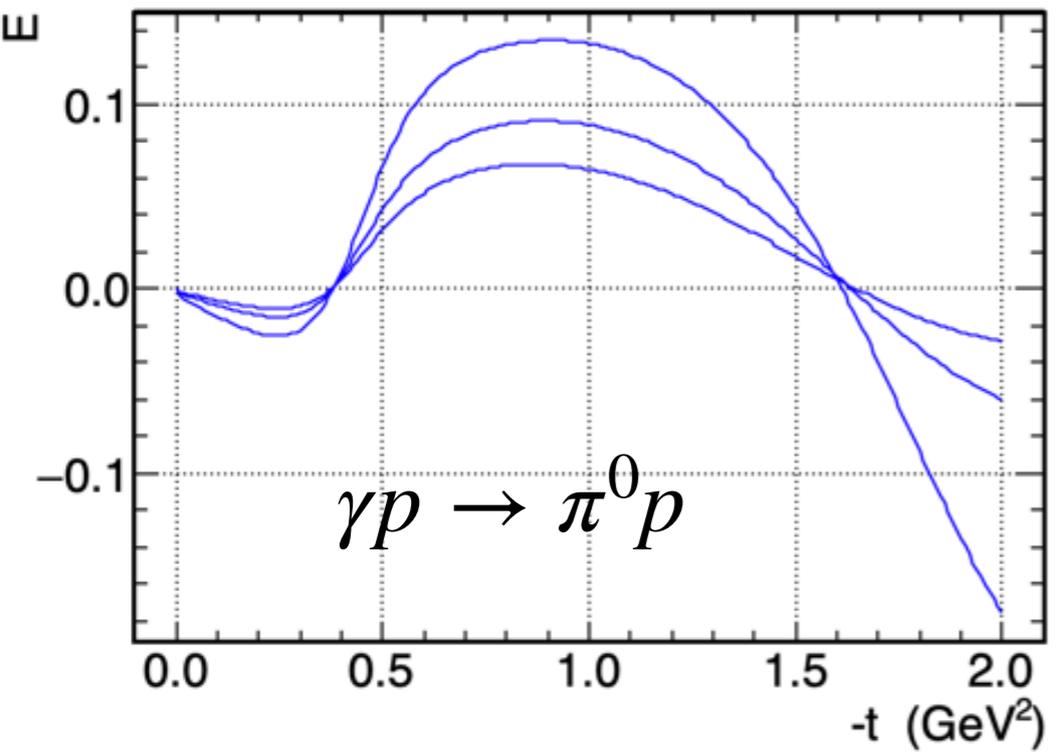


# Asymmetry E in single $\pi$ production

4.5, 7.5, 10.5 GeV

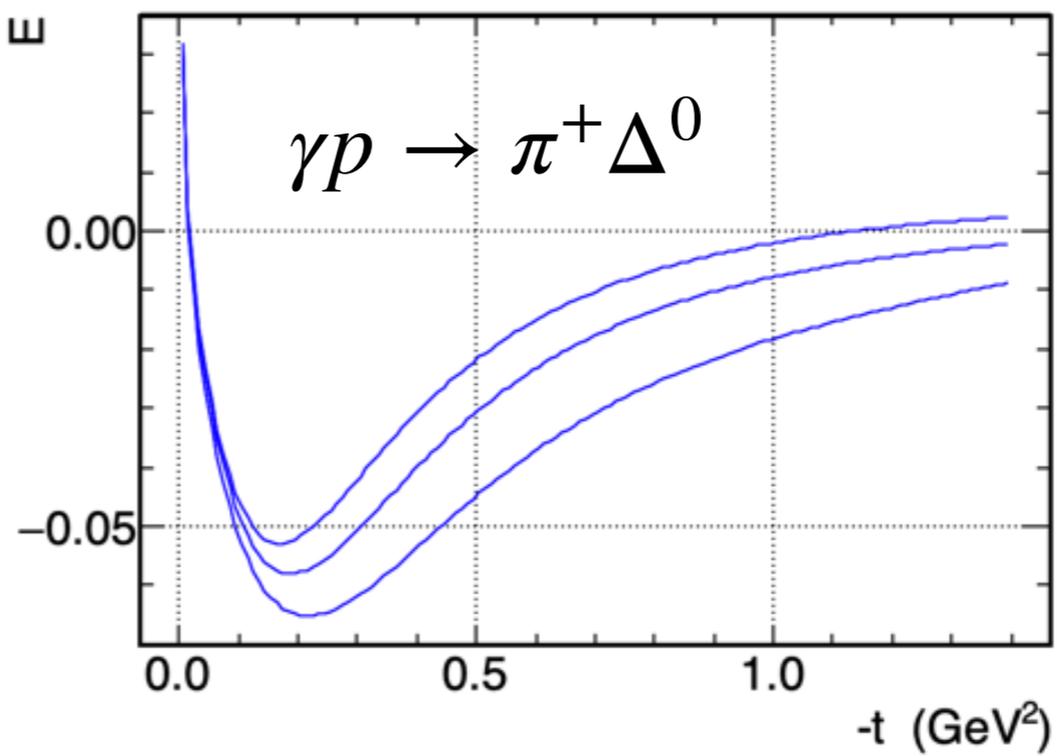
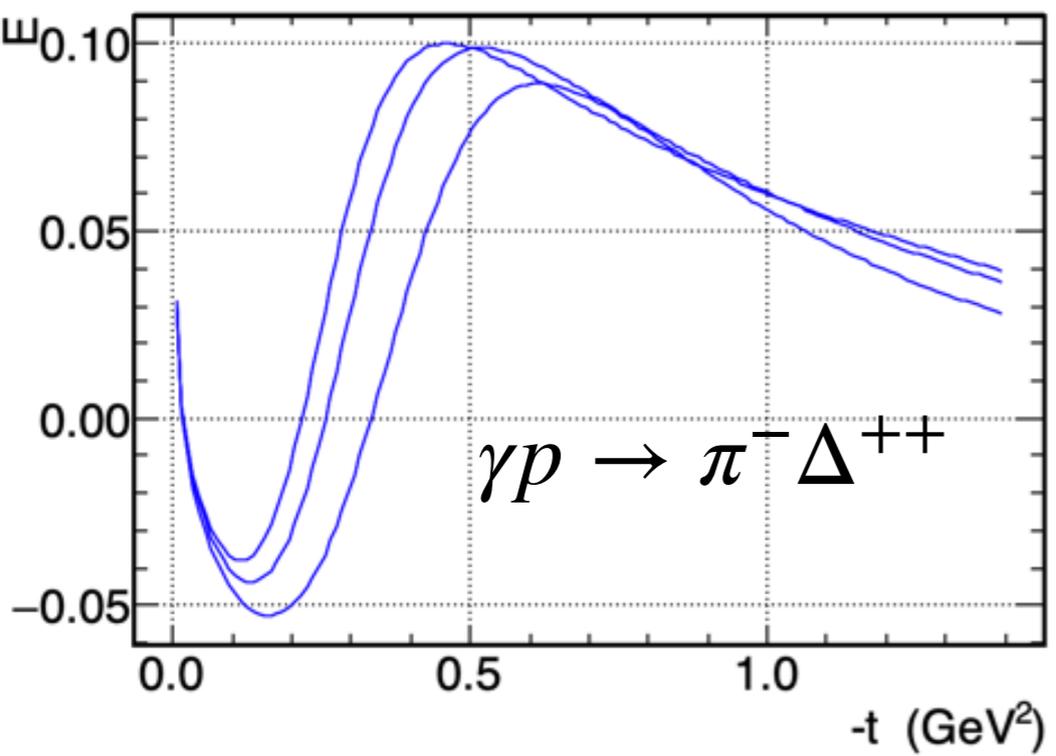
$\gamma p \rightarrow \pi^0 p$

$\gamma n \rightarrow \pi^- \Delta^+$



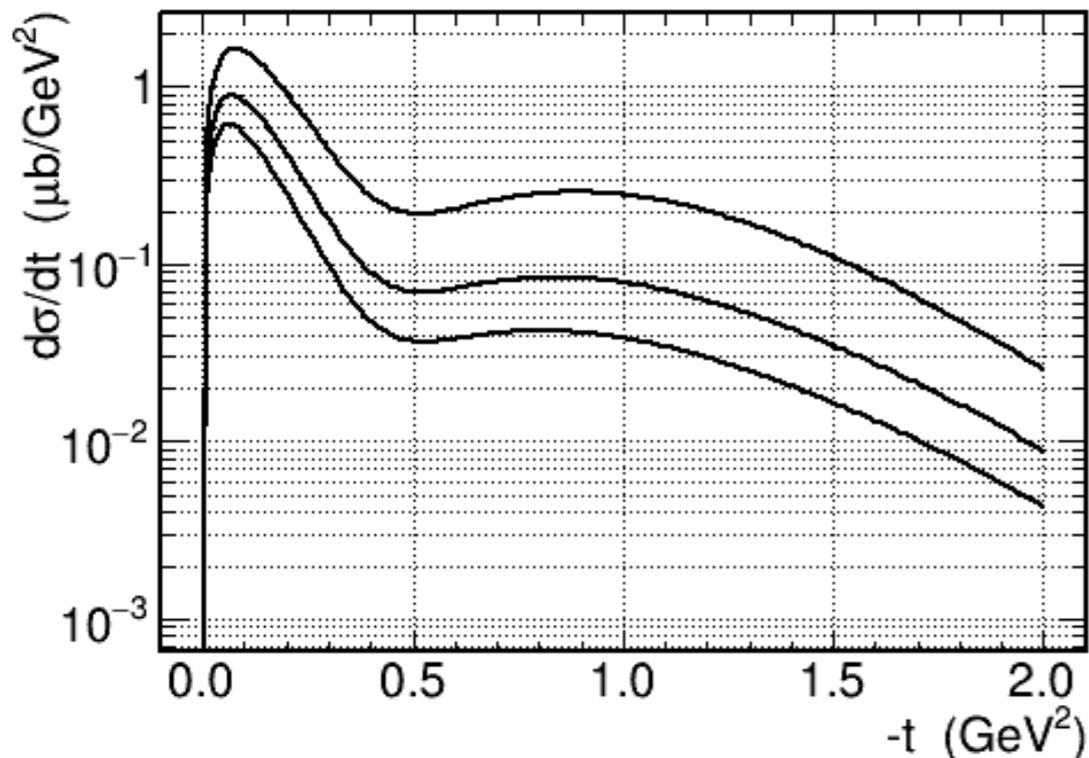
$\gamma p \rightarrow \pi^- \Delta^{++}$

$\gamma p \rightarrow \pi^+ \Delta^0$

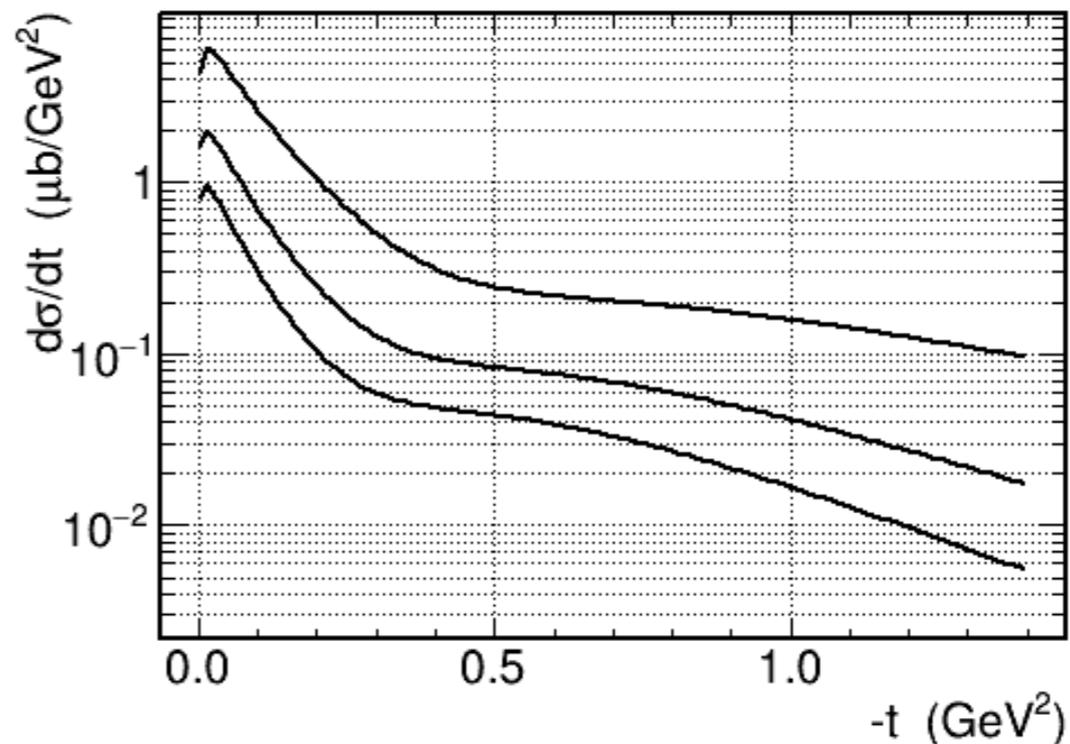


# Cross Section in single $\pi$ production

$\gamma p \rightarrow \pi^0 p$

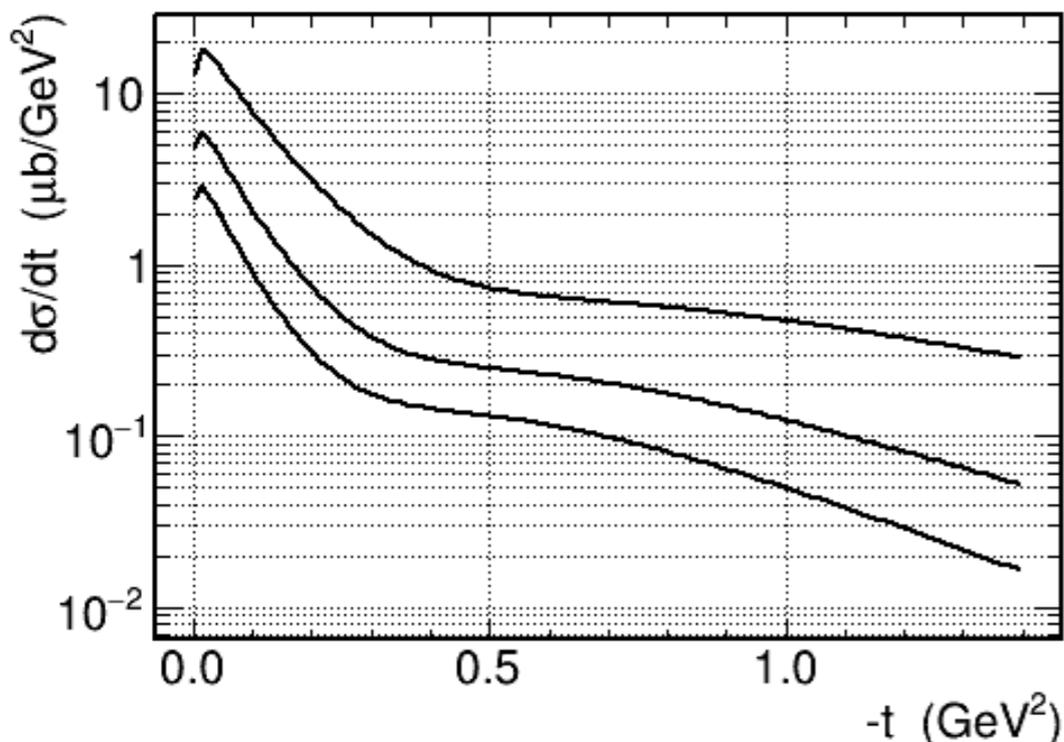


$\gamma n \rightarrow \pi^- \Delta^+$

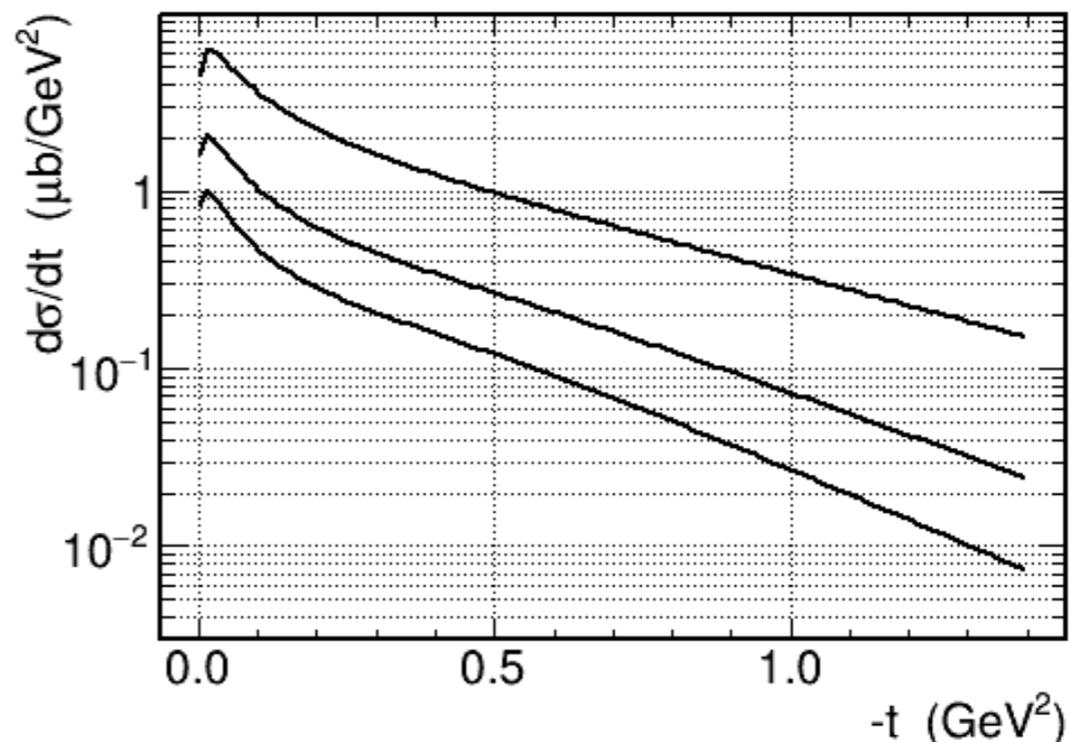


4.5 GeV  
7.5 GeV  
10.5 GeV

$\gamma p \rightarrow \pi^- \Delta^{++}$



$\gamma p \rightarrow \pi^+ \Delta^0$



# Prospects

The difficulty is primarily statistical

Predicted asymmetries are smallish: 1% to 5%

Cross sections are small for individual channels

The photon beam polarization drops with energy

There is a dilution from unpolarized nucleons

Detailed projections including the nuclear spectral function are needed

# Tensor Polarization

A photon beam allows a very high deuteron vector polarization to be achieved.

This also means a very high tensor polarization (alignment) +65% to +75%.

What can we learn with a tensor polarized deuteron target and polarized photon beam?

# Summary

Hall D has an approved polarized target program to measure the GDH integrand on hydrogen and deuterium.

The GDH integrand on nuclei may be sensitive to medium modifications in a novel way.

Application of the sum rule and Mean Field nuclear theory (QMC) suggest there will be a significant difference from free protons or neutrons in the Regge region.

Measurements of exclusive asymmetries as a function of pair relative momentum are feasible, beyond the Fermi momentum may be challenging.

Polarized targets are significantly easier with a photon beam which allows higher polarizations and potentially unique species. A very high tensor polarization is possible for deuterium.